



**The Abdus Salam
International Centre for Theoretical Physics**



2132-2

Winter College on Optics and Energy

8 - 19 February 2010

Physics of Solar Cells (I)

J. Nelson
*Imperial College
London
U.K.*



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Physics of Solar Cells (I)

Jenny Nelson
Department of Physics
Imperial College London
(jenny.nelson@imperial.ac.uk)



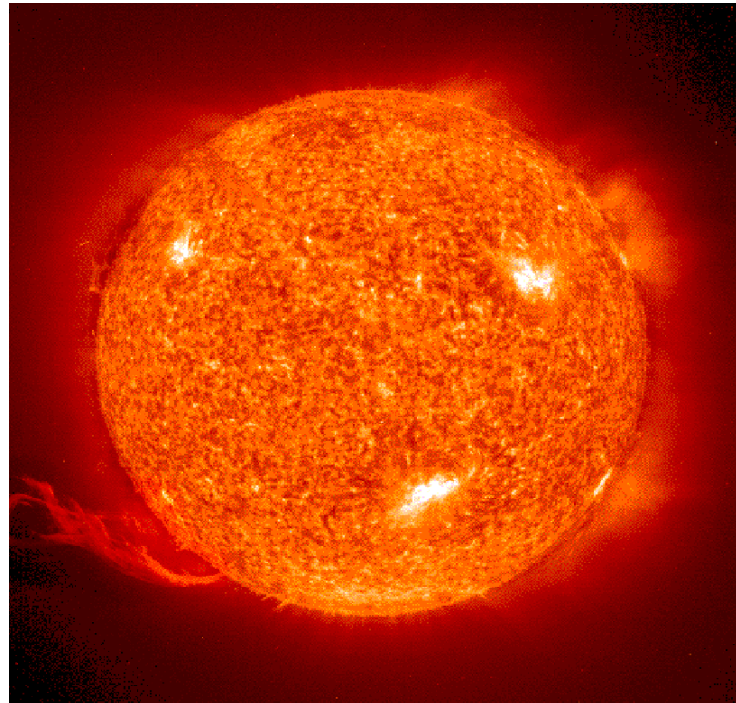
Outline

1. Photovoltaic applications
2. The solar resource
3. Photovoltaic energy conversion
4. The p-n junction solar cell
5. Solar cell performance characteristics



The solar energy resource

- Radiant power at Earth's surface ~ 100000 TW

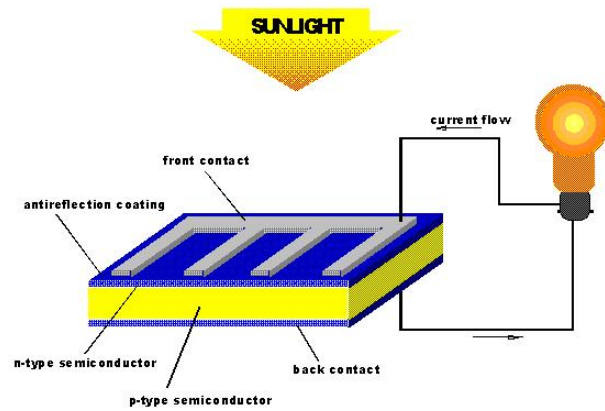


- Electricity consumption ~ 2 TW
- 80% from fossil fuels & nuclear, 0.1% from PV

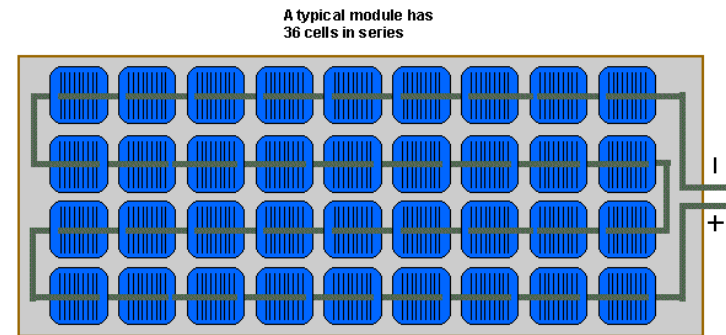


Some concepts in PV

Solar cell



Module



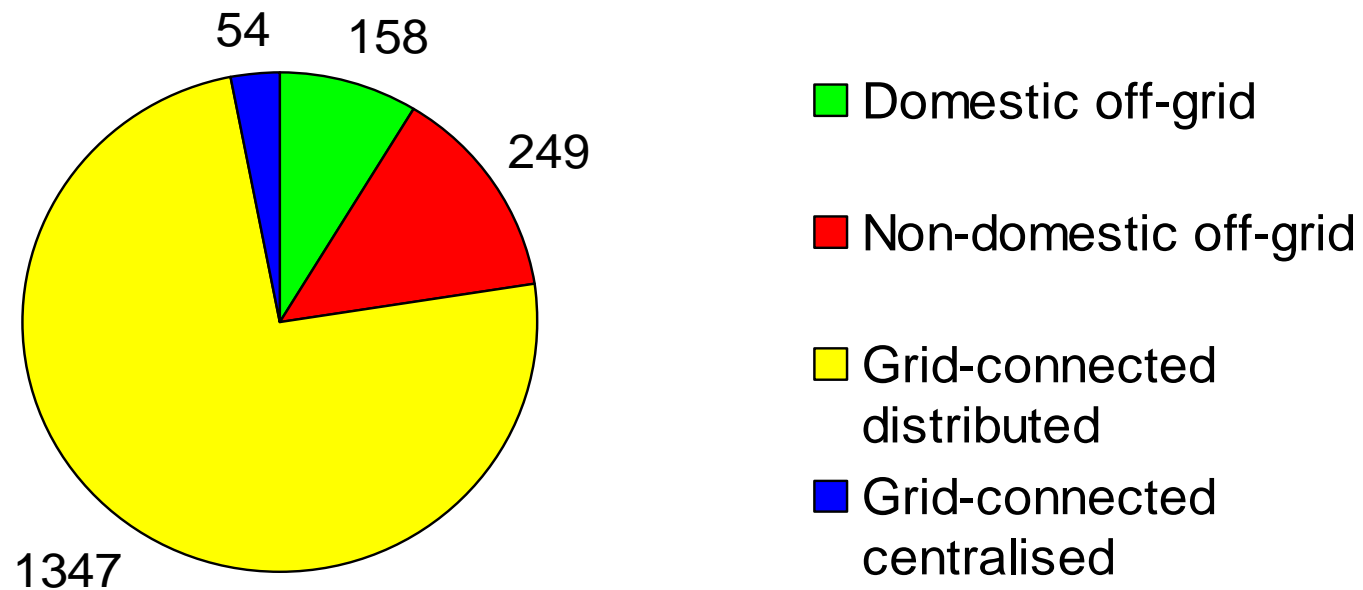
System



1.1. PHOTOVOLTAIC APPLICATIONS



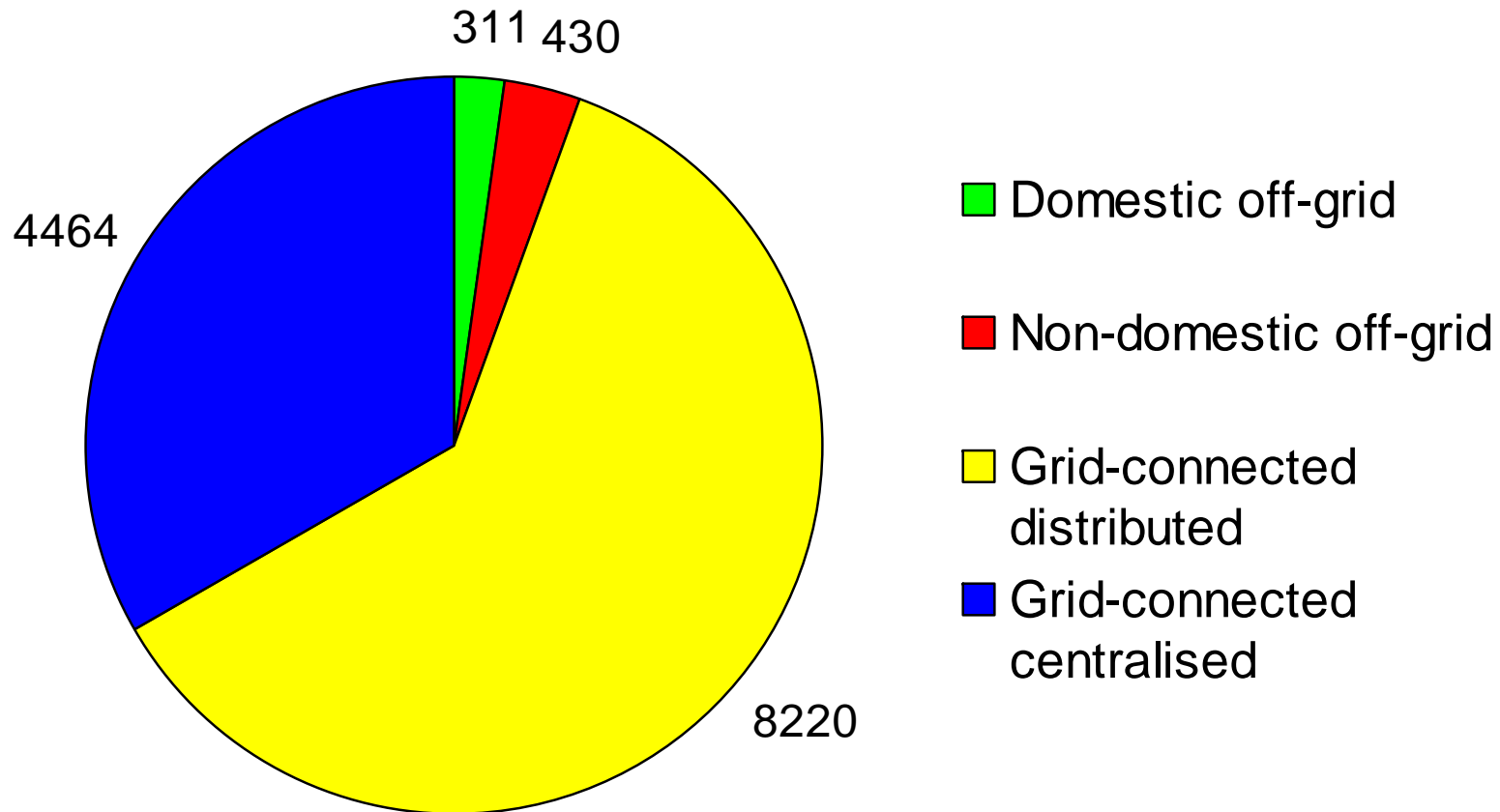
Photovoltaic applications



Cumulative PV capacity 2003 (MW): 1.8 GW_p



Photovoltaic applications



Cumulative PV capacity 2008 (MW): 13.4 GW_p





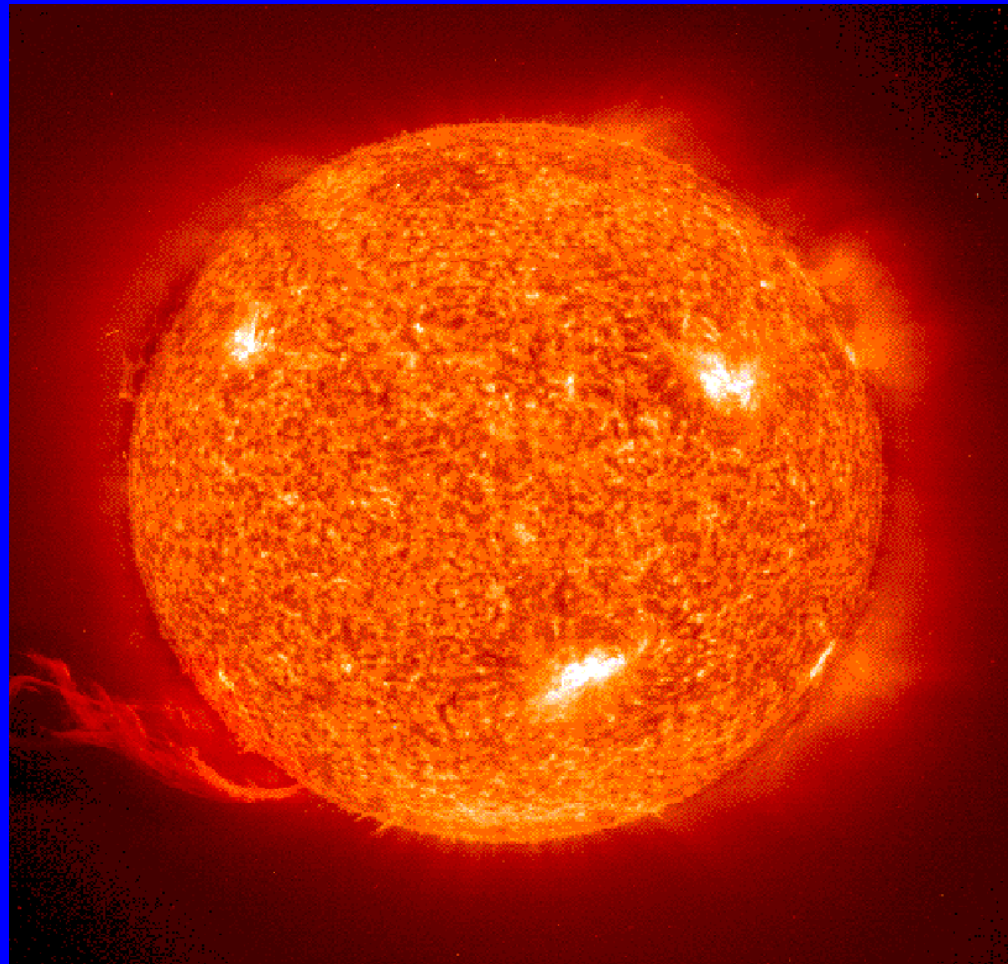




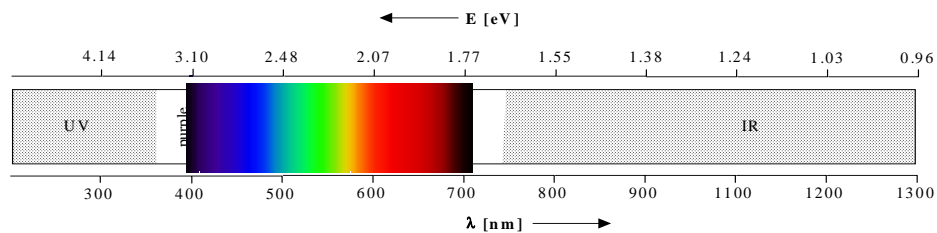
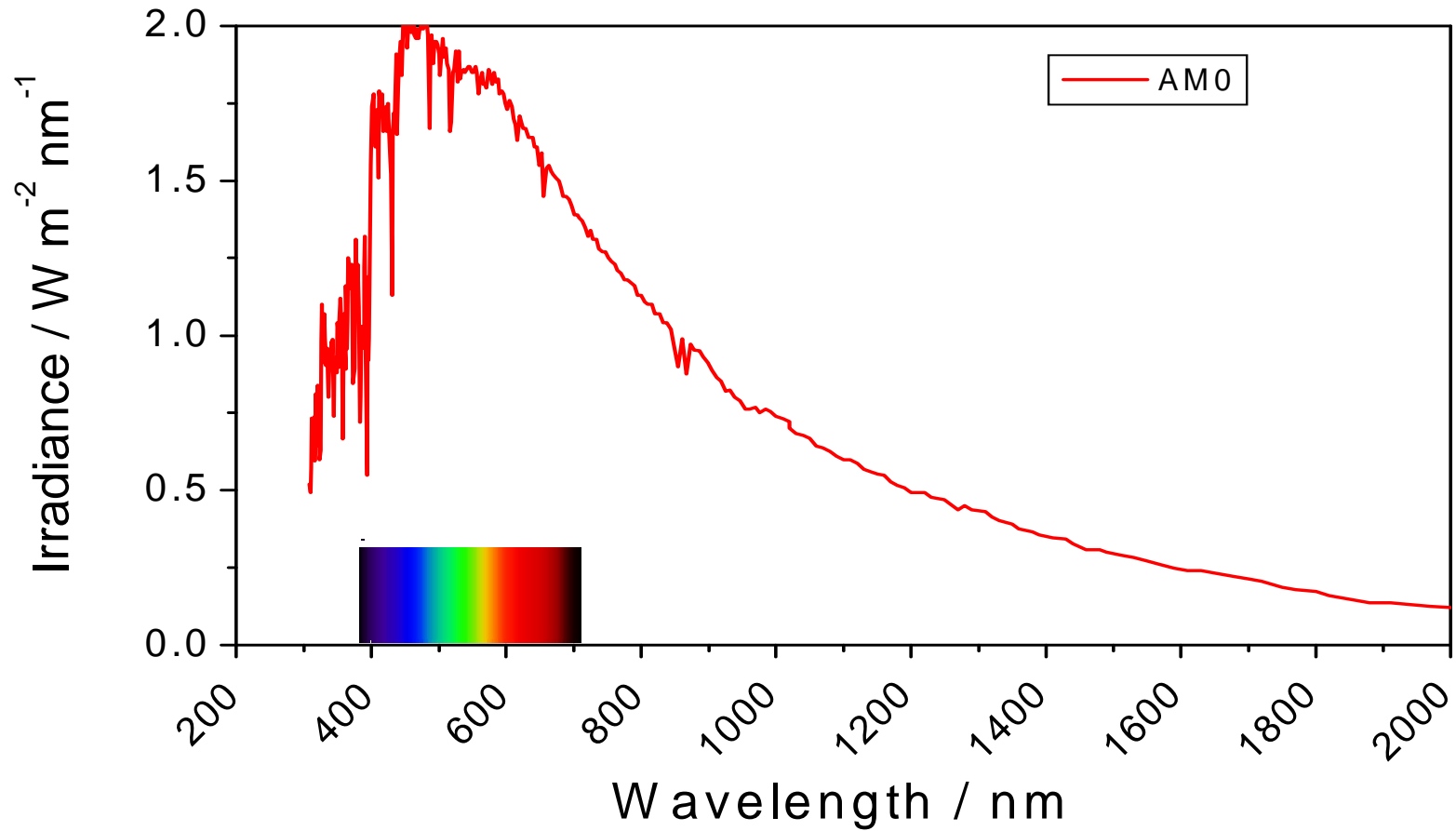




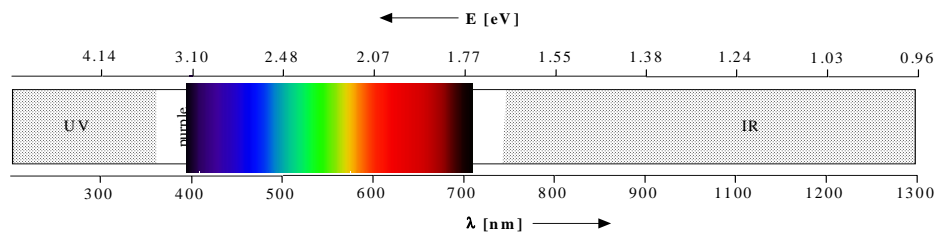
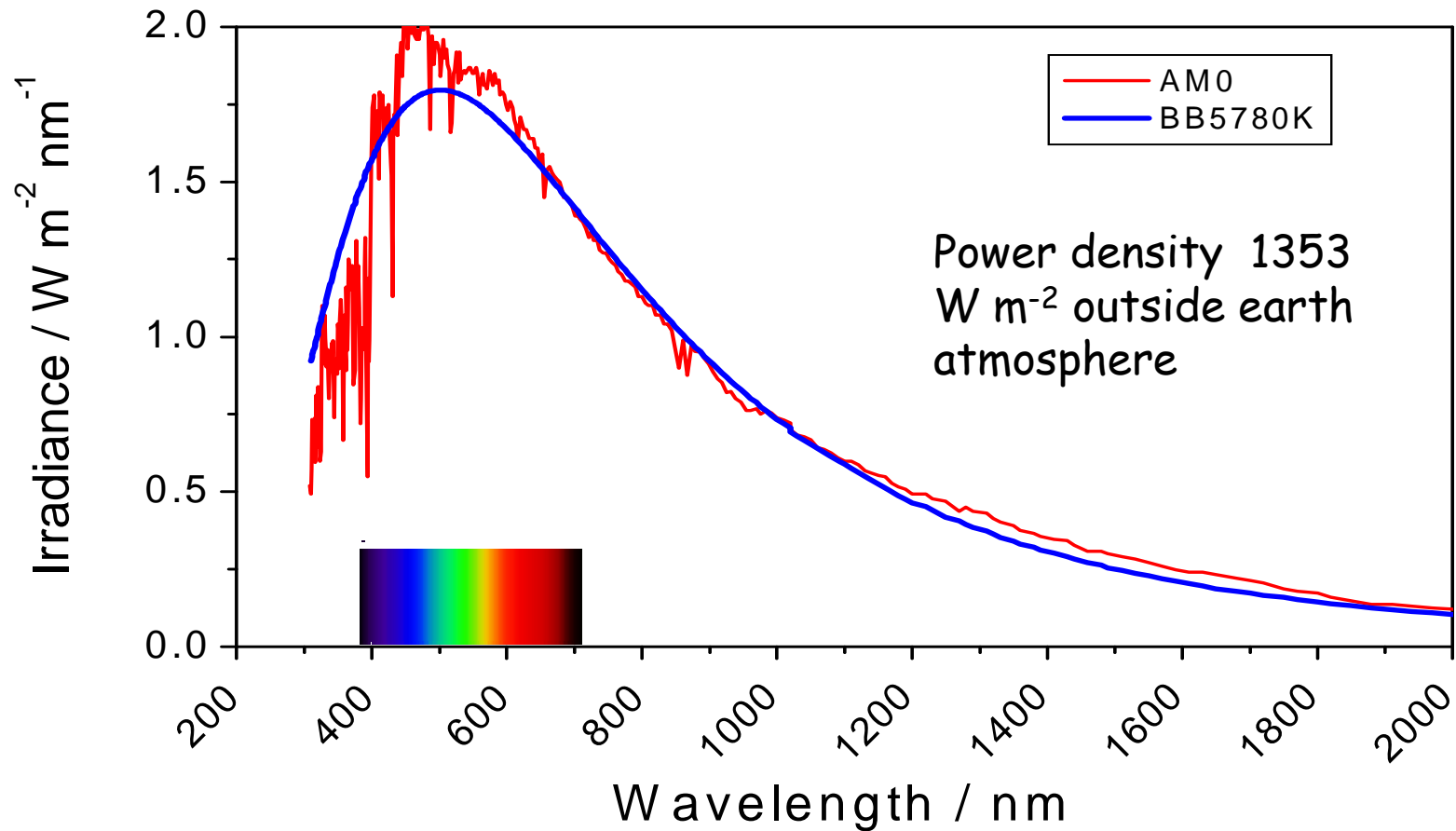
1.2. THE SOLAR RESOURCE



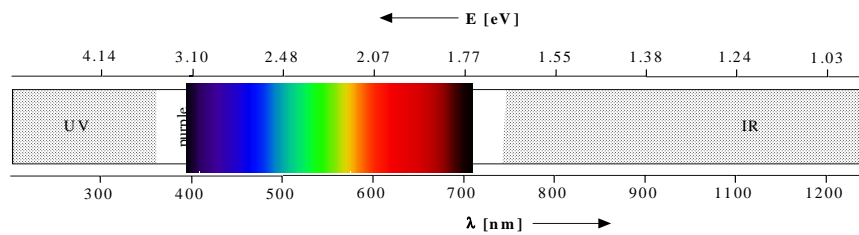
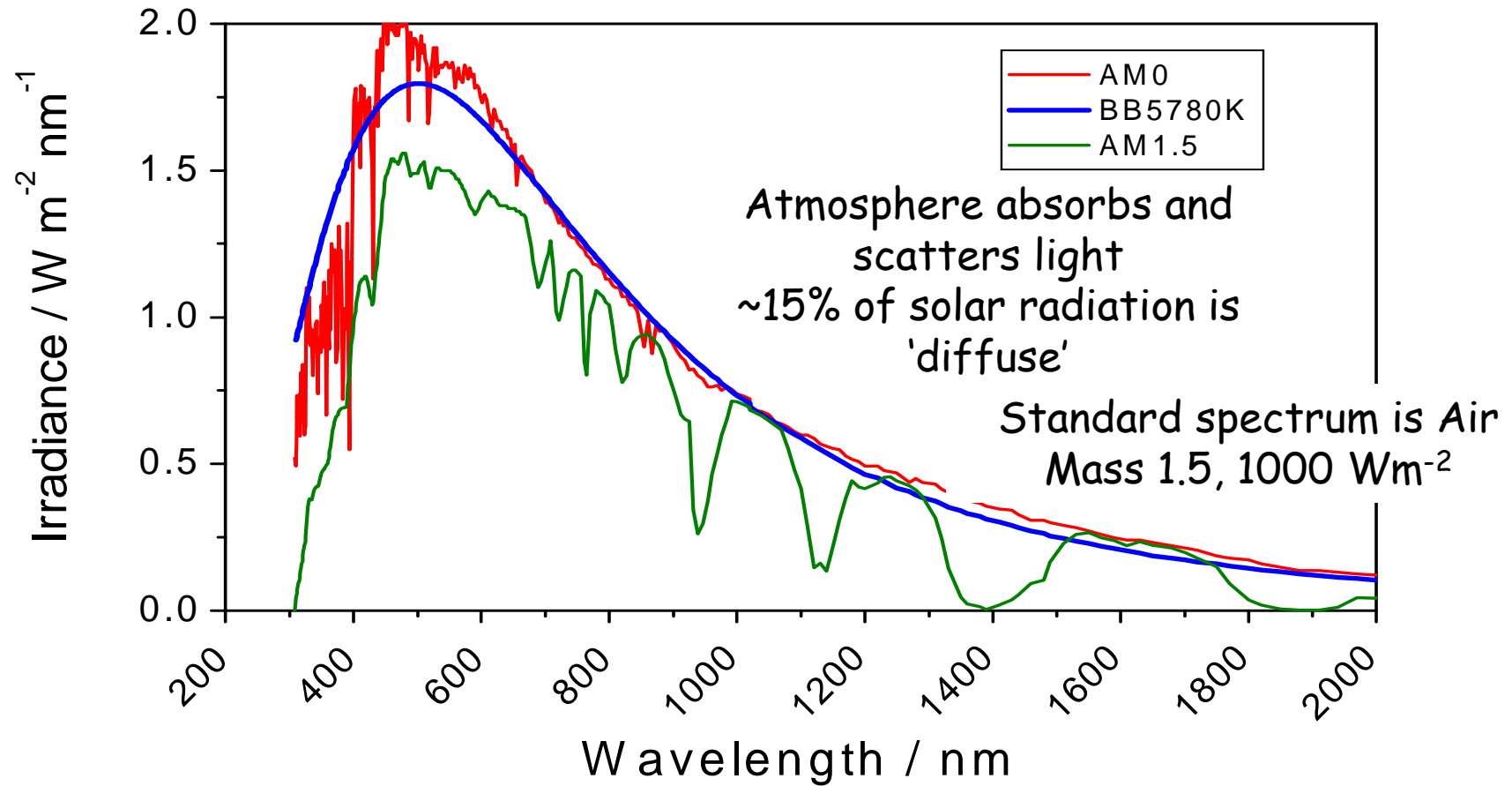
Solar power spectrum



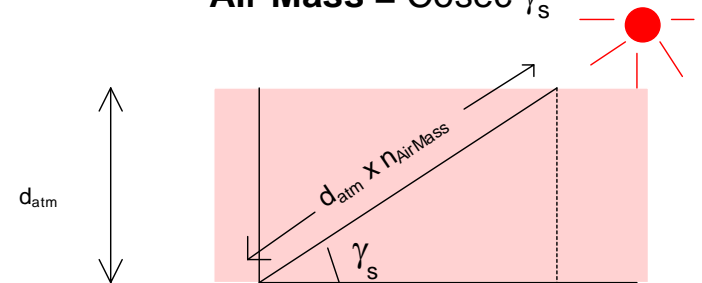
Solar power spectrum

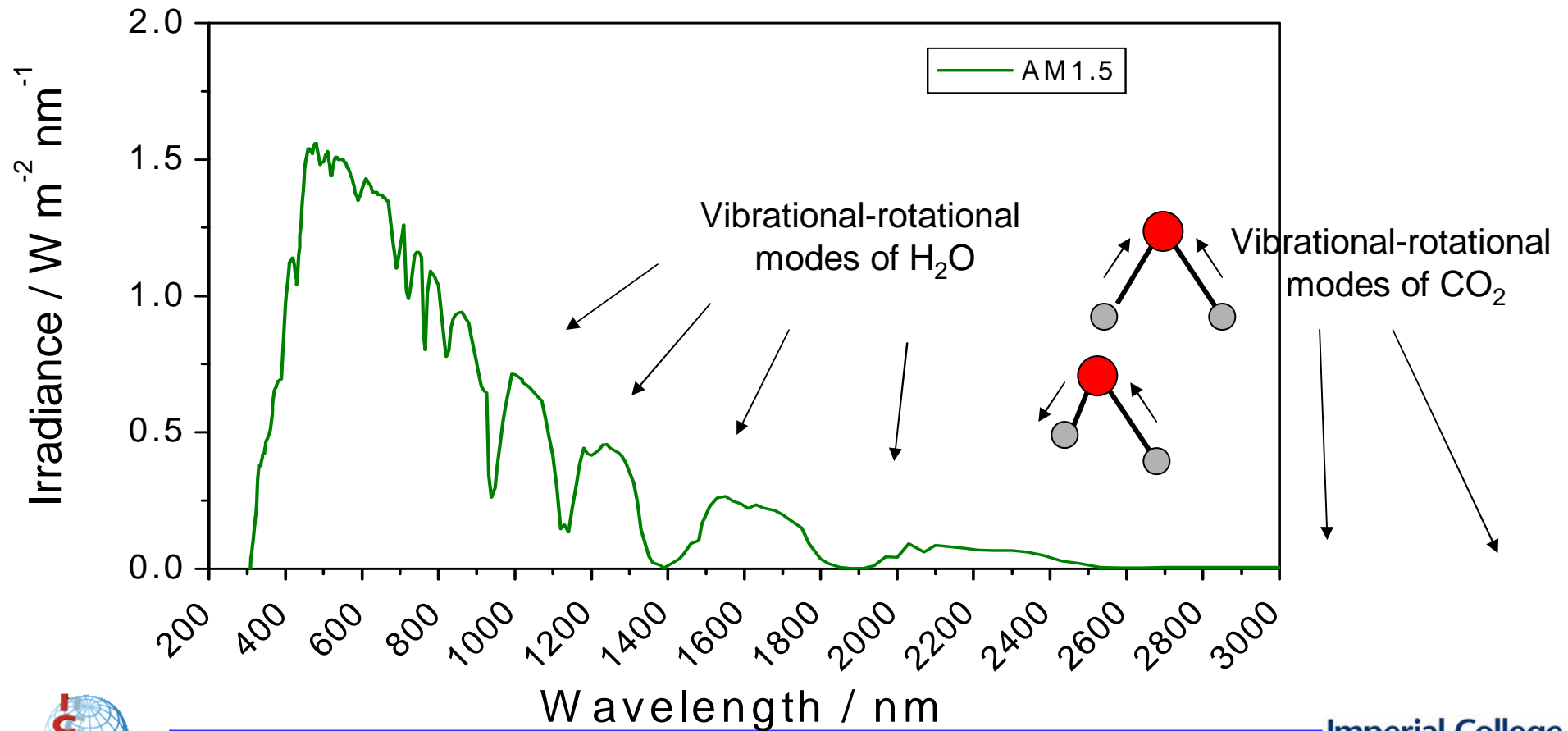
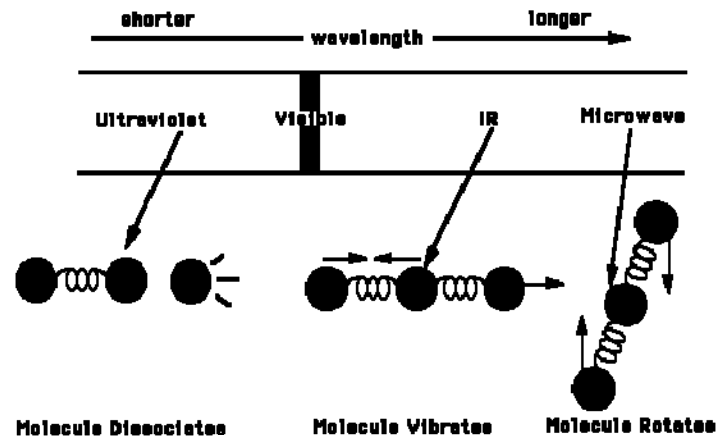


Solar power spectrum



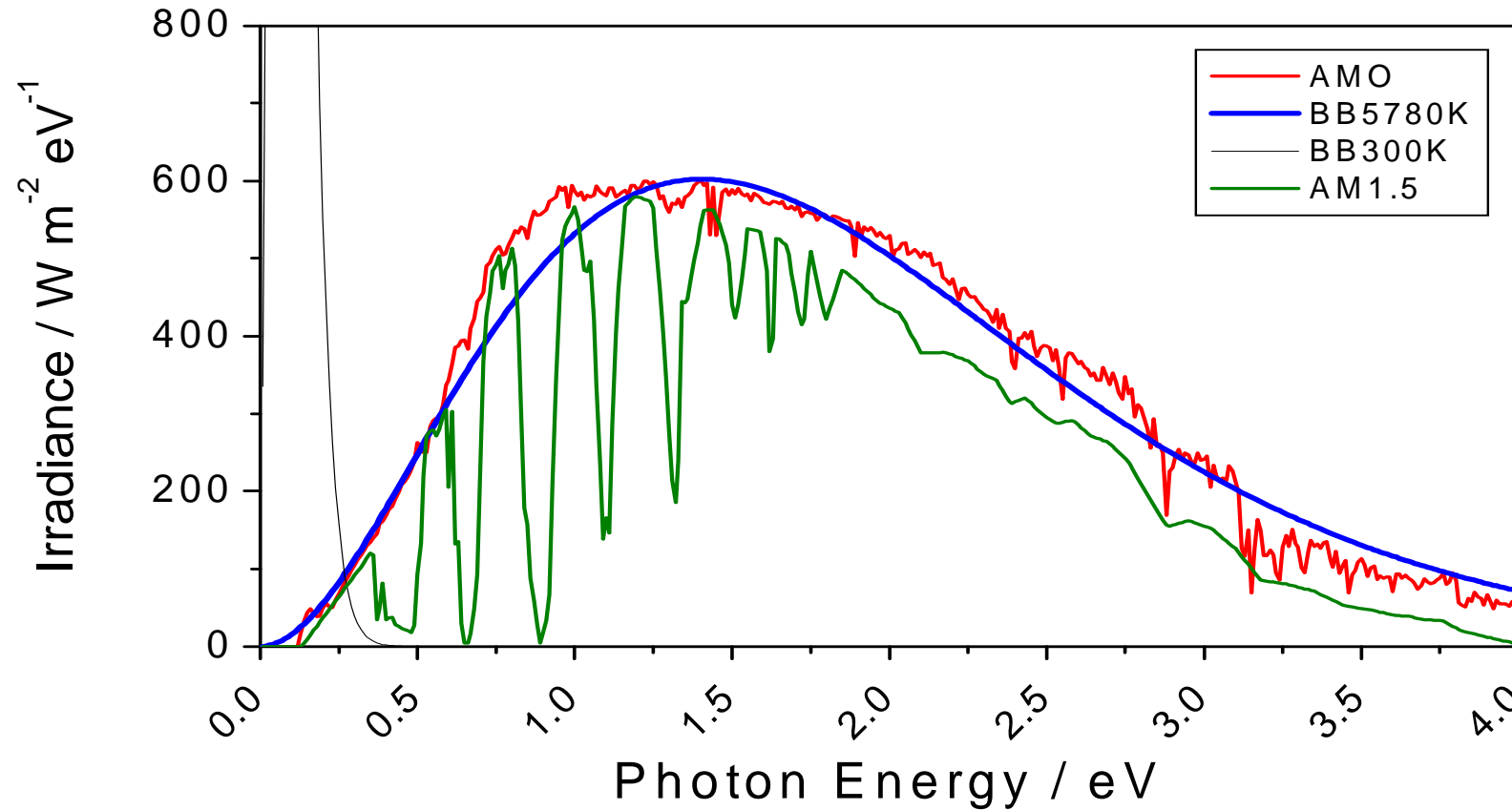
Air Mass = $\text{Cosec } \gamma_s$





Solar power spectrum

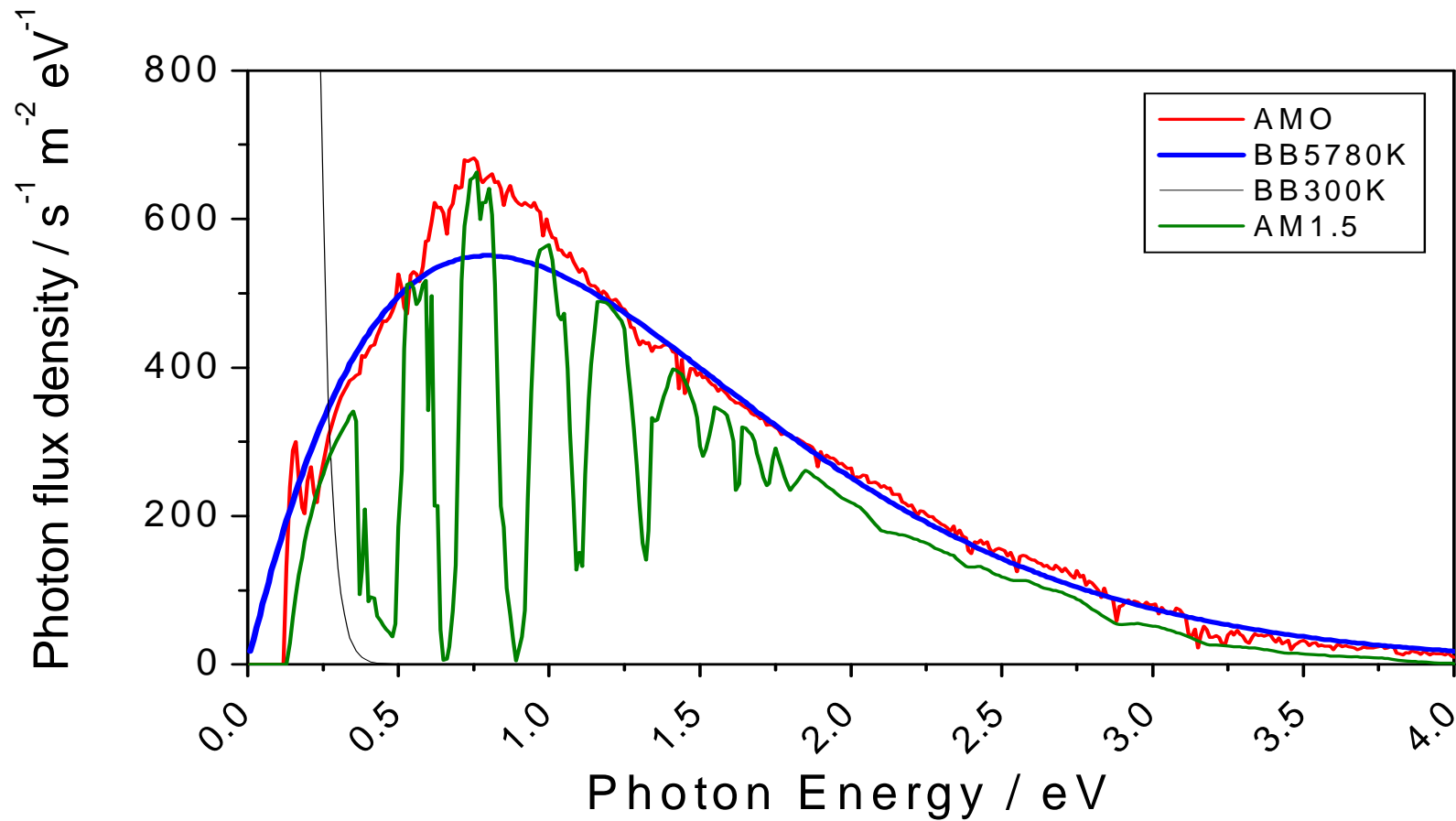
$$E / \text{eV} = 1240 / (\lambda / \text{nm})$$



← visible →



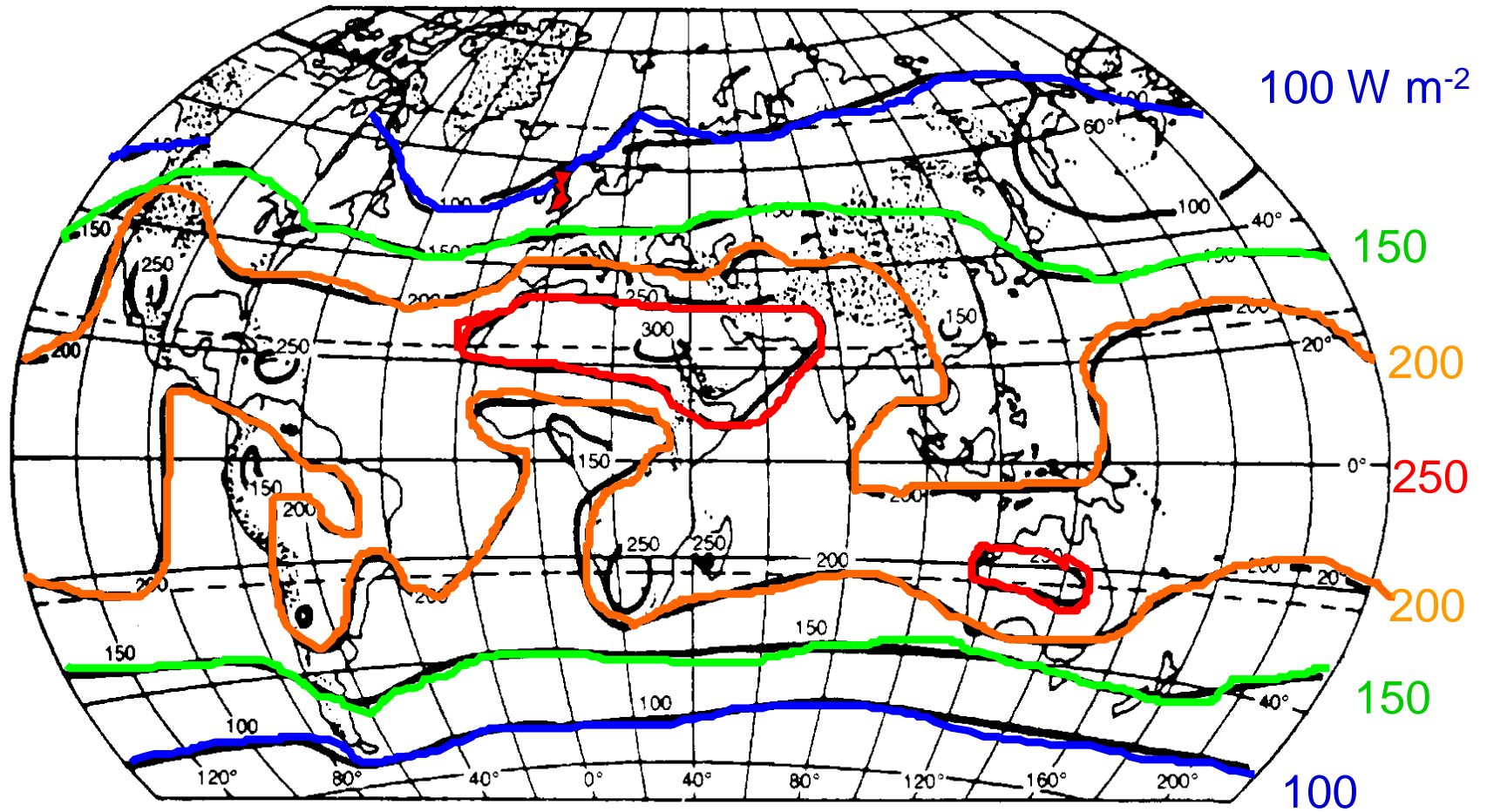
Solar photon flux spectrum



Important quantity for PV is solar photon *flux* density (not power density)

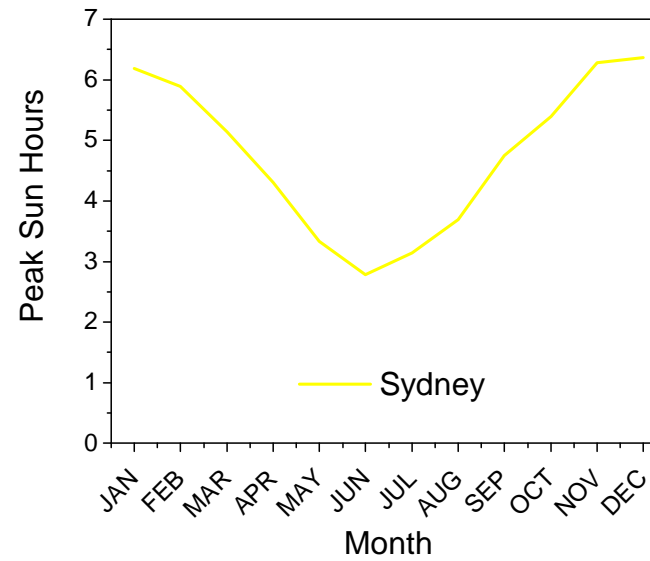
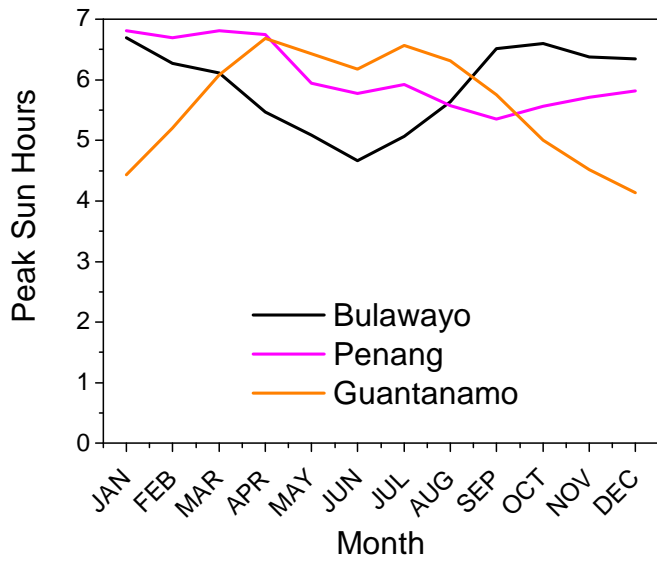
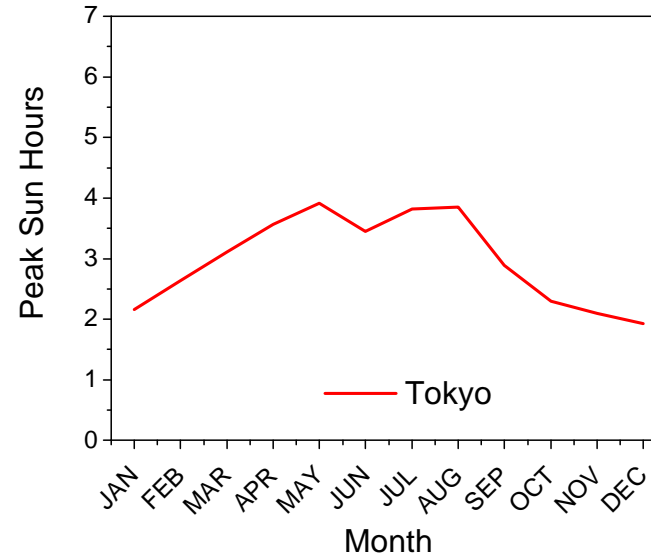
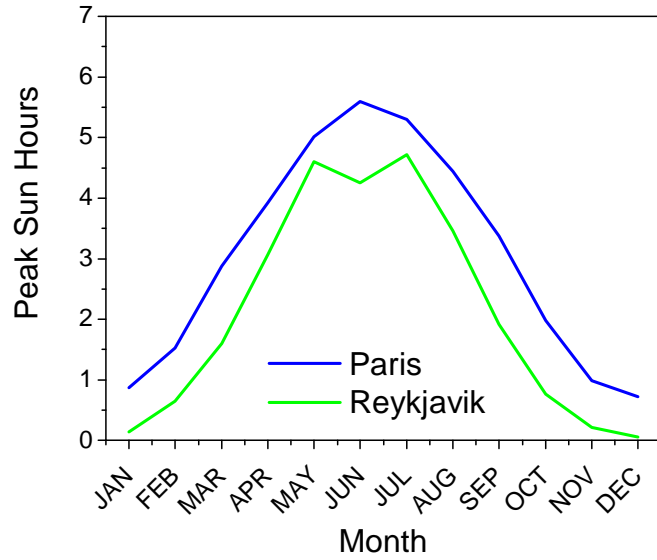


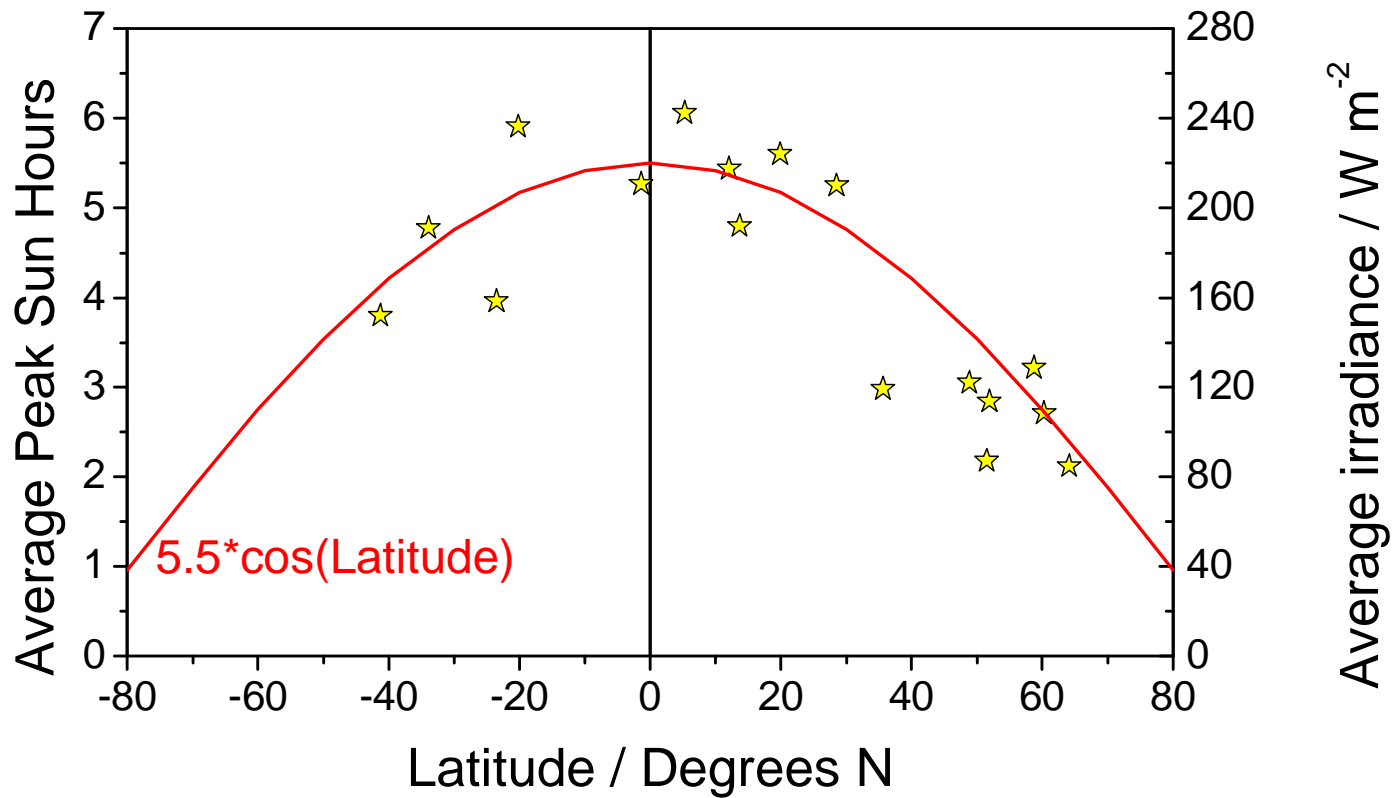
Average $\sim 200 \text{ Wm}^{-2}$ (5 peak sun hours)



Southern Britain $\sim 125 \text{ Wm}^{-2}$ (~ 3 peak sun hours)







What will be the consequences of latitude on off-grid power generation?



Energy consumption per capita in Western Europe ~ 5 kW

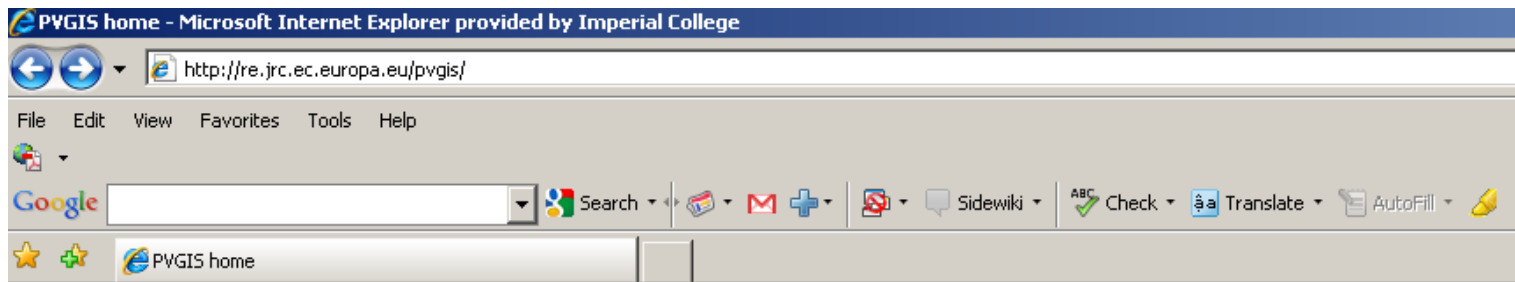
Mean solar irradiance in Southern Britain ~ 125 W m⁻²

What land area is needed to supply the energy needs of a city of 10 million people using solar irradiation:

(a) with conversion efficiency of 50%?

(b) with conversion efficiency of 5%





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Photovoltaic Geographical Information System (PVGIS)

Geographical Assessment of Solar Resource and Performance of Photovoltaic Technology

Interactive access to solar resource and photovoltaic potential:



Europe

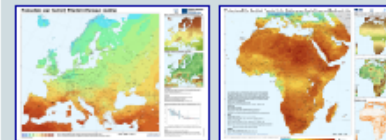


Africa

See also aggregated data of solar and PV potential for [European countries and regions](#).

The **old system** with French, German Italian, Spanish, and Slovak language interface still works.

Posters and maps of solar resource and photovoltaic electricity potential (Europe **NEW**, Africa)



[old version maps for Europe](#)

Topics

About PVGIS

How [database for Europe](#) was created

[Solar radiation data worldwide](#) (update)

[Air temperature](#) in Europe

News

You can now calculate performance for Cadmium Telluride (CdTe) modules [here](#)

Versione italiana finalmente pronta. Provala qui

New version of European country maps



PV potential estimation utility - Microsoft Internet Explorer provided by Imperial College

http://re.jrc.ec.europa.eu/pvgis/apps3/pvest.php#

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PV potential estimation utility

JRC Photovoltaic Geographical Information System - Interactive Maps

EUROPA > EC > JRC > IES > RE > SOLAREC > PVGIS > Interactive maps >

Contact Important legal notice

Europe Africa

e.g., "Ispra, Italy" or "45.256N, 16.9589E"

cursor position: 58.448, 33.926
selected position:

Search

Solar radiation Temperature Other maps

200 650 1100 1550 2000 [kWh/m²]

PV Estimation **Monthly radiation** Daily radiation

Global irradiation data by month

- Horizontal irradiation
- Irradiation at opt. angle
- Irradiation at chosen angle: 90 deg.
- Linke turbidity
- Dif. / global radiation
- Optimal inclination angle

Monthly ambient temperature data

- Average daytime temperature
- Daily average of temperature
- Number of heating degree days

Output options

- Show graphs
- Show horizon
- Web page
- Text file
- PDF

Calculate [help]



Monthly Solar Irradiation

PVGIS Estimates of long-term monthly averages

Location: 40°42'50" North, 3°36'12" West, Elevation: 827 m a.s.l.,

Optimal inclination angle is: 34 degrees

Annual irradiation deficit due to shadowing (horizontal): 0.0 %

Month	H_k	H_{opt}	$H(90)$	I_{opt}	T_{24h}	N_{DD}
Jan	1930	3200	3240	63	5.4	359
Feb	2680	3860	3440	55	6.6	292
Mar	4370	5570	4150	44	9.8	204
Apr	5080	5470	3150	27	11.5	149
May	6420	6240	2820	16	15.5	26
Jun	7170	6650	2580	7	21.3	4
Jul	7330	6950	2790	11	23.6	2
Aug	6400	6700	3420	23	23.3	3
Sep	4940	5960	4030	38	19.0	38
Oct	3340	4640	3920	51	14.4	154
Nov	2100	3310	3220	60	8.5	336
Dec	1560	2570	2640	64	5.7	378
Year	4450	5100	3280	34	13.7	1945

H_k : Irradiation on horizontal plane (Wh/m²)

H_{opt} : Irradiation on optimally inclined plane (Wh/m²)

$H(90)$: Irradiation on plane at angle: 90deg. (Wh/m²)

I_{opt} : Optimal inclination (deg.)

T_{24h} : 24 hour average of temperature (°C)

N_{DD} : Number of heating degree-days (-)

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1.3. PHOTOVOLTAIC ENERGY CONVERSION

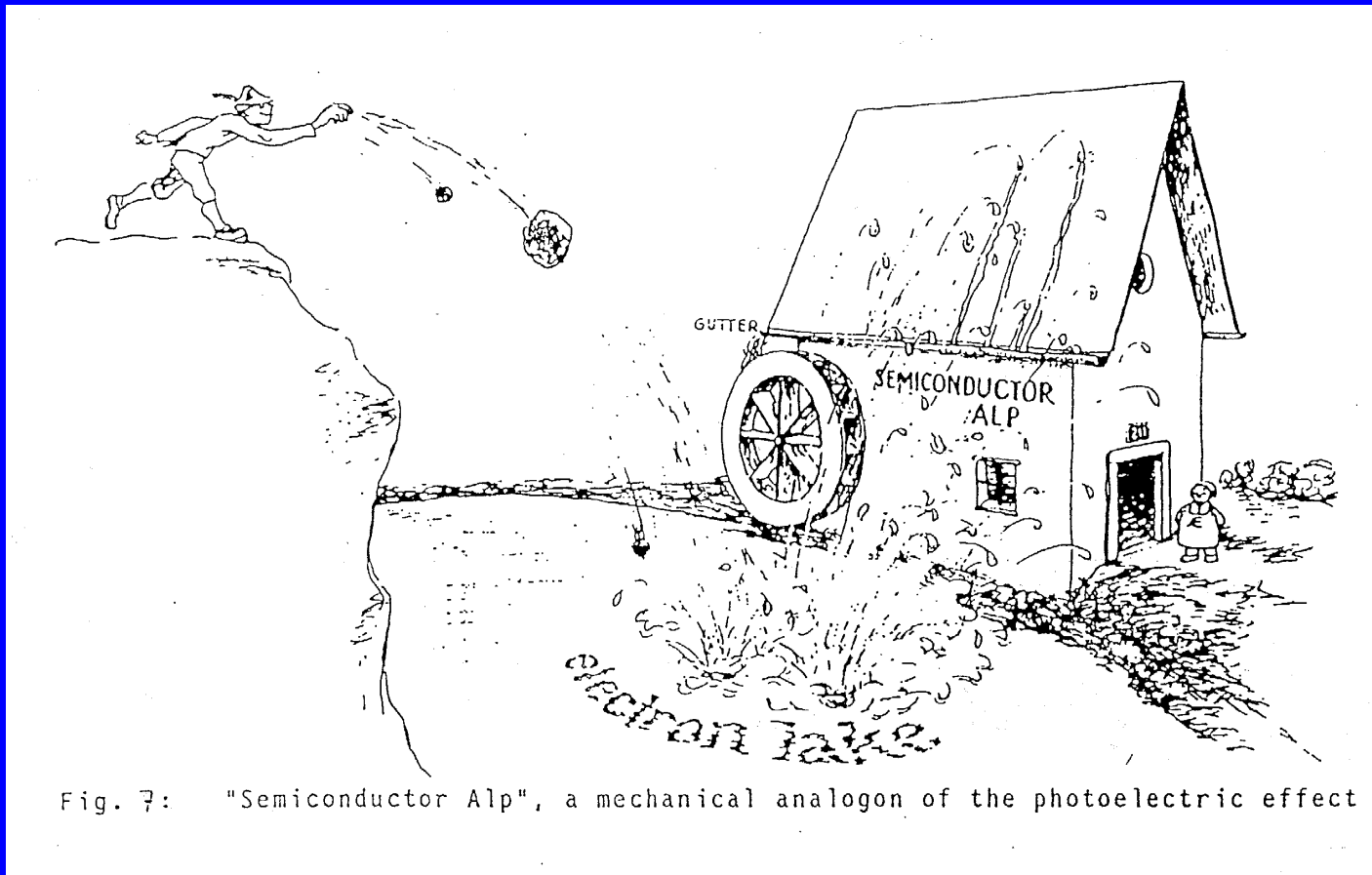
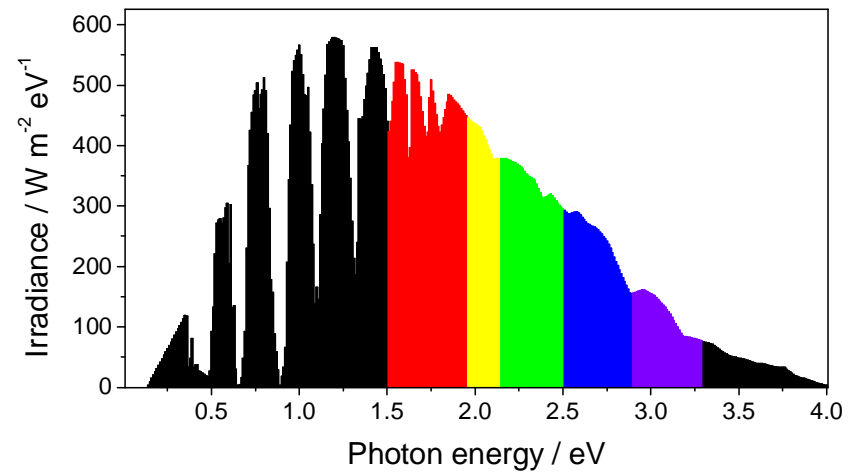
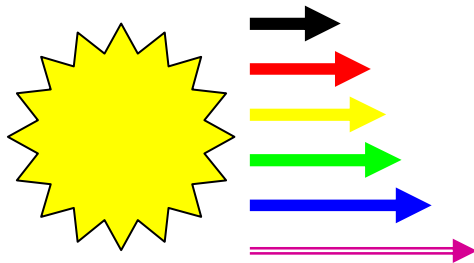


Fig. 7: "Semiconductor Alp", a mechanical analogon of the photoelectric effect

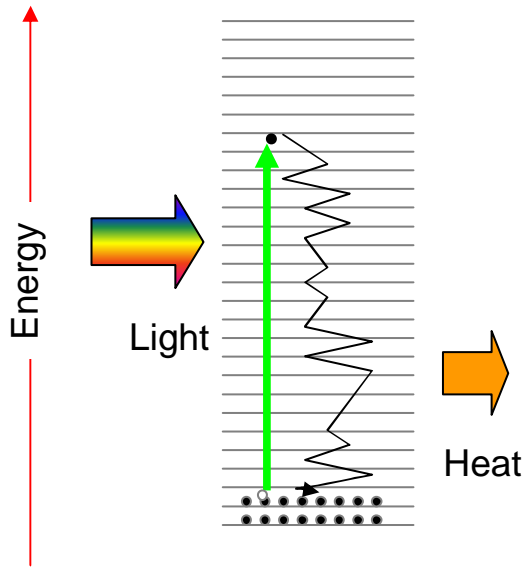
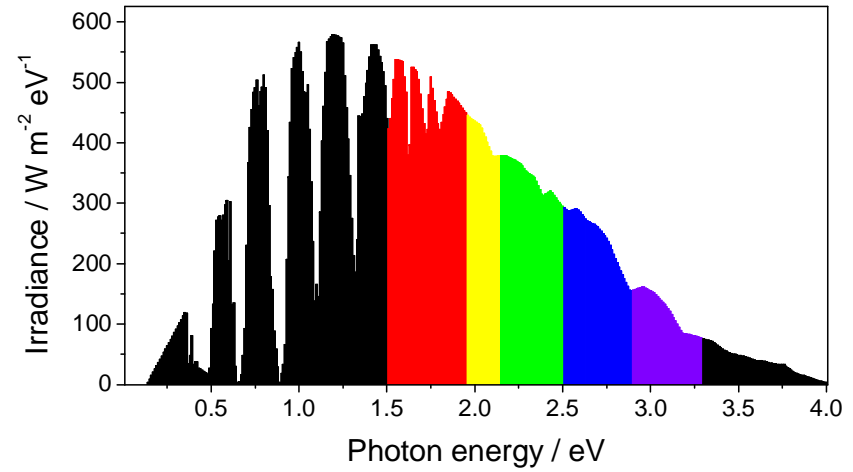
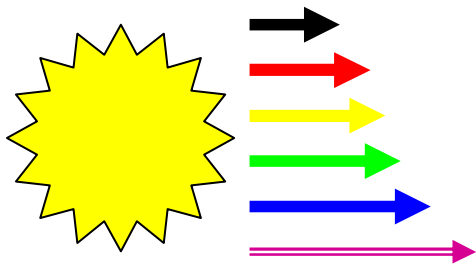
Light energy conversion

- Packets of light energy (photons) defined by the wavelength of light
- May be absorbed in matter to promote electrons to higher energy

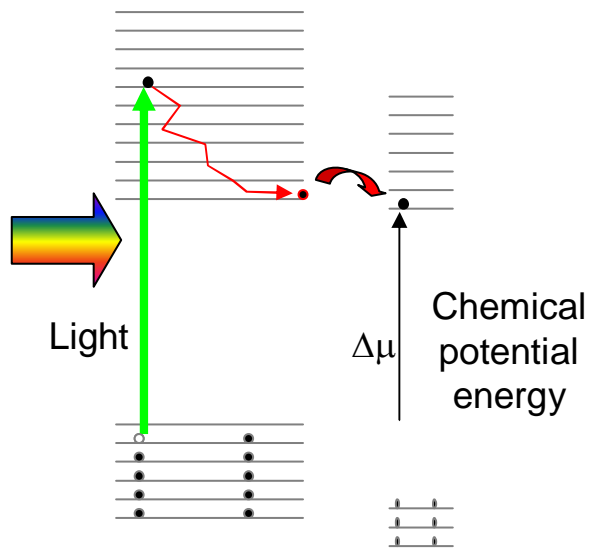


What happens next depends on the system ...

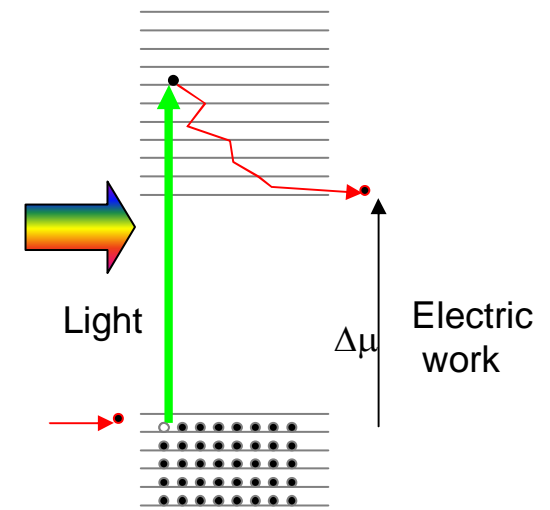




Solar thermal



Solar chemical

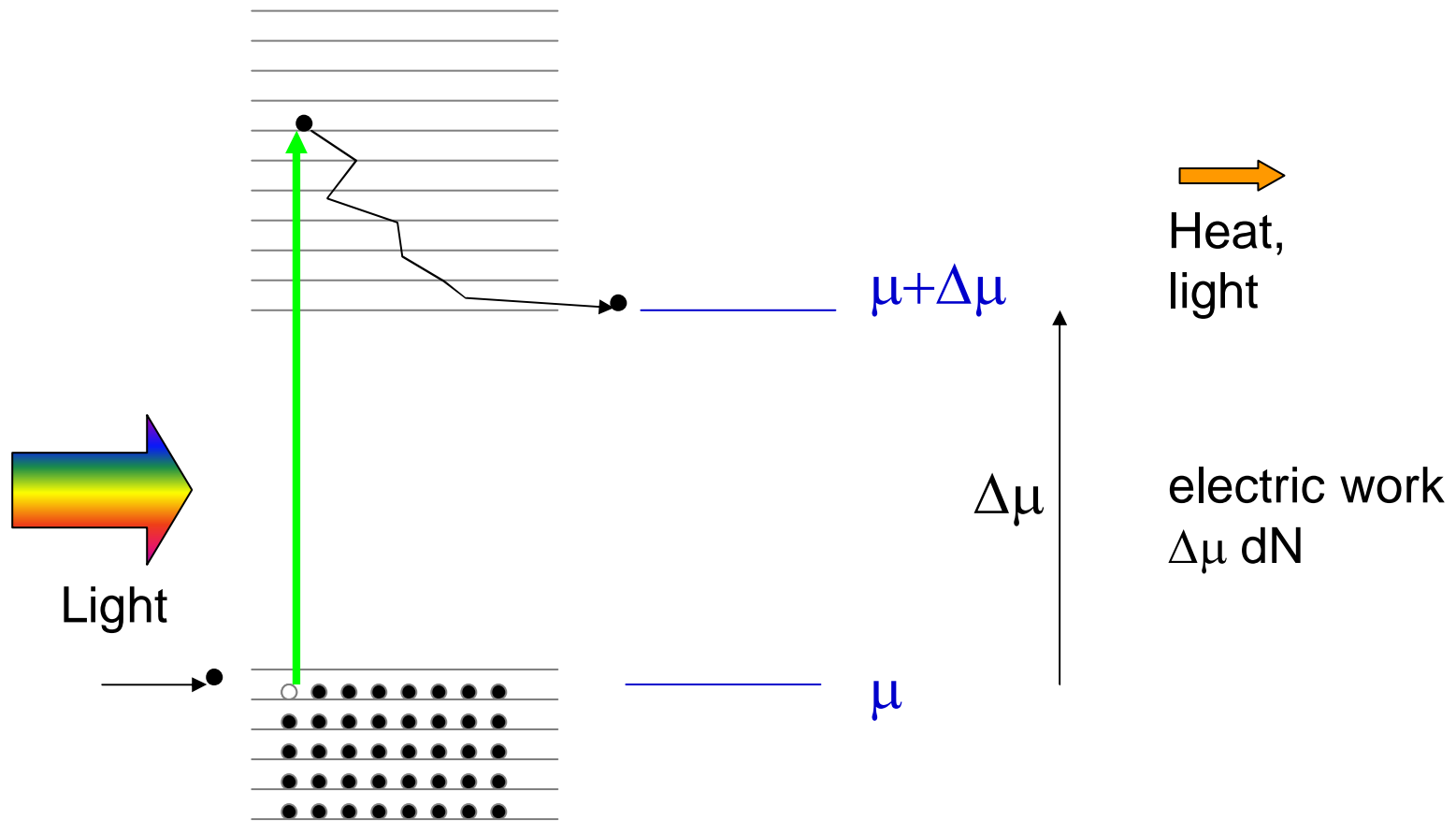


Solar photovoltaic

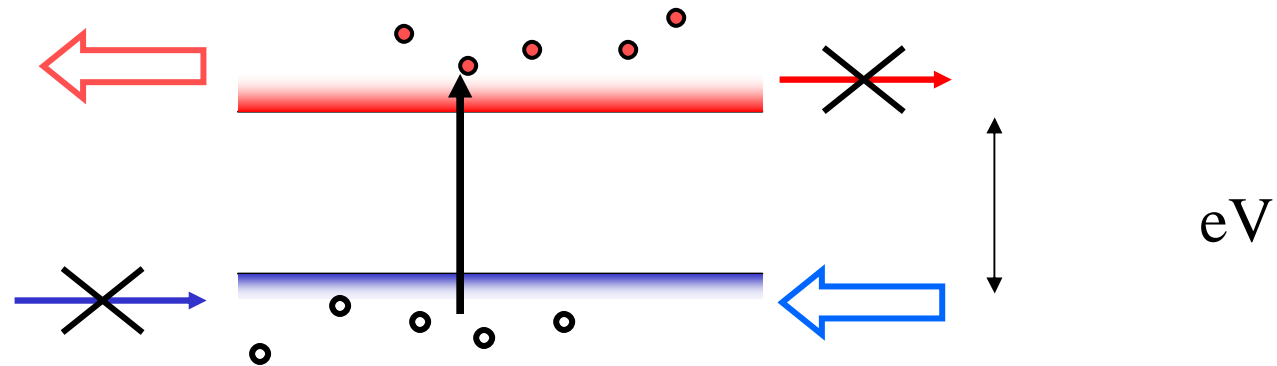


Energy

Semiconductor - open system

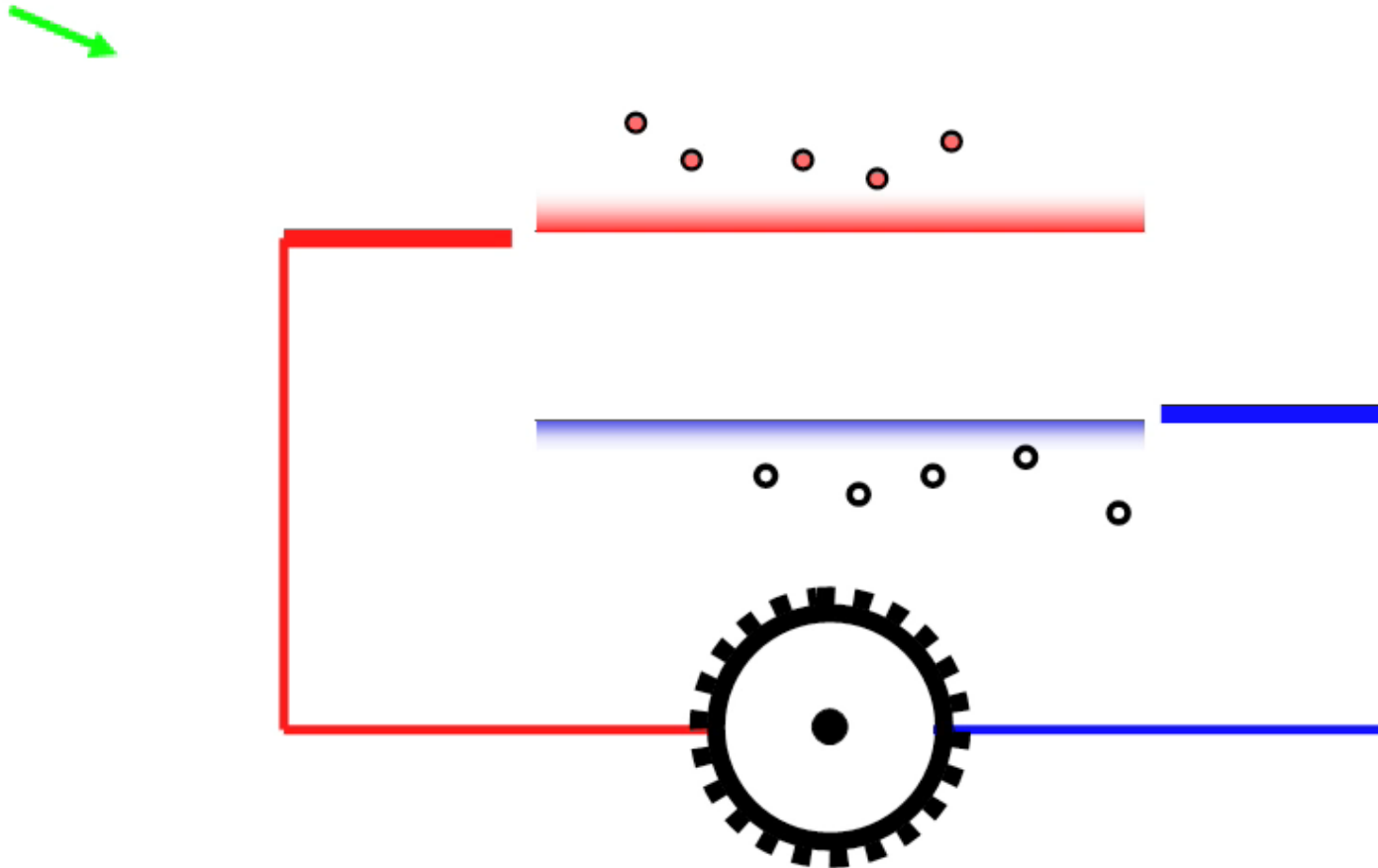


Photons in, electrons out



- Photovoltaic energy conversion requires:
 - photon **absorption** across an energy gap
 - **separation** of photogenerated charges
 - **asymmetric contacts** to an external circuit

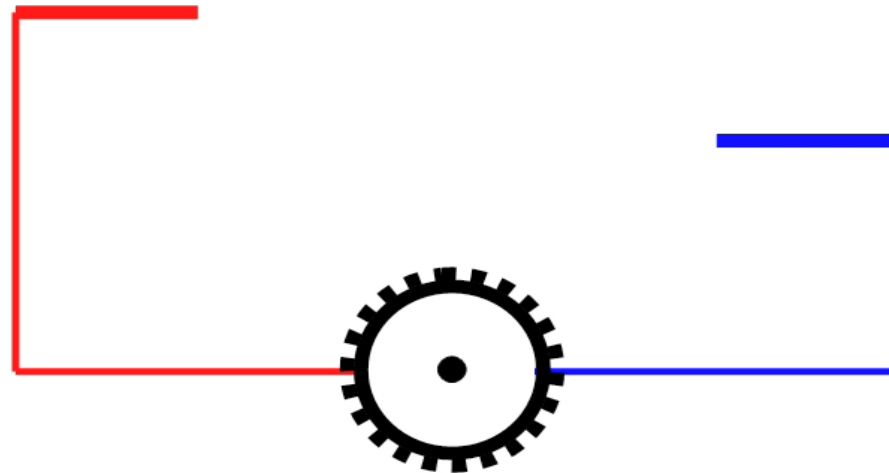
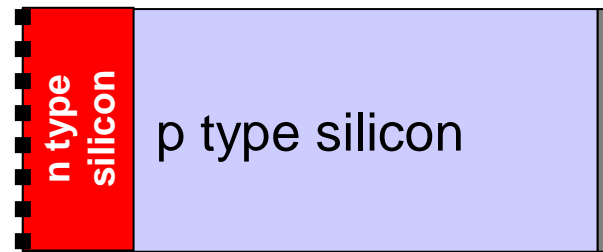
Photons in, electrons out



movie

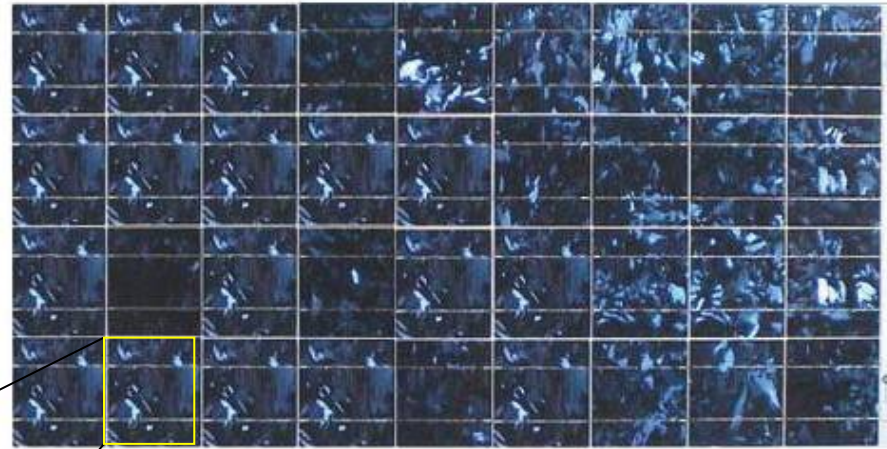
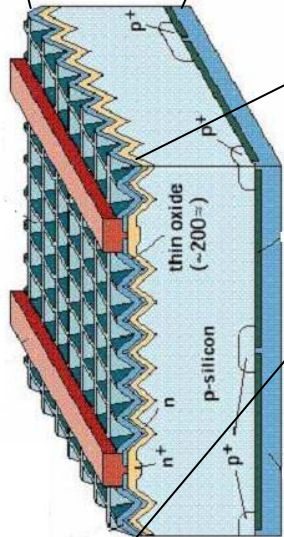
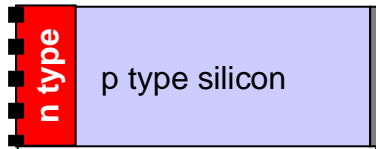


Photons in, electrons out



movie





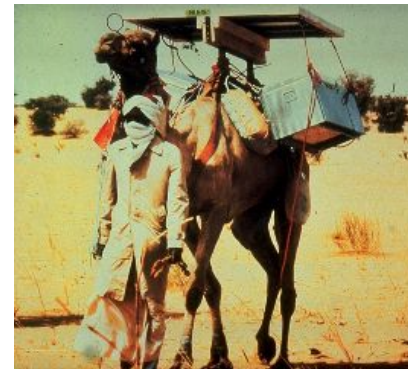
efficiency
~ 14%

power rating
~ 80 W_p



CIS Tower, Manchester
0.4 MW_p
(Solar Century)

Applications



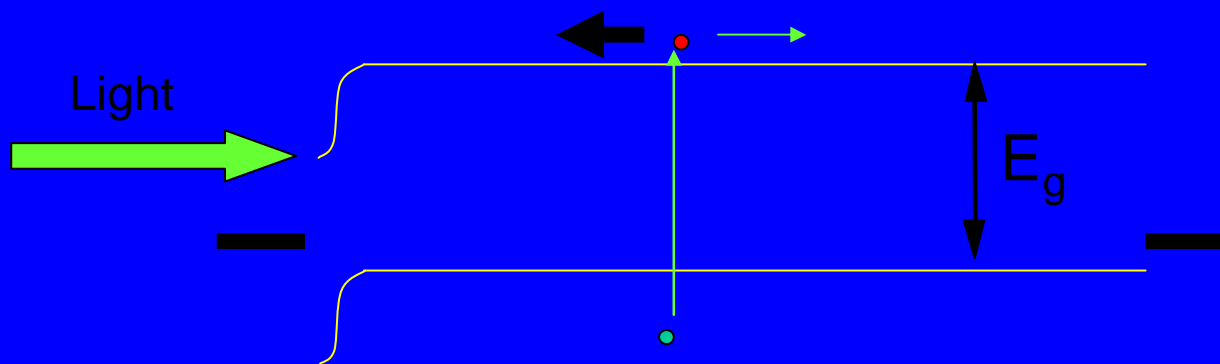
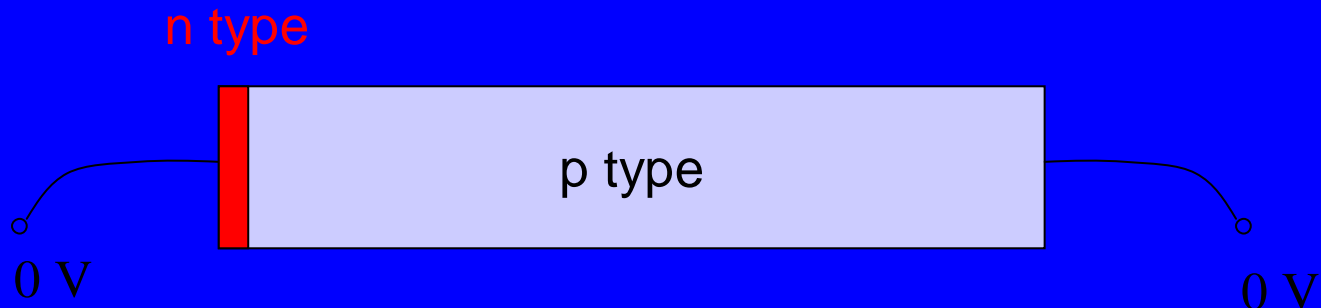
Solar powered refrigeration
~100 W_p



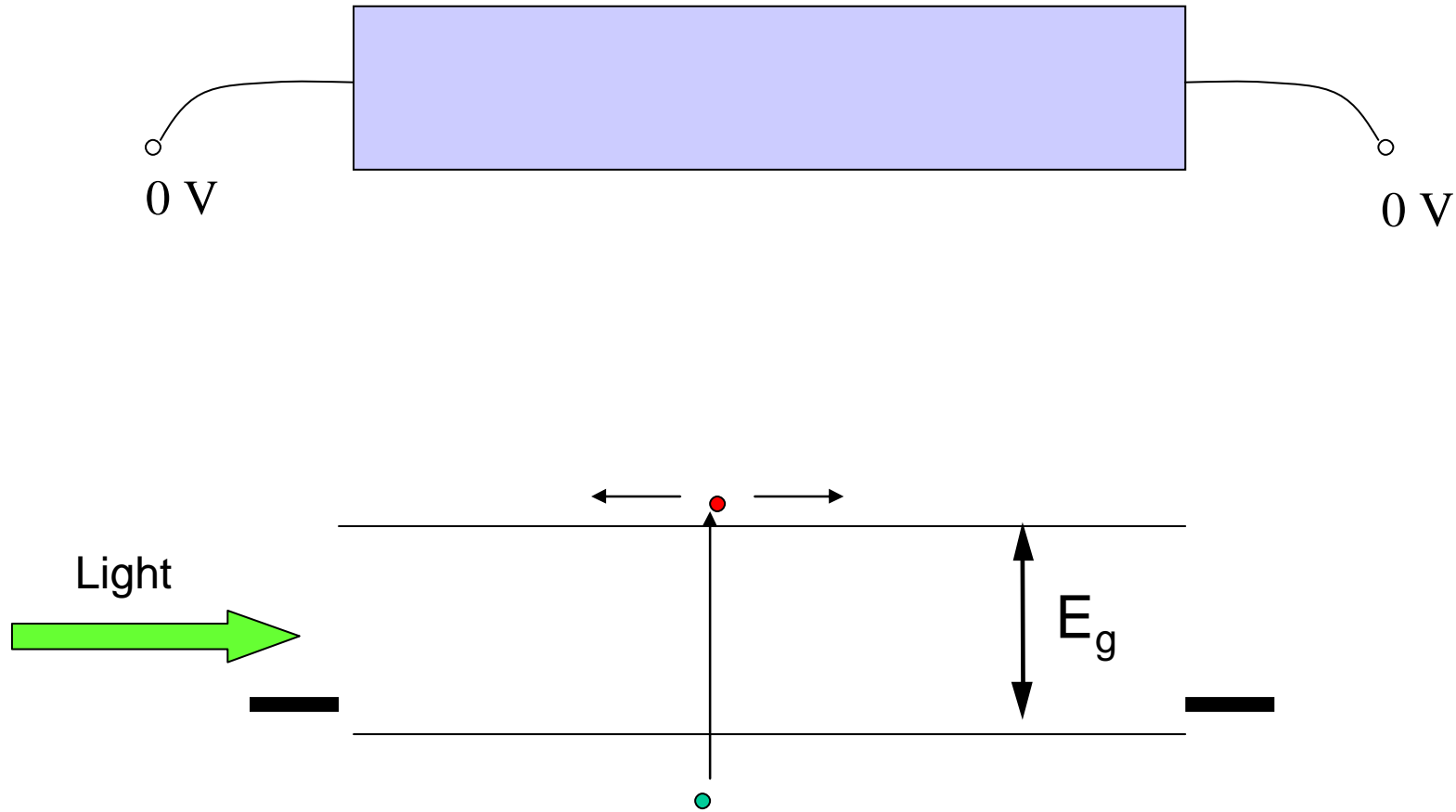
~1 mW_p



1.4. THE P-N JUNCTION

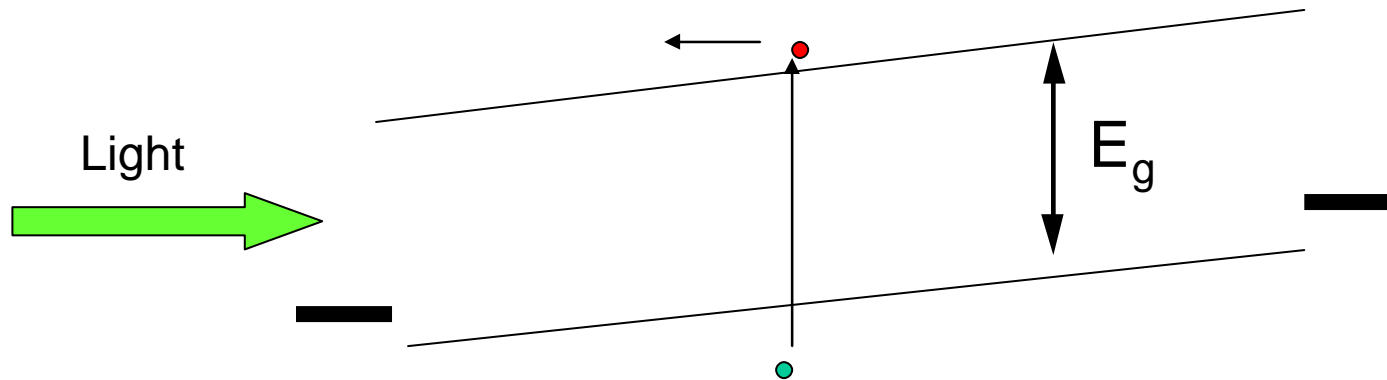
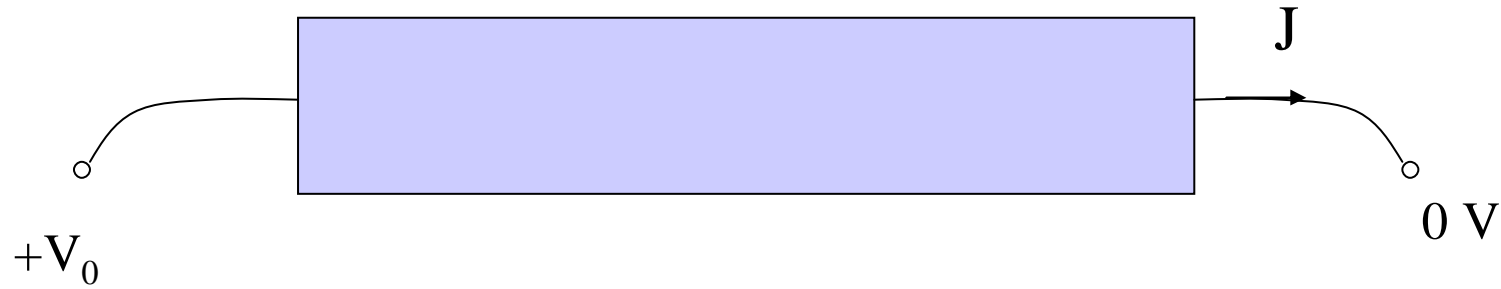


How do the electrons know which way to go??



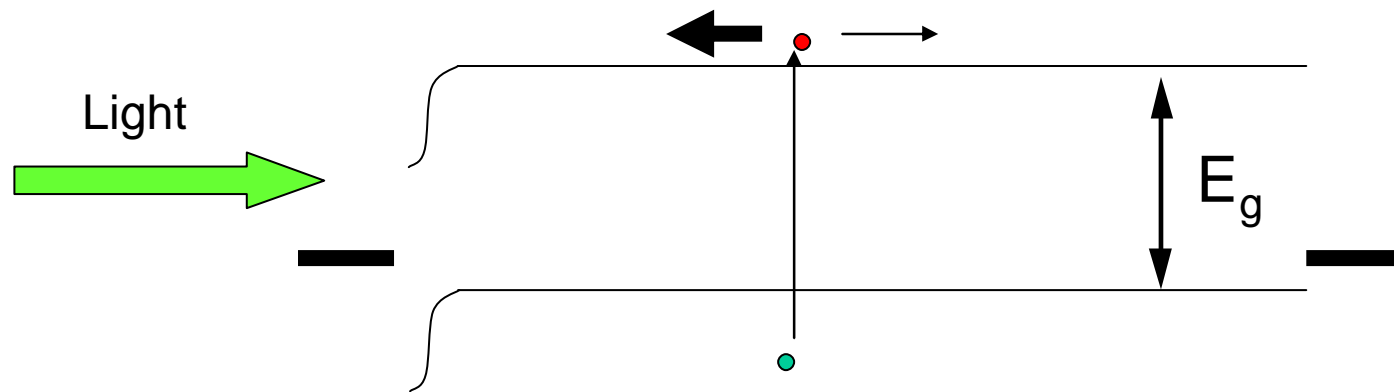
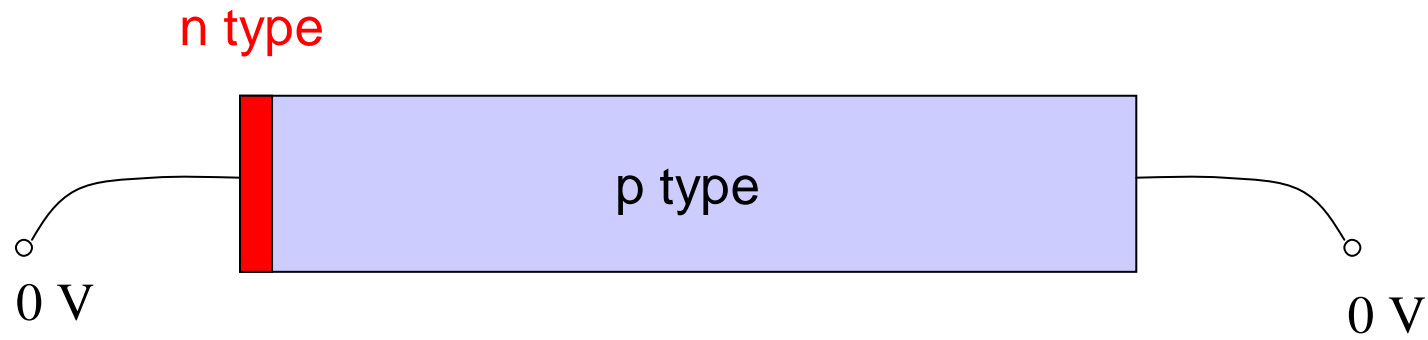
No driving force to direct photocurrent





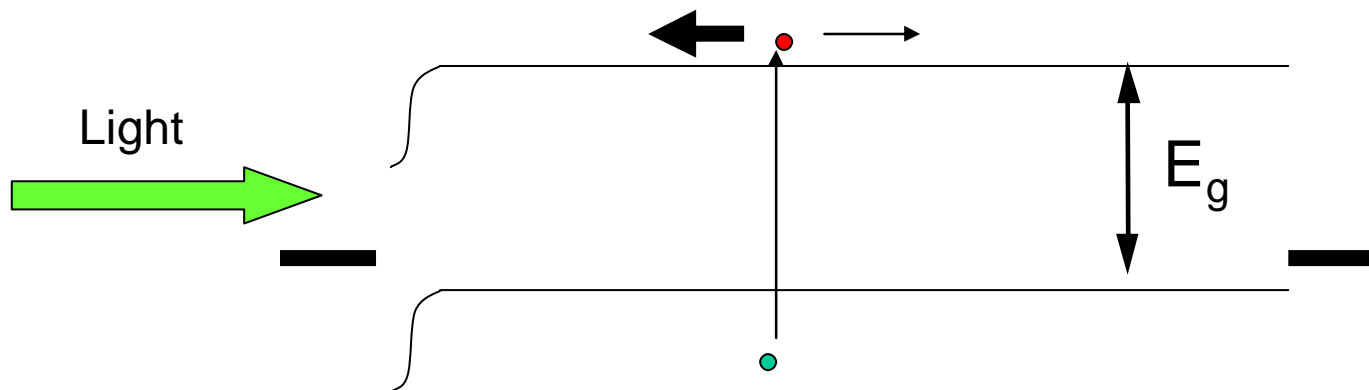
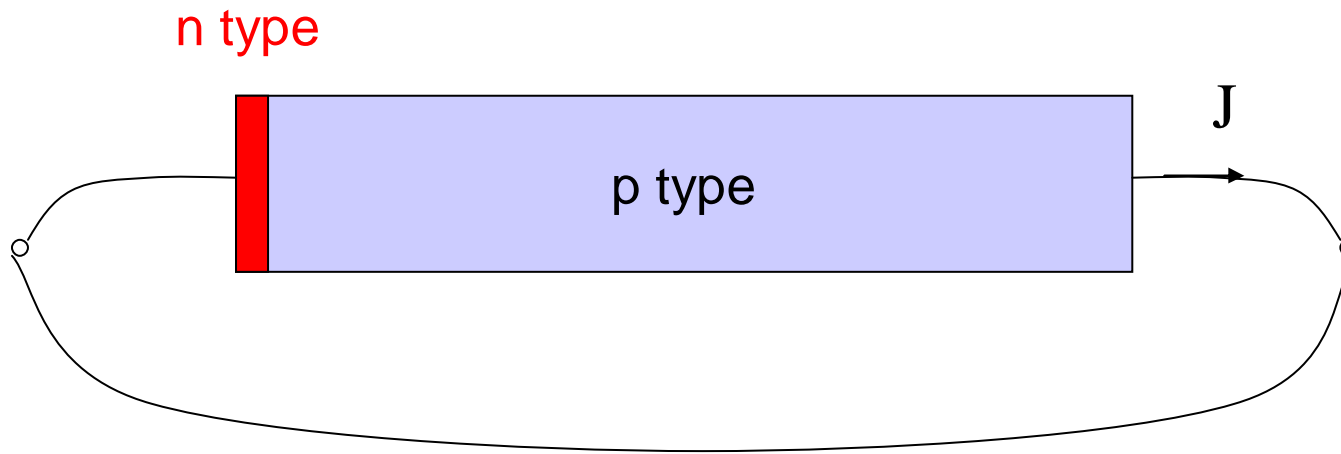
Applied voltage drives photocurrent, but power consumed





Compositional change drives photocurrent





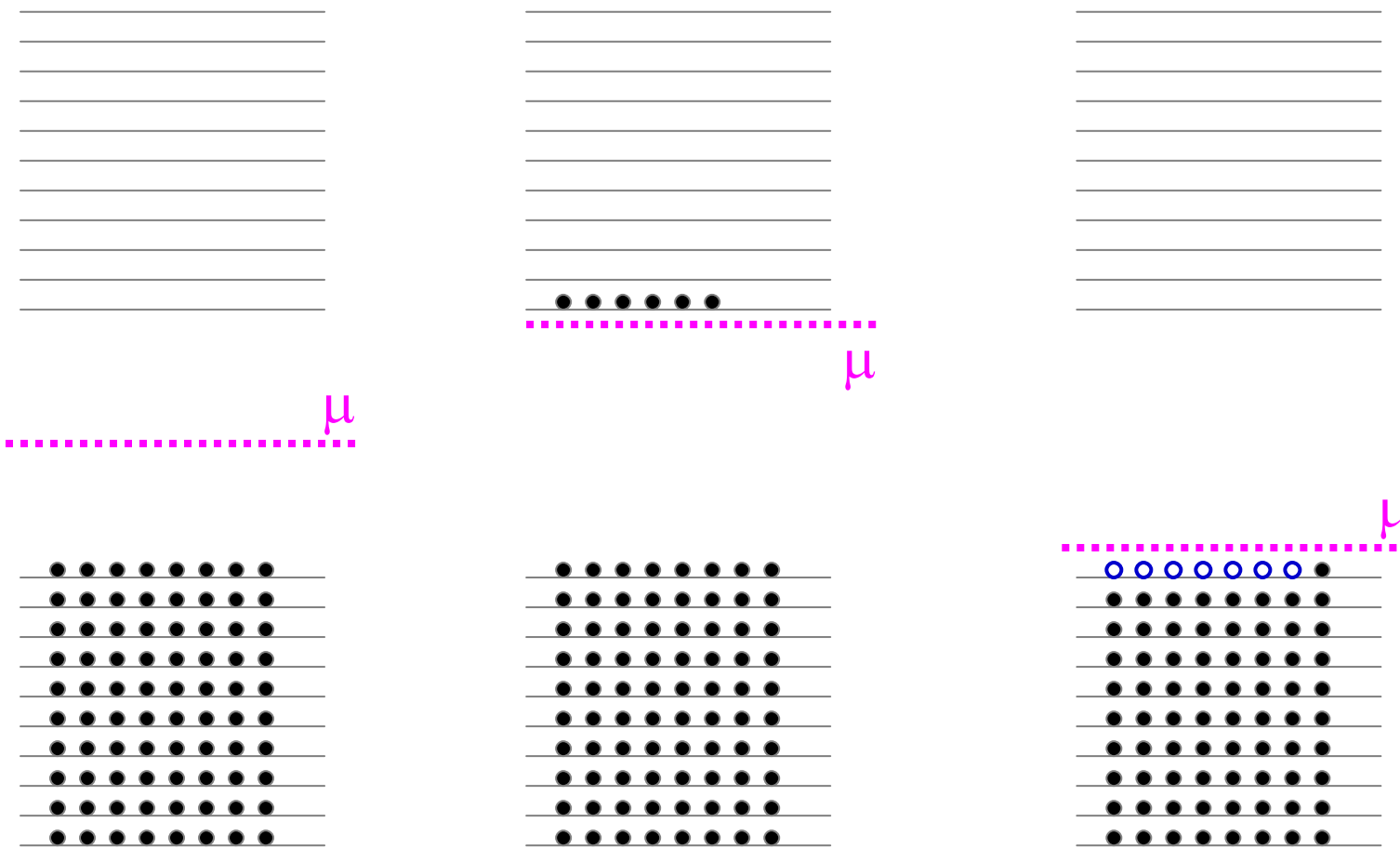
Compositional change drives photocurrent



- To generate electric power from solar radiation we need
 - An **energy gap** (to keep photo-generated electrons at high $\Delta\mu$)
 - A preferred **direction** for electron extraction
- A **semiconductor** provides the energy gap
- Asymmetric contacts (for directed charge extraction) can be provided by a **p-n** or **n-p junction**



Energy



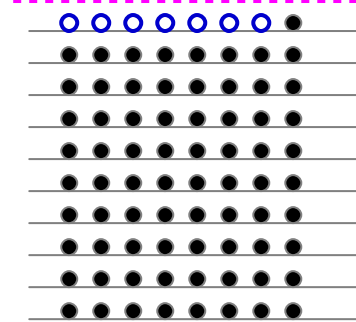
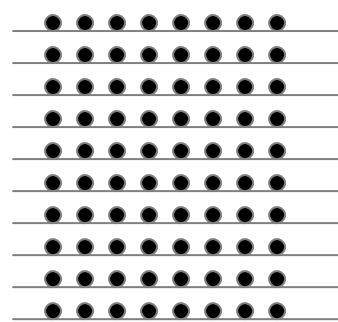
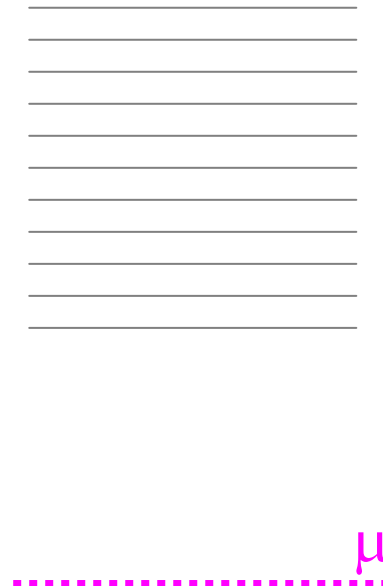
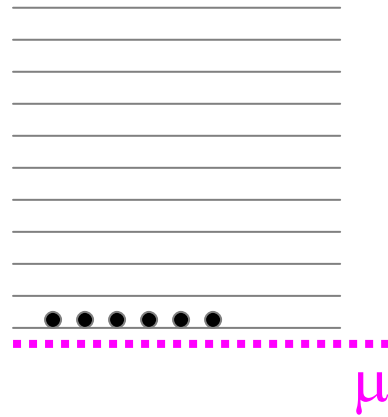
intrinsic

n-type

p-type



Energy

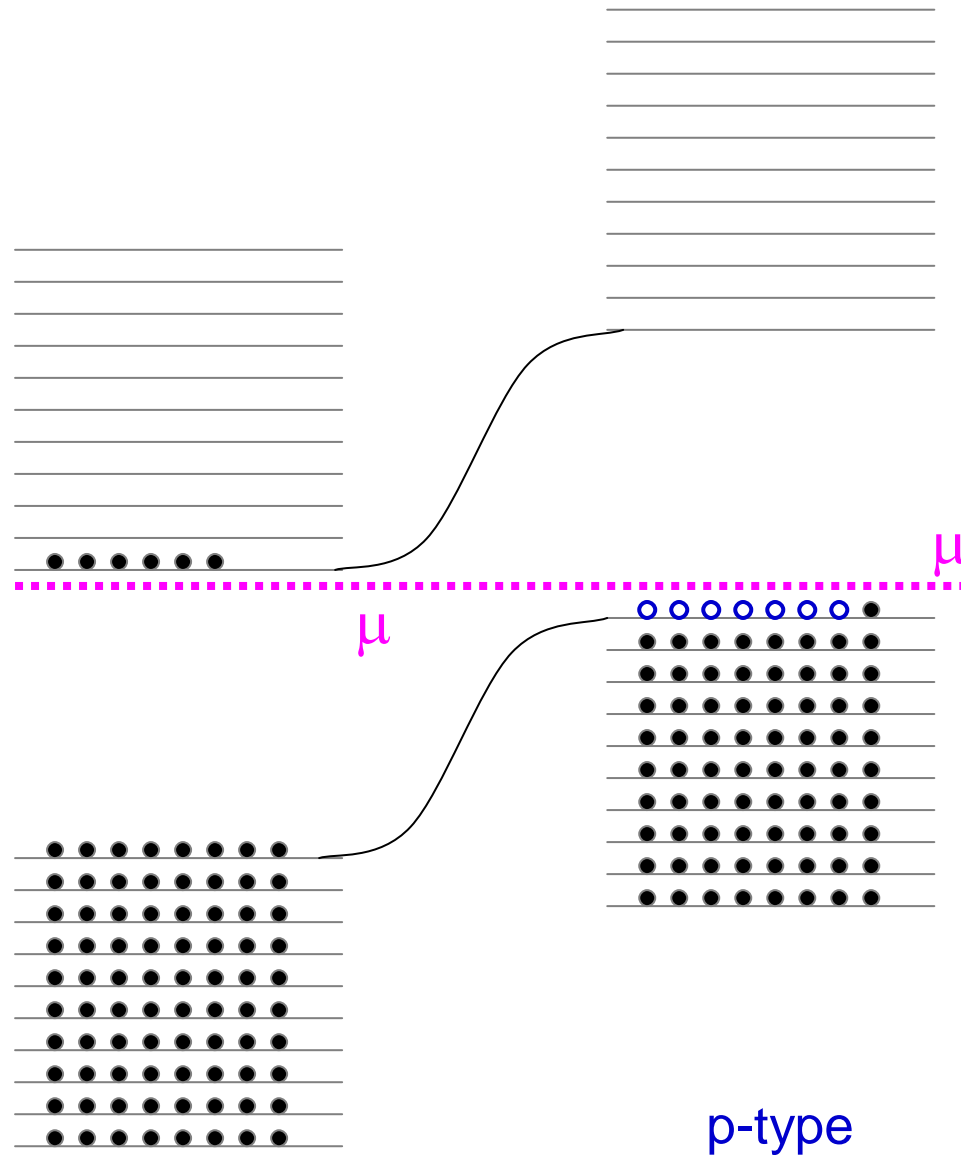


n-type

p-type



Energy



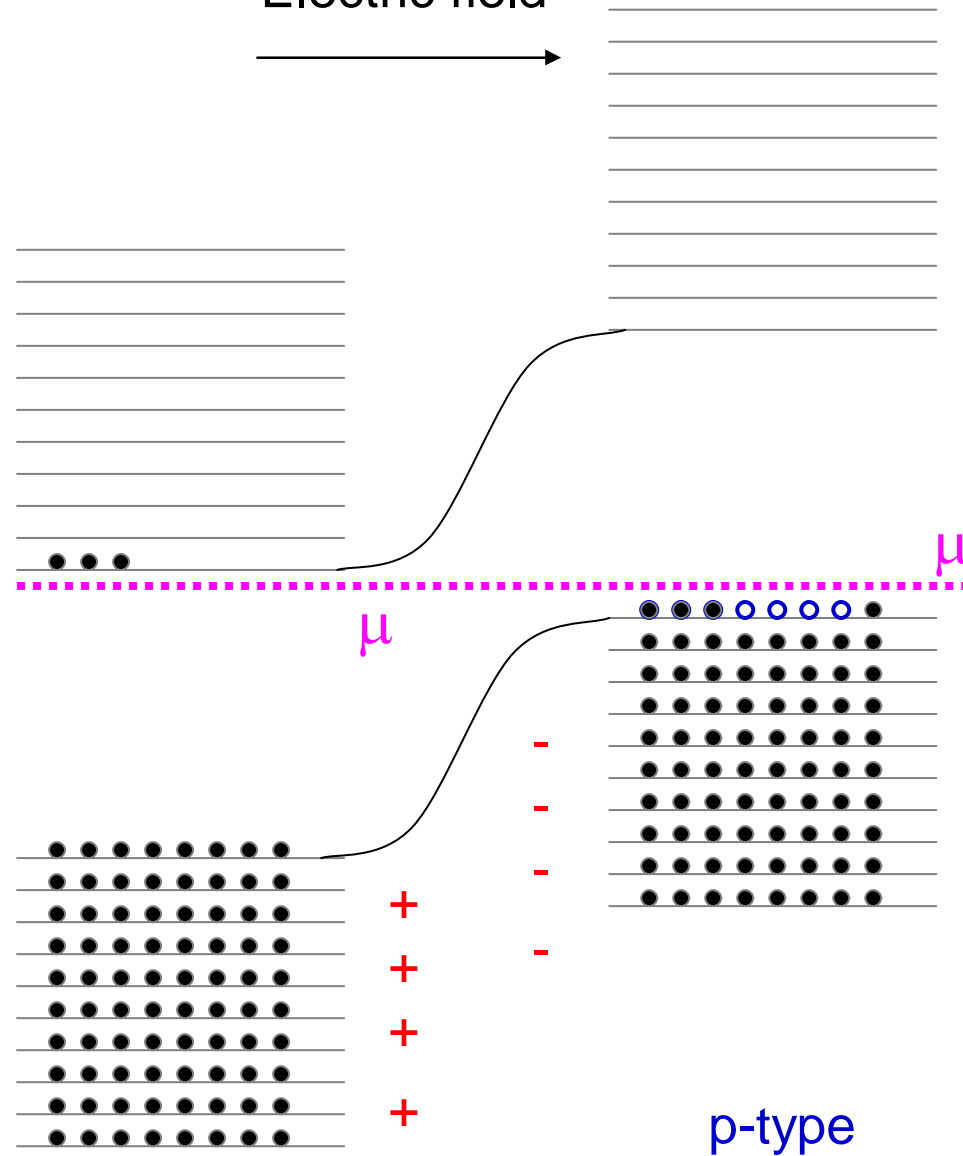
n-type

p-type



Energy

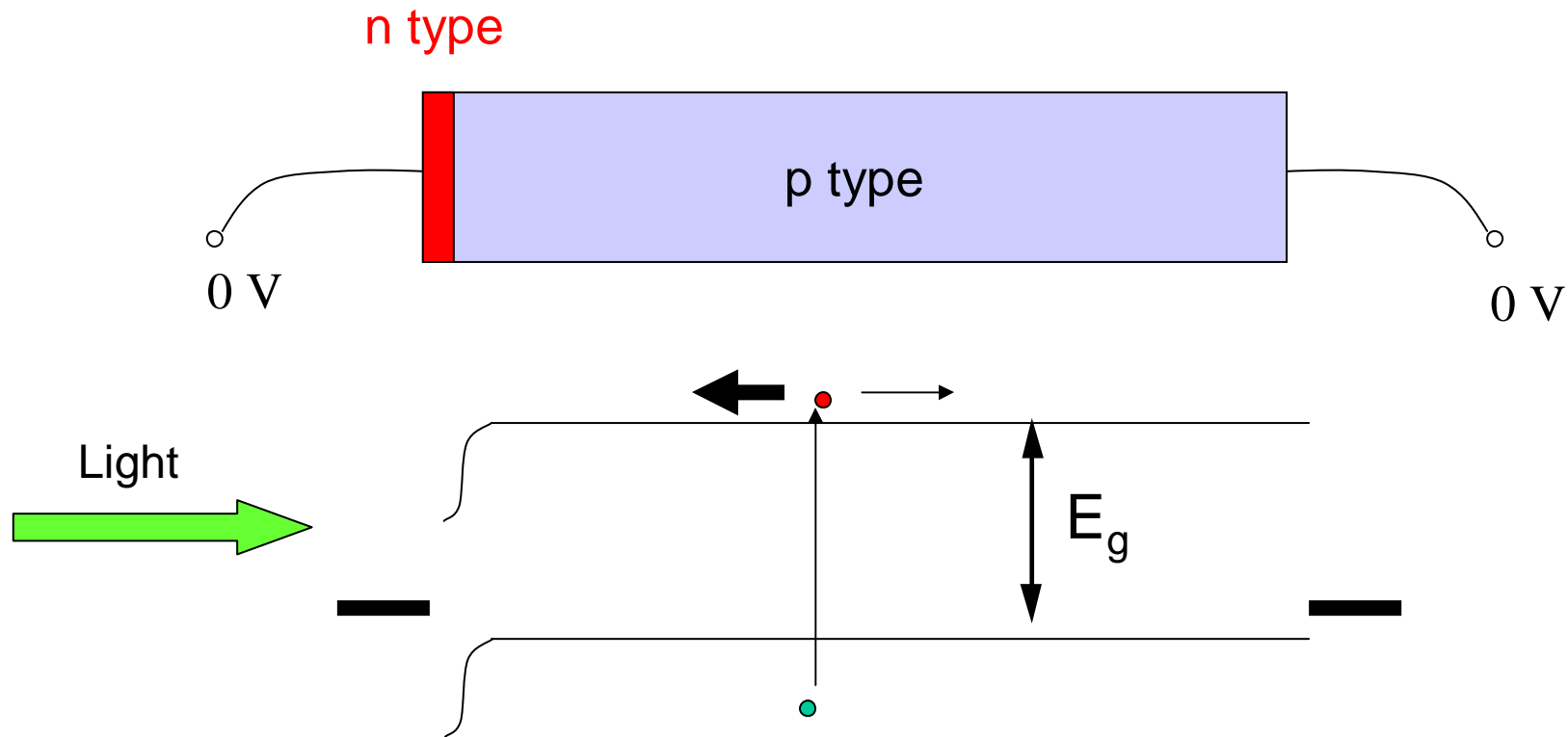
Electric field



n-type

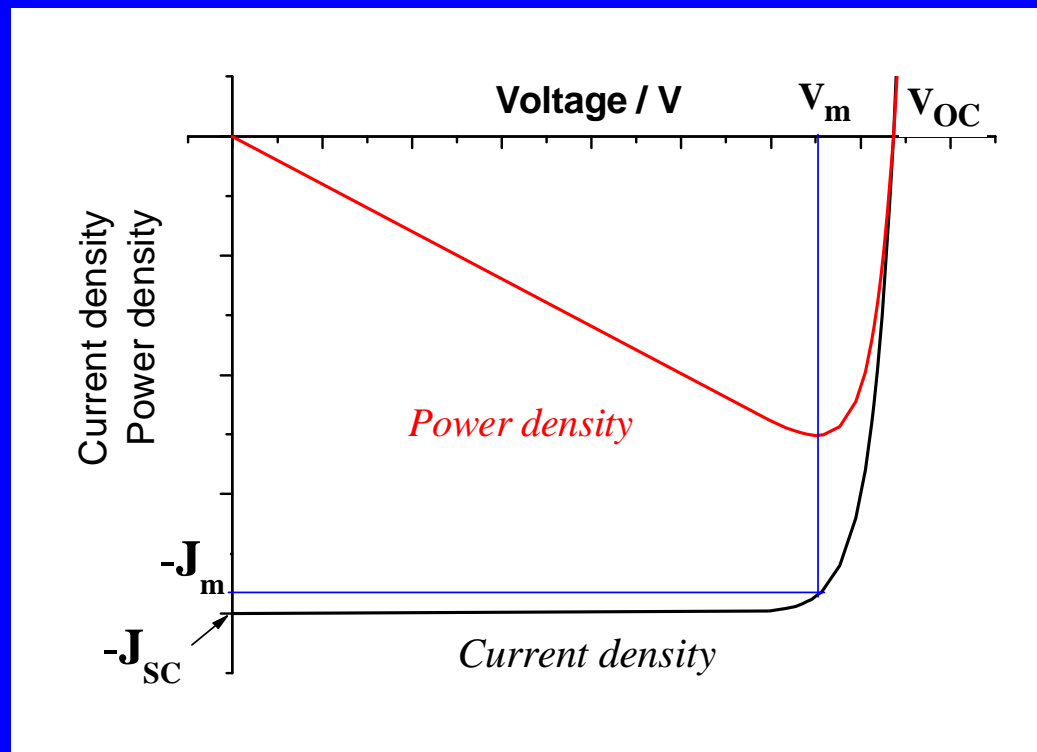
p-type

Semiconductor p-n junction

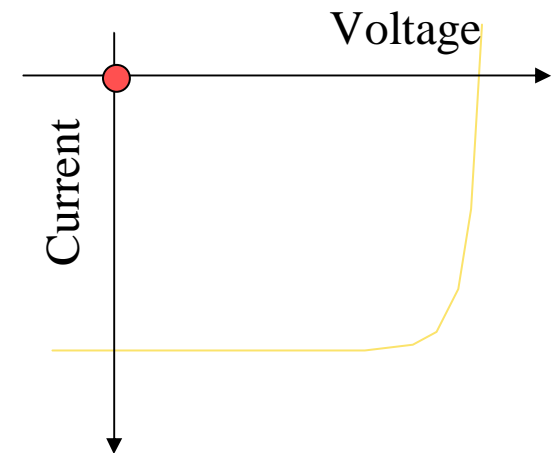
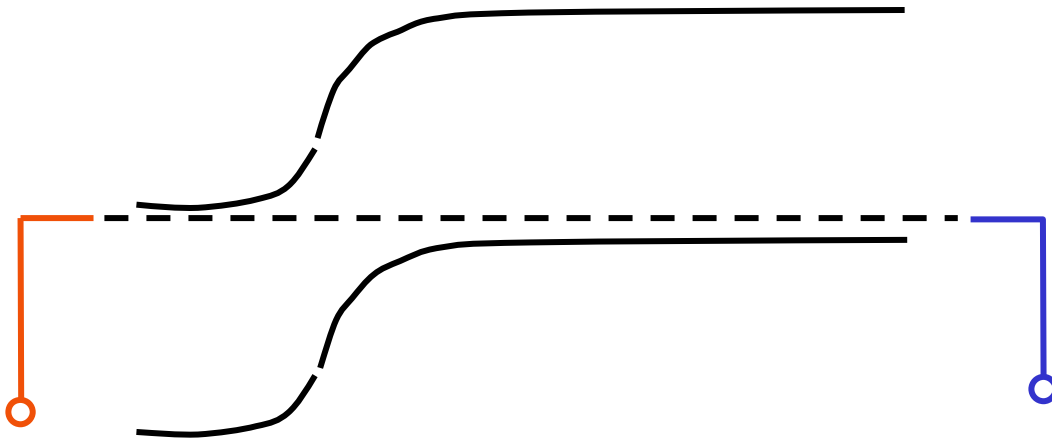


- Band gap enables photogeneration
- Compositional change drives photocurrent

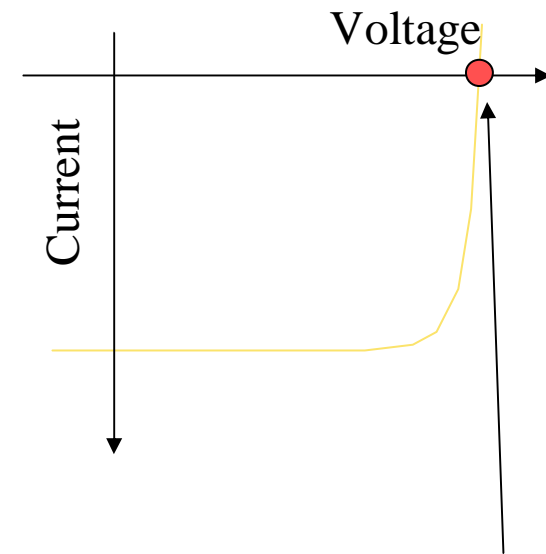
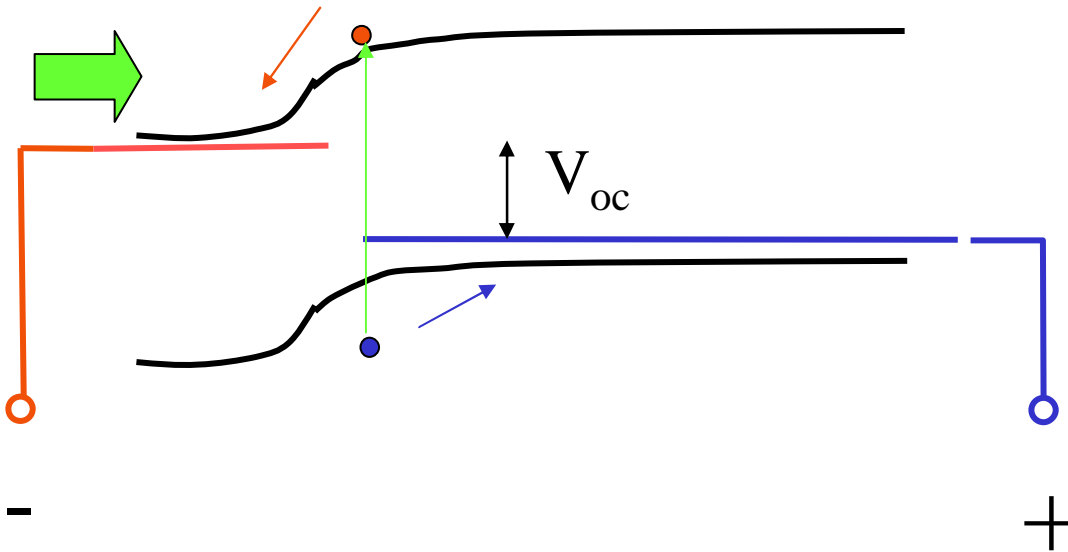
1.5. SOLAR CELL PERFORMANCE CHARACTERISTICS



In the dark

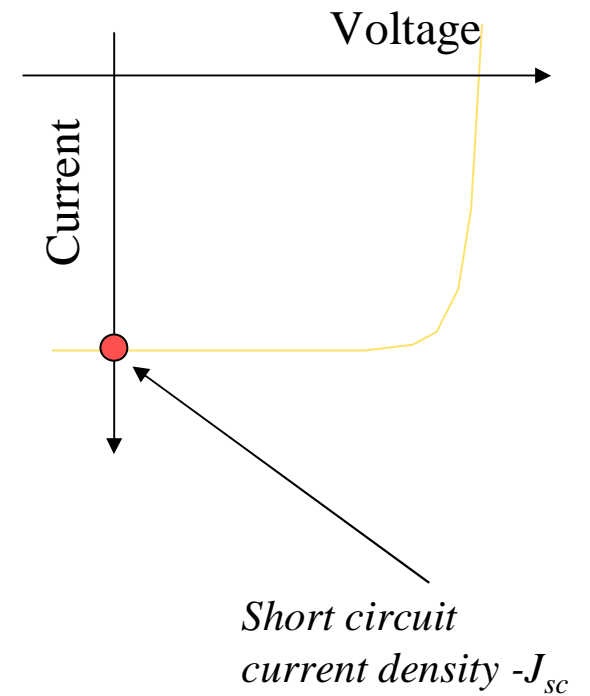
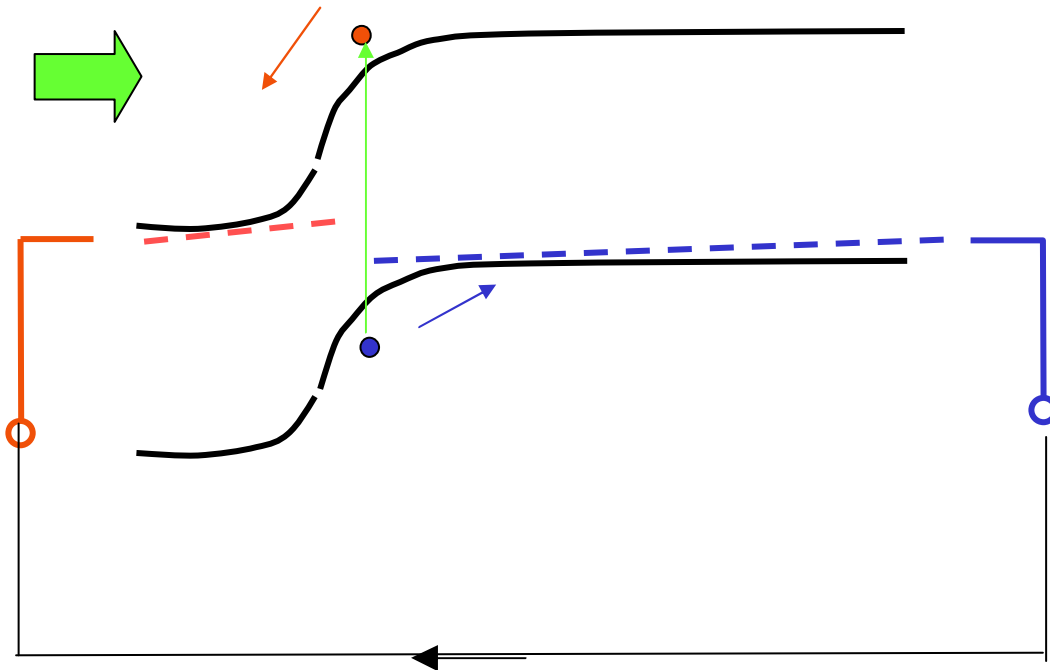


Open circuit

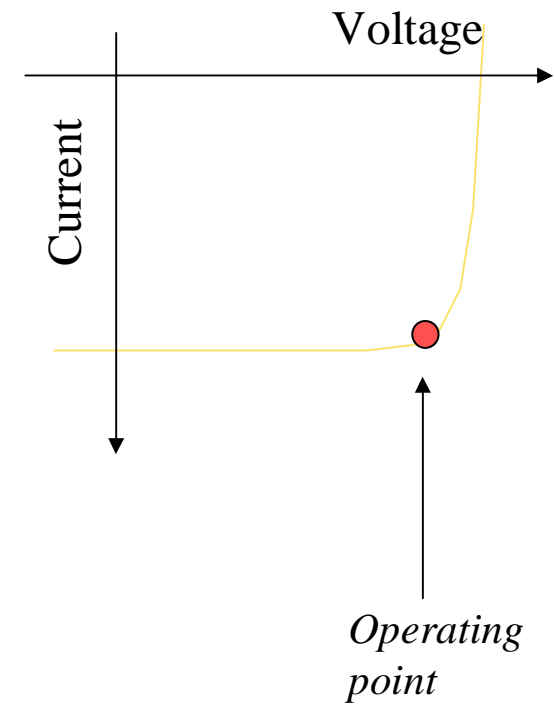
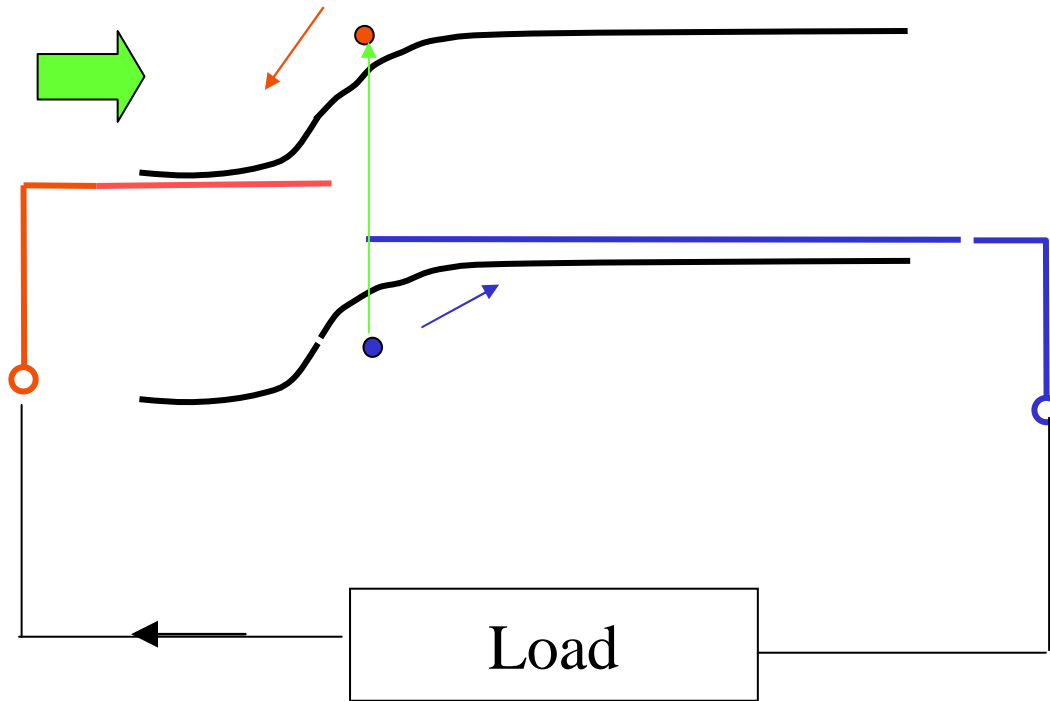


*Open circuit
voltage V_{oc}*

Short circuit



Operating: photovoltage x photocurrent = electric power



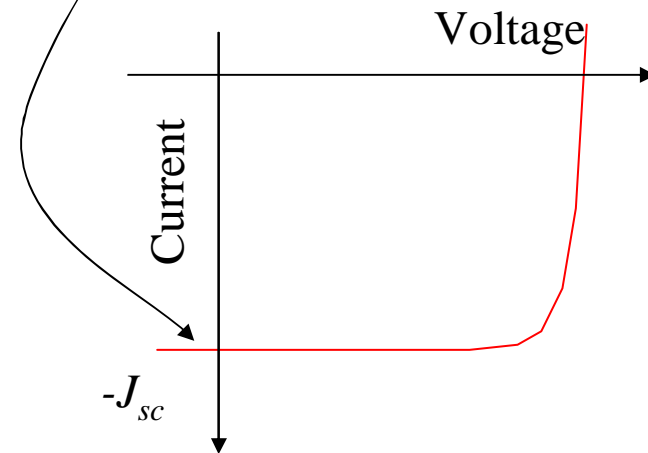
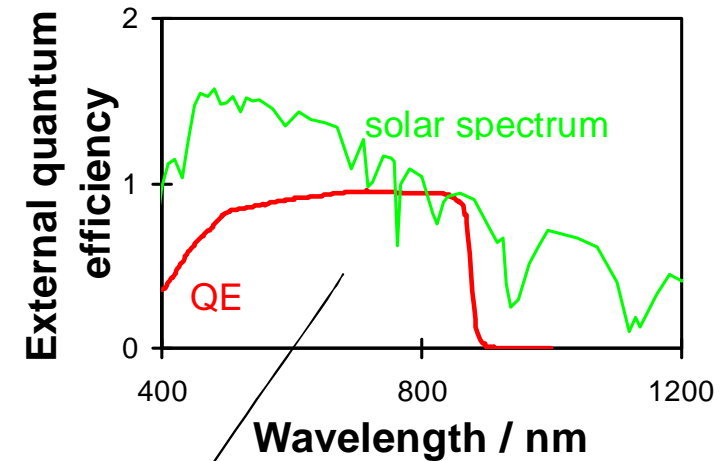
Solar cell characteristics

- Quantum efficiency

$$QE = \frac{\text{electrons out}}{\text{photons in}} = \frac{J_{sc}(E)}{qb_{sun}(E)}$$

- Short circuit current density

$$J_{sc} = q \int \text{photon flux density}(E) \times QE(E) dE$$



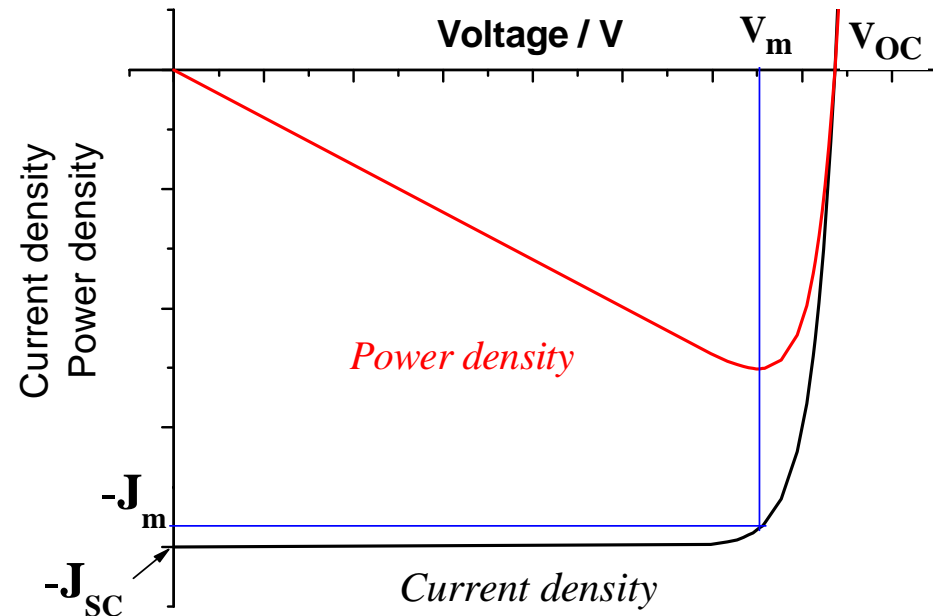
Solar cell characteristics

- Short circuit current density J_{sc} ,
- Open circuit voltage V_{oc}
- Fill factor $FF = \frac{J_m V_m}{J_{sc} V_{oc}}$
- Power conversion efficiency

$$PCE = \frac{J_{sc} V_{oc} FF}{P_{in}}$$

$$P_{in} = \int b_{in}(E) E dE$$

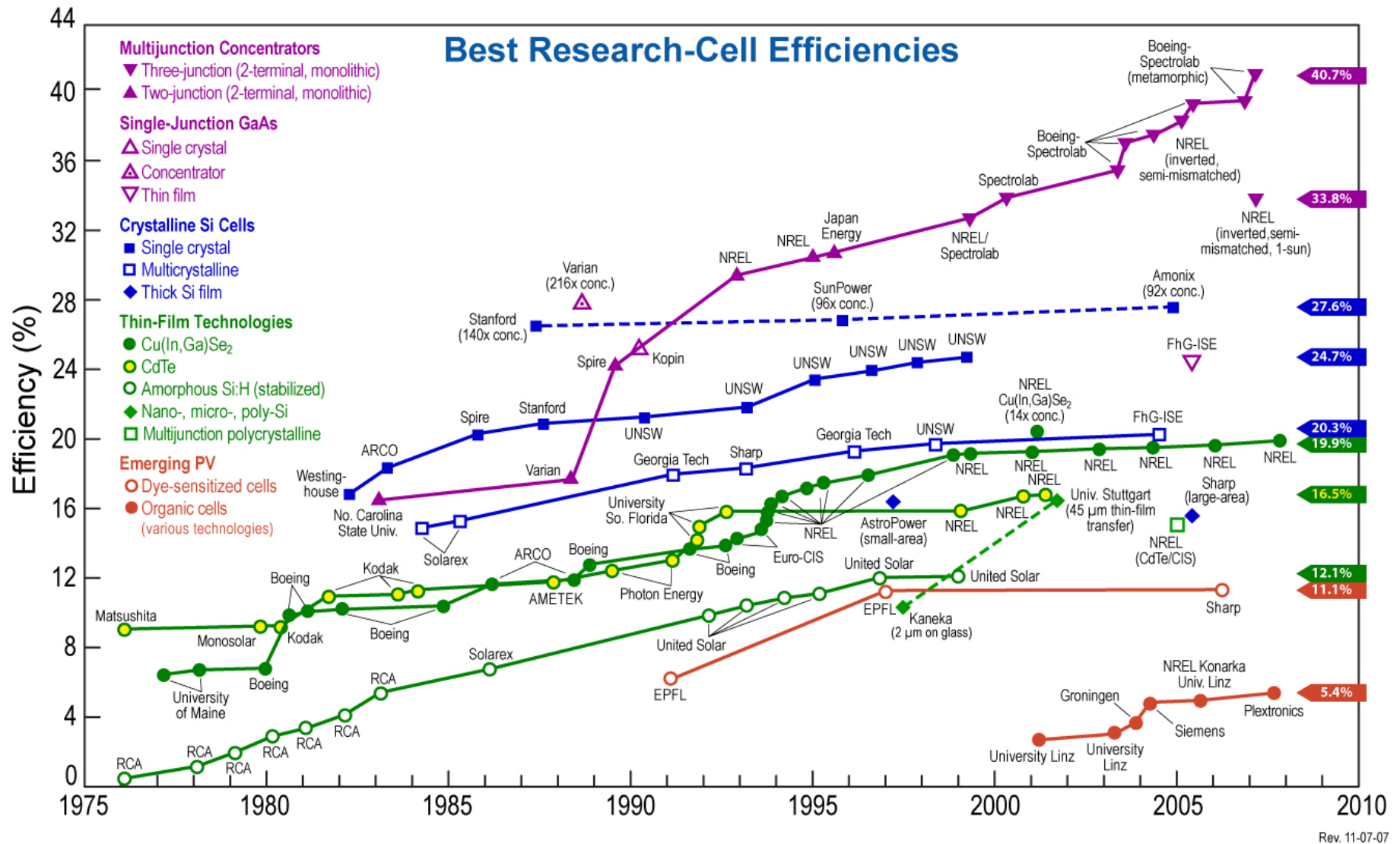
- Measured under Standard Test Conditions (AM1.5, 1000 Wm⁻², 25°C)



Solar cell performance

Cell Type		Area (cm ²)	V _{oc} (V)	J _{sc} (mA /cm ²)	FF (%)	Efficiency (%)
c-Si	UNSW PERL	4.0	0.696	42.0	83.6	24.9
c-GaAs	Kopin	3.91	1.022	28.2	87.1	25.1
poly-Si	UNSW/ Eurosolare	1.0	0.628	36.2	78.5	19.8
a-Si	Sanyo	1.0	0.887	19.4	74.1	12.7
CuInGaSe ₂	NREL	1.04	0.669	35.7	77.0	18.4
Cd Te	NREL	1.131	0.848	25.9	74.5	16.4
polymer / fullerene	various	0.1	~0.6-0.8	~12-15	~60	5 - 6





More on this in next Monday's lectures



Summary

- Installed photovoltaic capacity reached 13 GWp in 2008, mainly in grid connected applications
- Overhead sun provides $\sim 1 \text{ kW m}^{-2}$ of radiant power at the Earth's surface, annually averaged irradiance $\sim 100 - 200 \text{ W m}^{-2}$ depending on latitude
- In photovoltaic energy conversion,
 - absorbed photons promote electrons to higher energy levels within a semiconductor
 - opposite charges are driven towards opposite contact by electrode selectivity
 - charges are extracted (\Rightarrow current) with some electrochemical potential energy (\Rightarrow voltage)
- Power conversion efficiency is about 25% for the best single junction solar cells.



Energy consumption per capita in Western Europe ~ 5 kW
Mean solar irradiance in Southern Britain ~ 125 W m⁻²
What land area is needed to supply the energy needs of a city
of 10 million people using solar irradiation:

(a) with conversion efficiency of 50%?

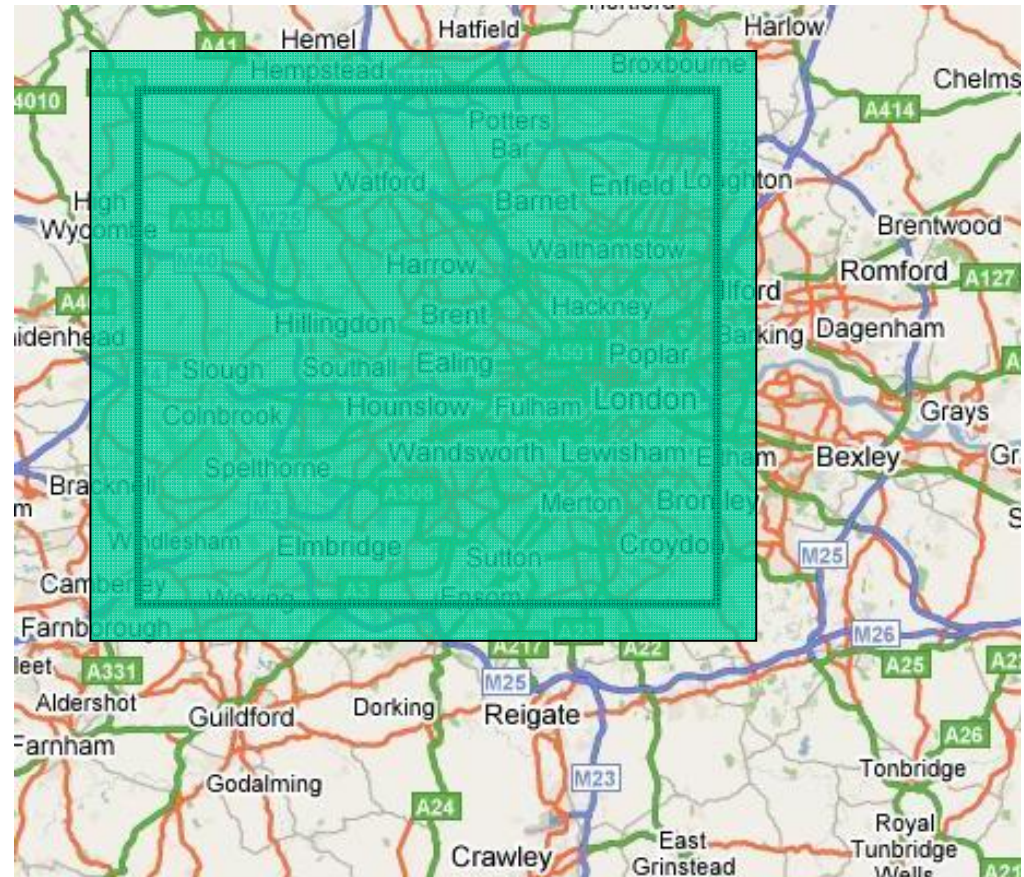
$$10^7 \times 5000 / (125 \times 0.5) \text{ m}^2 \\ = 8 \times 10^8 = 800 \text{ km}^2$$



Energy consumption per capita in Western Europe ~ 5 kW
Mean solar irradiance in Southern Britain ~ 125 W m⁻²
What land area is needed to supply the energy needs of a city
of 10 million people using solar irradiation:

(b) with conversion efficiency of 5%?

$$10^7 \times 5000 / (125 \times 0.05) \text{ m}^2 \\ = 8 \times 10^8 = 8000 \text{ km}^2$$



Device physics of solar cells

- Physics governed by charge continuity

$$\frac{1}{e} \frac{dJ}{dx} + G - R = 0$$

- Generation G = light absorption rate

$$G = \alpha b_{sun} e^{-\alpha x}$$

- Recombination R usually linear

$$R = Bnp \approx \frac{n}{\tau}$$

- Current density J Dominated by minority carrier diffusion.

$$J = qD \frac{dn}{dx} + qn\mu\varepsilon$$

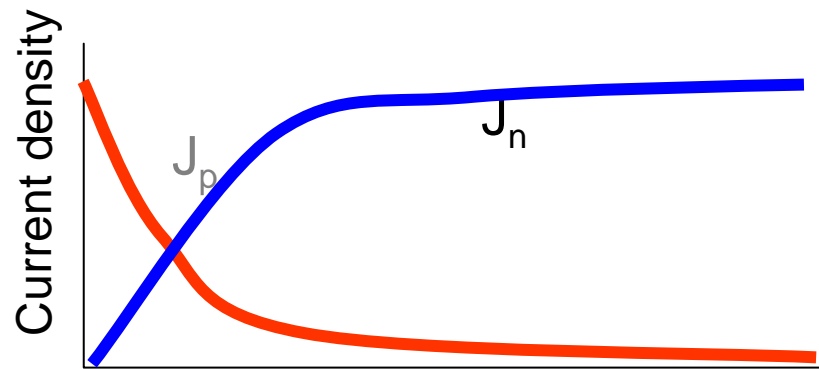
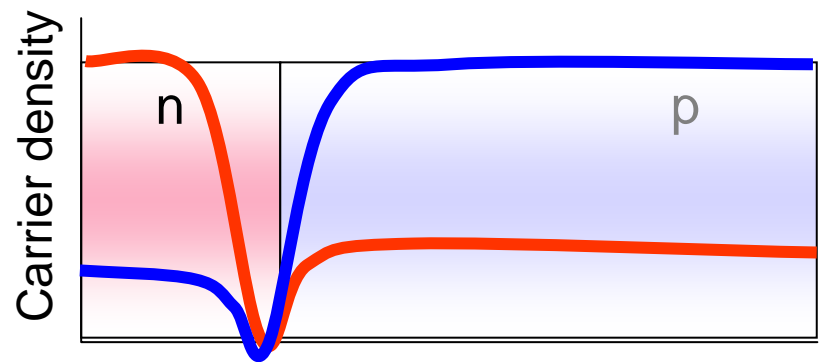
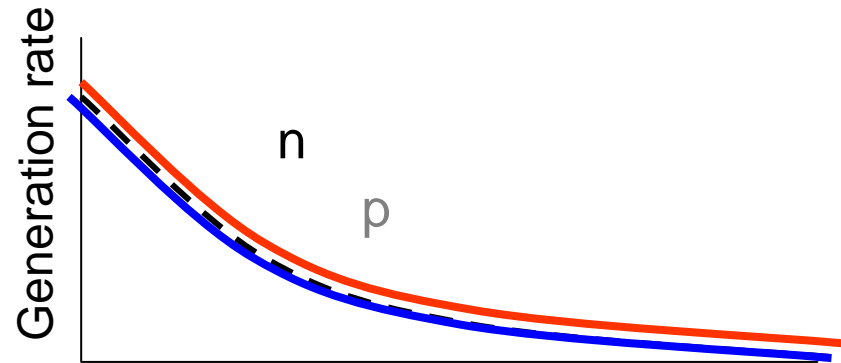
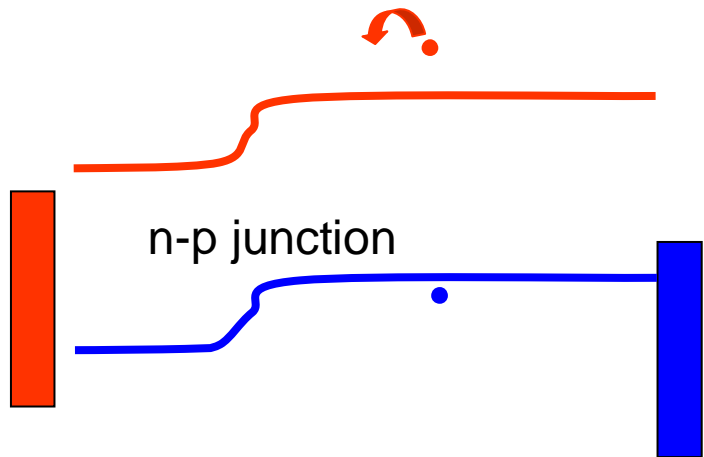
- Differential equation for carrier density

$$D_n \frac{d^2 n}{dx^2} - \frac{n}{t_n} = -G$$

- Boundary conditions

$$n(0) = n_0 e^{V/kT} \quad J_n(d) = 0$$





Device physics of solar cells

- Result: diode equation for J-V

$$J = -J_{sc} + J_0 \left(e^{qV/mkT} - 1 \right)$$

- Important parameters:

- absorption coefficient α , optical depth αd , reflectivity
- charge diffusion length $L = (D\tau)^{1/2}$
- type of recombination (e.g. linear, bimolecular, via defect states)
- parasitic resistances: series R and shunt R (leakage)



Solar cell design

- good optical absorption:
 - Increase thickness
 - Anti-reflection coating, texturing
 - Fine contacts
- efficient charge separation:
 - Increase junction built-in bias, junction area
 - Suppress recombination
- efficient transport
 - Improve material quality
- low electrical losses
 - reduce series resistance

24.4% efficient PERL cell

