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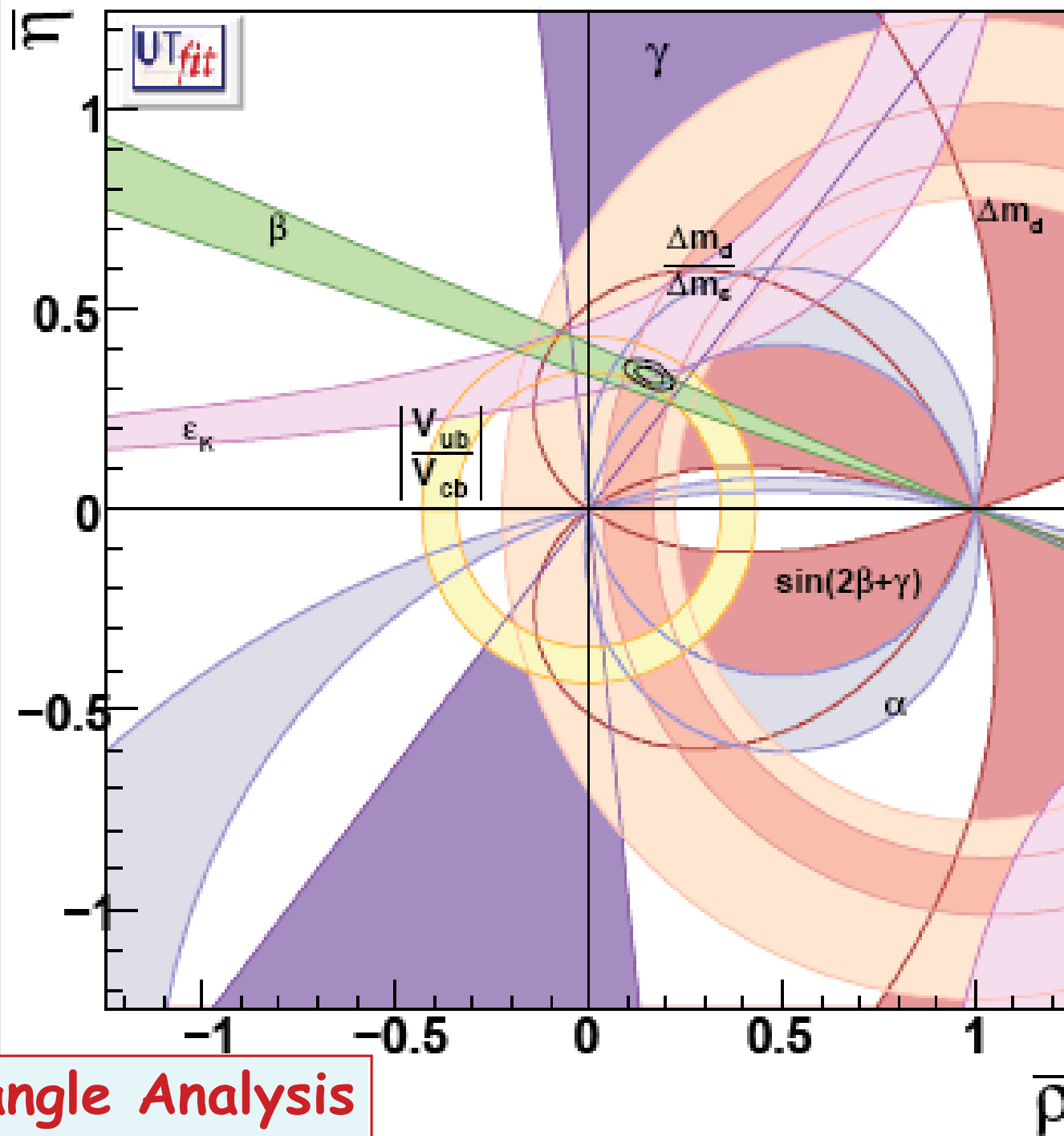
**Summer School on Particle Physics**

*6 - 17 June 2011*

**Flavor Physics - III**

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Italy*



Unitarity Triangle Analysis  
(UTA)

Weak eigenstates  $\bar{U}_L \gamma^\mu \underbrace{V_u^\dagger V_d}_{V_{CKM}} D_L W_\mu^+$

Mass eigenstates

**The CKM Matrix**

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = V_{CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

- 3x3 **unitary** matrix
- 4 parameters: 3 angles and 1 phase
- The **phase** is responsible of **CP-violation**  
(With exact CPT, CP is equivalent to T, T is a antiunitary operator  $\Rightarrow T V_{CKM} \rightarrow V_{CKM}^*$  which differs from  $V_{CKM}$  due to the phase)

**First important aim of Flavour Physics:**  
**Accurate determination of the CKM parameters**

**At present an accuracy of few % has been achieved!**

# Standard parameterization for a 3x3 unitary matrix

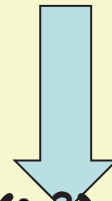
$$\hat{V}_{CKM} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -s_{23}c_{12} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$V_{us} \approx 0.2 \equiv \lambda$  is small,  
 $V_{CKM}$  can be expanded in  $\lambda$

$$c_{23} \approx c_{13} \approx 1$$

$$s_{23} = O(\lambda^2)$$

$$s_{13} = O(\lambda^3)$$



Expanding up to  $O(\lambda^3)$  and introducing  
 new convenient parameters ( $A, \lambda, \rho, \eta$ )

$$s_{23} \equiv A\lambda^2, \quad s_{13}e^{-i\delta} \equiv A\lambda^3(\rho - i\eta)$$

one gets:

# The Unitarity Triangle Analysis (UTA)

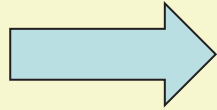
Wolfenstein parameterization (up to  $O(\lambda^3)$ )

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \cong \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

Accurately measured: -  $\lambda=0.225(1)$  (several kaon exp., among which KLOE@Frascati)  
-  $A=0.81(2)$  (B-factories)

$(\eta \neq 0 \leftrightarrow \text{CP-violation})$

Some  $O(\lambda^5)$  corrections are required by the present accuracy and are included by keeping higher order terms in the original parameterization reexpressed in terms of  $A, \lambda, \rho, \eta$  (so that the CKM matrix satisfies unitarity at all orders)



$$V_{ud} = 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 + \mathcal{O}(\lambda^6)$$

$$V_{us} = \lambda + \mathcal{O}(\lambda^7)$$

$$V_{ub} = A\lambda^3(\varrho - i\eta)$$

$$V_{cd} = -\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\varrho + i\eta)] + \mathcal{O}(\lambda^7)$$

$$V_{cs} = 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4(1 + 4A^2) + \mathcal{O}(\lambda^6)$$

$$V_{cb} = A\lambda^2 + \mathcal{O}(\lambda^8)$$

$$V_{td} = A\lambda^3 \left[ 1 - (\varrho + i\eta)\left(1 - \frac{1}{2}\lambda^2\right) \right] + \mathcal{O}(\lambda^7)$$

$$V_{ts} = -A\lambda^2 + \frac{1}{2}A(1 - 2\varrho)\lambda^4 - i\eta A\lambda^4 + \mathcal{O}(\lambda^6)$$

$$V_{tb} = 1 - \frac{1}{2}A^2\lambda^4 + \mathcal{O}(\lambda^6)$$

**To an excellent accuracy:**

$$V_{us} = \lambda, \quad V_{cb} = A\lambda^2,$$

$$V_{ub} = A\lambda^3(\varrho - i\eta), \quad V_{td} = A\lambda^3(1 - \bar{\varrho} - i\bar{\eta})$$

$$\bar{\rho} = \rho \left( 1 - \frac{\lambda^2}{2} \right), \quad \bar{\eta} = \eta \left( 1 - \frac{\lambda^2}{2} \right)$$

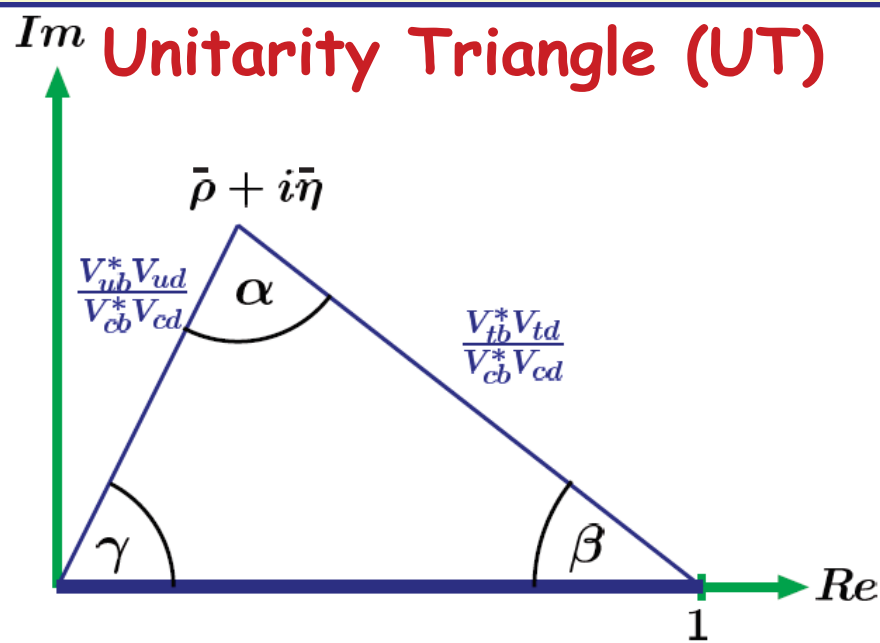
# The Unitarity Triangle Analysis (UTA)

It defines a triangle  
in the  $(\bar{\rho}, \bar{\eta})$ -plane  
(with sides of similar size,  
so that CP-violation is visible)

- Unitarity ( $V_{CKM}^\dagger V_{CKM} = 1$ )  
provides 9 conditions  
on the CKM parameters

- Among these it is of great  
phenomenological interest

$$V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 0$$



There are two collaborations working at the UTA



13 members from  
France, Switzerland, Germany and Japan



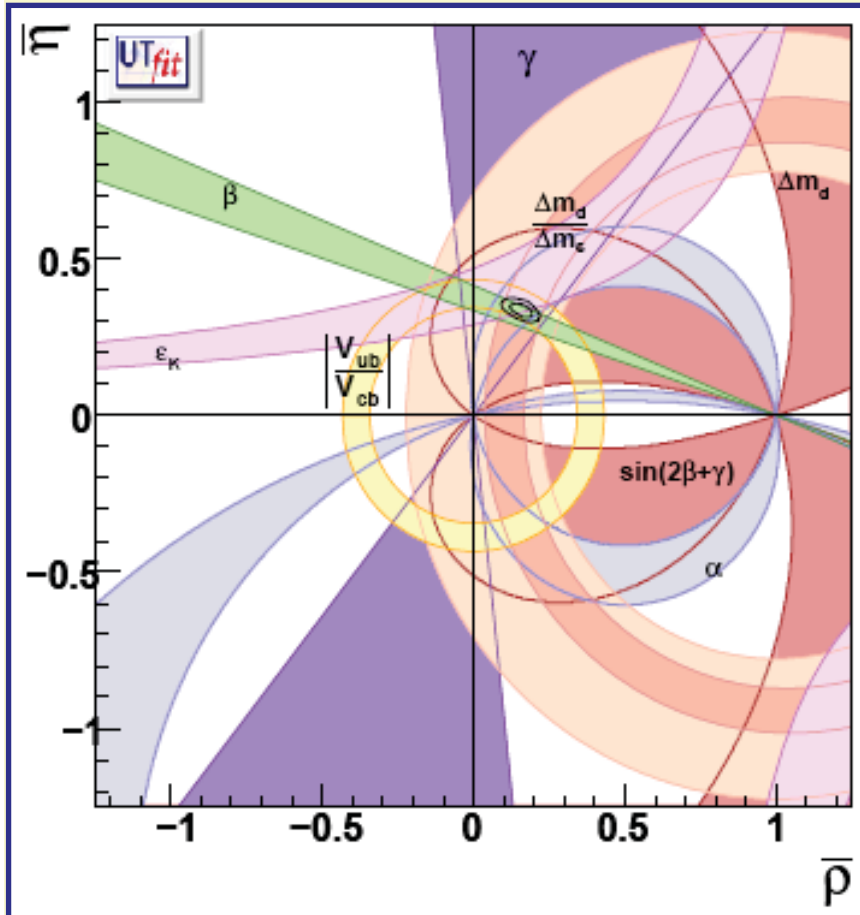
Collaboration of  
Theorists and  
Experimentalists

Adrian Bevan	Queen Mary, University of London
Marcella Bona	Queen Mary, University of London
Marco Ciuchini	INFN Sezione di Roma Tre
Denis Derkach	LAL-IN2P3 Orsay
Enrico Franco	University of Roma "La Sapienza"
Vittorio Lubicz	University of Roma Tre
Guido Martinelli	University of Roma "La Sapienza"
Fabrizio Parodi	University of Genova
Maurizio Pierini	CERN
Carlo Schiavi	University of Genova
Luca Silvestrini	INFN Sezione of Roma
Viola Sordini	IPNL-IN2P3 Lyon
Achille Stocchi	LAL-IN2P3 Orsay
Cecilia Tarantino	University of Roma Tre
Vincenzo Vagnoni	INFN Sezione of Bologna



# Great Accuracy achieved in the UTA

## Experimental Constraints



Obs.	Accuracy
$\epsilon_K$	$\approx 0.4\%$
$\Delta m_d$	$\approx 1\%$
$\left  \frac{\Delta m_s}{\Delta m_d} \right $	$\approx 1\%$
$\left  \frac{V_{ub}}{V_{cb}} \right $	$\approx 5\%$
$\sin 2\beta$	$\approx 4\%$
$\cos 2\beta$	$\approx 15\%$
$\alpha$	$\approx 7\%$
$\gamma$	$\approx 15\%$
$(2\beta + \gamma)$	$\approx 50\%$

Requiring the calculation of hadronic matrix elements

Not requiring it

For a significant comparison between exp. measurements and theor. predictions, hadronic uncertainties must be well under control

# The fundamental role of Lattice QCD

## Lattice QCD:

- ✓ **non-perturbative approach**  
(path-integral method)
- ✓ **only the QCD parameters**
- ✓ **theory regularization**
- ✗ **discrete space and finite volume**

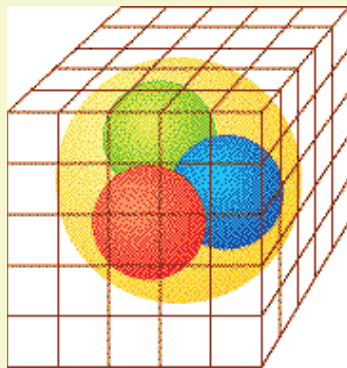
## Path Integral:

Green functions  $\equiv$  derivatives of the generating functional

$$Z(J_\mu, \eta, \bar{\eta}) = \int \delta A \delta \bar{q} \delta q e^{-S(A, q, \bar{q}) + \int J_\mu A_\mu + \int \bar{\eta} q + \int \bar{q} \eta}$$

In order to formally define the integrals, one considers a **discrete LATTICE** in a **finite volume**:

infinite-dimension integrals  $\longrightarrow$  ordinary multiple integrals



$$\langle O(A, q, \bar{q}) \rangle = \int \delta A \delta \bar{q} \delta q O(A, q, \bar{q}) e^{-S(A, q, \bar{q})}$$

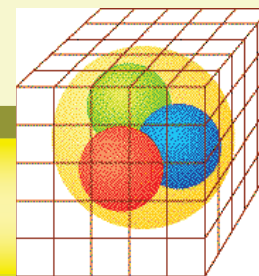
Few configurations only  
are relevant 😊

$$\cong \bar{O} = \frac{1}{N} \sum_{i=1}^N O(\mathbf{q}_i)$$

Generated by a Monte Carlo

In the era of precision Flavour Physics  
We have also entered the era of

## Precision LATTICE QCD



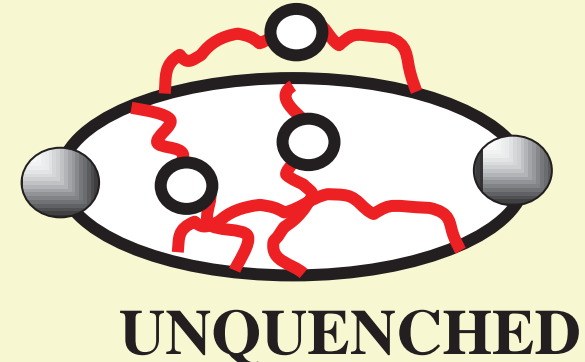
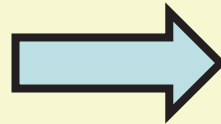
**Unquenched calculations** with relatively **low quark masses** are now being performed by **several groups** using **different approaches** (lattice action, renormalization,...).  
Crucial when aiming at a percent precision.

# "PRECISION" LATTICE QCD: **WHY NOW**

## 1) Increasing of computational power

(Several machines of  $O(10-100 \text{ TeraFlops})$ )

→ Unquenched simulations



## 2) Algorithmic improvements:

→ Light quark masses  
in the ChPT regime

# FLAVOUR PHYSICS ON THE LATTICE

Collaboration	Quark action	Nf	a [fm]	$(M_\pi)^{\min}$ [MeV]	Observables
MILC + FNAL, HPQCD,...	Improved staggered	2+1	$\geq 0.045$	230	$f_K, B_K, f_{D(s)},$ $D \rightarrow \pi/K l \nu, f_{B(s)},$ $B_{B(s)}, B \rightarrow D/\pi l \nu$
PACS-CS	Clover (NP)	2+1	0.09	156	$f_K$
RBC/UKQCD	DWF	2+1	$\geq 0.08$	290	$f_+(0), f_K, B_K$
BMW	Clover smeared	2+1	$\geq 0.07$	190	$f_K$
JLQCD	Overlap	2 2+1	0.12	290	$B_K$
ETMC	Twisted mass	2 2+1+1	$\geq 0.07$	260	$f_+(0), f_K, B_K, f_{D(s)},$ $D \rightarrow \pi/K l \nu, f_{B(s)}$
QCDSF	Clover (NP)	2	$\geq 0.06$	300	$f_+(0), f_K$

# Importance and Success of Lattice QCD in Flavour Physics

•  $V_{us}$  and the “1<sup>st</sup> row” unitarity test

• The Unitarity Triangle Analysis (UTA)

$|V_{us}| \equiv \lambda$   
(CKM parameter:  
 $\sin \theta_{\text{Cabibbo}}$ )

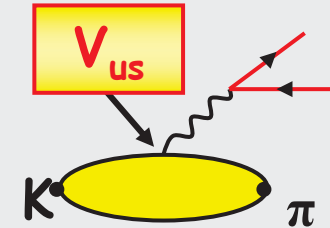
1<sup>st</sup> row: the most stringent unitarity test

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

Source: Nuclear  $\beta$ -dec. K13,K12       $b \rightarrow u$  semil.  
Abs. error:  $4 \cdot 10^{-4}$        $5 \cdot 10^{-4}$        $\sim 10^{-6}$

# $\lambda = V_{us}$ from $Kl3$ decays

$$\Gamma_{K \rightarrow \pi l \nu} = C_K^2 \frac{G_F^2 m_K^5}{192 \pi^2} / S_{EW} [1 + \Delta_{SU(2)} + 2\Delta_{EM}] \times (|V_{us}|^2 |f_+^{K\pi}(0)|^2)$$



Ademollo-Gatto:  $f_+(0) = 1 - O(m_s - m_u)^2 \leftarrow O(1\%)$ . But represents the largest theoret. uncertainty

## ChPT

$$f_+(0) = 1 + f_2 + f_4 + O(p^8)$$

Vector Current Conservation

$f_2 = -0.023$   
Independent of  $L_i$   
(Ademollo-Gatto)

THE LARGEST  
UNCERTAINTY

Old standard estimate:

Leutwyler, Roos  
(1984)

(QUARK MODEL)

$$f_4 = -0.016 \quad 0.008$$

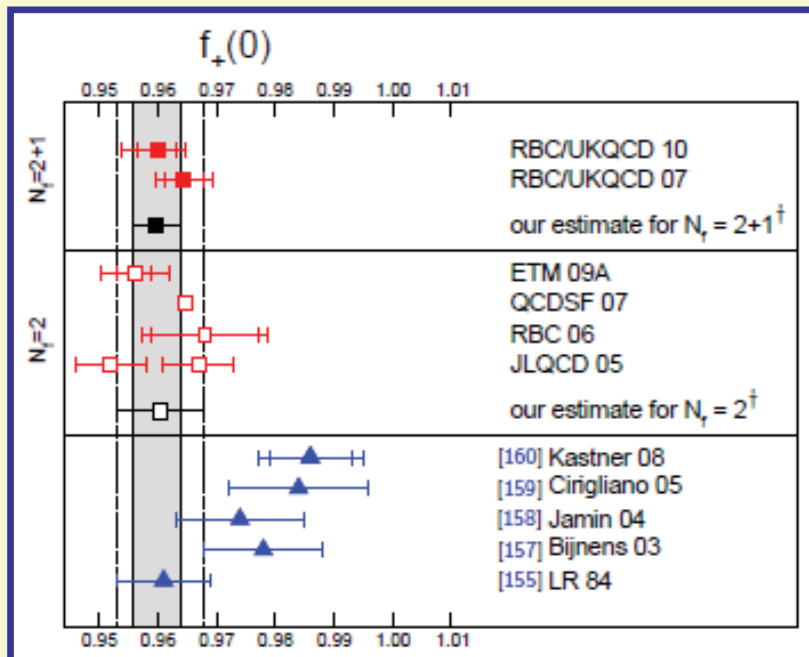
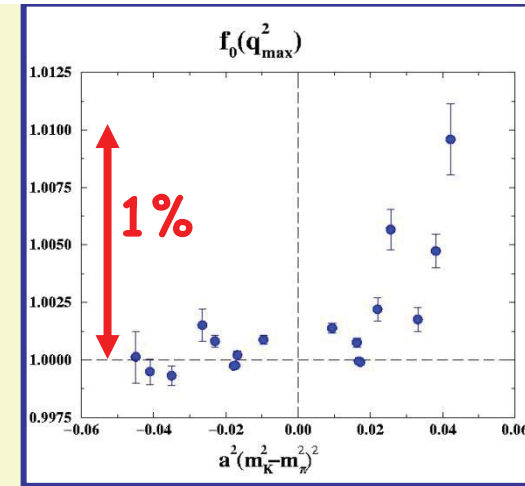


# Lattice QCD

THE **O(1%)** PRECISION CAN BE REACHED

D.Becirevic, G.Isidori, V.Lubicz, G.Martinelli, F.Mescia, S.Simula, C.T., G.Villadoro. [NPB 705,339,2005]

The basic ingredient is a **double ratio** of correlation functions [FNAL for  $B \rightarrow D, D^*$ ]



- **Good agreement** between  $N_f=2$  and  $2+1$  calculations and the first quenched result

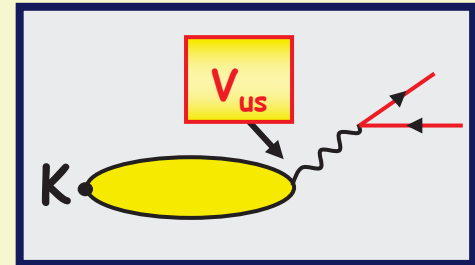
- **Analytical (model dependent) results slightly higher than Lattice QCD**

Flavour Lattice Averaging Group (FLAG)  
[1011.4408]

$$f_+(0)=0.956(8) \rightarrow |V_{us}|=0.225(1)$$

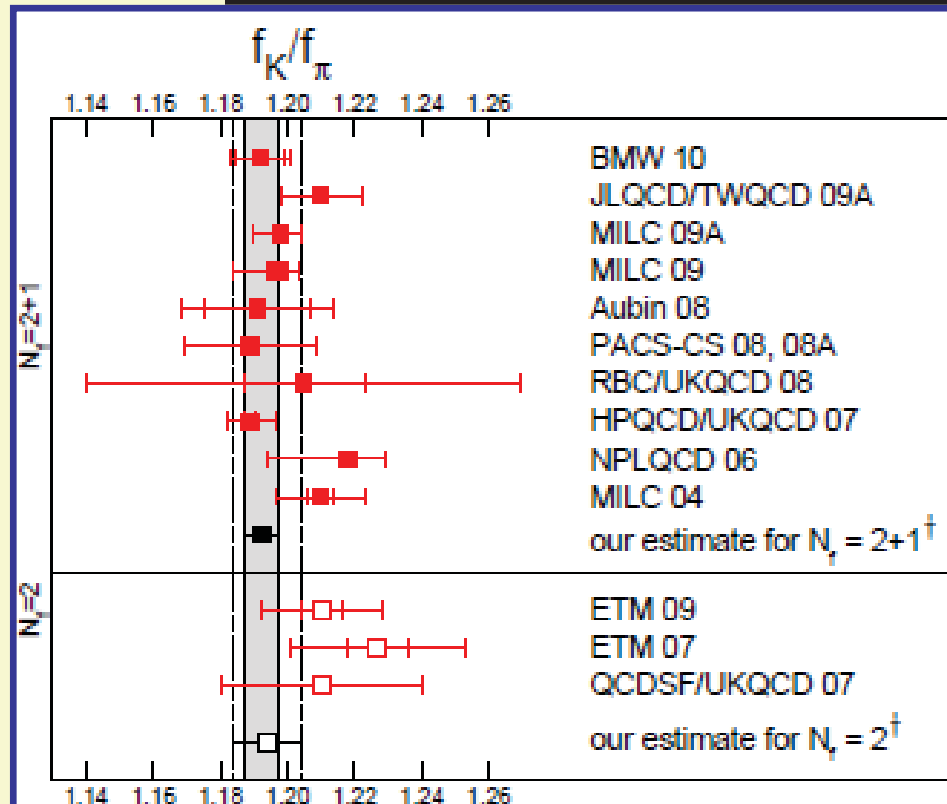
# $V_{us}/V_{ud}$ from $K\mu 2/\pi\mu 2$ decays

$$\frac{\Gamma(K \rightarrow \mu \bar{\nu}_\mu (\gamma))}{\Gamma(\pi \rightarrow \mu \bar{\nu}_\mu (\gamma))} = \frac{|V_{us}|^2}{|V_{ud}|^2} \left( \frac{f_K}{f_\pi} \right)^2 \frac{m_K (1 - \frac{m_\mu^2}{m_K^2})}{m_\pi (1 - \frac{m_\mu^2}{m_\pi^2})} \times 0.9930(35) \quad [\text{Marciano 04}]$$



The **lattice determination** of  $f_K/f_\pi$ , together with the experimental measurement of the leptonic decay Br's, and with  $|V_{ud}|$  from nucleon beta decays, allows to extract  $|V_{us}|$

# $f_K/f_\pi$ : LATTICE SUMMARY



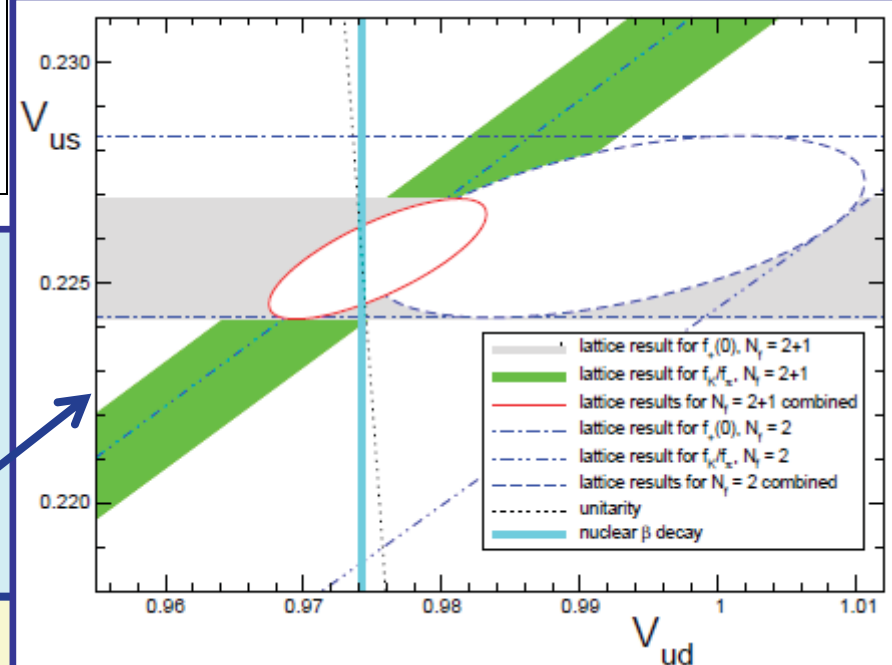
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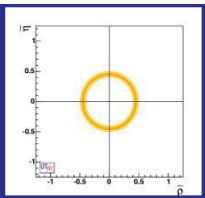
$$f_K/f_\pi = 1.193(6)$$

$$|V_{us}| = 0.225(1)$$

FLAG

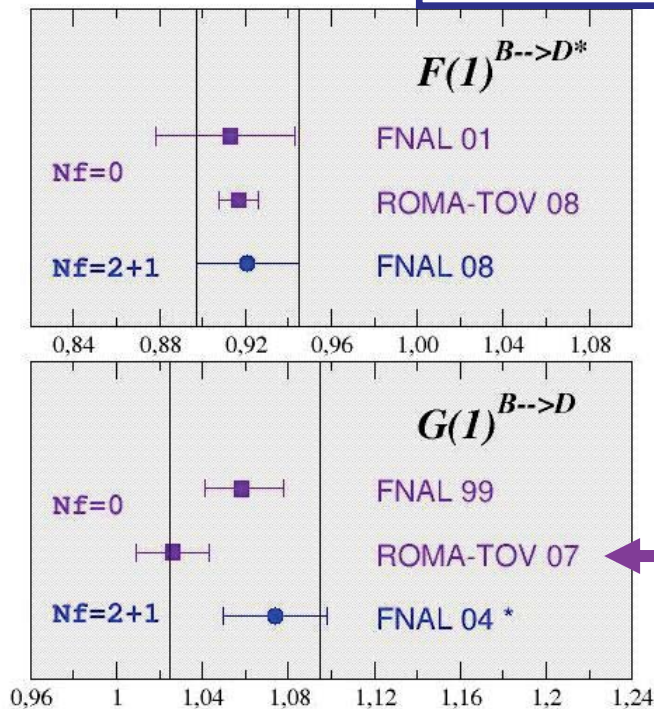
- There is no visible difference between  $N_f=2$  and  $2+1$  with present uncertainties
- K13 and K12 determinations of  $V_{us}$  are in perfect agreement
- First row unitarity test works well





# Exclusive $V_{cb} = A \lambda^2$

$$\frac{d\Gamma^{B \rightarrow D\ell\nu\ell}}{dw} = |V_{cb}|^2 \frac{G_F^2}{48\pi^3} (M_B + M_D)^2 M_D^3 (w^2 - 1)^{3/2} [G^{B \rightarrow D}(w)]^2$$



## TWO DIFFERENT APPROACHES:

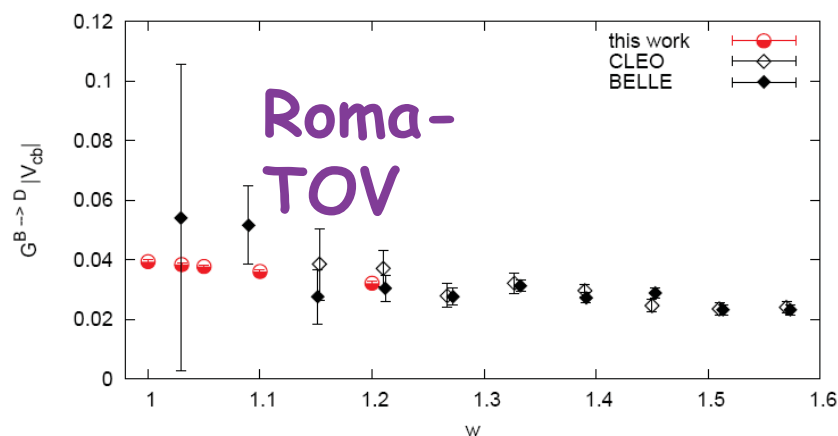
- "double ratios" (FNAL)
- "step scaling" (TOV)

Remarkable agreement

Averages from  
V. Lubicz, CT 0807.4605

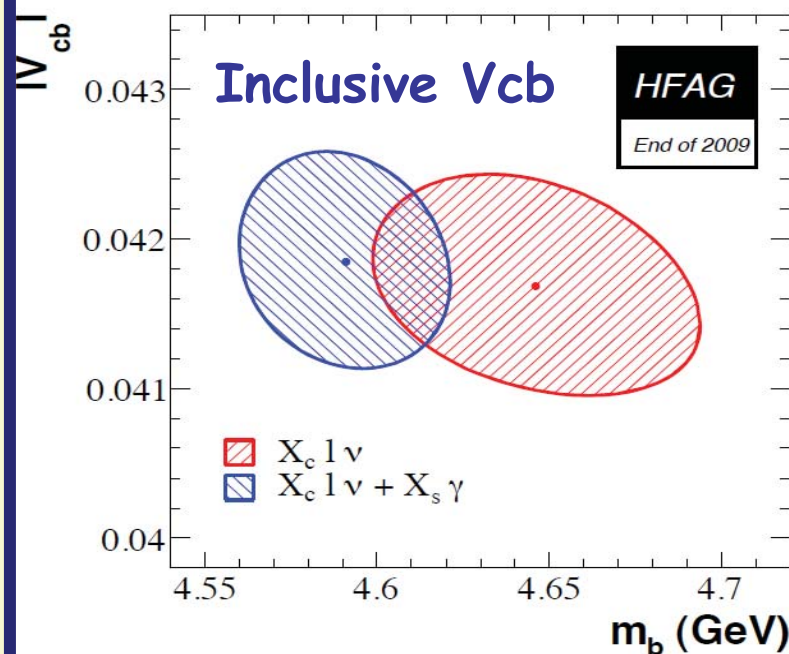
$F(1) = 0.924 \pm 0.022$  2%

$G(1) = 1.060 \pm 0.035$  3%



$$|V_{cb}|_{\text{excl.}} = (39.0 \pm 0.9) 10^{-3}$$

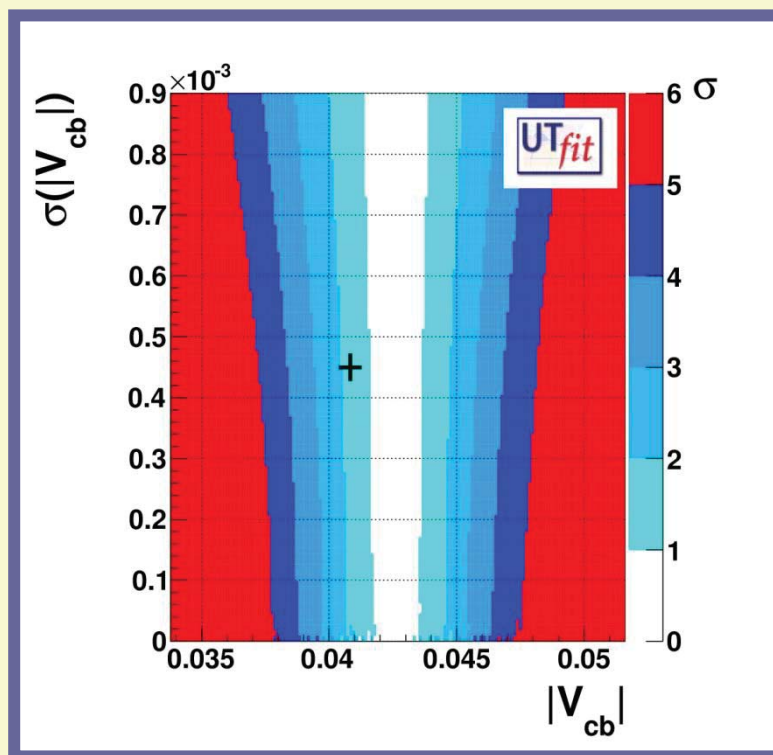
# Exclusive vs Inclusive $V_{cb}$



$$|V_{cb}|_{\text{incl.}} = (41.7 \pm 0.7) 10^{-3}$$

$\updownarrow$   **$2.5\sigma$**

$$|V_{cb}|_{\text{excl.}} = (39.0 \pm 0.9) 10^{-3}$$



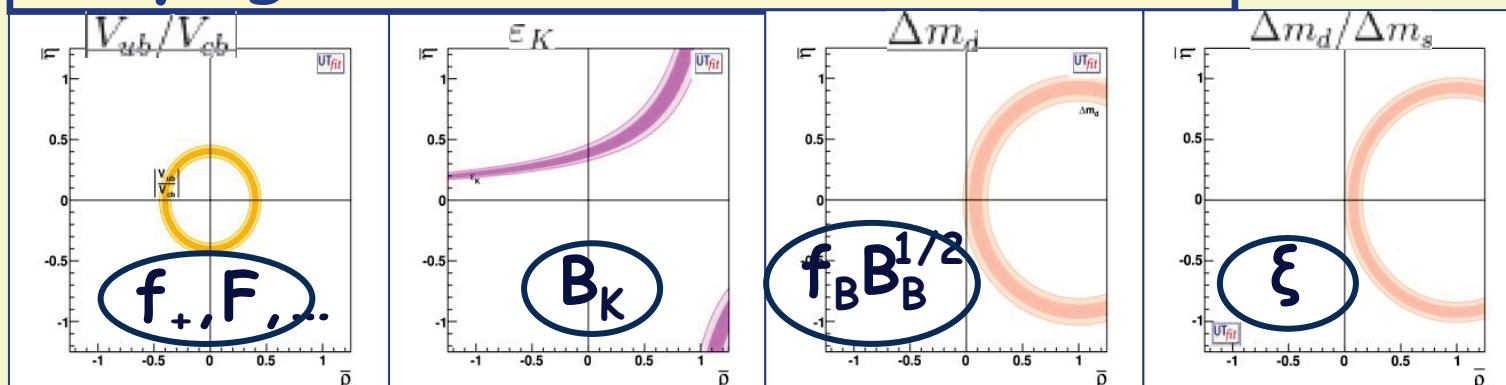
$$|V_{cb}|_{\text{SM-Fit}} = (42.7 \pm 1.0) 10^{-3}$$

**UTfit**

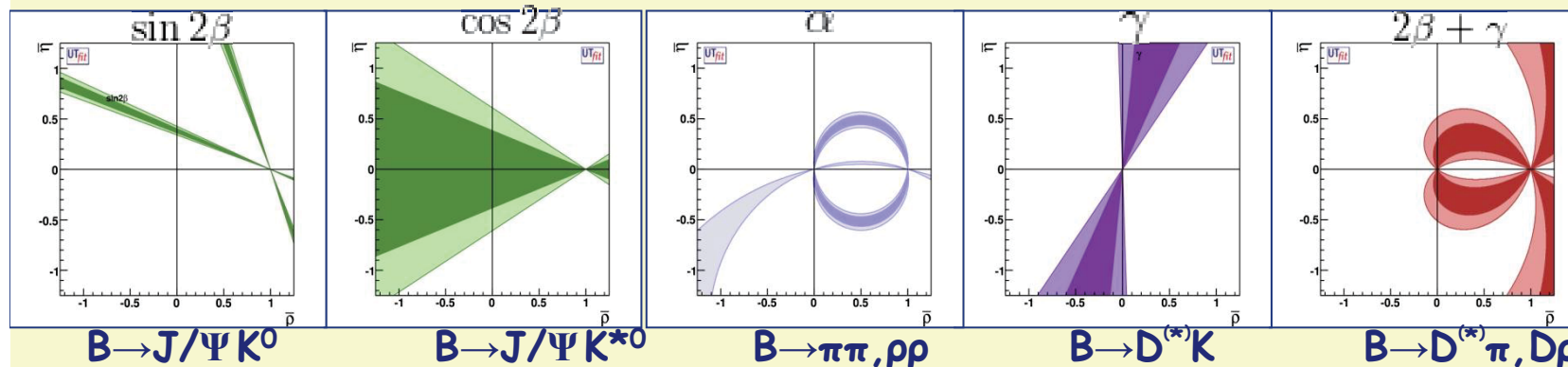
# THE UTA CONSTRAINTS



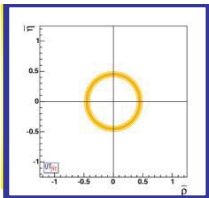
## Relying on LATTICE calculations



## UT-ANGLES



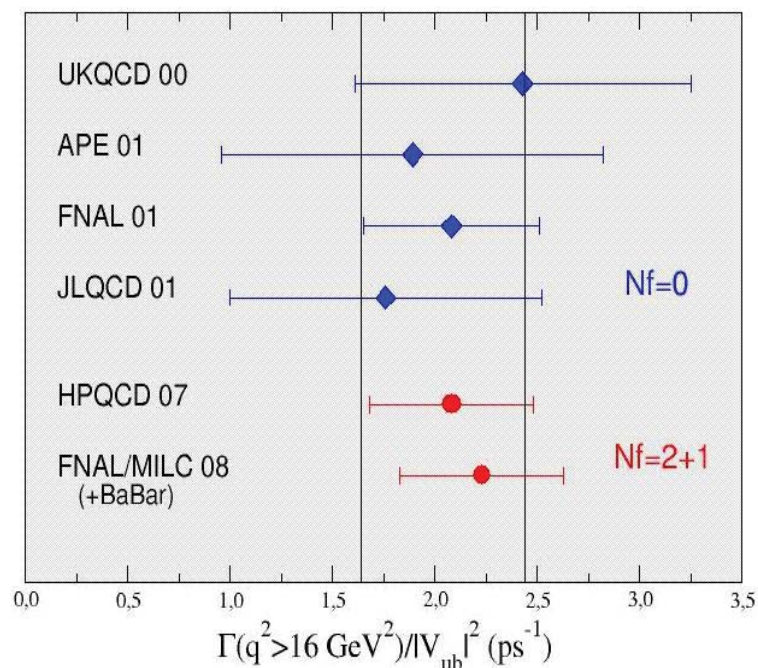




# Exclusive vs Inclusive $V_{ub}$

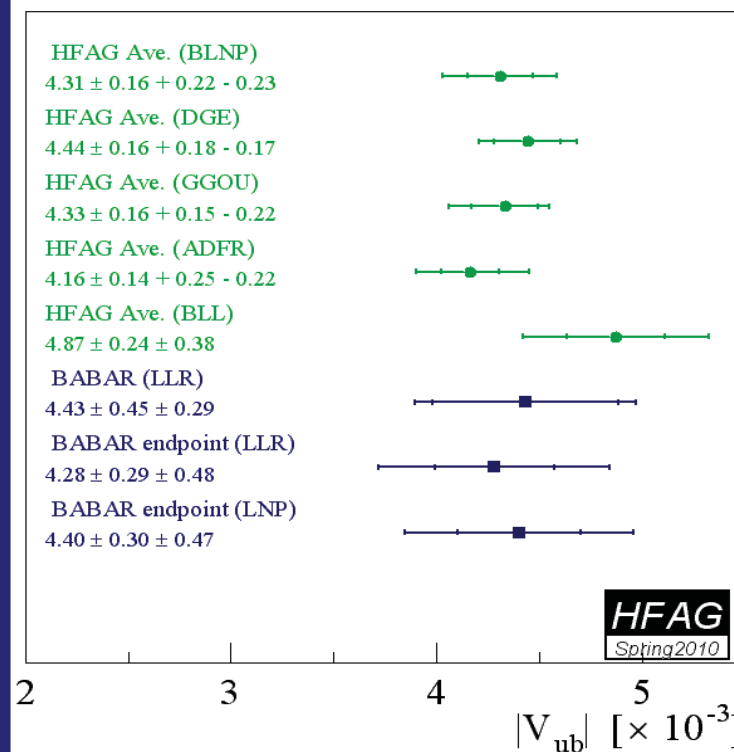
THEORETICALLY CLEAN  
BUT MORE LATTICE  
CALCULATIONS ARE WELCOME

$$\frac{d\Gamma(B \rightarrow \pi \ell \nu)}{dq^2} = \frac{G_F^2 |V_{ub}|^2}{192\pi^3 m_B^3} [(m_B^2 + m_\pi^2 - q^2)^2 - 4m_B^2 m_\pi^2]^{3/2} |f_+(q^2)|^2$$

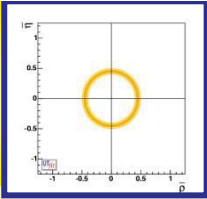


$$|V_{ub}|_{\text{excl.}} = (35.0 \pm 4.0) 10^{-4}$$

IMPORTANT LONG DISTANCE  
CONTRIBUTIONS (in the  
threshold region). THE RESULTS  
ARE MODEL DEPENDENT



$$|V_{ub}|_{\text{incl.}} = (42.0 \pm 1.5 \pm 5.0) 10^{-4}$$



# Exclusive vs Inclusive $V_{ub}$

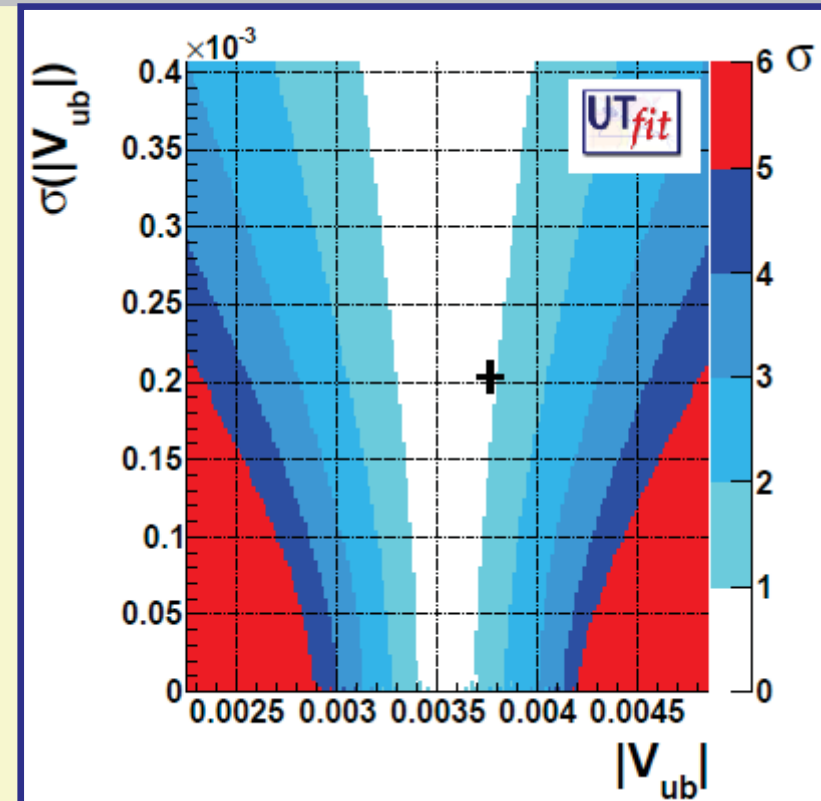
- The uncertainty of inclusive  $V_{ub}$  estimated from the spread among different models. This is questionable

- The fit in the SM favors a low value of  $V_{ub}$ , as indicated by exclusive decays

$$|V_{ub}|_{\text{incl.}} = (42.0 \pm 1.5 \pm 5.0) 10^{-4}$$

$$|V_{ub}|_{\text{excl.}} = (35.0 \pm 4.0) 10^{-4}$$

- Improve the accuracy of exclusive  $V_{ub}$  in order to clarify the issue

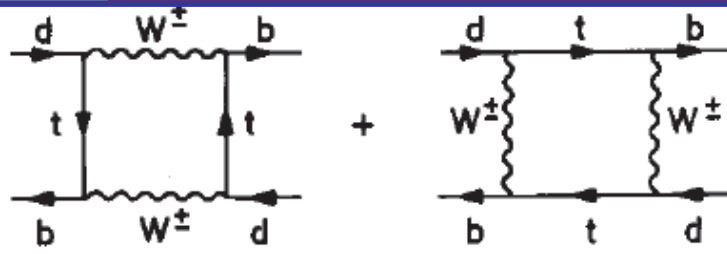


UT\_fit

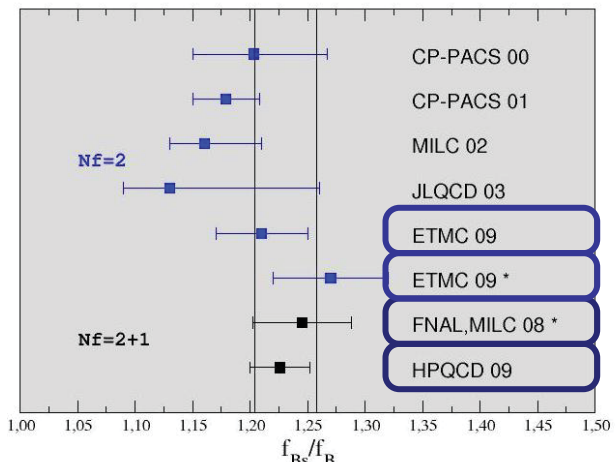
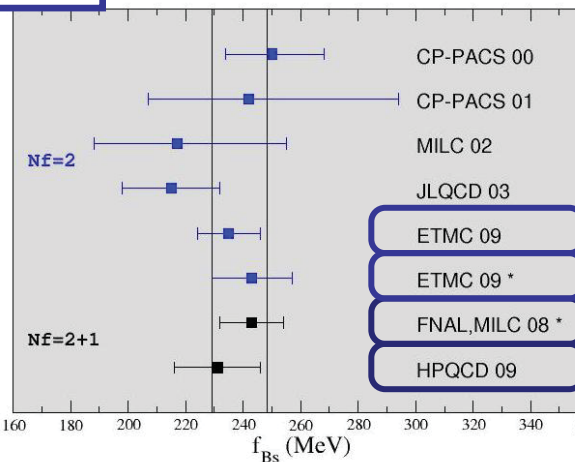
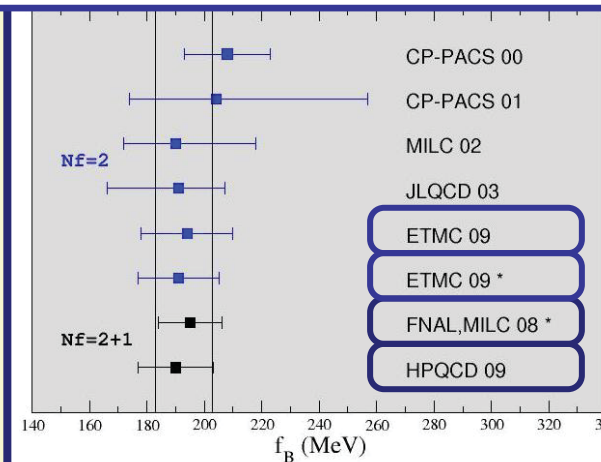
$$|V_{ub}|_{\text{SM-Fit}} = (35.5 \pm 1.4) 10^{-4}$$



# B-mesons decay constants $f_B, f_{B_s}$ and $B\text{-}\bar{B}$ mixing, $\hat{B}_{B_d/s}$



$$\Delta M_q = \frac{G_F^2}{6\pi^2} \eta_B m_{B_q} (\hat{B}_{B_q} F_{B_q}^2) M_W^2 S_0(x_t) |V_{tq}|^2$$



$$f_{B_s} = 238.8 \quad 9.5 \text{ MeV}$$

$$f_B = 192.8 \quad 9.9 \text{ MeV}$$

4-5%

$$f_{B_s}/f_B = 1.231 \quad 0.027$$

2%

Combining with the only modern calculation HPQCD [0902.1815]:

$$\hat{B}_{B_d} = 1.26 \pm 0.11, \hat{B}_{B_s} = 1.33 \pm 0.06$$

$$f_{B_s} \sqrt{\hat{B}_{B_s}} = 275 \quad 13 \text{ MeV}$$

5%

$$\xi = 1.243 \pm 0.028$$

2%

$\epsilon_K$ : indirect CP-violation due to  $K^0$ - $\bar{K}^0$  mixing

Mixing formalism as in the B system

$$CP|K^0\rangle = -|\bar{K}^0\rangle, \quad CP|\bar{K}^0\rangle = -|K^0\rangle$$

$$i\frac{d\psi(t)}{dt} = \hat{H}\psi(t) \quad \psi(t) = \begin{pmatrix} |K^0(t)\rangle \\ |\bar{K}^0(t)\rangle \end{pmatrix}$$

$$\hat{H} = \begin{pmatrix} M - i\frac{\Gamma}{2} & M_{12} - i\frac{\Gamma_{12}}{2} \\ M_{12}^* - i\frac{\Gamma_{12}^*}{2} & M - i\frac{\Gamma}{2} \end{pmatrix}$$

H eigenstates (in the flavor and CP bases)

$$K_{L,S} = \frac{(1 + \bar{\epsilon})K^0 \pm (1 - \bar{\epsilon})\bar{K}^0}{\sqrt{2(1 + |\bar{\epsilon}|^2)}}$$

$$K_S = \frac{K_1 + \bar{\epsilon}K_2}{\sqrt{1 + |\bar{\epsilon}|^2}}, \quad K_L = \frac{K_2 + \bar{\epsilon}K_1}{\sqrt{1 + |\bar{\epsilon}|^2}}$$

$$K_L \propto K_2 + \bar{\epsilon} K_1$$

indirect:  $\epsilon$

direct :  $\epsilon'$

$\rightarrow \pi\pi$

$\rightarrow \pi\pi$

Within the K system:

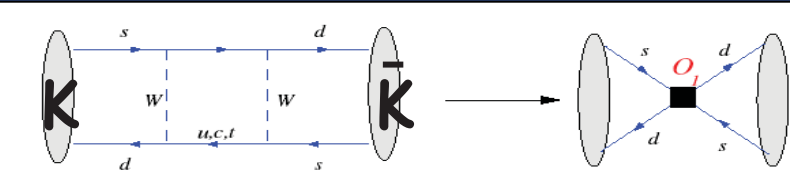
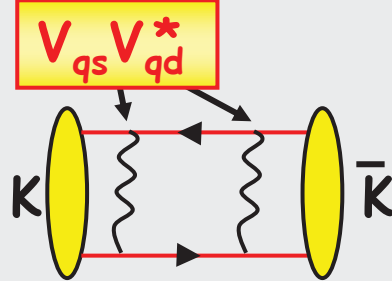
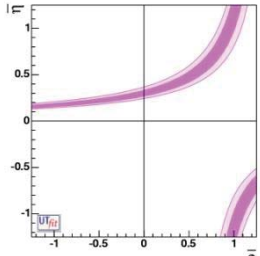
$$\text{Im}M_{12} \ll \text{Re}M_{12}, \quad \text{Im}\Gamma_{12} \ll \text{Re}\Gamma_{12}$$

$$\Delta M_K = 2\text{Re}M_{12}, \quad \Delta\Gamma_K = 2\text{Re}\Gamma_{12}$$

$$\epsilon_K = \sin\phi_\epsilon e^{i\phi_\epsilon} \left[ \frac{\text{Im}M_{12}^{(6)}}{\Delta m_K} + \rho\xi \right]$$

- Phase convention independent
- different CKM w.r.t B case
- The 3 GIM combinations are all relevant

# $K^0 - \bar{K}^0$ mixing: $B_K$



$$\langle \bar{K}^0 | Q(\mu) | K^0 \rangle = \frac{8}{3} f_K^2 m_K^2 B_K(\mu)$$

## Pre-history

**QCD SR**, Pich, De Rafael, **1985**:

$$\hat{B}_K = 0.33 \quad 0.09$$

**1/Nc exp.**, Buras, Gerard, **1985**:

$$\hat{B}_K = 0.75$$

**LQCD**, Gavela et al., **1987**:

$$\hat{B}_K = 0.90 \quad 0.20$$

## History

**Quench. error**

$$\hat{B}_K = 0.90 \quad 0.03 \quad 0.15$$

S. Sharpe@Latt'96 **17%**

$$\hat{B}_K = 0.86 \quad 0.05 \quad 0.14$$

L. Lellouch@Latt'00 **17%**

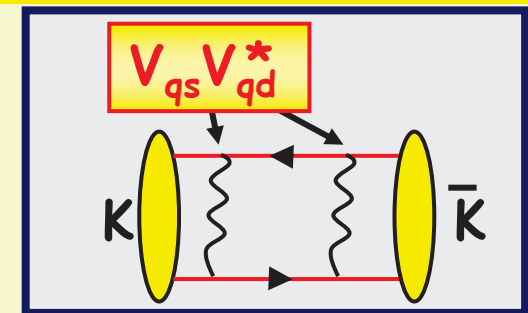
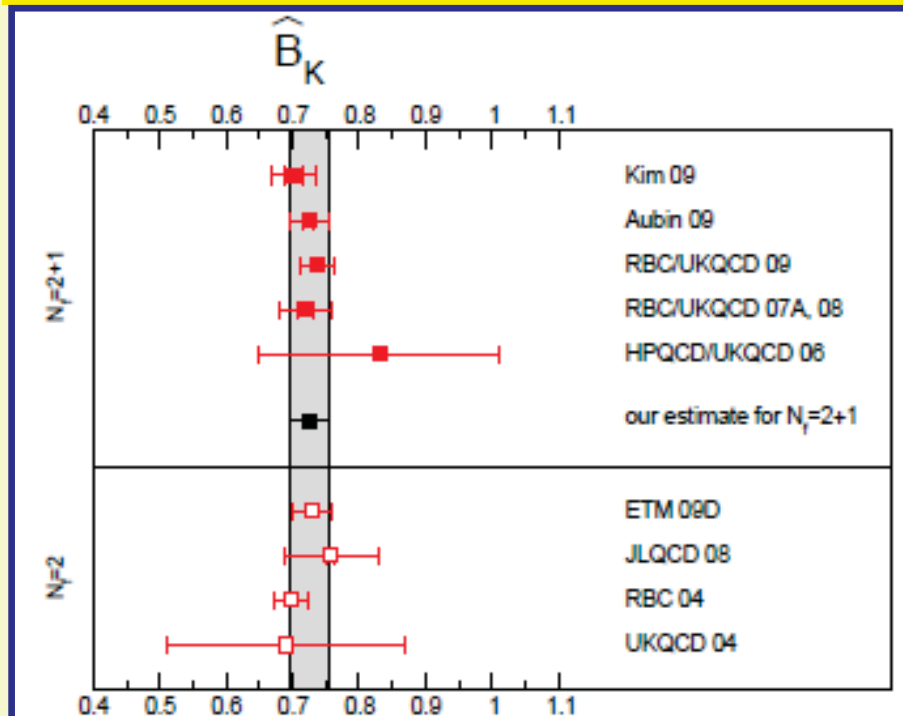
$$\hat{B}_K = 0.79 \quad 0.04 \quad 0.08$$

C. Dawson@Latt'05 **11%**

$$\hat{B}_K = 0.731 \quad 0.036$$

V. Lubicz@Latt'09 **5%**

# $K^0-\bar{K}^0$ mixing: $B_K$



$$\hat{B}_K = 0.724(8)(29)$$

[ FLAG ]

5%

Buras&Guadagnoli (0805.3887)+Buras&Guadagnoli&Isidori (1002.3612):

decrease of the SM prediction of  $\epsilon_K$  by ~6%

$$\epsilon_K = \sin \phi_\epsilon e^{i\phi_\epsilon} \left[ \frac{\text{Im} M_{12}^{(6)}}{\Delta m_K} + \rho \xi \right]$$

Long-distance

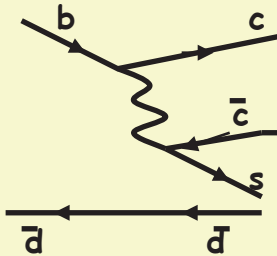
$$\beta (\phi_1)$$

$$V_{td} = |V_{td}| e^{-i\beta}$$

Golden mode:  $B \rightarrow J_\psi K_S$

Dominated by one tree-level  
amplitude  $b \rightarrow \bar{c}cs$

Simple expr. for the t-dep. CP-asymmetry  
 $A_{CP}(t) = -\sin 2\beta \sin(\Delta M_d t)$



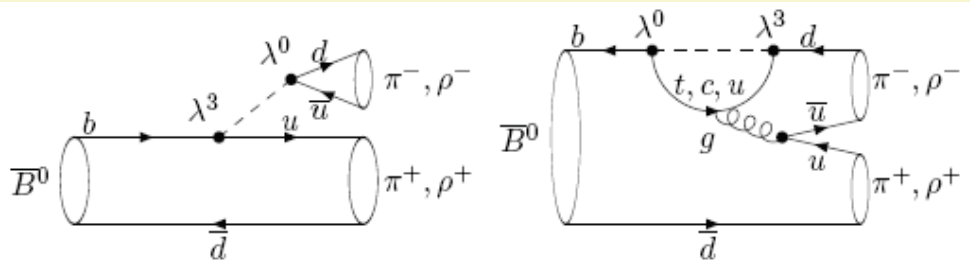
Main theoretical uncertainty from the hadronic matrix elements  
of the CKM-suppressed  $b \rightarrow \bar{u}us$  contribution  
(irreducible theory error  $\sim 1\%$ )

- Similar simplification in other  $b \rightarrow \bar{c}cs$  channels:  
 $\Psi(2S)K_S, \chi_{c1} K_S, \eta_c K_S, J_\psi K_L, J_\psi K^*, B_s \rightarrow \Psi\phi$
- Alternative determinations (sensitive to NP) from the  
charmless  $b \rightarrow s$  one-loop (penguin) amplitude:  $B \rightarrow \eta' K_{S,L}, B \rightarrow \phi K_S$
- $\cos 2\beta$  from a time-dep. analysis of  $B \rightarrow J_\psi K^*, B \rightarrow D \pi^0$   
( $\cos 2\beta > 0$  solving the  $\beta \leftrightarrow (\pi/2 - \beta)$  ambiguity)

$$\alpha (\phi_2)$$

$$\alpha = \arg \left[ - \frac{V_{td} V_{tb}^*}{V_{ud} V_{ub}^*} \right]$$

from **charmless decays**:  $B \rightarrow \pi\pi$ ,  $B \rightarrow \rho\rho$ ,  $B \rightarrow \rho\pi$   
 ( $\leftrightarrow$  **tree-level transition**  $b \rightarrow \bar{u}ud$  **carrying**  $V_{ub}$ )



The penguin contribution, introducing different CKM factors, complicate the extraction of  $\alpha$ :  
**tree-penguin disentanglement** is required

Analysis of a **large set of observables**:  
 $Br$ 's,  $A_{CP}(t)$  both in neutral and charged B decays

$B \rightarrow \pi\pi$ : **isospin analysis** [M.Gronau, D.London, 1990] + info from  $Br(B_s \rightarrow K^+ K^-)$  [M.Bona et al (UTfit), hep-ph/0701204]

$B \rightarrow \rho\rho$ : **advantage of the suppression of  $Br(B \rightarrow \rho^0 \rho^0)$  and of the related uncertainty**

$B \rightarrow \rho\pi$ : **advantage of  $\rho^+ \pi^-$  and  $\rho^- \pi^+$  reachable by both  $B^0$  and  $\bar{B}^0$ , no model-dependance for the strong phase**

[A.E.Snyder, H.R.Quinn, 1993]

Main theoretical uncertainty  
 from **isospin violations**  
 mainly in ew penguins and FSI  
 (irreducible theory error few%)

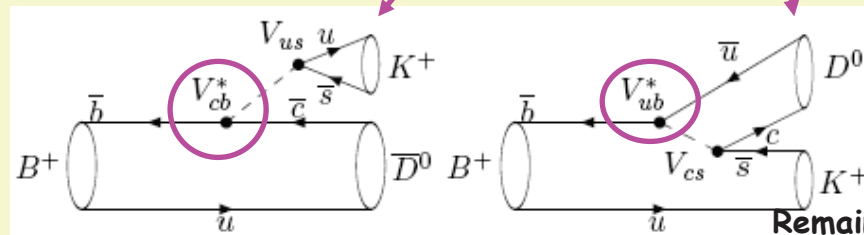
$$\gamma (\phi_3)$$

$$V_{ub} = |V_{ub}| e^{-i\gamma}$$

## Determination of $\gamma$ from $B \rightarrow DK$ decays:

[I.I.Y.Bigi, A.I.Sanda, 1988, A.B.Carter, A.I. Sanda, 1988]

- $B^+ \rightarrow DK^+$  can produce both  $D^0$  and  $\bar{D}^0$ , via  $\bar{b} \rightarrow \bar{c} u \bar{s}$  and  $\bar{b} \rightarrow \bar{u} c \bar{s}$
- $D^0$  and  $\bar{D}^0$  can decay to a common final state
- The two amplitudes interfere with a relative phase  $\delta_B \quad \gamma$ , for  $B^+(B^-)$



Main contributions  
from (theoretically clean)  
tree-level diagrams

Remaining theoretical uncertainty  
from simplifying  $D$ - $\bar{D}$  mixing neglect  
(irreducible theory error 0.1%)

## Various methods consider different final states:

- CP-eigenstates (Gronau, London, Wyler [GLW]) ( $\pi^+ \pi^-$ ,  $K^+ K^-$ ,  $K_S \pi^0$ ,  $K_S \phi$ ,  $K_S \omega$ , ...)
- doubly Cabibbo suppressed D modes (Atwood, Dunietz, Soni [ADS]) ( $K^+ \pi^-$ ,  $K^+ \rho^-$ ,  $K^* \pi^-$ , ...)
- three-body D decaying modes (Dalitz plot analysis) ( $K_S \pi^+ \pi^-$  provides the best estimate at present)

[A.Giri, hep-ph/0303187]

The best strategy is a combined analysis taking into account many  $D$  and  $D^*$  modes

# The UTA within the Standard Model

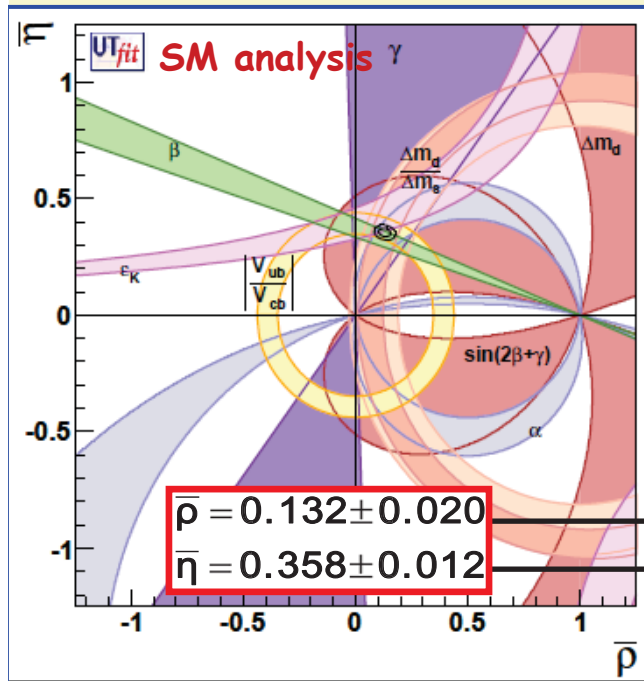


The experimental constraints:

$$\varepsilon_K, \Delta m_d, \left| \frac{\Delta m_s}{\Delta m_d} \right|, \left| \frac{V_{ub}}{V_{cb}} \right| \rightarrow \text{relying on theoretical calculations of hadronic matrix elements}$$

$$\sin 2\beta, \cos 2\beta, \alpha, \gamma (2\beta + \gamma) \rightarrow \text{independent from theoretical calculations of hadronic parameters}$$

overconstrain the CKM parameters consistently



The UTA has established that the CKM matrix is the dominant source of flavour mixing and CP violation





## From a closer look

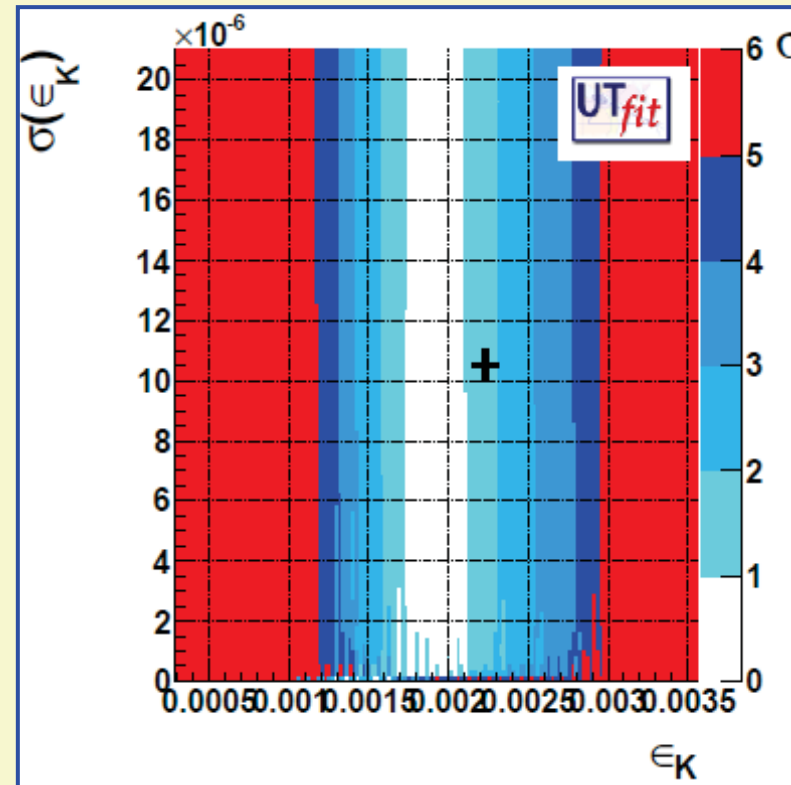


From the UTA  
(excluding its exp. constraint)

	Prediction	Measurement	Pull
$\sin 2\beta$	$0.771 \pm 0.036$	$0.654 \pm 0.026$	2.6 ←
$\gamma$	$69.6^\circ \pm 3.1^\circ$	$74^\circ \pm 11^\circ$	<1
$\alpha$	$85.4^\circ \pm 3.7^\circ$	$91.4^\circ \pm 6.1^\circ$	<1
$ V_{cb}  \cdot 10^3$	$42.69 \pm 0.99$	$40.83 \pm 0.45$	+1.6
$ V_{ub}  \cdot 10^3$	$3.55 \pm 0.14$	$3.76 \pm 0.20$	<1
$\varepsilon_K \cdot 10^3$	$1.92 \pm 0.18$	$2.230 \pm 0.010$	-1.7 ←
$\text{BR}(B \rightarrow \tau \nu) \cdot 10^4$	$0.805 \pm 0.071$	$1.72 \pm 0.28$	-3.2 ←

$\epsilon_K$ 

UTfit

**NEWS:**

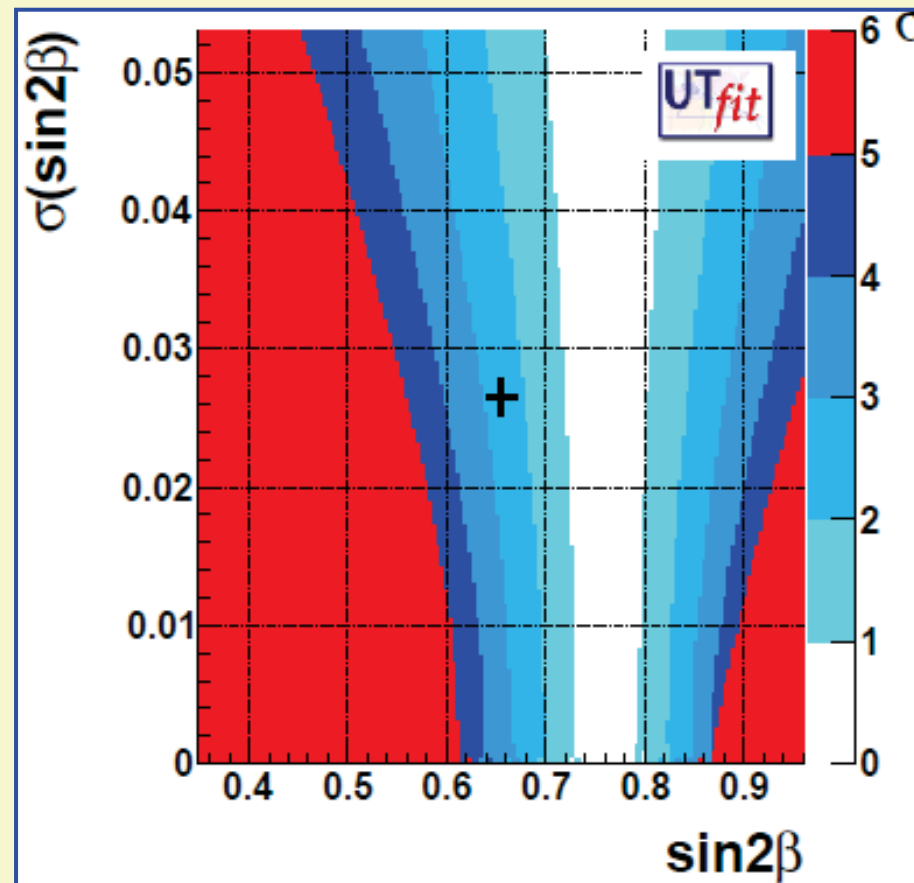
Brod&Gorbahn (1007.0684): **NNLO QCD analysis** of the charm-top contribution in box diagrams  
(3% **enhancement** of  $\epsilon_K$ ),  
charm-charm contribution in progress

**NEXT FUTURE:**

Further few percents could come from dimension-8 operators:  $\sim m_K^2/m_c^2$  corrections (calculation in progress)

$\sin 2\beta$

UTfit



The indirect determination of  $\sin(2\beta)$  turns out to be at  $\sim 2.6 \sigma$  from the experimental measurement (the theory error in the extraction from  $B \rightarrow J_\psi K_S$  is well under control)

$B \rightarrow \tau \nu$

UTfit

$BR(B \rightarrow \tau \nu)_{SM} = (0.805 \pm 0.071) \cdot 10^{-4}$   
[UTfit, update of 0908.3470]  
turns out to be **smaller** by  $\sim 3.2 \sigma$   
than the experimental value  
 $BR(B \rightarrow \tau \nu)_{exp} = (1.72 \pm 0.28) \cdot 10^{-4}$

The experimental state of the art

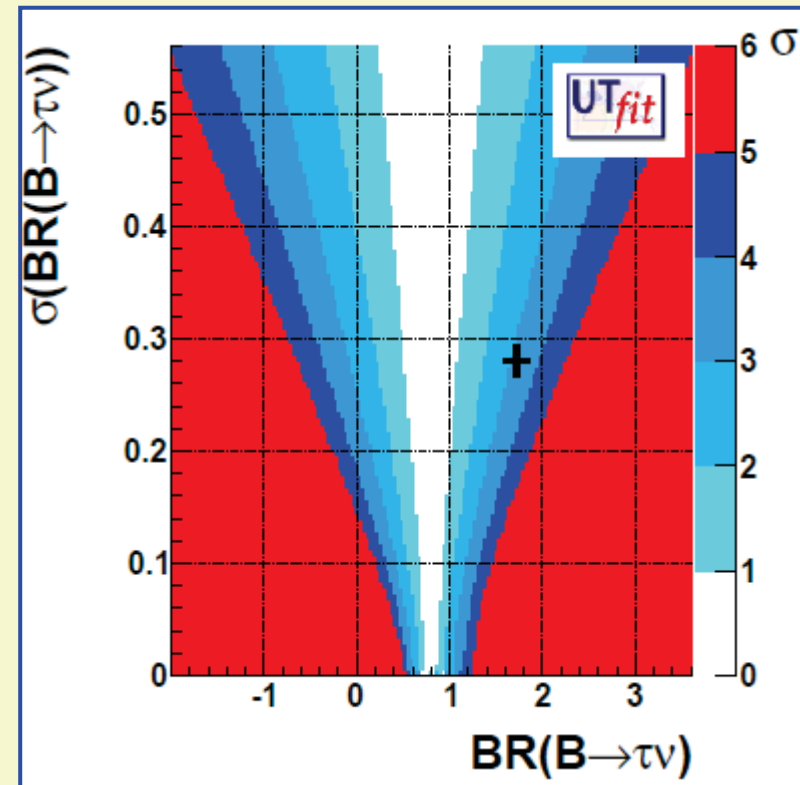
BaBar Semileptonic tag (0912.2453)

BaBar Hadronic tag (0708.226, 1008.0104)

Belle Semileptonic tag (1006.4201)

Belle Hadronic tag (hep-ex/0604018)

[full data set analysis is on the way]



$$BR(B \rightarrow \tau \nu) = \frac{G_F^2 m_B m_\tau^2}{8\pi} \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B$$

- $BR(B \rightarrow \tau \nu)_{exp}$  prefers a large value for  $|V_{ub}|$  ( $f_B$  under control and improved by the UTA)
- But a **shift** in the central value of  $|V_{ub}|$  **would not solve** the  $\beta$  tension  $\rightarrow$  the debate on  $V_{ub}$  (excl. vs incl, various models...) is not enough to explain all

# The UTA beyond the Standard Model

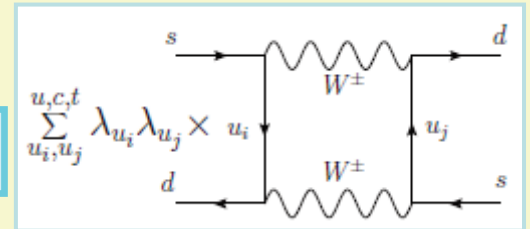


Update of UTfit 0909.5065

**Model-independent UTA:** bounds on deviations from the SM (+CKM)

- Parametrize generic NP in  $\Delta F=2$  processes, in all sectors
- Use all available experimental info
- Fit simultaneously the CKM and NP parameters

**NP contributions in the mixing amplitudes:**



$$H^{\Delta F=2} = m + \frac{i}{2} \Gamma \quad A = m_{12} = \langle M | m | \bar{M} \rangle \quad \Gamma_{12} = \langle M | \Gamma | \bar{M} \rangle$$

K mixing amplitude (2 real parameters):

$$\text{Re } A^K = C_{\Delta m_K} \text{Re } A_K^{SM} \quad \text{Im } A_K = C_{\phi_K} \text{Im } A_K^{SM}$$

$B_d$  and  $B_s$  mixing amplitudes (2+2 real parameters):

$$A_q e^{2i\phi_q} = C_{B_q} e^{2i\phi_{B_q}} A_q^{SM} e^{2i\phi_q^{SM}} = \left( 1 + \frac{A_q^{NP}}{A_q^{SM}} e^{2i(\phi_q^{NP} - \phi_q^{SM})} \right) A_q^{SM} e^{2i\phi_q^{SM}}$$

SM	→	SM+NP
$(V_{ub}/V_{cb})^{\text{SM}}$ $\gamma^{\text{SM}}$		$(V_{ub}/V_{cb})^{\text{SM}}$ $\gamma^{\text{SM}}$
$\beta^{\text{SM}}$ $\alpha^{\text{SM}}$ $\Delta m_d$	<b>Bd Mixing</b>	$\beta^{\text{SM}} + \phi_{\text{Bd}}$ $\alpha^{\text{SM}} - \phi_{\text{Bd}}$ $C_{\text{Bd}} \Delta m_d$
$\Delta m_s^{\text{SM}}$ $-\beta_s^{\text{SM}}$	<b>Bs Mixing</b>	$C_{\text{Bs}} \Delta m_s^{\text{SM}}$ $-\beta_s^{\text{SM}} + \phi_{\text{Bs}}$
$\epsilon_K^{\text{SM}}$ $\Delta m_K^{\text{SM}}$	<b>K Mixing</b>	$C_{\epsilon_K} \epsilon_K^{\text{SM}}$ $C_{\Delta m_K} \Delta m_K^{\text{SM}}$

From this (NP) analysis:

$$\bar{\rho} = 0.135 \pm 0.040$$

$$\bar{\eta} = 0.374 \pm 0.026$$

In good agreement  
with the results  
from the SM analysis

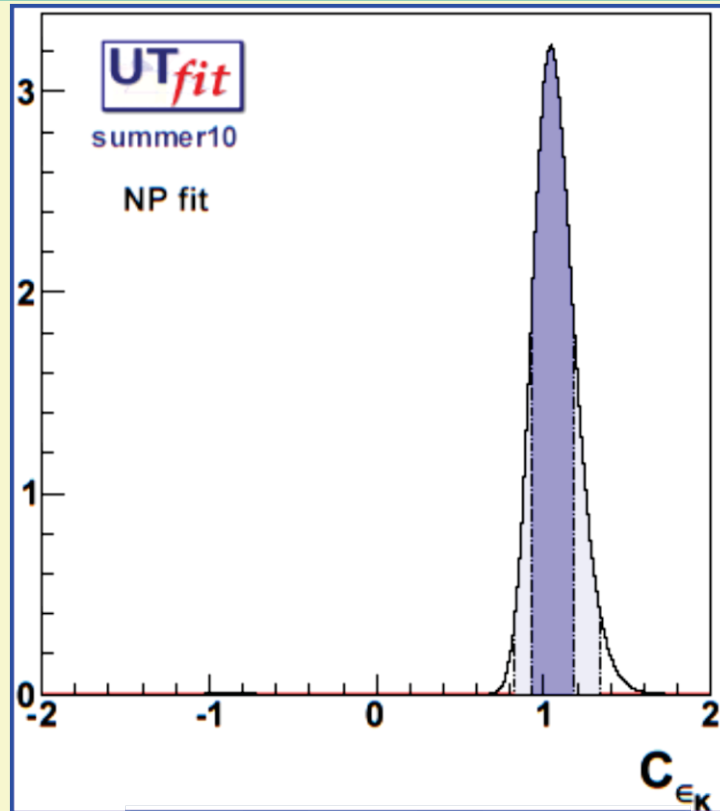
$$\bar{\rho} = 0.132 \pm 0.020$$

$$\bar{\eta} = 0.358 \pm 0.012$$

# Results for the $K$ and $B_d$ mixing amplitudes



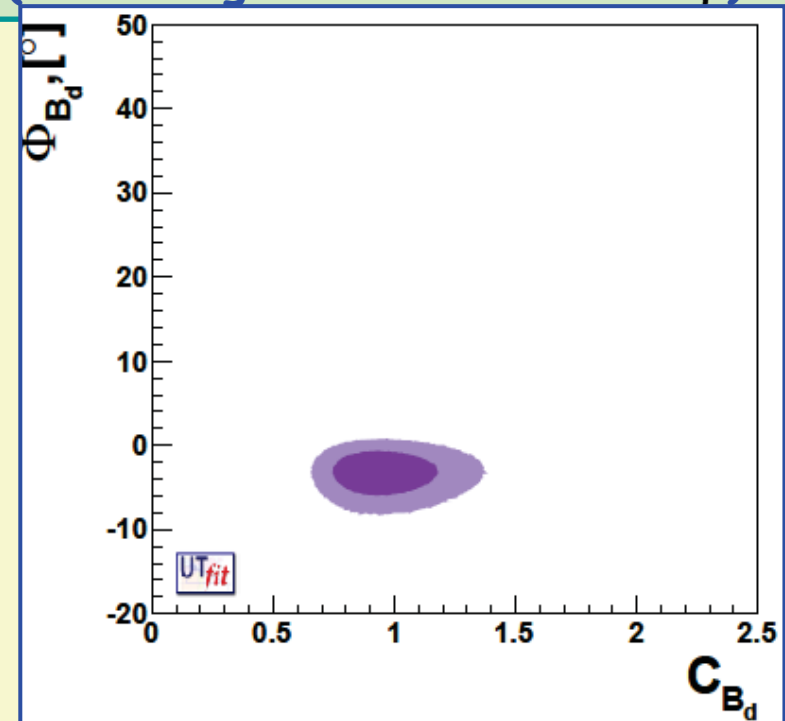
For  $K$ - $\bar{K}$  mixing,  
the NP parameter are found  
in agreement with  
the SM expectations



$$C_{\varepsilon_K} = 1.05 \pm 0.12$$

$$\Phi_{\varepsilon_K} = [0.82, 1.34] \leftrightarrow 95\%$$

For  $B_d$ - $\bar{B}_d$  mixing,  
the mixing phase  $\phi_{B_d}$  is found  
 $1.8 \sigma$  away from the SM  
expectation  
(reflecting the tension in  $\sin 2\beta$ )



$$C_{B_d} = 0.95 \pm 0.14$$

$$\Phi_{B_d} = [-7.0, 0.1] \leftrightarrow 95\%$$

$$\Phi_{B_d} = [-3.1 \pm 1.7]^\circ$$

$$\Phi_{B_d} = [-7.0, 0.1]^\circ \leftrightarrow 95\%$$

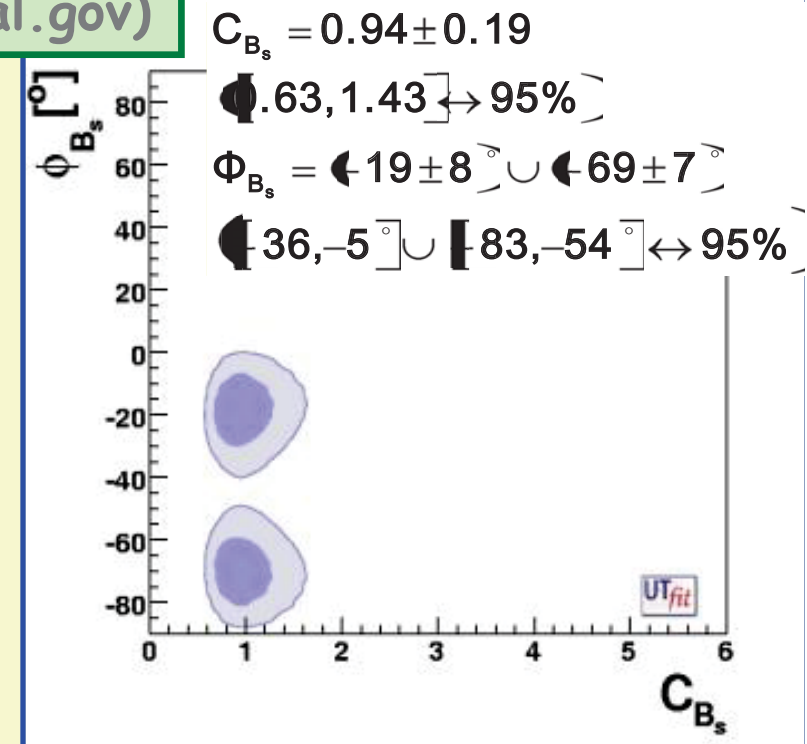
Results for the  $B_s$  mixing amplitude:  
INTERESTING NEWS  $\Rightarrow$  NEW QUESTION MARKS



In 2009, by combining CDF and DØ results for  $\phi_{B_s}$ :

UTfit:  $2.9\sigma$  (update of 0803.0659)  
HFAG:  $2.2\sigma$  (0808.1297)  
CKMfitter:  $2.5\sigma$  (0810.3139)  
Tevatron B w.g.:  $2.1\sigma$  (<http://tevbwg.fnal.gov>)

More than  $2\sigma$  deviation for  
every statistical approach!

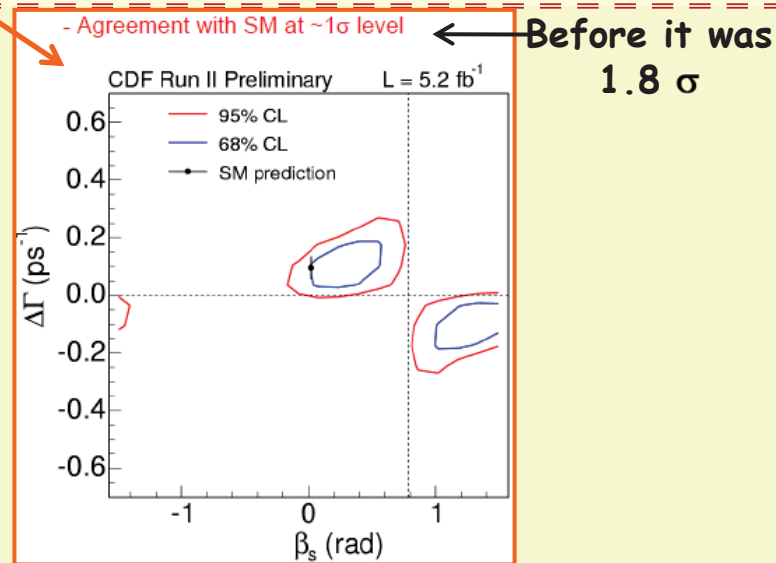




## In 2010, two surprising news:

The new CDF measurement reduces the significance of the deviation.

The likelihood is not yet available, a CDF Bayesian study is underway



The new  $D\bar{D}$  measurement of  $a_{\mu\mu}$  points to large  $\beta_s$  but also to large  $\Delta\Gamma_s$  requiring a non-standard  $\Gamma_{12}$  !?!

If confirmed, two (UNLIKELY) explanations:

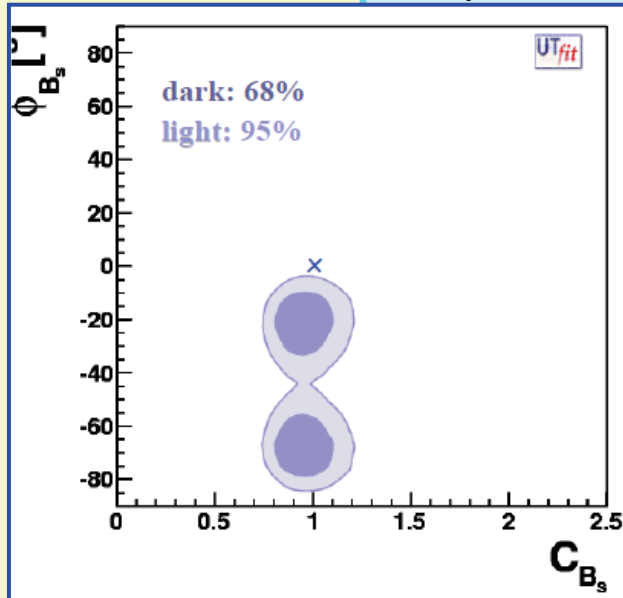
- Huge (tree-level-like) NP contributions in  $\Gamma_{12}$

(a factor 2.5: why only in  $\Gamma_{12}$ ??)

- Bad failure of the OPE in  $\Gamma_{12}$

(while in  $\Gamma_{11}$  (b-hadron lifetimes) works well)

# Updated Results including NEW $D\bar{D}$ results (new CDF results are not yet available)



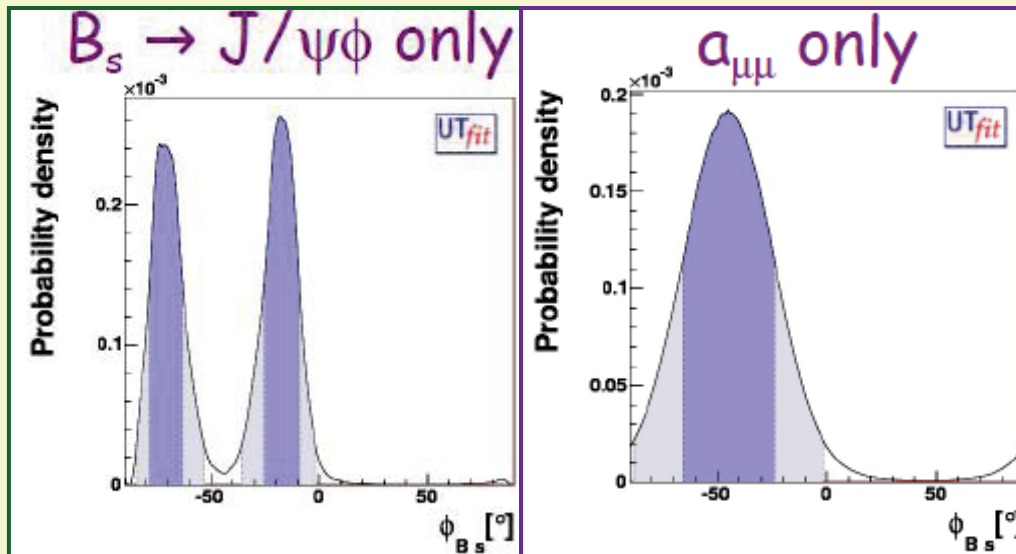
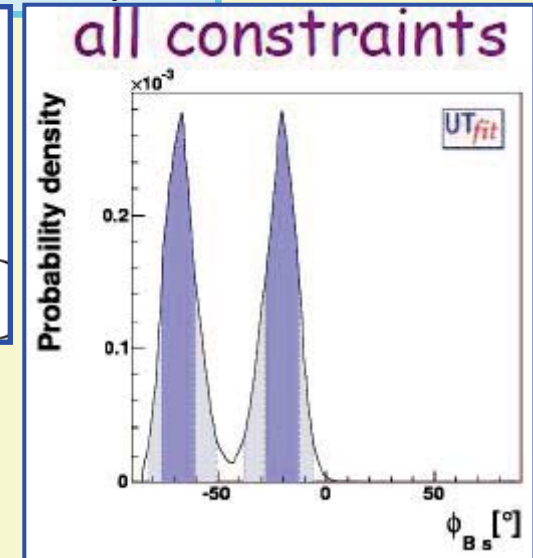
$$C_{B_s} = 0.95 \pm 0.10$$

$$[-0.78, 1.16] \leftrightarrow 95\%$$

$$\phi_{B_s} = [-20 \pm 8]^\circ \cup [-68 \pm 8]^\circ$$

$$[-38, -6]^\circ \cup [-81, -51]^\circ \leftrightarrow 95\%$$

Deviation from the SM  
at  $3.1\sigma$



$a_{\mu\mu}$  and  $B_s \rightarrow J/\Psi \phi$  point to large  
but **different** values of  $\phi_{B_s}$   
(N.B. the **UTA** beyond the SM  
allows for **NP in loops only**,  
i.e. tree-level NP in  $\Gamma_{12}$  is not allowed)

Further confirmations  
from experiments  
are looked forward!

- Are there NP models solving these tensions?
- What are the effects in Flavour Physics within various NP models?
- How to search and discriminate them?
- ...