



**The Abdus Salam  
International Centre for Theoretical Physics**



**2328-17**

**Preparatory School to the Winter College on Optics and  
the Winter College on Optics: Advances in Nano-Optics  
and Plasmonics**

***30 January - 17 February, 2012***

**Plasmonics basic, waveguides & crystals**

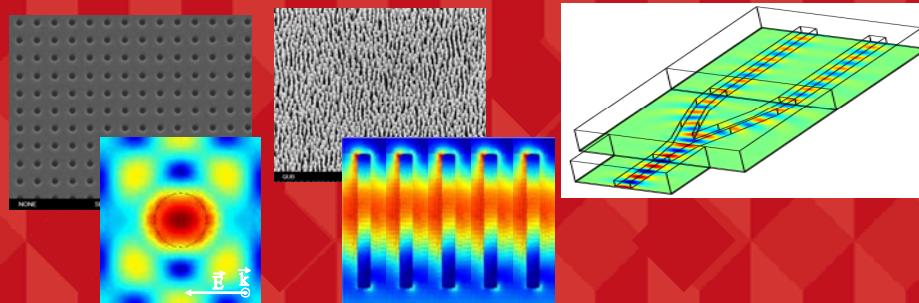
A. Zayats  
*The Queen's University of Belfast*  
U.K.

# Plasmonics, plasmonic waveguides plasmonics crystals

Anatoly V Zayats

*Nano-optics and Near-field Spectroscopy Group*

[www.nano-optics.org.uk](http://www.nano-optics.org.uk)



## Nanophotonics:

**generating, guiding, manipulating and  
detecting light on subwavelength scales**

- information processing
- opto-electronics
- healthcare
- energy



## OUTLINE:

- Surface plasmon polaritons
- SPP waveguides and circuits
- Surface polaritonic crystals:
  - principles
  - dispersion engineering
- Controlling light using plasmonic crystals:
  - all-optical control
  - electric field control
  - magnetic field control
  - mechanical control



## Surface plasmons

- **Plasmons:**  
collective excitation of electrons (in metal)

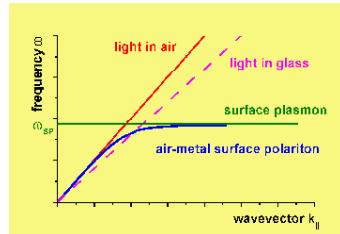
$$\omega_p^2 = \frac{4\pi Ne^2}{m} \quad \text{Re}\epsilon_m = 1 - \frac{\omega_p^2}{\omega^2} < 0 \quad \text{for } \omega < \omega_p$$

- **Surface plasmons:**  
collective excitation of electrons close to a surface

$$\omega_{SP} = \omega_p / \sqrt{2}$$

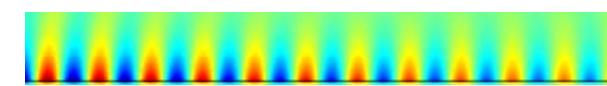
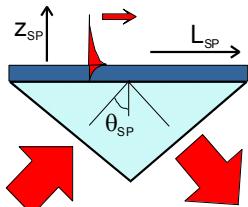
- **Surface plasmon polaritons:**  
propagating surface wave (surface plasmon + photon)

## Surface plasmon polaritons



**SPP dispersion:**

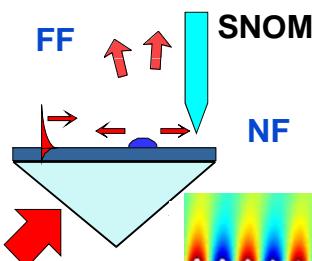
$$k_{SP} = \frac{\omega}{c} \left( \frac{\epsilon_i \epsilon_m}{\epsilon_i + \epsilon_m} \right)^{1/2}$$



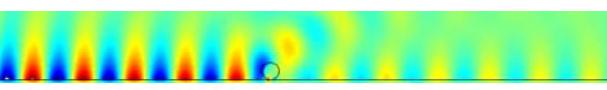
**SPP excitation:**

$$k_{\parallel} = \frac{\omega}{c} n_{prism} \sin \theta_{SP}$$

## Surface polariton optics

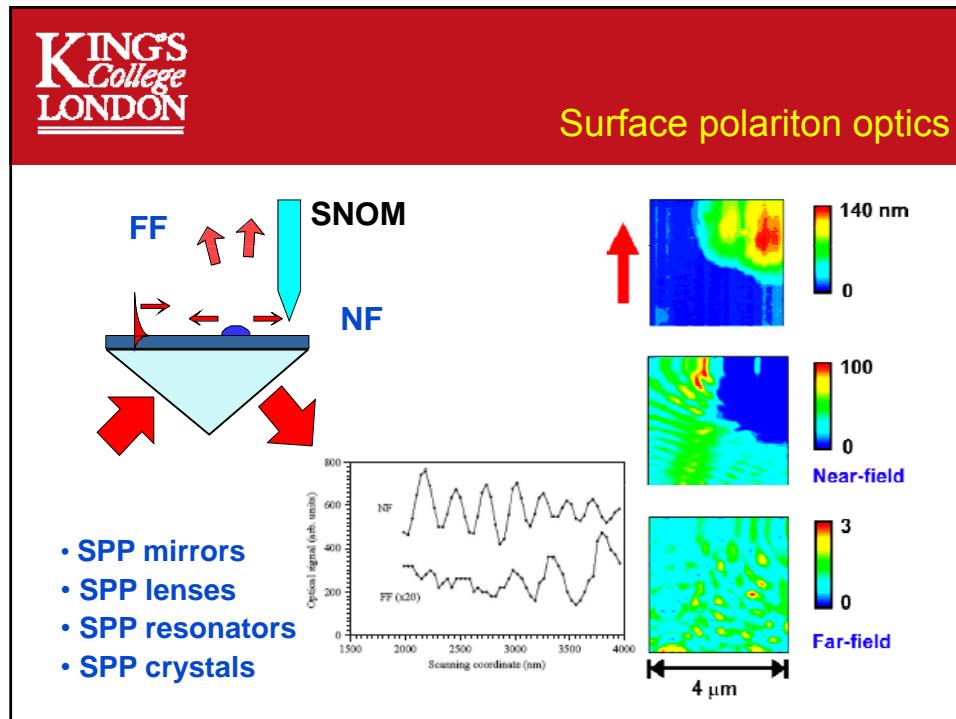


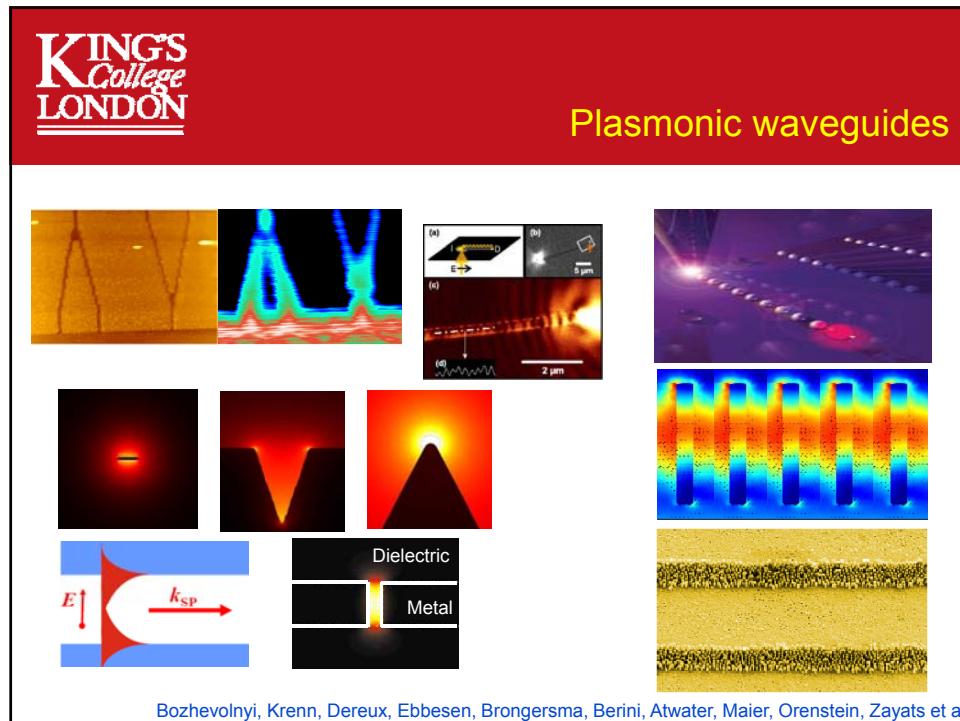
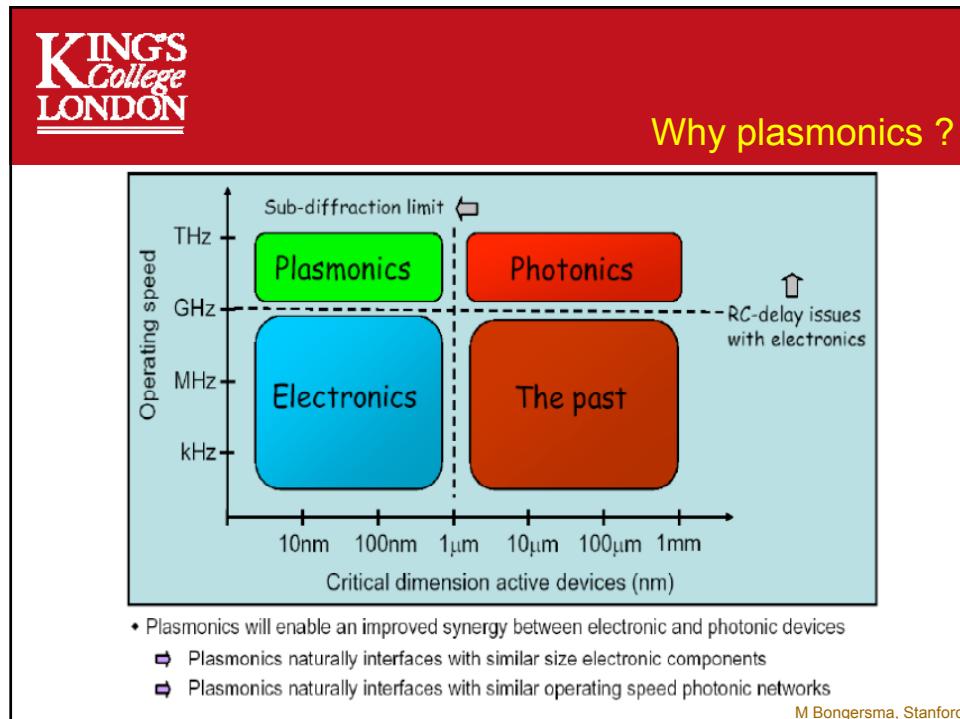
- Defect size
- Defect shape
- Defect dielectric constant

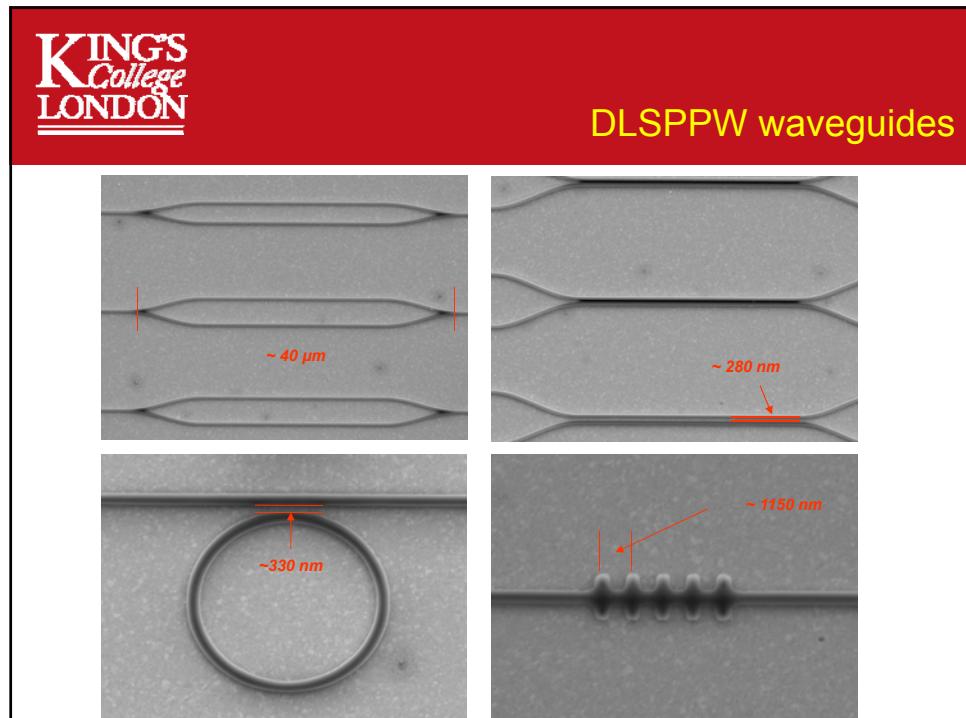
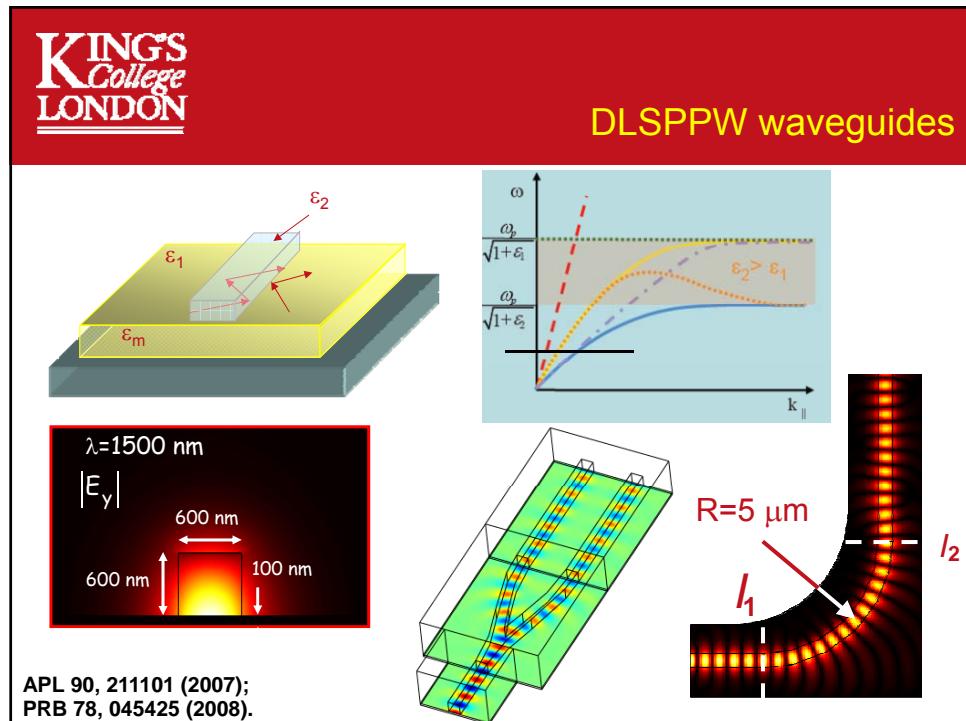


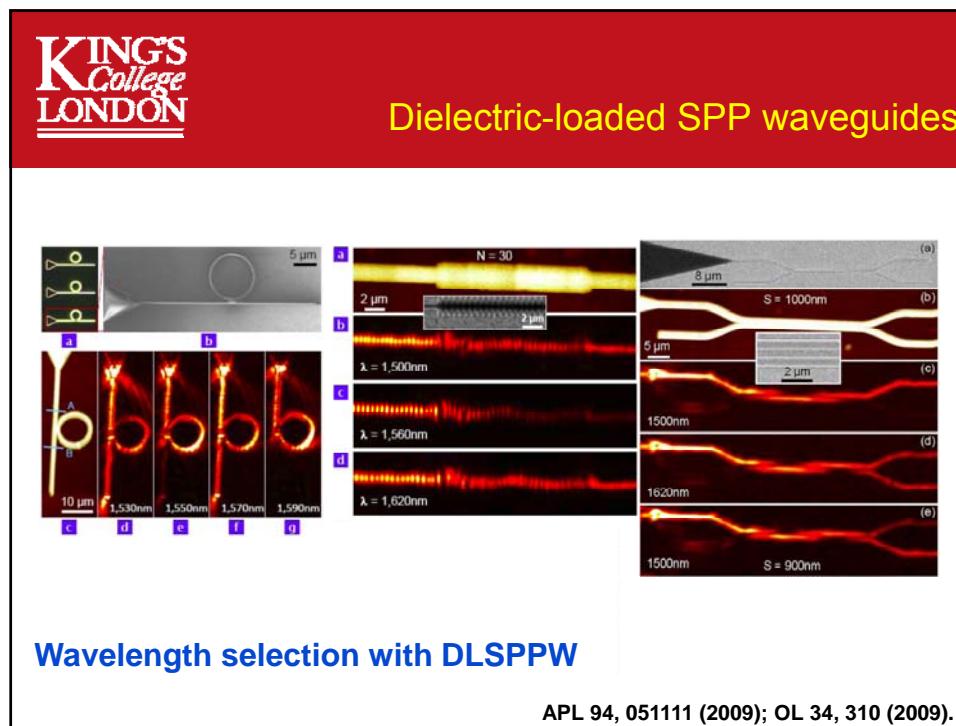
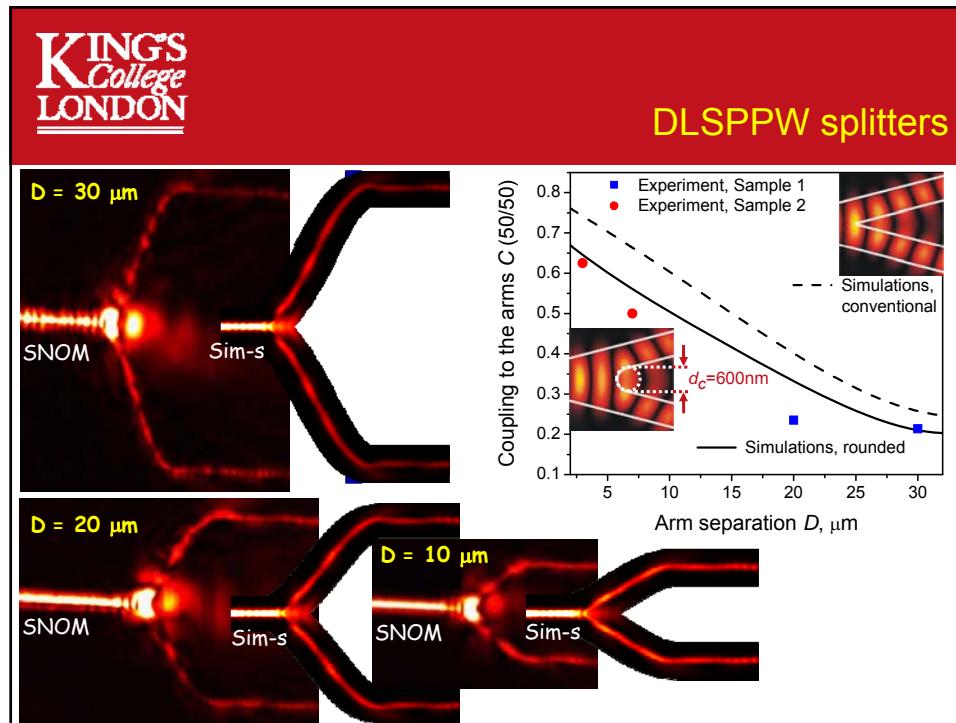
### 2D optics of surface polaritons

- SPP mirrors
- SPP lenses
- SPP resonators
- SPP crystals









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### Active DLSPPW components

WRR transmission  $T$  vs  $\Delta n$  plot showing resonance at  $n_0 + \Delta n$ . The inset shows the refractive index distribution  $M(\mu\text{m}^{-1})$  versus ring radius  $R(\mu\text{m})$ .

**Polymer can be “active”:**

- thermo-optical properties
- electro-optical properties
- nonlinear optical properties
- gain to compensate loss

**Resonant structures:**

- MZI
- waveguide ring resonator
- Bragg gratings

$$FOM \sim \frac{\partial T}{\partial \theta} \frac{\partial n_{eff}}{\partial n}$$

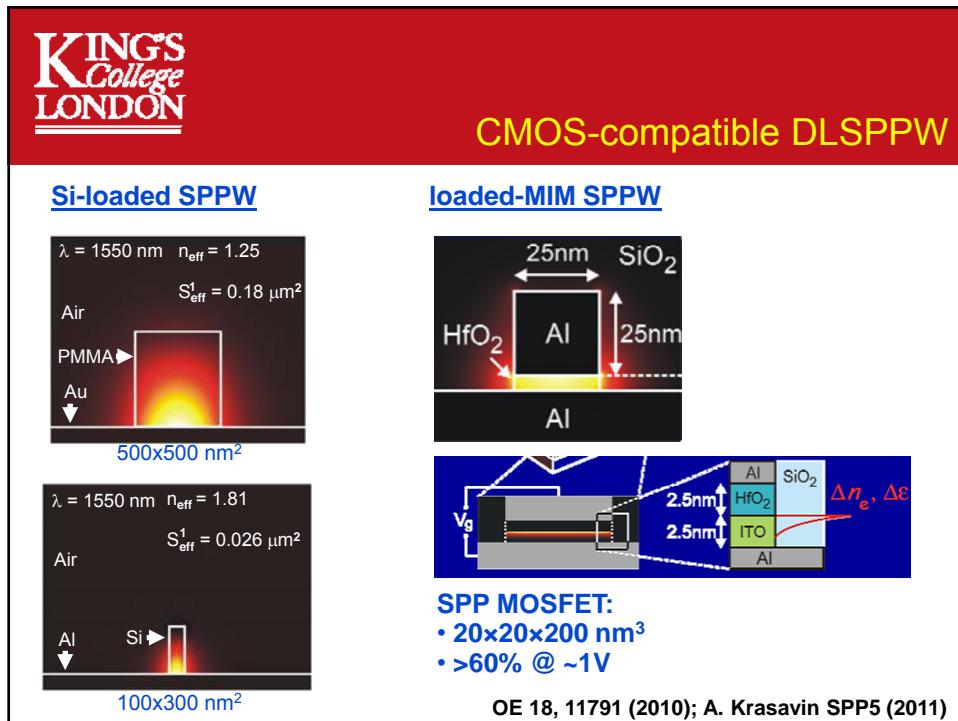
APL 97, 041107 (2010).

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### Si-SPP waveguides

**Si-loaded plasmonic waveguides**

Opt. Express 18, 11791 (2010).

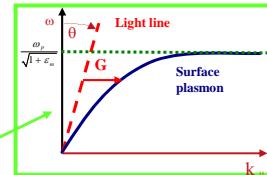
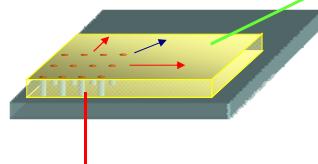




## Surface polaritonic crystals

$$k_{SP} = \frac{\omega}{c} \vec{u}_{xy} \delta_p \sin \theta \pm p \frac{2\pi}{D} \vec{u}_x \pm q \frac{2\pi}{D} \vec{u}_y$$

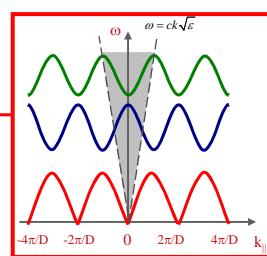
$$k_{SP} = \frac{\omega}{c} \left( \frac{\epsilon_m \epsilon_i}{\epsilon_m + \epsilon_i} \right)^{1/2}$$



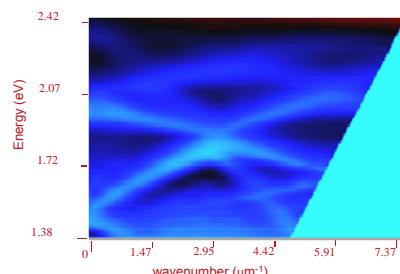
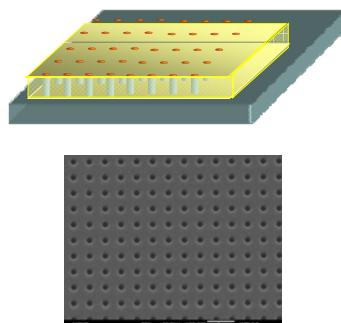
Periodic structure: SPP excitation

(p,q)-parameters:

- SPP spectrum
- SPP propagation direction

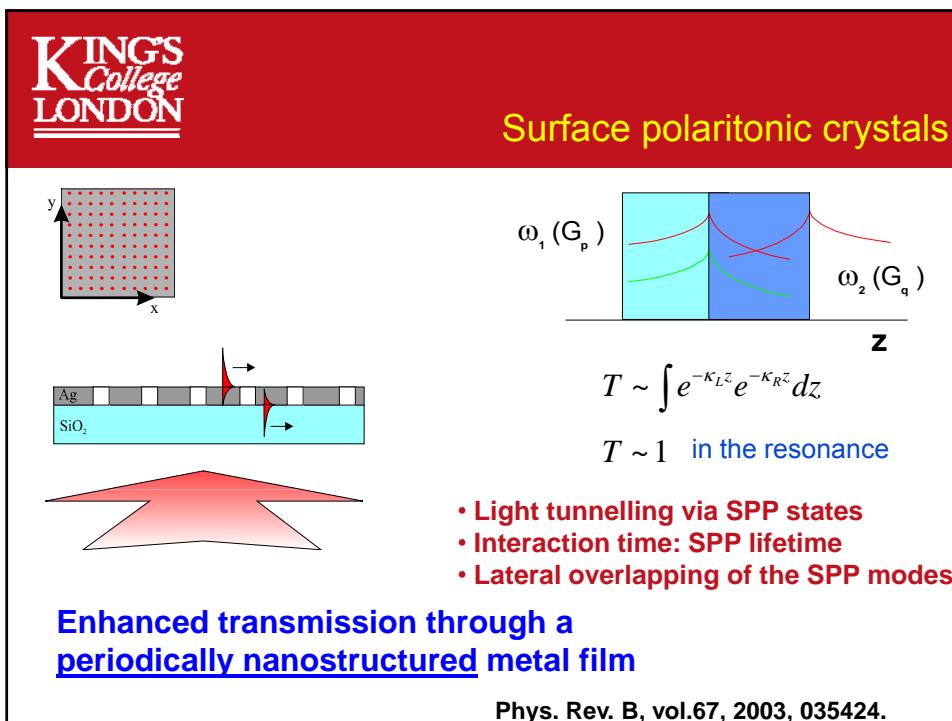
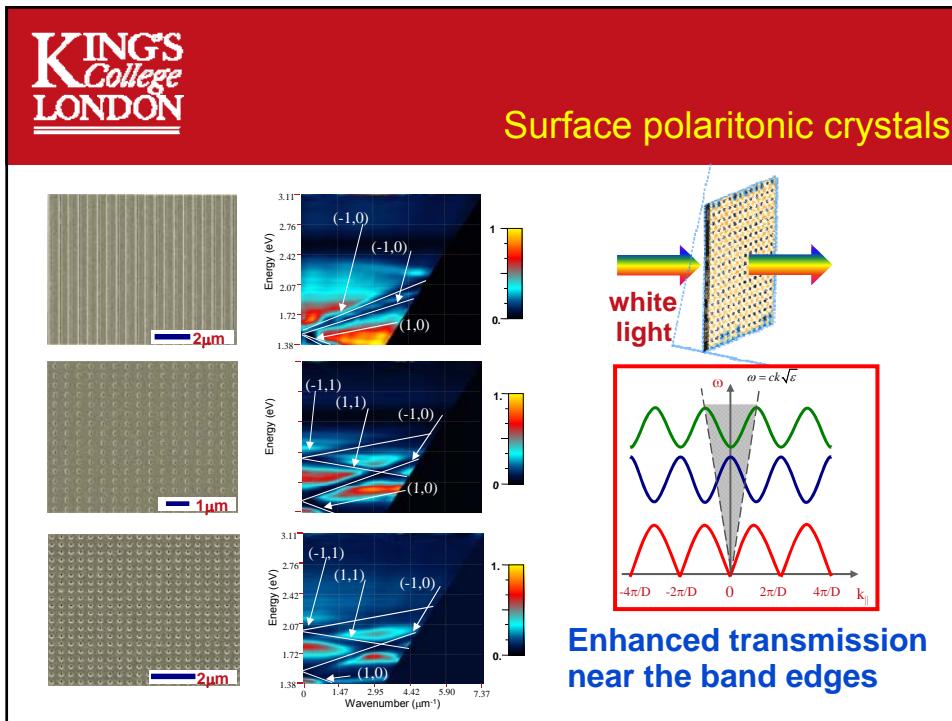


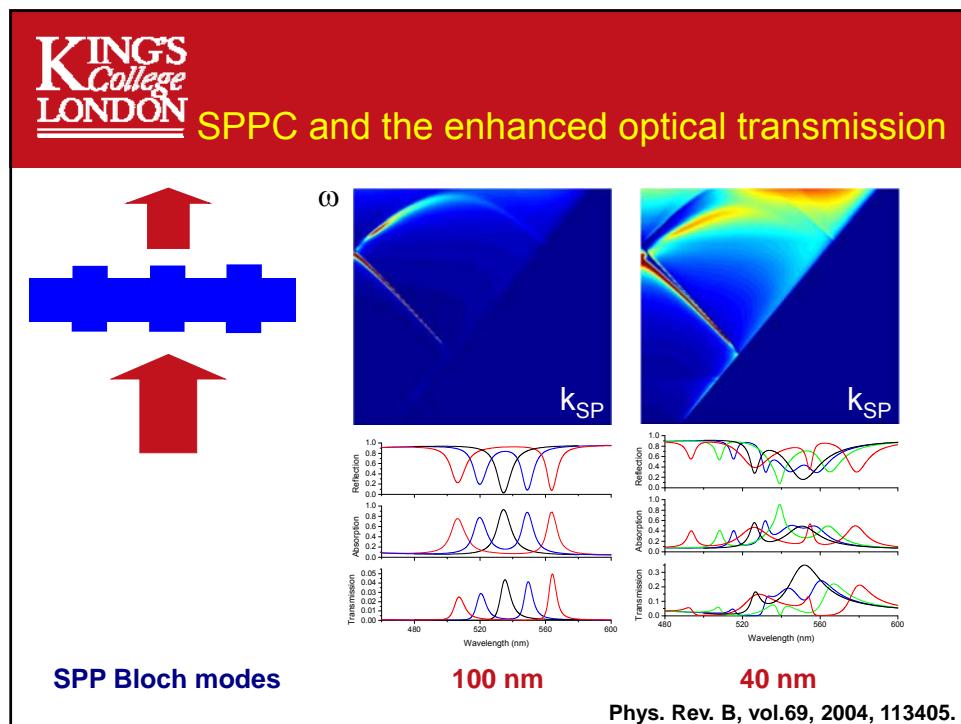
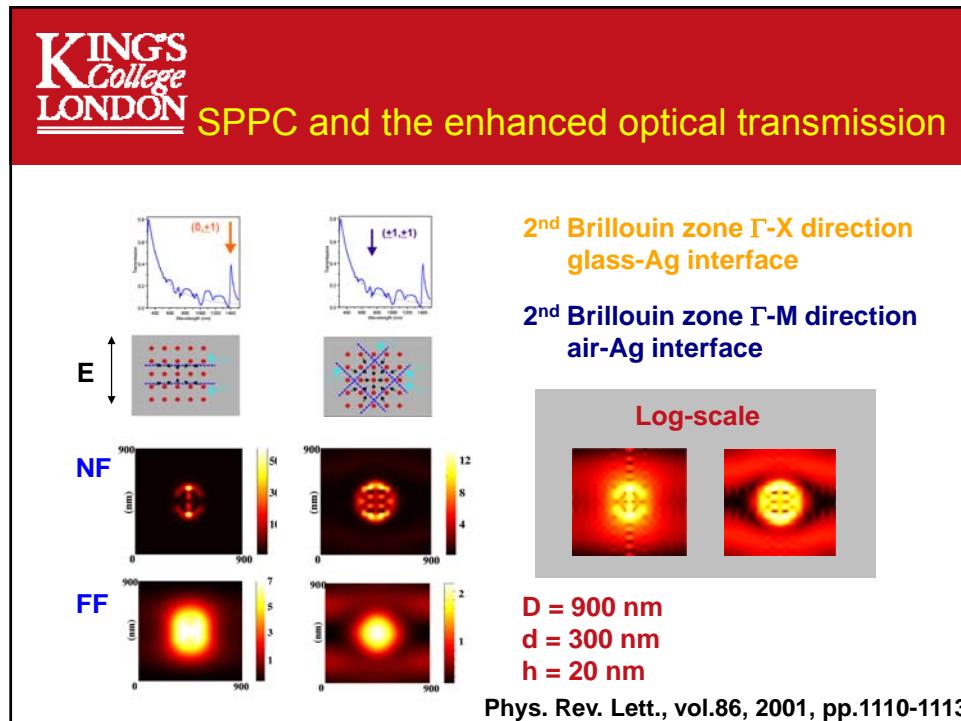
## Surface polaritonic crystals

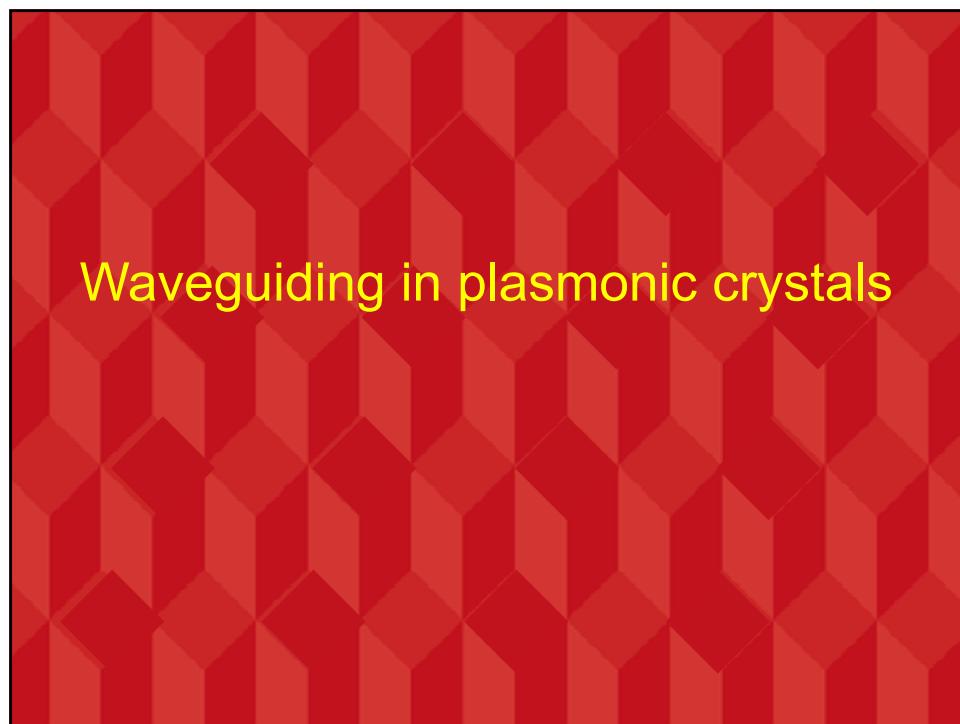
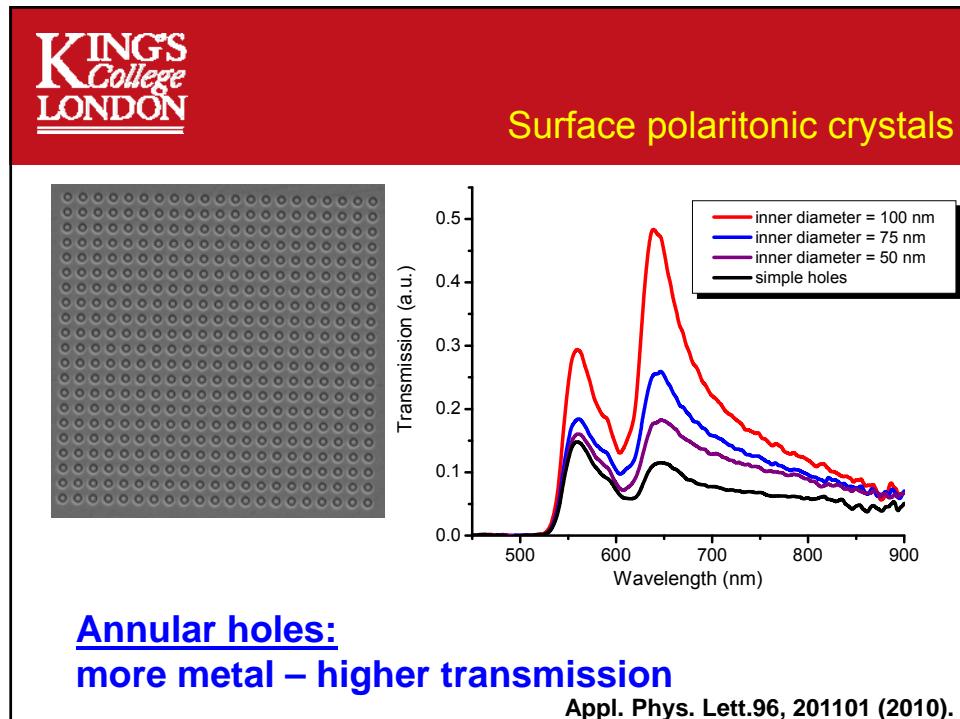


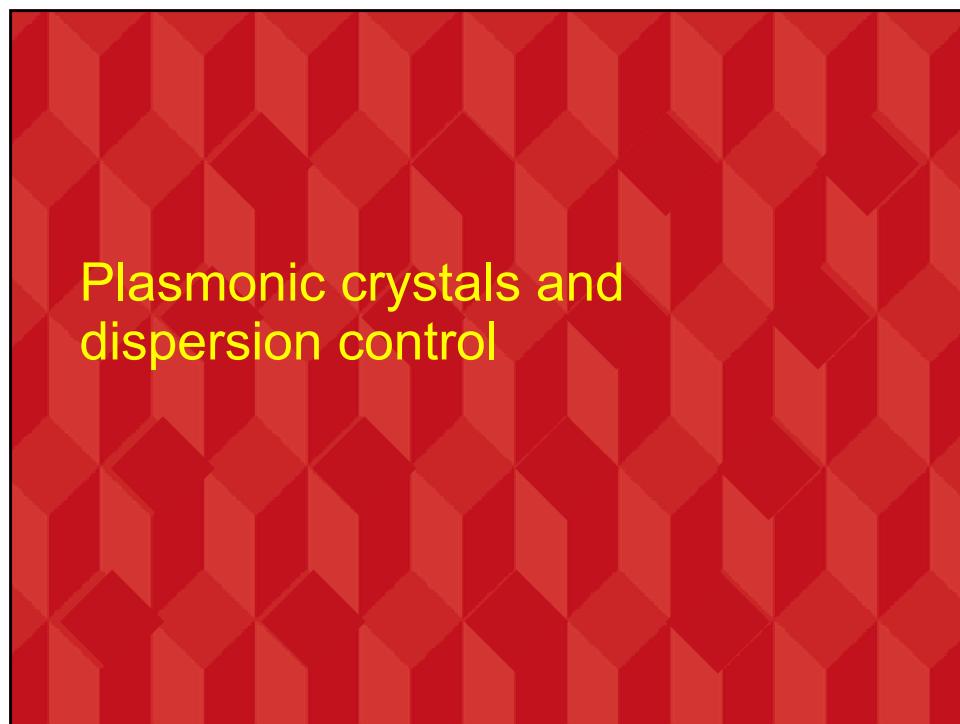
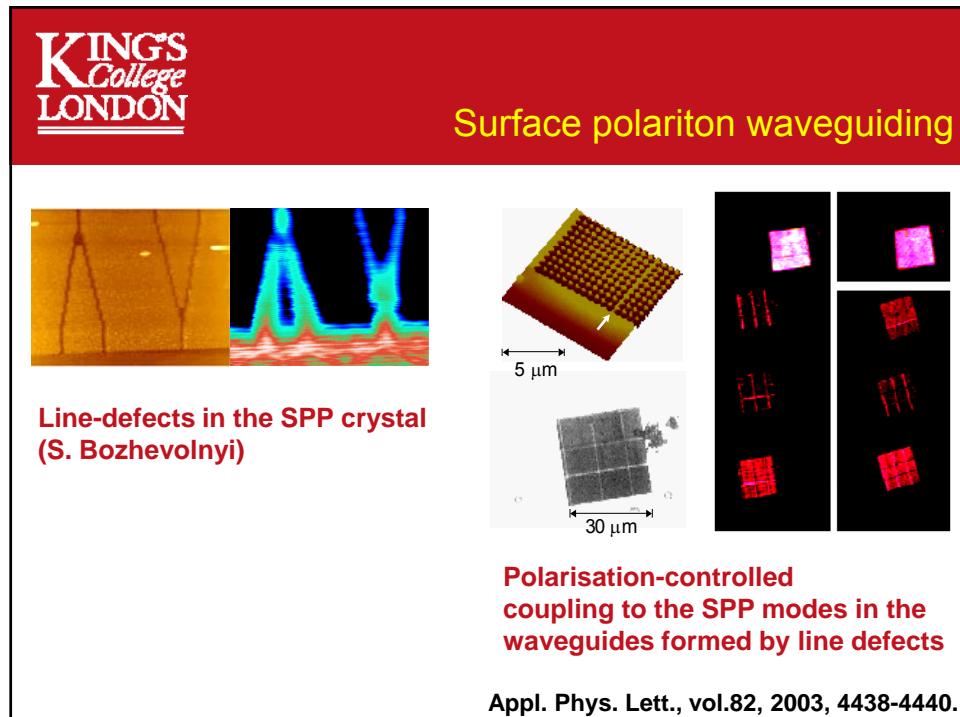
Flat SPP bands:

- field enhancement
- strong sensitivity to the refractive index changes



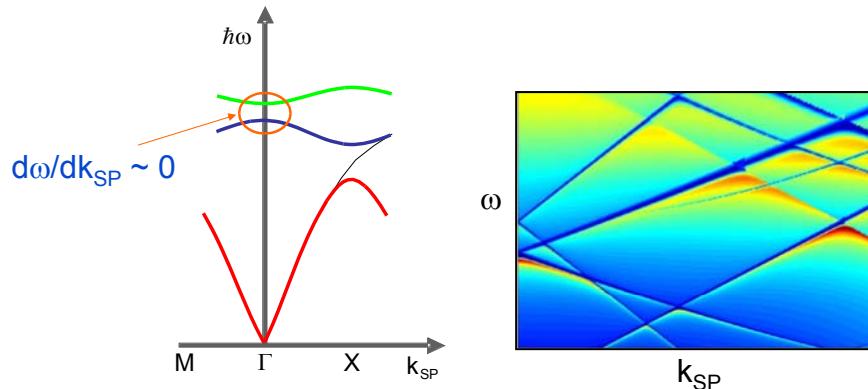




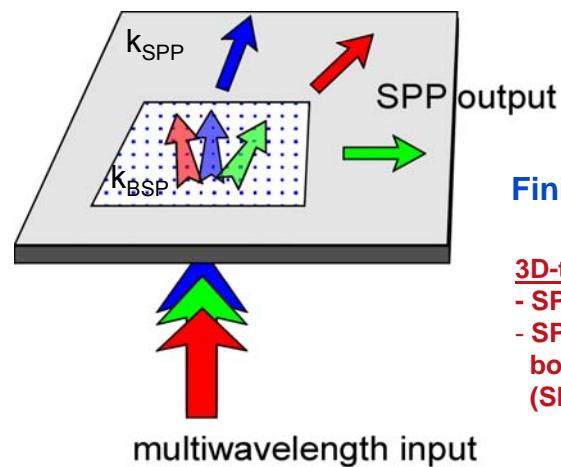




## Spectral dispersion of SPP crystal



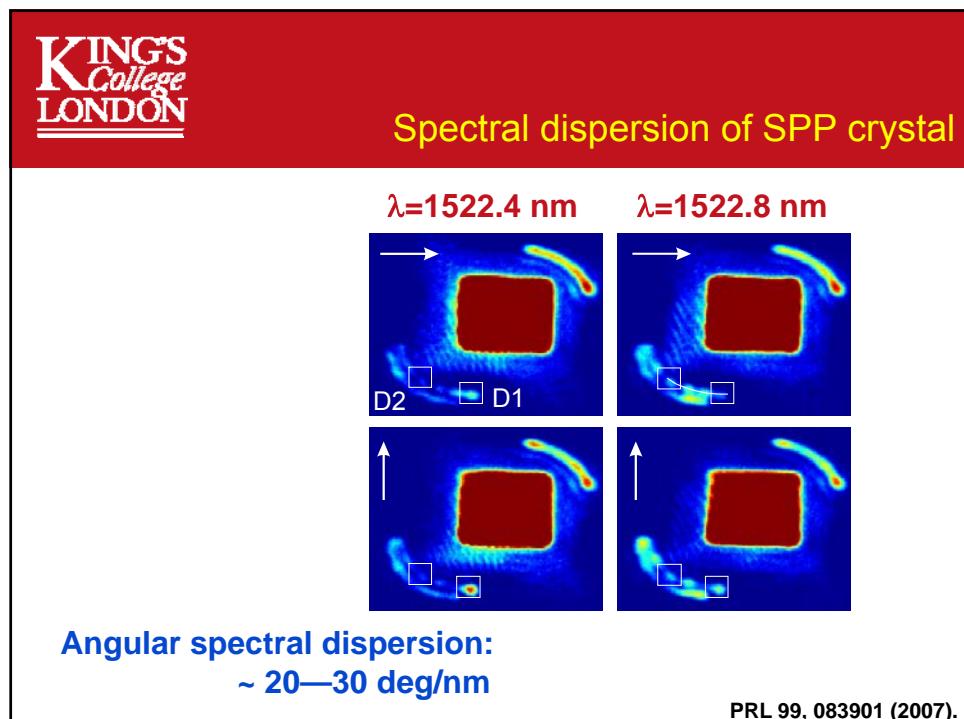
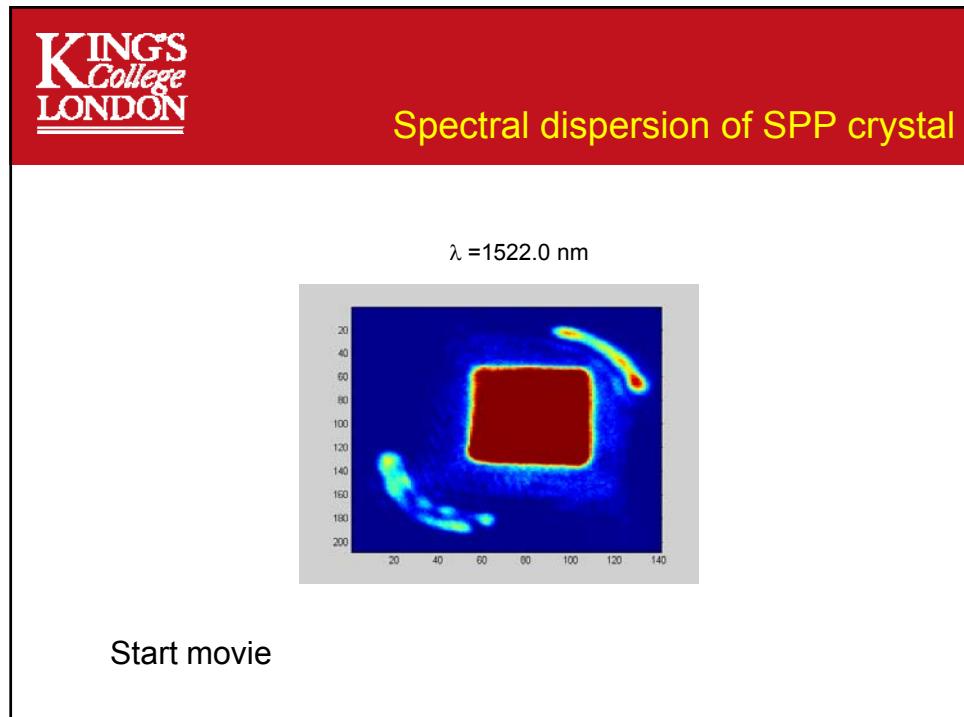
## Spectral dispersion of SPP crystal



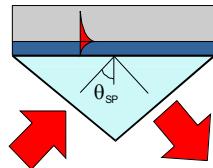
**Finite-size SPP crystal**

- 3D-to-2D diffraction**
- SPP Bloch mode excitation
- SPP modes crossing the boundary of SPP crystal (SPP refraction)

PRL 99, 083901 (2007).



## Plasmonic resonances



$$k_{SPP} = \frac{\omega}{c} \left( \frac{\epsilon_m \epsilon_d}{\epsilon_m + \epsilon_d} \right)^{1/2}$$

SPP and LSP resonances are extremely sensitive to dielectric environment:

$\epsilon_d = F(I_c)$  – optical control

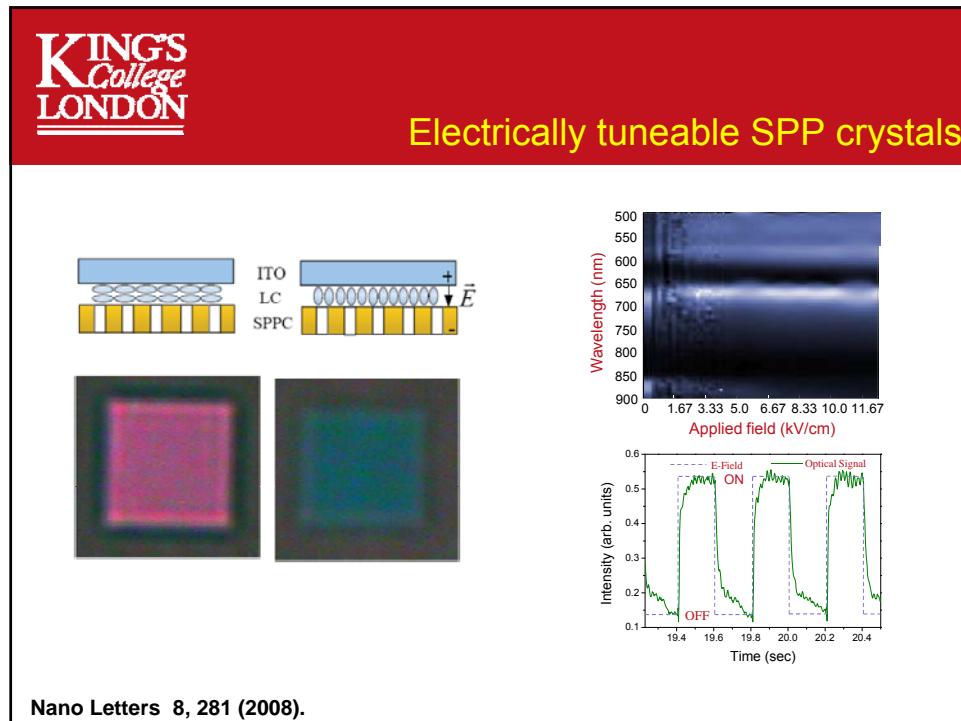
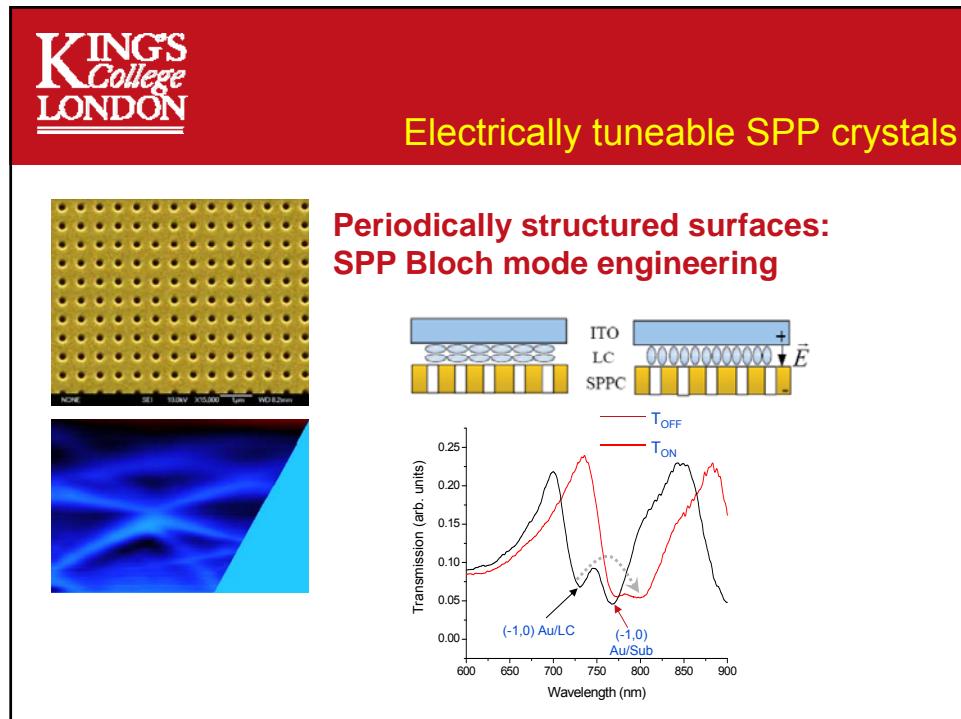
$\epsilon_d = F(E_{ext})$  – electric control

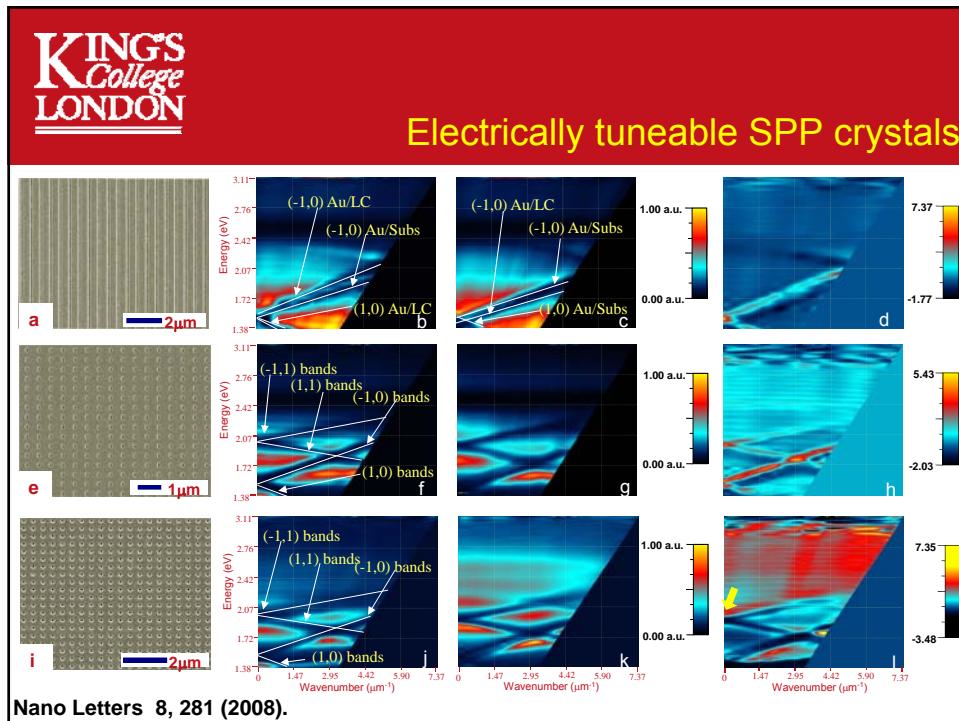
$\epsilon_d = F(M_{ext})$  – magnetic control

$\epsilon_d = F(f_{ext})$  – mechanical control

$\epsilon_d = F(T)$  – temperature control

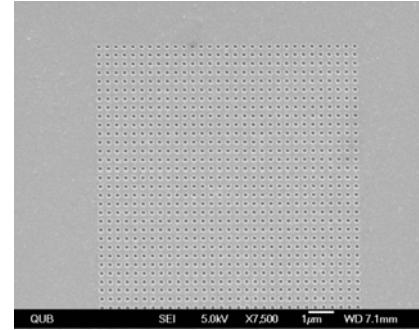
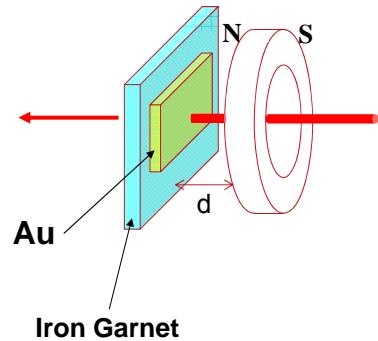
Electronically controlled SPPC







## Magneto-plasmonic crystals

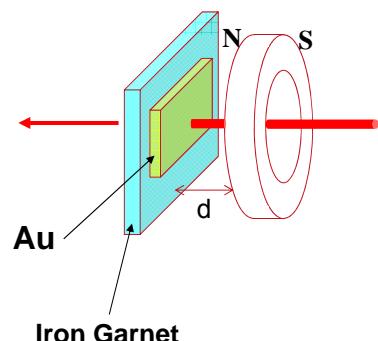


### Magneto-plasmonic crystal

New J. Phys. 10, 105012 (2008).



## Magneto-plasmonic crystals



$$\varepsilon = \begin{pmatrix} \varepsilon_0 & i\varepsilon_p & i\varepsilon_t \\ -i\varepsilon_p & \varepsilon_0 & i\varepsilon_l \\ -i\varepsilon_t & -i\varepsilon_l & \varepsilon_0 \end{pmatrix}$$

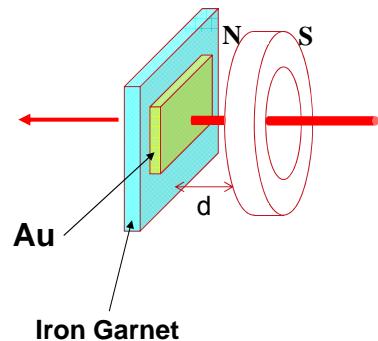
SPP field ( $E_x, E_z$ )

$\varepsilon_i = f(M) - ?$

### Magneto-plasmonic crystal

New J. Phys. 10, 105012 (2008).

## Magneto-plasmonic crystals



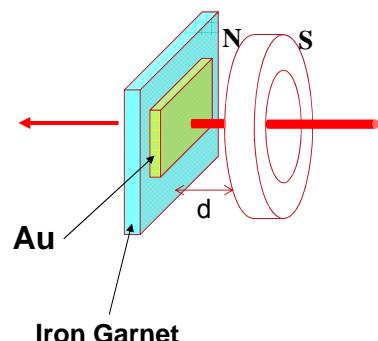
$$\varepsilon = \begin{pmatrix} \varepsilon_0 & i\varepsilon_p & i\varepsilon_t \\ -i\varepsilon_p & \varepsilon_0 & i\varepsilon_l \\ -i\varepsilon_t & -i\varepsilon_l & \varepsilon_0 \end{pmatrix}$$

No external magnetic field  
 (in-plane magnetisation)

### Magneto-plasmonic crystal

New J. Phys. 10, 105012 (2008).

## Magneto-plasmonic crystals

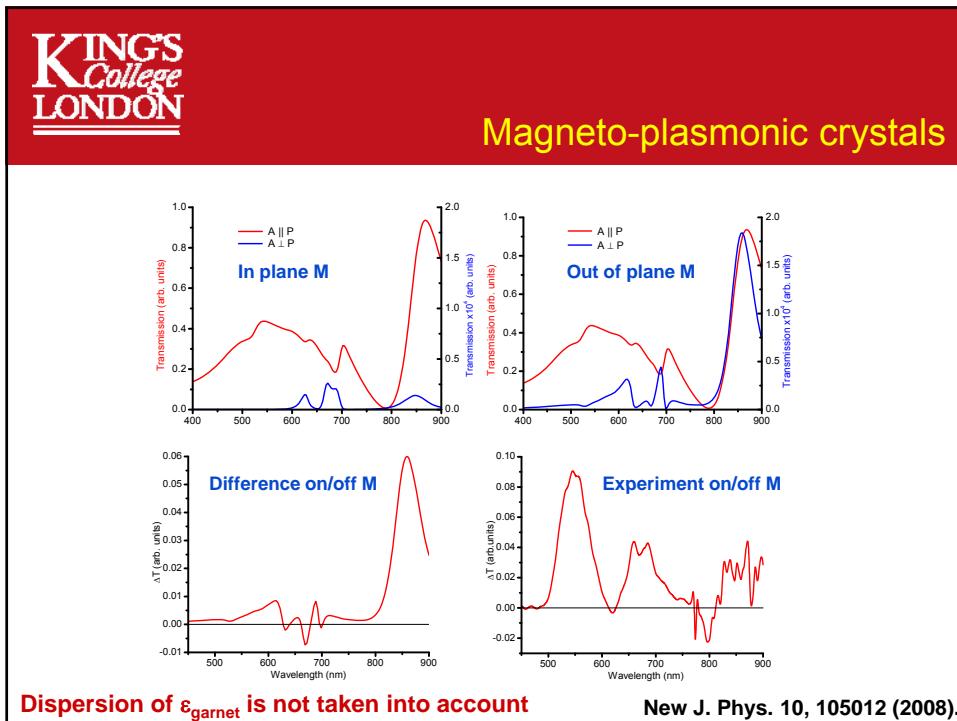
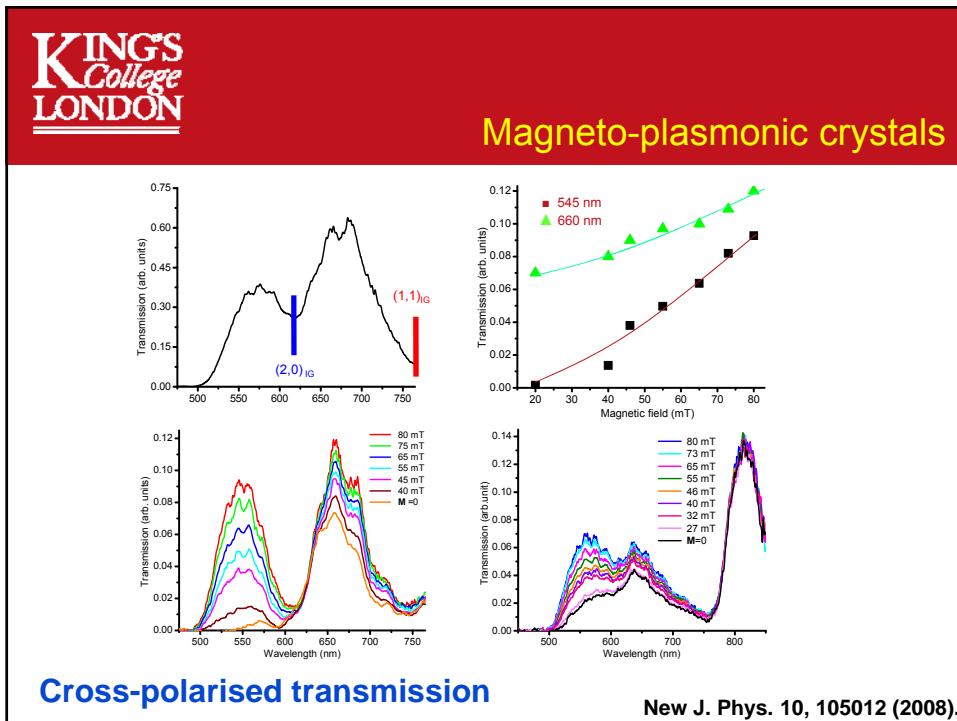


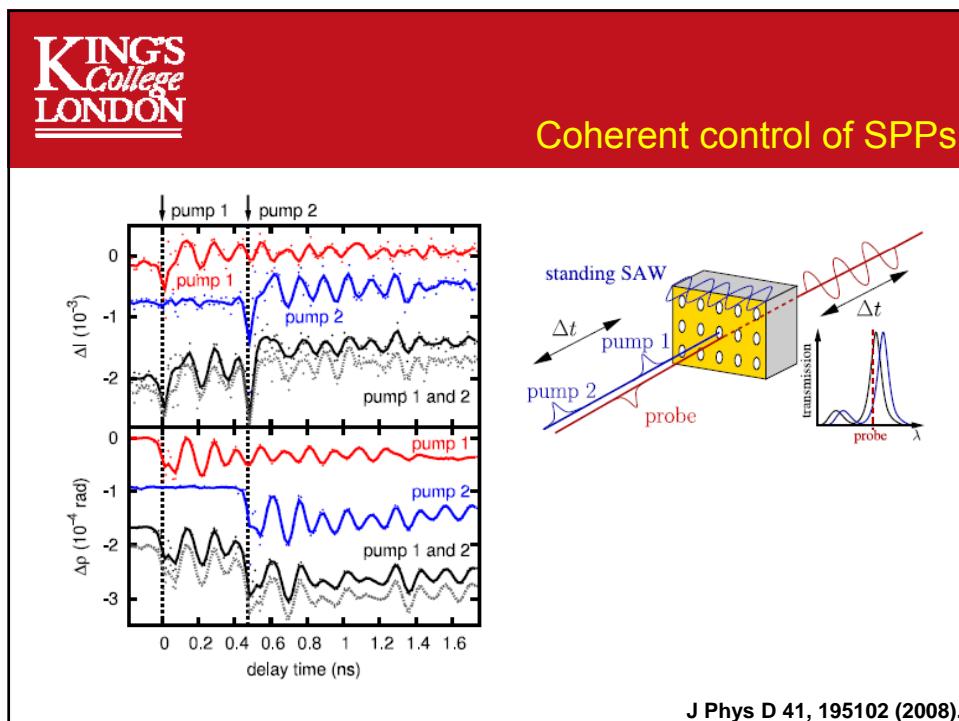
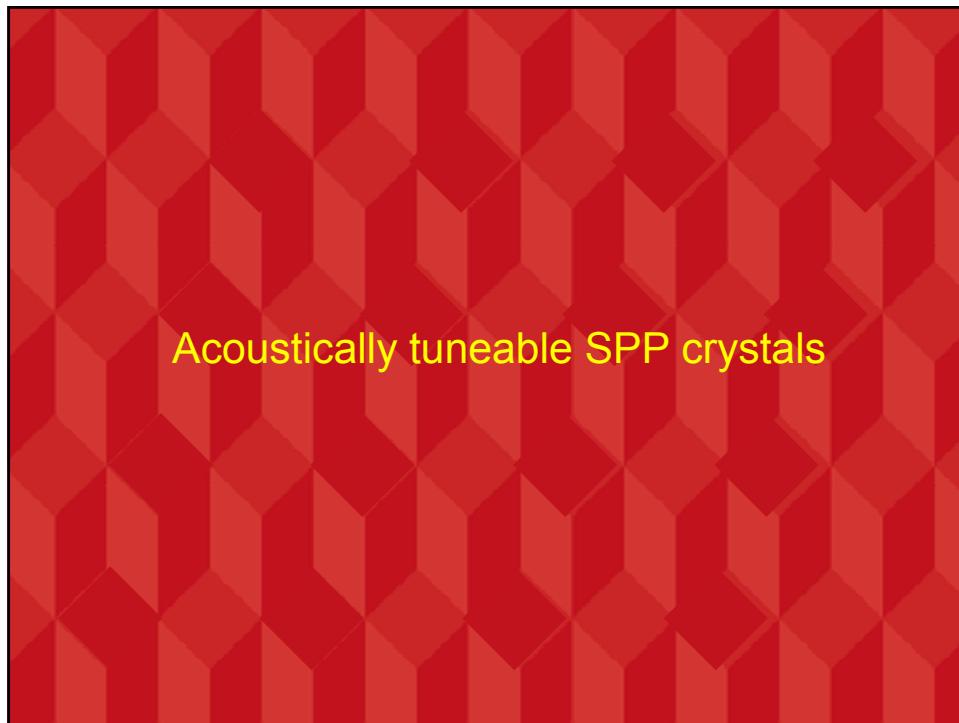
$$\varepsilon = \begin{pmatrix} \varepsilon_0 & i\varepsilon_p & i\varepsilon_t \\ -i\varepsilon_p & \varepsilon_0 & i\varepsilon_l \\ -i\varepsilon_t & -i\varepsilon_l & \varepsilon_0 \end{pmatrix}$$

External magnetic field  
 normal to the film  
 (out-of-plane magnetisation)

### Magneto-plasmonic crystal

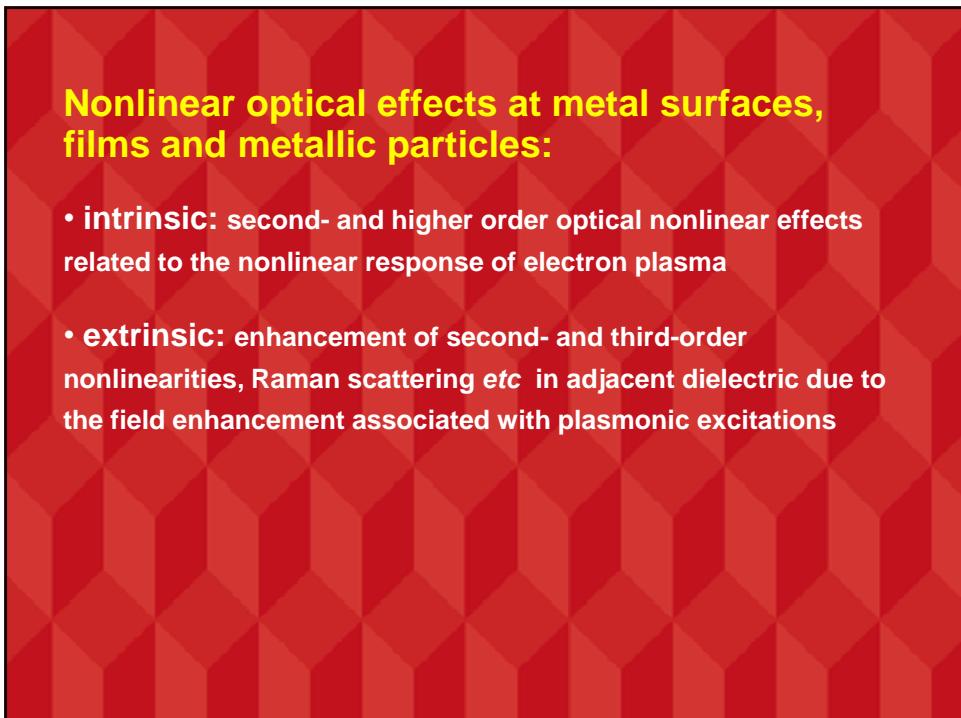
New J. Phys. 10, 105012 (2008).







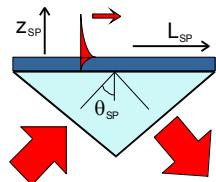
Nonlinear SPPC  
(all-optical effects)



**Nonlinear optical effects at metal surfaces,  
films and metallic particles:**

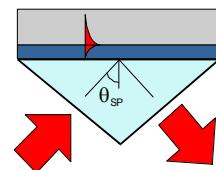
- **intrinsic:** second- and higher order optical nonlinear effects related to the nonlinear response of electron plasma
- **extrinsic:** enhancement of second- and third-order nonlinearities, Raman scattering etc in adjacent dielectric due to the field enhancement associated with plasmonic excitations

## Nonlinearity and surface plasmons



**Electromagnetic field enhancement:**

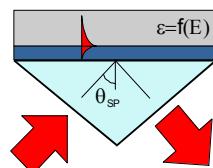
$$T = \left| \frac{E_{SP}(0^+)}{E_0} \right| \gg 1$$



**SPP resonance is sensitive to the dielectric constant of surroundings:**

$$k_{SP} = \frac{\omega}{c} \left( \frac{\epsilon_m \epsilon_i}{\epsilon_m + \epsilon_i} \right)^{1/2}$$

## Nonlinearity and surface plasmons

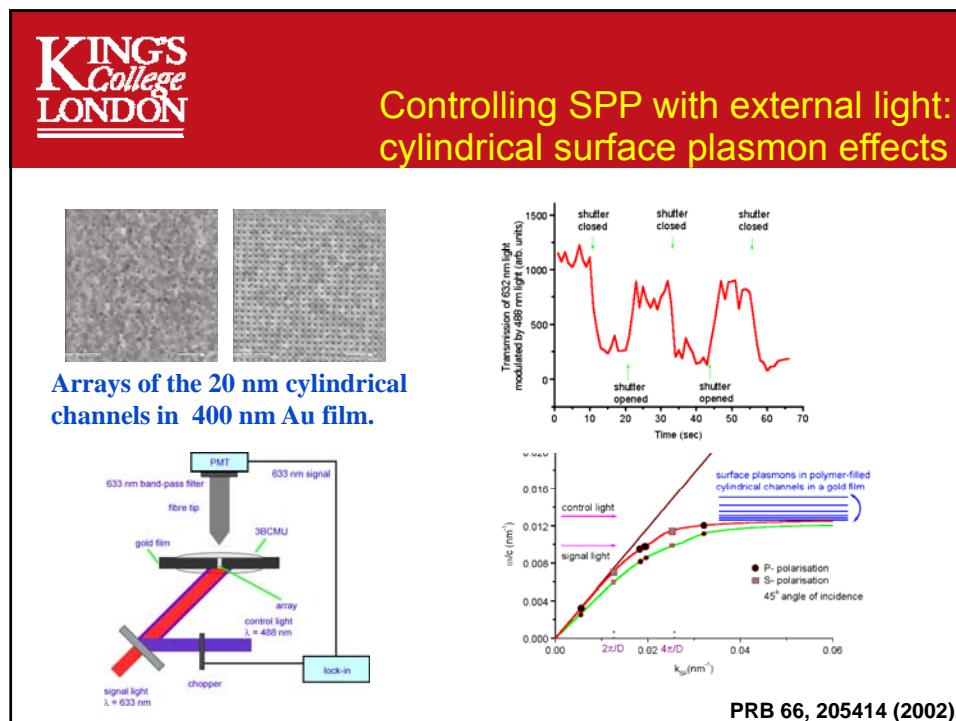
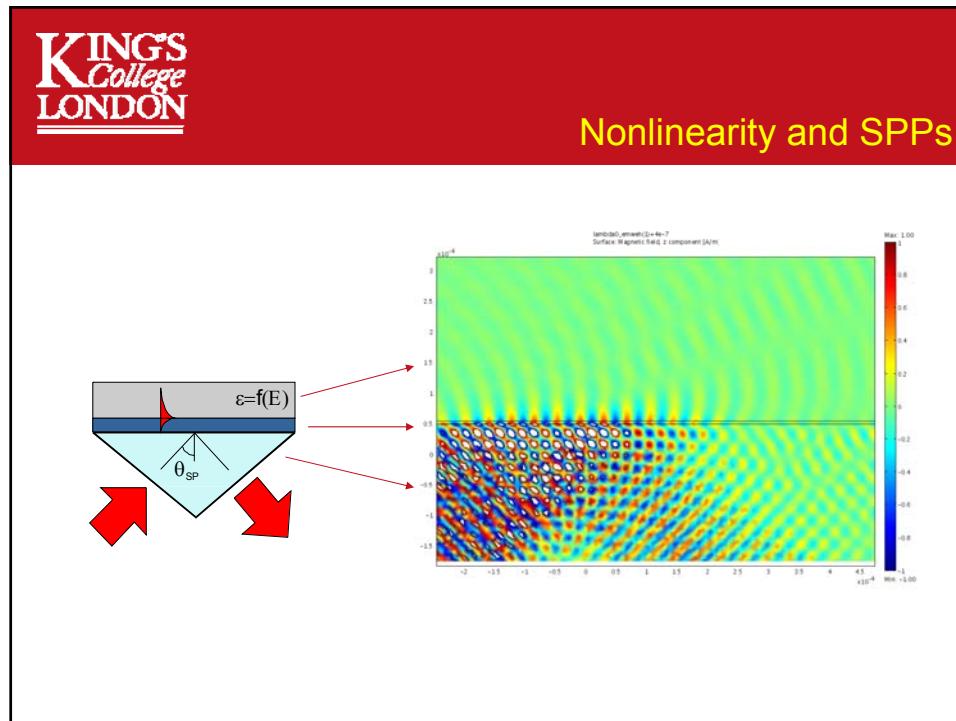


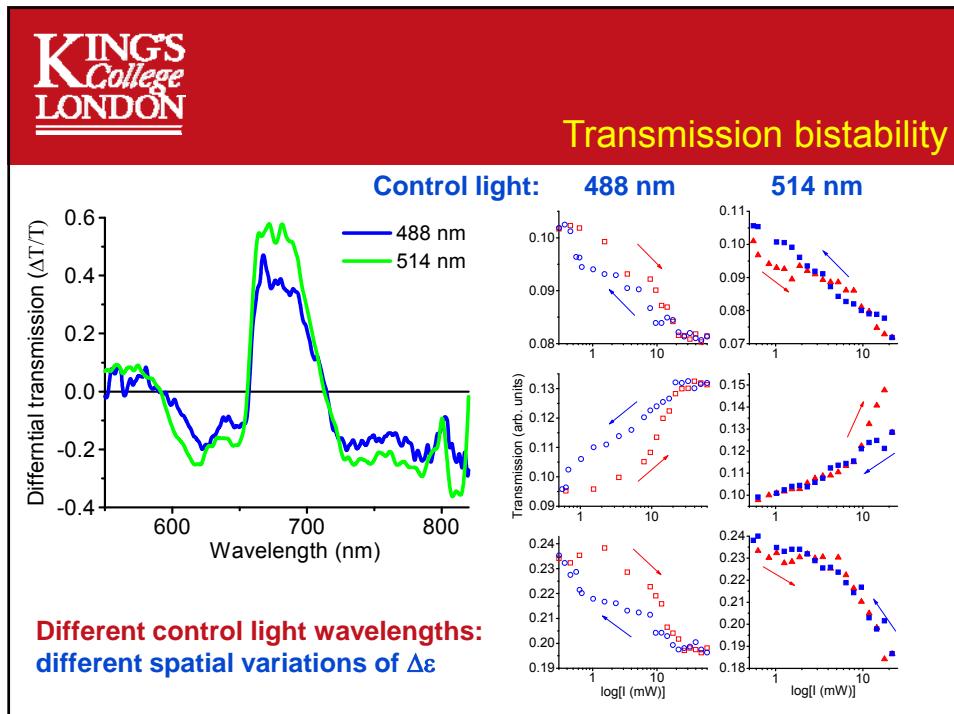
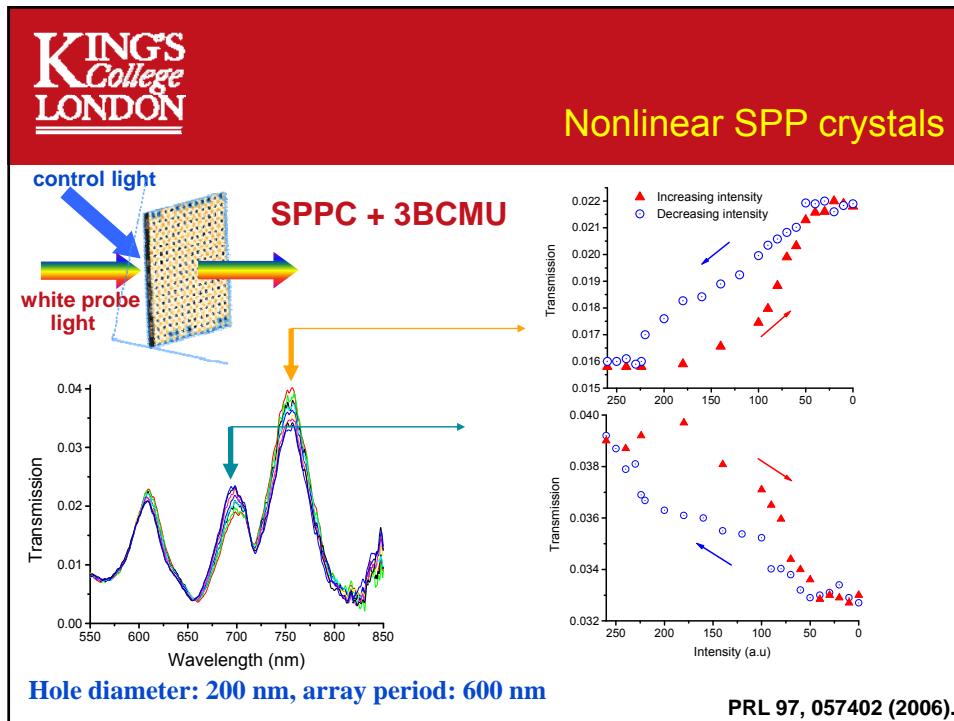
$$\epsilon_i = \epsilon_0 + 4\pi\chi^{(3)}|E_L|^2$$

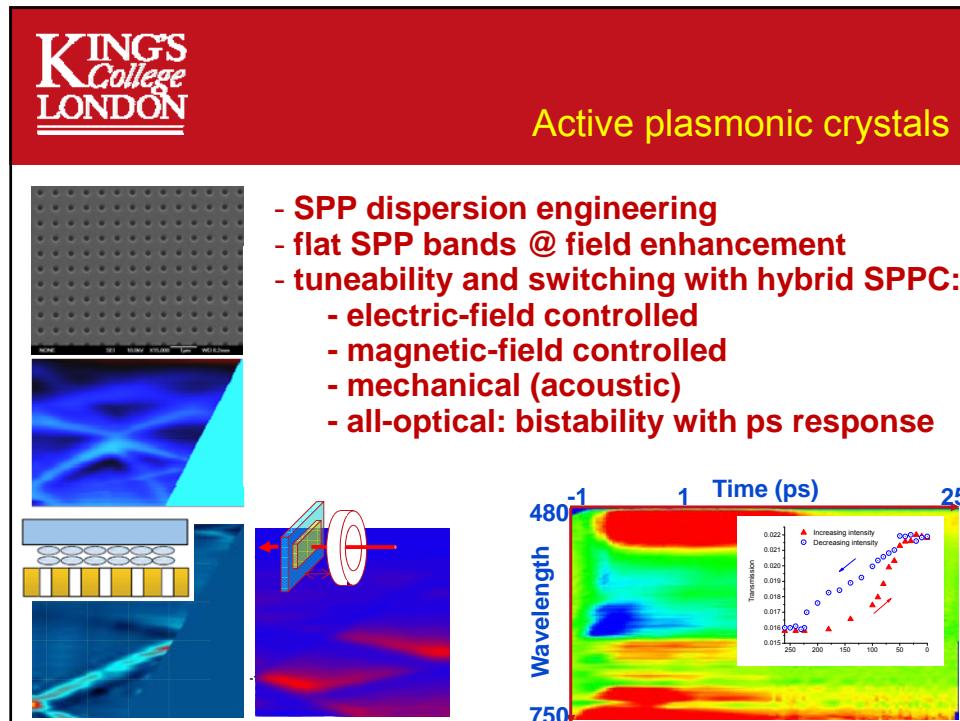
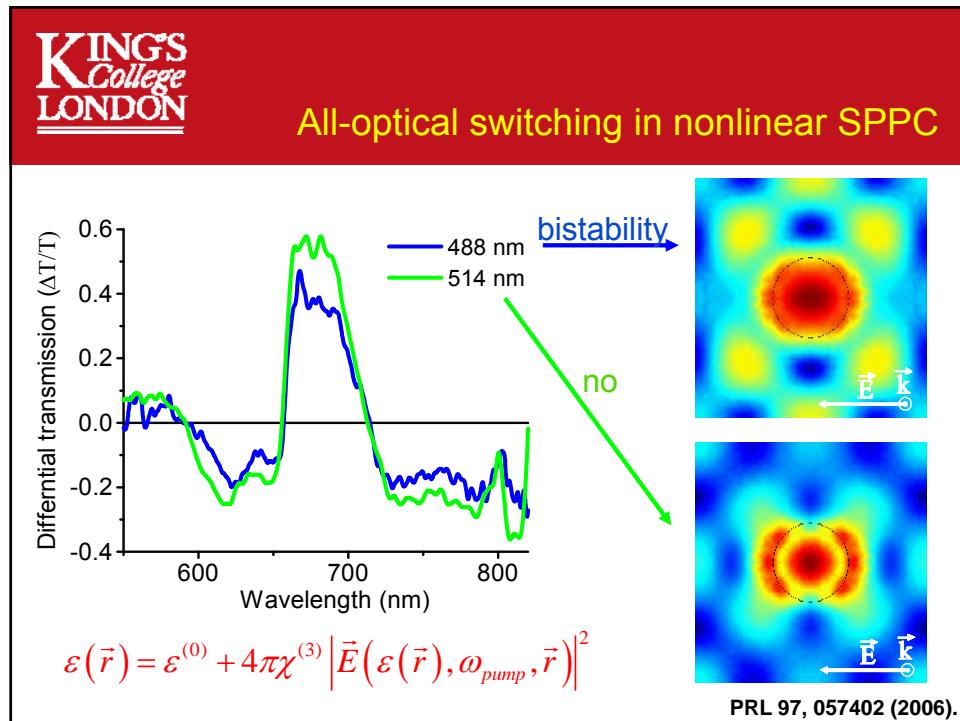
$$k_{SP} = \frac{\omega}{c} \left( \frac{\epsilon_m \epsilon_i}{\epsilon_m + \epsilon_i} \right)^{1/2}$$

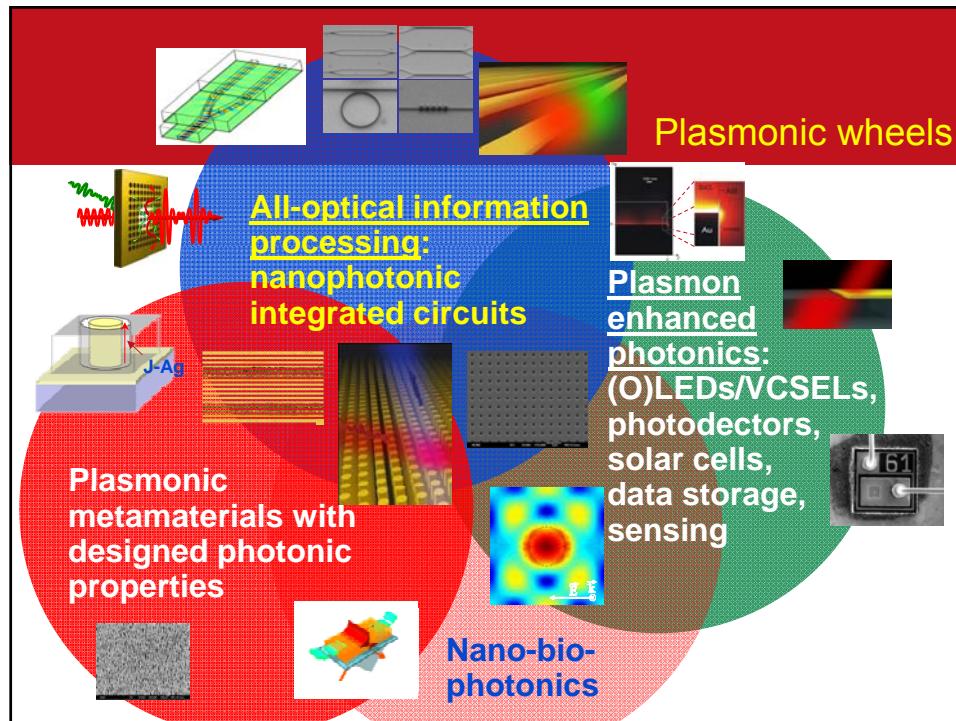
**Kerr-nonlinearity for controlling SPPs with SPPs**

Laser & Photon. Rev. 2, 125 (2008).









## Take home messages (1):

- Functional plasmonics with nanostructured metal films
- Plasmonics waveguides (careful analysis before choosing)
- Surface-plasmon polaritonic crystals:  
optical properties are determined by SPP Bloch modes  
 $SPPC + \text{functional dielectric} = \text{optical metamaterial with controlled optical properties}$   
optical control of SPP modes  
electric control of SPP modes  
acoustic (coherent) control of SPP modes  
magnetic control of SPP modes



**Fast growing area (follow new publications)**

- Nano-optics of surface plasmon polaritons,  
Phys. Rep., vol.408, 2005, pp.131-314.
- Near-field photonics: surface plasmon polaritons and localised  
surface plasmons, J. Opt. A: Pure Appl. Opt., vol. 5, 2003, pp.S16-S50.
- Nonlinear surface plasmon polaritonic crystals,  
Laser and Photon. Rev., vol. 2, 2008, pp. 125-135.
- Optics of metallic nanostructures, in *Handbook of Nanoscale Optics and Electronics*, G. Wiederrecht, Ed., pp. 1-52 (Elsevier, 2009).
- D. Richards, A.V. Zayats, Eds., *Nano-optics and near-field optical microscopy* (Artech, Boston, 2008), ISBN: 978-1-59693-238-8.

**WWW.NANO-OPTICS.ORG.UK**