

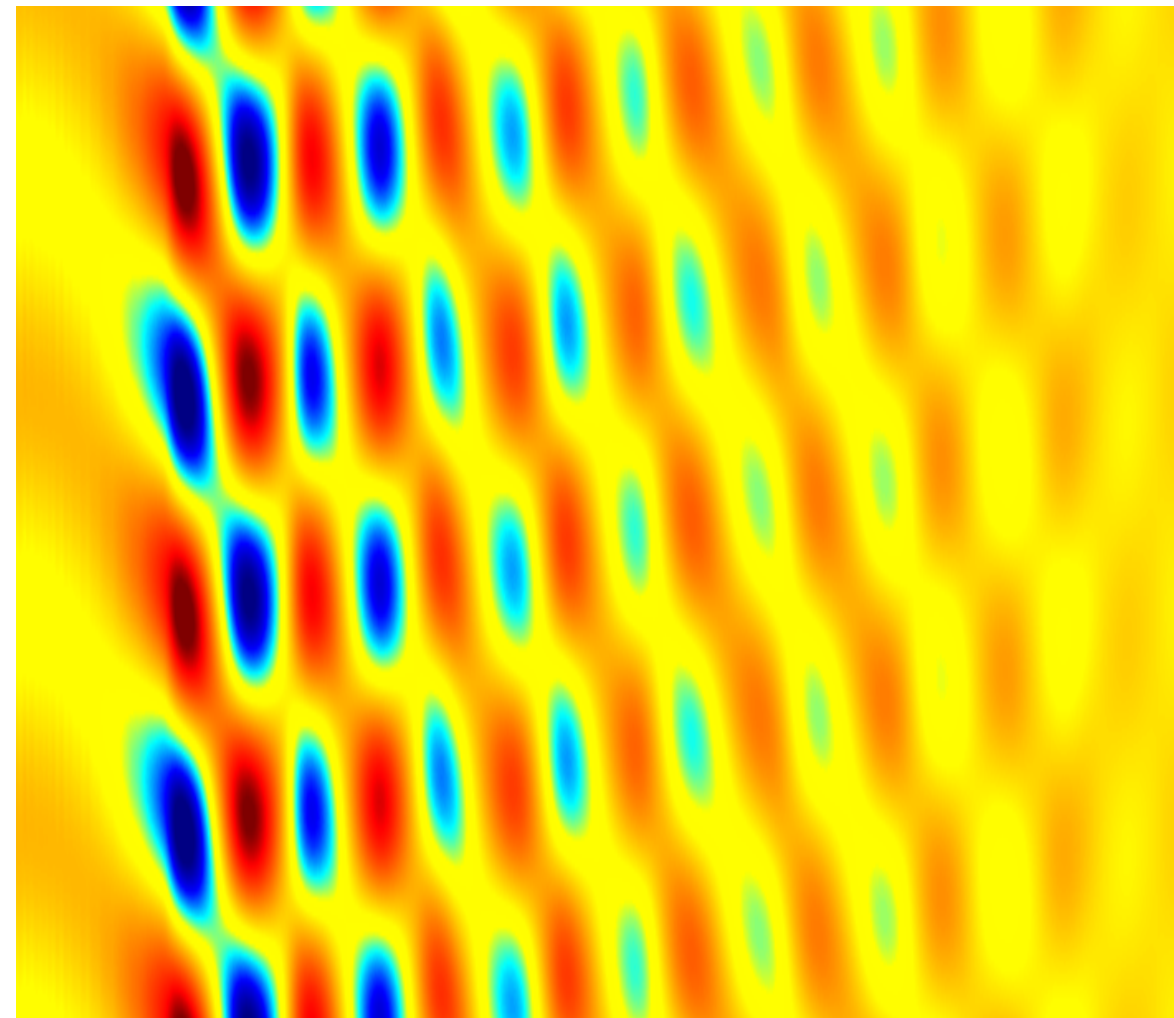


Measurement of *stimulated* **Hawking** emission in an analogue system

Phys. Rev. Lett. 106, 021302 (2011)



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- ⊠ **Matt Penrice**
- ⊠ **Ted Tedford**
- ⊠ **Bill Unruh**
- Silke Weinfurtnr**



Semi-classical gravity ➤ (Q)FT in curved spaces

Gravitational field is classical and **back-reaction** of the quantum processes onto the classical gravitational field are **negligible**.

Simple example:

(i) waves propagating on **flat** spacetime (massless minimally coupled Klein-Gordon scalar field):

$$\frac{1}{c^2} \frac{\partial^2}{\partial t^2} \psi = \nabla^2 \psi \quad \text{equivalently to} \quad \partial_a (\sqrt{-\eta} \eta^{ab} \partial_b \psi) = 0 \quad \text{where} \quad \eta_{ab} = \begin{bmatrix} -c^2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

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(ii) “minimal substitution” **curved** spacetime :

$$\partial_a (\sqrt{-g} g^{ab} \partial_b \psi) = 0 \quad \text{where} \quad g_{ab} = \begin{bmatrix} g_{00}(\mathbf{x}, t) & g_{01}(\mathbf{x}, t) & g_{02}(\mathbf{x}, t) & g_{03}(\mathbf{x}, t) \\ g_{01}(\mathbf{x}, t) & g_{11}(\mathbf{x}, t) & g_{12}(\mathbf{x}, t) & g_{13}(\mathbf{x}, t) \\ g_{02}(\mathbf{x}, t) & g_{12}(\mathbf{x}, t) & g_{22}(\mathbf{x}, t) & g_{23}(\mathbf{x}, t) \\ g_{03}(\mathbf{x}, t) & g_{13}(\mathbf{x}, t) & g_{23}(\mathbf{x}, t) & g_{33}(\mathbf{x}, t) \end{bmatrix}$$

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(iii) quantized Klein-Gordon scalar on generally curved-spacetime:

$$\partial_a (\sqrt{-g} g^{ab} \partial_b \hat{\psi}) = 0 \quad \text{where} \quad G_{ab}(g_{ab}, \Lambda) \neq 8\pi G_N \langle \hat{T}_{ab} \rangle$$

QFT in CS ➤ Analogue/Effective Gravity

Analogue gravity systems:

The equations of motion for linear perturbations in an analogue/effective/emergent gravity system can be simplified to

$$\frac{1}{\sqrt{-g}} \partial_a (\sqrt{-g} g^{ab} \partial_b \psi) = 0$$

defining an effective/acoustic/emergent metric tensor:

$$g_{ab} \propto \begin{bmatrix} -(c^2(\mathbf{x}, t) - v^2(\mathbf{x}, t)) & -\vec{v}^T(\mathbf{x}, t) \\ -\vec{v}(\mathbf{x}, t) & \mathbf{I}_{d \times d} \end{bmatrix}$$

Where do we expect such a behavior?

Broad class of systems with various dynamical equations, e.g. electromagnetic waveguide, fluids, ultra-cold gas of Bosons and Fermions.

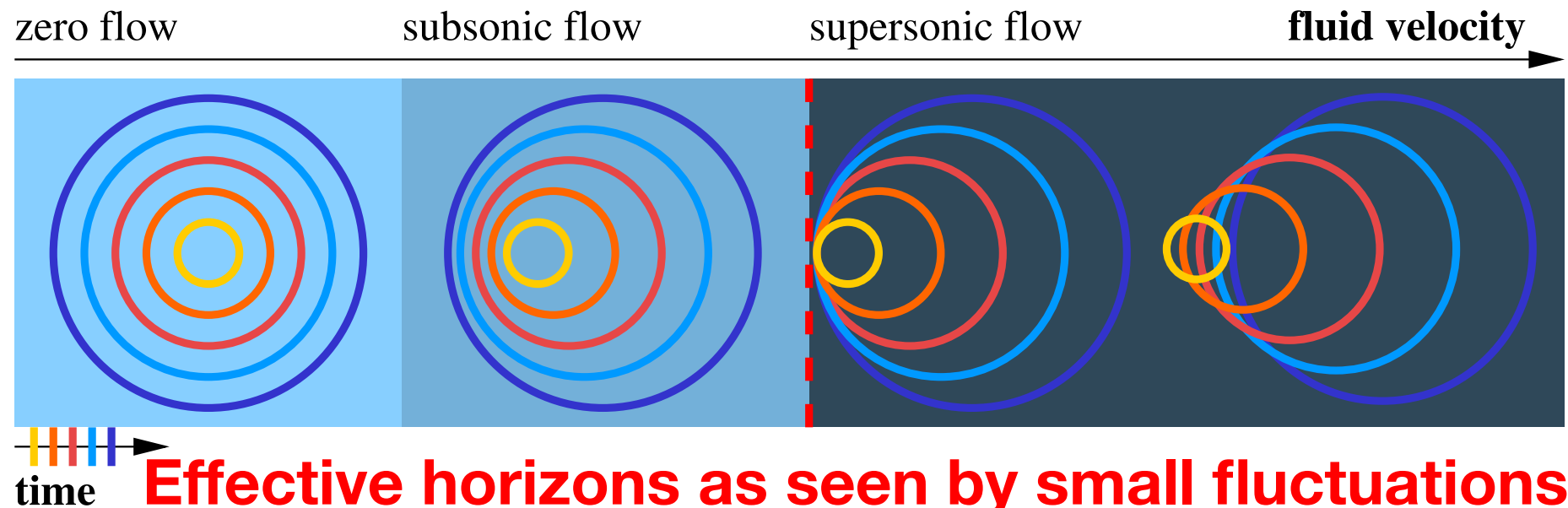
In example below: Fluid dynamics derived from conservation laws:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0 \quad \text{Continuity equation}$$

$$\rho \frac{D\mathbf{v}}{Dt} = -\nabla p \quad \text{Euler equation}$$

Simple example:

Small fluctuations in **inviscid, irrotational, incompressible** fluid flow



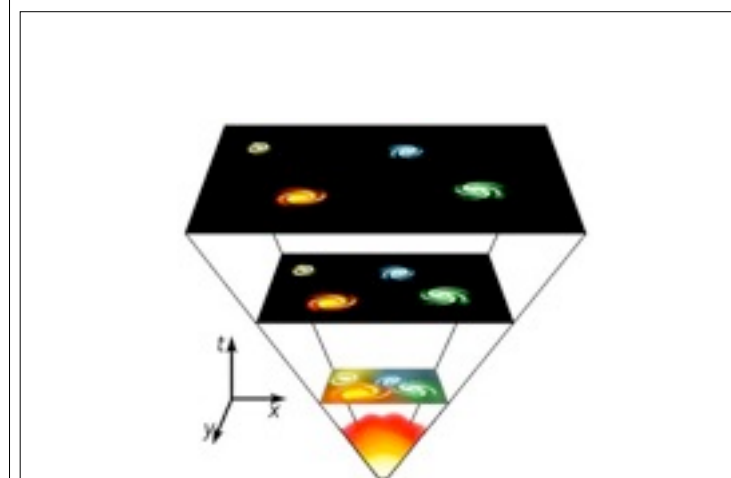
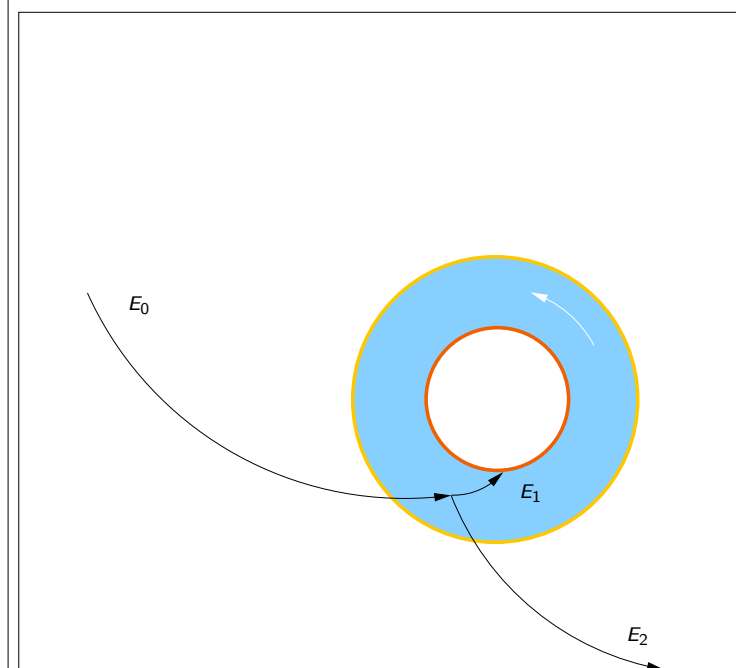
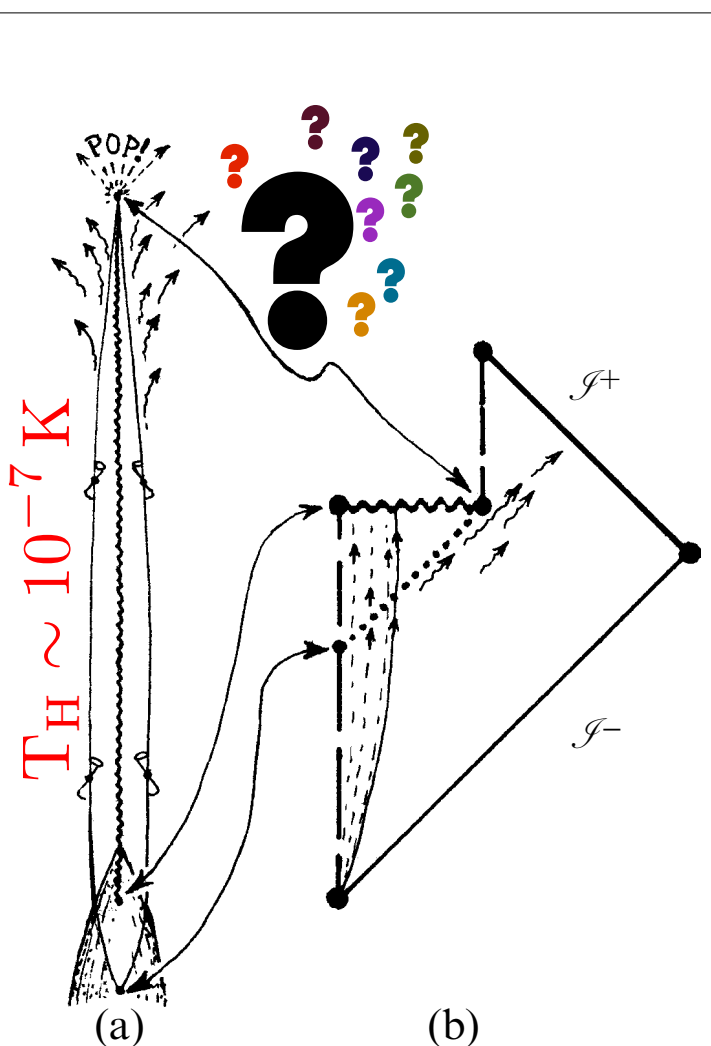
Analogue Gravity ➤ Applications

Let us first put aside the issue of classical versus quantum field theory in curved spacetimes...

1981: **Experimental black hole evaporation?**
W.G. Unruh

Possibility for experimental verification of the generality (UV-independence) of effects predicted within quantum field theory in curved spacetimes!

Analogy Gravity: Strong model dependent deviations and eventual break-down at 'small' scales expected!



Example 1:

Experimental Black Hole Evaporation

Example 2:

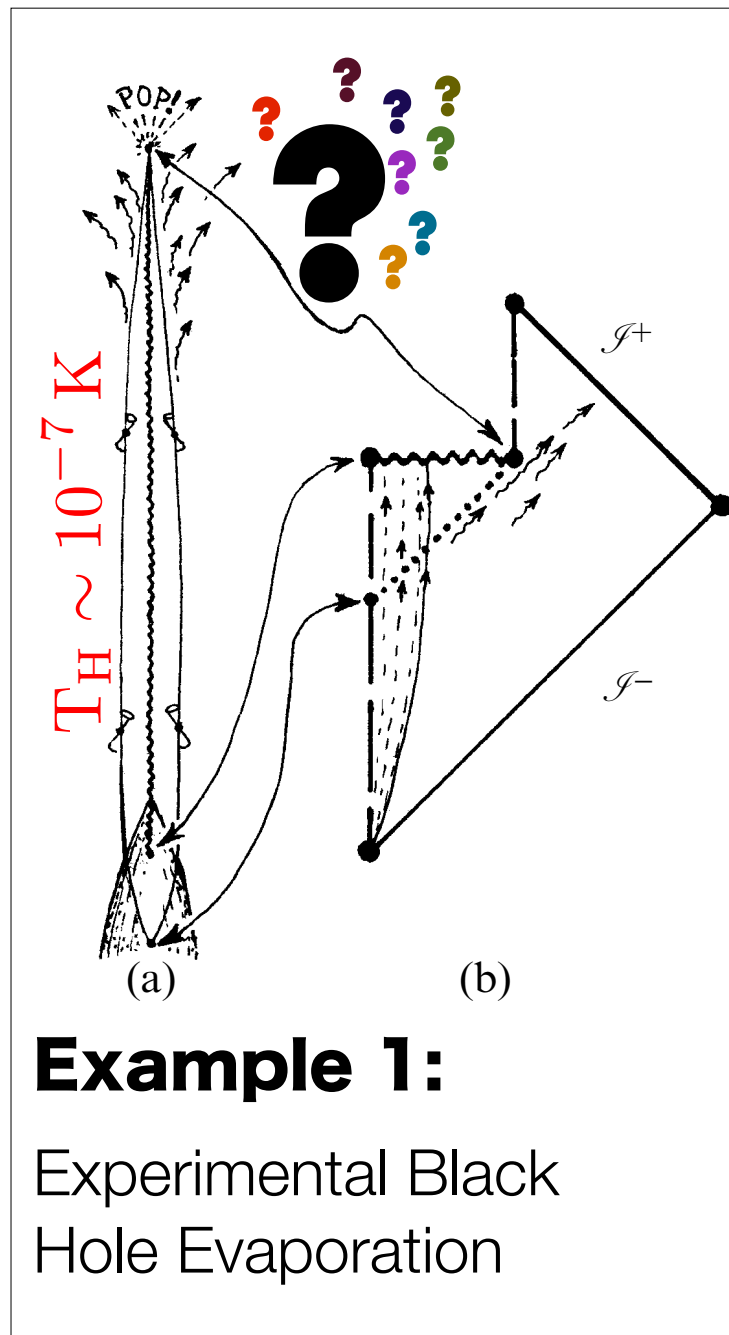
Superradiant scattering from rotating black holes

Example 3:

Cosmological particle production

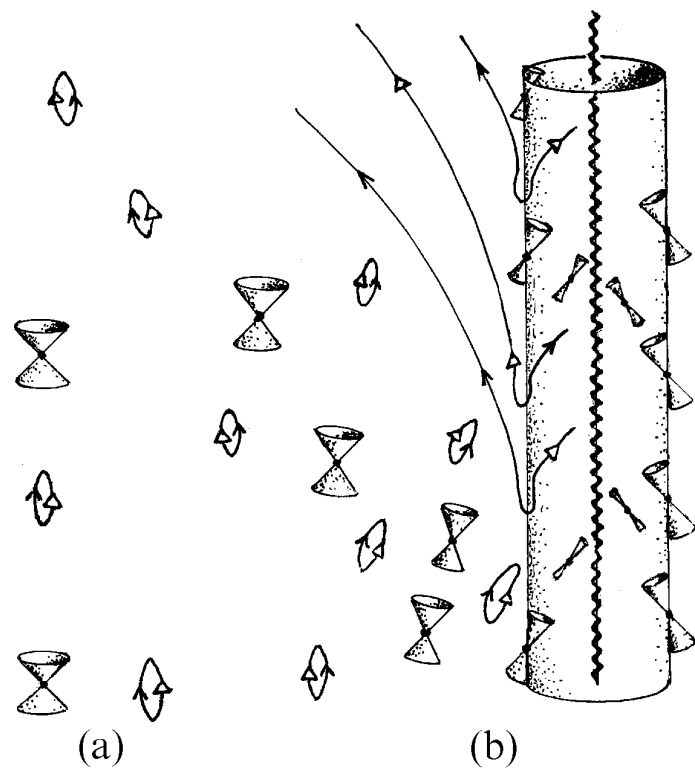
Experimental Black Hole Evaporation [Example 1]

How do black holes lose their mass..?



- (1) What is Hawking radiation?
- (2) Is there a reason why we should at all doubt that black holes evaporate..?
- (3) How can we set up a table-top experiment that “conclusively” tests Hawking/Unruh’s prediction?

BHE process ➤ What is Hawking radiation?



Pair-creation:

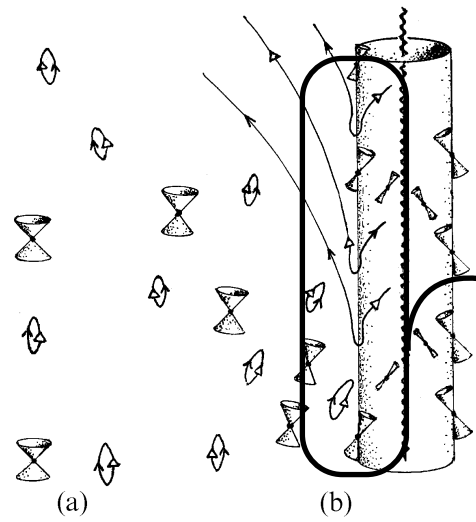
Separation of particle-anti-particle pairs from the quantum vacuum;
Negative norm modes absorbed by black hole;

[Particle Creation by Black Holes, by Stephen Hawking, in 1974]

$$\phi_{\omega}^{\text{in}} = \alpha_{+}^{\text{out}} + \beta_{-}^{\text{out}}$$

Let's try to understand Hawking radiation as a simple scattering process...

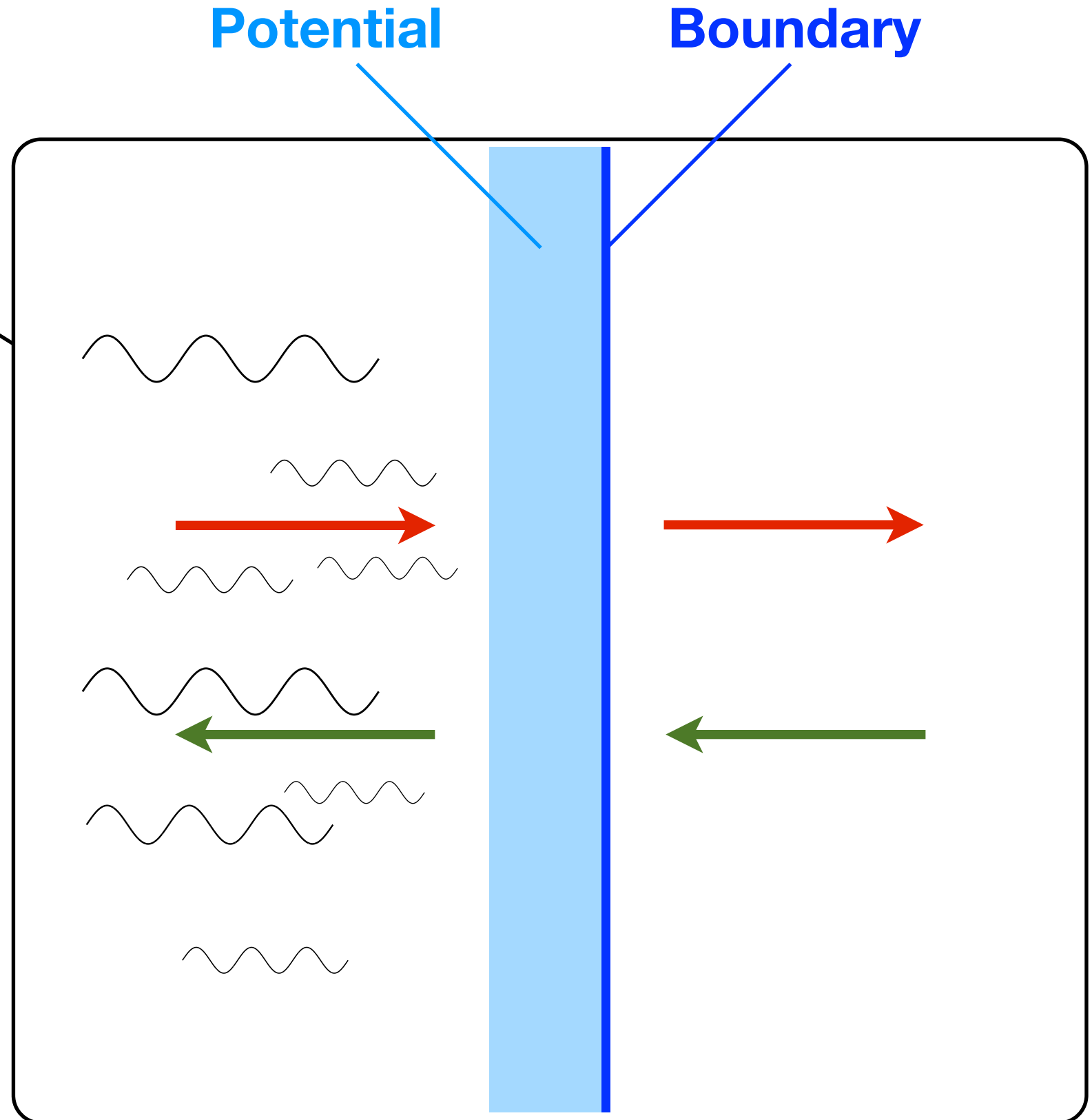
BHE process ➤ What is Hawking radiation?



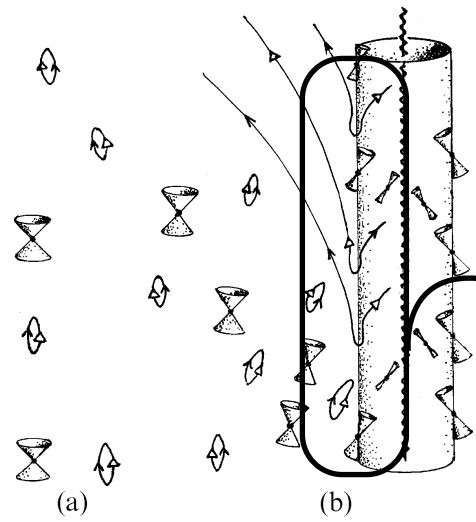
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Right moving modes

Left moving modes



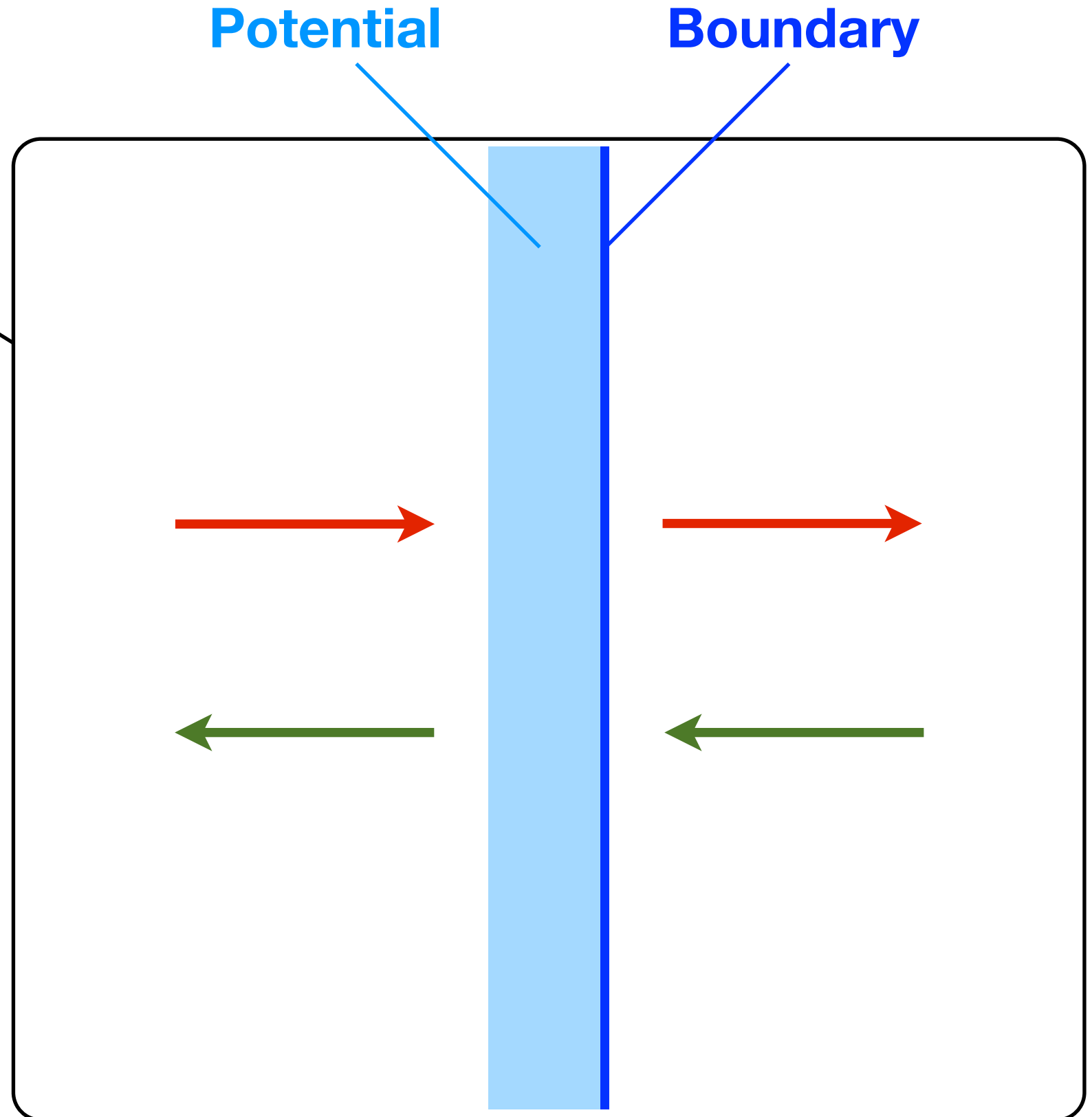
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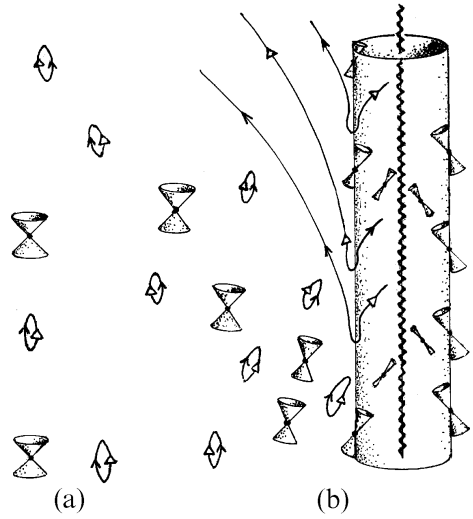
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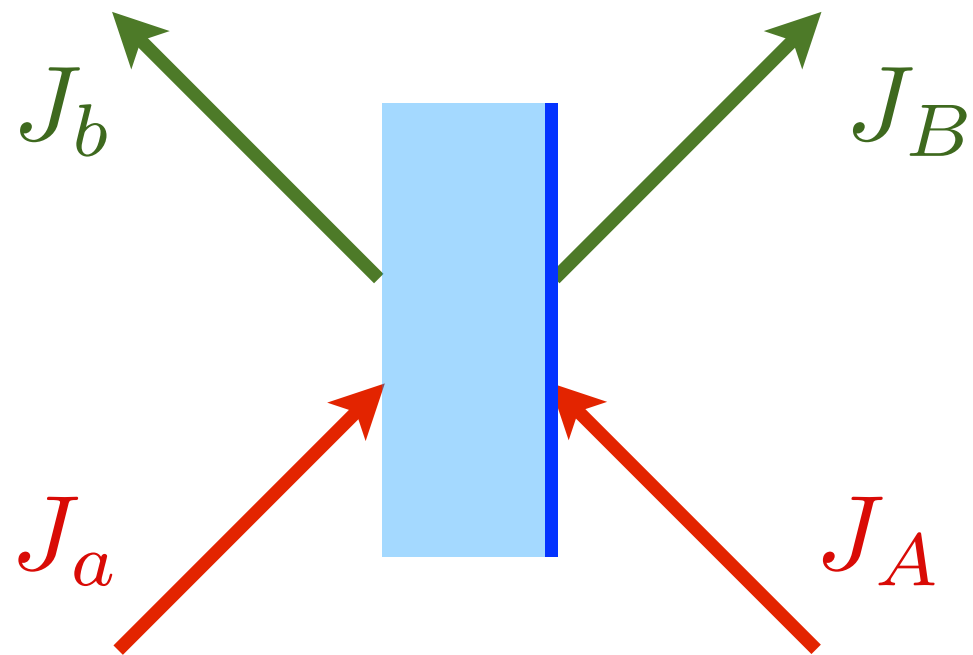
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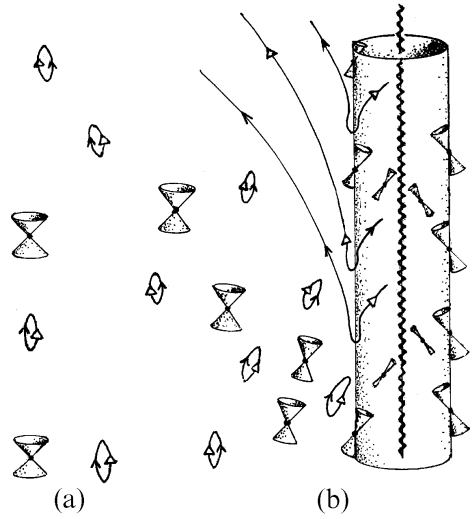
**Modes moving
into potential**

**Modes moving
out of potential**



$$J_a + J_A = J_b + J_B$$

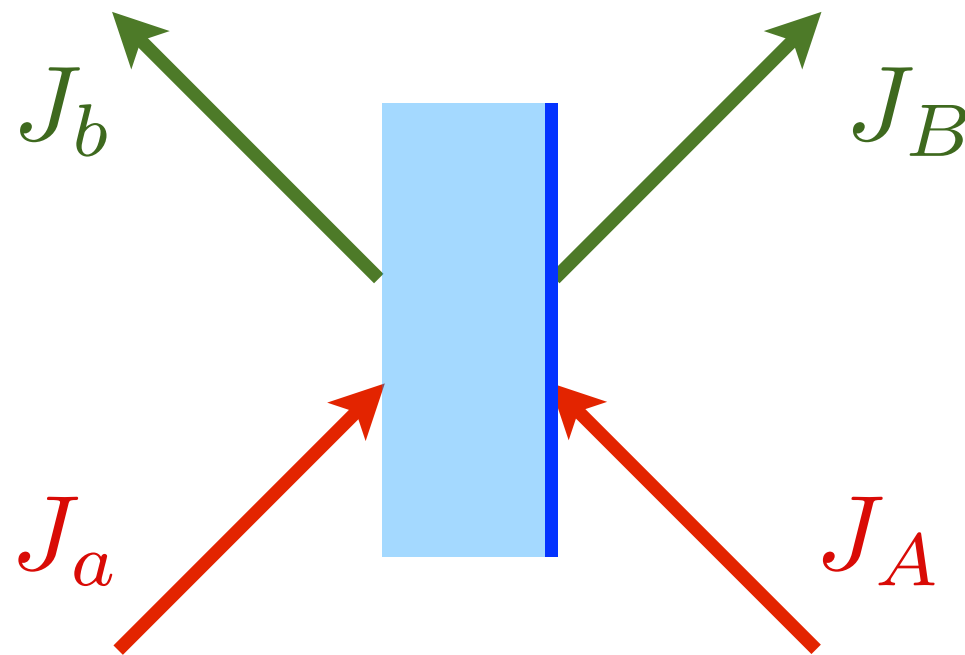
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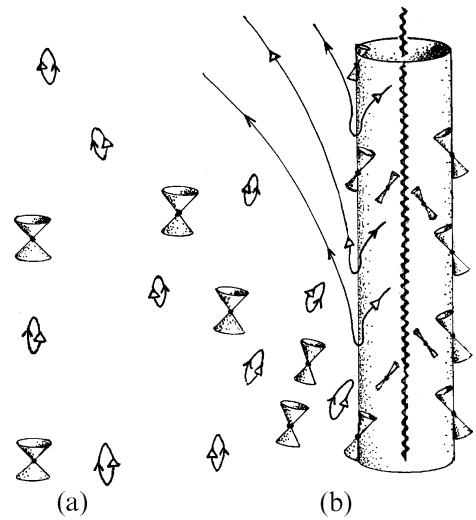
Conserved quantity: Particle current:

$$J_n := |A_n|^2 \Omega \Big|_{\pm\infty} \frac{d\omega}{dk} \Big|_{k_n}$$



$$J_a + J_A = J_b + J_B$$

BHE process ➤ What is Hawking radiation?



$$\phi_{\omega}^{\text{in}} = \alpha_{+}^{\text{out}} + \beta_{-}^{\text{out}}$$

Particle current: $J_n := |A_n|^2 \Omega|_{\pm\infty} \frac{d\omega}{dk} \Big|_{k_n}$

$$J_b \propto |\alpha_{\omega}|^2$$

$$J_B \propto -|\beta_{\omega}|^2$$

$$J_a \propto 1$$

$$J_A$$

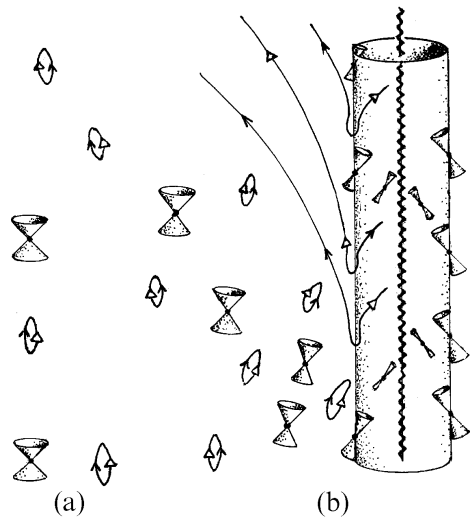
$$\frac{|\beta_{\omega}|^2}{|\alpha_{\omega}|^2} = e^{-\frac{2\pi\omega}{g_H}} = e^{-\frac{\hbar\omega}{k_B T}}$$

$$|\alpha_{\omega}|^2 - |\beta_{\omega}|^2 = 1$$

$$1 + 0 = |\alpha_{\omega}|^2 + -|\beta_{\omega}|^2$$

Black holes: Linear Classical and Quantum Field Amplifier!

BHE process ➤ What is Hawking radiation?



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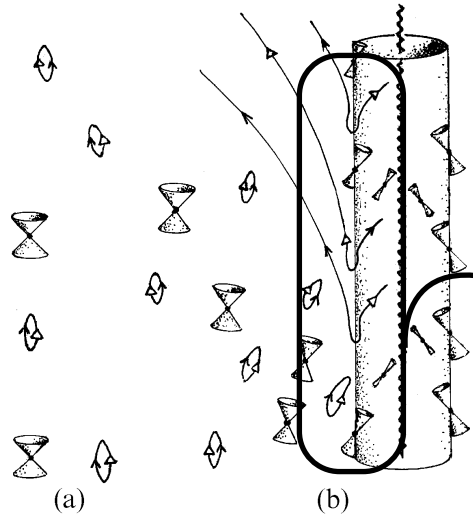
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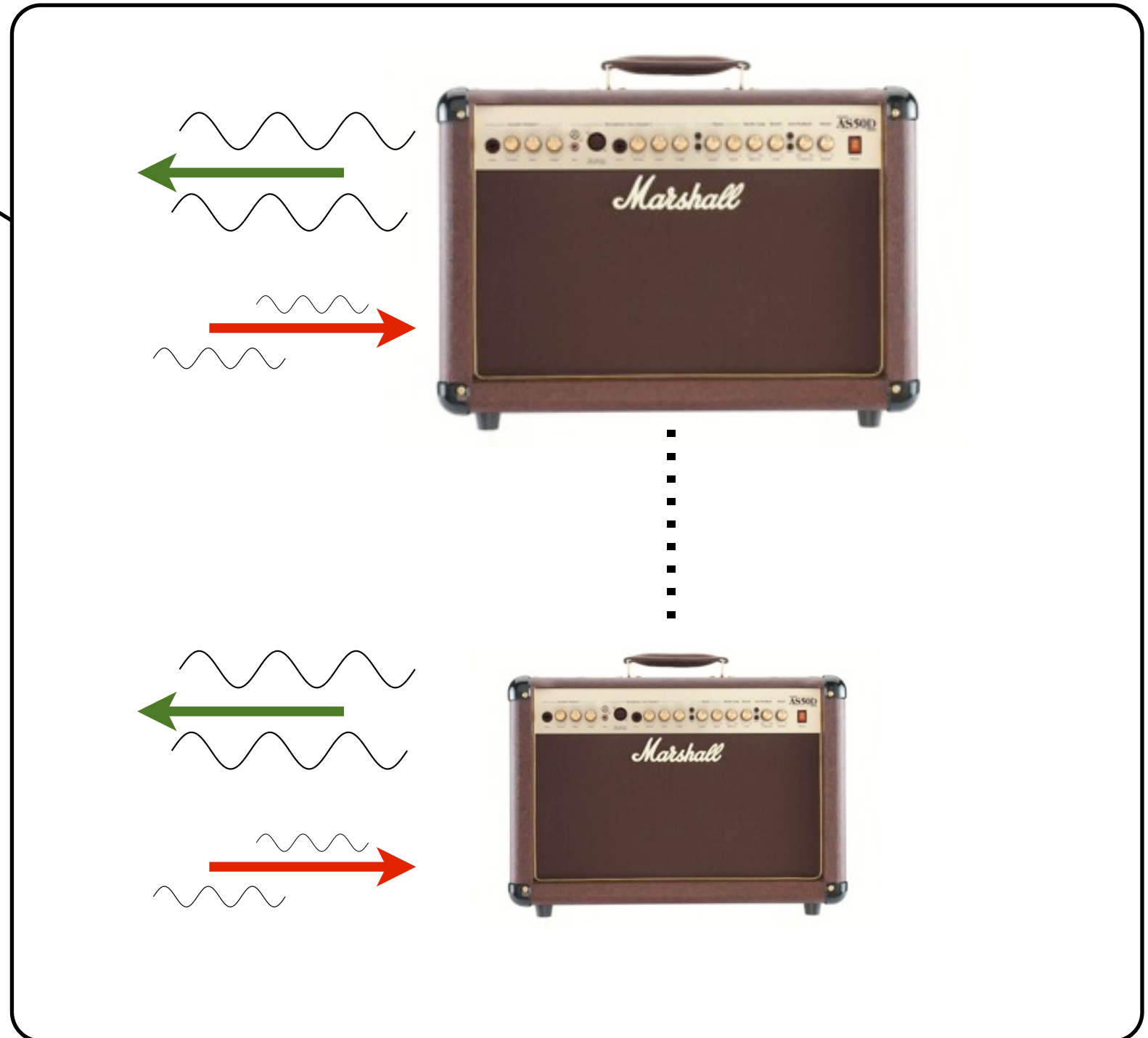
BHE process ➤ What is Hawking radiation?



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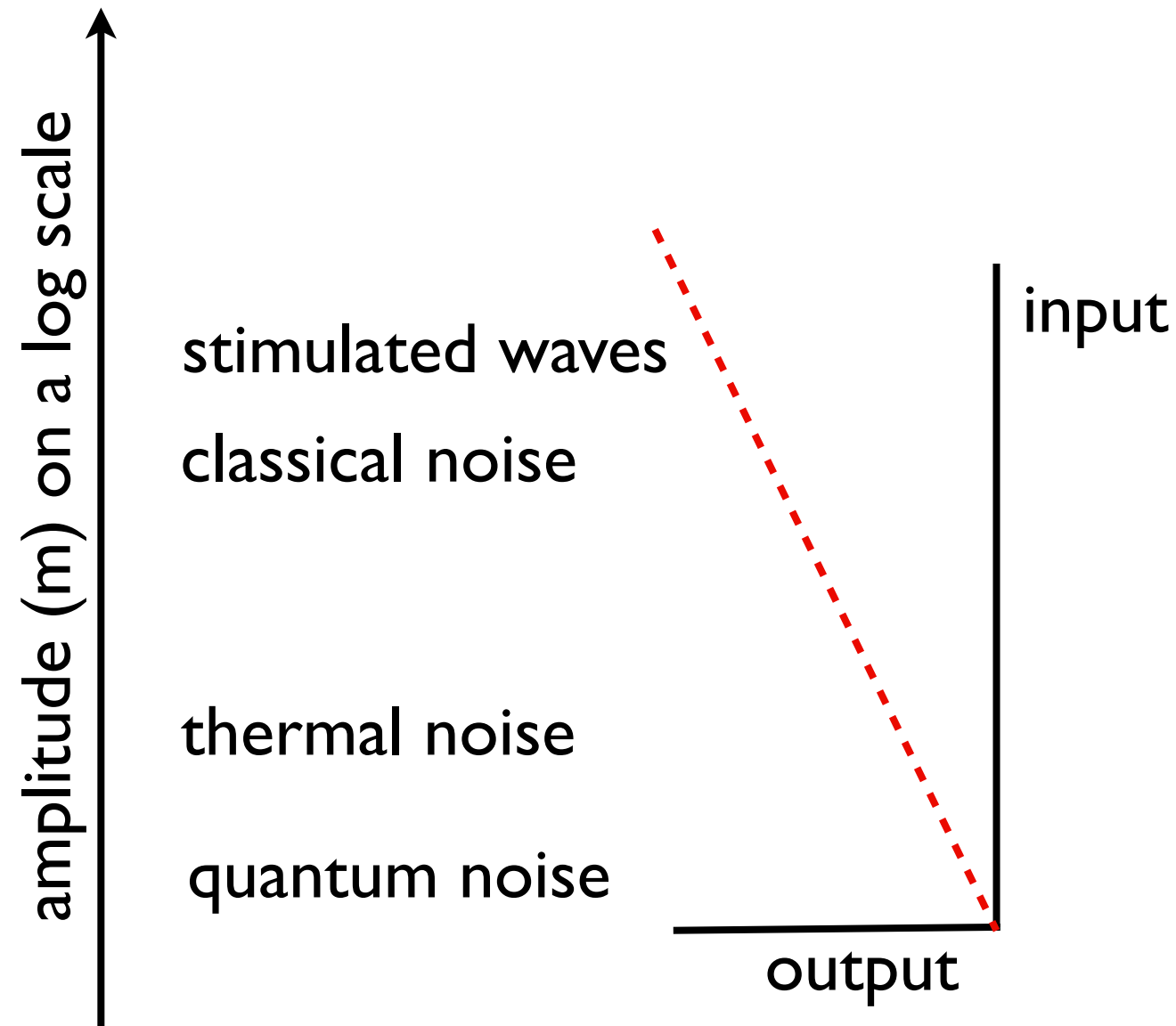
$$\frac{|\beta_{\omega}|^2}{|\alpha_{\omega}|^2} = e^{-\frac{2\pi\omega}{g_H}}$$

- ✓ pair-creation process
- ✓ Boltzmann distribution
- ✓ surface gravity





BHE process ➤ What is being amplified?



Assumption:

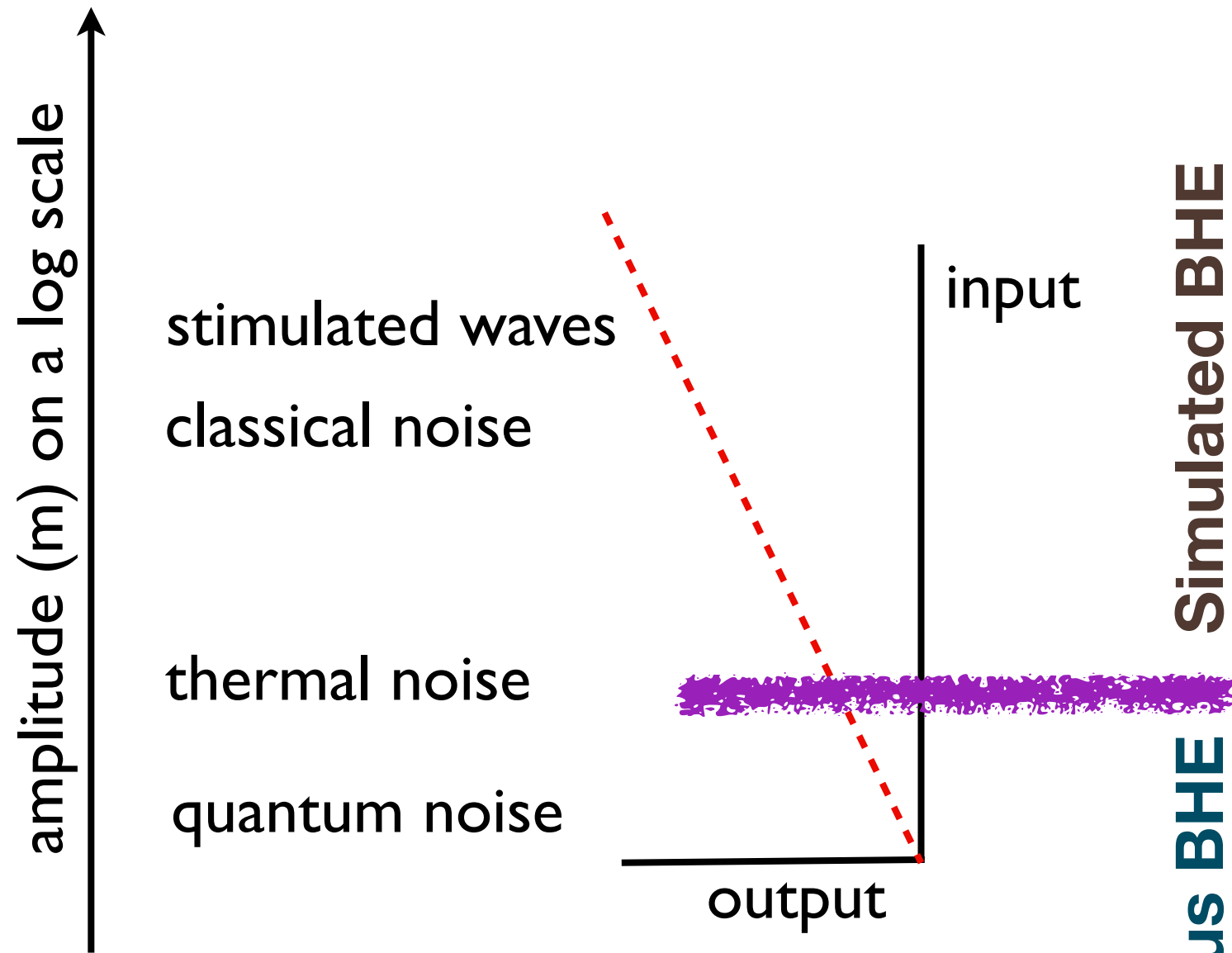
Linear amplifier over a huge range!

- ✓ pair-creation process (classical correlations)
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- ✓ surface gravity





BHE process ➤ What is being amplified?



Simulated BHE

Spontaneous BHE

Assumption:

Linear amplifier over a huge range!

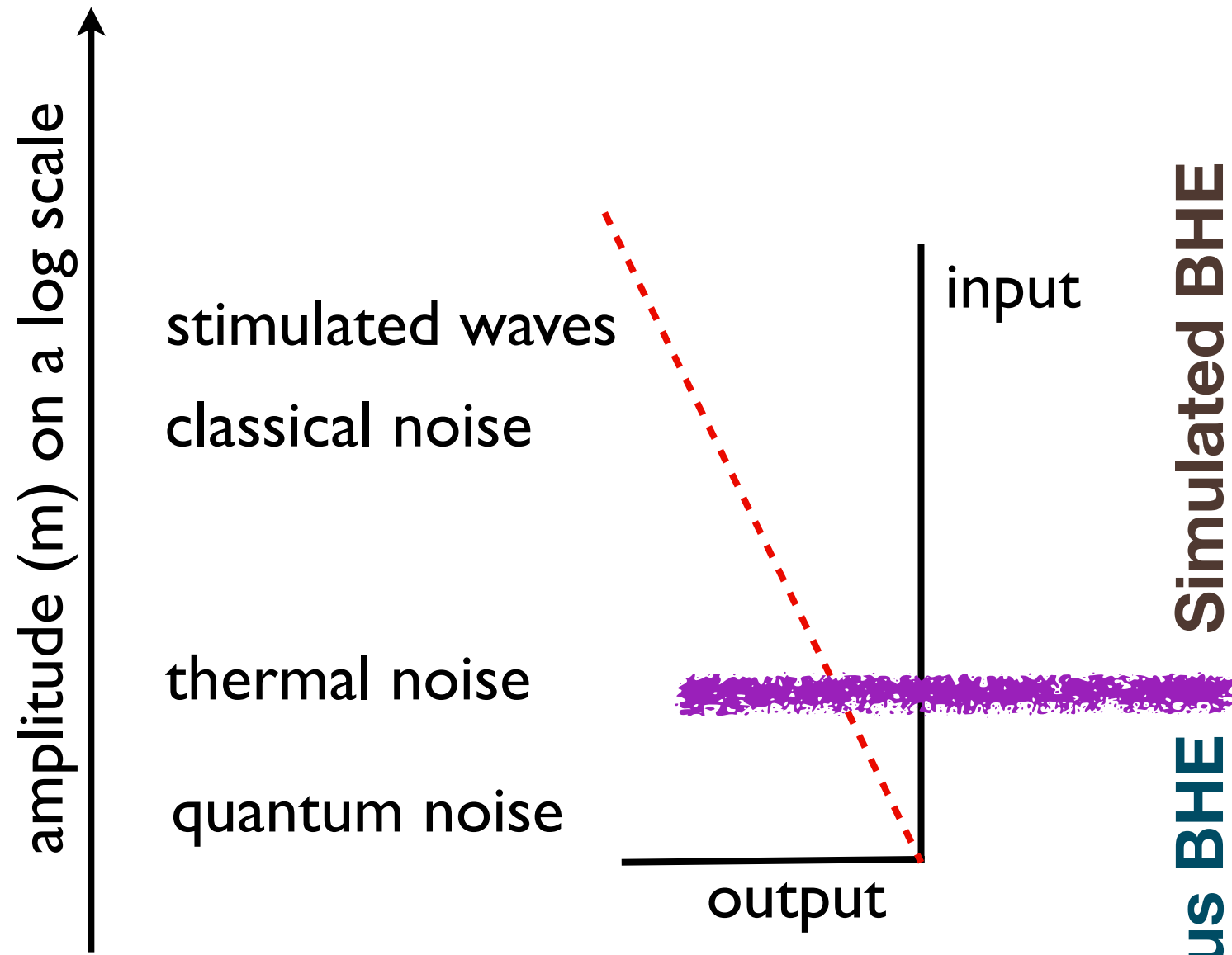
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- ✓ Boltzmann distribution
- ✓ surface gravity



- ✓ quantum correlations



BHE process ➤ What is being amplified?



Spontaneous BHE

Assumption:

Linear amplifier over a huge range!

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- ✓ Boltzmann distribution
- ✓ surface gravity



- ✓ quantum correlations

why do we care: the UV-problem

BHE process ➤ the UV-problem

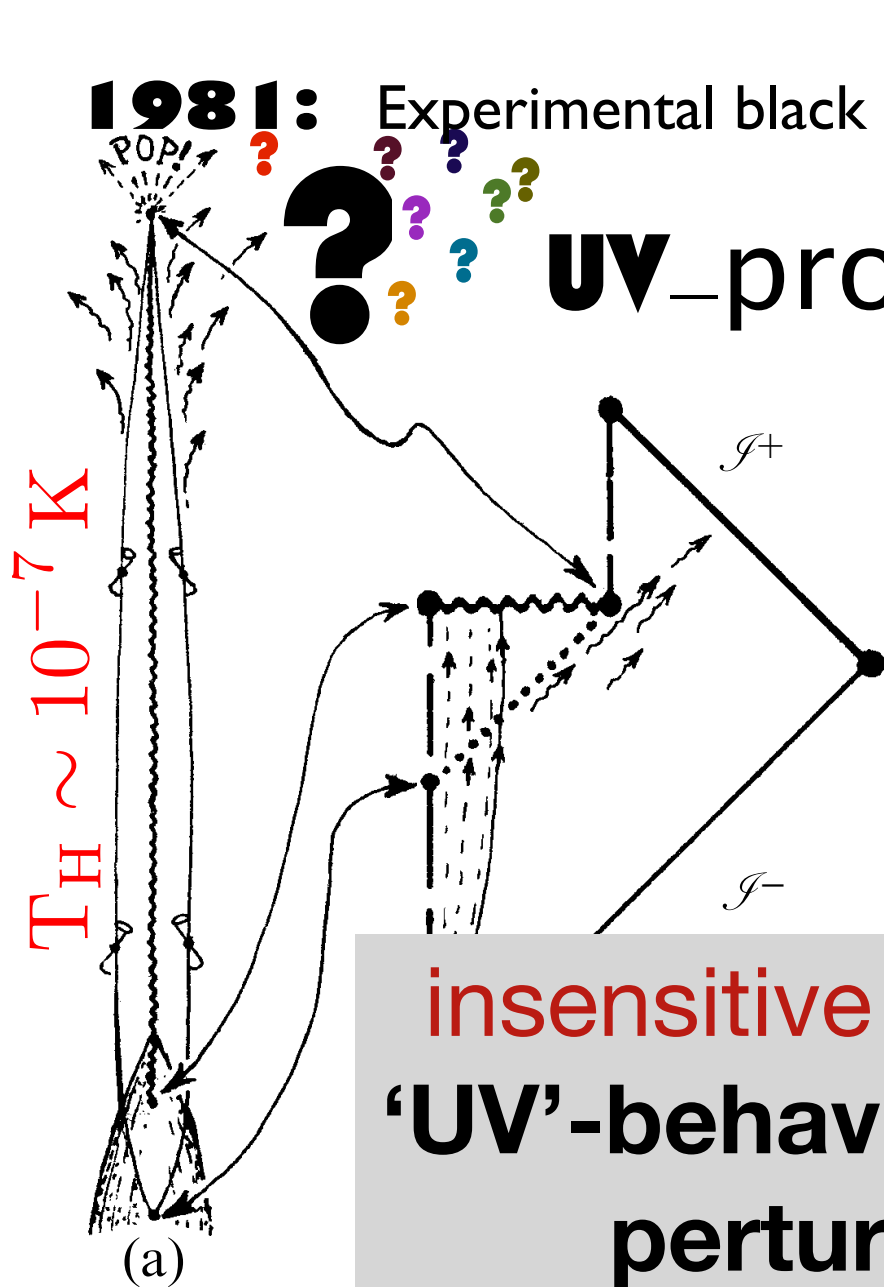
Equation of motion for **linear** perturbations in analogue gravity systems:

[Wave equation on effective curved spacetime]

$$\frac{1}{\sqrt{-g}} \partial_a \left(\sqrt{-g} g^{ab} \partial_b \phi_1 \right) = 0$$

1981: Experimental black hole evaporation **?**, by Bill Unruh; Vol 46, #21, PRL.

? **UV-problem?**



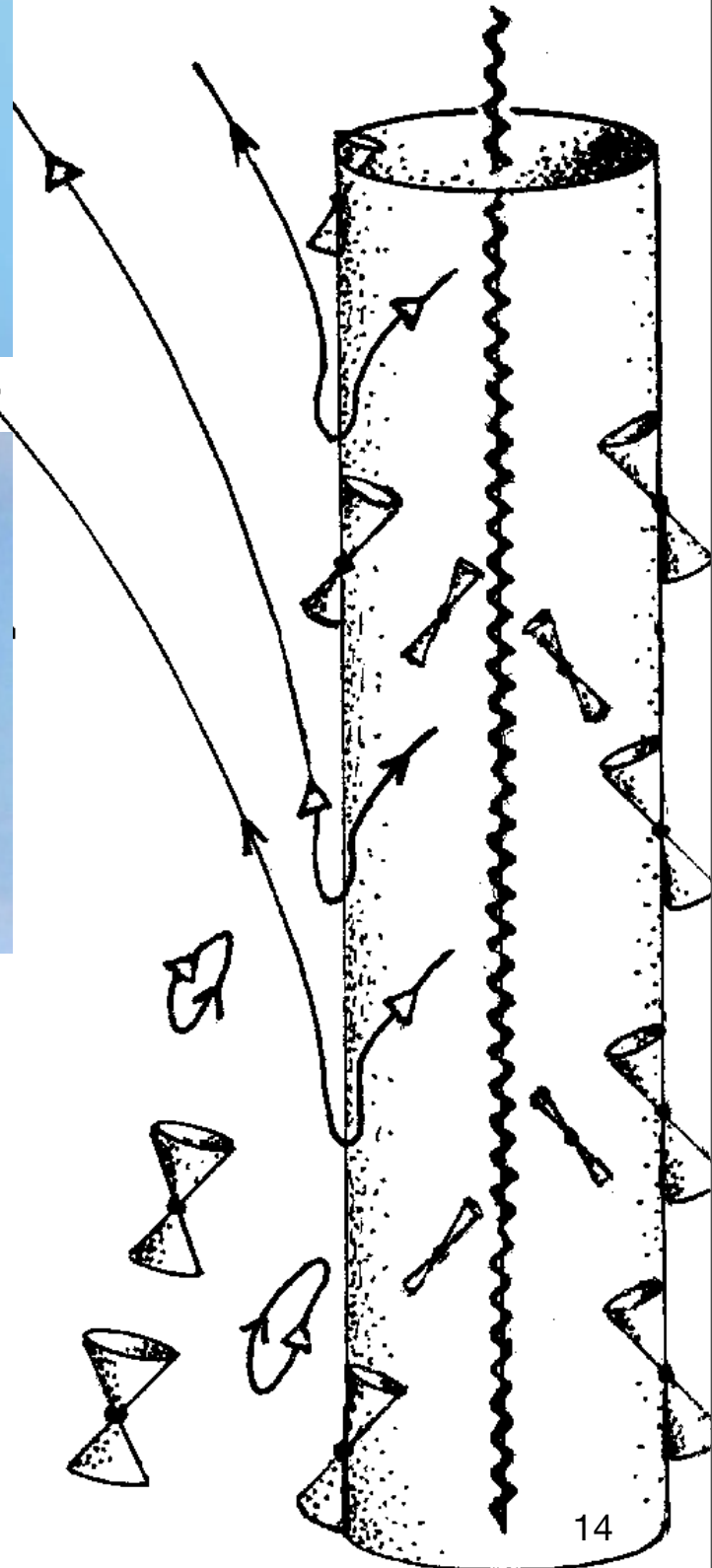
Possibility to test experimentally the **generality** of the Hawking process!

insensitive to particular 'UV'-behaviour of linear perturbations

robust against model-specific dynamics

Scientific goal ➤ conclusive detection of BHE

- Spontaneous versus stimulated emission: Black holes are phase insensitive linear amplifiers...
- Nature of Hawking process: Semi-classical quantum gravity effect, where the Einstein dynamics is not taken into consideration.
- Black versus white hole emission: White holes are the time-reversal of black holes, and the Hawking process applies to both.



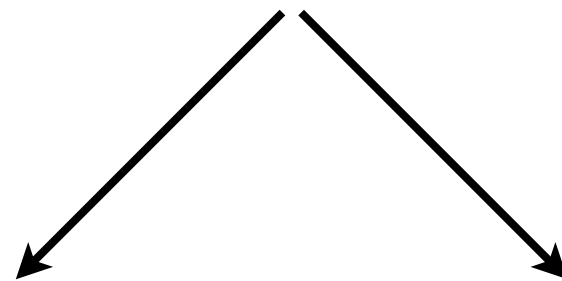
Our experiment ➤ Principle idea

2002: Schutzhold & Unruh: Gravity wave analogs of black holes (Phys. Rev. D66 044019)

Our experiment in a nutshell

Set-up: Surface waves on open channel flow with varying depth.

- stationary
- irrotational
- incompressible
- inviscid



$$v = v(x) = \frac{q}{h(x)} \propto \frac{1}{h(x)}$$

$$c = c(x) \approx \sqrt{gh(x)} \propto \sqrt{h(x)}$$

Let's recall the acoustic line-element:

$$g_{ab} \propto \begin{bmatrix} -(c^2 - v^2) & -\vec{v}^T \\ -\vec{v} & \mathbf{I}_{d \times d} \end{bmatrix}$$

Goal: Set up black and white horizon & detect stimulated conversion to pos. & neg. waves who's relative amplitudes obey HS.

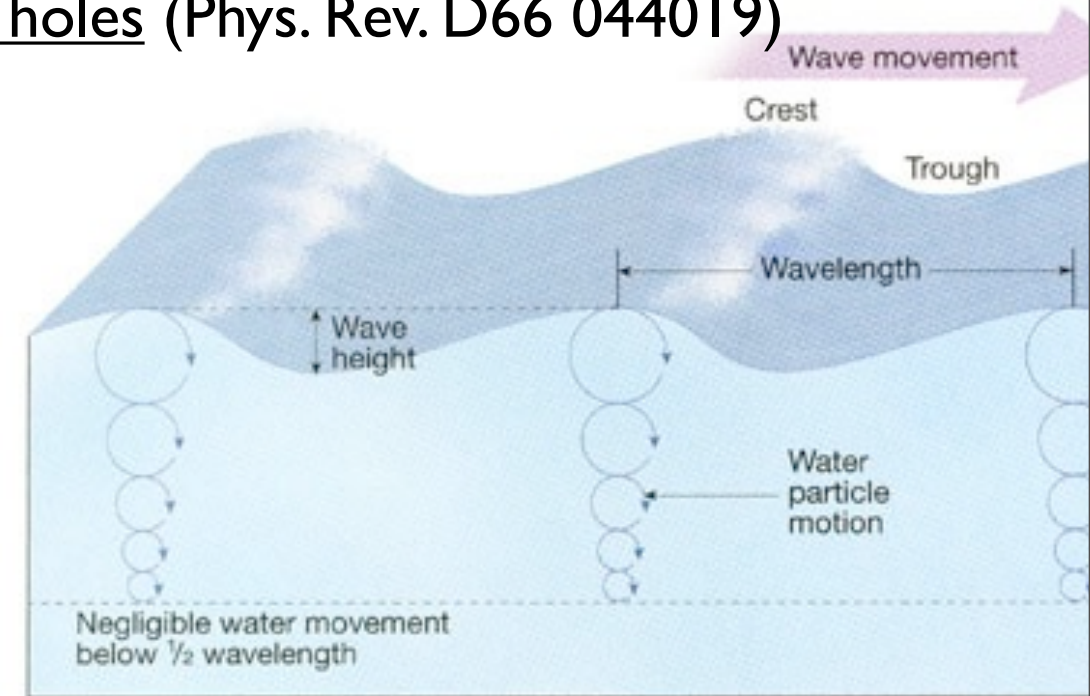
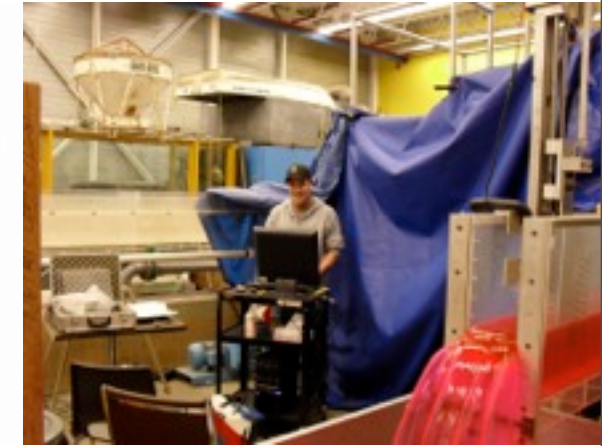
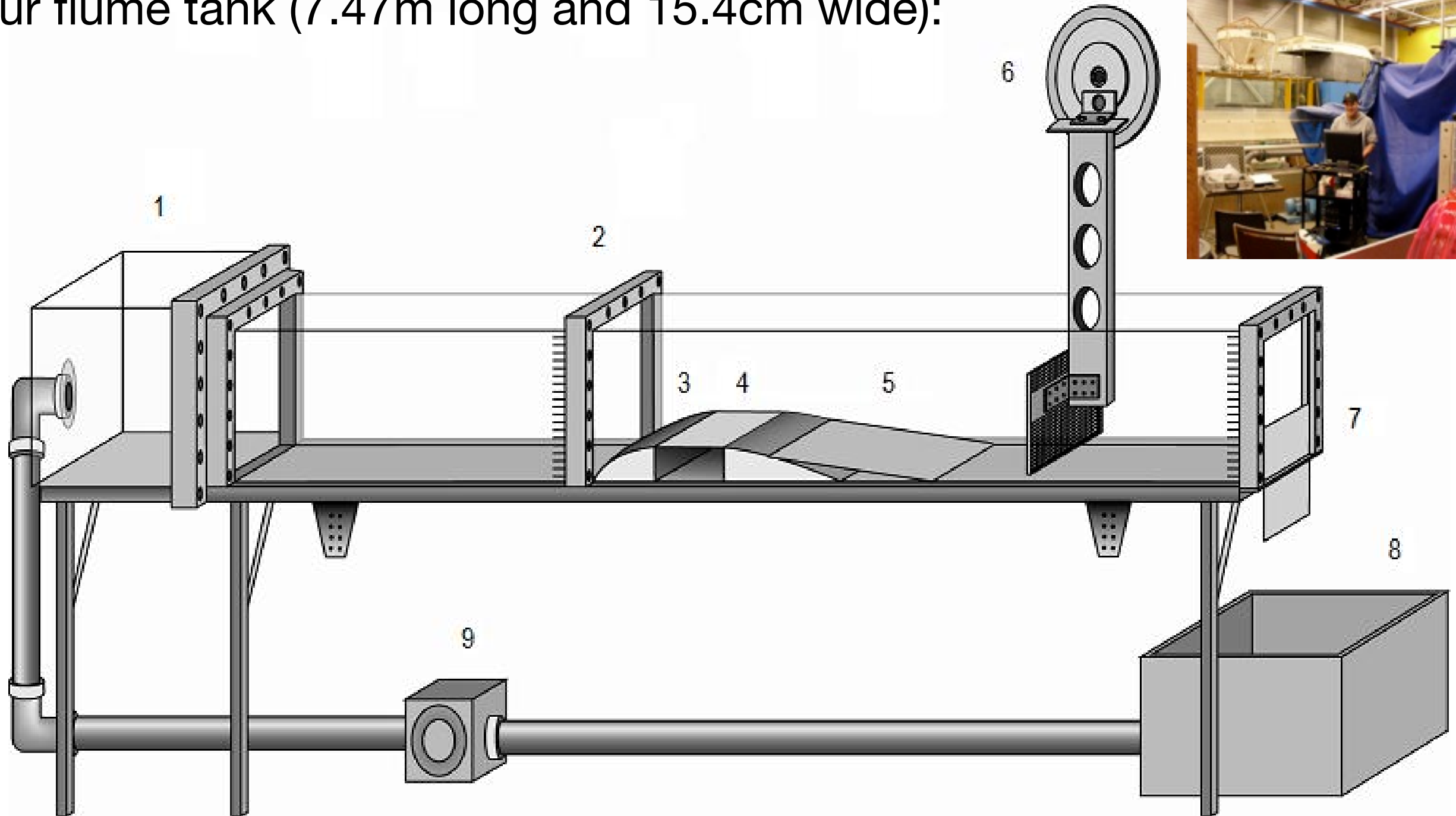


Figure 14.2 This diagram illustrates the basic parts of a wave as well as the m wave. Negligible water movement occurs below a depth equal to one-half the

Our experiment ➤ Setup

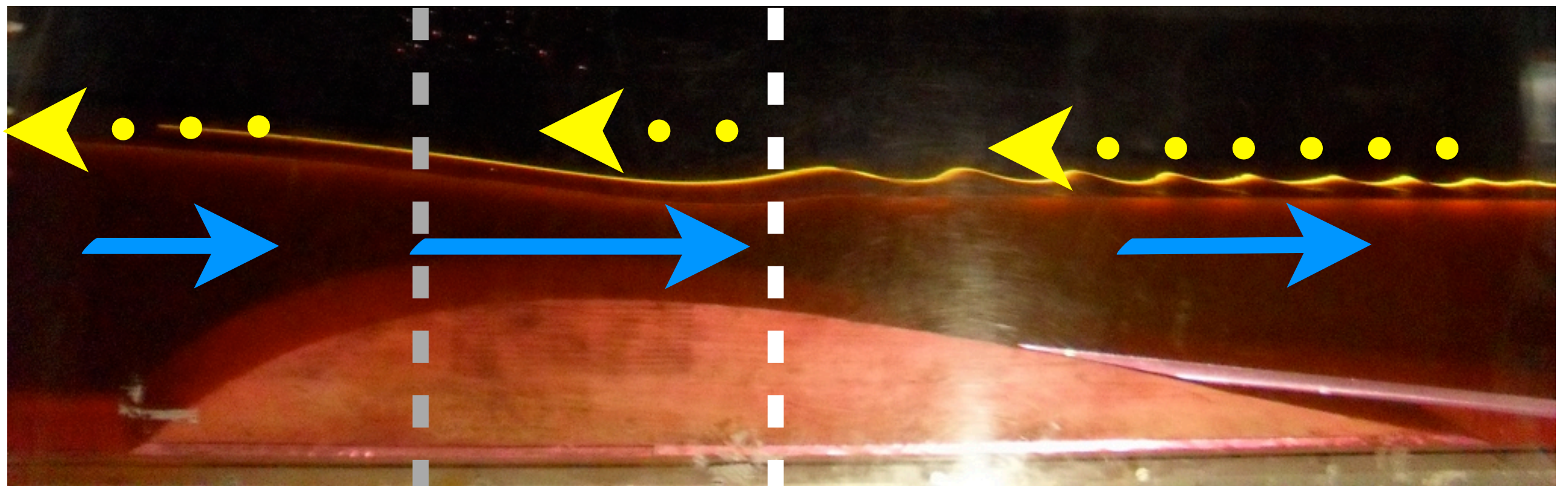


Our flume tank (7.47m long and 15.4cm wide):



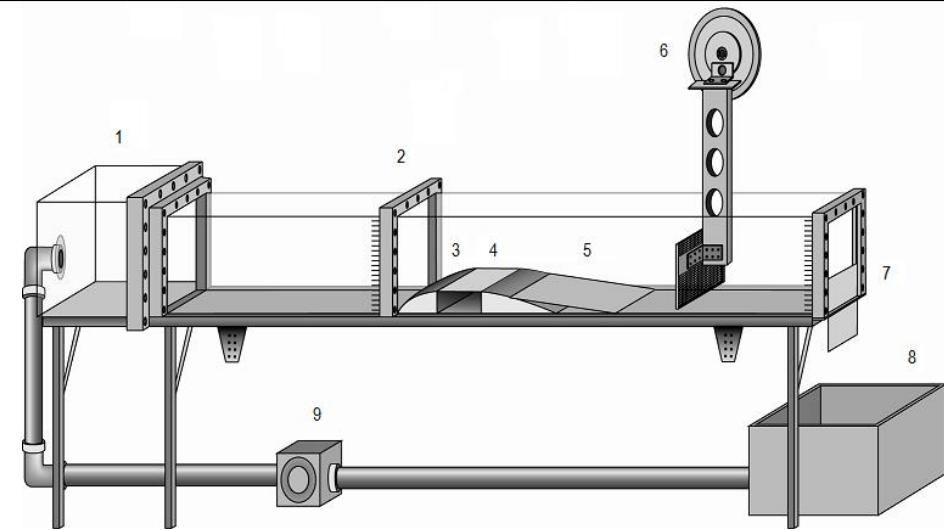
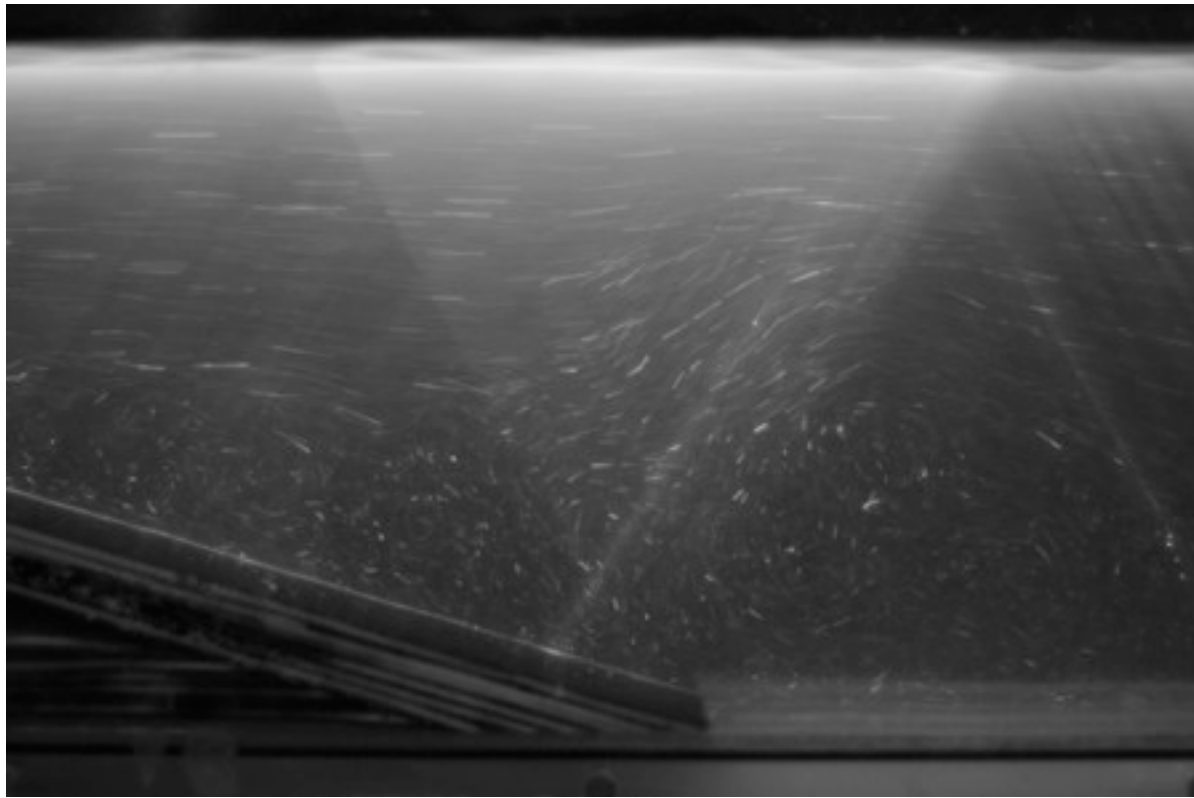
Our experiment ➤ Black & White hole horizons

effective
white hole

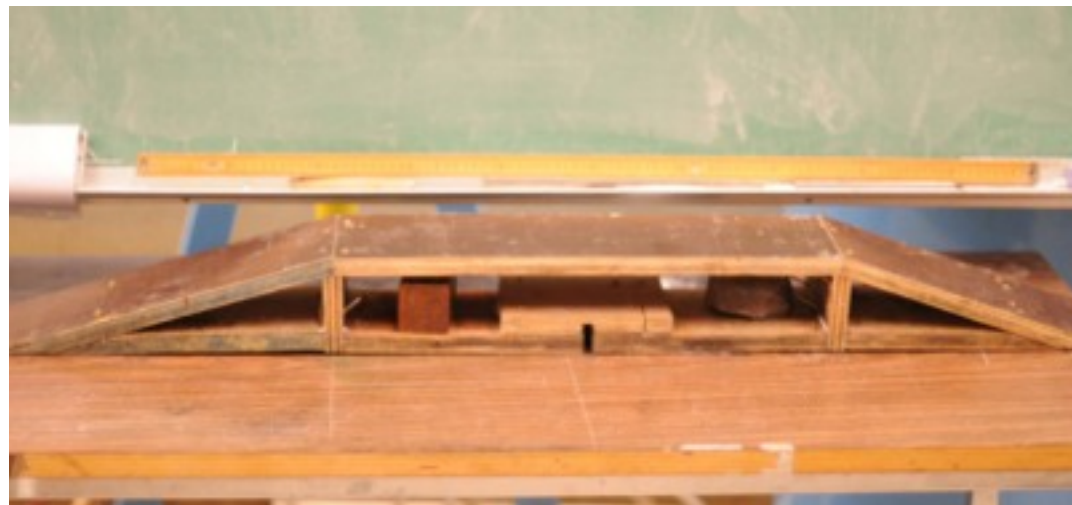


effective
black hole

Our experiment ➤ The design of our obstacle



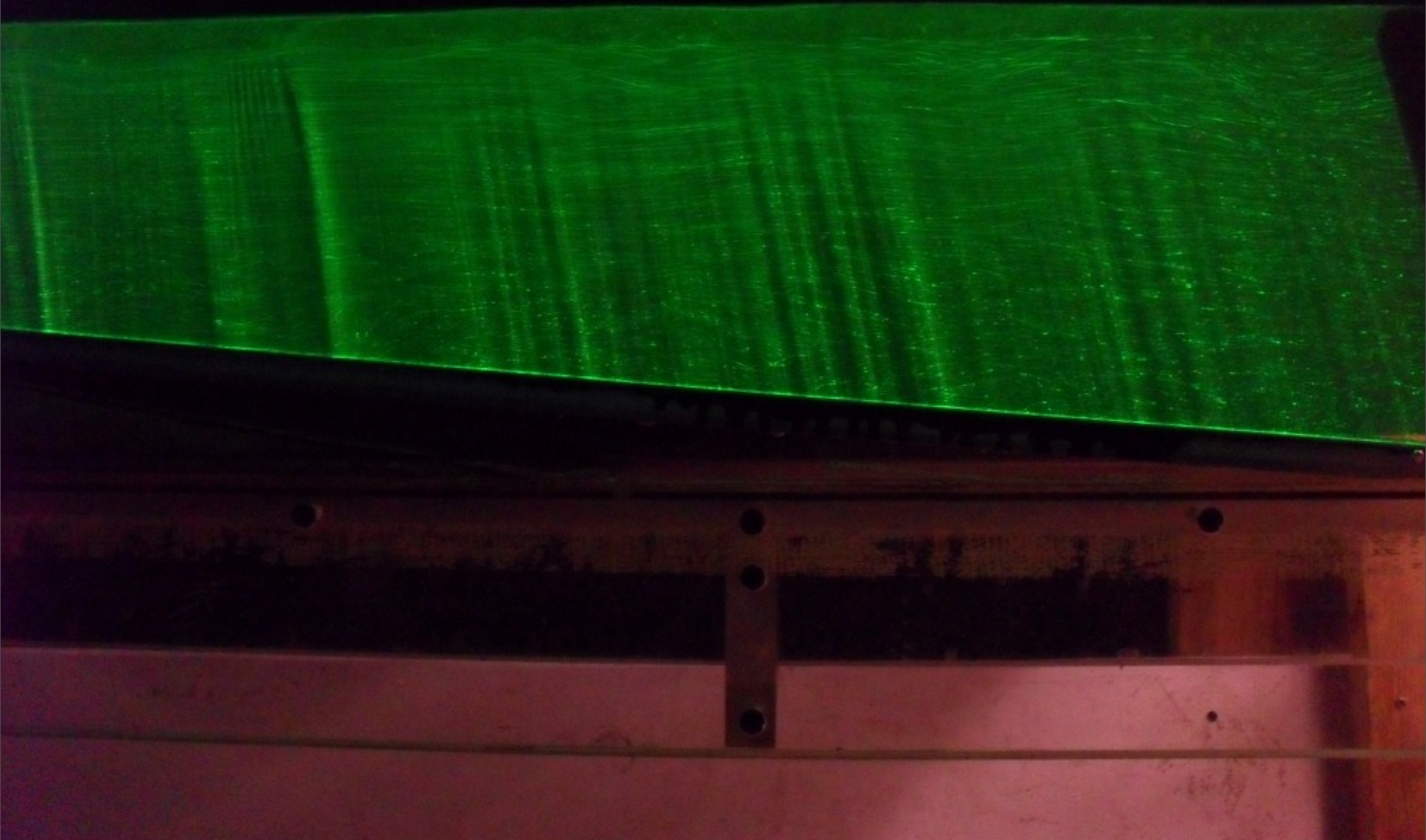
Initial design for our experiment



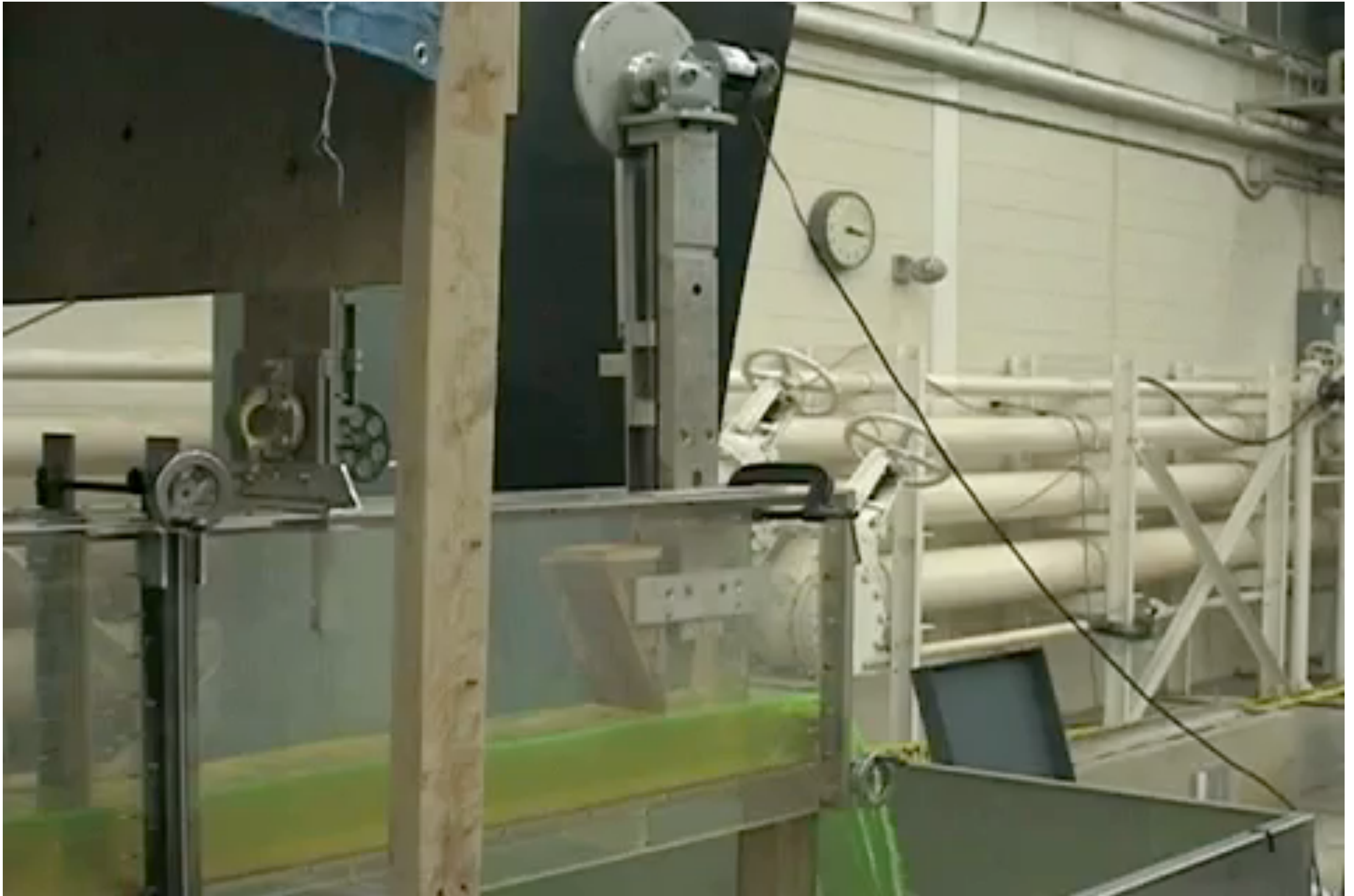
Down-scaled version of Germain Rousseaux et al. obstacle.
[length: 14m to 1m]



Our experiment > The design of our obstacle



Our experiment ➤ early experiment with bigger waves



Field theory ➤ physics of surface waves

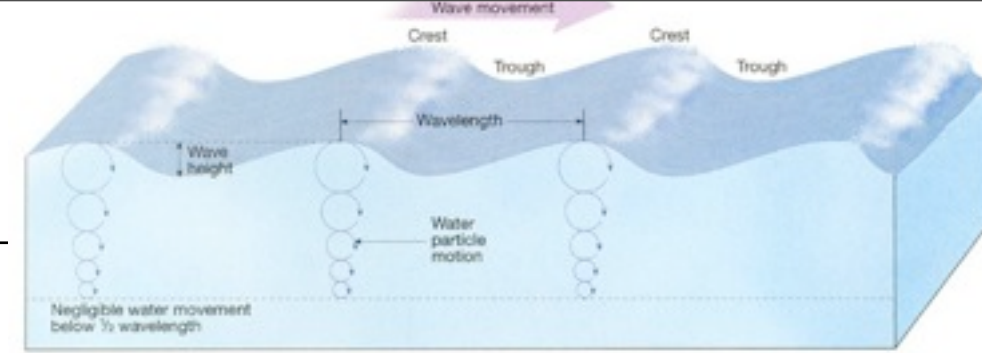
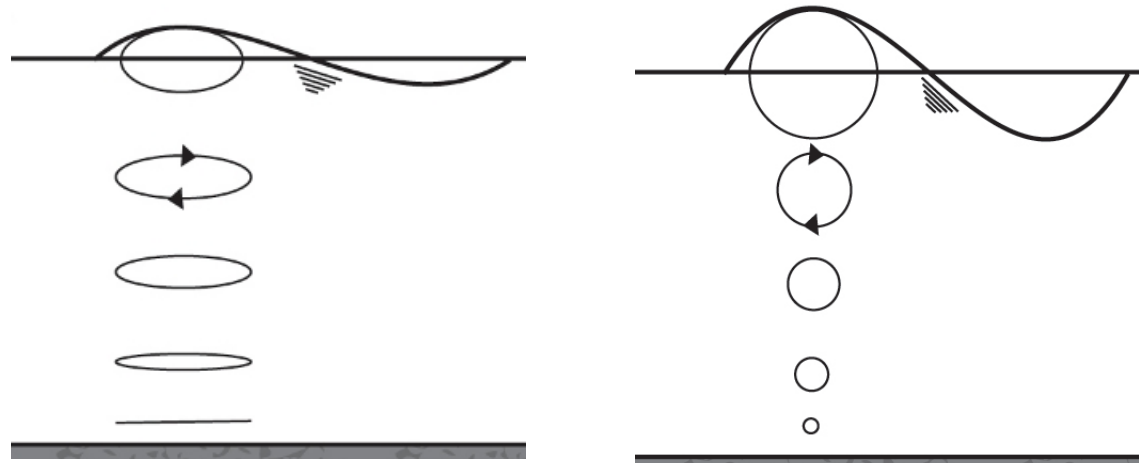


Figure 14.2 This diagram illustrates the basic parts of a wave as well as the movement of water particles with the passage of the wave. Negligible water movement occurs below a depth equal to one-half the wavelength (the level of the dashed line).

$$\Omega^2 = \left(gk + \frac{\sigma}{\rho} k^3 \right) \tanh(kh)$$



$$\omega_0 = \pm \Omega_x(\pm k), \text{ where } v_0 = 0$$

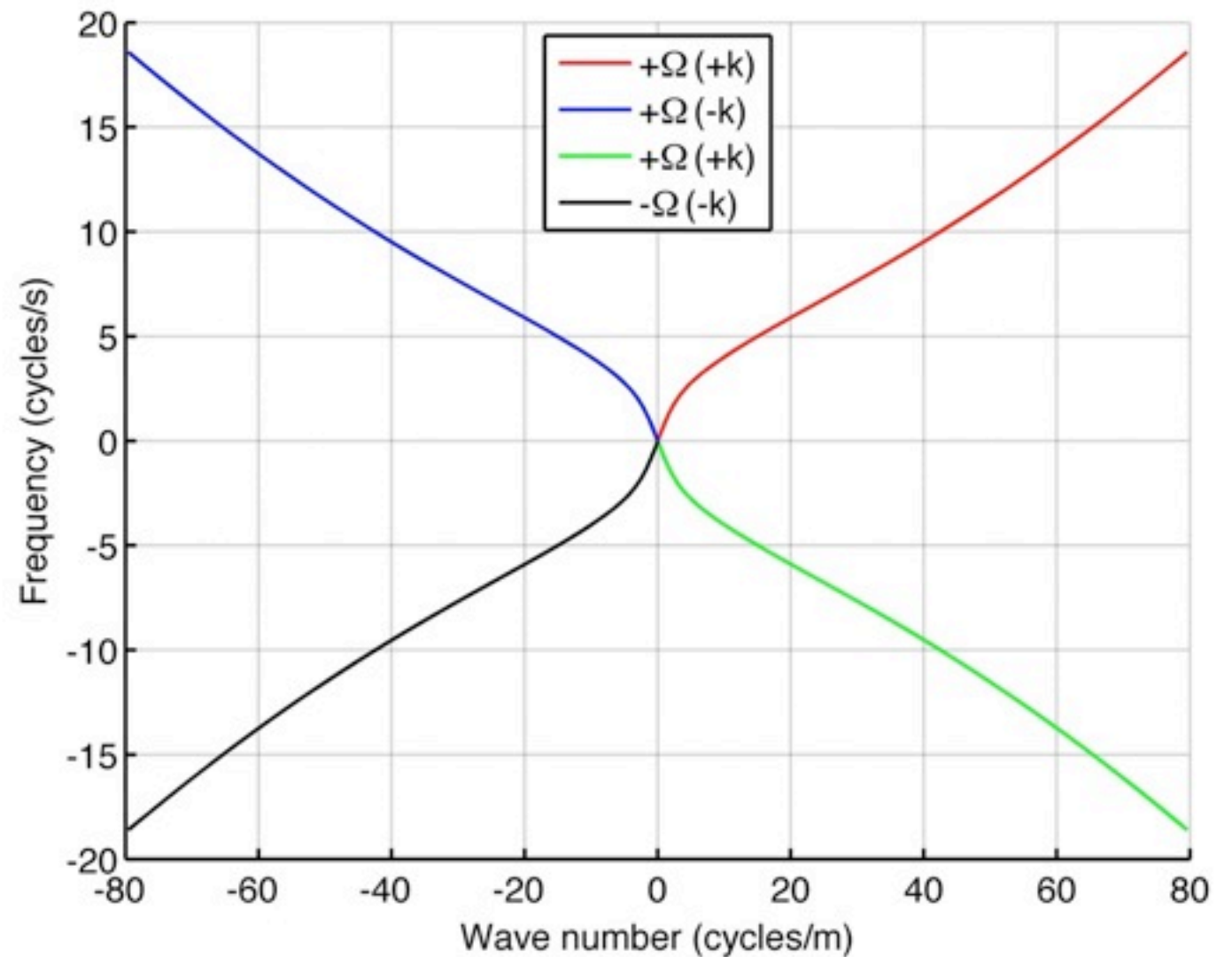
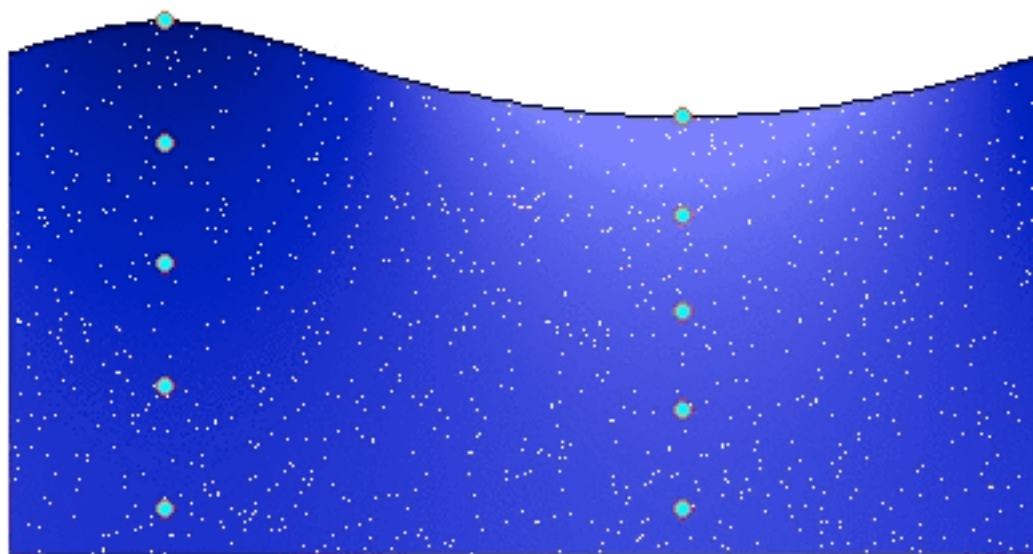
shallow:

$$\Omega = \sqrt{gh} k$$

deep:

$$\Omega = \sqrt{gk}$$

wave phase : $t/T = 0.000$



Field theory ➤ physics of surface waves

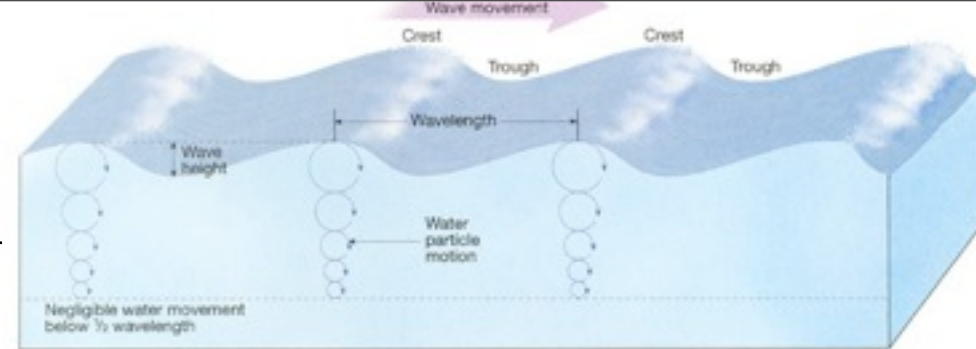
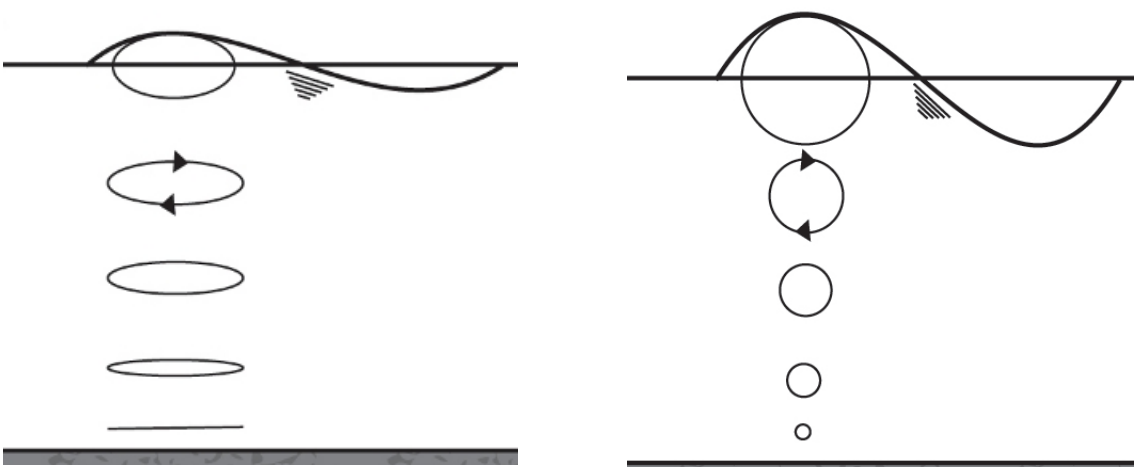


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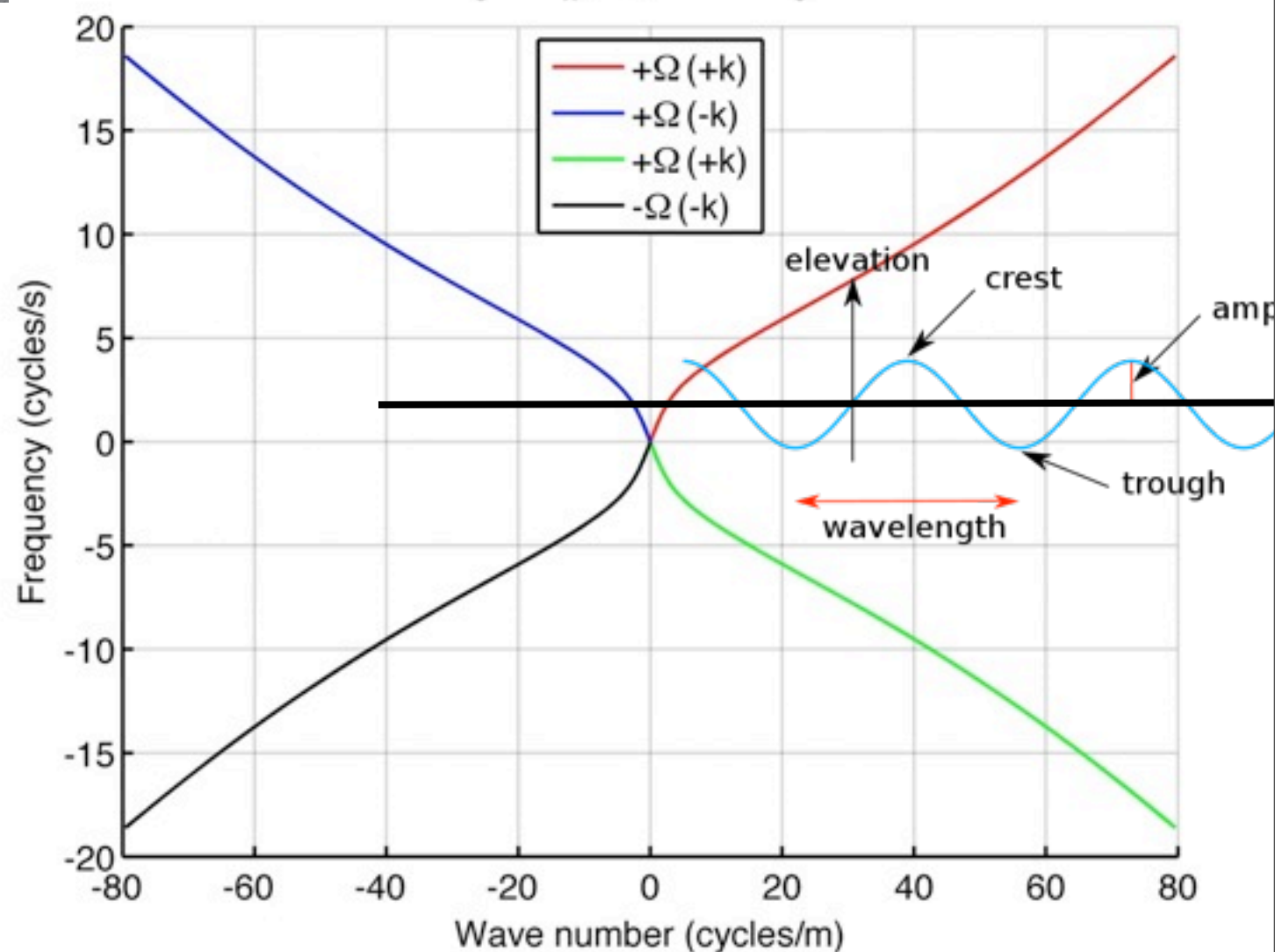
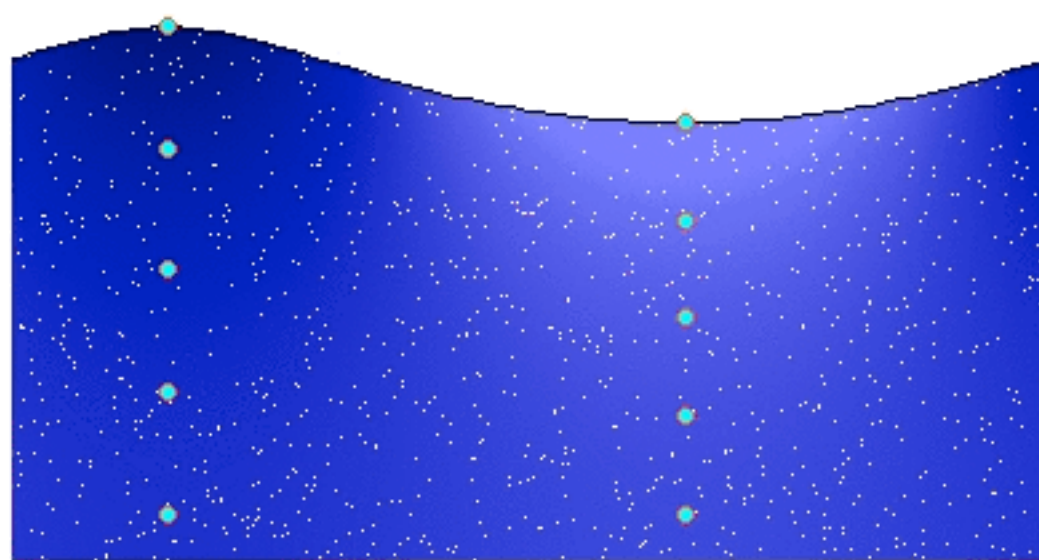
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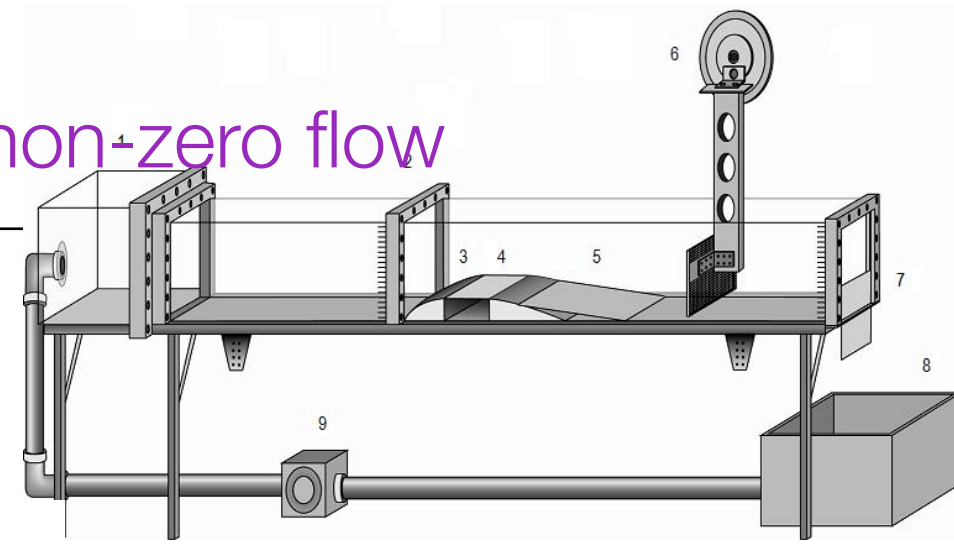
deep:

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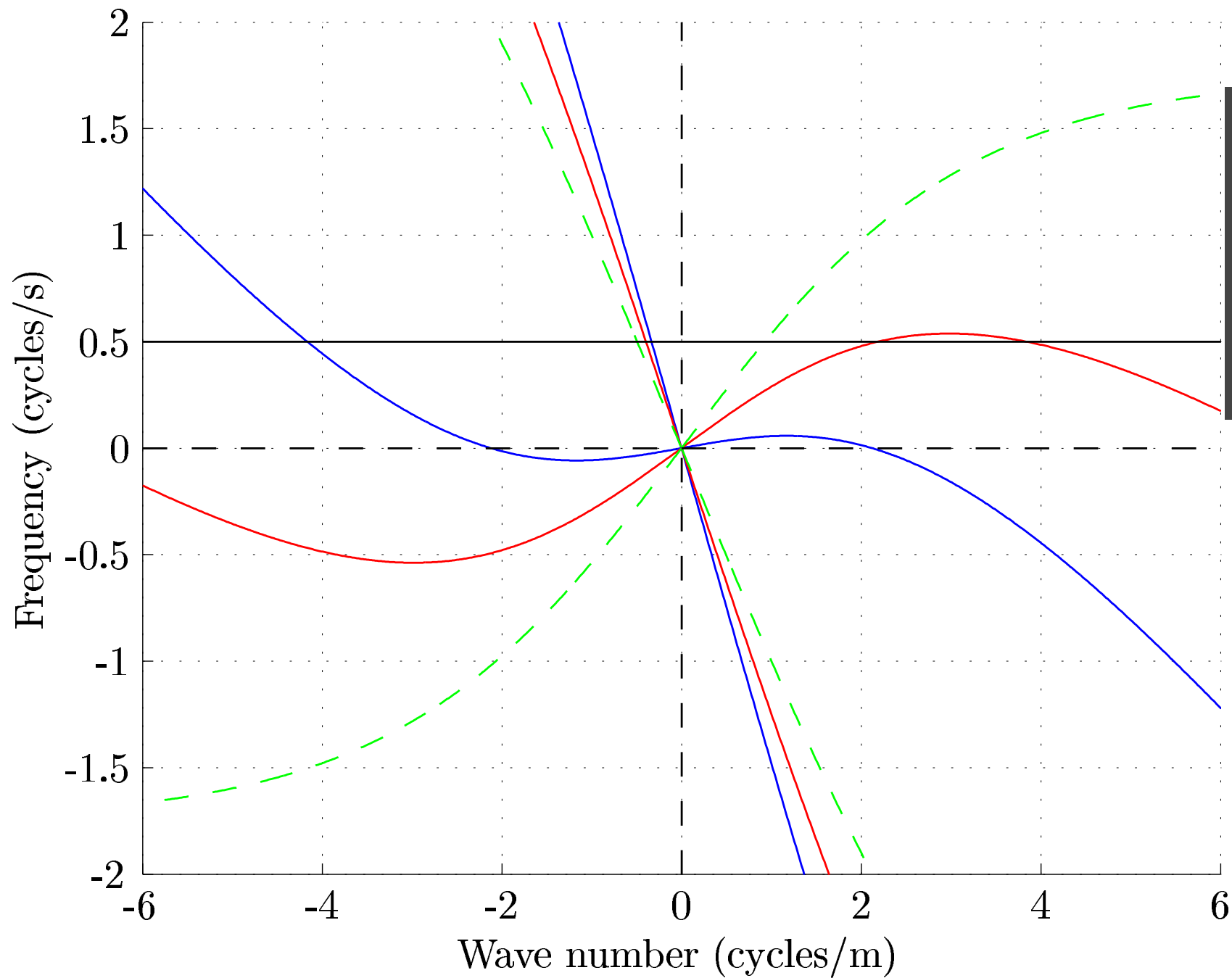
wave phase : $t/T = 0.000$



Field theory ➤ physics of surface waves non-zero flow



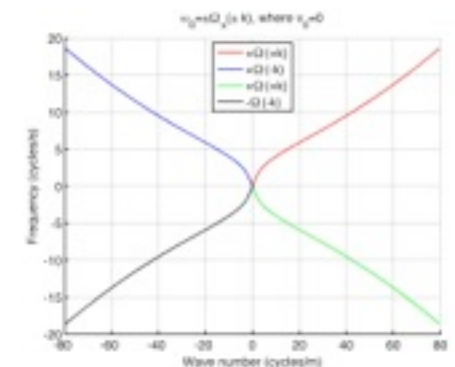
$$\Omega_{\text{LAB}} = \Omega_{\text{WATER}} \pm v k$$



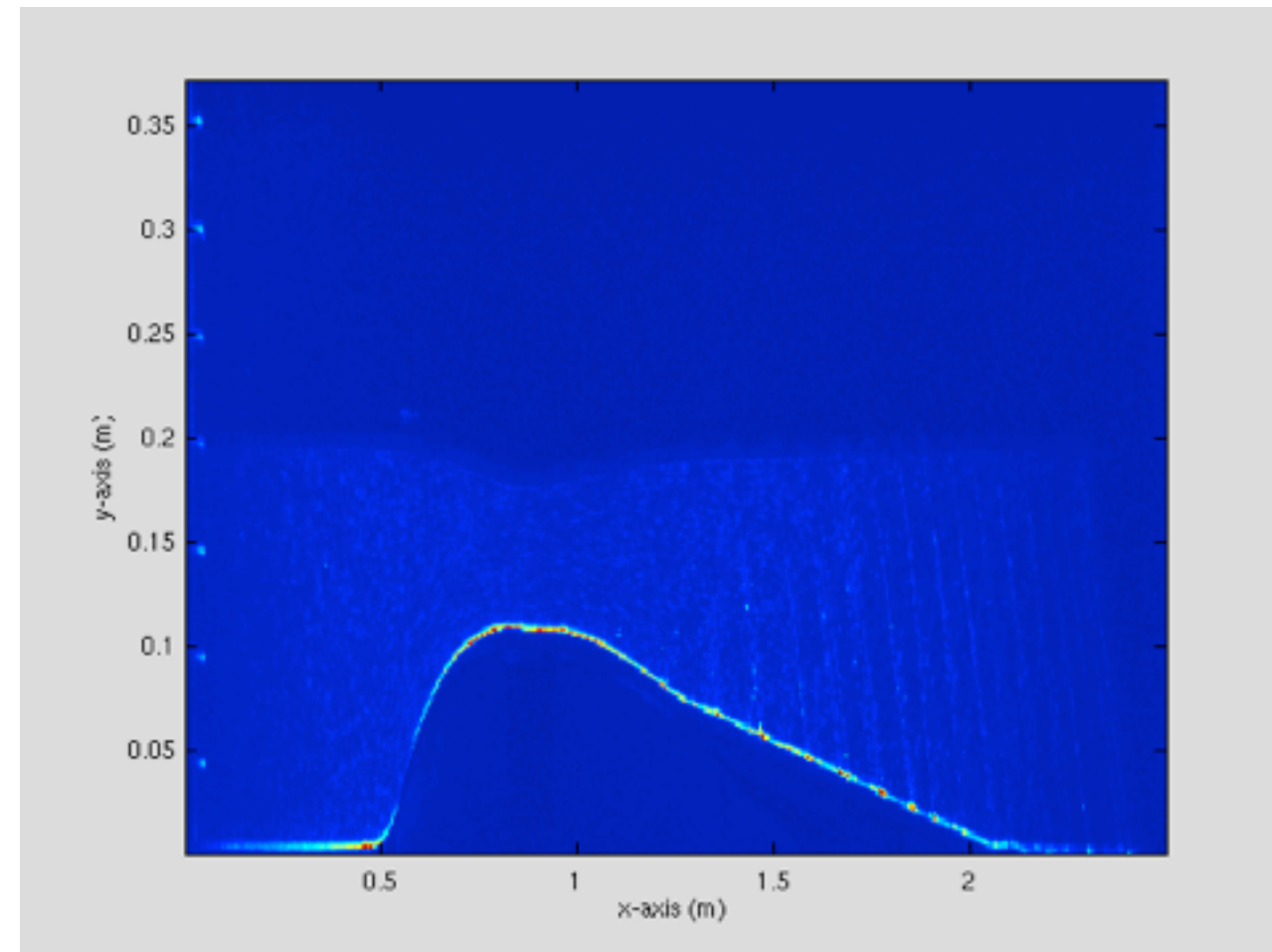
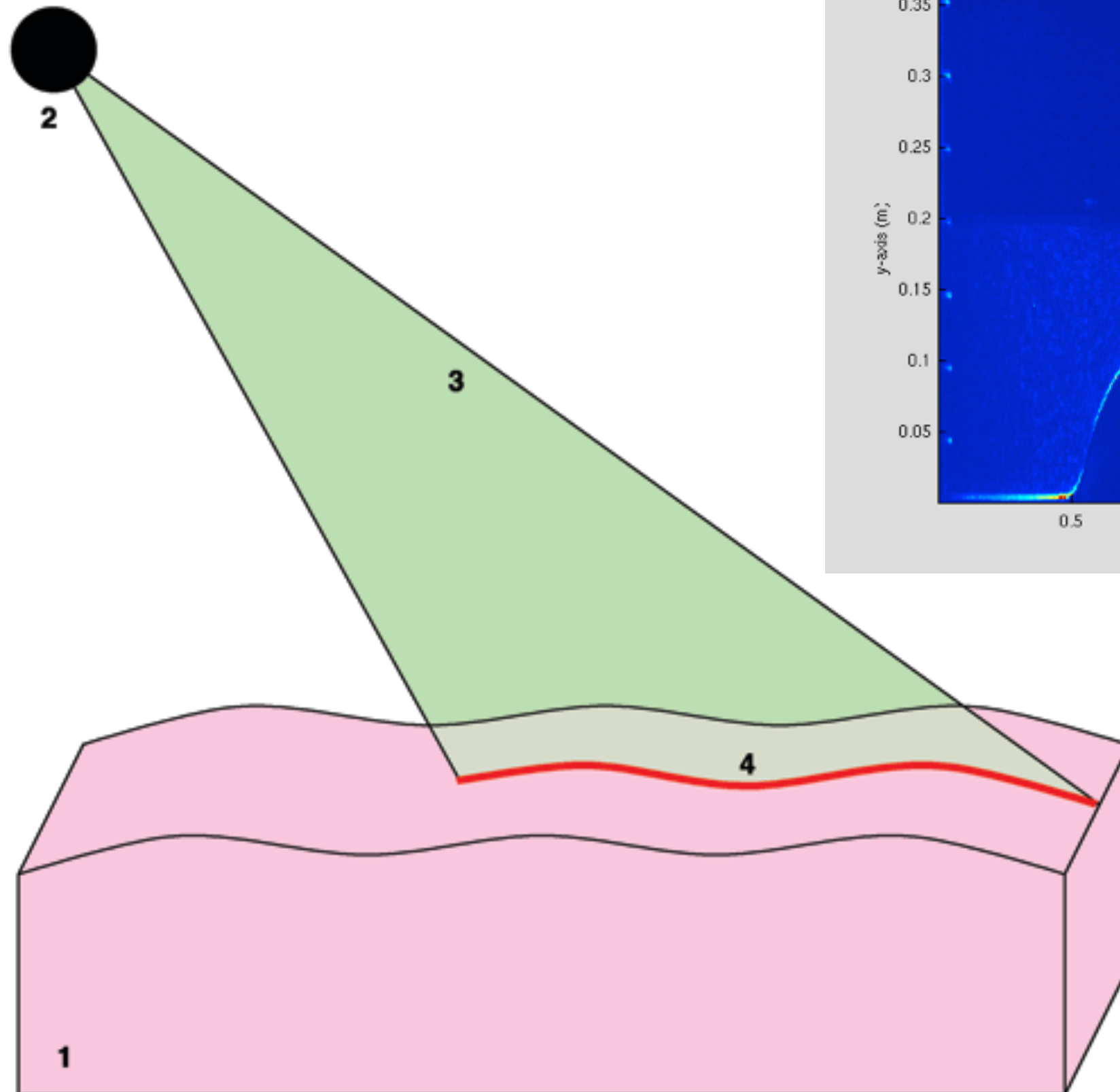
Dispersion relation for
 maximum height
 conversion point
 minimum height

shallow: $\Omega = \sqrt{gh} k$

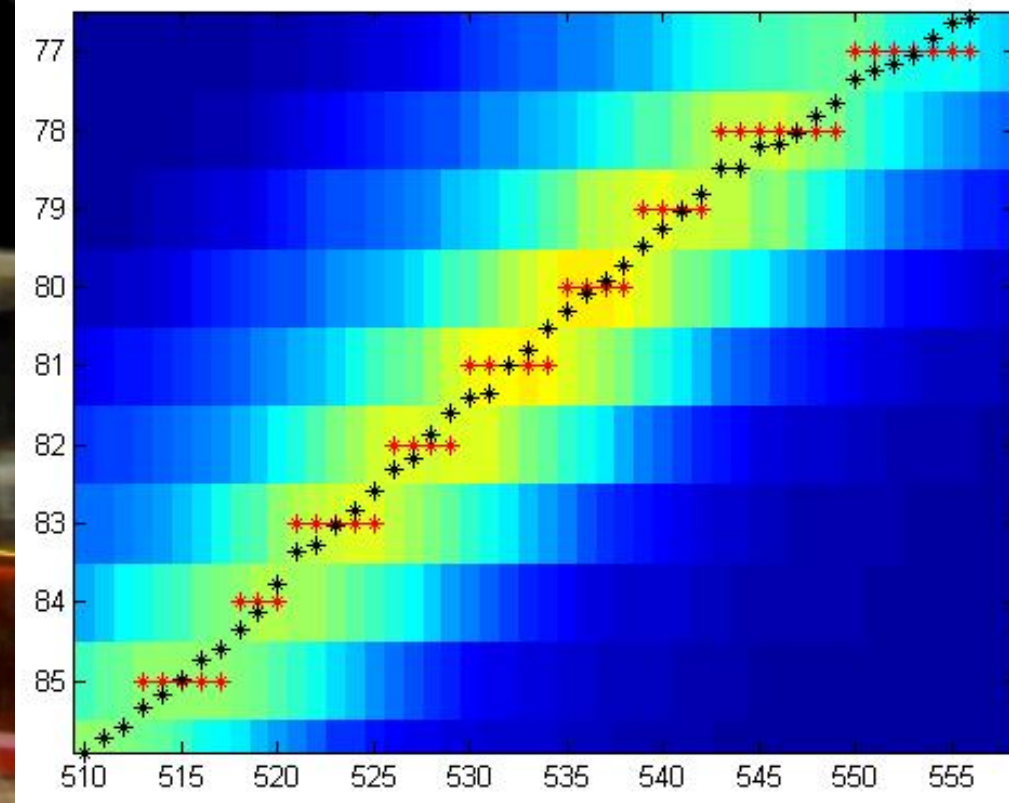
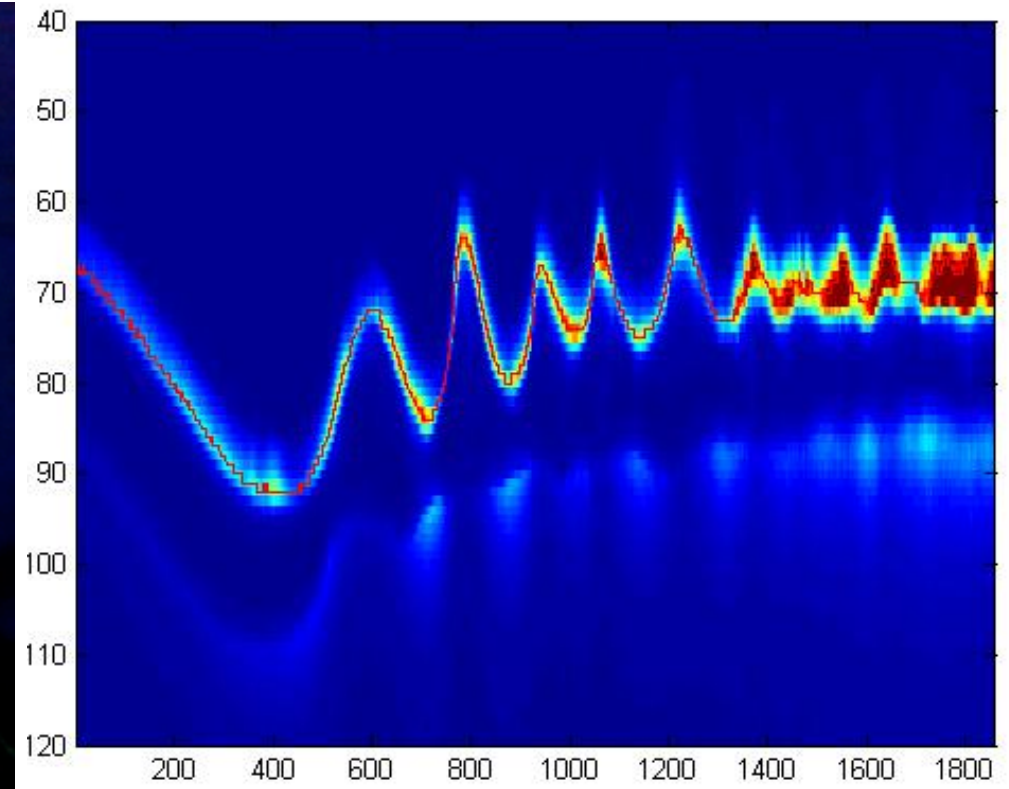
deep: $\Omega = \sqrt{gk}$

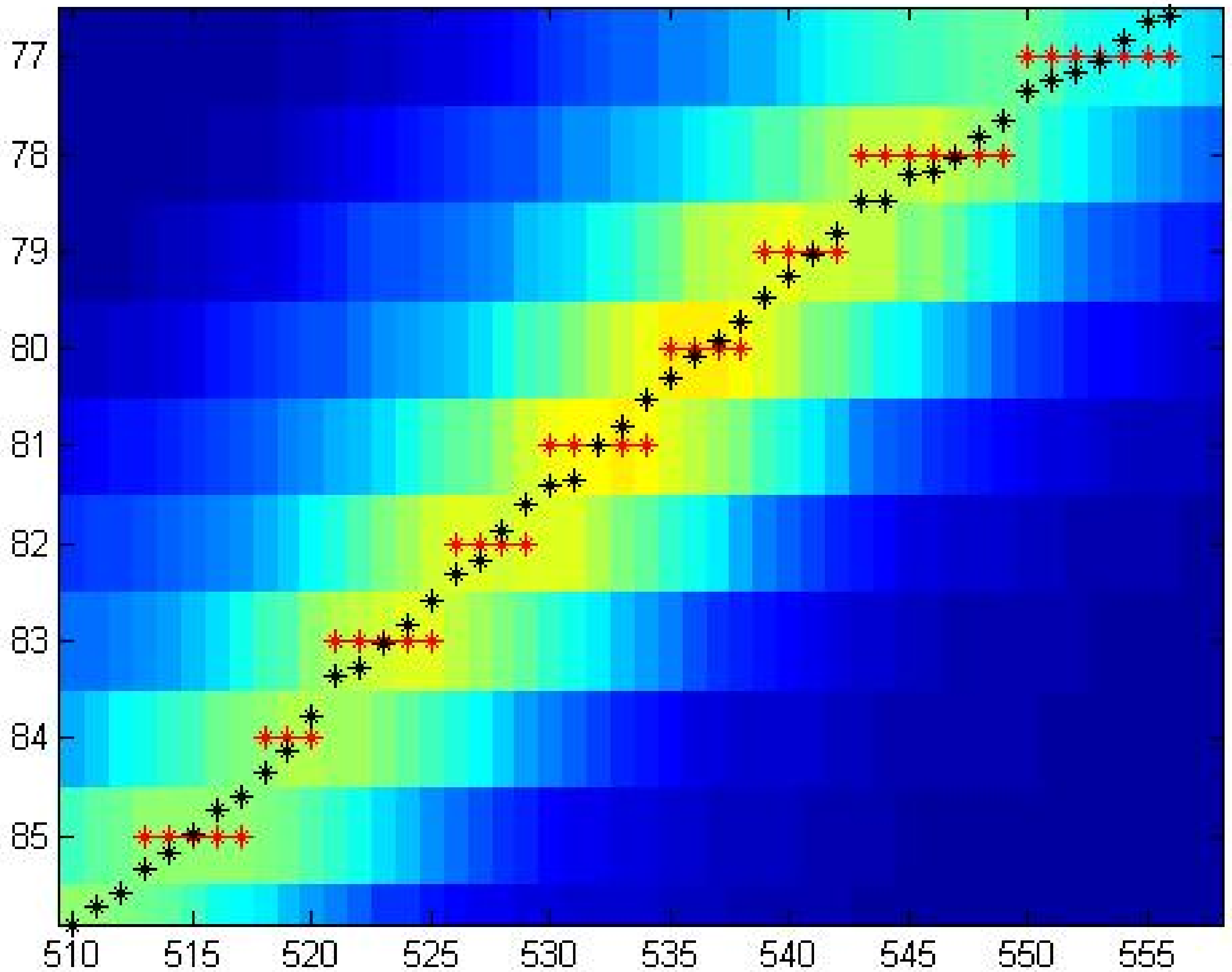


Our experiment ➤ Observable



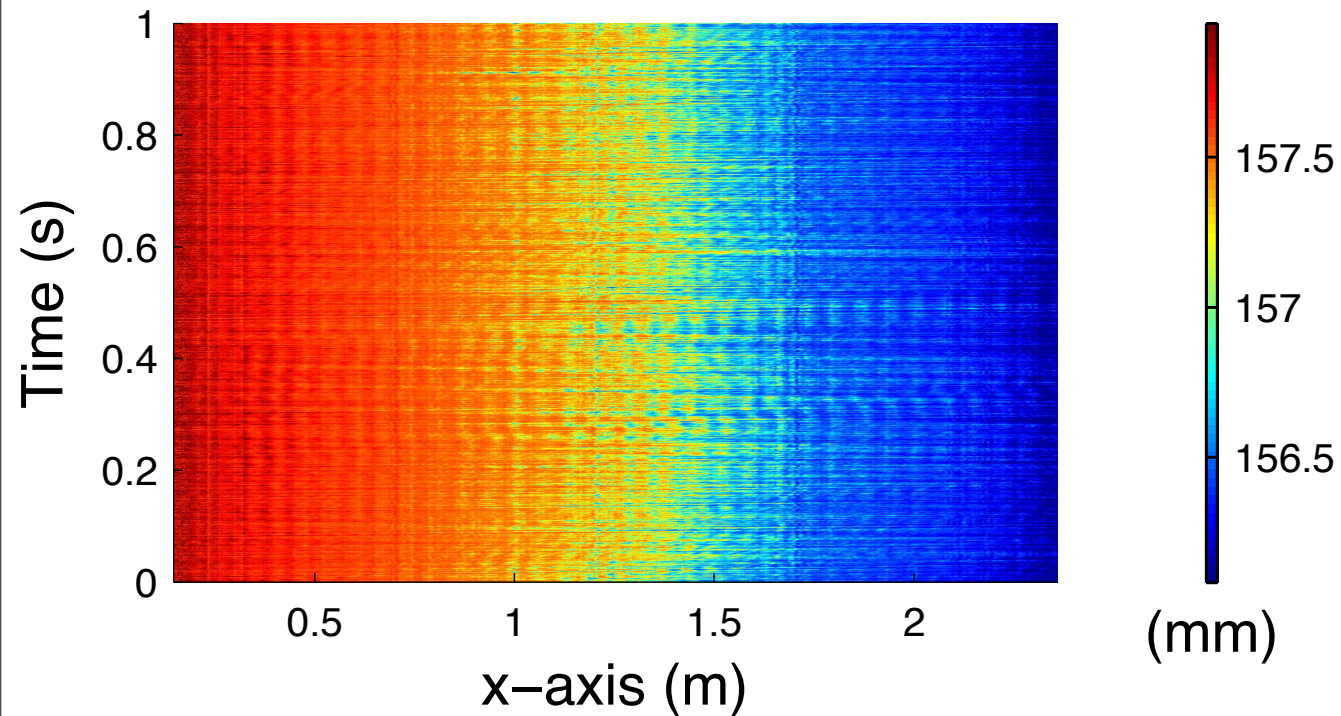
Our experiment ➤ Data analysis





Data analysis ➤ from wave characteristic to dispersion rel.

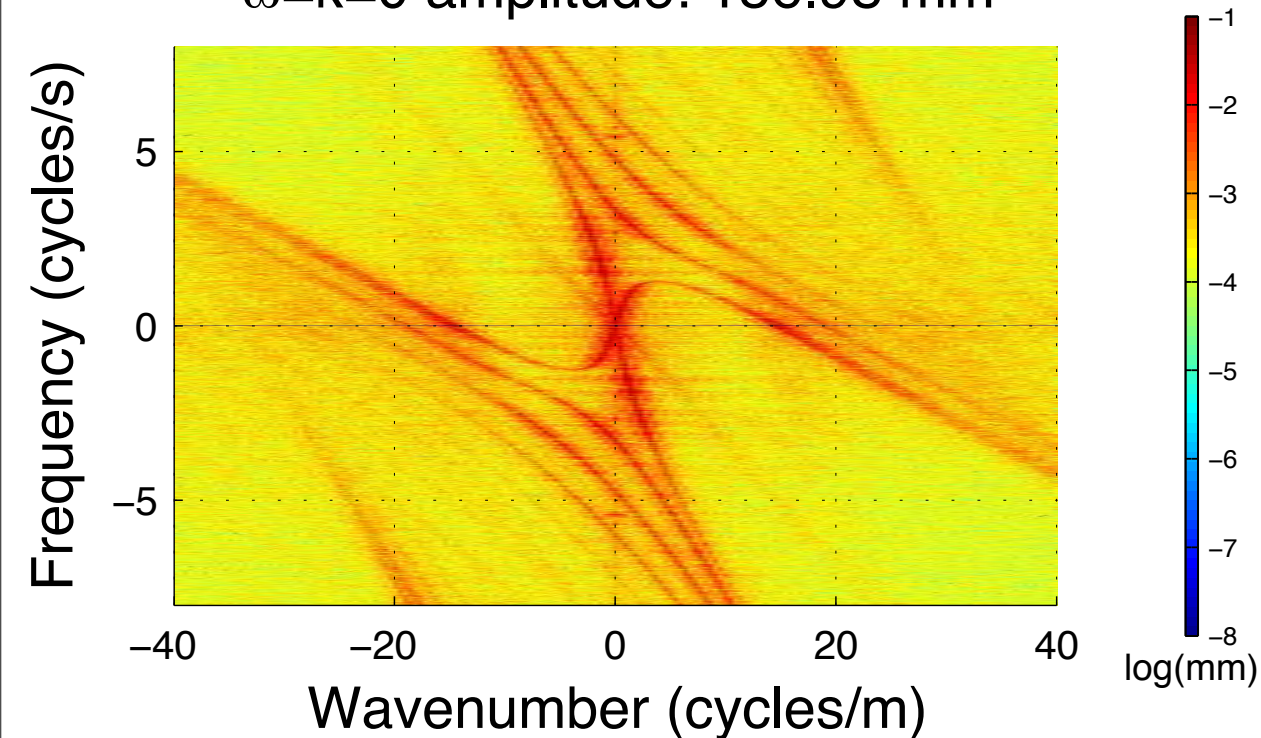
$\omega=k=0$ amplitude: 156.98 mm



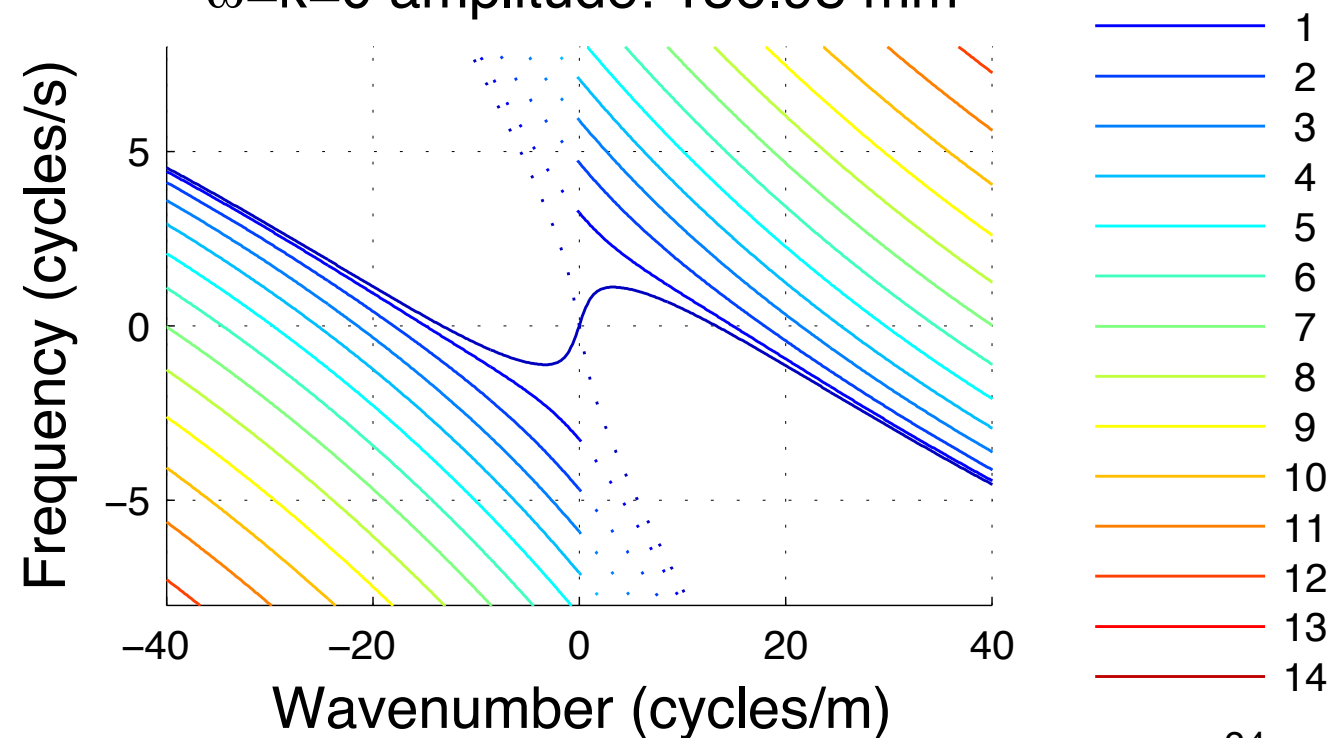
$$(f + \tilde{v} k)^2 = \left(\frac{g k}{2\pi} \right) \cdot \tanh(2\pi k h)$$

$$k = \sqrt{k_{\parallel}^2 + k_{\perp}^2} = \sqrt{(1/\lambda)^2 + (n/l_w)^2},$$

$\omega=k=0$ amplitude: 156.98 mm

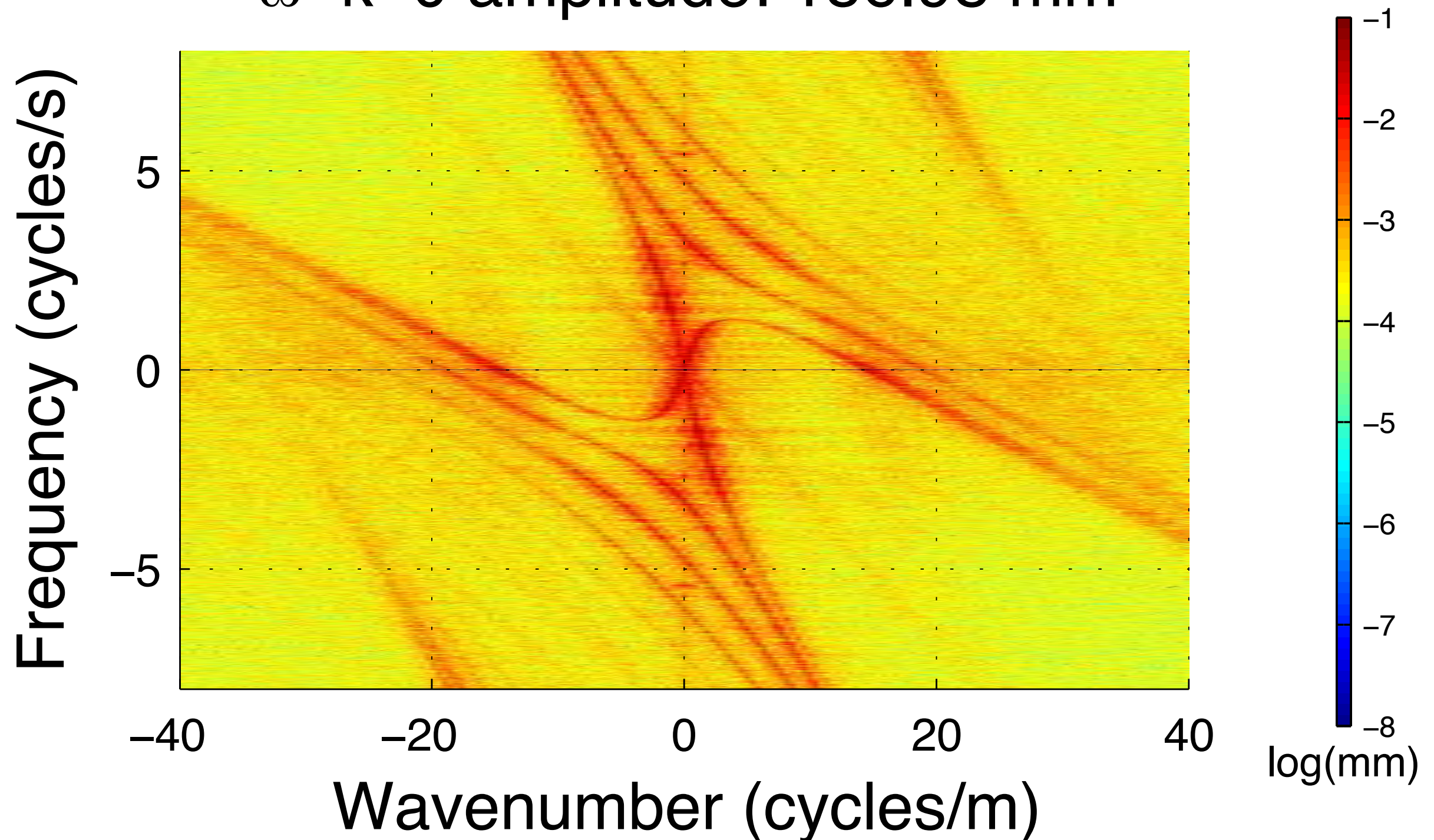


$\omega=k=0$ amplitude: 156.98 mm



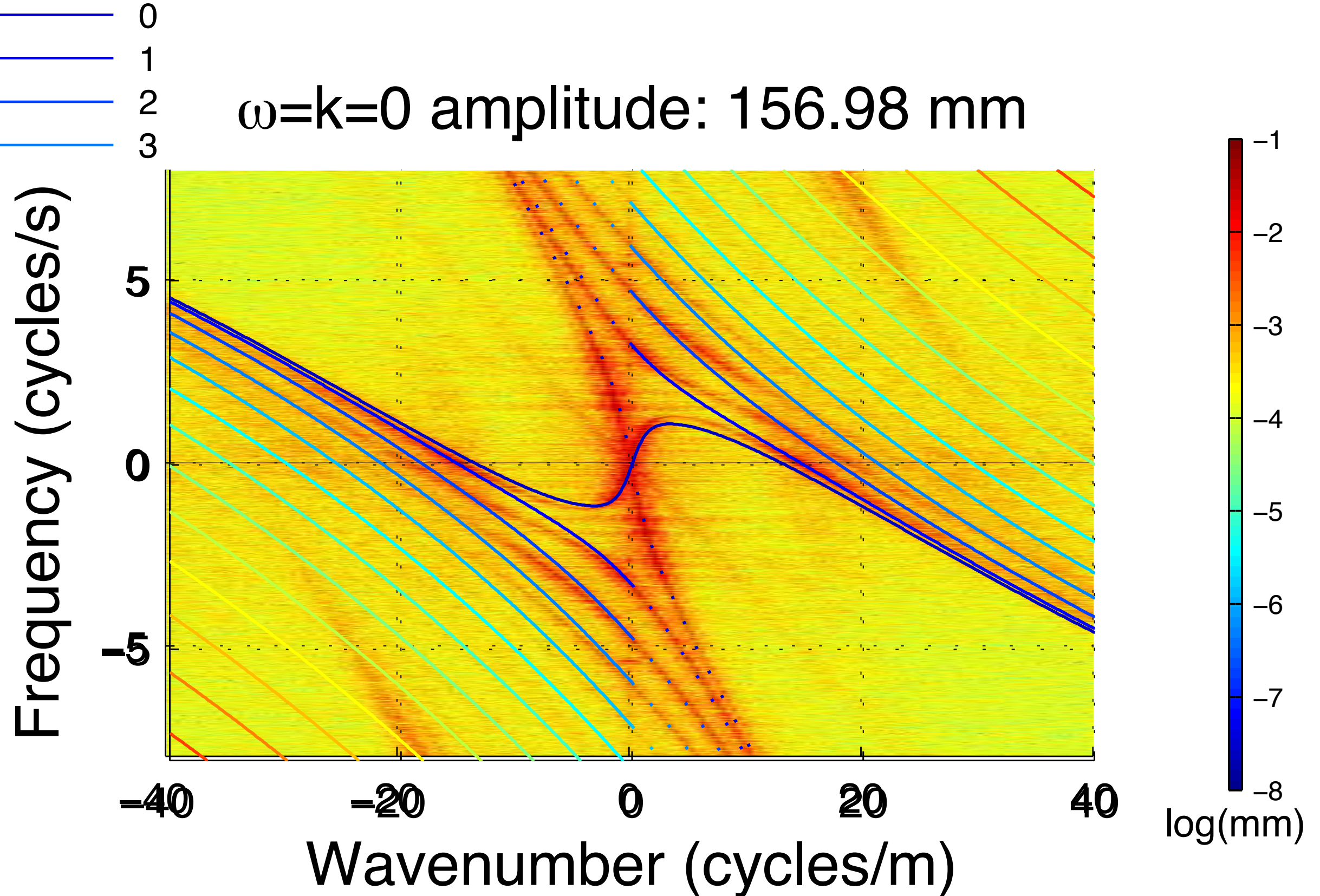
Data analysis ➤ from wave characteristic to dispersion rel.

$\omega=k=0$ amplitude: 156.98 mm



Data analysis ➤ from wave characteristic to dispersion rel.

$\omega=k=0$ amplitude: 156.98 mm



Data analysis ➤ from wave characteristic to dispersion rel.

$\omega=k=0$ amplitude: 156.98 mm

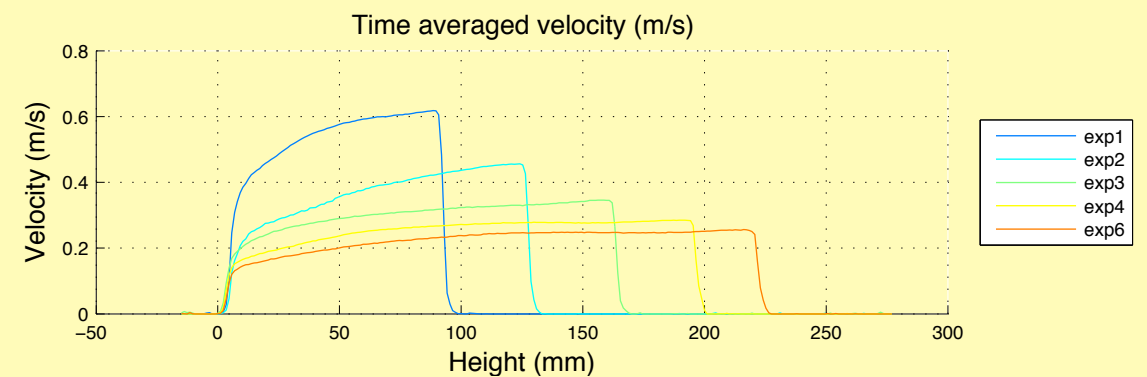
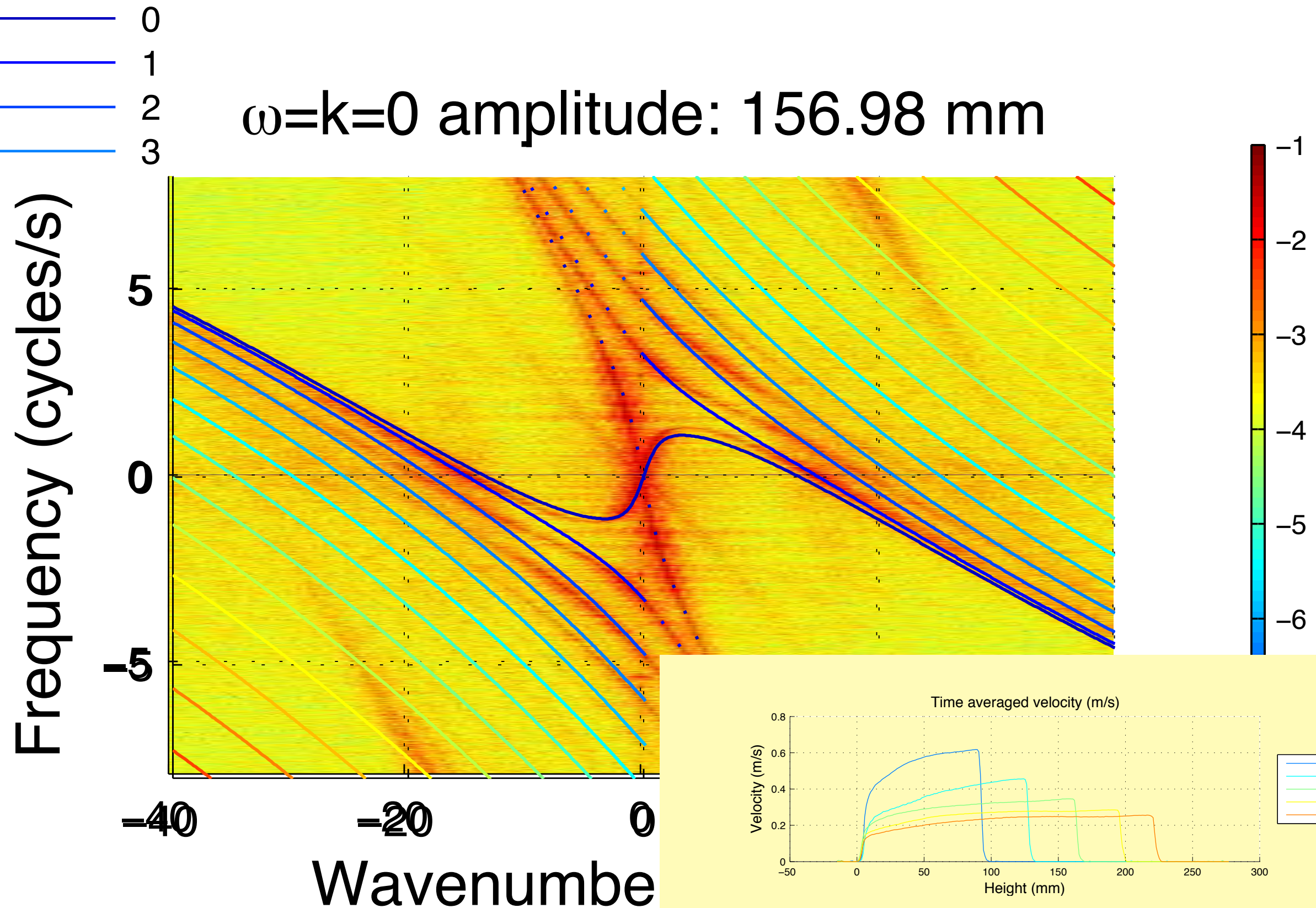
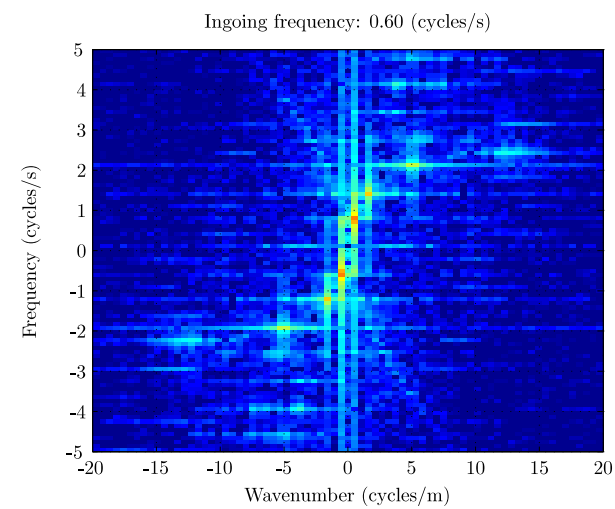
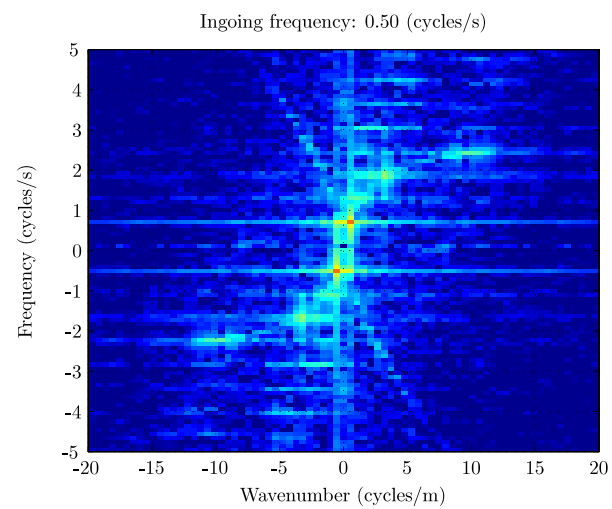
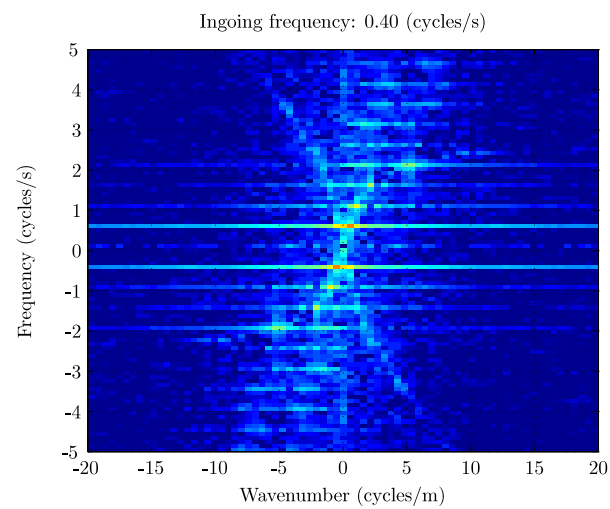
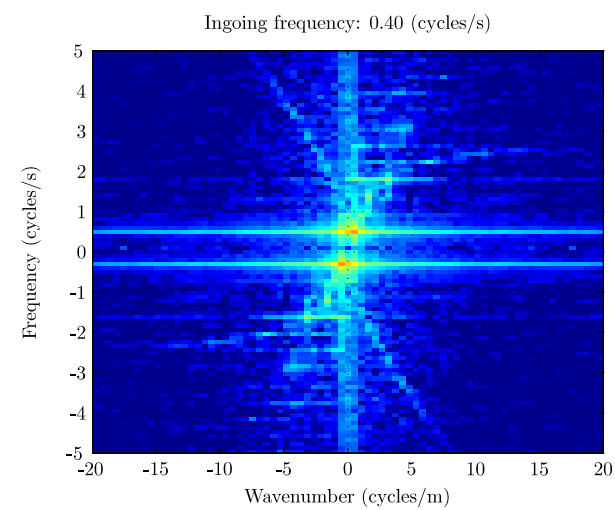
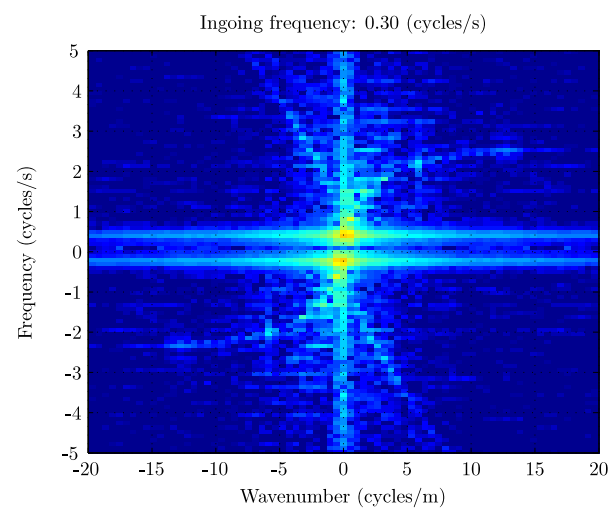
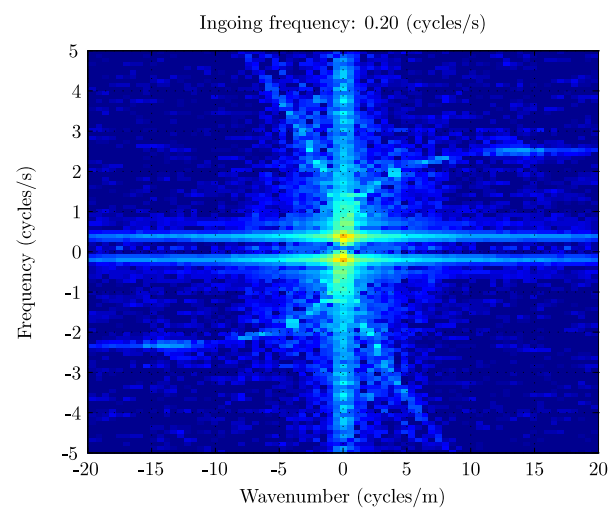
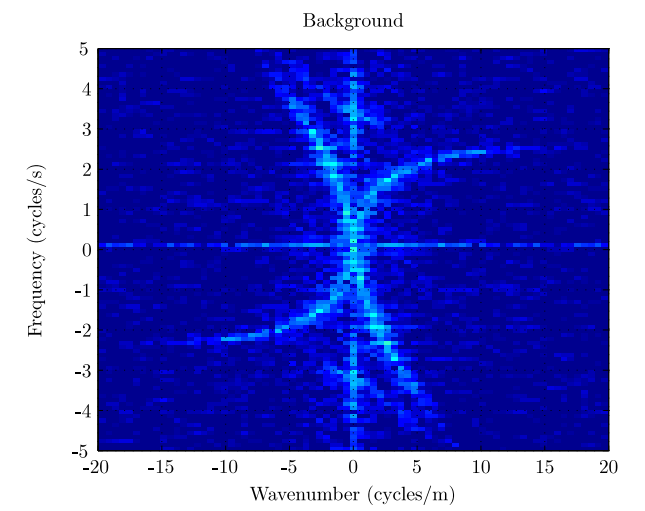
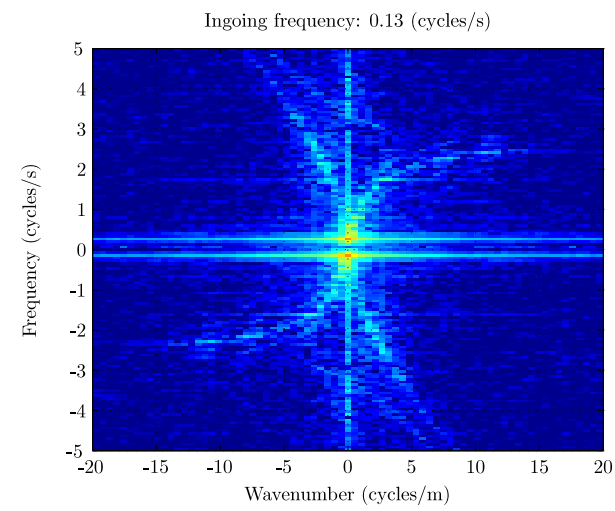
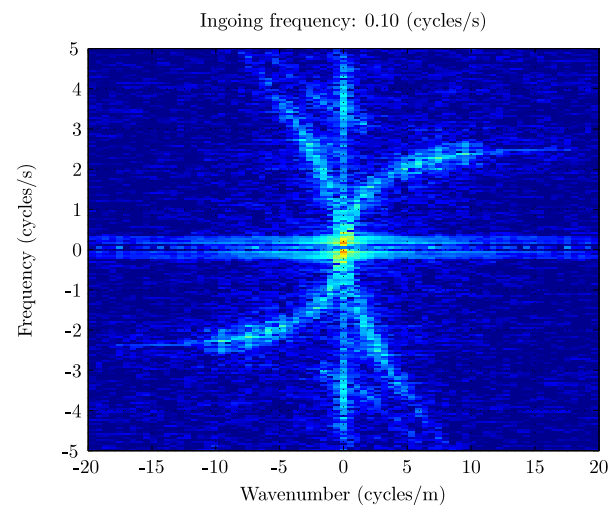
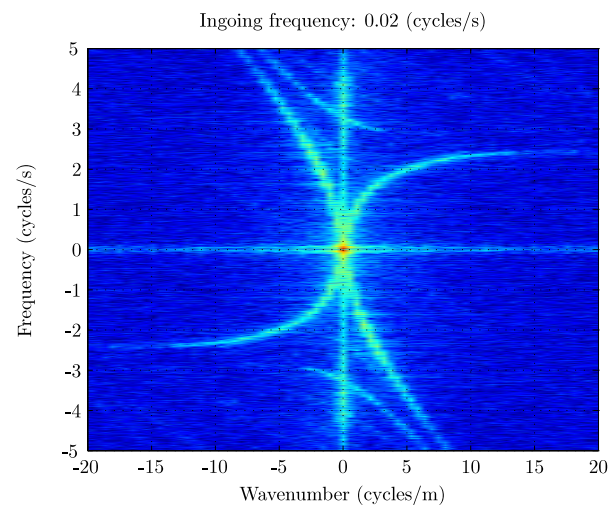
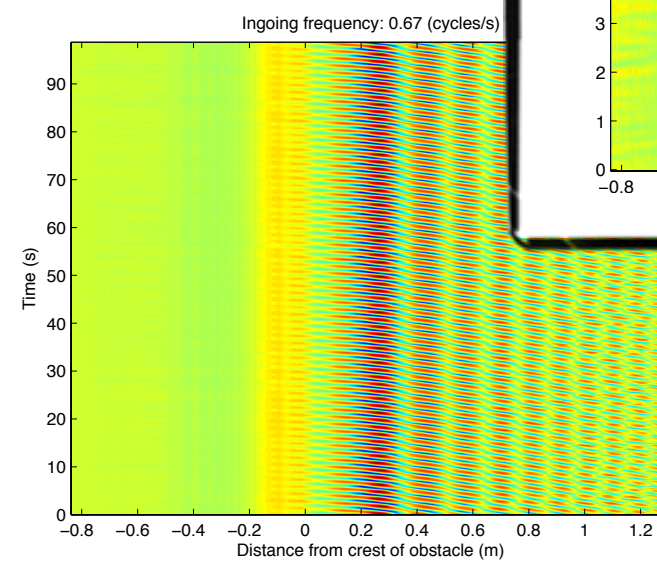
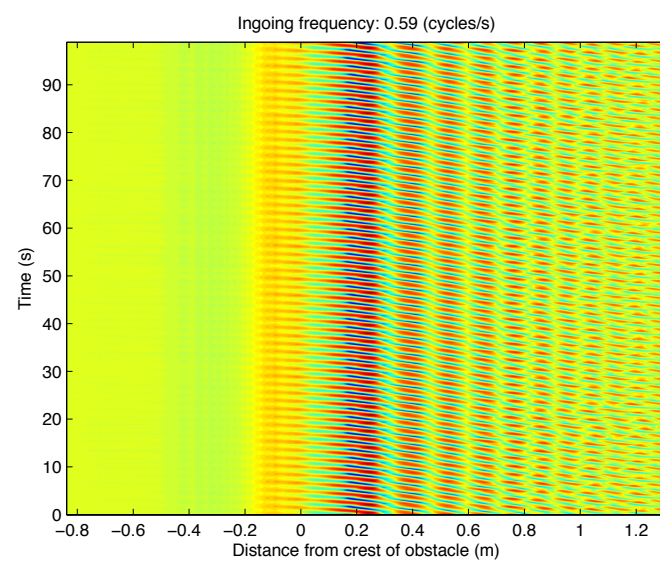
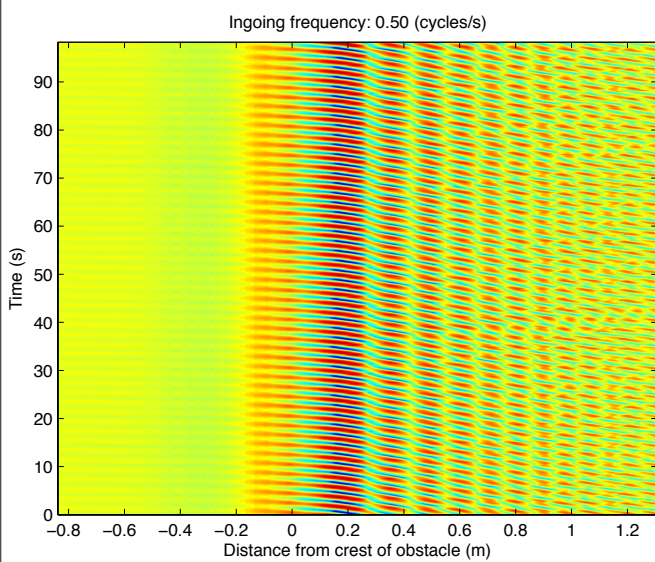
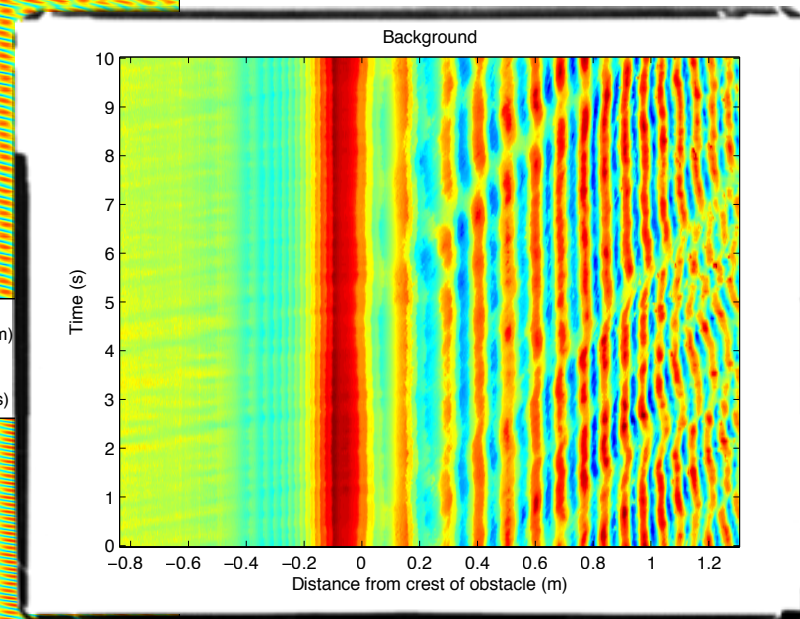
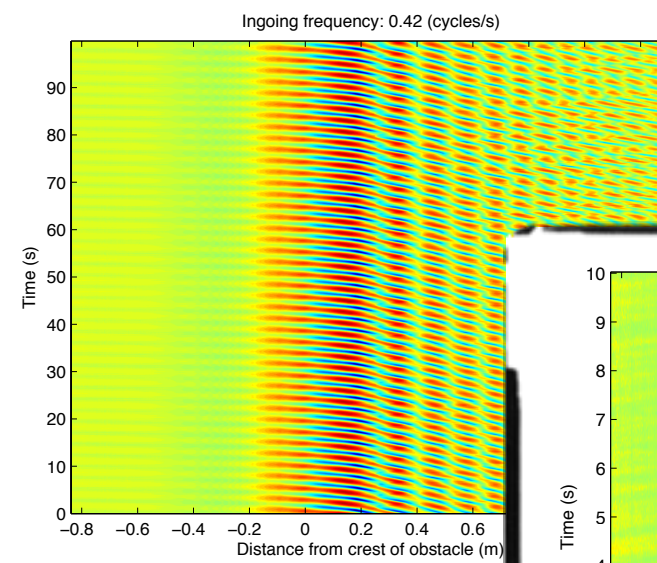
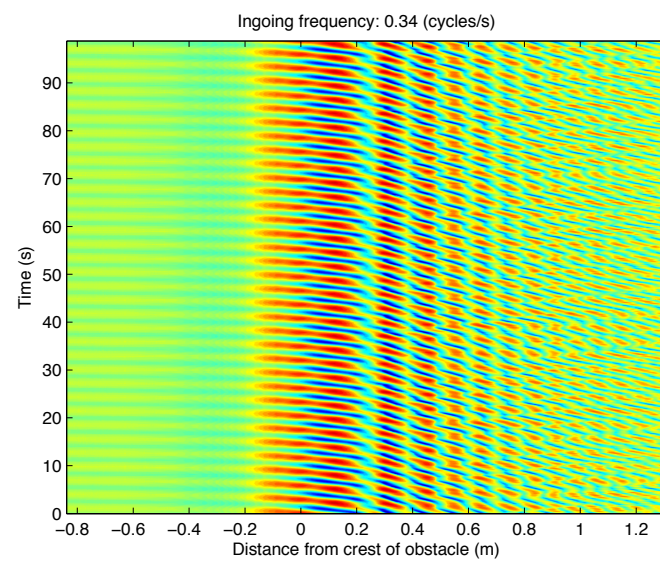
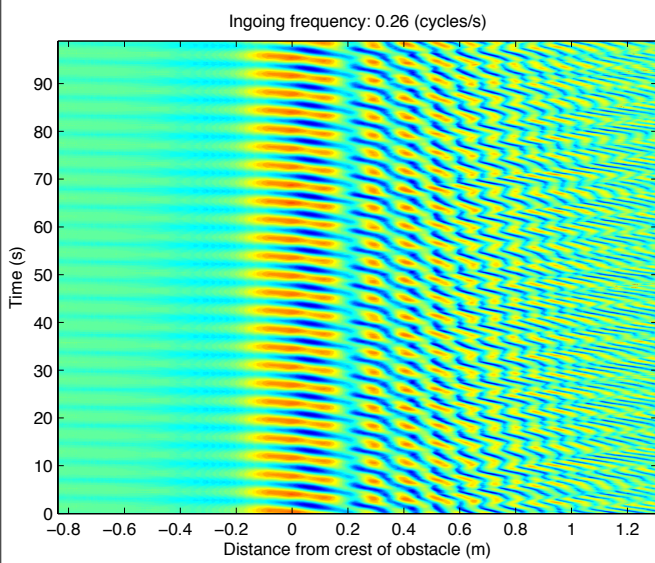
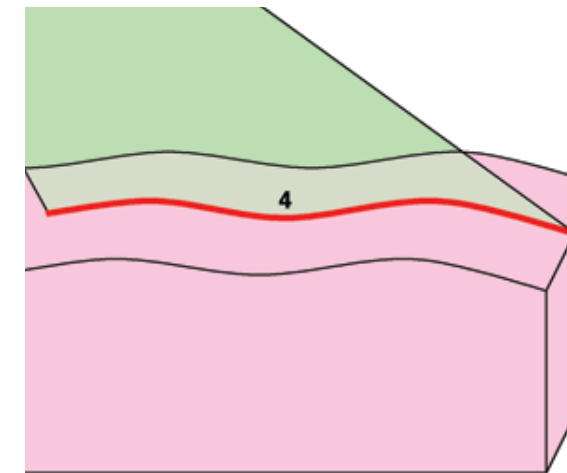
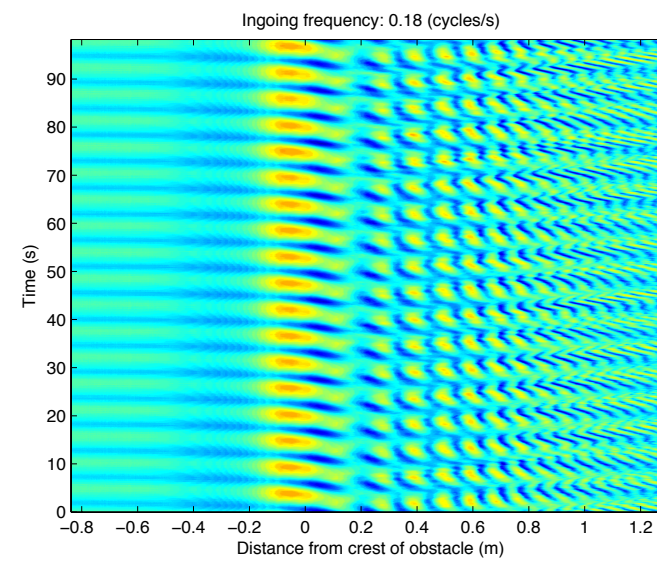
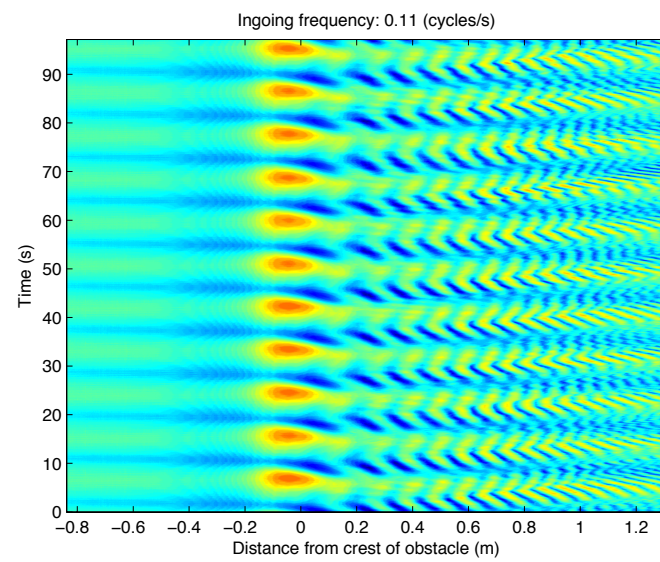
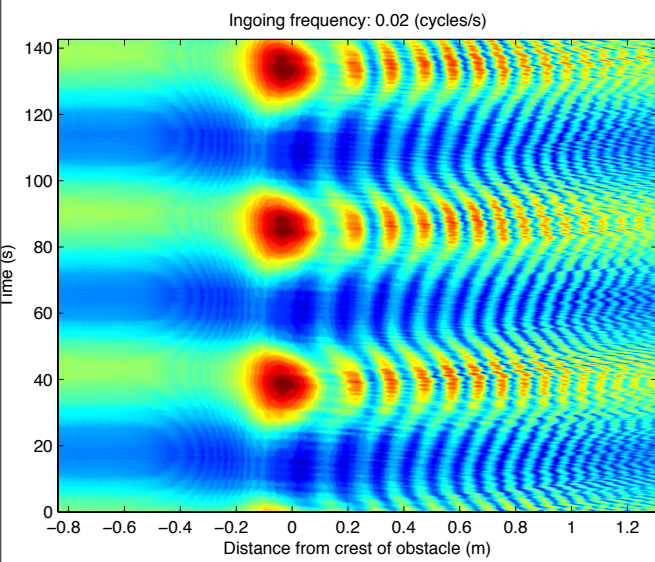


FIG. 16: (Colors online only.) Flow profiles from the PIV measurements.

Our experiment ➤ Exciting classical field modes

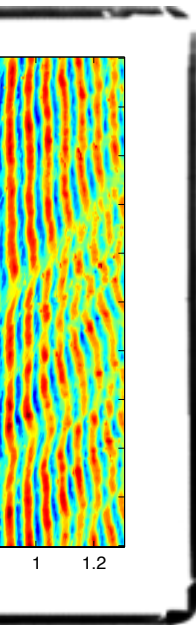
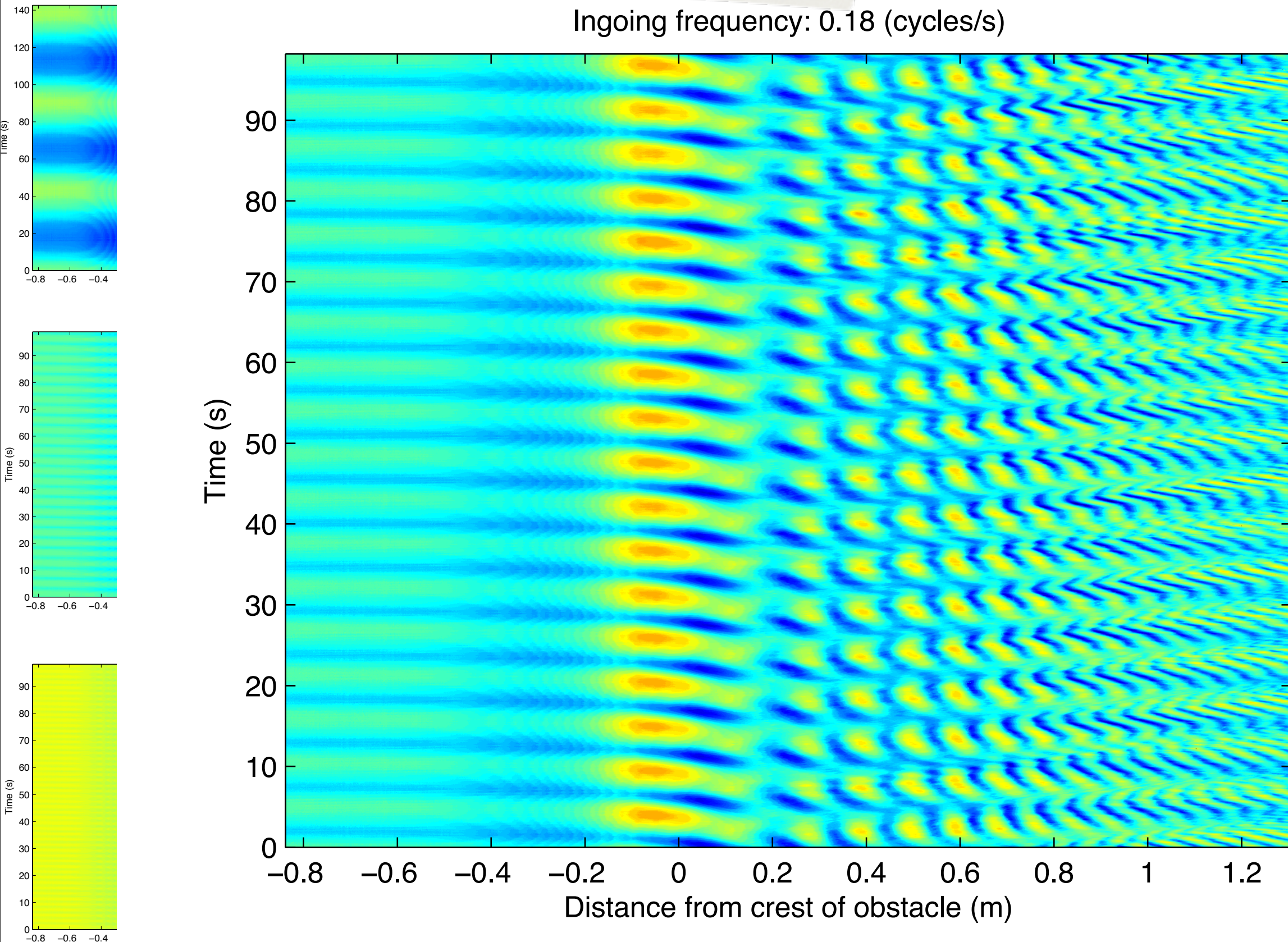


Our experiment ➤ Experimental procedure



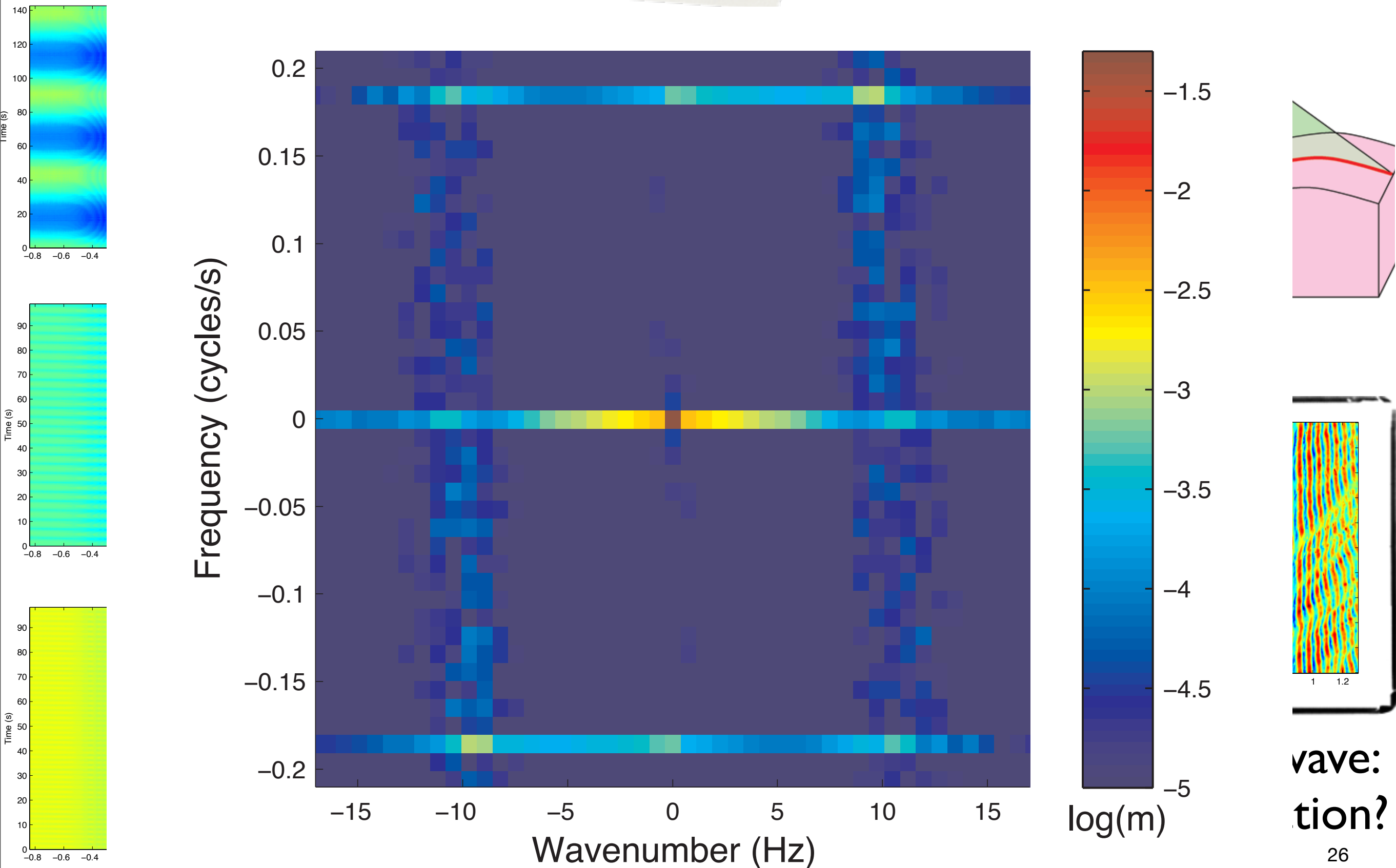
Standing wave:
the undulation?

Our experiment ➤ Experimental procedure

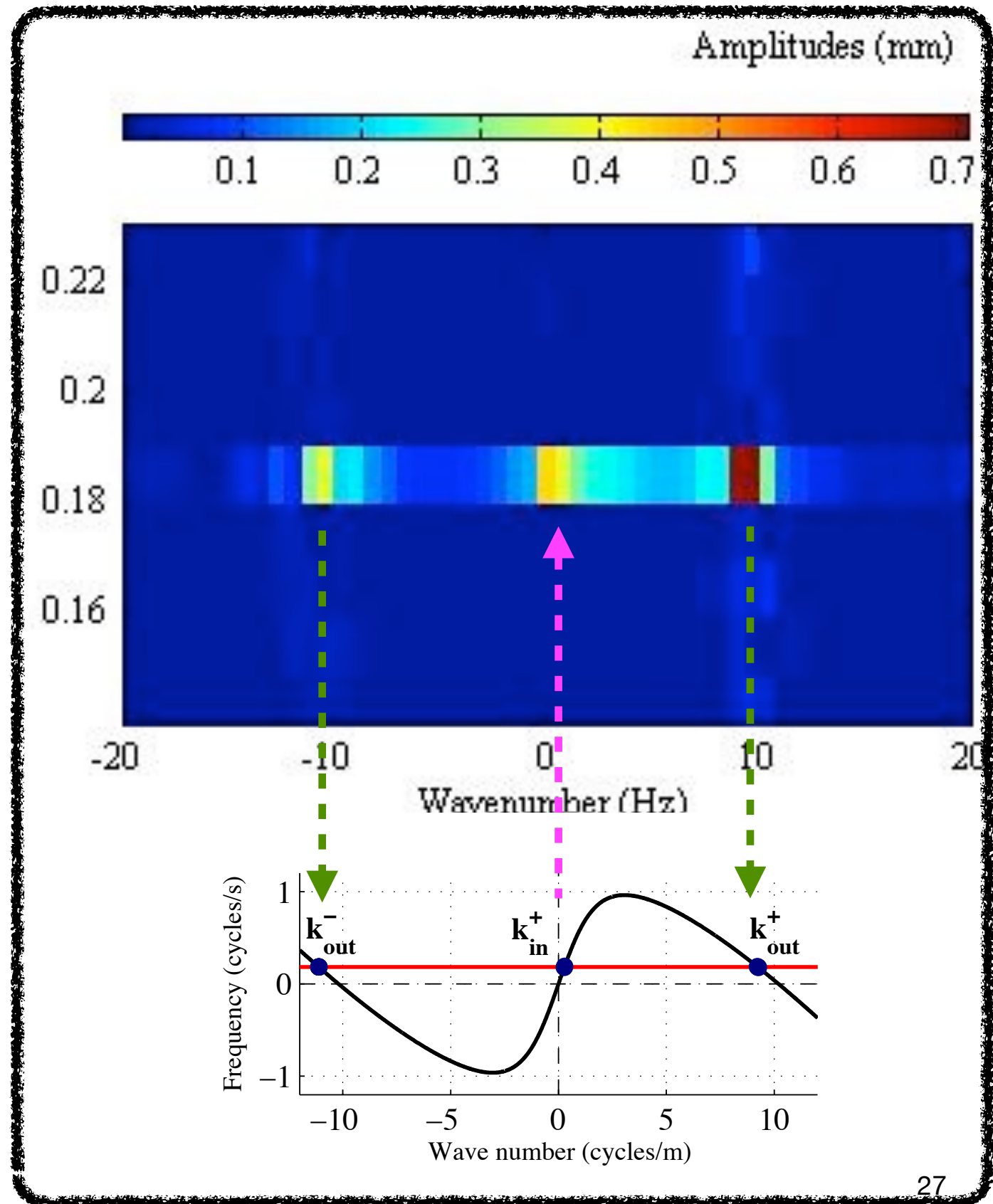
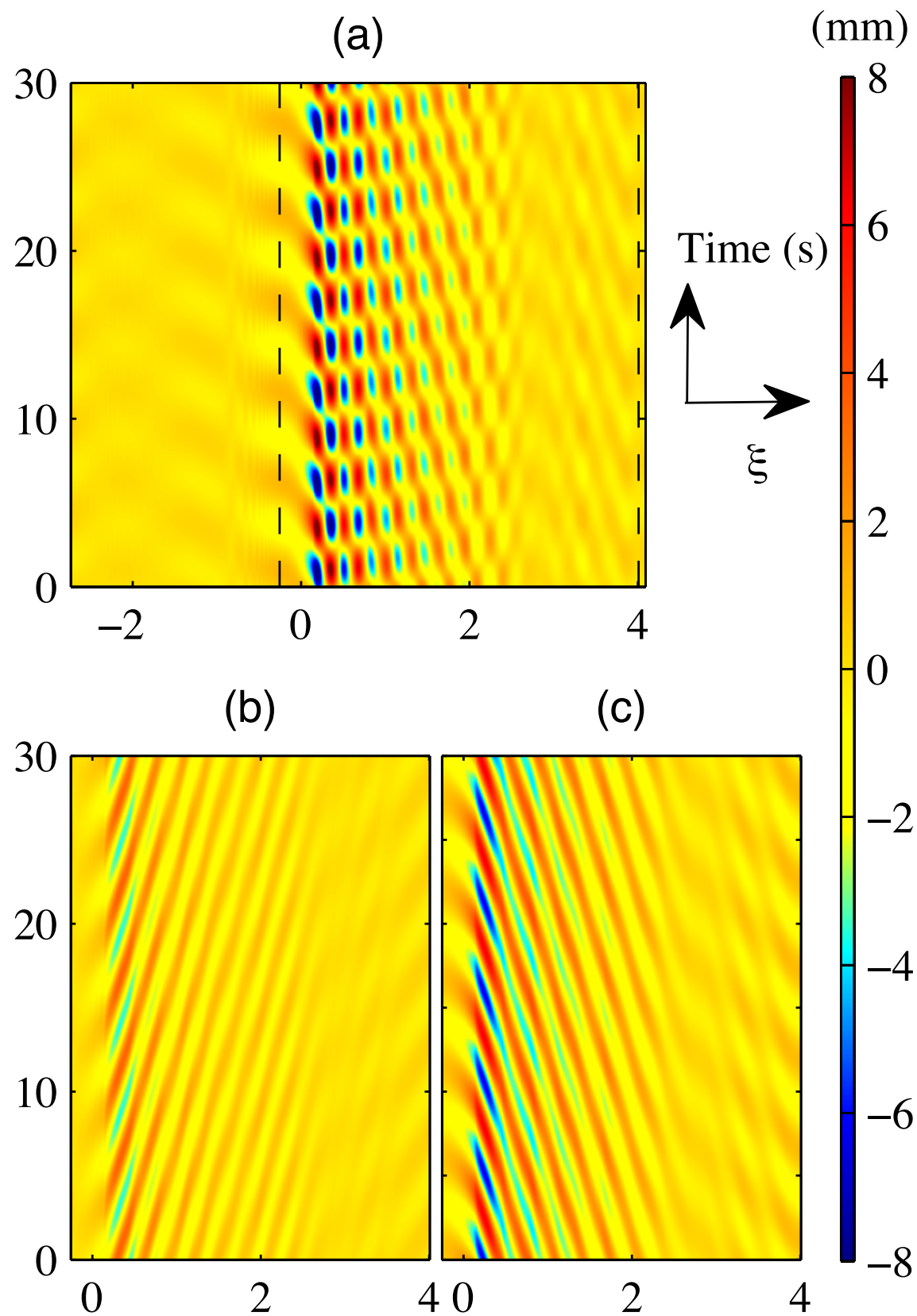


wave:
tion?

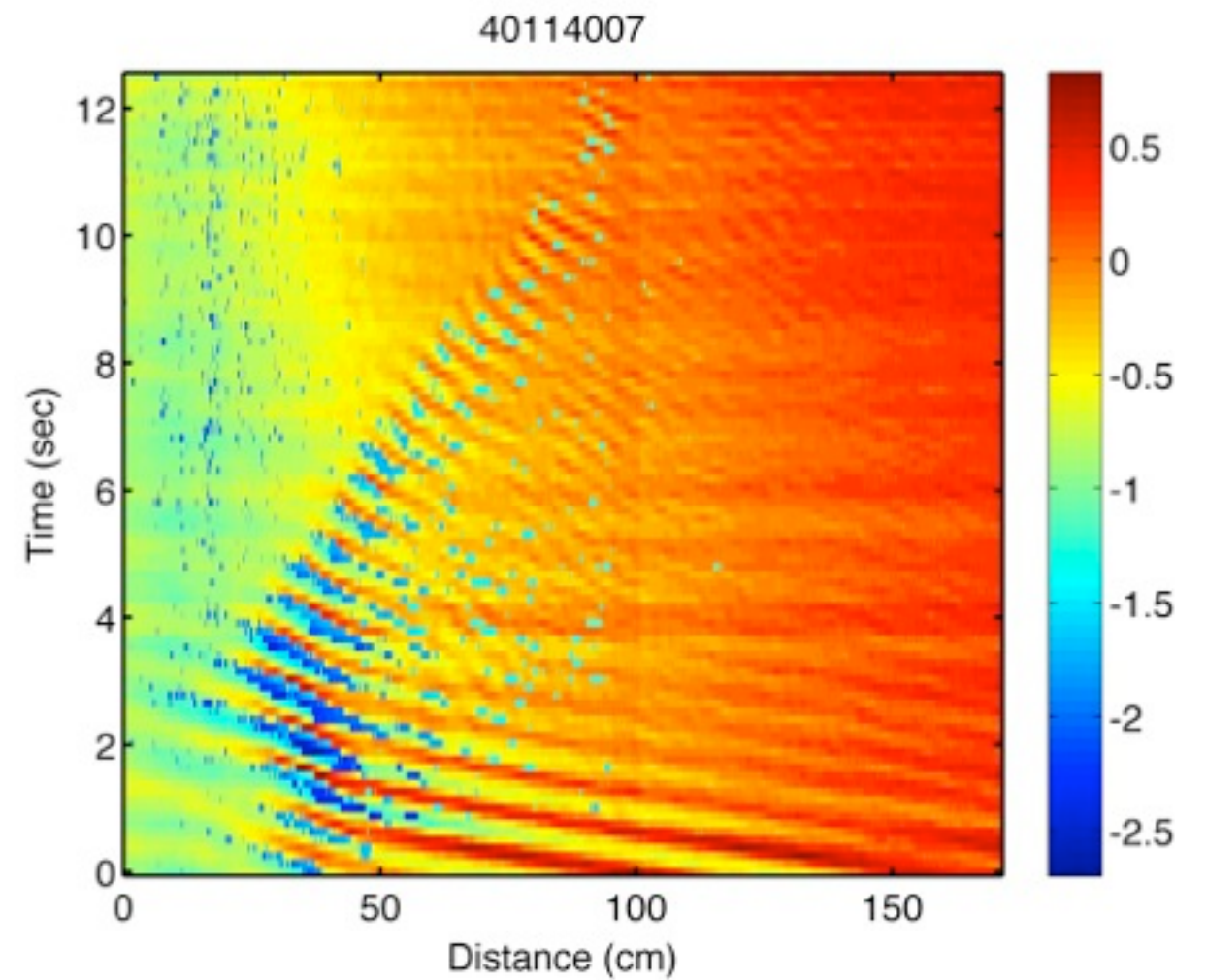
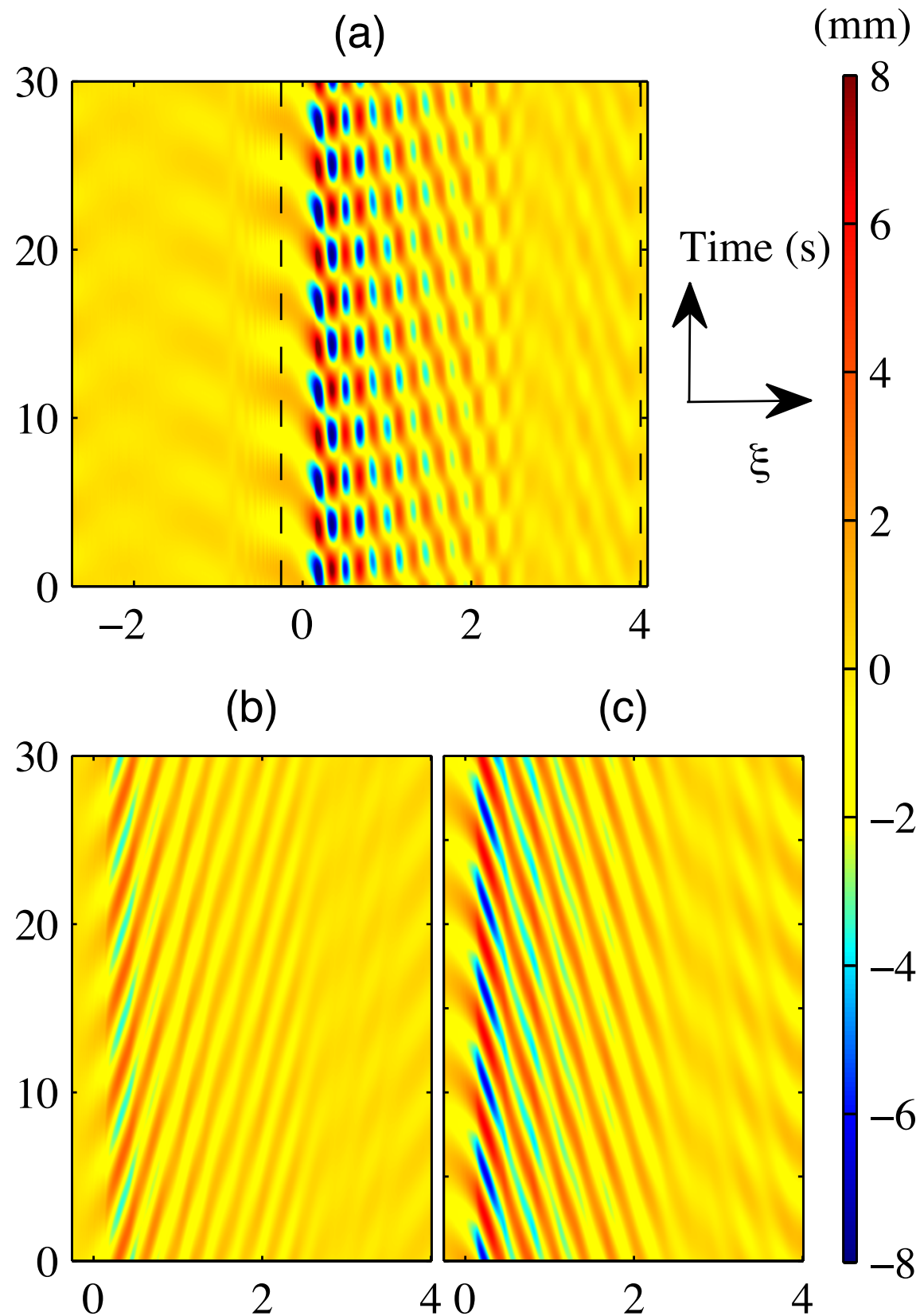
Our experiment ➤ Experimental procedure



Our experiment ➤ Pair-creation process

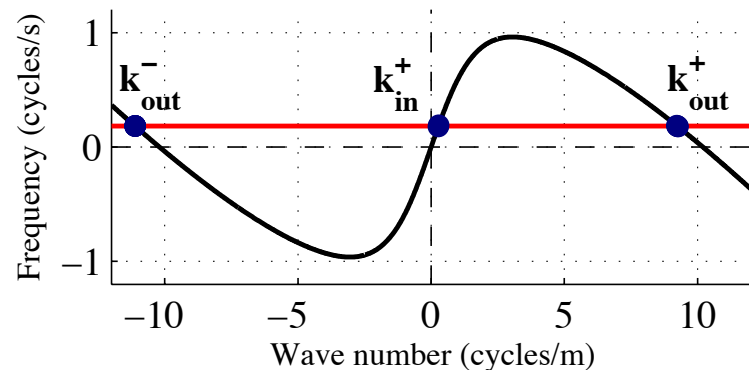


Our experiment ➤ Group versus phase velocity horizon

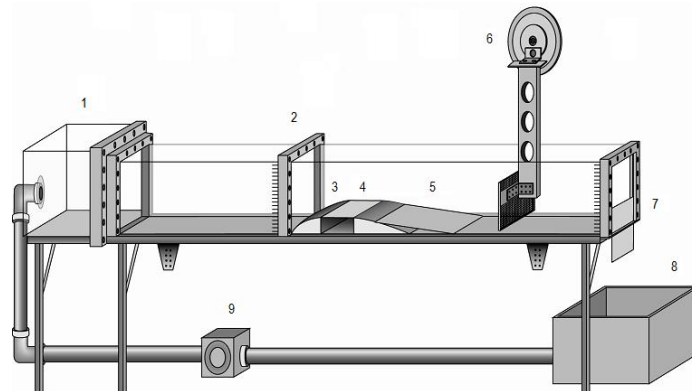
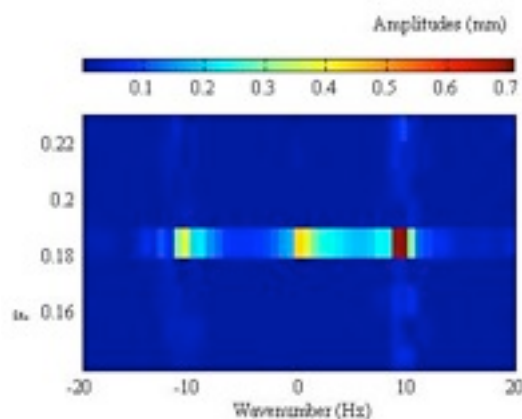


Our experiment ➤ Boltzmann distribution

(i) Amplitudes of converted waves depending on ingoing frequency:



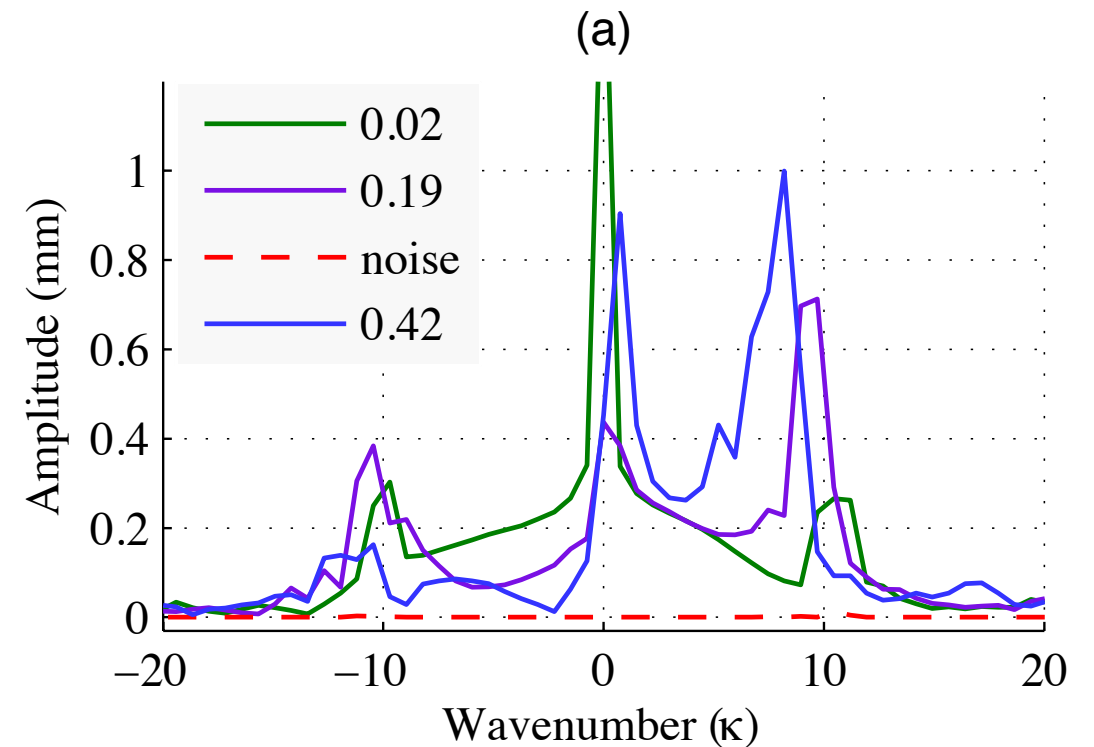
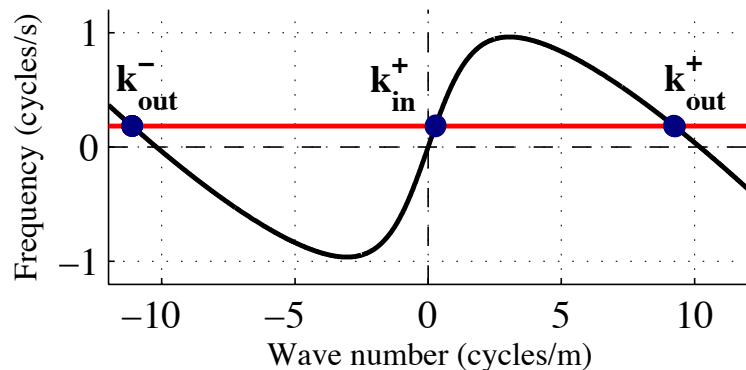
(ii) what is a wave (particle) nearby the white hole horizon..?



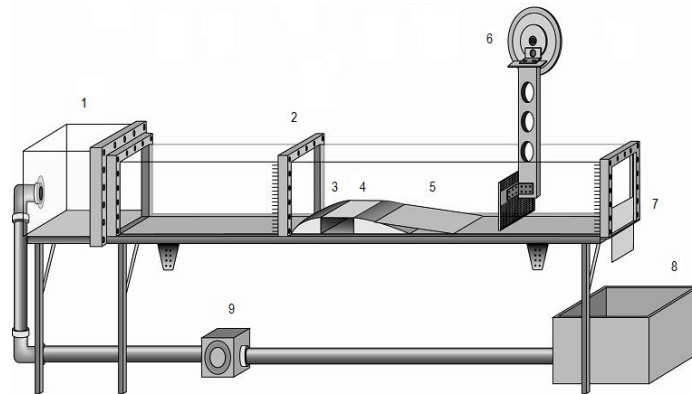
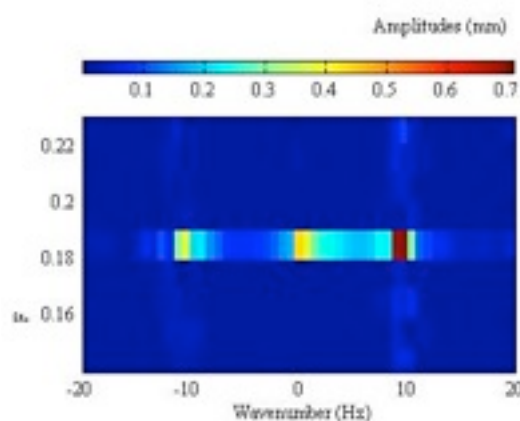
(ii) Norm is conserved: $\int \frac{|A(f, \kappa)|^2}{f + \kappa} d\kappa$

Our experiment ➤ Boltzmann distribution

(i) Amplitudes of converted waves depending on ingoing frequency:



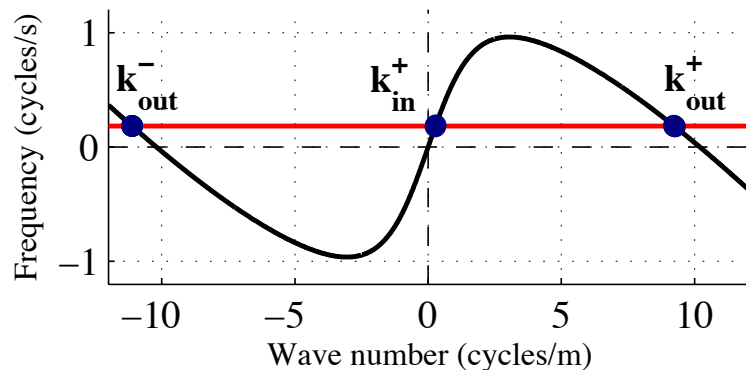
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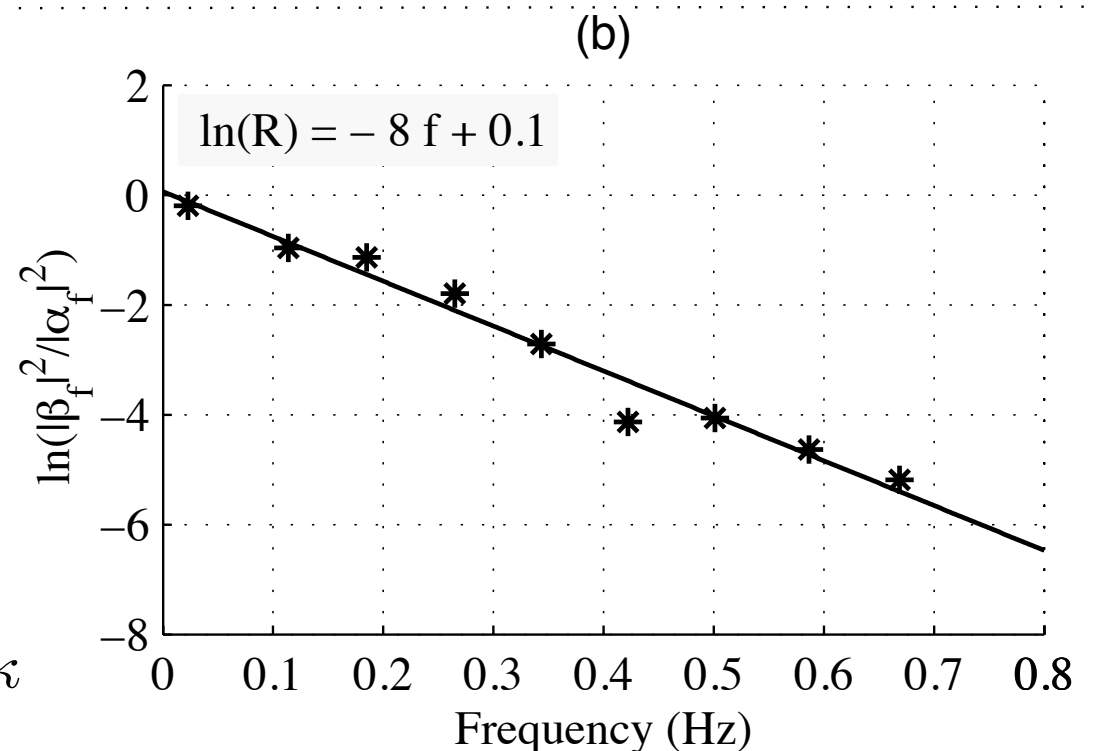
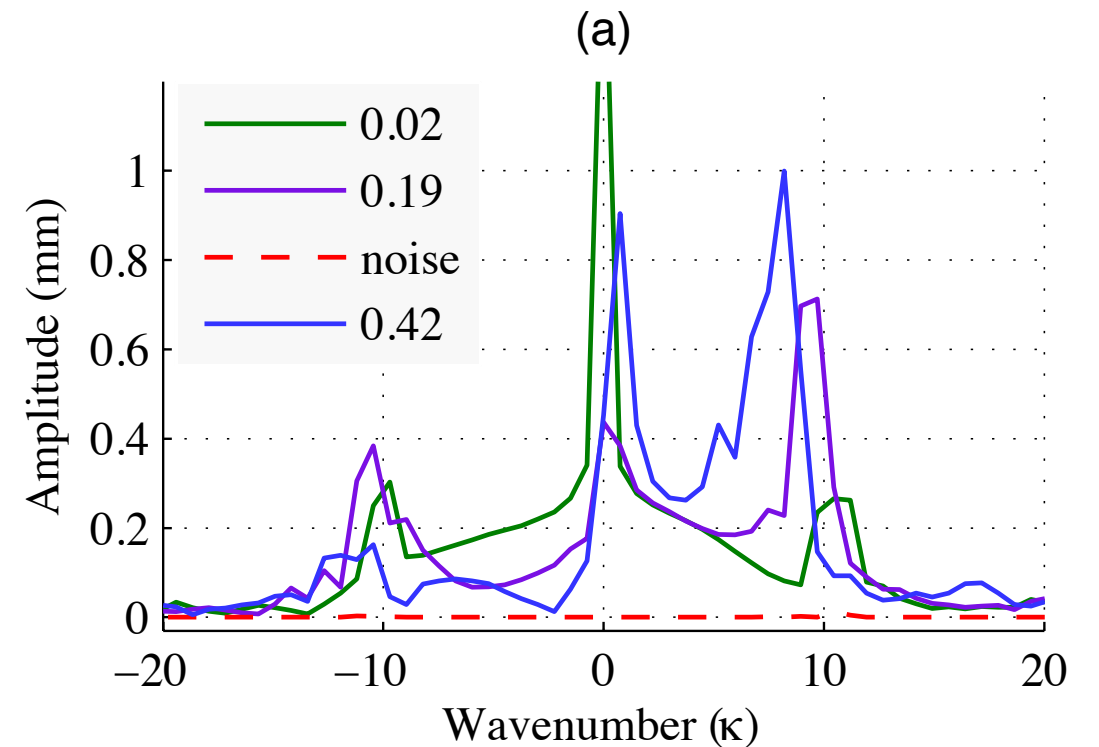
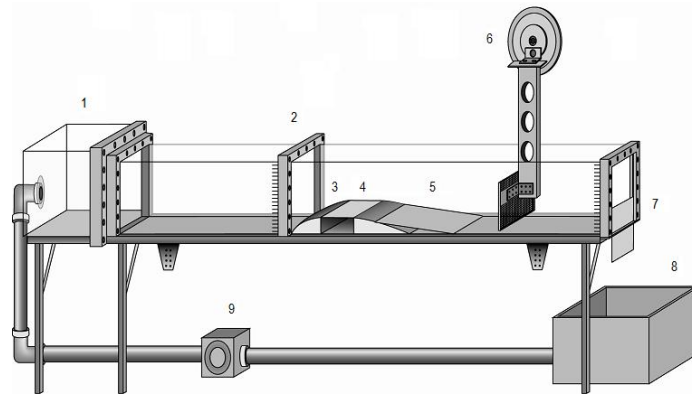
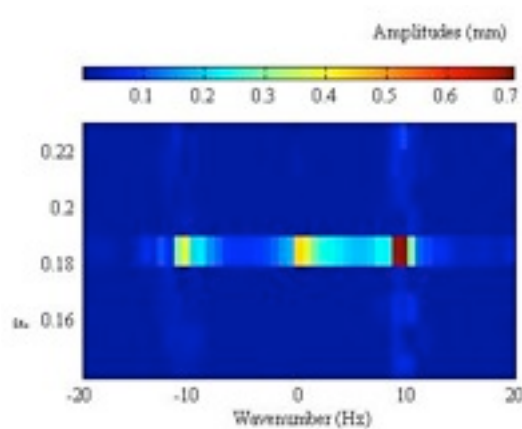
(ii) Norm is conserved:
$$\int \frac{|A(f, \kappa)|^2}{f + \kappa} d\kappa$$

Our experiment ➤ Boltzmann distribution

(i) Amplitudes of converted waves depending on ingoing frequency:



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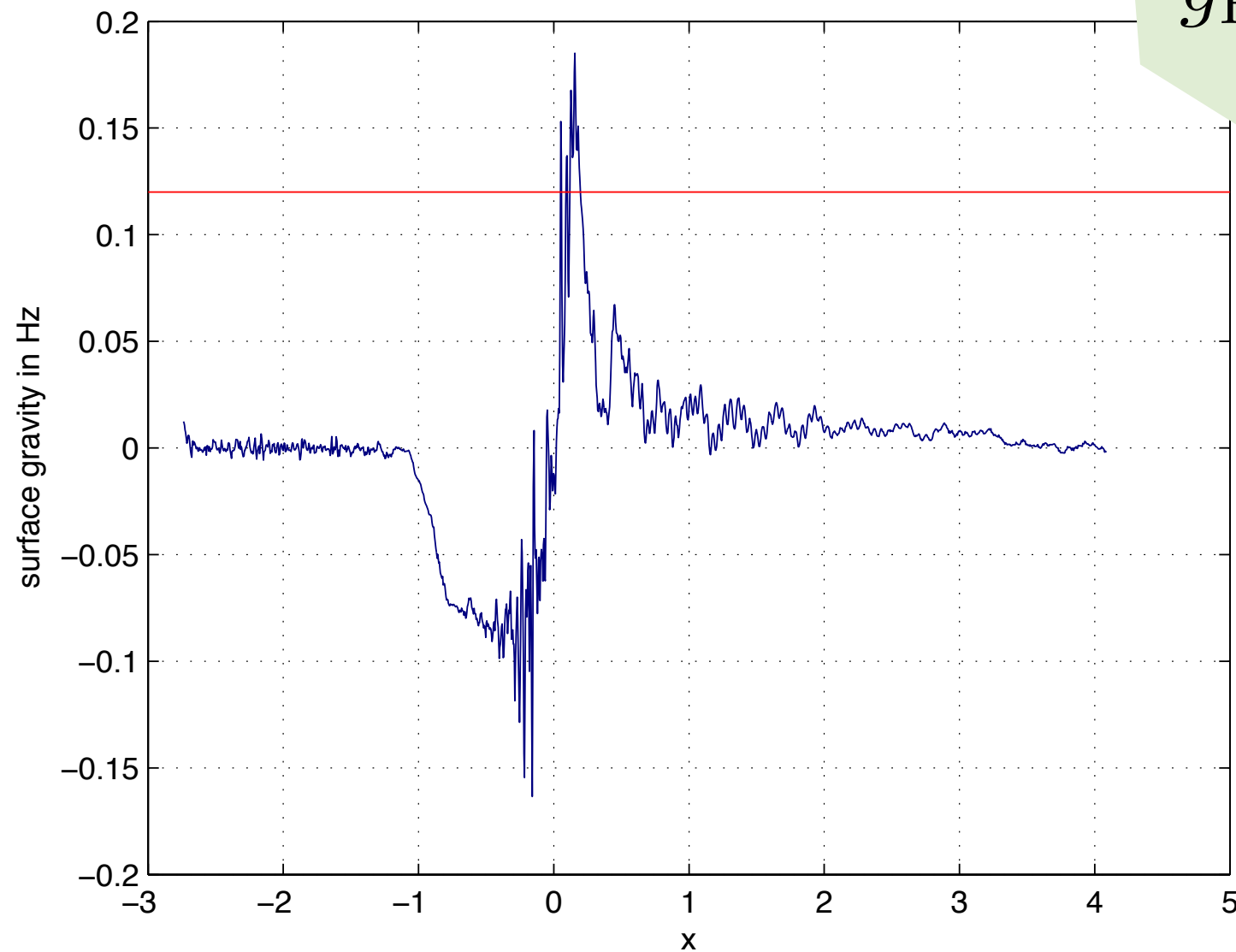


(ii) Norm is conserved: $\int \frac{|A(f, \kappa)|^2}{f + \kappa} d\kappa$

Our experiment ➤ Surface gravity

- BH evaporation: $|\beta_\omega|^2 = e^{-\frac{2\pi\omega}{g_H}} |\alpha_\omega|^2$

$$g_H = \frac{1}{2} \frac{\partial(c^2 - v^2)}{\partial n}$$



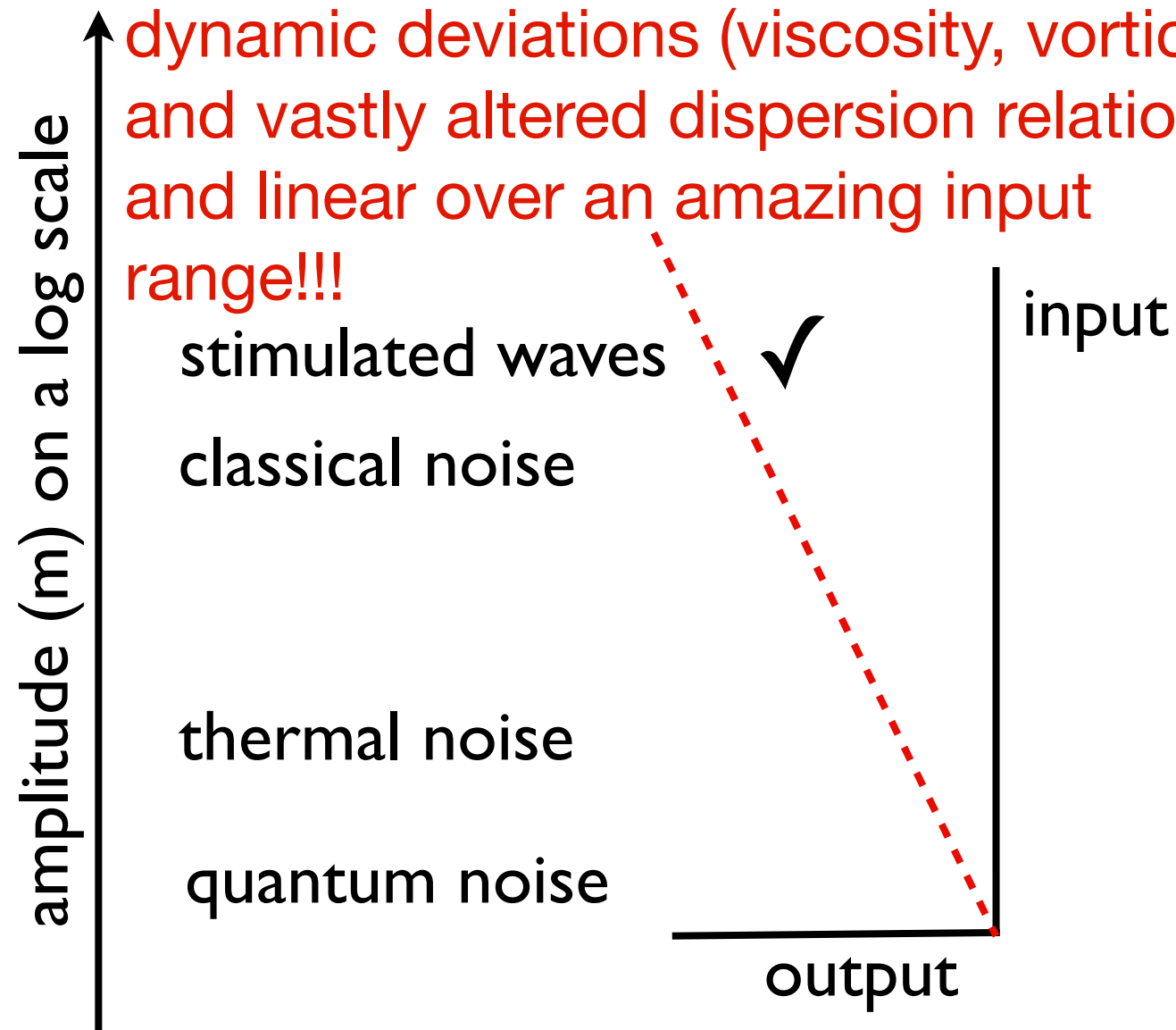
surface gravity (Hz)
via excitations:
0.12 Hz

surface gravity (Hz)
via background:
0.08-0.18 Hz

Our experiment ➤ Summary



Lesson: The thermal emission is a universal phenomenon, surviving fluid-dynamic deviations (viscosity, vorticity) and vastly altered dispersion relations, and linear over an amazing input range!!!



Assumption:

Linear amplifier over a huge range!

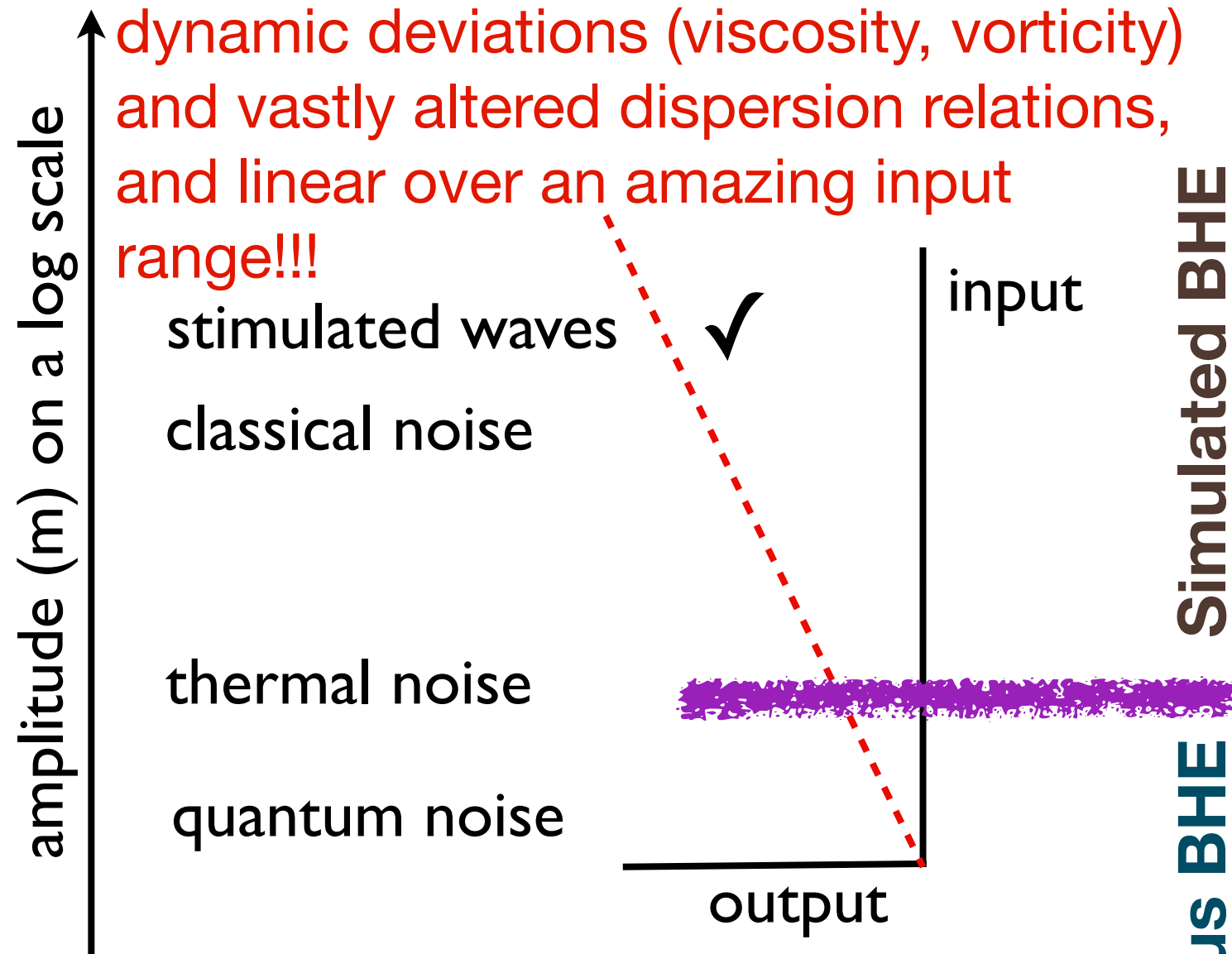
- ✓ pair-creation process (classical correlations)
- ✓ Boltzmann distribution
- ✓ surface gravity



Our experiment ➤ Summary



Lesson: The thermal emission is a universal phenomenon, surviving fluid-dynamic deviations (viscosity, vorticity) and vastly altered dispersion relations, and linear over an amazing input range!!!



Spontaneous BHE

Simulated BHE

Assumption:

Linear amplifier over a huge range!

- ✓ pair-creation process (classical correlations)
- ✓ Boltzmann distribution
- ✓ surface gravity

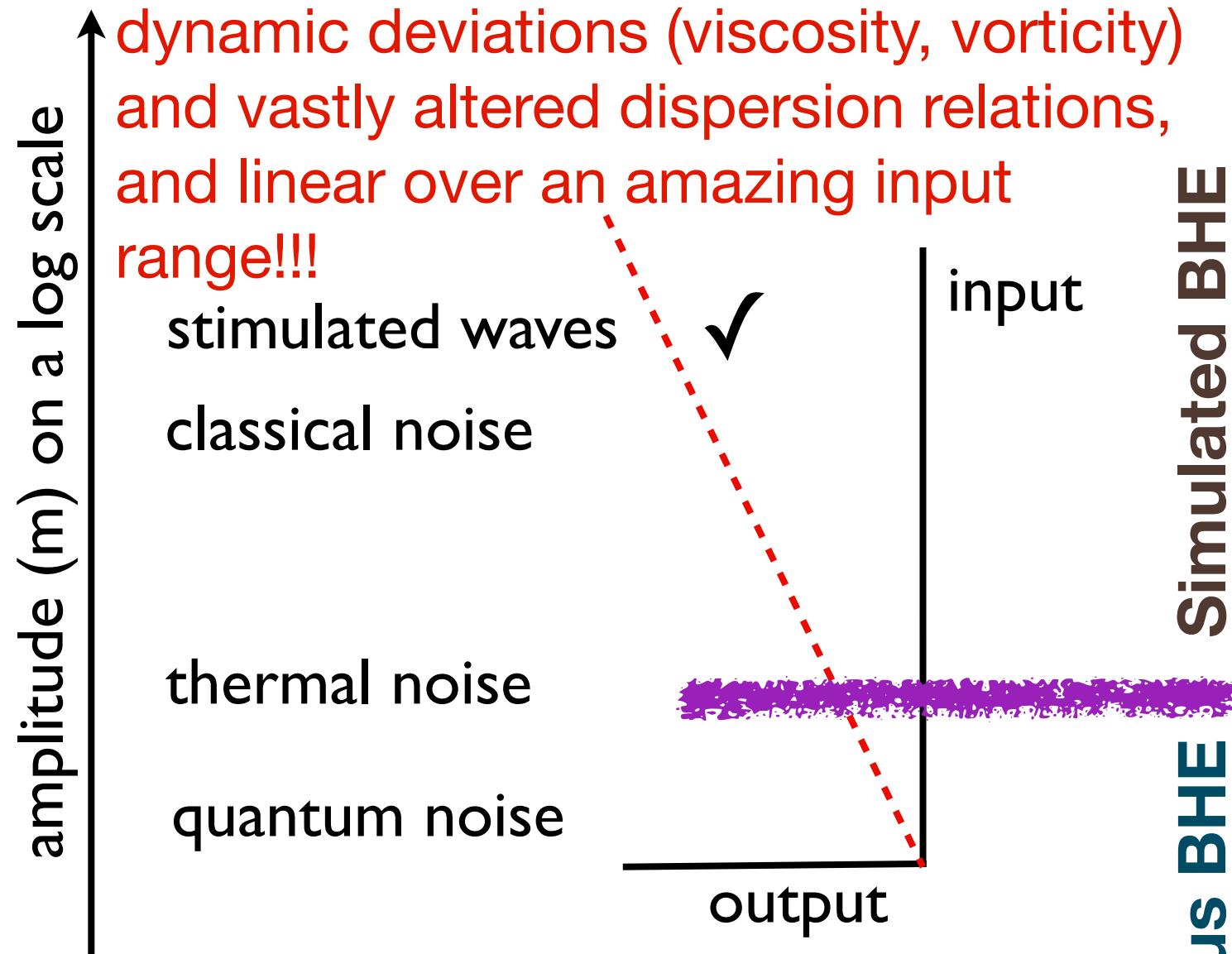


- ✓ quantum correlations

Our experiment ➤ Summary



Lesson: The thermal emission is a universal phenomenon, surviving fluid-dynamic deviations (viscosity, vorticity) and vastly altered dispersion relations, and linear over an amazing input range!!!



there is **NO UV-problem**
in our system...

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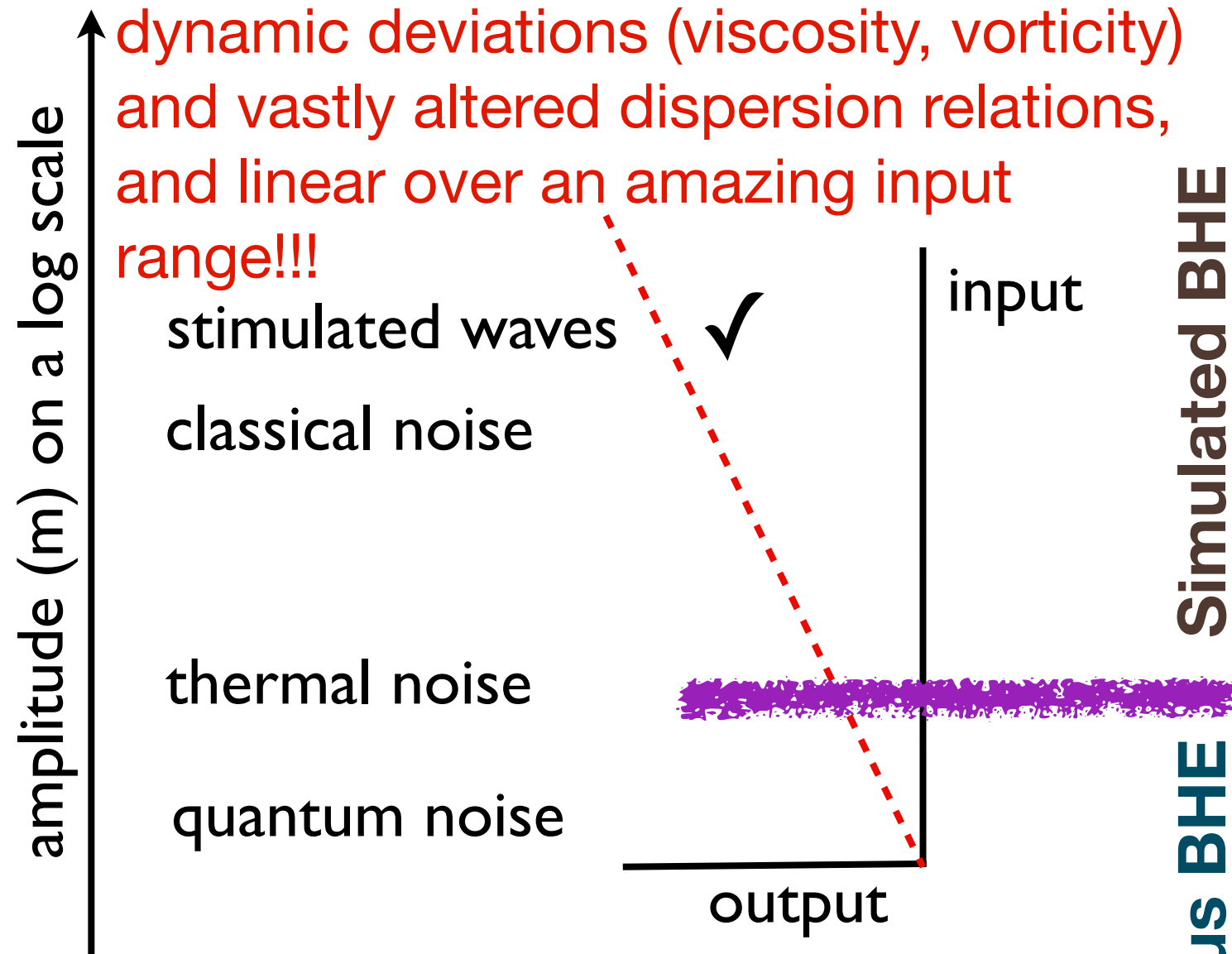


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Simulated BHE
Spontaneous BHE

Assumption:

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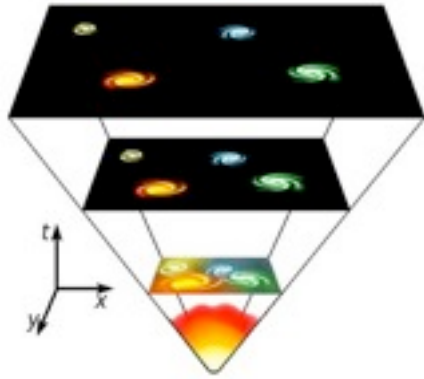


However: Spontaneous emission straightforward, but undetectable (6×10^{-12} K); superfluid experiments necessary...

- ✓ quantum correlations

there is **NO UV-problem** in our system...

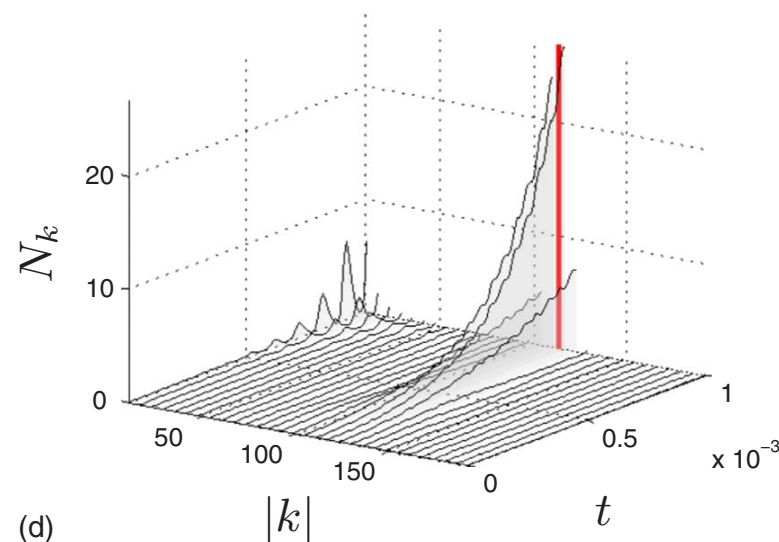
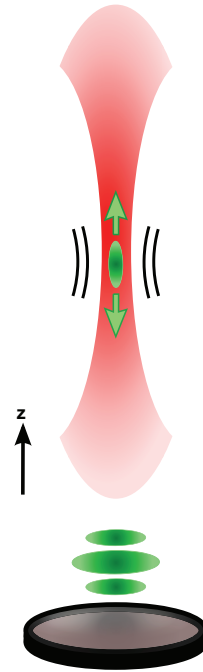
Other experiment(s) ➤ Classical versus quantum?



Example 3:

Cosmological particle production

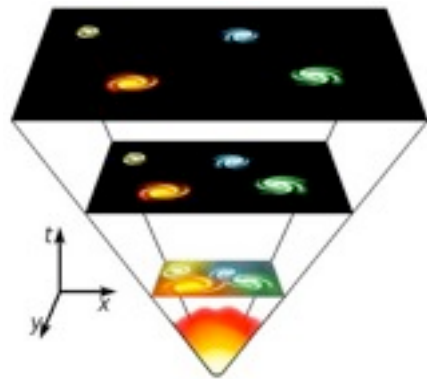
Cyclic universe:



(d)

'Analogue model of a FRW universe in Bose-Einstein condensates: Application of the classical field method', Phys. Rev. A 76, 033616 (2007), P. Jain, S.W., M. Visser and C. W. Gardiner.

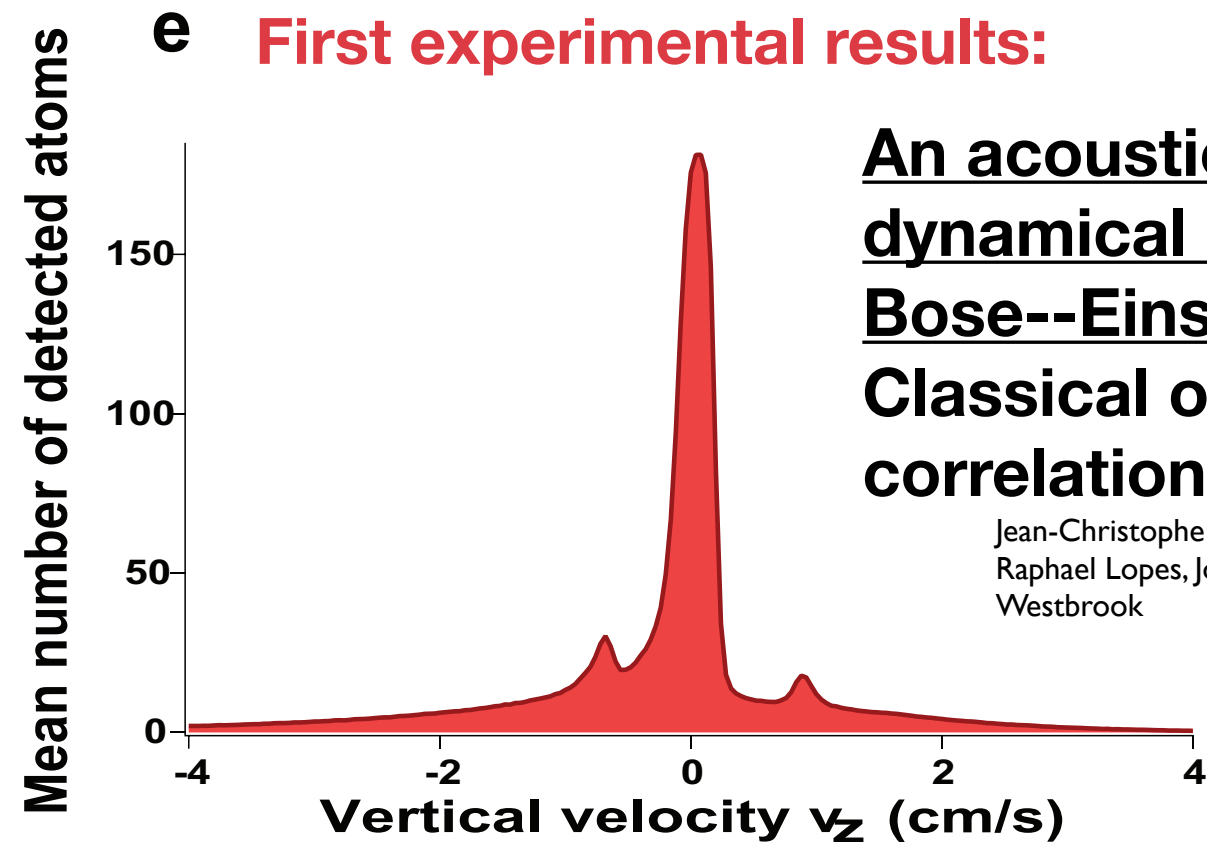
Other experiment(s) ➤ Classical versus quantum?



Example 3:

Cosmological particle production

Cyclic universe:



Phys. Rev. Lett. 108, 260401 (2012) [5 pages]

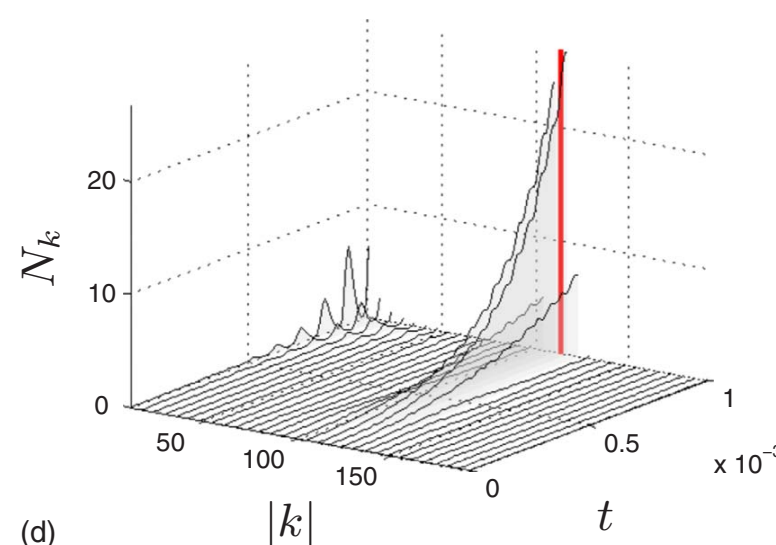
Violation of the Cauchy-Schwarz Inequality with Matter Waves

K. V. Kheruntsyan¹, J.-C. Jaskula^{2,*}, P. Deuar³, M. Bonneau², G. B. Partridge^{2,†}, J. Ruaudel², R. Lopes², D. Boiron², and C. I. Westbrook²

¹The University of Queensland, School of Mathematics and Physics, Brisbane, Queensland 4072, Australia

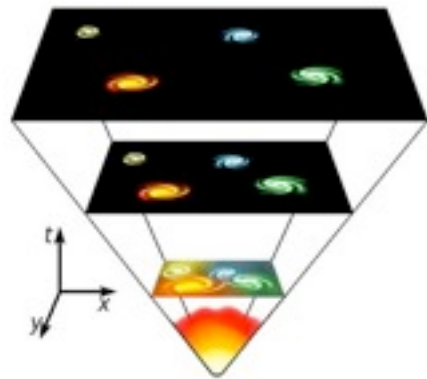
²Laboratoire Charles Fabry de l'Institut d'Optique, CNRS, Université Paris-Sud, Campus Polytechnique RD128, 91127 Palaiseau, France

³Institute of Physics, Polish Academy of Sciences, Al. Lotników 32/46, 02-668 Warsaw, Poland



'Analogue model of a FRW universe in Bose-Einstein condensates: Application of the classical field method', Phys. Rev. A 76, 033616 (2007), P. Jain, S.W., M. Visser and C. W. Gardiner.

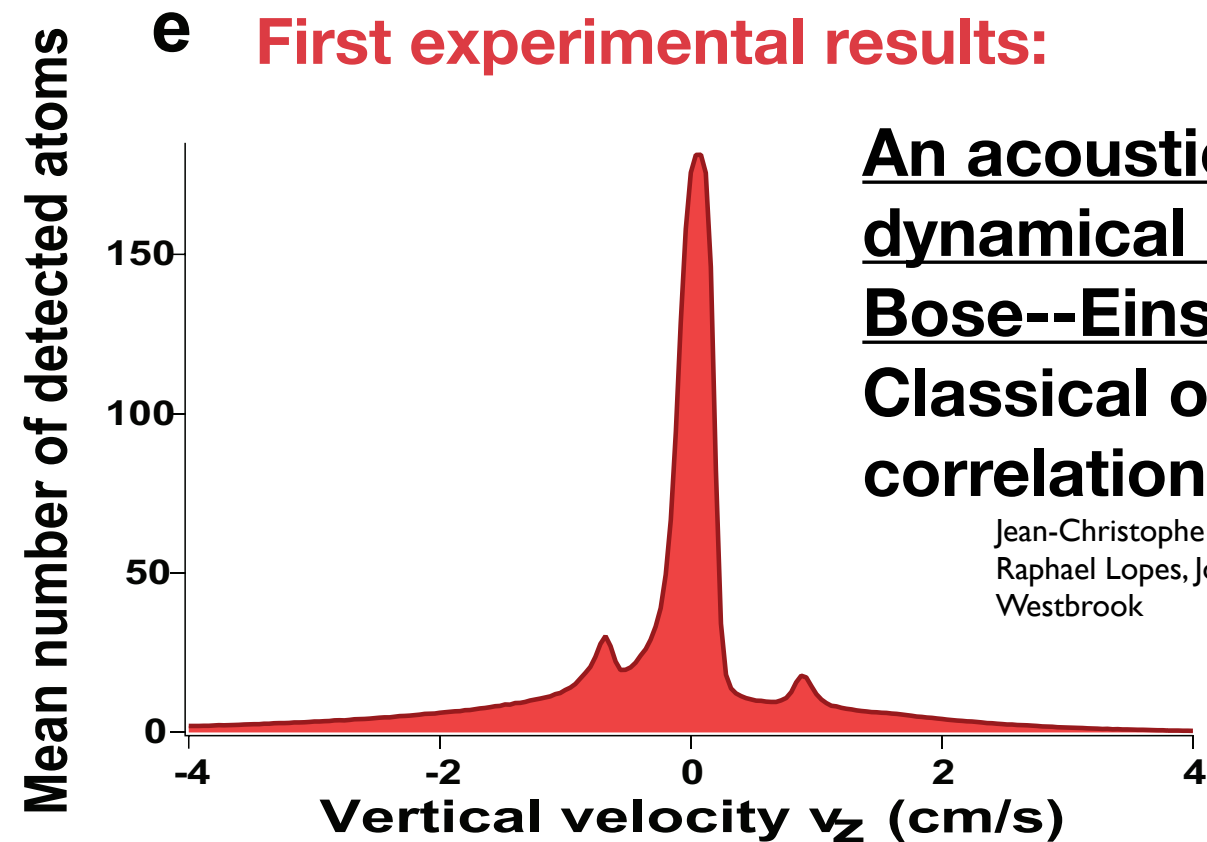
Other experiment(s) ➤ Classical versus quantum?



Example 3:

Cosmological particle production

Cyclic universe:



An acoustic analog to the dynamical Casimir effect in a Bose-Einstein condensate: Classical or quantum correlations?

Jean-Christophe Jaskula, Guthrie B. Partridge, Marie Bonneau, Raphael Lopes, Josselin Ruaudel, Denis Boiron, Christoph I Westbrook

Phys. Rev. Lett. 108, 260401 (2012) [5 pages]

Violation of the Cauchy-Schwarz Inequality with Matter Waves

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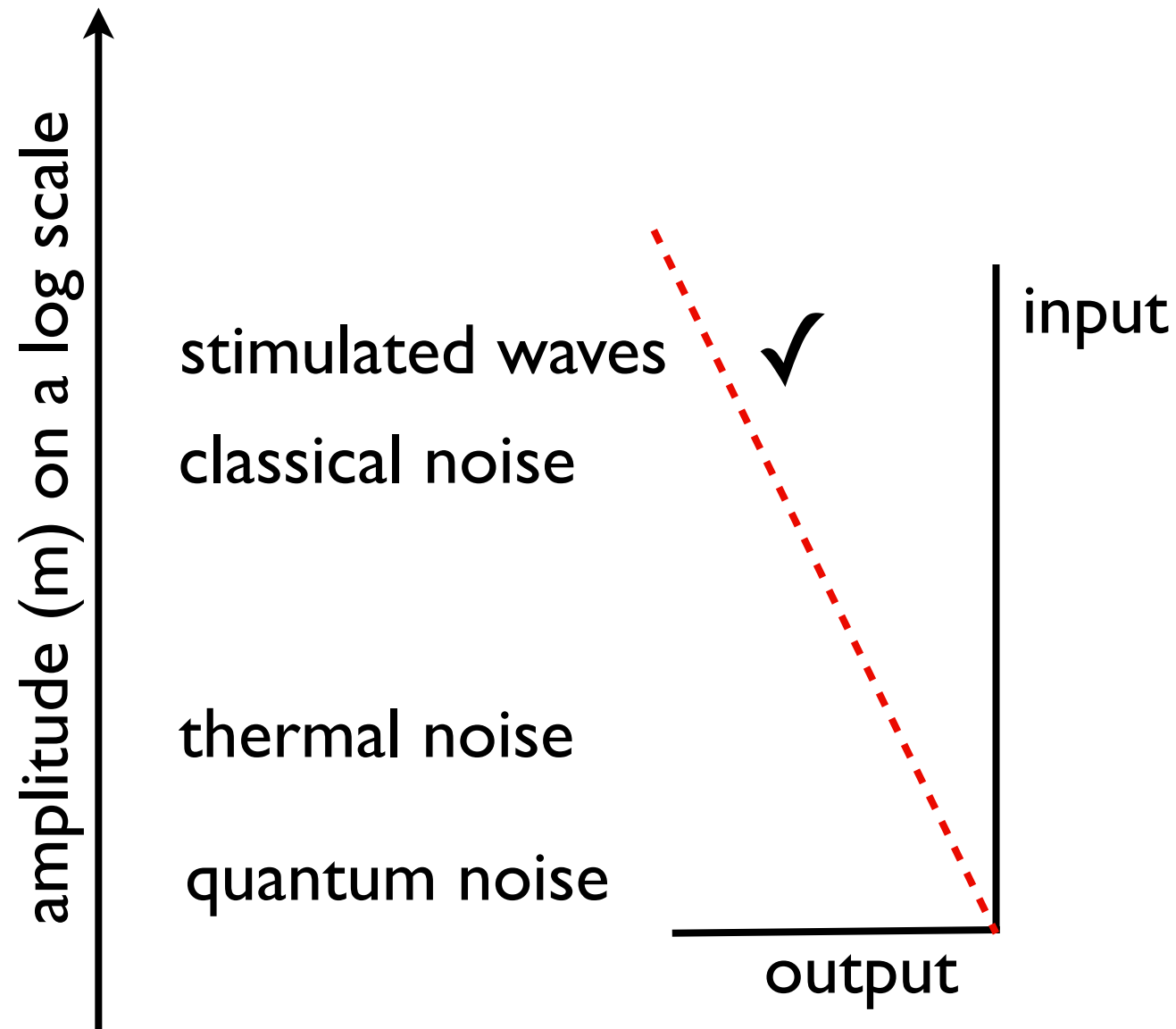
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²Laboratoire Charles Fabry de l'Institut d'Optique, CNRS, Université Paris-Sud, Campus Polytechnique RD128, 91127 Palaiseau, France

³Institute of Physics, Polish Academy of Sciences, Al. Lotników 32/46, 02-668 Warsaw, Poland

No stronger-than-classical correlations detected...

Our experiment ➤ “Quantum” field theory in CS..?



Assumption:

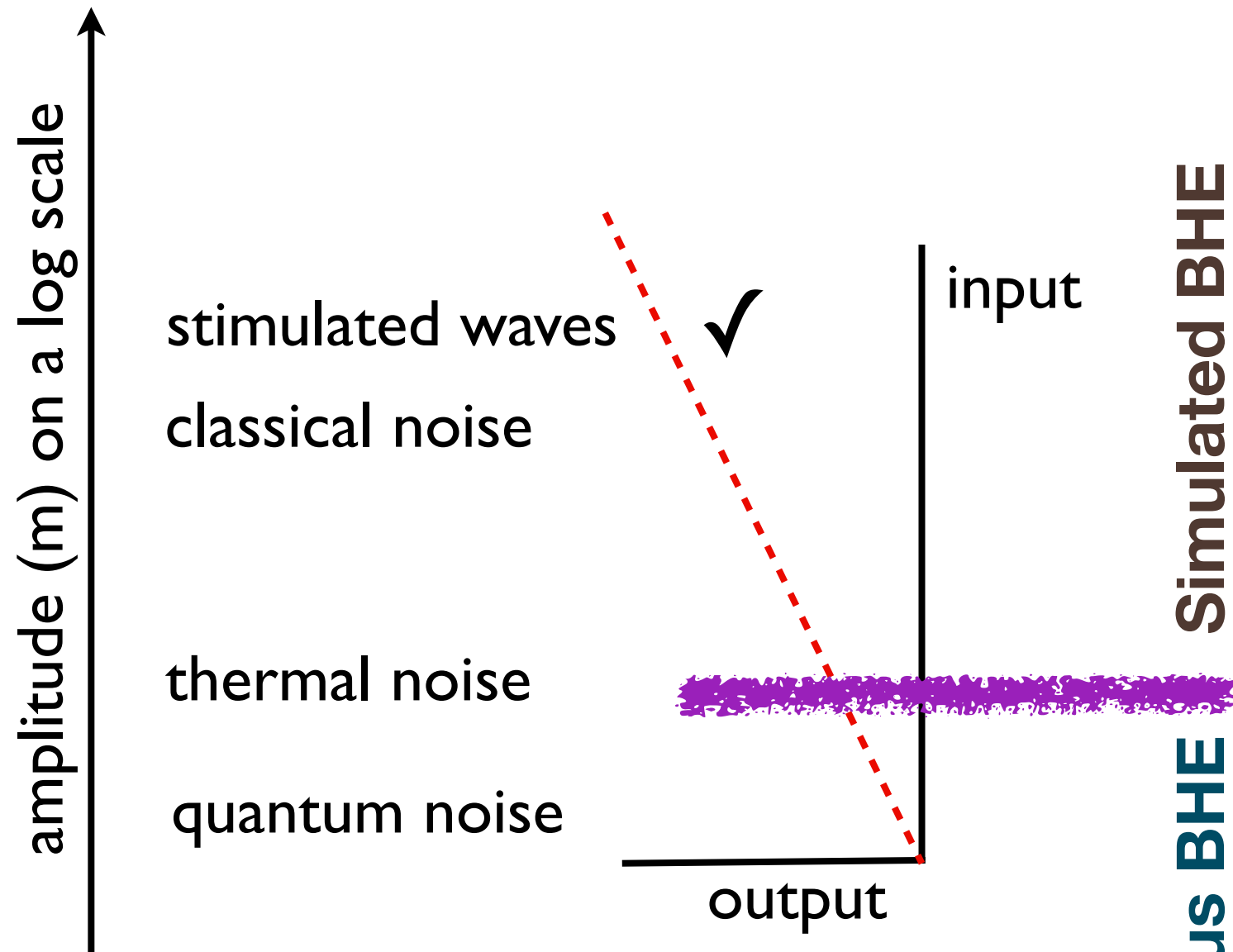
Linear amplifier over a huge range!

- ✓ pair-creation process (classical correlations)
- ✓ Boltzmann distribution
- ✓ surface gravity



“Quantum” Field Theory in curved spacetimes...?

Our experiment ➤ “Quantum” field theory in CS..?



Simulated BHE

Spontaneous BHE

Assumption:

Linear amplifier over a huge range!

- ✓ pair-creation process (classical correlations)
- ✓ Boltzmann distribution
- ✓ surface gravity



- ✓ quantum correlations

“Quantum” Field Theory in curved spacetimes...?

Summary ➤ Results from AM experiments

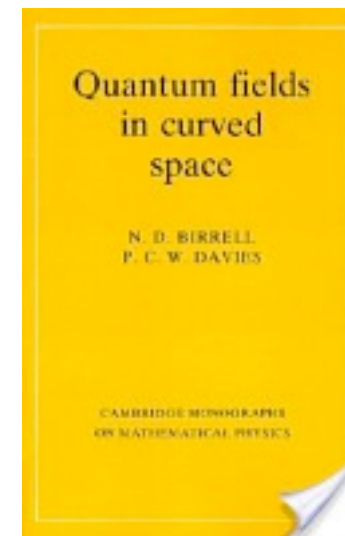
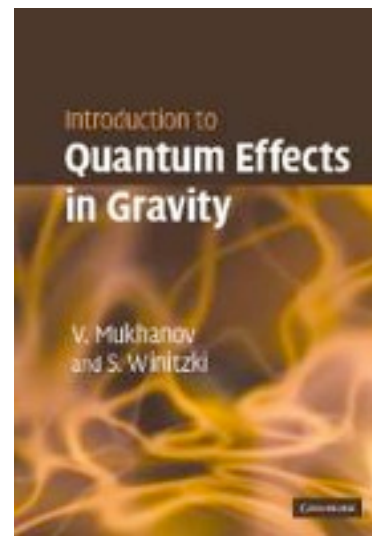
Analogue Gravity experiments	Vancouver: stimulated white hole emission	Daniele Faccio: spontaneous white hole emission	Westbrook: cosmological particle production
Pair-creation (classical correlations)	✓	?	✓
Boltzmann distribution	✓	? (impossible)	irrelevant
Effective gravity (determines physics)	✓	unclear	✓
Quantum correlations	impossible	?	tested, outcome so far negative ✓

Summary ➤ Results from AM experiments

Analogue Gravity experiments	Vancouver: stimulated white hole emission	Daniele Faccio: spontaneous white hole emission	Westbrook: cosmological particle production
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Quantum correlations	impossible	?	tested, outcome so far negative ✓
Interesting Physics	✓	✓	✓

Summary ➤ Results from AM experiments

(Q)FT in curved spacetimes



**Fluid
dynamics**

**Optical
systems**

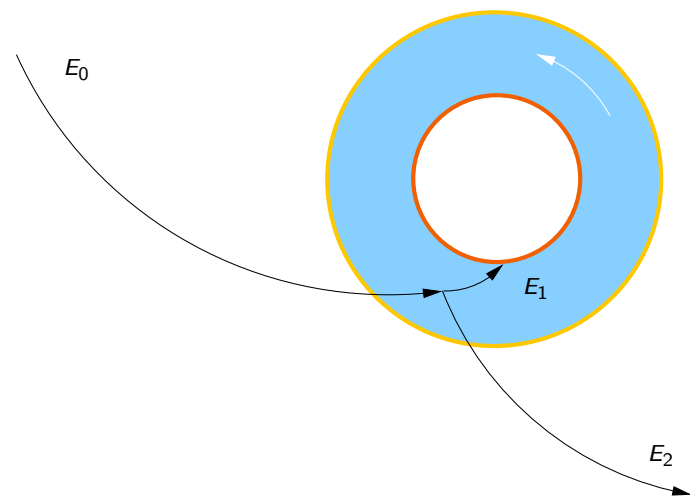
**Ultra-cold
atoms**

Interesting Physics	✓	✓	✓
------------------------	---	---	---

New experiment - ongoing experiments at SISSA

Description: Experimental studies of effective rotating black holes, to detect:

- superradiant wave-scattering
- stimulated black-hole emission



Surface waves on stationary draining water / bathtub vortex / analogue rotating black hole...



... superfluid bathtub vortex flows

Theoretical studies:

- * Vortex geometry for the equatorial slice of the Kerr black hole (M. Visser, S.W.);
- * **In preparation:** Generalized superradiant scattering (M. Richartz, S.W., A.J. Penner, W.G. Unruh);
- * **ArXiv:** Dispersive superradiant scattering (A. Prain, M. Richartz, S.W., S. Liberati)

Numerical studies:

- * In preparation: Experimental superradiant scattering (M. Richartz, J. Penner, A. Prain, J. Niemela, S.W.)

Experiment studies:

- * surface wave detection
- * design for water flume
- * prototype ready for experiments
- * big water flume (3 x 1.5 x 0.5 meter) under construction

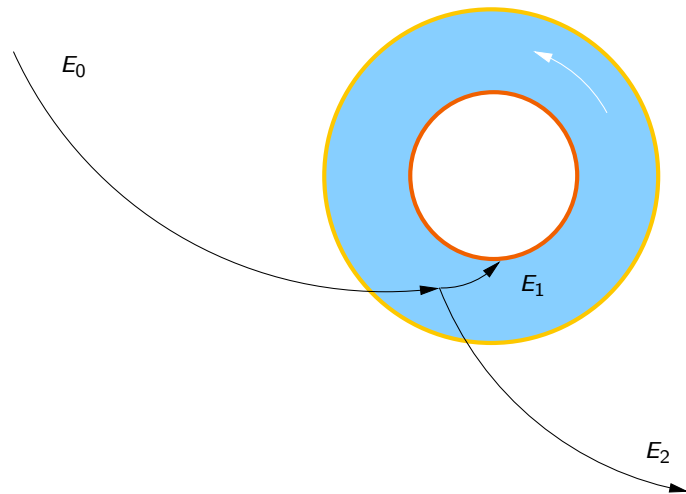


The team:

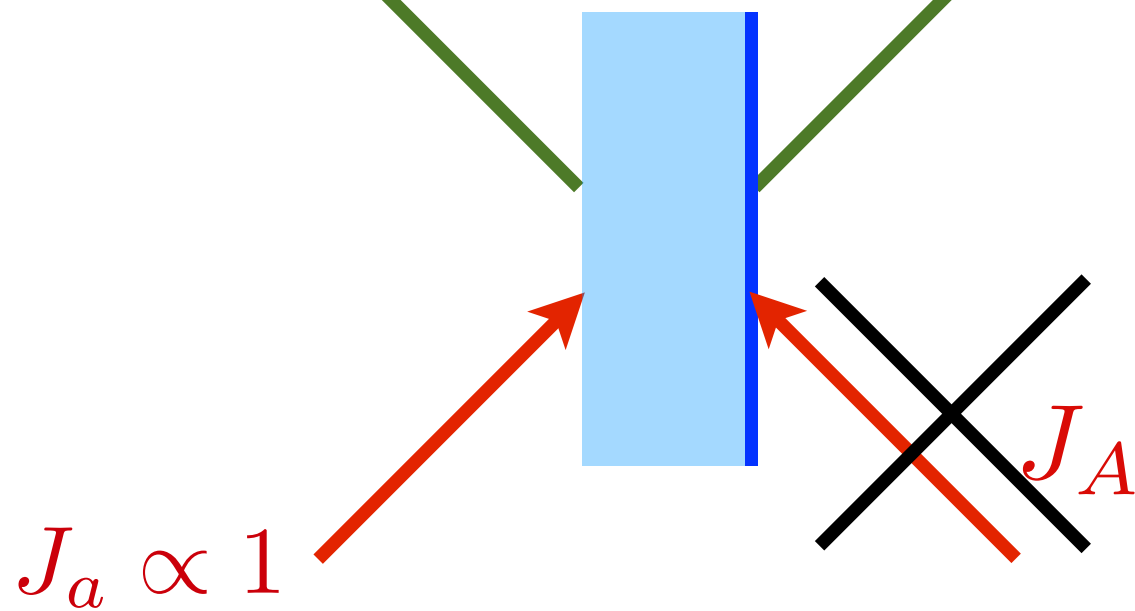
- * *Prof. J. Niemela* (ICTP), Prof. S. Liberati (SISSA), Dr. M. Richartz (Brasil), Dr. J. Penner (France), Dr. M. Danailov, A. Prain, M. Penrice

New experiment ➤ Superradiant wave scattering

Particle current: $J_n := |A_n|^2 \Omega|_{\pm\infty} \frac{d\omega}{dk} \Big|_{k_n}$



$$J_b \propto |\alpha_\omega|^2 \quad J_B \propto -\frac{(\omega - m\Omega_{BH})}{\omega} |\beta_\omega|^2$$



$$|R|^2 = 1 - \frac{(\omega - m\Omega_{BH})}{\omega} |T|^2$$

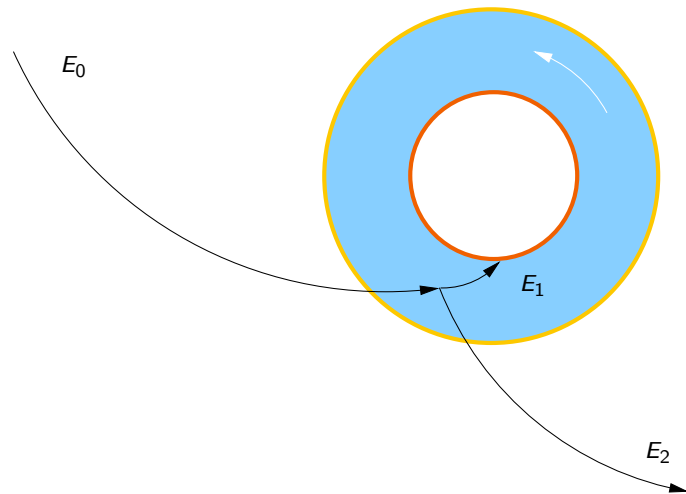
$$1 + 0 = |\alpha_\omega|^2 + \frac{(\omega - m\Omega_{BH})}{\omega} |\beta_\omega|^2$$

Dispersive superradiant scattering (A. Prain, M. Richartz, S.W., S. Liberati)

Rotating Black holes: Linear Classical and Quantum Field Amplifier!³⁶

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