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2146-29

**Gribov-80 Memorial Workshop on Quantum Chromodynamics and
Beyond'**

26 - 28 May 2010

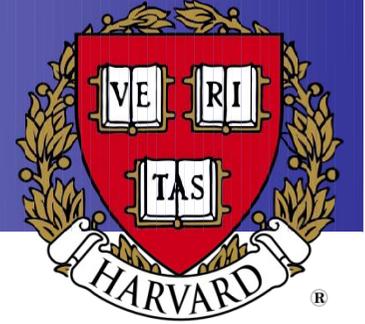
**U_A(1) symmetry restoration and in-medium eta' mass modification in $\sqrt{s_{NN}} =$
200 GeV Au+Au collisions at RHIC**

Tamas Csorgo

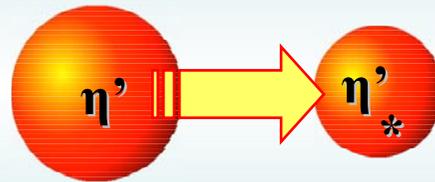
*MTA KFKI Research Institute for Particle and Nuclear Physics
Hungary*



Gribov – 80 Memorial Workshop on QCD and beyond



$U_A(1)$ symmetry restoration and
in-medium η' mass reduction
in $\sqrt{s_N} = 200$ GeV Au+Au collisions



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[arXiv:0905.2803 \[nucl-th\]](https://arxiv.org/abs/0905.2803)

[arXiv:0912.0258 \[nucl-ex\]](https://arxiv.org/abs/0912.0258)

[arXiv:0912.5526 \[nucl-ex\]](https://arxiv.org/abs/0912.5526)

Trieste, Italy, 5/28/2010

Outline

- Three-quark model, Chiral symmetry breaking
 - Restoration of symmetry in a hot, dense medium
- Role of the η' mass
 - Dilepton spectra in Heavy Ion Collisions
 - η' mass through π^\pm Bose-Einstein correlations
- Possible experimental signatures
 - BEC measurements at RHIC
 - Dilepton excess found by PHENIX
- BEC-calculations for different models
 - Spectra, $\lambda^*(m_T)$, systematics...

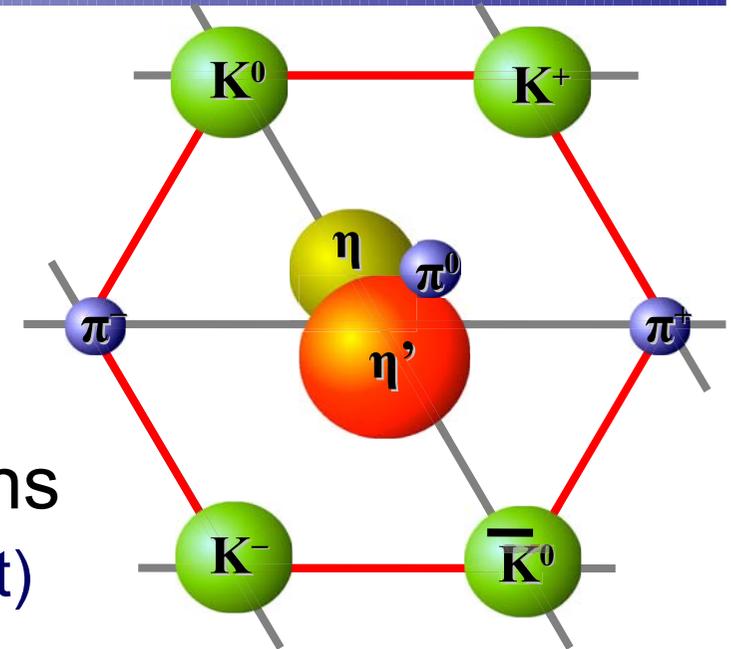
Chiral Symmetry Breaking

- The three-quark model

- SU(3) flavour-symmetry
- Spontaneously broken

⇒ 9 Goldstone bosons

- Corresponding to light mesons
 - There are only 8! (Meson-octet)

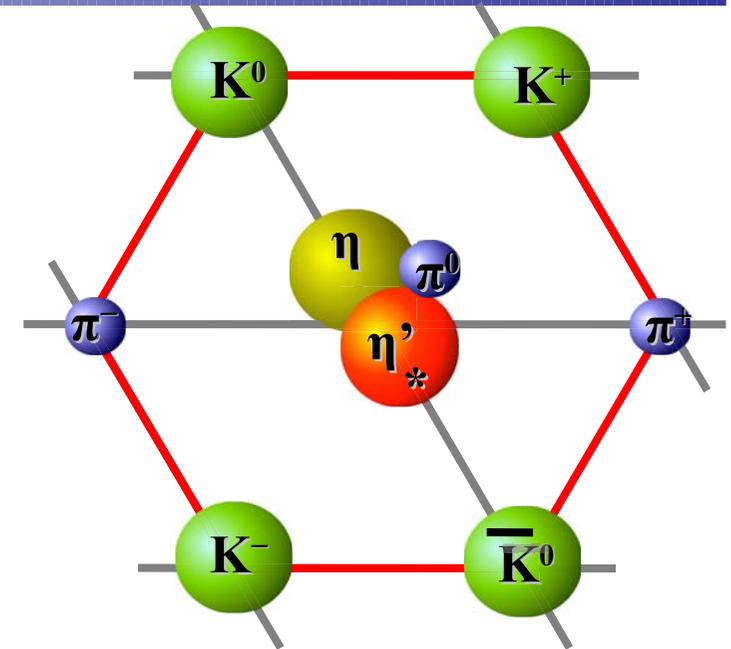


- $U_A(1)$ chiral symmetry explicitly broken

- Distinct topological vacuum-states
- Tunneling b/w them – quasiparticles (instantons)
- 9th boson gains mass – η' (958 MeV)

Restoration of the Symmetry in a Hot, Dense Medium

- High energy densities
 - Asymptotic freedom $\alpha_s \rightarrow 0$
 - Nontrivial topology vanishes
 - U(1) no more broken
 - SU(3) restored



Remark:

From SSB, One expects massless mesons.
However, the flavour symmetry is inexact.

$$m_{\eta'} = m_0 + \Delta m$$

Mass reduction

Lower bound (Gell-Mann - Okubo):

$$m_0^2 = \frac{1}{3} (2m_K^2 + m_\pi^2); m_0 \approx 400 \text{ MeV}$$

Upper bound (S, NS isosinglet eigenstates): $m_S^2 = 2m_K^2 + m_\pi^2; m_S \approx 700 \text{ MeV}$

Δm is the extra mass from instantons in a not-so-dense medium

Signature: Particle Abundancy

- Hagedorn-model

- Production of light mesons:

$$\sigma_i \sim \left(m / 2\pi\right)^{3/2} e^{-m/T_H} \quad T_H \sim 170 \text{ MeV Hagedorn-temperature}$$

- In case of a possible mass drop:

- Number of normal η' -s is small: $N_{\eta'} / N_{\pi^0} \sim 2 \times 10^{-2}$
- With a strongly reduced η' mass: $N_{\eta'} / N_{\pi^0} \sim 1$
 - An enhancement of a factor of 50 at maximum

- Consequence of the reduced mass:

An increased abundancy of η' mesons

The η' through Phase Transition

- Hadronization
 - Reduced-mass η' mesons produced with a decreased mass with an increased abundancy
- Decoupling from non-Goldstonic matter
 - Mean free path for annihilation is large
 - Long lived
- "Condensate" in the medium
 - Low- p_T η' mesons are unable to get on-shell in the vacuum
 - Medium acts as a trap for low- p_T η' 's
- As medium dissolves, the η' 's regain their original mass

The Return of the prodigal Goldstone boson: J. I. Kapusta, D. Kharzeev, L. D. McLerran Phys.Rev.D53:5028-5033,1996, hep-ph/9507343

Channels of Observation

- **Leptonic decay** $\eta' \rightarrow \ell^+ \ell^- \gamma$
 - Increased η'/π proportion in the low- p_T range
 - Excess in the $\ell^+\ell^-$ spectrum under the ρ mass
- **η meson (BR=63%)** $\eta' \rightarrow \eta \pi \pi$
 - Enhancement of η production
 - BEC of charged pions $\eta \rightarrow \pi^0 \pi^+ \pi^-$
 - Sensitive to the sources of the pions
- **Direct measurement?** $\eta' \rightarrow \gamma\gamma$
 - Would be convincing, however, poor S/B ratio ($\pi^0 \rightarrow \gamma\gamma$)

Dilepton Excess in CERES

VOLUME 75, NUMBER 7

PHYSICAL REVIEW

- Measurement
- Model calculations
- Excess
in the range b/w the π and ρ mass

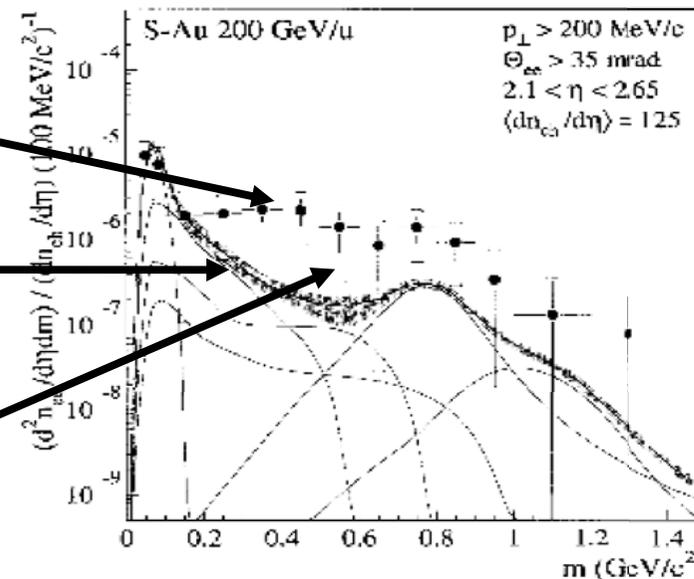


FIG. 4. Inclusive e^+e^- mass spectra in 200 GeV/nucleon S-Au collisions. For explanations see Fig. 2.

Invariant e^+e^- pair yield measurements compared to hadronic model yields

e^+e^- pair production in Pb - Au collisions at 158-GeV per nucleon.

CERES cn. (G. Agakichiev et al.). Jun 2005. 39pp.

Eur.Phys.J.C41:475-513,2005. e-Print: nucl-ex/0506002

Present understanding: broadening of the rho peak

2nd Channel: HBT effect (BEC)

- Discovered and still used in astrophysics

- Consider two plain waves: $\Psi_1 = e^{-ik_1 x_1}$
 $\Psi_2 = e^{-ik_2 x_2}$

- Bosons: symmetrization needed

$$\Psi_{1,2} = \frac{1}{\sqrt{2}} (e^{-ik_1 x_1} e^{-ik_2 x_2} + e^{-ik_1 x_2} e^{-ik_2 x_1})$$

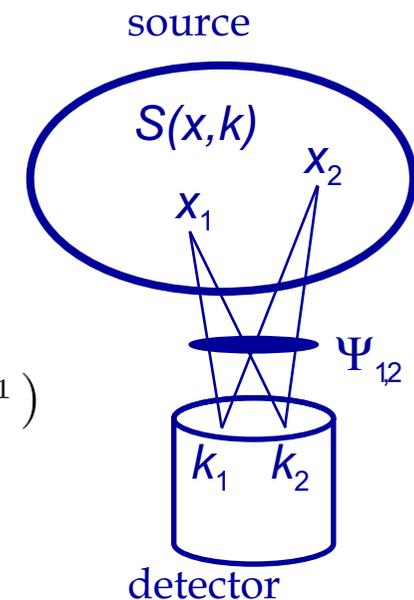
- Spectra: $N_1(k_1) = \int S(x_1, k_1) |\Psi_1|^2 dx_1$

$$N_2(k_1, k_2) = \int S(x_1, k_1) S(x_2, k_2) |\Psi_{1,2}|^2 dx_1 dx_2$$

- Correlation:

$$C(k, \Delta K) = \frac{N_2(k_1, k_2)}{N_1(k_1) N_2(k_2)} \quad \Delta K = k_1 - k_2$$

$$k = (k_1 + k_2) / 2$$



Simplified picture: plain wave, no multiparticle-interactions, thermalization etc.

$\pi^\pm \pi^\pm$ Correlations and the Core-Halo picture

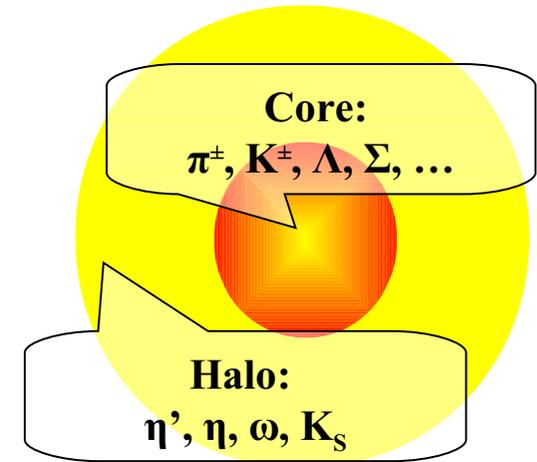
- Pions from freezeout

Primordial (from hot fireball)

Short lived resonances

Long-lived resonances ($\omega, \eta, \eta', K_S^0$)

} **Core**
→ **Halo**



- Correlation

$$C(\Delta k, K) \simeq 1 + \lambda_* R_c(\Delta k, K) \quad R_c(\Delta k, K) = \frac{|\tilde{S}_c(\Delta k, K)|^2}{|\tilde{S}_c(\Delta k = 0, K = p)|^2}$$

- Intercept $\lambda_*(m_t) = \left[\frac{N_{core}^{\pi^+}(m_t)}{N_{core}^{\pi^+}(m_t) + N_{halo}^{\pi^+}(m_t)} \right]^2$

$$N_{halo}^{\pi^+} = N_{\omega \rightarrow \pi^+} + N_{\eta \rightarrow \pi^+} + N_{\eta' \rightarrow \pi^+} + N_{K_S^0 \rightarrow \pi^+}$$

$$N = C m_t^\alpha e^{-m_T/T_{eff}}, T_{eff} = T_{fo} + m \langle u_T \rangle^2$$

- Correlation measurent $\leftrightarrow \lambda^*(m_T) \leftrightarrow$ core-halo ratio

Simulating the Condensate

- Resonance ratios from different models

ALCOR, FRITIOF, Kaneta *et al.*, Letessier *et al.*, Stachel *et al.*, UrQMD.

- η' excess:

$$\frac{N_{\eta'}^*}{N_{\eta'}} = \left(\frac{m_{\eta'}^*}{m_{\eta'}} \right)^\alpha e^{-\left(\frac{m_{\eta'}^* - m_{\eta'}}{T_{FO}} \right)}$$

- Restored η' mass:

$$p_{T,\eta'}^2 + m_{\eta'}^2 = p_{T,\eta'}^{*2} + m_{\eta'}^{*2}$$

- If $p_{T,\eta'}^* < \sqrt{m_{\eta'}^{*2} - m_{\eta'}^2}$, the η' can't get onshell; trapped till dissolution

After trap decays, a MB distribution:

$$f(p_x, p_y) = \left(\frac{1}{2\pi m_{\eta'} B^{-1}} \right) \exp\left(-\frac{p_x^2 + p_y^2}{2m_{\eta'} B^{-1}} \right) ; \quad p_{T,\eta'}^2 = p_x^2 + p_y^2$$

- Parameters

- From measurements

$$T_{FO} = 177 \text{ MeV}, \quad \langle u_T \rangle = 0.48$$
- Conservative assumption

$$T_{FO}^{\eta'} = T_{FO} \quad T_{\text{cool}} = T_{FO}$$
- Hydrodynamical models

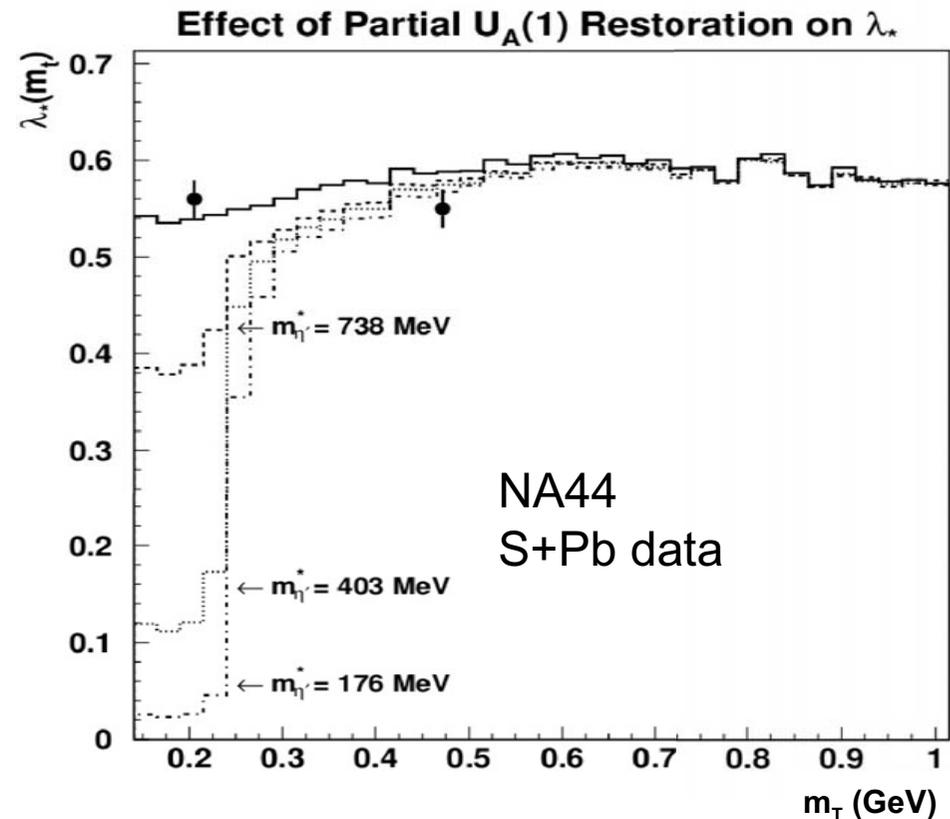
$$\alpha \text{ (related to the } d \text{ of expansion)}$$
- Looked for:

$$\text{in-medium mass } m_{\eta'}^* \quad \text{inverse slope } B^{-1}$$

- Spectra from decays using JETSET

SPS data and simulation: No signal

- Data:
NA44 200 GeV S+Pb
- Resonances:
FRITIOF
- Earlier, less refined
modelling of condensate
- No sign of mass reduction



Signal of partial $U(A)(1)$ symmetry restoration from two pion Bose-Einstein correlations
T. Cs., D. Kharzeev, S.E. Vance. e-Print: hep-ph/9910436

RHIC data

■ Properties

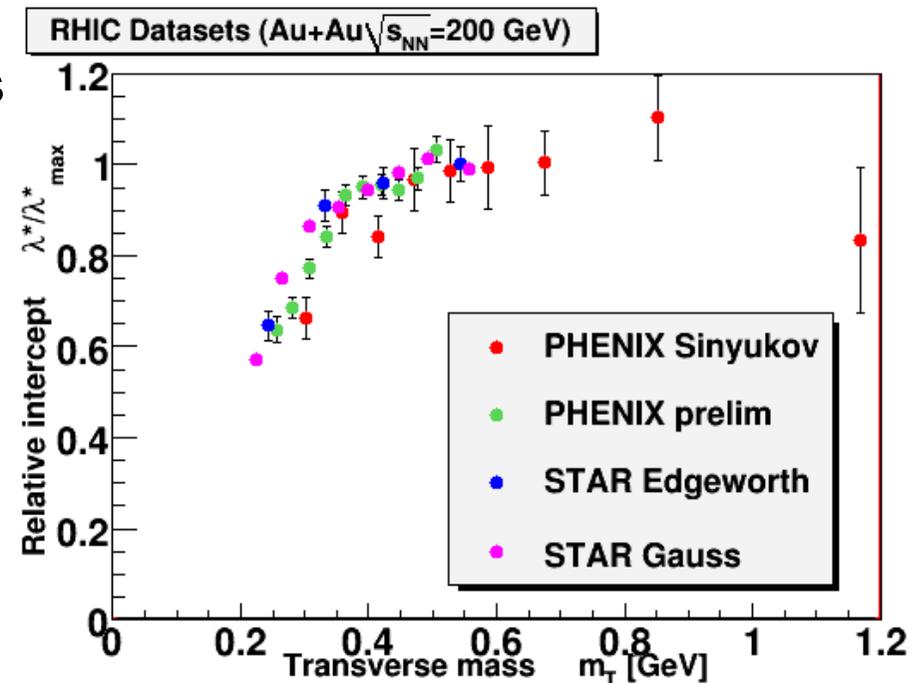
- Central Au+Au $s_{NN}^{1/2} = 200$ GeV
- Mid-rapidity $|\eta| < 0.1$
- $\pi^+\pi^+$ correlation measurements
- $\lambda^*(m_T)/\lambda^*_{\max}$
(different methods)

■ Data used in the analysis

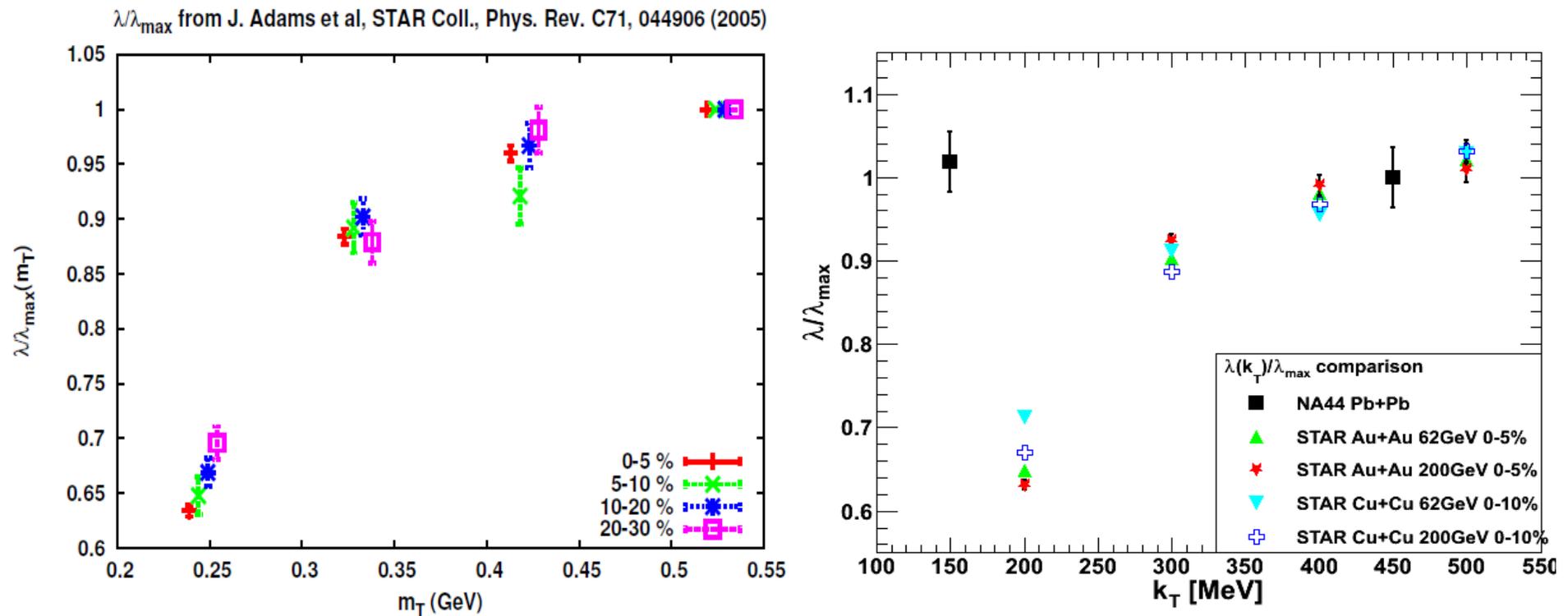
- **PHENIX** Sinyukov 50%
- **STAR** Edgeworth expansion
(6th order, only even)

■ Shown for comparison purposes

- PHENIX preliminary
- STAR Gauss

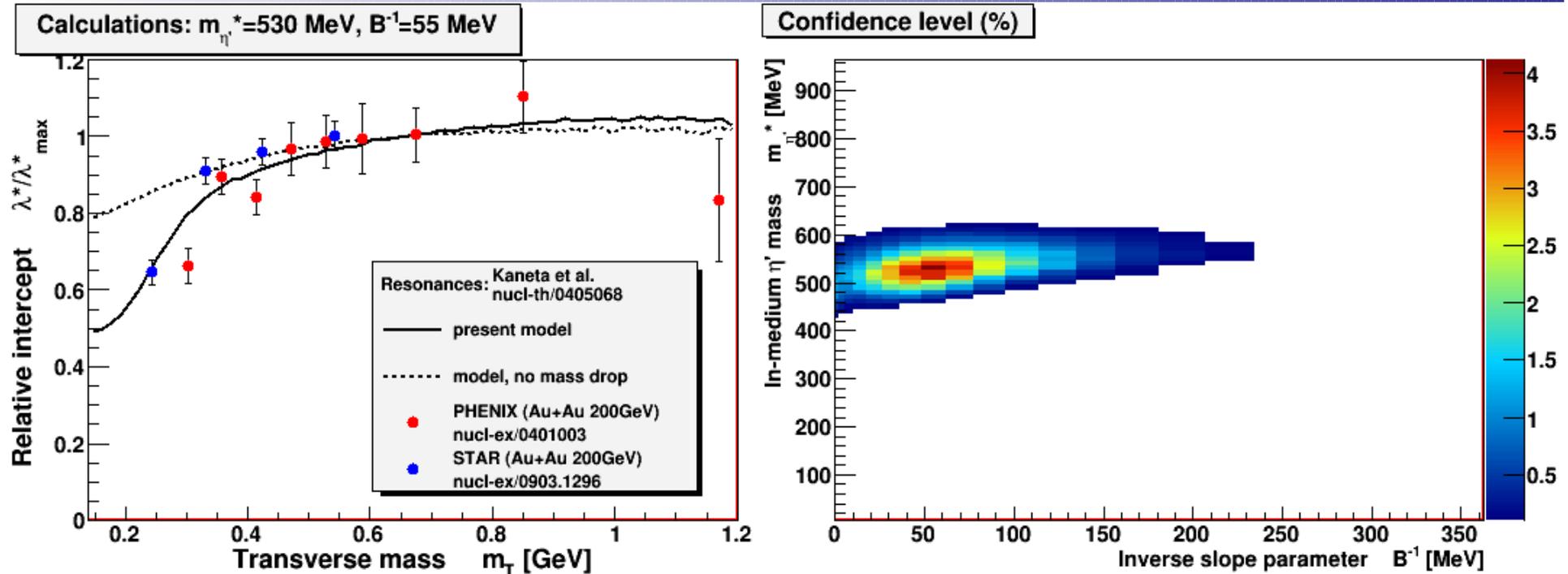


Centrality, energy and A dependence



STAR data: effect is present at all RHIC energies and centralities
Deeper hole: larger η' enhancement
Effect is slightly bigger for
more central reactions, bigger colliding nuclei, and larger energies

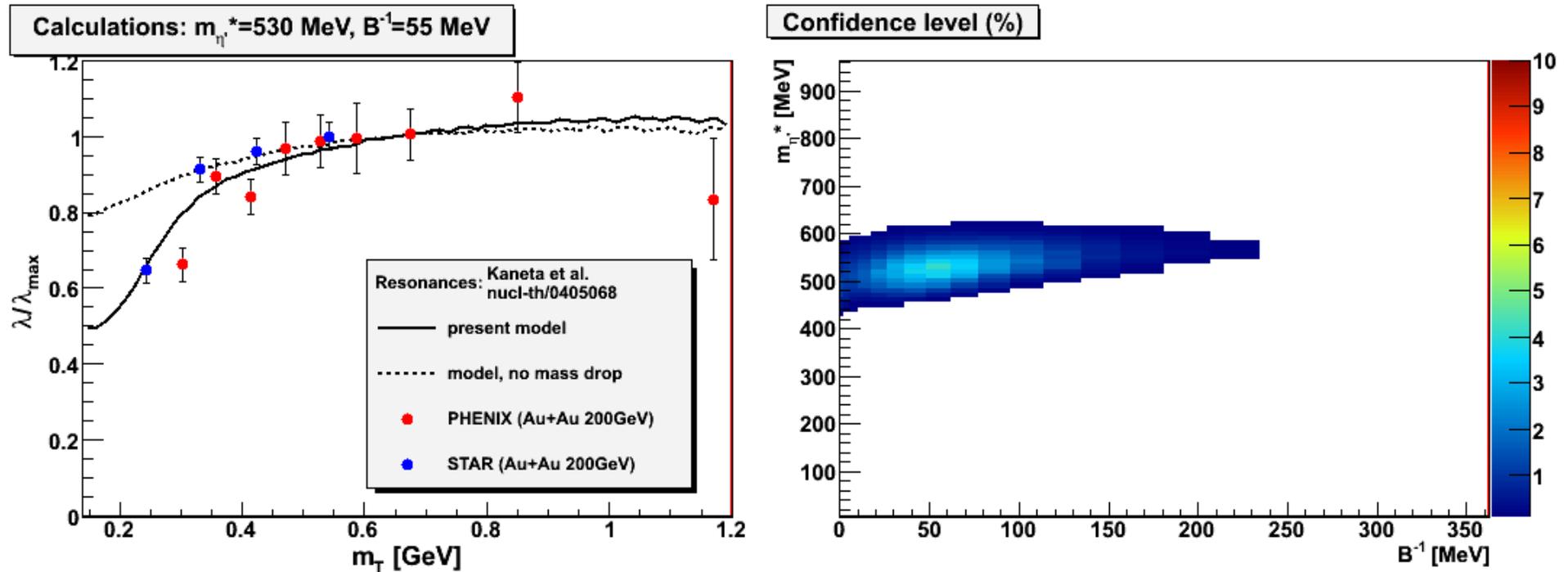
Finding the most likely mass



Simulations all over the $(B^{-1}, m_{\eta'}^*)$ plain

- Here: Resonance ratios of **Kaneta & Xu, arXiv:nucl-th/0405068**
- Mapping χ^2/NDF to confidence level
- Choose best $\lambda^*(m_T)/\lambda_{max}^*$ fit
 - By this model: $m_{\eta'}^* = 530$ MeV

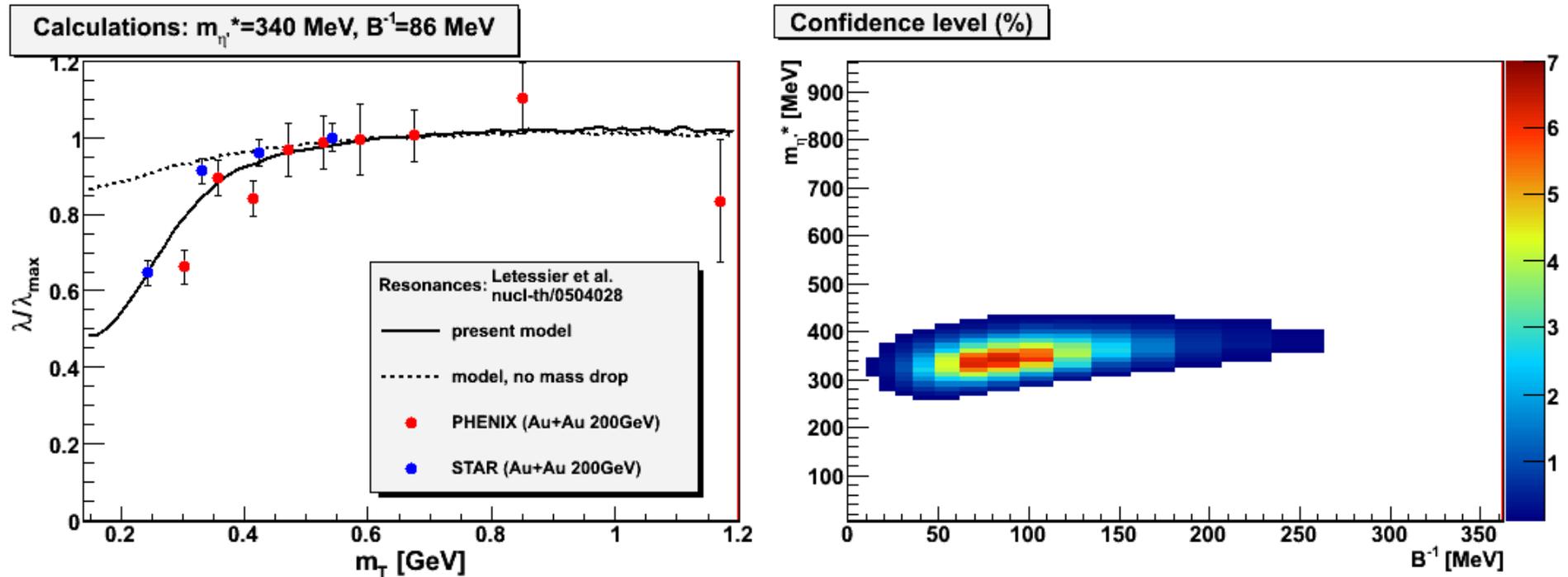
Resonances: Kaneta-Xu vs. RHIC



- Statistical chemical freezeout model
- Central mid- η 200 GeV Au+Au
- Describes PHENIX hadron spektrum well

Kaneta & Xu, arXiv:nucl-th/0405068

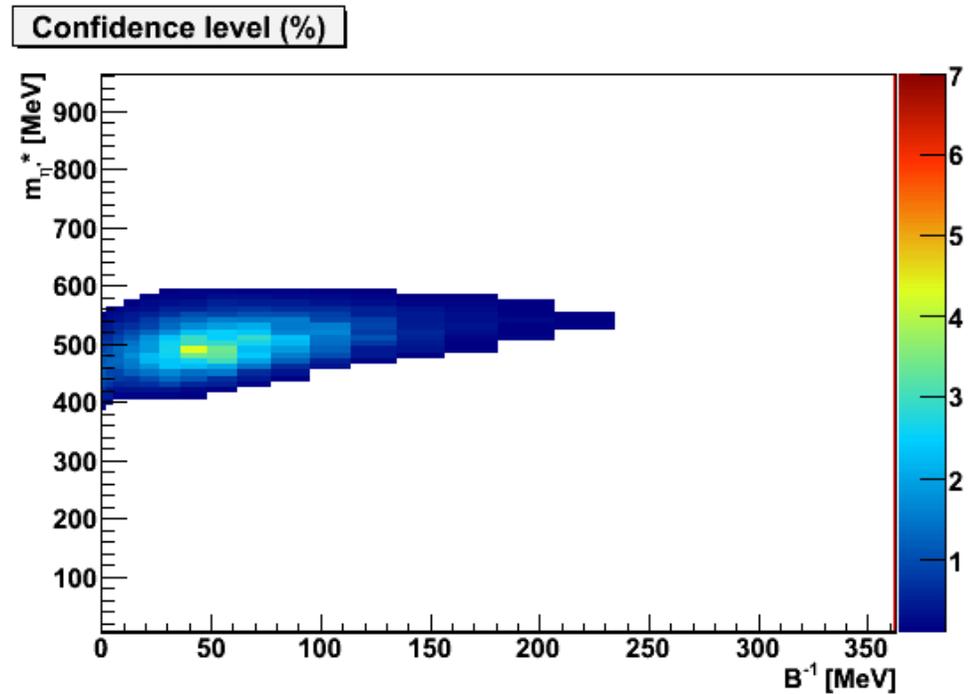
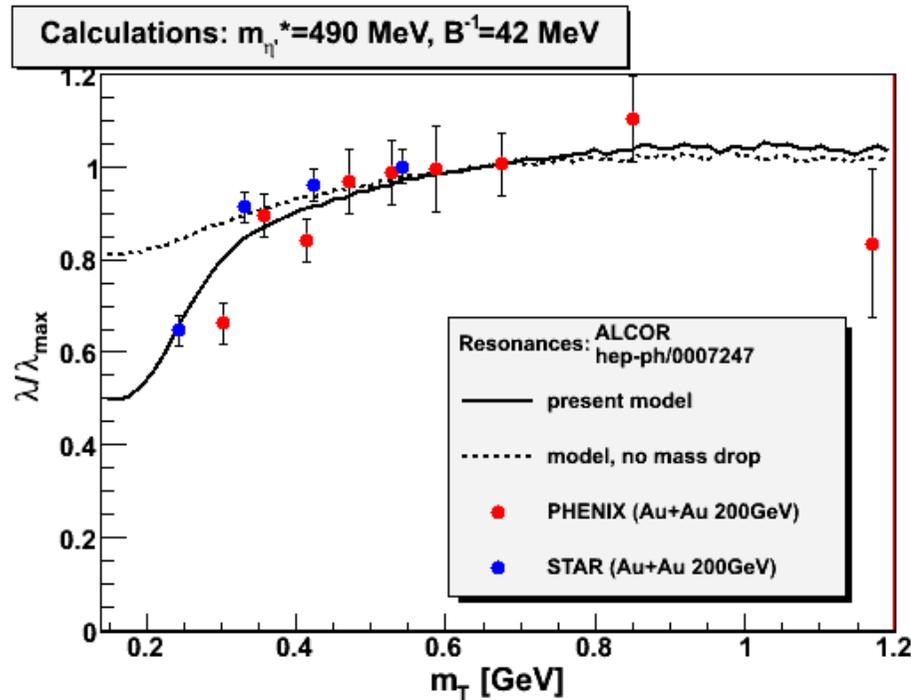
Resonances: Letessier-Rafelski vs. RHIC



- Statistical chemical freezeout model
- Central mid- η 200 GeV Au+Au

J.Letessier J.Rafelski, arXiv:nucl-th/0504028

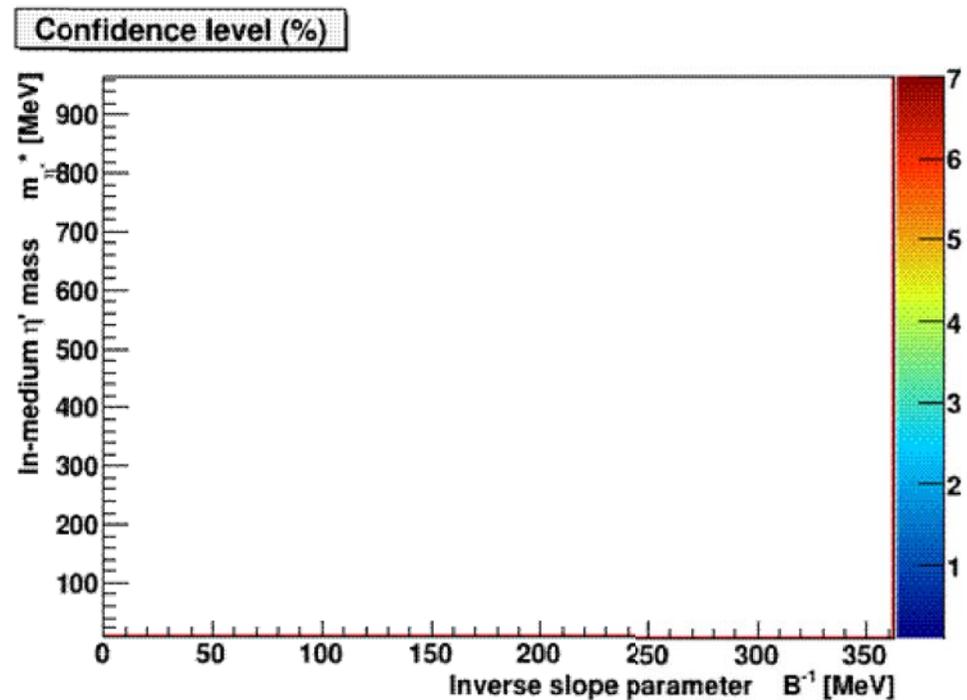
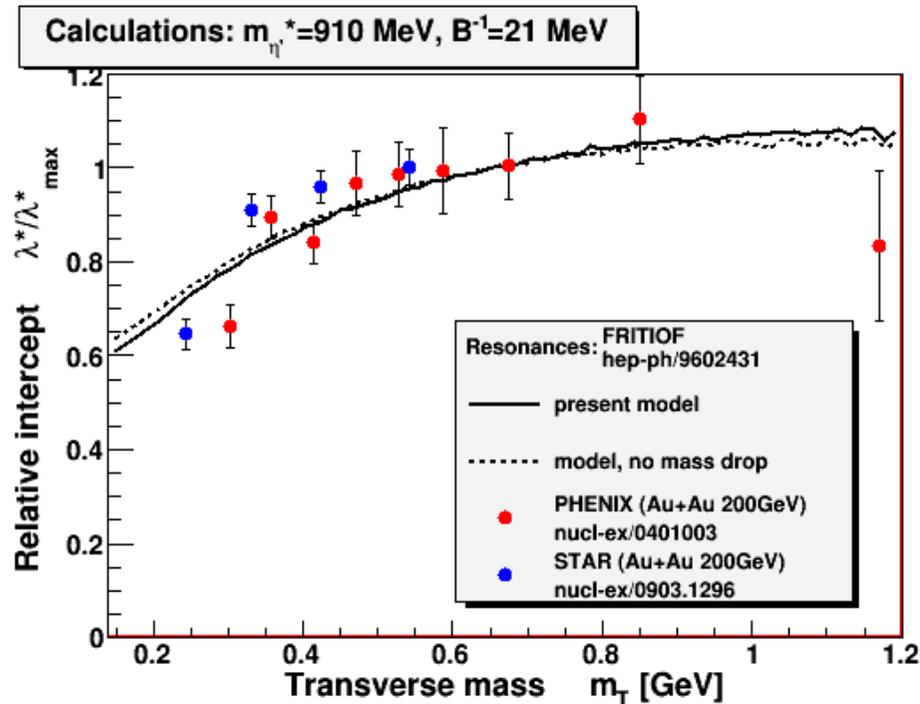
Resonances: ALCOR vs. RHIC



- Coalescence-model
- η'/η ratio has to be fixed from other models (Kaneta, here)

P. Levai, T.S. Biro, T. Csorgo, J. Zimanyi, hep-ph/0007247

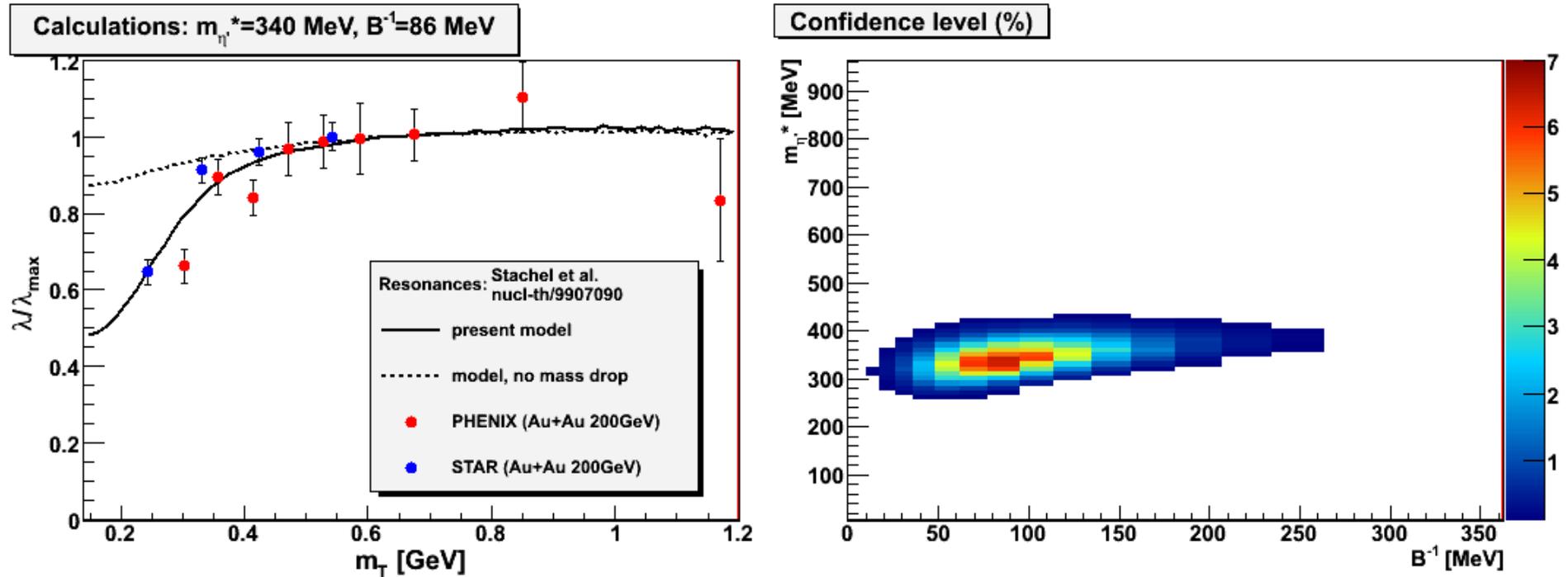
Resonances: FRITIOF vs. RHIC



- 200 GeV mid-rapidity Au+Au simulation
- Note: Does not describe STAR data, neither the unified PHENIX+STAR dataset. For PHENIX data only, it is consistent with $m_{\eta^*} = 958$ MeV.

B. Anderson et al., Nucl. Phys. B 281 (1987) 289.

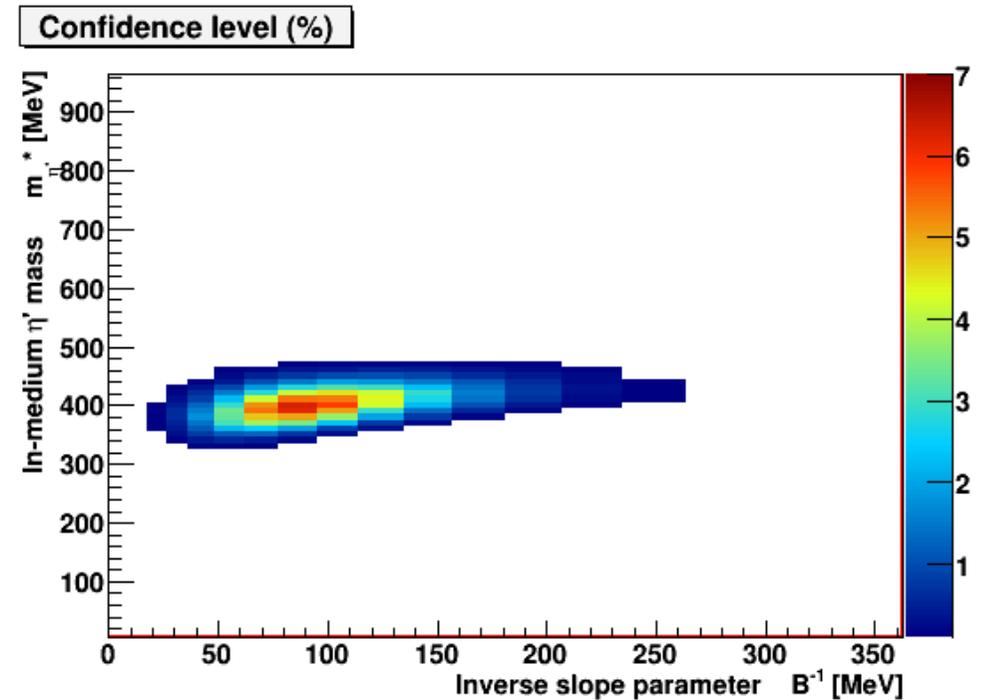
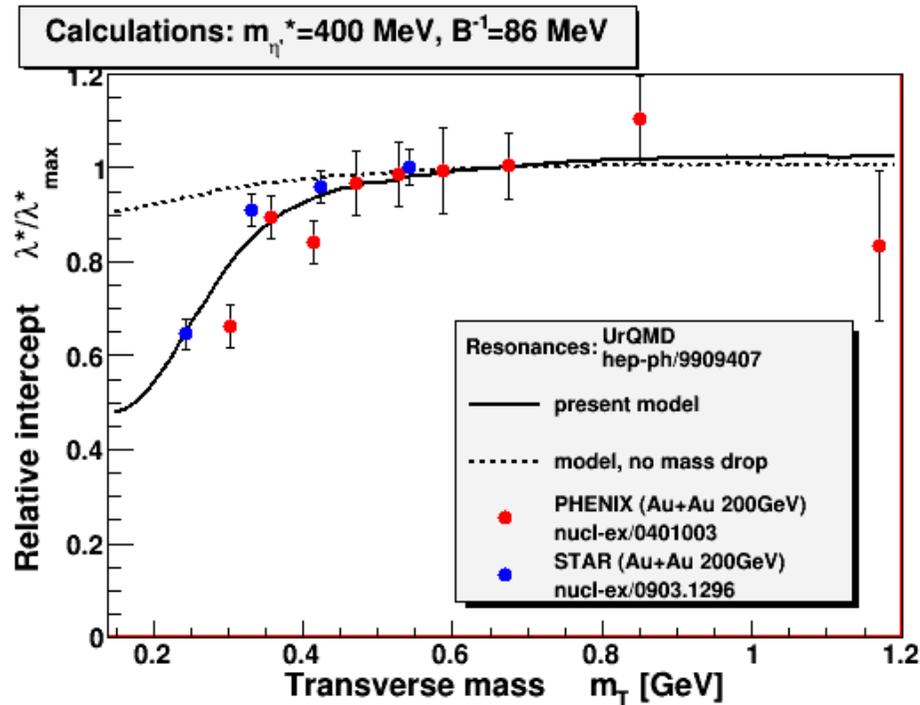
Resonances: Stachel et al. vs. RHIC



- Statistical chemical freezeout model
- Central mid- η 200 GeV Au+Au

J.Stachel et al., arXiv:nucl-th/9907090

Resonances: UrQMD vs. RHIC



- 200 GeV midrapidity
- Au+Au, RHIC $\sqrt{s_{NN}} = 200$ GeV

J. P. Sullivan et al., Phys. Rev. Lett. 70 (1993) 3000

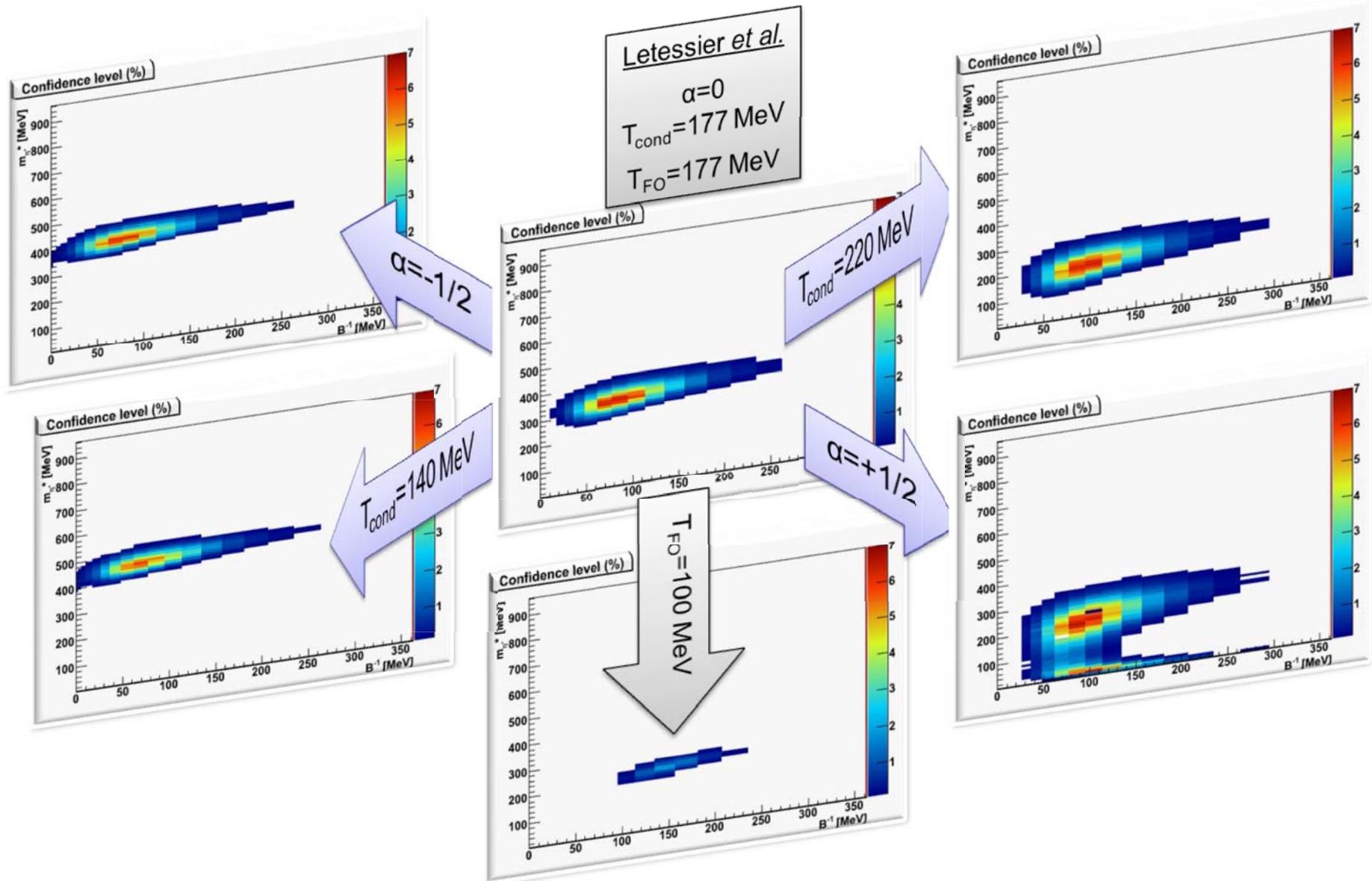
Systematics and Results

- Largest uncertainty: models for resonance ratios
- Modifying parameters in the widest reasonable range
 - $-1/2 \leq \alpha \leq +1/2$ (1)
 - $140 \text{ MeV} \leq T_{\text{cut}} \leq 220 \text{ MeV}$
 - $100 \text{ MeV} \leq T_{\text{FO}} \leq 177 \text{ MeV}$

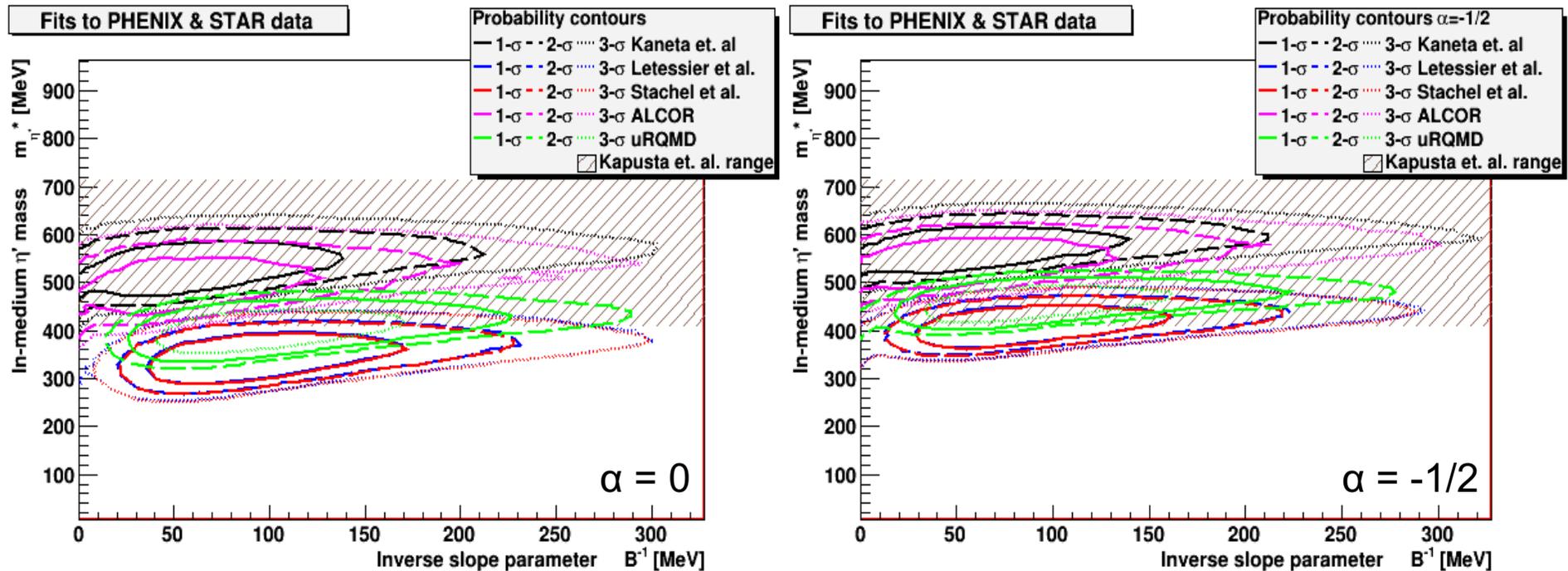
(altogether 17 x 1248 x 1000000 events simulated)

- An upper boundary can be determined for the η' mass:
Each and every setup fails when $m_{\eta'}^* > 750 \text{ MeV}$
(failure means $\text{CL} < 0.1\%$)

Systematics – a Visual Summary

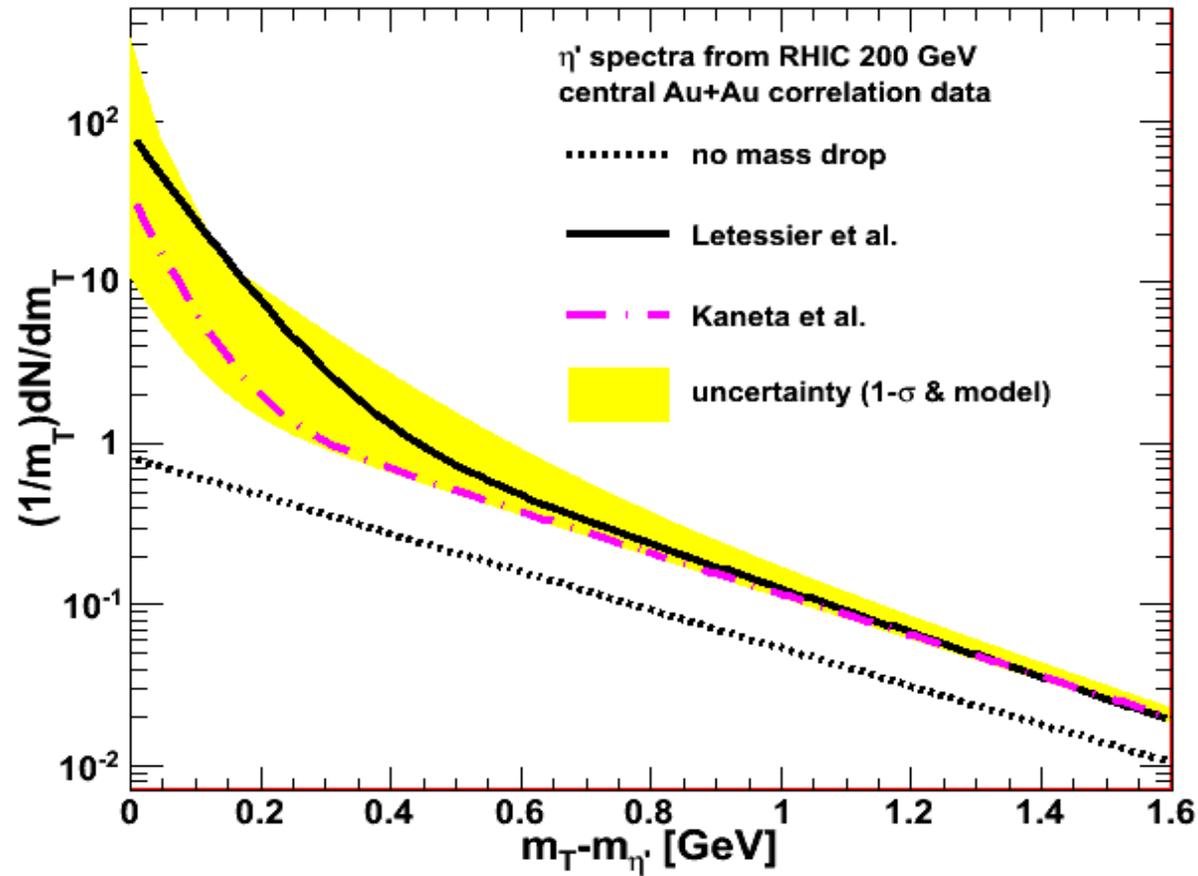


Calculations vs. Prediction



- Theoretical region: [Kapusta et al. arXiv:nucl-th/9507343](https://arxiv.org/abs/nucl-th/9507343)
- Sigma-contours from model calculations: either in accordance with theory, or slightly below
- Different α expansion exponents: systematic uncertainty

Output: η' Spectrum

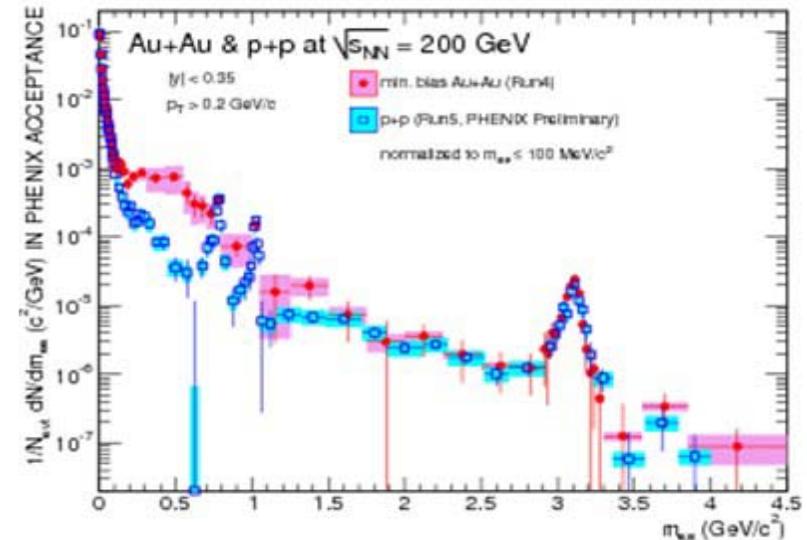
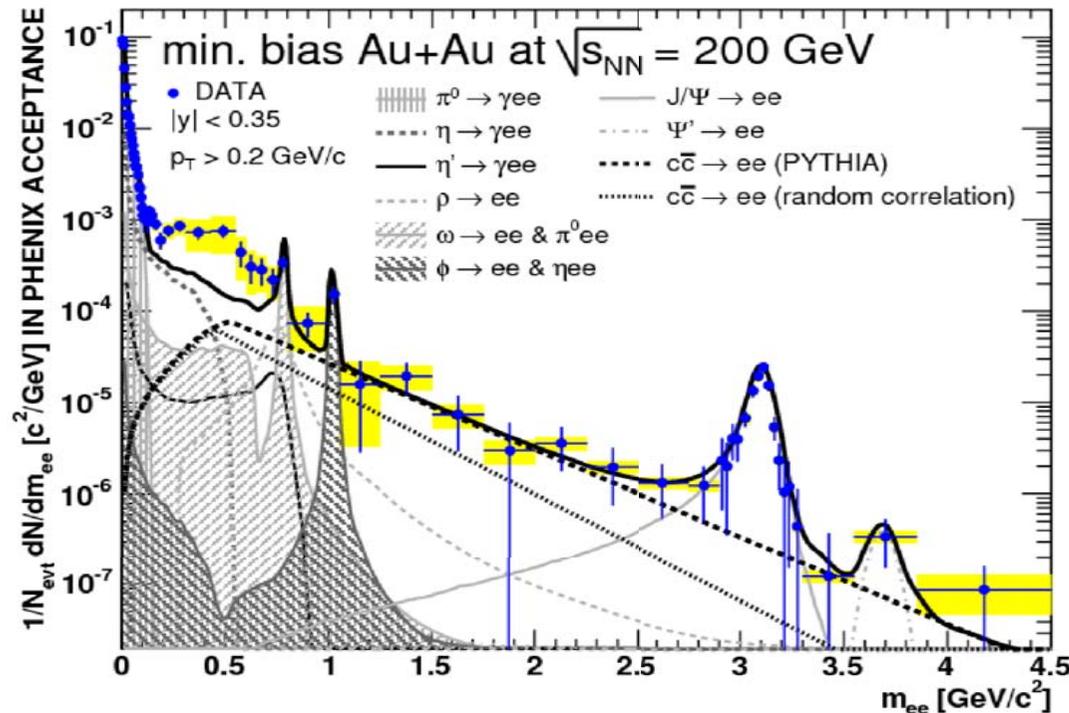


An enhancement factor of ~20-200, mostly at low- p_T

Model uncertainties in yellow band. Breaks m_T -scaling at low- p_T .

Possible explanation of the dilepton excess → needs check!

Dilepton Excess in PHENIX



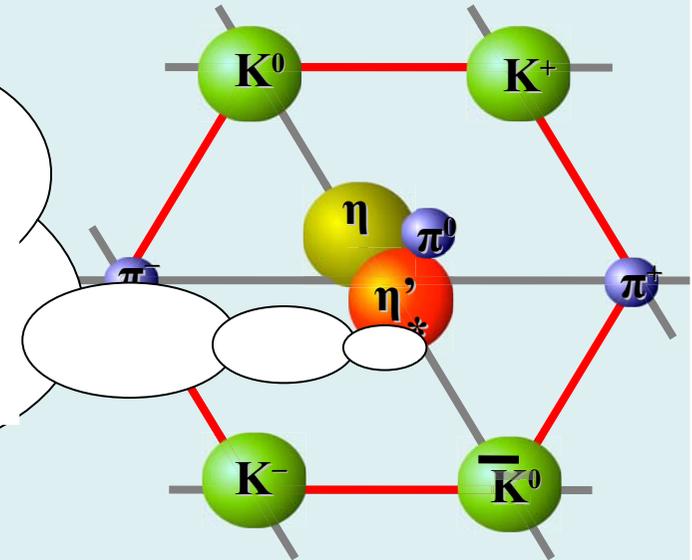
A. Adare *et al.* (PHENIX cn.)
 Phys.Lett.B670:313-320,2009.

S. Afanasiev *et al.* (PHENIX cn.)
 e-Print: arXiv:0706.3034

- Au+Au invariant $e^+ e^-$ pair yield
- **Significant excess** in PHENIX 200 GeV Au+Au measurements
- Not present in p+p data – in accordance with hadronic models
- Excess must be an effect of the hot, dense medium. **FURTHER studies.**

Conclusion

$m_{\eta}^* < m_{\eta} - 200 \text{ MeV}$
at the 99.9% confidence level
from PHENIX+STAR $\pi^+\pi^+$
correlation data + 6 models



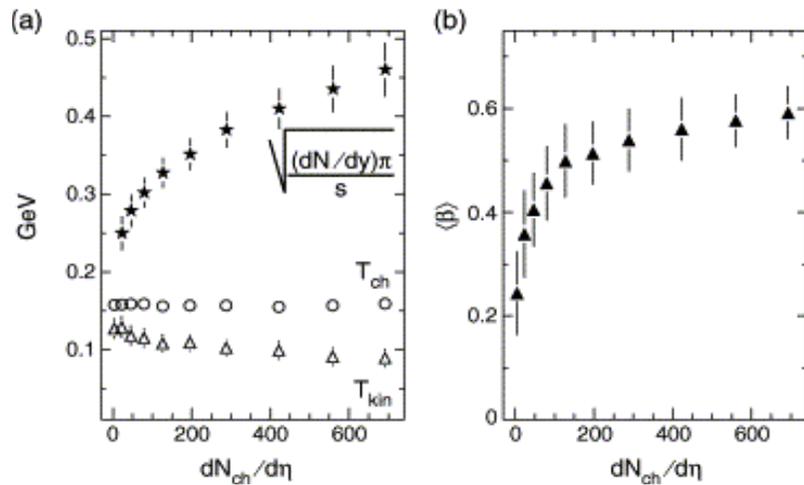
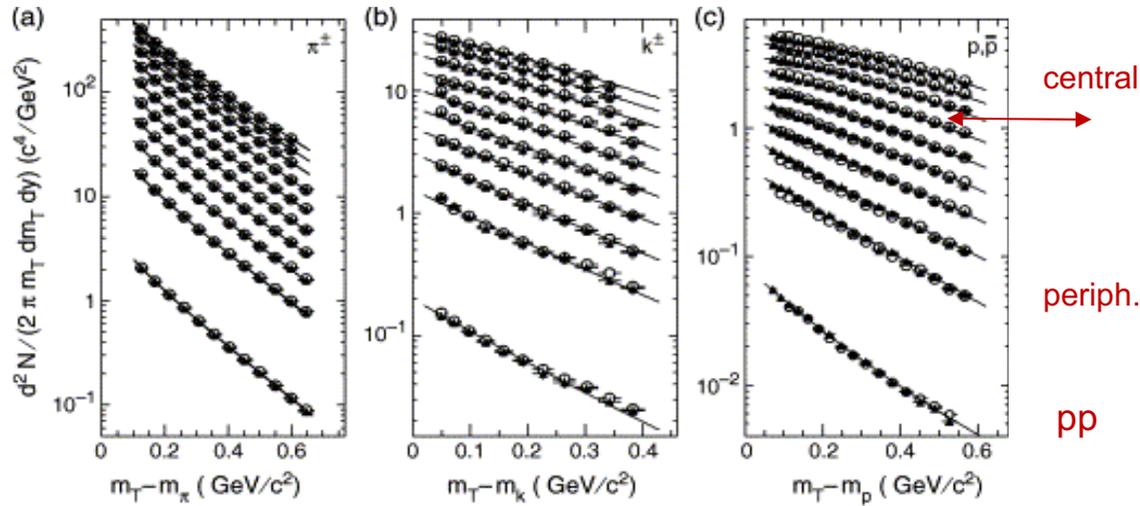
- **Cross-check with dilepton spectrum needed**
- **More λ^* data at low p_T is needed to reduce systematics**
- **Revitalize interest in chiral symmetry restoration**

The End



backup slides follow...

m_T -scaling



$$\frac{dN}{dp_t^2} \sim \exp\left(-\frac{m_t}{T}\right), \quad m_t^2 = p_t^2 + m^2$$

E. Shuryak, Prog.Part.Nucl.Phys.53:273-303,2004.

η' mass: Fitted values

	Model Fits for PHENIX+STAR data					Parameters		
	ALCOR	Kaneta <i>et al.</i>	Letessier <i>et al.</i>	Stachel <i>et al.</i>	UrQMD	α	T_{cond}	T_{FO}
$m_{\eta'}^*$ (MeV)	490^{+60}_{-50}	530^{+50}_{-50}	340^{+50}_{-60}	340^{+50}_{-60}	400^{+50}_{-40}	0	177	177
B^{-1} (MeV)	42	55	86	86	86			
CL (%)	4.29	4.12	6.35	6.38	6.28			
$m_{\eta'}^*$ (MeV)	540^{+50}_{-40}	560^{+60}_{-30}	410^{+40}_{-40}	410^{+40}_{-40}	460^{+40}_{-40}	-0.5	177	177
B^{-1} (MeV)	55	55	86	86	86			
CL (%)	2.80	3.35	6.07	5.97	6.14			
$m_{\eta'}^*$ (MeV)			210			+0.5	177	177
B^{-1} (MeV)			86					
CL (%)			6.54					
$m_{\eta'}^*$ (MeV)		620	460			0	140	177
B^{-1} (MeV)		42	69					
CL (%)		2.26	5.86					
$m_{\eta'}^*$ (MeV)		440	200			0	220	177
B^{-1} (MeV)		69	104					
CL (%)		5.61	6.33					
$m_{\eta'}^*$ (MeV)		410	240			0	177	100
B^{-1} (MeV)		145	145					
CL (%)		1.63	1.80					

TABLE II: Fitted values of the modified η' mass on the STAR+PHENIX combined dataset, for different resonance models and parameters. The Fritiof model has CL < 0.1% and therefore not shown here. 1- σ boundaries of the fits are given only for $m_{\eta'}^*$, and for the $\alpha = 0$ and $\alpha = -0.5$ simulations, not for all the systematic checks.

η' mass: Acceptability boundaries

Dataset	Acceptability boundaries of model fits						Parameters		
	ALCOR	FRITIOF	Kaneta <i>et al.</i>	Letessier <i>et al.</i>	Stachel <i>et al.</i>	UrQMD	α	T_{cond}	T_{FO}
PHENIX	0—750	680—958	0—720	0—510	0—500	0—530	0	177	177
STAR	380—600	none	430—630	190—450	190—450	260—500			
PHENIX+STAR	380—590	none	420—620	260—430	260—430	330—470			
PHENIX	30—770	420—958	50—730	0—540	0—540	0—560	-0.5	177	177
STAR	470—630	none	500—650	300—500	300—500	360—540			
PHENIX+STAR	450—620	670—760	490—640	340—480	340—480	400—510			
PHENIX				0—450			+0.5	177	177
STAR				0—390					
PHENIX+STAR				0—390					
PHENIX			0—760	0—450			0	140	177
STAR			560—690	0—390					
PHENIX+STAR			540—680	0—360					
PHENIX			0—680	0—410			0	220	177
STAR			270—580	0—350					
PHENIX+STAR			290—560	100—320					
PHENIX			220—470	30—310			0	177	100
STAR			360—470	190—300					
PHENIX+STAR			370—440	200—280					

TABLE III: Acceptability boundaries of the modified η' mass on the PHENIX, STAR, and the STAR+PHENIX combined datasets, for different resonance models and parameters. A fit is considered acceptable if $CL \geq 0.1\%$. There is no model and no sane set of parameters that contradict with an $m_{\eta'}^* \leq 760$ MeV assumption for the combined PHENIX+STAR dataset. However, all the models except for the FRITIOF, the one that completely fails on the STAR dataset, require an $m_{\eta'}^* \leq 640$ MeV.

Dilepton excess in details

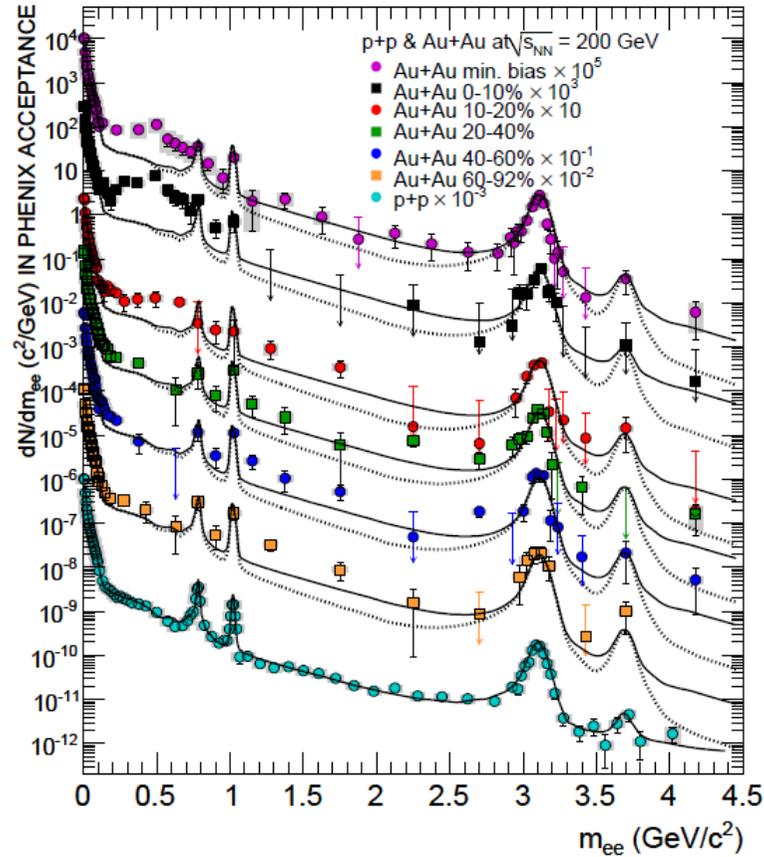


Fig.26: Invariant mass spectrum of e^+e^- pairs compared to expectations from the model of hadron decays for p+p and for different Au+Au centrality classes.

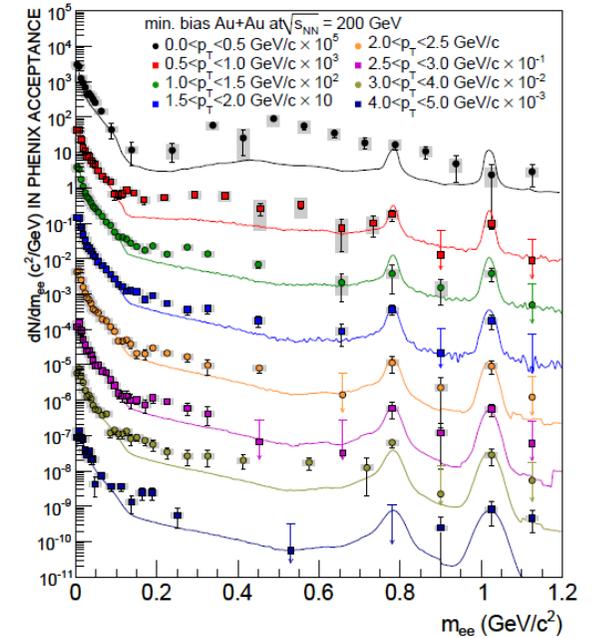
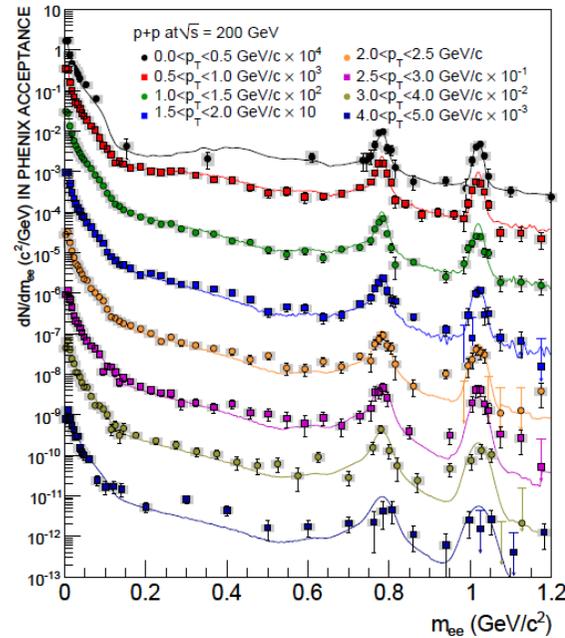
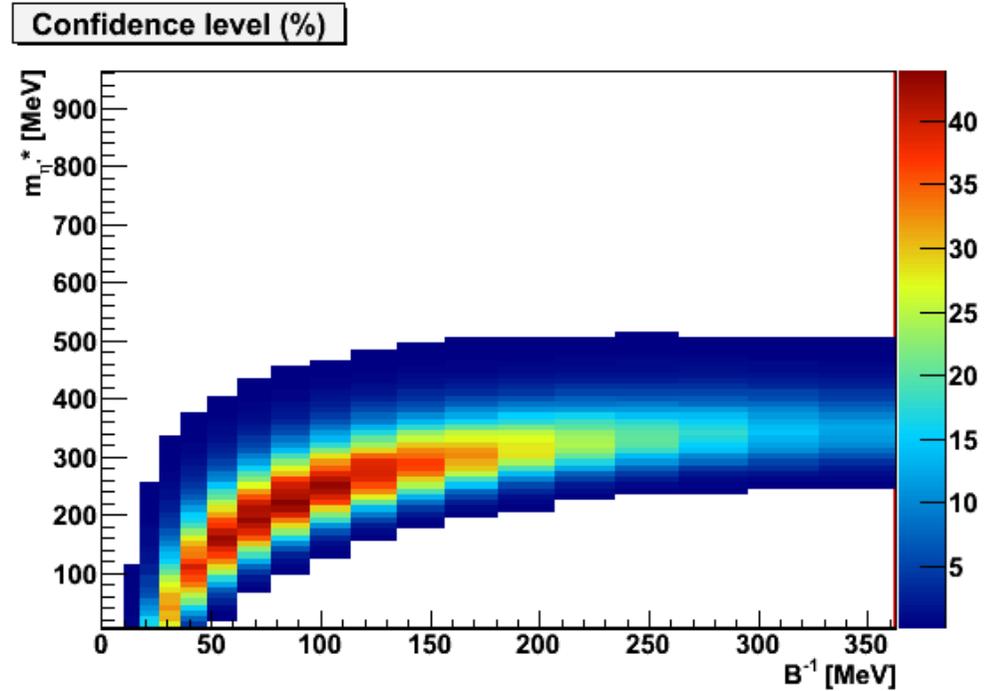
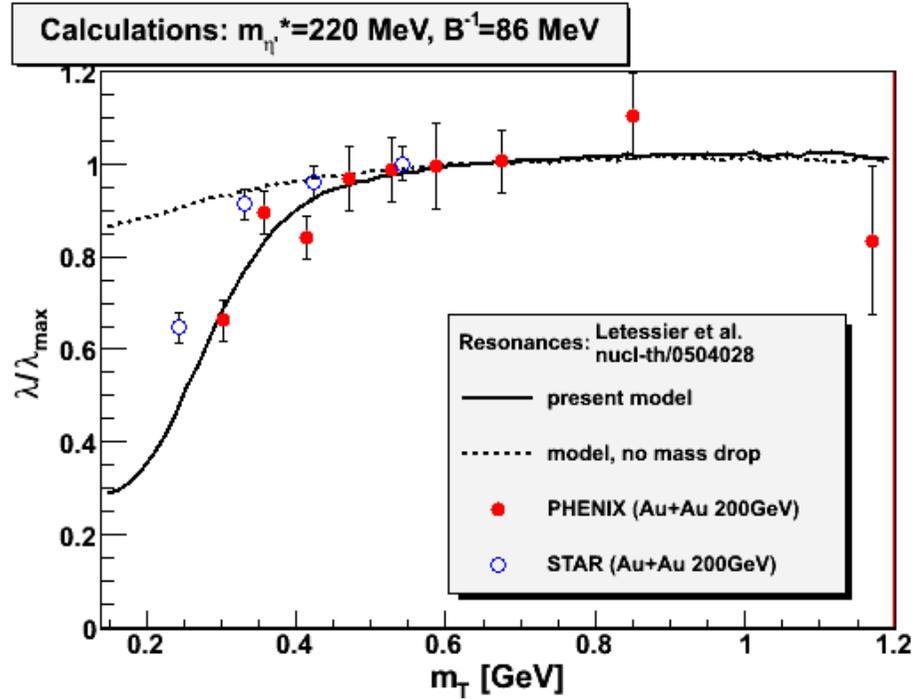
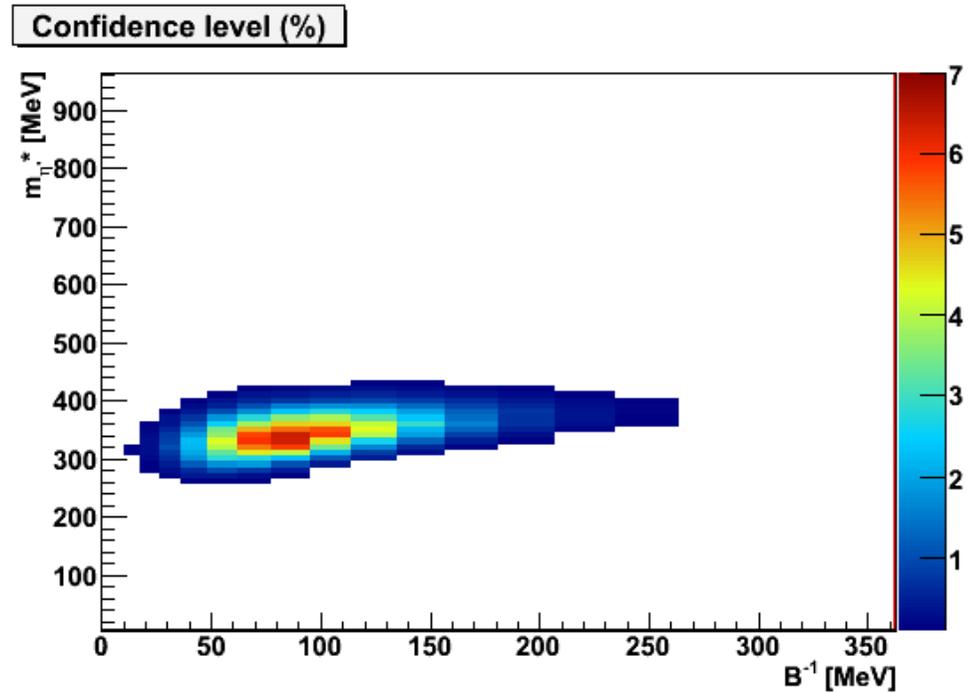
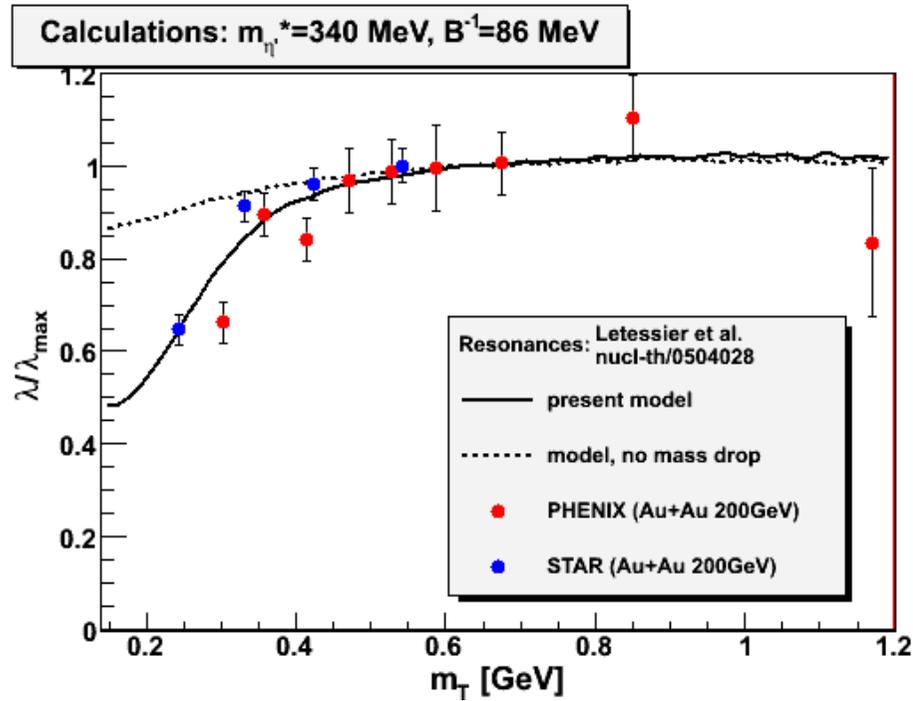


Fig.29: e^+e^- pair invariant mass distributions in p + p (left) and minimum bias Au+Au collisions (right). The p_T ranges are shown in the legend.

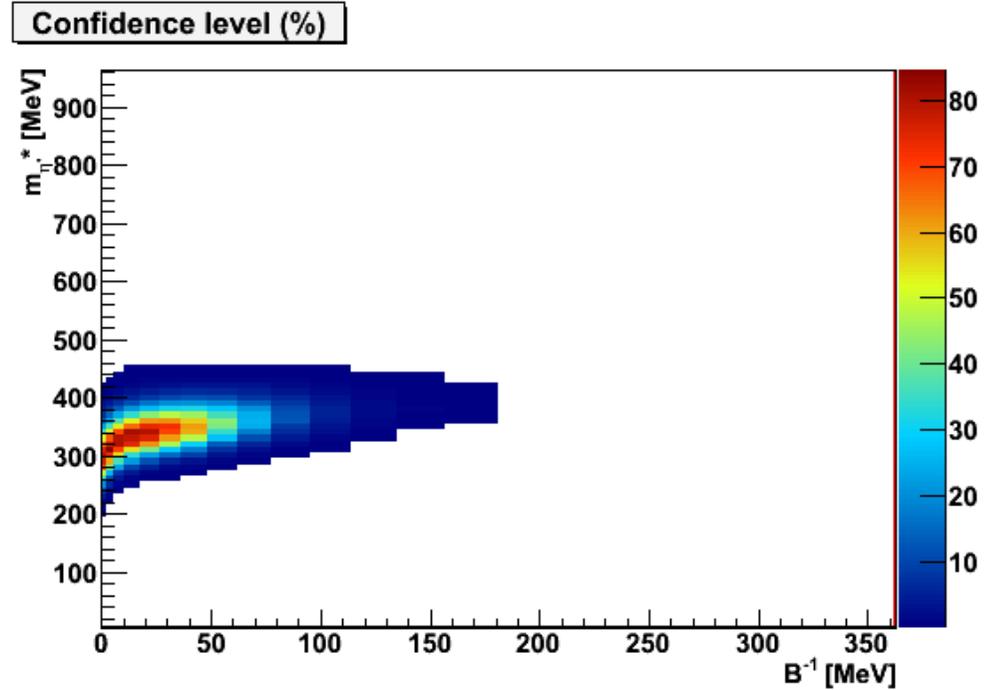
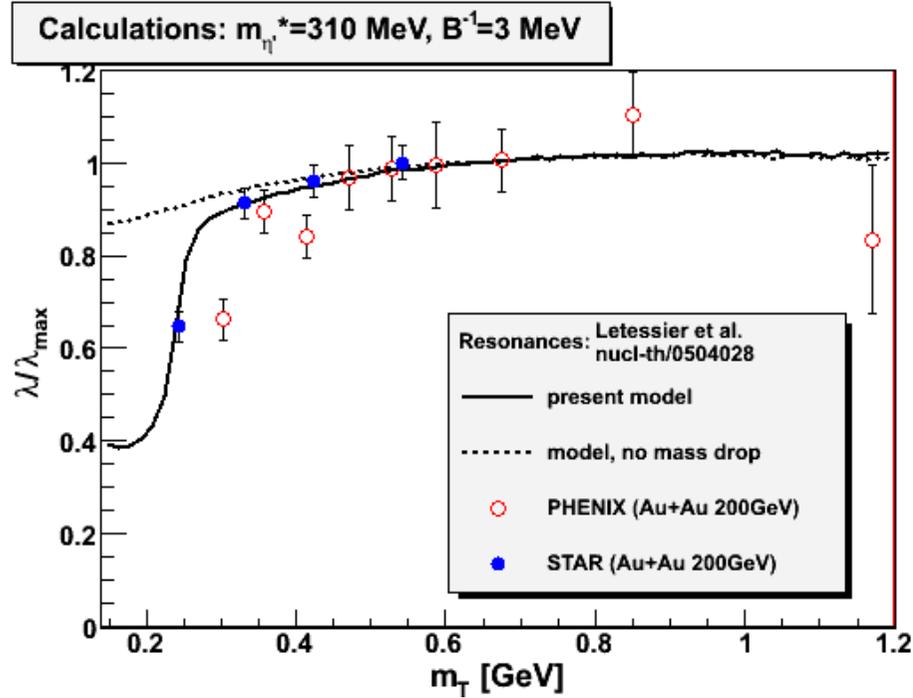
Rafelski vs. PHENIX



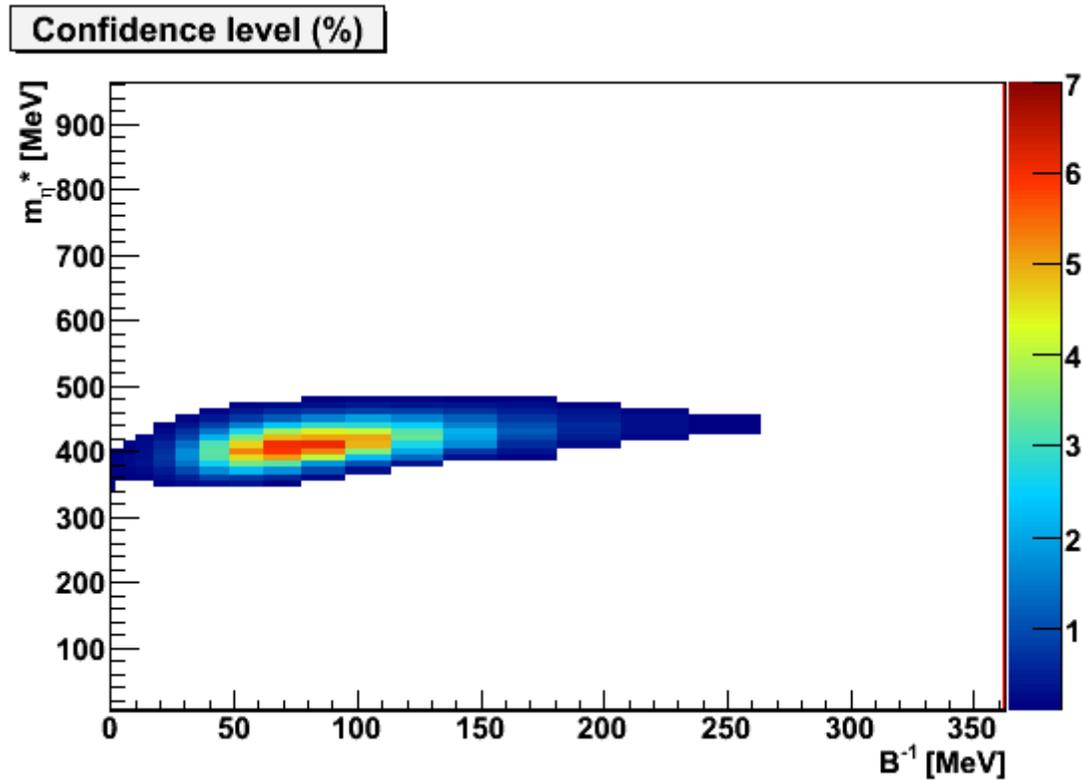
Rafelski vs. PHENIX & STAR



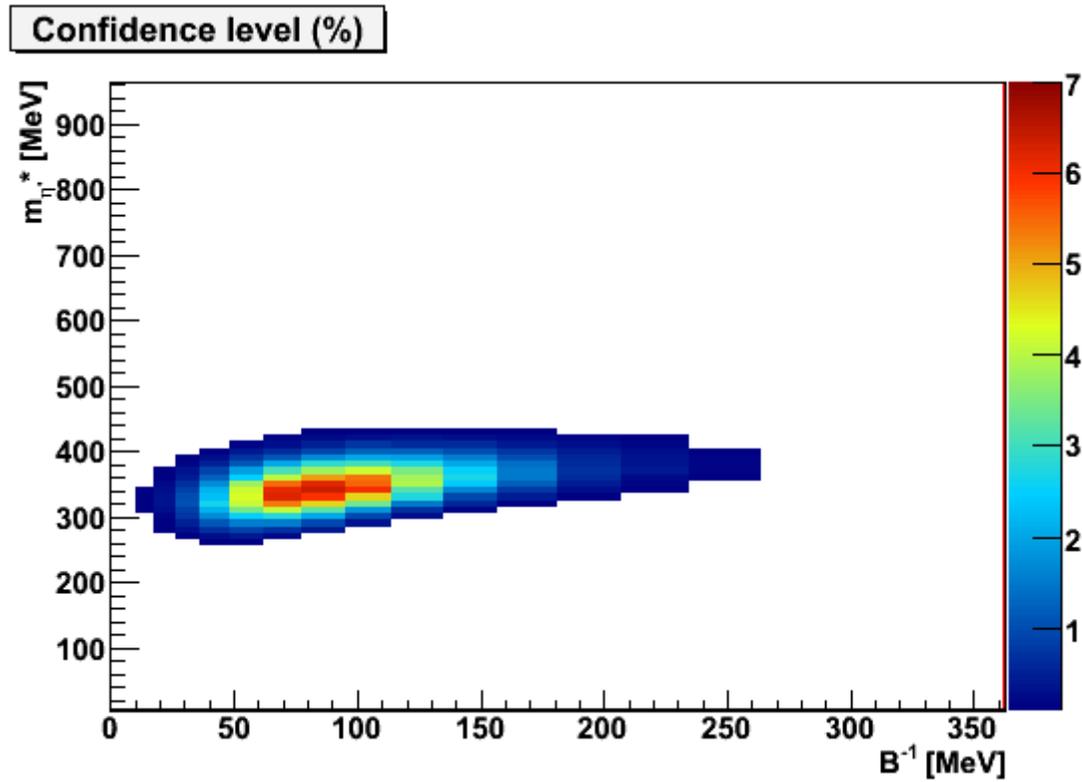
Rafelski vs. STAR



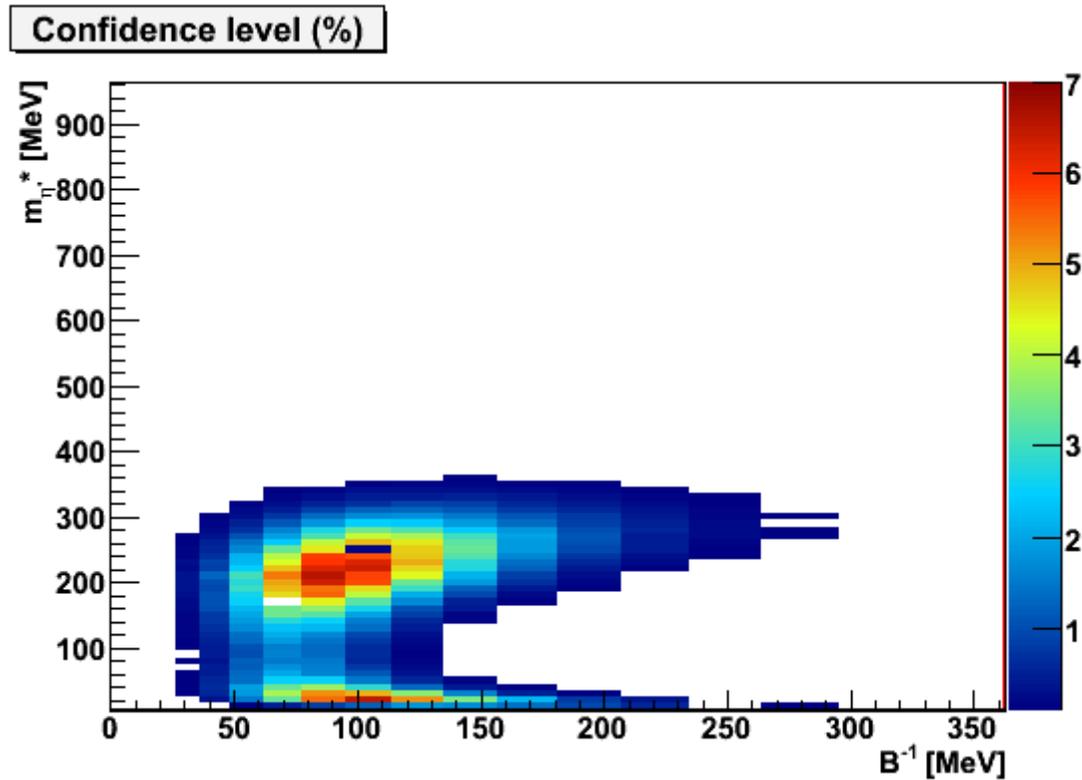
Systematics: Rafelski $\alpha = -1/2$



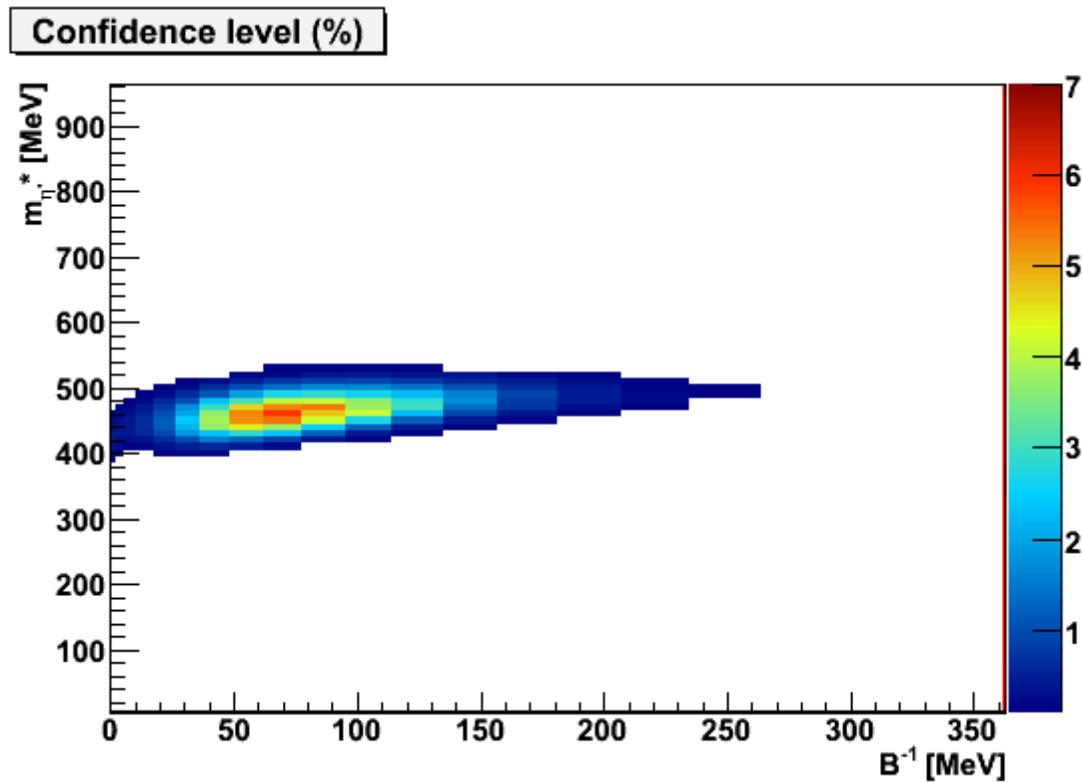
Systematics: Rafelski $\alpha=0$



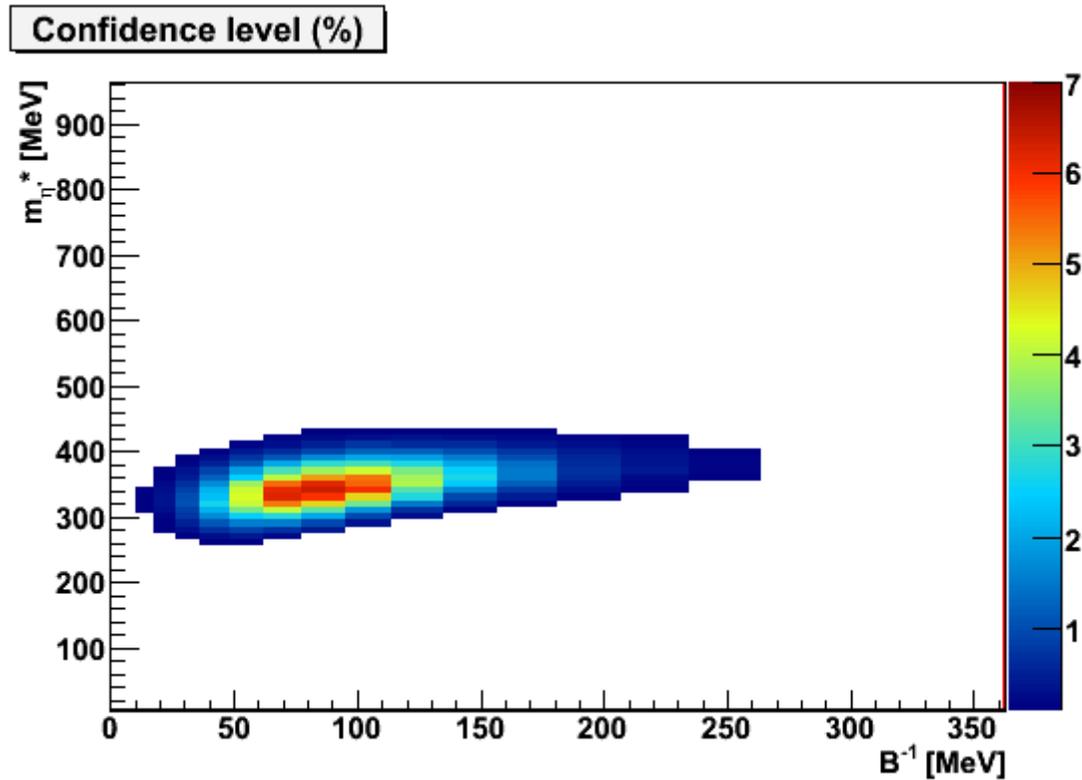
Systematics: Rafelski $\alpha=+1/2$



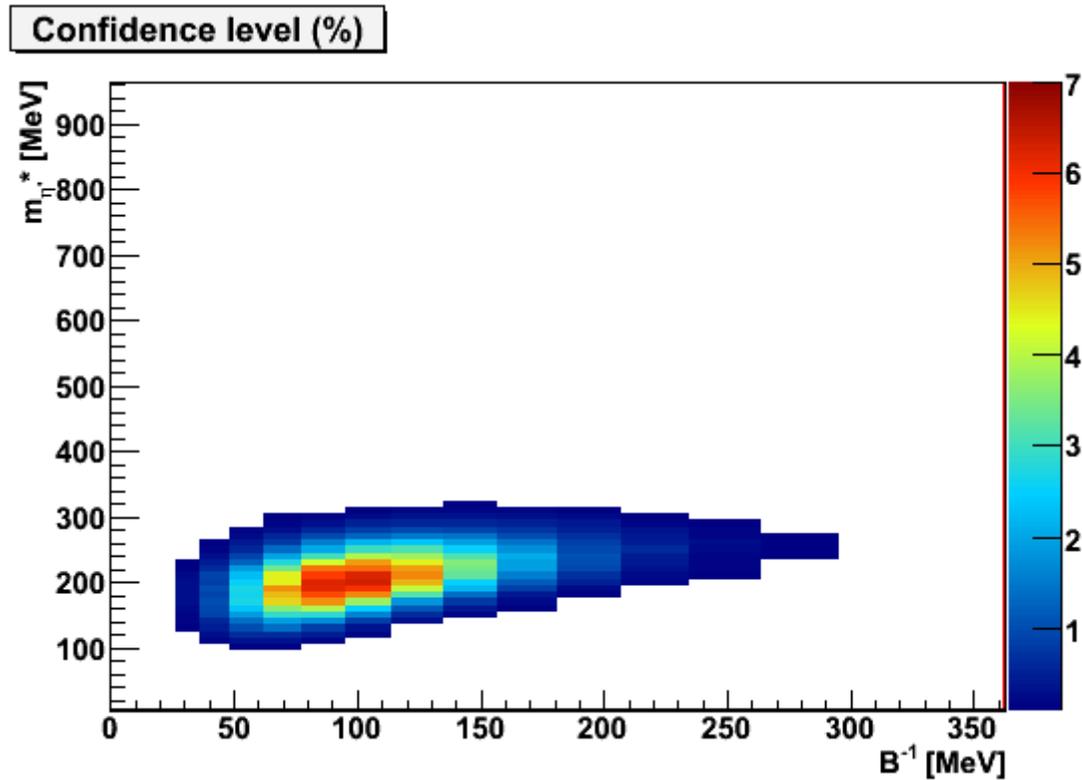
Systematics: Rafelski $T'=140$ MeV



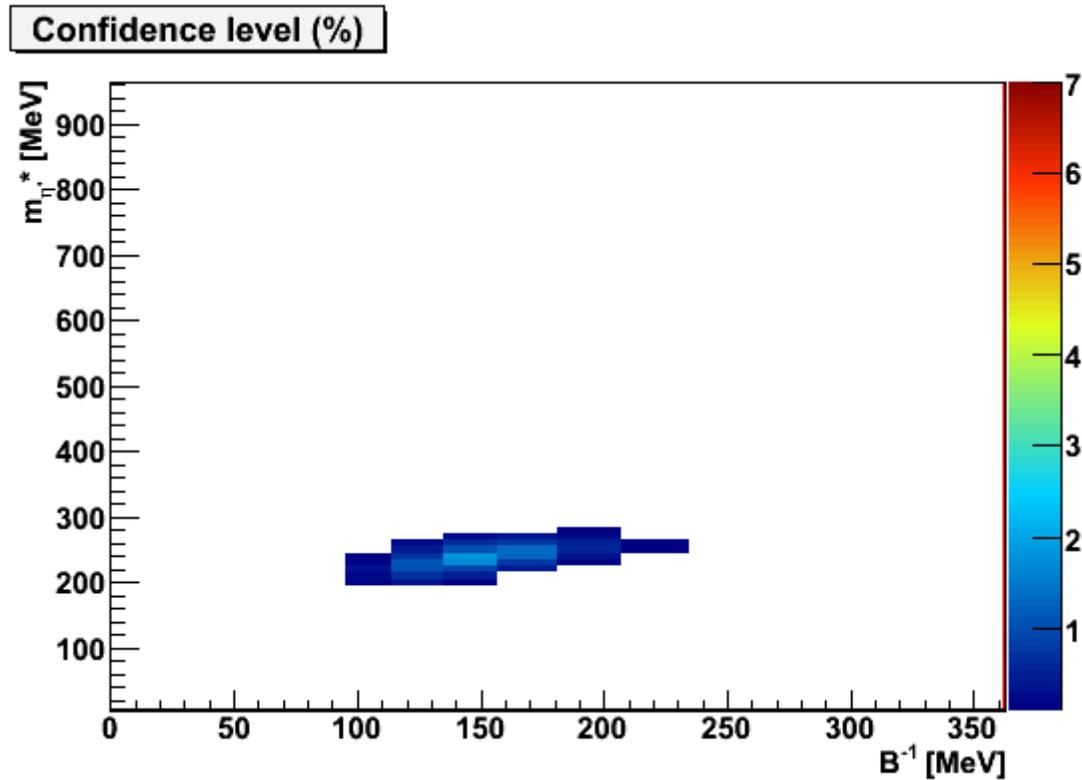
Systematics: Rafelski $T' = 177$ MeV



Systematics: Rafelski $T'=220$ MeV



Systematics: Rafelski $T_{FO} = 100$ MeV



Systematics: Rafelski $T_{FO} = 177$ MeV

