



2167-16

Advanced School on Direct and Inverse Problems of Seismology

27 September - 8 October, 2010

SURFACE WAVES

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SURFACE WAVES and UPPER MANTLE ANISOTROPY

Jean-Paul Montagner

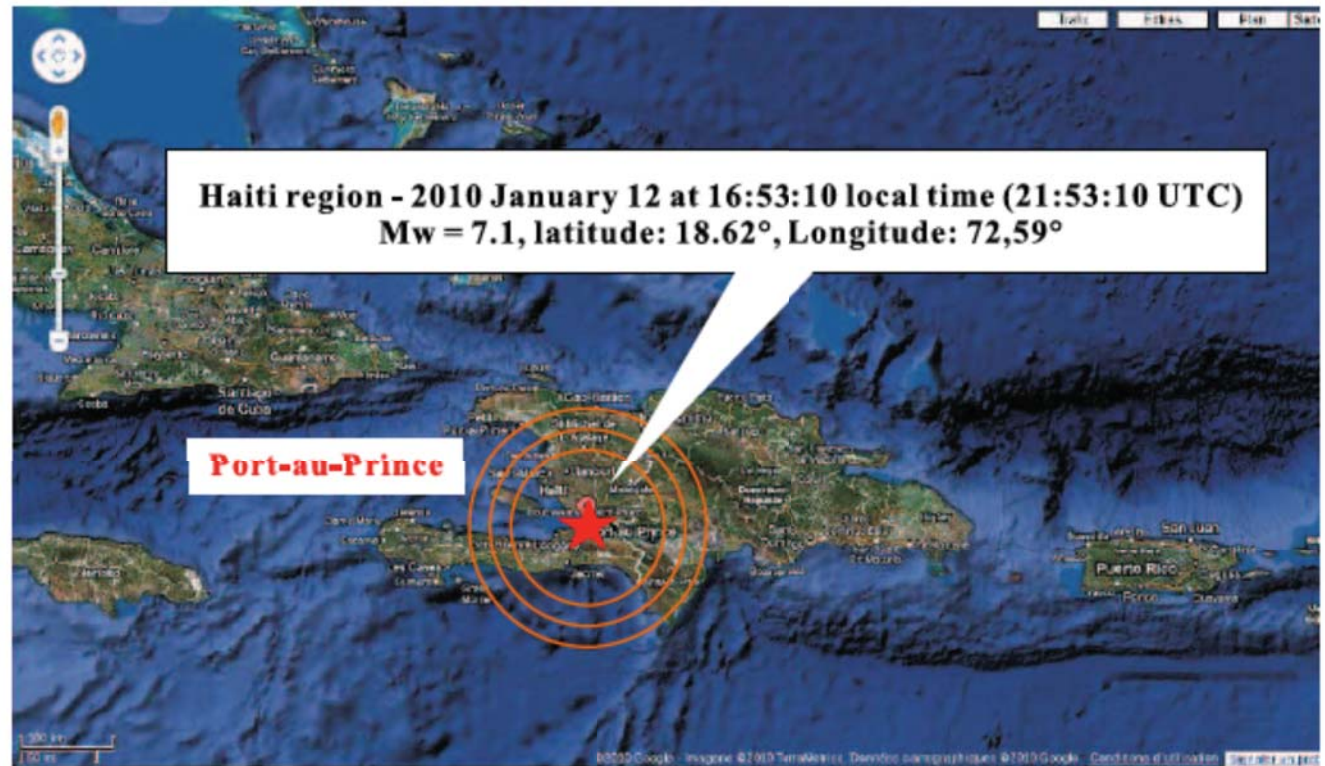
Dept. Seismology, I.P.G., Paris; France

Overview

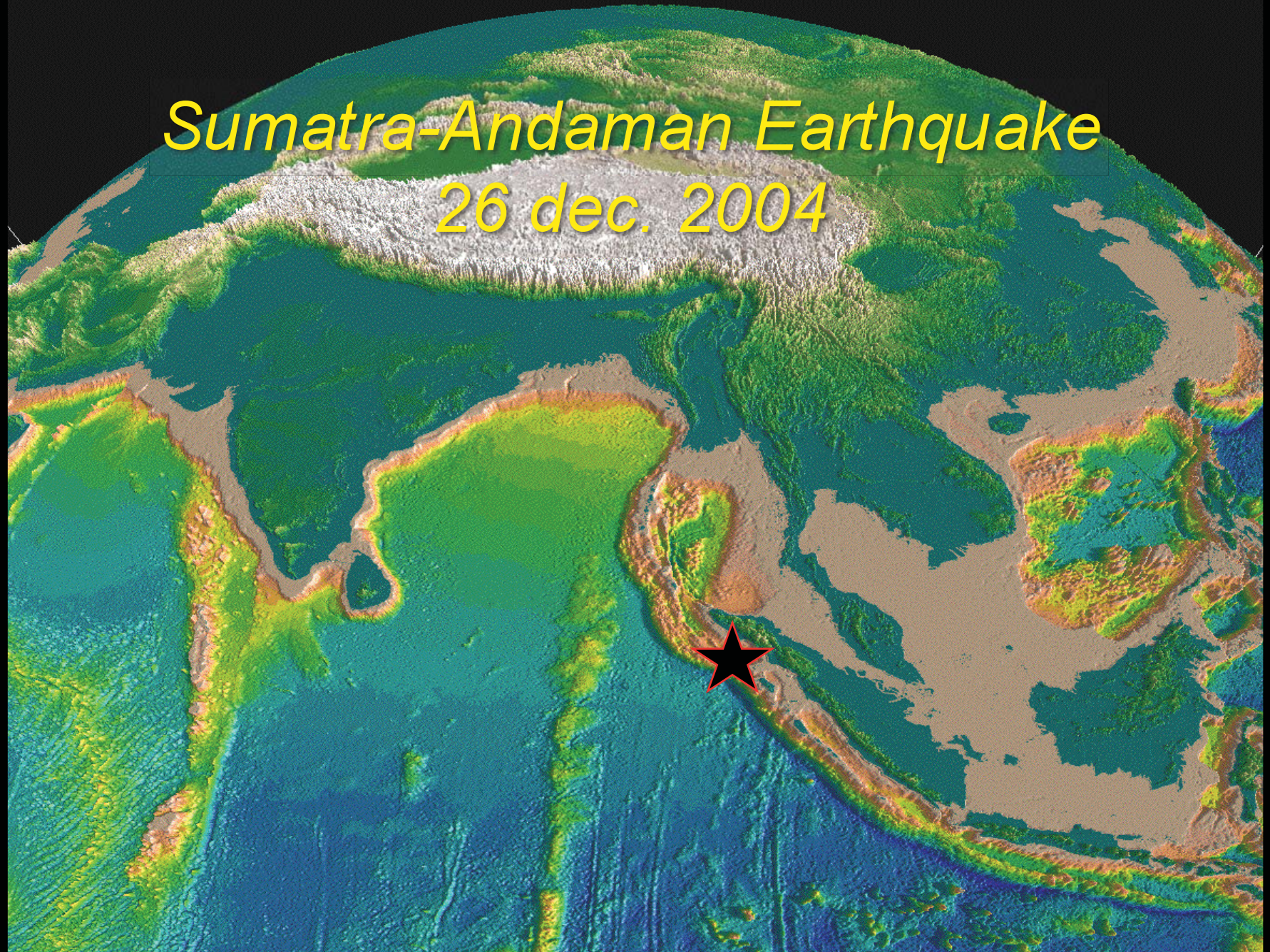
Large scale Seismology: an observational field

- Data (Seismic source) + Instrument (Seismometer) -> Observations (seismograms)
- Historical evolution: Ray theory, Normal mode theory, Numerical techniques (SEM, NM-SEM)
- Scientific Issues: Earthquakes (Sumatra-Andaman 04, Haiti 10),
Anisotropic structure of the Earth
- Tomographic Technique
- Geodynamic Applications: continental deformation
Seismic Experiment: Plume detection
- Adjoint and time reversal methods

Haiti earthquake, Jan. 12, 2010



Sumatra-Andaman Earthquake
26 dec. 2004



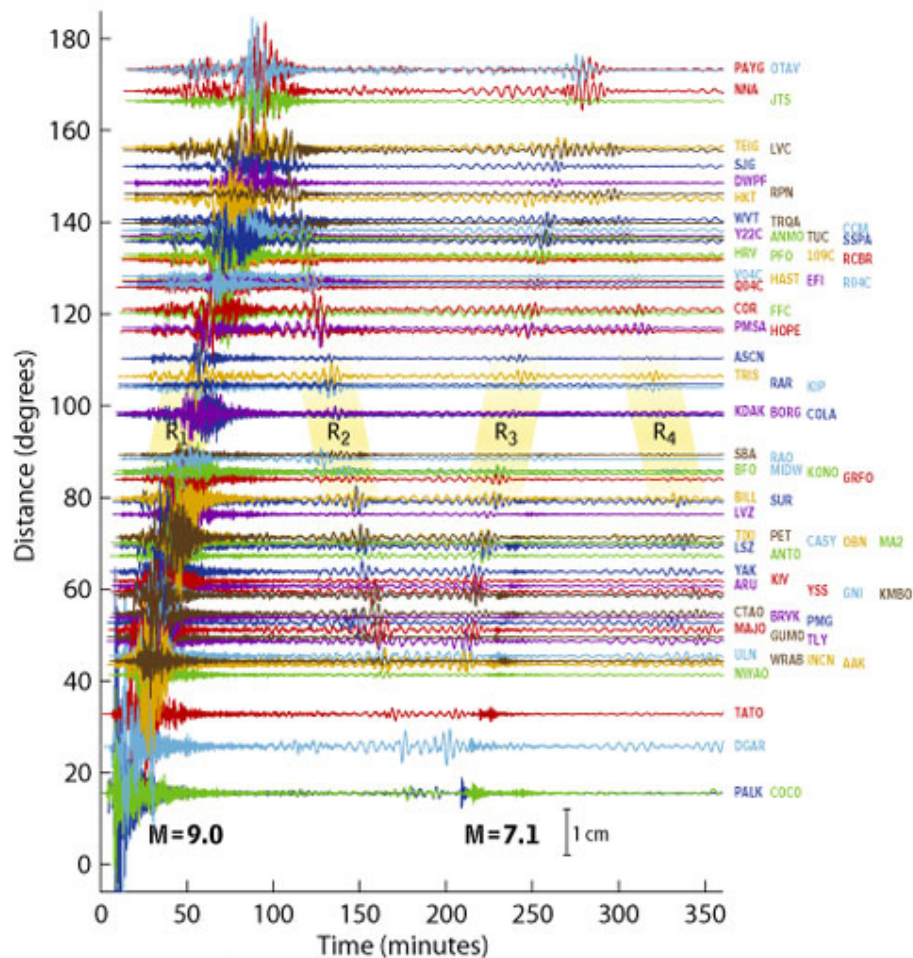
Sumatra-Andaman Earthquake

26 dec. 2004



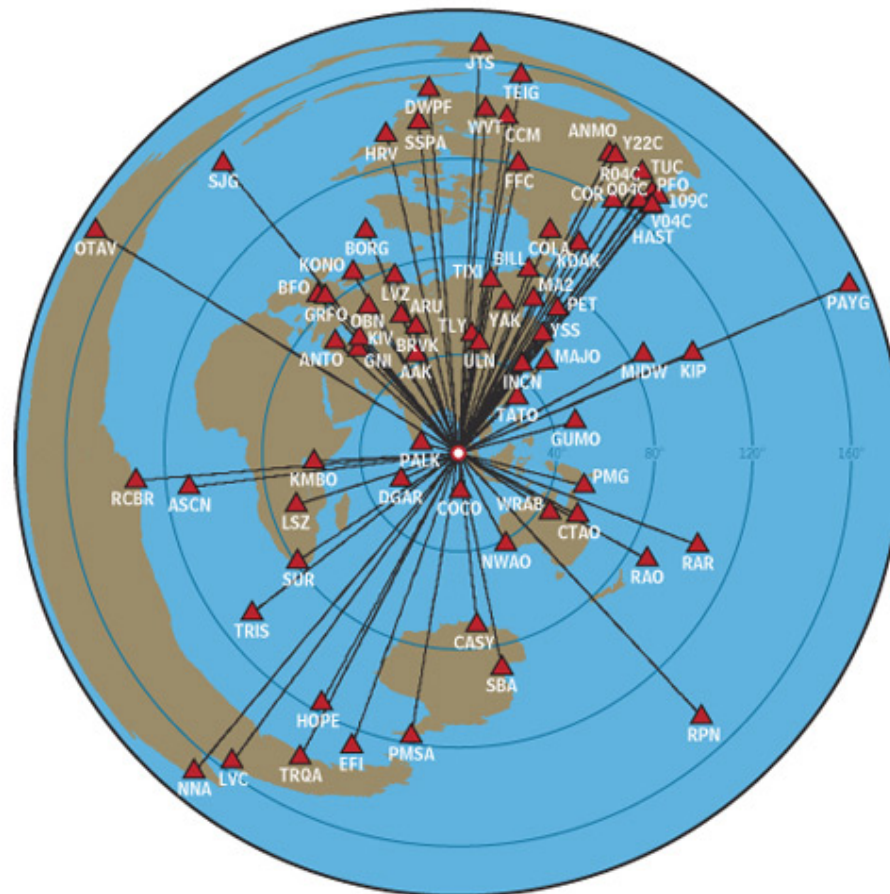
Sumatra - Andaman Islands Earthquake ($M_w=9.0$)

Global Displacement Wavefield from the Global Seismographic Network



Sumatra - Andaman Islands Earthquake

Global Seismographic Network Stations

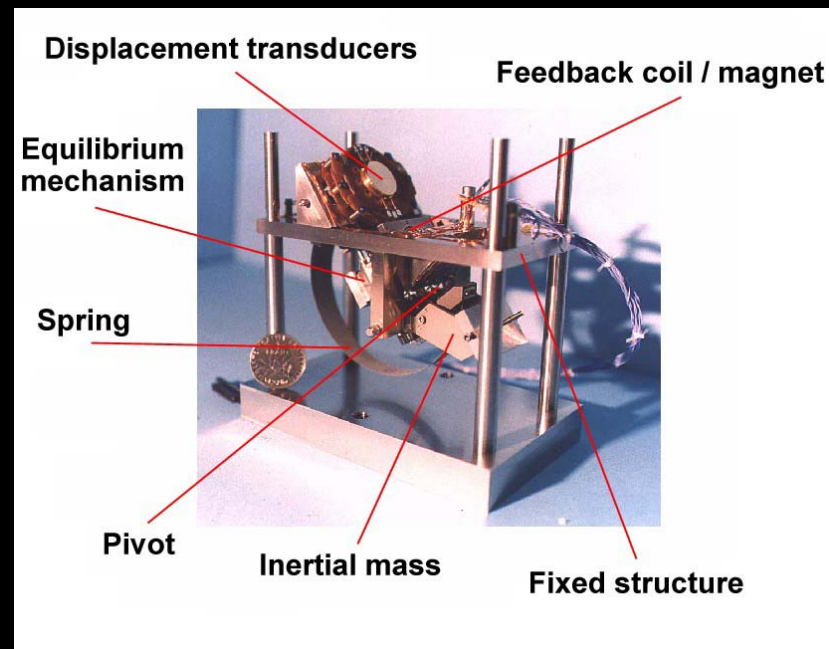


Seismic Instruments

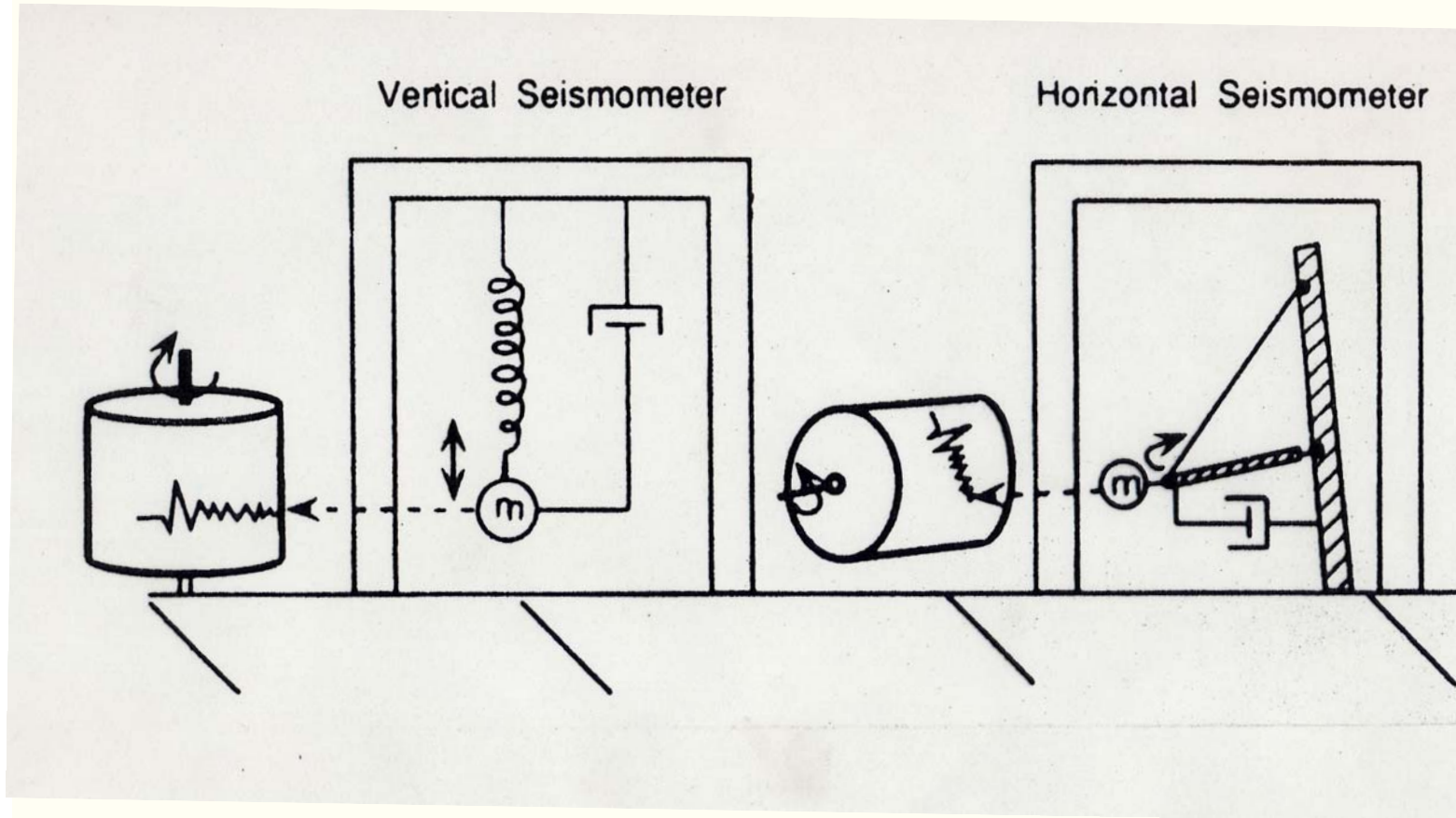
- Seismoscope
(China -100BC)



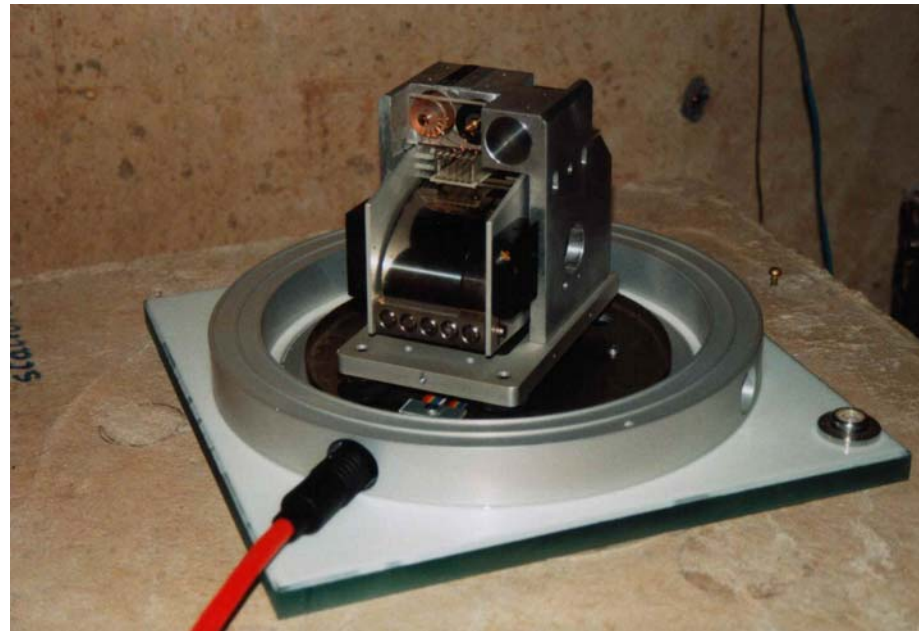
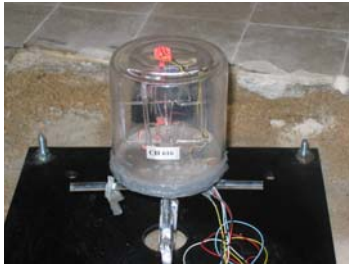
Broadband
Seismometer
(1mHz-20Hz)
(Cacho, 1998)



Principle of a Seismometer

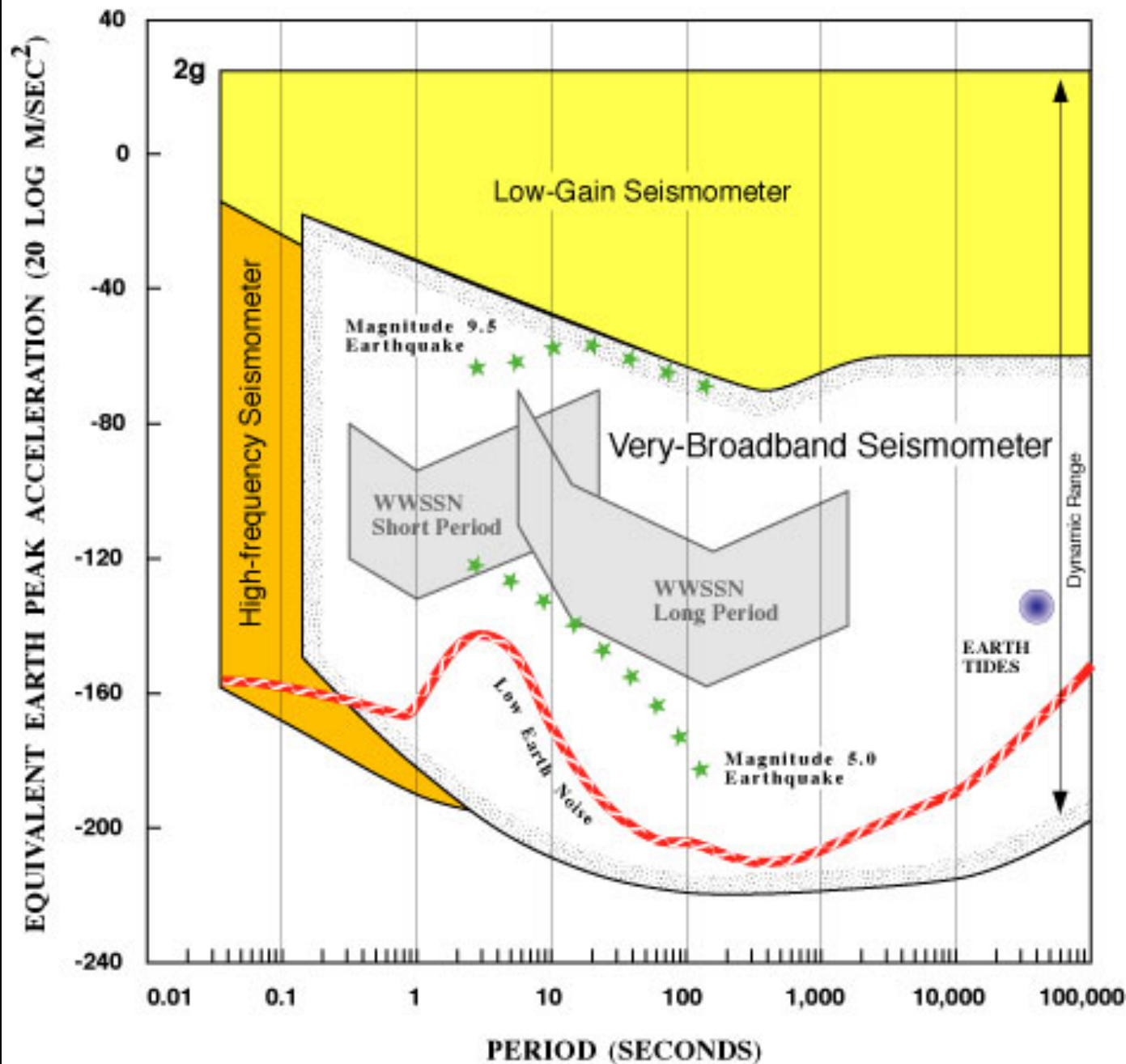


Tiltmeter (1960)



Broadband Seismometer (1982)
Streckeisen STS1: $0.05\text{s} < T < 5000\text{s}$

IRIS GSN SYSTEM

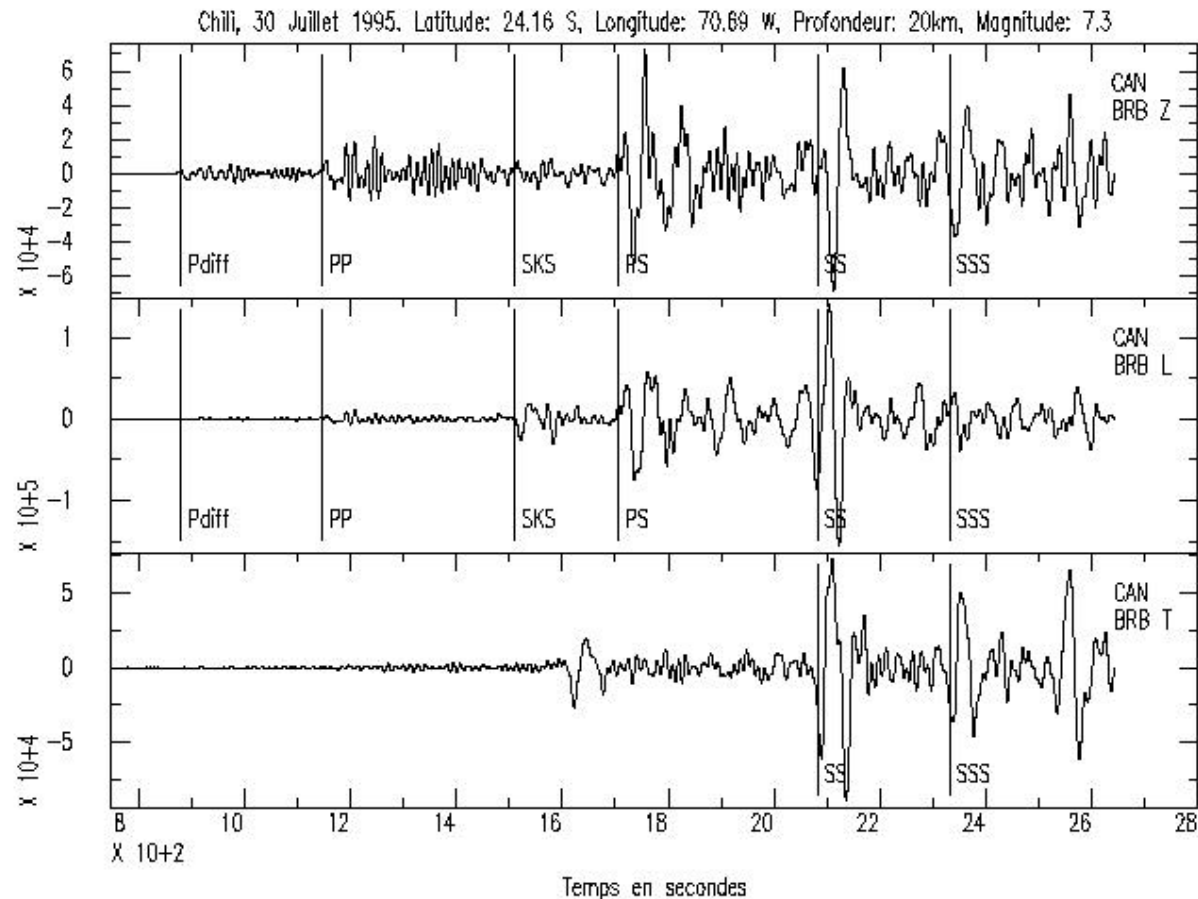


Butler et al., 2004

3 components

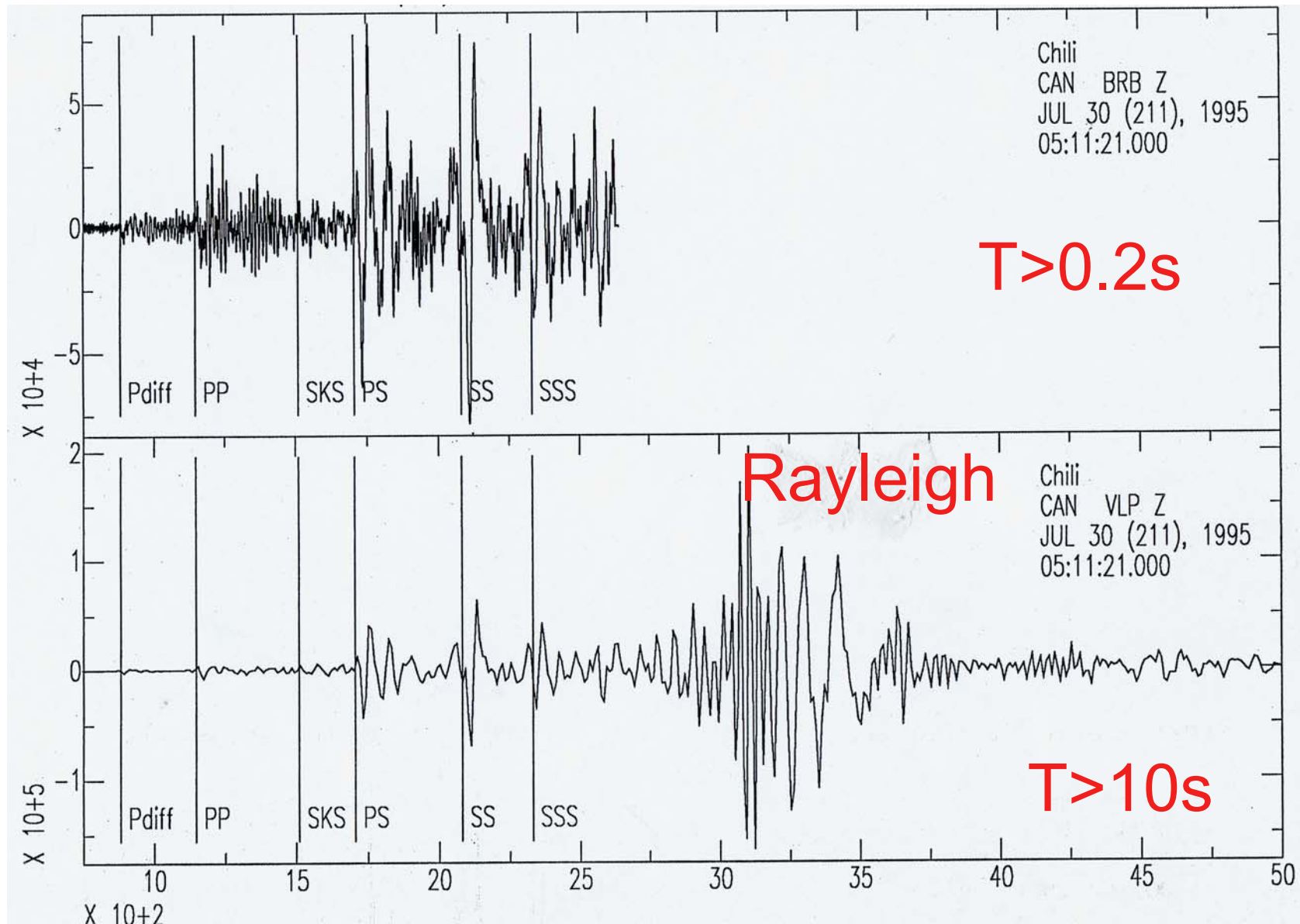
frequency range: 1mHz-20Hz
Period range: 0.05-1000s

Chile July 30, 1995, Ms=7.3

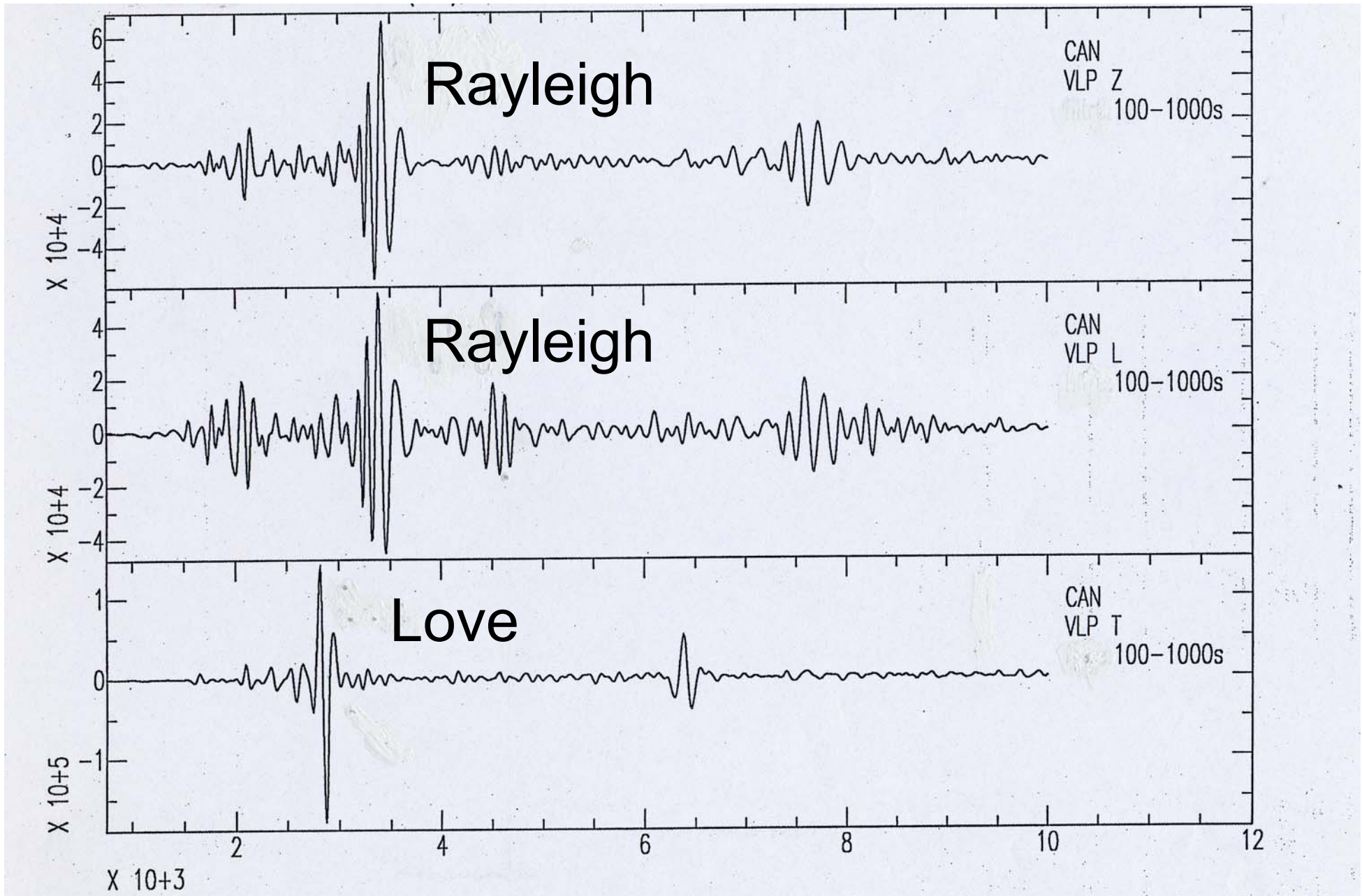


Chile earthquake magnitude= 7.3

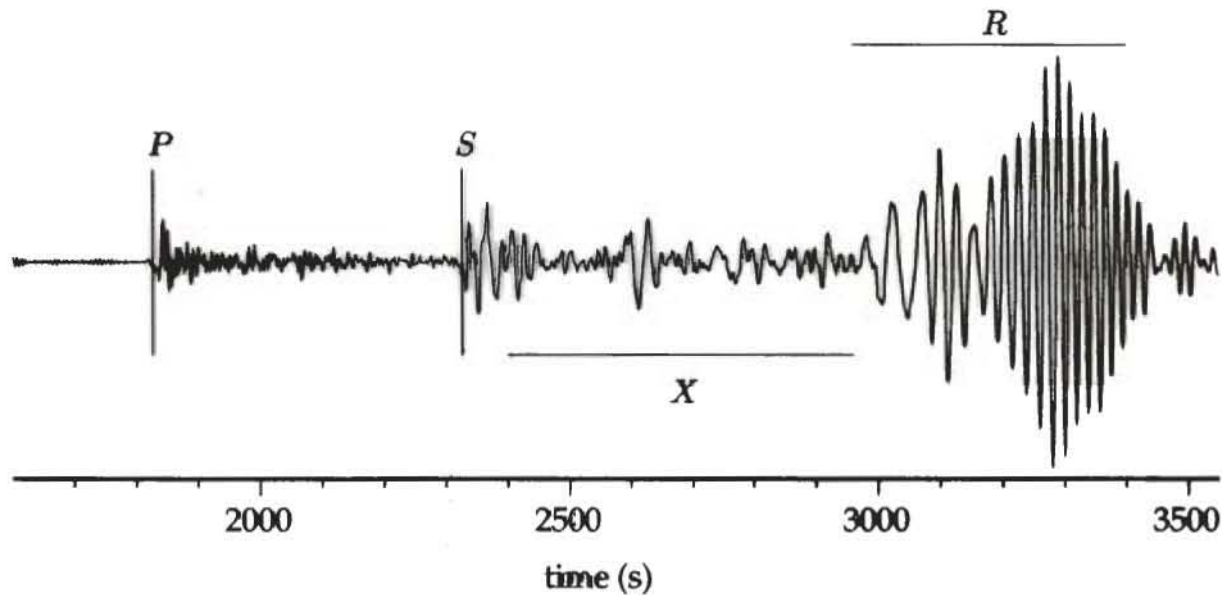
Epicentral distance = 12,300km-depth 20km



Chile Earthquake Jul. 1995



- Dispersive waves,
- Good global coverage,
- Large scale heterogeneities (min. 600 km).

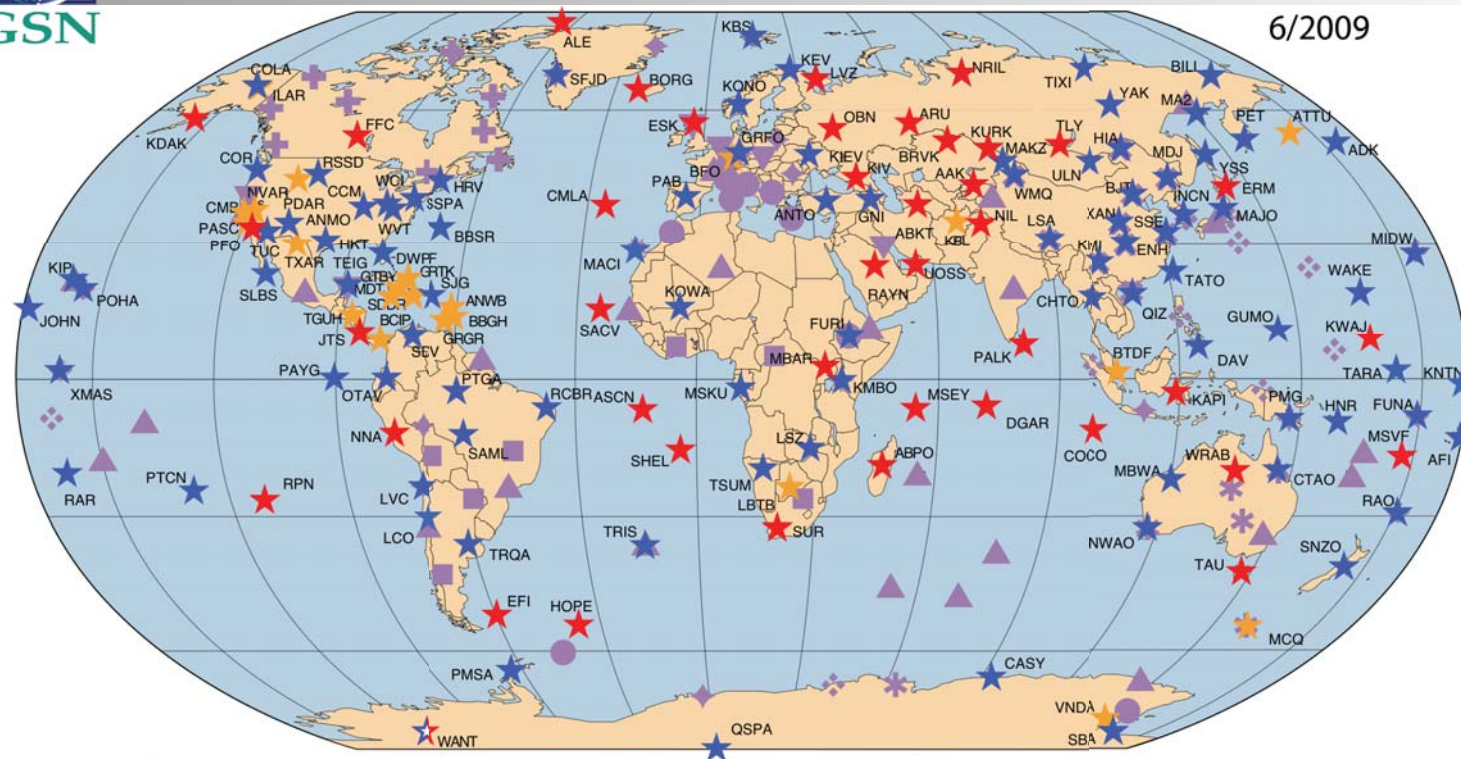


Vertical component of displacement field recorded at DRV station corresponding to the New-Guinea 05/16/1999 earthquake.

F.D.S.N. (Federation of Digital Broadband Seismic Networks)



GLOBAL SEISMOGRAPHIC NETWORK FEDERATION OF BROADBAND DIGITAL SEISMIC NETWORKS (FDSN)



6/2009

- | | | | | | | | | | | |
|---|---------------------|--------|----------------------|---------|--------------------|-------|------|-------|-------|-------|
| ★ | IRIS / IDA Stations | ★ | IRIS / USGS Stations | ★ | Affiliate Stations | | | | | |
| ★ | Planned Stations | | | | | | | | | |
| | Australia | Canada | France | Germany | Italy | Japan | U.S. | China | Spain | Other |
| | * | + | ▲ | ◆ | ● | ◇ | ■ | × | ✱ | ▼ |

Ocean Bottom Observatories

=> International Ocean network (I.O.N.)

- 2/3 of the Earth are covered by water.
- seafloor seismometers enable:
 - To investigate oceanic regions with a better resolution
 - To fill gaps in the global coverage

I.O.N.

International Ocean Network

ION (International Ocean network) France, Italy, Japan, UK, U.S....

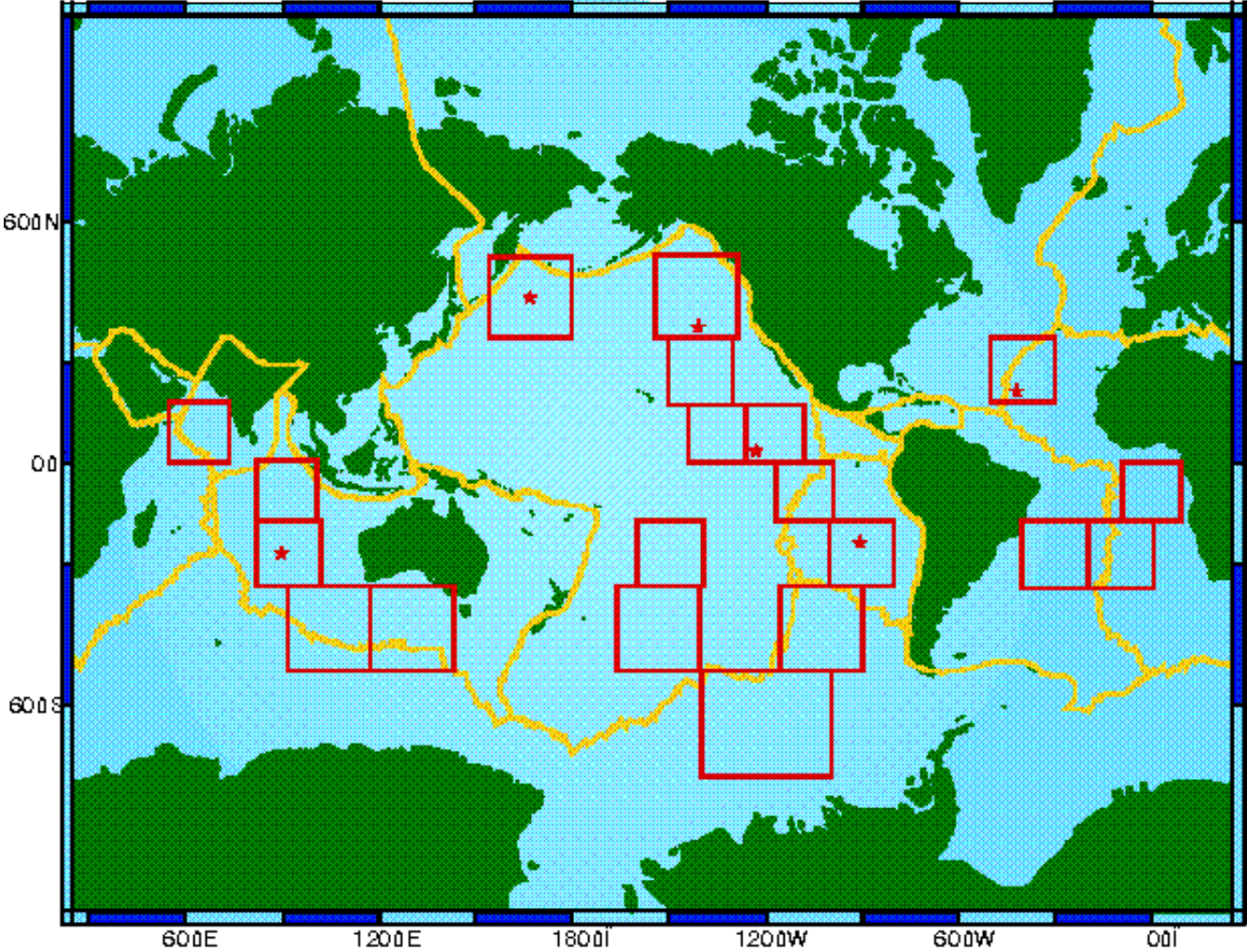
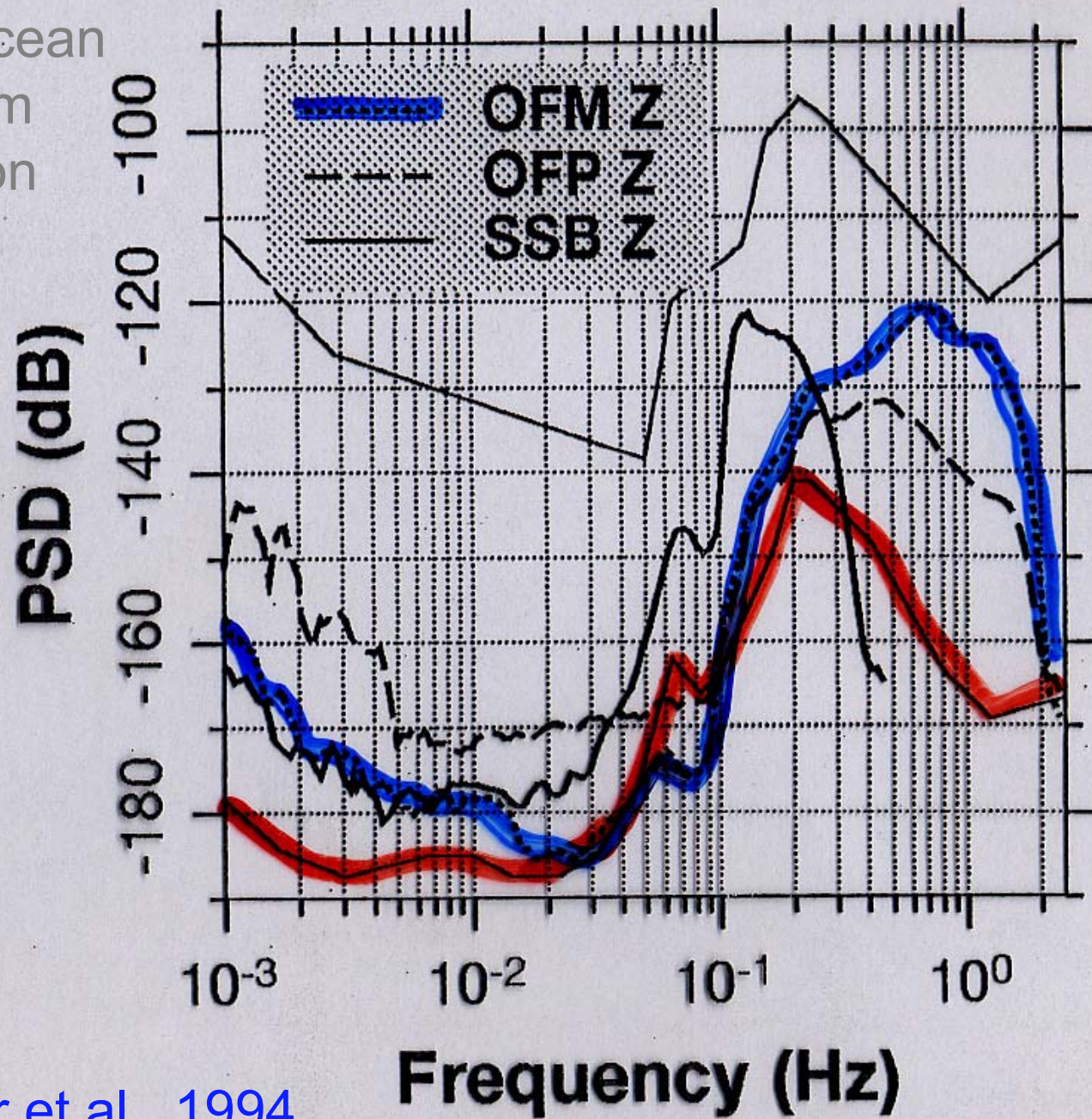


Figure 1: This map shows twenty regions which would require a seafloor seismic

OFM: Ocean
bottom
station

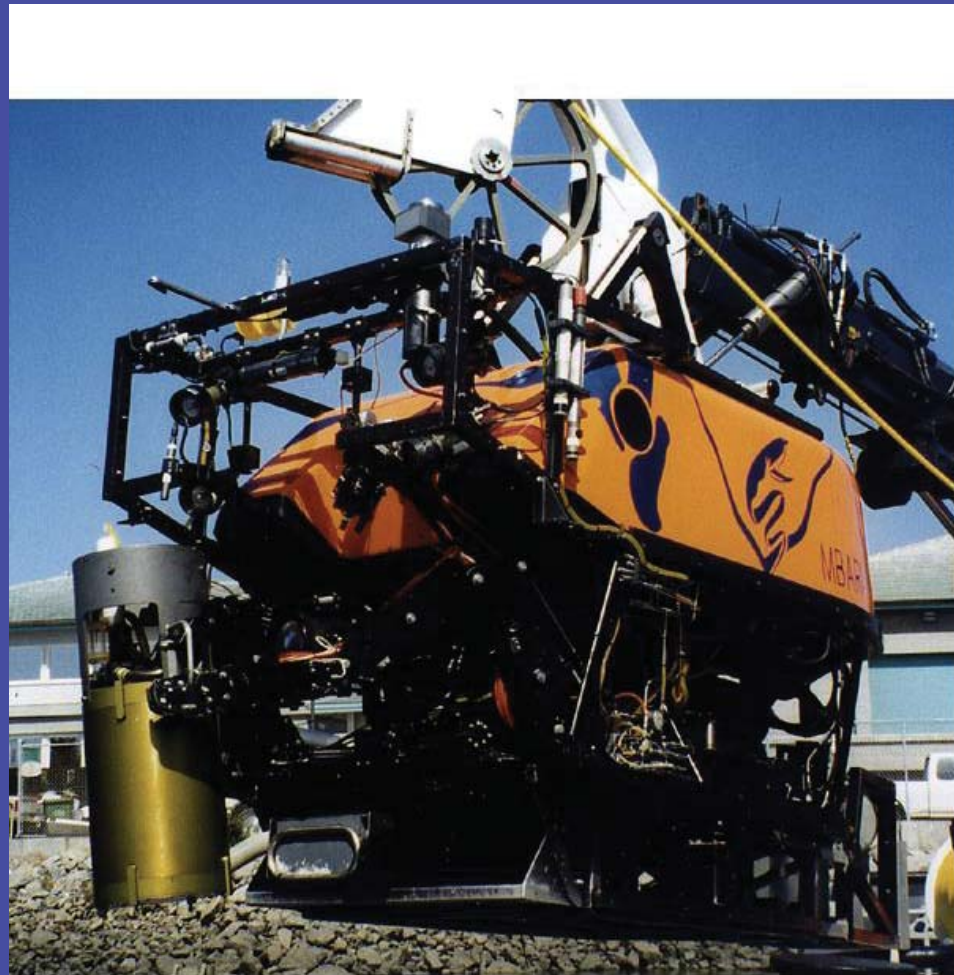




M.O.I.S.E (June-Sept. 1997)

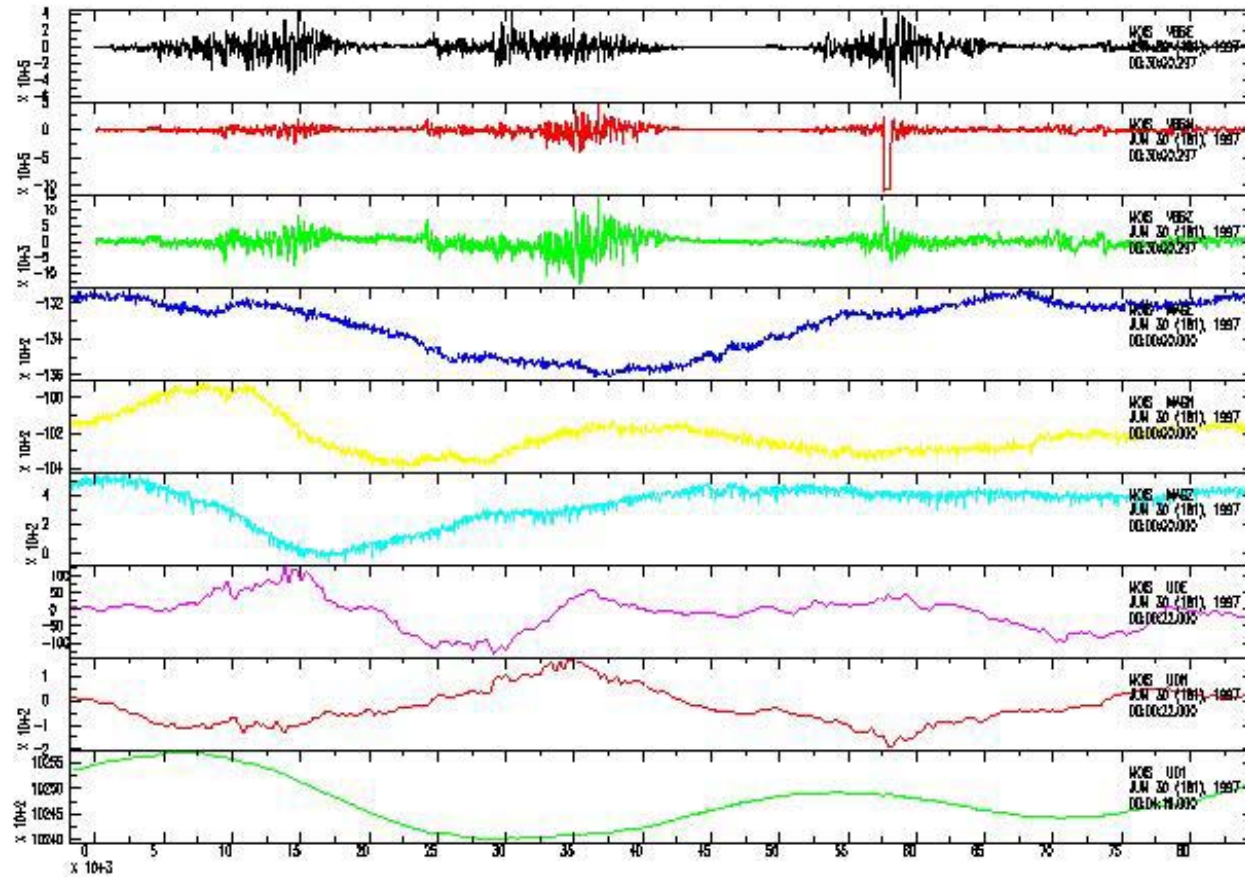
(Monterey bay Ocean bottom International Experiment)

MBARI, UC Berkeley, IPG-Paris, UBO-Brest

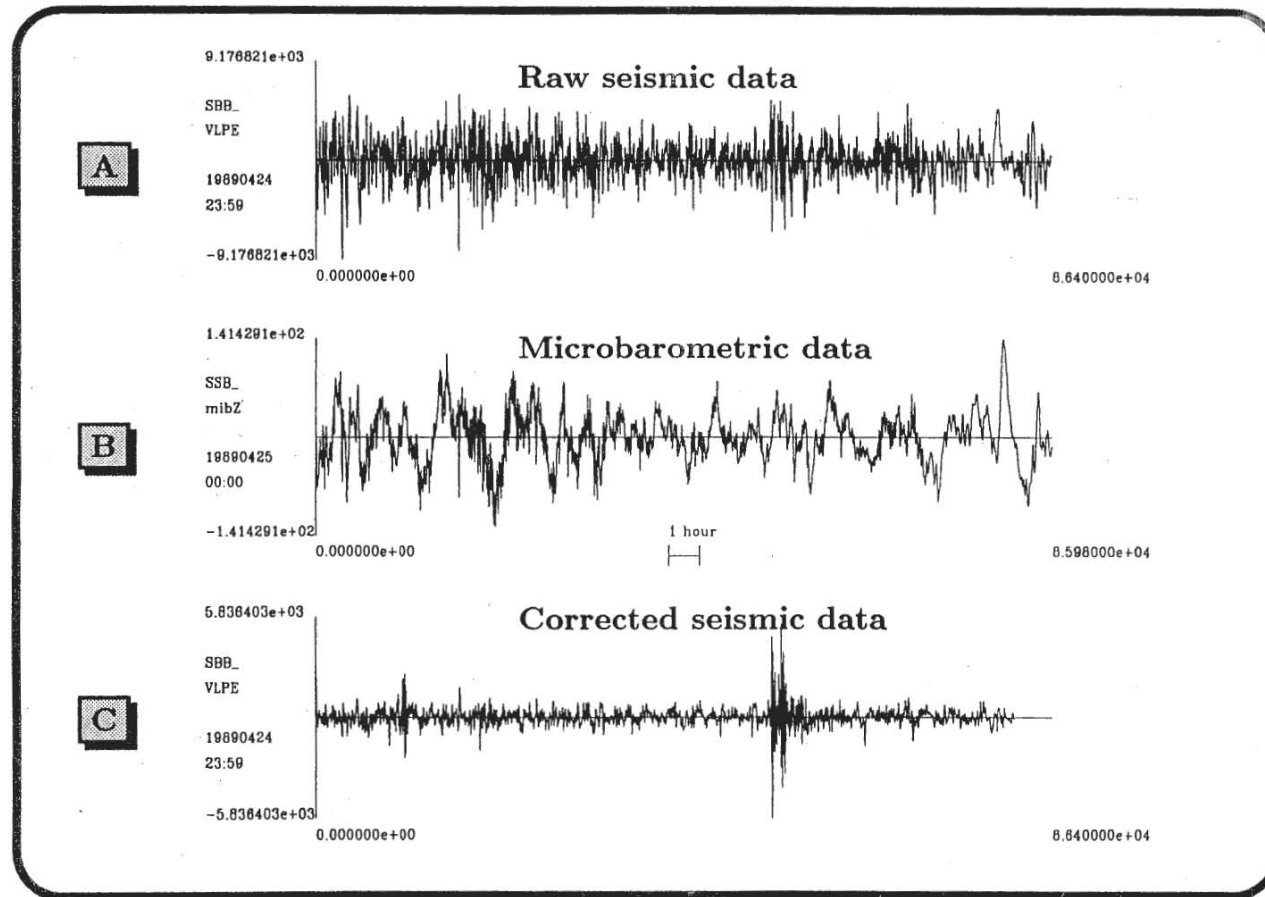




Multiparameter signals



Deconvolution of the seismic signal from the pressure influence

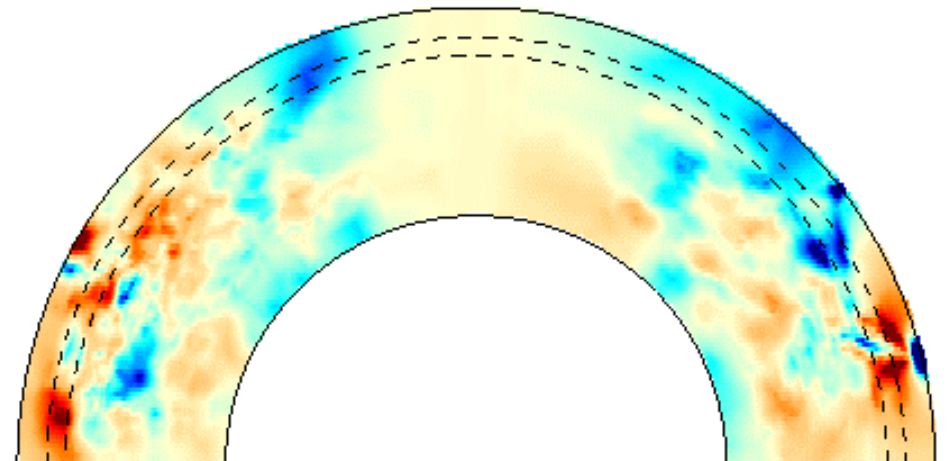




NERO observatory
Scientific Interest
Global scale

- To fill a gap in global station coverage
- To improve global tomographic model resolution
- To improve azimuthal distribution in determination of large earthquakes focal mechanisms

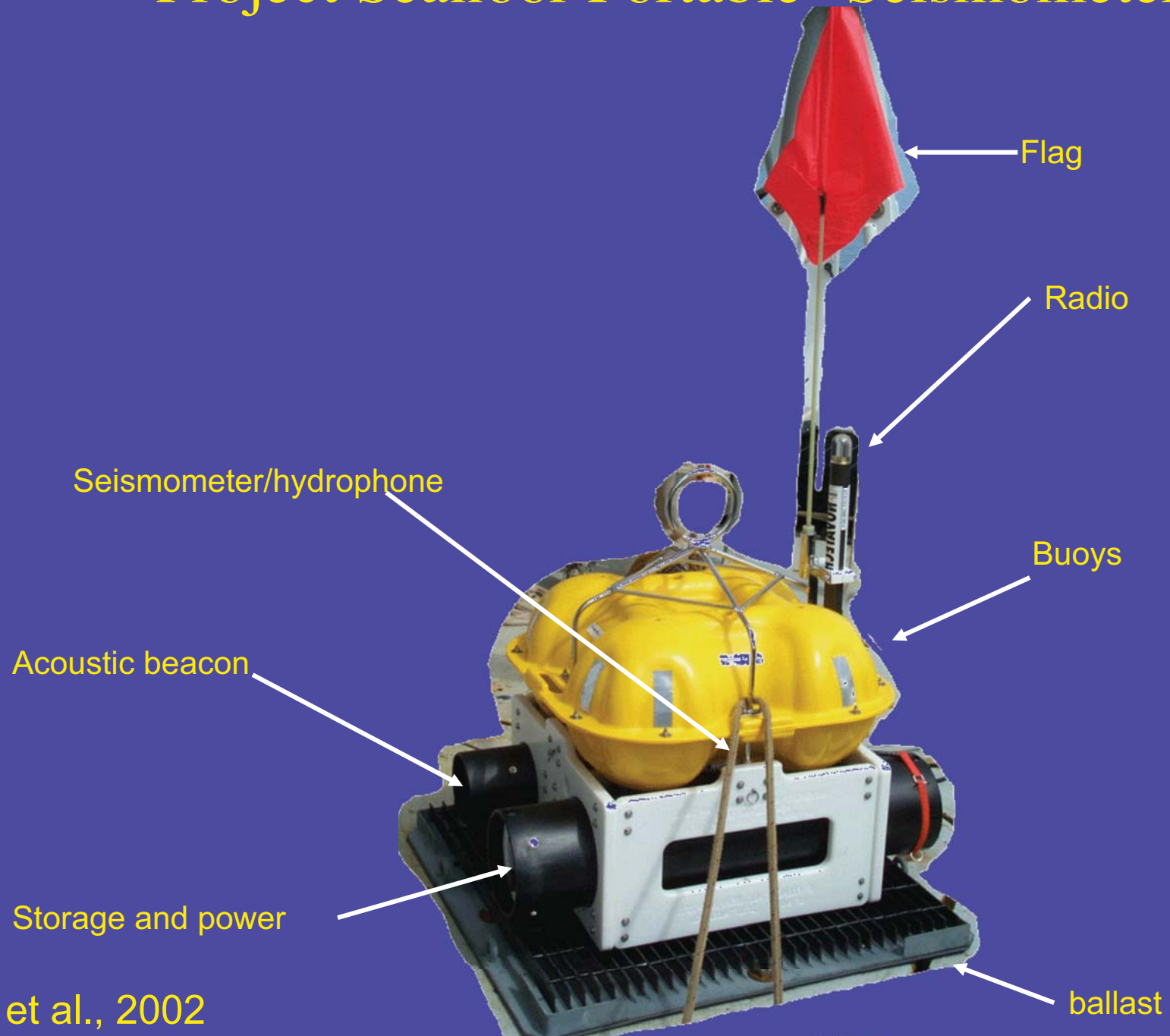
Karason & van der Hilst, 2003



NERO



Project Seafloor Portable Seismometers



Crawford et al., 2002

Overview

Large scale Seismology: an observational field

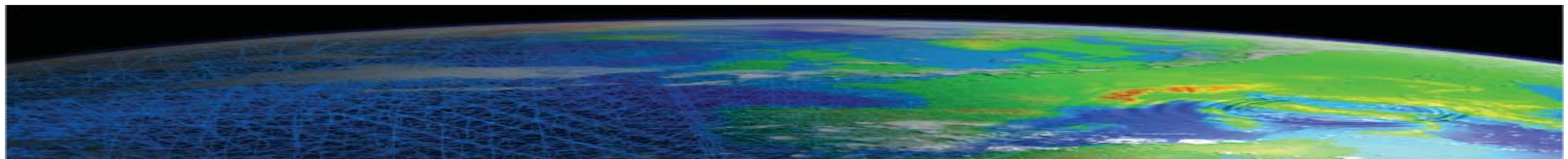
- ***Data (Seismic source) + Instrument (Seismometer) -> Observations (seismograms)***
New instruments
- Historical evolution: Ray theory, Normal mode theory, Numerical techniques (SEM, NM-SEM)
- Scientific Issues: Earthquakes (Sumatra-Andaman), Anisotropic structure of the Earth
- Tomographic Technique
- Geodynamic Applications
Seismic Experiment, Plume detection
- Adjoint and time reversal methods

Observing and inverting more than translations: rotations and strains

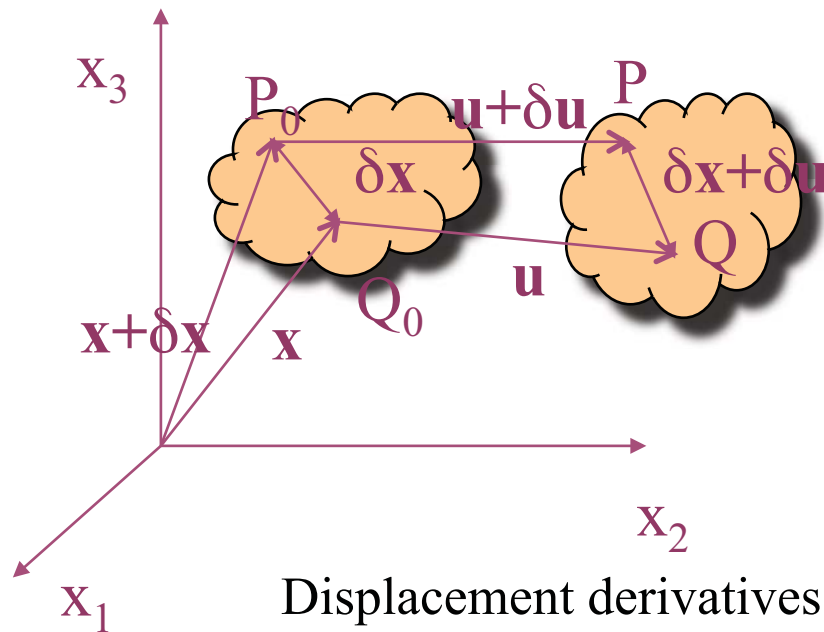
Johana Brokešová¹⁾ and Heiner Igel²⁾, Moritz Bernauer²⁾, and Andreas Fichtner²⁾

1) Charles University,
Department of Geophysics
V Holešovičkách 2, 180 00 Prague, Czech Republic

2) Ludwig-Maximilians-University,
Department of Earth Sciences – Geophysics
Theresienstrasse 41, 80333 Munich, Germany



Deformation of a continuum

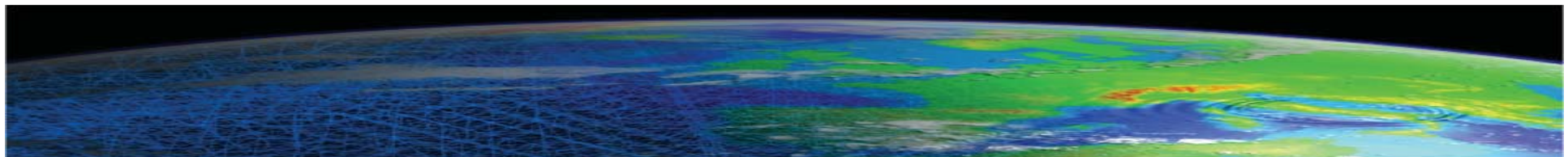


$P_0, Q_0 \dots$ undeformed medium
 $P, Q \dots$ deformed medium

$$u_i(\mathbf{x} + \delta\mathbf{x}) = u_i(\mathbf{x}) + \frac{\partial u_i(\mathbf{x})}{\partial x_j} \delta x_j + O\left(\frac{\partial \mathbf{u}}{\partial \mathbf{x}}\right)^2$$

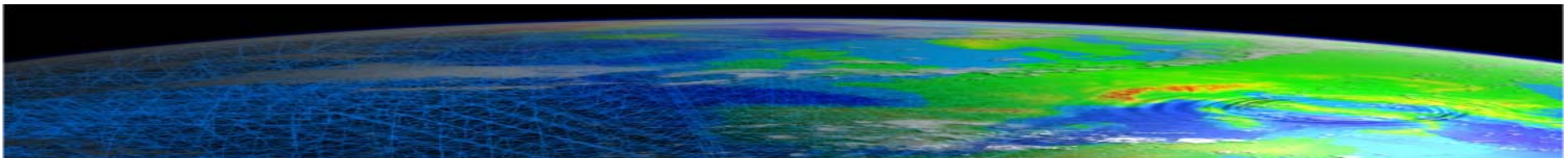
Displacement derivatives represent a second-rank tensor
 which can be resolved into
 a **symmetric** and **anti-symmetric** parts:

$$\frac{\partial u_i(\mathbf{x})}{\partial x_j} \delta x_j = \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \delta x_j + \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} - \frac{\partial u_j}{\partial x_i} \right) \delta x_j = \underbrace{\epsilon_{ij} \delta x_j}_{\text{strain tensor}} + \underbrace{\omega_{ij} \delta x_j}_{\text{rotation tensor}} = \underbrace{(\text{curl } \mathbf{u} \times \delta \mathbf{x})_i}$$

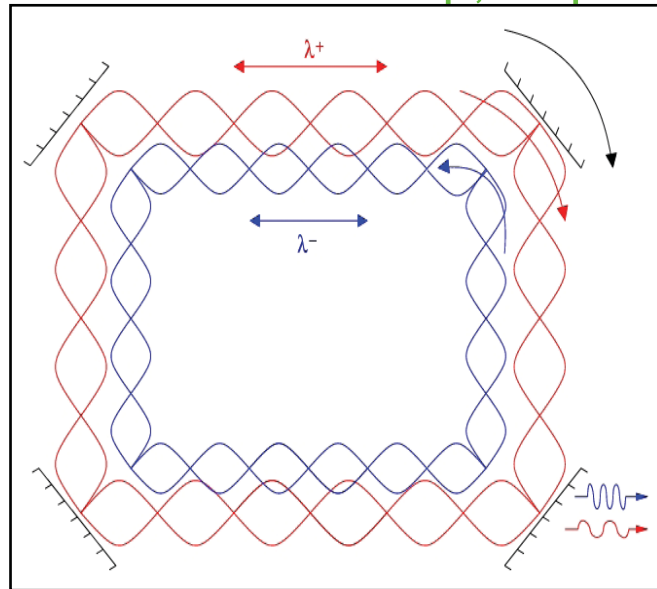


BASIC METHODOLOGIES OF SEISMIC ROTATIONAL MEASUREMENTS

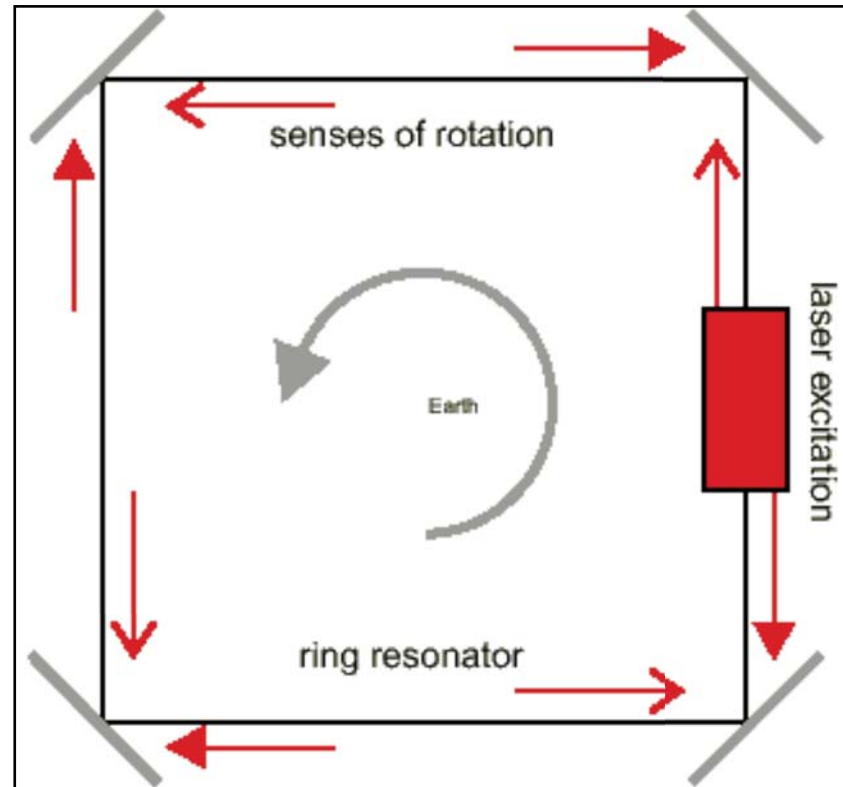
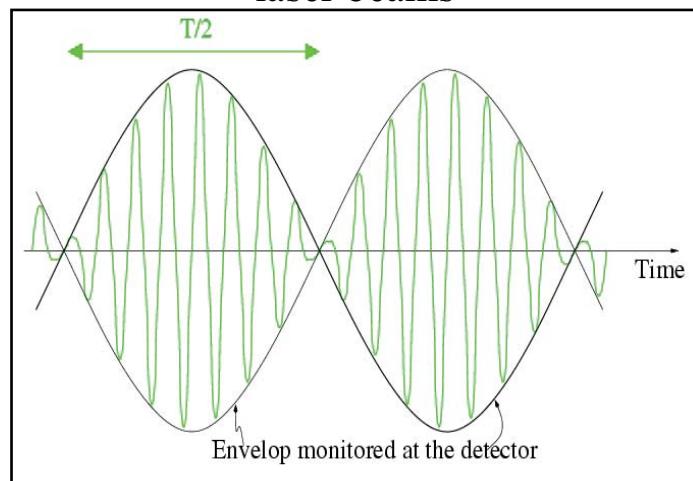
1. **Microarrays** measuring differential motions
(finite spatial derivatives)
2. **Ring laser gyroscopes** utilizing the Sagnac effect
3. **Small portable rotational sensors**



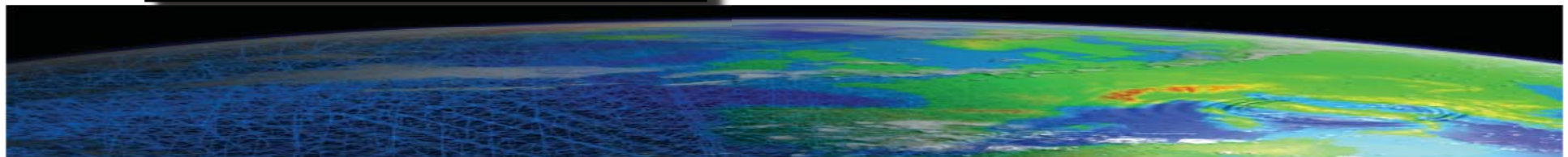
2. Ring lasers



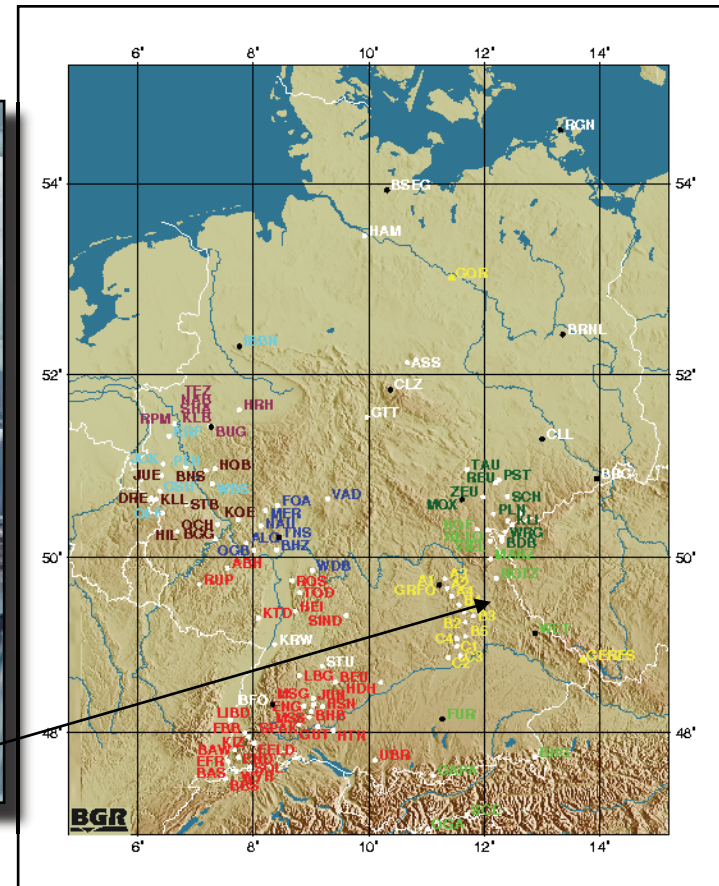
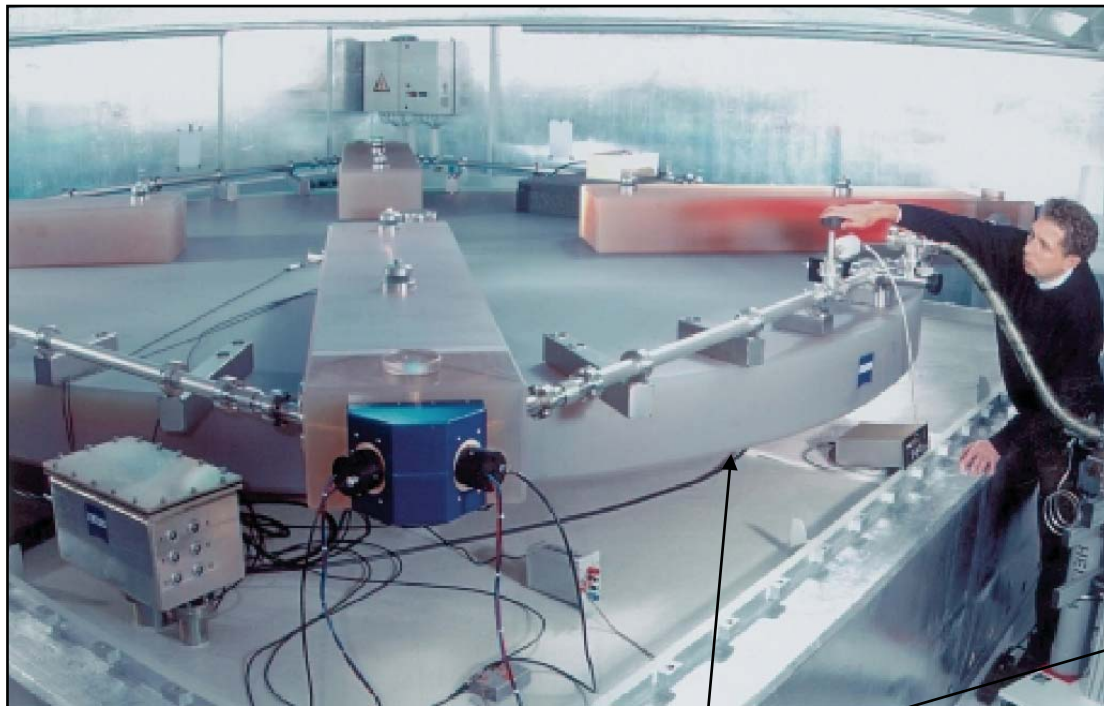
Superposition of co- and counter-rotating laser beams



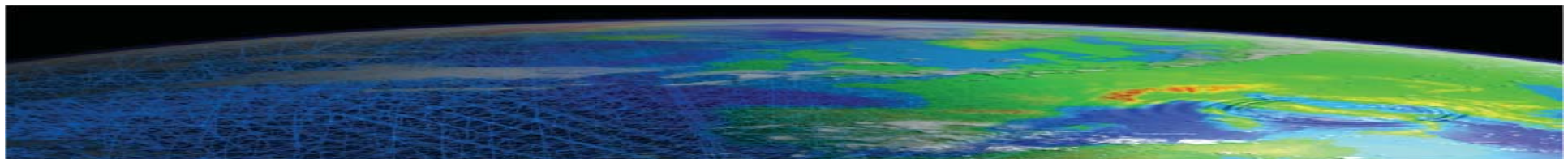
At the output, the frequency difference between the beams carries the information about the rotation rate.



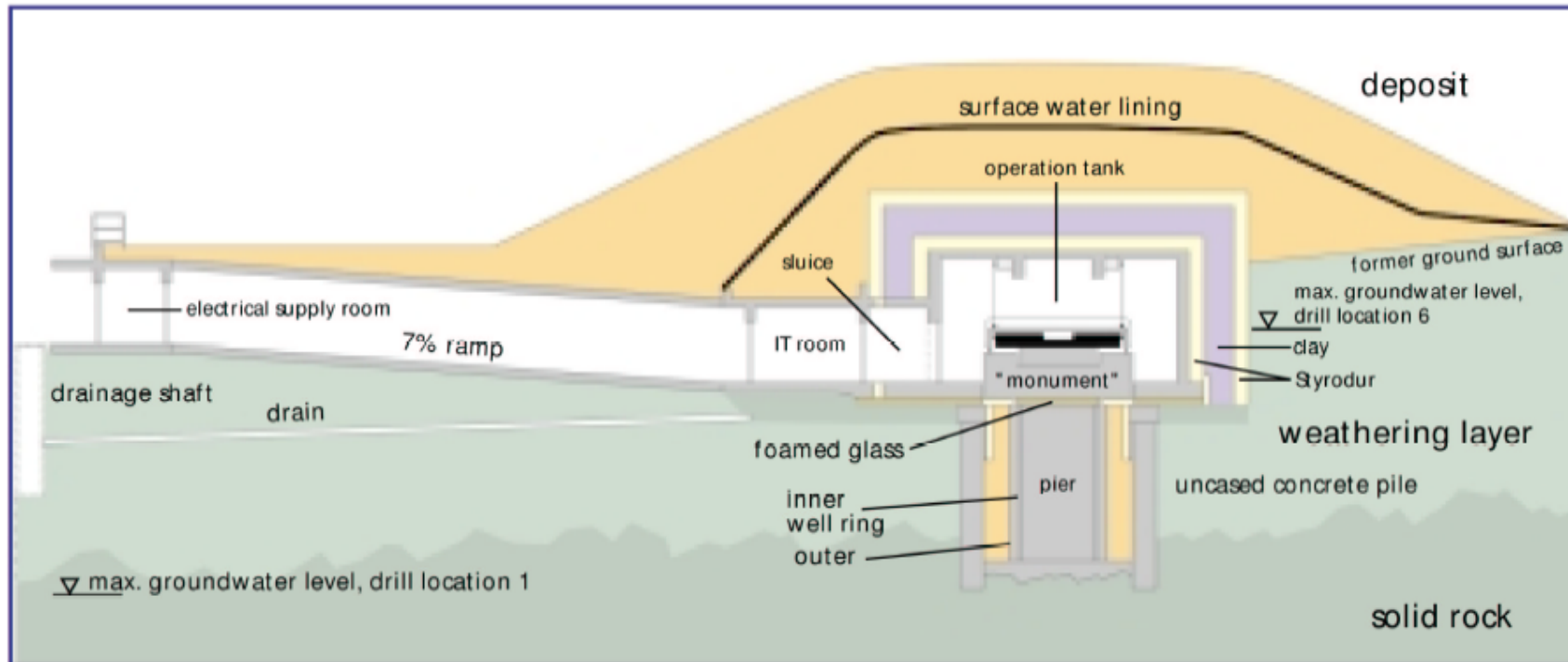
The ring laser at Wettzell



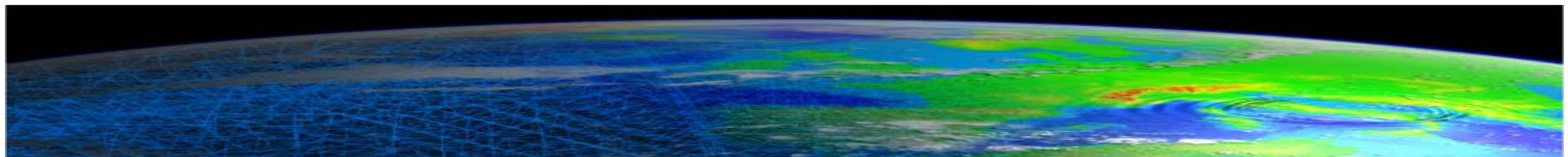
4 x 4 m ring laser
(resolution 10^{-12} rad/s)



Ring laser installation at Wettzell



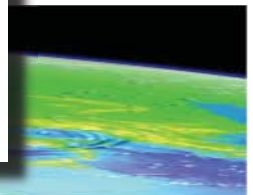
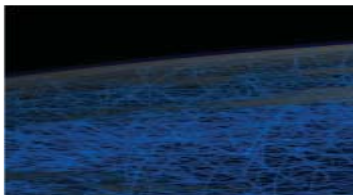
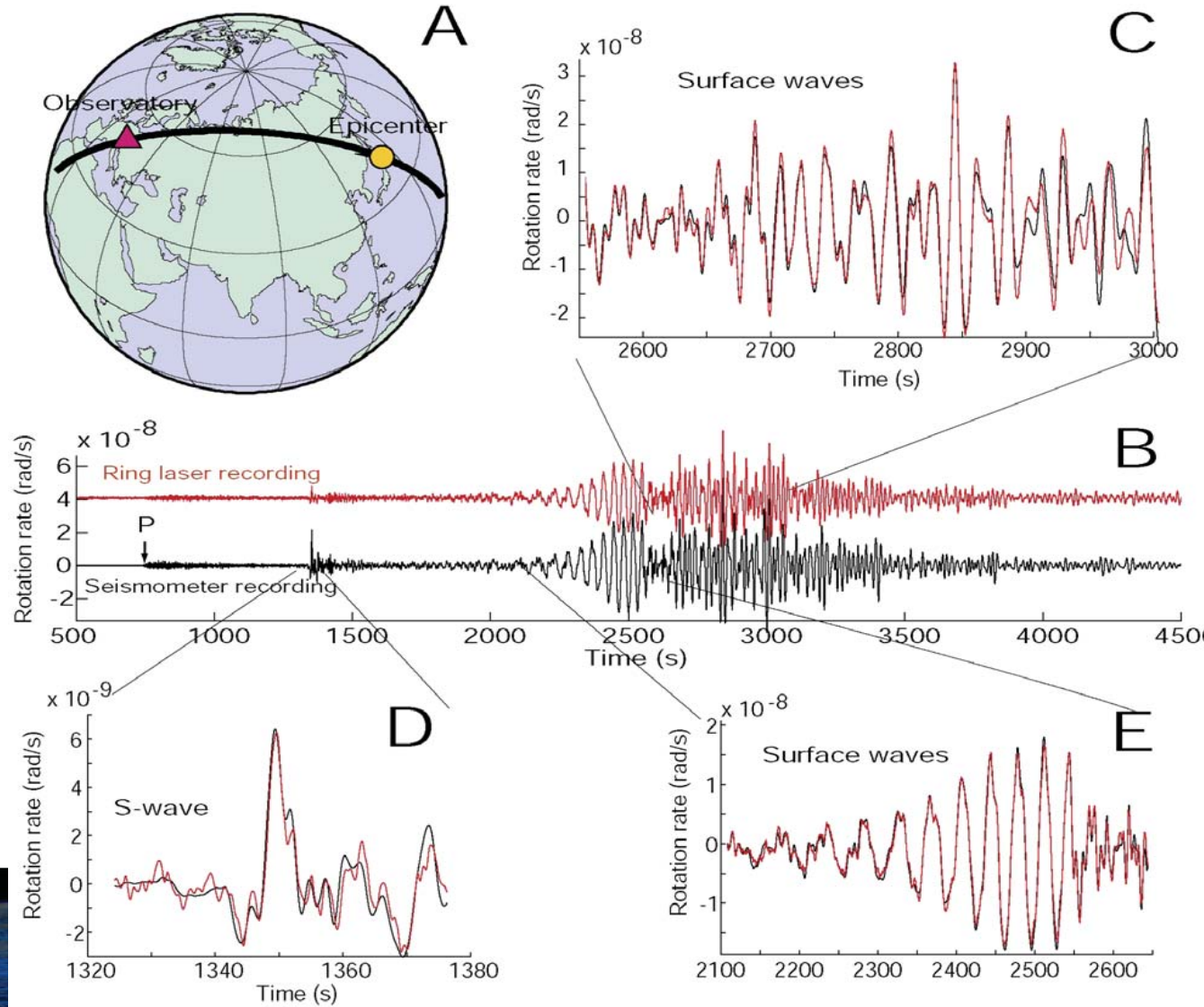
The cavern is located in southern Germany (49.1 N, 12.9 E)



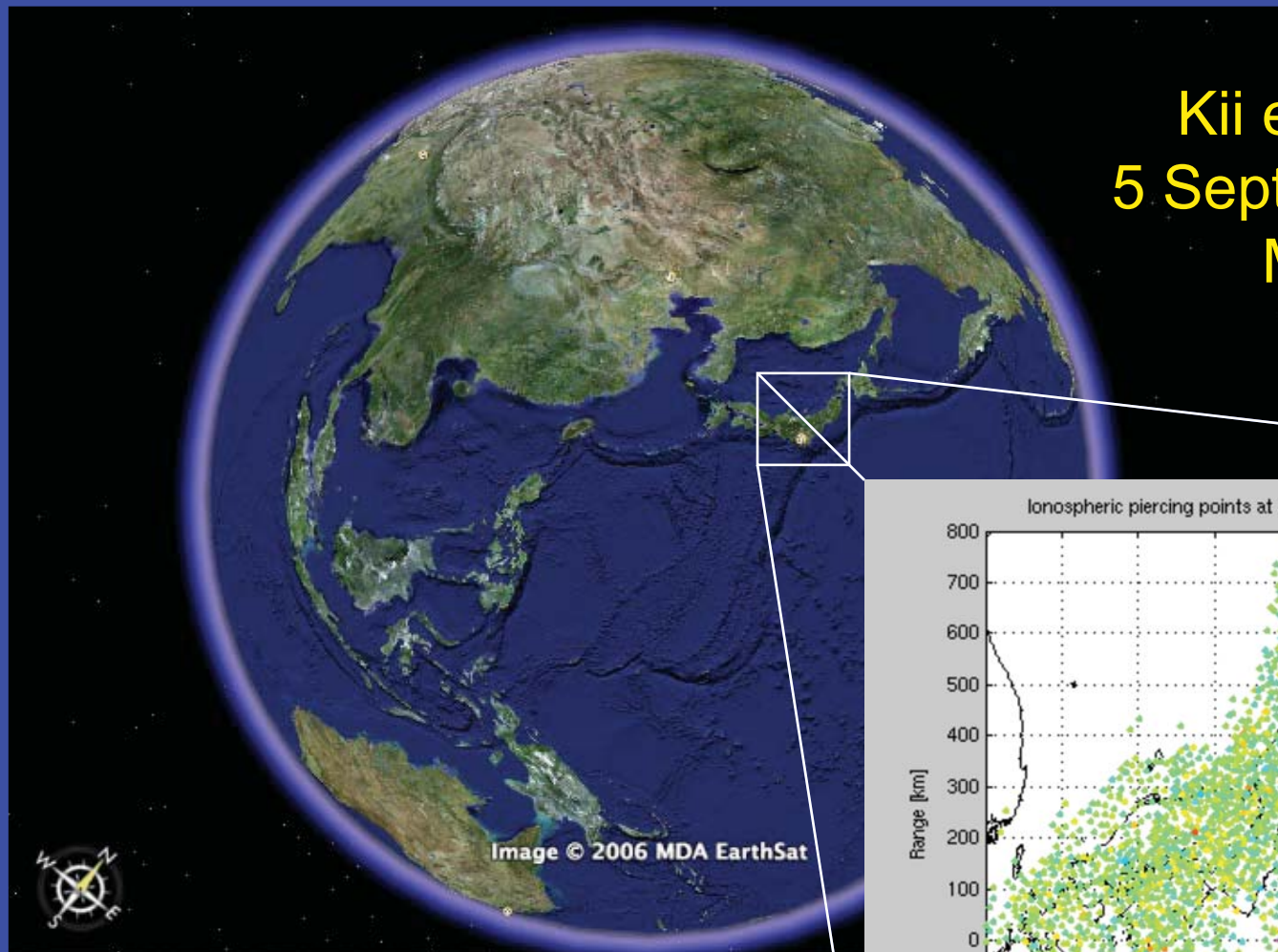
1st QUEST Workshop, Capo Caccia, Sardinia, September 19-26, 2010

Mw = 8.3 Tokachi-oki 25.09.2003 (Igel et al., GRL, 2005)

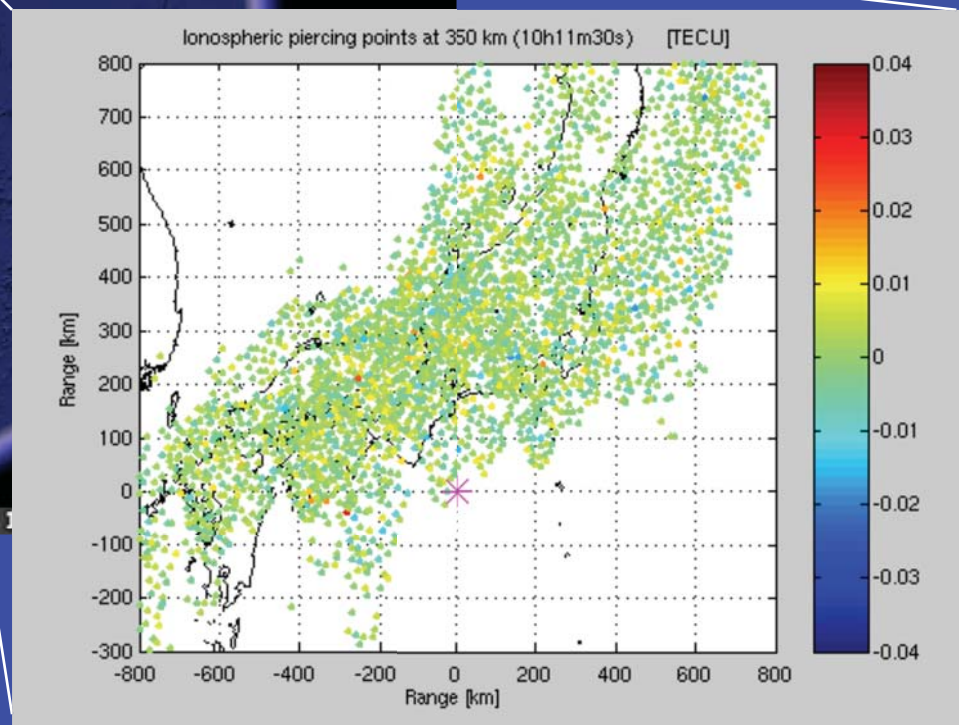
transverse acceleration – **rotation rate**



From Space: Terrestrial waves (in ionosphere)...

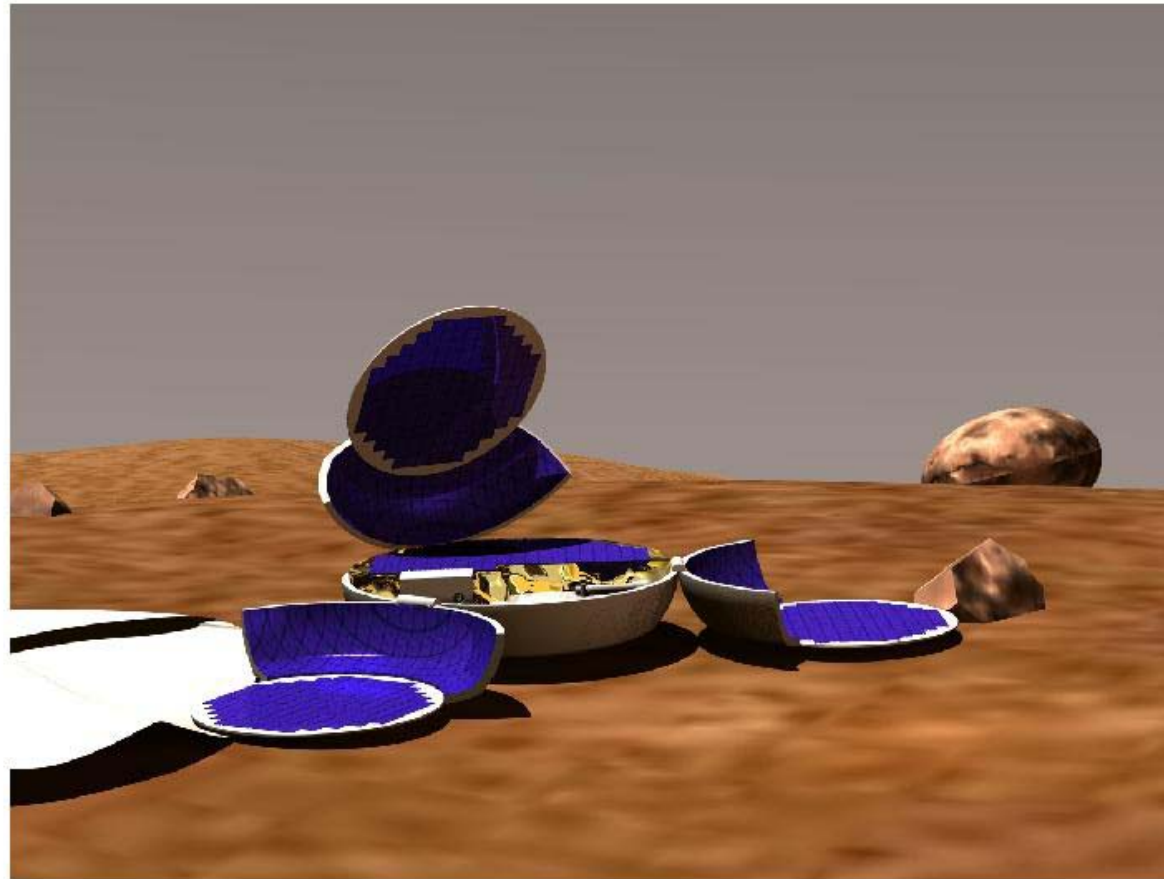


Kii earthquake
5 September 2004
Ms=7.4



Lognonne, 2006

EXPLORATION OF TERRESTRIAL PLANETS



NETLANDER: MARS

(Lognonné et al. 2004)

Overview

Large scale Seismology: an observational field

- Data (Seismic source) + Instrument (Seismometer) -> Observations (seismograms)
- **Historical evolution: Ray theory, Normal mode theory, Numerical techniques (SEM, NM-SEM)**
- Scientific Issues: Earthquakes (Sumatra-Andaman), Anisotropic structure of the Earth
- Tomographic Technique
- Geodynamic Applications
Seismic Experiment, Plume detection
- Adjoint and time reversal methods

Propagation of seismic waves

Hypothesis: Elastic Medium : $\sigma_{ij} = C_{ijkl} \varepsilon_{kl}$

Where ε_{kl} is the strain tensor, σ_{ij} the stress tensor

C_{ijkl} the elastic tensor: 81 elastic moduli

Symmetries of ε_{kl} , σ_{ij} and of the strain energy

$W = 1/2 \sigma_{ij} \varepsilon_{ij} \Rightarrow 21$ independent elements

Isotropic case $\Rightarrow 2$ independent elements

$$C_{ijkl} = \lambda \delta_{ij} \delta_{kl} + \mu (\delta_{ik} \delta_{jl} + \delta_{il} \delta_{jk})$$

λ , μ are Lamé parameters

Elastodynamic equation of motion

$$\partial_j (C_{ijkl} \partial_k u_l) - \rho \partial_{tt} u_i = 0$$

In the isotropic case, 2 solutions:

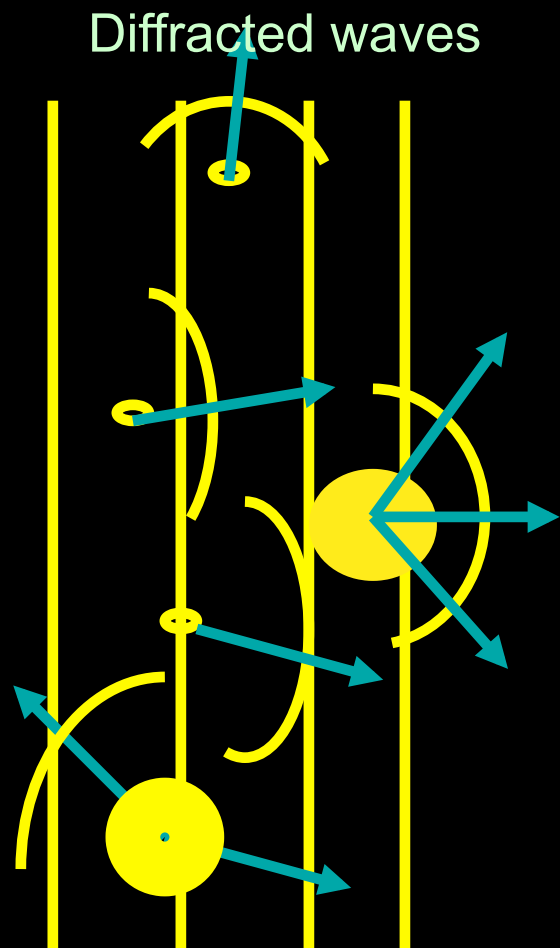
S-wave

P wave

In heterogeneous media, comparison between
Wavelength λ and scale of heterogeneity Λ

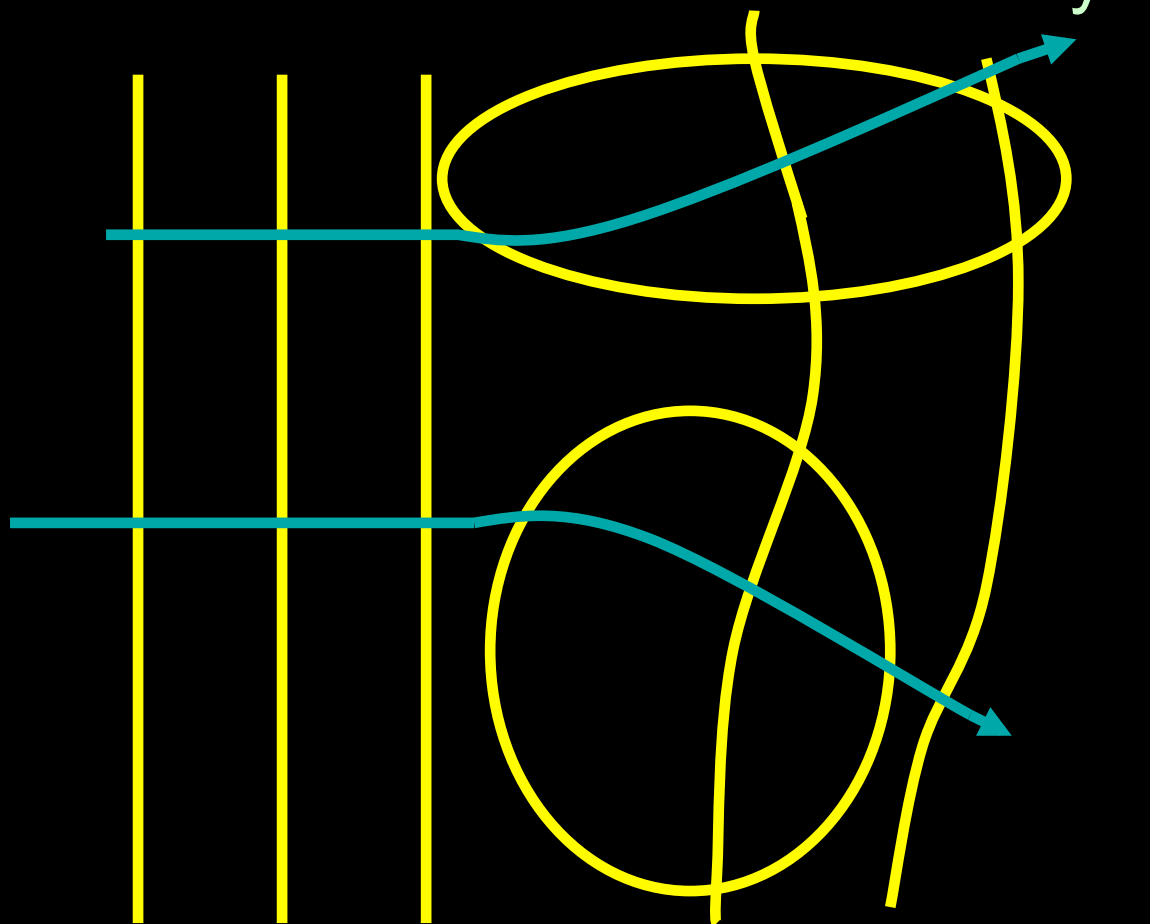
2 Two extremes cases $\lambda \gg \Lambda$ or $\lambda \ll \Lambda$

Λ heterogeneity scale, λ wavelength



wavefronts

$\lambda \sim \Lambda$ or $\lambda \gg \Lambda$



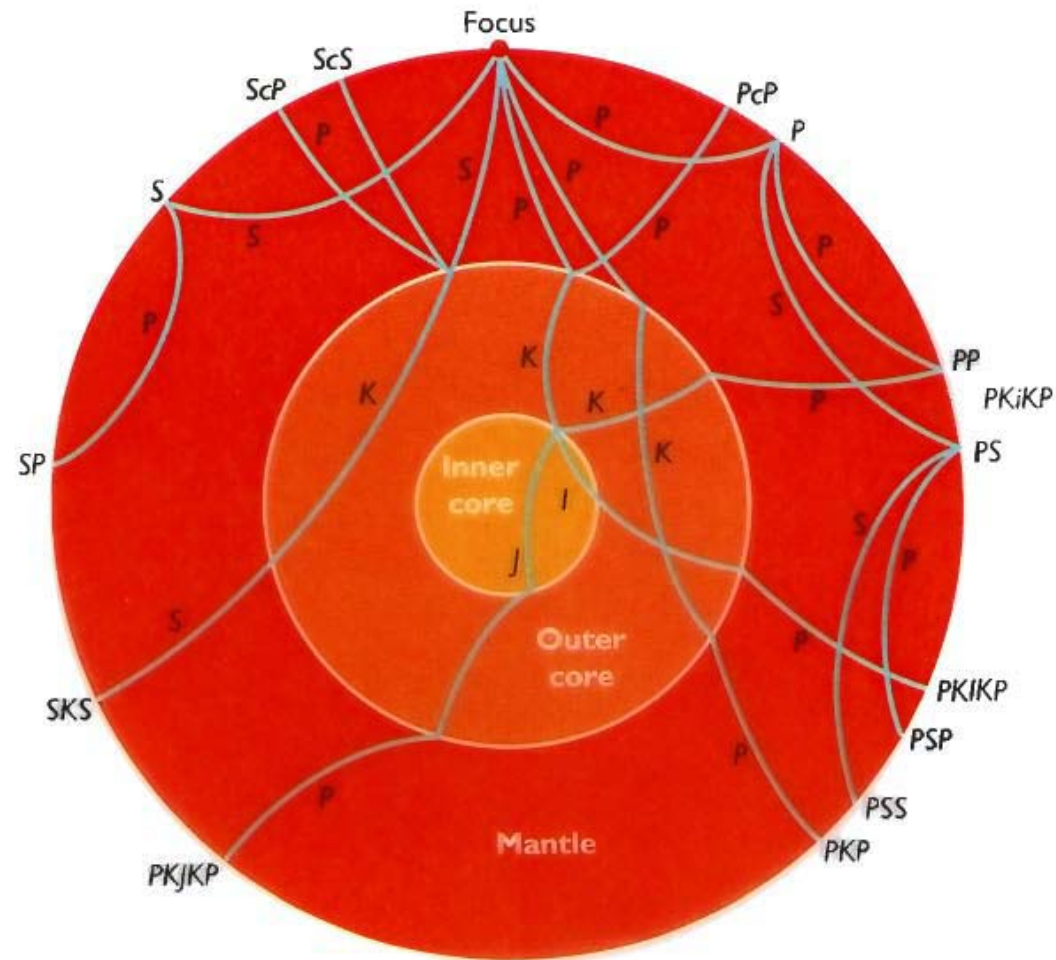
wavefronts

$\lambda \ll \Lambda$

Duality wave - particle:

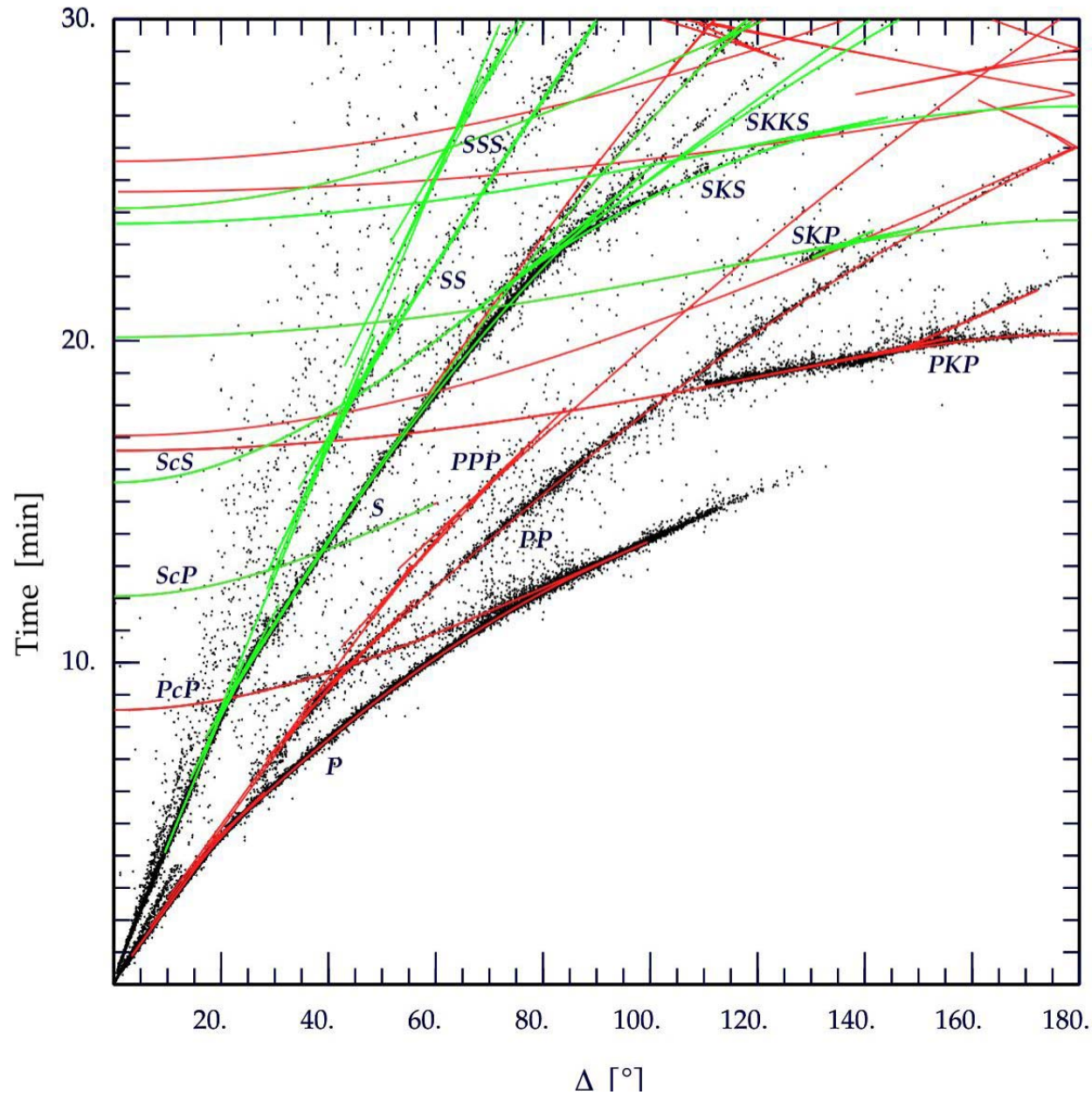
- λ seismic wavelength
- Λ scale heterogeneity
- Particle: Ray theory (XXth century)
 $\lambda \ll \Lambda$
- Wave: Normal mode theory (>1970)
(Finite frequency effects)

RAY PATHS INSIDE THE EARTH



Bolt, 1993

“Travel time” of certain seismic phases vs. epicentral distance

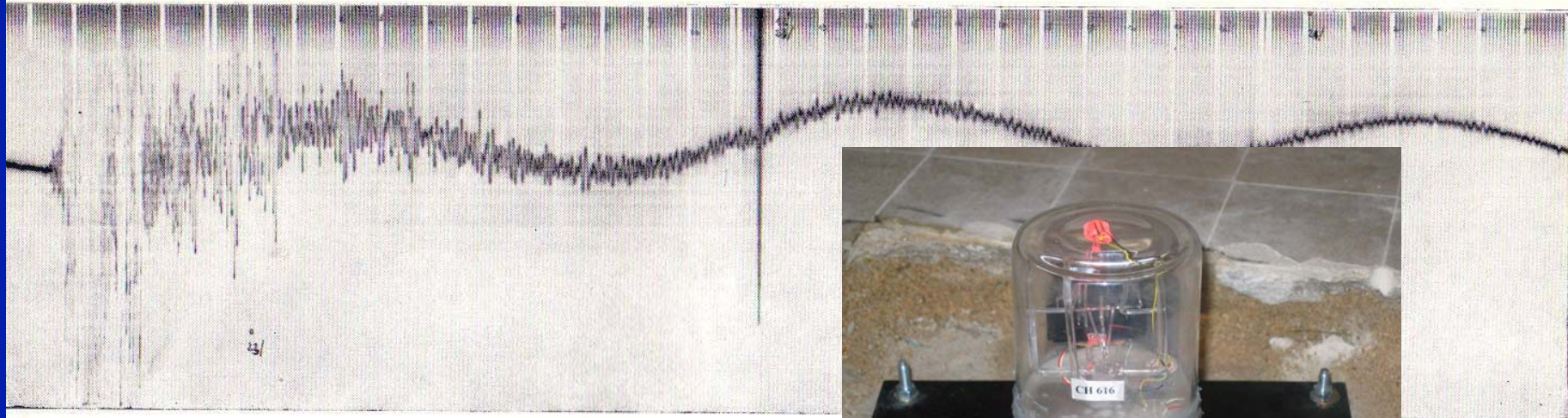


Duality wave - particle:

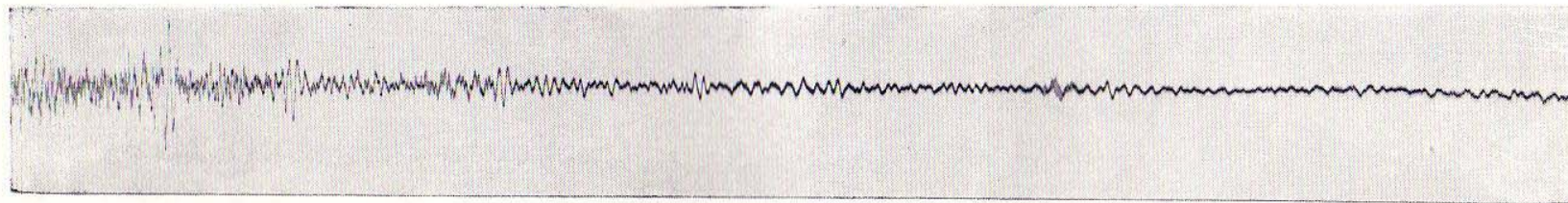
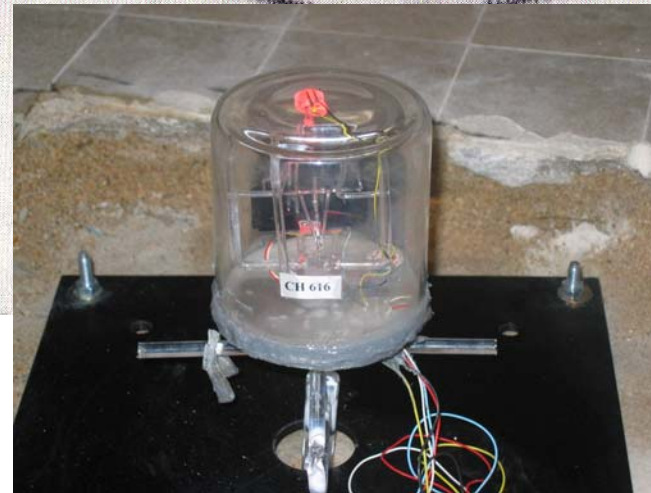
- λ seismic wavelength
- Λ scale heterogeneity

- Particle: Ray theory (XXth century)
 $\lambda \ll \Lambda$
- Wave: Normal mode theory (>1970)
(Finite frequency effects) $\lambda \gg \Lambda$

Normal modes Chile Earthquake (22 may 1960) recorded at Paris (IPGP)



1a



1b

FIG. 1. — a) Enregistrement du pendule E, n° 1 (voir tableau I).
b) Enregistrement du pendule B, n° 4 (voir tableau I). (Un intervalle de 5 minutes est représenté sur cette figure par 1,45 mm.)

Chile earthquake (may 22 1960) recorded at Paris (IPGP)

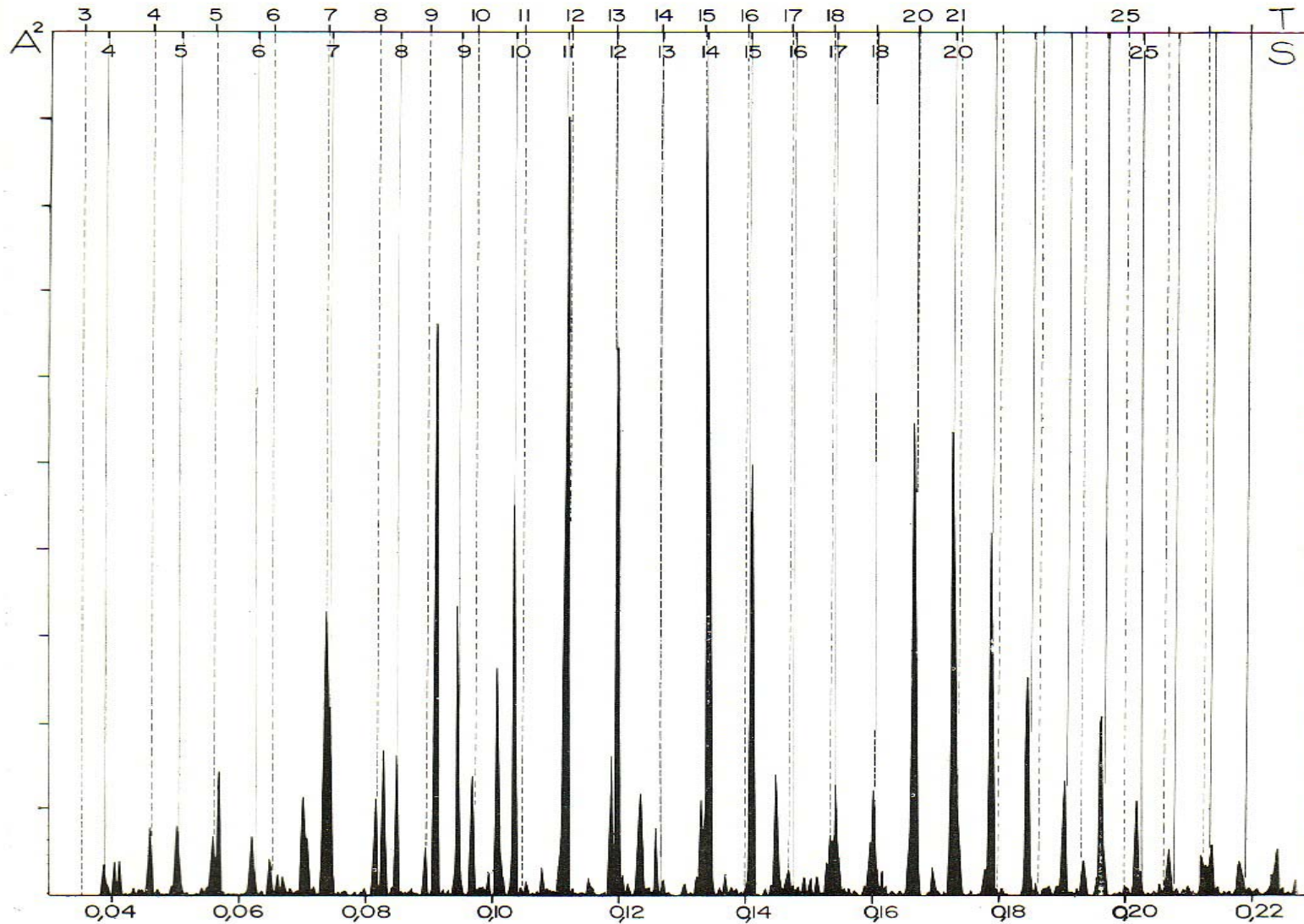


FIG. 3. — Spectre de l'enregistrement du pendule E (n° 1) — En haut : positions des pics théoriques pour les oscillations sphéroïdales S et les oscillations de torsion T du modèle de Gutenberg continental.

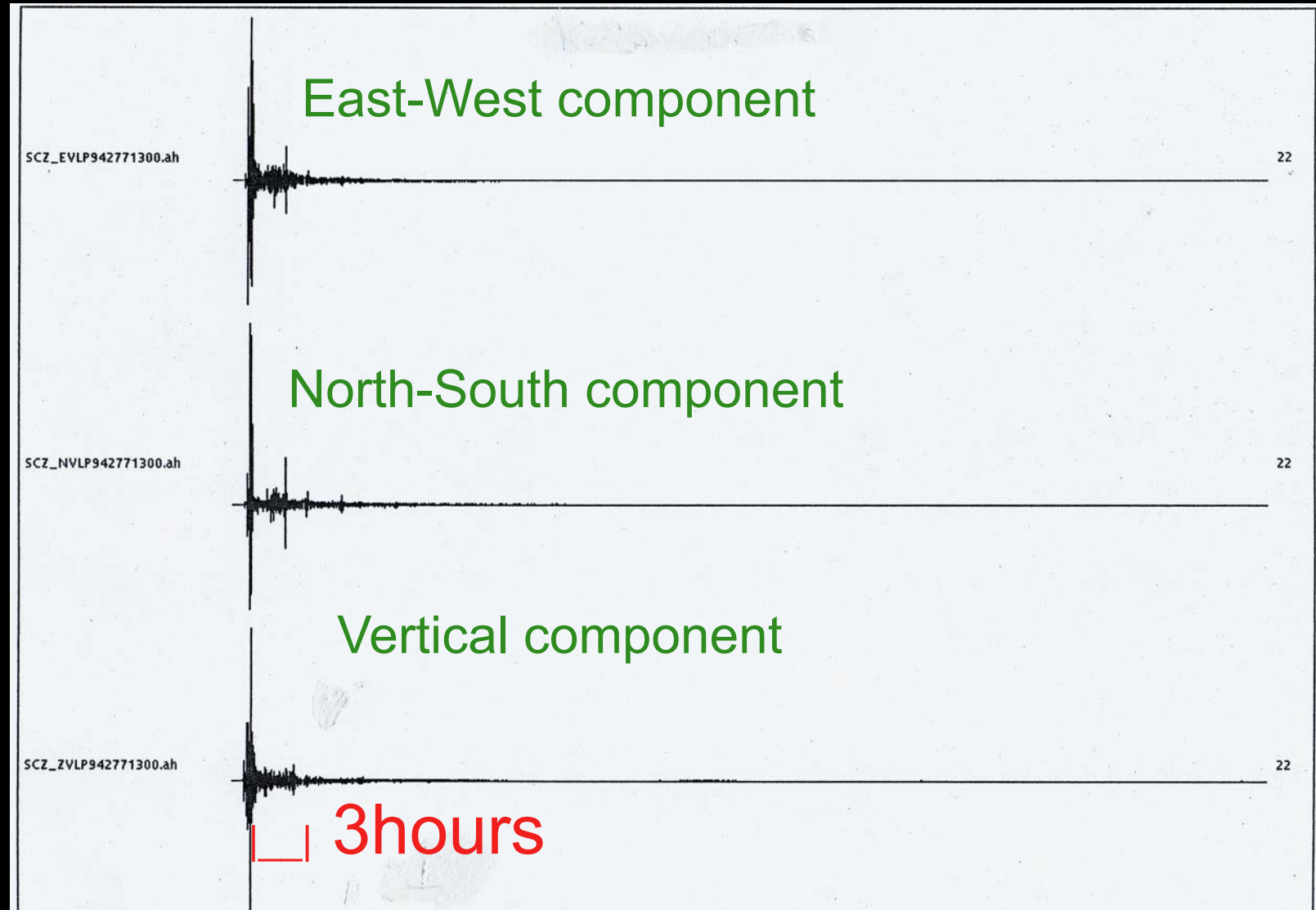
First observations of free oscillations of the Earth

1953? -> 1960 (Chile earthquake)

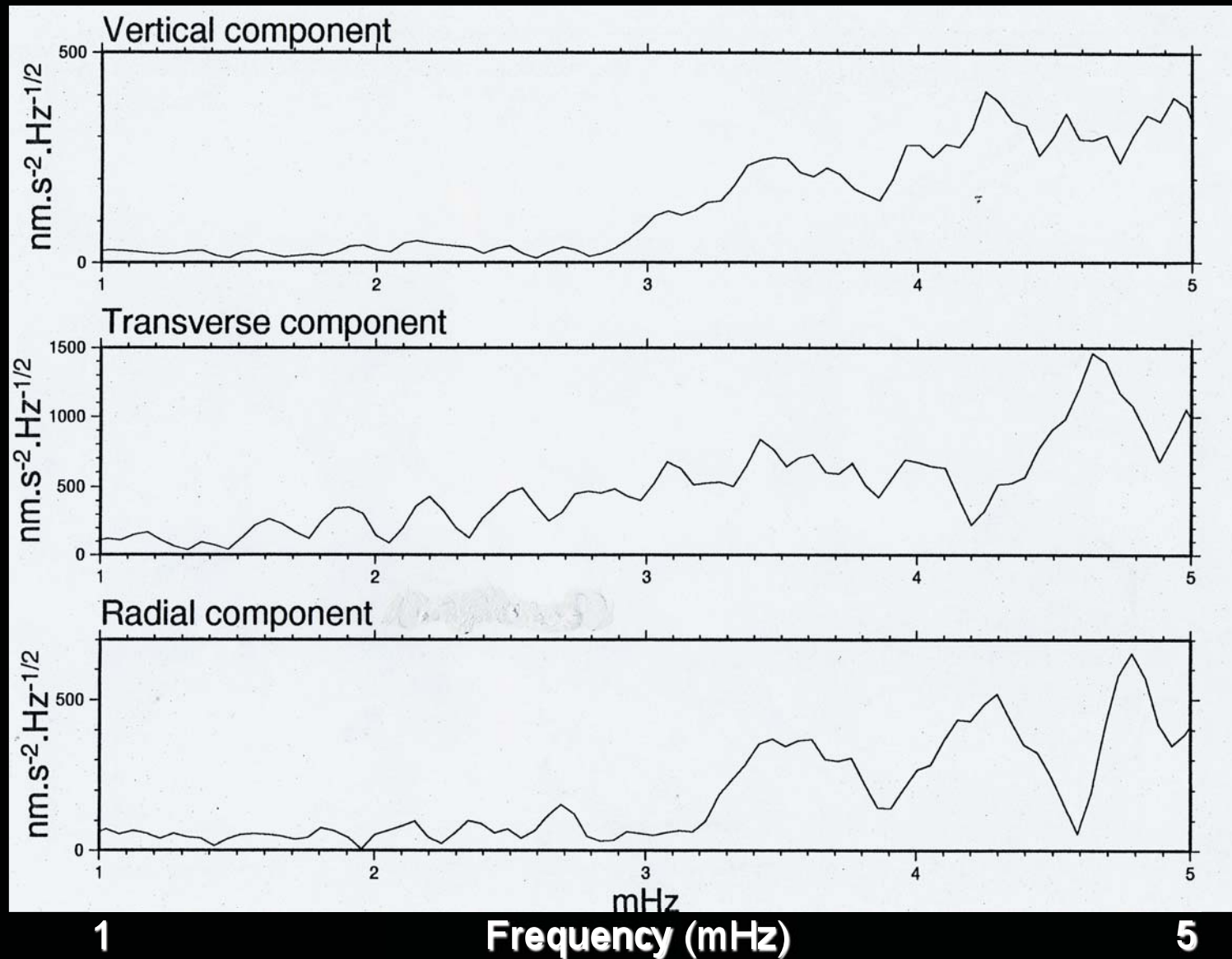
Frequency Peaks were not well understood

Theory was incomplete

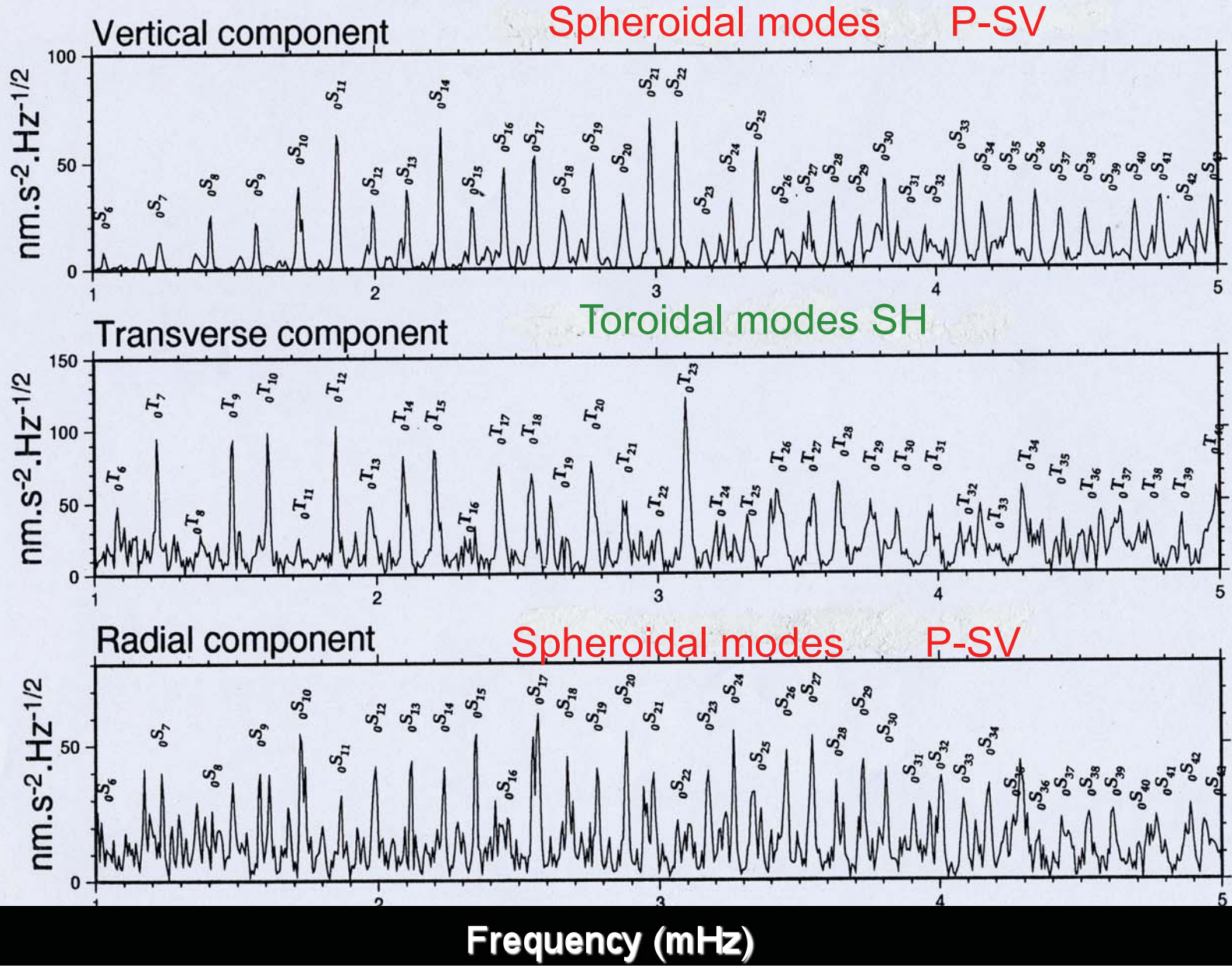
Kuril islands 1994-277 Ms=8.3



Kuril islands 1994-277 SCZ-VLP Spectra 3 hours



KURIL 94 277 - SCZ VLP - 36h.



Elastodynamic equation

$$\rho \partial_{tt} \mathbf{u}_{0i} = \partial_j \sigma_{ij} + \rho \mathbf{g}_i + \mathbf{F}_i (+ \mathbf{F} \mathbf{s}_i + \dots)$$

Which can be rewritten:

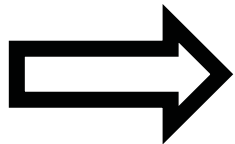
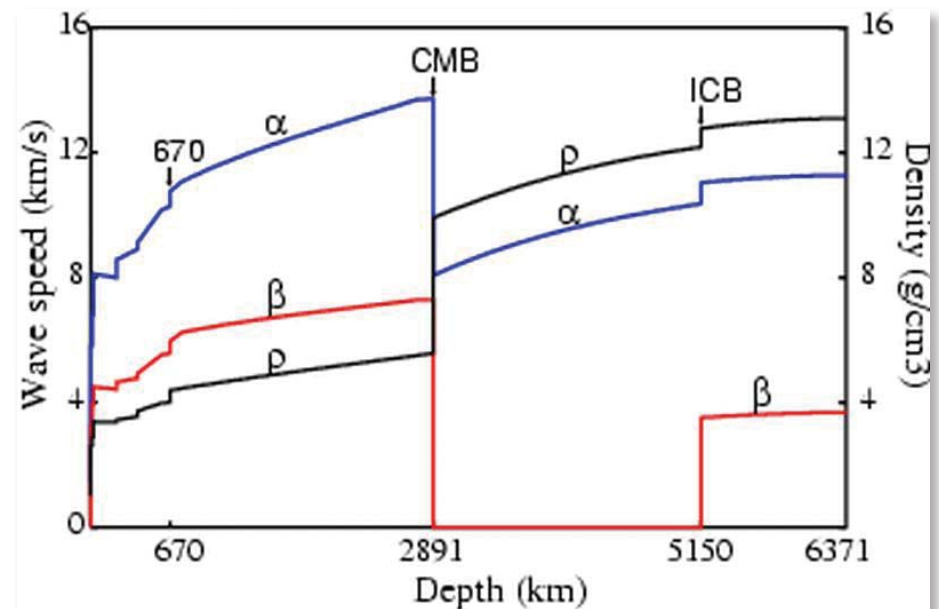
$$\rho \partial_{tt} \mathbf{u}_0 = \mathbf{H}_0 \mathbf{u}_0 (+ \mathbf{F} \mathbf{s})$$

\mathbf{H}_0 is an integro-differential operator

1D-Reference Earth Model:

$$M_0(r), \rho(r), V_P(r), V_S(r)$$

(PREM, Dziewonski and Anderson, 1981
or IASP91, Kennett and Engdahl, 1991)



John Woodhouse lecture

$$\rho \partial_{tt} \mathbf{u}_0 = \mathbf{H}_0 \mathbf{u}_0 \quad (+ \mathbf{F}s)$$

Eigenfrequencies: ${}_n \omega_l$

Eigenfunctions: ${}_n \mathbf{u}_l^m(\mathbf{r}, t) = |n, l, m\rangle \exp(-i {}_n \omega_l t)$

3 quantum numbers ($k = \{n, l, m\}$) $\Rightarrow \mathbf{u}_k(\mathbf{r}) \exp(-i {}_n \omega_l t)$

$$\int \rho \mathbf{u}_k^* \cdot \mathbf{u}_k \, d^3x = \delta_{ij}$$

$$\mathbf{H}_0 \mathbf{u}_k = \rho {}_n \omega_l^2 \mathbf{u}_k$$

Displacement:

$$\mathbf{u}(\mathbf{r}, t) = \sum_{n, l, m} {}_n \mathbf{a}_l^m |n, l, m\rangle \exp(-i {}_n \omega_l t)$$

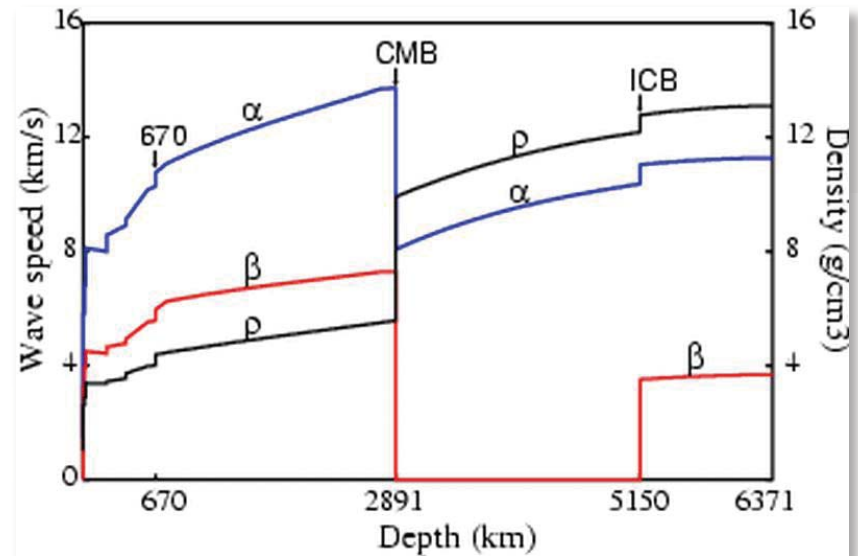
$$\begin{aligned} \mathbf{u}_k(\mathbf{r}) = & \{U(r) \mathbf{e}_r + V(r) \mathbf{e}_\theta \partial_\theta + V(r)/\sin\theta \mathbf{e}_\phi \partial_\phi\} Y_l^m(\theta, \phi) \\ & + \{W(r)/\sin\theta \mathbf{e}_\theta \partial_\phi - W(r) \mathbf{e}_\phi \partial_\theta\} Y_l^m(\theta, \phi) \end{aligned}$$

1D-Reference Earth Model:

$$M_0(r), \rho(r), V_P(r), V_S(r)$$

(PREM, Dziewonski and Anderson, 1981)

$$\rho \partial_{tt} \mathbf{u}_0 + \mathbf{H}_0 \mathbf{u}_0 = \mathbf{0}$$



Eigenfrequencies: ${}_n \omega_l$

Eigenfunctions: ${}_n u_l^m(r,t) = |n,l,m\rangle \exp(-i {}_n \omega_l t)$

2 kinds of modes: Toroidal ${}_n T_l$, Spheroidal ${}_n S_l$

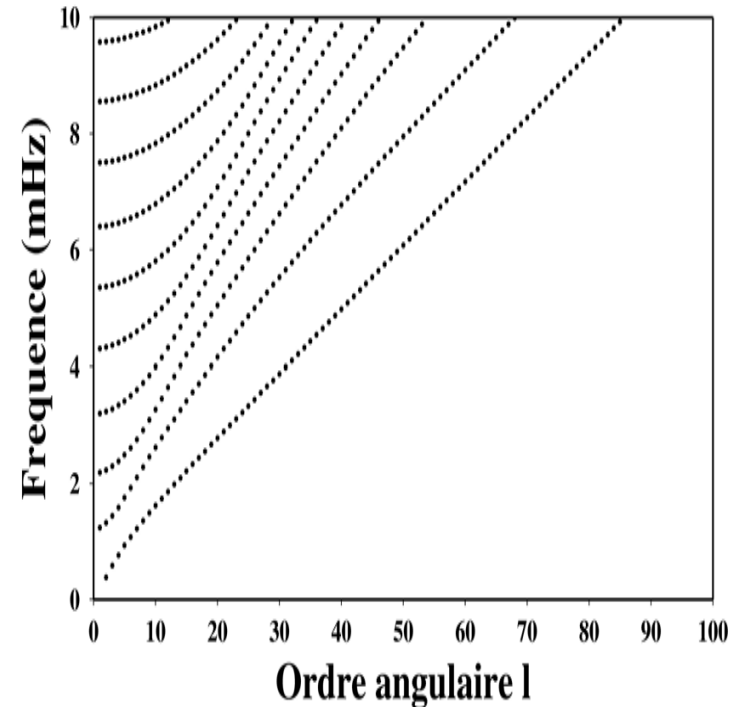
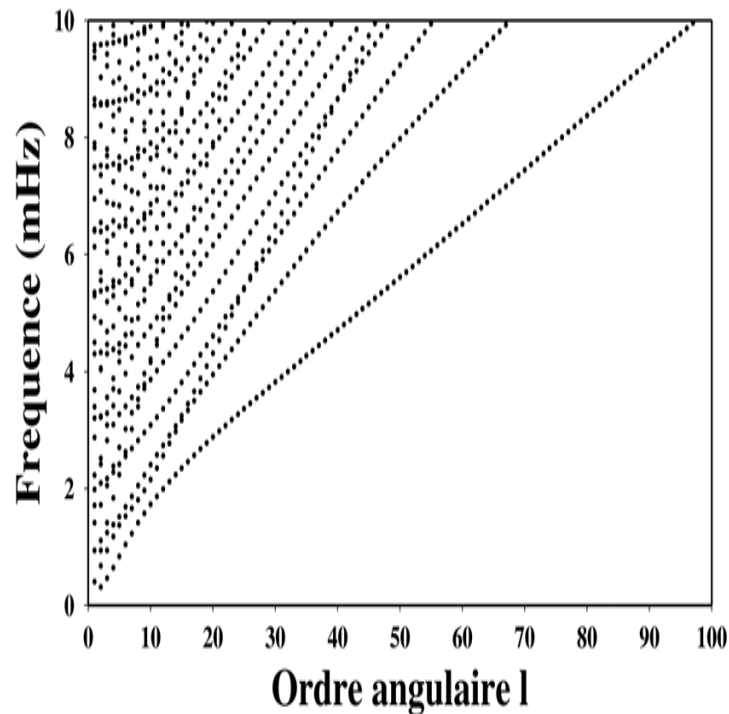
Degeneracy of eigenfrequencies ${}_n \omega_l : 2l + 1$

Spherical eigenfrequencies

Spheroidal Modes ${}_nS_l$
(P-SV / Rayleigh)

Toroidal modes ${}_nT_l$
(SH / Love)

Dispersion Branches



multiplet : $(n,l) = 2l+1$ singlets
singlet : (n,l,m)

n : radial order
 l : angular order
 m : azimuthal order

Spheroidal Modes

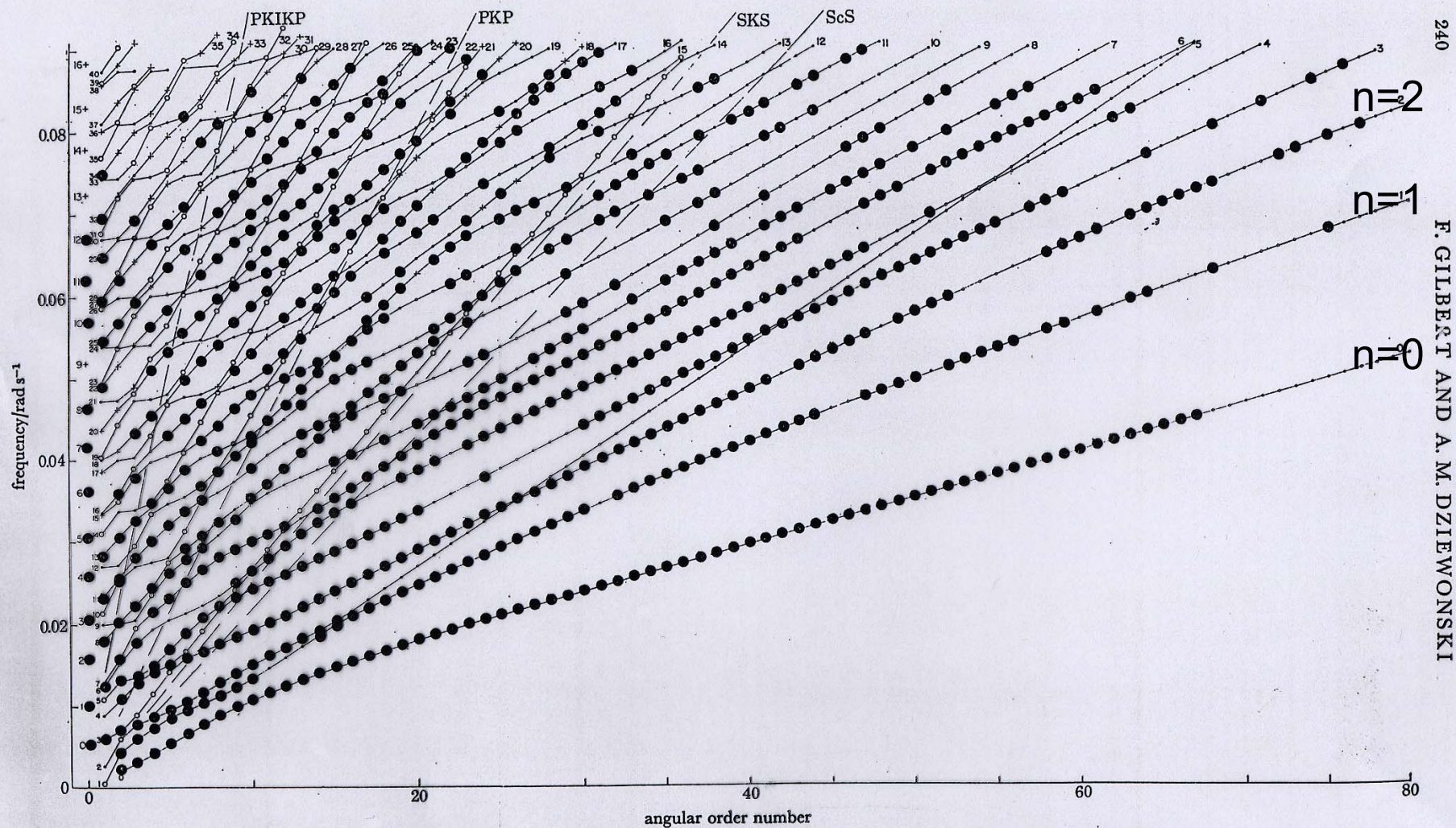
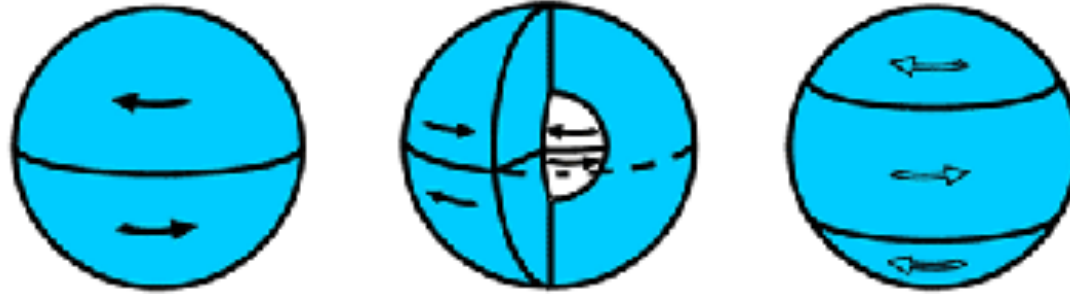


FIGURE 17. Spheroidal normal modes in the (ω, l) plane. The large dots indicate observed modes used in the inversions. For further details we refer the reader to §3 of Alaska II. •, $CE < 0.5$; +, $CE \geq 0.5$; o core modes.

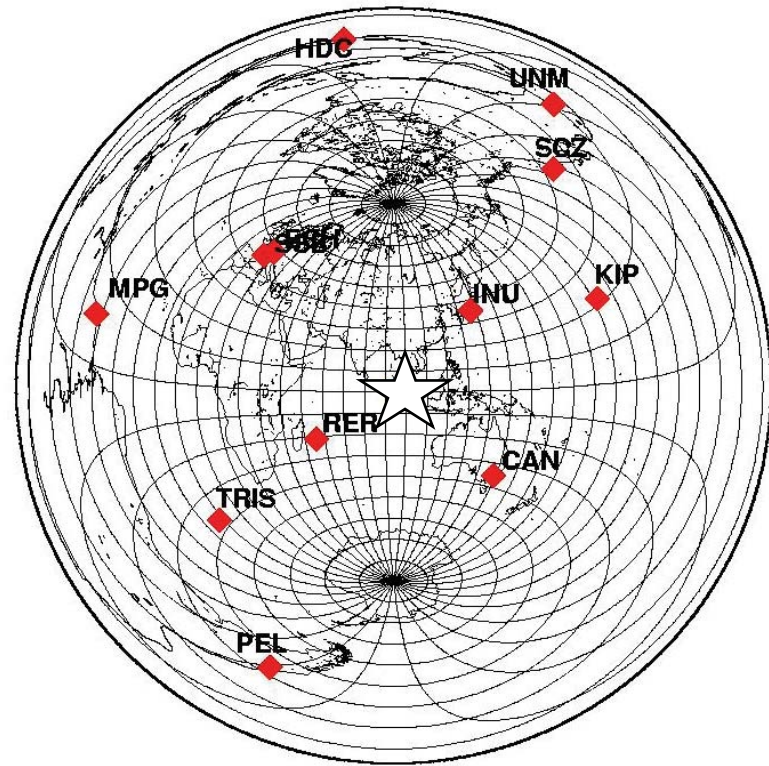
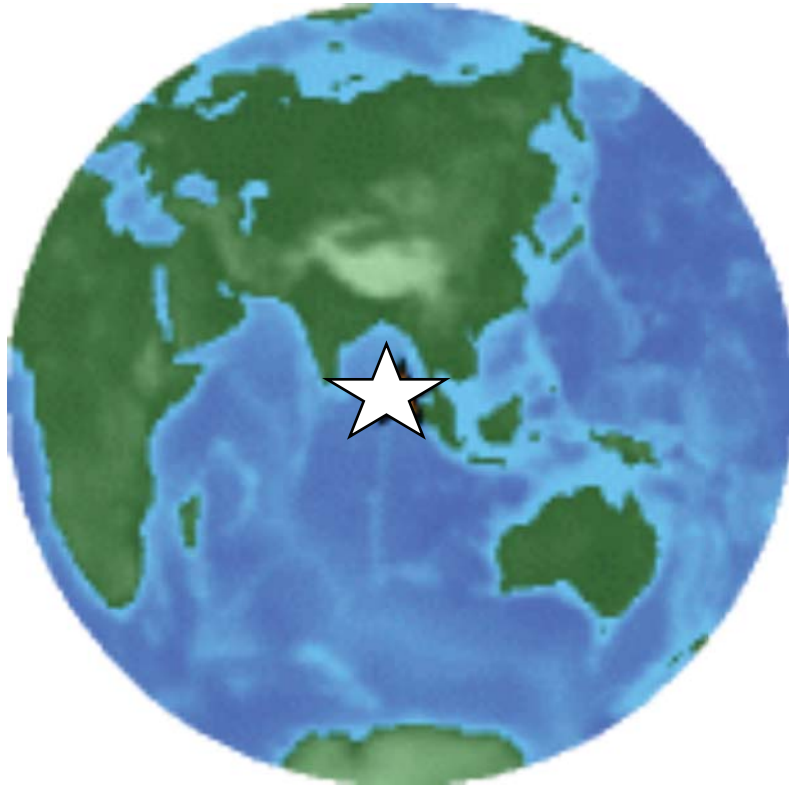


Toroidal modes ${}_0T_2$ (44.2 min), ${}_1T_2$ (12.6 min)
and ${}_0T_3$ (28.4 min)



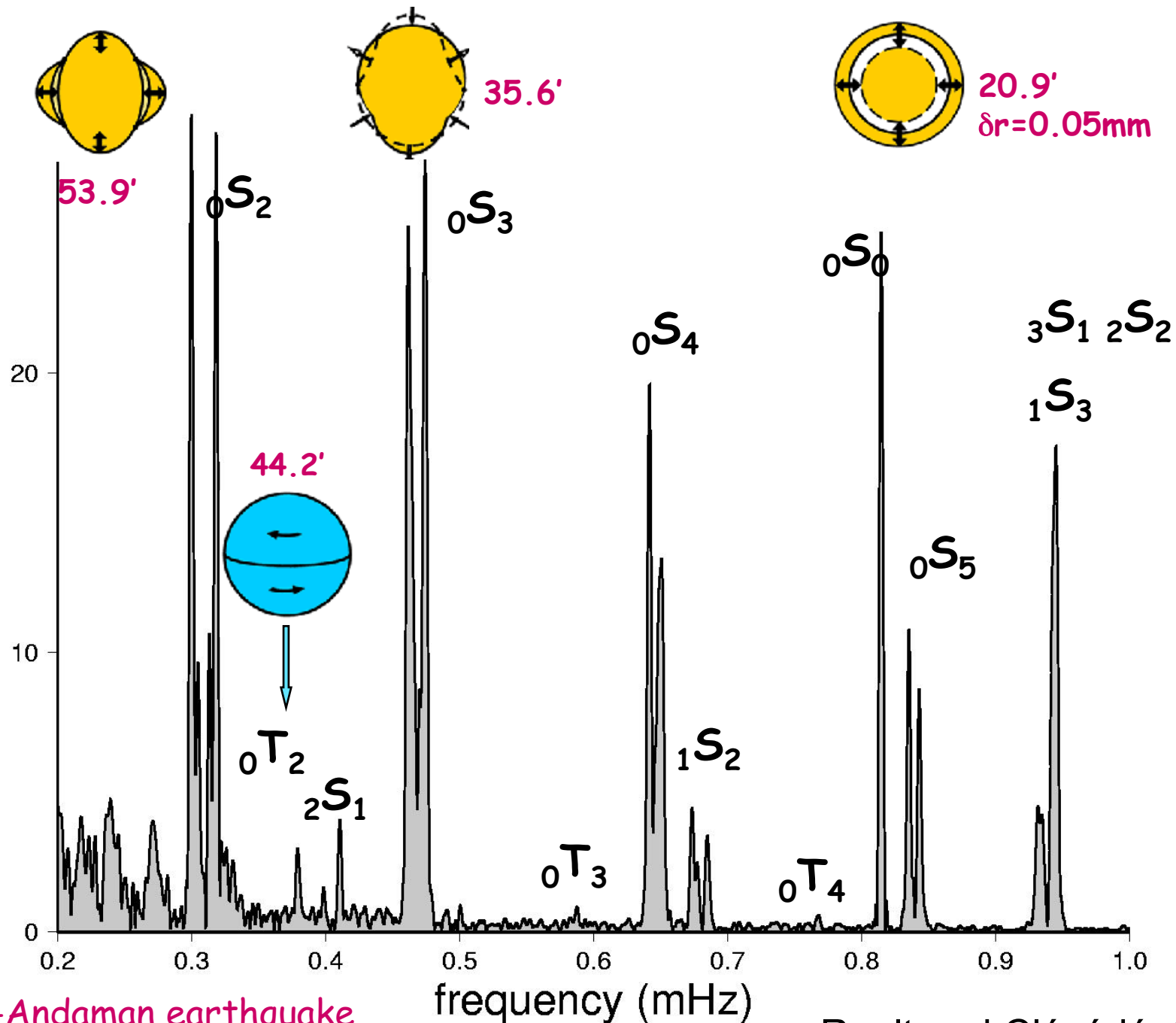
Spheroidal modes ${}_0S_0$ (20.5 min), ${}_0S_2$ (53.9 min)
and ${}_0S_3$ (35.6 min)

Study of Sumatra earthquake (26 december 2004) With GEOSCOPE stations



(Roult and Clévéde, 2005 ; Park et al., Science, 2005)

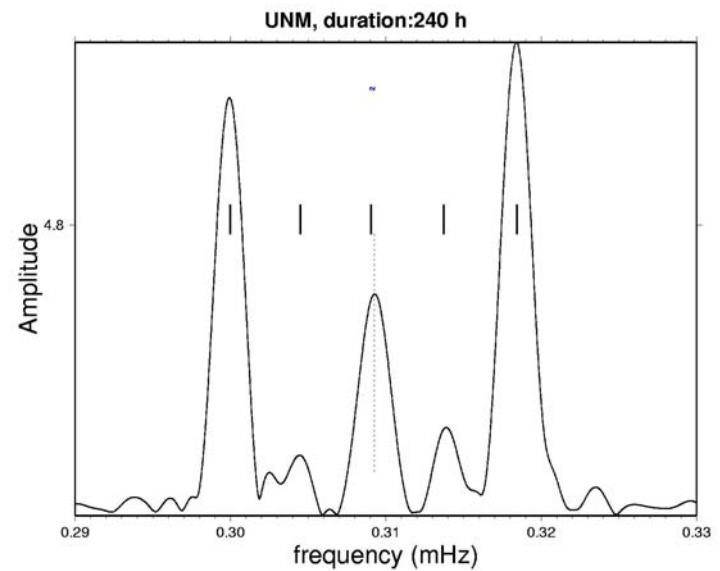
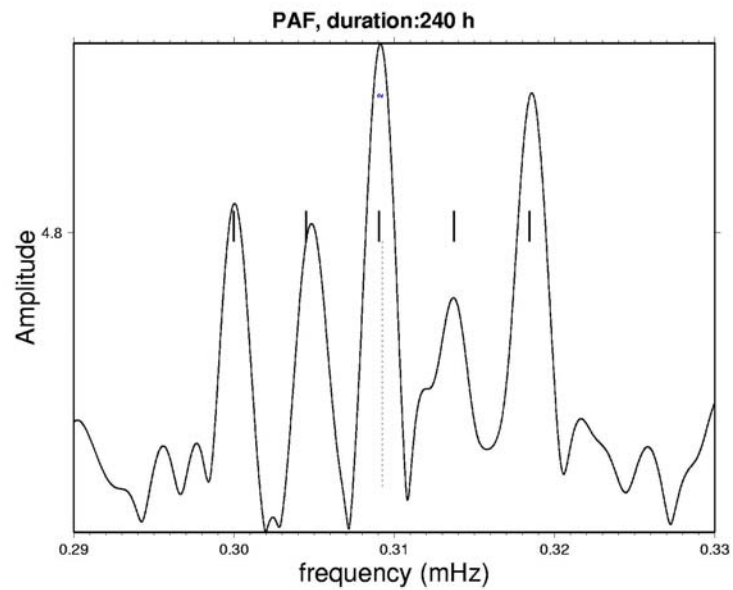
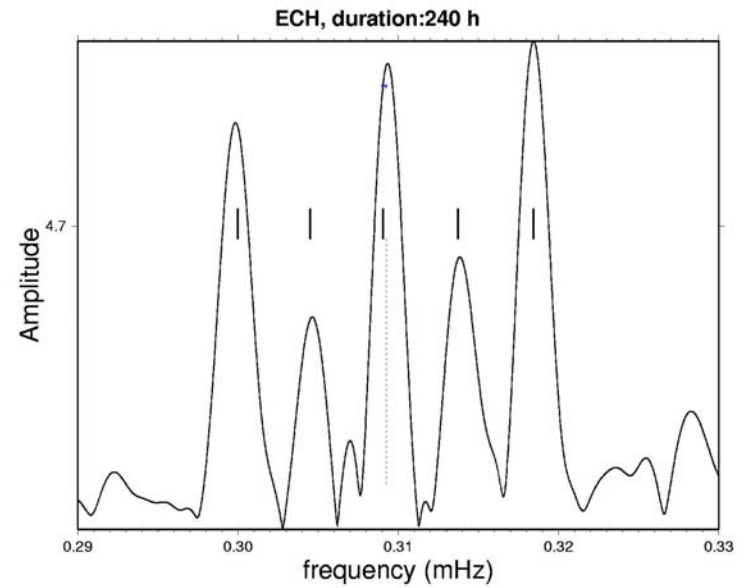
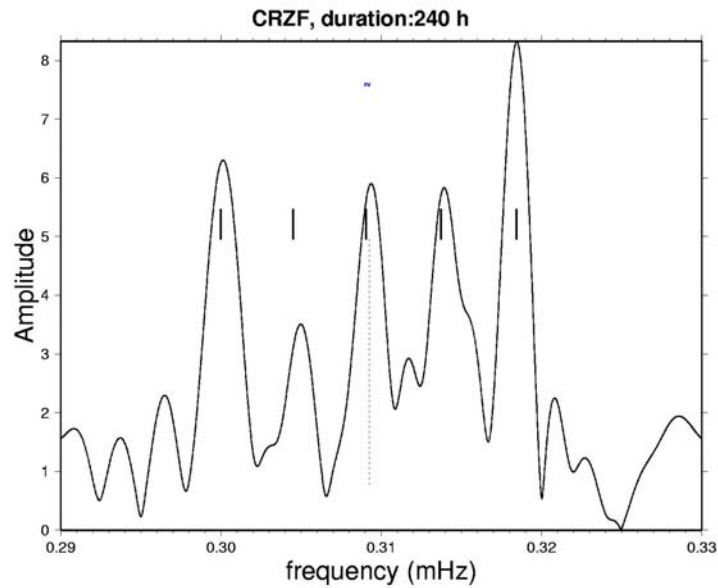
STS1
CAN



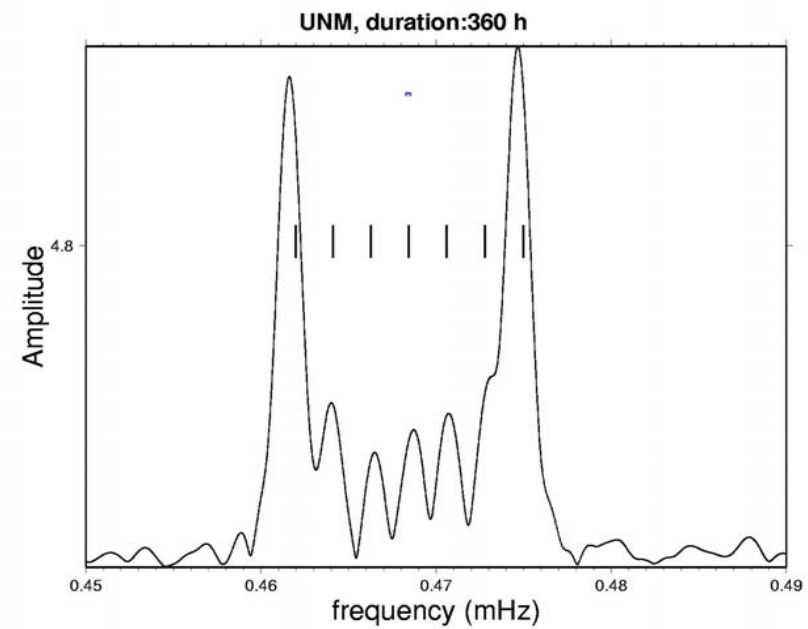
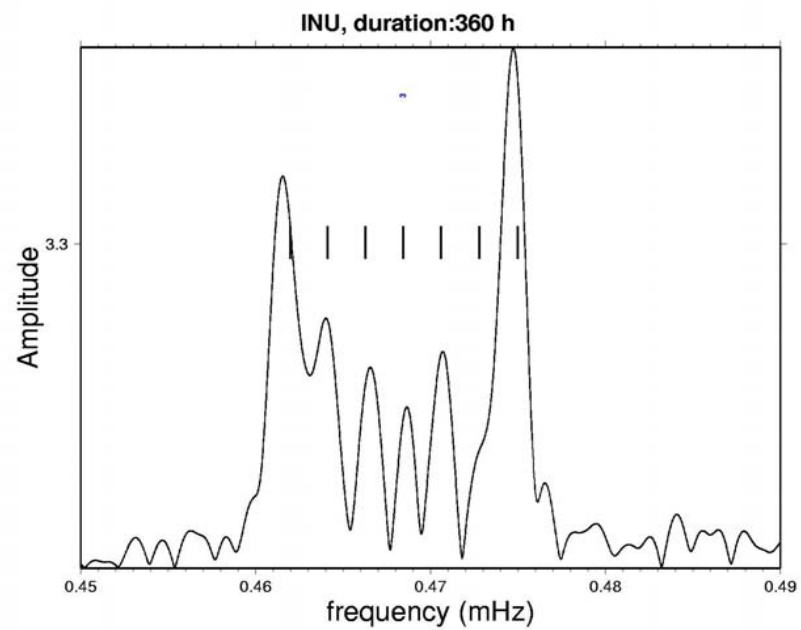
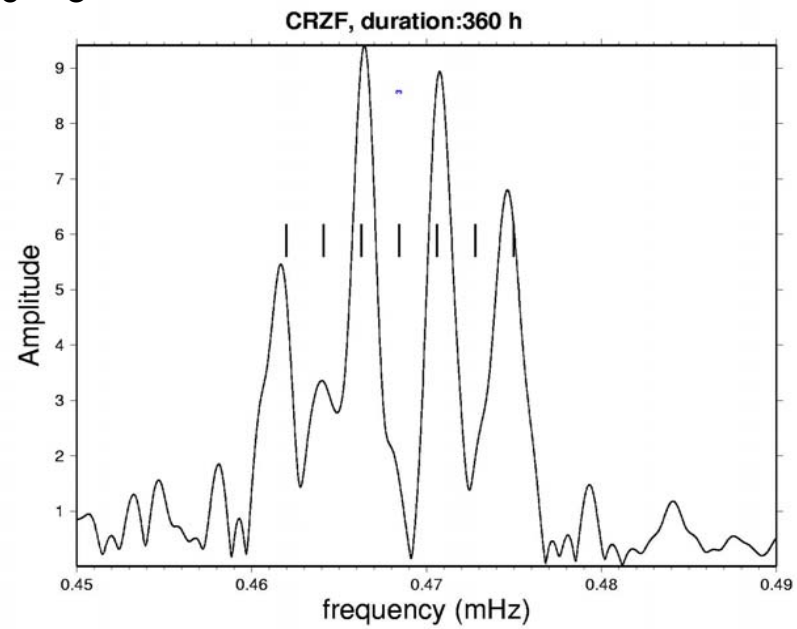
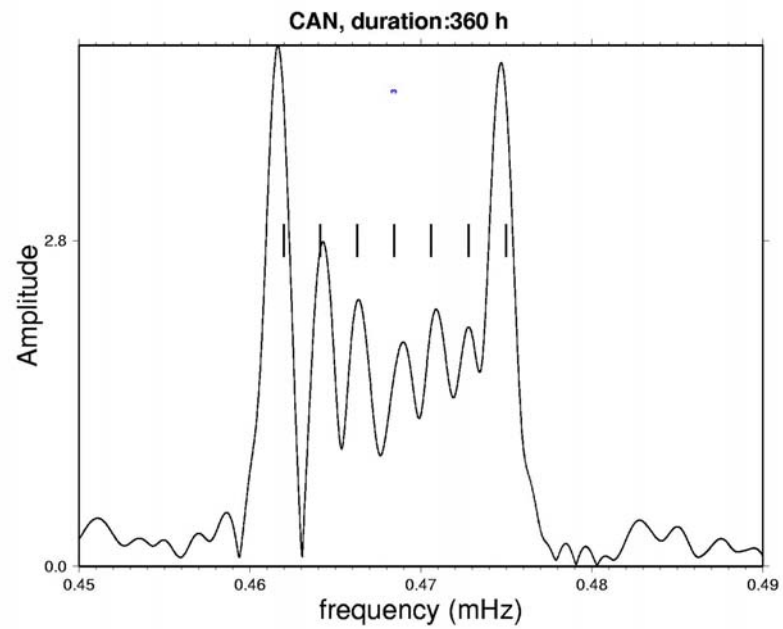
Sumatra-Andaman earthquake
26 December 2004

Roult and Clévédé, 2005

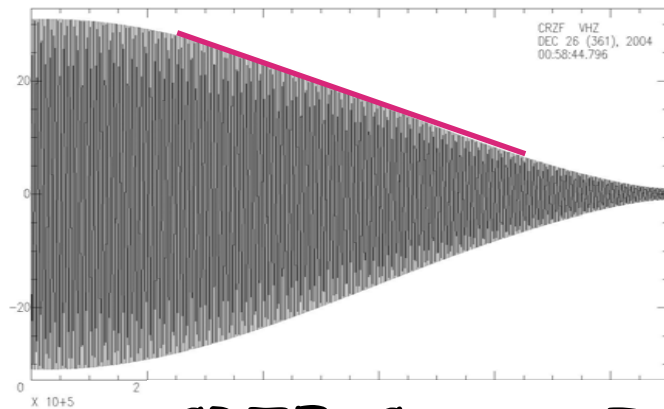
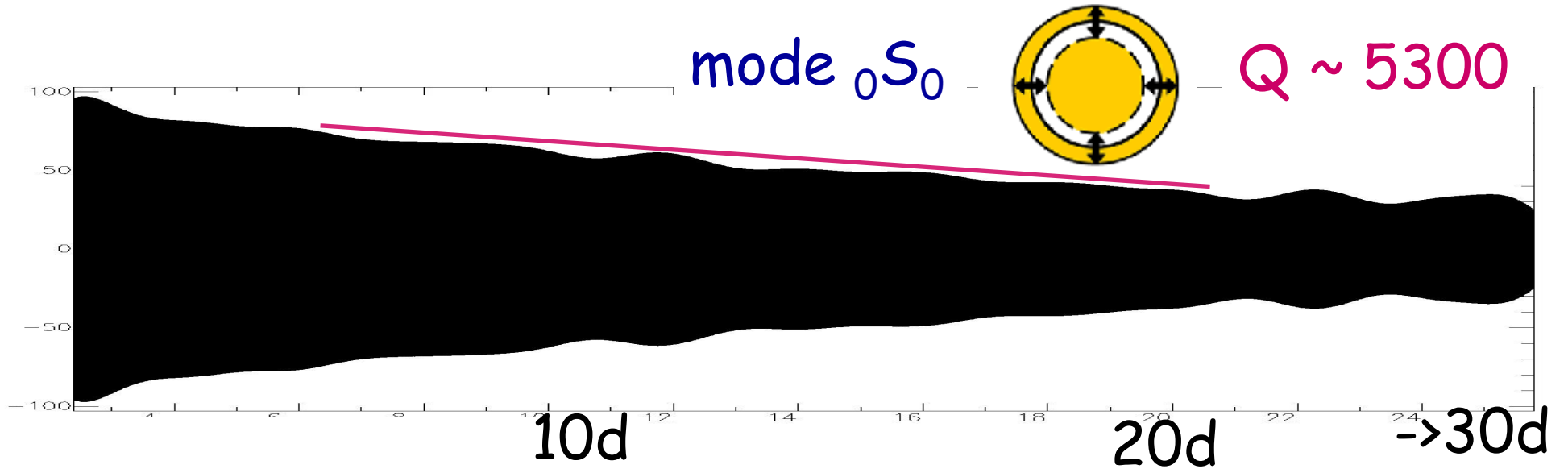
mode ${}_0S_2 \Rightarrow$ splitting 5 singlets



mode ${}_0S_3$



Attenuation of some modes



mode ${}_0S_2$
singlet $m=+2$



$Q \sim 500$

CRZF, Crozet, Indian Ocean

Seismic Source

$$\rho \partial_{tt} \mathbf{u} + \mathbf{H}_0 \mathbf{u} = \mathbf{F}_s$$

Displacement at point \mathbf{r} and time t due to a force system \mathbf{F}_s at point source \mathbf{r}_s

eigenfrequencies: ${}_n \omega_l$

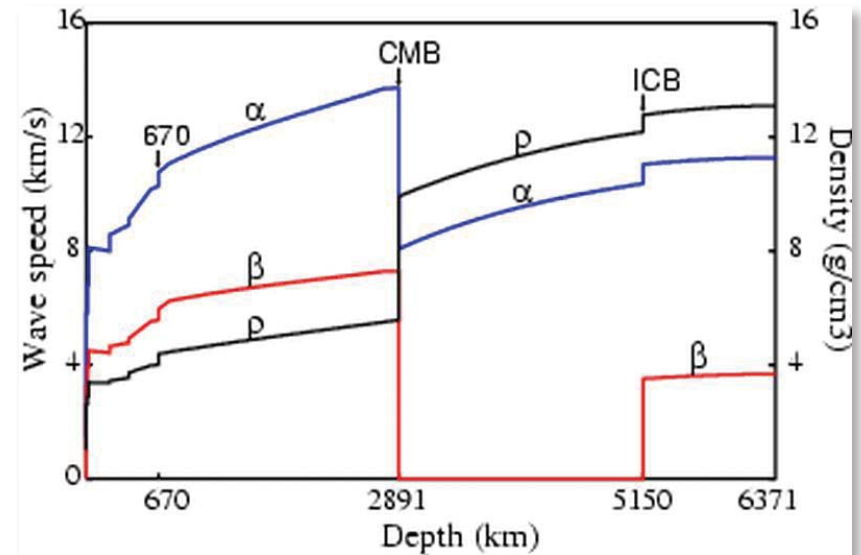
eigenfunctions: ${}_n u_l^m(\mathbf{r}, t) = |n, l, m\rangle \exp(-i {}_n \omega_l t)$

$$\mathbf{u}(\mathbf{r}, t) = \sum_{n, l, m} {}_n \mathbf{a}_l^m |n, l, m\rangle \exp(-i {}_n \omega_l t)$$

Eigenfunction basis is a complete basis \Rightarrow any wave can be modelled by normal mode summation including surface waves and body waves.

1D- Reference Earth Model

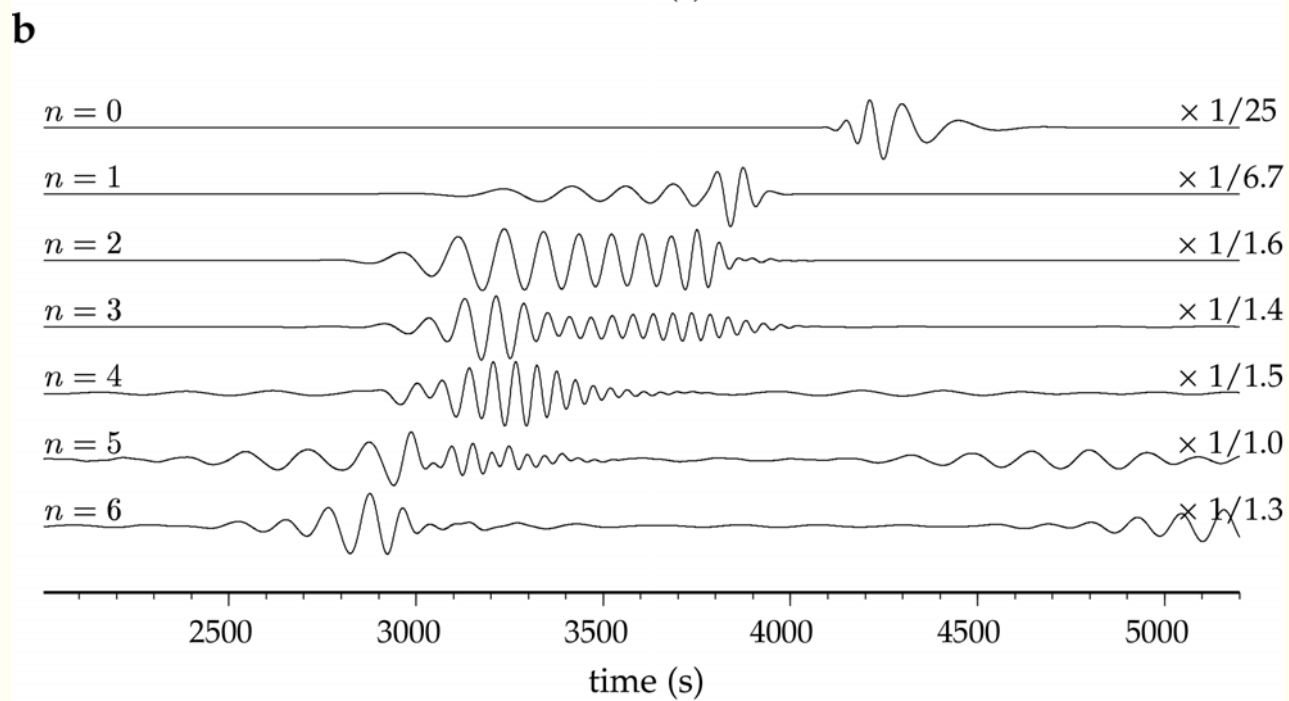
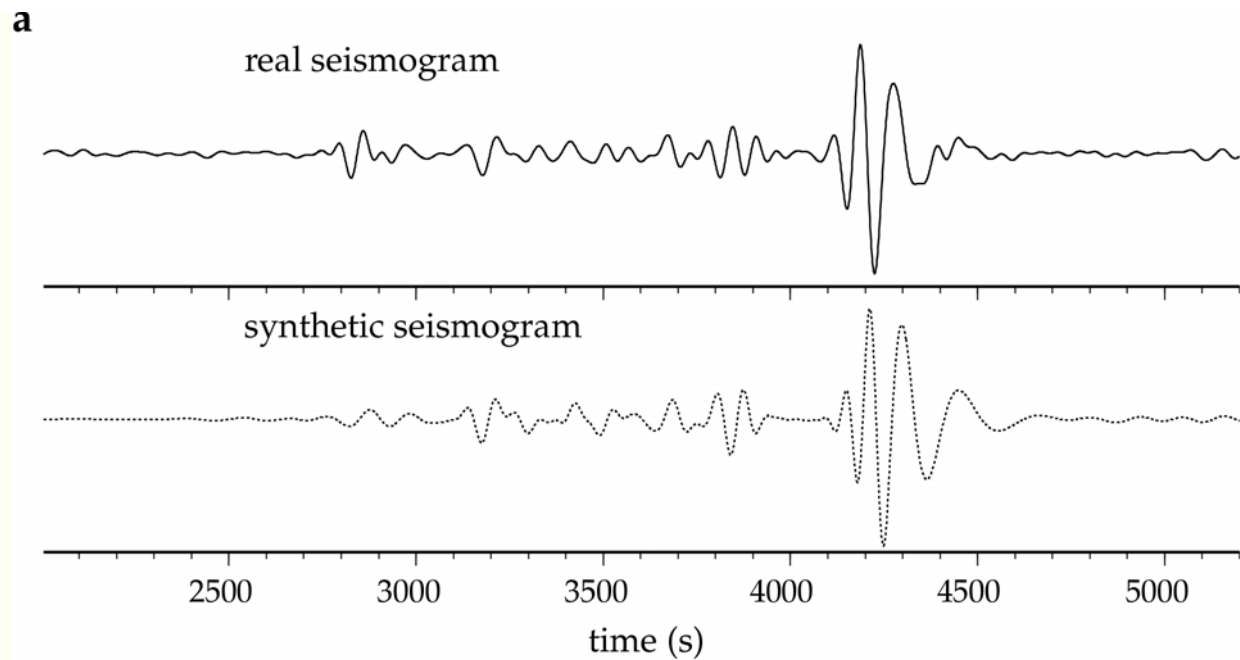
- Synthetic Seismograms by normal mode summation $\mathbf{u}_k(k=\{n,l,m\})$.



$$\mathbf{u}(\mathbf{r},t) = \sum_k \mathbf{u}_k(\mathbf{r}) \cos \omega_k t / \omega_k^2 \exp(-\omega_k t / 2Q_k) (\mathbf{u}_k \cdot \mathbf{F})_s$$

$$\text{Source Term } (\mathbf{u}_k \cdot \mathbf{F})_s = (\mathbf{M} : \boldsymbol{\varepsilon})_s$$

M Seismic moment tensor, $\boldsymbol{\varepsilon}$ deformation tensor



Beucler et al., 2003

Data

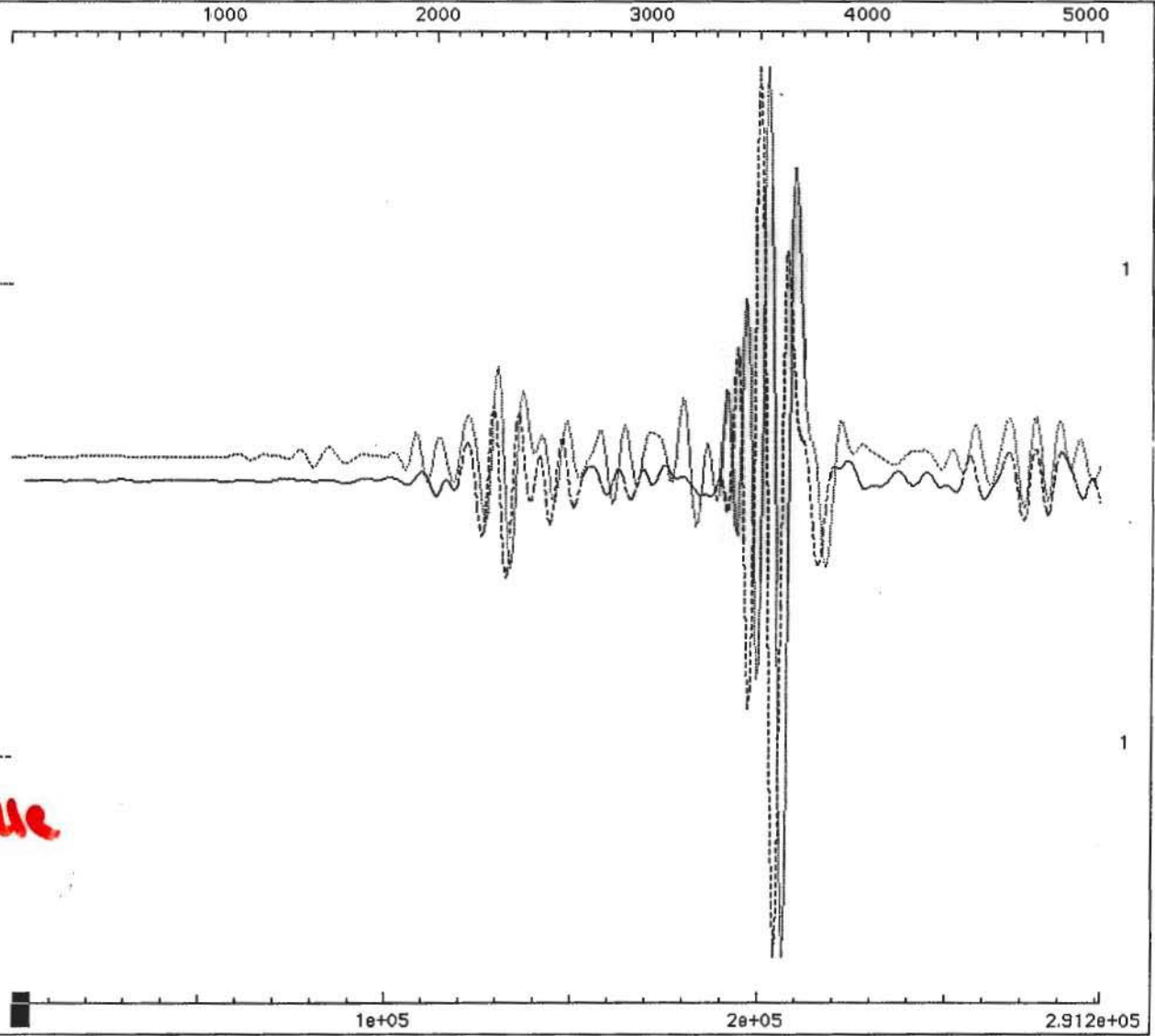
CAN_VHZ19952110511.ah

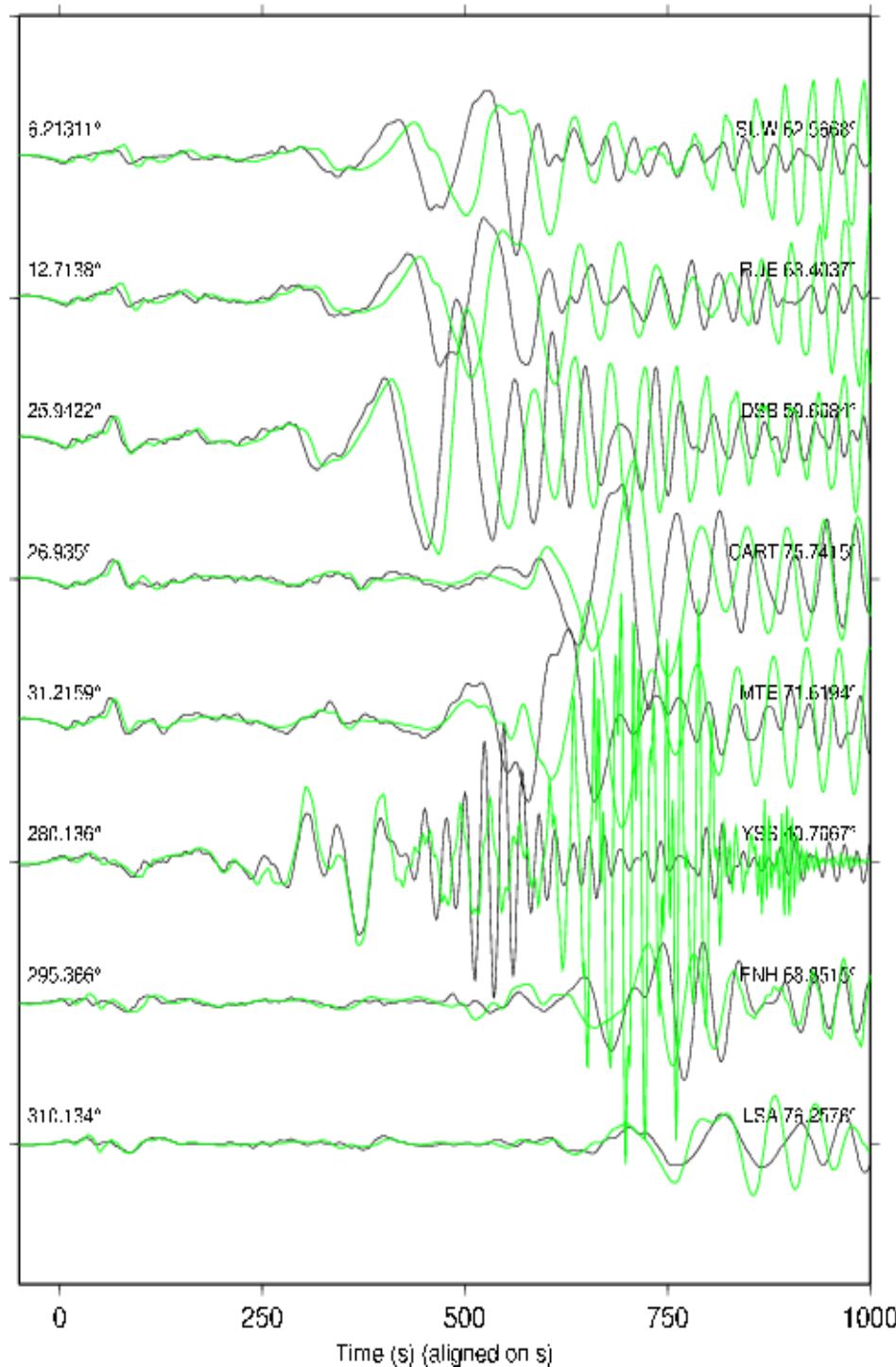
Donnée

Synthetics

HARMO/cansyn0-6.ah

Synthétique





Synthetic seismograms
By normal mode
summation

Denali-Alaska
earthquake (Nov. 2002)

Komatitsch and Tromp, 2003

Duality wave - particle:

λ seismic wavelength

Λ scale heterogeneity

Particle: **Ray** theory $\lambda \ll \Lambda$

(Finite frequency effects)

Wave: Normal **Mode** theory (NM) + Perturbation theories (small amplitude of 3D- heterogeneities) =>

John Woodhouse

Numerical modelling of wave equation

Strong or weak forms: $\lambda \approx \Lambda$

-Spectral Element Method (SEM)



(Dimitri Komatitsch)

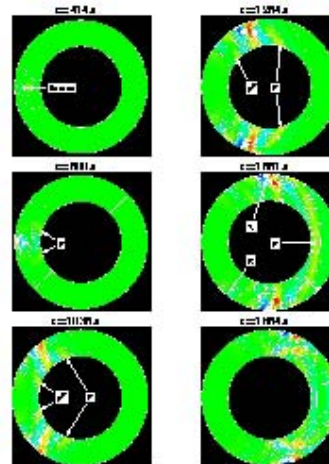
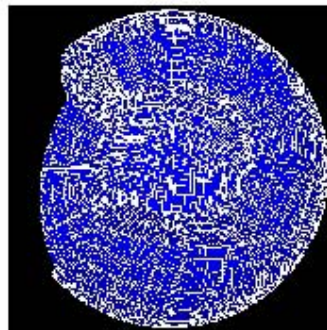
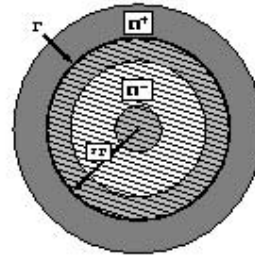
-Coupled SEM-NM method

Spectral Element Method: D. Komatitsch (1999)

Coupled method of Spectral Elements and Modal Solution

Principle:

- Ω^+ : Spectral Element area:
3D model
- Ω^- : Modal Solution area:
1D model



Capdeville et al., 2002

Overview

Large scale Seismology: an observational field

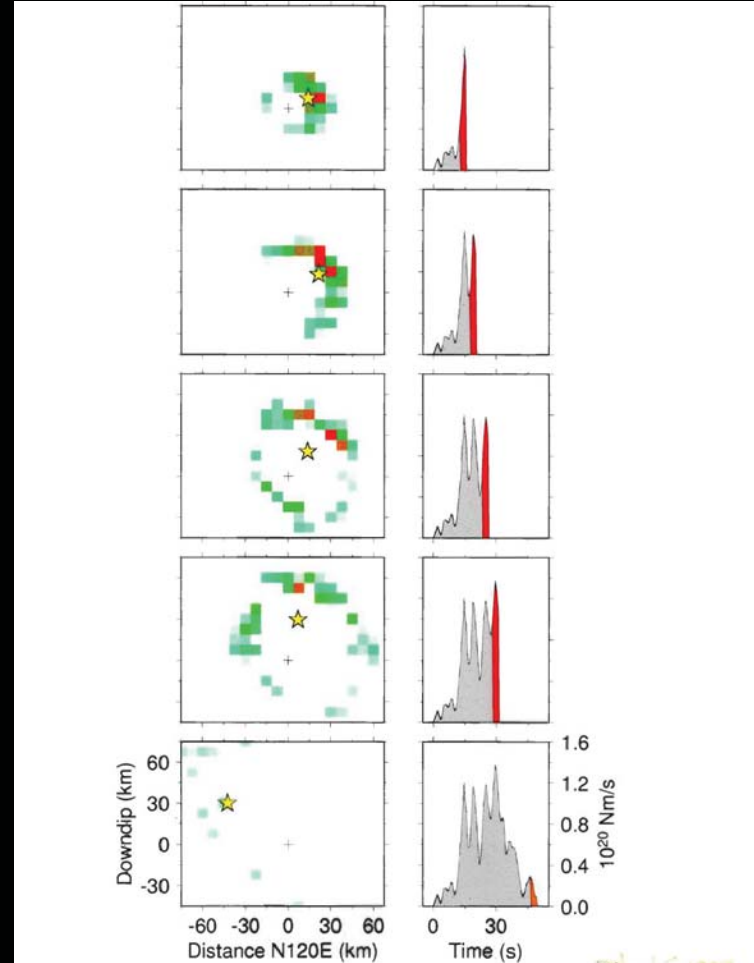
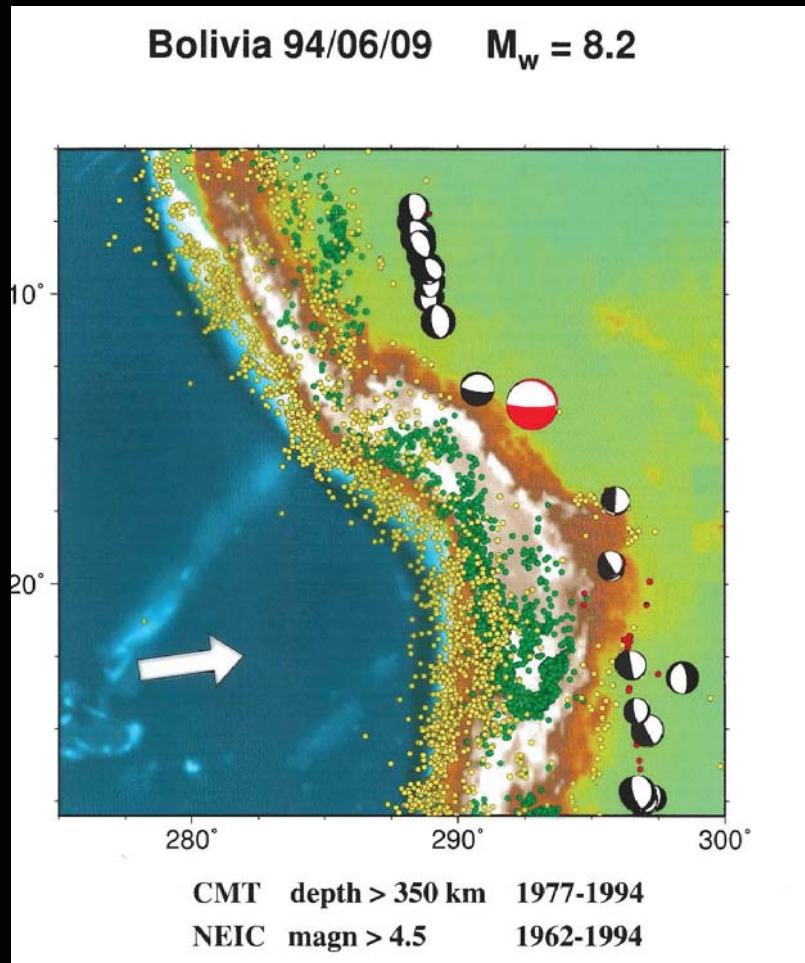
- Data (Seismic source) + Instrument (Seismometer)
-> Observations (seismograms)
- Historical evolution: Ray theory, Normal mode theory, Numerical techniques (SEM, NM-SEM)
- **Scientific Issues: Earthquakes (Sumatra), Anisotropic structure of the Earth**
- Tomographic Technique
- Geodynamic Applications.
Seismic Experiment Plume detection
- NM-SEM and time reversal

Seismic Source Studies

$$\mathbf{u}(\mathbf{r}, t) = \sum_k \mathbf{u}_k(\mathbf{r}) \cos \omega_k t / \omega_k^2 \exp(-\omega_k t / 2Q) (\mathbf{u}_k \cdot \mathbf{F})_S$$

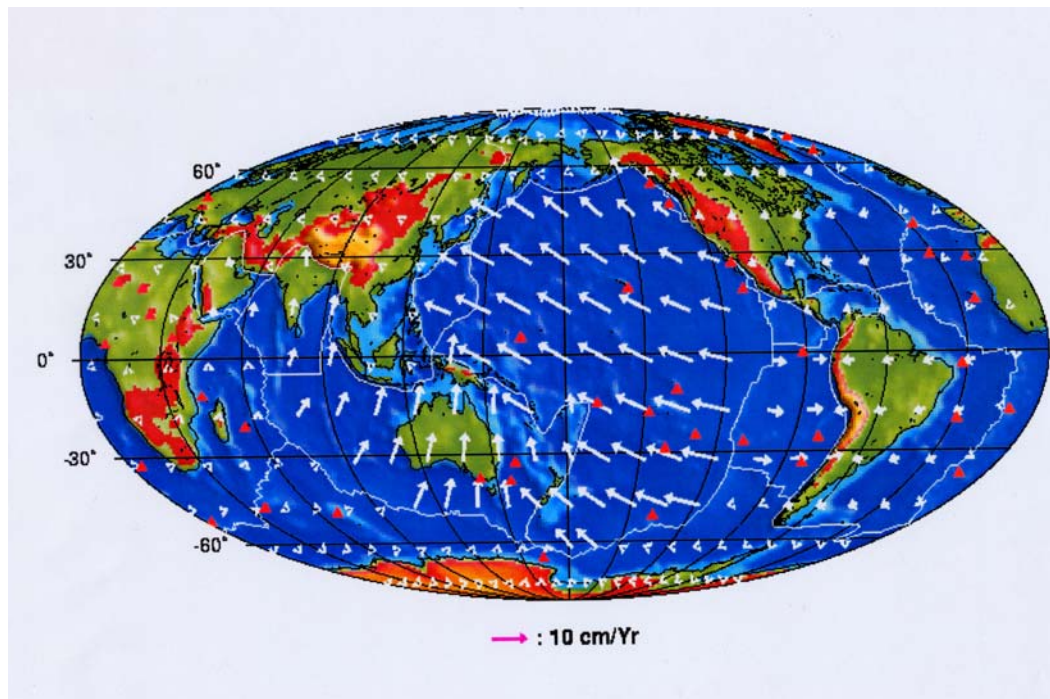
$$\text{Source Term } (\mathbf{u}_k \cdot \mathbf{F})_S = (\mathbf{M} : \boldsymbol{\varepsilon})_S$$

M Seismic moment tensor, $\boldsymbol{\varepsilon}$ deformation tensor

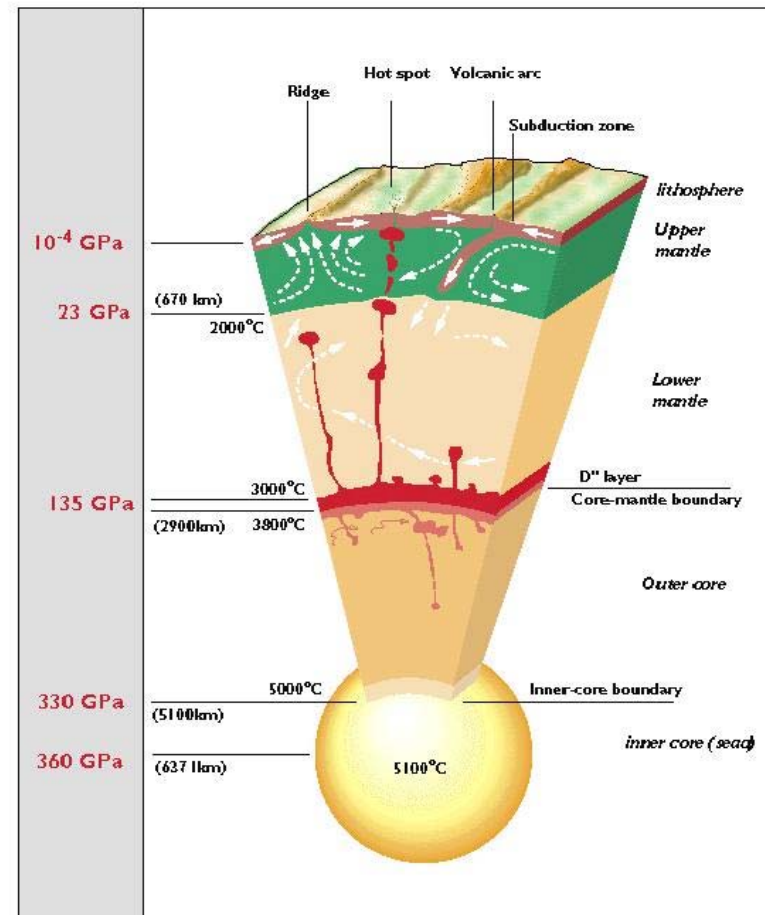


Structure of the Earth

Plate tectonics



Mantle Convection



Tomographic Technique

- **Forward Problem:** Theory $\mathbf{d}=\mathbf{g}(\mathbf{p})$

\mathbf{d} data space, \mathbf{p} parameter space

- Reference Earth model \mathbf{p}_0 :

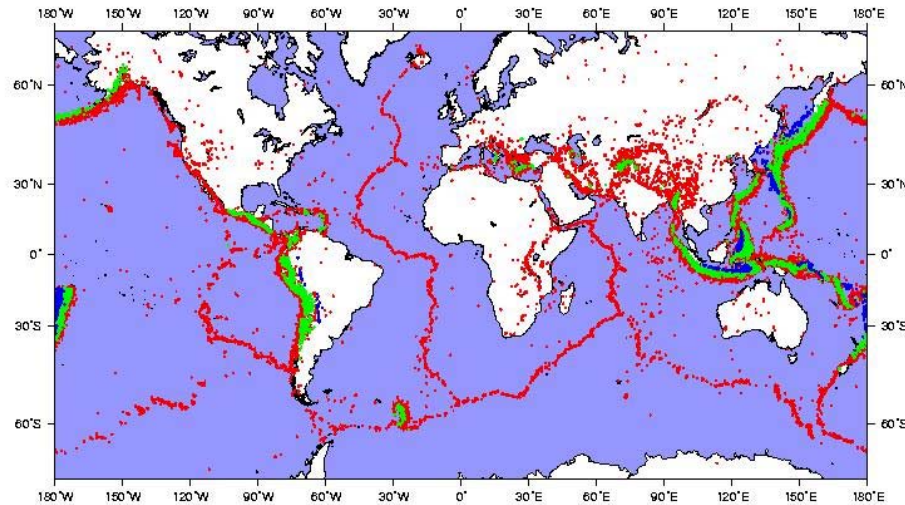
$$\mathbf{d}_0 = \mathbf{g}(\mathbf{p}_0)$$

- Kernels $\partial\mathbf{g}/\partial\mathbf{p}$
- Cd function (or matrix) of covariance of data

- **Inverse Problem:** $\mathbf{p}-\mathbf{p}_0 = \mathbf{g}^{-1}(\mathbf{d}-\mathbf{d}_0)$

- C_{p0} a priori Covariance function of parameters
- C_{pf} a posteriori Covariance function of parameters
- R Resolution

Global seismicity 1928-1999



Magnitude Mb or Ms ≥ 5.0

GEOSCOPE,
Fri July 7 08:26:53 MET 2000

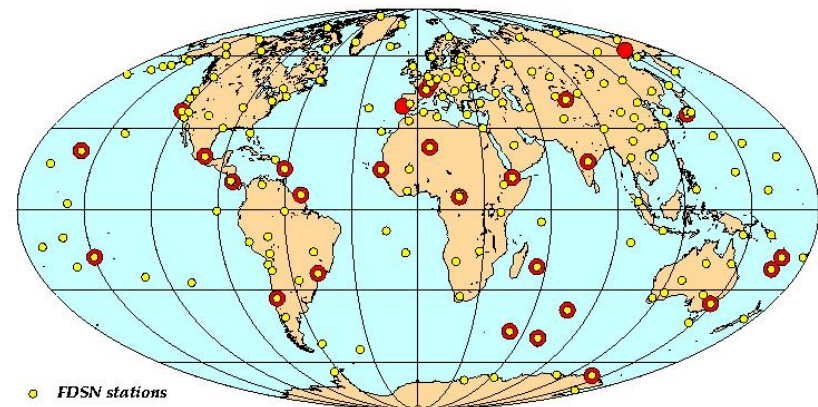
DATA

Receivers

Seismic sources:

- earthquakes
 - noise
- (1-20s microseismic)
(100-400s seismic Hum)

GEOSCOPE stations and FDSN stations

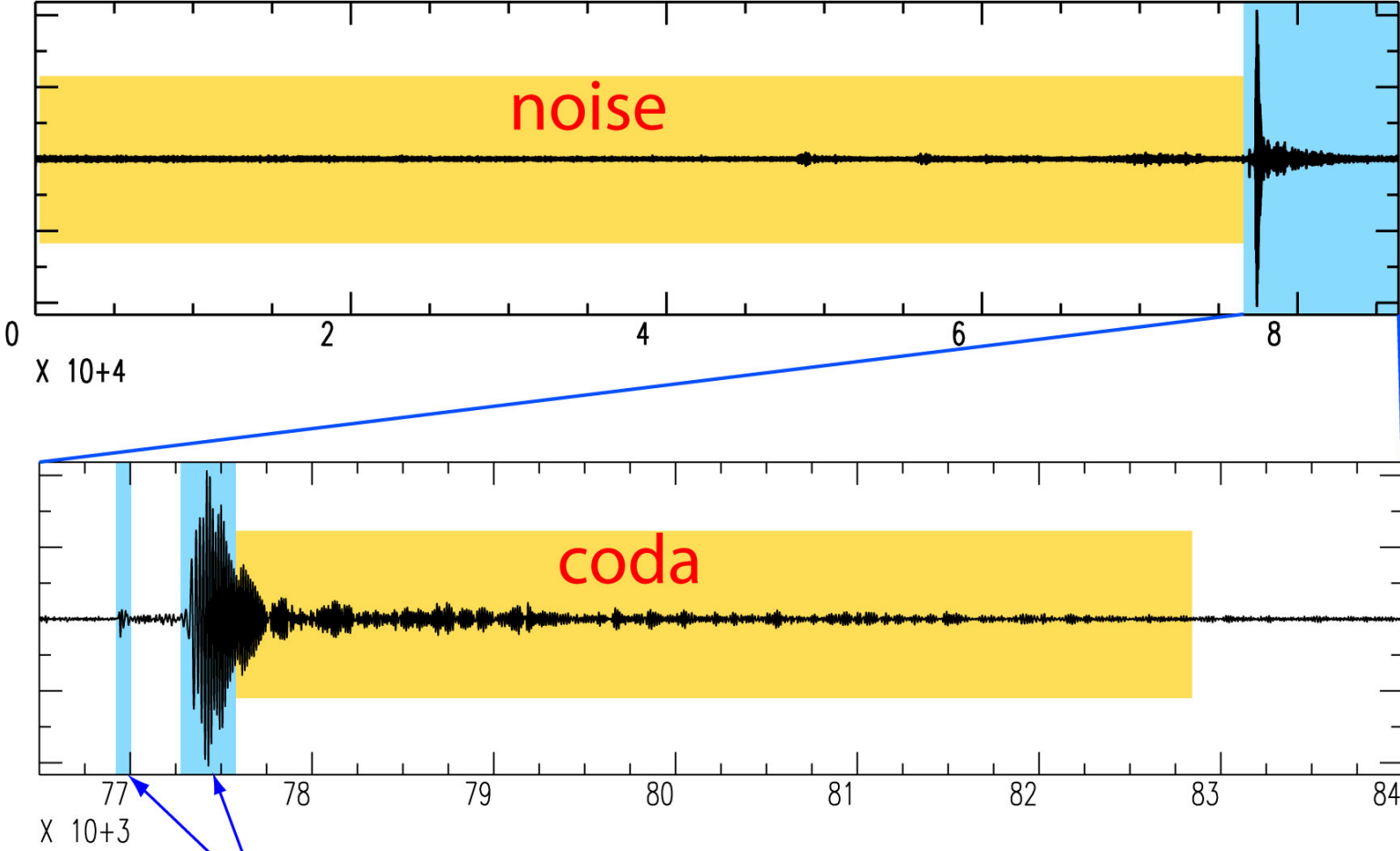


● FDSN stations

● Geoscope/FDSN stations

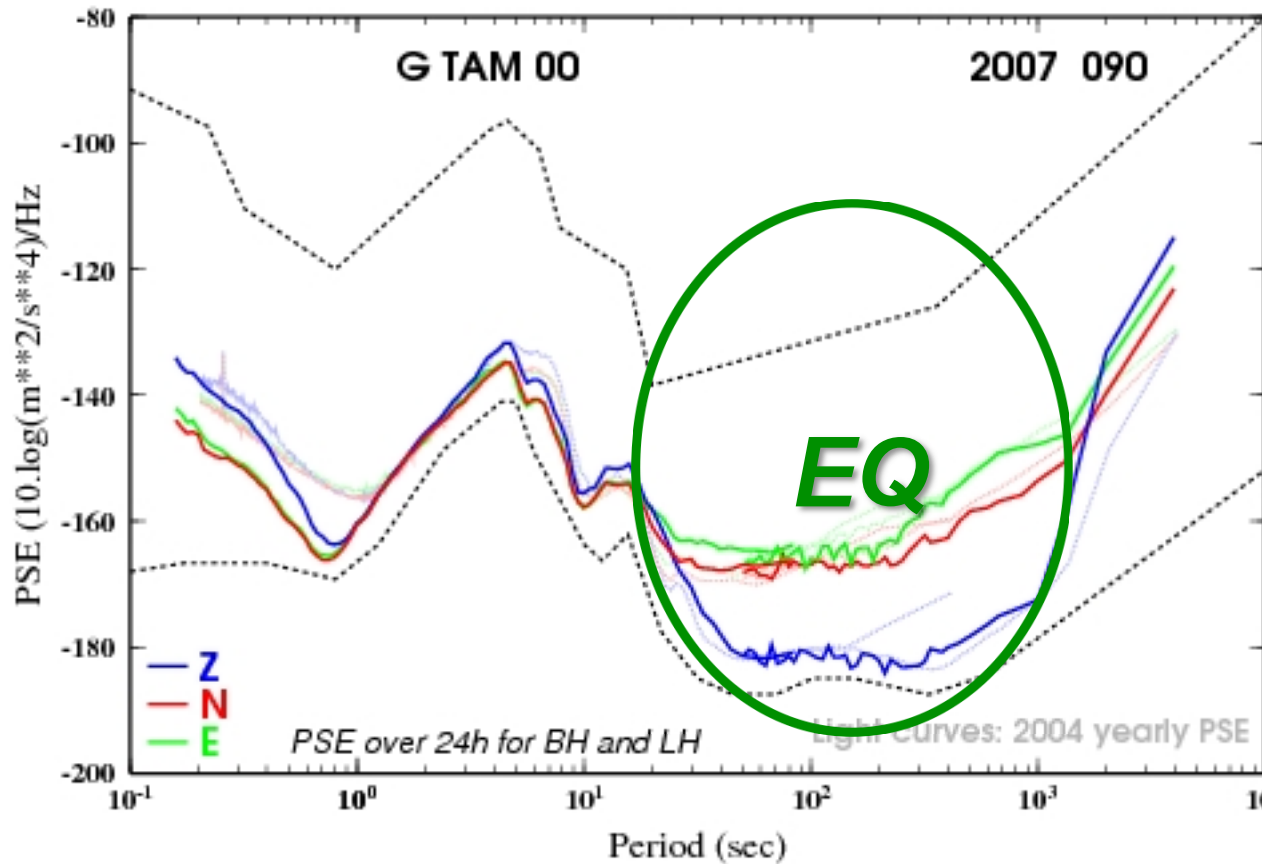
Geoscope/G.Roult

one day of seismic record



ballistic waves used in traditional tomography

GEOSCOPE and Noise

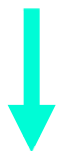


TAM (Tamanrasset, Algeria)

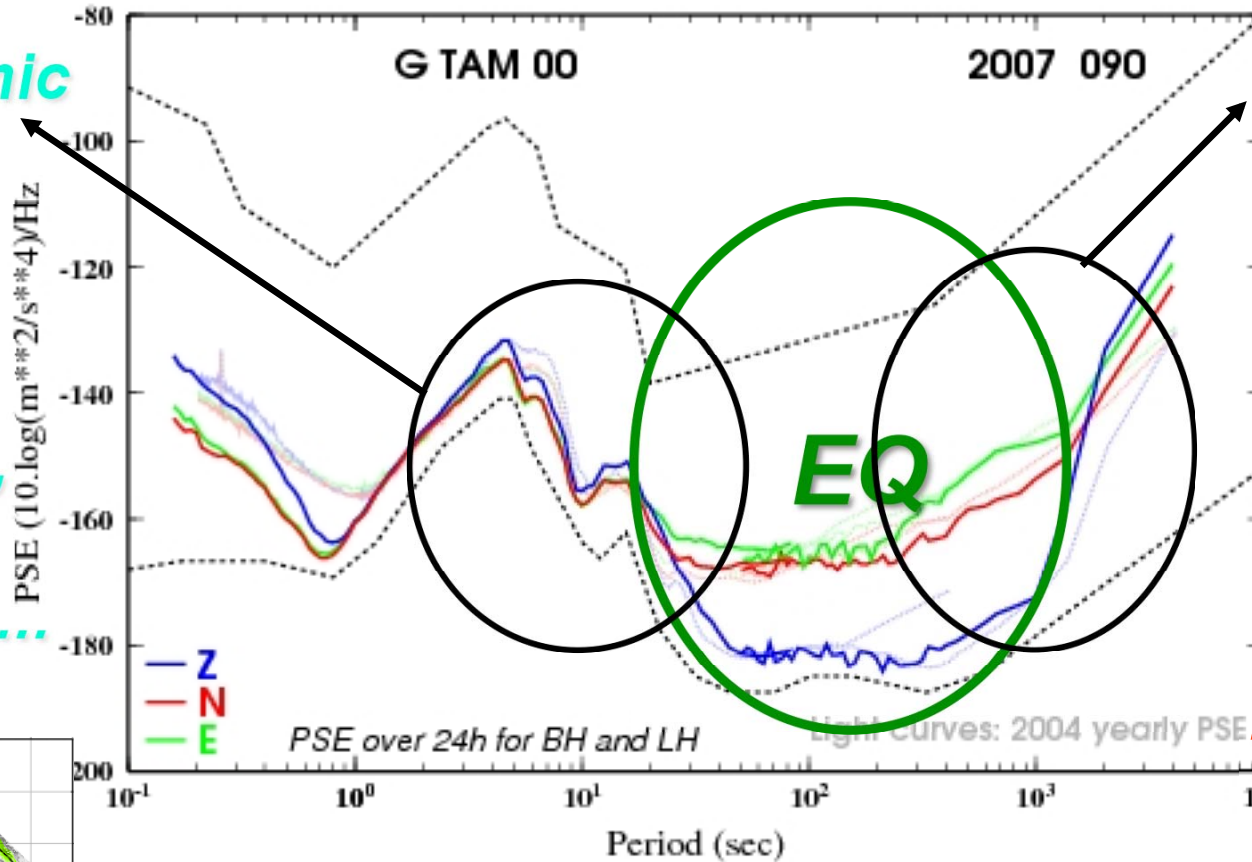
<http://geoscope.ipgp.fr>

GEOSCOPE and Noise

**Microseismic
Noise**



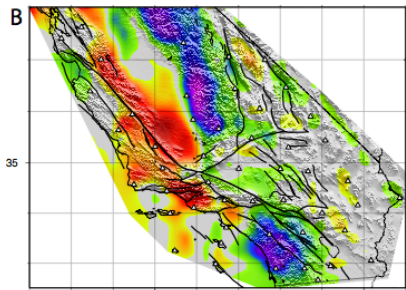
**Shapiro,
Campillo,
Roux,
Brenguier,...**



**VLP Noise
(transient,
Hum, ...)**



**Nishida,
Montagner,
Kawakatsu
(2009)**



2.00 2.35 2.55 2.65 2.75 2.85 2.95 3.05 3.15 3.40
group velocity (km/s)

TAM (Tamanrasset, Algeria)



Importance of seismic anisotropy

**ANISOTROPY is the Rule not the
Exception**

Seismic Anisotropy is present at all scales



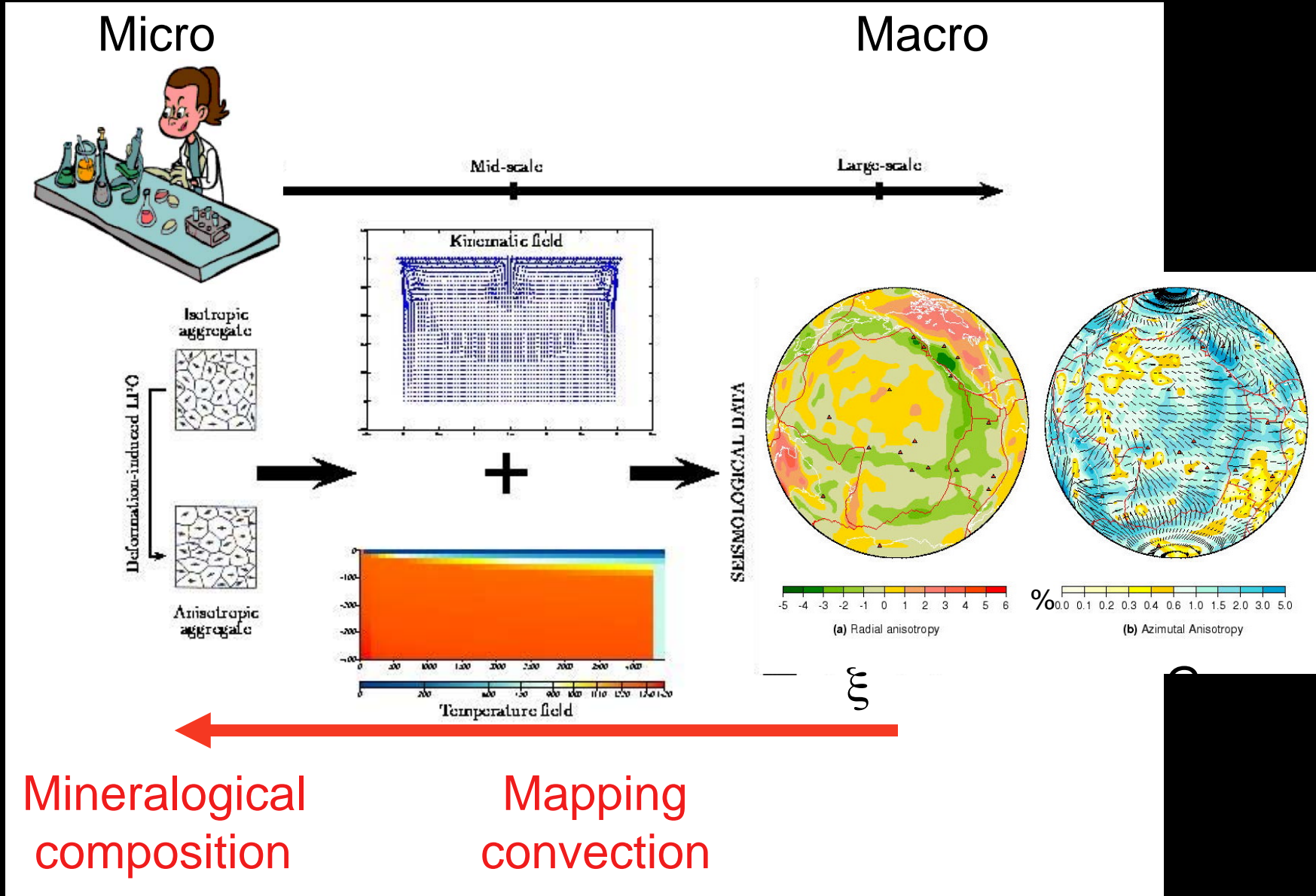
Importance of seismic anisotropy ANISOTROPY is the Rule not the Exception

Anisotropy is present at all scales

-From microscopic scale up to macroscopic scale

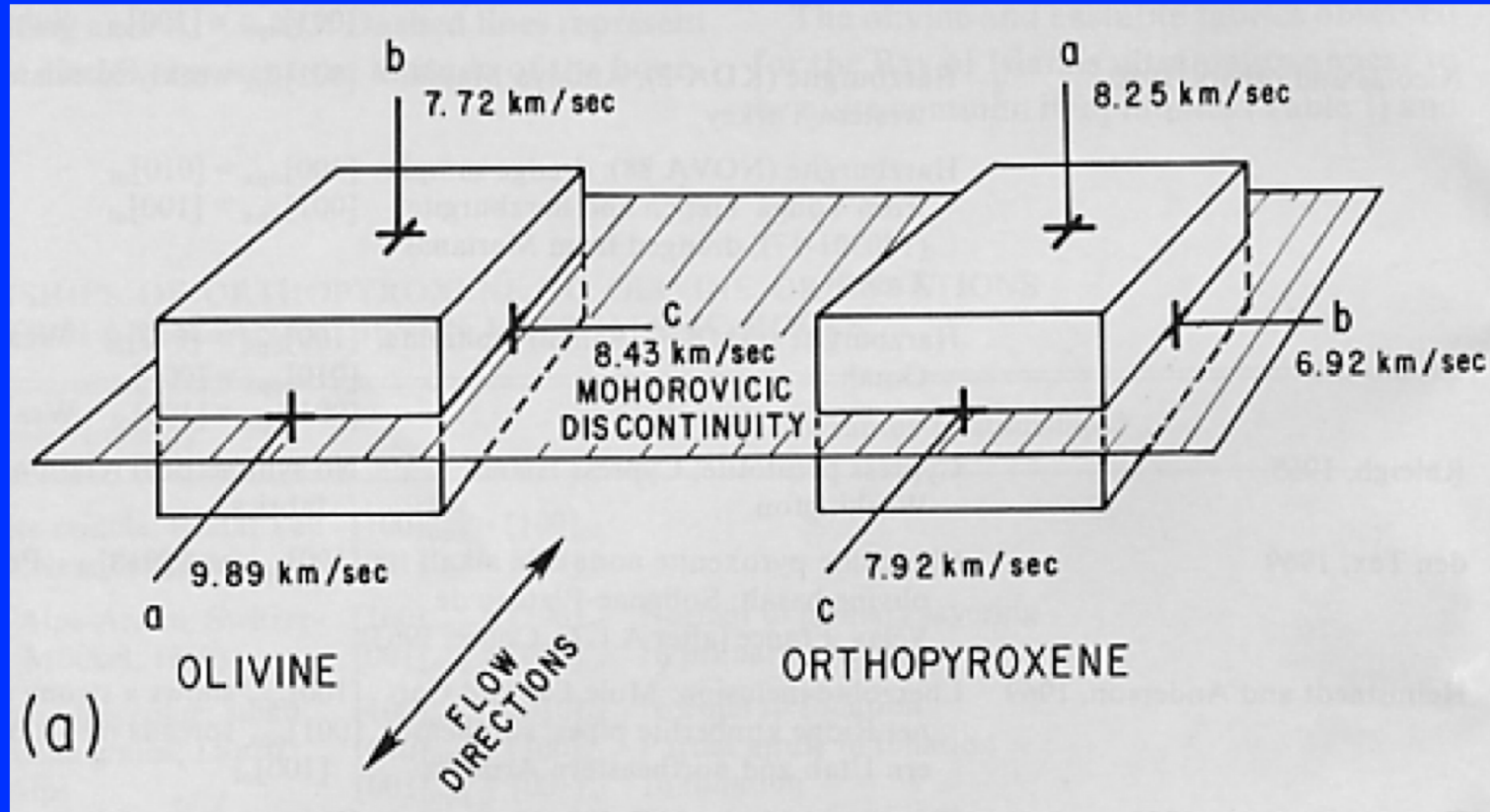
-Efficient mechanisms of alignment in the upper mantle:
(L.P.O.: lattice preferred orientation;
S.P.O.: shape preferred orientation;
FINE LAYERING)

NON UNIQUE INTERPRETATION



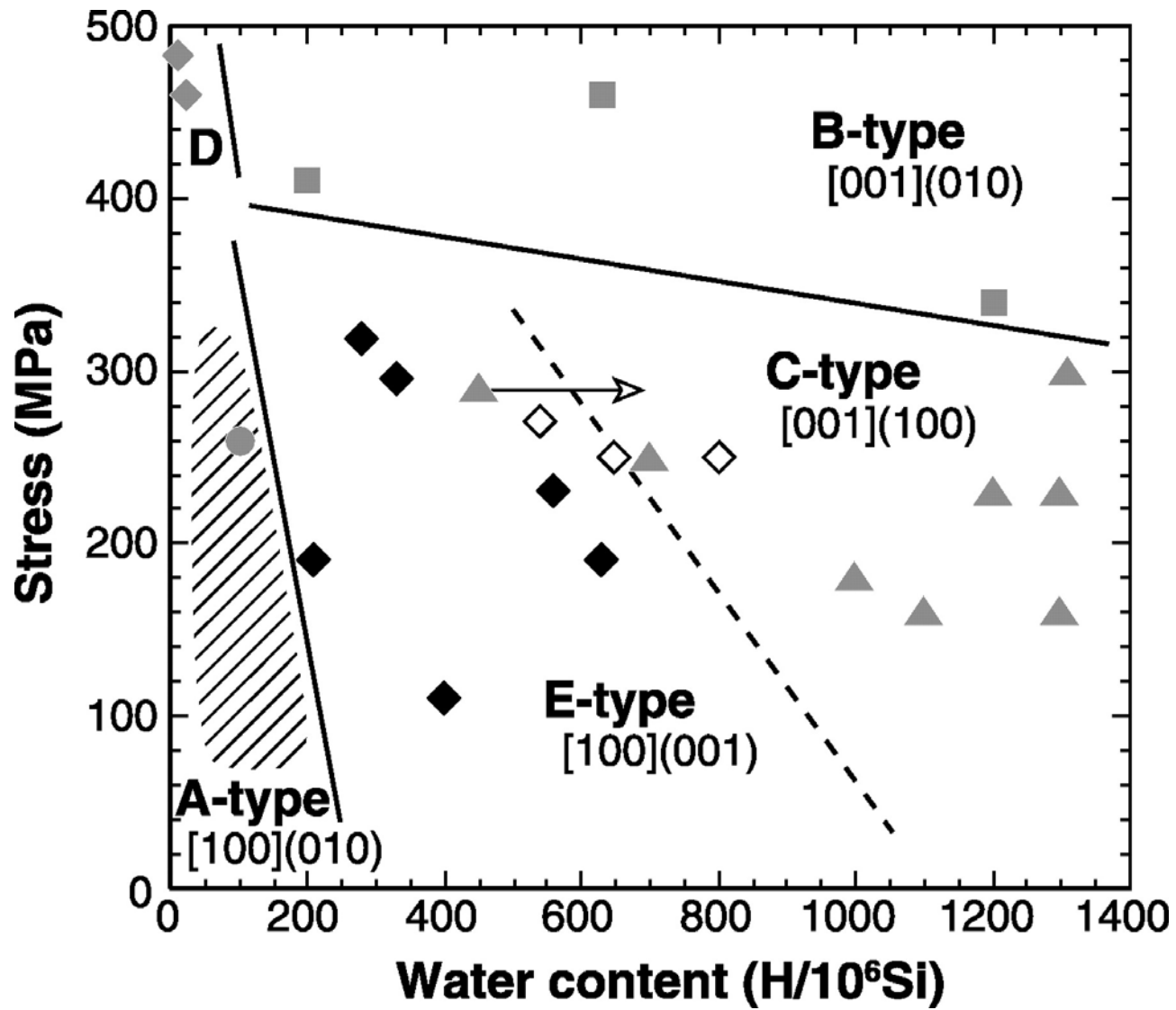
(Montagner and Guillot, 2001)

L.P.O. : Lattice Preferred Orientation (strain field)



Christensen and Lundquist, 1982

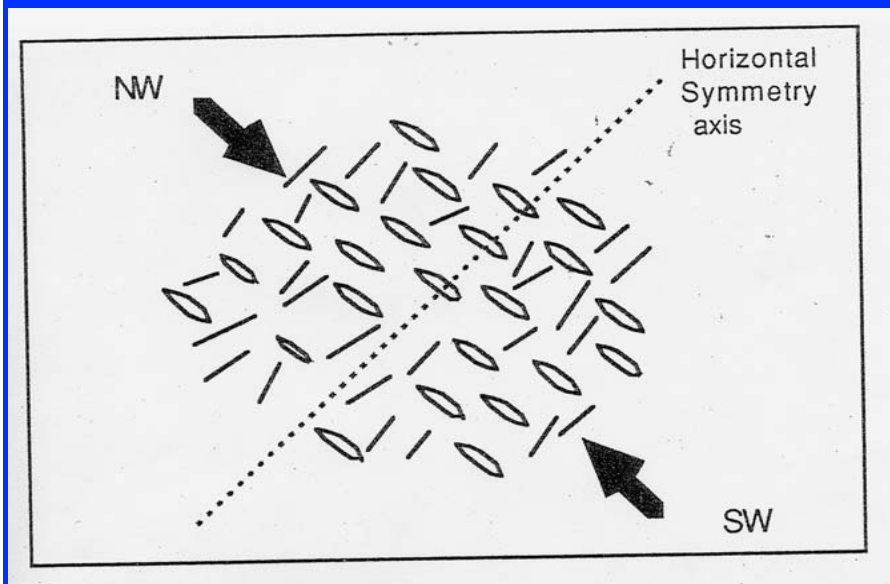
➔ ***Mapping of convection***



New Types of Olivine Fabric

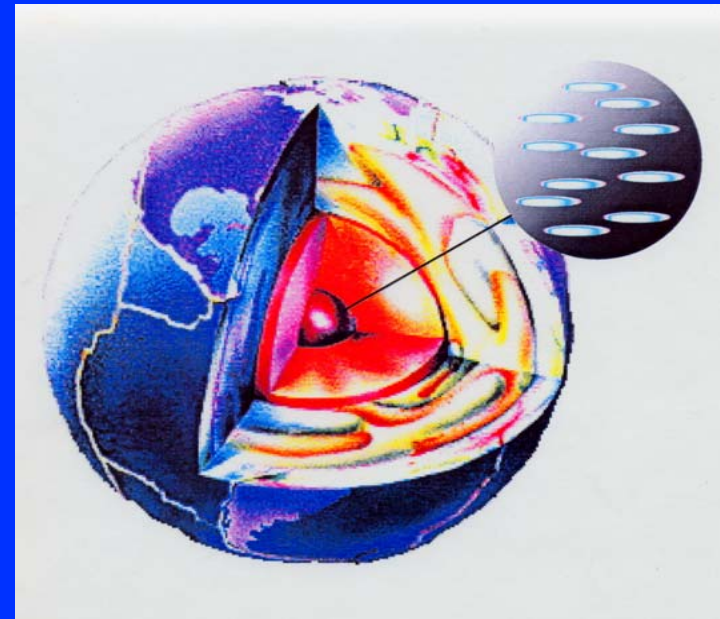
S.P.O.: Cracks, fluid inclusions, ... (stress field)

Crust (+lithosphere)



(Babuska and Cara, 1991)

Inner core



(Singh et al., 2001)



*Temporal variations of anisotropy?
Monitoring of seismogenic zones (Durand et al. 2010)*

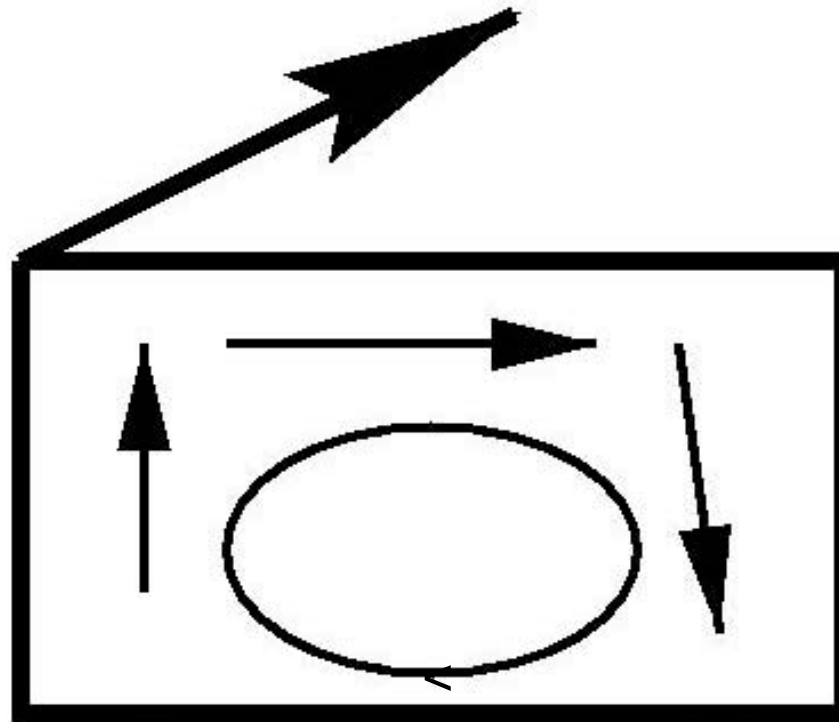


Importance of seismic anisotropy ANISOTROPY is the Rule not the Exception

Anisotropy is present at all scales

- From microscopic scale up to macroscopic scale
- Efficient mechanisms of alignment (L.P.O.: lattice preferred orientation; S.P.O.: shape preferred orientation; Fine layering)

NON UNIQUE INTERPRETATION



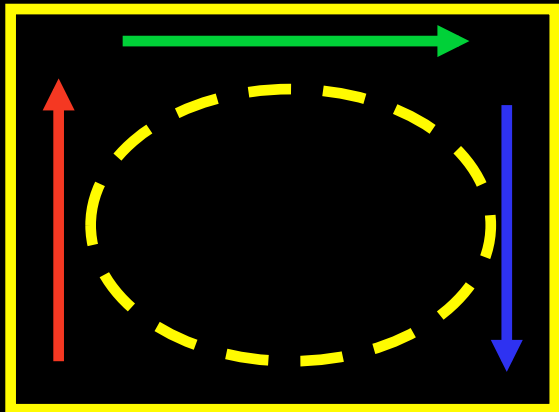
$\Delta\alpha$ Effect of Mineral Orientation

ΔT Effect of Temperature Heterogeneities

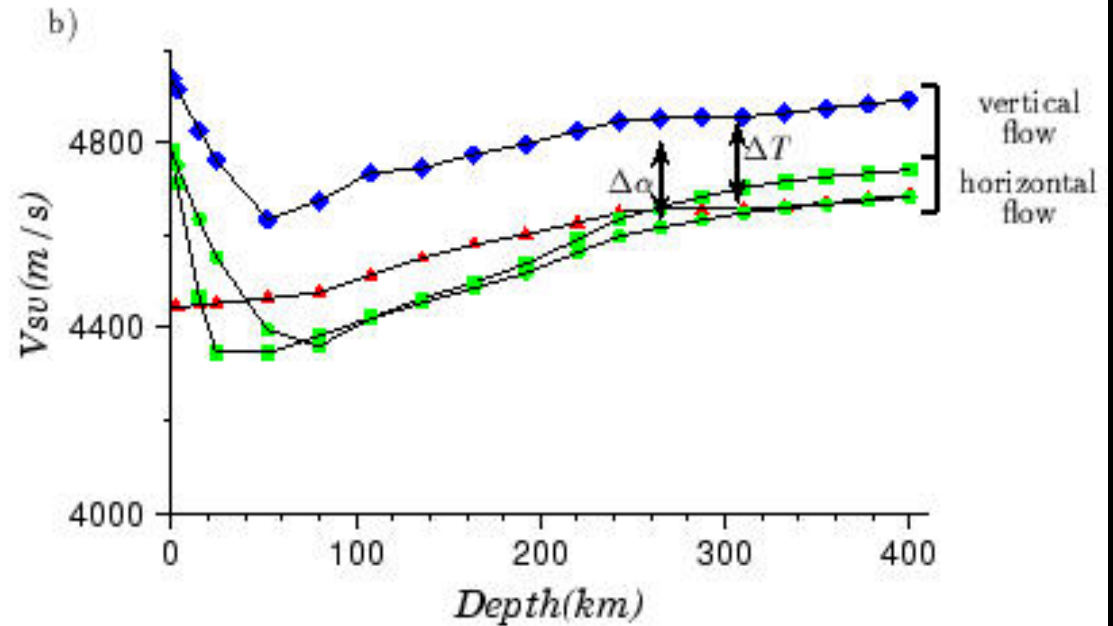
$\Delta\alpha$: Anisotropy
Effect

ΔT : Temperature
Effect

$$\Delta\alpha \approx \Delta T$$



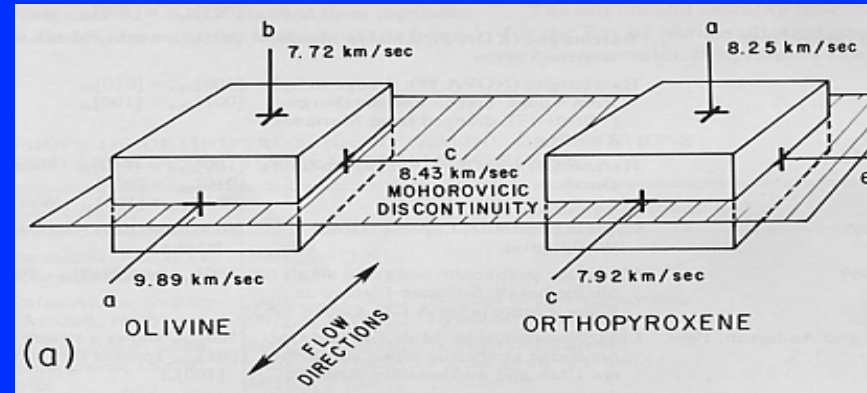
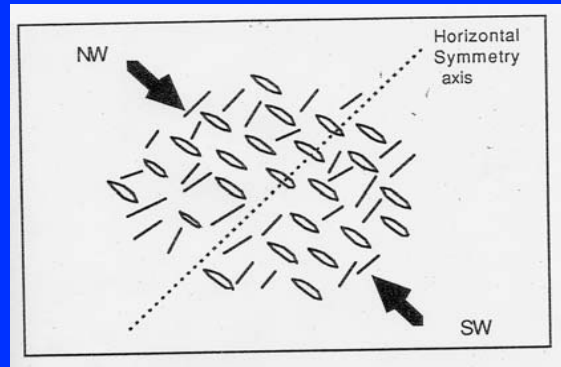
Olivine (60%) + Opx (40%)



Montagner & Guillot, 2002

Different processes in different layers

-S.P.O. ***-L.P.O.***



- ***Water content***
- ***Fine Layering***

- ***Present day tectonic, geodynamic processes***
 - ***Past processes (frozen anisotropy)***

Stratification of anisotropy in the upper mantle



Importance of seismic anisotropy
ANISOTROPY is the Rule not the Exception



Anisotropy is present at all scales

- from microscopic scale to macroscopic scale
- Efficient mechanisms of alignment
(L.P.O.: lattice preferred orientation
S.P.O.: shape preferred orientation; Fine layering)

Anisotropy is observed on different kinds of seismic waves

- Body waves (Pn; S-wave splitting)
- Surface waves (Rayleigh-Love discrepancy, azimuthal anisotropy)



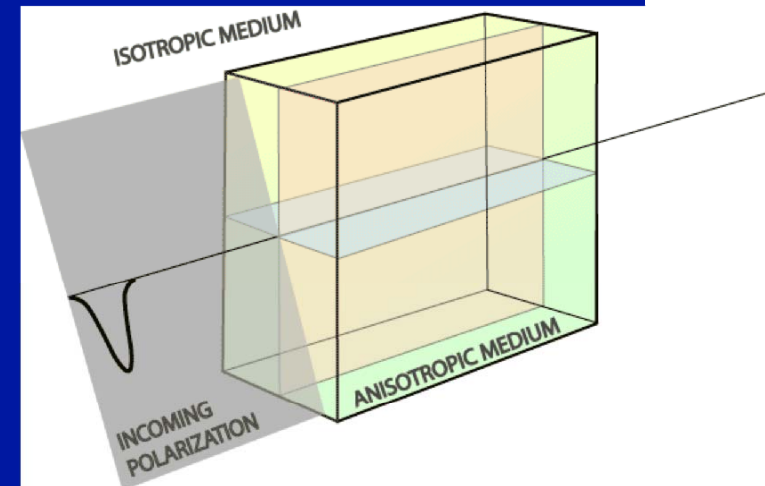
Different kinds of data

Body waves:

P-wave azimuthal variations
SKS, S-wave splitting

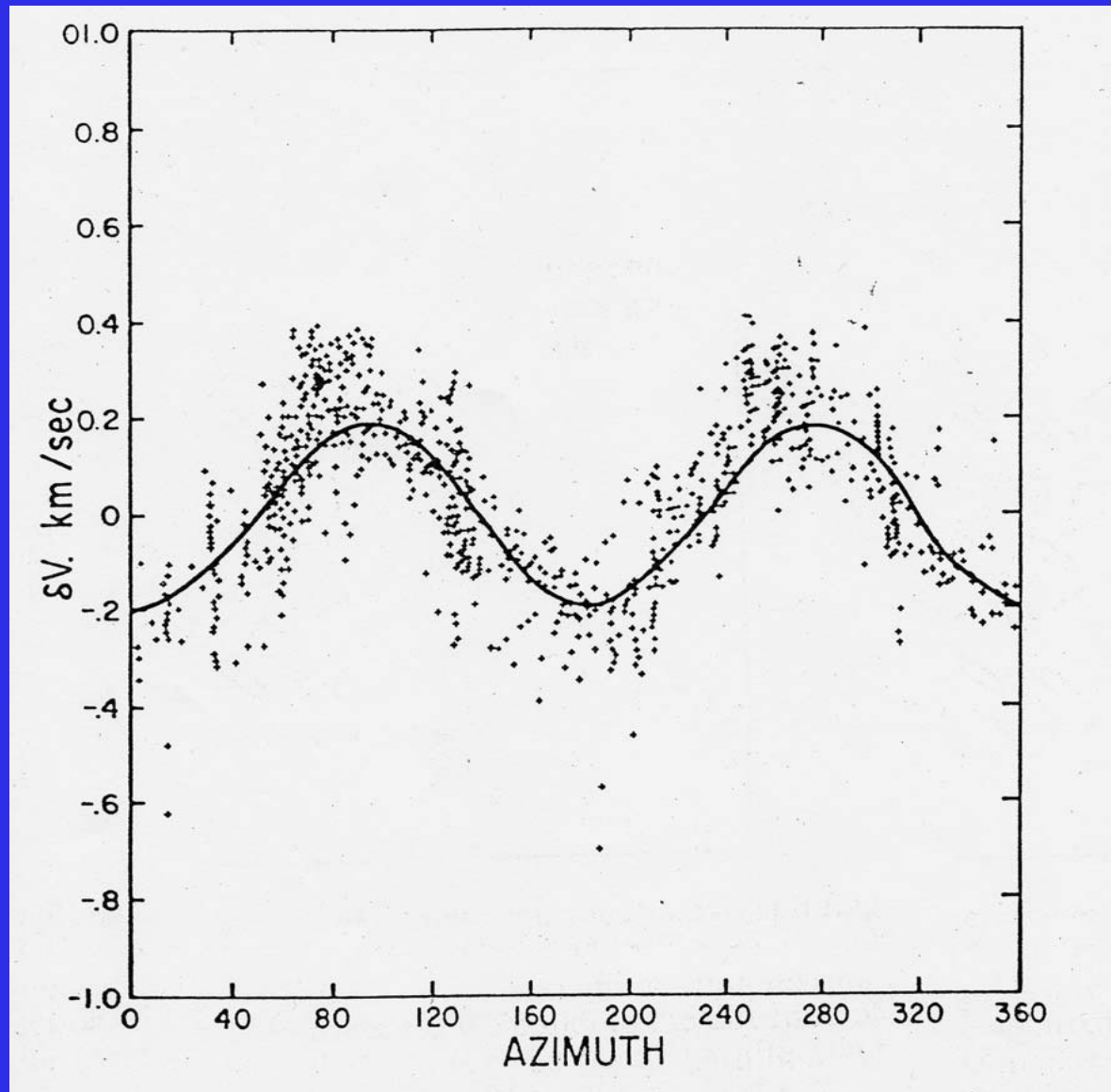
Surface waves:

- discrepancy Rayleigh Love (polarization anisotropy)
- Azimuthal variations of phase (or group) velocities
- Effects on amplitudes



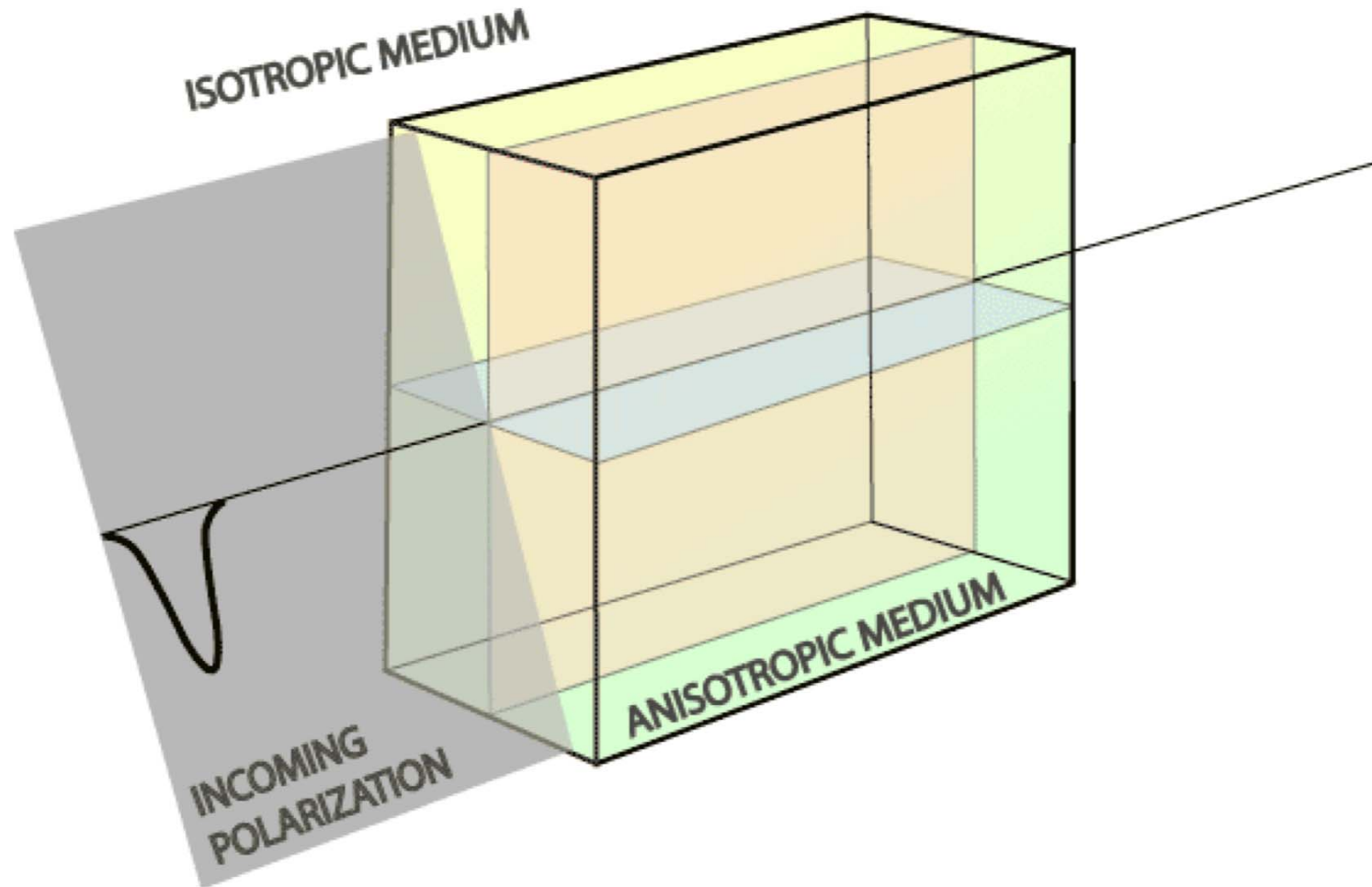
Animation courtesy of Ed Garnero

Pn- velocities



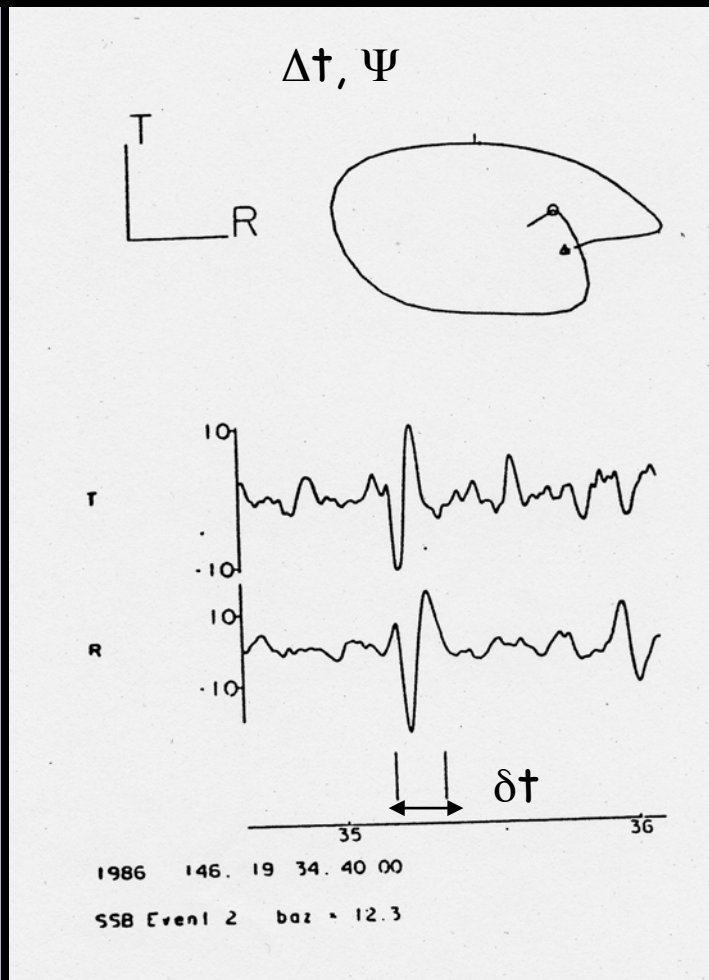
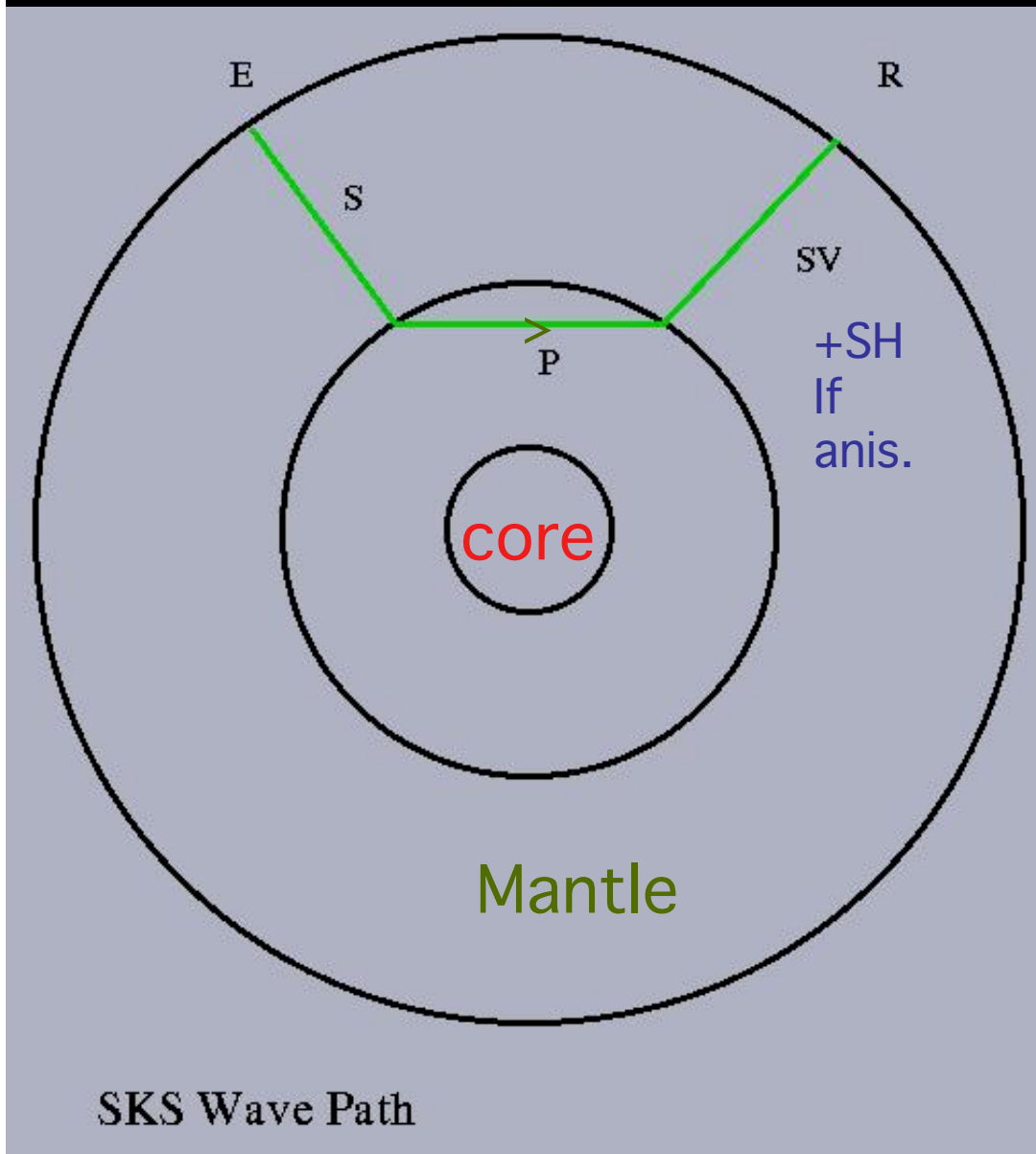
(Raitt et al., 1969)

Shear Wave Splitting (Birefringence)



Animation courtesy of Ed Garnero

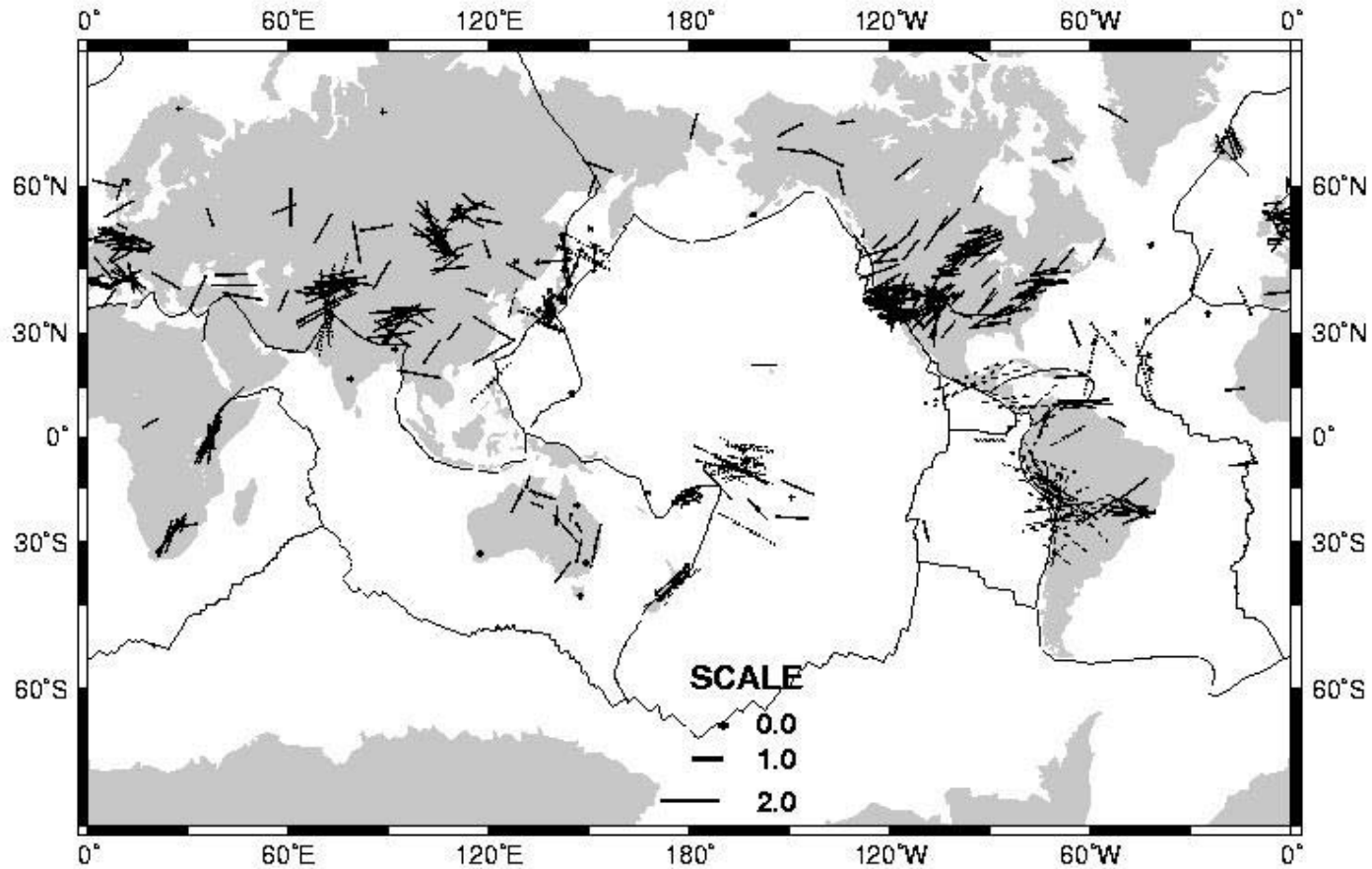
SKS- Splitting



T
R

Vinnik et al., 1989

Compilation of S-wave splitting measurements



Savage, Rev. Geophys., 1999



SURFACE WAVES



Importance of seismic anisotropy
ANISOTROPY is the Rule not the Exception



Anisotropy is present at all scales

- from microscopic scale to macroscopic scale
- Efficient mechanisms of alignment
(L.P.O.: lattice preferred orientation
S.P.O.: shape preferred orientation; fine layering)

Anisotropy is observed on different kinds of seismic waves

- Body waves (Pn; S-wave splitting)
- Surface waves (Rayleigh-Love discrepancy, azimuthal anisotropy)

ANISOTROPY REFLECTS AN INNER ORGANIZATION

ANISOTROPY IS NOT A SECOND ORDER EFFECT

BUT NON UNIQUE INTERPRETATION

Anisotropic Tomographic Technique

- **Forward Problem:** Theory $\mathbf{d}=\mathbf{g}(\mathbf{p})$ \Rightarrow 1st order perturbation theory

\mathbf{d} data space (seismograms)

\mathbf{p} parameter space (anisotropy)



- Reference Earth model \mathbf{p}_0 :

$$\mathbf{d}_0 = \mathbf{g}(\mathbf{p}_0)$$

- Kernels $\partial\mathbf{g}/\partial\mathbf{p}$

- Cd function (or matrix) of covariance of data

- **Inverse Problem:** $\mathbf{p}-\mathbf{p}_0 = \mathbf{g}^{-1}(\mathbf{d}-\mathbf{d}_0)$

- \mathbf{C}_{p_0} a priori Covariance function of parameters

- \mathbf{C}_{pf} a posteriori Covariance function of parameters

- R Resolution

Effect of anisotropy on surface waves

Effect on eigenfrequency ω_k for multiplet $k=\{n,l,m\}$ and phase velocity V

$$\frac{\delta\omega_k}{\omega_k} = \frac{\int_{\Omega} \varepsilon_{ij}^* \delta C_{ijkl} \varepsilon_{kl} d\Omega}{\int_{\Omega} \rho_0^* u_r^* u_r d\Omega} = \left. \frac{\delta V}{V} \right|_k$$

ε strain tensor, u displacement, δC_{ijkl} elastic tensor perturbation

Phase velocity perturbation $V(T, \theta, \phi, \Psi)$ at point $r(\theta, \phi)$ (Smith & Dahlen, 1973)

$$\begin{aligned} \delta V(T, \theta, \phi, \Psi) / V = & \alpha_0(T, \theta, \phi) + \alpha_1(T, \theta, \phi) \cos 2\Psi + \alpha_2(T, \theta, \phi) \sin 2\Psi \\ & + \alpha_3(T, \theta, \phi) \cos 4\Psi + \alpha_4(T, \theta, \phi) \sin 4\Psi \end{aligned}$$

Ψ Azimuth (angle between North and wave vector)

Table 1: Calculation of the various $c_{ij}\epsilon_i\epsilon_j$ for Love waves

$$\alpha = \cos\Psi; \beta = \sin\Psi$$

n	ij	$c_{ij}\epsilon_i\epsilon_j$
1	11	$c_{11}\alpha^2\beta^2.k^2W^2$
1	22	$c_{22}\alpha^2\beta^2.k^2W^2$
1	33	0
2	12	$-c_{12}\alpha^2\beta^2.k^2W^2$
2	13	0
2	23	0
2	24	
4	14	$c_{14}(-i\alpha^2\beta).\frac{kWW'}{2}$
4	15	$c_{15}(i\alpha^2\beta).\frac{kWW'}{2}$
4	16	$c_{16}(-\alpha\beta)(\alpha^2 - \beta^2).\frac{k^2W^2}{2}$
4	24	$c_{24}(-i\alpha^2\beta).\frac{kWW'}{2}$
4	25	$c_{25}(-i\alpha\beta^2).\frac{kWW'}{2}$
4	26	$c_{26}(\alpha\beta)(\alpha^2 - \beta^2).\frac{k^2W^2}{2}$
4	34	0
4	35	0
4	36	0
4	44	$c_{44}\alpha^2.\frac{W'^2}{4}$
8	45	$c_{45}(-\alpha\beta).\frac{W'^2}{4}$
8	46	$c_{46}(-i\alpha)(\alpha^2 - \beta^2).\frac{kWW'}{2}$
4	55	$c_{55}\beta^2.\frac{W'^2}{4}$
8	56	$c_{56}(i\beta)(\alpha^2 - \beta^2).\frac{kWW'}{2}$
4	66	$c_{66}(\alpha^2 - \beta^2).\frac{k^2W^2}{4}$

$$C_{mnpq} \longrightarrow C_{ij}$$

Indices:

$$i = 9 - m - n$$

$$j = 9 - p - q$$

$W(r)$ Love displacement

$$W' = \left(\frac{dW}{dr}\right)$$

The first order perturbation in Love wave phase velocity $\delta C_L(k, \Psi)$ can be expressed as:

$$\delta C_L(k, \Psi) = \frac{1}{2C_{0L}(k)} [L_1(k) + L_2(k)\cos 2\Psi + L_3(k)\sin 2\Psi + L_4(k)\cos 4\Psi + L_5(k)\sin 4\Psi]$$

where

$$\begin{aligned}
 & L_0(k) = \int_0^\infty \rho W^2 dz \\
 0-\Psi \quad & \left\{ \begin{aligned} L_1(k) &= \frac{1}{L_0} \int_0^\infty \left(W^2 \delta N + \frac{W'^2}{k^2} \delta L \right) dz \end{aligned} \right. \\
 2-\Psi \quad & \left\{ \begin{aligned} L_2(k) &= \frac{1}{L_0} \int_0^\infty -G_c \left(\frac{W'^2}{k^2} \right) dz \\ L_3(k) &= \frac{1}{L_0} \int_0^\infty -G_s \left(\frac{W'^2}{k^2} \right) dz \end{aligned} \right. \\
 4-\Psi \quad & \left\{ \begin{aligned} L_4(k) &= \frac{1}{L_0} \int_0^\infty -E_c \cdot W^2 dz \\ L_5(k) &= \frac{1}{L_0} \int_0^\infty -E_s \cdot W^2 dz \end{aligned} \right.
 \end{aligned}$$

The same procedure holds for Rayleigh waves, starting from the displacement given previously.

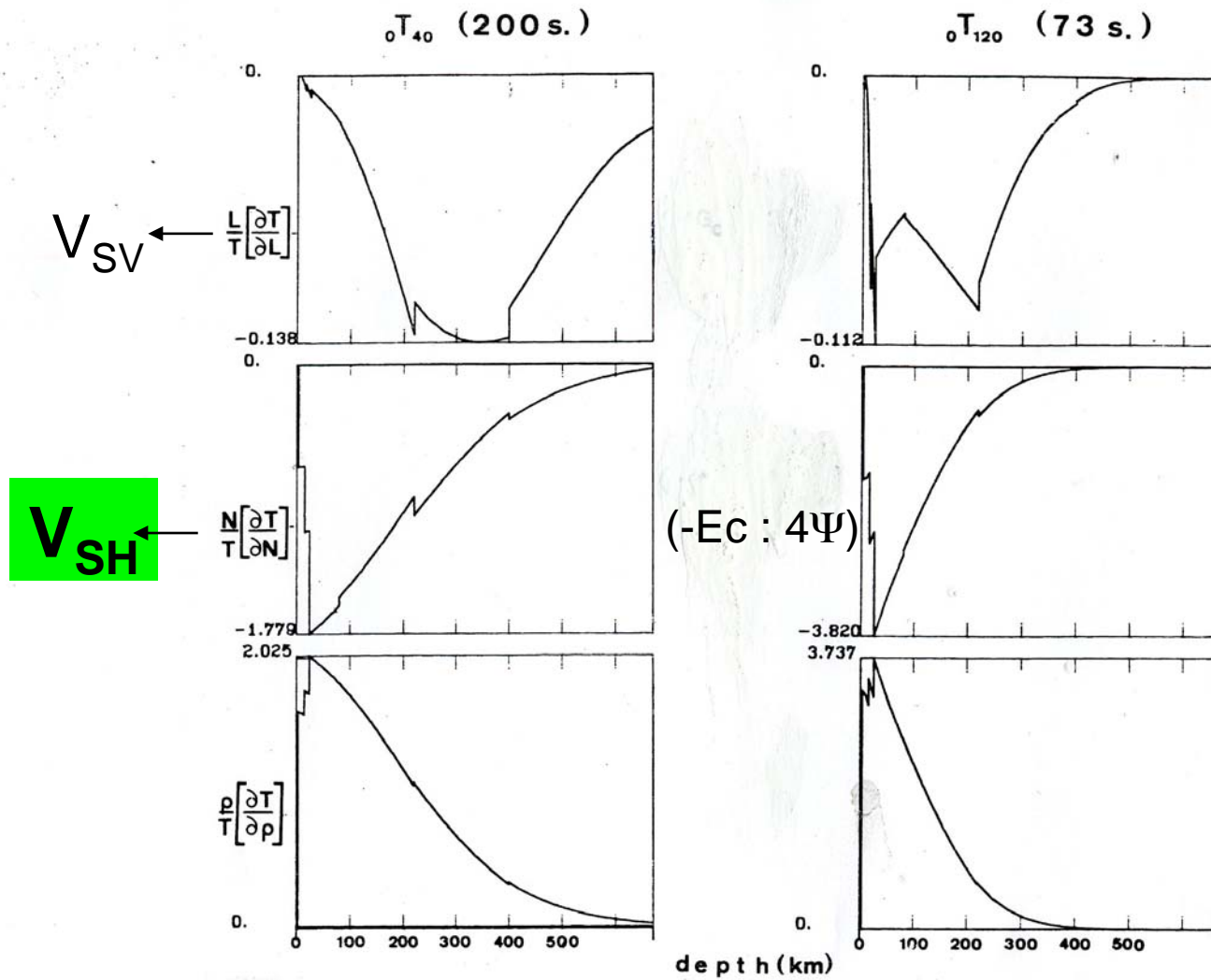
$$\delta C_R(k, \Psi) = \frac{1}{2C_{0R}(k)} [R_1(k) + R_2(k)\cos 2\Psi + R_3(k)\sin 2\Psi + R_4(k)\cos 4\Psi + R_5(k)\sin 4\Psi]$$

where

$$\begin{aligned} R_0(k) &= \int_0^\infty \rho(U^2 + V^2)dz \\ 0-\Psi \quad R_1(k) &= \frac{1}{R_0} \int_0^\infty [V^2 dA + \frac{U^2}{k^2} \cdot dC + \frac{2U'V}{k} \cdot dF + (\frac{V'}{k} - U)^2 dL] dz \\ 2-\Psi \quad \left\{ \begin{aligned} R_2(k) &= \frac{1}{R_0} \int_0^\infty [V^2 \cdot B_c + \frac{2U'V}{k} \cdot H_c + (\frac{V'}{k} - U)^2 G_c] dz \\ R_3(k) &= \frac{1}{R_0} \int_0^\infty [V^2 \cdot B_s + \frac{2U'V}{k} \cdot H_s + (\frac{V'}{k} - U)^2 G_s] dz \end{aligned} \right. \\ 4-\Psi \quad \left\{ \begin{aligned} R_4(k) &= \frac{1}{R_0} \int_0^\infty E_c \cdot V^2 dz \\ R_5(k) &= \frac{1}{R_0} \int_0^\infty E_s \cdot V^2 dz \end{aligned} \right. \end{aligned}$$

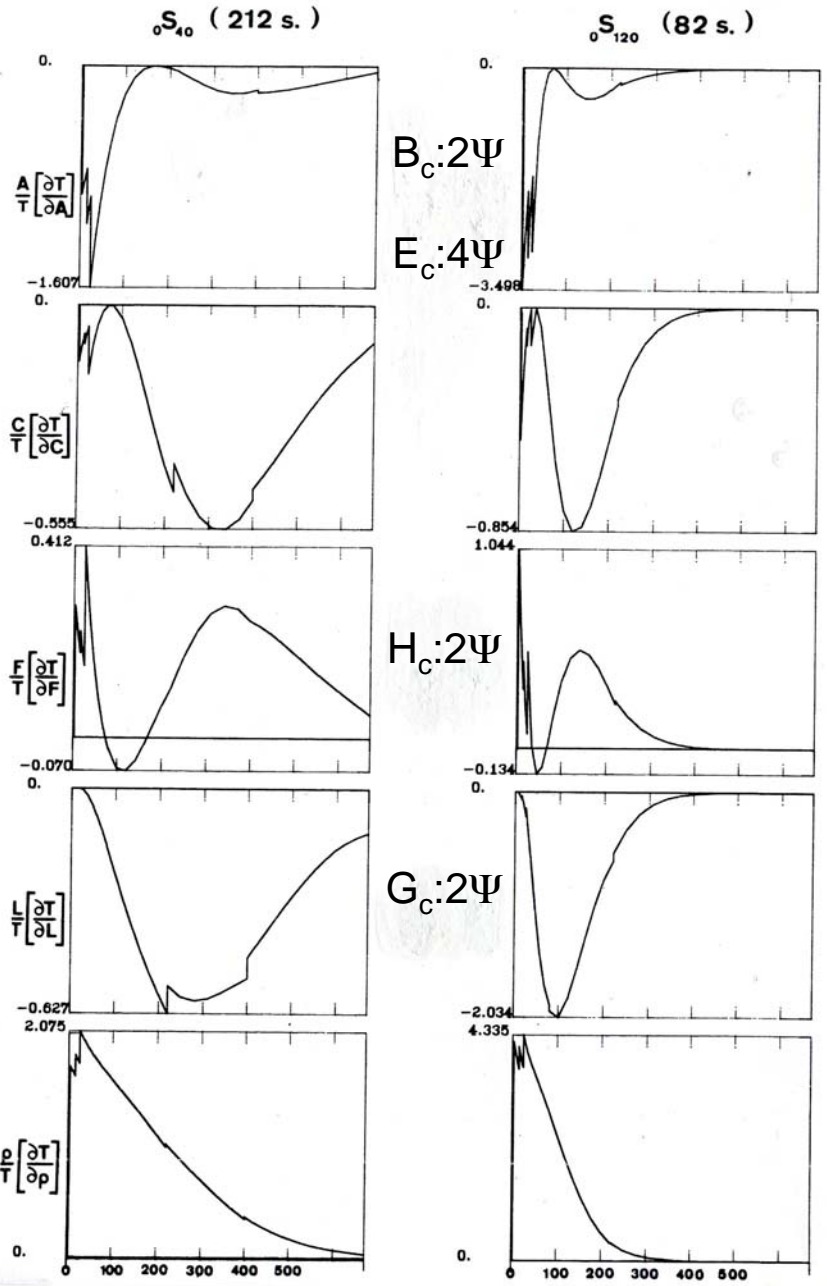
The 13 depth-functions $A, C, F, L, N, B_c, B_s, H_c, H_s, G_c, G_s, E_c, E_s$ are linear combinations of the elastic coefficients C_{ij} and are explicitly given as follows:

Love wave partial derivatives



Rayleigh wave partial derivatives

V_{PH} ←
 V_{PV} ←
 V_{SV} ←
 Density ←



13 parameters

Physical Meaning

0Ψ term	$A = \frac{3}{8}(C_{11} + C_{22}) + \frac{1}{4}C_{12} + \frac{1}{2}C_{66}$ $C = C_{33}$ $F = \frac{1}{2}(C_{13} + C_{23})$ $L = \frac{1}{2}(C_{44} + C_{55})$ $N = \frac{1}{8}(C_{11} + C_{22}) - \frac{1}{4}C_{12} + \frac{1}{2}C_{66}$	V_{PH} V_{PV} V_{SV} V_{SH}
	cos	sin
2Ψ term	$B_c = \frac{1}{2}(C_{11} - C_{22})$ $G_c = \frac{1}{2}(C_{55} - C_{44})$ $H_c = \frac{1}{2}(C_{13} - C_{23})$	$B_s = C_{16} + C_{26} \rightarrow B$ $G_s = C_{54} \rightarrow G$ $H_s = C_{36} \rightarrow H$
4Ψ term	$E_c = \frac{1}{8}(C_{11} + C_{22}) - \frac{1}{4}C_{12} - \frac{1}{2}C_{66}$	$E_s = \frac{1}{2}(C_{16} - C_{26}) \rightarrow E$

Transversely
Isotropic Medium
With Vertical Symmetry
Axis (VTI)

Azimuthal variation of

V_{PH}
 V_{SV}
 F
 V_{SH} (or V_{PH})

Isotropic medium: 2 parameters

VTI: 5 parameters (A,C,F,L,N)

General + 8 (from surface waves)

•Best resolved parameters from surface waves
(among 13 parameters)

$$L = \rho V_{SV}^2 \quad \text{Isotropic part of } V_{SV}$$

$$\xi = N/L = \frac{V_{SH}^2}{V_{SV}^2} \quad \text{Radial Anisotropy}$$

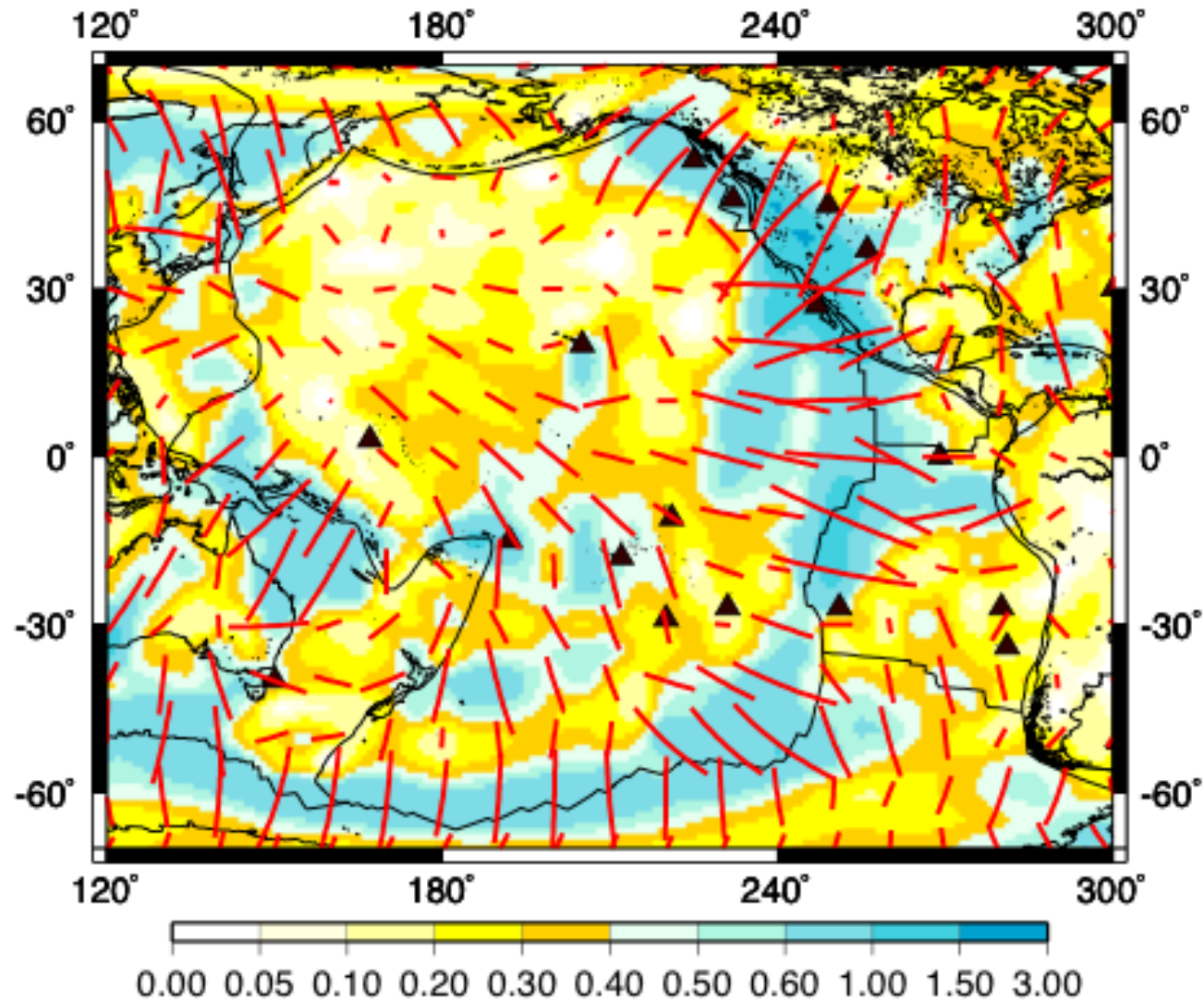
G, Ψ_G Azimuthal Anisotropy of V_{SV} , also related to SKS splitting (when horizontal symmetry axis, vertical propagation, Montagner et al., 2000)

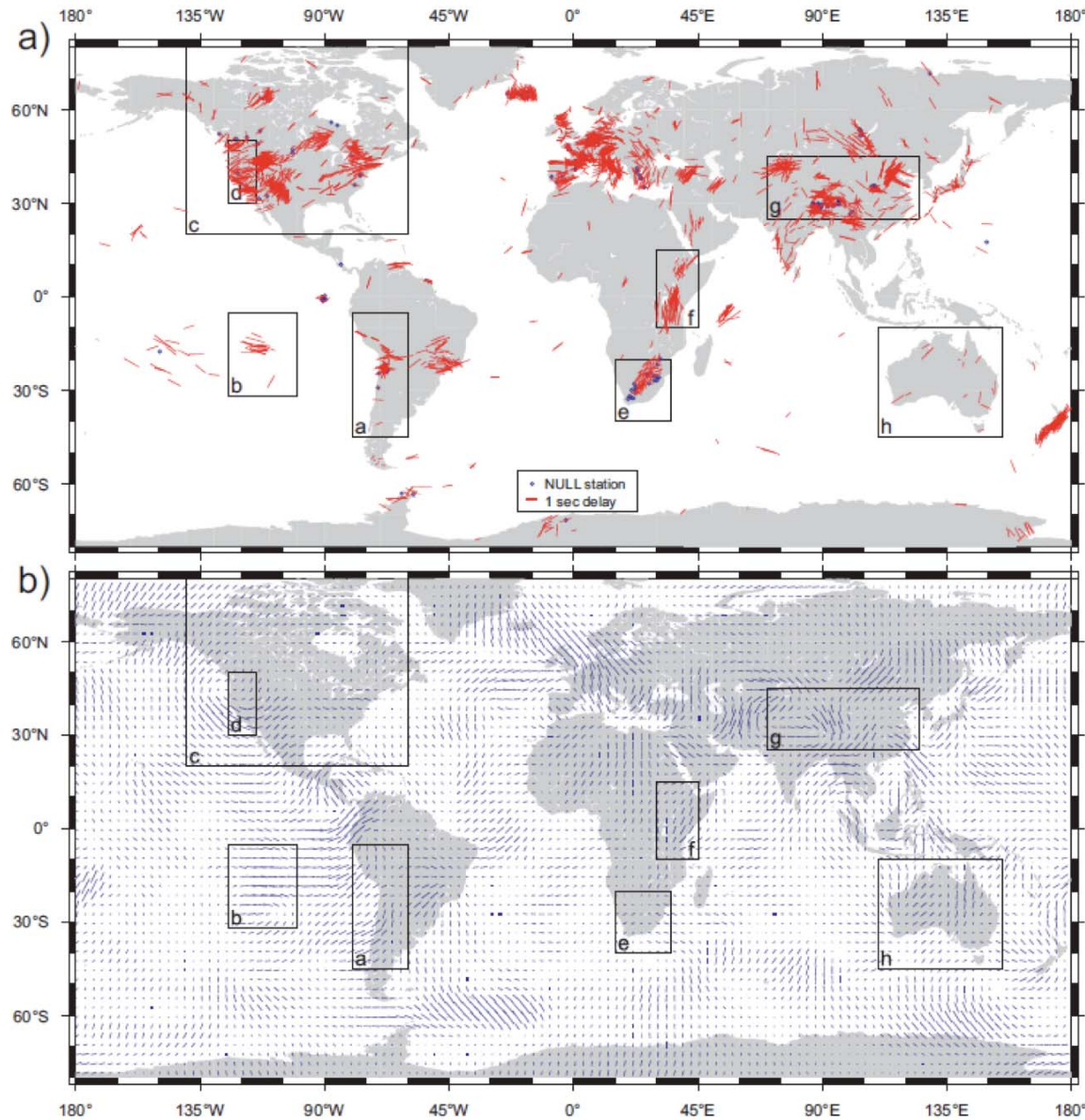
•Body waves (Crampin, 1984)

$$\rho V_{SV}^2 = L + G_c \cos 2\Psi + G_s \sin 2\Psi$$

$$\rho V_{SH}^2 = N - E_c \cos 4\Psi - E_s \sin 4\Psi$$

Synthetic SKS-wave splitting inferred in Pacific Ocean from surface wave anisotropy: \mathbf{L} , \mathbf{G}_c , \mathbf{G}_s parameters





Updated
SKS database

Synthetic SKS from
Surface Wave model
(Debayle et al., 2005)

Wüstefeld et al., 2009

Geodynamic Interpretation: 3 Maps

Convective cell: anisotropic parameters

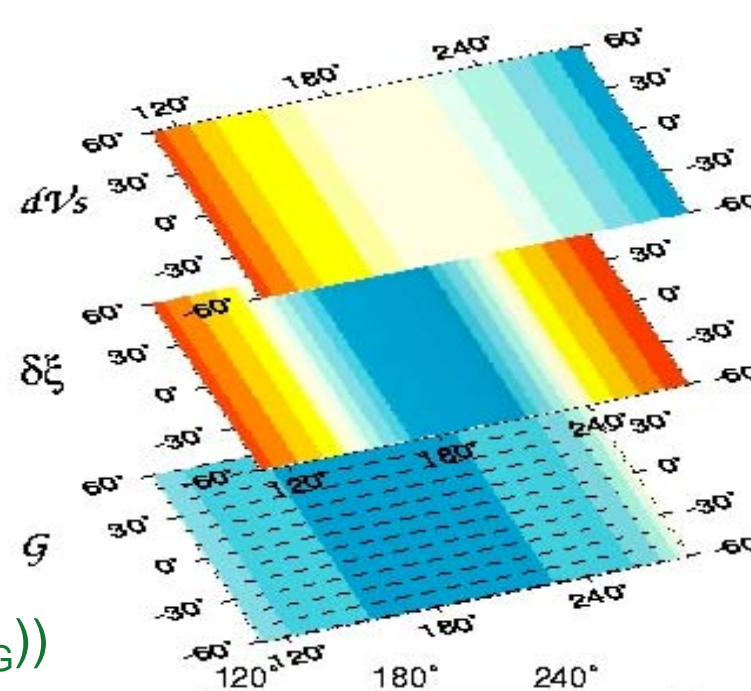
S- Velocity

Radial Anisotropy

$$\xi = (V_{SH}^2 - V_{SV}^2) / V_{SV}^2$$

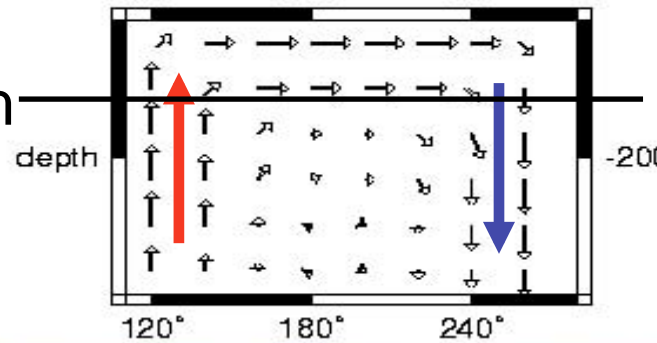
Azimuthal Anisotropy

$$V_{SV} \approx V_{SV0} + \frac{1}{2} G \cos(2(\Psi - \Psi_G))$$

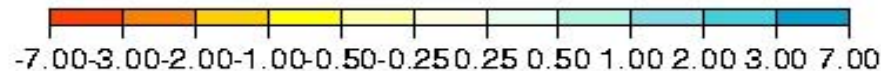


Interpretation
(L.P.O.)

At a given depth



Map Flow



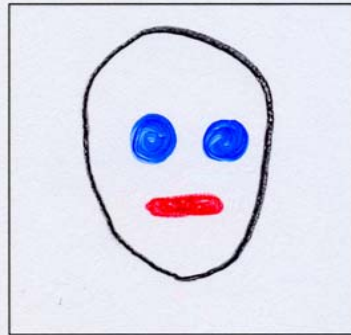
IMAGING OF FAMOUS SCIENTISTS



Anisotropic imaging



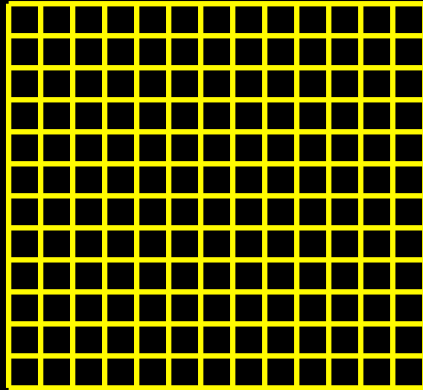
Isotropic Imaging



***How can we know whether
azimuthal anisotropy
is significant or not?***

Example of 2 D tomography (N cells)

Isotropic Inversion:

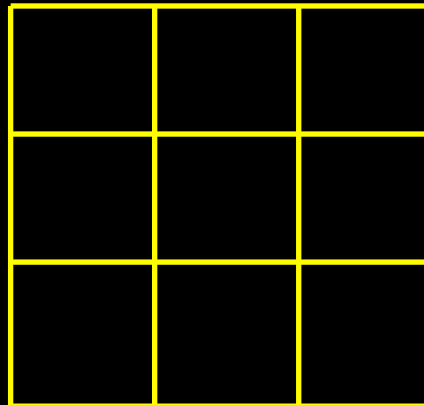


N independent parameters (1/cell)

0- Ψ term

Variance reduction: VR1

Anisotropic inversion



$3N' = N$ (3/cell)

(N' cells)

0+2 Ψ terms

Variance reduction: VR2

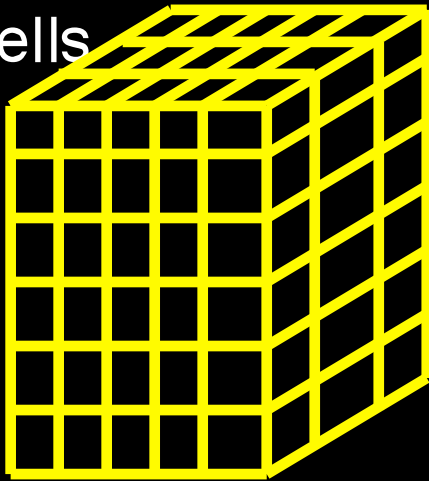
$VR2 > VR1 \Rightarrow$ the anisotropic model can be simpler than the isotropic model

Parameter Space

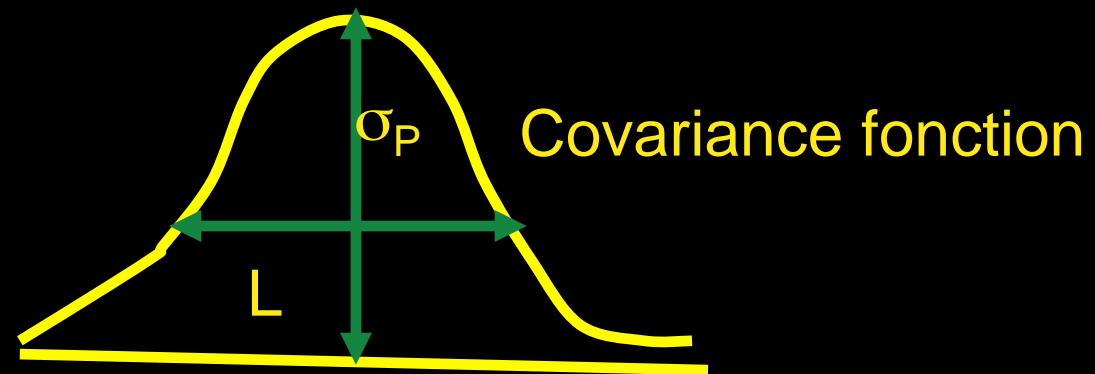
Physical parameters: $\rho + 13$ physical parameters

Geographical parameterization: $\mathbf{p}(r, \theta, \phi)$

- Cells



Continuous parameterization



- Spherical harmonic expansion \longrightarrow Global scale

- Lateral resolution (global scale):

Hor 1000km, Rad 50km $\Rightarrow 500 \cdot 60 \cdot 14 \approx 420,000$ parameters

Tomographic Technique

- **Forward Problem:** Theory $\mathbf{d}=\mathbf{g}(\mathbf{p})$

\mathbf{d} data space



Phase or group velocities

\mathbf{p} parameter space

- Reference Earth model \mathbf{p}_0 :

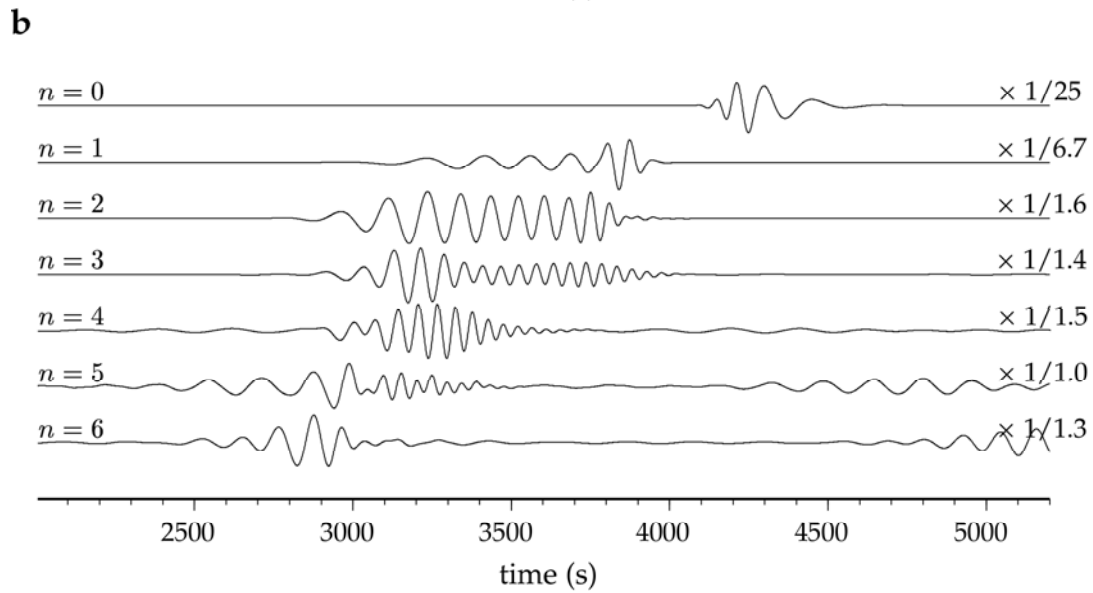
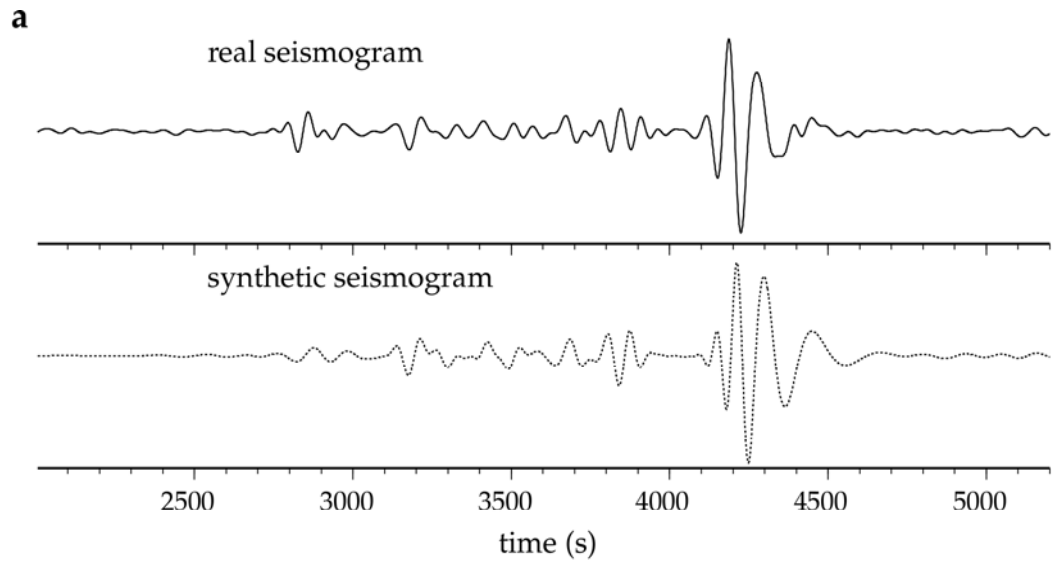
$$\mathbf{d}_0 = \mathbf{g}(\mathbf{p}_0)$$

- Kernels $\partial\mathbf{g}/\partial\mathbf{p}$
- Cd function (or matrix) of covariance of data

- **Inverse Problem:** $\mathbf{p}-\mathbf{p}_0 = \mathbf{g}^{-1}(\mathbf{d}-\mathbf{d}_0)$

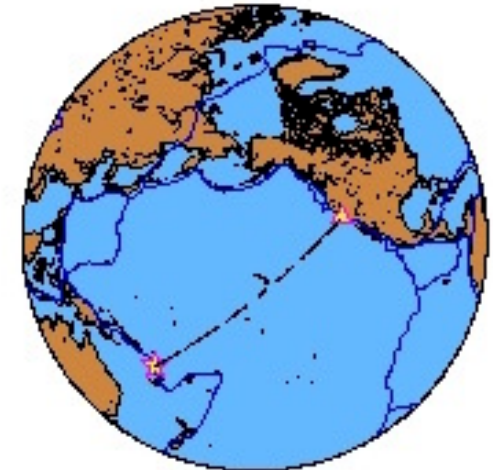
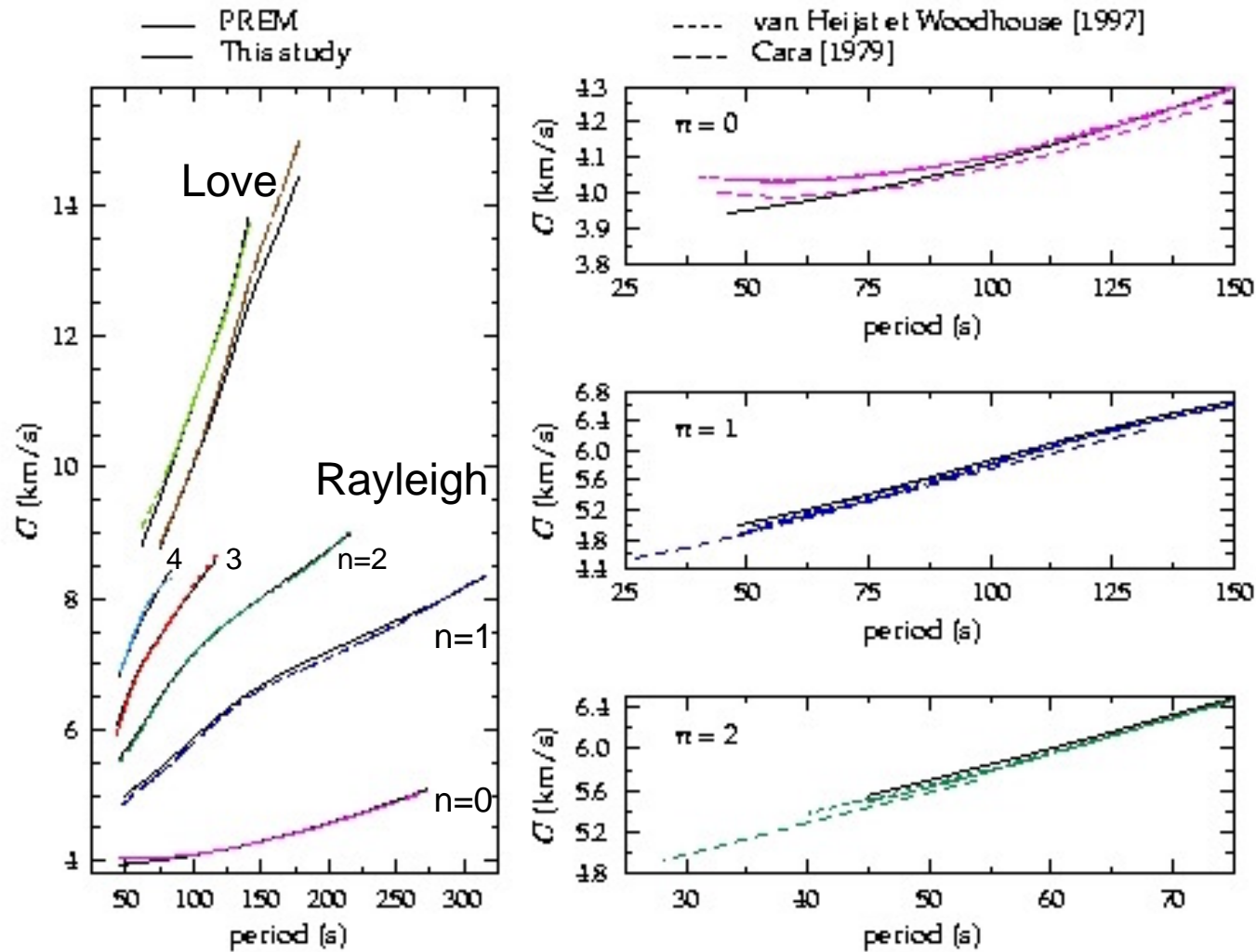
- C_{p0} a priori Covariance function of parameters
- C_{pf} a posteriori Covariance function of parameters
- R Resolution

Example of seismogram



Beucler, 2003

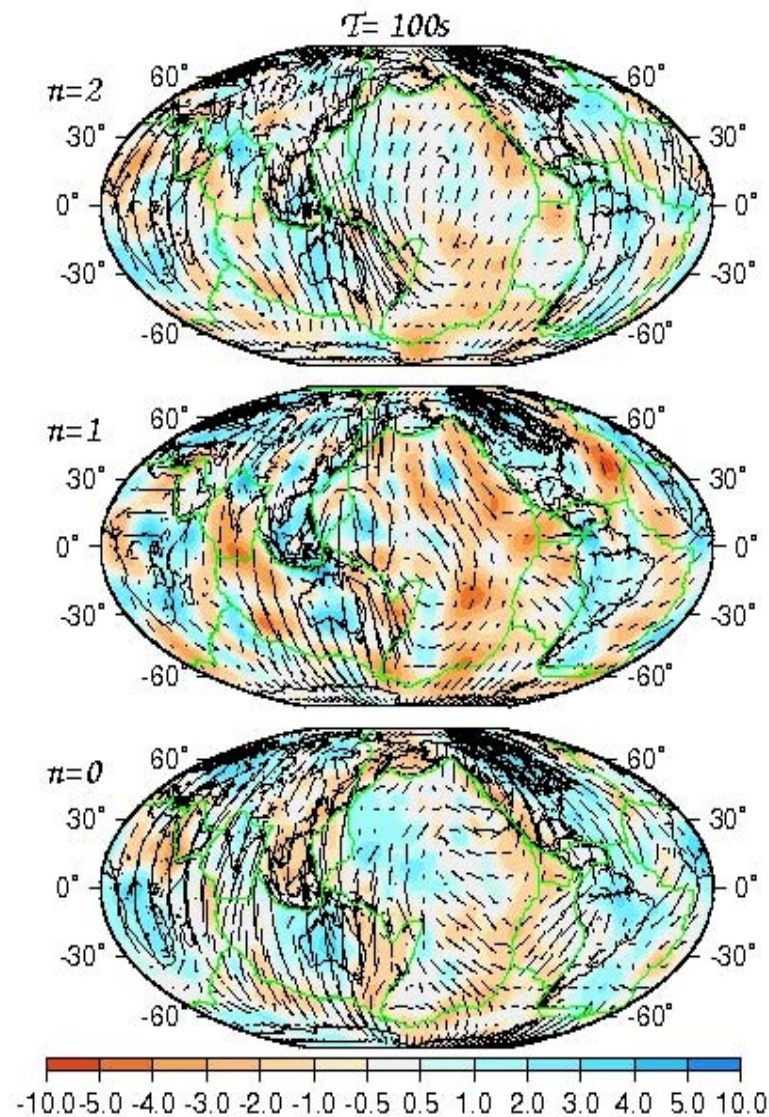
1st step: Calculation of dispersion curves: Fundamental modes and higher modes $c_n^R(T)$, $c_n^L(T)$ (Beucier et al., 2003)



Comparison with previous results along the Vanuatu-California path.

2nd step: Regionalization

Phase velocity maps
At 100s



2nd overtone

1st overtone

Fundamental mode

Beucler and Montagner, 2006

Global Tomography

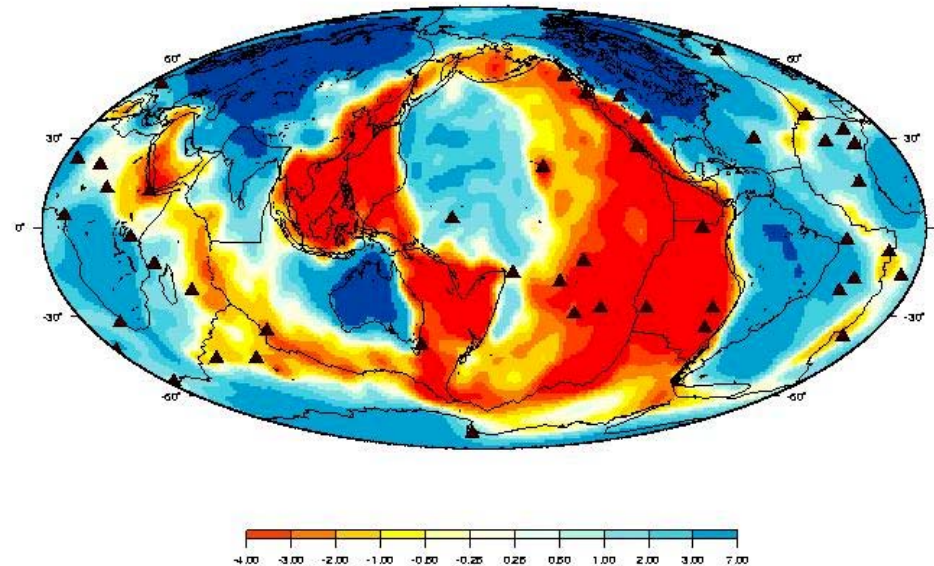
3rd step: inversion at depth

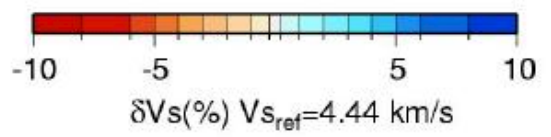
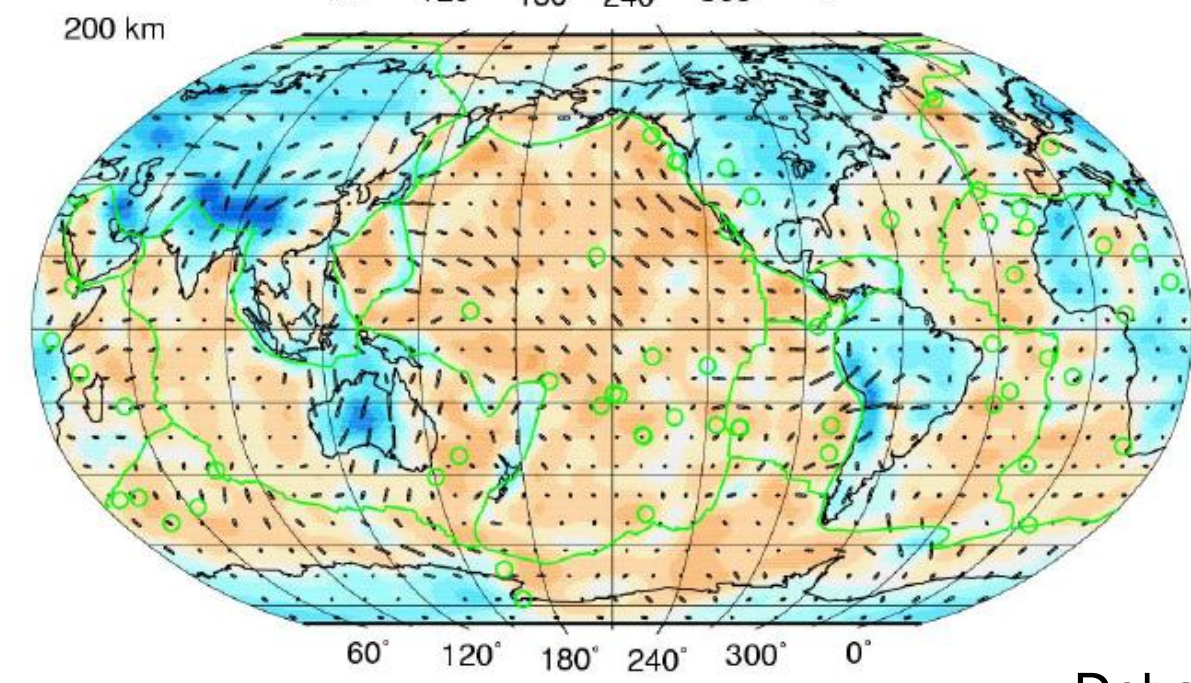
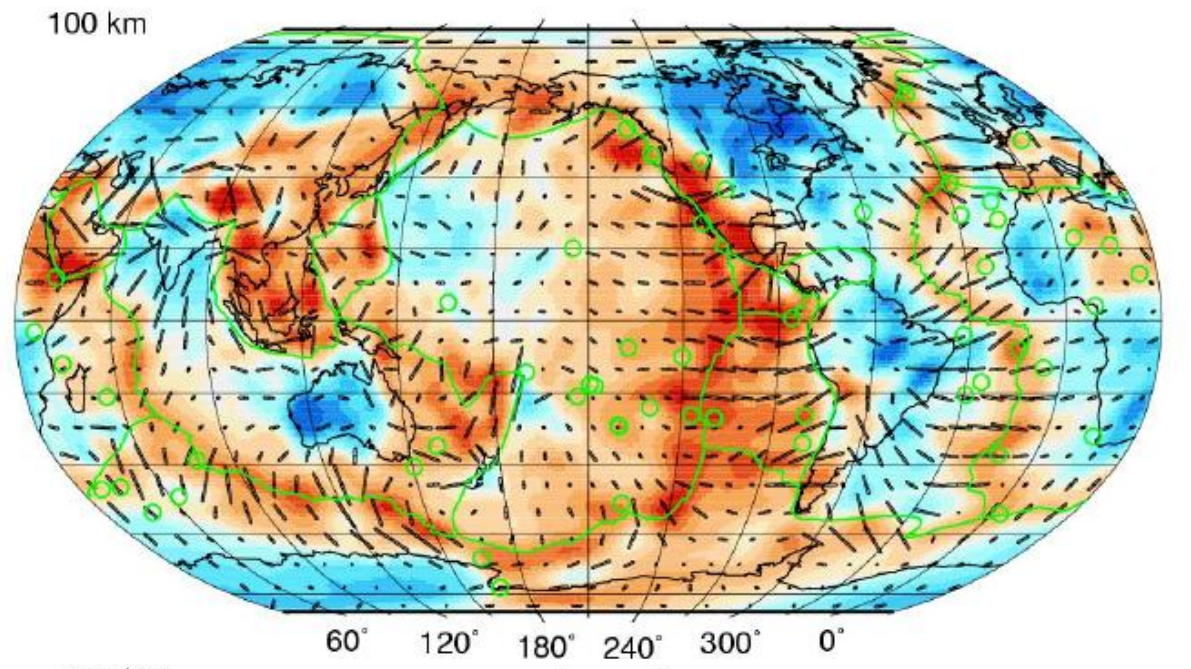
Scale $\Lambda \approx 2000\text{km}$ (degree 20)

Seismic wavelength $\lambda \leq 500\text{km}$

⇒ Ray theory applies

Shear wave velocities - depth = 100km





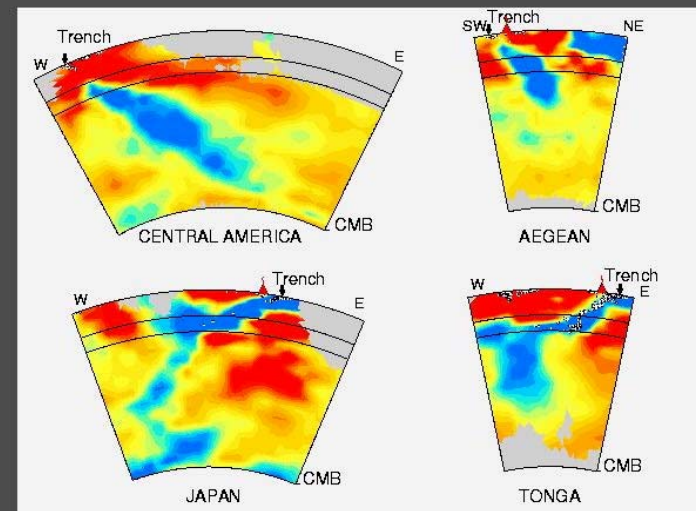
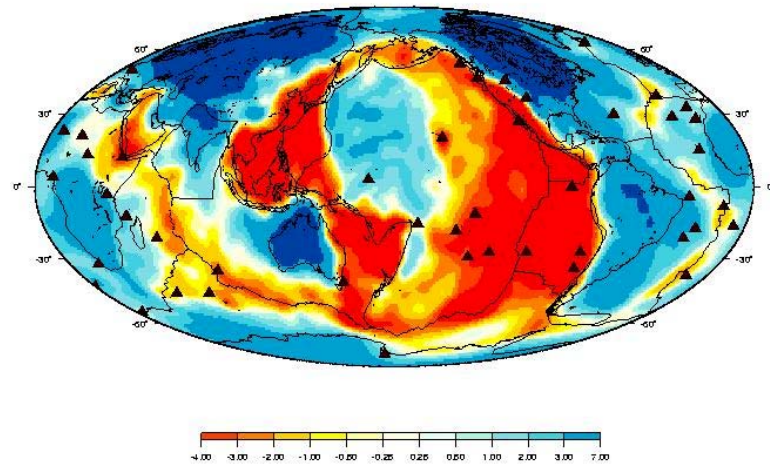
Debayle et al., 2005

CAN WE NEGLECT SMALL-SCALE HETEROGENEITIES?

From Global scale
Scale $\Lambda > 1000\text{km}$
Seismic wavelength

to Regional scale
 $\Lambda \approx 100\text{km}$
 $20\text{km} \leq \lambda \leq 500\text{km}$

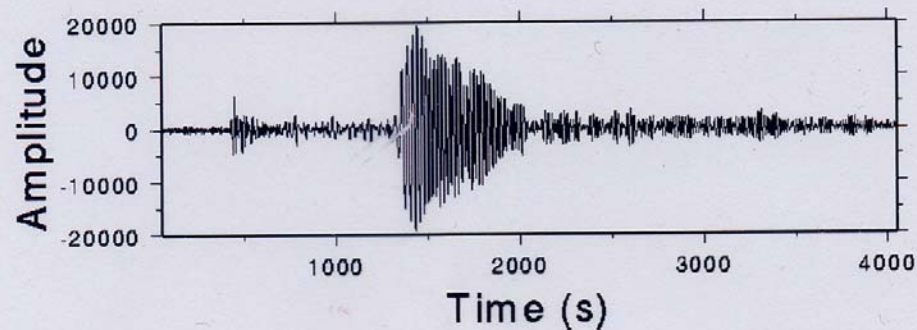
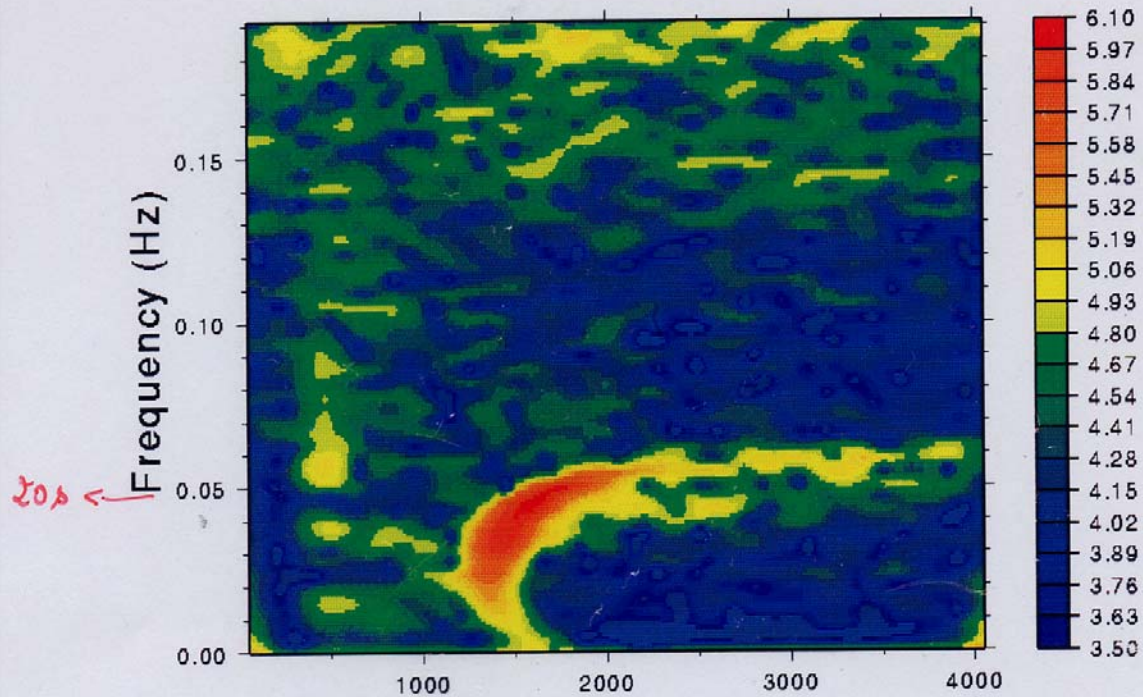
S-wave velocity -
depth = 100km



Van der Hilst et al., 1998

Spectrogram at station PPT (Z component, distance=82 degrees)

Aleutians 1992/03/02 depth=39km m s=6.8



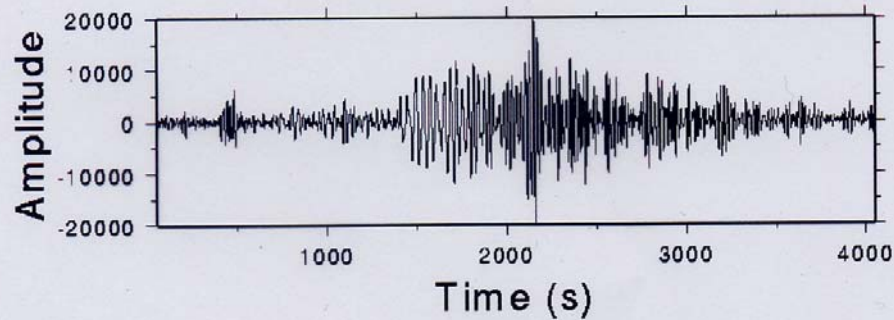
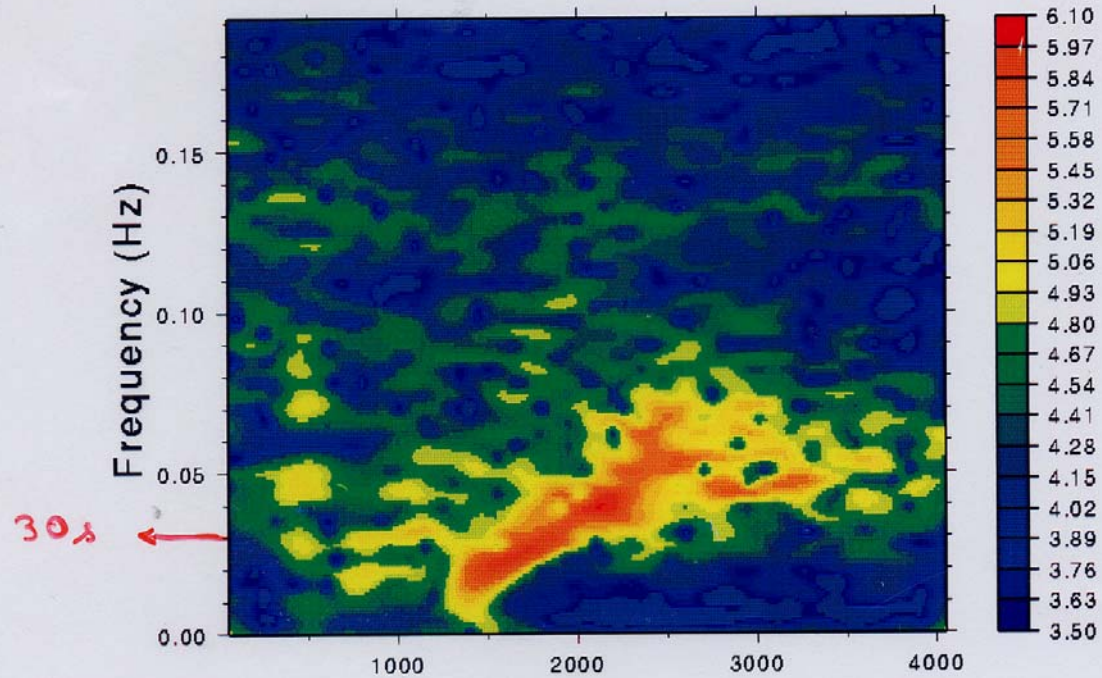
Oceanic
Path

simple
dispersion
Curve

Multiple scattering
For $T < 30s$

Spectrogram at station SSB (Z component, distance=80 degrees)

Aleutians 1992/03/02 depth=39km ms=6.8

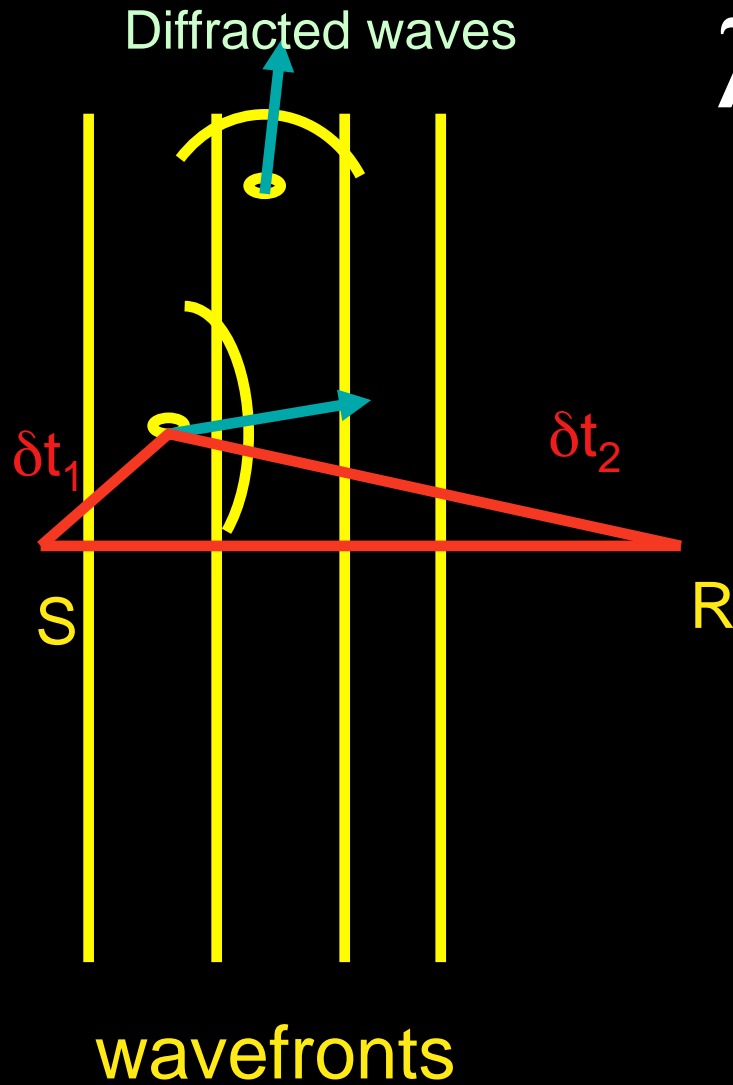


Continental
Path

complex
dispersion
Curve
Multiple scattering
For $T < 60s$

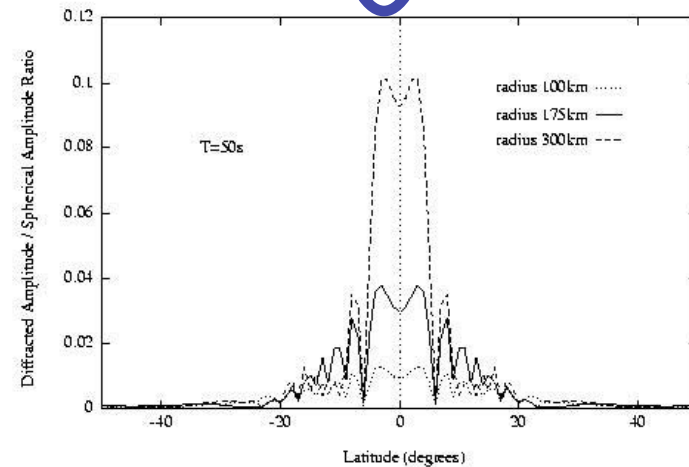
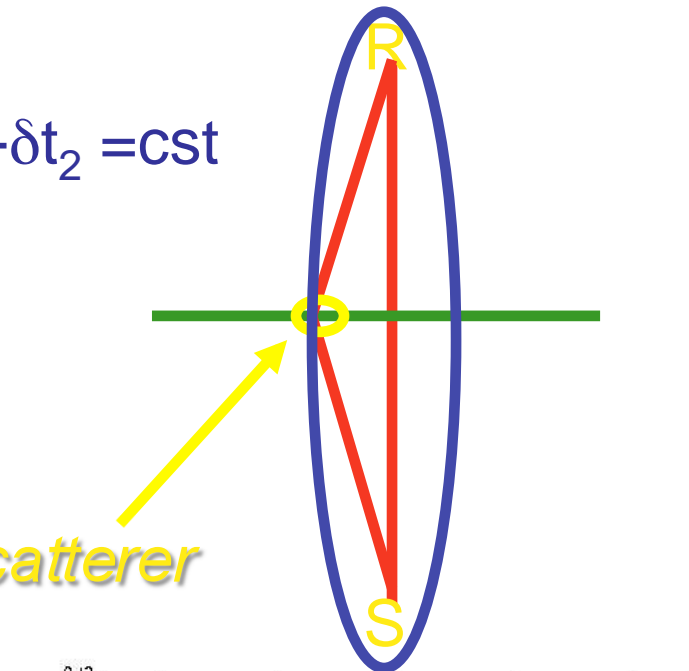
Λ heterogeneity scale, λ wavelength

$$\lambda \sim \Lambda \text{ or } \lambda \gg \Lambda$$



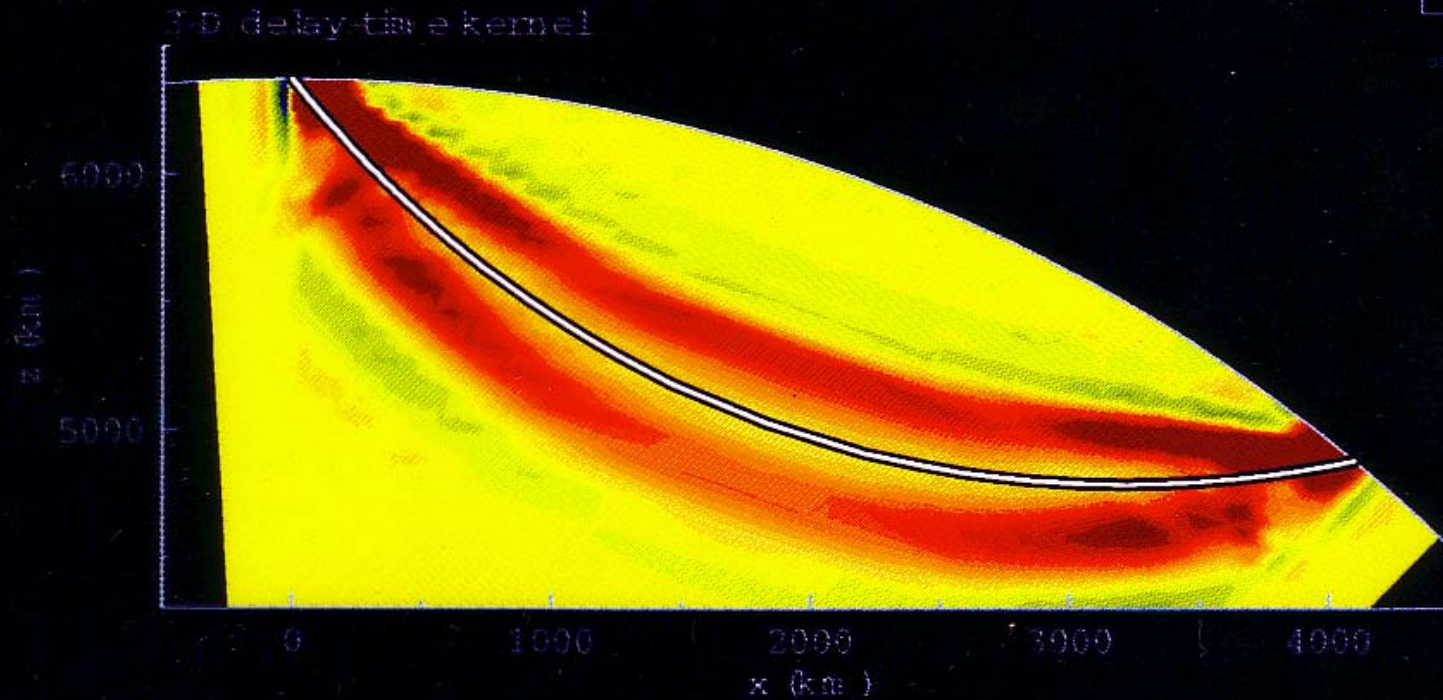
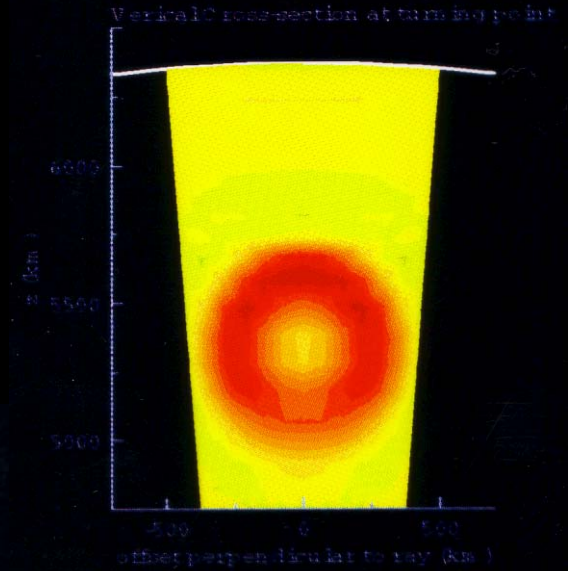
$$\delta t_1 + \delta t_2 = cst$$

scatterer

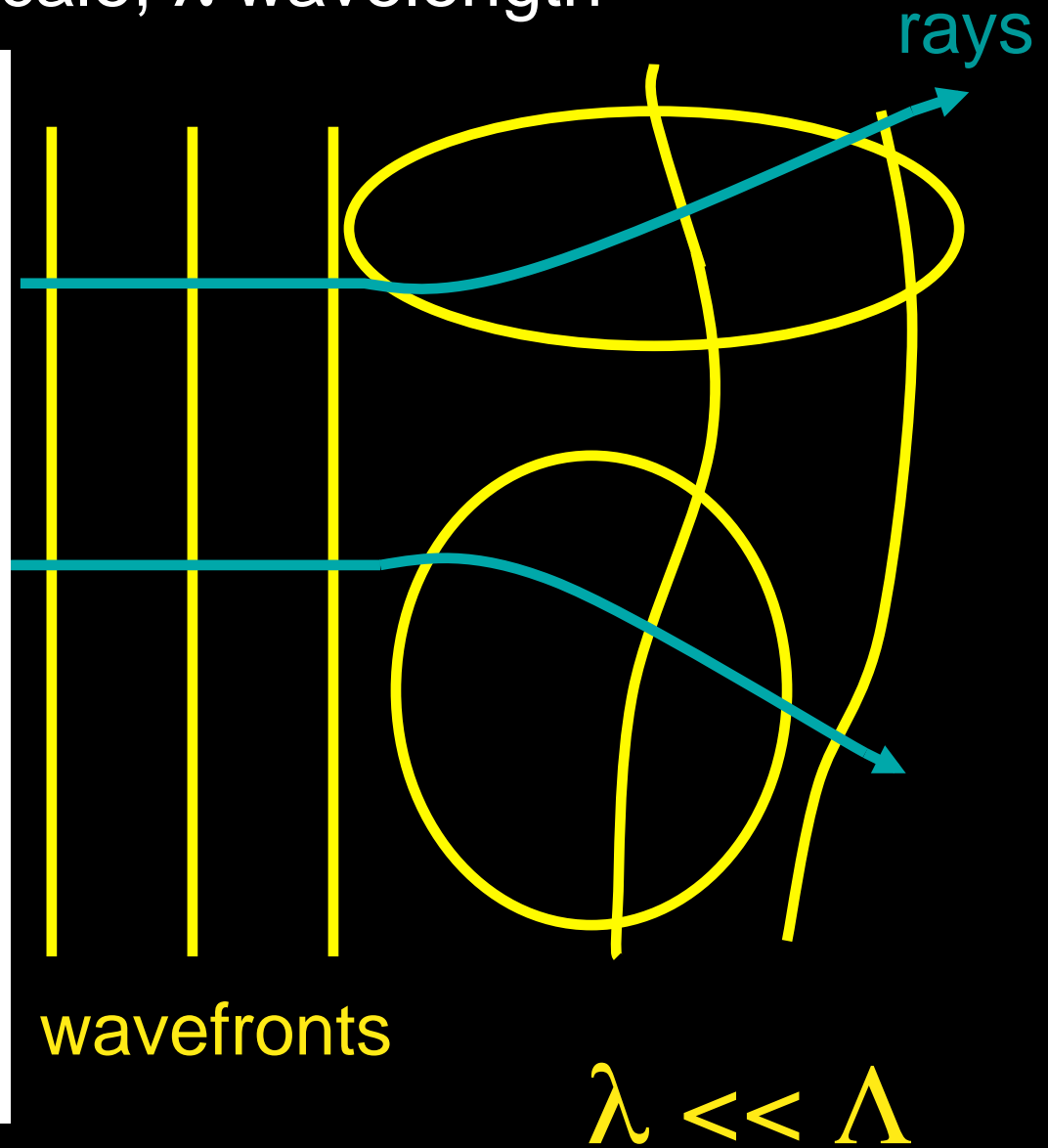
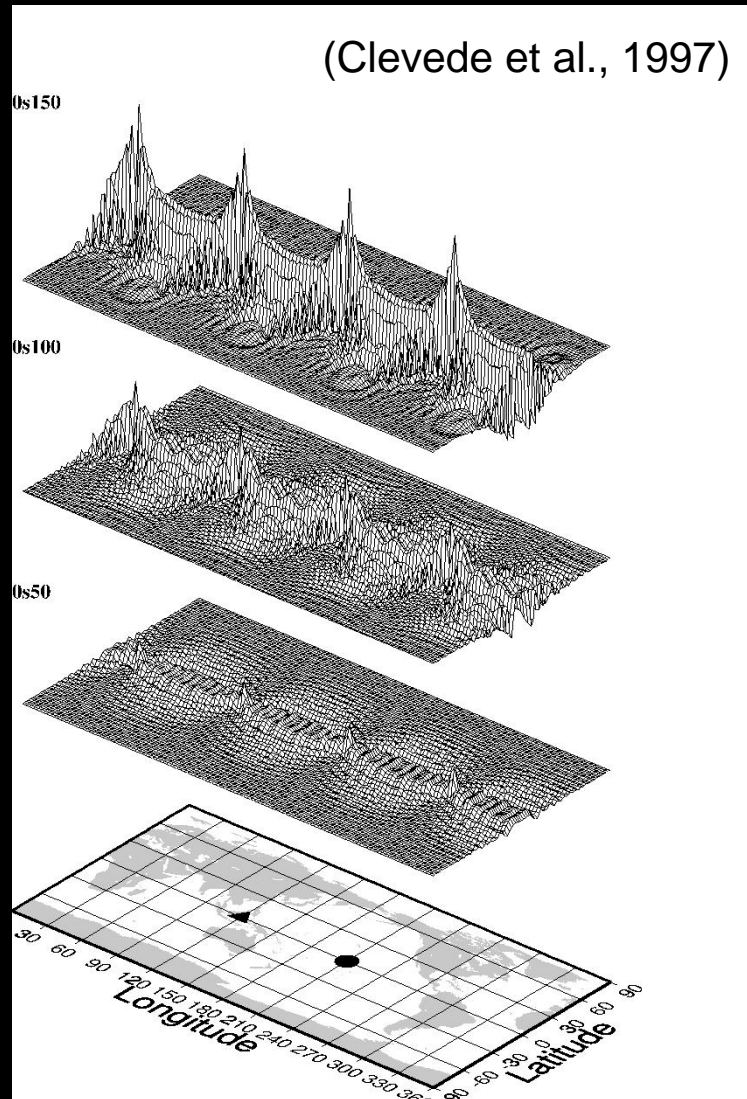


Sensitivity of the delay time to the local seismic velocity

→ Princeton Group (G. Nolet)



Λ heterogeneity scale, λ wavelength

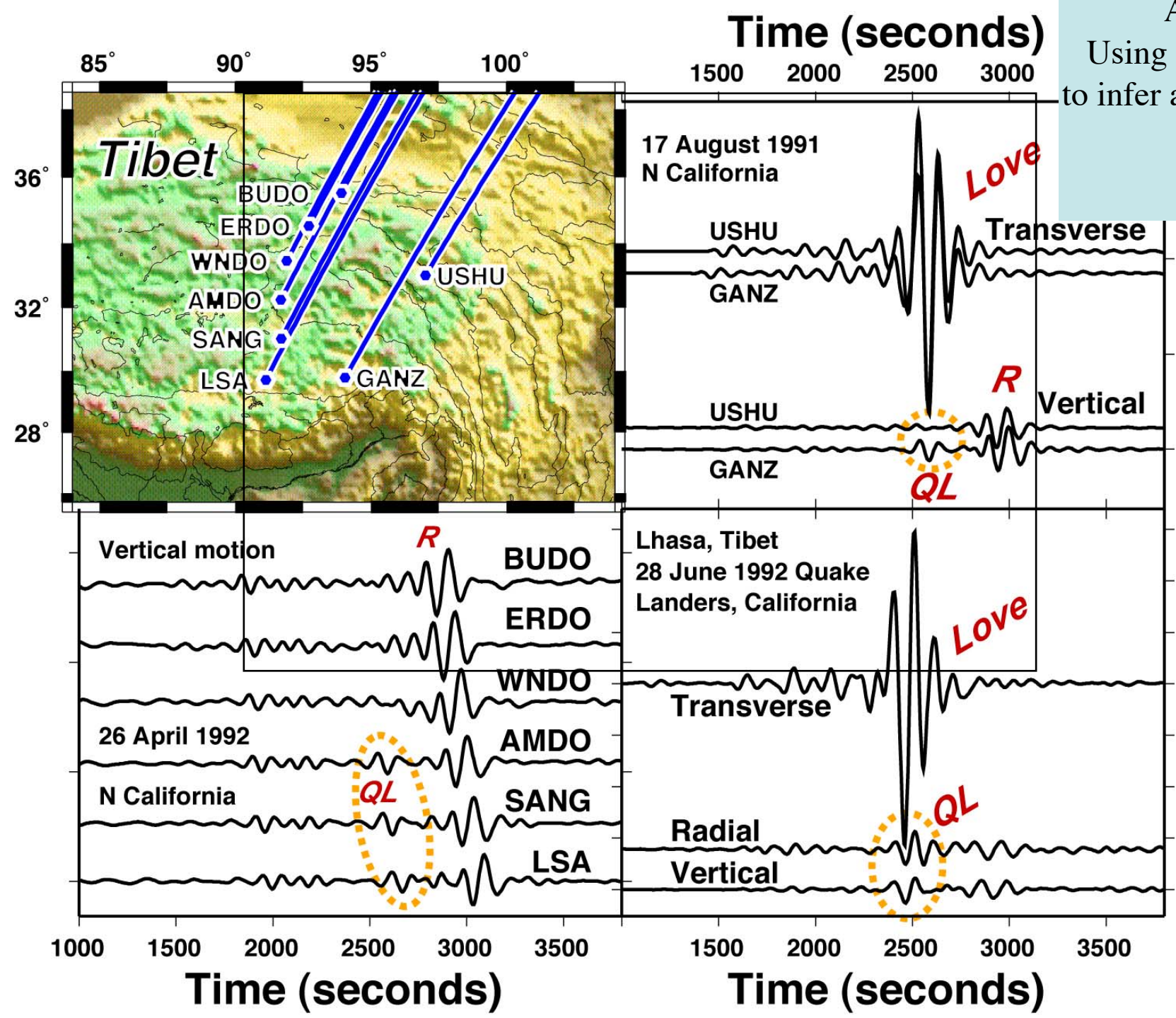


Typical scales $\Lambda \approx 2,000\text{km}$, $\lambda \approx 500\text{km}$

Effects on amplitude?

- Surface wave tomography of mantle anisotropy is based on ray theory
- Finite frequency tomography has been tested to improve the imaging of the isotropic mantle
- How do finite frequency surface waves "sense" anisotropy ?
- Computational tool : Adjoint Spectral Element Method (ASEM) (Tromp et al., 2005)

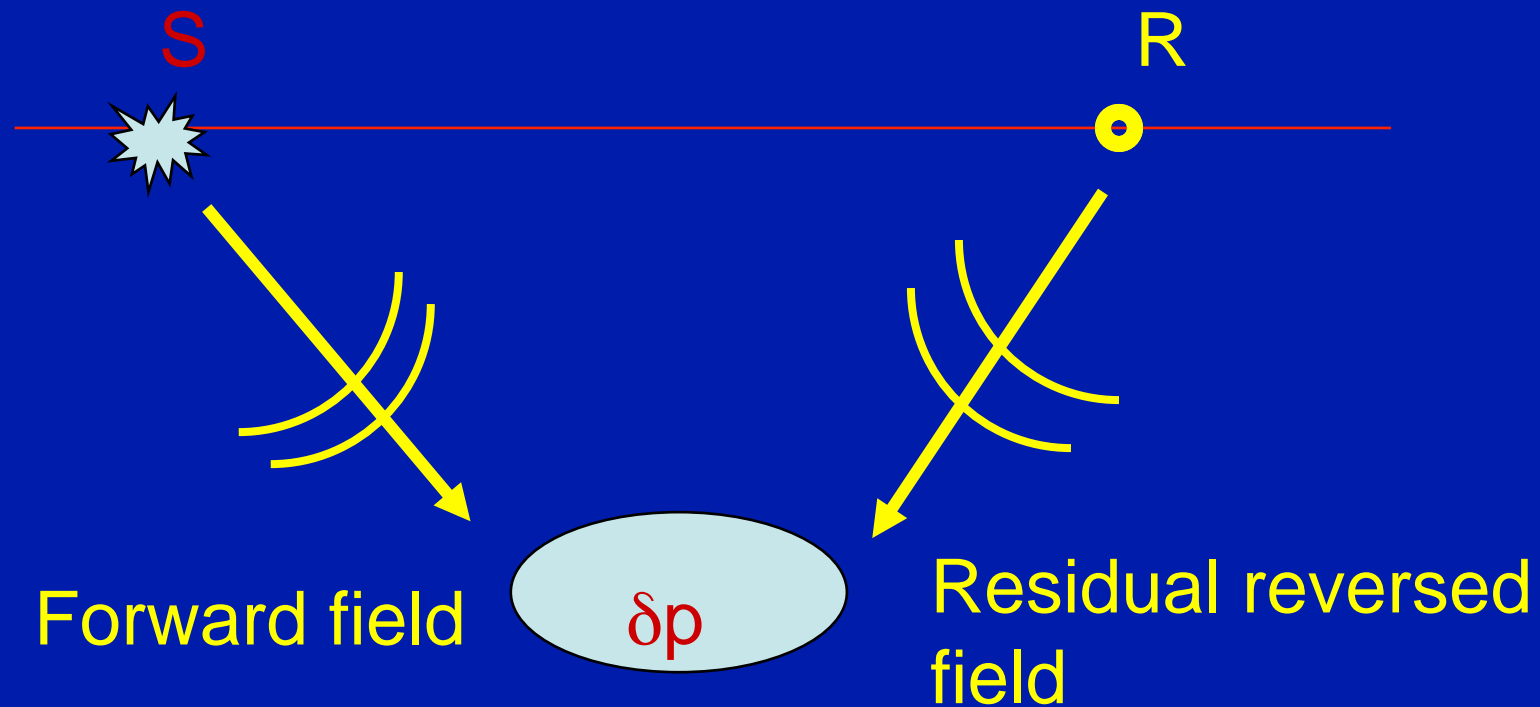
An Example of
Using Quasi-Love waves
to infer anisotropic gradients
(Park, 2006)



Time Reversal- Adjoint Method

(Tarantola, 1984, Tromp et al., 2005):

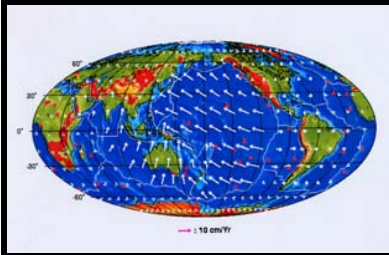
Adjoint \Rightarrow Fréchet Derivatives



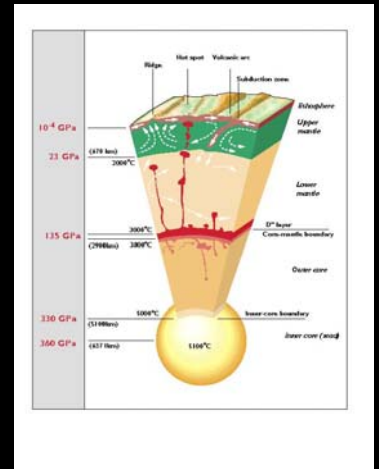
Overview

Large scale Seismology: an observational field

- Data (Seismic source) + Instrument (Seismometer)
-> Observations (seismograms)
- Historical evolution: Ray theory, Normal mode theory, Numerical techniques (SEM, NM-SEM)
- Scientific Issues: earthquakes (Sumatra-Andaman earthquake), Anisotropic structure of the Earth
- Tomographic technique
- **Geodynamic Applications:**
Continental deformation
Seismic Experiment: Plume detection

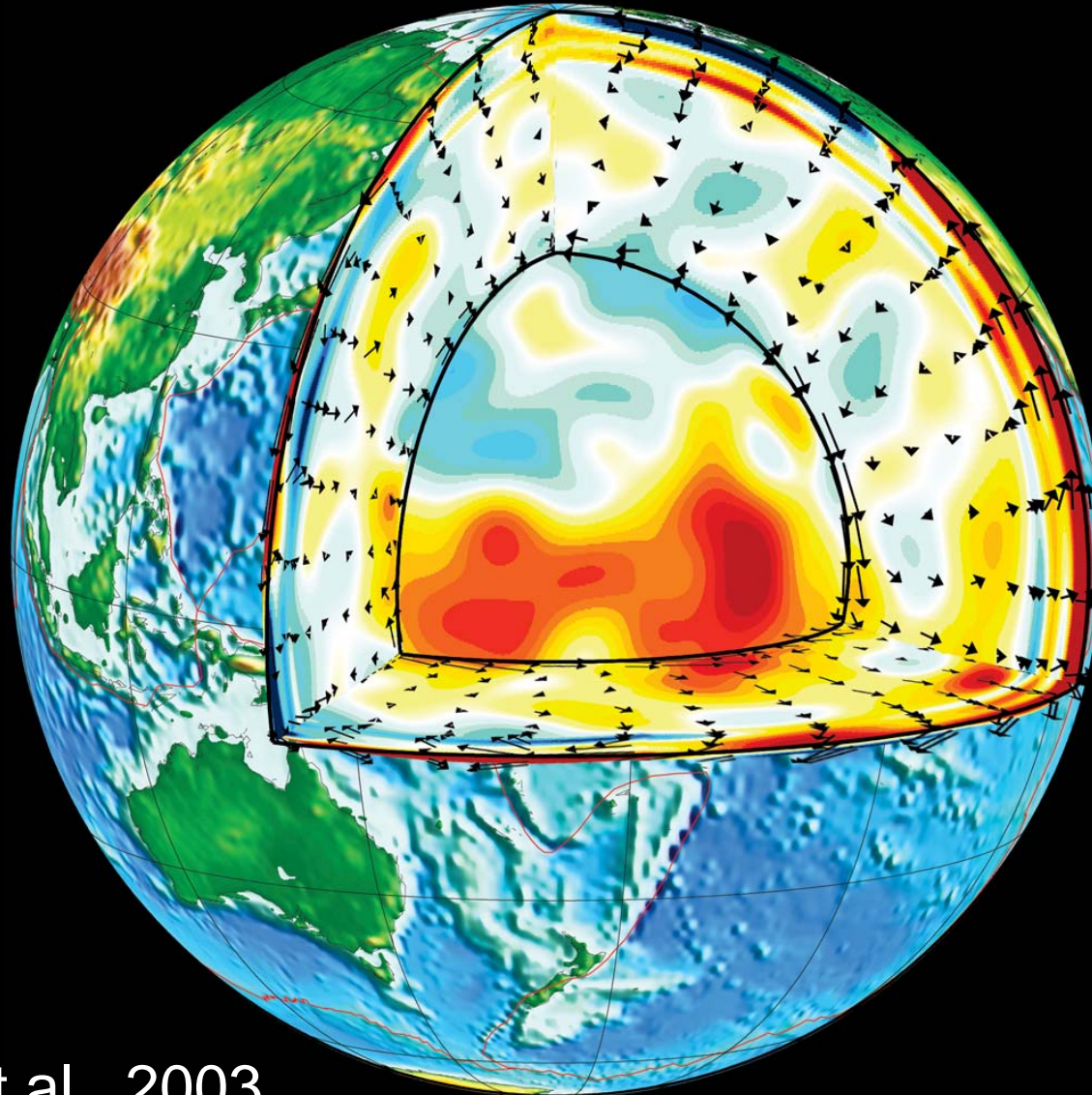


Anisotropy and Geodynamic processes



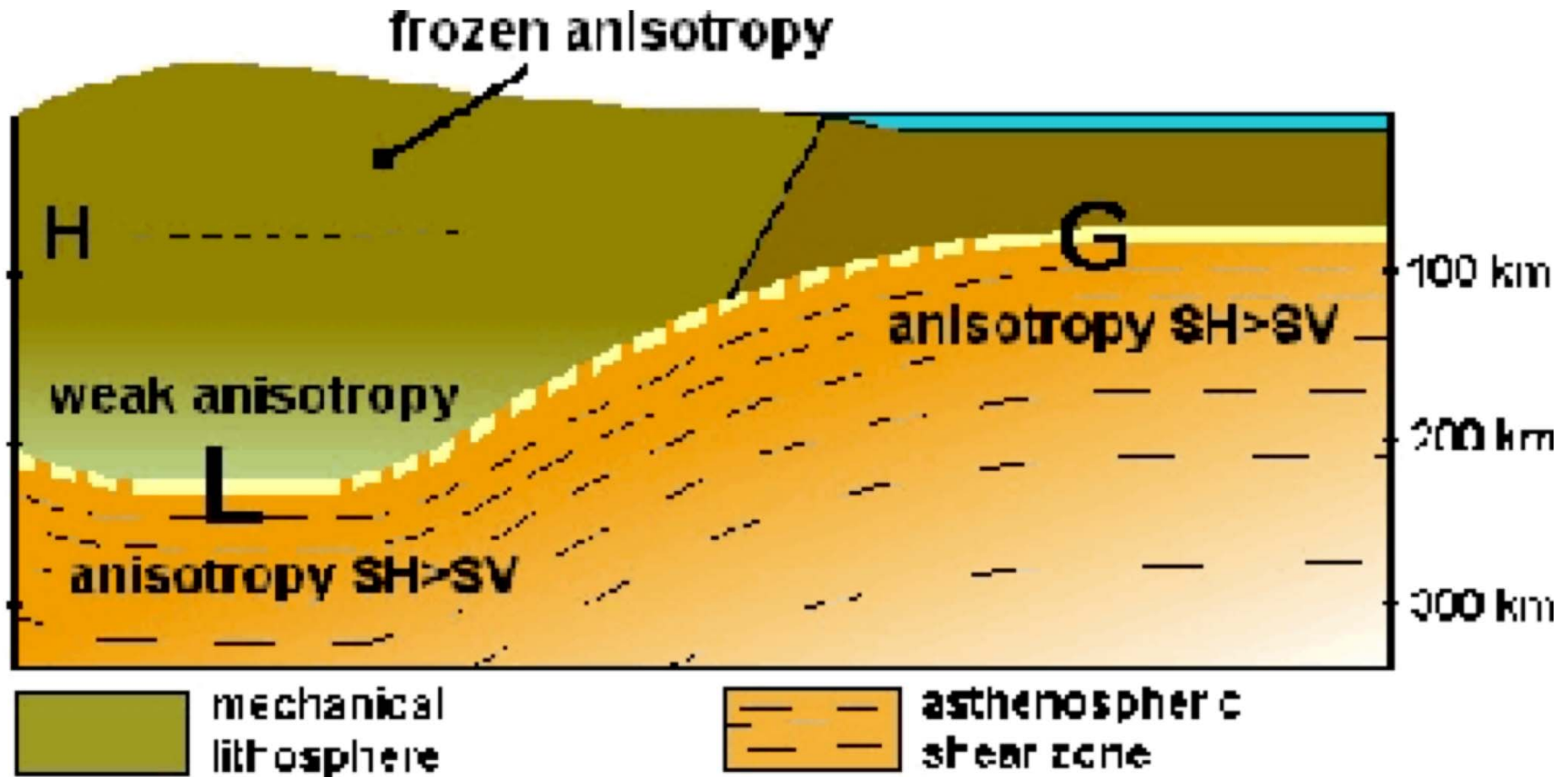
- Mapping of mantle convection (global scale) (Montagner & Tanimoto, 1991; Ekström, 2001; Debayle et al., 2005)
- **Collision India-Asia (Griot et al., 1998;)**
- Lithosphere roots (continents- oceans)
- Plume Detection- interaction lithosphere- asthenosphere
- Deformation Processes -> Fluid Mechanics (Gaboret et al., 2003; Becker et al., 2003, 2007...)

Seismic tomography: Instantaneous image Anisotropy- Geodynamics Relationship



Gaboret et al., 2003

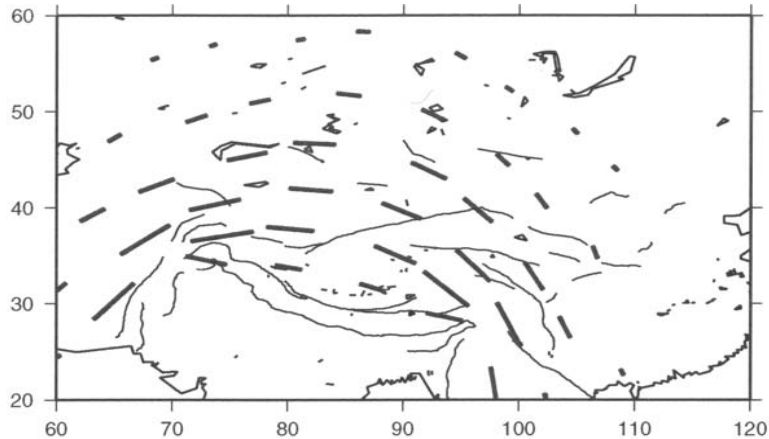
Difference Continent -Ocean



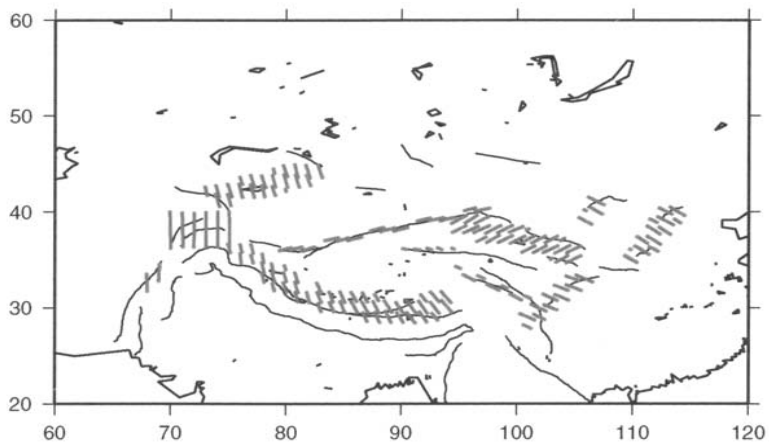
Gung & Romanowicz, (2003)

Central Asia: Heterogeneous versus homogeneous Deformation

Homogeneous Model



Heterogeneous Model

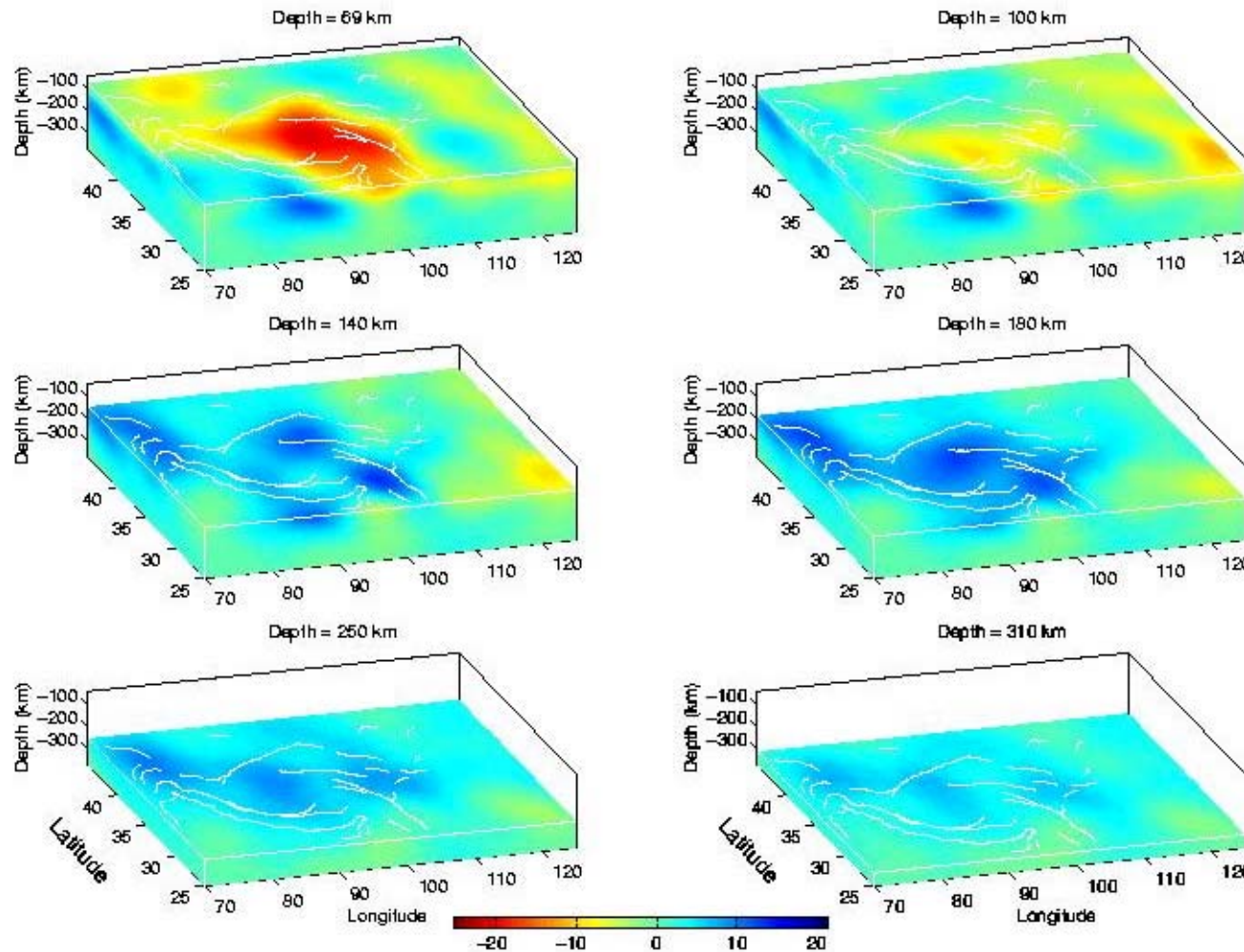
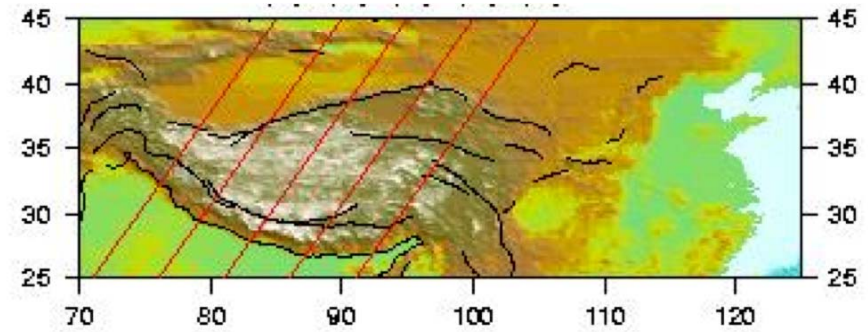


Problems:

- Direction of maximum extension?
- Fossil anisotropy
- Spatial filtering

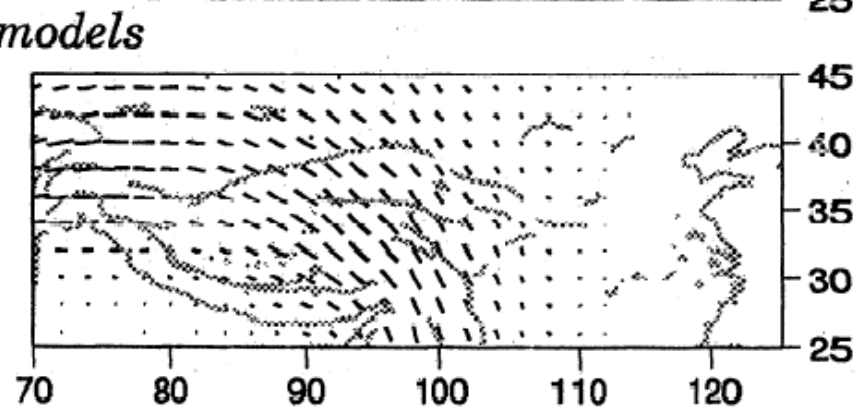
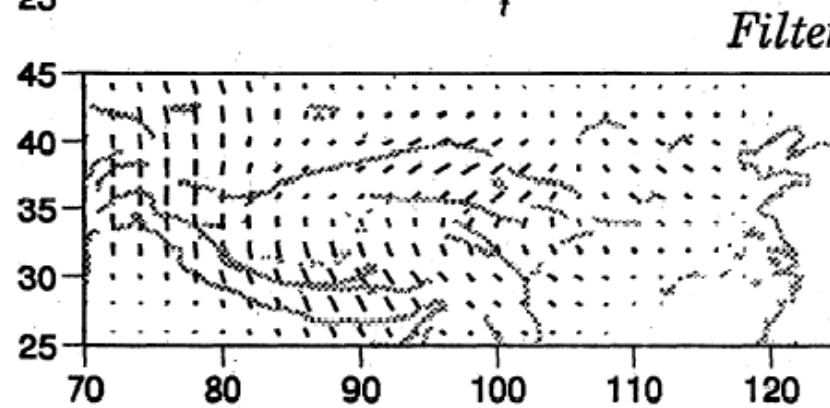
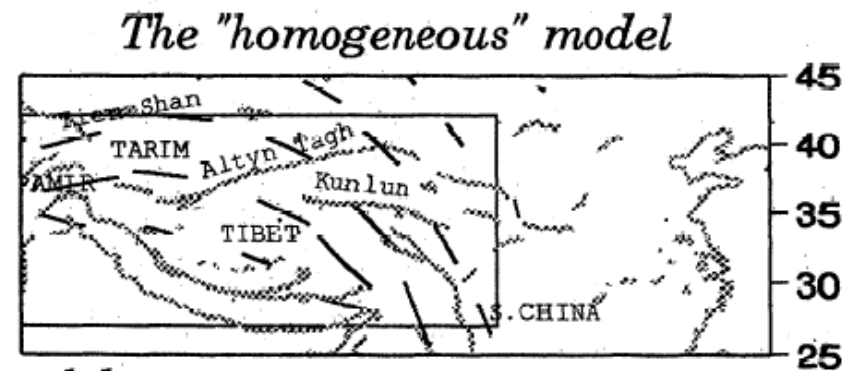
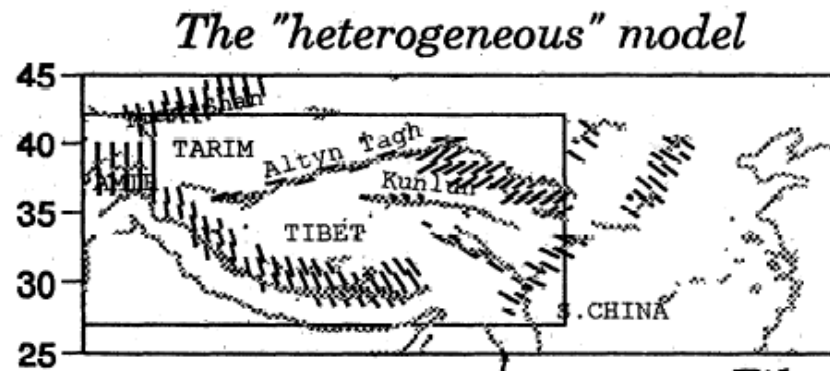
Griot et al., 1998

Heterogeneous versus Homogeneous Deformation

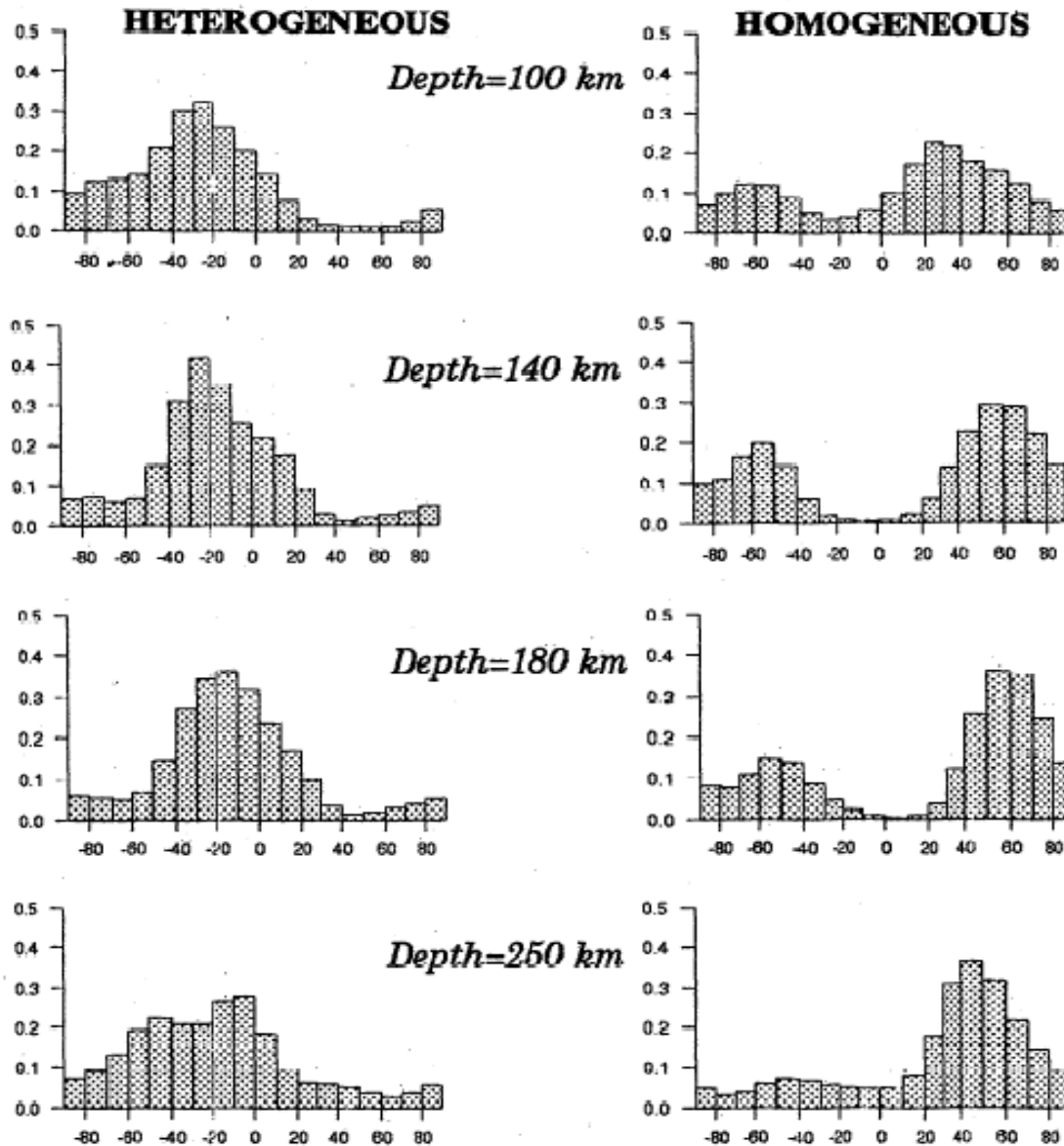


Griot et al., 1998

Heterogeneous vs homogeneous Deformation 2 competing models



Heterogeneous versus homogeneous Deformation



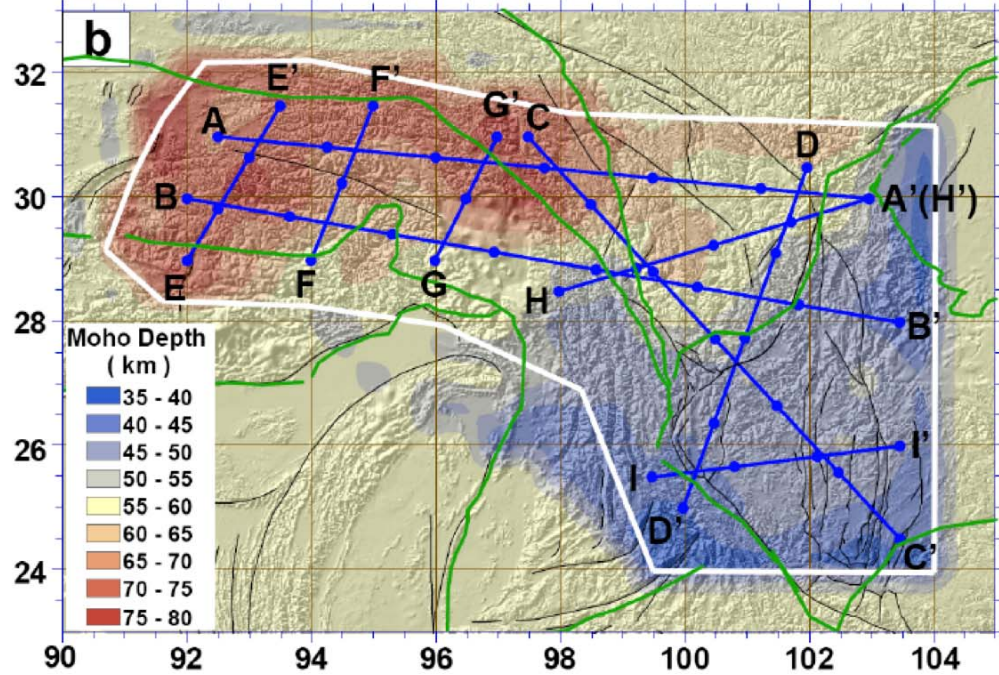
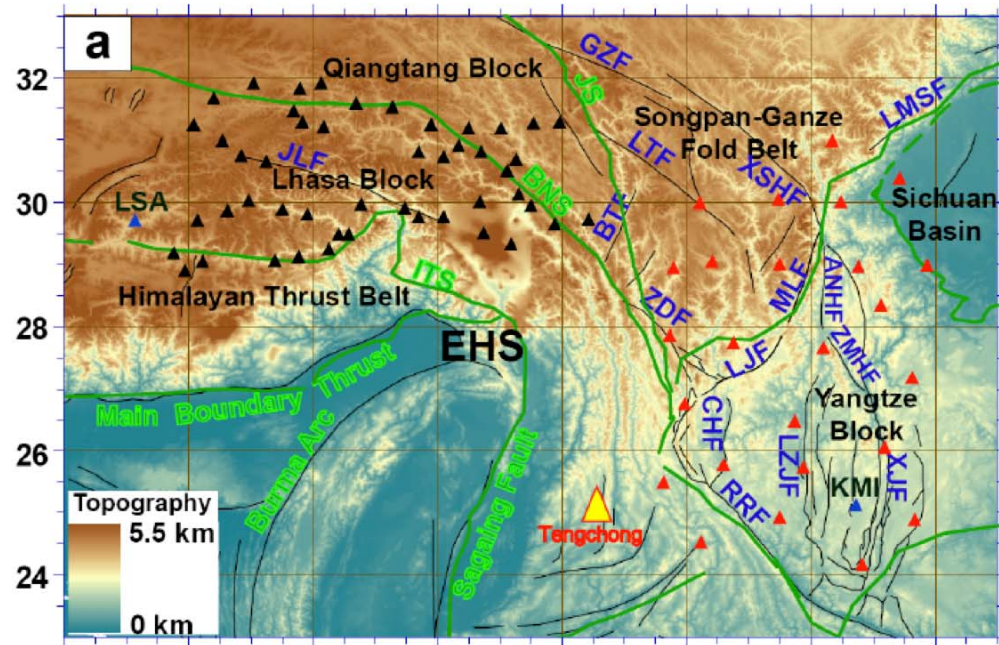
- Continental Root
around 200km

- Comparison with
SKS

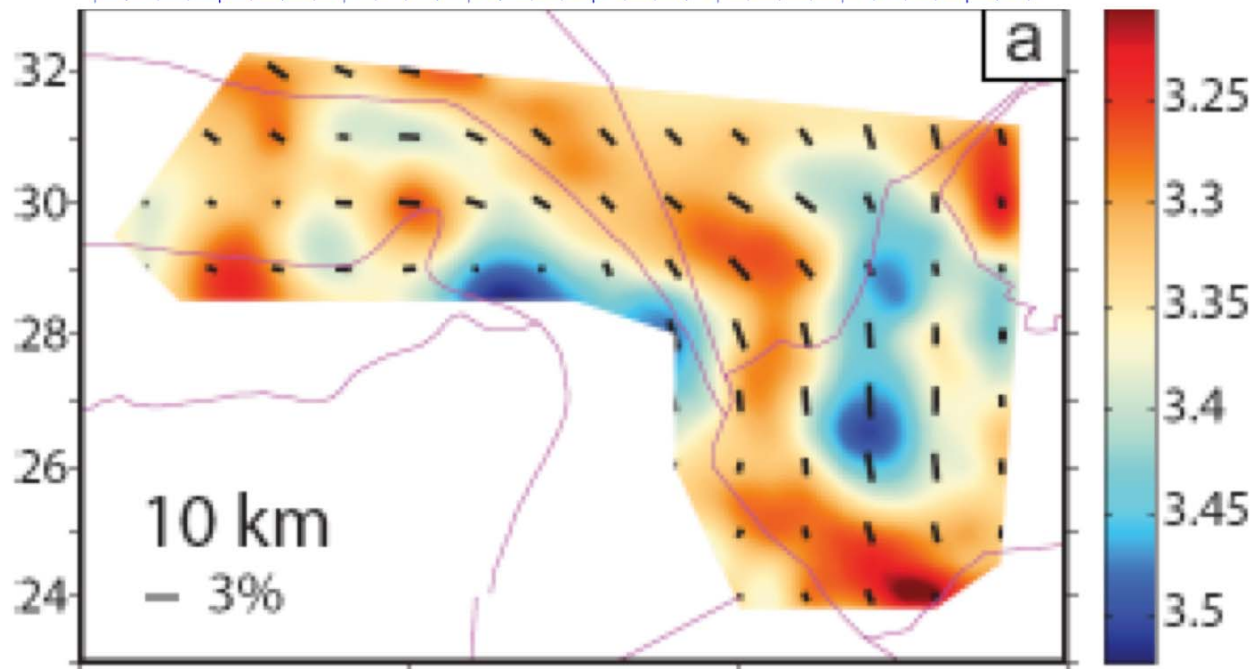
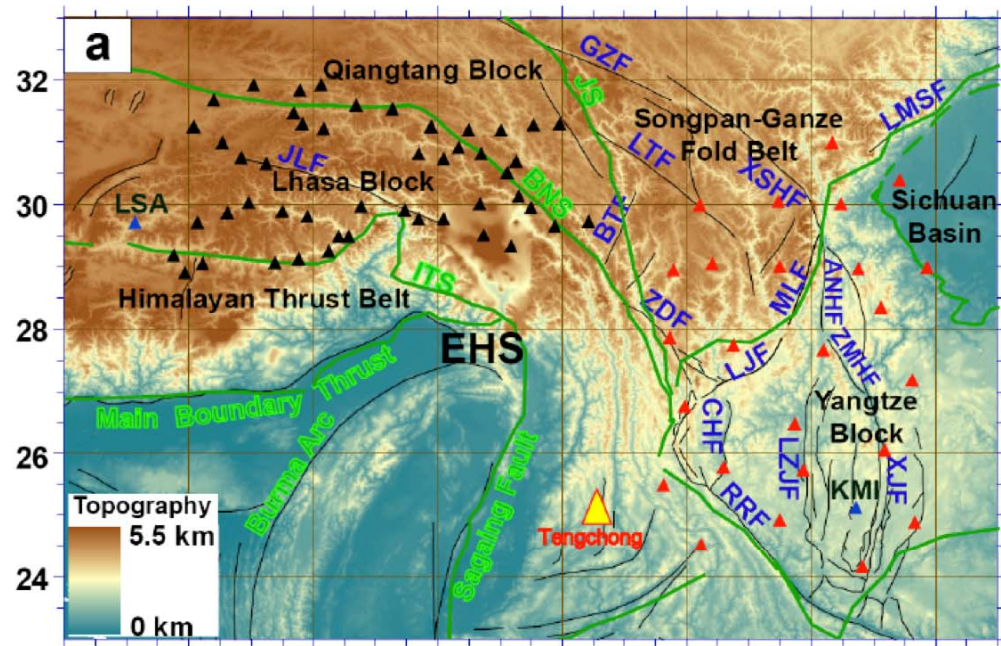
(Montagner et al., 2000)

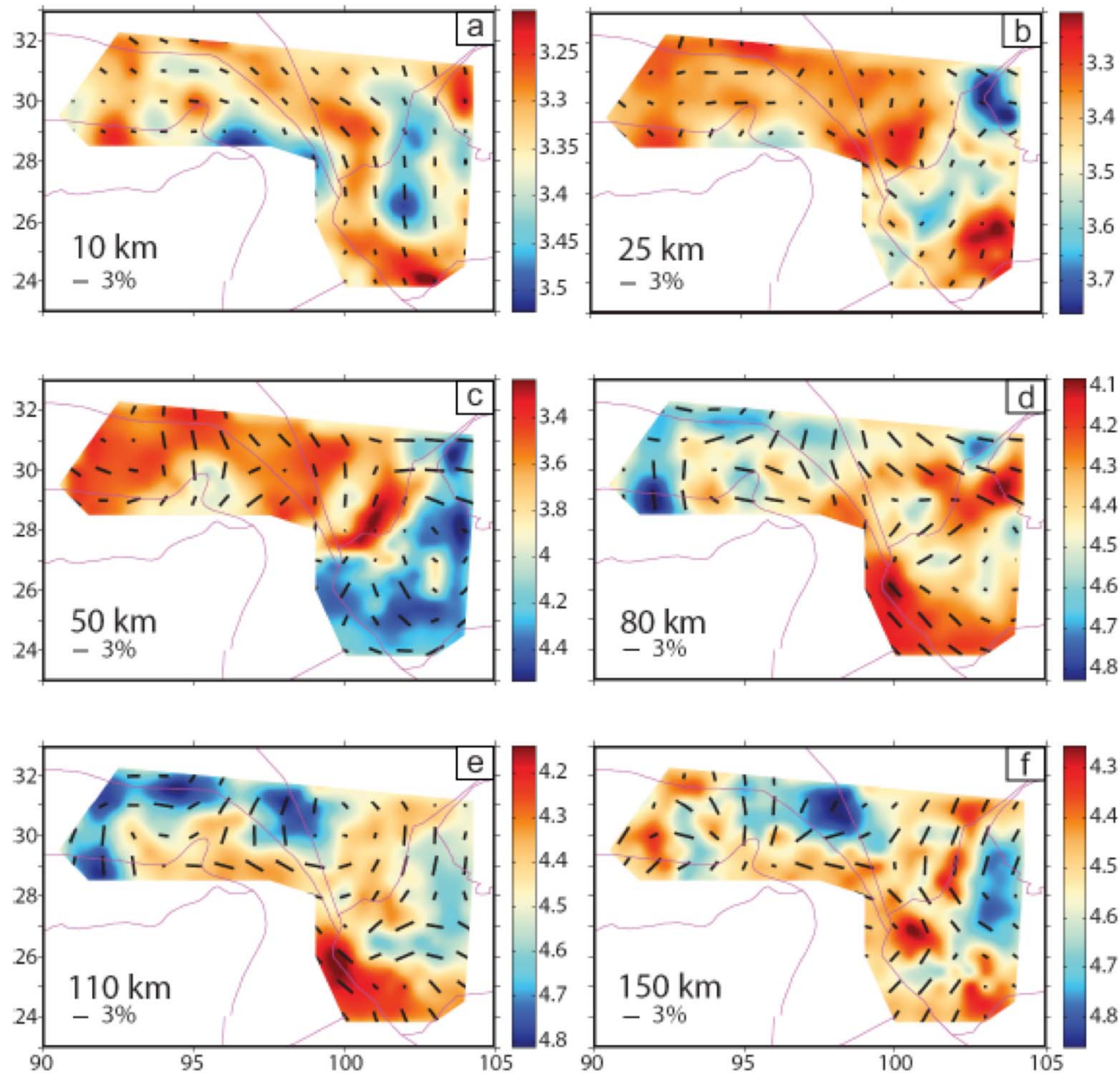
- Stratification of
anisotropy

(Different orientation below
200km)

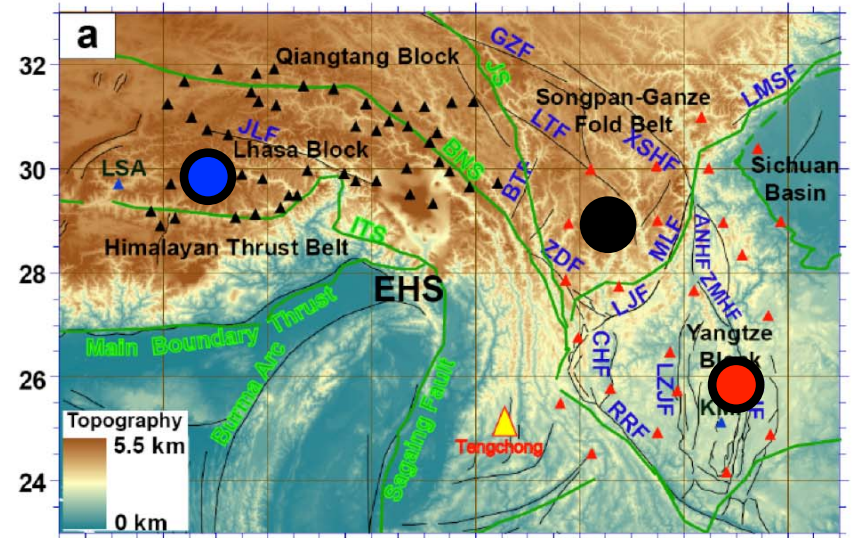
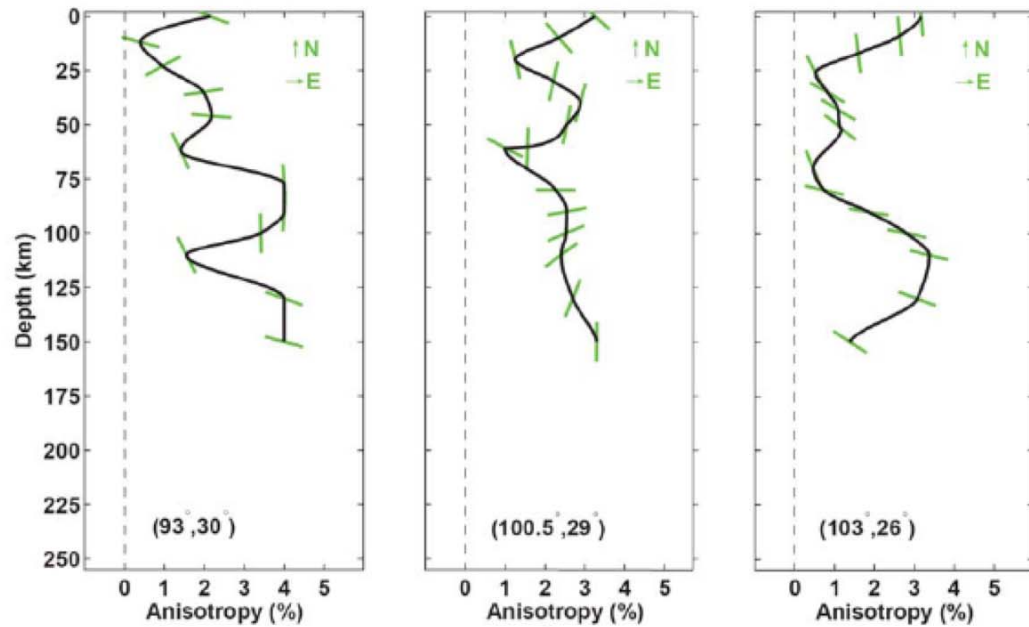
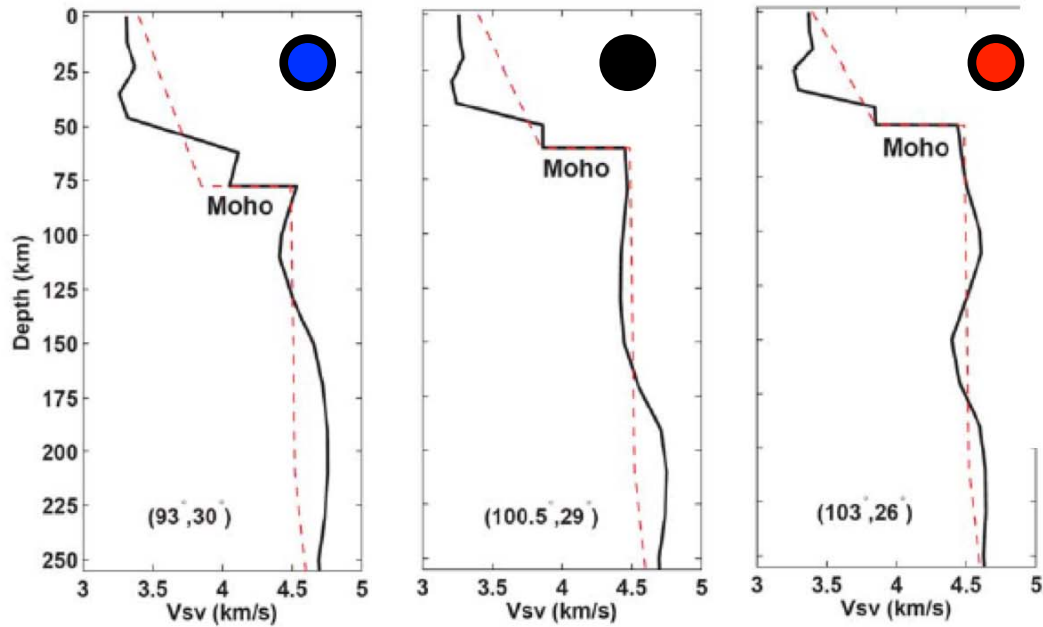


Yao, van der Hilst, Montagner, 2010



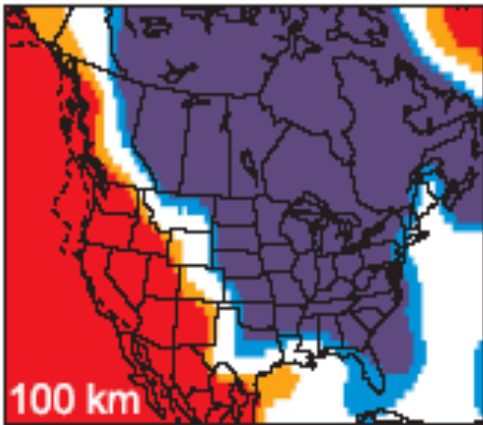


Heterogeneity and Anisotropy of SE Tibet

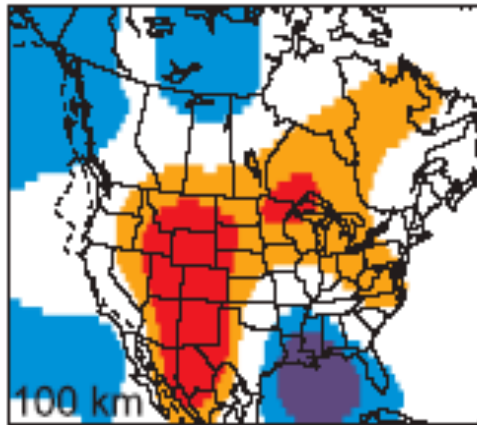


- Several anisotropic layers
- Crustal flow?
- Coupling Crust-Lithosphere?

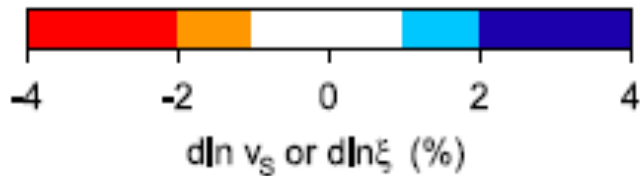
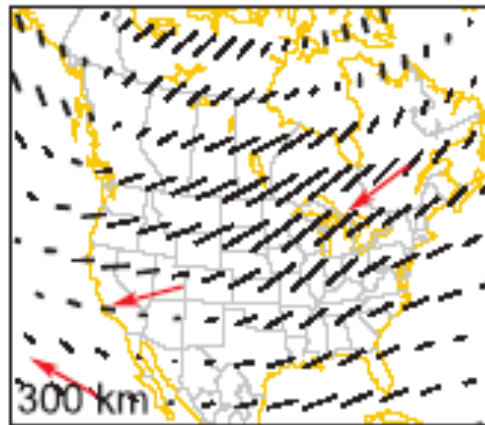
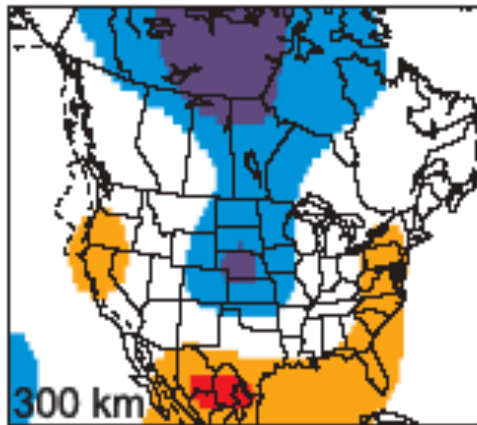
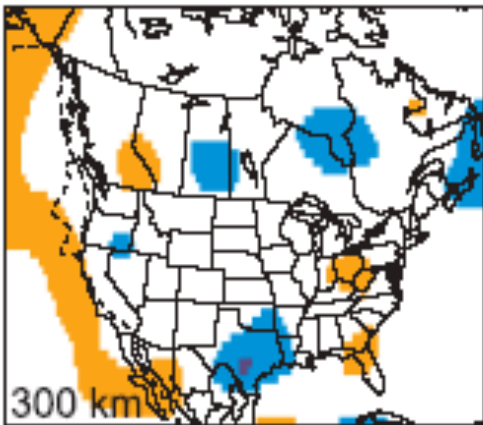
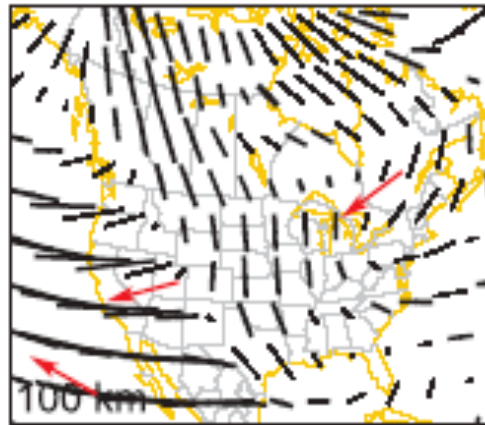
Isotropic S-velocity



Radial Anisotropy



Azimuthal Anisotropy



After Marone and Romanowicz (2007)

SKS splitting predictions compared to SKS splitting data

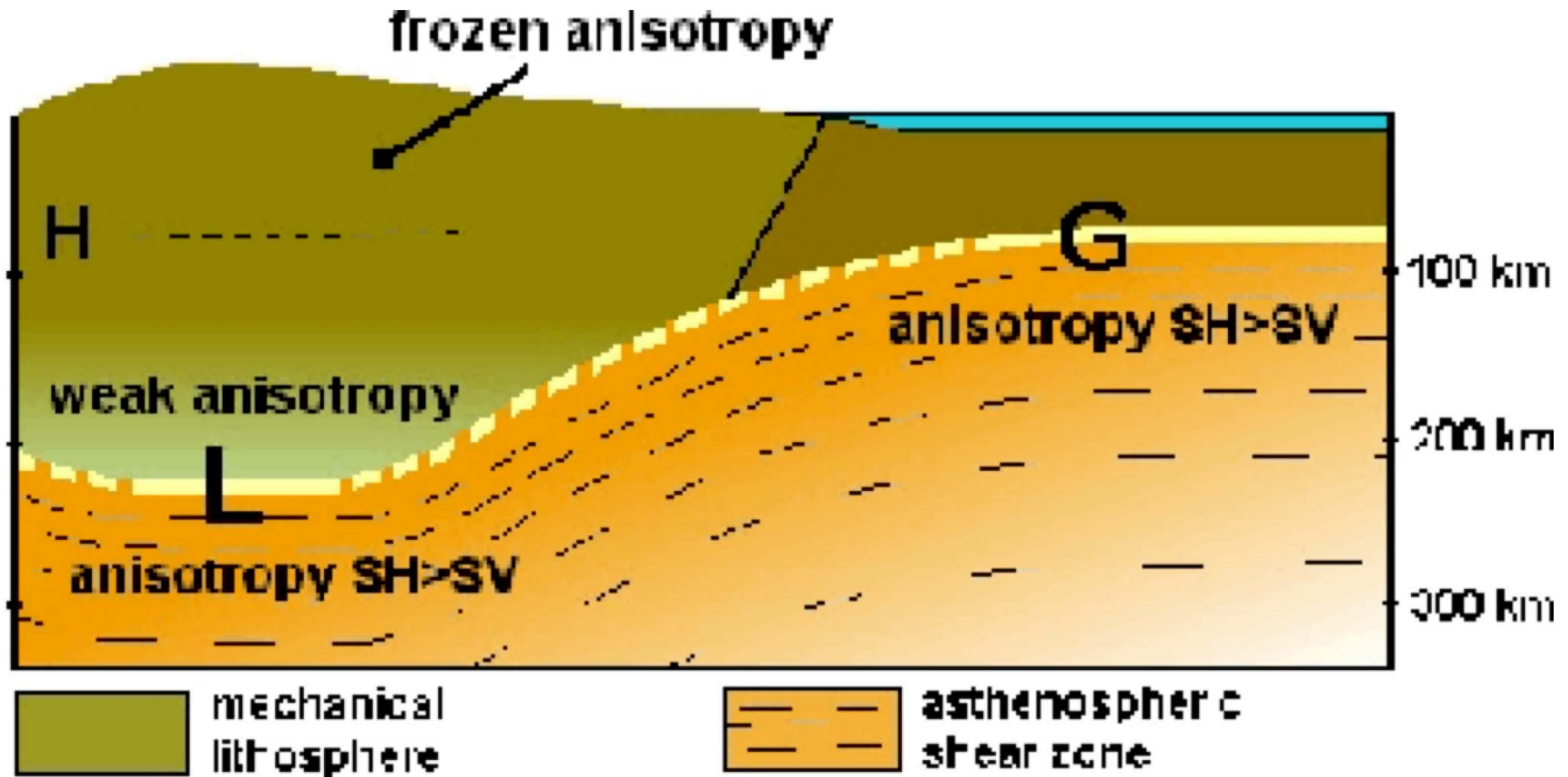
Model B



Delay time $\frac{1s}{2s}$ —
—

From: Marone and Romanowicz, Nature, 2007






Difference Continent - Ocean

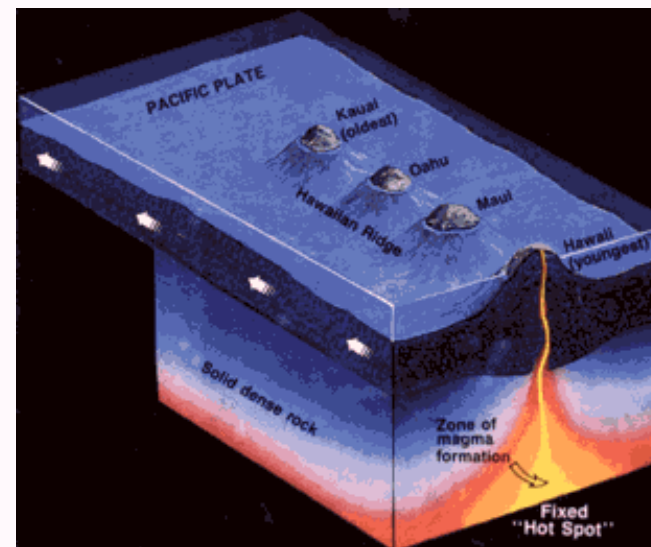
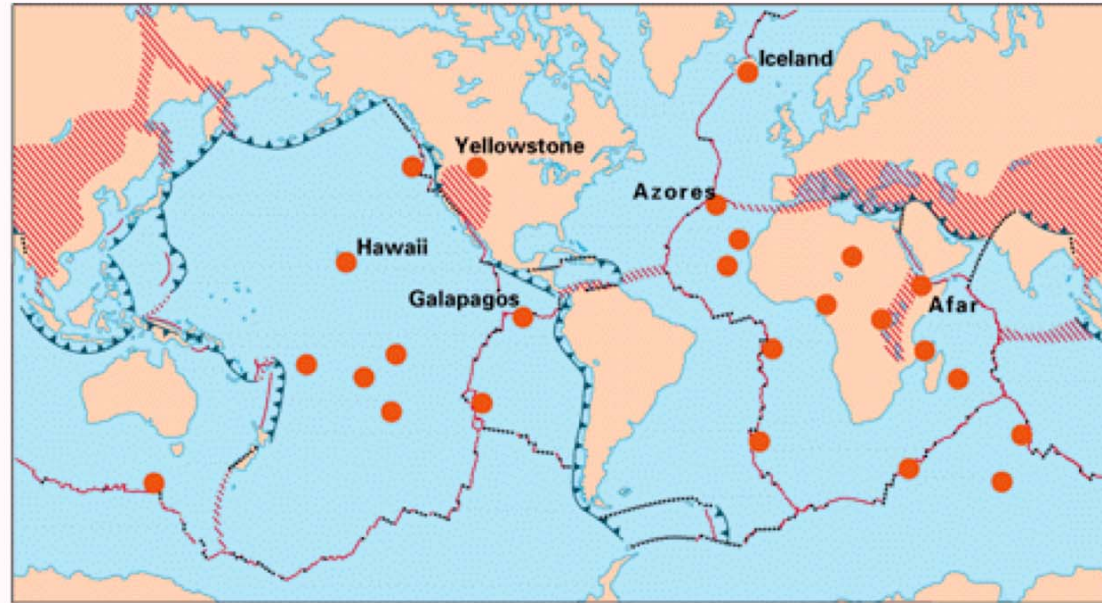


Gung & Romanowicz, (2003)

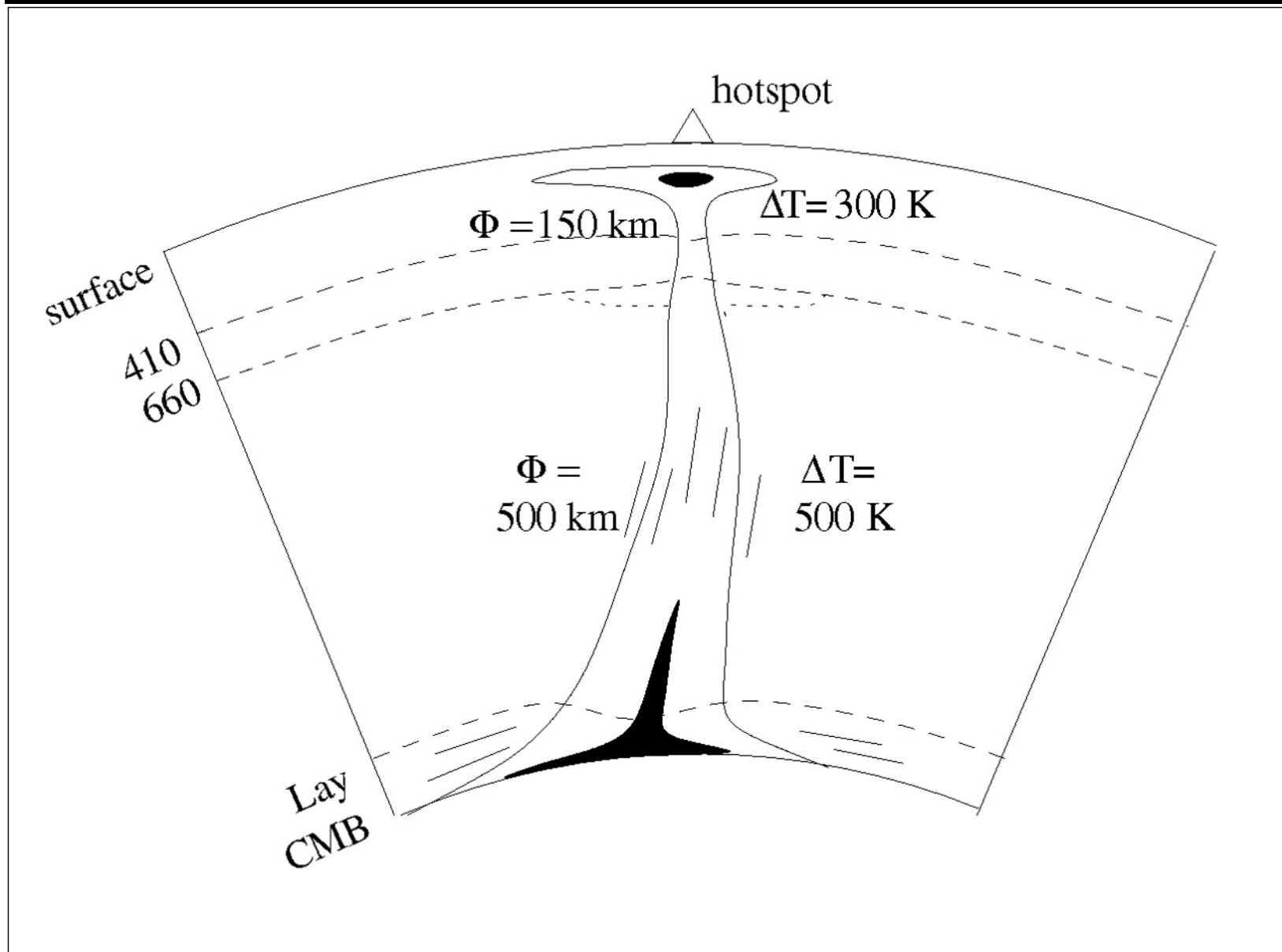
Hotspots - Plumes

EXPLANATION

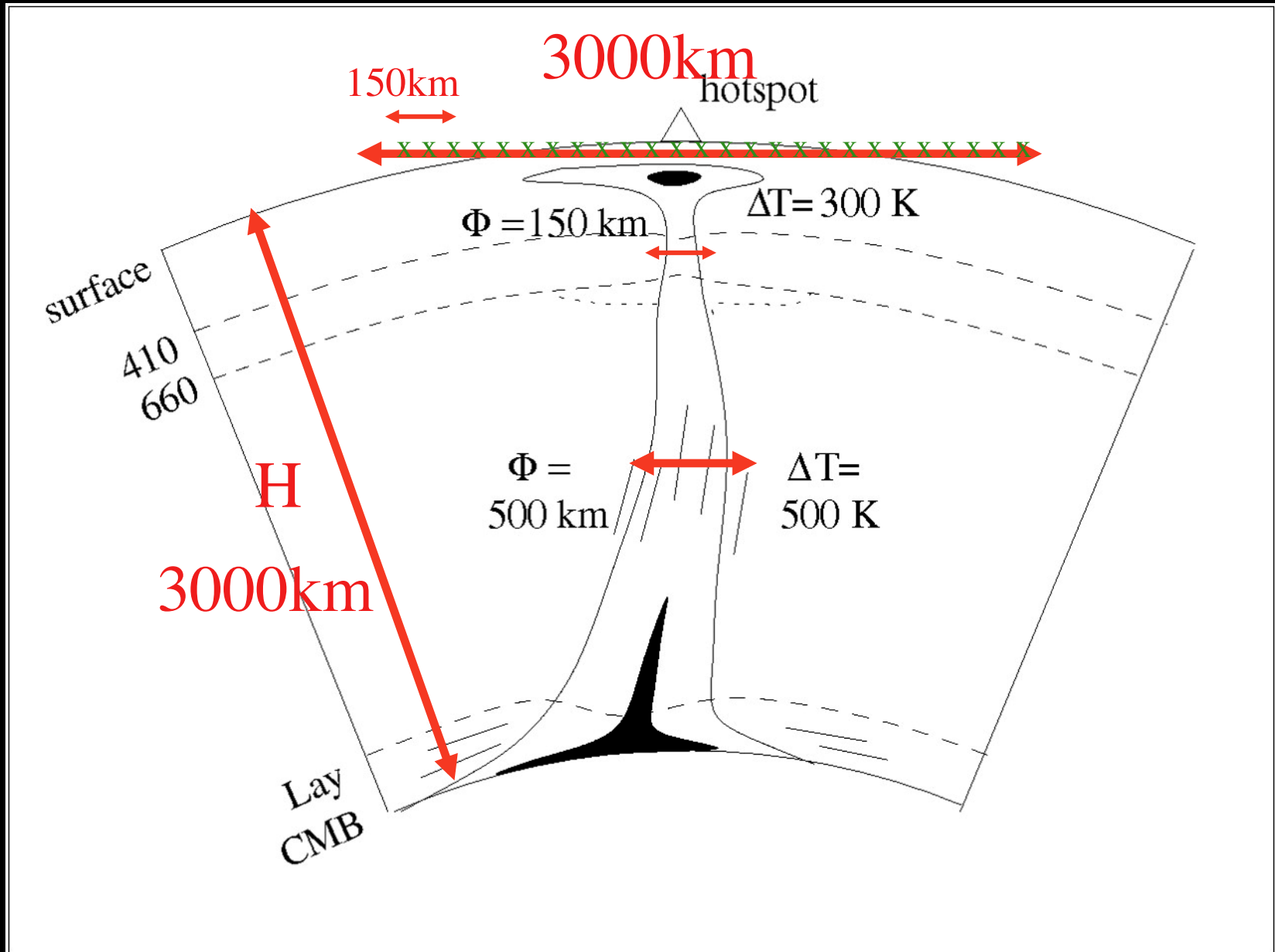
-  Divergent plate boundaries—Where new crust is generated as the plates pull away from each other.
-  Convergent plate boundaries—Where crust is consumed in the Earth's interior as one plate dives under another.
-  Transform plate boundaries—Where crust is neither produced nor destroyed as plates slide horizontally past each other.
-  Plate boundary zones—Broad belts in which deformation is diffuse and boundaries are not well defined.
-  Selected prominent hotspots



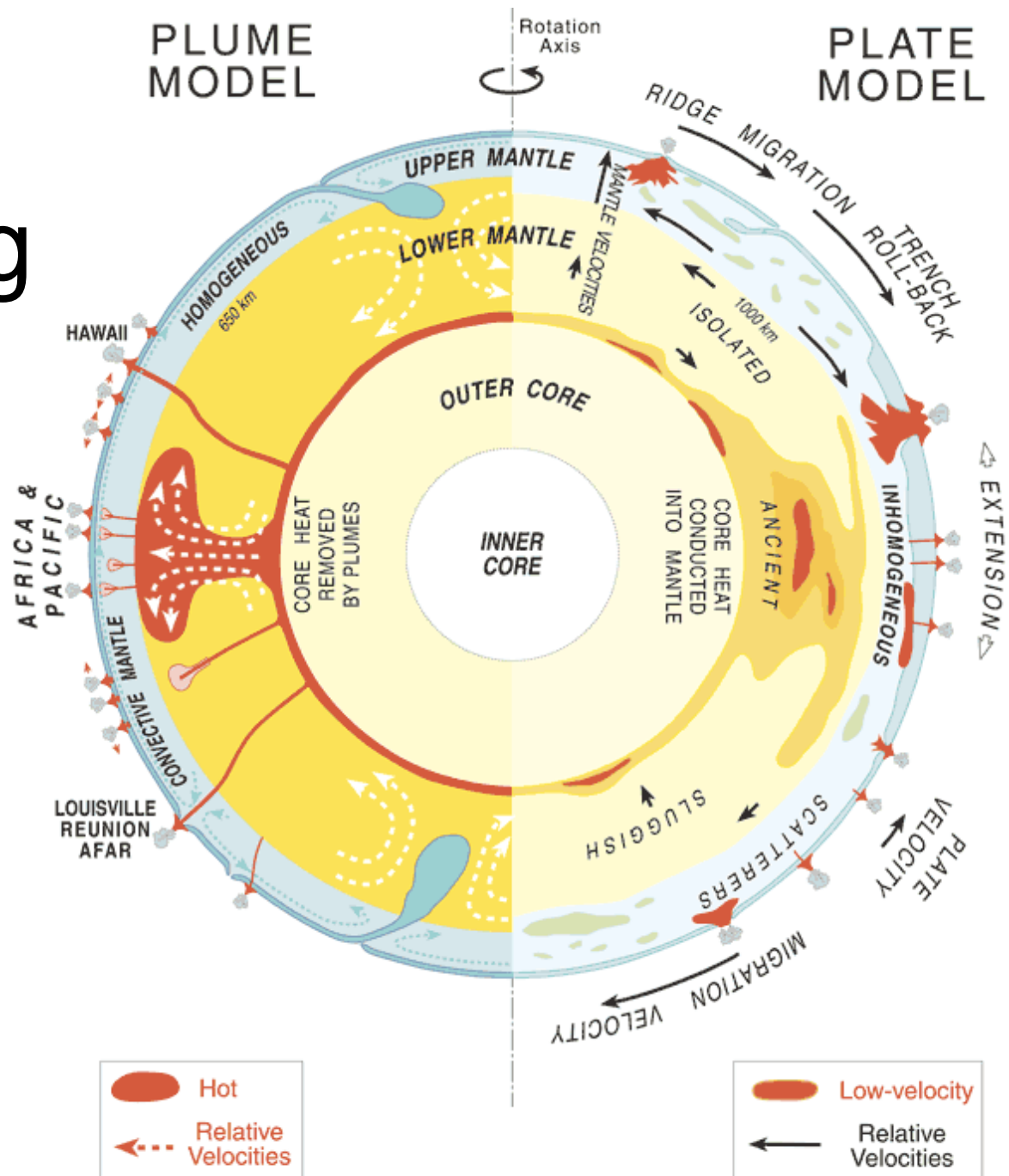
Classical Plume Model from Fluid dynamics(Nataf, 1999)



$H/\Phi \approx 20 \Rightarrow$ at least 40 stations (2 per λ)



At least, 2 Competing models



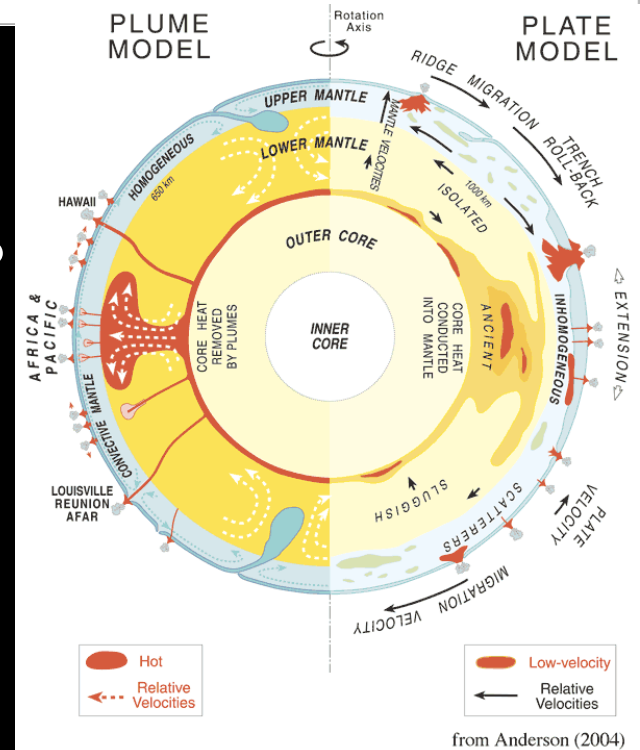
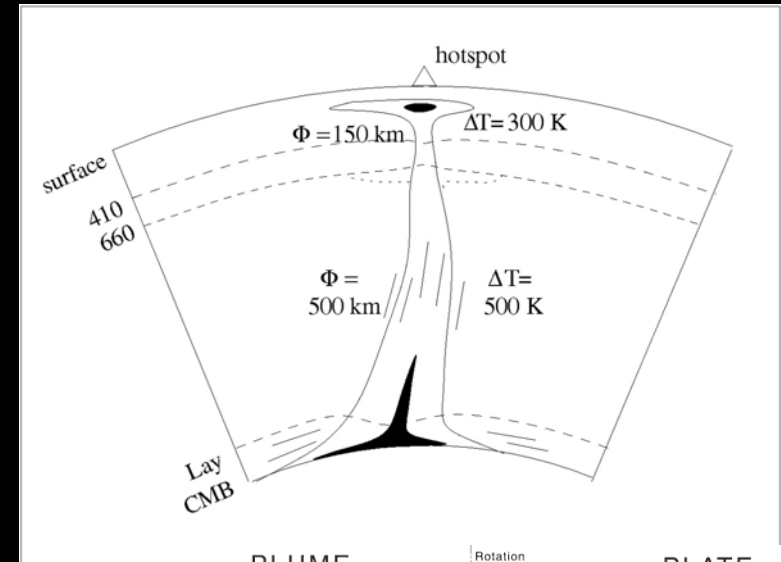
from Anderson (2004)

Definition of plume: thermal instability in a boundary layer:

- Core-mantle boundary
- Transition Zone (400-660- 1000km)?
- Asthenosphere- lithosphere?

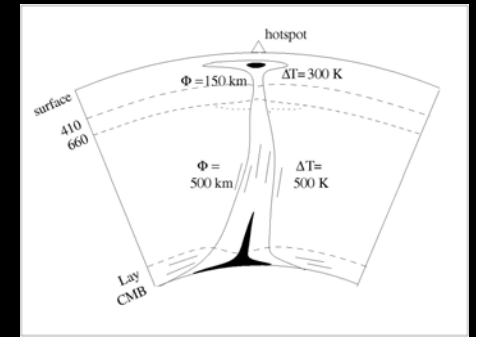
But

- Is the plume model correct?
- What is their geodynamical role?
- What is their biological role?
- What is their structure, their origin at depth?
- Are there really several types of plumes?



from Anderson (2004)

Detection of a Plume



Expected Effects of Plume on seismic data

- Thermal effect: $\Delta T > 0 \Rightarrow \delta V_S < 0, \delta V_P < 0$

- Upwelling flow \Rightarrow crystal alignment by LPO

Weak azimuthal seismic anisotropy,

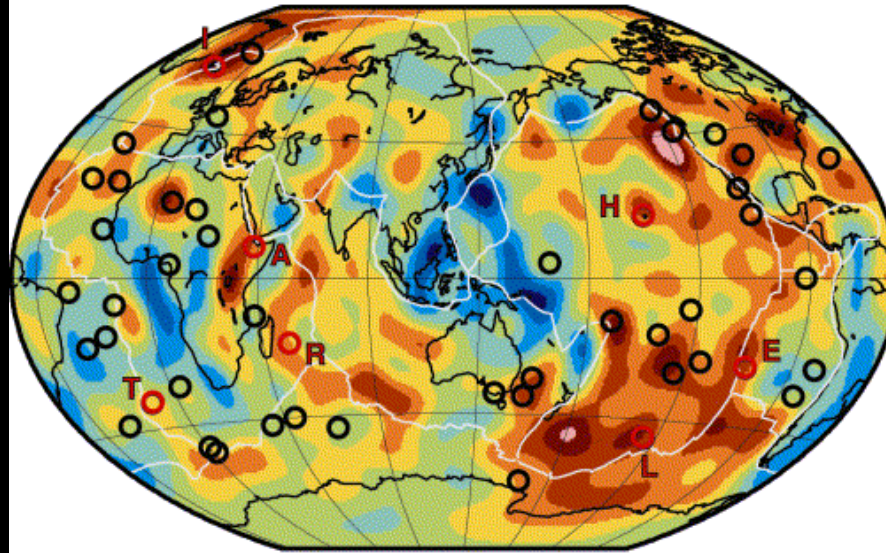
$V_{SV} > V_{SH}$ ($\xi < 1$: radial seismic anisotropy)

- Large attenuation \Rightarrow low quality factor Q

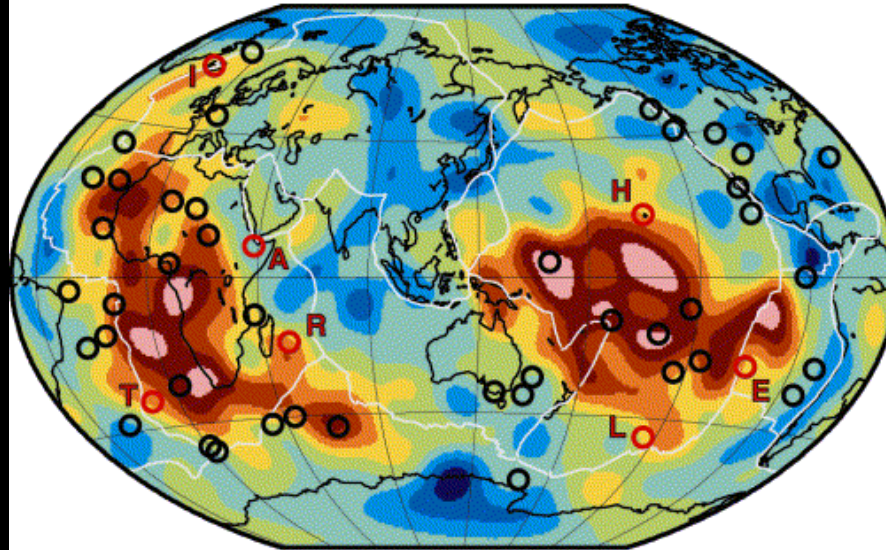
- Thinning of the Transition zone thickness
(410km deflected downward, 660km upward)

Global Scale

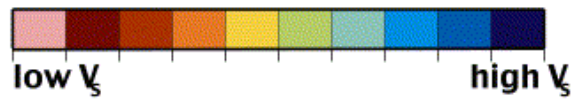
(a) 500 km (2%)

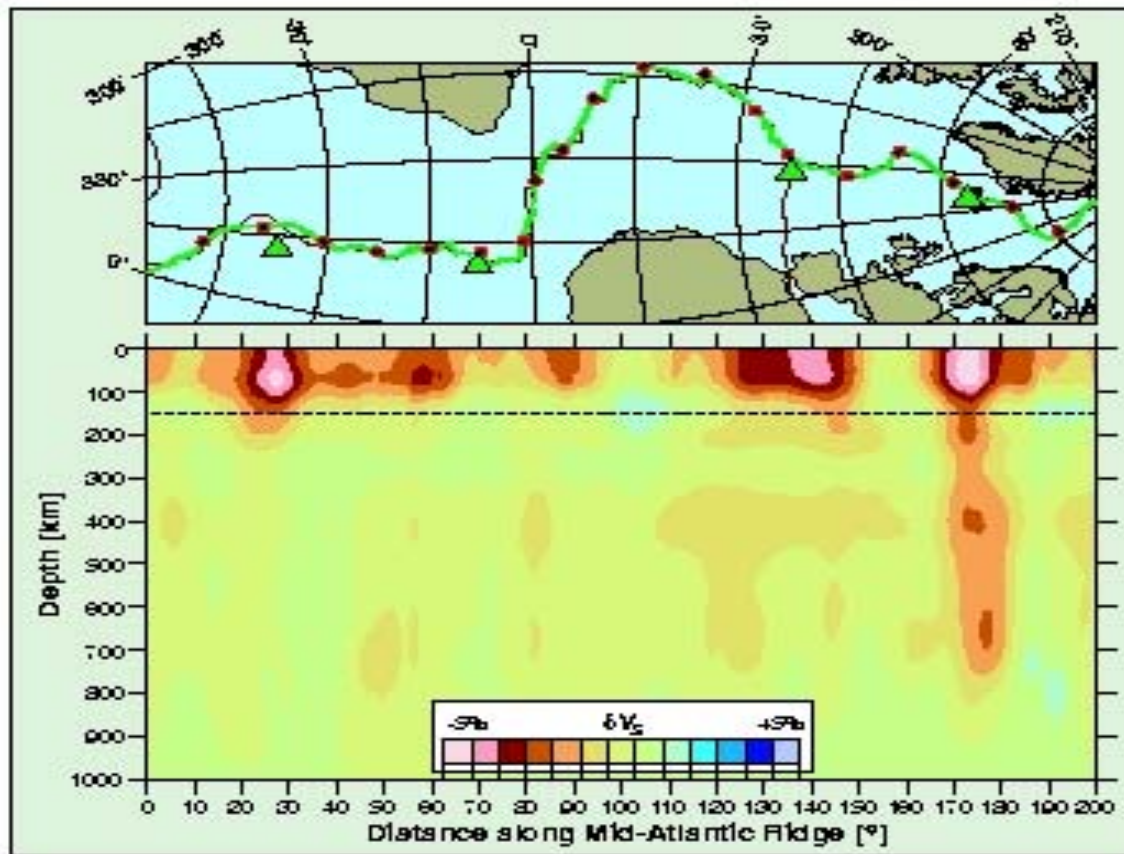


(b) 2850 km (2%)



Ritsema et al., 2000

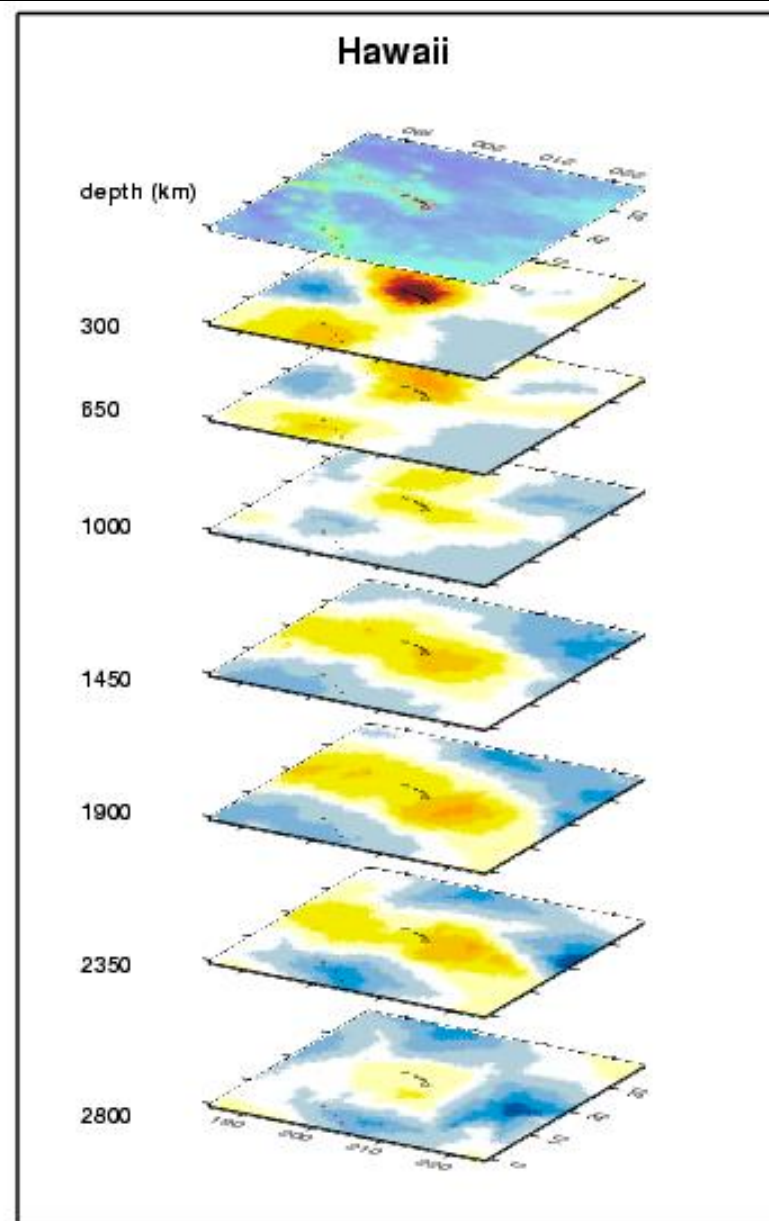




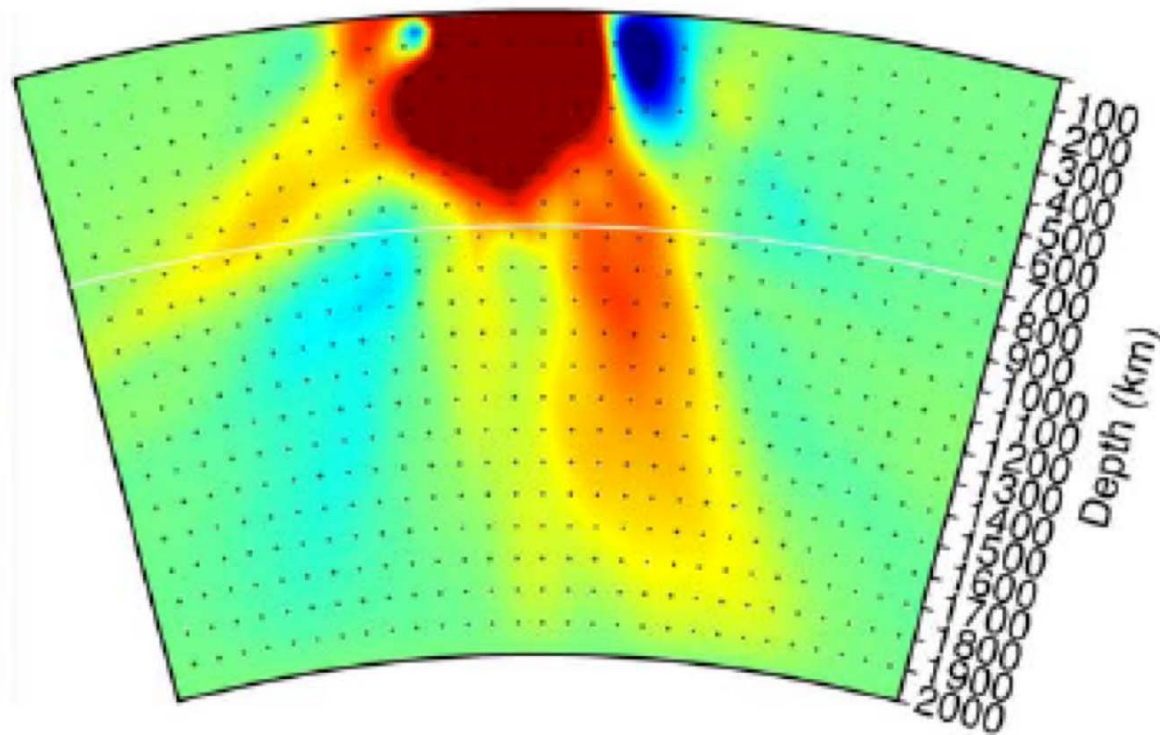
(Montagner and Ritsema, science, 2001)

From Banana-Doughnut Theory (Dahlen et al.)

Application to global tomography (Montelli et al., science, 2004)



Hawaii plume (Wolfe et al., science, 2009)



Complex Interaction of lithosphere, Asthenosphere and continents

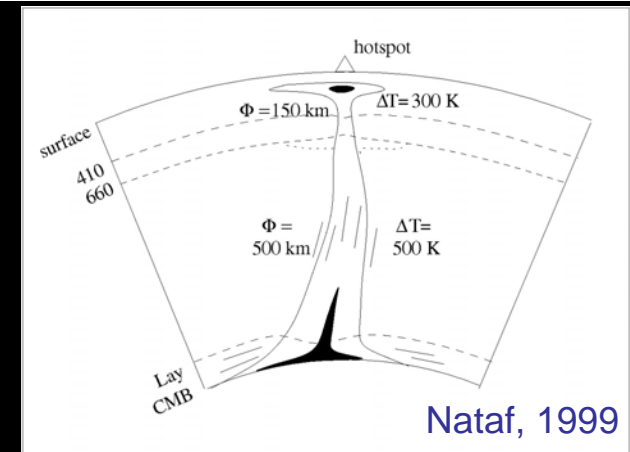
Plume Detection - interaction with the upper mantle

Regional studies:

Pacific Ocean (Montagner, 2002; Maggi et al., 2006)

Horn of Africa (Debayle et al., 2001; Sebai et al., 2006;
Montagner et al., 2007; Sicilia et al., 2008, Obrebski et al., 2010)

Anisotropy and Detection of Plume



Expected Effects of plume on seismic data in UM

- Thermal effect: $\Delta T > 0 \Rightarrow \delta V_S < 0, \delta V_P < 0$

- Upwelling flow \Rightarrow crystals alignment by LPO
Weak azimuthal seismic anisotropy,
 $V_{SV} > V_{SH}$ ($\xi < 1$: radial seismic anisotropy)

- Large attenuation \Rightarrow low quality factor Q

- Thinning of the Transition zone thickness
(410km deflected downward, 660km upward)




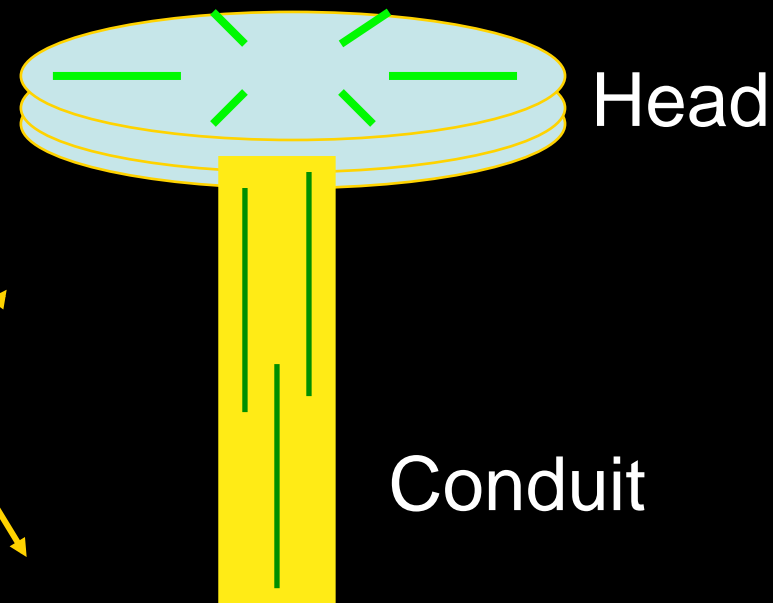
Plume affects not only S-wave distribution but also seismic anisotropy

- Head: easy to detect

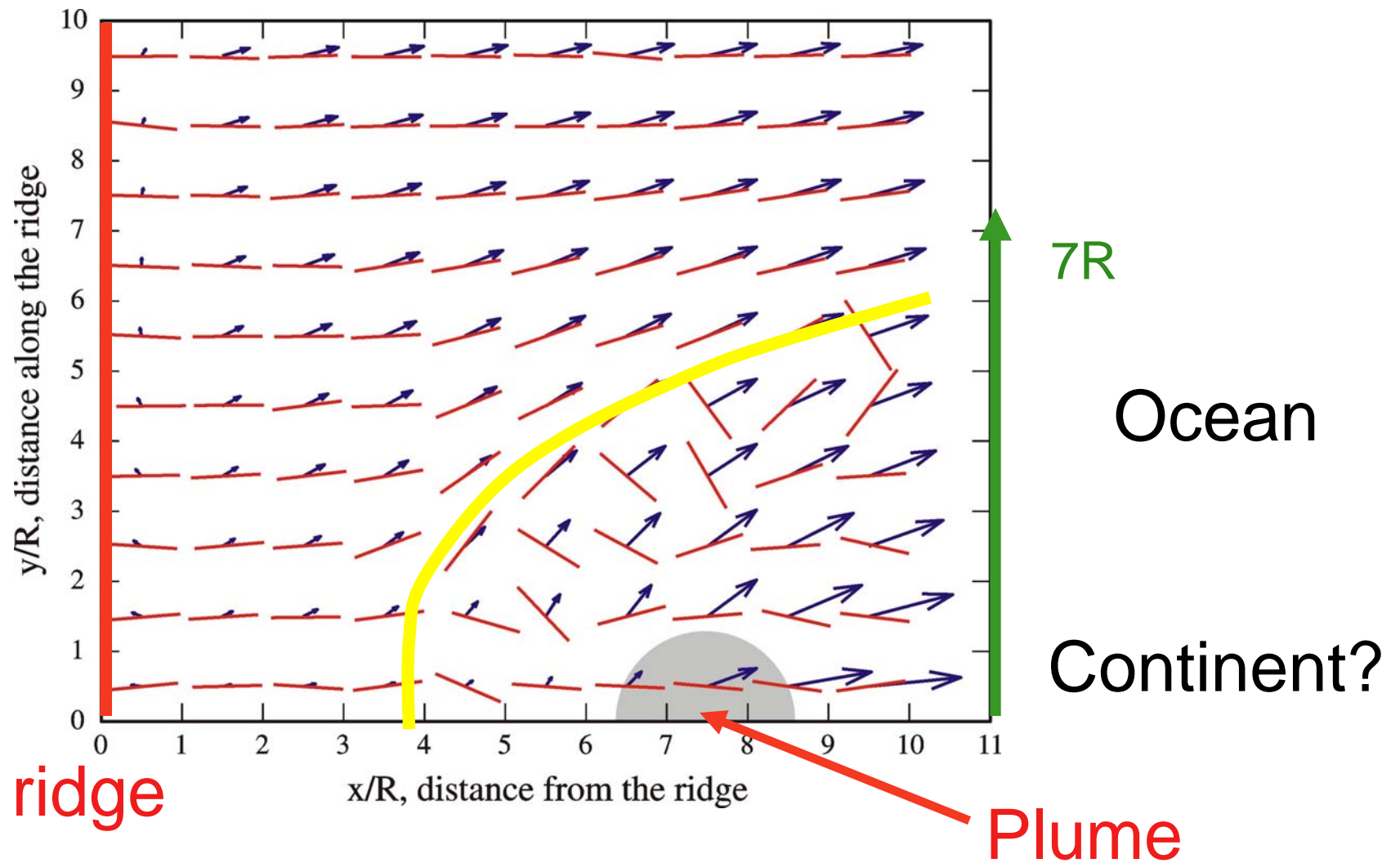
- Conduit: difficult to detect

$\Delta\alpha$: Anisotropic effect $\Rightarrow V_{SV}$ 

ΔT : Température effect $\Rightarrow V_{SV}$ 



Opposite effects \Rightarrow difficult to detect below asthenosphere



Azimuthal Anisotropy



Indirect detection of plume
(parabolic flow)

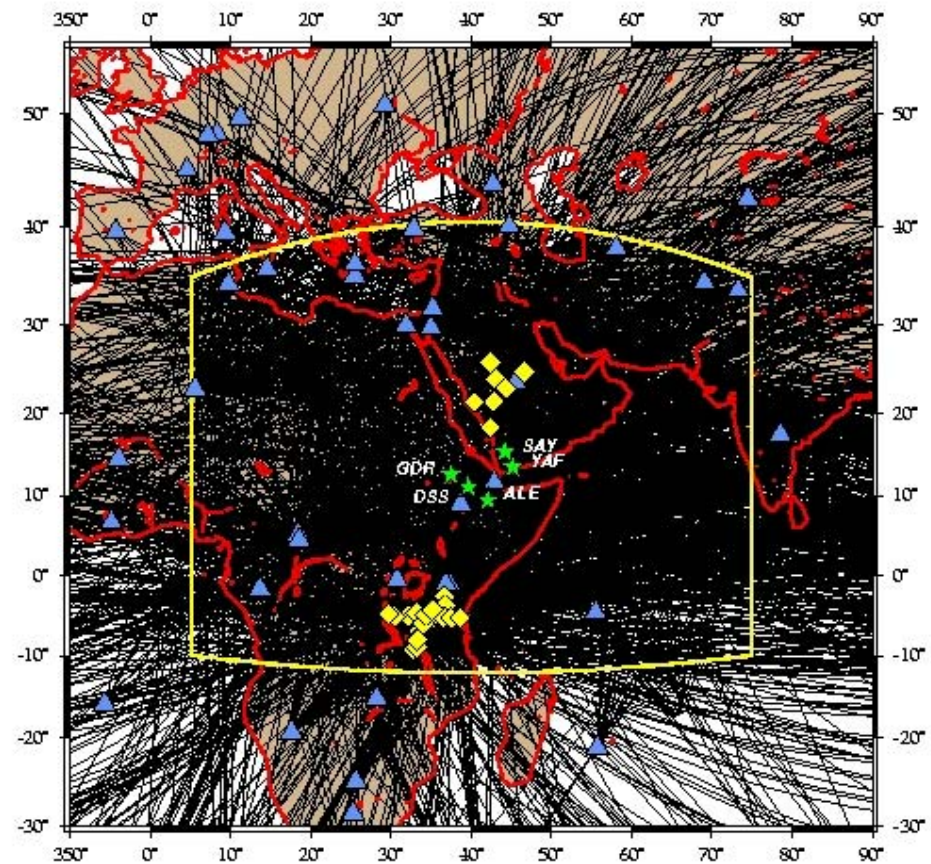
(Kaminski and Ribe, 2001)

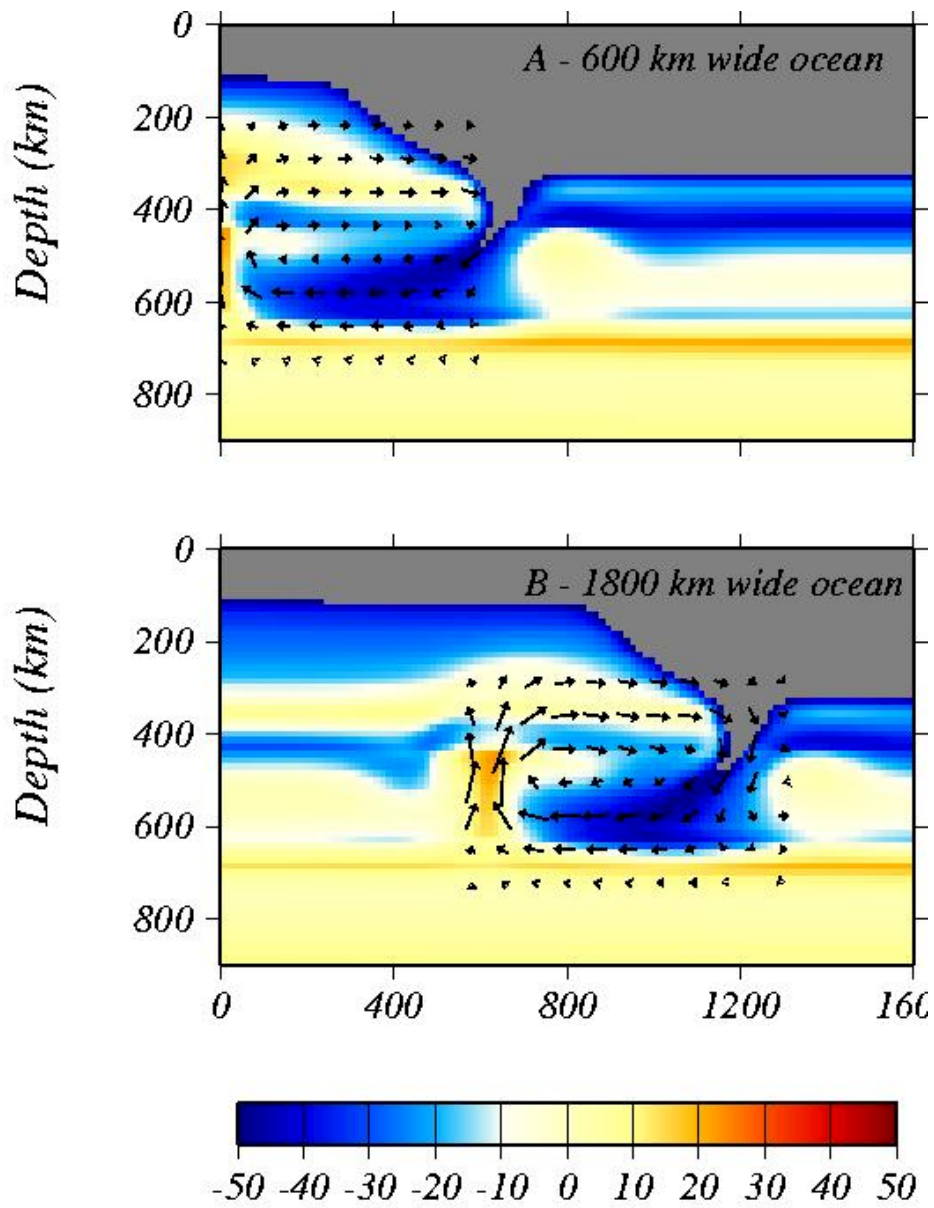
Complex Interaction of upwellings with lithosphere, asthenosphere, or continent will affect the anisotropy distribution

Continents

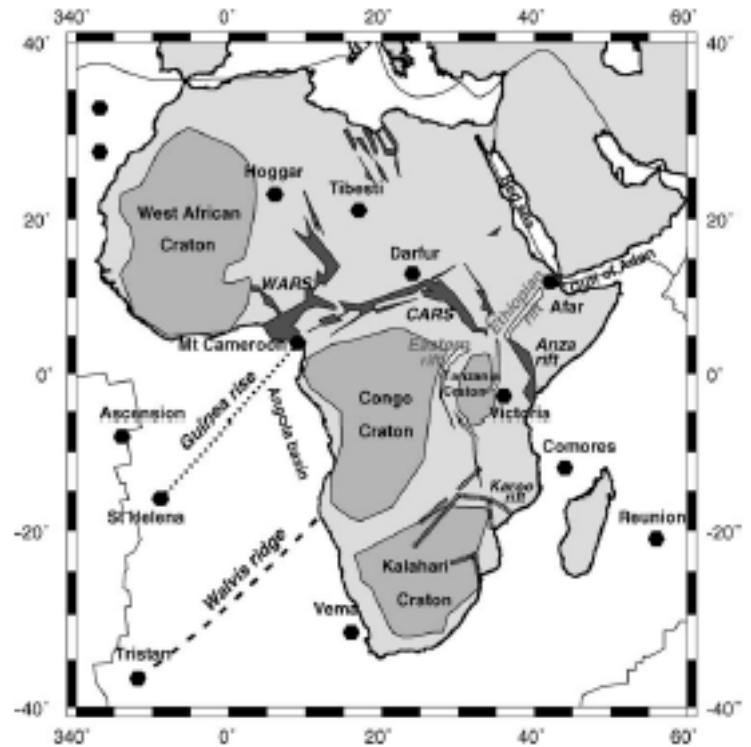
Horn of Africa

(Debayle et al., 2001;
Sebai et al., 2006;
Montagner et al., 2007
Sicilia et al., 2008
Obrebski et al., 2010)



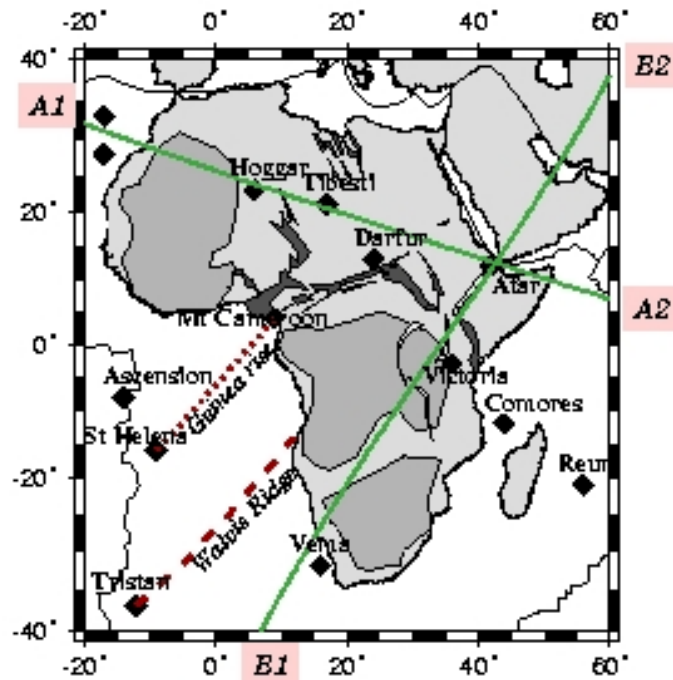


King & Ritsema, 1999

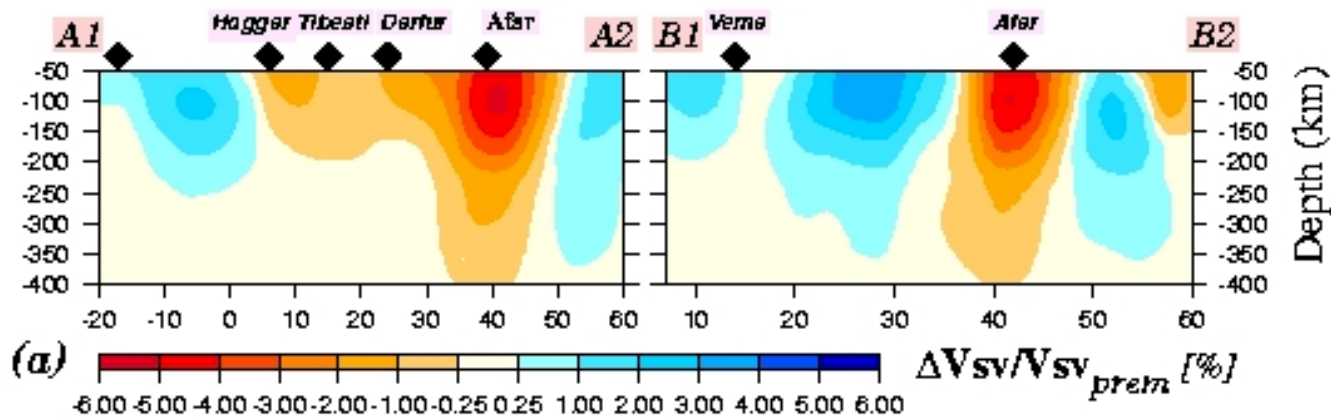


Sebai et al., 2006

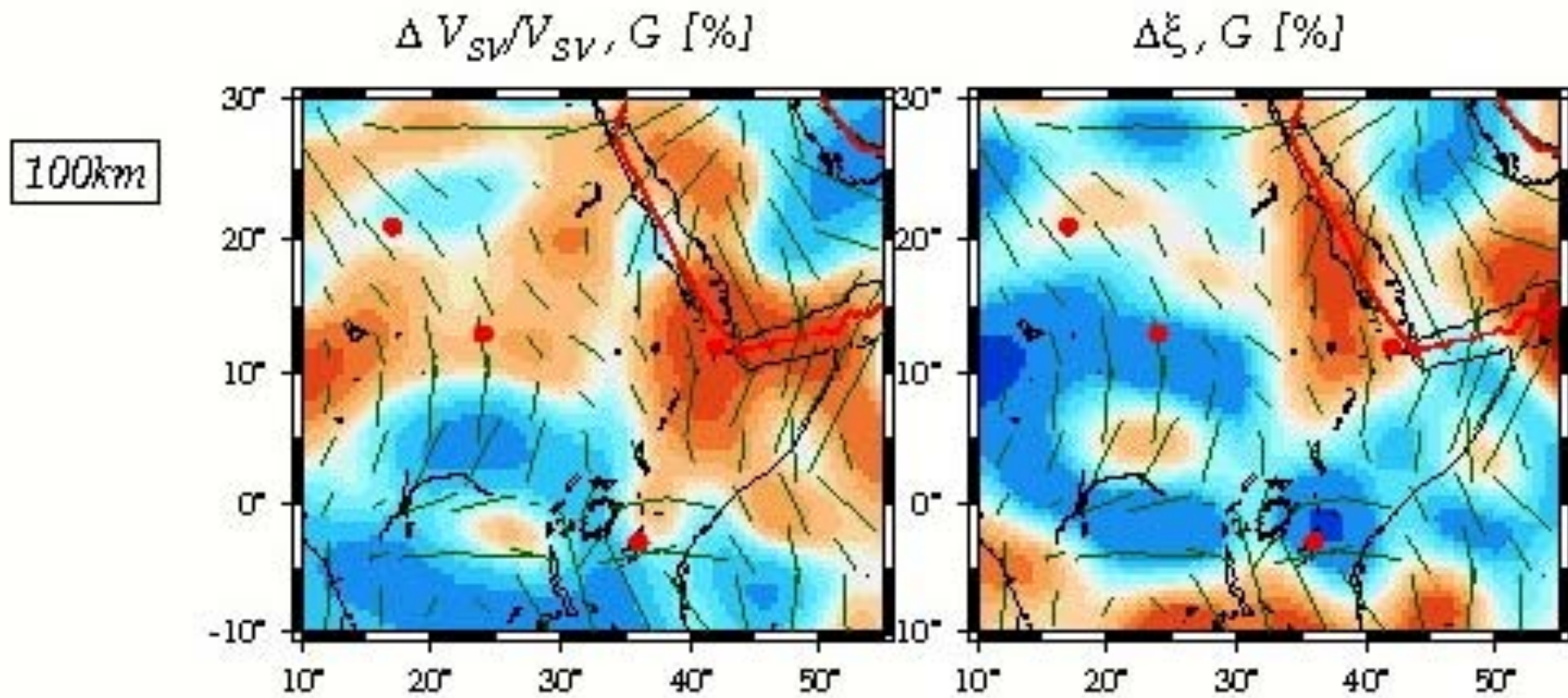
(Sebai et al., 2006)



Lateral resolution
~1000km



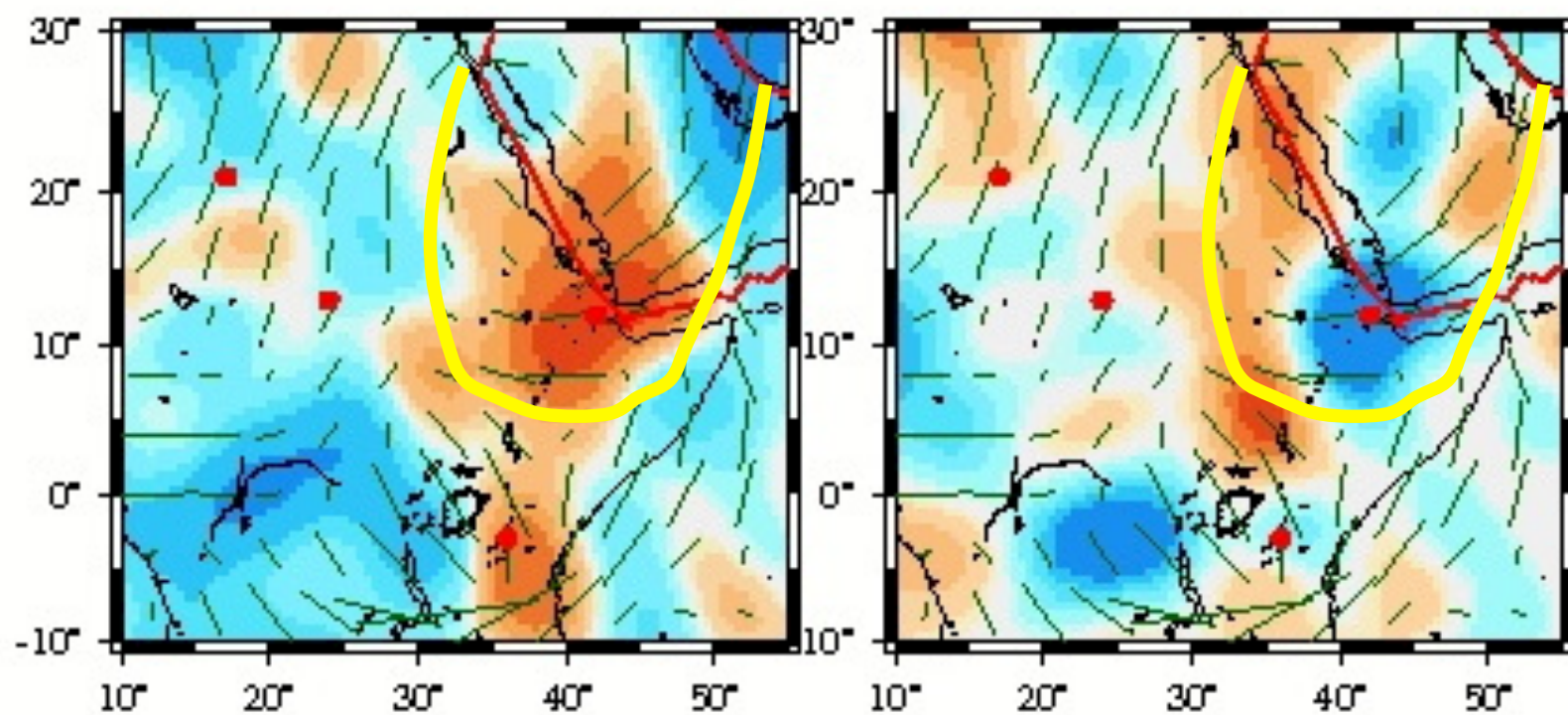
G azimuthal anisotropy
 $\Delta\xi$ radial anisotropy (Sicilia et al., 2008)



$\Delta V_{sw}/V_{sv}, G$ [%]

$\Delta \xi, G$ [%]

200km



$\Delta V_{sw}/V_{sv}, G$ [%]

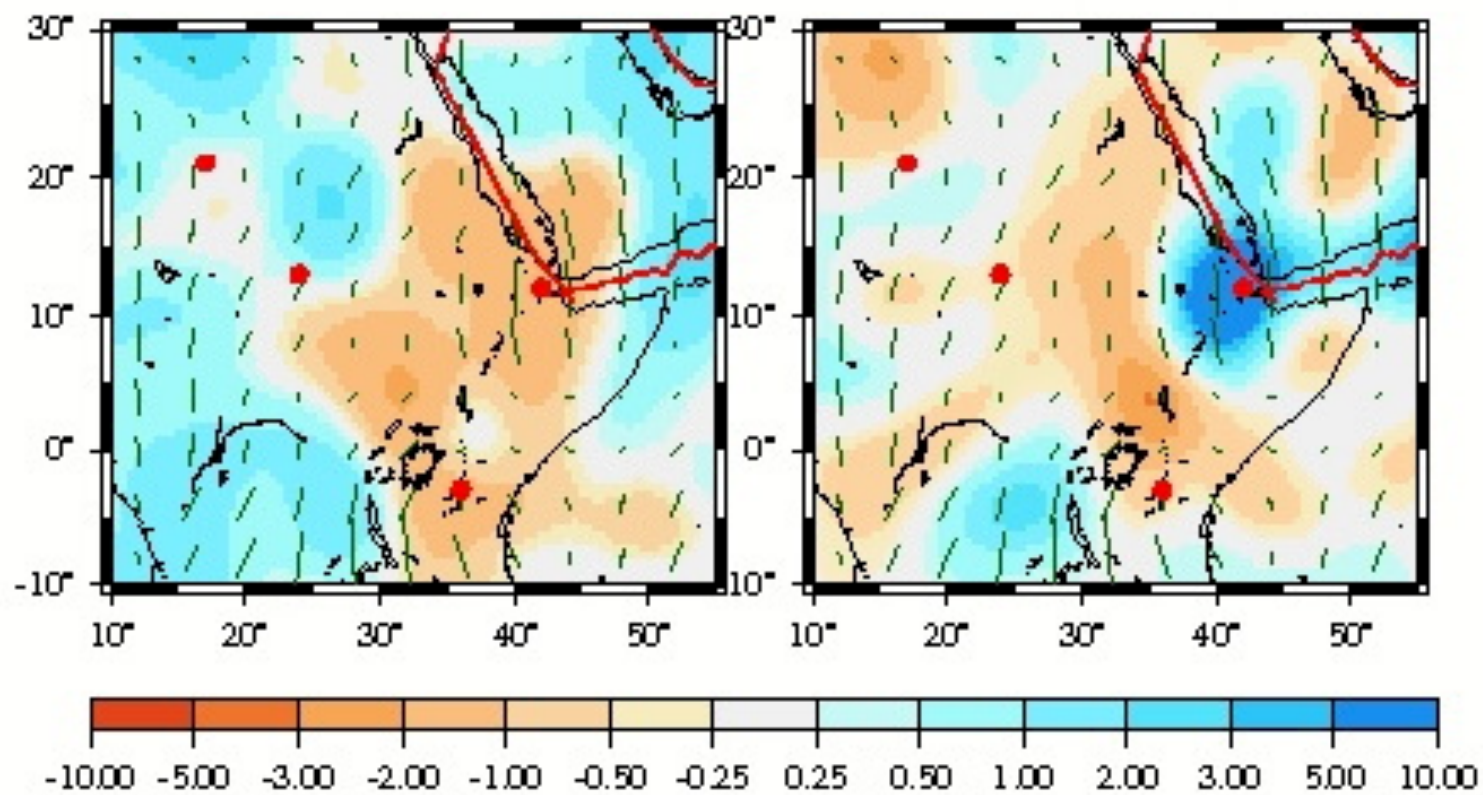
$\Delta \xi, G$ [%]

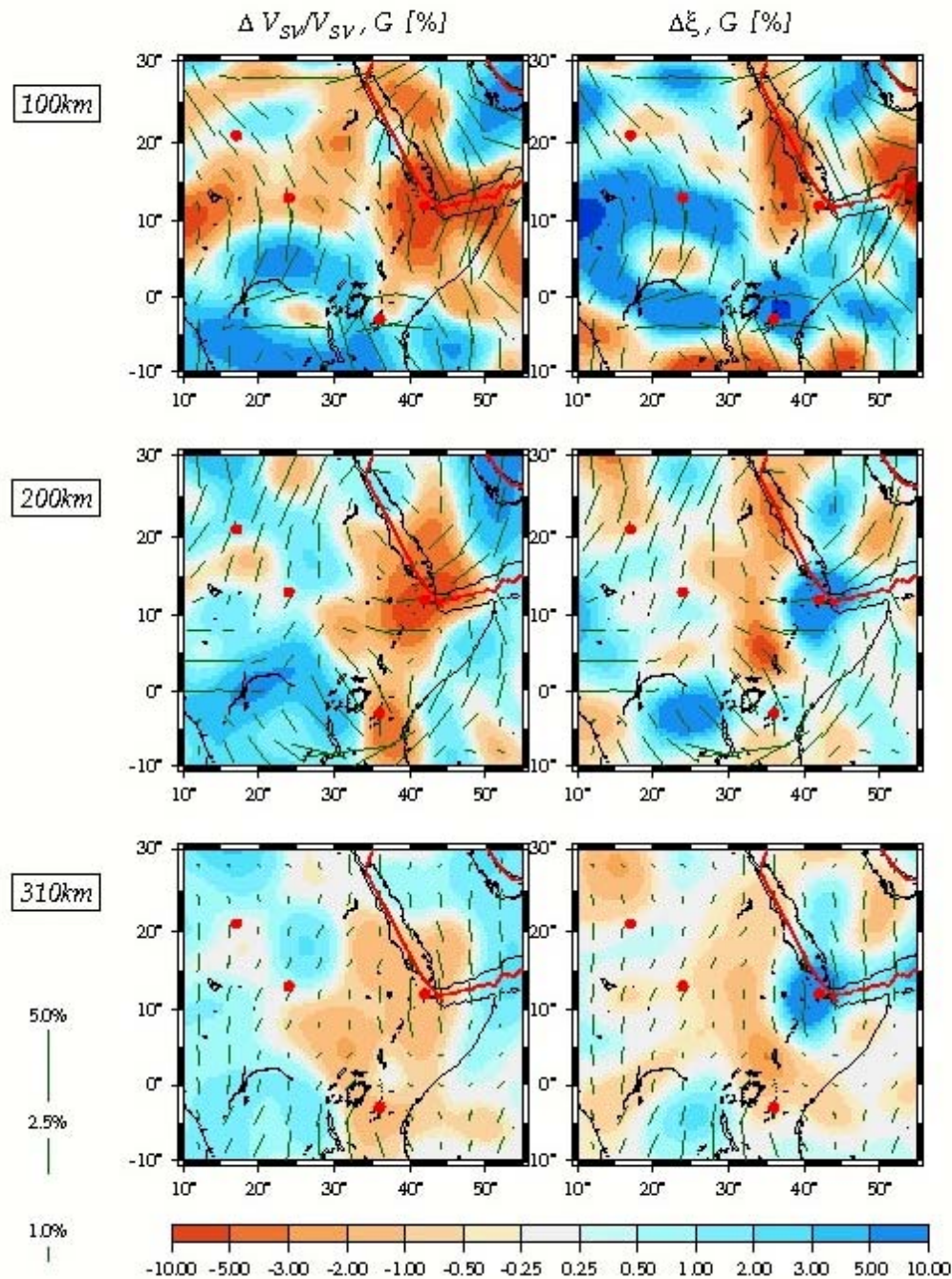
310km

5.0%

2.5%

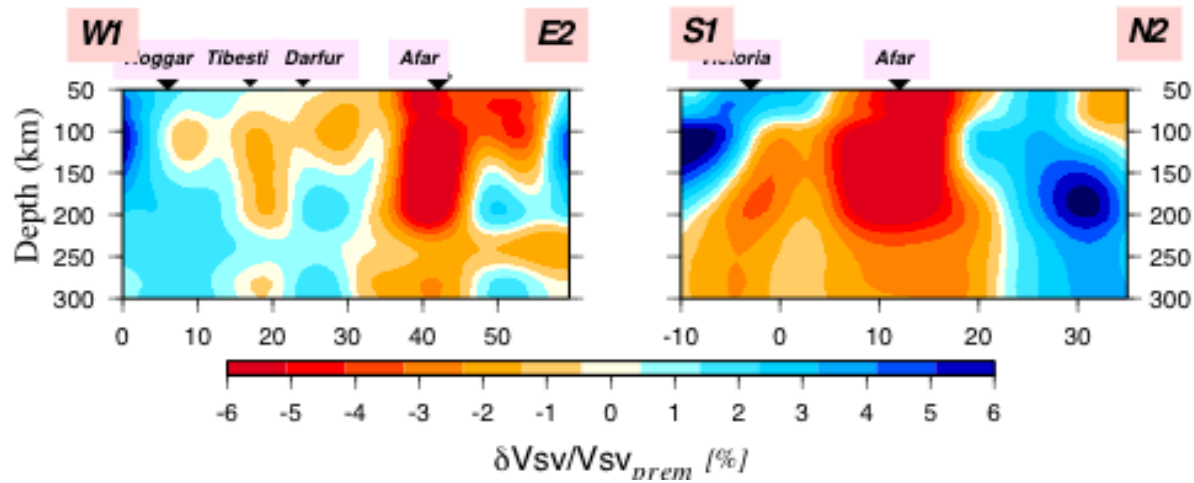
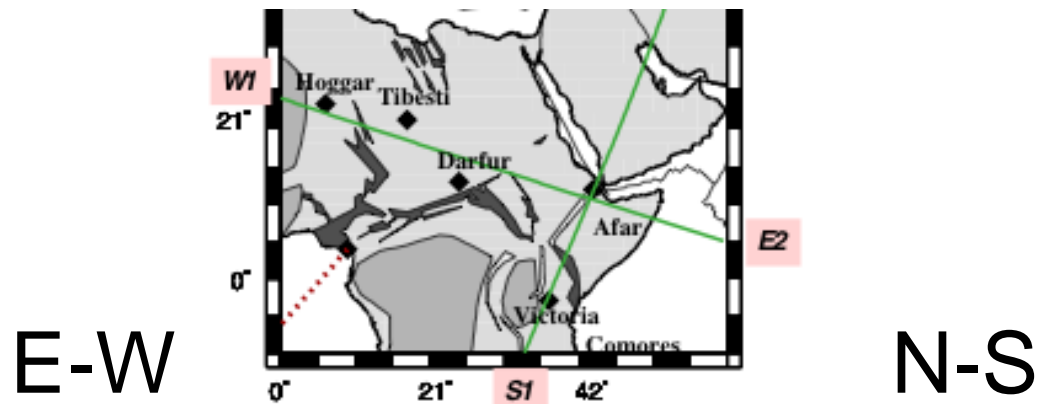
1.0%



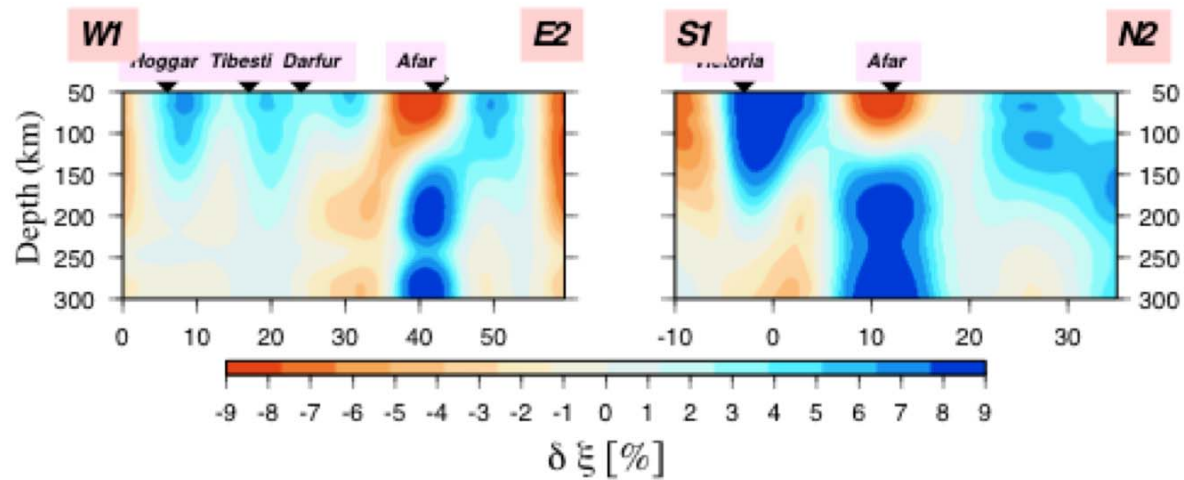


3D- Anisotropy Tomography of Eastern Africa

- Parabolic flow around Afar
- Stratification of Anisotropy: >3 layers in Eastern Africa



S-Velocity

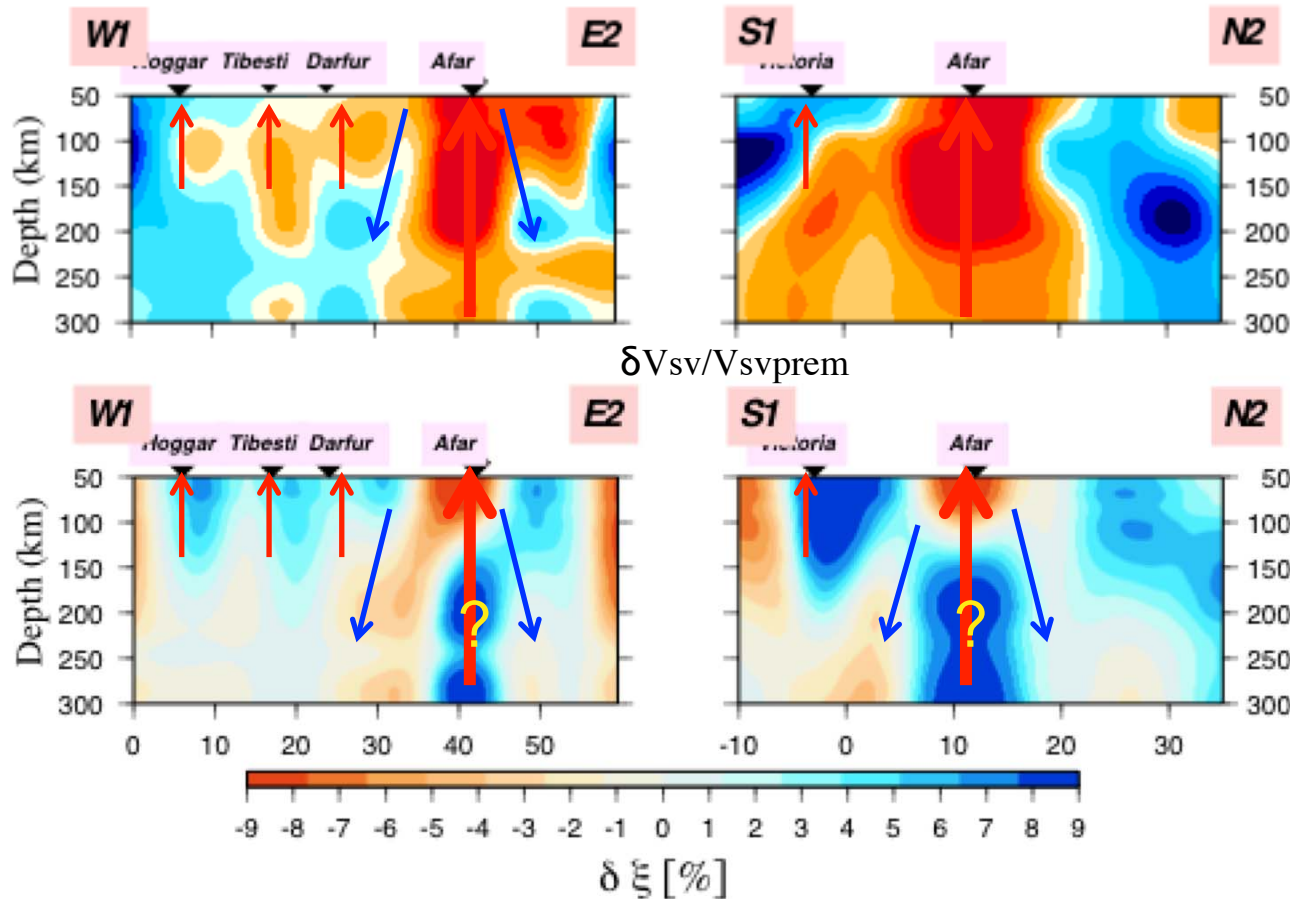
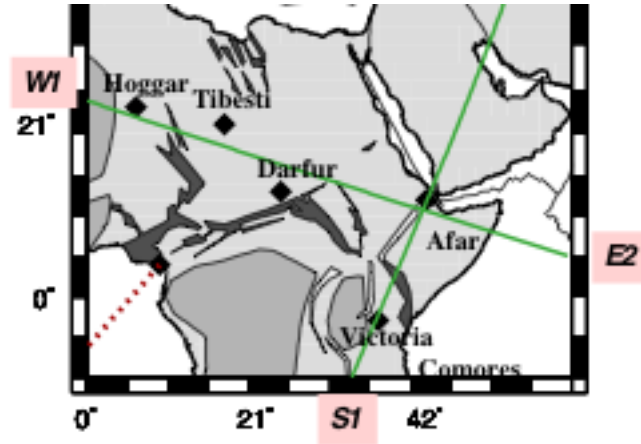


$\delta \xi$ Radial Anisotropy

Geodynamic Interpretation

E-W

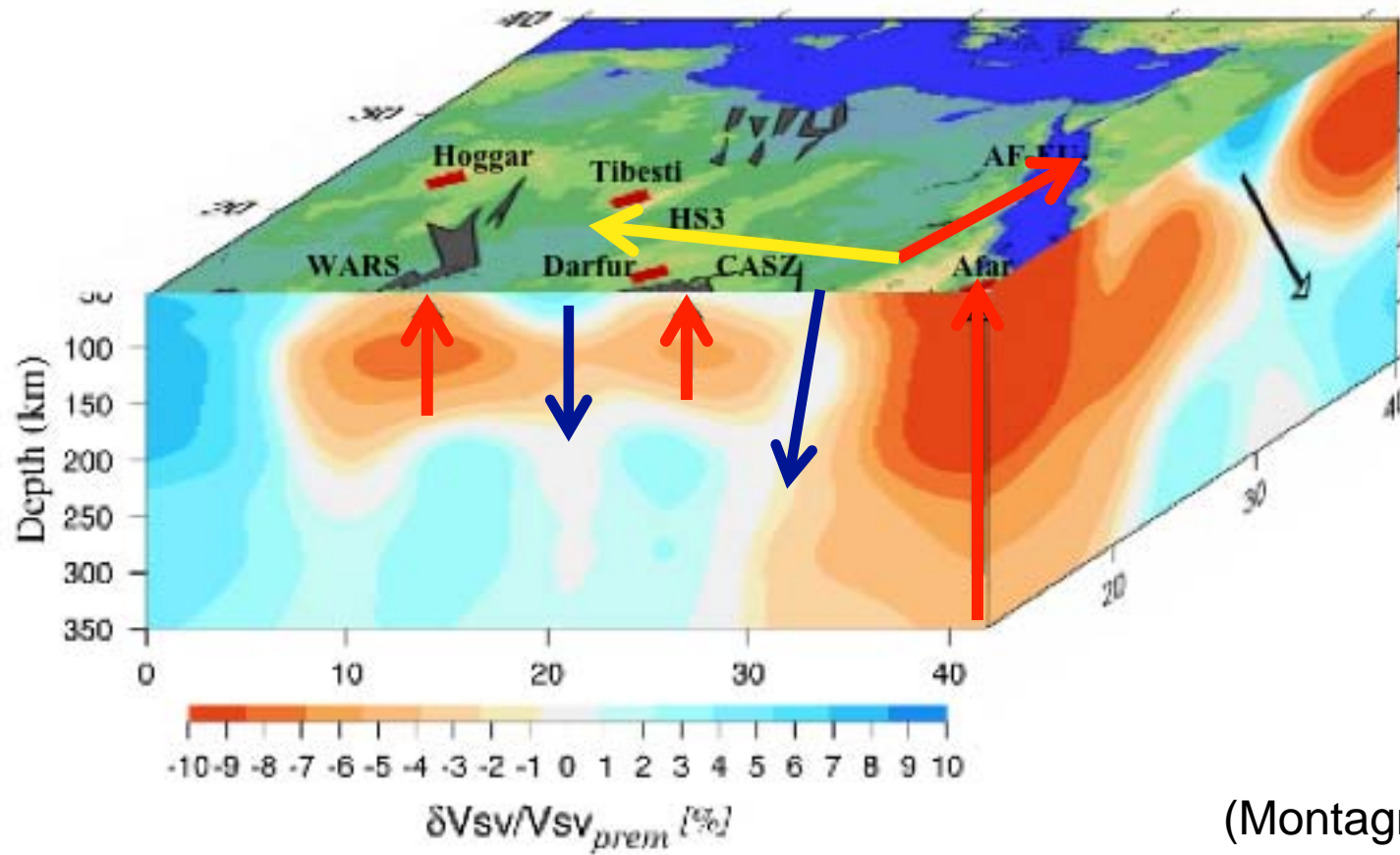
N-S



Stratification of anisotropy

Convective Instabilities (~1000km)

Water?



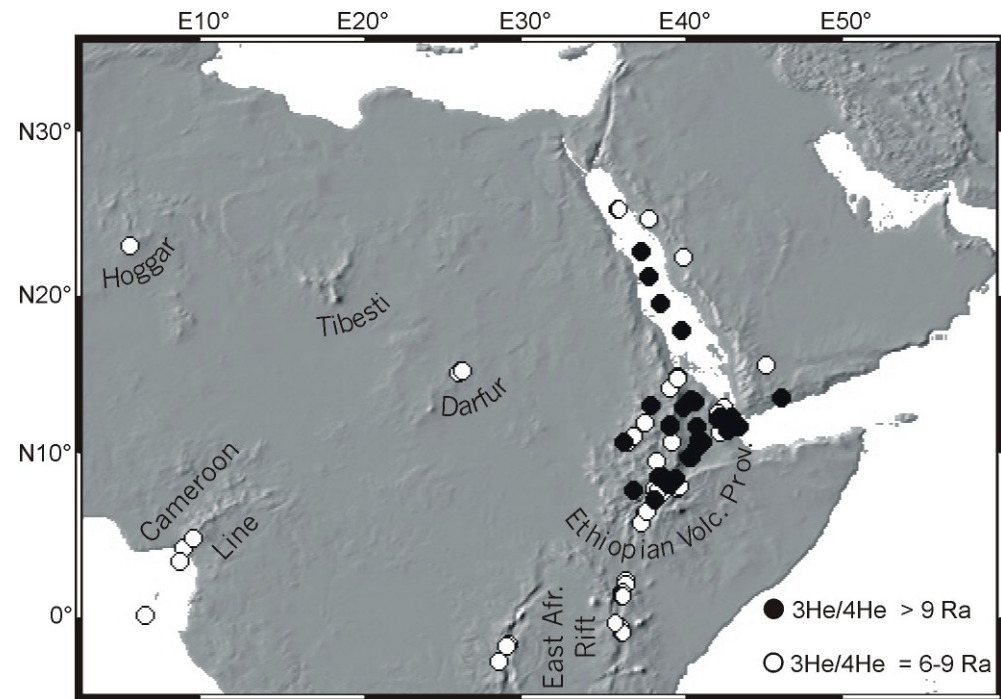
(Montagner et al., 2007)

2 kinds of Plumes

Stratification of anisotropy (>3 layers)

Secondary Convection below lithosphere $\lambda \sim 1000\text{km}$?

Geochemical data Helium (B. Marty, R. Pik)



How to retrieve the Stratification of anisotropy in the upper mantle?

-Surface waves

Good vertical resolution, bad lateral resolution

-SKS data

interpretation of SKS splitting data?

1 delay time δt , 1 angle Ψ : bad vertical resolution

Several layers: Silver, Savage, Wolfe, Rumpker...

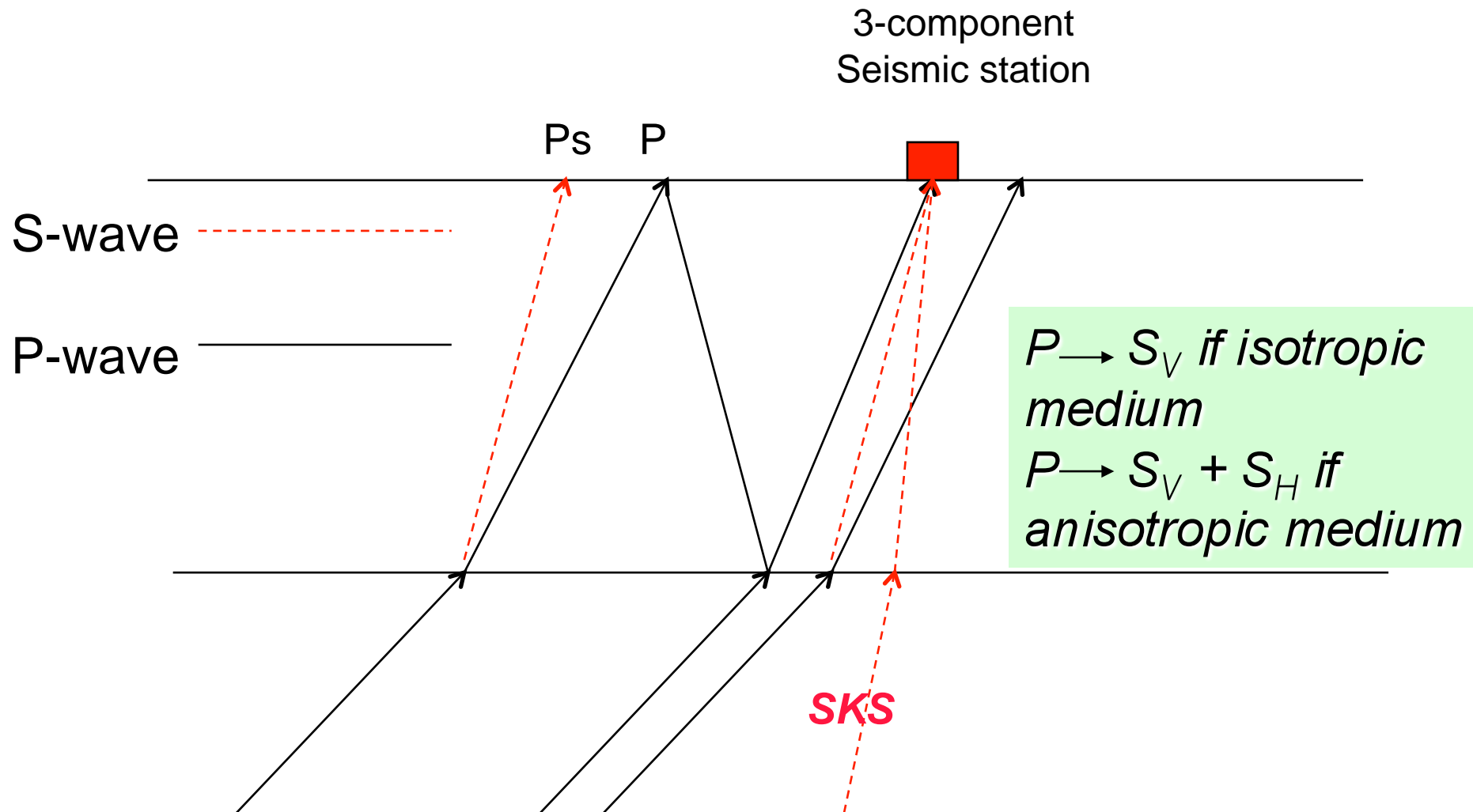
- Receiver function (R.F.)

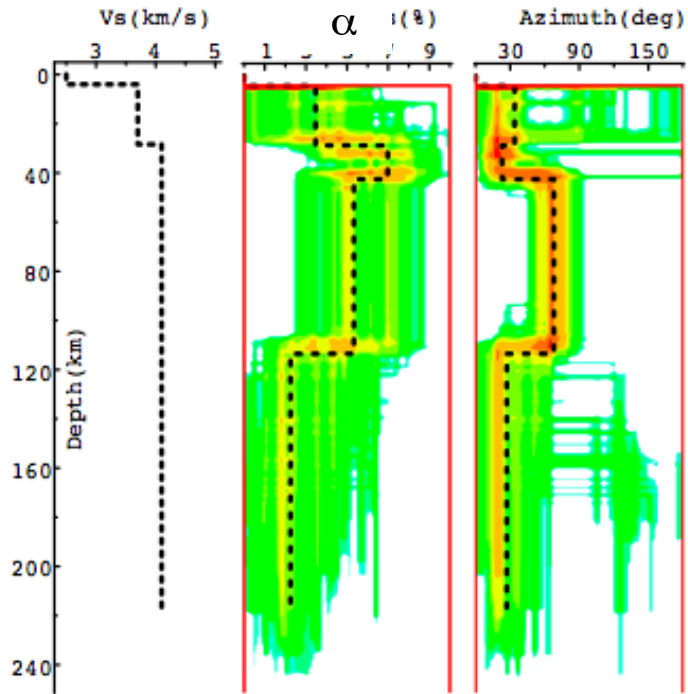
Joint inversion of SKS and R.F. data

(Vinnik et al., 2007)

Joint inversion of SKS and receiver functions

(M. Obrebski, S. Kiselev, L. Vinnik, J.P. Montagner)

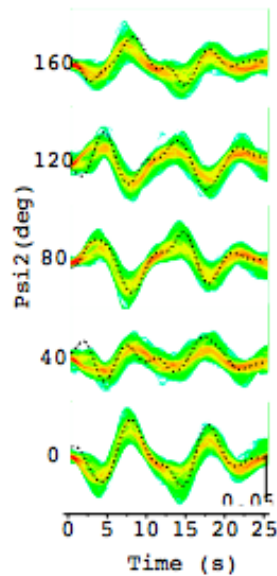




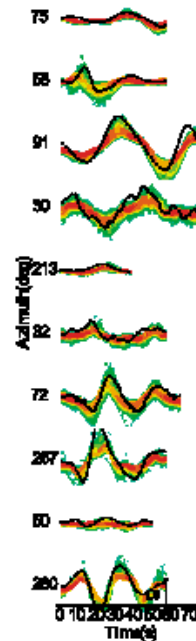
ATD Geoscope Station (Djibouti)

Receiver functions (RF)
+
SKS

RF



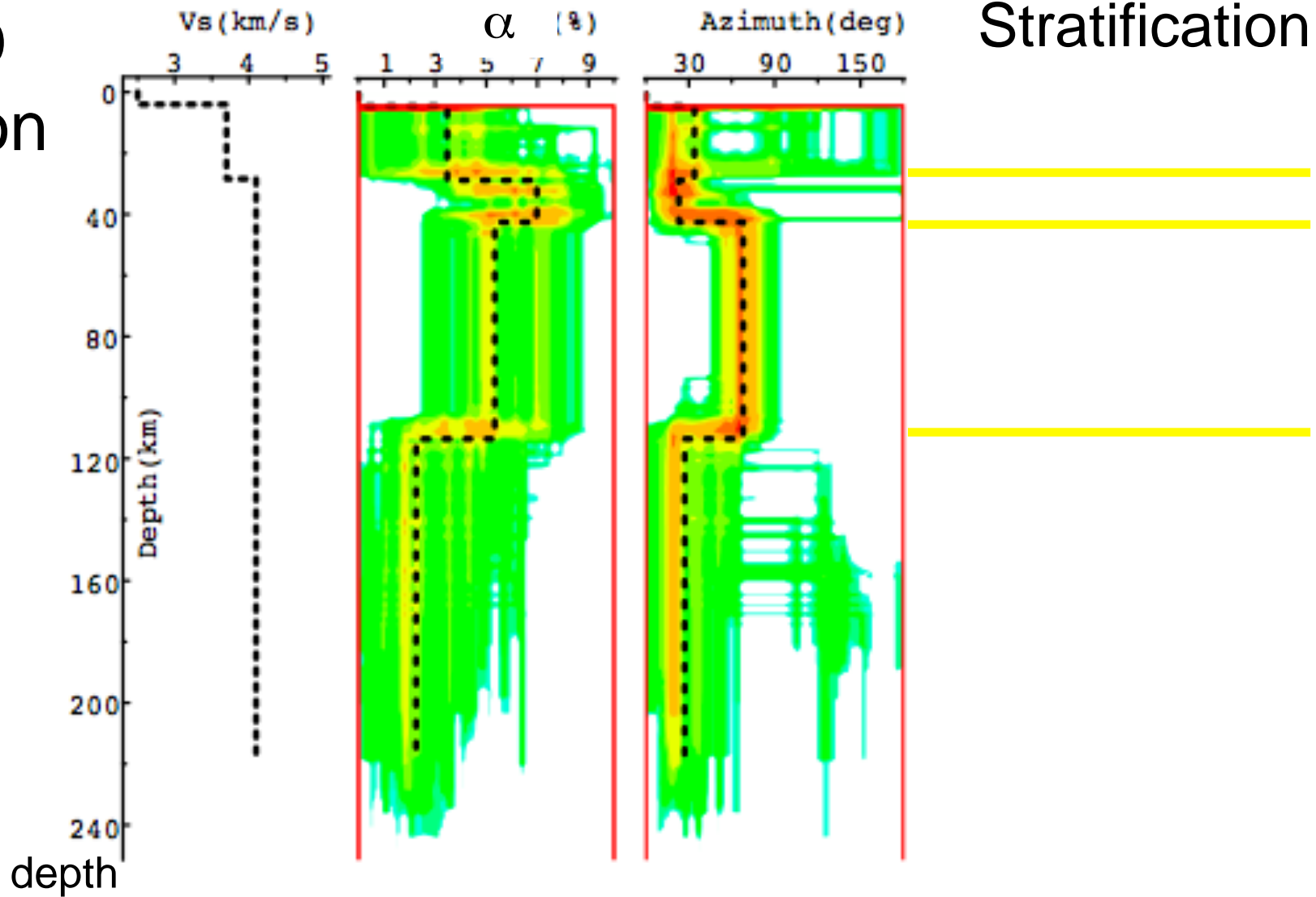
SKS

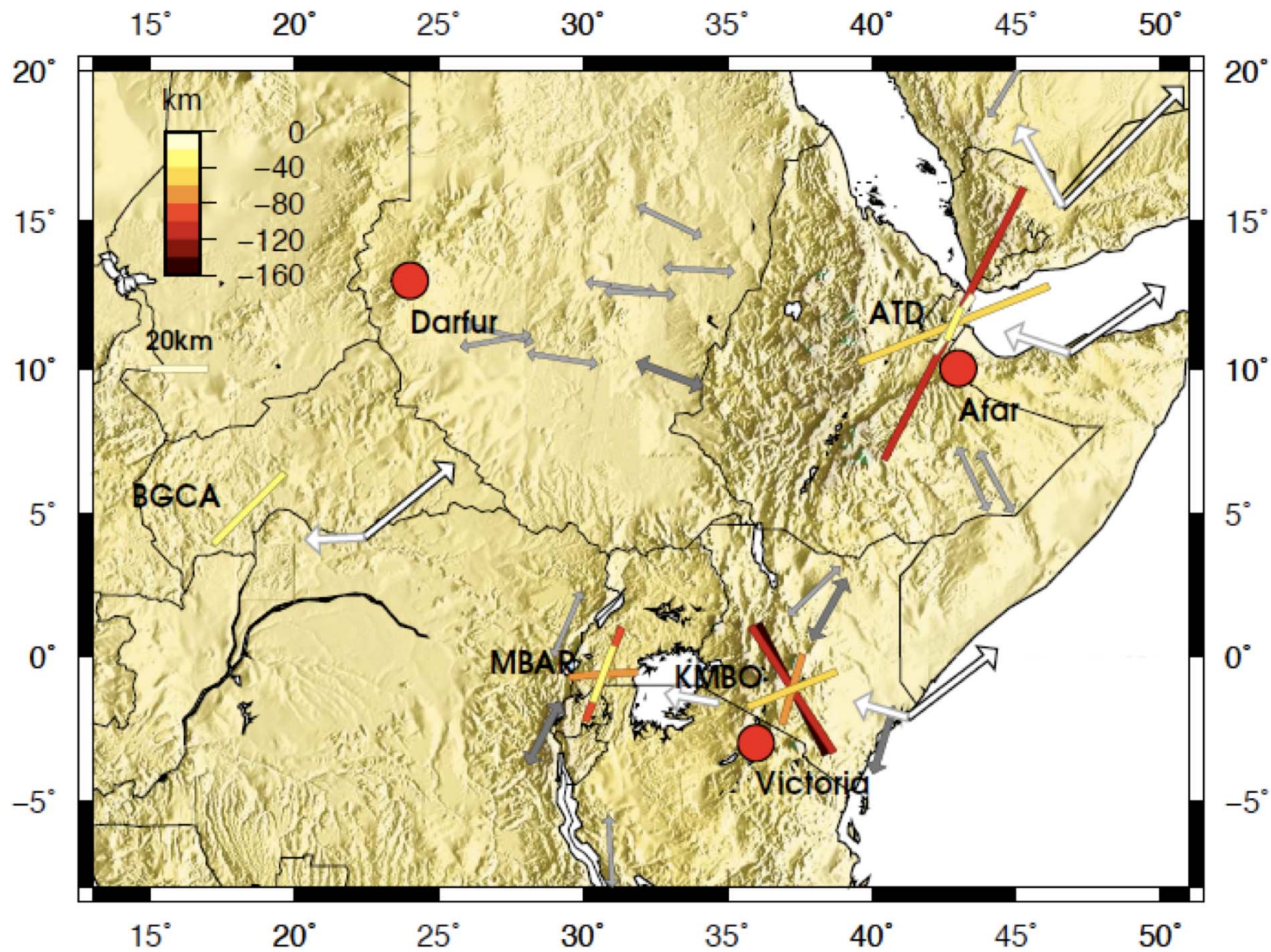


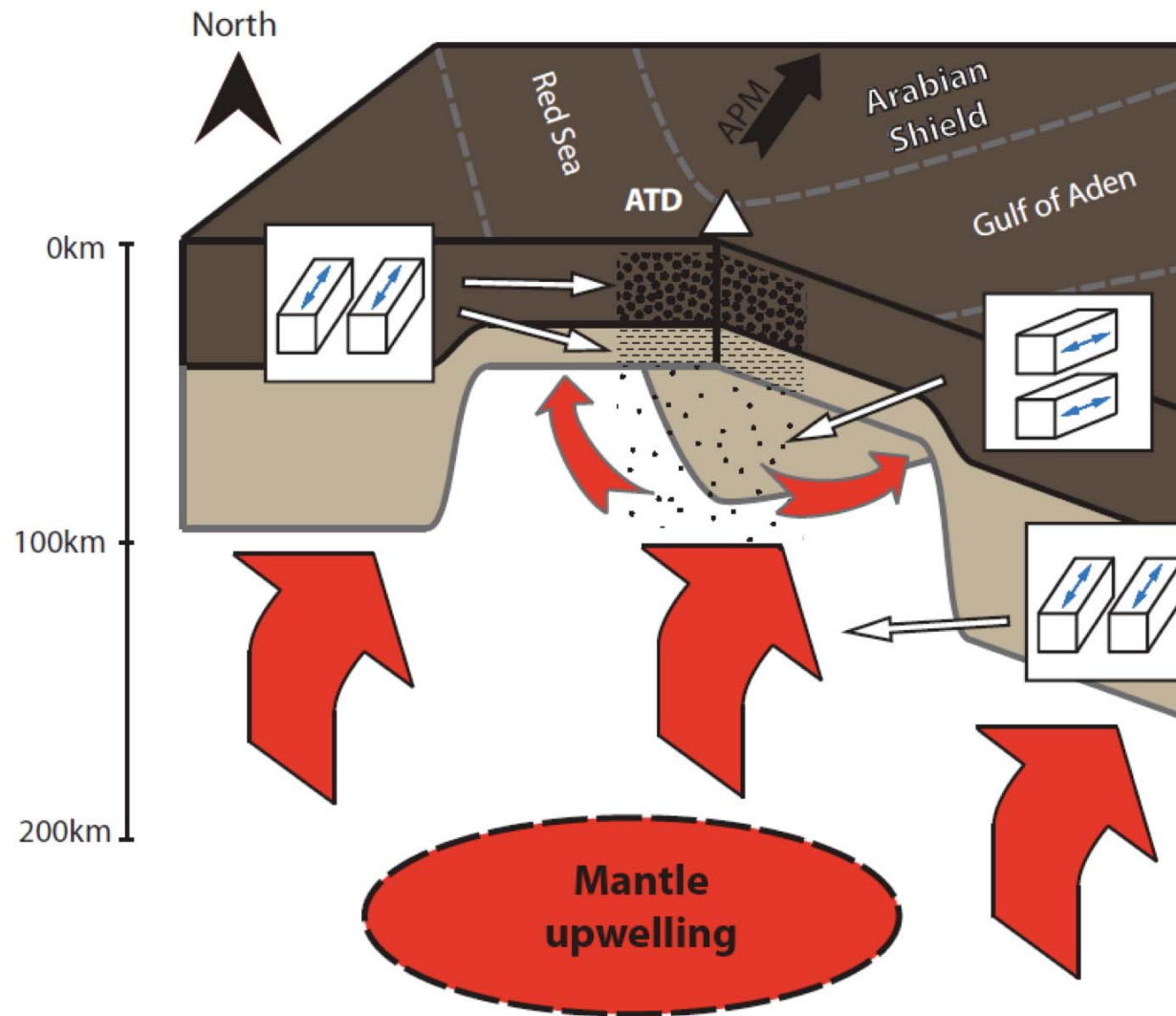
Good Azimuthal Coverage

Simultaneous inversion of SKS and receiver functions

ATD
Station







Tentative tectonic model to explain the stratification of anisotropy around Afar.

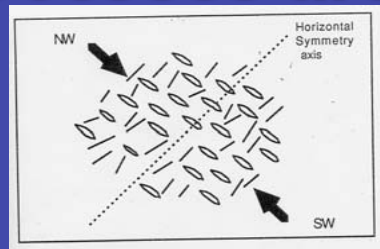
Stratification of anisotropy in The upper mantle is the rule Not the exception

What is the significance of geodynamic
interpretation of SKS splitting data?

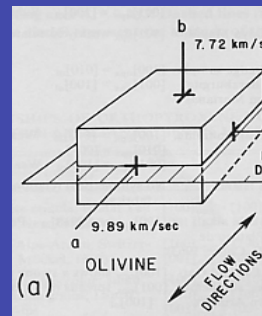
1 δt , 1 angle Ψ ?

Different processes are playing at the same time

-S.P.O.



-L.P.O.



-Water content
-Fine Layering



Conclusions



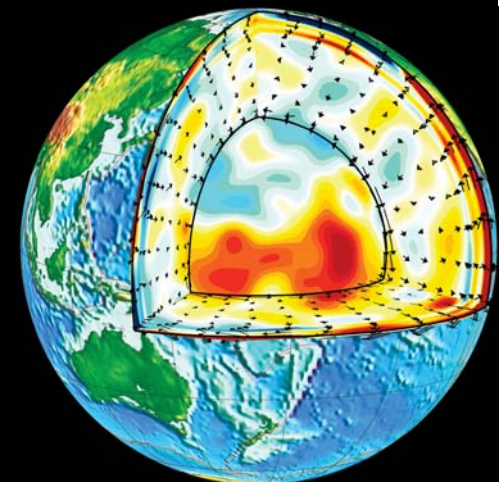
- ❑ Anisotropy: New insight into geodynamic processes.
- ❑ Anisotropy maps mantle flow.
- ❑ For Horn of Africa, anisotropy displays a complex pattern around AFAR and a complex interaction Plume-lithosphere-asthenosphere: Stratification of anisotropy
- ❑ 2 families of plumes have been detected beneath African Continent:
 - Plume from deep in the mantle, transition zone (or lower mantle?): AFAR
 - Babyplumes: consequence of secondary convection (<300km depth): Darfur, Tibesti, Hoggar, Cameroon
- ❑ Central Asia: Deformation processes (Mountain Building)
- ❑ Crustal anisotropy different from lithospheric anisotropy



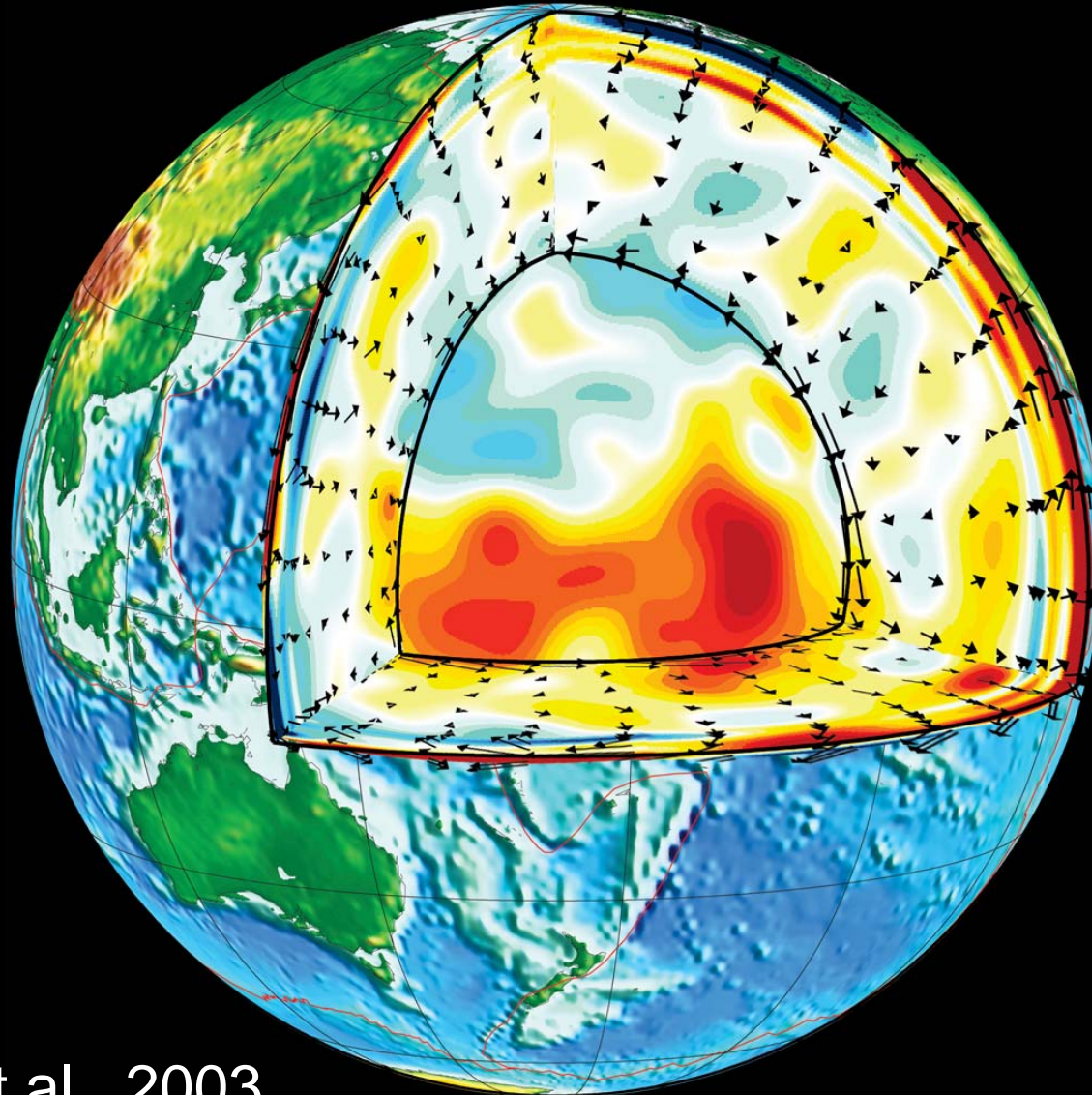
General CONCLUSIONS



- *From Seismic Anisotropy to Anisotropic Seismology*
- Anisotropy is not a second order effect (non-unique interpretation, layering of anisotropy)
- Anisotropy provides new insight into geodynamic issues:
 - Mapping of mantle convection (detection of boundary layers)
 - Plume- lithosphere- asthenosphere interactions
 - Indirect detection of upwellings in the upper mantle.
 - Deformation processes (Mountain Building)
 - Continental and oceanic lithosphere thickness



Seismic tomography: Instantaneous image Anisotropy- Geodynamics Relationship



Gaboret et al., 2003

CONCLUSIONS

- Progress in instrumentation (Dense networks, Ocean bottom, Planet Mars; Spatial exploration)
- Ray Theory - Normal Modes -> Numerical Methods more and more powerful and accurate by using more and more powerful computers.
- From Global scale towards regional scale:
Incorporation of new parameters (anisotropy, anelasticity) in tomography
Finite-frequency effects
- Systematic Multidisciplinary Approach: Confrontation of seismological results with numerical and laboratory experiments