

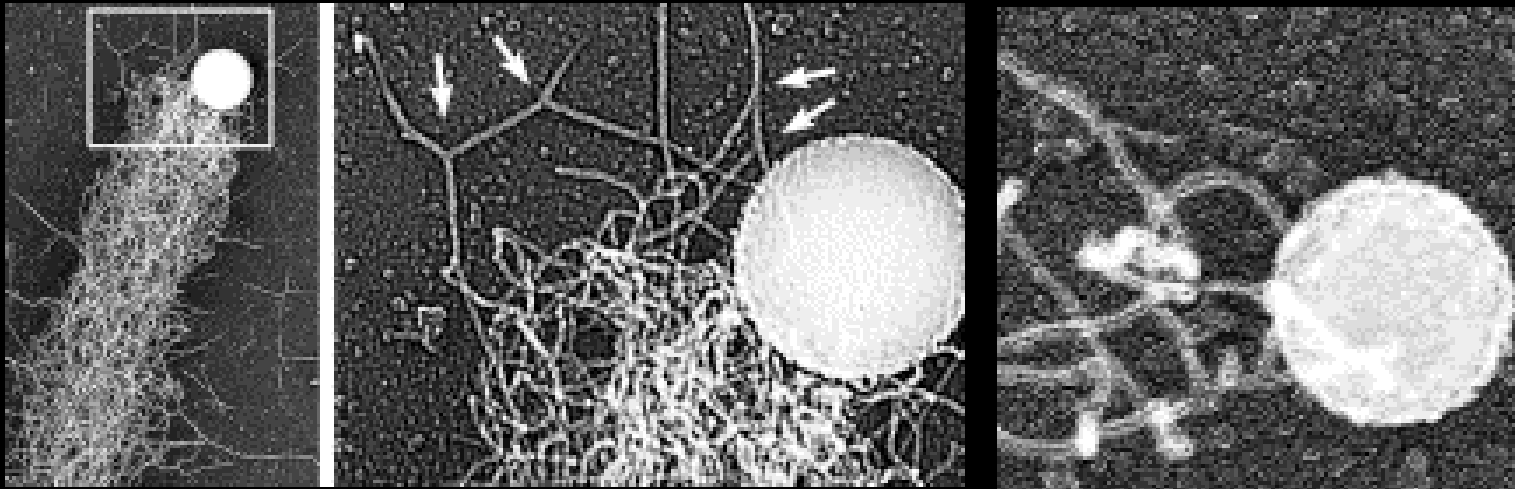


Mathematics & Neurobiology  
University of California at Davis



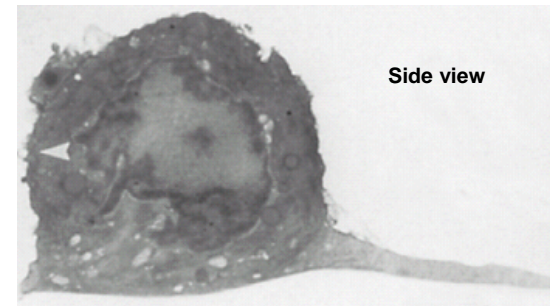
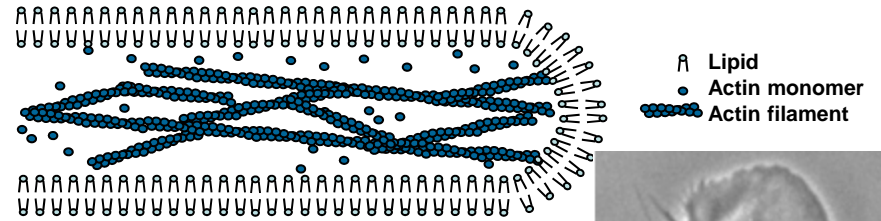
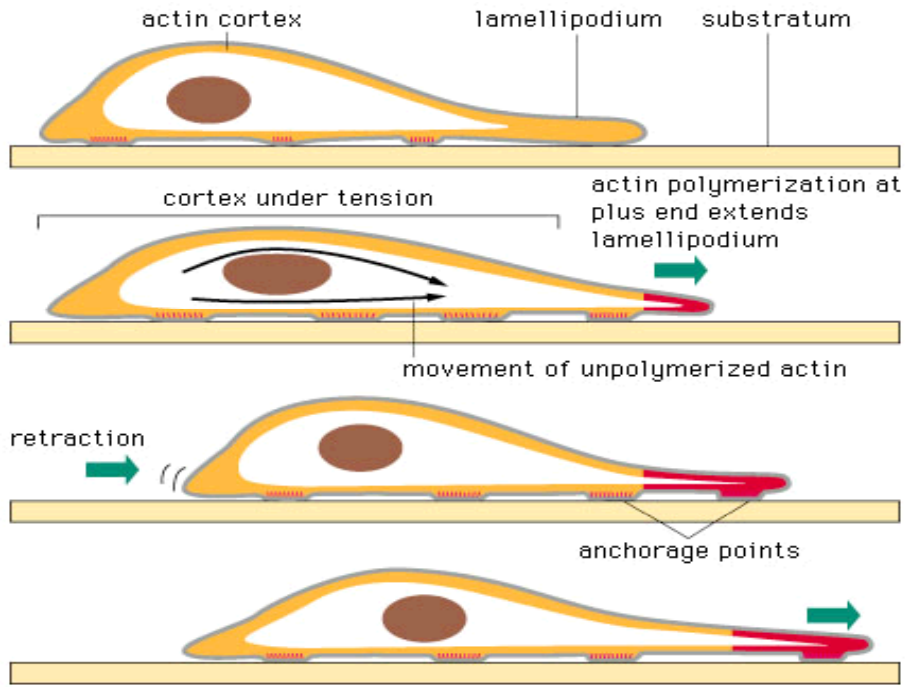
# Mesoscopic Model of Actin-Based Propulsion

Alex Mogilner

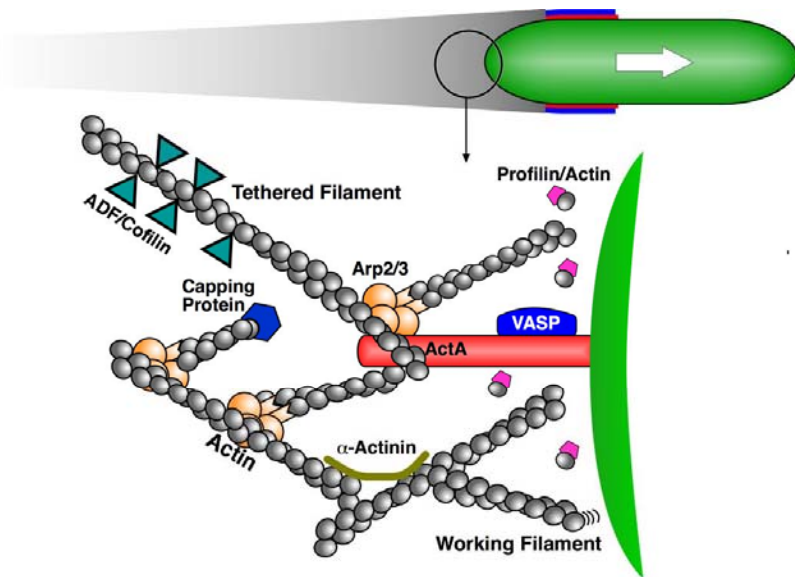


Cameron et al, 2001

# Actin based protrusion



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# Two theories of force generation

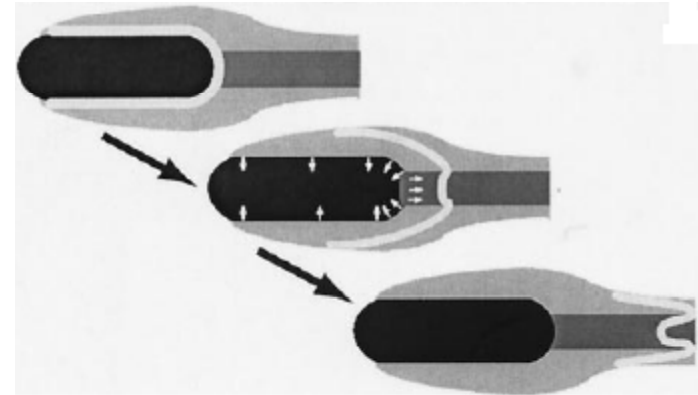
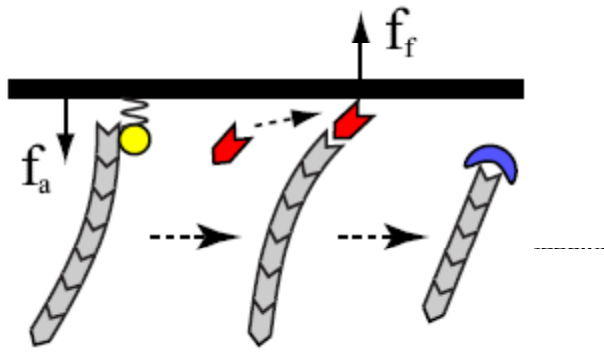
Polymerization Ratchet

vs

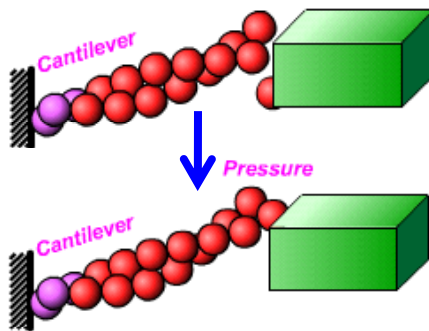
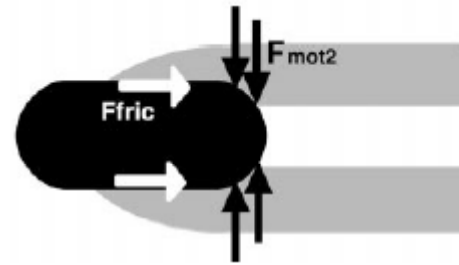
Elastic Propulsion



Mogilner & Oster, 2003

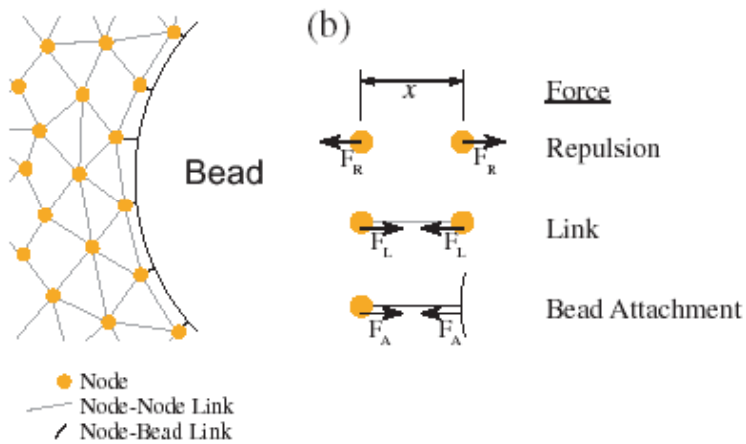


Gerbal, Prost et al, 2000 –



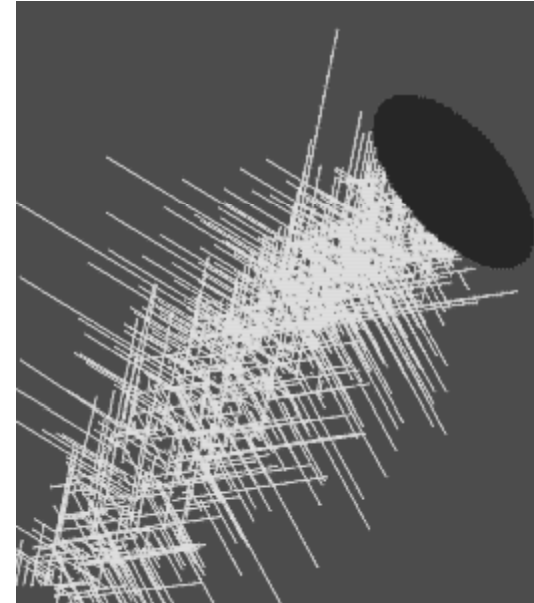
Mogilner & Oster, 1996

## Viscoelastic propulsion model:

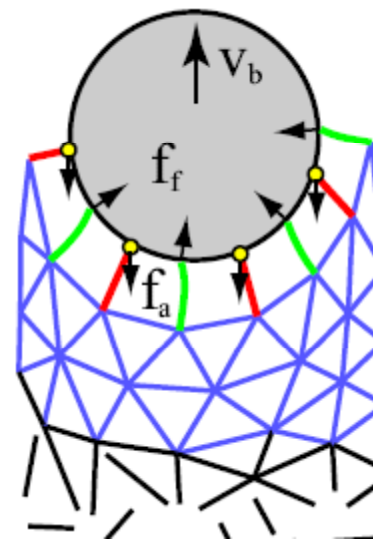
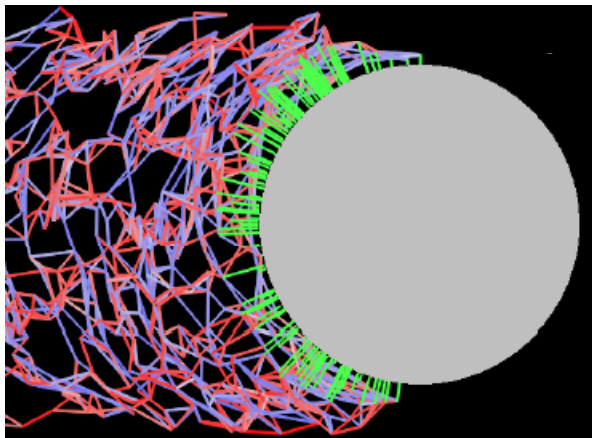


- 1) Nodes appear at the surface with constant rate and establish links with nearest neighbors with a given probability, decreasing linearly with distance; up to a given number of links.
- 2) The links are springs appearing in the unstressed state; if they are compressed, the neighboring nodes repel each other; if they are stretched, the neighboring nodes attract each other.
- 3) When the critical strain is reached, a link breaks irreversibly.
- 4) The bead attachments (also elastic) break with stress-dependent rate.

## Polymerization ratchet model:

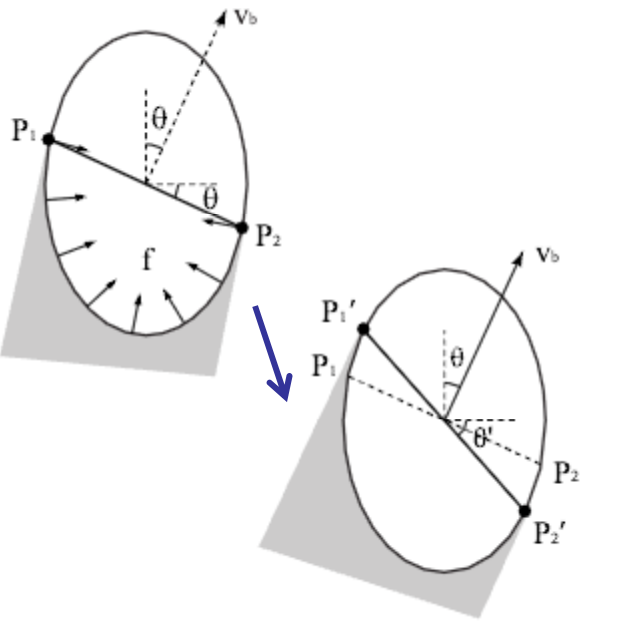
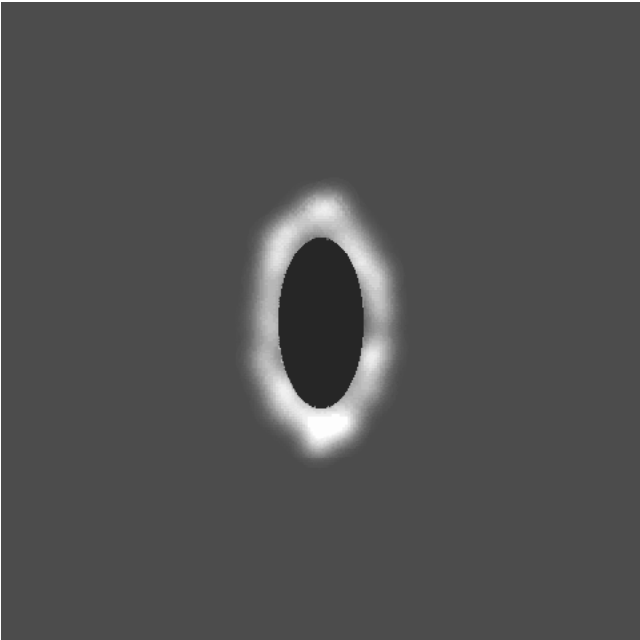


## Hybrid model:

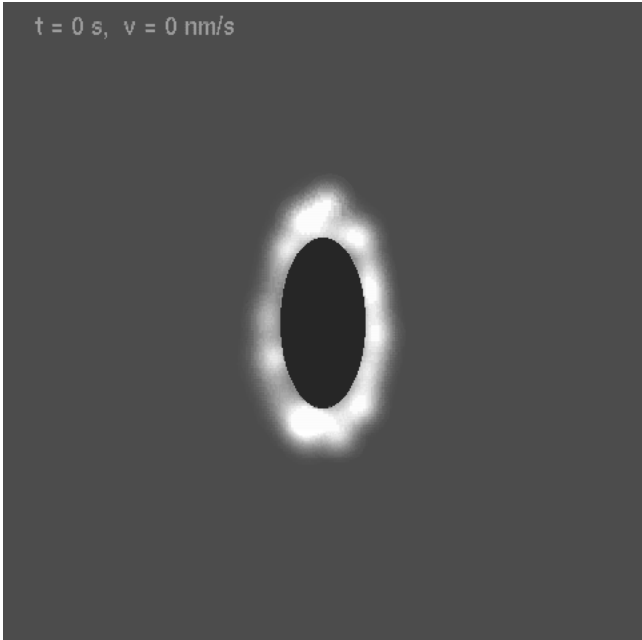


# Different predictions for ellipsoidal beads:

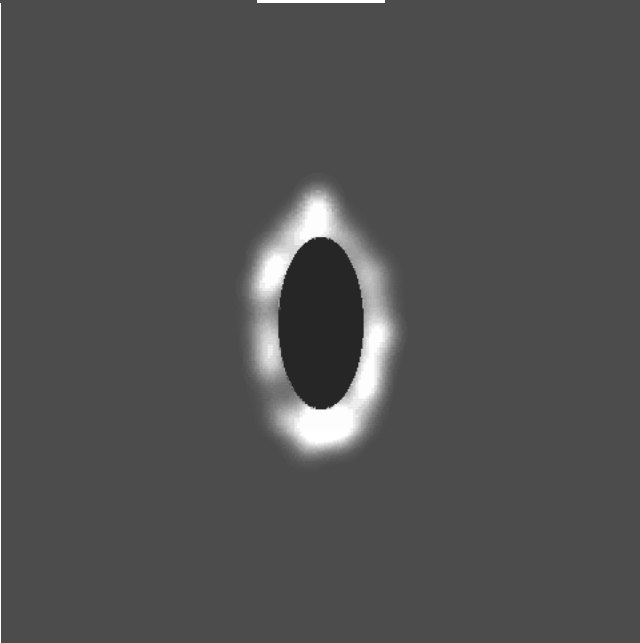
Growing viscoelastic actin network



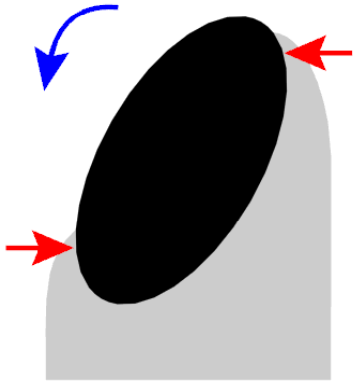
$t = 0 \text{ s}, v = 0 \text{ nm/s}$



Rigid actin ratchet network

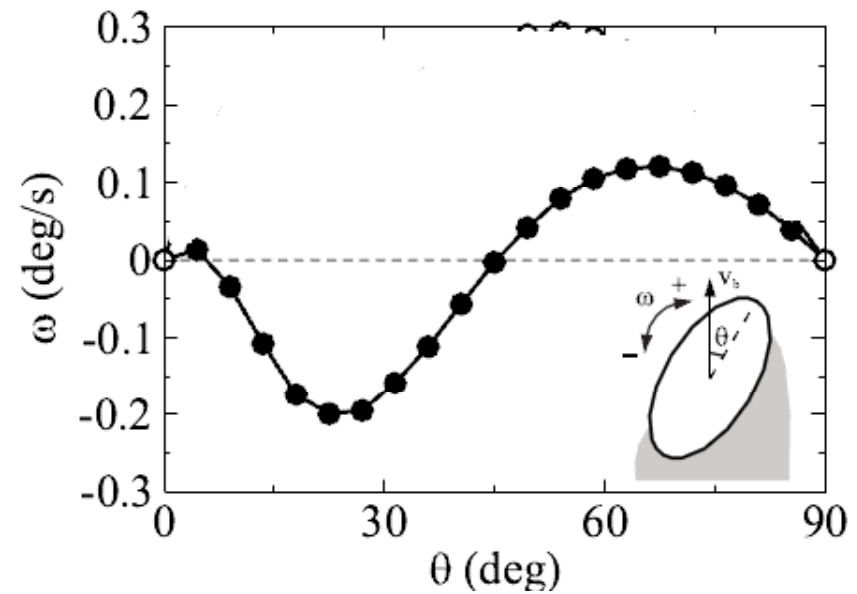
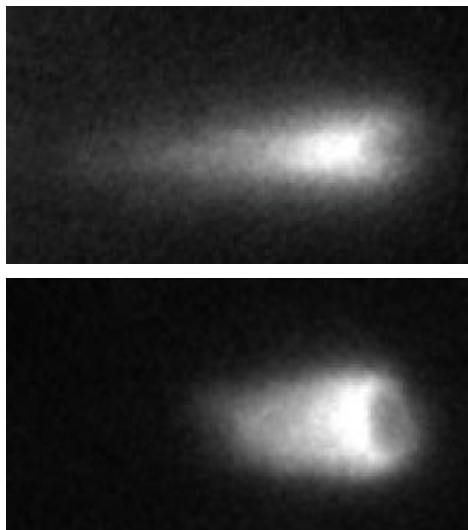
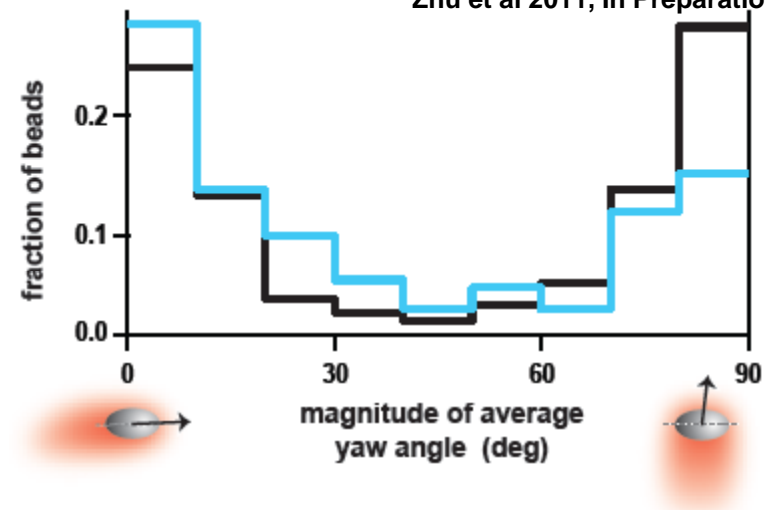
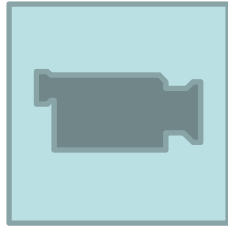


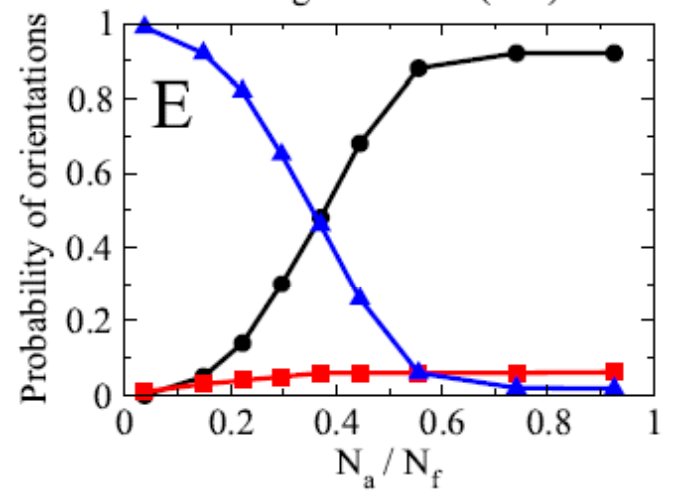
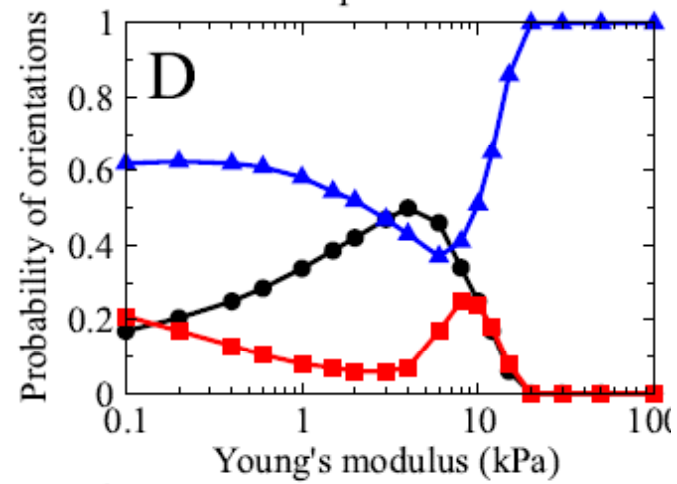
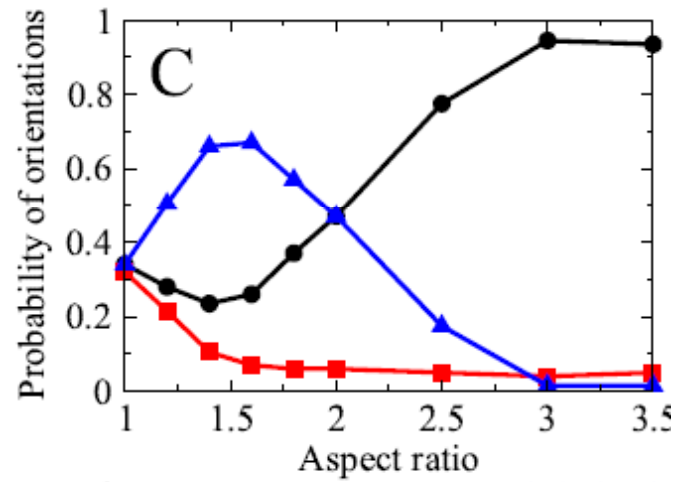
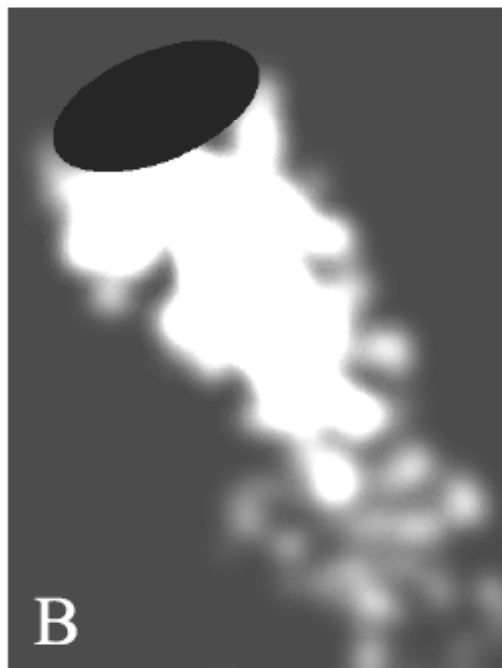
Viscoelastic-ratchet network



# Experiment with ellipsoidal beads

Lacayo et al 2011, PLoS Biology, submitted  
Zhu et al 2011, In Preparation



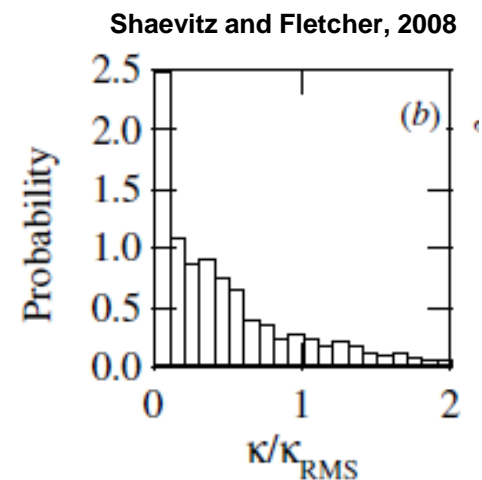
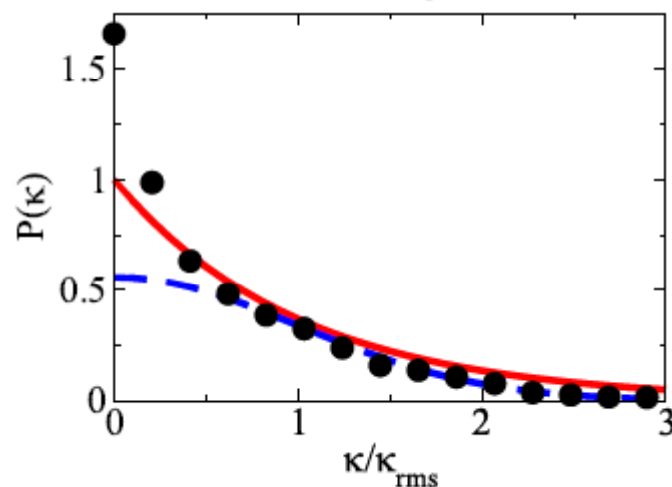
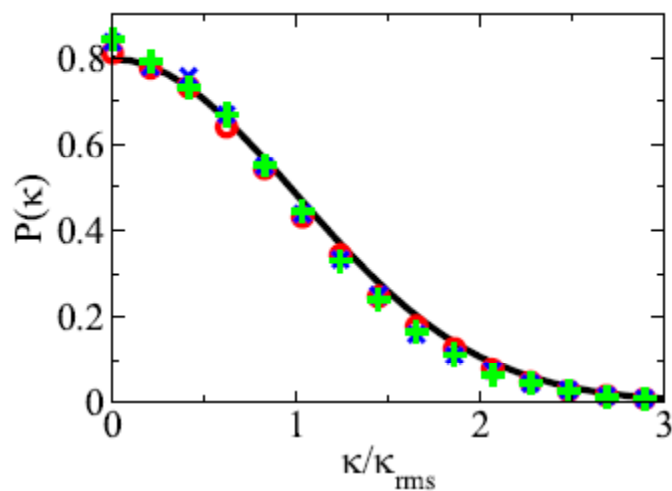
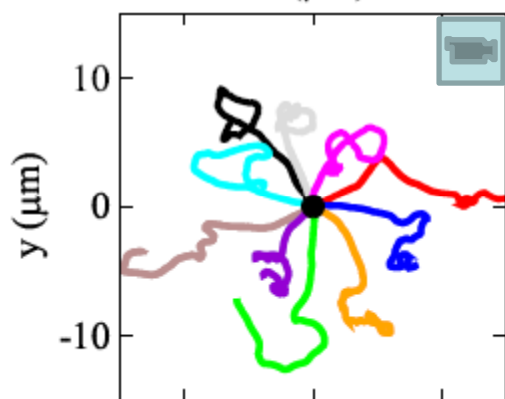
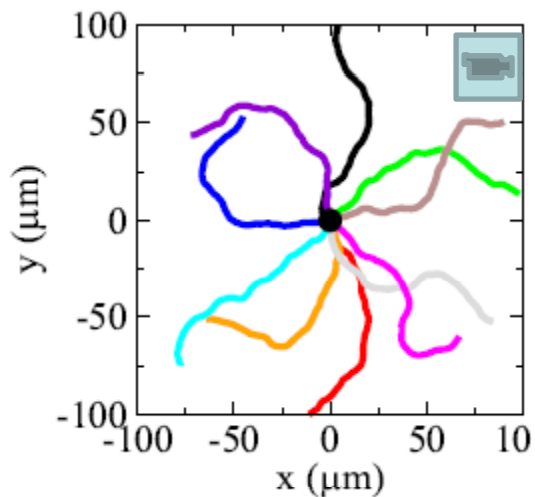
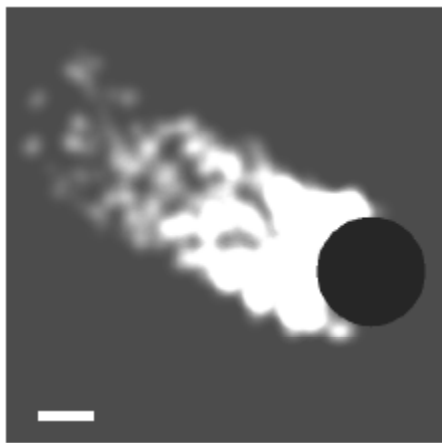


Zhu et al 2011,  
In Preparation



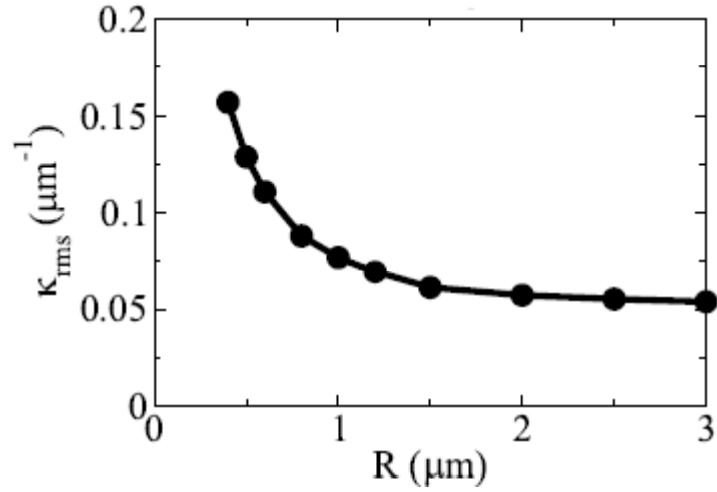
# Curvature of the spherical beads' trajectories

Zhu et al 2011, In Preparation

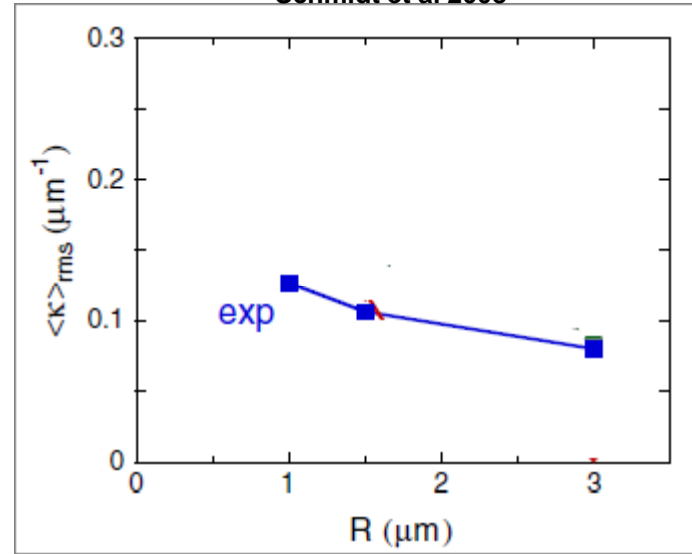




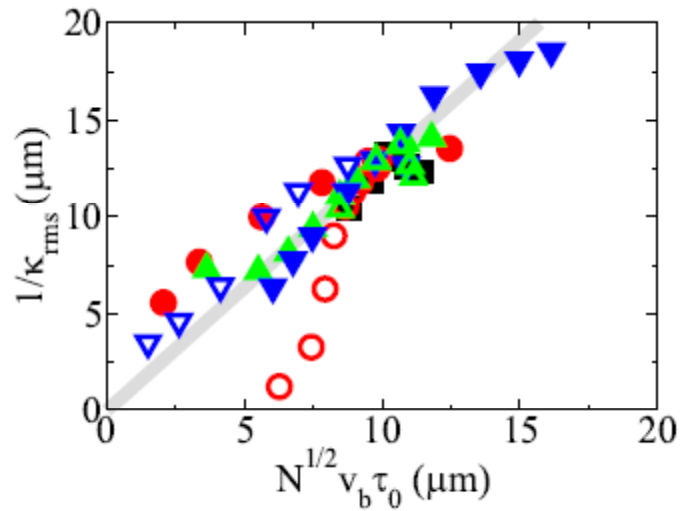
Zhu et al 2011, In Preparation



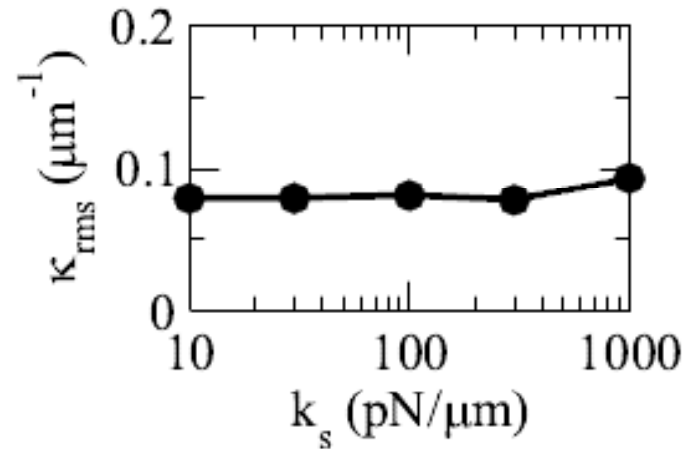
Schmidt et al 2008



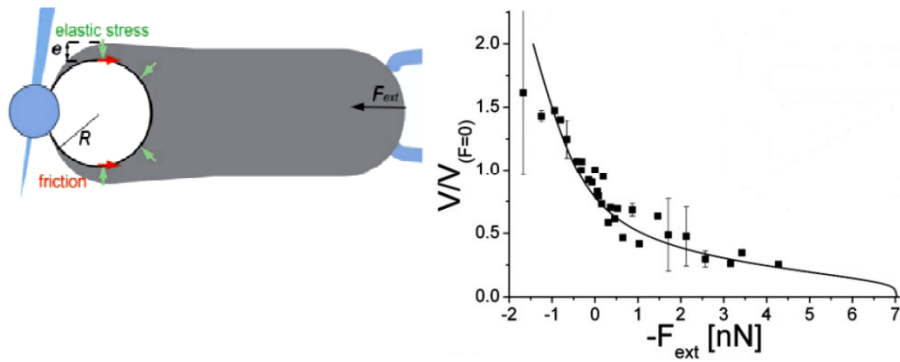
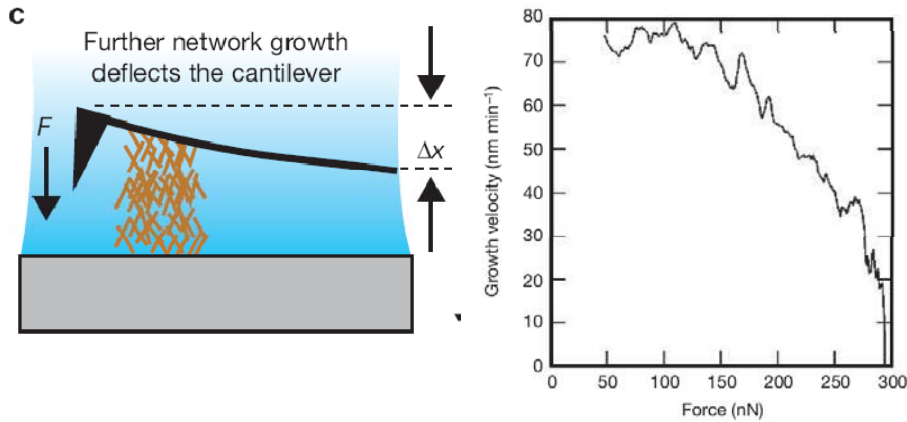
Nature of the curvature is random fluctuations of the filament density:



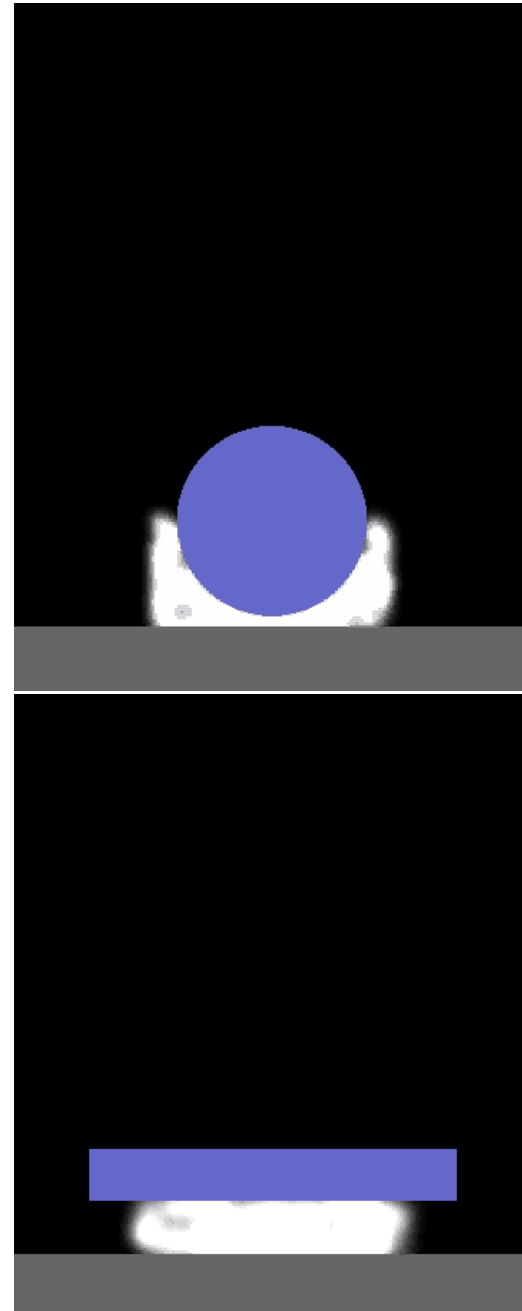
Elastic effects do not affect the curvature:

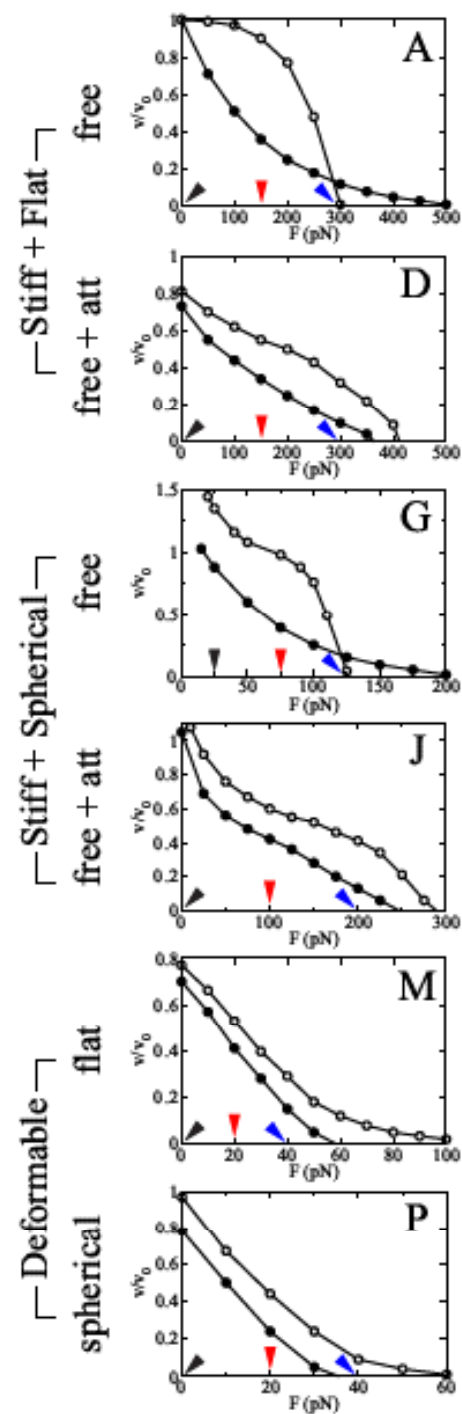
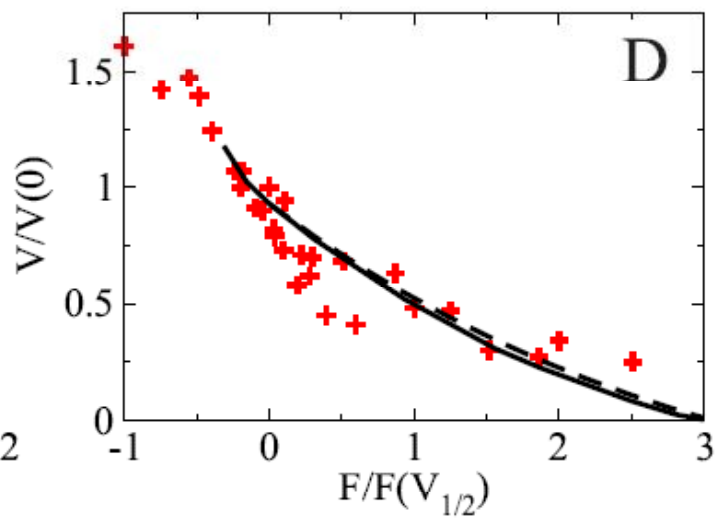
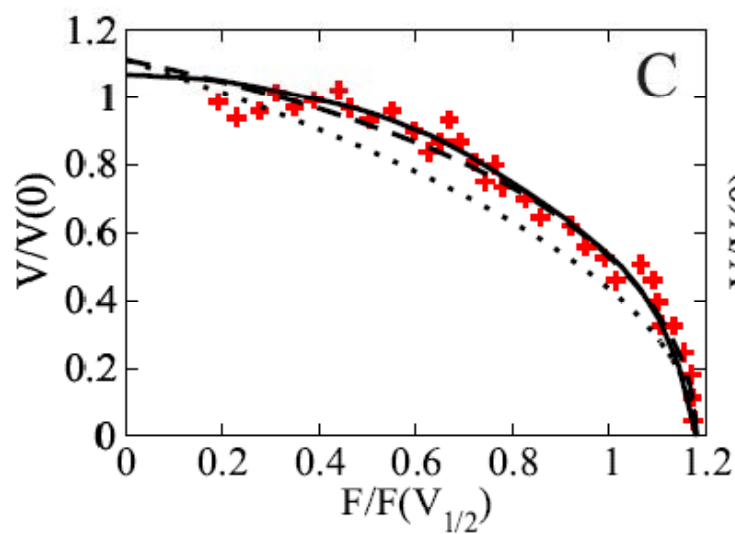
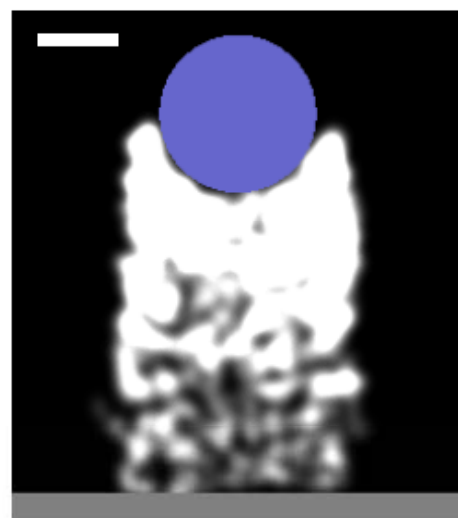
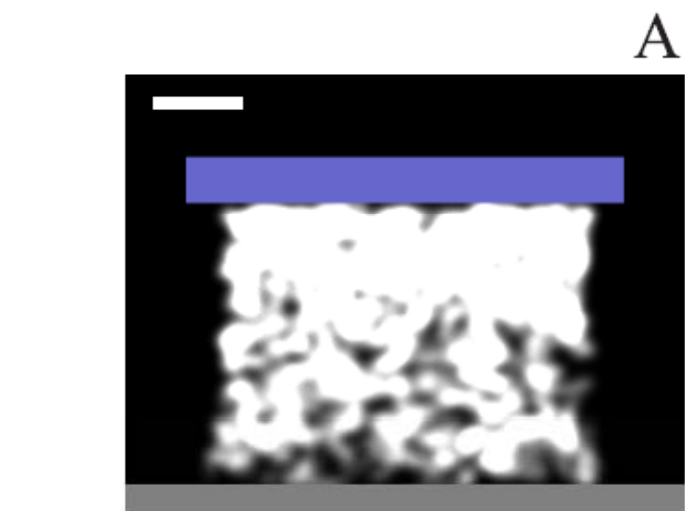


# Force-velocity properties of growing actin networks



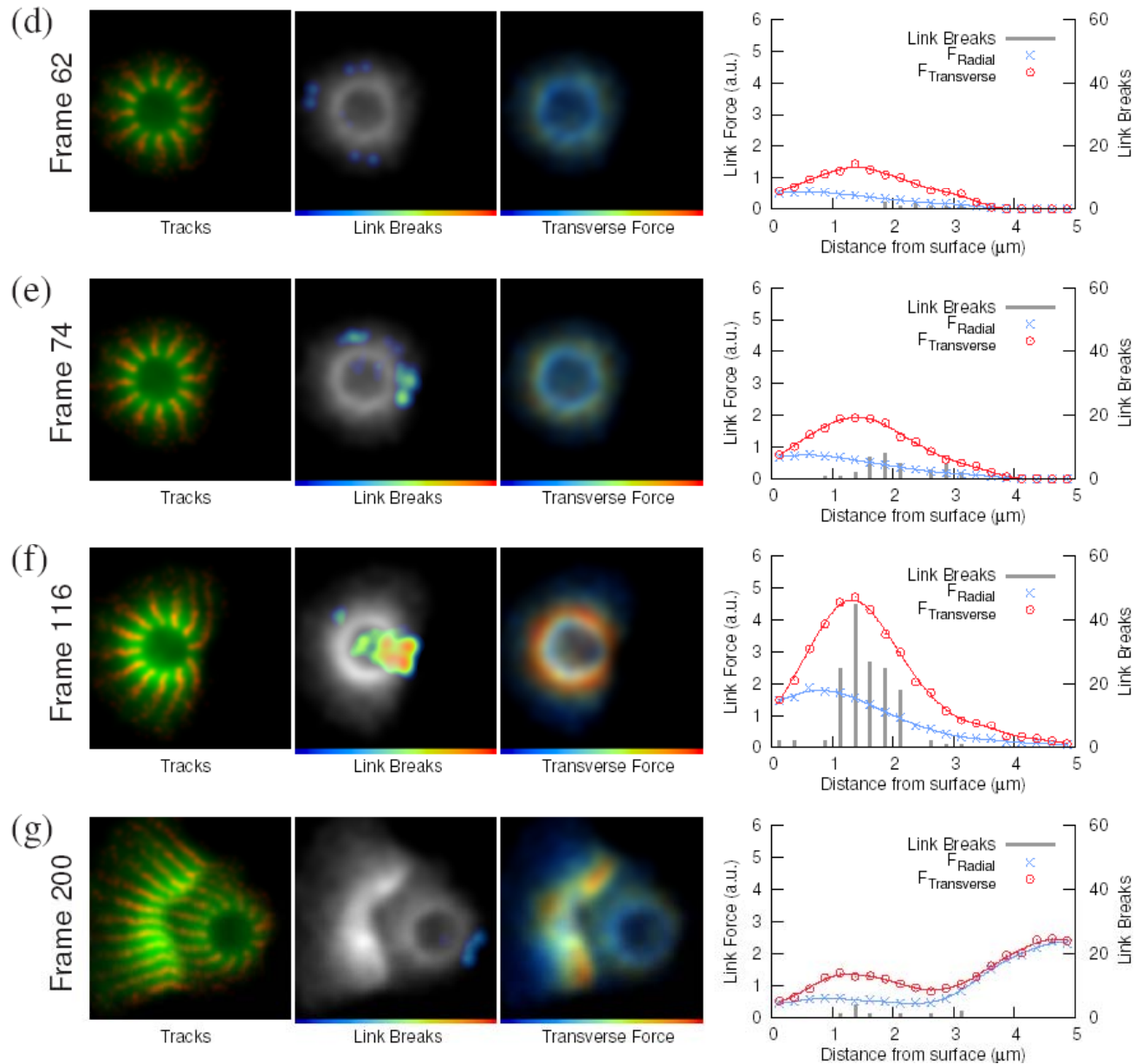
Different shapes of measured force-velocity relation:  
 Concave-down (Parekh *et al.* 2005)  
 Concave-up (Marcy *et al.* 2004)





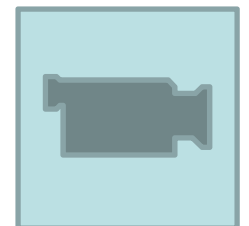
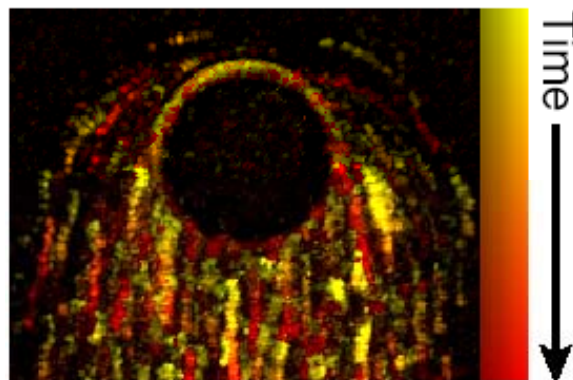
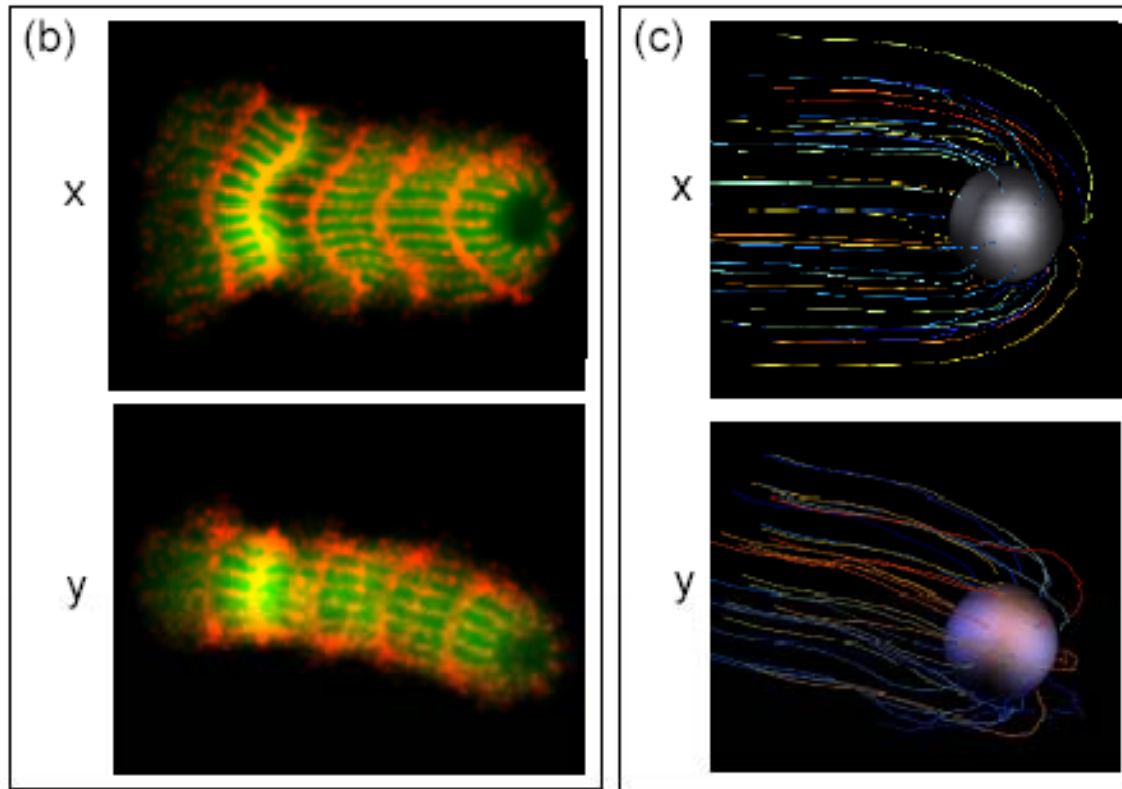
# Mechanics of symmetry breaking: stress distribution; positive feedback; inner vs middle vs outer shell

Dayel et al PLoS Biology 2009



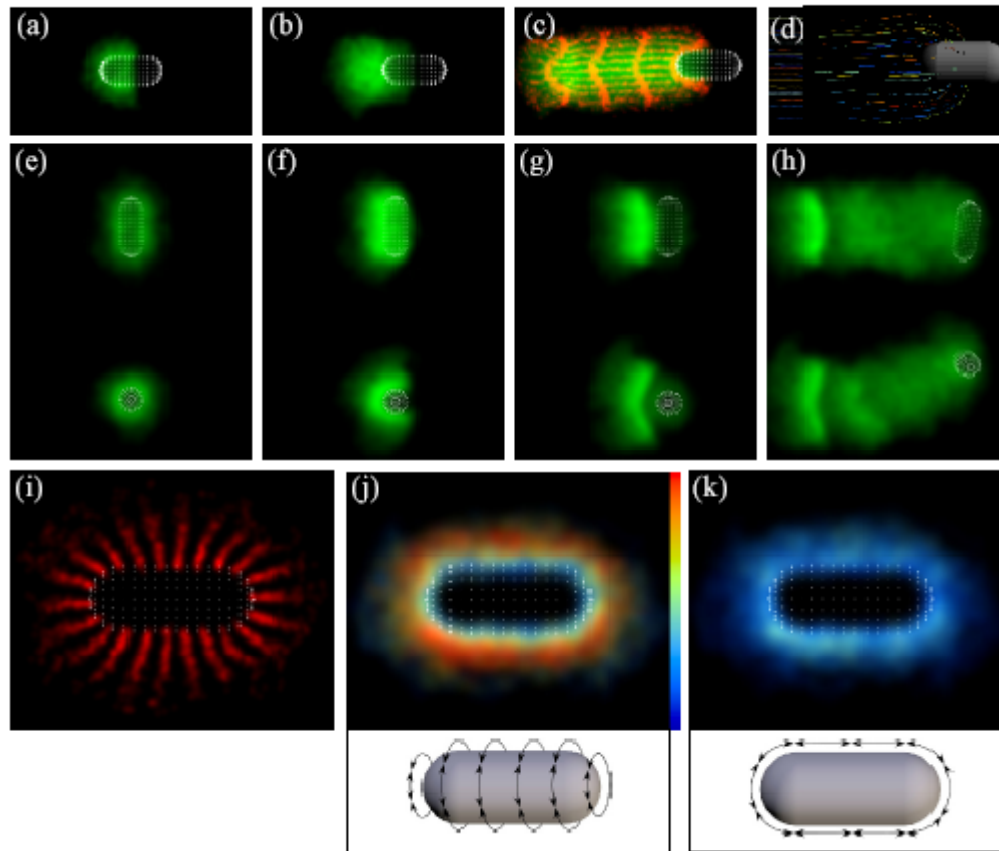
# Motility: no 'soap-squeezing', but 'sustained rip'

Dayel et al PLoS Biology 2009



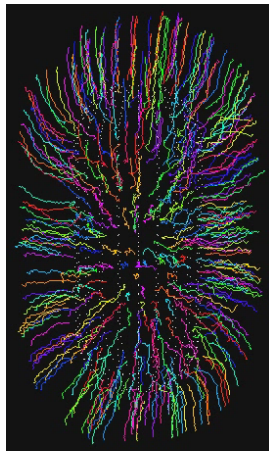
# Motility of Listeria-like shape

Dayel et al PLoS Biology 2009



Gel 'oozes' from Listeria

Capsule breaks and moves  
sidewise



## Summary:

Microscopic ratchet and macroscopic elastic models do not predict behavior of ellipsoidal beads correctly;

Mesoscopic hybrid model combines ratchet and elastic models;

- Explains 1) bi-orientation of ellipsoidal beads;  
2) Distribution of curvatures of spherical bead trajectories;  
3) Force-velocity properties of growing actin networks in two regimes

### UC Davis:

Jie Zhu



### UCSF:

Mark Dayel, Dyche Mullins + others



### Stanford:

Catherine Lacayo, Julie Theriot + others



Supported by NSF, NIH