



**The Abdus Salam
International Centre for Theoretical Physics**



2210-5

**MedCLIVAR Workshop on: "Scenarios of Mediterranean Climate
Change under Increased Radiative Active Gas Concentration and the
Role of Aerosols**

23 - 25 September 2010

**Applying Analysis of Variance on a Multi-Model Ensemble of Global Climate Models
in the Mediterranean Area**

VOGT Gernot
*University of Wuerzburg
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Applying Anova on a multi-model ensemble of GCMs in the Med-Area

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University of Wuerzburg, Germany

5th ESF-MedCLIVAR Workshop 23.09.2010, Trieste

Global model simulations (GCMs) from CMIP3

- WCRP CMIP3 Multi-Model Dataset Archive at PCMDI
- ~24 GCMs
- GHG-Emission-Scenarios: A1b, A2, B1 (former times: 20c3m)
- Spatial resolution (Long: 5-1.13°/Lat: 4-1.13°)
- Earliest and latest simulated year:
1850/2349 i.e. miroc3 med run1/ ccs3 run7

Method

- Variables: Precipitation, Temperature, Sea-level pressure
- Processing Steps:

Spatial
Interpolation

Correct time
and space output

Preprocessing

Spatial resolution on $3 \times 3^\circ$

Total time slice from 1901-2098 (special focus on 1901-2098, 1961-2000, 1961-2050, 2001-2098)

Mediterranean Area: $21^\circ\text{W} - 45^\circ\text{E} / 24^\circ\text{S} - 45^\circ\text{N}$

Available Models and Runs

Scenario→ ↓Model	A1B	A2	B1
bccr:bcm2.0	1	1	1
cnrm:cm3	1	1	1
gfdl:cm2.0	1	1	1
gfdl:cm2.1	1	1	1
giss:aom	2	0	2
iap:fgoals1.0g	3	0	3
ipsl:cm4	1	1	1
ingv:echam4	1	1	0
miroc3.2 hires	1	0	1
miroc3.2 medres	3	3	3
mri:cgcm2.3.2a	5	5	5
csiro:mk3.0	1	1	1
csiro:mk5.0	1	1	1
mpi:echam5	4	3	3
ncar:ccsm3	7	5	8
ncar:pcm1	4	4	2
ukmo:hadcm3	1	1	1
ukmo:hadgem3	1	1	0

Method

- All data is based on monthly means
- Calculation of yearly values (JFMAMJJASOND = yea) ...and
- Calculation of seasonal values (DJF = win; MAM = spr; JJA = sum; SON = aut)
- Processing Steps:

Interpolation on
3x3°

Correct time
and space outcut

Preprocessing

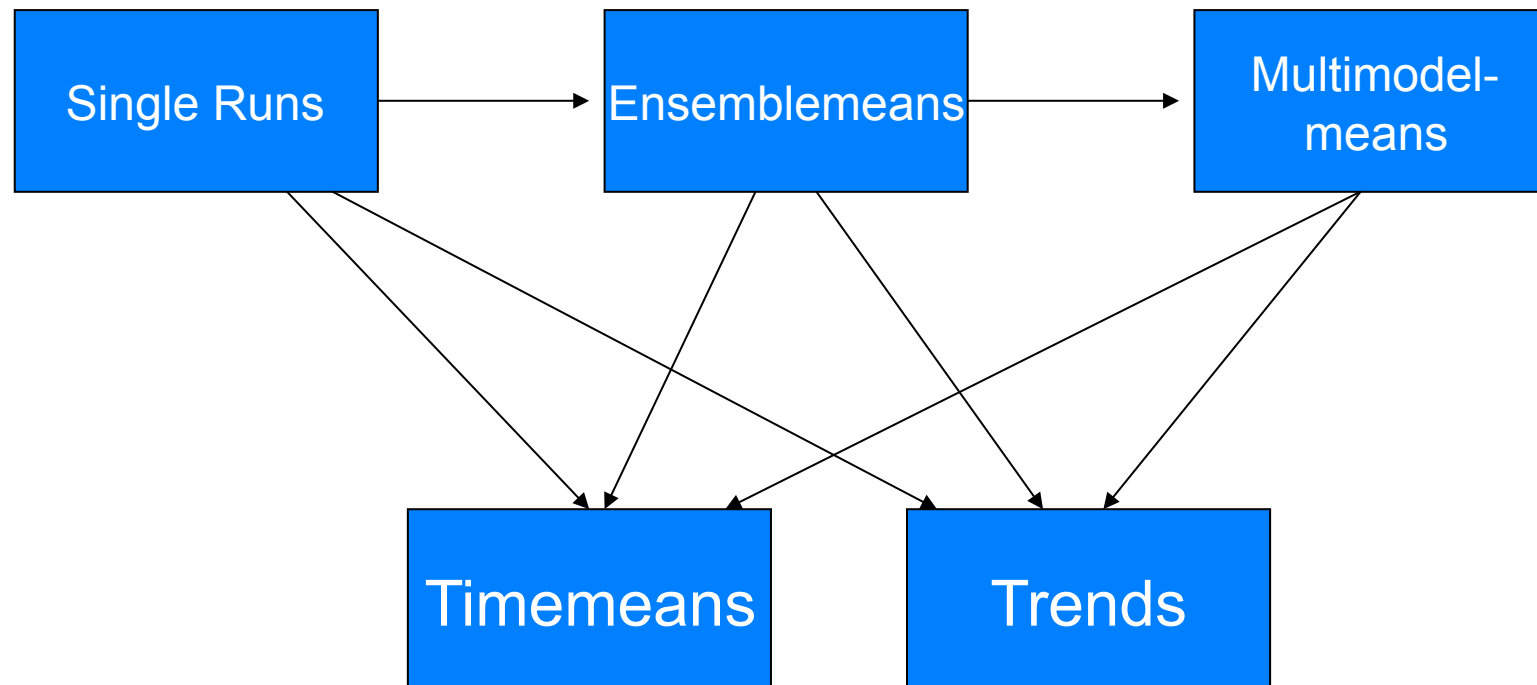
Analysis of tem-
poral
means

Trends

Analysis

Szenarios: A1B, A2, B1

- Processing over time



Precipitation, Temperature, Pressure,...

Method

- All data is based on monthly means
- Calculation of yearly values (JFMAMJJASOND = yea) ...and
- Calculation of seasonal values (DJF = win; MAM = spr; JJA = sum; SON = aut)
- Processing Steps:

Interpolation on
3x3°

Correct time
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Analysis of tem-
poral
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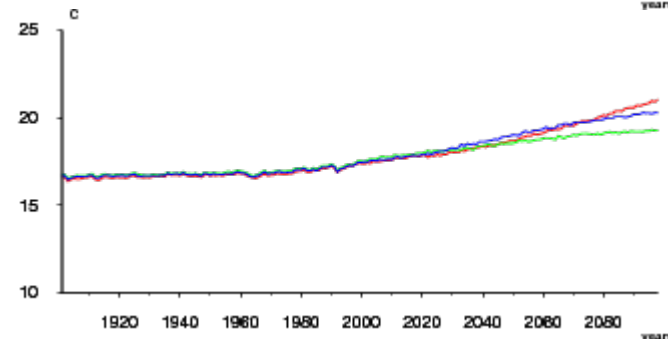
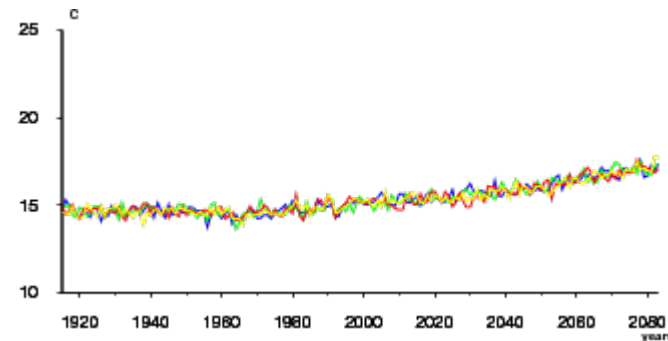
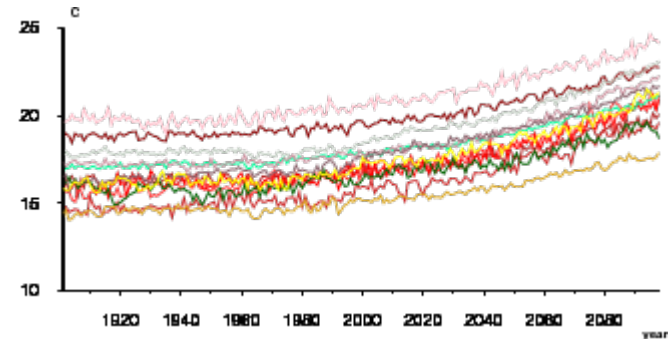
Trends

Analysis

1-way-anova

2-way-anova

- Climate Model (t2m, A2)
- Single Run (t2m, A2)
- Scenario (t2m)



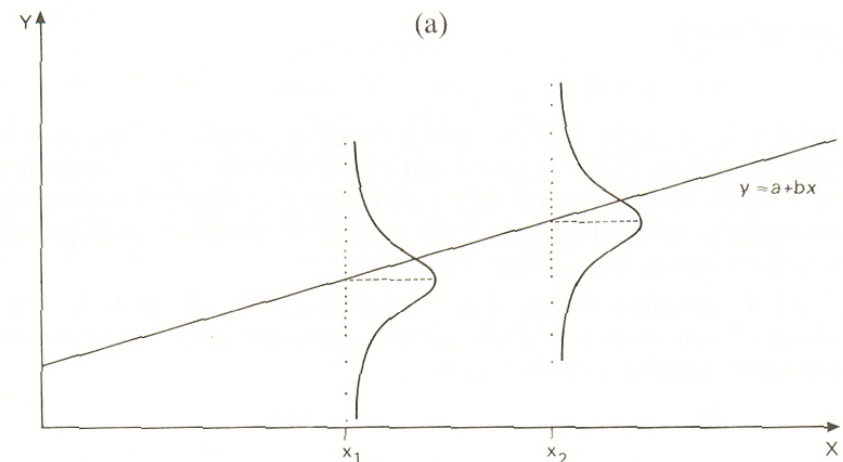
-Some kind of regression analysis.

-But the dependent variable is metric and the independent variable is in a nominal or ordinal scale

$$Y = \alpha + \beta X + \varepsilon$$

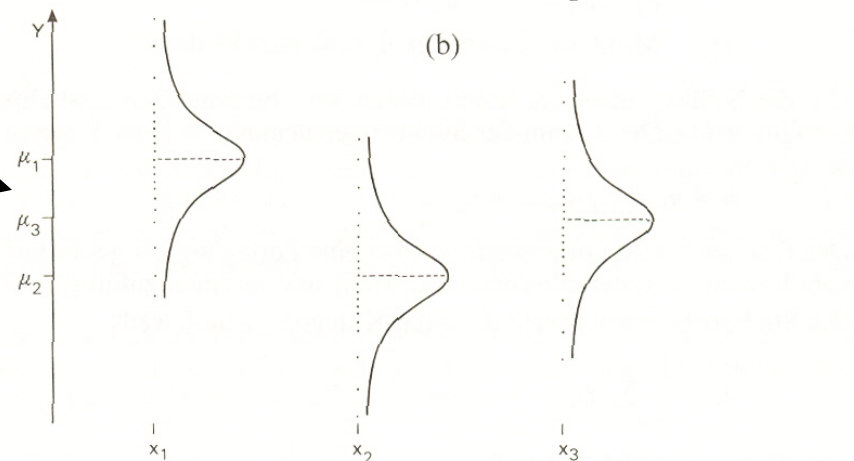
(Bahrenberg et al. 2008)

Regression analysis



Analysis of variance

-A linear dependence cannot be determined. Though it is possible to detect significant influences of variable X on variable Y



1)

$$\delta_i = \mu_i - \mu$$

$i=1 \dots n$ runs

2)

$$\varepsilon_{ji} = y_{ji} - \mu_i$$

$j=1 \dots m$ time units

So within the time i of the model j the observed value can be described with a simple linear ansatz.

$$y_{ji} = \mu + \delta_i + \varepsilon_{ji}$$

To prove whether the different mean values have significant influence on the total mean, the total amount of variation (sum of square errors or total variance) is calculated and divided into a known and an unknown part of variance

With using the sum of square errors the Anova is finally based on the decomposition of the total variance into its different partitions dedicated to a common signal and ist noise

$$\sum_{i=1}^q \sum_{j=1}^{n_i} (y_{ij} - \bar{Y})^2 = \sum_{i=1}^q \sum_{j=1}^{n_i} ((y_{ij} - \bar{Y}_i) + (\bar{Y}_i - \bar{Y}))^2$$

i=1...n runs

j=1...m time units

$$= \sum_{i=1}^q \sum_{j=1}^{n_i} ((y_{ij} - \bar{Y}_i)^2 + \sum_{i=1}^q \sum_{j=1}^{n_i} (\bar{Y}_i - \bar{Y})^2 + 2 \sum_{i=1}^q \sum_{j=1}^{n_i} (y_{ij} - \bar{Y}_i) + (\bar{Y}_i - \bar{Y}))$$

$$2 \sum_{i=1}^q \sum_{j=1}^{n_i} (y_{ij} - \bar{Y}_i) + (\bar{Y}_i - \bar{Y}) = 2 \sum_{i=1}^q ((\bar{Y}_i - \bar{Y}) \underbrace{\sum_{j=1}^{n_i} (y_{ij} - \bar{Y}_i)}_0) = 0$$

Differences between the runs = epsilon

$$\sum_{i=1}^q \sum_{j=1}^{n_i} (y_{ij} - \bar{Y})^2 = \sum_{i=1}^q \sum_{j=1}^{n_i} ((y_{ij} - \bar{Y}_i)^2 + \sum_{i=1}^q \sum_{j=1}^{n_i} (\bar{Y}_i - \bar{Y})^2$$

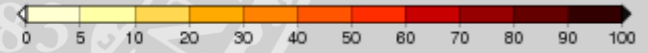
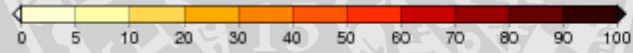
Sum of square errors

Differences in time =
beta

1-Way-Anova

- A measure of the uncertainty of a model
- Relation between single runs and the ensemble mean
- Divided in unknown variability (residuals = ϵ) and known variability (common treatment of all runs = β)

1-way-Anova A2 t2m ECHAM5 2001-2098_{epsilon}



Year

beta

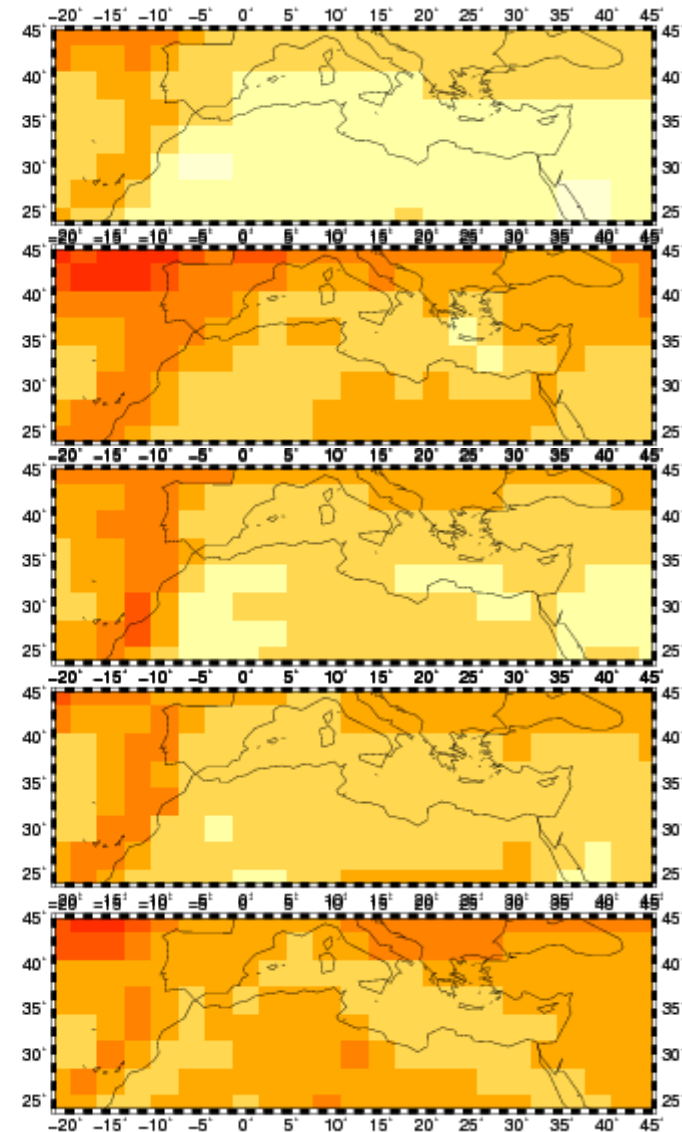
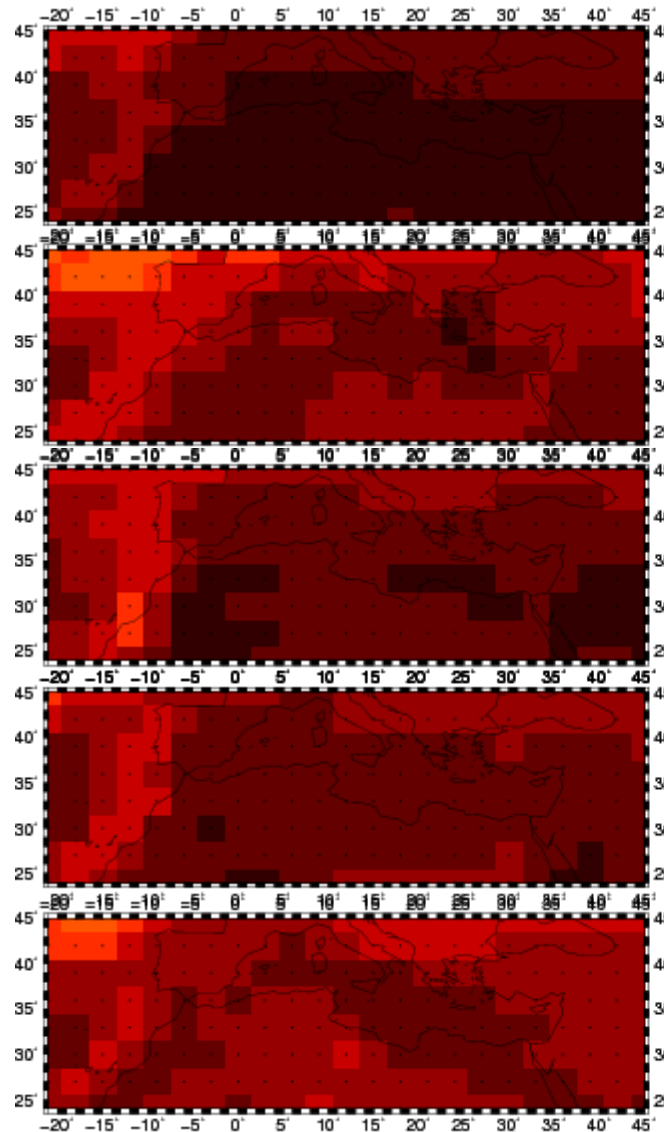


Spring

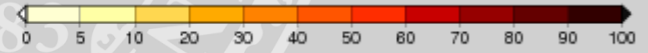
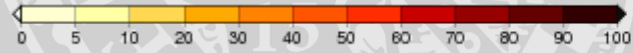
Summer

Autumn

Winter



1-way-Anova B1 t2m ECHAM5 2001-20098_{epsilon} ↓



Year ↓

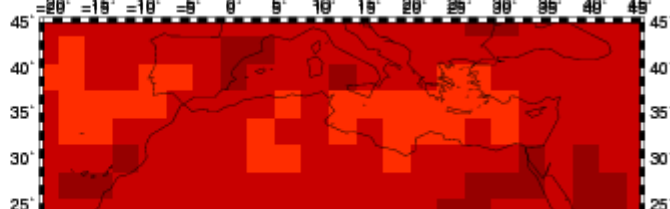
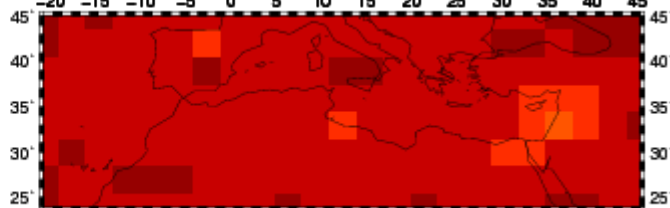
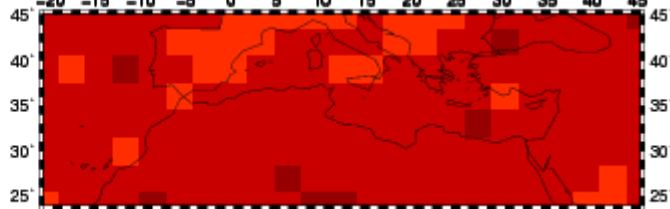
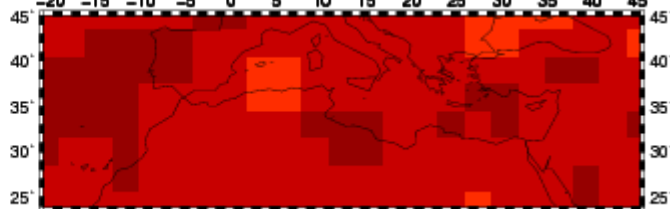
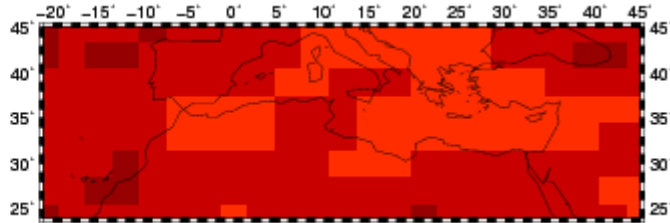
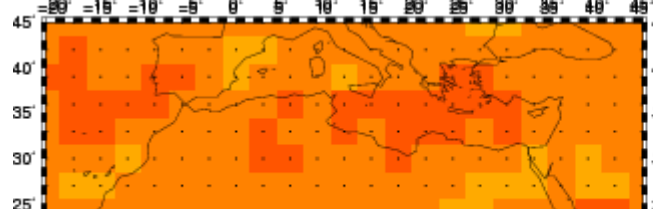
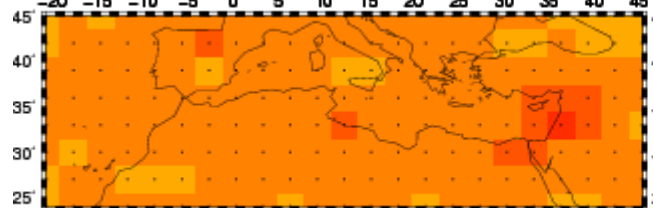
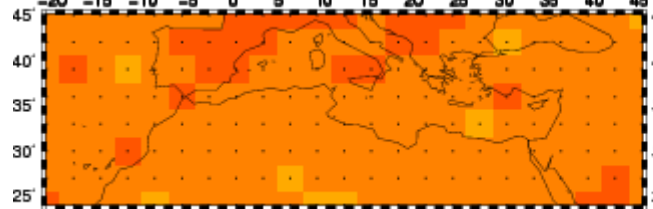
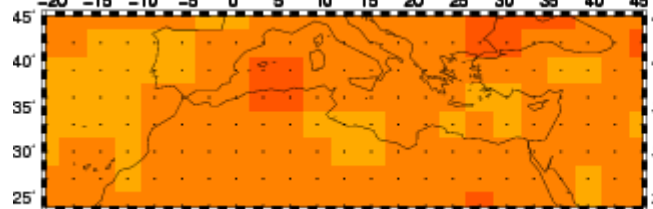
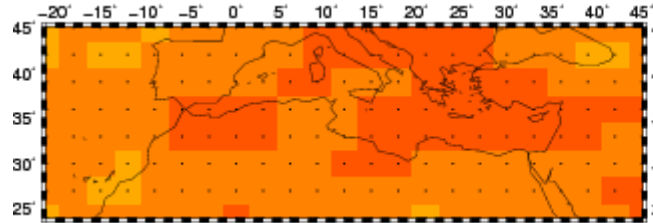
beta ↓

Spring

Summer

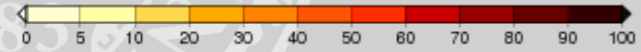
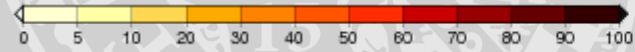
Autumn

Winter



1-way-Anova 20c3m t2m ECHAM5 1961-2000

epsilon ↓



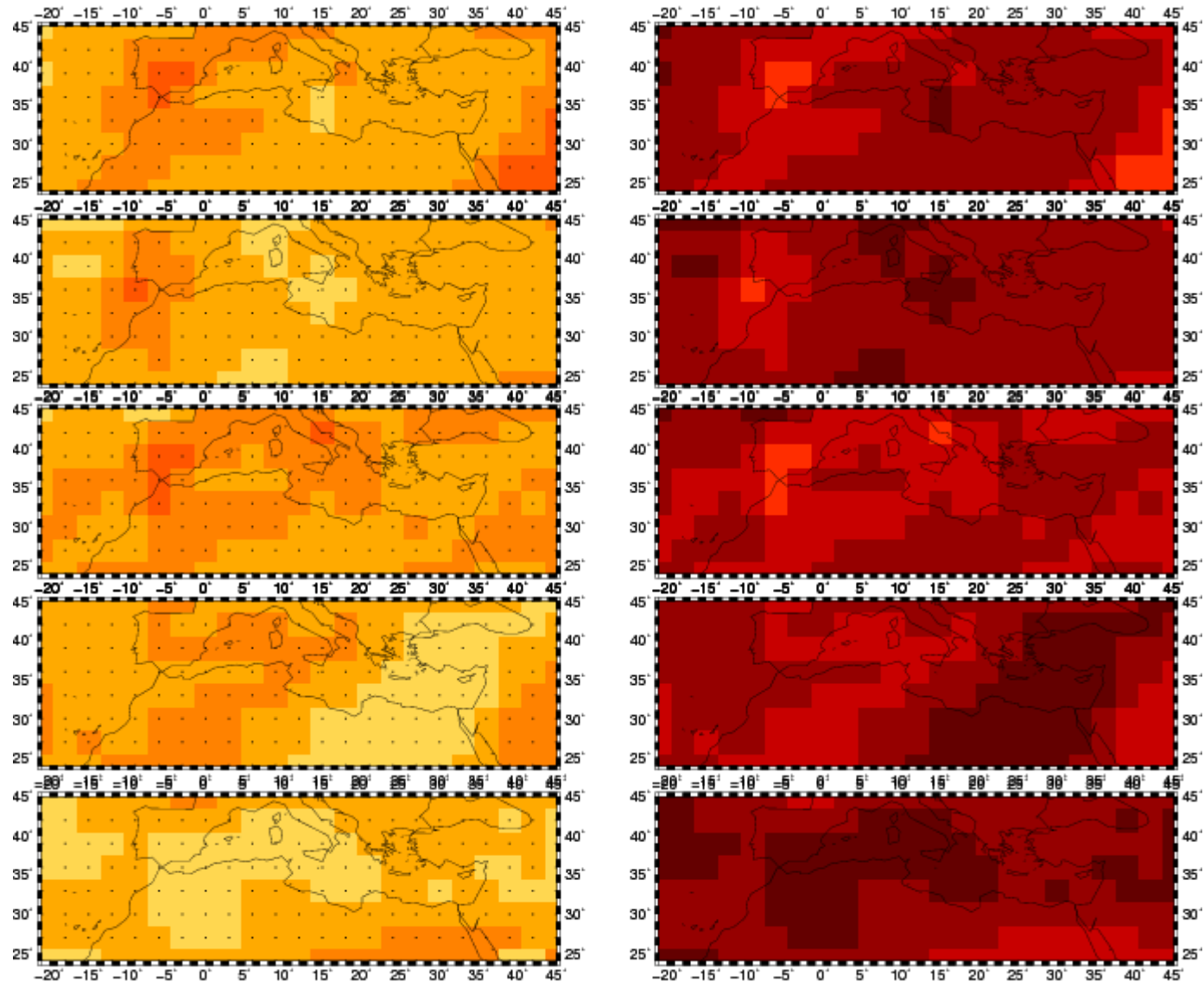
Year
beta ↓

Spring

Summer

Autumn

Winter



1-way-Anova A2 pre ECHAM5 2001-20098 epsilon ↓

Year

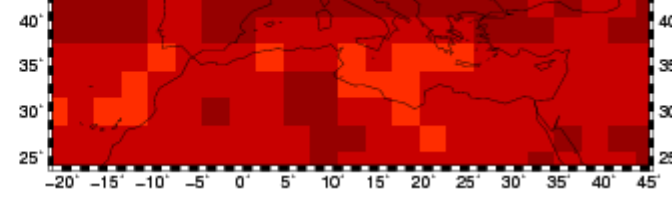
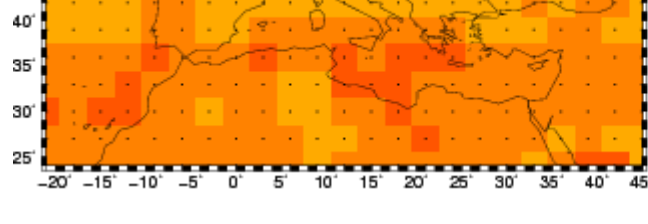
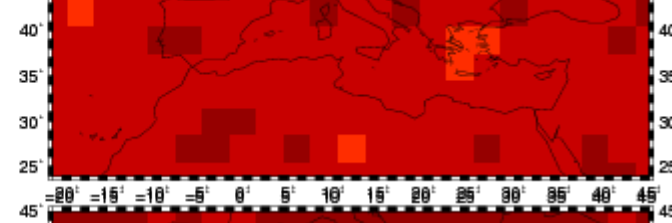
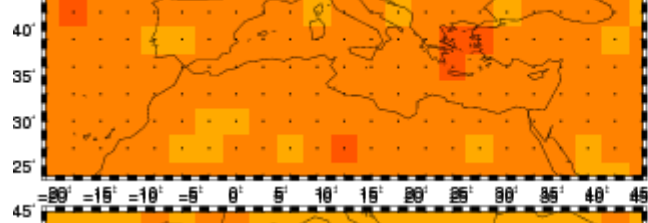
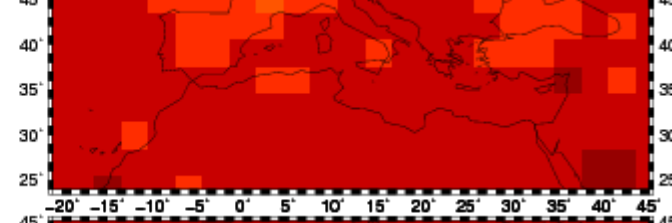
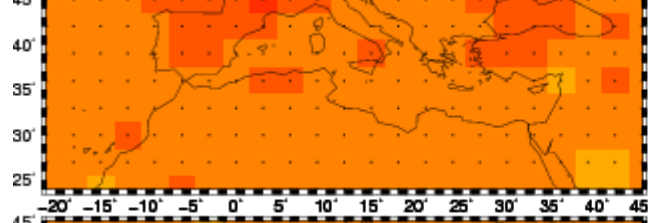
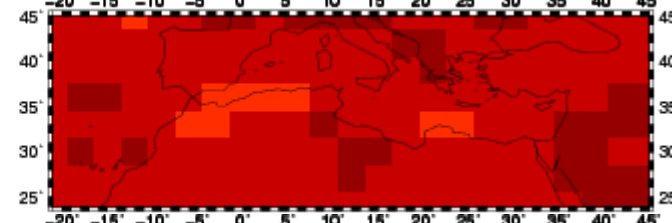
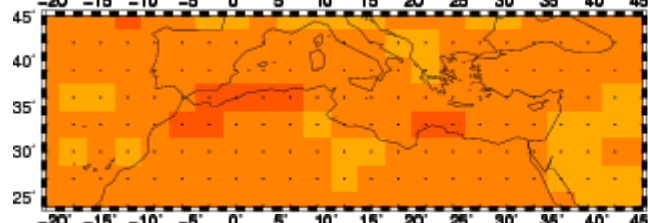
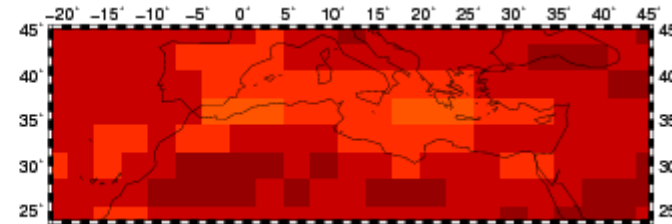
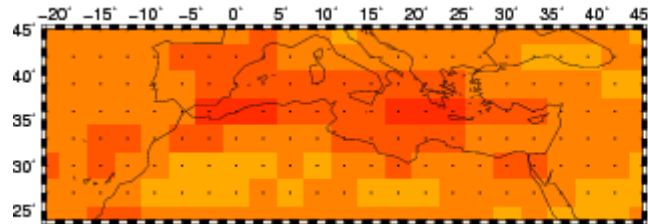
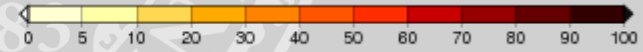
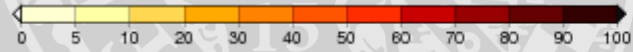
beta ↓

Spring

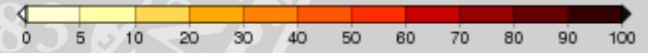
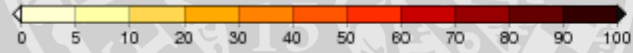
Summer

Autumn

Winter



1-way-Anova A2 slp ECHAM5 2001-2098 epsilon ↓



Year

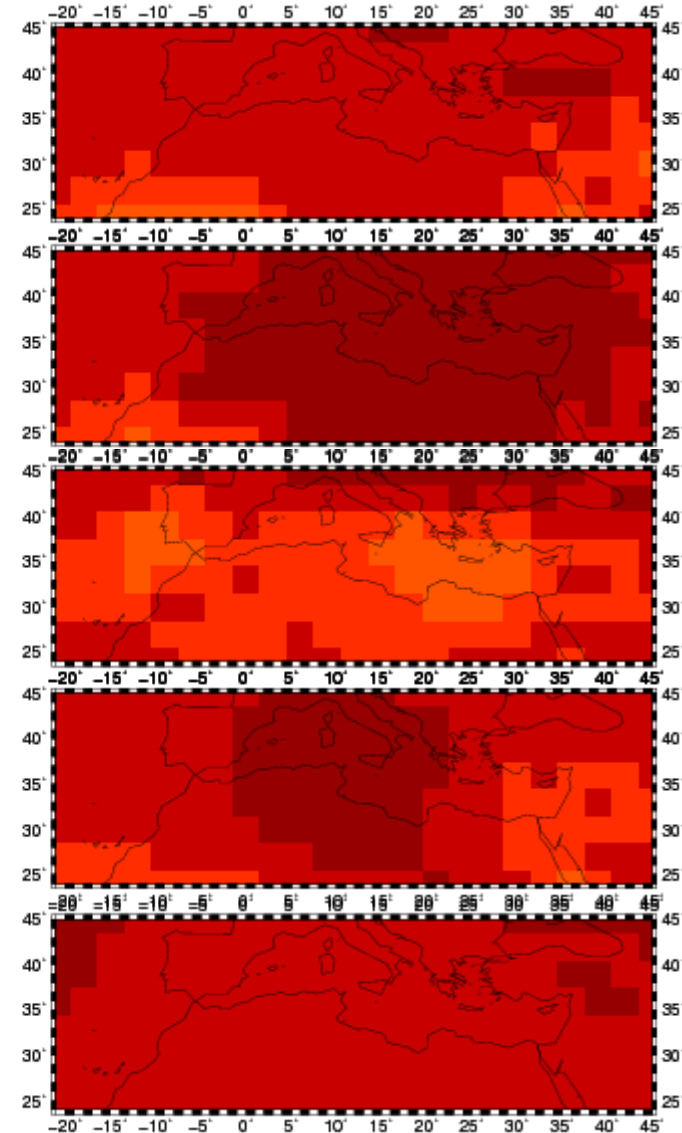
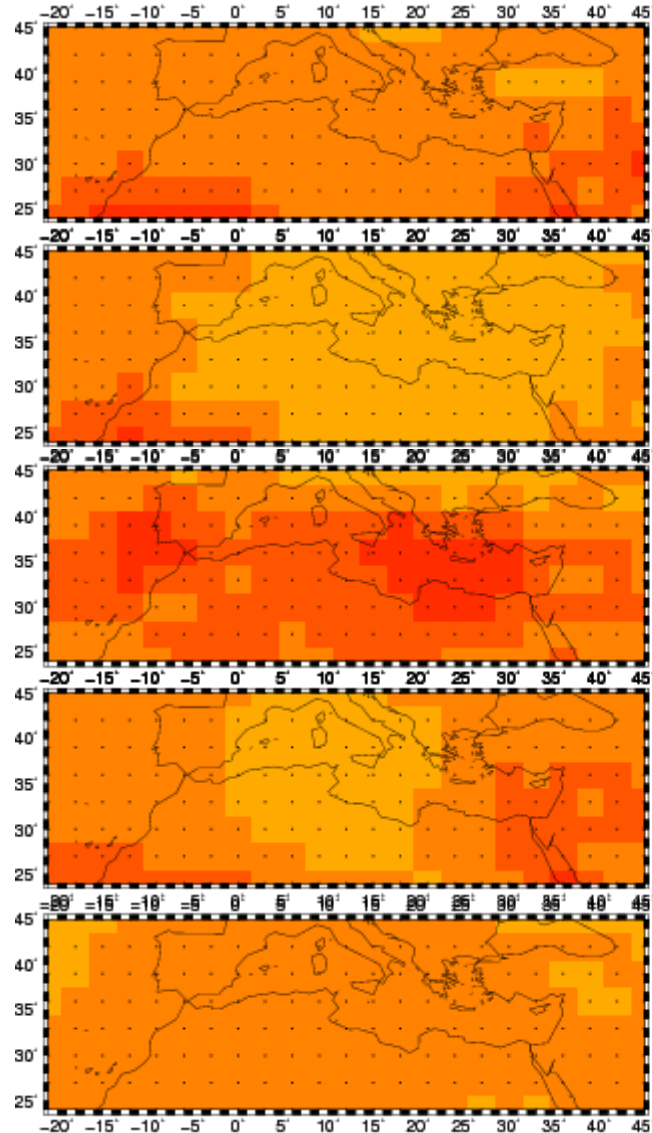
beta ↓

Spring

Summer

Autumn

Winter



- 30year time window is used to create means
- This time slice is shifted over the whole time-period from 1901-2098

➡ new timeslice from 1915-2083

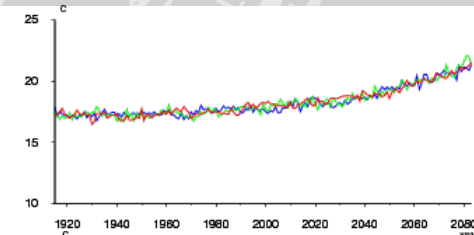
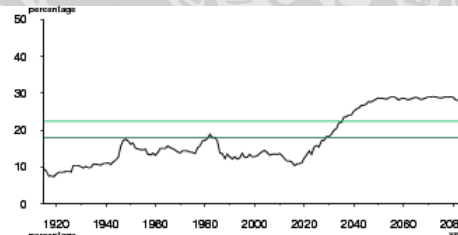
- Anova is calculated for each year in this sliding window, where the 30yr mean value is projected to the mid-year of this period

➡ Temporal evolution of the Anova...

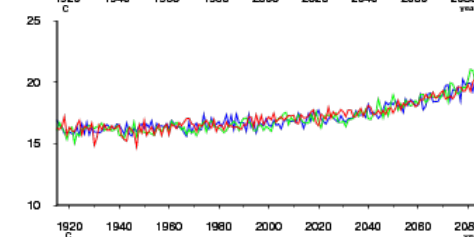
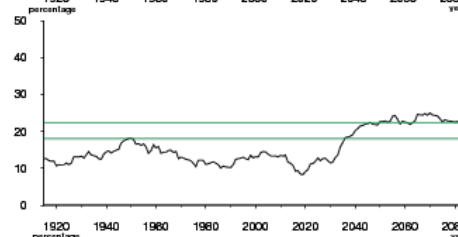
Temporal Approach 1-Anova

ECHAM5 A2 t2m 1915-2083

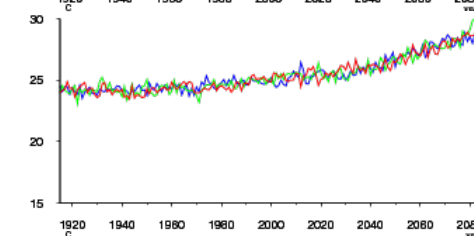
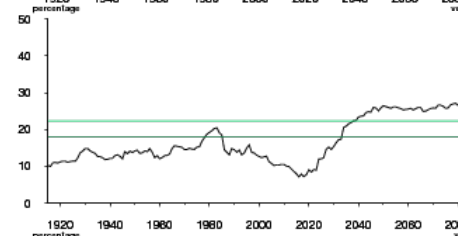
Year



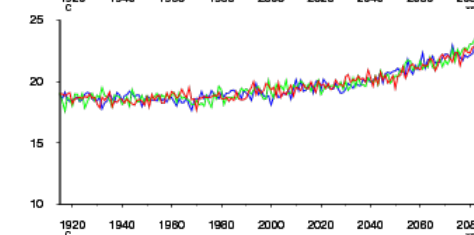
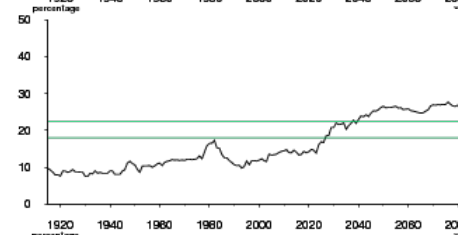
Spring



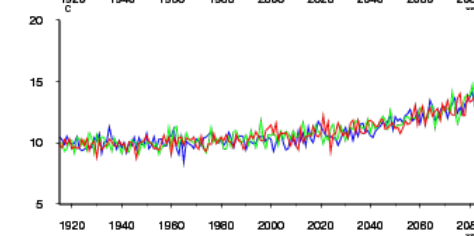
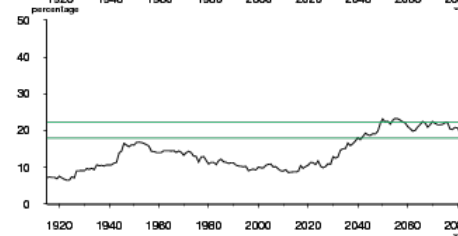
Summer



Autumn



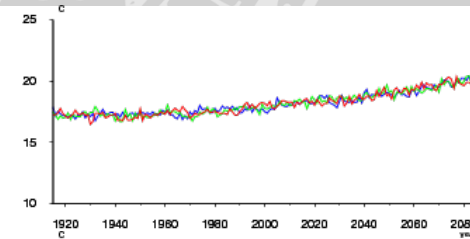
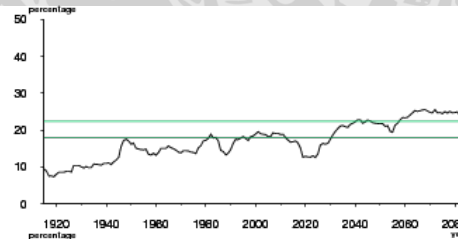
Winter



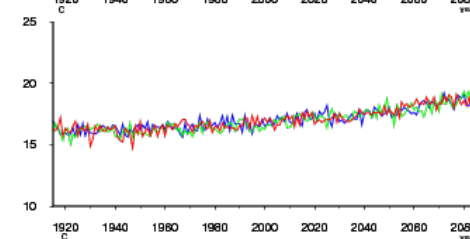
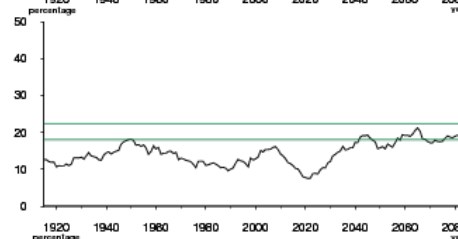
Temporal Approach 1-Anova

ECHAM5 B1 t2m 1915-2083

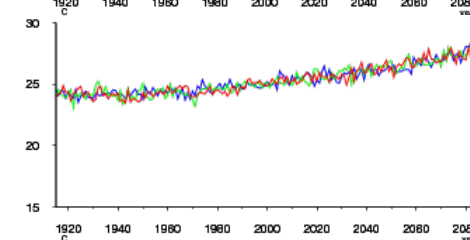
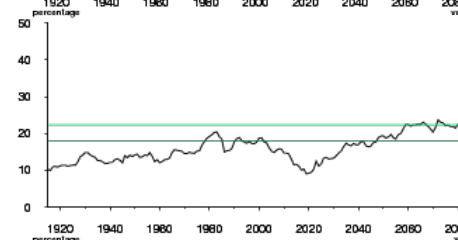
Year



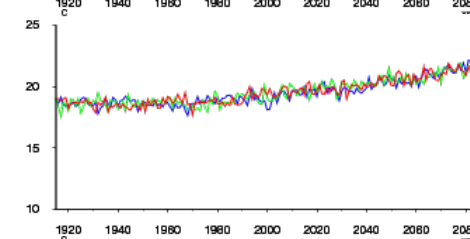
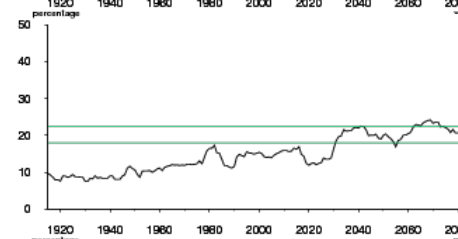
Spring



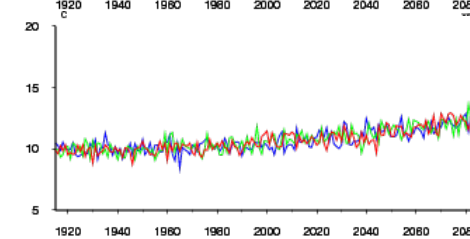
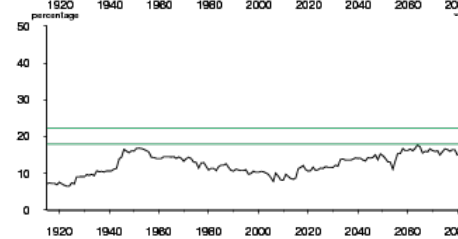
Summer



Autumn



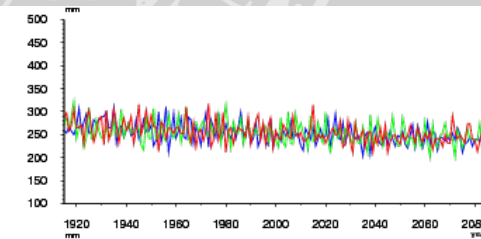
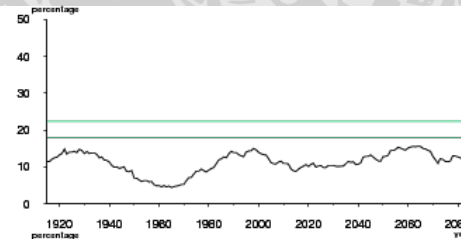
Winter



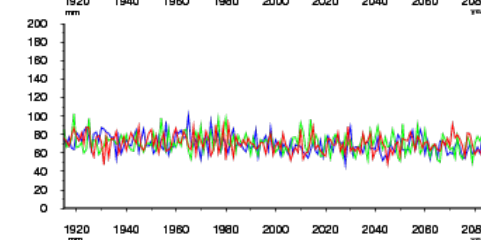
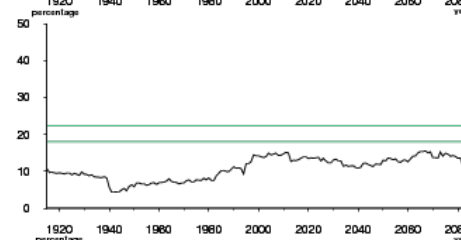
Temporal Approach 1-Anova

FGOALS 1 B1 pre 1915-2083

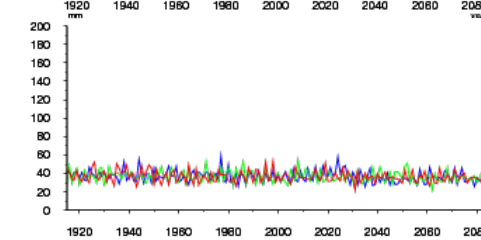
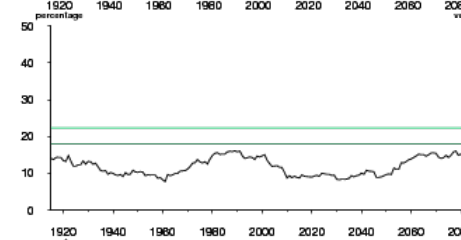
Year



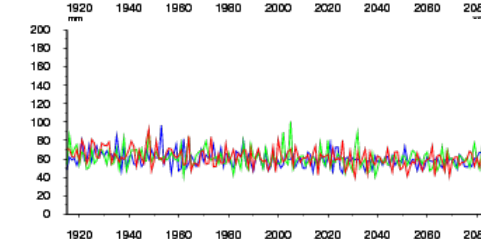
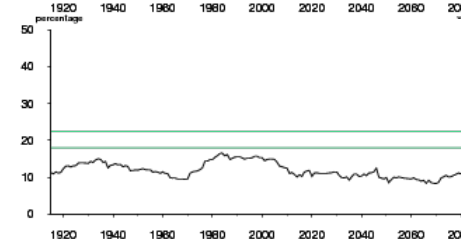
Spring



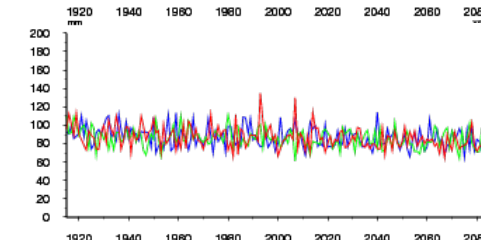
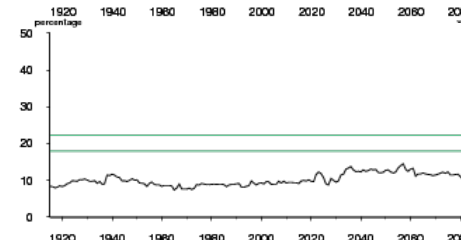
Summer



Autumn



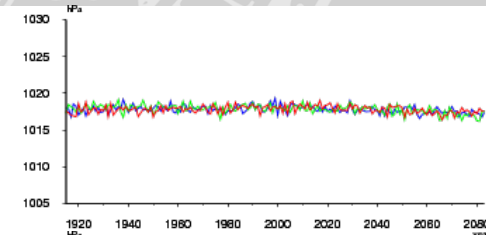
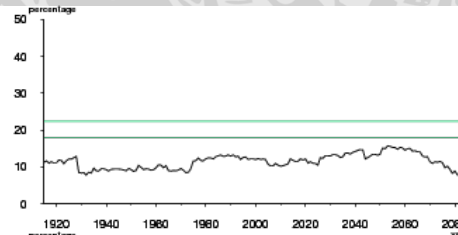
Winter



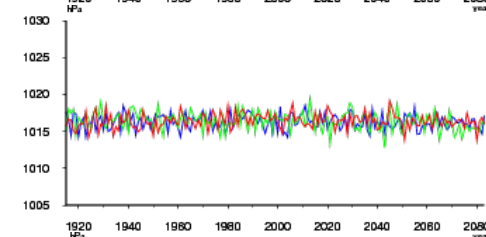
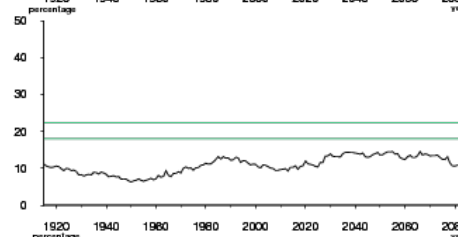
Temporal Approach 1-Anova

FGOALS 1 A1B slp 1915-2083

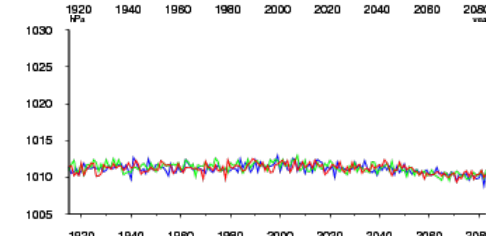
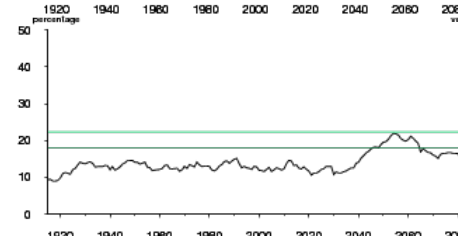
Year



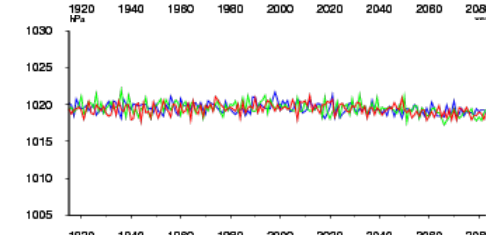
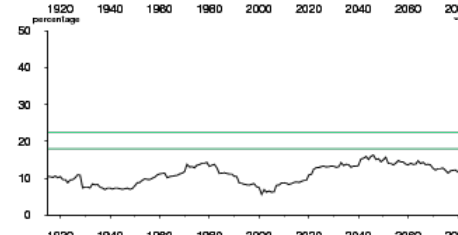
Spring



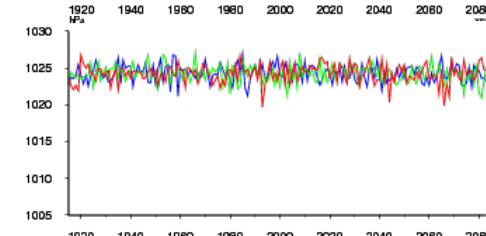
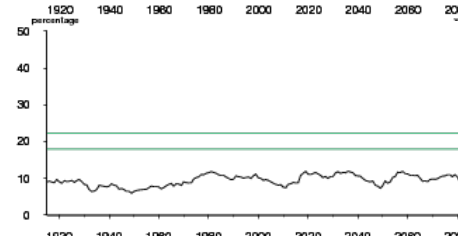
Summer



Autumn



Winter

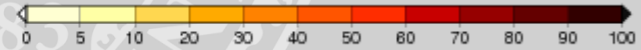
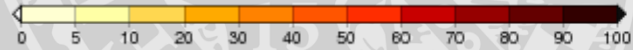


2-Way-Anova

- A measure of the uncertainty of a several climate models
- Relation between single runs and the ensemble mean and the multimodel mean
- Divided in
 - common model uncertainty/failing (α)
 - common treatment effect/influence of the scenario (β)
 - influence of different forcings which is time dependant (γ)
 - internal model variability (ϵ)

....in percentage

2-way-Anova A2 t2m 2001-2008 beta



Year

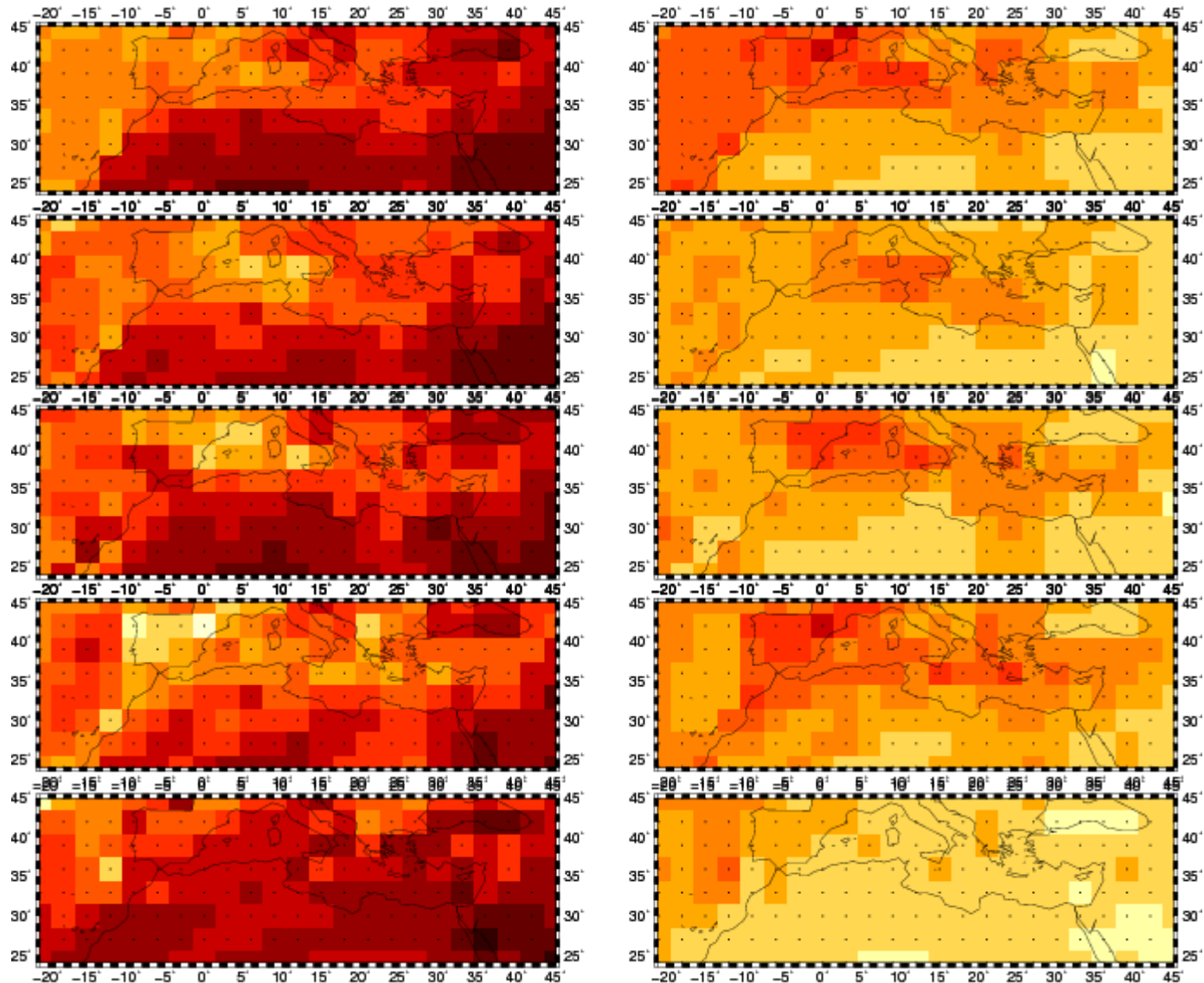
alpha ↓

Spring

Summer

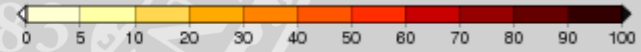
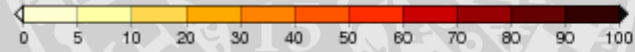
Autumn

Winter



2-way-Anova A2 t2m 2001-2008

epsilon ↓



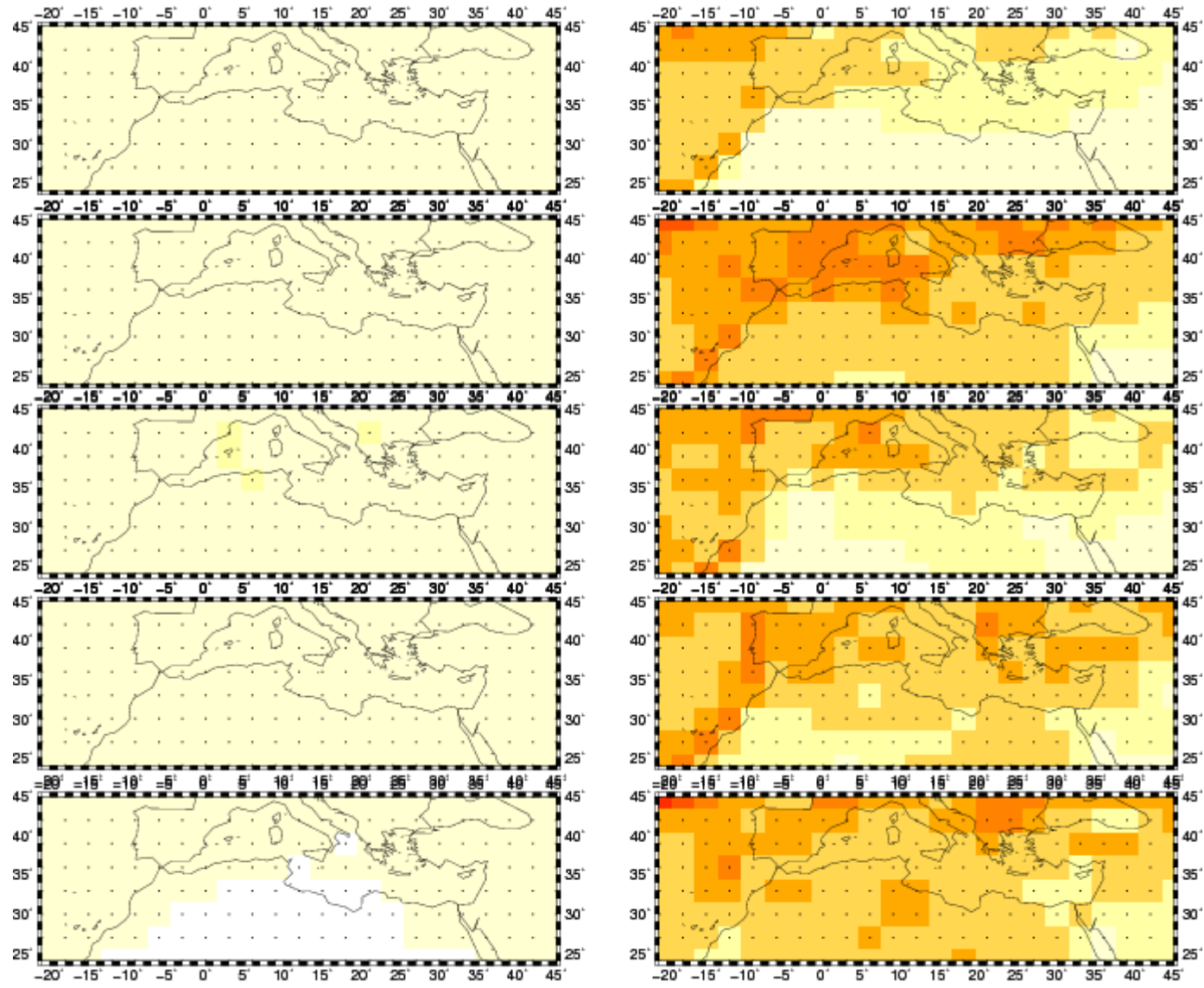
Year gamma ↓

Spring

Summer

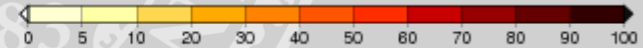
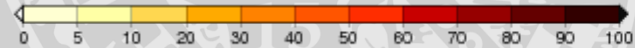
Autumn

Winter



2-way-Anova A2 pre 2001-20098

beta ↓



Year

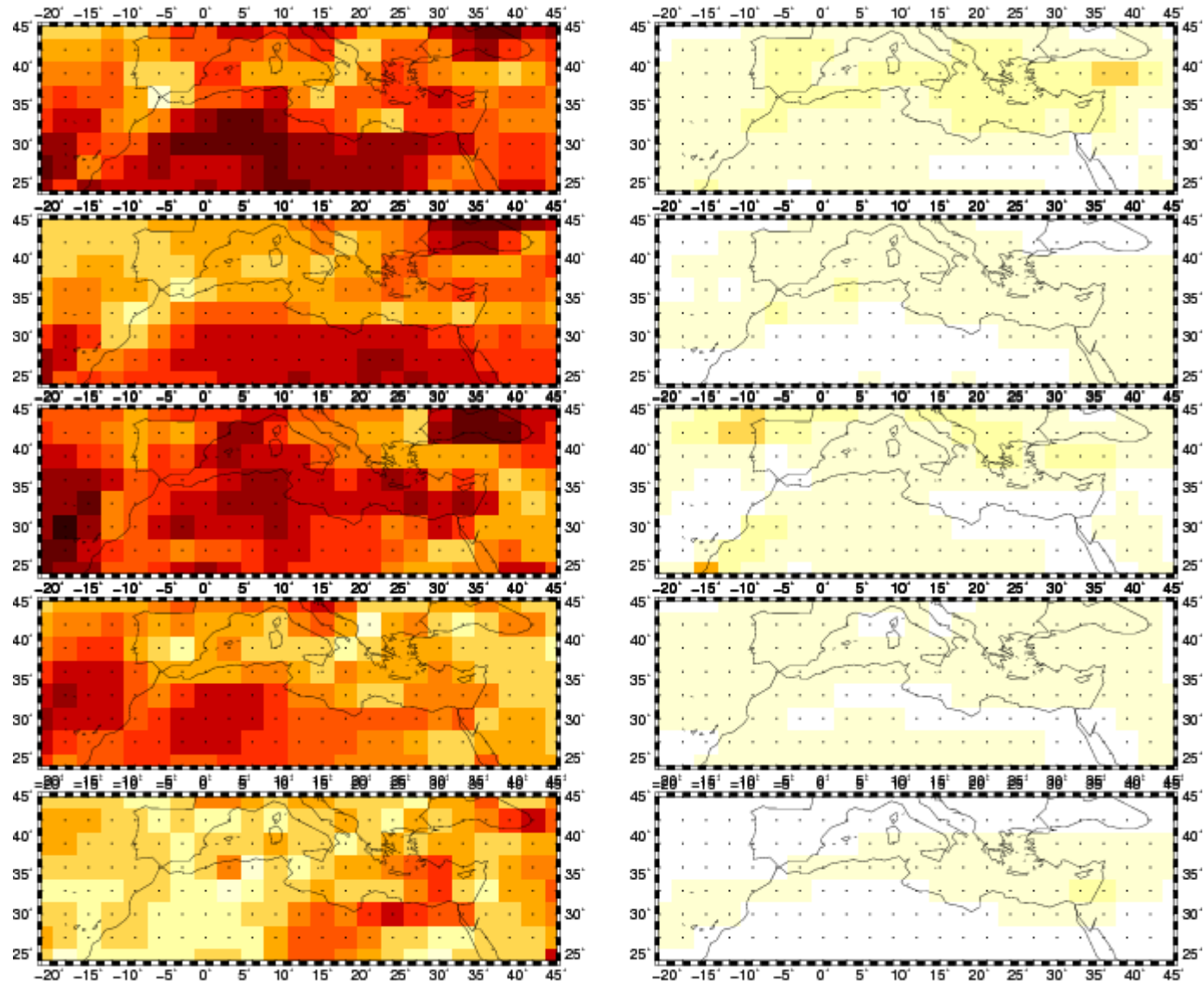
alpha ↓

Spring

Summer

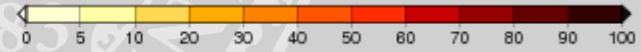
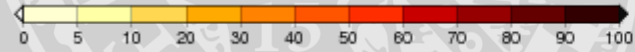
Autumn

Winter



2-way-Anova A2 pre 2001-20098

epsilon ↓



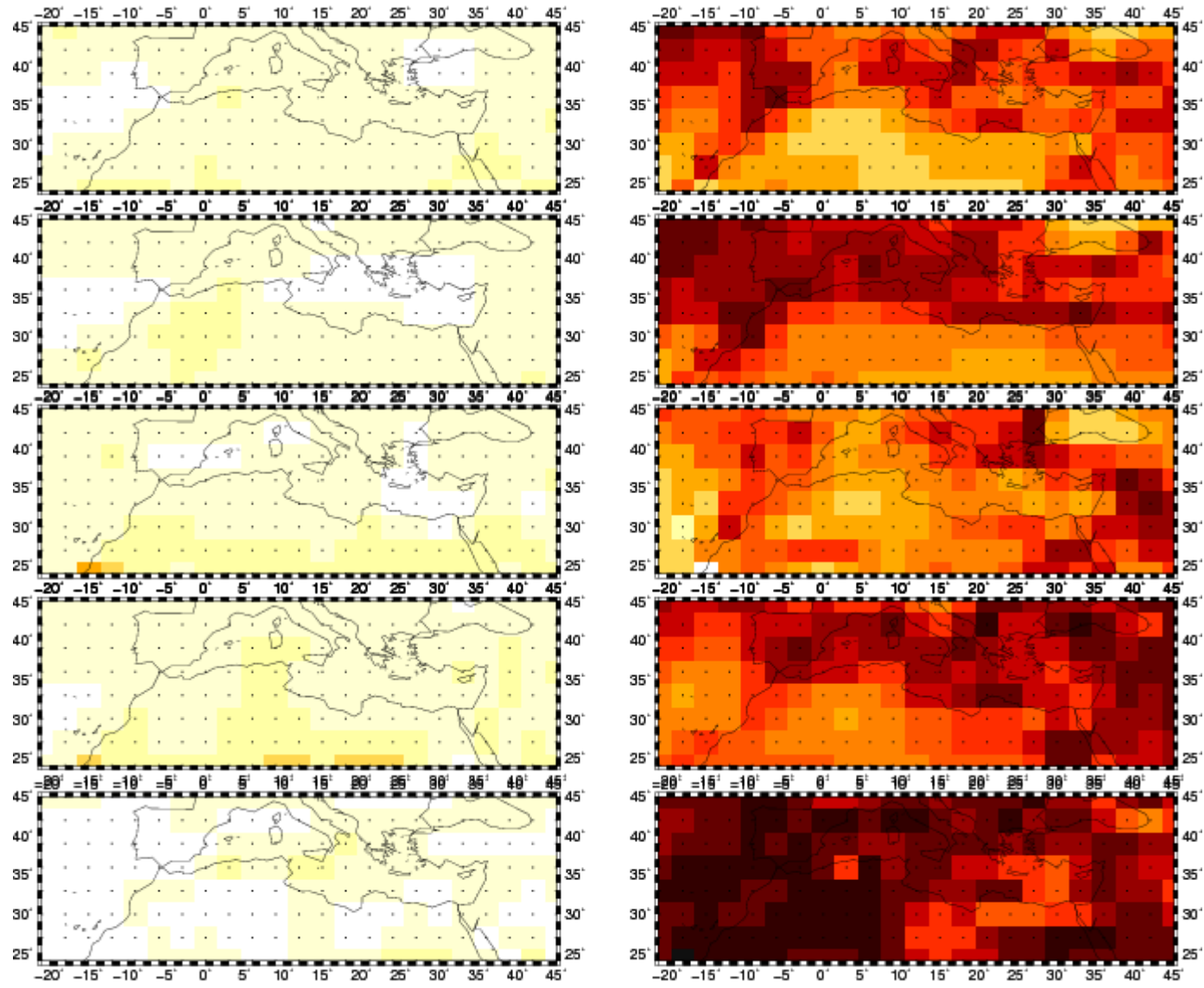
Year
gamma ↓

Spring

Summer

Autumn

Winter

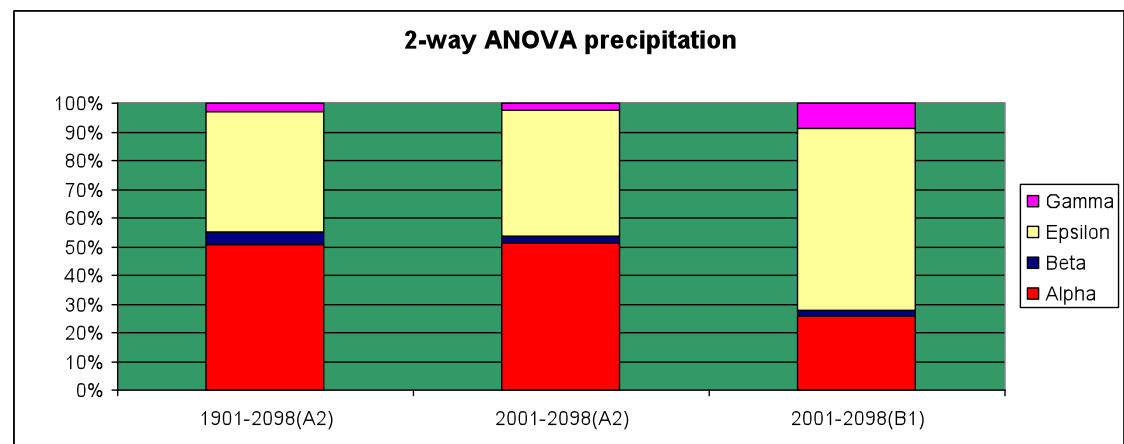
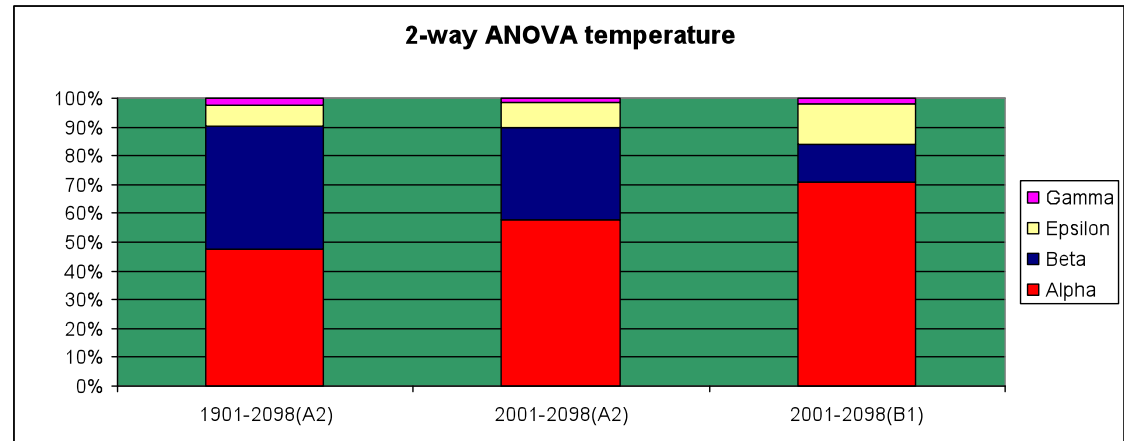


Regional means of the 2-way Anova

-temperature shows a higher common signal than precipitation

-the longer the time slice, the higher is beta

-the common signal seems to be stronger for A2 than for B1



Summary

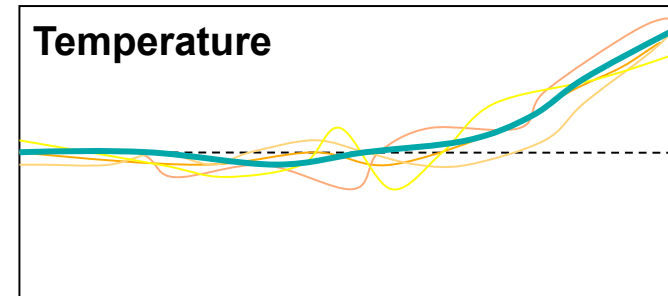
- The relative importance of GCMs and runs depends strongly on
 - the chosen time slice
 - the region
 - the climate variable
 - the season
 - the scenario
 - →The higher the variability over -maybe GCMs- the more the choice -of the “best” GCMs- matters
- Weighting of models?
 - Future Research: 1) sorting out erroneous data of slp
 - 2) investigation of temporal evolution of the 2-Anova
 - 3) investigation of extremes with daily GCM-data
 - 4) Analysis of Variance with Extremes...?

Thank you for your
attention!!!

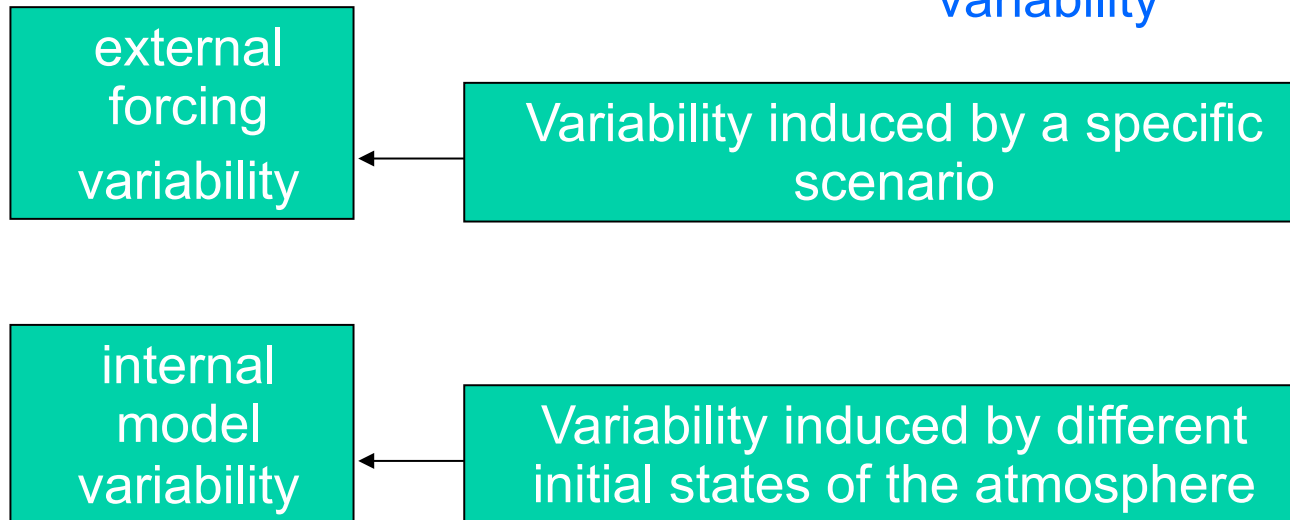


- Signal-to-noise ratio

$$= \frac{\textit{External Variability}}{\textit{Internal Variability}}$$

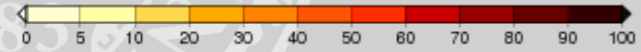
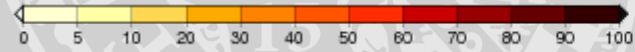


With respect to
inter-model
variability



2-way-Anova B1 t2m 2001-2008

beta ↓



Year

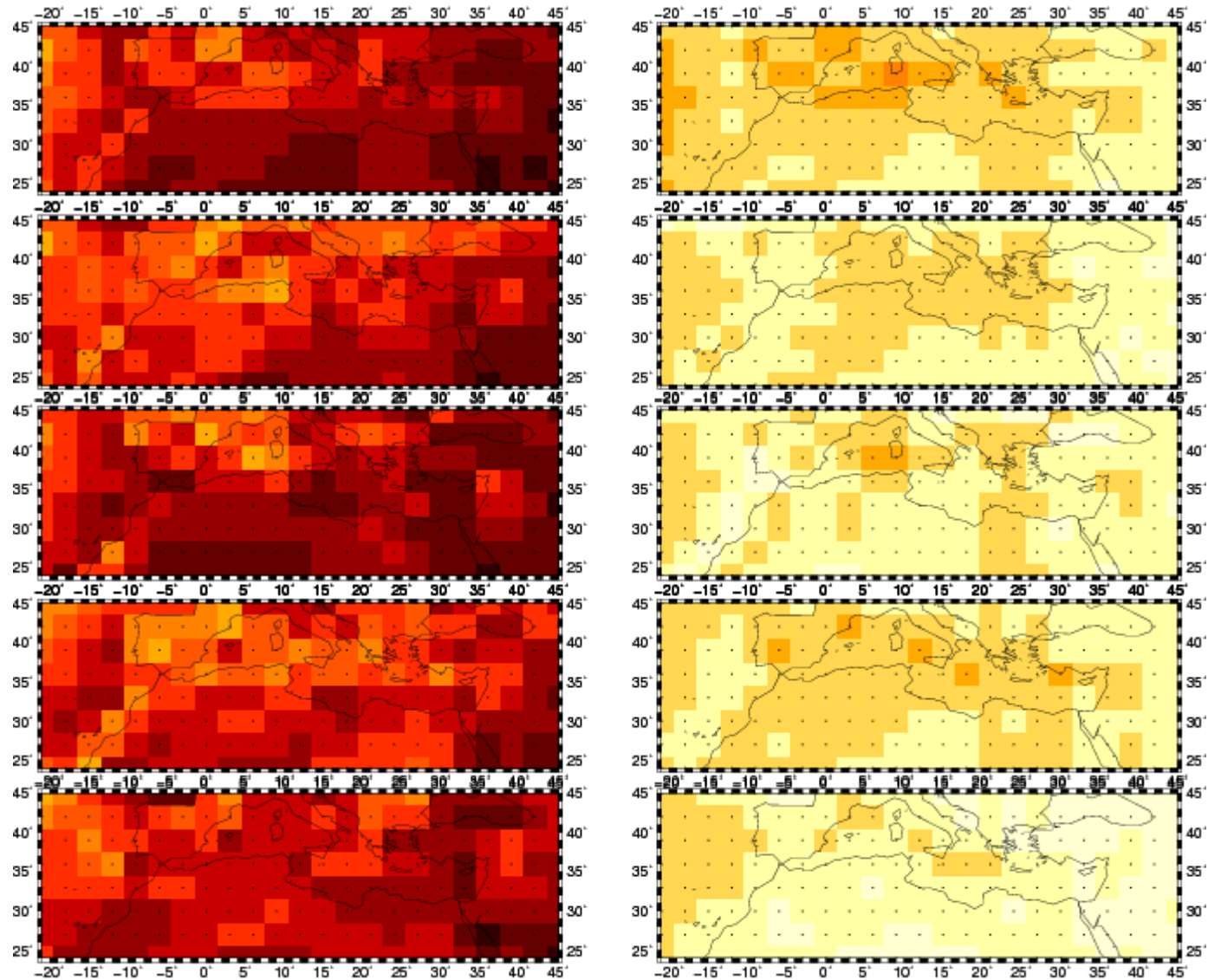
alpha ↓

Spring

Summer

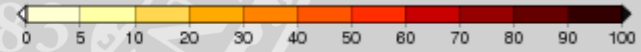
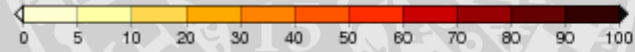
Autumn

Winter



2-way-Anova B1 t2m 2001-2008

epsilon ↓



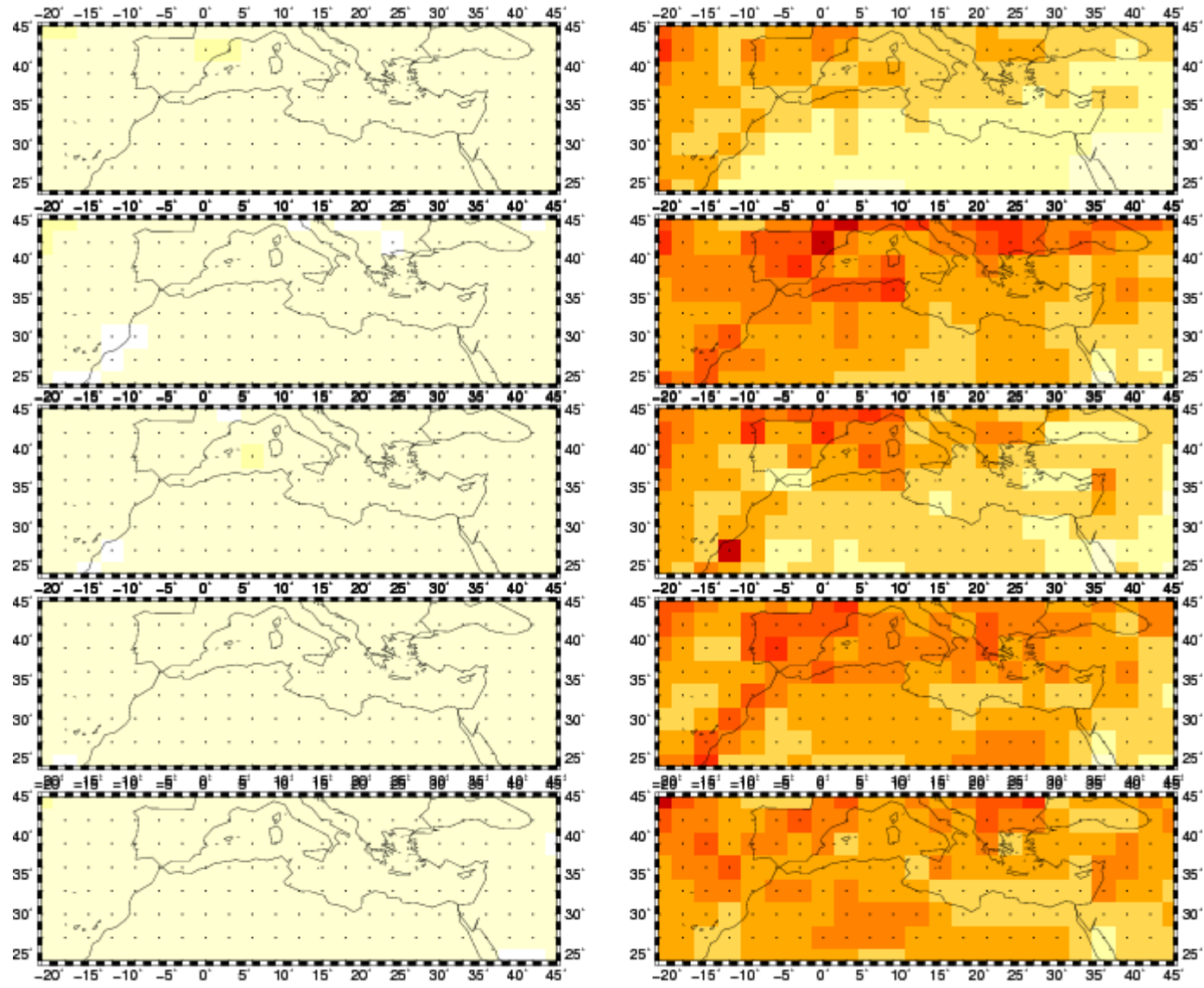
Year gamma ↓

Spring

Summer

Autumn

Winter

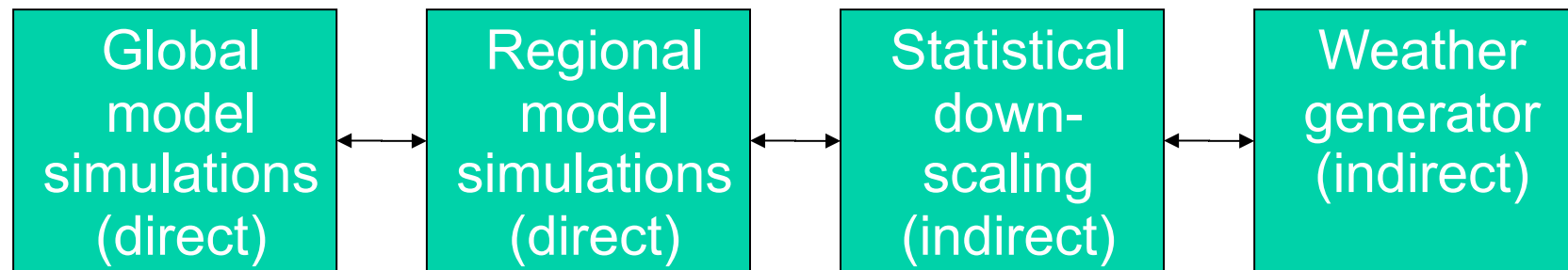


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Project overview

- Main goal:
Detection of climate change and extreme events in the Mediterranean basin and probabilistic quantification of uncertainties
- Broad spectrum of different methods:



- Comparison of different scenarios and models
→ evaluation with observations

- Processing over time

