



**2333-19**

**Workshop on Science Applications of GNSS in Developing Countries (11-27 April), followed by the: Seminar on Development and Use of the Ionospheric NeQuick Model (30 April-1 May)**

*11 April - 1 May, 2012*

**Satellite Navigation for Guidance of Aircraft  
(Part 2)**

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# Satellite Navigation for Guidance of Aircraft



**Todd Walter**  
**Stanford University**

<http://waas.stanford.edu>



# Outline

- ➔ **Ionospheric Modeling**
- ➔ Ionospheric Threats
- ➔ Other Integrity Threats
- ➔ Integrity Methodology
- ➔ Next Generation Satellite Navigation
- ➔ Future Signals
- ➔ Conclusions



# How Are Measurements Correlated Over Distance?

- Translate Our Measurements of the Ionosphere Into User Corrections
- How Does the Ionosphere Behave Spatially?
  - *What is the underlying structure?*
  - *What does one measurement tell us about the nearby ionosphere?*
  - *How should we combine multiple samples?*
  - *What confidence can we have in our prediction?*
- We Need to Determine the Ionospheric Decorrelation Function



# “Supertruth” Data

- ➔ Raw Data Collected From Each WRS
  - ➔ *3 independent receivers per WRS*
- ➔ Postprocessed to Create “Supertruth”
  - ➔ *Carrier tracks “leveled” to reduce multipath*
  - ➔ *Interfrequency biases estimated and removed for satellites and receivers*
  - ➔ *Comparisons made between co-located receivers (voting to remove artifacts)*
- ➔ Multipath and Bias Residuals are ~50 cm
- ➔ Without Voting, Receiver Artifacts Cloud Results and Make It Impossible to See Tails of the Distribution



# Decorrelation Estimation

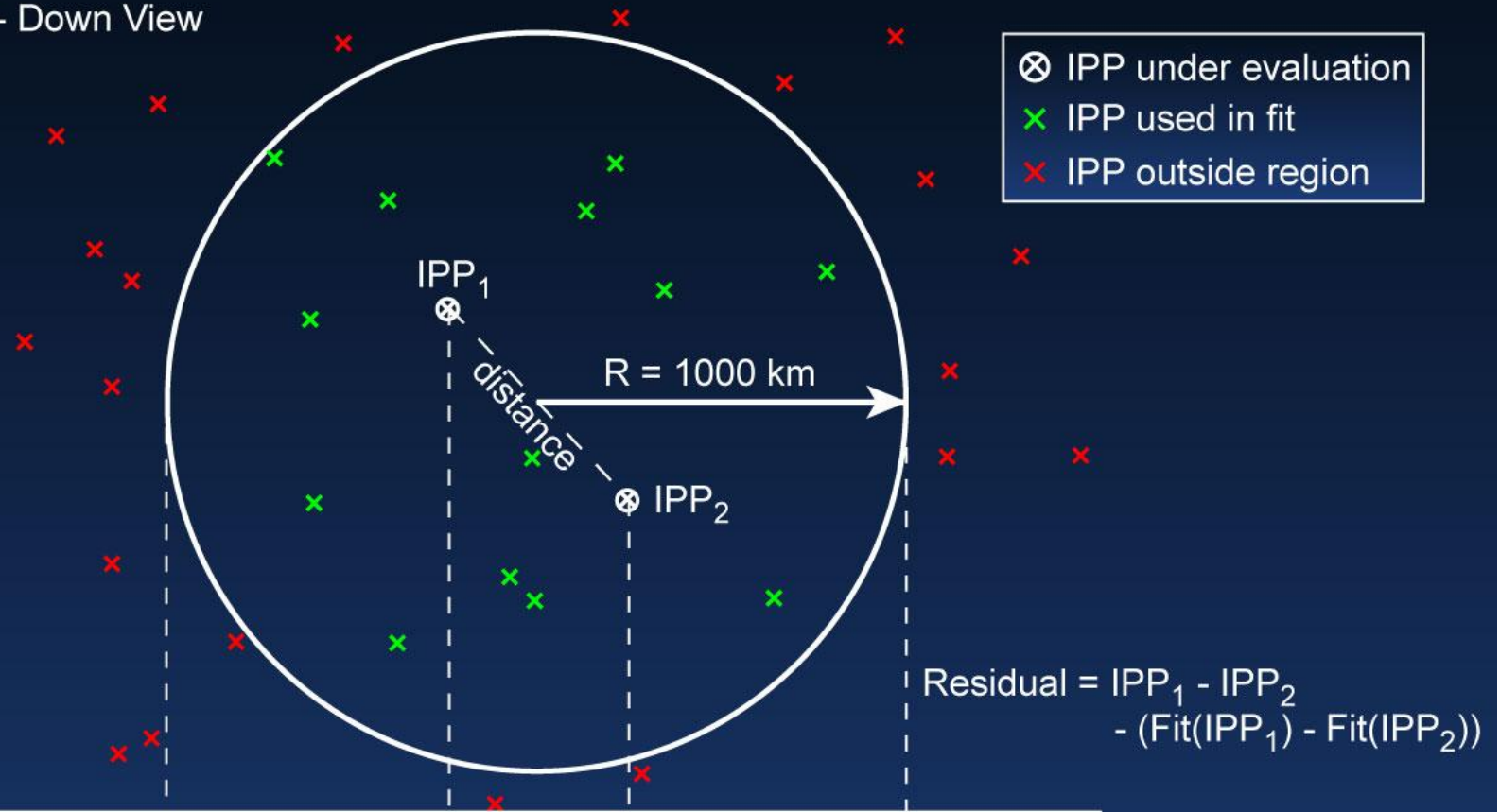
- ➔ Every Supertruth IPP Is Compared to All Others
- ➔ The Great Circle Distance Between the IPPs Is Calculated
- ➔ The Difference in Vertical Ionosphere Is Calculated
- ➔ A Two-dimensional Histogram Is Formed: Each Bin Corresponds to a Distance Range and a Vertical Difference Range
- ➔ Histogram Contains the Counts for Each Time an IPP Pair Fell in a Particular Bin





# Correlation Estimation Process

Top - Down View



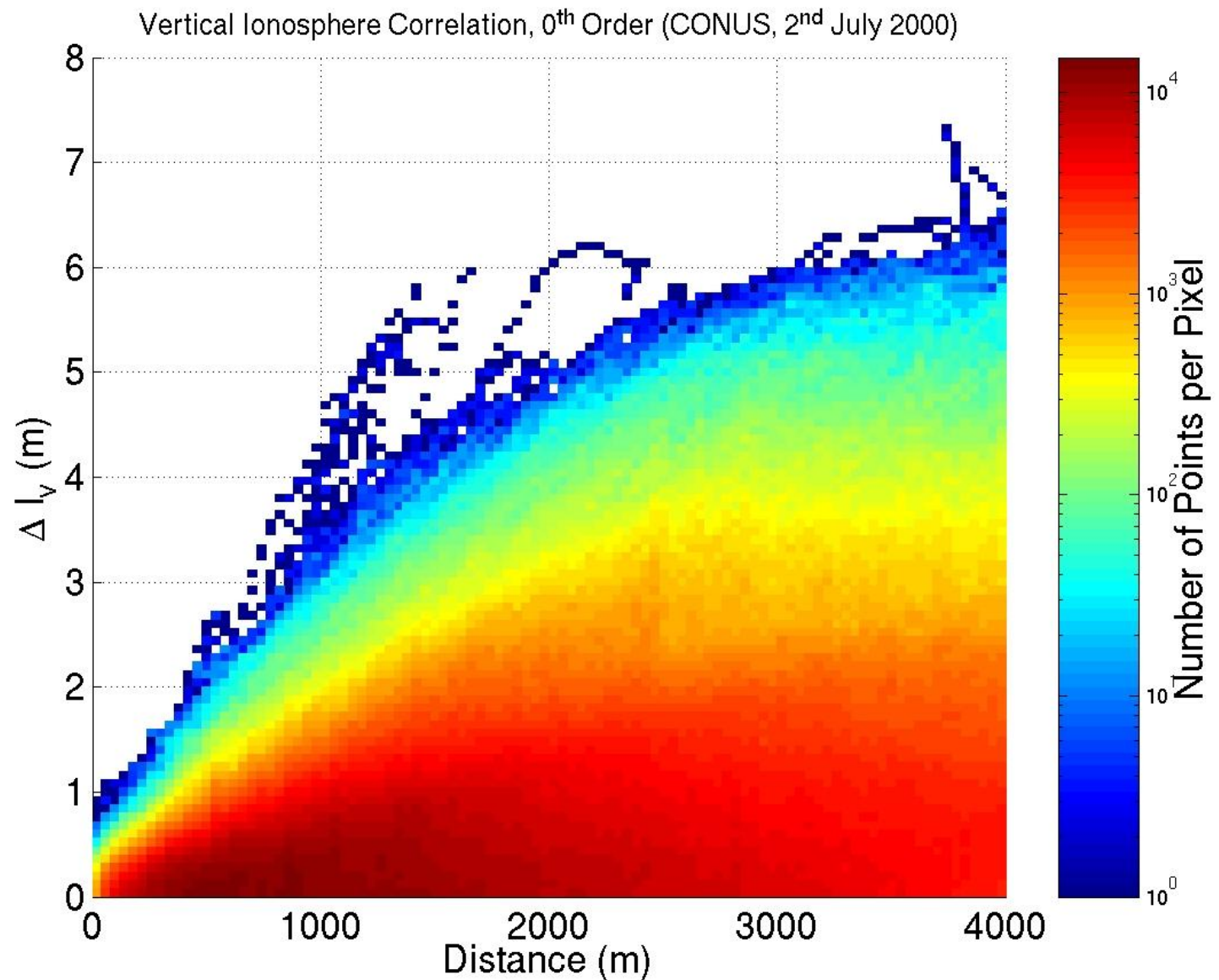
Side View



Presented at ICTP  
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# Ionospheric Decorrelation (0<sup>th</sup> Order)



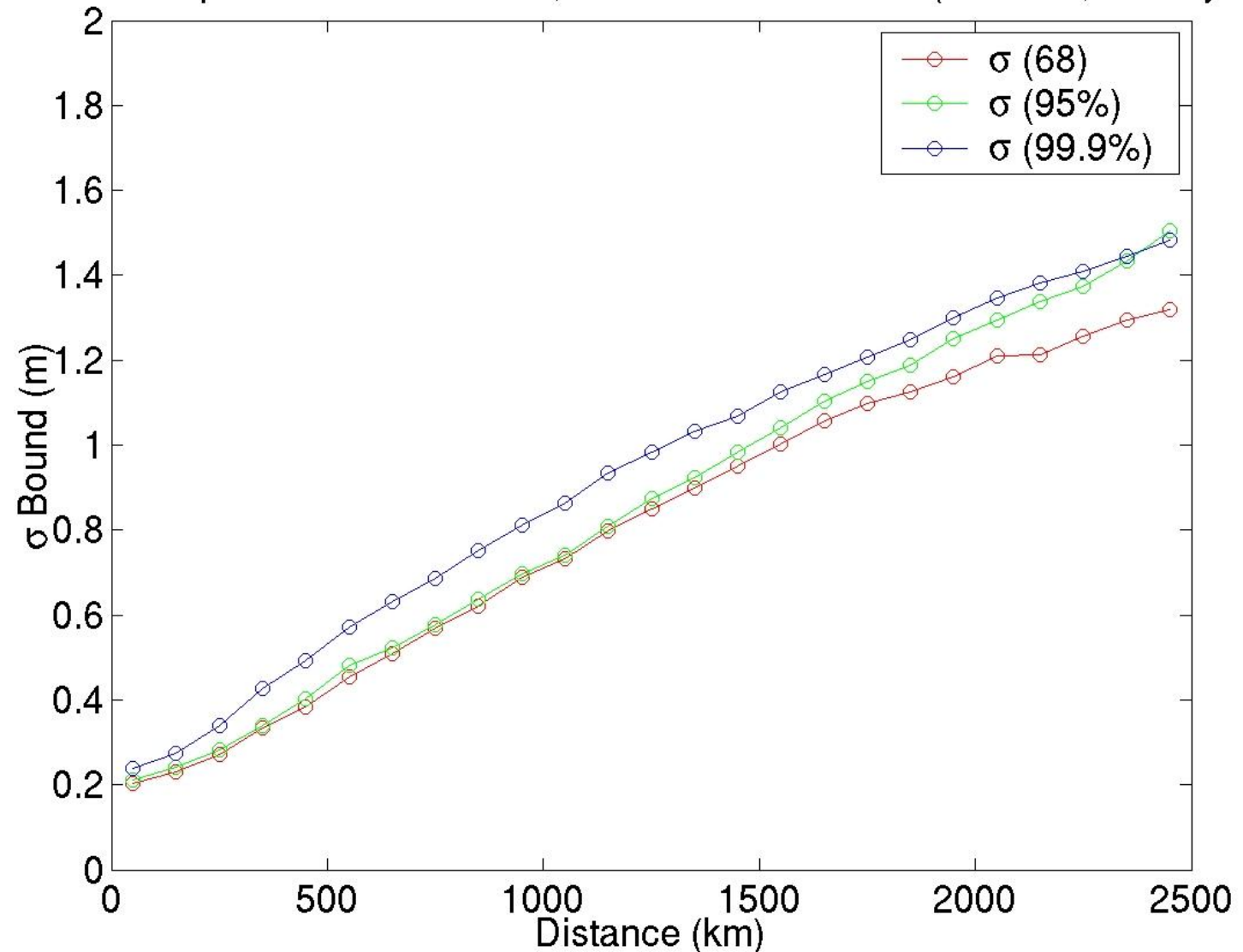
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# Ionospheric Decorrelation Function (0<sup>th</sup> Order)

Vertical Ionosphere Containment  $\sigma$ , 0<sup>th</sup> Order Correlation (CONUS, 2<sup>nd</sup> July 2000)





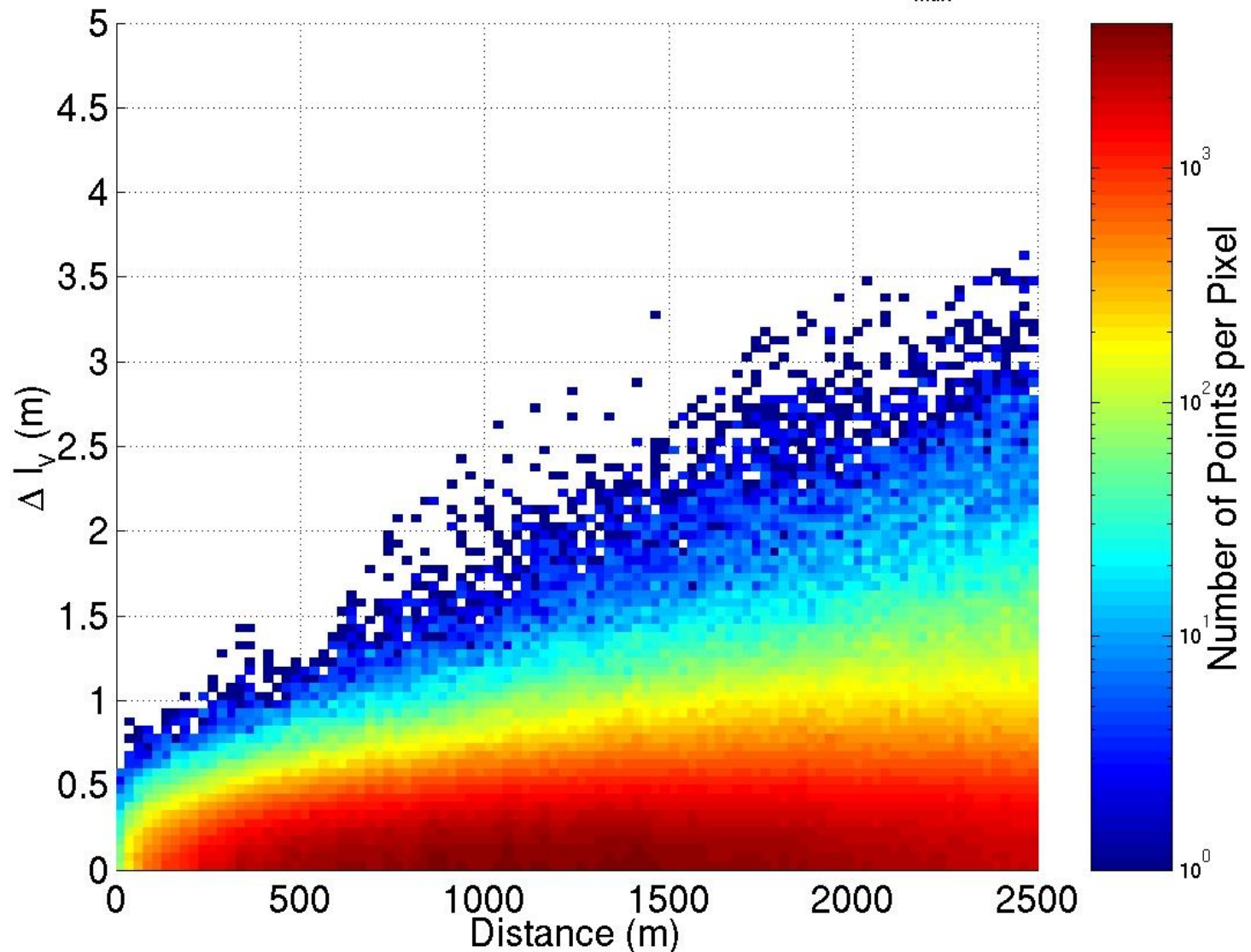
# Preliminary Decorrelation Findings

- ➔ Nominal Ionosphere is Relatively Smooth
  - ➔ *Nearby IPPs Well Correlated*
- ➔ Confidence About a Single Measurement Can Be Described As:
$$\sigma^2 = \sigma_m^2 + (0.3 m + d * 0.5 m / 1000 km)^2$$
- ➔ There Appears to Be a Deterministic Component
- ➔ Next Try Removing a Planar Fit



# Ionospheric Decorrelation About a Planar Fit (1<sup>st</sup> Order)

Vertical Ionosphere Correlation, 1<sup>st</sup> Order (CONUS, 2<sup>nd</sup> July 2000,  $R_{\max} = 1500\text{km}$ )

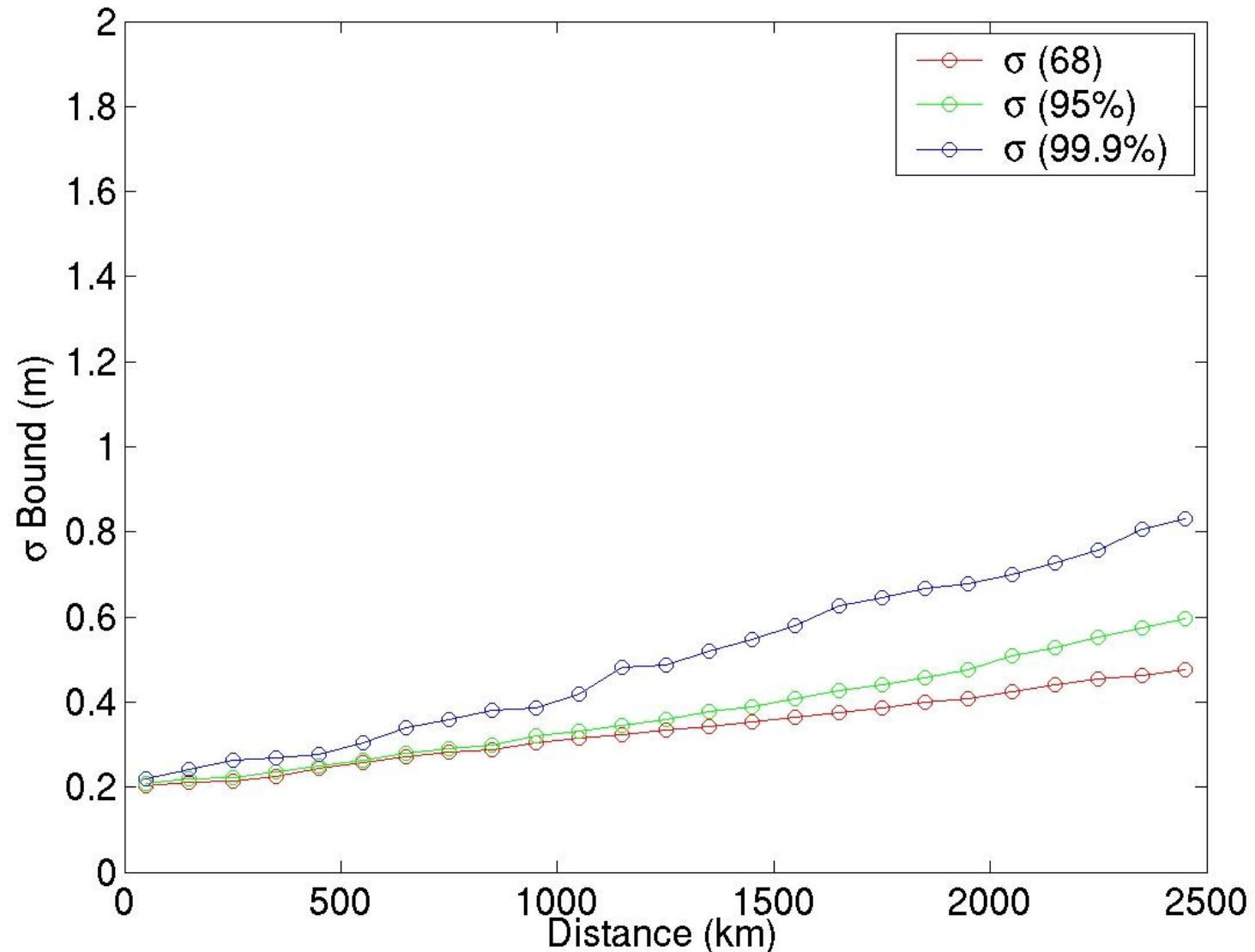


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# Ionospheric Decorrelation Function (1<sup>st</sup> Order)

Vertical Ionosphere Containment  $\sigma$ , 1<sup>st</sup> Order Correlation (CONUS, 2<sup>nd</sup> July 2000)

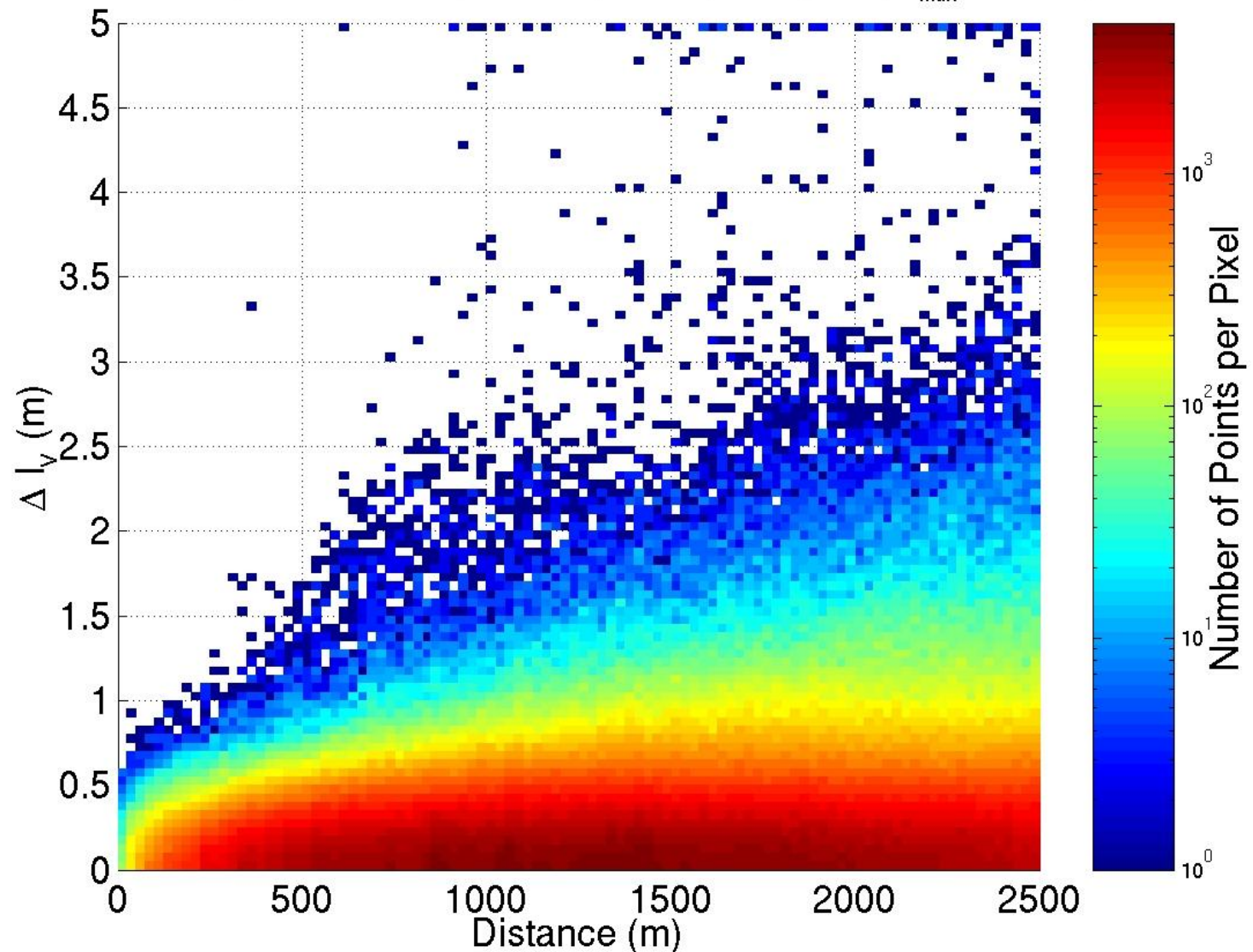






# Ionospheric Decorrelation About a Quadratic Fit

Vertical Ionosphere Correlation, 2<sup>nd</sup> Order (CONUS, 2<sup>nd</sup> July 2000,  $R_{\max} = 1500\text{km}$ )

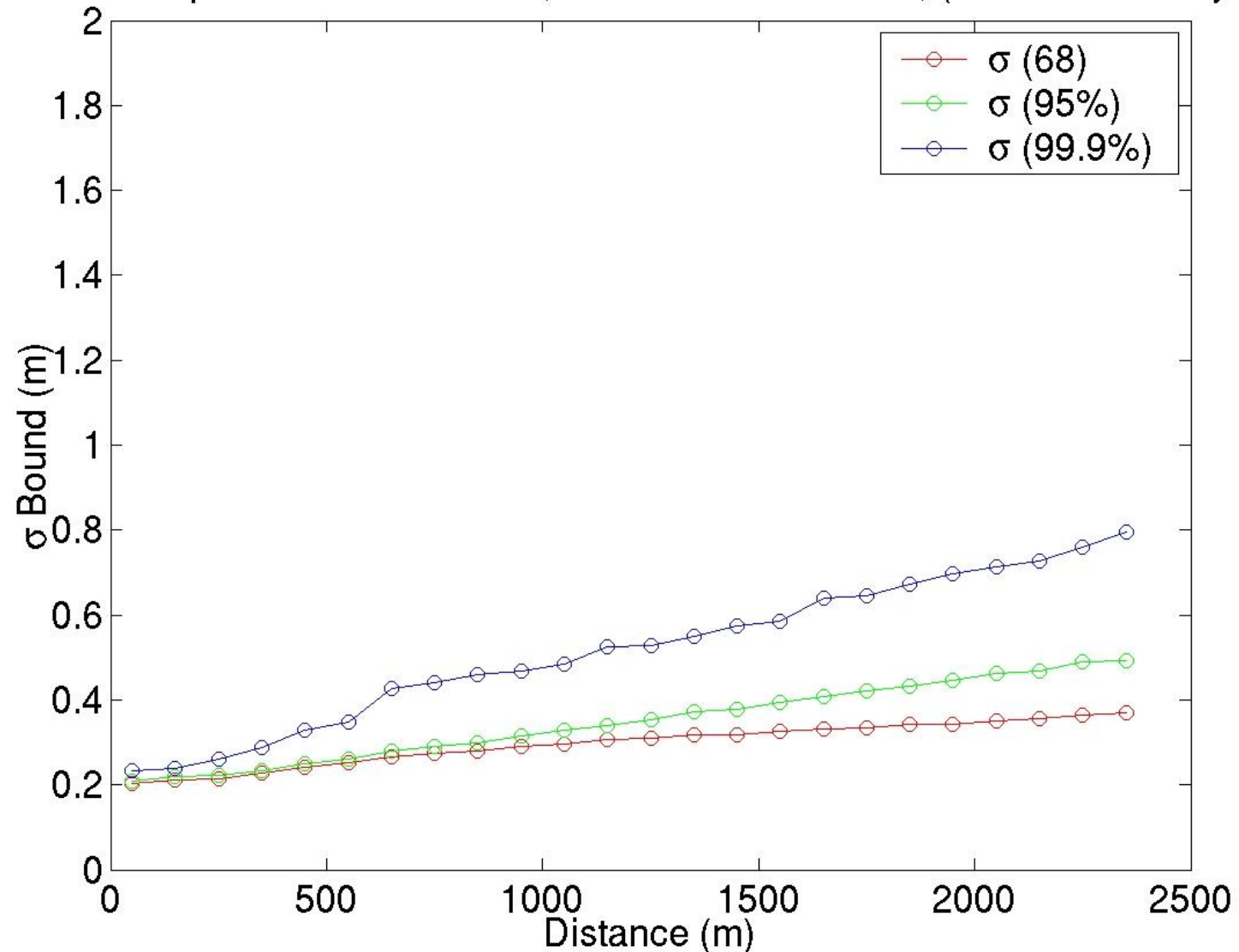


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# Ionospheric Decorrelation Function (2<sup>nd</sup> Order)

Vertical Ionosphere Containment  $\sigma$ , 2<sup>nd</sup> Order Correlation, (CONUS 2<sup>nd</sup> July 2000)



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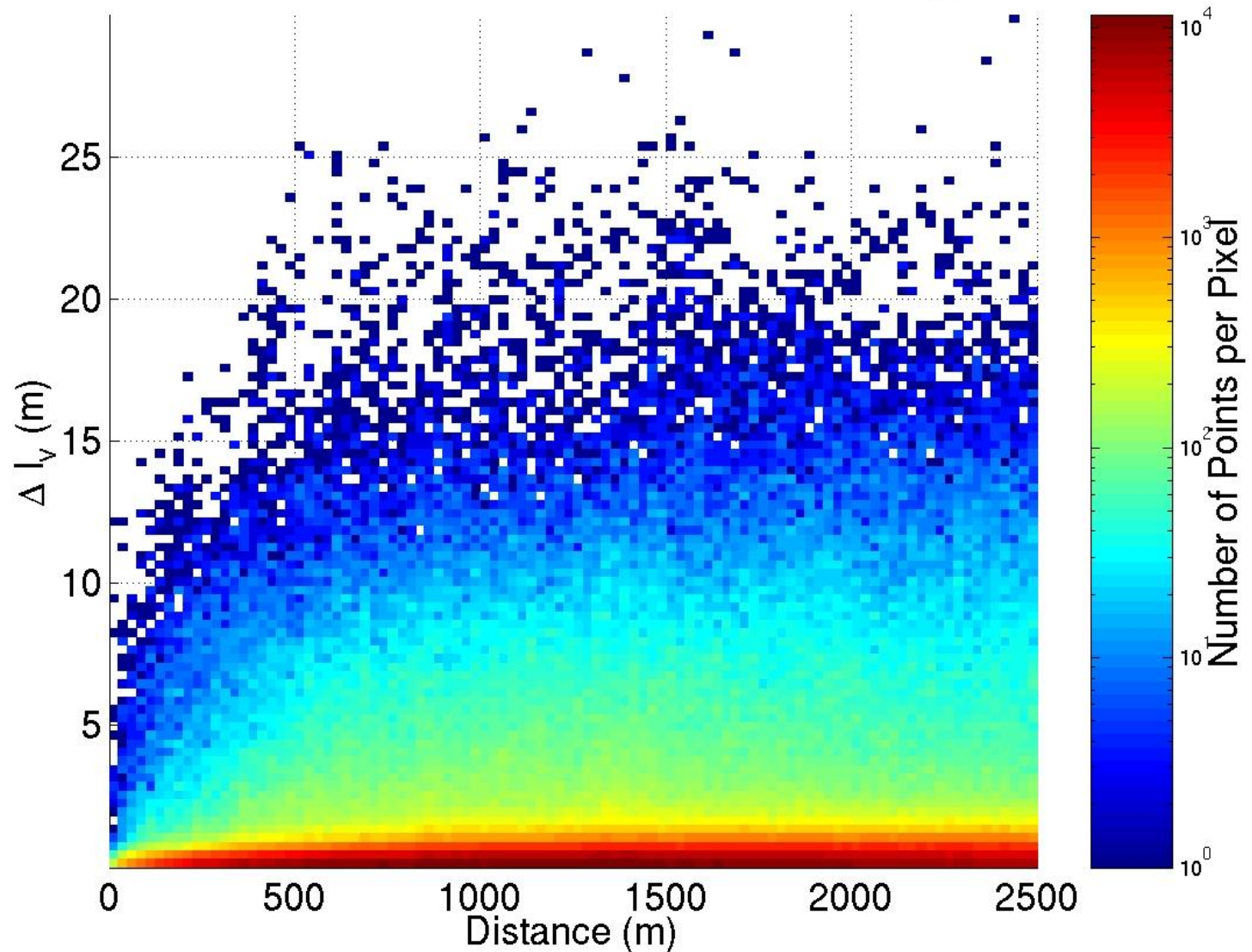
# Initial Decorrelation Summary

- ➔ Planar Fit Appears to Remove Nearly All Deterministic Elements
- ➔ No Decorrelation Variation With Elevation Angle or vs Day/Night
  - ➔ *Decorrelation appears to result from residual error in supertruth data*
- ➔ 35 cm Valid for Mid-Latitude Nominal Decorrelation ( $R < \sim 1000$  km)
- ➔ Decorrelation at Lower Latitudes Is Likely Different (larger, more orders?)



# Disturbed Ionosphere

Vertical Ionosphere Correlation, 1<sup>st</sup> Order (CONUS, 15<sup>th</sup> July 2000,  $R_{\max} = 1500\text{km}$ )

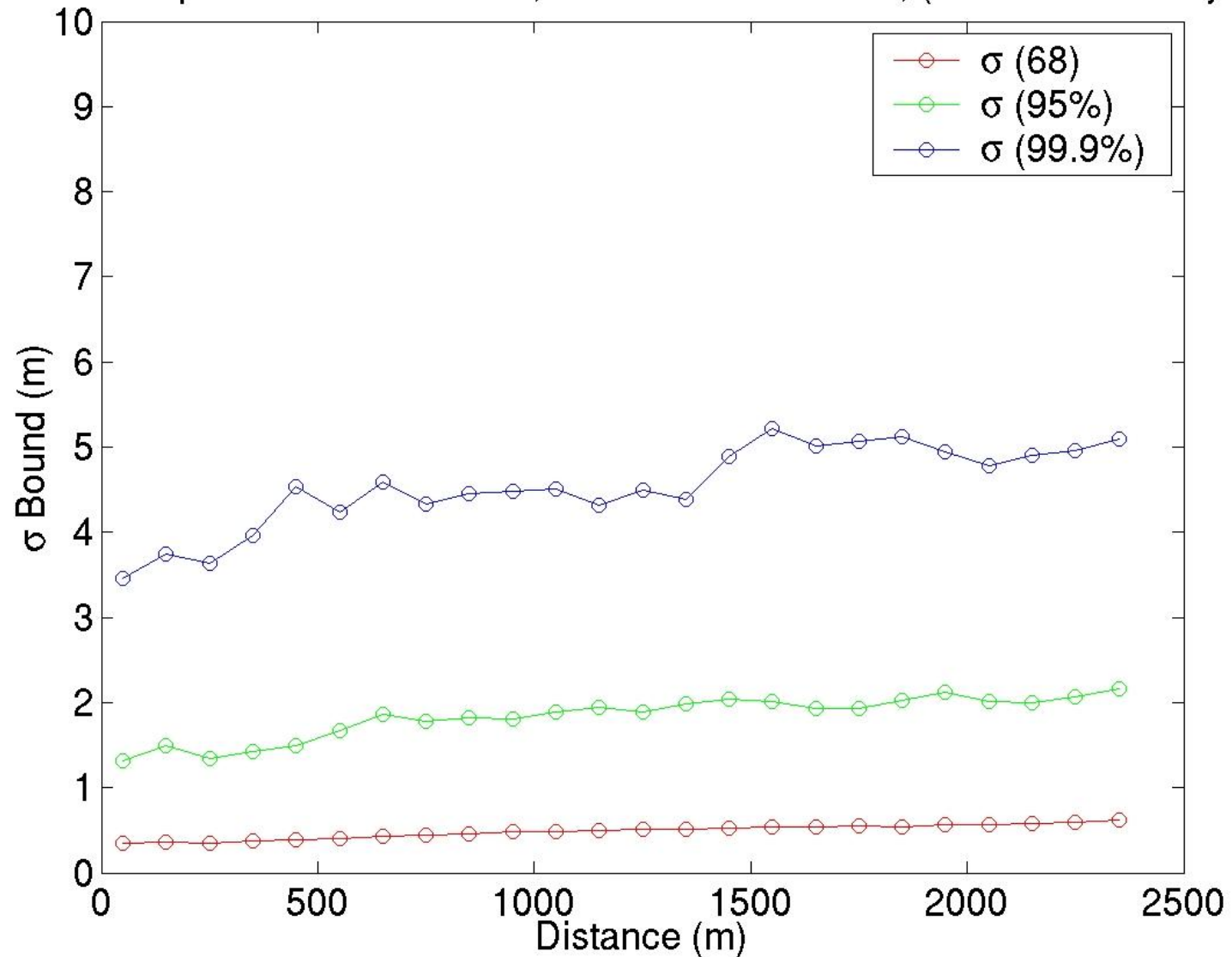


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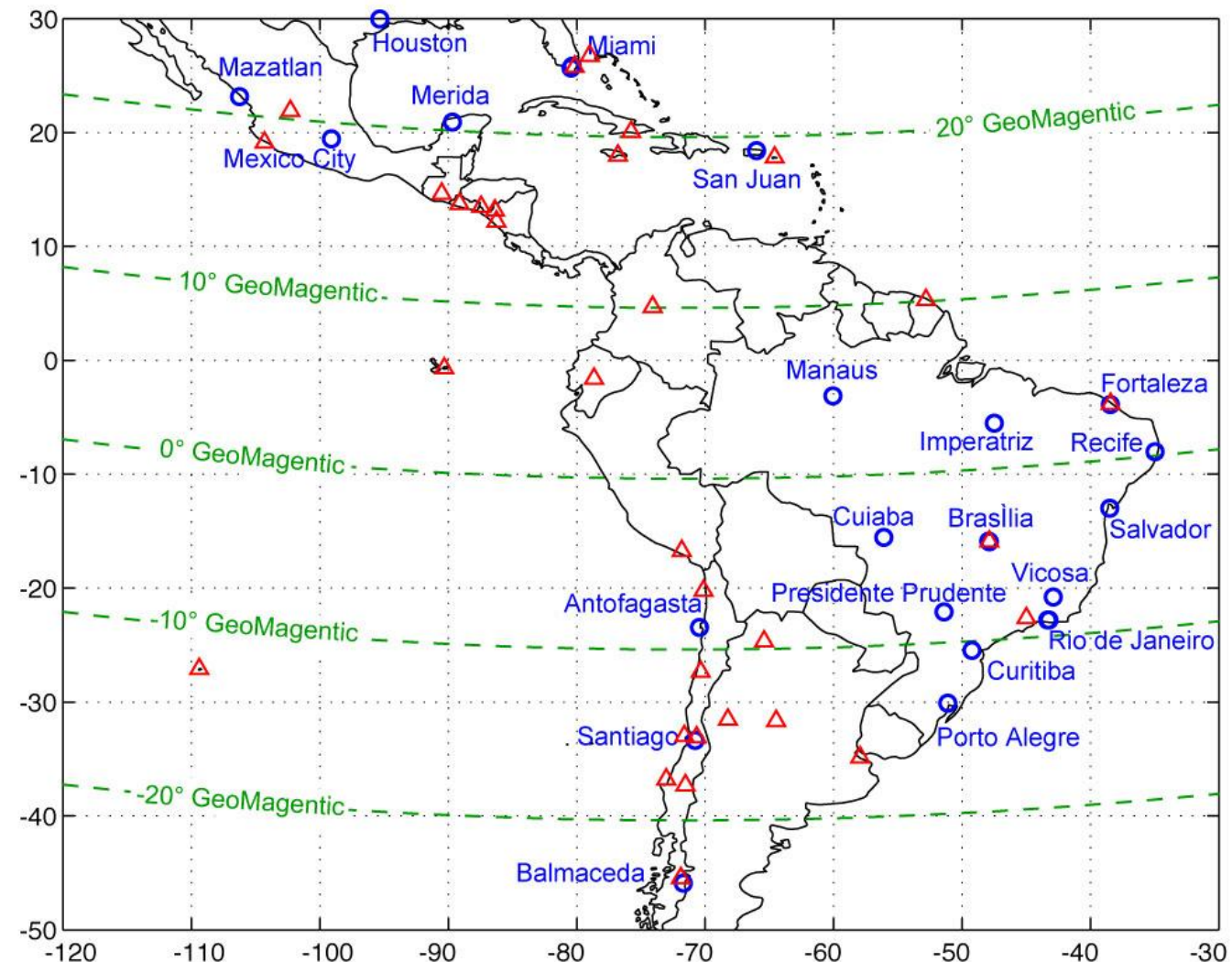
# Disturbed Ionosphere

Vertical Ionosphere Containment  $\sigma$ , 1<sup>st</sup> Order Correlation, (CONUS 15<sup>th</sup> July 2000)





# Map of South American Stations



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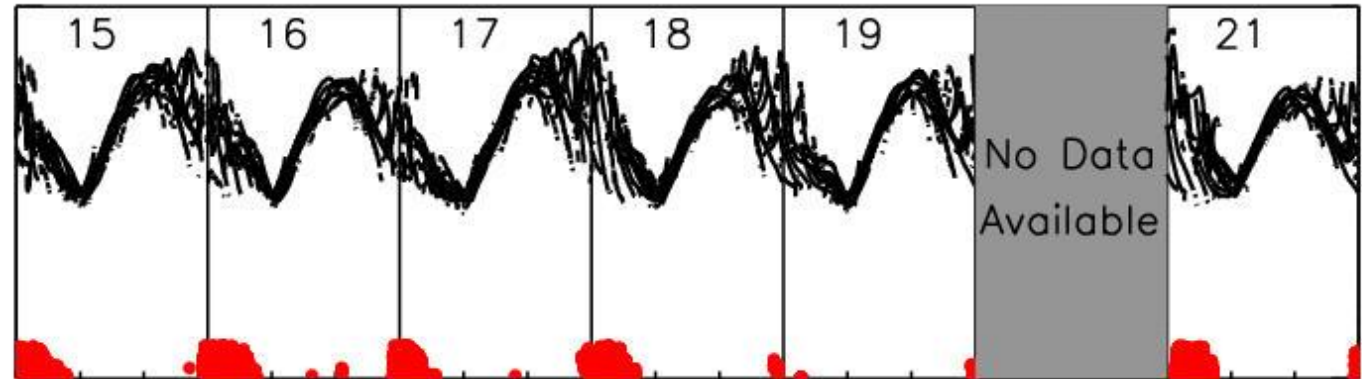
# Determination of Quiet Days

- ➔ First wish to identify “undisturbed” days to use as basis for “nominal” model
  - ➔ *Want a day free of depletions and scintillation*

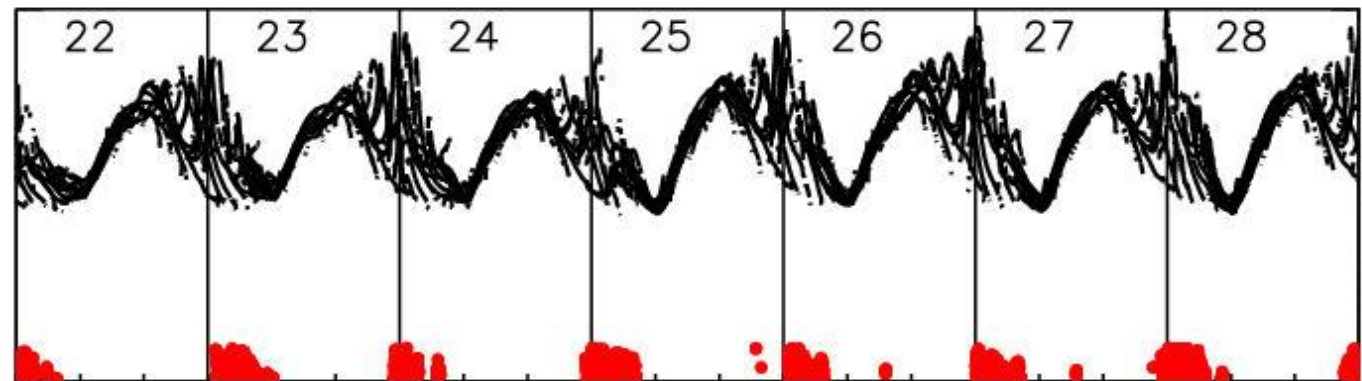


# Daily Observations of TEC and S4

S4, Range Delay (m)



S4, Range Delay (m)



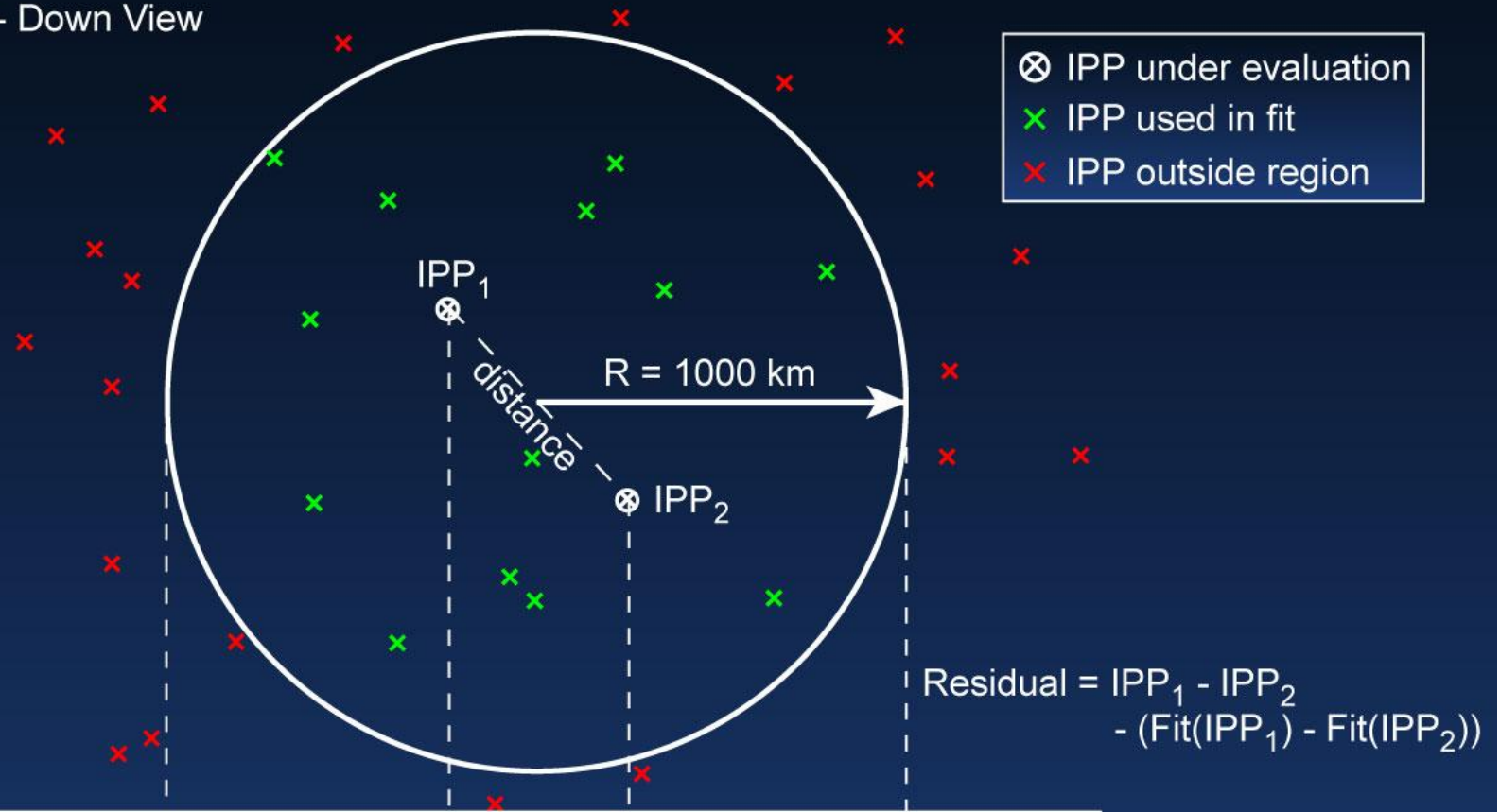
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# Correlation Estimation Process

Top - Down View



Side View

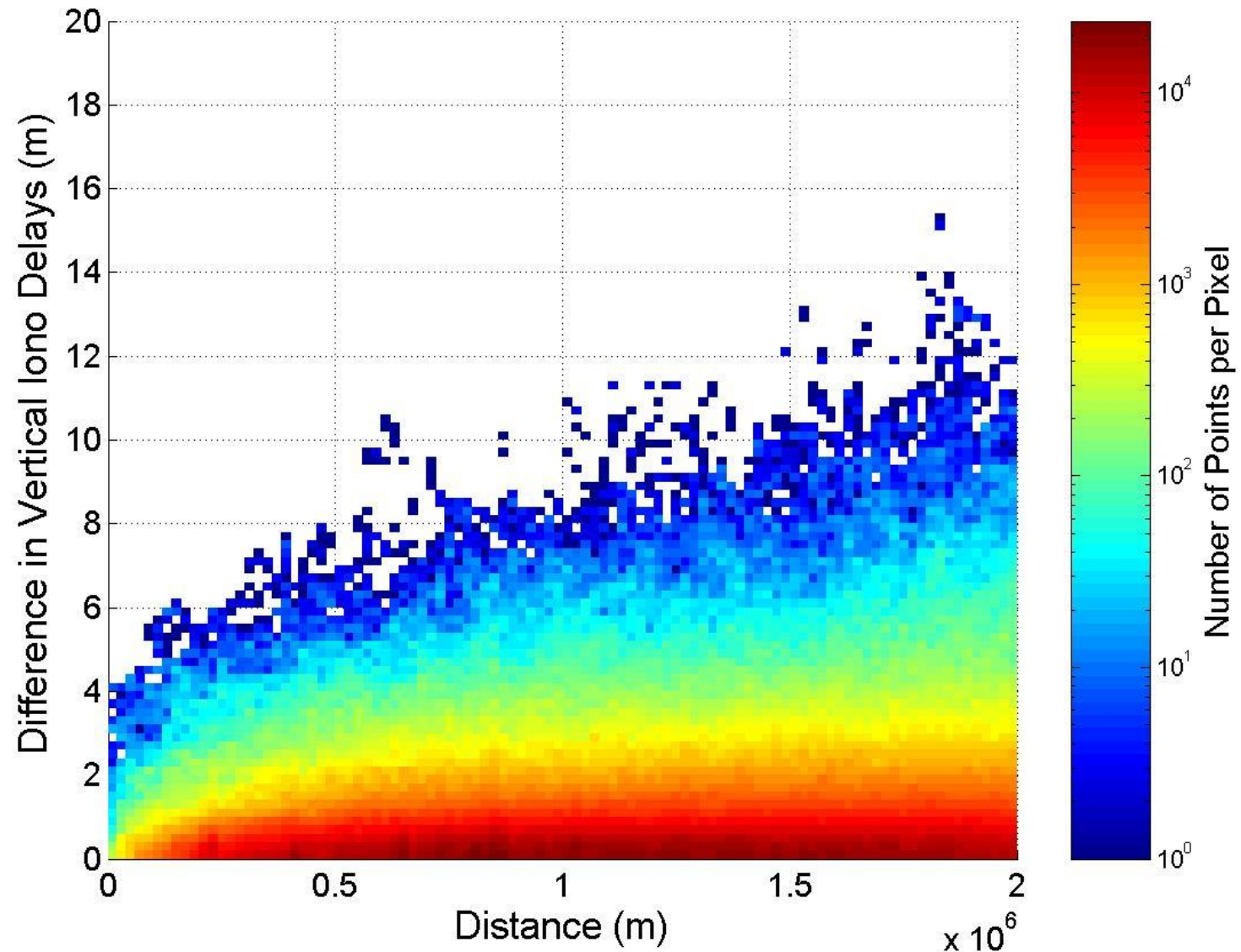


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# Two-D Histogram 1<sup>st</sup> Order

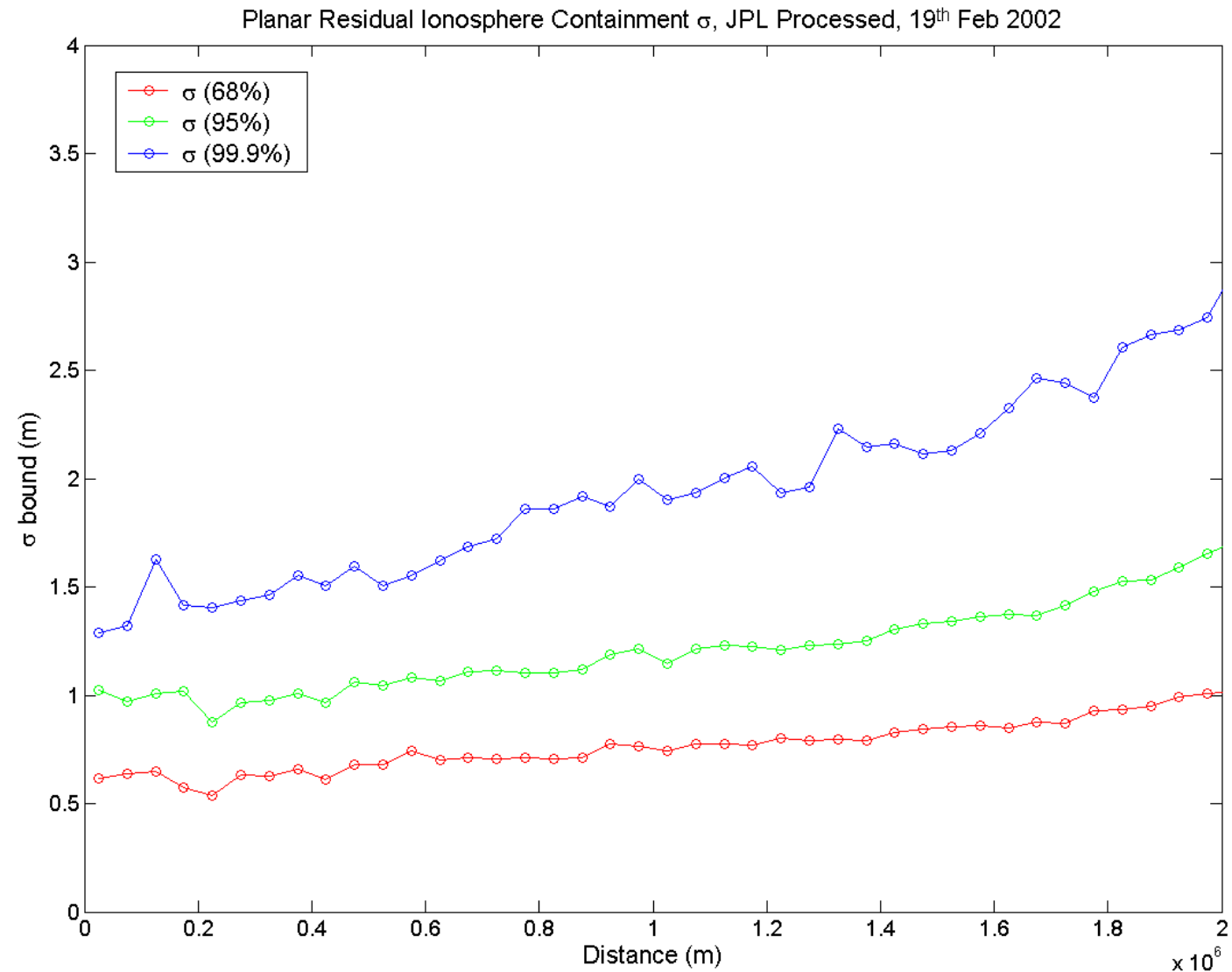
Residues of Planar Fit,  $R_{\max} = 1000$  km, JPL Processed, 19<sup>th</sup> Feb 2002



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# Sigma Estimate 1<sup>st</sup> Order

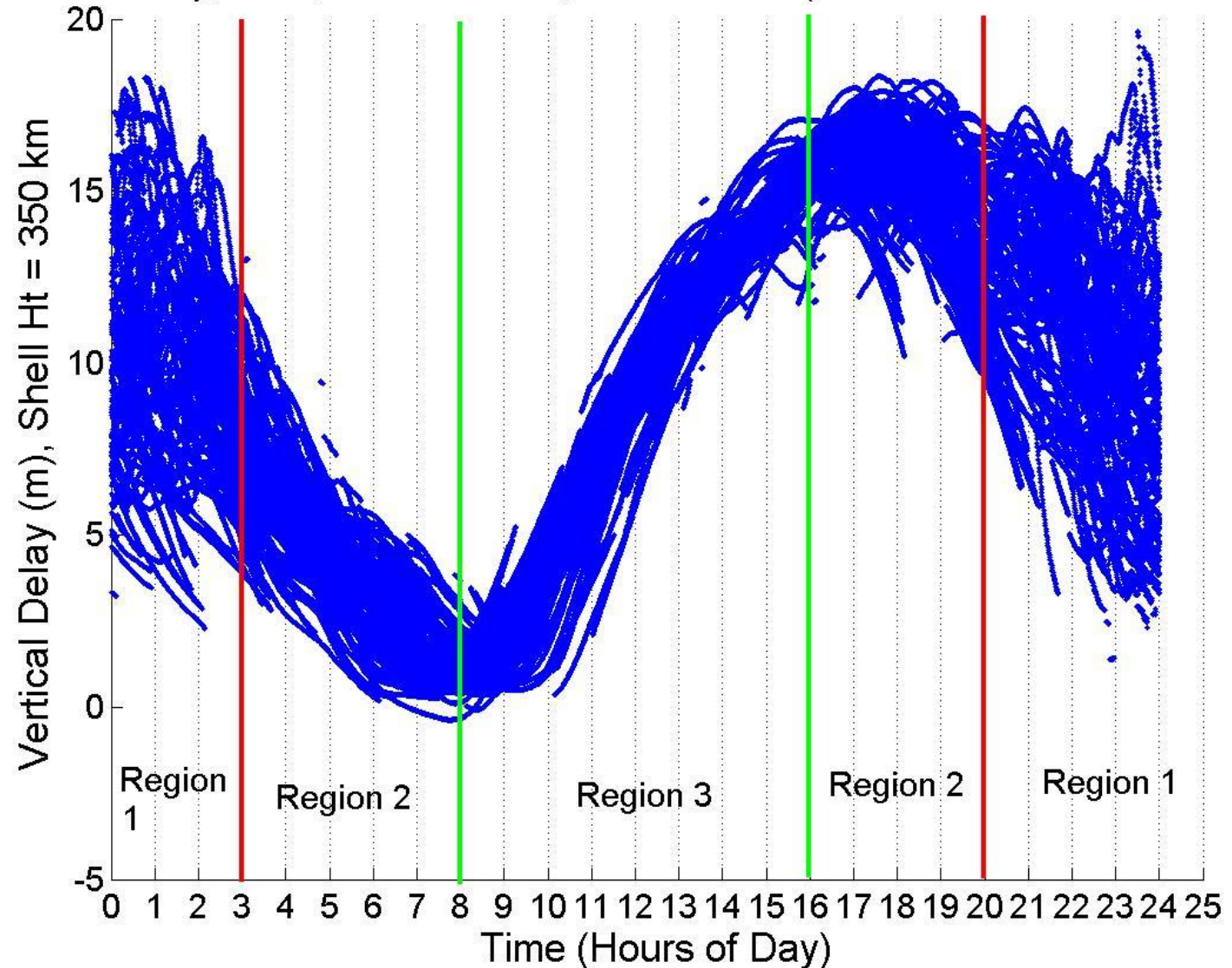


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# Vertical TEC

Vertical Delay, Brazil, JPL Processed, 19<sup>th</sup> Feb 2002 (UTC Start time = 698112000sec)

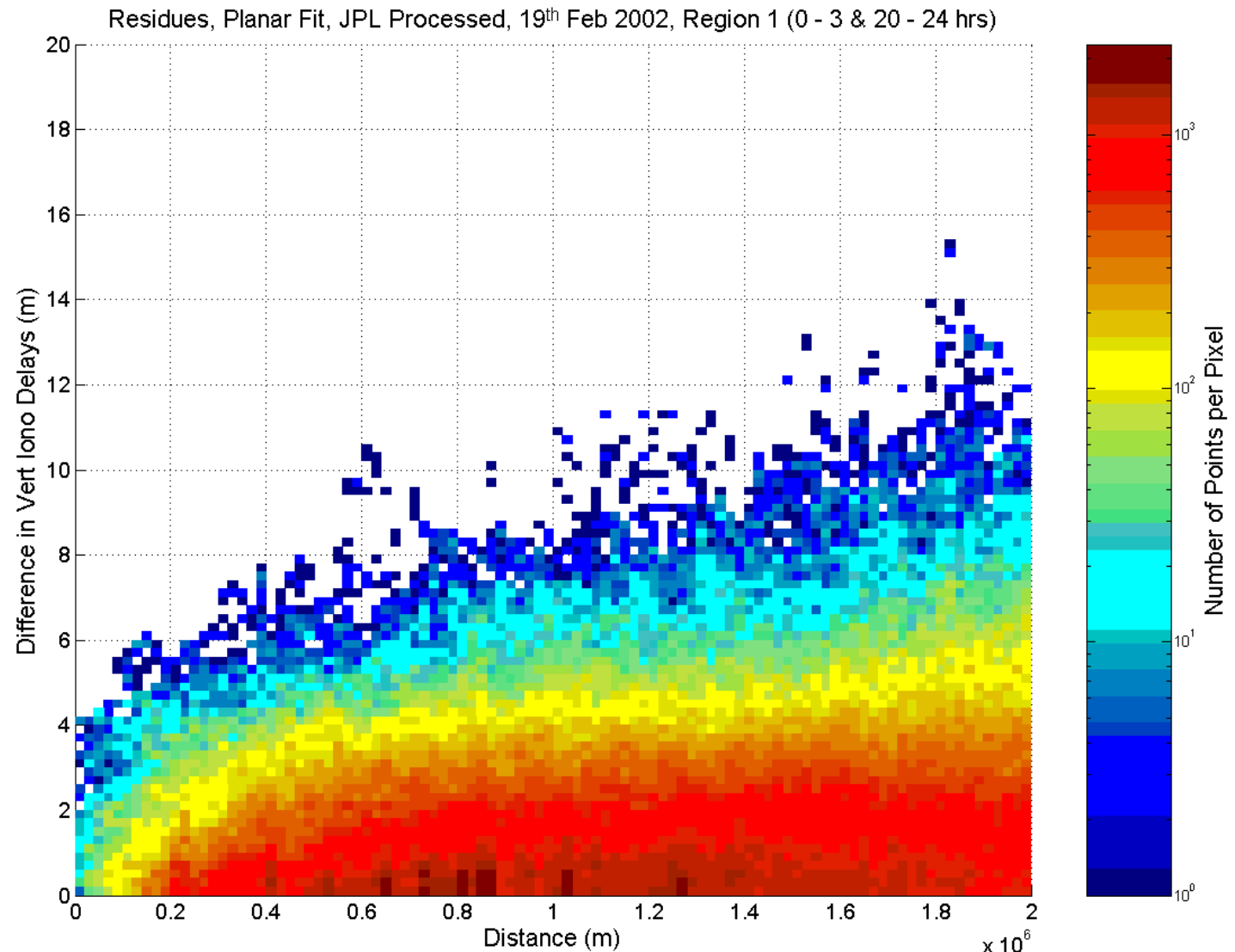


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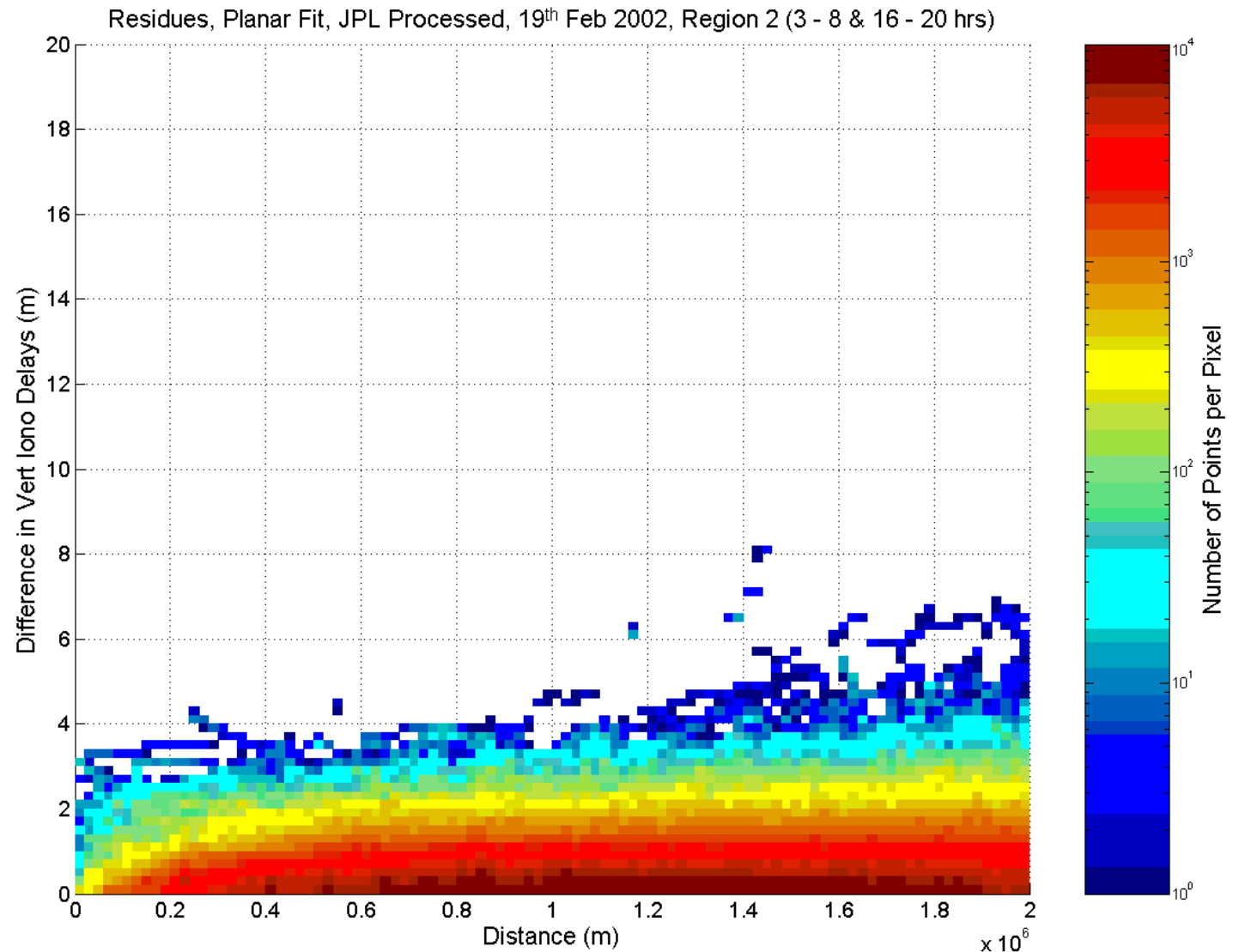
# Two-D Histogram 1<sup>st</sup> Order (Region 1)



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# Two-D Histogram 1<sup>st</sup> Order (Region 2)

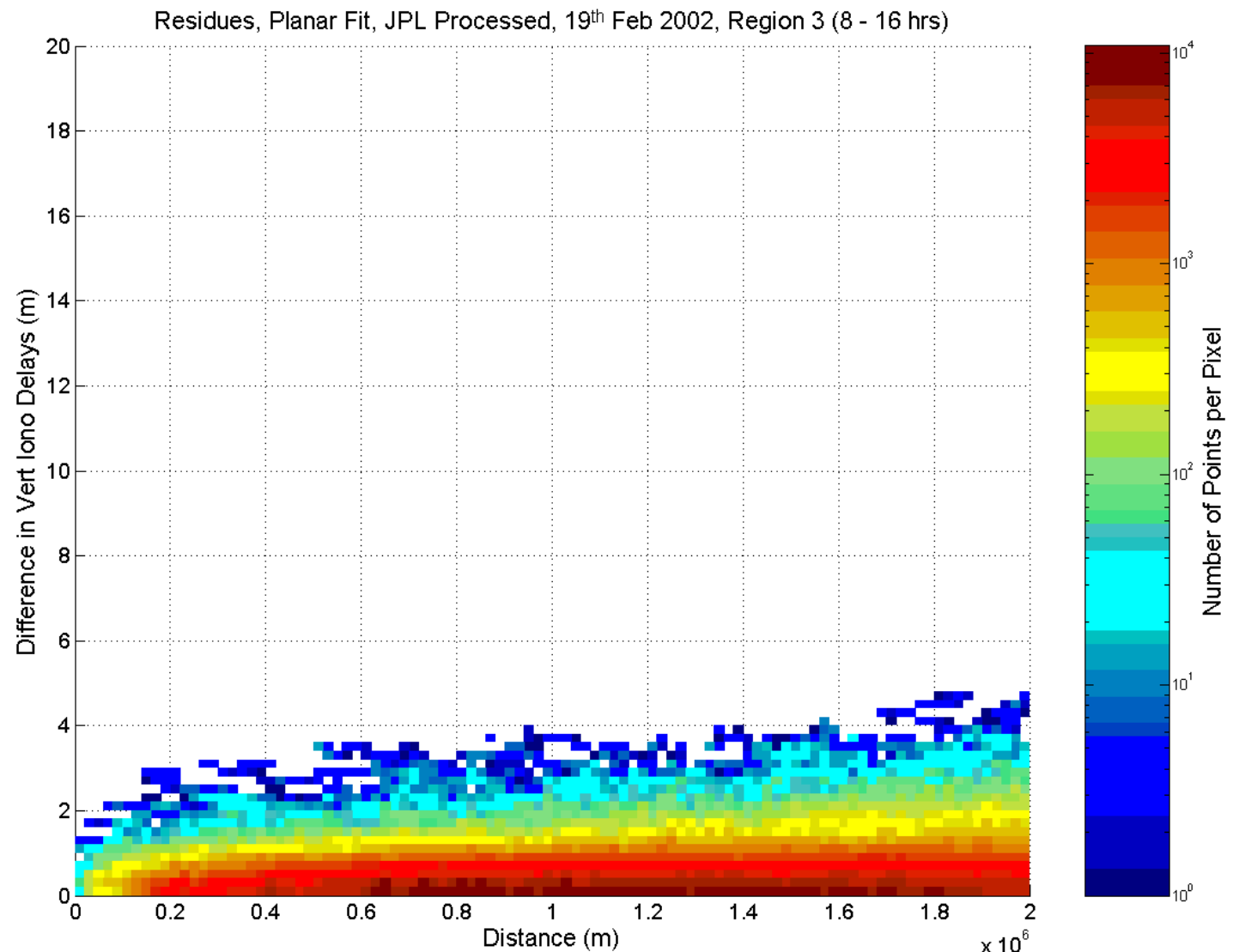


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# Two-D Histogram 1<sup>st</sup> Order (Region 3)

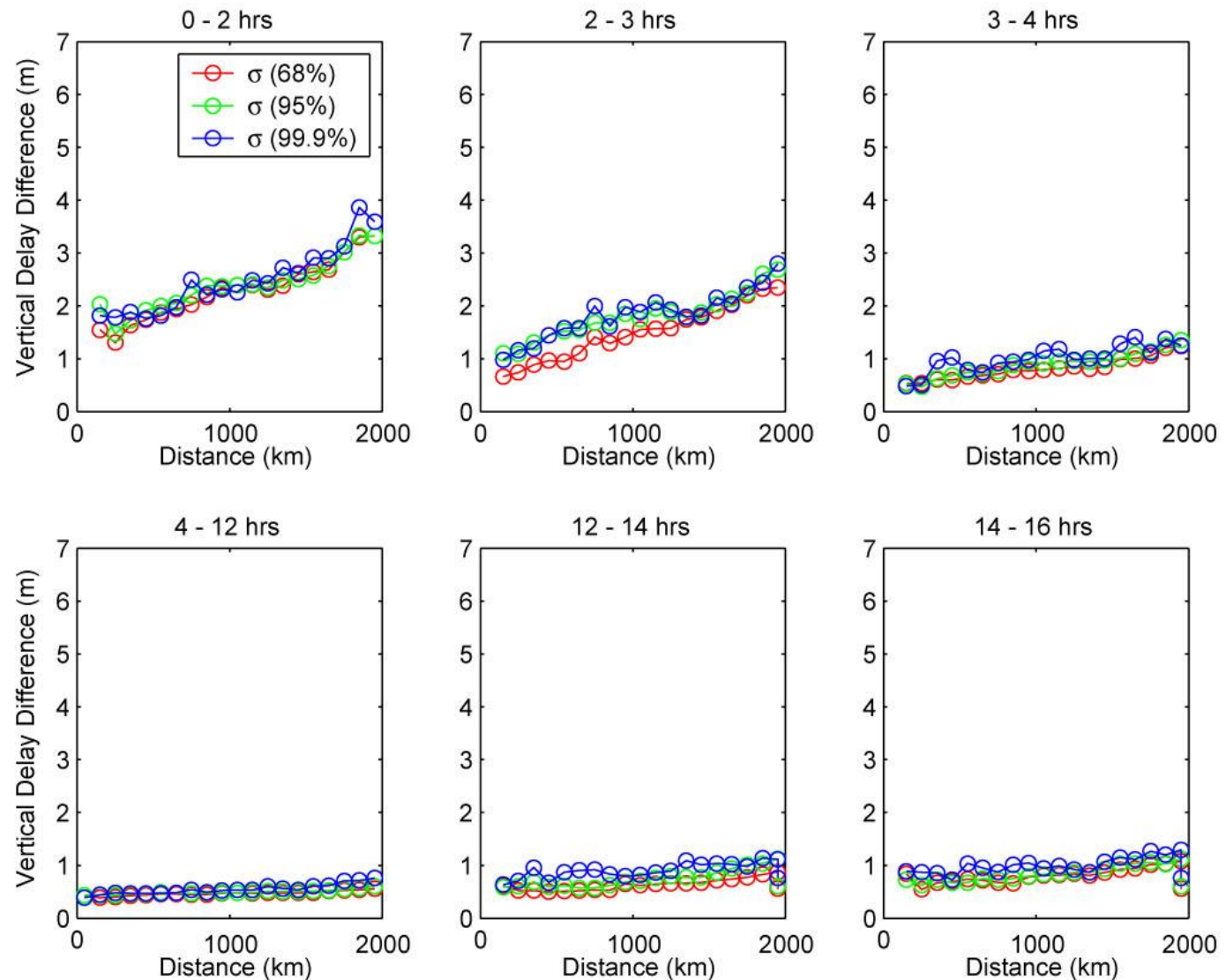


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# Sigma Estimate 1<sup>st</sup> Order (Sliced by Time)

Planar Fit 19<sup>th</sup> Feb 2002

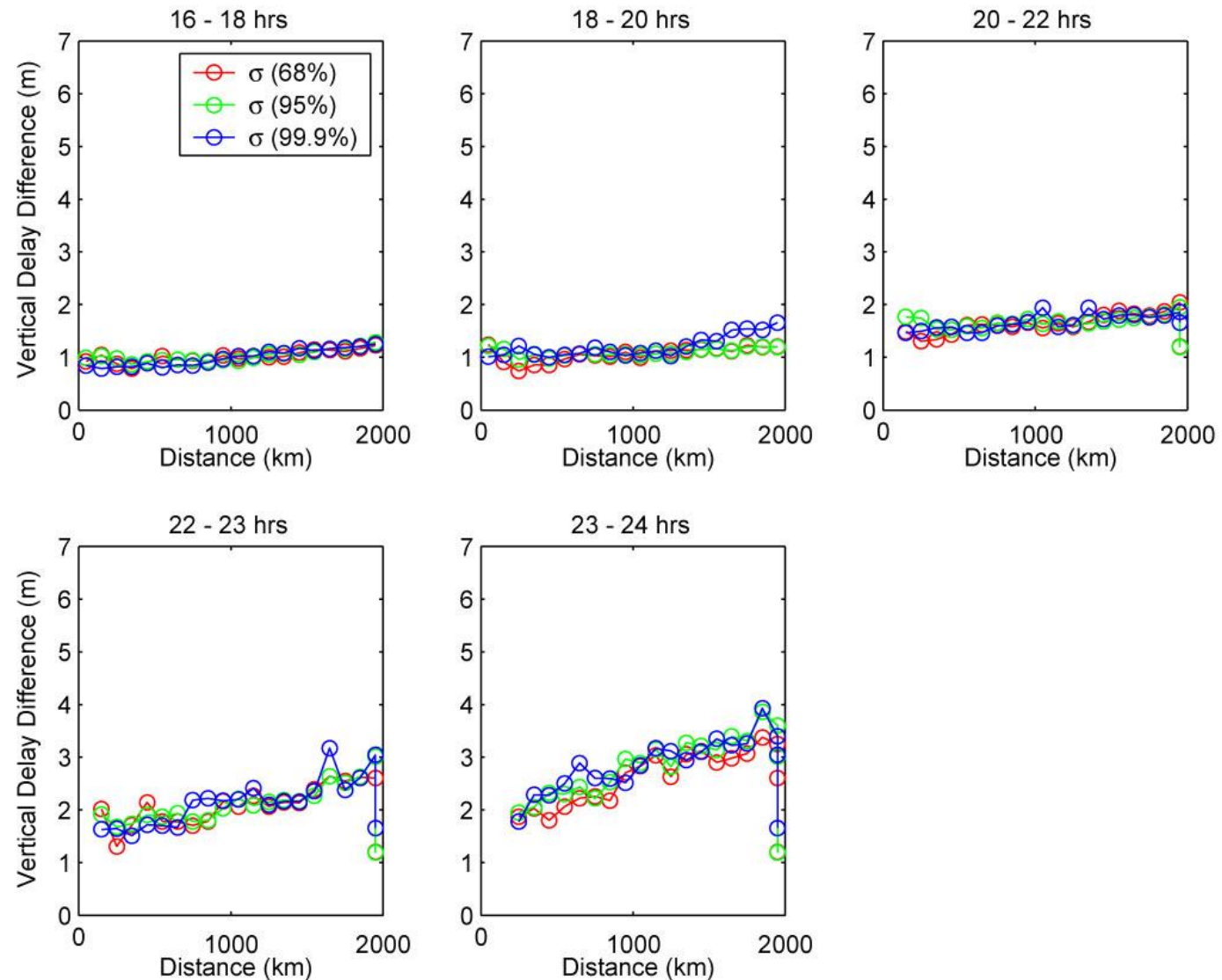


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# Sigma Estimate 1<sup>st</sup> Order (Sliced by Time)

Planar Fit 19<sup>th</sup> Feb 2002



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# Correlation Observations

- ➔ Clear temporal dependencies in the variogram ( $\sigma_{\text{decorr}}$  term)
  - ➔ *Evening into nighttime is worst*
  - ➔ *Daytime more easily modeled*
- ➔ Clear spatial trends in the data
  - ➔ *1<sup>st</sup> and 2<sup>nd</sup> order model the trend about equally well, both better than 0<sup>th</sup> order*
- ➔ Random Component significantly larger than mid-latitude
  - ➔ *Gaussian over short times*

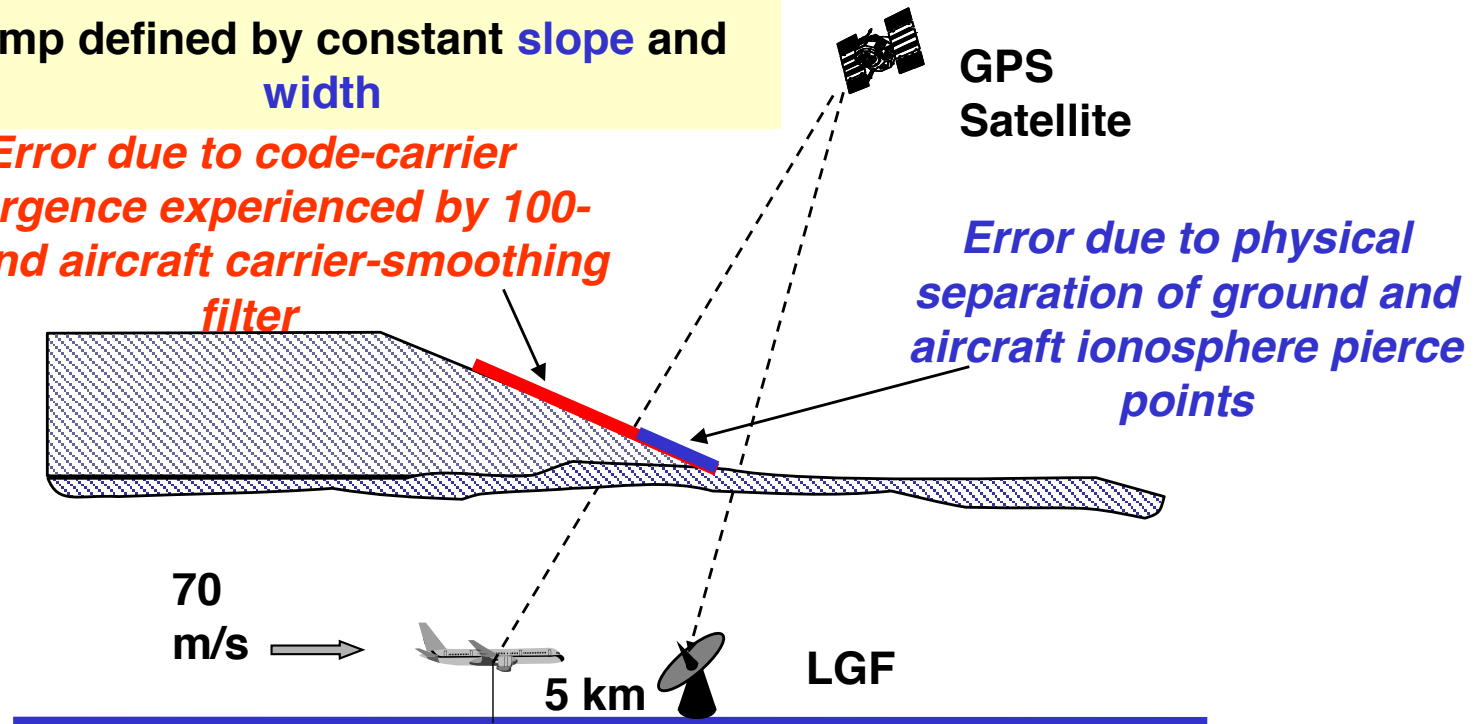


# Contributors to Differential Ionosphere Error

## Simplified Ionosphere Wave Front Model:

a ramp defined by constant **slope** and **width**

*Error due to code-carrier divergence experienced by 100-second aircraft carrier-smoothing filter*



$$\text{Diff. Iono Range Error} = \text{gradient slope} \cdot \min\{ (x + 2 \tau v_{air}), \text{gradient width} \}$$

For 5 km ground-to-air separation at CAT I DH:  $x = 5 \text{ km}$ ;  $\tau = 100 \text{ sec}$ ;  $v_{air} = 70 \text{ m/s}$

$$\Rightarrow \text{"virtual baseline" at DH} = x + 2 \tau v_{air} = 5 + 14 = 19 \text{ km}$$

Courtesy:  
Sam Pullen

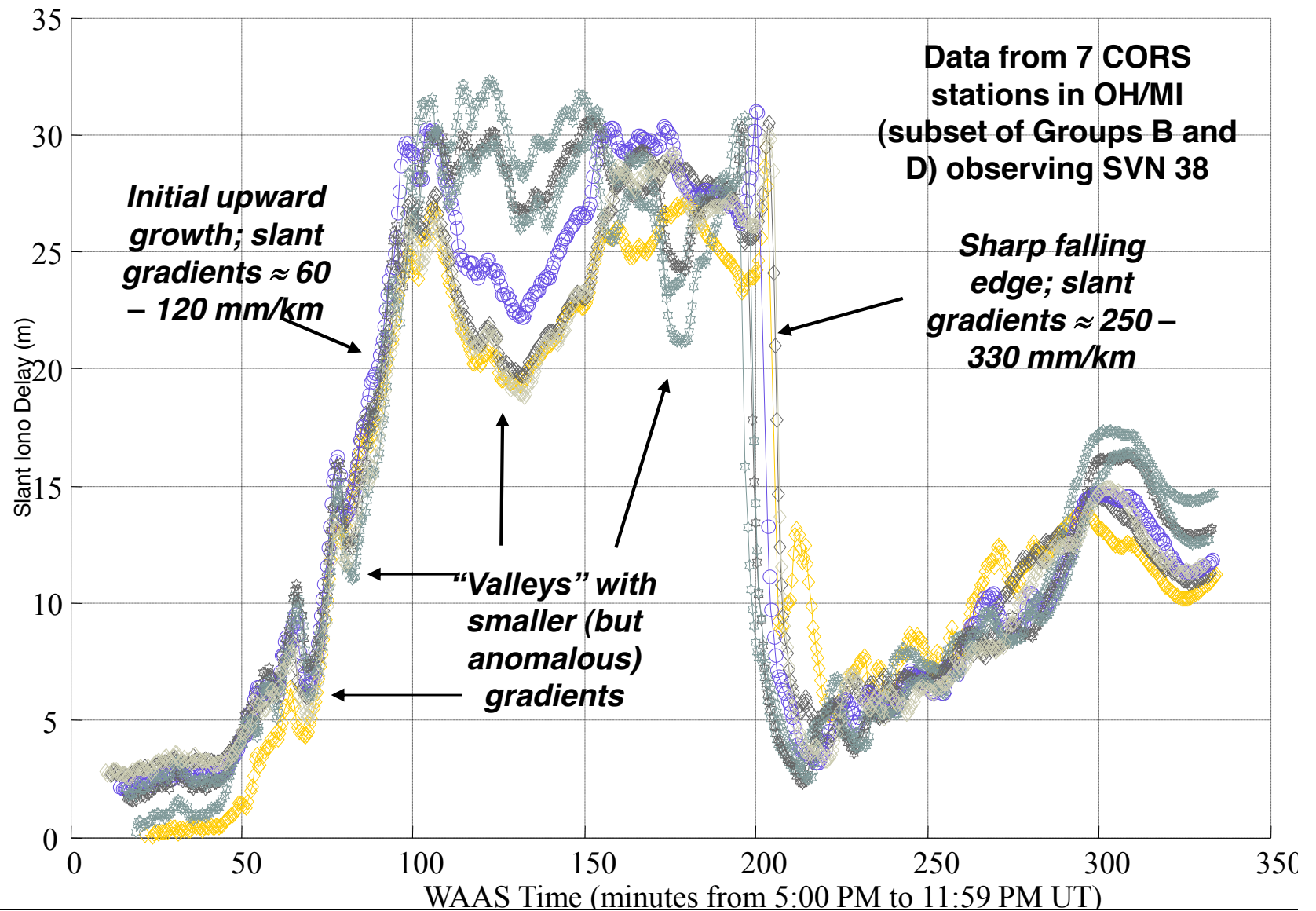
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# Ionosphere Delay Gradients

## 20 Nov. 2003



Courtesy:  
Sam Pullen

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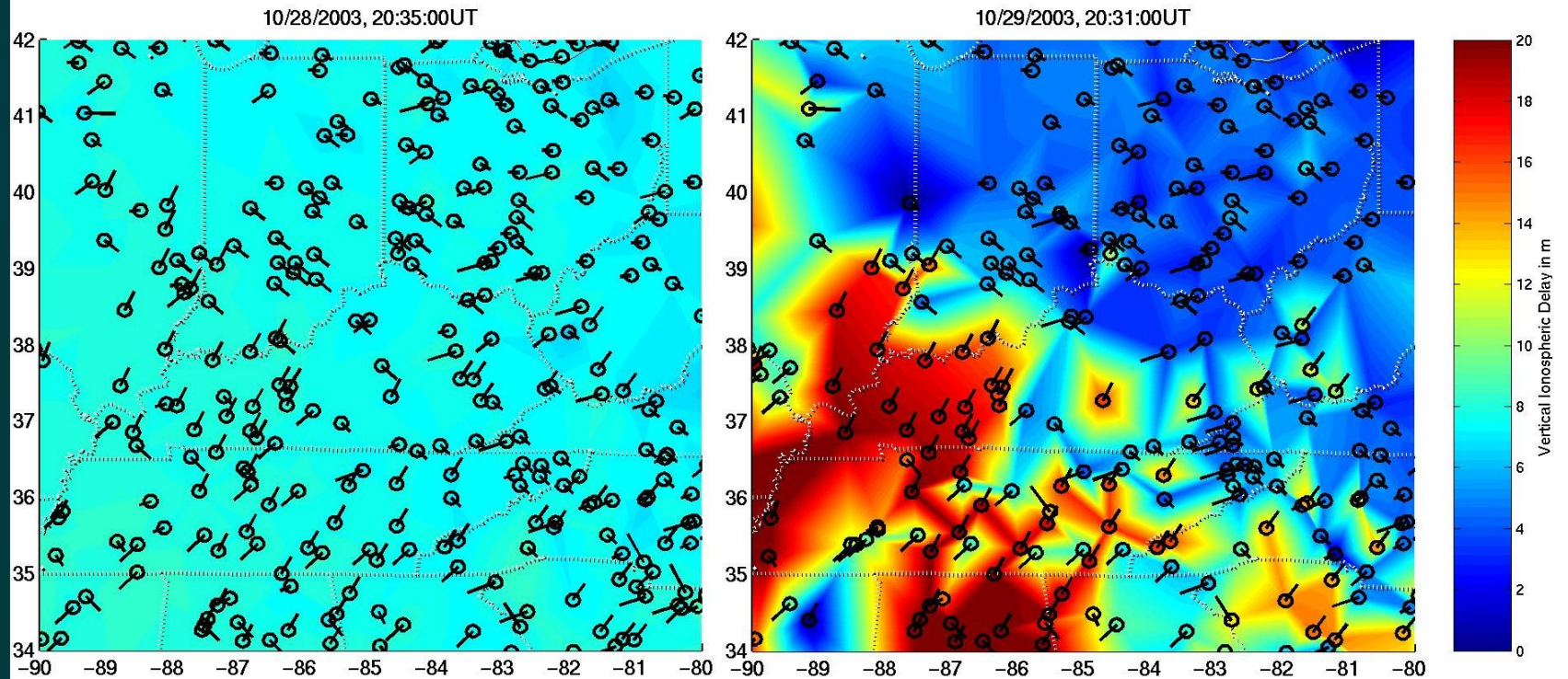


# SBAS Ionospheric Threats

- ➔ WAAS Was Commissioned on 10 July 2003
  - ➔ *Availability > 99% for first 3 months*
- ➔ October 29-31 Two Large Disturbances Each Cause the Storm Detectors to Trip for Hours
  - ➔ *Protection factor set to ~15 m 1-sigma*
- ➔ November 20-21 Another Large Disturbance Limits Vertical Guidance for Several Hours



# Failure of Thin Shell Model



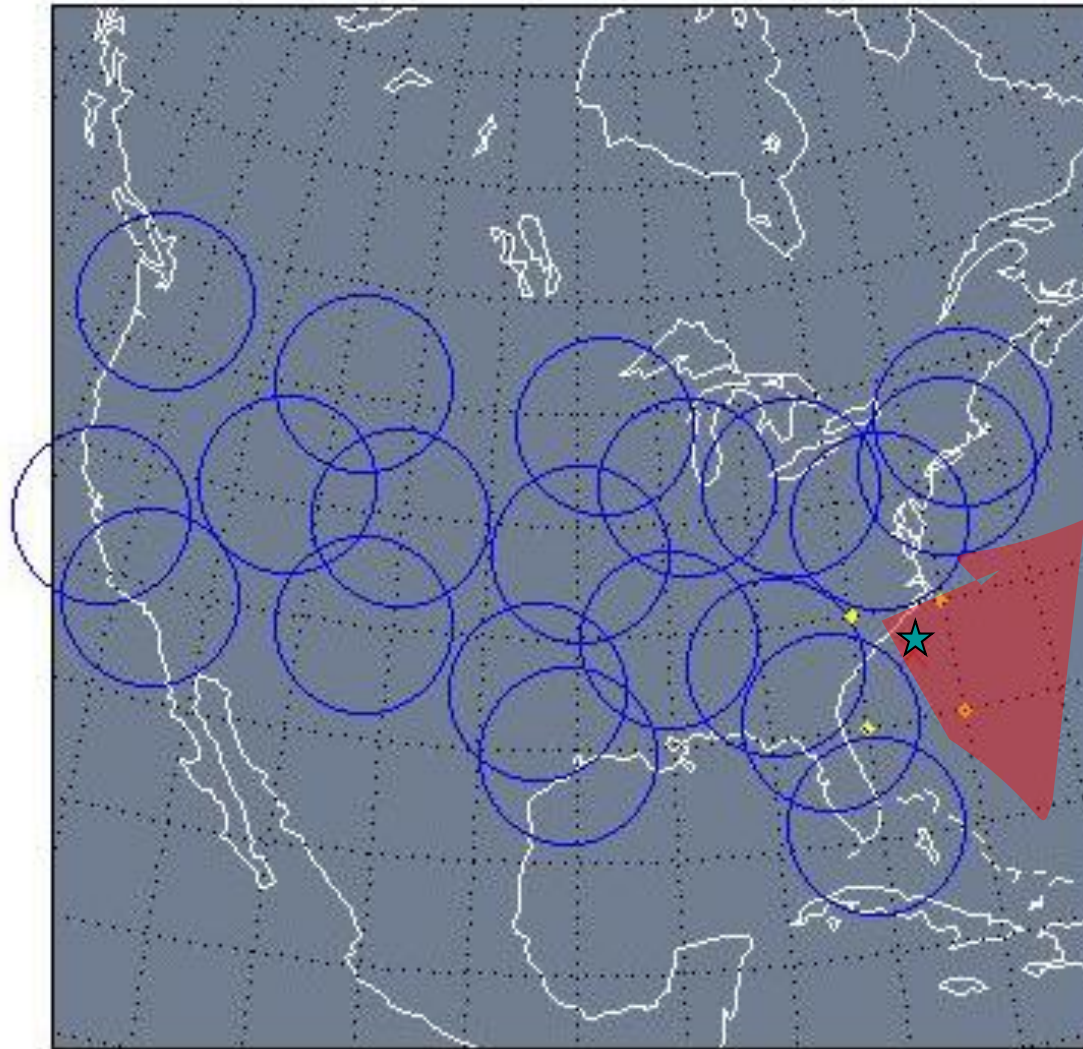
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Quiet Day

Disturbed Day



# Threats at the Edge of Coverage

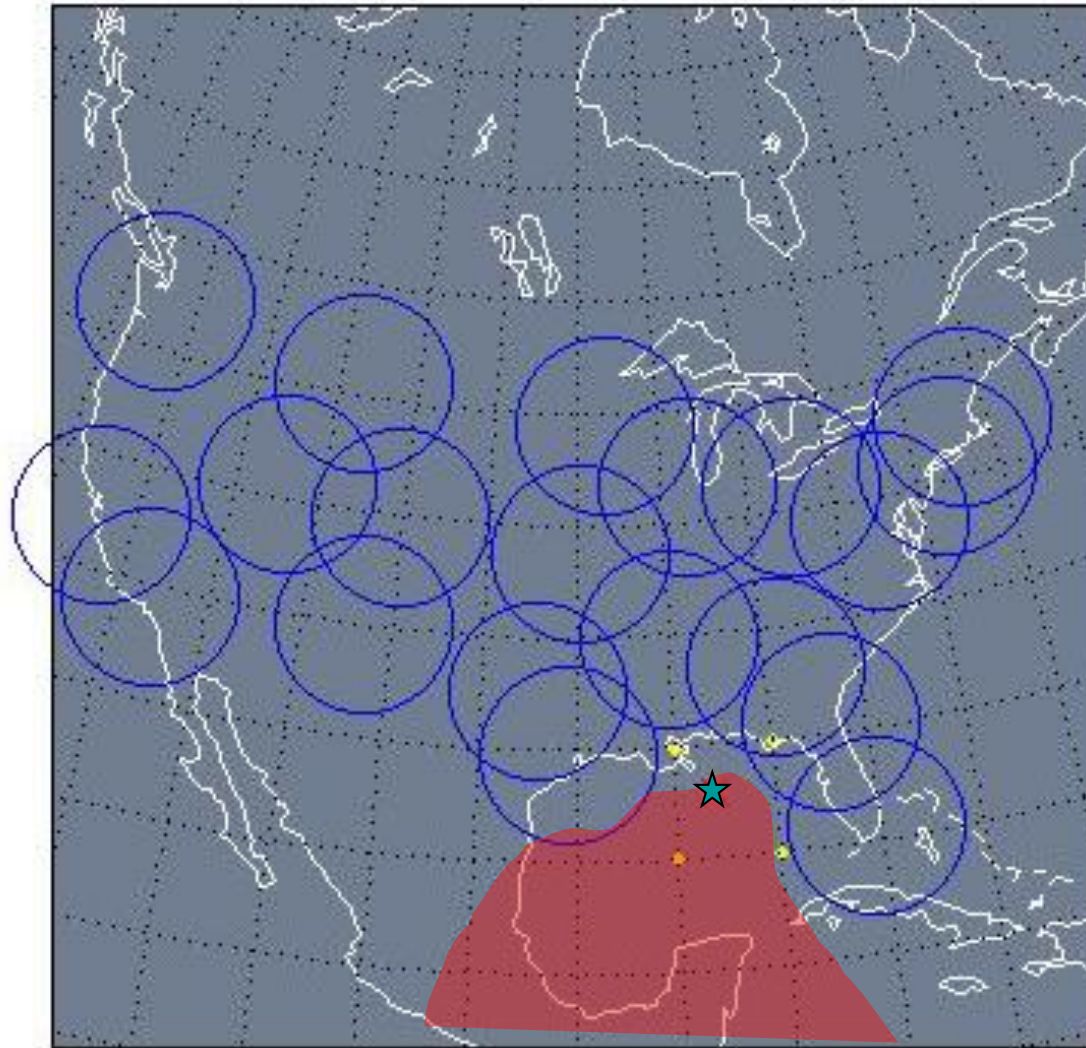


Courtesy:  
Seebany  
Datta-Barua





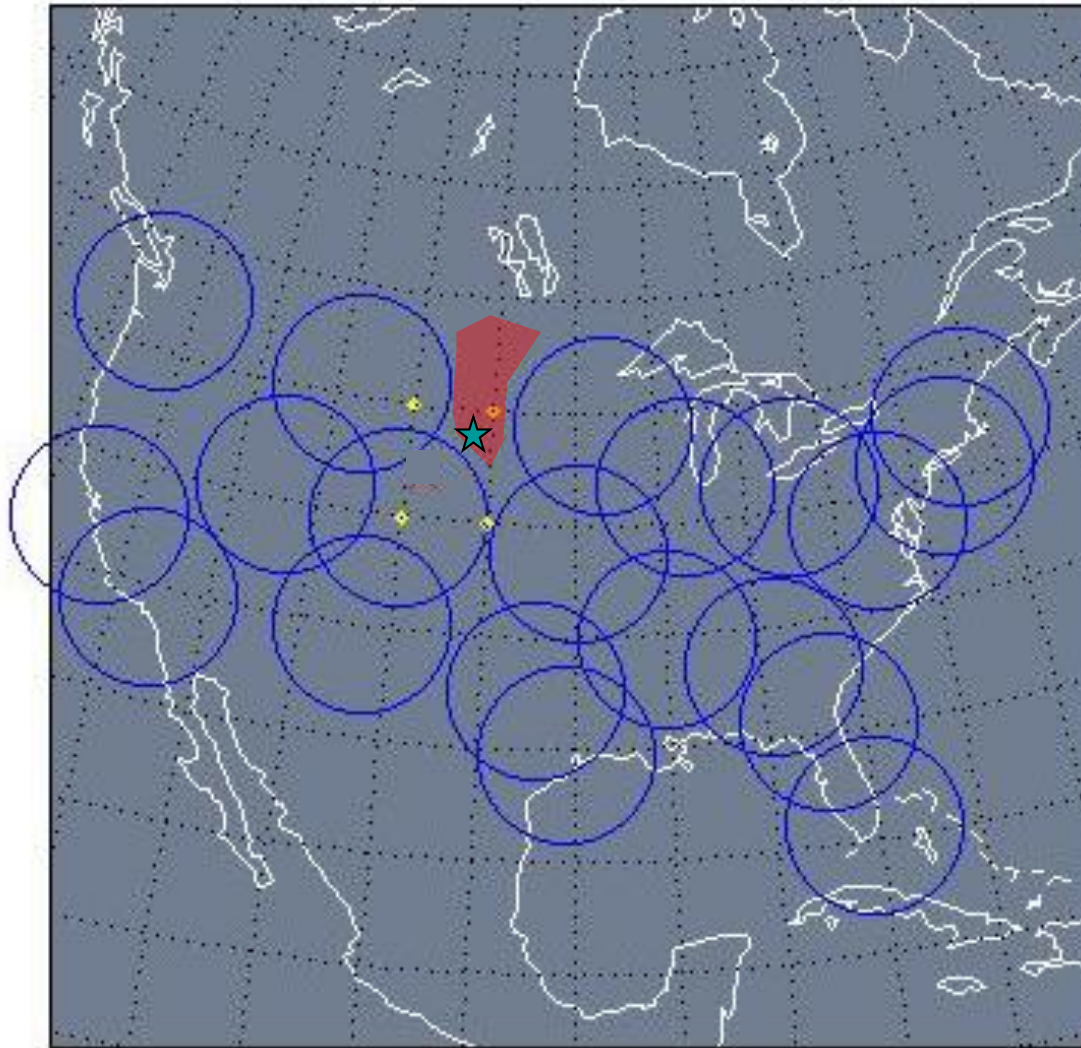
# Edge of Coverage 2



Courtesy:  
Seebany  
Datta-Barua



# Undersampling Within CONUS

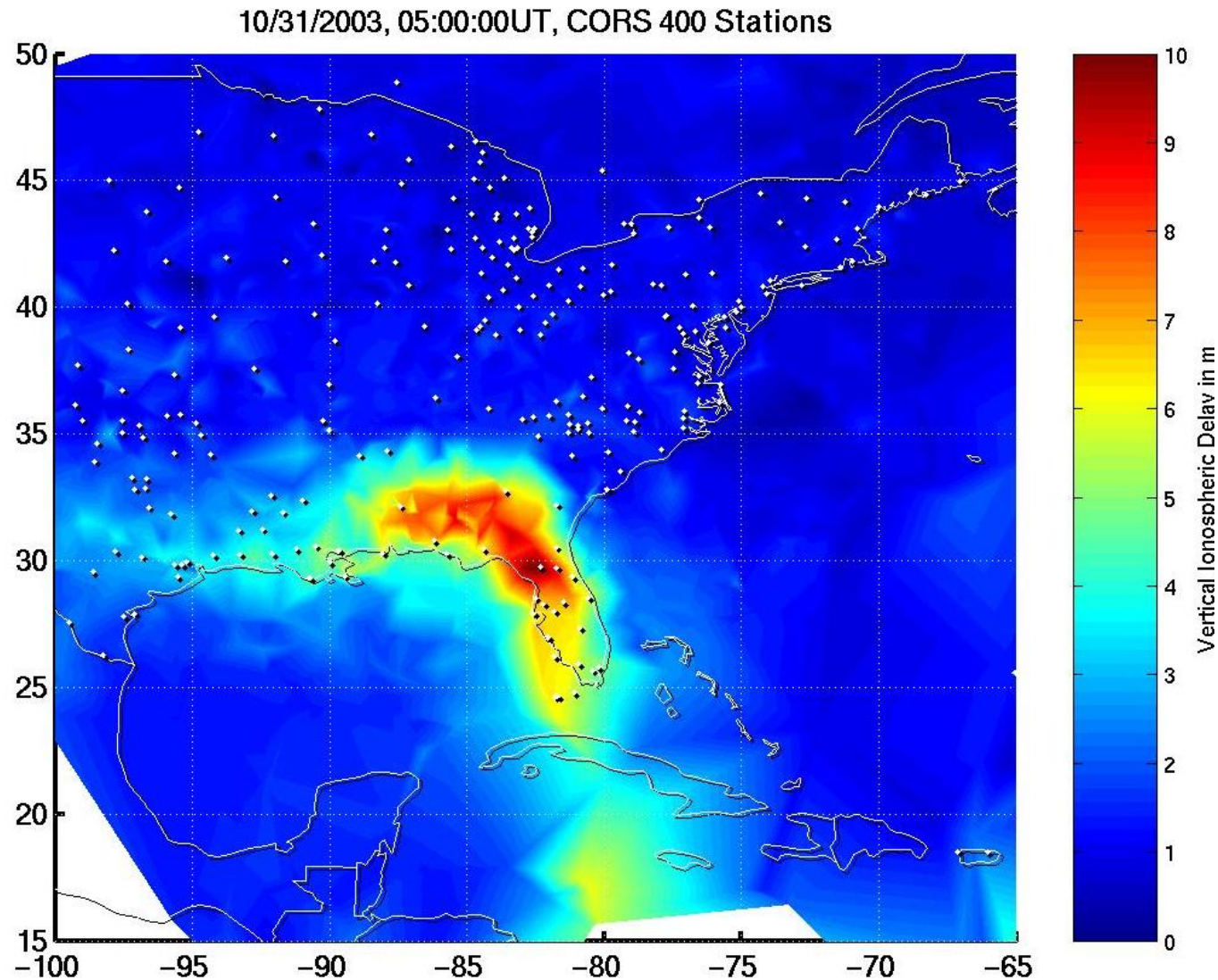


Courtesy:  
Seebany  
Datta-Barua





# Small-scale Irregularity



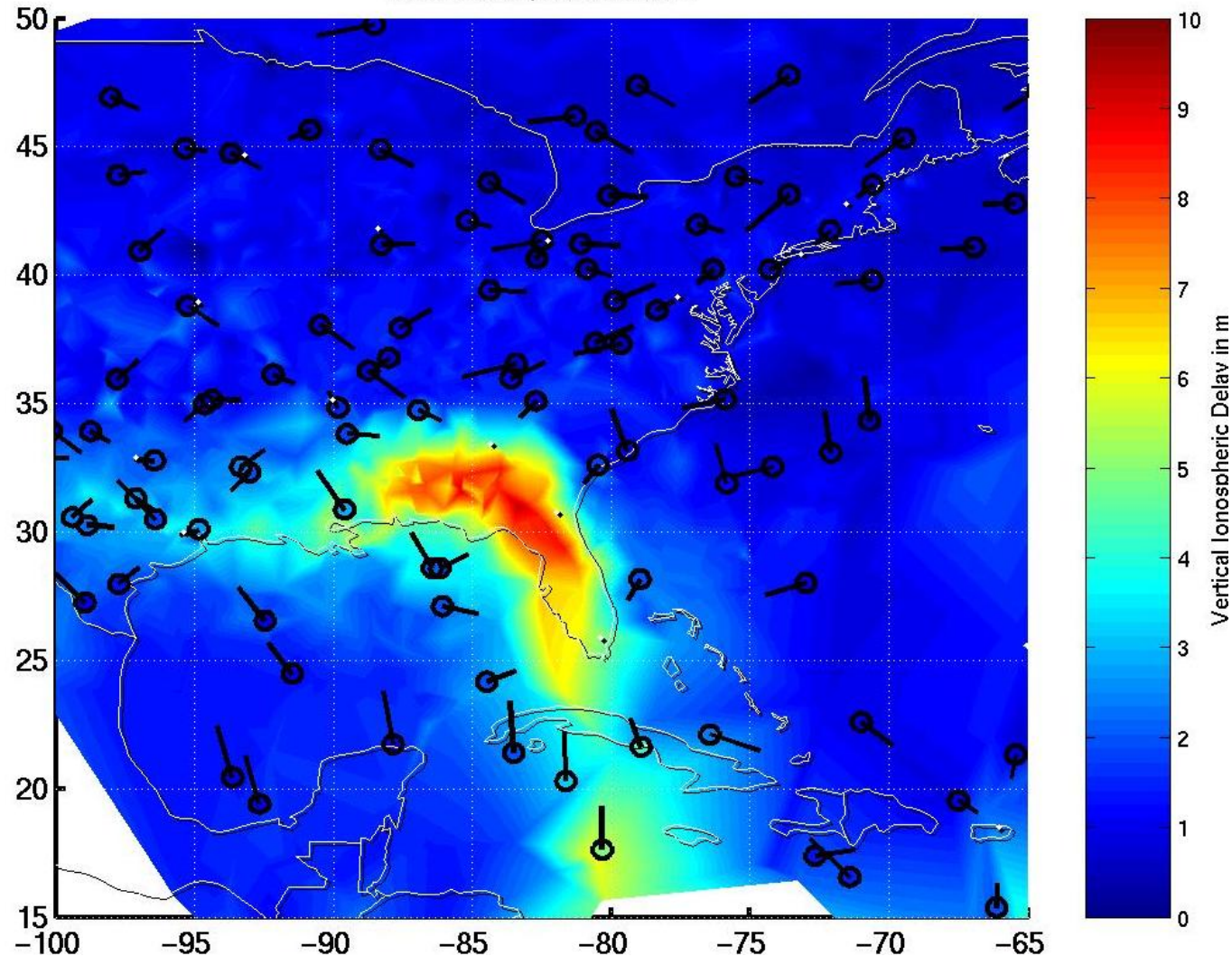
Courtesy:  
Seebany  
Datta-Barua



# Artificial Undersampled Scenario



10/31/2003, 05:00:00UT

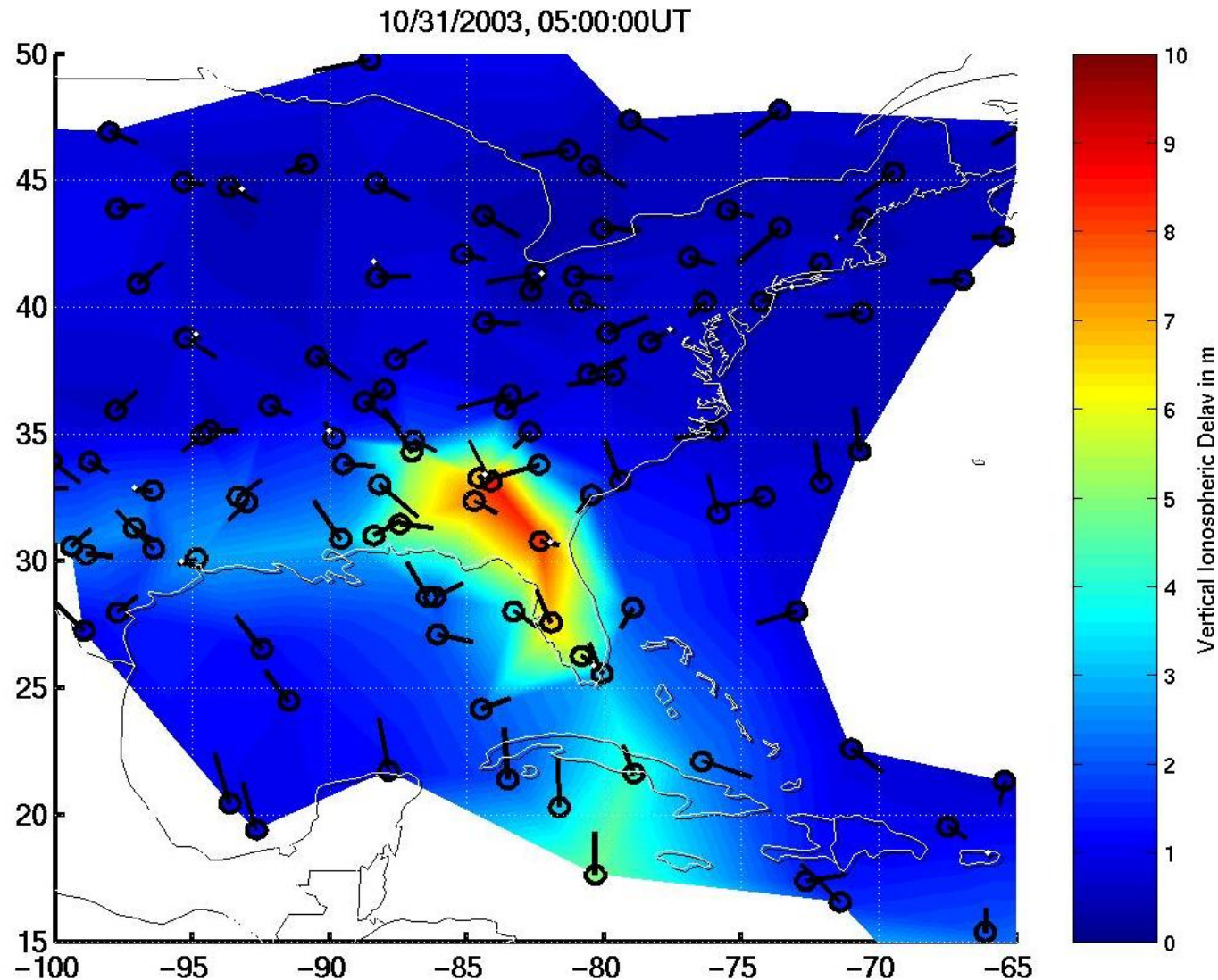


Courtesy:  
Seebany  
Datta-Barua





# WAAS Measurements



Courtesy:  
Seebany  
Datta-Barua

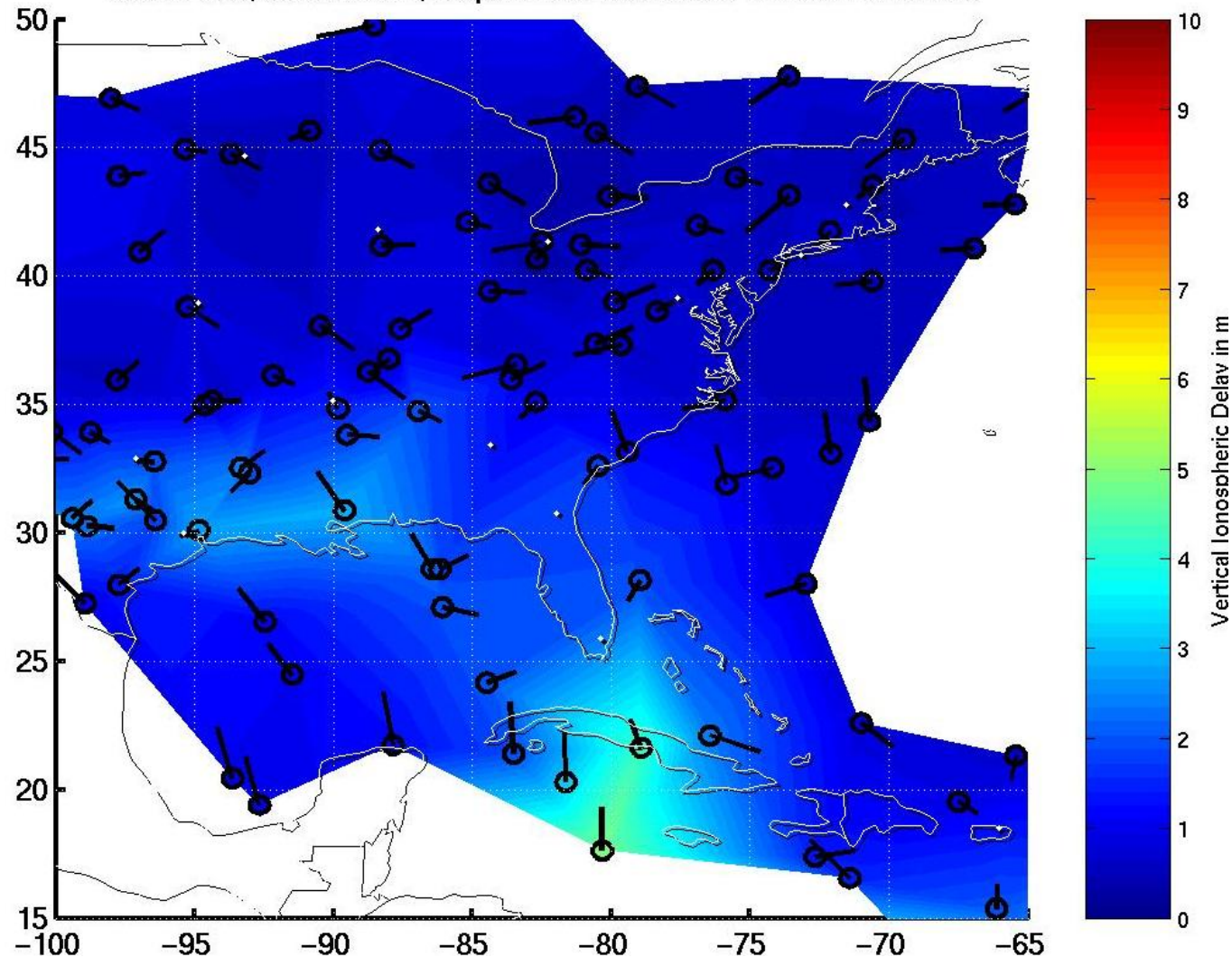


# Artificial WAAS

## Undersampling Scenario



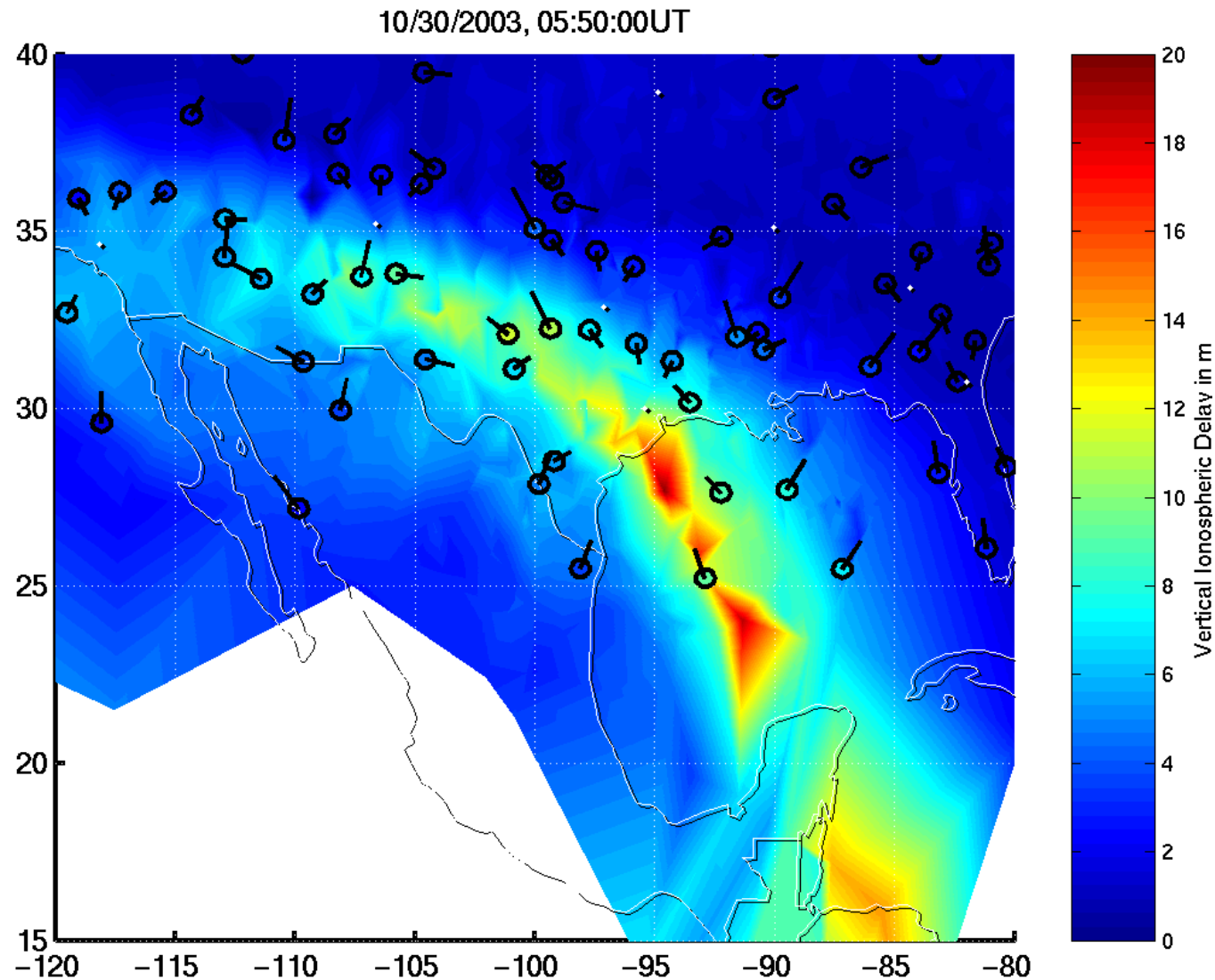
10/31/2003, 05:00:00UT, Supertruth Malicious Threat Removed



Courtesy:  
Seebany  
Datta-Barua



# Real Undersampled Condition

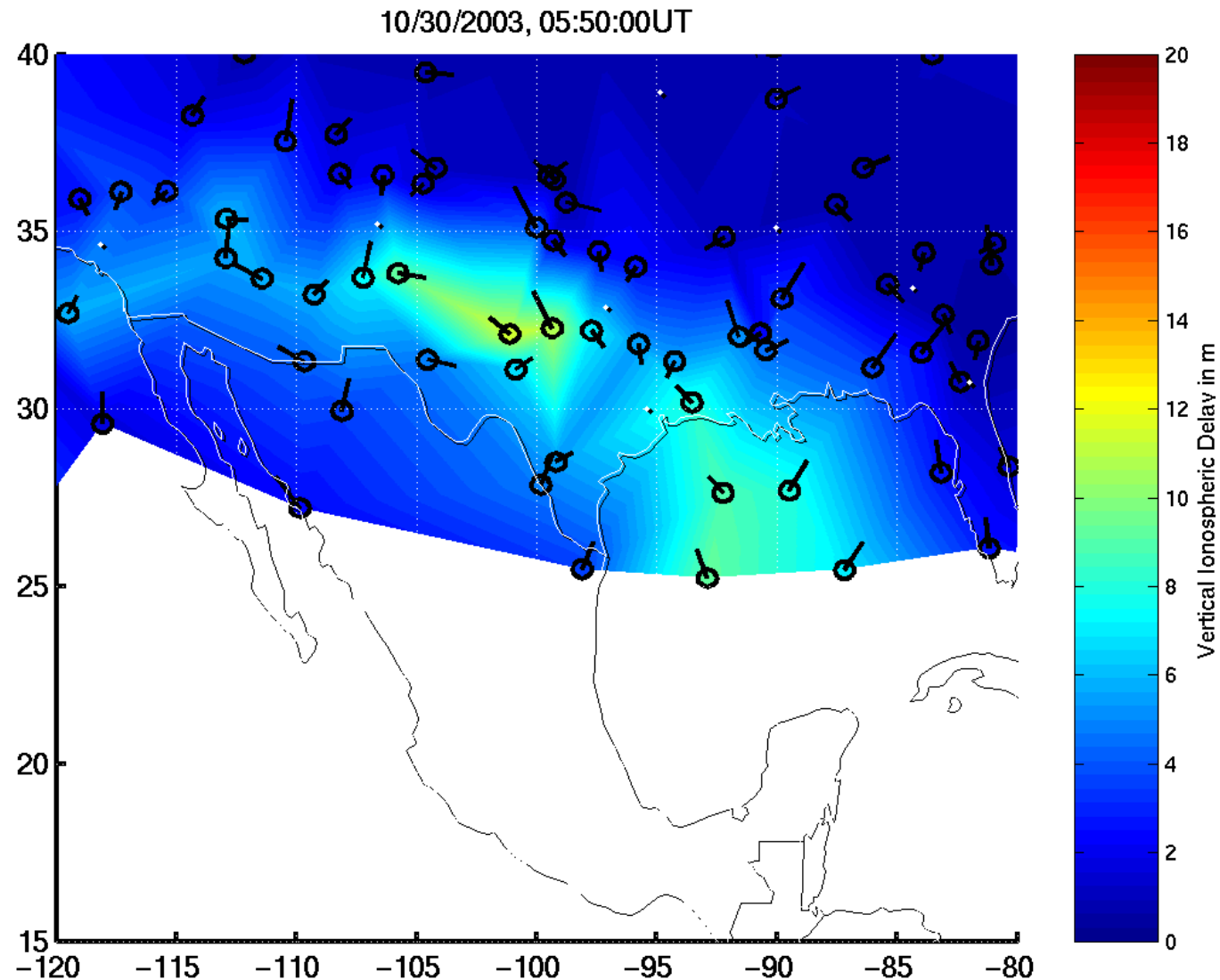


Courtesy:  
Seebany  
Datta-Barua





# WAAS Measurements



Courtesy:  
Seebany  
Datta-Barua

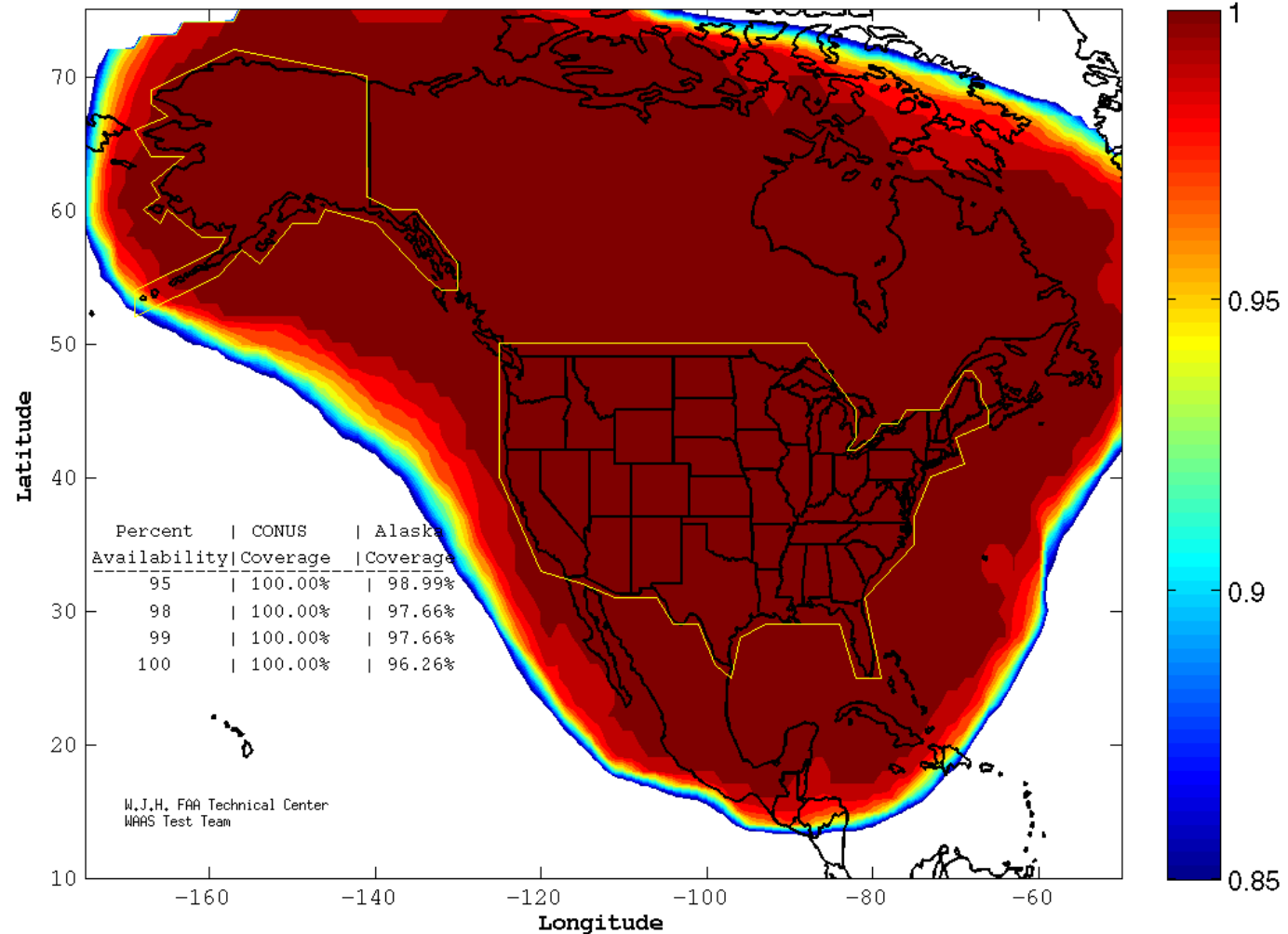


# Nominal WAAS Vertical Guidance Performance

WAAS LPV Coverage Contours

04/22/11

Week 1632 Day 5



Courtesy: FAA

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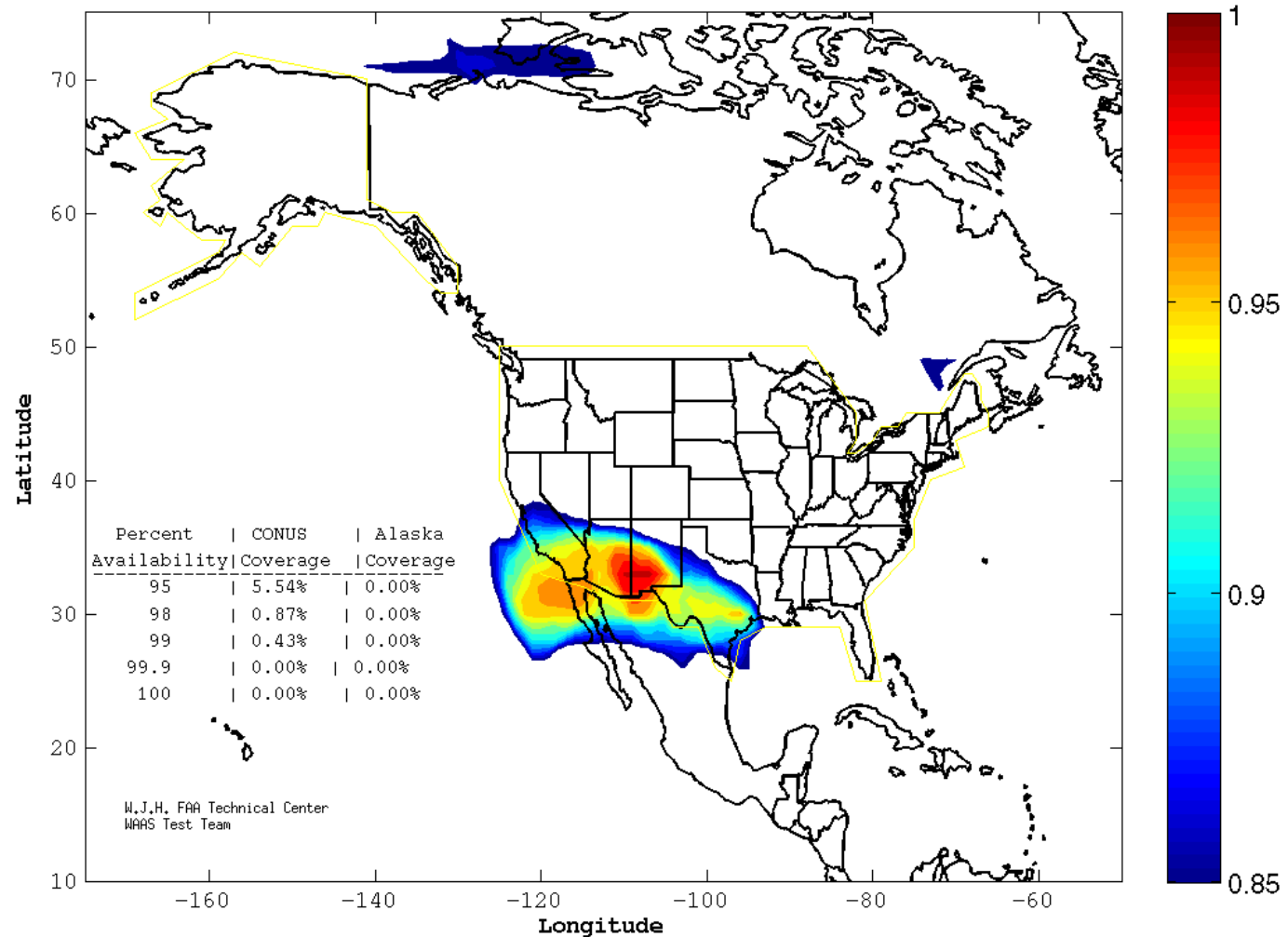


# Vertical Guidance with Major Ionospheric Disturbance

WAAS LPV Coverage Contours

10/25/11

Week 1659 Day 2



Courtesy: FAA

Presented at ICTP  
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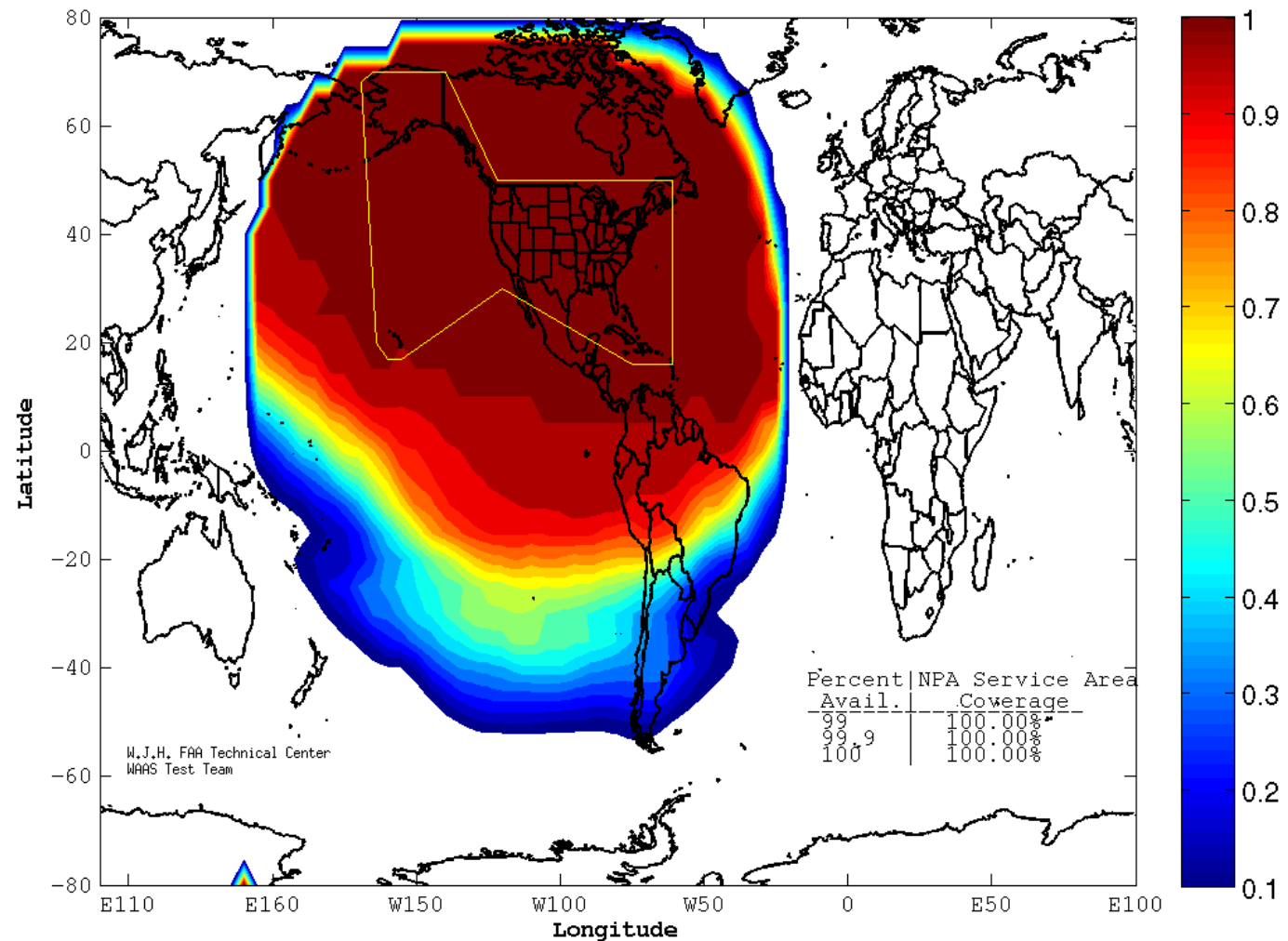


# Nominal WAAS Horizontal Guidance Performance

WAAS RNP 0.1 Coverage Contours

04/22/11

Week 1632 Day 5



Courtesy: FAA

Presented at ICTP  
Copyright 2012  
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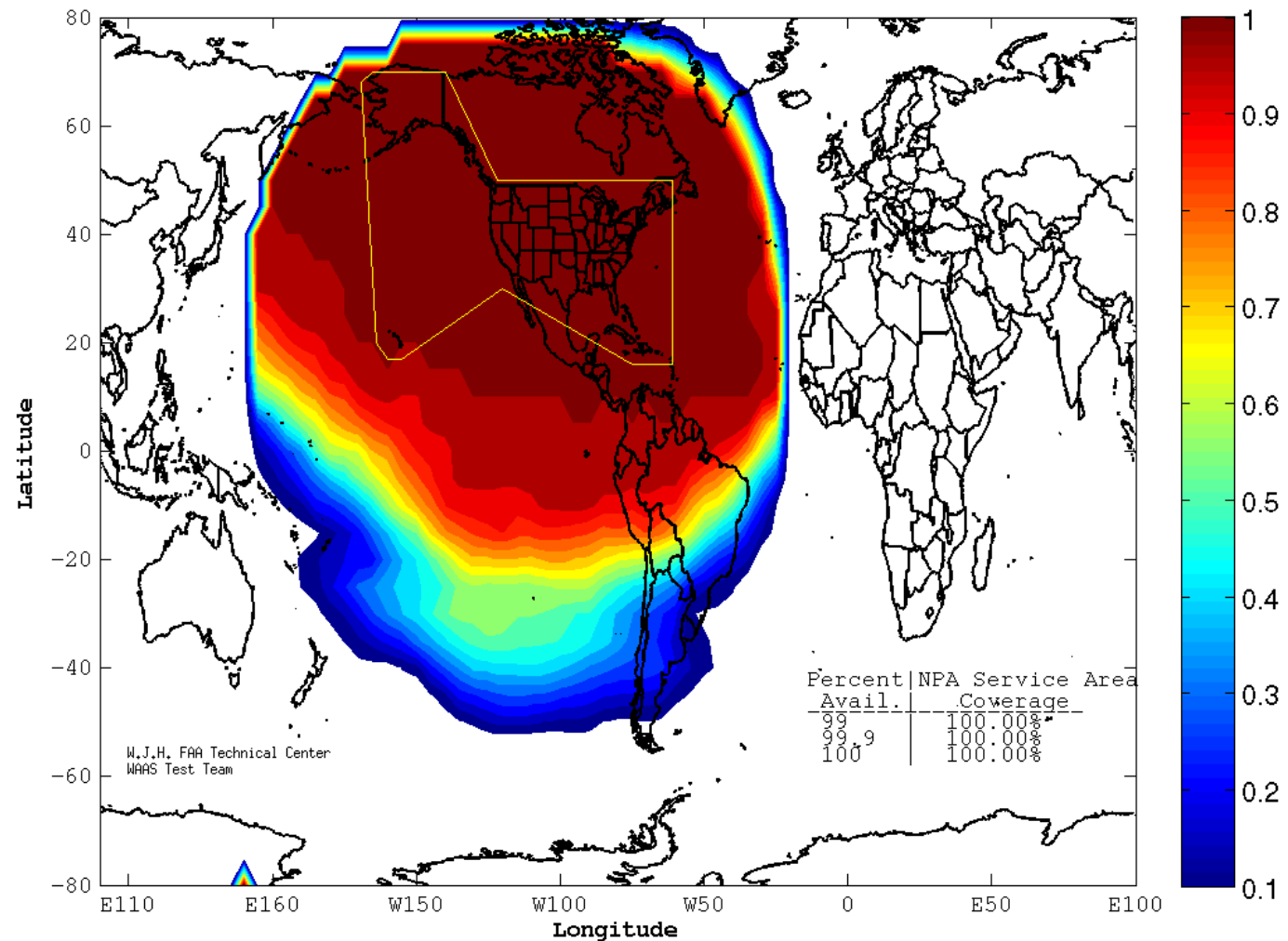


# Horizontal Guidance in Major Ionospheric Disturbance

WAAS RNP 0.1 Coverage Contours

10/25/11

Week 1659 Day 2



Courtesy: FAA

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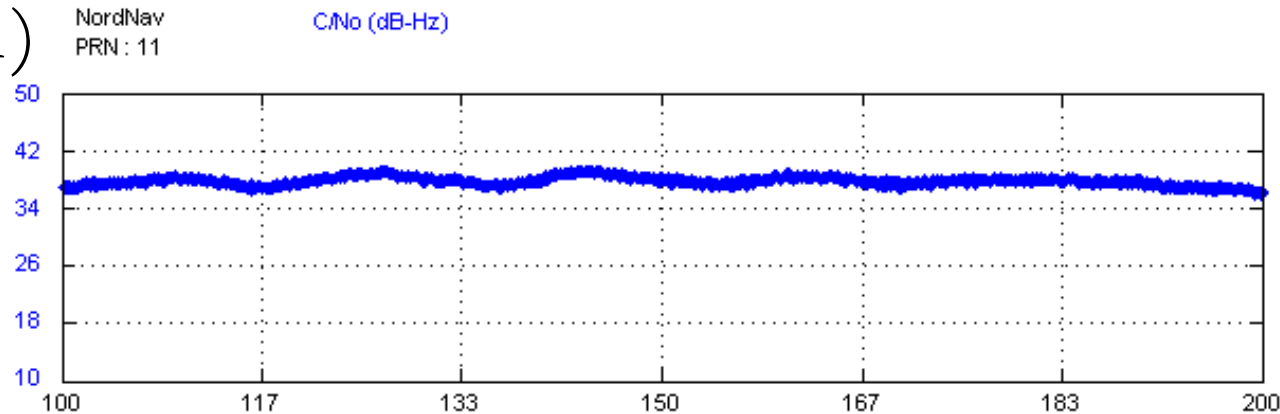
# Scintillation and Deep Signal Fading



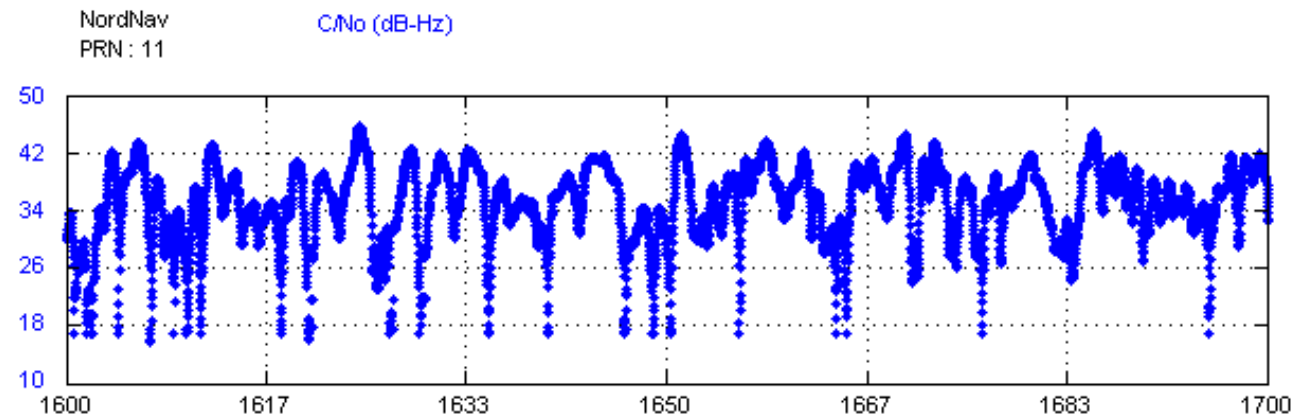
- Signal to noise ratio ( $C/N_0$ ) of PRN 11 (Mar. 18, 2001)

$C/N_0$

Nominal



Scintillation  
(equatorial &  
solar max)



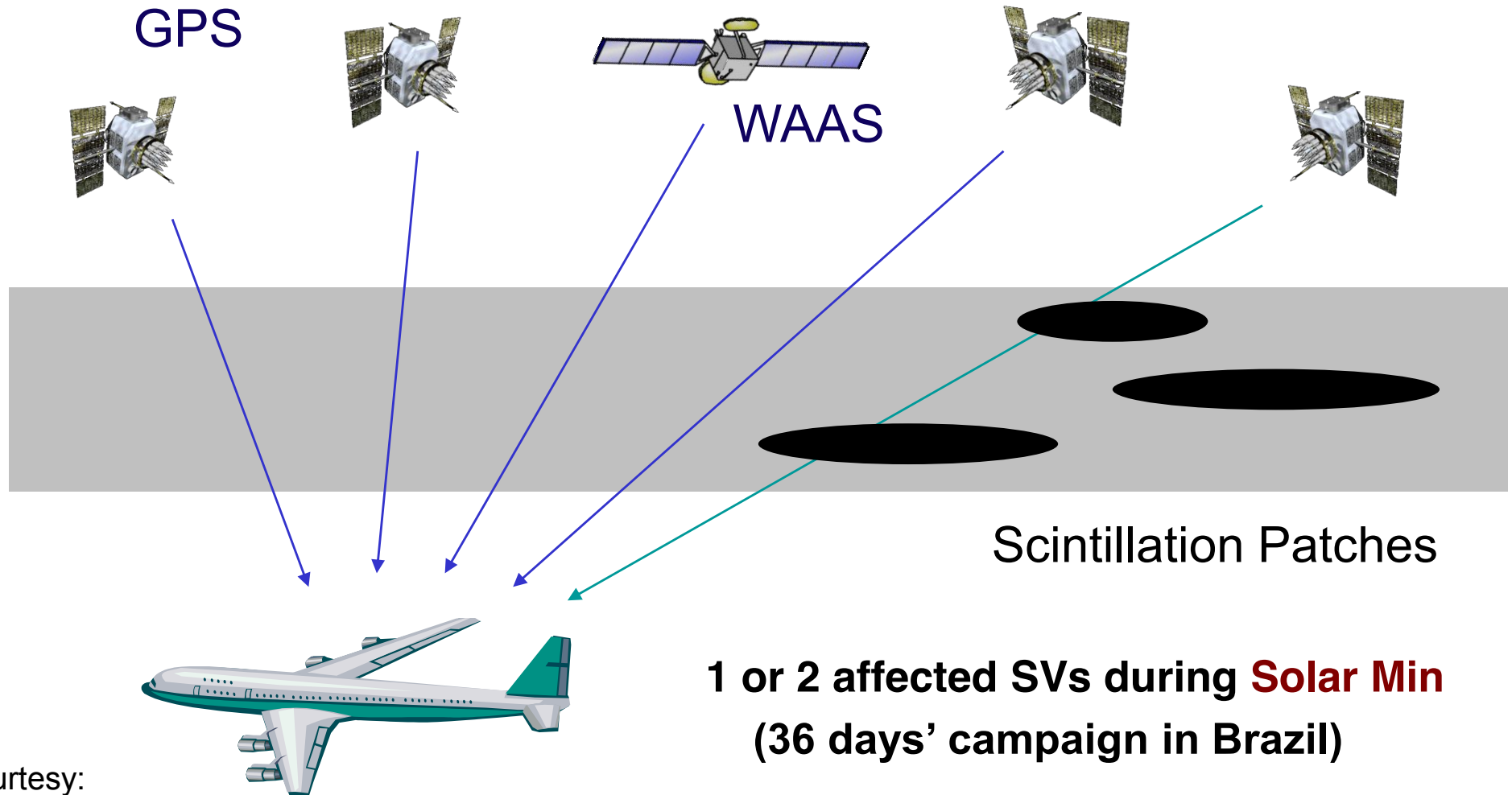
25 dB

Courtesy:  
Jiwon Seo

100 sec



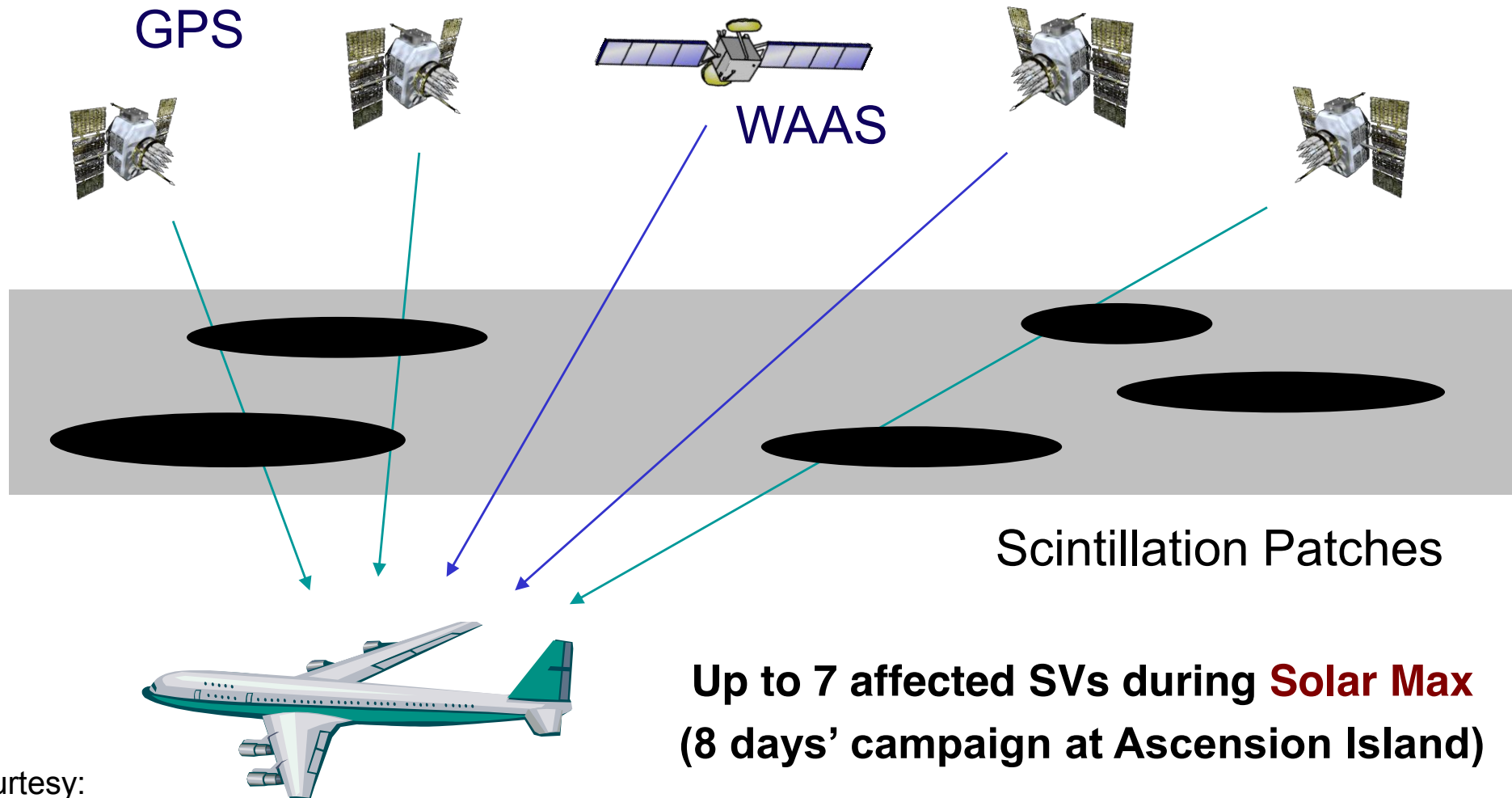
# Scintillation and Navigation



Courtesy:  
Jiwon Seo



# Scintillation and Navigation



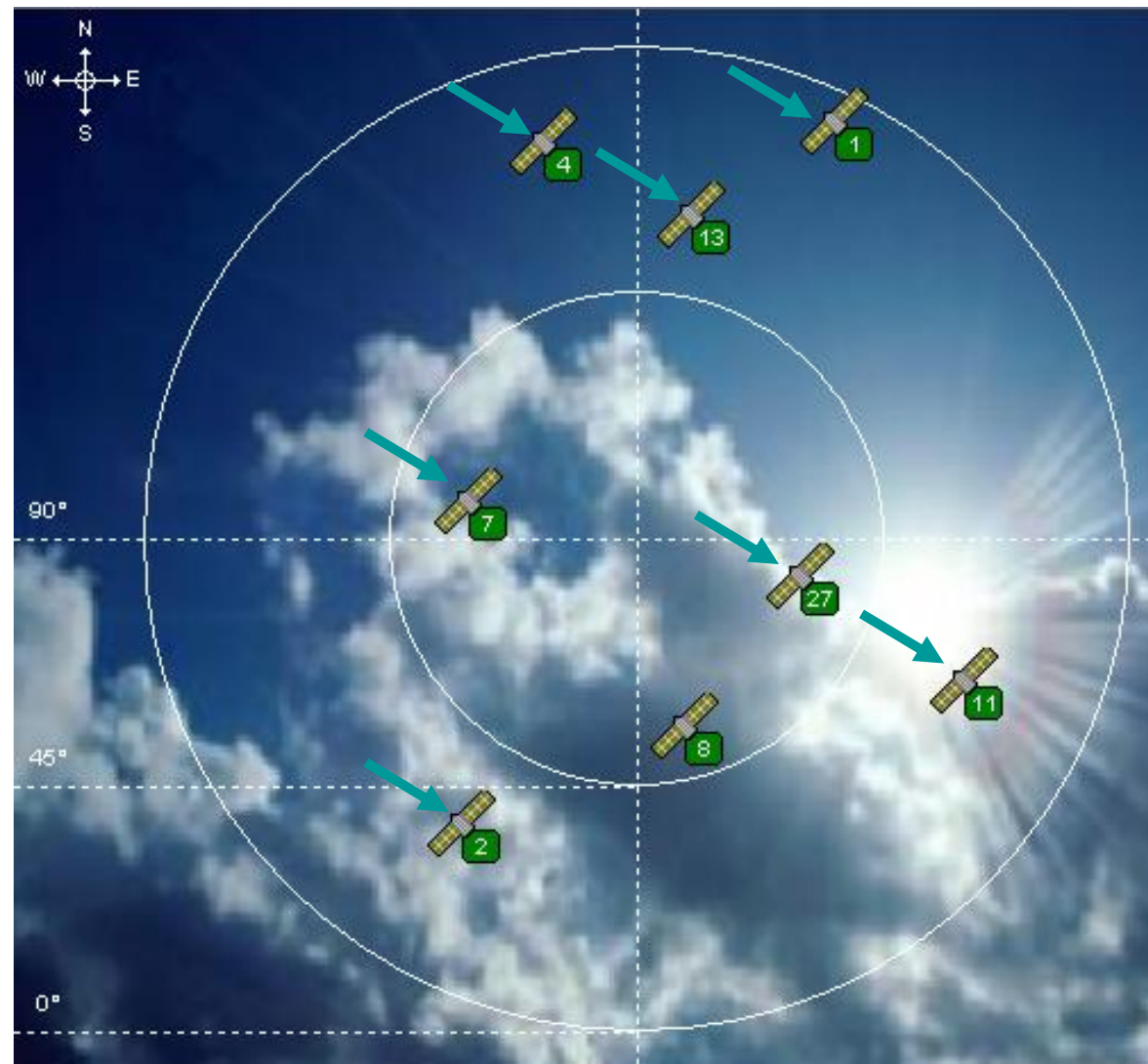
Courtesy:  
Jiwon Seo



# Severe Scintillation Data



Solar Max  
(worst 45 min  
in 8 days)



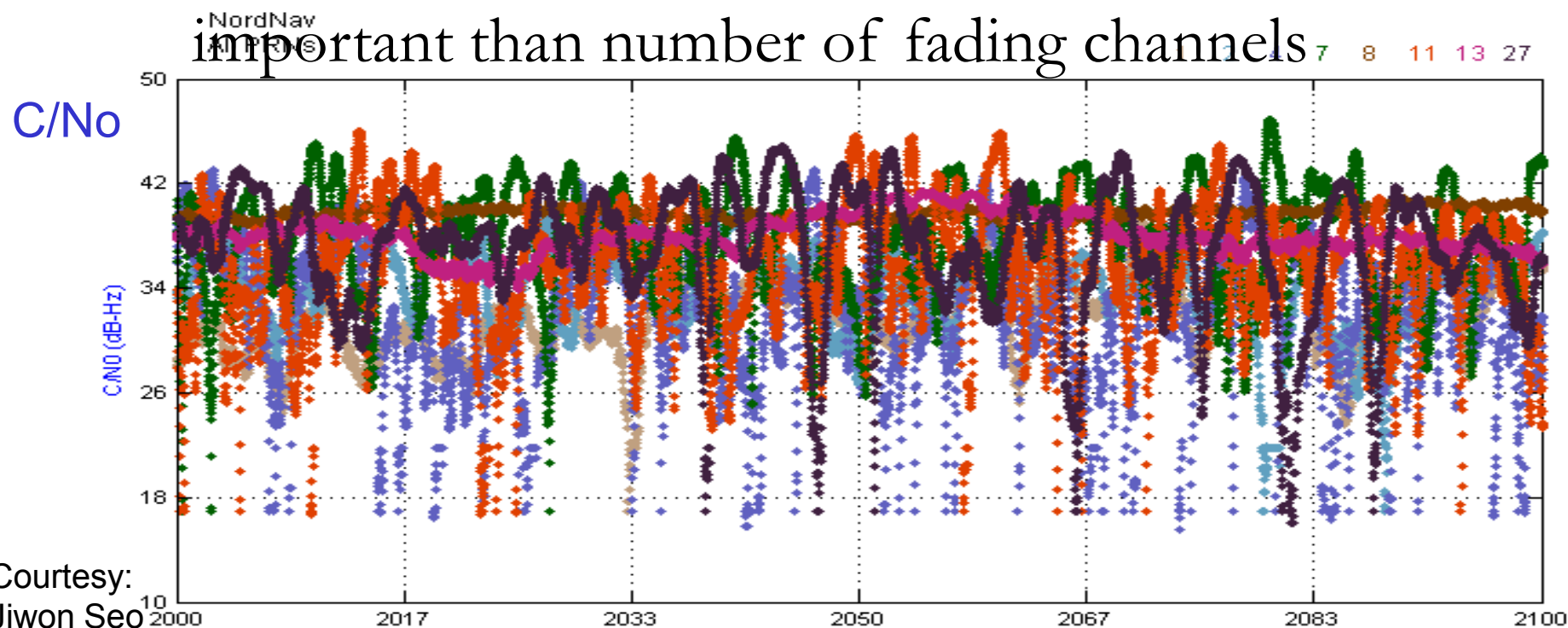
Courtesy:  
Jiwon Seo



# Severe Scintillation (example)



- 50 Hz C/No outputs of all 8 satellites on sky (100 sec out of 45 min data as an example)
- Number of simultaneous loss of satellites is more important than number of fading channels



Courtesy:  
Jiwon Seo

100 sec





# Hatch Filter Model



NordNav  
PRN : 11

C/No (dB-Hz)

50 dB-Hz

C/No

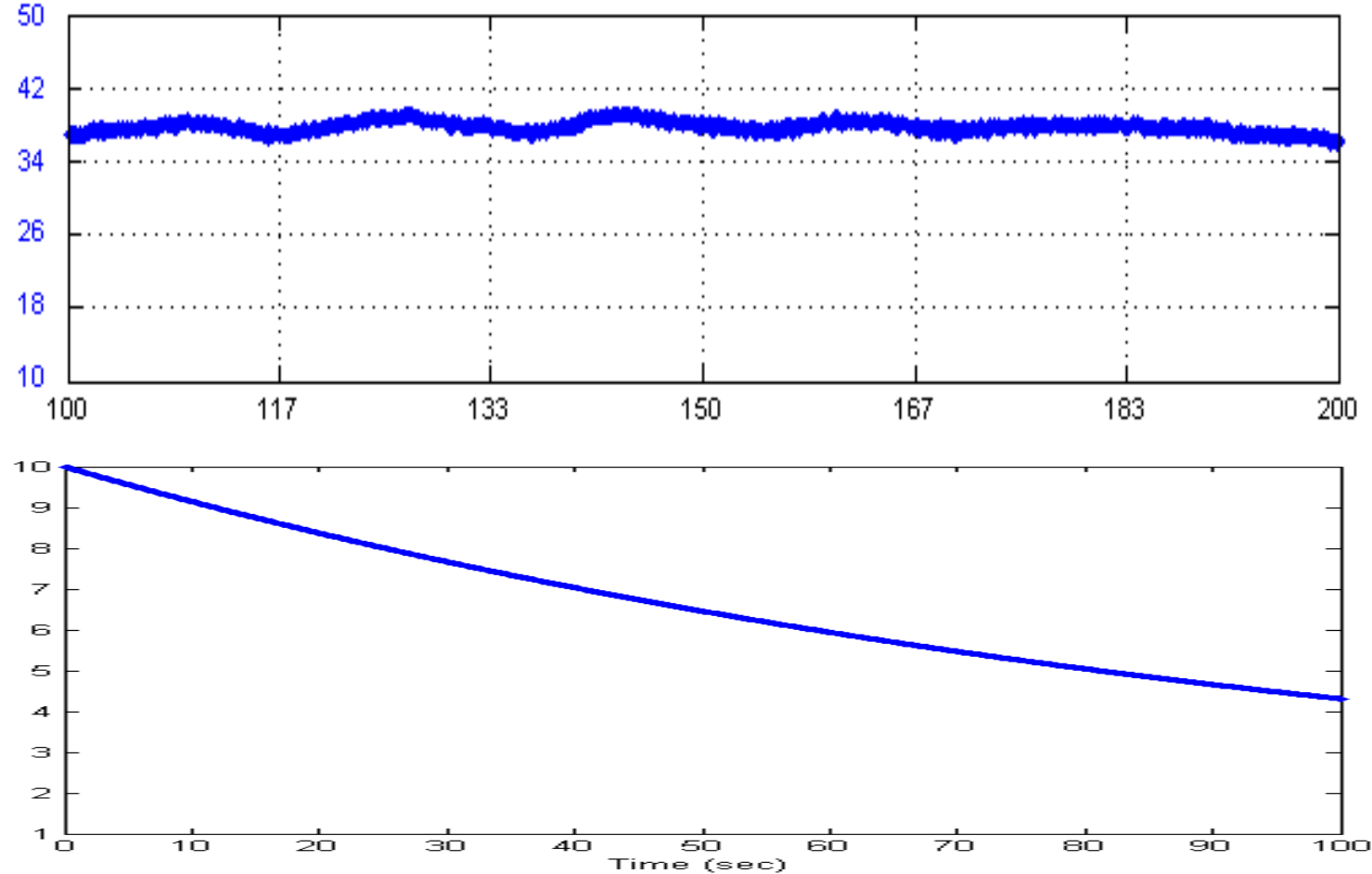
10 dB-Hz

10

Relative  
Noise  
Level

1

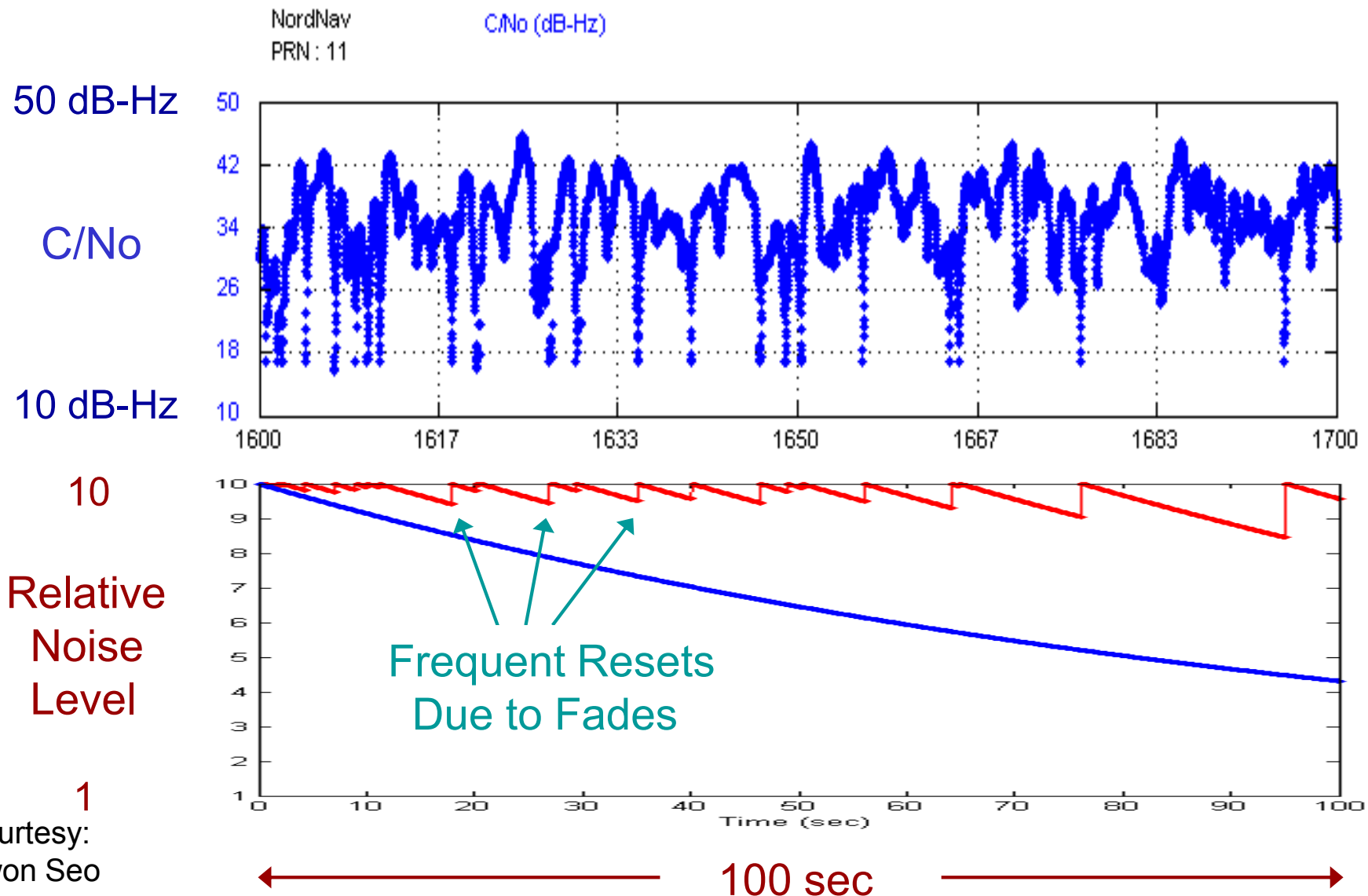
Courtesy:  
Jiwon Seo



← 100 sec →



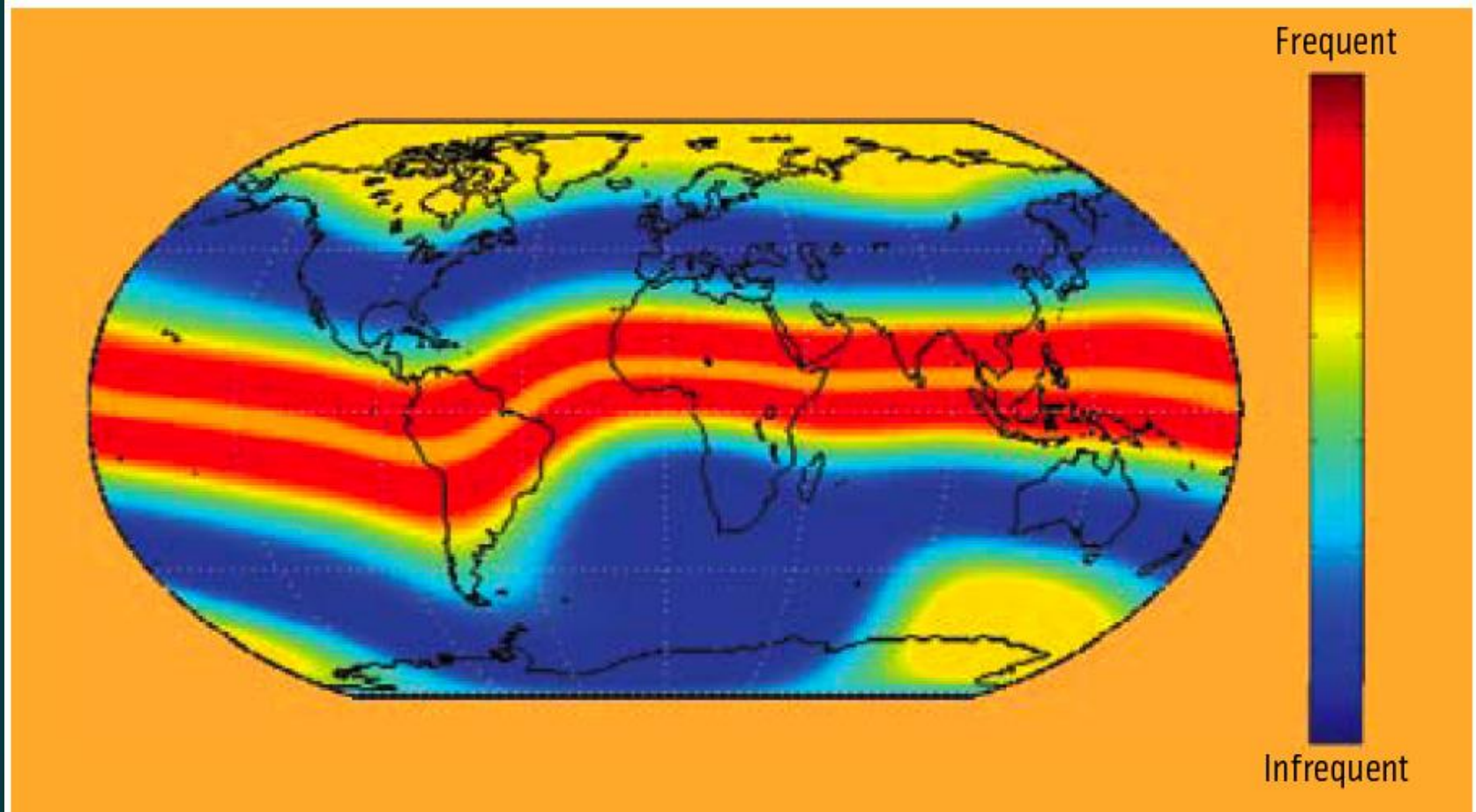
# Hatch Filter Model



Courtesy:  
Jiwon Seo



# Regions with Scintillation



Courtesy: Paul Kintner

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**FIGURE 1** Scintillation map showing the frequency of disturbances at solar maximum. Scintillation is most intense and most frequent in two bands surrounding the magnetic equator, up to 100 days per year. At poleward latitudes, it is less frequent and it is least frequent at mid-latitude, a few to ten days per year.



# Outline

- ➔ Ionospheric Modeling
- ➔ Ionospheric Threats
- ➔ **Other Integrity Threats**
- ➔ Integrity Methodology
- ➔ Next Generation Satellite Navigation
- ➔ Future Signals
- ➔ Conclusions





# Integrity

- ➔ Monitor network or signal redundancy identifies observable threats
  - ➔ *Protection against satellite failures*
    - ➔ Ephemeris errors
    - ➔ Clock errors
    - ➔ Signal errors
  - ➔ *Protection against ionospheric errors*
- ➔ Design assumes worst credible values for all unobservable threats



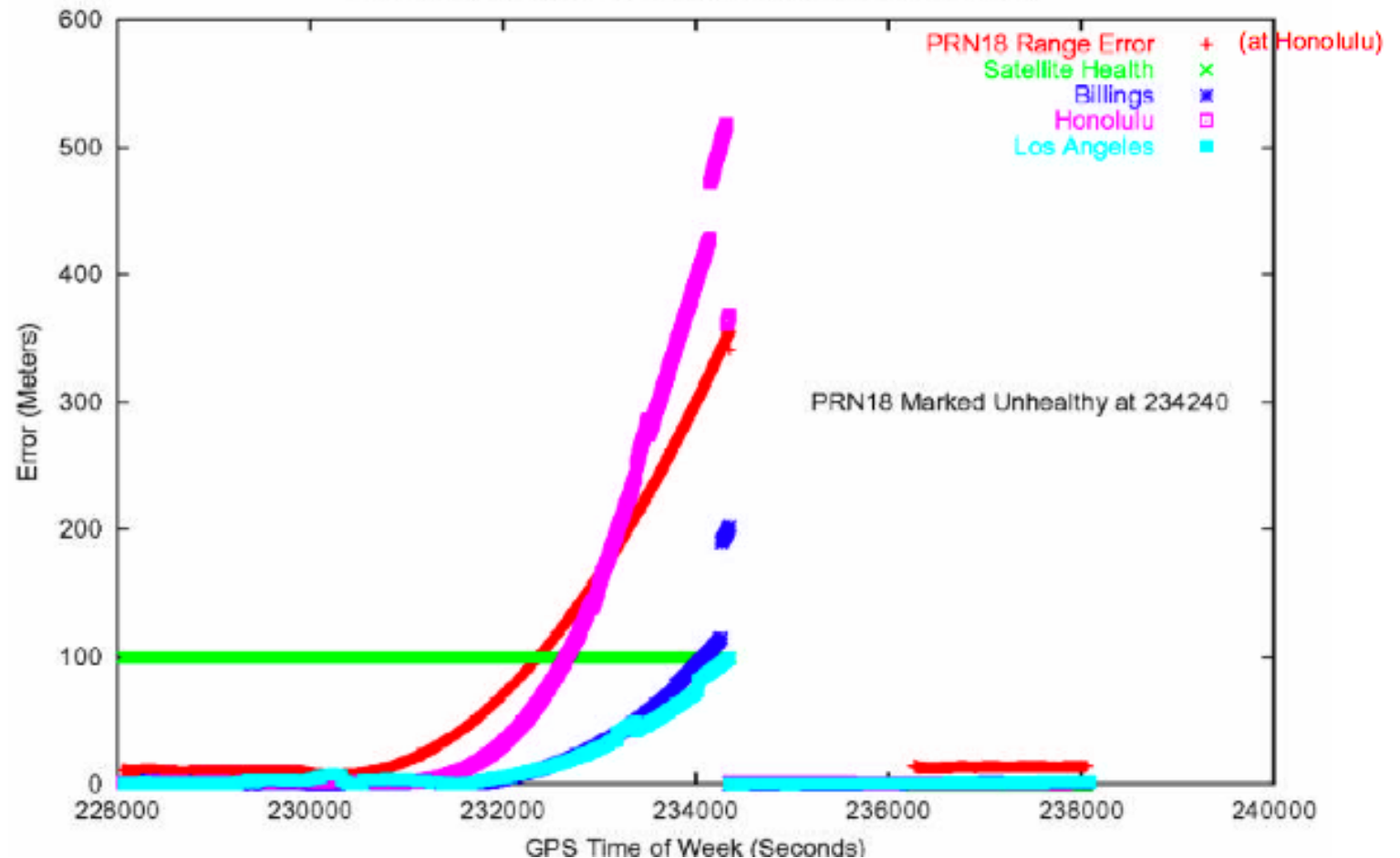
# Satellite Ephemeris Anomaly



## Observed GPS SPS 3-D Position Errors on April 10, 2007

**Source: FAATC GPS SPS PAN Report #58, 31 July 2007.**

SPS 3D Position Error During PRN18 Anomaly: 10 April 2007



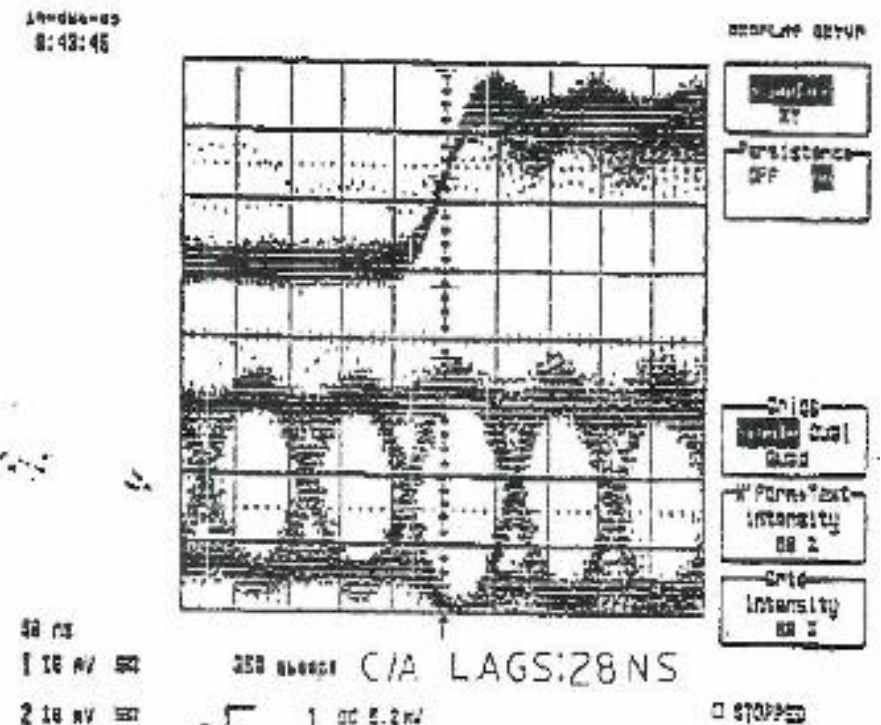
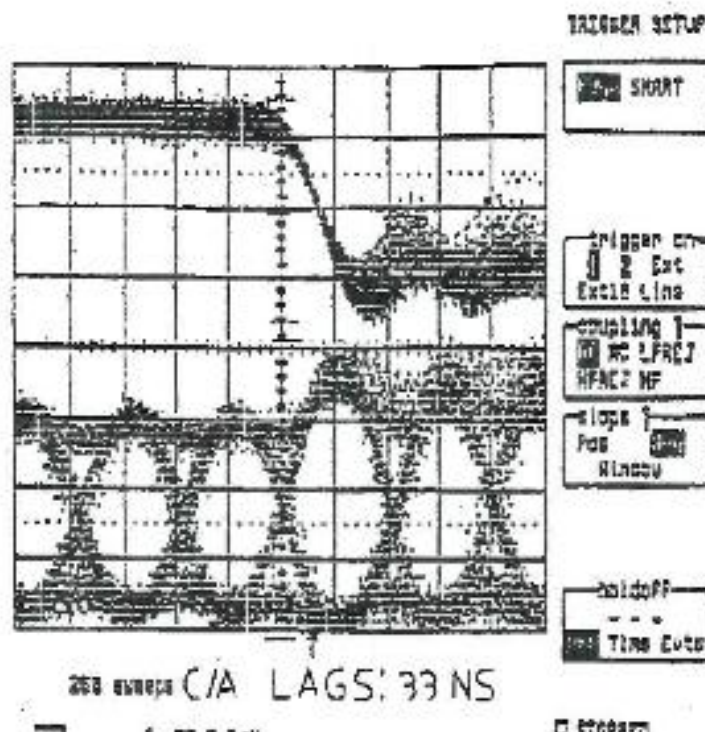


# Satellite Signal Anomaly

## L1 C/A Lags L1 P Code Falling Edge or Leading Edge

Oct 13, 1993, 23:45

Oct 14, 1993, 08:43



Courtesy:  
Per Enge

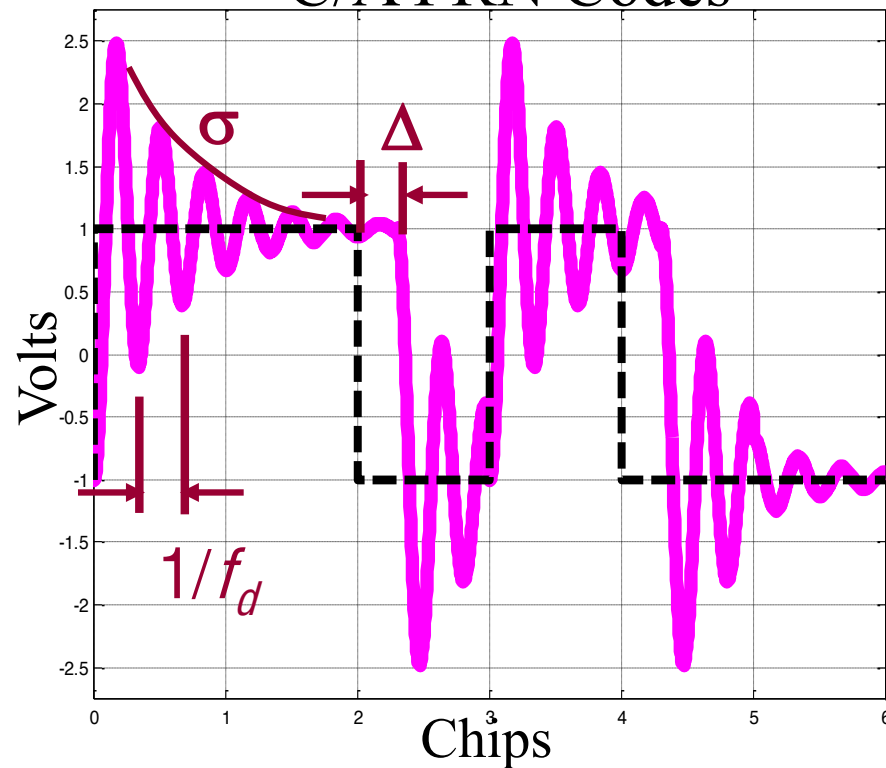
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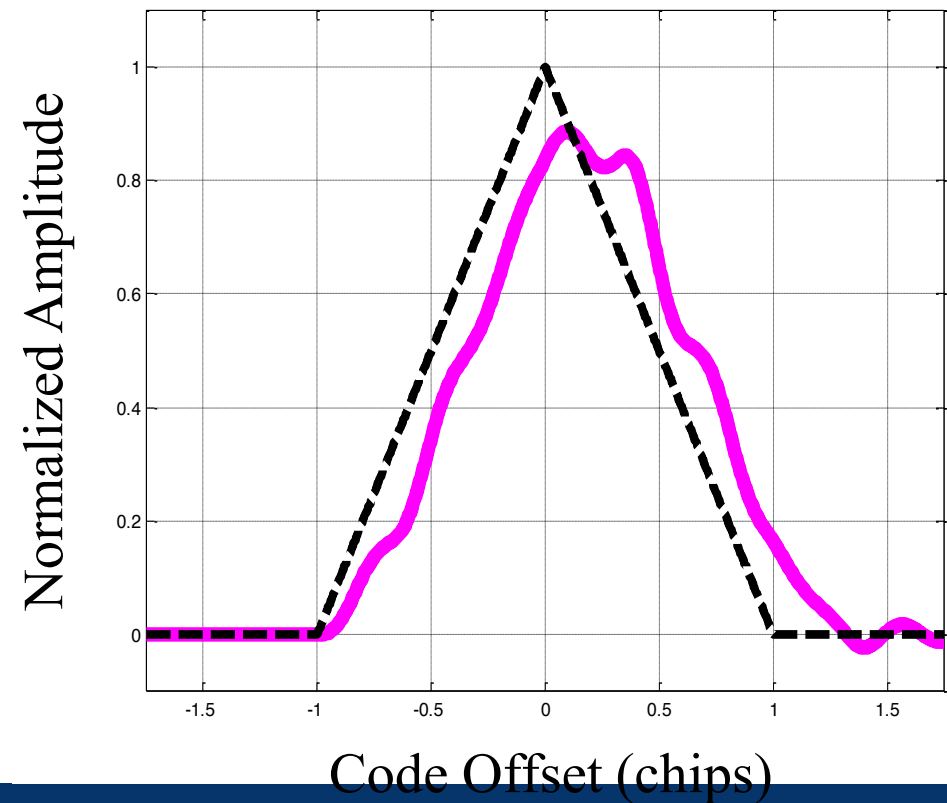
# “Evil Waveform” Failure Mode Example

*Comparison of Ideal and “Evil Waveform” Signals for Threat Model C*

C/A PRN Codes



Correlation Peaks



Todd Walter

59

Courtesy:  
Eric Phelts

Note:

Threat Model A: Digital Failure Mode (Lead/Lag Only:  $\Delta$ )

Threat Model B: Analog Failure Mode (“Ringing” Only:  $f_d\sigma$ )





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- ➔ **Integrity Methodology**
- ➔ Next Generation Satellite Navigation
- ➔ Future Signals
- ➔ Conclusions



# Overall Integrity Approach

- ➔ Conventional Differential GPS Systems Rely on Lack of Disproof
  - ➔ *“I’ve been using it for N years and I’ve never had a problem”*
- ➔  $10^{-7}$  Integrity Requires Active Proof
- ➔ Analysis, Simulation, and Data Must Each Support Each Other
  - ➔ *None sufficient by themselves*
- ➔ Clear Documentation of Safety Rationale is Essential



# Interpretation of “Probability of HMI $< 10^{-7}$ Per Approach”

## → Possible Interpretations

- *Ensemble Average of All Approaches Over Space and Time*
- *Ensemble Average of All Approaches Over Time for the Worst Location*
- *Previous Plus No Discernable Pattern (Rare & No Correlation With User Behavior)*
- *Worst Time and Location*



# Probability of Integrity Failure

## → Average Risk

$$\sum_{all\ conditions} P(fault \mid condition) \times P(condition)$$

## → Specific Risk

$$P(fault \mid condition)$$





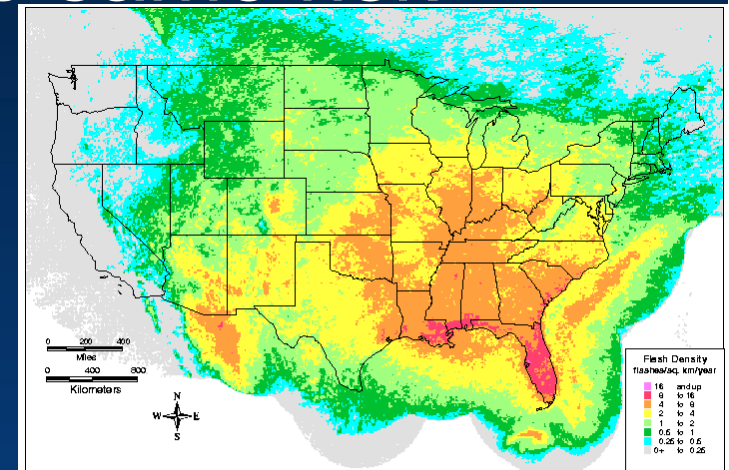
# Probability of Being Struck by Lightning

- ➔ From the Lightning Safety Institute
  - ➔ *USA population = 280,000,000*
  - ➔ *1000 lightning victims/year/average*
  - ➔ *Odds = 1 : 280,000 of being struck by lightning*
- ➔ Not everyone has the same risk

One person struck 7 times

Naïve calculation:  
< 1e-38 probability

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Todd Walter



Global Atmospherics, Inc.  
Light Analysis and Lightning Location System

1996-2000 Flash Density Map  
10 kilometer grid

Jan 1, 1996 00:00:00 GMT  
TO  
Dec 31, 2000 23:59:59 GMT



# WAAS Interpretation

- ➔ Events handled case by case
- ➔ Events that are rare and random may take advantage of an *a priori*
- ➔ Deterministic events must be monitored or treated as worst-case
- ➔ Events that are observable must be detected (if risk  $> 10^{-7}$ )
- ➔ Must account for worst-case undetected events



# Outline

- ➔ Ionospheric Modeling
- ➔ Ionospheric Threats
- ➔ Other Integrity Threats
- ➔ Integrity Methodology
- ➔ **Next Generation Satellite Navigation**
- ➔ Future Signals
- ➔ Conclusions



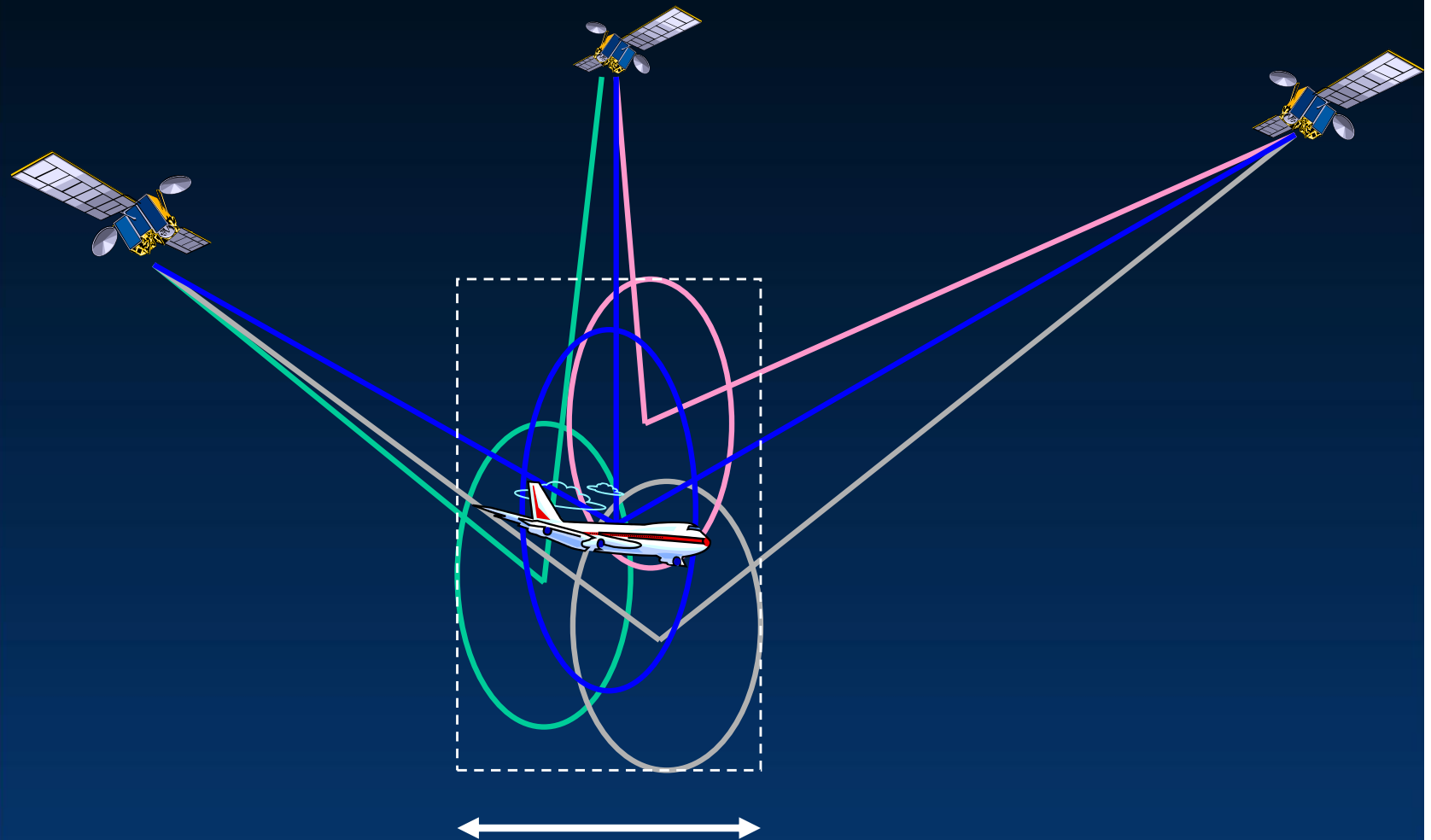
# Looking Ahead

- ➔ Next generation of satellite navigation will exploit new signals and new systems
  - ➔ *GPS is being modernized*
  - ➔ *Other nations developing SatNav*
- ➔ It is time to plan ahead
  - ➔ *What new capabilities can we provide?*
  - ➔ *Are there more efficient ways to provide them?*





# RAIM Protection



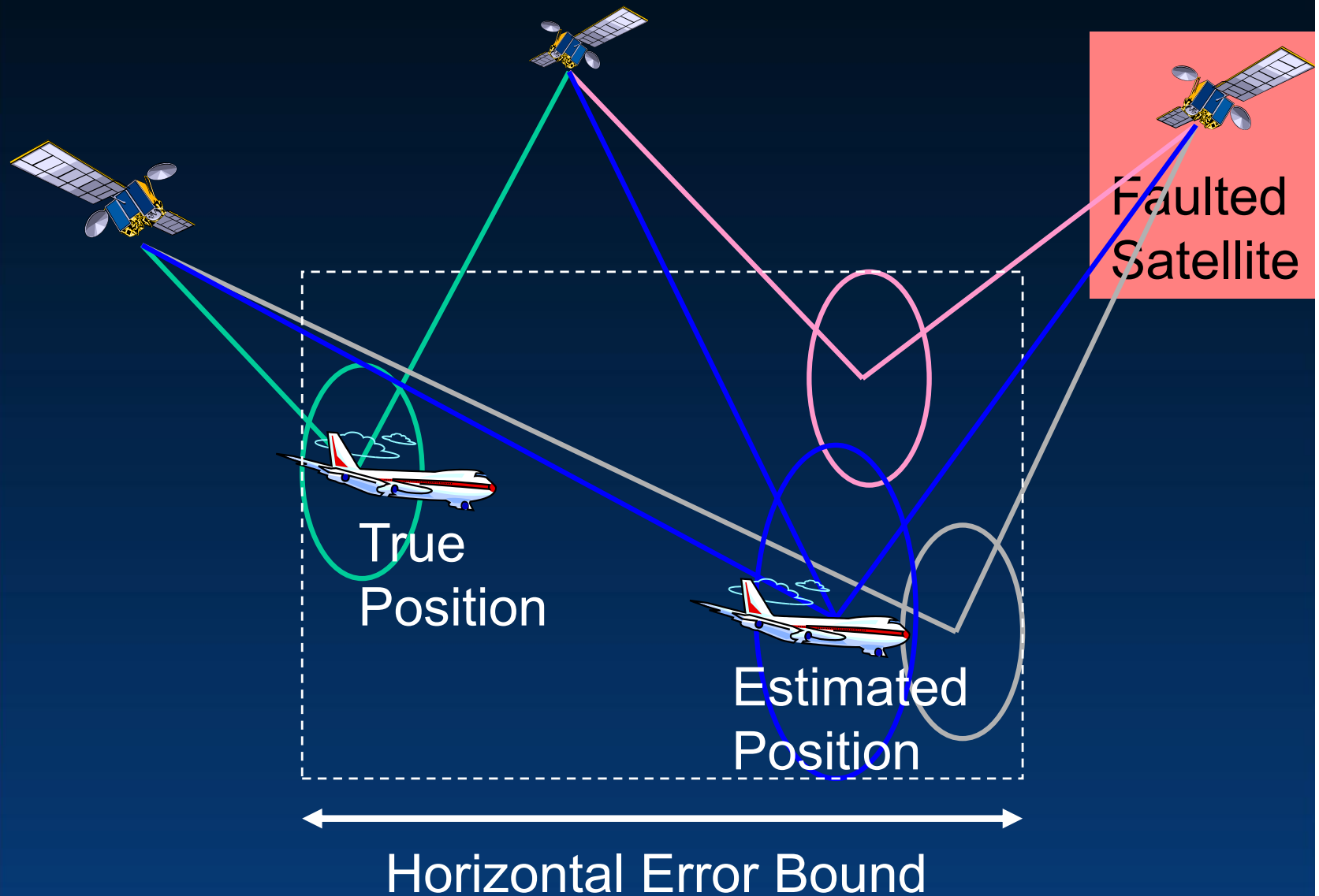
Courtesy:  
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Horizontal Error Bound



# RAIM Protection



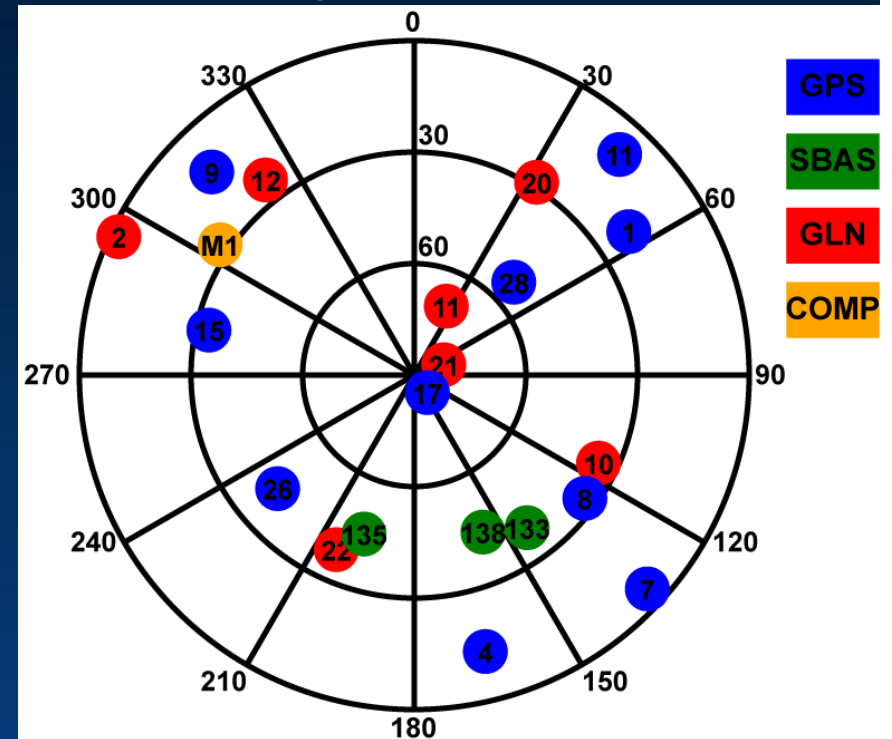
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# New GNSS Constellations

- ➔ A solution to constellation weakness
  - ➔ *Many more ranging sources*
  - ➔ *Fills in gaps*
  - ➔ *Provides extra redundancy*
  - ➔ *Averages down uncertainty*



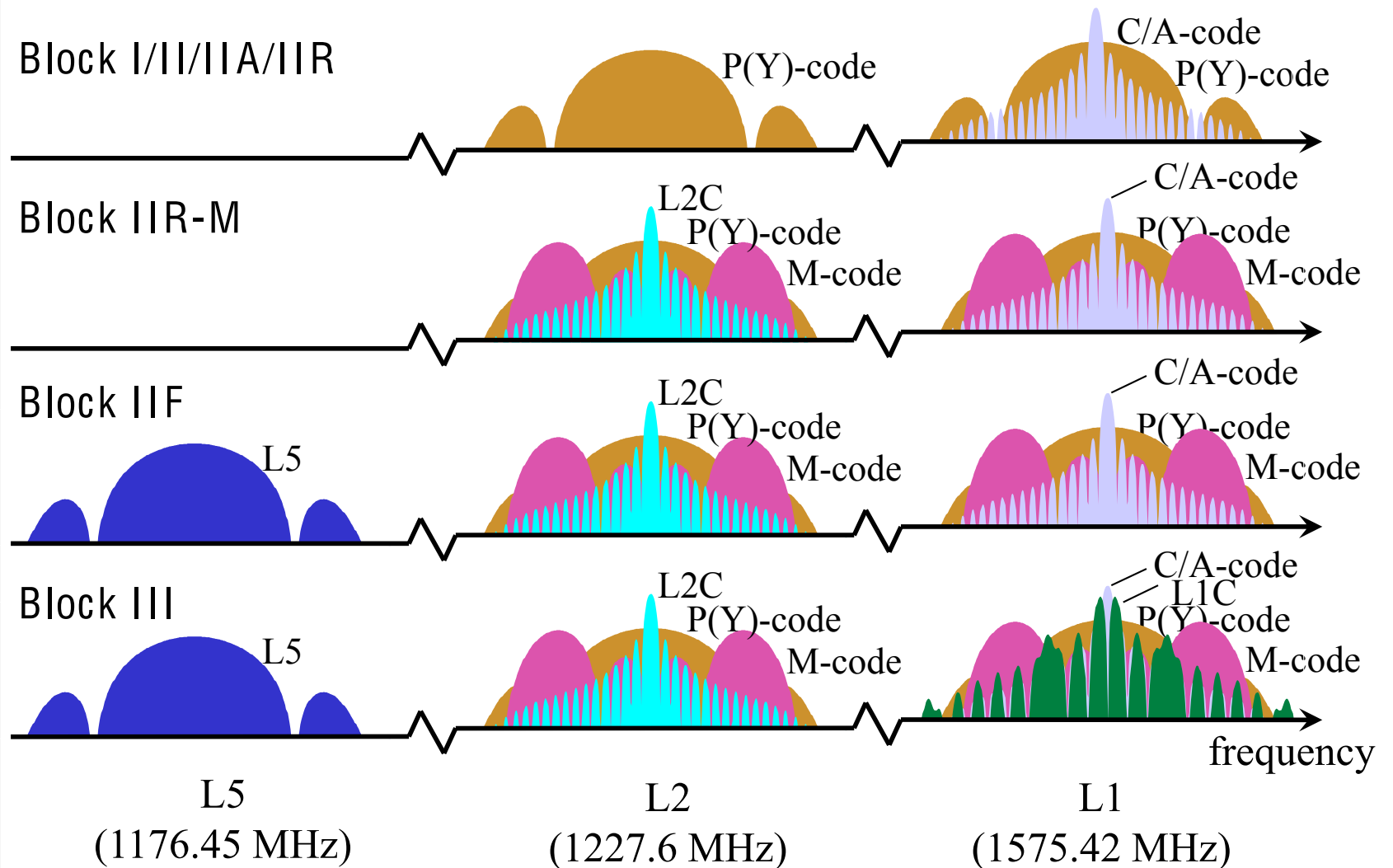


# Advanced RAIM (ARAIM)

- ➔ Dual Frequency - Multi-constellation
  - ➔ *Eliminates multiple SV iono threat*
  - ➔ *Strong geometries*
- ➔ Support for vertical guidance
  - ➔ *Requires a more stringent level of certification than RAIM for lateral*
  - ➔ *May require ground monitoring by approving agency*
- ➔ Potential for near global coverage
  - ➔ *Modest infrastructure requirements*



# GPS Signals



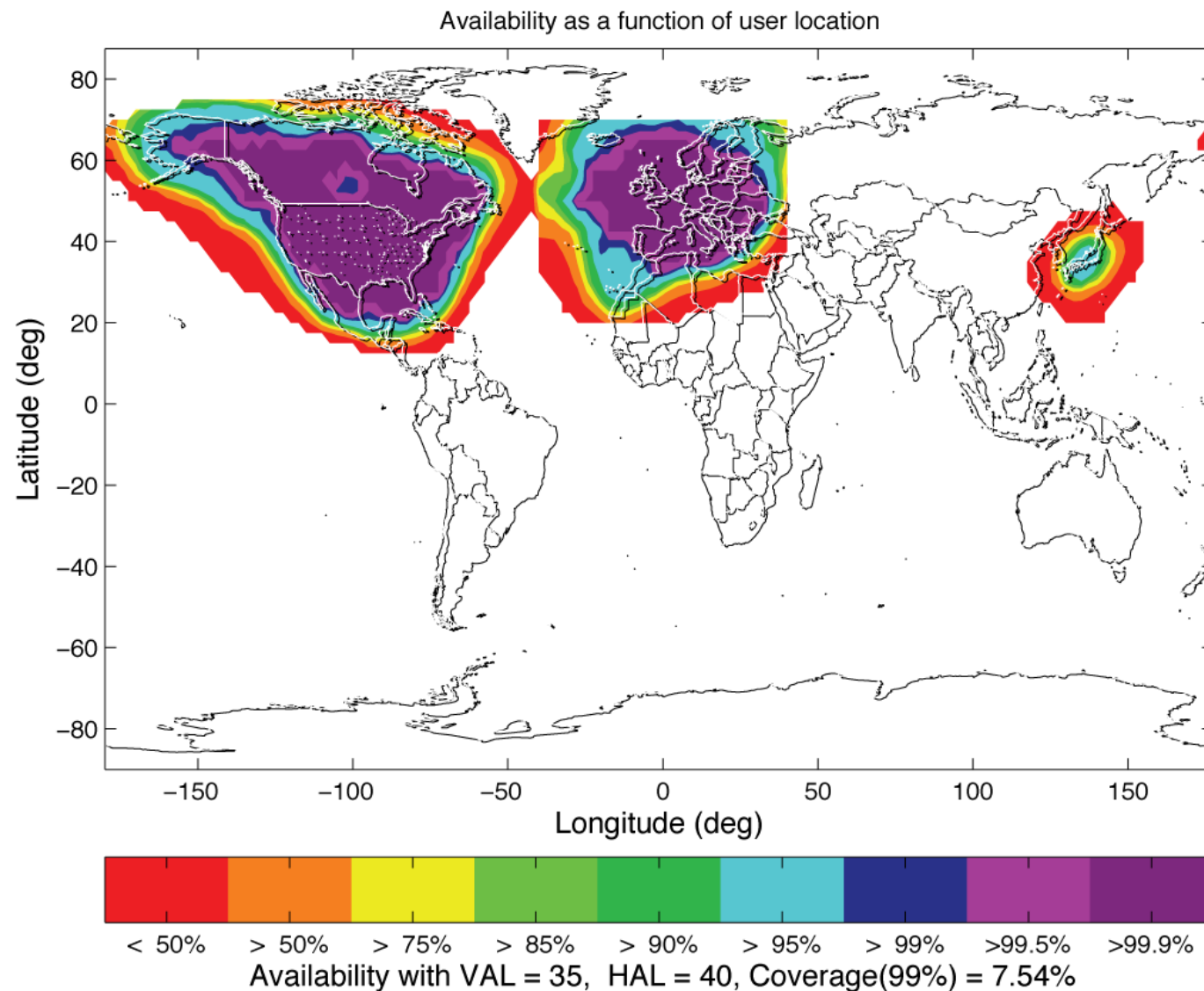




WAAS  
EGNOS  
MSAS

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# Current SBAS Coverage

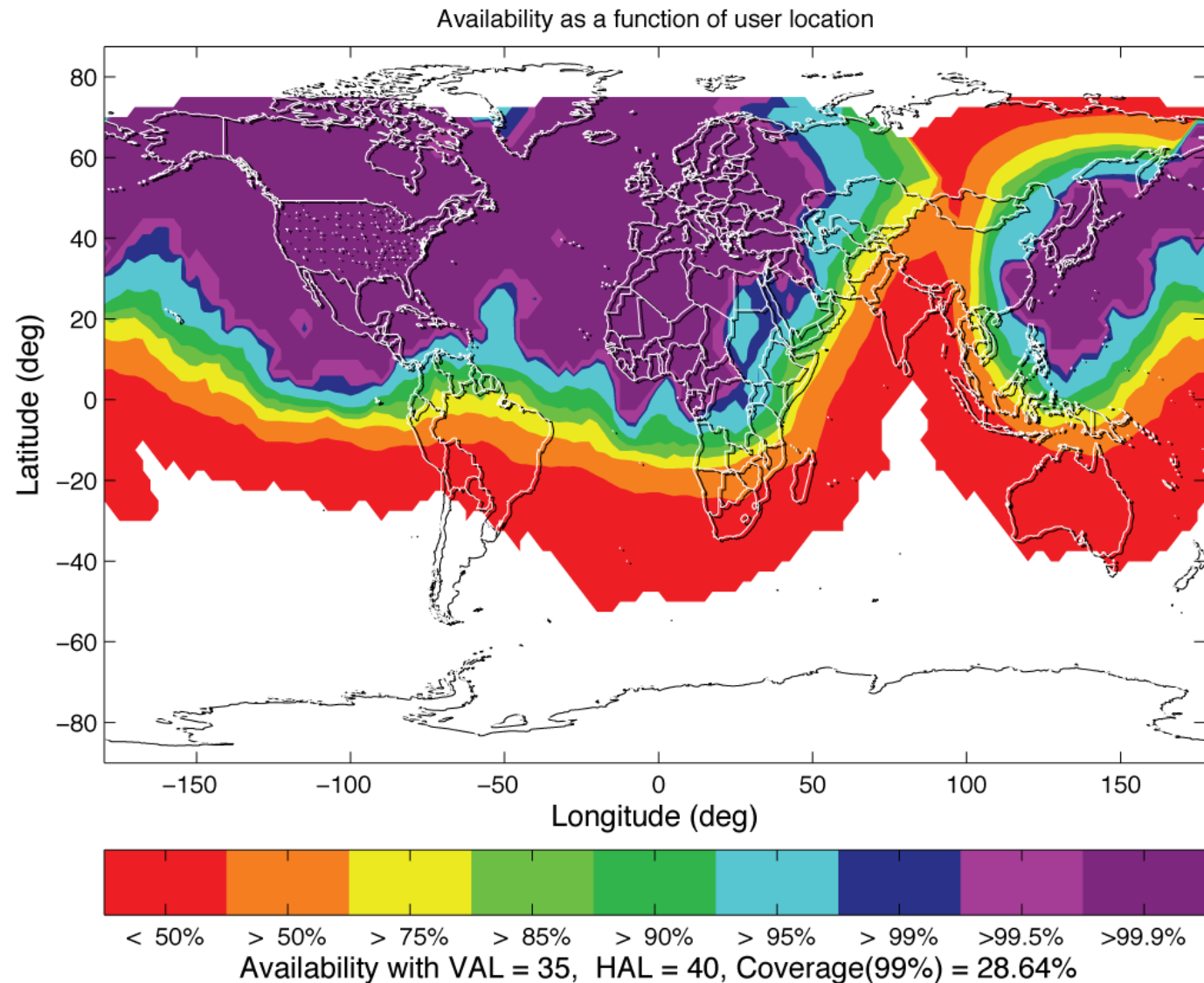




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# Dual Frequency Coverage (WAAS, EGNOS, MSAS)

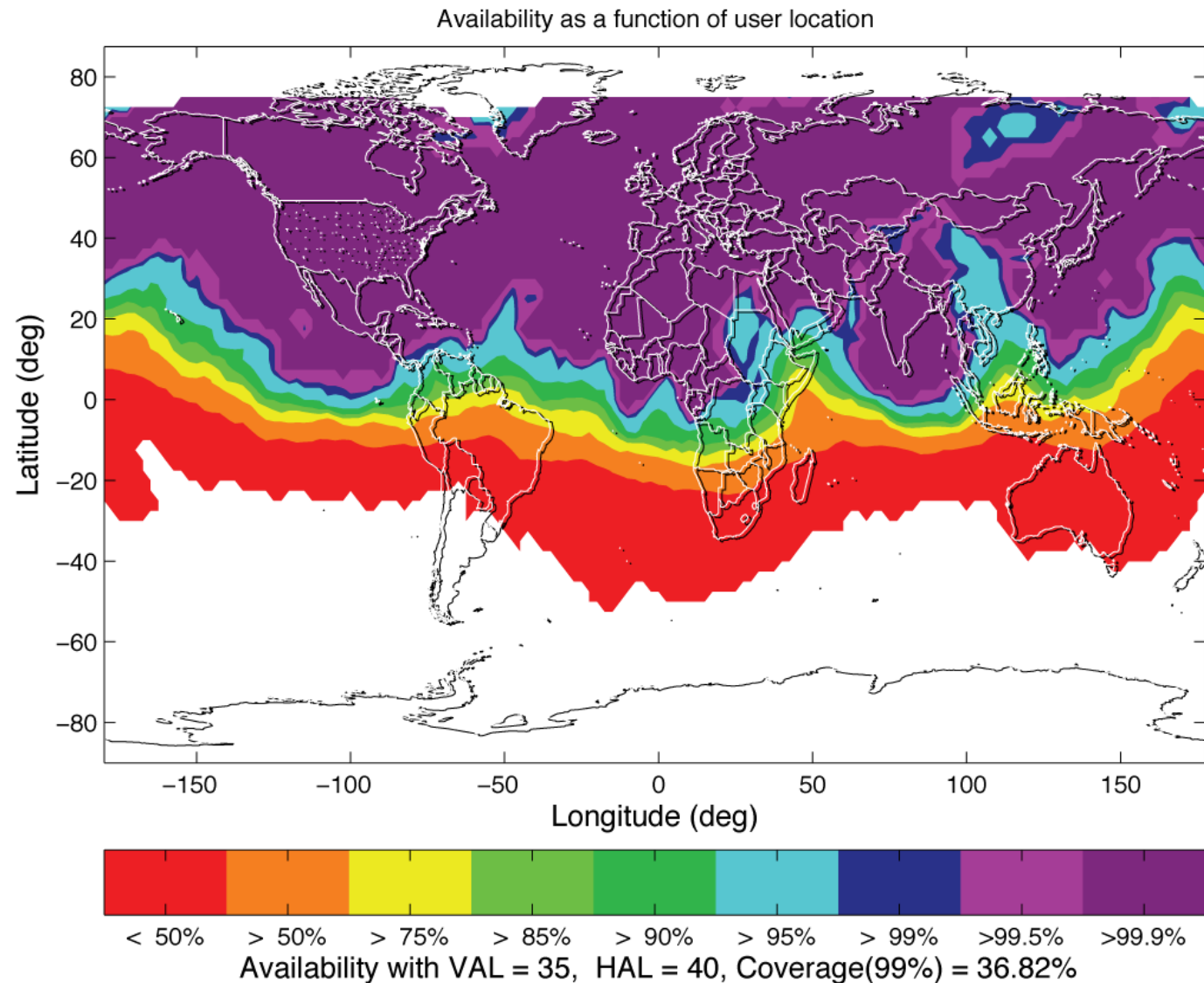




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EGNOS  
MSAS  
GAGAN  
SDCM

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# Dual Frequency Coverage (with GAGAN + Russia)

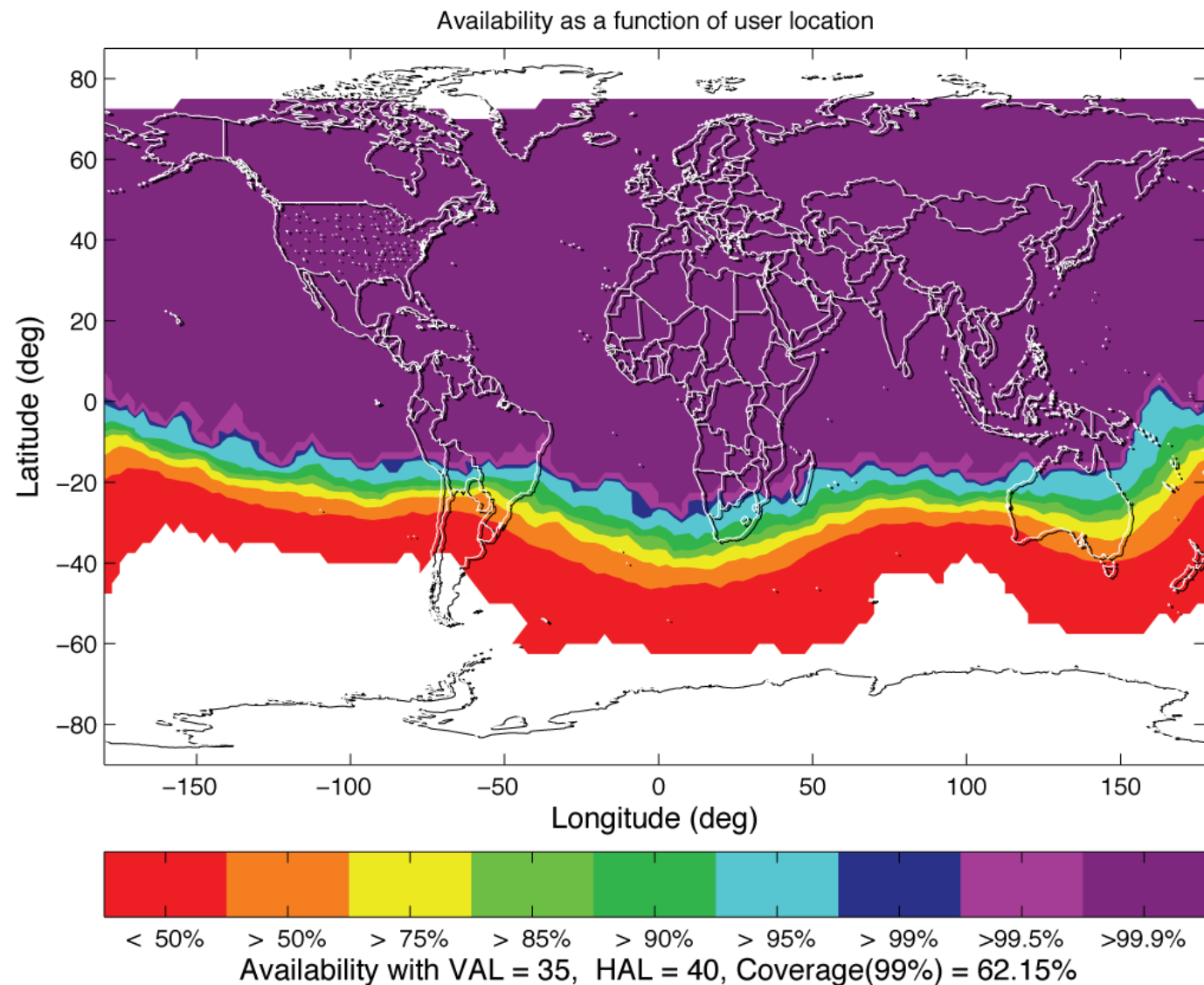




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# Dual Frequency + Second Constellation (Galileo)



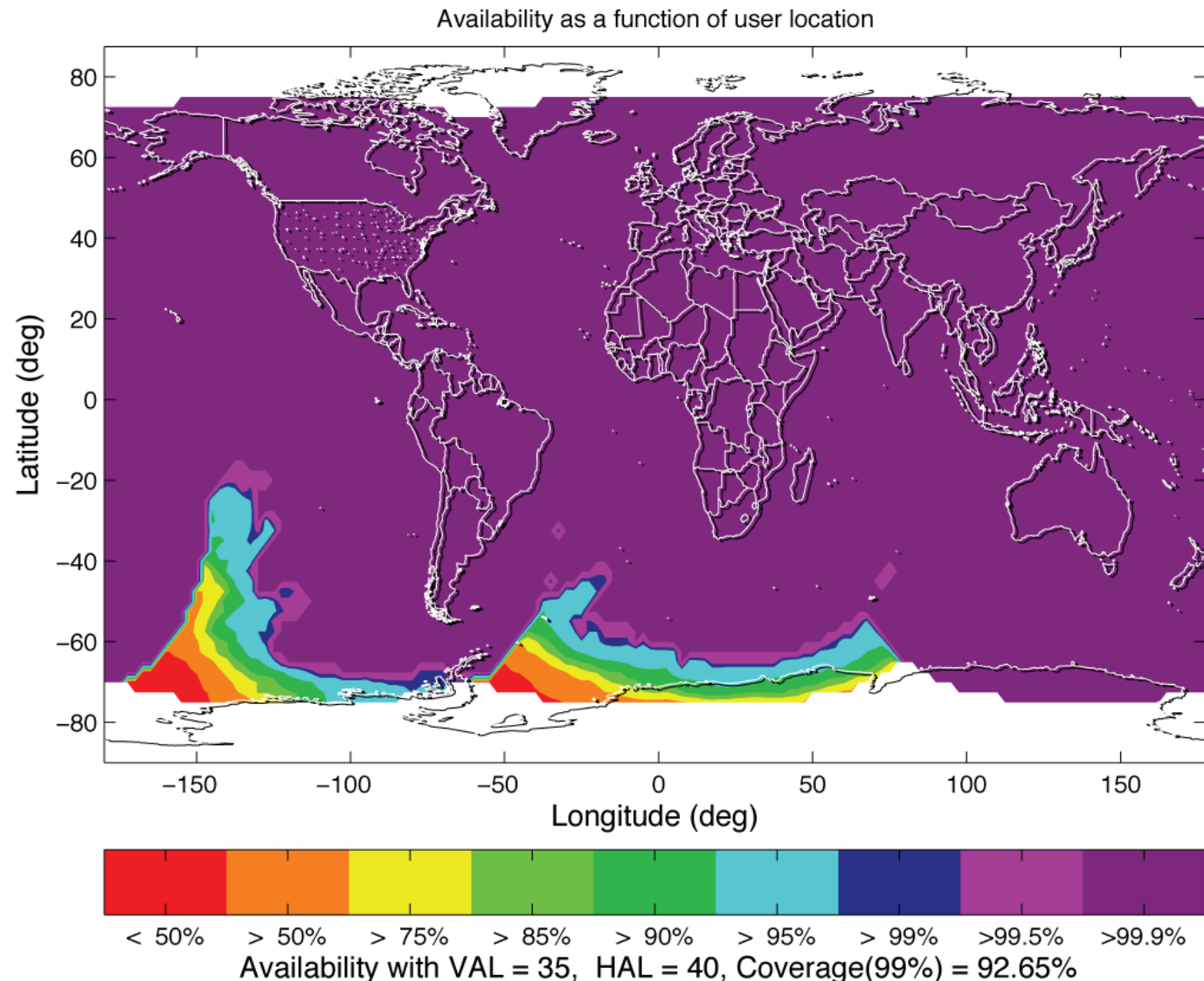




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# Dual Frequency, Dual GNSS, Expanded Networks







# Conclusions

- ➔ GNSS can be used to provide aircraft navigation for all levels of service
- ➔ Integrity is a key concern
  - ➔ *Important to understand what can go wrong and how to protect users*
- ➔ Observation and data collection are key to understanding behavior
  - ➔ *A long history of careful and consistent data monitoring are required*
  - ➔ *Practical experience leads to trust and acceptance*