



**The Abdus Salam  
International Centre for Theoretical Physics**



**2328-26**

**Preparatory School to the Winter College on Optics and the Winter College on  
Optics: Advances in Nano-Optics and Plasmonics**

*30 January - 17 February, 2012*

**Metamaterials current trends**

N. Zheludev  
*University of Southampton  
Southampton  
U.K.*

# Metamaterials

Nikolay Zheludev

*Optoelectronics Research Centre  
Centre for Photonic Metamaterials  
University of Southampton, UK*

[www.nanophotonics.org.uk](http://www.nanophotonics.org.uk)

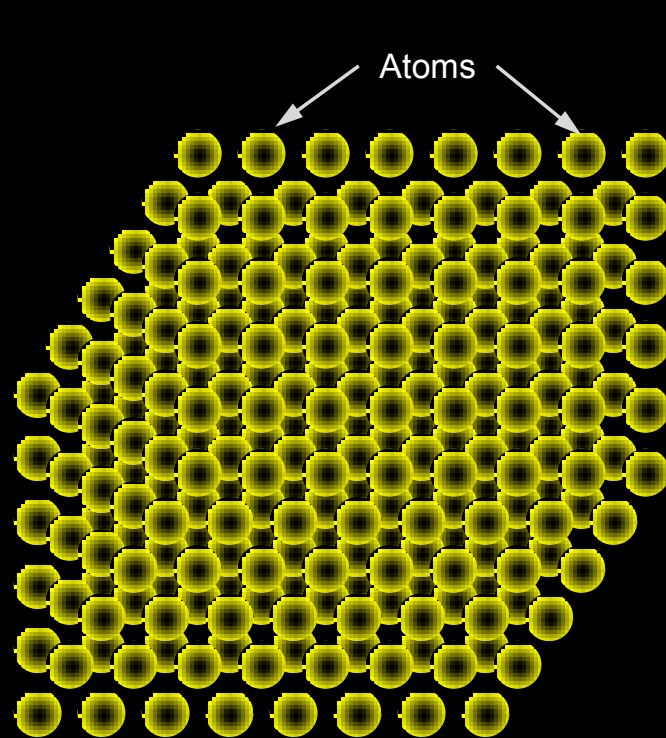
Winter College on Optics: Advances in Nano-Optics and Plasmonics  
Triest, Italy 6-17 February, 2012



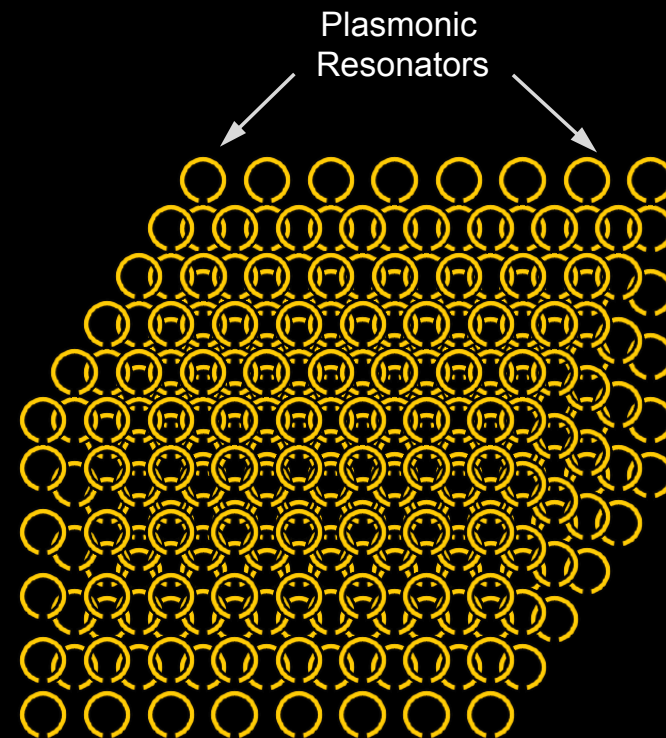
# Metamaterials: mimicking Nature

Metamaterial is a manmade media with all sorts of unusual functionalities that can be achieved by **artificial structuring smaller than the length scale of the external stimulus.**

*NIZ. Nature Materials 7, 420 (2008)*



Natural Solid



Electromagnetic  
Metamaterial



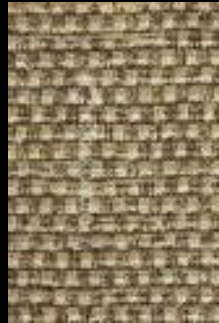
# Materials: from mega to nano

Pyramid Brick wall: 1m



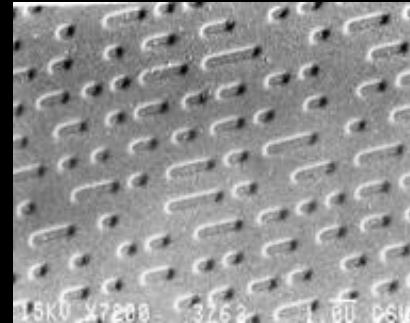
1000:1

Tweed wool: 1mm



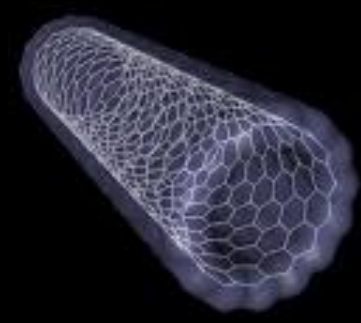
1000:1

CD tracks: 1micron



1000:1

Carbon nano-tubes: 1nm



Parthenon columns: 1m



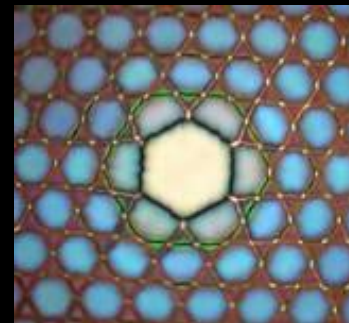
1000:1

Computer PCB: 1mm



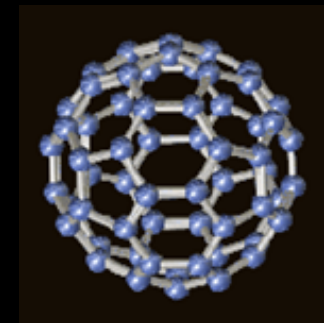
1000:1

Crystal fiber: 1micron



1000:1

Carbon buckyball: 1nm



Corresponding electromagnetic scale



Microwave meta-materials

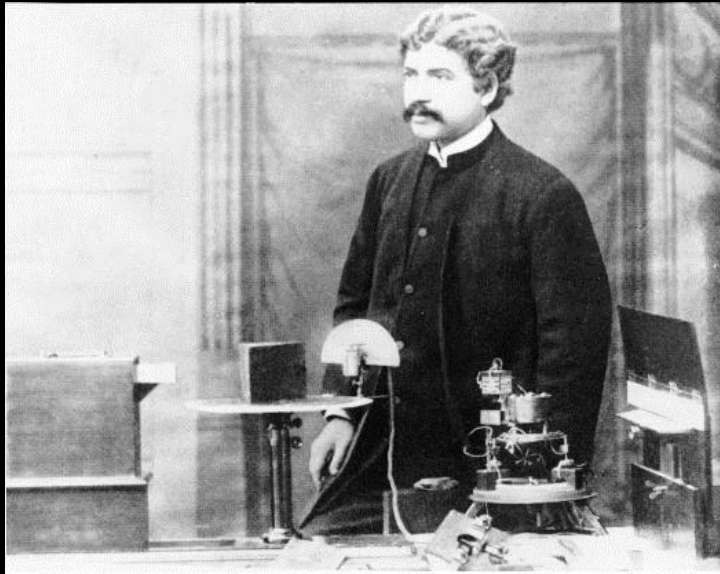
THz meta-materials

Photonic meta-materials





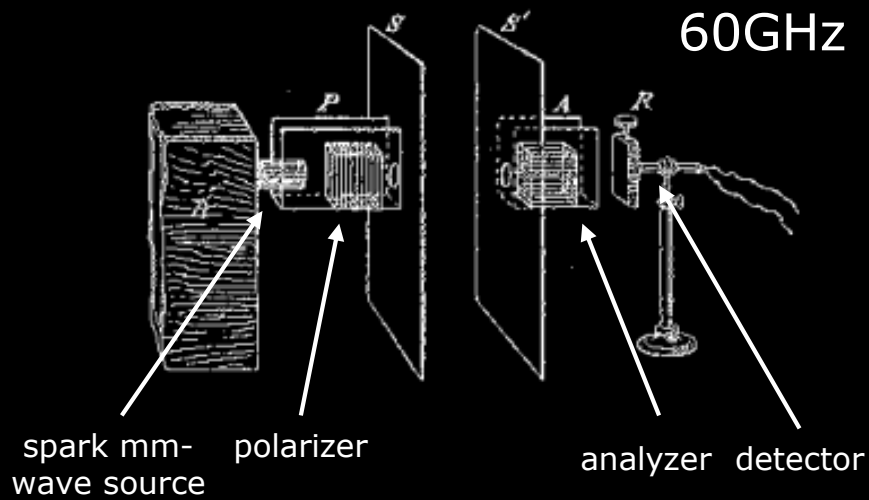
# 1<sup>st</sup> Metamaterial (J.Bose, 1898)



Sir Jagadish Chandra Bose, 1858 – 1937



Anisotropic Meta-molecule



Chiral Meta-molecule

J.Bose. Proc. Royal Soc. of London, **63**, 146 (1898)

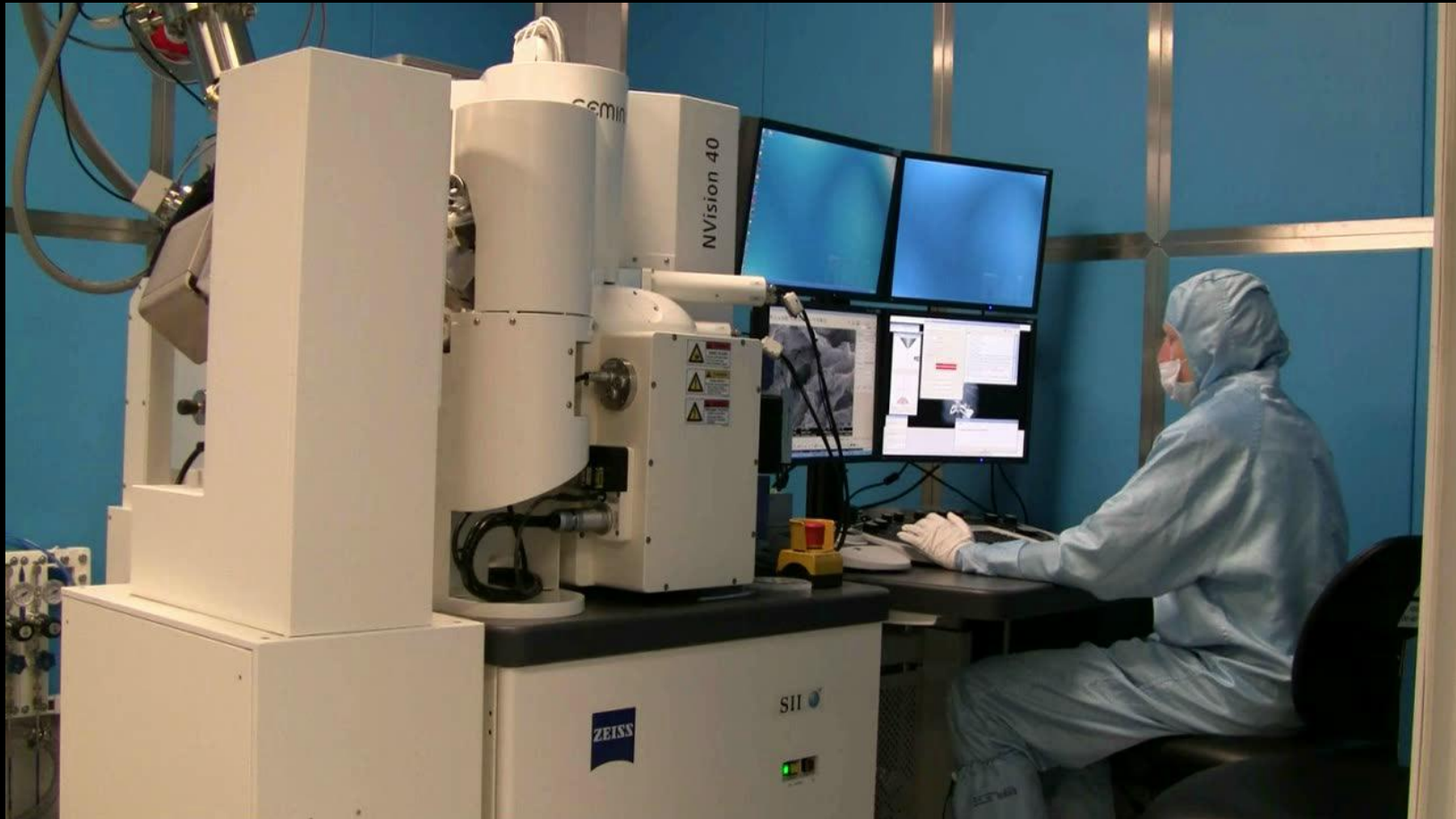
# Challenging nature through nanofabrication

Optical lithography

E-beam lithography

Ion-beam milling (FIB)

Nano-imprint



*Light*

# Metamaterials = Negative Index Media & Superlens

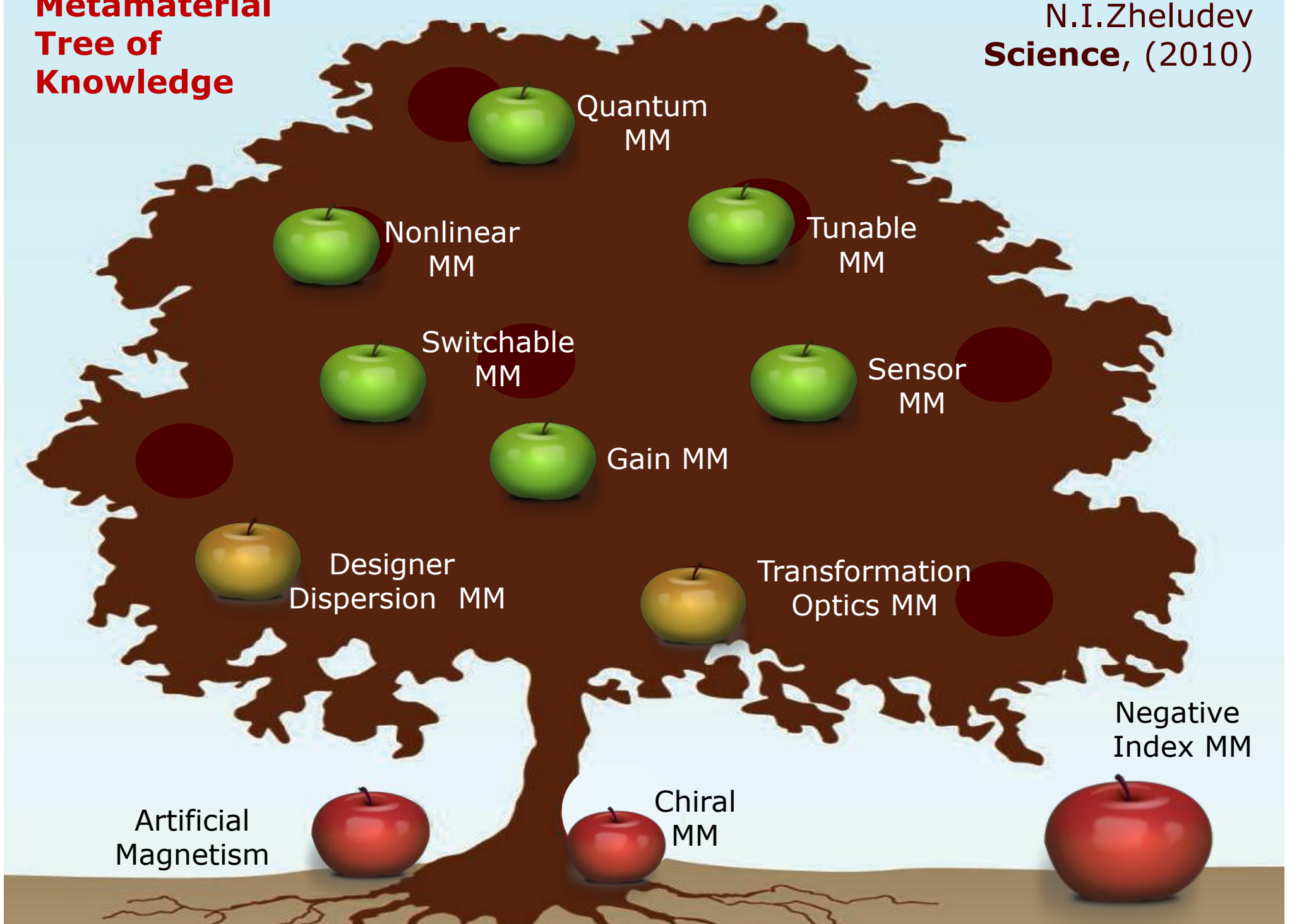
## Metamaterials = Invisibility & Cloaking





# Metamaterial Tree of Knowledge

N.I.Zheludev  
**Science**, (2010)



# Metamaterials and Southampton

- 2005: "Invisible Metals"
- 2007: Optical Magnetic Mirror
- 2006-2009: Chiral & "Stereo" metamaterials
  - 2006-2009 Asymmetric Transmission
  - 2006 EIT in metamaterials
  - 2008 Lasing Spaser
- 2009 Coherent & incoherent metamaterials
  - 2009-2010 Toroidal metamaterials
- 2010: Spectral collapse in metamaterials
  - 2010 Bas-relief metamaterials
  - 2010 Superconducting metamaterials
- 2010 CNT in metamaterials (ultrafast switching)
  - 2010 Graphene in Metamaterials
- 2010 Chalcogenide Glass in metamaterials (switching)
  - 2010 Coherent control in metamaterials
  - 2010 Superconducting H-Tc metamaterials



A major driver  
in research

\$10B to \$30B  
market in 2020

**Photonics  
METAMATERIALS:  
New  
functionalities**

**Active/gain  
Meta  
materiails**

**Negative  
refraction  
(superlens)**

**Artificial  
Magnetic  
properties**

**Switchable  
media  
(photonics)**

**High/low  
Refractive  
ind.**

**Chiral &  
anizotropic  
Polarization  
control**

**Engineered  
dispersion  
(slow light)**

**Frequency  
selective  
Surfaces  
filters**

**Modelling**

**Mimicking**

**Unique  
Environ-  
ment**

**Metamaterial  
as platform  
for science**

**Templating**

**Atomic  
& Nuclear  
physics**

**Cosmology**

**Solid-State  
&  
Supercon.**

**Security  
and  
defence**

**Imaging &  
Lithography**

**Data  
storage**

**Telecom  
& fiber**

**New Platform  
for  
technology**

**Sensors &  
detectors**

**Light  
harvesting  
& energy**

**Light  
Sources**

**Nano-  
photonic  
circuits**





# Photonic Metamaterials with engineered dispersion



## **Goal:**

Controlling optical  
properties

## **Applications:**

Spectral filters

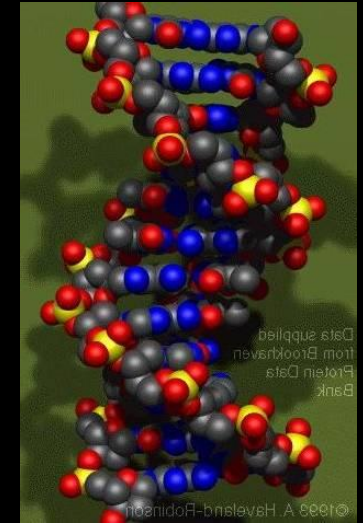
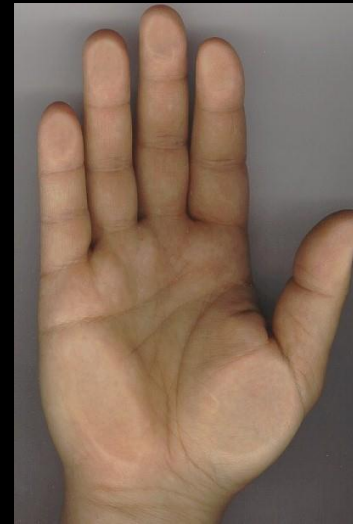
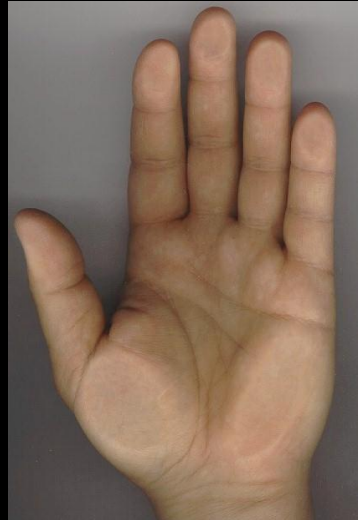
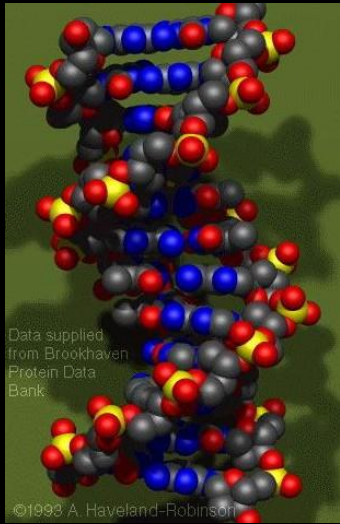
Delay lines

Dispersion compensation

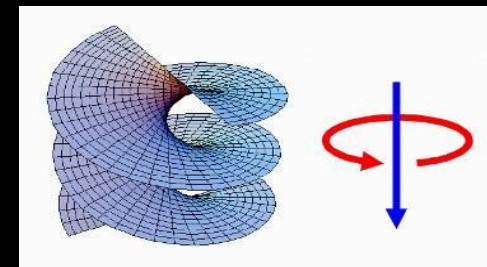
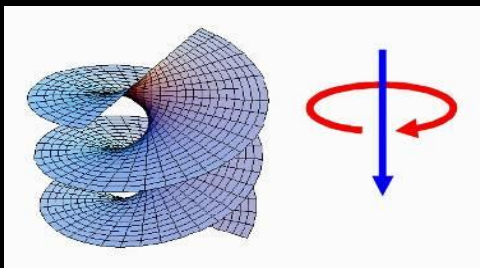
Slow light

# 3D chirality ( $\chi\rho\sigma$ )

Enantiomeric forms of chiral structures



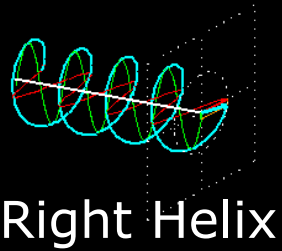
Plane of reflection



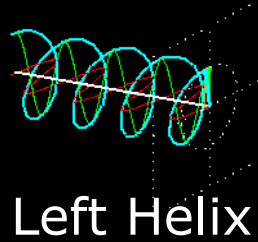
“Any man who, upon looking down at his bare feet, does not laugh, has either no sense of symmetry or no sense of humour” (Descartes)

# Optical Activity

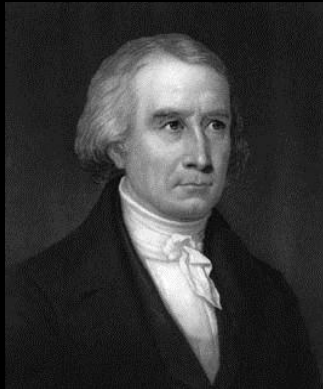
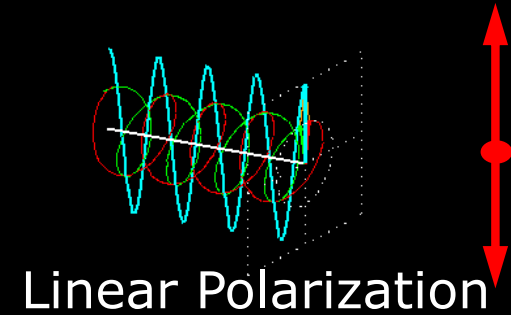
In Vacuum



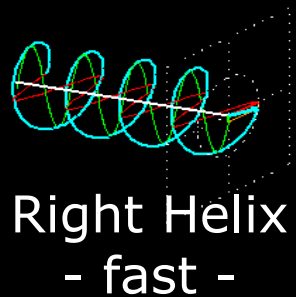
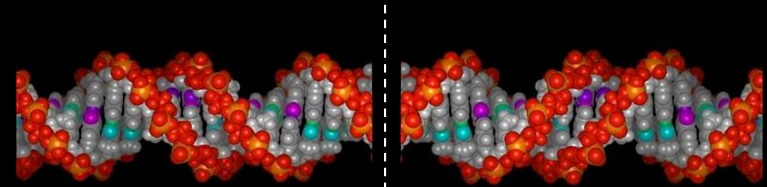
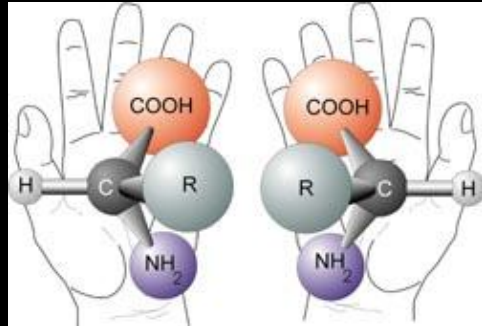
+



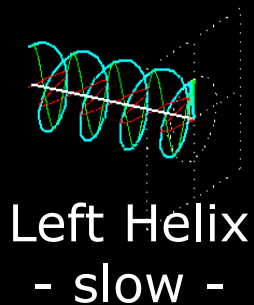
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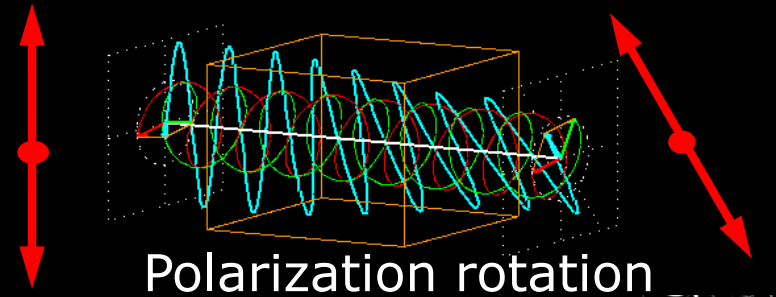
D. F. J. Arago  
1786 - 1853



+

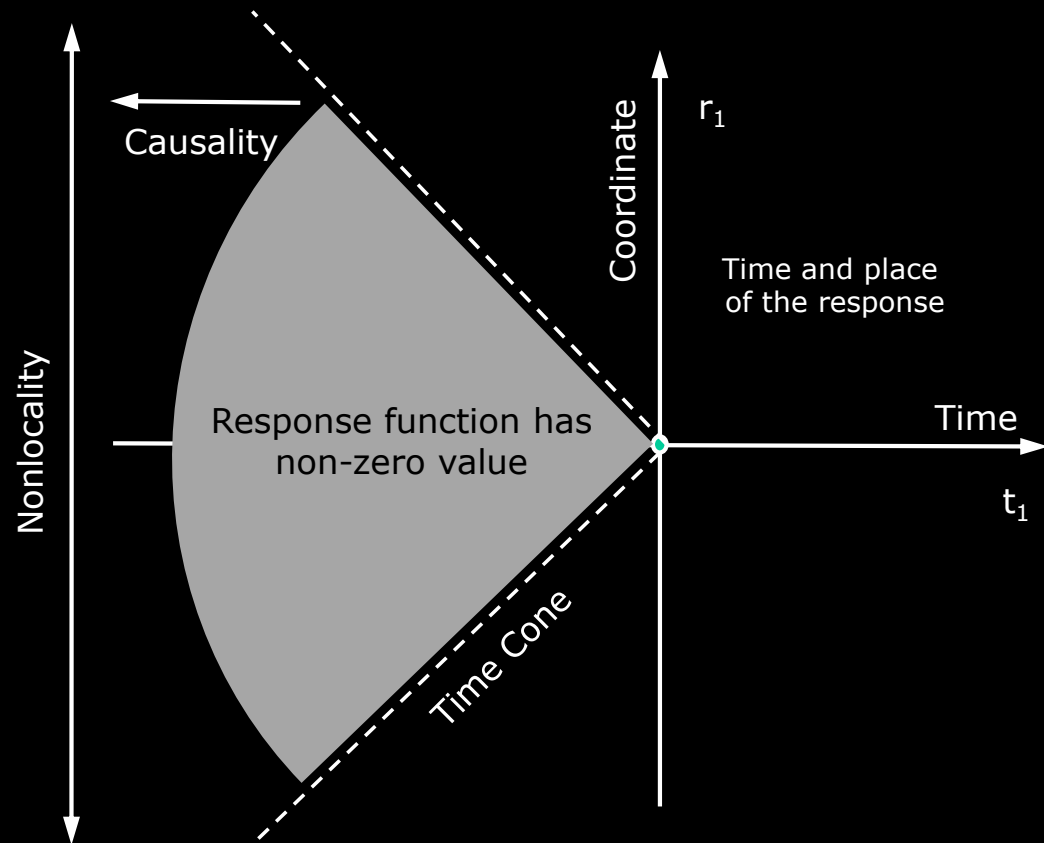


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# Nonlocality & Causality of Optical Response & Constitutive Equation



Nonlocality

Causality

Constitutive equation

$$P_i(r, t) = \sum_{j=X,Y,Z,V} \int dr_j \int_{-\infty}^t dt_1 \psi_{ij}(r - r_1, t - t_1) E_j(r_1, t_1)$$

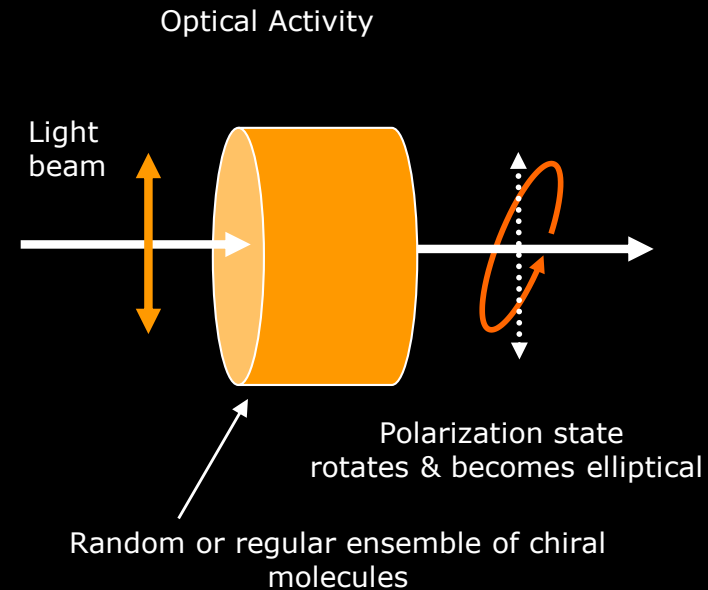
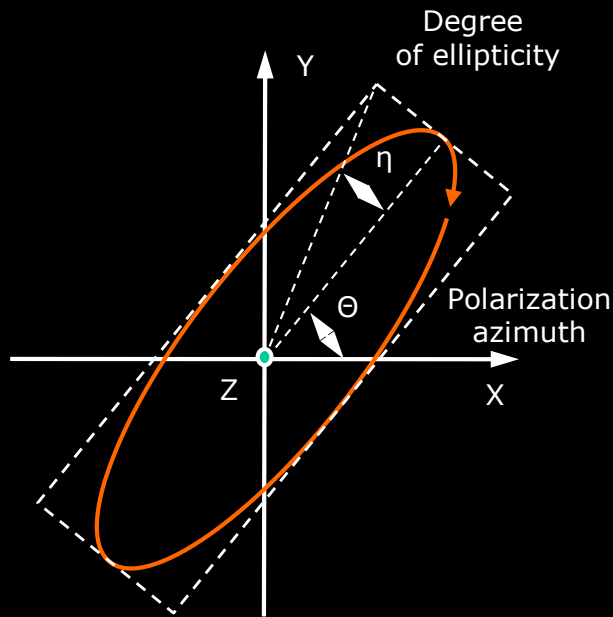
Response

Excitation

$$P_i(\omega) = \frac{1}{4\pi} (\epsilon_{ij} - \delta_{ij} + i k_k \Gamma^{(1)}_{ijk}) E_j(\omega)$$

# Optical Rotatory Power (optical activity) & Polarization

D. F. J. Arago and J-B. Biot at the beginning of the XIX century



Constitutive equation

$$P_i = \frac{1}{4\pi} (\epsilon_{ij} - \delta_{ij} + i k_k \Gamma^{(1)}_{ijk}) E_j$$

$$\epsilon_{ij} = \epsilon \delta_{ij}$$

$$\Gamma^{(1)}_{ijk} = -\Gamma^{(1)}_{jik} = \Gamma e_{ijk}$$

$$\Theta = \Theta_0 + \frac{2\pi L}{\lambda^2} \text{Re}\{\Gamma\}$$

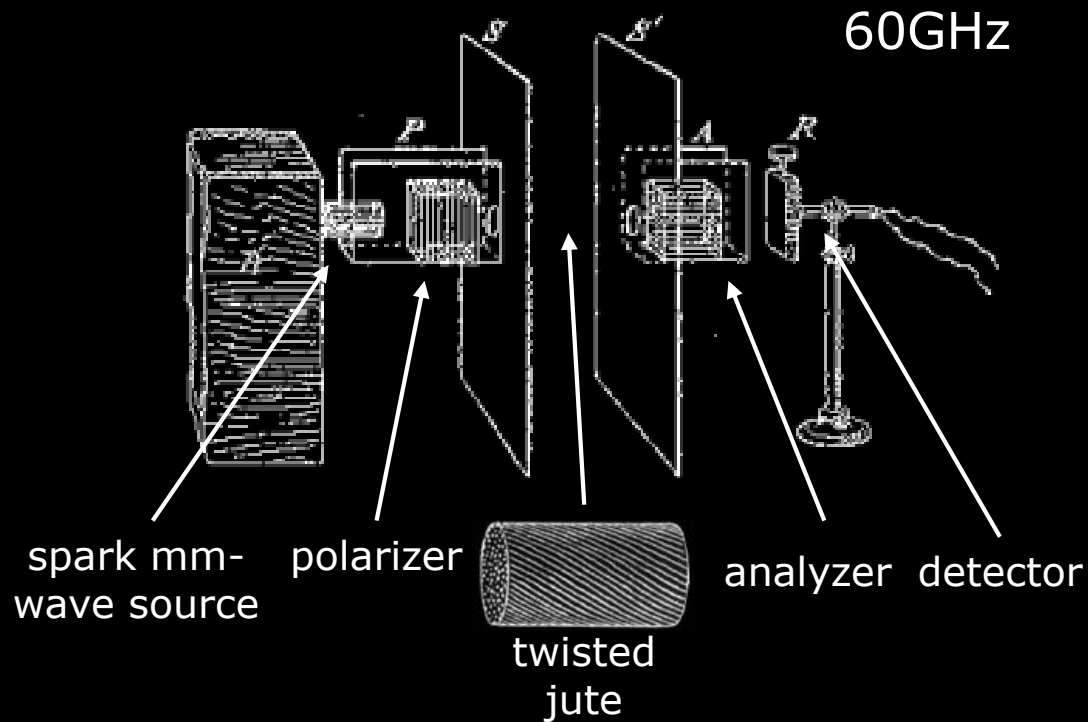
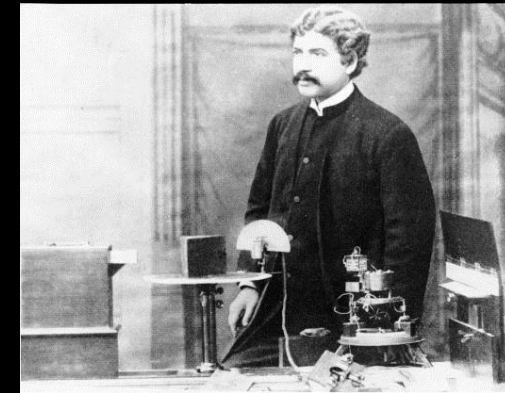
Polarization rotation

$$\eta = f(\text{Im}\{\Gamma\}, L)$$

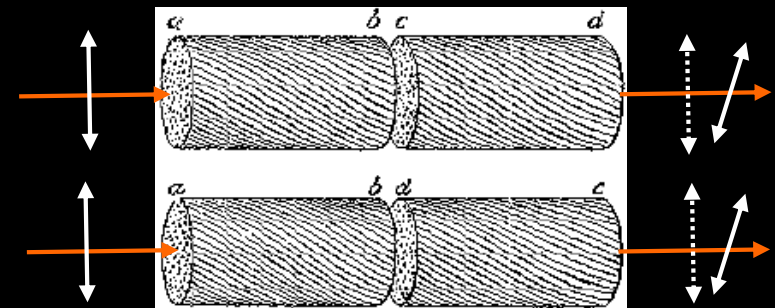
Induced ellipticity (circular dichroism)

# 1<sup>st</sup> Metamaterial (J. Bose, 1898)

"In order to imitate the rotation by liquids like sugar solutions, I made elements of "molecules" of twisted jute, of two varieties, one kind being twisted to the right (positive) and the other twisted to the left (negative)..."

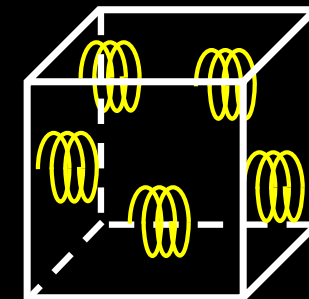


Polarization effect does not depend on the propagation direction



"The twisted structure [of jute] produces an optical twist of the plane of polarization"

J. Bose. Proc. Royal Soc. of London, **63**, 146 (1898)



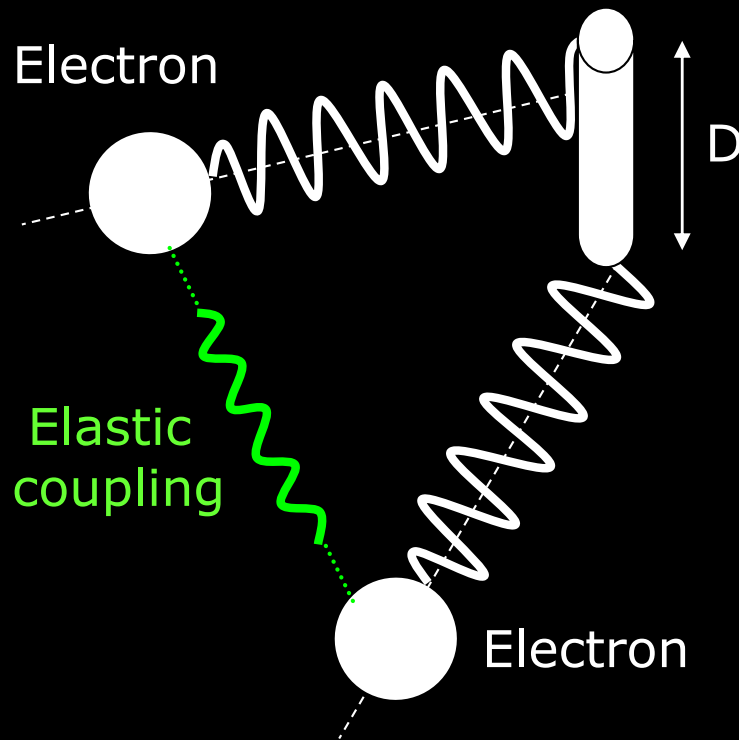
Karl Lindman (1920)



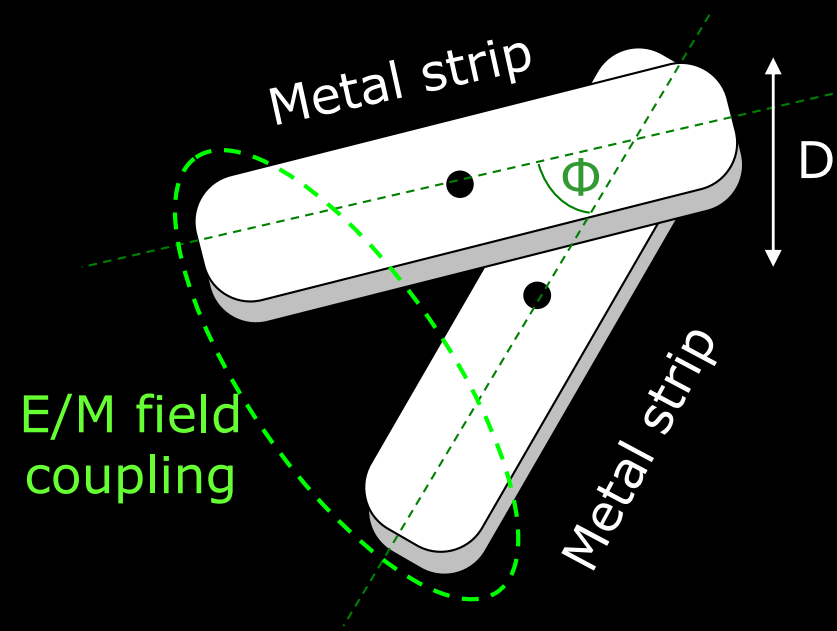


# The First concept of Chiral Metal Metamaterial, 2000

The Born-Kuhn  
Molecular model (1915)



Svirko-Zheludev-Osipov  
Meta-material solution (2000)



APPLIED PHYSICS LETTERS

VOLUME 78, NUMBER 4

22 JANUARY 2001

## Layered chiral metallic microstructures with inductive coupling

Yuri Svirko<sup>a)</sup> and Nikolay Zheludev<sup>b)</sup>

*Department of Physics and Astronomy, University of Southampton, SO17 1BJ United Kingdom*

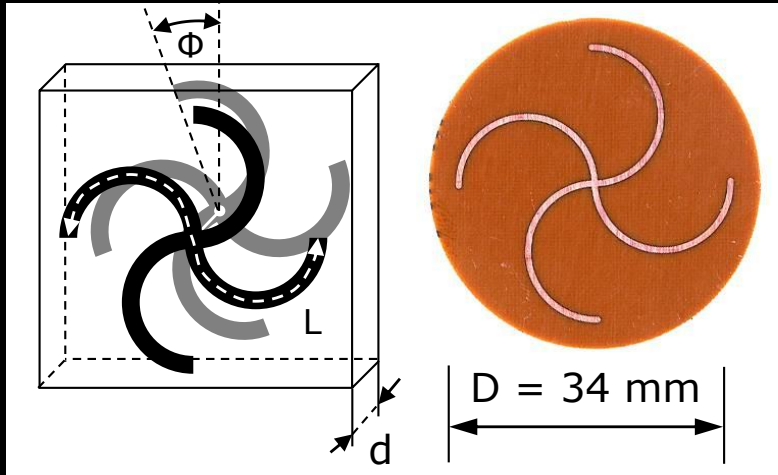
Michail Osipov<sup>c)</sup>

*School of Physics, University of Exeter, Exeter, EX4 4QL United Kingdom*

(Received 13 June 2000; accepted for publication 18 November 2000)

# Microwave Chiral Metamaterials

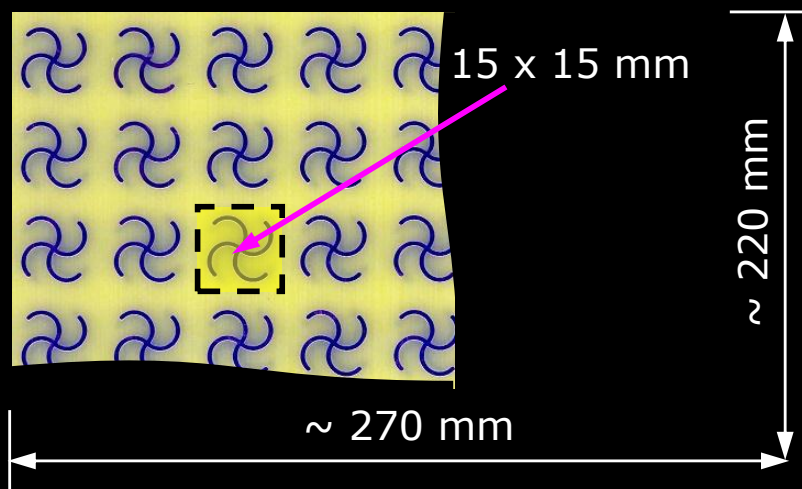
Chiral Meta-molecule



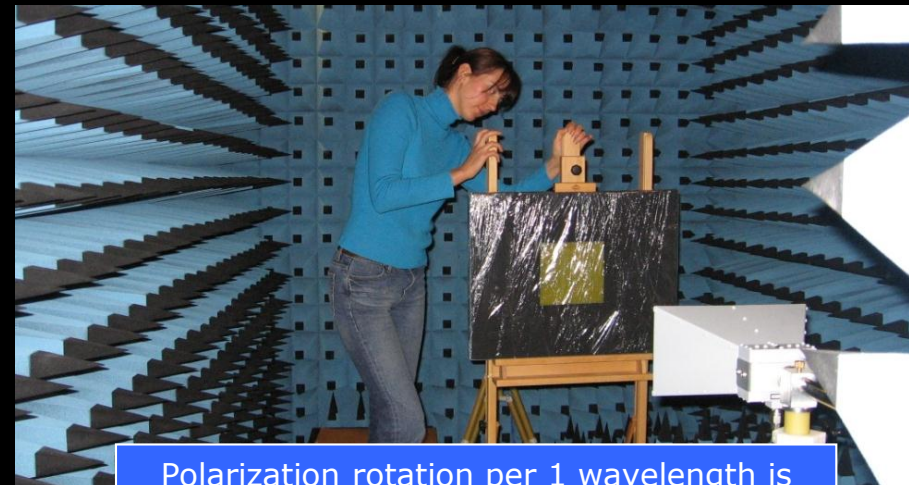
Waveguide polarimeter



Chiral Metamaterial



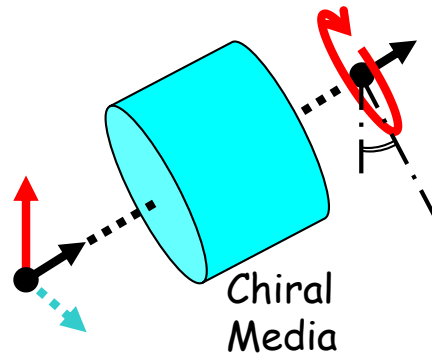
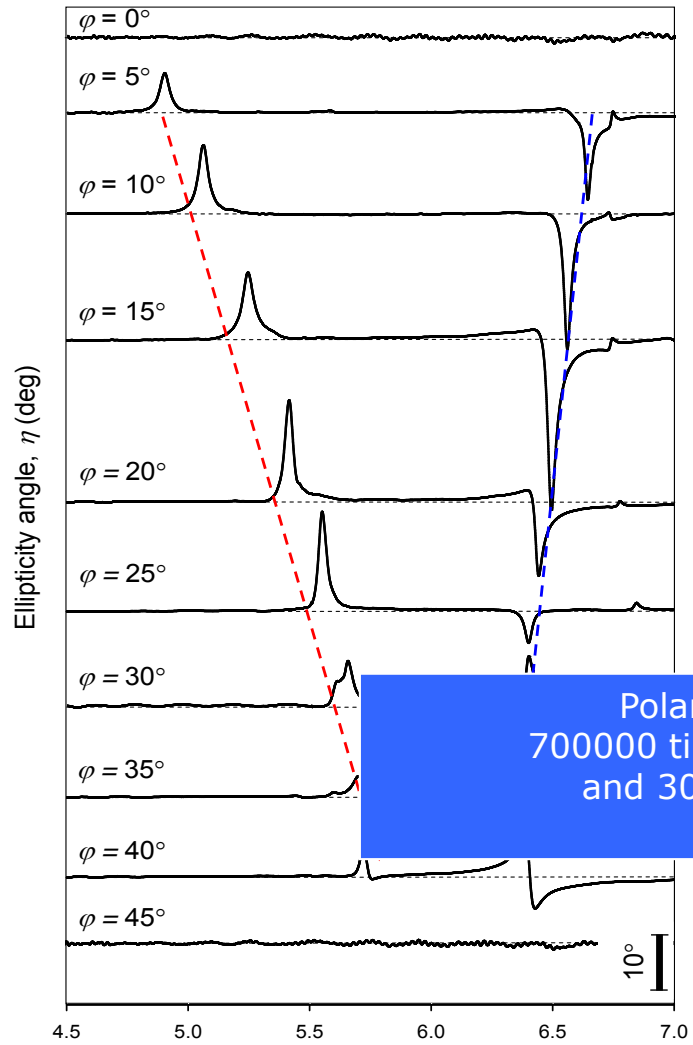
Anechoic chamber



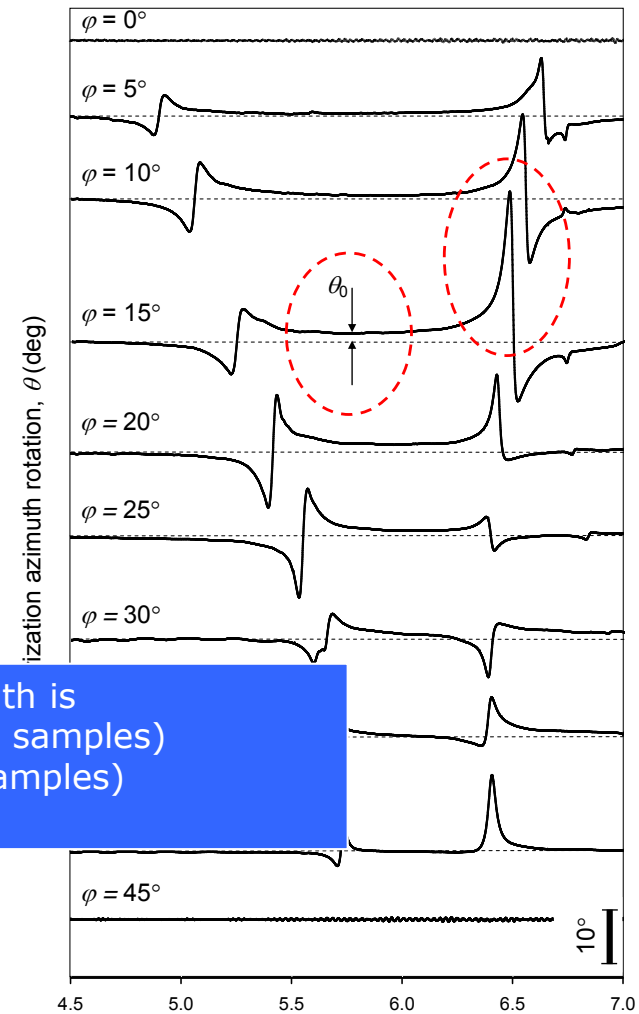
Polarization rotation per 1 wavelength is 70000 times that of quartz (microwave samples) and 30 times that of quartz (optical samples)

# Ellipticity and Polarization Rotation in Bi-layered Chiral Structure

Rogacheva, Fedotov, Schwanecke, and Zheludev. PRL, **97**, 177401 (2006)



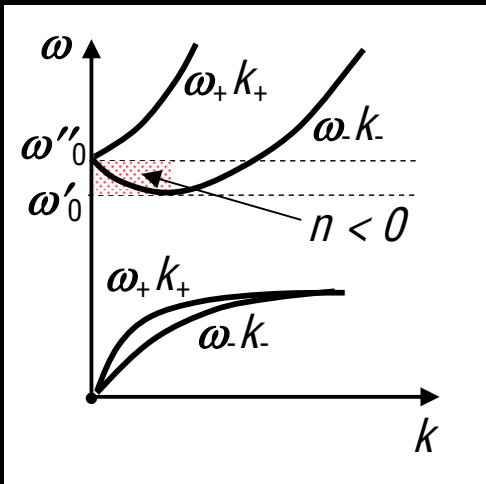
Polarization rotation per 1 wavelength is 700000 times that of quartz (microwave samples) and 30 times that of quartz (optical samples)



# First Metamaterials Were Chiral

Rogacheva, Fedotov, Schwanecke, and Zheludev. PRL, **97**, 177401 (2006)

## Chirality and Negative Refraction

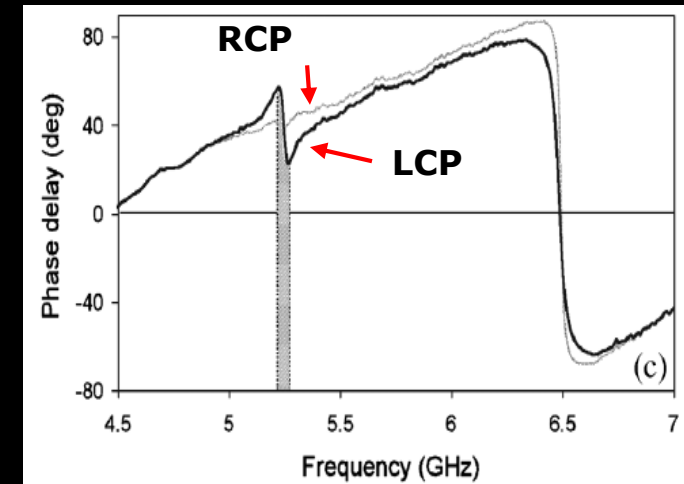


In chiral materials strong chirality yields negative refraction for one circular polarization

$$\left( \frac{\text{rotation}}{\text{elliptization}} \right) \propto N_0 \left( \frac{f(\omega)}{g(\omega)} \right) \text{Im}\{R_{mn} d_{nm}\}$$

Tretyakov et al. (2003)  
Pendry (2004)

## Phase delay in chiral metamaterial



PRL **97**, 177401 (2006)

PHYSICAL REVIEW LETTERS

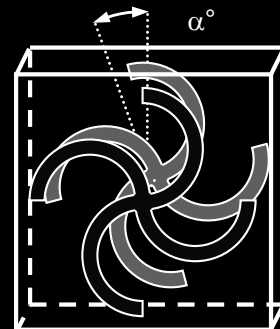
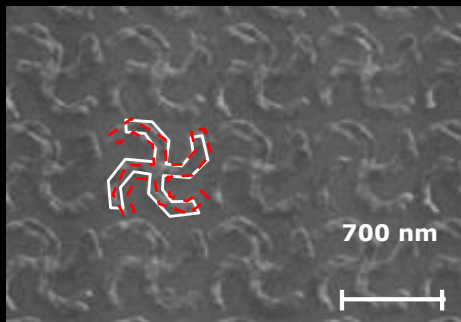
week ending  
27 OCTOBER 2006

## Giant Gyrotropy due to Electromagnetic-Field Coupling in a Bilayered Chiral Structure

A. V. Rogacheva, V. A. Fedotov,\* A. S. Schwanecke, and N. I. Zheludev†

EPSRC NanoPhotonics Portfolio Centre, School of Physics and Astronomy, University of Southampton, SO17 1BJ, United Kingdom

(Received 7 April 2006; published 26 October 2006)



In the proximity of resonance the group velocity for right circular polarization in the sinistral structure has opposite sign to the phase velocity... this is a signature, or the necessary condition of negative refraction in chiral media.

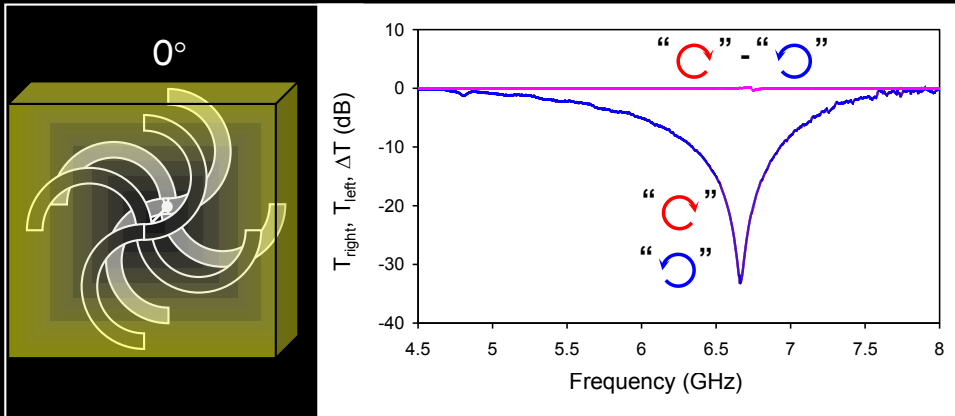
Plum, Zhou, Dong, Fedotov, Koschny, Soukoulis, Zheludev, *Phys. Rev. B* **79**, 035407 (2009)

The first "stereo" photonics metamaterial (2007)

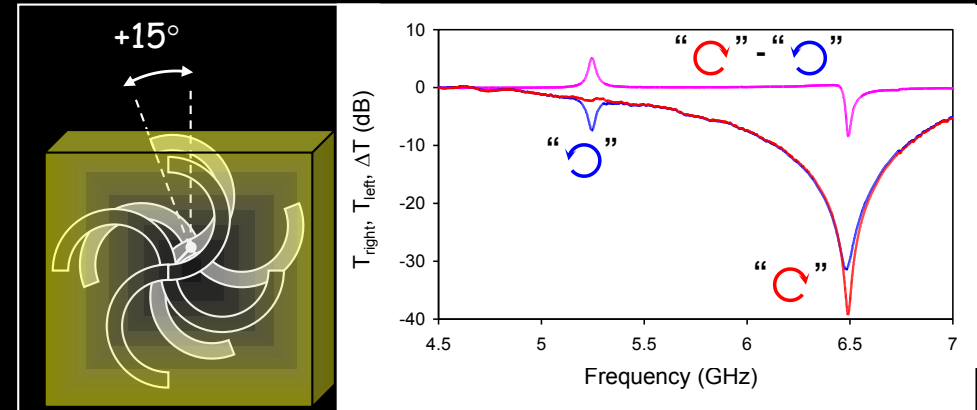


# Gyrotropy vs Chirality

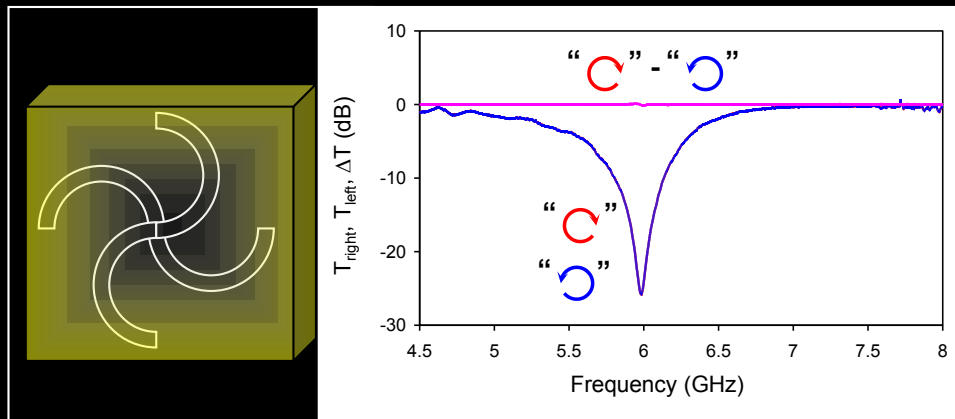
## No gyrotropy



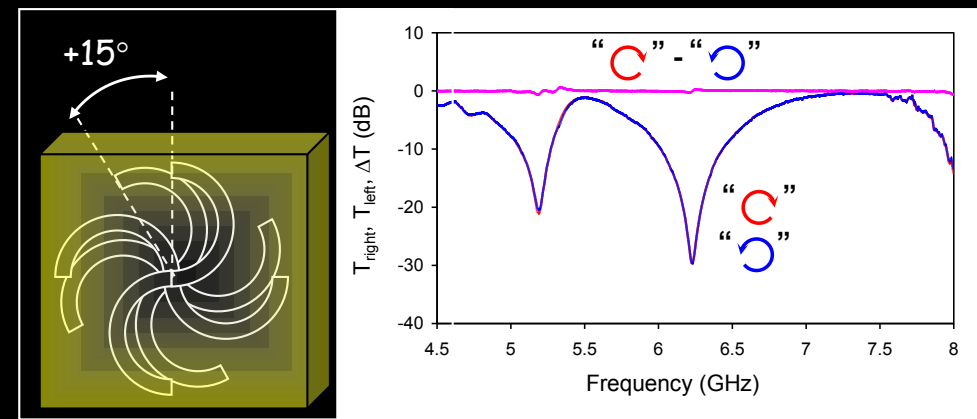
## Yes gyrotropy



## No gyrotropy



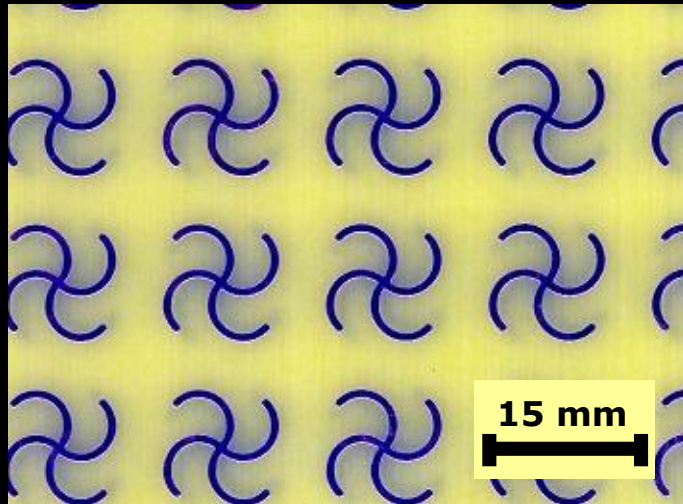
## No gyrotropy



Polarization rotation per 1 wavelength is 700000 times that of quartz (microwave samples) and 30 times that of quartz (optical samples)



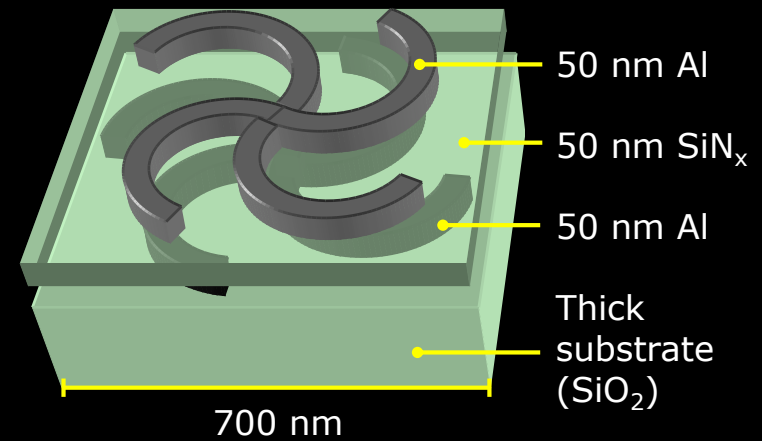
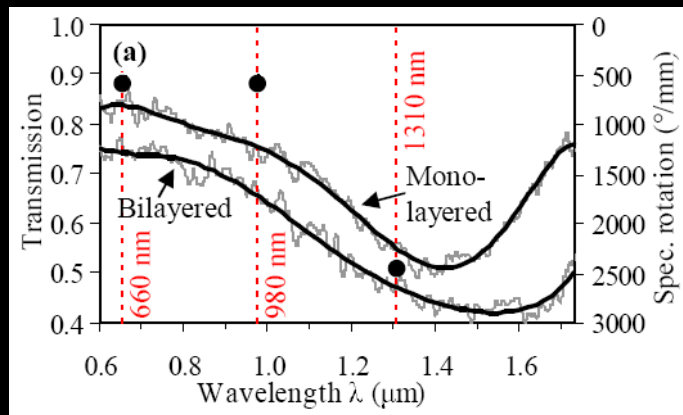
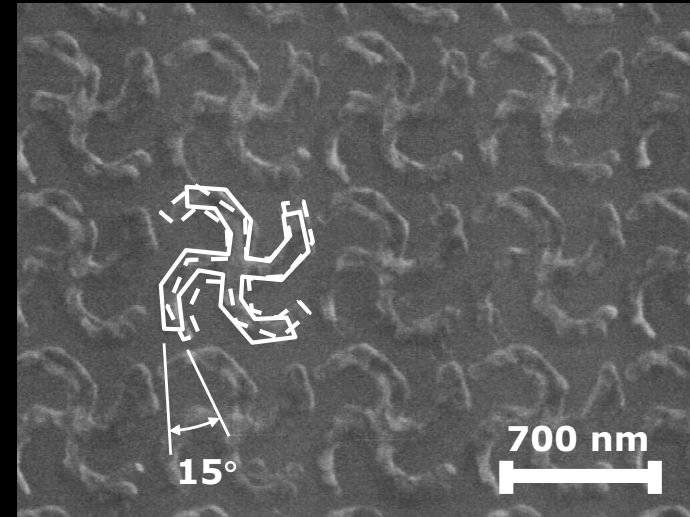
# Photonic Chiral Bilayered (Stereo) Metamaterial



Scaling  
1 : 21429



MW → near-IR

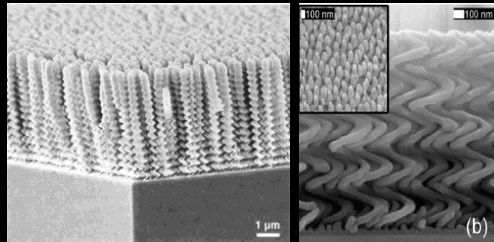


Fedotov, Plum, Schwanecke, Chen and Zheludev. APL **90**, 223113 (2007)

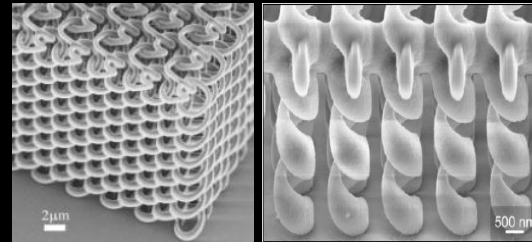


# Key experimental results in 3D chiral metamaterials

## Sculptured chiral photonic films & PCs

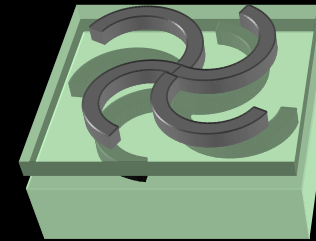


Young and Kowal (1956)  
Robbie, Brett, Lakhtakia (1996)  
Hrudey, Szeto, Brett (2006)



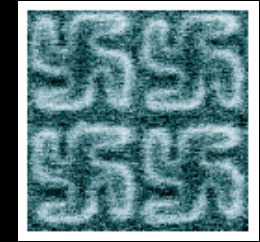
Kennedy, John et.al (2002)  
Seet, Misawa et al (2005)  
Pang, Sheng et.al (2005)  
Thiel, Wegener et al (2007)

## Negative refraction & NI in microwave Chiral MM



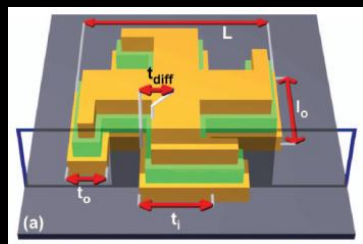
Rogacheva, Zheludev et al (2006)  
Plum, Soukoulis, Zheludev (2009)

## Gyrotropy in single-layered MM



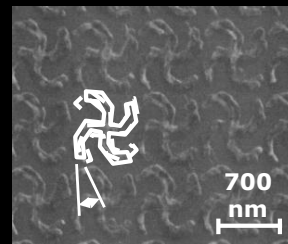
Kuwata-Gonokami et al (2005)

## Strong dichroism in bi-layered structure



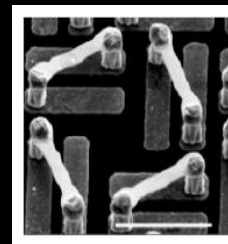
Decker, Wegener et al. (2007)

## Stereo photonic metamaterials



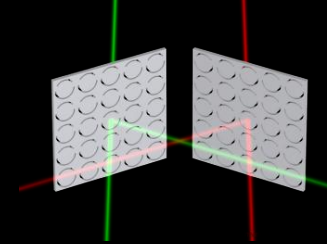
Plum, Zheludev et al (2007)

## NI in THz



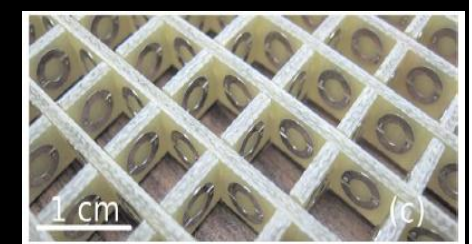
Zhang et al (2009)

## Extrinsic Chirality & NR



Plum, Zheludev et al (2008)

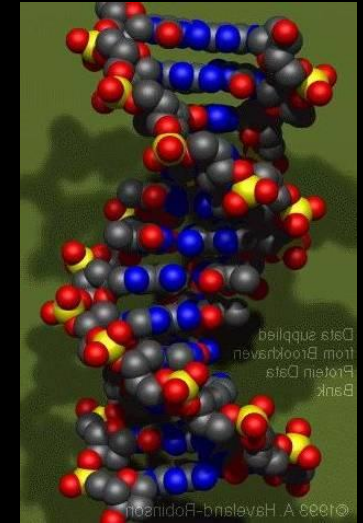
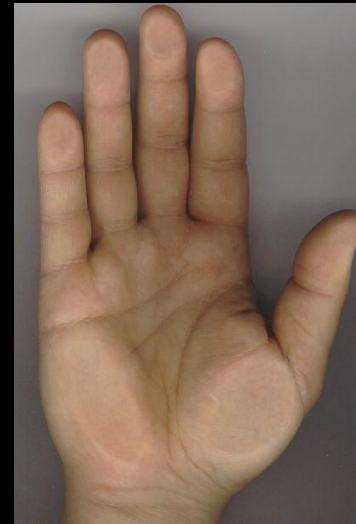
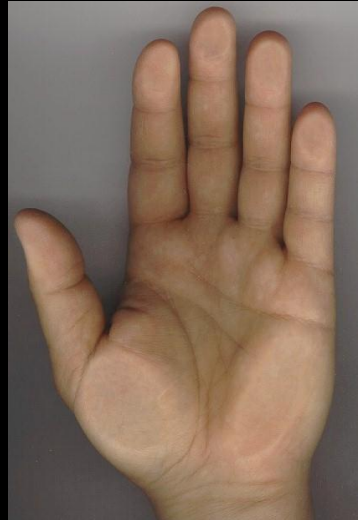
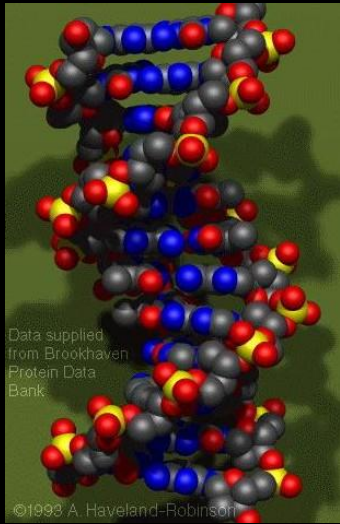
## Volume Chiral NI Metamaterial



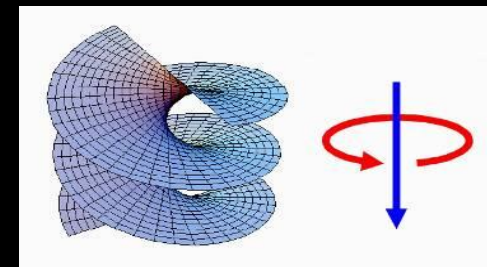
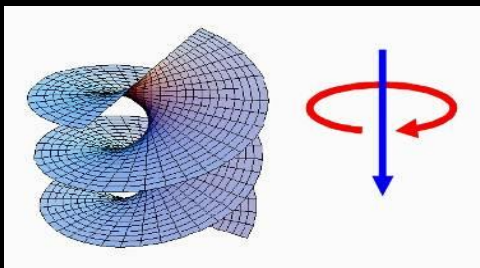
Wang, Soukoulis et al (2009)

# 3D chirality ( $\chi\rho\sigma$ )

Enantiomeric forms of chiral structures



--- Plane of reflection



“Any man who, upon looking down at his bare feet, does not laugh, has either no sense of symmetry or no sense of humour” (Descartes)



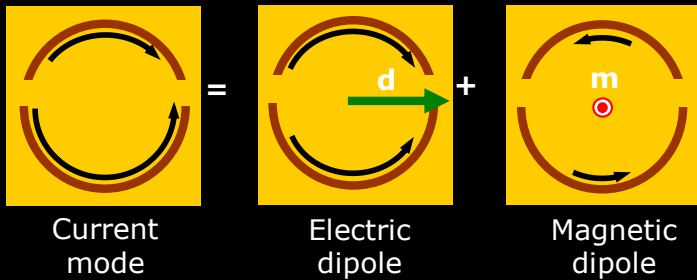
# Is Molecular Chirality Needed for Optical Activity?

In **randomly oriented** ensembles of molecules molecular chirality IS needed for optical activity

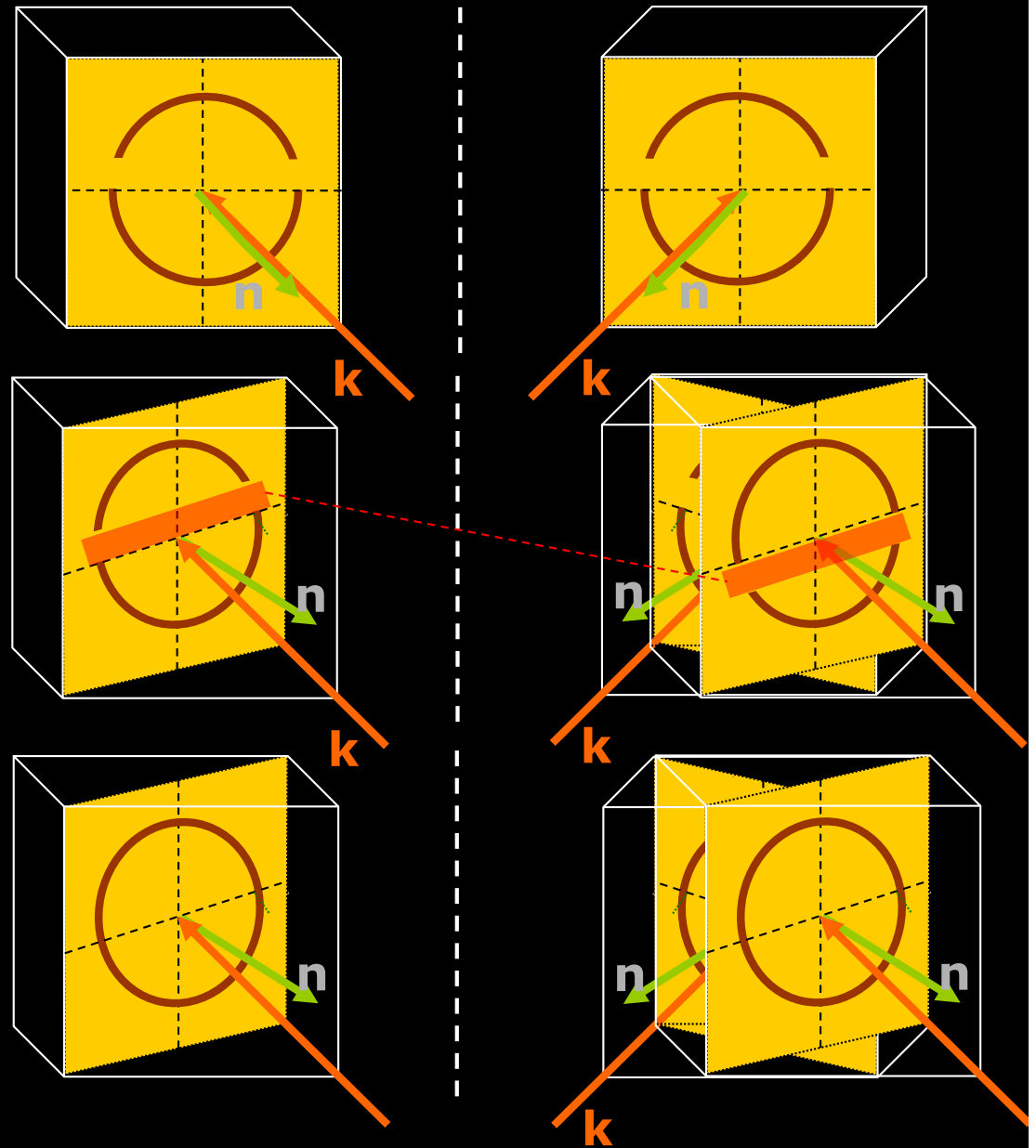
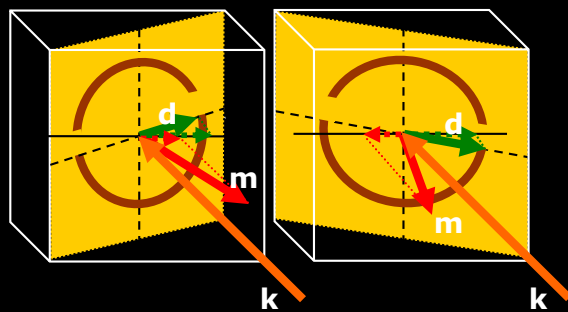
**Intrinsic chirality**  
depends on symmetry of the medium

In **ordered structures** (crystal, meta-material) optical activity will be seen along a "screw direction" of light propagation

**Extrinsic chirality**  
depends on combined symmetry of the medium and light wave



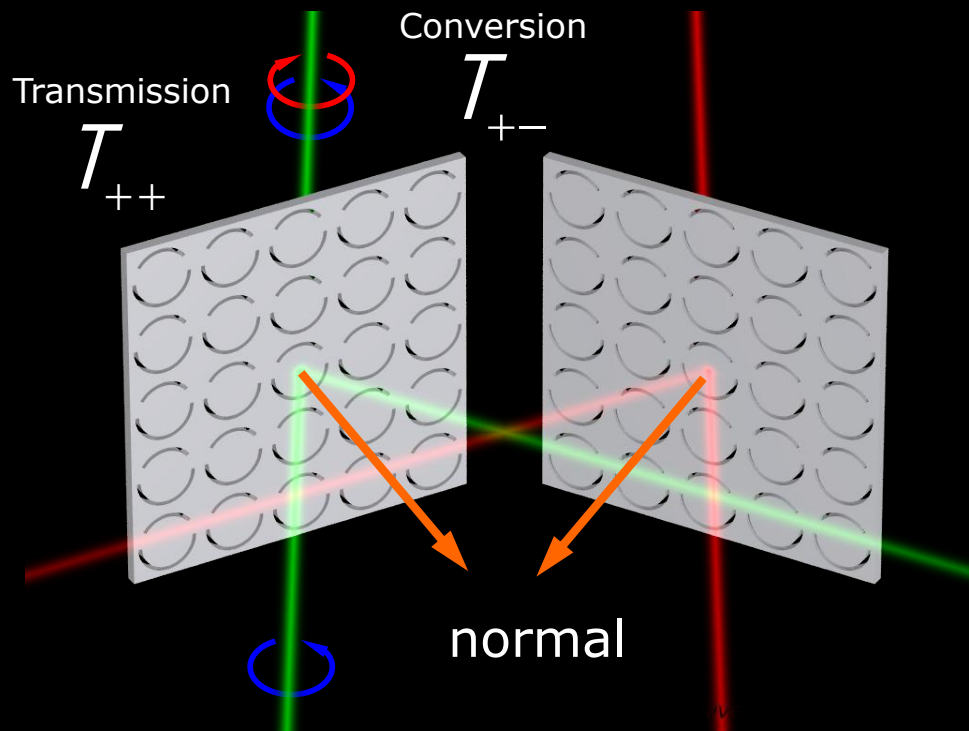
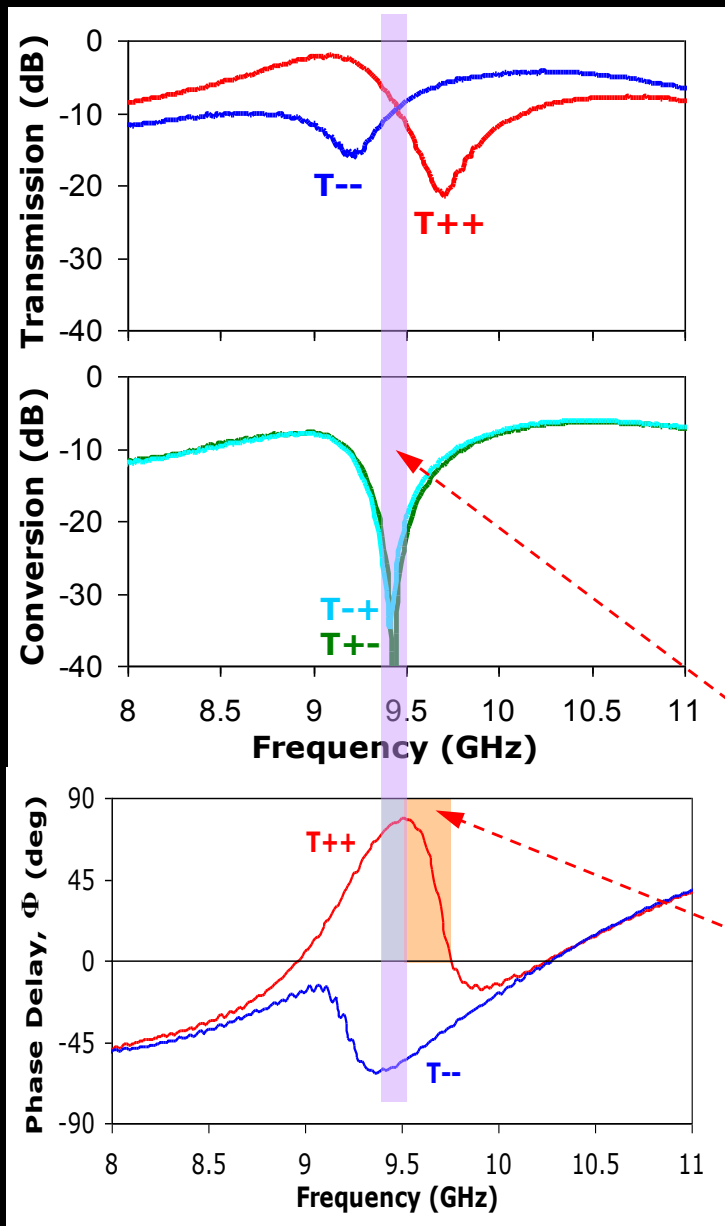
Oblique incidence



**Metamaterials: optical activity without chirality**

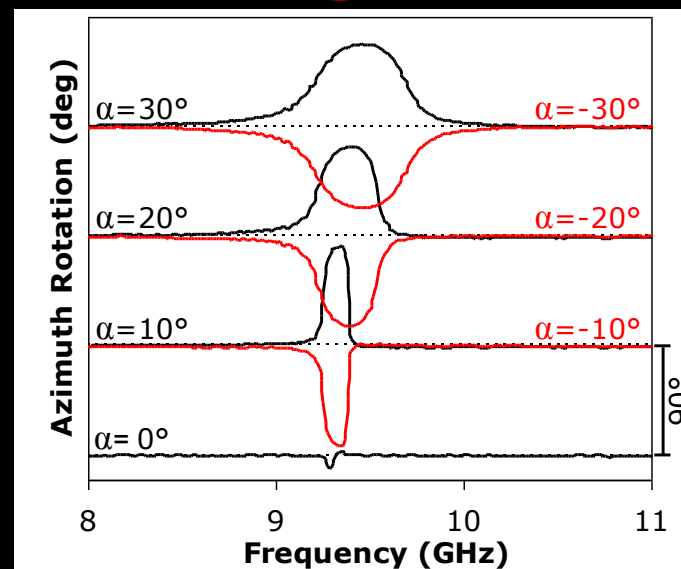
Plum, Liu, Fedotov, Chen, Tsai, and Zheludev, *PRL* **102**, 113902 (2009)

# Extrinsic Chirality in Asymmetrically Split-ring Metamaterial

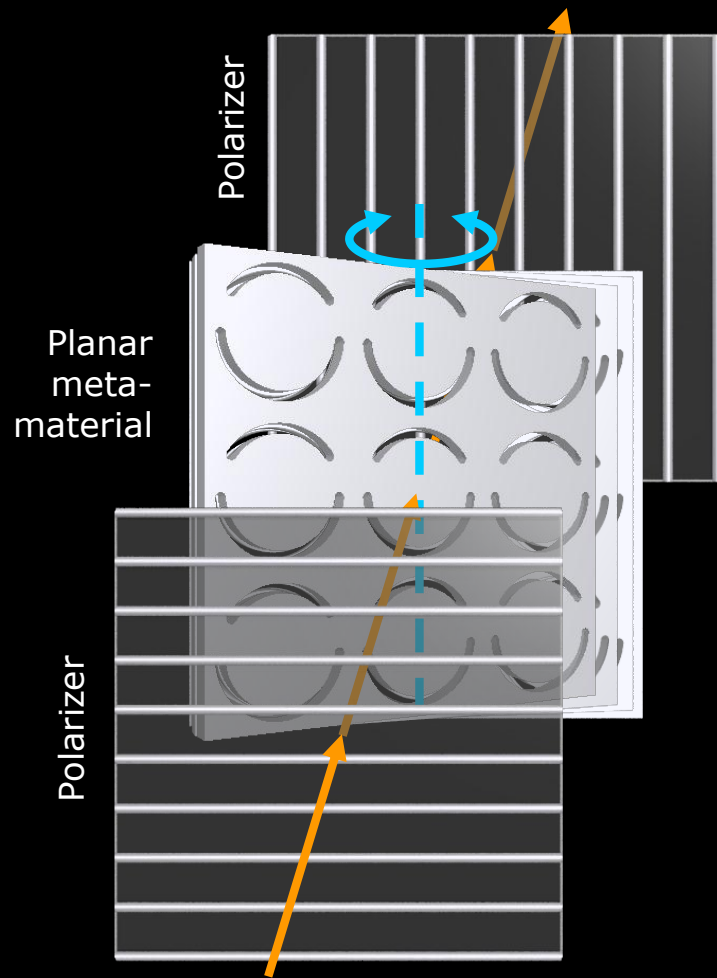


Almost circular eigenstates:  
true optical activity

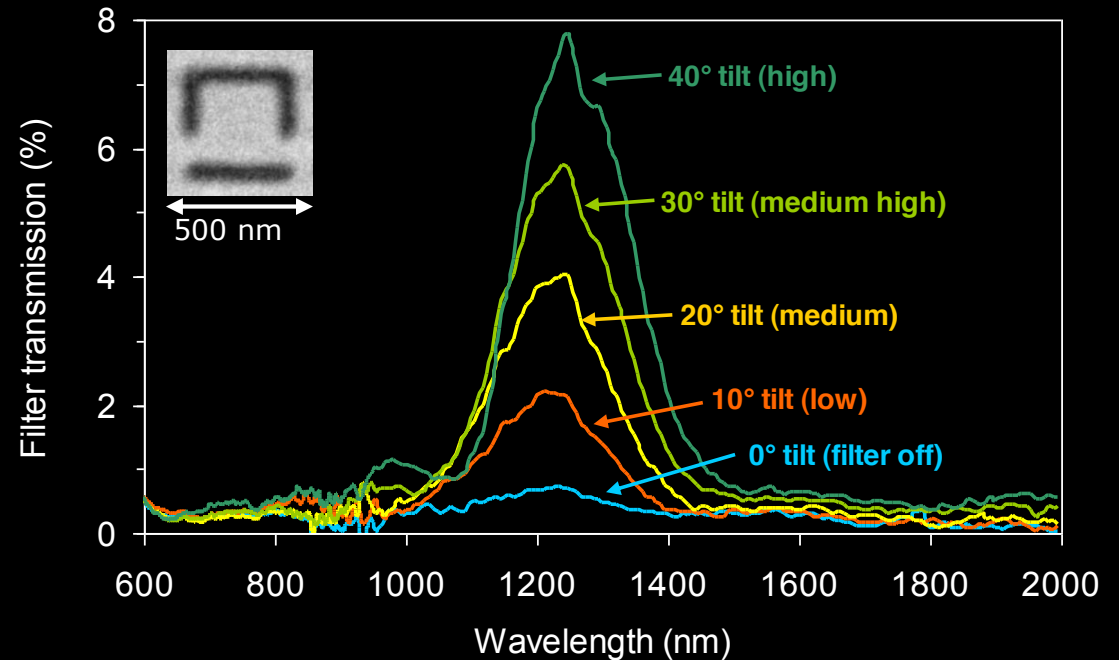
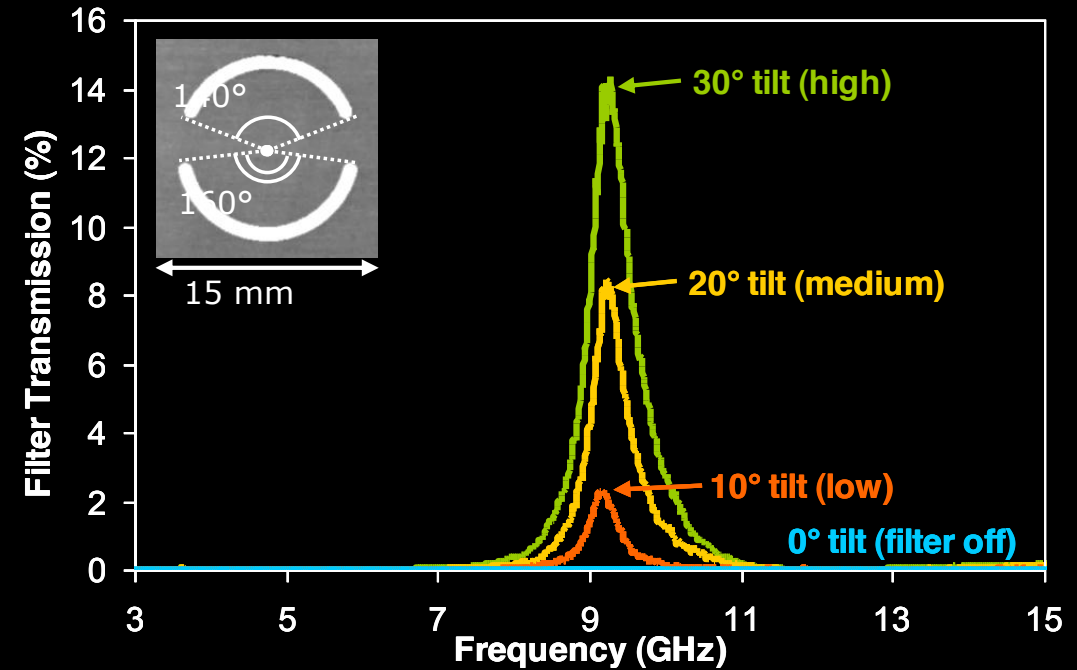
Negative group velocity



# Metamaterial isoindex chiral microwave, and optical filters



Tunable throughput  
Well-isolated pass-band  
simple planar metamaterial  
Q-factors of  $>700$  are achievable

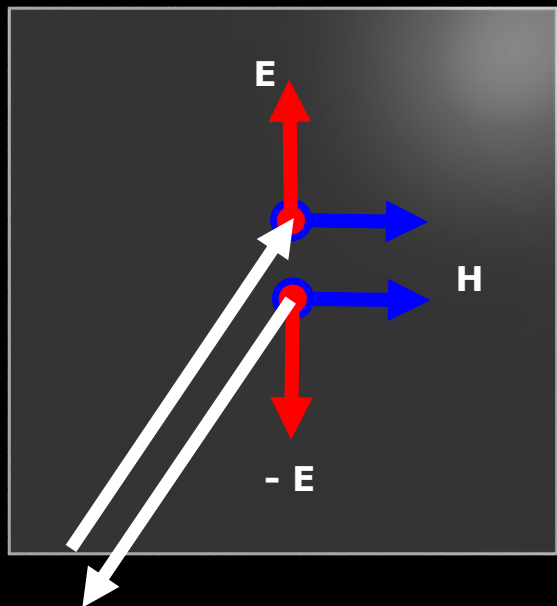


# Magnetic Mirror



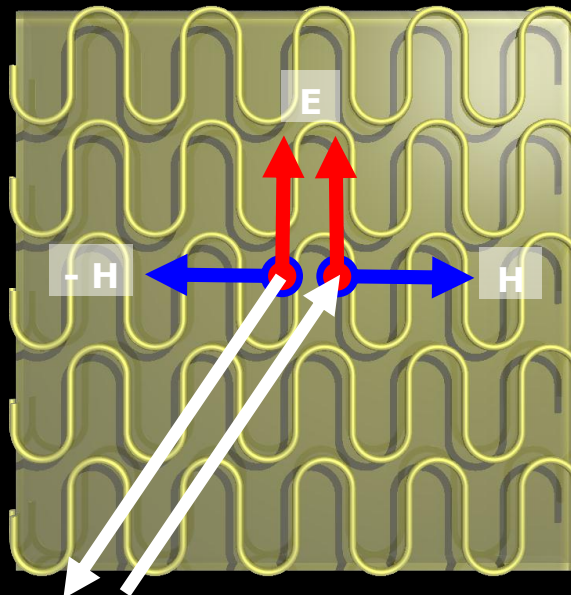
# Metamaterial Optical Magnetic Mirror (2005-2007)

"Electric mirror"



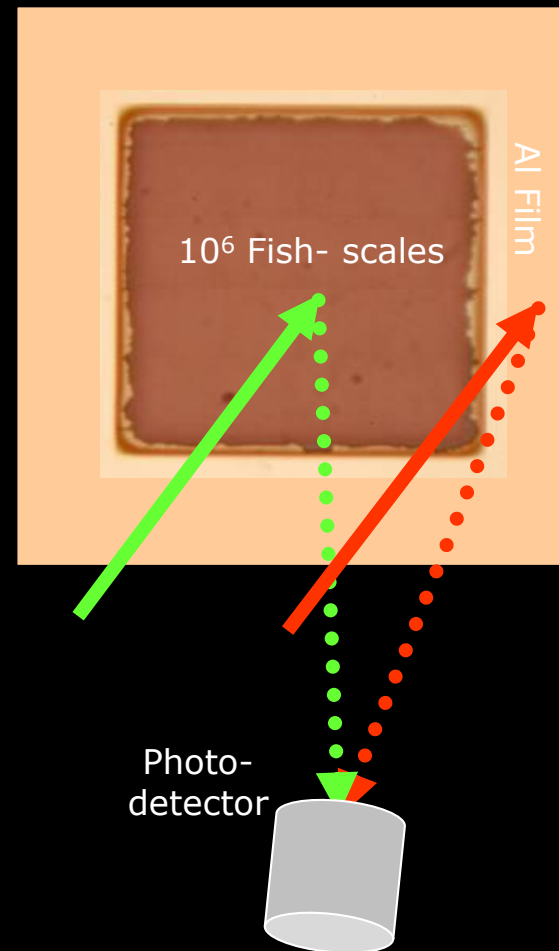
Quenched Dipolar Radiation

"Magnetic mirror"



Enhanced Dipolar Radiation

"Optical Magnetic Mirror"  
@ 630nm



APPLIED PHYSICS LETTERS 88, 091119 (2006)

**Mirror that does not change the phase of reflected waves**

V. A. Fedotov, A. V. Rogacheva, and N. I. Zheludev<sup>a)</sup>

Loss enhancement &  
Optical Analogue of the Meissner effect (superconductivity)

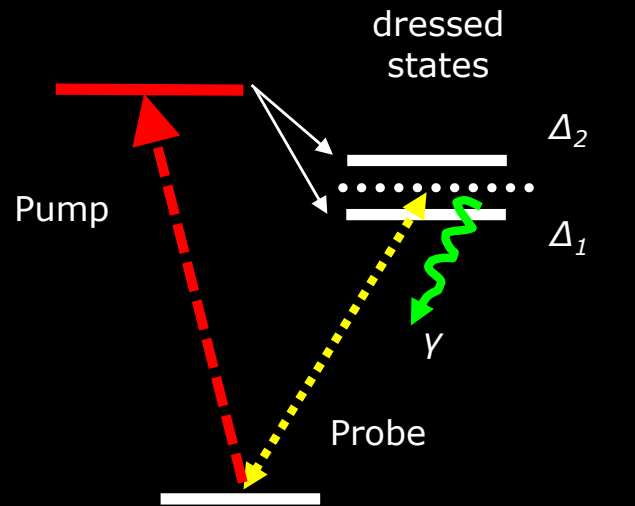
J. Opt. A: Pure Appl. Opt. 9 (2007) L1-L2

RAPID COMMUNICATION

**Optical magnetic mirrors**

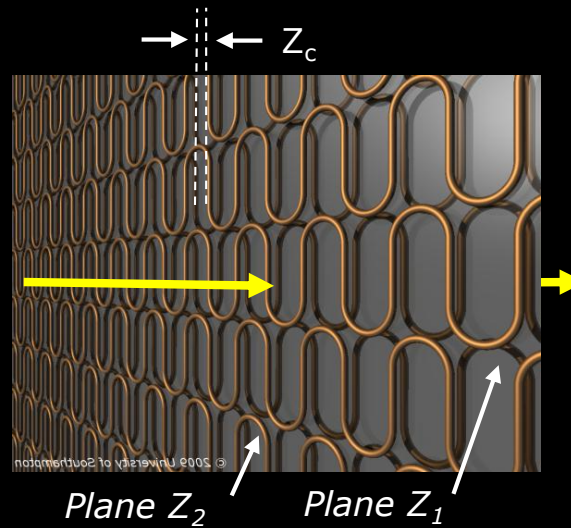
A S Schwanecke<sup>1</sup>, V A Fedotov<sup>1</sup>, V V Khardikov<sup>2</sup>, S L Prosvirnin<sup>2</sup>,  
Y Chen<sup>3</sup> and N I Zheludev<sup>1</sup>

# Metamaterial Analog of EIT (2007)



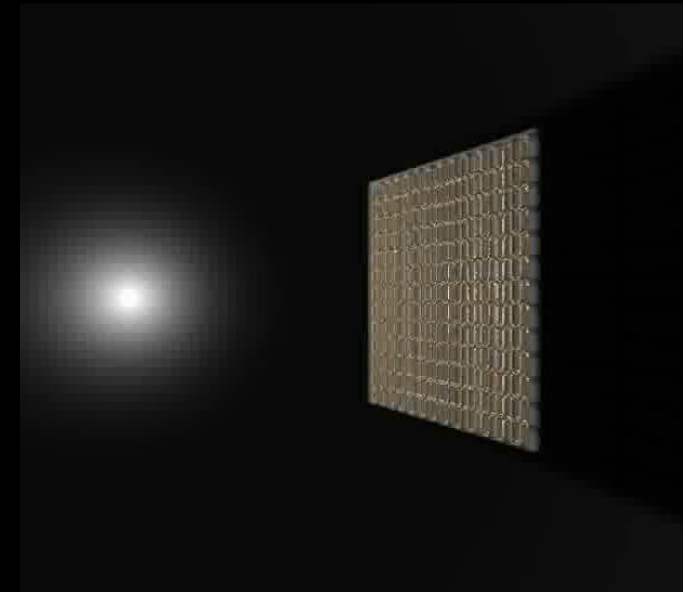
Absorption Losses  $\sim \frac{(\Delta_1 + \Delta_2)^2}{\gamma^2 (\Delta_1 + \Delta_2)^2 + (4\Delta_1\Delta_2)^2}$

Quantum interference of probability amplitudes



Reflection Losses  $\sim \frac{|Z_1 + Z_2|^2}{|Z_c(Z_1 + Z_2) + Z_1 Z_2|^2}$

Classical interference of electromagnetic fields



Slow light in metamaterials

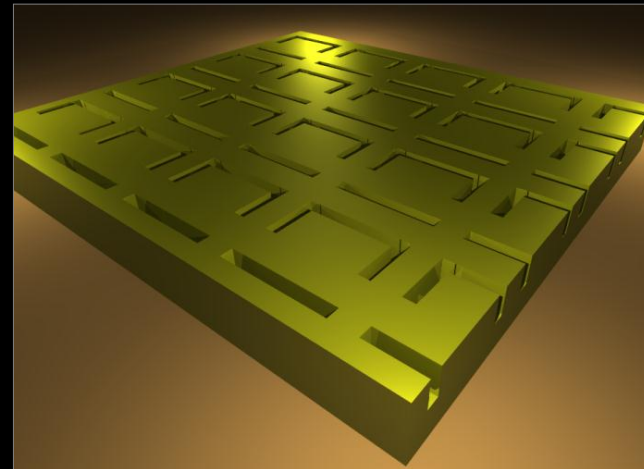
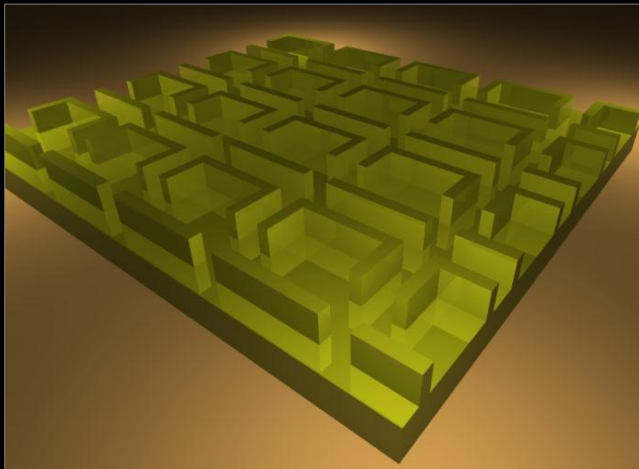
# New classes of metamaterial: Bas-relief & Intaglio (2010) (Continuous metallic metamaterials)



Bas-relief: Pattern raised above surface of the same material

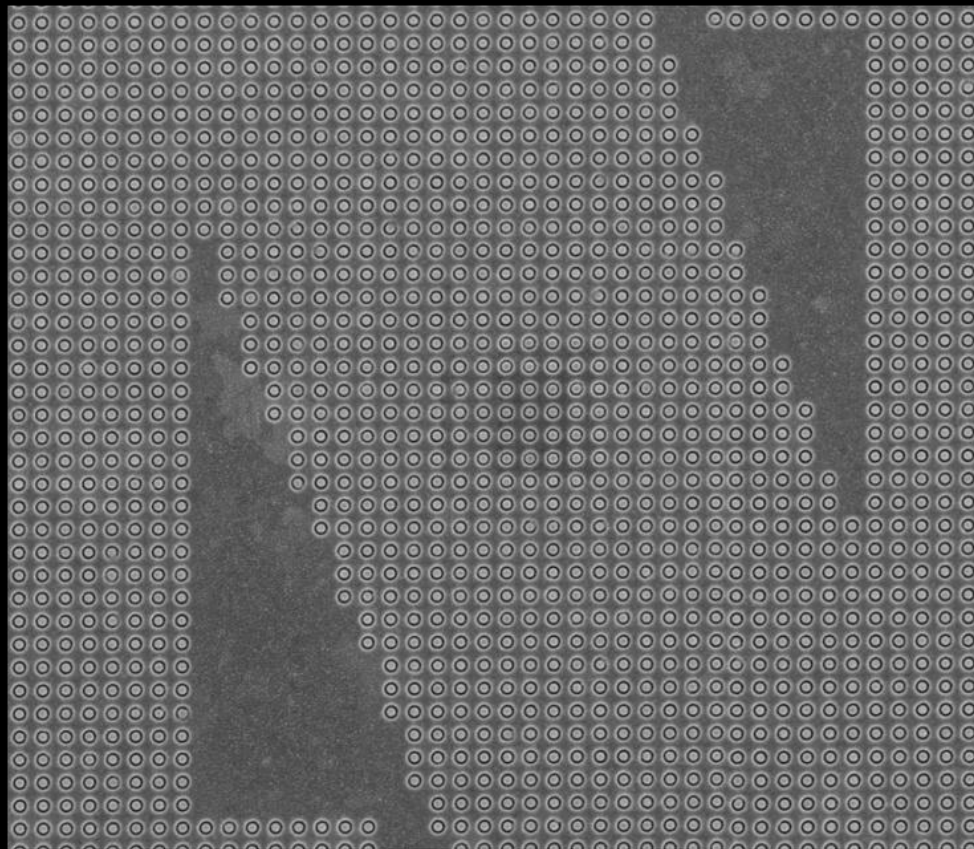
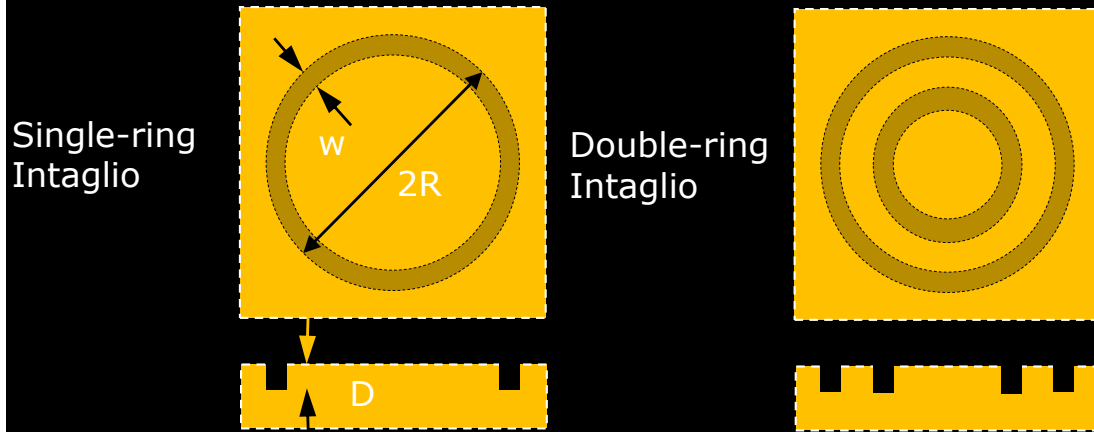


Intaglio: Pattern inscribed in (not cut through) surface



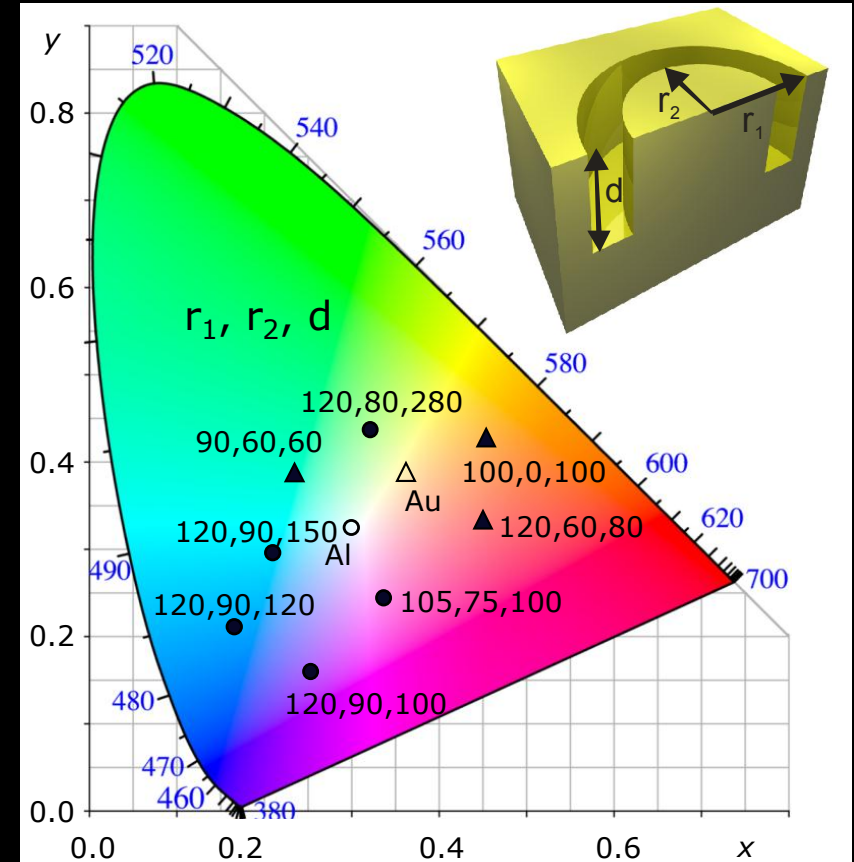


# Bas-relief & Intaglio Metamaterials: Colour by design

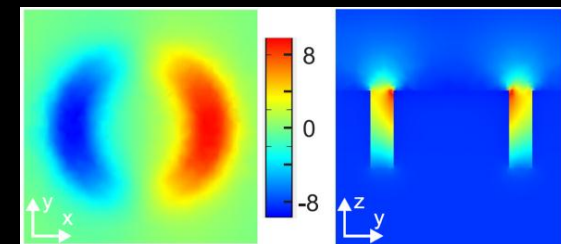


curr	det	HV	mag	WD	HFW	4 $\mu\text{m}$	
86 pA	TLD	5.00 kV	10 000 x	4.1 mm	12.8 $\mu\text{m}$	Helios 600	

International Commission on Illumination CIE1931 colour space chromaticity diagram



Plasmonic mode in intaglio Metamaterial





## **Would it be nice to have ...?**

Tuneable magnetic mirror (for spectroscopy ...)

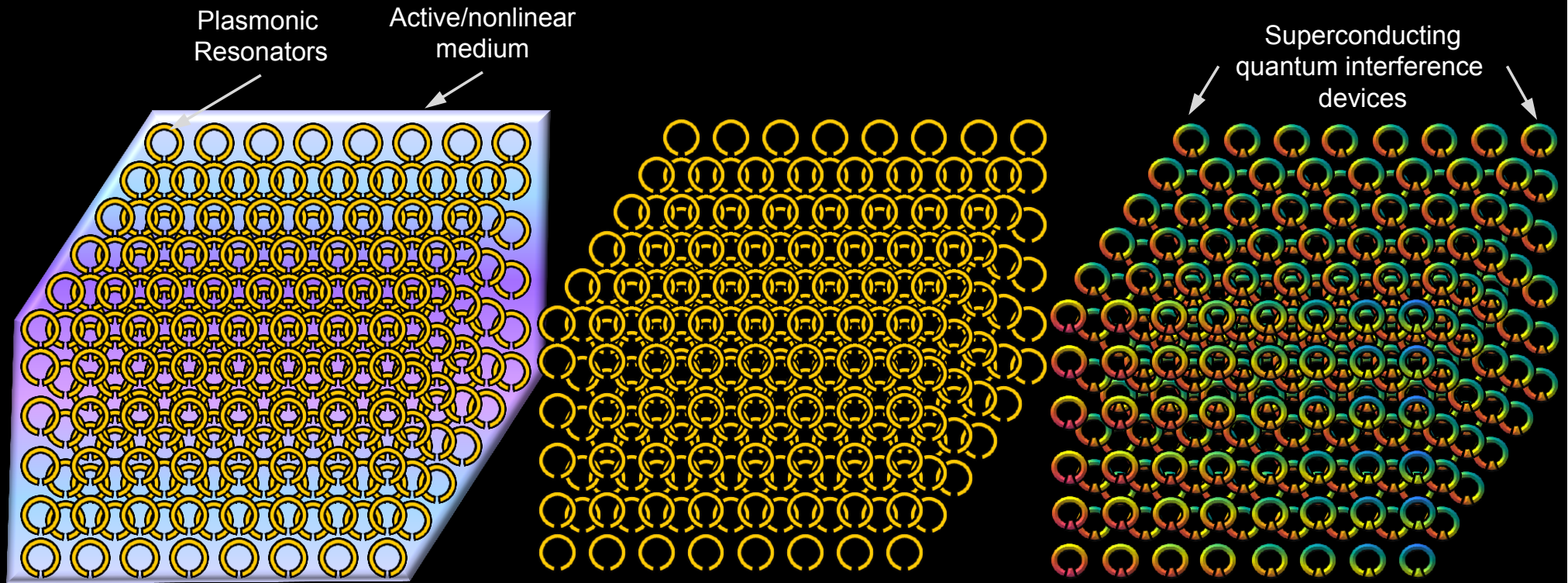
Tuneable delay line (for telecoms ...)

Tuneable colour (for my watch dial ...)

Tuneable spectral filter (for my camera ...)



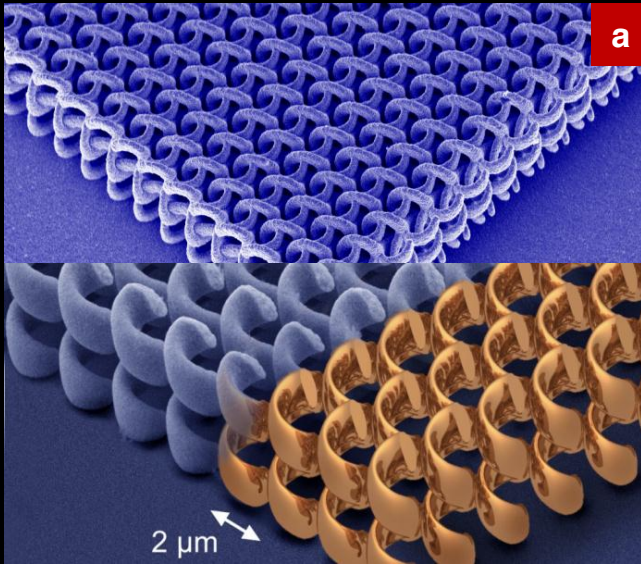
# Metamaterials: mimicking Nature, step 2



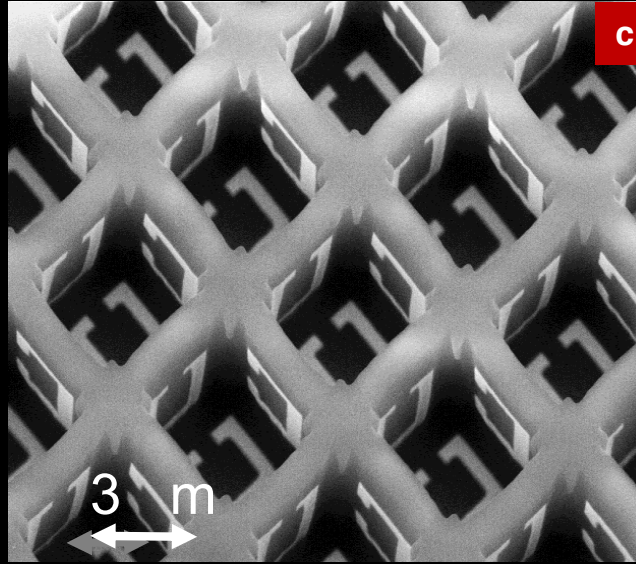
Electromagnetic  
Metamaterial

Reconfigurable  
metamaterial

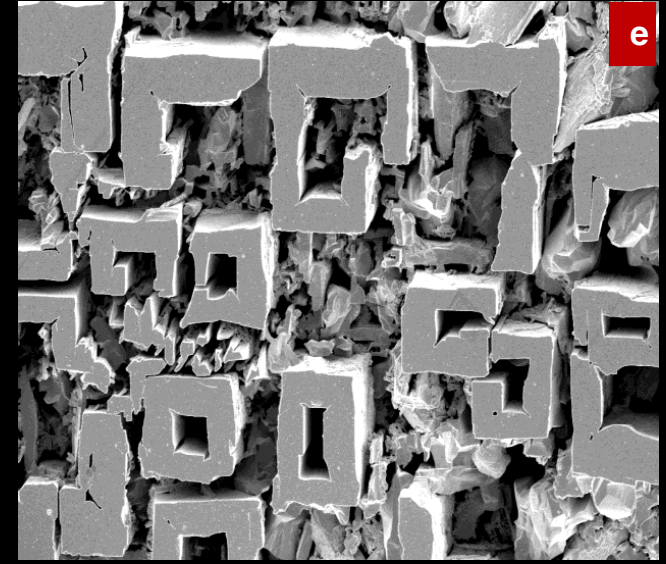
"Quantum"  
Metamaterial



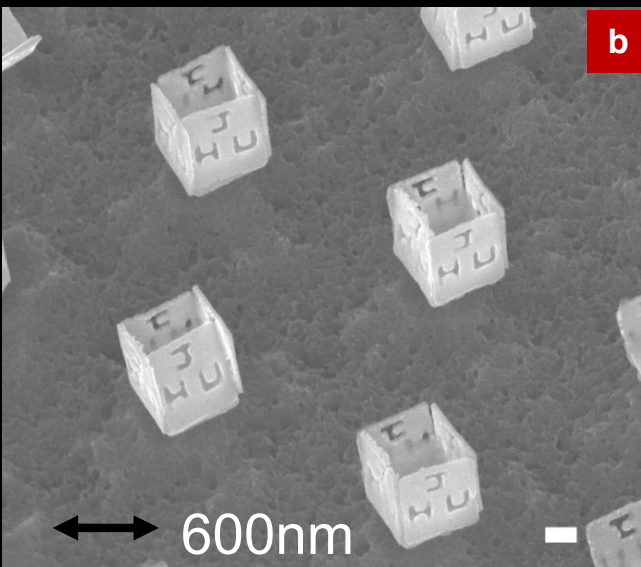
Laser Lithography,  
Stuttgart & Karlsruhe



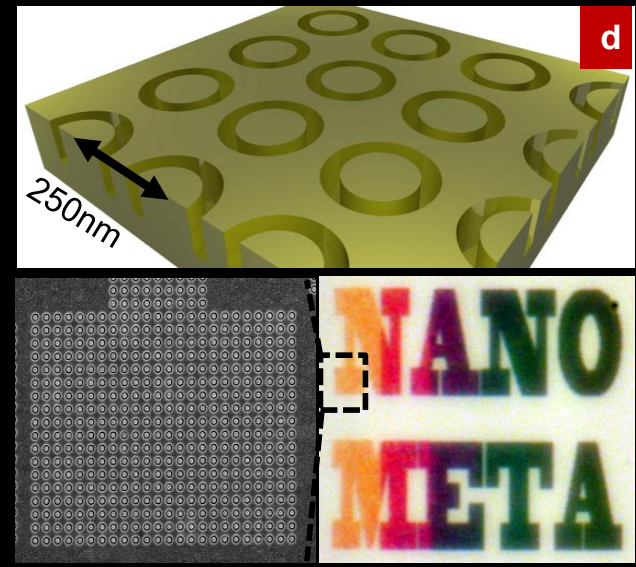
Projection lithography,  
Sandia



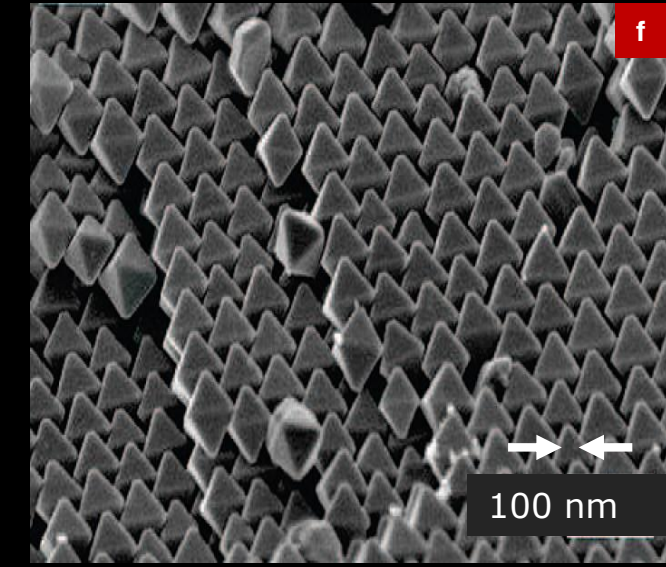
Directional solidification of eutectic,  
IEM, Warsaw



Self-assembled hinged pattern,  
John Hopkins

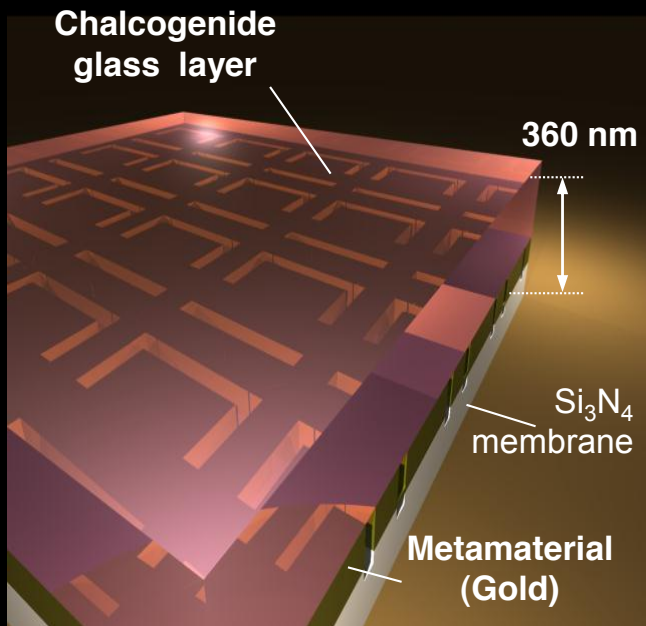


"Intaglio" all-metal metamaterial,  
Southampton

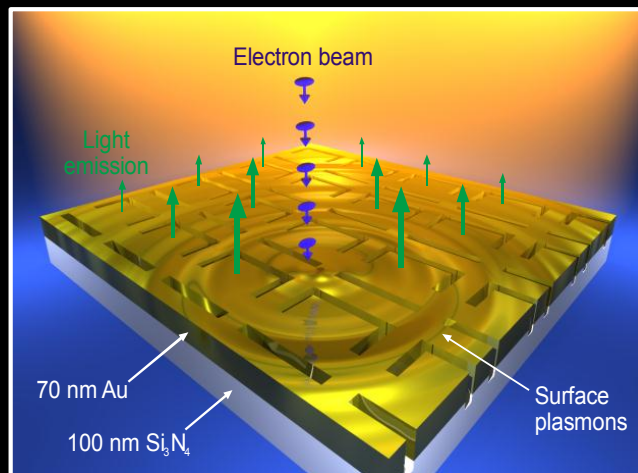


Colloidal nanocrystal arrays,  
Berkeley

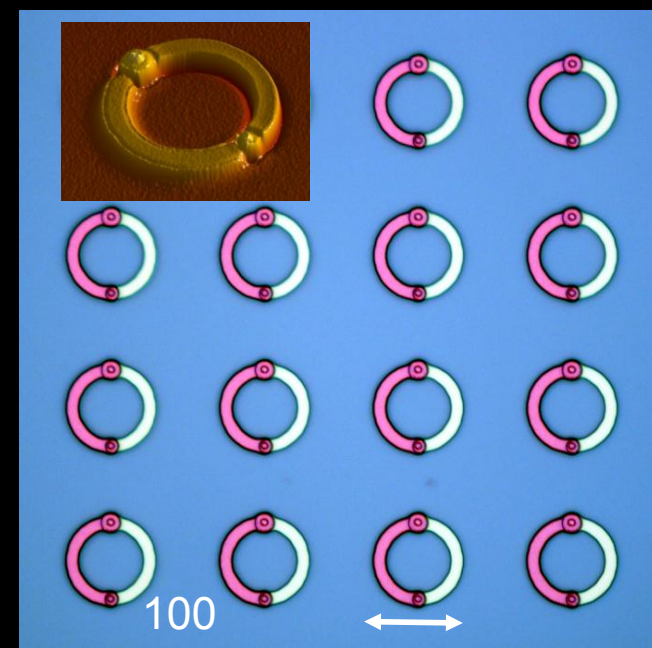




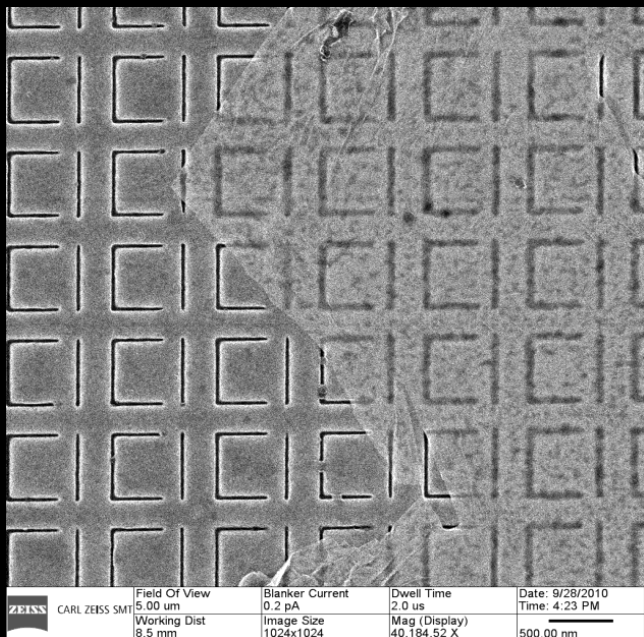
Switchable metamaterial (ChG),  
Southampton



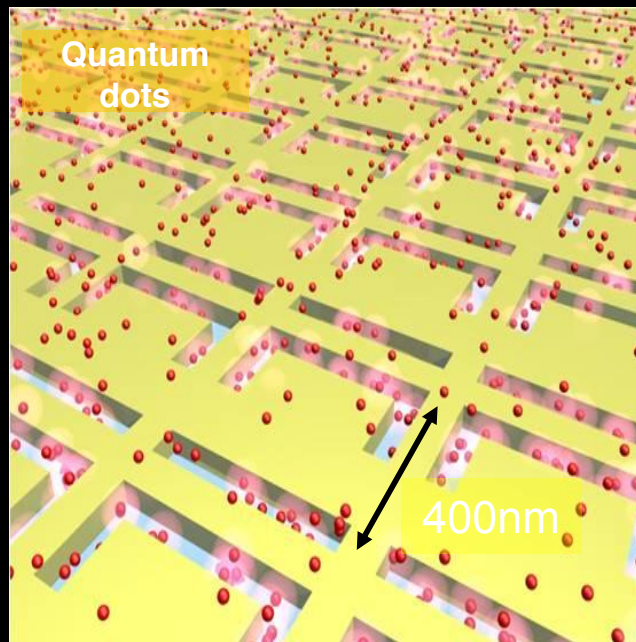
Electron-beam driven light source  
Southampton



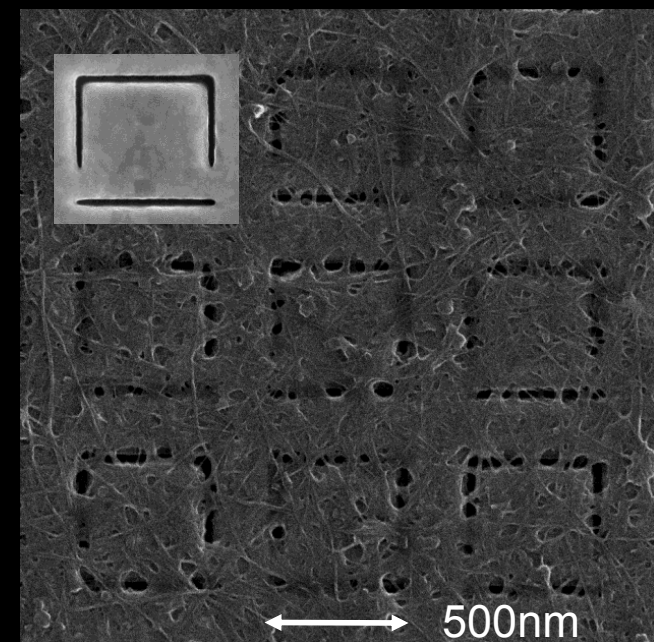
Quantum metamaterial,  
Southampton



Nonlinear metamaterial & Graphene  
Southampton & NTU, Singapore



Switchable metamaterial (QDs),  
Southampton



Nonlinear metamaterial (CNTs),  
Southampton

# MEMS & NEMS reconfigurable Metamaterials

## **Switchable & tuneable metamaterials**



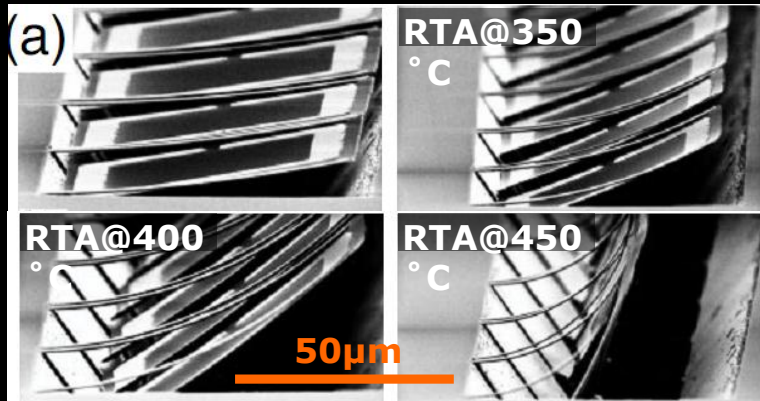
**Goal:**  
switchable and  
controllable  
properties

**Applications:**  
modulators,  
adaptable surfaces



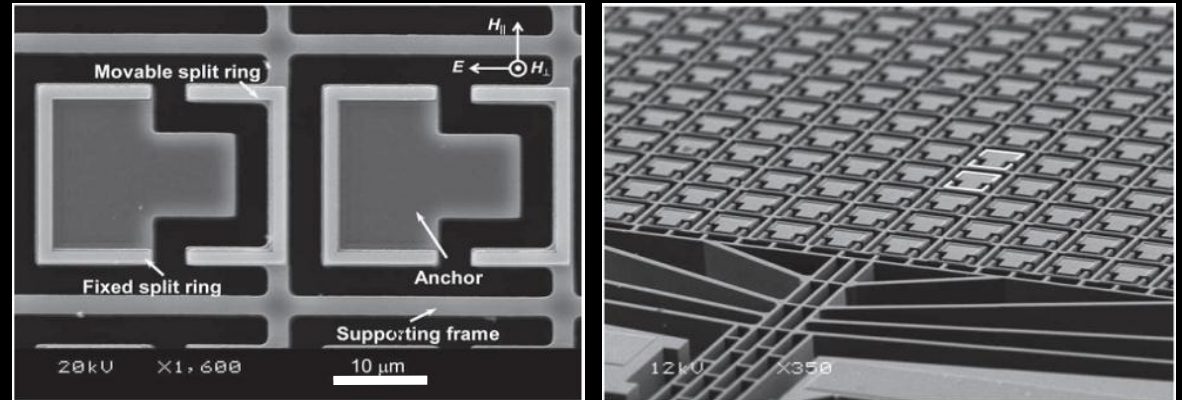
# Reconfigurable Metamaterials

Rapid thermal annealing



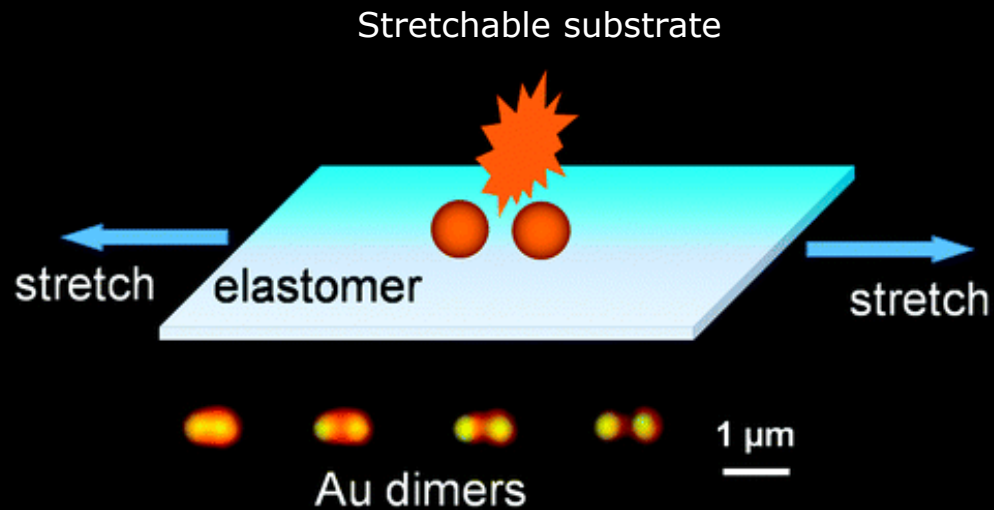
H. Tao, Padilla, Averitt et al (2009)

MEMS reconfigurable meta-molecules



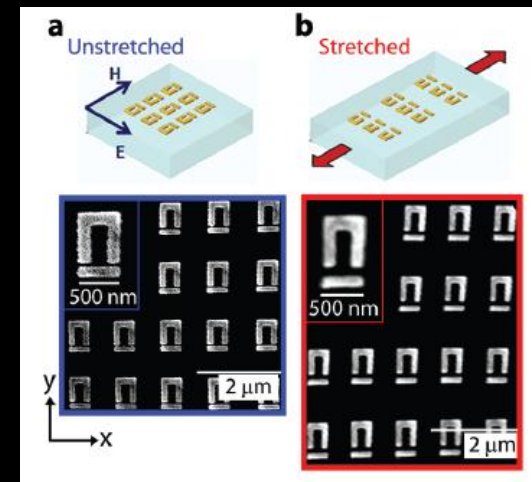
W.M. Zhu, Ai Qun Liu et al. (2011)

Nanoscale features & movements are required for photonic metamaterials



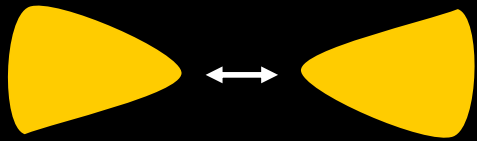
Huang & Baumberg (2010)

Stretchable substrate

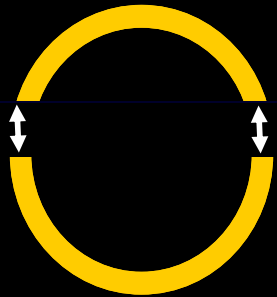


Pryce, Atwater et al. (2010)

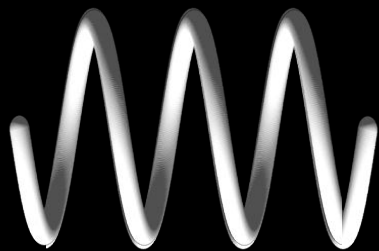
# From controlling meta-molecules to controlling arrays



Tunable nano-Antenna

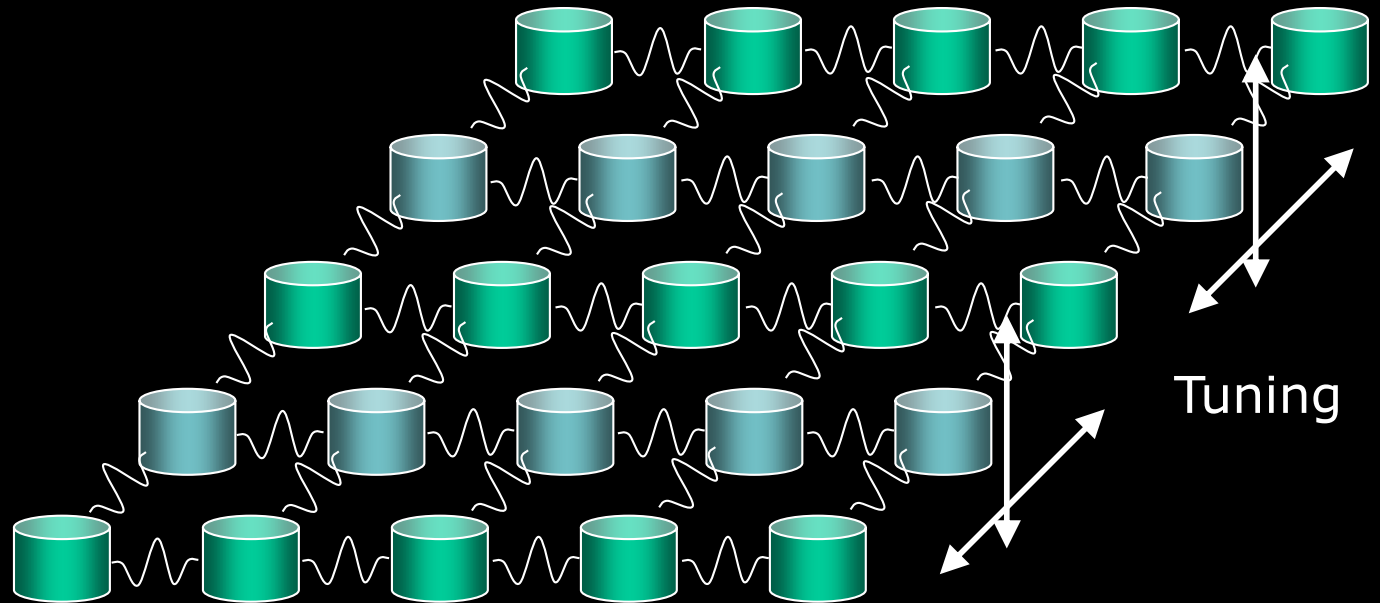


Tunable split-ring



Chiral meta-molecule

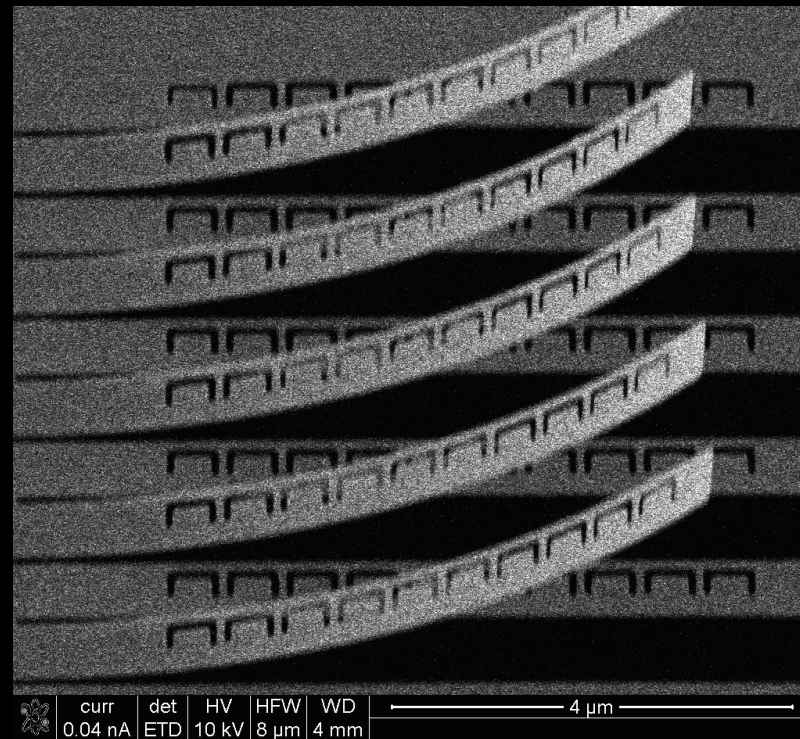
Meta-molecular spacing  
controls optical properties



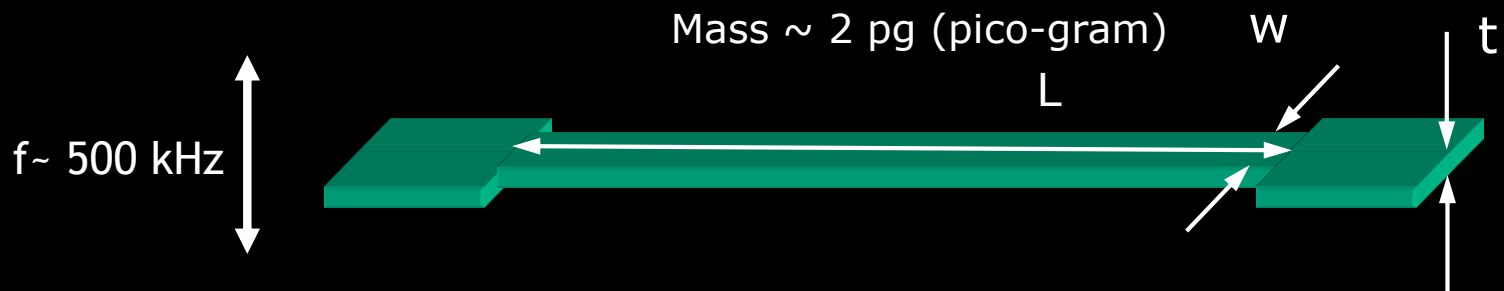
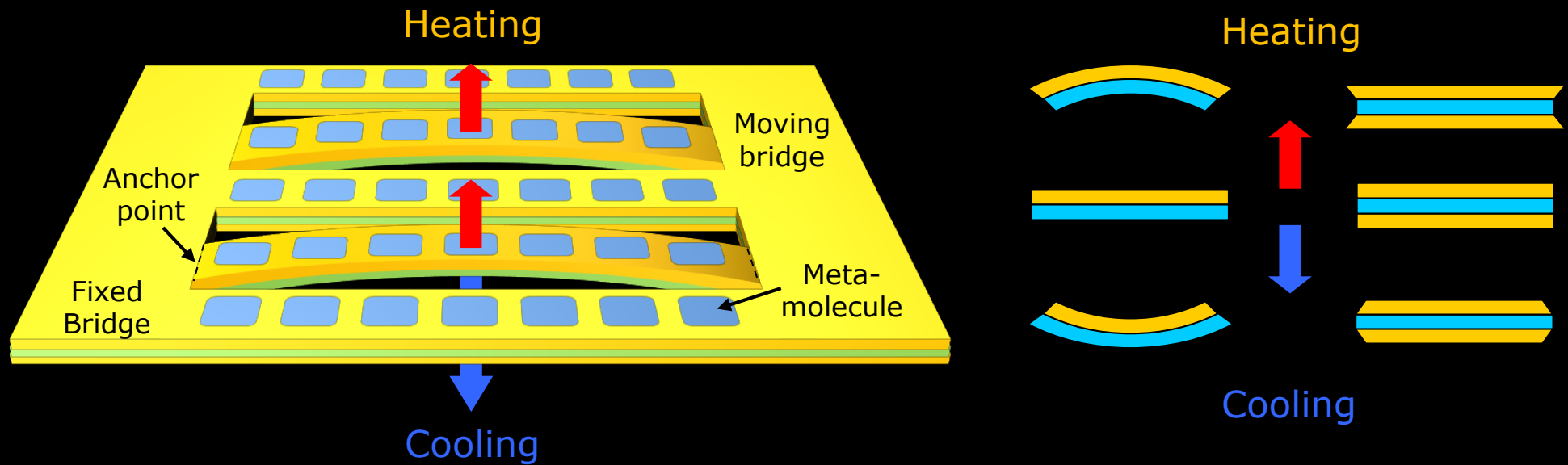
Tuning



# Temperature-Controlled Photonic Metamaterials



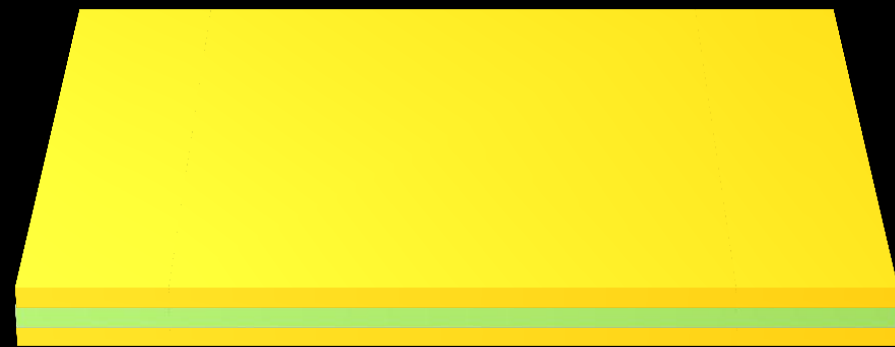
# Temperature-Controlled RPMs: Concept



Mechanical resonance frequency:  
 Silicon nitride bridge  
 $L = 25\mu\text{m}$ ;  $t = 50\text{nm}$ ;  $E = 260$  GPa,  $\rho = 3.44$  g/cm<sup>3</sup>

$$f = \frac{1}{2\pi} \frac{t}{l^2} \sqrt{\frac{185 E}{12 \rho}}$$

# Temperature-Controlled RPM: Fabrication



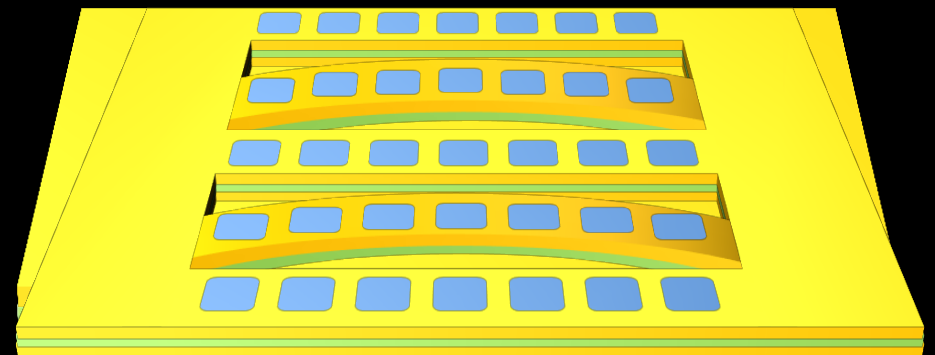
Au on both sides of Si<sub>3</sub>N<sub>4</sub> membrane



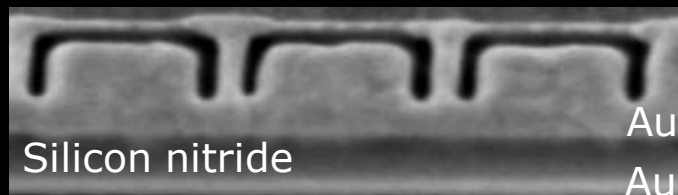
Alternating Gold slits removed by FIB



Flip Sample

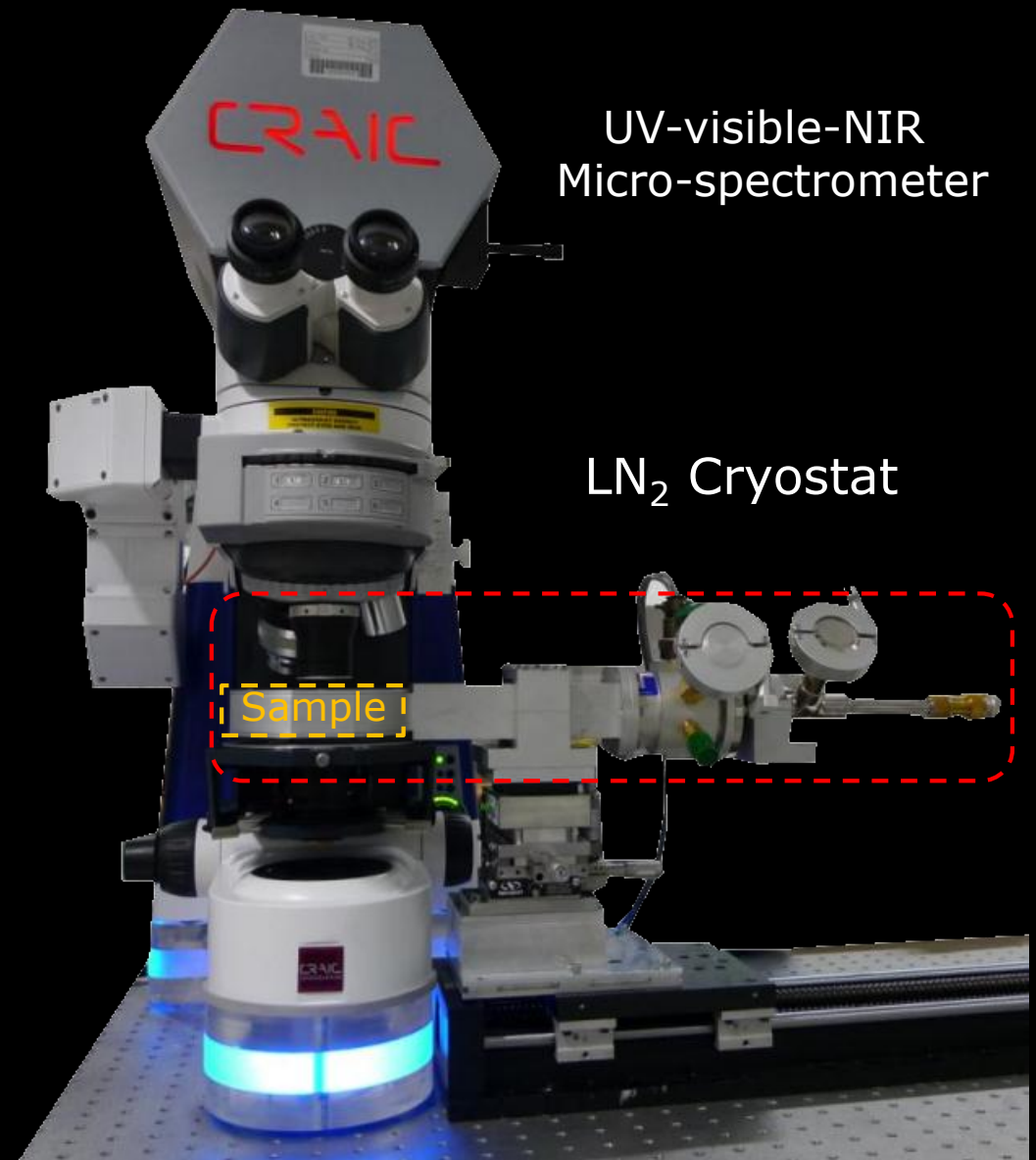
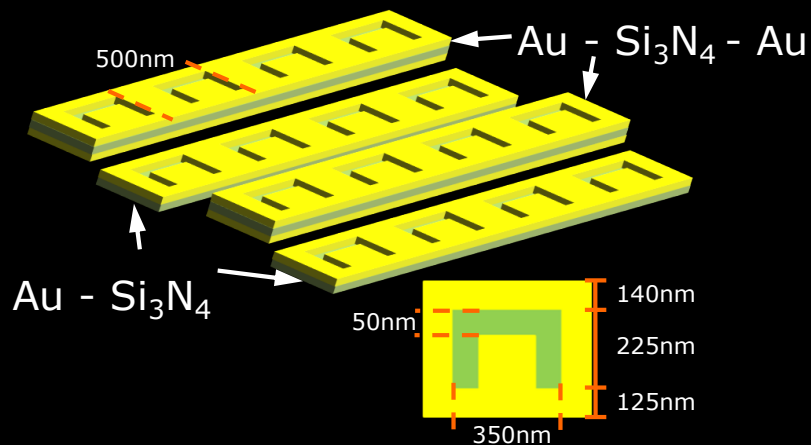
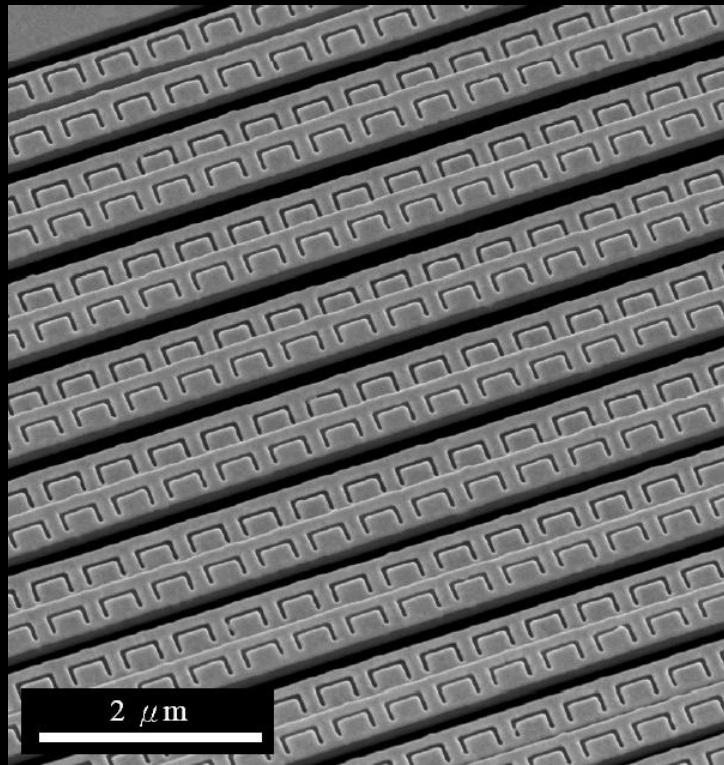


Meta-molecules patterning by FIB  
Bridges cut through

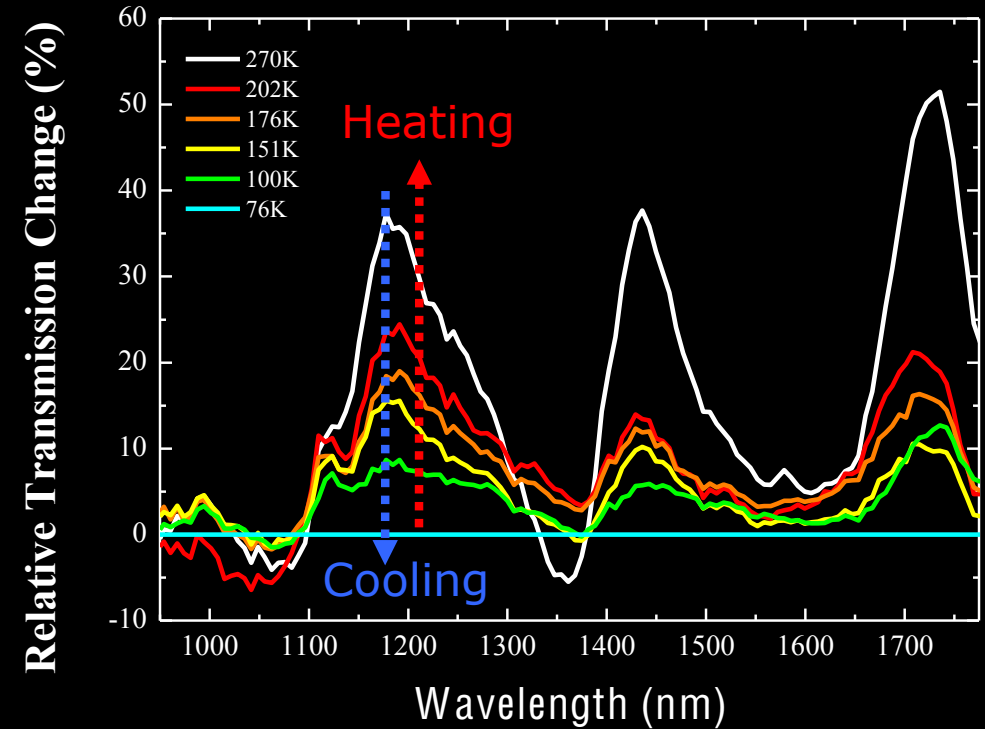
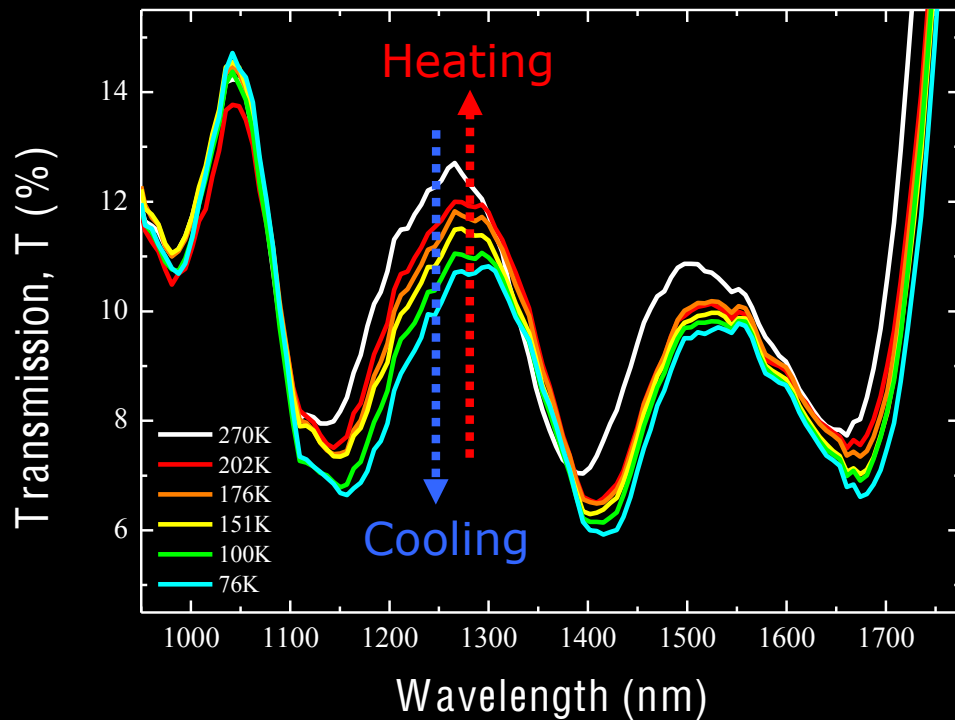




# Temperature-Controlled RPM: Optical Characterization



# Temperature-Controlled RPM: Performance



Reversible continuous tuning by cooling/heating  
Relative changes in transmission up to **50%**

## **Optical Forces in Metamaterials**



### **Goal:**

Controlling adhesion forces

### **Applications:**

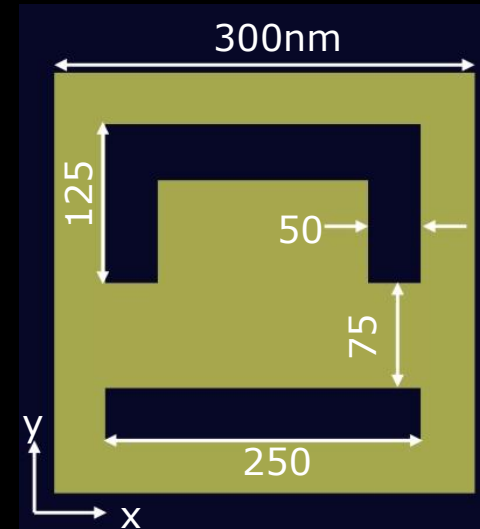
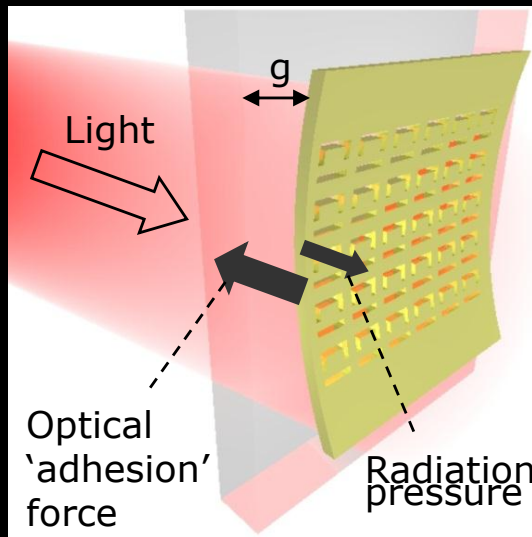
Handling of small objects

# Optical 'Gecko Toe'

Gecko toes

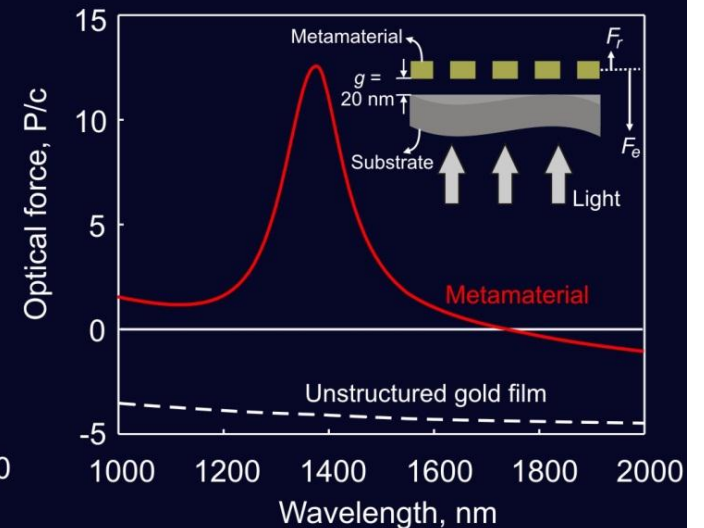
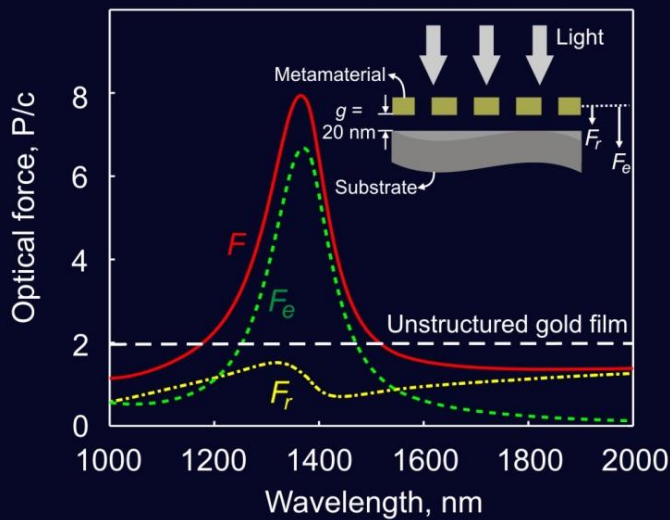
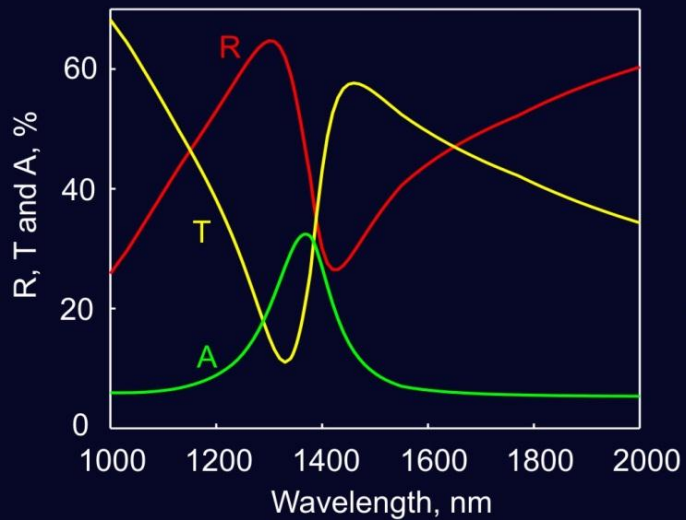


Optical 'adhesion' force



Simulated spectra for y-polarization

Optical force for light impinges from air side and through substrate





# Nonlinear & Switchable Metamaterials



## Applications:

all-optical data processing

telecom switching

data storage

Displays

Lasers (modelocking/q-switching)

Optical limiting and conditioning



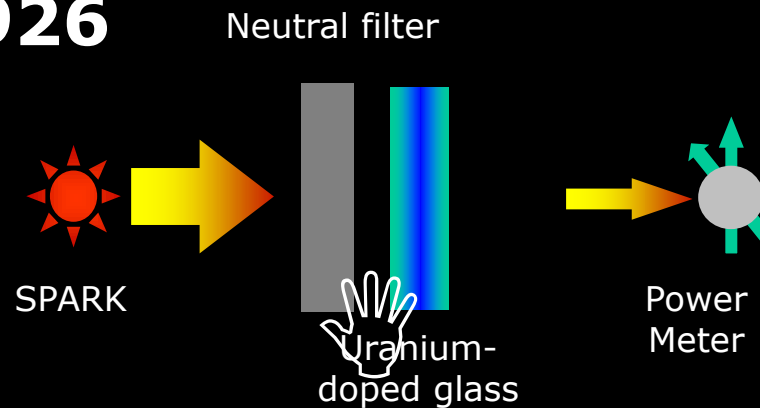
# Violation of the Superposition Principle



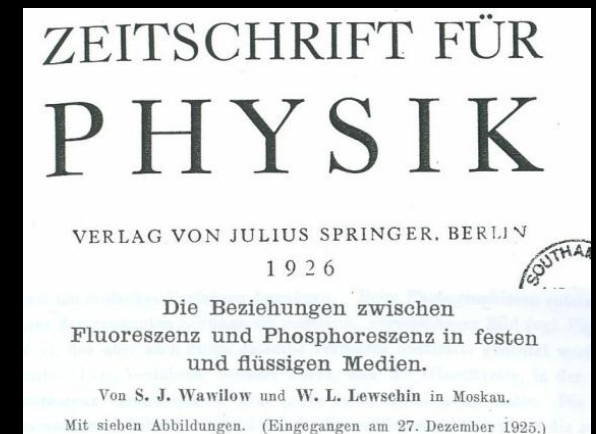
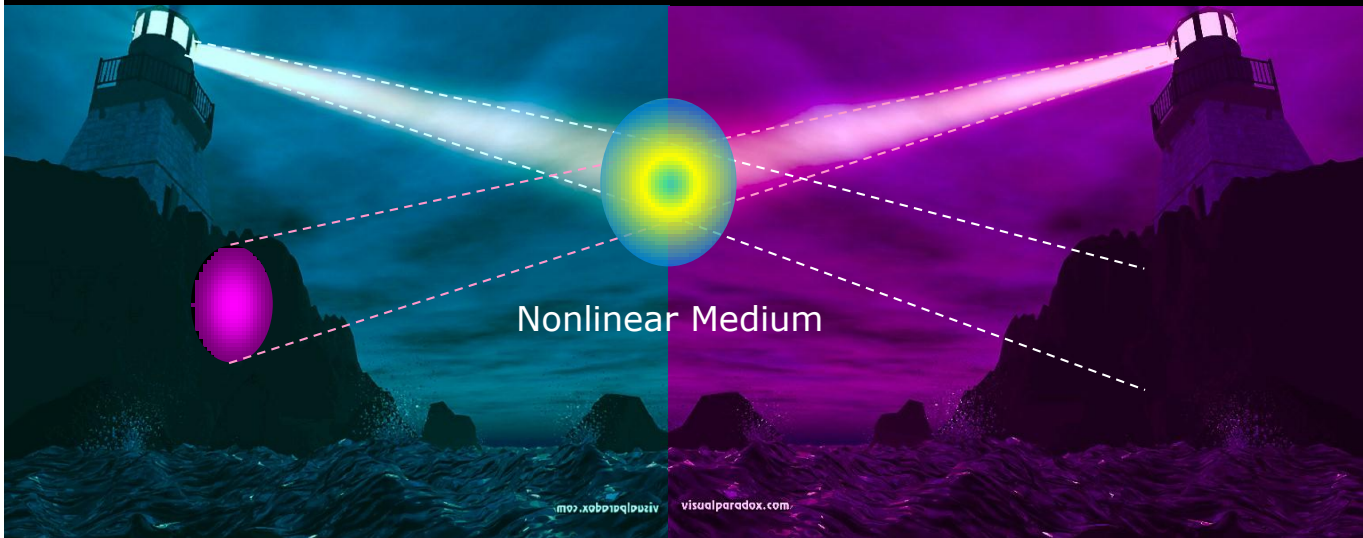
Christian Huygens  
1629 - 1695

"The most remarkable property of light is that light beams travelling in different and even opposite directions pass through one another without mutual disturbance"  
"Abhandlung über das Licht" 1678

1926

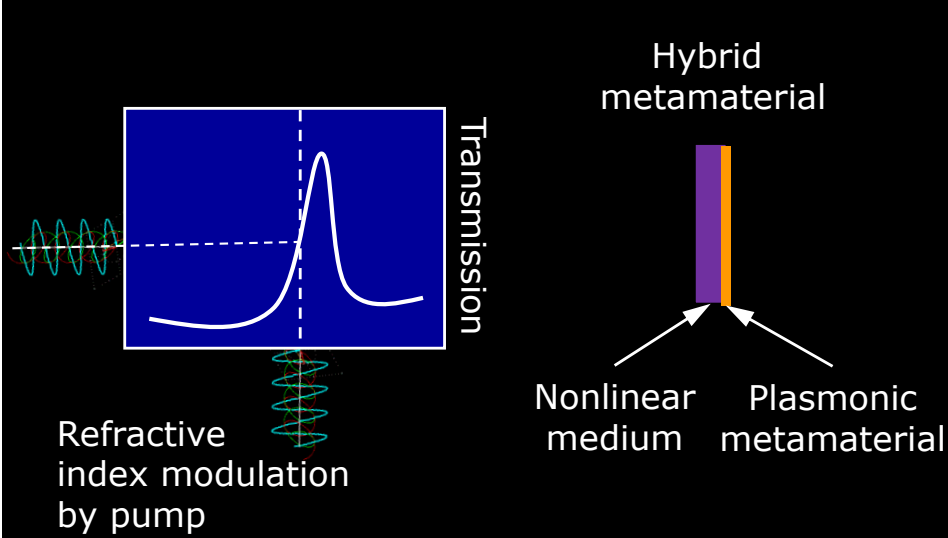


V.L. Levshin (1896-1969)  
& S.I. Vavilov (1891-1951)

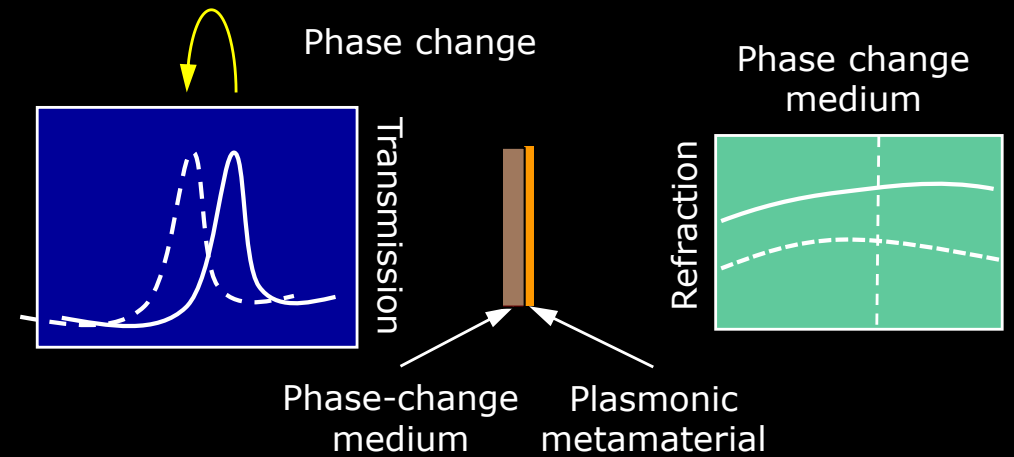


# Giant nonlinearity and switching with photonic metamaterials

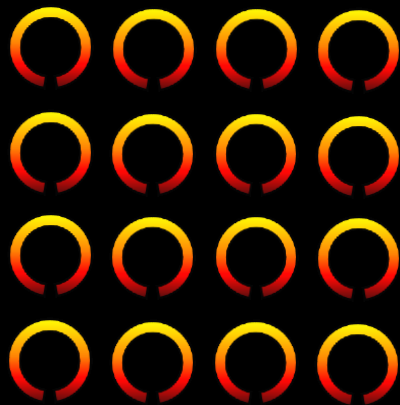
## Resonant enhancement of nonlinearity In Metamaterials



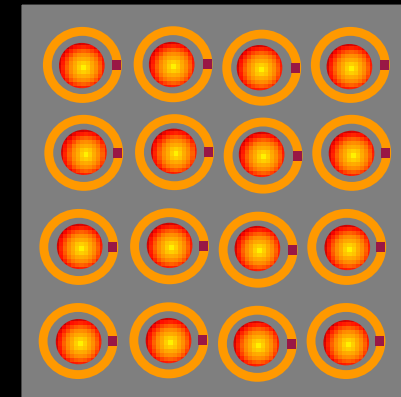
## Phase Change Metamaterials



## Reconfigurable MM



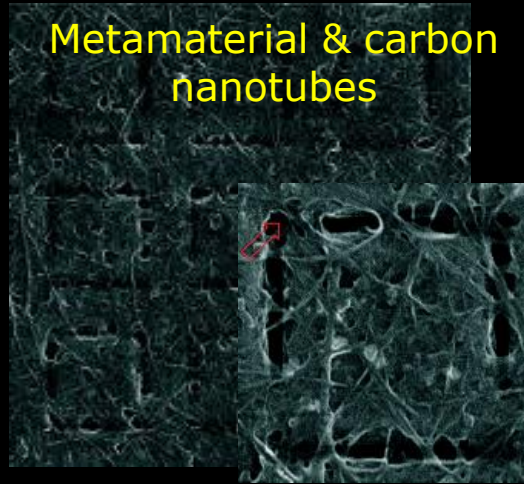
## Flux quantization MM Josephson SQIDs



Quantum-level nonlinearity

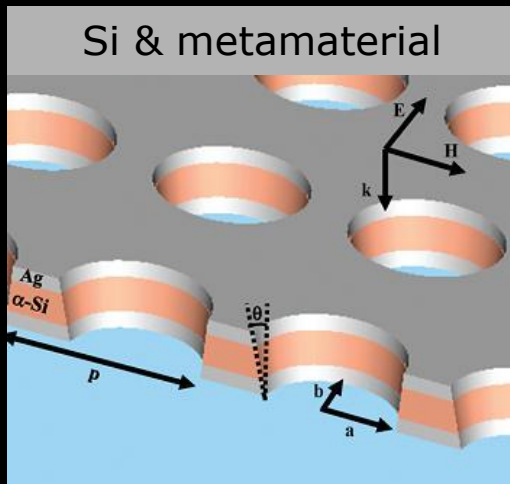
# Plasmonic enhanced cubic nonlinearity

Metamaterial & carbon nanotubes

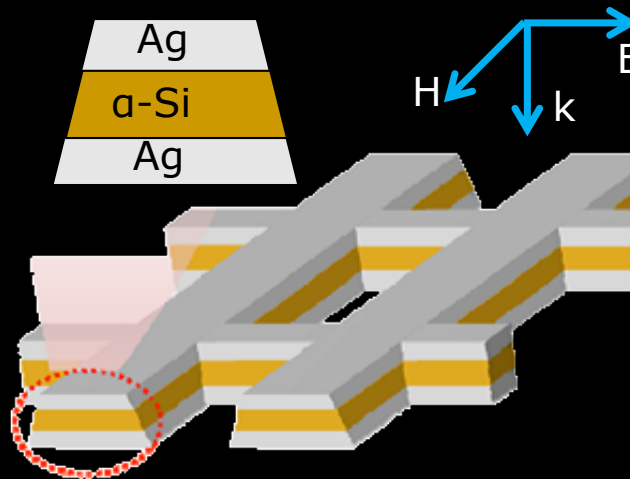
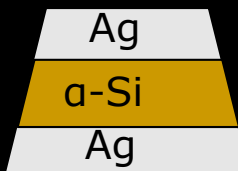


Nikolaenko, Angelis, Boden, Papasimakis, et. al. Phys. Rev. Lett. 104, 153902 (2010)

Si & metamaterial

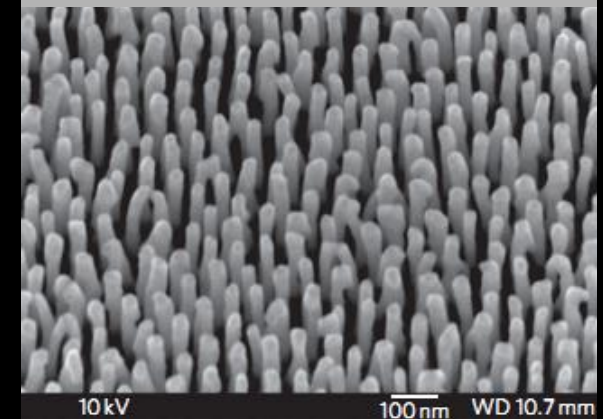


Dani, Ku, Upadhya, Prasankumar, Brueck, Taylor Nano Lett. 9, 3565 (2009)



Cho, Wu, Ponizovskaya, Chaturvedi, Bratkovsky, Wang, Zhang, Wang and Shen Opt. Express 17, 17652 (2009)

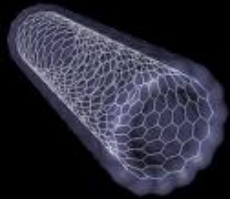
Gold nanorods



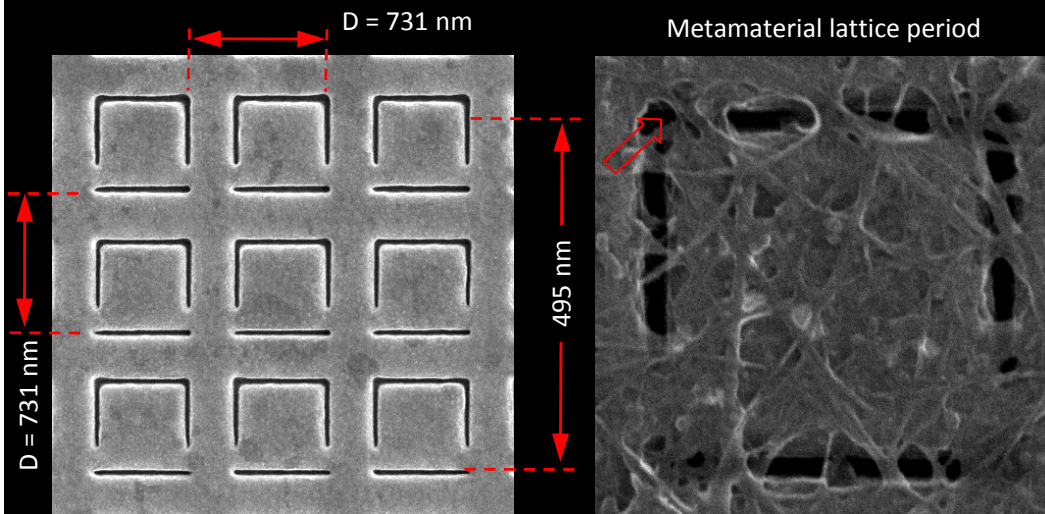
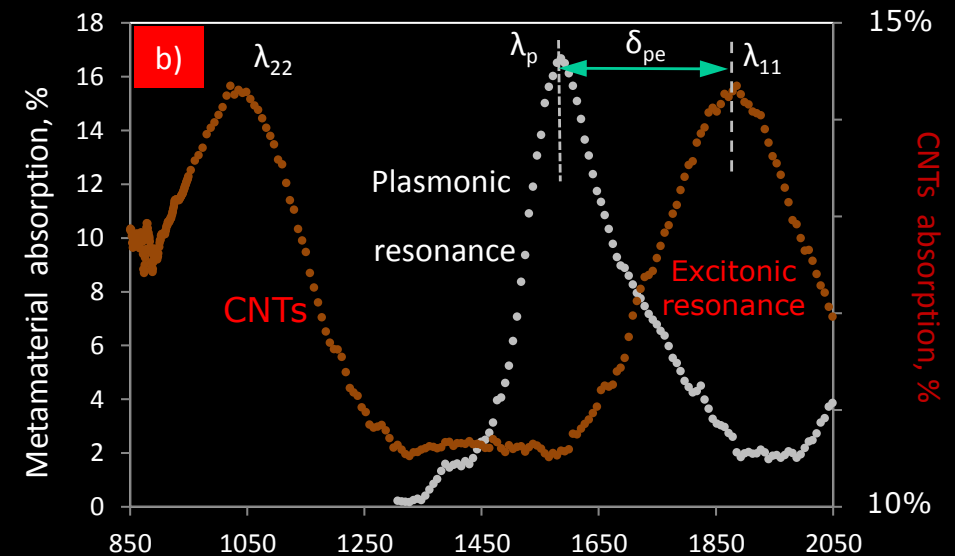
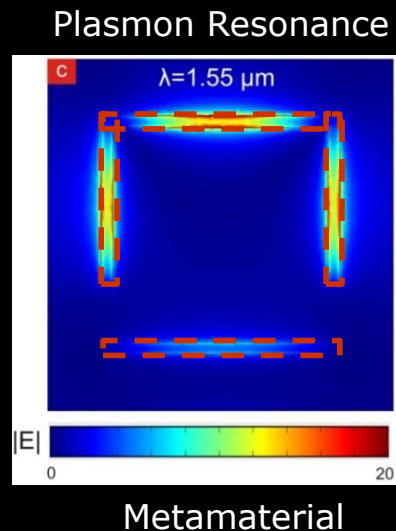
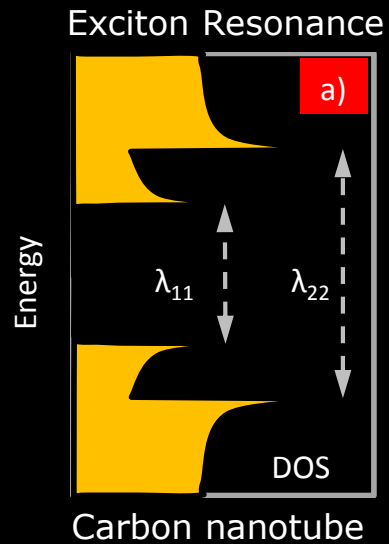
Wurtz, Pollard, Hendren, Wiederrecht, et. al. Nat. Nanotech. 6, 107 (2011)



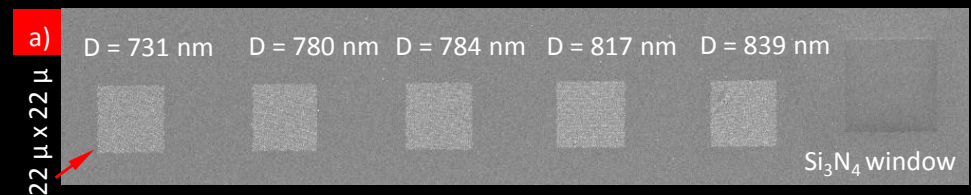
# Ultrafast Nonlinear Metamaterials with Carbon Nanotubes through plasmon- exciton coupling



Plasmonic & Excitonic absorption lines



Combinatorial approach to metamaterials research

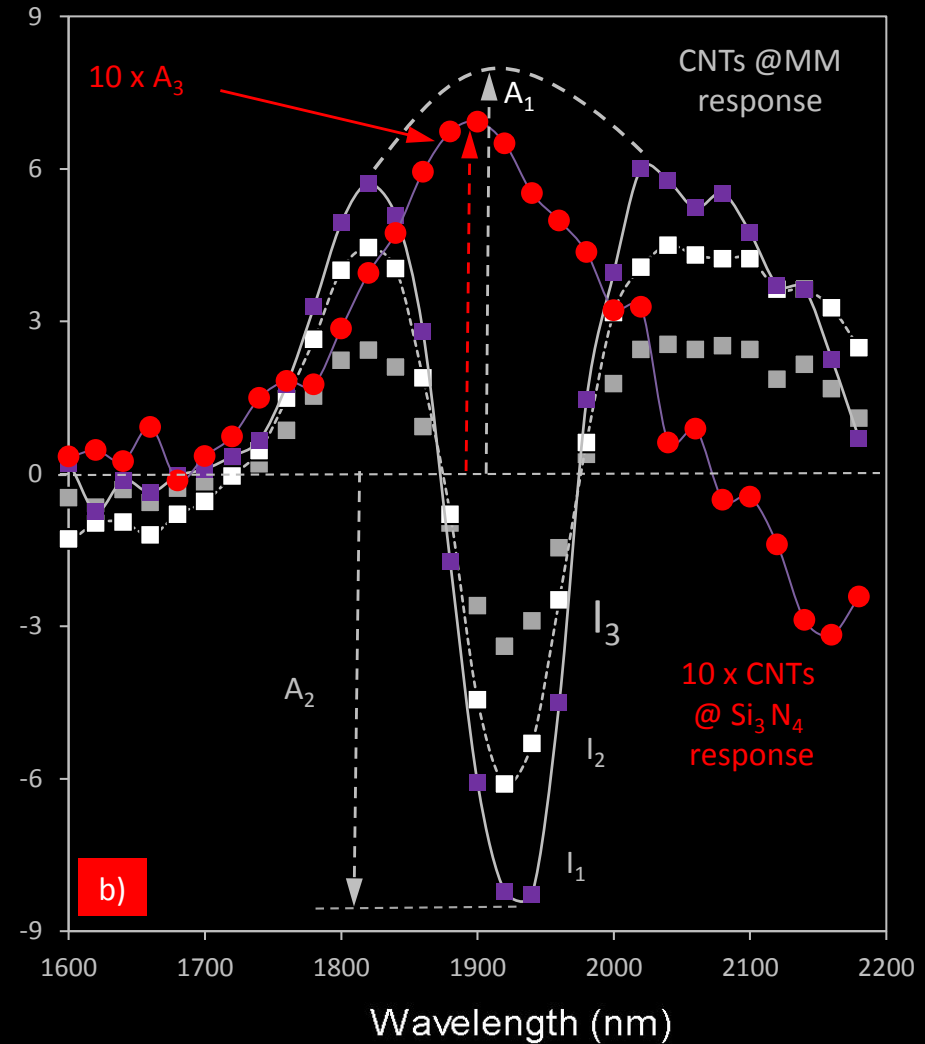
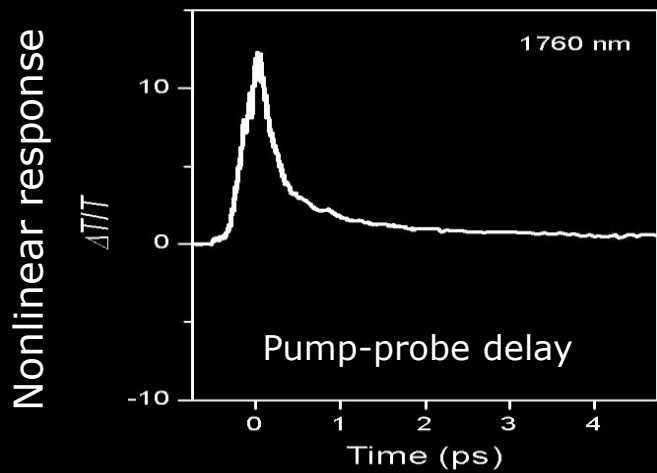
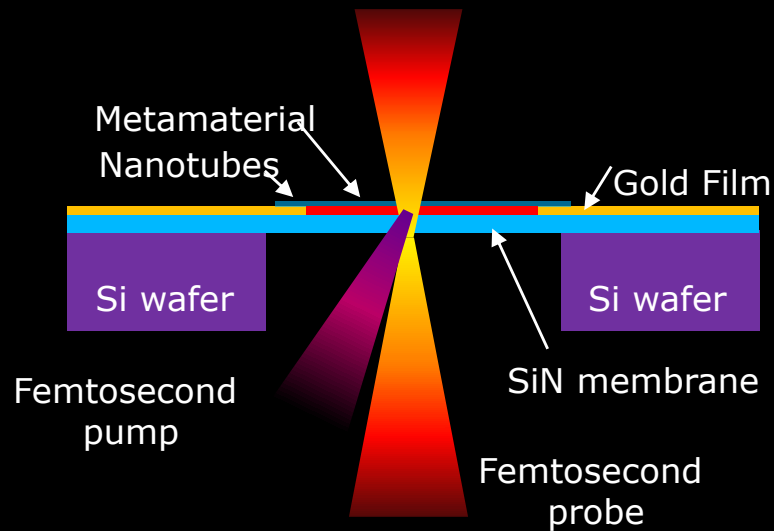


PRL 104, 153902 (2010)   PHYSICAL REVIEW LETTERS   week ending 16 APRIL 2010

## Carbon Nanotubes in a Photonic Metamaterial

Andrey E. Nikolaenko,<sup>1</sup> Francesco De Angelis,<sup>2</sup> Stuart A. Boden,<sup>3</sup> Nikitas Papisimakis,<sup>1</sup> Peter Ashburn,<sup>3</sup> Enzo Di Fabrizio,<sup>2</sup> and Nikolay I. Zheludev<sup>1</sup>

# Giant Nonlinearity through plasmon-exciton coupling



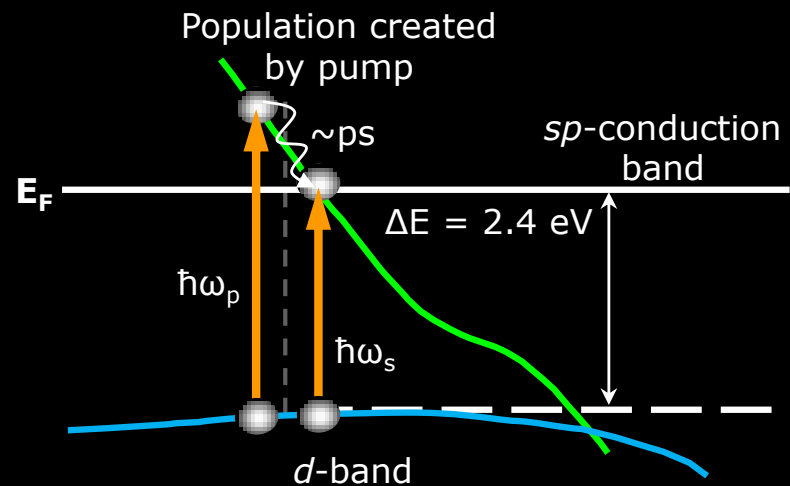
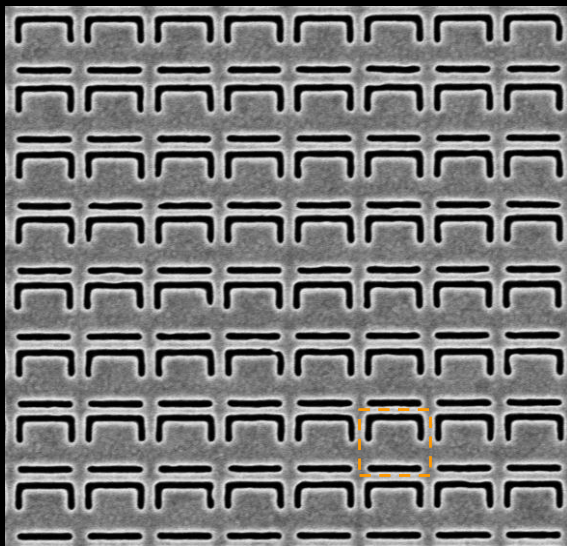
System	% T modulation	Fluence, $\mu J/cm^2$	Response time, fs	J x fs/cm <sup>2</sup>
Metamaterial + CNTs PRL,104, 153902 (2010)	<b>10 %</b>	<b>40</b>	<b>~500fs</b>	<b>0.02</b>

# Nonlinearity of the Metamaterial's framework



# Gold Nonlinear Metamaterial

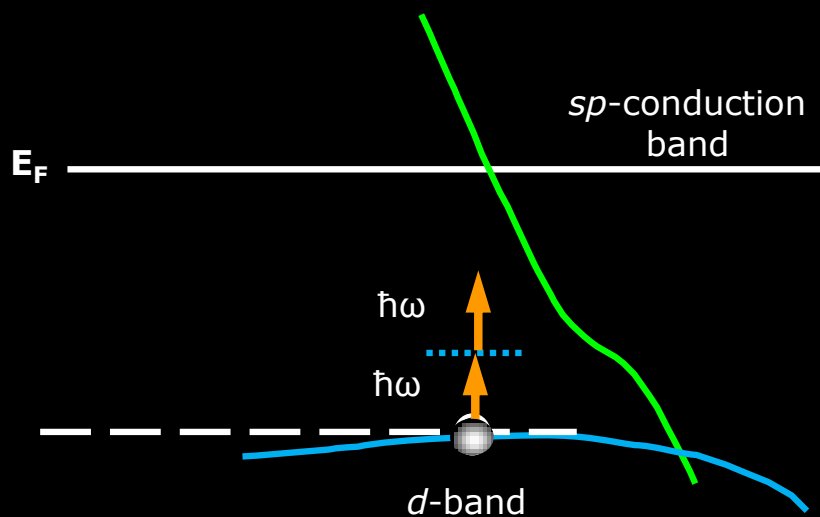
Metamaterial nanostructure



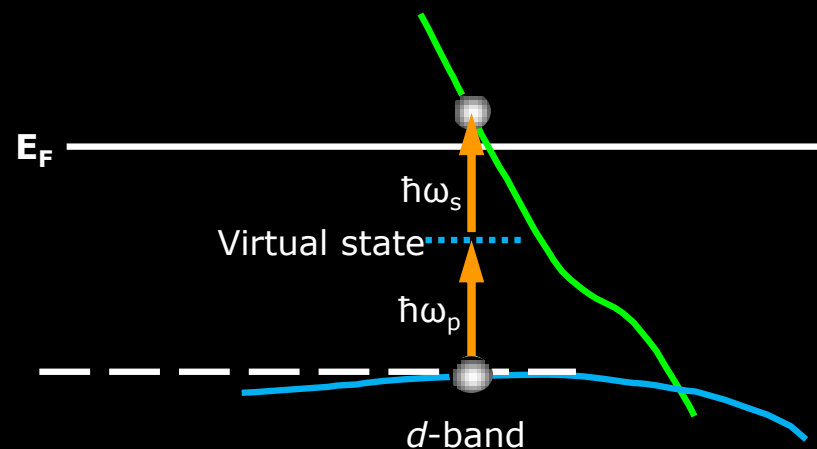
**Fermi Smearing Nonlinearity**  $\hbar\omega \sim 2.4\text{eV}$

$\beta \sim 10^{-5}$  m/W peaking at  $\sim 516$  nm

Few ps response (hot e- thermalization)



**Au Nonlinear Absorption is negligible**  
for  $2\hbar\omega < 2.4\text{eV}$



**Two Photon Absorption nonlinearity**

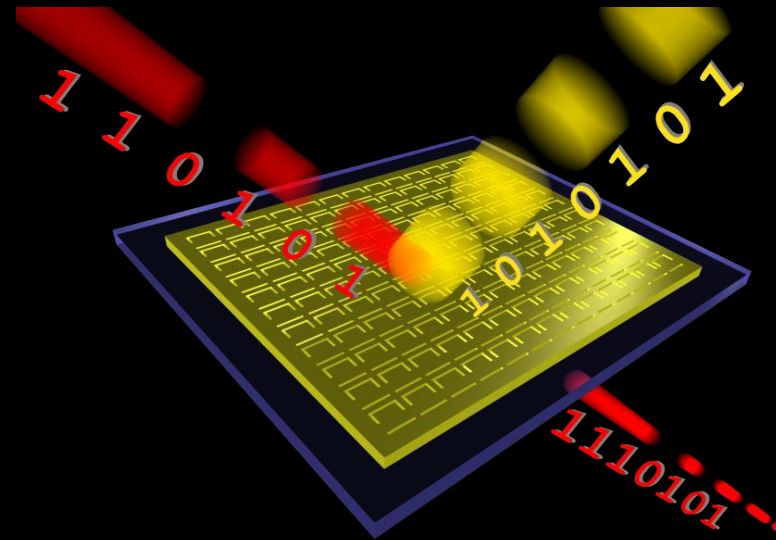
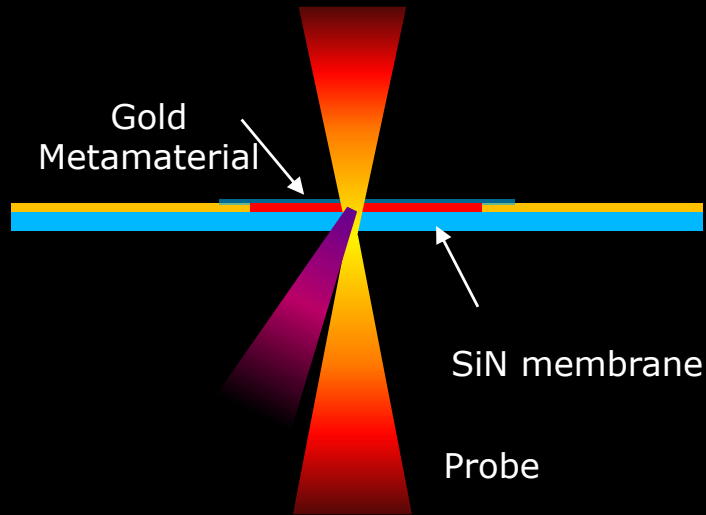
$2.4\text{eV} > \hbar\omega > 1.2\text{eV}$

$\beta \sim 10^{-8}$  m/W, Virtual level lifetime  $\sim 2\hbar/\Delta E < 1$  fs



# Nonlinear Metamaterial: THz optical modulation bandwidth

100fs Z-Scan and Pump-probe



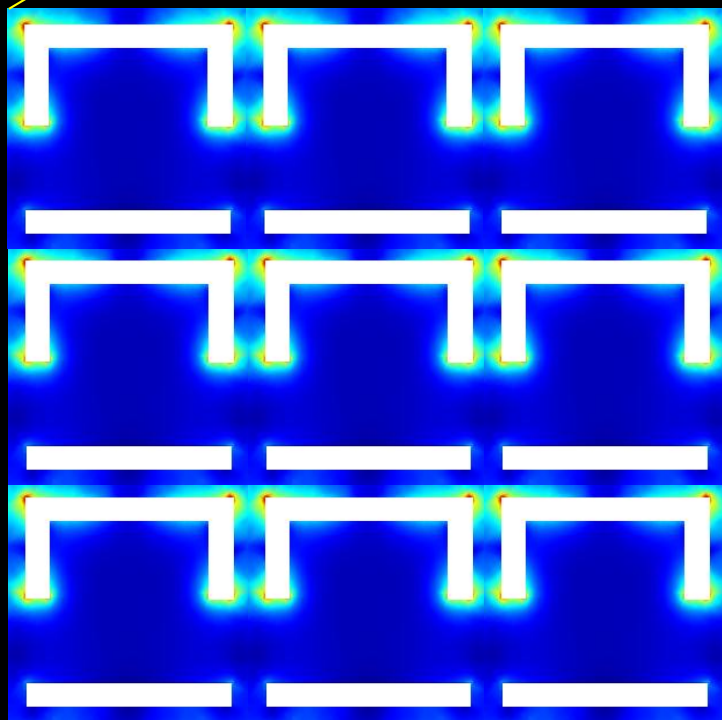
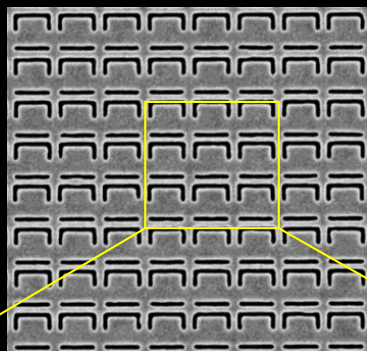
Average Laser power  $\sim 3$  mW

Ren, Zheludev et.al.  
Adv. Mat. DOI: 10.1002/adma.201103162

System	% T modulation	Fluence, $\mu\text{J}/\text{cm}^2$	Response time, fs	J x fs/cm <sup>2</sup>
Gold metamaterial	40 %	270	$\sim 40\text{fs}$	0.01

# Strong Resonant Field Localization (in the metal itself!)

Metamaterial  
nanostructure



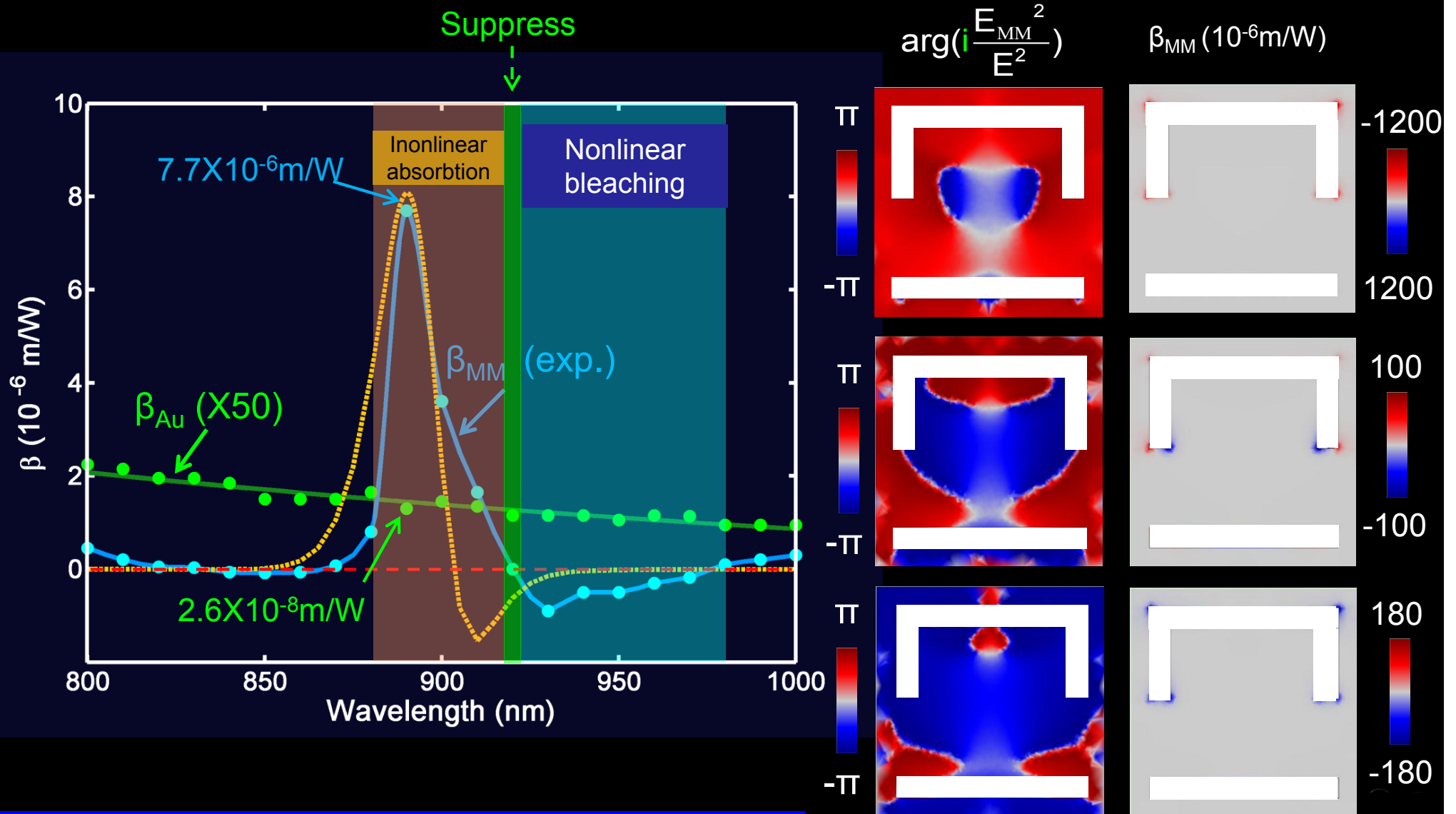
Nonlinear absorption coefficient  
of plasmonic metamaterial

$$\beta_{\text{eff}} = \beta_{\text{Au}} \frac{n^2}{n_{\text{eff}}^2} \text{Re} \left\{ \frac{\int \mathbf{E}_{\text{loc}}^2 |\mathbf{E}_{\text{loc}}|^2 dv}{E_0^2 |E_0|^2 V} \right\}$$

Local field

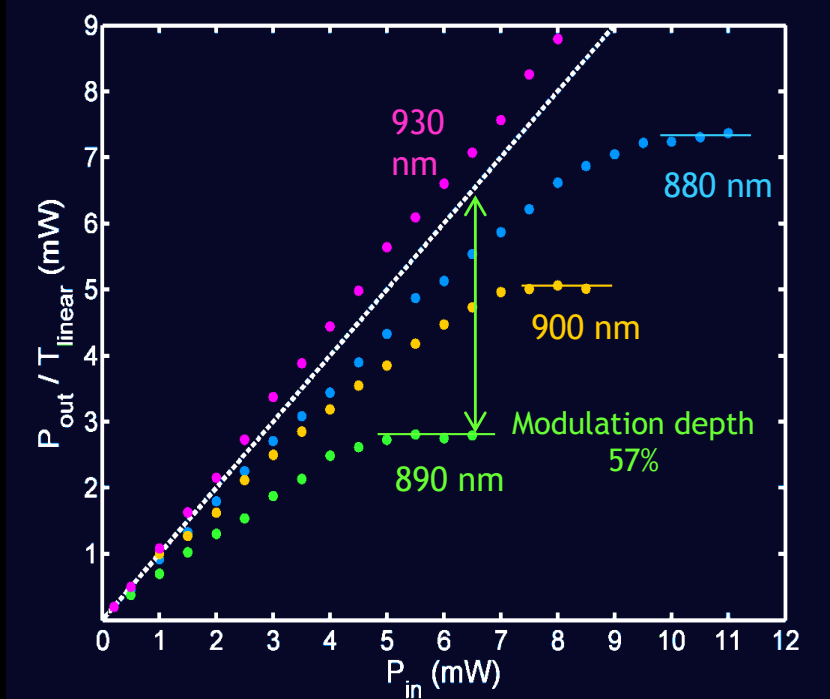
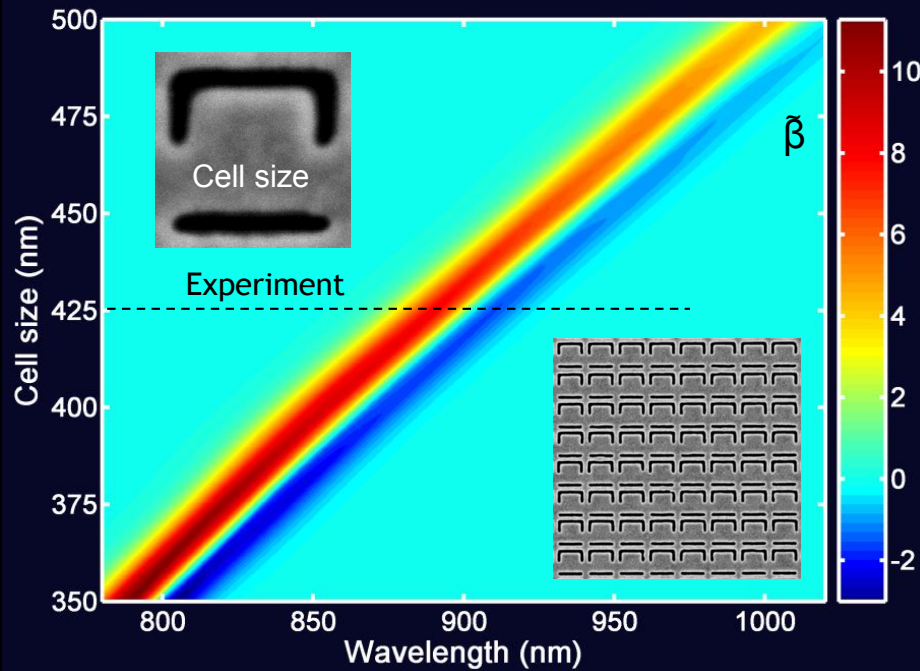
Incident field

# Nonlinearity control: enhancement OR loss compensation



Ren, Jia, Ou, Plum, Zhang, MacDonald, Xu, Gu, Nikolaenko,  
and Zheludev . Adv. Mat. DOI: 10.1002/adma.201103162

# Ultrafast Au metamaterial: Tuneability & Application



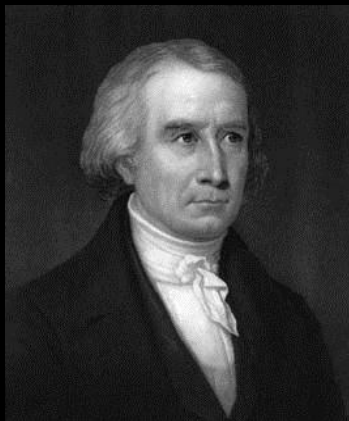
System	% T modulation	Fluence, $\mu\text{J}/\text{cm}^2$	Response time, fs
<b>Gold metamaterial</b>	<b>40 %</b>	<b>270</b>	<b><math>\sim 40\text{fs}</math></b>
Metamaterial + $\alpha$ -Si Opt. Exp. 17, 17652 (2009)	<b>30 %</b>	<b>300</b>	<b><math>&gt;750\text{fs}</math></b>
Metamaterial + CNTs PRL,104, 153902 (2010)	<b>10 %</b>	<b>40</b>	<b><math>\sim 500\text{fs}</math></b>
Plasmonic nanorods Nature NanT 6,107 (2011)	<b>80 %</b>	<b>7000</b>	<b><math>\sim 1\text{ps}</math></b>



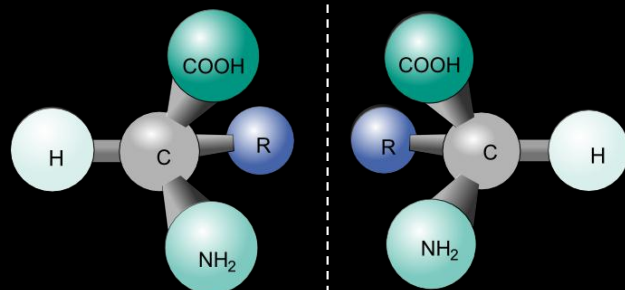
# From Nonlinear Optics to Nonlinear Plasmonics



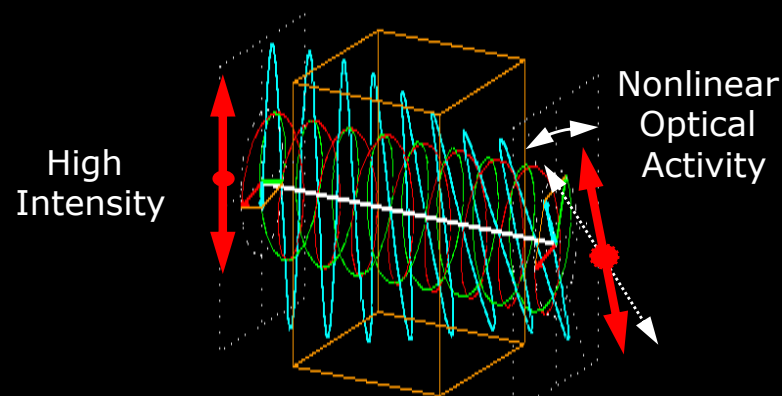
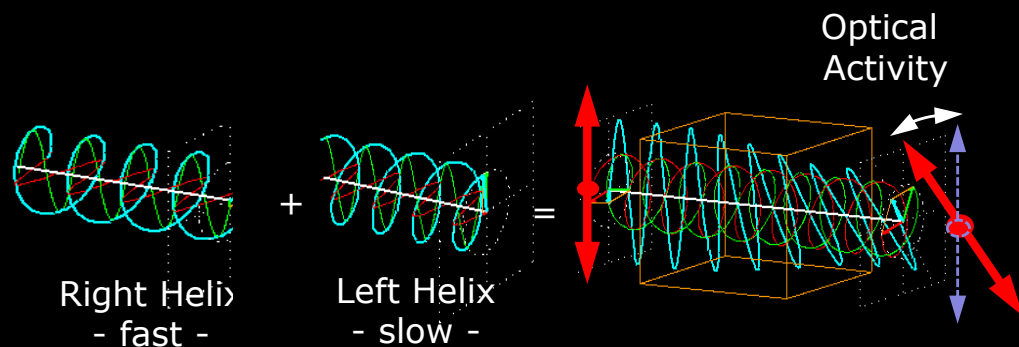
# Nonlinear Optical Activity



D. F. J. Arago  
1786 - 1853



S.A. Akhmanov  
1929-1991



$$P_i = \frac{1}{4\pi} (\epsilon_{ij} - \delta_{ij} + i k_n \Gamma^{(1)}_{ijn}) E_j$$

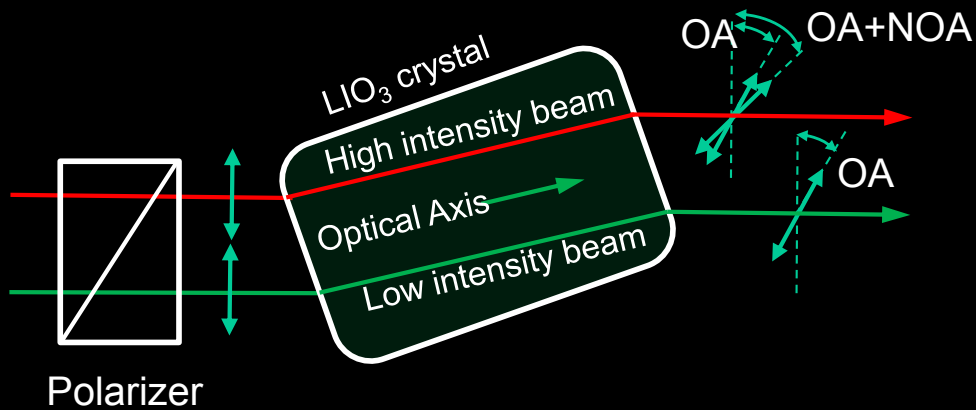
$$\Theta = \Theta_0 + \frac{2\pi L}{\lambda^2} \text{Re}\{\Gamma^{(1)}\}$$

$$+ (\chi^{(3)}_{ijkl} + i k_n \Gamma^{(3)}_{ijkln}) E_j E_k E_l^*$$

$$+ \frac{64\pi^4 L}{c \lambda^2 (1+n)^2} \text{Re}\{\Gamma^{(3)}_{xyz}\} I$$

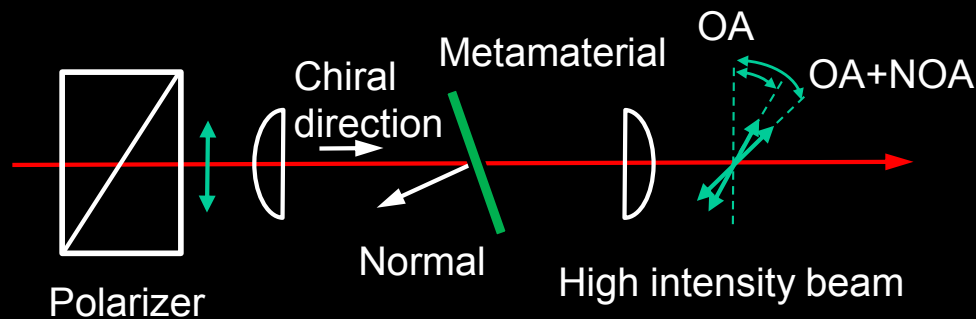
# Nonlinear optical activity: $10^7$ times stronger than natural media

1979: Ahmanov, Zheludev et.al, JETP Lett, 29, 5 (1979)

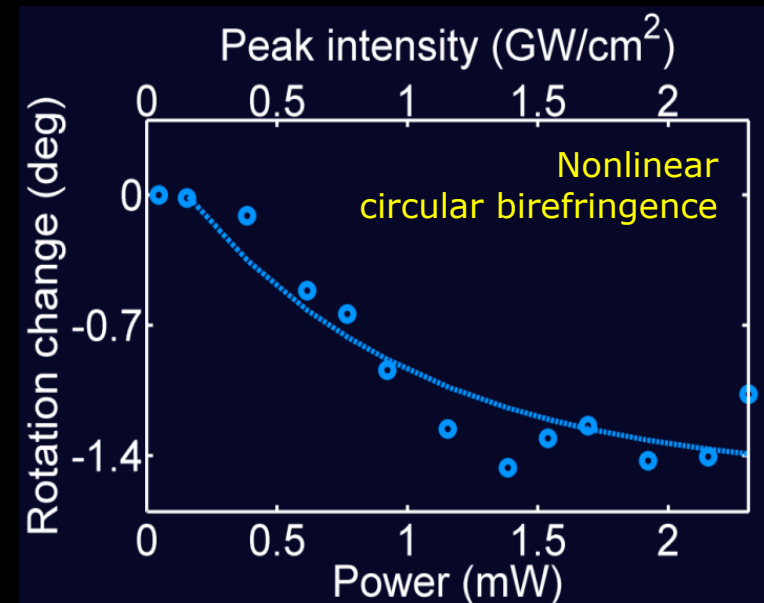


FOM  $\sim 10^{-11}$ deg·cm/W

2011: Ren, Plum Zheludev, TBP



FOM  $\sim 10^{-4}$ deg·cm/W



# Phase Change Metamaterials

## Phase change metamaterials



### **Goal:**

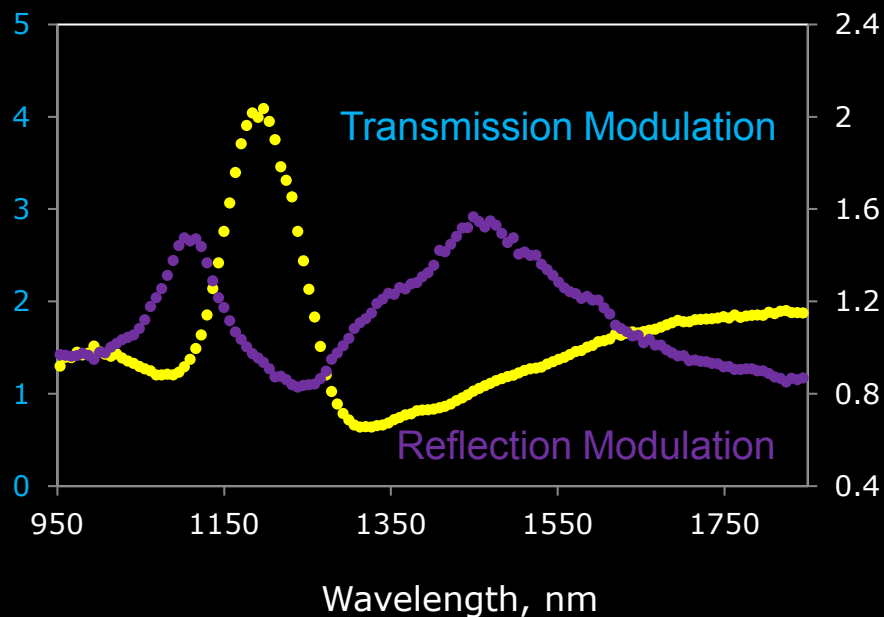
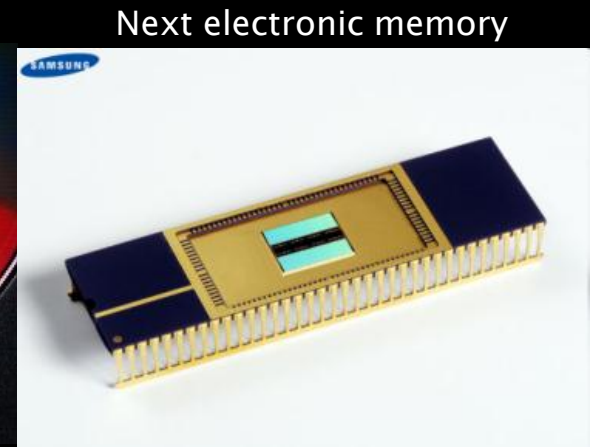
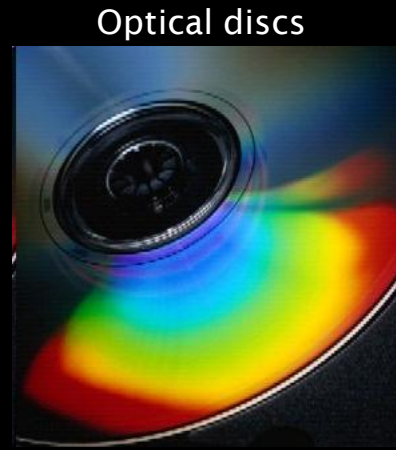
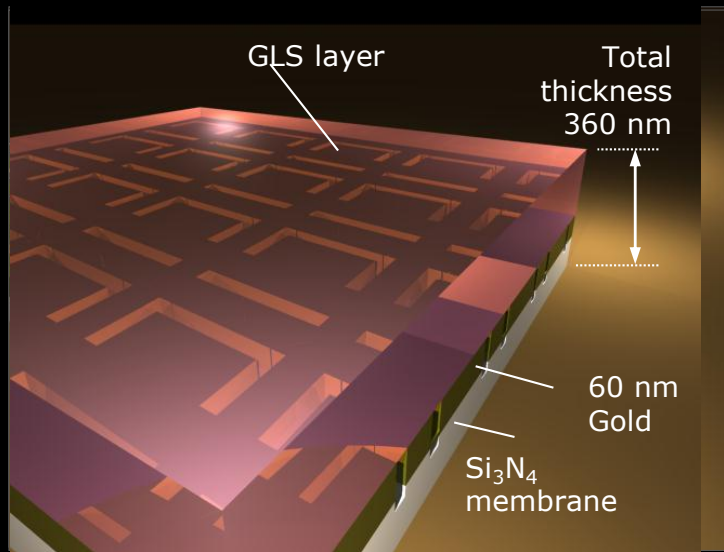
Non-volatile switching

### **Applications:**

data storage,  
displays



# Nanoscale Thickness Electro-optical Modulator: Chalcogenide Glass @ Metamaterial



**nature materials** REVIEW ARTICLE  
PUBLISHED ONLINE: 23 AUGUST 2010 | DOI: 10.1038/NMAT2810

## The Fano resonance in plasmonic nanostructures and metamaterials

Boris Luk'yanchuk<sup>1</sup>, Nikolay I. Zheludev<sup>2</sup>, Stefan A. Maier<sup>3</sup>, Naomi J. Halas<sup>4</sup>, Peter Nordlander<sup>5\*</sup>, Harald Giessen<sup>6</sup> and Chong Tow Chong<sup>1,7</sup>

APPLIED PHYSICS LETTERS 96, 143105 (2010)

### Metamaterial electro-optic switch of nanoscale thickness

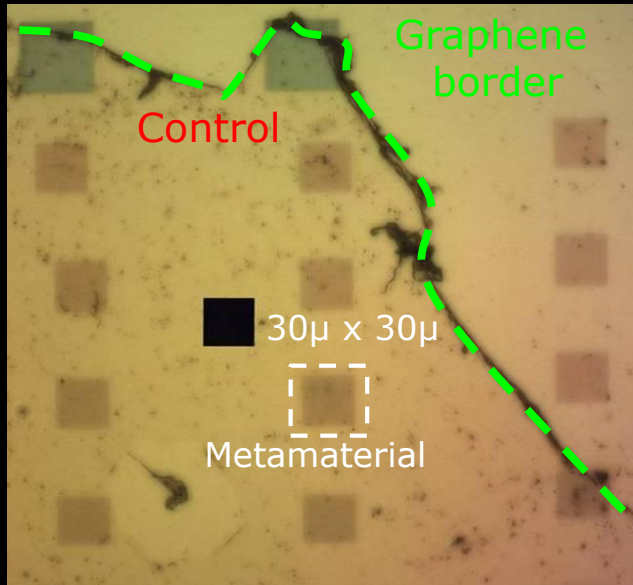
Z. L. Sámson,<sup>1</sup> K. F. MacDonald,<sup>1(a)</sup> F. De Angelis,<sup>2</sup> B. Gholipour,<sup>1</sup> K. Knight,<sup>1</sup> C. C. Huang,<sup>1</sup> E. Di Fabrizio,<sup>2</sup> D. W. Hewak,<sup>1</sup> and N. I. Zheludev<sup>1</sup>



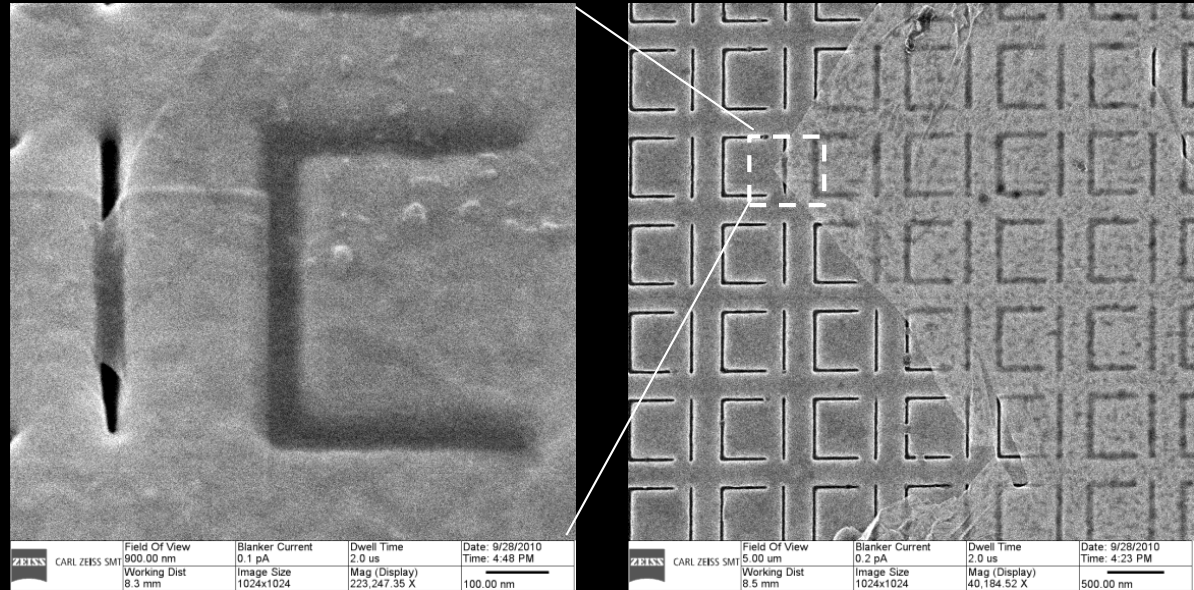
# Graphene @ Metamaterials

## Graphene in a photonic metamaterial

12 April 2010 / Vol. 18, No. 8 / OPTICS EXPRESS 8353  
 Nikitas Papisimakis,<sup>1</sup> Zhiqiang Luo,<sup>2</sup> Ze Xiang Shen,<sup>2</sup> Francesco De Angelis,<sup>3,4</sup>  
 Enzo Di Fabrizio,<sup>3,4</sup> Andrey E. Nikolaenko,<sup>1</sup> and Nikolay I. Zheludev<sup>1\*</sup>

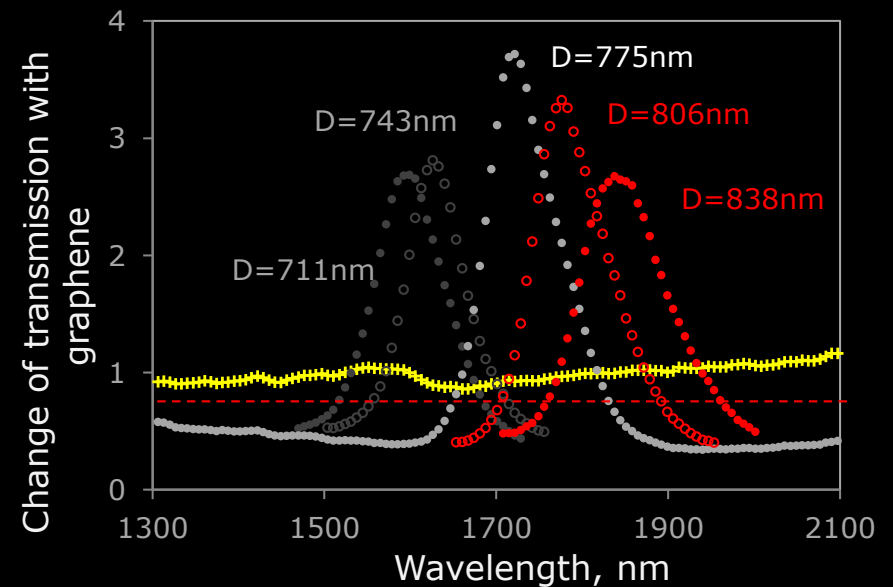
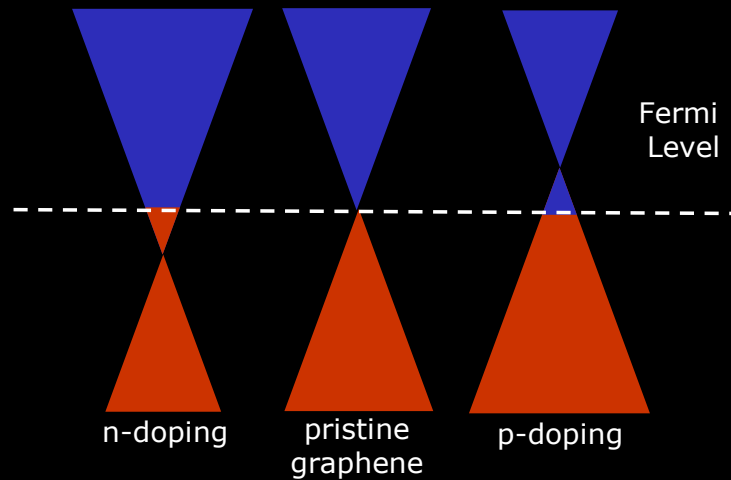


Optical microscope images



Helim-Ion microscope images

Modulating graphene properties by carrier injection



**Nanoscale light  
localization in  
metamaterials**



**Goal:**

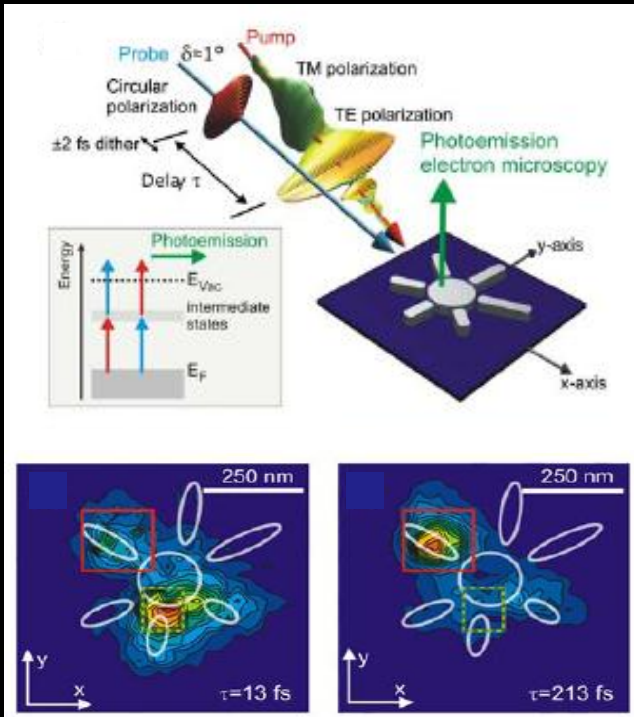
Controlable hot-spots  
in metamaterials

**Applications:**

Imaging & data  
storage, routing

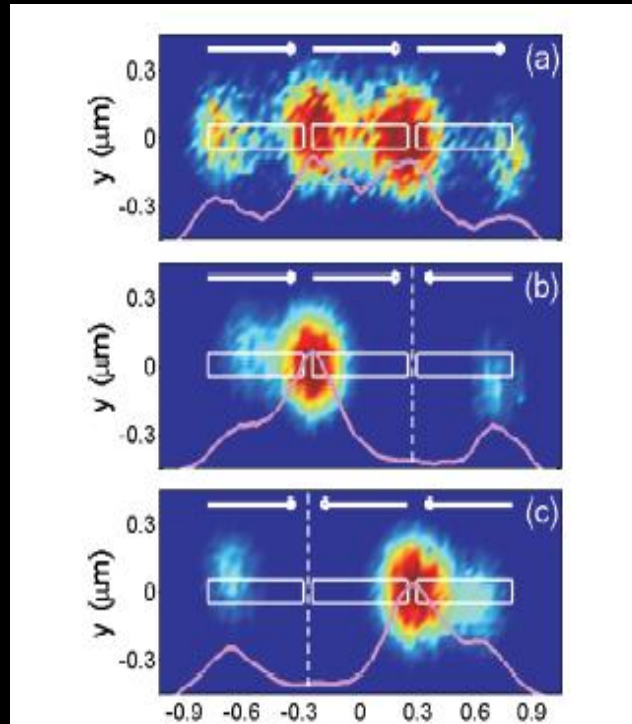
# Manipulation of nanoscale optical fields

## Ultrafast coherent control



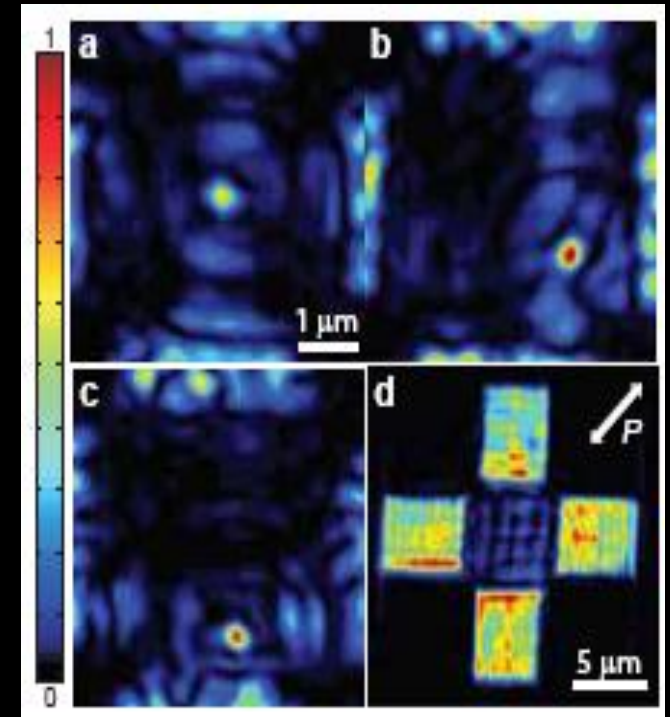
M. Stockman, M. Aeschlimann, *et. al*, (2006-2010)

## Spatial phase-shaped beams



G. Volpe, *et. al*, (2009)

## Tailored plasmon interference

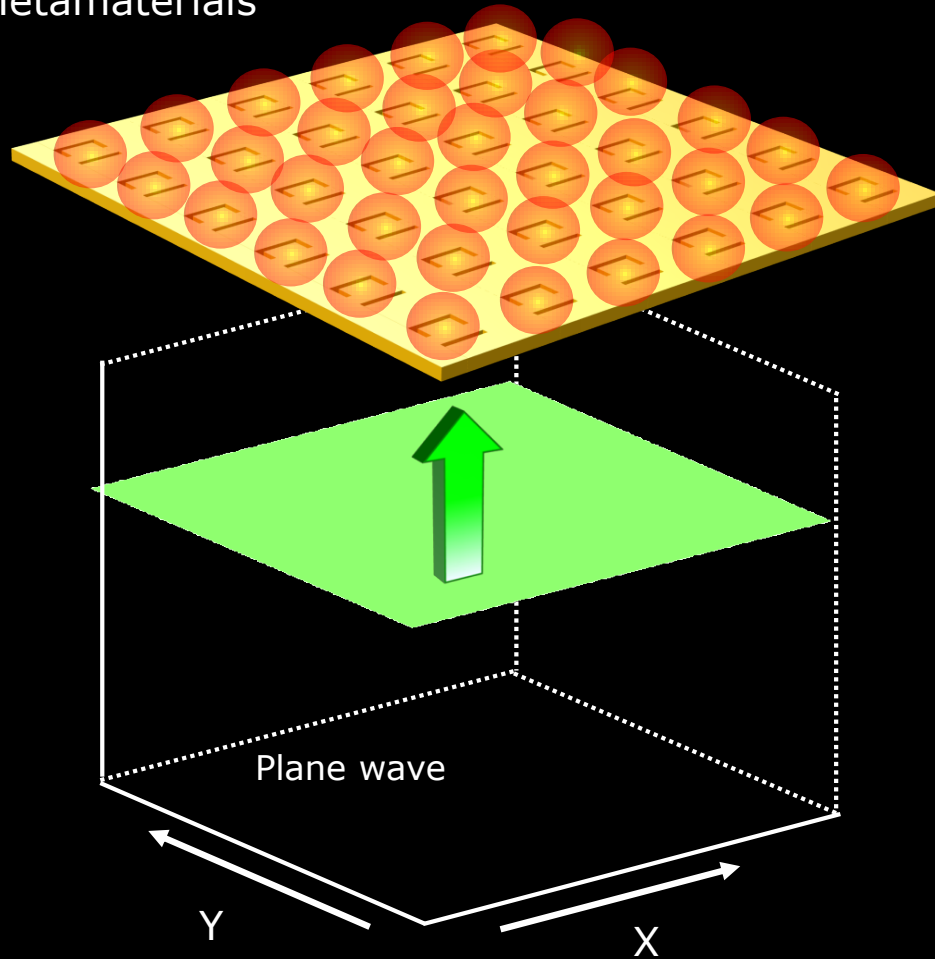


B. Gjonag, *et. al*, (2011)

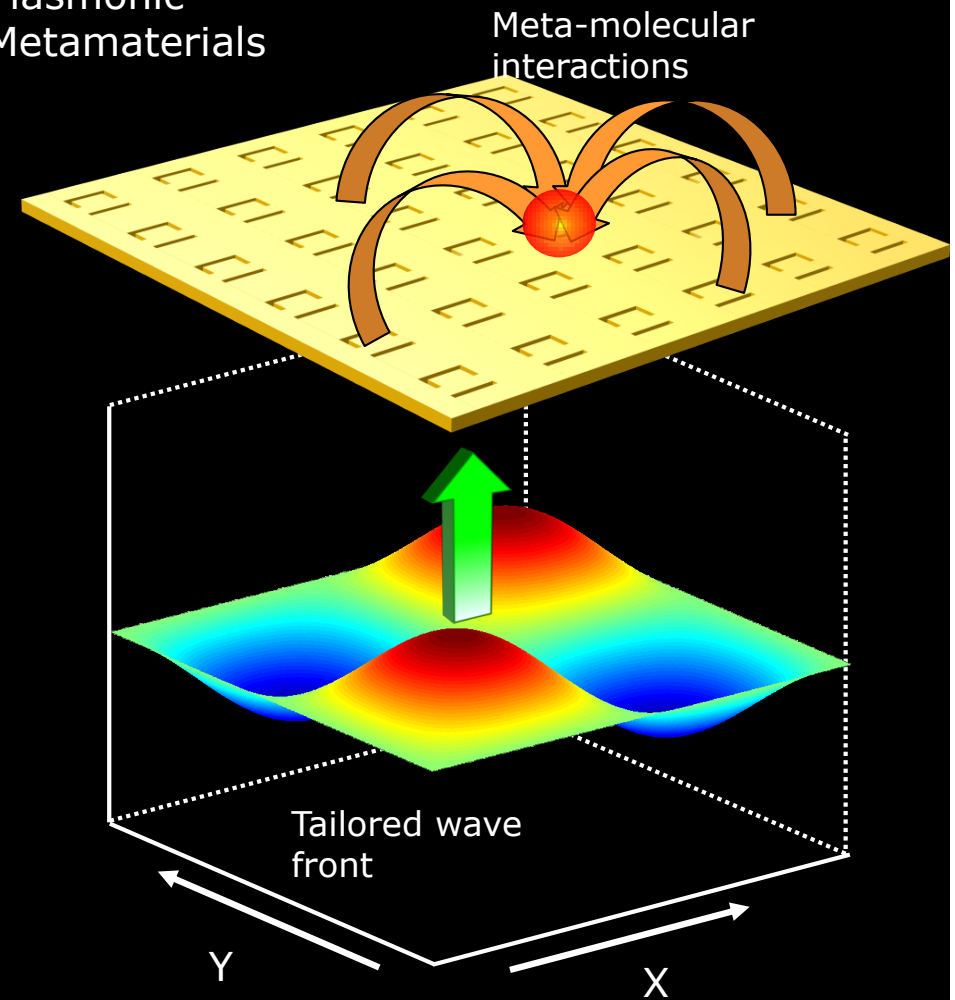


# Coherent control of nanoscale field localization

Plasmonic  
Metamaterials



Plasmonic  
Metamaterials



PRL 106, 085501 (2011)

PHYSICAL REVIEW LETTERS

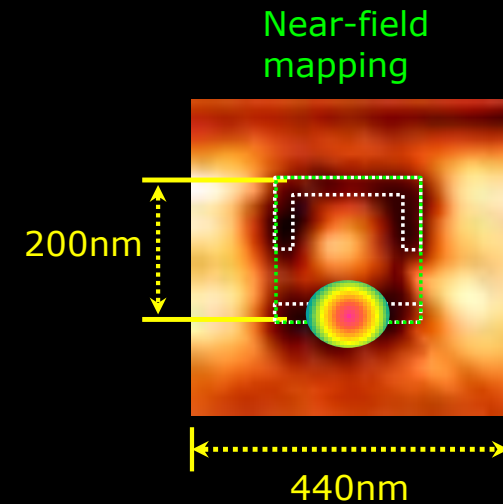
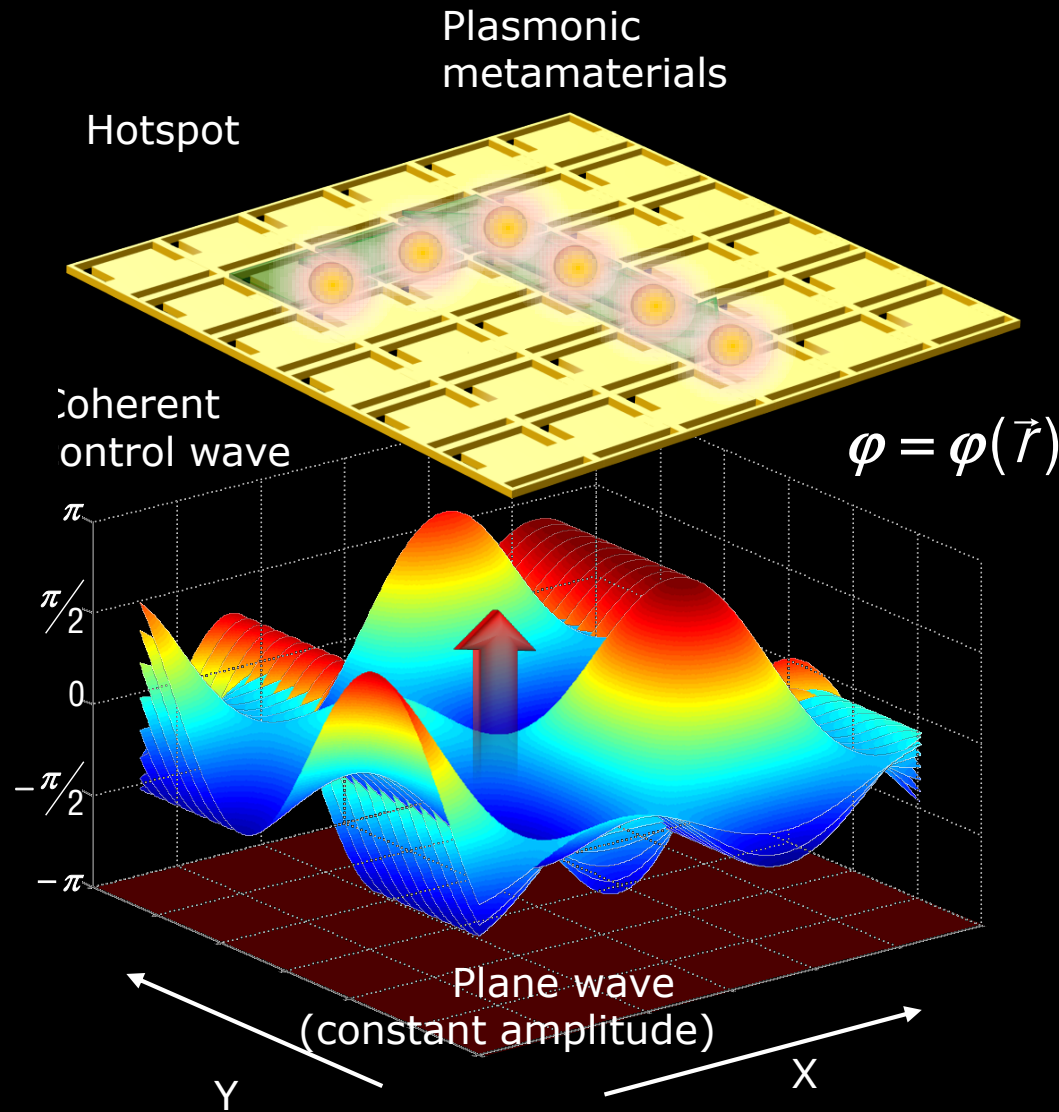
week ending  
25 FEBRUARY 2011

Coherent Control of Nanoscale Light Localization in Metamaterial: Creating and Positioning Isolated Subwavelength Energy Hot Spots

T. S. Kao,<sup>1</sup> S. D. Jenkins,<sup>2</sup> J. Ruostekoski,<sup>2</sup> and N. I. Zheludev<sup>1,\*</sup>

*Light*

# "Digitally" addressable nanoscale light localization



PRL 106, 085501 (2011)

PHYSICAL REVIEW LETTERS

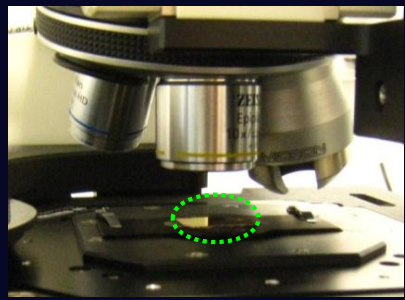
week ending  
25 FEBRUARY 2011

Coherent Control of Nanoscale Light Localization in Metamaterial: Creating and Positioning Isolated Subwavelength Energy Hot Spots

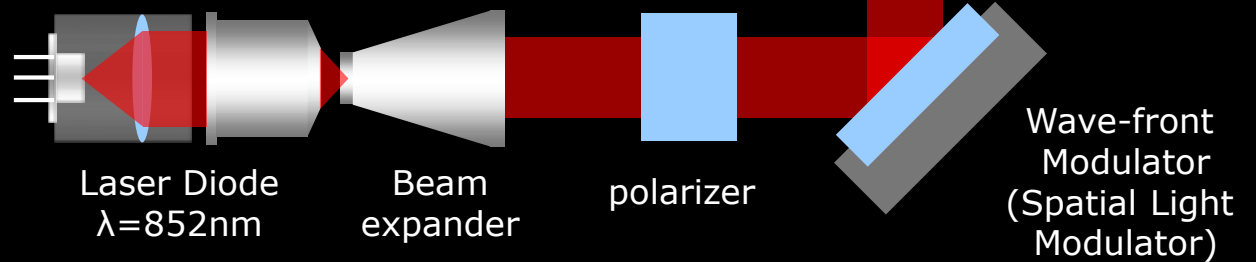
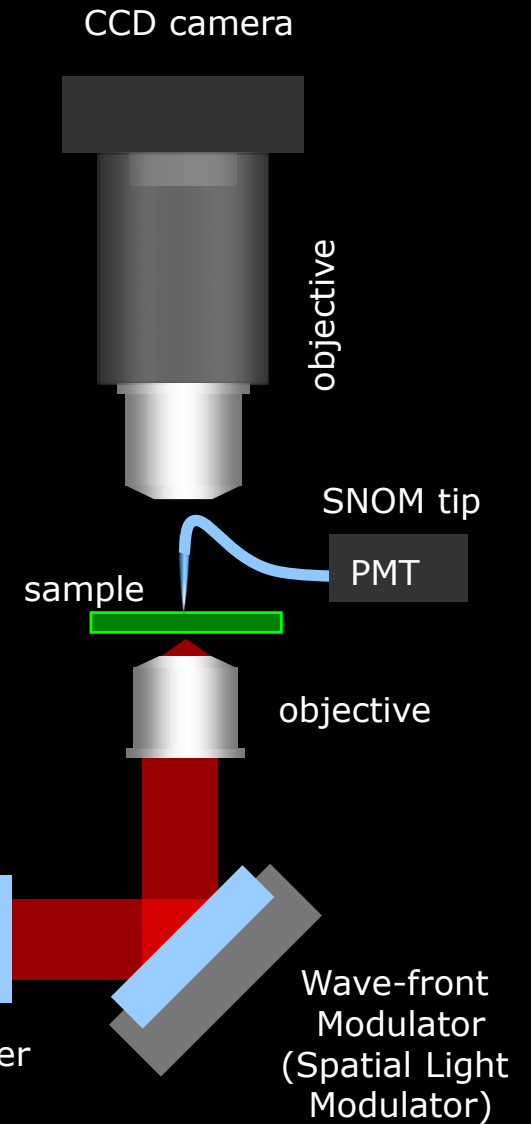
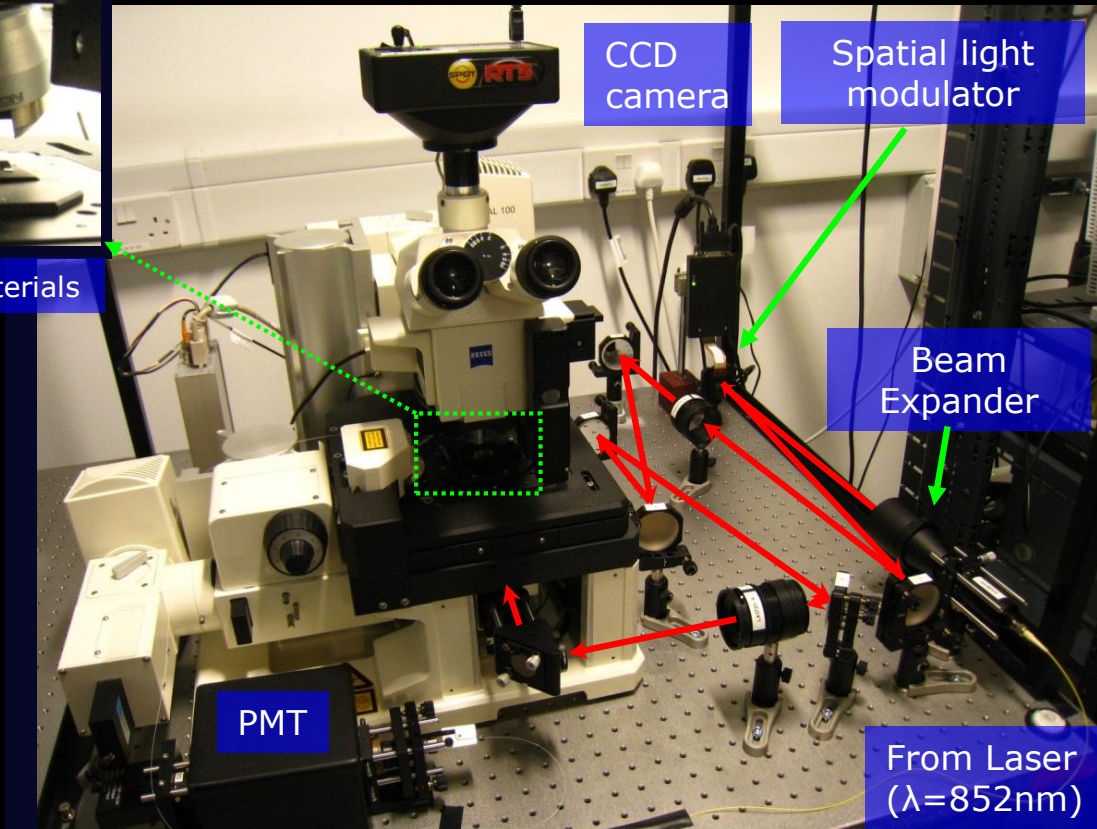
T. S. Kao,<sup>1</sup> S. D. Jenkins,<sup>2</sup> J. Ruostekoski,<sup>2</sup> and N. I. Zheludev<sup>1,\*</sup>

*Light*

# Coherent control of nanospots: experiment



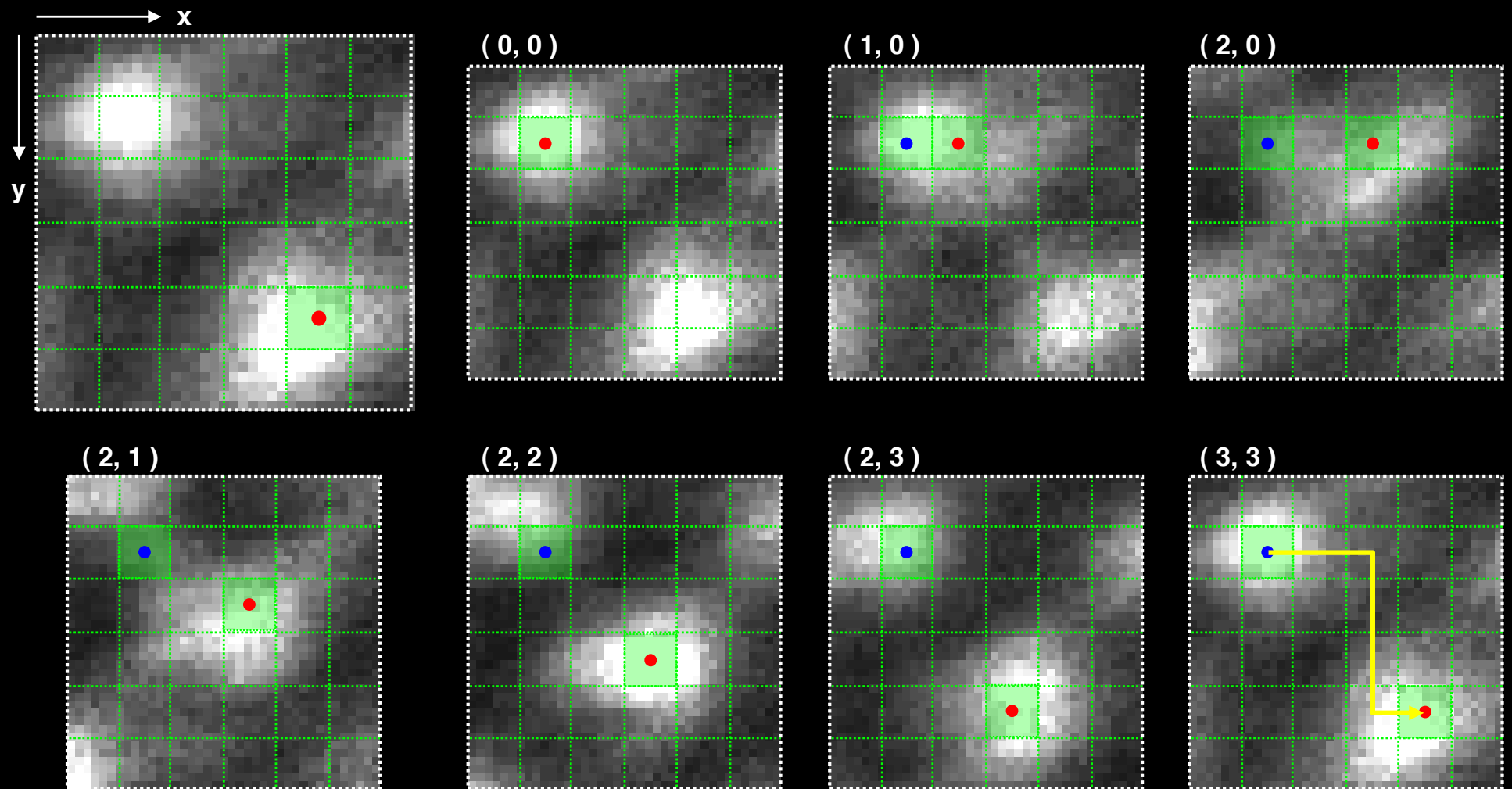
Plasmonic metamaterials



# Digitally addressable placing of the hotspot

Metamaterials unit cell: 440nm,  $\lambda=852\text{nm}$ . Spatial wave-front profile:  $\varphi(\vec{r}) = (\Delta\varphi/2)\sin(kx)\sin(ky)$ ,  $k = 2\pi/a$

## CCD images



**Metamaterial  
Light sources**



**Goal:**

Plasmonic & optical  
sources & lasers

**Applications:**  
nanophotonics

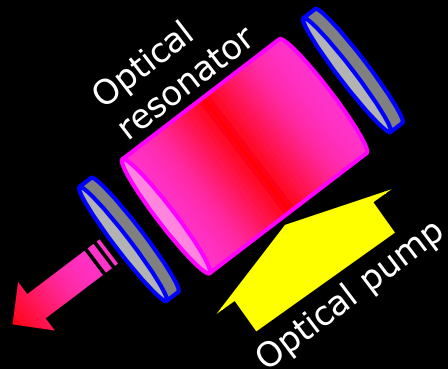


# The Lasing Spaser (2008)

(a coherent source of optical radiation fuelled by plasmons)

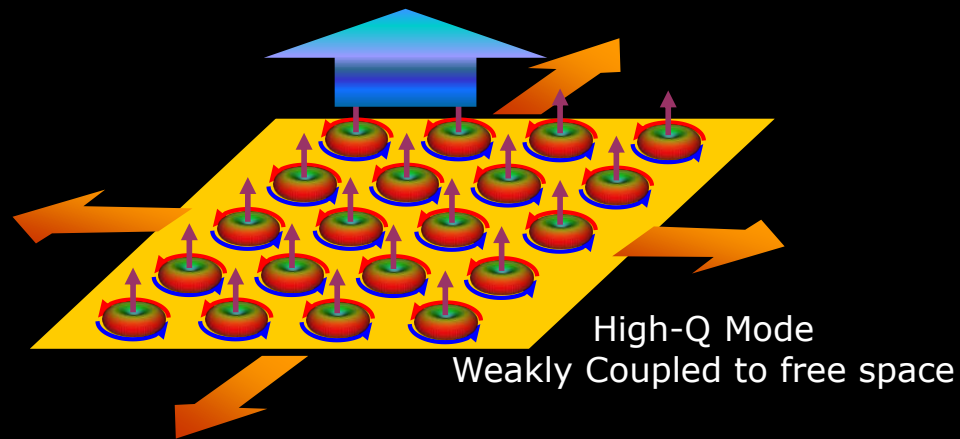
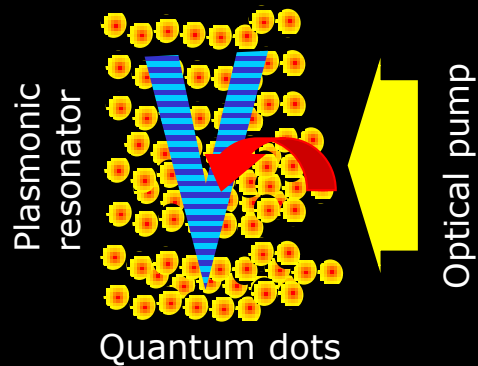
## Laser 1953

Townes, Schawlow  
Basov, Prokhorov



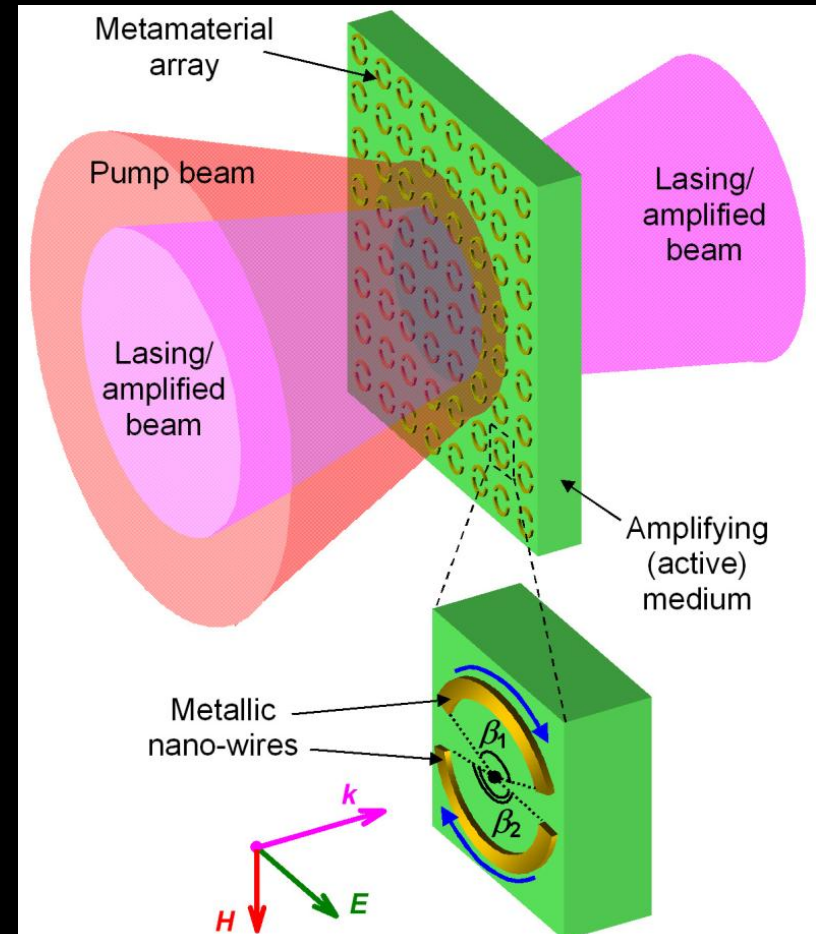
## Spaser 2003

Bergman & Stockman



## Lasing Spaser (2008)

Zheludev, Papasimakis, Prosvirnin, Fedotov



Lasing spaser

N. I. ZHELUDEV<sup>1,\*</sup>, S. L. PROSVIRNIN<sup>2</sup>, N. PAPANIMAKIS<sup>1</sup> AND V. A. FEDOTOV<sup>1</sup>

nature photonics | VOL 2 | JUNE 2008 |

PRL 104, 223901 (2010)

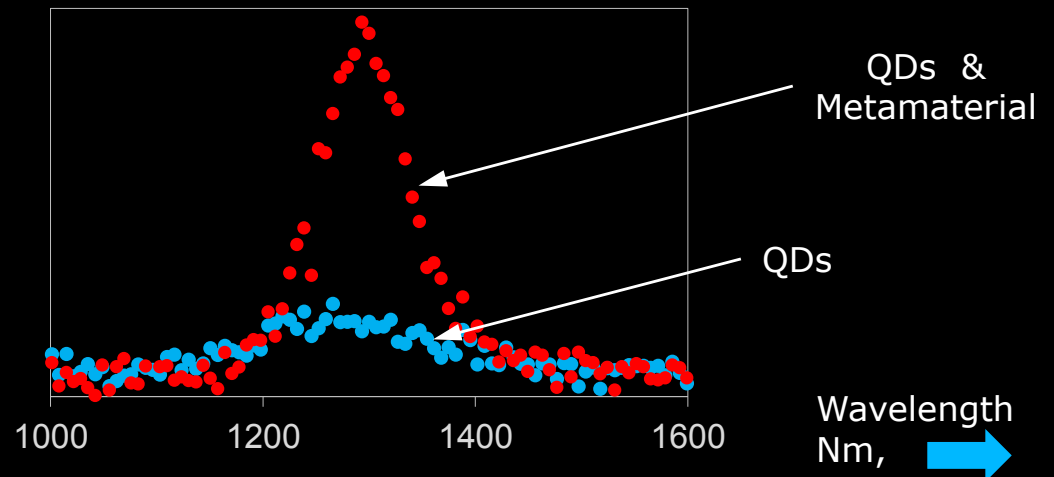
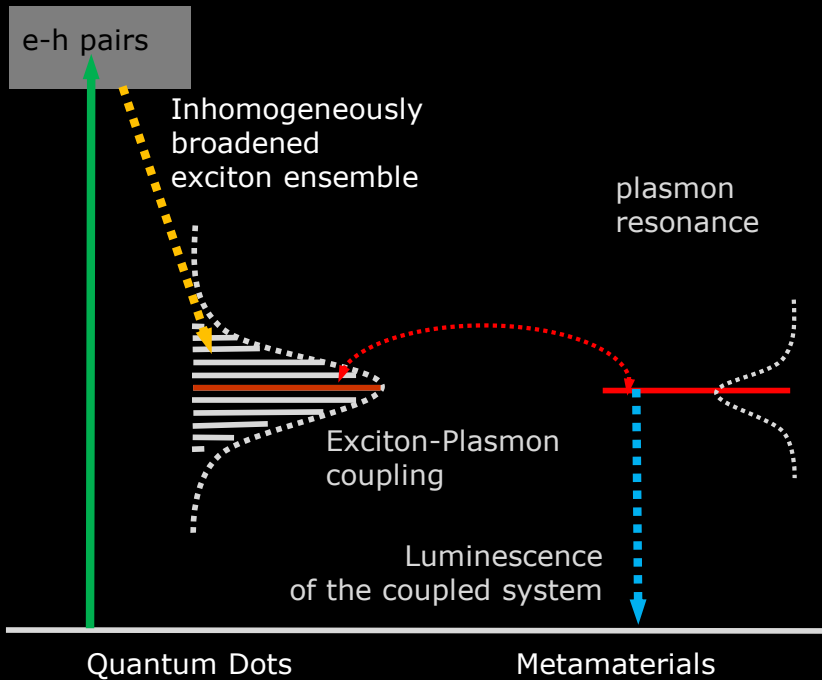
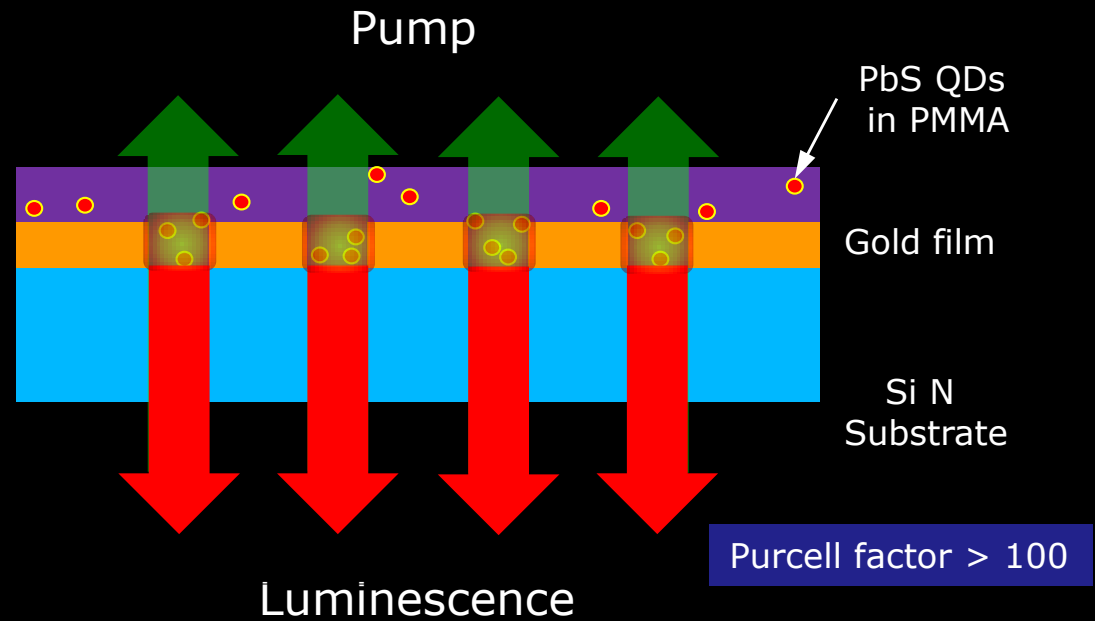
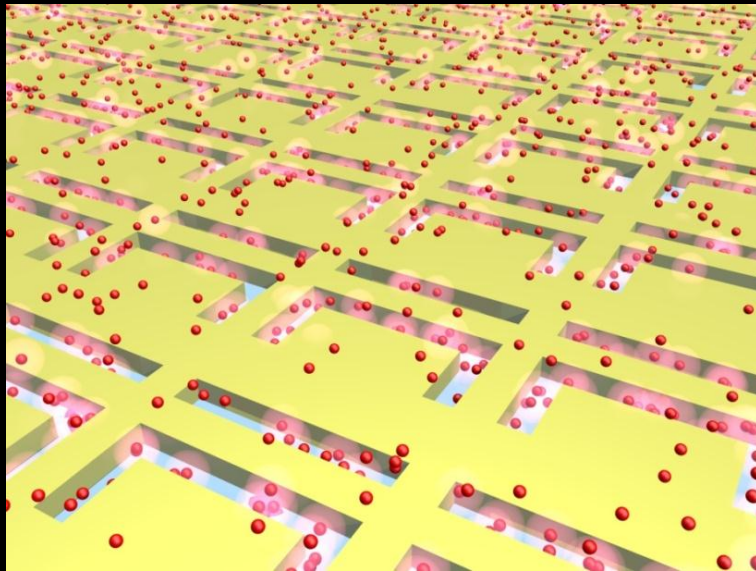
PHYSICAL REVIEW LETTERS

week ending  
4 JUNE 2010

Spectral Collapse in Ensembles of Metamolecules

V. A. Fedotov,<sup>1,\*</sup> N. Papasimakis,<sup>1</sup> E. Plum,<sup>1</sup> A. Bitzer,<sup>2,3</sup> M. Walther,<sup>2</sup> P. Kuo,<sup>4</sup> D. P. Tsai,<sup>5</sup> and N. I. Zheludev<sup>1,†</sup>

# Quantum Dots in Plasmonic Metamaterial: Enhanced Luminescence



PHYSICAL REVIEW LETTERS October 2010

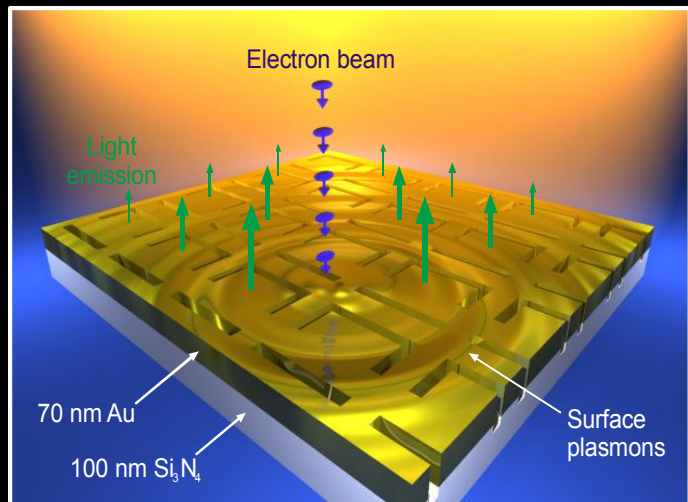
Multifold Enhancement of Quantum Dot Luminescence in a Plasmonic Metamaterial

K. Tanaka,<sup>1,2,\*</sup> E. Plum,<sup>1,†</sup> J. Y. Ou,<sup>1</sup> T. Uchino,<sup>3</sup> and N. I. Zheludev<sup>1,3</sup>

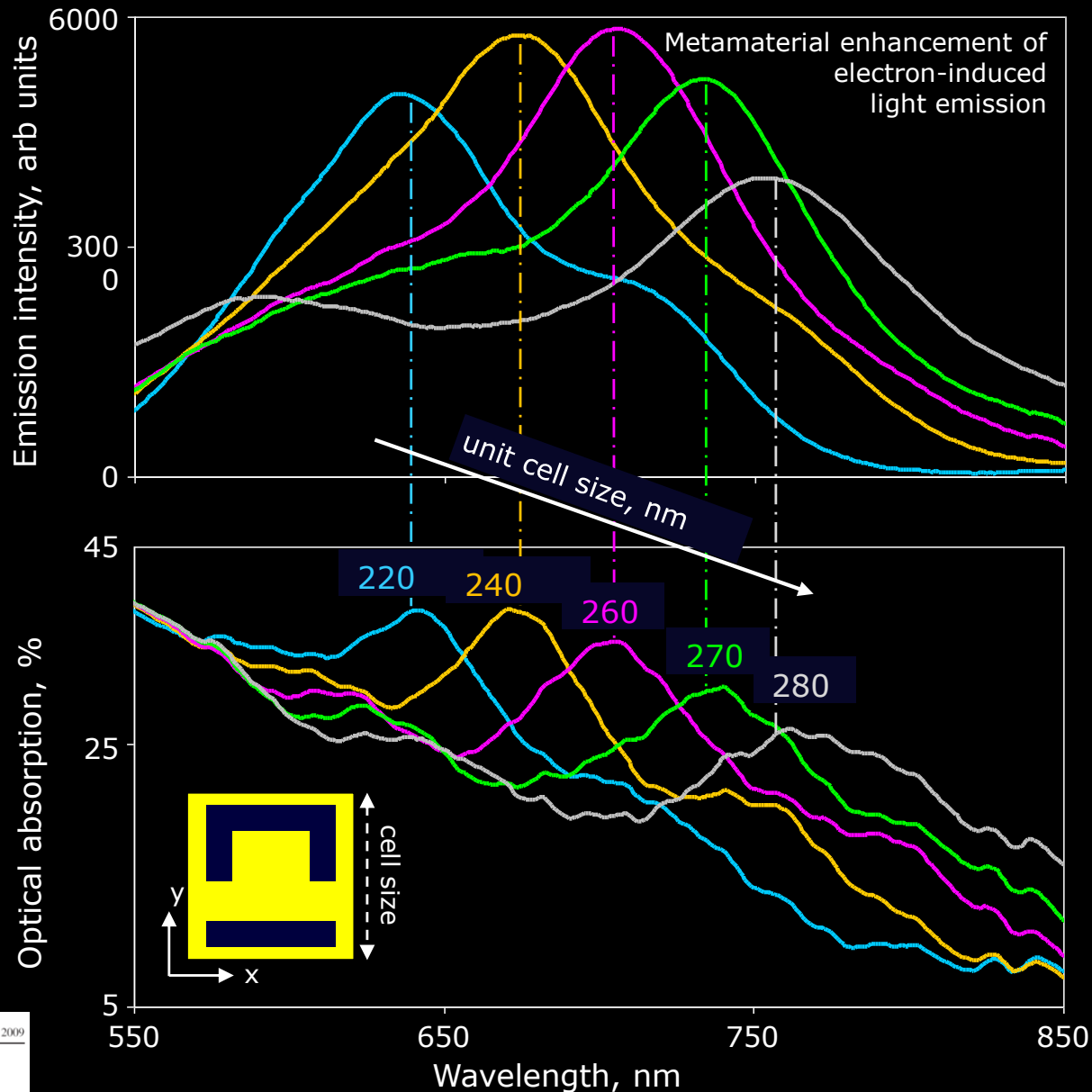
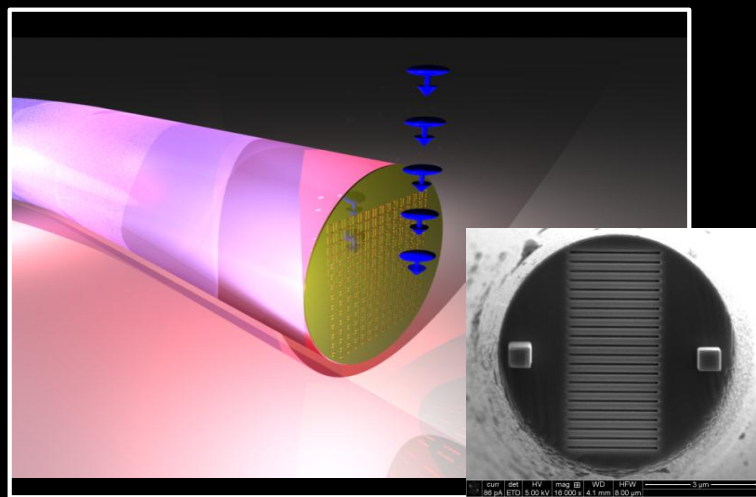
# Emission Linked to Plasmonic Resonance

Electron-induced emission spectra Au/Si<sub>3</sub>N<sub>4</sub> METAMATERIAL

Impact configuration



Fly by configuration




PRL 103, 113901 (2009)

PHYSICAL REVIEW LETTERS

week ending  
11 SEPTEMBER 2009

## Light Well: A Tunable Free-Electron Light Source on a Chip

G. Adamo,<sup>1</sup> K. F. MacDonald,<sup>1,\*</sup> Y. H. Fu,<sup>2</sup> C.-M. Wang,<sup>2</sup> D. P. Tsai,<sup>2</sup> F. J. García de Abajo,<sup>3</sup> and N. I. Zheludev<sup>1</sup>



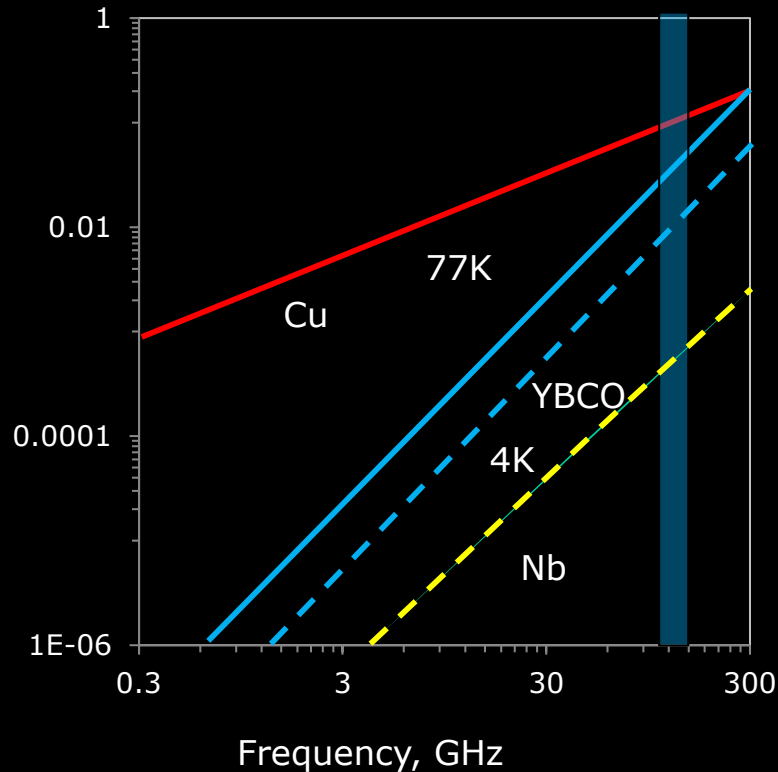
**Quntum  
Superconducting  
Metamaterials**

**Goal:**  
High sensetivity

**Applications:**  
New THz & Millimetre  
wave devices &  
quantum information  
platform

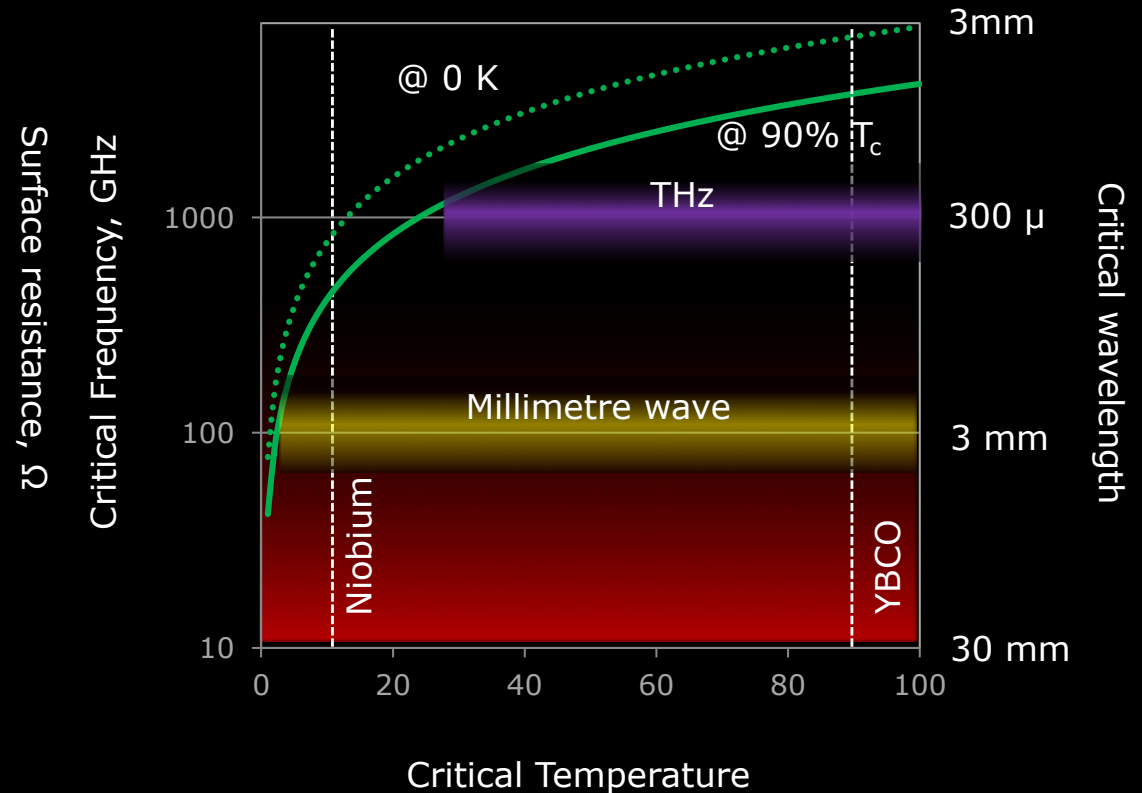
# Low- vs high- temperature superconductors

Surface resistance vs frequency



Photon energy to destroy superconductivity

$$h\nu = 2\Delta \sim 3.5kT_c$$



Anlage Group - University of Maryland - Nb, waveguide microwave

Los Alamos group - High- $T_c$ , THz free space

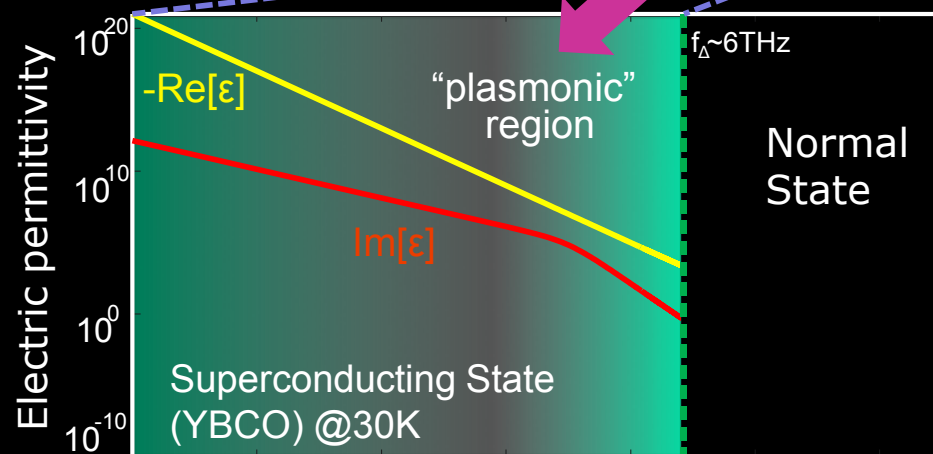
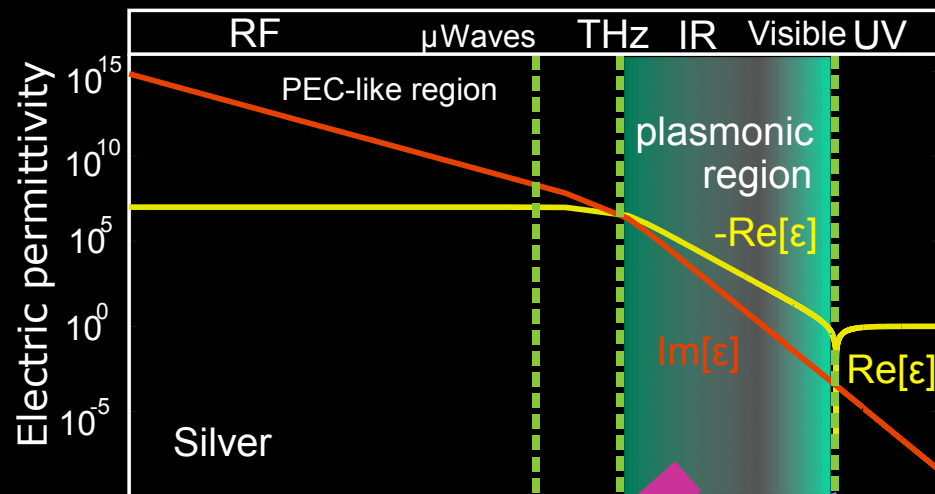
Southampton group - High  $T_c$  and Nb, Millimetre wave free space

APL **97**, 111106 (2010)

*OptExp* **18**, 9015, (2010)



# Case for Superconducting Plasmonics



When  $T < T_c$  in superconductors :

- losses are vanishing
- $e^-$  inertia prevails



**Superconductors are intrinsic plasmonic media**

Controlled by

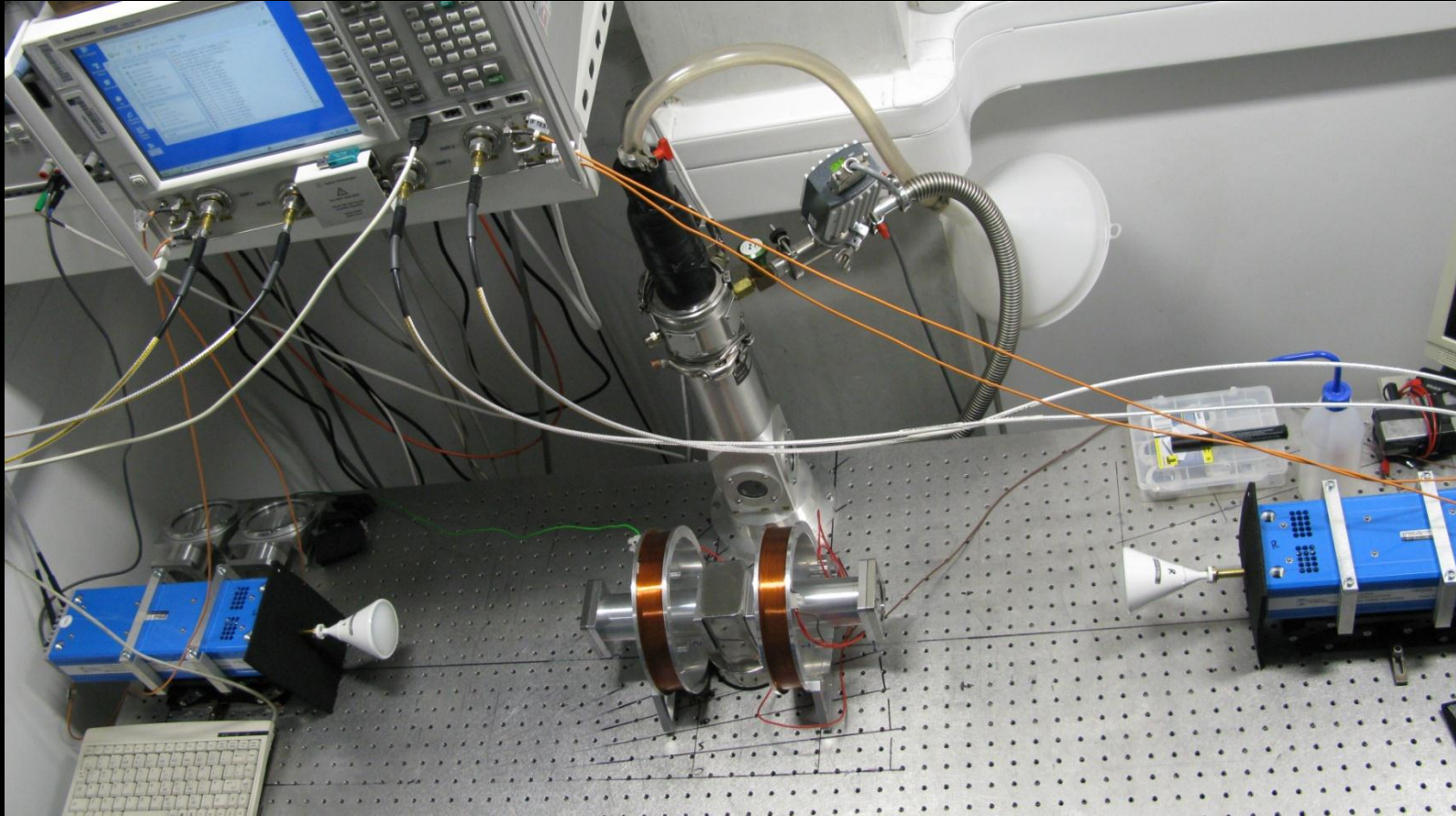


- proper structuring
- frequency
- temperature
- magnetic field
- laser irradiation
- electric current

**Low frequency plasmonics with easily integrated active control functionality**



# 100GHz free-space (millimetre waves) spectrometer

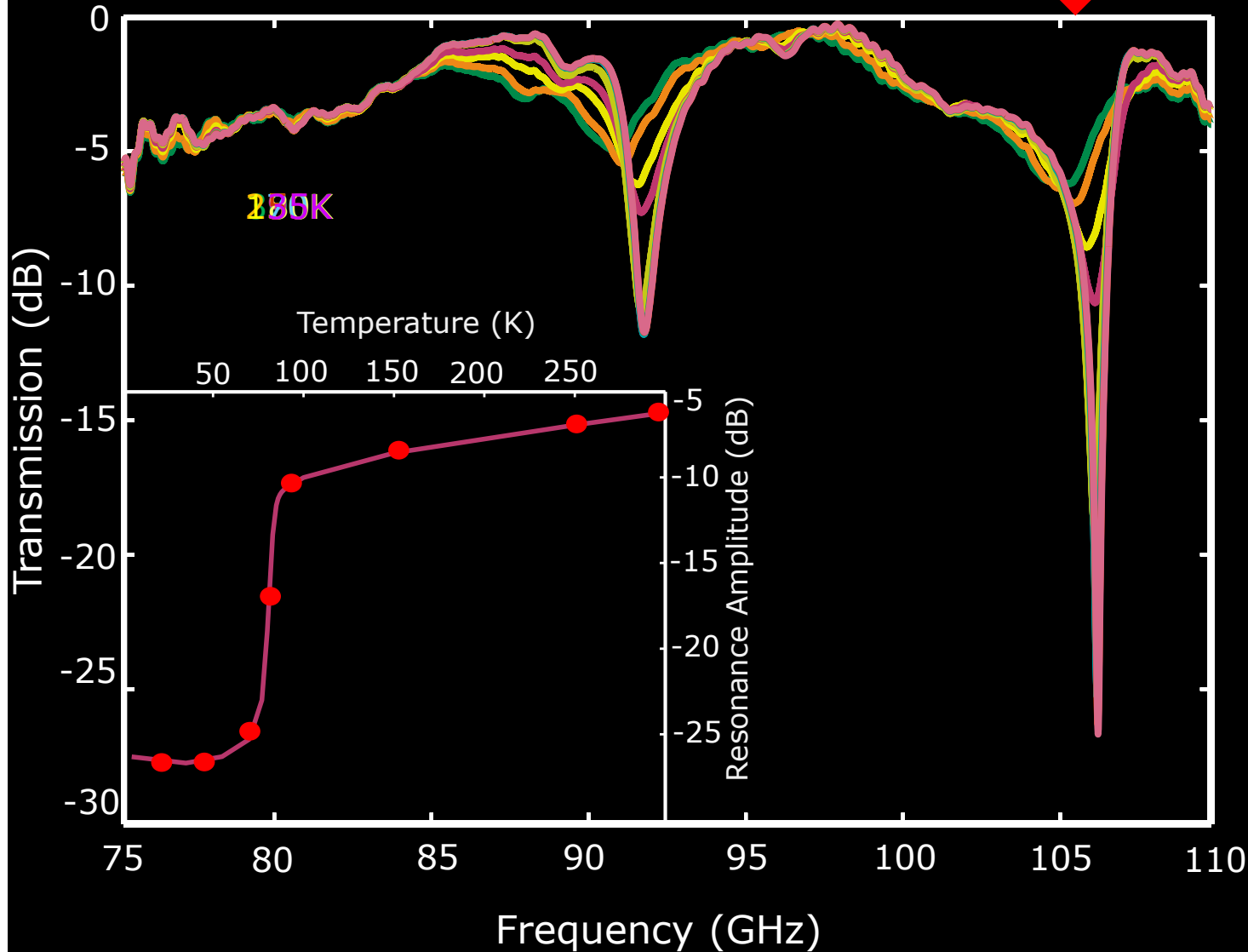


Receiving/Transmitting  
Antenna

He Cryostat  
Coldfinger

Receiving/Transmitting  
Antenna

# Sharp resonances in superconducting metamaterials disk array



YBCO disks 0.5mm diameter  
1.5mm period

Resonance becomes much sharper in Superconducting state  
Q-factor > 60

A. Tsiatmas N.I.Zheludev *et al.*,  
*Appl. Phys. Lett.* **97**, 111106  
(2010)  
Fedotov, Tsiatmas, Zheludev *et al.*  
*Opt. Exp.* **18**, 9015  
(2010)

# Towards digital / quantum metamaterials



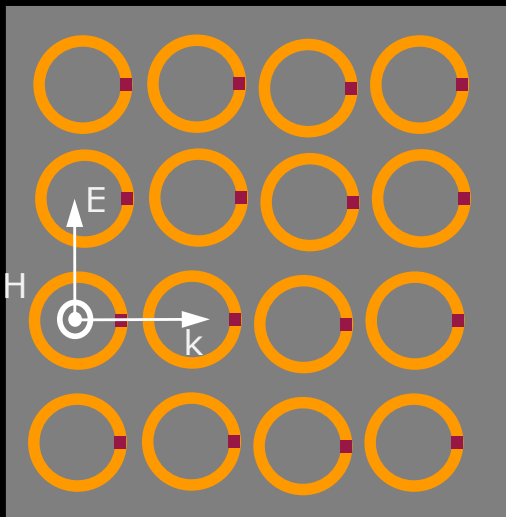
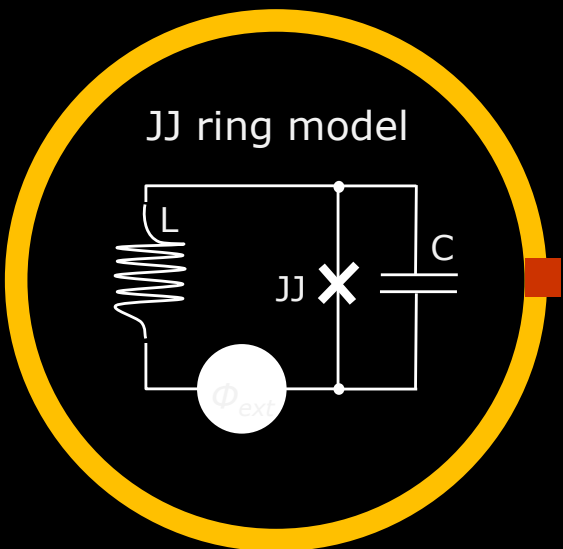
<b>Conventional metamaterial</b>	<b>Quantum metamaterial</b>
Classical plasmonic resonator	Quantum-interference circuit



<b>Classical plasmonic resonator</b>	<b>Quantum-interference circuit</b>
<b>Excitation</b>	
Plasmon	Quantum Qbit
<b>Mode of Operation</b>	
Analogue	Digital (Quantized flux)
<b>Advantages</b>	
Simple	Quantum level of operation, extremely high nonlinearities (100 000 times higher than p-n junction)



# Superconducting metamaterial: Josephson Junctions

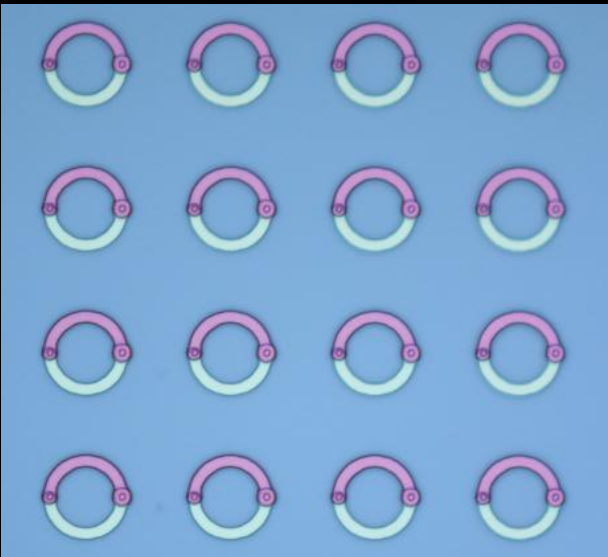


Flux dynamics

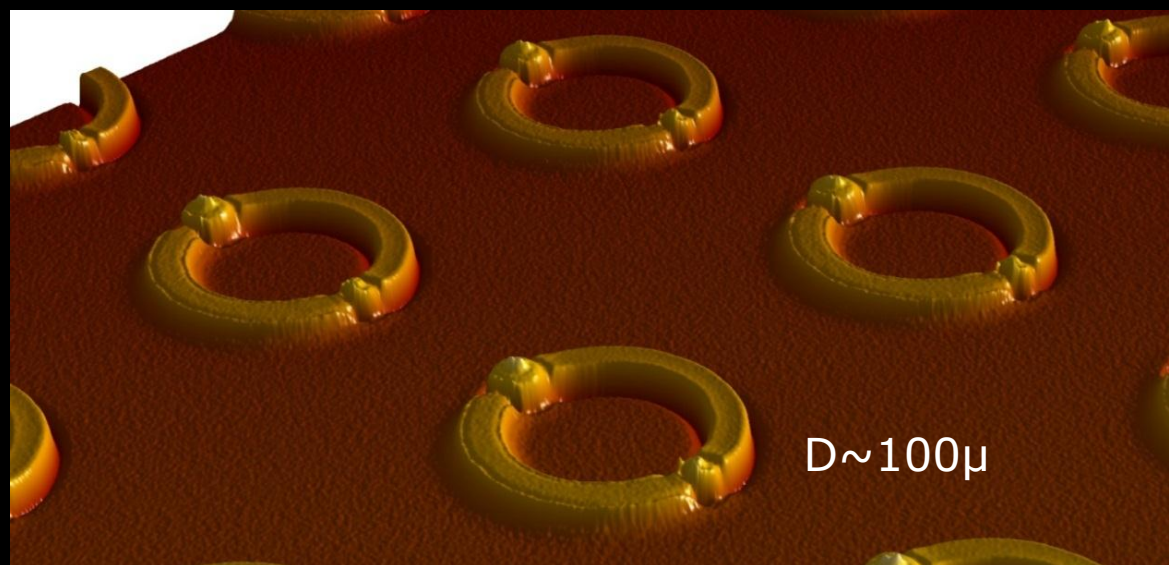
$$\ddot{\Phi} + \gamma \dot{\Phi} + \beta \sin(2\pi \Phi) + \Phi = \Phi_{ext}$$

Du, Chen, Li, 2006  
Lazarides & Tsironis, 2007

Southampton Nb - Al<sub>2</sub>O<sub>3</sub> - Nb Josephson Junction Arrays



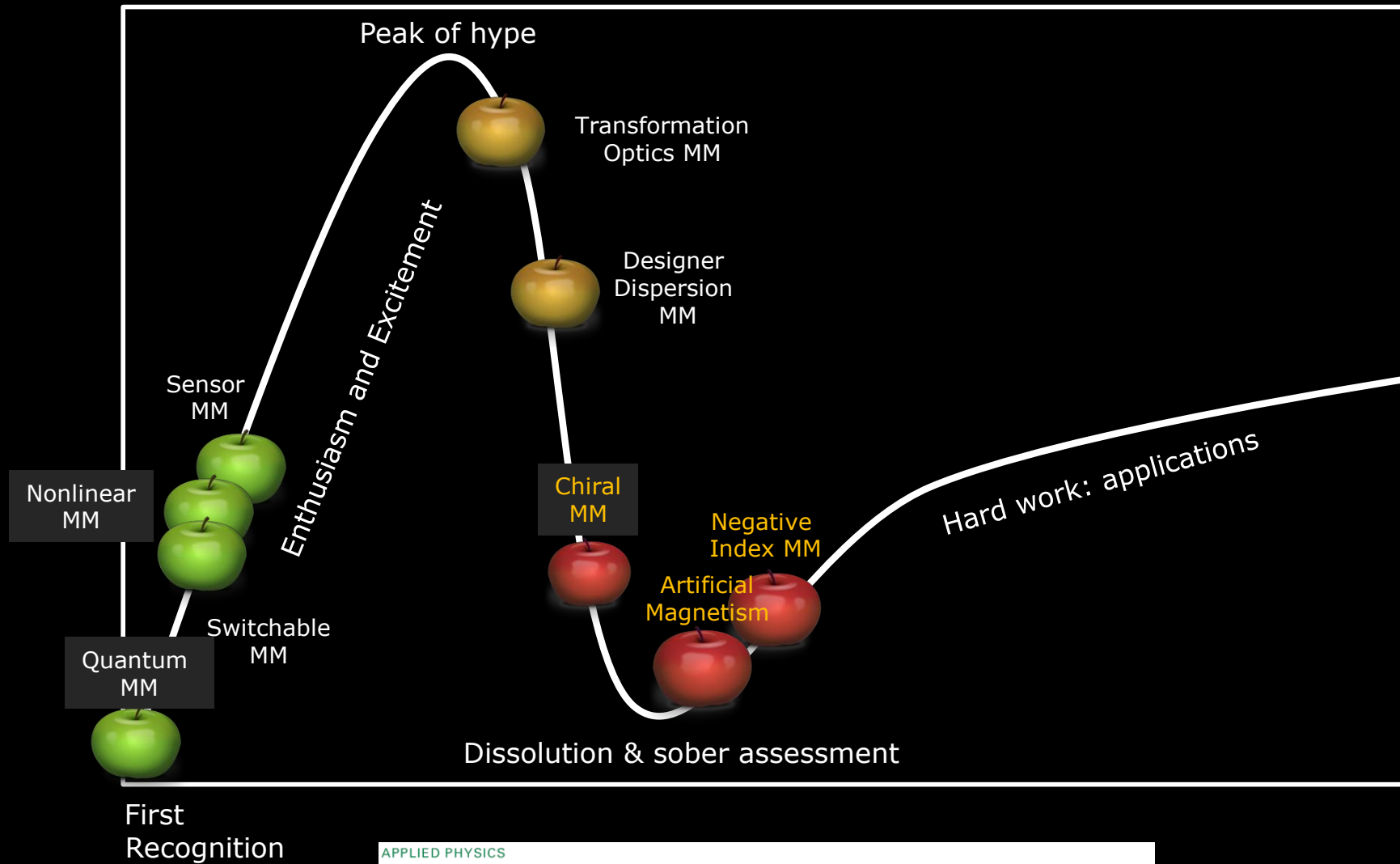
Optical micrograph



Profile



# Metamaterials: the technology development curve



APPLIED PHYSICS

## The Road Ahead for Metamaterials

Nikolay I. Zheludev

30 APRIL 2010 VOL 328 SCIENCE [www.sciencemag.org](http://www.sciencemag.org)

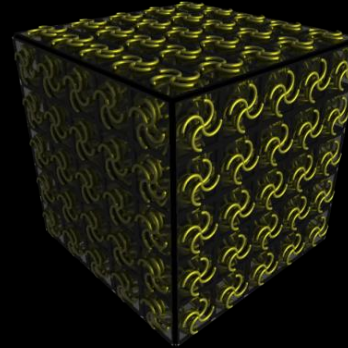
Metamaterials enable us to design our own "atoms" and thus create materials with new properties and functions.



In the Past:

Metamaterial is a **material**

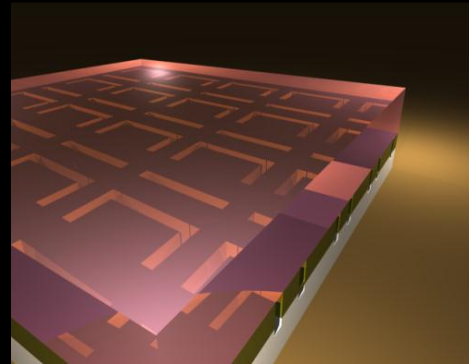
Structuring brings new properties



At Present:

Metamaterial is a **device**

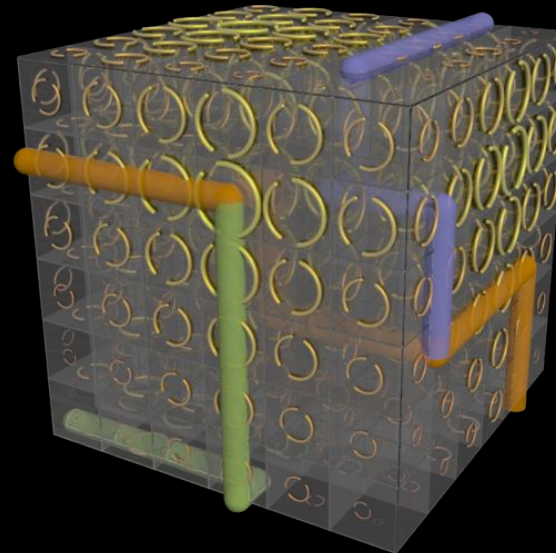
Structuring brings new functionality



In the Future:

Metamaterial is a **system**

Structuring brings new functionalities & integration



Analogue-  
linear

Analogue-  
Nonlinear

Digital

*Light*

# Southampton Centre for Photonic Metamaterials



[www.nanophotonics.org.uk](http://www.nanophotonics.org.uk)

