



**The Abdus Salam  
International Centre for Theoretical Physics**



**2144-3**

**Workshop on Localization Phenomena in Novel Phases of Condensed  
Matter**

*17 - 23 May 2010*

**Asymmetric Metal-Insulator Transition in Ferromagnetic Films**

Khandker A. MUTTALIB

*University of Florida, Dept. of Physics  
P.O. Box 118440, 32611-8440 FL Gainesville  
U.S.A.*

# Asymmetric metal-insulator transition in ferromagnetic films

KAM



Collaborators:

**Rajiv Misra:** Penn State

Art Hebard: UF

Peter Wölfle: KIT

# Why ferromagnets?

- What happens to itinerant spins when charges localize?
- Is there a separation of spin and charge degrees of freedom that changes the nature of the metal-insulator transition?

Is M-I transition any different in itinerant magnetic systems ?

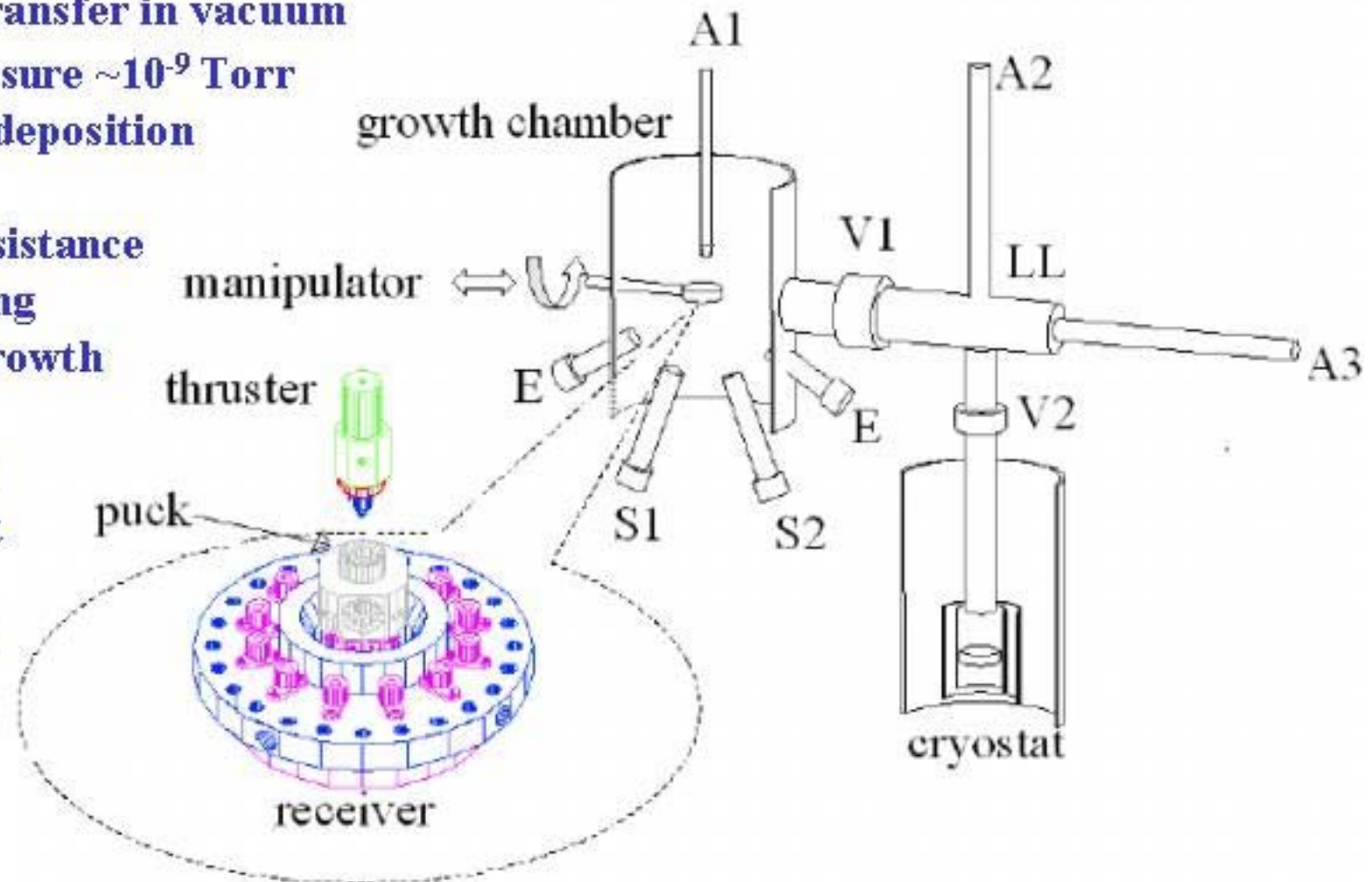
# Why films?

- Gd films show weak localization effects as well as quantum corrections due to scattering off spin waves. Both disorder and spin important.
- Film geometry allows one to change disorder in small steps, over a wide range across M-I transition, by varying deposition parameters.
- Highly reproducible T-dependent conductivity.

Problem: ferromagnetic films oxidize easily.  
Need *in situ* measurements in high vacuum.

## “SHIVA”: SAMPLE HANDLING IN VACUUM

- Sample transfer in vacuum
- Base pressure  $\sim 10^{-9}$  Torr
- Multiple deposition sources
- *In situ* resistance monitoring during growth
- *In situ* magneto transport up to 7T, 4.5K



*In situ* measurements for air sensitive films

# Experimental constraints and limitations

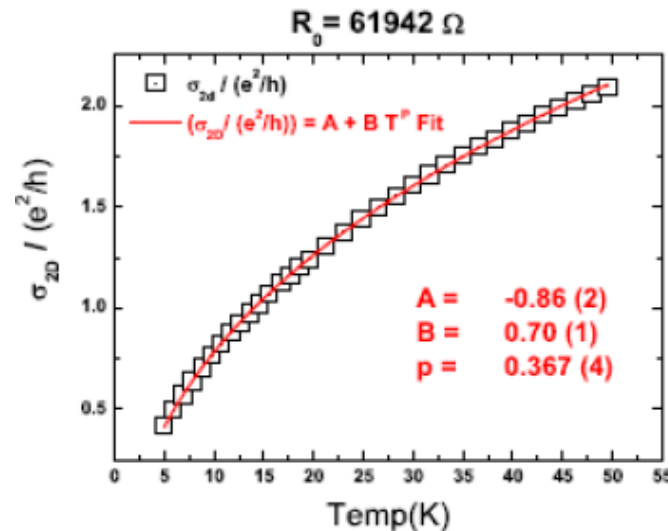
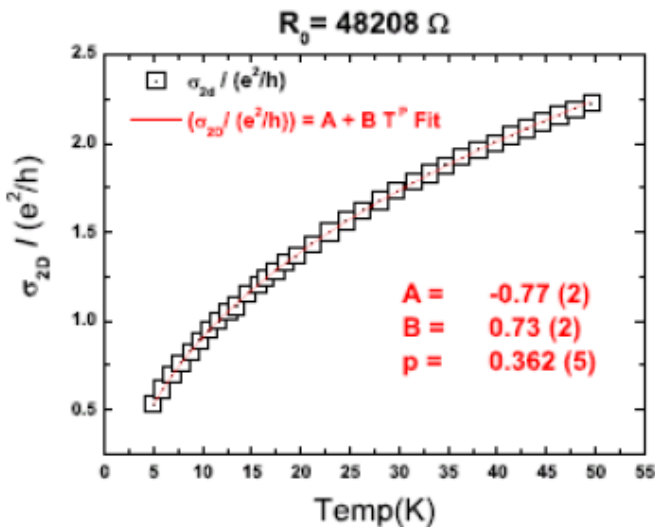
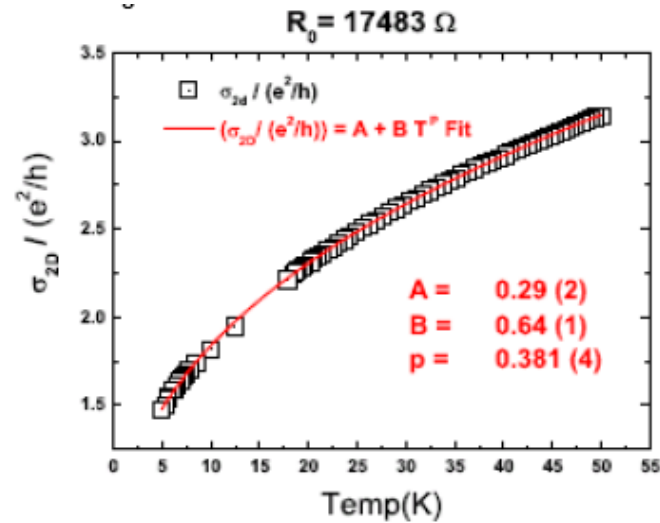
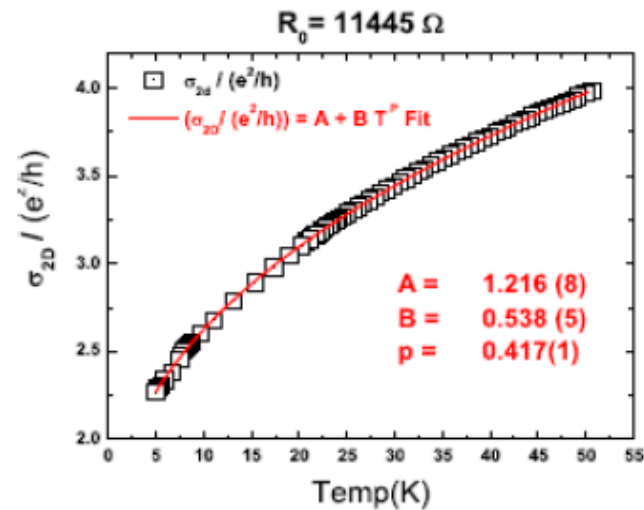
- SHIVA limited to  $T \geq 5 \text{ K}$  . Can not extrapolate to  $T=0$ .
- High disorder requires thin films:  $\sim 20 - 30 \text{ \AA}$ .
- Thickness of such films can not be measured very accurately.

# Resolution of experimental limitations

- Use finite temperature scaling to analyze data. No need to extrapolate to  $T=0$ .
- Use sheet resistance  $R_0$  as measure of disorder. No need to know the thickness accurately.
- Same thickness for annealed samples. Check reproducibility when grown separately.

Critical region is well-defined If scaling collapses all  $T$  and  $R_0$  dependent data onto a single curve.

# Data: T dependent conductivity



power law fit:

$$\begin{aligned} \sigma(T; R_0) / L_0 \\ = A + B T^p \end{aligned}$$

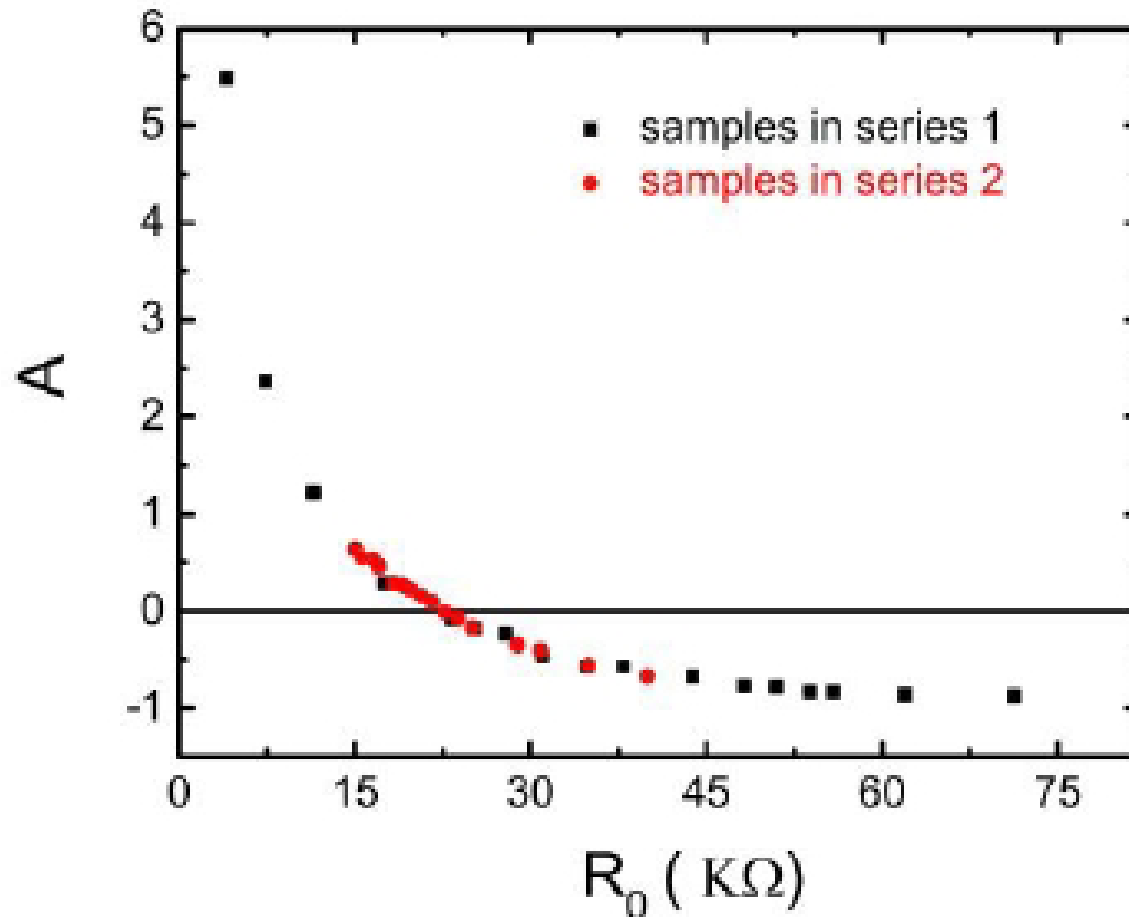
where

$$L_0 = e^2/h;$$

A, B, p vary  
with disorder



# A as a function of disorder

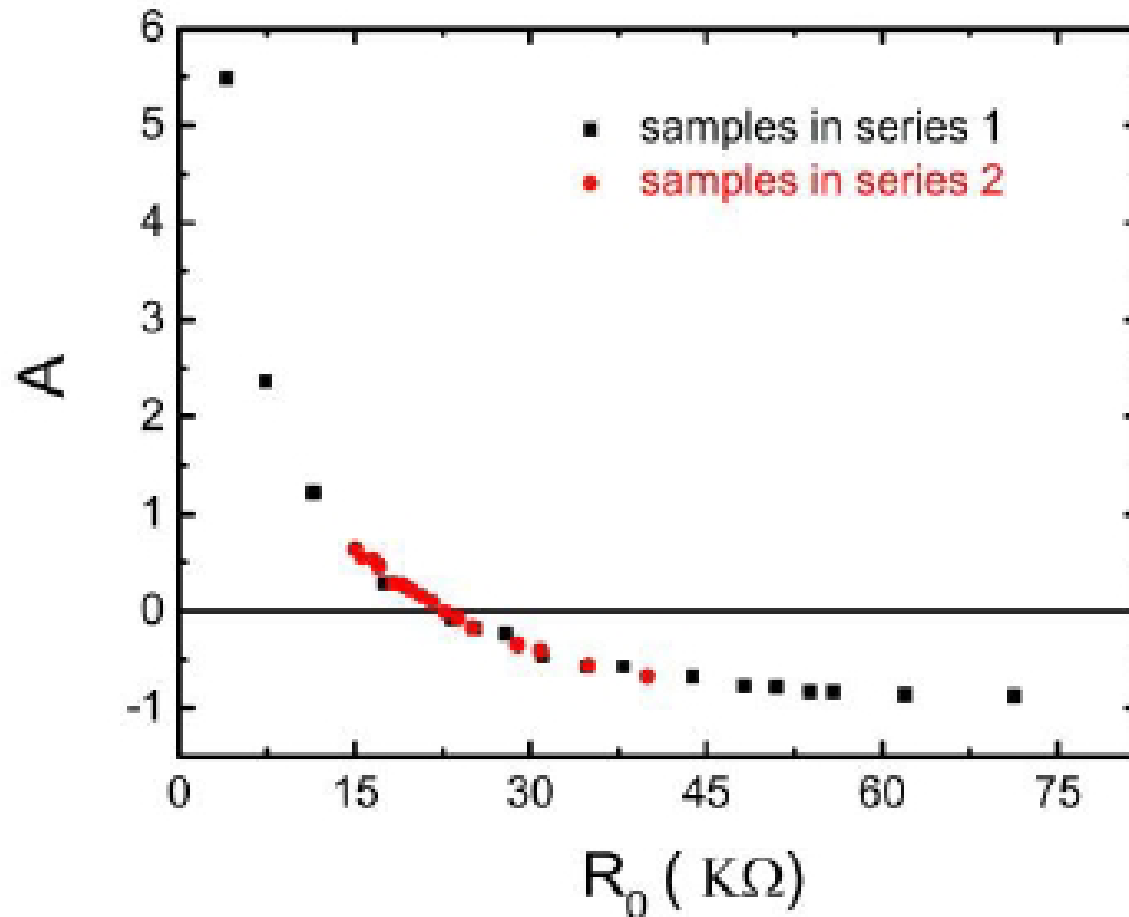


$$\sigma(T;R_0)/L_0 = A + B T^p$$

A, B, p  
allowed to  
vary with  
disorder

A changes sign !

# A as a function of disorder



Highly reproducible

Series 1:  
5 separate  
depositions;  
2 annealed  
12 times;  
Total 17 data

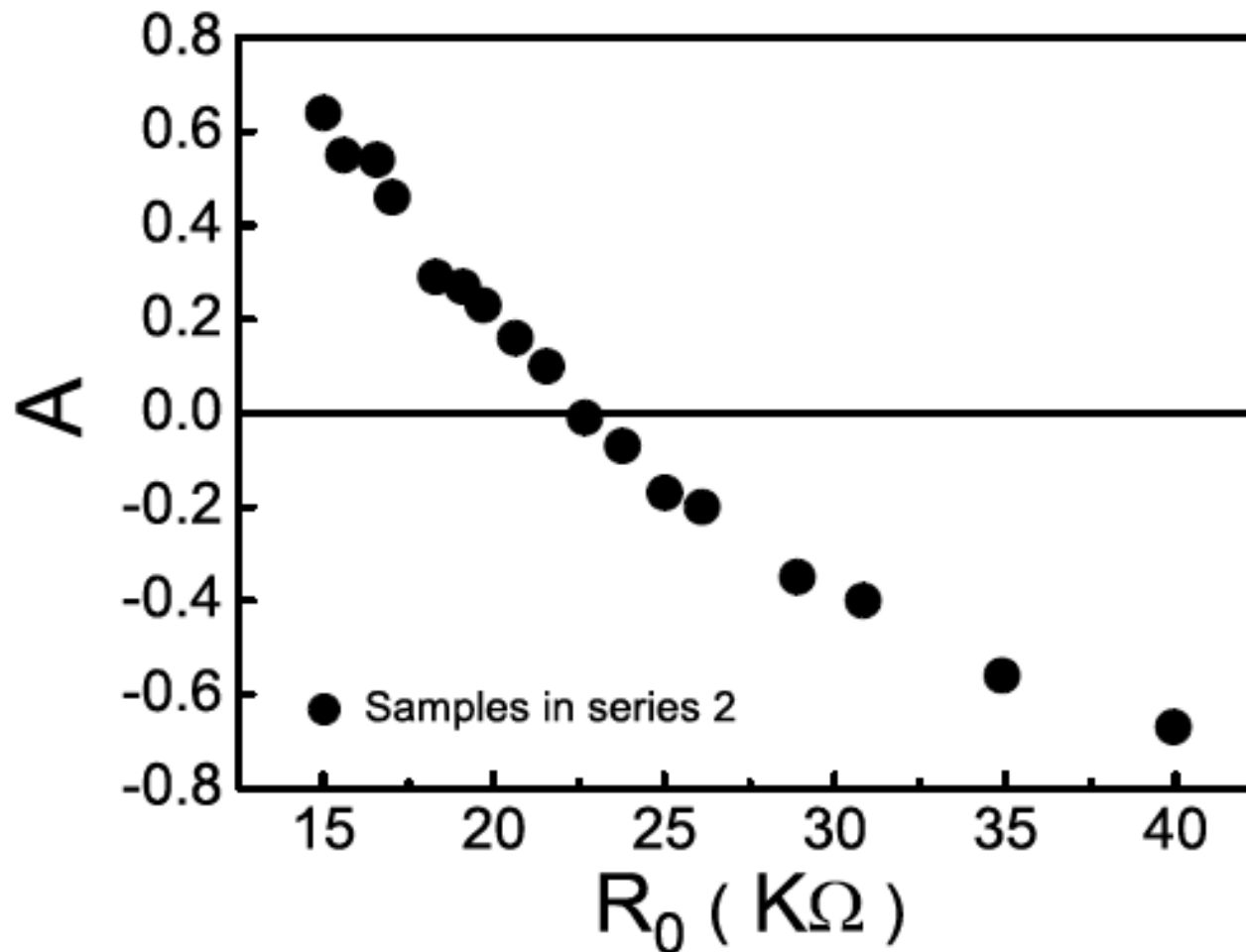
Series 2:  
single sample;  
annealed  
15 times;  
Total 16 data

# What does negative $A$ mean?

- Conductivity can not be negative. Negative  $A$  means the extrapolation to  $T=0$  must include opposite curvature, sign of an insulator.
- Exactly at the critical point, conductivity should follow a pure power law.

$A=0$  must be the critical point.

# Critical point: $A=0$

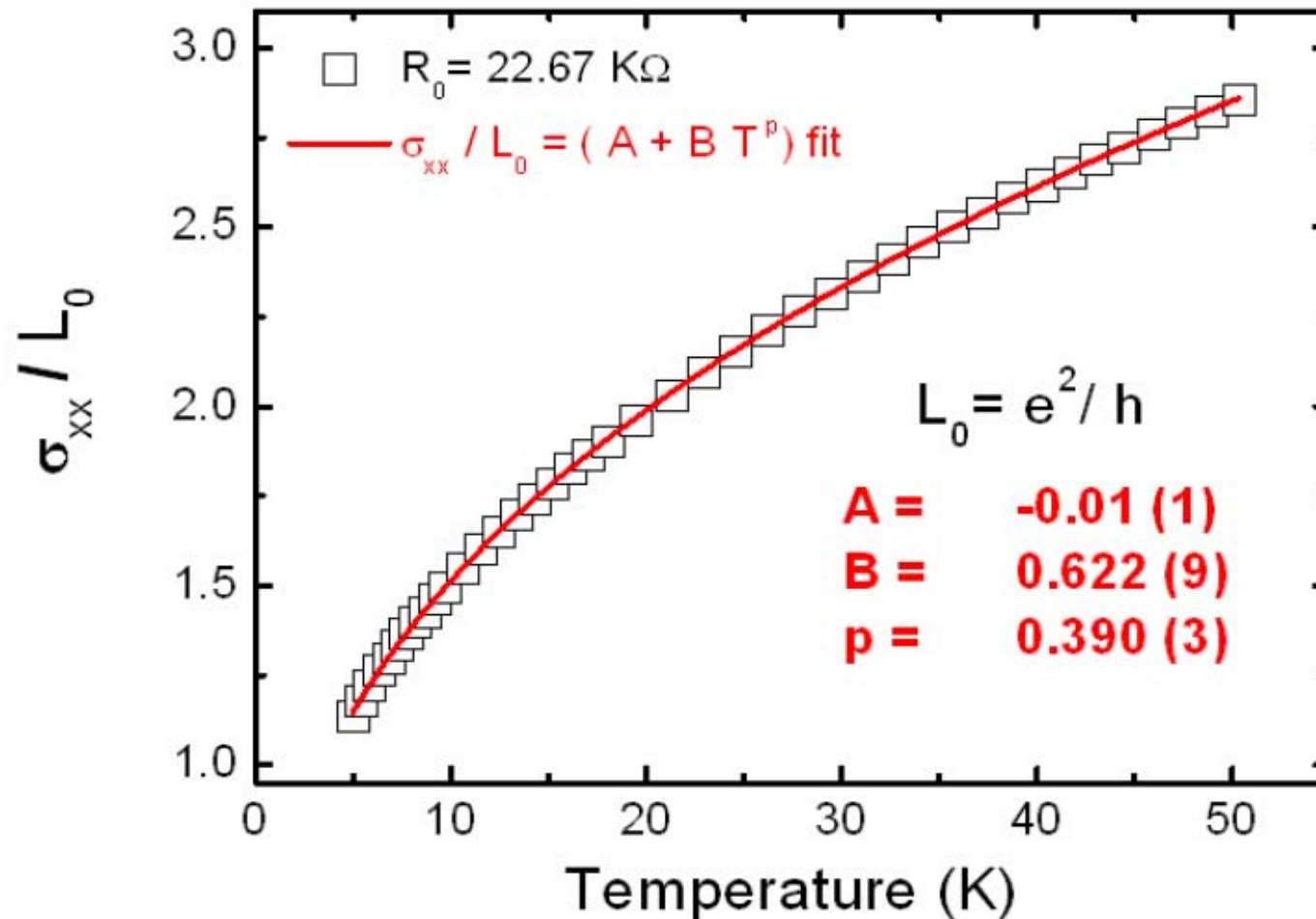


One data point with  $A \approx 0$  at  $R_0 \approx 22.67$  k $\Omega$

Precise determination of the critical point.

No extrapolation needed

# Critical point: pure power law



$$R_c \approx 22.67 \text{ k}\Omega; p \approx 0.39$$

# Critical exponents: definitions

$$\sigma(R_0) \sim |R_c - R_0|^s, \quad s: \text{conductivity exponent}$$

$$\sigma(\omega, R_c) \sim \omega^{1/z}, \quad z: \text{dynamical exponent}$$

$$\xi \sim |R_c - R_0|^{-\nu'}; \quad R_0 < R_c, \quad \nu': \text{correlation length exponent}$$

$$\xi \sim |R_c - R_0|^{-\nu}; \quad R_0 > R_c, \quad \nu: \text{localization length exponent}$$

$\nu$  and  $\nu'$  can be different

# Exponents: theoretical expectations

Non Linear Sigma Model (epsilon expansion):

$$s = \nu^{-1} = 1; \quad z = 3 \quad \text{in 3d} \quad \text{Wegner}$$

Numerical simulations (Anderson model):

$$s = 1.6 \quad \text{Slevin and Ohtsuki}$$

Interacting systems: No reliable theoretical way

No statement on asymmetric exponents

# Exponents: experiments on non-magnetic systems

$s = 0.5$ , **Si:P** (uniaxial stress) Paanalen et al '82

$s = 1$ , **Ge:Sb** (doping) Field et al '85, Hirsch et al '88  
Thomas et al '82, Zabrodskii et al '84

$\nu' = \nu = 1.6$  and  $z = 2$ , **Si:B** (uniaxial stress)  
Bogdanovich et al '99

$\nu' = \nu = 1$  and  $z = 2.94$ , **Si:P** (uniaxial stress)  
Waffenschmidt et al '99

$s = \nu' = \nu$ : same exponent on both sides

Note: expts at 3 – 700 mK, emphasizing  $T \rightarrow 0$



# Finite T: scaling relation

For  $\omega > \omega_\xi \sim (\xi/\ell)^{-z}$  :

$$\begin{aligned}\sigma(R_0; \omega) &= \xi^{-1} G(\xi^{1/\nu} |R_c - R_0|; \xi^z \omega) \\ &= \xi^{-1} G(\pm 1; \xi \omega^{1/z})\end{aligned}$$

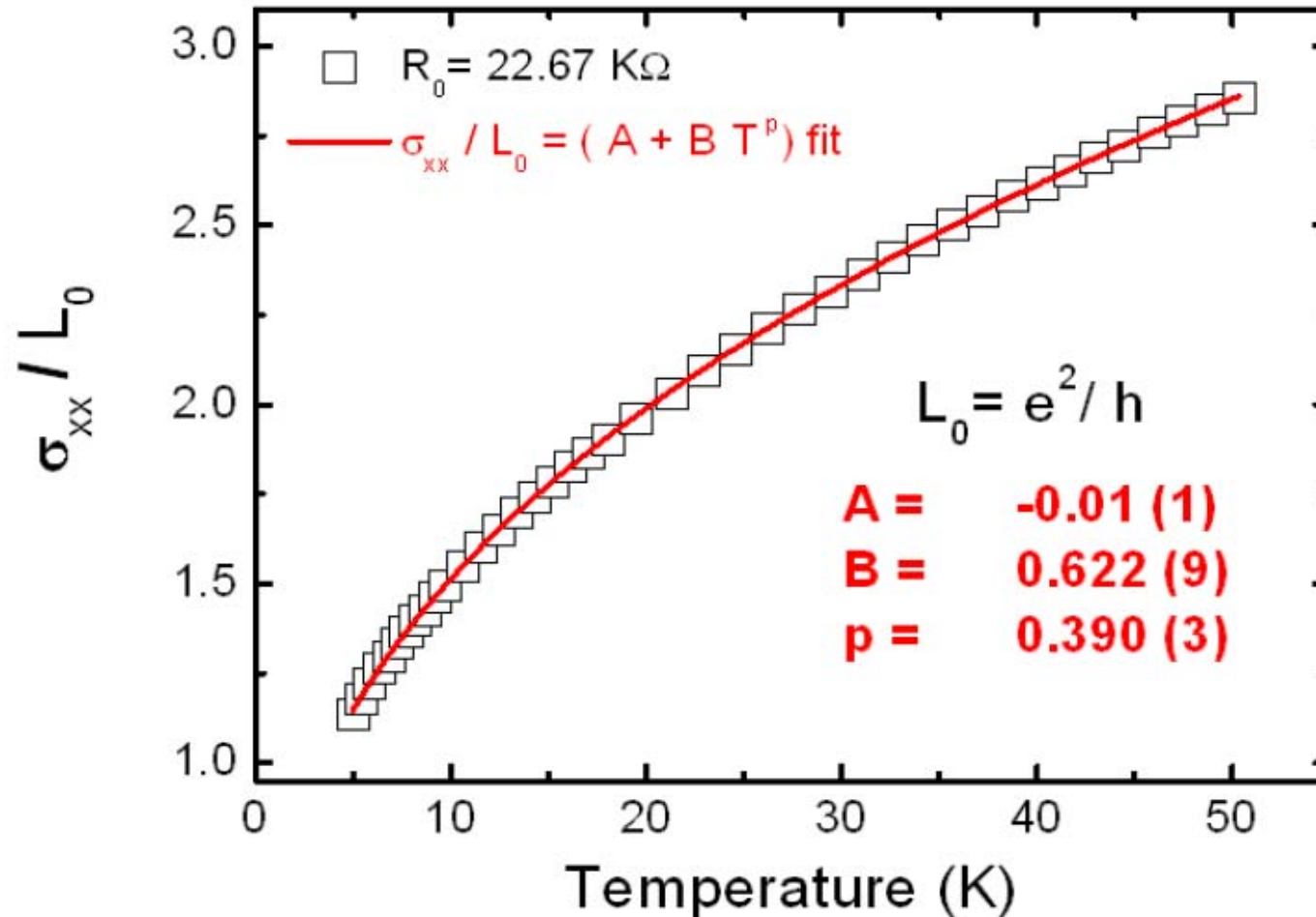
At critical point:  $G(\pm 1; \xi \omega^{1/z}) \sim \xi \omega^{1/z}$

For  $\xi \sim |R_c - R_0|^{-\nu}$  and  $\omega \rightarrow T$   
conductivity should obey the scaling at  $T > T_\xi$  :

$$|R_c - R_0|^{-\nu} \sigma(T; R_0) = G(+/-1; |R_c - R_0|^{-\nu} T^{1/z})$$

Compare: expts at 3 – 700 mK, emphasizing  $T \rightarrow 0$

# Critical point: dynamical exponent



$$\sigma(T, R_c) \sim T^{1/z} \quad \square \quad p = 0.39 = 1/z$$

# Scaling function G

Scaling regime:

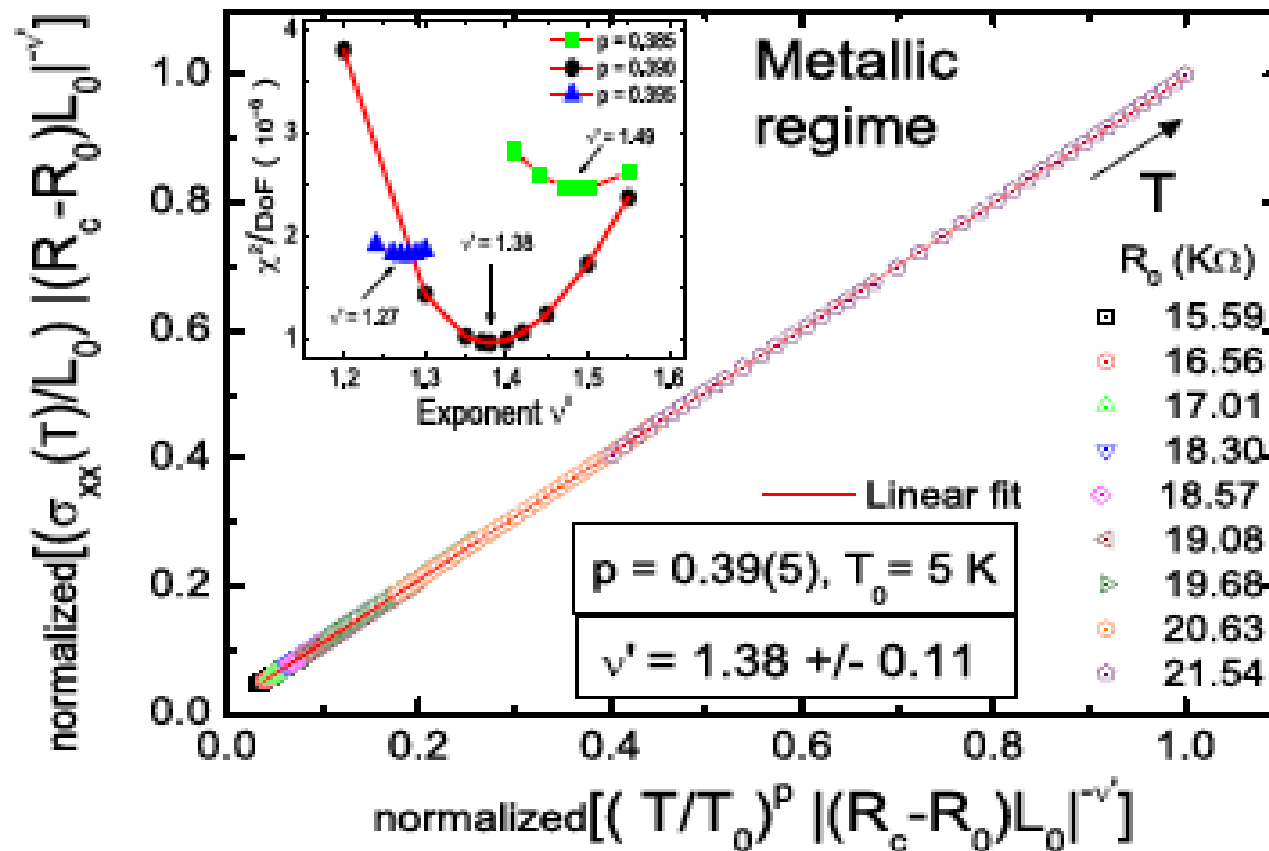
$$|R_0 - R_c|^{-\nu} \sigma(T; R_0) = G(\pm 1; |R_0 - R_c|^{-\nu} T^{1/z})$$

Use  $1/z = p = 0.39$

Plot  $|R_0 - R_c|^{-\nu} \sigma(T; R_0)$  as a function of  $|R_0 - R_c|^{-\nu} T^{1/z}$

All data should collapse on a single scaling function G for one particular value of

# Scaling of the data: metallic side

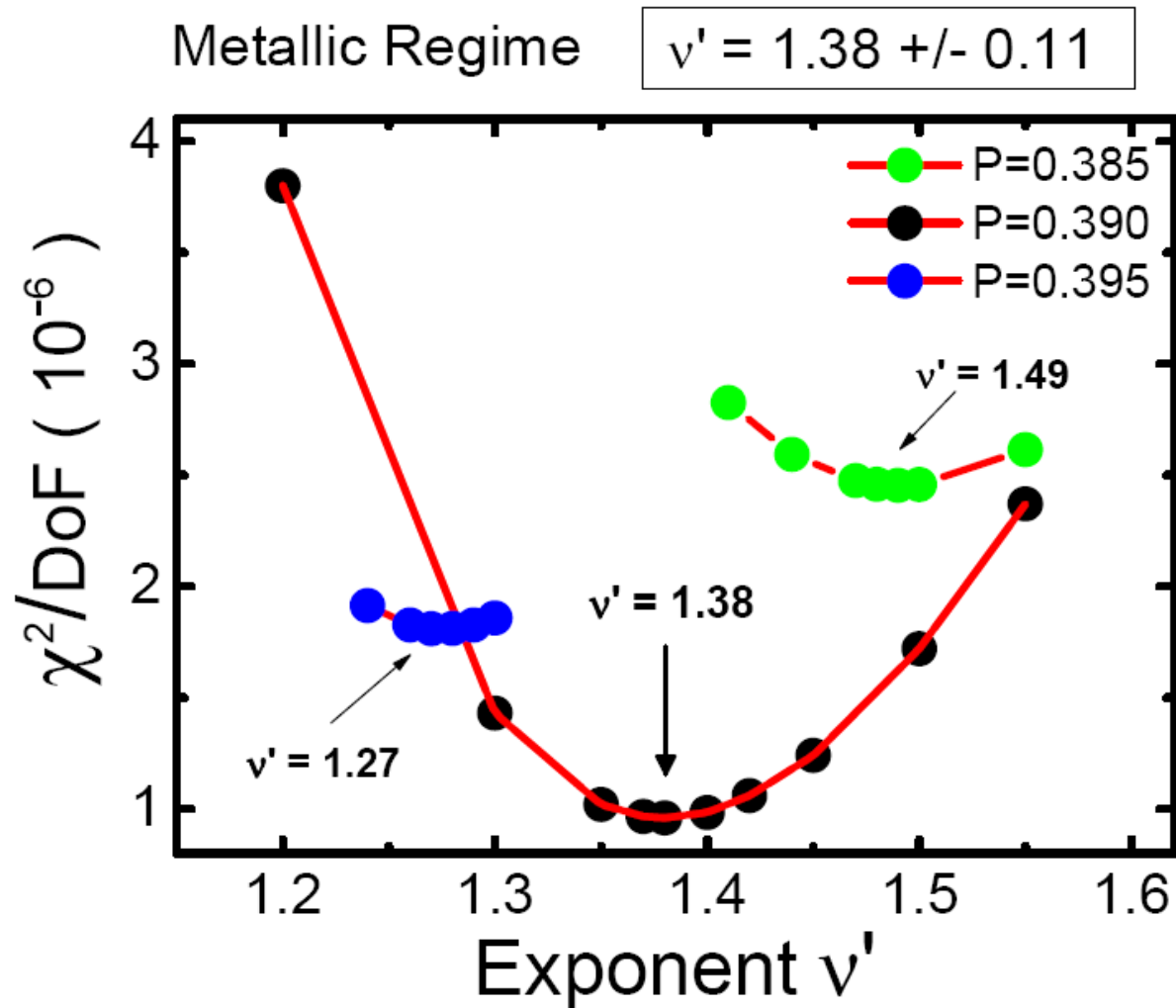


scaling points  
include  
41 values of T  
for each of the  
9 values of  $R_0$

Total 369  
data points

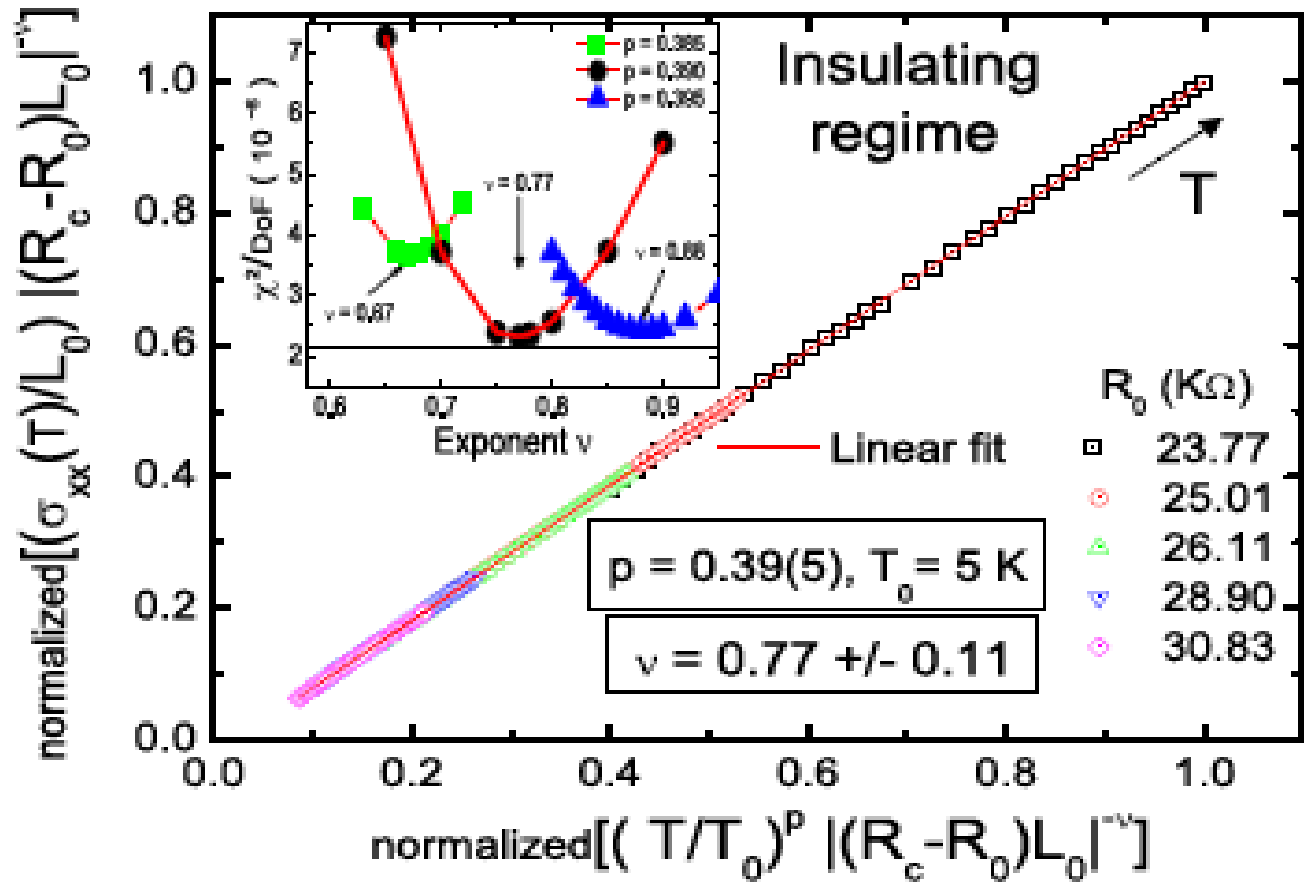
Correlation length exponent  $\nu' \approx 1.38$

# $\chi^2$ fit allowing uncertainty in $p$



Observed  $p = 0.39$  gives the best fit

# Scaling of the data: insulating side

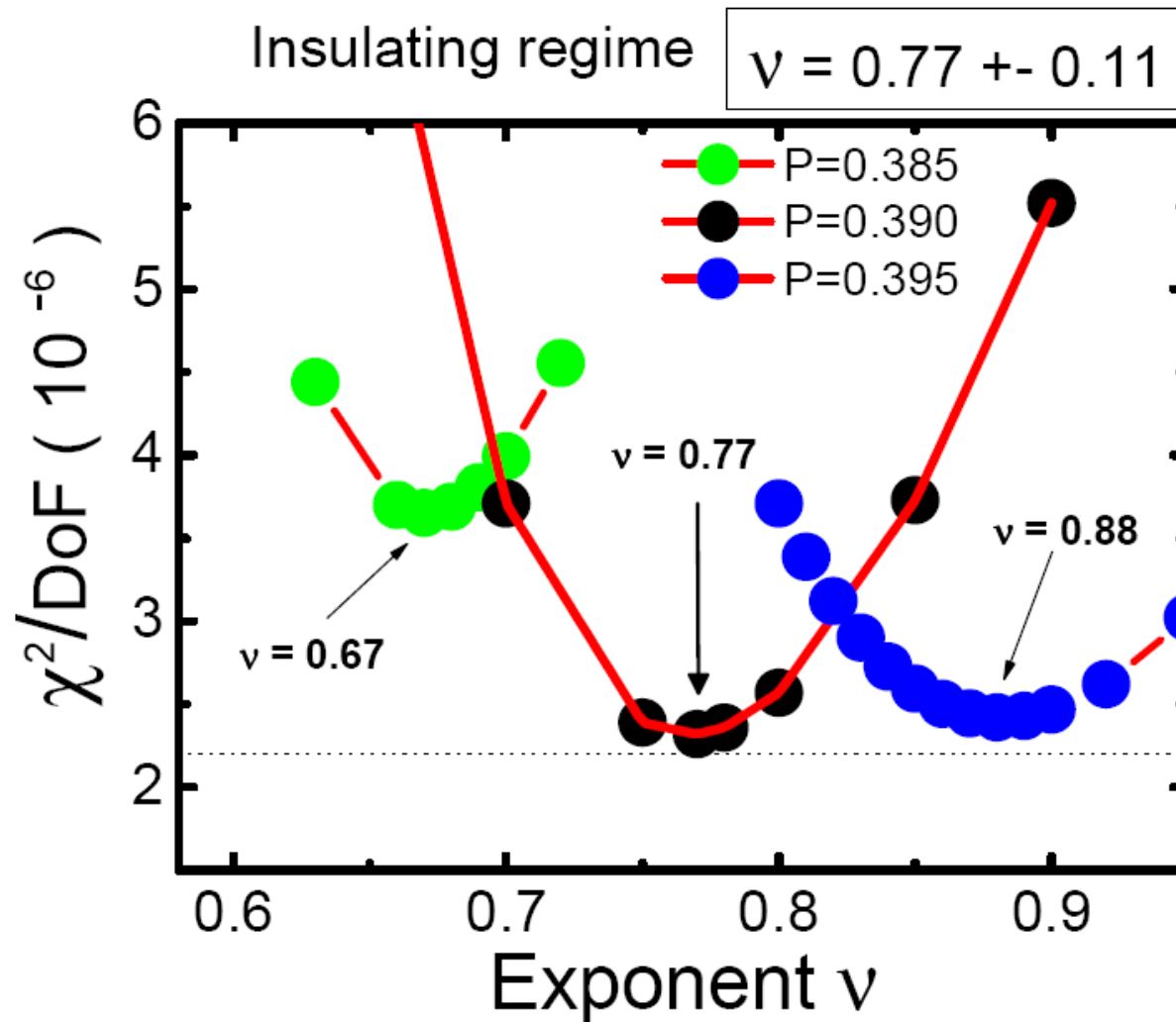


scaling points include 41 values of T for each of the 5 values of  $R_0$

Total 205 data points

localization length exponent  $\nu \approx 0.77$

# $\chi^2$ fit allowing uncertainty in $p$



Observed  $p = 0.39$  gives the best fit

# Critical region

Experimentally: Minimum in  $\chi^2$  fit for data  
restricted to 15 – 31 k $\Omega$

Theoretical estimate:

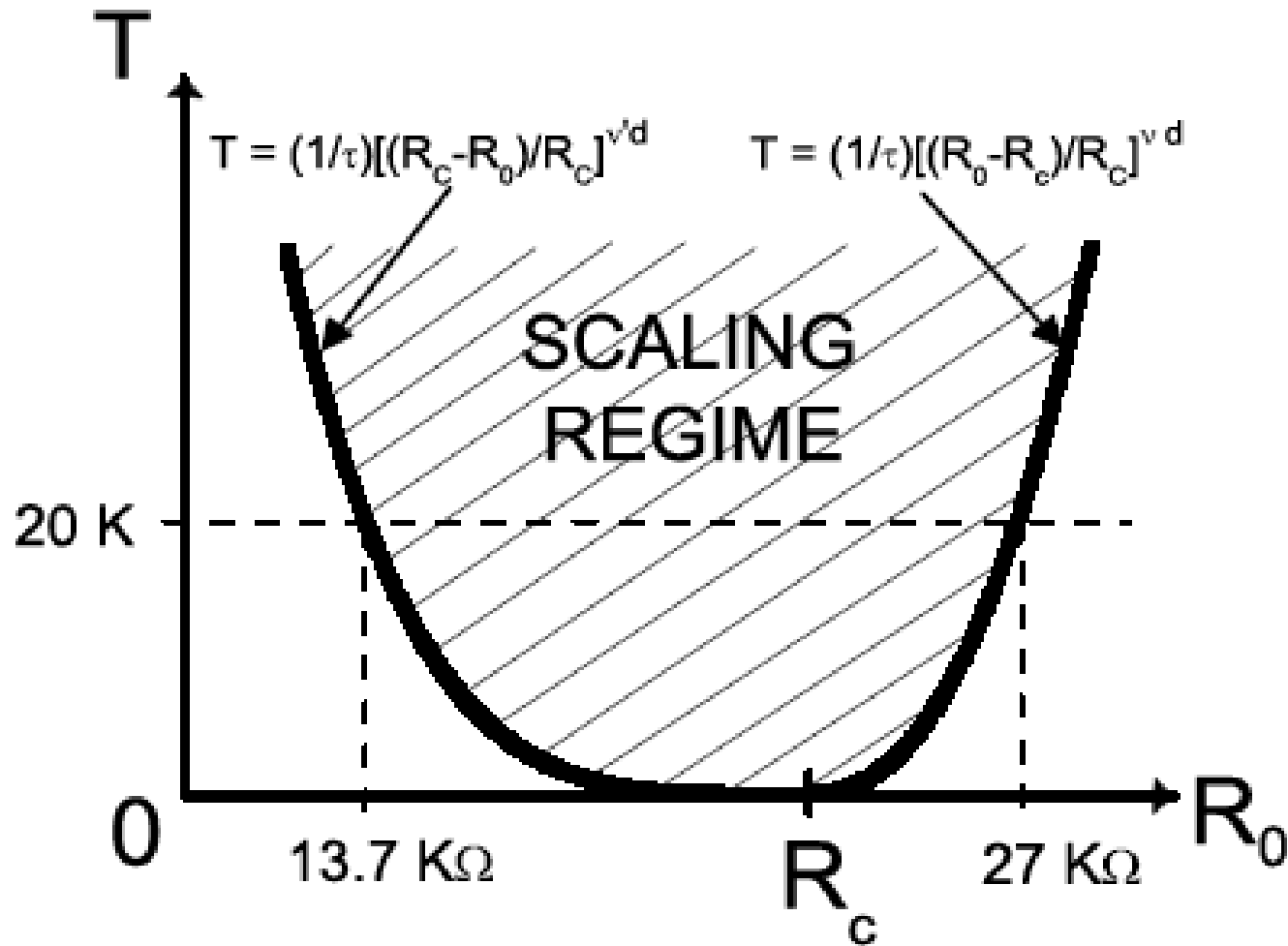
$$T_\xi \sim (\xi/\ell)^{-z}/\tau \sim (|R_0 - R_c|/R_c)^{\nu z}/\tau ;$$
$$1/\tau \sim 10^3 \text{ K} ; \quad T = T_\xi = 20 \text{ K}$$

→  $|R_0 - R_c|/R_c \sim 0.4$  : metallic side and  
 $|R_0 - R_c|/R_c \sim 0.2$  : insulating side.

Critical region extends from  $\sim 15 - 30$  k $\Omega$  at 20K



# Estimate of critical region



Large  $T$  better!

## 3d vs 2d

Film thickness: 20 – 35 Å

Effectively 3d if T-dependent correlation length

$$L_{\varphi}(T) \equiv \sqrt{\sigma \tau_{\varphi}/N_0} < \text{film thickness}$$

Phase relaxation rate in ferromagnetic films dominated by scattering off spin waves:

$$\tau_{\varphi}^{-1} \sim T \quad \text{Wölfle and KAM '10}$$

Inequality satisfied if  $T \sim 1\text{K}$  or larger

# Summary

- **Distinctly different exponents** for correlation lengths on two sides of the M-I transition in ferromagnetic Gd films.
- Unambiguous Identification of critical point and wide critical regime results in excellent scaling.
- **Magnetism** seems important. Thin film geometry might also be relevant.
- Scaling function  $G$  seems **linear**.

**No theoretical model available**