



**The Abdus Salam
International Centre for Theoretical Physics**



2139-22c

**School on Synchrotron and Free-Electron-Laser Sources and their
Multidisciplinary Applications**

26 April - 7 May, 2010

**Surface, Interface, and Materials Studies Using Photoelectron Spectroscopy,
Diffraction, and Holography
(Part 4)**

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*Lawrence Berkeley National Laboratory
USA*

Outline

Surface, interface, and nanoscience—short introduction

Some surface concepts and techniques→photoemission

Synchrotron radiation: experimental aspects

Electronic structure—a brief review

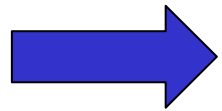
**The basic synchrotron radiation techniques:
more experimental and theoretical details**

 **Valence-level photoemission**

Core-level photoemission

**Photoemission with high ambient pressure
around the sample**

Outline



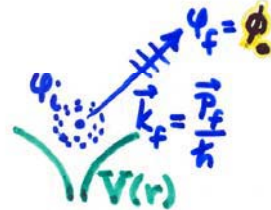
- Valence-band spectra: low-energy UPS limit and high-energy XPS limit
- Core-level chemical shifts: the potential model
- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
- Multiplet splittings
- Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons
- Magnetic circular dichroism (MCD) in core-level emission
- Non-magnetic circular dichroism in core-level emission: a.k.a. circular dichroism in angular distributions (CDAD)
- Various other final state effects providing information in core-level spectra

PHOTOELECTRON EMISSION-

BASIC MATRIX ELEMENTS + SELECTION RULES:

- ATOMIC-LIKE (LOCALIZED) STATES \Rightarrow CORE:

$$\psi_i(\vec{r}) = \psi_{n_i, l_i, m_i}(r, \theta, \phi) = R_{n_i, l_i}(r) Y_{l_i, m_i}(\theta, \phi)$$



$$\psi_f(\vec{r}, \vec{k}_f) = \psi_{E_f}(\vec{r}, \vec{k}_f)$$

$$= 4\pi \sum_{l_f, m_f} i^{l_f} e^{-i\delta_{l_f}} Y_{l_f, m_f}^*(\theta, \phi) Y_{l_i, m_i}(\theta, \phi) R_{E_f, l_f}(r)$$

PHASE SHIFT OF l_f WAVE IN $V(r)$

DIPOLE: INT. $\propto |\langle \psi_f | \hat{E} \cdot \vec{r} | \psi_i \rangle|^2 = |\hat{E} \cdot \langle \psi_f | \vec{r} | \psi_i \rangle|^2$

EQUIVALENT WITHIN CONSTANT FACTOR



- $\Delta l = l_f - l_i = \pm 1$
TWO CHANNELS
- $\Delta m = m_f - m_i = 0, \pm 1$
LINEAR POLARIZ.
- $\Delta m = \pm 1$, CIRCULAR POLARIZATION

VALENCE BANDS IN SOLIDS:

- BLOCH-FUNCTION (DELOCALIZED) STATES \Rightarrow VALENCE:

$$\psi_i(\vec{r}) = u_{\vec{k}_i}(\vec{r}) e^{i\vec{k}_i \cdot \vec{r}}$$

$$\psi_f(\vec{r}) = u_{\vec{k}_f}(\vec{r}) e^{i\vec{k}_f \cdot \vec{r}}; E_f = \frac{p_f^2}{2m} = \frac{\hbar^2 k_f^2}{2m}$$

USUALLY NEGLIG.



$$|\langle \psi_f | \hat{E} \cdot \vec{p} | \psi_i \rangle|^2 = |\hat{E} \cdot \langle \psi_f | \vec{p} | \psi_i \rangle|^2 \Rightarrow \Delta \vec{k} = \vec{k}_f - \vec{k}_i = \vec{k}_{ph} + \vec{k}_{phonon}$$

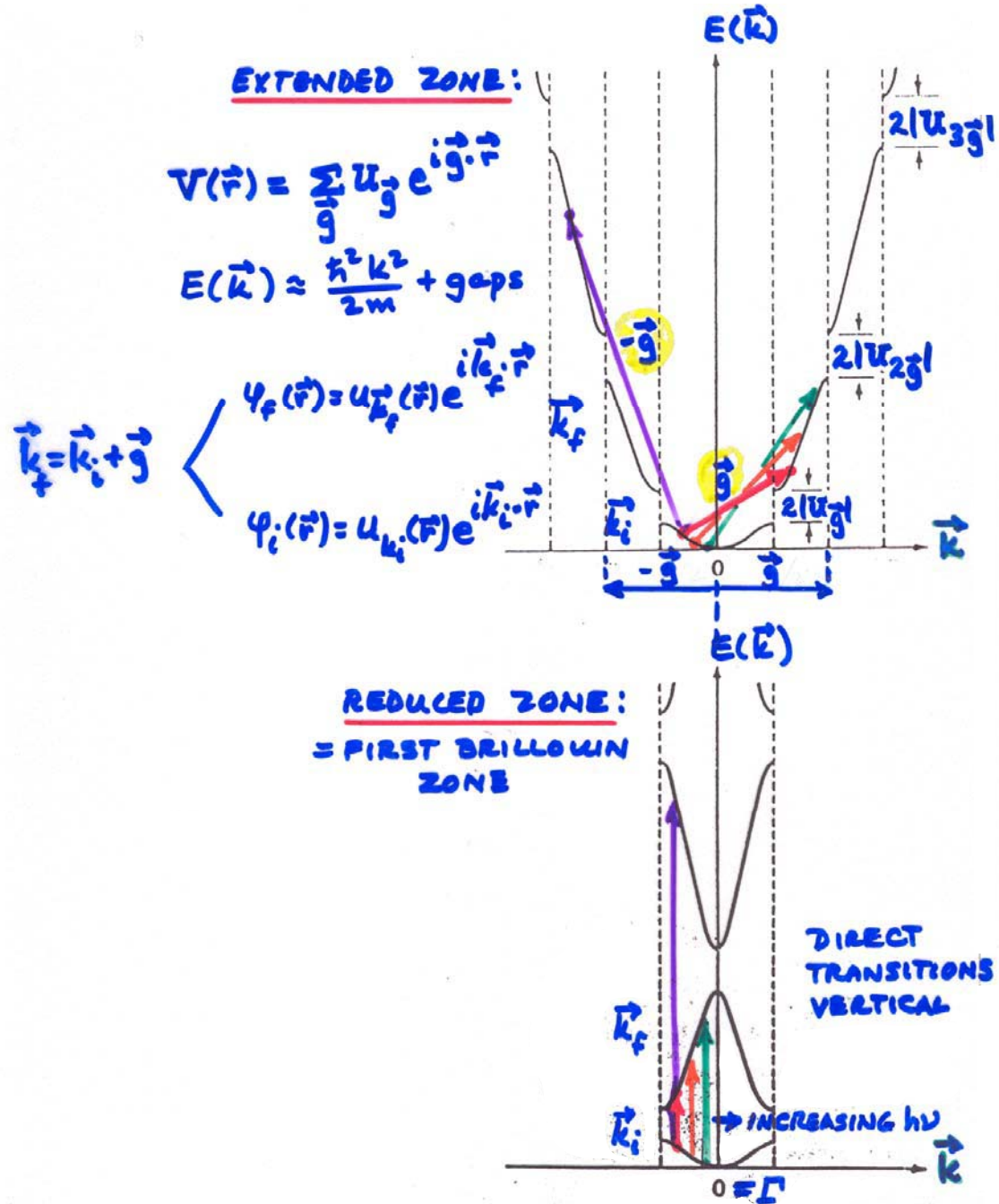
$$= \vec{g}_{BULK} \text{ (or } \vec{g}_{SURF})$$

"DIRECT" TRANSITIONS

BUT LATTICE VIBRATIONS \Rightarrow SUM OVER \vec{k}_{PHONON}

\Rightarrow FRACTION DIRECT \approx DEBYE-WALLER FACTOR $= \exp[-g^2 \bar{u}^2]$

NEARLY-FREE ELECTRONS IN A WEAK PERIODIC POTENTIAL—1 DIM.

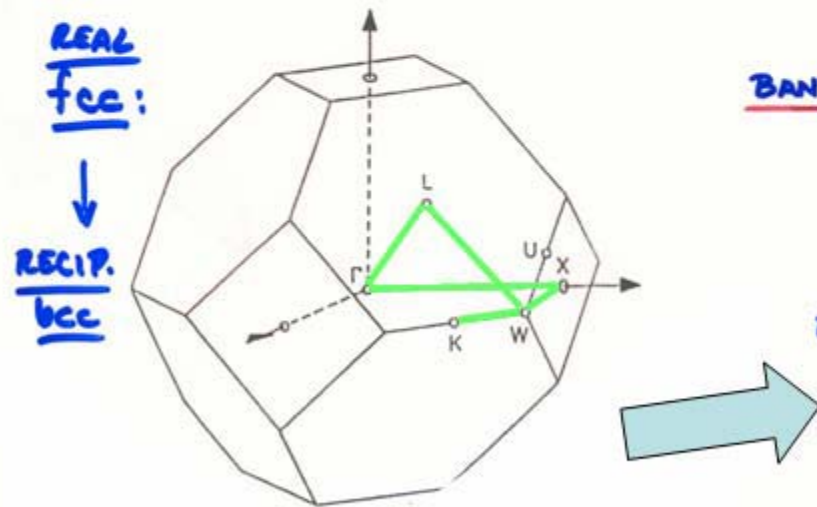


The electronic structure of a nearly free-electron metal—fcc Al

$$\phi(\vec{r}) = u_{\vec{k}}(\vec{r}) e^{i\vec{k}\cdot\vec{r}}; E(\vec{k}) \approx \frac{\hbar^2 k^2}{2m}$$

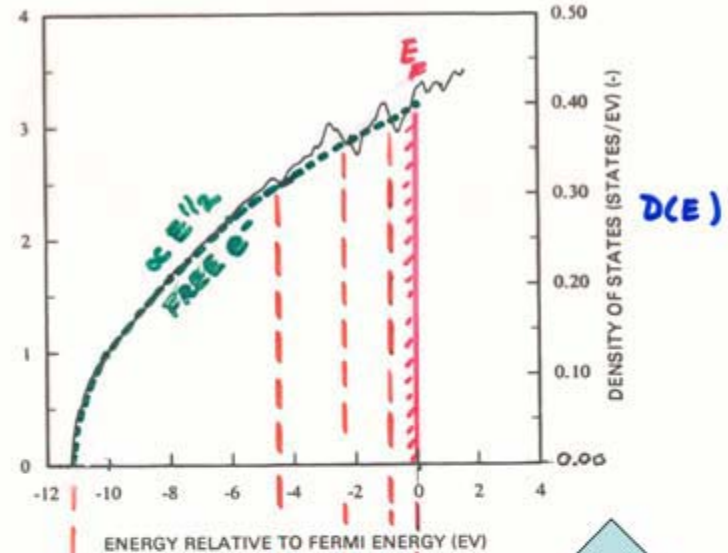
(Bloch)

3D Brillouin zone

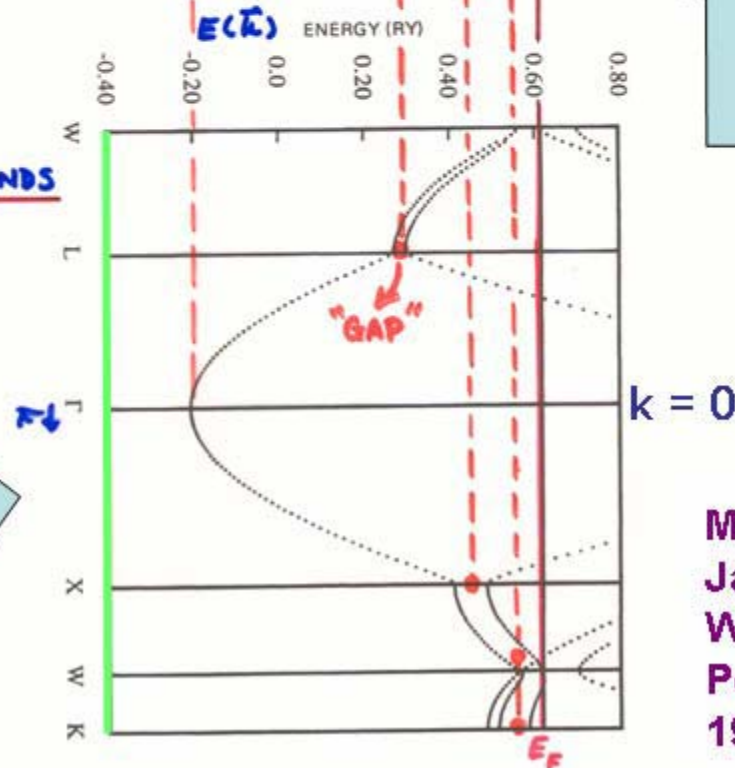


ALUMINUM - ELECTRONIC BANDS & D.O.S.

D.O.S.

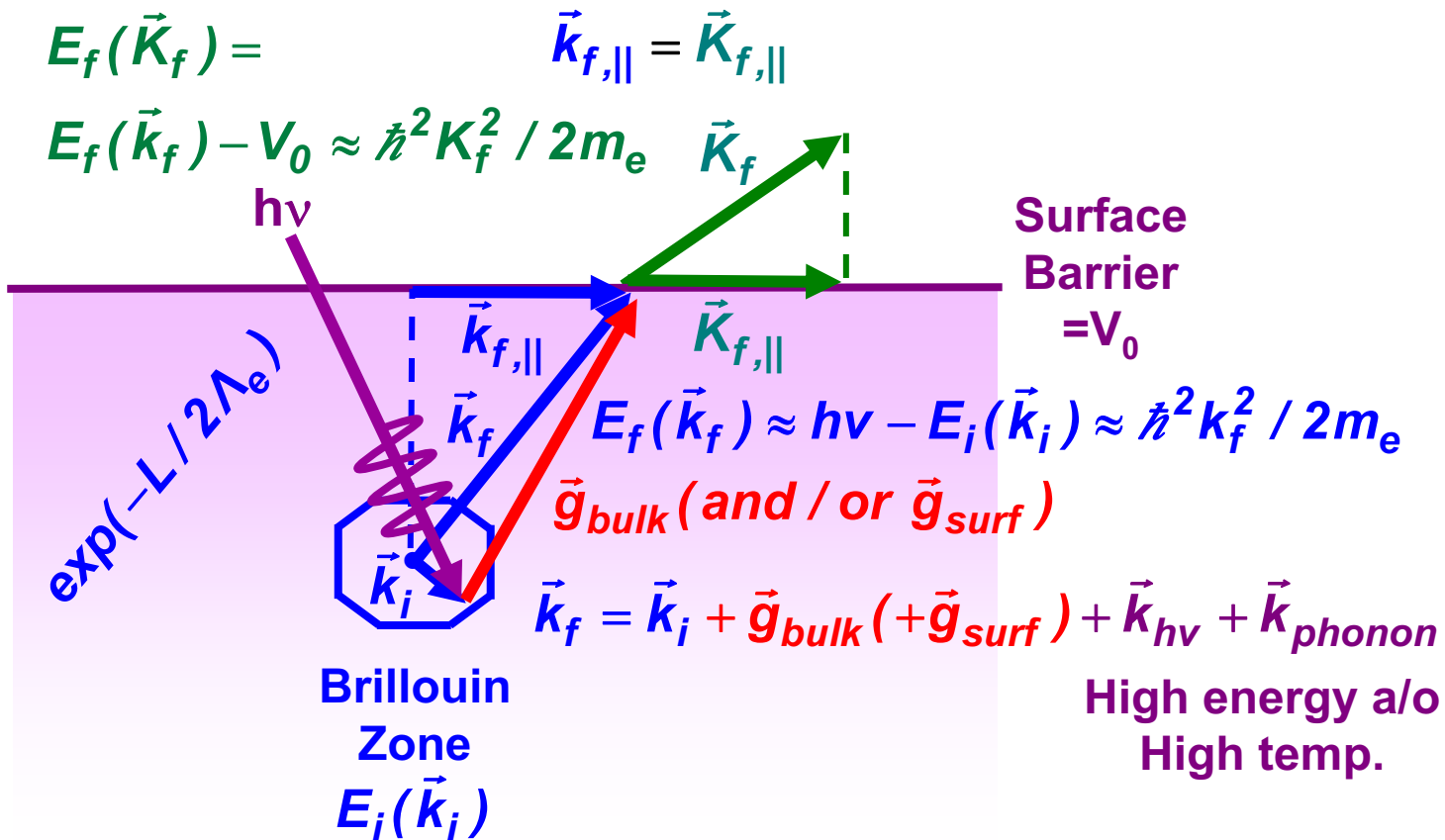


BANDS



Moruzzi,
Janak,
Williams,
Pergamon,
1978

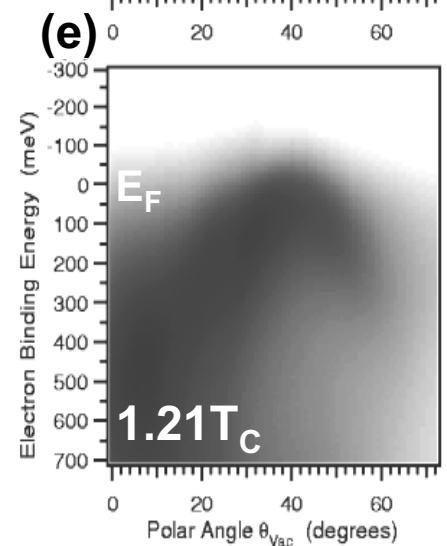
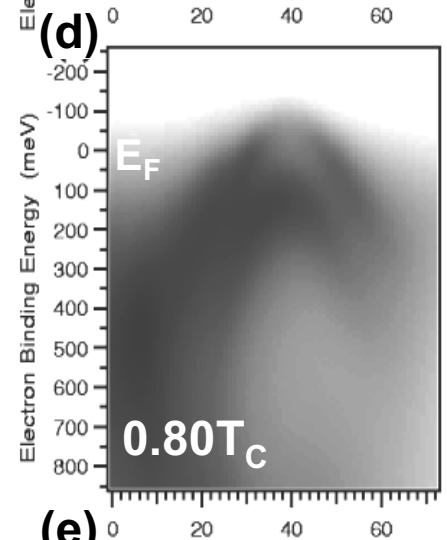
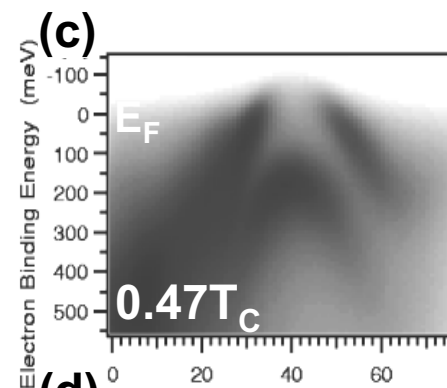
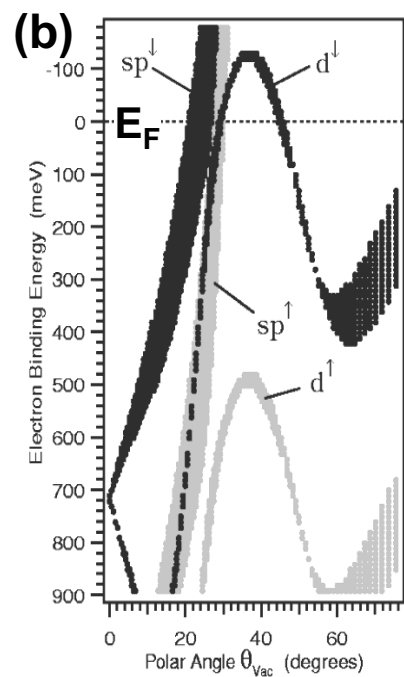
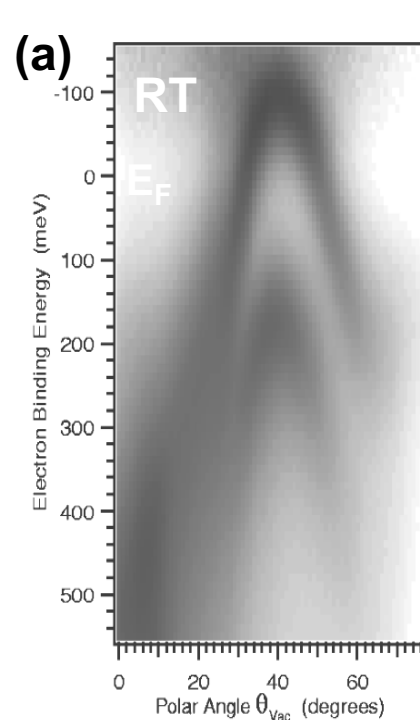
Valence-band photoemission: Angle-Resolved Photoemission (ARPES)



$$I(E_f, \vec{k}_f) \propto \left| \hat{\epsilon} \cdot \left\langle \psi_{photoe}(E_f = h\nu + E_i, \vec{k}_f = \vec{k}_i + \vec{g}) \middle| \vec{r} \middle| \psi(E_i, \vec{k}_i) \right\rangle \right|^2$$

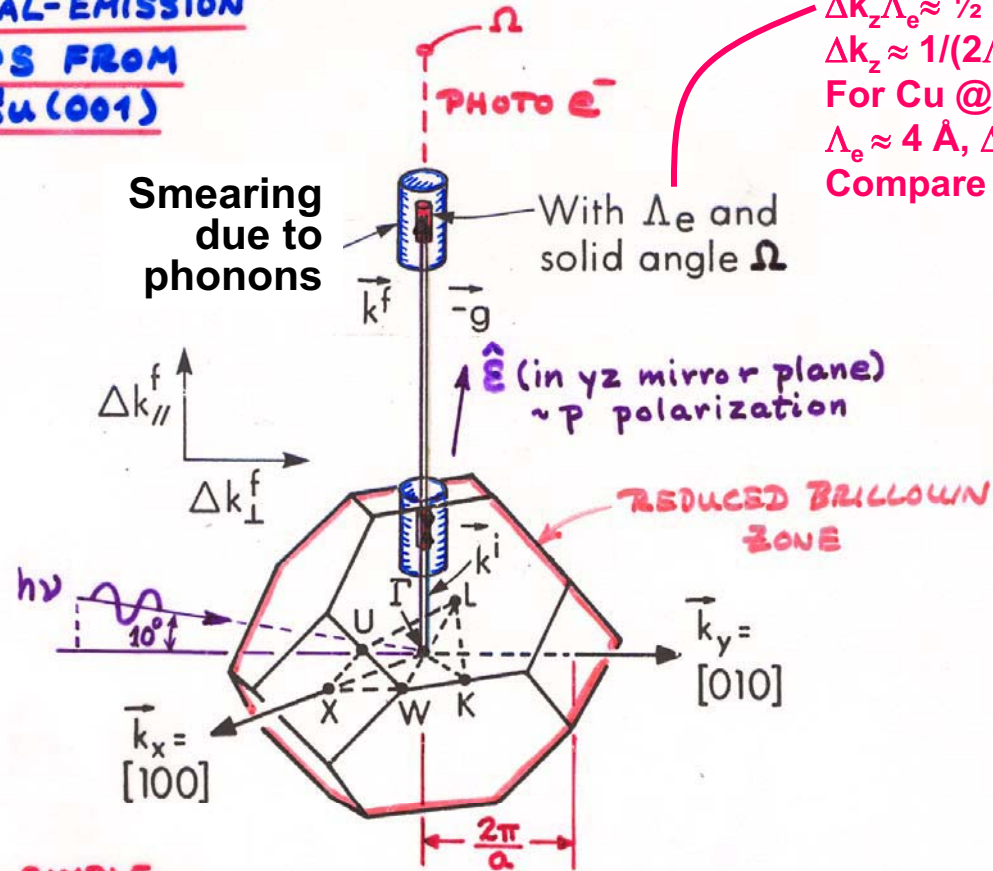
“Direct” or k-conserving transitions

**Angle-Resolved
Photoemission
from ferromagnetic
Ni(111)
 $h\nu = 21.2$ eV
Spin-split
bands**



Kreutz et al.,
Phys. Rev. B 58 (1998) 1300

EXAMPLE:
NORMAL-EMISSION
UPS FROM
Cu(001)



$\Delta p_z \Delta z \approx \hbar / 2$
 $\Delta k_z \Lambda_e \approx 1/2$
 $\Delta k_z \approx 1/(2\Lambda_e)$
 For Cu @ $E_{kin} \approx 80$ eV,
 $\Lambda_e \approx 4 \text{ \AA}$, $\Delta k_z \approx 0.12 \text{ \AA}^{-1}$
 Compare $2\pi/a = 0.98 \text{ \AA}^{-1}$

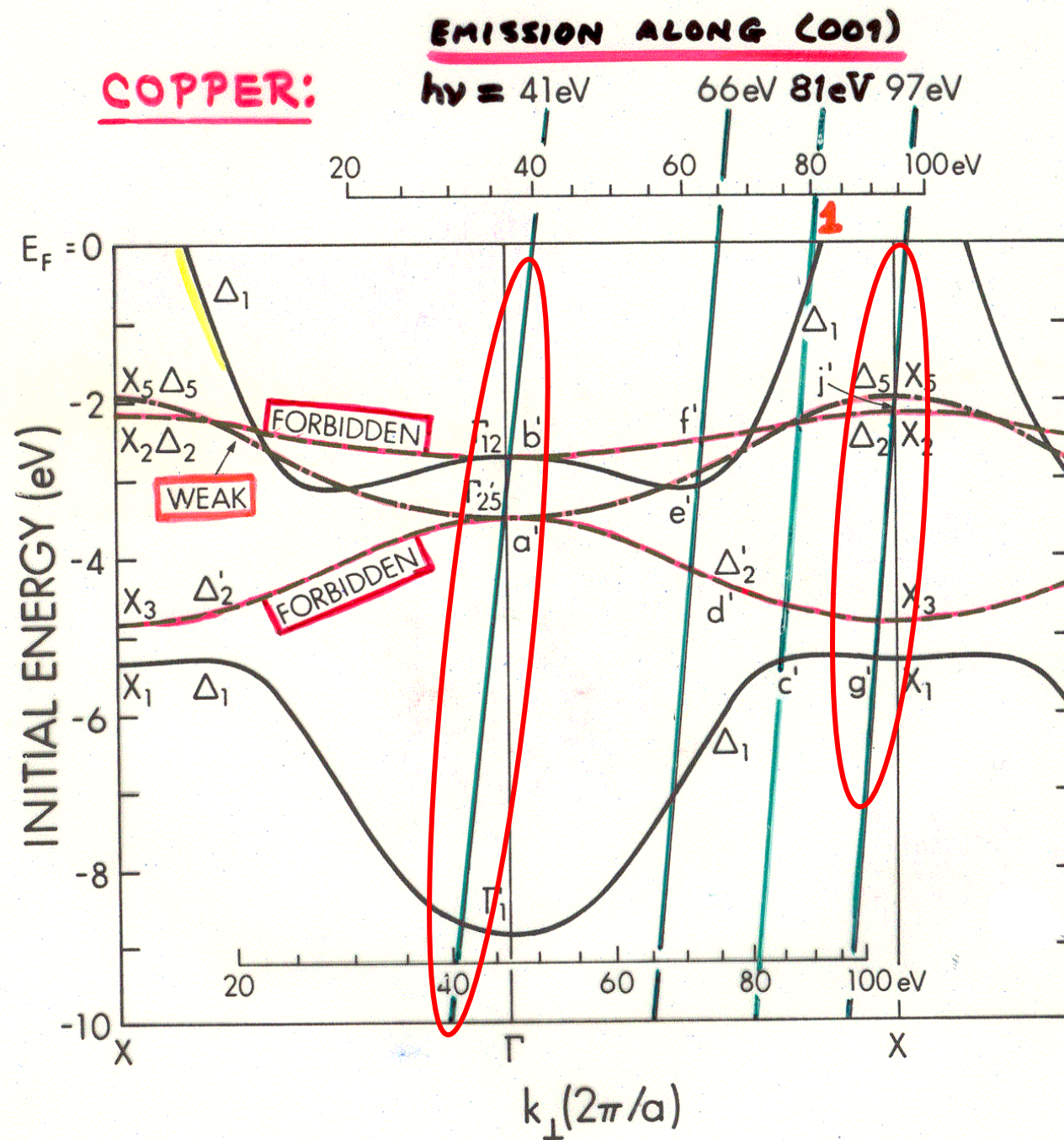
SIMPLE DT MODEL: Direct: $\vec{k}^f = \vec{k}^i + \vec{g} + \vec{k}_{hv}$

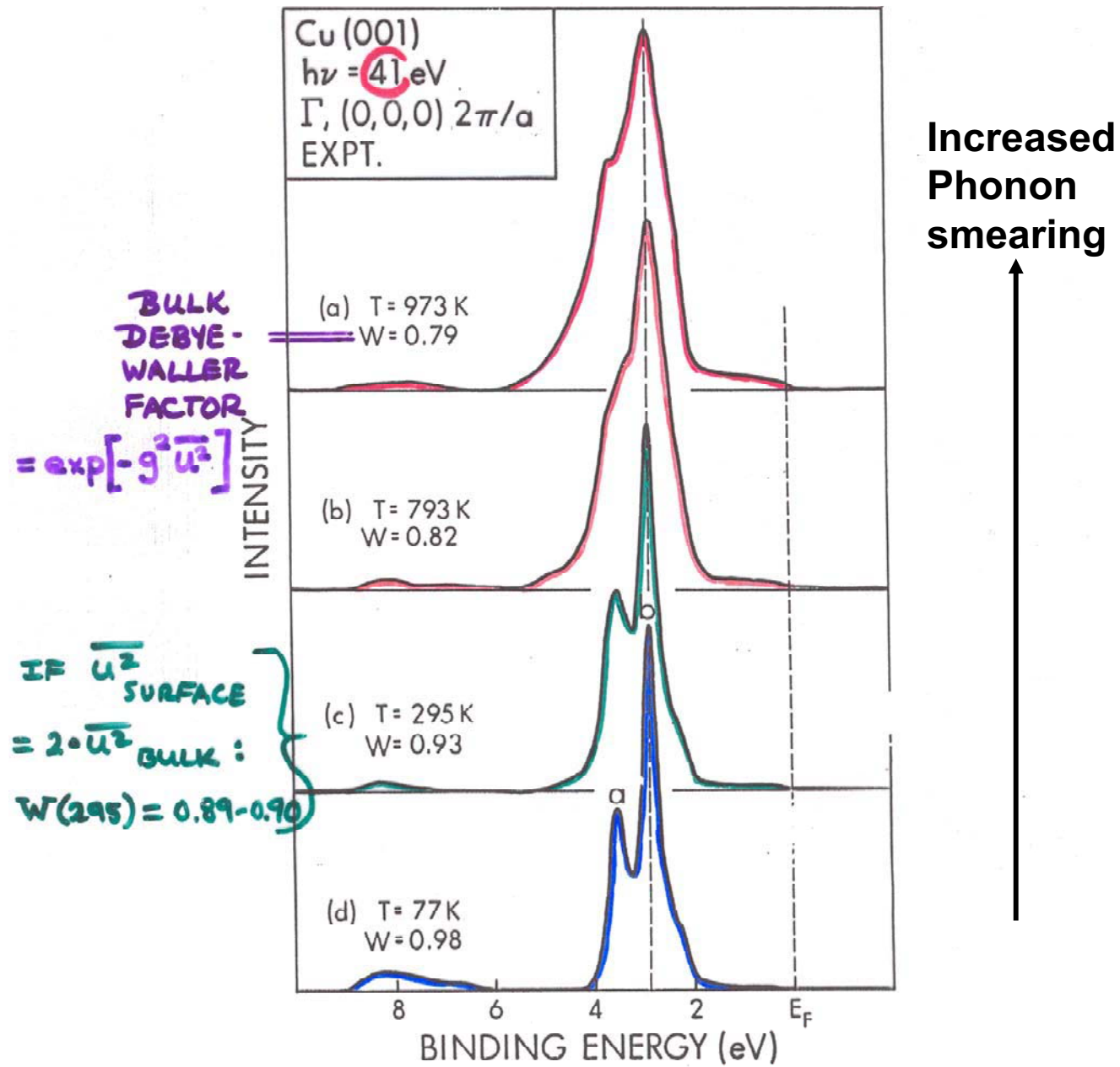
$E^i(\vec{k}^i)$ = initial band structure

$E^f(\vec{k}^f) \approx \hbar^2 (k^f)^2 / 2m$

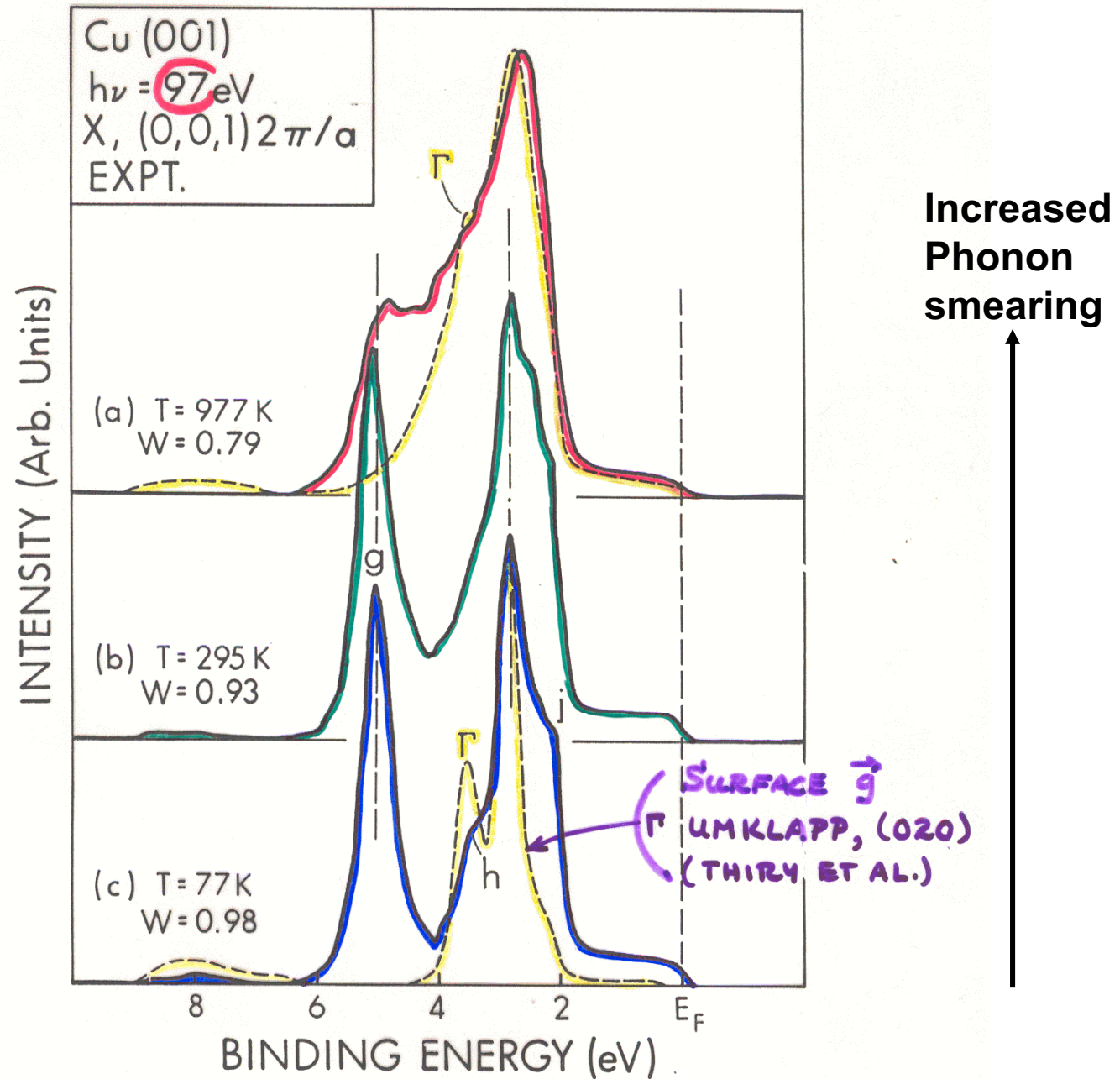
Constant matrix elements

Expectations
 from simple
 direct-
 transition
 theory
 + symmetry
 considerations
 in matrix
 elements

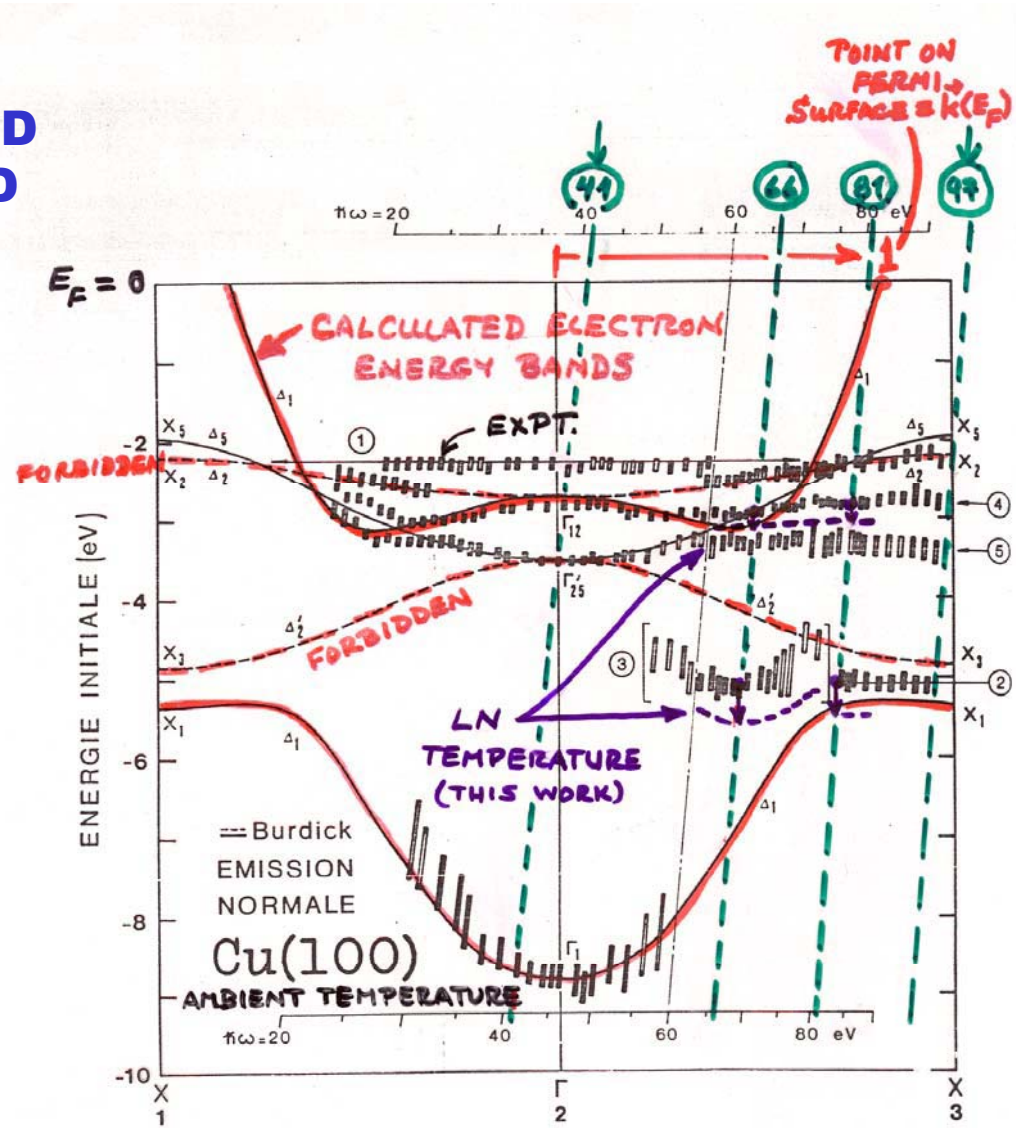




R.C. WHITE ET AL., PHYS. REV. B 35, 1147 (1987)



Cu: ANGLE-RESOLVED PHOTOEMISSION AND BAND-MAPPING ALONG (001)



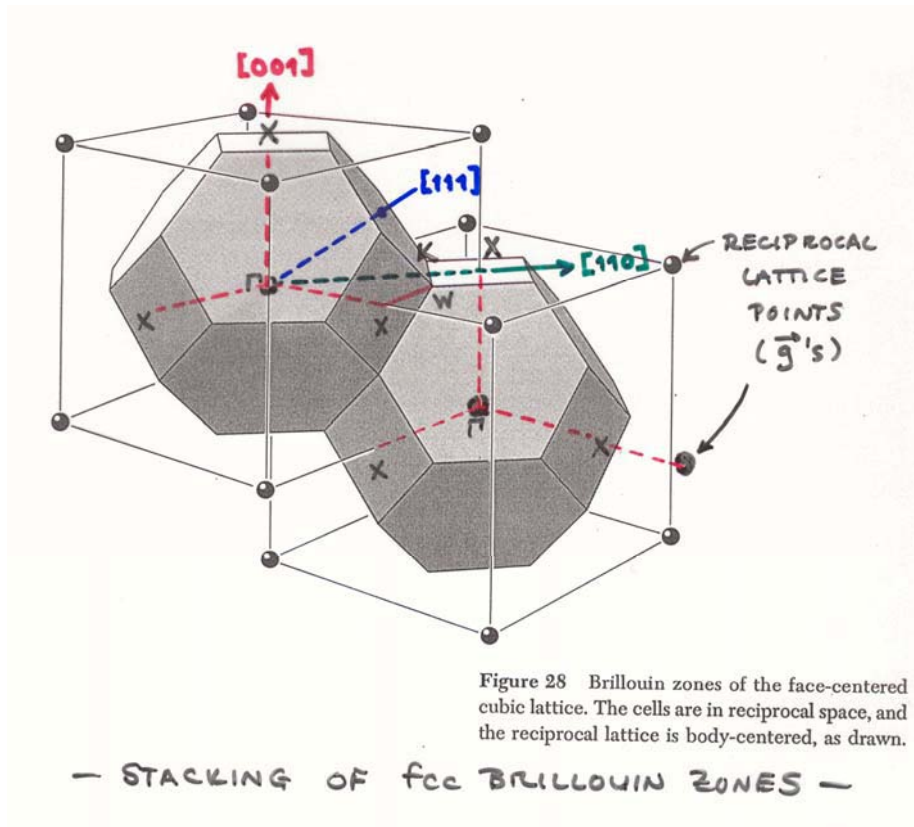
$$k_{\perp} (2\pi/a)$$

P. THIRY, THESIS, UNIV. OF PARIS (1980)

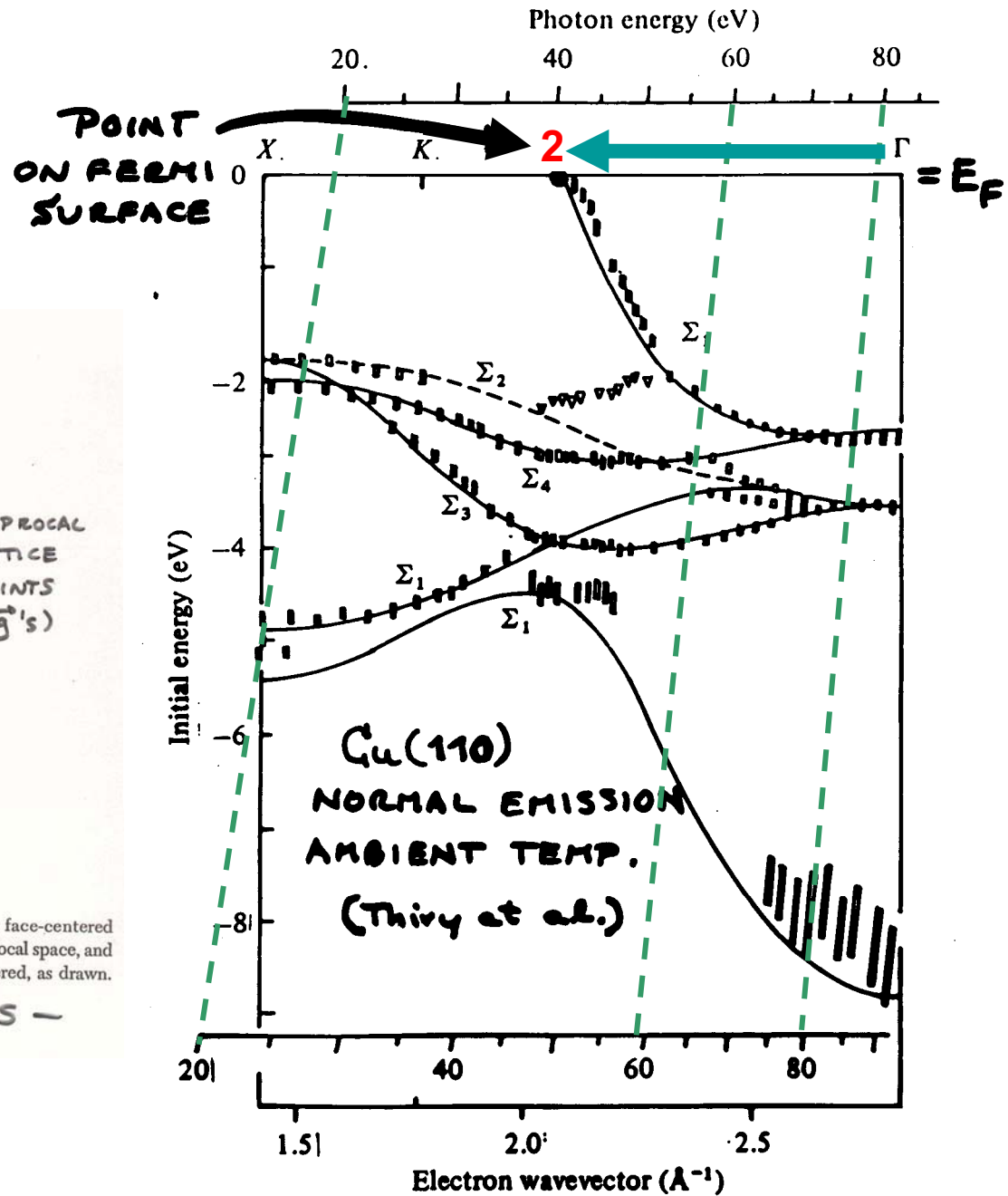
+ WHITE ET AL. P.R. 835,1147 (1987)

FIG.56

Cu: ANGLE-RESOLVED PHOTOEMISSION AND BAND-MAPPING ALONG (110)



P.Thiry, Ph.D. thesis, Univ. of Paris (1980)



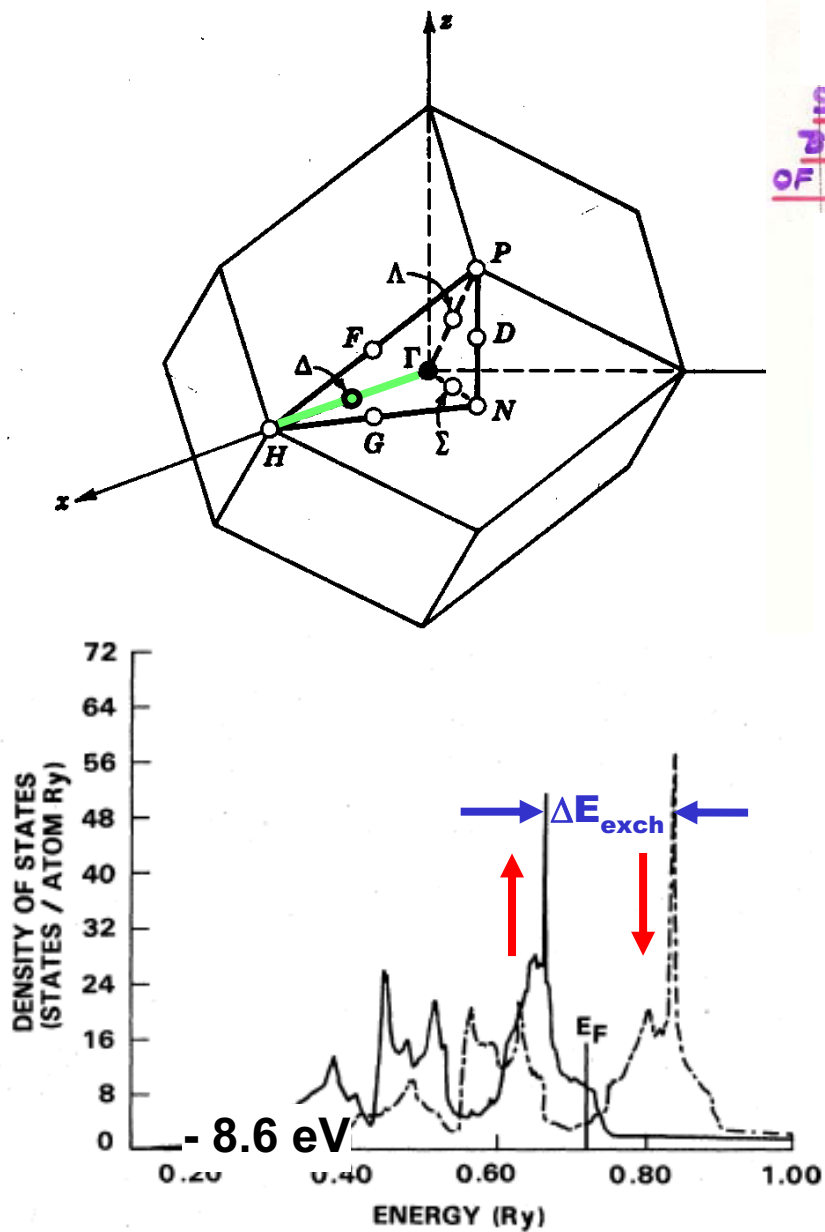
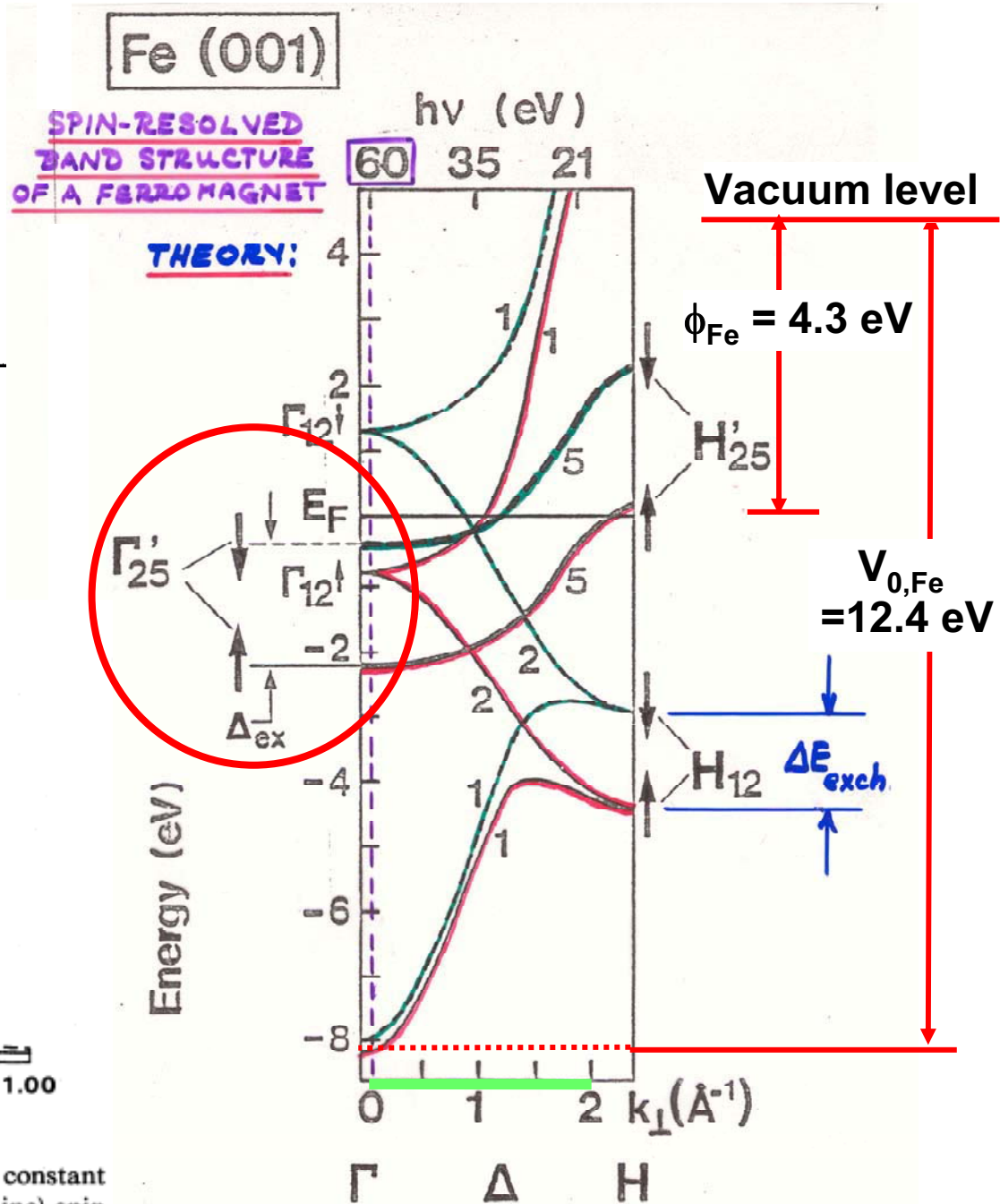


FIG. 4. Density of states at the equilibrium lattice constant of Fe for majority- (solid line) and minority- (broken line) spin states.

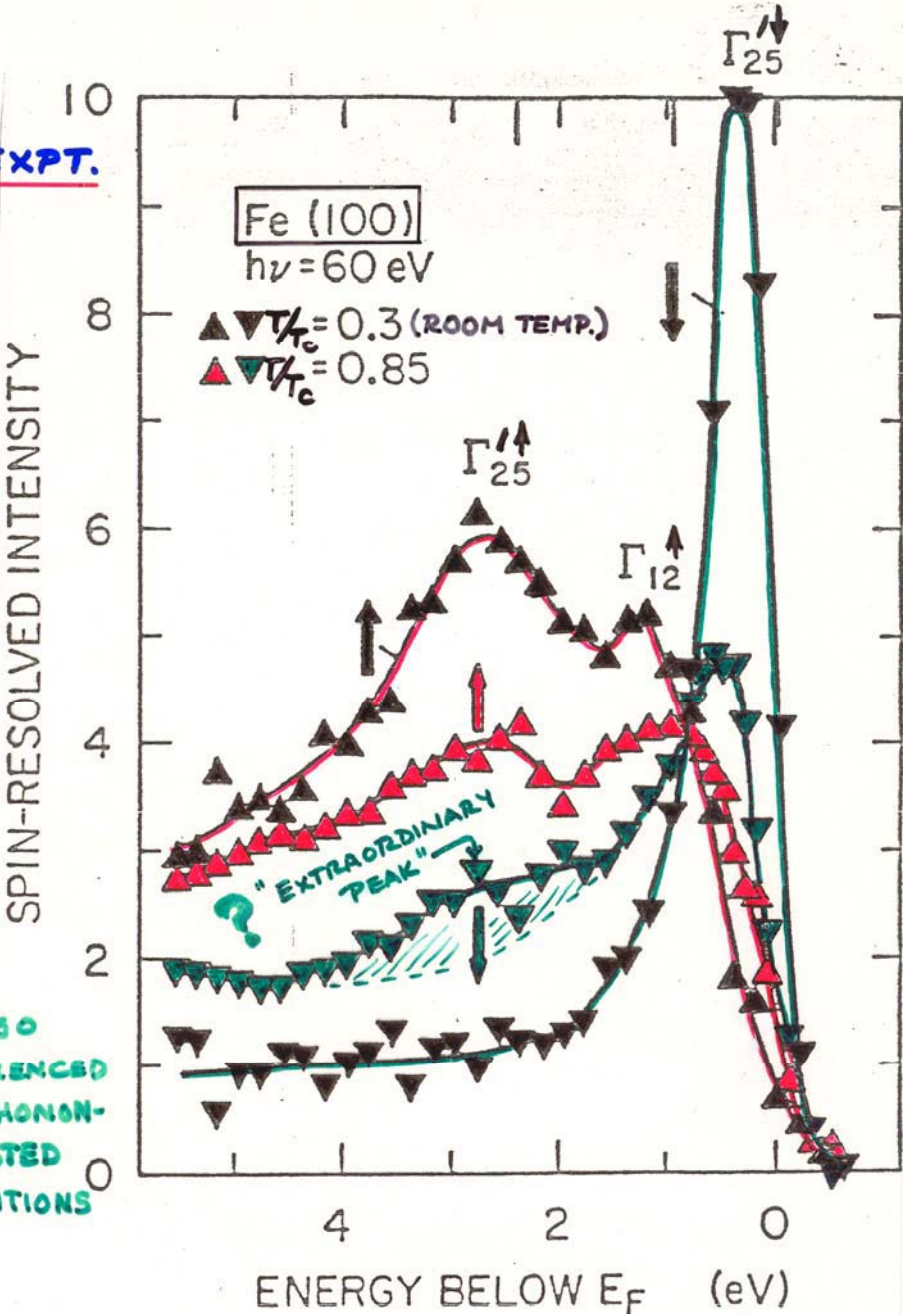
Hathaway et al., Phys. Rev. B 31, 7603 ('85)



E. KISKER ET AL., PHYS. REV. B
31, 329 (1985)

Fe: ANGLE AND SPIN-RESOLVED SPECTRA AT Γ POINT

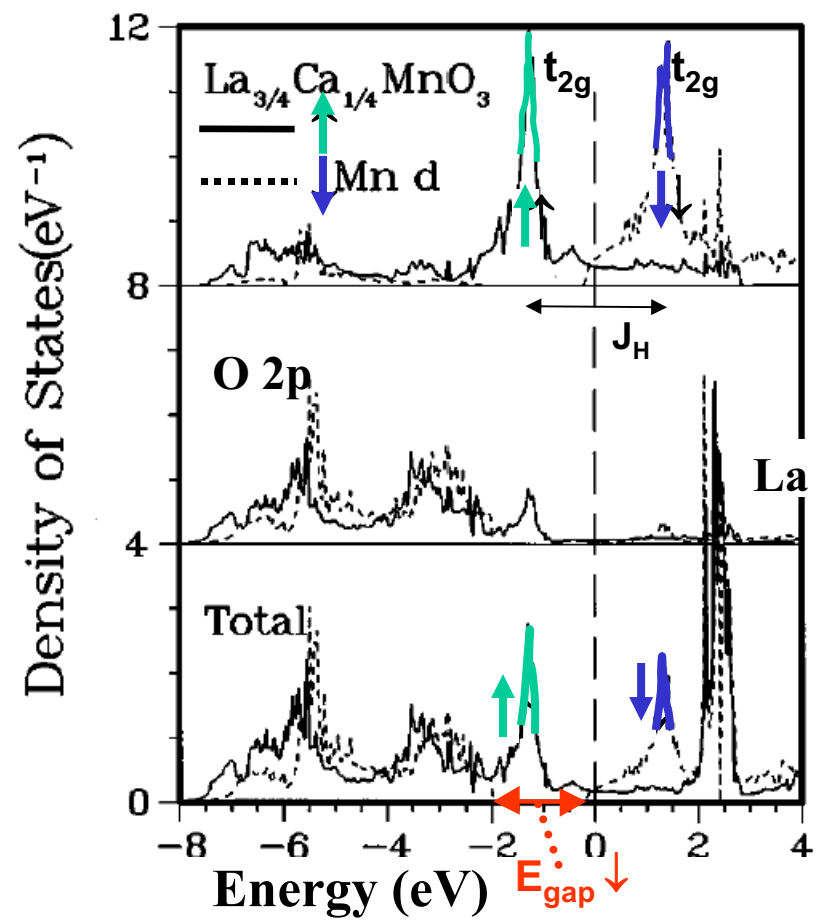
EXPT.



E. KISKER ET AL., PHYS. REV. B 31, 329 (1985)

Half-Metallic Ferromagnetism

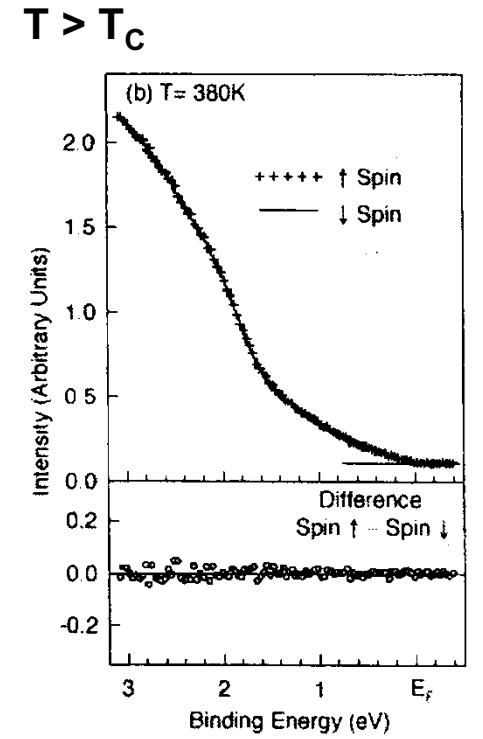
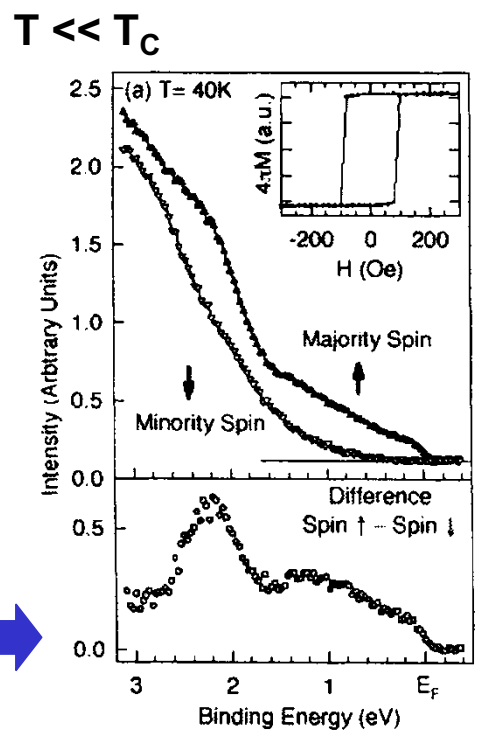
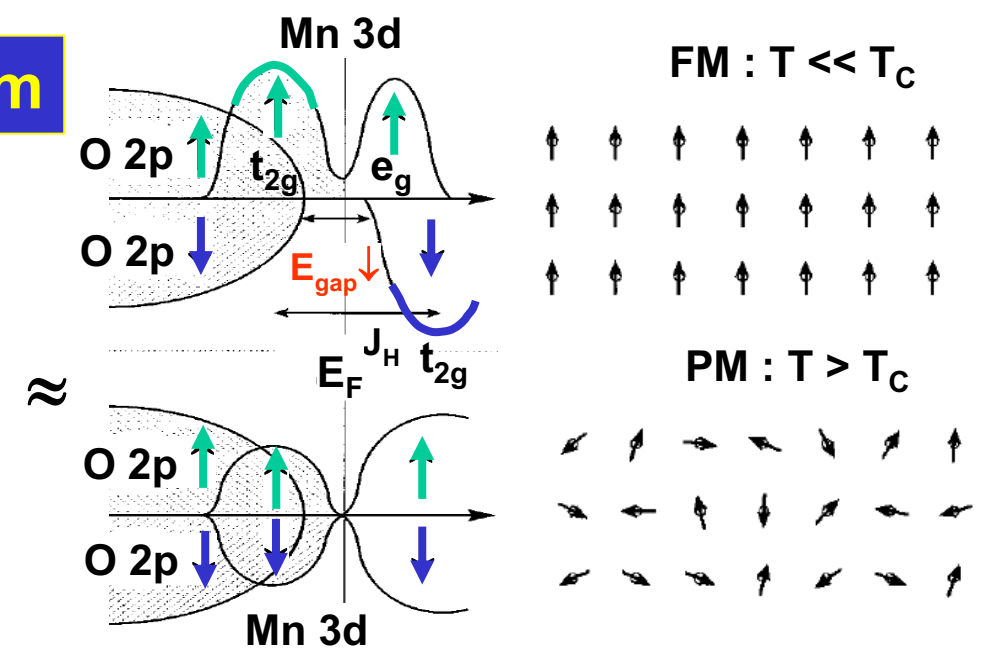
LDA theory- FM $\text{La}_{0.75}\text{Ca}_{0.25}\text{MnO}_3$



Pickett and Singh, PRB 53, 1146 (1996)

Experiment- spin-resolved PS $\text{La}_{0.70}\text{Sr}_{0.30}\text{MnO}_3$ as thin film

Park et al., Nature, PRB 392, 794 (1998)



Vacuum level

The electronic structure of a transition metal—fcc Cu

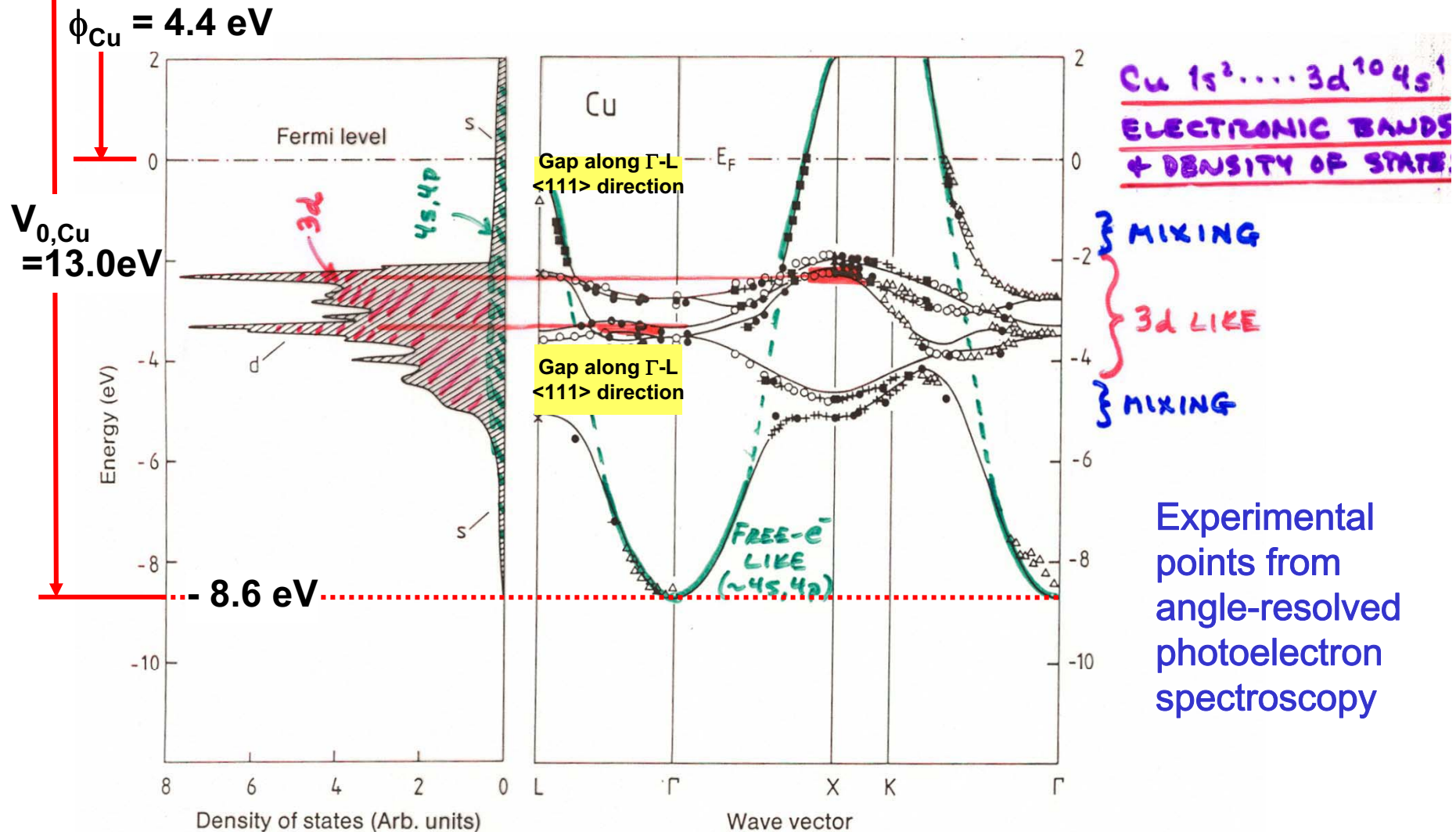


Fig. 7.12. Bandstructure $E(k)$ for copper along directions of high crystal symmetry (right). The experimental data were measured by various authors and were presented collectively by Courths and Hufner [7.4]. The full lines showing the calculated energy bands and the density of states (left) are from [7.5]. The experimental data agree very well, not only among themselves, but also with the calculation

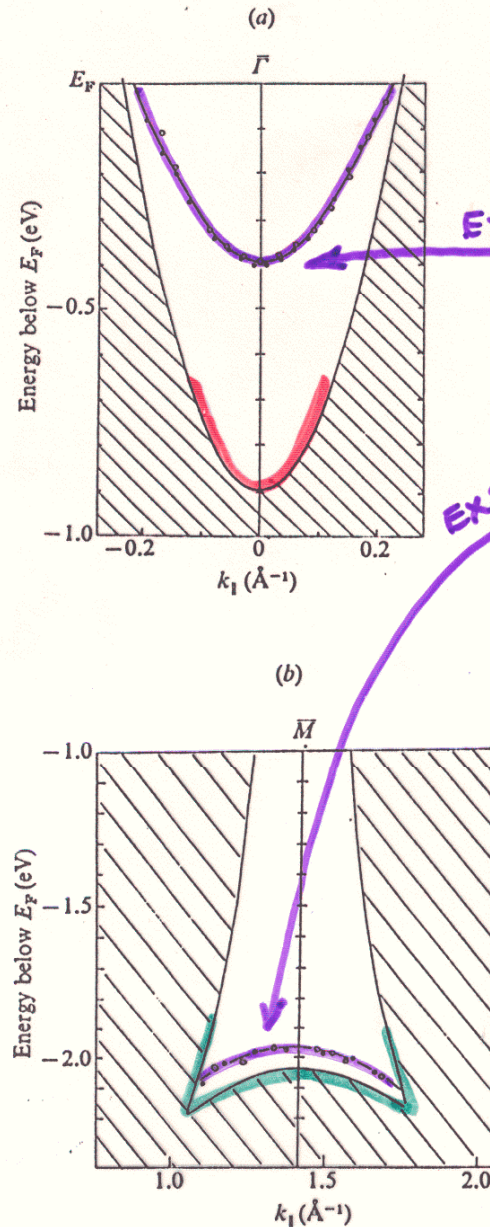
Surface states on Cu(111)

Fig. 4.21. Experimental dispersion of Cu(111) surface states plotted with a projection of the bulk bands: (a) Shockley state near the zone center (Γ); (b) Tamm state near the zone boundary (\bar{M}). Compare with Fig. 4.17.

Shockley surface state

Tamm surface state

Zangwill, Surface Physics,



THEORY

Fig. 4.17. Surface states (dashed curves) and bulk projected bands of Cu(111) surface according to a six-layer surface band structure calculation (Euceda, Bylander & Kleinman, 1983).

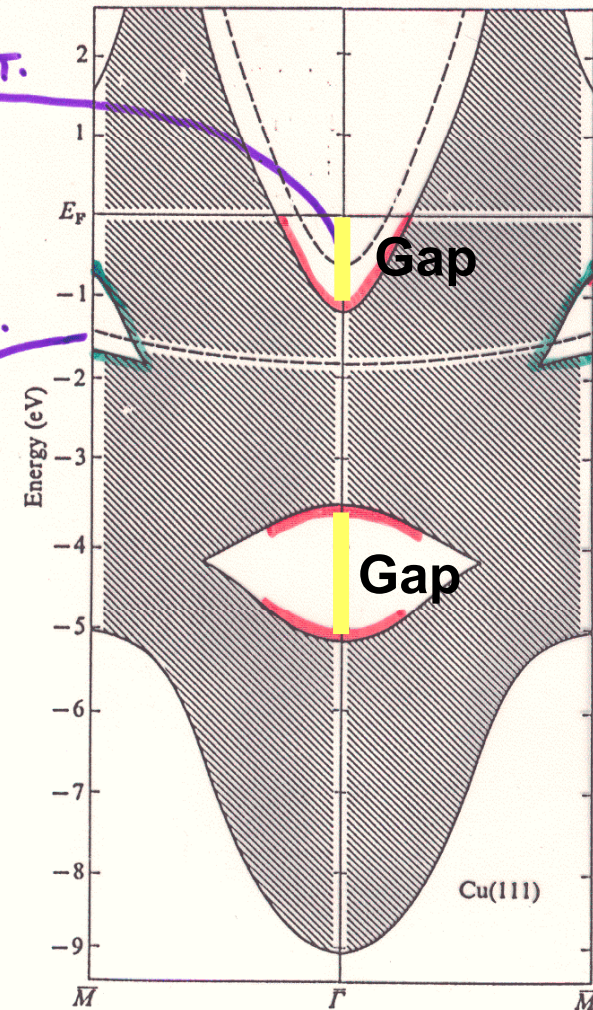
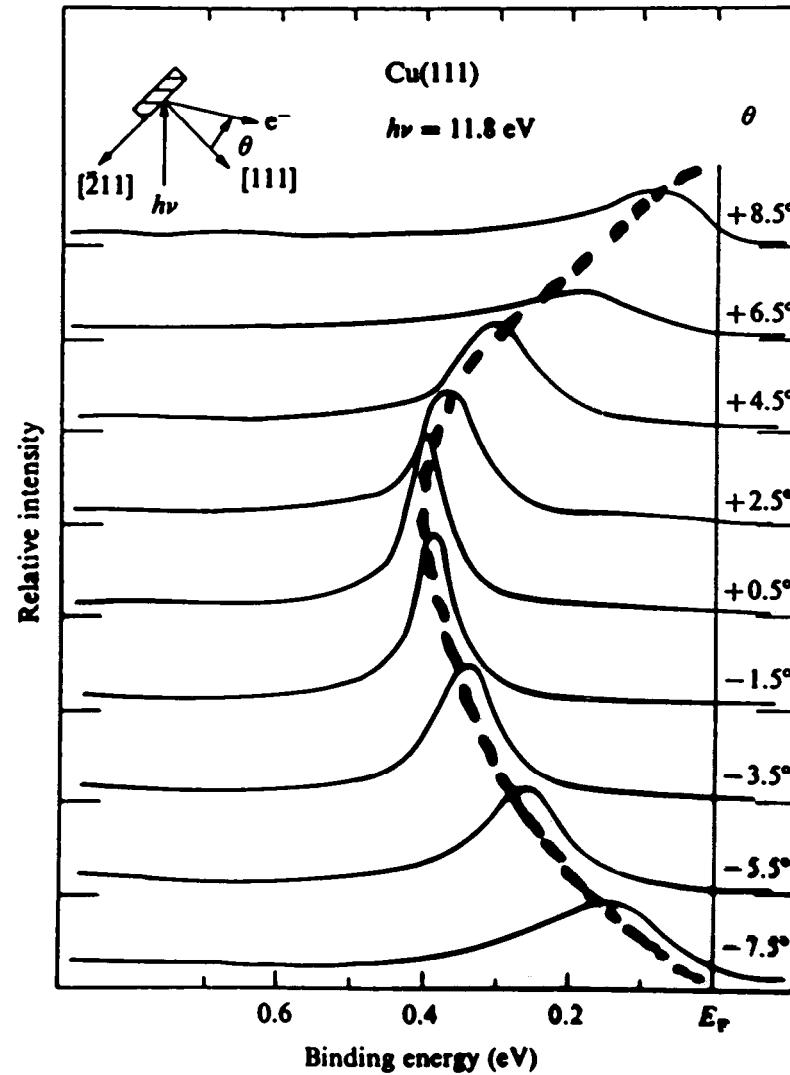
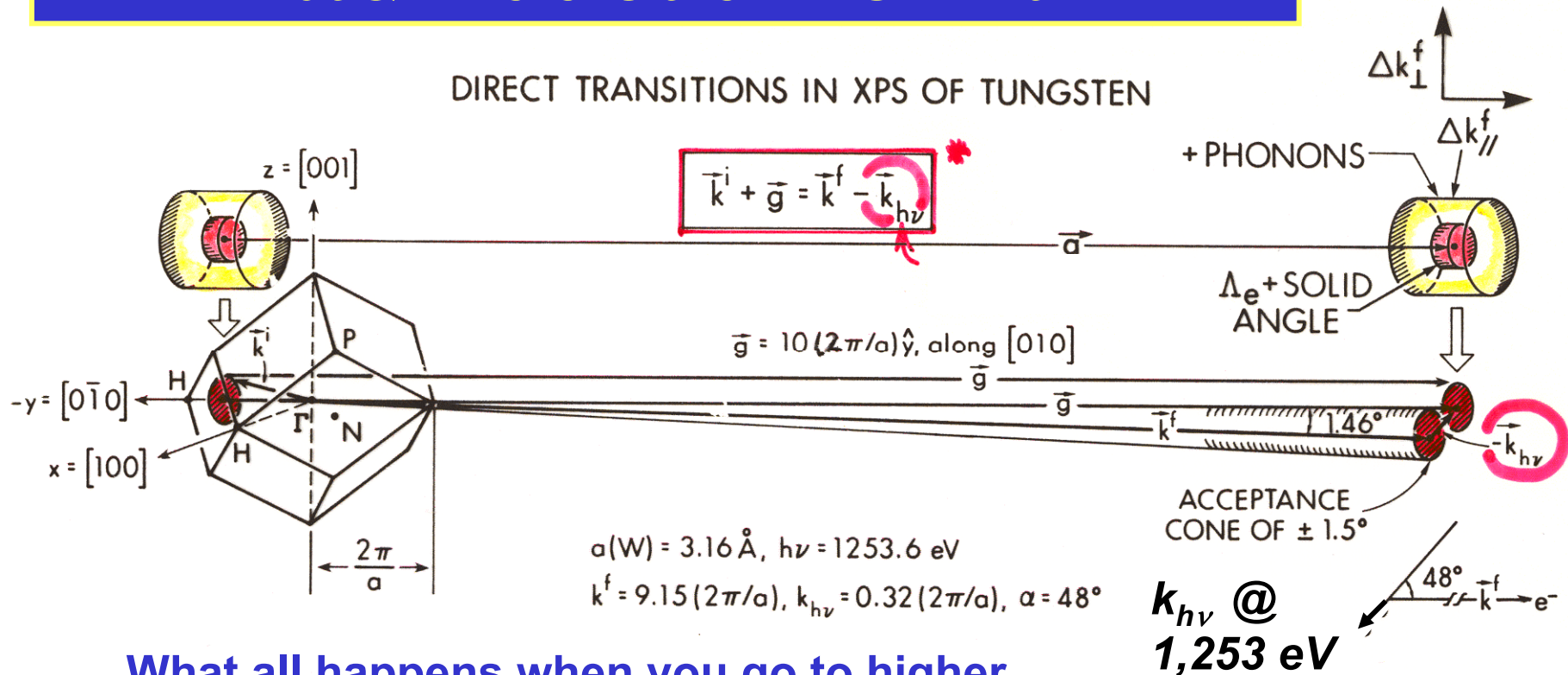


Fig. 4.20. Photoemission energy distribution curves from Cu(111) at different collection angles. Equation (4.32) has been used to express the electron kinetic energy in terms of the binding energy of the electron state (Kevan, 1983).



Valence-Band Photoemission at High Energy-- What & Where is the “XPS Limit”?:



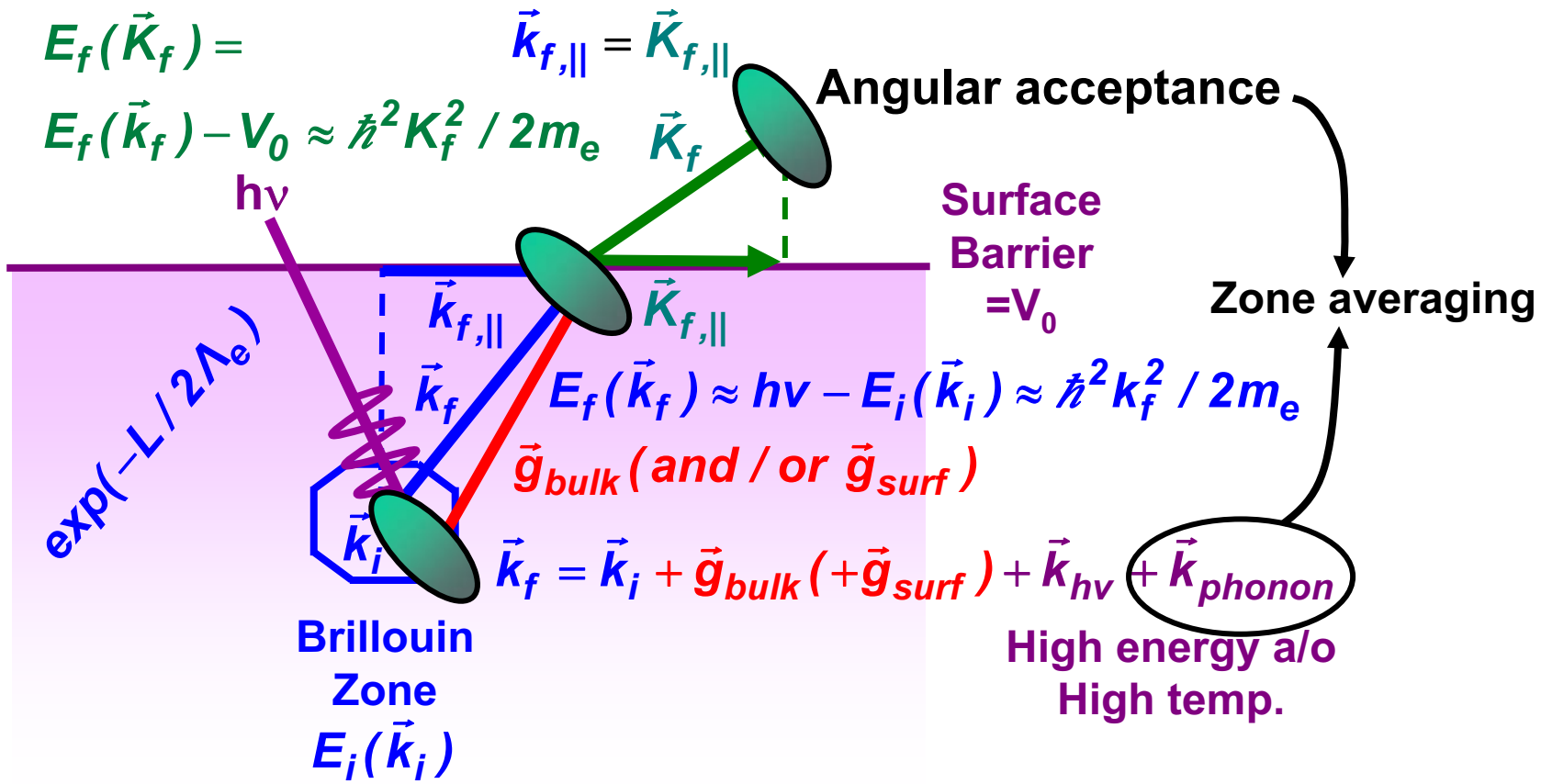
What all happens when you go to higher photon energies?

- non-dipole effect → the photon momentum
- angular acceptance → B.Z. averaging
- lattice recoil, phonon creation → more Brillouin Zone averaging

→ The XPS limit of full B.Z. averaging and D.O.S. sensitivity

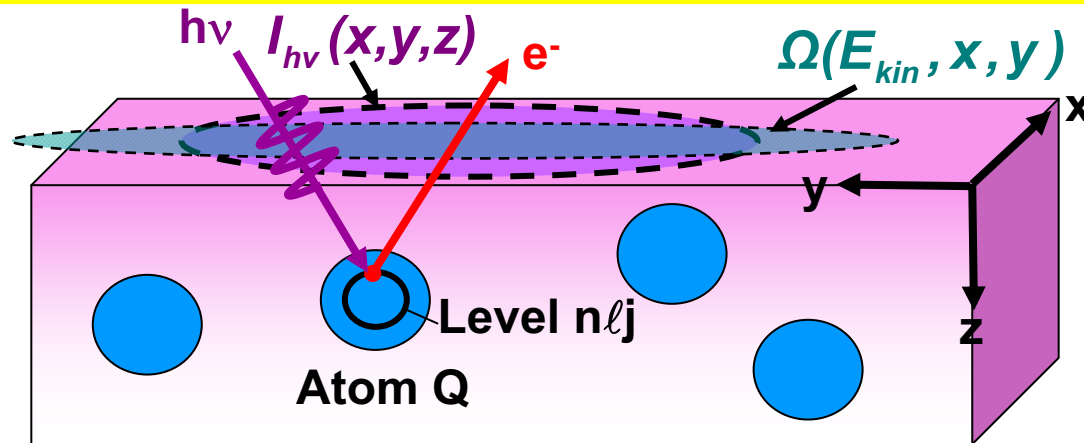
Hussain et al., Phys. Rev. B 22, 3750 ('80)

Valence-band photoemission—at higher energy



$$I(E_f, \vec{k}_f) \propto \left| \hat{\epsilon} \cdot \left\langle \psi_{photoe}(E_f = h\nu + E_i, \vec{k}_f = \vec{k}_i + \vec{g}) \middle| \vec{r} \middle| \psi(E_i, \vec{k}_i) \right\rangle \right|^2$$

CORE PHOTOELECTRON INTENSITIES AND COMPOSITION



$$I(Qn\ell j) =$$

$$c \int_0^{\infty} I_{h\nu}(x,y,z) \rho_Q(x,y,z) \frac{d\sigma_{Qn\ell j}(h\nu)}{d\Omega} \exp\left[-\frac{z}{\Lambda_e(E_{kin}) \sin\theta}\right] \Omega(E_{kin}, x, y) dx dy dz$$

$$I_{h\nu}(x,y,z) = \text{x-ray flux}$$

$\rho_Q(x,y,z)$ = density of atoms Q → quantitative analysis

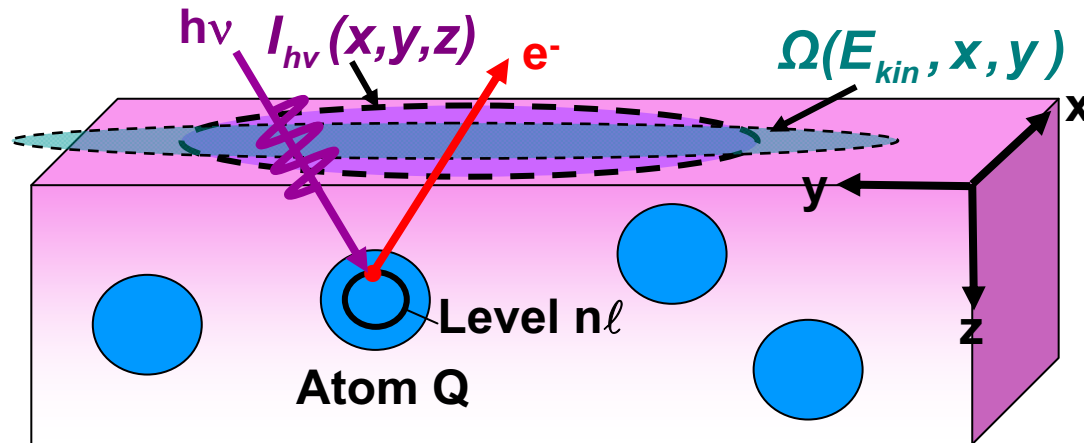
$\frac{d\sigma_{Qn\ell j}(h\nu)}{d\Omega}$ = **energy-dependent** differential photoelectric cross section for subshell Qnℓj

$\Lambda_e(E_{kin})$ = **energy-dependent** inelastic attenuation length

→ Effective Attenuation Length (EAD) → Mean Emission Depth (MED)

$\Omega(E_{kin}, x, y)$ = **energy-dependent** spectrometer acceptance solid angle

VALENCE-BAND PHOTOELECTRON INTENSITIES AND DENSITIES OF STATES



$$I(E_{kin}, Qn\ell) =$$

$$C' \int_0^{\infty} I_{h\nu}(x,y,z) \rho_{Qn\ell}(E_b, x,y,z) \frac{d\sigma_{Qn\ell}(h\nu)}{d\Omega} \exp\left[-\frac{z}{\Lambda_e(E_{kin}) \sin\theta}\right] \Omega(E_{kin}, x, y) dx dy dz$$

$I_{h\nu}(x,y,z)$ = x-ray flux

$\rho_{Qn\ell}(E_b, x,y,z)$ = density of states, projected onto $Qn\ell$ character

$\frac{d\sigma_{Qn\ell}(h\nu)}{d\Omega}$ = **energy-dependent** differential photoelectric cross section for subshell $Qn\ell$

$\Lambda_e(E_{kin})$ = **energy-dependent** inelastic attenuation length

→ Mean Emission Depth

$\Omega(E_{kin}, x, y)$ = **energy-dependent** spectrometer acceptance solid angle

$h\nu = 1487 \text{ eV}$

Estimating phonon effects: 1st approx.

$W(T) =$
Debye-Waller factor
 $= \exp(-\frac{1}{3}g^2 \langle U^2(T) \rangle)$

$I(E, T) =$
 $W(T)I_{DT}$
 $+ [1 - W(T)]I_{NDT}$

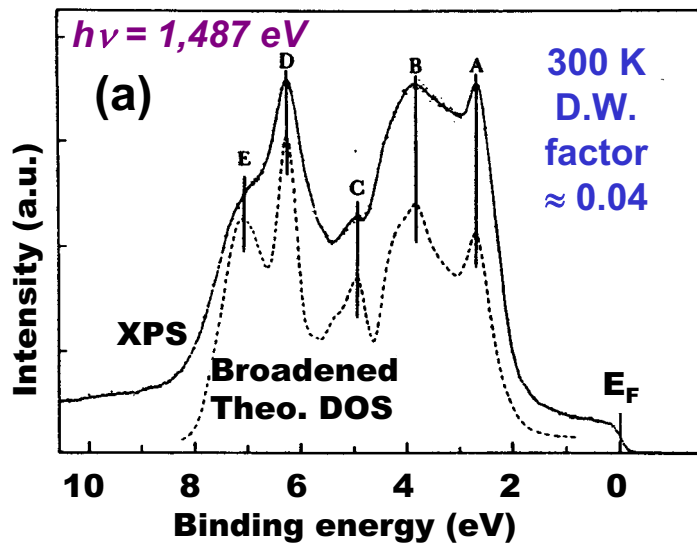
Shevchik, Phys. Rev. B 20, 3020 ('79); Hussain et al., Phys. Rev. 22, 3750 ('80)

TABLE I. Tabulation of thermal displacements $\langle U^2 \rangle$ and Debye-Waller factors $[W(T) = \exp(-\frac{1}{3} \langle U^2 \rangle g^2)]$ in the NPS regime ($E_{\text{kin}} = 1482 \text{ eV}$) for various elements. The Debye temperatures are taken from Ref. 30. The solid line divides the Debye-Waller factors so as to indicate when $\approx \frac{1}{2}$ of the transitions will be direct. Elements are in order of Z .

Element	Z	A (amu)	$T = 4 \text{ K}$		$T = 77 \text{ K}$		$T = 300 \text{ K}$		$T = 1000 \text{ K}$	
			$\langle U^2 \rangle$ (10^{-18} cm^2)	W	$\langle U^2 \rangle$ (10^{-18} cm^2)	W	$\langle U^2 \rangle$ (10^{-18} cm^2)	W	$\langle U^2 \rangle$ (10^{-18} cm^2)	W
Be	1440	9.012	0.54	0.34	0.56	0.33	1.07	0.25	2.47	0.04
C	2230	12.001	0.51	0.33	0.51	0.33	0.46	0.53	0.83	0.34
Mg	400	24.312	1.13	0.22	1.48	0.16	2.52	0.01		
Al	428	26.981	0.95	0.29	1.15	0.22	2.79	0.03		
Si	643	28.086	0.60	0.46	0.66	0.42	1.26	0.19	3.07	0.02
Ca	230	40.08	1.13	0.21	1.94	0.08	6.24	0.0		
Ti	420	47.9	0.54	0.49	0.66	0.42	1.63	0.12	5.16	0.0
V	390	50.942	0.56	0.48	0.72	0.39	1.85	0.09	5.93	0.0
Cr	630	51.996	0.38	0.68	0.37	0.62	0.71	0.40	2.15	0.06
Mn	410	54.938	0.48	0.56	0.60	0.46	1.49	0.14	4.72	0.0
Fe	470	55.847	0.42	0.58	0.43	0.53	1.13	0.23	3.58	0.01
Co	443	58.933	0.42	0.58	0.50	0.52	1.19	0.21	3.74	0.0
Ni	450	58.71	0.41	0.59	0.43	0.53	1.17	0.22	3.67	0.01
Cu	343	63.54	0.30	0.69	0.67	0.42	1.82	0.09	5.84	0.0
Zn	327	65.37	0.31	0.61	0.70	0.40	1.82	0.08		
Gc	374	72.59	0.30	0.59	0.50	0.51	1.34	0.17	4.28	0.0
As	282	74.922	0.32	0.51	0.77	0.37	2.25	0.05	7.33	0.0
Zr	291	91.22	0.41	0.59	0.60	0.48	1.74	0.10	5.65	0.0
Nb	275	92.906	0.43	0.57	0.68	0.43	1.90	0.08	6.21	0.0
Mo	450	95.94	0.25	0.72	0.30	0.65	0.71	0.39	2.25	0.03
Ru	600	101.07	0.18	0.78	0.26	0.77	0.40	0.50	1.21	0.21
Rh	450	102.905	0.22	0.75	0.26	0.71	0.59	0.46	1.84	0.09
Pd	274	106.4	0.37	0.61	0.57	0.48	1.68	0.11	5.46	0.0
Ag	225	107.87	0.45	0.56	0.75	0.38	2.44	0.04	8.00	0.0
Cd	209	112.40	0.47	0.55	0.81	0.35	2.70	0.03		
Sa	300	118.69	0.46	0.55	0.80	0.34	2.53	0.04		
Sb	211	121.75	0.49	0.57	0.79	0.35	2.40	0.04		
Hf	252	178.49	0.24	0.73	0.30	0.68	1.18	0.22	3.85	0.01
Ta	240	180.948	0.25	0.72	0.30	0.68	1.23	0.19	4.19	0.0
W	400	183.85	0.15	0.82	0.18	0.79	0.47	0.55	1.48	0.14
Re	430	186.2	0.16	0.80	0.17	0.81	0.40	0.60	1.23	0.19
Os	500	190.2	0.11	0.86	0.15	0.84	0.30	0.68	0.92	0.30
Ir	420	192.2	0.14	0.84	0.17	0.81	0.41	0.53	1.29	0.13
Pt	240	195.09	0.23	0.74	0.33	0.60	1.19	0.21	3.88	0.01
Au	163	196.967	0.34	0.63	0.52	0.39	2.46	0.04	8.14	0.0
Pb	105	207.19	0.51	0.32	1.54	0.13	5.75	0.0		

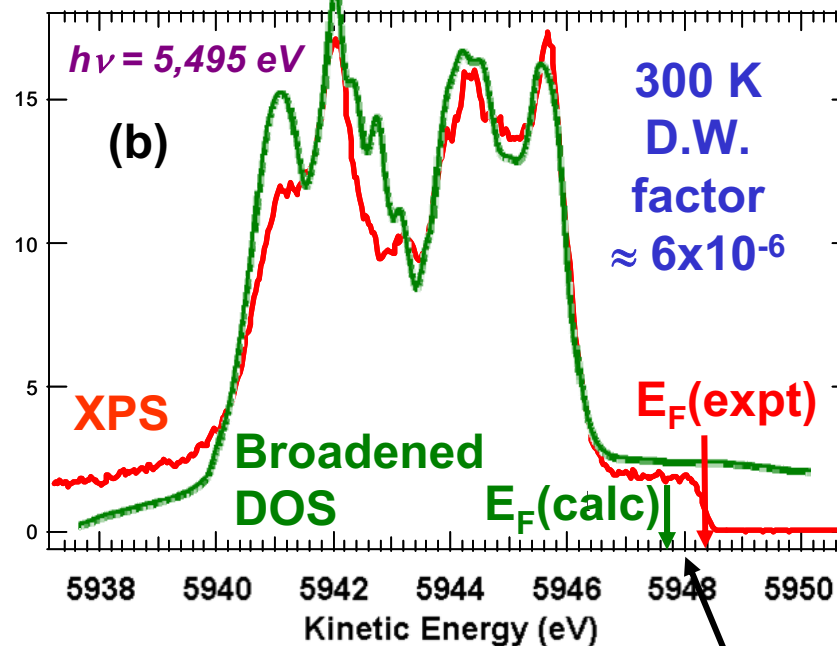
Greater than 50% direct transitions

Gold Valence Spectrum



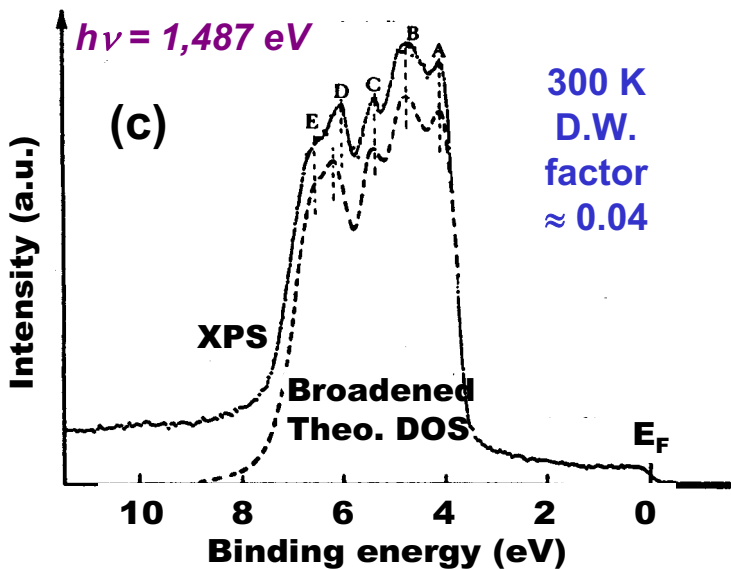
Valence spectra in the XPS Limit

Gold Valence Spectrum

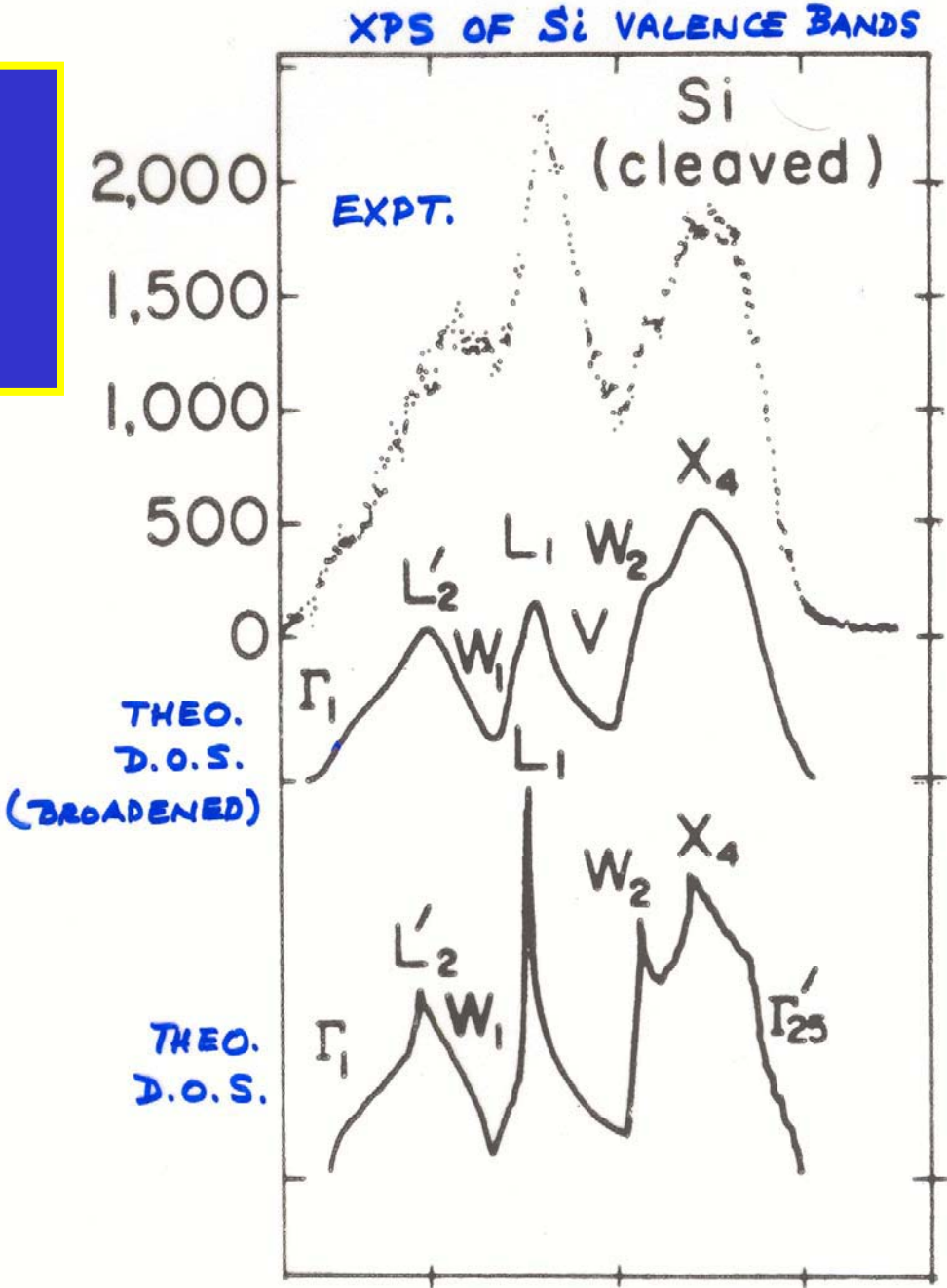


Screening/
self-energy
correction

Silver Valence Spectrum

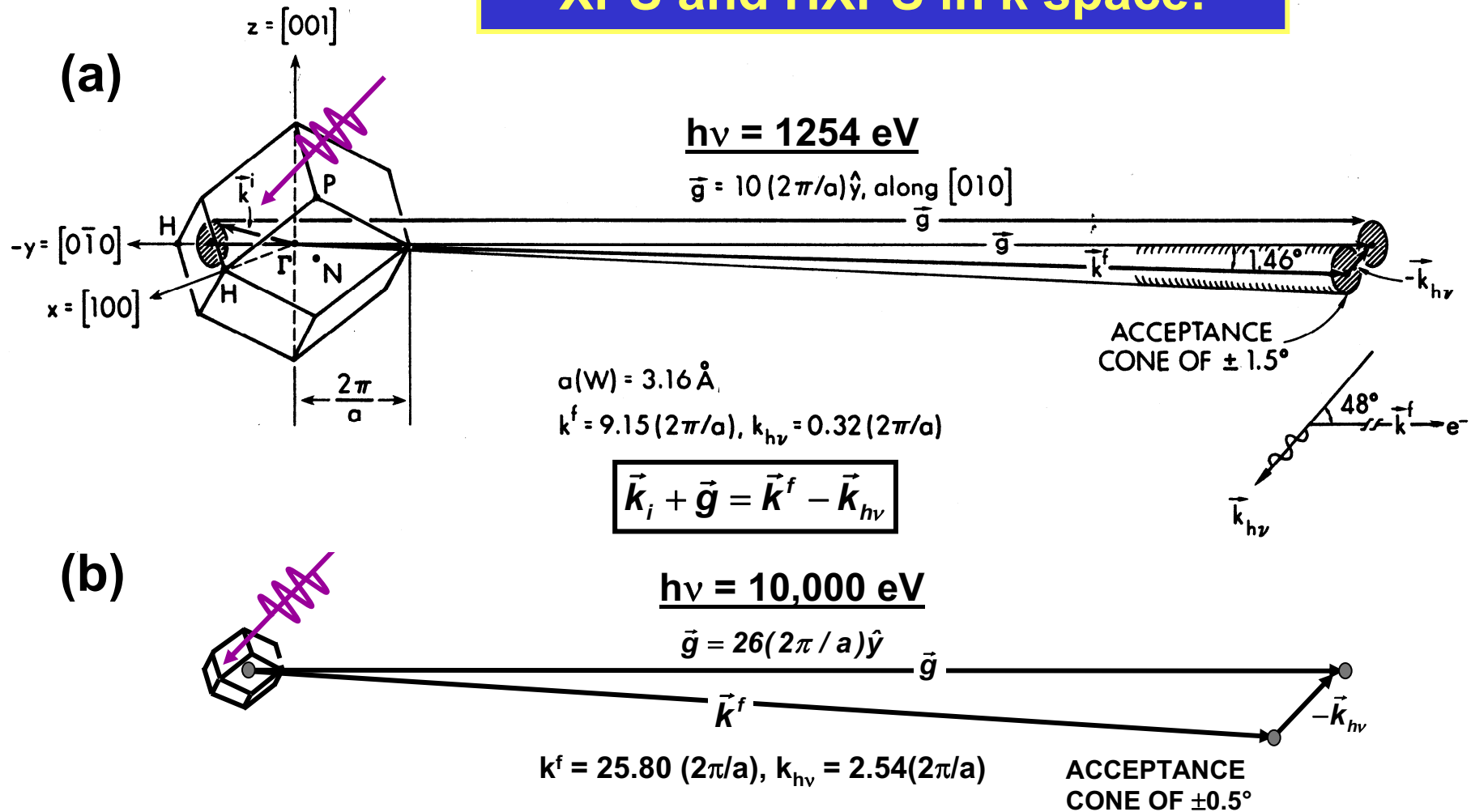


Some classic cases in the XPS limit:



“Basic Concepts of XPS”
Figure 14

XPS and HXPS in k space:

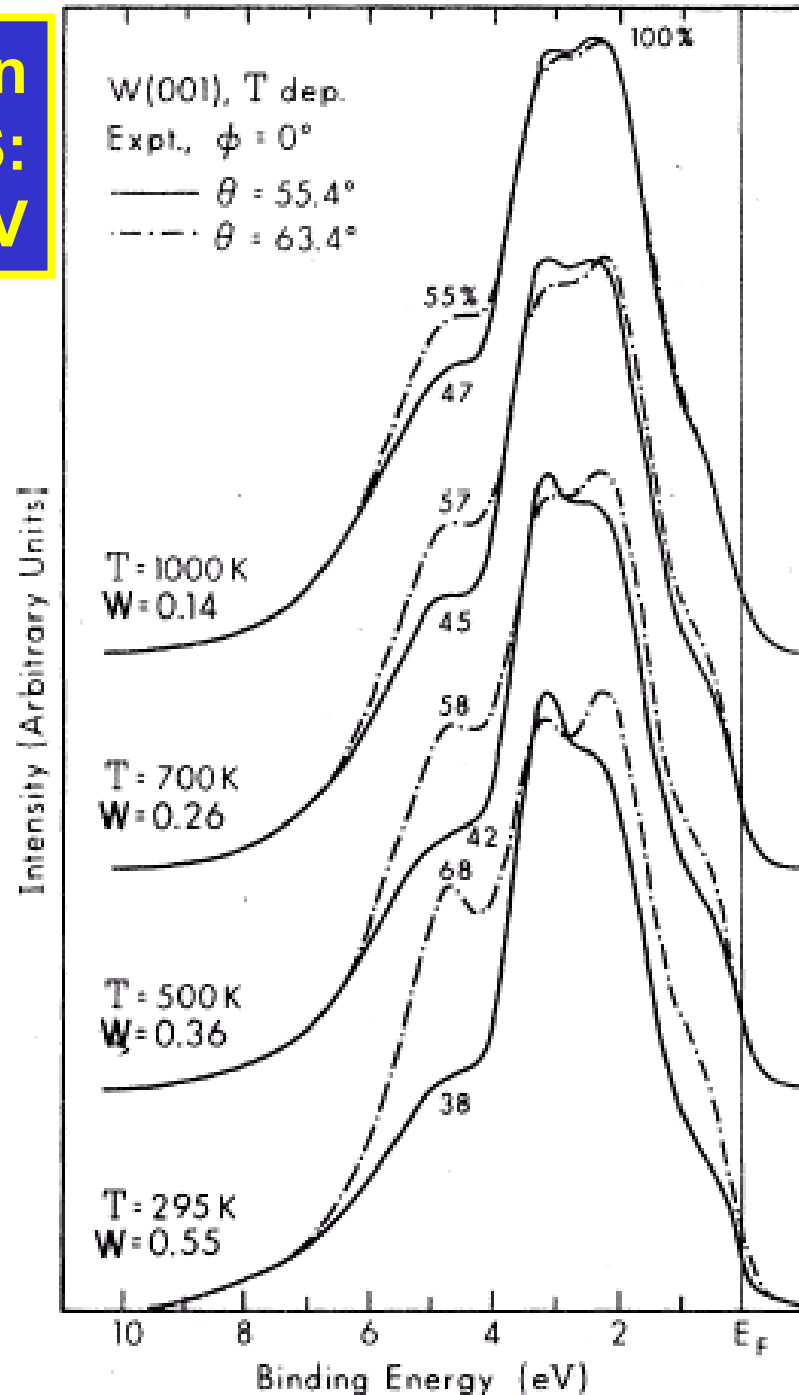


Phonon effects: Approximate fraction of “good” direct transitions

$$\approx \text{Debye-Waller factor} = W(T) \approx \exp[-g^2 \langle u^2(T) \rangle]$$

= Mean-squared
vibrational displacement

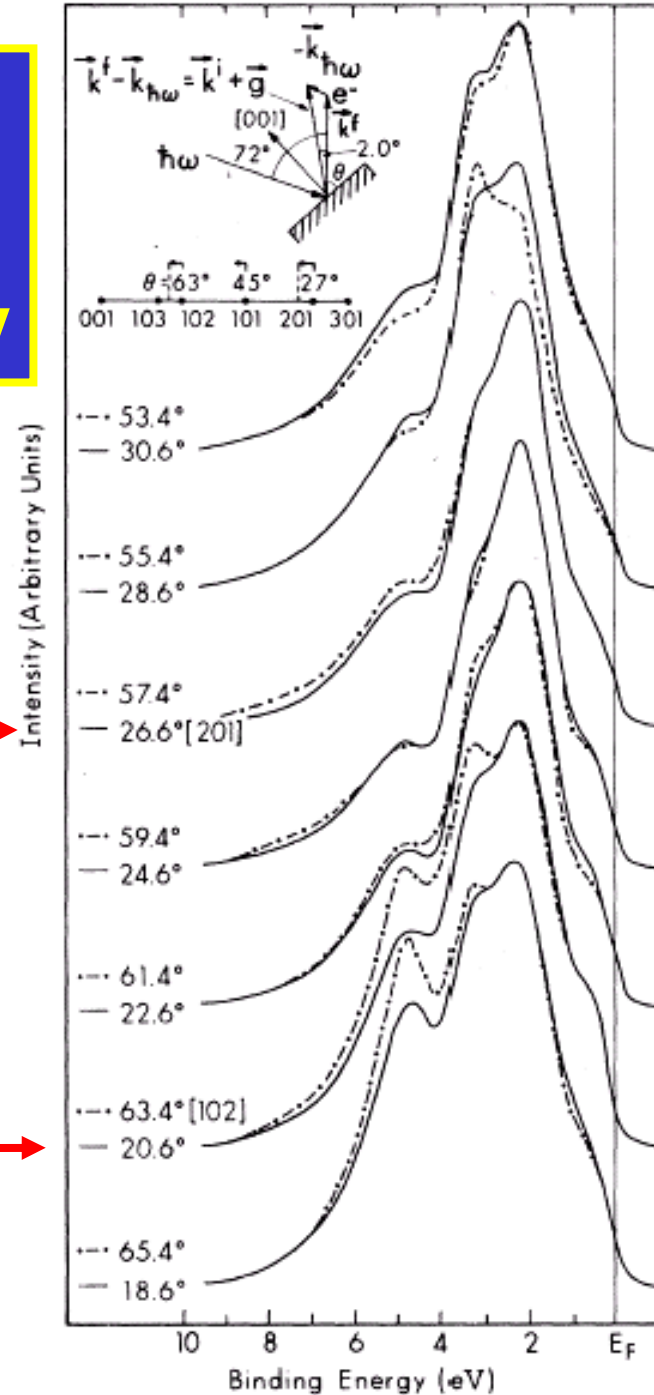
**Direct-transition
effects in XPS:
W(110) at 1253.6 eV**



Present if
vibrations stiff
enough (Debye
T high enough),
but suppressed
as temperature is
raised.

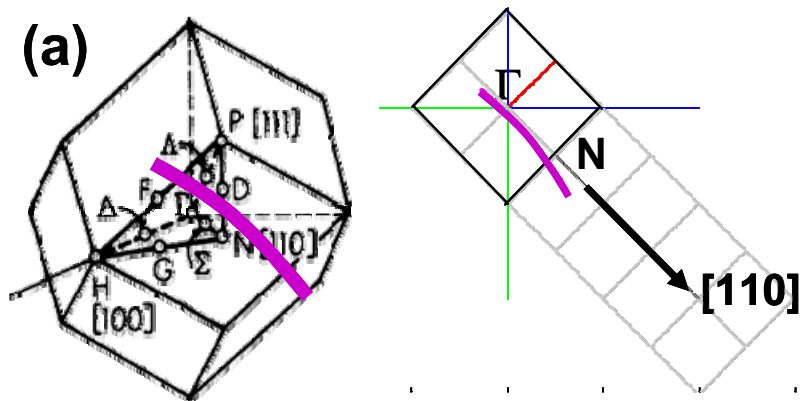
Hussain et al.,
Phys. Rev. 22,
3750 (1980)

Effect of photon momentum on k conservation: W(110) at 1253.6 eV



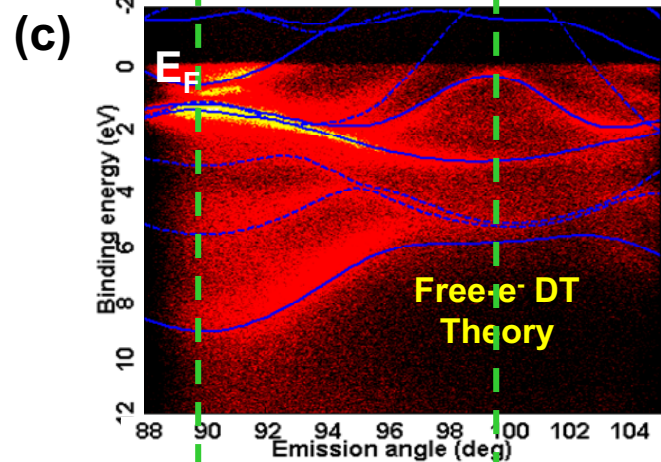
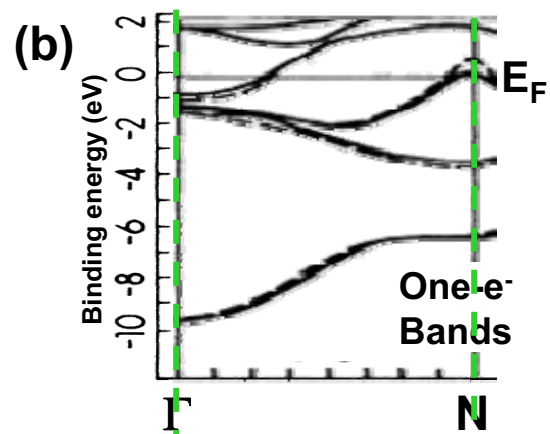
Symmetry-related spectra shifted by 6.0° for best match. Theoretical 4.8° due to k_{hv}

Hussain et al.,
Phys. Rev. 22,
3750 (1980)

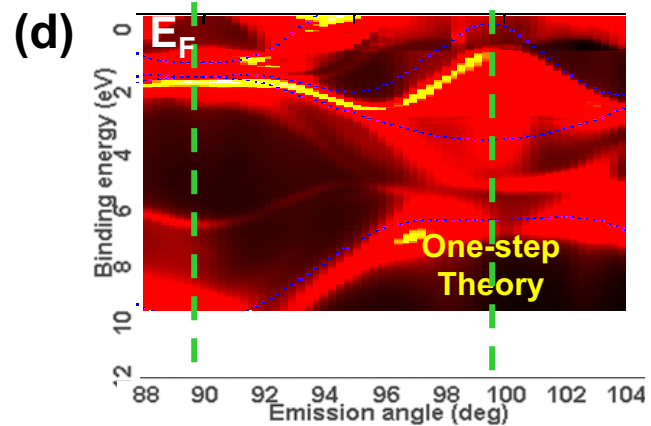


**Angle-Resolved
 Photoemission
 from W(110)**
 $h\nu = 260 \text{ eV}$
 $90^\circ = \text{normal}$
 $\Theta_{\text{Debye}} = 400\text{K}$

Plucinski et al., Phys.
 Rev. B, submitted

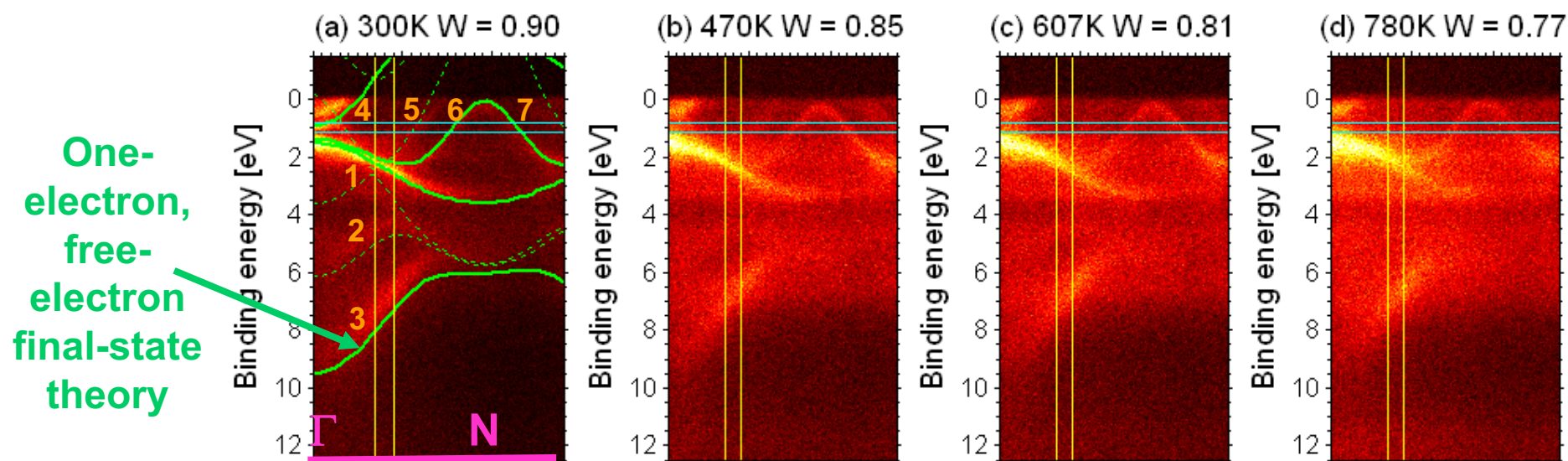


Plucinski

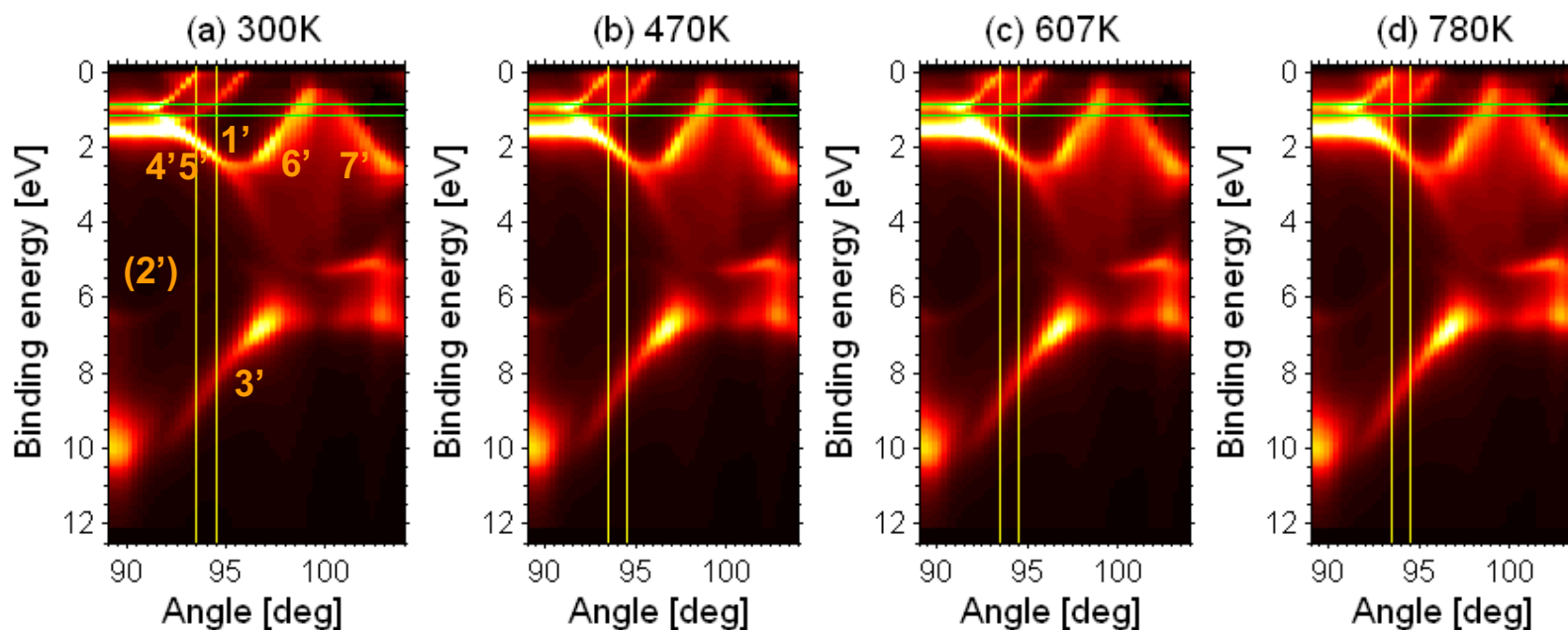


Braun, Minar,
Ebert

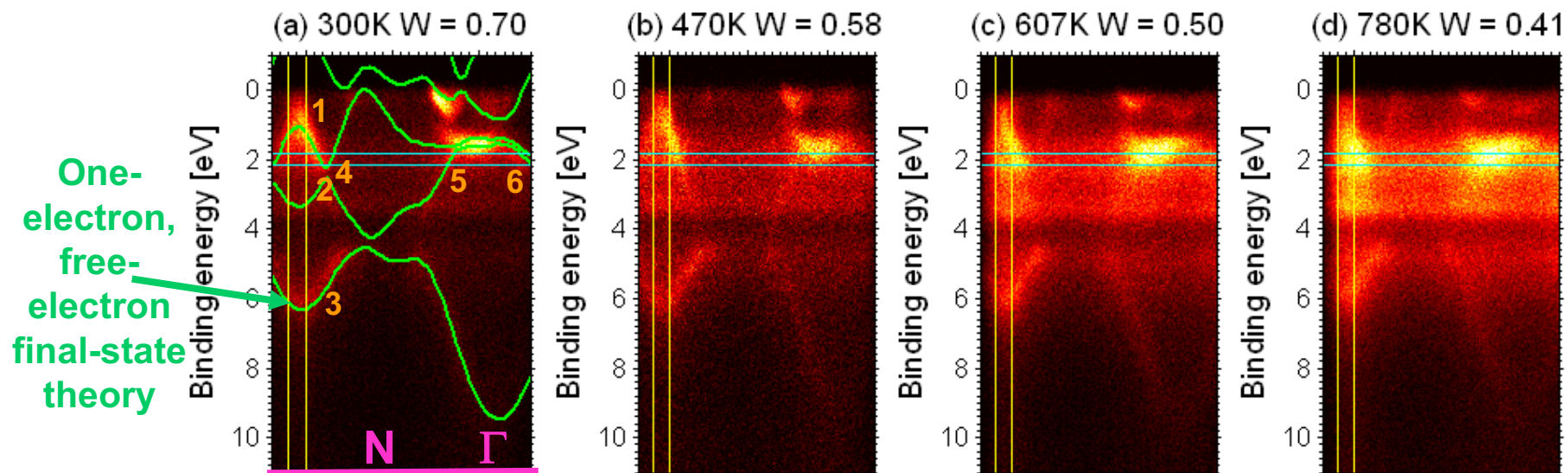
ARPES from W(110): Expt, $h\nu = 260$ eV, near-normal emission, $\Theta_{\text{Debye}} = 400\text{K}$



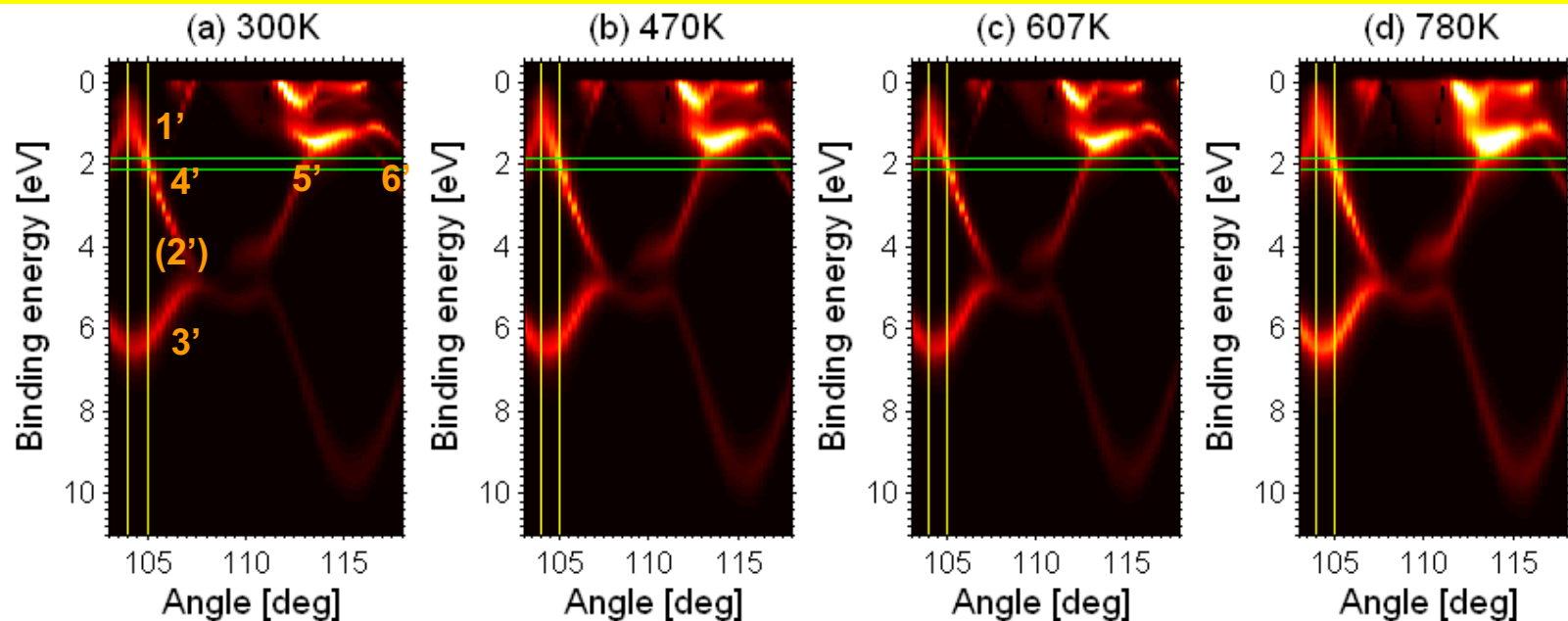
ARPES from W(110): 1-Step Theory, $h\nu = 260$ eV, near-normal emission, $\Theta_{\text{Debye}} = 400\text{K}$



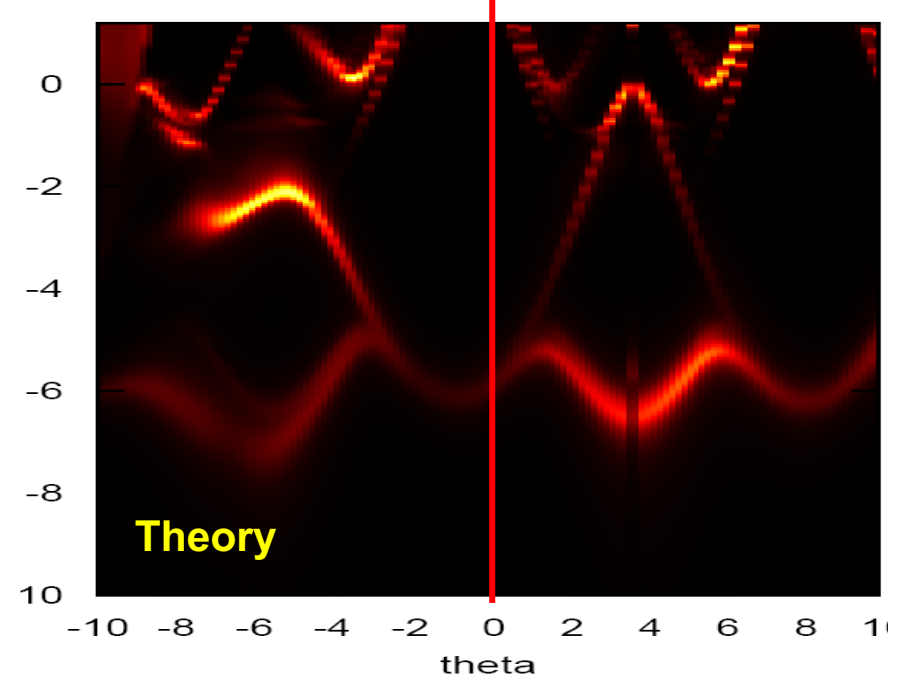
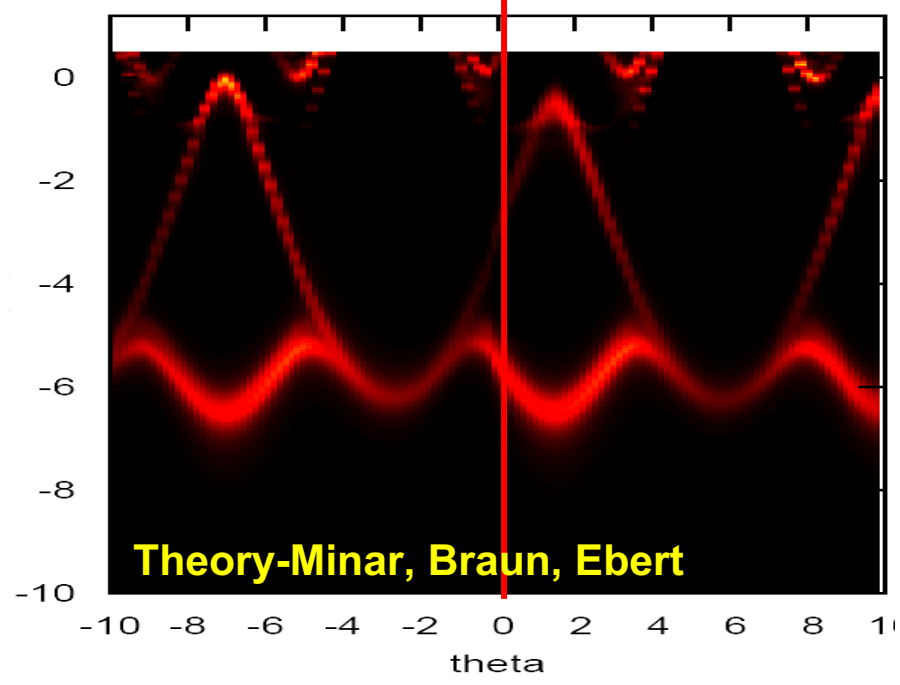
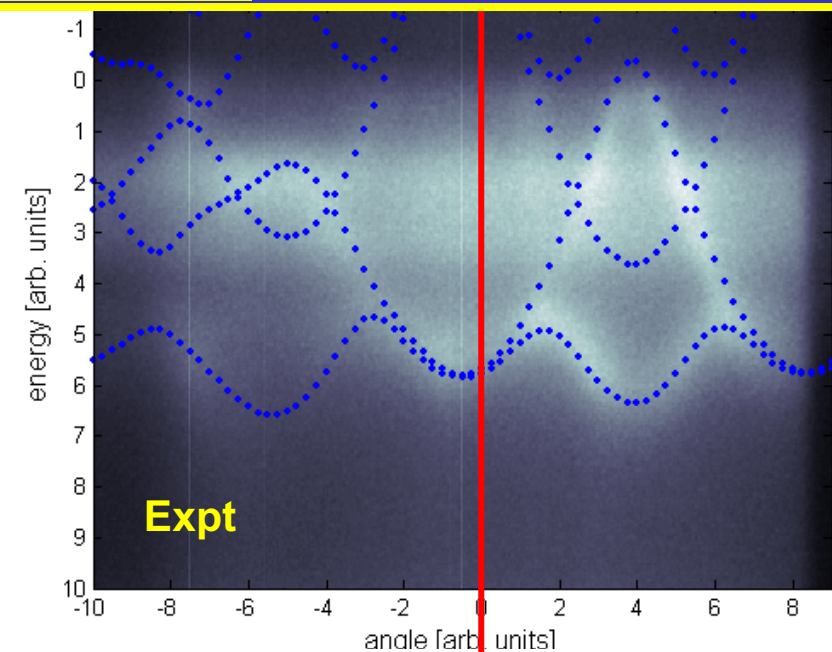
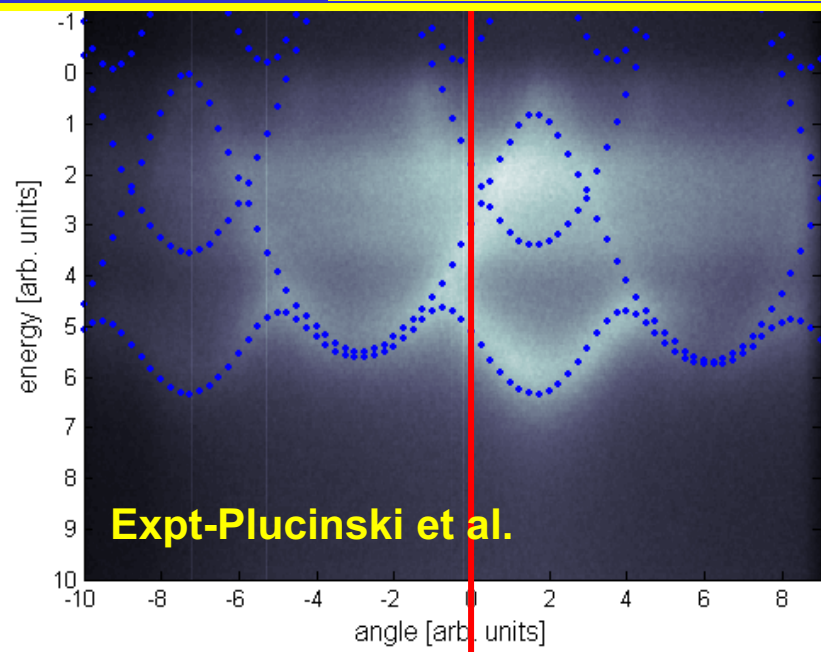
ARPES from W(110): Expt, $h\nu = 860$ eV, near-normal emission, $\Theta_{\text{Debye}} = 400\text{K}$



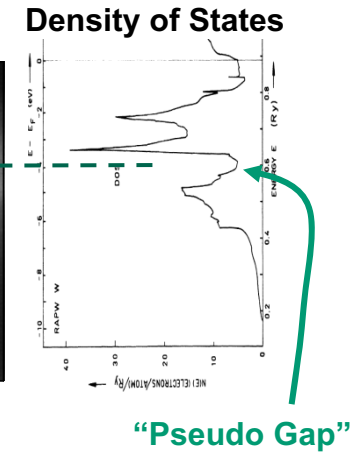
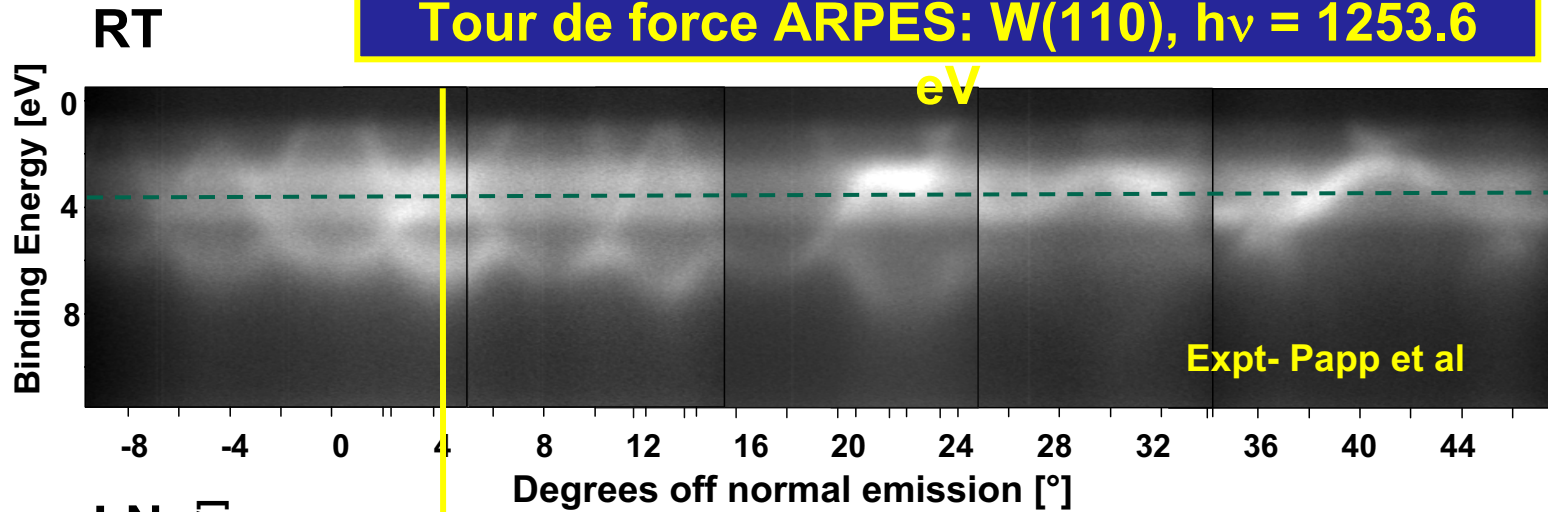
ARPES from W(110): 1-Step Theory, $h\nu = 870$ eV, near-normal emission, $\Theta_{\text{Debye}} = 400\text{K}$



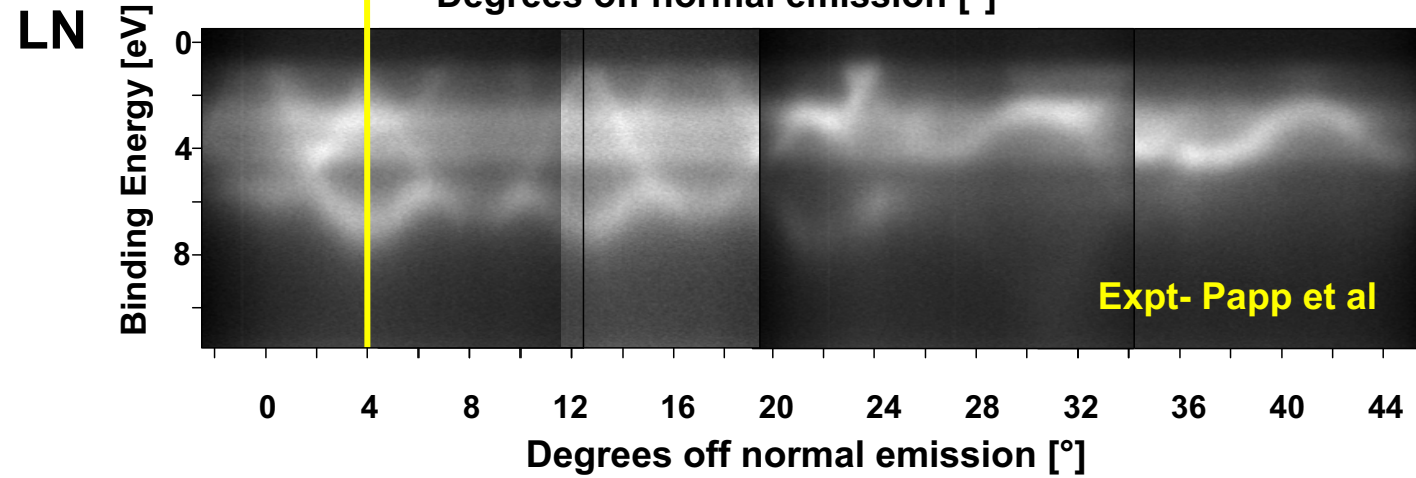
ARPES with a non-monochromatized lab. x-ray source: $h\nu = 1253.6$ eV, $T = \sim 77$ K



Tour de force ARPES: W(110), $h\nu = 1253.6$

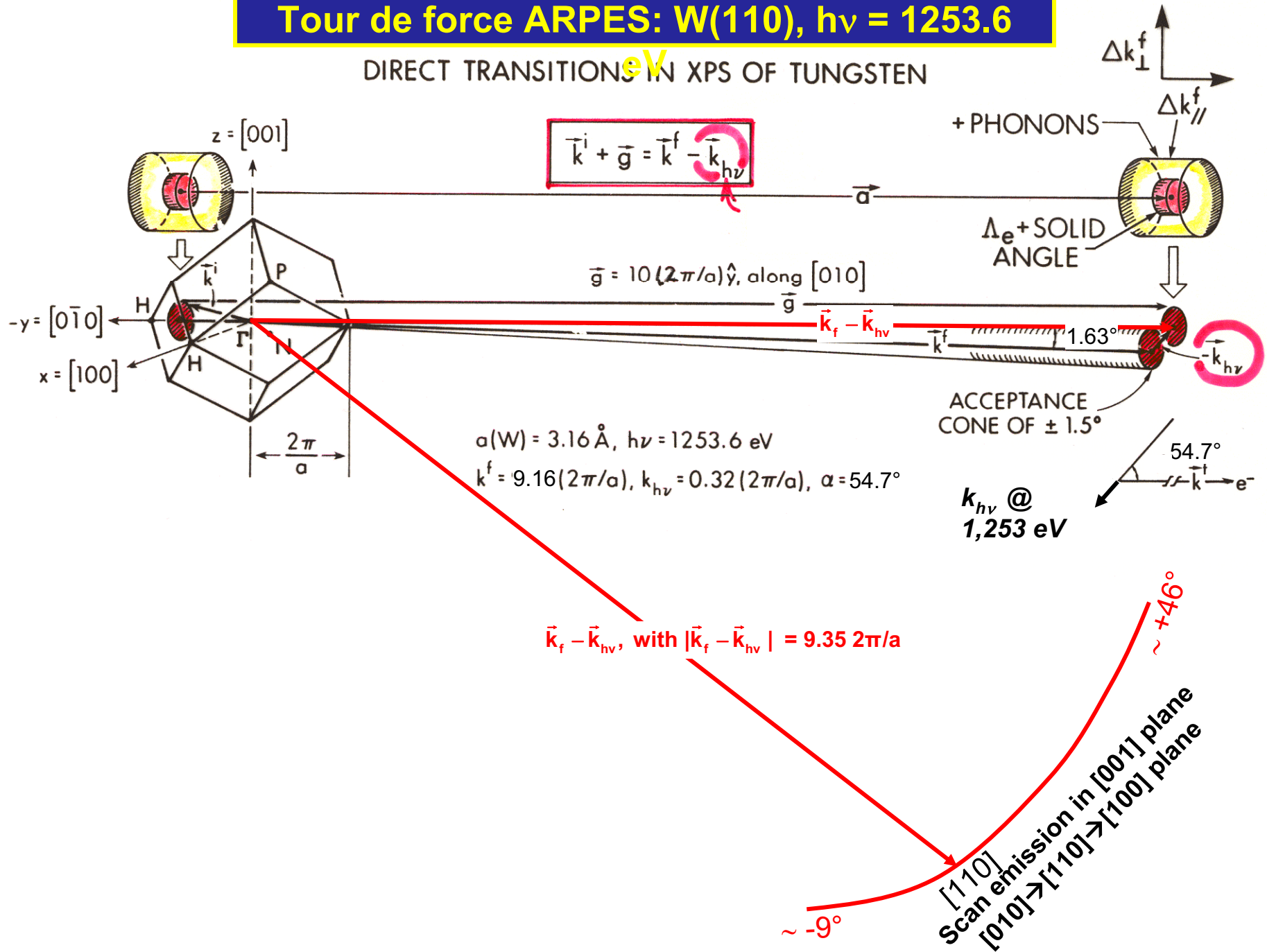


Christensen & Feuerbacher, PRB 10, 2349 ('74)

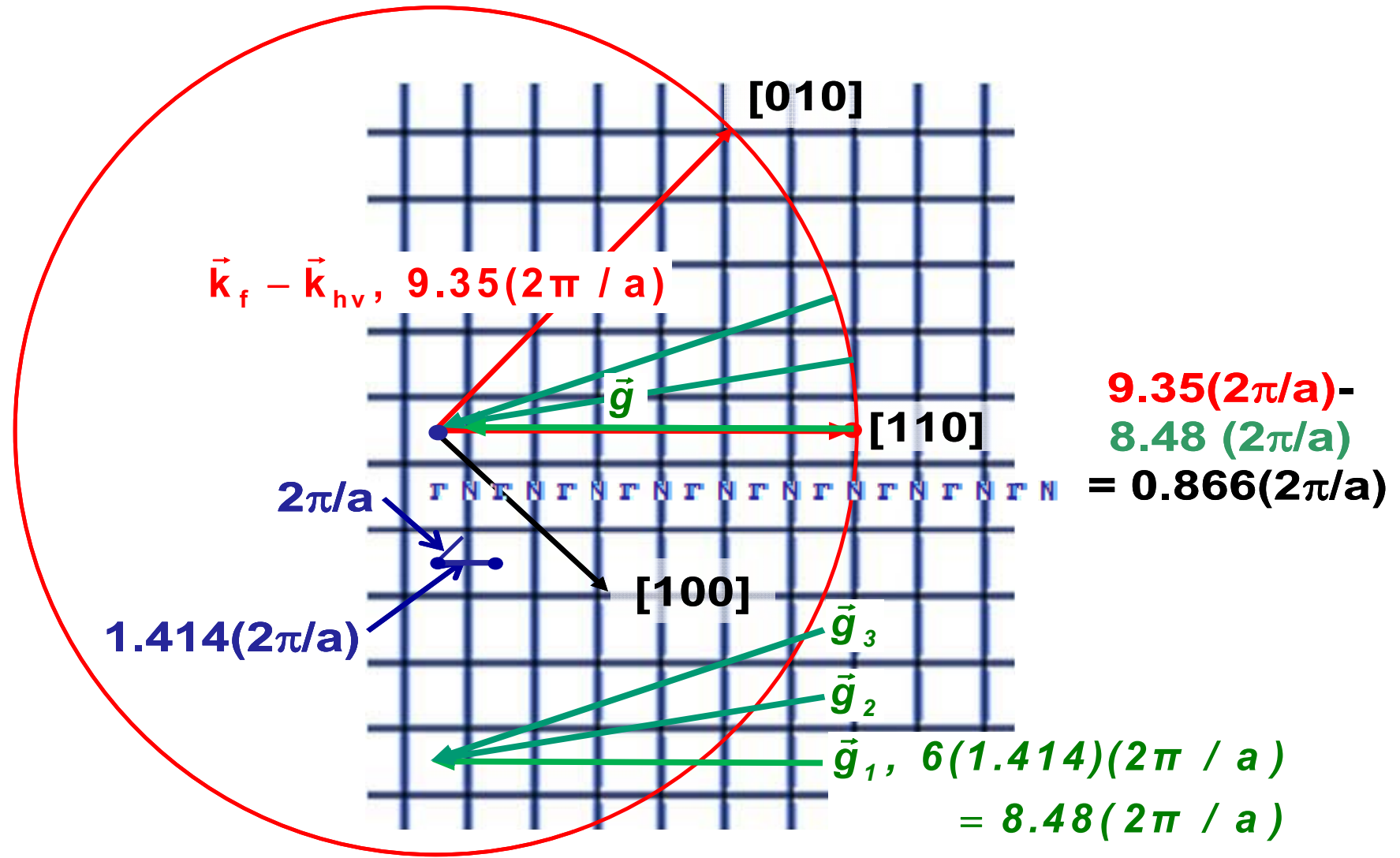


Tour de force ARPES: W(110), $h\nu = 1253.6$

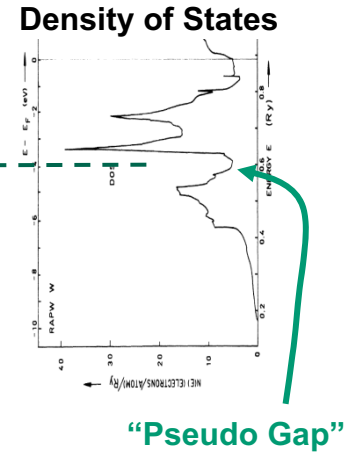
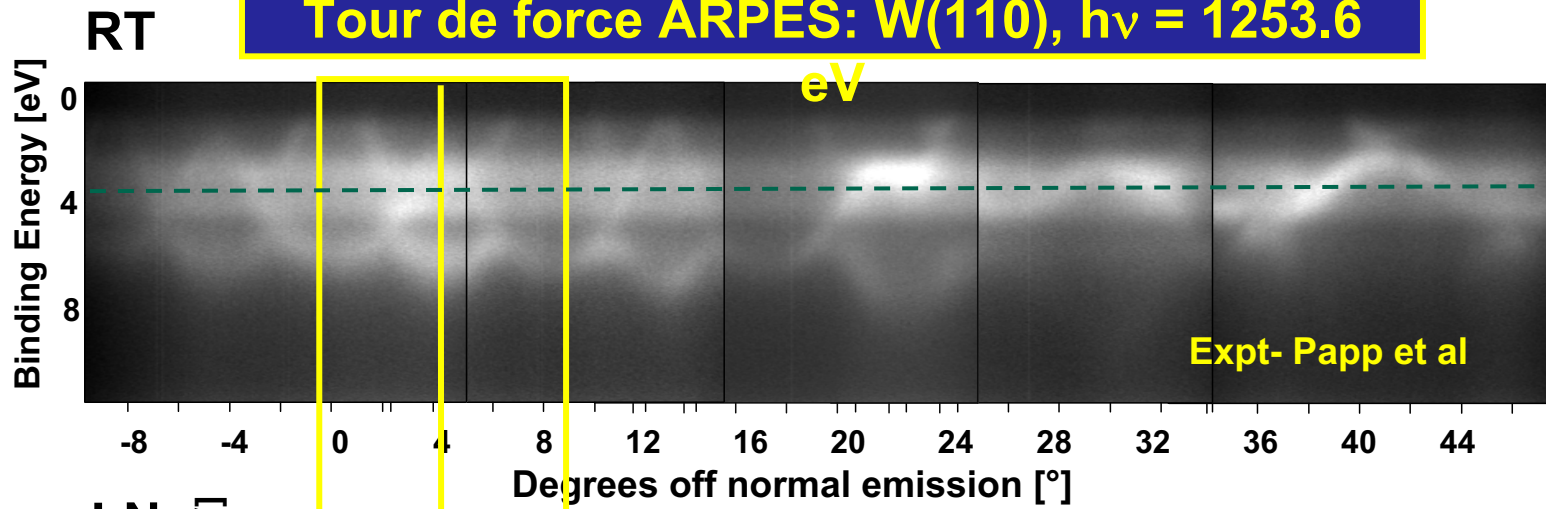
DIRECT TRANSITIONS IN XPS OF TUNGSTEN



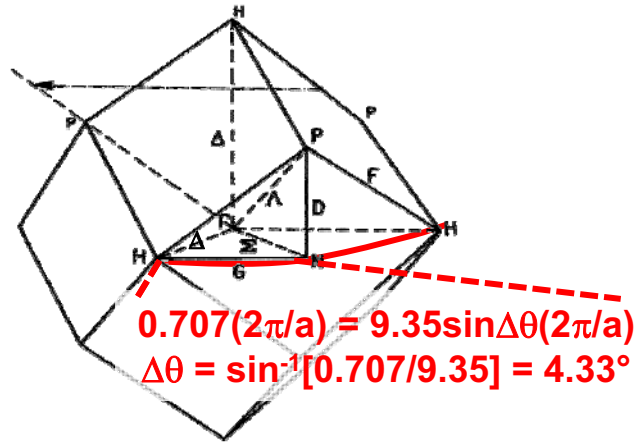
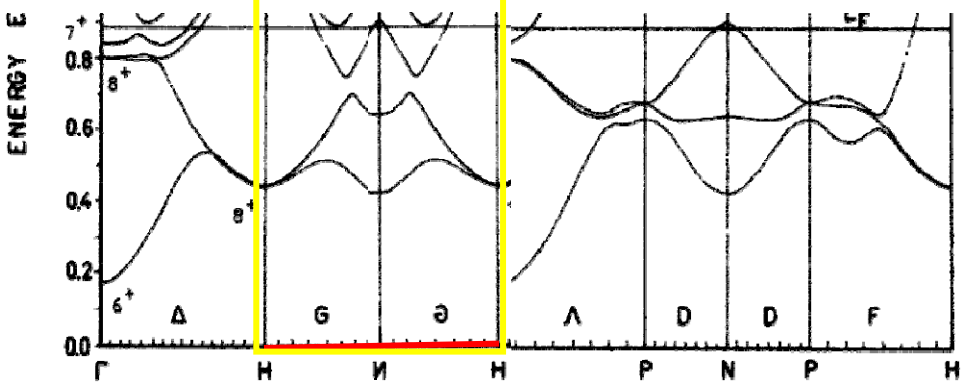
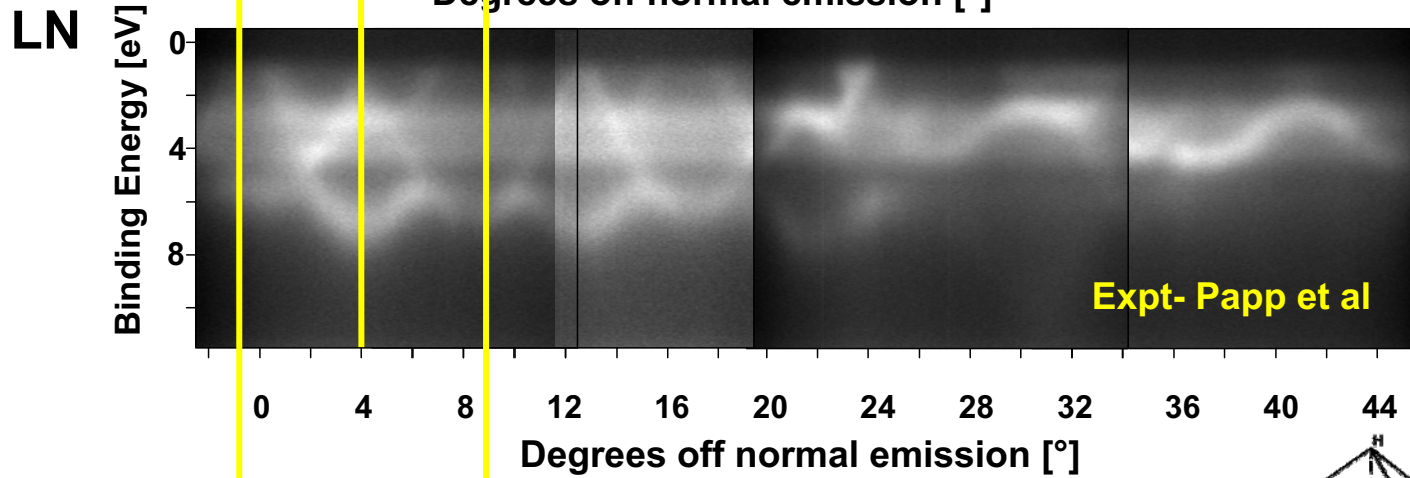
Tour de force ARPES in an extended zone scheme: W(110), [001] plane, $h\nu = 1253.6$ eV



Tour de force ARPES: W(110), $h\nu = 1253.6$

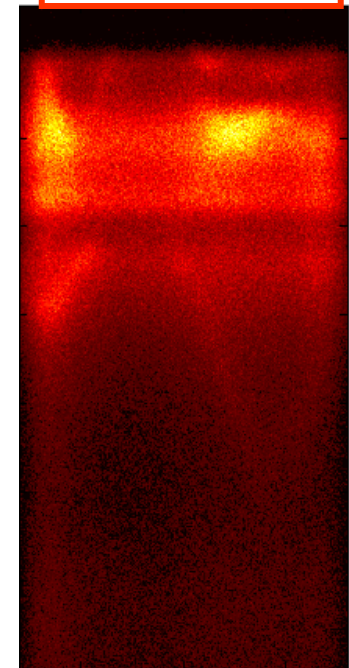
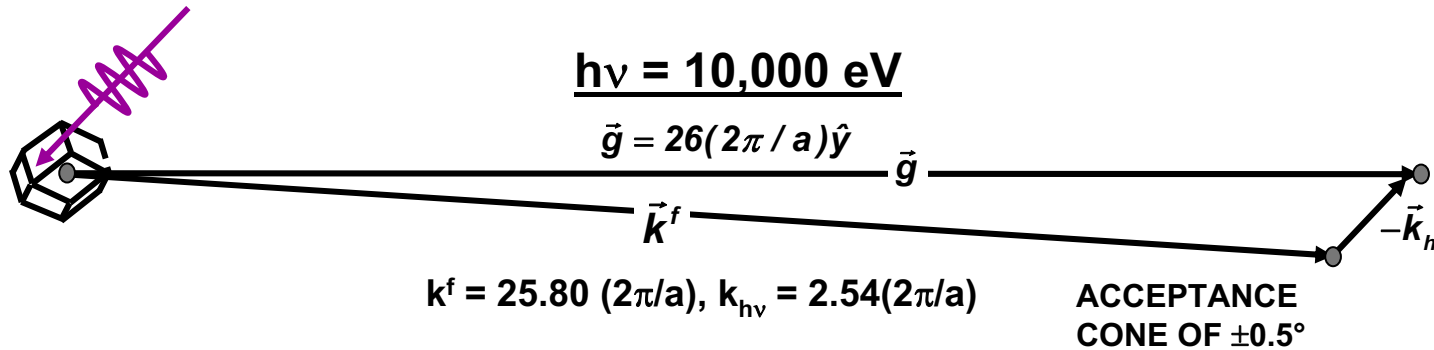


Christensen & Feuerbacher, PRB 10, 2349 ('74)



And what would happen at 10 keV?:

$h\nu = 870 \text{ eV}$
 $T = 780\text{K}$
 $W \approx 0.41$



$\Theta_{\text{Debye}} = 310\text{K}, \langle u^2 \rangle (10^{-20} \text{ cm}^2) = 5.34 + 0.0583T \xrightarrow{\text{High } T} 0.0583T$

Debye-Waller Factor = $W(T) \approx \exp(-k_e^2 \langle u^2(T) \rangle)$

$= \exp(-C_1 E_{\text{kin}} \langle u^2(T) \rangle) \xrightarrow{\text{High } T} \exp(-C_2 E_{\text{kin}} T)$

W at 4K: $W \approx 0.27$, $\approx 27\%$ direct

at 77K: $W \approx 0.20$, $\approx 20\%$ direct

at 300K: $W \approx 0.017$, $\approx 2\%$ direct

Correlated vibrations and better theory (e.g. Phys. Rev. B 35, 1147

('87) and 53, 7524 ('96) + 54, 14703 ('96)) may yield different DT

percentages, but needs further experimental and theoretical study

For W(110): $h\nu = 5,946$ eV: Where are we in the Brillouin Zone? Calculation of Photon Momentum Effect on k Conservation

The free-electron picture:

$$(2\pi / a) = 1.988 \text{ \AA}^{-1}$$

$$h\nu = 5945 \text{ eV}$$

$$|\vec{k}_f| = 0.512E_{\text{kin}}^{0.5} (\text{eV}) = 39.48 \text{ \AA}^{-1} = 19.85 (2\pi / a)$$

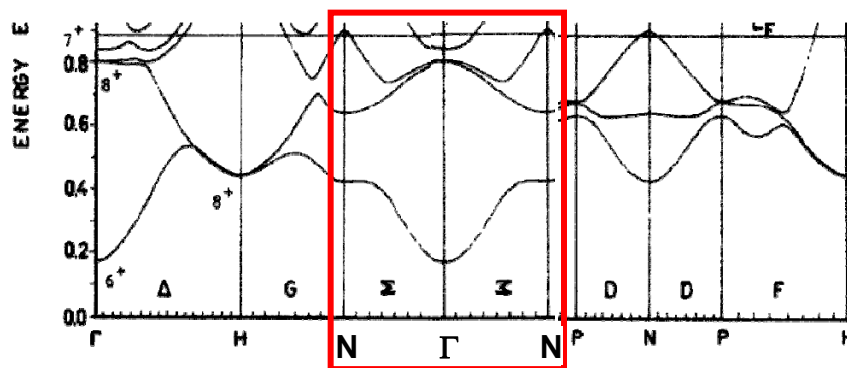
$$|\vec{k}_{h\nu}| = 0.000507(h\nu(\text{eV})) = 3.01 \text{ \AA}^{-1} = 1.51 (2\pi / a)$$

$$|\vec{k}_f - \vec{k}_{h\nu}| = [39.48^2 + 3.01^2] = 39.59 \text{ \AA}^{-1} = 19.91 (2\pi / a) \rightarrow 14.08 [1.414((2\pi / a))]$$

$$|\vec{g}_1| = 14.00 [1.414((2\pi / a))]$$

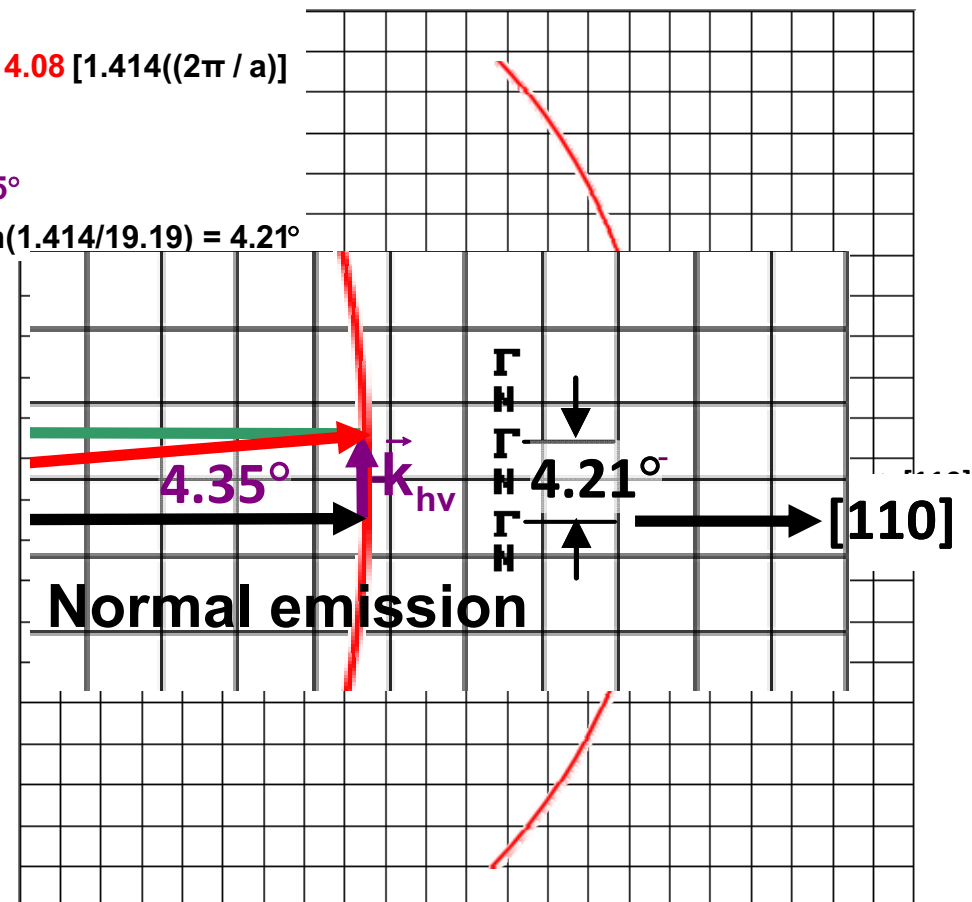
Angular deflection due to $\vec{k}_{h\nu}$ is : $\arctan(3.01 / 39.48) = 4.35^\circ$

$\Gamma - N - \Gamma$ is $1.414(2\pi / a)$, so angular range of this is $\arctan(1.414/19.19) = 4.21^\circ$



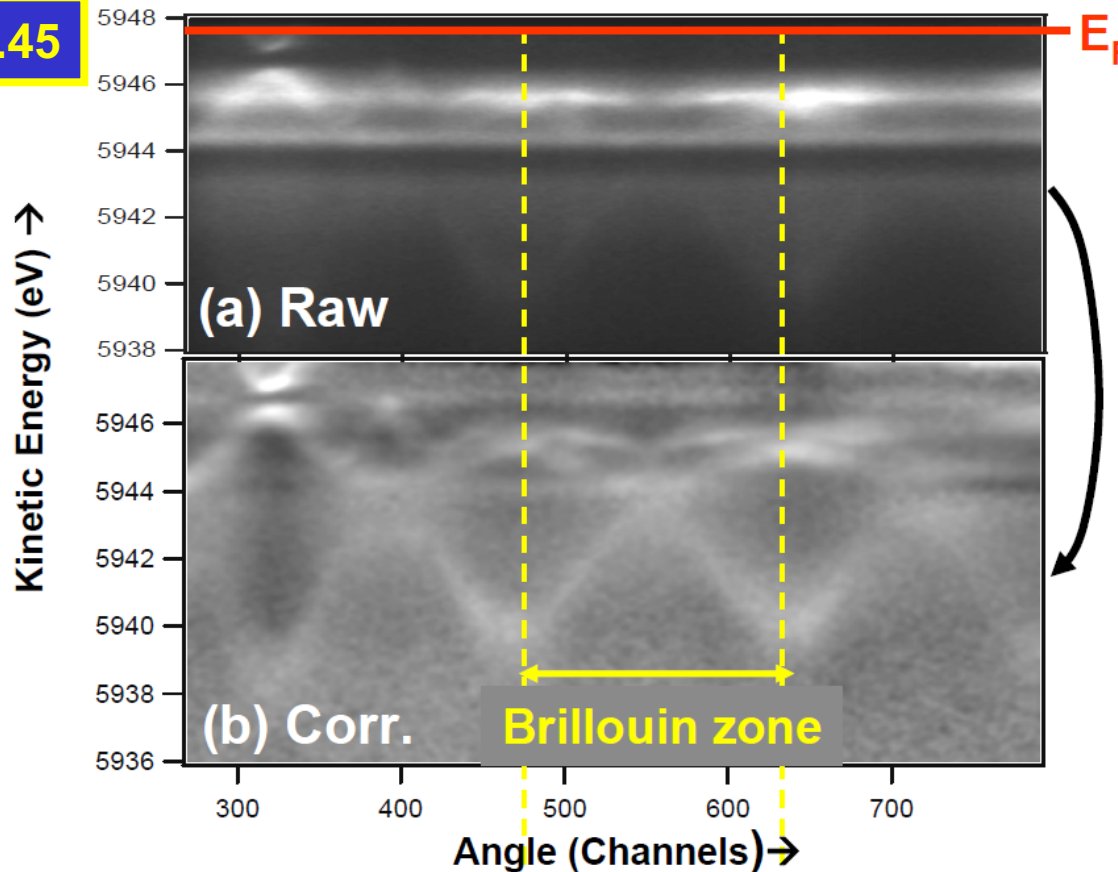
Ueda, Papp,
Kobayashi,
Minar, et al.
to be publ

Experiment in the Extended Brillouin Zone

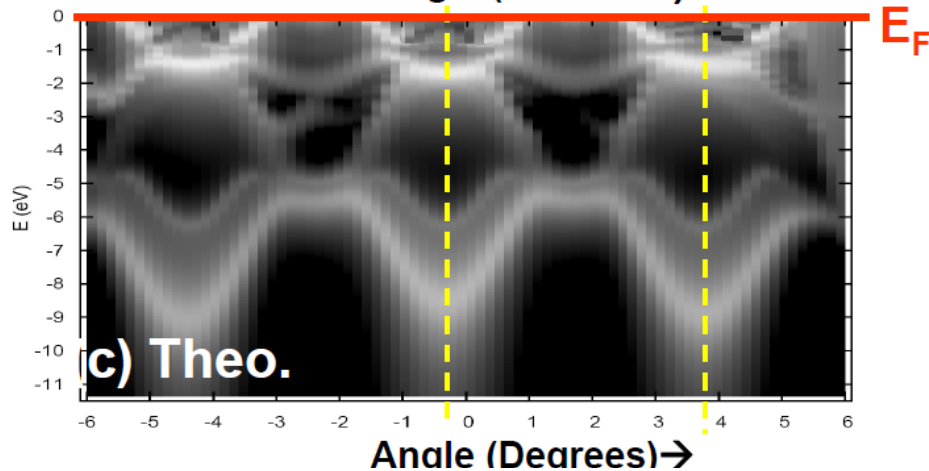


W(110), $h\nu = 5,954$ eV, $T = 30$ K: Comparison to one-step theory, matrix elements

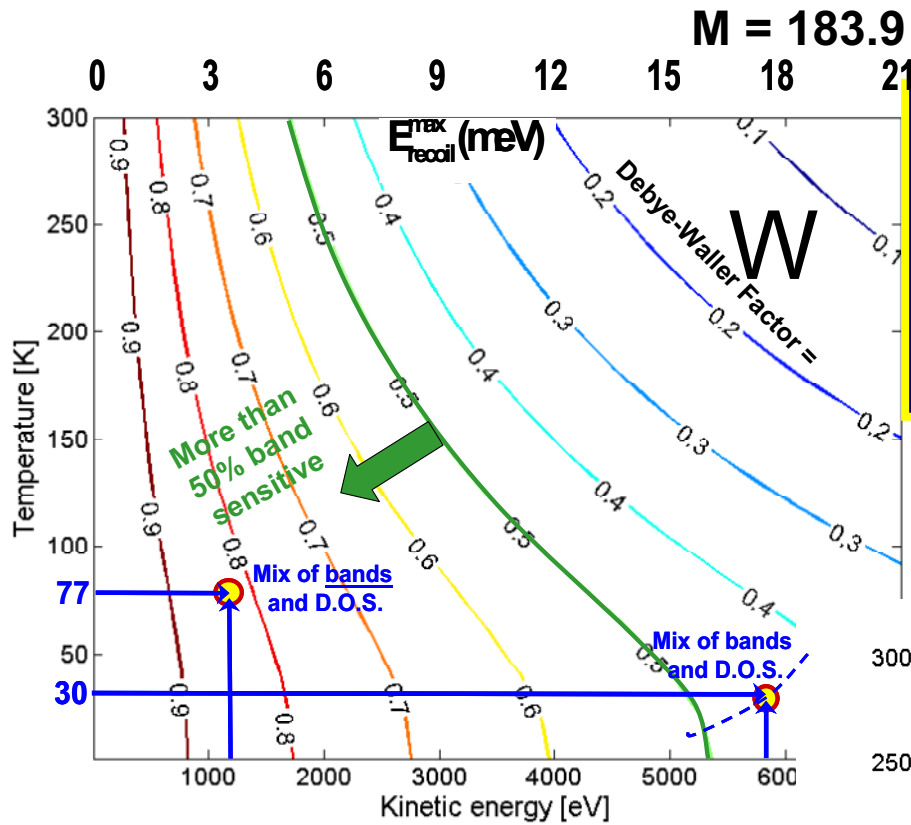
W = 0.45



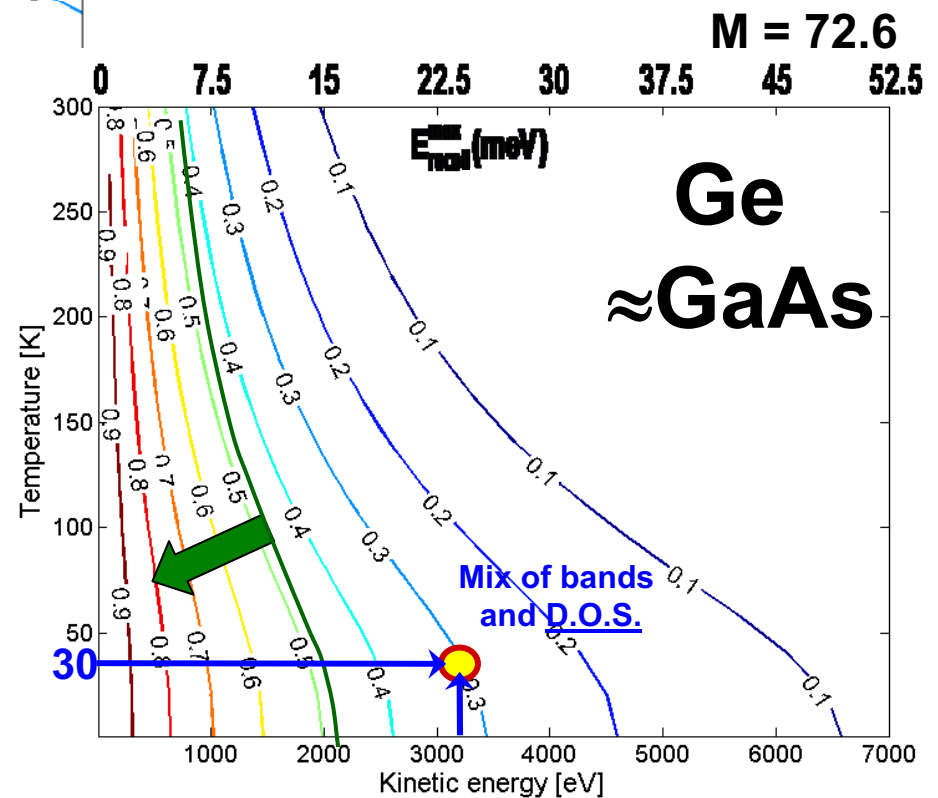
Corrected for phonon-induced density-of-states-like intensity (Bostwick, Papp)



Expt.-Ueda, Kobayashi, SPring8
Data analysis-Papp, Gray, Plucinski, C.F.
Theory-Minar, Braun, Ebert

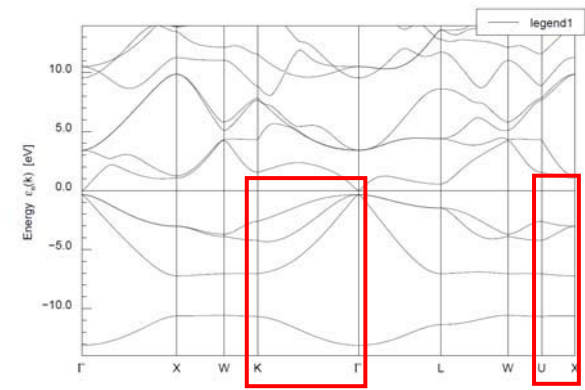
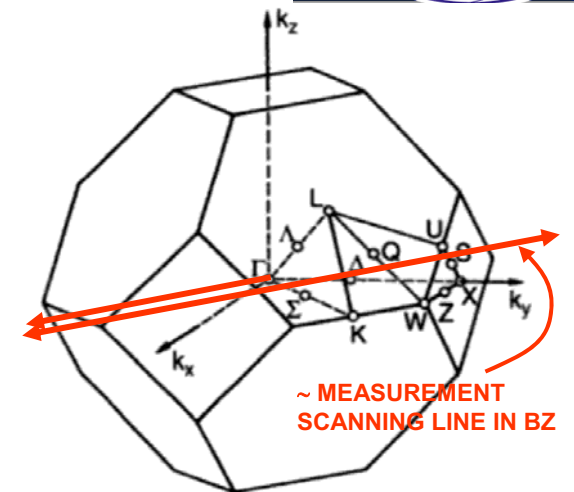
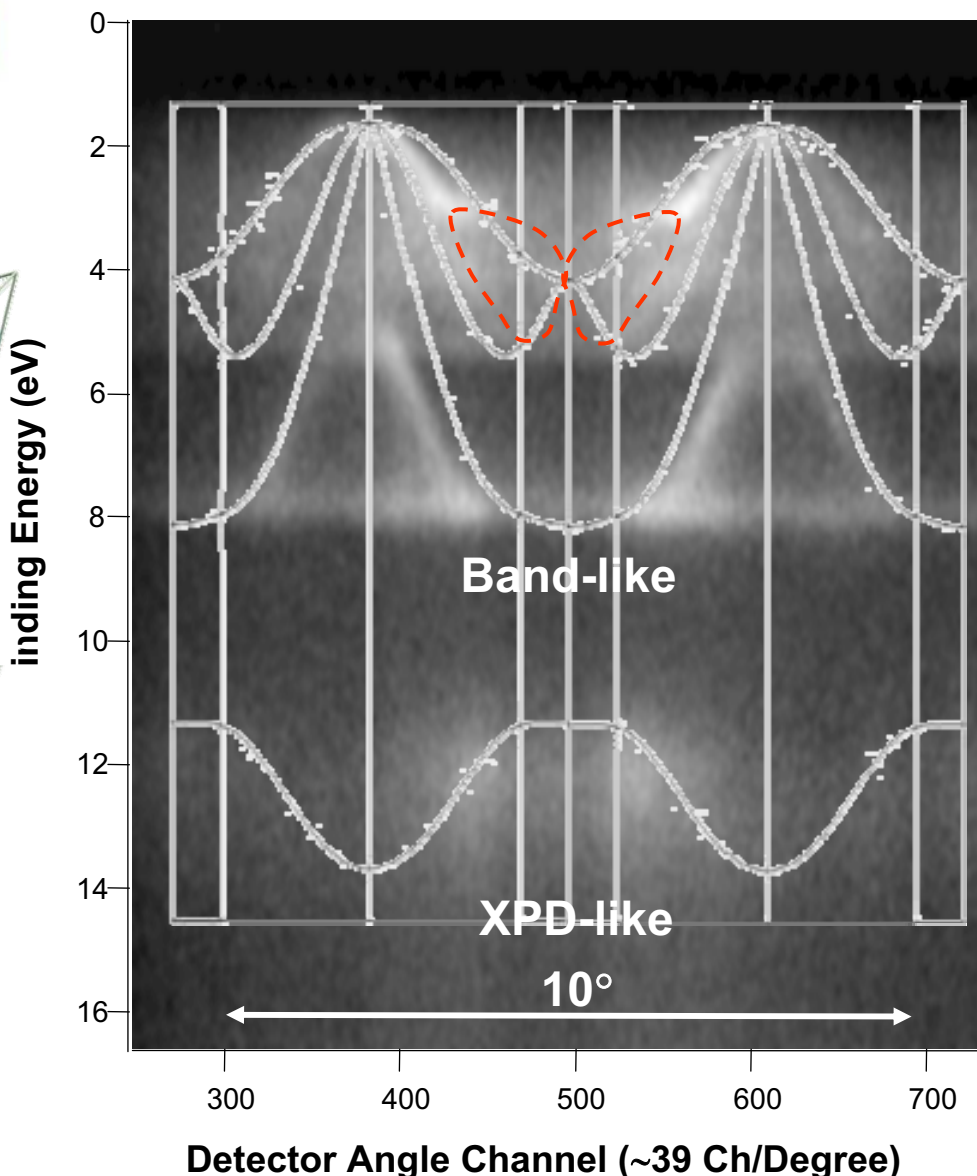
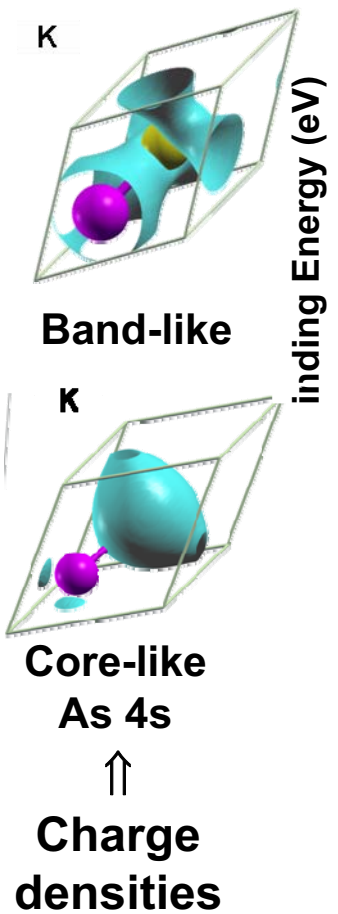


**$W(T, E_{\text{kin}})$ = Approximate
recoil-free
fraction \rightarrow fraction direct
transitions**



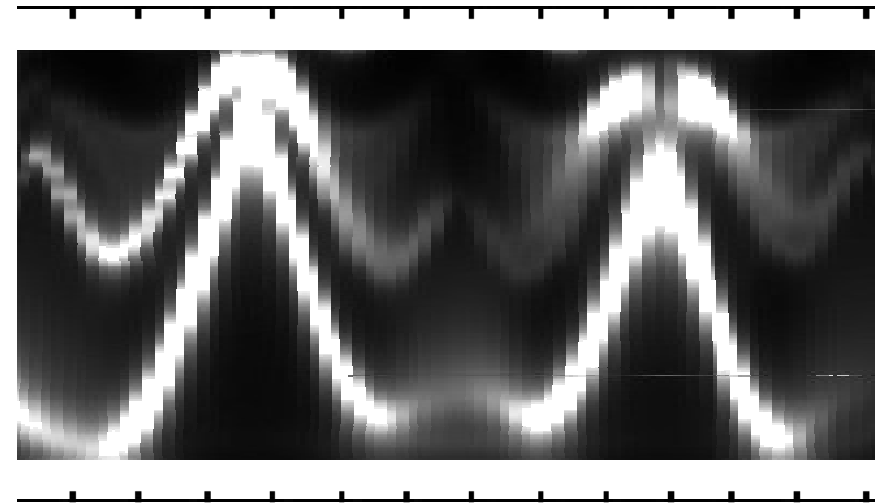
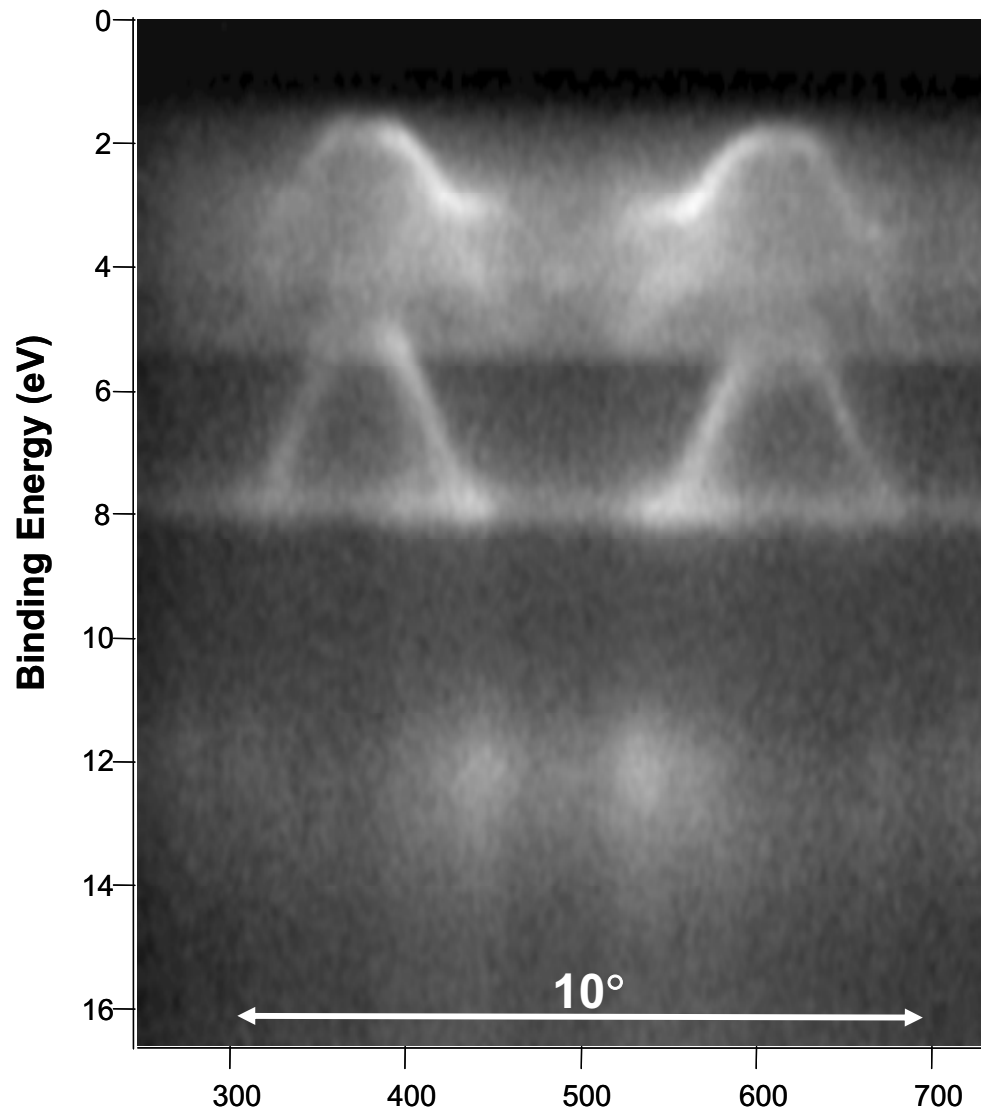
Plucinski

Hard x-ray ARPES from GaAs(001)-3.2 keV, 30 K, W = 0.31



Expt.-Gray, Papp, Ueda, Yamashita, Kobayashi
Theory- Pickett, Ylvisaker

Comparing Experiment and One-Step KKR Theory GaAs Valence Bands

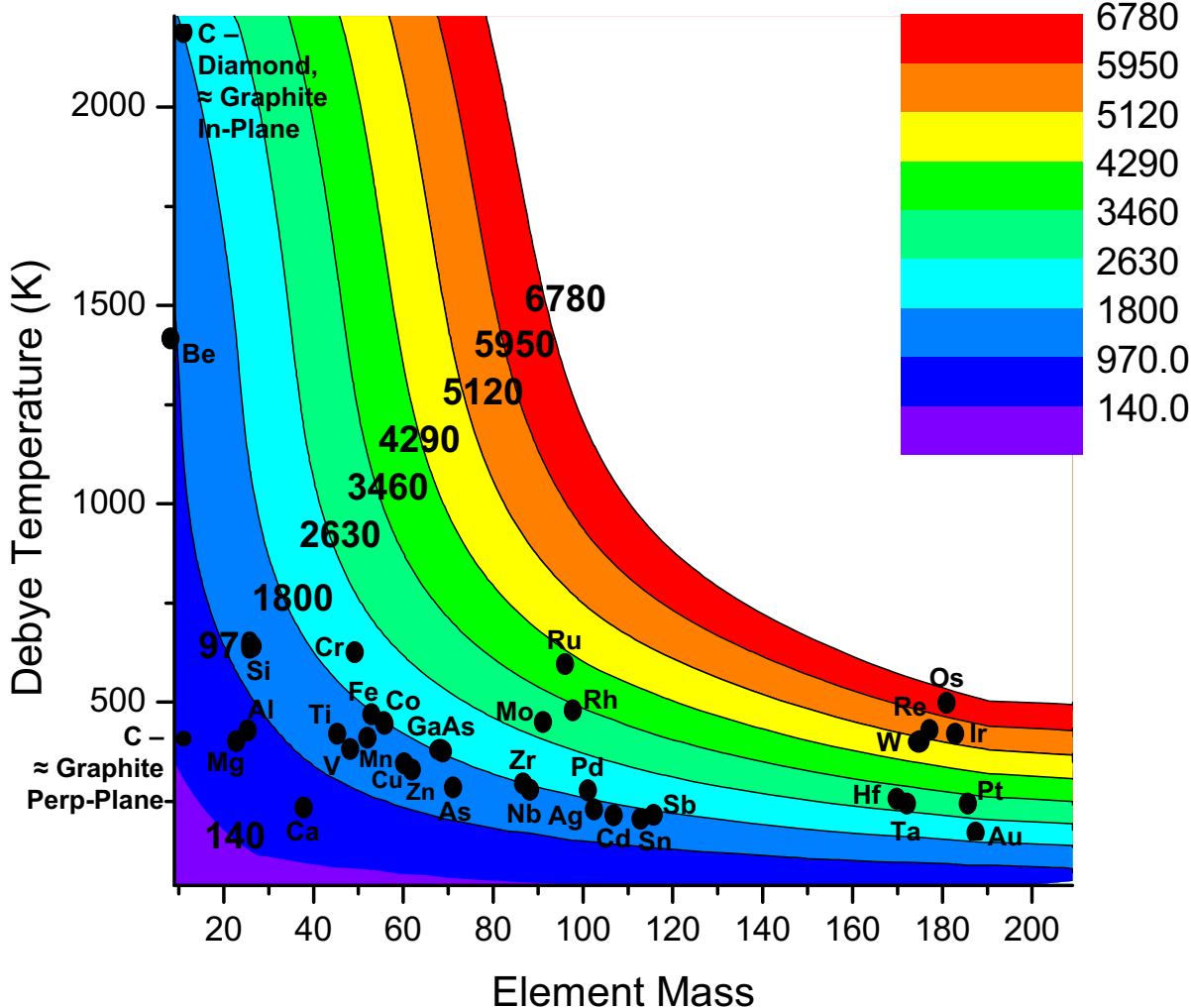


One-step theory-Minar, Braun, Ebert

Expt.-Gray, Papp, Ueda, Yamashita, Kobayashi

Looking ahead-conservatively Photon energies yielding DW factors of 0.5 at 20 K

Photon energy for D-W = 0.5



Plucinski, Gray

Outline

Surface, interface, and nanoscience—short introduction

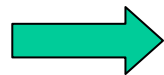
Some surface concepts and techniques→photoemission

Synchrotron radiation: experimental aspects

Electronic structure—a brief review

**The basic synchrotron radiation techniques:
more experimental and theoretical details**

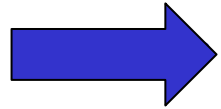
Valence-level photoemission



Core-level photoemission

**Photoemission with high ambient pressure
around the sample**

Outline



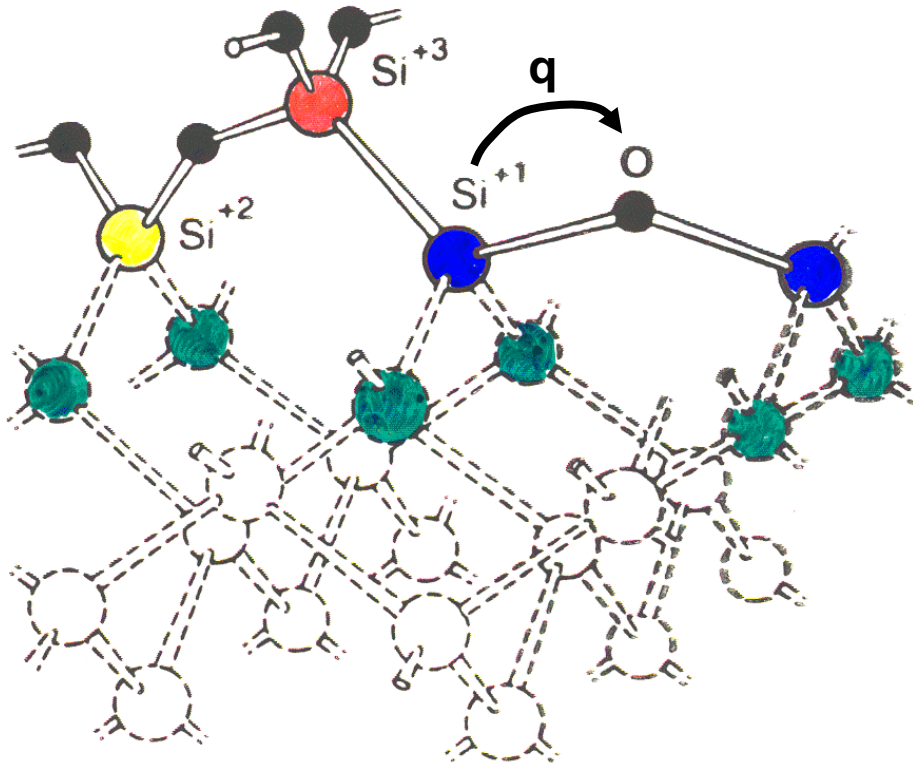
Core-level chemical shifts: the potential model

- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
- Multiplet splittings
- Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons
- Magnetic circular dichroism (MCD) in core-level emission
- Non-magnetic circular dichroism in core-level emission: a.k.a. circular dichroism in angular distributions (CDAD)
- Various other final state effects providing information in core-level spectra

Looking into the silicon dioxide layer with photoelectron spectroscopy

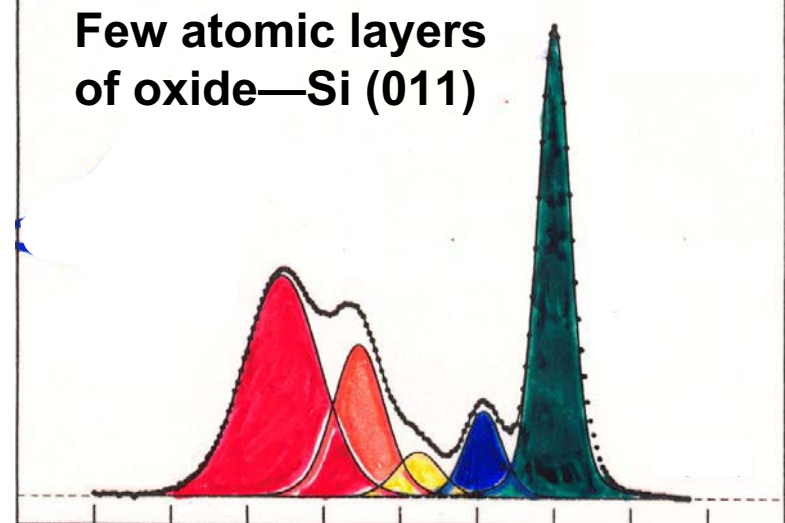
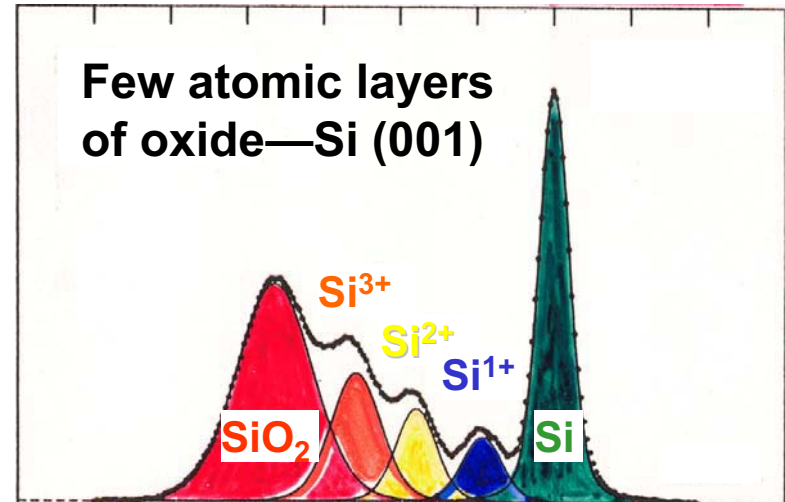
Charge transfer, $e^- - e^-$ coulomb integral:

$$\text{Shift} \approx q_{\text{Si}} J_{\text{Si}2p, \text{Si}3p} = \int \varphi_{2p}^*(\vec{r}_1) \varphi_{3p}^*(\vec{r}_2) \frac{e^2}{r_{12}} \varphi_{2p}(\vec{r}_1) \varphi_{3p}(\vec{r}_2) dV_1 dV_2$$



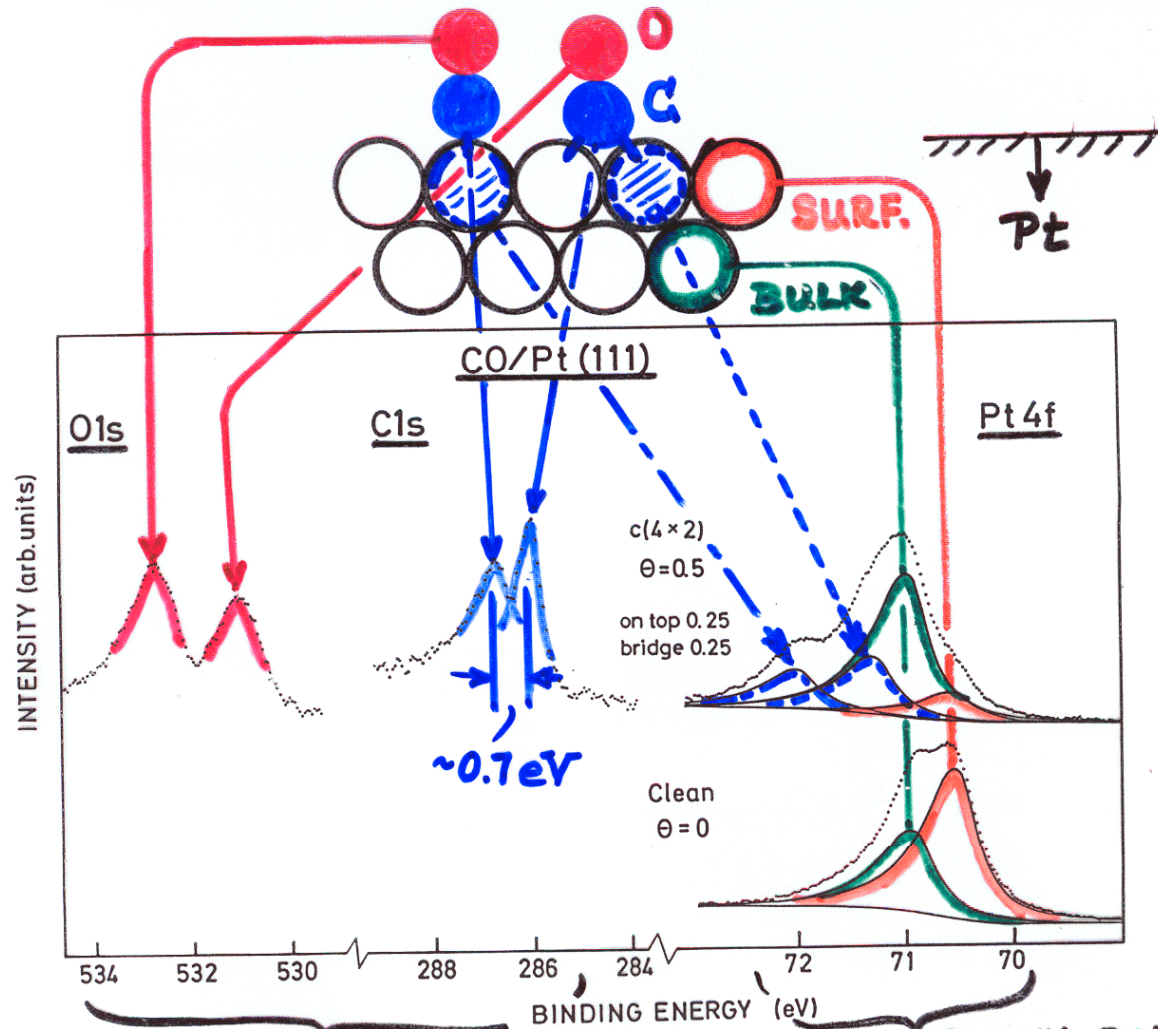
Himpsel et al., Phys. Rev. B 38, 6086 ('88)

No. of photoelectrons from the silicon 2p level



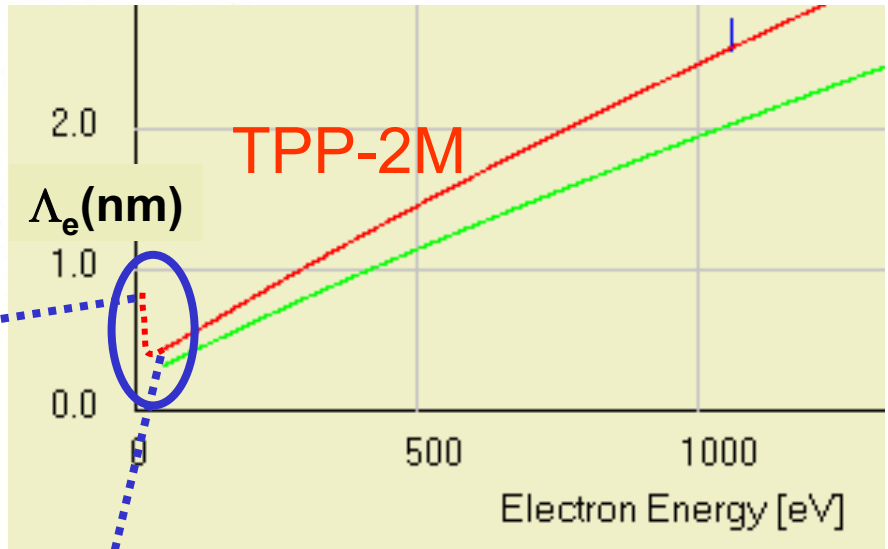
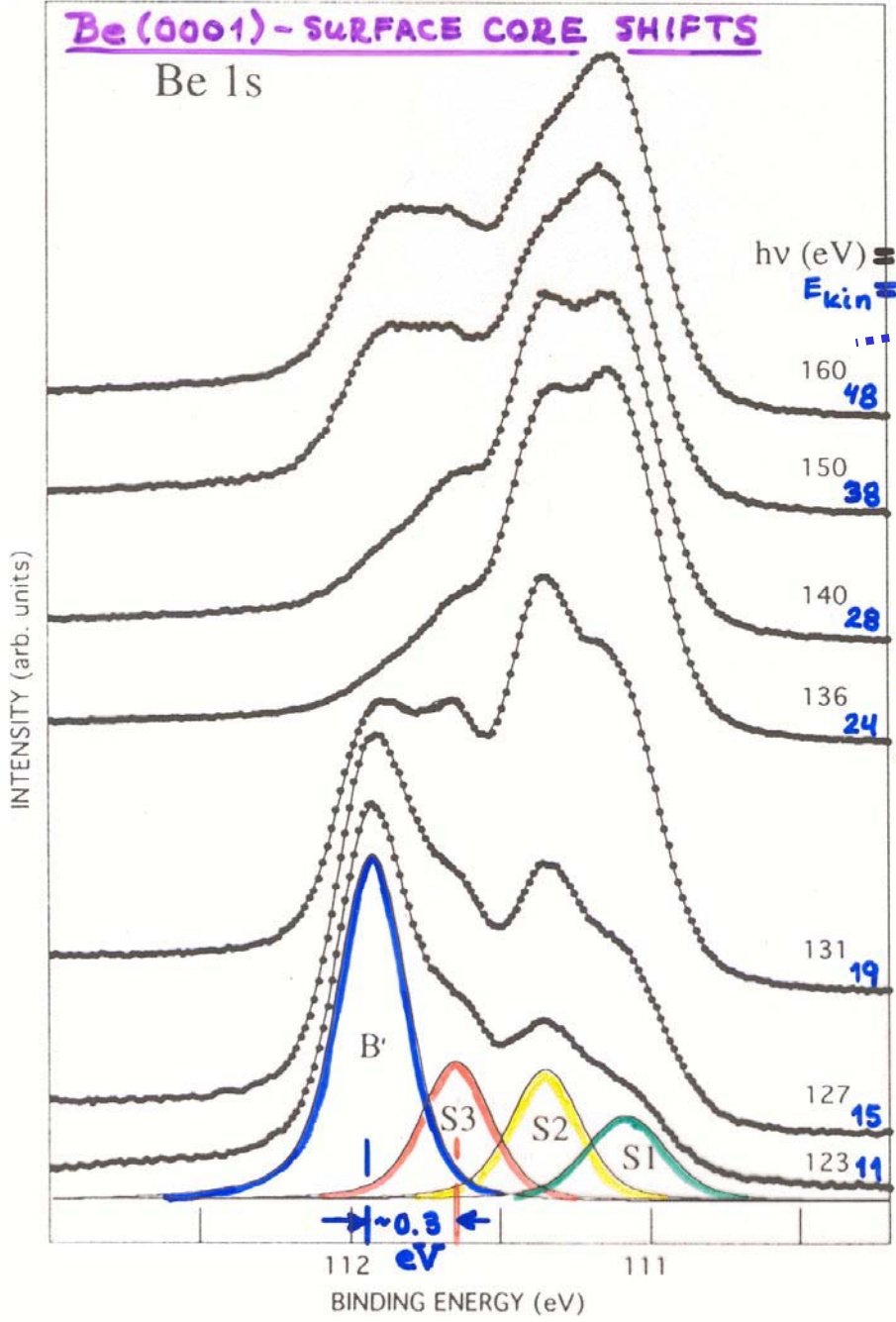
-7 -6 -5 -4 -3 -2 -1 0 1 2 3
Relative energy (in electron-volts)

CHEMICAL SHIFTS IN ADSORBATE & SUBSTRATE

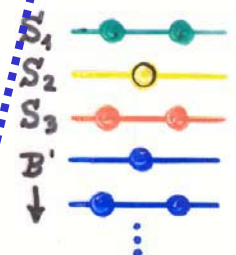


**BJÖRNE HOLM
ET AL.
(NILSSON GRP.,
UPPSALA)**

Be (0001) - SURFACE CORE SHIFTS



MINIMUM IN e^- ESCAPE DEPTH



JOHANSSON ET AL., P.R.L. 71, 2453 (1993)

What does the hole do?

BINDING ENERGIES + KOOPMANS' THEOREM:

N - e^- SCH. EQN. — $\hat{H}(N)\Psi_j(N) = E_j(N)\Psi_j(N), j=1,2,\dots$

MINIMIZE $E_j(N) \left\{ \begin{array}{l} \Psi_j \approx \Phi_j = \text{SLATER DET.} \end{array} \right.$

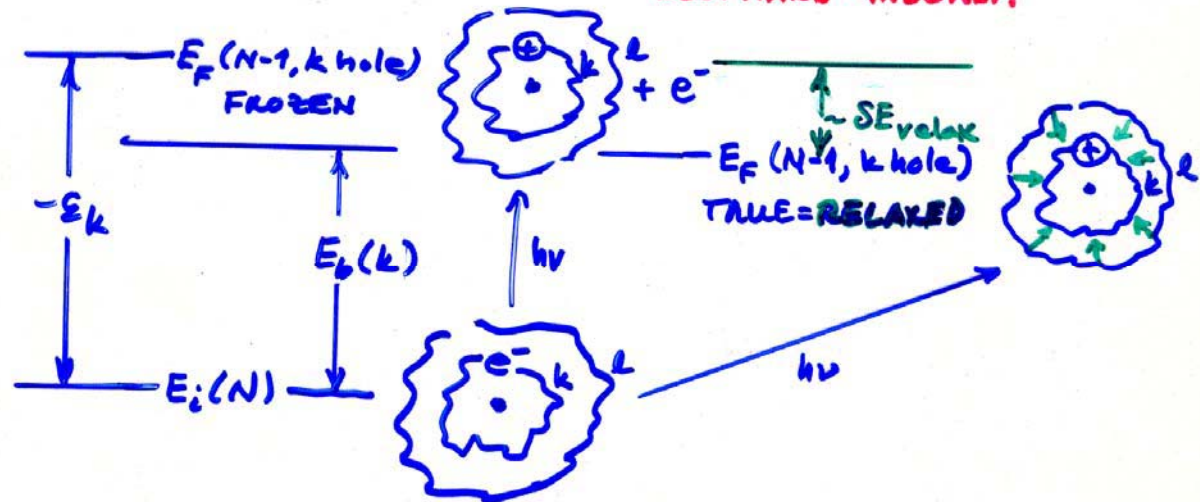
$N-1$ - e^- HARTREE-FOCK EQNS. — $\hat{H}(1)\psi_k(1) = \epsilon_k(1)\psi_k(1)$

- COUPLED INTEGRO-DIFF.
- COULOMB + EXCHANGE

$E_b(k) = k^{\text{th}}$ BINDING ENERGY = $E_f(N-1, k \text{ hole}) - E_i(N)$

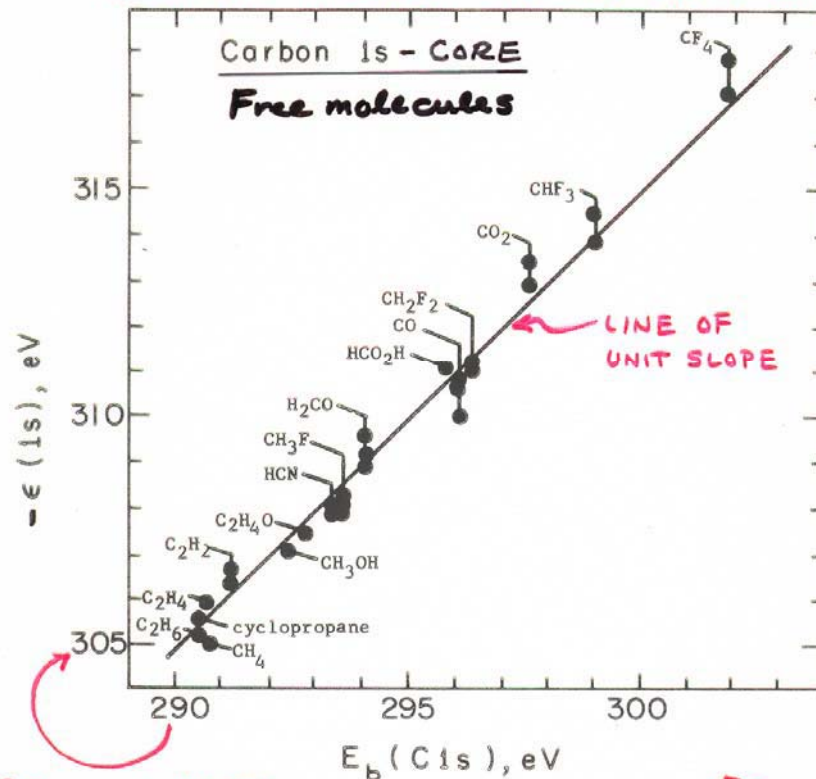
(+) EXACT
OR $E_b(k) = -\epsilon_k$ IF $\psi_{ki} = \psi_{kf}$ (FROZEN ORBITAL)

KOOPMANS' THEOREM



⇒ RELAXATION, SCREENING, CONFIGURATION INTERACTION, SELF-ENERGY EFFECT ALWAYS PRESENT; ANDERSON IMPURITY MODEL ETC.

KOOPMANS' THEOREM CALCULATION OF SHIFTS



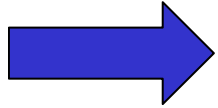
$$DIFF. = \Delta E_{relax} \approx 15 eV \approx \text{CONSTANT} \approx 5\% \text{ OF } E_b^V$$

$$\rightarrow \Delta E_b (C 1s, "1" - CH_4) = -\Delta E_{C 1s, "1" - CH_4}$$

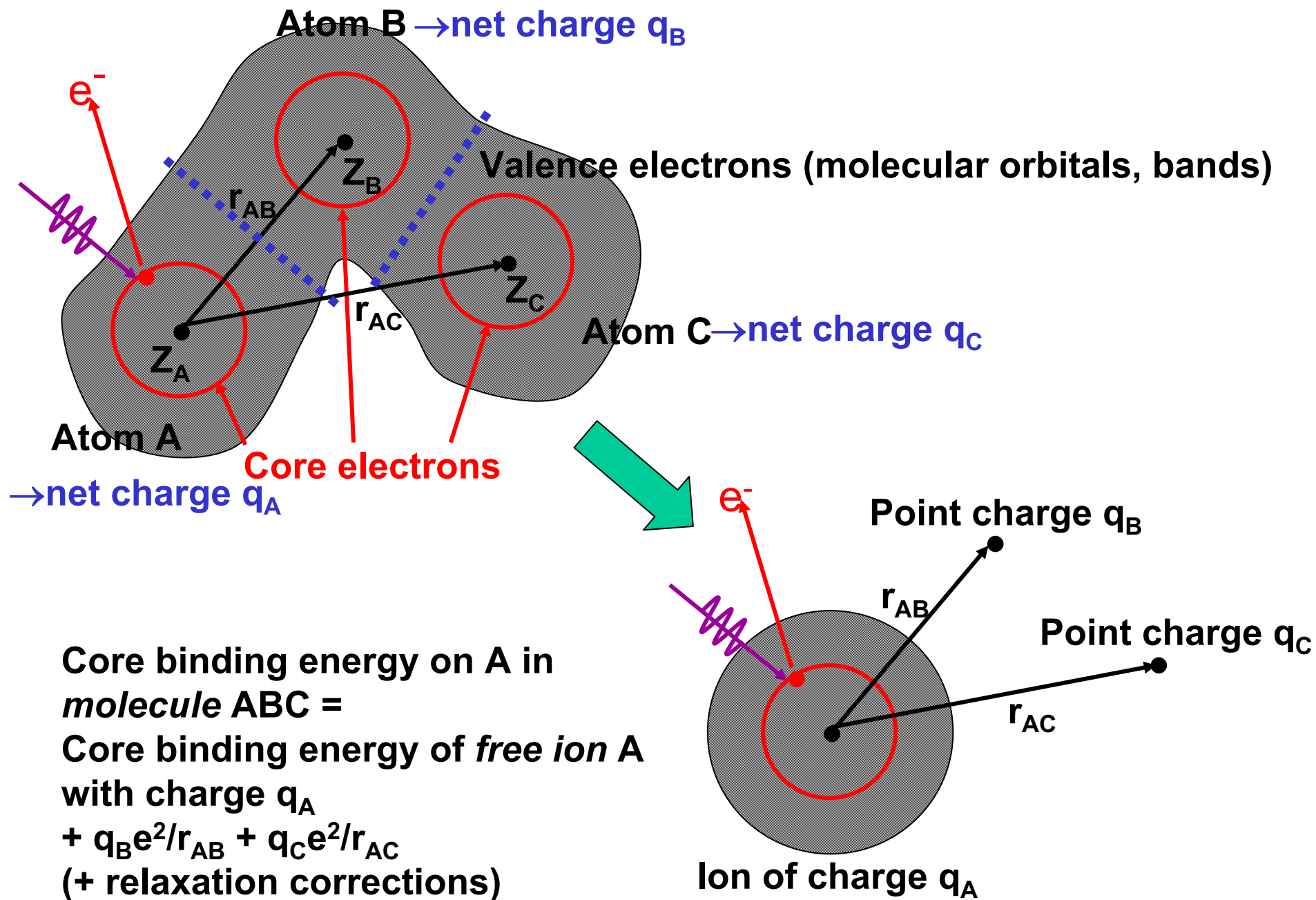
Figure 18 -- Plot of carbon 1s binding energies calculated via Koopmans' Theorem against experimental binding energies for several carbon-containing gaseous molecules. For some molecules, more than one calculated value is presented. The slope of the straight line is unity. The two scales are shifted with respect to one another by 15 eV, largely due to relaxation effects. All of the theoretical calculations were of roughly double-zeta accuracy or better. (From Shirley, reference 7.)

Outline

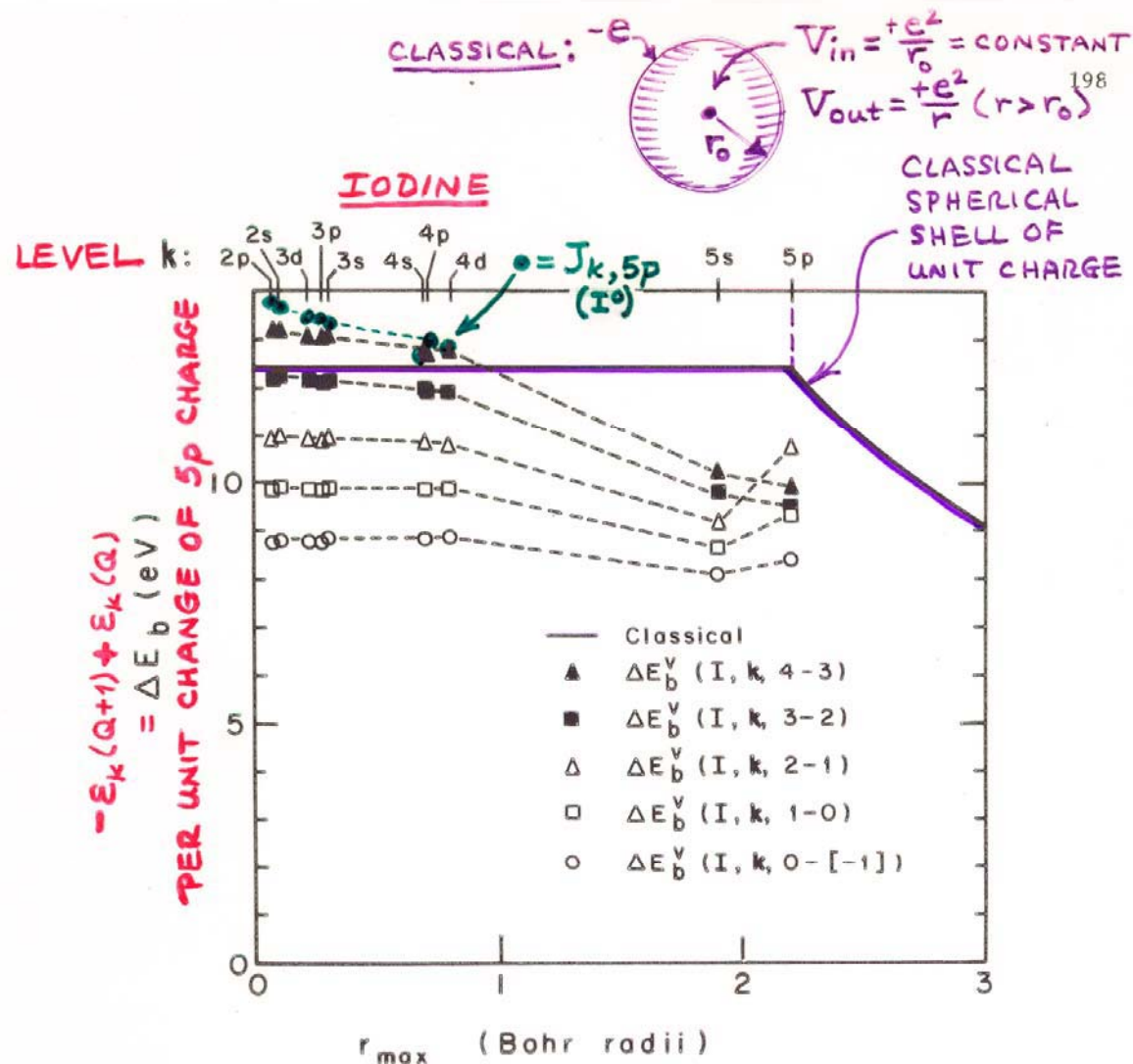
- Core-level chemical shifts: the potential model
- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
- Multiplet splittings
- Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons
- Magnetic circular dichroism (MCD) in core-level emission
- Non-magnetic circular dichroism in core-level emission: a.k.a. circular dichroism in angular distributions (CDAD)
- Various other final state effects providing information in core-level spectra



POTENTIAL MODEL FOR CORE-LEVEL CHEMICAL SHIFTS



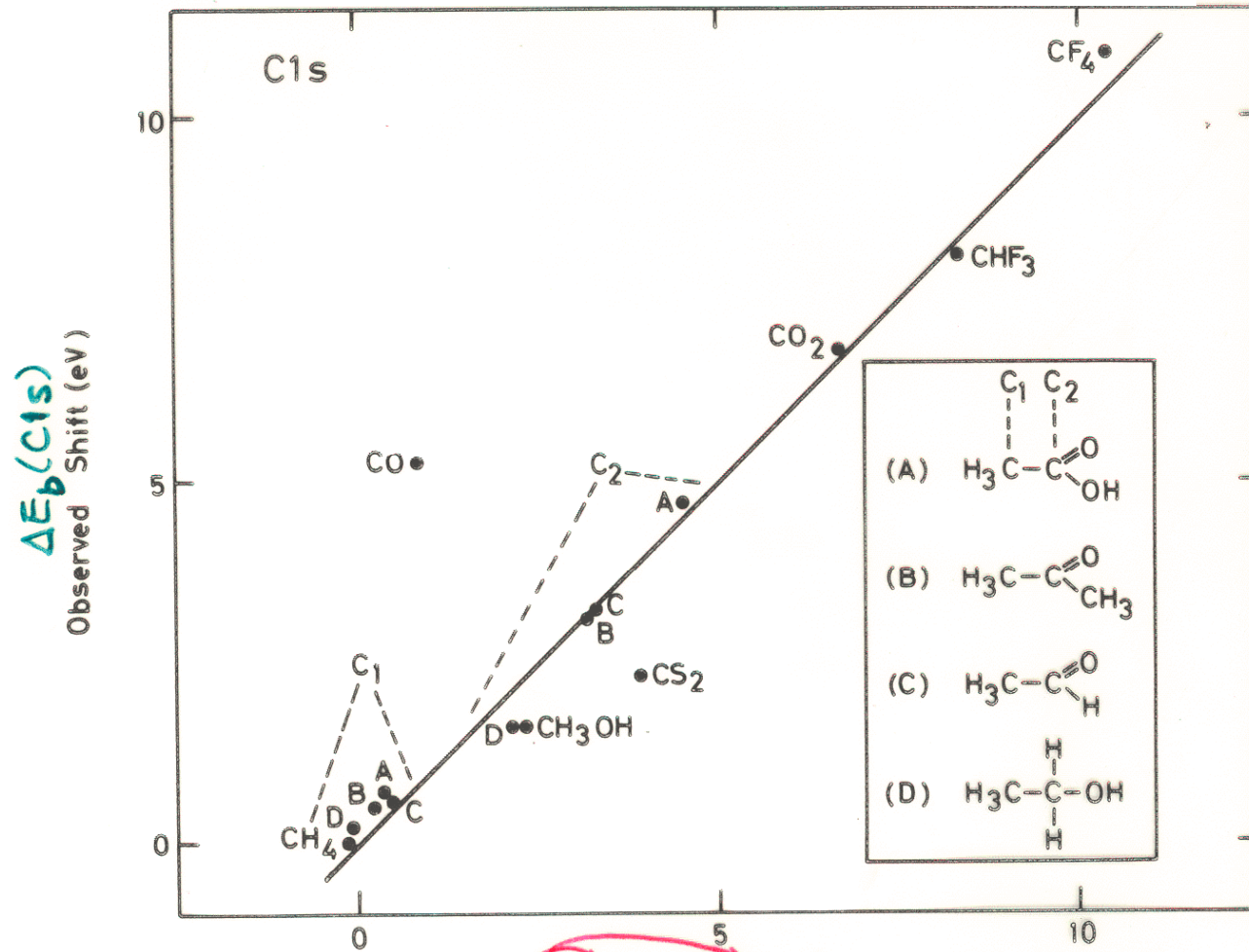
**FREE-ION
(INTRAAOMIC)
ASPECTS OF
SHIFTS:
Koopmans'
THEOREM &
CLASSICAL
CHARGED SHELL**



⇒ REMOVAL/ADDITION OF VALENCE e^-
 CHARGE IN BONDING SHIFTS ALL
 INNER $e^- E_b$ 'S $\approx E_k$ 'S BY SAME AMOUNT

“Basic Concepts of XPS”
 Figure 19


POTENTIAL MODEL CALCULATION OF CARBON CHEMICAL SHIFTS



$C_A q_A + V + I$ (eV)
 $(\sum q_i / r_{Ai}, q_i$'s FROM CNDO
 THEORY
 EMPIRICAL:
 $C_A = 21.9$ eV
 $\approx J_{1s, valence}$
 $I \approx 0.80$ eV

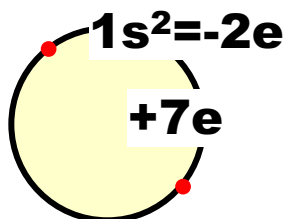
“Basic Concepts of XPS”
Figure 24

Outline

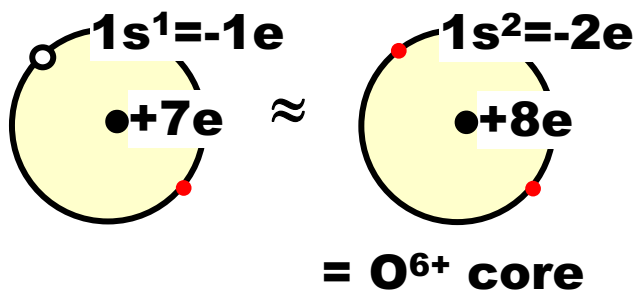
- Valence-band spectra: low-energy UPS limit and high-energy XPS limit
- Core-level chemical shifts: the potential model
-  • Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
- Multiplet splittings
- Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons
- Magnetic circular dichroism (MCD) in core-level emission
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- Various other final state effects providing information in core-level spectra

CORRELATION OF THERMOCHEMICAL DATA WITH CHEMICAL SHIFTS: EQUIVALENT-CORE OR (Z+1) MODEL

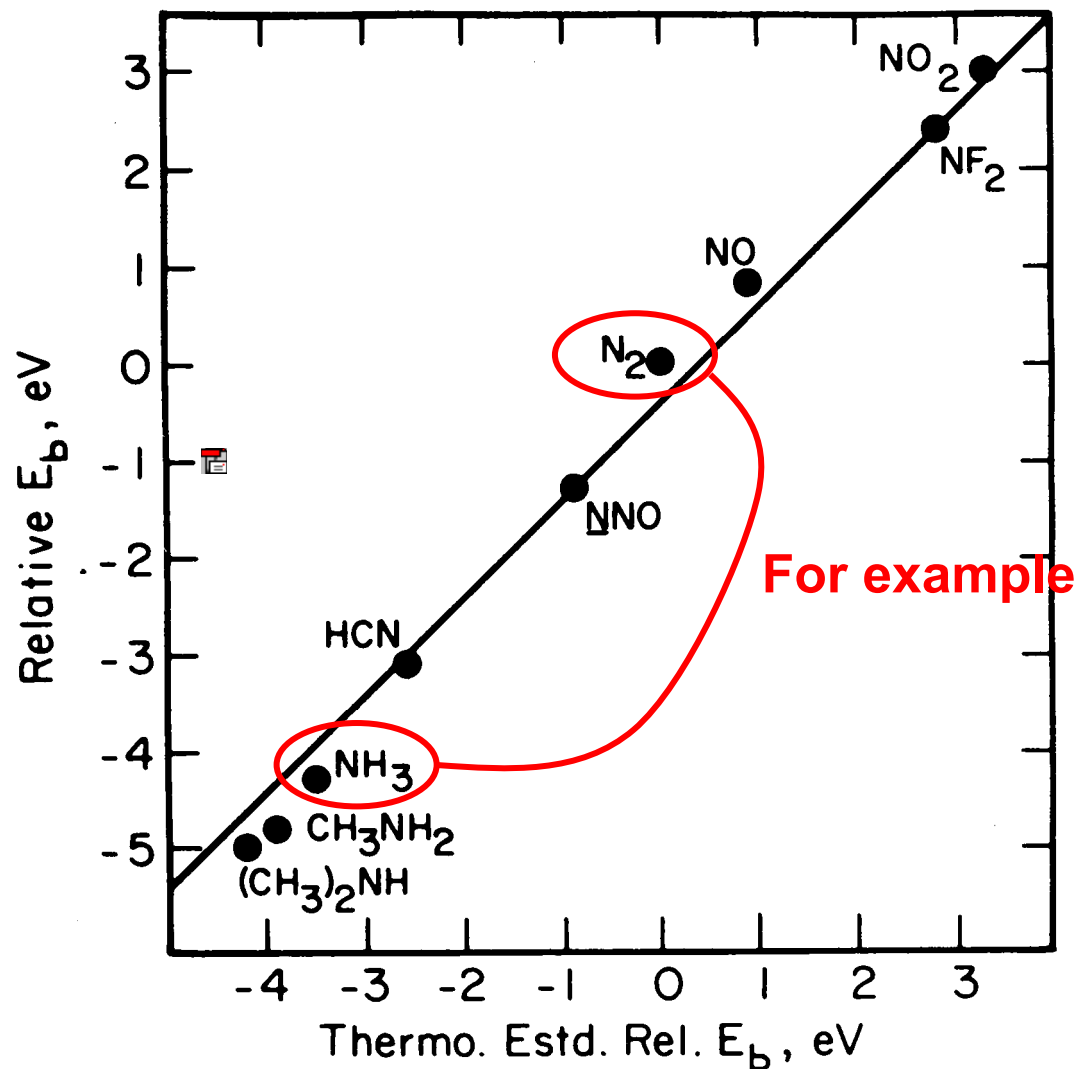
N core = N $1s^2$ = N^{5+}



**Assume:
 N^{6+} core with
1s hole = N^{6+} =**



Plus see pp. 92-93
in "Basic Concepts
of XPS"

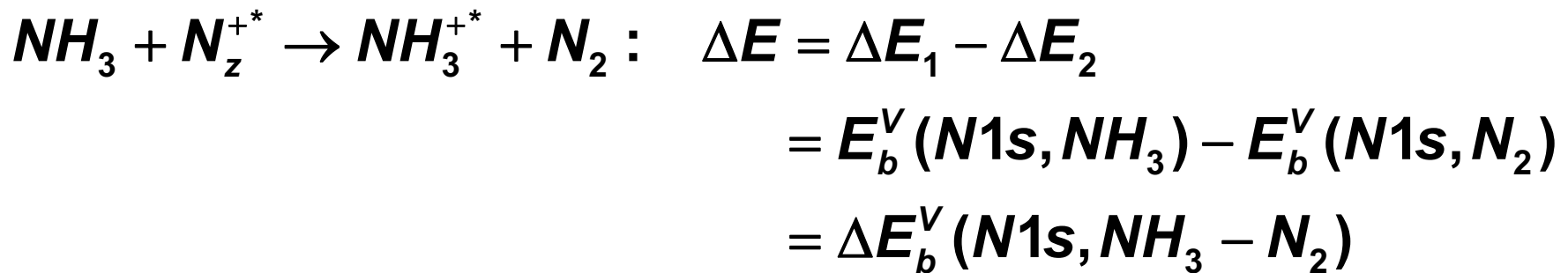


Jolly et al.

Binding energies: * = N 1s core hole present

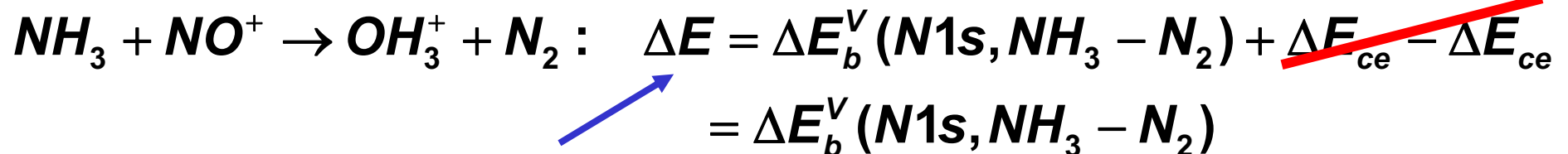


Adding and subtracting:



The chemical shift

Replacing real N 1s core with equivalent O 1s core:

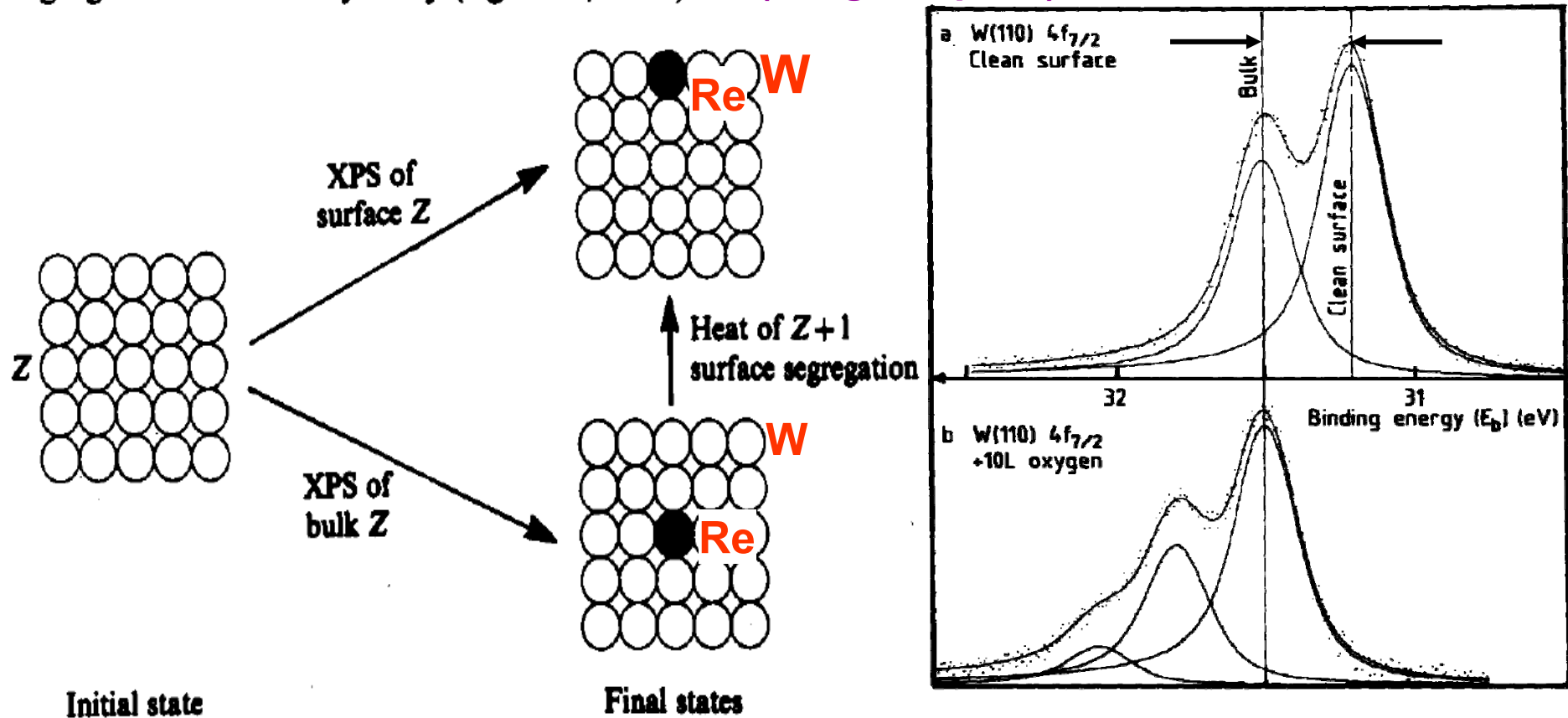


A thermochemical energy

DERIVATION OF HEAT OF SURFACE SEGREGATION FROM SURFACE CORE-LEVEL CHEMICAL SHIFTS

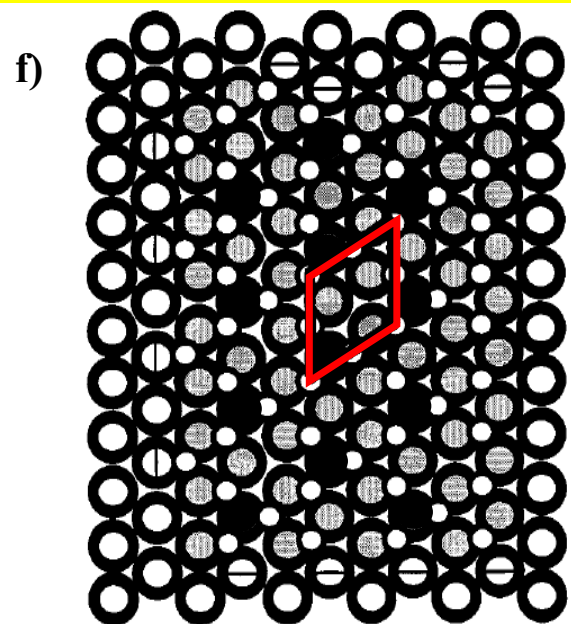
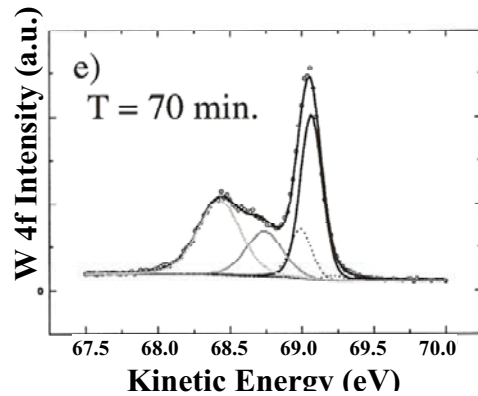
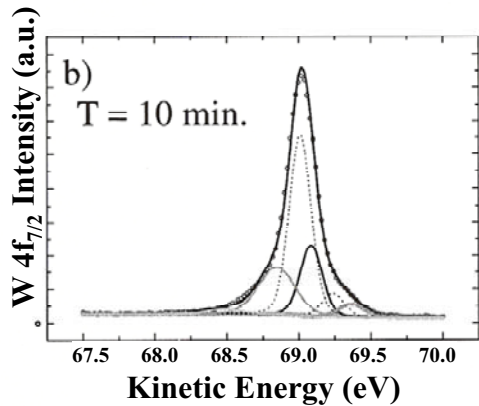
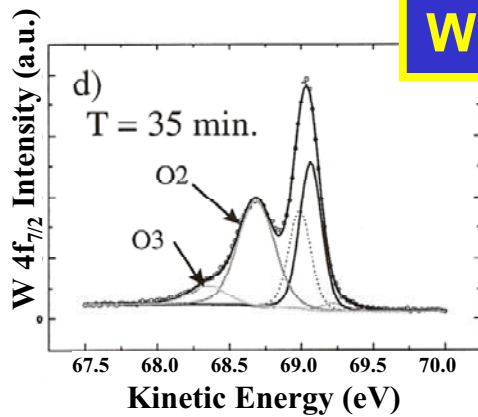
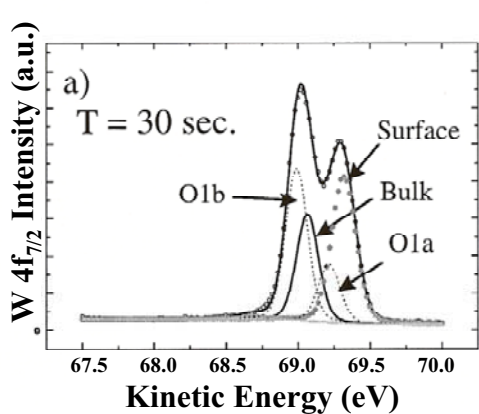
Fig. 4.30. The XPS surface core level shift approach to the heat of segregation of a binary alloy (Egelhoff, 1983). (Zangwill, p. 87)

$$\Delta E_b = \Delta H_{\text{surf. segregation}}$$

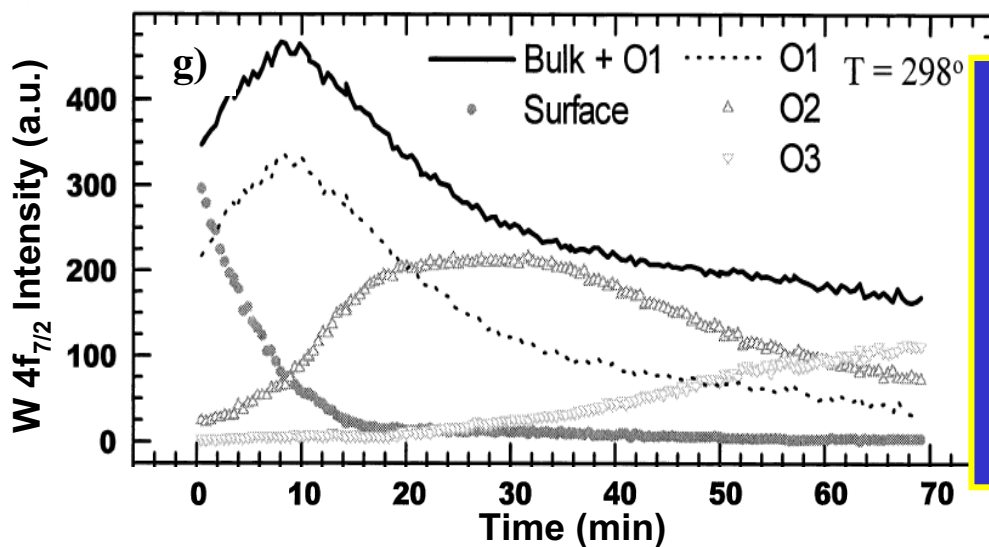
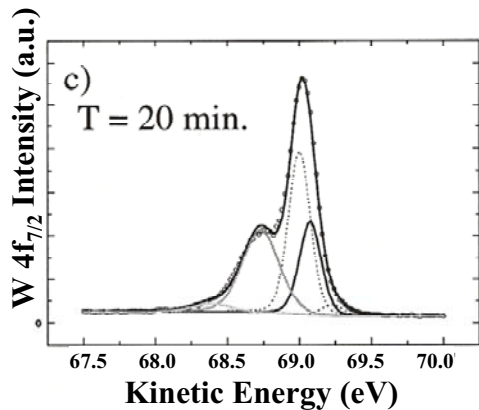
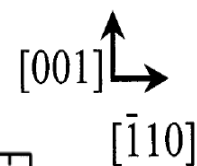


Spanjaard et al., Surf. Sci. Repts. 5, 1 (1985)

W(110)/O—W 4f_{7/2} Chemical Shifts




- Oxygen
- Surface
- ⊖ O1a
- ⊖ O1b
- ⊙ O2
- O3



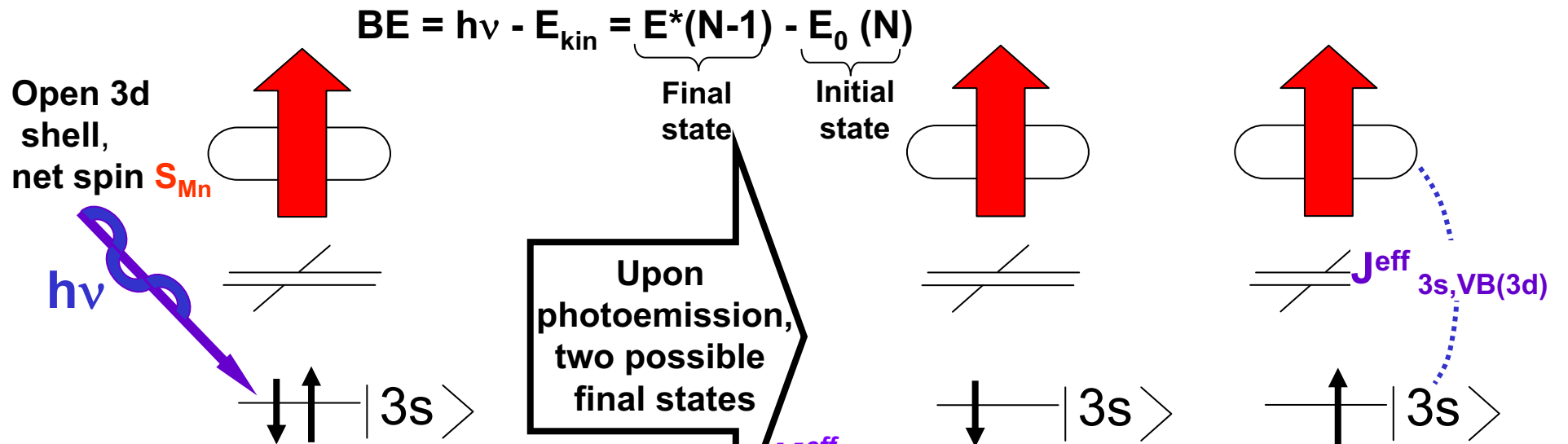
An early time-resolved reaction study (more later)

Ynzunza et al.,
Surf. Sci. 459 (2000) 69

Outline

- Valence-band spectra: low-energy UPS limit and high-energy XPS limit
- Core-level chemical shifts: the potential model
- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
-  Multiplet splittings and magnetism
- Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons
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Multiplet splitting in core levels of transition metal oxides



The splitting between the two peaks is given by

$$\Delta E_{3s} \approx (2S_{Mn} + 1) K_{3s,VB(3d)}^{eff} \quad (\text{Van Vleck Theorem})$$

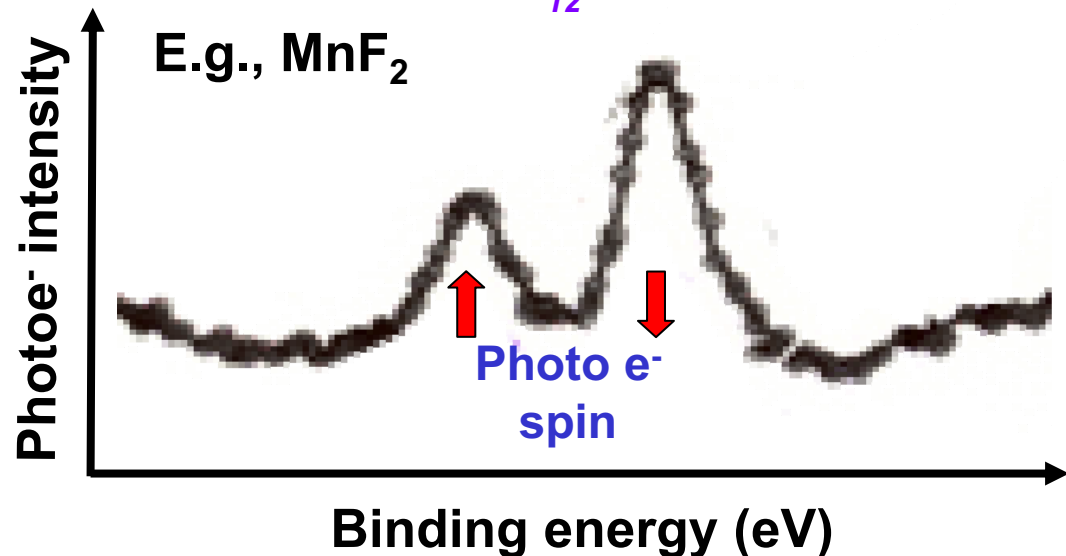
For the cubic manganites in simplest doping model,

$$S_{Mn} = 1/2(4-x) \rightarrow$$

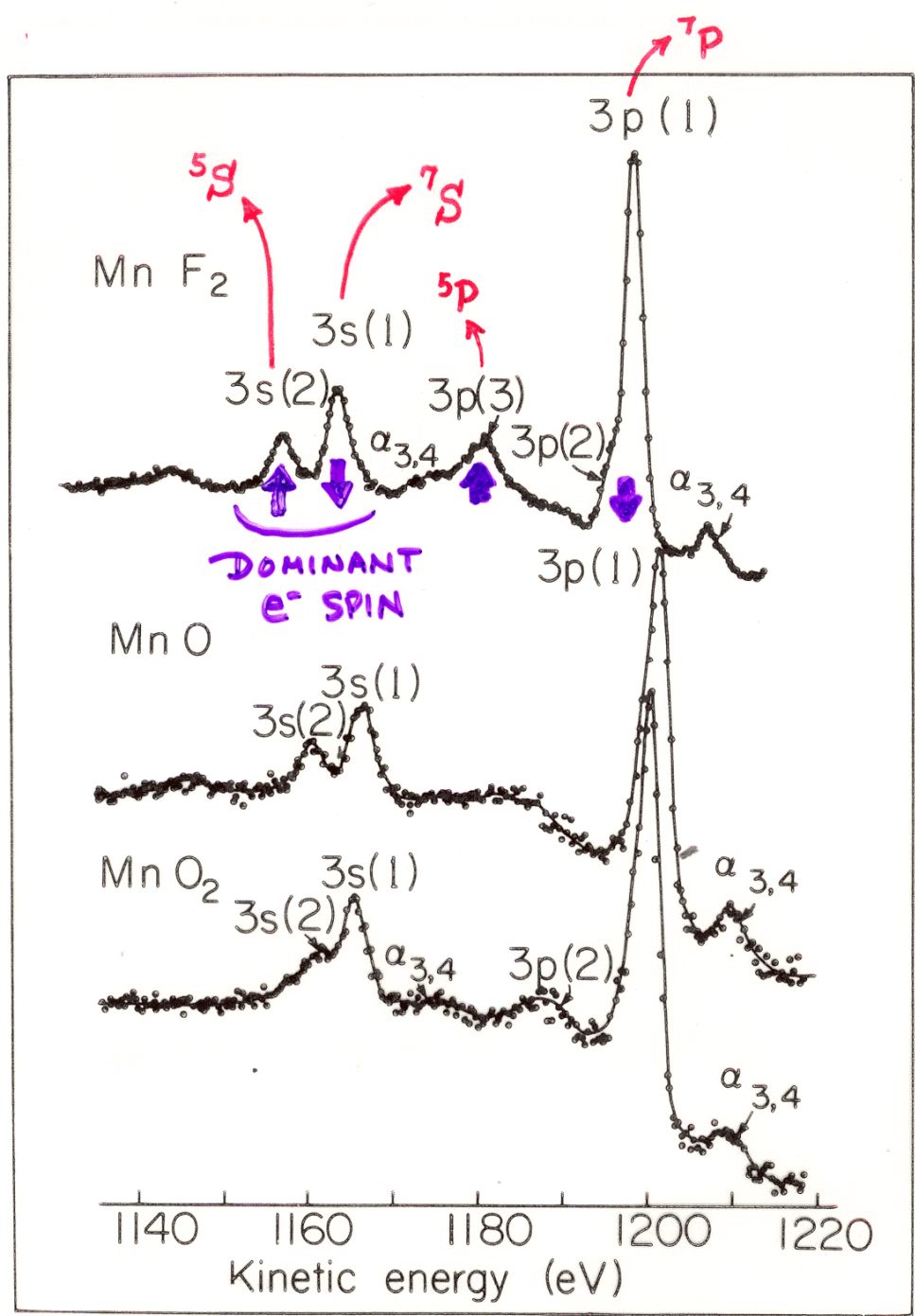
$$\Delta E_{3s} \approx [5-x] K_{3s,VB(3d)}^{eff}$$

with $K_{3s,VB}^{eff} \approx 1.1 \text{ eV}$

$$\int \varphi_{3s}(\vec{r}_1) \varphi_{3d}(\vec{r}_2) \frac{e^2}{r_{12}} \varphi_{3d}(\vec{r}_1) \varphi_{3s}(\vec{r}_2) dV_1 dV_2$$

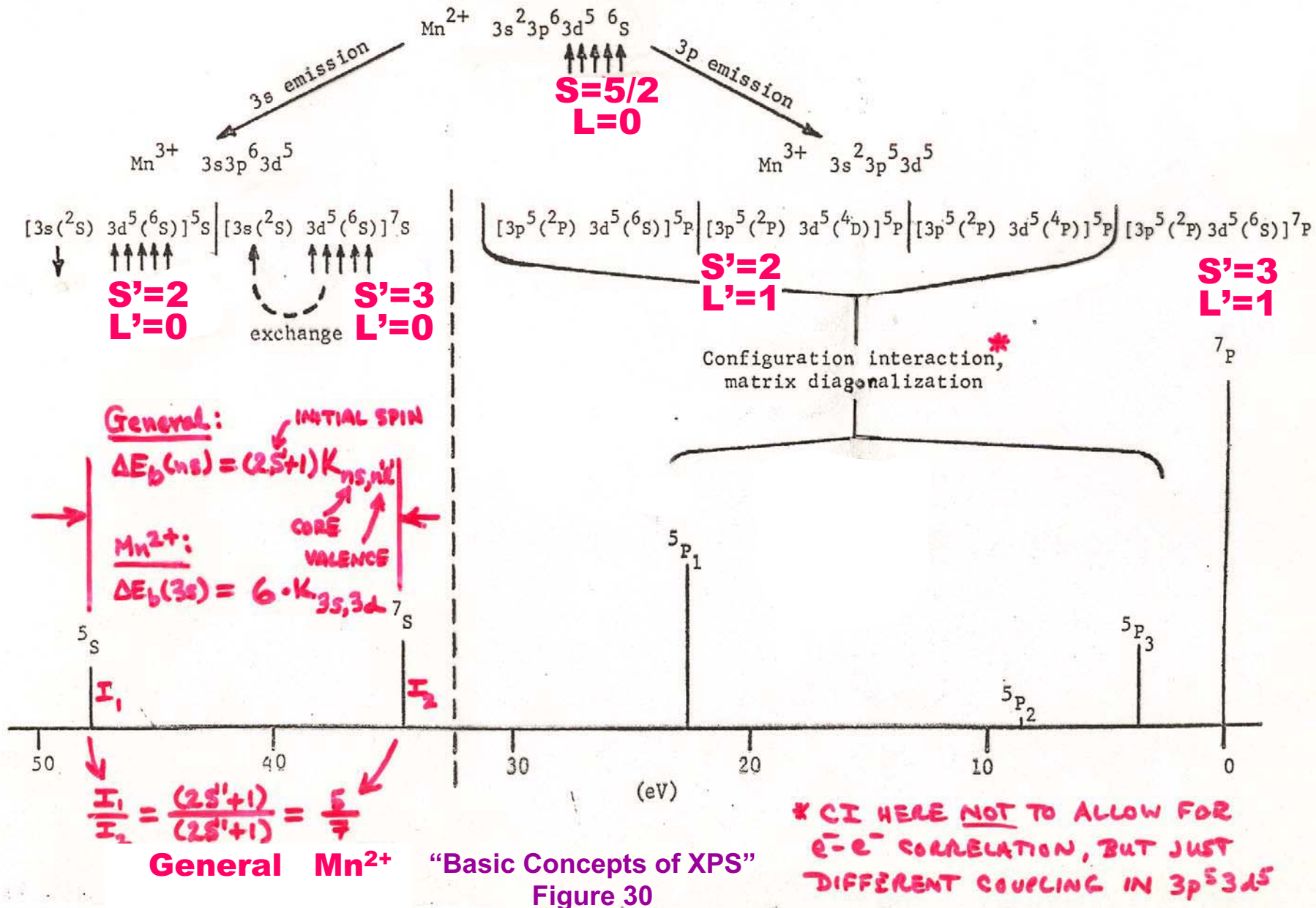


CORE-LEVEL MULTIPLY SPLITTINGS IN Mn COMPOUNDS



“Basic Concepts of XPS”
Figure 31

ORIGIN OF MULTIPLLET SPLITTINGS IN Mn²⁺: "ONE-ELECTRON" THEORY

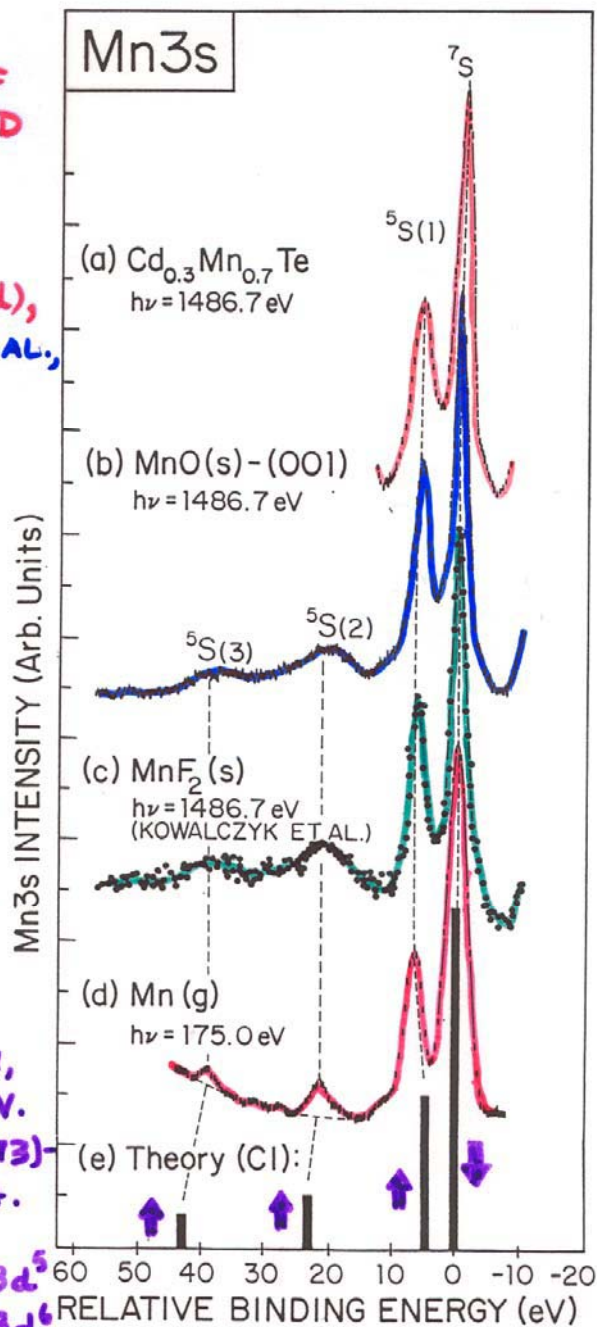


"Basic Concepts of XPS"
Figure 30

* CI HERE NOT TO ALLOW FOR e⁻-e⁻ CORRELATION, BUT JUST DIFFERENT COUPLING IN 3p⁵3d⁵

**COMPARISON OF
GAS-PHASE AND
SOLID-STATE
SPECTRA**

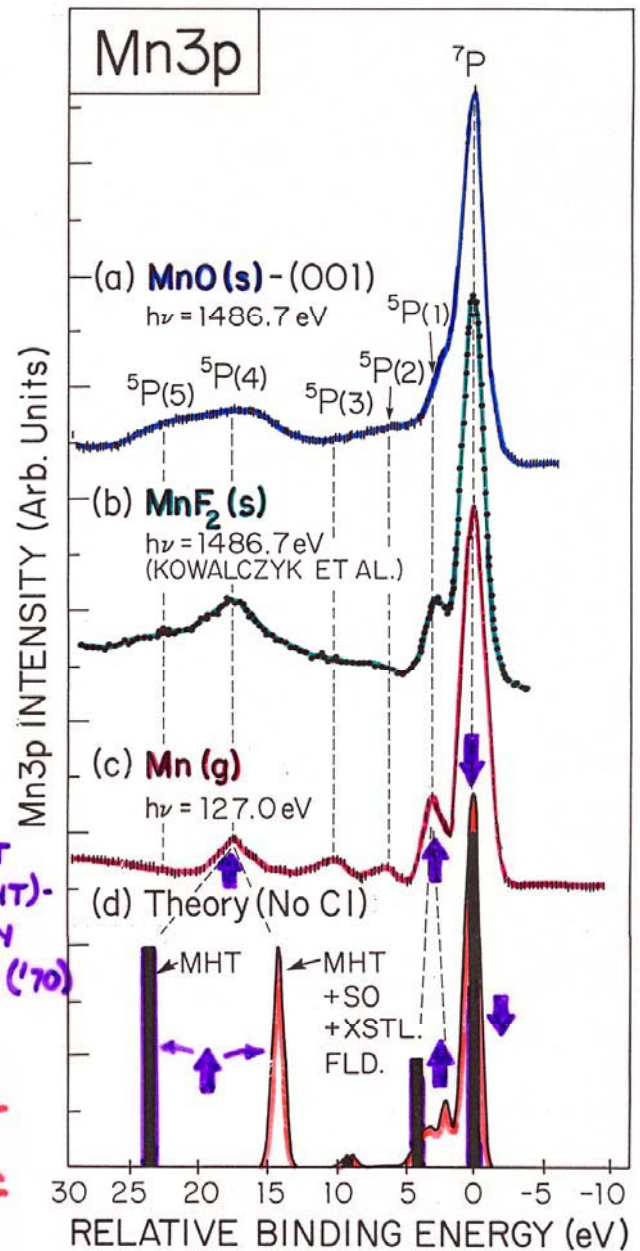
**EXPT. : (a), (b), (d),
HERMSMEIER ET AL.,
PHYS. REV. LETT.
61, 2592 (1988)
(OUR GROUP)**



**Correlation
CI effects:
anti-parallel
electrons**

**THEORY:
BAGUS, FREEMAN,
SASAKI, PHYS. REV.
LETT. 30, 850 (1973)
ATOMIC CONFIG.
INT. IN
 $\text{Mn}^{2+} \dots 3s^2 \dots 3d^5$
 $+ \text{Mn}^{3+} \dots 3s^2 3p^4 3d^6$**

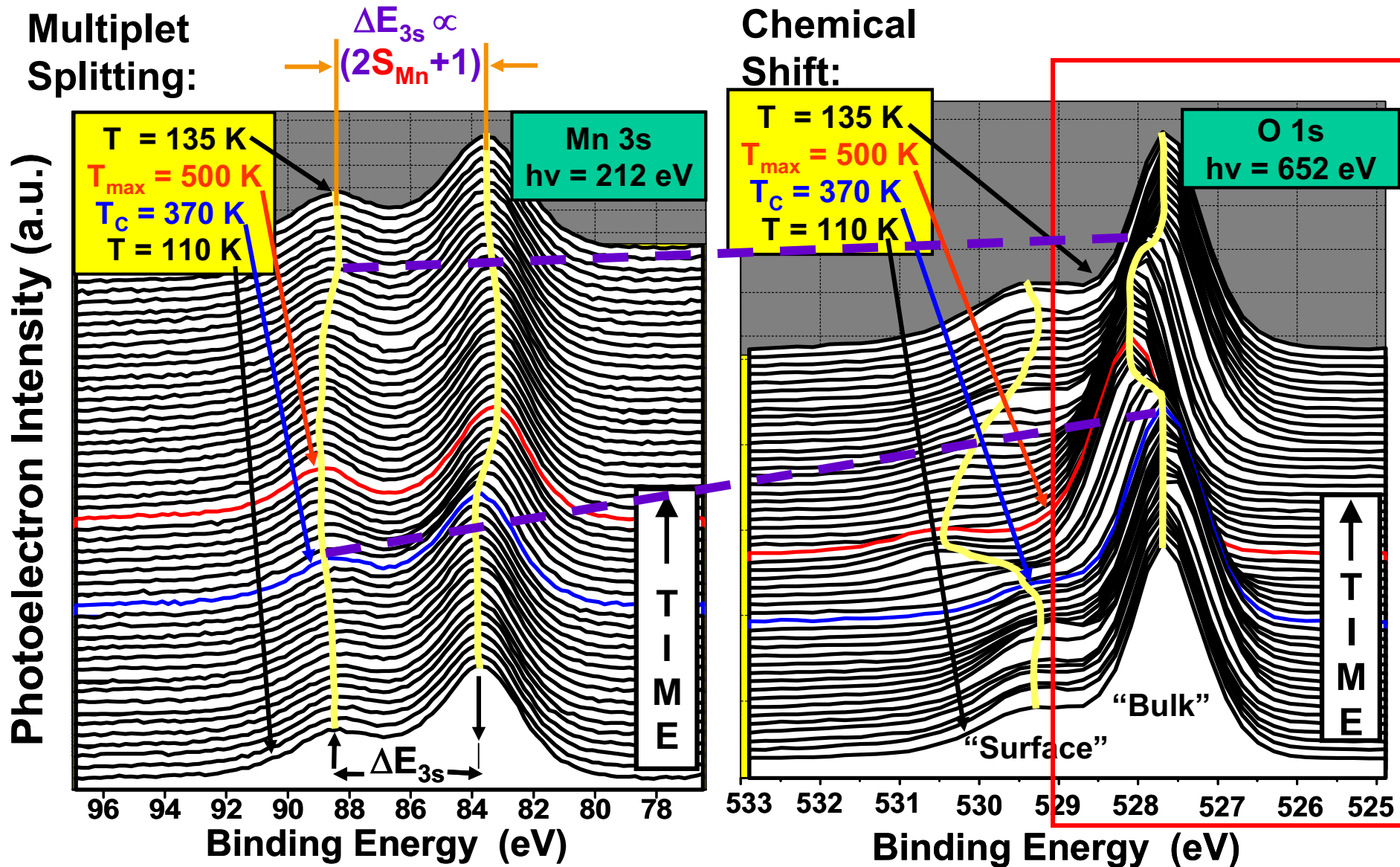
**“Basic Concepts of XPS”
Figure 33**



THEORY: NO CI
**SIMPLE MULTIPLY
 HOLE THEORY (MHT)-
 FADLEY, SHIRLEY
 PHYS. REV. A2, 1109 ('70)**
**EMPIRICAL
 MHT WITH SPIN
 ORBIT & CRYSTAL
 FIELD - SUGANO
 ET AL., J. PHYS. C
 15, 2625 (1982)**

**HERMSMEIER
 ET AL.,
 P.R.L. 61, 2592 ('88)**

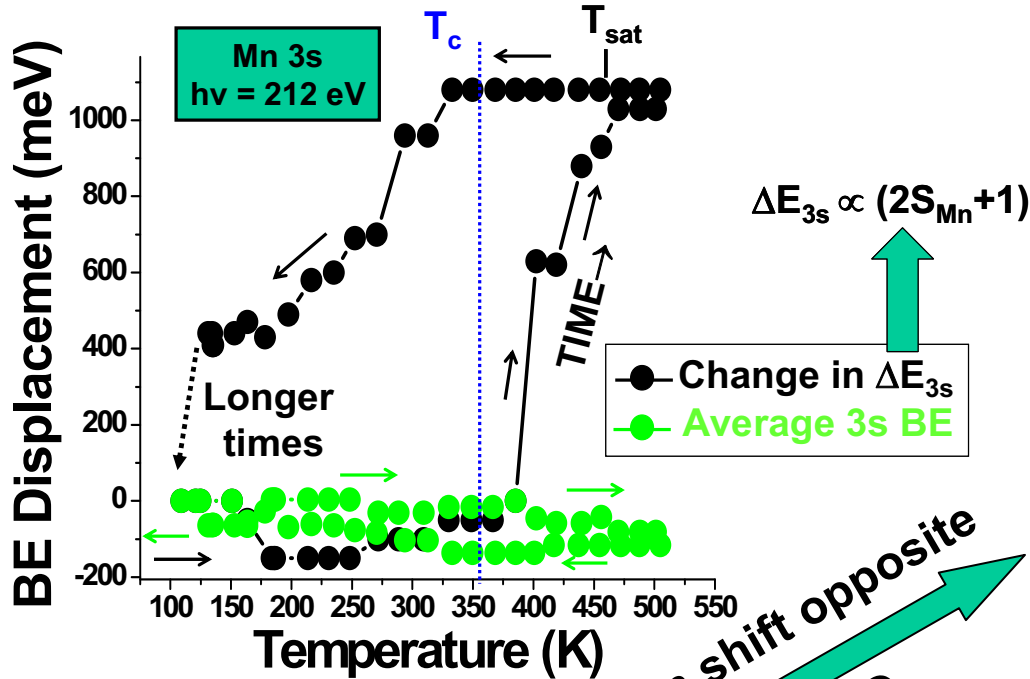
Temperature dependence of Mn3s and O1s spectra in a colossal magnetorestrictive (CMR) oxide: $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$



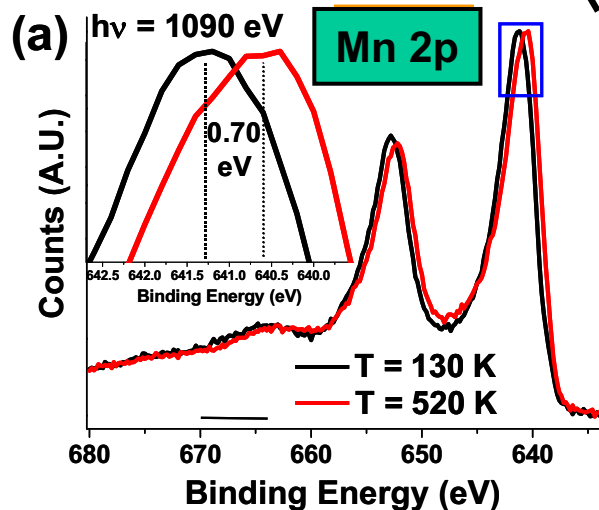
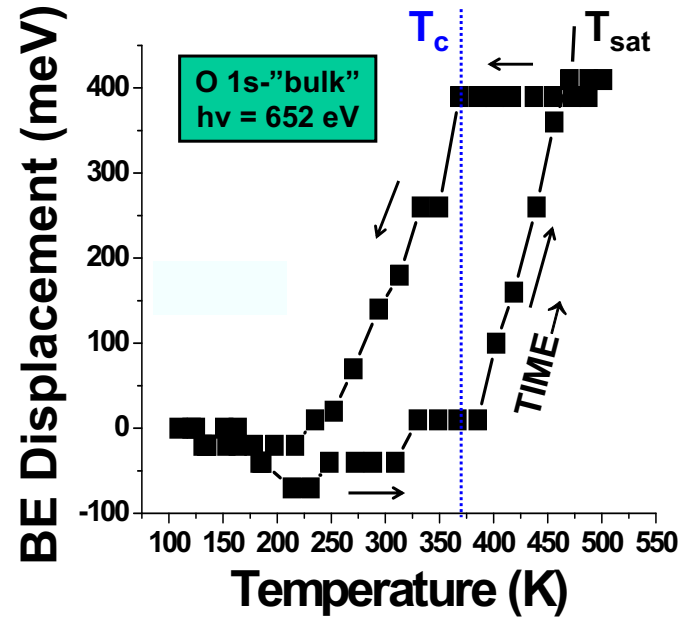
Increase of the Mn3s splitting-reversible

Increase of O1s BE-reversible

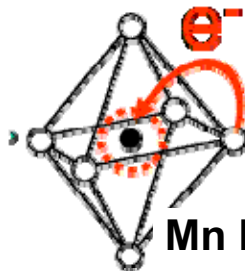
T dependence of Mn 3s binding energies



T dependence of bulk O 1s binding energy



Mn shift opposite
to O

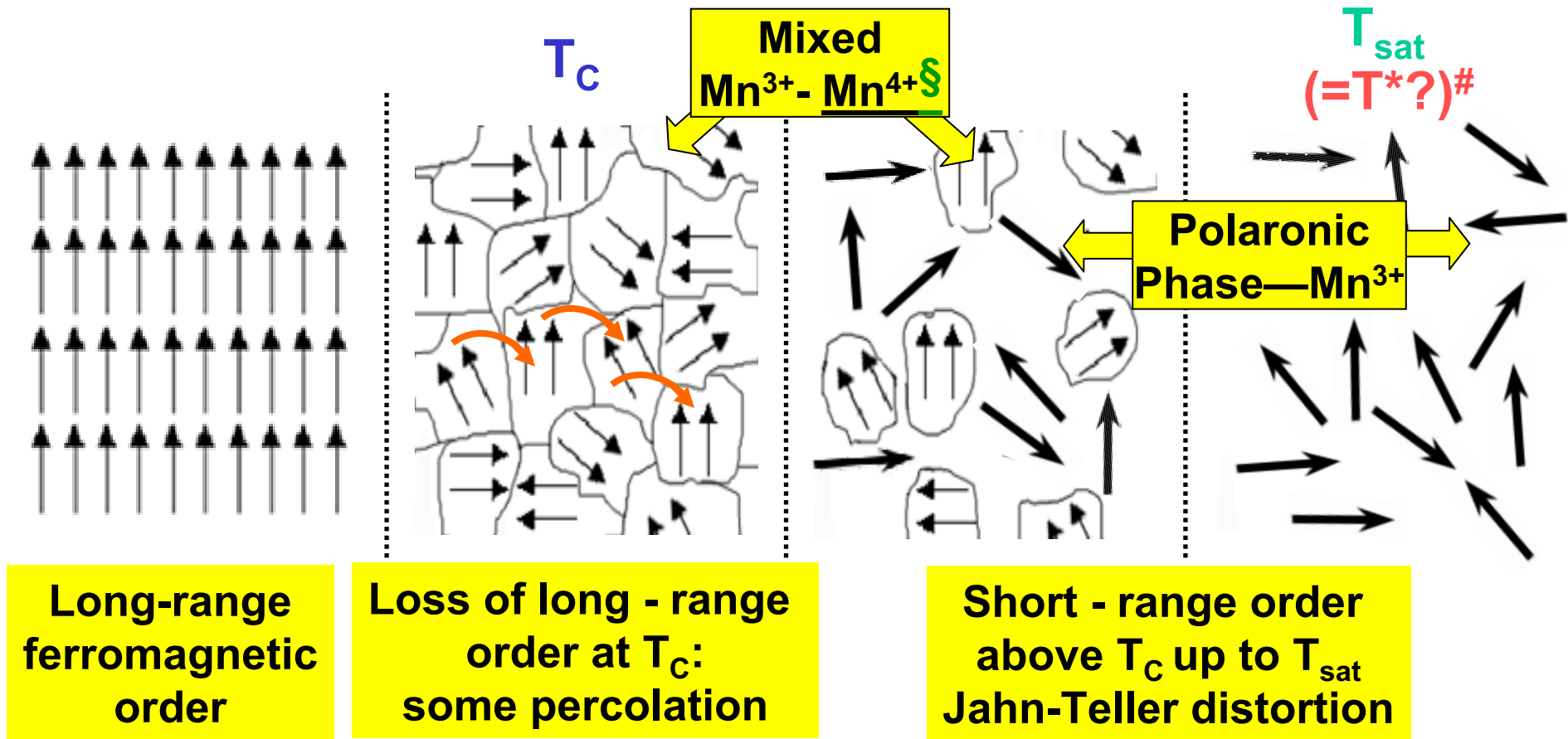


O more positive
Mn higher spin,
more negative

Theory: self-interaction corrected local spin density results for LSMO → elongating octahedron makes Mn³⁺ more stable than Mn⁴⁺
Banach, Temmerman, PRB 69, 054427 ('04)

Mannella et al., Phys. Rev. Lett. 92, 166401 (2004)

Suggested scenario—LSMO, $x = 0.3, 0.4$



Long-range ferromagnetic order

Loss of long - range order at T_C : some percolation

Short - range order above T_C up to T_{sat} Jahn-Teller distortion

§ Self-interaction corrected local spin density calcs. suggest Mn^{4+} dominant, but conversion to Mn^{3+} with JT distortion
Banach, Temmerman, PRB 69, 054427 ('04)

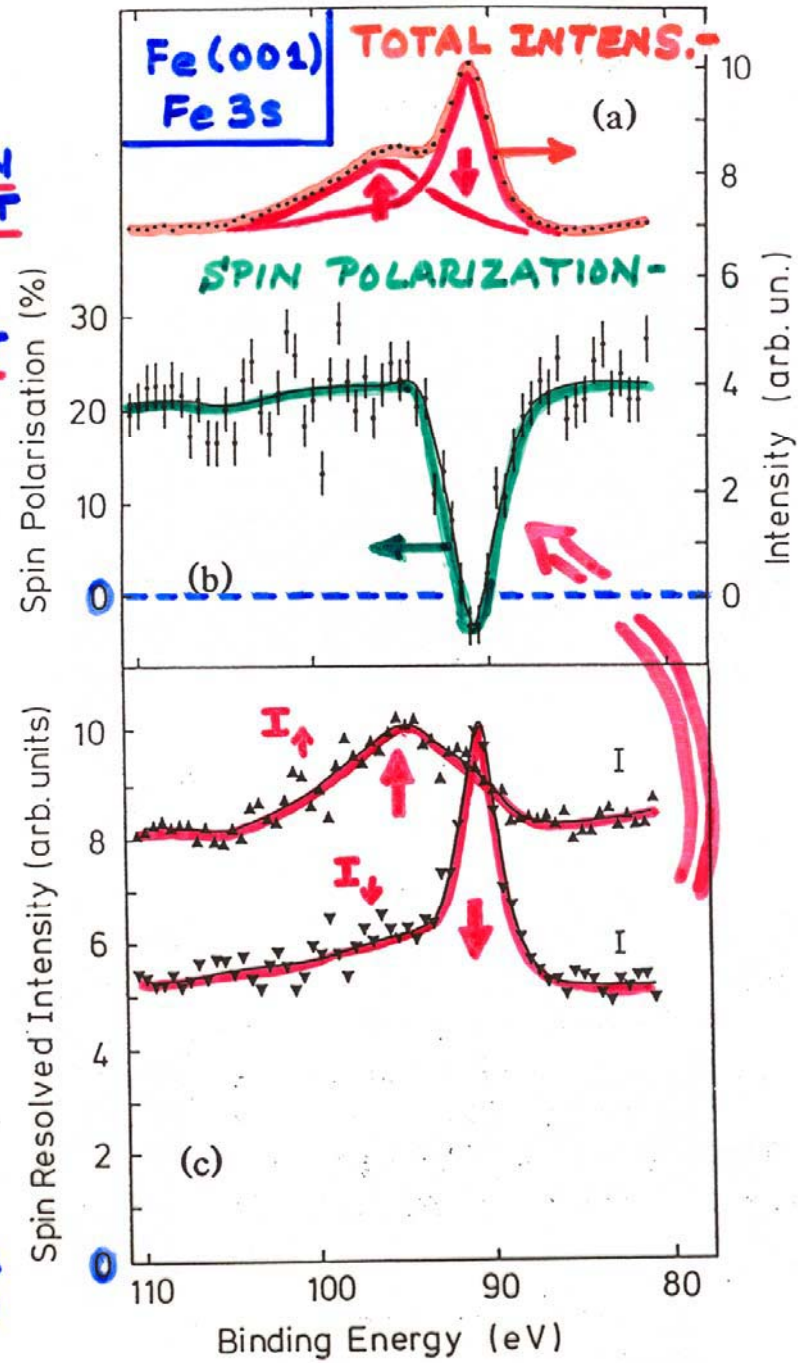
T^* = new T scale suggested from theory
Dagotto et al. PRL 87, 277202 (2001)

Mannella et al., PRL 92, 166401 ('04); PRB 70, 224433 ('04), and to be publ.

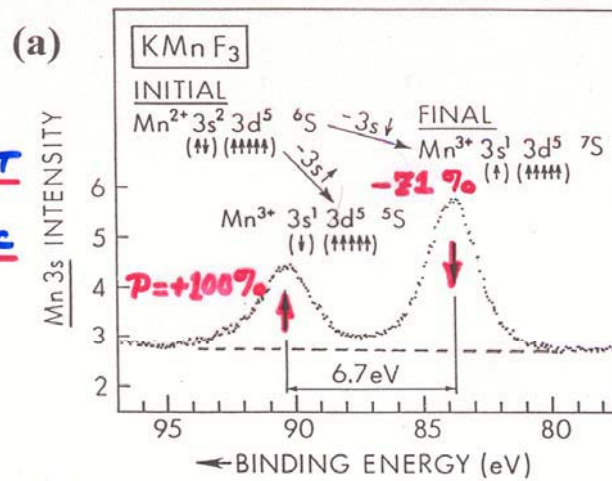
DIRECT
OBSERVATION
OF SPIN-SPLIT
CORE LEVELS
IN A
FERROMAGNET

$$\frac{I_{\uparrow} - I_{\downarrow}}{I_{\uparrow} + I_{\downarrow}}$$

HILLEBRECHT
ET AL.,
PHYS. REV. LETT.
65, 2450 (1990)



①
MULTIPL
ET
IN A
MAGNETIC
ATOM

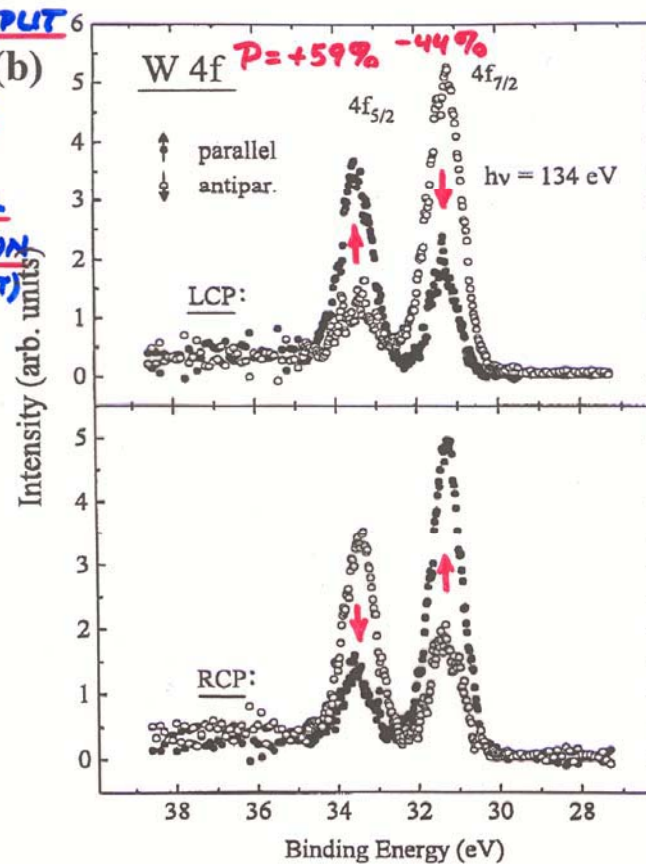


**SPIN POLARIZATION
IN CORE SPECTRA**

$$P = \frac{I_{\uparrow} - I_{\downarrow}}{I_{\uparrow} + I_{\downarrow}}$$

EXPT. - ZINKOVIC
ET AL.
P.R.L. 55,
1227 (1985)

②
SPIN-ORBIT SPLIT
LEVEL
EXCITED
WITH
CIRCULAR
POLARIZATION
(FANO EFFECT)



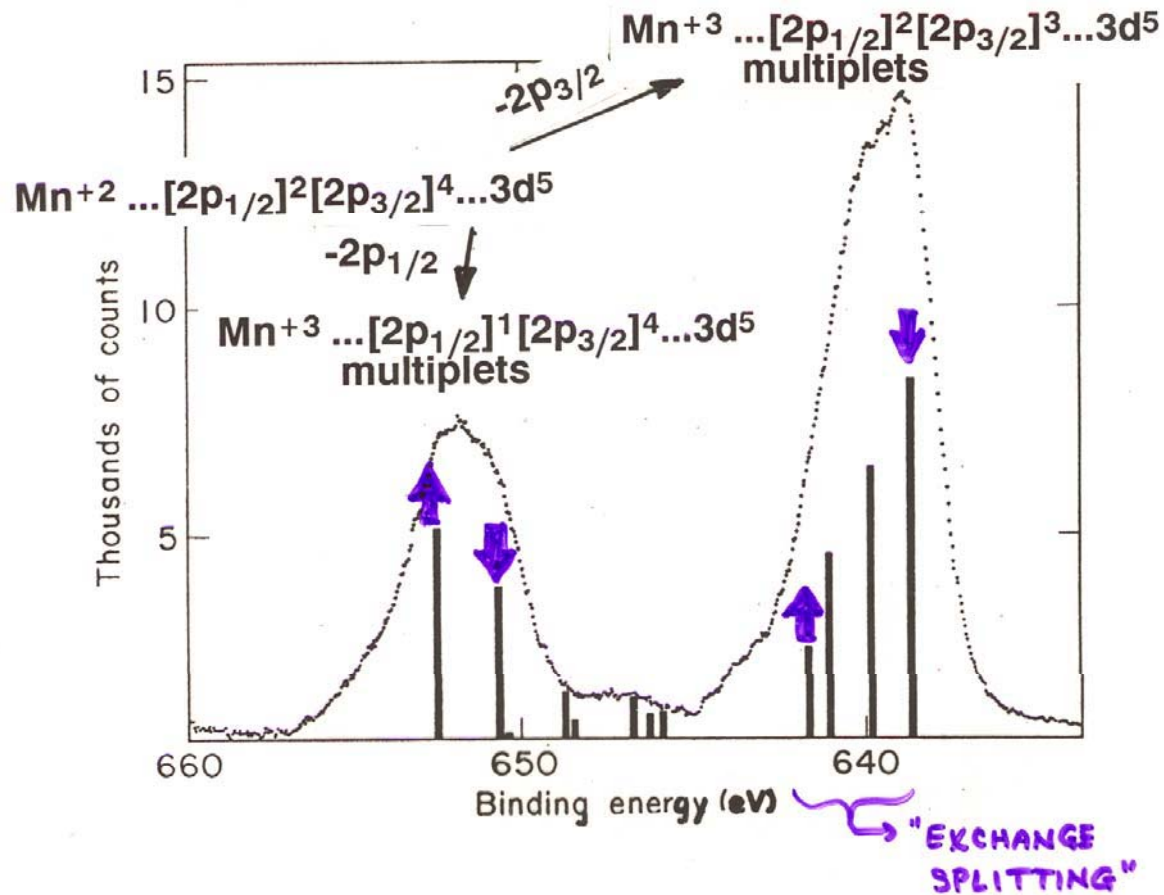
EXPT. - STARKE ET
AL.
PRB 53, R10544
(1996)

Spin
internally
referenced
to spin of
each ion

Spin
externally
referenced
to \vec{k}_{hv} and \vec{M}
of sample

**+ MORE COMPLEX MULTIPLETS FOR $L > 0$
WITH SPIN-ORBIT COUPLING:**

Mn 2p emission from MnF_2 :

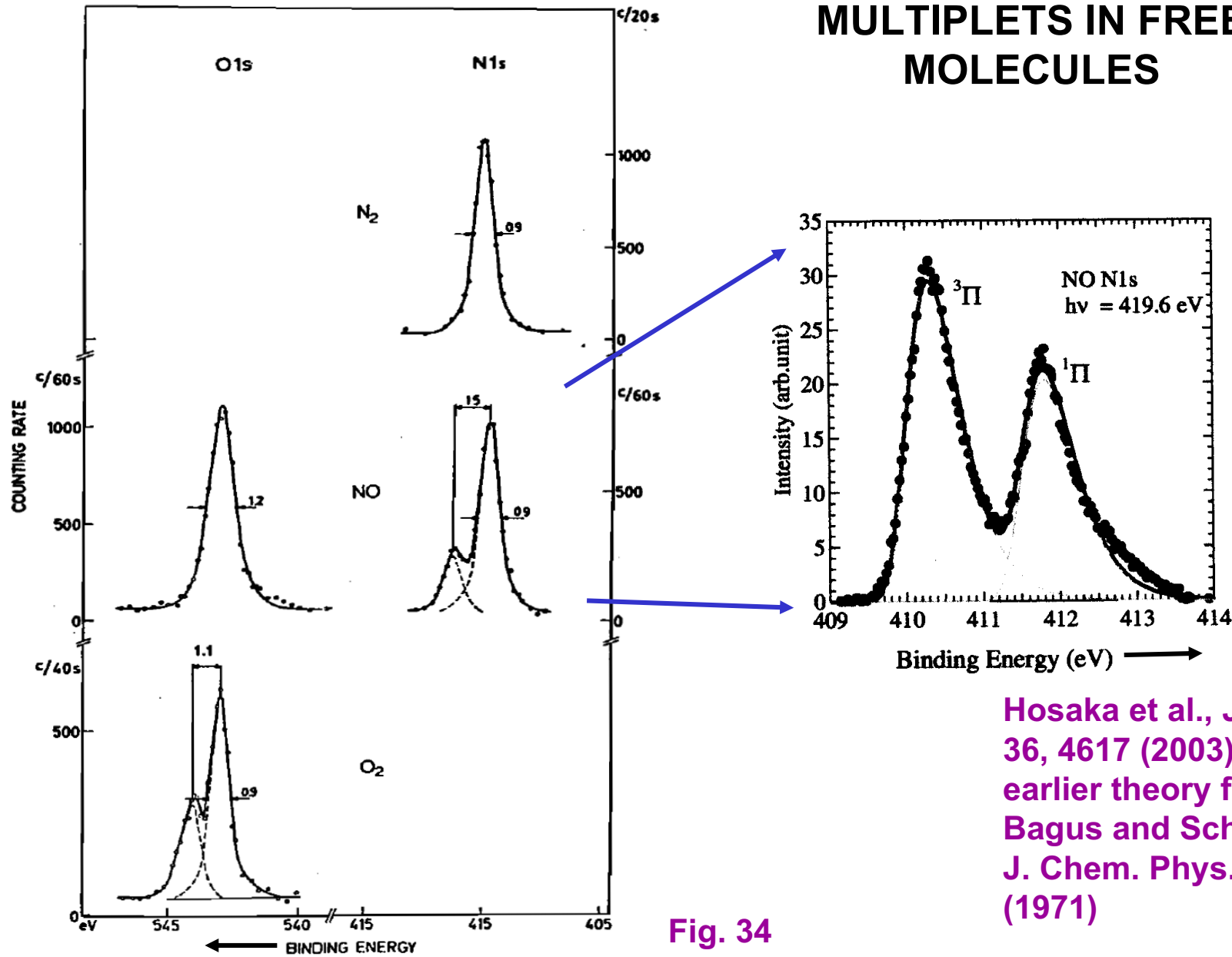


Expt.--Kowalczyk et al., Phys. Rev. B11, 1721 (1975)

Theory--Gupta and Sen, Phys. Rev. B10, 71 (1974)

Park et al., Phys. Rev. B37, 10867 (1988)

MULTIPLETS IN FREE MOLECULES

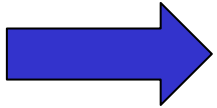


Hosaka et al., J. Phys. B
36, 4617 (2003), and
earlier theory from
Bagus and Schaefer,
J. Chem. Phys. 55, 1474
(1971)

Fig. 34
Basic Concepts of XPS

Outline

- Valence-band spectra: low-energy UPS limit and high-energy XPS limit
- Core-level chemical shifts: the potential model
- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
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- Various other final state effects providing information in core-level spectra



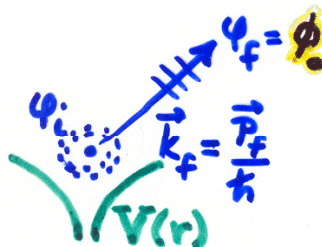
PHOTOELECTRON EMISSION-

BASIC MATRIX ELEMENTS + SELECTION RULES:

● ATOMIC-LIKE (LOCALIZED) STATES ⇒ CORE:

PLUS SPIN:

$$\psi_i(\vec{r}) = \psi_{n_i l_i m_i}(r, \theta, \phi) = R_{n_i l_i}(r) Y_{l_i m_i}(\theta, \phi) \begin{cases} \alpha(\sigma) = m_{s_i} = +1/2 = \uparrow \\ \beta(\sigma) = m_{s_i} = -1/2 = \downarrow \end{cases}$$



$$\psi_f(\vec{r}, \vec{k}_f) = \psi_{E_f}(\vec{r}, \vec{k}_f) \begin{cases} \alpha(\sigma) \\ \beta(\sigma) \end{cases}$$

$$= 4\pi \sum_{l_f, m_f} i^{l_f} e^{-i\delta_{l_f}} Y_{l_f m_f}^*(\theta, \phi) Y_{l_f m_f}(\theta, \phi) R_{E_f, l_f}(r) \begin{cases} \alpha(\sigma) \\ \beta(\sigma) \end{cases}$$

PHASE SHIFT OF l_f WAVE IN $V(r)$

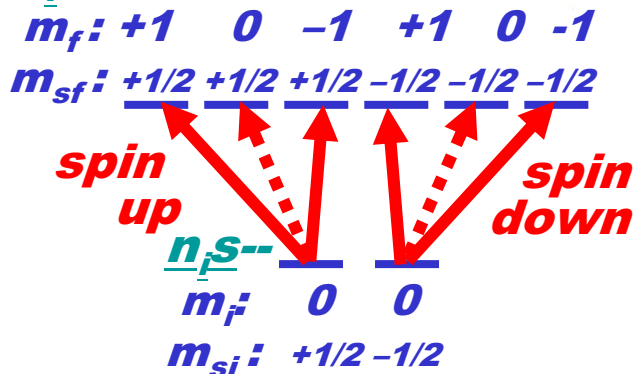
DIPOLE APPROX.: INT. $\propto |\langle \psi_f | \hat{E} \cdot \vec{r} | \psi_i \rangle|^2 = |\hat{E} \cdot \langle \psi_f | \vec{r} | \psi_i \rangle|^2 \Rightarrow$

EQUIVALENT WITHIN CONSTANT FACTOR



- $\Delta l = l_f - l_i = \pm 1$
TWO CHANNELS
 - $\Delta m = m_f - m_i = 0, \pm 1$
LINEAR POLARIZ.
 - $\Delta m = \pm 1$, CIRCULAR POLARIZATION
- $\Delta m_s = m_{s_f} - m_{s_i} = 0!$

$E_f p$

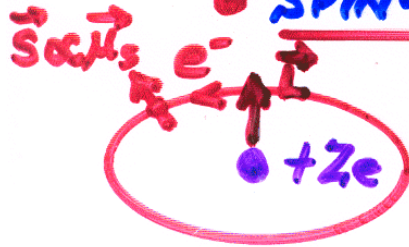


FOR A GIVEN $n_i / l_i m_i m_{s_i}$: SUM OVER DEGENERATE INITIAL STATES $m_i m_{s_i}$ AND AVERAGE OVER FINAL STATES $E_f / m_f m_{s_f}$ ACCESSED FROM EACH m_i TO YIELD DIFFERENTIAL SUBSHELL PHOTOELECTRIC CROSS SECTION:

$$d\sigma_{n_i l_i} / d\Omega$$

\propto PROBABILITY PER UNIT SOLID ANGLE OF EXCITING ONE ELECTRON FROM SUBSHELL n_i / l_i INTO THE DIRECTION k_f

• SPIN-ORBIT SPLITTING OF LEVELS:



⇒ EFFECTIVE \vec{B} (NUCLEUS AROUND e^-) $\propto \vec{L}$

$$\hat{H}_{s-o} = \xi(r) \vec{L} \cdot \vec{S}$$

- SPLITS ALL nl LEVELS $2(2l+1)$
 - $nl_j = l + 1/2 \rightarrow 2l+2$
 - $nl_j = l - 1/2 \rightarrow 2l$

• MIXES SPIN + ORBITAL ANGULAR MOM.:

$$\psi_{nljm_j} = C_1 \psi_{nl, m_j - 1/2} \begin{pmatrix} 1 \\ 0 \end{pmatrix} + C_2 \psi_{nl, m_j + 1/2} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

\parallel
 $m_s = +1/2$
 \parallel
 \uparrow

\parallel
 $m_s = -1/2$
 \parallel
 \downarrow

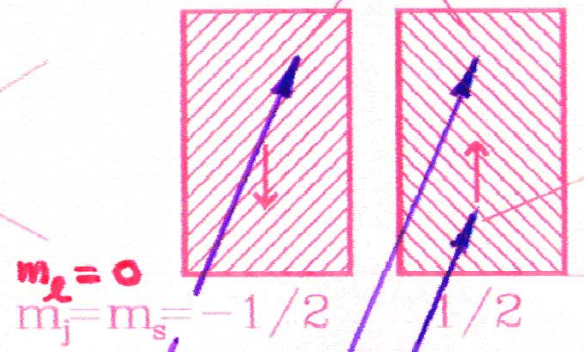
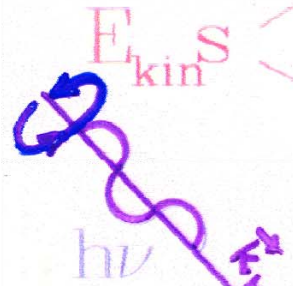
WITH C_1 AND C_2 TABULATED CLEBSCH-GORDAN OR WIGNER $3j$ SYMBOLS

PHOTOELECTRON SPIN POLARIZATION FROM CIRCULAR POLARIZATION AND SPIN-ORBIT SPLITTING (THE FANO EFFECT)

$$P = -50\% = \frac{I_{up} - I_{down}}{I_{up} + I_{down}} = \frac{\sqrt{1/3^2 - 1^2}}{\sqrt{1/3^2 + 1^2}} \times 100$$

$$= \frac{-2/3}{4/3} \times 100 = -50\%$$

(Neglect $E_{kin,d}$)



$$P = +100\%$$

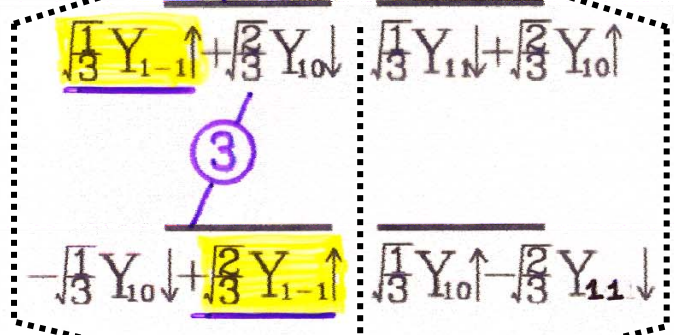
E_{vacuum}

LCP
 $\Delta m_l = +1$

: PURE

Spin externally referenced to \vec{k}_{hv} and \vec{M} of sample

Degenerate $np_{3/2}$



: MIXED

: MIXED

$np_{1/2}$

$m_j = m_l + m_s = -3/2 \quad -1/2 \quad 1/2 \quad 3/2$

Spin polarization in core photoelectron spectra—expt.

SPIN-ORBIT SPLIT

LEVEL (b)

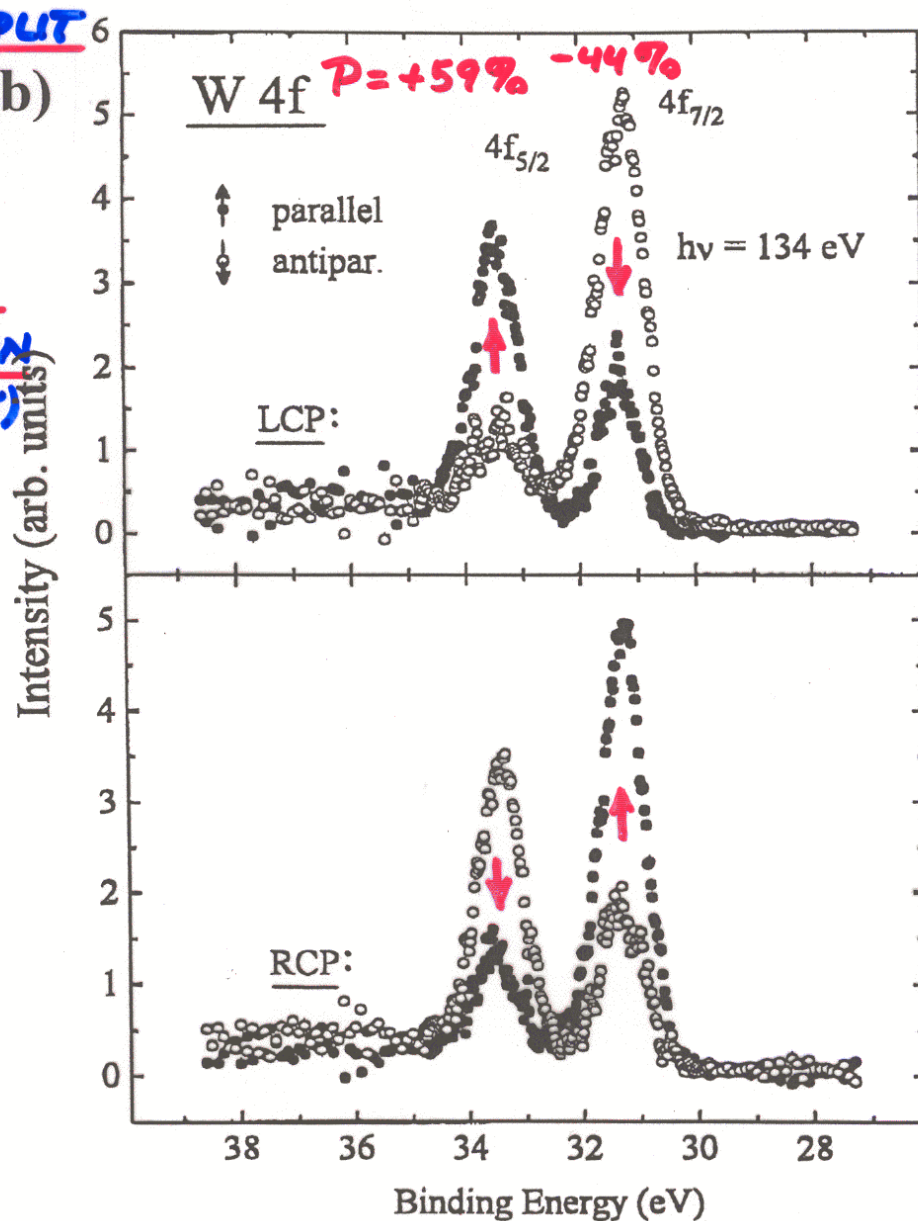
EXCITED

WITH

CIRCULAR


POLARIZATION

(FANO EFFECT)

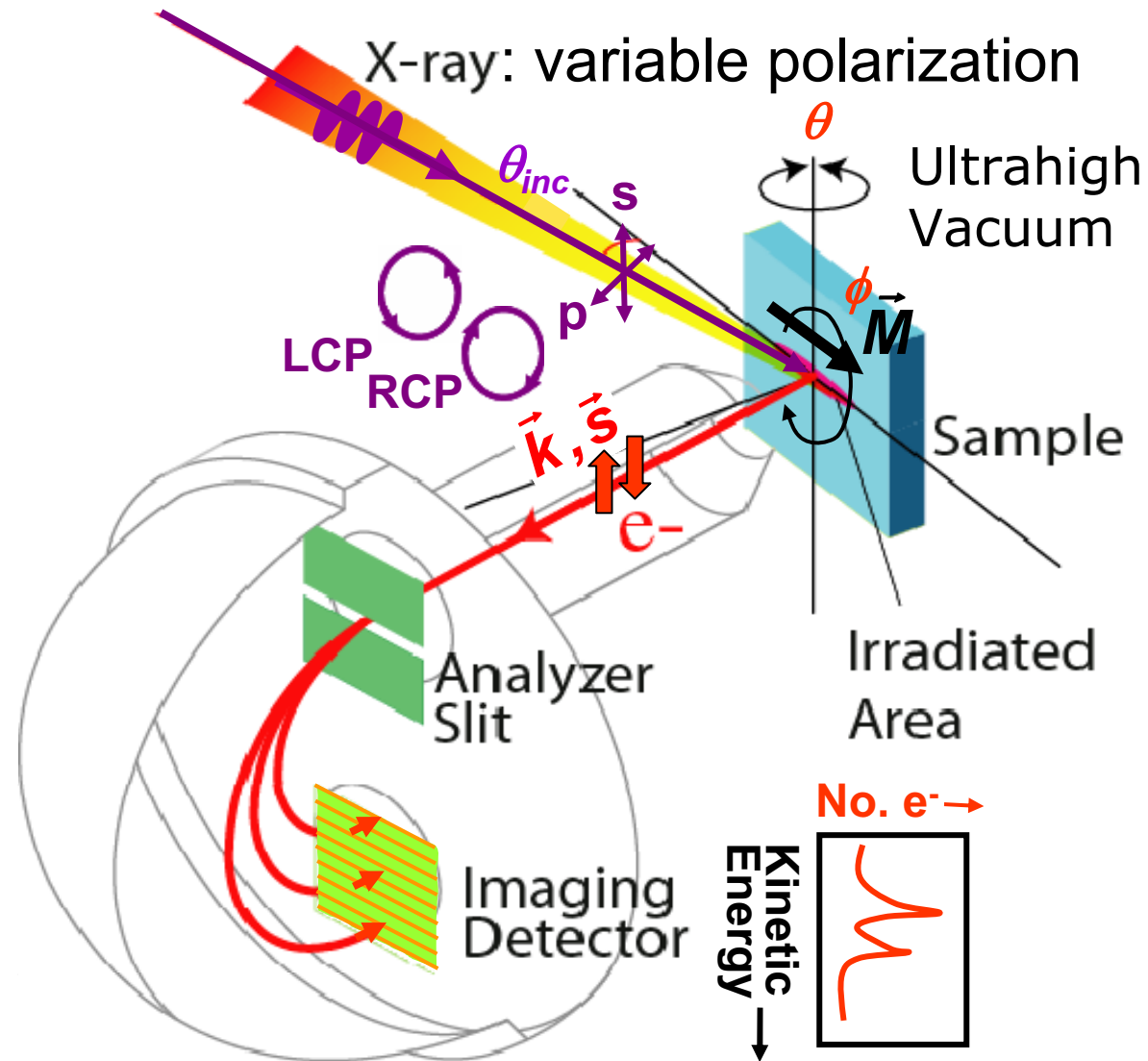


EXPT. - STARR ET AL.
PRB 53, R10544
(1996)

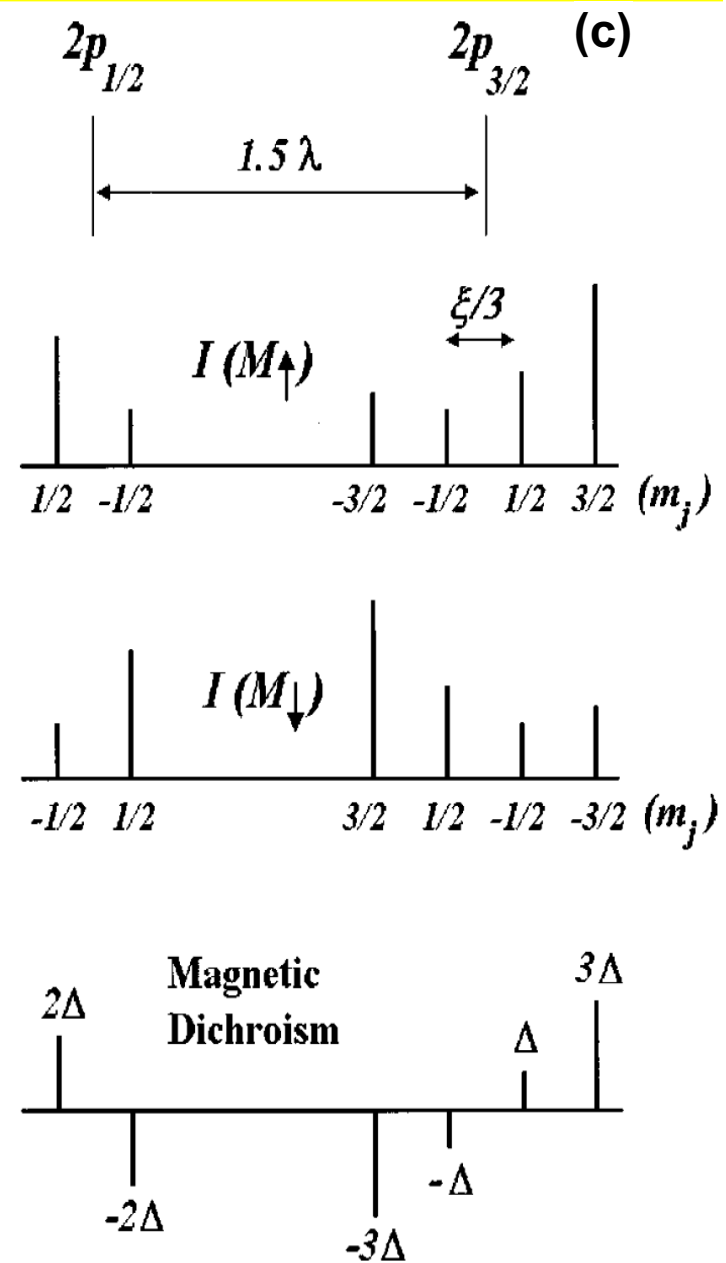
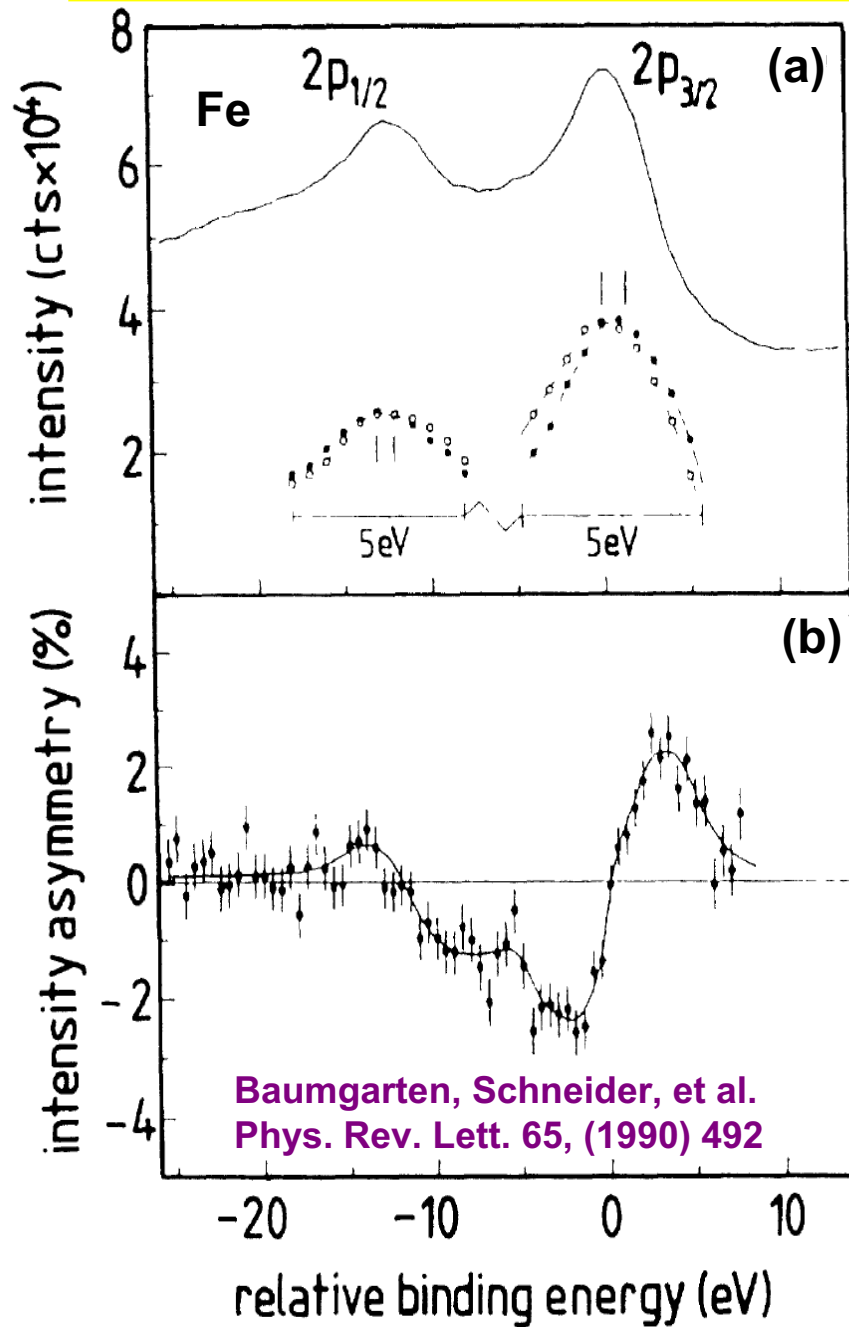
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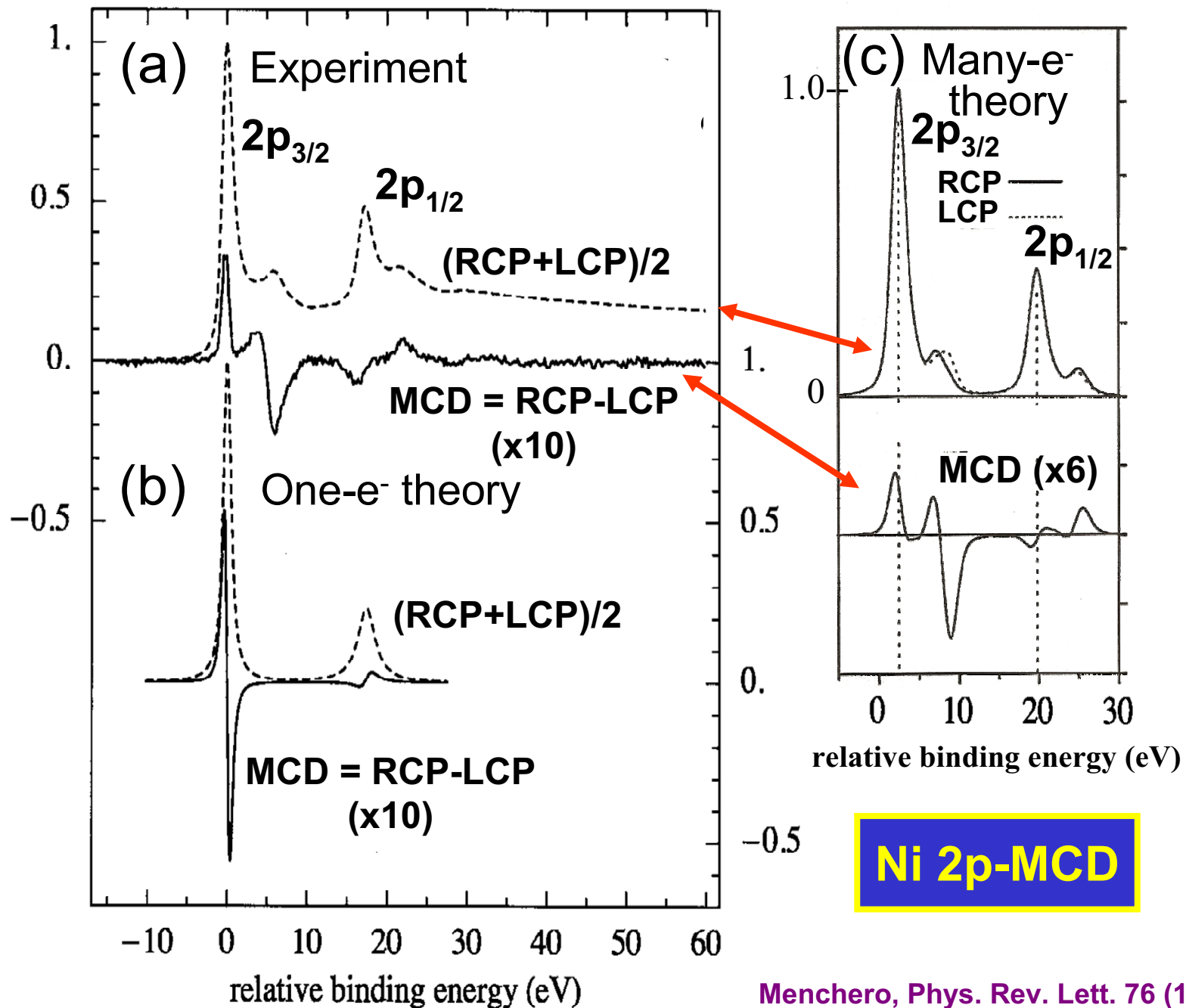
Typical experimental geometry for energy- and angle-resolved photoemission measurements



1st Expt. Magnetic Circular Dichroism 1-e⁻ Theo.



Menchero, Phys. Rev. B 57 (1998) 993



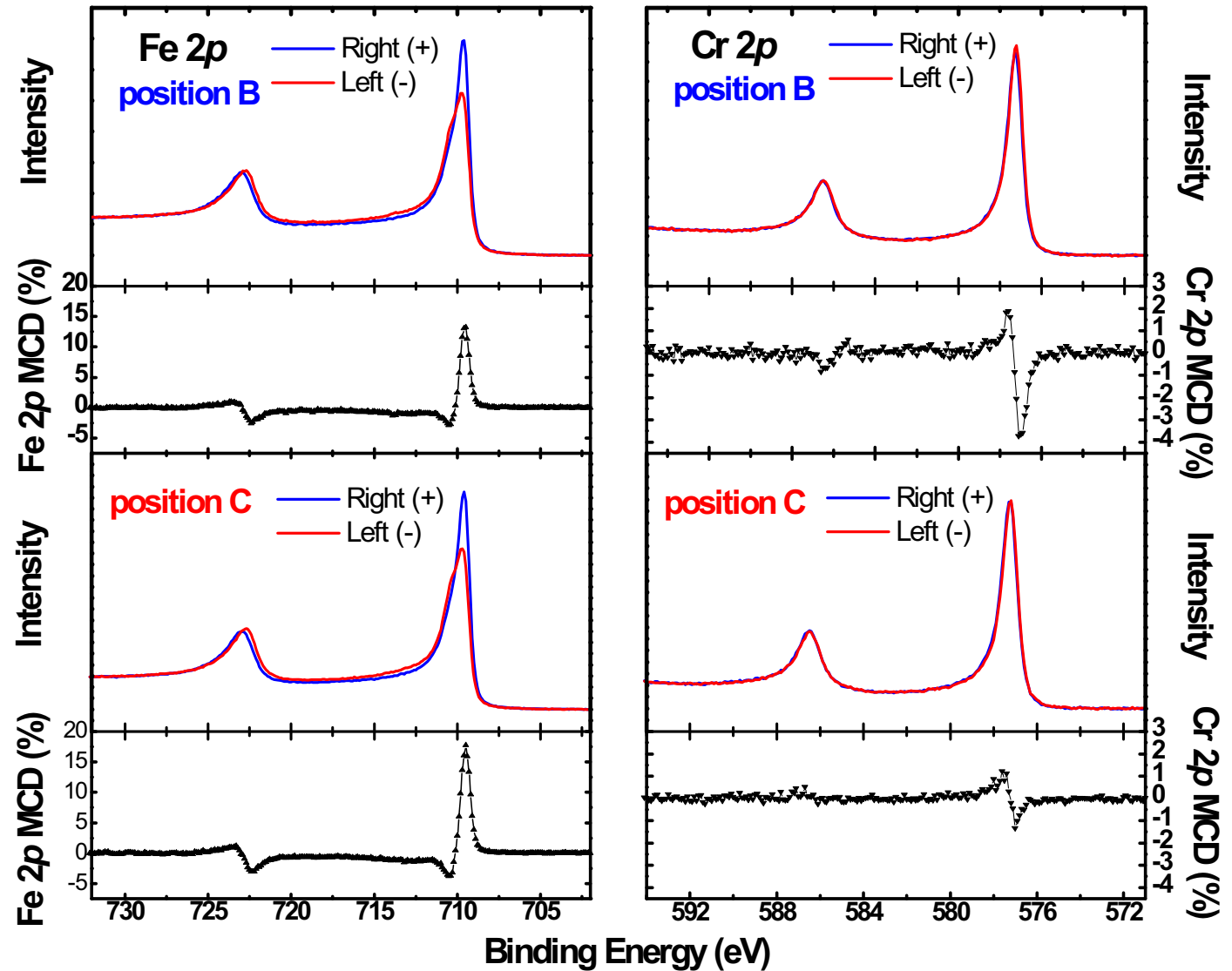
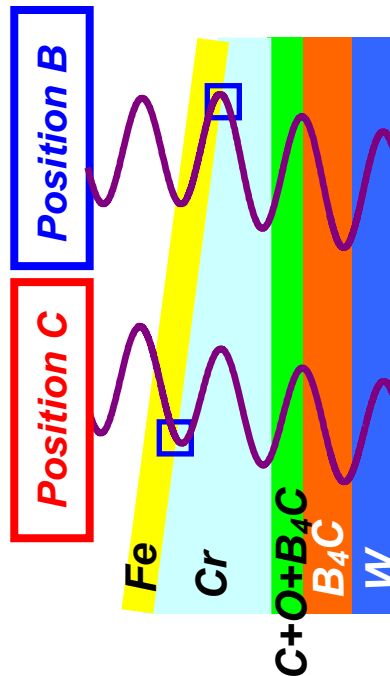
Menchero, Phys. Rev. Lett. 76 (1996) 3208

Van der Laan et al., J. Phys. Condens. Matter 12 (2000) L275

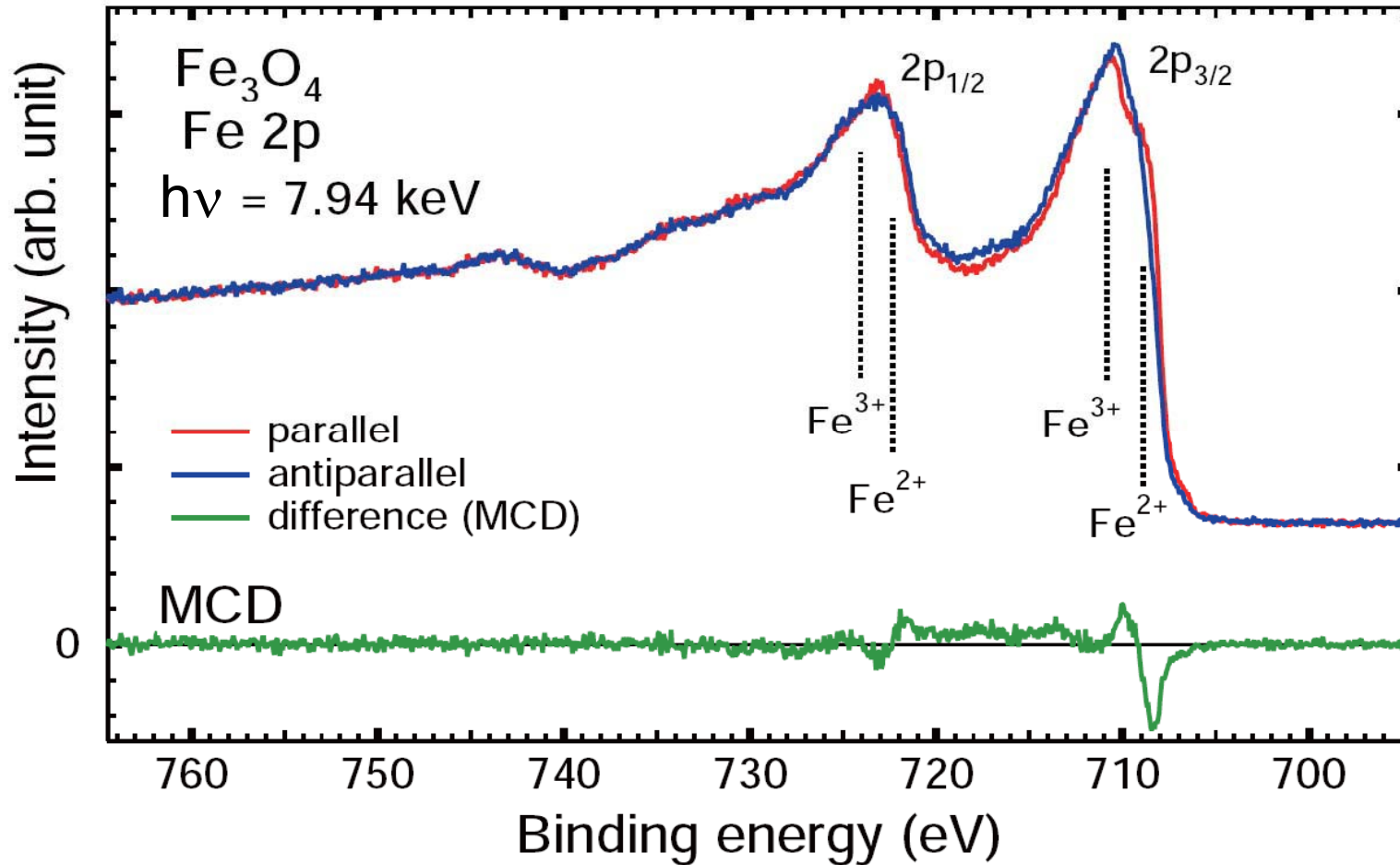
Application to a buried interface: with standing wave excitation

Fe & Cr 2p MCD Data from wedge (Fe/Cr)+SWG

*Cr magnetization
Is antiparallel to
Fe; systematic
variation of MCD
strengths vs d_{cr}*

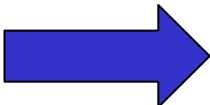


Some first MCD data with hard x-ray excitation



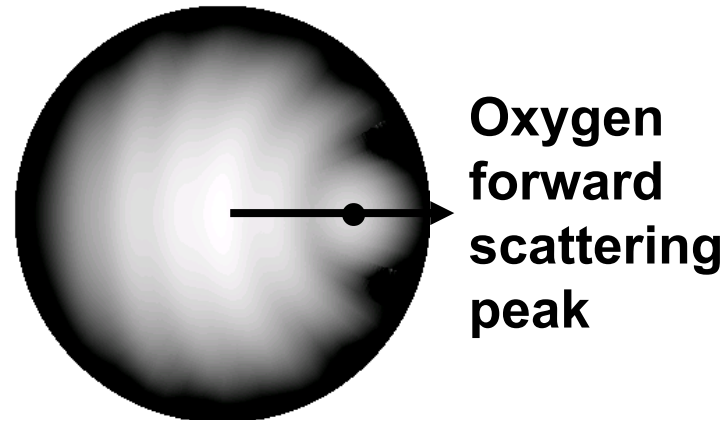
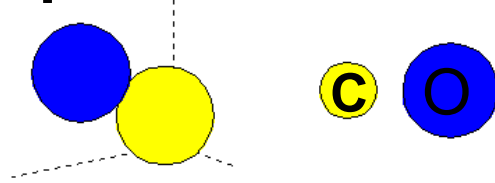
S. Ueda et al., Appl. Phys. Exp., in press
SPring8-BL15XU

Outline

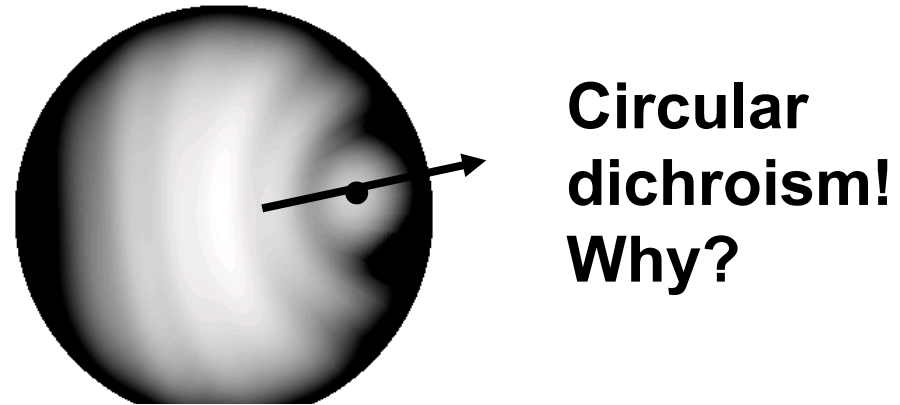
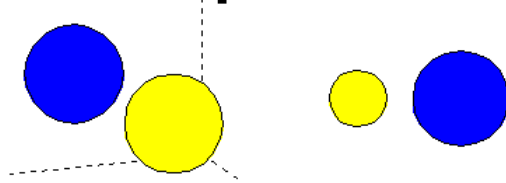
- Valence-band spectra: low-energy UPS limit and high-energy XPS limit
- Core-level chemical shifts: the potential model
- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
- Multiplet splittings
- Spin-orbit splitting, the Fano effect, and spin-polarized outgoing electrons
- Magnetic circular dichroism (MCD) in core-level emission
-  • Non-magnetic circular dichroism in core-level emission: a.k.a. circular dichroism in angular distributions (CDAD)
- Various other final state effects providing information in core-level spectra

**Circular dichroism in angular distributions:
C 1s emission from CO, $E_{\text{kin}} = 200$ eV**

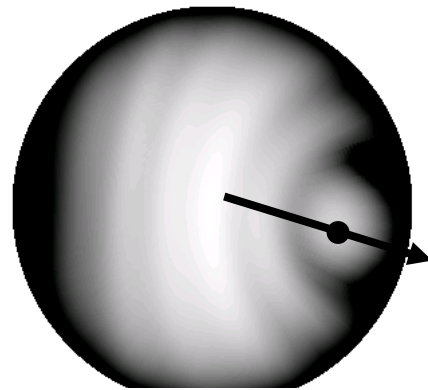
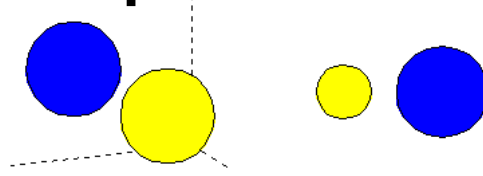
Linear p polarization:



Right circular polarization:

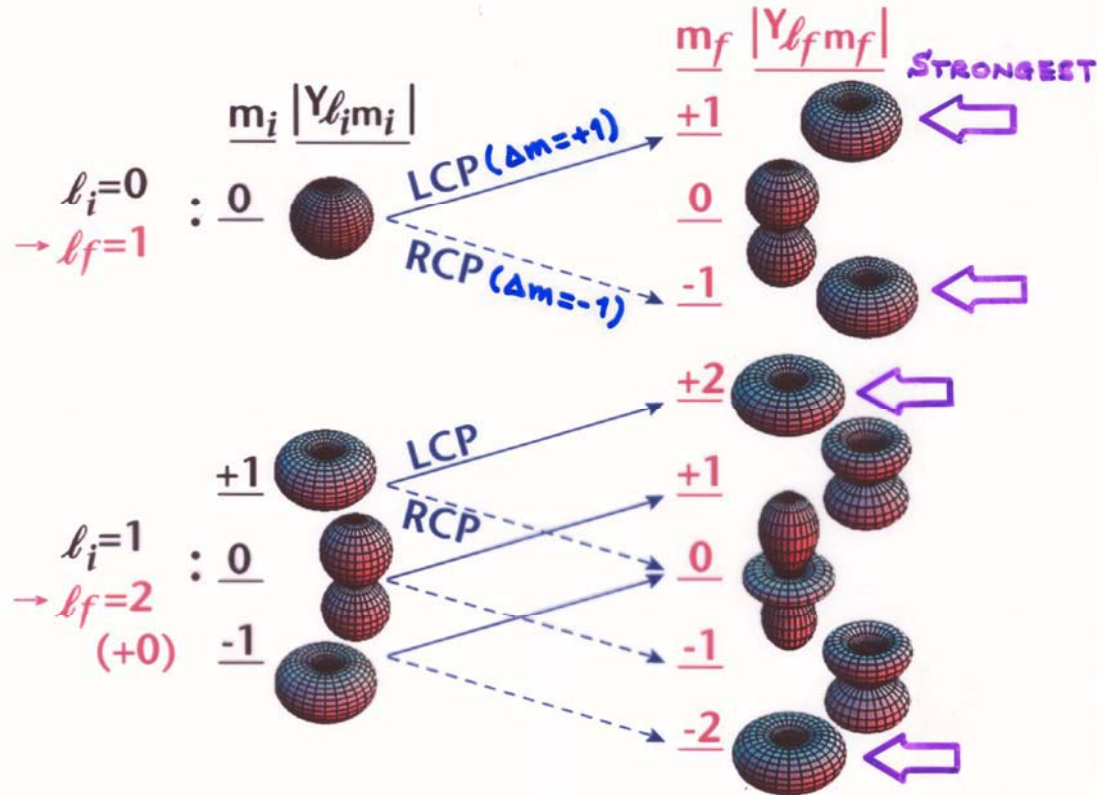
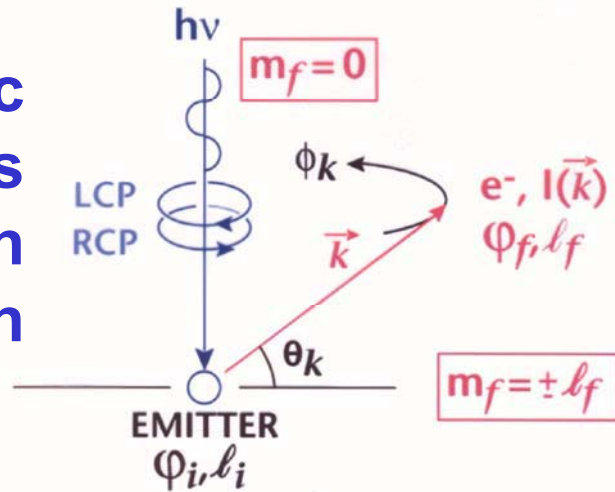


Left circular polarization:



CIRCULAR DICHROISM IN PHOTOELECTRON ANGULAR DISTRIBUTIONS (CDAD)

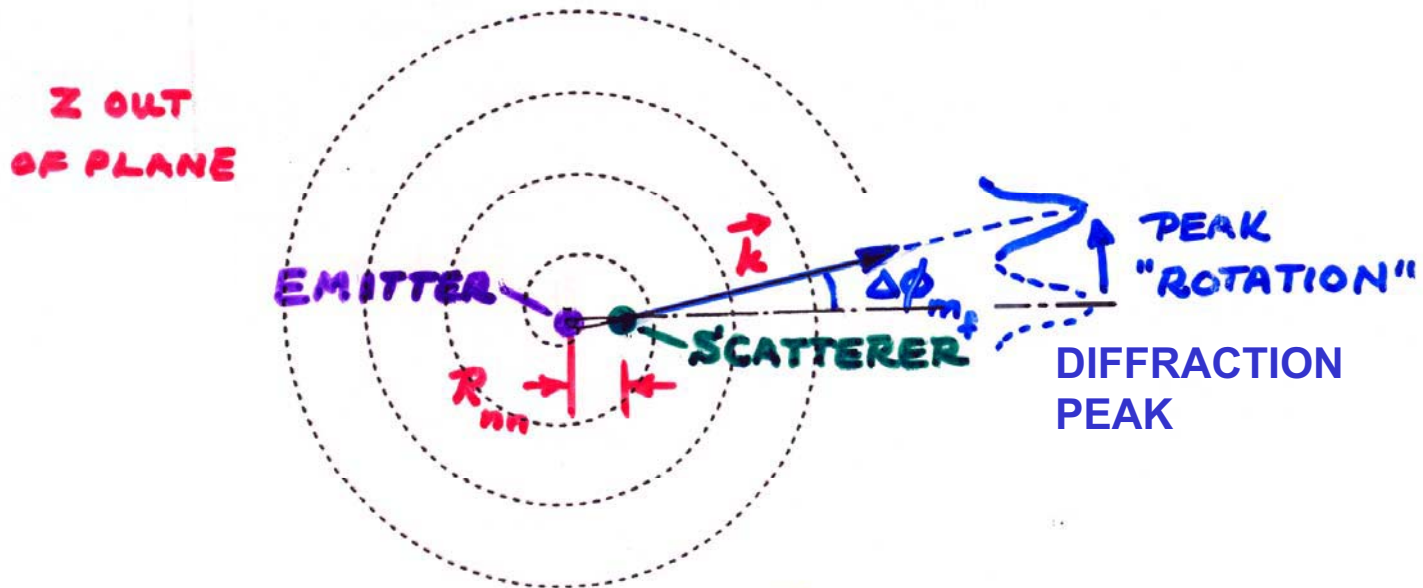
➔ Non-magnetic dichroism effects due to photoelectron diffraction



CIRCULAR DICHOISM IN PHOTOELECTRON DIFFRACTION

CONSTANT-PHASE SURFACE OF:

$$\psi_{\text{PHOTOE}^-}(r, \theta, \phi) \propto \frac{e^{ikr}}{r} \textcircled{H}_{lm} e^{im_f \phi}$$



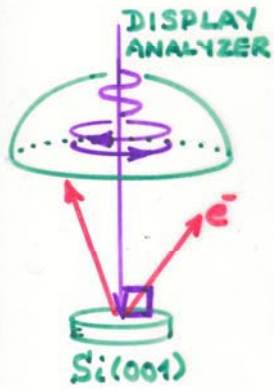
$$\left\| \Delta\phi_{m_f} = \frac{m_f}{R_{nn}, \|k\|} \right\|$$

$$\overline{m_f} \approx m_{f, \text{max}}$$

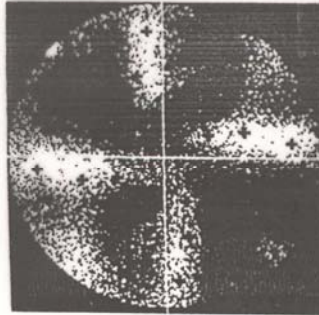
DAIMON ET AL.
JPN. J. APPL. PHYS.
32, L1480 ('93)

CIRCULAR DICHOISM - NON-MAGNETIC SYSTEMS

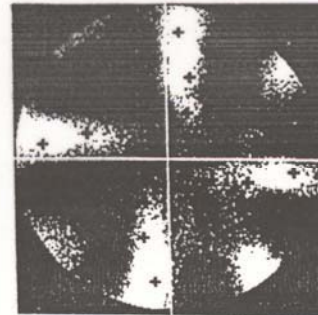
Si2p -- 250eV = E_{kin}
EXPERIMENT



(a) LCP



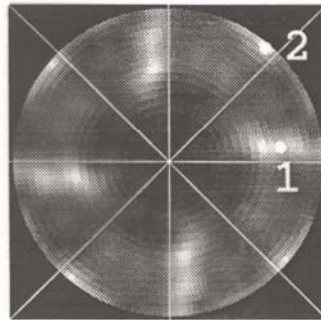
(b) RCP



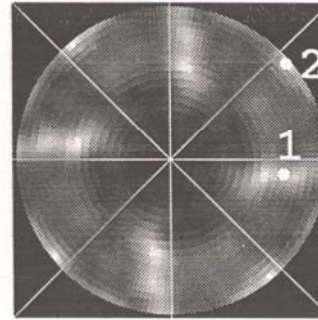
DAIMON ET AL.
JPN. J. APPL. PHYS.
32, L1480 ('93)

THEORY

(c) LCP

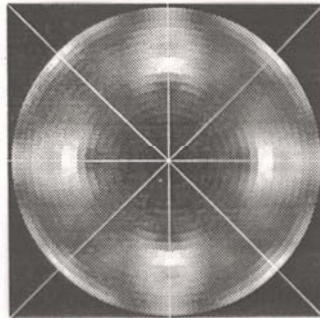


(d) RCP



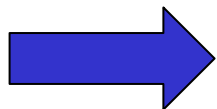
IKADUWELA ET AL.
P. R. B 50, 6203 ('94)

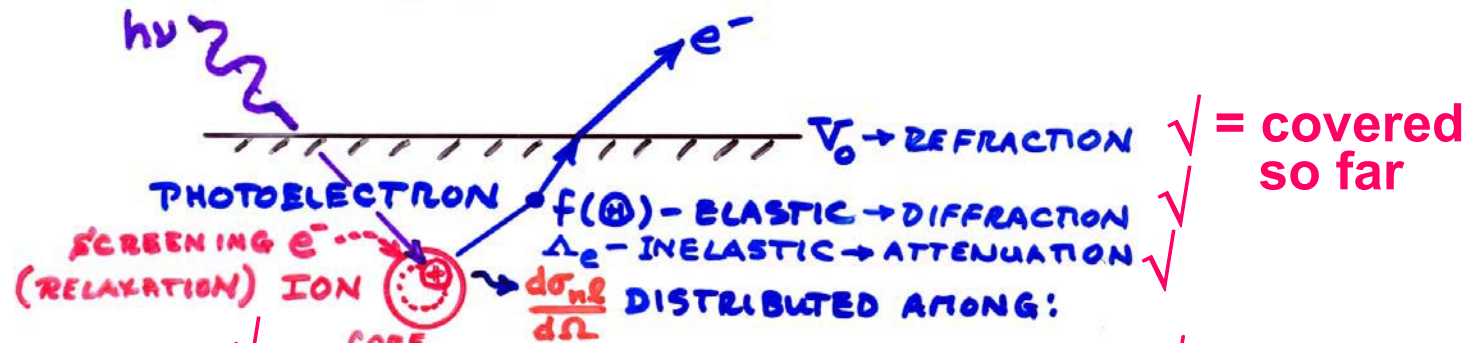
(e) UNPOLARIZED



Outline

- Valence-band spectra: low-energy UPS limit and high-energy XPS limit
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- Core-level chemical shifts: equivalent-core ($Z+1$) and thermochemical energies
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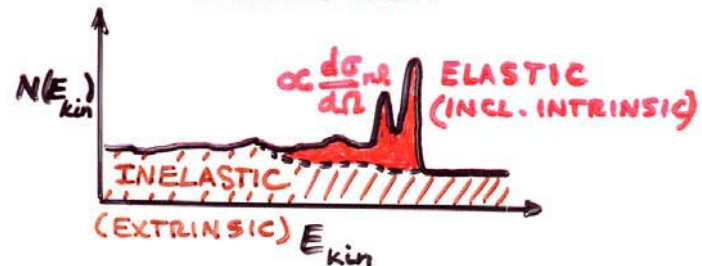


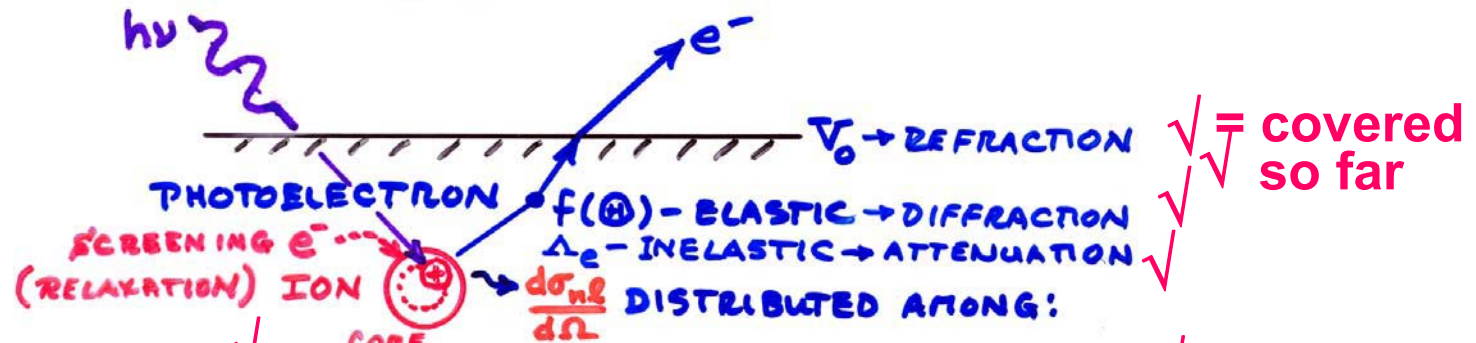


ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS

- + SPIN-ORBIT SPLITTING (EASY) \checkmark
- + MULTIPLLET SPLITTING (OPEN-SHELL SYSTEMS), XSTAL FIELD \checkmark
- + CORRELATION / CONFIGURATION INTERACTION \checkmark
- + SHAKE-UP / SHAKE-OFF / e^- -HOLE \checkmark
- + SCREENING / NON-SCREENING: CONFIGURATION INTERACTION \checkmark
- + VIBRATIONAL EXCITATIONS \checkmark
- + RESONANT PHOTOEMISSION ($h\nu \approx E_{b, n'l}$) \checkmark

REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP





covered so far

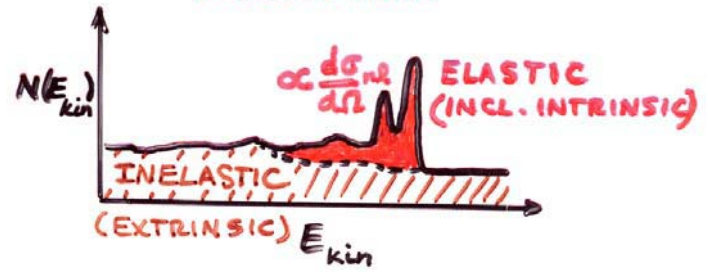
ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS

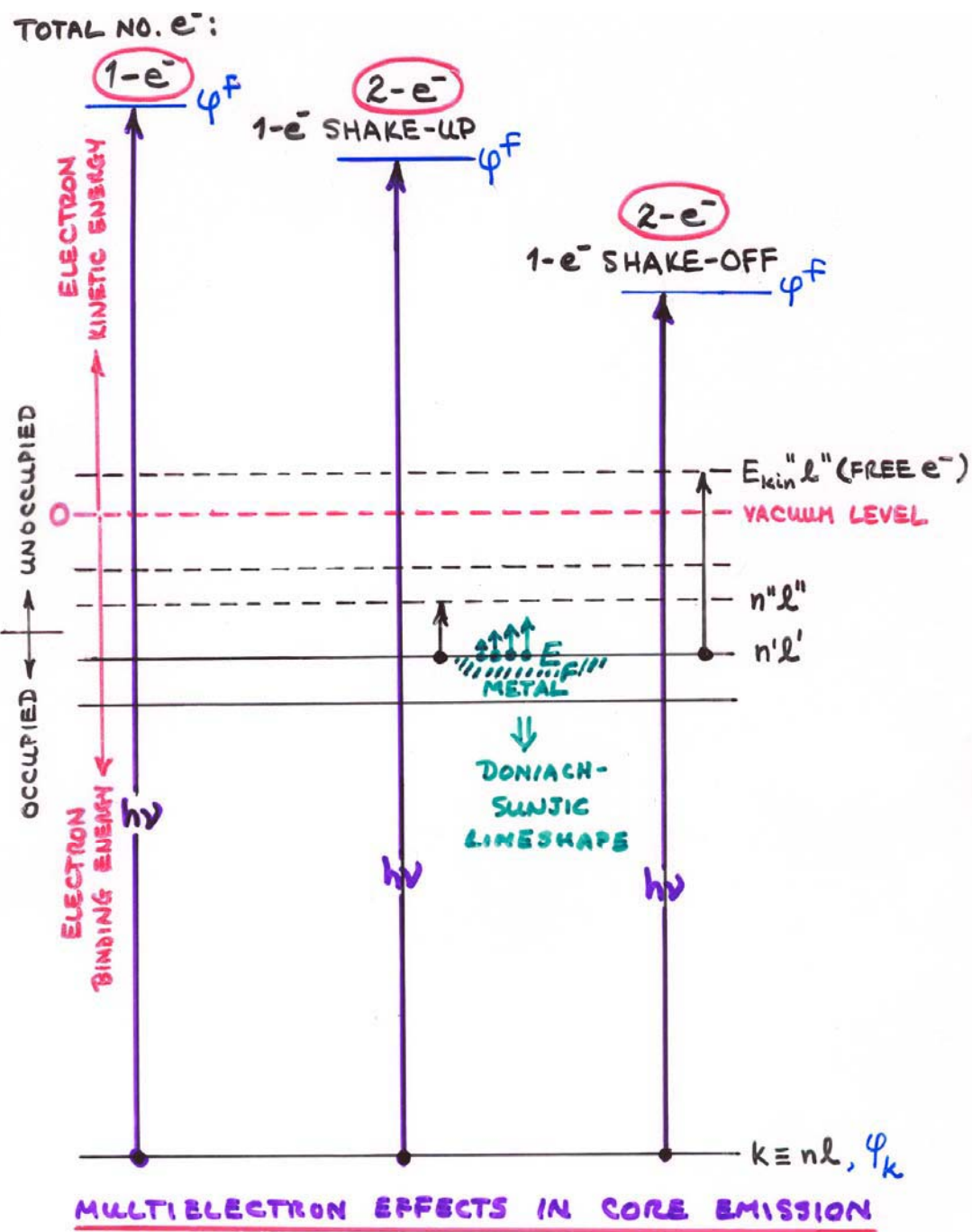
CORE HOLE $k = n, l$

- + SPIN-ORBIT SPLITTING (EASY)
- + MULTIPLLET SPLITTING (OPEN-SHELL SYSTEMS), XSTAL FIELD
- + CORRELATION / CONFIGURATION INTERACTION
- + SHAKE-UP / SHAKE-OFF / e^- -HOLE
- + SCREENING / NON-SCREENING: CONFIGURATION INTERACTION
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- + RESONANT PHOTOEMISSION ($h\nu \approx E_{b, n'l}$)



REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP





MULTIELECTRON EFFECTS IN CORE EMISSION

INTENSITIES IN PHOTOELECTRON SPECTRA:

- GENERAL: FINAL STATE K (k -SUBSHELL + ALL OTHER DESIG.)

$$\text{INT.}_K \propto |\hat{e} \cdot \langle \Psi_{\text{tot}}^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi^i(N) \rangle|^2 \quad (\text{DIPOLE APPROX.})$$

- BORN-OPPENHEIMER: e^- 's FAST, VIBRATIONS SLOW

$$\text{INT.}_K \propto \underbrace{|\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2}_{\text{FRANCK-CONDON FACTOR}} |\hat{e} \cdot \langle \Psi_e^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_e^i(N) \rangle|^2$$

- SUDDEN APPROXIMATION: $\Psi_K \rightarrow \Psi_C = \text{PHOTO}e^-$ (FAST)



$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2 |\langle \Psi_e^f(N-1, K) | \Psi_e^i(N-1, K) \rangle|^2$$

$$|\hat{e} \cdot \langle \Psi_f | \vec{r} | \Psi_K \rangle|^2 \quad \text{SAME SUBSHELL COUPLING + TOTAL L, S} \rightarrow \text{"MONOPOLE"}$$

↳ NORMAL $\frac{d\sigma_K}{d\Omega}$

- SLATER DETS. FOR $\Psi_e^f = \det(\psi_1', \psi_2', \dots, \psi_{k-1}', \psi_{k+1}', \dots, \psi_N')$

$$\Psi_e^i = \det(\psi_1, \psi_2, \dots, \psi_{k-1}, \psi_{k+1}, \dots, \psi_N)$$

$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2 |\langle \psi_1' | \psi_1 \rangle|^2 |\langle \psi_2' | \psi_2 \rangle|^2 \dots$$

$$|\langle \psi_{k-1}' | \psi_{k-1} \rangle|^2 |\langle \psi_{k+1}' | \psi_{k+1} \rangle|^2 \dots |\langle \psi_N' | \psi_N \rangle|^2$$

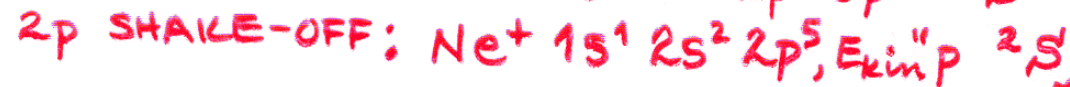
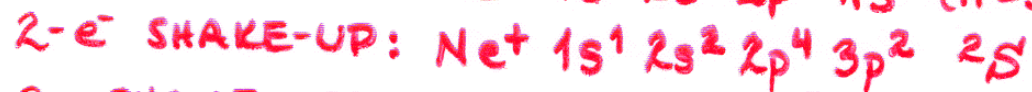
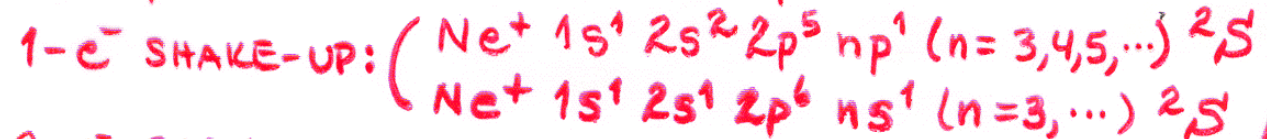
$$|\hat{e} \cdot \langle \Psi_f | \vec{r} | \Psi_K \rangle|^2$$

1e- DIPOLE $\rightarrow d\sigma/d\Omega$

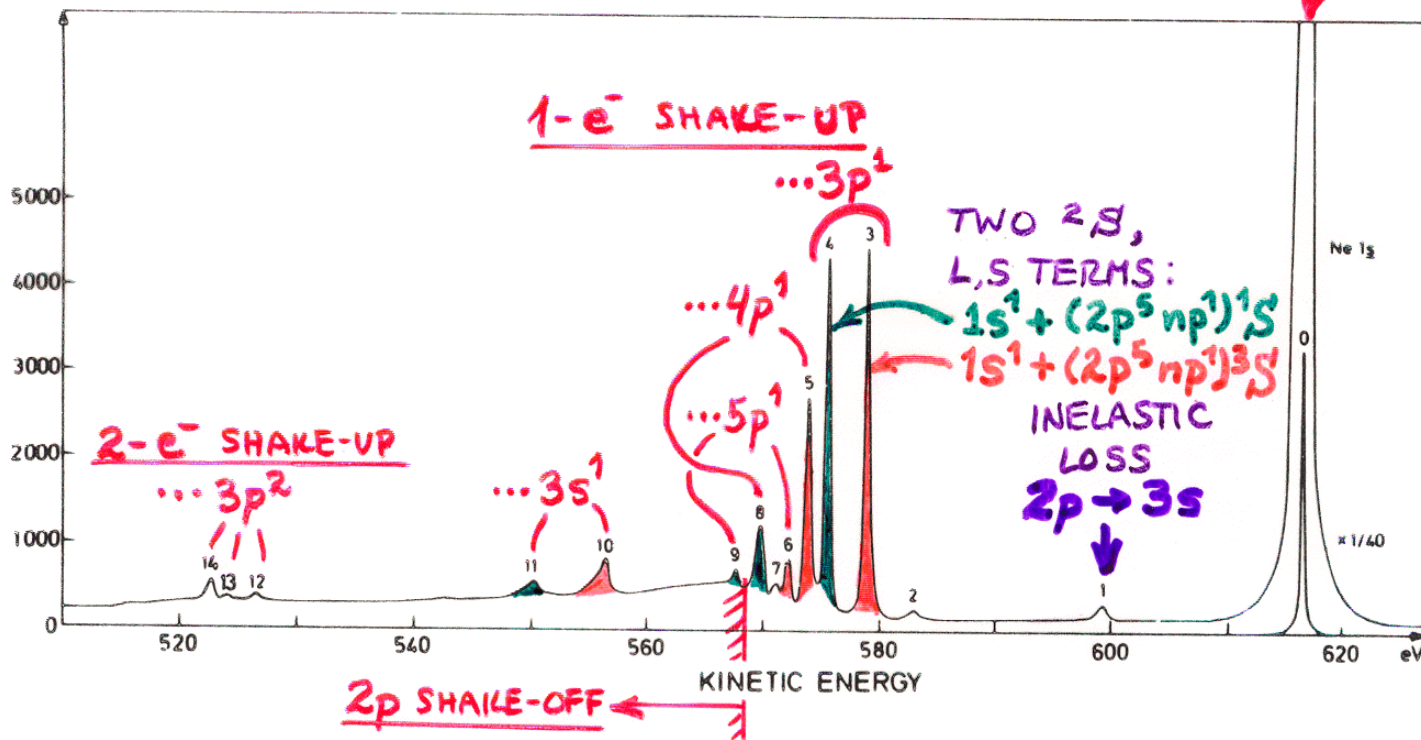
(N-1)e- SHAKE-UP/
SHAKE-OFF \rightarrow
"MONOPOLE"

- PLUS DIFFRACTION EFFECTS IN Ψ_C ESCAPE

NEON 1S SHAKE-UP/SHAKE-OFF:



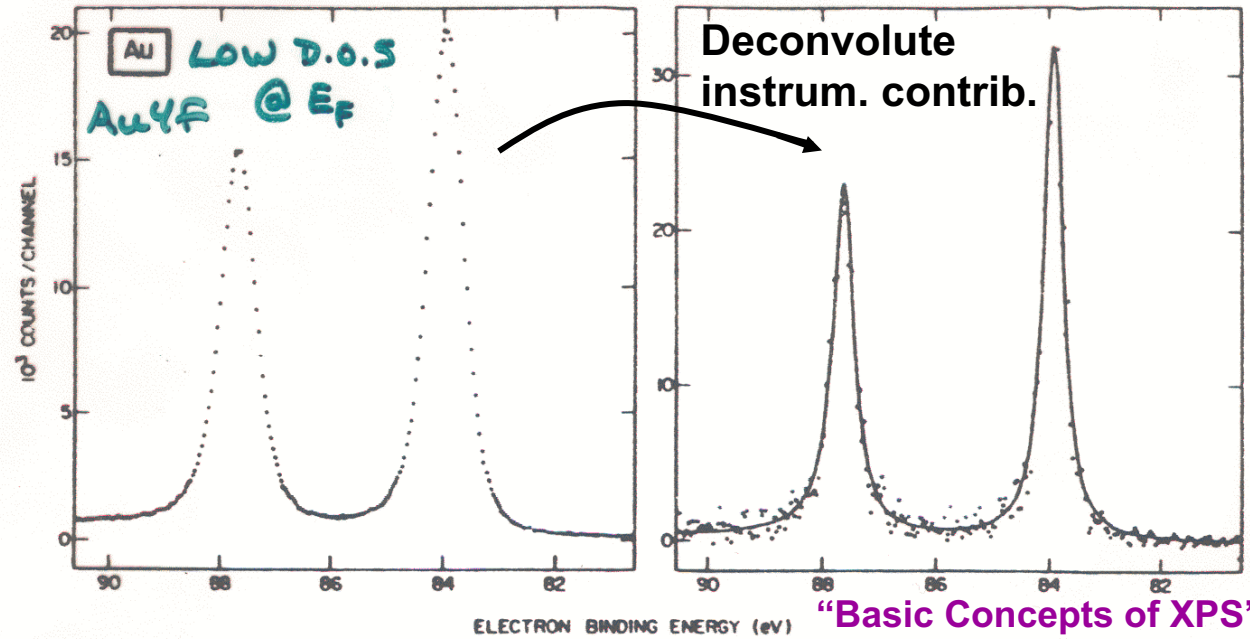
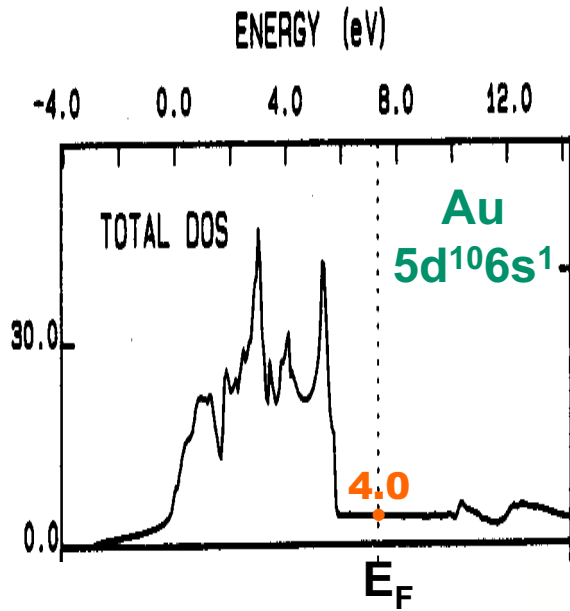
“Basic Concepts of XPS”
Figure 36



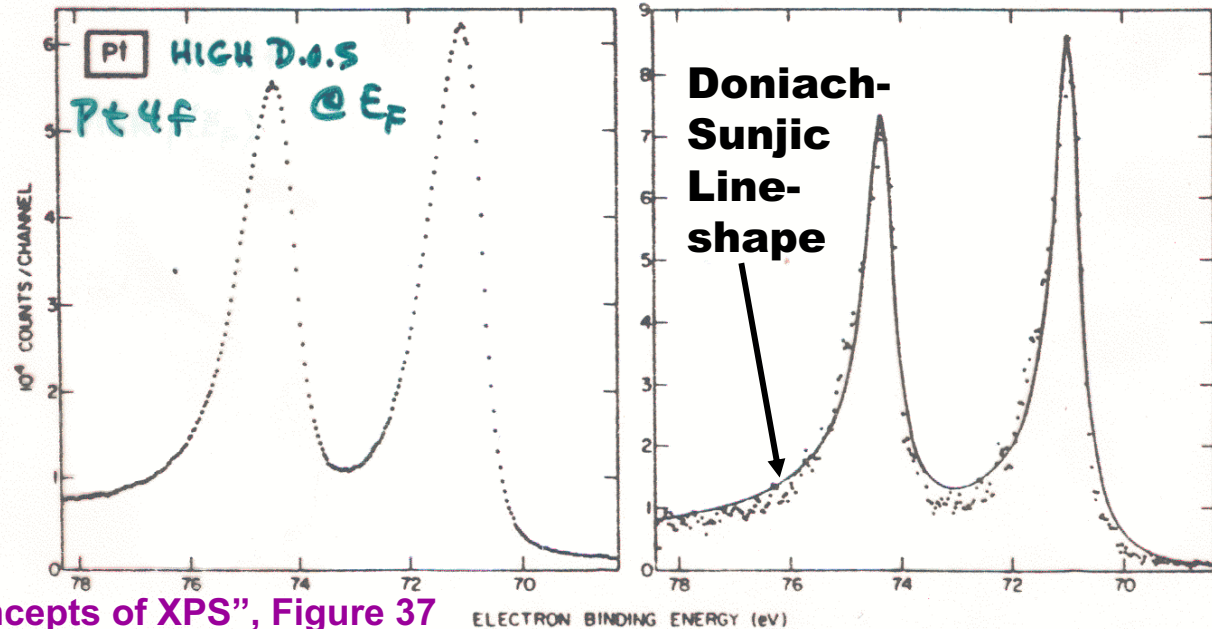
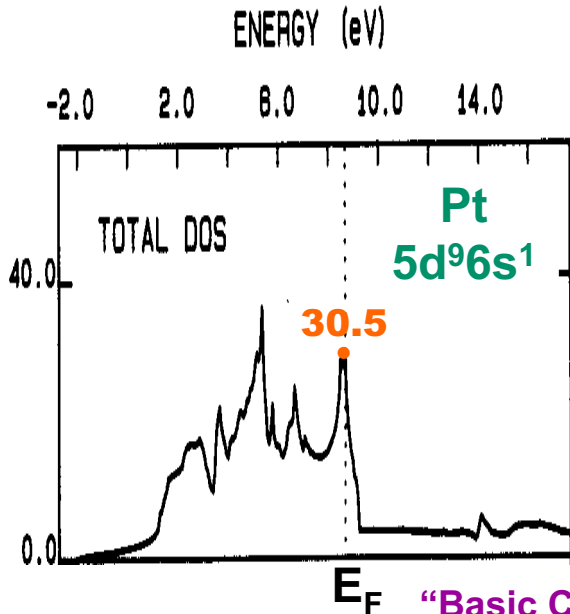
OVERALL: ~12% SHAKE-UP + 16% SHAKE-OFF \approx 28% OF EVENTS

BAND THEORY—D.O.S:

ELECTRON-HOLE EXCITATIONS IN METALS:



“Basic Concepts of XPS”
Figure 10



“Basic Concepts of XPS”, Figure 37

TWO SUDDEN-APPROXIMATION

SUM RULES:

① $\left\{ \begin{array}{l} \text{AVERAGE} \\ \text{BINDING} \\ \text{ENERGY} \end{array} \right\} = \frac{\sum_{j=1}^{\text{ALL}} I_j E_b^V(k)_j}{\sum_{j=1}^{\text{ALL}} I_j} = \text{Koopmans' } -\epsilon_k$

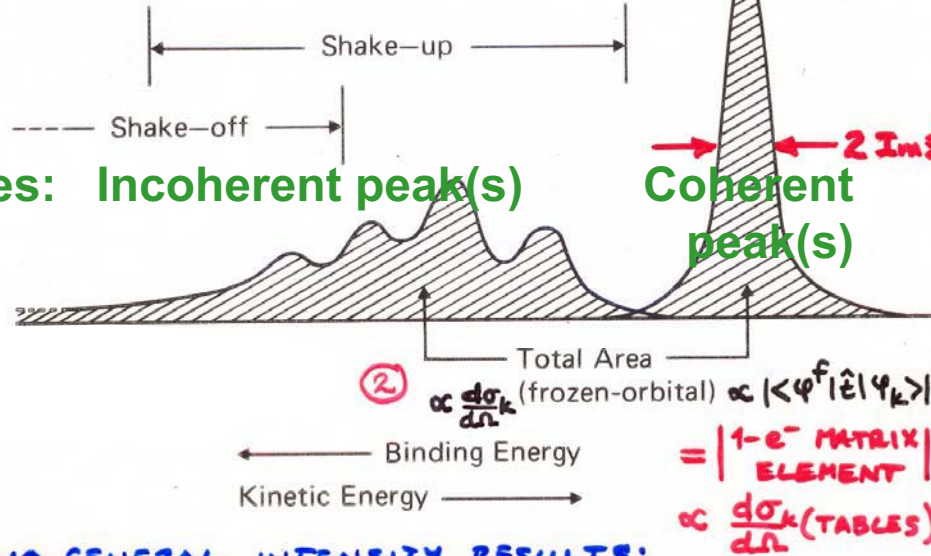
Ground-State of Ion = Adiabatic peak

$\Sigma = \text{many-body "self energy"}$
 $= \text{Re}\Sigma + i\text{Im}\Sigma$

In valence-band studies: Incoherent peak(s)

Coherent peak(s)

$\Delta E \tau_{\text{lifetime}} \approx \hbar/2$

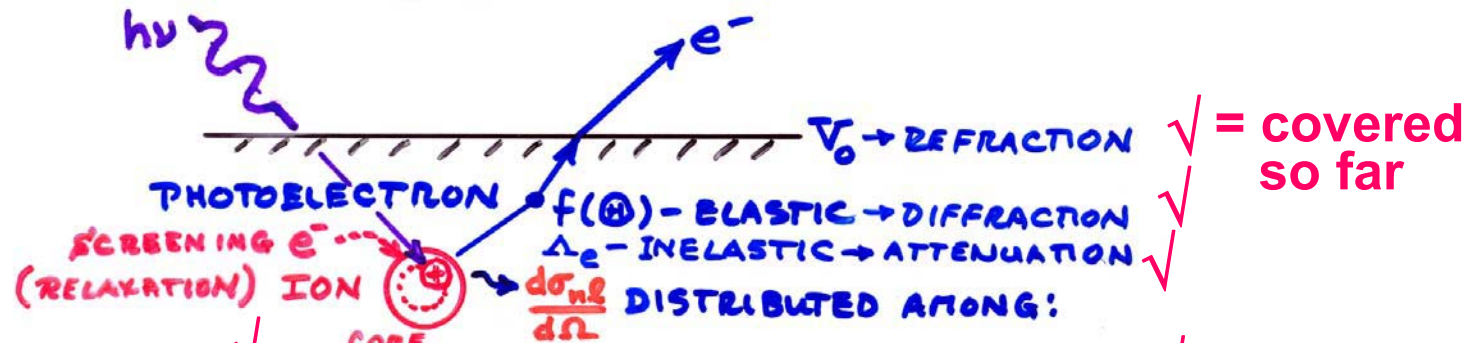


TWO GENERAL INTENSITY RESULTS:

① $I_j \propto |\langle \varphi^f(i) | \hat{\epsilon} | \varphi_k(i) \rangle|^2 |\langle \Psi^F(N-1, j) | \Psi_R(N-1) \rangle|^2$
 k e⁻ MISSING

Figure 8 -- Schematic illustration of a photoelectron spectrum involving shake-up and shake-off satellites. The weighted average of all binding energies yields the Koopmans' Theorem binding energy $-\epsilon_k$ (sum rule (77)), and the sum of all intensities is proportional to a frozen-orbital cross section σ_k (sum rule (78)). The adiabatic peak corresponds to formation of the ground-state of the ion ($E_b(k)_1 \equiv E_b(K=1)$).

② $\left(\begin{array}{l} \text{TOTAL SHAKE-UP} \\ + \text{SHAKE-OFF} \end{array} \right) = 1 - |\langle \Psi^F(N-1, 1) | \Psi_R(N-1) \rangle|^2$
 $\approx 15-25\% \text{ FOR ATOMS/MOLEC.}$

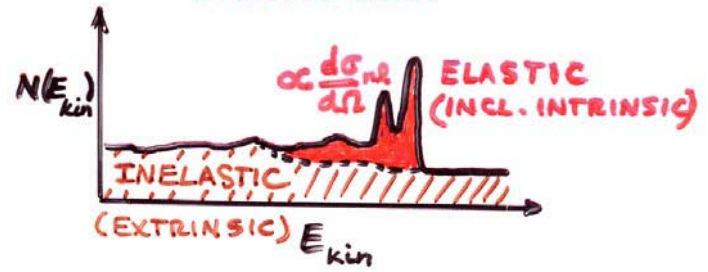


= covered so far

ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS

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- + SHAKE-UP / SHAKE-OFF / e^- -HOLE
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- + VIBRATIONAL EXCITATIONS
- + RESONANT PHOTOEMISSION ($h\nu \approx E_{b,n\ell}$)

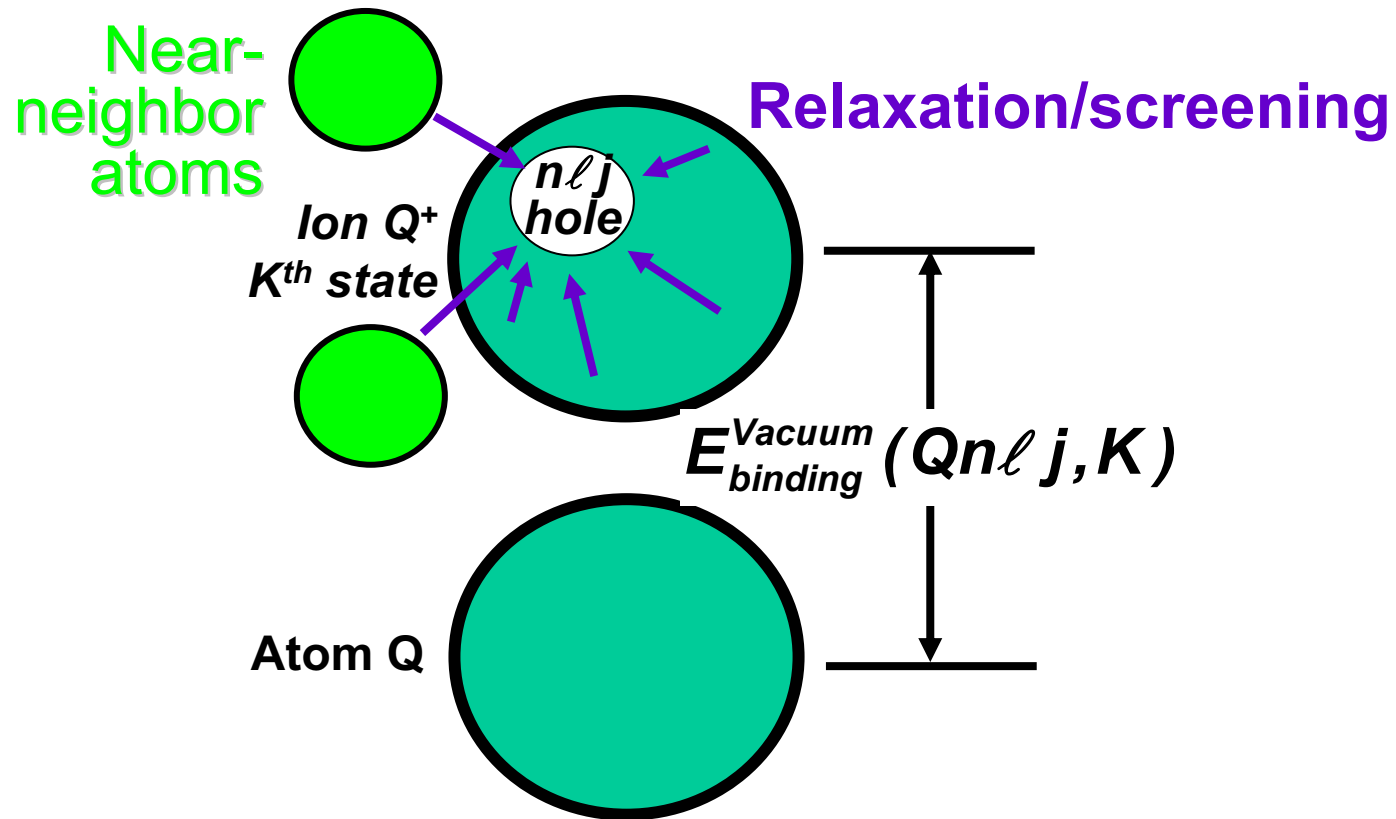
REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP

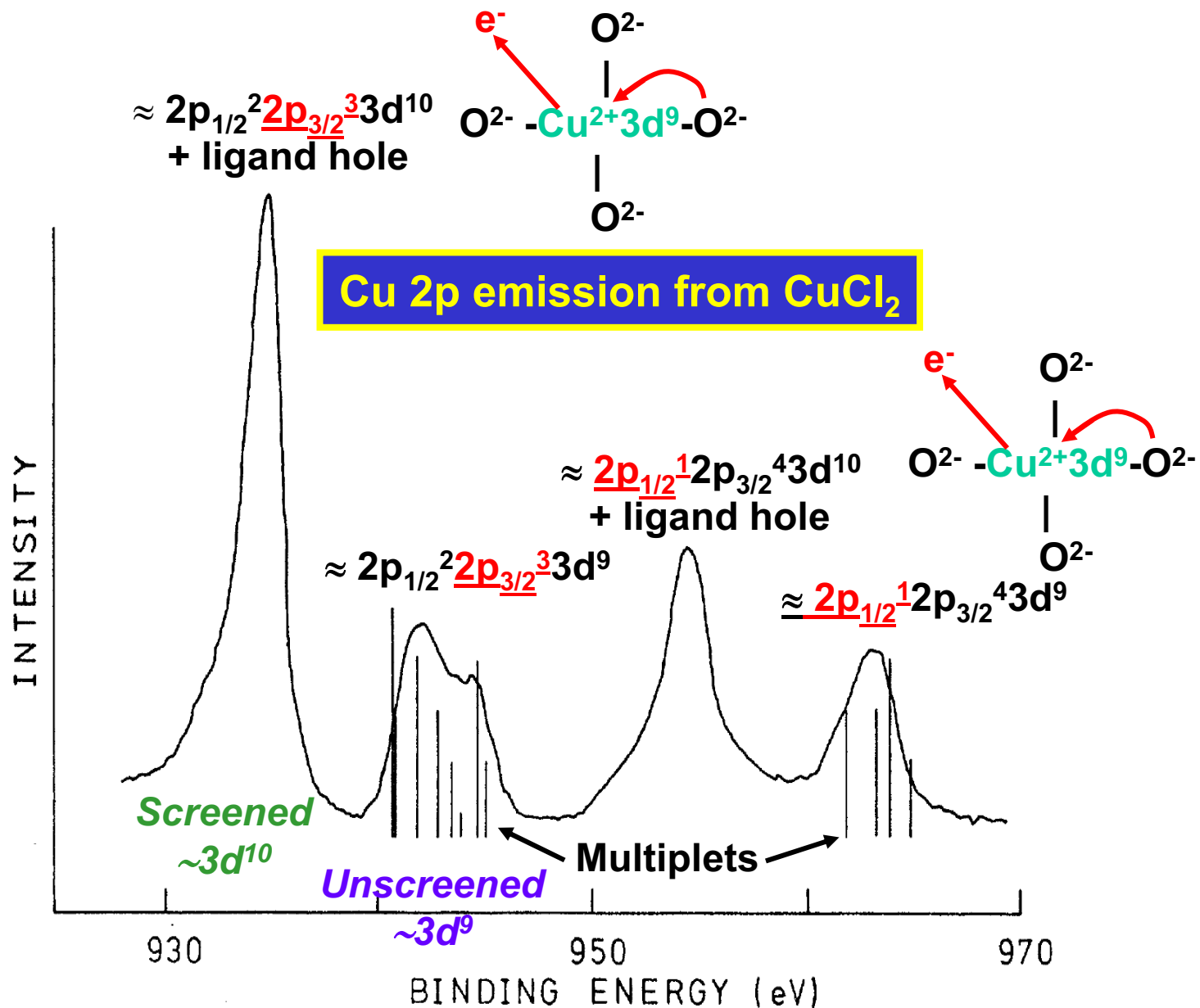


Basic energetics—Many e⁻ & many atom picture

$$h\nu = E_{\text{binding}}^{\text{Vacuum}} + E_{\text{kinetic}} = E_{\text{binding}}^{\text{Fermi}} + \varphi_{\text{spectrometer}} + E_{\text{kinetic}}$$

$$E_{\text{binding}}^{\text{Vacuum}}(Qn\ell j, K) = E_{\text{final}}(N-1, Qn\ell j \text{ hole}, K) - E_{\text{initial}}(N)$$





$$\Psi_{final,K}(N-1) = C_{1,K}(2p_{1/2}^2 2p_{3/2}^3 3d^{10} + C_{\ell} \text{ hole}) + C_{2,K}(2p_{1/2}^2 2p_{3/2}^3 3d^9)$$

Screening depends on Ionicity/covalency → satellite intensities can be used to measure interaction parameters

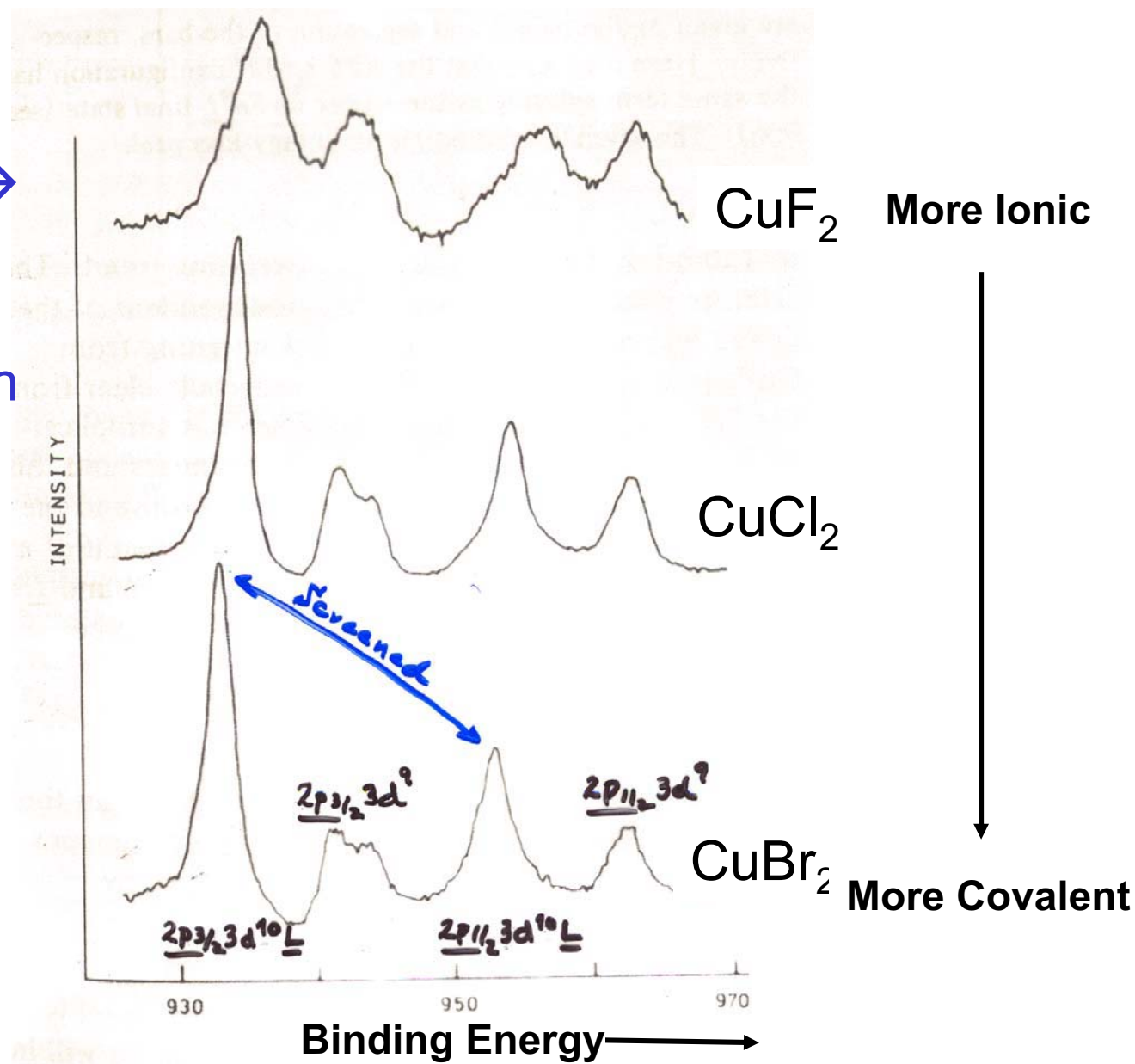


FIG. 1. Cu 2p photoelectron spectra of Cu dihalides. The lines leading to a final state with a ligand hole (L) show a chemical shift.

Screening depends on Ionicity/covalency → satellite intensities can be used to measure interaction parameters

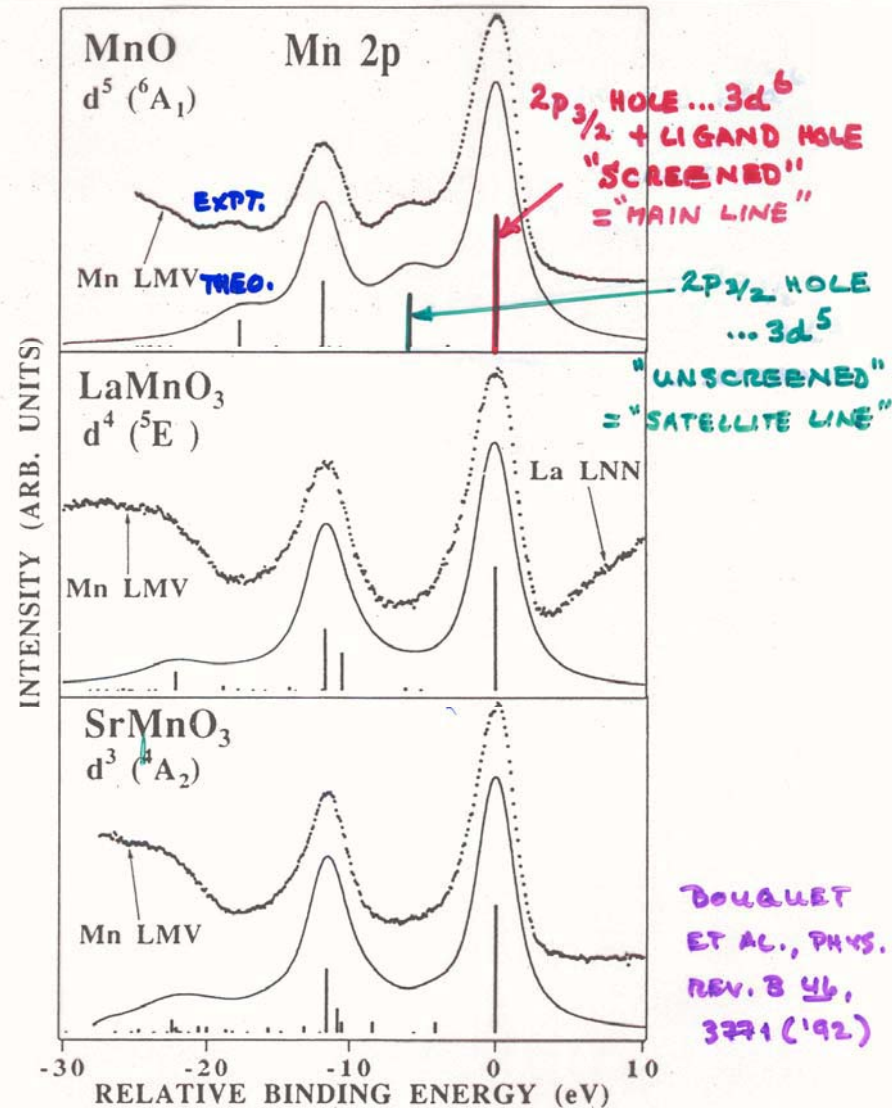
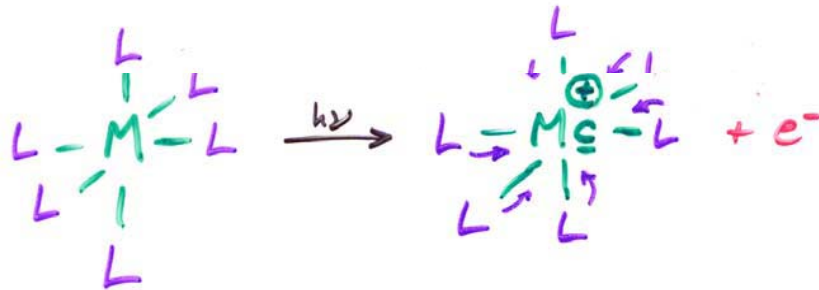


FIG. 1. Theoretical $2p$ core-level XPS spectra (solid line) compared with experimental data (dots) after background subtraction for Mn cations with varying valence. Emission due to the Mn LMV Auger peak is observed on the high-binding-energy side of the $2p_{1/2}$ spin-orbit peak, partially obscuring the $2p_{1/2}$ satellite structure.

Anderson Impurity Model Configuration Interaction Approach to Core-Hole Screening in Transition Metals and Rare Earths

(SUGANO, LARSSON → SAWATZKY, VANDER LAAN, FURIMONE, OH, ET AL.)



\underline{c} = CORE HOLE ON METAL
 \bar{l} = VALENCE (?) HOLE ON LIGAND

de Groot
computer
program

$$\psi_i = a_0 |d^n\rangle + \sum_m a_m |d^{(n+m)} \bar{l}^m\rangle$$

$$\psi_f = b_0 |\underline{c} d^n\rangle + \sum_m b_m |\underline{c} d^{(n+m)} \bar{l}^m\rangle$$

WITH INTERACTIONS OF :

Δ_0 = CRYSTAL FIELD (OFTEN NEGLECTED)

Δ = LIGAND-TO-METAL CHARGE TRANSF. ENERGY
 $= E(d^{n+1} \bar{l}) - E(d^n)$

U = d-d COULOMB REPULSION ENERGY
 $= E(d^{n-1}) + E(d^{n+1}) - 2E(d^n)$

T = LIGAND p-TO-METAL d HYBRIDIZATION
 $= \langle d_\alpha | \hat{H} | p_\alpha \rangle$ (α = SAME SYMMETRY)

Q = CORE-HOLE-TO-d INTERACTION: $\langle \underline{c} | \hat{H} | d \rangle \approx J_{cd}$

WITH INTENSITIES FROM SUDDEN APPROX.

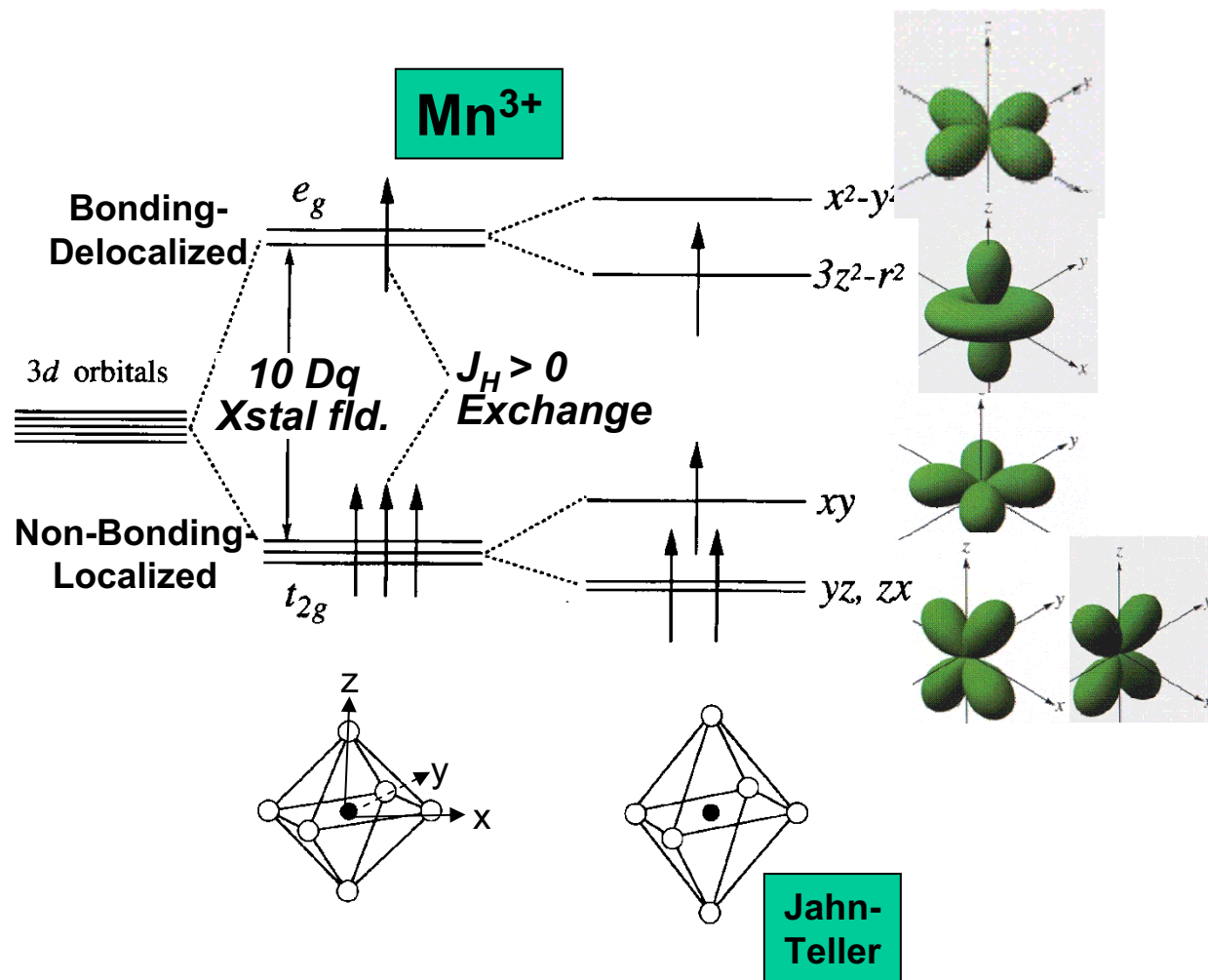
AS:

$$I(E_{kin}) \propto \sum_{f,k} |\langle \psi_f(N-1,k) | \psi_i(N-1,k) \rangle|^2 \delta(h\nu - E_f - E_{kin})$$

$\bar{l} = \underline{c}$ = CORE HOLE

WHERE: $\psi_f(N-1,k) = \psi_i(N \text{ WITH } k \text{ HOLE} = \underline{c})$

E.g.—Crystal field in Mn^{3+} with negative octahedral ligands



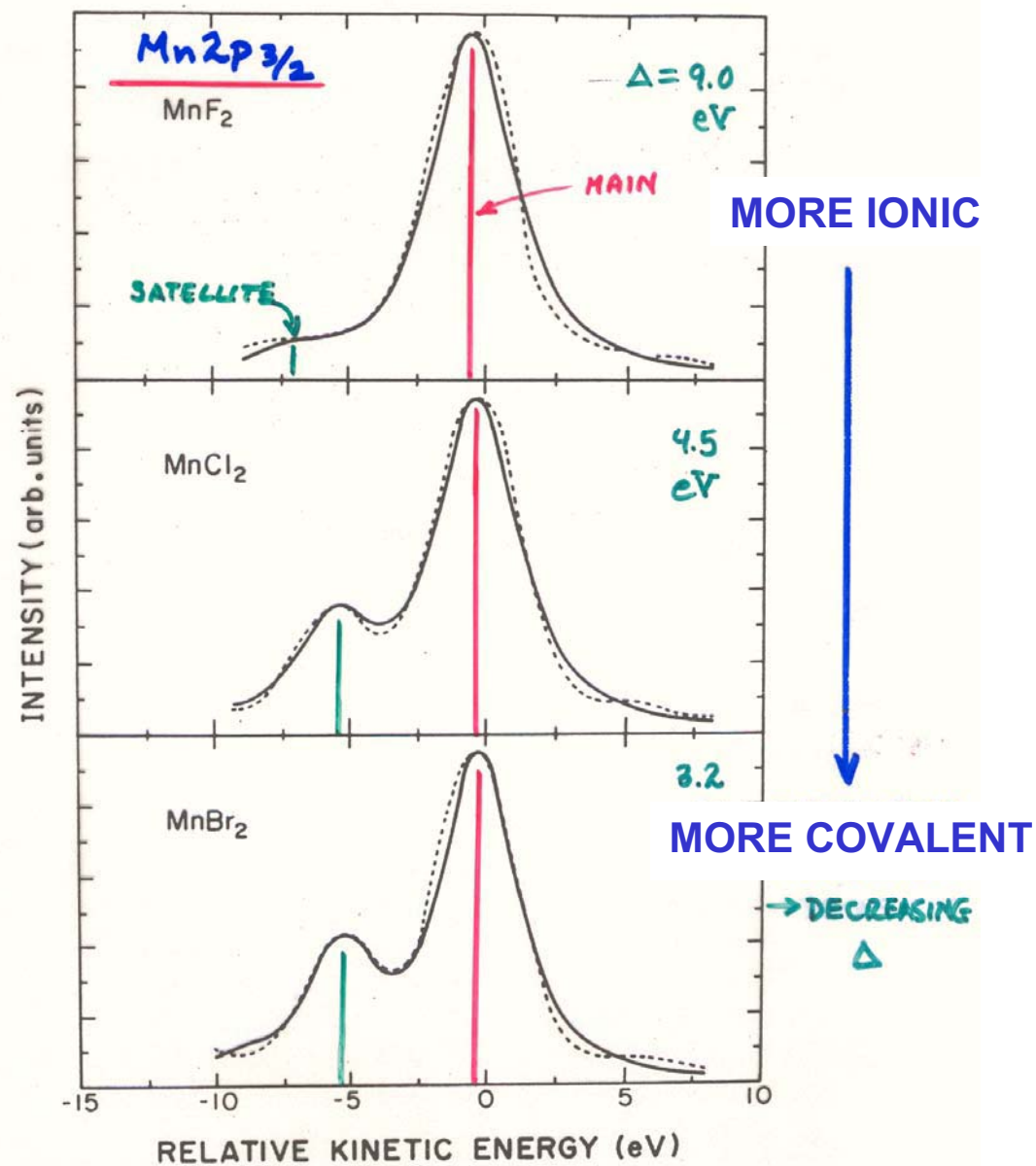
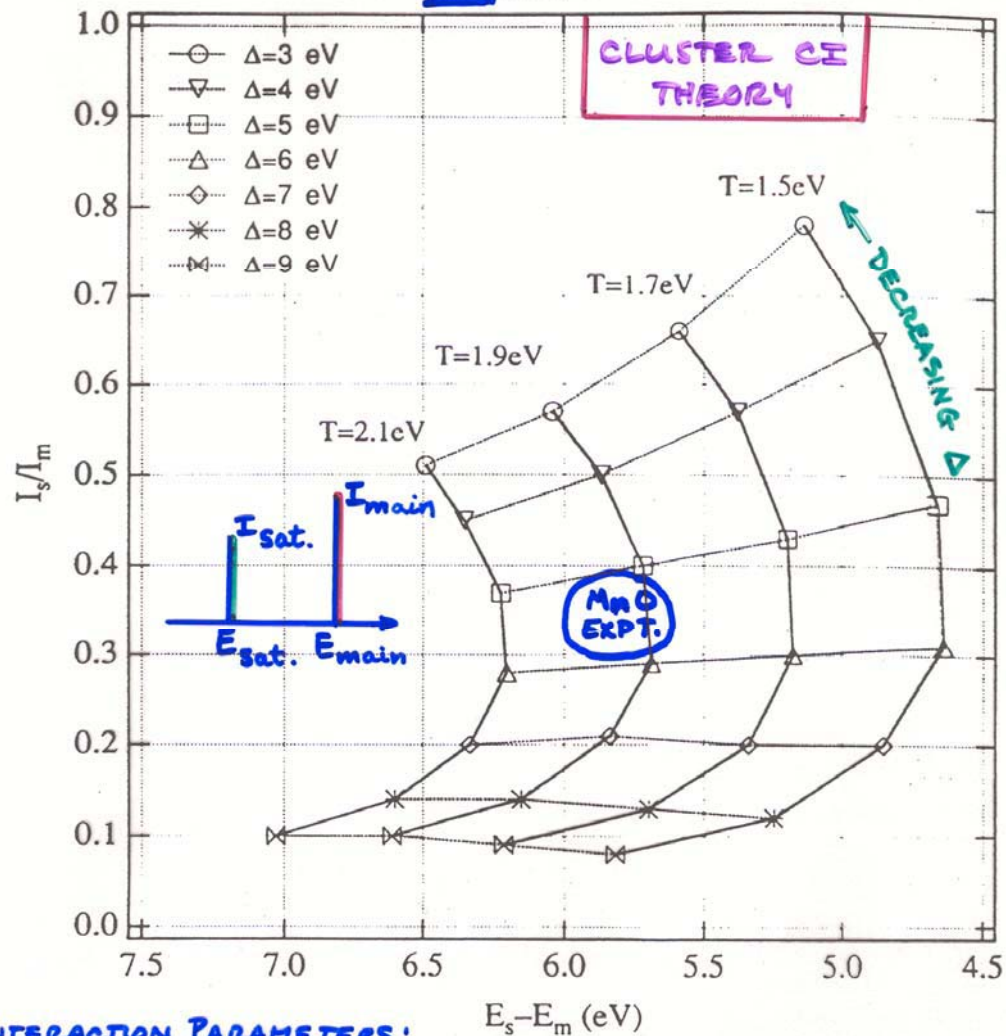


FIG. 6. Fits of the cluster model results with the experimental $2p_{3/2}$ spectra of the manganese dihalides. The parameters used are listed in Table II. A Lorentzian broadening is 2.6–3.0 eV, and a Gaussian broadening of 1.2 eV (FWHM) was used.

ANALYSIS VIA ANDERSON IMPURITY MODEL

$\text{Mn}^{2+}(\text{HS})$ $U=6.0$ eV



INTERACTION PARAMETERS:

$U = 3d-3d$ COULOMB REPULSION ENERGY

$\Delta =$ LIGAND-TO-METAL CHARGE TRANSFER ENERGY

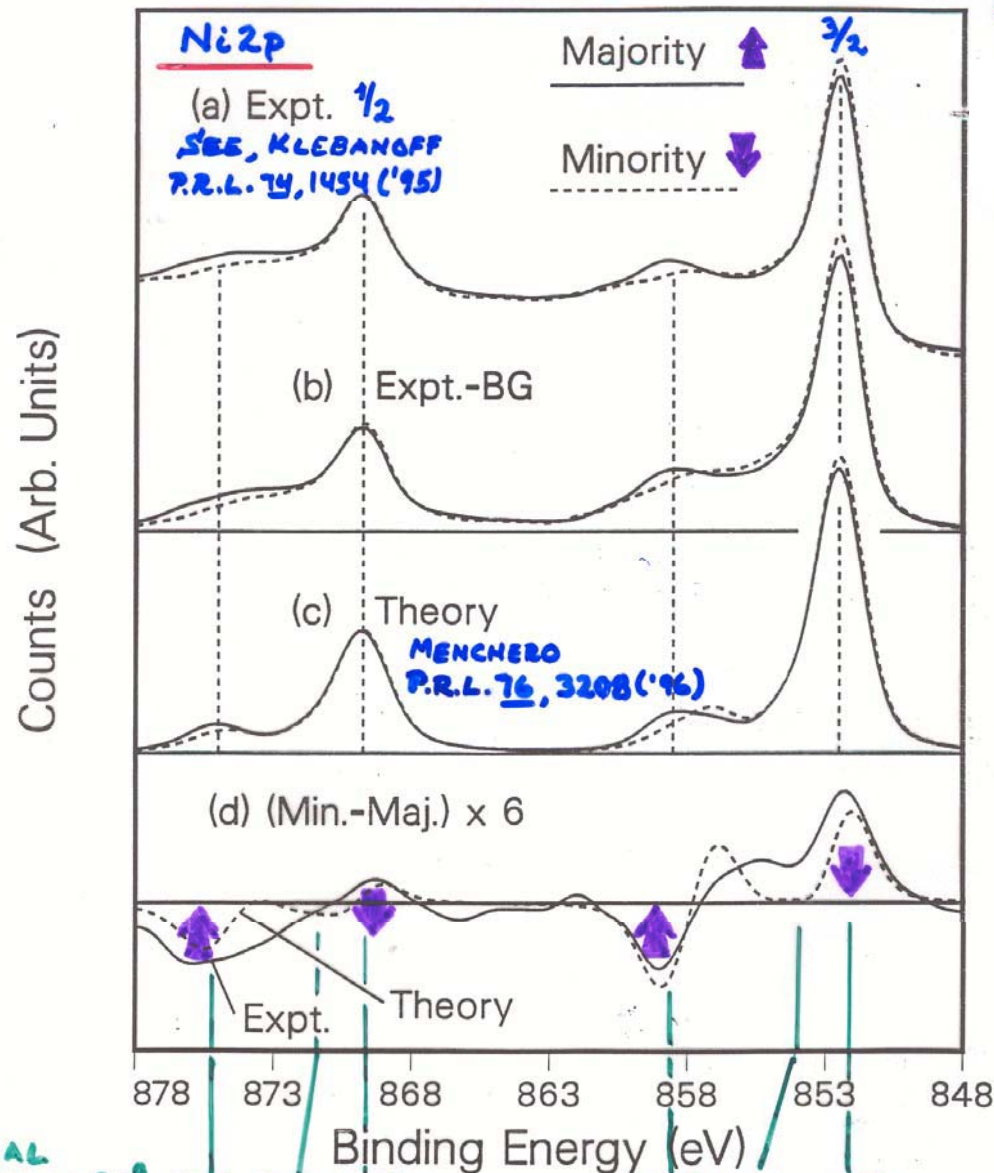
$T =$ LIGAND p - METAL $3d$ HYBRIDIZATION ENERGY

$Q =$ CORE HOLE- $3d$ COULOMB

BOUQUET ET AL.,
J. EL. SP. 82, 87 (196)

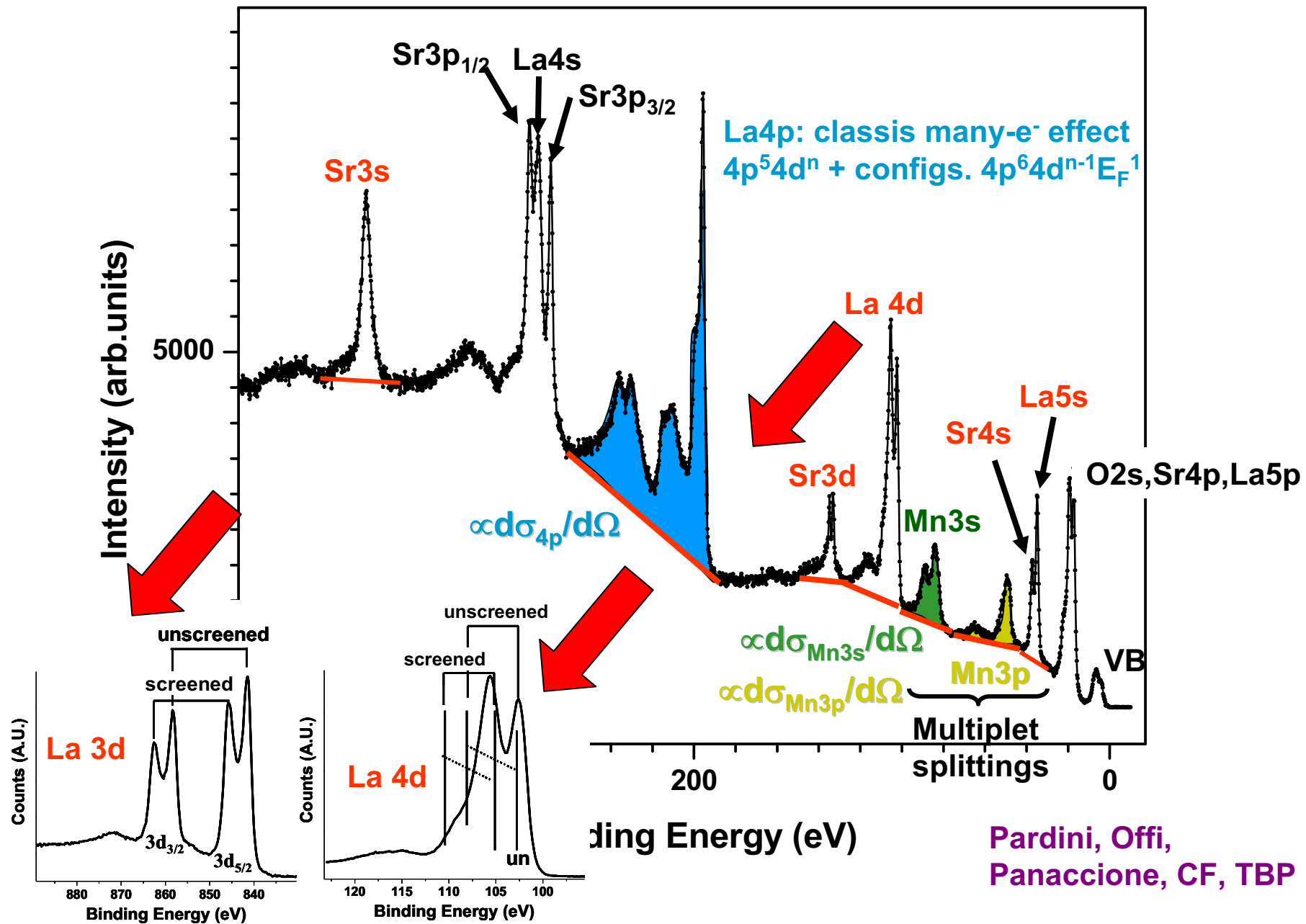
SPIN-ORBIT SPLITTING + MULTIPLETS + SCREENING IN A METAL: Ni

~15% $3d^8$
43% $3d^9$
42% $3d^{10}$

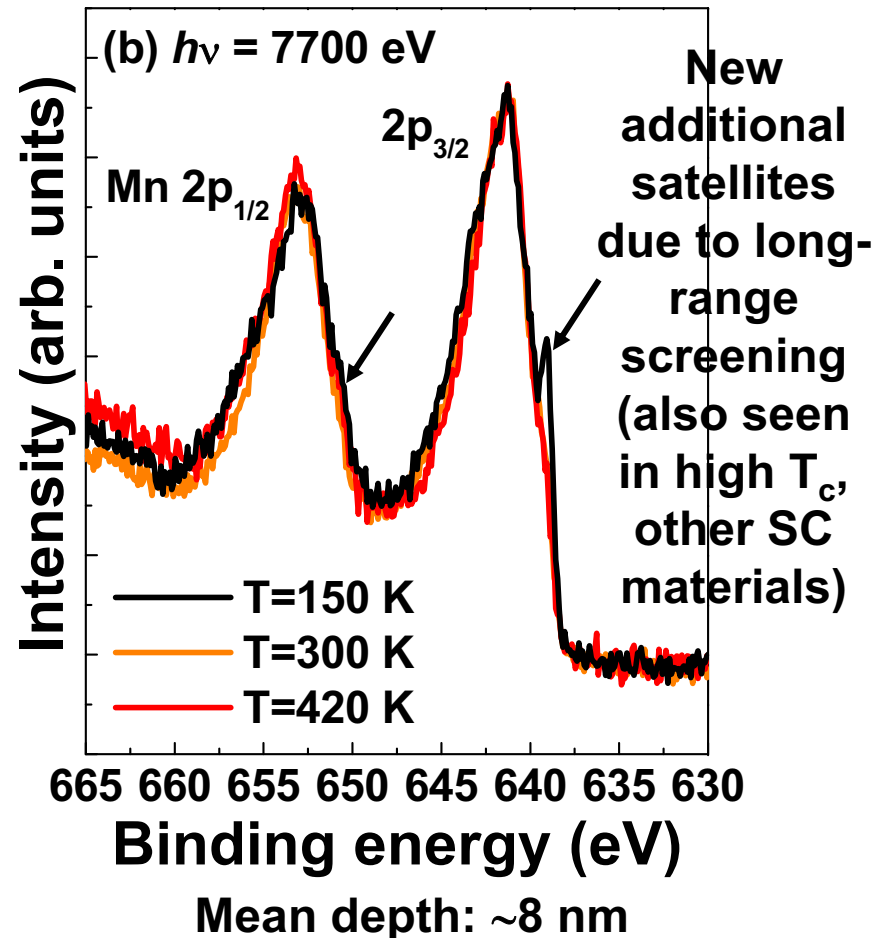
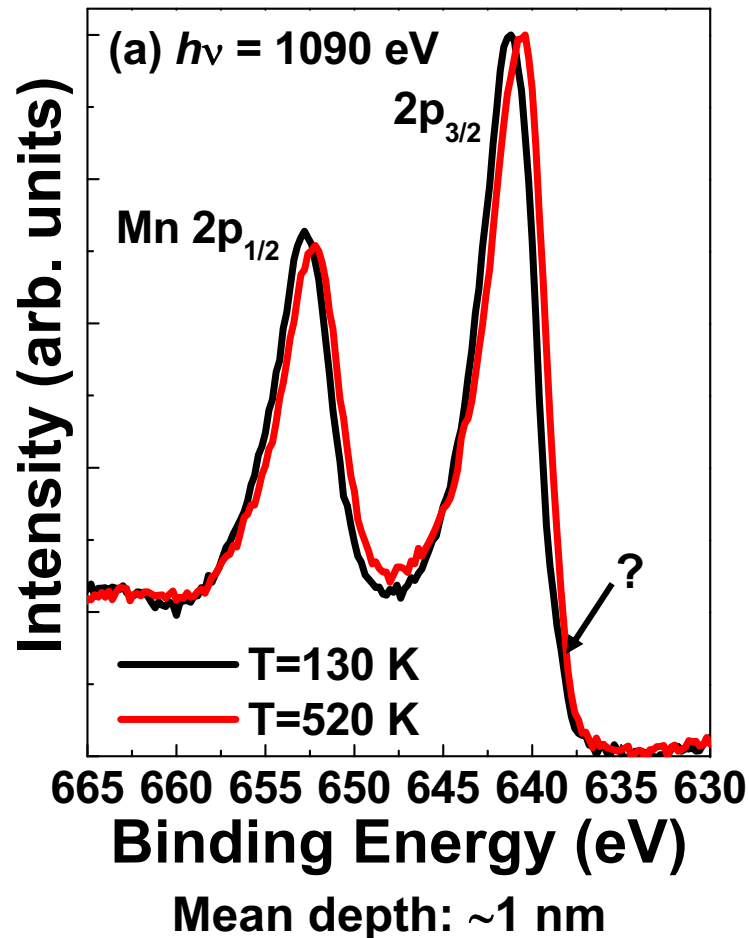


FINAL CONFIG.: $3d^9$ 65% 15% 10% "UNSCREENED" { 65% 15% 10% } "SCREENED"
 $3d^{10}$ 35% 85% 90% { 35% 85% 90% }

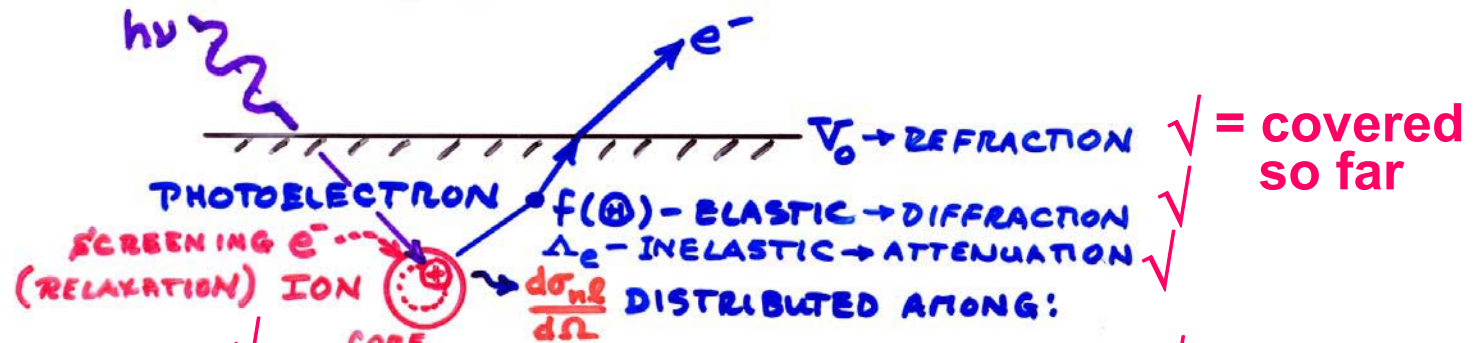
Many-electron and screening effects: $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$, $h\nu = 7700 \text{ eV}$



Temperature dependence of Mn2p spectra: $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$
 New satellite structures in hard x-ray core spectra



→ Suggests bulk electronic structure not reached until ca. 8 nm depth

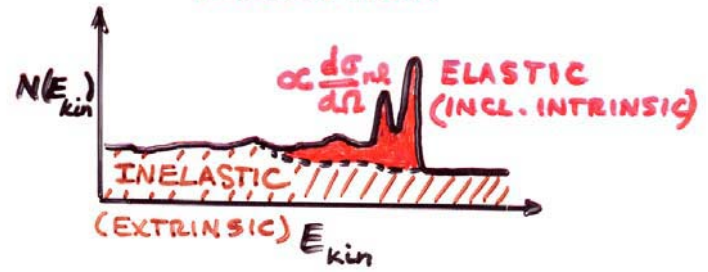


= covered so far

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REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP



INTENSITIES IN PHOTOELECTRON SPECTRA:

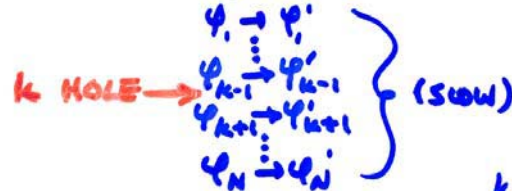
- GENERAL: FINAL STATE K (k -SUBSHELL + ALL OTHER DESIG.)

$$\text{INT.}_K \propto |\hat{e} \cdot \langle \Psi_{\text{tot}}^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_i^i(N) \rangle|^2 \quad (\text{DIPOLE APPROX.})$$

- BORN-OPPENHEIMER: e^- 's FAST, VIBRATIONS SLOW

$$\text{INT.}_K \propto \underbrace{|\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2}_{\text{FRANCIS-LONDON FACTOR}} |\hat{e} \cdot \langle \Psi_e^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_e^i(N) \rangle|^2$$

- SUDDEN APPROXIMATION: $\Psi_K \rightarrow \Psi_K = \text{PHOTO}^-$ (FAST)



$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2 \underbrace{|\langle \Psi_e^f(N-1, K) | \Psi_e^i(N-1, K) \rangle|^2}_{k \text{ MISSING}}$$

$|\hat{e} \cdot \langle \Psi_f | \vec{r} | \Psi_K \rangle|^2$ SAME SUBSHELL COUPLING +
TOTAL L, S → "MONOPOLE"
 $\hookrightarrow \text{NORMAL } \frac{d\sigma_K}{d\Omega}$

- SLATER DETS. FOR $\Psi_e^f = \det(\psi'_1, \psi'_2, \dots, \psi'_{k-1}, \psi'_{k+1}, \dots, \psi'_N)$

$$\Psi_e^i = \det(\psi_1, \psi_2, \dots, \psi_{k-1}, \psi_{k+1}, \dots, \psi_N)$$

$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2 \underbrace{|\langle \psi'_1 | \psi_1 \rangle|^2 |\langle \psi'_2 | \psi_2 \rangle|^2 \dots}_{\text{SHAKE-UP/OFF}} \dots$$

$$|\langle \psi'_{k-1} | \psi_{k-1} \rangle|^2 |\langle \psi'_{k+1} | \psi_{k+1} \rangle|^2 \dots |\langle \psi'_N | \psi_N \rangle|^2$$

$|\hat{e} \cdot \langle \Psi_f | \vec{r} | \Psi_K \rangle|^2$
1e- DIPOLE → $d\sigma/d\Omega$

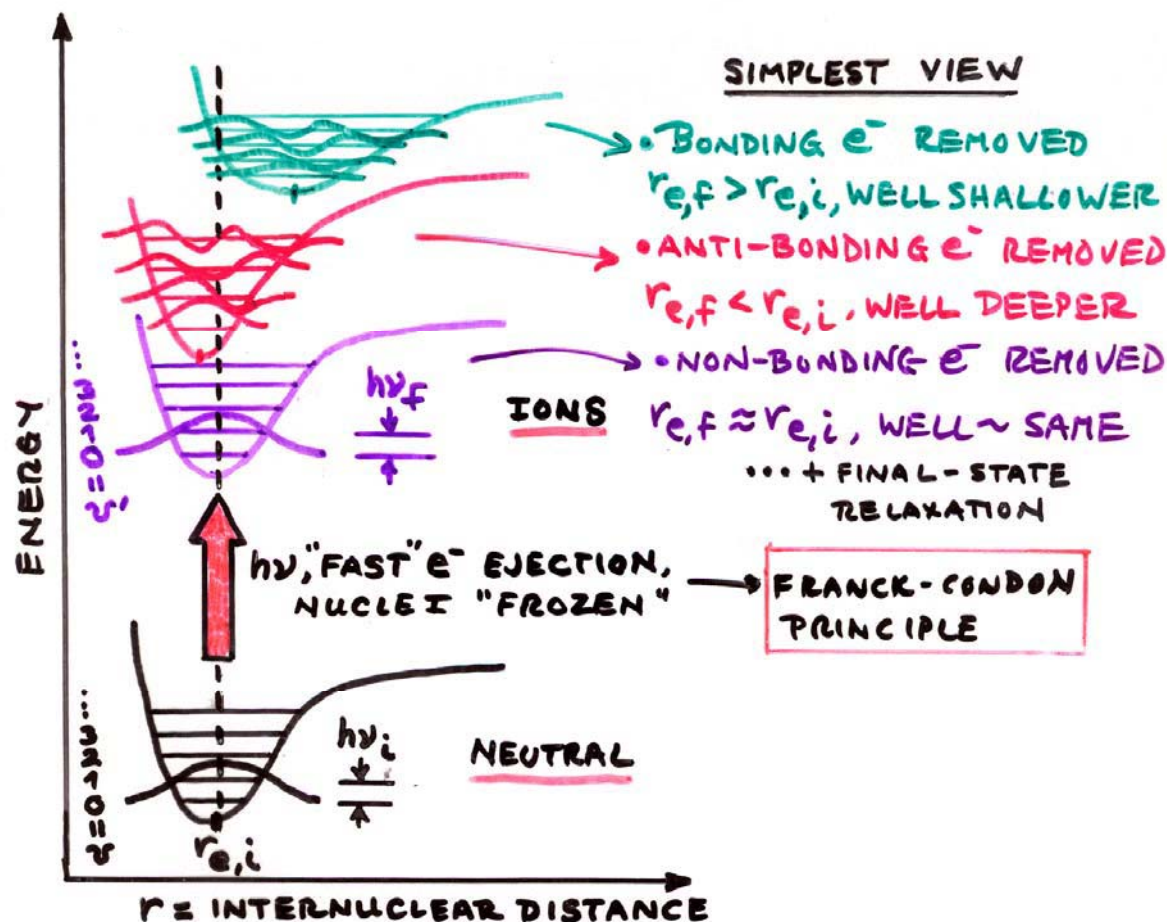
(N-1)e- SHAKE-UP/
 SHAKE-OFF →
 "MONOPOLE"

- PLUS DIFFRACTION EFFECTS IN Ψ_f ESCAPE

VIBRATIONAL STRUCTURE IN VALENCE-LEVEL (MO) SPECTRA

Diatomic A-B example

(Also applies to core-level emission if equilibrium distance changes on forming core hole)

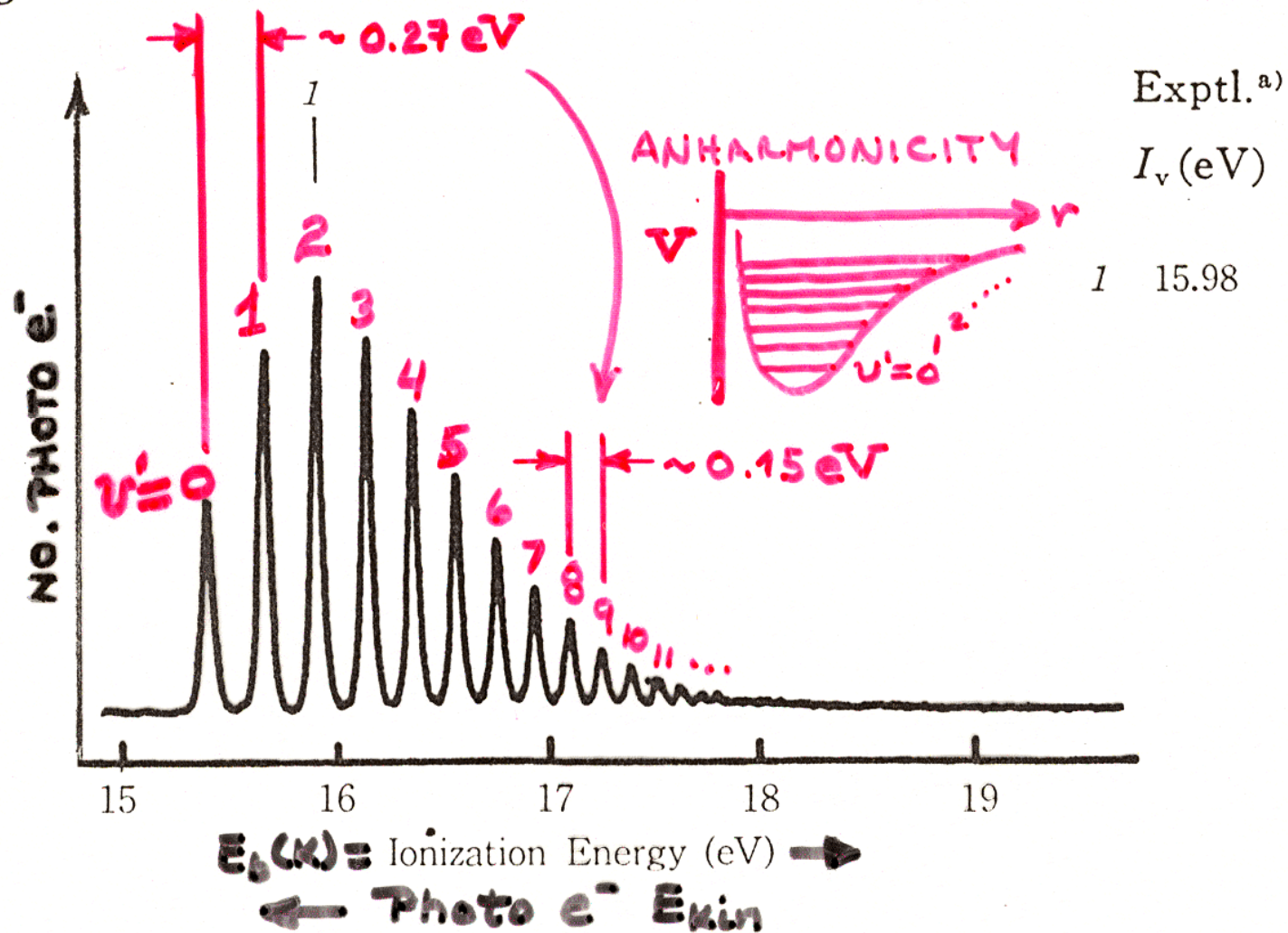


e^- REMOVED	r_e	$h\nu_{VIB}$	BAND APPEARANCE
BONDING	$r_{e,f} > r_{e,i}$	$h\nu_f < h\nu_i$	<p>$v=0 \rightarrow v'=0$ ="ADIABATIC" "VERTICAL" = MOST INTENSE</p>
ANTI-BONDING	$r_{e,f} < r_{e,i}$	$h\nu_f > h\nu_i$	<p>$v'=10$ $v=0 \rightarrow v'=10$</p>
NON-BONDING (E.G., LONE PAIR)	$r_{e,f} \approx r_{e,i}$	$h\nu_f \approx h\nu_i$	<p>$v=A$ $v=A$</p>

← I.P. = E_b

VIBRATIONAL STRUCTURE IN VALENCE-LEVEL (MO) SPECTRA

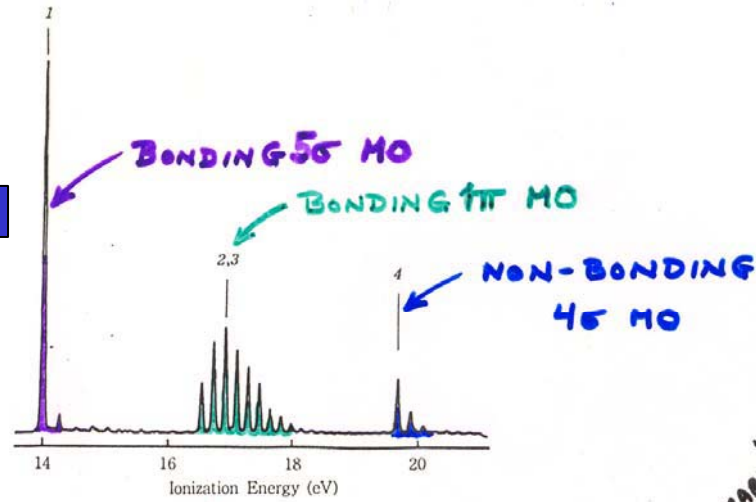
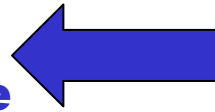
H₂ Hydrogen



(9) CO Carbon Monoxide

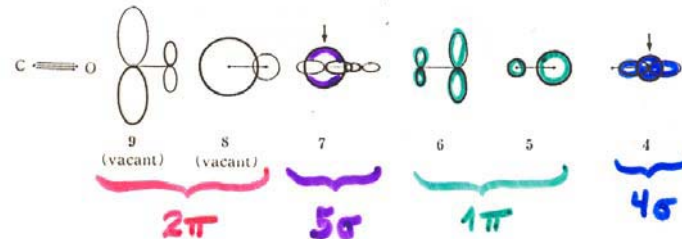
UV PHOTOELECTRON SPECTRUM OF CO

Vibrational fine structure



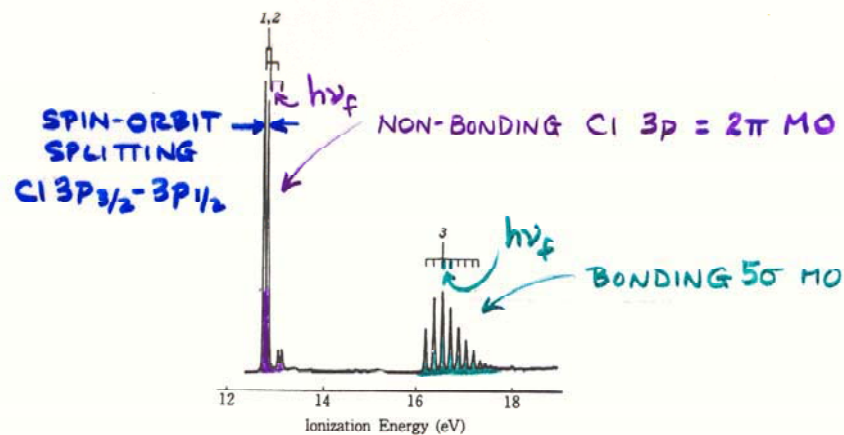
Exptl. ^{a)} I_v (eV)	SCF MO [6-31 G] ^{b)}		CI FINAL STATE "PRIMARY HOLES"		
	$-\epsilon$ (eV)	MO Character	E (eV)	State	Configuration
1 14.01	14.99	5σ (7) σ_{CO}	13.11	$1^2\Sigma^+$	0.93(7 ⁻¹) -0.15(6 ⁻¹ , 7 ⁻¹ , 9 ¹) _x -0.15(5 ⁻¹ , 7 ⁻¹ , 8 ¹) _x
2 16.91	17.48	1π (6, 5) π_{bond}	16.69	$1^2\Pi$	0.95(6 ⁻¹) ; 0.95(5 ⁻¹)
3 16.91	17.48				
4 19.72	21.69	4σ (4) n_O	19.29	$2^2\Sigma^+$	0.92(4 ⁻¹) +0.16(6 ⁻¹ , 7 ⁻¹ , 9 ¹) _x +0.16(5 ⁻¹ , 7 ⁻¹ , 8 ¹) _x

a) The spectrum : this work. The I_v 's : Turner *et al.* (215). See also other works : Turner and May (215 a) ; Carlson and Jonas (54) ; Gardner and Samson (104) ; Edqvist *et al.* (90) ; Potts and Williams (182 a) ; and Natalis *et al.* (165).
 b) We used the bond length reported (A 3) ; symmetry $C_{\infty h}$. $E_{SCF} = -112.6672$ hartree. In 4-31G calculations, $E_{SCF} = -112.5524$ hartree and $-\epsilon$ (eV) = 14.93, 17.41, 17.41, and 21.60.
 c) CI-II. (9, 8) = 1π. |N> = 0.98 (SCF). The results obtained in other CI levels are given in Appendix B.



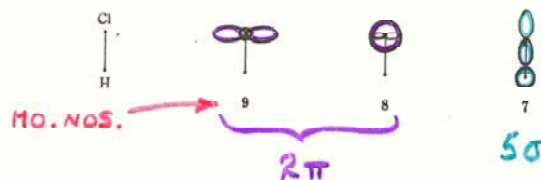
Kimura et al.,
 "Handbook of Hel
 Photoelectron Spectra"

THE UV PHOTOELECTRON SPECTRUM OF HCl



Exptl. ^{a)}	SCF MO [4-31 G] ^{b)}		Koopmans' Theo. CONFIG. INT. ON FINAL STATE			
	I, (eV)	-ε (eV)	MO	Character	~Cl (Ionic State) [4-31 G] ^{c)}	
					E (eV) State Configuration	
1	12.75	12.77	2π (9, 8)	n _{Cl}	11.97 1 ² I ⁻ 0.98(9 ⁻¹); 0.98(9 ⁻¹)	Cl HOLE
2	12.85	12.77				WEIGHTING
3	16.28	16.50	σ (7)	σ _{HCl}}	16.10 1 ² Σ ⁺ 0.98(7 ⁻¹)	

- a) The spectrum: this work. The I_v's: Frost *et al.* (102). See also other works: Lempka *et al.* (150); Turner *et al.* (215); and Weiss *et al.* (224).
 b) We used the bond length reported in Ref. (A 5); symmetry C_{∞v}. E_{SCF} = -459.5631 hartree.
 c) CI-V: |N⟩ = 0.99 (SCF).
 CI-V': E (eV) = 12.01 and 16.11.
 CI-III: E (eV) = 12.60 and 16.79.



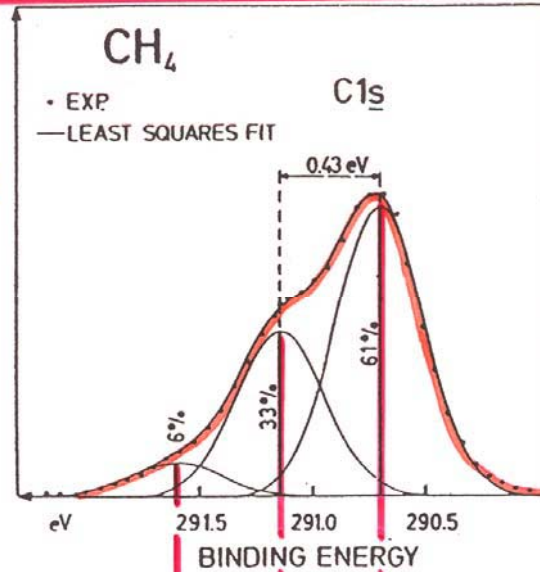
(FROM KIMURA ET AL., "HANDBOOK OF He I PHOTO-ELECTRON SPECTRA OF FUND. ORGANIC MOLECULES")

VIBRATIONAL FINE STRUCTURE IN CORE SPECTRA

MONOCHROMATIZED
LABORATORY
X-RAY SOURCE

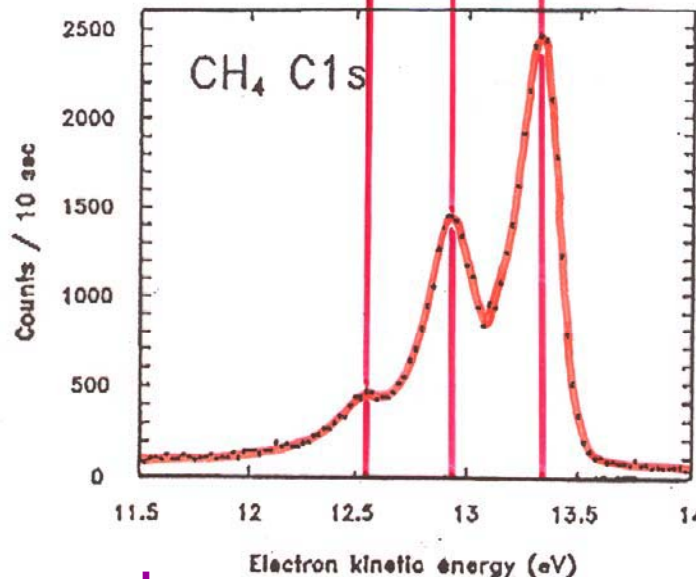
1970
SIEGBAHN,
GELWIS,
ET AL.

"Basic Concepts of XPS"
Figure 40

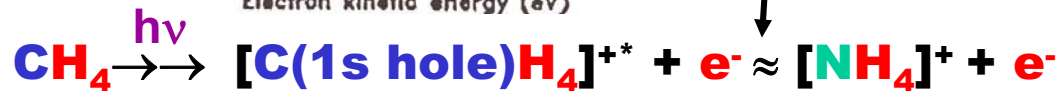


NEW SR
BEAMLINE
AT
BROOK-
HAVEN
(~5-10X
FASTER
@ALS)

1991
BRADSHAW,
KAINDL,
ET AL.

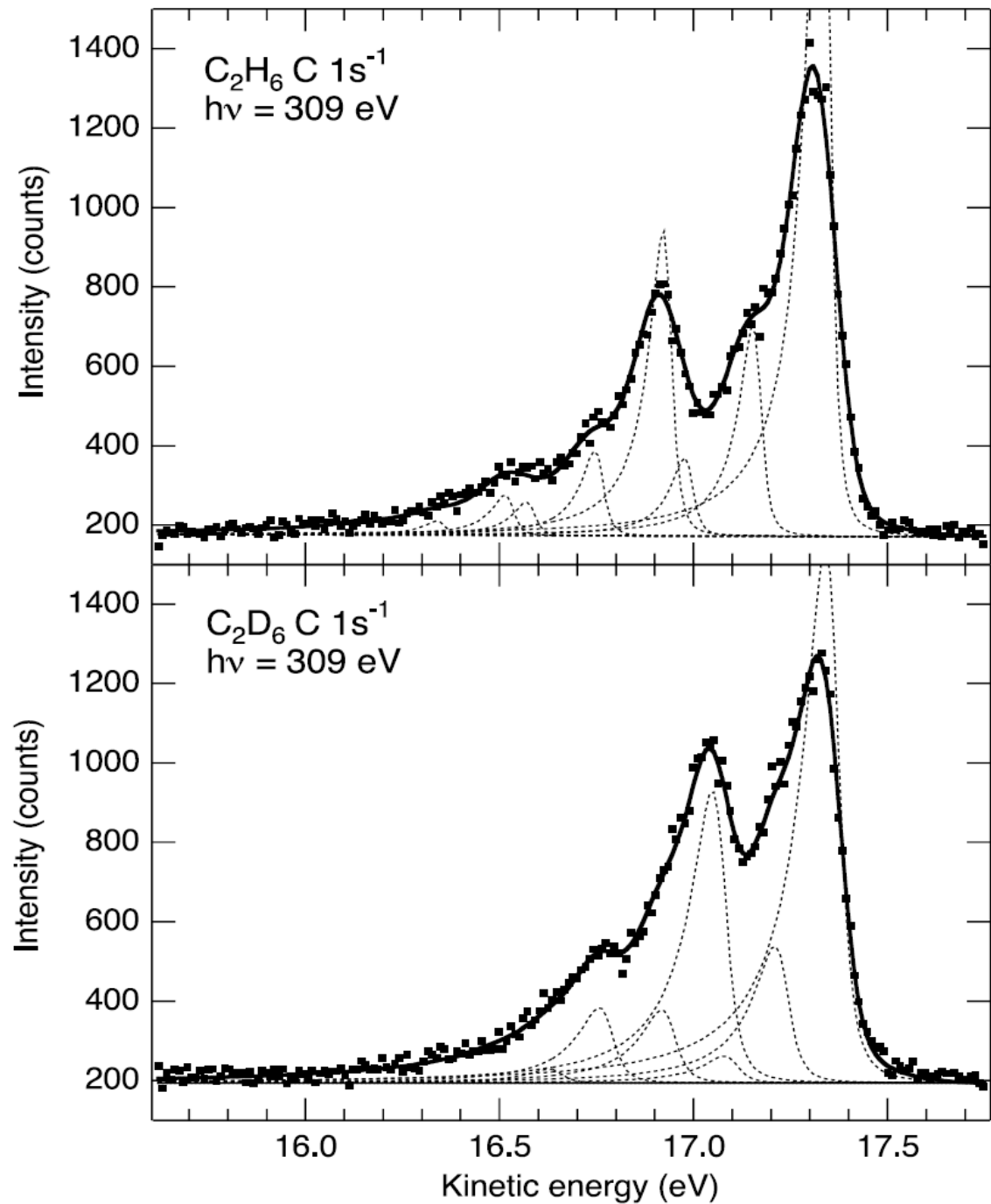


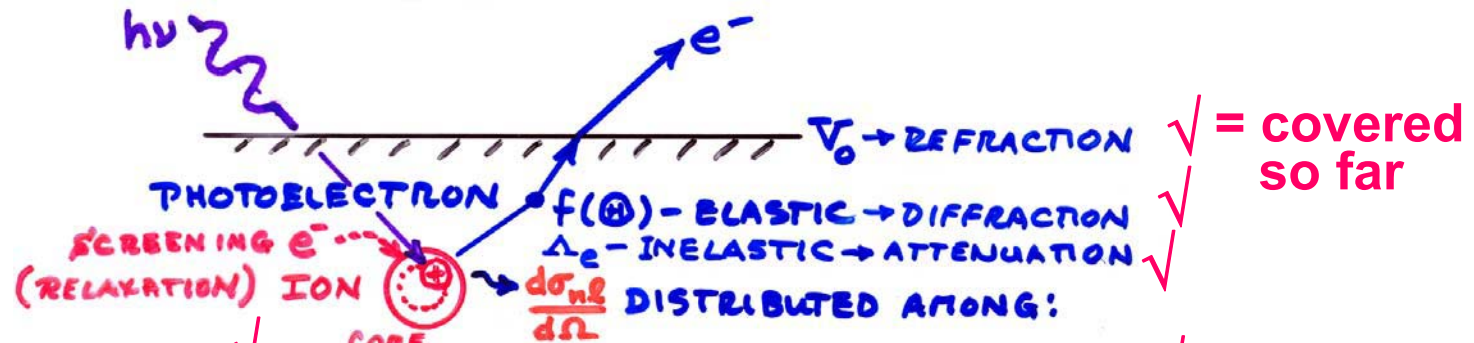
CH distance = 1.10 Å
NH distance = 1.00 Å
Equivalent-core



Vibrational fine structure in C 1s photoemission from ethane: two progressions ν_a at 0.407 eV and ν_b at 0.176 eV and various excitations (ν_a, ν_b)

Rennie et al.,
J. Phys. At. Mol. Opt. Phys. 32, 2691 (1999)



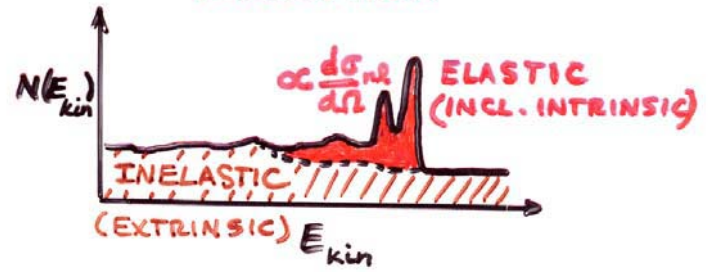


= covered so far

ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS

- + SPIN-ORBIT SPLITTING (EASY)
- + MULTIPLLET SPLITTING (OPEN-SHELL SYSTEMS), XSTAL FIELD
- + CORRELATION / CONFIGURATION INTERACTION
- + SHAKE-UP / SHAKE-OFF / e^- -HOLE
- + SCREENING / NON-SCREENING: CONFIGURATION INTERACTION
- + VIBRATIONAL EXCITATIONS
- + RESONANT PHOTOEMISSION ($h\nu \approx E_{b,n\ell}$)

REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP



Outline

Surface, interface, and nanoscience—short introduction

Some surface concepts and techniques→photoemission

Synchrotron radiation: experimental aspects

Electronic structure—a brief review

**The basic synchrotron radiation techniques:
more experimental and theoretical details**

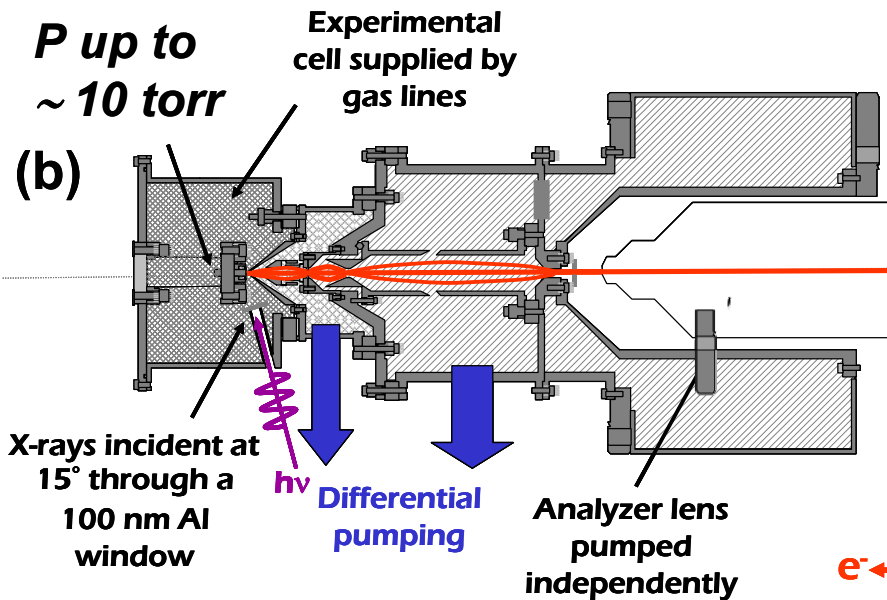
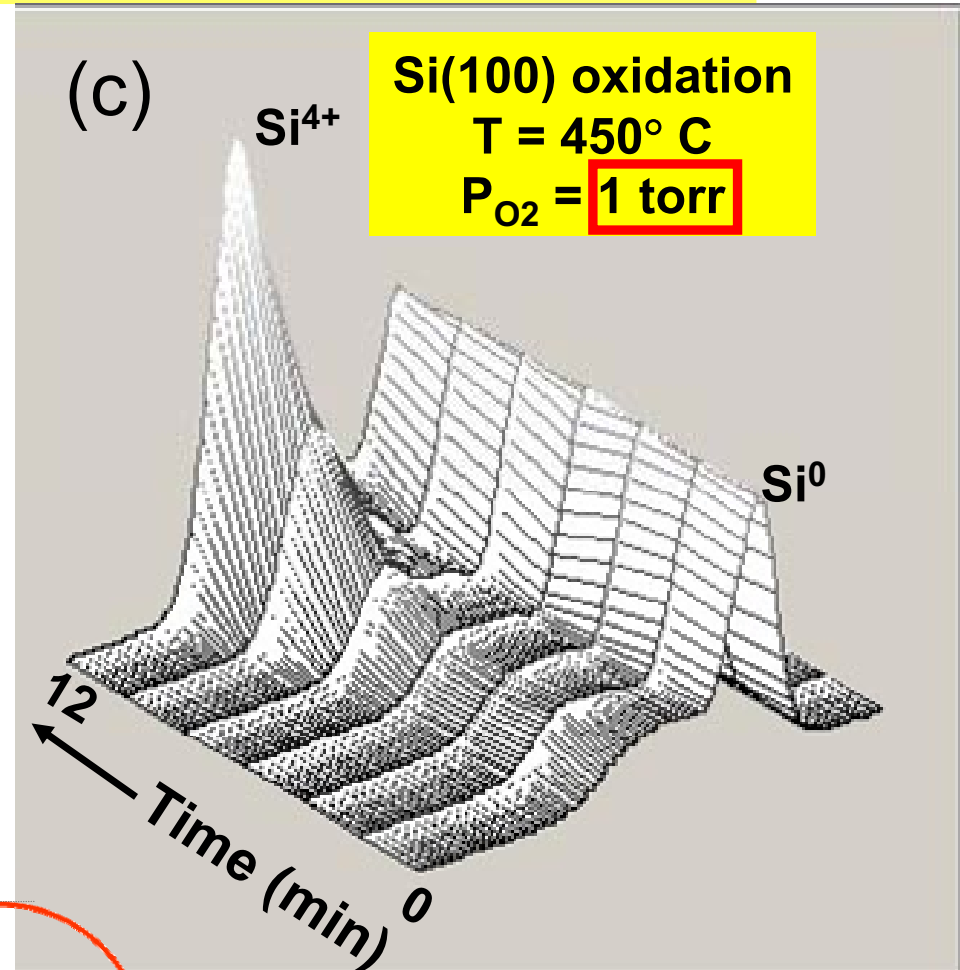
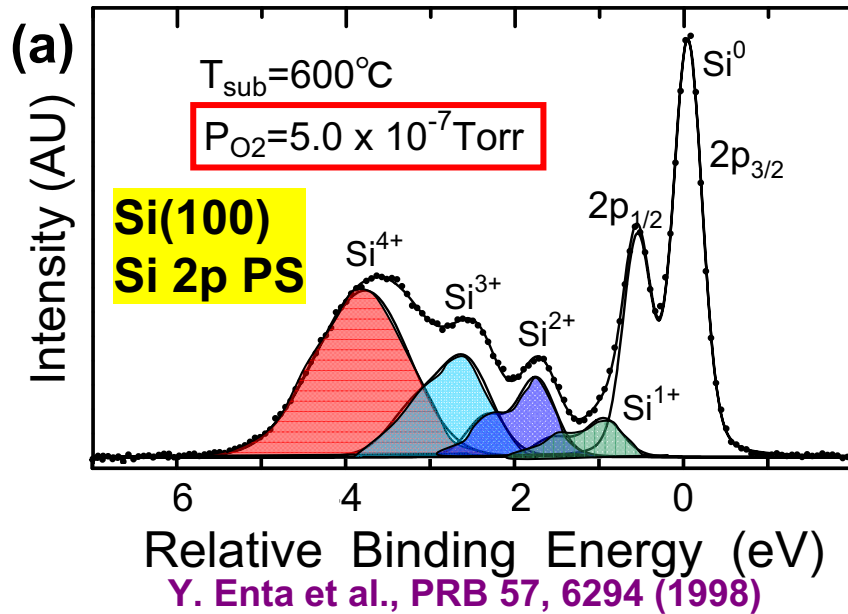
Valence-level photoemission

Core-level photoemission



**Photoemission with high ambient pressure
around the sample**

Bridging the Pressure Gap: Chemical-State- and Time-Resolved Oxidation of Si at Multi-Torr Pressures

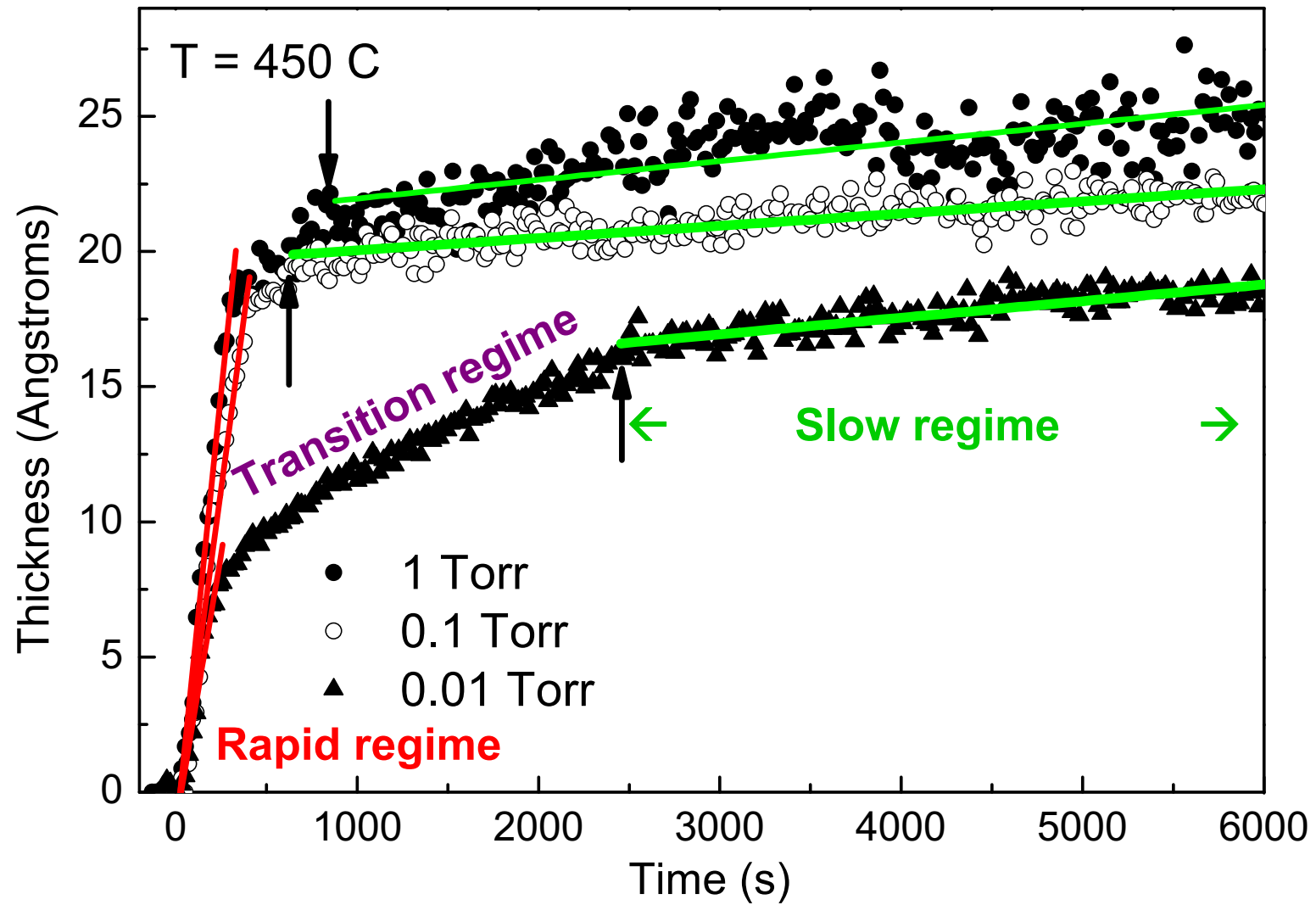


Energy Analysis $P \approx 10^{-7} \text{ torr}$ or better

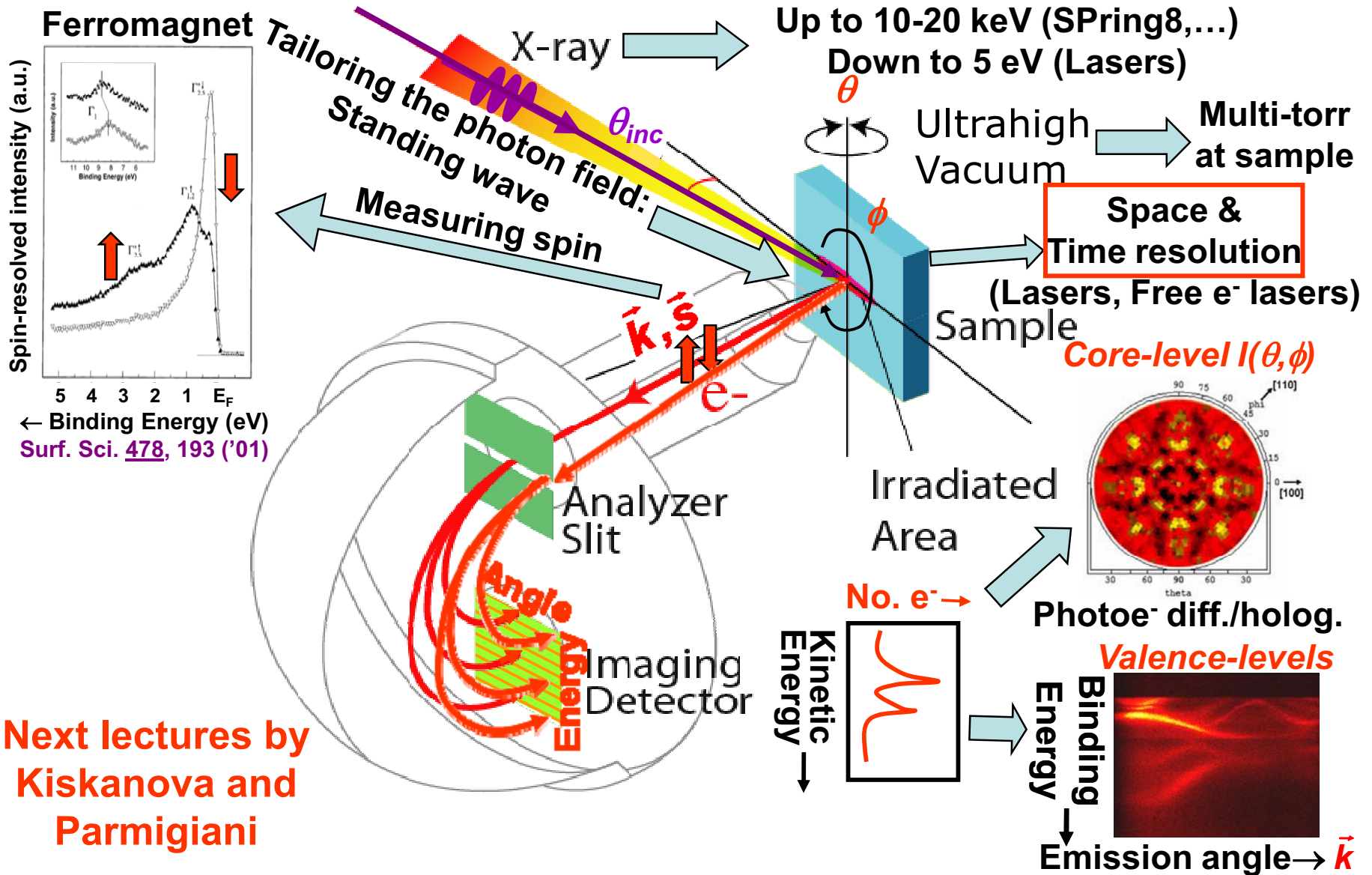
Ogletree et al., Rev. Sci. Instr. 73, 3872 (2002)—SR, ALS
 Bluhm, Salmeron, Schlögl—ALS, BESSY

Enta, Mun et al., Appl. Phys. Lett. 92, 012110 (2008); J. Appl. Phys. 103, 044104(2008)

Watching the oxide grow in real time: constant P, variable T



Typical experimental geometry for energy- and angle-resolved photoemission measurements



Next lectures by
Kiskanova and
Parmigiani

Thank you for your attention!