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**Workshop on Cosmic Rays and Cosmic Neutrinos: Looking at the  
Neutrino Sky**

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**A novel method to extract dark matter parameters from neutrino telescope data**

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Iran*

# A Novel Method to Extract Dark Matter Parameters from Neutrino Telescope Data



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# Dark matter



$$\rho_{DM} / (\rho_{DM} + \rho_{baryon}) = 82 \%$$

What is DM composed of??

A popular class of candidates: **WIMP**

**WIMP**: Weakly Interacting Massive Particle

# WIMP



- Lightest **supersymmetric** particle (**LSP**)
- Lightest **KK** mode in extra large dimension models
- .....
- **AMEND and SLIM** : Y.F, S. Pascoli and Schimdtt, **JHEP 1010 (2010)**; Y.F., **Phys.Rev. D80 (2009)**

# WIMP



- Direct detection
- Indirect detection

# Direct DM Detection

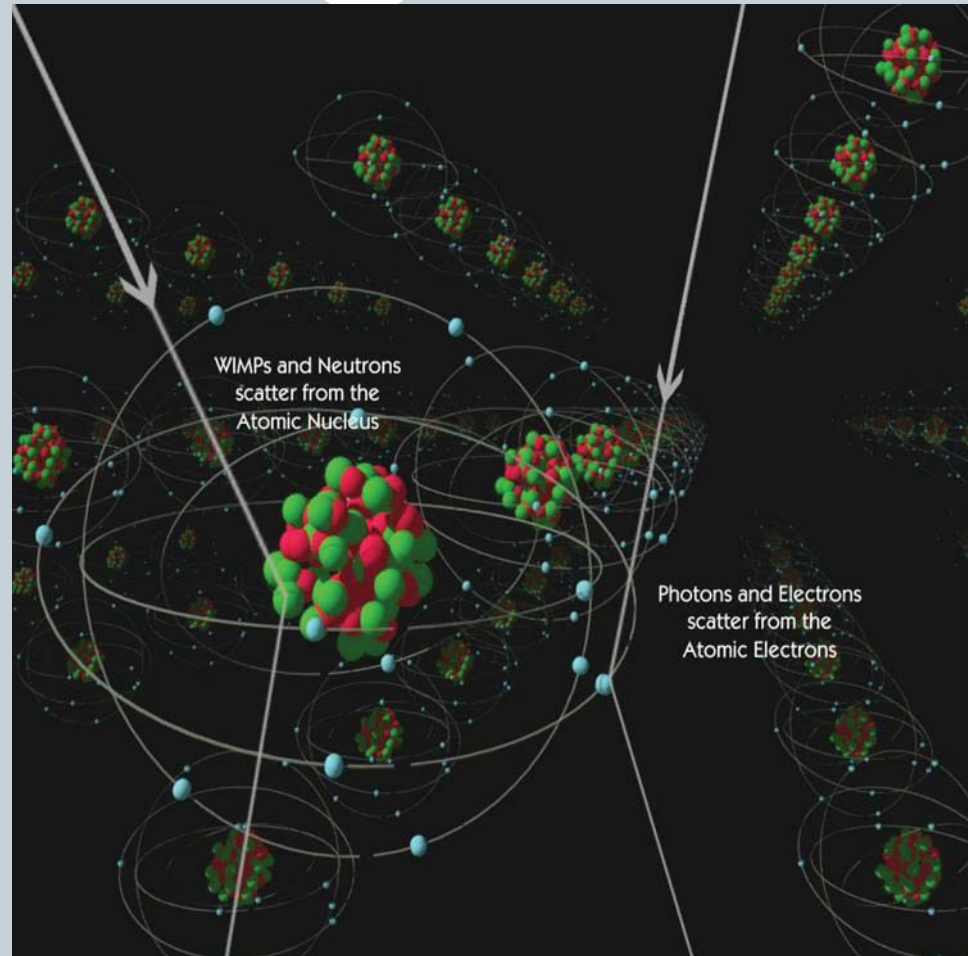
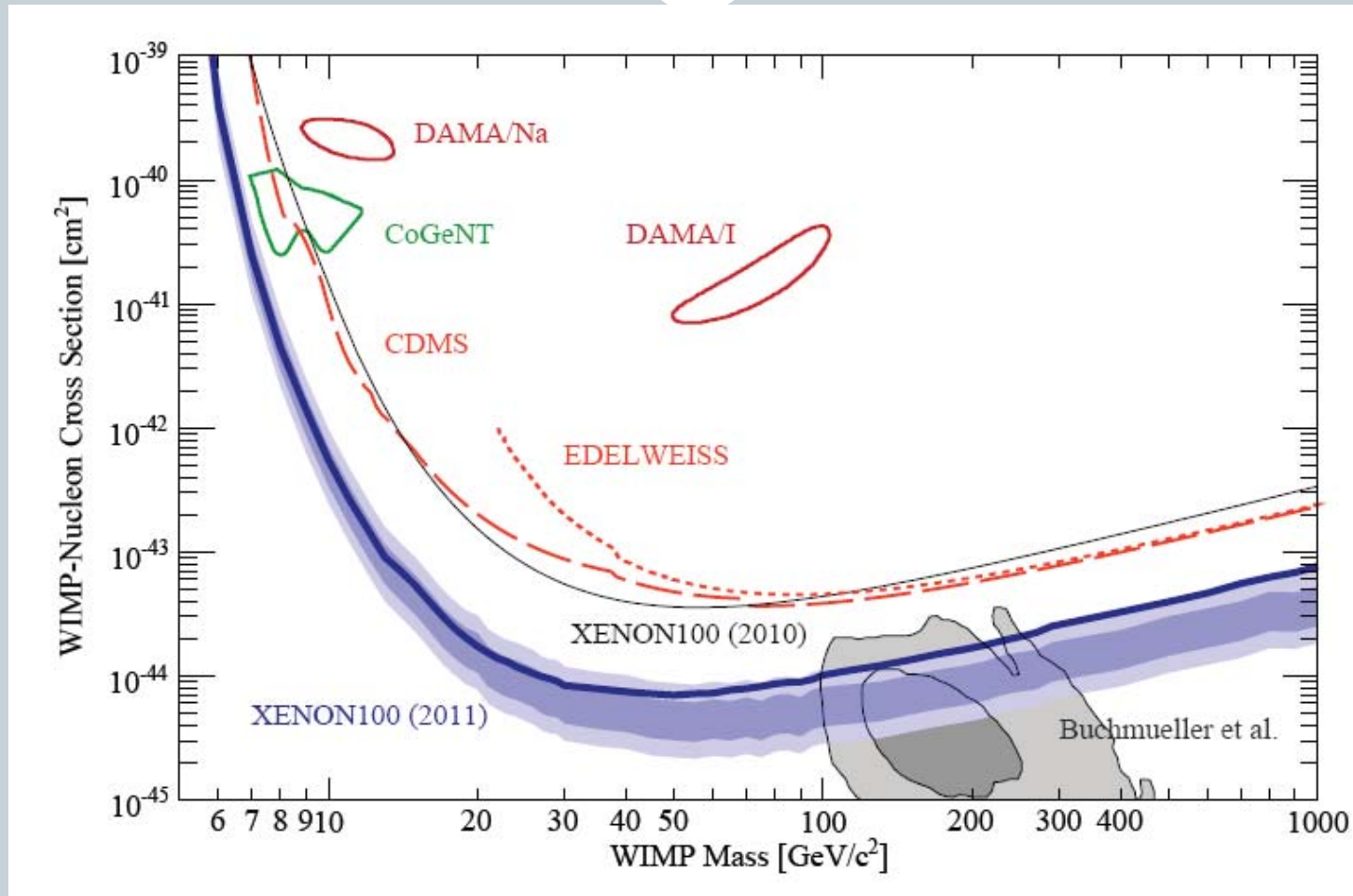


Image courtesy of:

<http://cdms.berkeley.edu/Education/DMpages/science/directDetection.shtml>

# DAMA signal and Direct bounds



XENON100, arXiv:1104.2549

# Indirect detection



- Detection of the products of DM pair annihilation in the DM halo, galaxy center, Sun, Earth ....

$$\text{DM} + \text{DM} \rightarrow e^- e^+$$

$$\text{DM} + \text{DM} \rightarrow \gamma\gamma$$

$$\text{Inverse Compton : } e^\pm + \gamma \rightarrow e^\pm + \gamma$$

$$\text{pair annihilation : } e^+ e^- \rightarrow \gamma\gamma$$



# Signal from the Sun



$$\text{DM}(v_i) + N \rightarrow \text{DM}(v_f) + N$$

$$v_i \sim 200 \text{ km/sec} \quad v_i > v_f$$

Trapped inside the  
gravitational well

$n_{DM}$  **Grows**.

$$\Gamma(\text{DM} + \text{DM} \rightarrow \text{anything}) \propto n_{DM}^2$$

Only  $\nu$  and  $\bar{\nu}$  come out of the Sun center and reach our detectors.

# DM capture in the Sun



$$C \sim \frac{\rho_{DM}}{m_{DM} v_{DM}} \left( \frac{M_{\odot}}{m_p} \right) \sigma_{DM-nucleon} \langle v_{esc}^2 \rangle$$

$$\rho_{DM} = 0.39 \text{ GeV cm}^{-3}$$

$$v_{DM} \sim 270 \text{ km sec}^{-1}$$

The maximal possible capture rate is therefore  $O[10^{24} \text{ sec}^{-1}]$ .



$$E_{kinetic} = \frac{3kT}{2}$$

$$E_{Gravity} = G_N \left( \frac{4\pi}{3} \rho r_{DM}^3 \right) \frac{m_{DM}}{r_{DM}}$$

$$E_{kinetic} = E_{Gravity}$$

$$r_{DM} \approx \left( \frac{9T}{8\pi G_N \rho m_{DM}} \right)^{1/2}$$

$$r_{DM} = 0.003 R_{\odot} \left( \frac{100 \text{ GeV}}{m_{DM}} \right)^{1/2}$$

# Some conventional neutrino production modes



$$\text{DM} + \text{DM} \rightarrow \nu \bar{\nu}$$

$$\frac{v}{c} \sim 10^{-4} \ll 1 \quad E_\nu \simeq m_{DM}$$

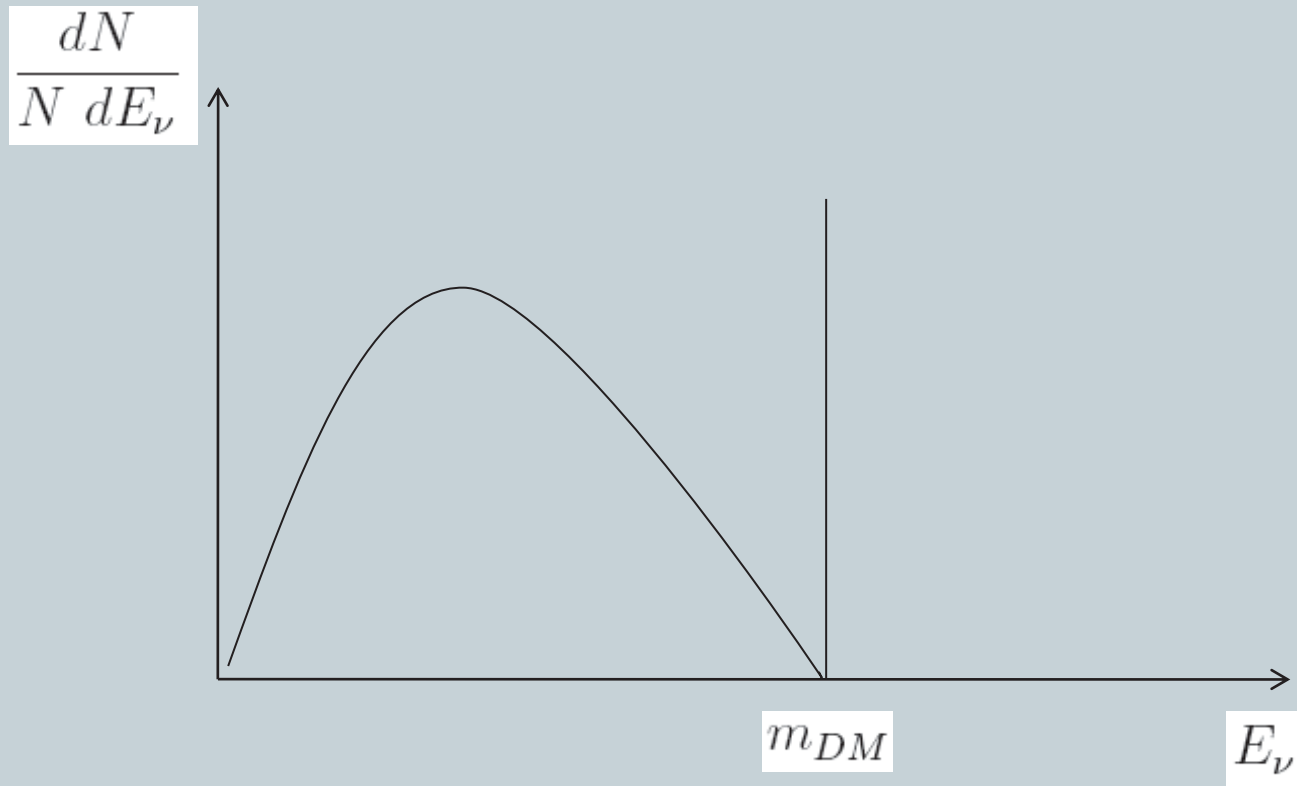
$$\text{DM} + \text{DM} \rightarrow ZZ, W^+W^-$$

$$W^- \rightarrow l_\alpha^- \bar{\nu}_\alpha, \quad Z \rightarrow \nu \bar{\nu}$$

$$\text{DM} + \text{DM} \rightarrow b\bar{b} \quad b \rightarrow c \bar{\nu}_\alpha l_\alpha$$

$$E_\nu < m_{DM}$$

# Spectrum



## models



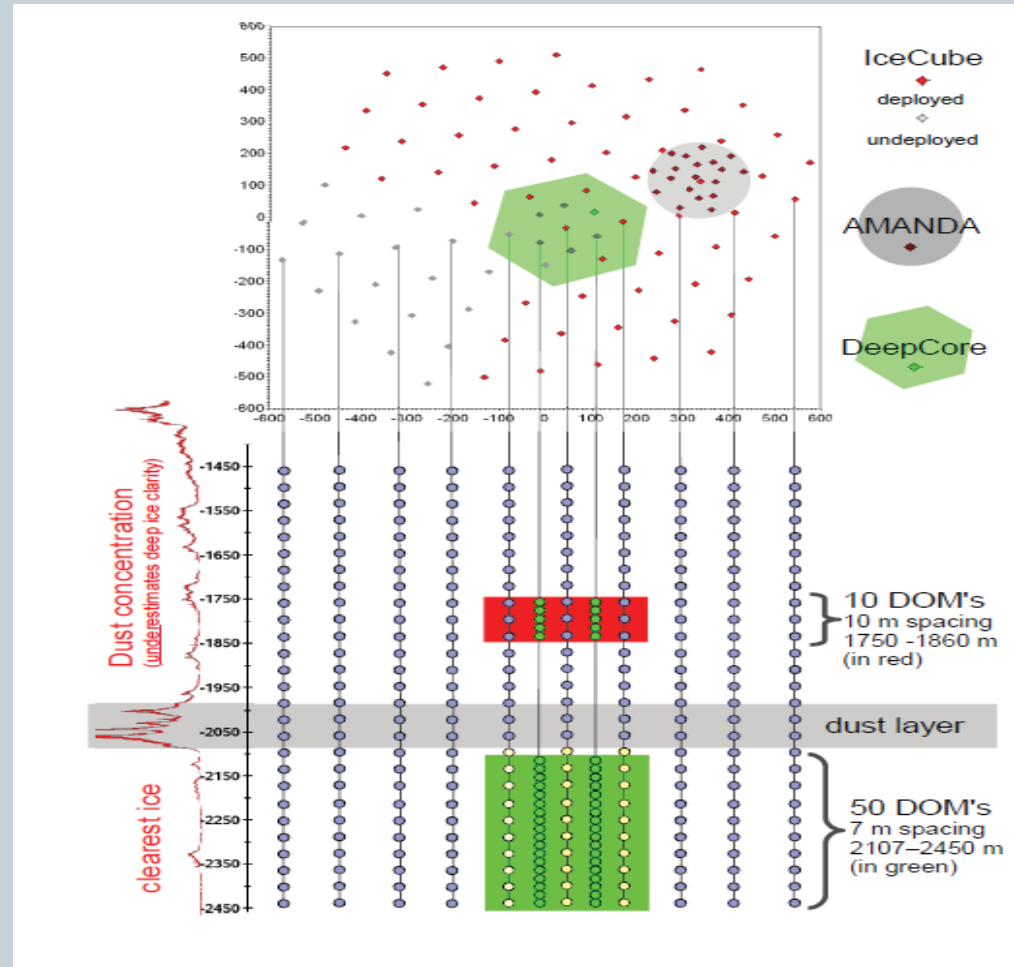
- Lindner, Merle and Niro, **Enhancing Dark Matter Annihilation into Neutrinos, PRD82**
- Arman Esmaili and YF, **JCAP**

# ICECUBE and DEEPCORE

[Physics Capabilities of the IceCube  
DeepCore Detector.](#)

, for the IceCube Collaboration.

arXiv:0907.2263



# Shower and muon track



- CC:  $\nu_\mu + N \rightarrow \mu + X$

Muon-track

- NC:  $\nu + N \rightarrow \nu + X$

- CC:  $\nu_e + N \rightarrow e + X$

$$\nu_\tau + N \rightarrow \tau + X, \quad \tau \rightarrow \nu_\tau + X$$

Shower or cascade



# Background



- Background from solar atmosphere < 10 per year  
Fogli et al, PRD74

Atmospheric muons: During summer and spring  
The rest of **ICECUBE** acts as filter for **DeepCore**.

Atmospheric neutrino background

# Atmospheric background



a cone with half angle  $1^\circ$  around the direction of Sun,

Whole ICECUBE:  $\sim 6 \text{ yr}^{-1}$

Deepcore:  $\sim 2.5 \text{ yr}^{-1}$

Fogli, Lisi, Kasahara PRD75

# Scattering of neutrinos inside the Sun



- Scattered neutrinos:

$$\nu N \rightarrow \nu X$$

- Absorbed neutrinos:

$$\nu_{\alpha} N \rightarrow l_{\alpha} X$$

- Regenerated neutrinos:

$$\nu_{\tau} N \rightarrow \tau X, \quad \tau \rightarrow \nu_{\tau} \mu \bar{\nu}_{\mu}$$

# Sharp line remains sharp!

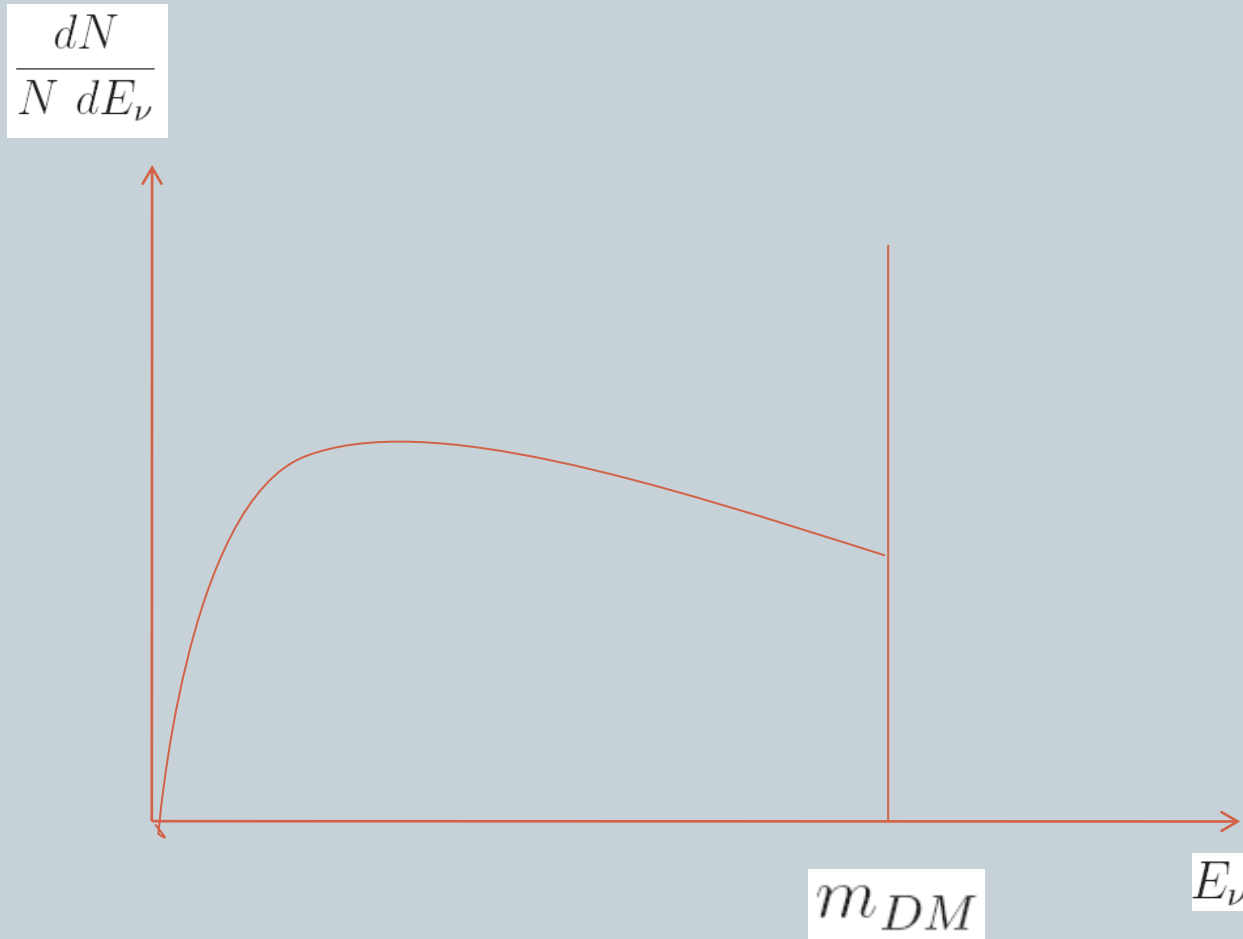


$$\frac{d\sigma[\nu(k)N \rightarrow \nu(k')X]}{dk'}$$

has no peak at

$$k' \rightarrow k$$

# Spectrum after emerging from the Sun



# Oscillation of neutrinos

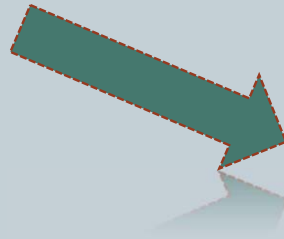


- Oscillation inside the Sun
- Oscillation between Sun and Earth
- Oscillation in the Earth???

# Oscillation in the Earth



$$\Delta m_{ij}^2 / p \ll V_e$$



$$\theta_{eff} \rightarrow 0$$

# Oscillation in matter



$$i\frac{d|\nu_\gamma\rangle}{dt} = \left[\frac{m_\nu^\dagger \cdot m_\nu}{2p} + \text{diag}(V_e, 0, 0)\right]_{\gamma\sigma} |\nu_\sigma\rangle$$

$$i\frac{d|\bar{\nu}_\gamma\rangle}{dt} = \left[\frac{m_\nu^T \cdot m_\nu^*}{2p} - \text{diag}(V_e, 0, 0)\right]_{\gamma\sigma} |\bar{\nu}_\sigma\rangle$$

$$V_e = \sqrt{2}G_F N_e.$$

$$N_e \begin{cases} \neq 0 & r < r_{sun} \\ = 0 & r > r_{sun} \end{cases}$$



# Neutrino oscillation in matter



$$|\nu'_\alpha; \text{surface}\rangle = a_{\alpha 1}|1\rangle + a_{\alpha 2}|2\rangle + a_{\alpha 3}|3\rangle$$

$$|\nu'_\alpha; \text{detector}\rangle = a_{\alpha 1}|1\rangle + a_{\alpha 2}e^{i\Delta_{12}}|2\rangle + a_{\alpha 3}e^{i\Delta_{13}}|3\rangle$$

$$\Delta_{ij} \equiv \Delta m_{ij}^2 L / (2E).$$

$$P(\nu_\alpha \rightarrow \nu_\mu) = \sum_i |a_{\alpha i}|^2 |U_{\mu i}|^2 +$$

$$2\Re[a_{\alpha 1}^* a_{\alpha 2} U_{\mu 1} U_{\mu 2}^* e^{i\Delta_{12}}] + 2\Re[a_{\alpha 1}^* a_{\alpha 3} U_{\mu 1} U_{\mu 3}^* e^{i\Delta_{13}}] \\ + 2\Re[a_{\alpha 2}^* a_{\alpha 3} U_{\mu 2} U_{\mu 3}^* e^{i(\Delta_{13} - \Delta_{12})}]$$

# Neutrino versus antineutrino



$$|\nu'_\alpha; \text{surface}\rangle = a_{\alpha 1}|1\rangle + a_{\alpha 2}|2\rangle + a_{\alpha 3}|3\rangle .$$

$$|\bar{\nu}'_\alpha; \text{surface}\rangle = \bar{a}_{\alpha 1}|\bar{1}\rangle + \bar{a}_{\alpha 2}|\bar{2}\rangle + \bar{a}_{\alpha 3}|\bar{3}\rangle .$$

# Literature



- Lehner and Weiler, PRD77, Erkoca, Reno and Sarcevic PRD80, Cirelli, Fornengo, Montaruli, Sokalski, Strumia and Vissani, NPB727
- Barger, Keung and Shaughnessy, PLB664
- Blennow, Melbeus and Ohlsson, JCAP 100
- Blennow, Edsjo and Ohlsson, JCAP 0801

# WimpSIM



- **J. Edsjö, WimpSim Neutrino Monte Carlo, <http://www.physto.se/~edsjo/wimpsim/>**
- **M. Blennow, J. Edsjö and T. Ohlsson, [[arXiv:0709.3898](#)]**

# Oscillatory terms



$$|\nu'_\alpha; \text{detector}\rangle = a_{\alpha 1}|1\rangle + a_{\alpha 2}e^{i\Delta_{12}}|2\rangle + a_{\alpha 3}e^{i\Delta_{13}}|3\rangle$$

$$\Delta_{ij} \equiv \Delta m_{ij}^2 L / (2E).$$

$$P(\nu_\alpha \rightarrow \nu_\mu) = \sum_i |a_{\alpha i}|^2 |U_{\mu i}|^2 +$$

$$2\Re[a_{\alpha 1}^* a_{\alpha 2} U_{\mu 1} U_{\mu 2}^* e^{i\Delta_{12}}] + 2\Re[a_{\alpha 1}^* a_{\alpha 3} U_{\mu 1} U_{\mu 3}^* e^{i\Delta_{13}}] \\ + 2\Re[a_{\alpha 2}^* a_{\alpha 3} U_{\mu 2} U_{\mu 3}^* e^{i(\Delta_{13} - \Delta_{12})}]$$

# Our work



- A. Esmaili and Y.F., **“A Novel Method to Extract Dark Matter Parameters from Neutrino Telescope Data,”** JCAP 1104 (2011) 007

A. Esmaili and Y.F., **“An Analysis of Cosmic Neutrinos: Flavor Composition at Source and Neutrino Mixing Parameters ,”** Nucl.Phys. B821 (2009) 197-214

# Neutrino oscillation length



$$L_{osc} = \frac{4\pi E_\nu}{\Delta m_{12}^2} \sim 3 \times 10^{11} \text{ cm} \left( \frac{E_\nu}{100 \text{ GeV}} \right) \left( \frac{8 \times 10^{-5} \text{ eV}^2}{\Delta m_{12}^2} \right)$$

Earth Sun distance:  $L = 1.5 \times 10^{13} \text{ cm}$

If the energy resolution  $(\delta E/E)$  is worse than 1 % and the width of the spectrum is larger than  $(\delta E/E)$ , the oscillatory terms will average to zero.

# Averaging limit



$$|\nu_\alpha; p; L\rangle = a_{\alpha 1}(L)|1; p\rangle + a_{\alpha 2}(L)|2; p\rangle + a_{\alpha 3}(L)|3; p\rangle$$

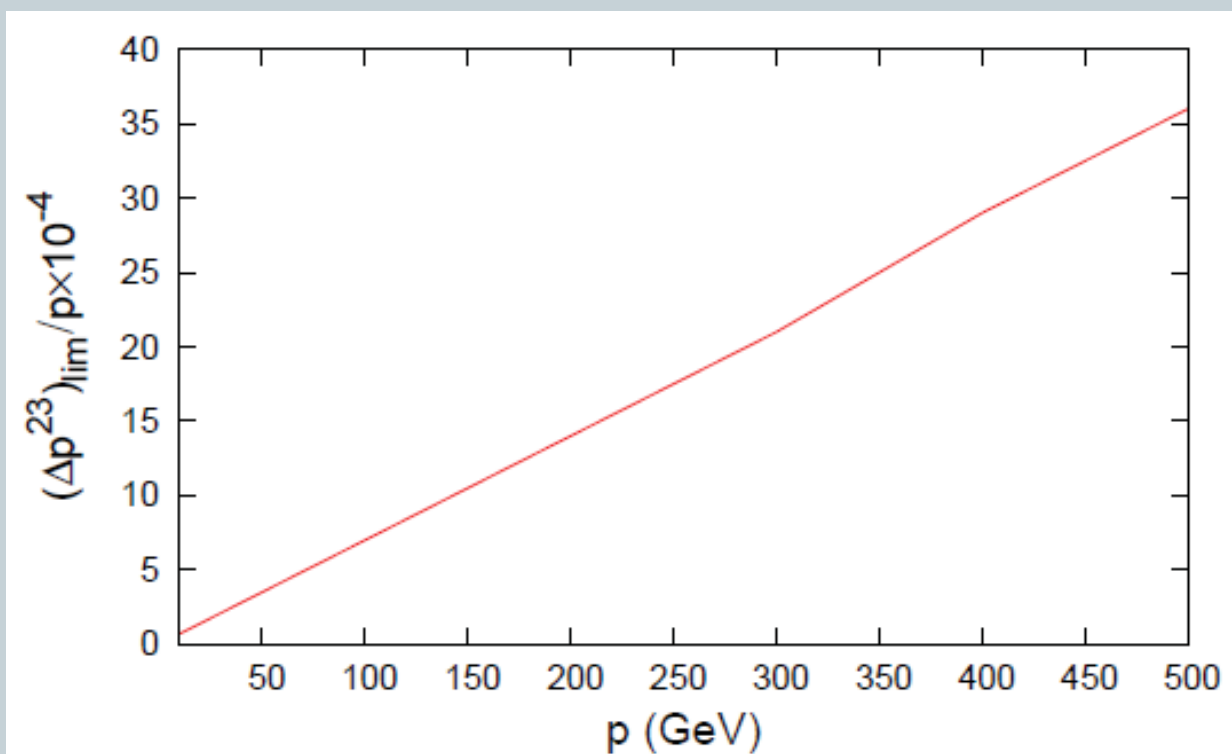
$$\arg \left[ \frac{[a_{\beta i}(0)(a_{\beta j}(0))^*(a_{\alpha i}(L/c))^*a_{\alpha j}(L/c)]|_{p+(\Delta p^{ij})_{lim}}}{[a_{\beta i}(0)(a_{\beta j}(0))^*(a_{\alpha i}(L/c))^*a_{\alpha j}(L/c)]|_p} \right] = 2\pi$$

In vacuum:

$$\frac{(\Delta p^{ij})_{lim}}{p} = \frac{2\pi p}{L\Delta m_{ij}^2},$$

Independent of  $\alpha$  and  $\beta$





Independent of  $\theta_{13}$

# Thermal widening



$$\bar{v} = (3T/m_{DM})^{1/2} \simeq 60 \text{ km/sec} (100 \text{ GeV}/m_{DM})^{1/2}.$$

$$\frac{\Delta E}{E} \sim \frac{\bar{v}}{c} \sim 10^{-4} \left( \frac{T}{1.3 \text{ keV}} \right)^{1/2} \left( \frac{100 \text{ GeV}}{m_{DM}} \right)^{1/2}.$$

Robust against solar models

# Averaging due to production point

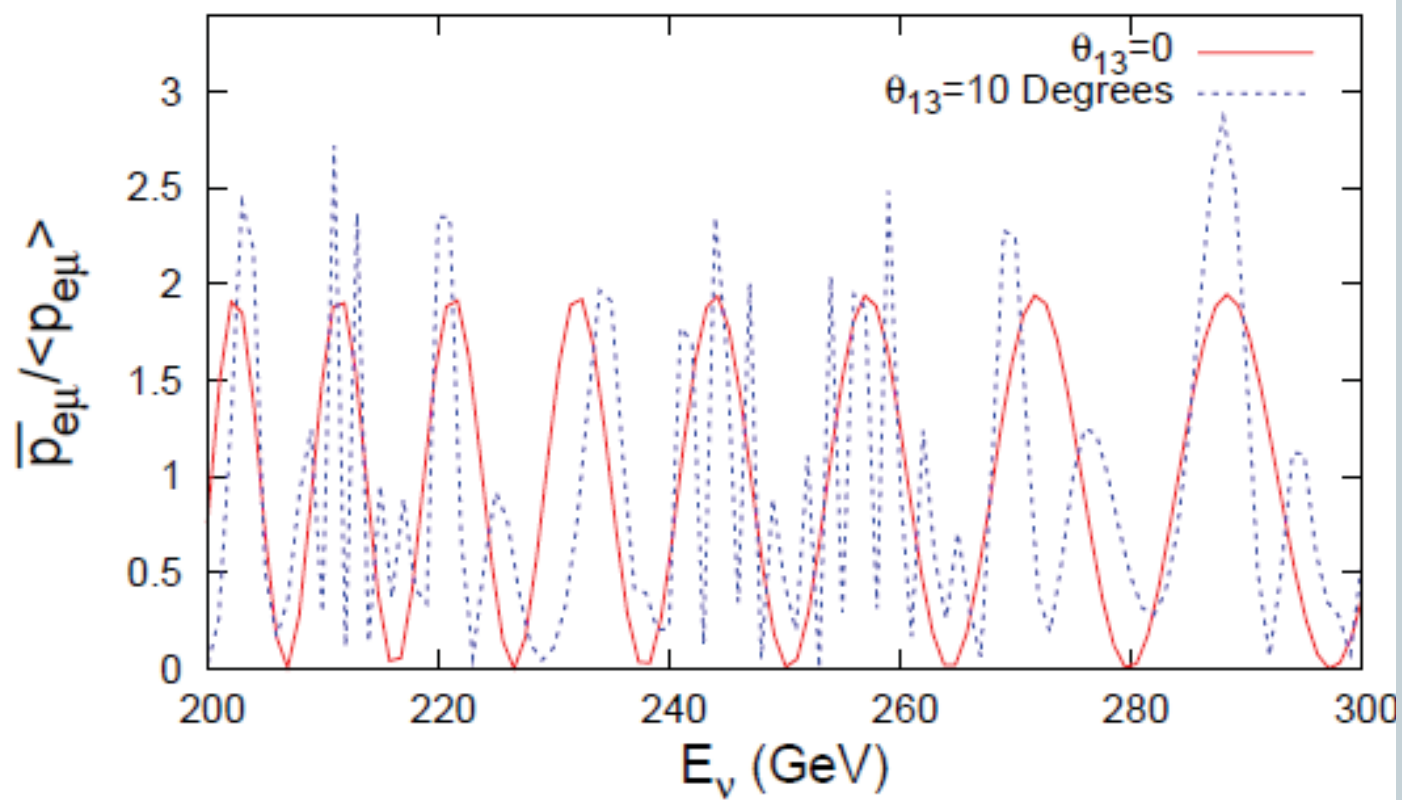


$$r_{DM} \approx \left( \frac{9T}{8\pi G_N \rho m_{DM}} \right)^{1/2},$$

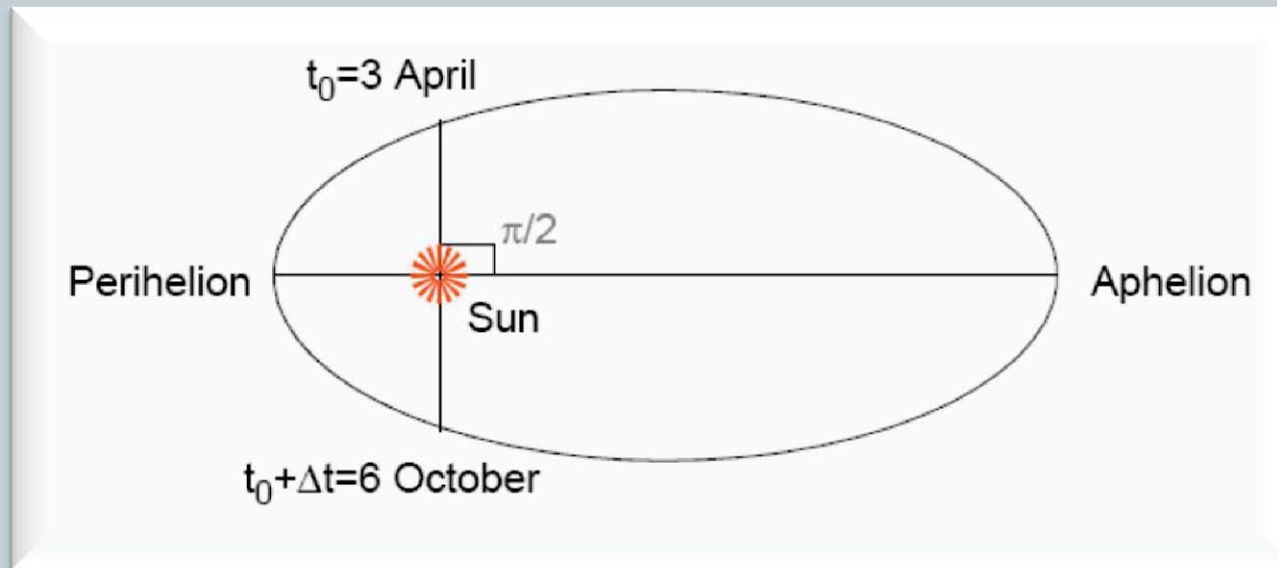
$$0.003 R_\odot (100 \text{ GeV} / m_{DM})^{1/2}$$

The average over production point:  $\bar{P}_{\alpha\beta}$

Dropping the oscillatory terms:  $\langle P_{\alpha\beta} \rangle$



# The earth orbit



Earth Sun distance variation is of order of

$$L_{osc} = \frac{4\pi E_\nu}{\Delta m_{12}^2} \sim 3 \times 10^{11} \text{ cm} \left( \frac{E_\nu}{100 \text{ GeV}} \right) \left( \frac{8 \times 10^{-5} \text{ eV}^2}{\Delta m_{12}^2} \right)$$



$$P(\nu_\alpha \rightarrow \nu_\mu) = \sum_i |a_{\alpha i}|^2 |U_{\mu i}|^2 +$$

$$2\Re[a_{\alpha 1}^* a_{\alpha 2} U_{\mu 1} U_{\mu 2}^* e^{i\Delta_{12}}] + 2\Re[a_{\alpha 1}^* a_{\alpha 3} U_{\mu 1} U_{\mu 3}^* e^{i\Delta_{13}}] + 2\Re[a_{\alpha 2}^* a_{\alpha 3} U_{\mu 2} U_{\mu 3}^* e^{i(\Delta_{13}-\Delta_{12})}]$$

$$O_{12}(t, \Delta t) \equiv \frac{\int_t^{t+\Delta t} e^{i\Delta_{12}(t)} A_{eff}(t) L^{-2}(t) dt}{\int_t^{t+\Delta t} A_{eff}(t) L^{-2}(t) dt},$$

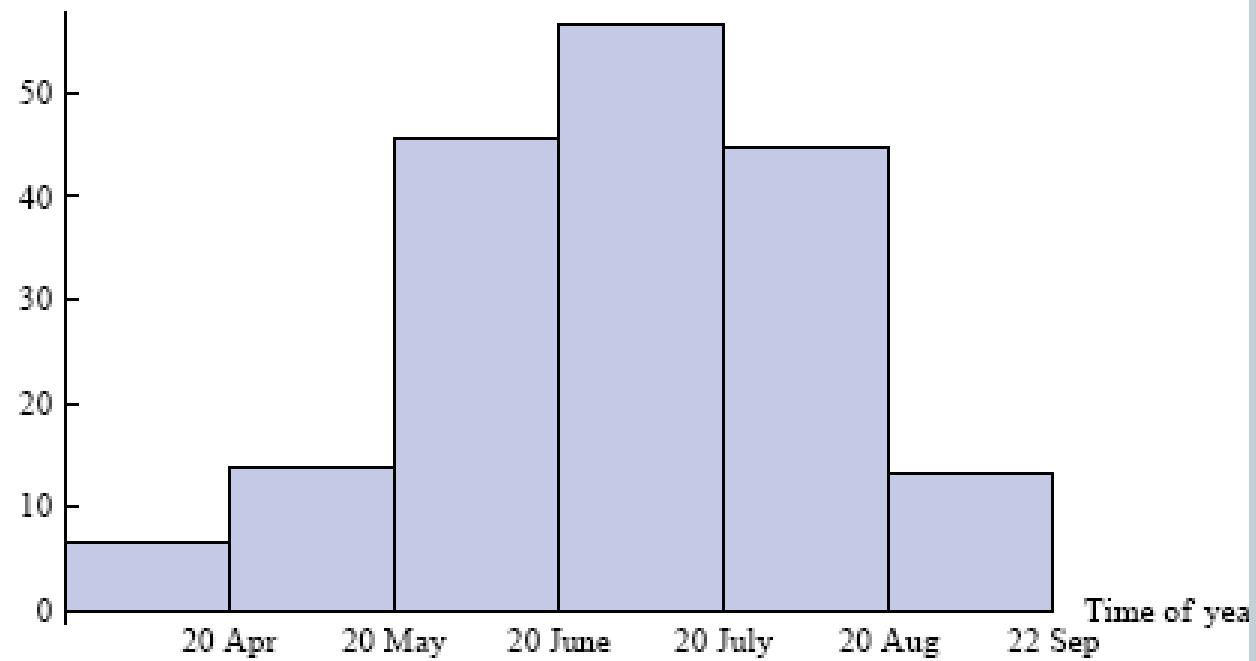
$$O_{13}(t, \Delta t) \equiv \frac{\int_t^{t+\Delta t} e^{i\Delta_{13}(t)} A_{eff}(t) L^{-2}(t) dt}{\int_t^{t+\Delta t} A_{eff}(t) L^{-2}(t) dt}.$$

For  $E_\nu \sim 100$  GeV,  $|O_{12}| \sim 1$  and  $|O_{13}| \sim 0.1$

# Variation of muon track



number of muon tracks



$$DM+DM \rightarrow \nu_e \bar{\nu}_e.$$

$$m_{DM} = 270 \text{ GeV}$$

$$C_{\odot} = 3.4 \times 10^{22} \text{ s}^{-1}$$

# Factoring out the distance factor



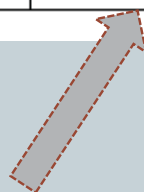
$$\tilde{N}(t_0, \Delta t) \equiv \frac{\int_{t_0}^{t_0+\Delta t} (dN_\mu/dt) dt}{\int_{t_0}^{t_0+\Delta t} A_{eff}(\theta[t])/[L(t)]^2 dt}.$$

$$\Delta(t_0, \Delta t) \equiv \frac{\tilde{N}(t_0, \Delta t) - \tilde{N}(t_0 + \Delta t, 1 \text{ year} - \Delta t)}{\tilde{N}(t_0, \Delta t) + \tilde{N}(t_0 + \Delta t, 1 \text{ year} - \Delta t)}$$





$E_\nu$ (GeV)	$\Delta(20\text{March}, 186\text{days})$				$\Delta(3\text{April}, 186\text{days})$			
	$\theta_{13} = 0^\circ$		$\theta_{13} = 10^\circ$		$\theta_{13} = 0^\circ$		$\theta_{13} = 10^\circ$	
	NH	IH	NH	IH	NH	IH	NH	IH
100	18 %	18 %	9 %	11 %	12 %	12 %	6 %	7 %
300	57 %	57 %	37 %	42 %	60 %	60 %	39 %	43 %



$$\text{DM} + \text{DM} \rightarrow \nu_e + \nu_e$$



$E_\nu$ (GeV)	$\Delta(20\text{March}, 186\text{days})$				$\Delta(3\text{April}, 186\text{days})$			
	$\theta_{13} = 0^\circ$		$\theta_{13} = 10^\circ$		$\theta_{13} = 0^\circ$		$\theta_{13} = 10^\circ$	
	NH	IH	NH	IH	NH	IH	NH	IH
100	9 %	6 %	4 %	1 %	7 %	4 %	3 %	0.3 %
300	12 %	7 %	6 %	19 %	13 %	7 %	6 %	20 %

$$\text{DM} + \text{DM} \rightarrow \nu_\mu + \nu_\mu$$

# A measure of oscillation



$$\Delta(t_1, \Delta t_1; t_2, \Delta t_2) \equiv \frac{\tilde{N}(t_1, \Delta t_1) - \tilde{N}(t_2, \Delta t_2)}{\tilde{N}(t_1, \Delta t_1) + \tilde{N}(t_2, \Delta t_2)}$$

$$\tilde{N}(t, \Delta t) \equiv \frac{\int_t^{t+\Delta t} (dN_\mu/dt) dt}{\int_t^{t+\Delta t} A_{eff}(\theta[t]) L^{-2}(t) dt}$$

# Application



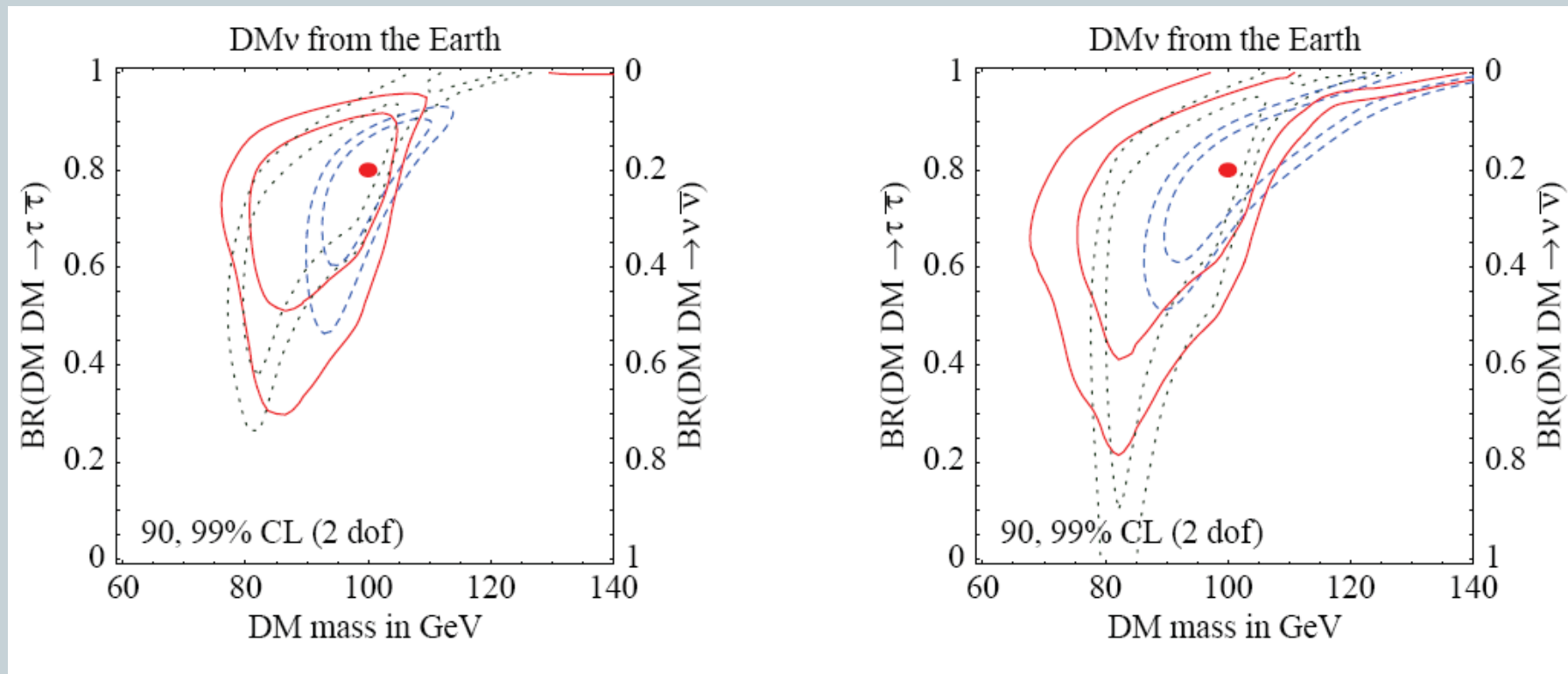
- Is there a sharp feature?
- Is production democratic?

$$n_0 \equiv n_{\nu_e} = n_{\nu_\mu} = n_{\nu_\tau}$$

$$\sum_{\alpha} P(\nu_{\alpha} \rightarrow \nu_{\beta}) = 1$$

$$\sum_{\alpha} n_{\nu_{\alpha}} P(\nu_{\alpha} \rightarrow \nu_e) = \sum_{\alpha} n_{\nu_{\alpha}} P(\nu_{\alpha} \rightarrow \nu_{\mu}) = \sum_{\alpha} n_{\nu_{\alpha}} P(\nu_{\alpha} \rightarrow \nu_{\tau}) = n_0$$

# Energy measurement



# Systematic analysis



$$\mathcal{M}_{\alpha\beta} \quad \text{DM} + \text{DM} \rightarrow \nu_\alpha + \bar{\nu}_\beta^{(-)}$$

$$|\psi\rangle = \sum_{\alpha\beta} \mathcal{M}_{\alpha\beta} |\nu_\alpha(\vec{p}_1) \bar{\nu}_\beta^{(-)}(\vec{p}_2)\rangle$$

$$|\psi\rangle\langle\psi| = \sum_{\alpha\beta\gamma\sigma} \tilde{\rho}_{\alpha\beta,\gamma\sigma} |\nu_\alpha \bar{\nu}_\beta^{(-)}\rangle\langle\nu_\gamma \bar{\nu}_\sigma^{(-)}|$$

$$\tilde{\rho}_{\alpha\beta,\gamma\sigma} = \mathcal{M}_{\alpha\beta} \mathcal{M}_{\gamma\sigma}^* \quad (\text{i.e., } \tilde{\rho} \log \tilde{\rho} = 0)$$



“reduced” matrix

$$(\text{i.e., } \rho \log \rho \neq 0)$$

$$\rho_{\alpha\beta} |\nu_\alpha\rangle\langle\nu_\beta| \quad \text{with} \quad \rho_{\alpha\beta} = \sum_{\gamma} \tilde{\rho}_{\alpha\gamma,\beta\gamma} = (\mathcal{M} \mathcal{M}^\dagger)_{\alpha\beta}$$

# Energy measurement



- Through going
- Contained events

Can we reconstruct  $\mathcal{M}_{\alpha\beta}$  ?



$$\rho = V \rho_{diag} V^\dagger$$

$$\text{DM} + \text{DM} \rightarrow \nu_\alpha + \nu_\beta, \bar{\nu}_\alpha + \bar{\nu}_\beta$$

$$\mathcal{M} = V (\rho_{diag})^{1/2} V^T$$

$$\text{DM} + \text{DM} \rightarrow \nu_\alpha + \bar{\nu}_\beta$$

$$\mathcal{M} = V (\rho_{diag})^{1/2} V^\dagger$$



# General case



$$\rho = \sum_{\alpha} n_{\alpha} |\nu'_{\alpha}\rangle \langle \nu'_{\alpha}|$$

$$|\nu'_{\alpha}; \text{surface}\rangle = a_{\alpha 1} |1\rangle + a_{\alpha 2} |2\rangle + a_{\alpha 3} |3\rangle$$

$$\bar{\rho} = \sum_{\alpha} n_{\alpha} |\bar{\nu}'_{\alpha}\rangle \langle \bar{\nu}'_{\alpha}|.$$

$$|\bar{\nu}'_{\alpha}; \text{surface}\rangle = \bar{a}_{\alpha 1} |\bar{1}\rangle + \bar{a}_{\alpha 2} |\bar{2}\rangle + \bar{a}_{\alpha 3} |\bar{3}\rangle$$

# Definitions



$$O_{12}(t, \Delta t) \equiv \frac{\int_t^{t+\Delta t} e^{i\Delta_{12}(t)} A_{eff}(t) L^{-2}(t) dt}{\int_t^{t+\Delta t} A_{eff}(t) L^{-2}(t) dt},$$

$$O_{13}(t, \Delta t) \equiv \frac{\int_t^{t+\Delta t} e^{i\Delta_{13}(t)} A_{eff}(t) L^{-2}(t) dt}{\int_t^{t+\Delta t} A_{eff}(t) L^{-2}(t) dt}.$$

For  $E_\nu \sim 100$  GeV,  $|O_{12}| \sim 1$  and  $|O_{13}| \sim 0.1$

# Averaged oscillation probability



$$\langle P(\nu_\alpha \rightarrow \nu_\mu) \rangle|_t^{t+\Delta t} \equiv \frac{\int_t^{t+\Delta t} P(\nu_\alpha \rightarrow \nu_\mu) A_{eff} L^{-2}(t) dt}{\int_t^{t+\Delta t} A_{eff} L^{-2}(t)} =$$

$$\sum_i |a_{\alpha i}|^2 |U_{\mu i}|^2 + 2\Re[a_{\alpha 1}^* a_{\alpha 2} U_{\mu 1} U_{\mu 2}^* O_{12}] + \mathcal{O}(a_{\alpha i}^2 U_{\mu i}^2 O_{13}).$$

# Muon tracks



- Muon track events from the sharp line are proportional to

$$K(t, \Delta t) \equiv \sum_{\alpha} n_{\alpha} \left( \langle P(\nu_{\alpha} \rightarrow \nu_{\mu}) \rangle|_t^{t+\Delta t} + r \frac{\sigma(\bar{\nu})}{\sigma(\nu)} \langle P(\bar{\nu}_{\alpha} \rightarrow \bar{\nu}_{\mu}) \rangle|_t^{t+\Delta t} \right)$$

Whole muon track events

$$\mathcal{A} + \mathcal{B}K(t, \Delta t).$$

# What can be derived



$$\Delta m_{12}^2 / m_{DM}$$

$$\mathcal{A} + \mathcal{B} \sum_{\alpha, i} n_{\alpha} \left( |a_{\alpha i}|^2 |U_{\mu i}|^2 + r \frac{\sigma(\bar{\nu})}{\sigma(\nu)} |\bar{a}_{\alpha i}|^2 |U_{\mu i}|^2 \right)$$

$$\mathcal{B} \left| \sum_{\alpha} n_{\alpha} \left( a_{\alpha 1}^* a_{\alpha 2} U_{\mu 1} U_{\mu 2}^* + r \frac{\sigma(\bar{\nu})}{\sigma(\nu)} \bar{a}_{\alpha 1}^* \bar{a}_{\alpha 2} U_{\mu i}^* U_{\mu 2} \right) \right|$$

Valuable information but not enough to reconstruct the amplitude



- By dividing the time interval between spring equinox to autumn equinox to four periods, one can derive these combinations.
- If the present bounds are saturated, after **10 years** of data taking, enough data can be collected to perform a ten per cent accuracy measurement.

The range for which the method is effective



$$m_{DM} < 500 \text{ GeV},$$

For larger masses, the sharp line will be reduced by scattering.

# Conclusions



- For  $100 \text{ GeV} < m_{DM} < 500 \text{ GeV}$ , observing seasonal variation (i.e., nonzero  $\Delta$ ) means  $DM + DM \rightarrow \nu\nu$  takes place dominantly and the flavor structure is **not** democratic.
- By studying the variation, the **dark matter mass** can be derived.
- Such a derivation (with 10 percent accuracy) requires more than 400 DM events.



# Democratic production



$$n_0 \equiv n_{\nu_e} = n_{\nu_\mu} = n_{\nu_\tau}$$

$$\sum_{\alpha} P(\nu_{\alpha} \rightarrow \nu_{\beta}) = 1$$

$$\sum_{\alpha} n_{\nu_{\alpha}} P(\nu_{\alpha} \rightarrow \nu_e) = \sum_{\alpha} n_{\nu_{\alpha}} P(\nu_{\alpha} \rightarrow \nu_{\mu}) = \sum_{\alpha} n_{\nu_{\alpha}} P(\nu_{\alpha} \rightarrow \nu_{\tau}) = n_0$$

Oscillatory terms do not show up.

In general  $\text{DM} + \text{DM} \rightarrow \nu_{\alpha} + \nu_{\beta}$