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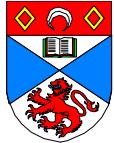
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**Workshop on Principles and Design of Strongly Correlated Electronic Systems**

*2 - 13 August 2010*

**Thermodynamic Studies of Sr<sub>3</sub>Ru<sub>2</sub>O<sub>7</sub>**

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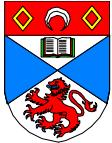


# **Thermodynamic studies of $\text{Sr}_3\text{Ru}_2\text{O}_7$**

**Andy Mackenzie**

University of St Andrews, Scotland





## Recent collaborators

A. Rost<sup>1</sup>, S. A. Grigera<sup>1</sup>, J.-F. Mercure<sup>1</sup>, R. S. Perry<sup>1,2</sup>,  
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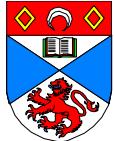
<sup>4</sup> University of Cambridge

<sup>5</sup> University of Göttingen

<sup>6</sup> Brookhaven National Laboratory

<sup>7</sup> Cornell University

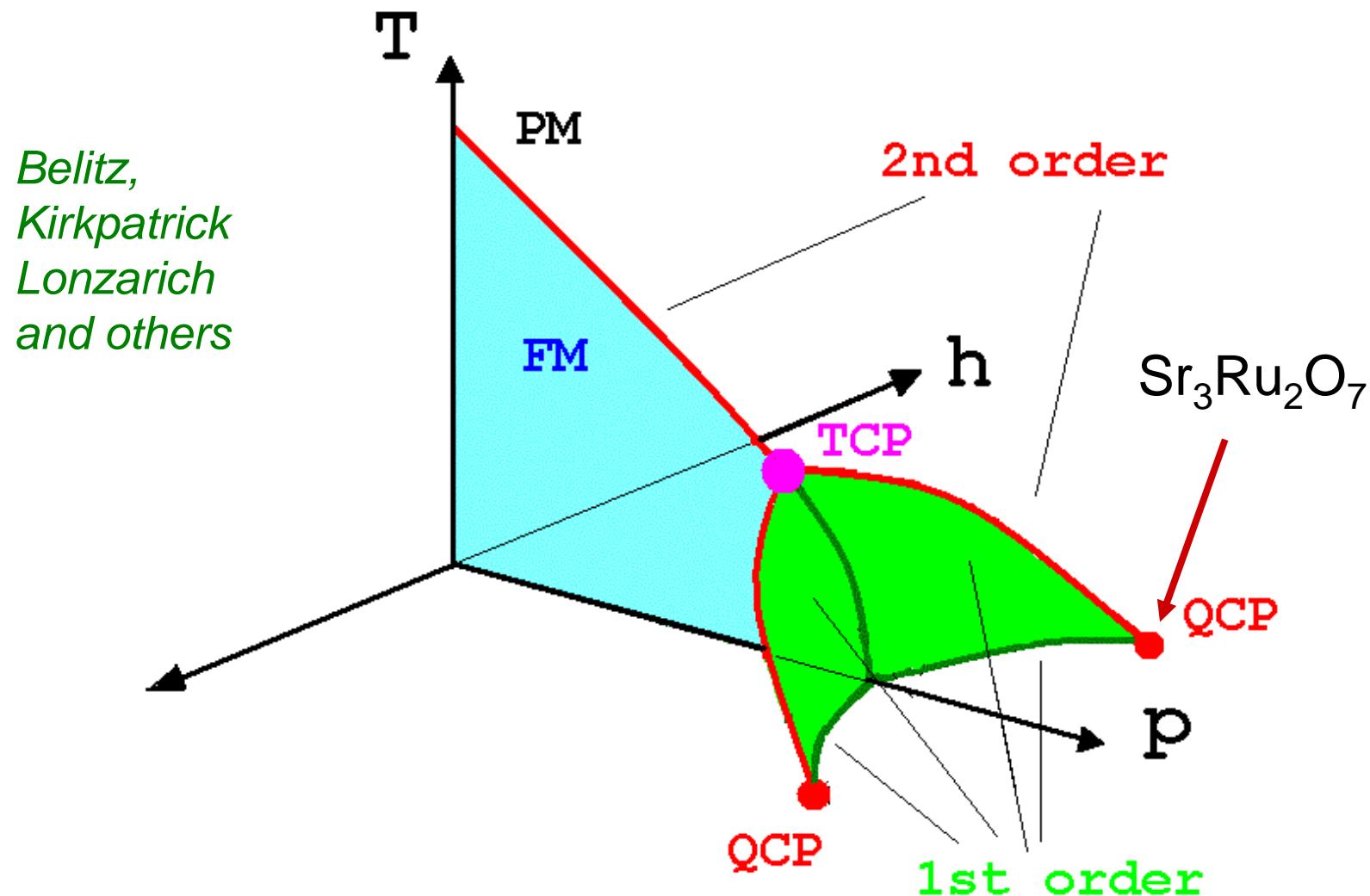




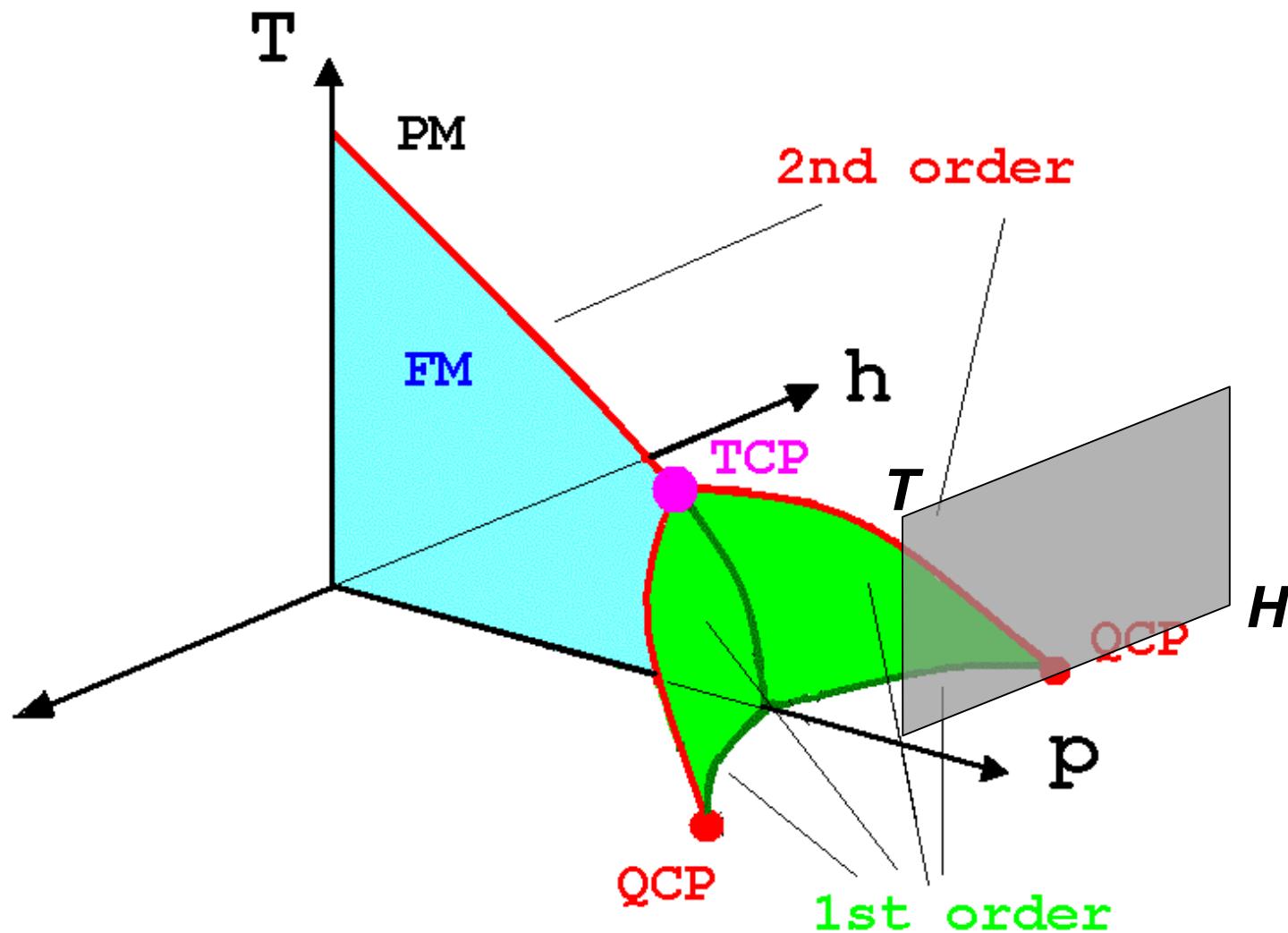
## Contents

1.  $\text{Sr}_3\text{Ru}_2\text{O}_7$  and the phase diagram of itinerant ferromagnetism
2. Thermodynamic probes used in our group: magnetisation, quantum oscillations, specific heat and magneto-caloric effect
3. Quantum critical entropy pileup
4. A novel phase with nematic transport properties and additional degrees of freedom
5. Broader perspectives: relevance to surface spectroscopy, electronic nematics, heavy fermion physics and beyond.

# $\text{Sr}_3\text{Ru}_2\text{O}_7$ in the phase diagram of itinerant ferromagnetism

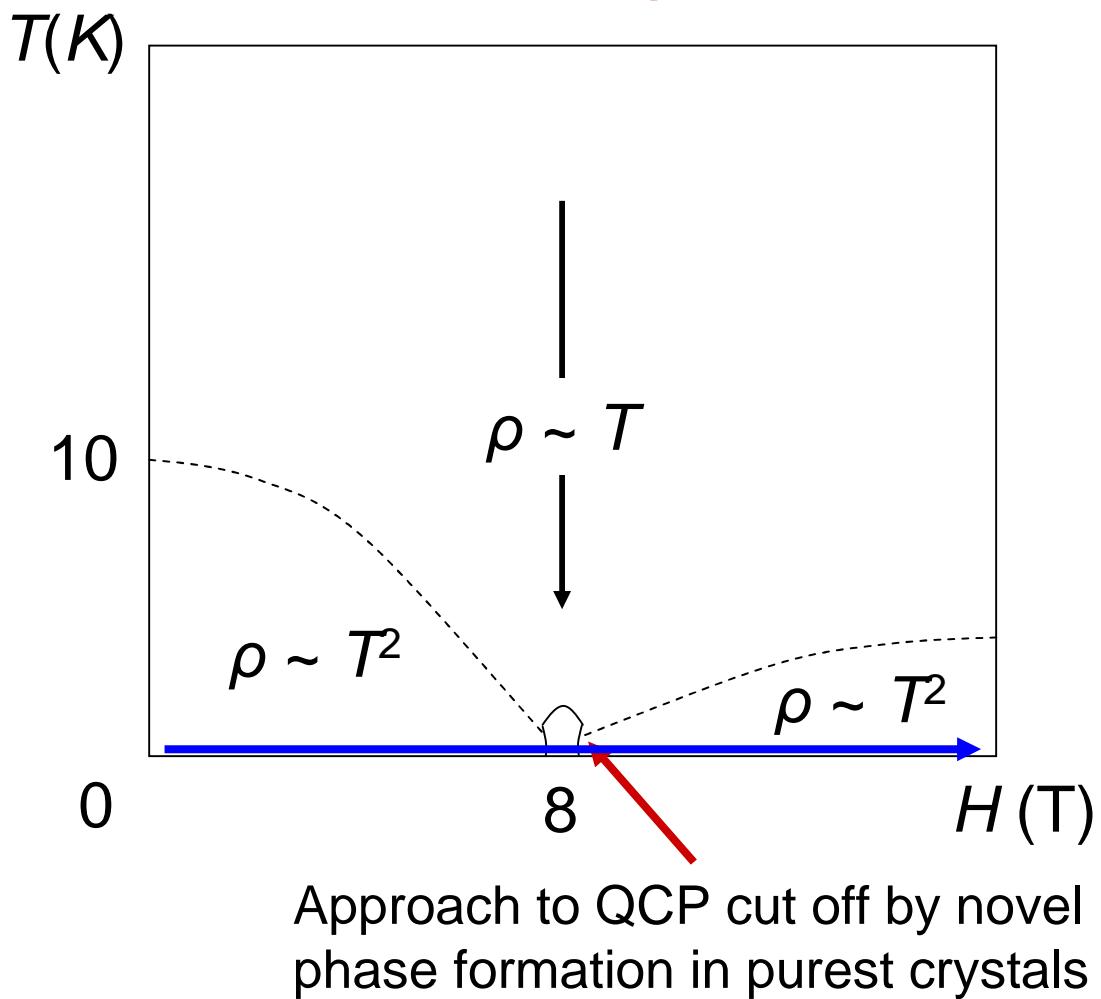


## Data presented in this talk



Relevant electronic shells are Ru 4d and O 2p; no *f* electrons

# Quantum critical transport phase diagram



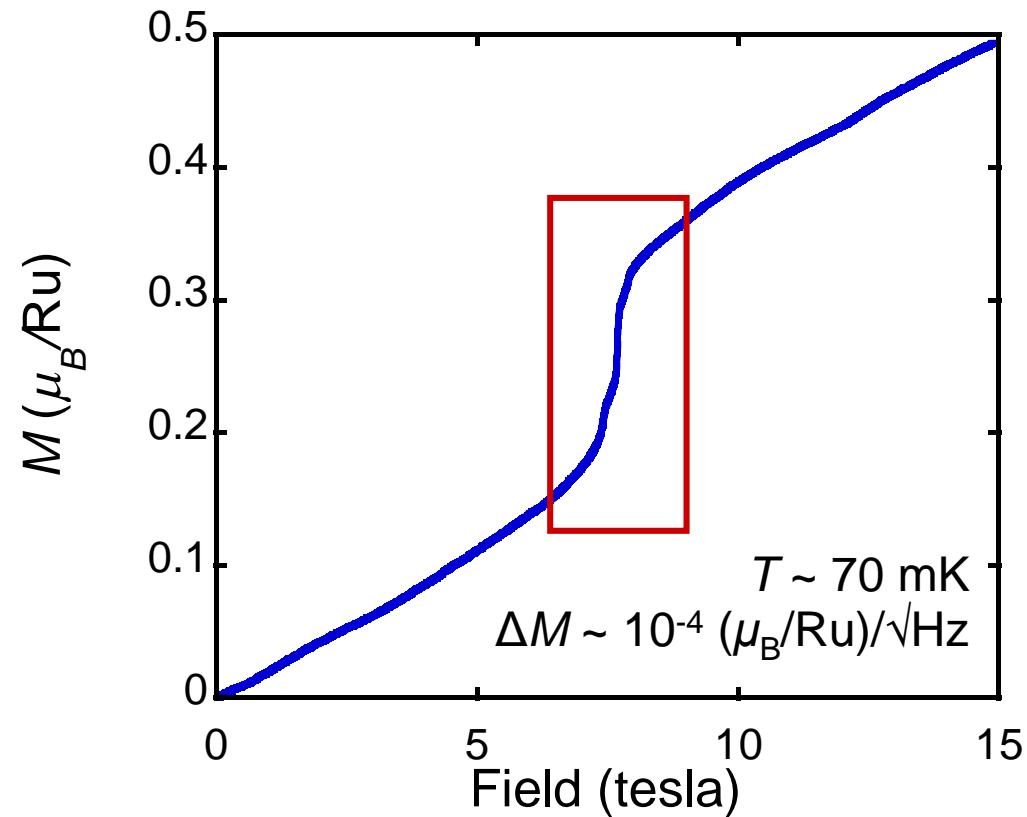
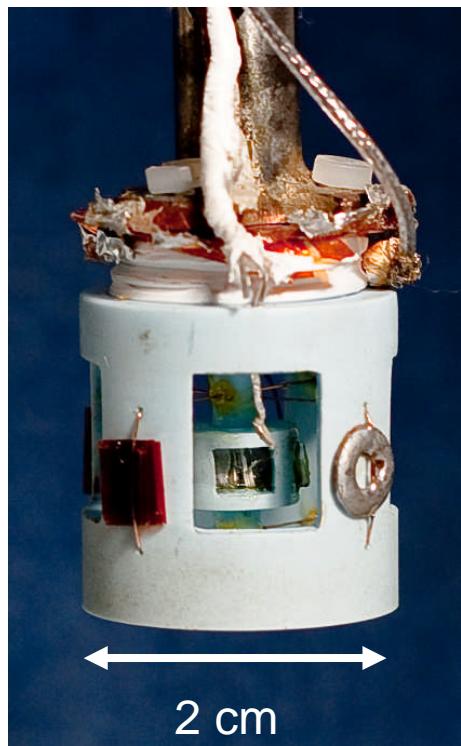
S.A. Grigera et al., *Science* **294**, 321 (2001); *Science* **306**, 1154 (2004).



Image furnace grown single crystals now with mean free paths greater than 3000 Å

R.S. Perry & Y. Maeno, *J. Cryst. Growth* **271**, 134 (2004)

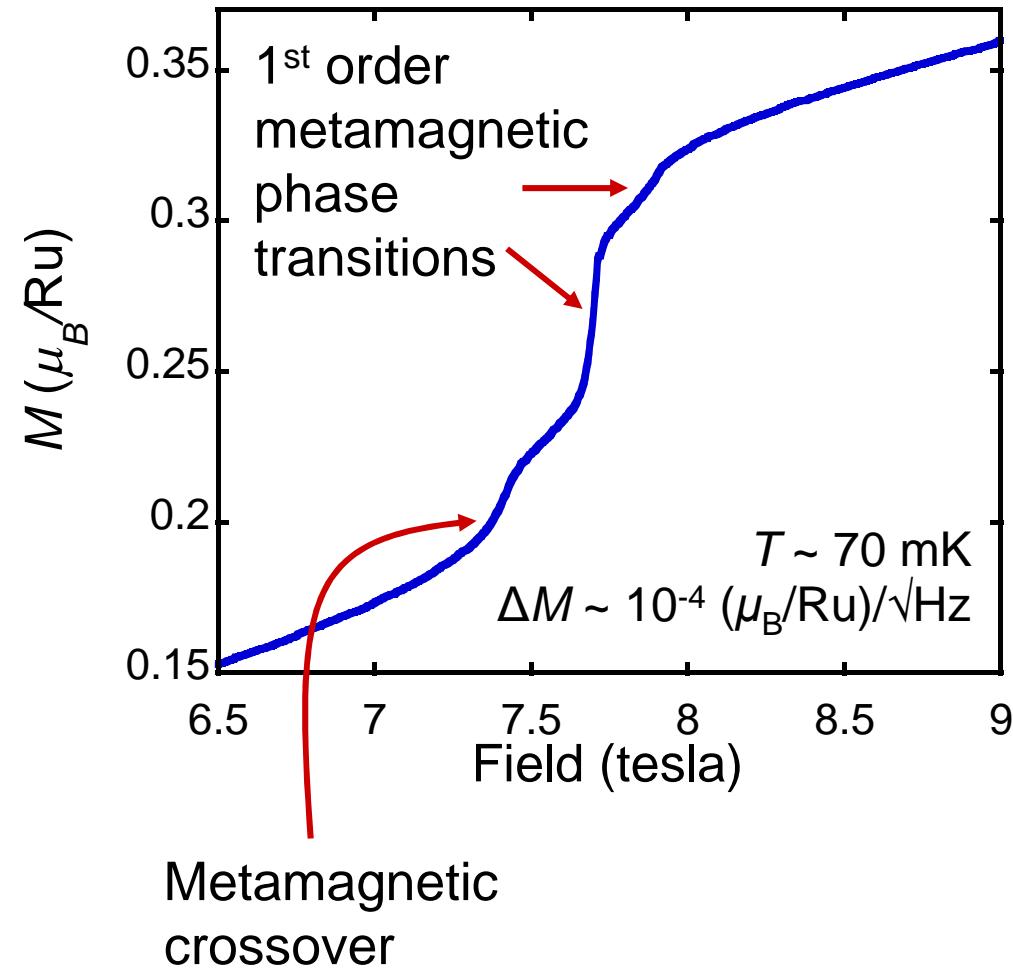
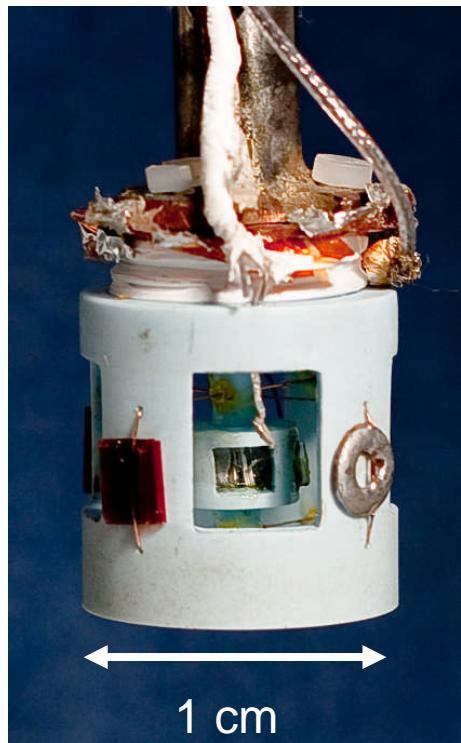
# Low temperature magnetisation of $\text{Sr}_3\text{Ru}_2\text{O}_7$



Lightweight plastic construction Faraday force magnetometer with independent sample temperature measurement, capacitive displacement sensing and reversible field gradient for isolation of torque and magnetisation signals.

*D. Slobinsky, R.A. Borzi, R.S. Perry, S.A. Grigera et al.*

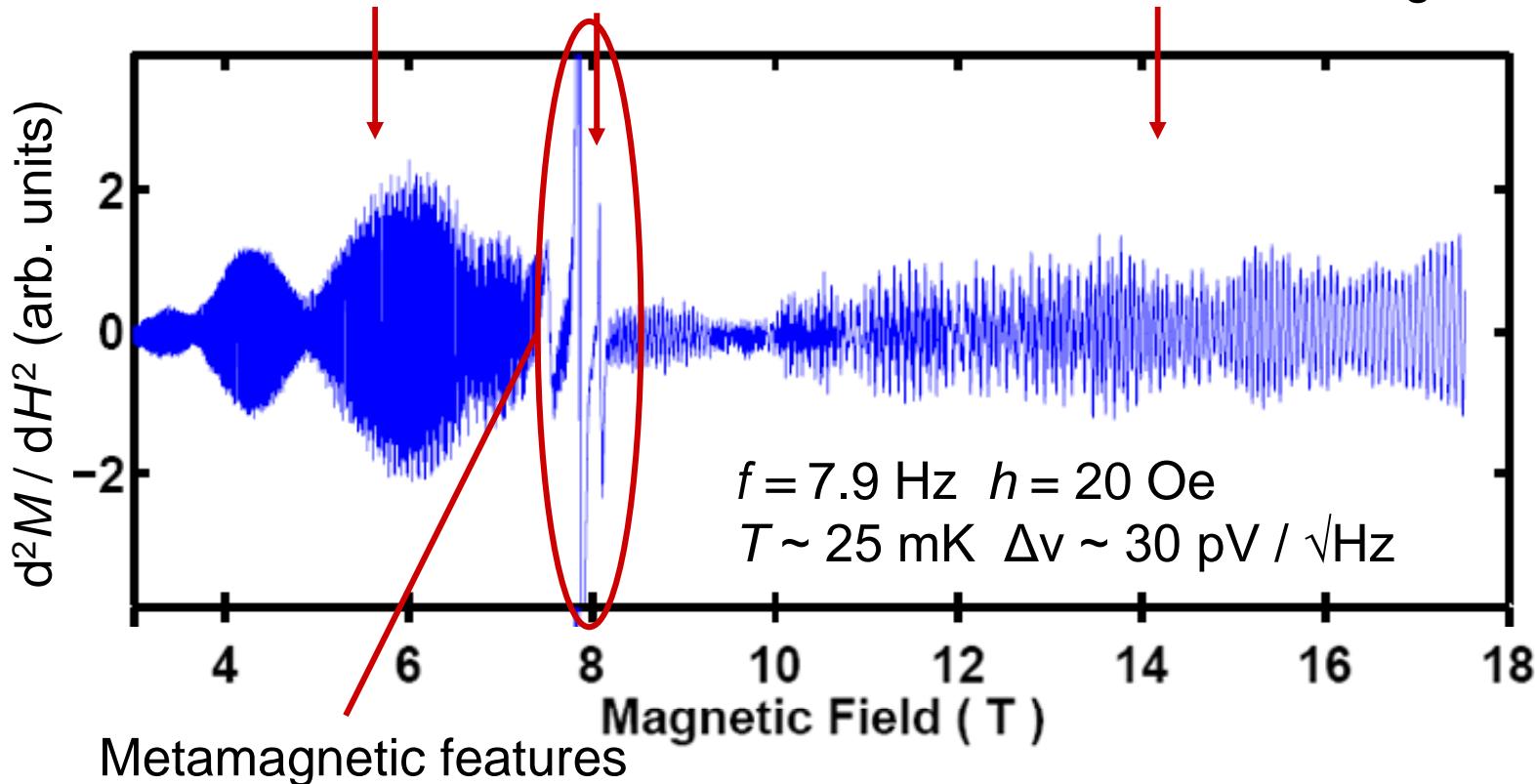
# Low temperature magnetisation of $\text{Sr}_3\text{Ru}_2\text{O}_7$



D. Slobinsky, R.A. Borzi, R.S. Perry, S.A. Grigera et al.

# The de Haas – van Alphen Effect in $\text{Sr}_3\text{Ru}_2\text{O}_7$

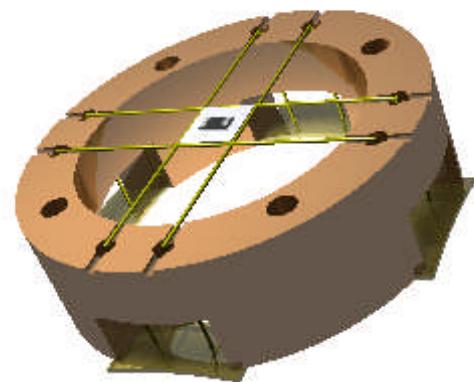
dHvA oscillations seen below, above and within the transition region.



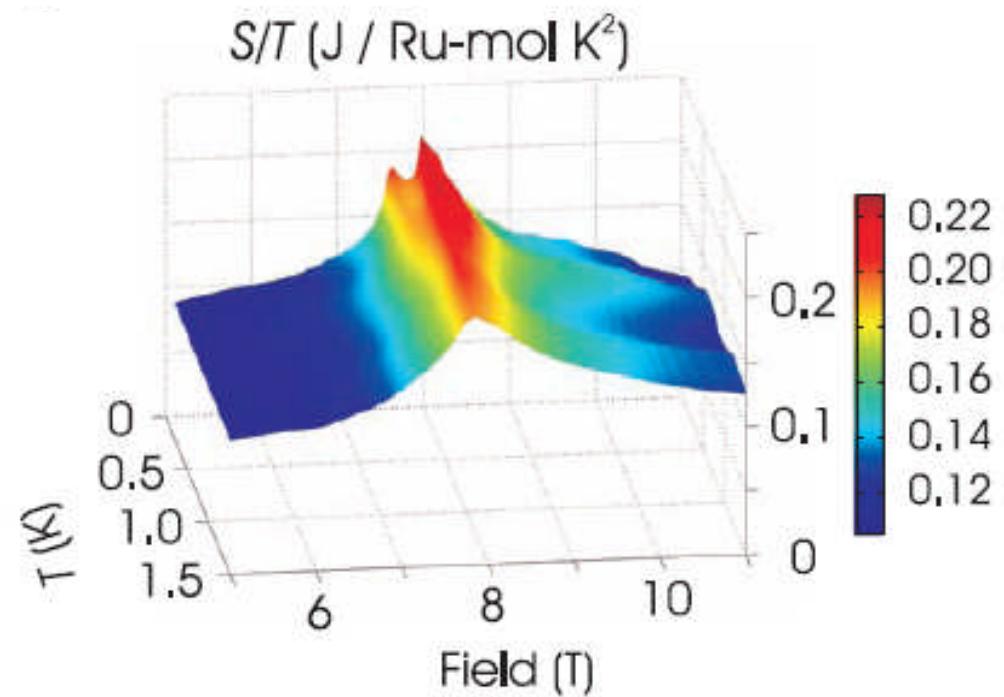
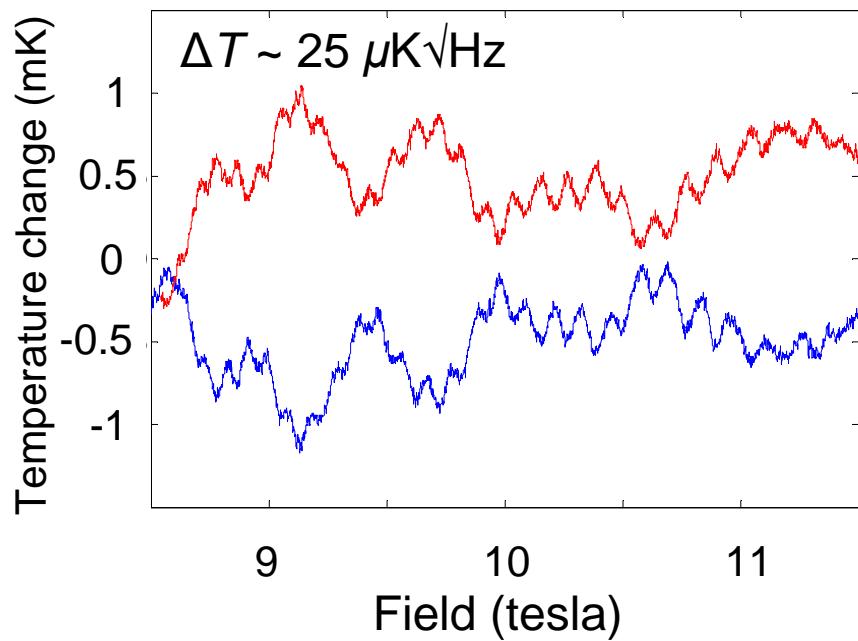
The  $\text{Sr}_3\text{Ru}_2\text{O}_7$  phase diagram comprises a series of metallic fluids.

*St. Andrews – Cambridge collaboration: J.F. Mercure et al., Phys. Rev. Lett. 103, 176401 (2009); Phys. Rev. B 81, 235103 (2010).*

# Combined magneto-caloric effect / specific heat in $\text{Sr}_3\text{Ru}_2\text{O}_7$

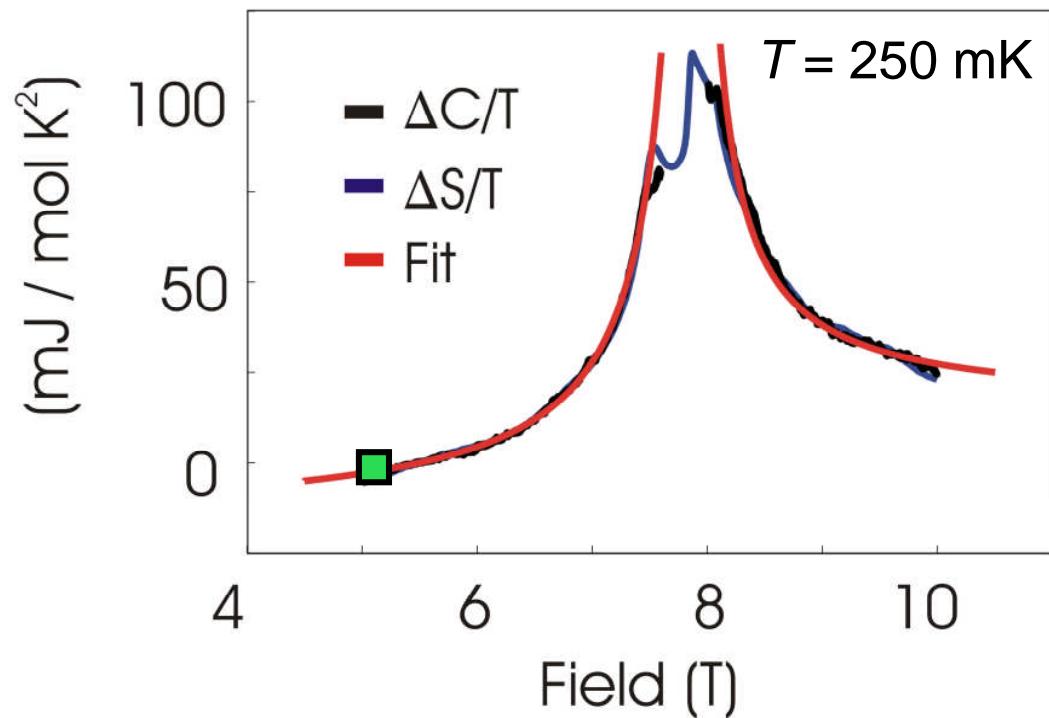


Silver platform suspended from tensioned kevlar fibres with variable thermal coupling to bath. Combination of precision and capability to take data rapidly.



A.W. Rost *et al.*, Science 325, 1360 (2009)

# Low $T$ field-dependent specific heat and entropy in $\text{Sr}_3\text{Ru}_2\text{O}_7$



$$S(T') = \int_0^{T'} \frac{C}{T} dT$$

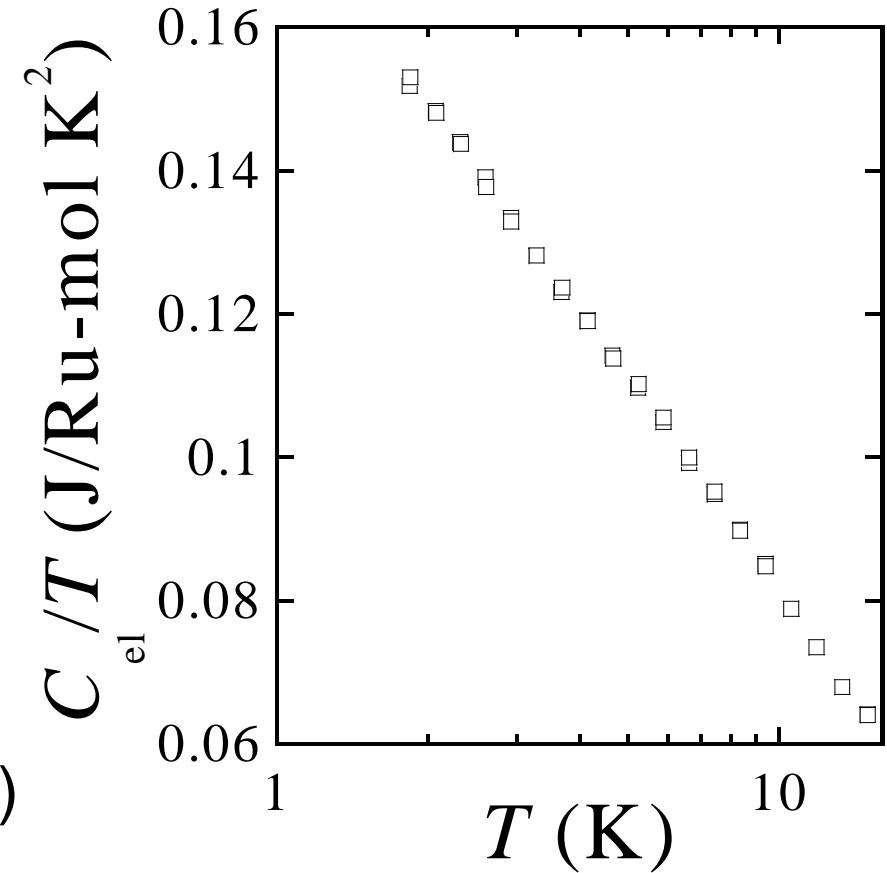
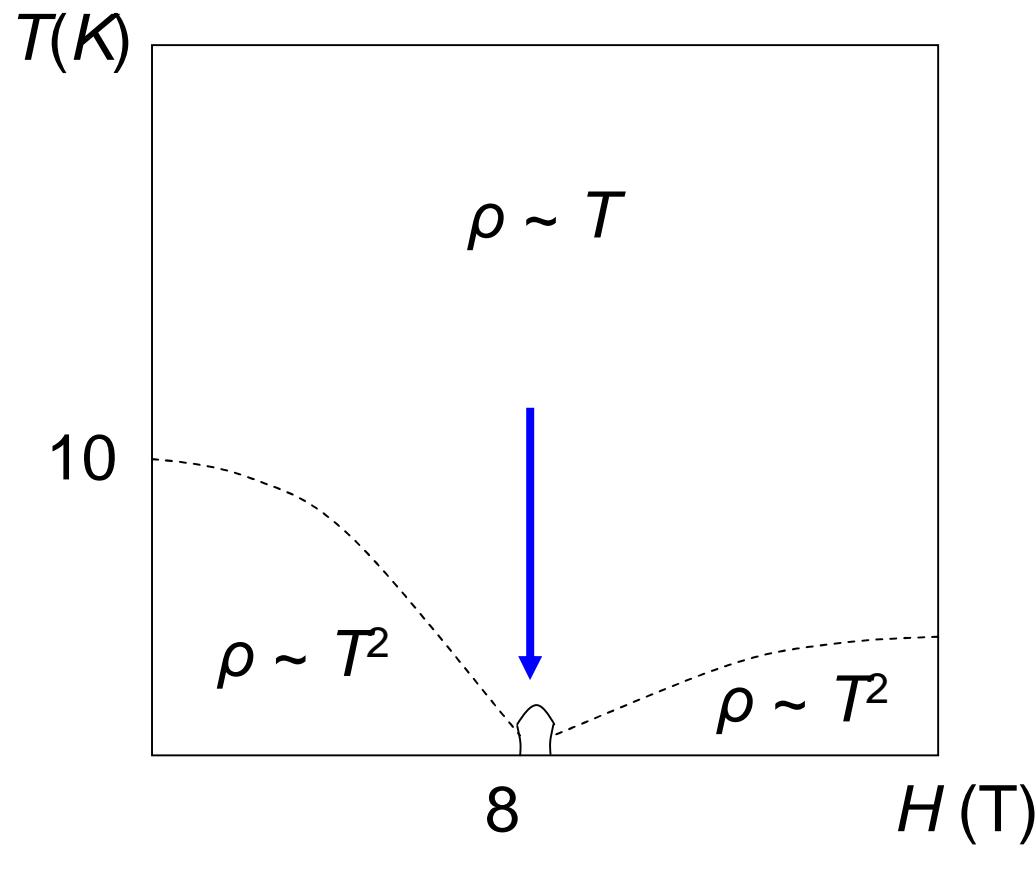
Fermions:  $C = \gamma T$

$$\therefore S(T') = \gamma T' = C(T')$$

Consistent with a mass diverging Fermi liquid (but no direct dHvA observation of a strongly field-dependent mass).

See also L.J. Zhu et al., *Phys. Rev. Lett.* **91**, 066404 (2003)

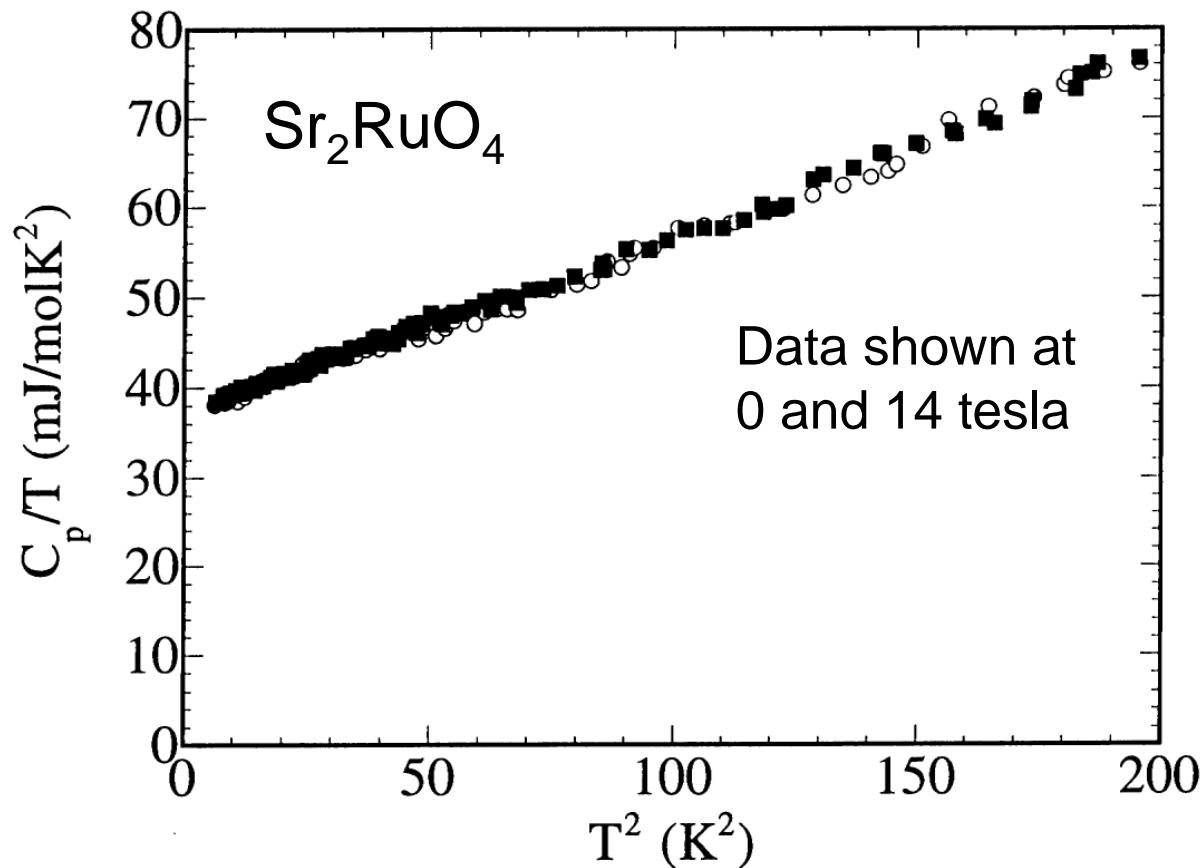
## Logarithmically diverging $C/T$ above the critical field



**Conclusion** – the overall phase diagram of  $Sr_3Ru_2O_7$  bears the main qualitative hallmarks of quantum criticality in the vicinity of metamagnetism.

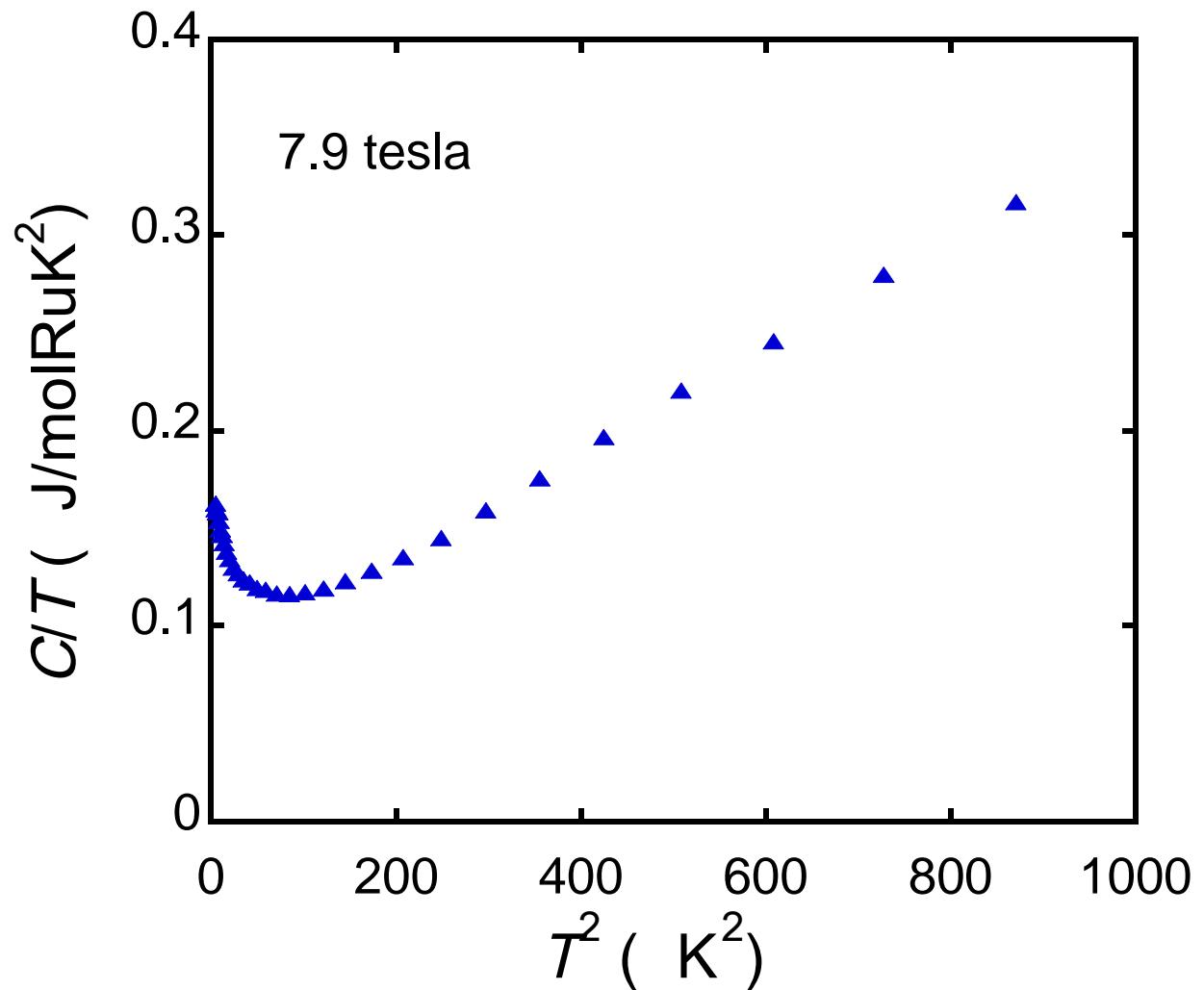
# What is the root of this logarithmic divergence?

Consider the total  $C/T$  in a related system that is a conventional Fermi liquid

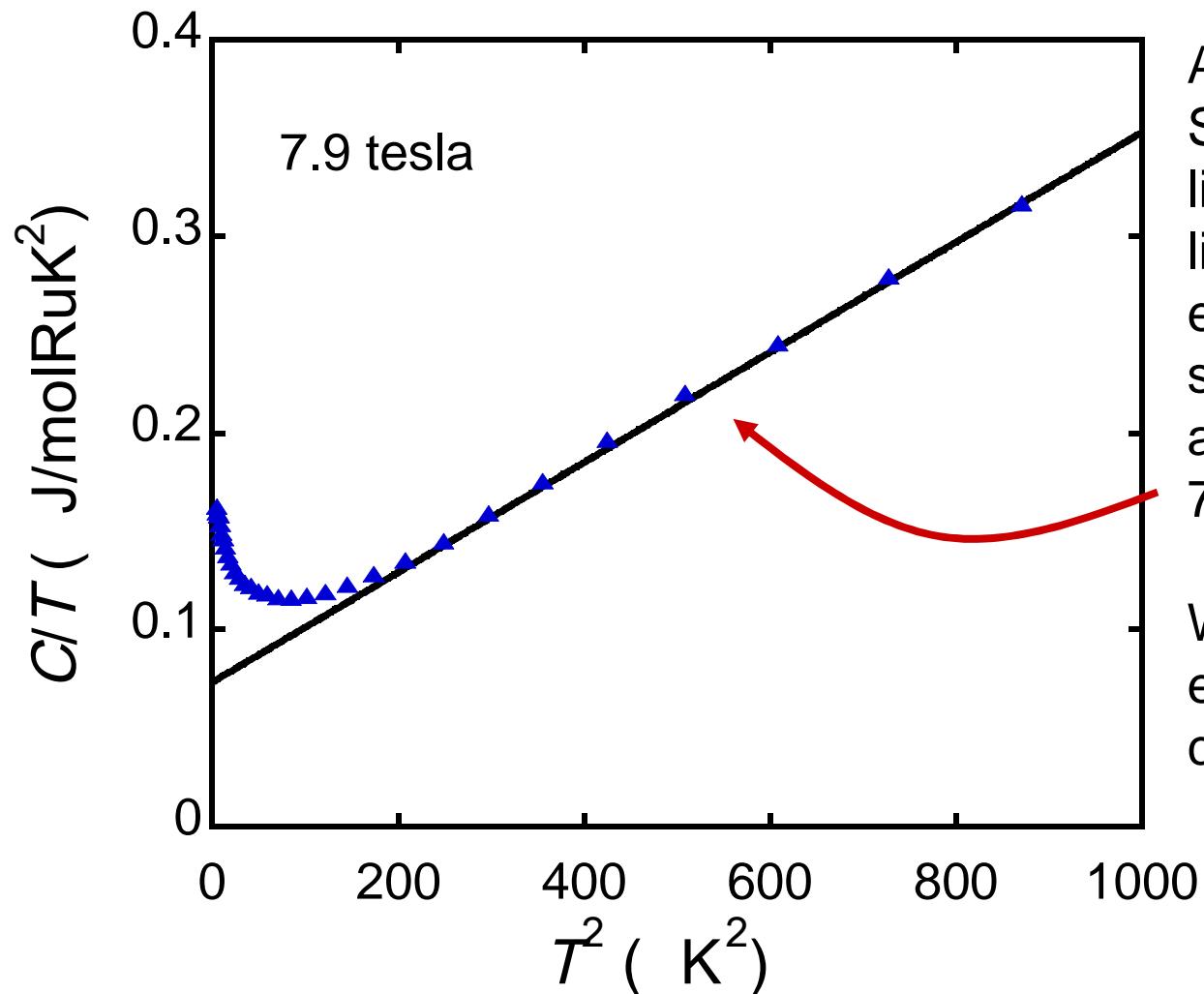


A.P. Mackenzie *et al.*, J. Phys. Soc. Jpn. **67**, 385 (1998)

## Contrast with $\text{Sr}_3\text{Ru}_2\text{O}_7$ at the critical field



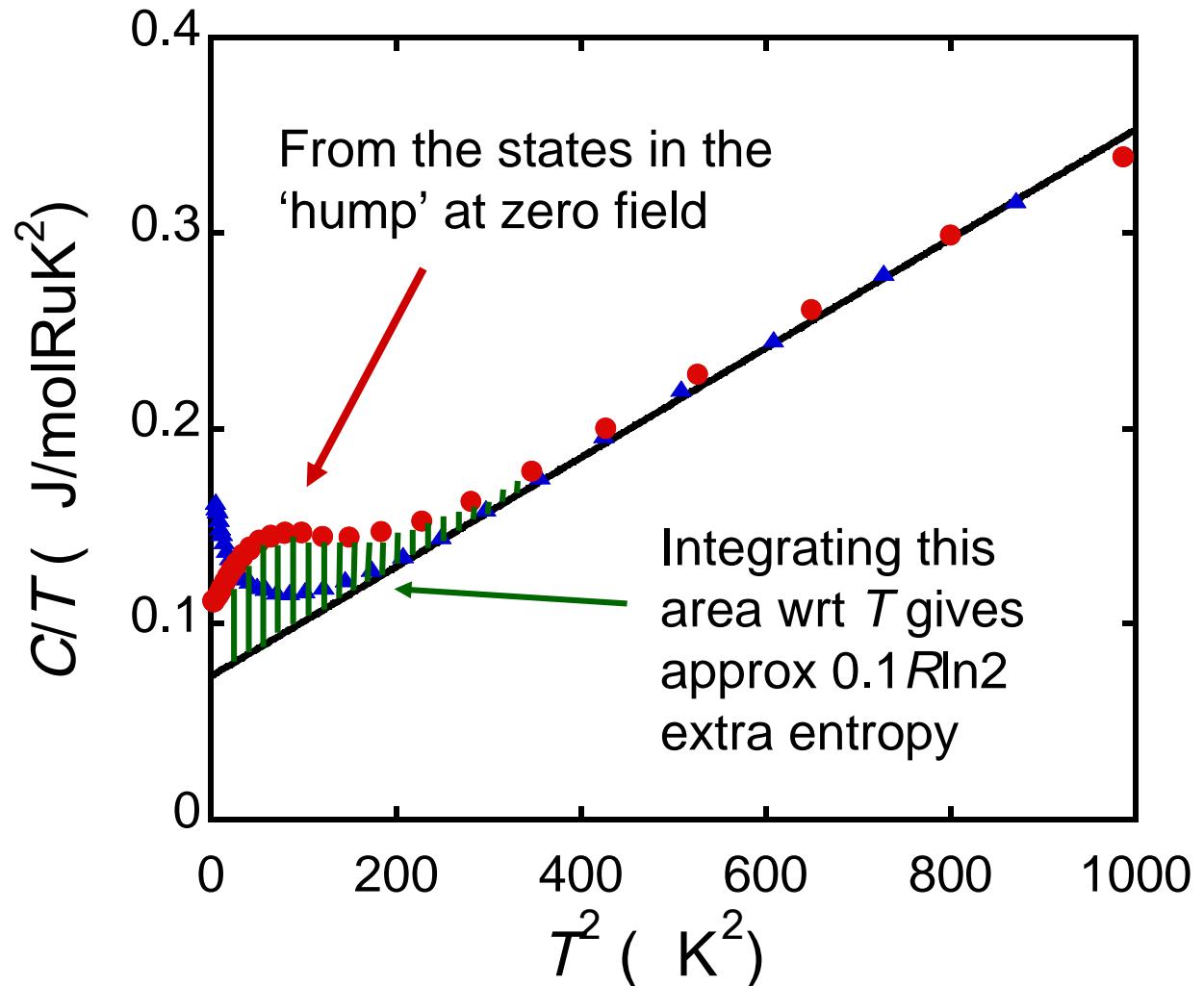
## Contrast with $\text{Sr}_3\text{Ru}_2\text{O}_7$ at the critical field



Above  $\sim 15 \text{ K}$ ,  
 $\text{Sr}_3\text{Ru}_2\text{O}_7$  looks  
like a Fermi  
liquid with an  
electronic  
specific heat of  
approximately  
 $75 \text{ mJ/molK}^2$ .

Where did the  
extra states  
come from?

## Contrast with $\text{Sr}_3\text{Ru}_2\text{O}_7$ at the critical field



## Towards a microscopic understanding in $\text{Sr}_3\text{Ru}_2\text{O}_7$

Key question seems to be the microscopic origin of the 10K energy scale.

It is NOT, apparently, a rigid band feature through which one simply Zeeman shifts.

*K. Iwaya et al., Phys. Rev. Lett. **99**, 057208 (2007)*

*J. Farrell et al., Phys. Rev. B **78**, 180409 (2008)*

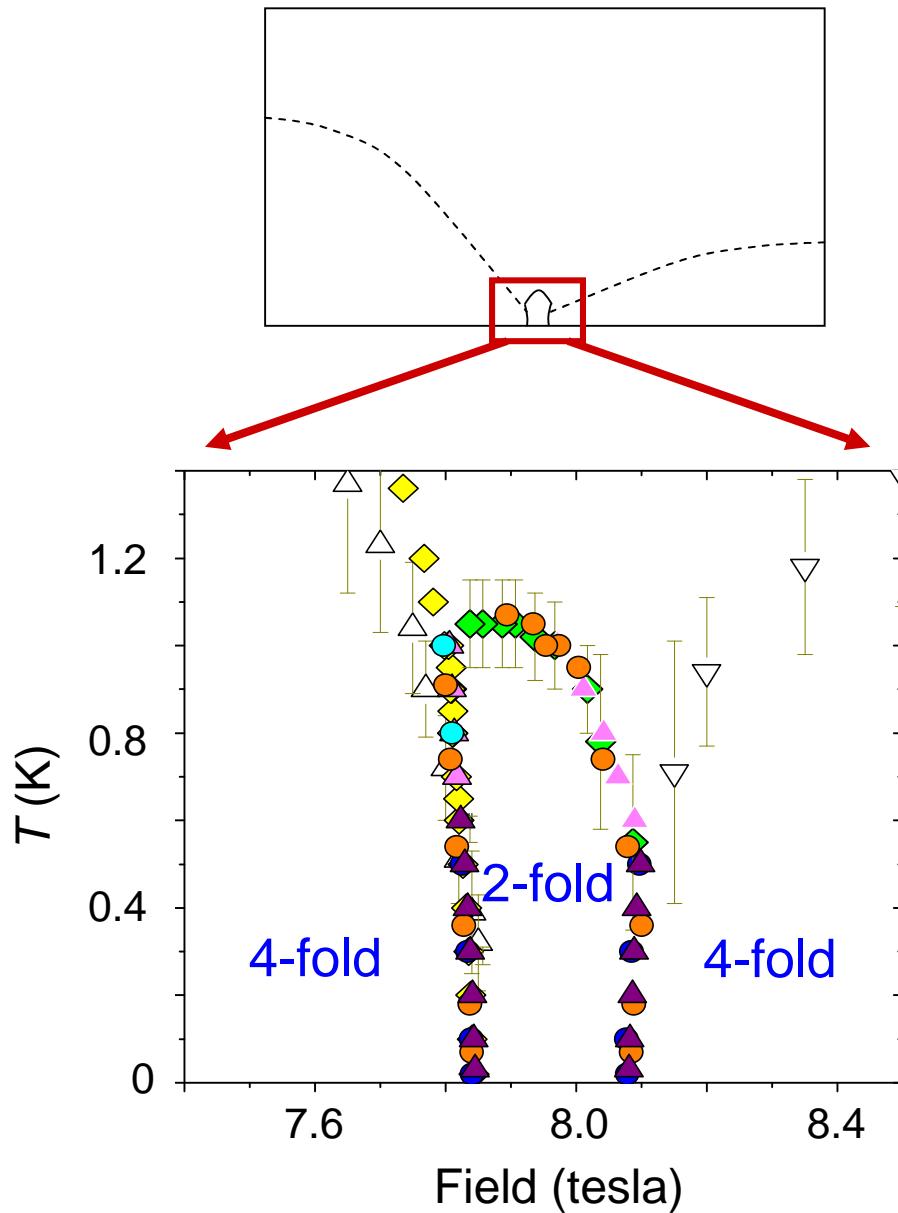
Spin-orbit coupling almost certainly plays a role.

*e.g. W.C. Lee and C. Wu, preprint (2010)*

# The low temperature, purity dependent nematic phase

Critical mean free path for observation of phase:  
1000 Å.

Equivalent scattering rate  
 $\sim T_c \Rightarrow$  phase is anisotropic in  $k$ -space



S.A. Grigera et al.,  
Science 306, 1154  
(2004).

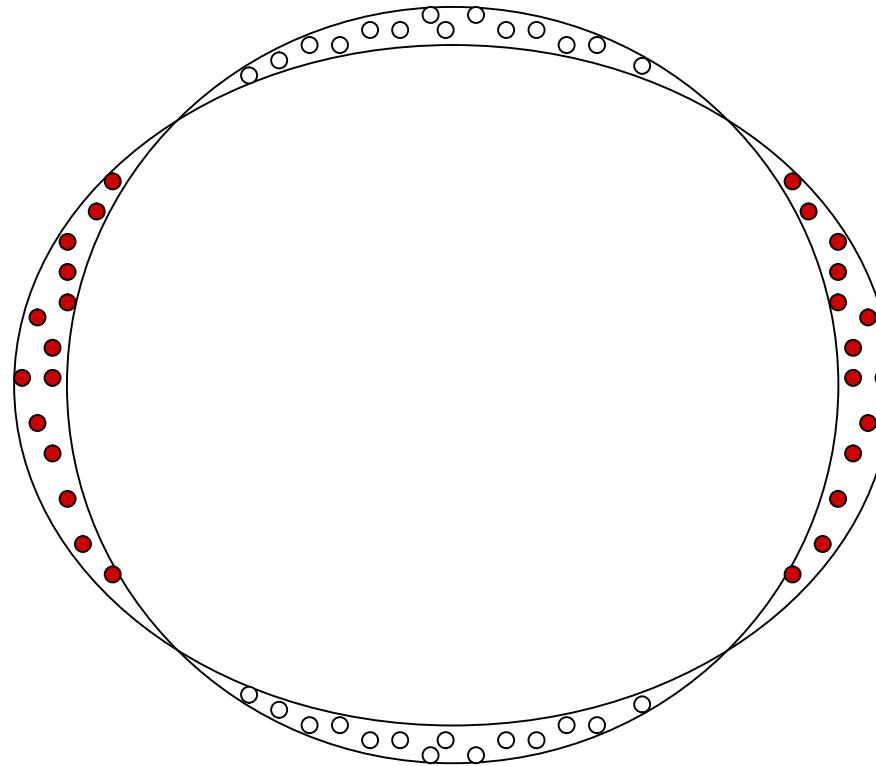
P. Gegenwart et al.,  
Phys. Rev. Lett. 96,  
136402 (2006).

R.A. Borzi et al.,  
Science 315, 214  
(2007)

E. Fradkin et al.,  
arXiv:0910.4166;  
Ann. Rev. Cond. Matt.  
Phys. 1, 153 (2010).

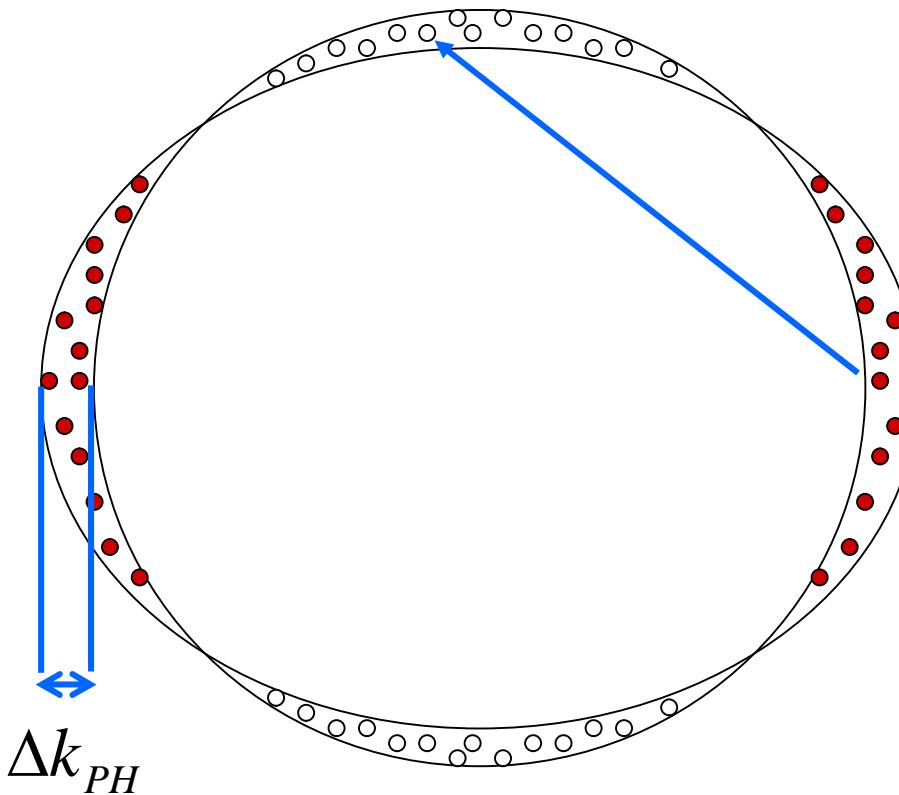
## Analogy with unconventional superconductivity

Imagine a weak ‘Pomeranchuk distortion’



$N_\ell = \sum_{\mathbf{k}} n(\mathbf{k}) \exp[i\ell \theta(\mathbf{k})]$  ; here  $\ell = 2$  and this is a ‘d-wave distortion in the particle-hole channel’

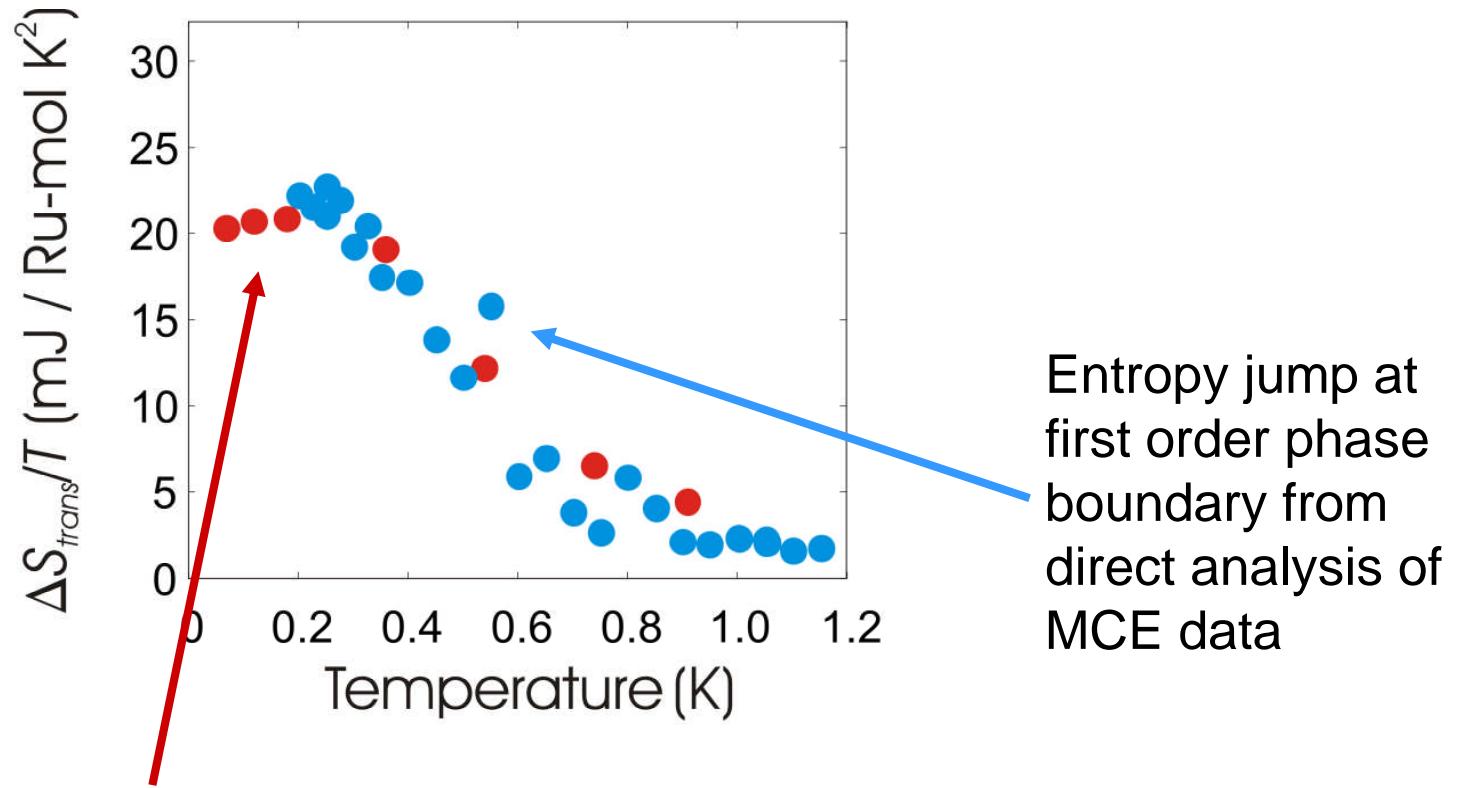
## Consequence: sensitivity to disorder



Condition for destruction of state:  $v_F \Delta k_{PH} \approx \Delta_{PH} \approx \frac{h}{\tau}$

Explicit calculation: *A.F. Ho and A.J. Schofield, EPL 84, 27007 (2008)*

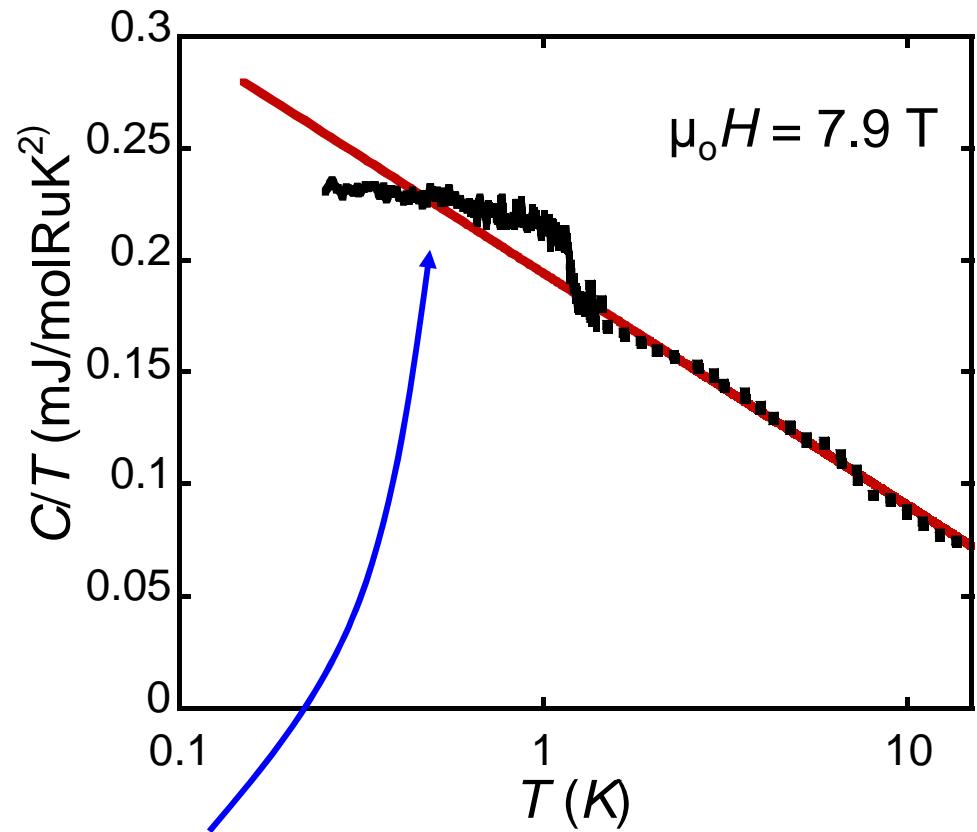
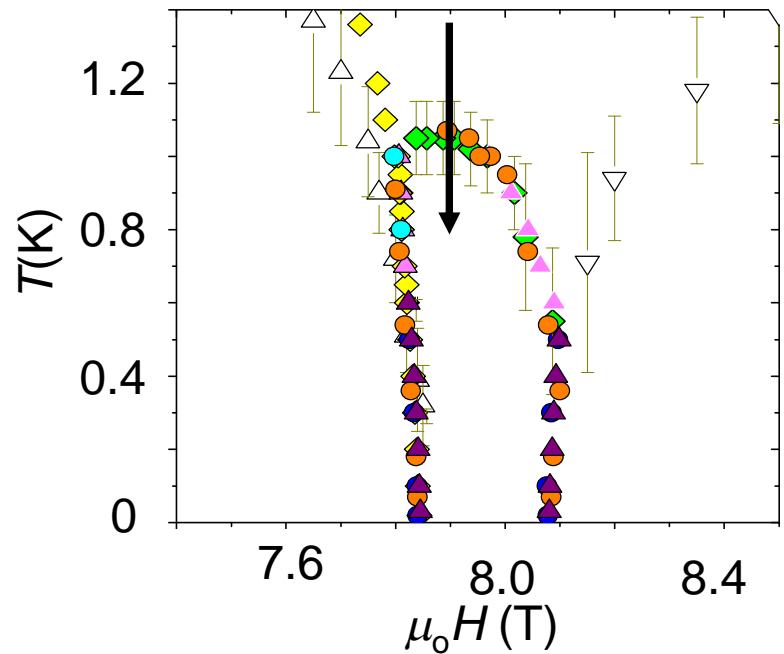
# Quantitative thermodynamic consistency via application of the Clausius-Clapeyron relationship for 1<sup>st</sup> order transitions



Entropy jump determined independently from magnetisation data and Clausius Clapeyron relation  $\frac{dH_c}{dT_c} = -\frac{\Delta S}{\Delta M}$

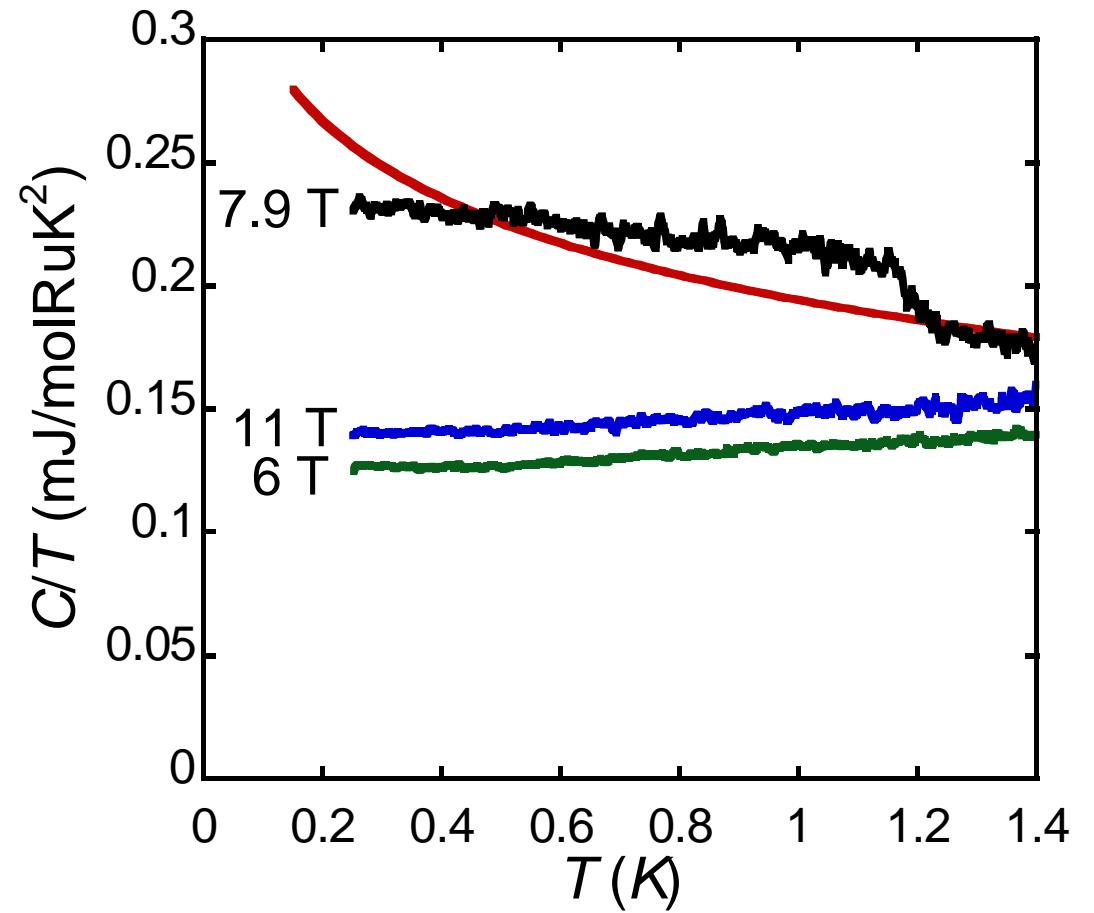
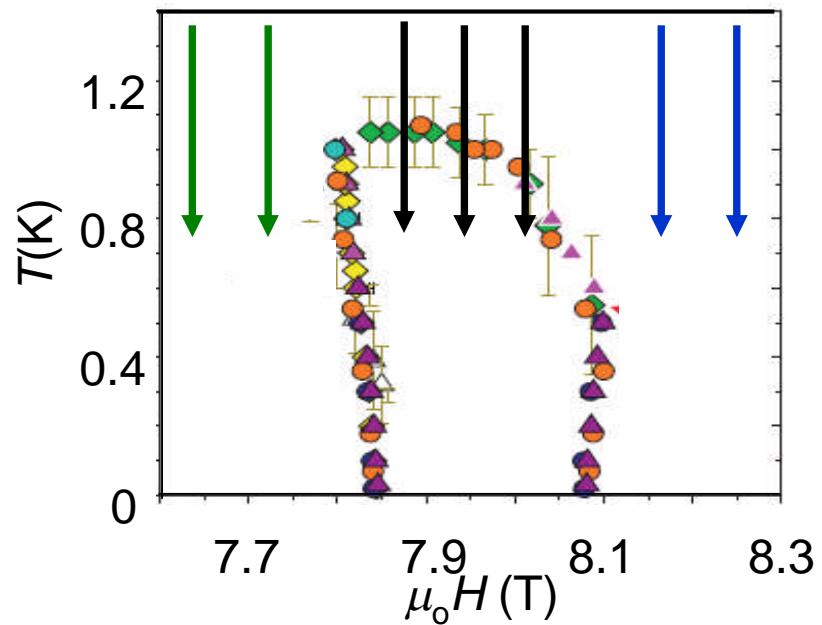
Unusually, the entropy is higher within the phase than outside it.

## Specific heat on cooling into the phase



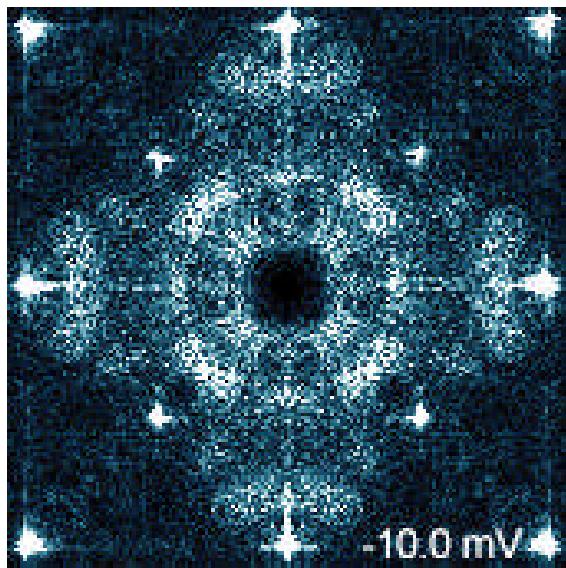
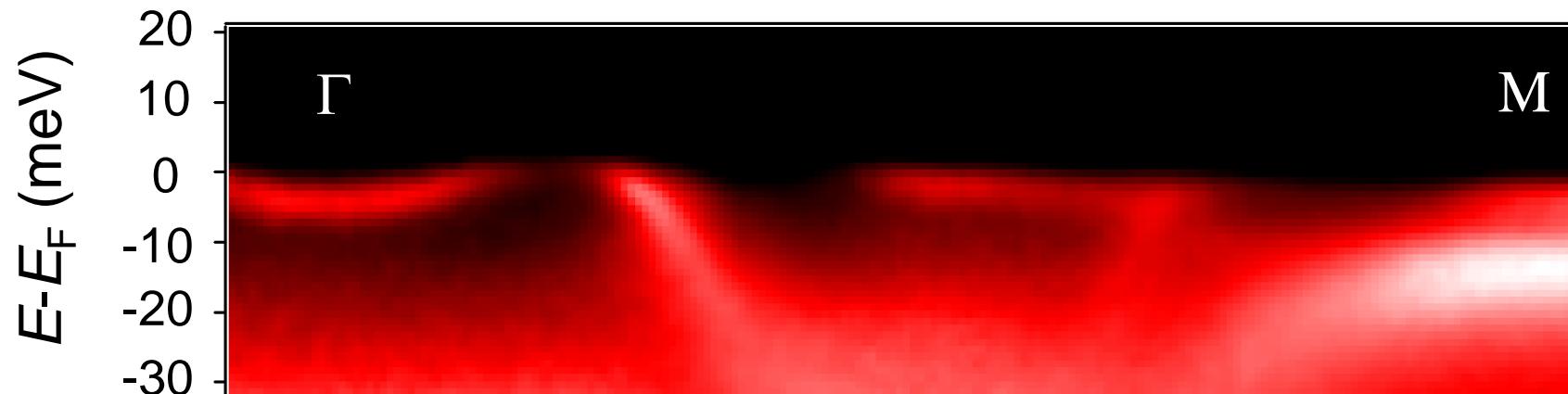
Even below  $T_c$ ,  $C/T$  keeps rising as  $T$  decreases

## Rising $C/T$ is a property of the phase and not its surroundings



Although the phase is metallic and shows quantum oscillations, it seems to be associated with degrees of freedom additional to those of a standard Fermi liquid.

# Policing surface spectroscopies of $\text{Sr}_3\text{Ru}_2\text{O}_7$



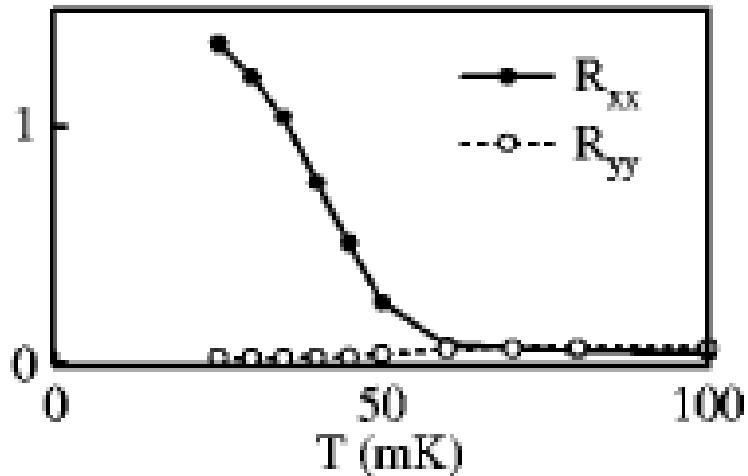
Bulk dHvA is consistent with characteristic velocities from Angle Resolved Photoemission and Spectroscopic Imaging Scanning Tunneling Microscopy.

A. Tamai *et al.*, *Phys. Rev. Lett.* **101**, 026407 (2008).

J. Lee *et al.*, *Nature Physics* **11**, 800 (2009).

W.C. Lee *et al.*, *Phys. Rev. B* **81**, 184403 (2010).

# Policing the increasing study of electronic nematicity



- Theory: *S.A. Kivelson et al., Nature 393, 550 (1998).*  
*S. Raghu et al., Phys. Rev. B 79, 214402 (2009).*  
*A.M. Berridge et al., Phys. Rev. Lett. 102, 136404 (2009).*
- 2DEGs: *M.P. Lilly et al., Phys. Rev. Lett. 82, 394 (1999).*

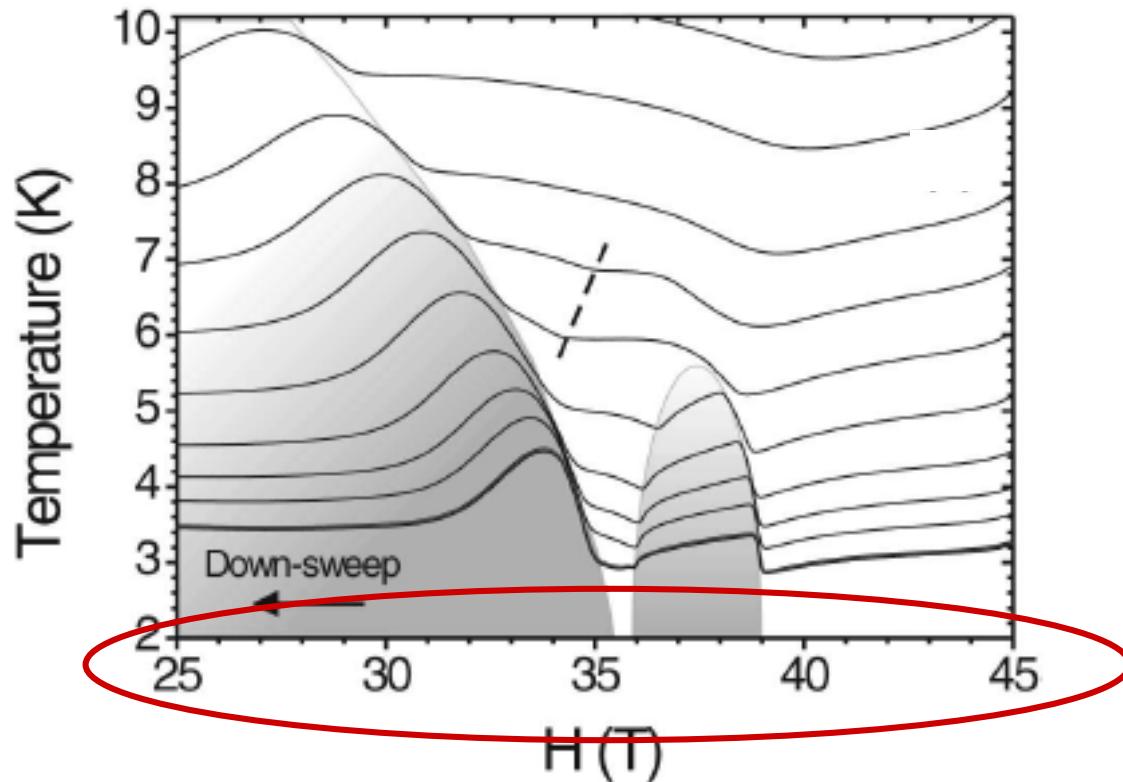
Cuprates: *Y. Ando et al., Phys. Rev. Lett. 88, 137005 (2002).*  
*Y. Kohsaka et al., Science 315, 1380 (2007).*  
*V. Hinkov et al., Science 319, 597 (2008).*  
*R. Daou et al., Nature 463, 519 (2010).*

Pnictides: *T.M. Chuang et al., Science 327, 181 (2010).*  
*J.H. Chu et al., arXiv:1002.3364 (2010).*

$\text{Sr}_3\text{Ru}_2\text{O}_7$  is unique (to date) in giving access to detailed thermodynamic information relevant to this problem.

## Comparison with metamagnetic *f*-electron systems

Reviews: *H. von Löhneysen et al., Rev. Mod. Phys.* **79**, 1015 (2007)  
*G.R. Stewart, Rev. Mod. Phys* **78**, 743 (2006)



*M. Jaime et al., Phys. Rev. Lett.* **89**, 287201 (2002)

*N. Harrison et al., Phys. Rev. Lett.* **90**, 096402 (2003)

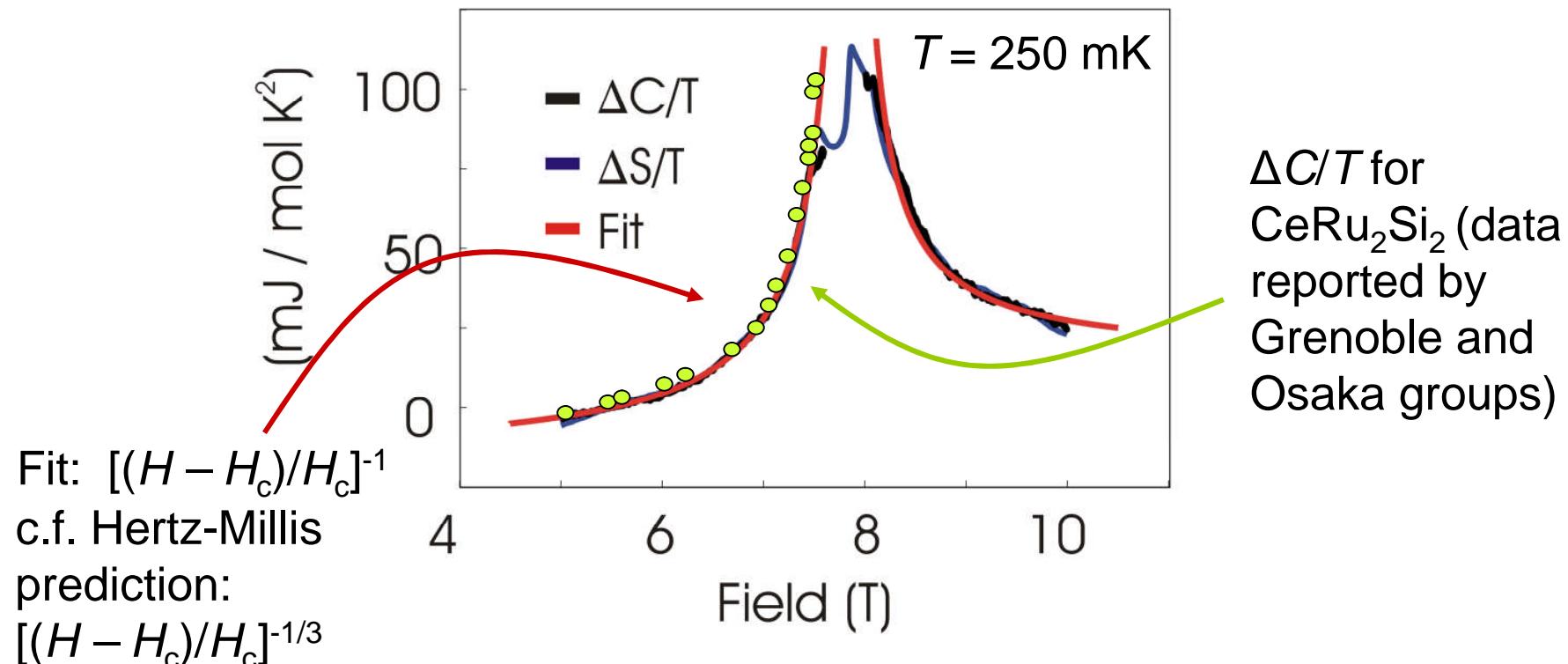
Also report of nematicity in  
hidden order phase  
*Matsuda group preprint*

$\text{CeRu}_2\text{Si}_2$  *Y. Aoki et al., JMMM* **177**, 271 (1998).

*J. Flouquet et al., Physica B* **319**, 251 (2002).

*F. Weickert et al., Phys. Rev. B* **81**, 134438 (2010).

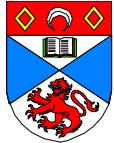
## Field dependence of $C$ , $S$ is surprisingly strong



Also, the scale of the entropy is interesting: the entropy by  $T_c$  of the nematic phase is ~5% of Rln2, similar to that at  $T_c$  in quite a wide range of unconventional superconductors [Y.E. Yang *et al.*, *Nature* **454**, 611 (2008)]

Is there something that we are missing with current approaches?

S.A. Hartnoll *et al.*, *Phys Rev B* **76**, 144502 (2007)



## Conclusions

1.  $\text{Sr}_3\text{Ru}_2\text{O}_7$  provides the opportunity to test and refine a number of modern ideas about quantum criticality and phase formation
2. The comparison with *f*-electron physics provides challenges and insights
3. High purity crystals and thermodynamic measurements are good for you!