



**The Abdus Salam  
International Centre for Theoretical Physics**



**2139-11**

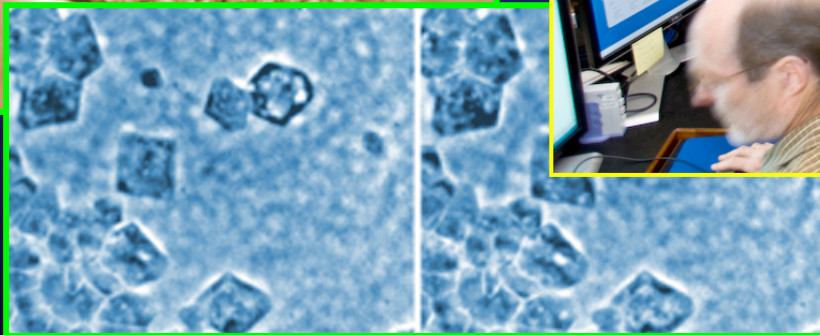
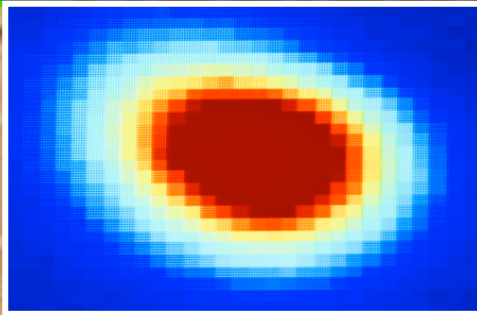
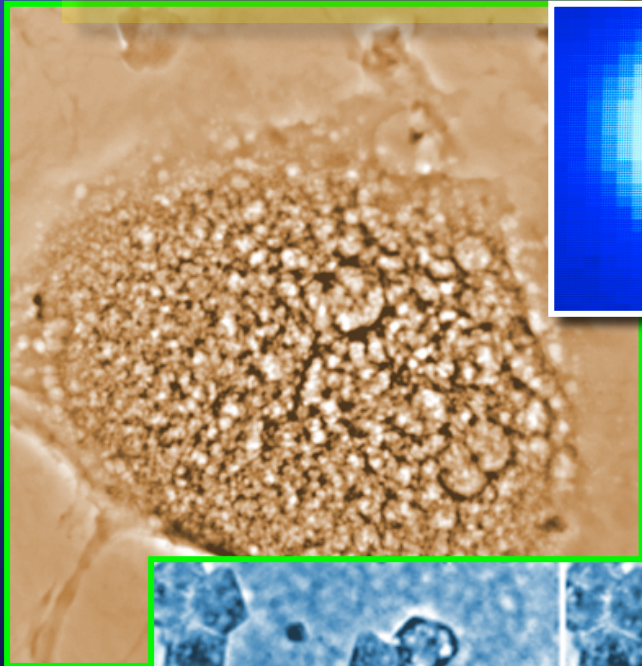
**School on Synchrotron and Free-Electron-Laser Sources and their  
Multidisciplinary Applications**

*26 April - 7 May, 2010*

**Properties of Synchrotron Radiation**

Giorgio Margaritondo  
*EPFL  
Switzerland*

# Properties of Synchrotron Radiation



**Giorgio Margaritondo**

**Ecole Polytechnique Fédérale de Lausanne (EPFL)**

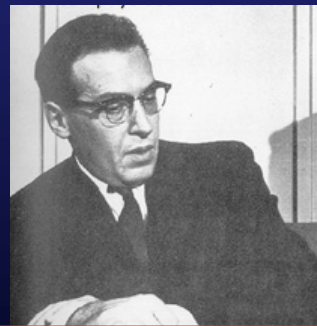
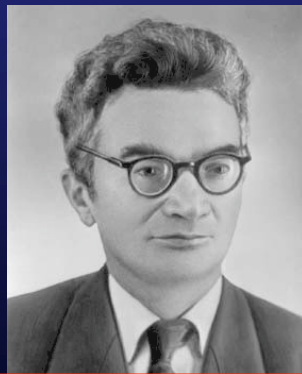
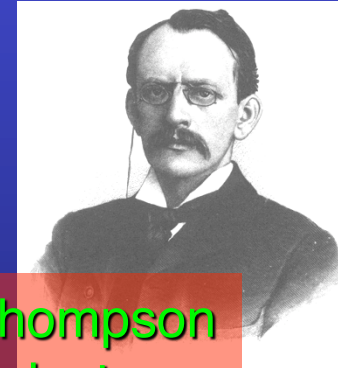
# An interesting history, a bright future:

## The origins:

1898 -- Alfréd  
Lienard conceives  
synchrotron light



1897 -- J. J. Thompson  
discovers the electron



1940s: Isaak Pomeranchuk, Dmitri Ivanenko  
and Julian Schwinger develop a full theory

**A8. Electron Radiation in High Energy Accelerators.**  
JULIAN SCHWINGER, *Harvard University*.<sup>\*</sup>—The only fundamental limitation to the attainment of very high energy electrons in devices such as the betatron and synchrotron is the radiative energy loss accompanying the circular motion. For an electron of energy  $E \gg mc^2$ , moving in a circular path of radius  $R$ , the energy radiated per revolution is

$$\delta E = \frac{4\pi}{3} \frac{e^2}{R} \left( \frac{E}{mc^2} \right)^4$$

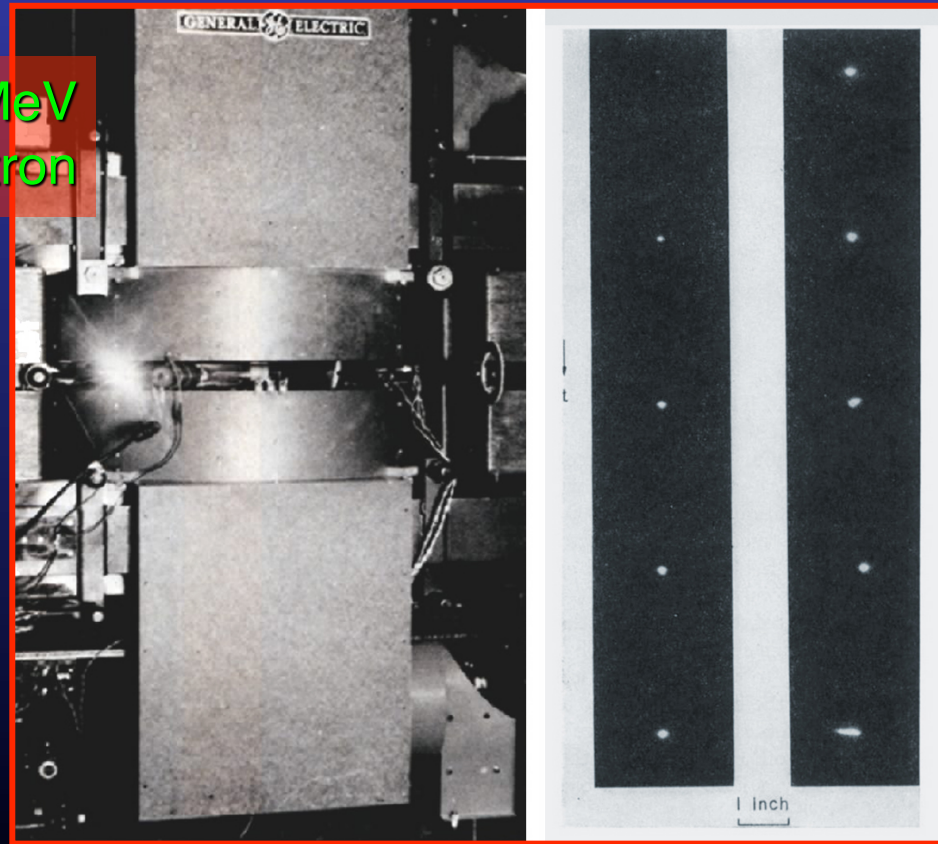
which amounts to roughly 30 keV for an electron of 1 BeV in a magnetic field of  $10^4$  gauss. The radiation spectrum consists of harmonics of the rotation angular frequency



**24 April 1947: at General Electric in Schenectady, Herb Pollock, Robert Langmuir, Frank Elder and Anatole Gurewitsch see synchrotron light for the first time:**

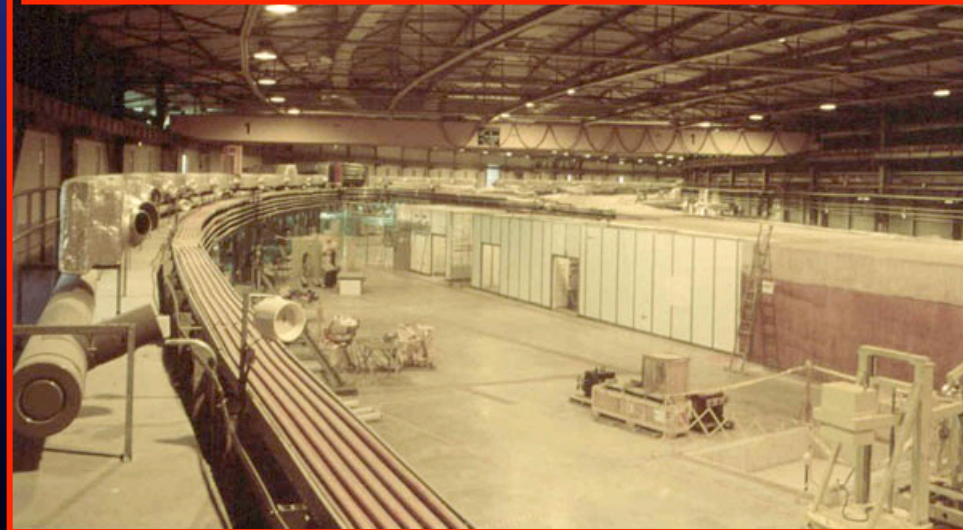
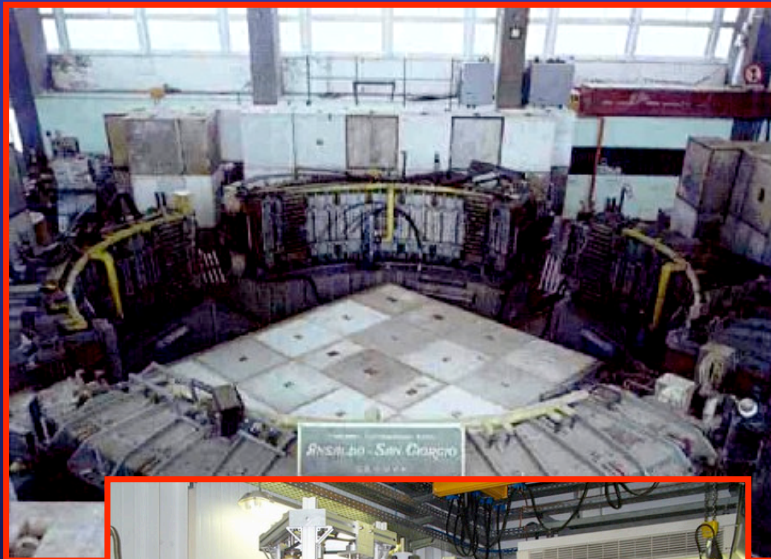
The GE 70 MeV synchrotron

*“a trivial design change and ... a conscious disregard for the rules of radiation safety”*





# From the mid-1960s: Pioneering tests at the Frascati Electron Synchrotron (and then ADONE) and the PULS (Progetto Utilizzazione Luce di Sincrotrone)



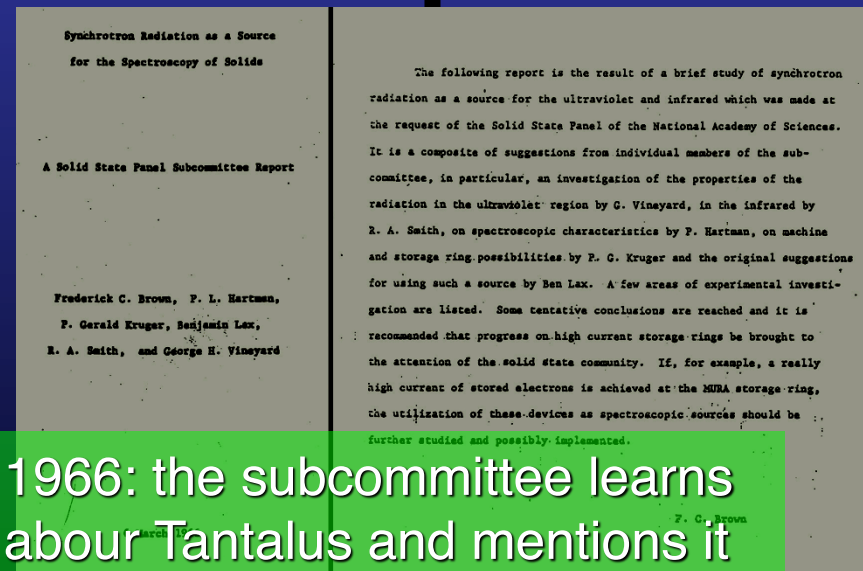
# A parallel series of lucky coincidences:

1953: 15 institutions form MURA (Midwest Universities Research Association) to bid for the future Fermilab

1963: The Batavia site obtains Fermilab, MURA dies in 1967

In the meantime (1965) MURA started in Stoughton, Wisconsin, the construction of the 240 MeV storage ring Tantalus, that no longer had a mission

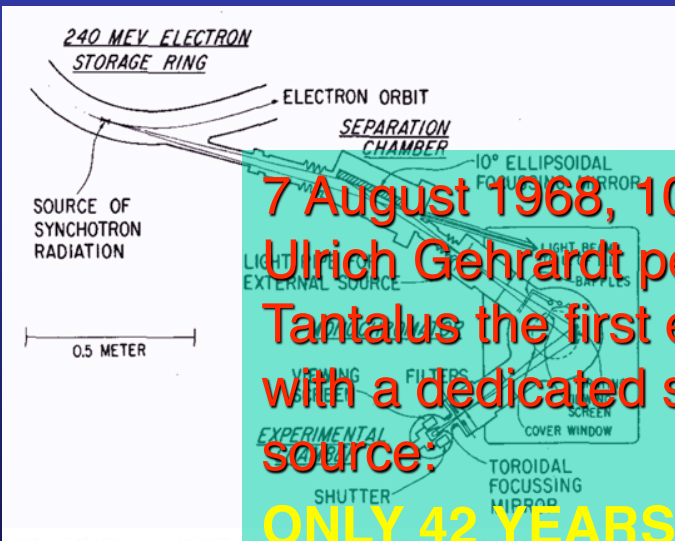
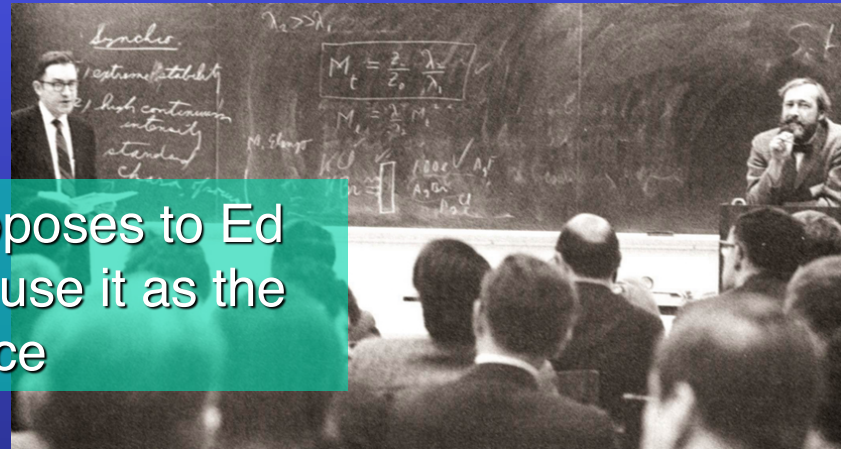
1965: a subcommittee of the National Research Council starts exploring the use of synchrotron light



1966: the subcommittee learns about Tantalus and mentions it in its final report



1966: Fred Brown (Urbana) proposes to Ed Rowe, the father of Tantalus, to use it as the first dedicated synchrotron source

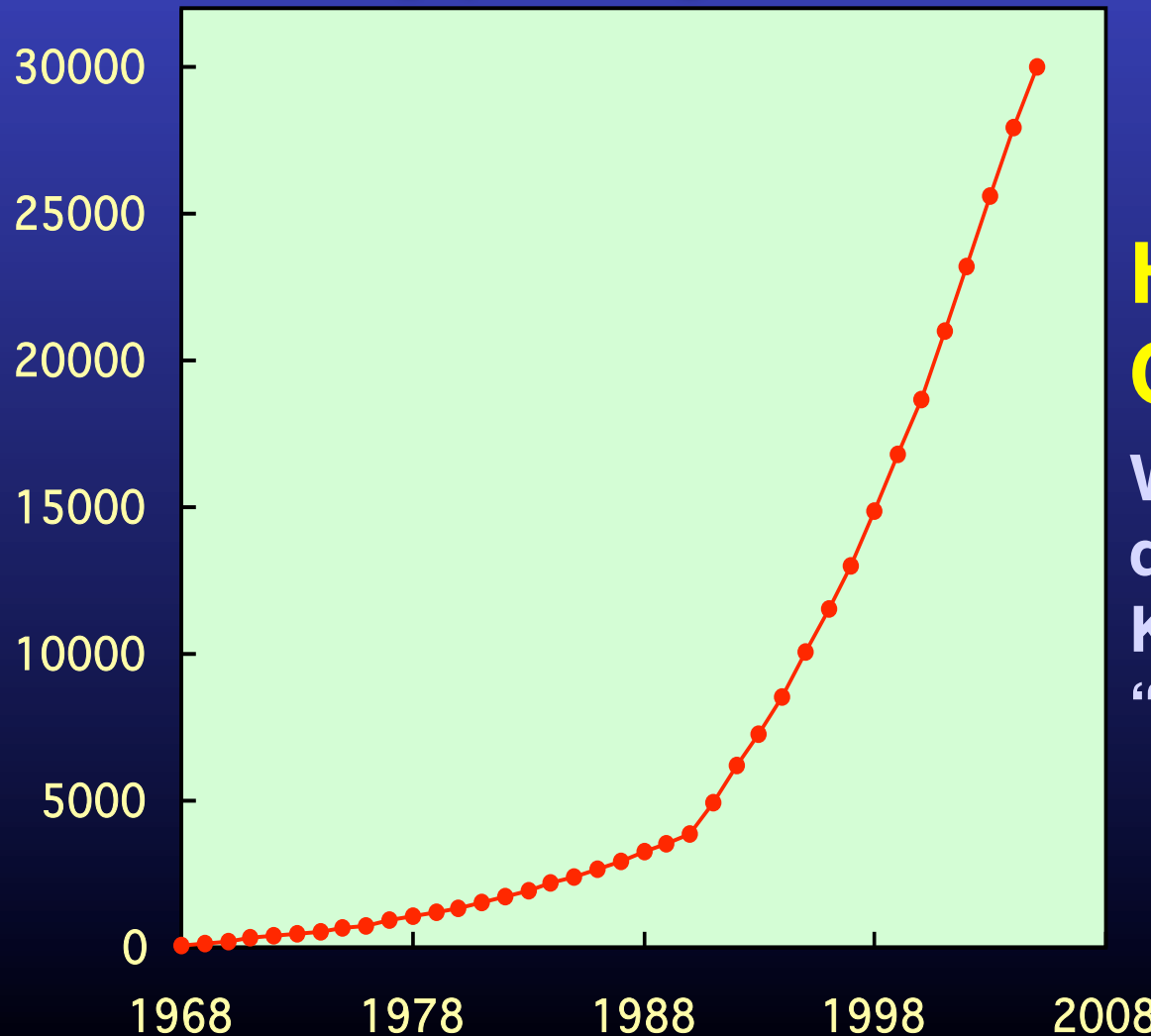


**7 August 1968, 10:40 a.m.:**  
**Ulrich Gehrardt performs on Tantalus the first experiment with a dedicated synchrotron source:**  
**ONLY 42 YEARS AGO!!!**





# Synchrotron Facilities in the World (2010): 69 in 25 Countries (operating or under construction)



## Historical Growth:

Worldwide ISI data 1968-2006,  
Keyword:  
“synchrotron”

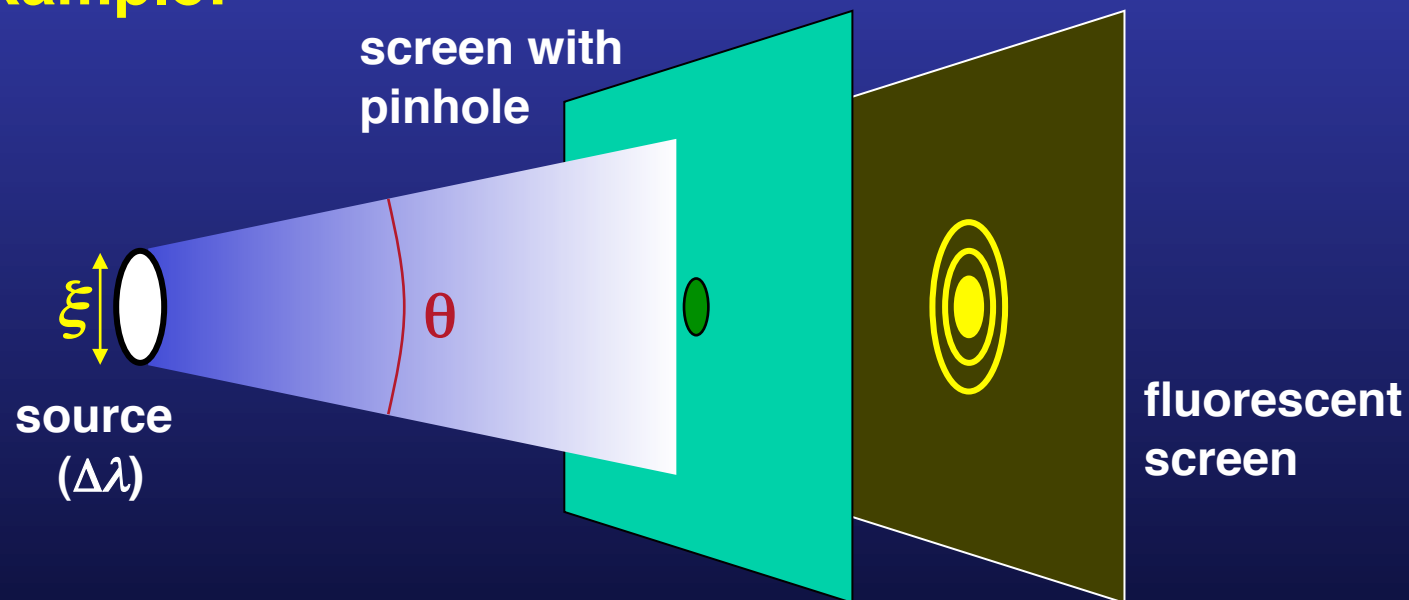
... but, for a broader picture:

Hits from a 2010 Google search:

<b>“Synchrotron”</b>	<b>2,090,000</b>
<b>“Free electron laser”</b>	<b>2,070,000</b>
<b>“LINAC”</b>	<b>431,000</b>
<b>“Hadron collider”</b>	<b>1,370,000</b>
<b>“Protein crystallography”</b>	<b>469,000</b>
<b>“Synchrotron photoemission”</b>	<b>186,000</b>
<b>“Margaritondo”</b>	<b>64,800</b>
<b>“Pamela Anderson”</b>	<b>21,300,000</b>
<b>“Viagra”</b>	<b>53,700,000</b>

**Coherence:** “the property that enables a wave to produce **visible** diffraction and interference effects”

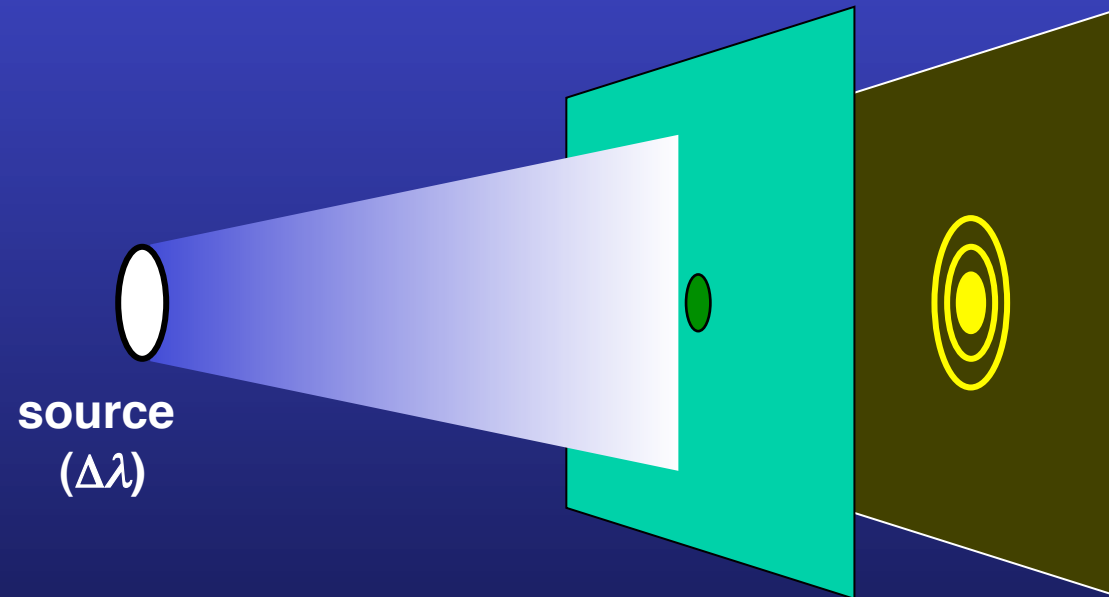
**Example:**



The diffraction pattern may or may not be visible on the fluorescent screen depending on the source size  $\xi$ , on its angular divergence  $\theta$  and on its wavelength bandwidth  $\Delta\lambda$

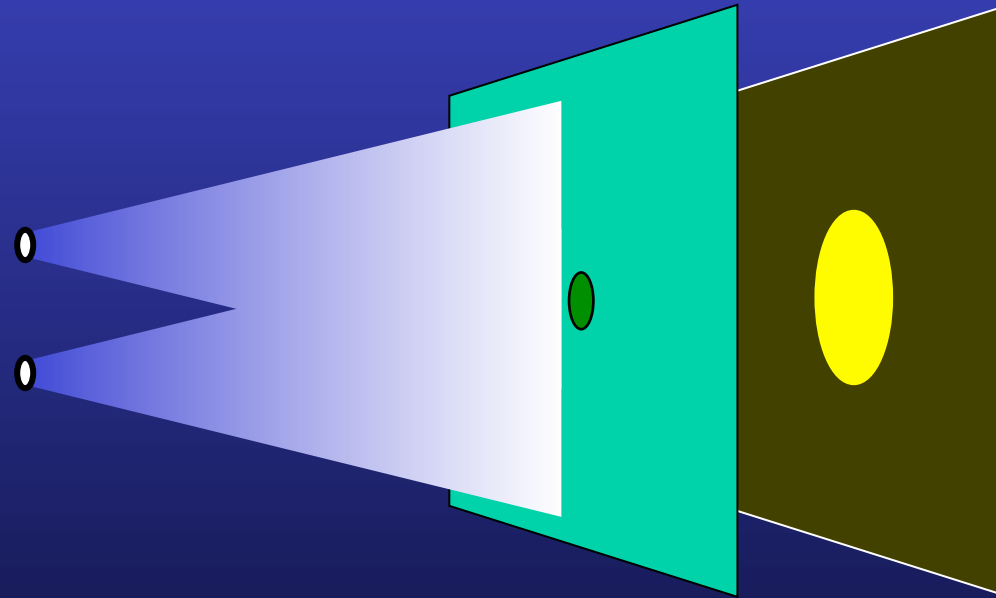


## Longitudinal (time) coherence:



- Condition to see the pattern:  $\Delta\lambda/\lambda < 1$
- Parameter characterizing the longitudinal coherence:  
“coherence length”:  $L_c = \lambda^2/\Delta\lambda$
- Condition of longitudinal coherence:  $L_c > \lambda$

## Lateral (space) coherence — analyzed with a source formed by two point sources:



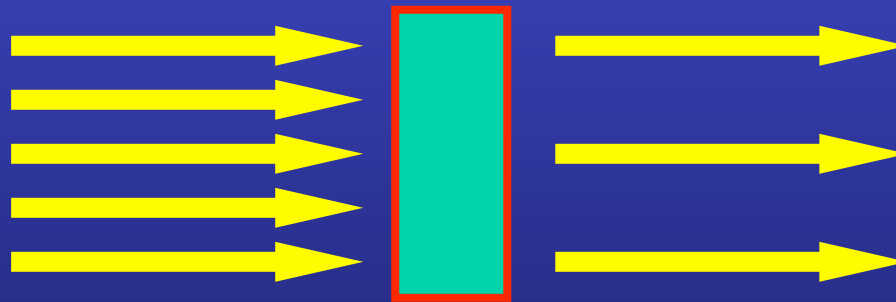
- Two point sources produce overlapping patterns: diffraction effects are no longer visible.
- However, if the two source are close to each other an overall diffraction pattern may still be visible: the condition is to have a **large “coherent power”**  $(2\lambda/\xi\theta)^2$

# Coherence – summary:

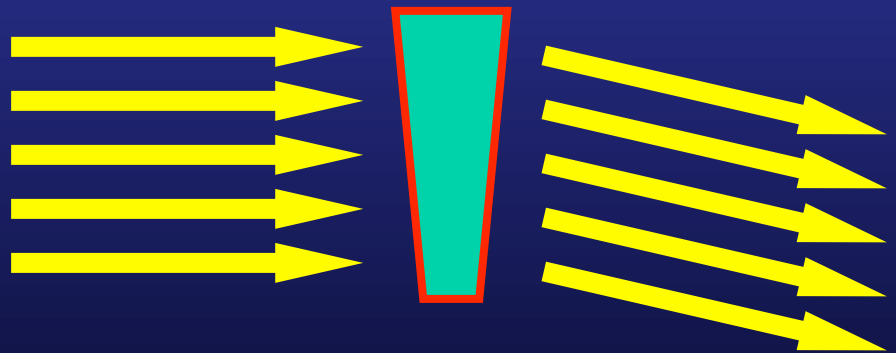
- Large coherence length  $L_c = \lambda^2 / \Delta\lambda$
- Large coherent power  $(2\lambda / \xi\theta)^2$
- **Both difficult to achieve for small wavelengths (x-rays)**
- **The conditions for large coherent power are equivalent to the geometric conditions for high brightness**



# Light-matter interactions in radiology:



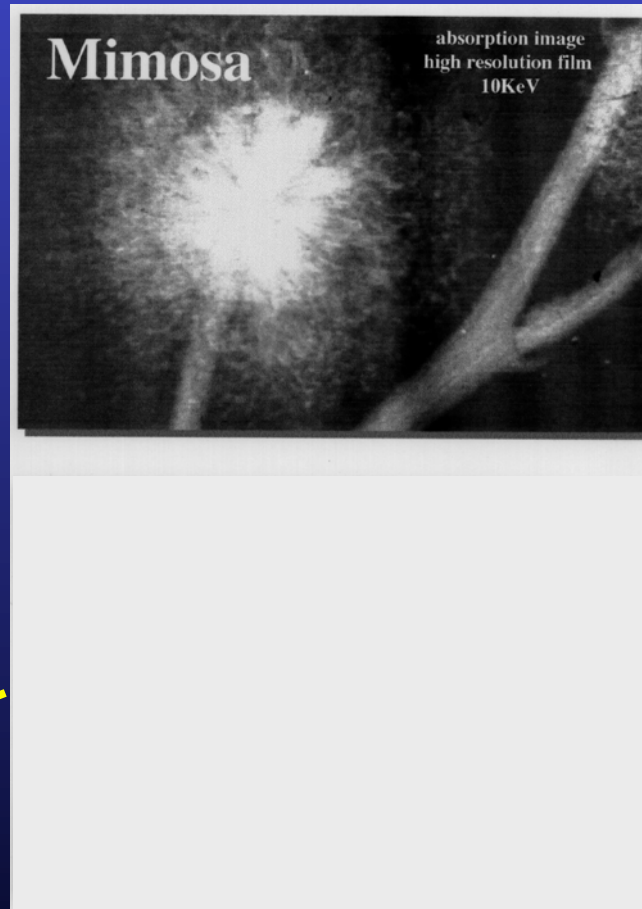
Absorption -- described by the absorption coefficient  $\alpha$



Refraction (and diffraction/interference) -- described by the refractive index  $n$

**For over one century, radiology was based on absorption: why not on refraction /diffraction?**

# Conventional radiology



# Refractive-index radiology (Giuliana Tromba)

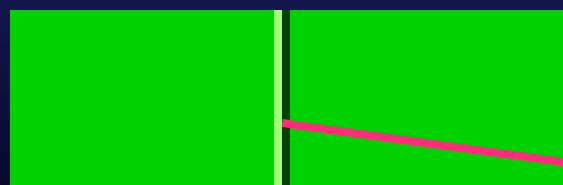
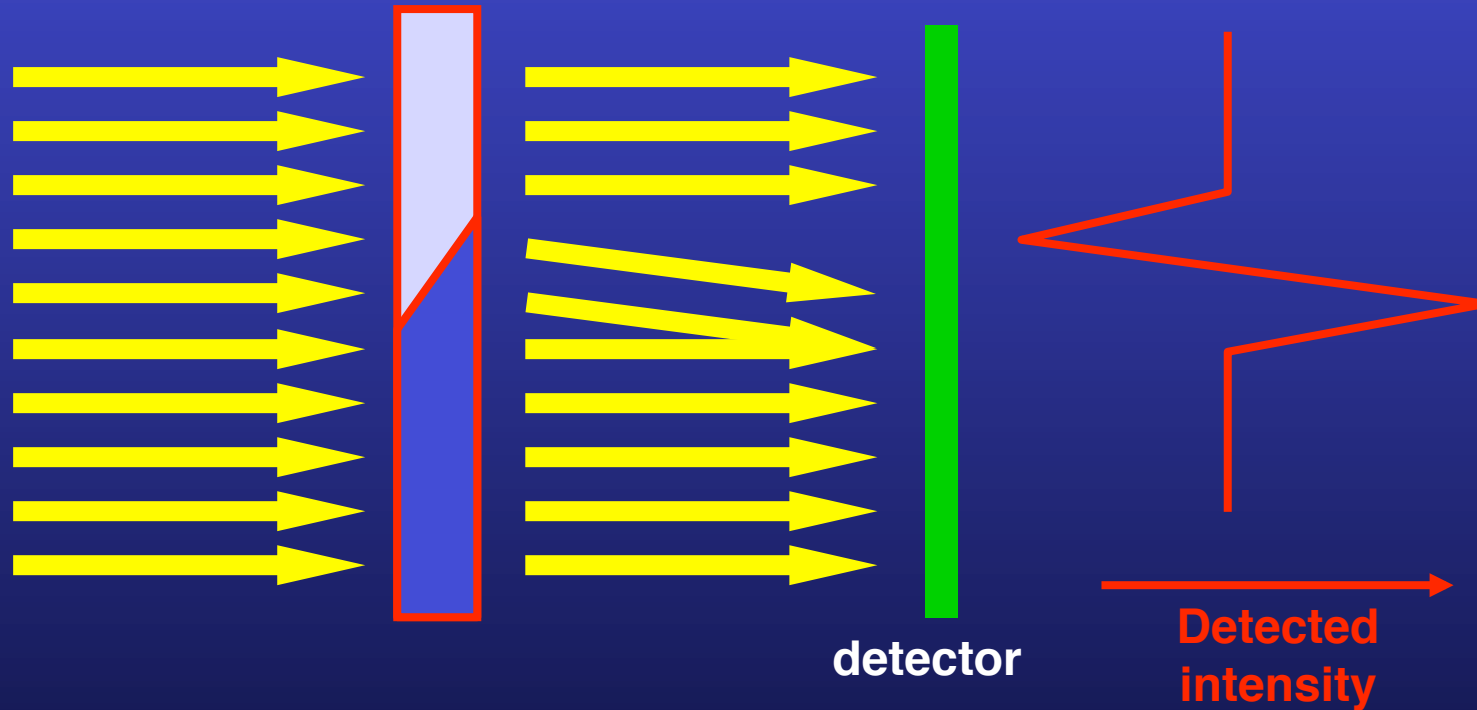
# “Refraction” x-ray imaging:



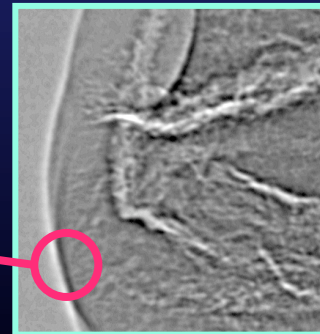
Edge between  
regions with  
different  $n$ -values



# “Refraction” x-ray imaging:



Idealized edge image



Real example  
(frog egg)

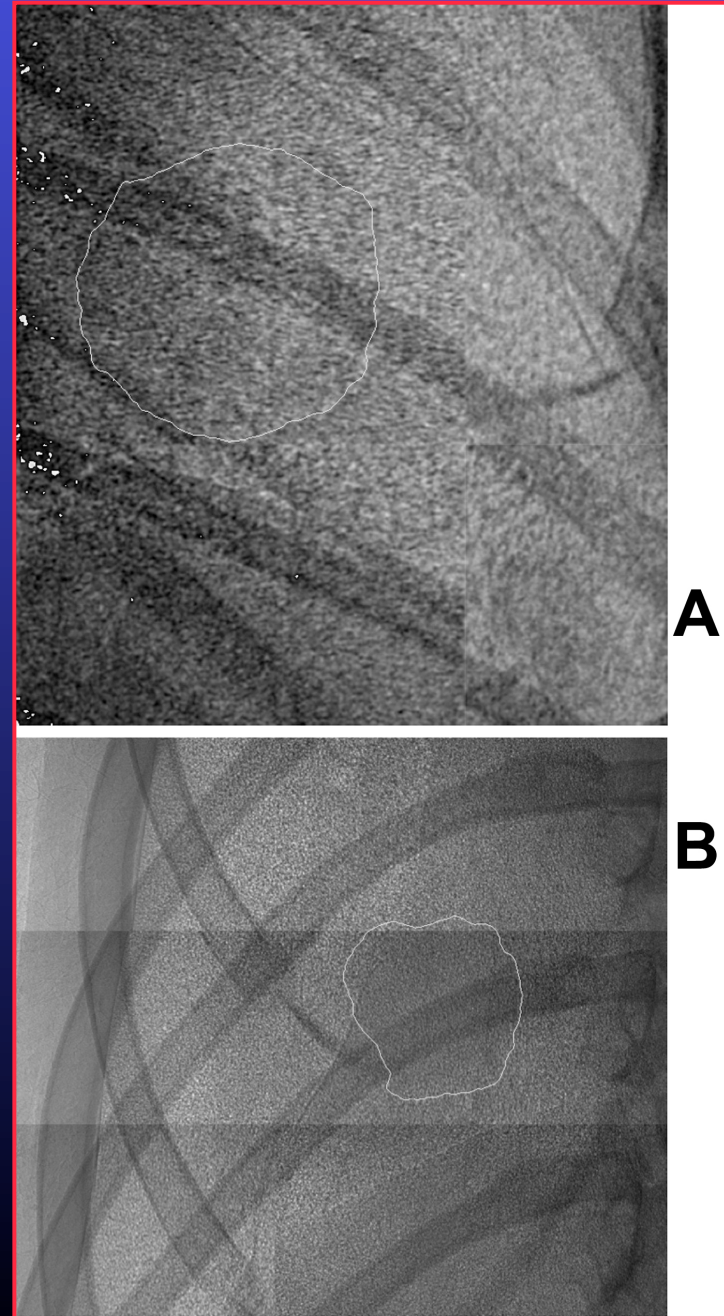
# Microradiology study of mutant drosophila fly evolution

[Charron, Vassalli et al.]

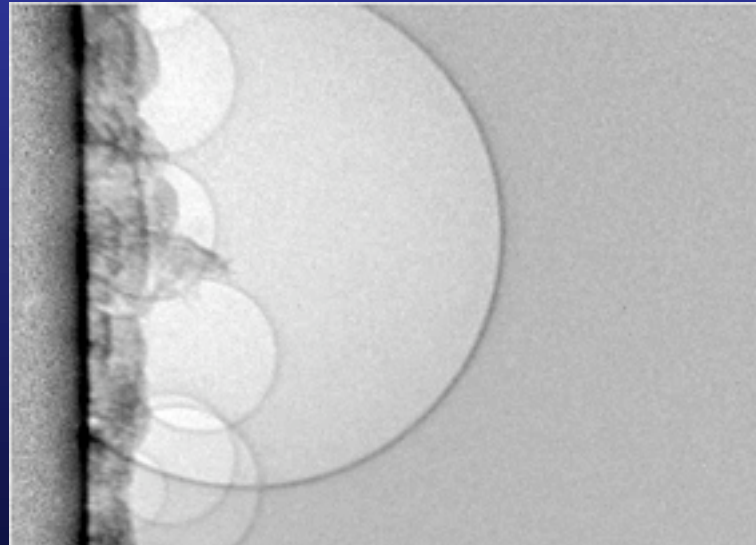


## Very Early Detection of Lung Cancer in Mouse Models

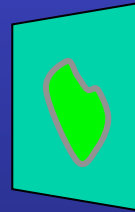
Guilin Zhang, Chia-Chi Chien, Ping Liu, Weisheng Yue, Jiangi Sun, Yan Li, Hong-Jie Xue, Xuemin Xu, Chang Hai Wang, Y. Hwu, Nanyow Chen, Chien Hung Lu, Ting-Kuo Lee, M. Hsiao, Yuh-Cheng Yang, Yen-Ta Lu, Yu-Tai Ching, P. C. Yang, J. H. Je, G. Margaritondo



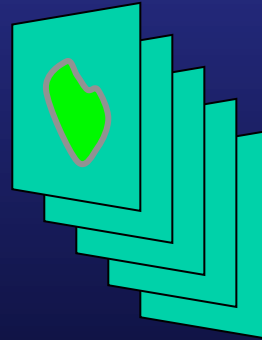
# Building on bubbles (zinc electrodeposition):



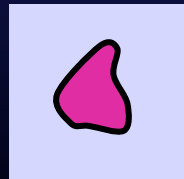
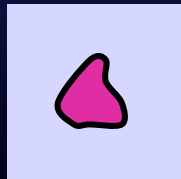
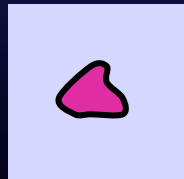
# X-ray (micro)tomography:



A single (projection) x-ray image does not deliver three-dimensional information



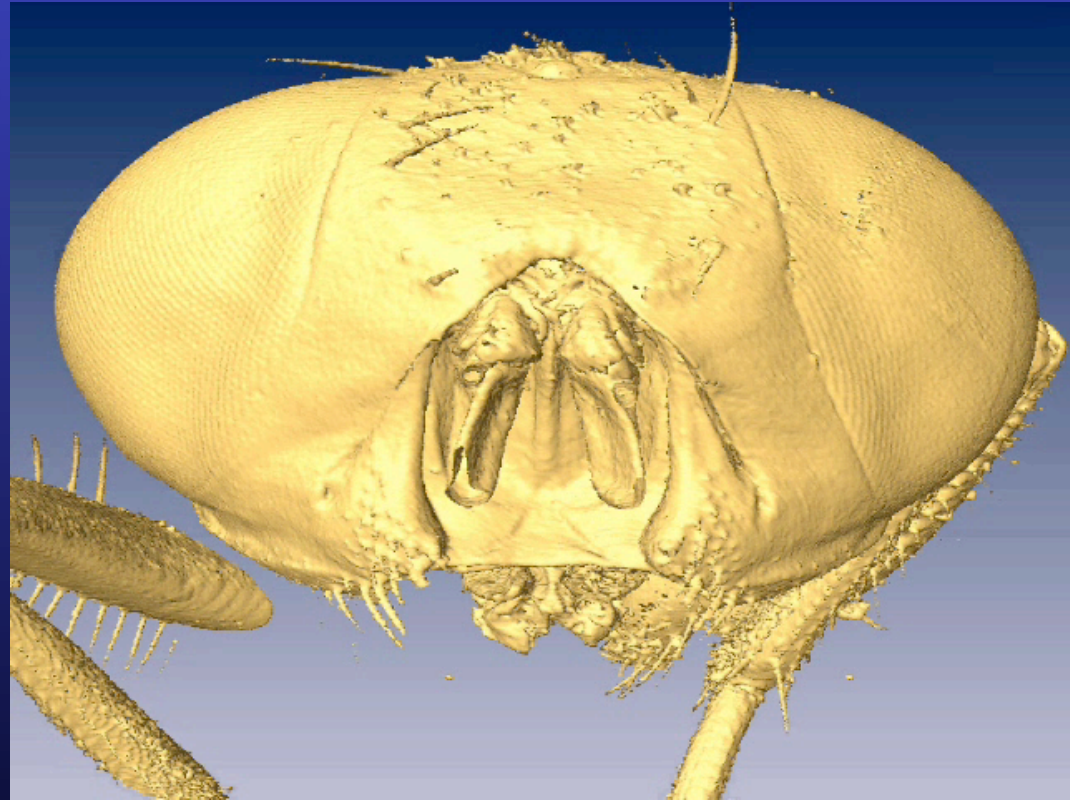
Many x-ray images taken at different angles can be computer-reconstructed in three dimensions -- and can even give movies





# Phase contrast micro-tomography: housefly

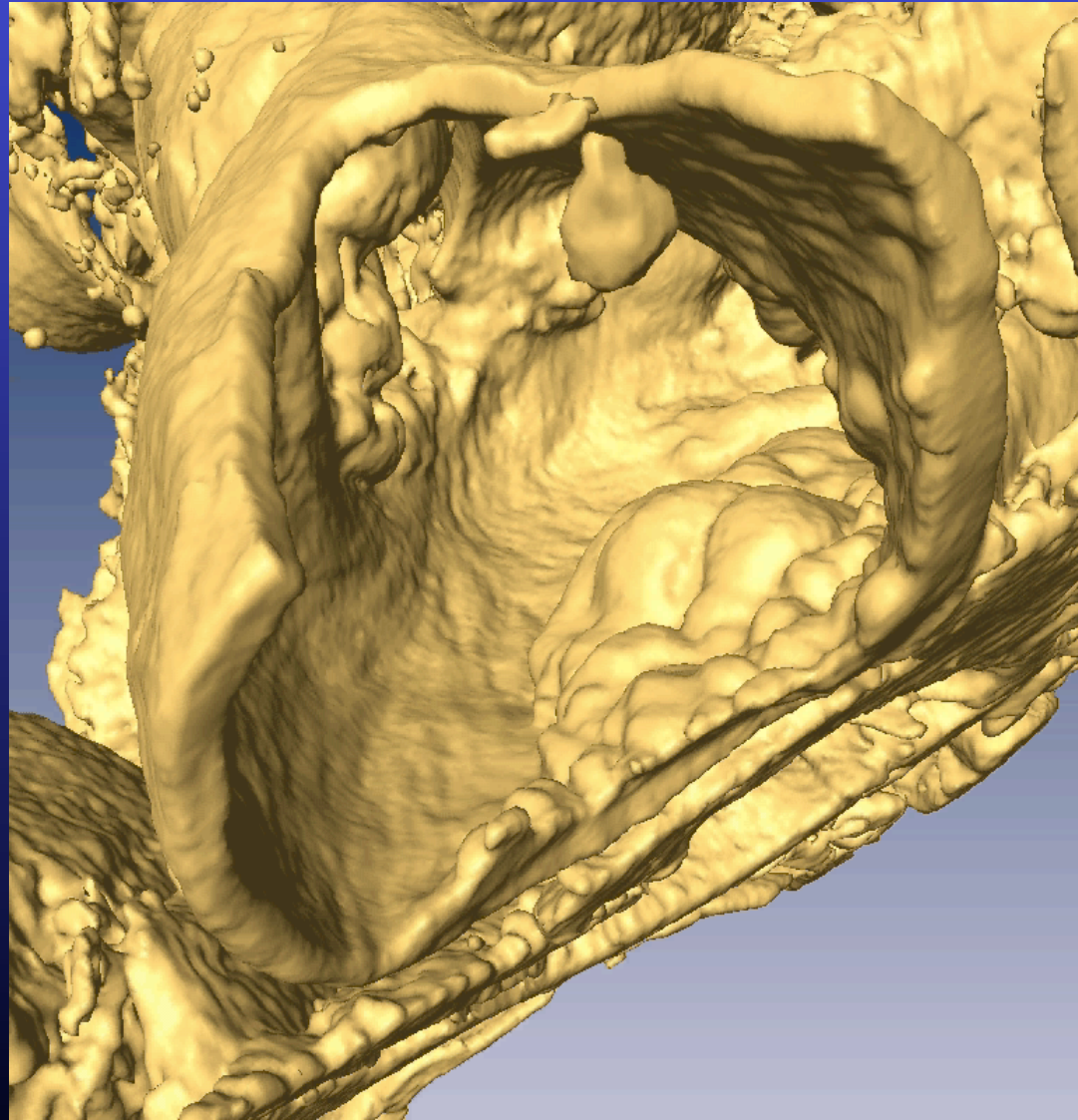
Yeukuang  
Hwu, Jung  
Ho Je et al.





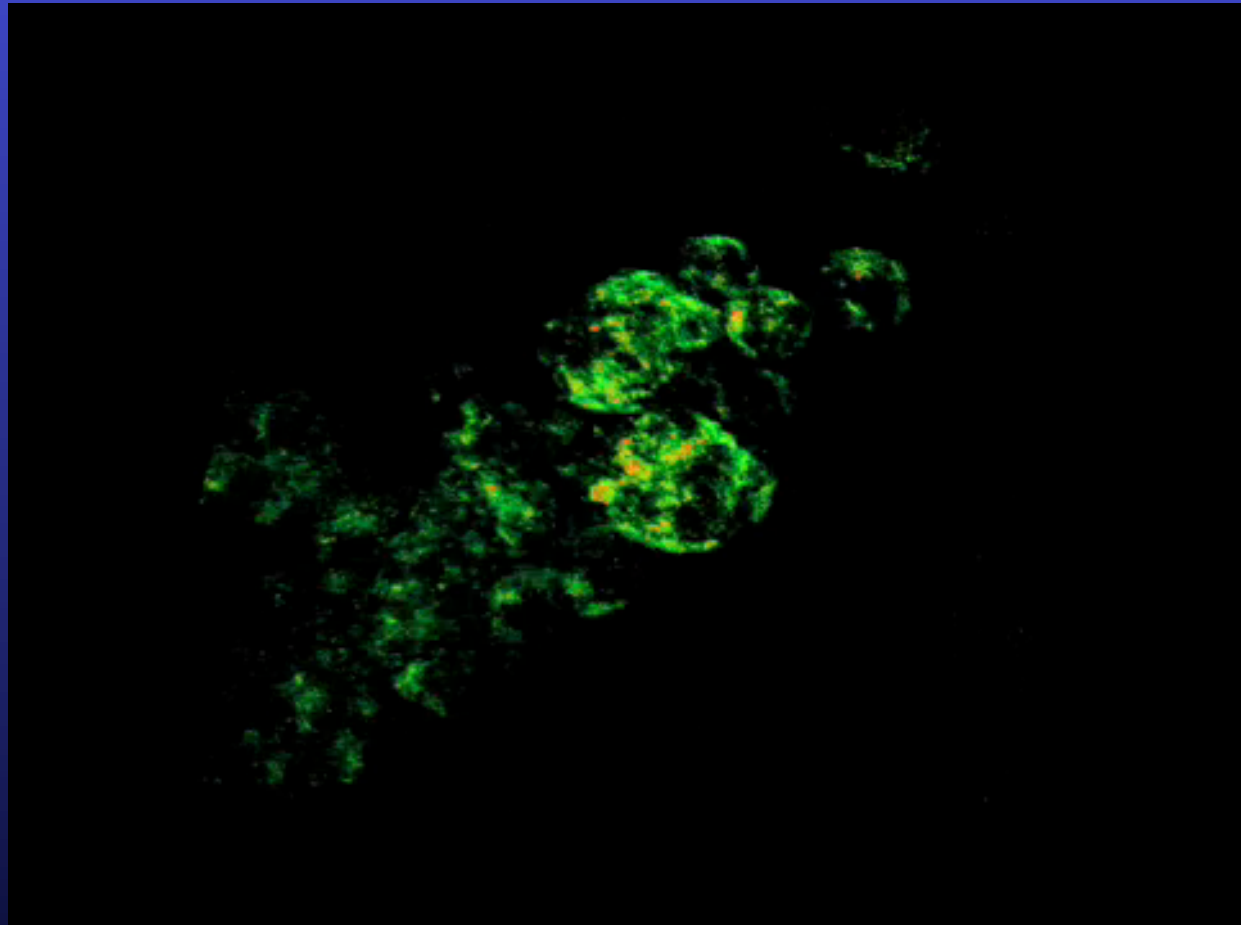
# Phase contrast micro-tomography: navigating inside micro-vessels

Yeukuang  
Hwu, Jung  
Ho Je et al.



## From detection to treatment?

Y. S. Chu, J. M. Yi, F. De  
Carlo, Q. Shen, W.-K-  
Lee, H. J. Wu, C. L.  
Wang, J. Y. Wang, C. J.  
Liu, C. H. Wang, S. R.  
Wu, C. C. Chien, Y. Hwu,  
A. Tkachuk, W. Yun, M.  
Feser, K. S. Liang, C. S.  
Yang, J. H. Je, G.  
Margaritondo

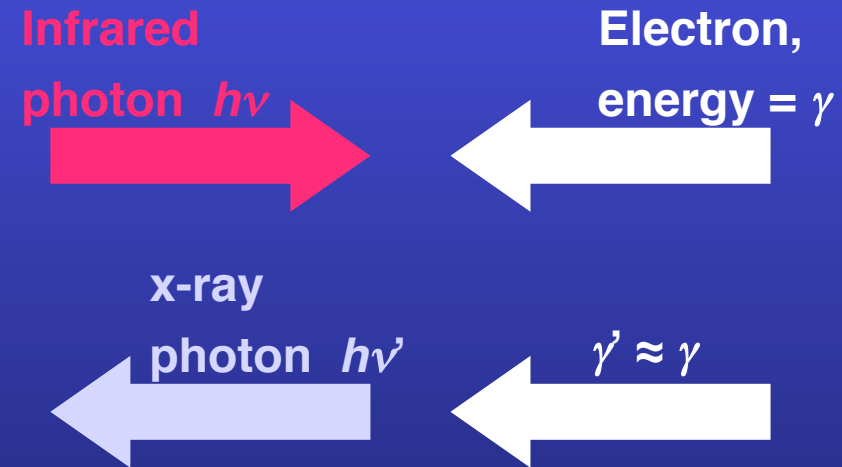


**Agglomerated Au nanoparticles  
attached to cancer cells**

## New types of sources:

- **Ultrabright storage rings (SLS, new Grenoble project) approaching the diffraction limit**
- **Self-amplified spontaneous emission (SASE) X-ray free electron lasers**
- **VUV FEL's (such as CLIO)**
- **Energy-recovery machines**
- **Inverse-Compton-scattering table-top sources**

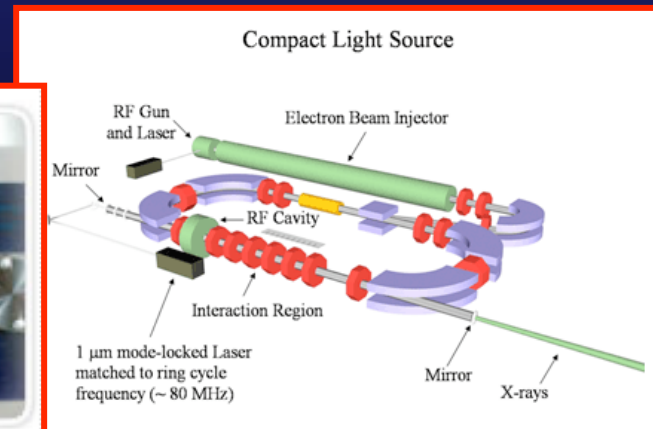
# The magic of Compton backscattering: changing infrared into x-rays



Doppler effect: in the electron beam frame, the photon energy  $\approx 2\gamma h\nu$ . This is also the energy of the backscattered photon in the electron-beam frame.

In the laboratory frame, there is again a Doppler shift with a  $2\gamma$  factor, thus:

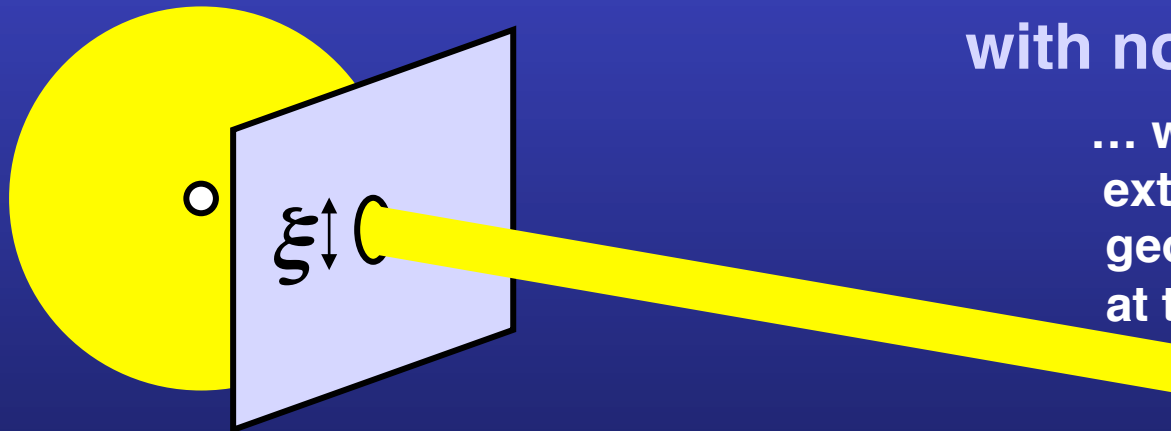
$$h\nu' \approx 4\gamma^2 h\nu$$



# The absolute limit for coherence -- and brightness

Take a standard photon source  
with no lateral coherence ...

... with a pinhole (size  $\xi$ ), we can  
extract coherent light with good  
geometrical characteristics (but  
at the cost of losing most of the  
emission)



However, if the pinhole size is too small  
diffraction effects increase the beam  
divergence so that:

$$\xi\theta > \lambda$$

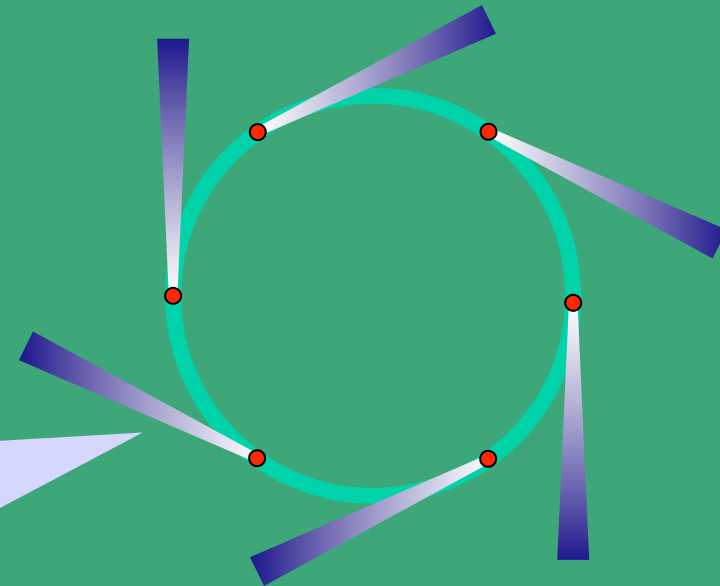
**No source geometry beats this diffraction limit**



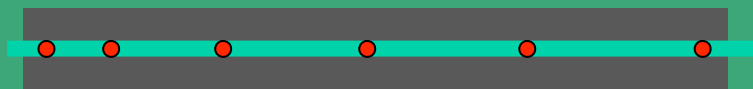
# Energy-recovery LINAC sources

The brightness depends on the geometry of the source, i.e., of the electron beam

In a storage ring, the electrons continuously emit photons. This “warms up” the electron beam and negatively affects its geometry

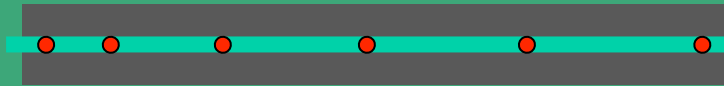


Controlling the electron beam geometry is much easier in a linear accelerator (LINAC). Thus, LINAC sources can reach higher brightness levels





# Energy-recovery LINAC sources



However, contrary to the electrons in a storage ring, the electrons in a LINAC produce photons only once: the power cost is too high

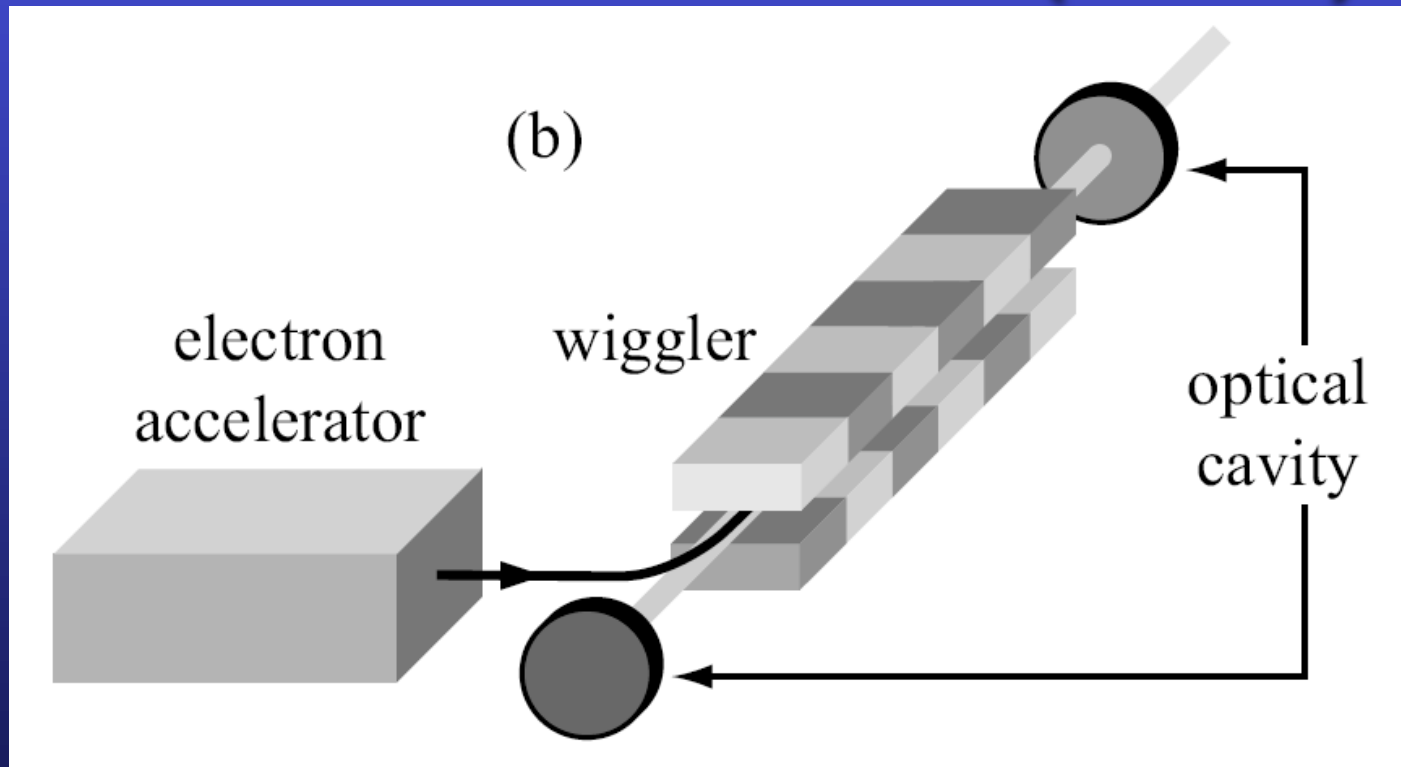
## Solution: recovering energy



Accelerating section

Energy-recovery section

# Free-electron lasers (FEL's):



A lasing mechanism requires **optical amplification** in an **optically active medium**.

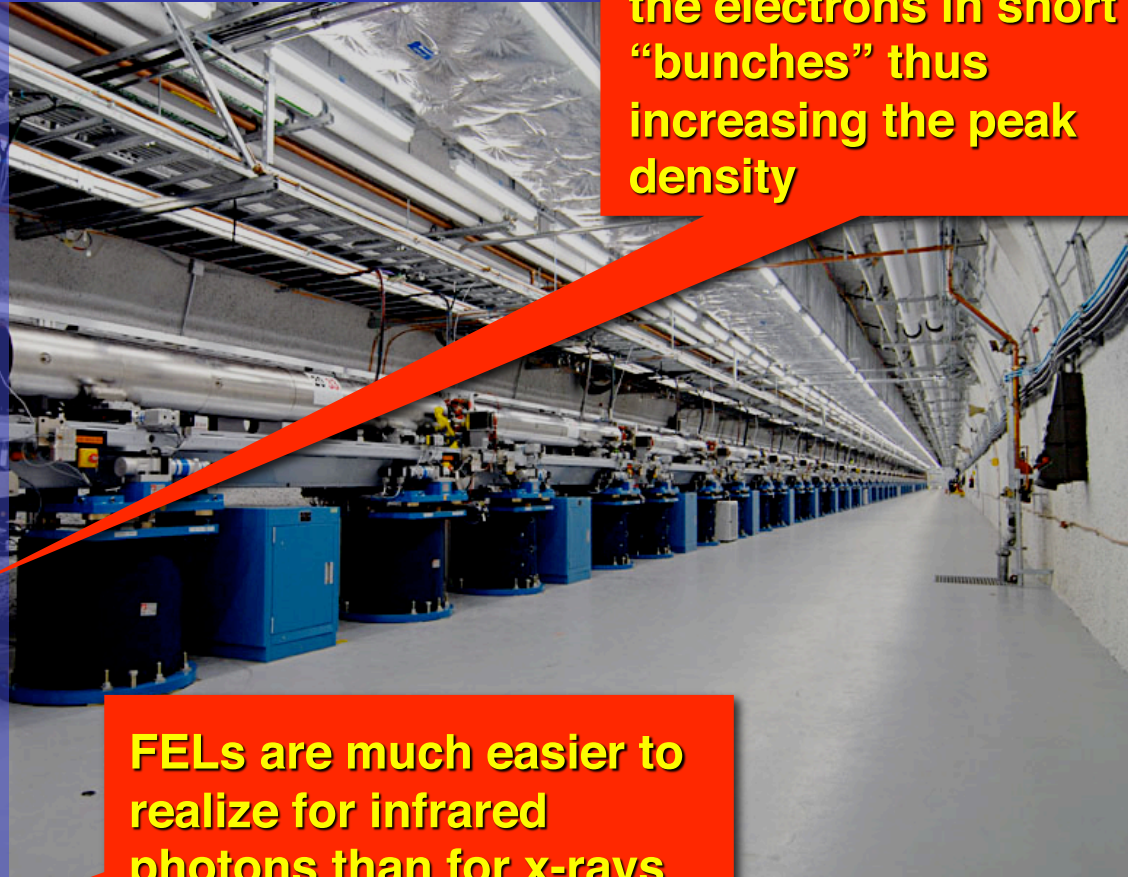
In an FEL, the medium is an electron bunch passing through a wiggler or undulator; its interaction with previously emitted photons causes the amplification

# FEL's: main requirements for strong optical amplification

1. A well-defined electron energy: limited "energy spread"
2. A small transverse cross section of the electron beam.
3. Small angular deviations of the real electron trajectories from the "reference path"
4. In general, a very high density of electrons
5. The optical amplification *increases with the wavelength*

**It is better to close-pack the electrons in short "bunches" thus increasing the peak density**

**FELs are much easier to realize for infrared photons than for x-rays**



# Self-amplified spontaneous emission x-ray free-electron lasers (SASE X-FEL's)

Normal (visible, IR, UV) lasers:

optical amplification in amplifying medium

plus optical cavity (two mirrors)



X-ray lasers: no mirrors → no optical cavity → need for one-pass high optical amplification



## SASE strategy:

electron bunch



LINAC (linear accelerator)

Wiggler

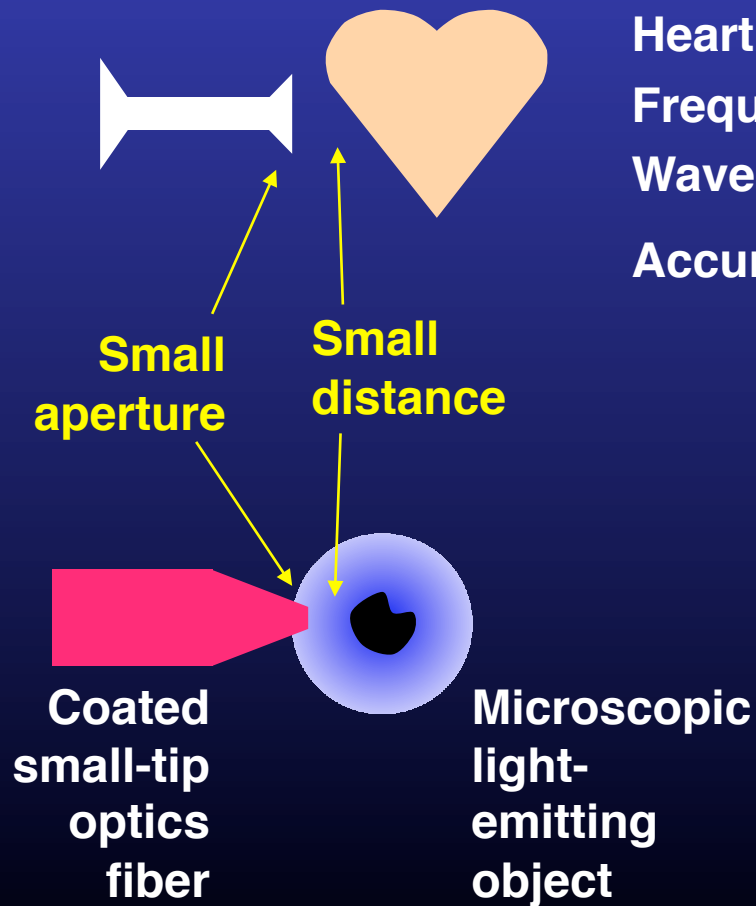


The microbunching increases the electron density and the amplification and creates very short pulses



# Use of infrared FEL's:

## The scanning near-field optical microscope (SNOM) -- like a "stethoscope"



Heart:

Frequency  $\approx 30\text{-}100$  Hz

Wavelength  $\lambda \approx 102$  m

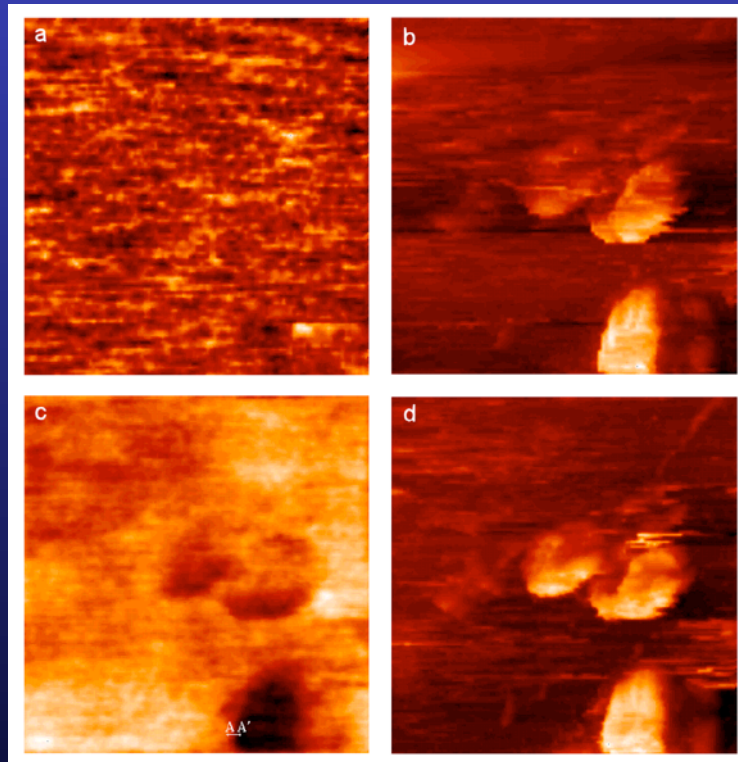
Accuracy in localization  $\approx 10$  cm  $\approx \lambda/1000$

**SNOM resolution: well below the "diffraction limit" of standard microscopy ( $\approx \lambda$ )**

# 20x20 $\mu\text{m}^2$ SNOM image of growth medium (A. Cricenti et al.):

$\lambda = 6.6 \mu\text{m}$

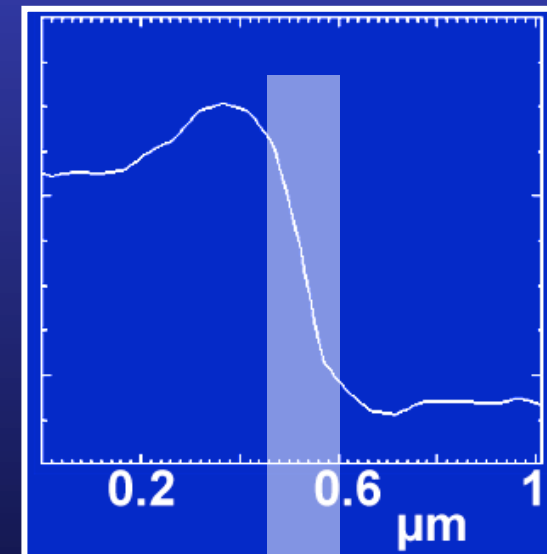
S-O & N-O  
vibrations  
( $\lambda = 6.95 \mu\text{m}$ )



SNOM

topography

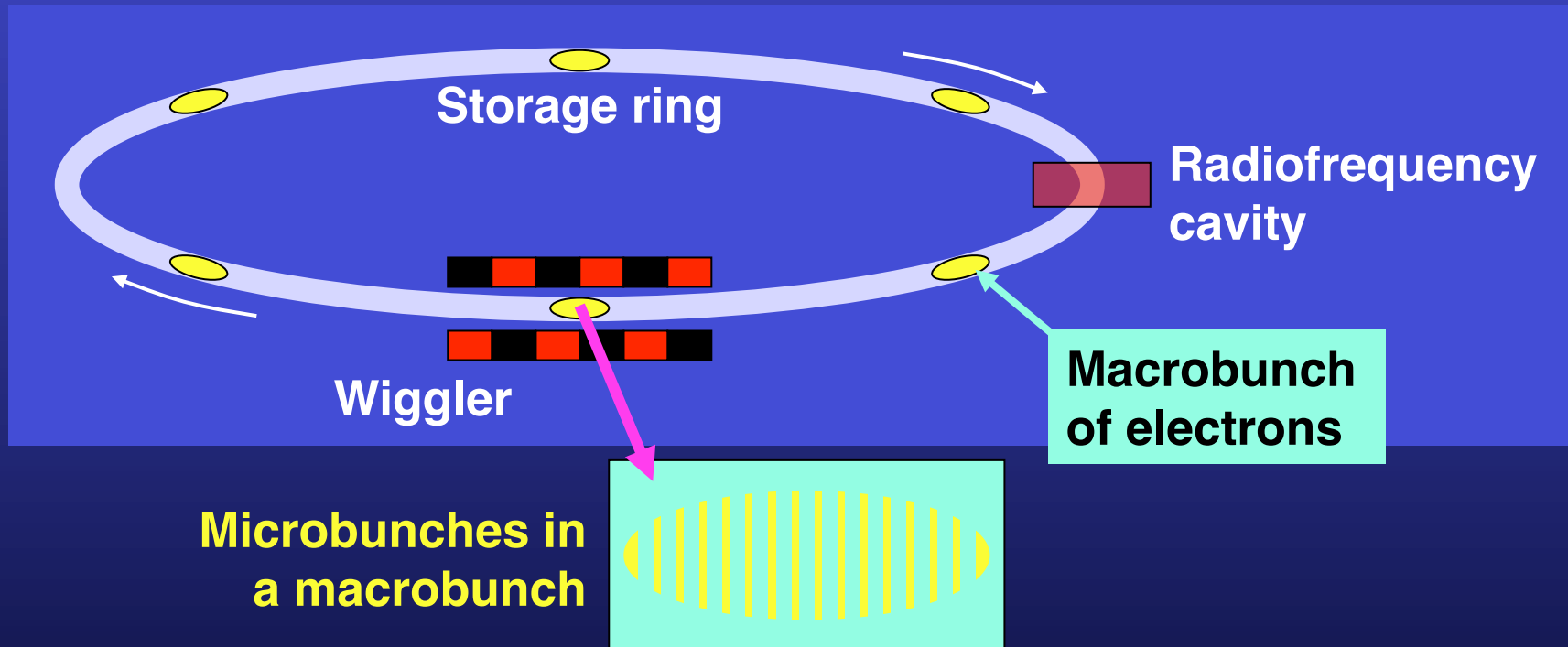
Intensity line scan



Resolution

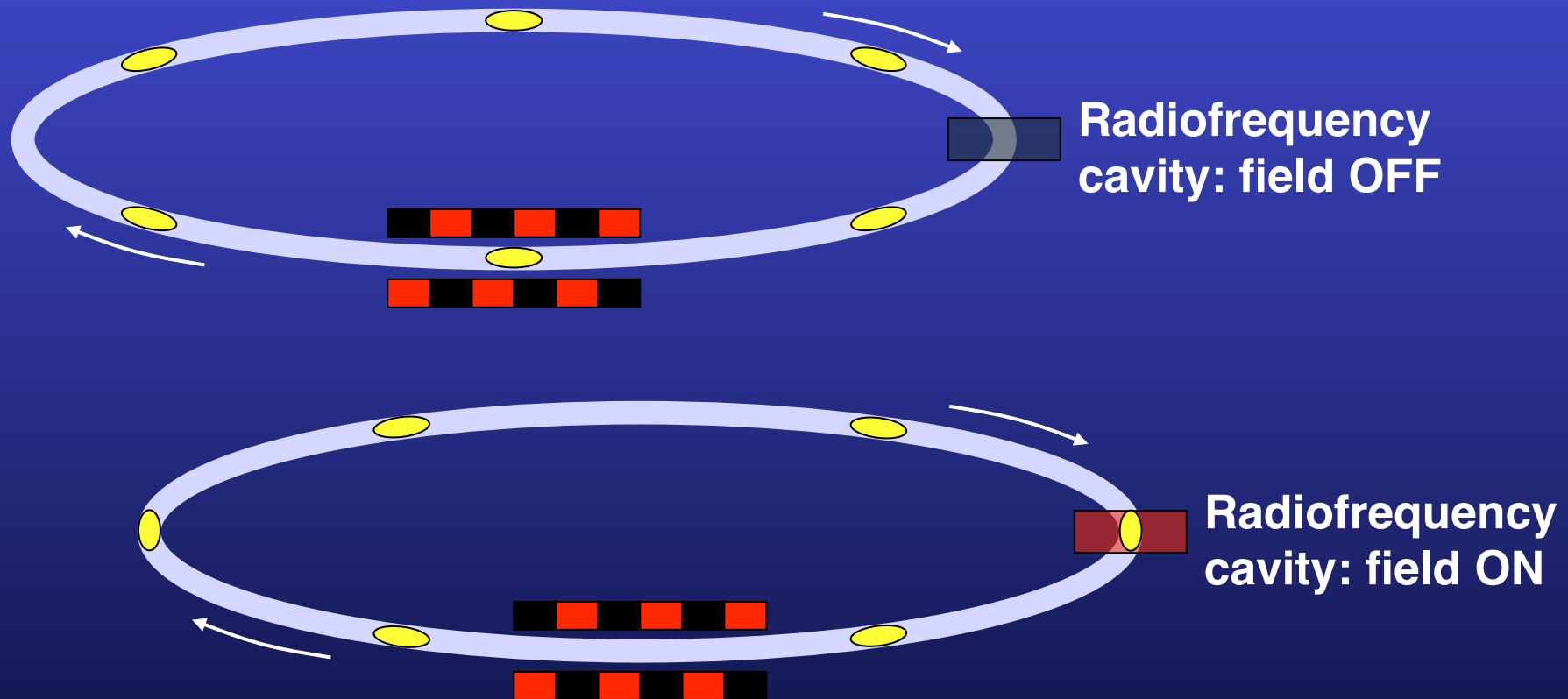
$\approx 0.15 \mu\text{m} \ll \lambda$

# Electron bunches in an FEL



The electrons passing through a wiggler in a storage ring are concentrated in “macro bunches”; within each macrobunch, the electrons are further concentrated in a series of “microbunches”

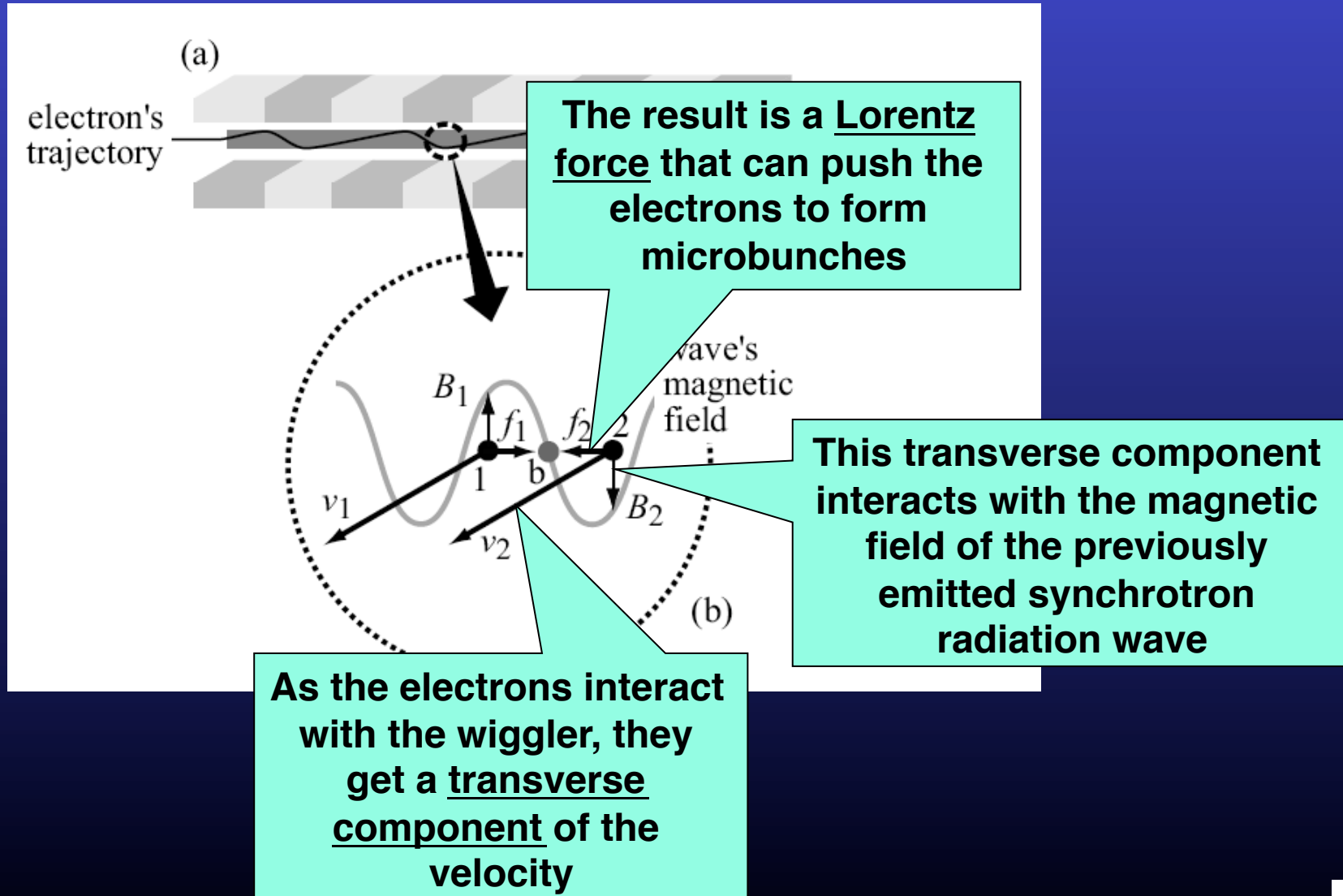
# What causes the macrobunches?



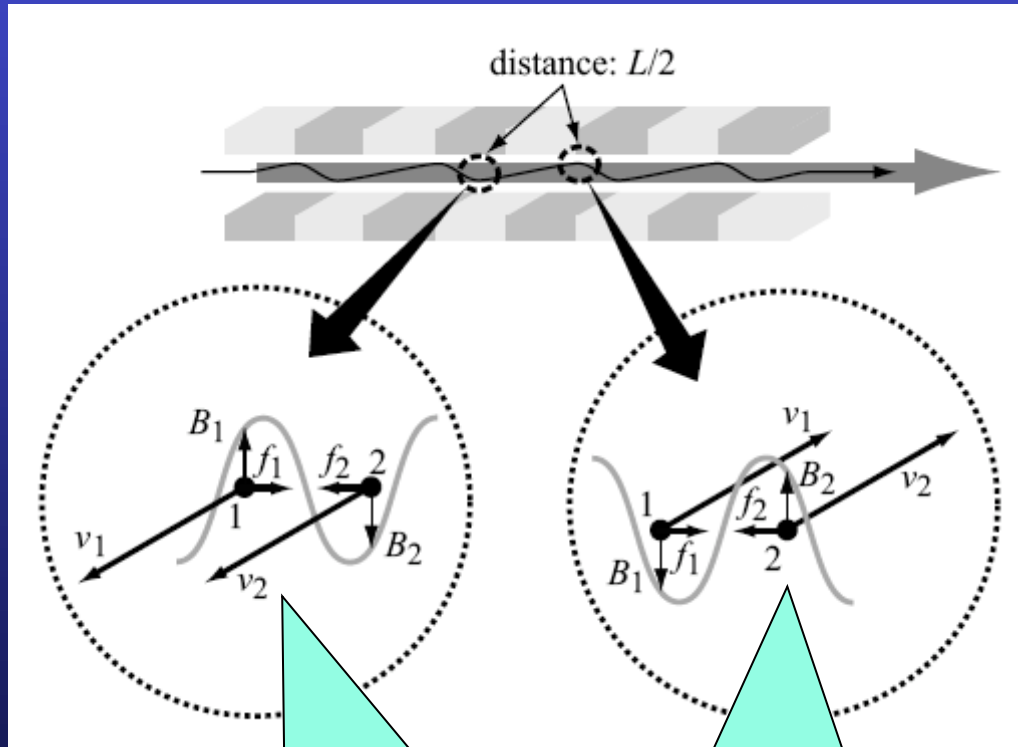
The circulating electrons lose energy by emitting synchrotron radiation. This energy is given back to them by a radiofrequency cavity that produces an accelerating electric field. But this only works for electrons that pass through the cavity at the right time: only the electrons in the corresponding macrobunches can steadily circulate -- the others decay



# What causes the microbunches?



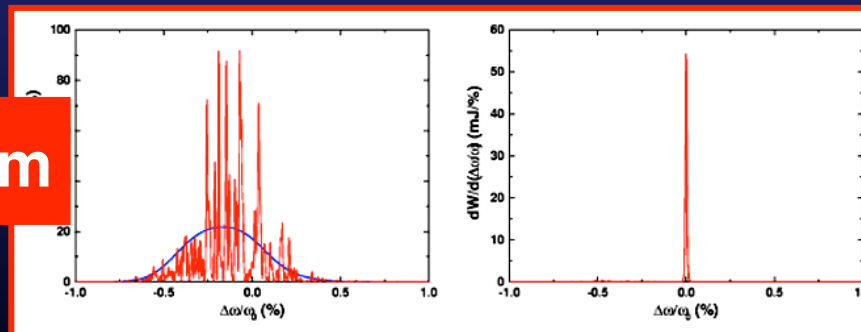
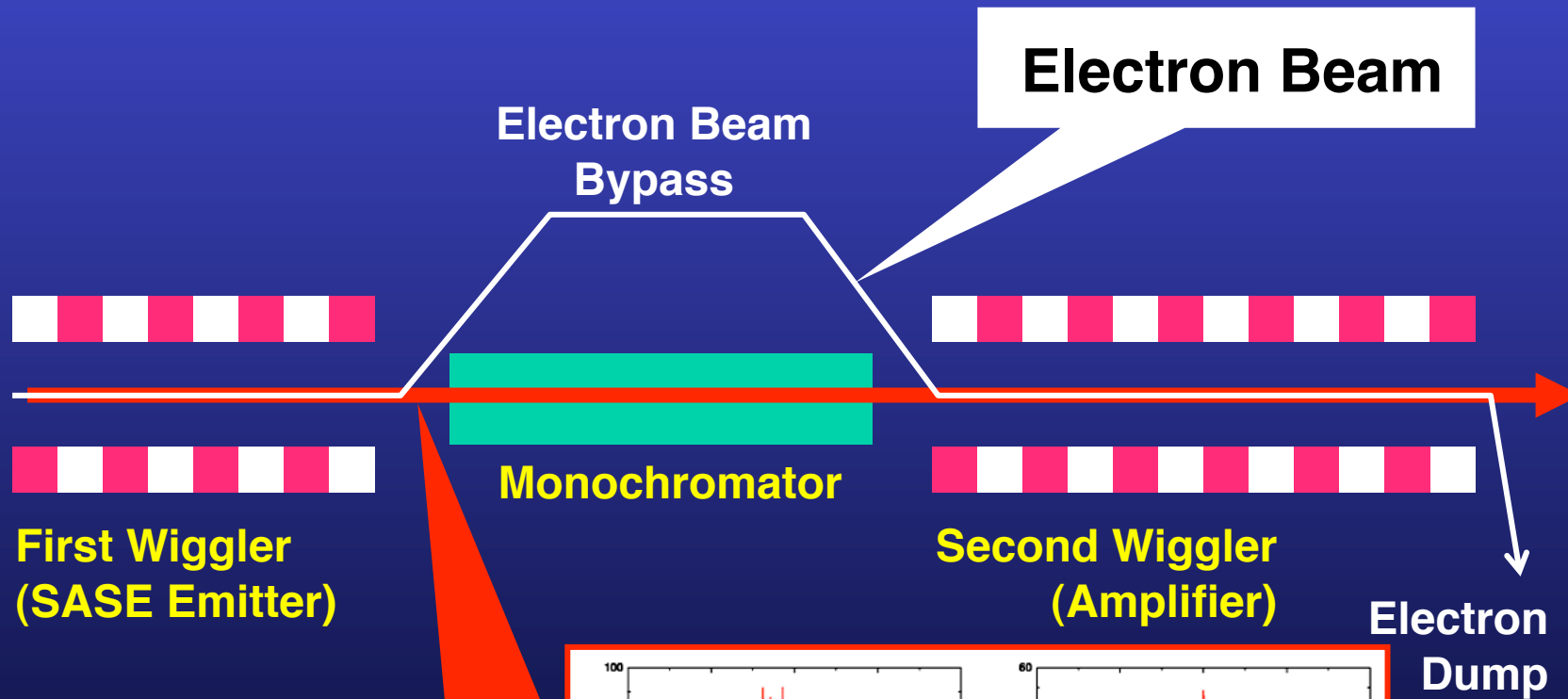
# The right conditions for microbunching:



Specifically, within  $1/2$  of the wiggler period, the electrons shift by  $1/2$  wavelength with respect to the wave, which is just right for microbunching

Microbunching could not occur if the Lorentz forces were not continuously pushing the electrons towards the microbunches. This is made possible by the shift in space between the electrons and the photon wave caused within one wiggler period by the difference between the speed of light  $c$  and that of the electrons,  $u$

# Seeding-Amplifier X-FELs

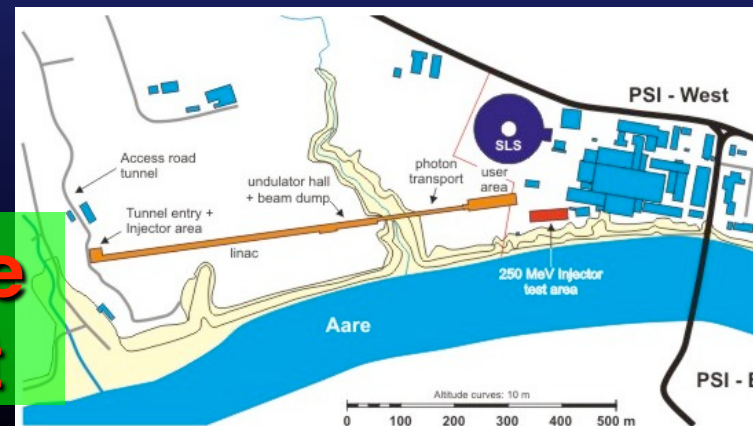


# The FERMI X-FEL at Elettra, Trieste



# The European X-FEL project underway at DESY, Hamburg

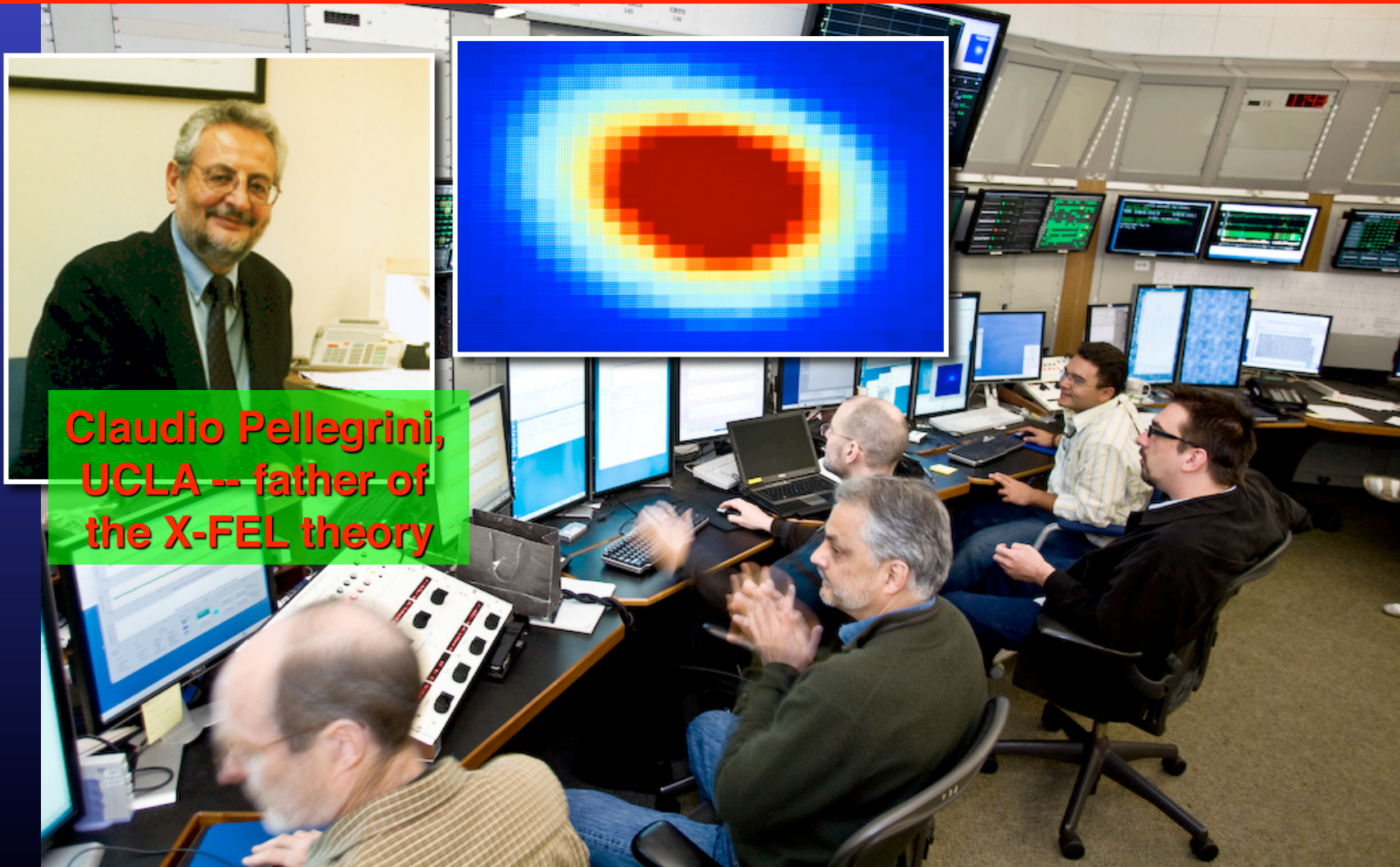
# The Swiss X-FEL at the Paul-Scherrer Institut





## April 21, 2009 - New Era of Research Begins as World's First Hard X-ray Laser Achieves "First Light"

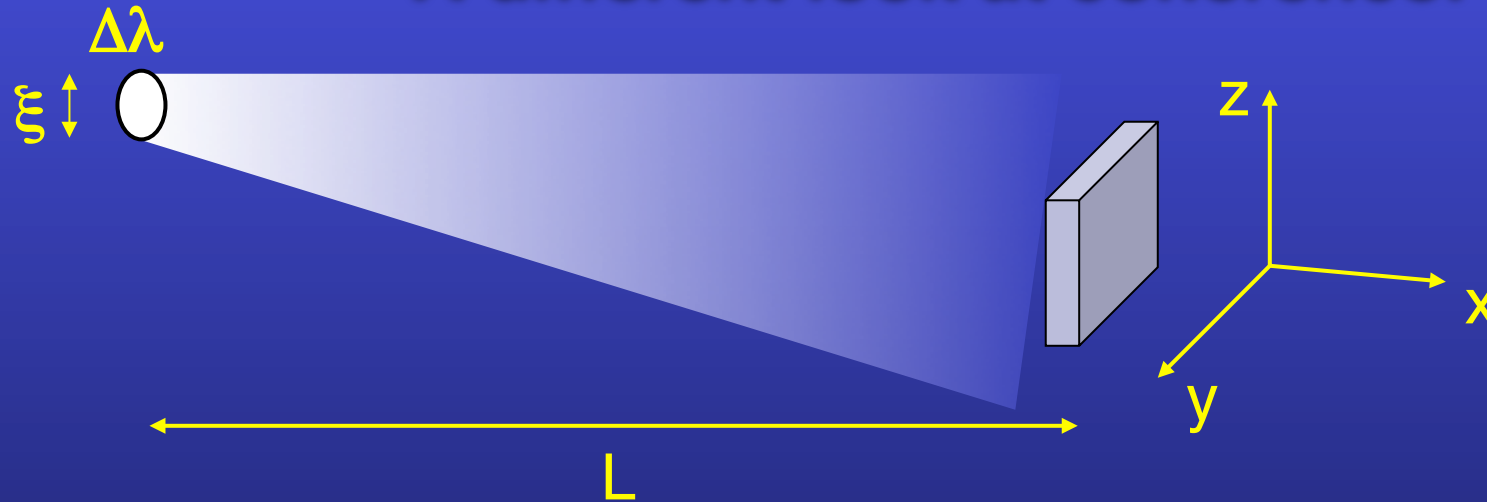
*X-ray laser pulses of unprecedented energy and brilliance produced at SLAC*



**Claudio Pellegrini,  
UCLA -- father of  
the X-FEL theory**



# A different look at coherence:



A source of size  $\xi$  and bandwidth  $\Delta\lambda$  can illuminate coherently a volume  $\Delta x\Delta y\Delta z$ .

Along  $x$ : if two waves of wavelength  $\lambda$  and  $\lambda + \Delta\lambda$  are in phase at a certain time, they will be out of phase after  $\Delta t$  such that  $\Delta\omega\Delta t = 2\pi$  or  $\Delta t = 2\pi/\Delta\omega = \lambda^2/(c\Delta\lambda)$ .

Thus,  $\Delta x = c\Delta t = \lambda^2/\Delta\lambda = L_c$ .

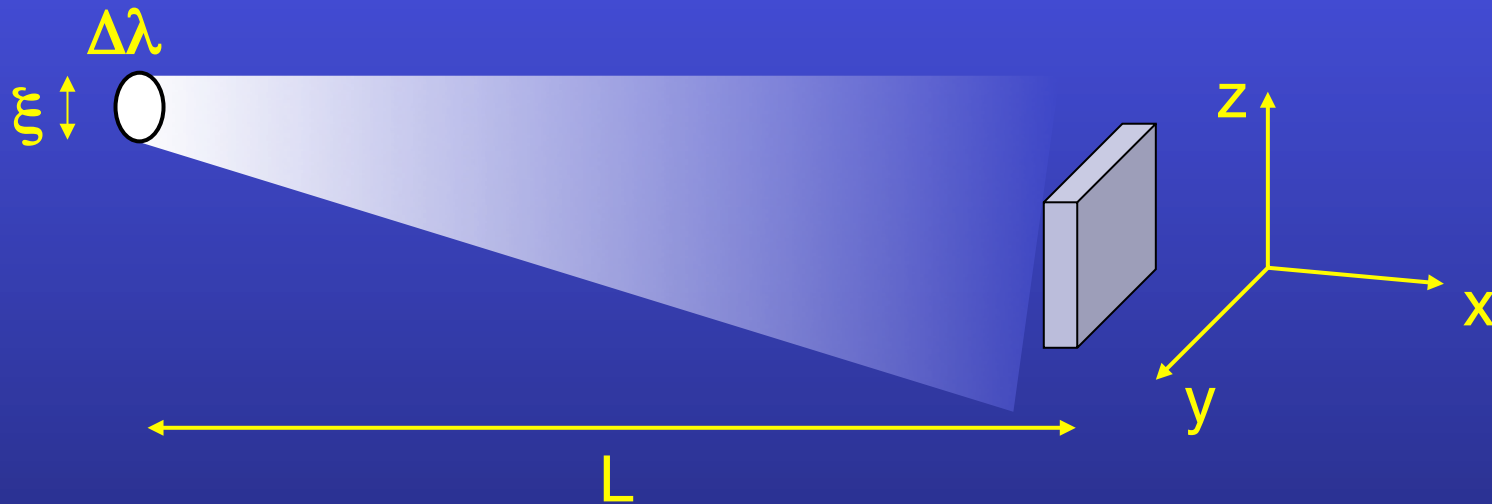
Along  $y$ : the spread in  $k$ -vector is  $\Delta k = k\xi/L = 2\pi\xi/(L\lambda)$ .

If two waves with  $k$ -vectors  $0$  and  $\Delta k$  along  $y$  are in phase at a certain point, they will be out of phase at a distance  $\Delta y$  such that  $\Delta k\Delta y = 2\pi$  or  $\Delta y = L\lambda/\xi$ .

Along  $z$ : same as along  $y$ .

Coherence volume:  $V_c \Delta x\Delta y\Delta z = L^2\lambda^4/(\xi^2\Delta\lambda)$

## Behind all this: Heisenberg!



**Heisenberg:** photons are indistinguishable from each other - and therefore coherent - within a transverse length  $\Delta y$  such that  $\Delta y \Delta p_y = [h/(2\pi)]$ .

But  $\Delta p_y = |p| (\xi/L) = [h/(2\pi\lambda)](\xi/L)$ , thus  $\Delta y = \lambda L/\xi$

Likewise,  $\Delta x$  and  $\Delta z$  can be derived from Heisenberg's principle obtaining the coherence volume  $V_c = \lambda^4 L^2 / (\Delta\lambda \xi^2)$

**Due to the laser action and high brightness, for a SASE-FEL the number of photons in the "coherence volume" is > 9 orders of magnitude larger than for a synchrotron**

What is the number  $n_c$  of photons in the “coherence volume” for a SASE-FEL with full transverse coherence?

Full transverse coherence means that all the emitted photons are within the “coherence volume”. Thus, their number  $n_c$  is given by the flux  $F$  times  $L_c/c = \lambda^2/(c\Delta\lambda)$ .

The brightness  $B$  is proportional to  $F/(\xi\theta)$ ; for full transverse coherence,  $F/(\xi\theta) \approx F/(\lambda^2)$  and  $F$  is proportional to  $\lambda^2 B$ .

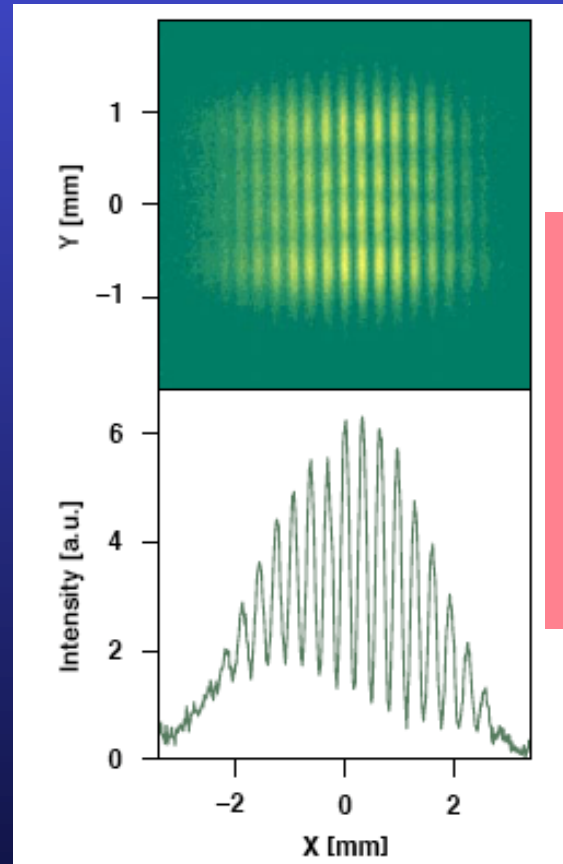
The F-B proportionality factor contains the relative bandwidth  $\Delta\lambda/\lambda$ .

Thus,  $n_c = F\lambda^2/(c\Delta\lambda)$  is proportional to  $(\lambda^2 B)[\lambda^2/(c\Delta\lambda)](\Delta\lambda/\lambda)$ :

**Overall, the number of photons in the “coherence volume” is proportional to  $B\lambda^3$  : high brightness helps, but short wavelengths are a problem!**

# SASE-FEL coherence:

Full lateral (space) coherence all the way to the hard x-rays



First coherence experiments on the Tesla Test Facility: full lateral coherence at  $\lambda = 95$  nm

Longitudinal (time) coherence: determined by the bandwidth/pulse structure -- can be improved, e.g., by seeding

# Thanks:

- The EPFL colleagues (Marco Grioni, Davor Pavuna, Mike Abrecht, Amela Groso, Luca Perfetti, Eva Stefanekova, Slobodan Mitrovic, Dusan Vobornik, Helmuth Berger, Daniel Ariosa, Johanna Generosi, Vinko Gajdosic, Primoz Rebernik).
- The POSTECH colleagues (group of Jung Ho Je).
- The Academia Sinica Taiwan colleagues (group of Yeukuang Hwu).
- The Vanderbilt colleagues (group of Norman Tolk).
- The ISM-Frascati colleagues (group of Antonio Cricenti and Paolo Perfetti)
- The facilities: PAL-Korea, Elettra-Trieste, Vanderbilt FEL, SRRC-Taiwan, APS-Argonne, SLS-Villigen, LURE-Orsay