# The Ventilated Ocean: Stratification and overturning in an ocean with adiabatic interior and Lagrangian ocean modeling

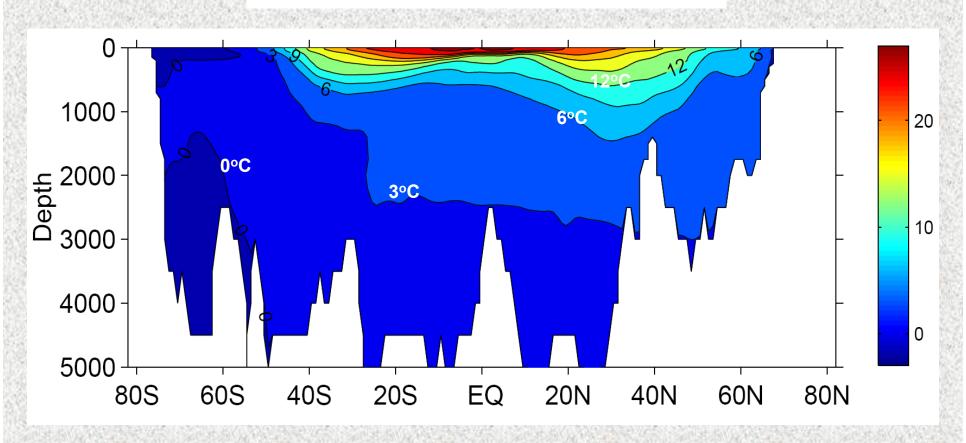
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Yale University

July 2011

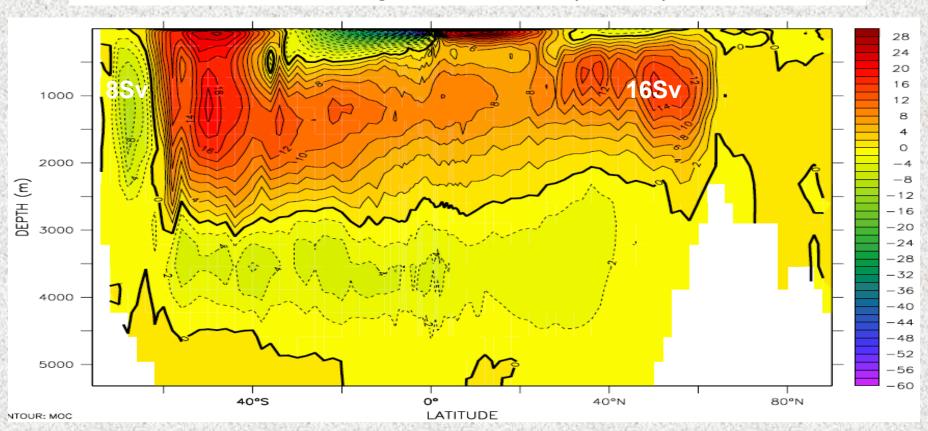
## What controls ocean stratification and overturning circulation?

## Atlantic ocean thermal structure

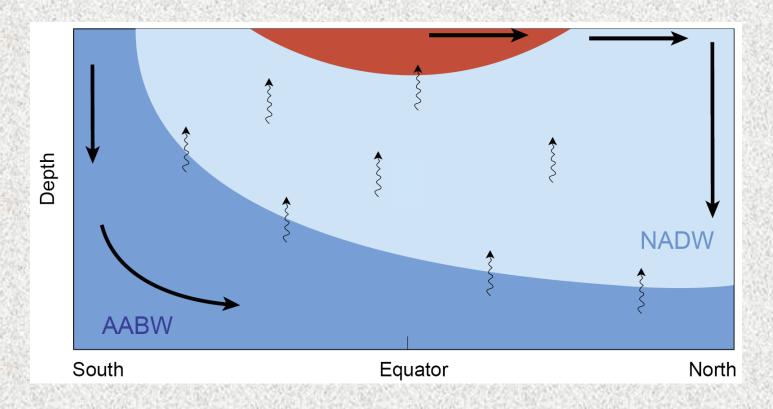


## What controls ocean stratification and overturning circulation?

# Meridional overturning circulation (MOC), GFDL model



# Diffusive theories for the ocean thermal structure and deep ocean circulation

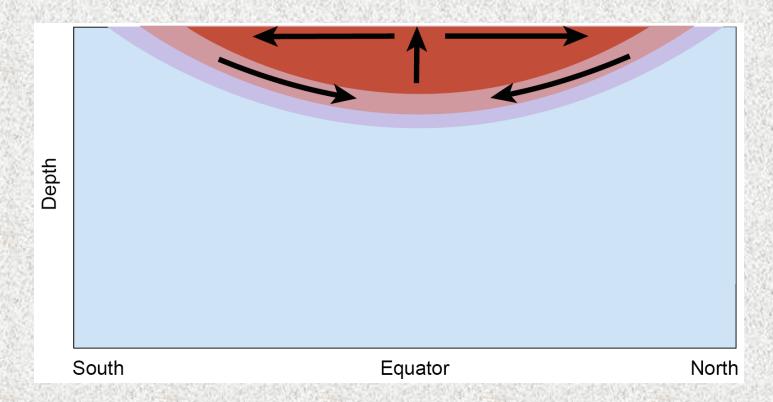


$$w \frac{\partial \rho}{\partial z} = k_d \frac{\partial^2 \rho}{\partial z^2}$$

 $k_d$  - diapycnal (vertical) diffusivity

Stommel 1958, Stommel and Arons 1960, Veronis 1976, others: **Downward** diffusion of heat is balanced by a broad upwelling of cold water

#### Adiabatic theories

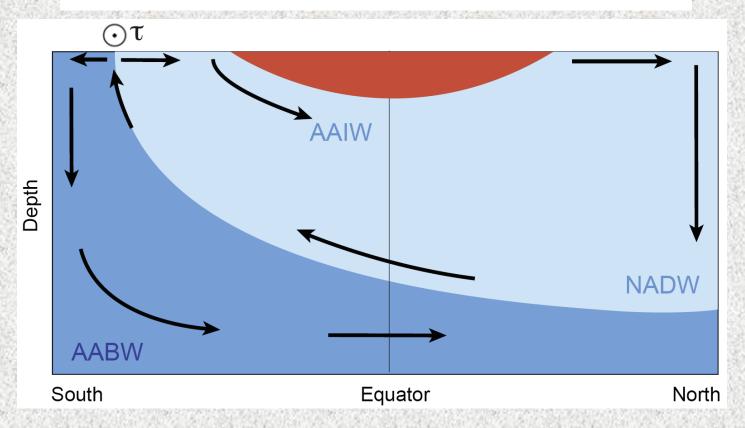


$$u\frac{\partial\rho}{\partial x} + v\frac{\partial\rho}{\partial y} + w\frac{\partial\rho}{\partial z} = 0$$

# Ekman pumping pushes water down along isopycnal surfaces.

Luyten, Pedlosky, and Stommel 1983: "The ventilated thermocline"; Iselin (1939), Welander (1959), Huang (1986)

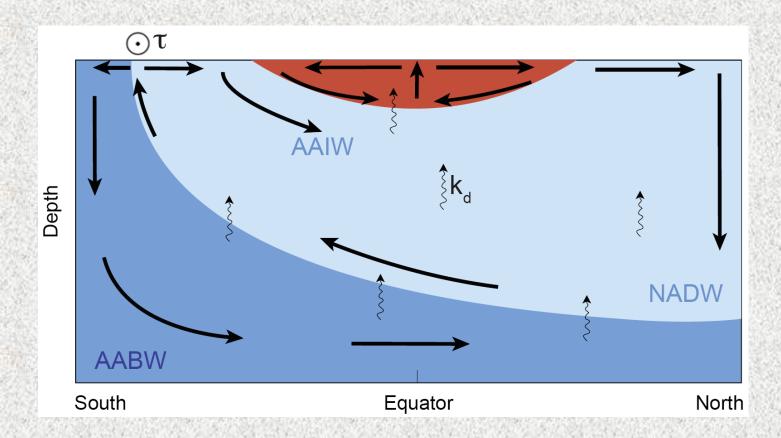
# The role of the wind-driven upwelling in the Southern Ocean



 $\tau$  – zonal wind stress in the Southern ocean

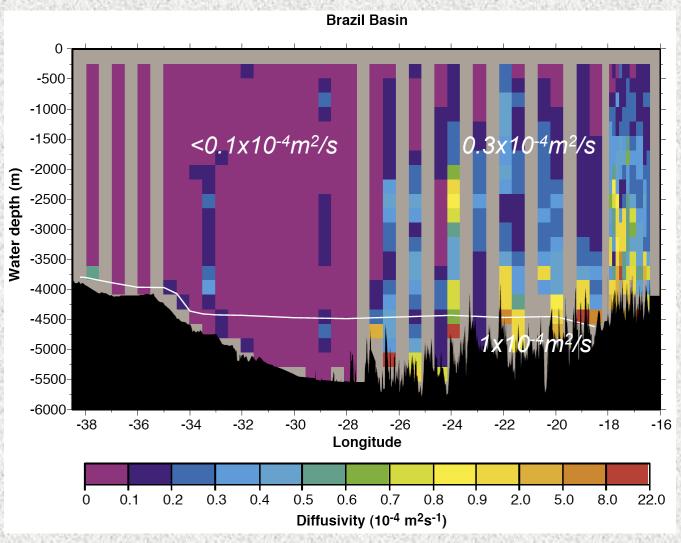
(e.g. Toggweiler and Samuels 1995, 1998, Gnanadesikan 1999)

# A full schematic picture of the MOC



(e.g. Barreiro, Fedorov and co-authors 2008)

 $k_d$  - diapycnal (vertical) diffusivity; very non-uniform  $0.1x10^{-4}m^2/s$  in the upper and deep ocean to  $20 x10^{-4}m^2/s$  in patches near bottom topography



Polzin et al 1997 (also Ledwell et al 1993)

#### **Questions:**

How important is diffusion (diabatic mixing) in the ocean interior for the ocean circulation and thermal structure?

What is the first-order solution for the ocean circulation and thermal structure? Is it diffusive or adiabatic?

What controls the ocean overturning circulation and stratification in an ocean with zero interior diffusion?

#### Approach:

Setting up a Lagrangian ocean model with a fully adiabatic interior flow

#### Navier-Stokes equations used in traditional GCMs

$$u_{t} = -\nabla \cdot (u \mathbf{u}) + v \left( f + \frac{u \tan \phi}{a} \right) - \left( \frac{1}{a \rho_{\circ} \cdot \cos \phi} \right) p_{\lambda} + (\kappa_{m} u_{z})_{z} + F^{u}$$

$$V_{t} = -\nabla \cdot (v \mathbf{u}) - u \left( f + \frac{u \tan \phi}{a} \right) - \left( \frac{1}{a \rho_{\circ}} \right) p_{\phi} + (\kappa_{m} v_{z})_{z} + F^{v}$$

$$W_Z = -\nabla_h \cdot \mathbf{u}_h$$

Vertical velocity

$$p_Z = -\rho g$$

Pressure

$$\theta_t \equiv -\nabla \cdot [\mathbf{u}\,\theta + \mathbf{F}(\theta)]$$

Potential temperature

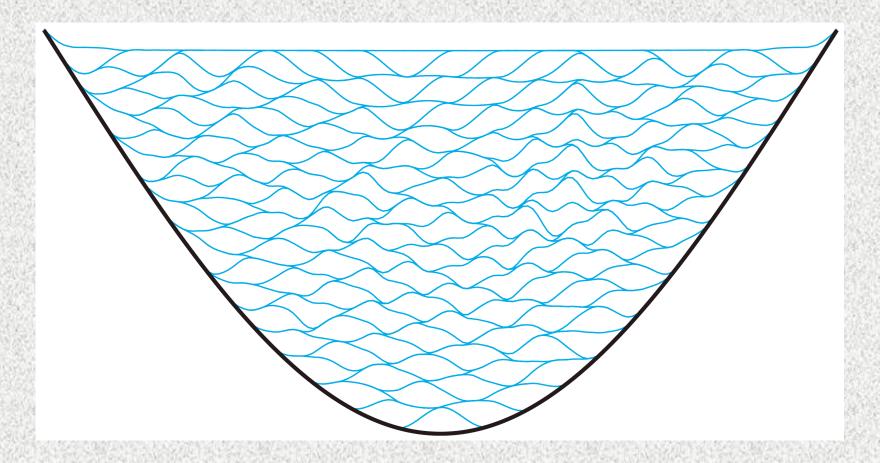
$$S_f = -\nabla \cdot [\mathbf{u} \, s + \mathbf{F}(s)]$$

Salinity

$$\rho \equiv \rho(\theta, s, z).$$

**Density** 

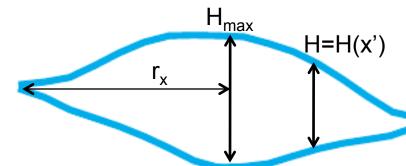
#### Lagrangian Ocean Model (Haertel et al 2010)



#### A stack of water parcels:

The stacking is done from the bottom up. Parcels conserve mass but change volume and shape. Pressure is hydrostatic. Dense parcels slide underneath less dense parcels.

# Parcel's shape



$$H(x', y') = H_{\text{max}} p\left(\frac{|x'|}{r_x}\right) p\left(\frac{|y'|}{r_y}\right)$$
 - parcel's thickness

p(x) - bell-shaped when set on a flat surface

$$p(x) = 1 + (2x - 3)x^2$$
 for  $x < 1$ 

# Parcel's shape

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p(x) is fixed

 $H_{\text{max}} = f(M, \rho)$ 

 $\begin{array}{l} \text{M}-\text{mass} \\ \rho-\text{density} \end{array}$ 

# **Equations of motions**



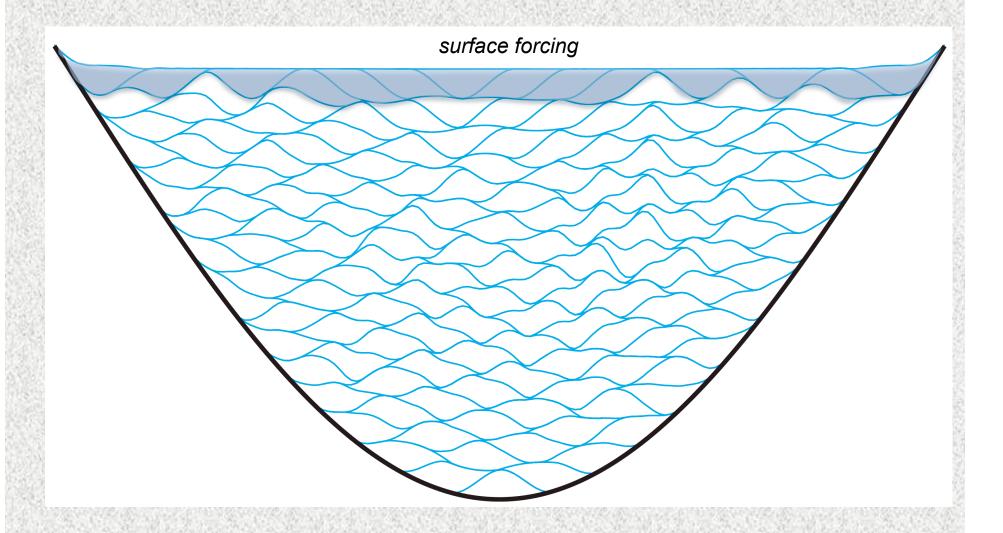
#### Newton's law:

$$\frac{d\mathbf{u}}{dt} = -f\,\mathbf{k} \times \mathbf{u} + \frac{1}{M} \int p ds + v \nabla^2 \mathbf{u}$$

$$\frac{dx}{dt} = u$$

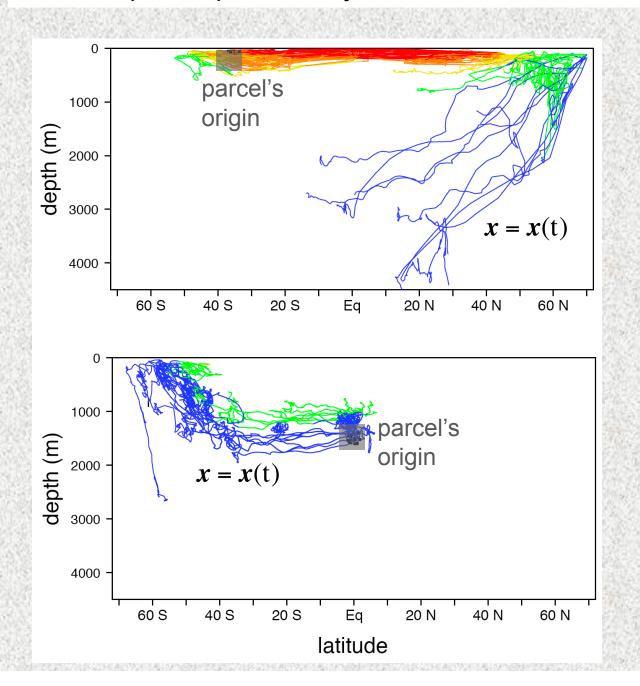
#### Density changes:

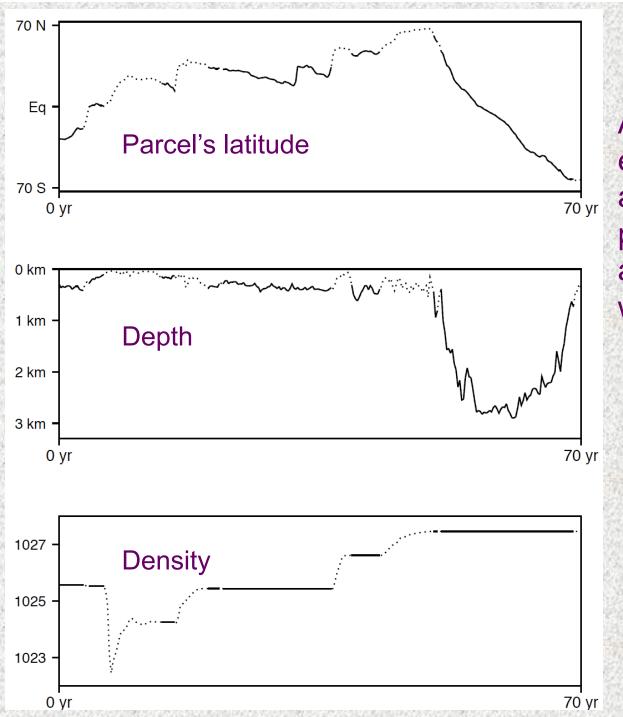
$$\frac{d\rho}{dt} = k_d \frac{\partial^2 \rho}{\partial z^2}$$



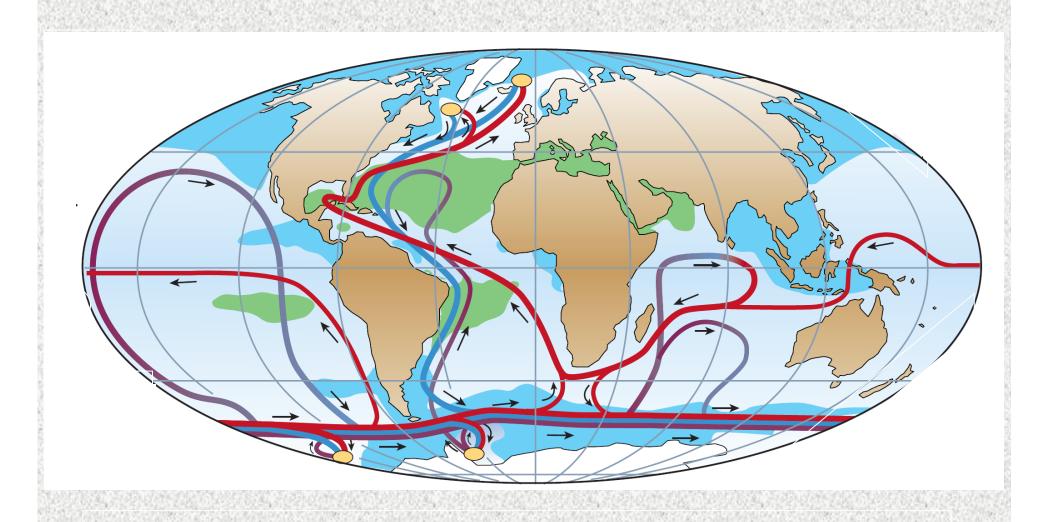
if 
$$k_d = 0$$
, then below the surface layer  $\frac{d\rho}{dt} = 0$ 

#### Examples of parcel's trajectories in the ocean

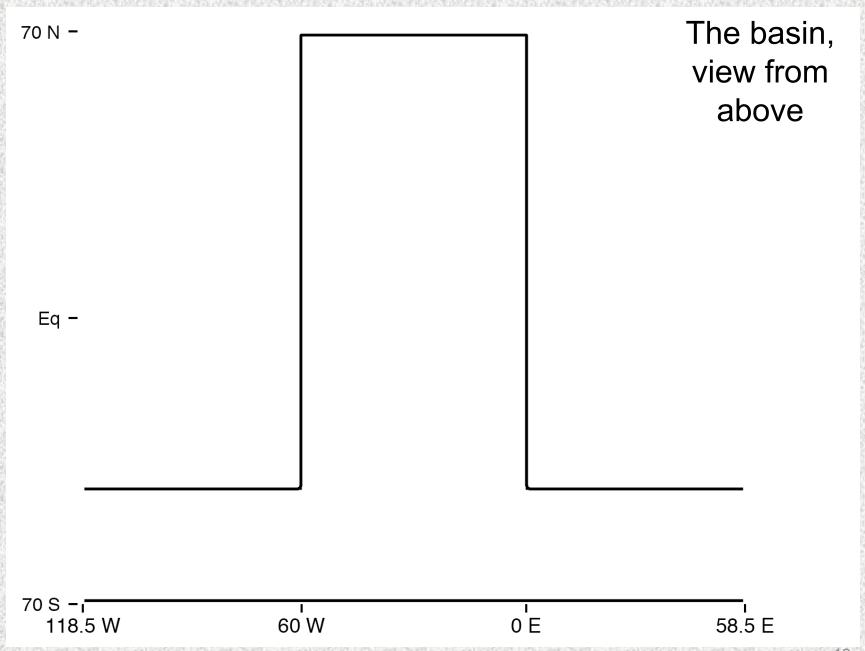




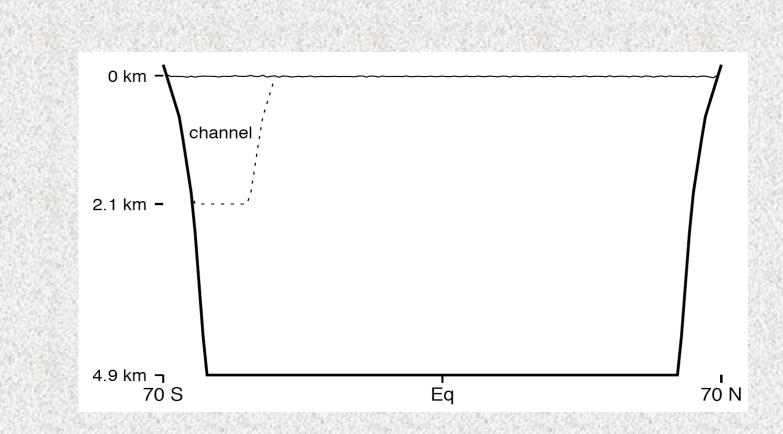
An example of a parcel's position and density with time



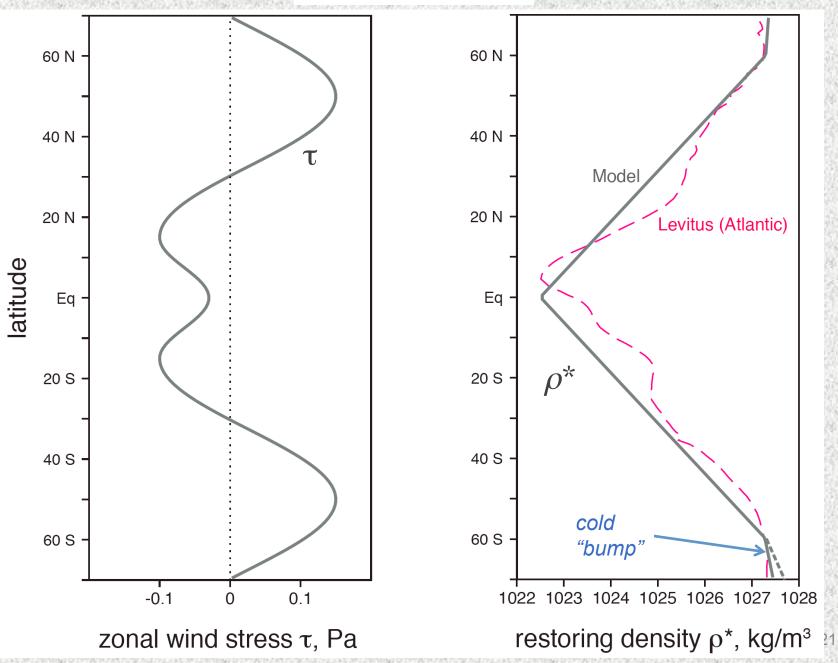
A cartoon of the global thermohaline circulation after Rahmstorf 2003

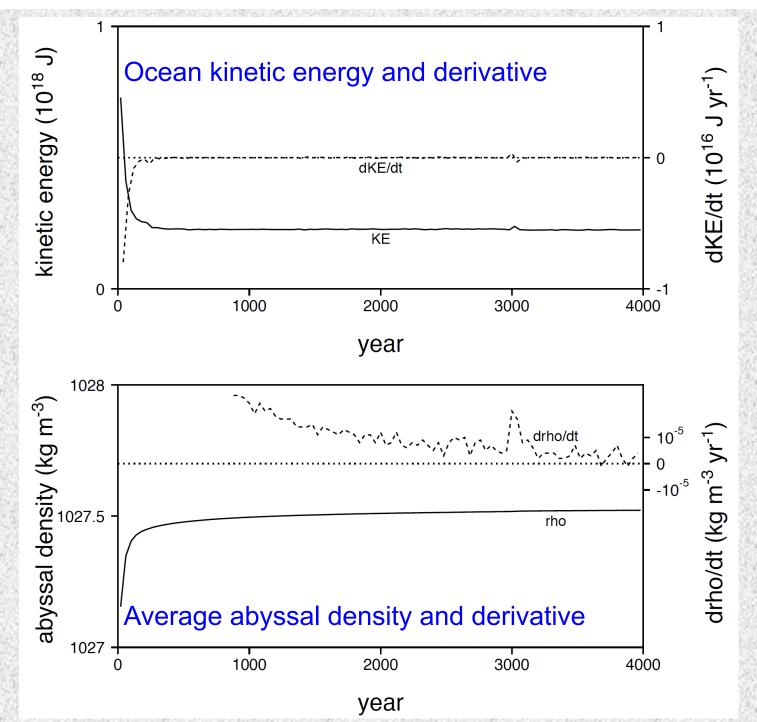


# The basin, side view

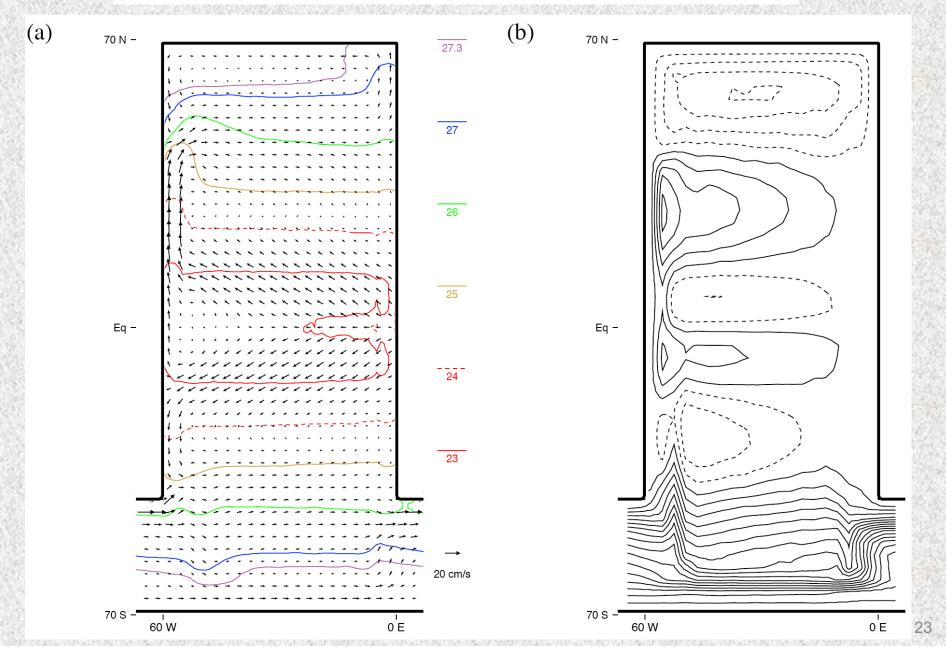


## Surface forcing

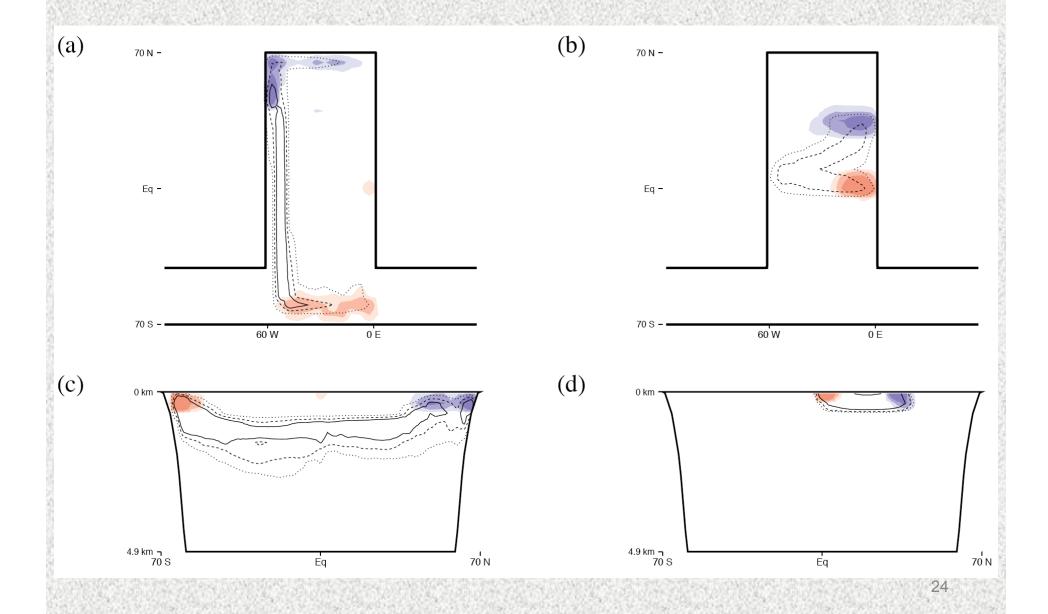




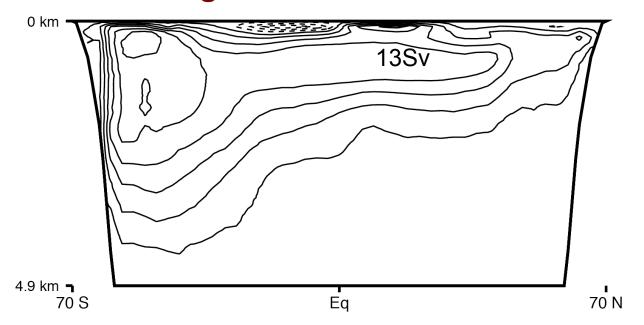
#### (a) Simulated surface density (kg/m³) and ocean currents (b) Barotropic stream function, 7 Sv intervals

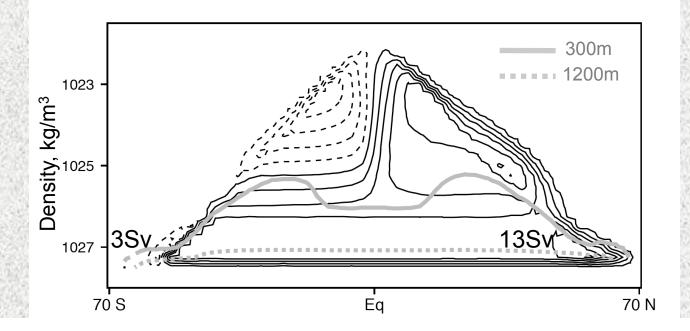


# Examples of parcel routes : Blue – subduction, red – upwelling

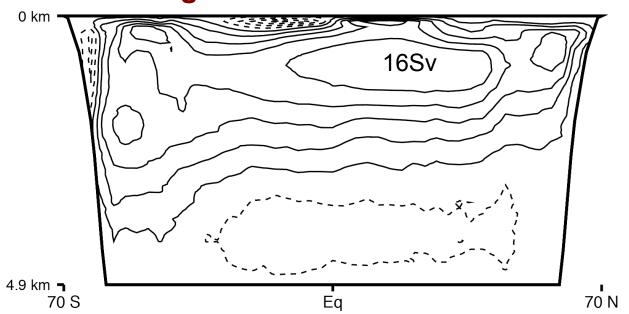


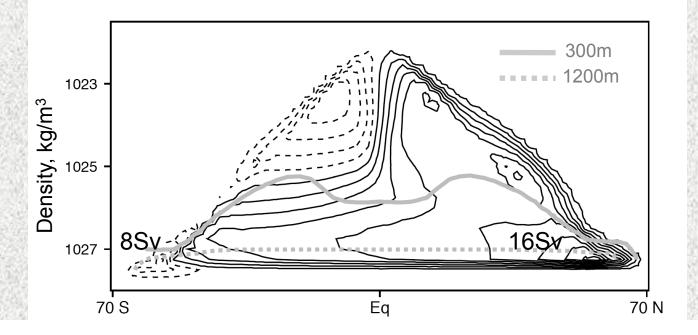
## **Overturning circulation: Non-diffusive**

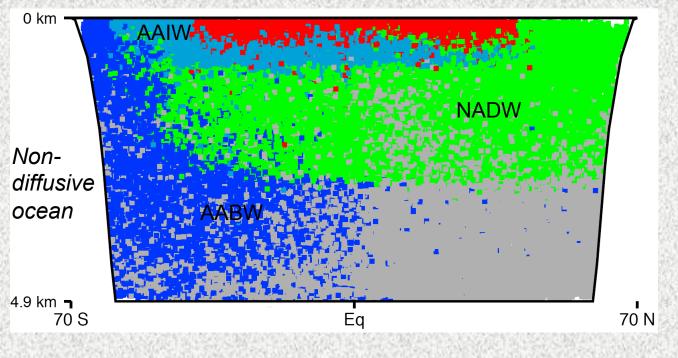


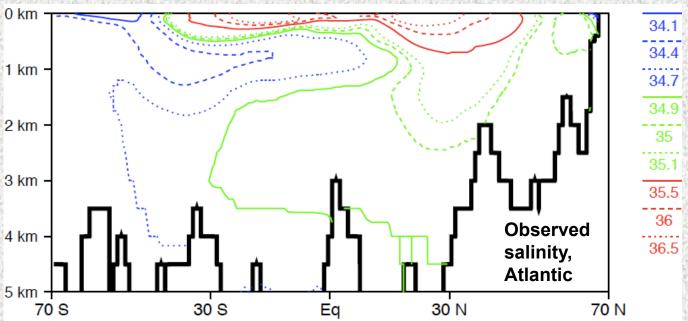


## Overturning circulation: Diffusive ocean









## Water Masses

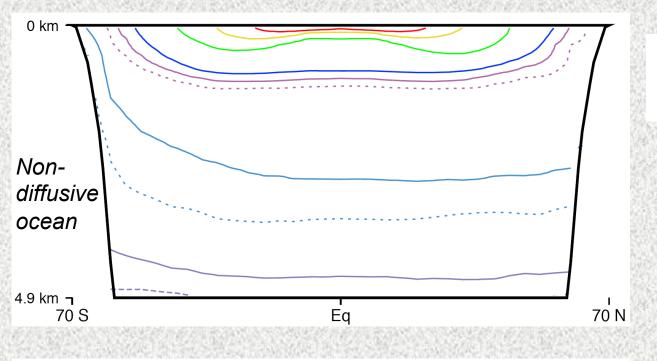
40°S - 40°N

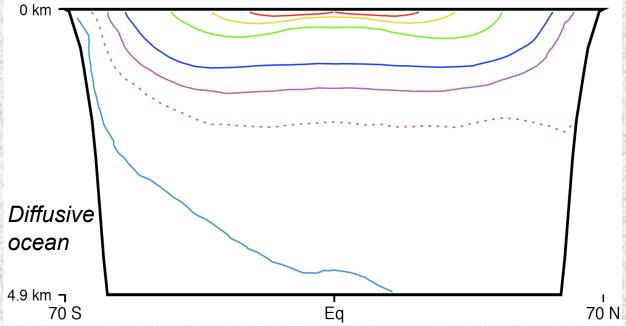
60°S - 40°S

 $> 40^{\circ}N$ 

< 60°S

not ventilated after 700yrs

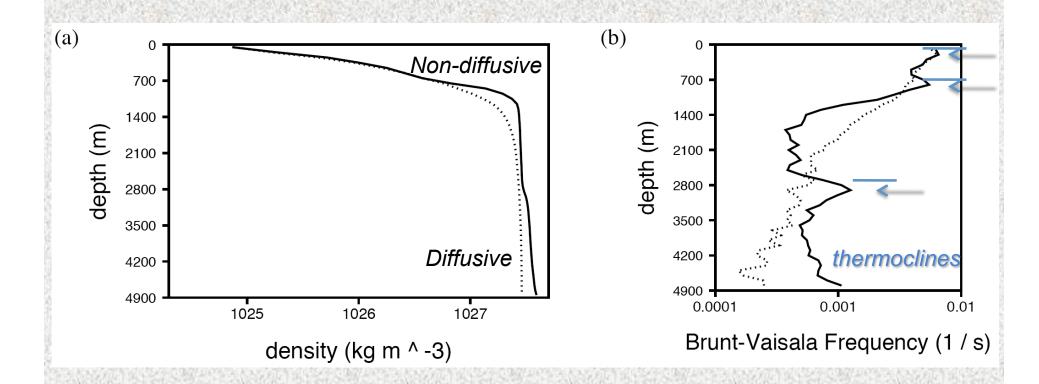




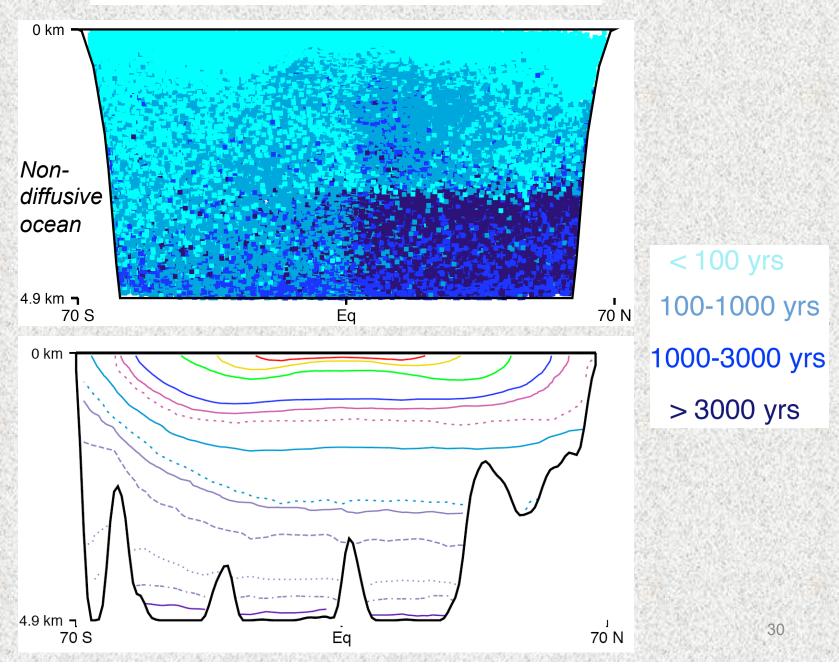
# Ocean Stratification



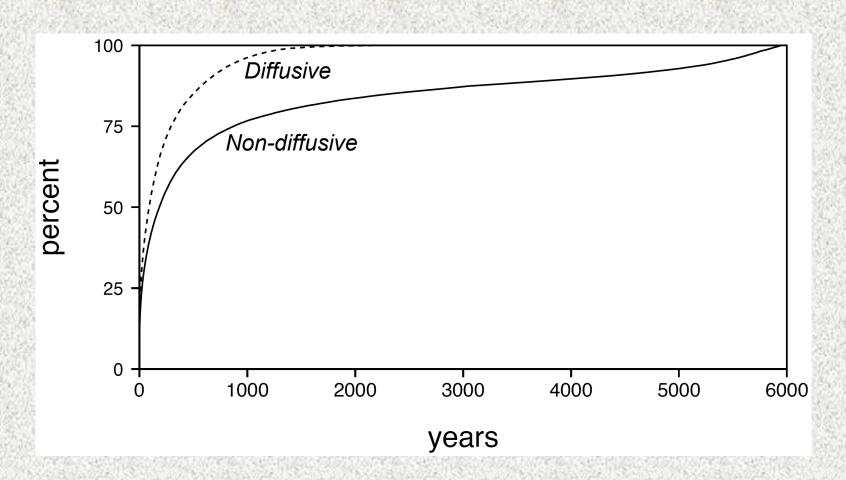
# Stratification and buoyancy frequency at 10°W, 30°N



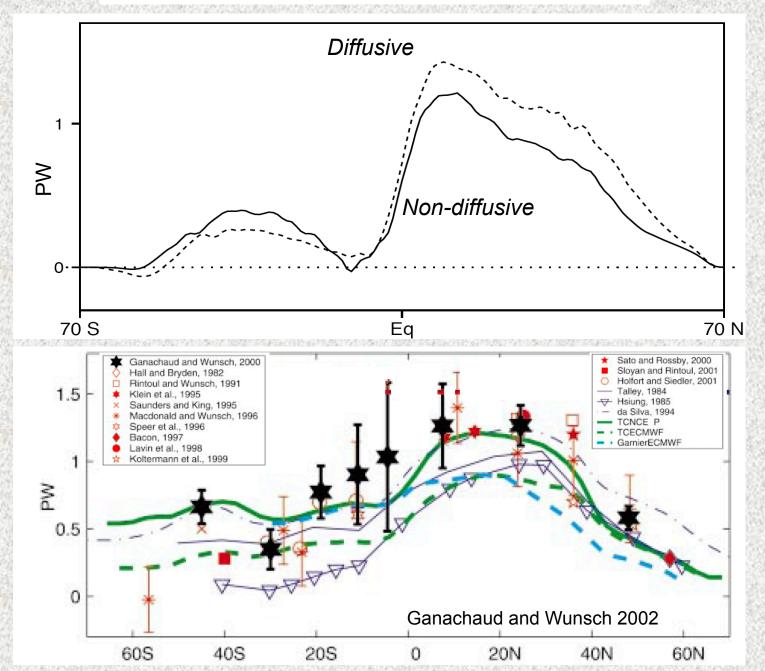
## Water Ventilation Age / Transit times



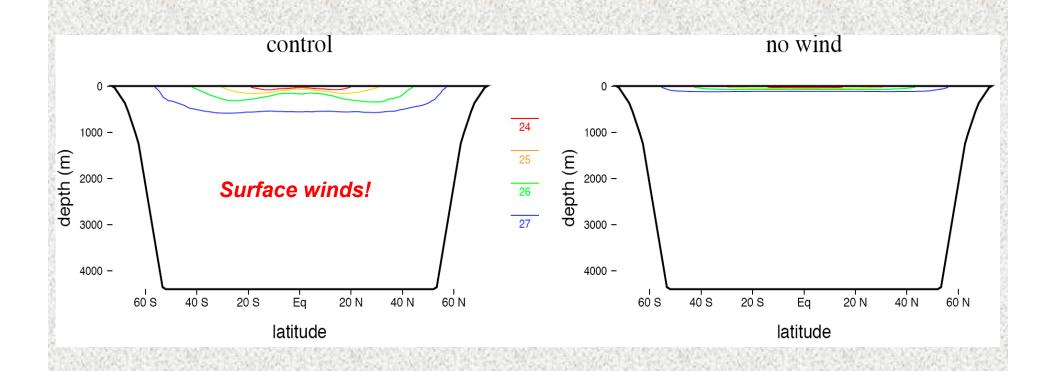
# Model cumulative distribution of water ventilation age (percentage of parcels younger than a certain "age")



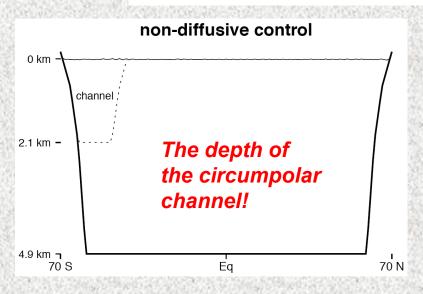
## **Northward heat transport in the Atlantic**

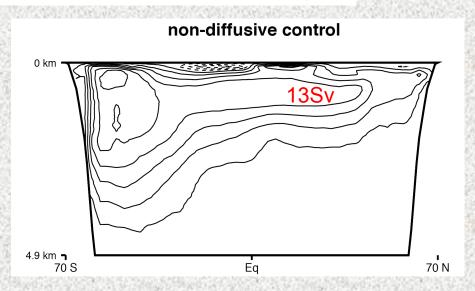


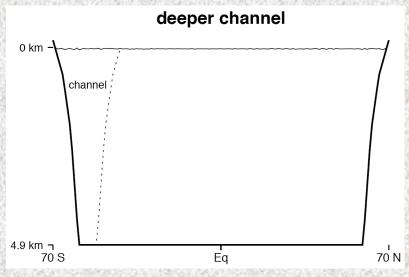
# Non-diffusive ocean: what controls stratification and the AMOC intensity?

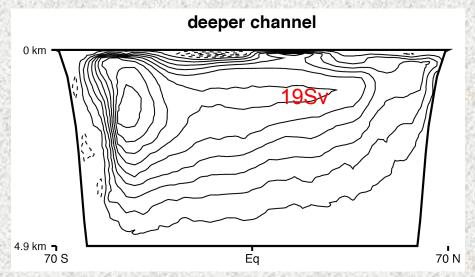


# Non-diffusive ocean: what controls stratification and the AMOC intensity?





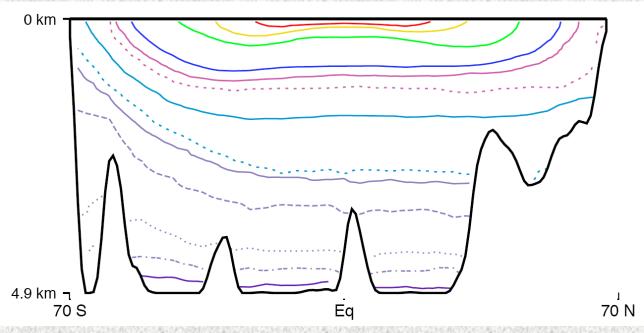


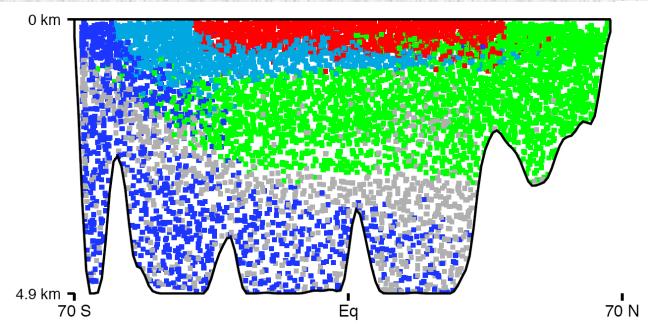


#### **Summary:**

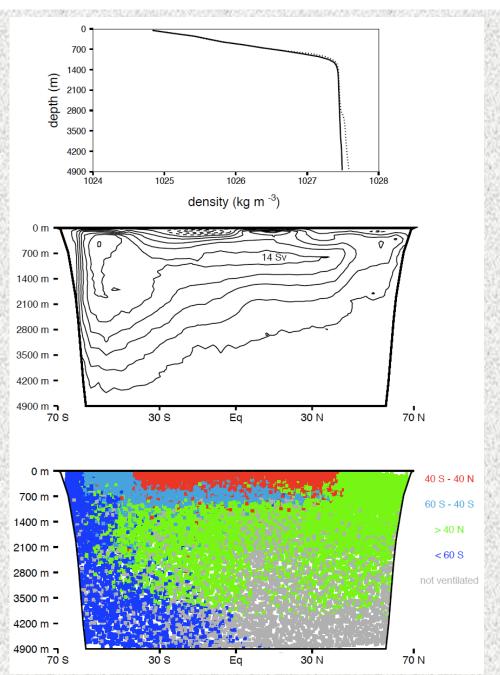
- An ocean with a fully adiabatic interior gives the first-order solution for the ocean overturning and stratification problem, as long as the model includes zonal winds and a circumpolar channel.
- > Deepening the channel or increasing the wind stress intensifies the overturning
- ➤ Diffusion provides the second-order perturbations, increasing stratification in the deep ocean (between 1000 and 3000m) and producing a more realistic bottom overturning cell

## The role of bottom

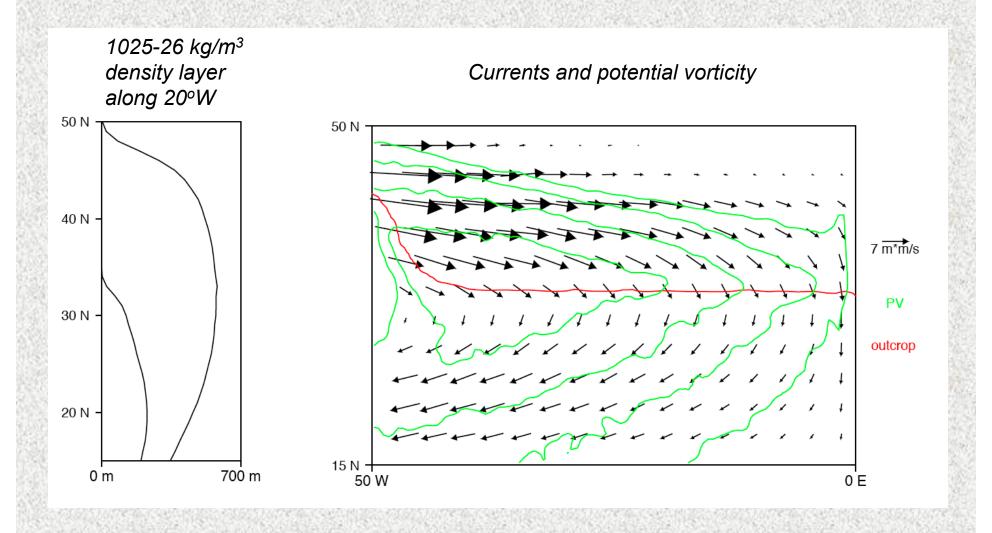


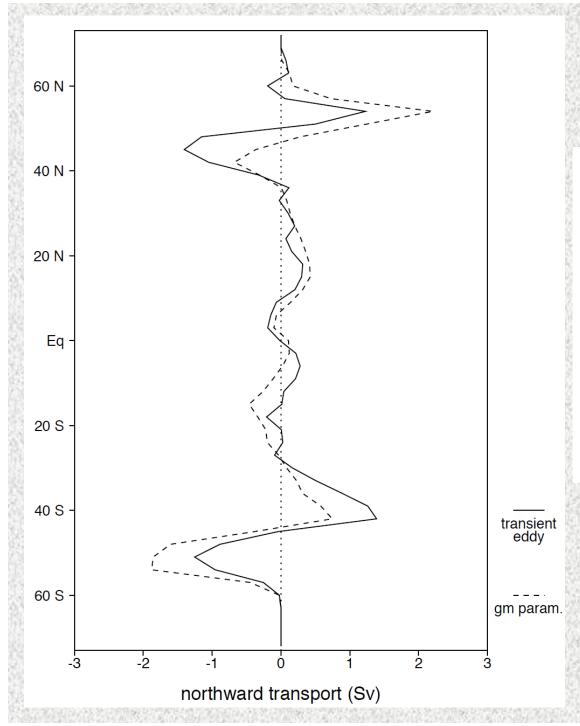


#### What controls stratification in the bottom ocean



#### The ventilated thermocline





# Adiabatic horizontal eddy mixing in the model:

**Northward bolus transport** of 1026-1027 kg m<sup>-3</sup> layer thickness for 3° model resolution in the non-diffusive run (solid line), \( \sqrt{v}'H'dx, \) and **bolus transport** in a conventional GM parameterization with a coefficient of 500 m<sup>2</sup>s<sup>-1</sup> (dotted line)