



**The Abdus Salam  
International Centre for Theoretical Physics**



**2240-21**

**Advanced School on Scaling Laws in Geophysics: Mechanical and  
Thermal Processes in Geodynamics**

*23 May - 3 June, 2011*

**DEEP CONVECTION II  
(Compressible Mantle Convection)**

Shijie ZHONG  
*Department of Physics  
University of Colorado, Boulder  
Colorado  
U.S.A.*

# **Compressible mantle convection**

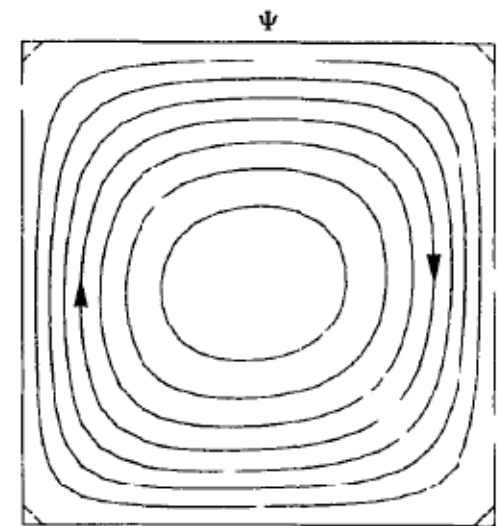
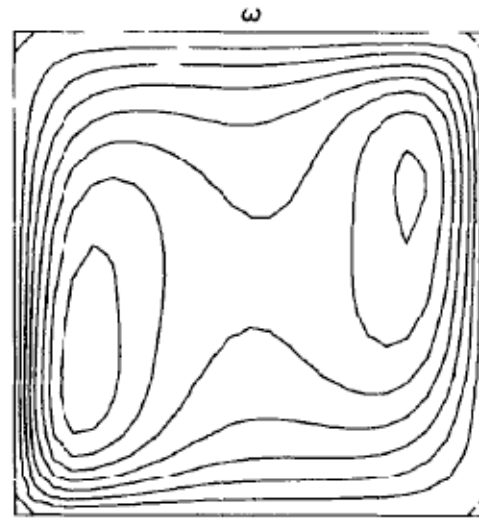
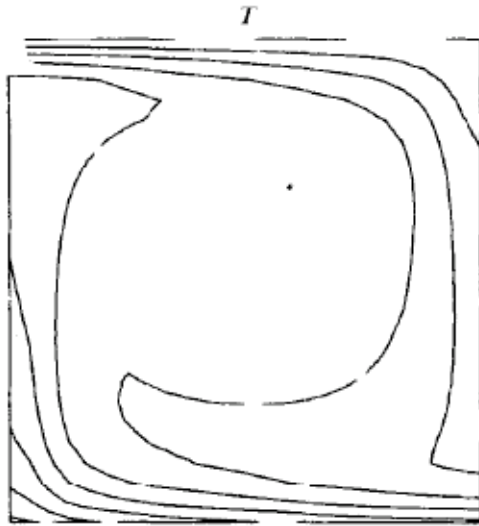
**Shijie Zhong**

**Department of Physics  
University of Colorado  
Boulder, Colorado  
USA**

**ICTP Advanced School on Scaling Laws in Geophysics  
6/3, 2011**

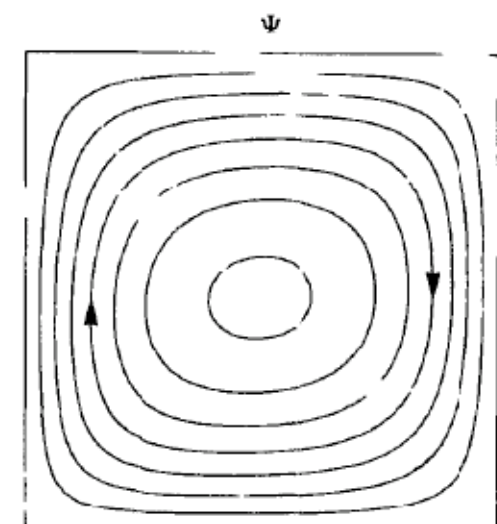
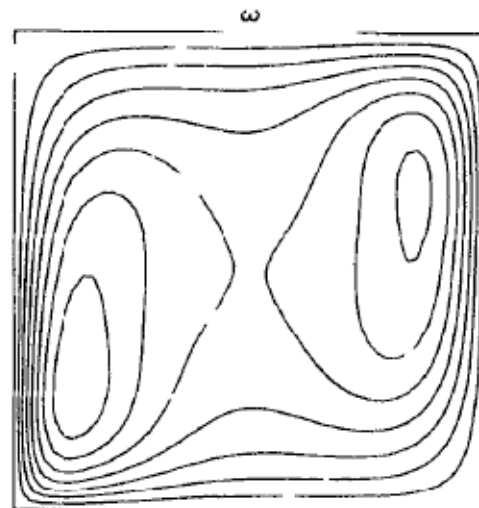
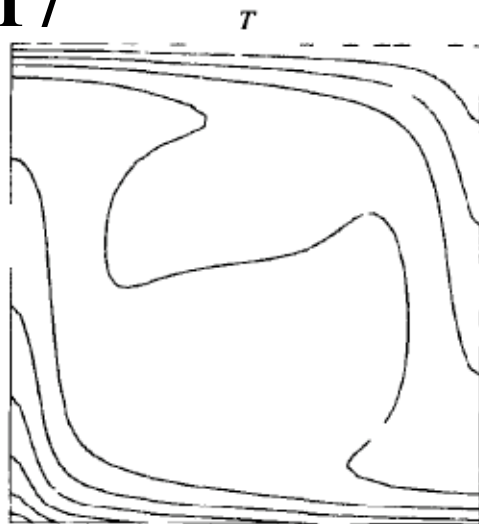
# Compressible convection with different $Di$ (Jarvis and McKenzie, 1981)

**$Di=0$**



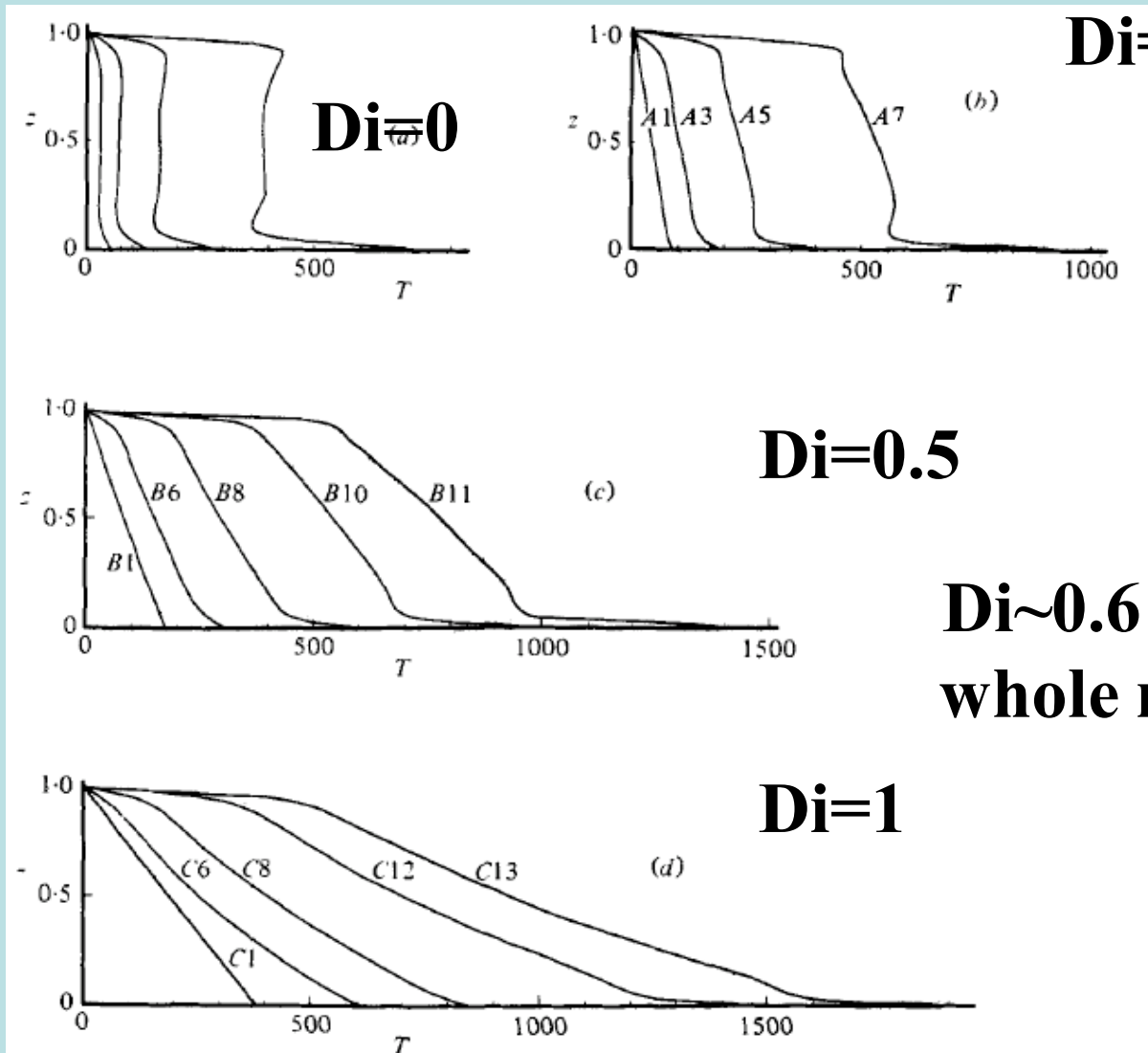
(a)

**$Di=0.117$**



(b)

# Di's effect on Tave



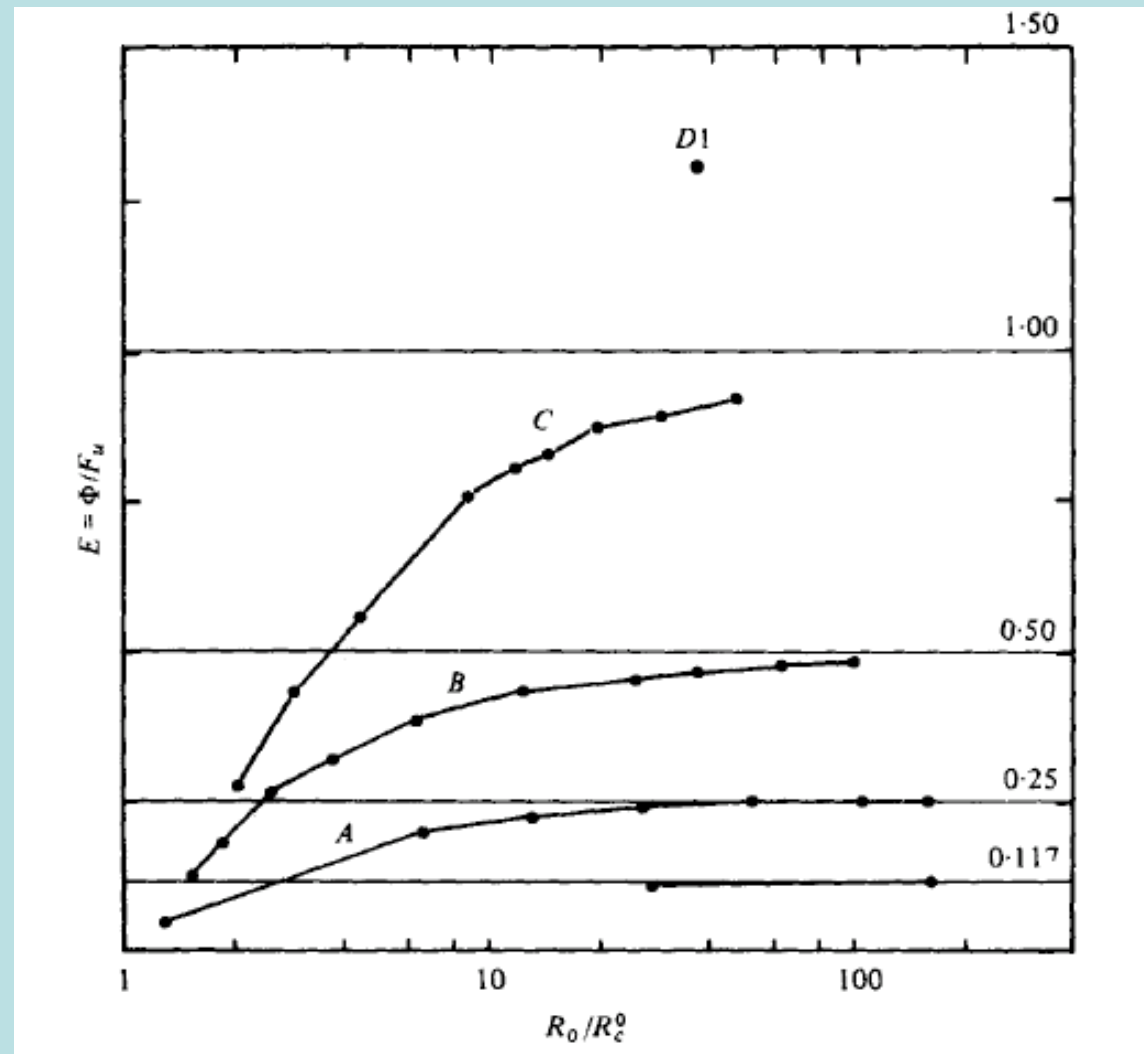
**Di=0.117**

**Di=0.5**

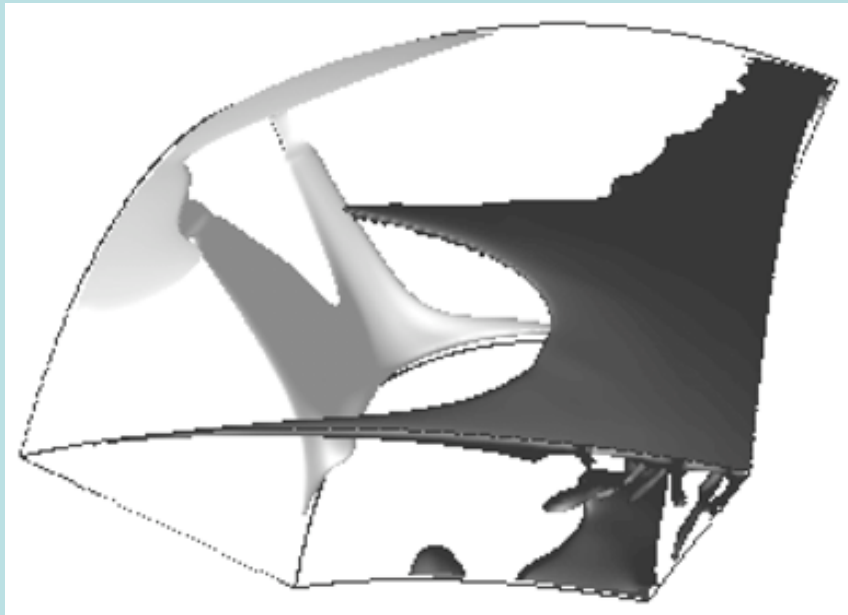
**Di~0.6 for Earth's  
whole mantle**

**Di=1**

$\Phi/F_s = Di$  for large  $Ra$  and basal heating convection (Hewitt et al., 1975)



# Effect of adiabatic heating/cooling on plume excess temperature and plume buoyancy flux



**As plumes rise, they cool due to adiabatic cooling effect (expanding at smaller pressure).**

**How does it affect plume dynamics?**

# Adiabatic temperature gradient and temperature (Leng and Zhong, JGR, 2008)

$$\frac{dT_{ave}}{dr} = -\frac{\alpha g T_{ave}}{C_p},$$

$$\frac{dT_{ave}}{dr} = -\gamma D_i (T_{ave} + T_s),$$

$$D_i = \frac{\alpha_0 g d}{C_p}, \quad \gamma = R_e/d$$

$$T_{ave} + T_s = A e^{-\gamma D_i r},$$

**For plumes:**

$$\frac{dT_p}{dr} = -\frac{\alpha g T_p}{C_p}.$$

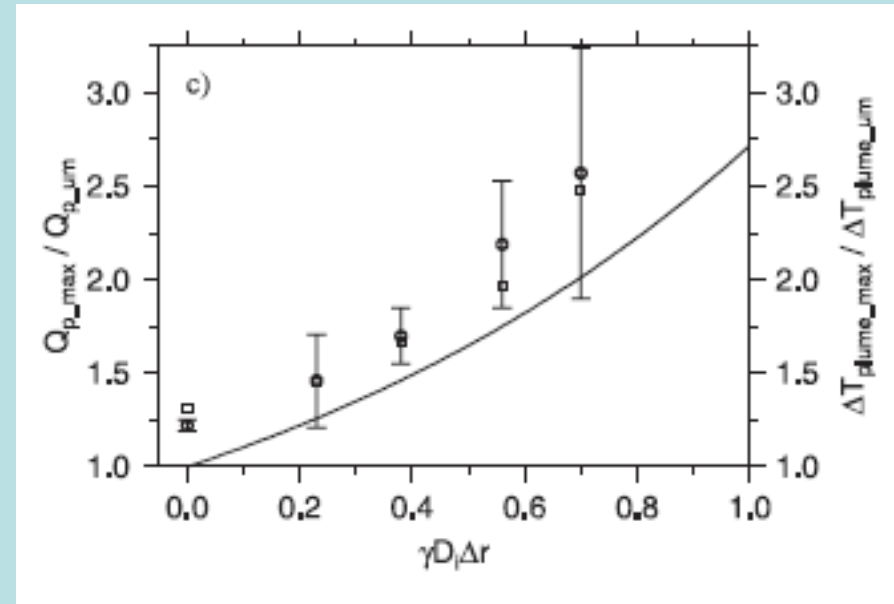
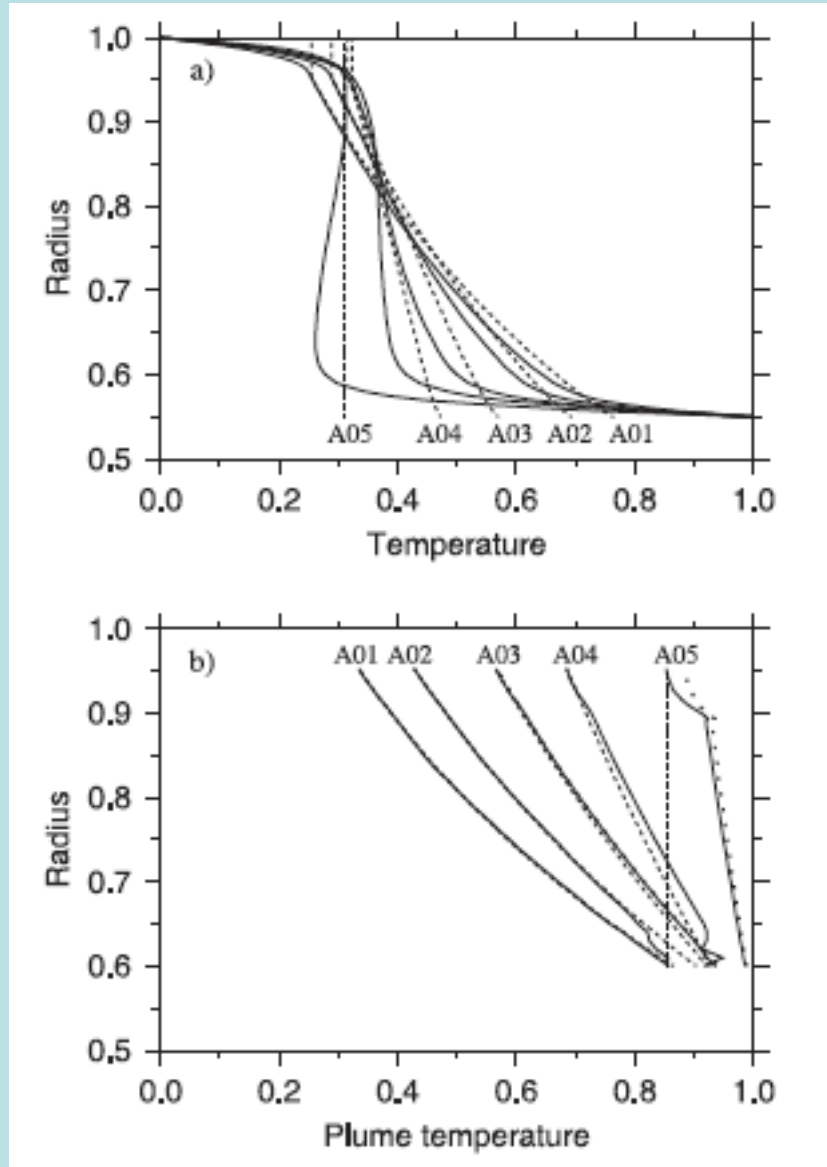
$$T_p + T_s = B e^{-\gamma D_i r},$$

$$\Delta T_{plume} = T_p - T_{ave} = (B - A) e^{-\gamma D_i r}.$$

$$\frac{\Delta T_{plume}(r_1)}{\Delta T_{plume}(r_2)} = e^{\gamma D_i (r_2 - r_1)}.$$

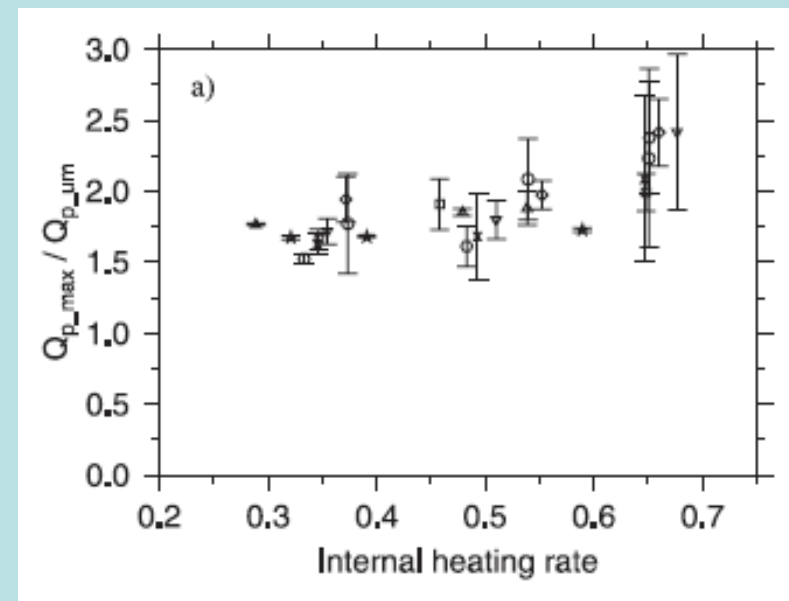
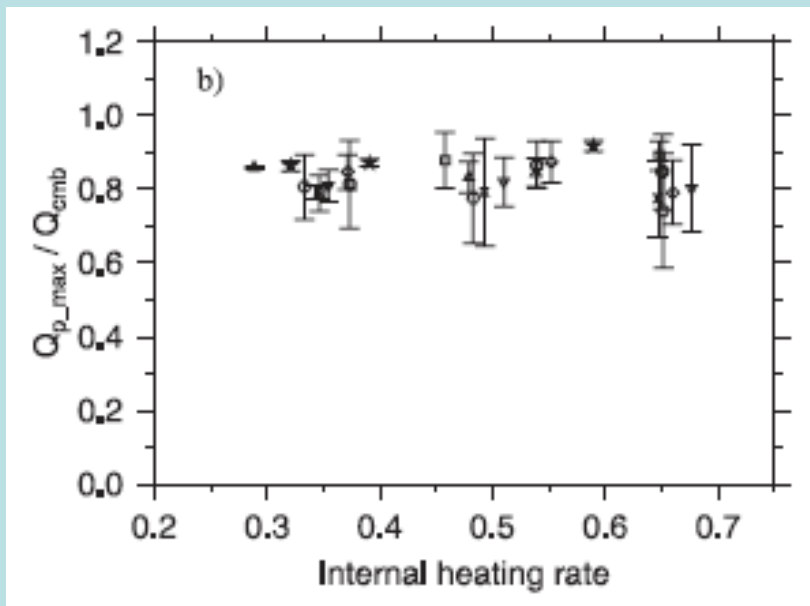
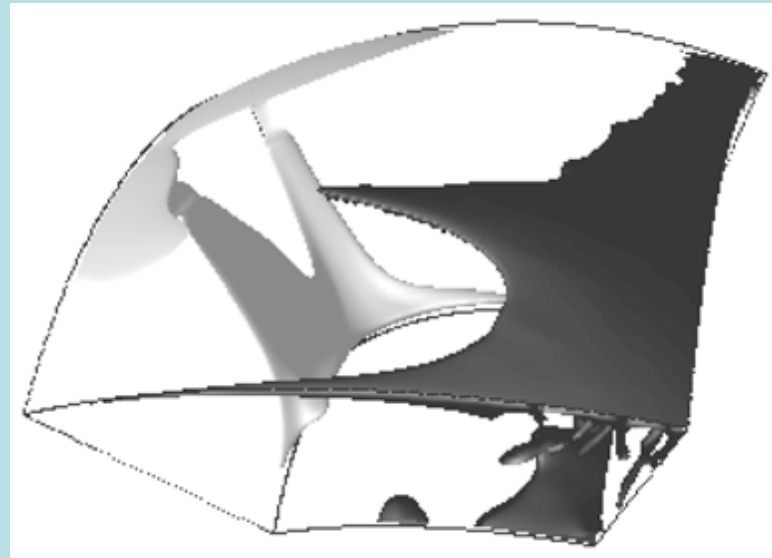
$$\frac{Q(r_1)}{Q(r_2)} = e^{\gamma D_i (r_2 - r_1)}.$$

# Effect of adiabatic heating/cooling on plume excess temperature and plume buoyancy flux





# Plume buoyancy flux = CMB heat flux?



# Conclusion

- Compressible mantle convection may be important for plume dynamics for the Earth.
- Pressure-dependent buoyancy is important for balancing the viscous dissipation and adiabatic heating.
- $\Phi/Fs = Di(1-1/2\xi)$  for large Ra.