



**The Abdus Salam  
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**2052-49**

**Summer College on Plasma Physics**

*10 - 28 August 2009*

**Discoveries in Dusty Plasmas**

Padma K. Shukla  
*Ruhr-Universität Bochum  
Germany*

# Discoveries in Dusty Plasmas: 20 Years of the Dust Acoustic Wave

AS-ICTP, Trieste, 25 August 2009

**PADMA KANT SHUKLA**

SUPA, Dept. Physics, U. Strathclyde, Glasgow, Scotland  
Faculty of Physics & Astronomy, Ruhr-U. Bochum, Germany

<http://www.tp4.rub.de/~ps>  
<http://www.padmakantshukla.com>

Collaborator: Bengt Eliasson (Ruhr-U. Bochum, Germany)

## OUTLINE

- A. INTRODUCTION
- B. PROPERTIES OF DUSTY PLASMAS
- C. DUST CHARGING
- D. NEW WAVES/NEW INSTABILITIES
- E. NEW FORCES: WAKE FIELDS
- F. NONLINEAR STRUCTURES: MACH CONES, DIA SHOCKS, VOIDS, VORTICES
- G. CONCLUSION

## INTRODUCTION

- ❑ OCCURRENCE OF DUSTY PLASMAS: IN SPACE NEBULAS, MOLECULAR CLOUDS, SUPERNOVAE, SATURN RINGS, MARTIAN ENVIRONMENTS AND COMETARY TAILS
- ❑ IN UPPER ATMOSPHERE AND NOCTILUCENT CLOUDS IN POLAR MESOSPHERE
- ❑ IN COMMERCIAL PLASMA ETCHING REACTORS: MICROELECTRONICS & NANOTECHNOLOGY
- ❑ NEW MATERIALS: DUST-PLASMA CRYSTALS
- ❑ IN FUSION REACTORS: IN MANY TOKAMAKS AND IN ITER
- ❑ IN MICROBIOLOGY AND DESINFECTION IN MEDICINE/DENTAL TREATMENT

## **DUSTY PLASMA DEFINITION**

- DUSTY PLASMAS ARE MULTI-COMPONENT PLASMAS
- THEY CONTAIN ELECTRONS, IONS, NEUTRAL ATOMS/MOLECULES, AND MICRO-PARTICLES/CHARGED DUST GRAINS
- THEY ARE SIGNIFICANTLY DIFFERENT FROM THE USUAL ELECTRON-ION PLASMAS
- DUST CHARGING AS A DYNAMICAL VARIABLE
- NEW SPACE AND TIME SCALES ASSOCIATED WITH DUST PARTICLE MOTION

**Rev. Mod. Phys. 81, 25 (2009) [20 pages]**

## **Colloquium: Fundamentals of dust-plasma interactions**

**Abstract**

**References (293)**

**No Citing Articles**

**Download: PDF (927 kB)** **or Buy this Article (US\$35) (Use Article Pack)**

**P. K. Shukla**

*Institut für Theoretische Physik IV, Ruhr-Universität Bochum, D-44780 Bochum, Germany*

**B. Eliasson**

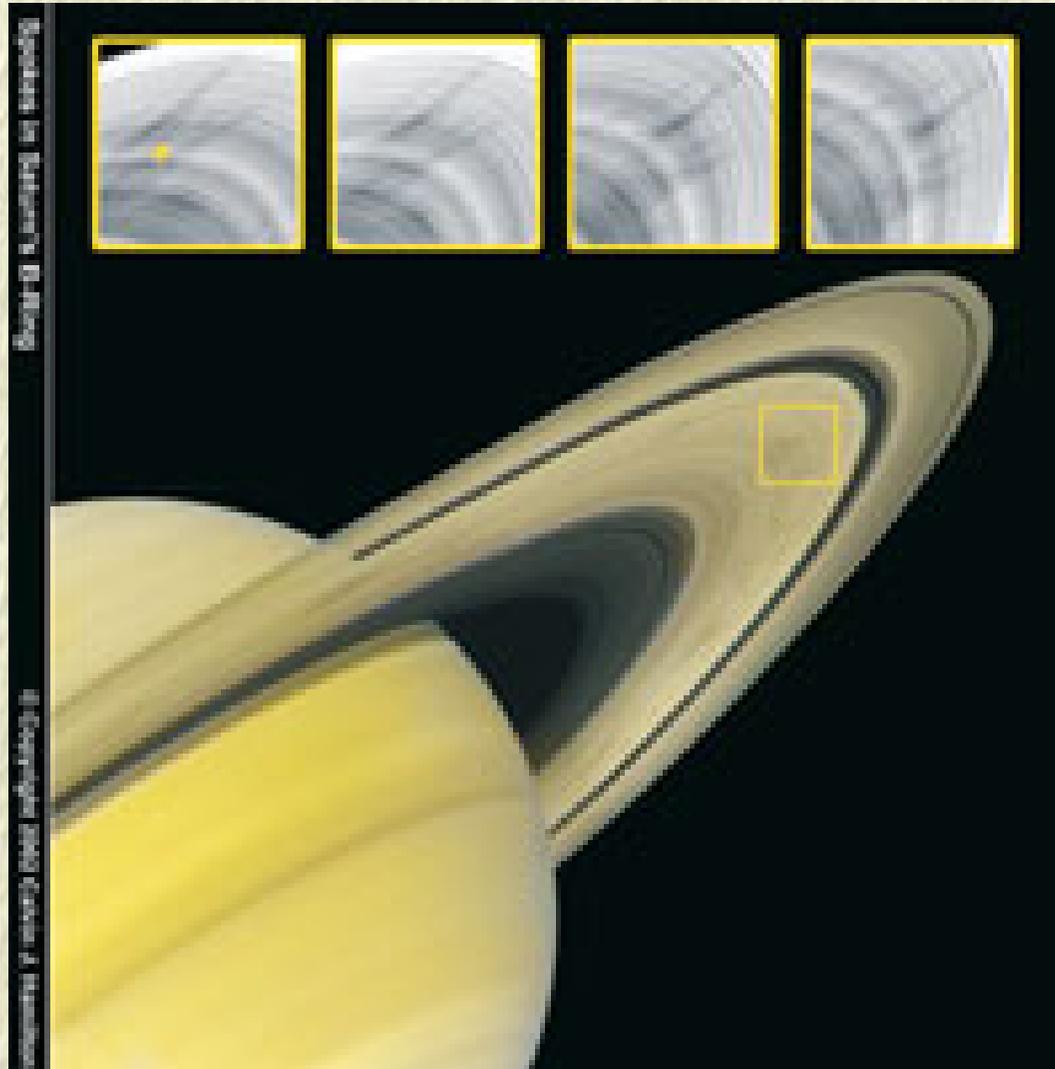
*Institut für Theoretische Physik IV, Ruhr-Universität Bochum, D-44780 Bochum, Germany  
and Department of Physics, Umeå University, SE 901 87 Umeå, Sweden*

Published 7 January 2009

# EAGLE NEBULA



# SATURN RINGS



# HALE-BOPP & HYAKUTAKE

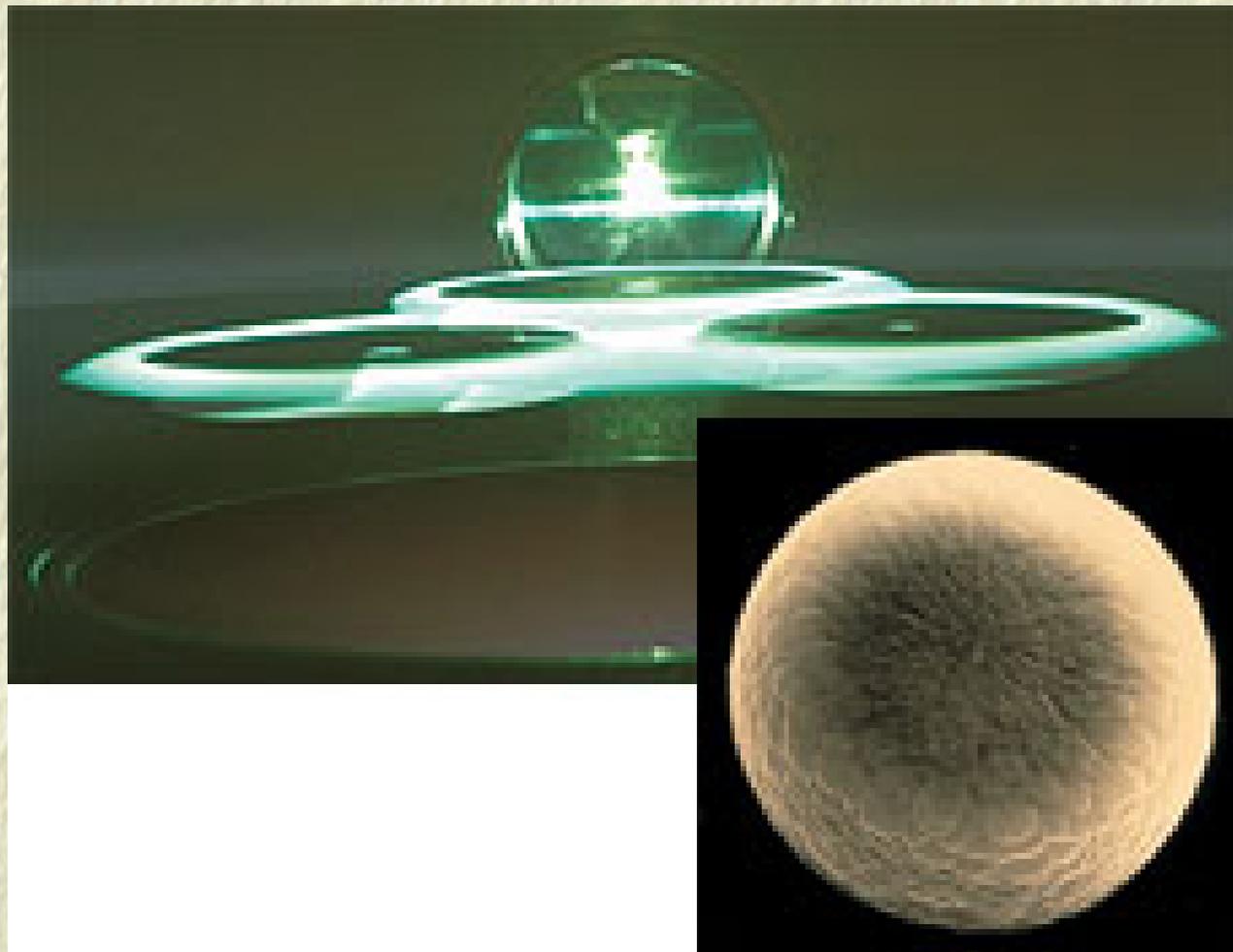


## MESOSPHERIC NOCTILUCENT CLOUDS

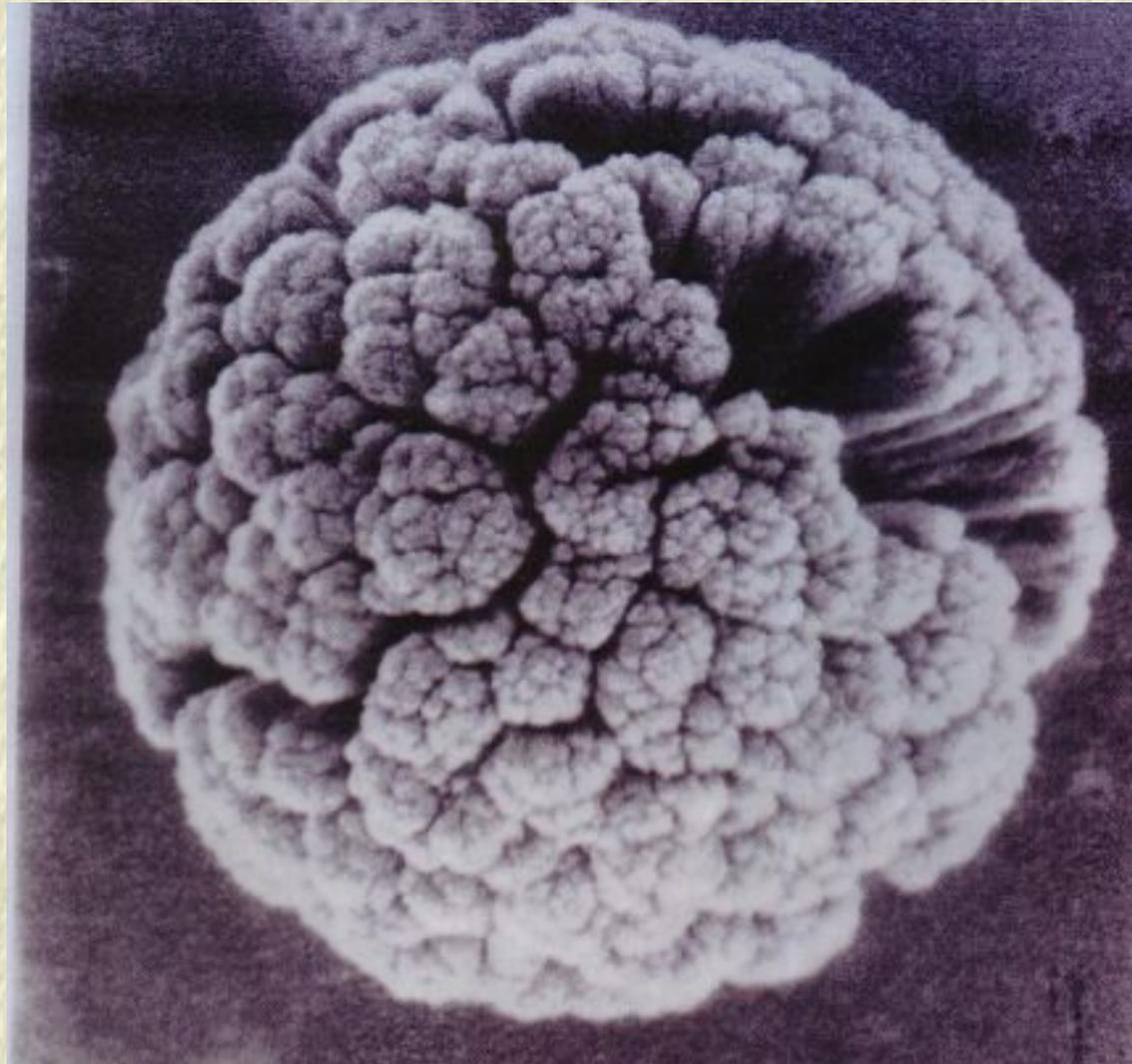


T. W. Backhouse, Meteorol. Mag. **20**, 133 (1885).

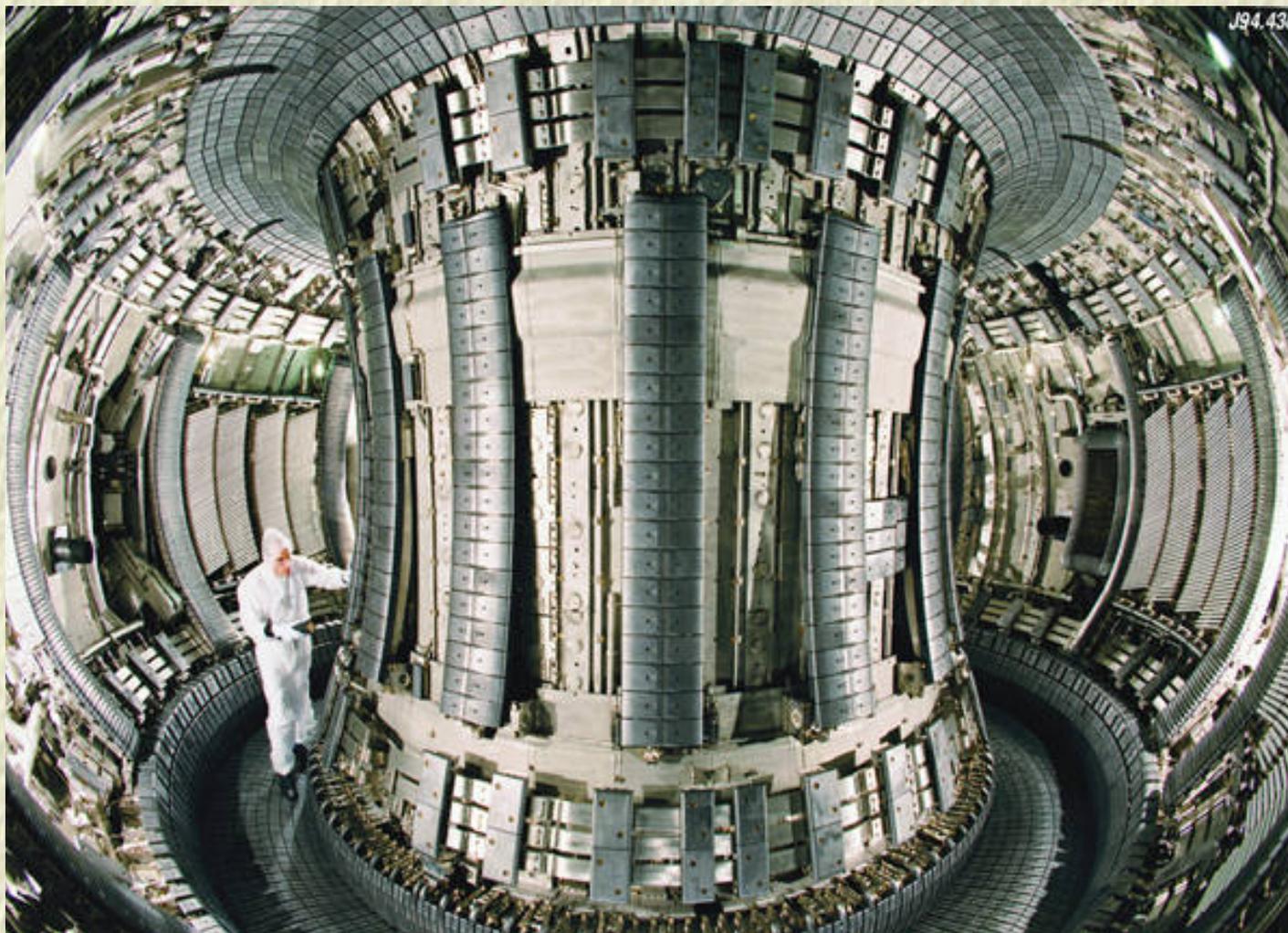
# MICROELECTRONICS



## FORMATION OF DUST STRUCTURES



# JET TOKAMAK

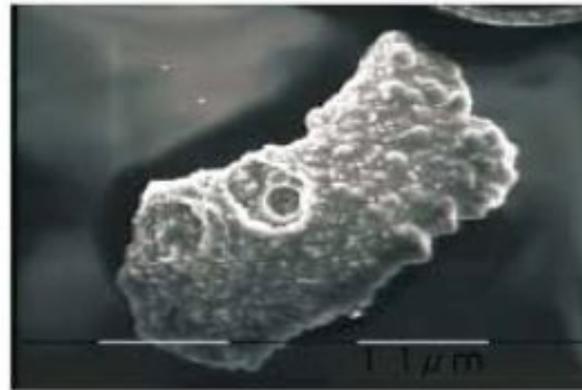


## DUST IN FUSION DEVICES

- Significant amount of dust particles is observed in the chambers of fusion devices



0.1 mm



1  $\mu$ m

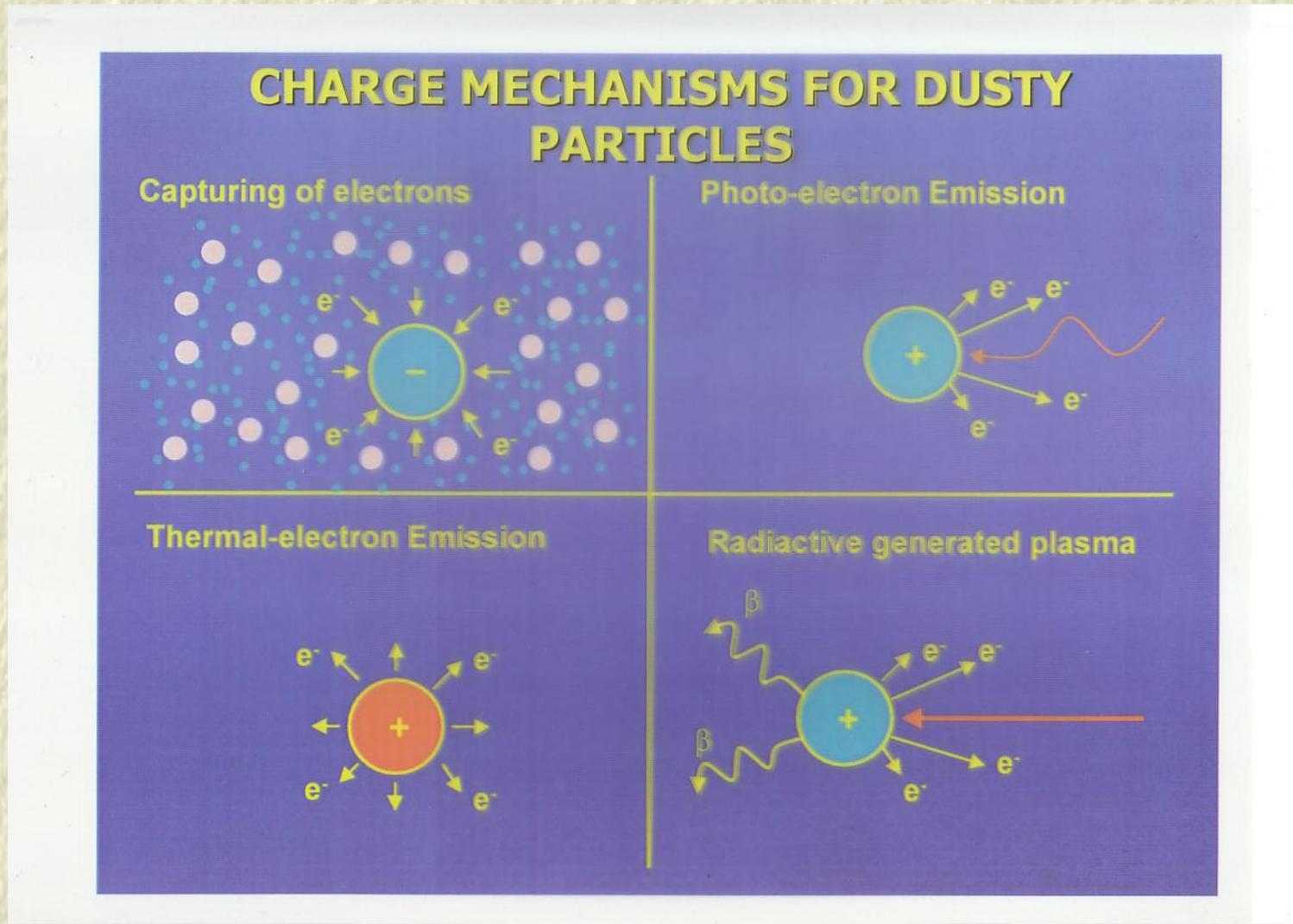


200 nm

Winter PPCF 1998

- But so far an impact of dust on the performance of current fusion devices is not clear

# CHARGING MECHANISMS



## CHARGING MECHANISMS (continued)

### Complex Plasmas

**Plasma (electrons/ions)**

- 4th state of matter (99%)
- most disordered state

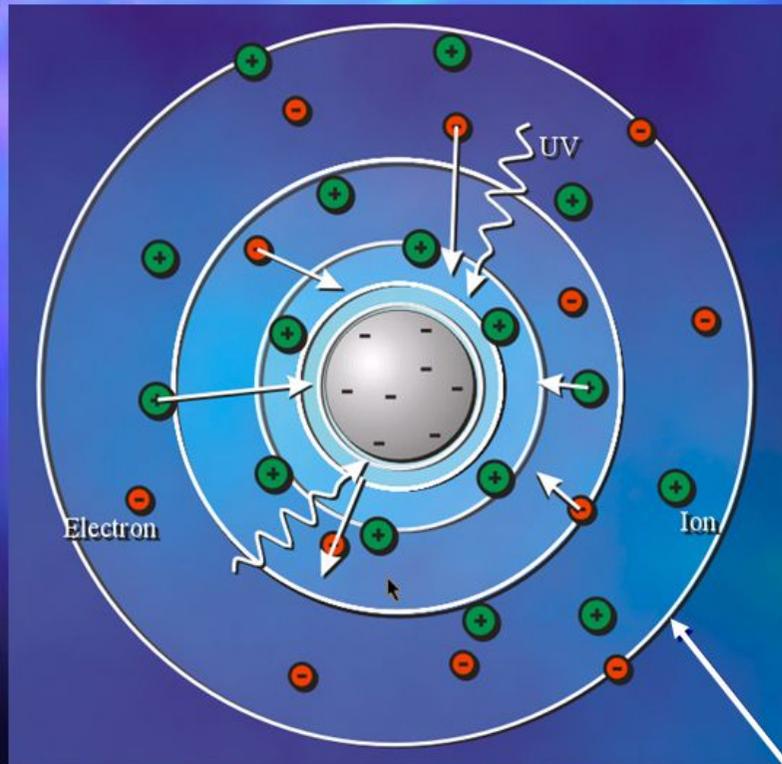
**Complex plasma (+ particles)**

- $Z \sim 10.000 e^-$  on a particle of  $5\mu\text{m}$  diameter

**CIPS**

## CHARGING MECHANISMS (continued)

### Charging of a single particle in a plasma



#### Collection of charges

particle is negatively charged due to higher mobility of electrons  
 positive charge cloud around particle  $\Rightarrow$  Debye screening

#### Temporal charge variation

$$\frac{dQ}{dt} = I_{\text{electrons}} + I_{\text{ions}} + I_{\dots}$$

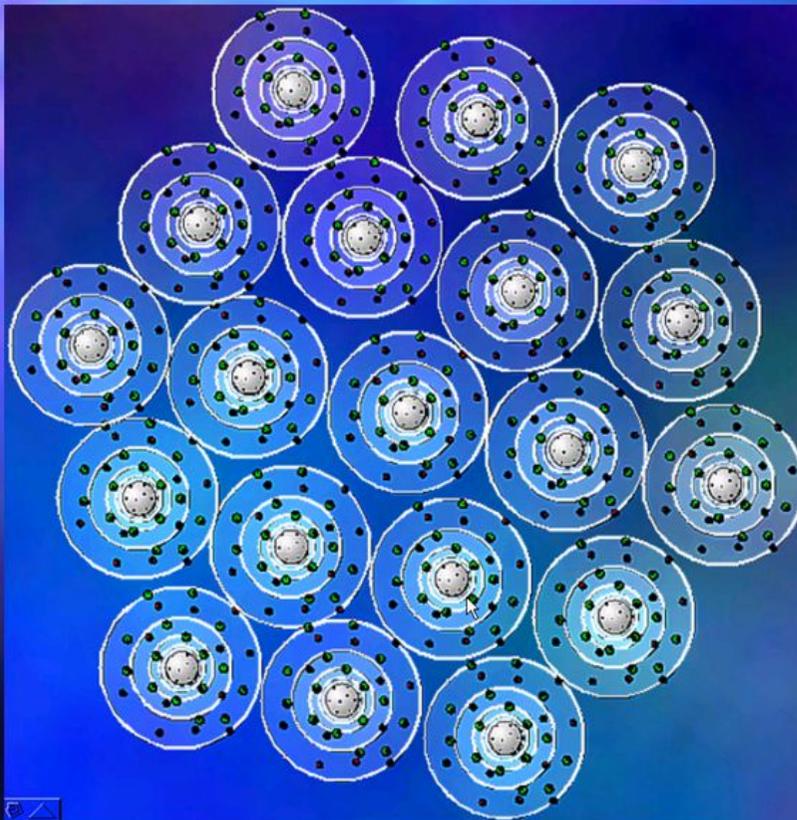
Steady state:  $\frac{dQ}{dt} = 0$

For a particle of  $1\mu\text{m}$  diameter:  $Q = -1500e$

Debye length:  $\lambda_D = \sqrt{\frac{kT}{4\pi e^2 n}}$

Potential contour lines

# Plasma crystallisation



$$\lambda_i \approx 50 \mu\text{m} \ll \lambda_e \approx \Delta$$

## Phase diagram depends on:

a) Coulomb coupling parameter for interacting particles:

$$\Gamma = Q^2 / 4\pi\epsilon_0 \Delta k_B T$$

Coulomb energy/Thermal energy

$\Gamma < 1$ : system is weakly coupled (common)

$\Gamma > 1$ : system is strongly coupled (uncommon)

b) Lattice parameter:

$$\kappa \leq \Delta \lambda_D$$

( $\Delta$ : particle distance,  $\lambda_D$ : Debye length)

$$\Gamma \gg 1 \text{ and } \kappa \sim 1$$

⇒ plasma crystal

$\Gamma = 172$  for one component,  
pure Coulomb interaction

First prediction by H. Ikezi, Phys. Fluids (1986); Observations: Wu & Lin I, PRL (1994), Thomas et al, PRL (1994).

# Phase diagram

## Coulomb coupling parameter for interacting particles:

$\Gamma = (\text{shielded}) \text{ Coulomb energy} / \text{Thermal energy}$   
 $\Rightarrow \Gamma < 1$ : system is weakly coupled (common)  
 $\Rightarrow \Gamma > 1$ : system is strongly coupled (uncommon)

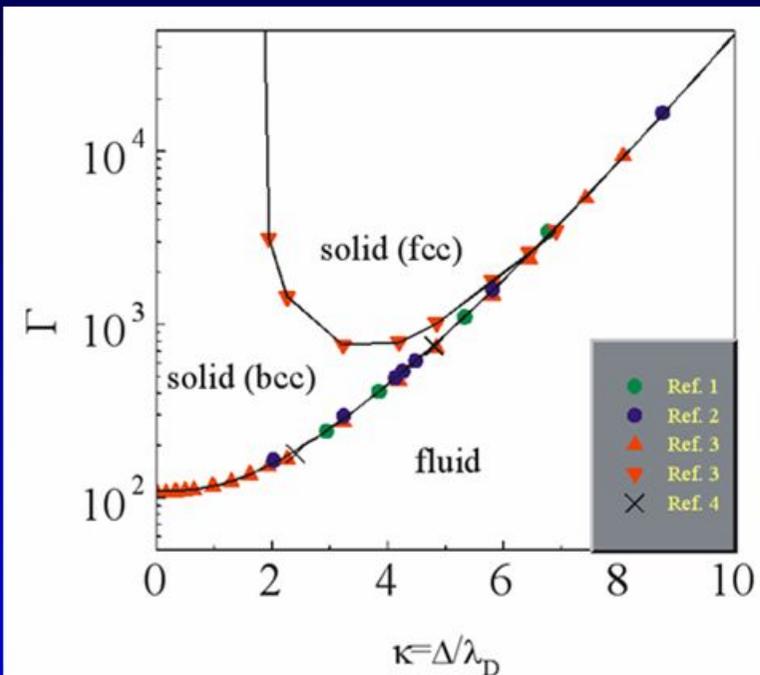
## Lattice parameter:

$$\kappa \leq \Delta / \lambda_D$$

( $\Delta$  : particle distance.  $\lambda_D$ : Debye length)

## For complex plasmas:

$\kappa \sim 1, \Gamma \geq \Gamma_c \Rightarrow \text{Plasma Crystals}$



### References:

- [1] E.J. Meijer and D. Frenkel, J. Chem. Phys. 94, 2269 (1991)
- [2] M.J. Stevens and M.O. Robbins, ibid. 98, 2319 (1993)
- [3] S. Hamaguchi et al., Phys. Rev. E 56, 4671 (1997)
- [4] O. Vaulina and S. Khrapak, JETP 92, 228 (2001)

## PROPERTIES OF DUSTY PLASMAS

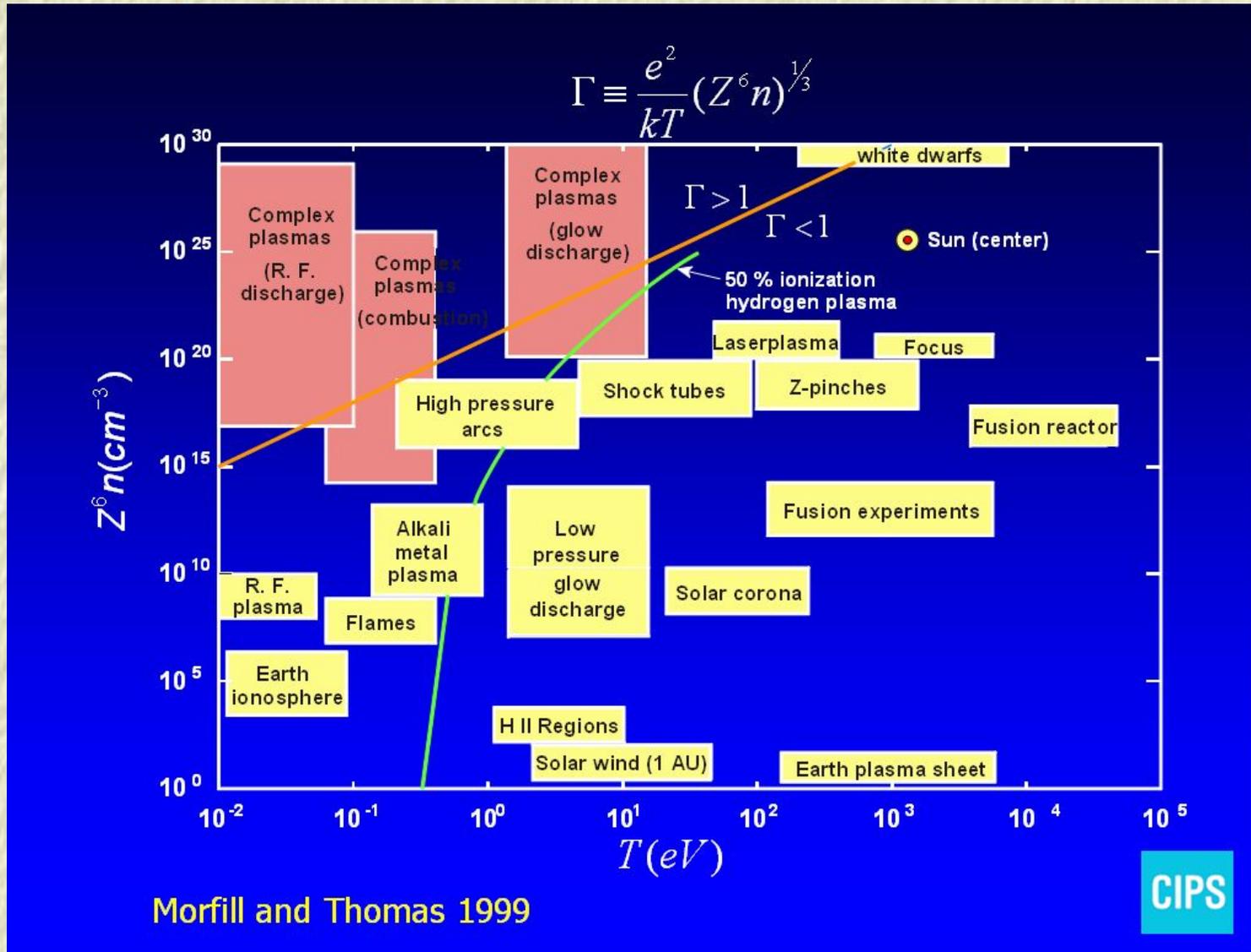
| <b>Electron–ion plasma</b>                                    | <b>Dusty plasma</b>  |
|---|--|
| $n_{e0} = \sum_i Z_i n_{i0}$                                  | $Q_d n_{d0} + e n_{e0} = e \sum_i Z_i n_{i0}$                            |
| $Q_i = Z_i e$   | $Q_d = Z_d e \gg Q_i$  |
| $Z_i = \text{const.}$   | $dQ_d/dt = I_e + I_i + I_s + \dots$                                      |
| $m_i$   | $m_d \sim 10^{12} m_i$   |
| $\lambda_{De}$  | $\lambda_D \sim \lambda_{Di}$  |
| Uniform particle sizes  | Size distributions   |
| Particle $\mathbf{E} \times \mathbf{B}_0$ motion at low $B_0$ | Dust $\mathbf{E} \times \mathbf{B}_0$ motion requires high (Tesla) $B_0$ |
| IAW, EIC, $f \sim 1$ kHz                                      | DAW, DLW, SW, $f \sim 10$ Hz,  |

## PROPERTIES OF DUSTY PLASMAS

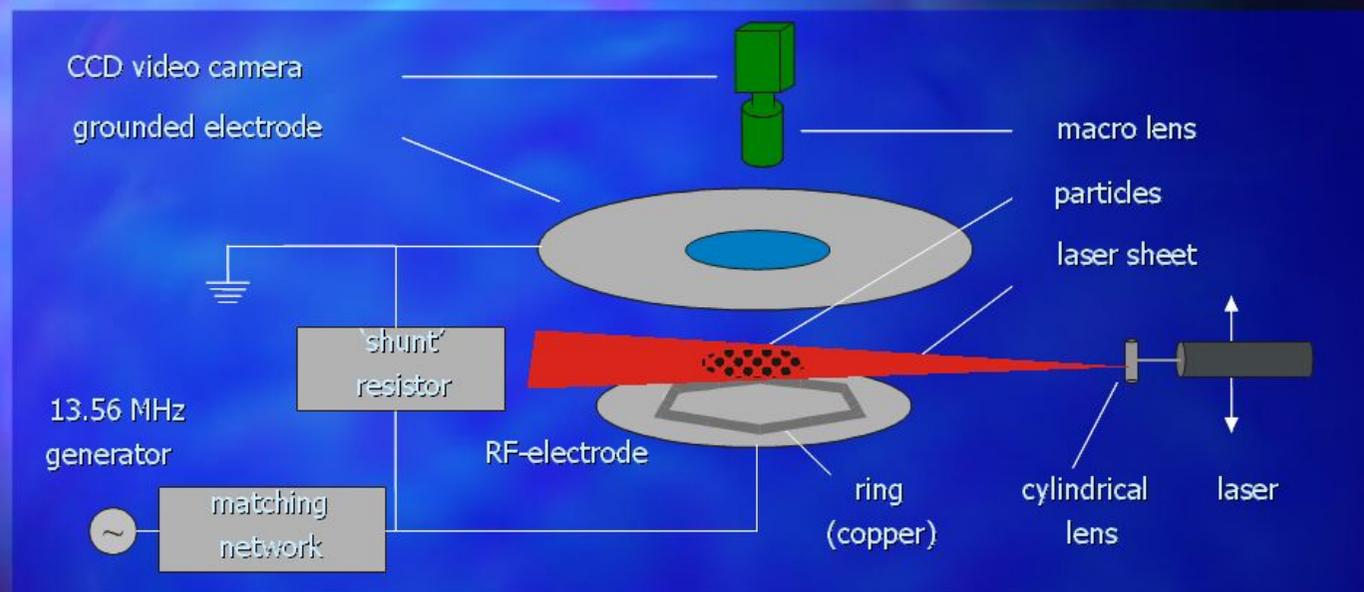
| <b>Electron–ion plasma</b> | <b>Dusty plasma</b>         |
|----------------------------|-----------------------------|
| IA Solitons                | DAW Shock Waves/Holes       |
| Compression/Rarefaction    | Mach Cones                  |
| Debye–Hückel Interactions  | Attractive Forces, Ion Drag |
| El. & Ion Crystalization   | Dust Crystals               |
| Wigner Crystals            | Cryogenic Plasmas           |
| Phase Transition           | Phase Transition            |

| <b>Solid State Crystals</b>                 | <b>Dust Crystals</b>                                   |
|---|--|
| $Z_i > 1$                                   | $Z_d \sim 10^3 - 10^5$                                 |
| $\mathcal{E}_{\text{interaction}}$ a few eV | $\mathcal{E}_{\text{interaction}} \geq 900 \text{ eV}$ |
| Lattice Spacing $L \sim 0.1 \text{ nm}$     | $L \sim 1 \text{ mm}$                                  |

# EXISTENCE DIAGRAM

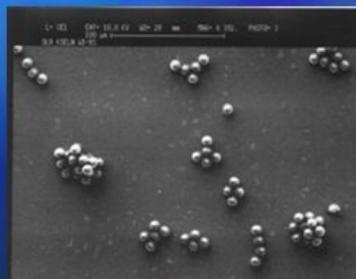


## Experimental Setup on Earth



### Particles:

Melamine-Formaldehyde  
diameter: few  $\mu\text{m}$



### Gas:

nobel gas (argon, krypton)  
pressure: few Pa ... 100 Pa (=1 mbar)

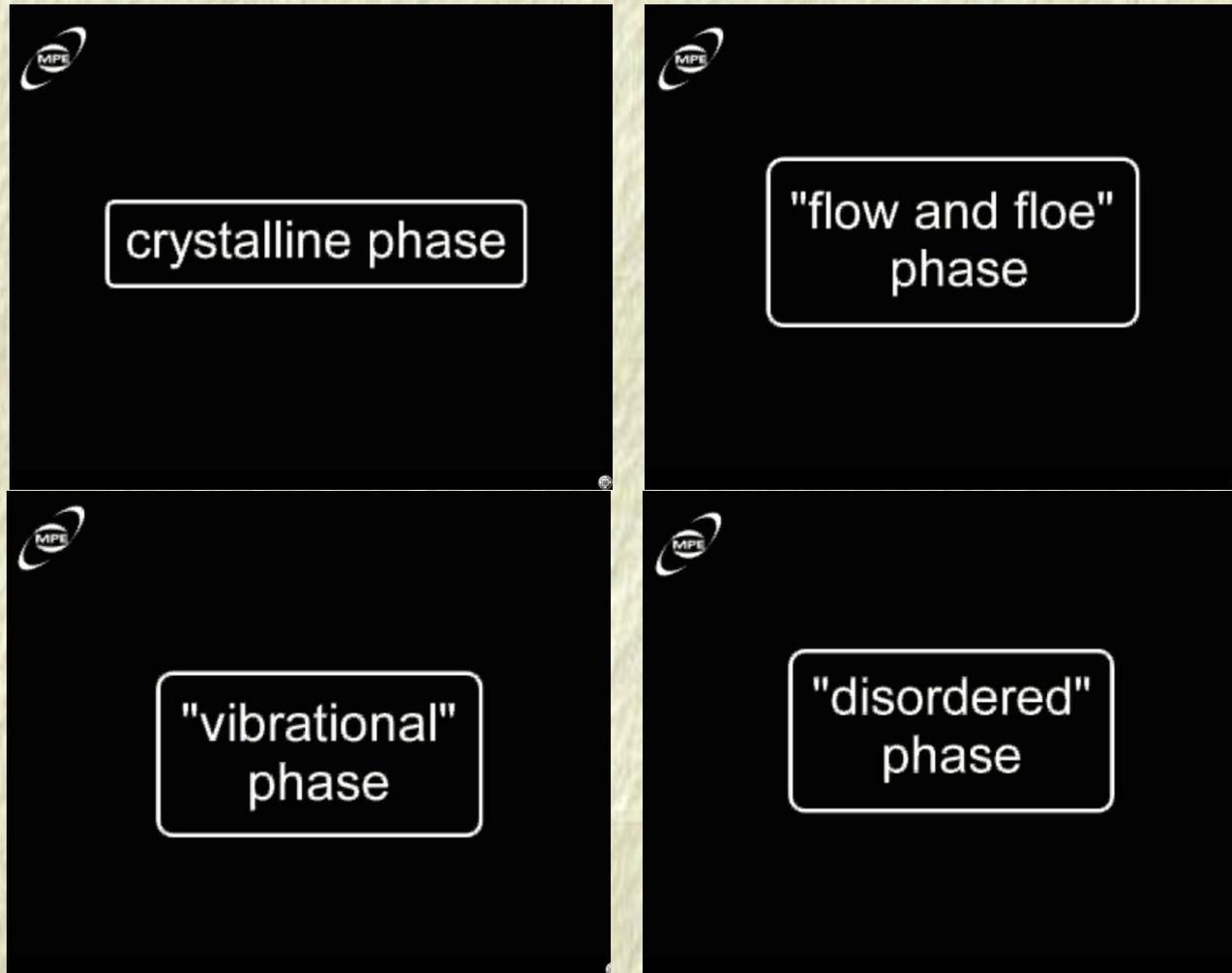
**Ionisation** fraction:  $10^{-6}$  -  $10^{-7}$

### Temperatures:

$kT_{e,v} \sim 2-4$  eV (electrons)  
 $kT_i \sim 0.03$  eV (ions)  
dust particles  $\sim$  room temperature  
( $kT_n = 0.025$  eV)

Thomas et al., PRL (1994).

## DIFFERENT PHASES

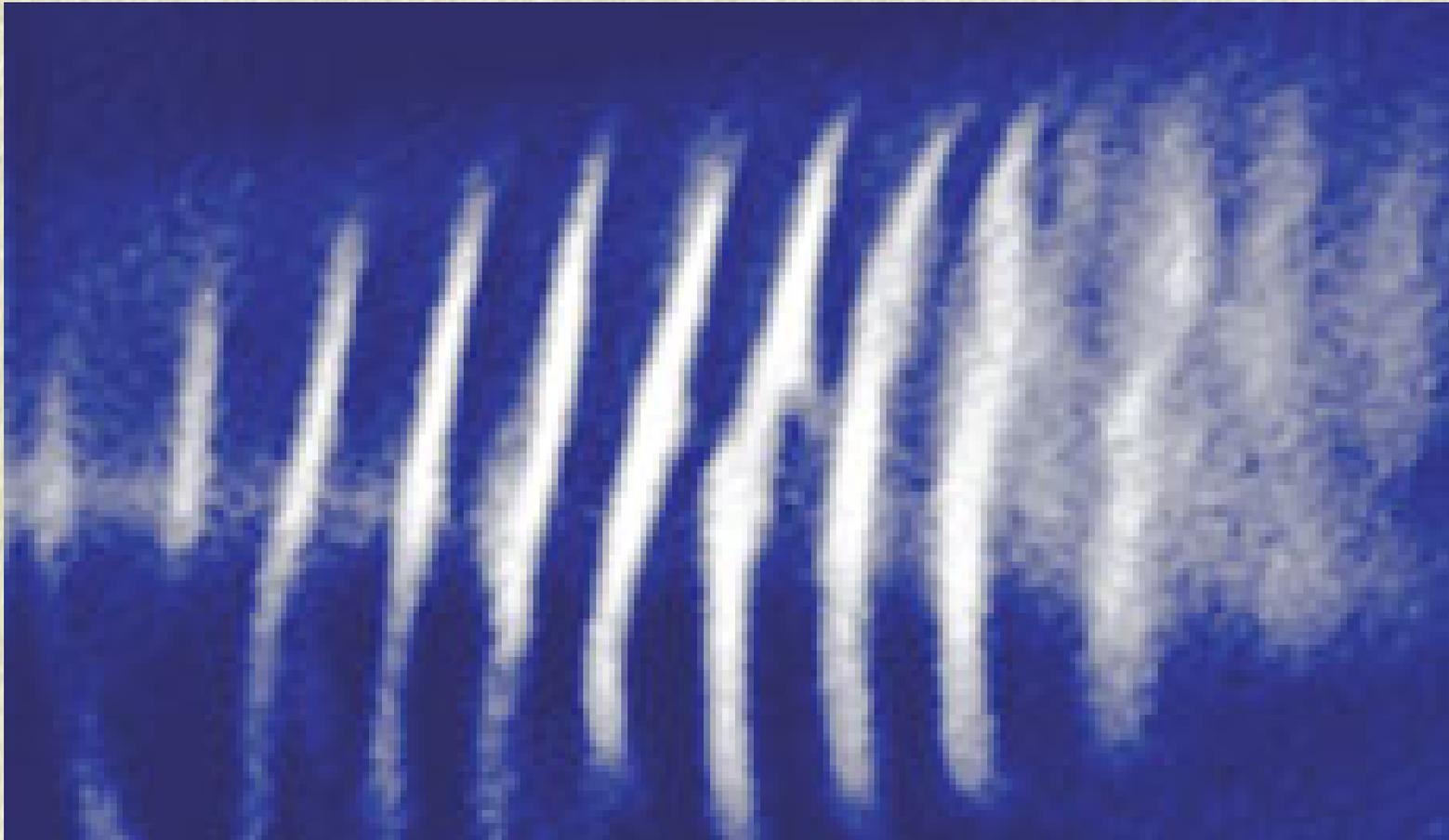


Morfill & Thomas, Nature, 1996.

## COLLECTIVE PROCESSES: PHYSICS OF WAVES

|             | <b>Restoring Forces</b>           | <b>Inertia</b>         | <b>Phase Speed</b>   |
|-------------|-----------------------------------|------------------------|--|
| <b>SW</b>   | Neutral Gas Pressure              | Mass of Neutral Atoms  | $(T_n/m_n)^{1/2}$  |
| <b>IAW</b>  | Electron Pressure                 | Ion Mass               | $C_s = (T_e/m_i)^{1/2}$  |
| <b>DAIW</b> | Electron Pressure                 | Ion Mass               | $(n_{i0}/n_{e0})^{1/2}C_s$   |
| <b>DAW</b>  | Ion Pressure<br>Electron Pressure | Dust Mass<br>Dust Mass | $Z_d(n_{d0}T_i/n_{i0}m_d)^{1/2}$<br>$Z_d(n_{d0}T_e/n_{e0}m_d)^{1/2}$ |
| <b>AW</b>   | Magnetic Tension                  | Ion Mass               | $(B_0^2/8\pi n_{i0}m_i)^{1/2}$                                       |
| <b>DALW</b> | Magnetic Tension                  | Dust Mass              | $(B_0^2/8\pi n_{i0}m_d)^{1/2}$                                       |

## DUST ACOUSTIC WAVES



Observation: A. Barkan, R. L. Merlino, and N. D'Angelo, 1995, Phys. Plasmas  
2 3563; Prediction: P. K. Shukla, 1st Dusty Plasma Workshop Proc., July  
1989.

## RSY Linear & Nonlinear DAW Theory and Observation

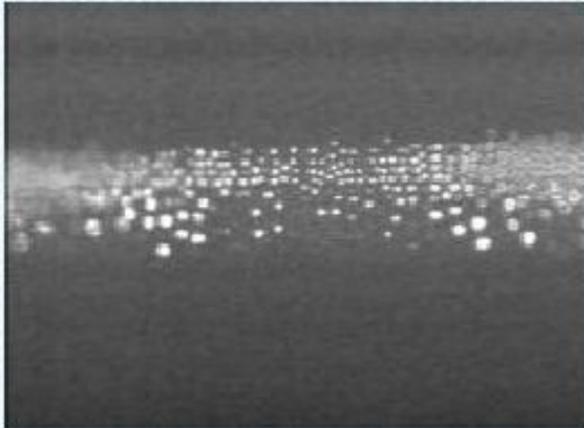
- N. N. Rao, P. K. Shukla, and M. Y. Yu, 1990, Planet. Space. Sci **38**, 543.
- A. Barkan, R. L. Merlino, and N. D'Angelo, 1995, Phys. Plasmas **2** 3563.

( $n_d/n_i \sim 5 \times 10^{-4}$ ,  $Z_d \sim 2 \times 10^3$ ,  $m_d \sim 10^{-12}$  g,  $T_i \sim 0.2$  eV,  $T_e \sim 3$  eV)

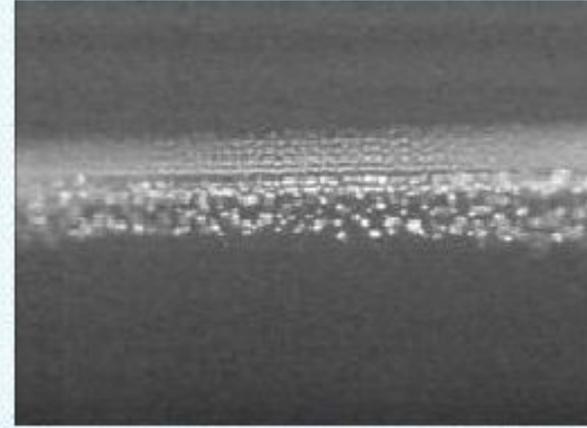
| Theory   | Observation                |
|--|----------------------------|
| $v_{ph} = Z_d \left( \frac{T_i n_d}{m_d n_i} \right) = 9 \text{ cm/s}$ $(\lambda = 0.6 \text{ cm}, \nu = 15 \text{ Hz})$ | $v_{ph} = 10 \text{ cm/s}$ |

## DUST ACOUSTIC-LIKE WAVES

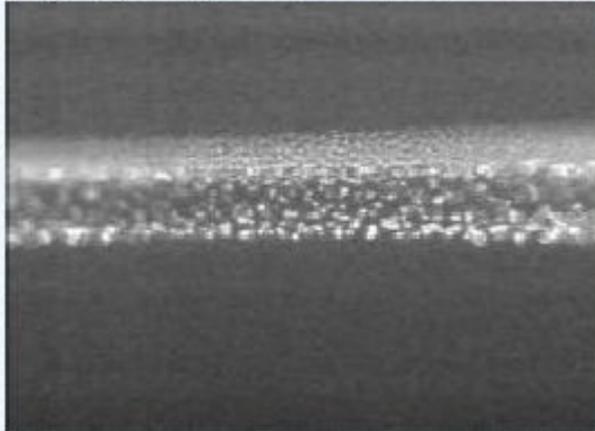
Stable crystal:  $P=0.198$  Torr



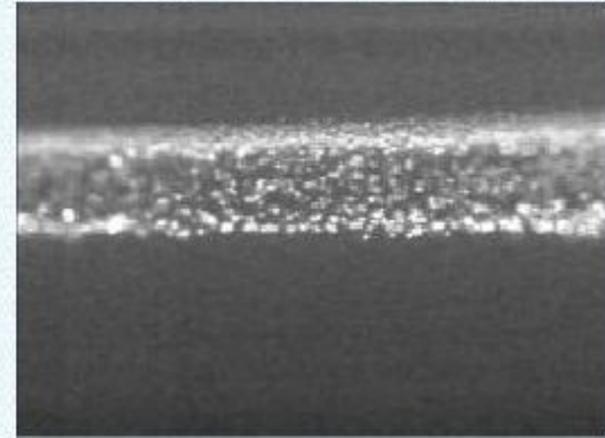
Onset of the instability:  $P=0.185$  Torr



Propagating waves:  $P=0.175$  Torr



Propagating waves:  $P=0.165$  Torr



Ticos, Smith & Shukla, Plasma Phys. Contr. Fusion, 2004.

## TWO-STREAM ION-DUST INSTABILITY

Dispersion relation (Shukla & Mamun, *Introduction to Dusty Plasma Physics*, IOP, 2002)

$$1 + \frac{1}{k^2 \lambda_D^2} - \frac{\omega_{pi}^2}{(\omega - ku)(\omega - ku + i\nu_i)} - \frac{\omega_{pd}^2}{\omega(\omega + i\nu_d)} = 0$$

Definitions:

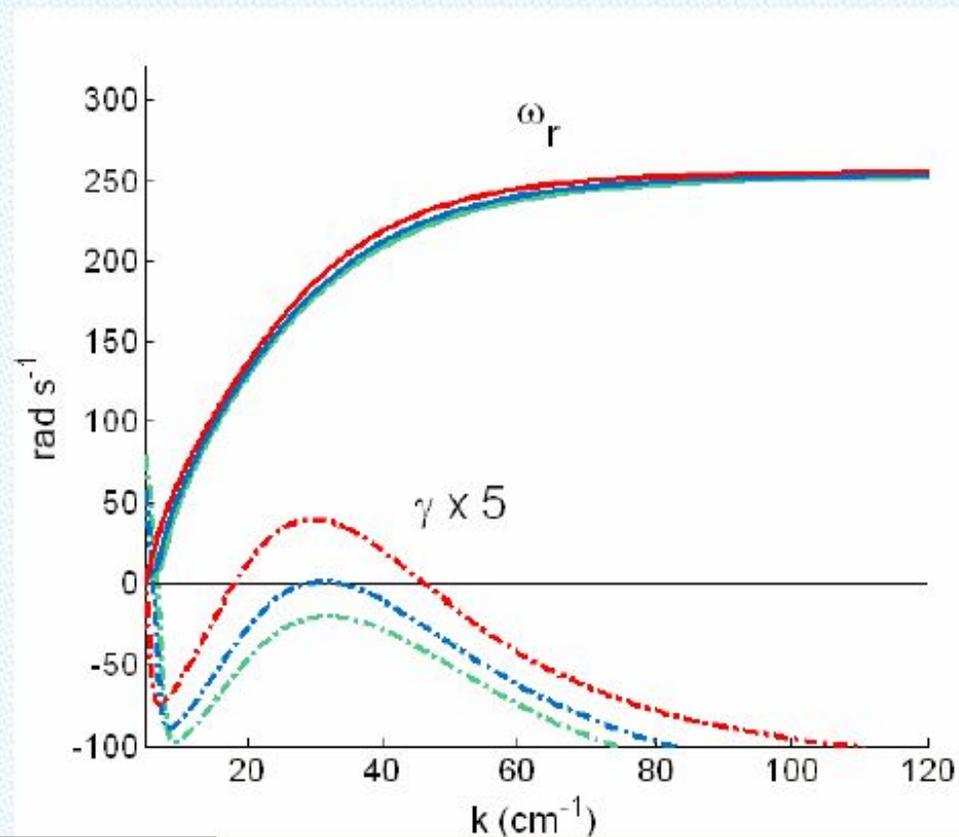
$$\nu_i = \sigma_i \left( \frac{P_n}{T_n} \right) u_B$$

$$\nu_d = \frac{4}{3} \pi r_d^2 \left( \frac{P_n}{T_n} \right) V_{Tn} \frac{m_n}{m_d}$$

## SOLUTION OF THE DISPERSION RELATION

$$u = u_B = 2.9 \cdot 10^3 \text{ ms}^{-1}, \quad n_d = 2 \cdot 10^{11} \text{ m}^{-3}, \quad Z_d = -2 \cdot 10^3 e,$$

$$T_e = 3.5 \text{ eV}, \quad T_i = 0.03 \text{ eV}, \quad n_e = n_i = 2 \cdot 10^{15} \text{ m}^{-3}, \quad \omega_{pi} = 9.3 \cdot 10^6 \text{ s}^{-1}$$



$\gamma < 0$ ,  $P = 0.3$  Torr (green)

$\gamma = 0$ ,  $P_C \approx 0.275$  Torr (blue)

$\gamma > 0$ ,  $P = 0.23$  Torr (red)

- $\omega_r$  strongly depends on  $Z_d$ .

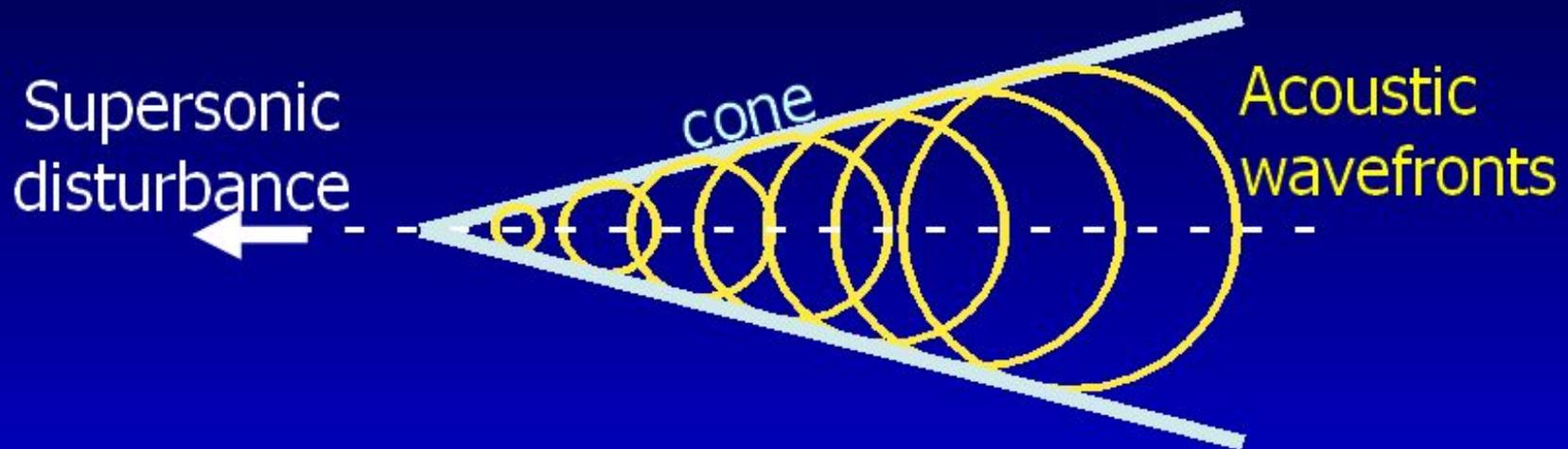
- $Z_d = -2 \cdot 10^3 e$  chosen such that  $\omega_r$  agrees with the experiment.

## **Mach Cone: Movie**

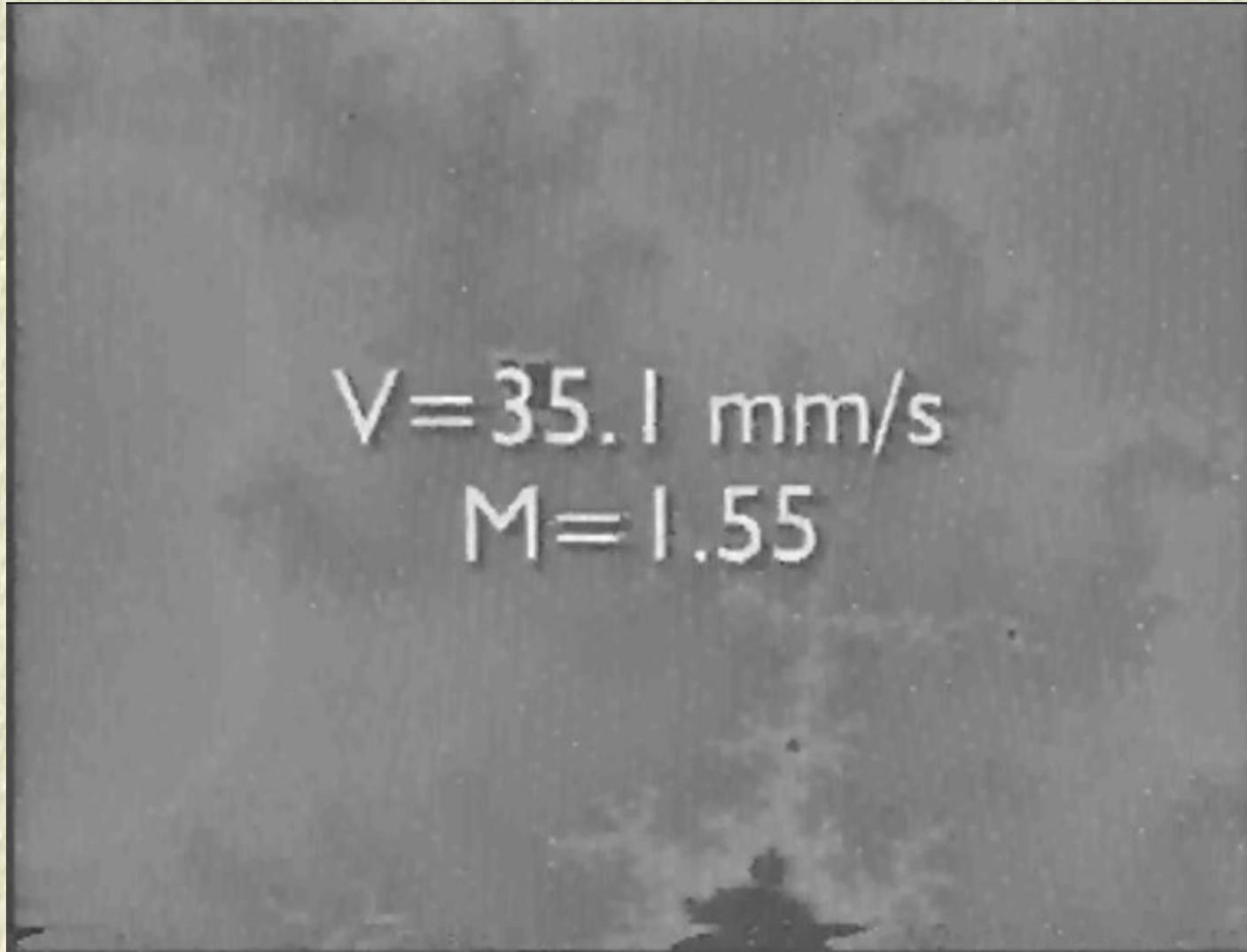


## PHYSICS OF MACH CONES

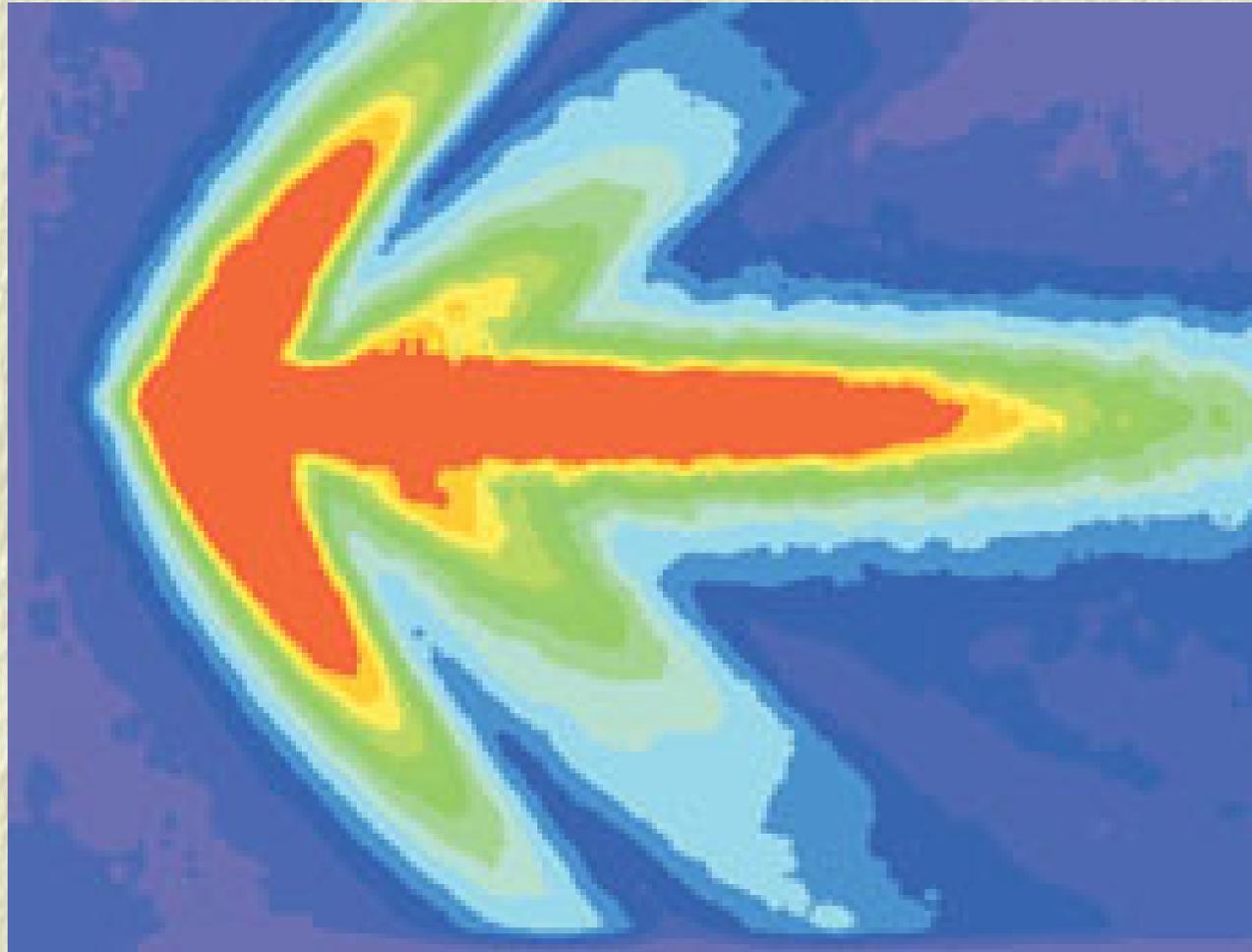
### Laser-excited Mach Cones



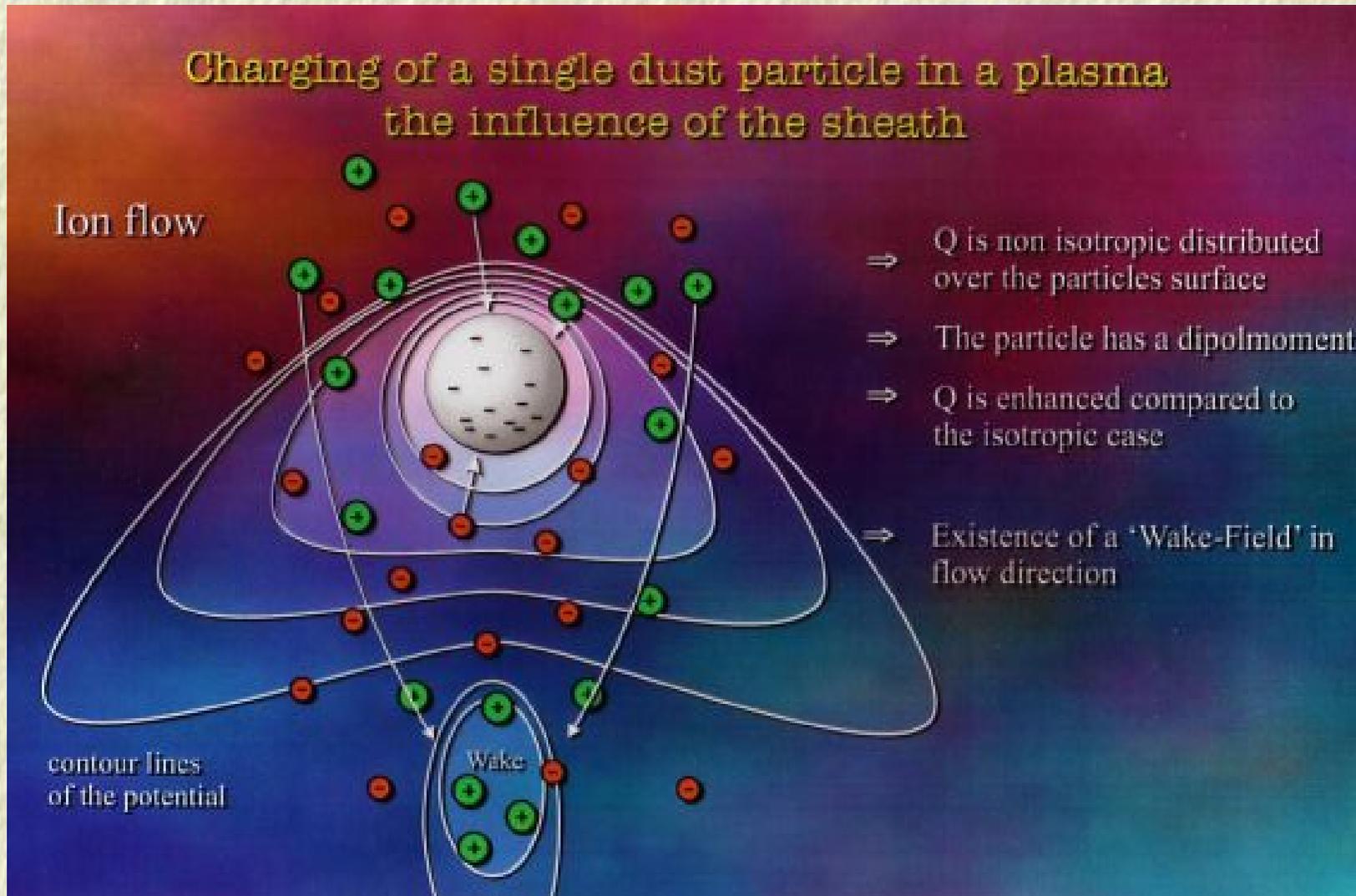
## MACH CONES IN DUST CRYSTALS



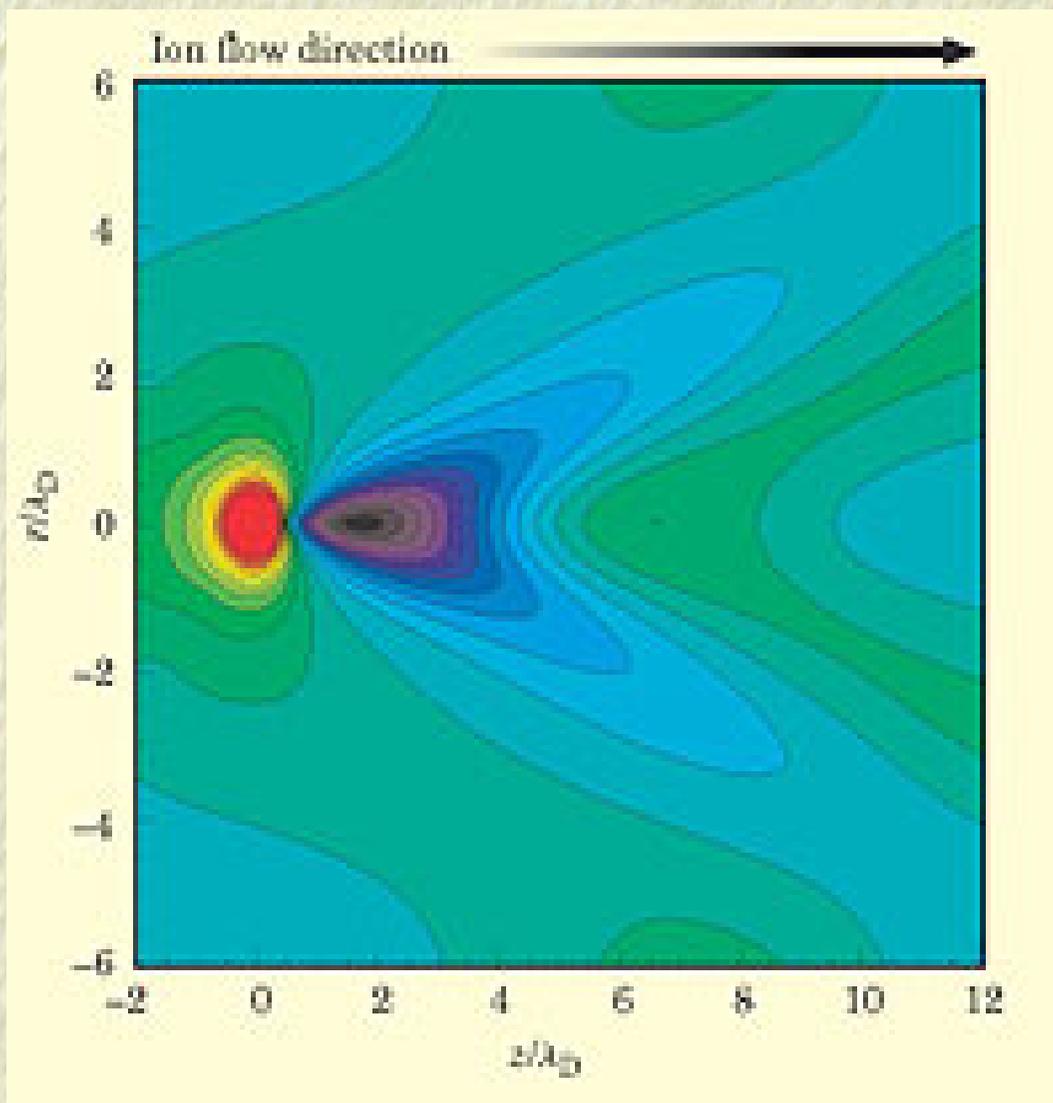
## DOUBLE MACH CONES



## WAKE FIELD

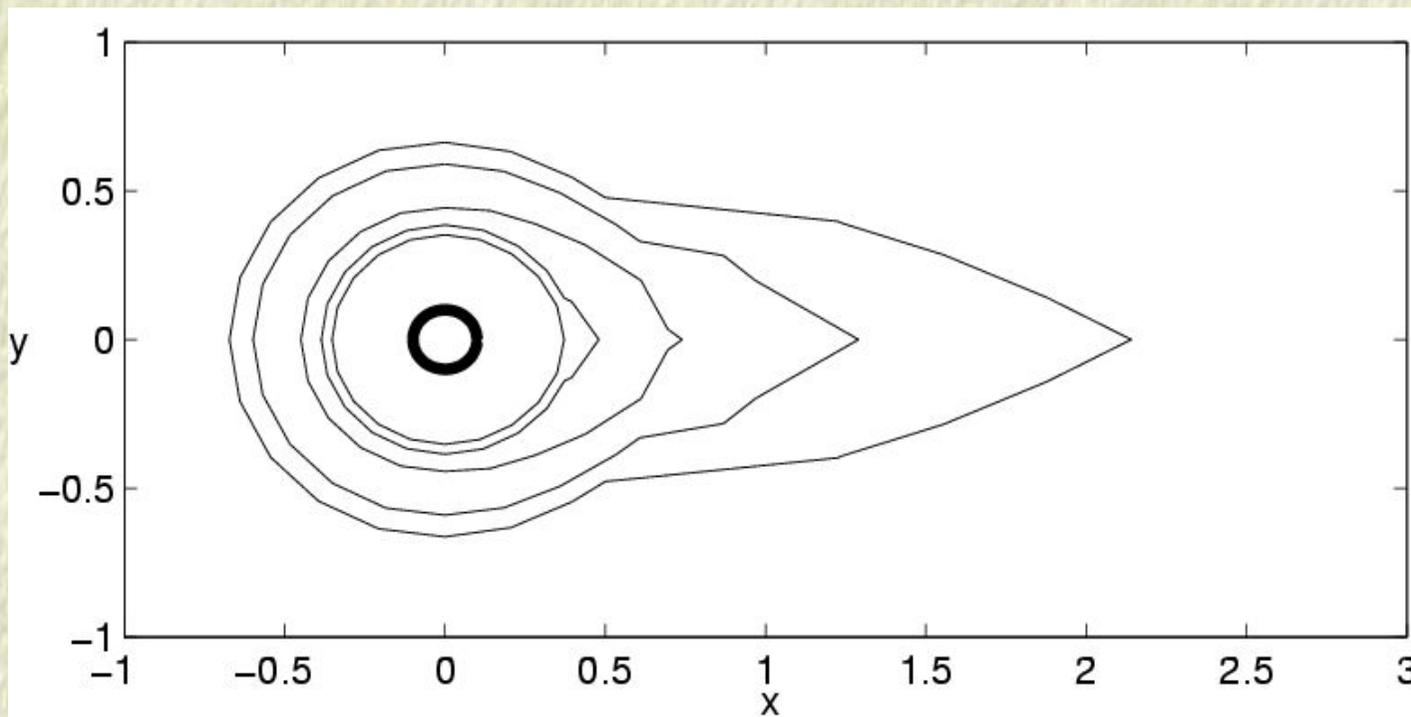


# ION WAKE



## ION WAKE, KINETIC DESCRIPTION

D. D. Tskhakaya, P. K. Shukla, and B. Eliasson, Phys. Lett. A 331,404 2004.



## THEORY OF DIA SHOCK WAVES

### DISSIPATION + DISPERSION

$$\omega \approx kC_s \left( 1 - \frac{k^2}{2k_0^2} \right) - i\nu k^2 \lambda^2$$

### WAVES IN A DISSIPATIVE MEDIUM

$$\frac{\partial u}{\partial t} + C_s \frac{\partial u}{\partial x} + \frac{C_s}{2k_0} \frac{\partial^3 u}{\partial x^3} = \nu \lambda^2 \frac{\partial^2 u}{\partial x^2}$$

## THEORY OF DIA SHOCK WAVES

### K-dV-BURGERS EQUATION

$$\frac{\partial u}{\partial t} + \alpha u \frac{\partial u}{\partial x} + \frac{C_s}{2k_0^2} \frac{\partial^3 u}{\partial x^3} = \nu \lambda^2 \frac{\partial^2 u}{\partial x^2}$$

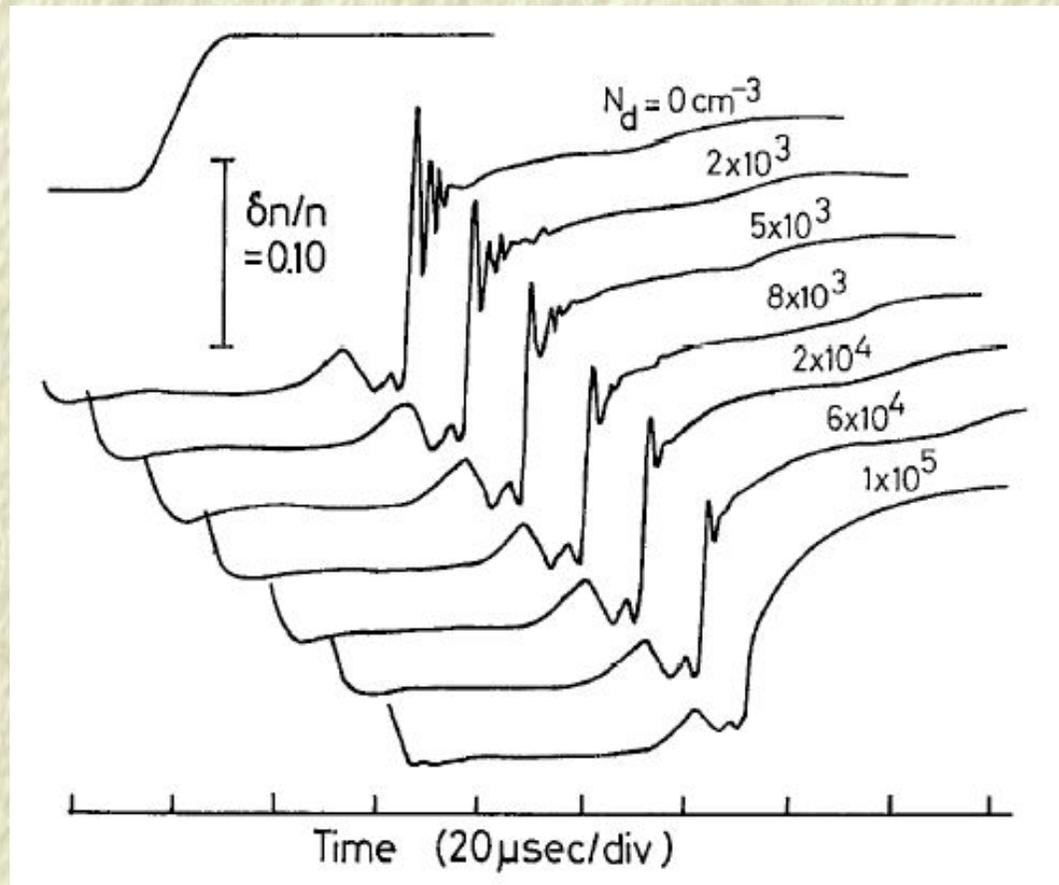
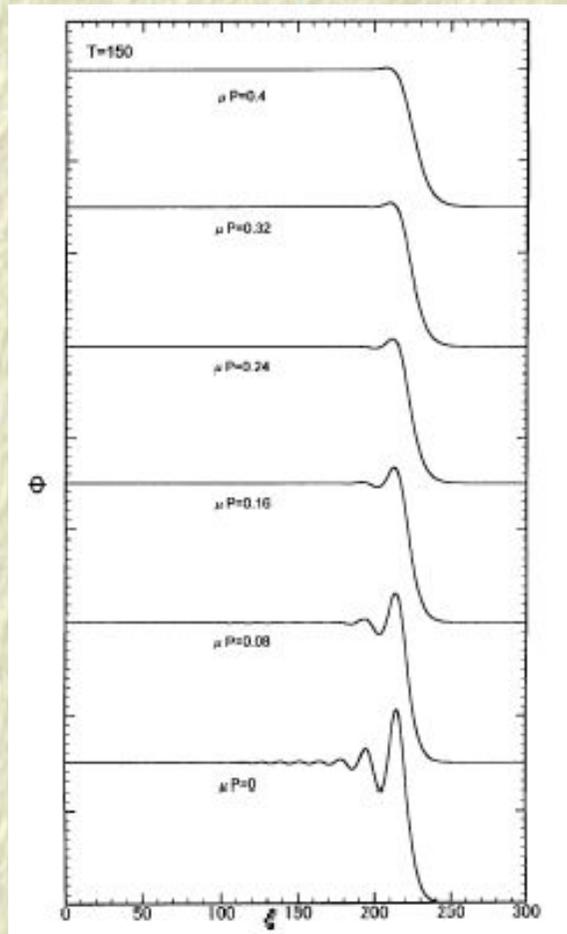
### WITHOUT DISPERSION

$$u = V(1 - \tanh\theta)$$

### WITH

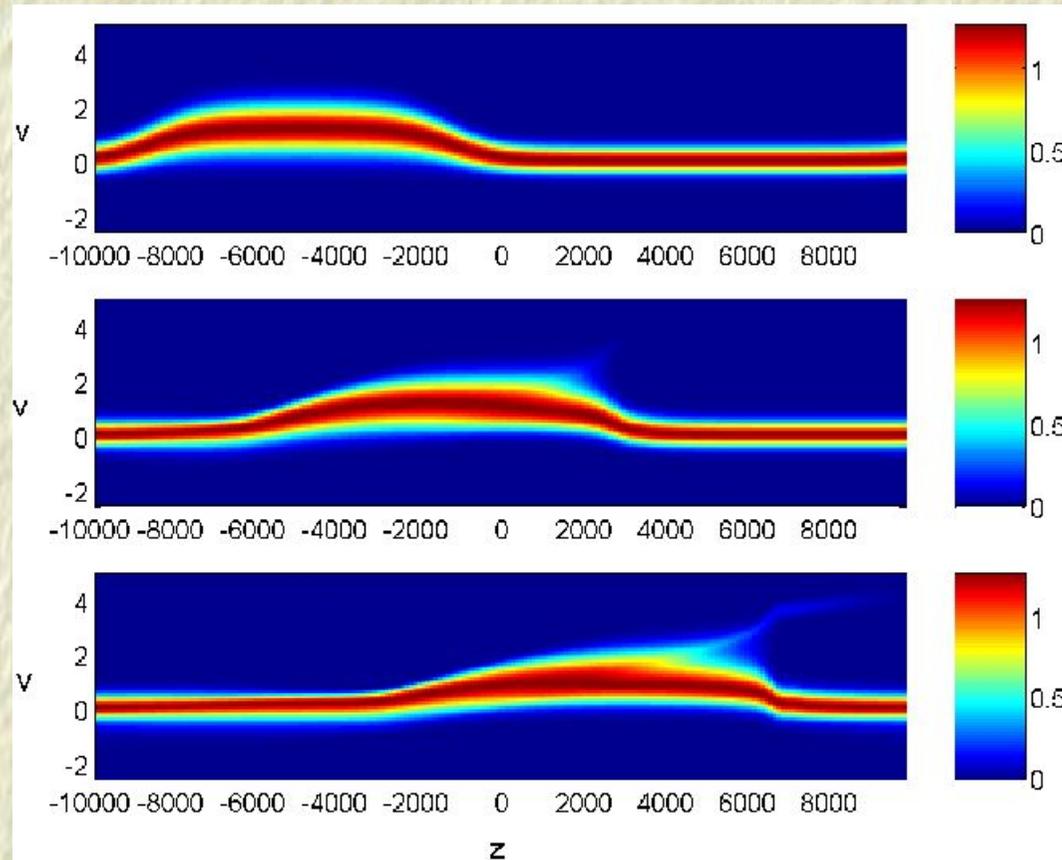
$$\theta = \frac{V(x - Vt)}{\delta_s}, \quad \delta_s = 2\nu\lambda^2, \quad \alpha = 1$$

## DIA SHOCK WAVE: SIMULATIONS & OBSERVATIONS



Nakamura, Bailung & Shukla, Phys. Rev. Lett. 1999

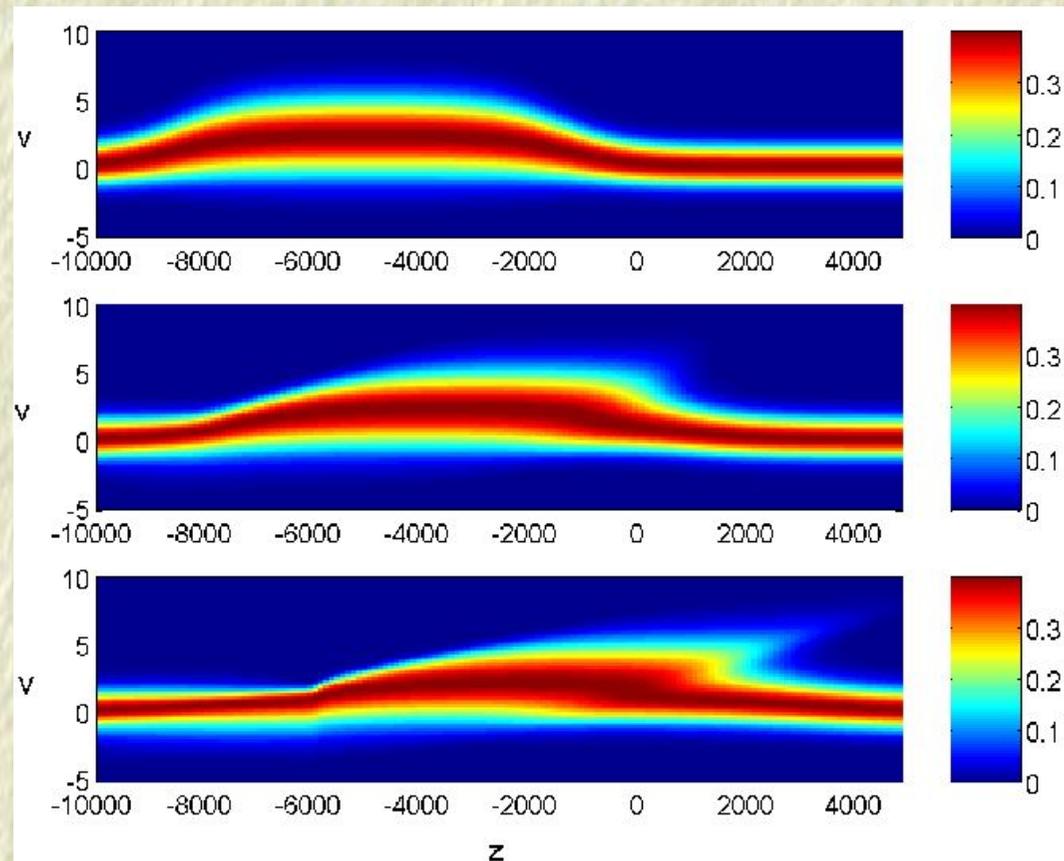
## DIA SHOCK WAVE: VLASOV SIMULATION



$$T_i/T_e = 0.1, \quad n_{e0}/n_{i0} = 0.25$$

Eliasson & Shukla, Phys. Plasmas, 2004.

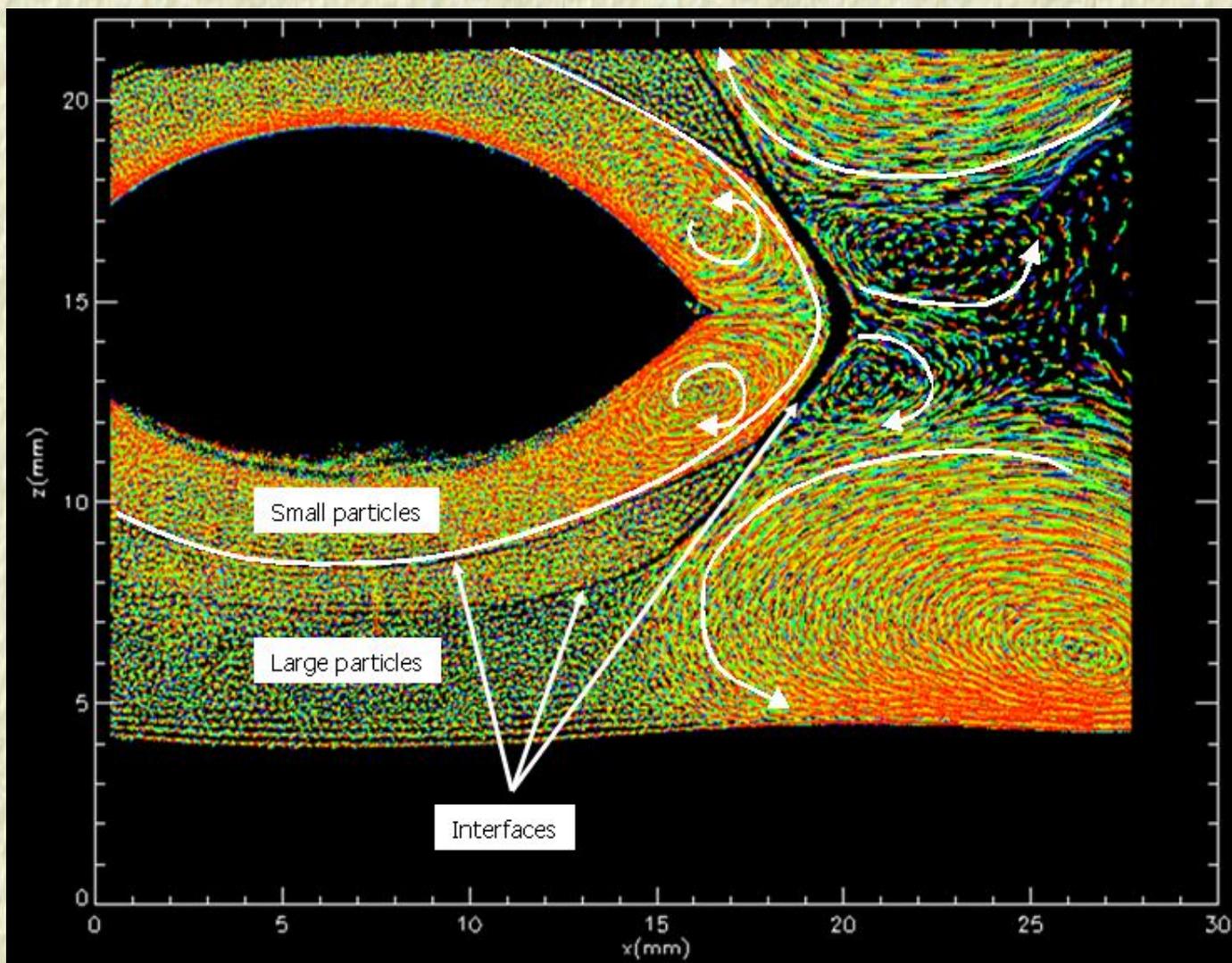
## DIA SHOCK WAVE: VLASOV SIMULATION



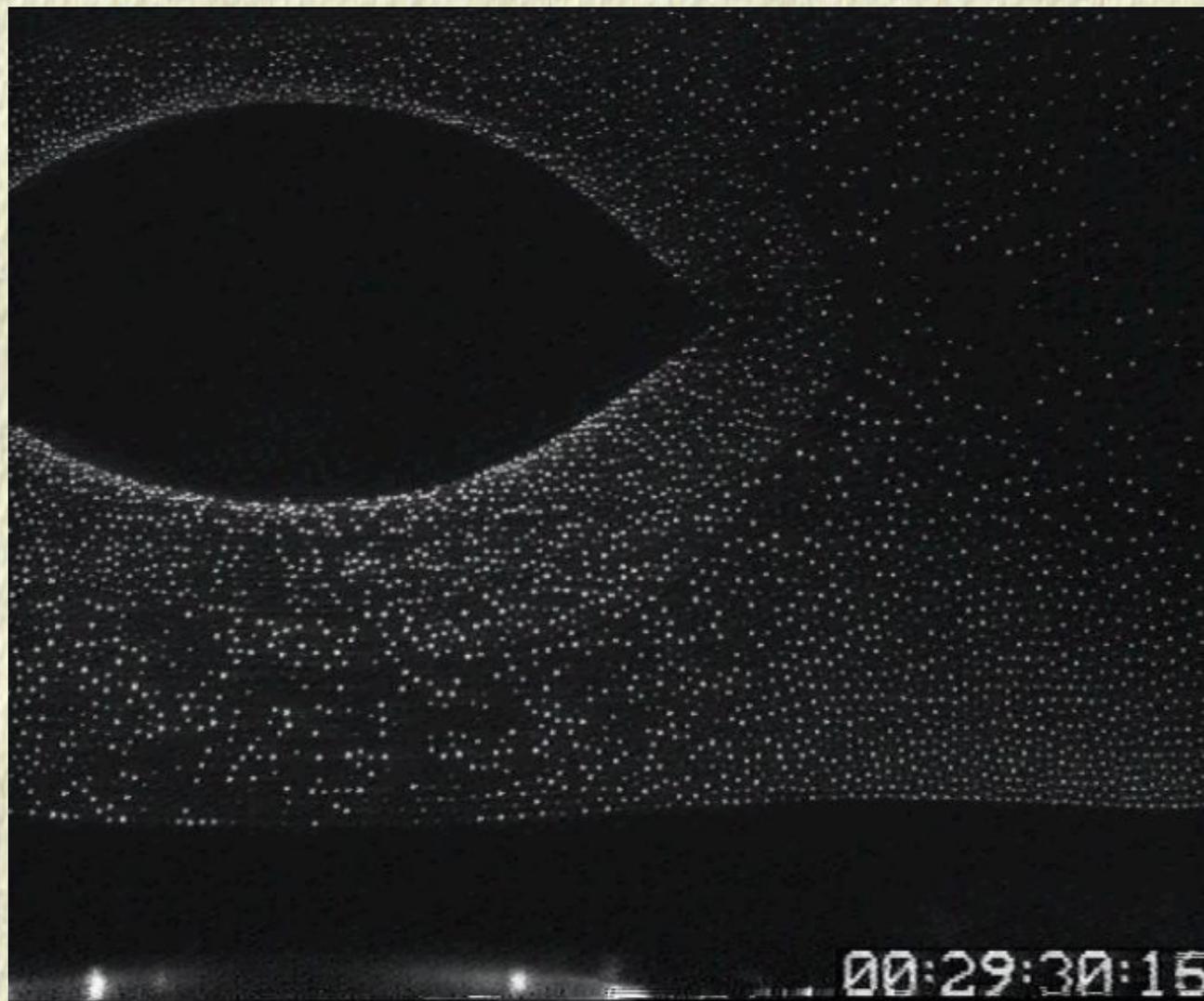
$$T_i/T_e = 1, \quad n_{e0}/n_{i0} = 0.05$$

Eliasson & Shukla, Phys. Plasmas, 2004.

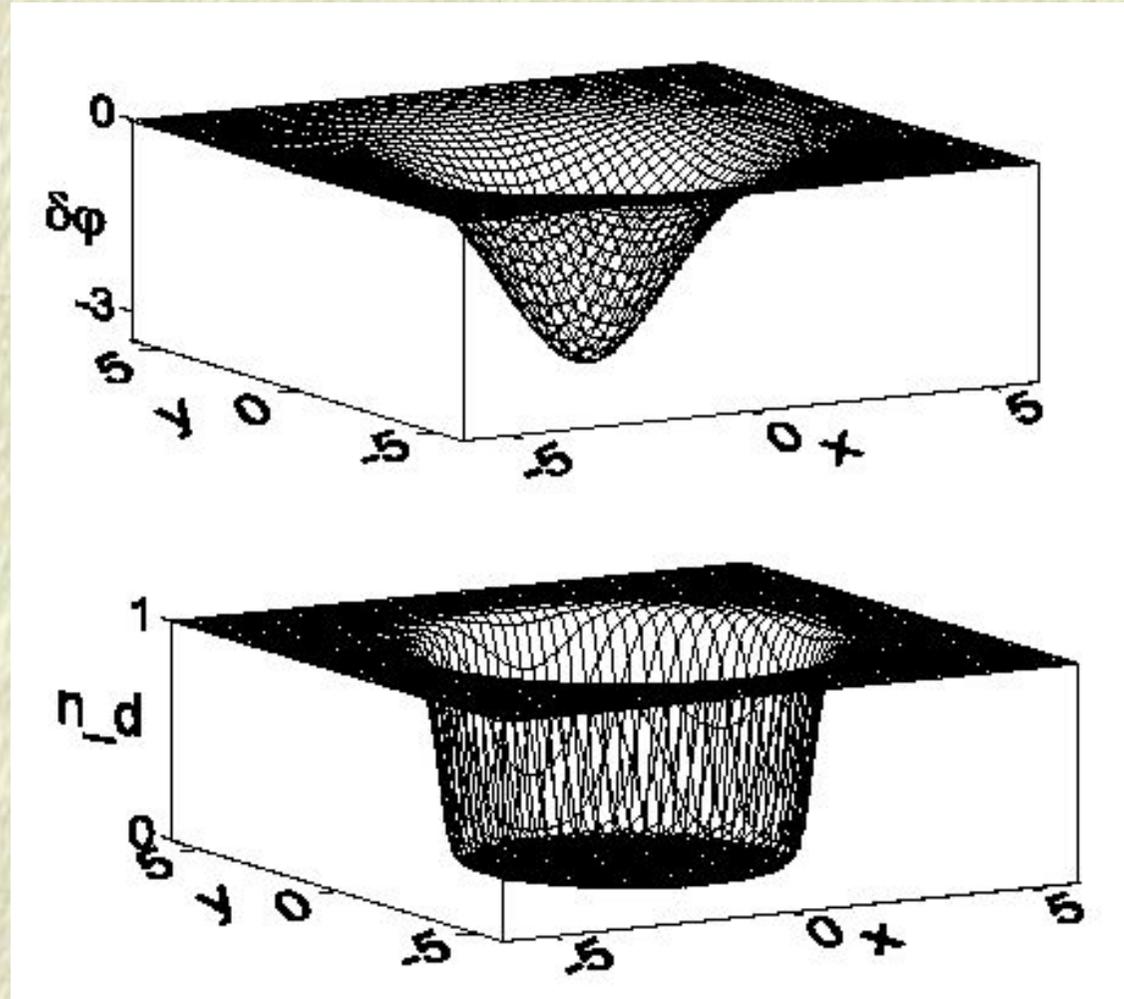
# MOVIE OF VORTICES AROUND DUST VOID



## MOVIE OF DUST VOID CLOSURE



## DUST VOID IN MAGNETIZED PLASMAS



Jovanović & Shukla, Phys. Lett A, 2004.

## **SUMMARY & CONCLUSIONS**

- A. WE HAVE DISCUSSED PROPERTIES OF DUSTY PLASMAS
- B. DUST CHARGING
- C. OCCURRENCE OF DUSTY PLASMAS IN SATURN RINGS, COMET TAILS, SPACE NEBULAS AND IN NOCTILUCENT CLOUDS IN POLAR MESOSPHERE
- D. DUST IN COMMERCIAL PLASMA ETCHING REACTORS AND IN TOKAMAKS
- E. NEW FORCES: WAKE FIELDS
- F. NONLINEAR STRUCTURES: MACH CONES, DIA SHOCKS, VOIDS, VORTICES