



The Abdus Salam
International Centre for Theoretical Physics



2234-5

**Meeting of Modern Science and School Physics: College for School
Teachers of Physics in ICTP**

27 April - 3 May, 2011

Quest to absolute zero and Bose condensation

Alexandre Bouzdine
University of Bordeaux
France

QUEST TO ABSOLUTE ZERO AND BOSE-EINSTEIN CONDENSATION

A. Buzdin

*Condensed Matter Theory Group, University of
Bordeaux I
and Institut Universitaire de France*



**Meeting of Modern Science and School Physics,
ICTP, Trieste, Italy
27 April - 3 May, 2011**

TEMPERATURE

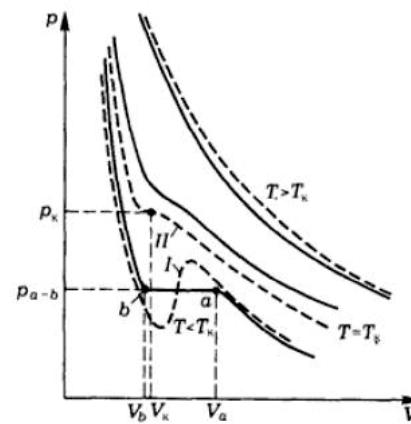
$$\left(\frac{mv^2}{2}\right) = k_B T$$

$$k_B = 1.380\,6504 \times 10^{-23} \text{ J K}^{-1}$$

$$pV = NkT$$

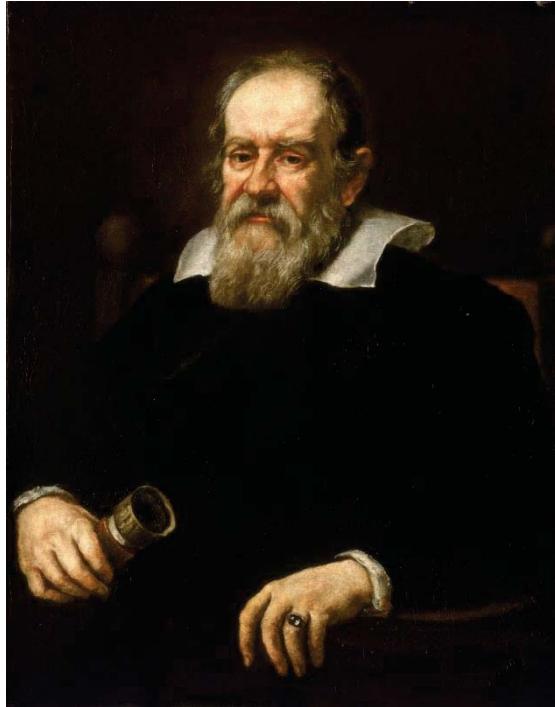


Boltzmann



First thermometers - thermoscopes

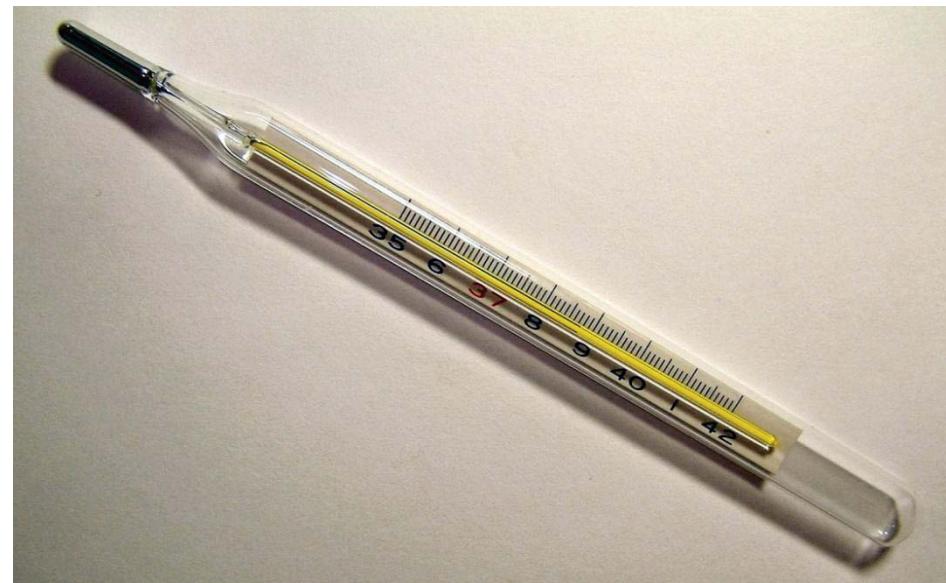
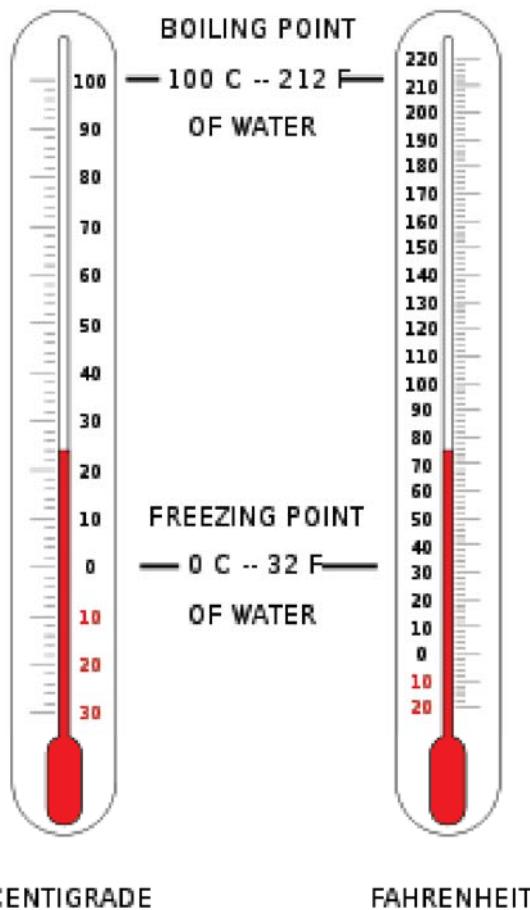
First thermometers - thermoscopes

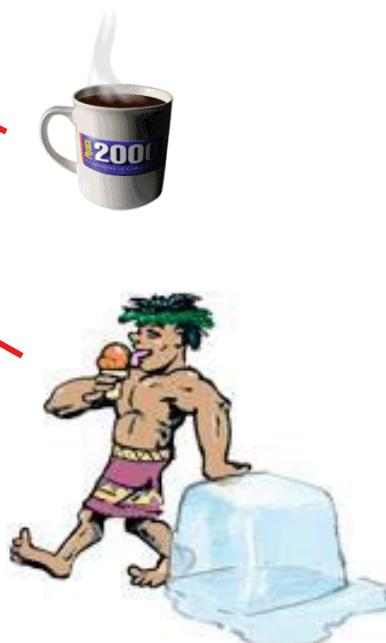
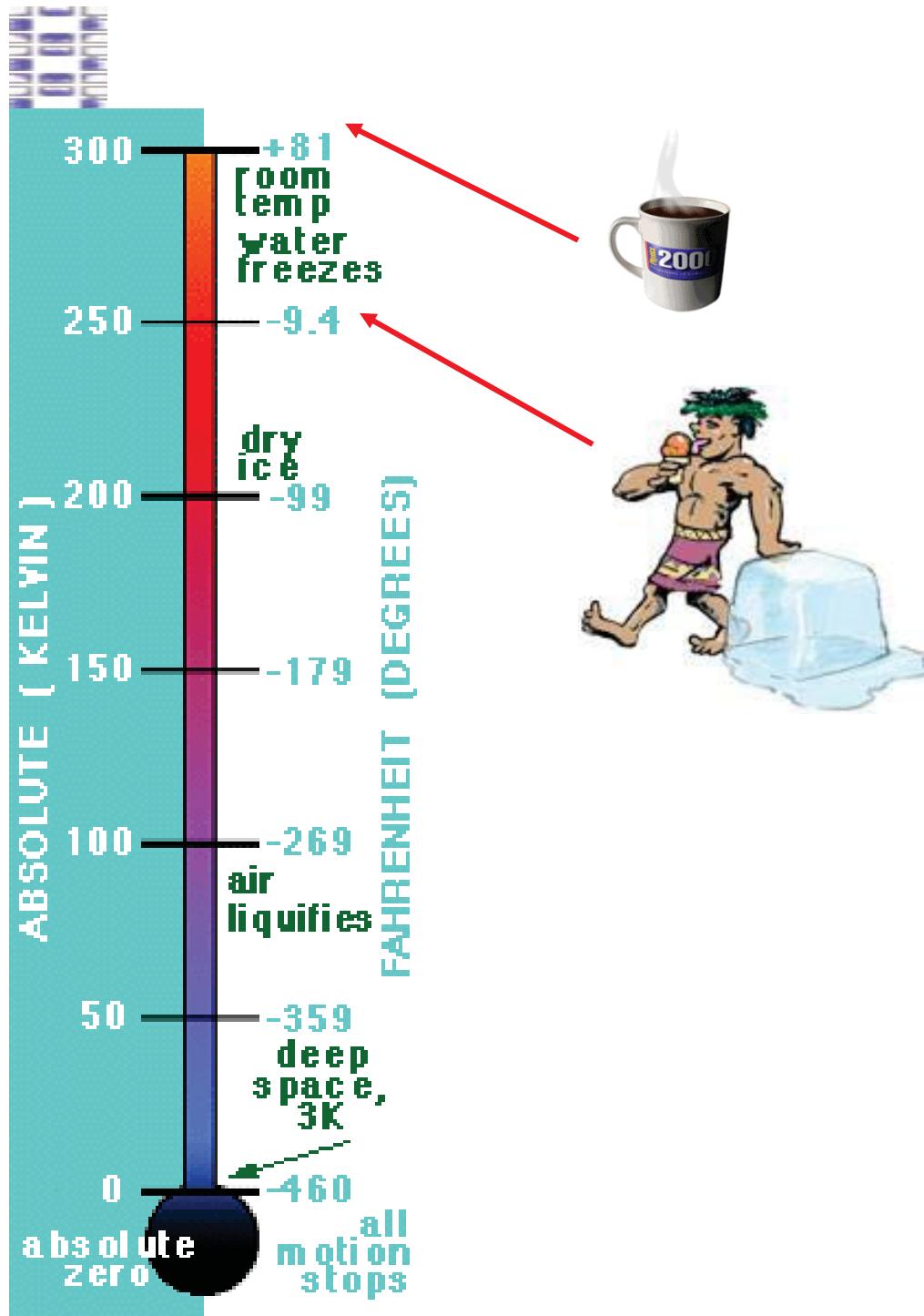


Galileo Galilei (1564 – 1642)

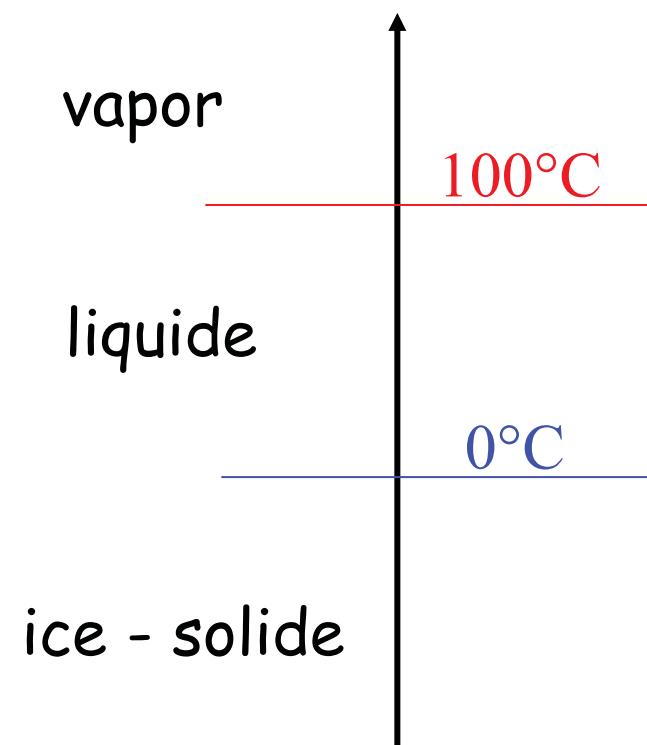


Thermometers

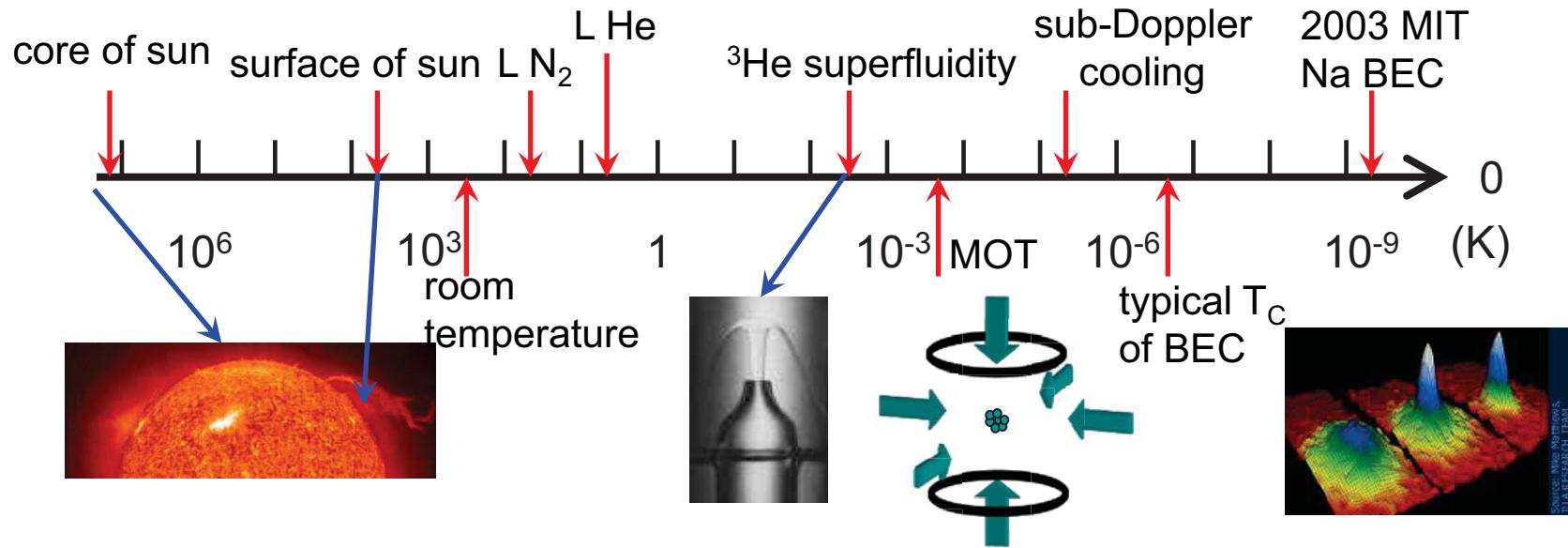




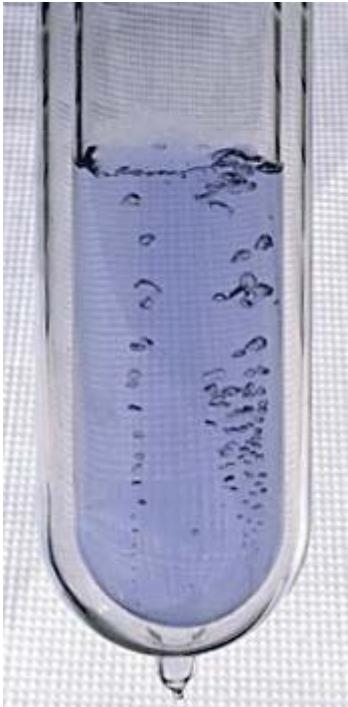
Water



Temperature scale



By 1845, [Michael Faraday](#) had managed to liquefy most permanent gases then known to exist.



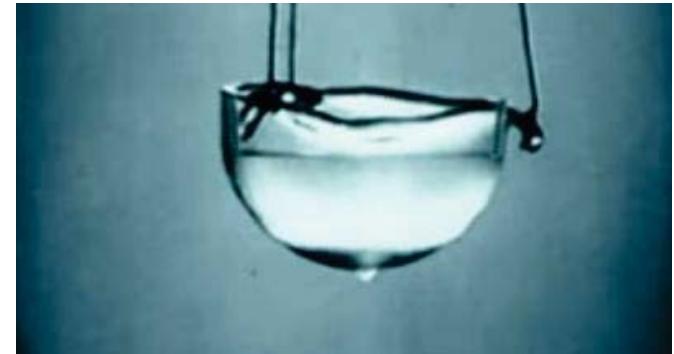
In 1877, [Louis Paul Cailletet](#) (1832–1913) in France and [Raoul Pictet](#) (1846–1929) in Switzerland succeeded in producing the first droplets of liquid air.



Nitrogen was first liquefied at the [Jagiellonian University](#) on 15 April 1883 by Polish physicists, [Zygmunt Wróblewski](#) and [Karol Olszewski](#).

Quest to liquefy Helium

Helium-4 was first liquefied on 10 July 1908 by Dutch physicist [Heike Kamerlingh Onnes](#).



Properties of liquid helium	Helium-4	Helium-3
<u>Critical temperature</u>	5.2 K	3.3 K
<u>Boiling point at 1 atm</u>	4.2 K	3.2 K
<u>Minimum melting pressure</u>	25 atm	29 atm at 0.3 K
<u>Superfluid transition temperature at saturated vapor pressure</u>	2.17 K	1 m K in zero magnetic field

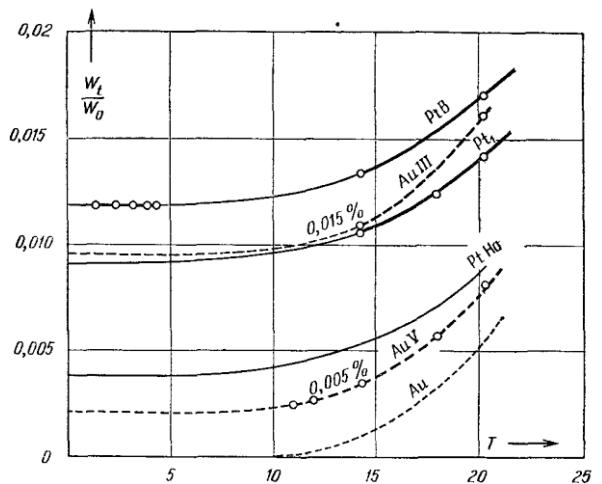


Рис. 4.3. Сопротивление двух образцов из платины и двух — из золота (тонкие пунктирные линии для образцов из золота — экстраполяция) [Commun. Phys. Lab. Univ. Leiden, № 119 (1911), лист III рис. 3]

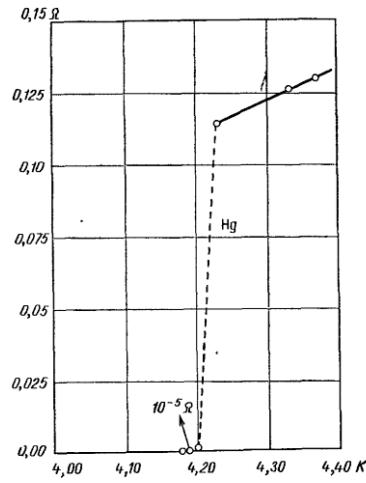
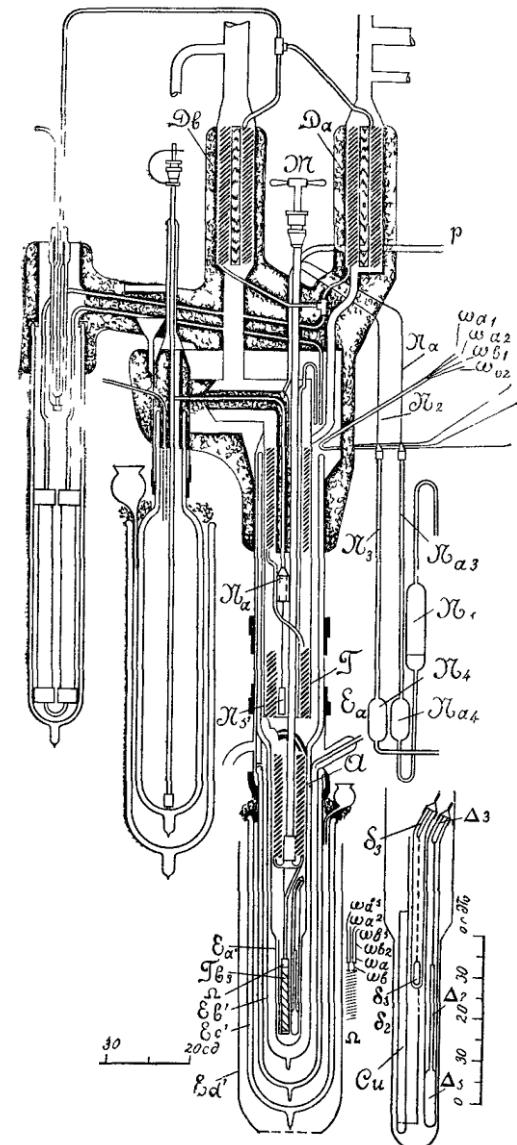
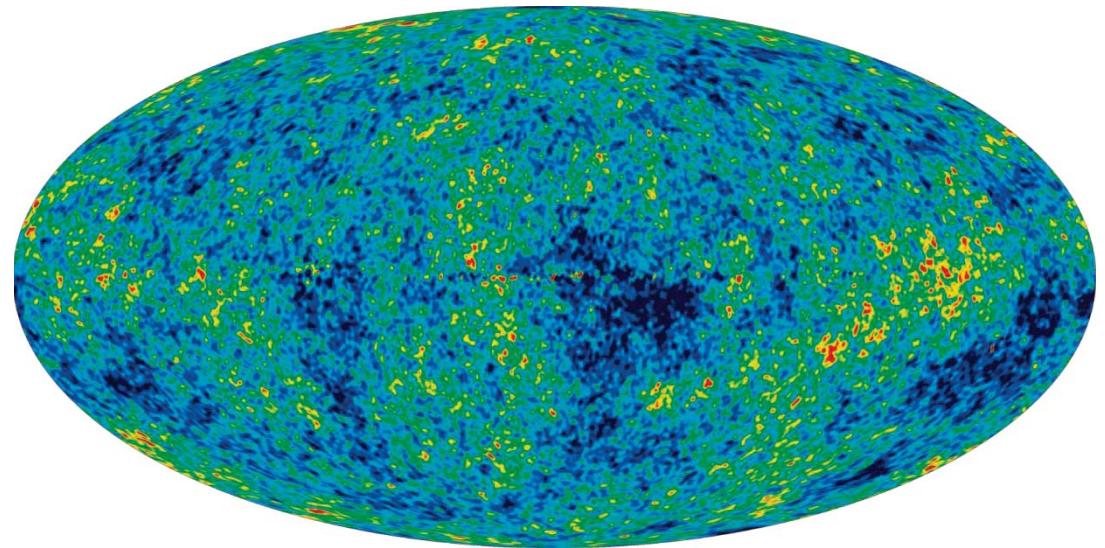
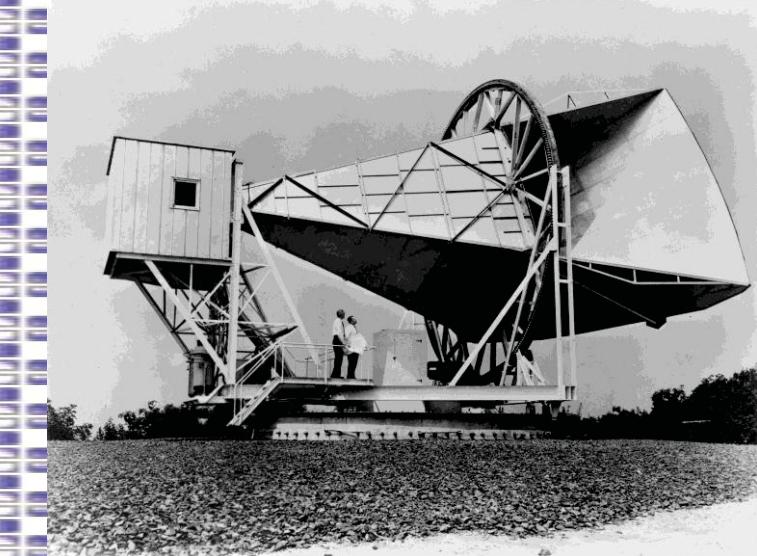


Рис. 4.5. Зависимость сопротивления образца ртути от температуры [Commun. Phys. Lab. Univ. Leiden, № 124 (1912), стр. 23, рис. без номера].



Physics of low temperature was born !

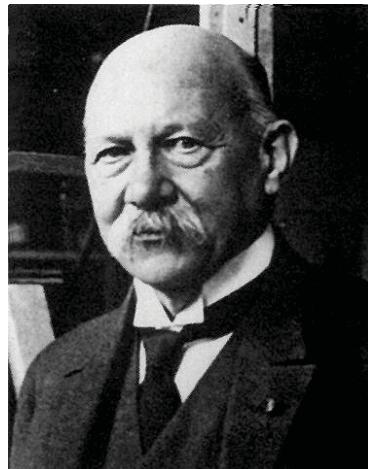


cosmic microwave background radiation
has a thermal black body spectrum at a temperature of 2.725 K

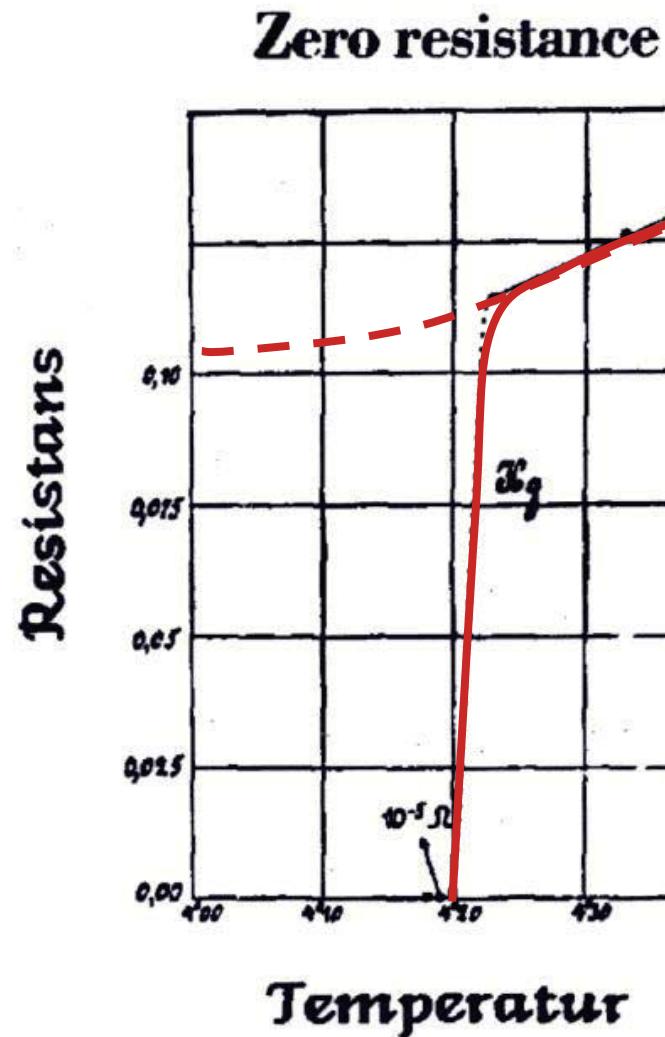
Arno Allan Penzias and Robert Woodrow Wilson

We may have the temperature below 2.7 K only in our laboratories.

1911: discovery of superconductivity

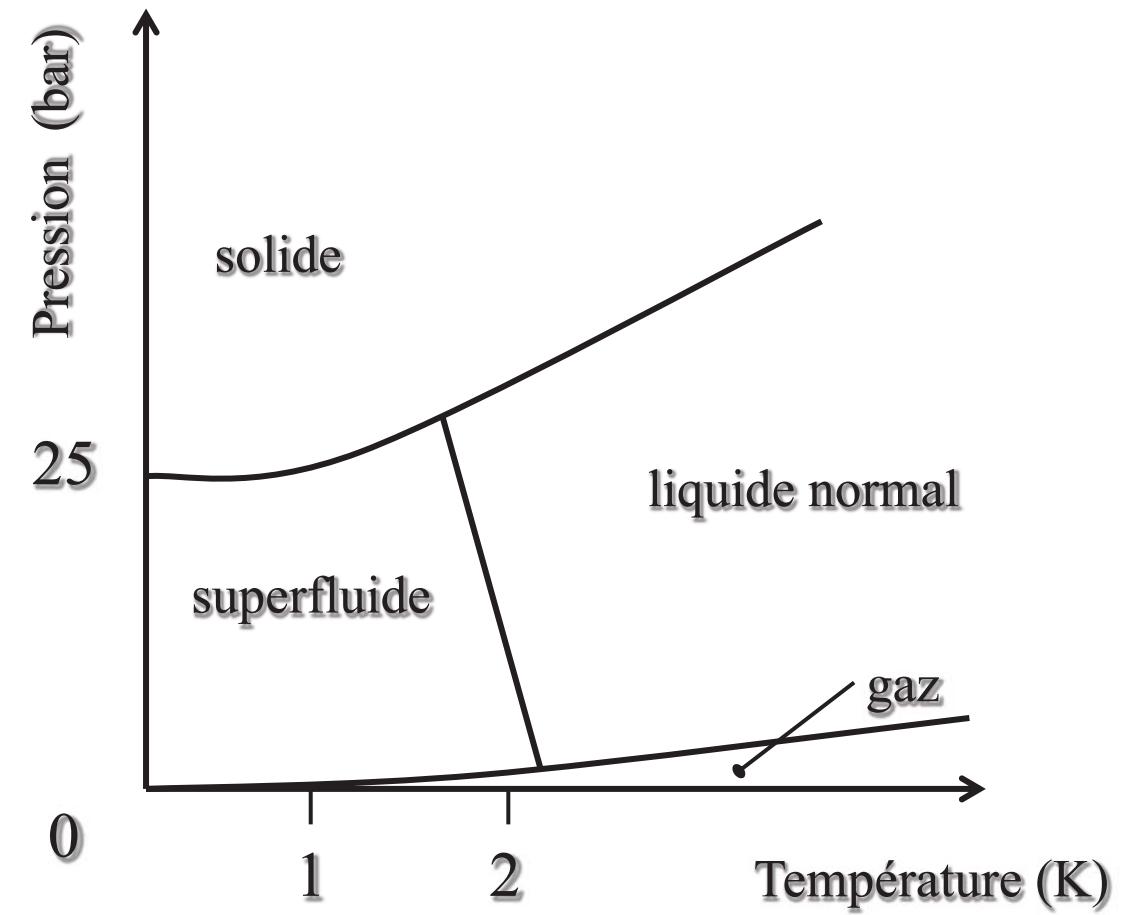


- Discovered by **Kamerlingh Onnes** in 1911 during first low temperature measurements to liquefy helium
- Whilst measuring the resistivity of “pure” Hg he noticed that the electrical resistance dropped to zero at 4.2K
- In 1912 he found that the resistive state is restored in a magnetic field or at high transport currents



1913

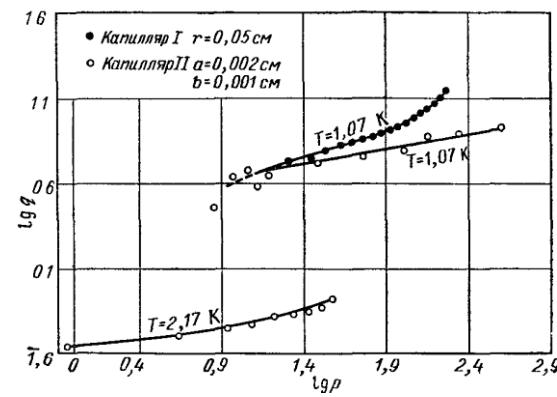
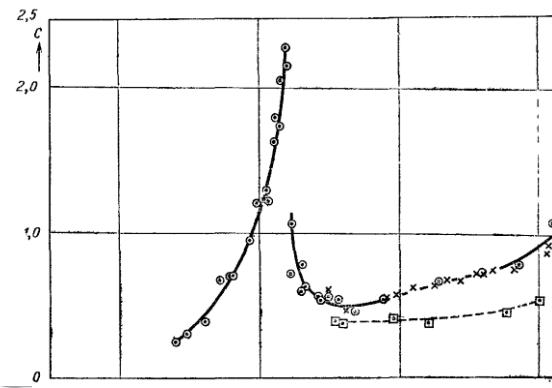
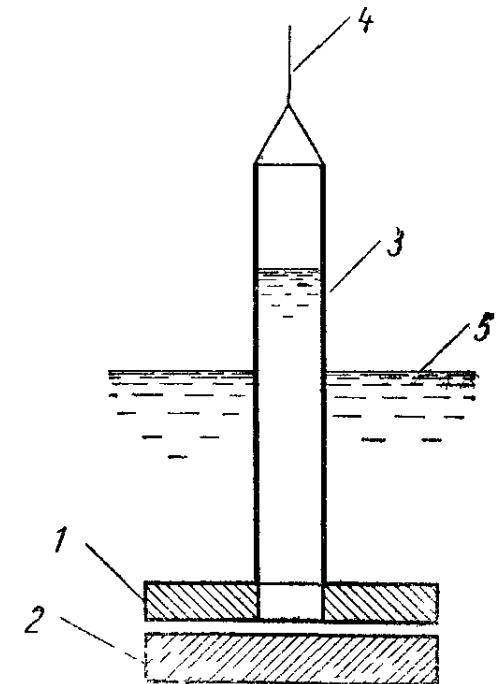
Phase diagram of He



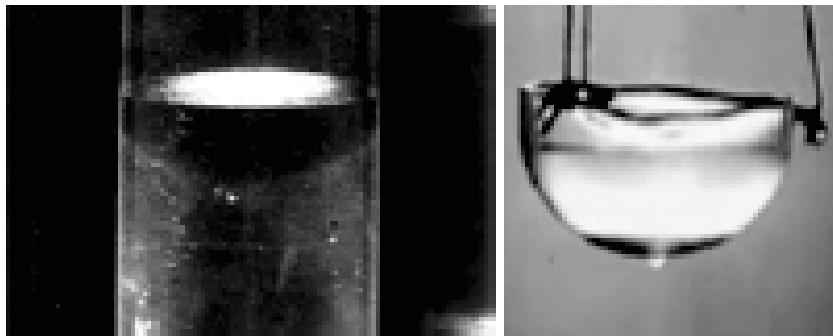
1937: Superfluidity of liquid He₄



Piotr Kapitza

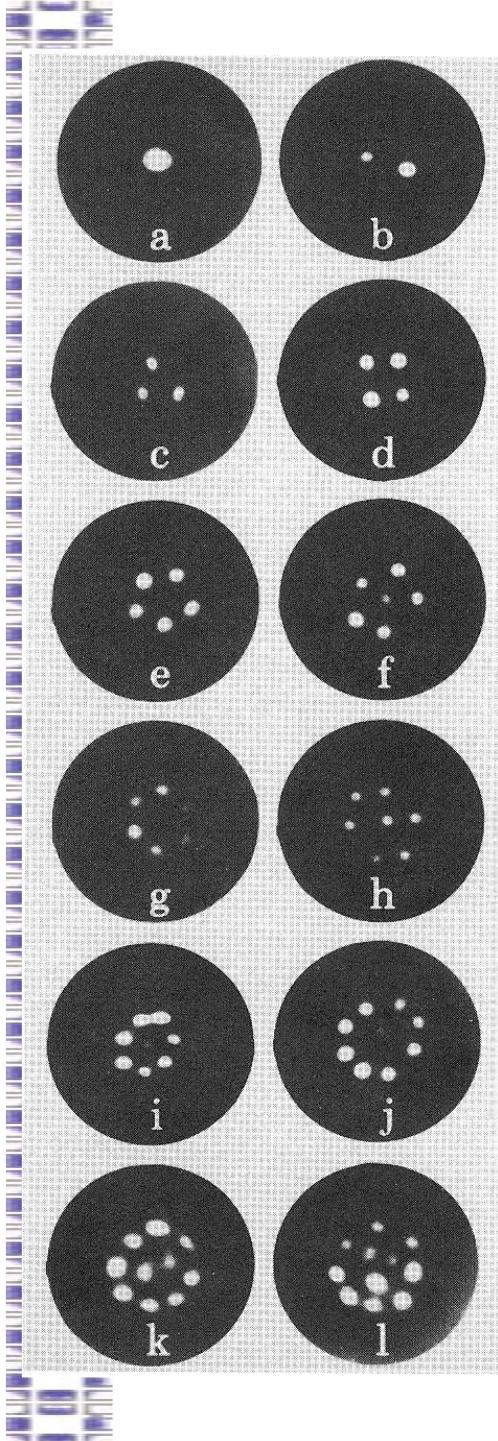


1978



*Superfluidity in liquid Helium at 2.17?K, fluid without viscosity:
No bubbles, no movement of liquid
during circulation of its container*





Rotaion of superfluid: vortices

helium

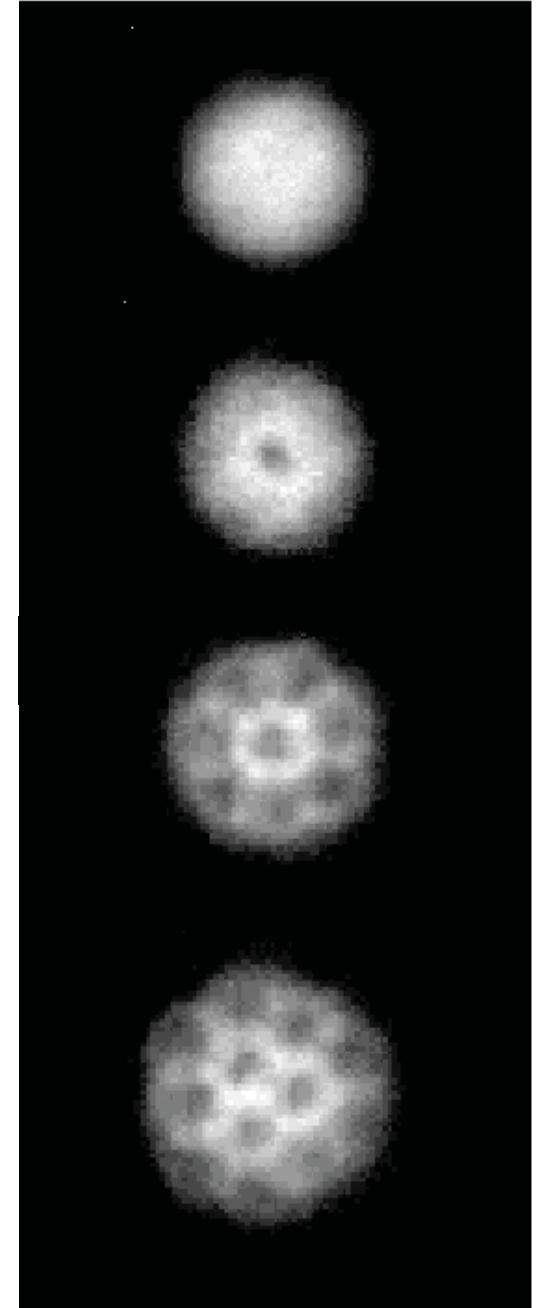
at 1979 :

*E.J. Yarmchuk,
M.J.V. Gordon et
R.E. Packard*

*et le rubidium
gazeux*

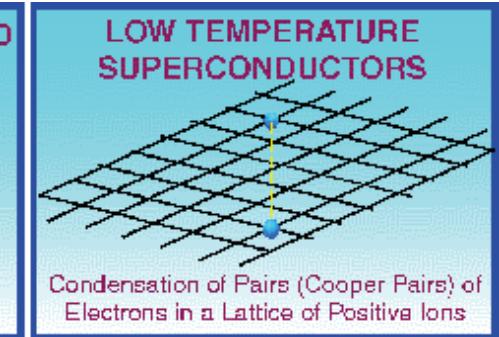
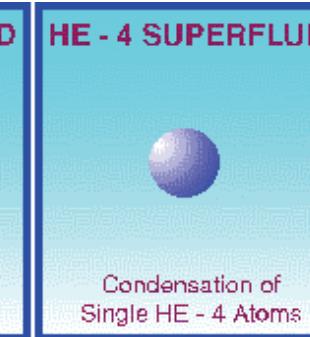
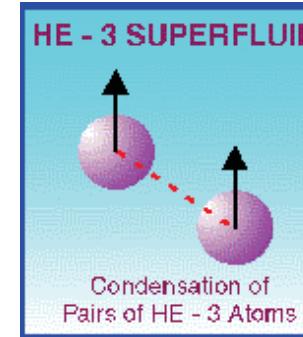
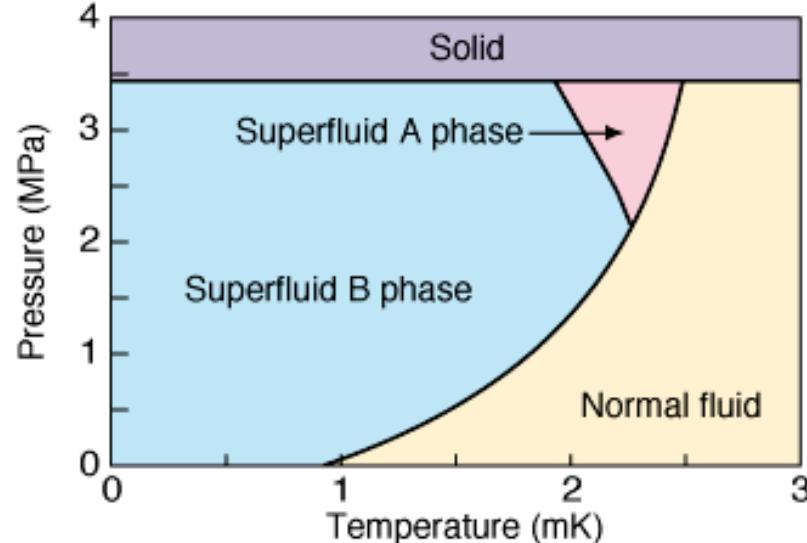
en 2000 :

*KW Madison,
F. Chevy, W.
Wohlleben et
J. Dalibard*





1973: Superfluidity in liquid He₃



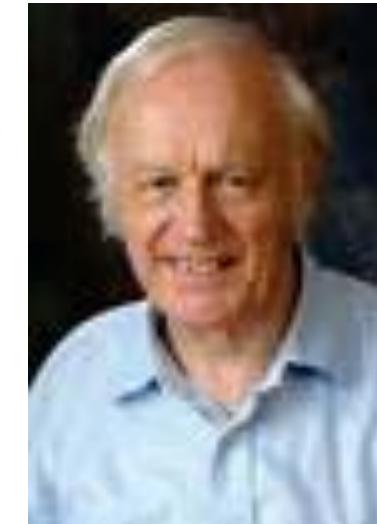
David M. Lee, **Douglas Dean**
Osheroff and Robert C. Richardson

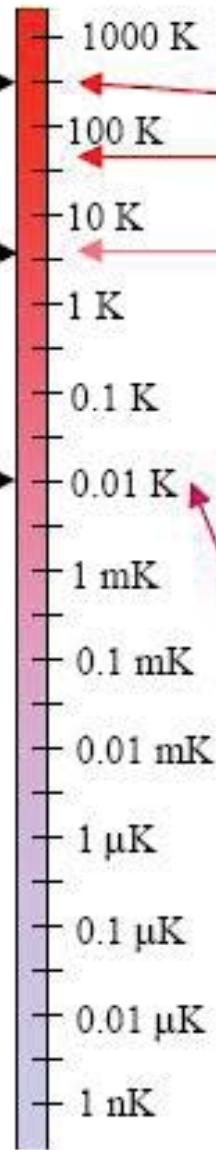


1996



2003





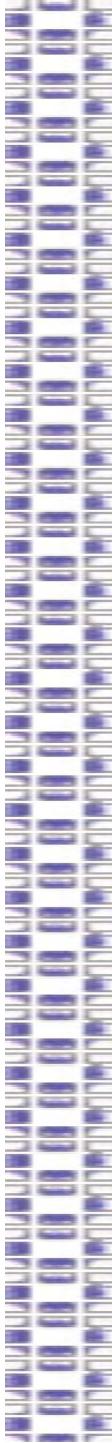
Glace: 273 K



azote liquide: 77 K



Hélium liquide: 4 K



1000 K

100 K

10 K

1 K

0.1 K

0.01 K

1 mK

0.1 mK

0.01 mK

1 μ K

0.1 μ K

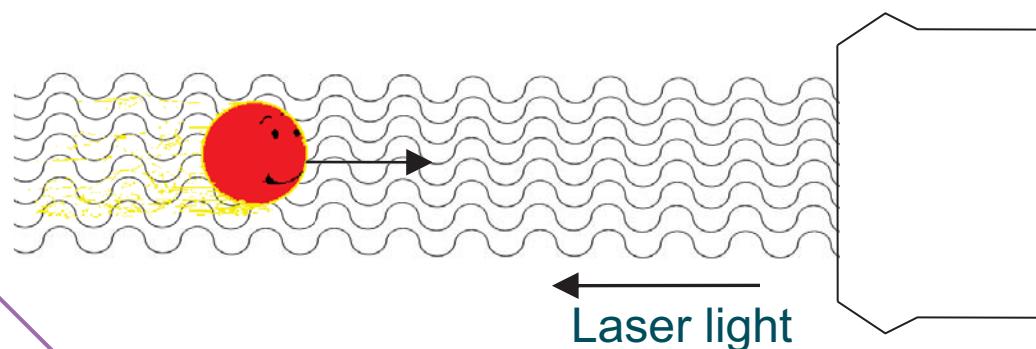
0.01 μ K

1 nK

Laser cooling



Chu, Cohen-Tannoudji et
Phillips – Nobel Prize 1997
*"for development of methods
to cool and trap atoms with
laser light".*

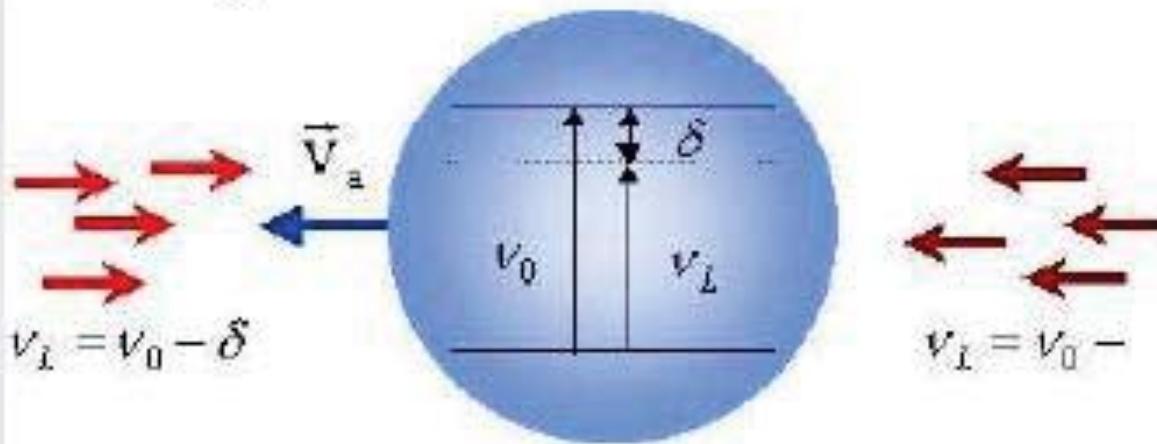


10-100 microkelvin
 $= 0.00001 - 0.0001 \text{ K}$

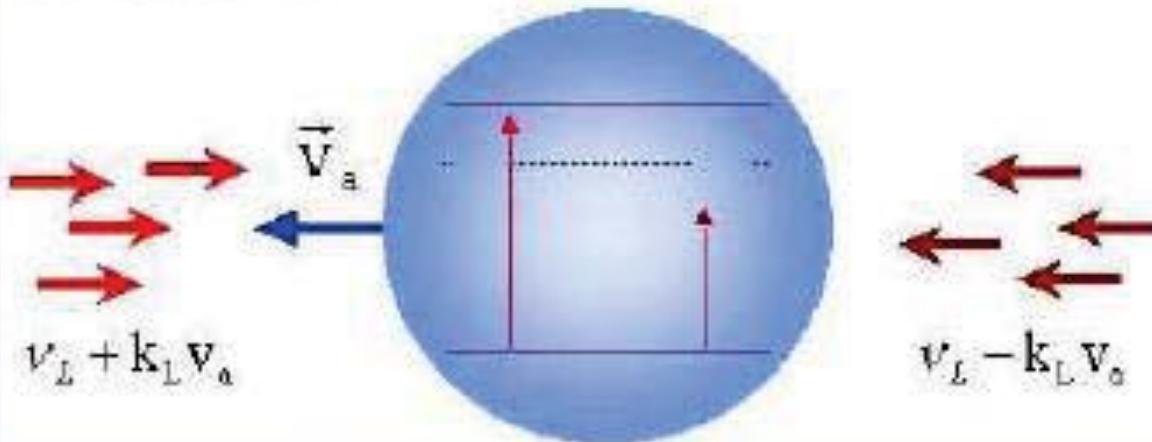
[demo](#)

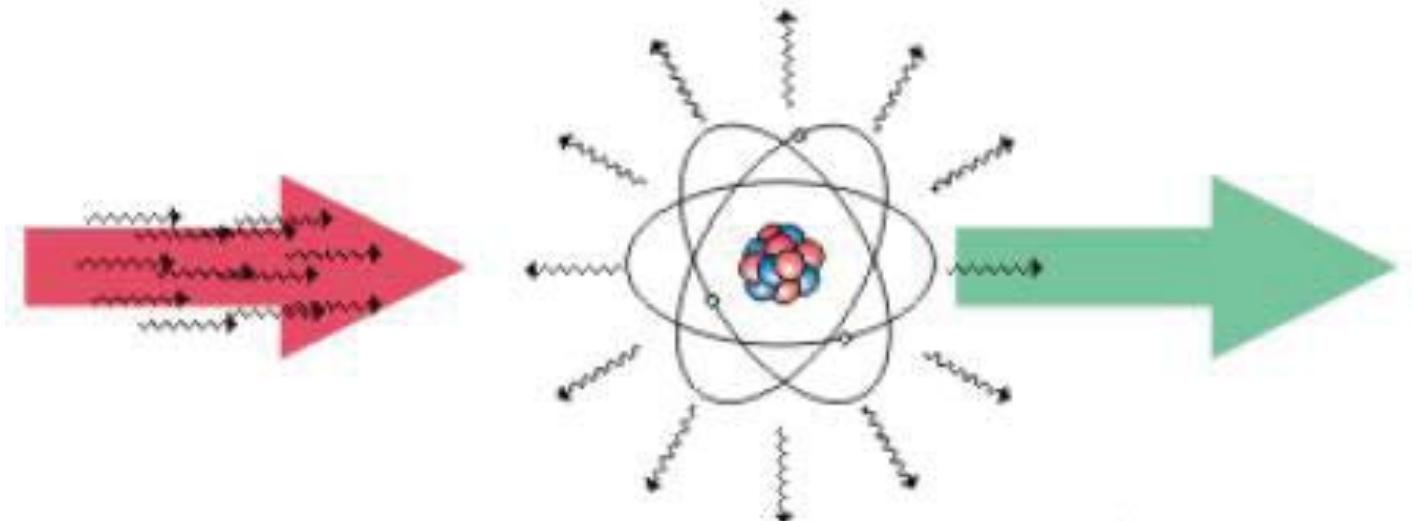
Laser cooling

Laboratory Frame



Atomic Frame



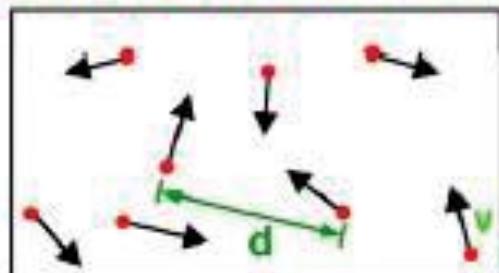


Incident photons absorbed:
momentum transfer = $\hbar k$

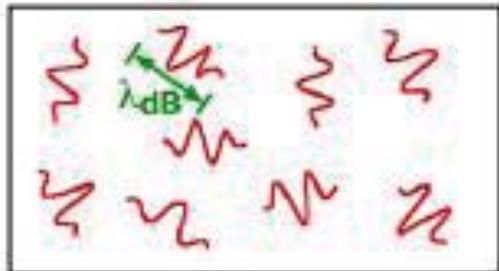
Spontaneous emission: total
momentum transfer = 0

Net momentum
transfer to atom in
direction of laser

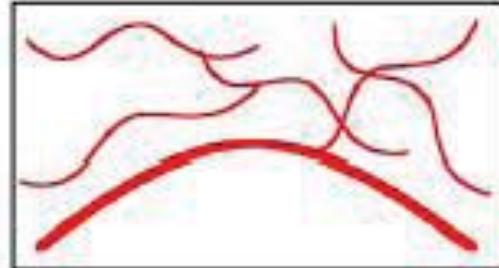
What is Bose-Einstein condensation (BEC)?



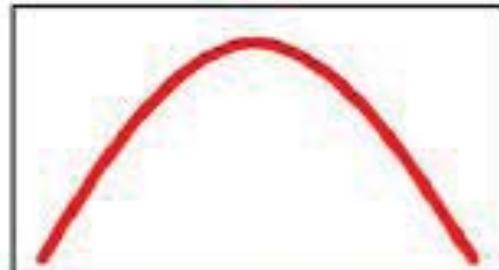
High Temperature T:
thermal velocity v
density d^{-3}
"Billiard balls"



Low Temperature T:
De Broglie wavelength
 $\lambda_{dB} = h/mv \propto T^{-1/2}$
"Wave packets"



T=T_{crit}:
Bose-Einstein Condensation
 $\lambda_{dB} \approx d$
"Matter wave overlap"



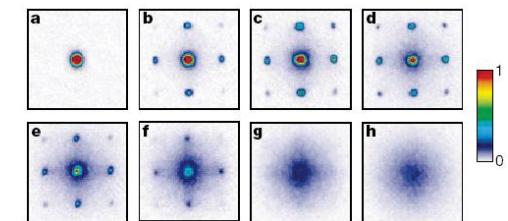
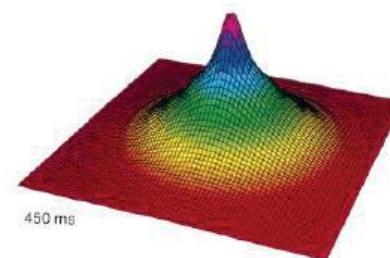
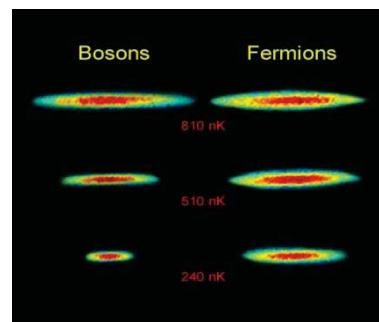
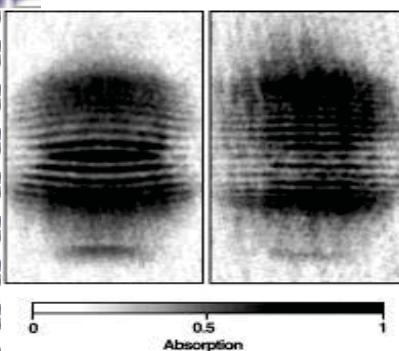
T=0:
Pure Bose condensate
"Giant matter wave"

$$\lambda = \frac{h}{\sqrt{2\pi mkT}}$$

$$T_c = \left(\frac{n}{\zeta(3/2)} \right)^{2/3} \frac{2\pi\hbar^2}{mk_B} \approx 3.31 \frac{\hbar^2 n^{2/3}}{mk_B}$$

Particles are transformed to waves...

- World of Quantum Mechanics
 - Wave nature of matter, interference, tunneling, resonance
$$\lambda = h/\sqrt{2\pi m k_B T} \sim 1\mu\text{m} \text{ for Na @ 100nK}$$
 - Quantum statistics
 - Uncertainty principle, zero-point energy
 - Quantum phase transition



Experimental observation of Bose-Einstein condensation



E. Cornell,



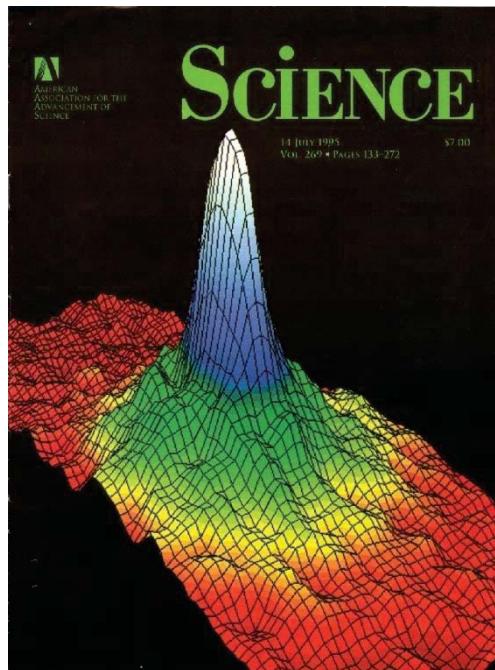
Nobel Prize 2001
W. Ketterle and C. Wieman



"for the achievement of Bose-Einstein condensation in dilute gases of alkali atoms, and for early fundamental studies of the properties of the condensates"

The first condensates at en 1995

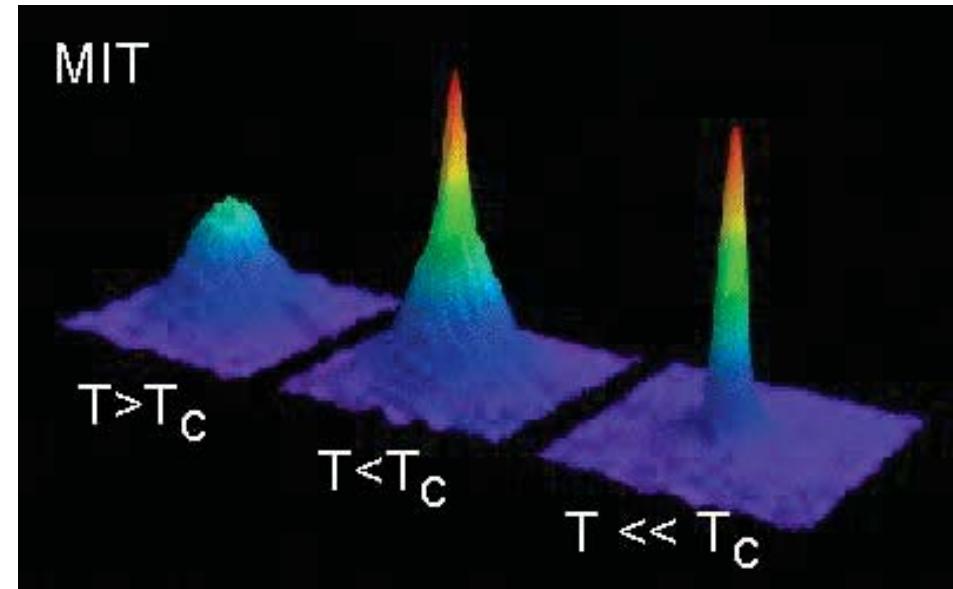
$T_c \sim 0,0000001$ K !!!!!!!



Rubidium

C. Wieman et E. Cornell

Boulder, Colorado

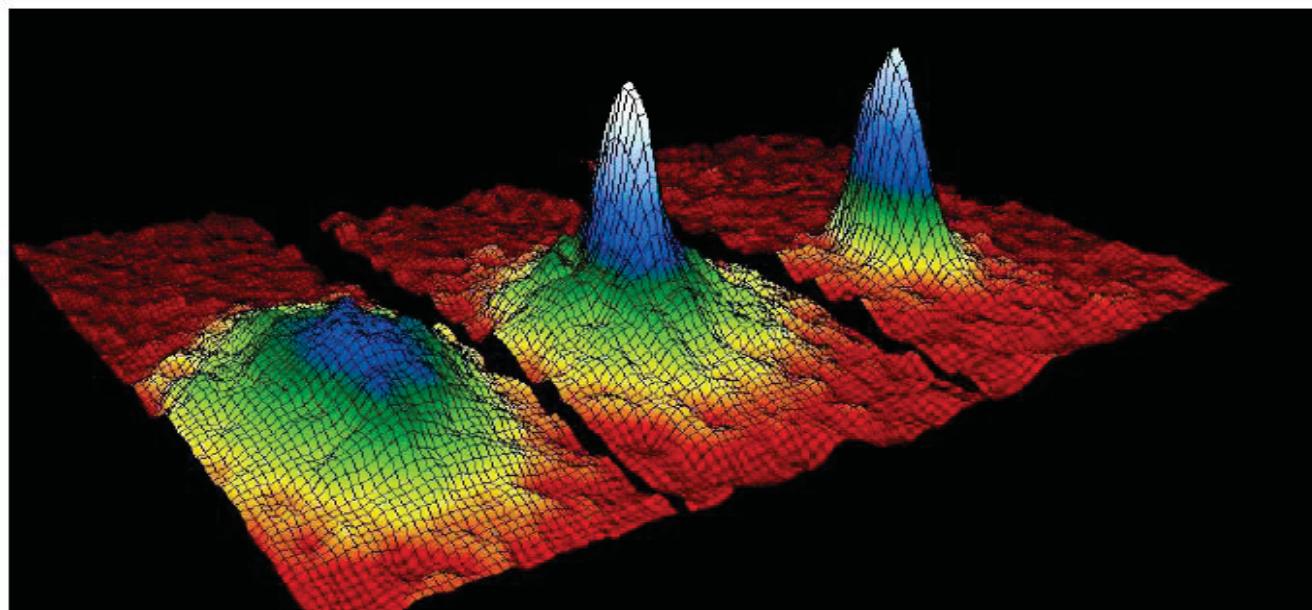


Sodium

W. Ketterle

MIT

Bose-Einstein condensation of weakly interacting atoms



Typical distance between atoms 300 nm
Typical scattering length 10 nm

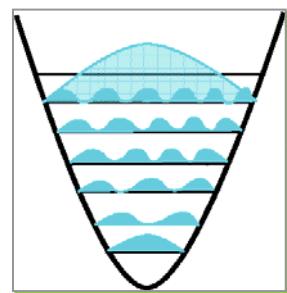
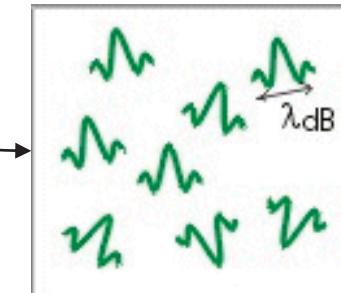
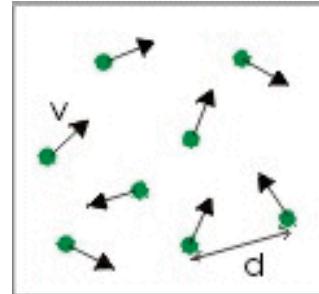
$$T_{\text{BEC}} \sim 1 \mu\text{K}$$

Scattering length is much smaller than characteristic interparticle distances.
Interactions are weak

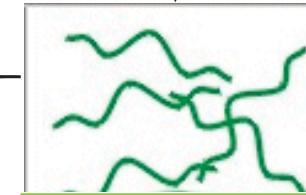
Atomic gases



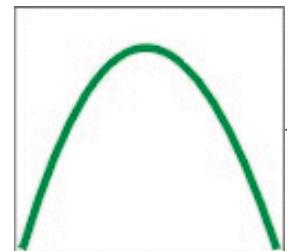
Theory of ideal classic gaz



Das Pauli-verbot



$\Delta p \cdot \Delta x > \hbar$



Condensation of non interacting atoms

© Falguni Salkar



↑
S.N. Bose and other Bosons

Bose-Einstein condensate

$T < T_c$



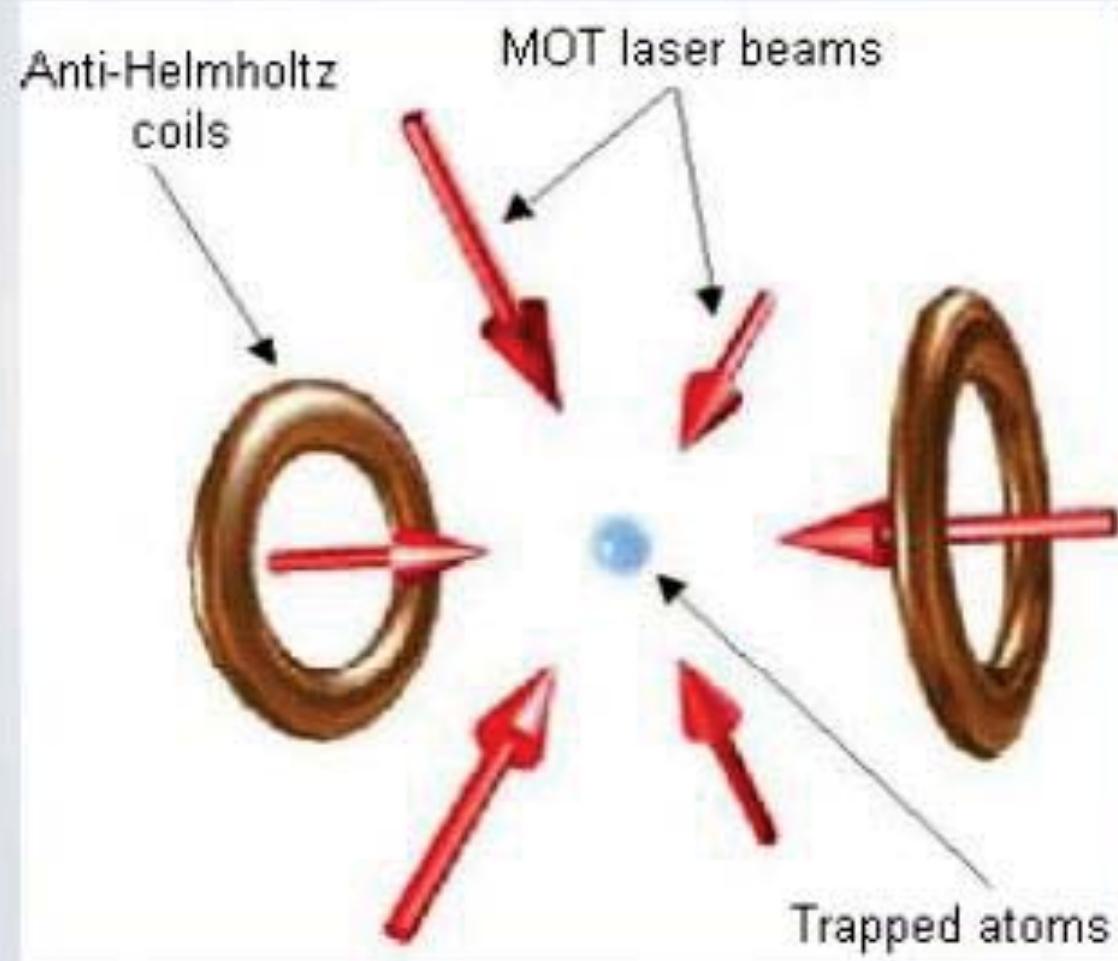
$T > T_c$

vs.



cf. le laser atomique

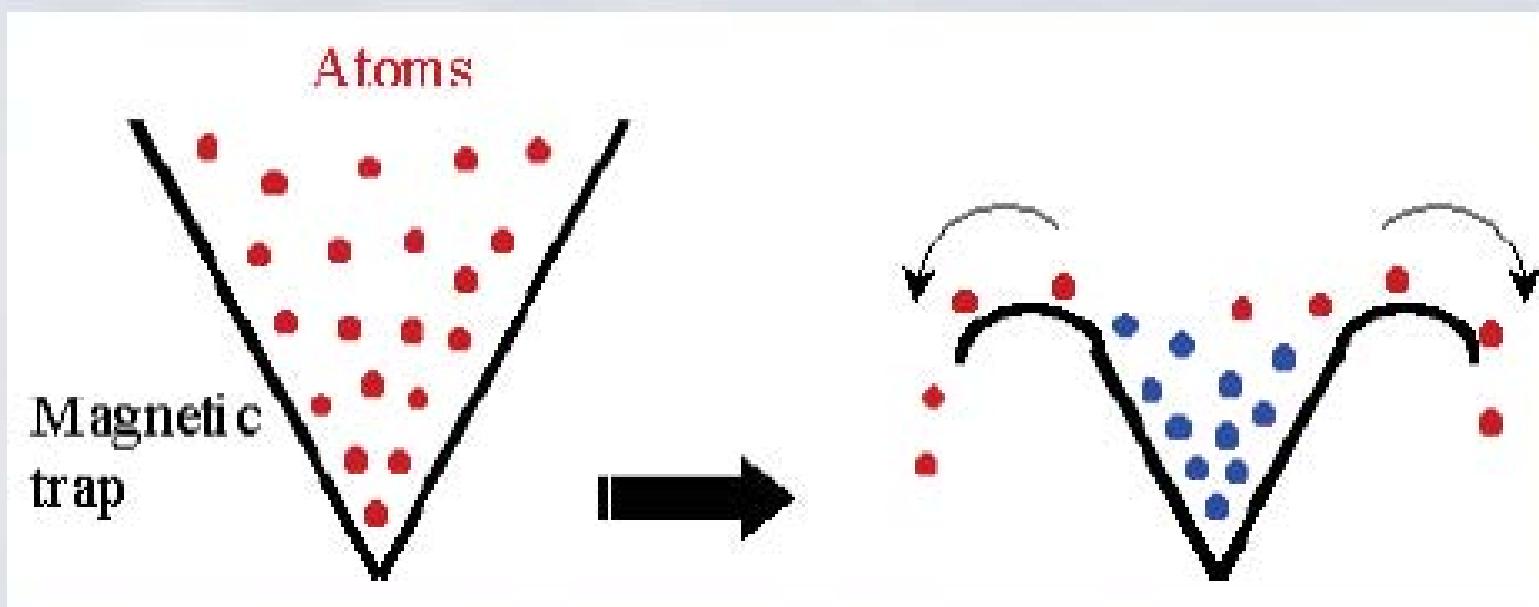
Magneto-Optical trap



Evaporative Cooling



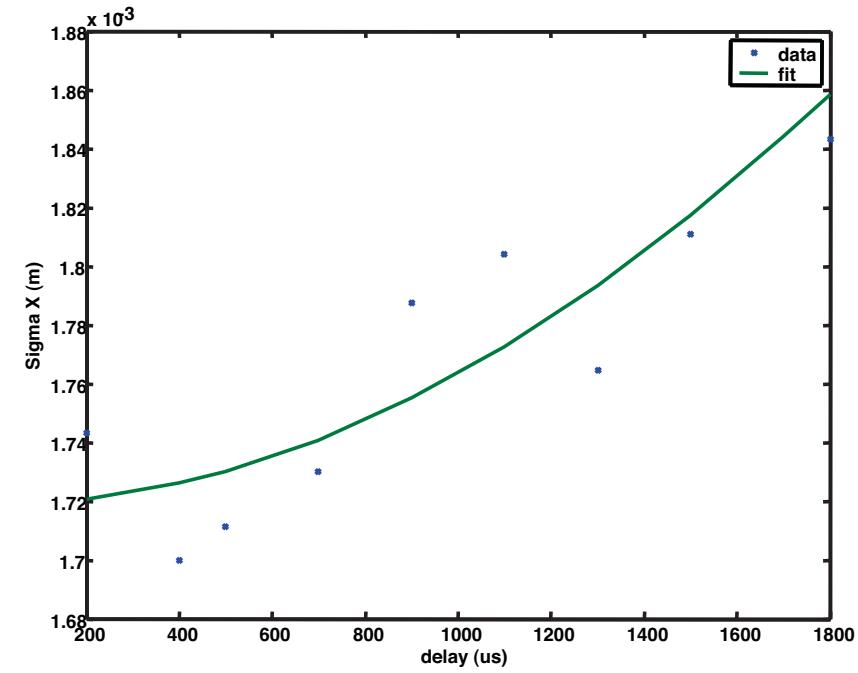
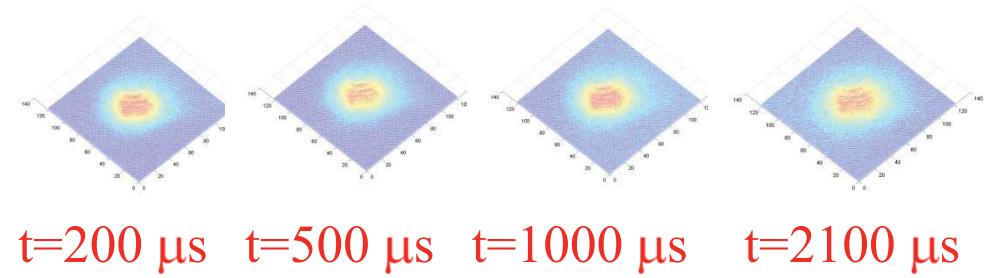
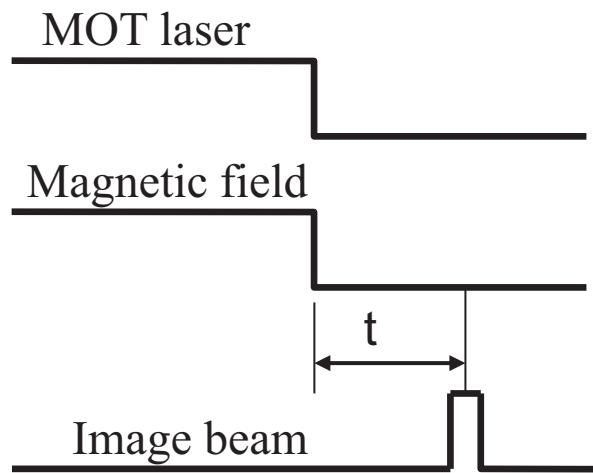
Magnetic Evaporative cooling



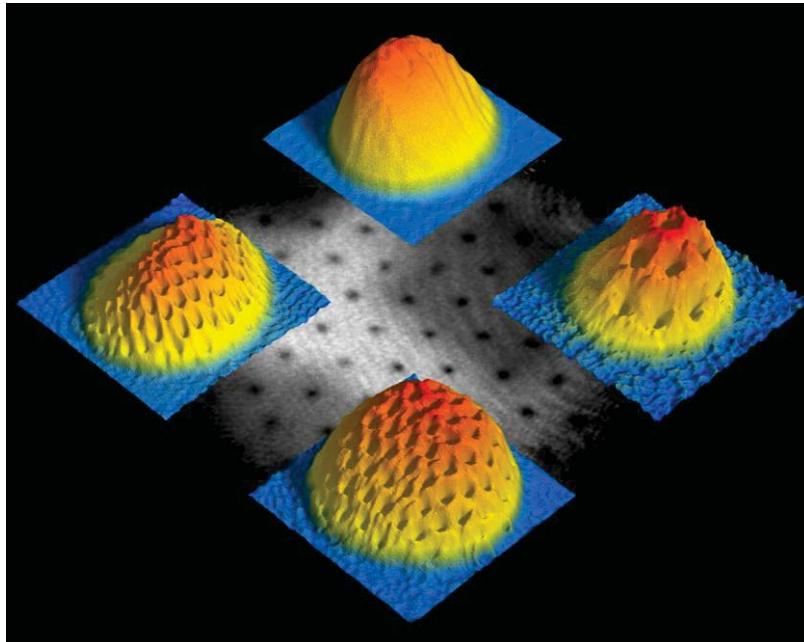
How to determine the temperature?

$$\sigma^2(t) = \sigma_0^2 + V^2 t^2$$

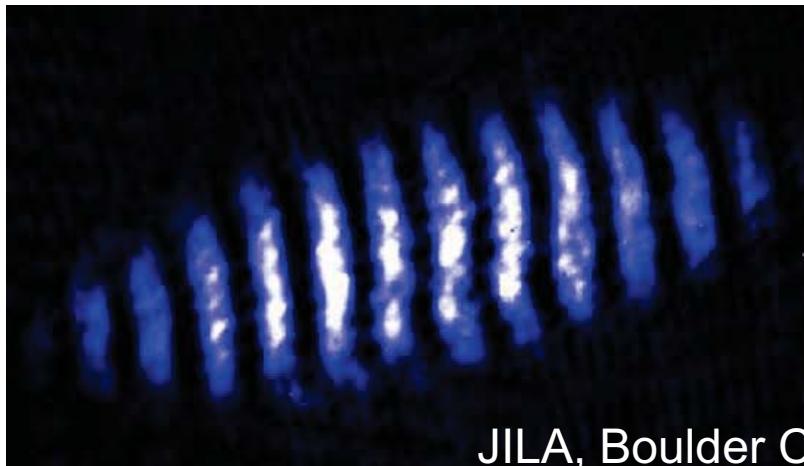
$$V = \sqrt{\frac{2k_B T}{m}}$$



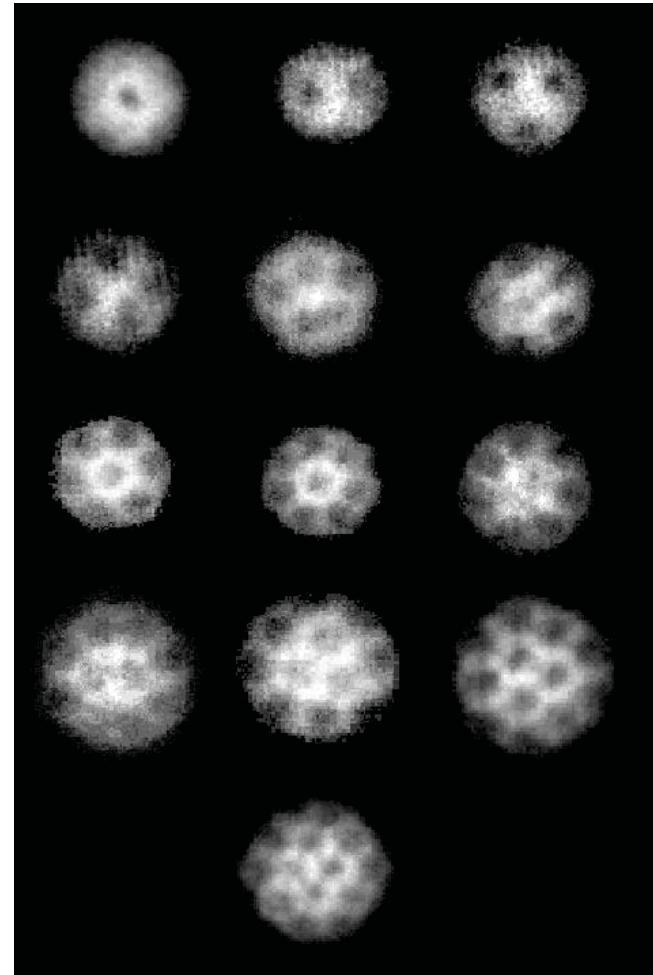
Rotating condensate and vortices



MIT, Cambridge MA, USA

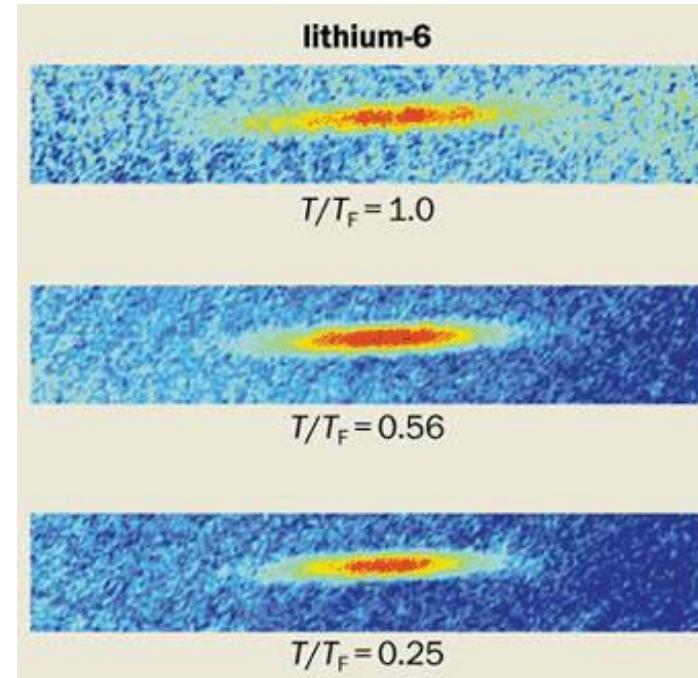
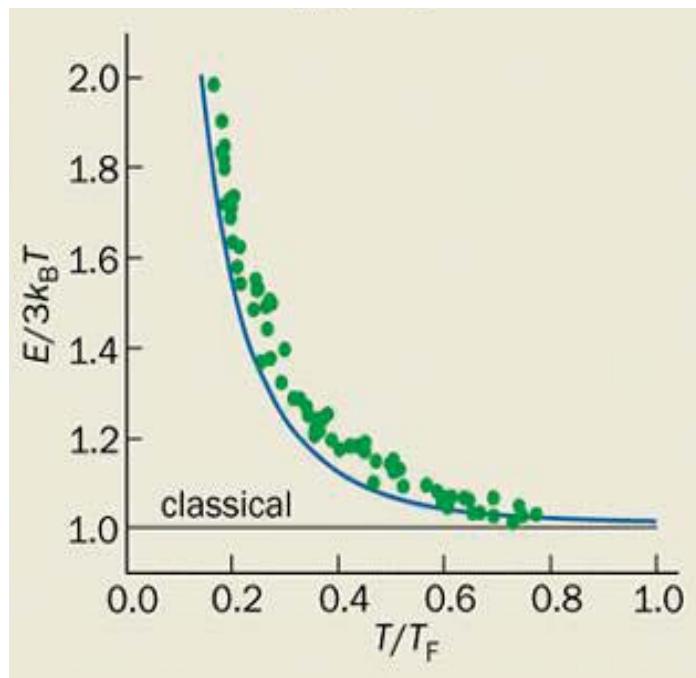
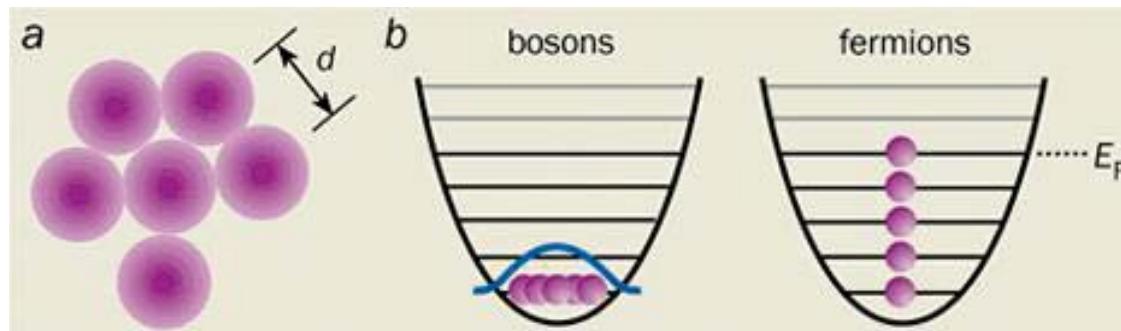


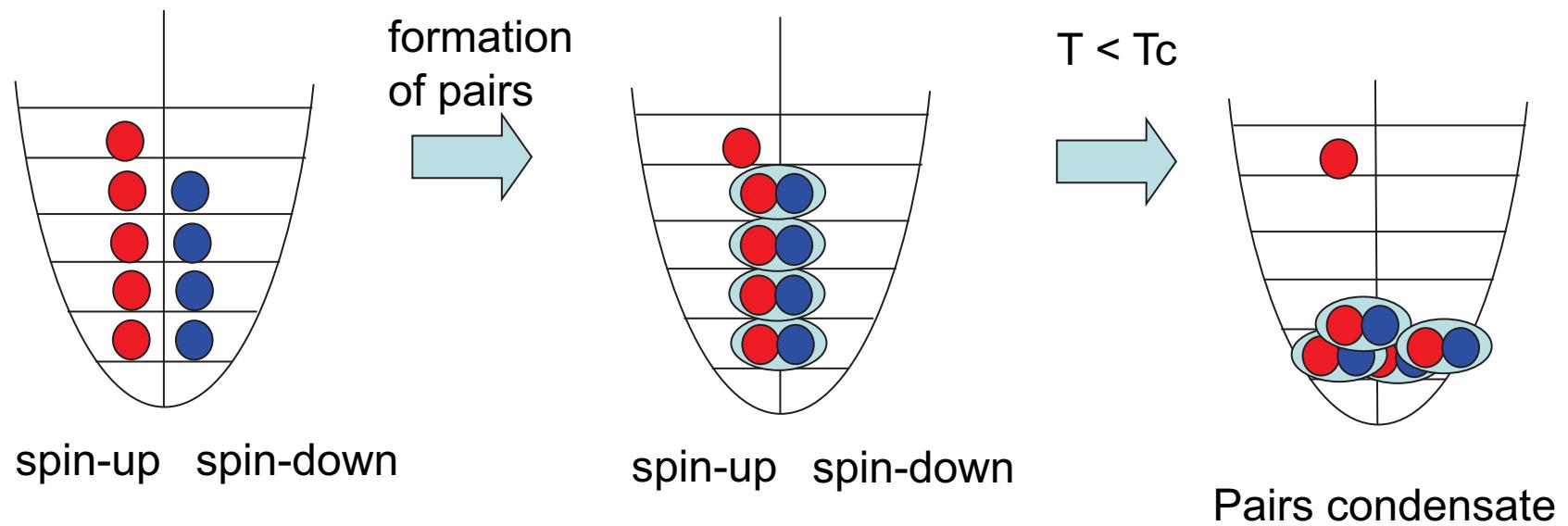
JILA, Boulder C



ENS, Paris, France

Fermions







Further quest to absolute zero ?

What are the applications of the cold gazes and BEC ?