



The Abdus Salam
International Centre for Theoretical Physics



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Workshop on Principles and Design of Strongly Correlated Electronic Systems

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Bipartite Elementary Excitations in a Two-dimensional Quantum Spin Liquid

Yuji MATSUDA

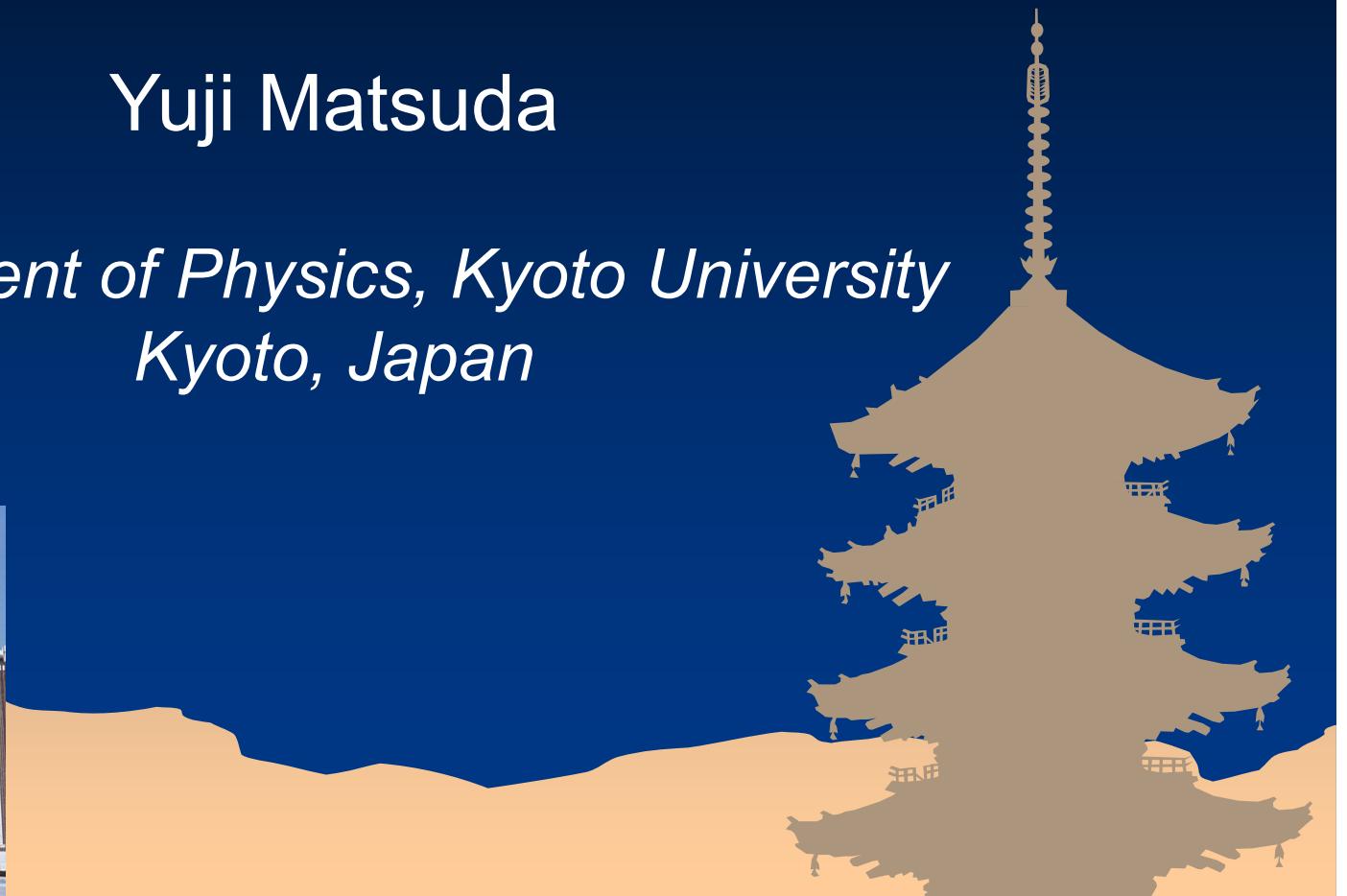
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Elementary excitations in a two-dimensional candidate quantum spin liquid



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Collaborators



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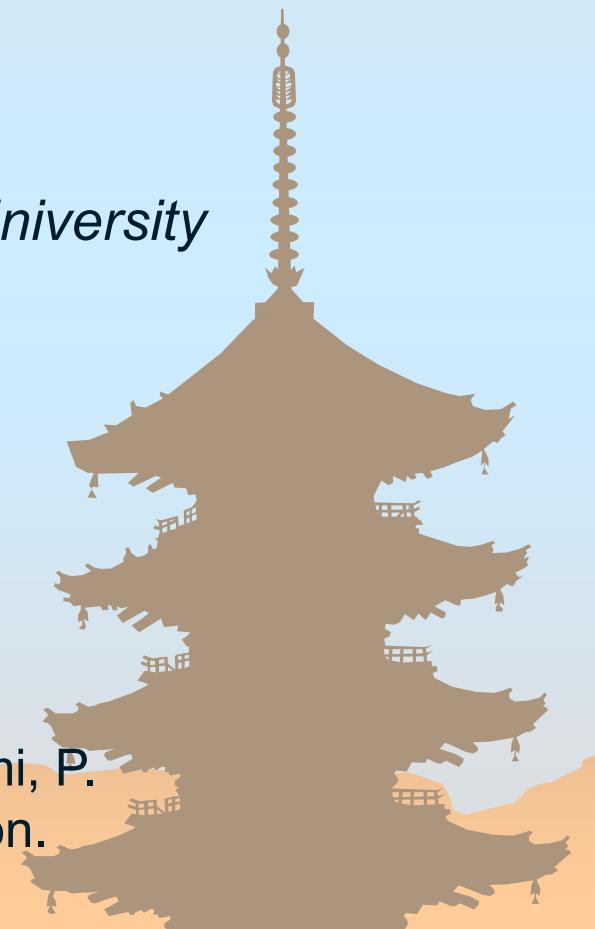


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We thank S. Fujimoto, K. Kanoda, H. Katsura, N. Kawakami, P. A. Lee, N. Nagaosa and G. Misguich for valuable discussion.



Outline

1. Introduction
2. A possible quantum spin liquid state of 2D triangular lattices in organic insulators
$$\kappa\text{-}(\text{BEDT-TTF})_2\text{Cu}_2(\text{CN})_3 \quad (\text{ET})$$
$$\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2 \quad (\text{MIT})$$
3. Highly unusual elementary excitations in a QSL state
4. Comparison between experiment and theory
5. Summary

M.Yamashita, Y.M. *et al.* Nature Phys. **5**, 44 (2009)

M. Yamashita, Y.M. *et al.* Science **328**, 1246 (2010)

Introduction

Exotic spin state

Liquid, Ice, Nematic, Chiral, ...

Spin Liquids are states which do not break any simple symmetry: neither spin-rotational symmetry nor lattice symmetry.

Quantum spin liquid (QSL)

A novel state of matter where strong quantum fluctuations destroy the long-range magnetic order even at $T=0$

QSL has attracted much theoretical attention since its proposal in 1973.

The problem of the quantum spin liquid may have close relation to the high- T_c problem

P.W. Anderson, Mater. Res. Bull. 8, 153 (1973)
P.W. Anderson, Science 235, 1196 (1987)

Introduction : Quantum spin liquid (QSL)

One dimension

Notion of QSL is firmly established

Spinon excitation ($S=1/2, e=0$)

Two and three dimensions

Geometrical frustration

Classical A large ground-state degeneracy

Quantum Quantum fluctuation lifts the degeneracy and a QSL ground state may appear

There are few candidates of the real materials.

2D triangular lattice

^3He on graphite

Organic insulators

κ -(BEDT-TTF)₂Cu₂(CN)₃
EtMe₃Sb[Pd(dmit)₂]₂

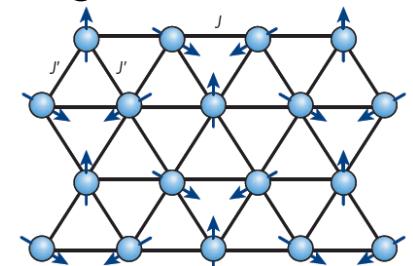
2D kagome lattice

ZnCu₃(OH)₆Cl₂ (Herbertsmithite)
BaCu₃V₂O₈(OH)₂ (Vesigniete)

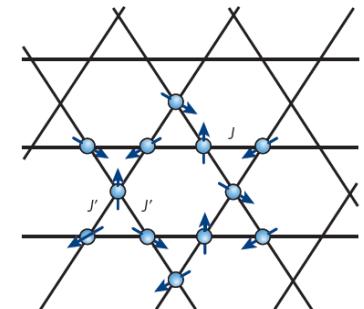
Hyperkagome

Na₄Ir₃O₈

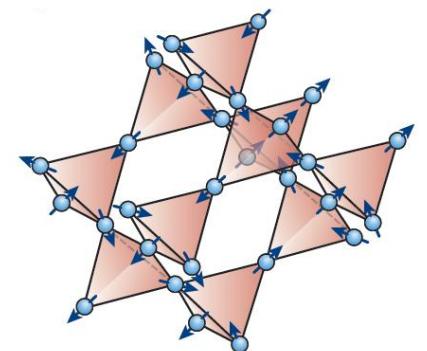
Triangular lattice



kagome lattice



Pyrochlore lattice

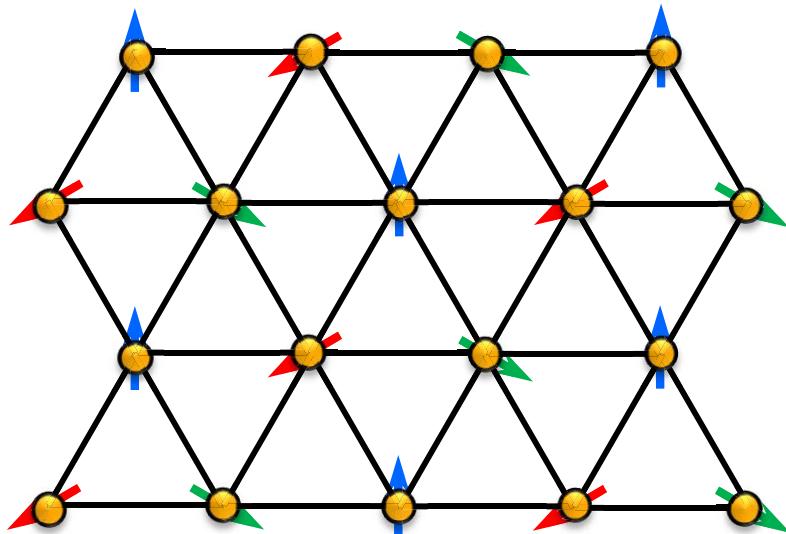


L. Balents, Nature 464, 199 (10)

2D triangular lattice

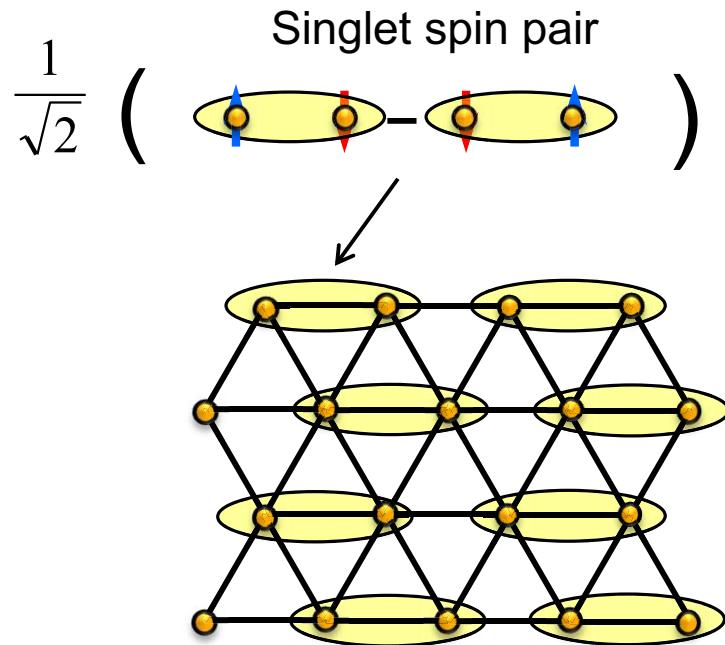
The 120 degrees antiferromagnetic Néel structure

Three sublattice Néel state



2D triangular lattice

Valence Bond Solid

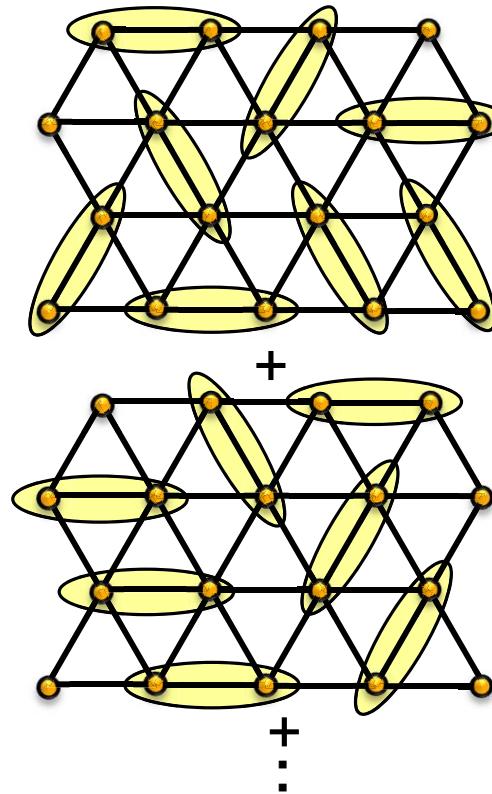


Breaking of the lattice symmetry
Localized singlets
Long range order of singlet

Resonating Valence Bond (RVB) Liquid

Superposition of different configurations

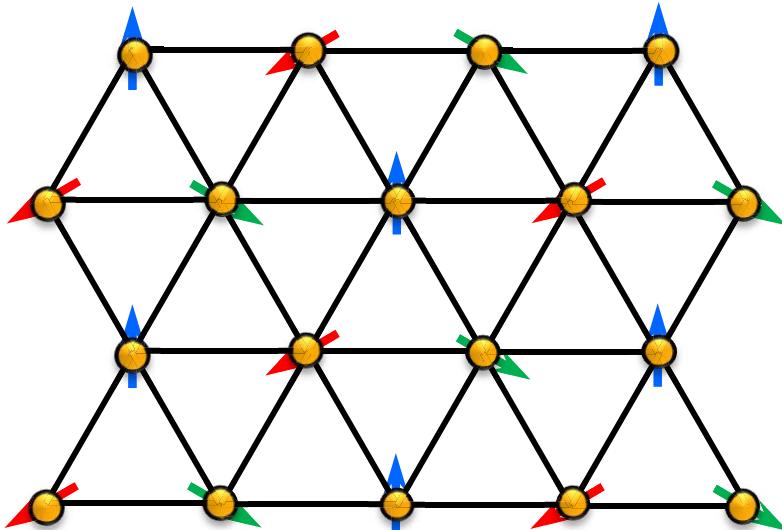
Resonation between highly degenerated spin configurations leads to a liquid-like wavefunction.



No simple symmetry breaking

2D triangular lattice

Neel order at $T=0$ even for nearest Heisenberg model with $S=1/2$



Three sublattice N'eel state

D. Huse and V. Elser, PRL 60, 2531 (88)

B. Bernu, C. Lhuillier and L. Pierre, PRL 69, 2590 (92)

L. Capriotti, A. E.E. Trumper and S. Sorella, PRL 82, 3899 (99)

In real systems, the Neel order occurs at finite temperature due to small but finite interlayer interaction

Additional frustration that enhances the quantum fluctuation is necessary to realize a QSL.

Introduction

How can we identify a QSL in the experiments?

If no symmetry breaking (magnetic order) is observed down to very low temperatures, the system is assumed to be in a QSL state.

What is the elementary excitation of QSLs in the 2D triangular lattice?

Does a QSL host some exotic excitations?

Gapped or gapless?

Magnetic or nonmagnetic?

Localized or itinerant?

If itinerant, what is the statistics, fermion, boson or some exotic?

A wide range of experimental probes are available.

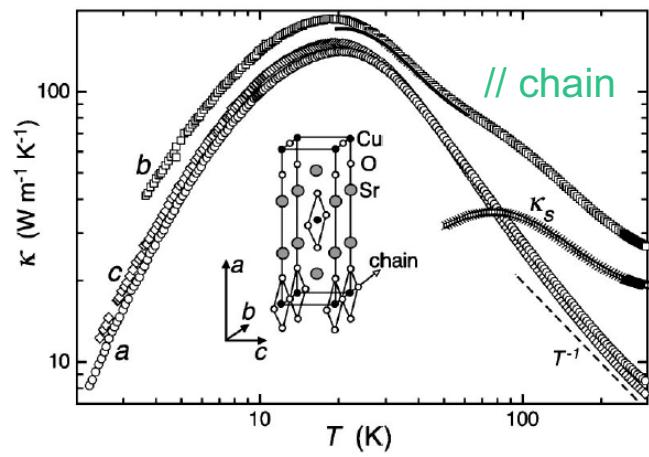
NMR, μ SR, Susceptibility, Torque . . .

Specific heat, Thermal conductivity . . .

What the thermal conductivity tells us

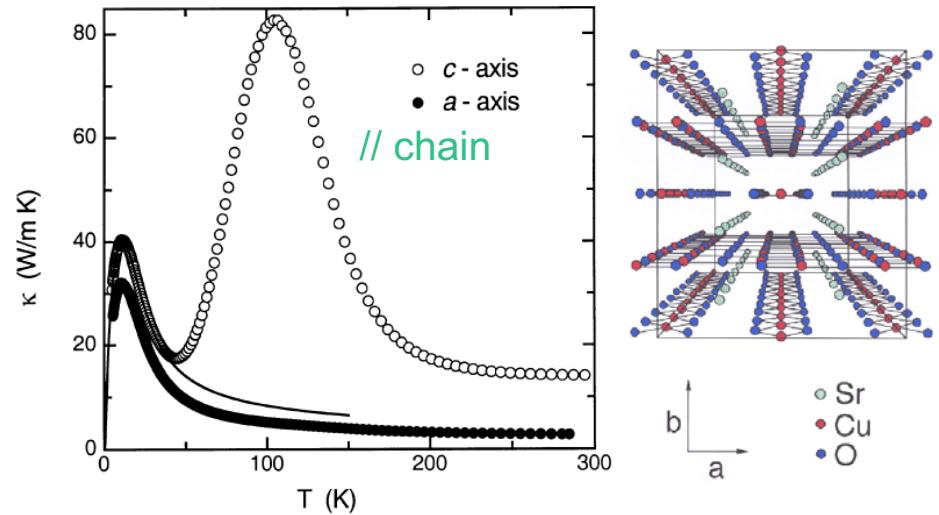
Thermal conductivity provides important information on the elementary excitations, similar to the electronic transport properties in metals.

1D Heisenberg $S=1/2$ Sr_2CuO_3



A.V. Sologubenko *et al.* PRB 62, R6108 (00)

Spin ladder compound $\text{Sr}_{12}\text{Ca}_2\text{Cu}_{24}\text{O}_{41}$



A.V. Sologubenko *et al.* PRL 84, 2714 (00)

Large heat transport by magnetic excitation (spinon) along the 1D chain

What the thermal conductivity tells us

Very powerful probe for *low-energy* and *itinerant* excitations

- ✓ Free from localized excitation coming from impurities
(such as free spins in χ , Schottky anomaly in C)
⇒ *Reliable down to mK temperatures*

$$\kappa_s = C_s v_s \ell_s$$

C_s specific heat

v_s velocity of excitation

ℓ_s mean free path of excitation

$$\kappa = \kappa_{spin} + \kappa_{phonon}$$

$$\kappa_{phonon} \sim T^3$$

Gapped or gapless?

Gapless spin liquid

$$\kappa_{spin} \sim \gamma T$$

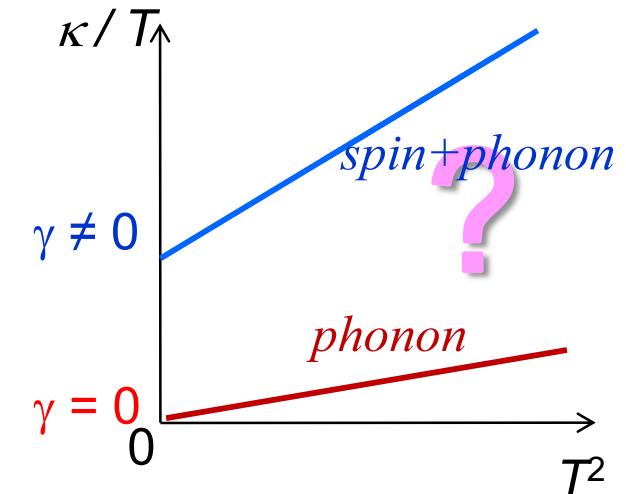
$$\kappa_{spin}/T \sim \gamma \neq 0$$

Gapped spin liquid

$$\gamma = 0$$

$$\kappa_{spin} \sim \exp(-\Delta/T)$$

Residual thermal conductivity
 κ_s/T at $T \rightarrow 0$ K



Finite κ/T at $T \rightarrow 0$ K immediately indicates the presence of gapless excitation

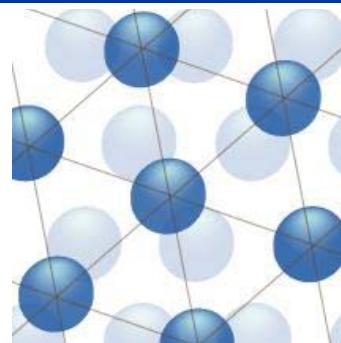
Magnetic or nonmagnetic?

Field dependence of κ_s

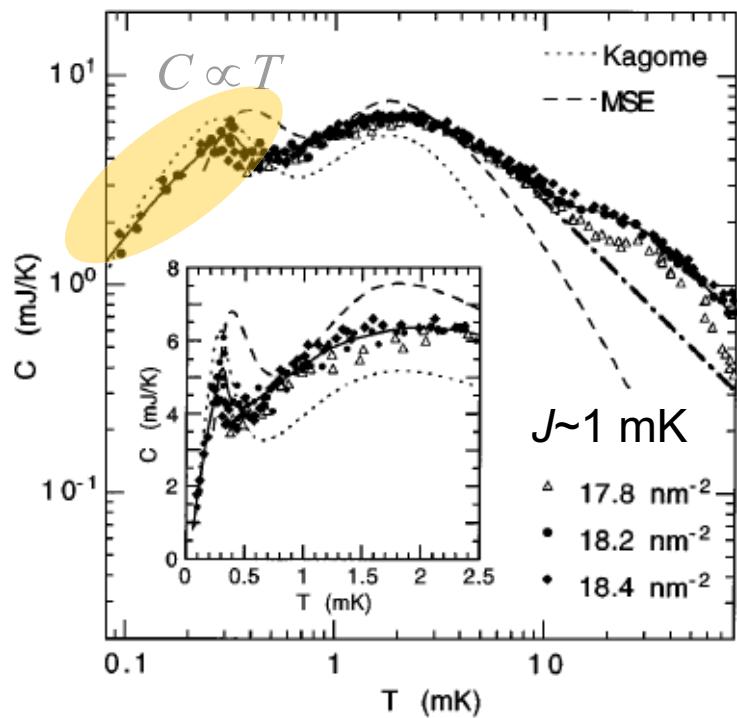
Localized or itinerant?

Magnitude of the mean free path ℓ_s

Spin liquid state in 2D ^3He on graphite



Specific heat of $^3\text{He}/\text{Graphite}$

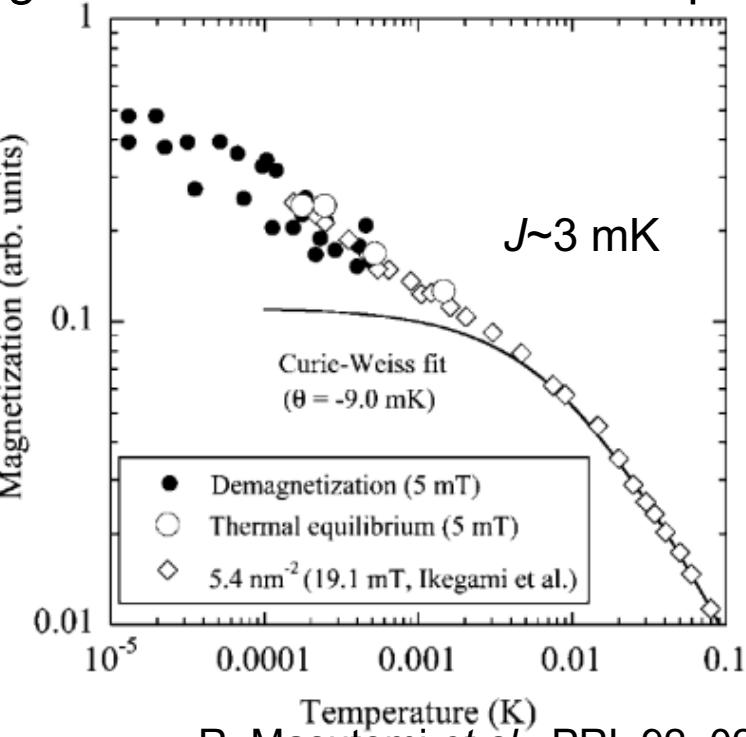


K. Ishida *et al.* PRL 79, 3451 (97)

Gapless down to $T \sim J/10$

“4/7 phase”
Triangular lattice formed by ^3He atom

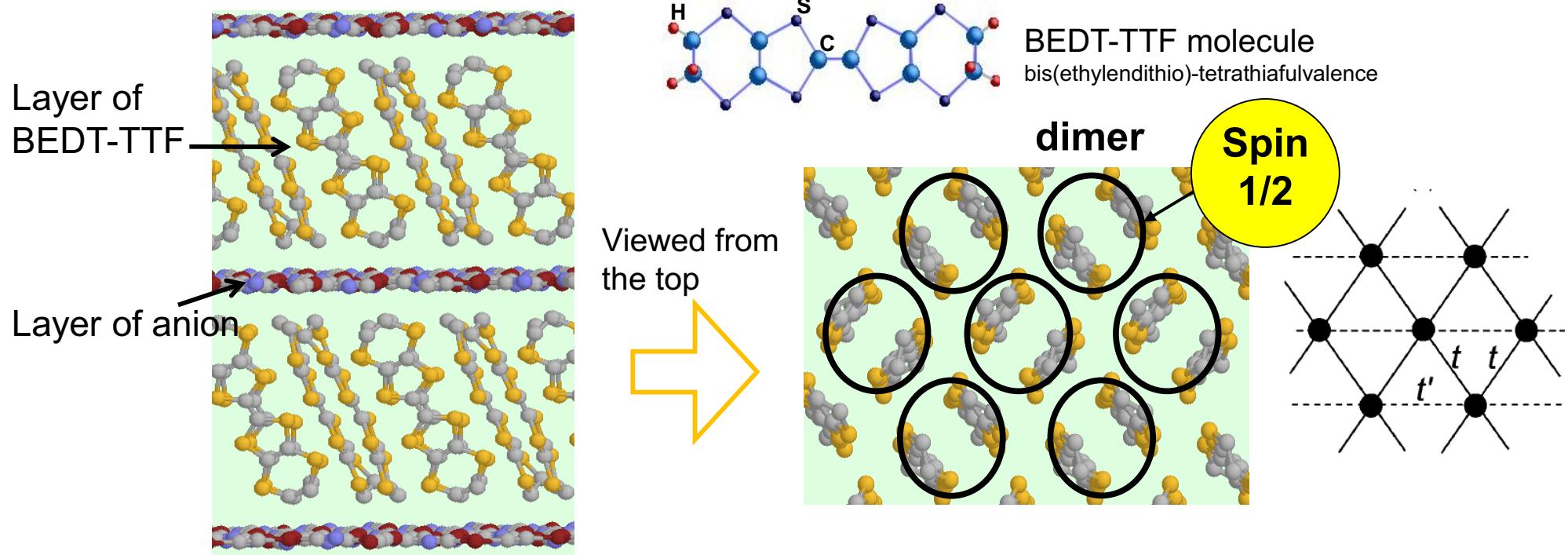
Magnetization of $^3\text{He}/\text{HD}/\text{HD}/\text{Graphite}$



R. Masutomi *et al.*, PRL 92, 025301 (04)

No spin gap down to $T \sim J/300$

κ -(BEDT-TTF)₂Cu₂(CN)₃

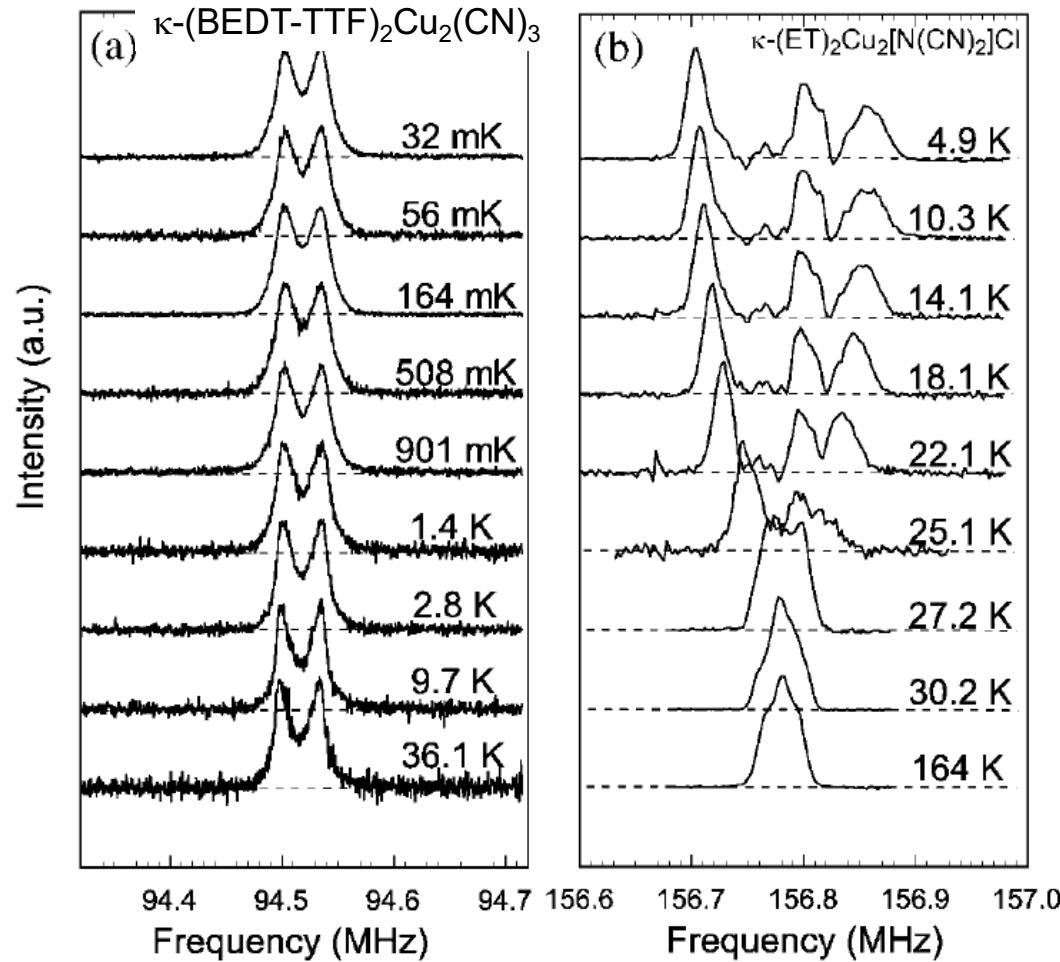


- Mott insulator : $t \sim 54.5$ meV, $t' \sim 57.5$ meV and $U \sim 448$ meV ($U/t \sim 8.2$)
- Pairs of BEDT-TTF molecule with spin $1/2$ form dimers arranged in a 2D triangular lattice in terms of transfer integrals t and t' between the dimers. ($t'/t = 1.06$. by Hückel Method)
- Superconductivity under pressure

κ -(BEDT-TTF)₂Cu₂(CN)₃

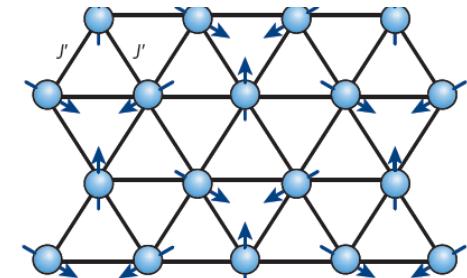
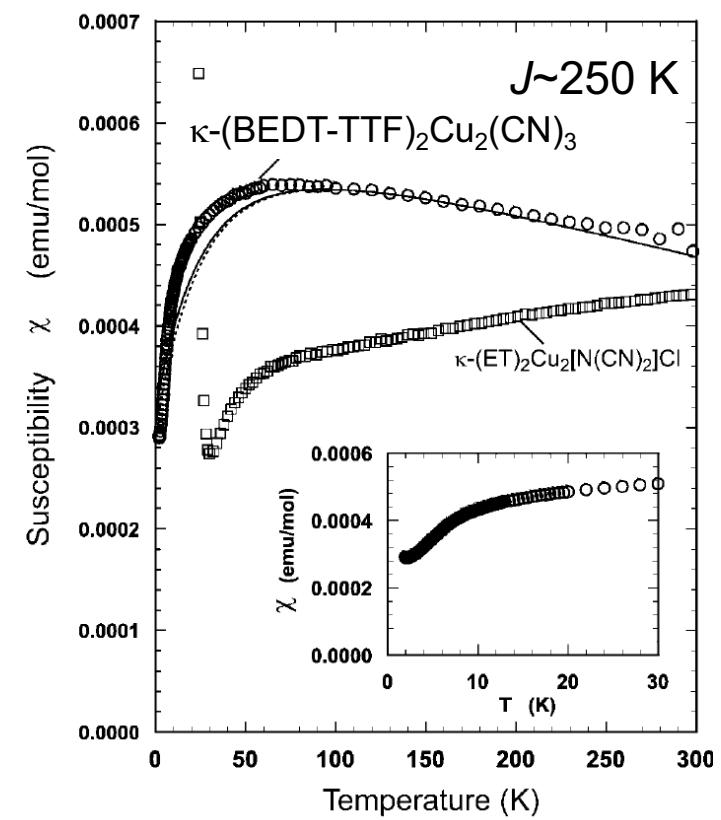
¹H NMR

No internal magnetic field



Y. Shimizu et al. PRL 91, 107001 (03)

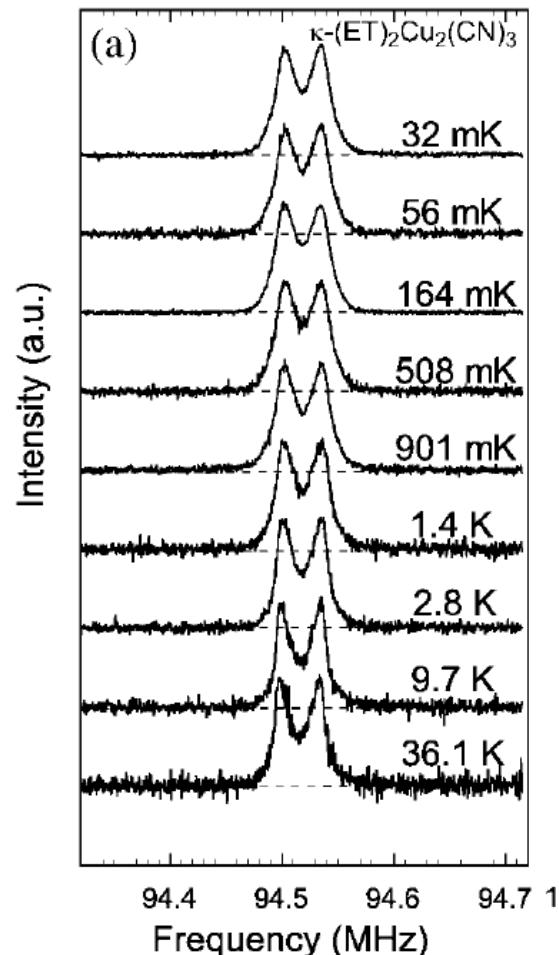
Magnetic susceptibility



κ -(BEDT-TTF)₂Cu₂(CN)₃

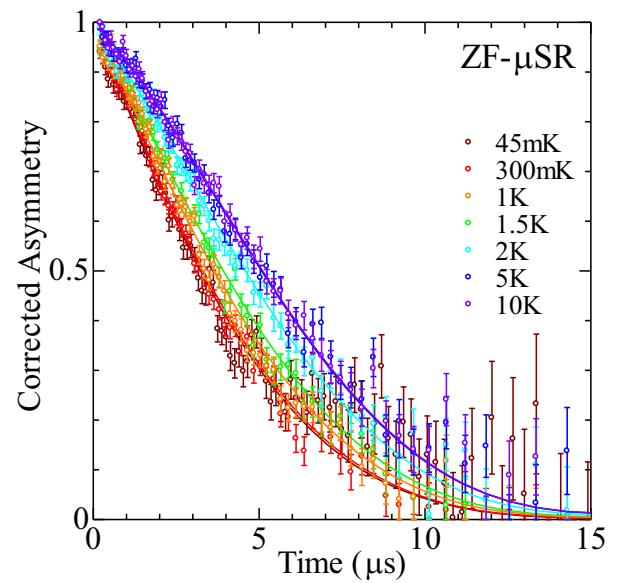
¹H NMR

No internal magnetic field

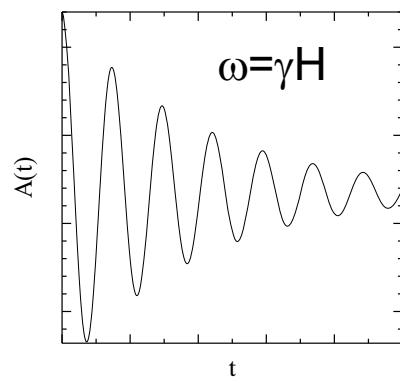


μ SR

No muon spin rotation



If magnetic order occurs,



T. Goto *et al.* a preprint (10)

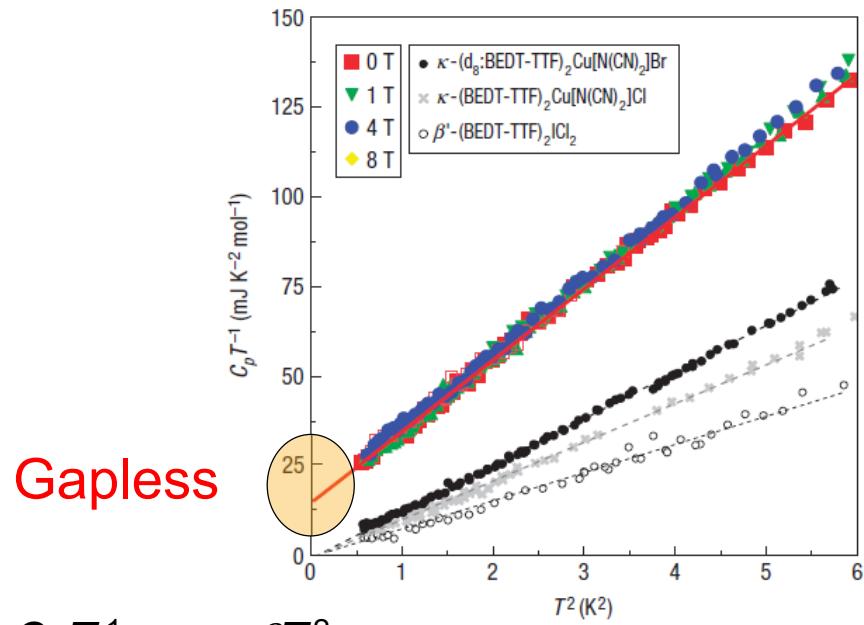
See also S. Oohira, *et al.*, JLTP **142** (2007)

No magnetic order down to \sim 20 mK ($\sim J/12,000$)

Y. Shimizu *et al.* PRL 91, 107001 (03)

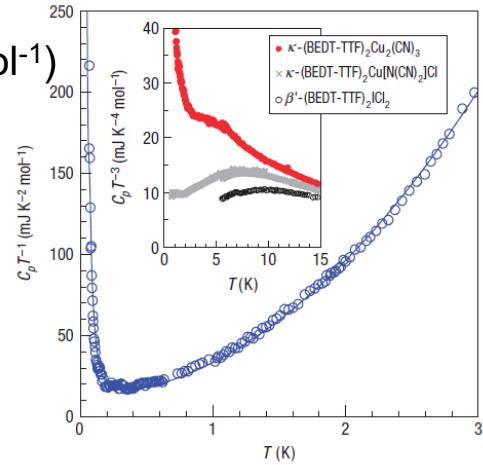
κ -(BEDT-TTF)₂Cu₂(CN)₃ : elementary excitation

Specific heat



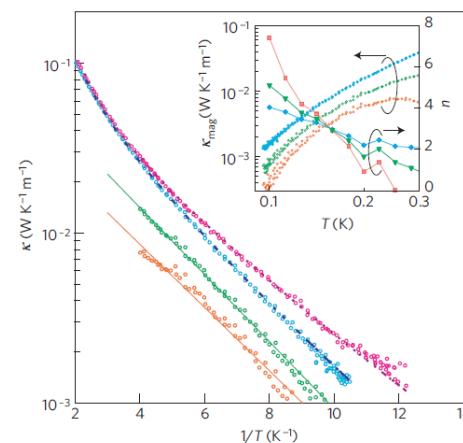
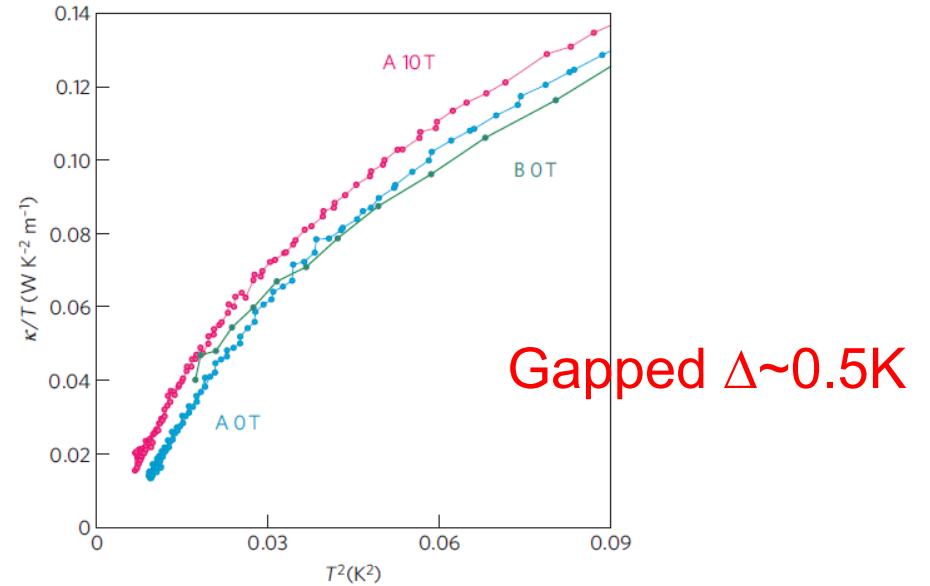
$$C_p T^{-1} = \gamma + \beta T^2$$

$$(\gamma \approx 13 \text{ mJ K}^{-2} \text{mol}^{-1})$$



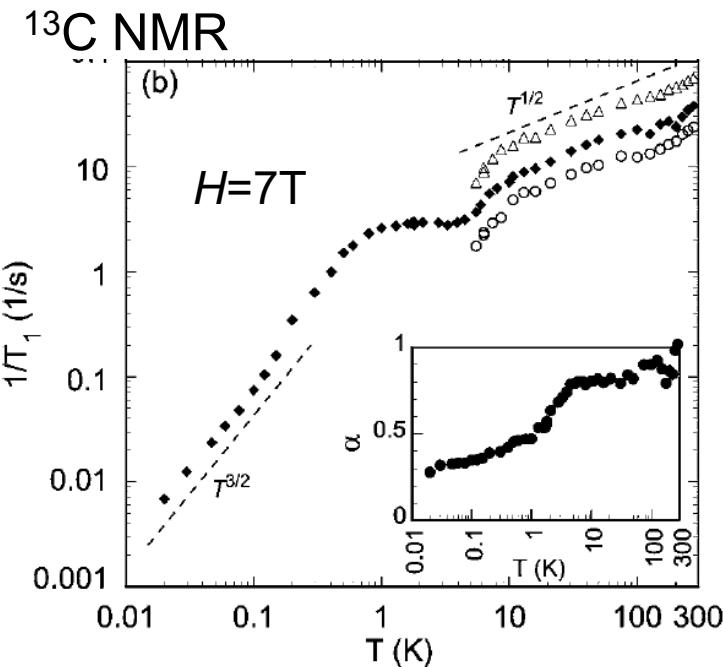
S. Yamashita *et al.* Nature Phys.4, 459 (08)

Thermal conductivity



M. Yamashita *et al.* Nature Phys.5, 44 (09)

κ -(BEDT-TTF)₂Cu₂(CN)₃ : inhomogeneity



$$-M(t)/M(\infty) = \exp[-(t/T_1)^\alpha]$$

Y. Shimizu *et al.* PRB 73, 140407 (06)

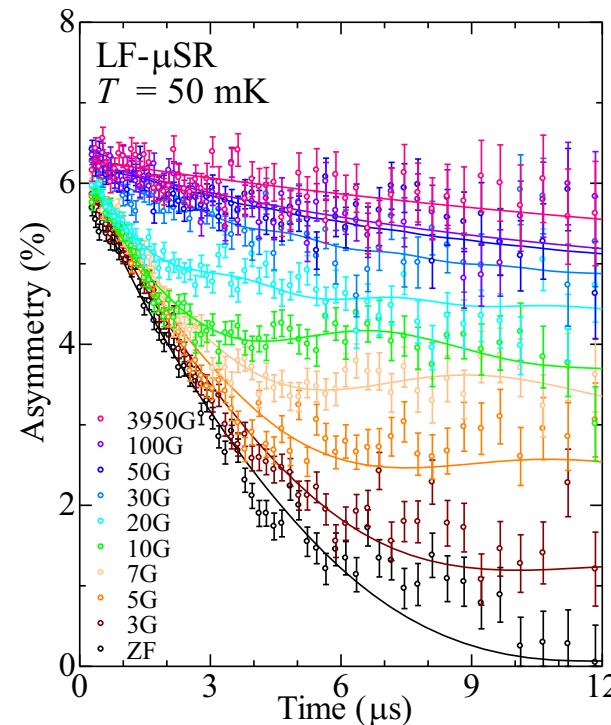
NMR recovery curve shows
stretched exponential

$\alpha < 0.5$ below 1K

Distribution of T_1

See also

A. Kawamoto *et al.* PRB 70, 060510 (04)



Relaxation curve
below 300 mK

two components

T. Goto *et al.*

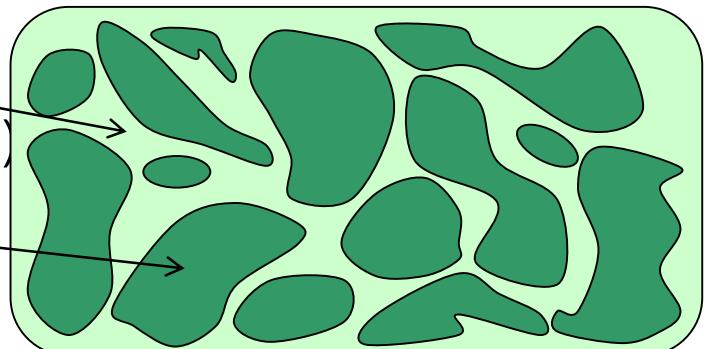
Microscopic phase separation between gapped and gapless regions

singlet region

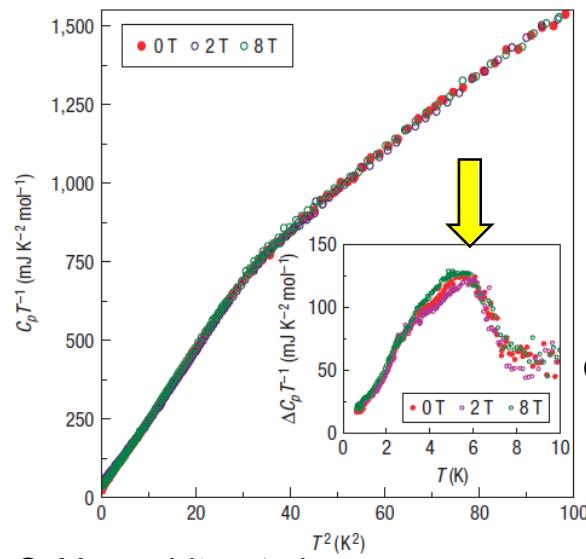
(non-magnetic gapped)

magnetic phase

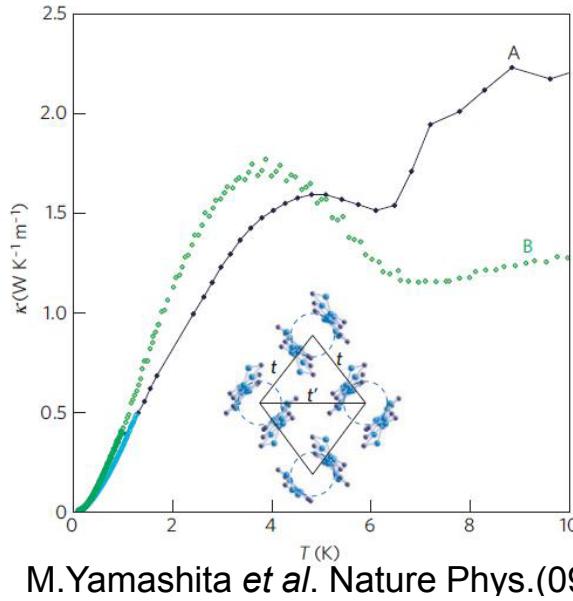
(gapless)



κ -(BEDT-TTF)₂Cu₂(CN)₃ : phase transition at 6 K

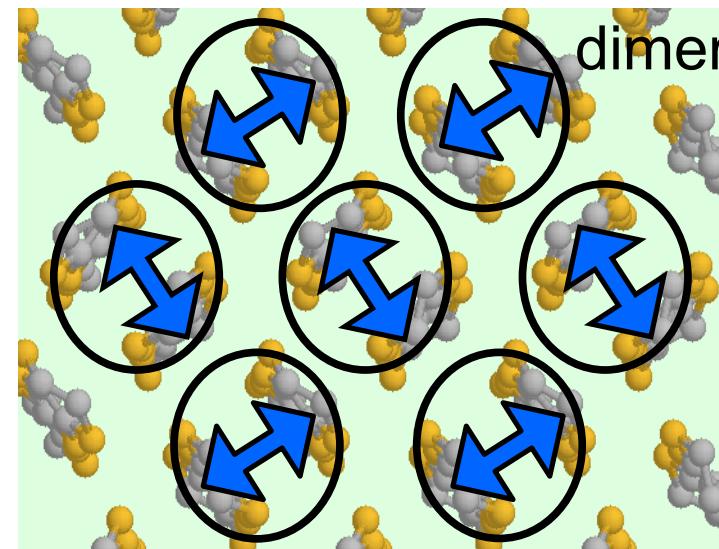
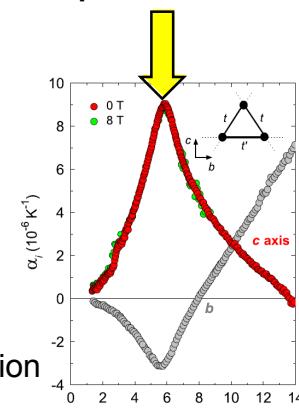


S. Yamashita et al. Nature Phys. (08)
Thermal conductivity

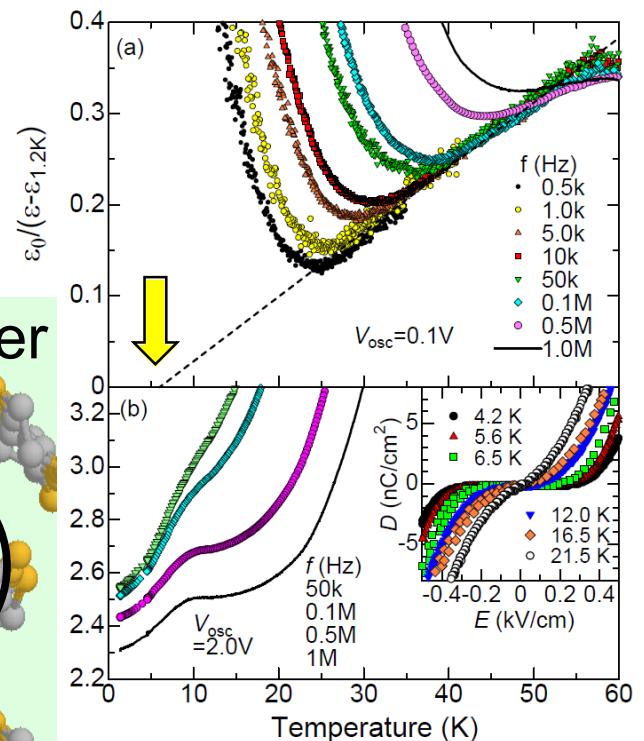


Thermal expansion

Charge disproportionation
within the dimer?



Frequency dependent dielectric constant

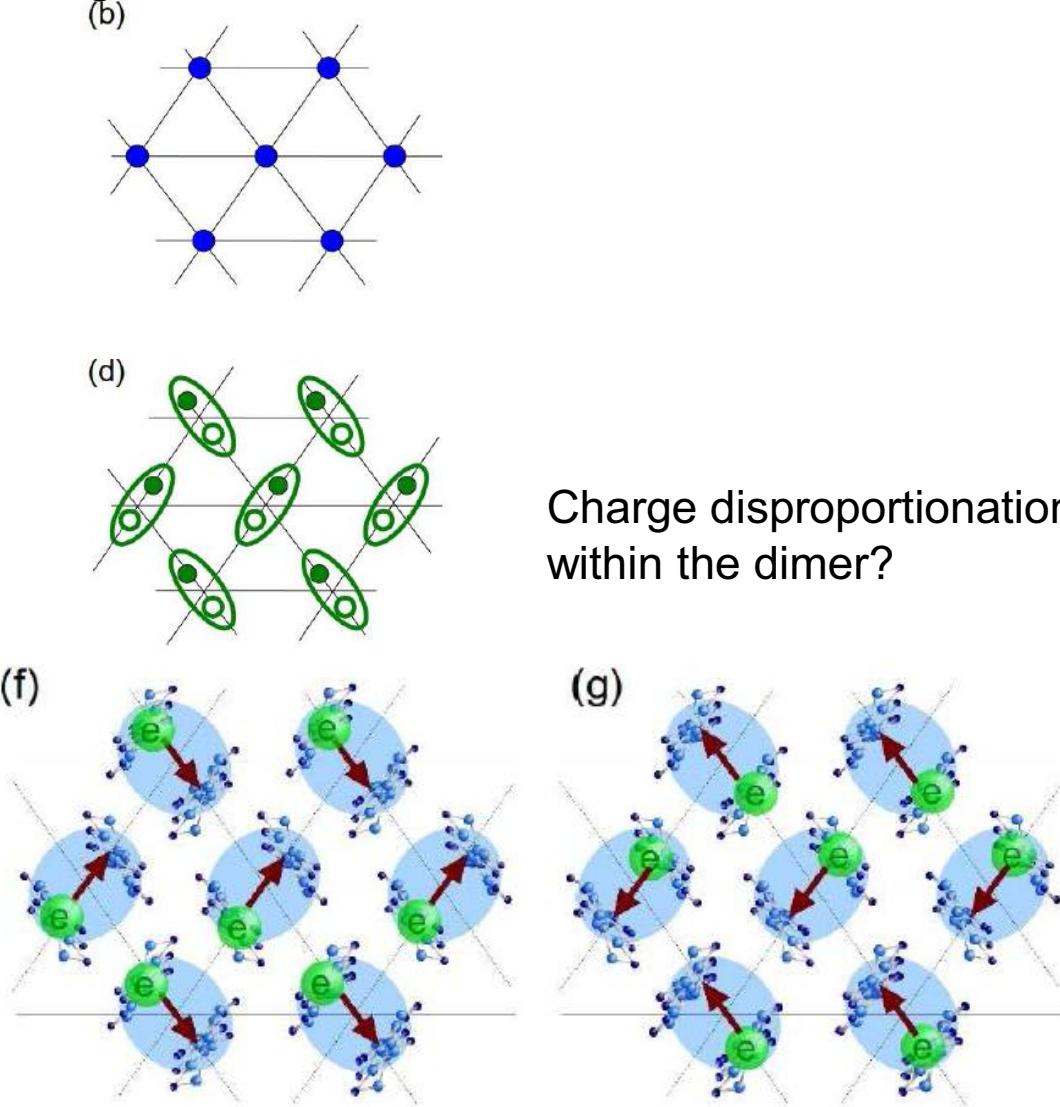
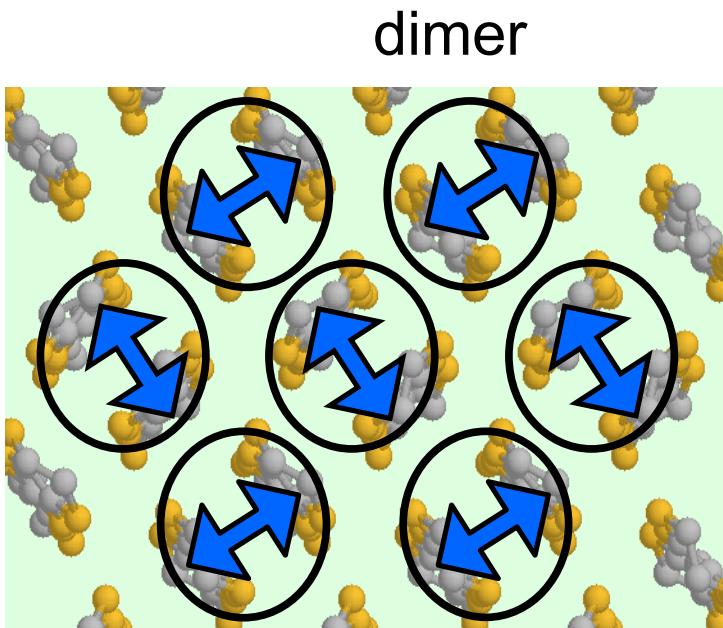


M. Abdel-Jawad et al. arXiv:1003.3902

Structural transition associated with
the charge degree of freedom?

κ -(BEDT-TTF)₂Cu₂(CN)₃ : Anomalous dielectric response

Nontrivial charge degree of freedom within the dimer



κ -(BEDT-TTF)₂Cu₂(CN)₃ : Summary

No magnetic order down to very low temperature $T \sim J/12,000$

NMR, μ SR, susceptibility

Excitation

Gapless Specific heat

Gapped Thermal conductivity

However,

Strong inhomogeneity and microscopic phase separation

NMR, μ SR

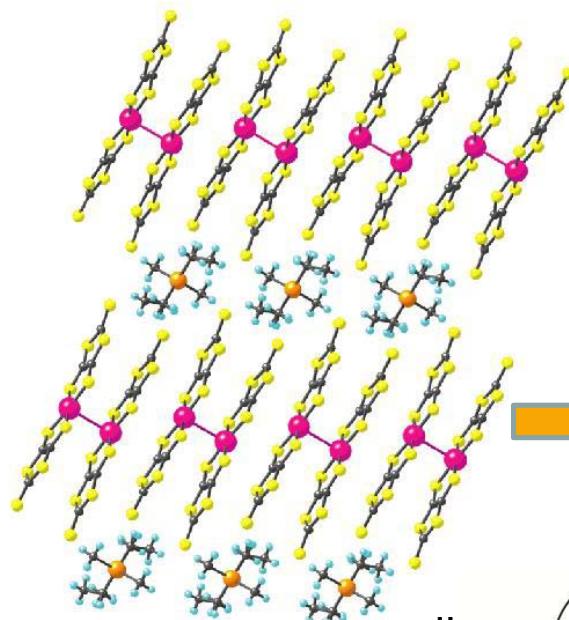
Phase transition at 6 K possibly associated with charge degree of freedom within the dimer

NMR, Heat capacity, Thermal conductivity,
Thermal expansion, Dielectric constant

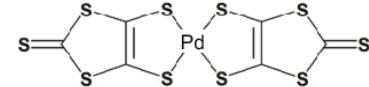
Genuine feature of a QSL appears to be masked by inhomogeneity.
To investigate the QSL, more homogeneous system is required.

Quantum spin liquid state in β' - EtMe₃Sb[Pd(dmit)₂]₂

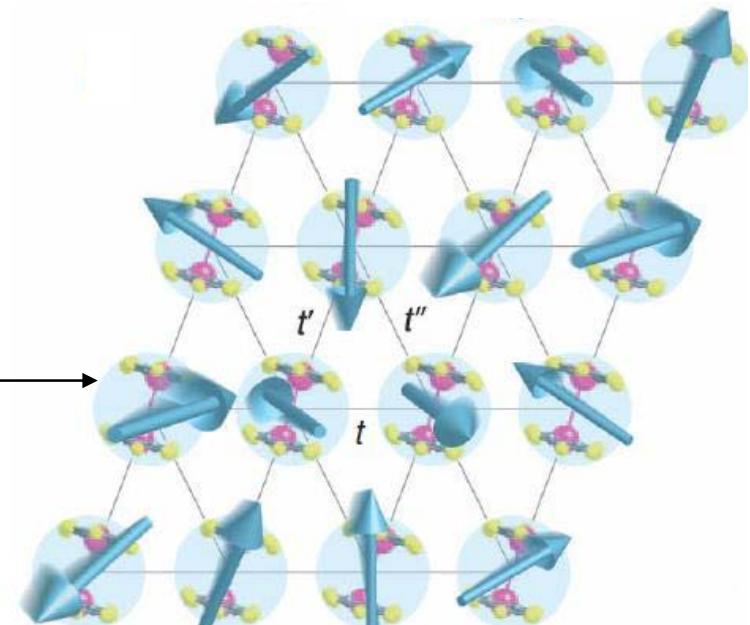
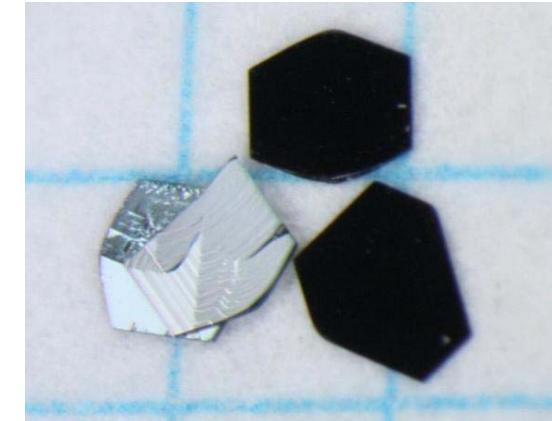
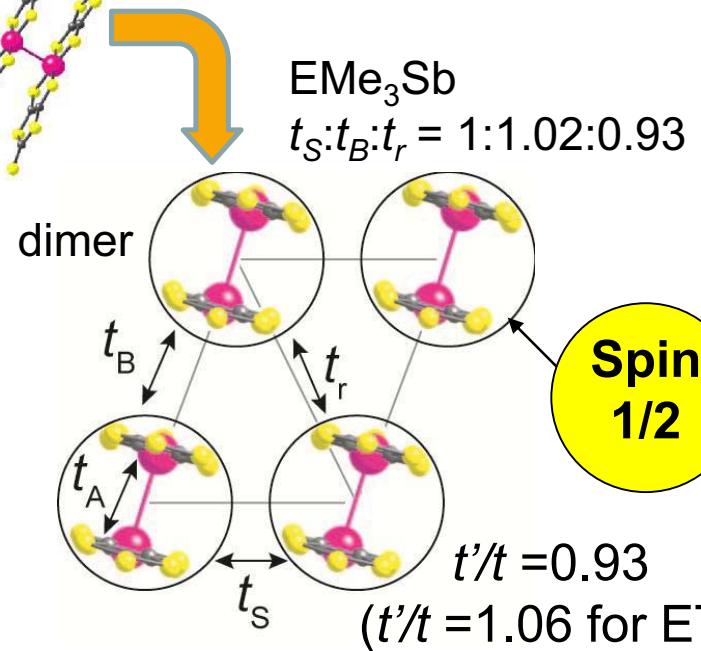
Two-dimensional Mott system with a quasi-triangular lattice
Clean system with small defects



2D layer of
Pd(dmit)₂ molecule

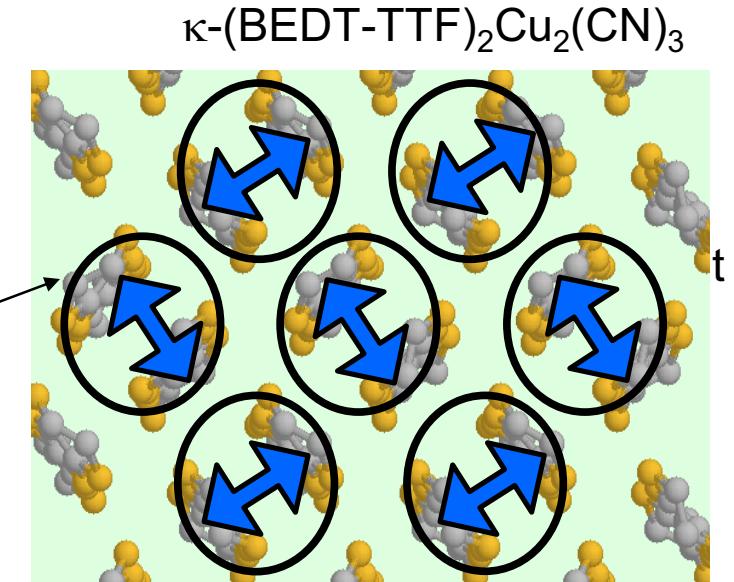
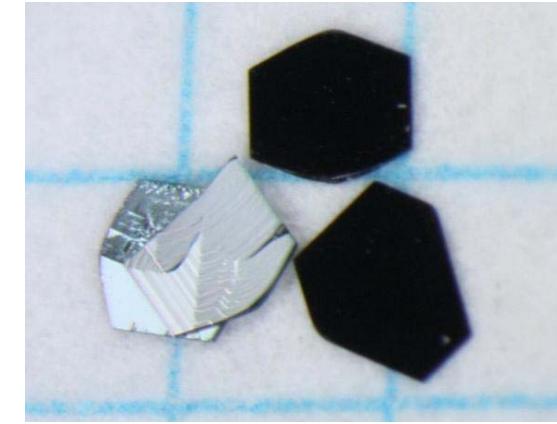
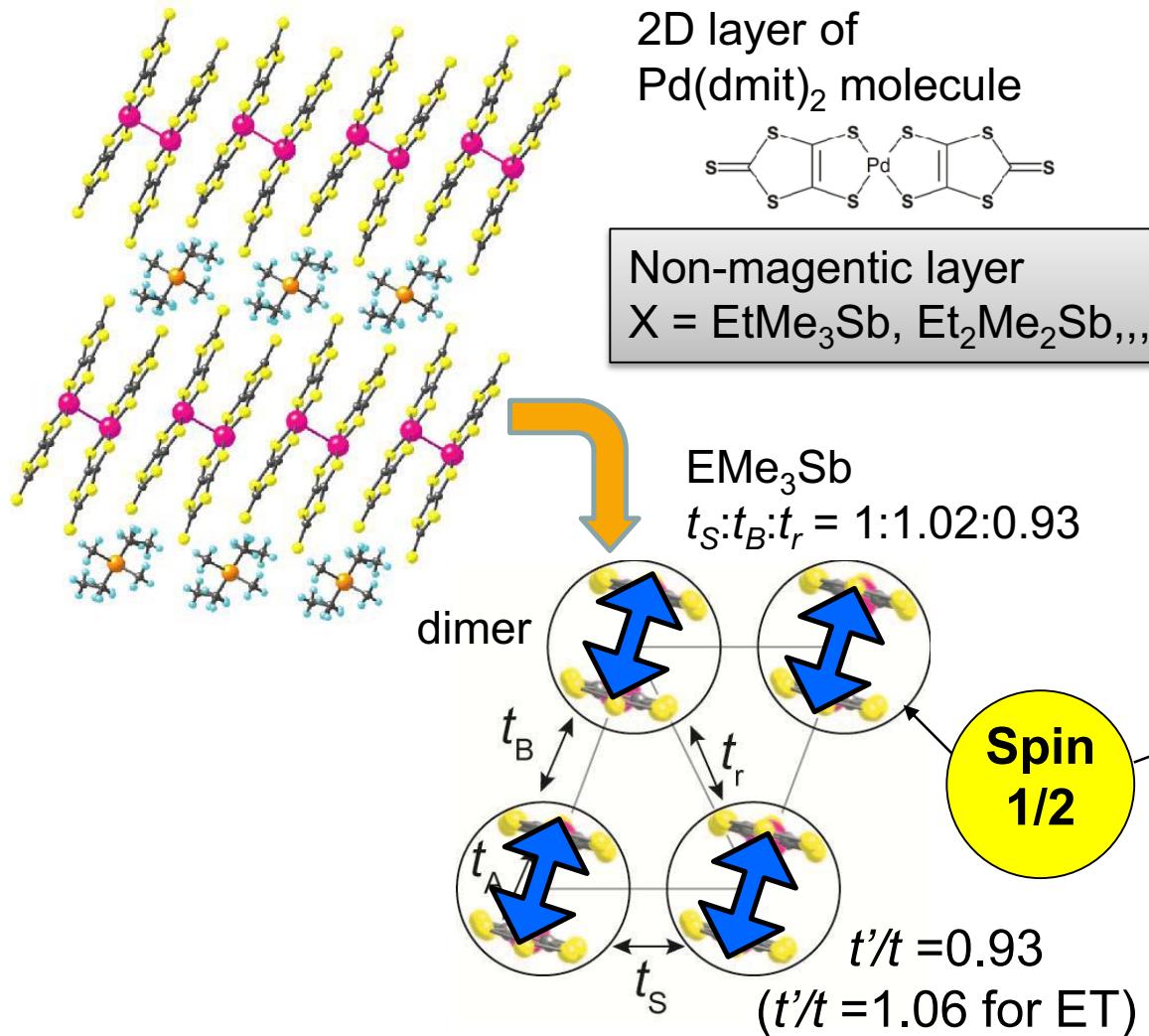


Non-magnetic layer
 $X = \text{EtMe}_3\text{Sb}, \text{Et}_2\text{Me}_2\text{Sb}, \dots$

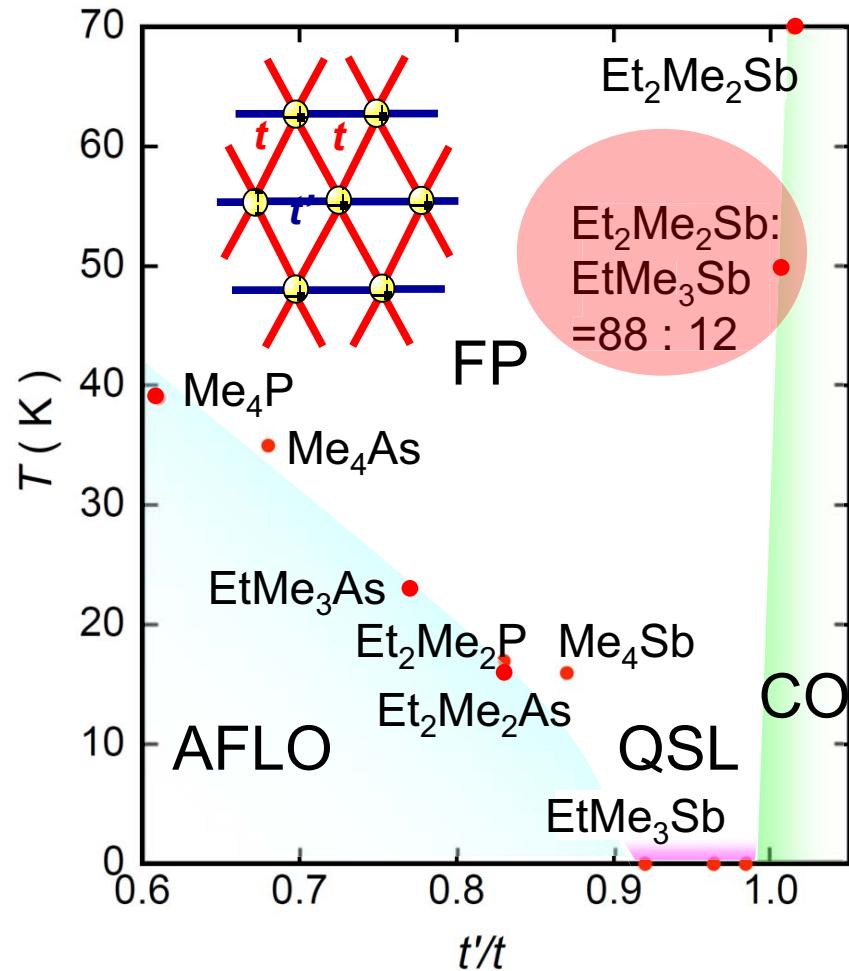


Quantum spin liquid state in β' - EtMe₃Sb[Pd(dmit)₂]₂

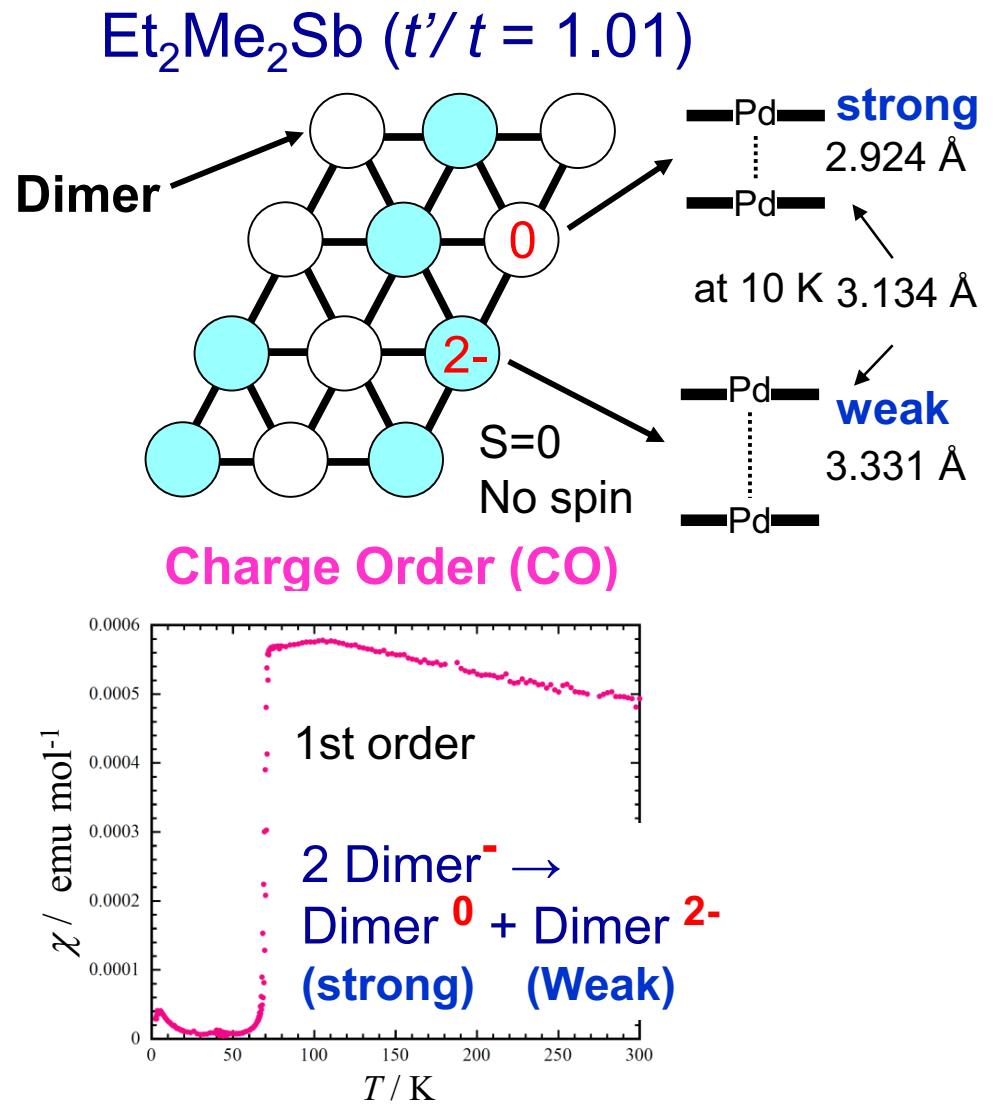
Two-dimensional Mott system with a quasi-triangular lattice
Clean system with small defects



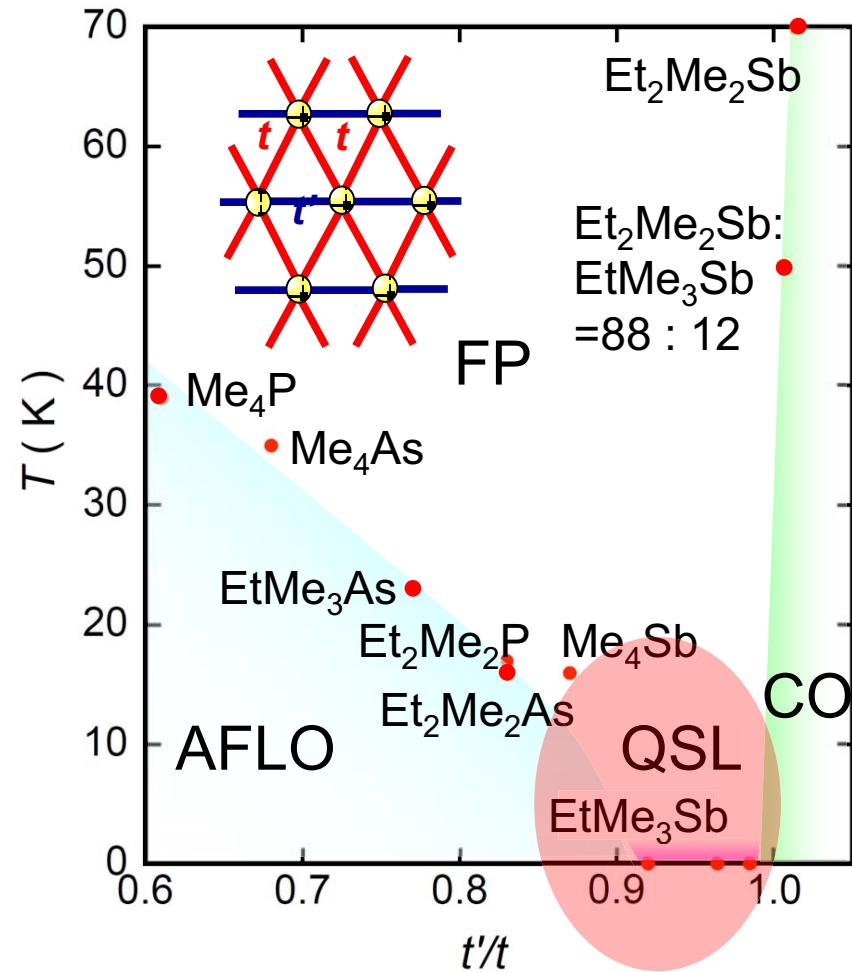
β' -(Cation)[Pd(dmit)₂]₂



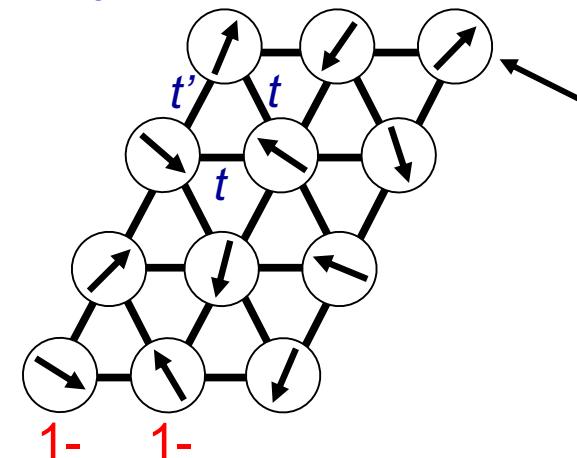
FP: Frustrated paramagnetic state
 AFLO: Antiferromagnetic ordered state
 CO: Charge ordered state
 QSL: Quantum spin liquid state



β' -(Cation)[Pd(dmit)₂]₂



EtMe_3Sb ($t'/t = 0.92$)



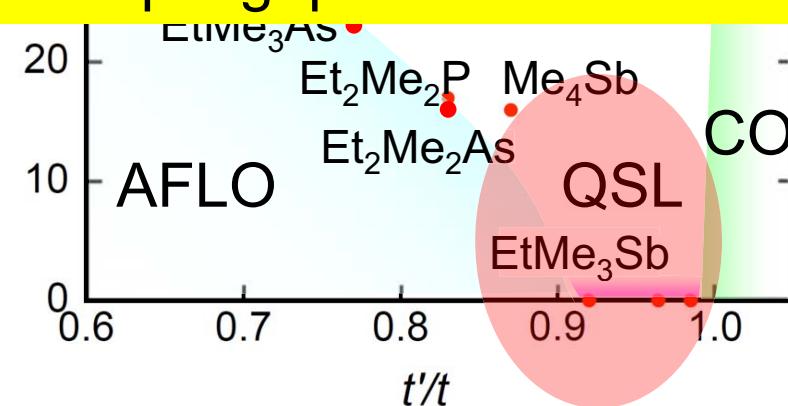
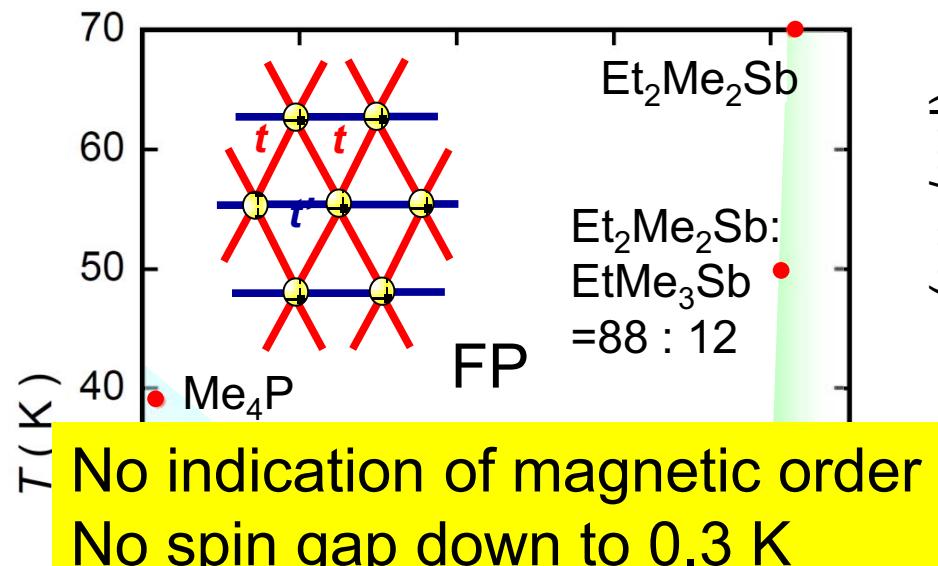
FP: Frustrated paramagnetic state

AFLO: Antiferromagnetic ordered state

CO: Charge ordered state

QSL: Quantum spin liquid state

$\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$ Magnetic susceptibility

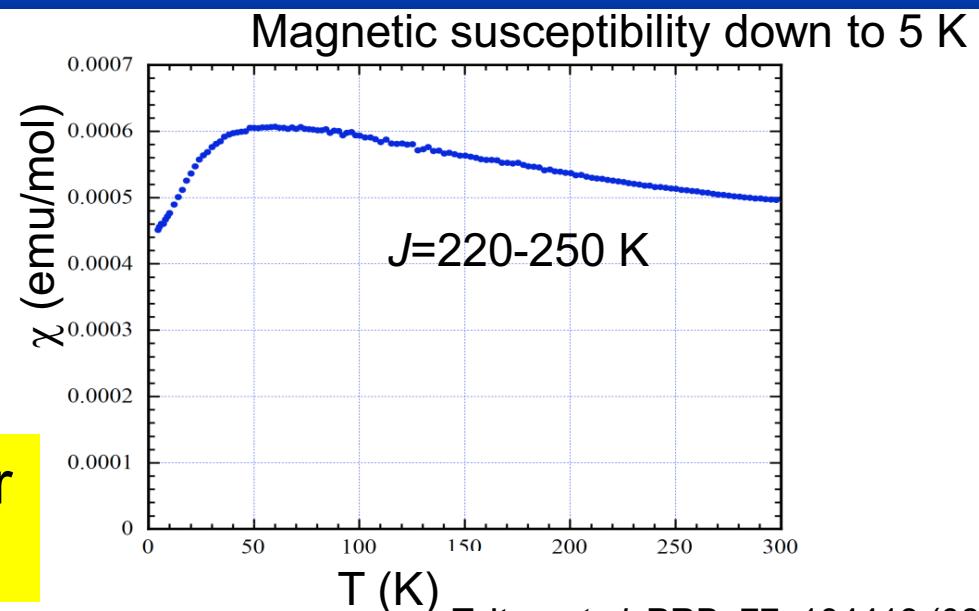


FP: Frustrated paramagnetic state

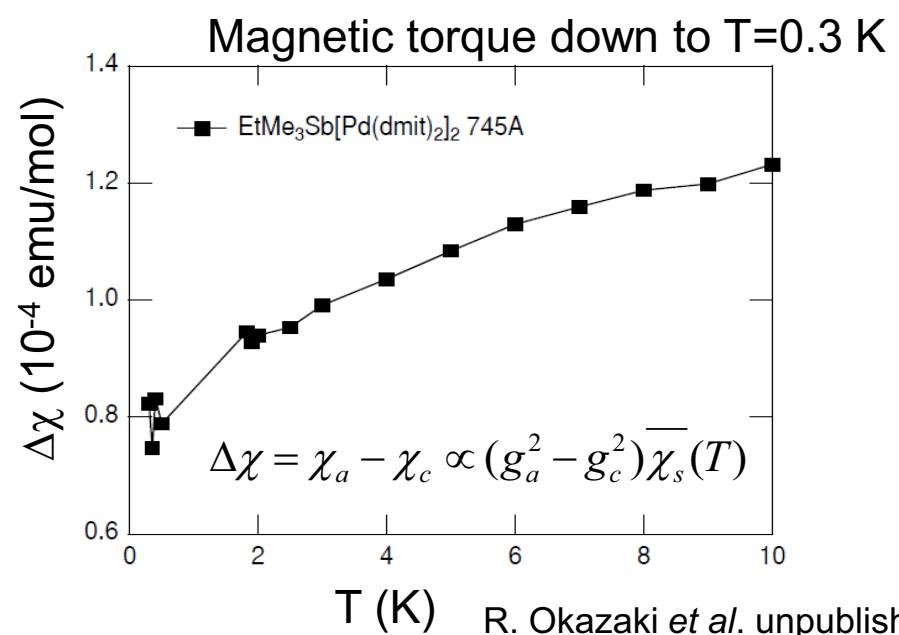
AFLO: Antiferromagnetic ordered state

CO: Charge ordered state

QSL: Quantum spin liquid state



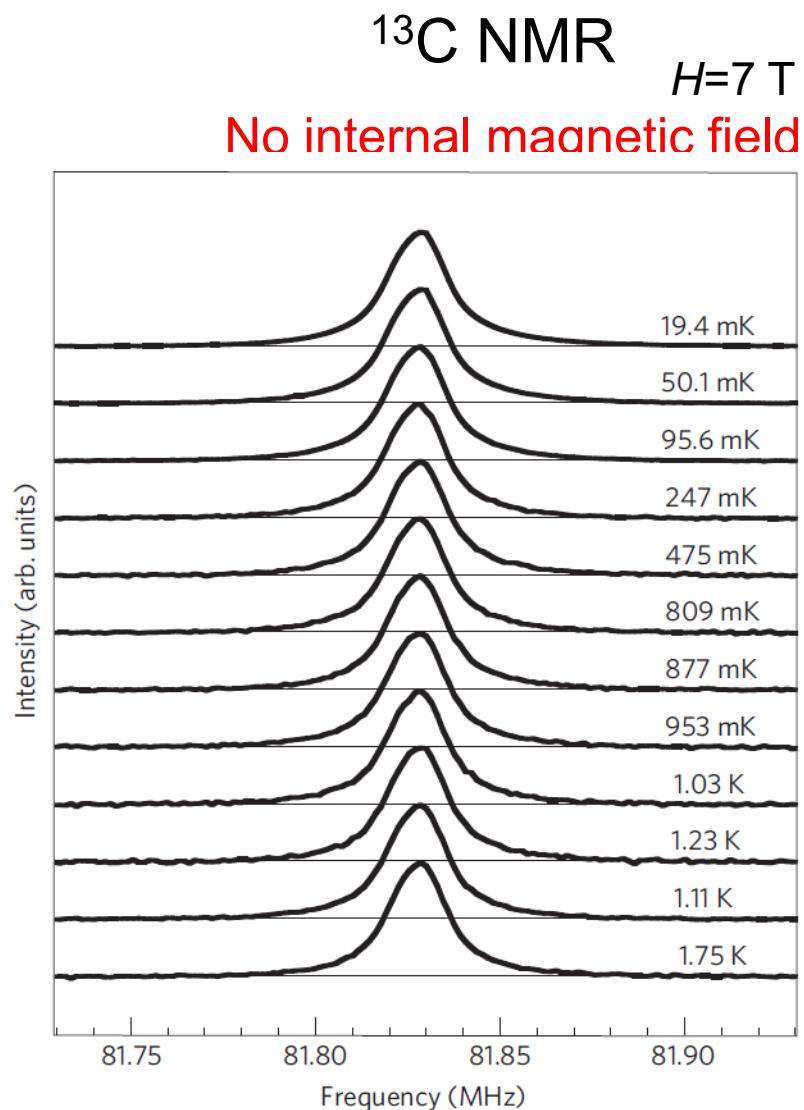
T. Itou *et al.* PRB, 77, 104413 (08)



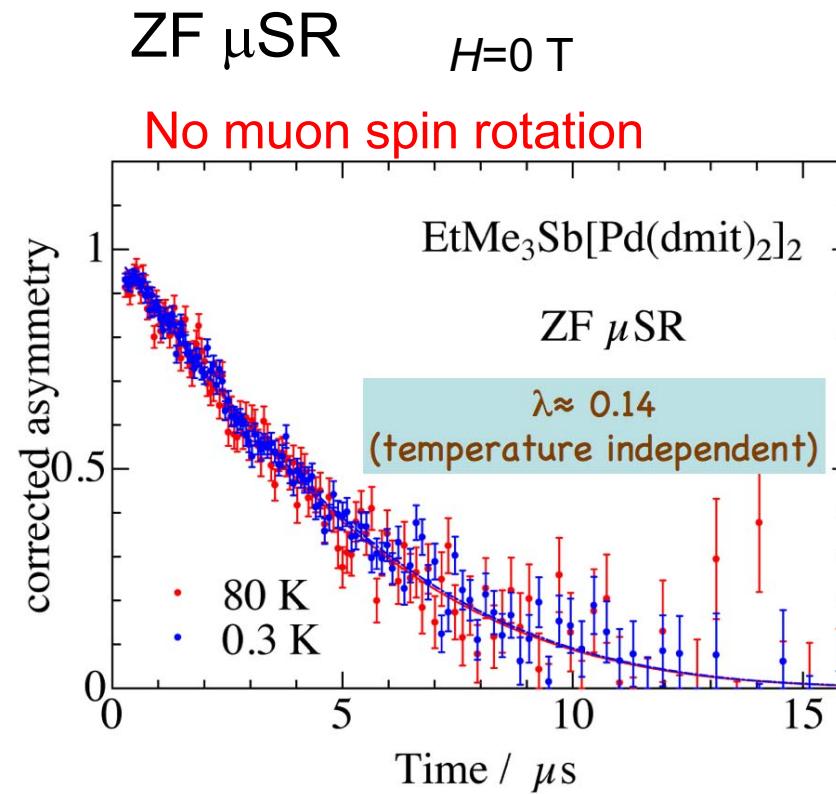
R. Okazaki *et al.* unpublished

$$\Delta\chi = \chi_a - \chi_c \propto (g_a^2 - g_c^2) \chi_s(T)$$

$\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$:NMR and μ SR



Itou et al., Nature Phys. 11, 1 (10)



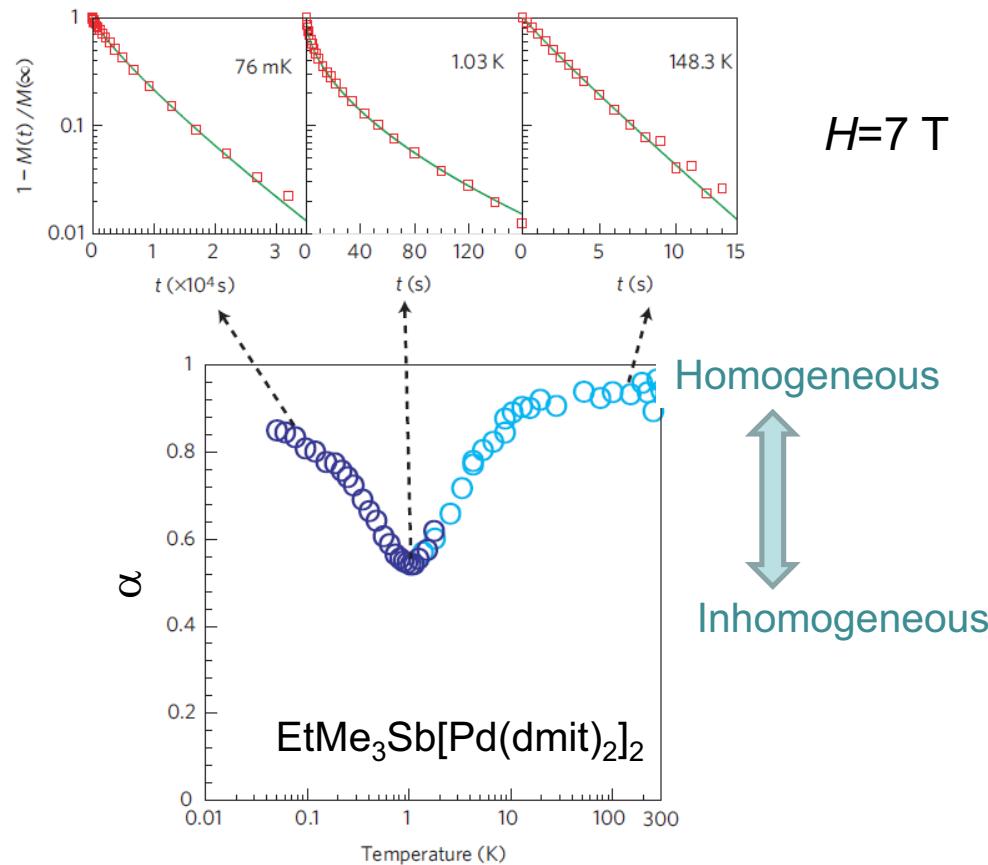
Y. Ishii (RIKEN-RAL) et al.

No indication of magnetic order
down to $\sim J/12,000$

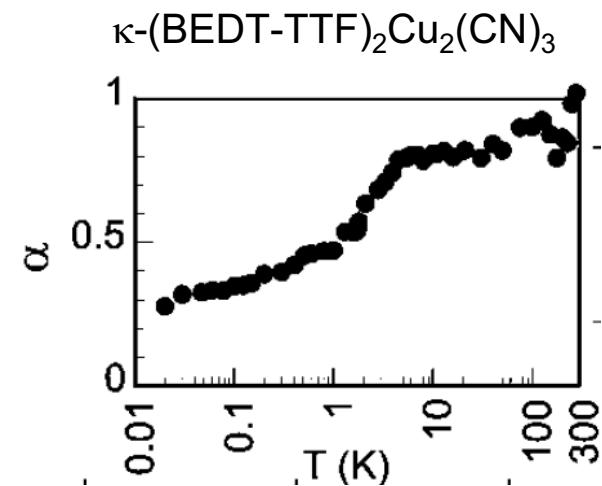
$\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$:NMR

^{13}C NMR

$$-M(t)/M(\infty) = \exp[-(t/T_1)^\alpha]$$



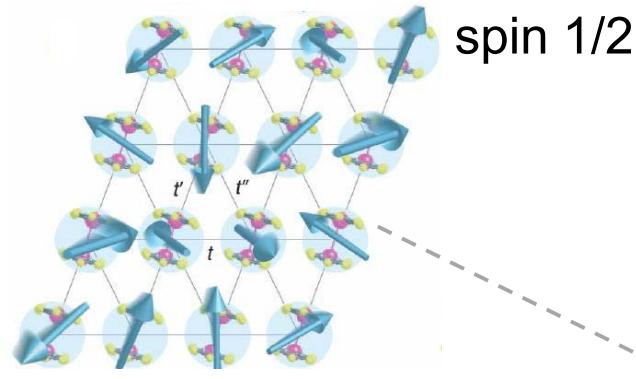
$H=7$ T



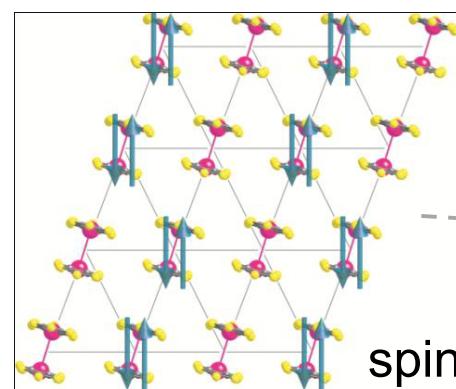
Itou *et al.*, Nature Phys. 11, 1 (10)

At low temperatures, homogeneous spin liquid state is realized

$\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$: Low energy excitation



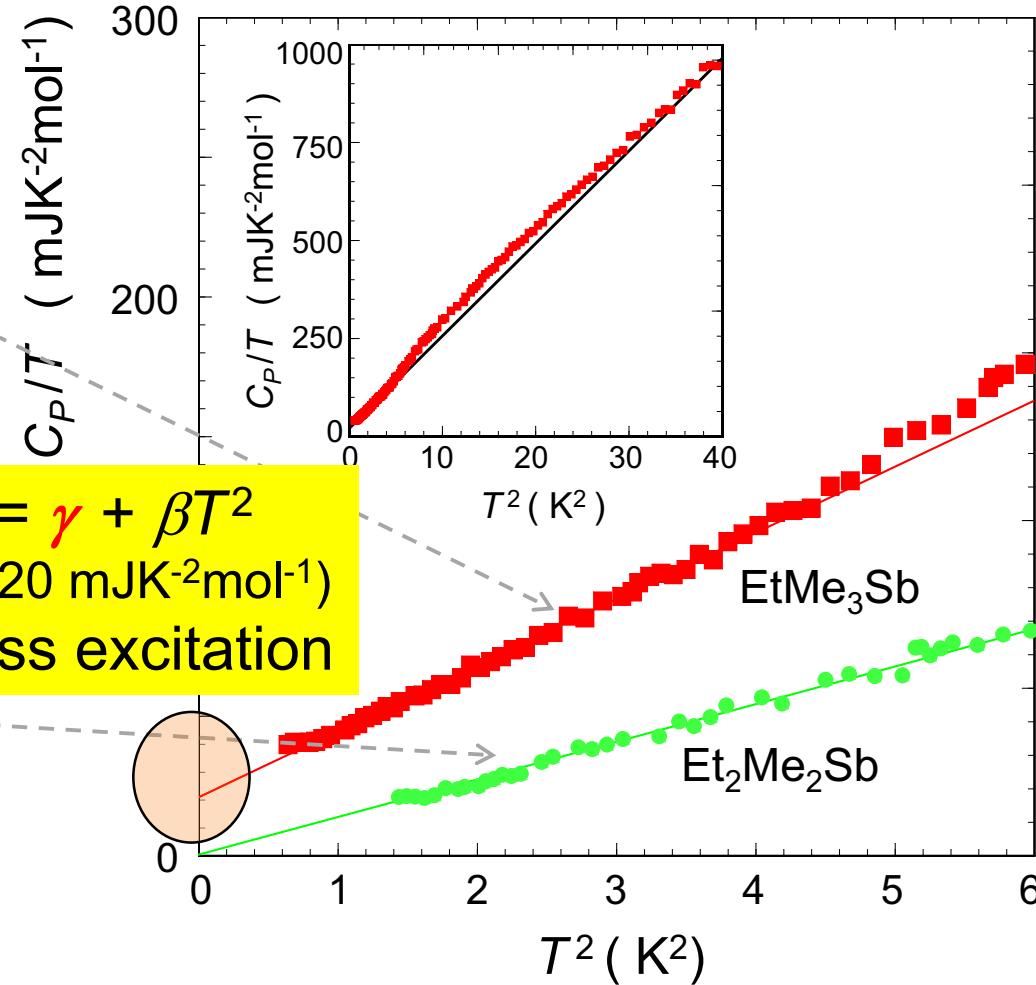
Spin liquid



spin 0

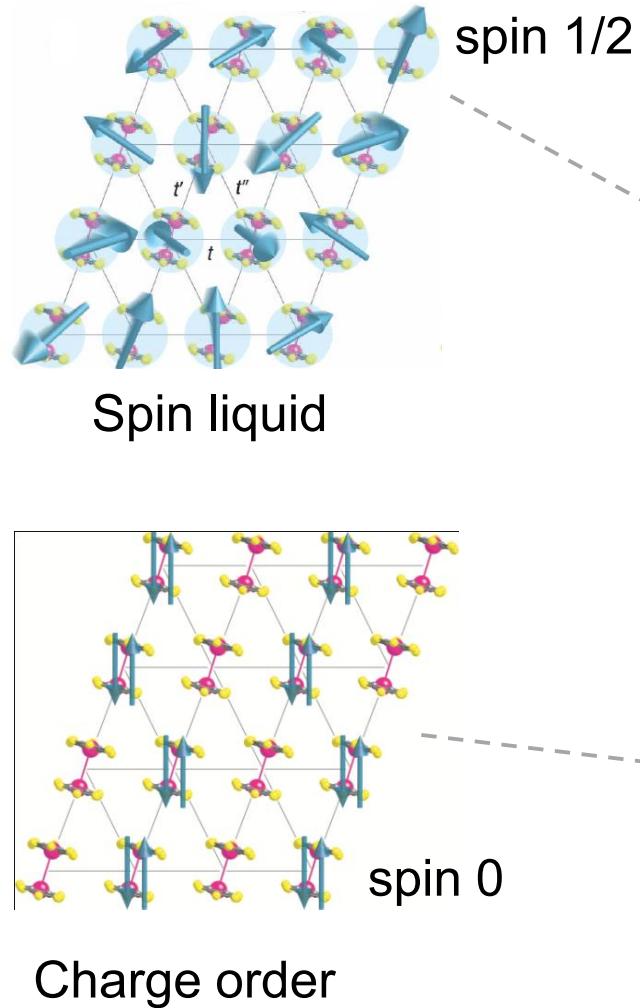
Charge order

Specific heat

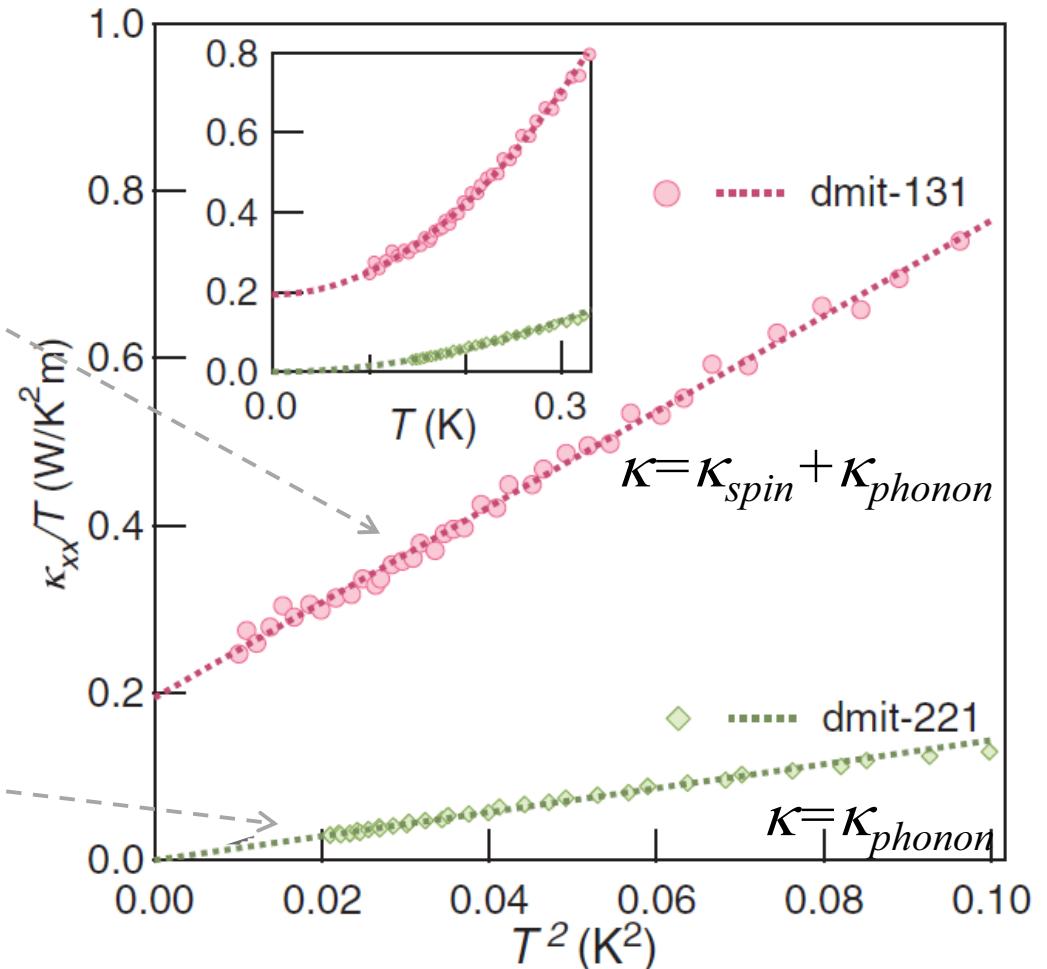


S. Yamashita & Y. Nakazawa (Osaka Univ.)

$\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$: Low energy excitation



Thermal conductivity



M. Yamashita *et al.* Science 328, 1246 (10)

$\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$: Low energy excitation

Enhancement of κ in spin liquid state

$$\rightarrow \kappa = \kappa_{\text{spin}} + \kappa_{\text{phonon}}$$

Clear residual of κ/T !

$$\kappa/T (T \rightarrow 0) = 0.19 \text{ W/K}^2\text{m}$$

Evidence for a **gapless excitation**,
like electrons in normal metals.

Estimation of mean free path

$$\kappa = C \cdot v_s \cdot \ell$$

$$C/T \sim 20 \text{ mJ/K}^2\text{mol}$$

$$v_s = J a \pi / 2 \hbar$$

$$\rightarrow \ell = 1.2 \mu\text{m} \gg a \sim 1 \text{ nm}$$

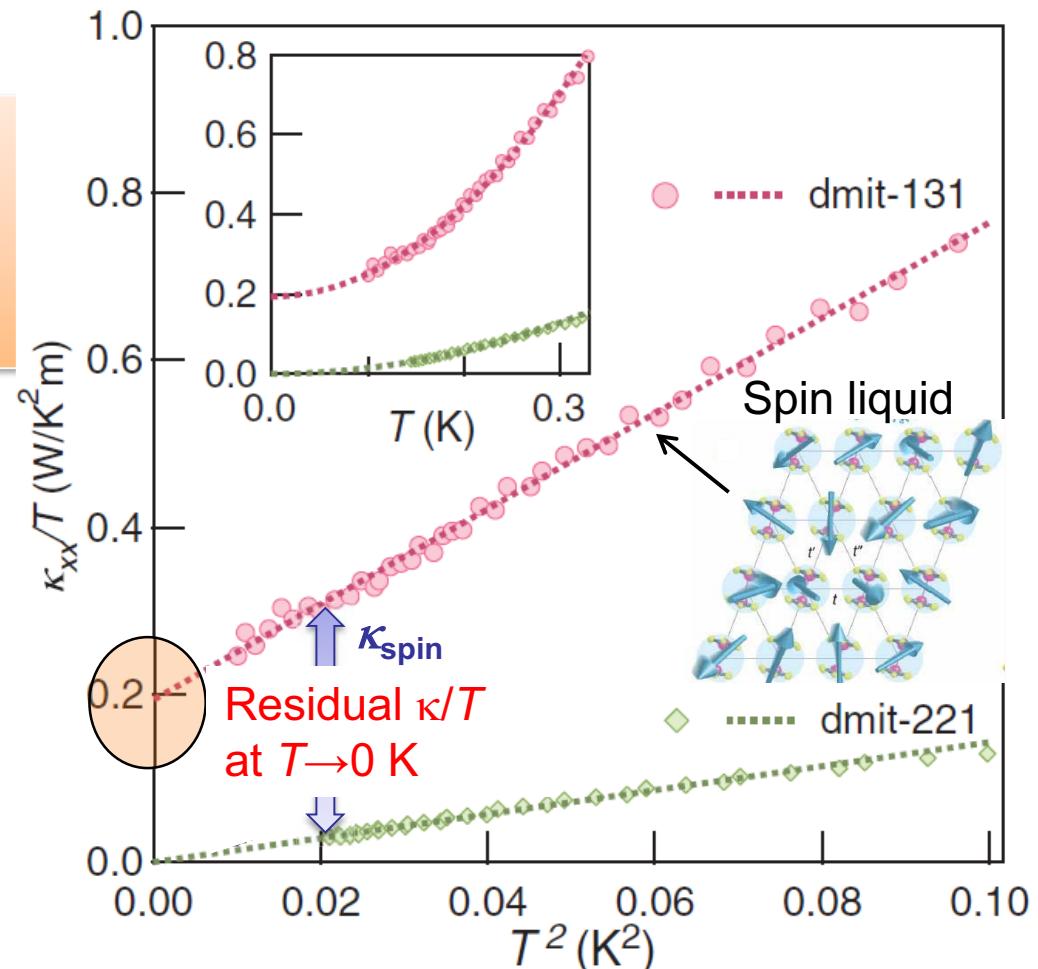
More than 1000 times longer than the
interspin distance!!

Itinerant excitation

Homogeneous

Extremely long correlation length

Thermal conductivity



M. Yamashita et al. Science 328, 1246 (10)

Thermal conductivity of 1D Heisenberg chain

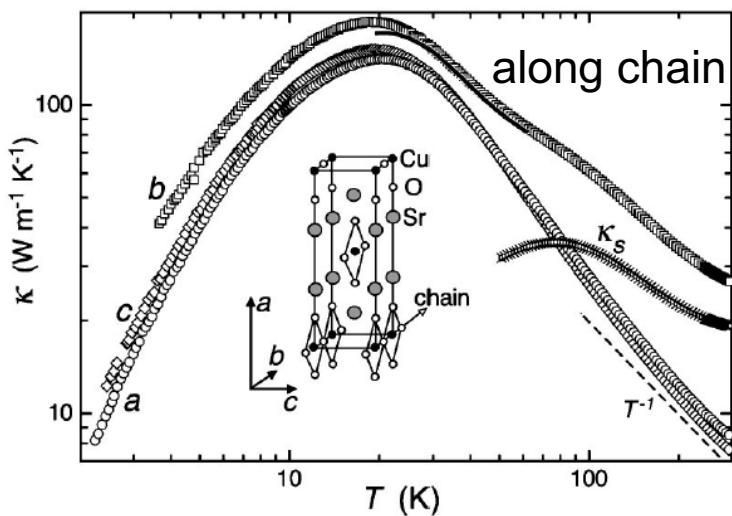
In an integrable system such as the Heisenberg spin-1/2 chain, thermal conductivity along the chain is infinite.

X. Zotos *et al.* PRB 55, 11029 (97)

K.Saito, S.Takesue and S. Miyashita, PRE 54, 2404 (96)

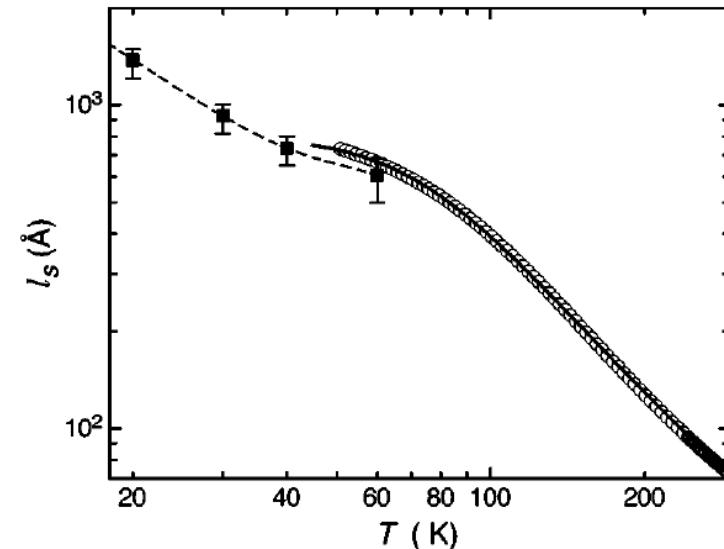
Thermal conductivity in a real material is finite due to impurities, phonons or an interchain interaction

1D Heisenberg $S=1/2$ Sr_2CuO_3
 $J \sim 2500$ K



Unusually high quasi-1D thermal conductivity

$$\kappa_s = C_s v_s \ell_s \quad C_s \text{ specific heat}$$
$$v_s = J a \pi / 2 \hbar \quad \text{velocity of spinon}$$
$$\ell_s \text{ spinon mean free path}$$



Very long spinon mean free path
A.V. Sologubenko *et al.* PRB 62, R6108 (00)

$\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$: Low energy excitation

1-yen



Alminium



5-yen (~5 cent)



Brass (Cu0.7+Zn0.3)



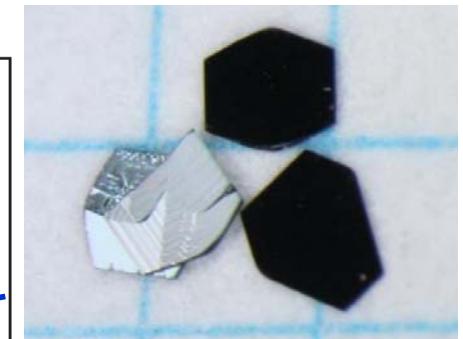
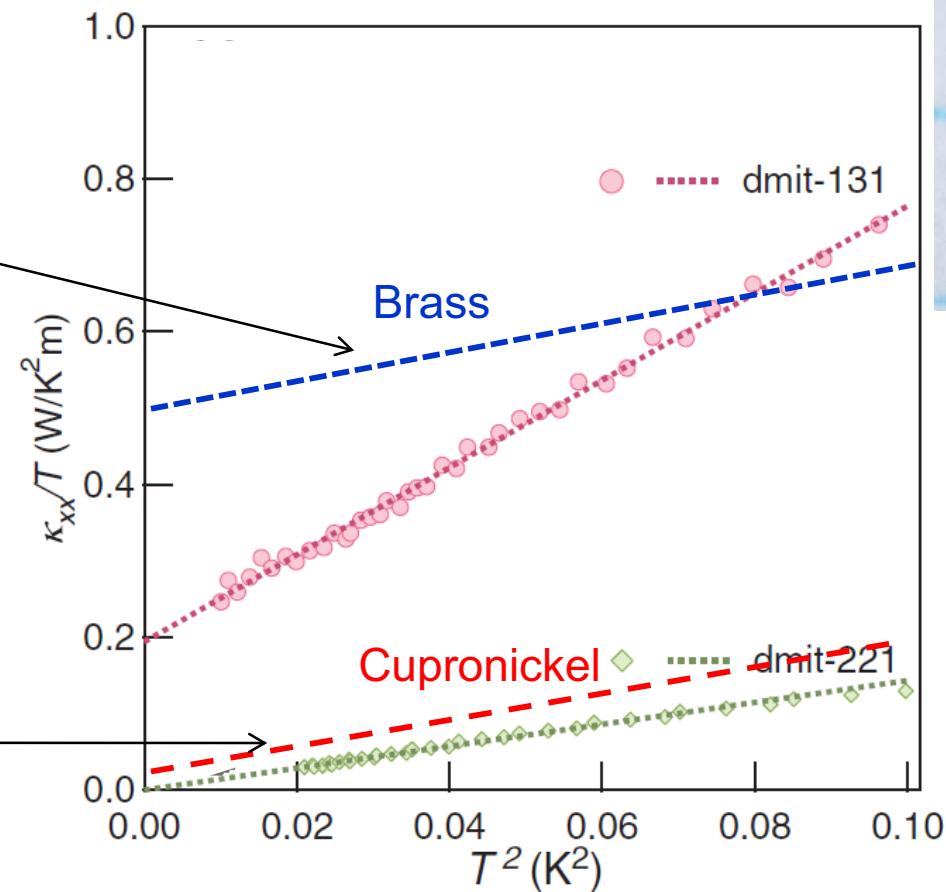
10-yen



100-yen(~\$1~€1)

Cupronickel (Cu0.75+Ni0.25)

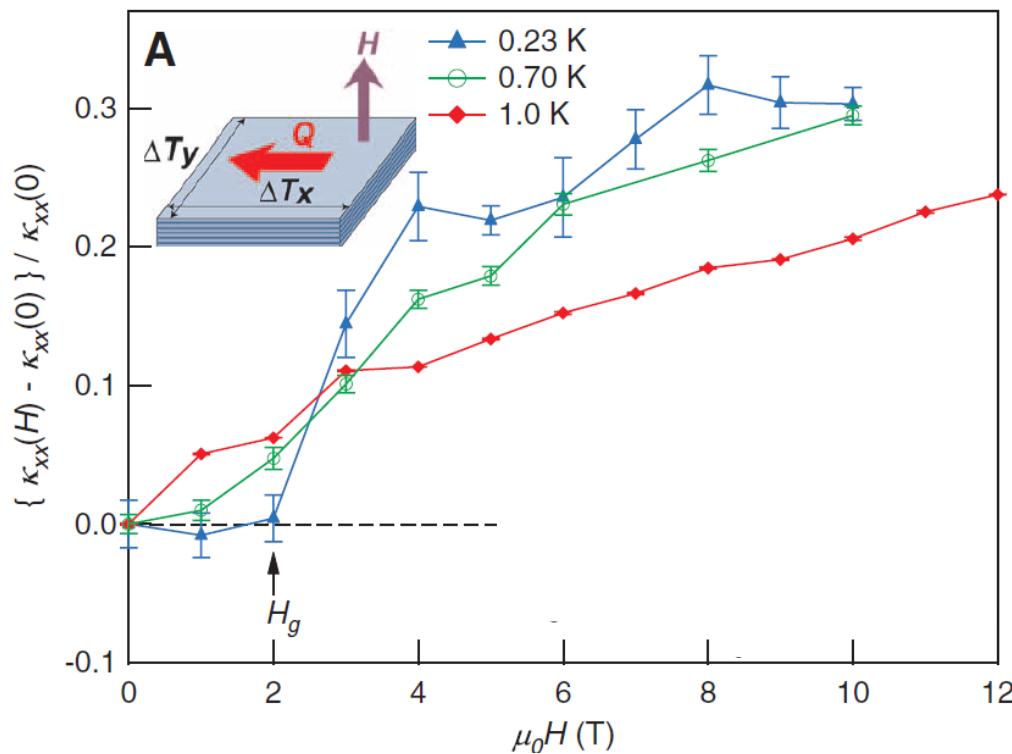
Quantum spin liquid conducts heat very well.
as good as brass



$\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$: Nature of the low energy excitation

Field dependence of the elementary excitations

H -dependence of κ_{xx}



M. Yamashita *et al.* Science 328, 1246 (10)

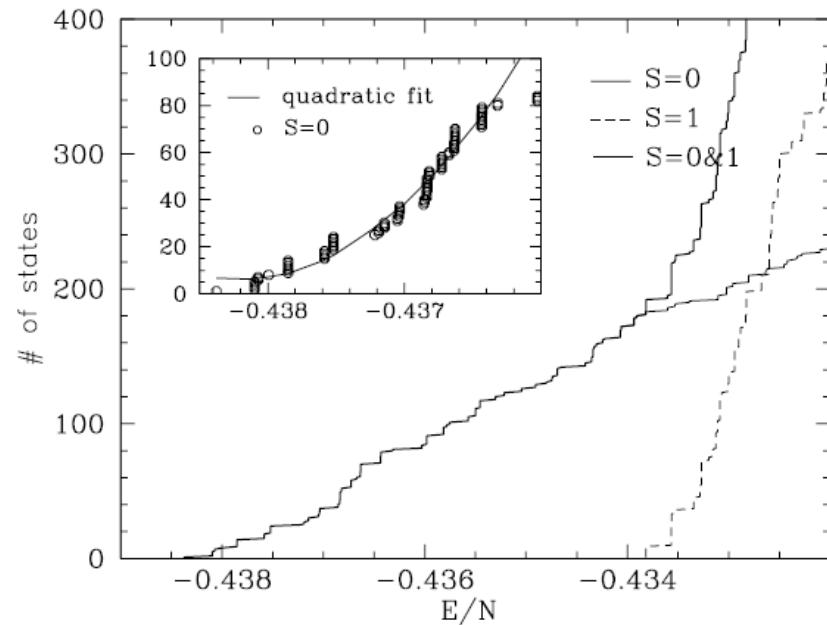
➤ $H > 1$ K
Linear increase
Clear signature of κ_{spin}

➤ $H < 1$ K
Spin-gap like behavior
 $\mu_0 H_g \sim 2$ T

Bipartite nature of excitations

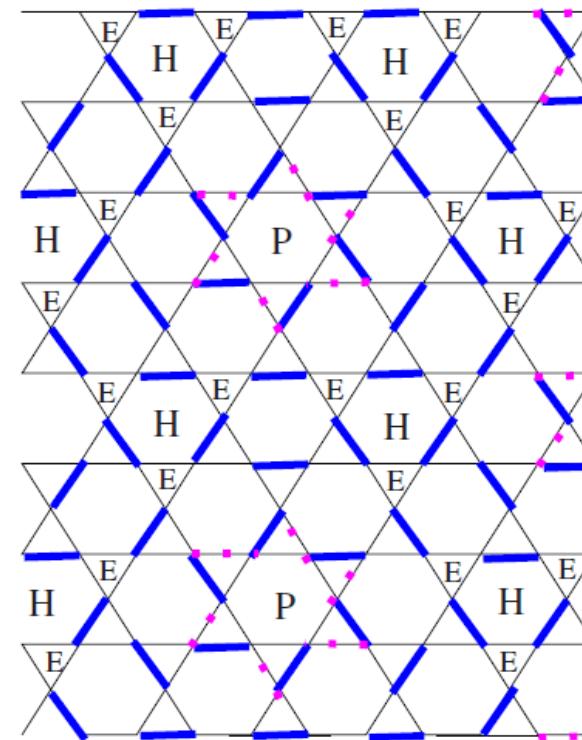
Coexistence of
Nonmagnetic gapless excitation
and
Spin-gap-like excitation that
couples to magnetic field

Kagome lattice Heisenberg magnet with $S=1/2$



Gapped magnetic excitation filled with nonmagnetic excitations

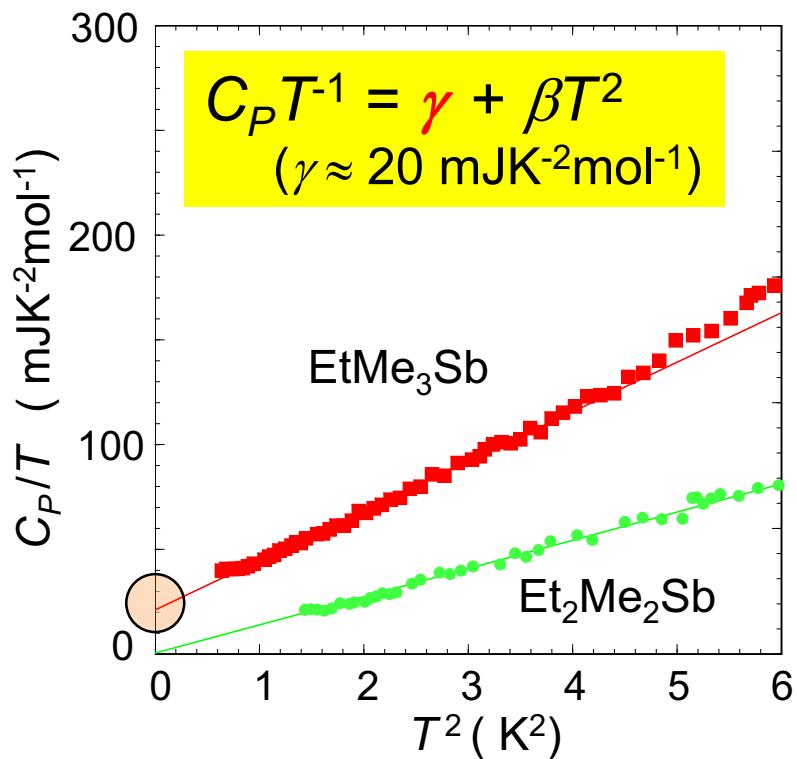
Ch. Waldtmann *et al.* Eur. Phys. J. B 2, 501 (98)



Valence bond solid with a 36 site unit cell

R.P. Singh and D.A. Huse, PRB 76, 180407 (07)

Wilson ratio



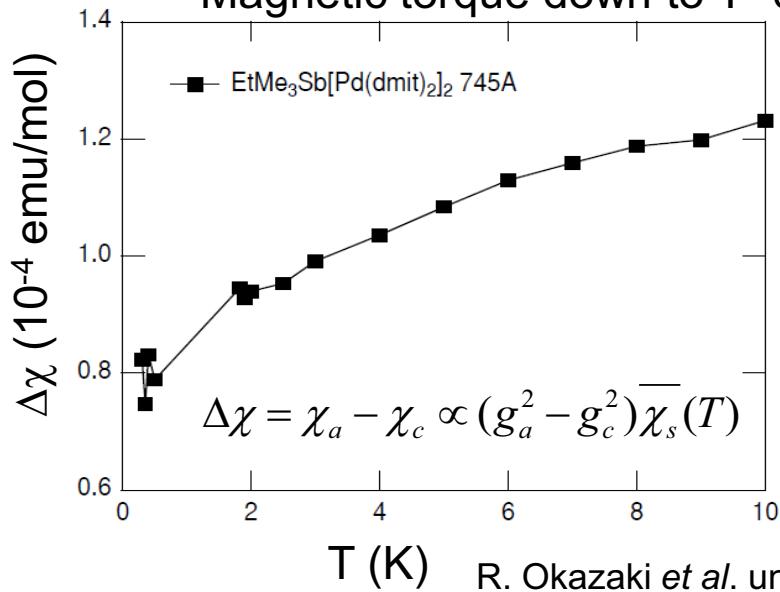
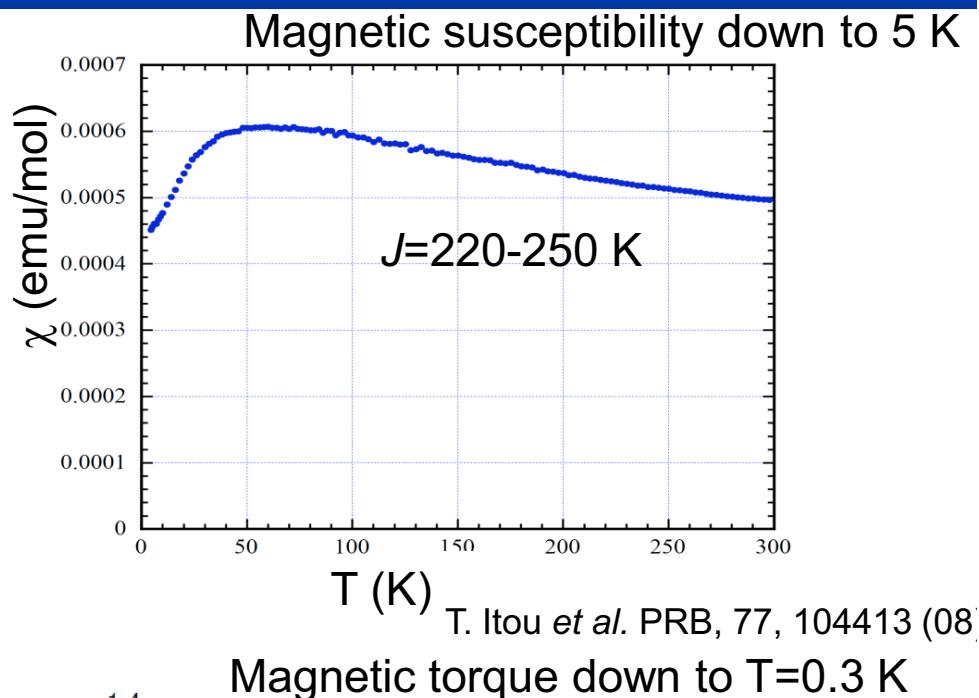
$$R = \frac{4\pi^2 k_B^2 \chi}{3(g\mu_B)^2 \gamma}$$

$$\chi \sim 4.5 \times 10^{-4} \text{ emu/mol}$$

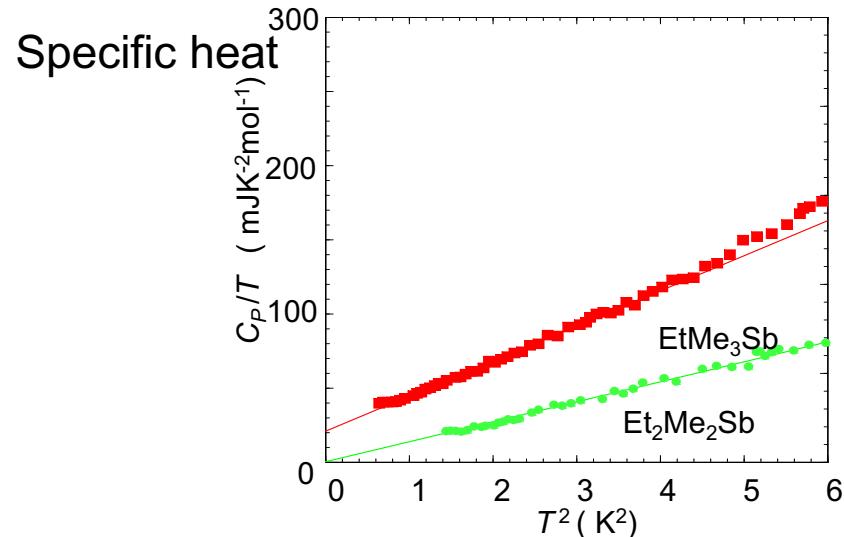
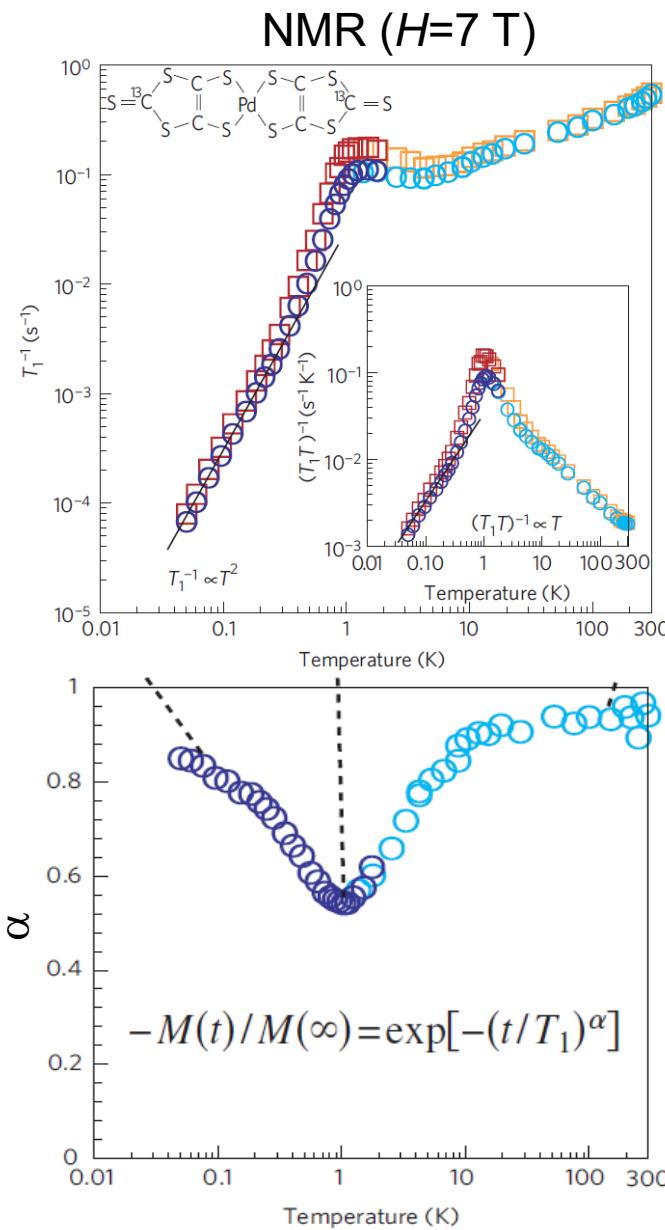
$$\gamma \sim 20 \text{ mJ/K}^2 \text{mol}$$

$R \sim 1.2$ Close to metals

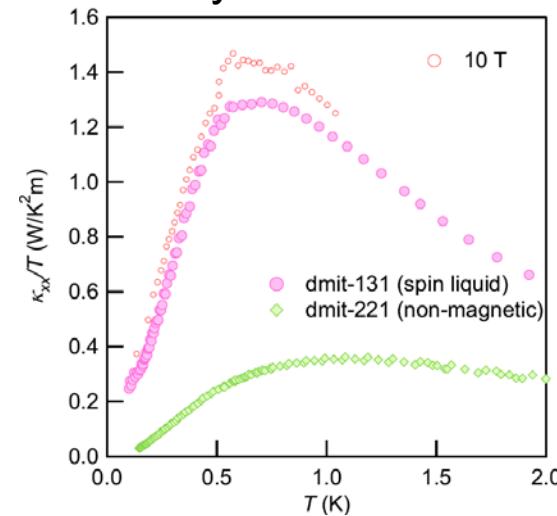
What does this mean??



EtMe₃Sb[Pd(dmit)₂]₂ :Symmetry breaking in the QSL?



Thermal conductivity



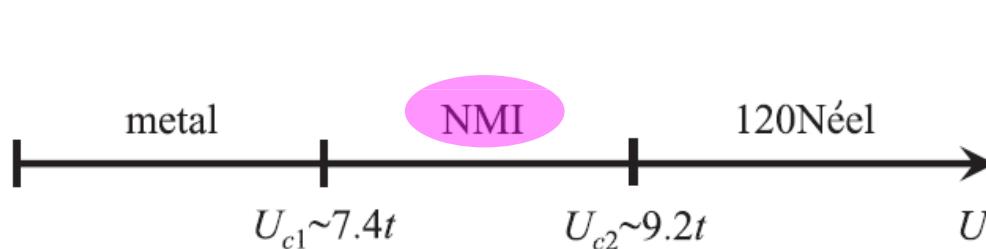
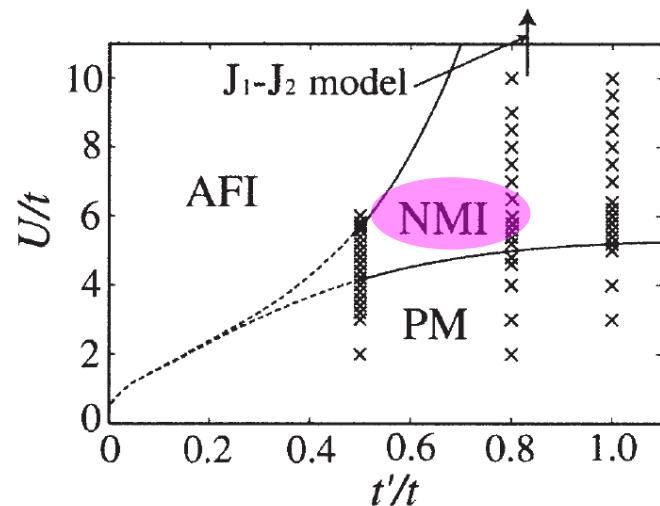
The phase transition suggested by NMR is not confirmed by specific heat, thermal conductivity and magnetic susceptibility

QSL: theory (Hubbard model)

Hubbard model for a triangular lattice

$$\hat{\mathcal{H}} = -t \sum_{\langle i,j \rangle, \sigma} (\hat{c}_{i\sigma}^\dagger \hat{c}_{j\sigma} + \text{H.c.}) + U \sum_i \hat{n}_{i\uparrow} \hat{n}_{i\downarrow}$$

A nonmagnetic insulating state, most likely a QSL ground state, near the Mott transition



T. Yoshioka, A. Koga and N. Kawakami, PRL 103, 036401 (09)

See also

- B. Kyung and A.M.S. Tremblay, PRL 97, 046402 (06)
- T. Koretsune, Y. Motome and A. Furusaki, JPSJ 76, 07419 (07)
- T. Mizusaki and M. Imada, PRB 74, 014421 (06)

Gapless excitation
Localized excitation

Energy resolution of these calculations is not enough to discuss low energy excitations ($E \sim J/100$)

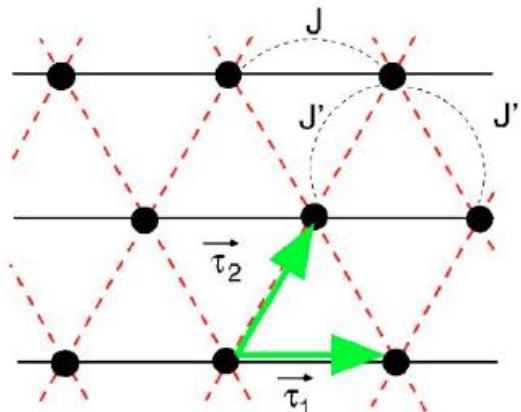
H. Morita, S. Watanabe and M. Imada,
JPSJ 71, 2109 (02)

QSL: theory (One dimensionalization)

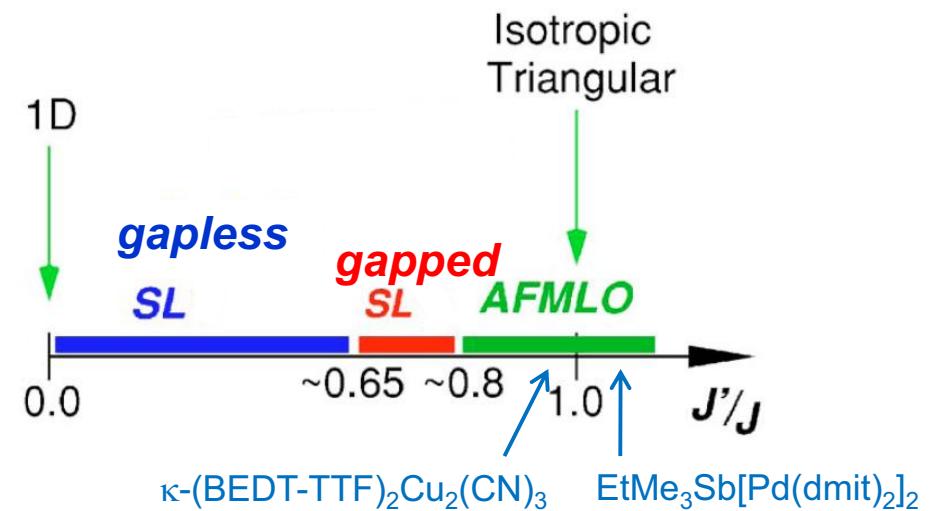
Heisenberg model

One dimensionalization

$$\hat{H} = J \sum_{\langle i,j \rangle} \vec{S}_i \cdot \vec{S}_j + J' \sum_{\langle\langle i,j \rangle\rangle} \vec{S}_i \cdot \vec{S}_j,$$



S. Yunoki and S. Sorella, PRB 74, 014408 (06)



See also Y. Hayashi and M. Ogata, JPSJ 76, 053705 (07)

The present systems are not in the QSL regime in one dimensionalization models.

QSL: theory (Ring exchange)

Heisenberg model for a triangular lattice

4 spin ring exchange model

$$\hat{H}_{\text{ring}} = J_2 \sum_{\bullet\bullet} P_{12} + J_4 \sum_{\bullet\bullet\bullet\bullet} (P_{1234} + P_{1234}^\dagger)$$

$$P_{1234} = (\mathbf{s}_1 \cdot \mathbf{s}_2)(\mathbf{s}_3 \cdot \mathbf{s}_4) + (\mathbf{s}_1 \cdot \mathbf{s}_4)(\mathbf{s}_3 \cdot \mathbf{s}_2) - (\mathbf{s}_1 \cdot \mathbf{s}_3)(\mathbf{s}_2 \cdot \mathbf{s}_4)$$

$$\text{When } J_4 > 0 \quad \theta_1 - \theta_2 + \theta_3 - \theta_4 = \pi$$

4-spin ring exchange in triangular lattice yields a strong frustration

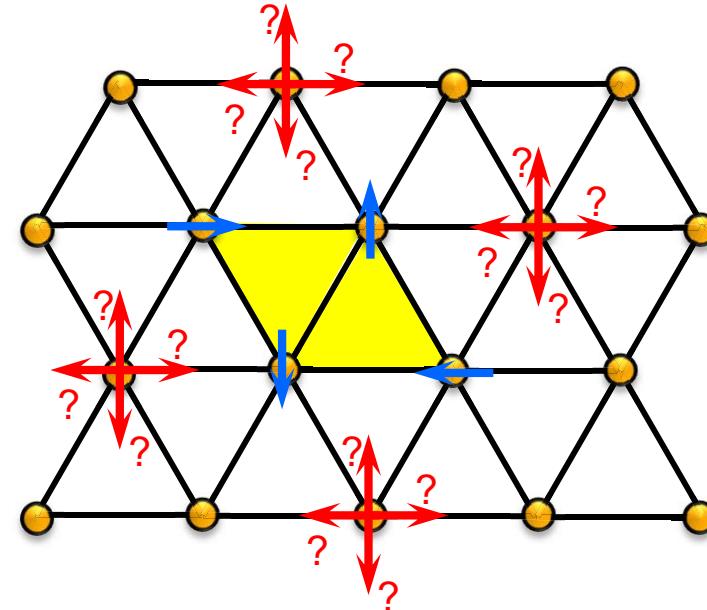
Quantum Spin Liquid

G. Misguich, C. Lhuillier, B. Bernu and C. Waldtmann, PRB 60, 1064 (99)

Excitation is gapped

W. LiMing, G. Misguish, P. Sindzingre and C. Luhuiller , PRB 62, 6370 (00)

Spin gap filled with a large number of singlets appear in some parameter range



QSL: theory (spinon with Fermi surface)

Fermionic excitation
Nodal gap
Gapless excitation

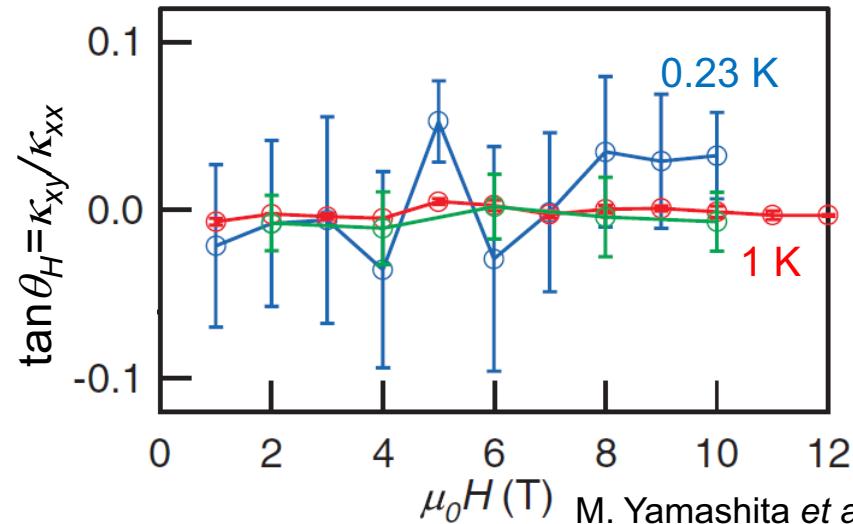
γ -term in specific heat
Finite κ_{xx}/T at $T \rightarrow 0$ K

Wilson ratio $R \sim 1$

NMR T_1 (nodal)

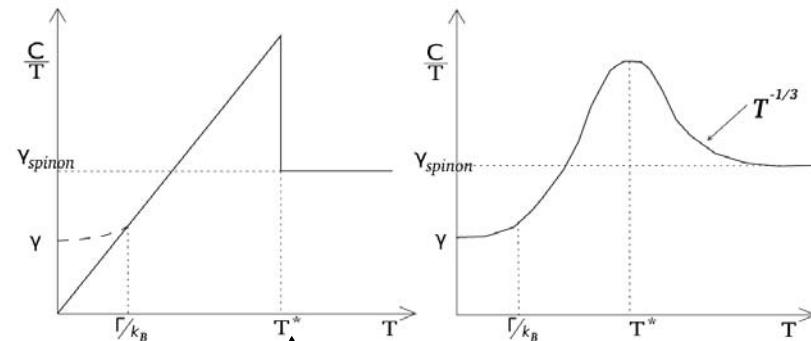
Thermal Hall angle $\tan\theta_H = \kappa_{xy}/\kappa_{xx}$ no

H. Katsura, N. Nagaosa and P.A. Lee,
PRL 104, 066403 (10)



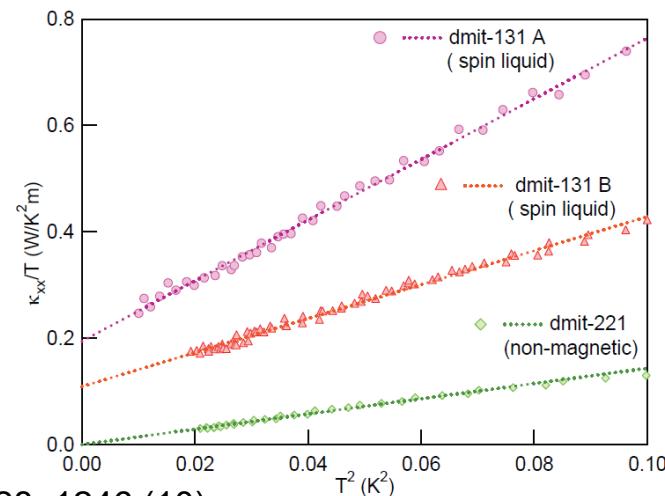
M. Yamashita et al. Science 328, 1246 (10)

O.I. Motrunich, PRB 72, 045105 (05).
S.-S.Lee and P.A. Lee, PRL 95, 036403 (05)
S.-S.Lee, P.A. Lee and T. Senthil, PRL 98, 067006 (07)
T. Grover et al. PRB 81, 245121 (10)



Spinon instability Impurity induced DOS
(d -wave superconductor)

Universal thermal conductivity κ_{xx}/T no



QSL: theory

Quantum dimer model

Gapped

R. Moessner and S. Sondhi
PRL 86, 1881 (01)

Chiral spin liquid

Gapped

V. Kalmeyer and R. B. Laughlin
PRL 59, 2095–2098 (1987)

Z_2 spin liquid

Gapped (Vison)

Y. Qi, C. Xu, and S. Sachdev
Phys. Rev. Lett. 102, 176401 (09)

Algebraic spin liquid

Gapless spinon

X. G. Wen, PRB 65, 165113 (02)

Spin Bose-metal

Gapless boson

D.N. Sheng, O.I.Motrunich and M.P.A.Fisher
PRB 79, 205112 (09)

Summary: Remarkable features in a 2D candidate quantum spin liquid

κ -(BEDT-TTF)₂Cu₂(CN)₃

No magnetic order down to $T \sim J/10,000$

Gapless or gapped?

Inhomogeneity and microscopic phase separation

EtMe₃Sb[Pd(dmit)₂]₂

No magnetic order down to $T \sim J/10,000$

Homogeneous (Suitable for the study of genuine feature in a QSL state)

Highly unusual elementary excitations

Nonmagnetic **gapless** excitations

Bipartite nature

Magnetic **gapped** excitation

Excitation is **itinerant** (highly mobile: mean free path $\sim 1 \mu\text{m}$)

Extremely long correlation length (Power law correlation function)

No thermal Hall effect up to 12 T

Wilson ratio ~ 1.2

Symmetry breaking in the QSL state?

Thermal conductivity

M. Yamashita and Y.M. *et al.* Nature Phys. **5**, 44 (09)

M. Yamashita and Y.M. *et al.* Science **328**, 1246 (10)

Future experiments

Thermal Hall conductivity and torque measurements up to 30 T
In-plane anisotropy (nodal, nematic ···)