# Physical oceanography Lecture 1 Introduction to the ocean general circulation Thermodynamics and dynamics

ICTP: The General Circulation of the Atmosphere and Oceans: A Modern Perspective

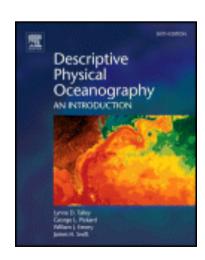
Lynne Talley, Scripps Institution of Oceanography, UCSD Monday July 11, 2011

Descriptive Physical Oceanography: An Introduction (6<sup>th</sup> edition) Talley, Pickard, Emery, Swift (2011) (Elsevier)

Just published in April: hard copy and ebook, extensive web materials, including open access chapters on Dynamics, Climate and the Oceans, adjacent seas including the Mediterranean

Background, in-depth coverage of all topics can be found in DPO

http://www-pord.ucsd.edu/~ltalley/DPO/ has links to all materials



## 1. Thermodynamics

- Equation of state of seawater (dependence of density on pressure, temperature, salinity)
- External forcings for ocean density
- Adiabatic compression effects: potential temperature and potential density
- Typical distributions of temperature, salinity, density
  in physical space and using density as a vertical coordinate

#### 1. Thermodynamics: Pressure

#### Pressure is a force per unit area

```
Units of pressure: dyne/cm² and N/m²

1 Pascal = 1 N/m²

1 bar = 106 dynes/cm² = 105 N/m²

approximately the atmospheric pressure at sea level

1 atmosphere = 1000 millibar = 1 bar

1 dbar = 0.1 bar
```

For motions slower and larger than gravity waves, the ocean is in hydrostatic balance to a very good approximation

Vertical momentum equation reduces to

Dw/Dt 
$$\approx 0 = - (\Delta p/\Delta z) - \rho g$$
  
For  $\Delta z = 1$  meter, density  $\rho \sim 1025$  kg/m³, and  $g = 9.8$  m/s², we get  $\Delta p = \rho g \Delta z = (1025 \text{ kg/m}^3)(9.8 \text{ m/s}^2)(1 \text{ m}) = 10045 \text{ kg/(m s}^2) = 0.10045 \text{ bar} = 1.0045 \text{ dbar}$ 

Temperature: standard concept

Ocean range: freezing point (about -1.8°C) to about 30°C

(Freezing point is < 0°C because of salt content)

Temperature is changed externally by heating and cooling.

Potential temperature  $\theta$ : water is slightly compressible. Remove passive effects of compression on temperature.

 $\theta$  is the temperature a parcel of water has if moved adiabatically (without heat exchanges or mixing) to the sea surface.

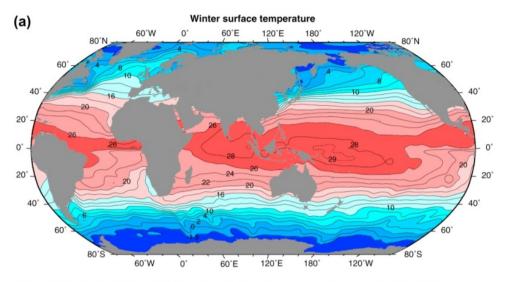
**Heat:** units are Joules

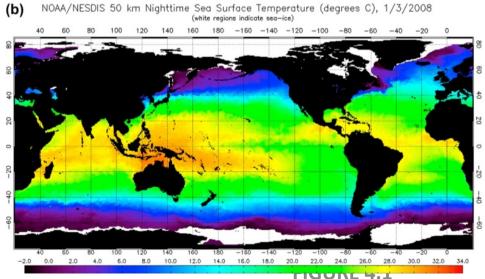
Heat change: units are Joules/sec = Watts

Heat content per unit volume (q in  $J/m^3$ ):

 $dq/dT = \rho c_p$  where  $c_p$  is specific heat

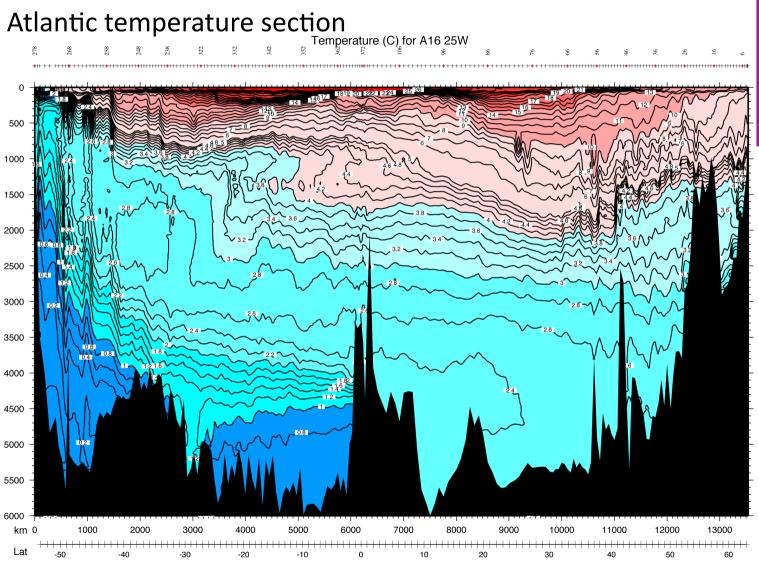
Typical seawater values:  $c_p \sim 3850 \text{ J/kg }^{\circ}\text{C}$ ;  $\rho \sim 1025 \text{ kg/m}^{3}$ 



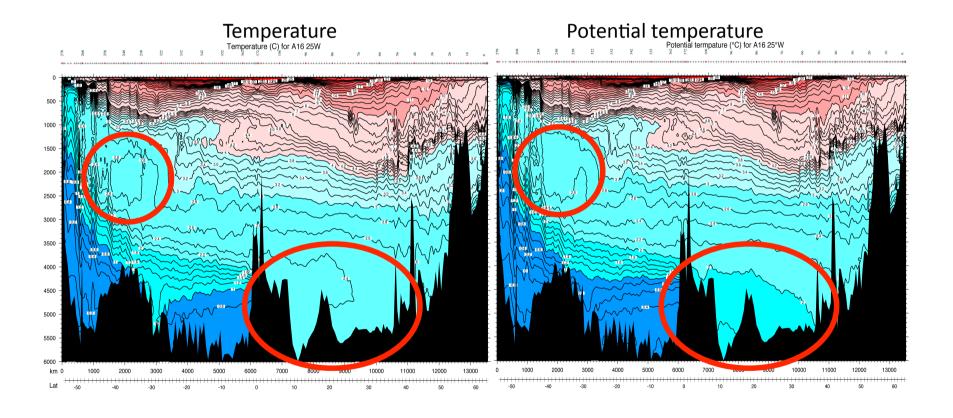


(a) Surface temperature (°C) of the oceans in winter (January, February, March north of the equator; July, August, September south of the equator) based on averaged (climatological) data from Levitus and Boyer (1994). (b) Satellite infrared sea surface temperature (°C; nighttime only), averaged to 50 km and 1 week, for January 3, 2008. White is sea ice. (See Figure S4.1 from the online supplementary material for this image and an image from July 3, 2008, both in color).

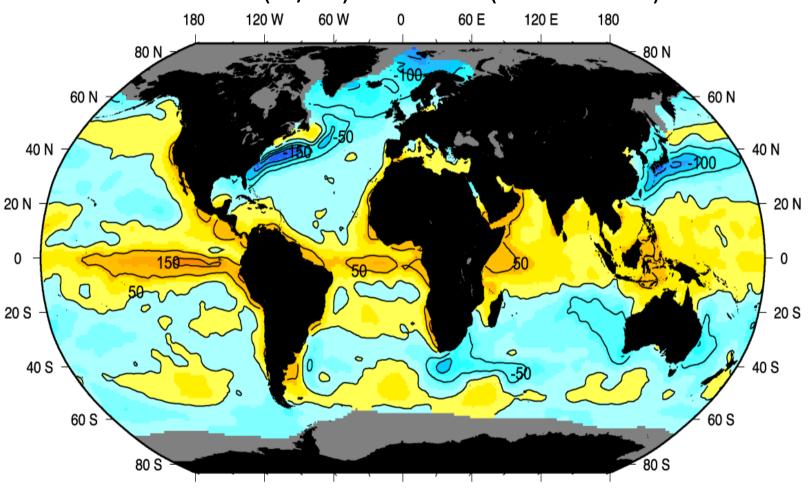




Atlantic temperature and potential temperature sections for contrast

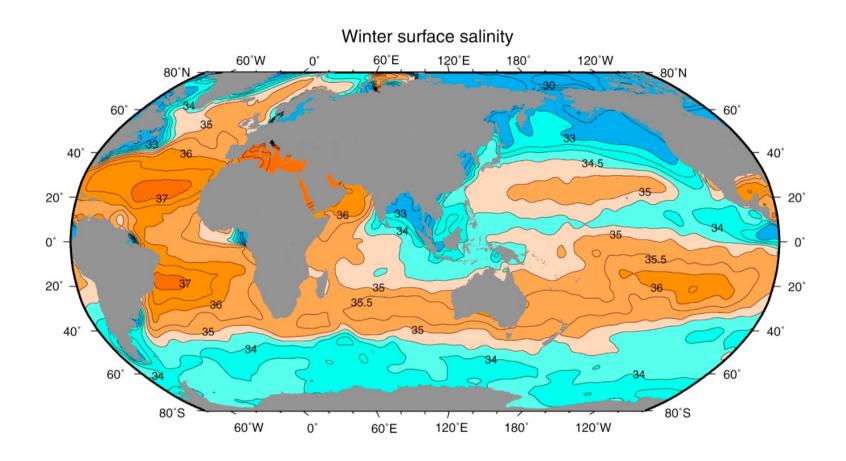


Surface heat flux (W/m²) into ocean (annual mean)



Salinity: mass of dissolved matter (expressed in grams) in a kilogram of seawater = Absolute salinity

- •Units are parts per thousand (o/oo) or "psu" (practical salinity units), or unitless (mass/mass)
- "Law of equal proportions": the constituents of sea salt are present in almost equal proportion everywhere in the ocean because the ocean is well mixed on the time scale of weathering (source of most salts)
- •Typical ocean salinity is 34 to 36 (i.e. 34 to 36 gm salt/kg seawater); total range in open ocean is about 30 (sea ice regions) to 40 (Red Sea)
- •Salinity is changed by DILUTION with freshwater (from precipitation, evaporation, runoff). The total amount of salt in the ocean does not change on non-geological time scales.
- •New international definition of salinity in 2010. Measurements and archived observations are still to be based on the conductivity methods (standard in 1978), but corrections to salinity are to be applied henceforth.



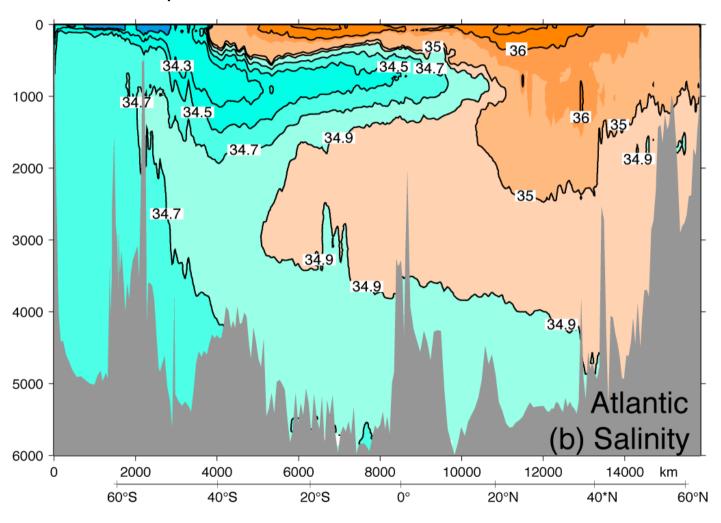
Surface salinity (psu) in winter (January, February, and March north of the equator; July, August, and September south of the equator) based on averaged (climatological) data from Levitus et al. (1994b).

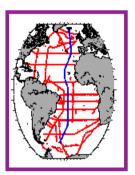
FIGURE 4.15

**TALLEY** 

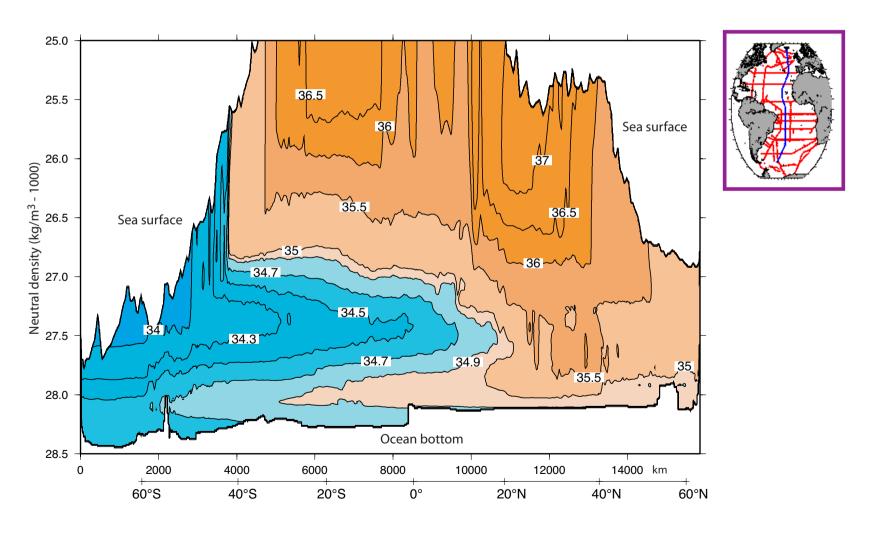
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#### Atlantic salinity section

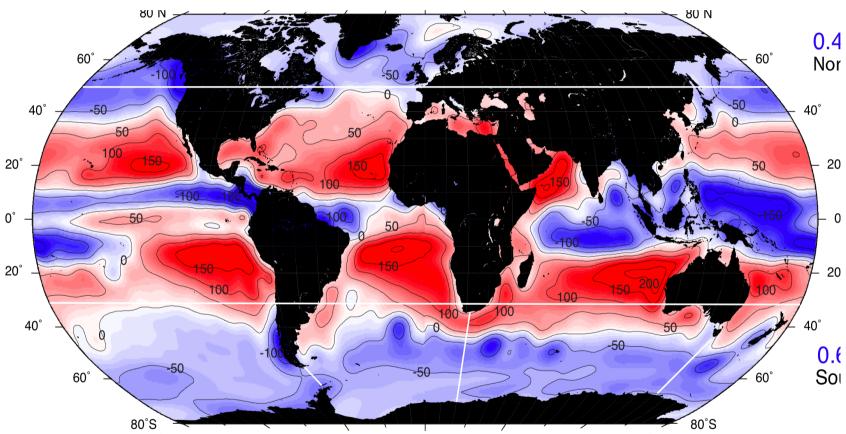




Atlantic salinity section with neutral density as the vertical coordinate (oceanography equivalent to isentropic coordinates)



What sets salinity? Precipitation + runoff minus evaporation (cm/yr)



Salinity is set by freshwater inputs and exports since the total amount of salt in the ocean is constant, except on the longest geological timescales

## Equation of state (EOS) of seawater

Seawater density is determined empirically (in the lab)

$$\rho = \rho(S, T, p)$$
 Units are mass/volume (kg/m<sup>3</sup>)

The EOS is nonlinear; modelers often approximate it as linear.

Most commonly used EOS: EOS80

Newest EOS: TEOS-10 (IOC, SCOR, IAPSO, 2010)

ρ ranges from about 1020 kg/m³ at the sea surface to 1050 kg/m³ at bottom of ocean, mainly due to compression (pressure dependence)

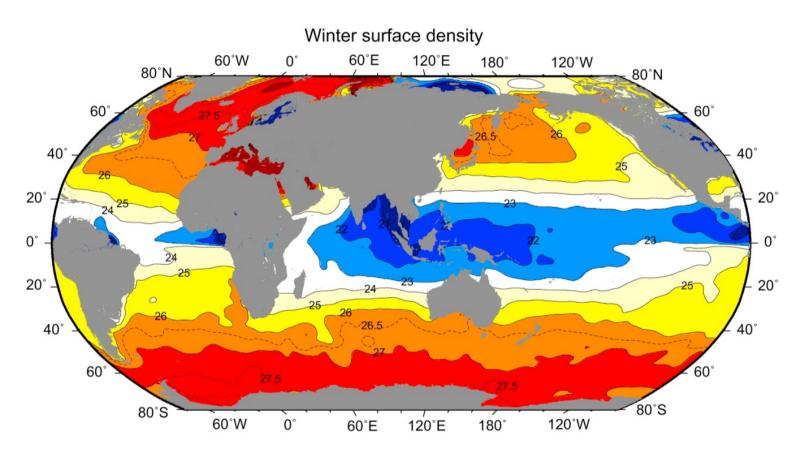
We often express density as

$$\sigma$$
 (S, T, p) =  $\rho$ (S, T, p) - 1000 kg/m<sup>3</sup>

Thus  $\sigma$  ranges from about 20 to 50 kg/m<sup>3</sup>

Potential density: Remove effect of mechanical compression. Create potential density profile by finding the density a water parcel has if moved adiabatically to a reference pressure.

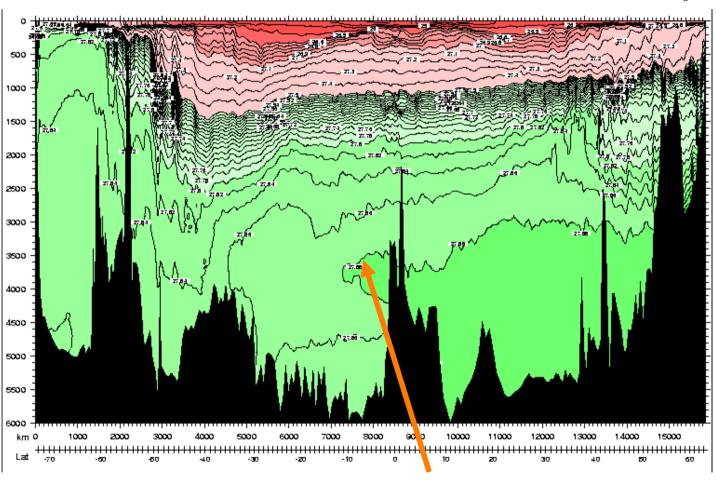
Compressibility depends on temperature: cold water is more compressible than warm. Therefore two parcels (one cold/fresh and the other warm/salty) that might be the SAME density at their actual pressure (for example, at 4000 dbar), would not have the same density at the sea surface (0 dbar). This results in all kinds of complications; choice of reference pressure therefore depends entirely on what you want to do (your application).

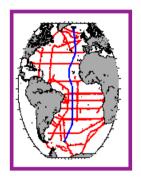


Surface density  $\sigma\theta$  (kg m<sup>-3</sup>) in winter (January, February, and March north of the equator; July, August, and September south of the equator) based on averaged (climatological) data from Levitus and Boyer (1994) and Levitus et al. (1994b).

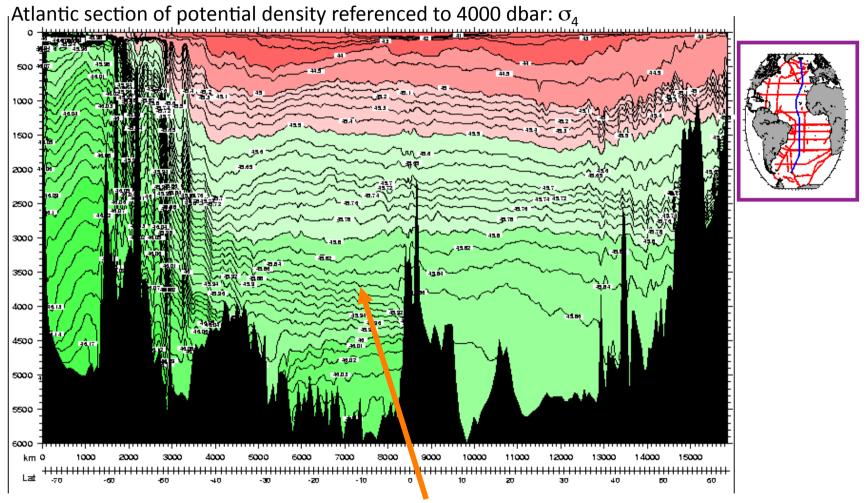
**FIGURE 4.19** 

Atlantic section of potential density referenced to 0 dbar (sea surface):  $\sigma_{\theta}$ 



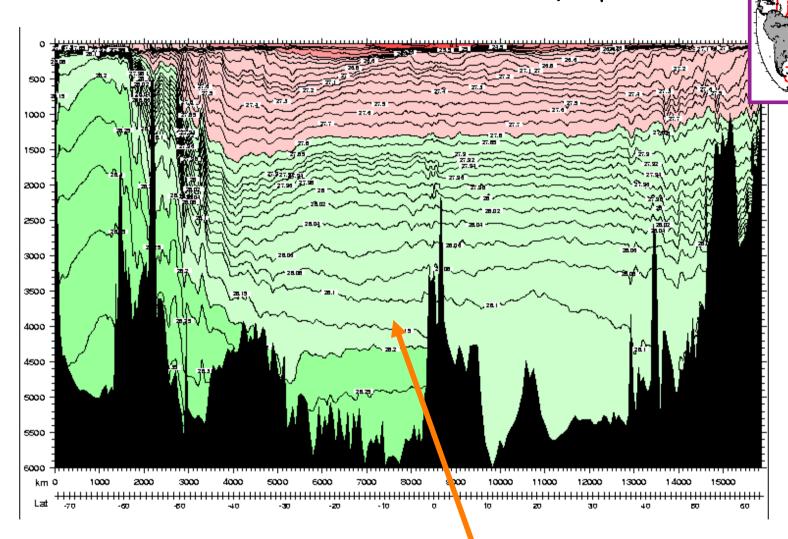


Need to use deeper reference pressures to check local vertical stability (e.g.  $\sigma_4$ )



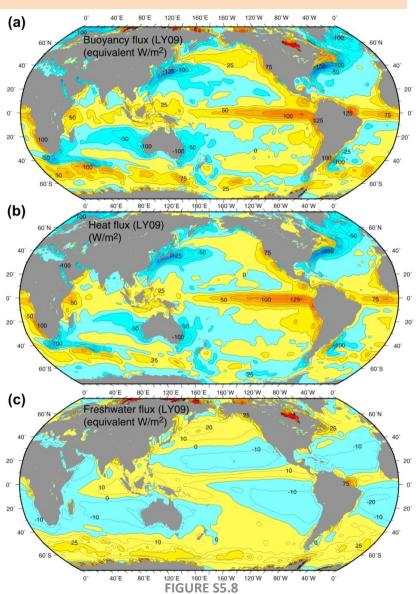
Potential density  $\sigma_{\theta}$  inversion vanishes with use of deeper reference ( $\sigma_4$ ): in fact, extremely stable!!

# Atlantic section of "neutral density": γ<sup>n</sup>



Jackett and McDougall (1997)

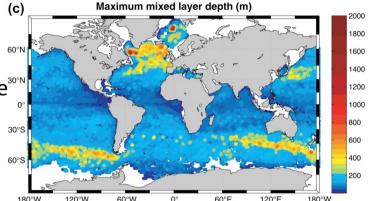
- External forcings for ocean
   density: heating/cooling and
   precipitation/evaporation/runoff/brine rejection
- Buoyancy flux: buoyancy is 1/density
- When buoyancy increases, density decreases
- Heating increases buoyancy
- Rain increases buoyancy
- From these maps, you can see that the buoyancy is mostly changed by heat flux



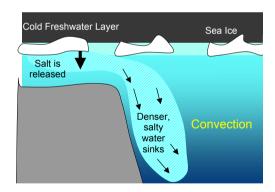
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Mechanisms to change ocean temperature, salinity, density

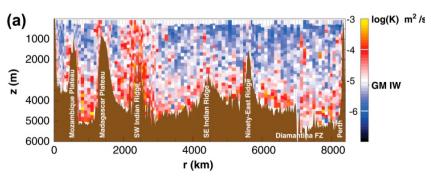
 Through the mixed layer: convection and restratification (external buoyancy flux through the sea surface)



 Brine rejection (external buoyancy flux that creates sea ice, removal of salt from ice)



 Internal mixing (diapycnal and along-isopycnal diffusion): spatially and temporally dependent diffusivities – much stronger at ocean bottom



- Governing equations (momentum, mass, S, T, EOS)
- Coriolis force
- Geostrophic balance
- Ekman balance
- Potential vorticity evolution

### Governing equations

- Mass conservation (continuity) (no holes)
- Force balance: Newton's Law ( $\vec{F} = m\vec{a}$ ) (3 equations)
- Equation of state (for oceanography, dependence of density on temperature, salinity and pressure) (1 equation)
- Equations for temperature and salinity change in terms of external forcing, or alternatively an equation for density change in terms of external forcing (2 equations)

#### Momentum equations with Earth's rotation

```
Horizontal (x) (west-east)
    acceleration + advection + Coriolis = pressure gradient force + viscous term

Horizontal (y) (south-north)
    acceleration + advection + Coriolis = pressure gradient force + viscous term

Vertical (z) (down-up)
    acceleration +advection (+ neglected very small Coriolis) =
        pressure gradient force + effective gravity (including centrifugal force) +
        viscous term
```

Momentum equations with rotation Coordinates are (x, y, z) (east, north, up) Velocities are (u, v, w)

x: 
$$\partial u/\partial t + u \, \partial u/\partial x + v \, \partial u/\partial y + w \, \partial u/\partial z - fv = -(1/\rho)\partial \rho/\partial x \\ + \partial/\partial x (A_H \partial u/\partial x) + \partial/\partial y (A_H \partial u/\partial y) + \partial/\partial z (A_V \partial u/\partial z)$$
 (7.11a)

y:  $\partial v/\partial t + u \, \partial v/\partial x + v \, \partial v/\partial y + w \, \partial v/\partial z + fu = -(1/\rho)\partial \rho/\partial y \\ + \partial/\partial x (A_H \partial v/\partial x) + \partial/\partial y (A_H \partial v/\partial y) + \partial/\partial z (A_V \partial v/\partial z)$  (7.11b)

z:  $\partial w/\partial t + u \, \partial w/\partial x + v \, \partial w/\partial y + w \, \partial w/\partial z$  (+ neglected small Coriolis) = -  $(1/\rho)\partial \rho/\partial z - g + \partial/\partial x (A_H \partial w/\partial x) + \partial/\partial y (A_H \partial w/\partial y) + \partial/\partial z (A_V \partial w/\partial z)$  (7.11c)

f is the Coriolis parameter  $f = 2\Omega \sin(\text{latitude})$ g is gravitational acceleration Eddy viscosity rather than molecular viscosity;  $A_H$  is horizontal and  $A_V$  is vertical eddy viscosity

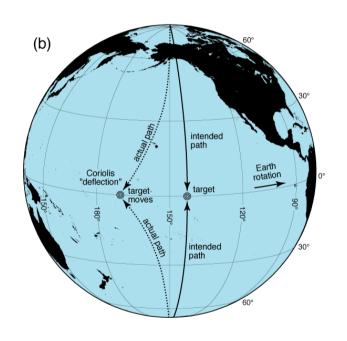
#### **Coriolis force**

Deflection relative to Earth's rotating surface, to the right in the northern hemisphere, to the left in the southern hemisphere

#### Inertial motion observations:

Surface drifters after passing of a storm in the NE Pacific

(d'Asaro et al., 1995)



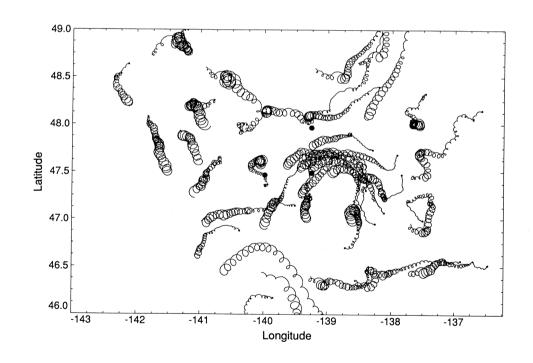
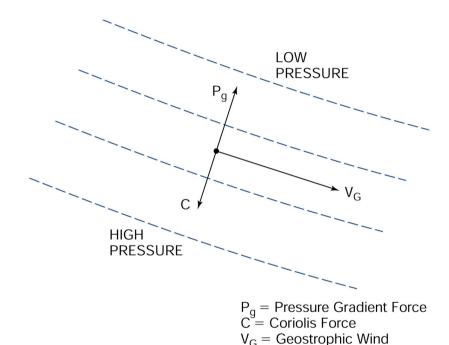


FIGURE S7.2 FIGURE S7.8

Geostrophic balance: pressure gradient force balanced by Coriolis force



The approximation (small Rossby number, small aspect ration, small Ekman number)

Horizontal (x): Coriolis = pressure gradient force

- fv = - 
$$(1/\rho)\partial p/\partial x$$

Horizontal (y): Coriolis = pressure gradient force

$$fu = -(1/\rho)\partial p/\partial y$$

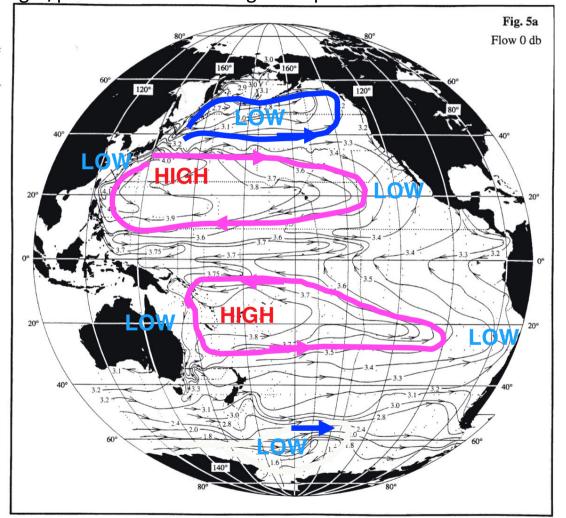
(and hydrostatic balance:

Vertical (z): 0 = pressure gradient force + effective gravity

$$0 = -(1/\rho)\partial p/\partial z - g$$

Example from ocean of geostrophic flow

Surface height/pressure and surface geostrophic circulation



Circulation is counterclockwise around the Low (cyclonic) and clockwise around the High (anticyclonic).

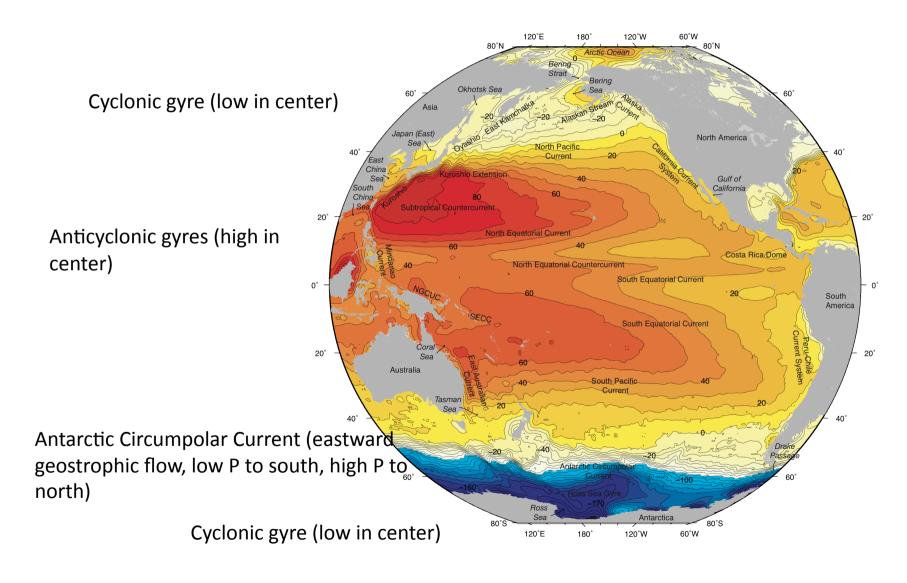
(northern hemisphere)

Southern Hem:

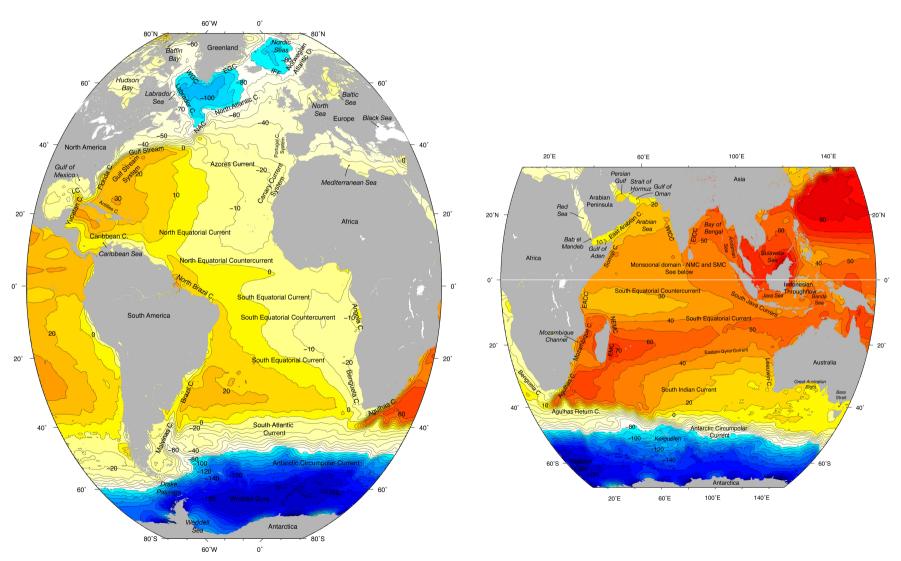
Cyclonic is clockwise, etc..

Reid, 1997

Sea surface height in the Pacific. (Using Niiler et al., 2003, surface heights based on drifters)



Sea surface height. (Using Niiler et al., 2003, surface heights based on drifters)



# 2. Dynamics: Thermal wind and geostrophic method

Thermal wind relation:

- 
$$f\partial v/\partial z = (g/\rho_0)\partial \rho/\partial x$$
  
 $f\partial u/\partial z = (g/\rho_0)\partial \rho/\partial y$ 

Relates vertical shear to horizontal density variations. Variants of this constitute the "geostrophic method" or "dynamical method" for estimating geostrophic velocities from density profiles.

Requires measurement or estimate of velocity at one depth. This has traditionally been the trickiest part of large-scale circulation estimation.

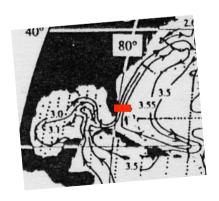
"Reference level velocity": determined through overall mass balances, excellent observed velocities (floats or drifters) but carefully matched with synoptic observations (e.g. through data assimilation or inverse methods). This used to be called setting the "level of no motion", but it is really finding the "level of known motion"

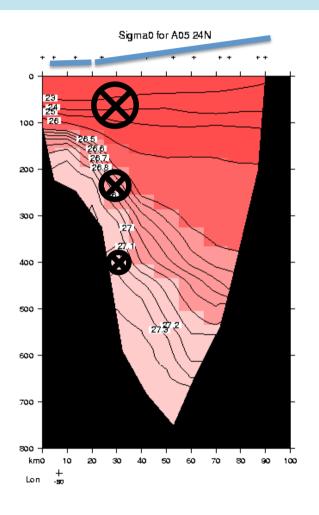
# 2. Dynamics: Thermal wind and geostrophic method

Gulf Stream in Florida Strait:

Potential density section and velocity section.

Inferred sea surface height is low inshore and high offshore





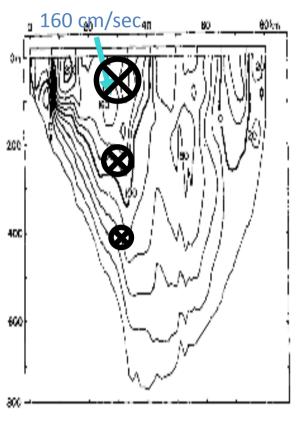
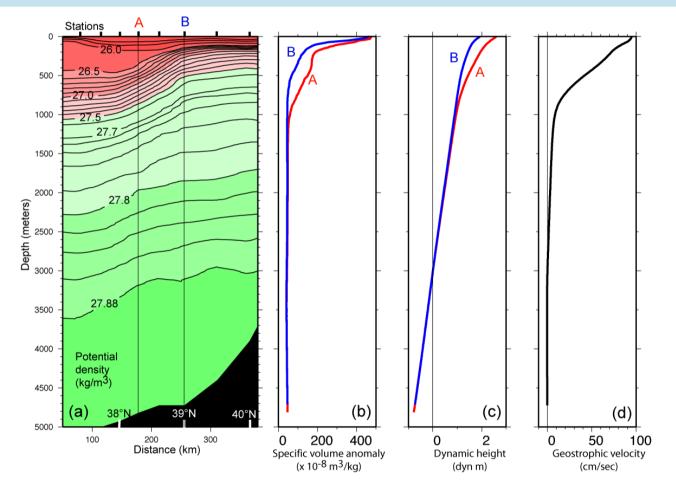


Fig. 7. Geostrophic velocity relative to the bottom. Prograve is northward. The contour interval is 20 cm s<sup>-1</sup>.

Roemmich, 1983

#### 2 Dynamics: thermal wind and geostrophic method

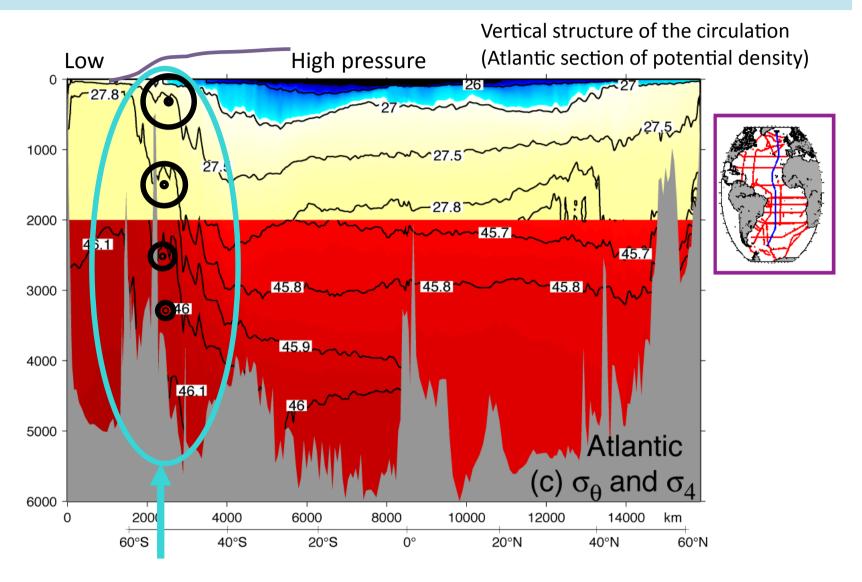


In this example, compute geostrophic velocities relative to 0 cm/sec at 3000 dbar. If we KNOW v at 3000 dbar, then just add it to the whole profile

Gulf Stream density, dynamic height and geostrophic velocity

DPO Fig. 7.11

#### 2. Dynamics: thermal wind and geostrophic method



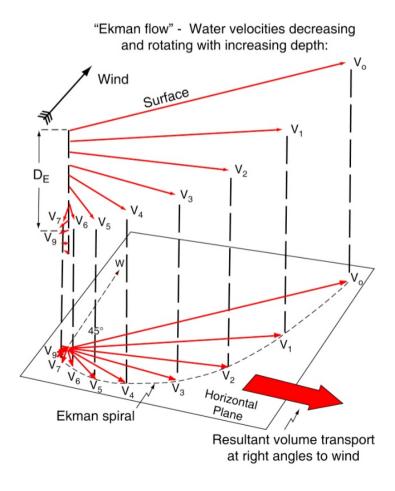
Antarctic Circumpolar Current

DPO Fig. 4.10

# 2. Dynamics: Ekman balance

#### Ekman balance

 Frictional balance in the surface layer: driven by wind stress, subject to Coriolis force



In the surface boundary layer, the approximate force balance is

x: 
$$-fv = \partial/\partial z(A_V \partial u/\partial z)$$

y: 
$$fu = \partial/\partial z(A_V\partial v/\partial z)$$

Integrate vertically to obtain the Ekman layer "transport", which depends only on the wind stress and not on the eddy viscosity magnitude or distribution

x: 
$$-fV_{EK} = A_V \partial u / \partial z = \tau^{(x)} / \rho$$

y: 
$$fU_{EK} = A_V \partial v / \partial z = \tau^{(y)} / \rho$$

90°W

120°W

### Ekman balance: observed response to wind stress

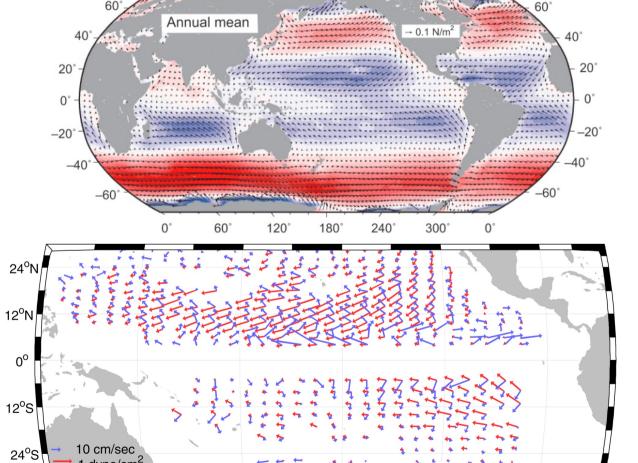
120°

(a)

120°E

150°E

180°W



150°W

Annual mean wind stress (NCEP)
Color is zonal stress

Mean currents at 15 m (blue) plotted with mean wind stress (red) (Ralph and Niiler, 1999)