



The Abdus Salam  
International Centre for Theoretical Physics



1936-33

**Advanced School on Synchrotron and Free Electron Laser Sources  
and their Multidisciplinary Applications**

*7 - 25 April 2008*

**Very low-photoemission spectroscopy.**

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*Sincrotrone Trieste*  
*Italy*

Very low-energy  
photoemission spectroscopy

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Sincrotrone Trieste S.C.p.A.



# Outline

- How low photon energy are produced
- The Bad ElPh beamline
- Reasons for low photon energy: bulk sensitivity, higher momentum resolution, good energy resolution easier
- Sudden Approx still valid?
- Final state effects?
- Other problems

# How low photon energies can be obtained ?

## 1) Gas discharge lamp (He=21.22 eV, Ne=16.85 eV, Ar= 11.62-11.83 eV, H<sub>2</sub>= 10.2 eV)

Large spot size (several mm),  $\sim 10^{14}$  photons/s, intrinsic linewidth  $\sim 1$ -2meV  
satellite lines

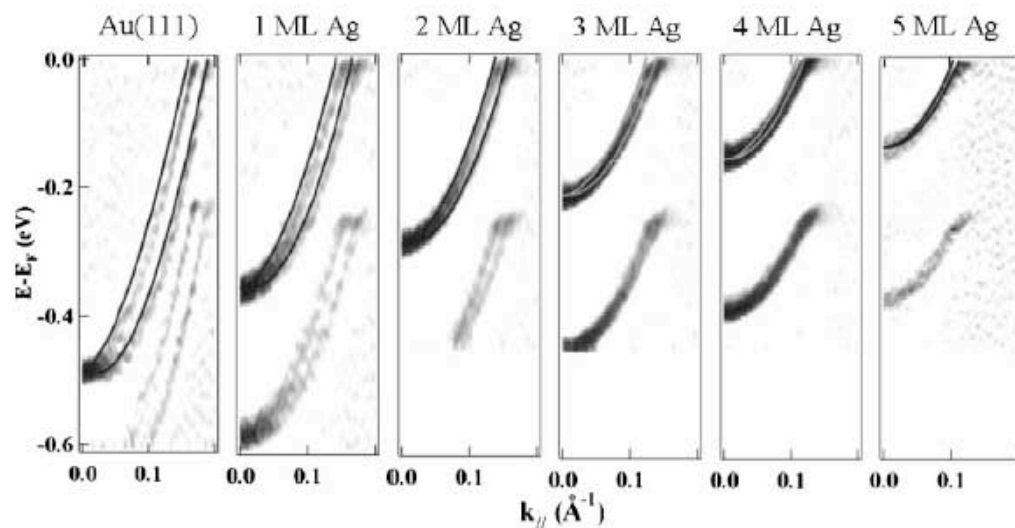
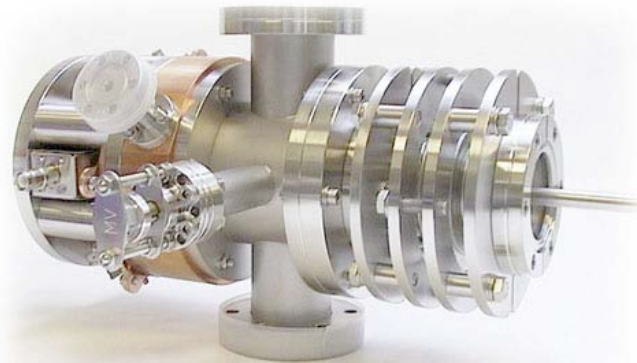


FIG. 2. Surface state dispersion changes with silver coverage taken with Ar I. The grey-scale maps represent the second derivative of the measured intensity. The calculations of the Shockley state (black lines) have been shifted for each coverage to fit the measured binding energies. The replica at higher BEs is due to the Ar satellite.

# How low photon energies can be obtained ?

## 2) Laser systems (6 - 7 eV)

Spot size 1-500 $\mu\text{m}$ ,  $> 10^{15}$  photons/s on the sample, intrinsic linewidth 0.26-0.1meV, only one energy

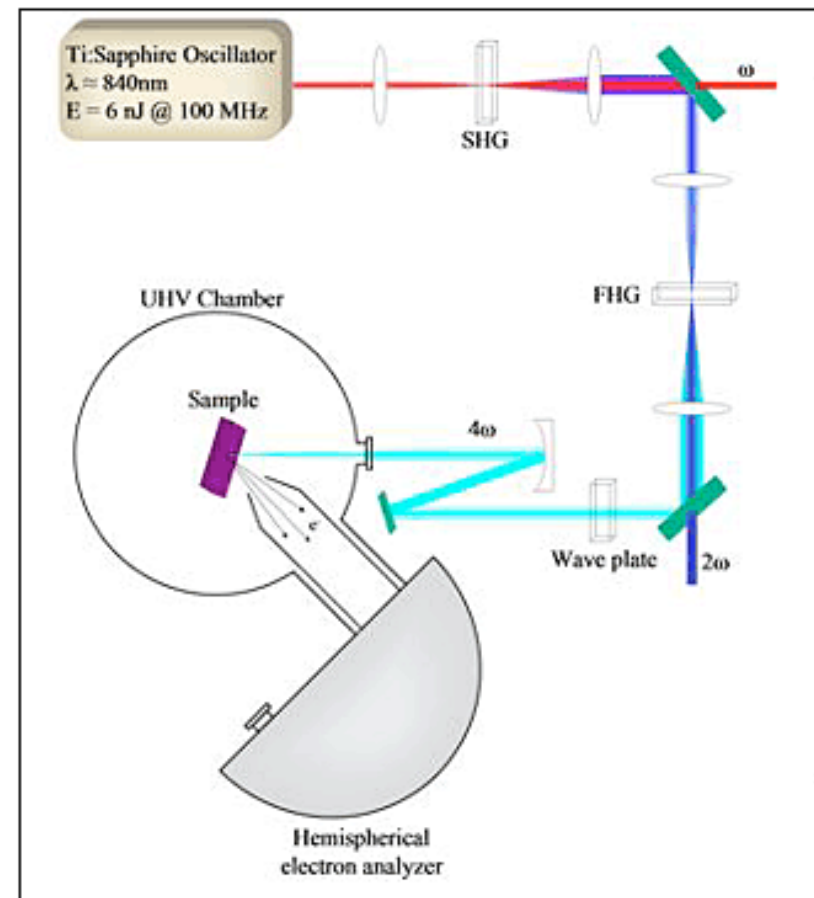
**Schematic of a system for performing photoemission spectroscopy based on a frequency quadrupled Ti:sapphire oscillator (6 eV) running at 100 MHz.**

### Note the high repetition rate:

Needed for a high signal to noise while keeping the instantaneous electron emission rate low.

**This last aspect is critical for keeping the electronic response of the sample in the linear regime and to minimize space-charge and other spurious effects.**

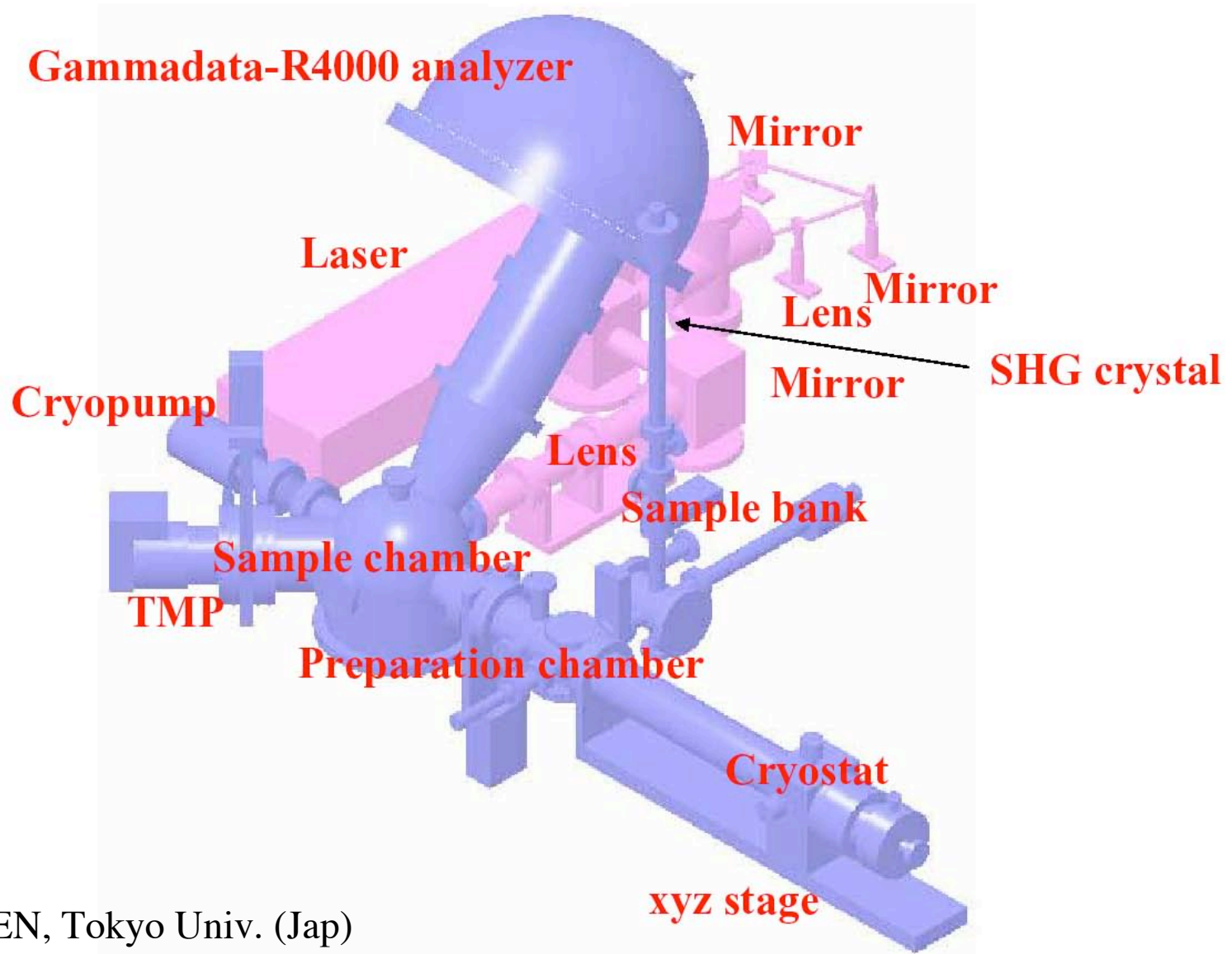
S. Shin, RIKEN, Tokyo Univ. (Jap)  
D.S. Dessau, Univ. Colorado (USA)



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# Laser excitation photoemission spectrometer

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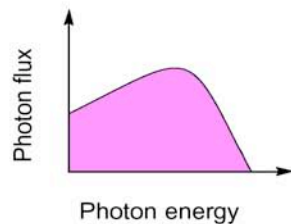
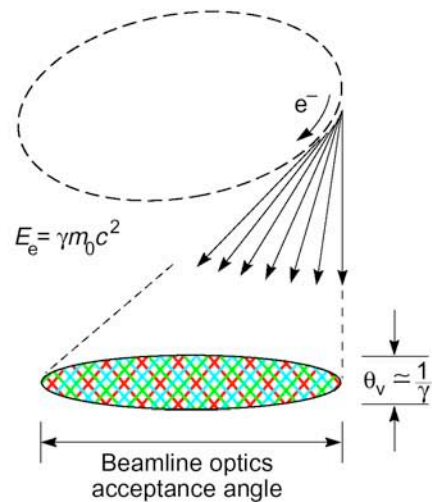


# How low photon energies can be obtained ?

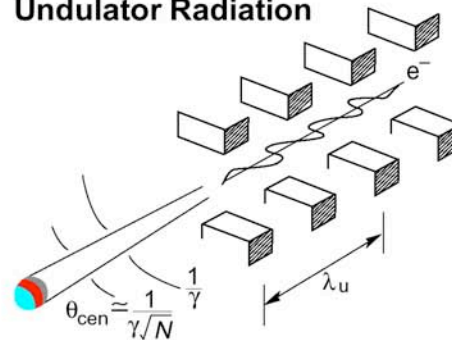
## 3) Synchrotron radiation

Spot size  $10\text{-}400\mu\text{m}$ ,  $> 10^{12}$  photons/s on the sample, intrinsic linewidth  $< 1\text{meV}$ , continuous energy range

Bend-Magnet Radiation



Undulator Radiation

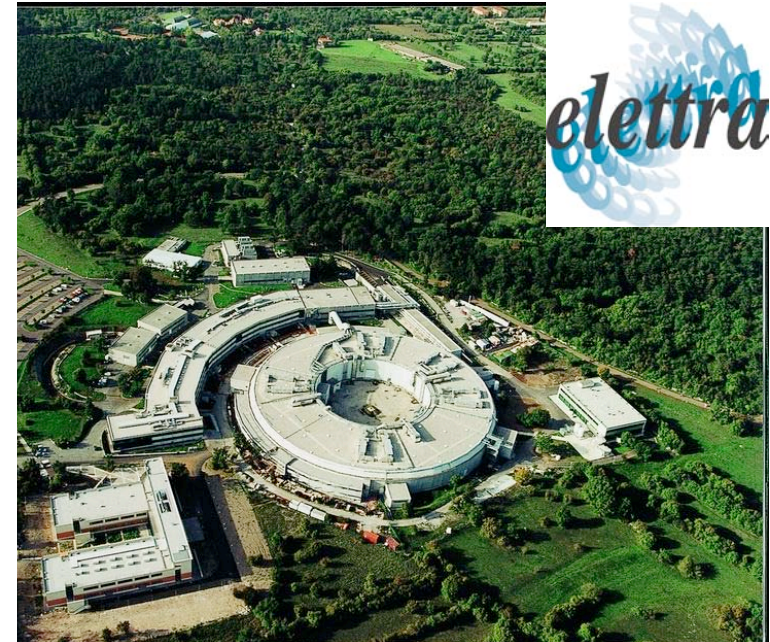
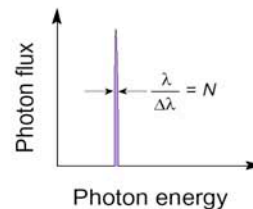


$$\lambda_x = \frac{\lambda_u}{2\gamma^2} \left( 1 + \frac{K^2}{2} + \gamma^2 \theta^2 \right)$$

In the central radiation cone:

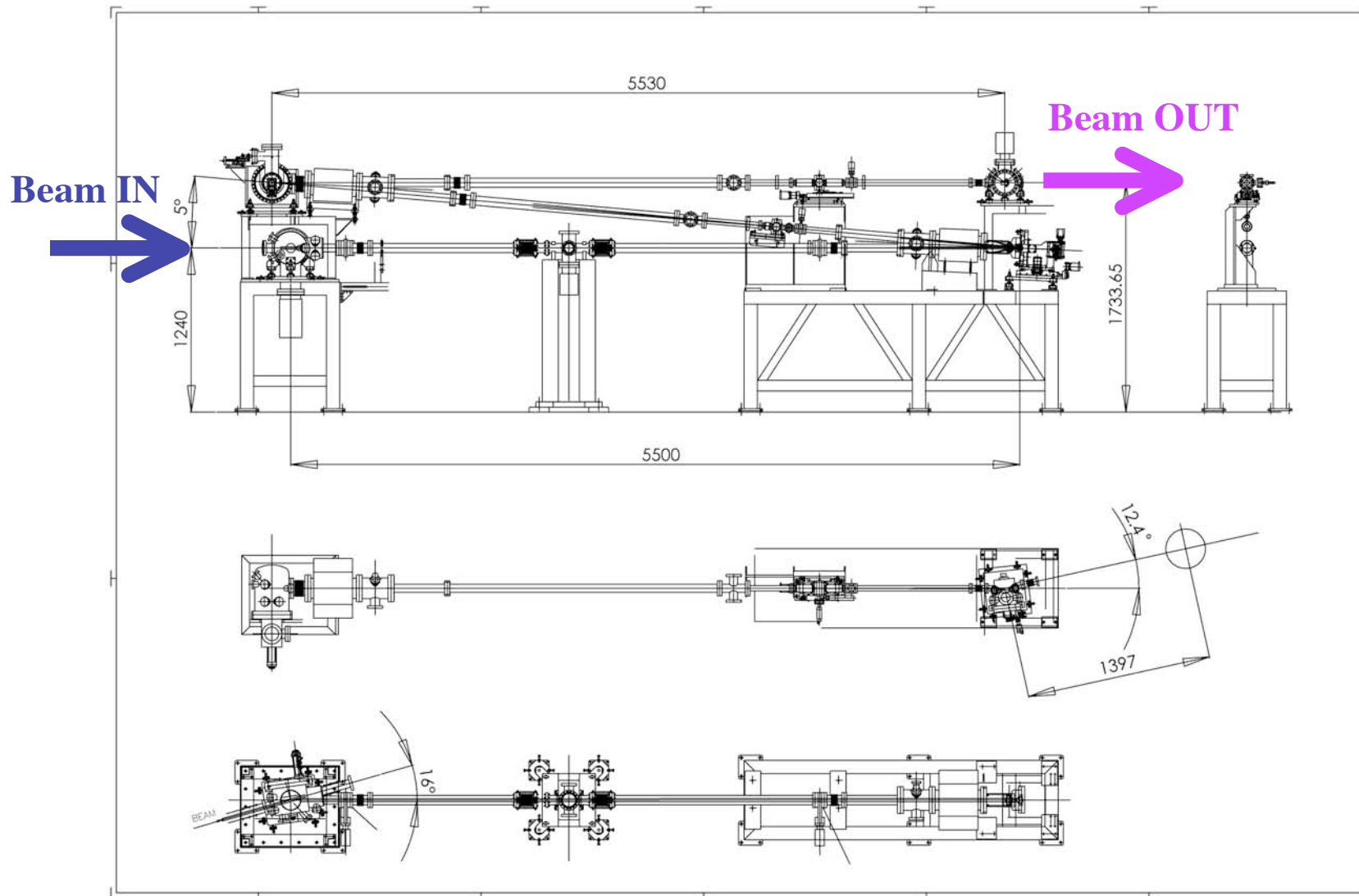
$$\frac{\Delta\omega}{\omega} \approx \frac{1}{N}$$

$$\theta_{cen} \approx \frac{1}{\gamma}$$



# BaD ElPh Layout

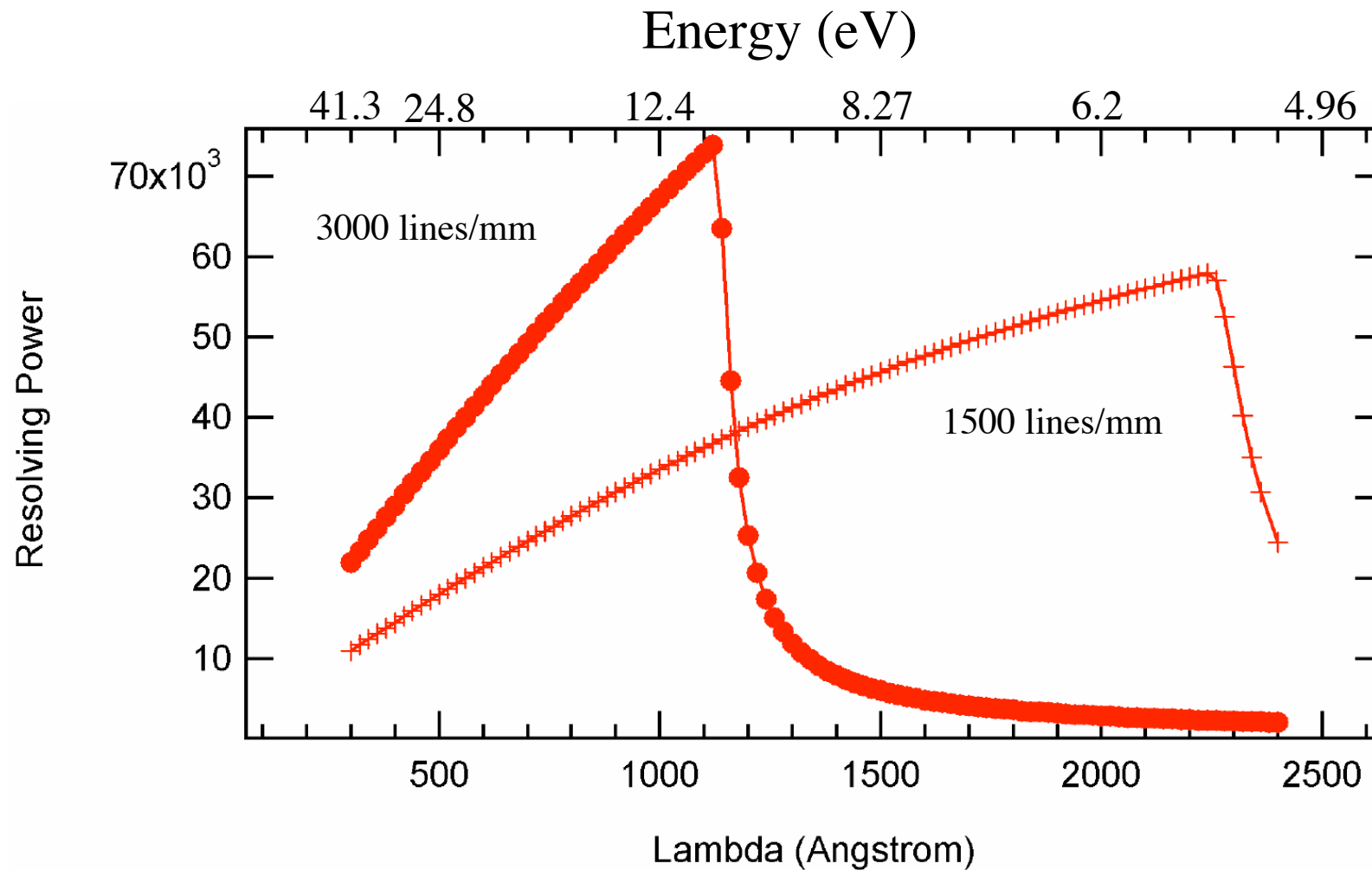
4m Normal Incidence Monochromator: 5°



Energy range: 5 - 23 eV with two gratings, a third grating foreseen for 23-35 eV



# The monochromator performances



**20 eV, resolving power 45000 ( $10 \mu\text{m}$ )**

**12 eV, resolving power 75000 ( $10 \mu\text{m}$ )**

**8 eV, resolving power 50000 ( $10 \mu\text{m}$ )**

## Expected performances:

**Cryostat/manipulator**

**T ~ 4 K**

**Total energy resolution**

**~ 3 meV**

**Momentum resolution**

**< 0.005 Å<sup>-1</sup>**

## Actual performances:

**Cryostat/manipulator**

**T ~ 11 K (on the sample)**

**Total energy resolution**

**~ 5.7 meV**

**Momentum resolution**

**< 0.005 Å<sup>-1</sup>**



GAMMADATA  
—SCIENTA—

### Features:

- < 3 meV energy resolution
- Angle multiplexing recording from small area samples
- Extremely low noise, high stability power supplies
- Customized lens design
- Multi-channel resistive anode detector

### Main application:

- High resolution electron spectroscopy
- High resolution photo-electron diffraction
- High resolution angular resolved spectroscopy

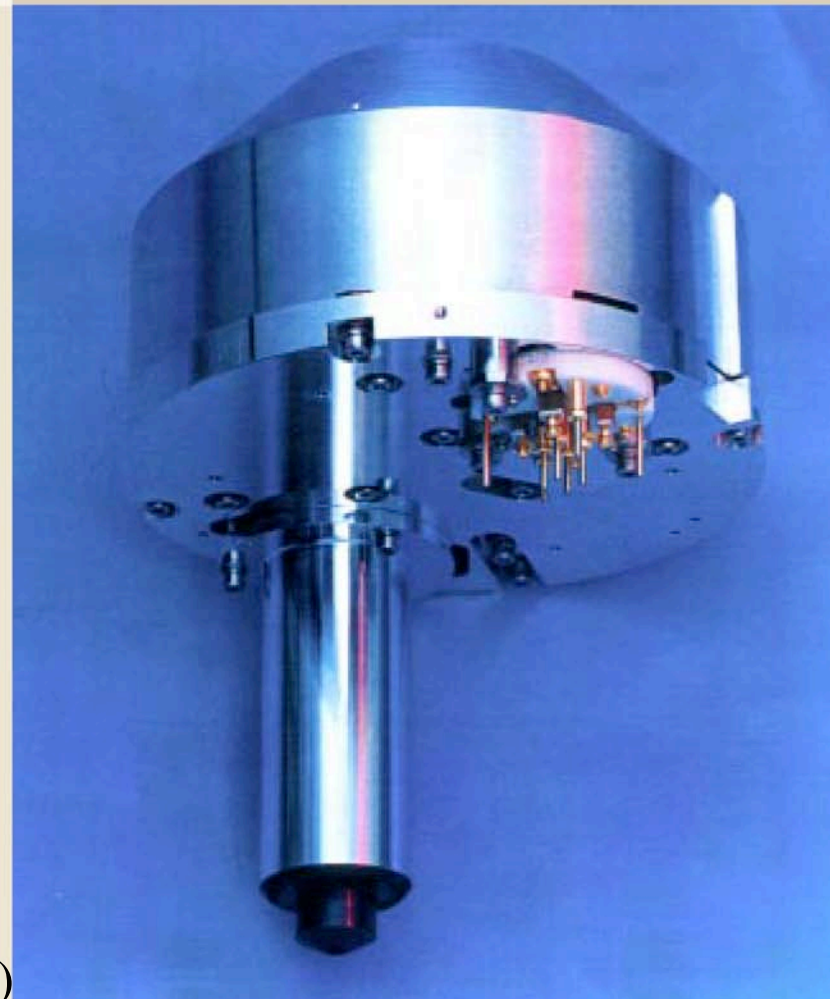
256x256 pixels

128 slices (spectra)

3 MHz count-rate

ELECTRON SPECTROMETER

SCIENTA SES 50

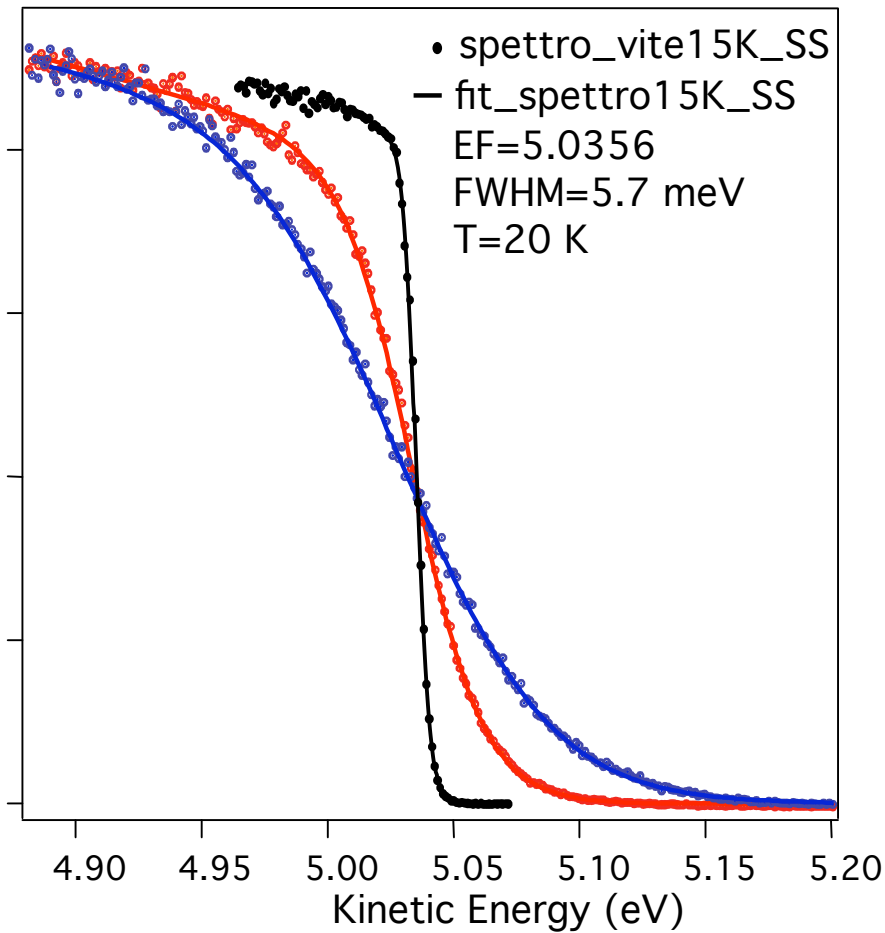


Mounted on a two-axis goniometer

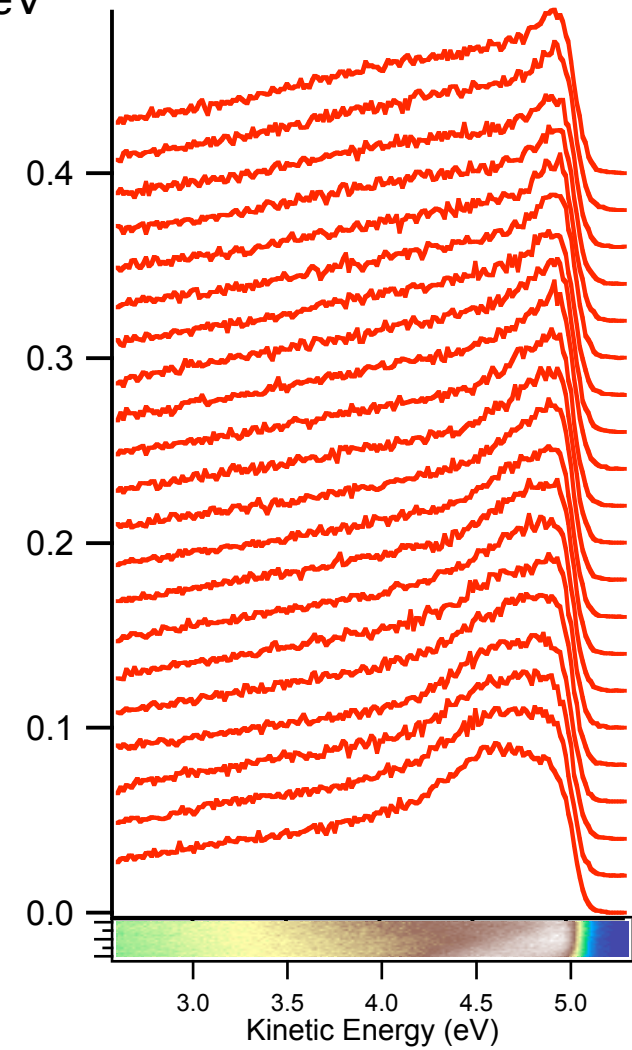
Courtesy of R. Claessen (Univ. of Wuerzburg)

$h\nu = 9 \text{ eV}$

$PE=2 \text{ eV}$



- somma\_vite 160K  
— fit\_somma\_vite 160K  
EF=5.03563; FWHM:5.8meV; T=164 K
- somma\_vite 300K  
— fit\_somma\_vite 300K  
EF=5.0356; FWHM:5.8meV; T=300 K



$\theta \text{ range} = 5^\circ$   
21 slices;  $\Delta\theta \sim 0.25^\circ$   
 $\Delta K < 0.005 \text{ \AA}^{-1}$

Why going to very low photon energies?

$$4 \text{ eV} < h\nu < 20 \text{ eV}$$

- 1) Bulk sensitivity
- 2) Higher momentum resolution
- 3) Good energy resolution easier

Why going to very low photon energies?

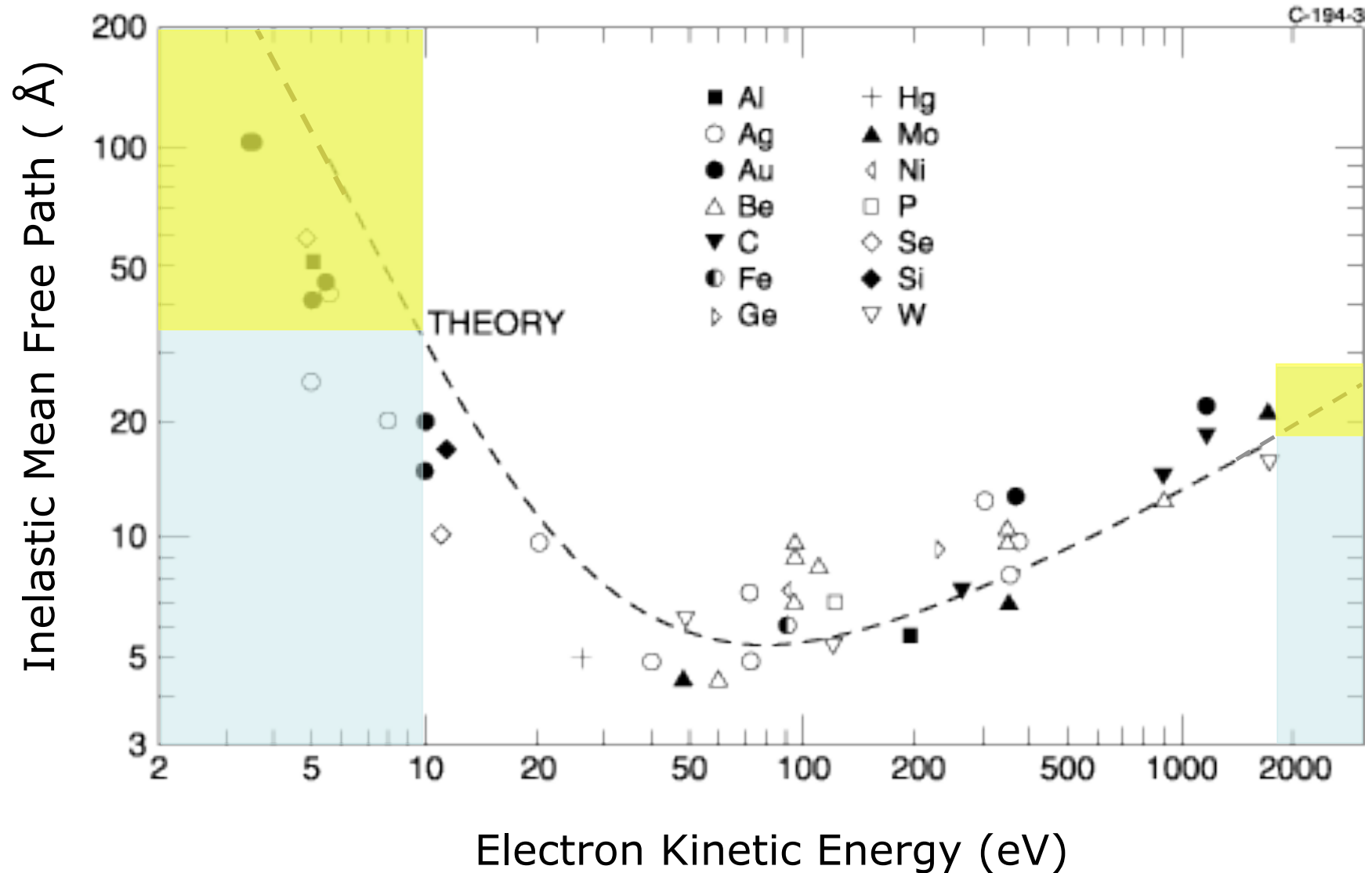
$$4 \text{ eV} < h\nu < 20 \text{ eV}$$

**1) Bulk sensitivity**

2) Higher momentum resolution

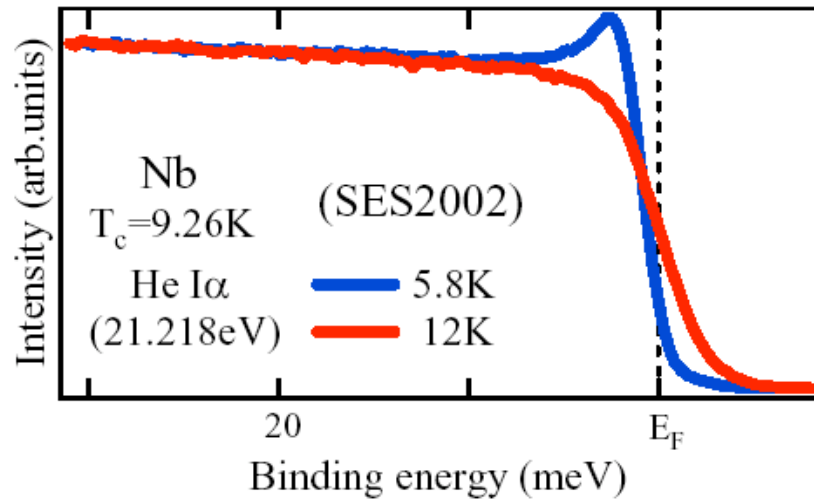
3) Good energy resolution easier

# Electrons photoemitted with low photon energies are the most bulk sensitive

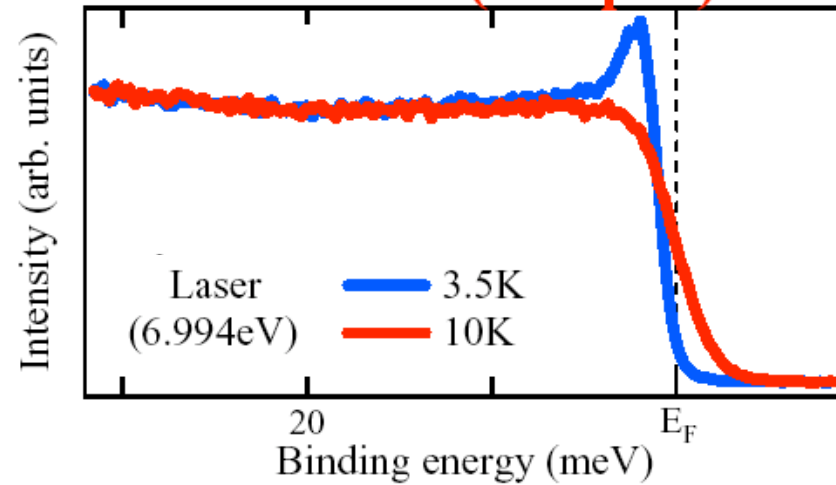


# Superconducting gap of Nb

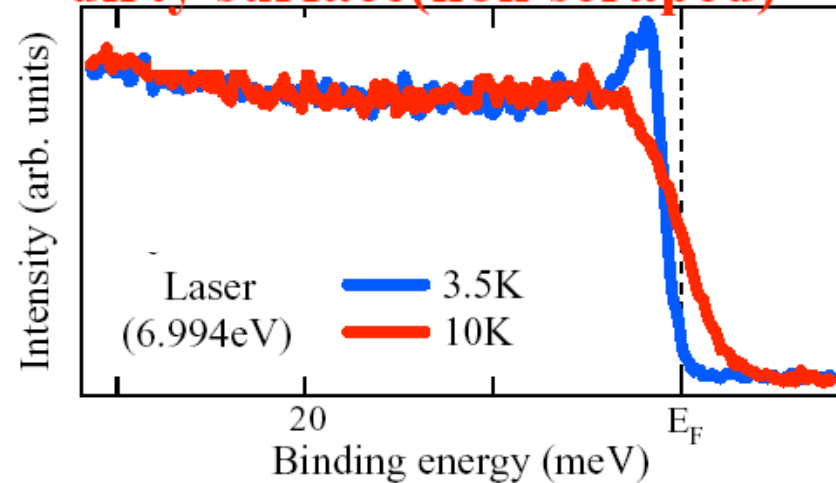
Chainani et.al., PRL, 85(2000)1966



**clean surface(scraped)**



**dirty surface(non scraped)**



We can measure  
superconducting gap  
without clean surface

# Fermi surface of Bi(111): Bulk vs Surface states

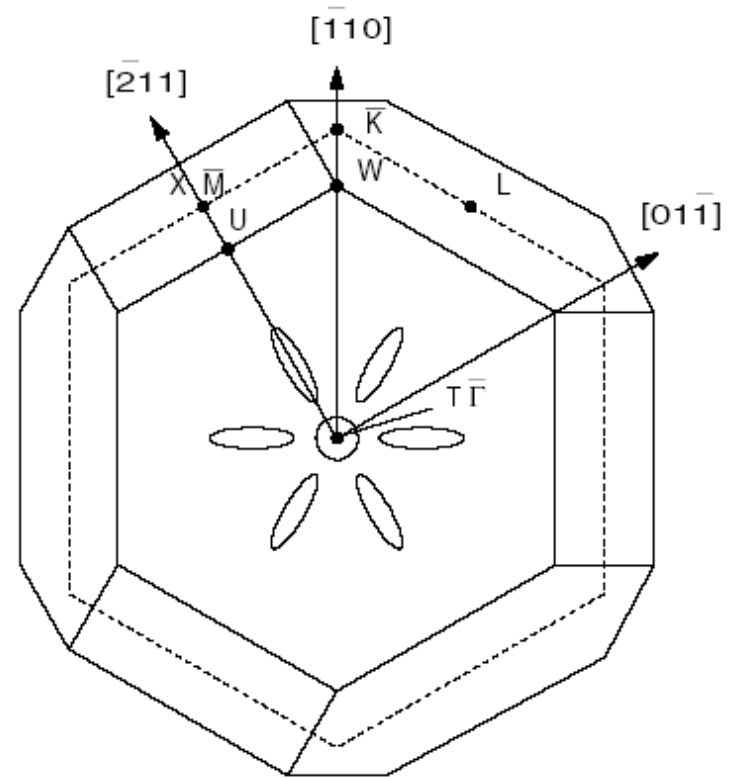
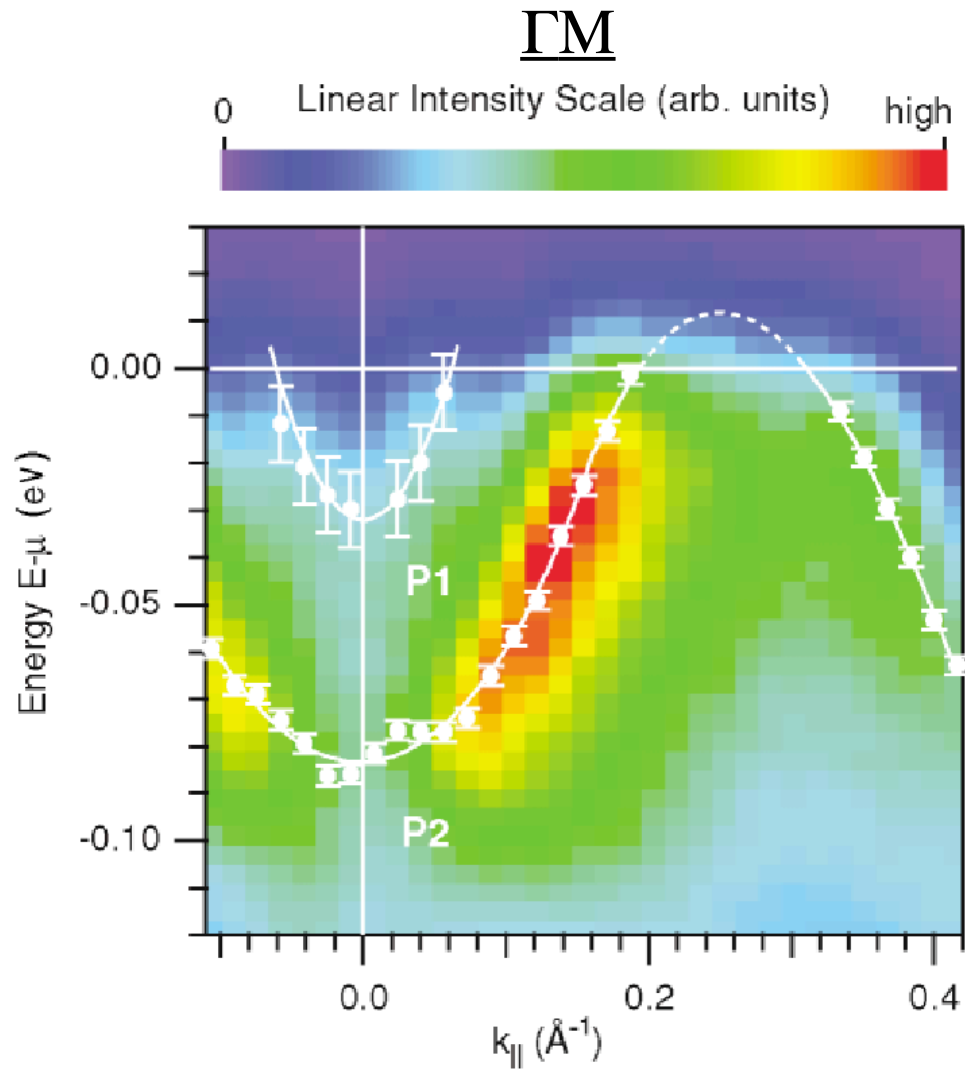


FIG. 4 (color). Band structure of Bi(111) at  $h\nu = 18$  eV.  $k_{\parallel}$  along  $\Gamma\bar{M}$ . Solid lines: Polynomial fit to peak positions. Energies relative to chemical potential  $\mu$ .



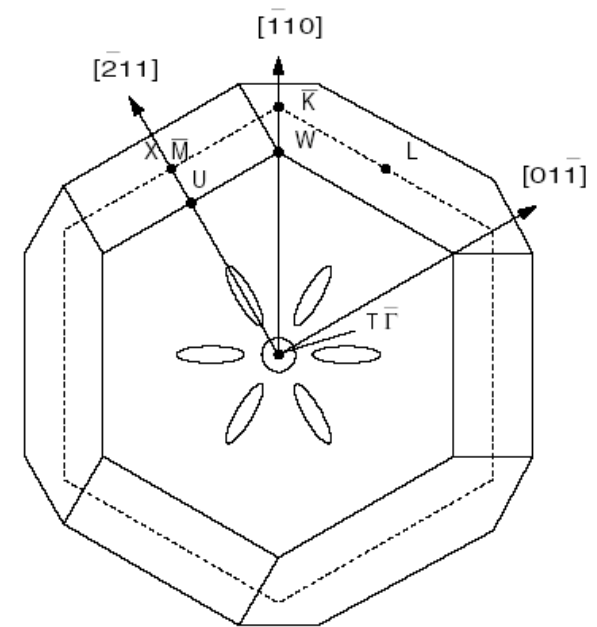
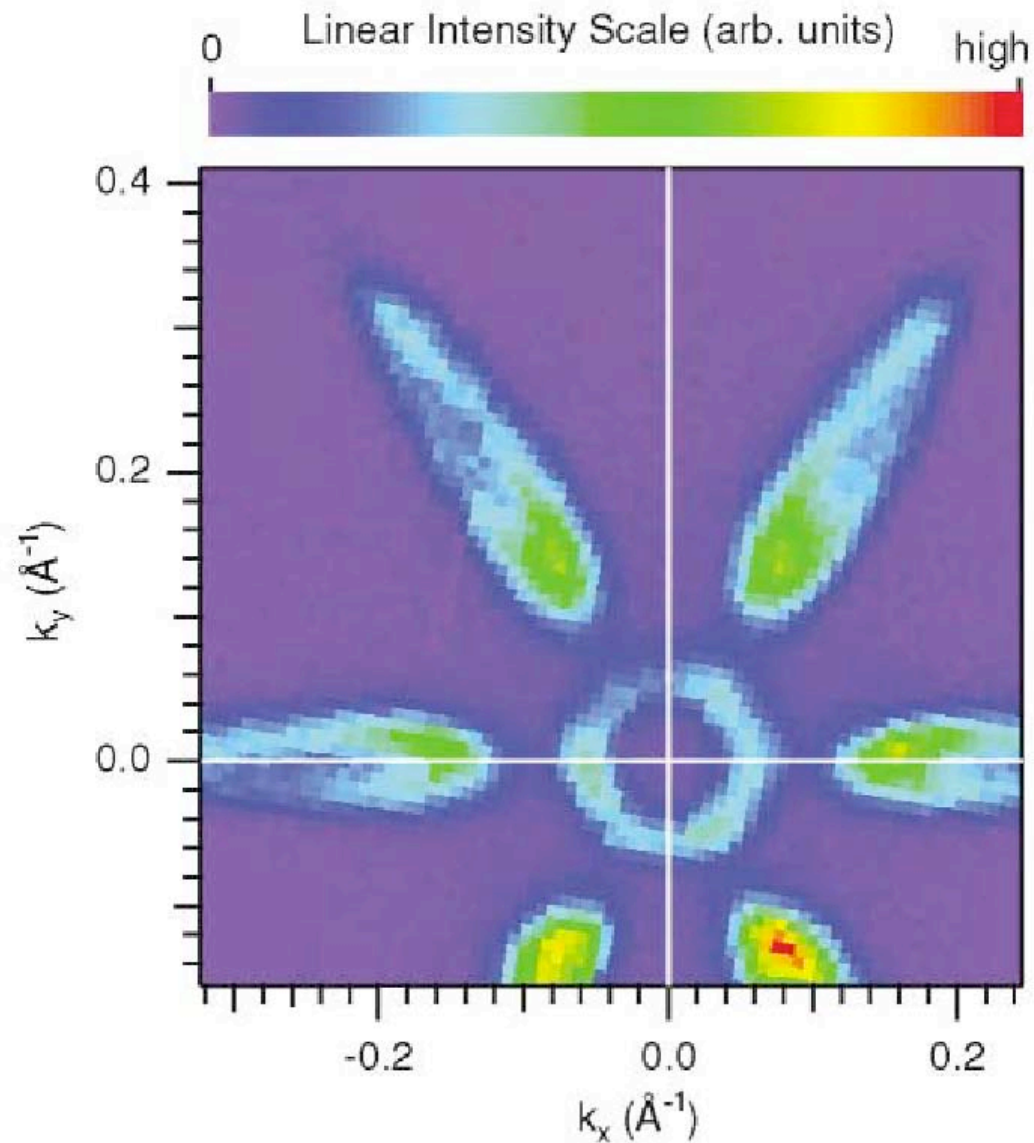
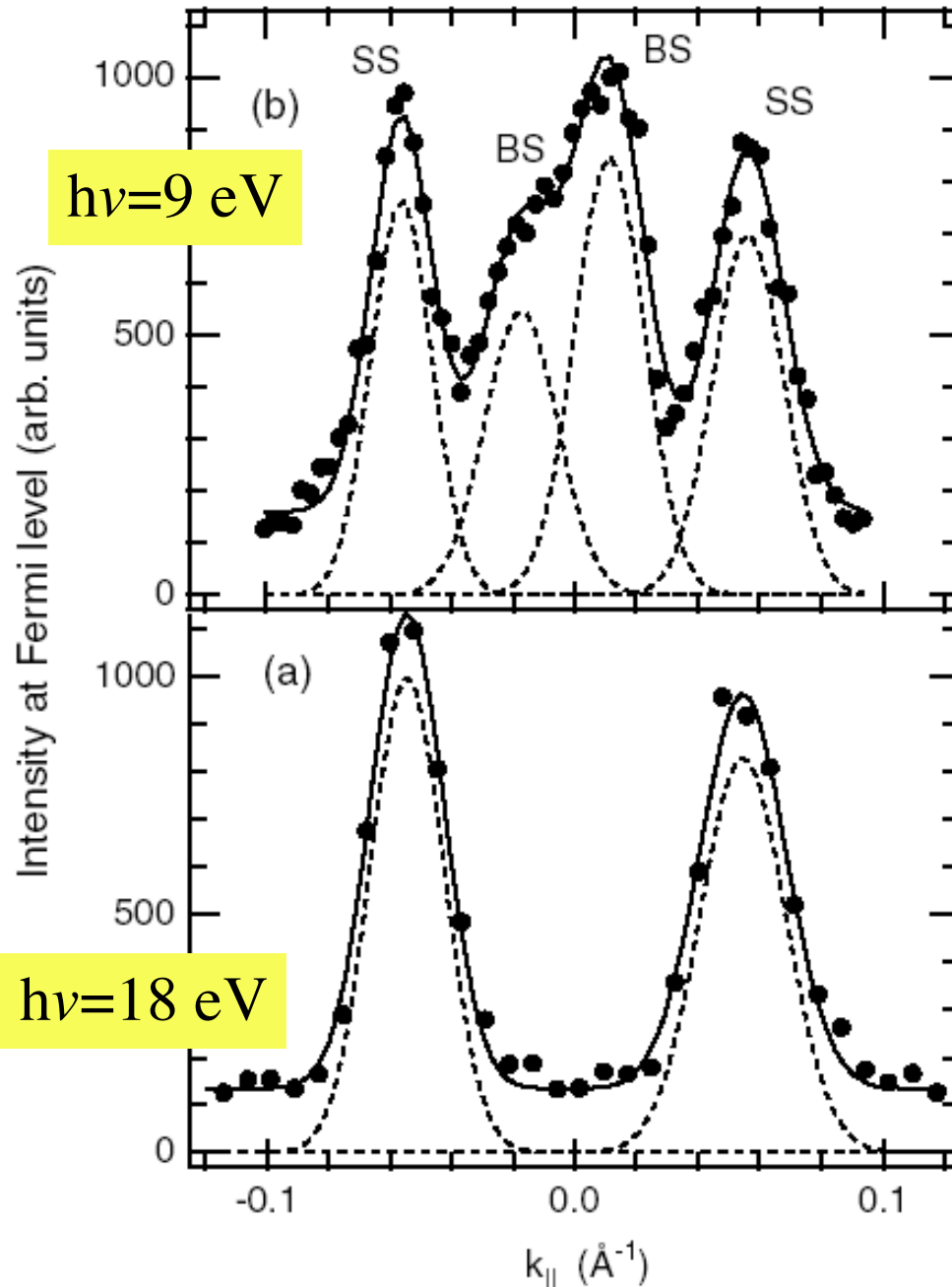


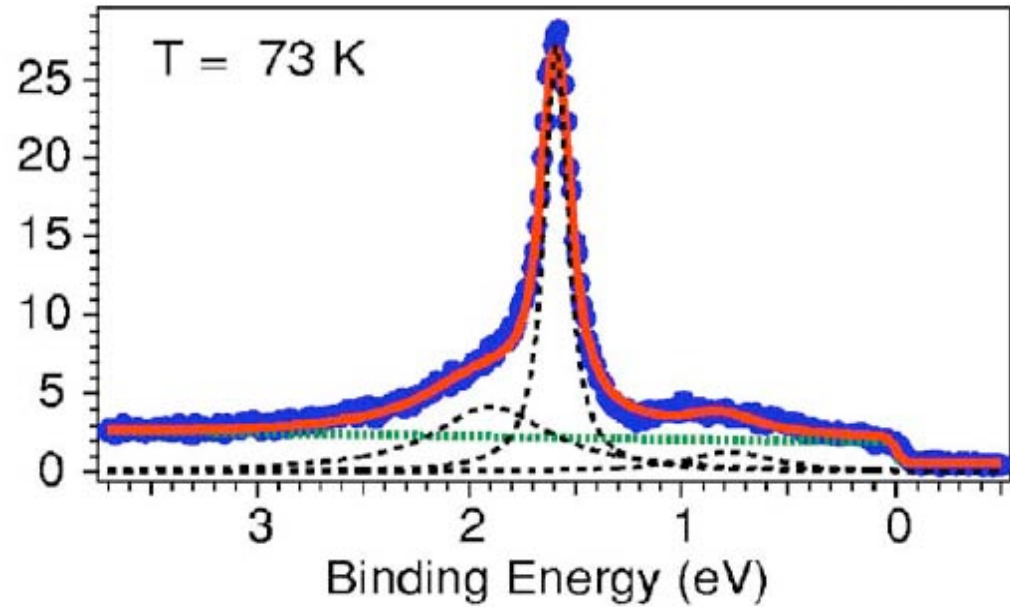
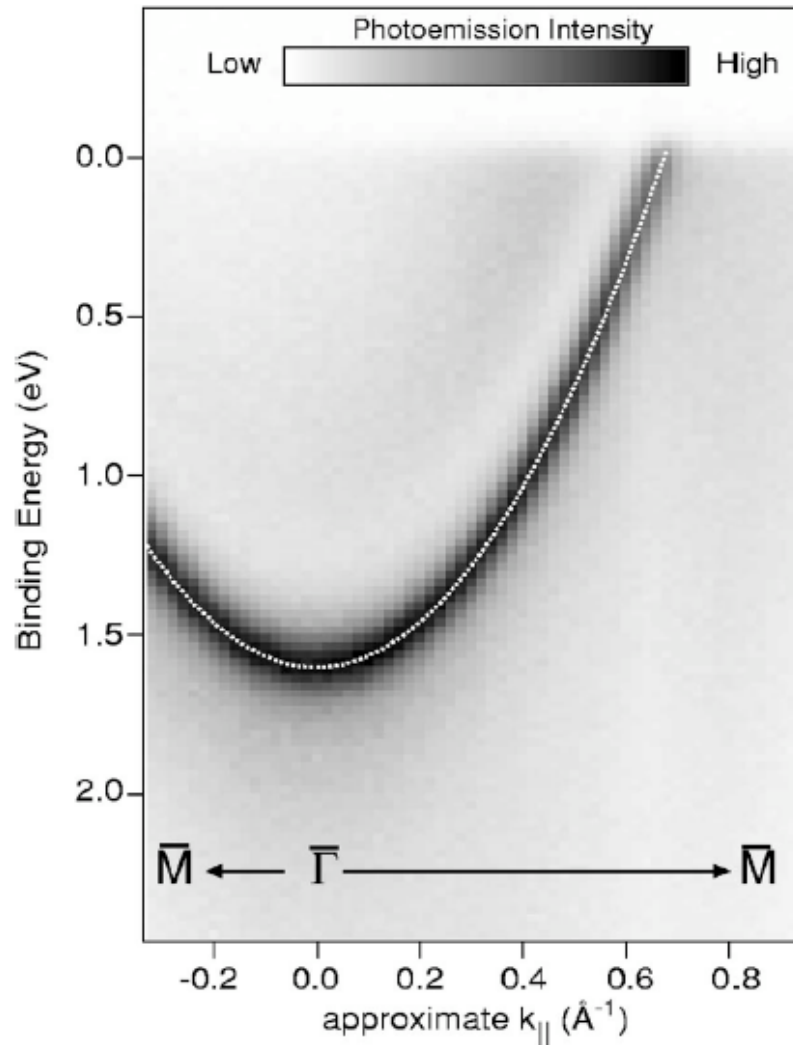
FIG. 1 (color). Intensity map at the Fermi level of Bi(111) measured at  $h\nu = 18$  eV. The angular steps were  $0.25^\circ$ .  $k_x$  and  $k_y$  are the parallel components of the electron momentum along the  $\overline{\Gamma M}$  and the  $\overline{\Gamma K}$  direction, respectively.



Momentum  
Distribution  
Curves at  $E_F$  for  
Bi(111) along the  $\Gamma K$

**Note:**  
bulk states (BS) appear  
at low photon energies

# Photoemission from Mg(0001): surface vs bulk states

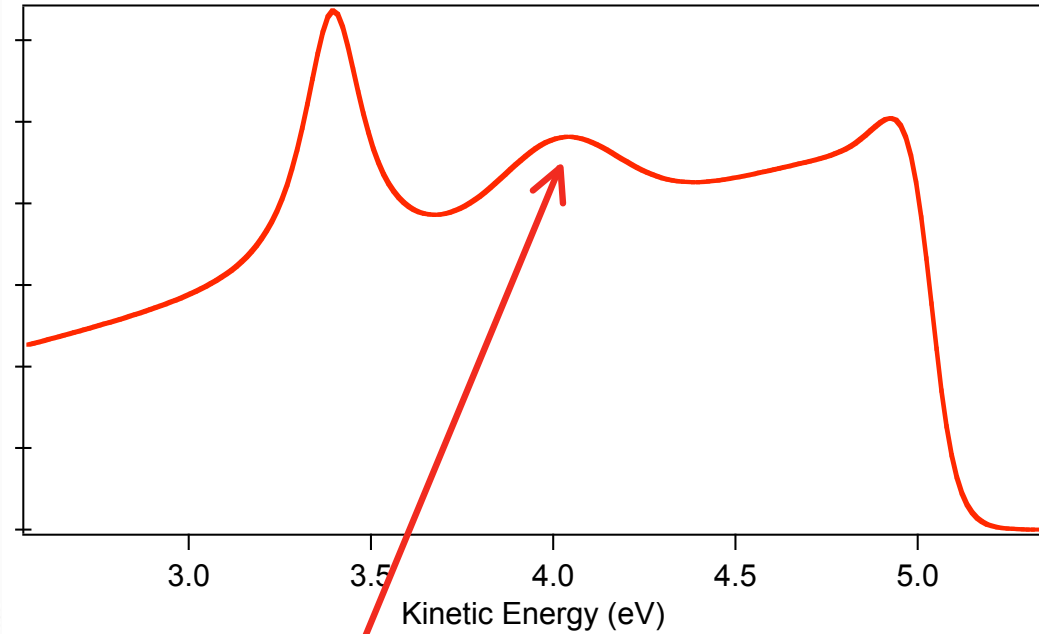
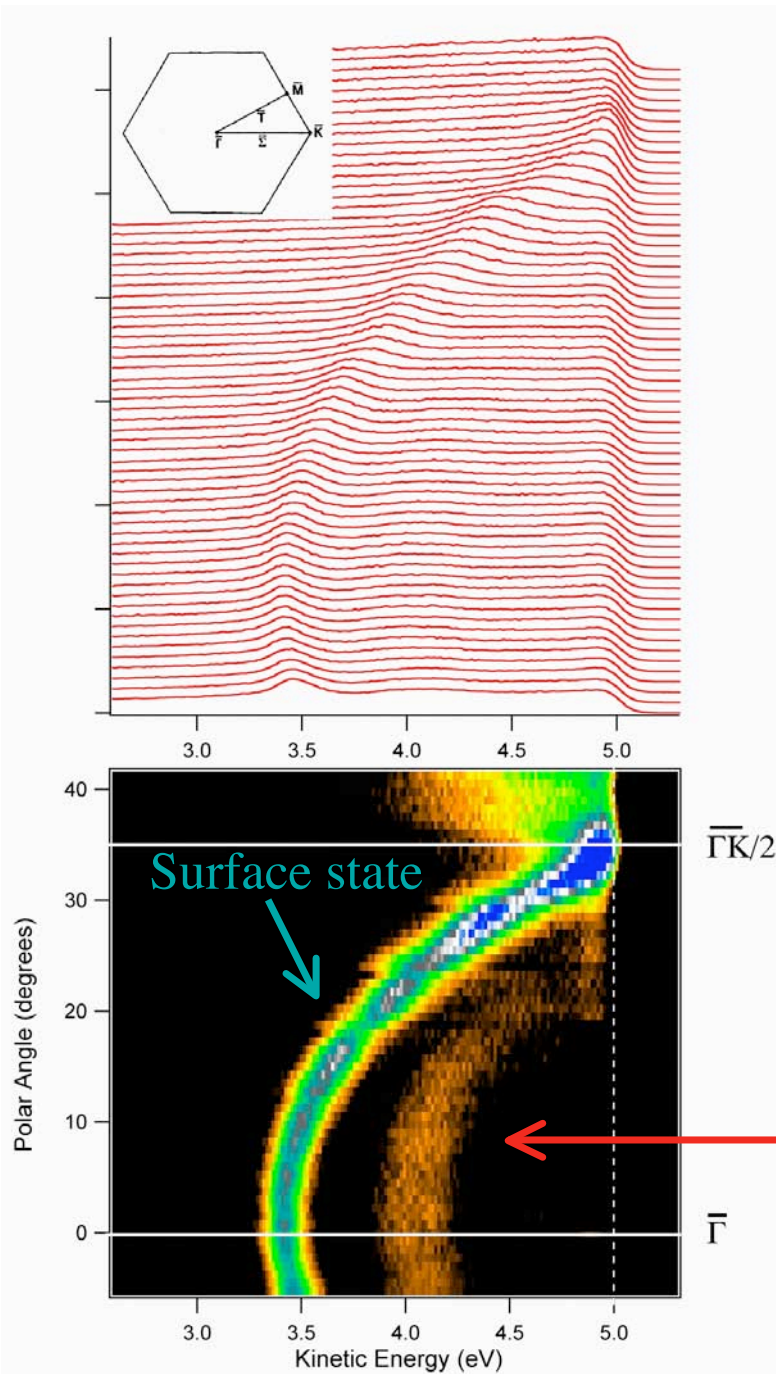


Measured at  $h\nu=44 \text{ eV}$

Bulk states intensity very very small

# Mg(0001) measured at $h\nu = 9$ eV

Enhanced bulk sensitivity at low photon energy



**Bulk band  
(now well visible)**

# Mott transition in $V_2O_3$

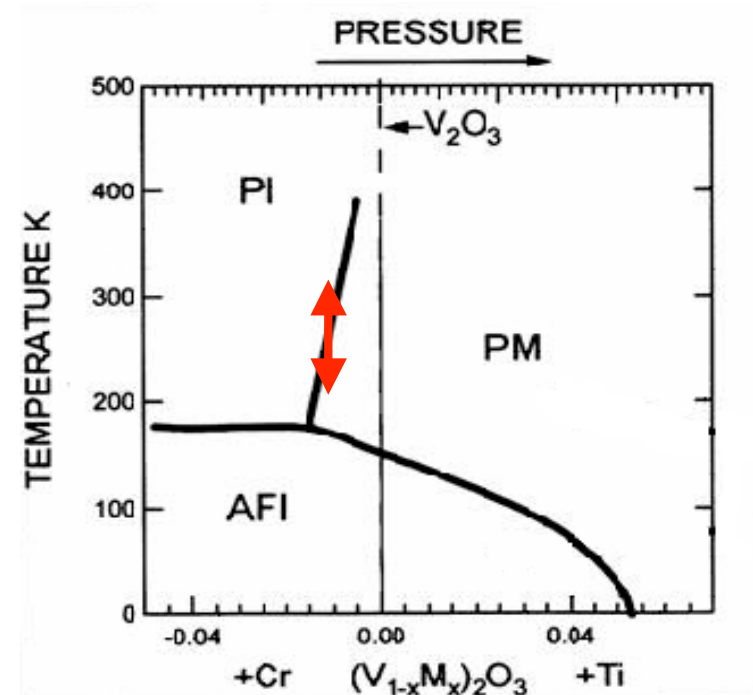
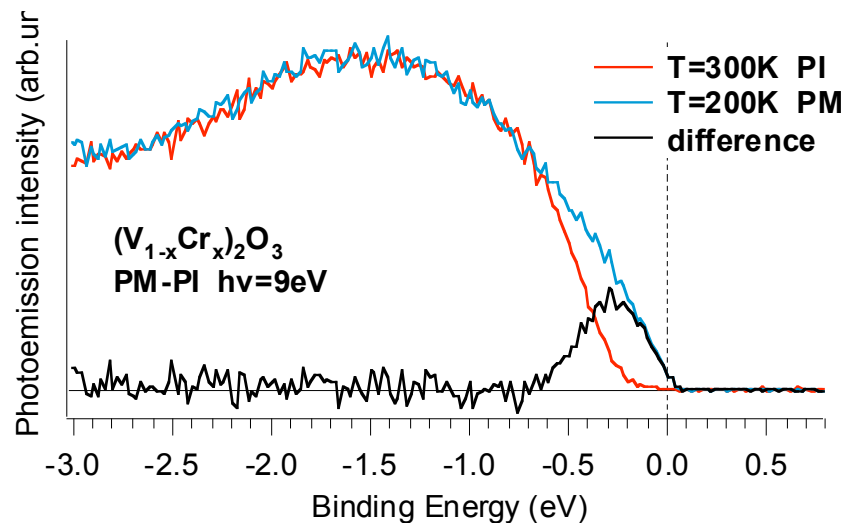
M. Marsi et al., submitted to PRB  
(similar experiment made by R. Claessen et al.)

$(V_{1-x}Cr_x)_2O_3$  prototype system for isostructural  
metal-insulator transition induced by electron correlations

$(V_{1-x}Cr_x)_2O_3$   $x = 0,011$

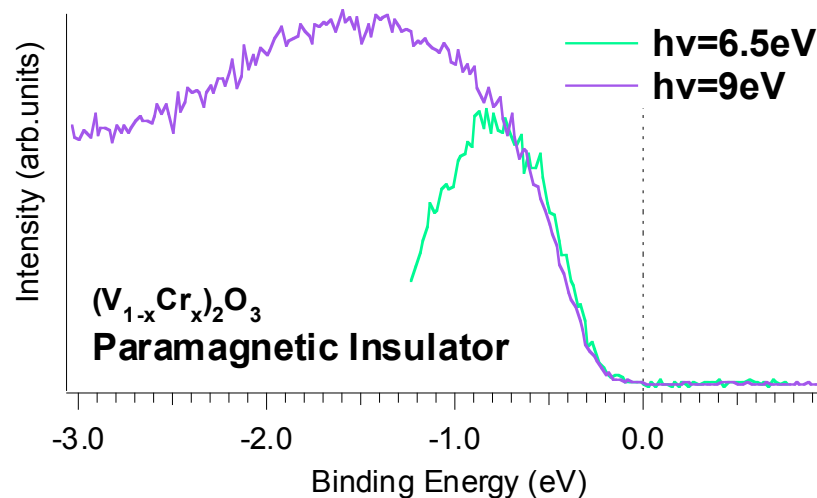
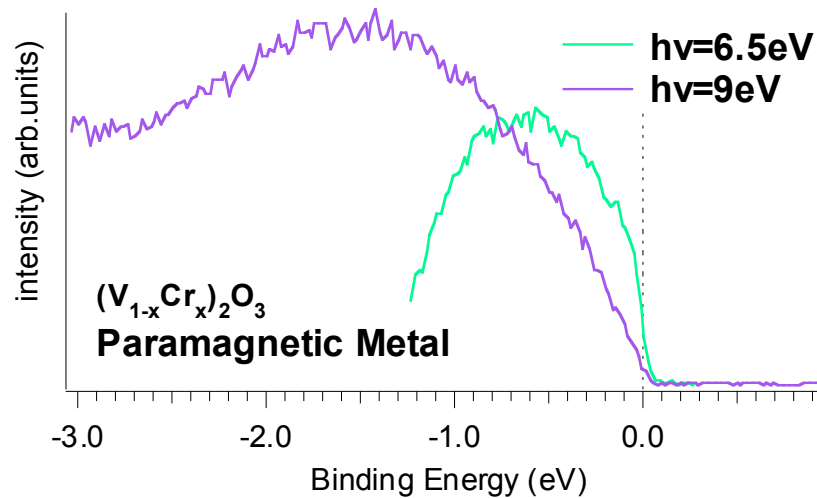
T=300K paramagnetic insulator

T=200K paramagnetic metal



# Mott transition in $V_2O_3$

M. Marsi et al., submitted to PRB



Photoemission on BaD EIPh

Low photon energy

Normal emission

**metallic phase shows larger  
difference between  
surface and bulk**

→ Surface is more  
correlated than bulk

→ True also for other  
strongly correlated systems ?

# Coronene (C<sub>24</sub>H<sub>12</sub>) on Au(110), intercalated with Rb



Petra Rudolf et al.

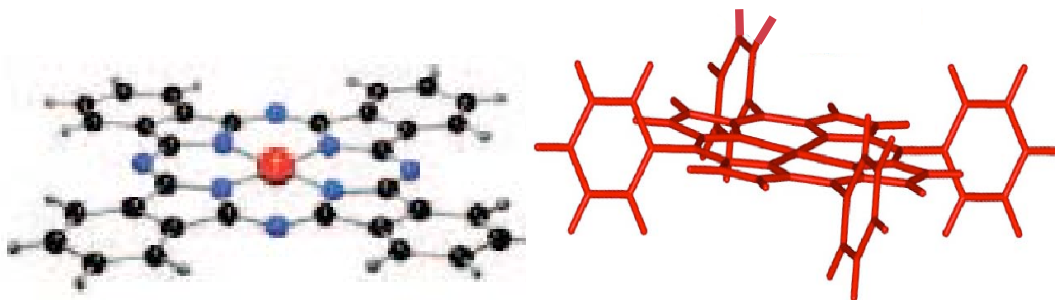
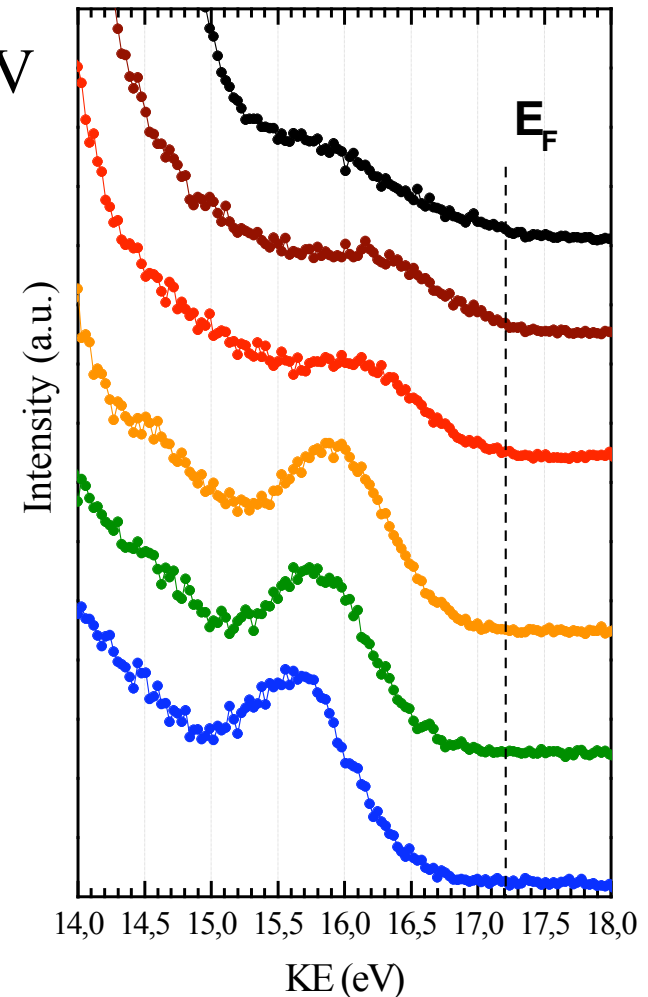


University of Groningen  
Zernike Institute  
for Advanced Materials

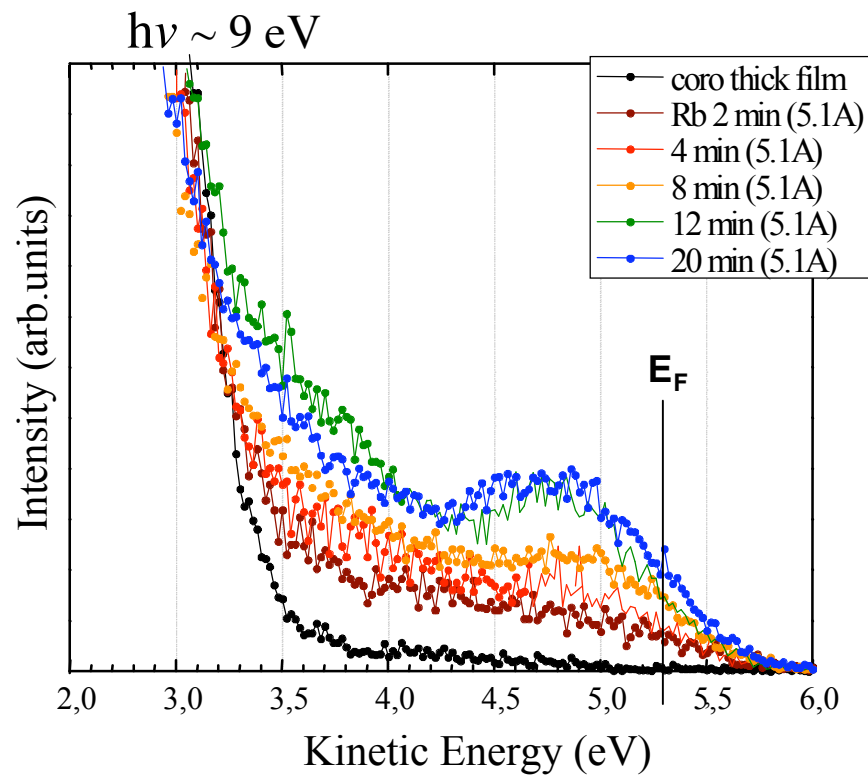
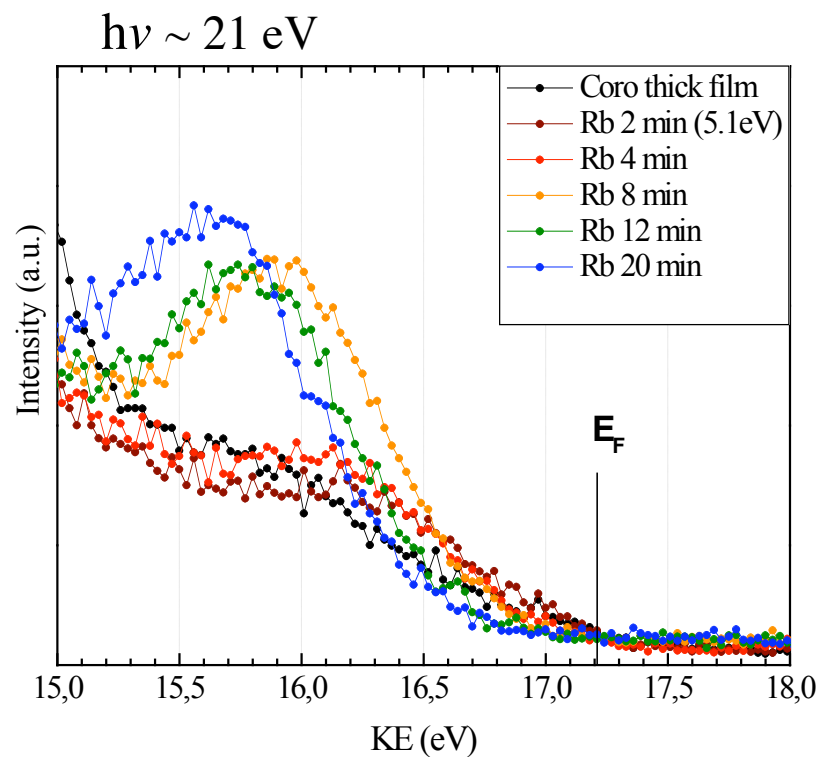
$h\nu = 21 \text{ eV}$

As the LUMO fills no states near  $E_F$ :  
always insulating

Plenty of similar photoemission  
examples in the literature:  
phthalocynins, porphyrins, ...



# *Rb-Coronene: Fermi region with $h\nu < 10$ eV*



At  $h\nu = 9$  eV the evolution is completely different:  
density of states crossing Fermi

The LUMO states are closer to Fermi and crosses  $E_F$

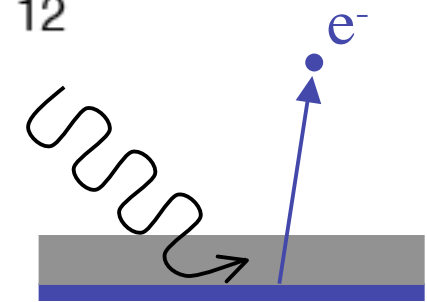
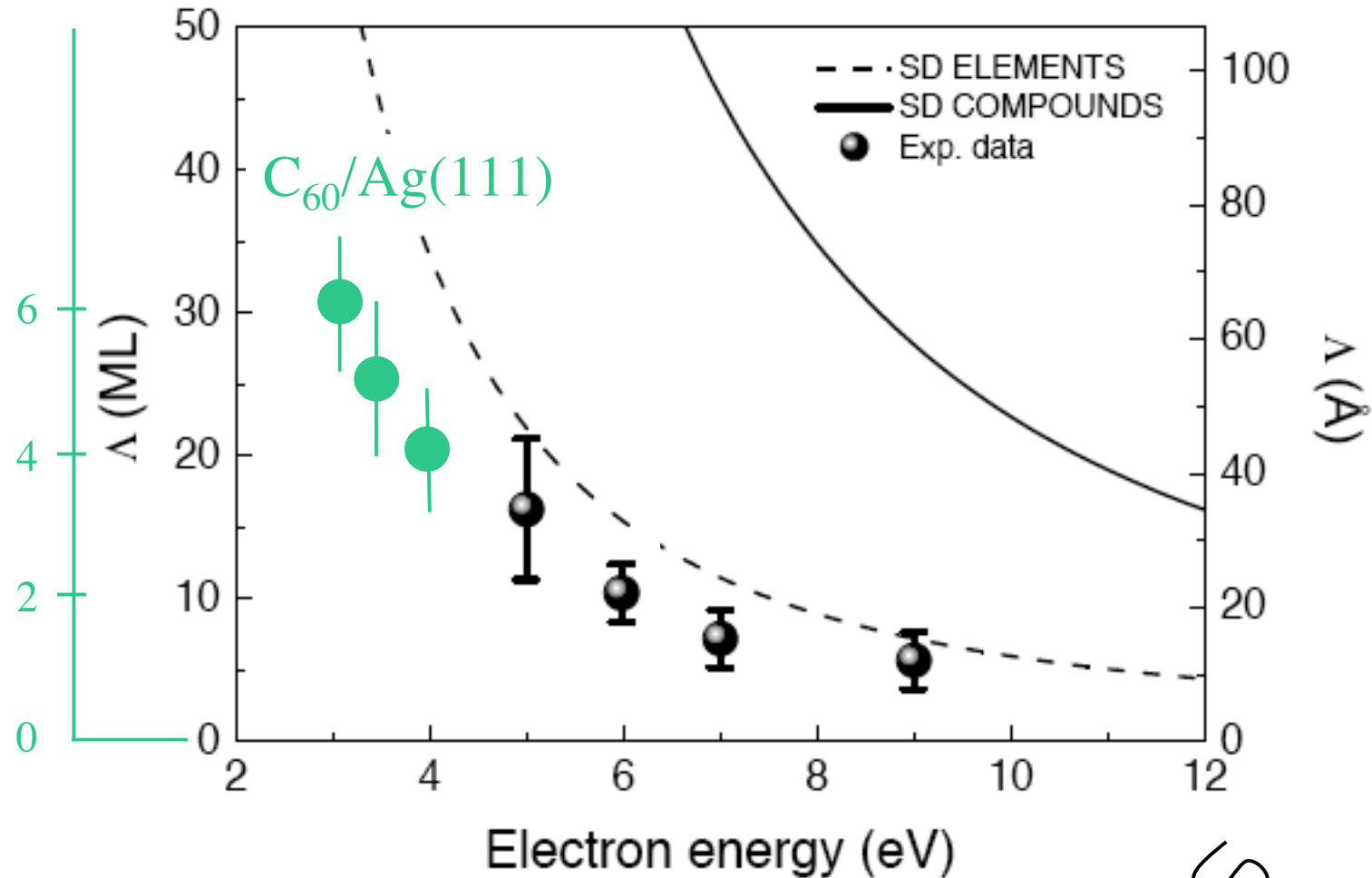
Petra Rudolf et al.



University of Groningen  
Zernike Institute  
for Advanced Materials



# Attenuation length of low electron in solids: CoO/Ag and C<sub>60</sub>/Ag

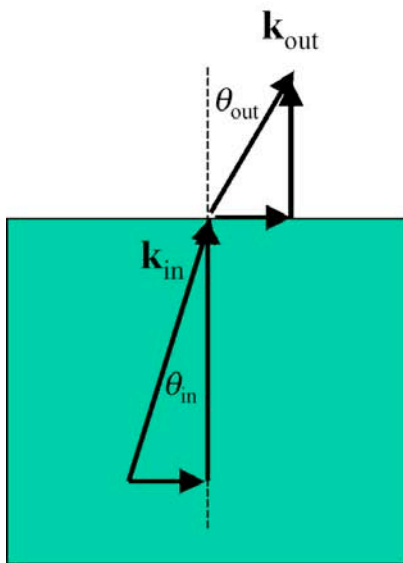


# Why going to very low photon energies?

$$4 \text{ eV} < h\nu < 20 \text{ eV}$$

1) Bulk sensitivity

2) Higher momentum resolution



*Kinematic relations*

$$k_{out} = \sqrt{\frac{2m}{\hbar^2} E_{kin}}$$

$$k_{in} = \sqrt{\frac{2m}{\hbar^2} (E_{kin} + V_0)}$$

$$k_{out,\parallel} = k_{in,\parallel} \equiv k_{\parallel}$$

*“Snell’s Law”*

$$k_{\parallel} = \sin\theta_{out} \sqrt{\frac{2m}{\hbar^2} E_{kin}} = \sin\theta_{in} \sqrt{\frac{2m}{\hbar^2} (E_{kin} + V_0)}$$

*Critical angle for emission*

$$(\sin\theta_{out})_{\max} = \sqrt{\frac{E_{kin}}{E_{kin} + V_0}}$$

At the surface the crystal symmetry is conserved in the surface plane but is broken perpendicularly to the surface: the component of the electron momentum parallel to the surface plane ( $k_{\parallel}$ ) is conserved, but  $k_{\perp}$  is not

$$k_{//} = \sqrt{\frac{2m^* E_k}{\hbar^2}} \sin \theta_{\text{out}} \approx 0.512 \sqrt{E_k} \sin \theta_{\text{out}}$$

The angular resolution is defined by the electron energy analyzer. Suppose it is  $0.5^\circ$  and the BZ boundary is  $\sim 0.25 \text{ \AA}^{-1}$ .

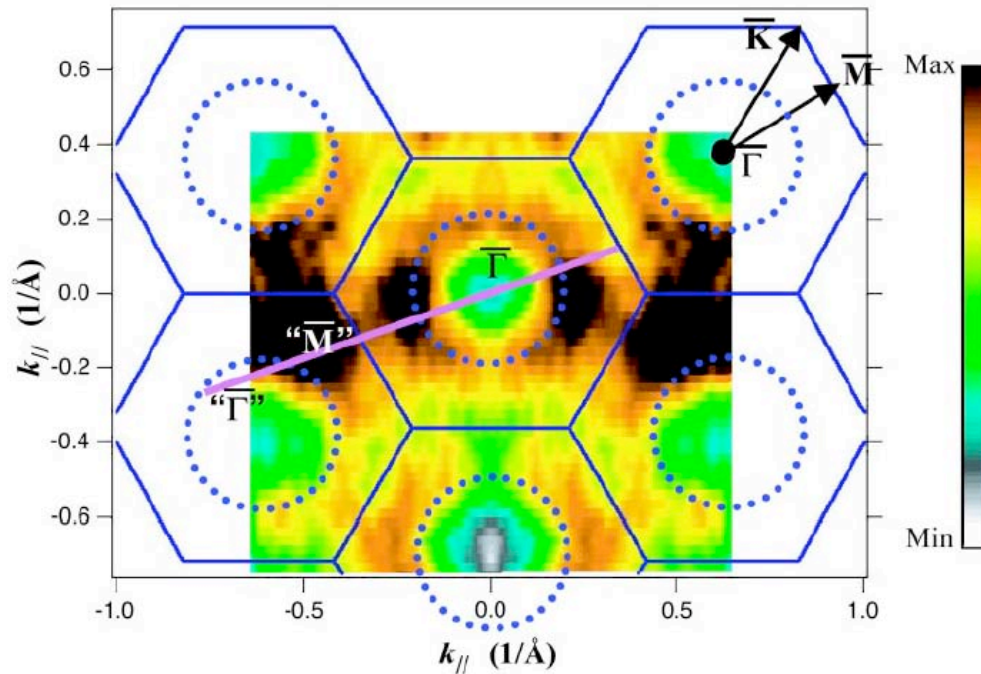
At  $E_k=25 \text{ eV}$  the BZ boundary is reached after  $\sim 5.5^\circ$   
We have 11 sampling points  $\rightarrow \Delta k_{//} \sim 0.025 \text{ \AA}^{-1}$

At  $E_k=9 \text{ eV}$  the BZ boundary is reached after  $\sim 9.5^\circ$   
We have 19 sampling points  $\rightarrow \Delta k_{//} \sim 0.014 \text{ \AA}^{-1}$

**GOOD for systems with small BZ**

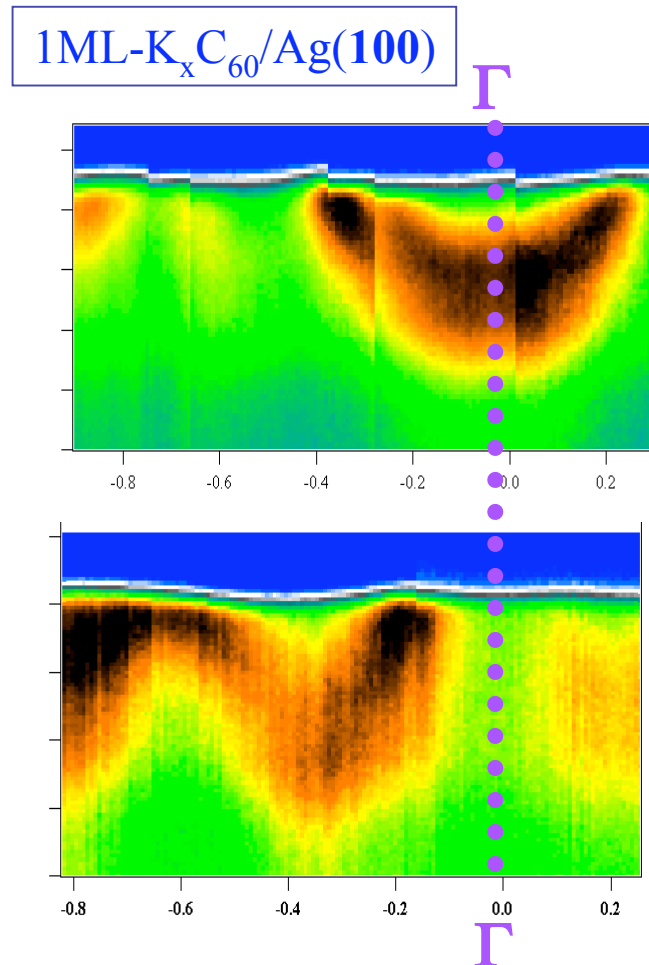
# Example: Band structure in fullerides

Typical hexagonal surface lattice parameter  $> 10 \text{ \AA}$



Measured at 22 eV. Lower photon energy should allow better Fermi surface mapping.

W. Yang et al., Science **300**, 303 (2003);  
V. Brouet et al., PRL (2004)



1ML- $K_3C_{60}/Ag(111)$

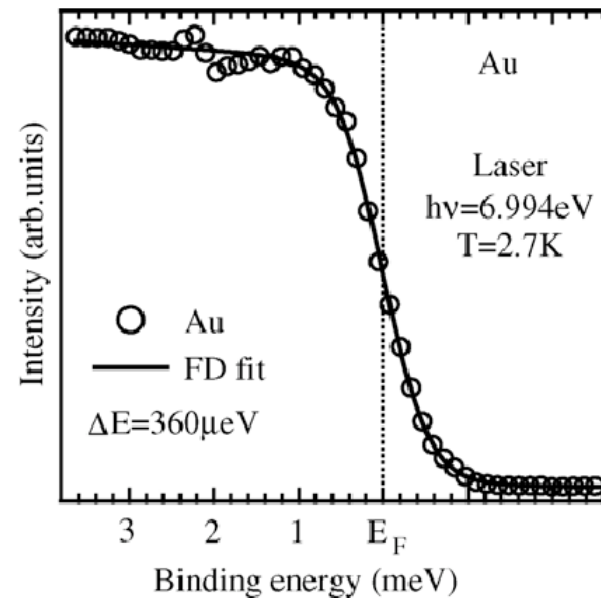
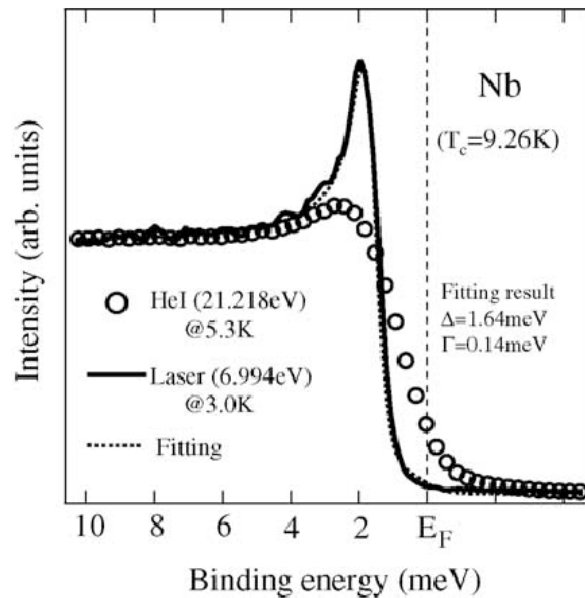
# Why going to very low photon energies?

$$4 \text{ eV} < h\nu < 20 \text{ eV}$$

1) Bulk sensitivity

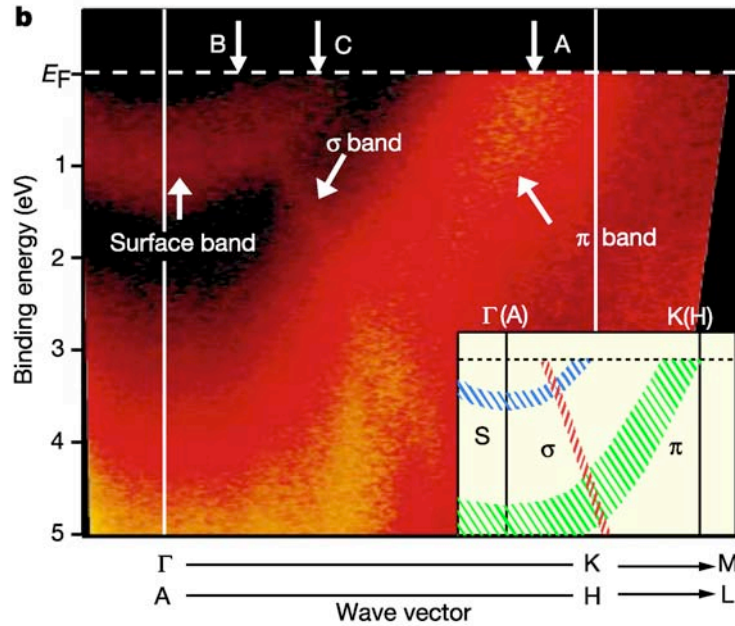
2) Higher momentum resolution

**3) Good energy resolution easier**

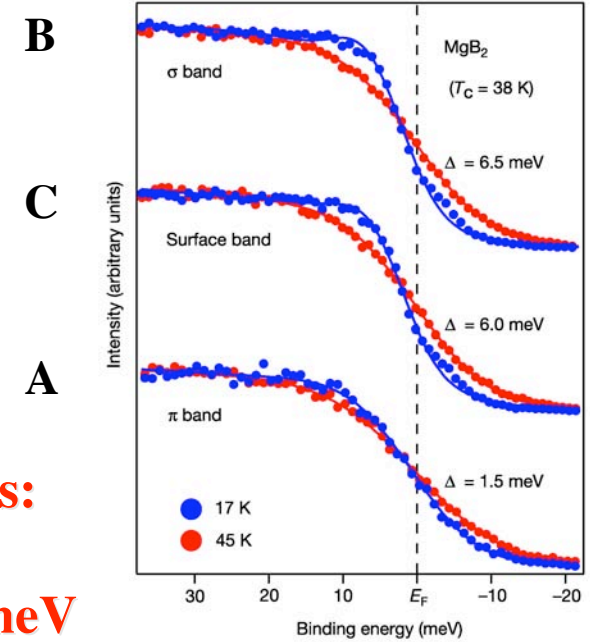


# Angle Resolved Photoemission Spectroscopy of MgB<sub>2</sub> Single Crystals

S. Souma et al. Nature **423**, 65 (2003)

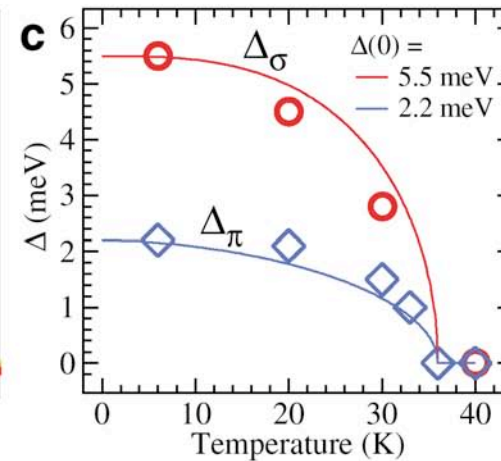
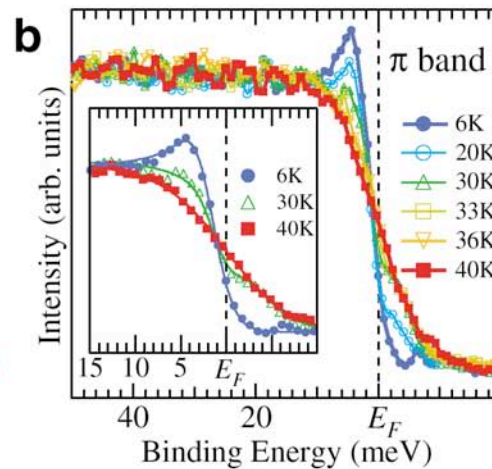
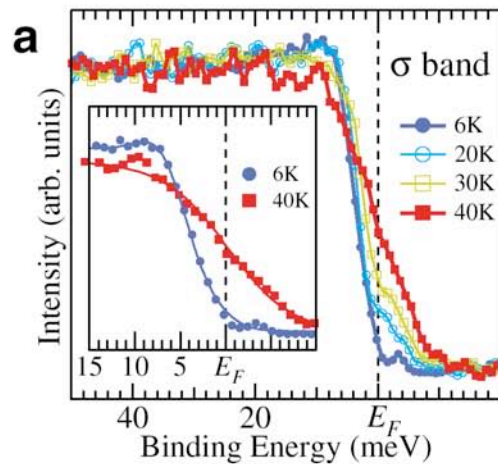


## s and p superconducting gaps



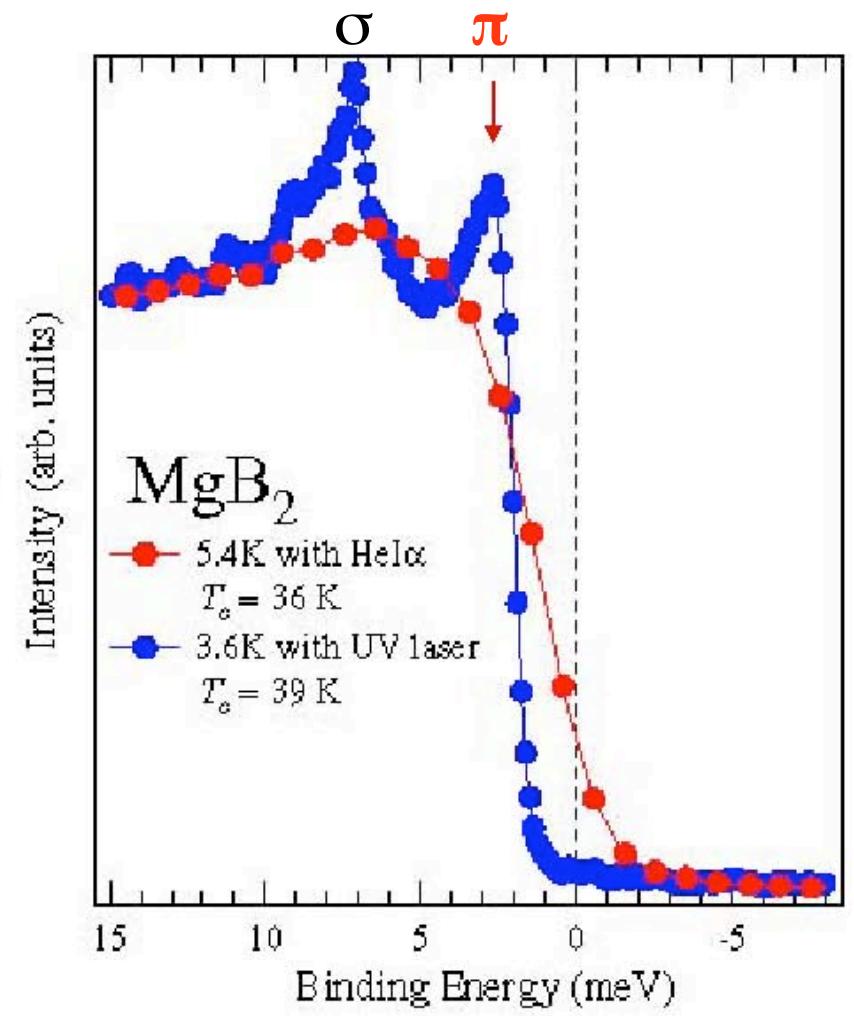
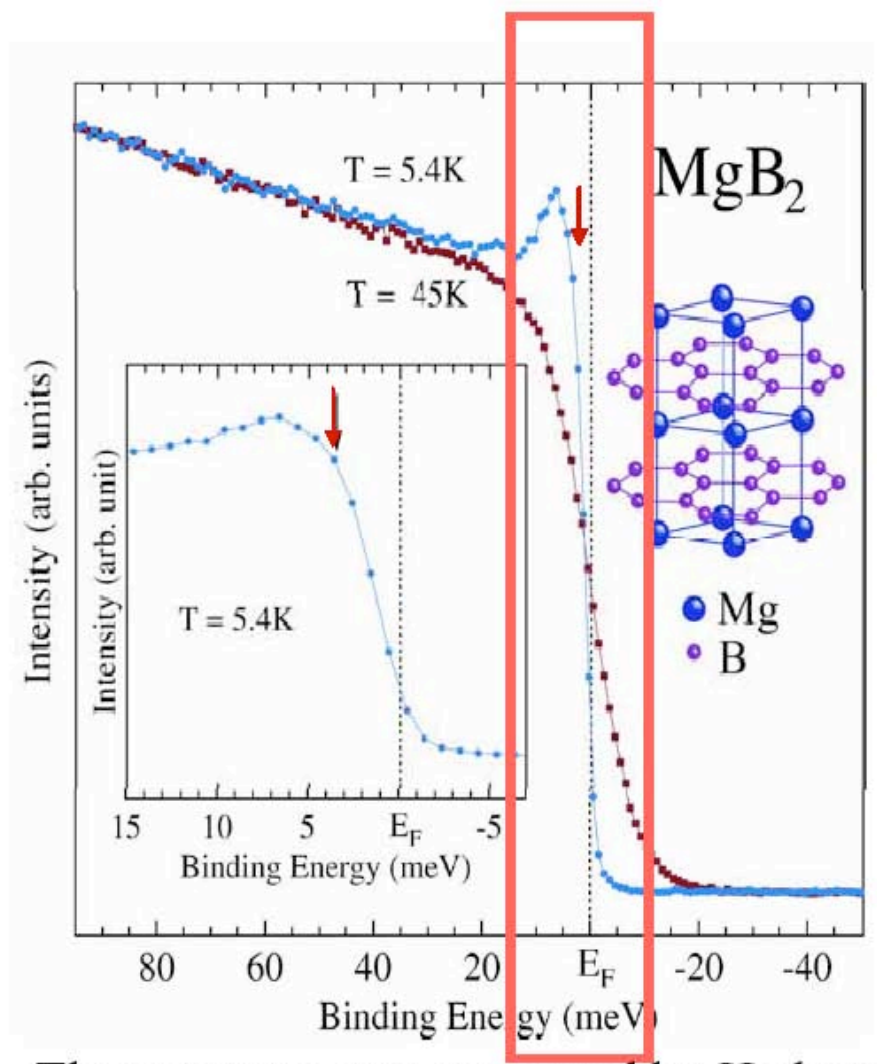
Two superconducting gaps:

$$D_s = 5.5 \text{ meV} \quad D_p = 2.2 \text{ meV}$$



S. Tsuda et al. Phys. Rev. Lett. **91**, 127001 (2003)

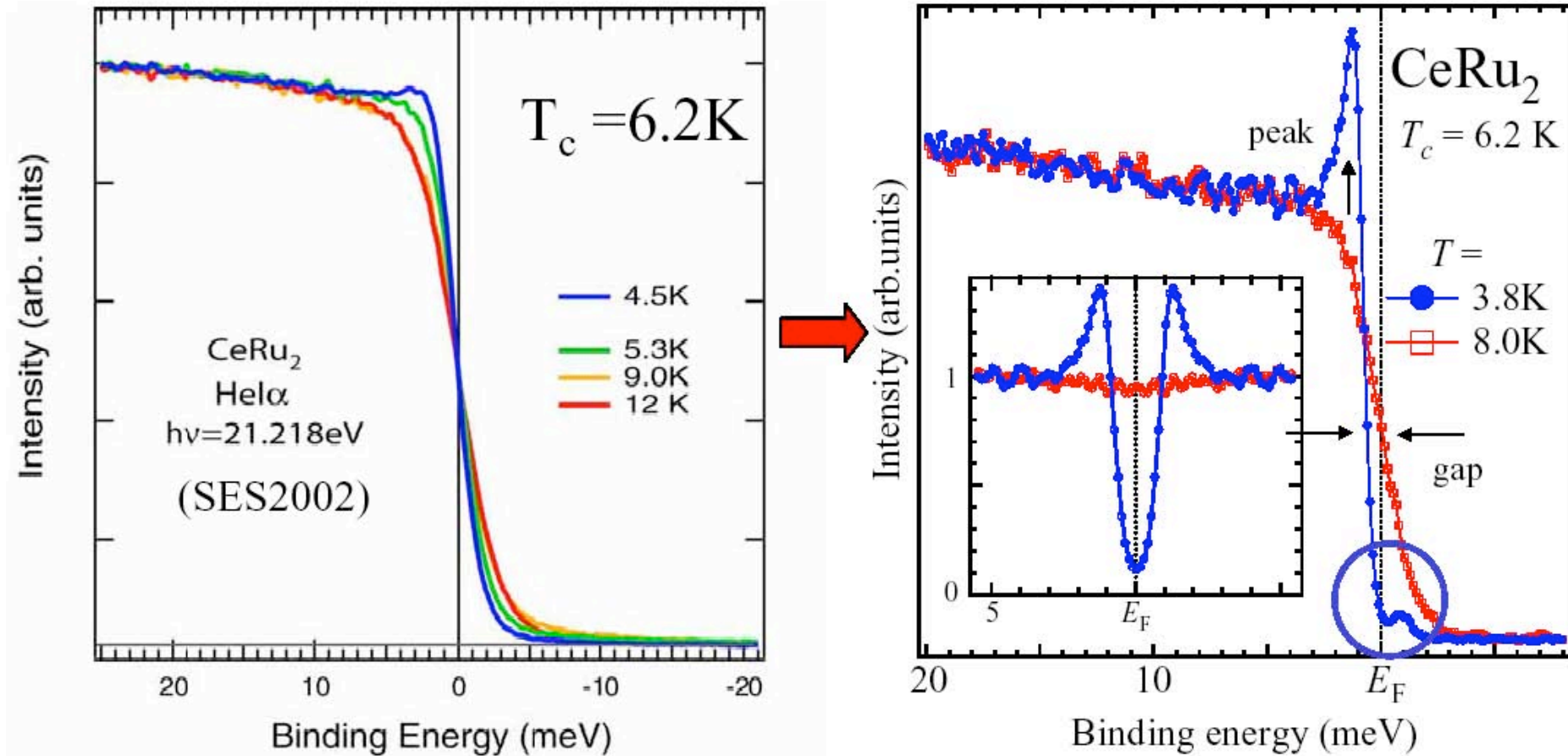
# “sub meV” resolution spectra on MgB<sub>2</sub> by laser-PES



The spectrum was measured by He lamp and show the two gap structure for the first time  
Tsuda et al., PRL87,17006(2001)

Laser-PES  
Tsuda et al.

# Superconducting gap of CeRu<sub>2</sub>



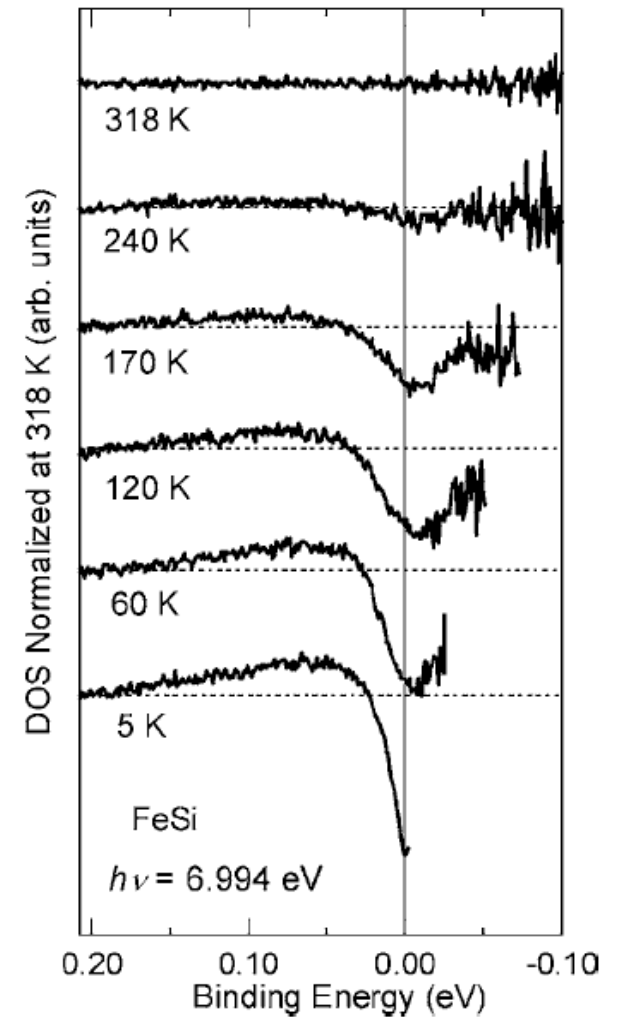
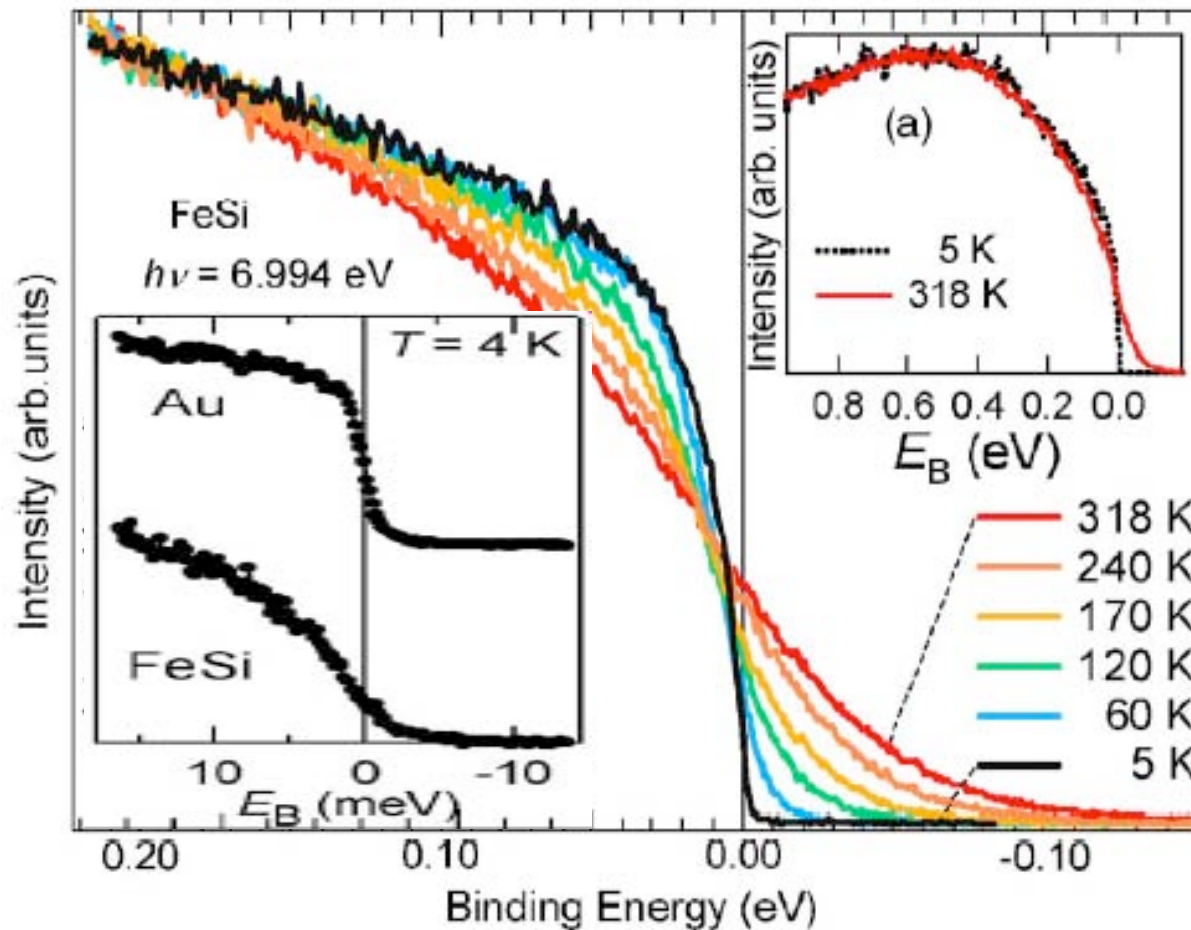
Superconducting gap was clearly observed by laser-PES

Kiss et al., PRL **94** (2005)57001



# Pseudo-gap opening in FeSi

K. Ishizaka et al., PRB 72, 233202 (2005)



# Critical question for ARPES at such low energies: is the Sudden Approx still valid?

**Fermi's Golden Rule for  $N$ -particle states:**

$$I(\vec{k}, \varepsilon) \propto \sum_s \left| \langle \Psi_{f,s} | \hat{\Delta} | \Psi_{i,0} \rangle \right|^2 \delta(E_{N,s} - E_{N,0} - h\nu)$$

## SUDDEN APPROXIMATION:

$$|\Psi_{f,s}\rangle = |\vec{k}, N-1, s\rangle = c_{\vec{k}}^+ |N-1, s\rangle \quad \text{Factorization !}$$

photoelectron

$s^{\text{th}}$  eigenstate of remaining  $N-1$  electron system

### Physical meaning:

photoelectron decouples from remaining system immediately after photoexcitation, *before* relaxation sets in

This is the most important result: in the sudden approx. the photoemission spectrum is proportional to the single particle spectral density function  $A(k, \omega)$

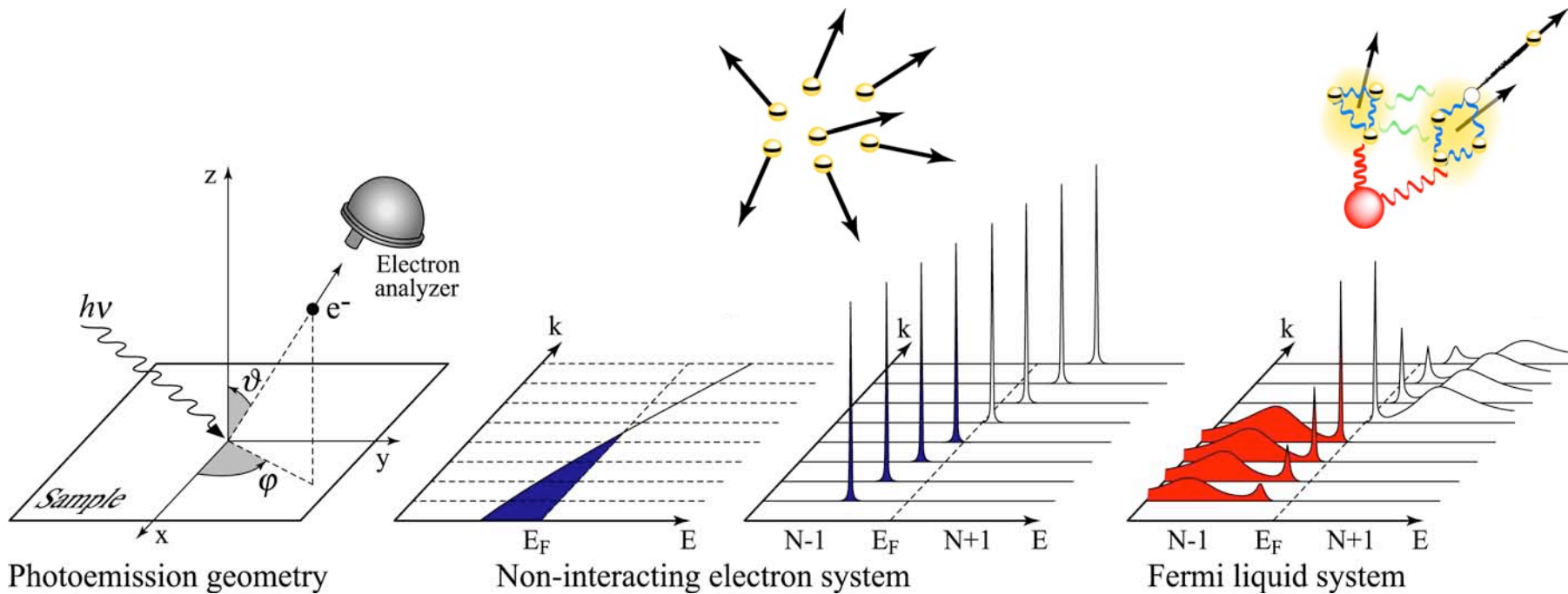
$$I(k, \omega) = I_{if}(k, \mathbf{A}, \nu) A(k, \omega) f_d(\omega, T)$$

↑
↑
↑

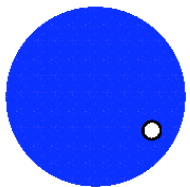
Proportional to  
Matrix elements
Spectral function
Fermi-Dirac

$$A(k, \omega) = \frac{1}{\pi} \text{Im} G(k, \omega) = \frac{\Gamma}{\pi} \sum_s \frac{|\langle N-1, s | c_k | N, i \rangle|^2}{(\omega - E_s^{N-1} + E_i^N)^2 + \Gamma^2}$$

The single particle spectral function  $A(k, \omega)$  gives the probability that the original system plus the bare hole (electron suddenly removed) will be found in an exact eigenstate of the (N-1)-system

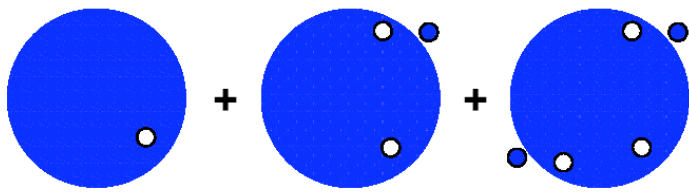


### non-interacting system



$$A(k, \omega) = -\frac{1}{\pi} \text{Im} G(k, \omega) = \frac{\Gamma}{\pi} \frac{|\langle N-1, i | c_k | N, i \rangle|^2}{(\omega - \varepsilon(k))^2 + \Gamma^2} = \frac{\Gamma}{\pi} \frac{1}{(\omega - \varepsilon_0(k))^2 + \Gamma^2}$$

### interacting system

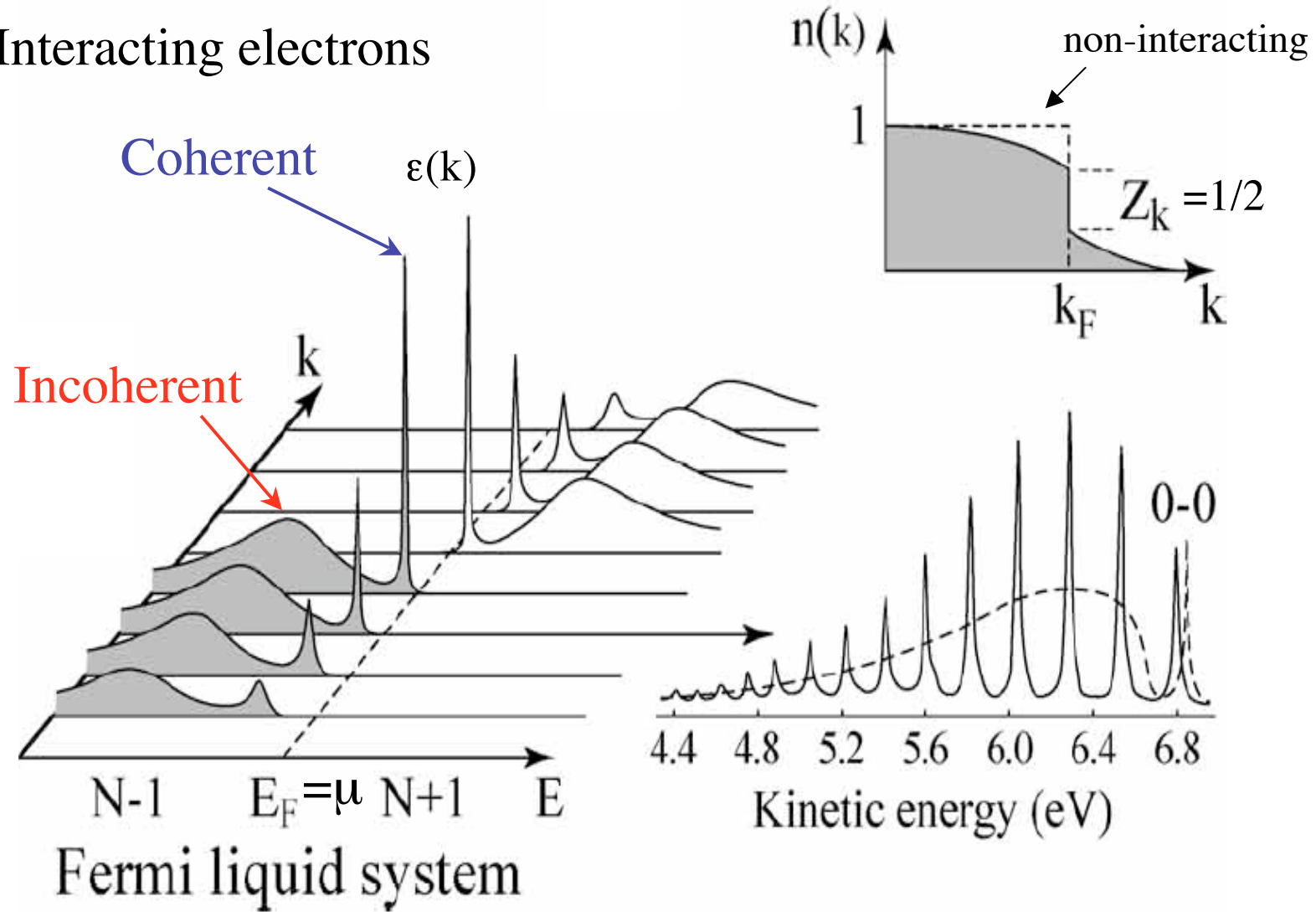


quasiparticle weight  $Z < 1$

$$A(k, \omega) = -\frac{1}{\pi} \text{Im} G(k, \omega) = \frac{\Gamma}{\pi} \frac{|\langle N-1, i | c_k | N, i \rangle|^2}{(\omega - \varepsilon(k))^2 + \Gamma^2} + \frac{\Gamma}{\pi} \sum_{s \neq i} \frac{|\langle N-1, s | c_k | N, i \rangle|^2}{(\omega - \varepsilon_s(k))^2 + \Gamma^2}$$

$$= A(k, \omega)_{\text{coh.}} + A(k, \omega)_{\text{incoh}}$$

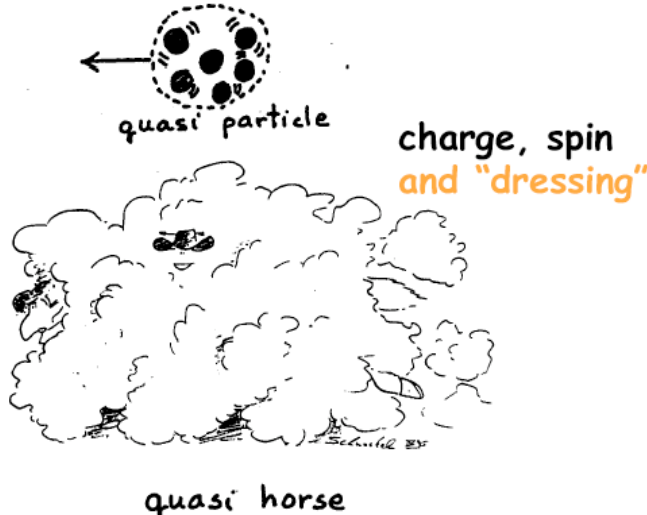
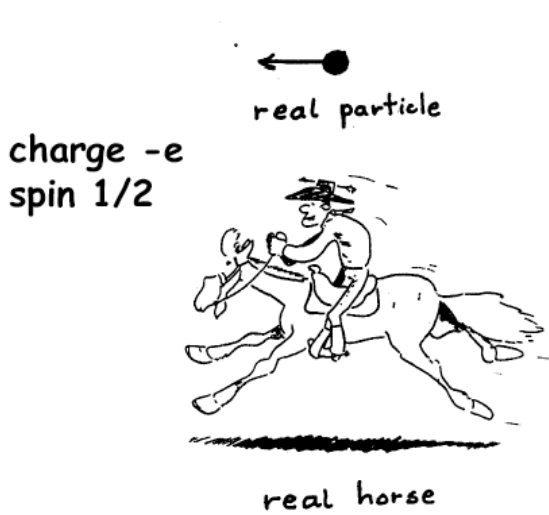
# Interacting electrons



$$A(k, \omega) = \frac{\Gamma}{\pi} \frac{Z_k}{(\omega - \epsilon(k))^2 + \Gamma^2} + \frac{\Gamma}{\pi} \sum_{s \neq i} \frac{|\langle N-1, s | c_k | N, i \rangle|^2}{(\omega - \epsilon_s(k))^2 + \Gamma^2} = A(k, \omega)_{\text{coh.}} + A(k, \omega)_{\text{incoh}}$$

**non-interacting**  
electrons

**interacting**  
electrons

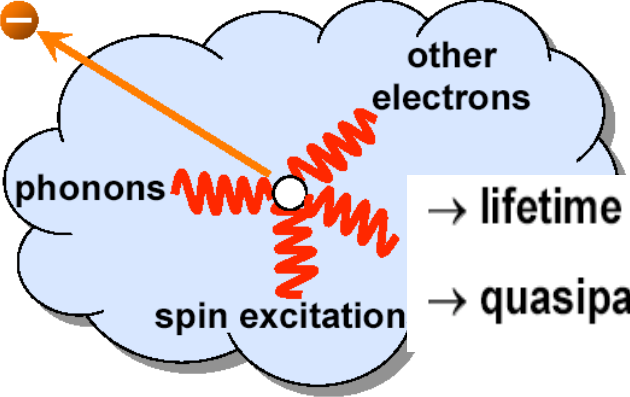


band structure  
 $\epsilon_0(\mathbf{k})$

quasiparticle band structure  
 $\epsilon(k) = [\epsilon_0(k) + \Sigma_1(k, \omega)]$

$\Sigma(k, \omega) = \Sigma_1(k, \omega) + i\Sigma_2(k, \omega)$  Self Energy

- **photohole probes interactions** between electrons and with other dynamical degrees of freedom
  - energy shifts
  - shake-up satellites
  - line broadening
  - line shape
 (*generalized Franck-Condon effect*)



→ lifetime broadening:

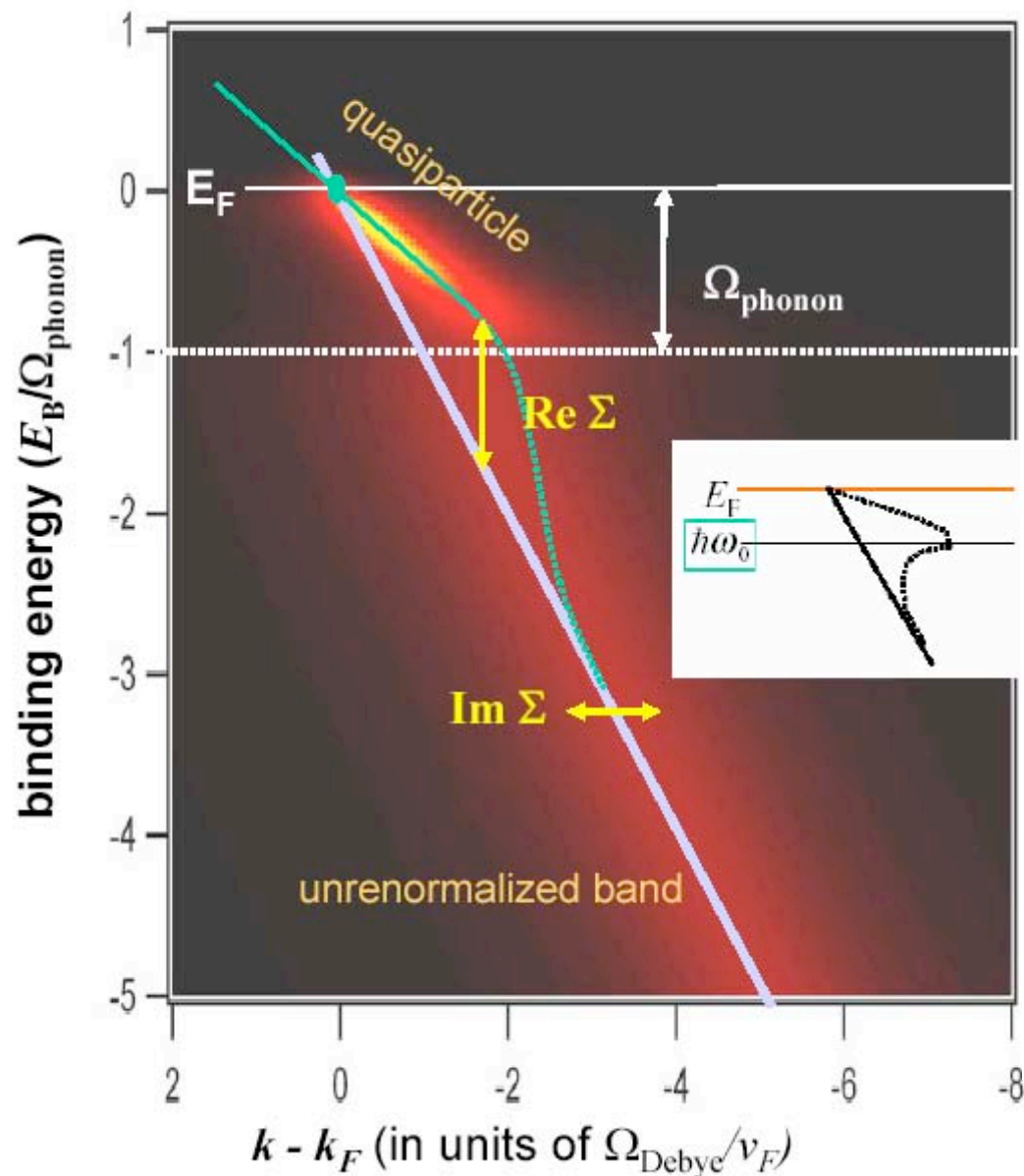
$$\Gamma_{\vec{k}} = \text{Im}\Sigma$$

→ quasiparticle weight:

$$Z_{\vec{k}} = \left(1 - \frac{\partial \Sigma}{\partial \omega}\right)^{-1} \leq 1$$

$|$   
 $= m_0 / m_{\text{eff}}$

## Debye Model ( $\lambda = 1$ )



$$\text{Im } \Sigma(\omega) \propto \lambda \int_0^\omega \rho_{\text{phonon}}(\Omega) d\Omega$$

energy scale  $\Omega_{\text{phonon}}$ :

separates between *virtual* and *real* scattering processes

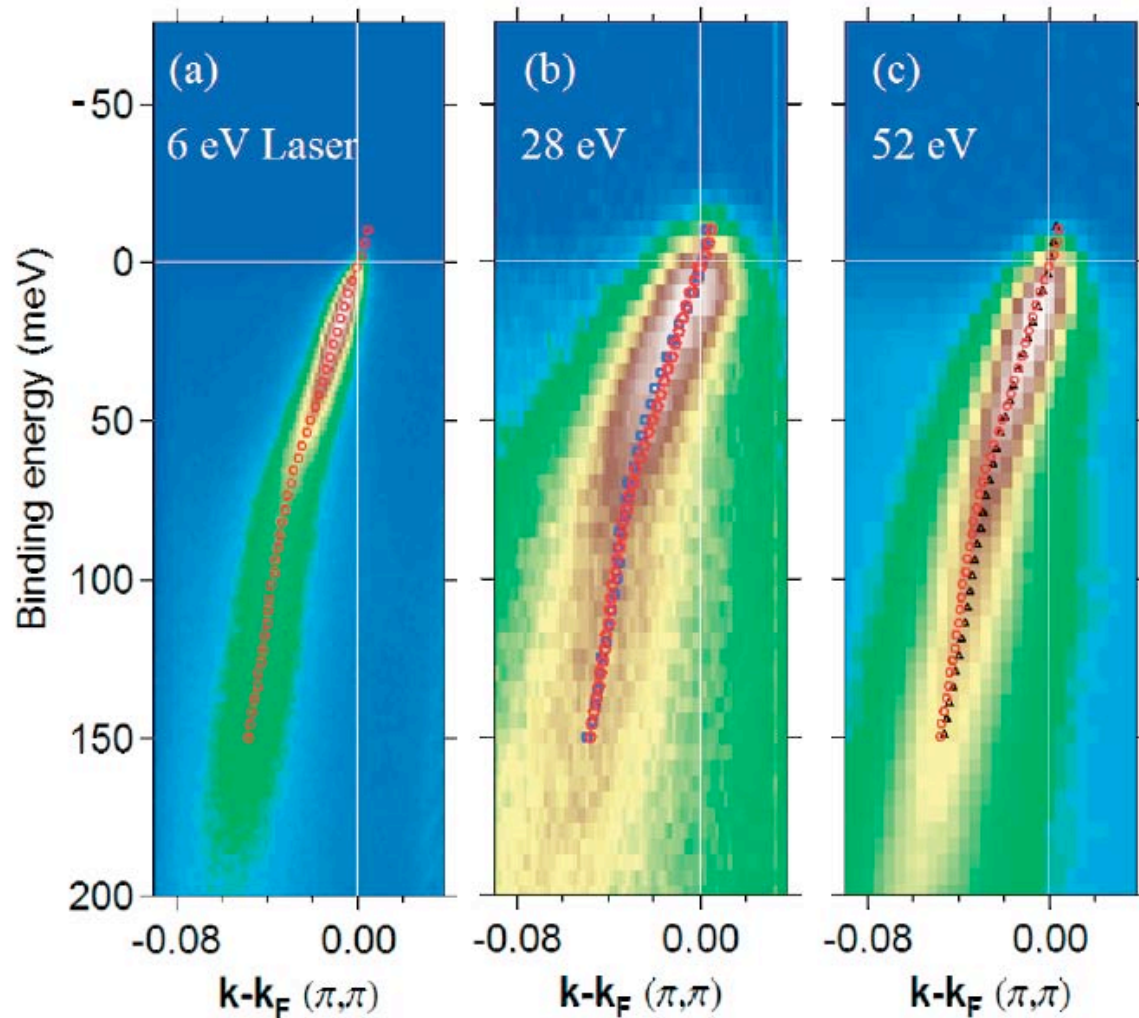
coupling constant  $\lambda$ :

effective Fermi velocity

$$v_F^* = v_F^0 / (1 + \lambda)$$

effective mass  $m^* = (1 + \lambda)m_0$

i.e.  $Z = (1 + \lambda)^{-1}$

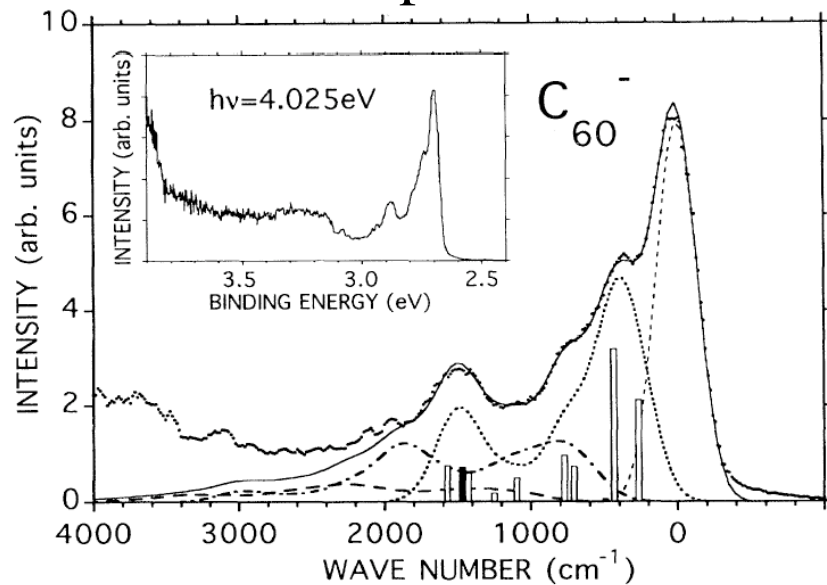


No dramatic changes in the electronic spectra near the Fermi surface. The sudden approx seems to be still valid or its breakdown may be not so important for the states near  $E_F$ .



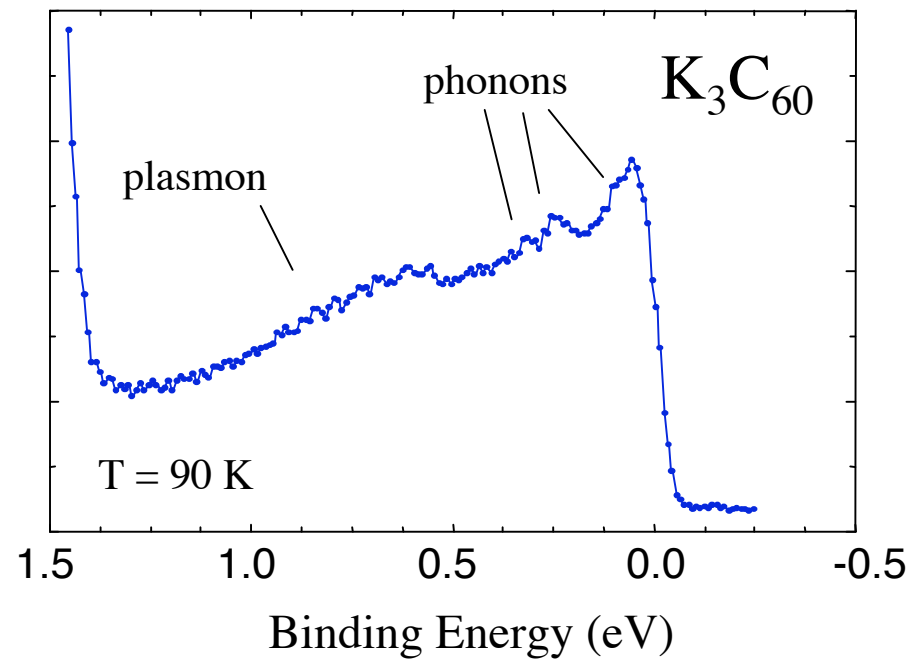
# Phonon features in $C_{60}$

Gas phase



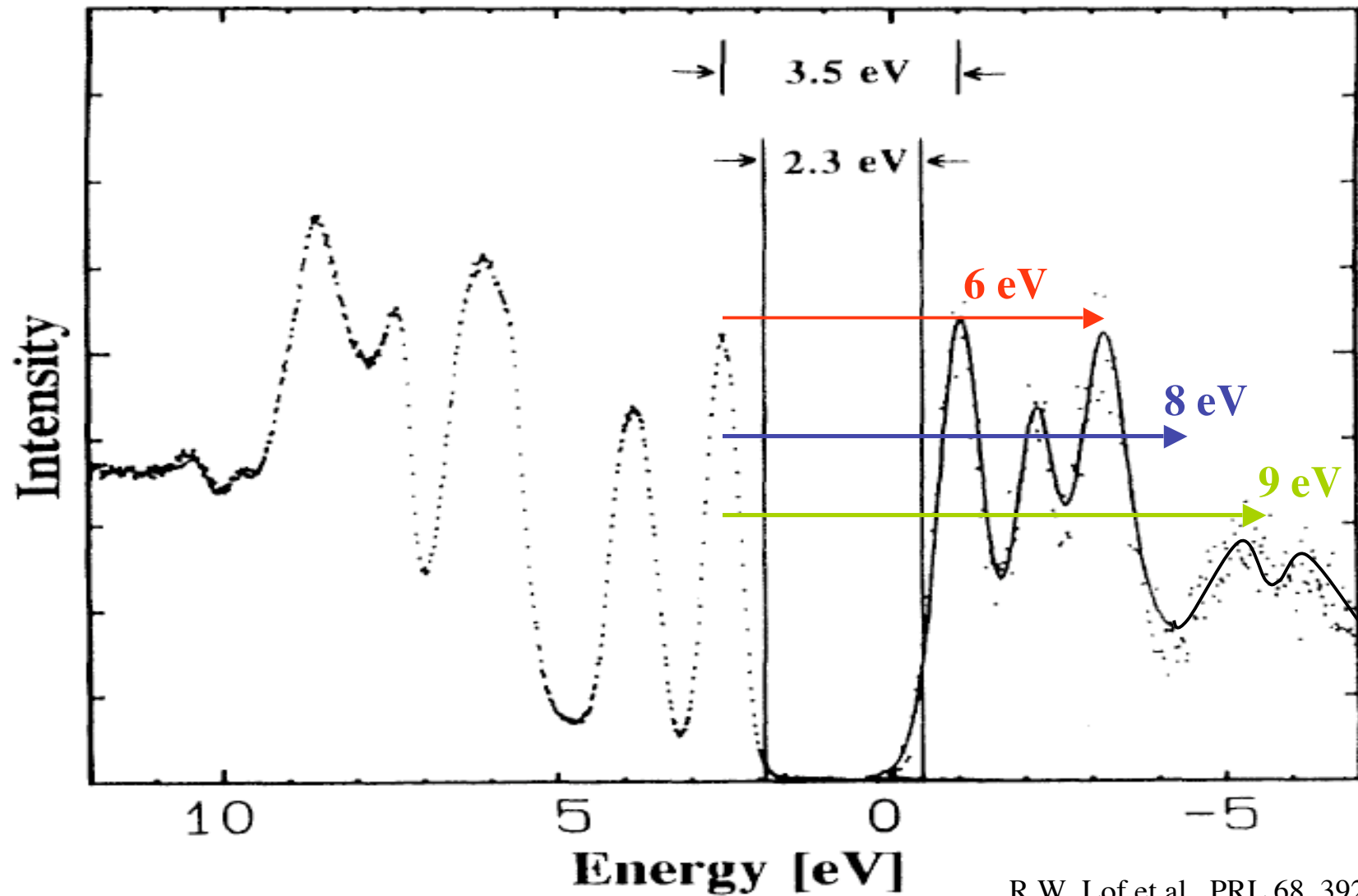
O. Gunnarsson et al. PRL74, 1875 (1995)

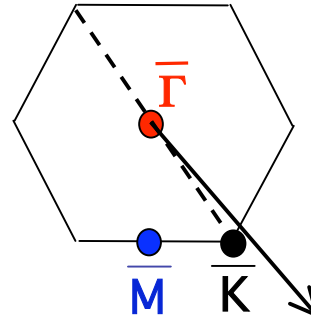
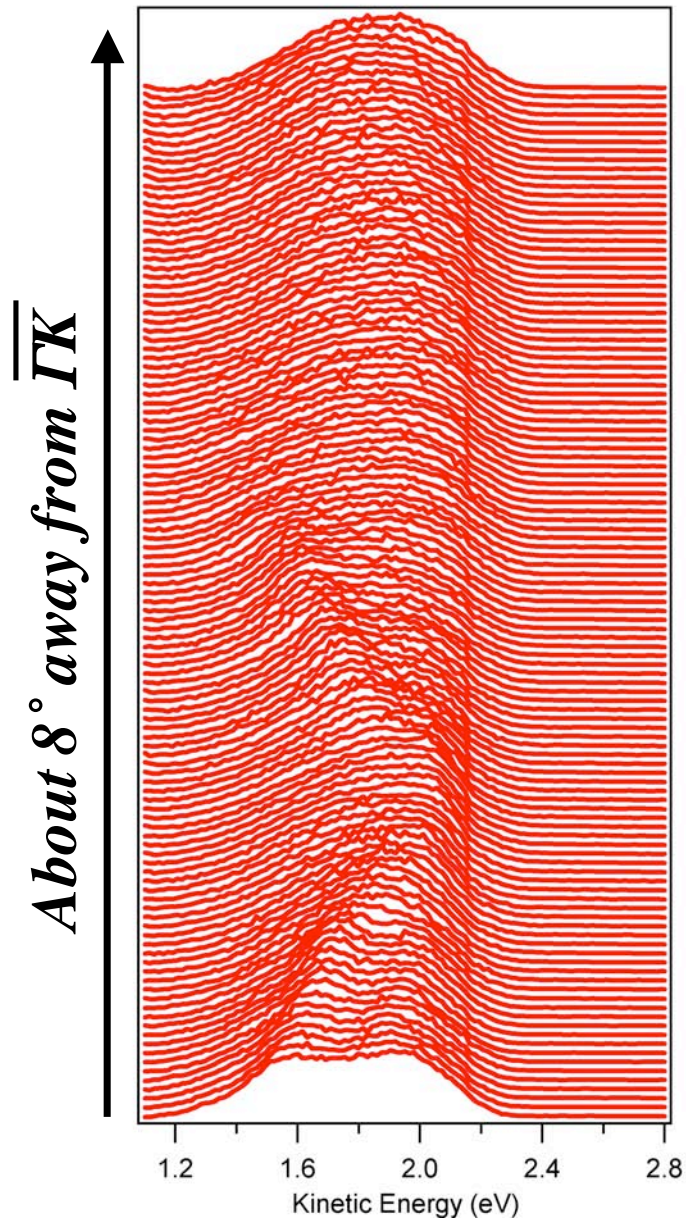
Solid



A. Goldoni et al. PRB 58,11023 (1998)

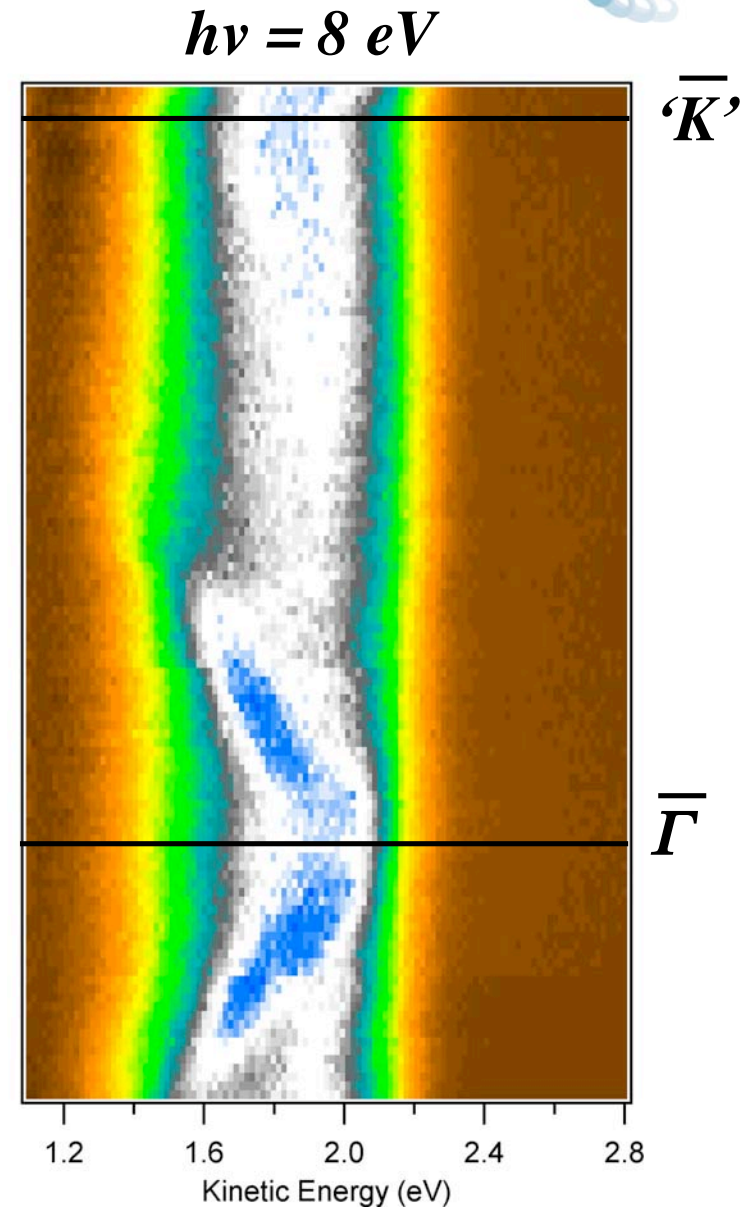
Another critical point for ARPES at low energies:  
“Final state” effects

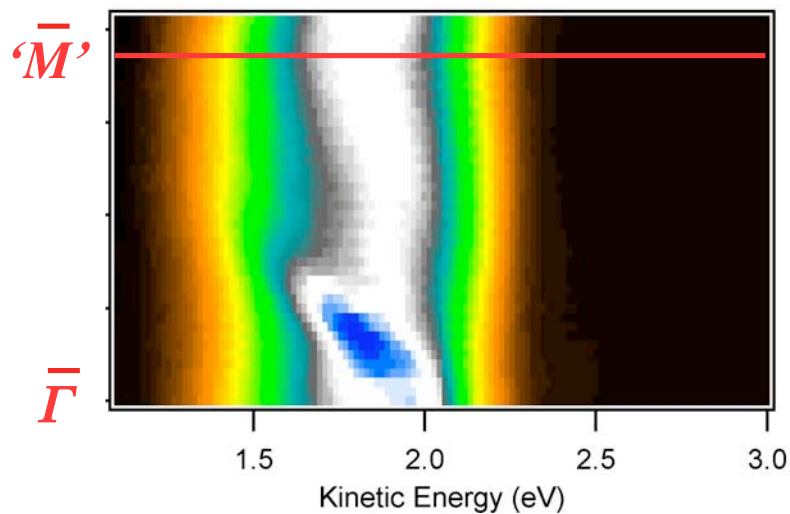
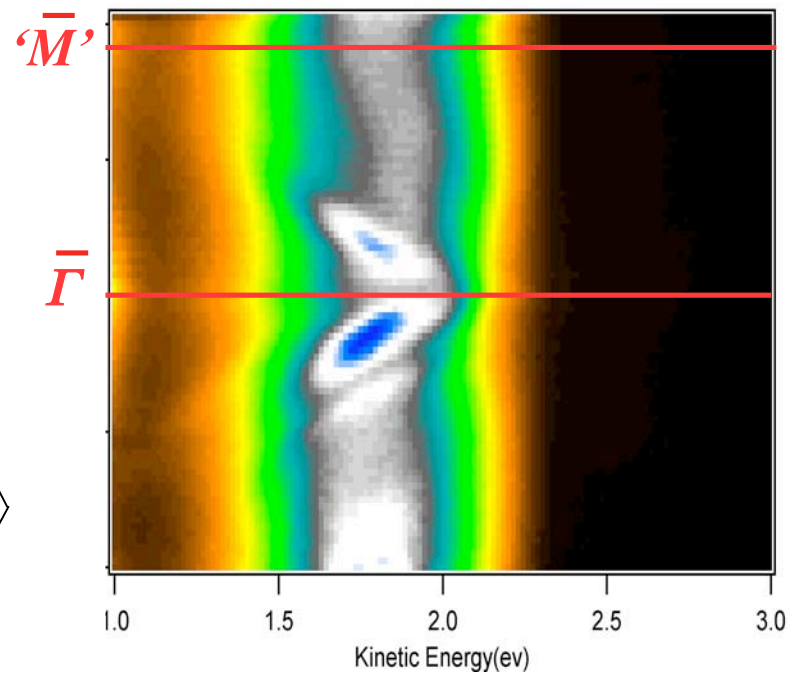
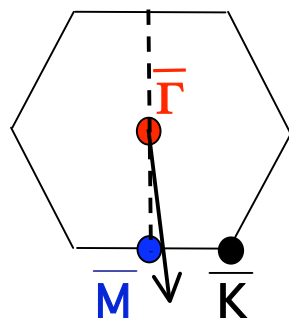
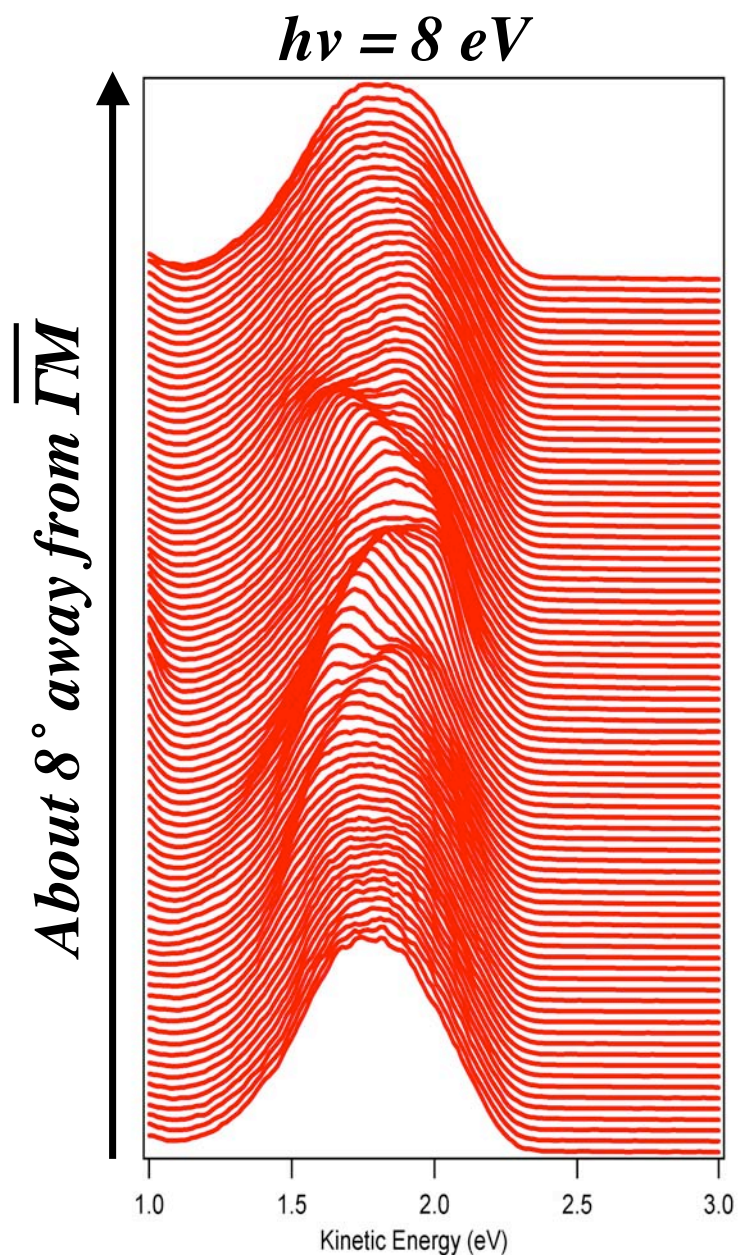


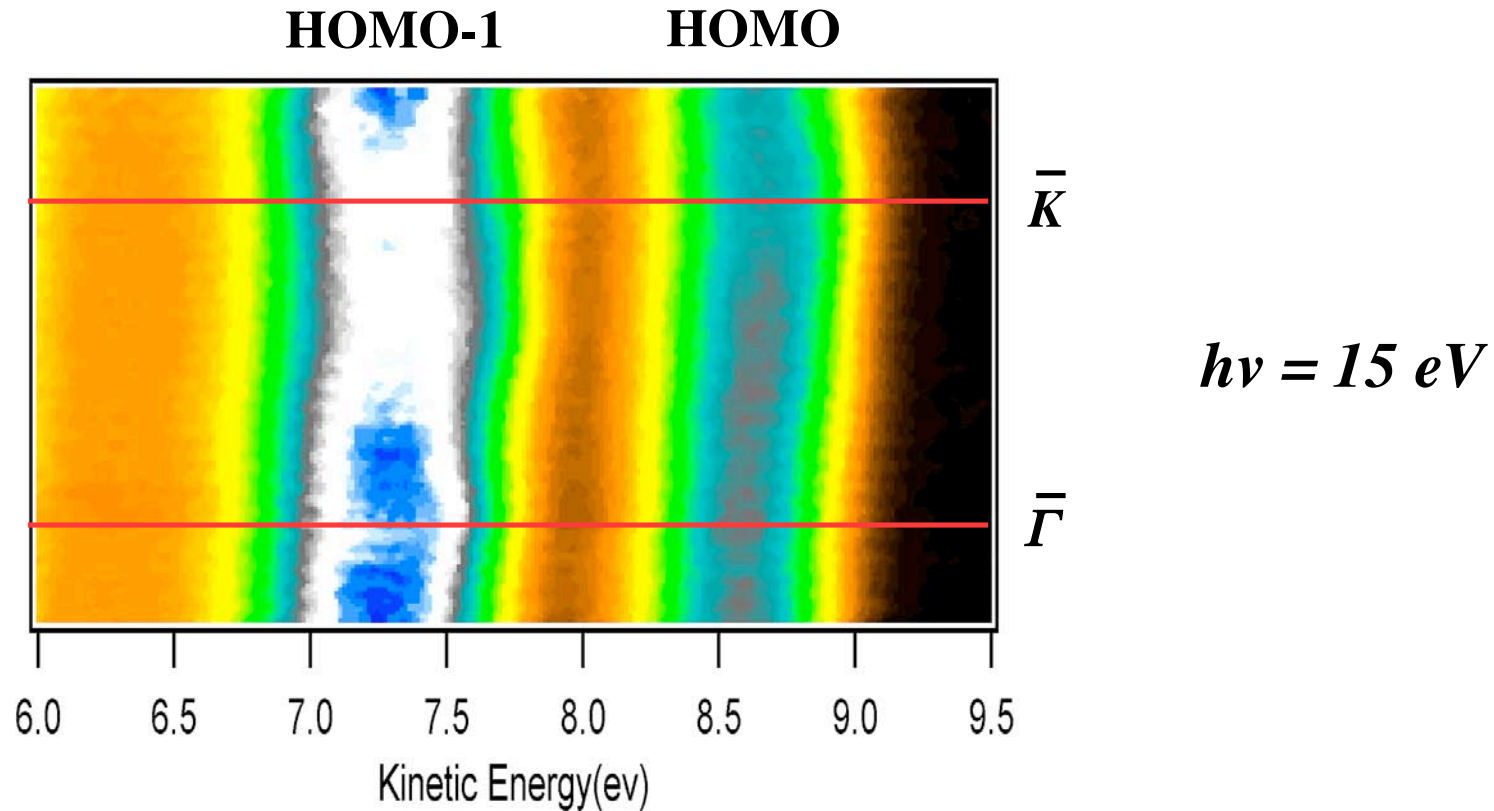


*HOMO  
band dispersion  
~ 0.6 eV*

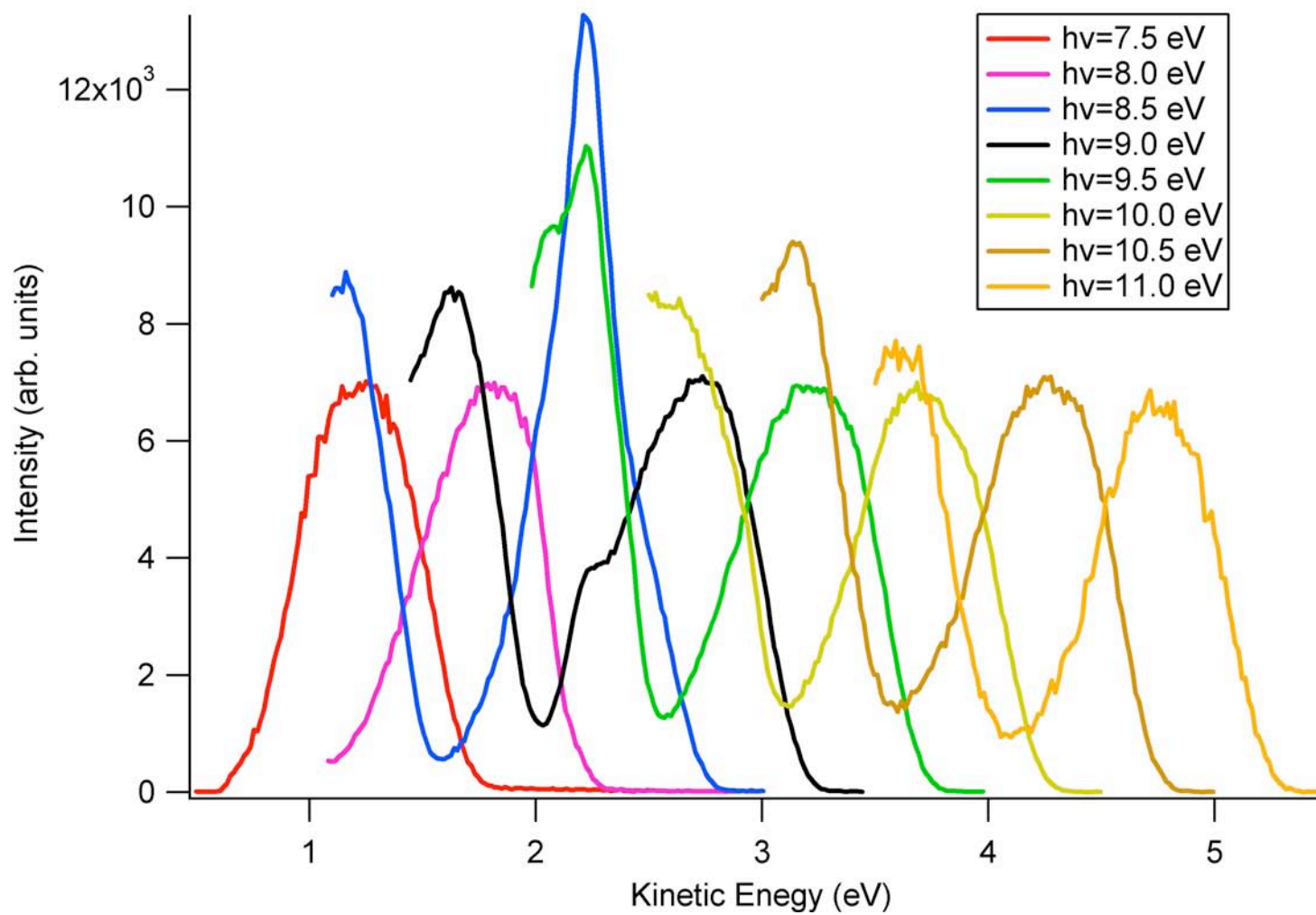
*No difference  
@ 77 K*





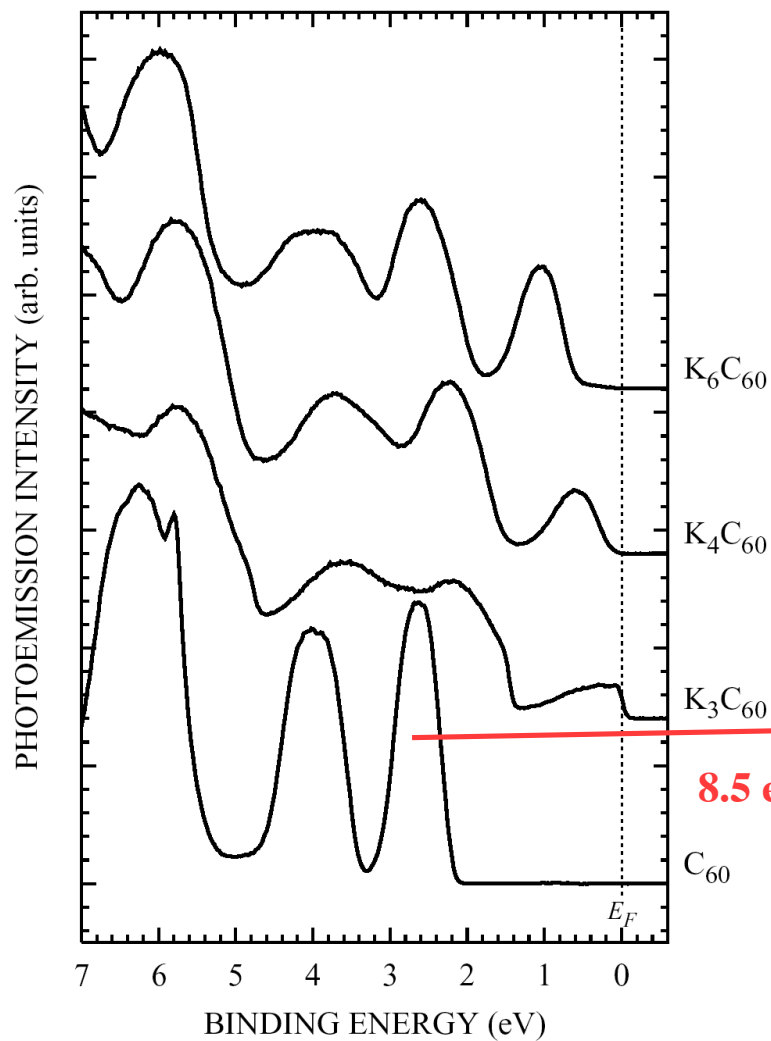


*HOMO dispersion apparently smaller than at 8 eV, but of the order of 0.2 eV ( $K_{||}$  integration? Final state effects?)*

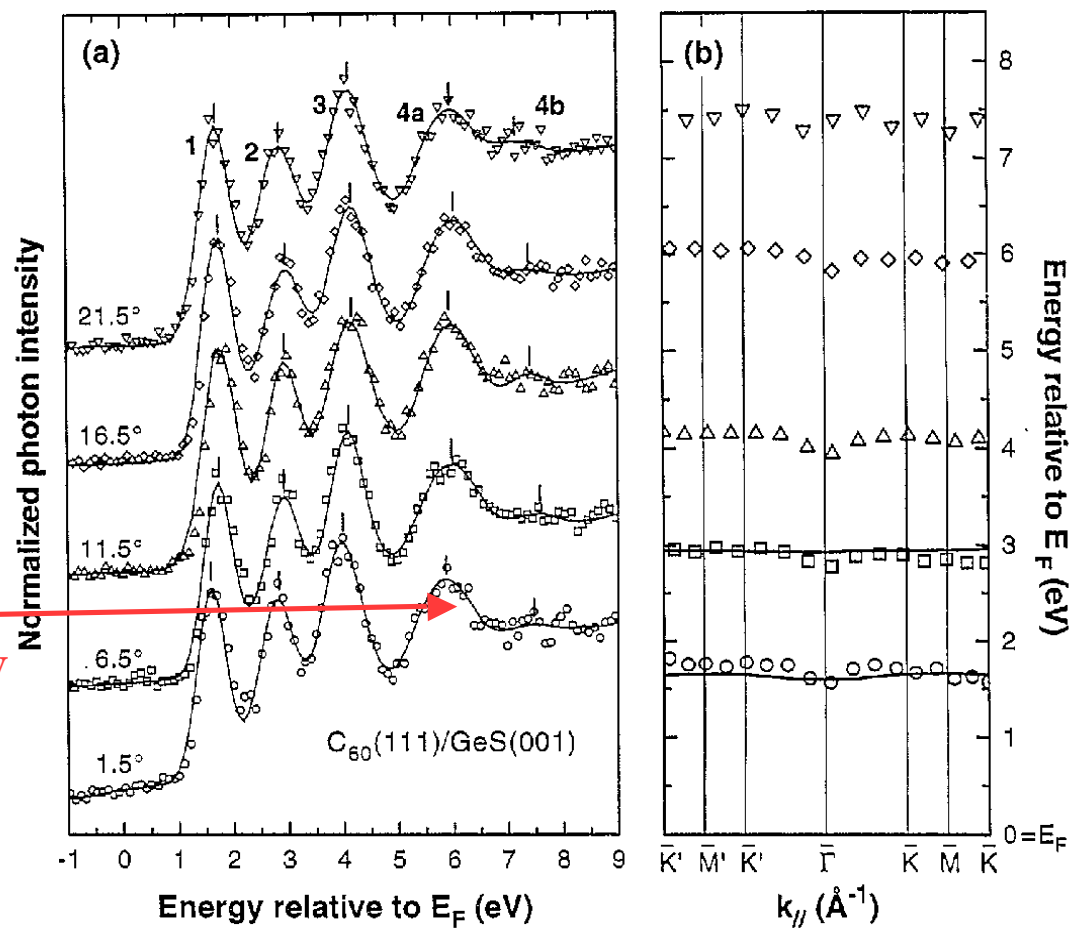


# $C_{60}(111)$ multilayer

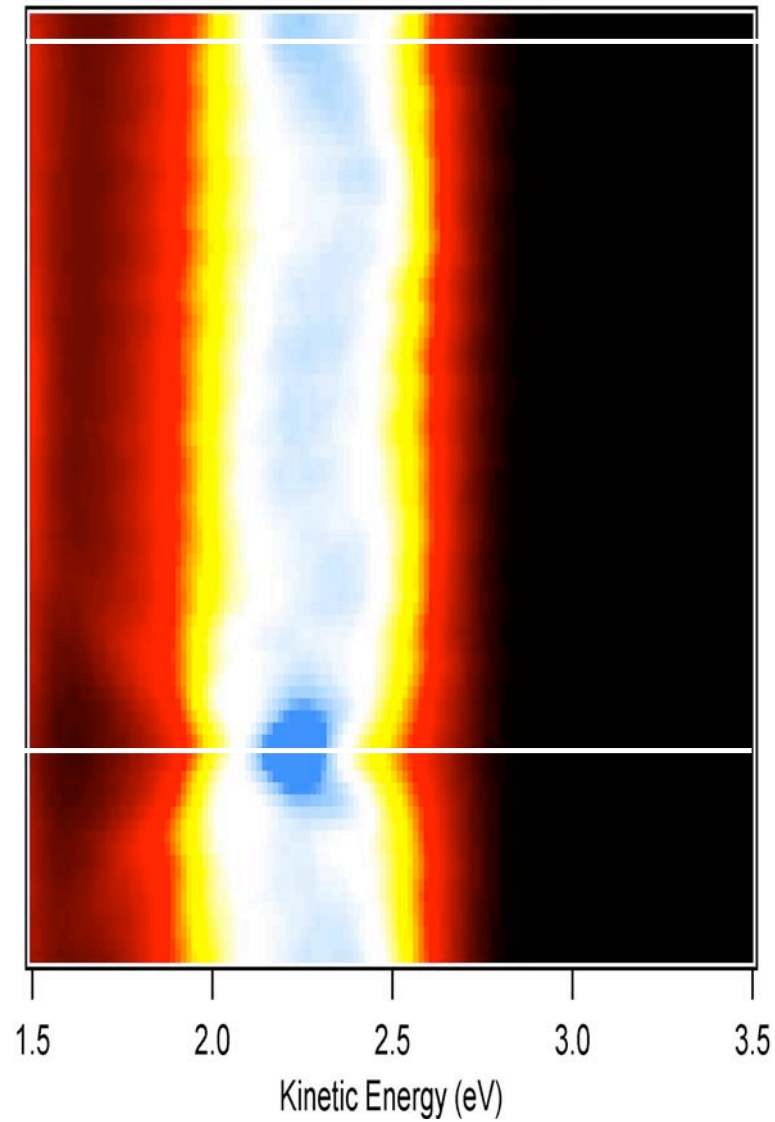
*photoemission*



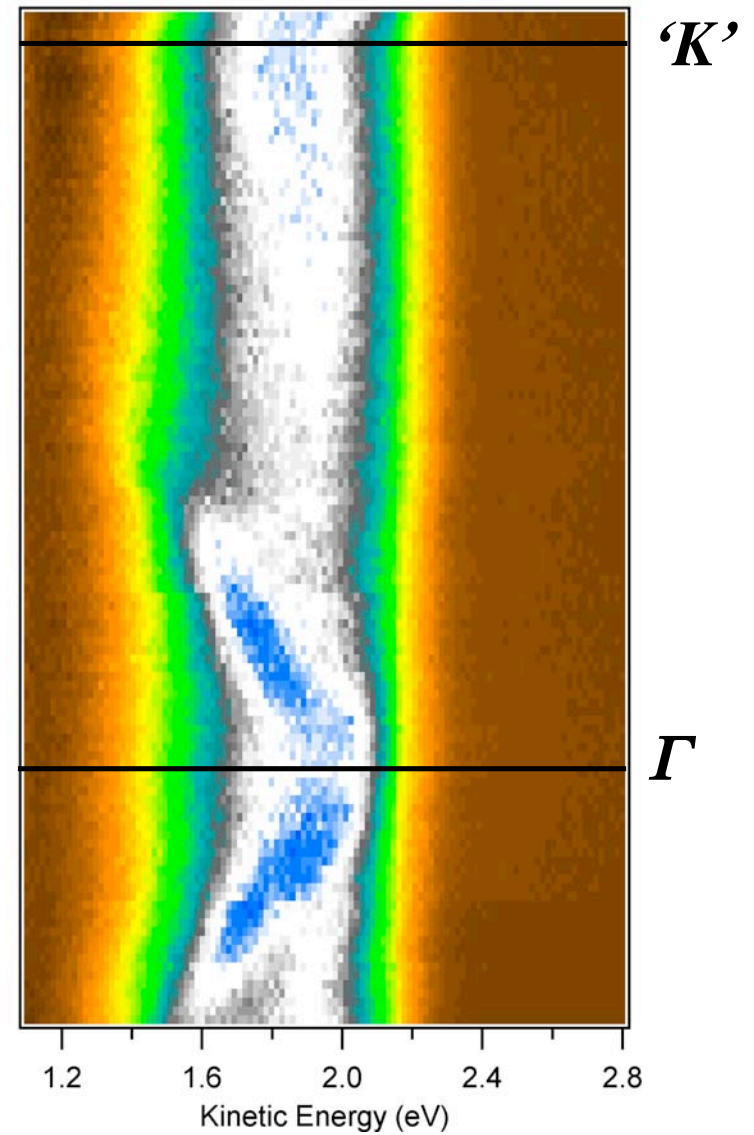
*inverse photoemission*



$h\nu = 8.5 \text{ eV}$

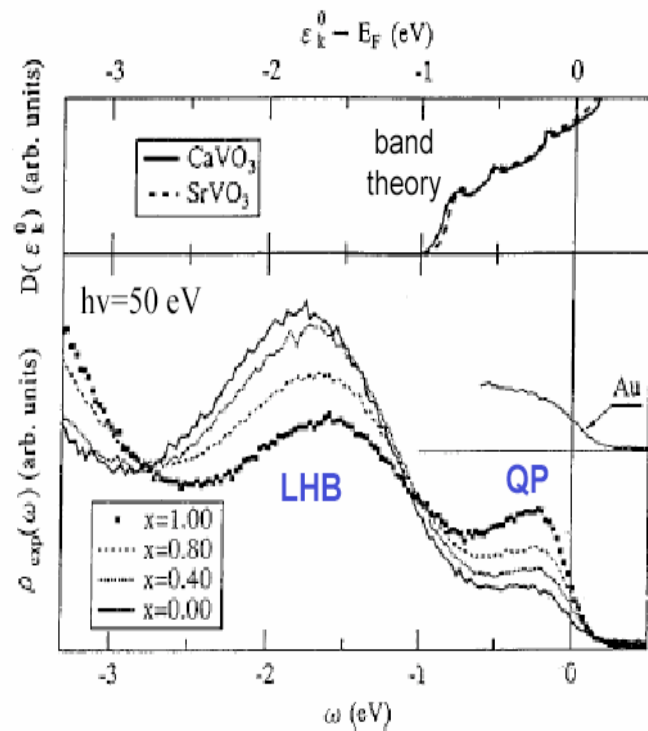


$h\nu = 8 \text{ eV}$



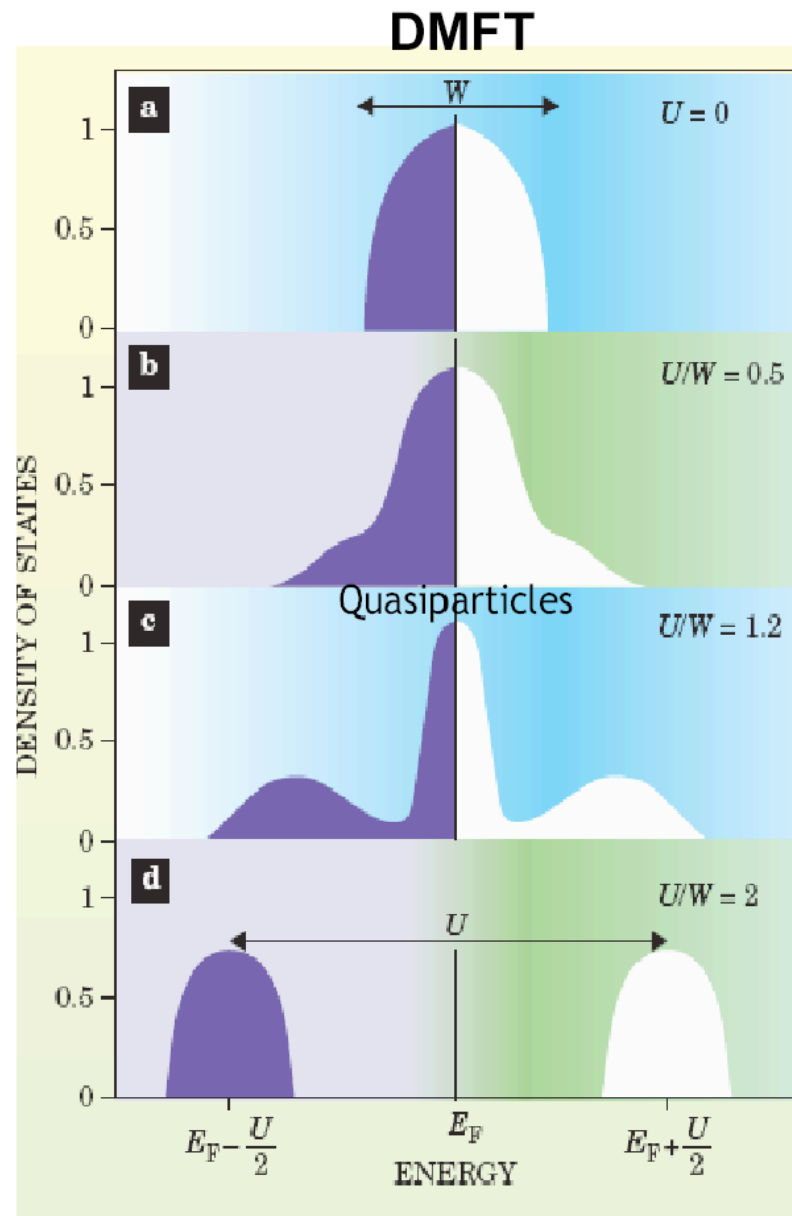


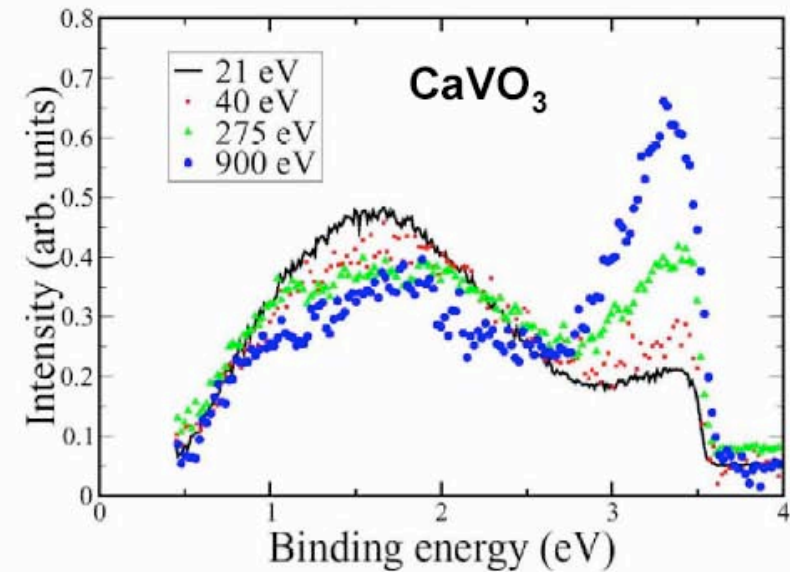
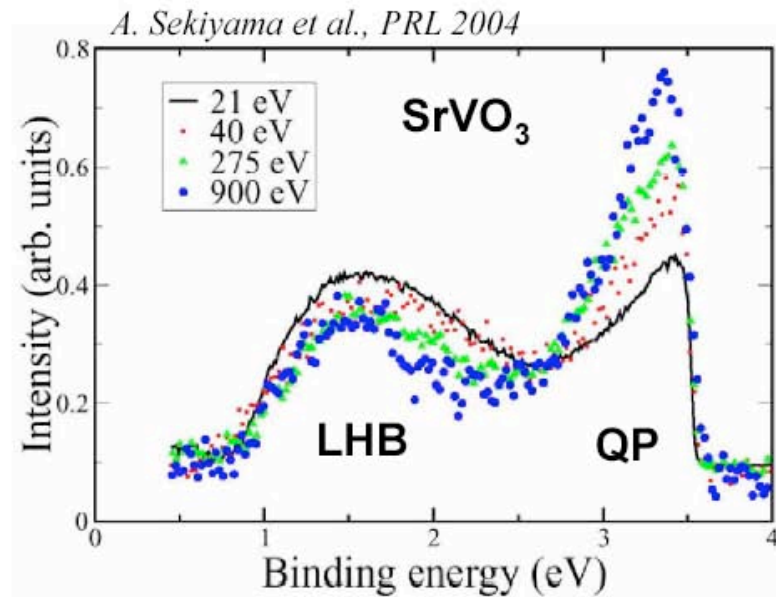
# Ca<sub>1-x</sub>Sr<sub>x</sub>VO<sub>3</sub>: angle-integrated photoemission



Inoue et al., PRL 1995

→ CaVO<sub>3</sub> more strongly correlated metal than SrVO<sub>3</sub> ?





⇒ **at surface: reduced atomic coordination**

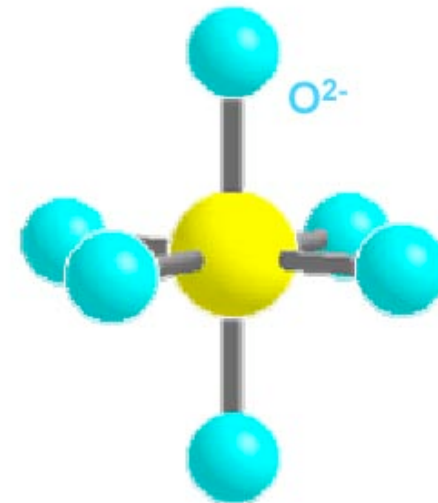
⇒ **effective bandwidth smaller:**

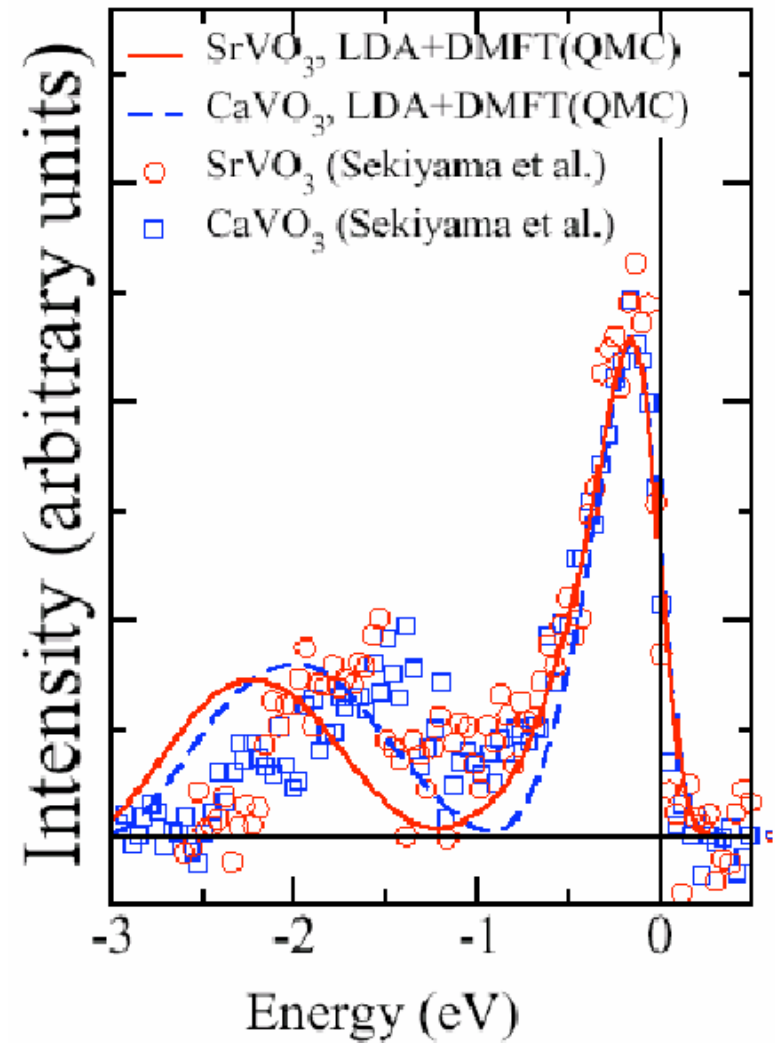
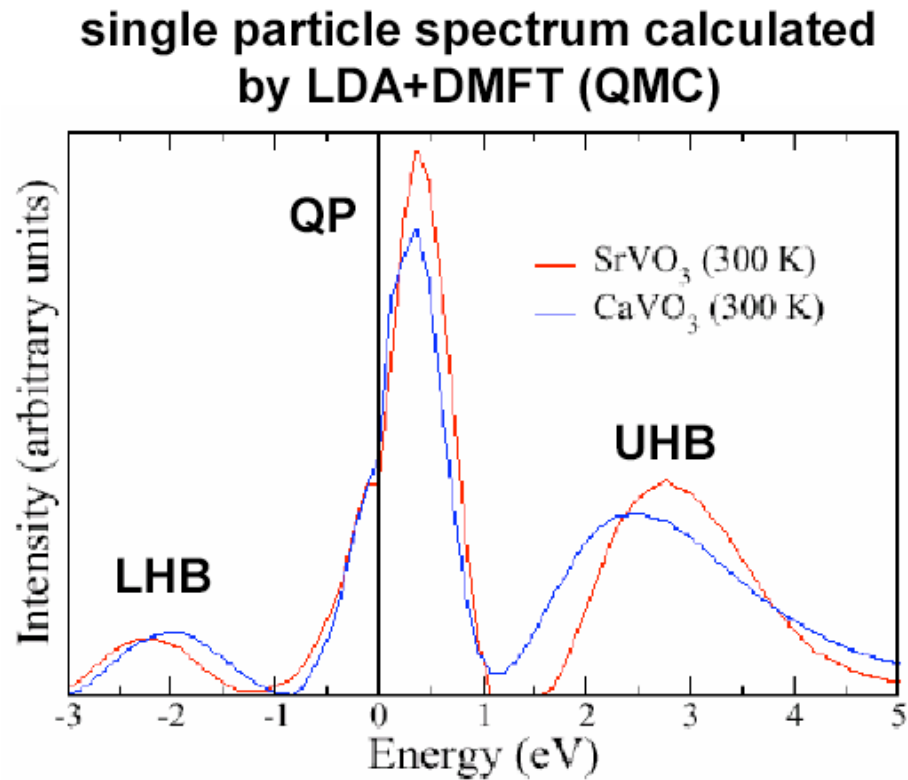
$$W_{surf} < W_{bulk}$$

⇒ **surface stronger correlated:**

$$U / W_{surf} > U / W_{bulk}$$

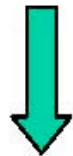
⇒ **surface effect stronger for CaVO<sub>3</sub>, but in bulk ~ identical for all compositions**





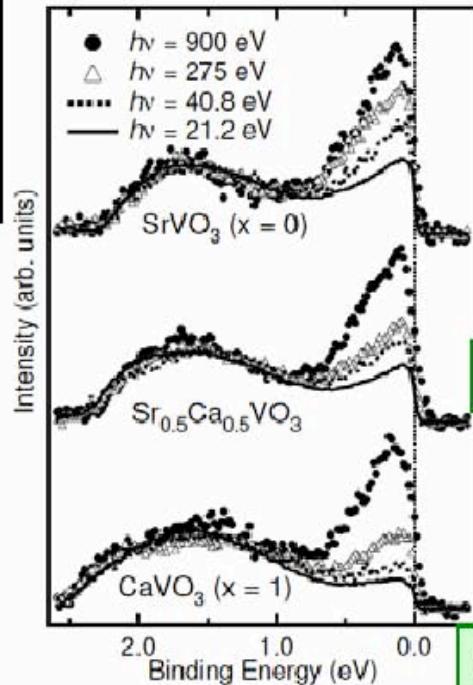
Good agreement, everything seems understood

- Incoherent peak becomes weak in SX PES
- $\text{CaVO}_3$  and  $\text{SrVO}_3$  spectra are similar in SX PES



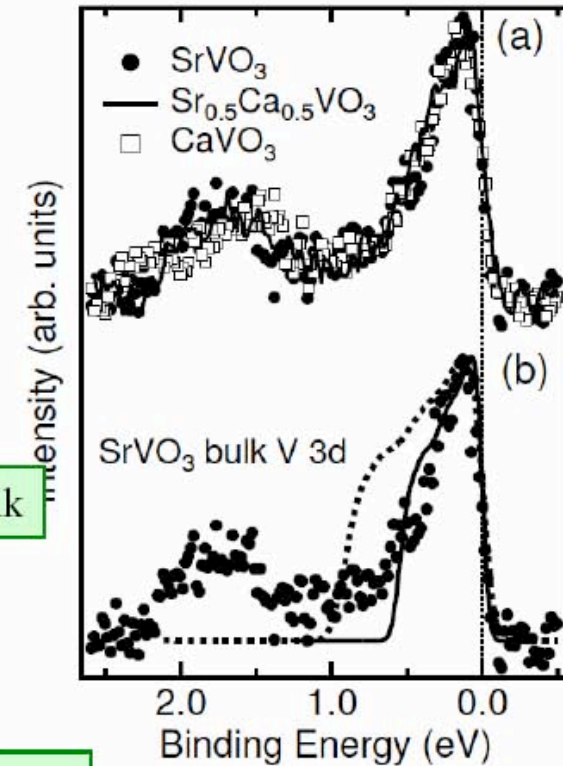
What happens in the bulk sensitive spectra using VUV laser ?

- More bulk sensitive
- much higher resolution



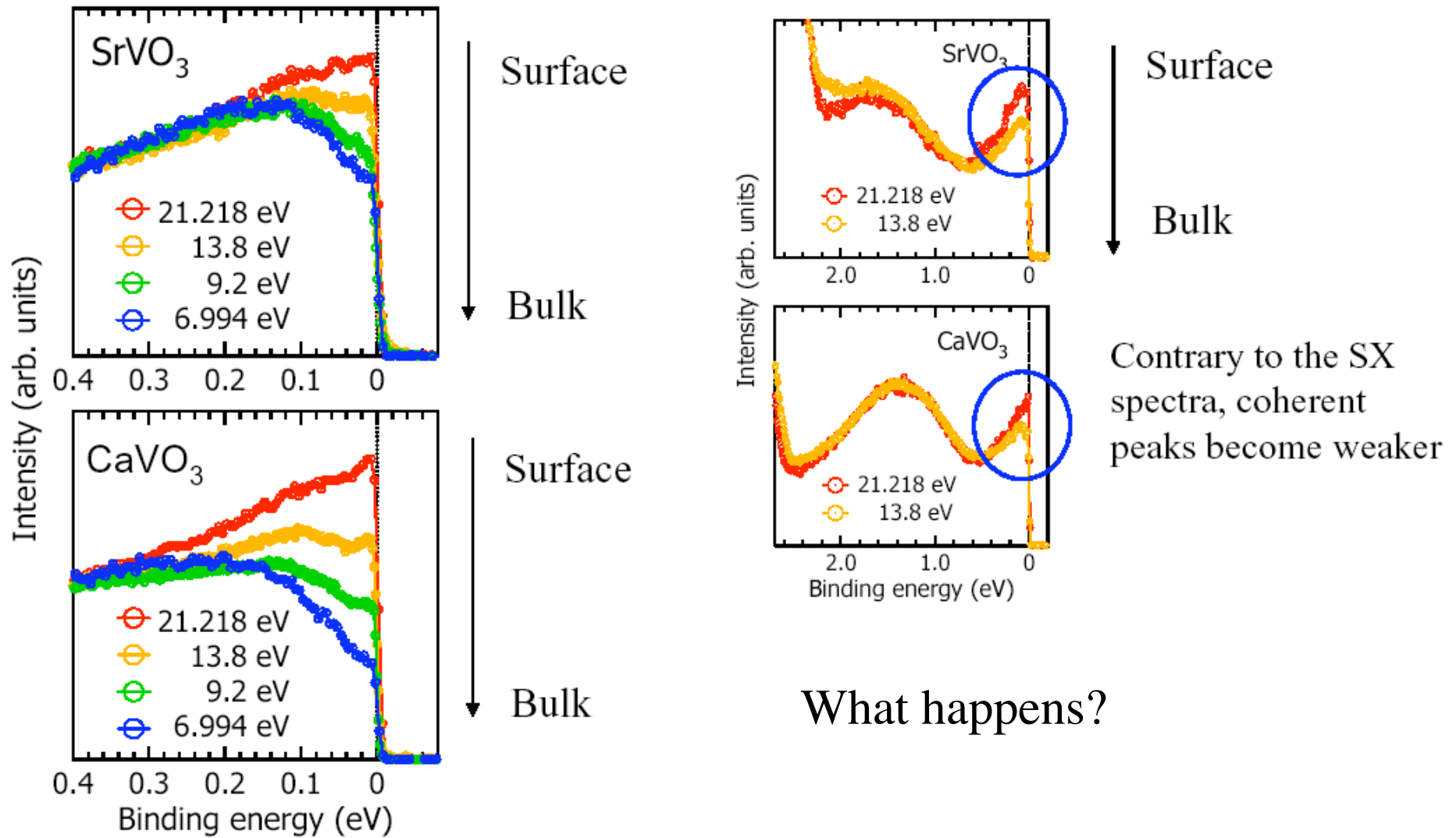
Photon-energy dependence of the V 3d spectral weights for  $\text{Sr}_{1-x}\text{Ca}_x\text{VO}_3$ . The V 3d spectra are normalized by the integrated intensities of the incoherent part ranging from 0.8 to 2.6 eV.

Sekiyama, PRL(2004)



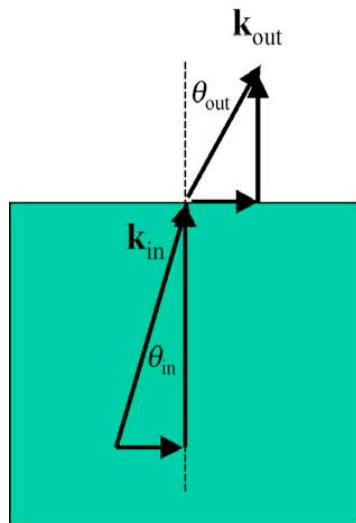
(a) Bulk V 3d spectral functions of  $\text{SrVO}_3$  (closed circles),  $\text{Sr}_{0.5}\text{Ca}_{0.5}\text{VO}_3$  (solid line) and  $\text{CaVO}_3$  (open squares).  
 (b) Comparison of the experimentally obtained bulk V 3d spectral function of  $\text{SrVO}_3$  (closed circles) to the V 3d partial density of states for  $\text{SrVO}_3$  (dashed curve) obtained from the band-structure calculation, which has been broadened by the experimental resolution of 140 meV. The solid curve shows the same V 3d partial density of states but the energy is scaled down by a factor of 0.6.

# Excitation energy dependence of coherence peak



# Other problems:

- Magnetic fields must be screened very well
- The total reflection angle for bulk state emission can be reached



### *Kinematic relations*

$$k_{out} = \sqrt{\frac{2m}{\hbar^2} E_{kin}}$$

$$k_{in} = \sqrt{\frac{2m}{\hbar^2} (E_{kin} + V_0)}$$

$$k_{out,\parallel} = k_{in,\parallel} \equiv k_{\parallel}$$

### *"Snell's Law"*

$$k_{\parallel} = \sin \theta_{out} \sqrt{\frac{2m}{\hbar^2} E_{kin}} = \sin \theta_{in} \sqrt{\frac{2m}{\hbar^2} (E_{kin} + V_0)}$$

### *Critical angle for emission*

$$(\sin \theta_{out})_{\max} = \sqrt{\frac{E_{kin}}{E_{kin} + V_0}}$$

- Large Brillouin zones cannot be mapped completely