



The Abdus Salam  
**International Centre**  
for Theoretical Physics



**2356-16**

**Targeted Training Activity: ENSO-Monsoon in the Current and Future Climate**

*30 July - 10 August, 2012*

**ENSO: Role of the Ocean**

KIRTMAN Benjamin Paul  
*Rosenstiel School of Marine and Atmospheric Science, University of Miami  
4600 Rickenbacker Causeway Miami 33149  
Florida  
U.S.A.*

UNIVERSITY  
OF MIAMI

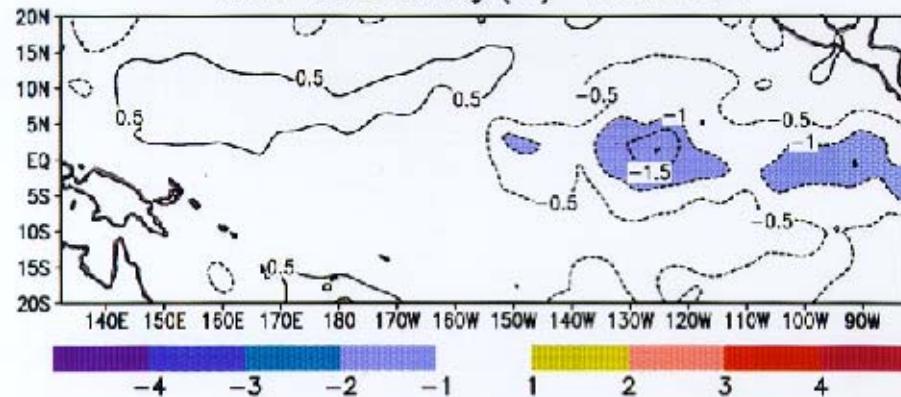
ROSENSTIEL  
SCHOOL OF MARINE &  
ATMOSPHERIC SCIENCE



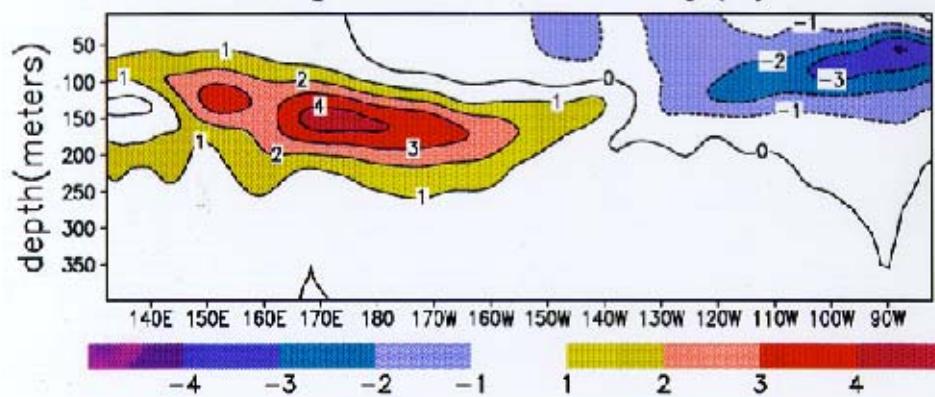
# ENSO: Role of the Ocean

Ben Kirtman  
University of Miami – Rosenstiel School

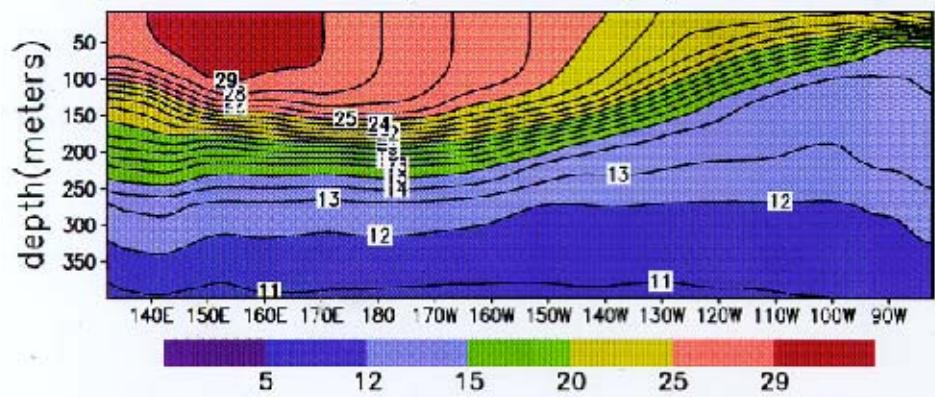
SST Anomaly(C) JAN1997



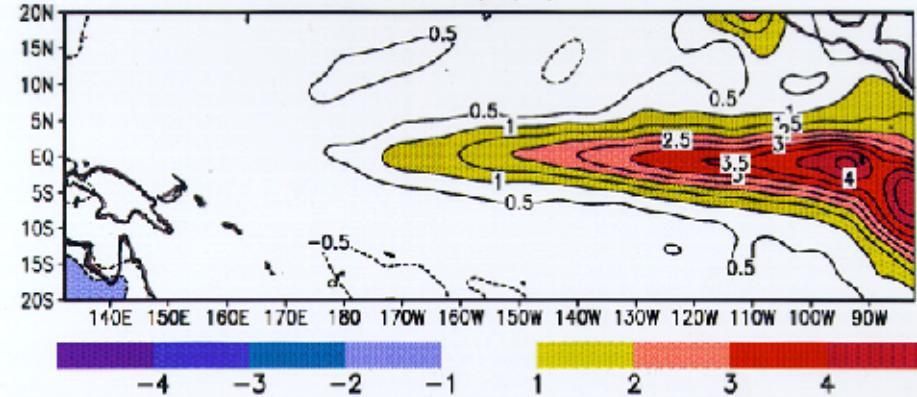
Ocean Temperature Anomaly(C) JAN1999



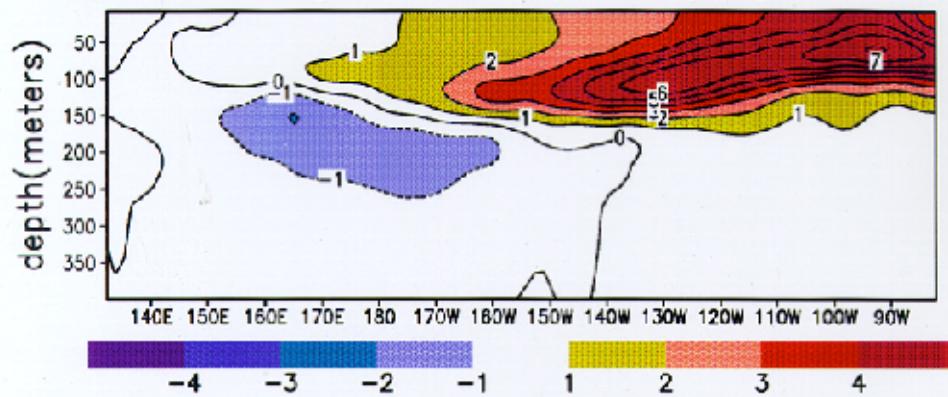
Ocean Temperature (C) JAN1997



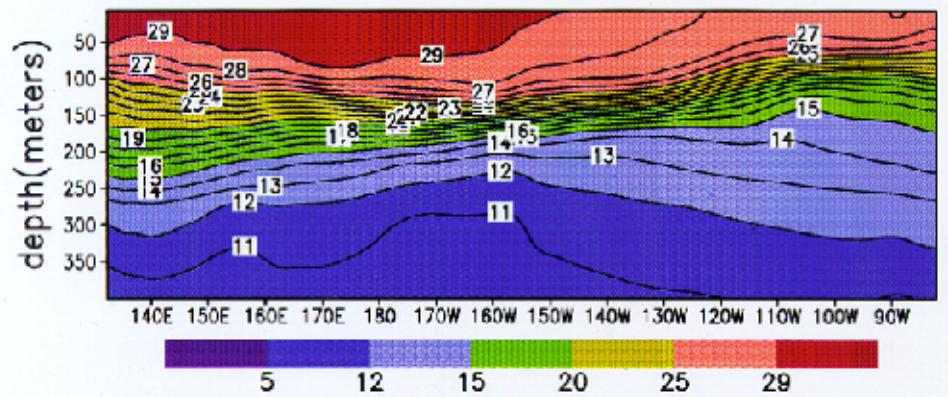
SST Anomaly(C) JUL1997



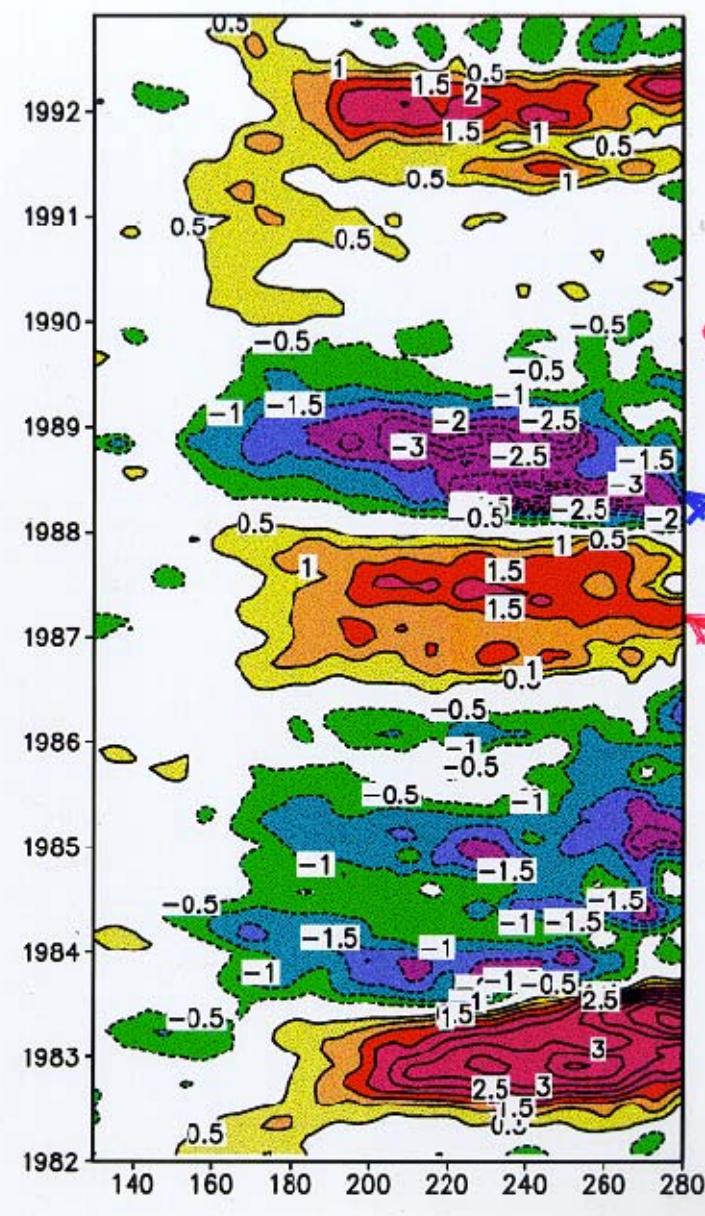
Ocean Temperature Anomaly(C) JUL1997



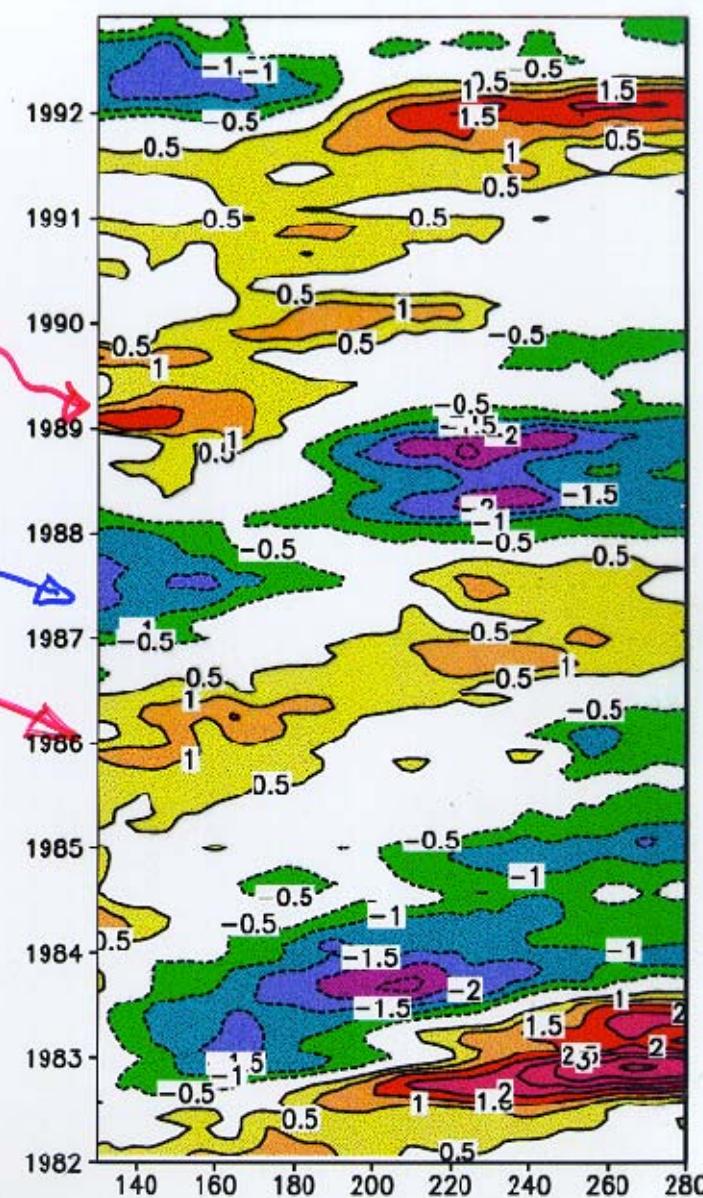
Ocean Temperature (C) JUL1997



### Observed SSTAs



### Observed Heat Content



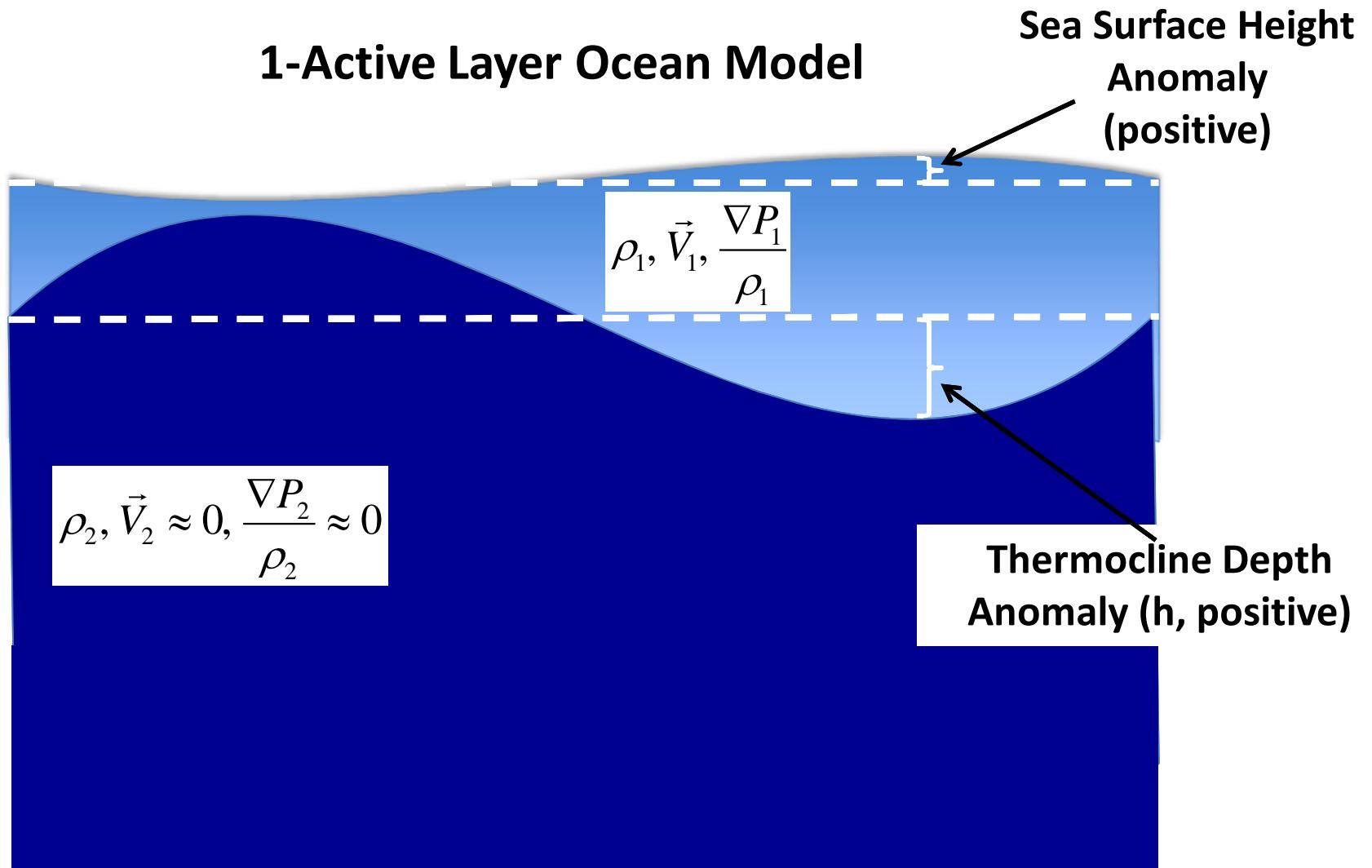
Sufficient?

# Outline

- **Free Equatorial Waves**
  - Rossby and Kelvin Wave
- **Forced Equatorial Waves**
  - Equatorial Sverdrup Balance
- **Coupled Problem**
  - Delayed Oscillator, Recharge Oscillator, Fast Wave – Slow SST

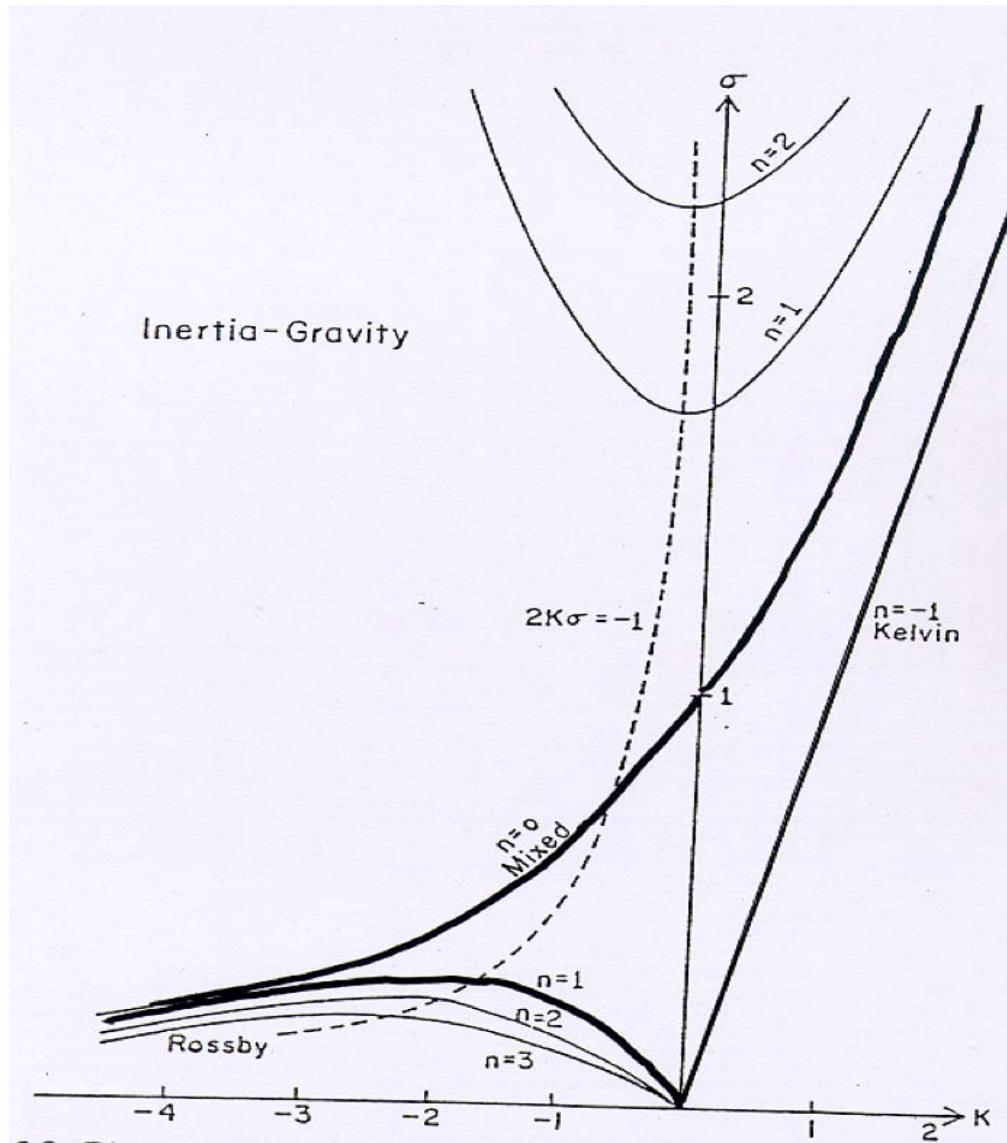


## 1-Active Layer Ocean Model



$$\rho_2 > \rho_1; \frac{1}{\rho_2} \nabla P_2 \approx 0; \vec{V}_2 \approx 0 \quad \longrightarrow \quad h = \frac{\Delta \rho}{\rho} (\text{SSH Anomaly})$$

## Equatorial Ocean Wave Dynamics



$$\frac{\partial u}{\partial t} - \beta y v = -g' \frac{\partial h}{\partial x}$$

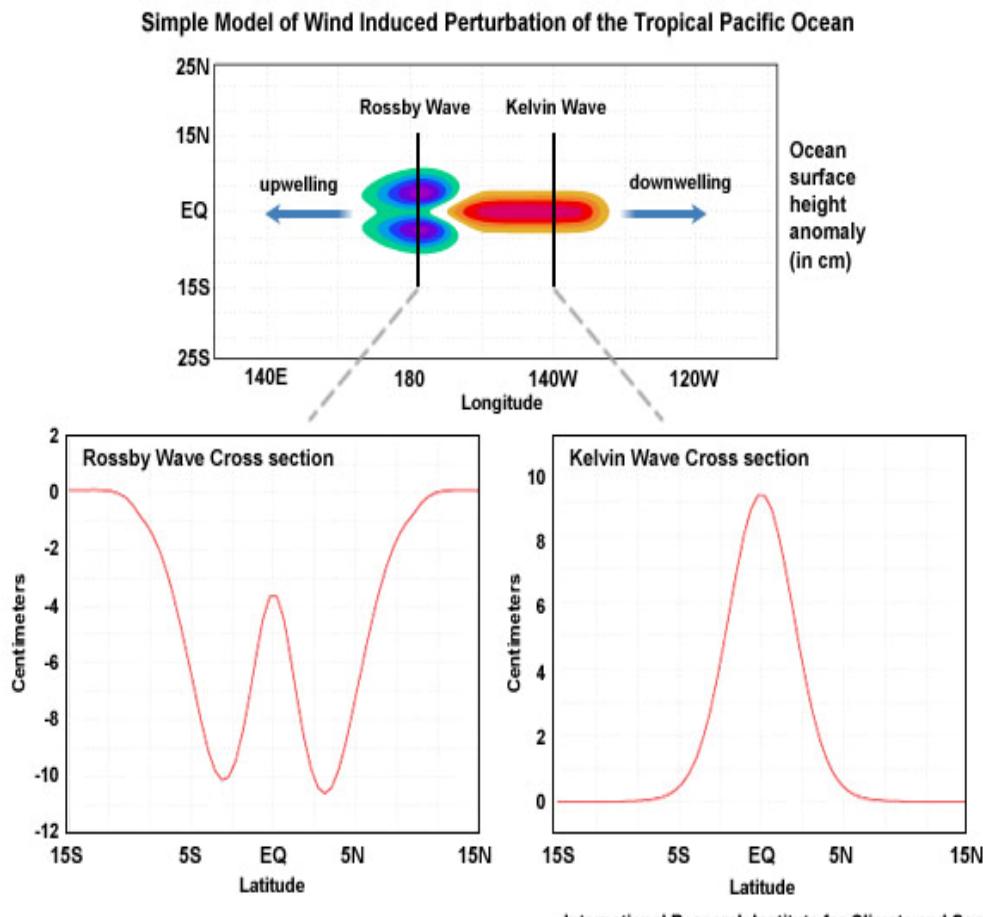
$$\frac{\partial v}{\partial t} + \beta y u = -g' \frac{\partial h}{\partial y}$$

$$\frac{\partial h}{\partial t} + H \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) = 0$$

$$g' = \frac{\Delta \rho}{\rho} g$$

**Frequency vs Wave Number  
Diagram – Dispersion Relation**

# Equatorial Ocean Wave Dynamics



$$\frac{\partial u}{\partial t} - \beta y v = -g' \frac{\partial h}{\partial x}$$

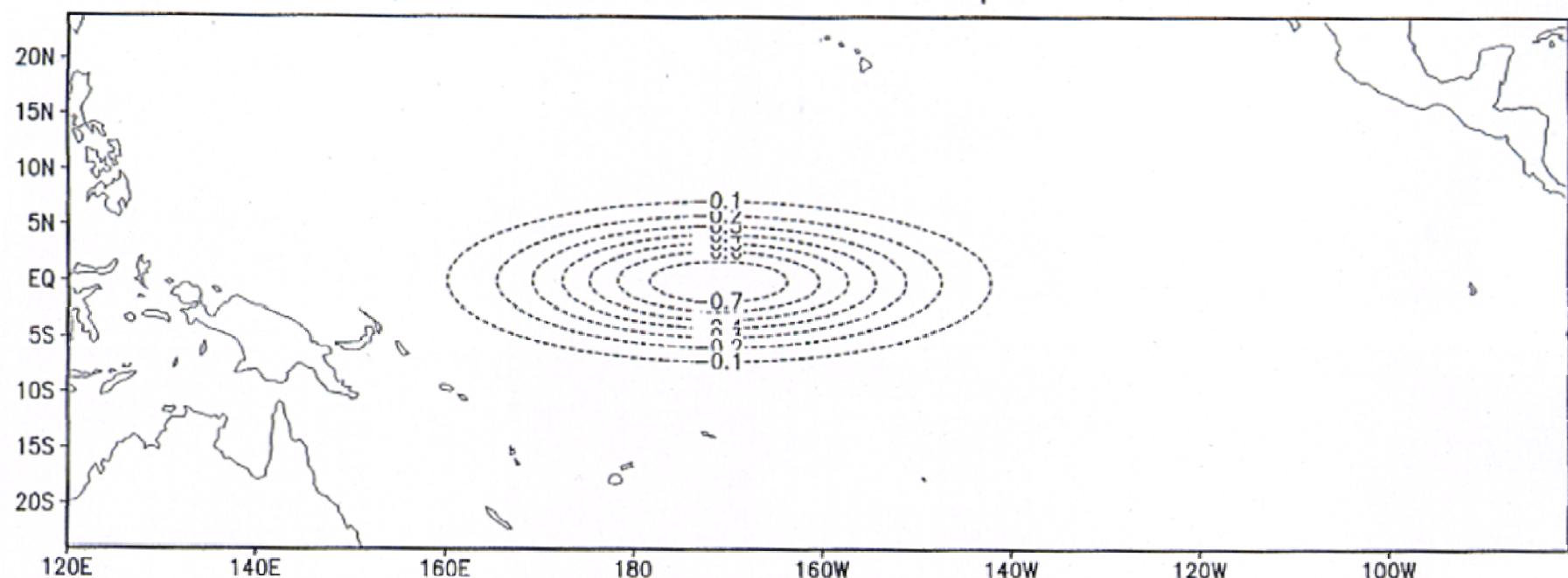
$$\frac{\partial v}{\partial t} + \beta y u = -g' \frac{\partial h}{\partial y}$$

$$\frac{\partial h}{\partial t} + H \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) = 0$$

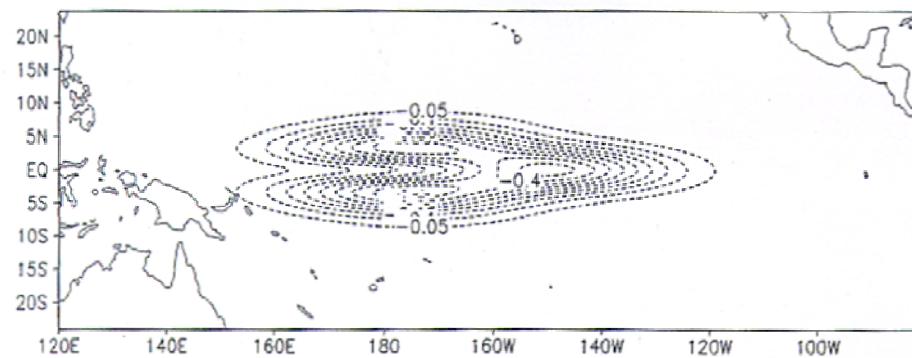
$$g' = \frac{\Delta \rho}{\rho} g$$

# A Simple Numerical Example

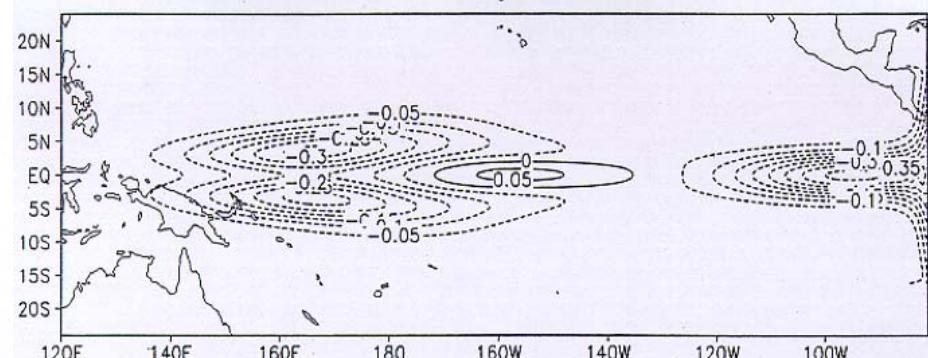
Initial Thermocline Depression



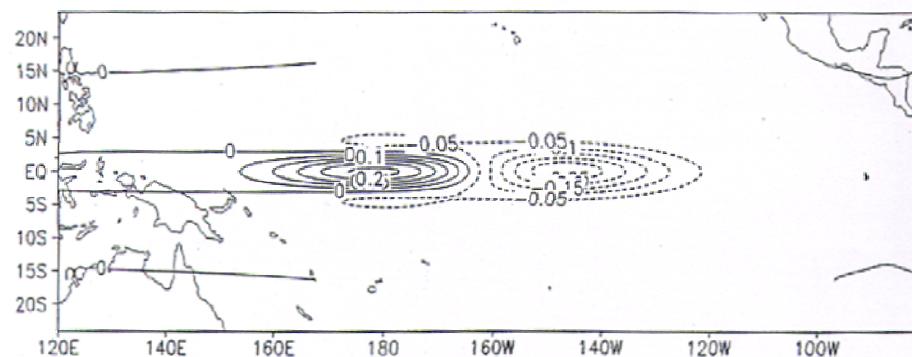
H day 20



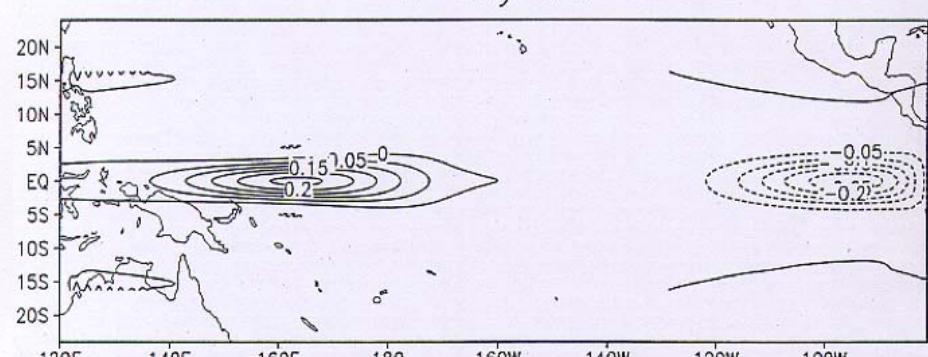
H day 70



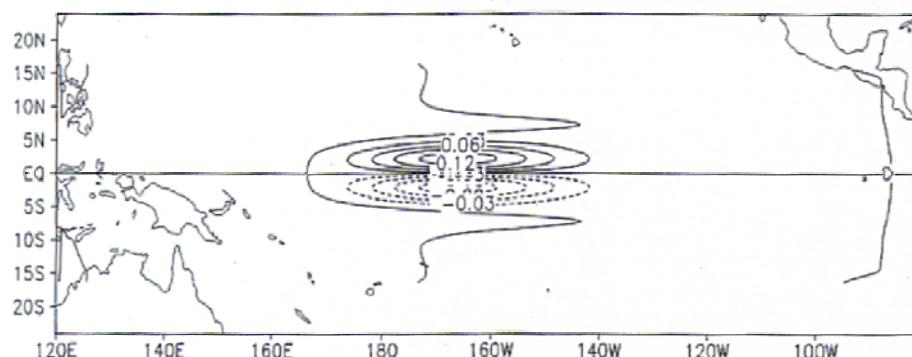
U day 20



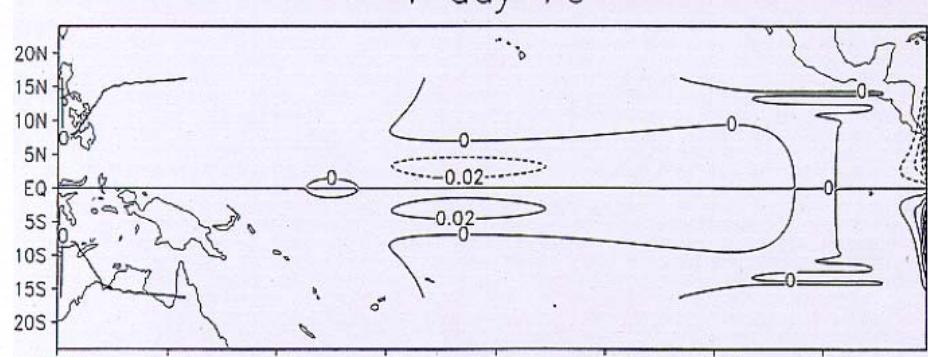
U day 70

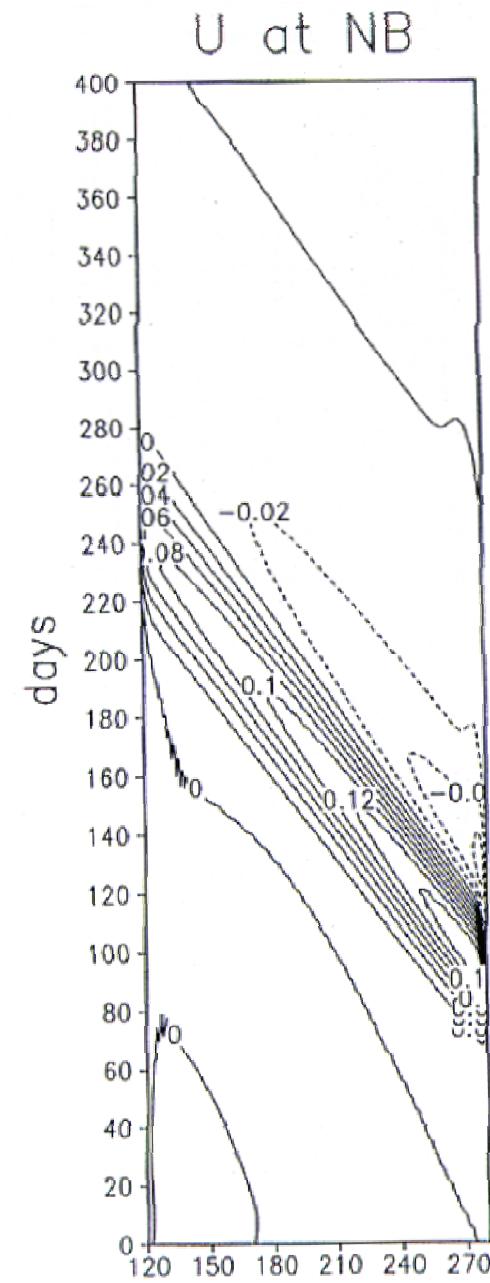
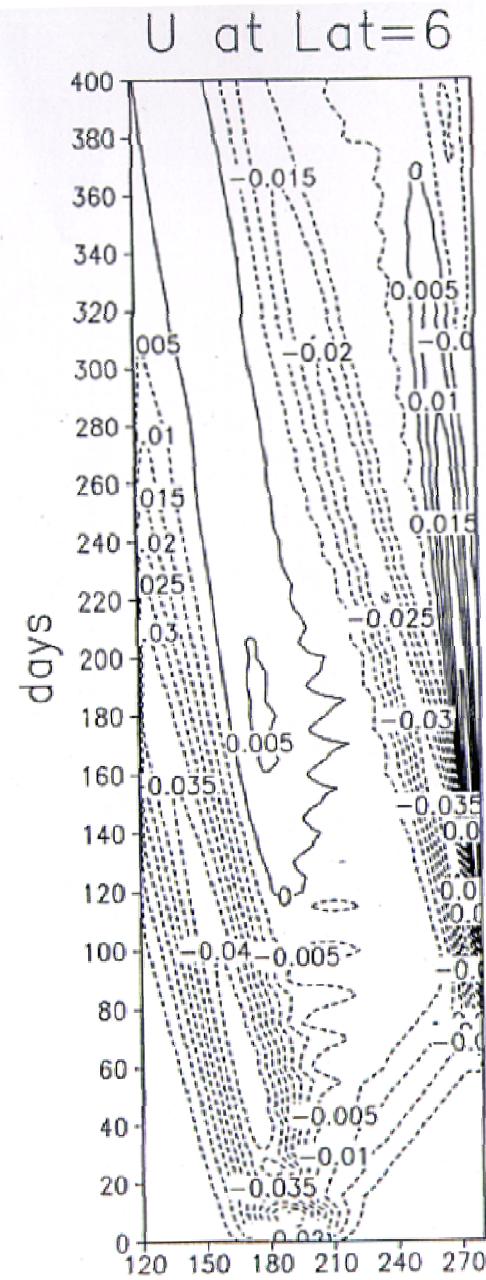
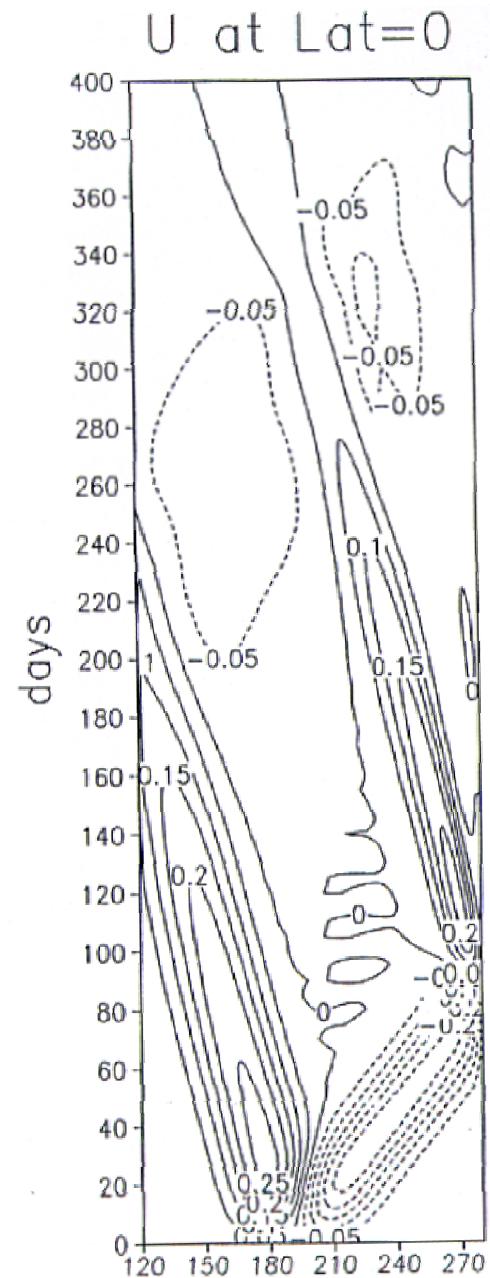


V day 20



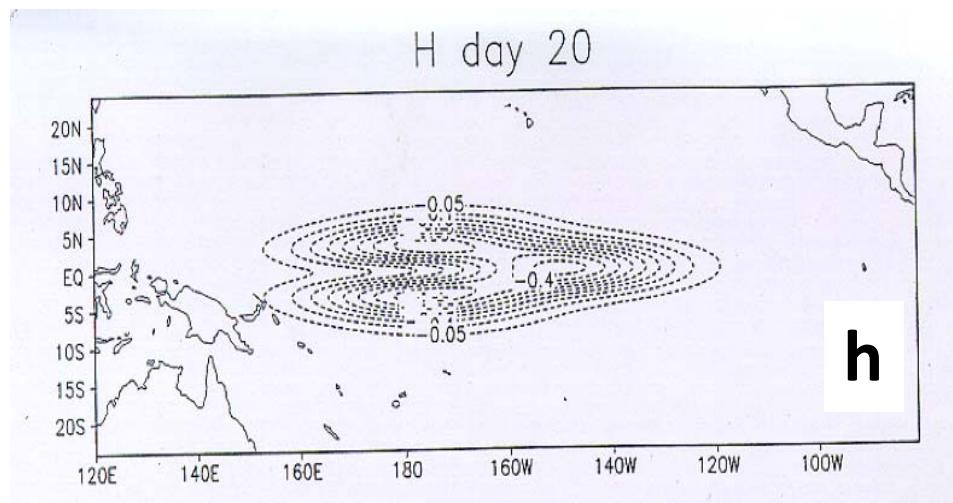
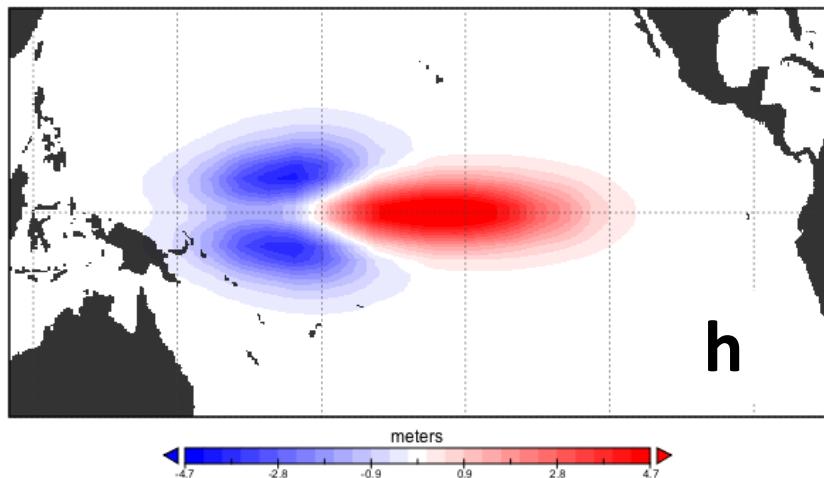
V day 70





# Equatorial Ocean Wave Dynamics

Thermocline Depth Anomalies Day-10



$$\frac{\partial u}{\partial t} - \beta y v = -g' \frac{\partial h}{\partial x} + \frac{\tau_x}{\rho_1 H} - \varepsilon u$$

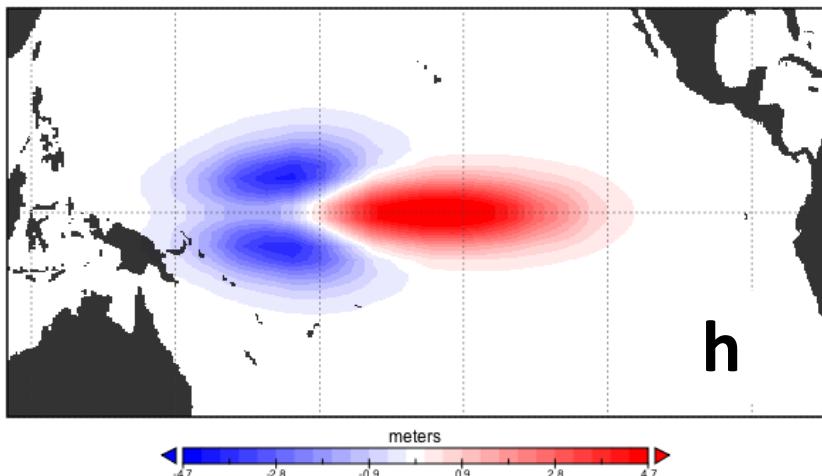
$$\frac{\partial v}{\partial t} + \beta y u = -g' \frac{\partial h}{\partial y} + \frac{\tau_y}{\rho_1 H} - \varepsilon v$$

$$\frac{\partial h}{\partial t} + H \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) = -\alpha h$$

**Free vs. Steady Response**

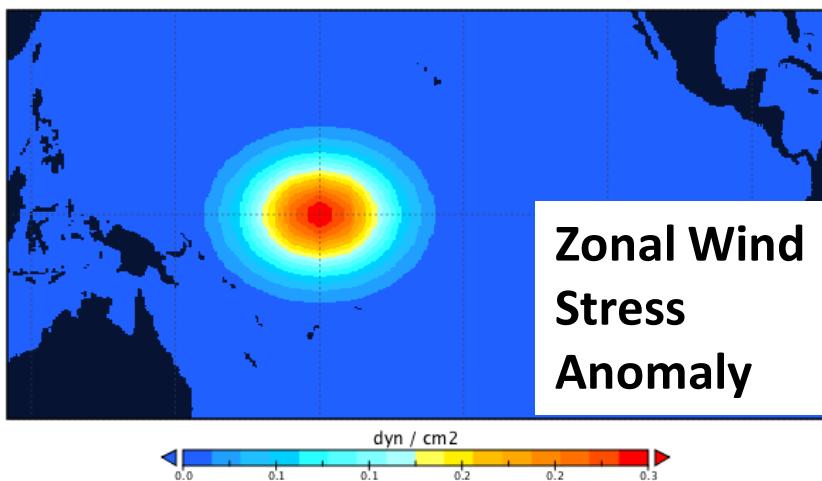
## Equatorial Ocean Wave Dynamics

Thermocline Depth Anomalies Day-10



**h**

Zonal Wind Stress Anomaly



**Zonal Wind  
Stress  
Anomaly**

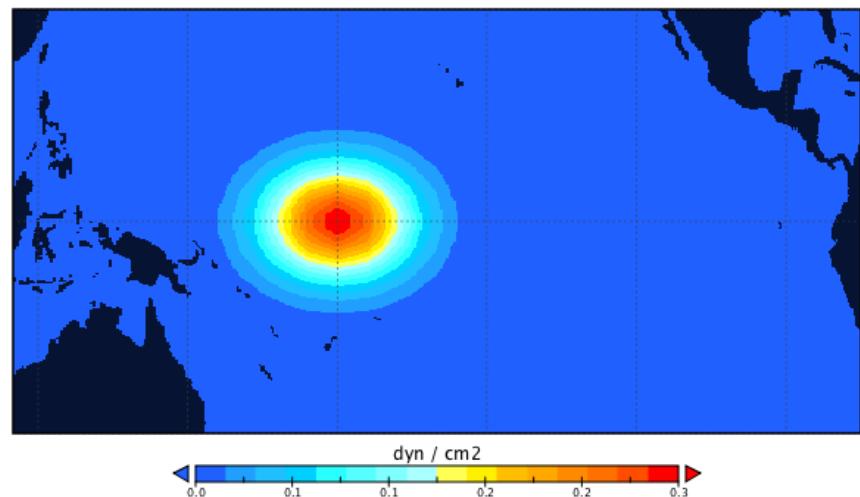
$$\frac{\partial u}{\partial t} - \beta y v = -g' \frac{\partial h}{\partial x} + \frac{\tau_x}{\rho_1 H} - \varepsilon u$$

$$\frac{\partial v}{\partial t} + \beta y u = -g' \frac{\partial h}{\partial y} + \frac{\tau_y}{\rho_1 H} - \varepsilon v$$

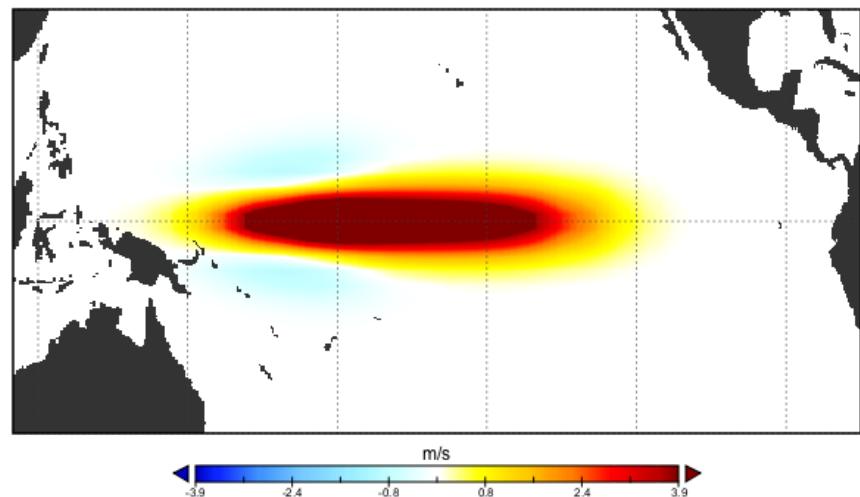
$$\frac{\partial h}{\partial t} + H \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) = -\alpha h$$

## Free vs. Steady Response

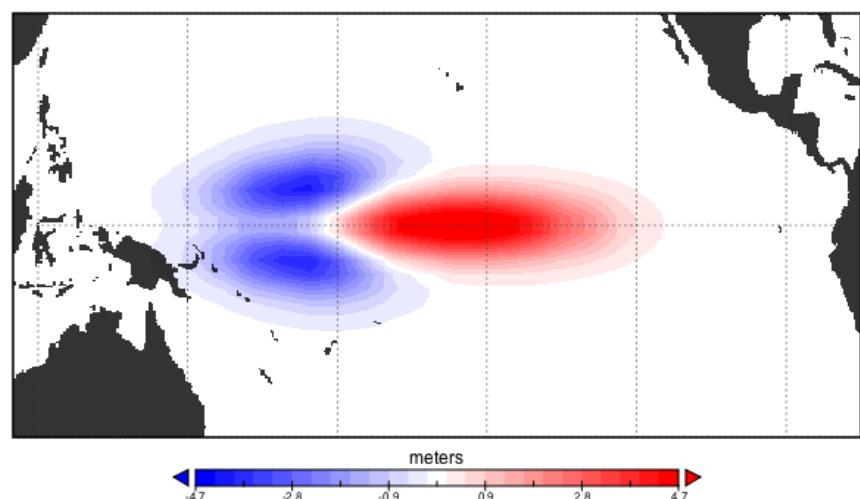
Zonal Wind Stress Anomaly



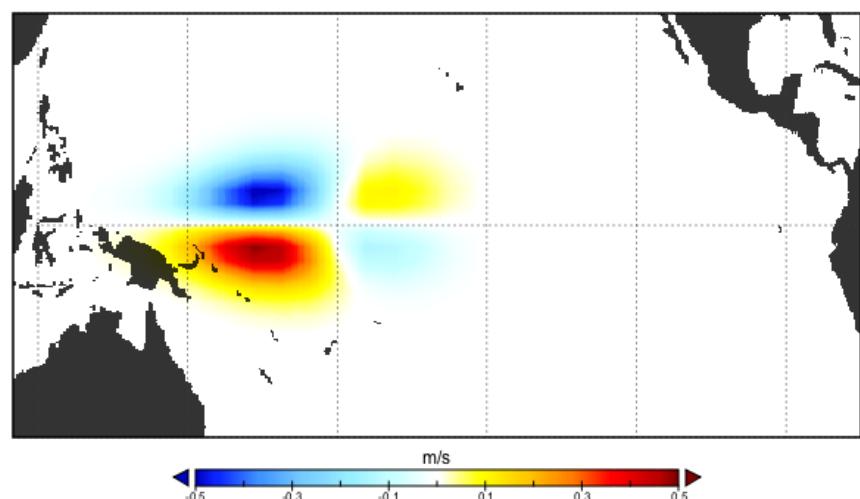
Zonal Current Anomaly Day-10



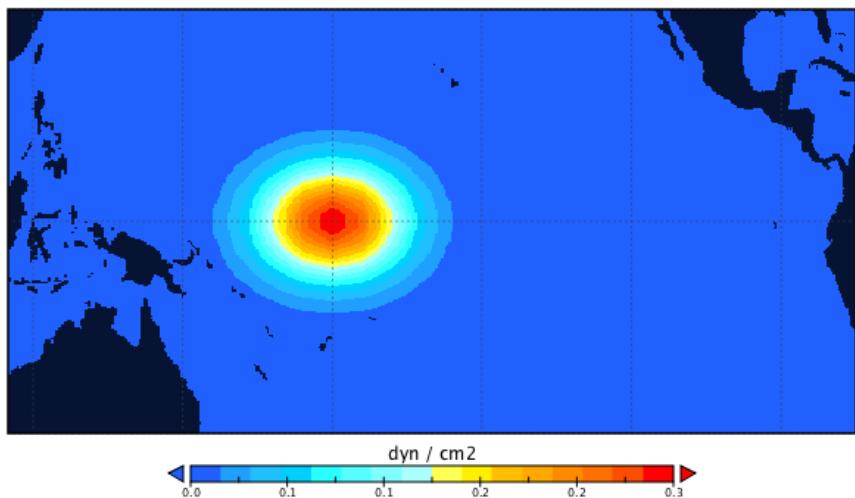
Thermocline Depth Anomalies Day-10



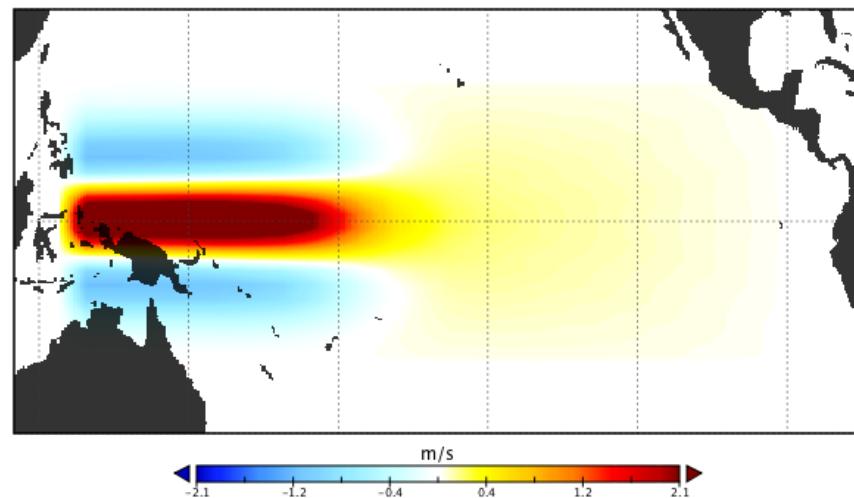
Meridional Current Anomaly Day-10



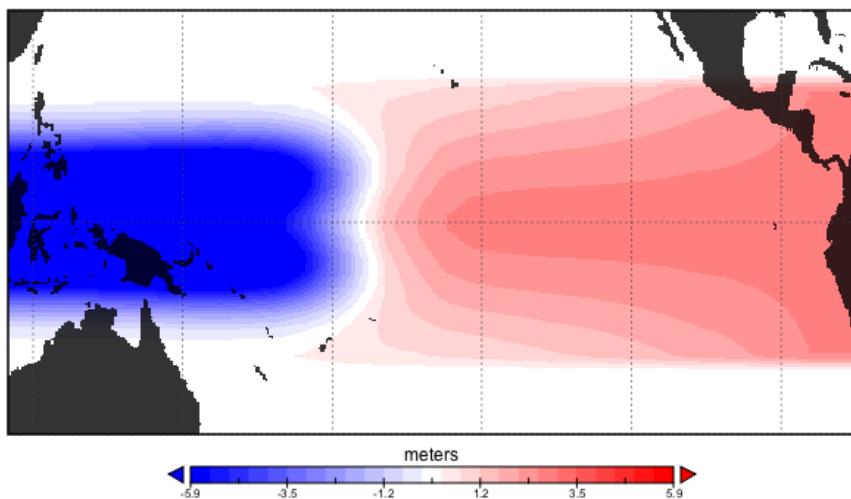
Zonal Wind Stress Anomaly



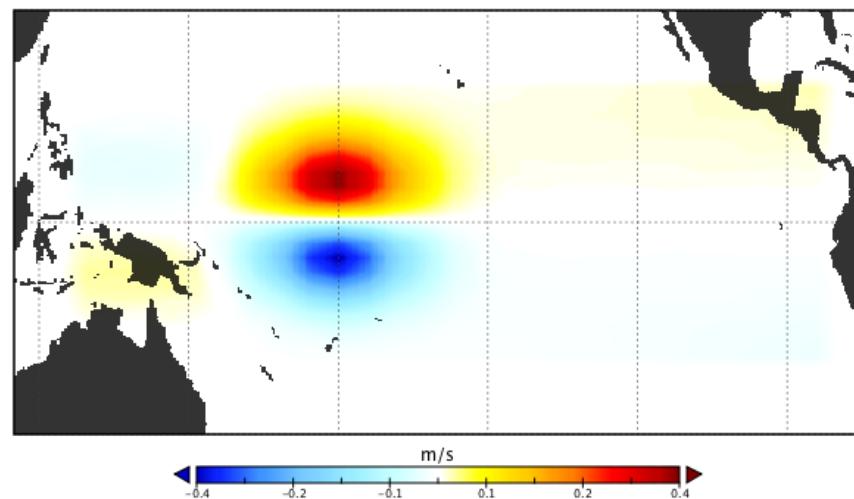
Zonal Current Anomaly Day 300



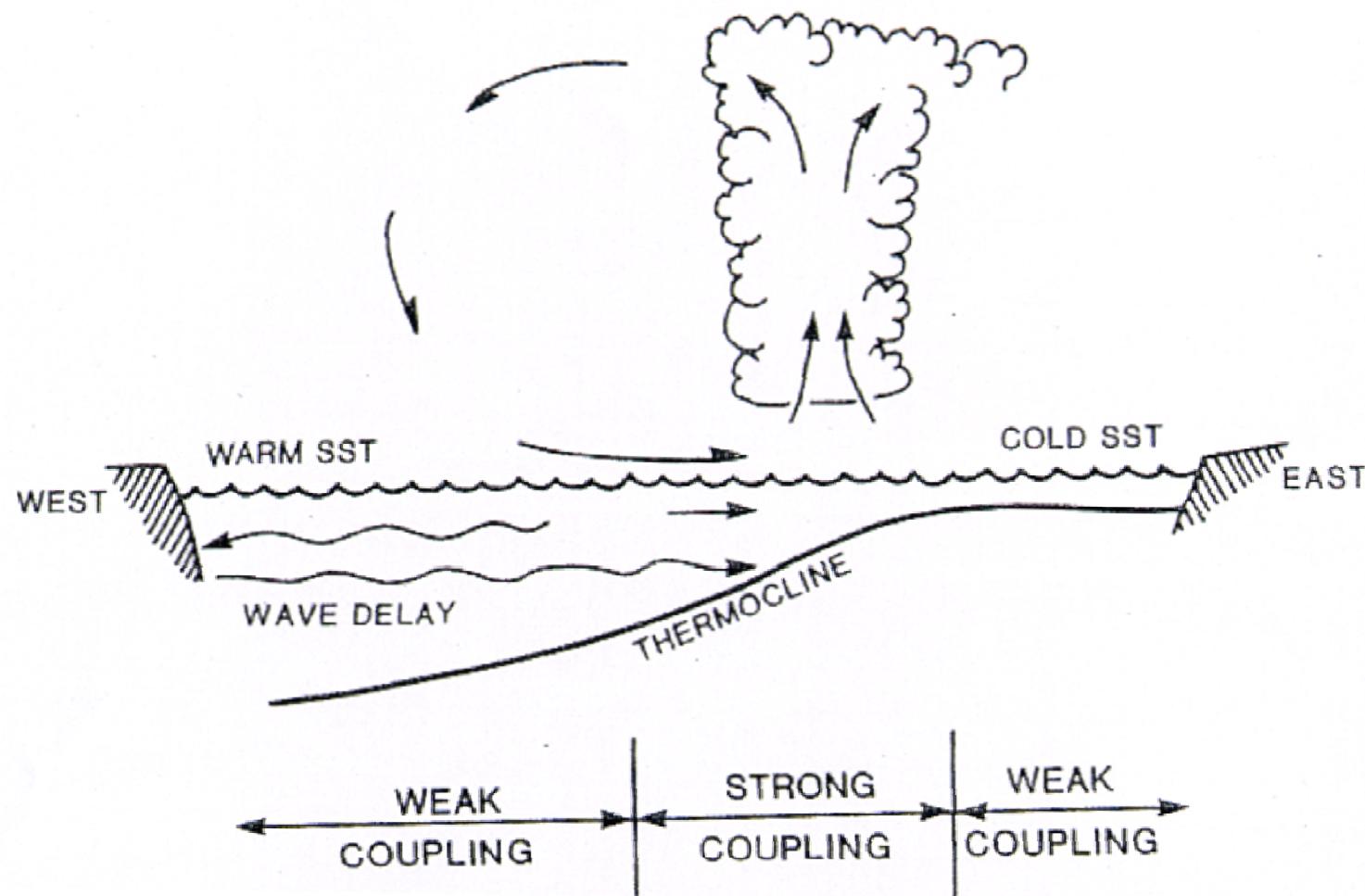
Thermocline Depth Anomalies Day-300



Meridional Current Anomaly Day-300



## Role of the Ocean in the Delayed Oscillator Theory for ENSO



# A Very Simple Coupled Model

## Delayed Oscillator – Rossby Waves

$$\frac{\partial u}{\partial t} - \beta y v = -g' \frac{\partial h}{\partial x} + \frac{\tau_x}{\rho_1 H} \xleftarrow{\varepsilon u}$$

Atmosphere

$$\frac{\partial v}{\partial t} + \beta y u = -g' \frac{\partial h}{\partial y} + \frac{\tau_y}{\rho_1 H} \xleftarrow{\varepsilon v}$$

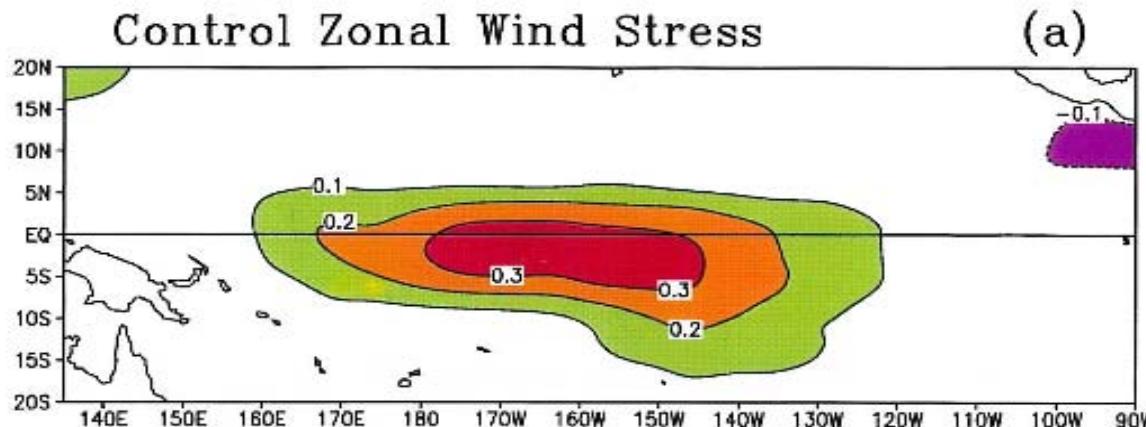
$$\frac{\partial h}{\partial t} + H \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) = -\alpha h$$

$$\frac{\partial (SST)}{\partial t} = -\vec{V} \cdot \nabla (SST) + \text{upwelling} + \text{dissipation}$$

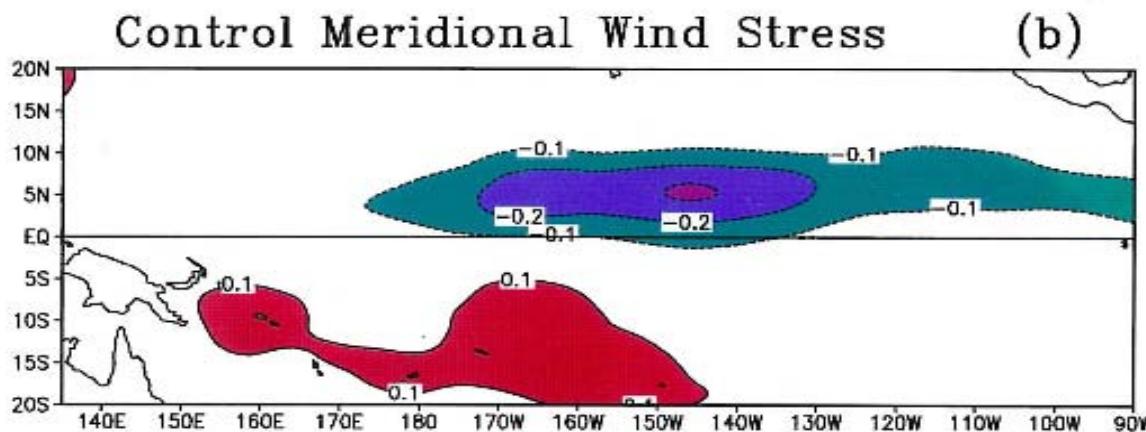
Source of Non-linearity

# An Empirical Atmospheric Component Model

$\alpha(x,y)$



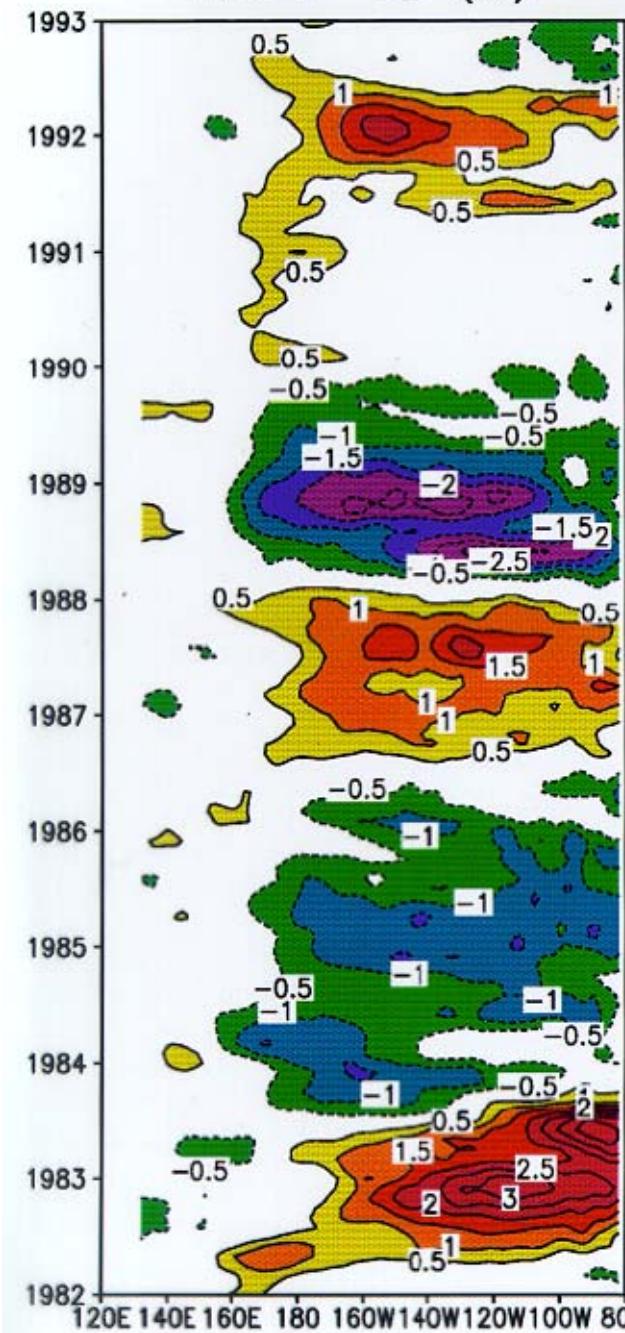
$\beta(x,y)$



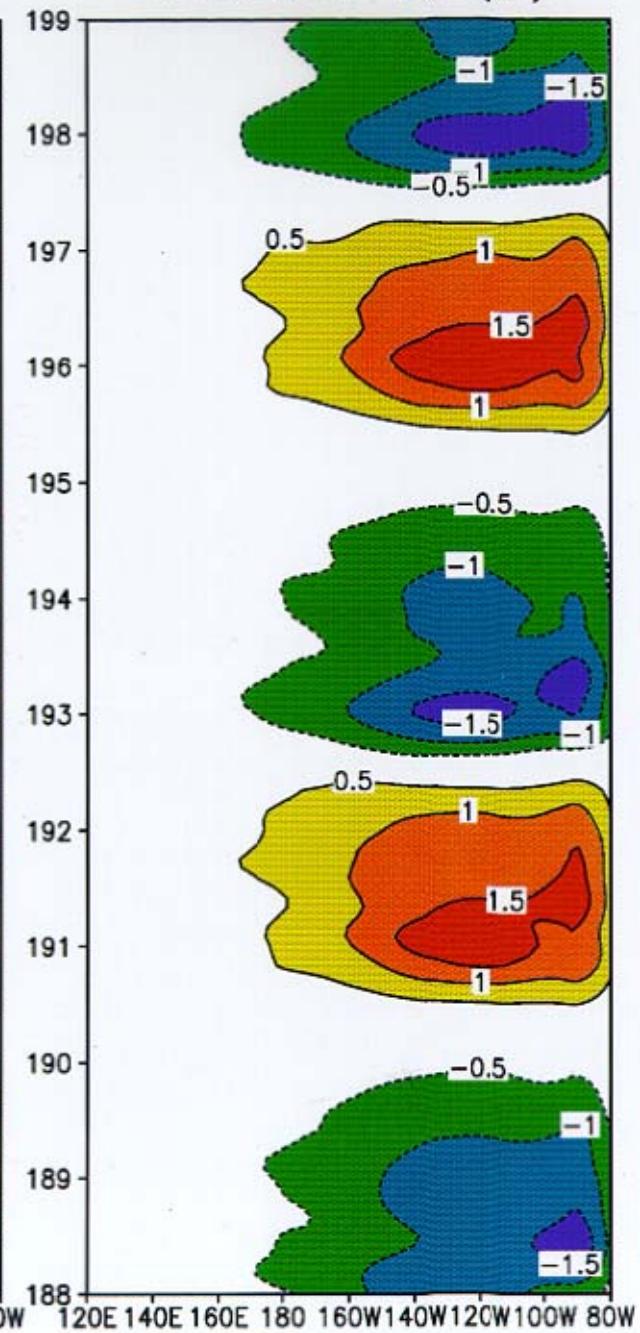
$$\tau_x(x,y) = \alpha(x,y) * NINO3$$

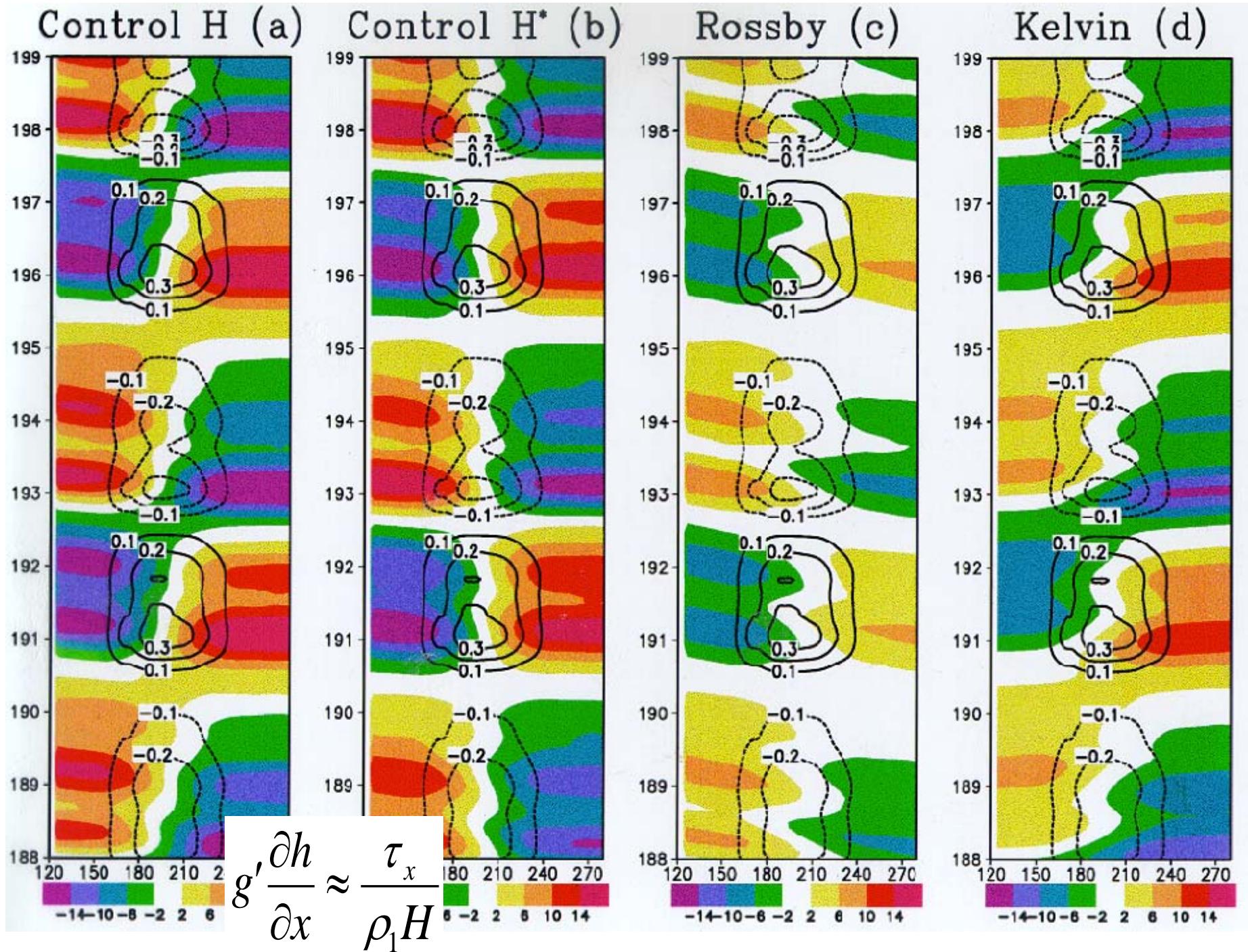
$$\tau_y(x,y) = \beta(x,y) * NINO3$$

NCEP  $T_s$  (a)



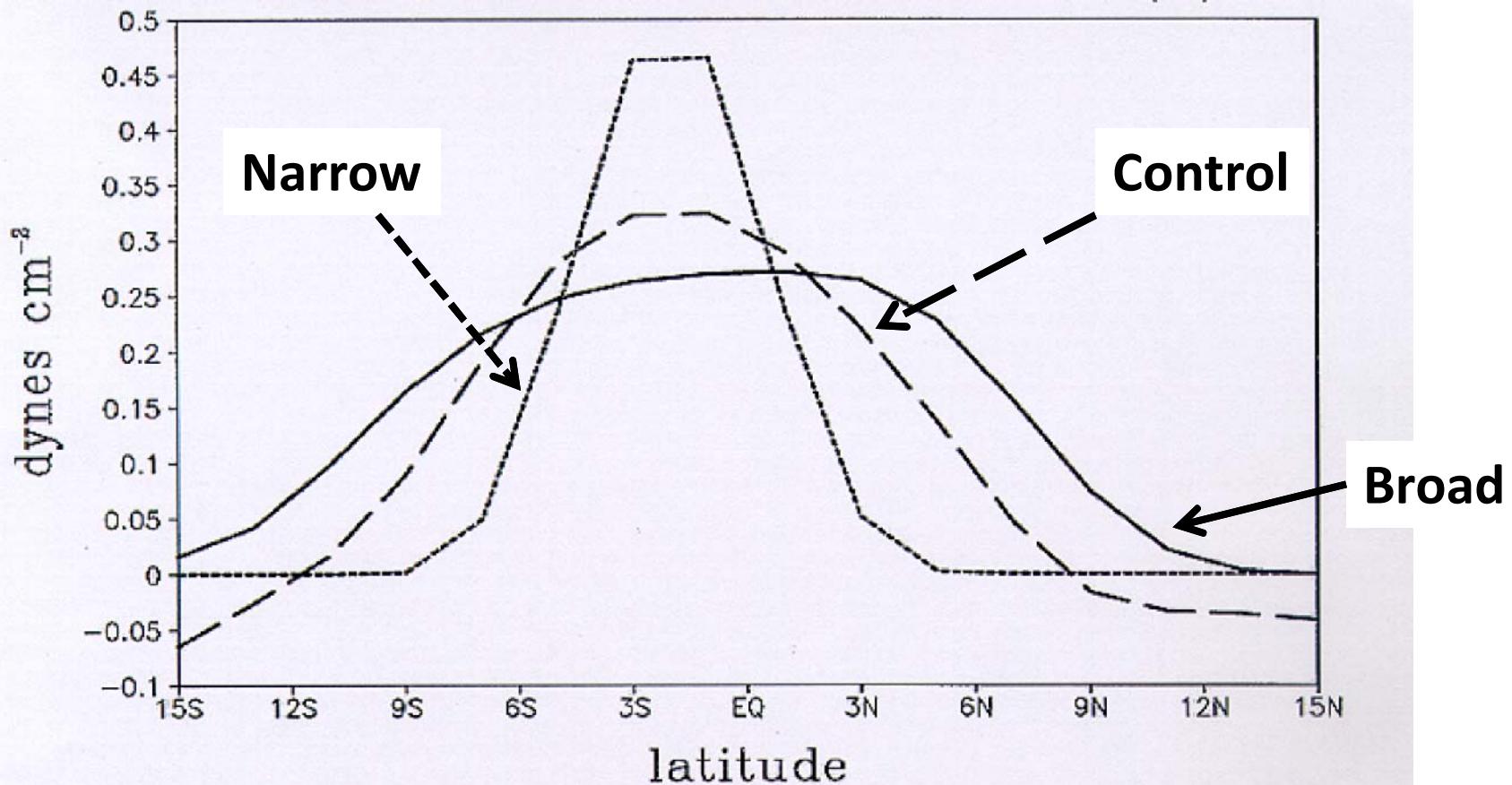
Control  $T_s$  (b)





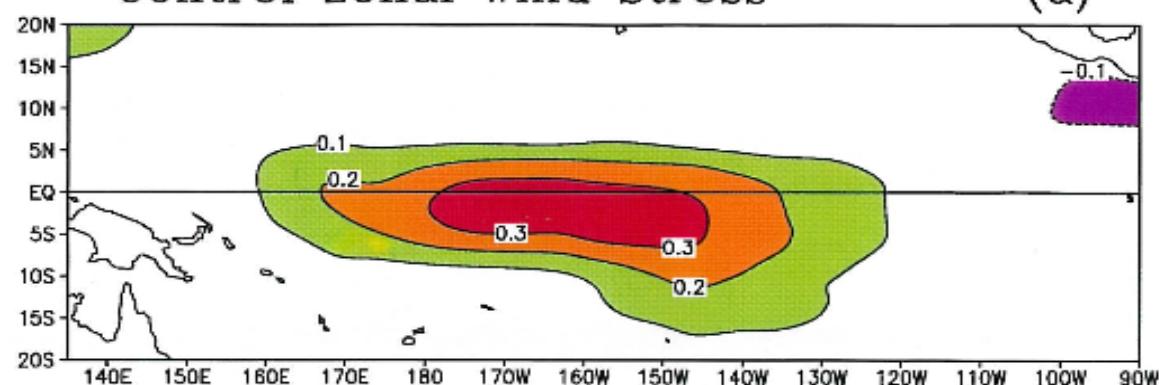
# Zonal Wind Stress

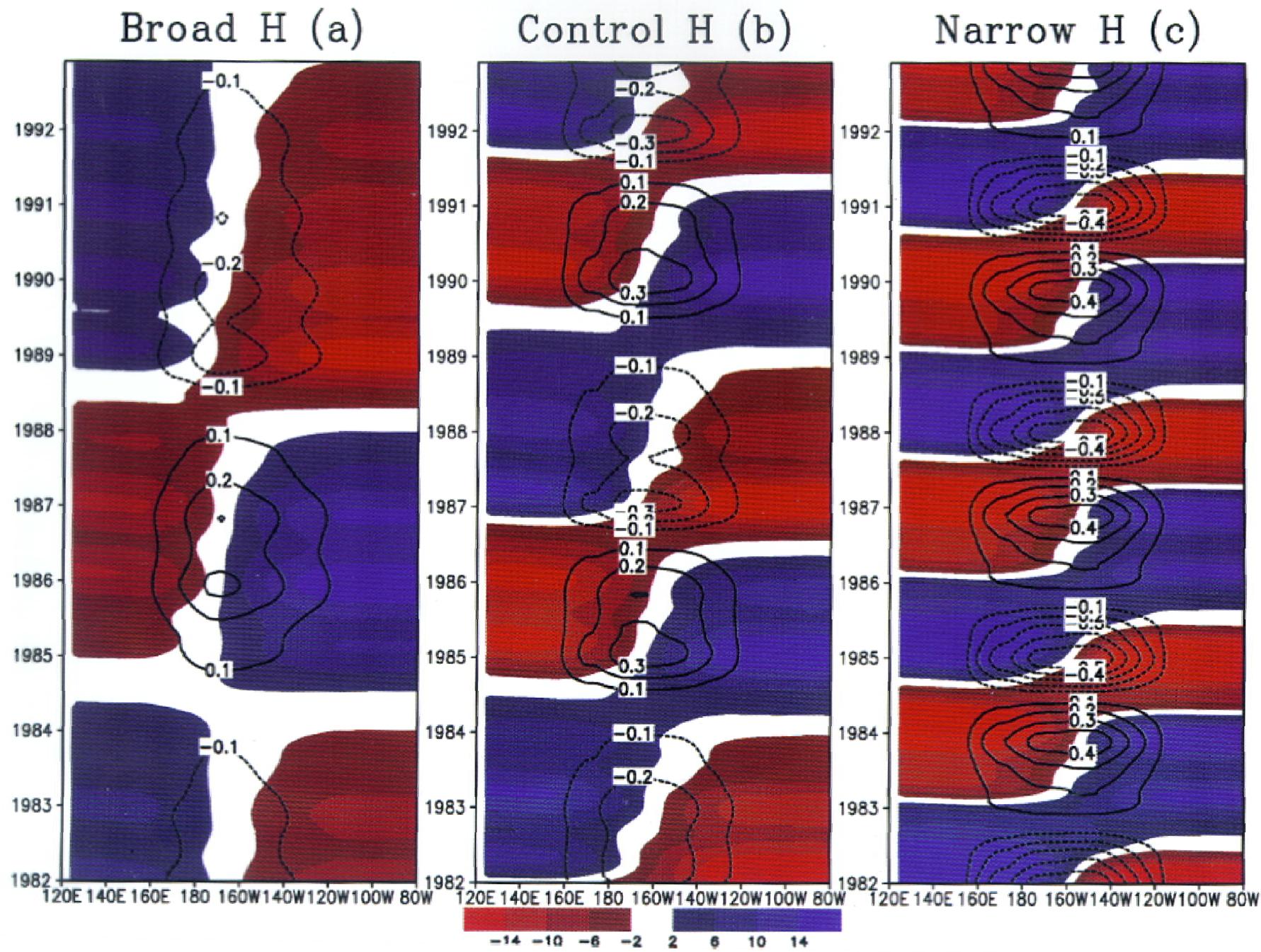
(a)



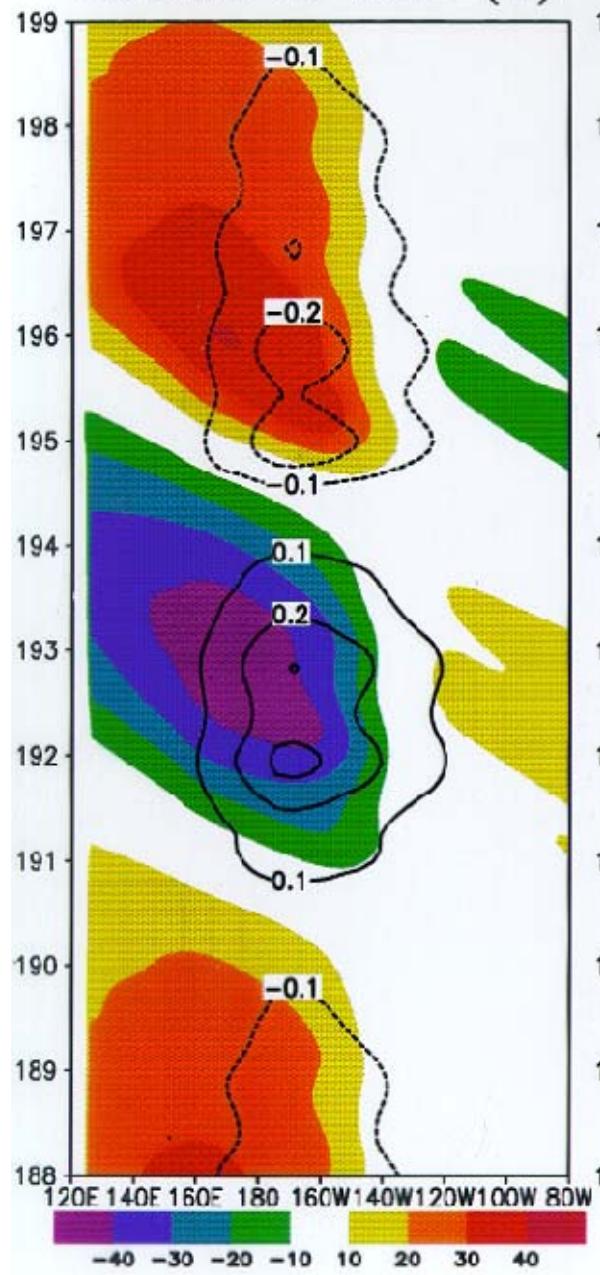
# Control Zonal Wind Stress

(a)

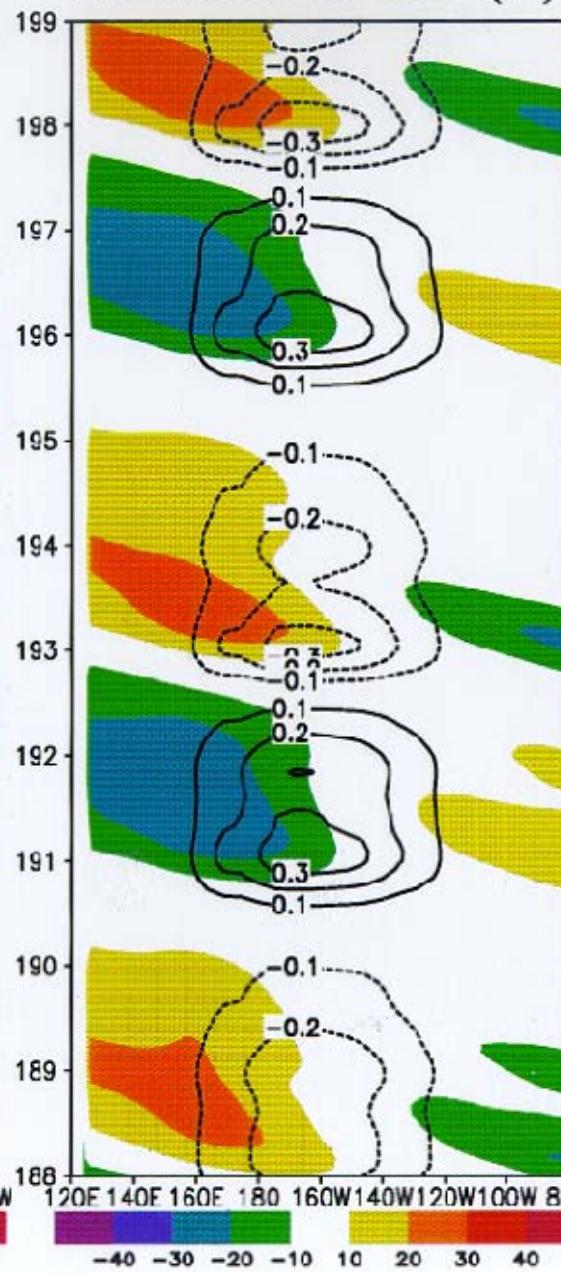




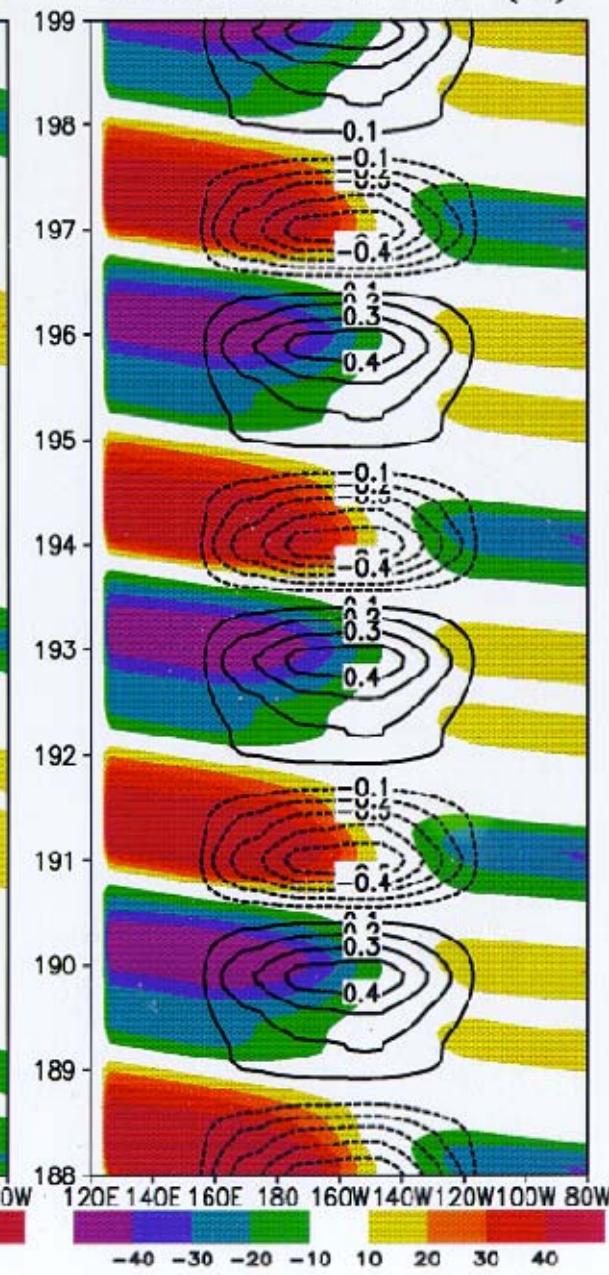
Broad H 12S (a)



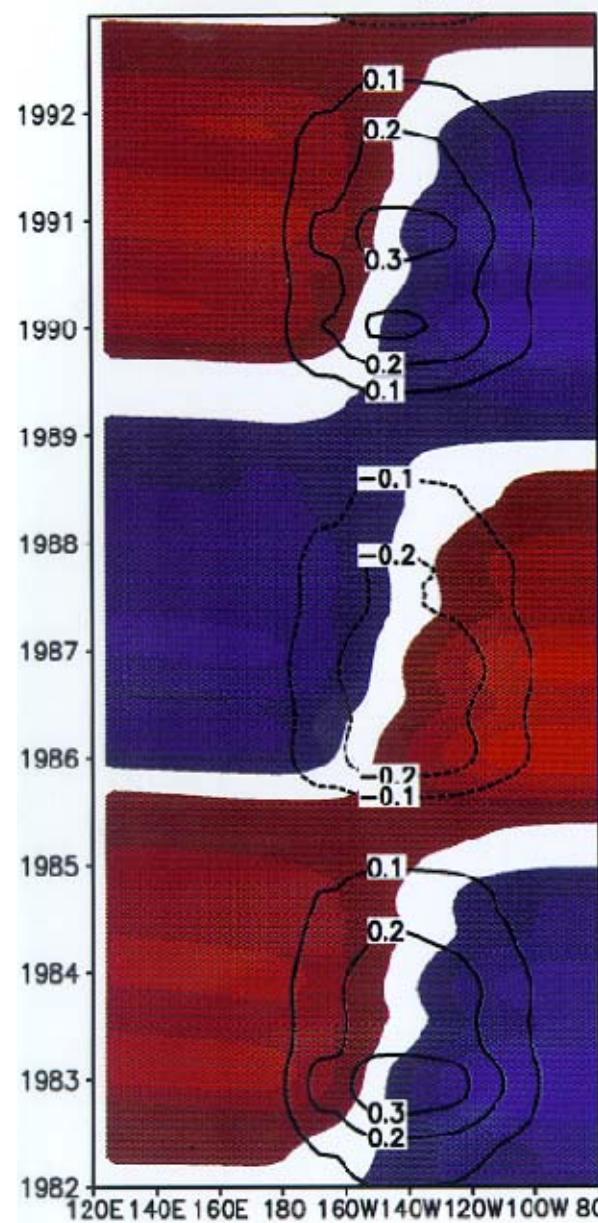
Control H 8S (b)



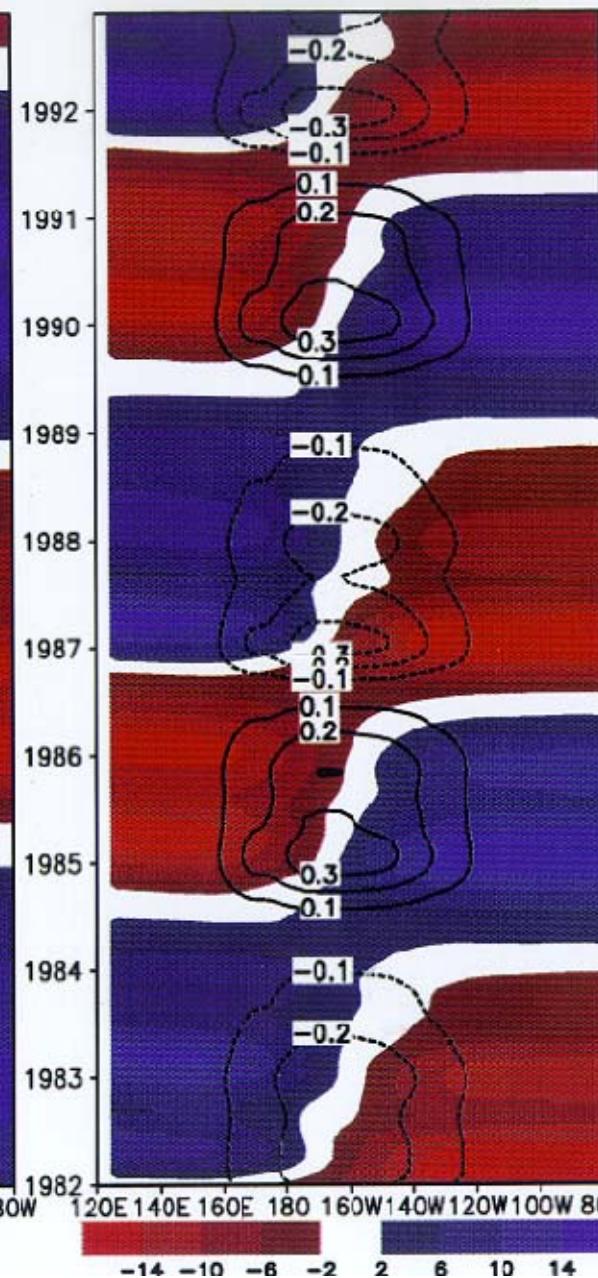
Narrow H 5S (c)



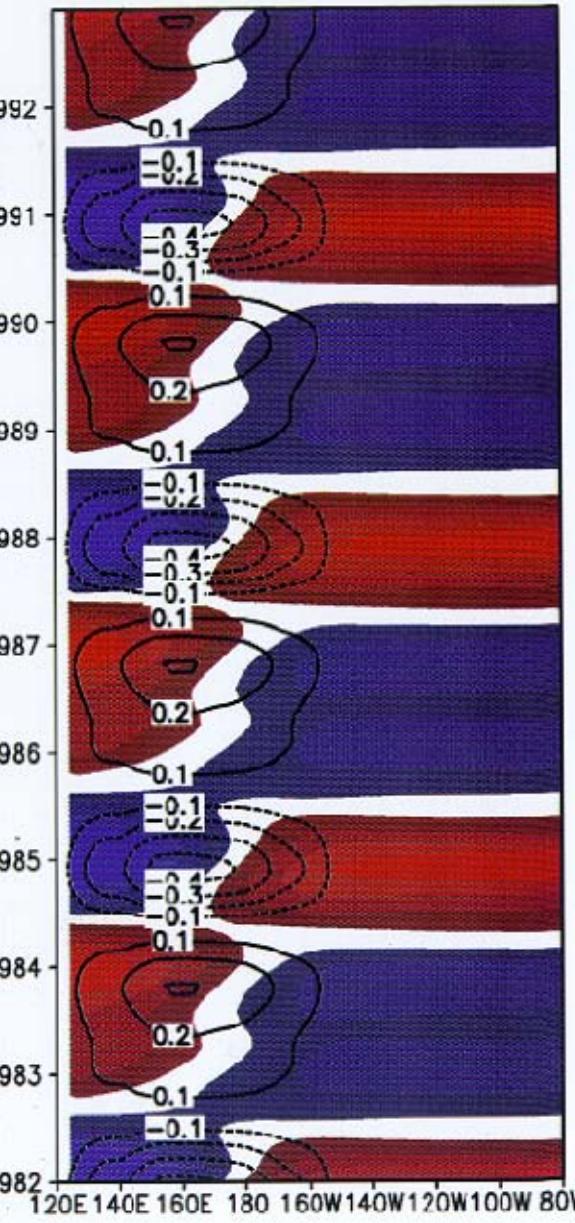
East H (a)



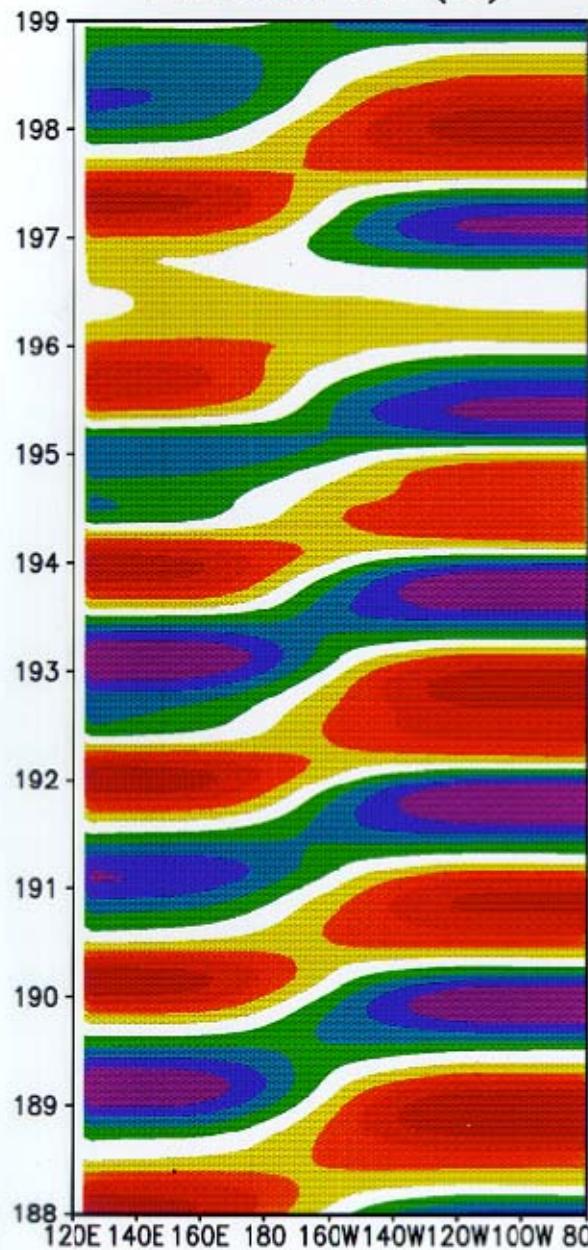
Control H (b)



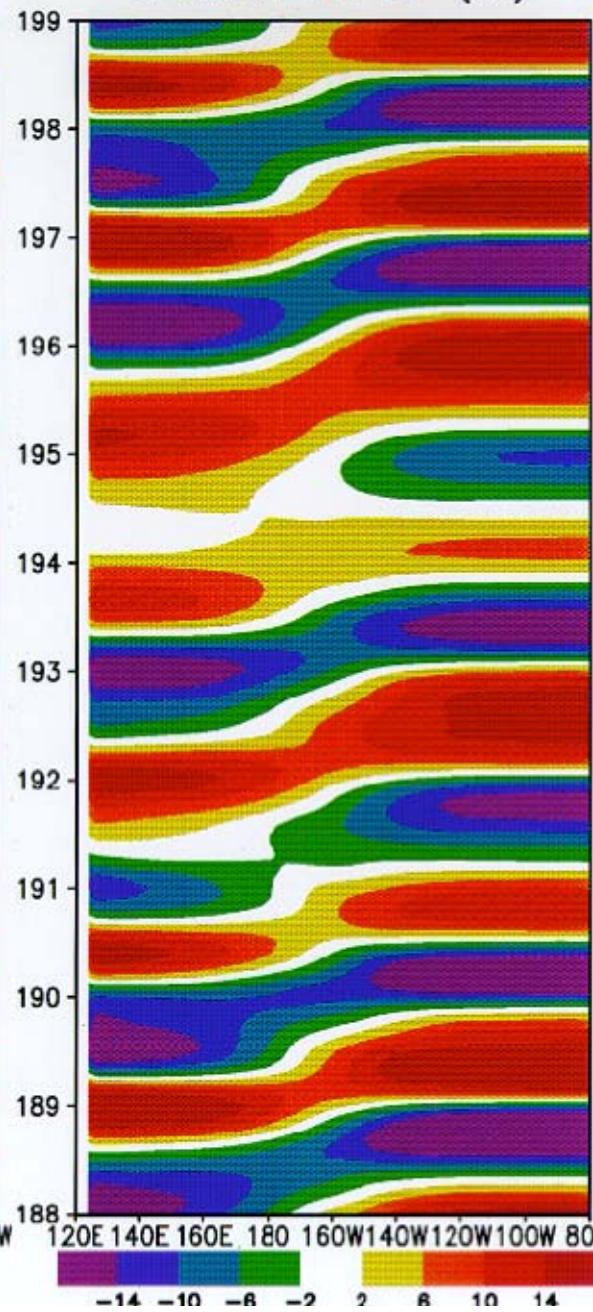
West H (c)



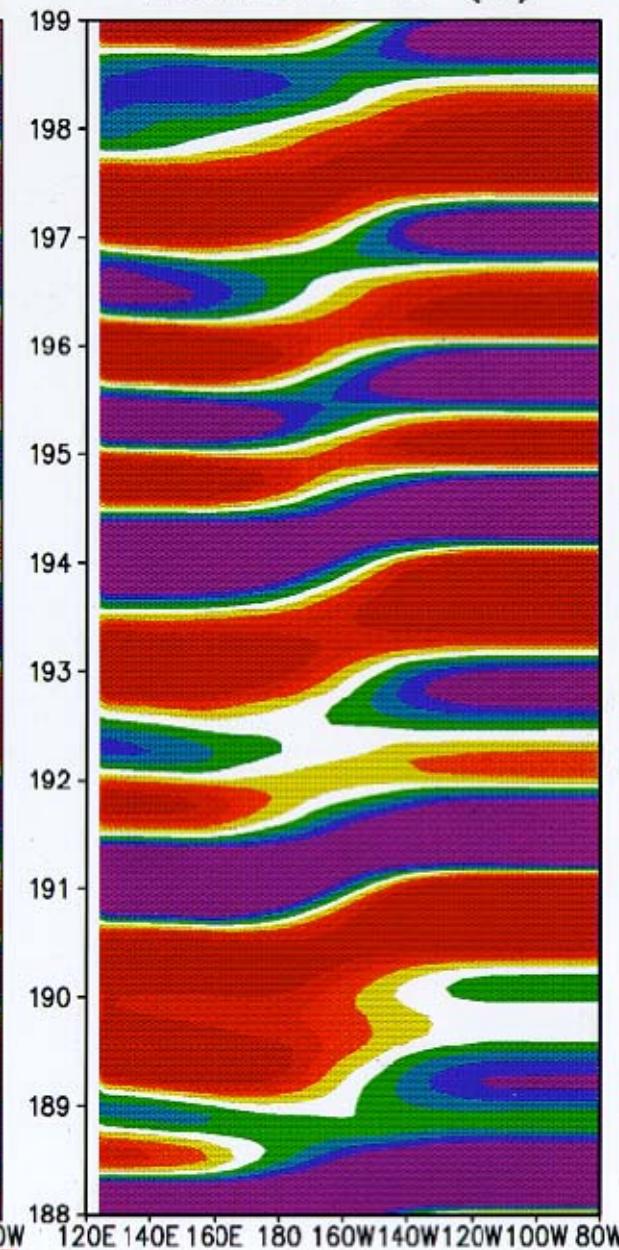
Broad H (a)



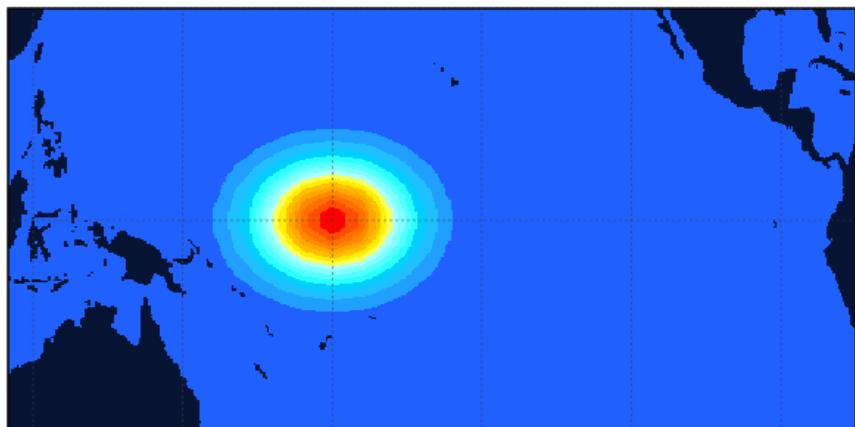
Control H (b)



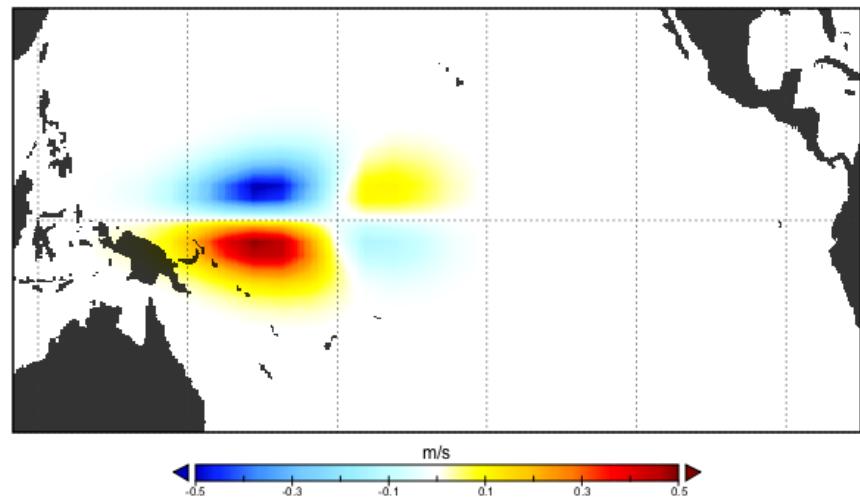
Narrow H (c)



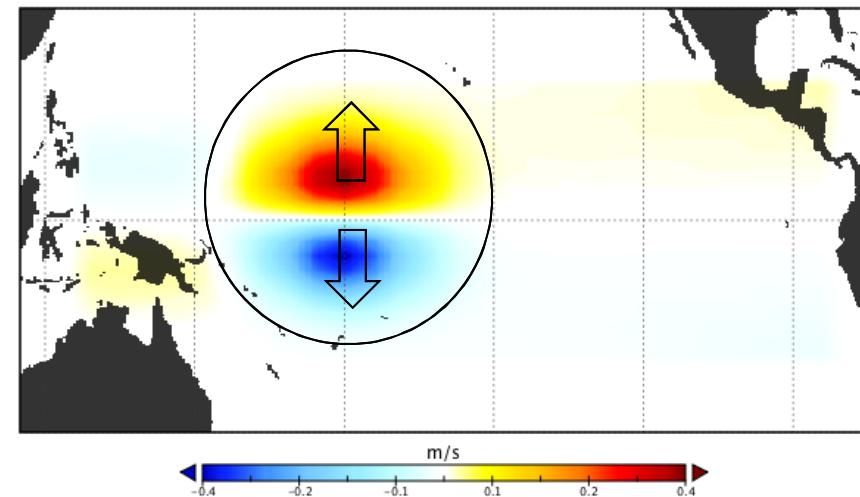
Zonal Wind Stress Anomaly



Meridional Current Anomaly Day-10

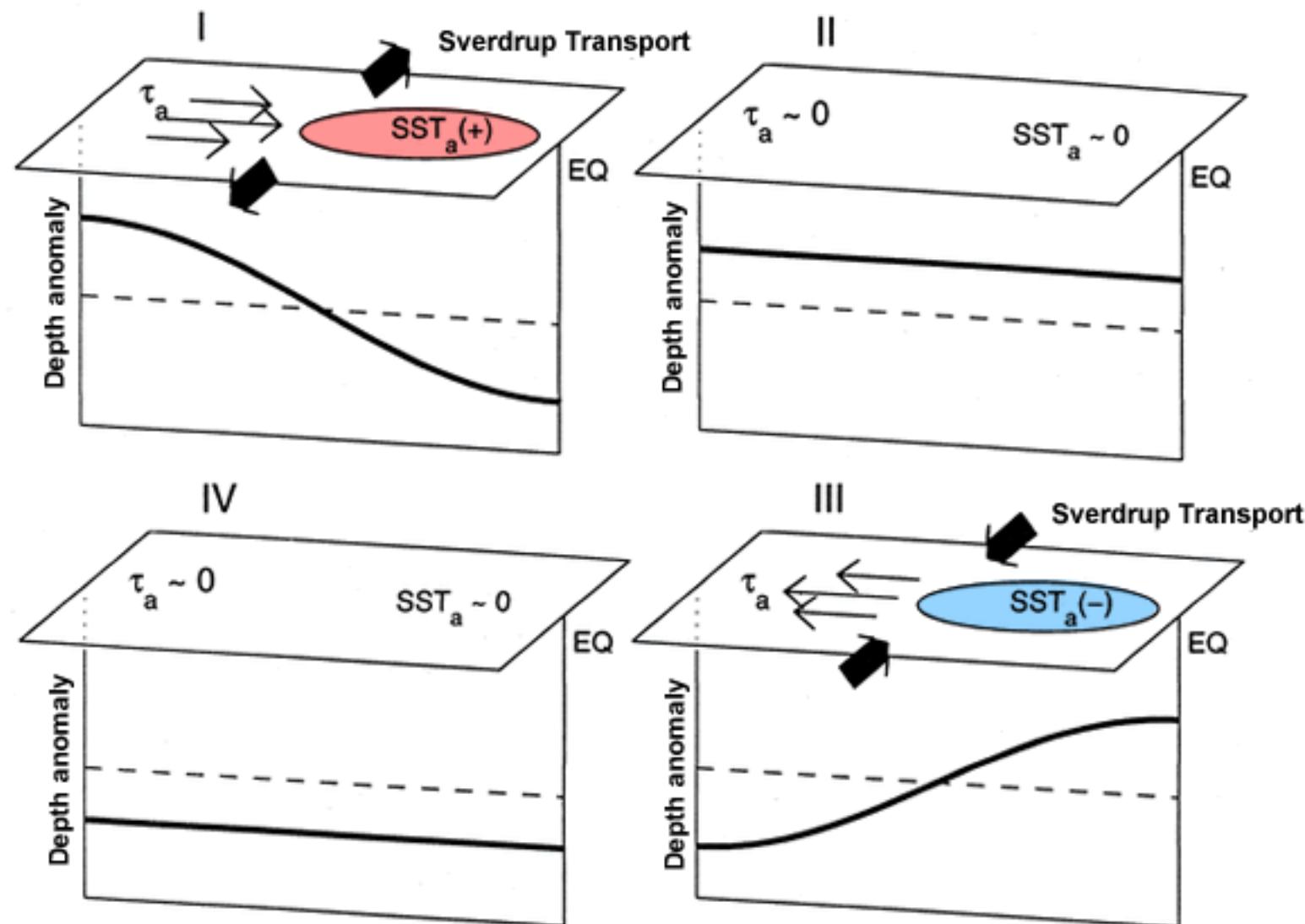


Meridional Current Anomaly Day-300



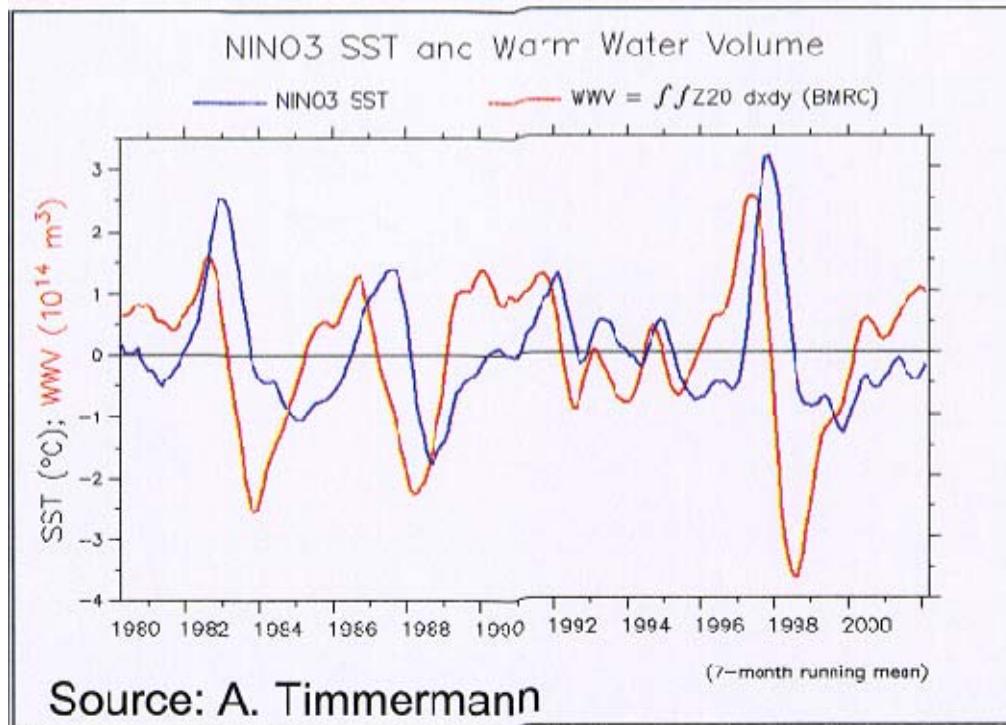
Recharge Oscillator Model:  
“Steady State” – Sverdrup Response  
Warm Phase – Equatorial Discharge

### Schematic of the Recharge/Discharge Theory of ENSO

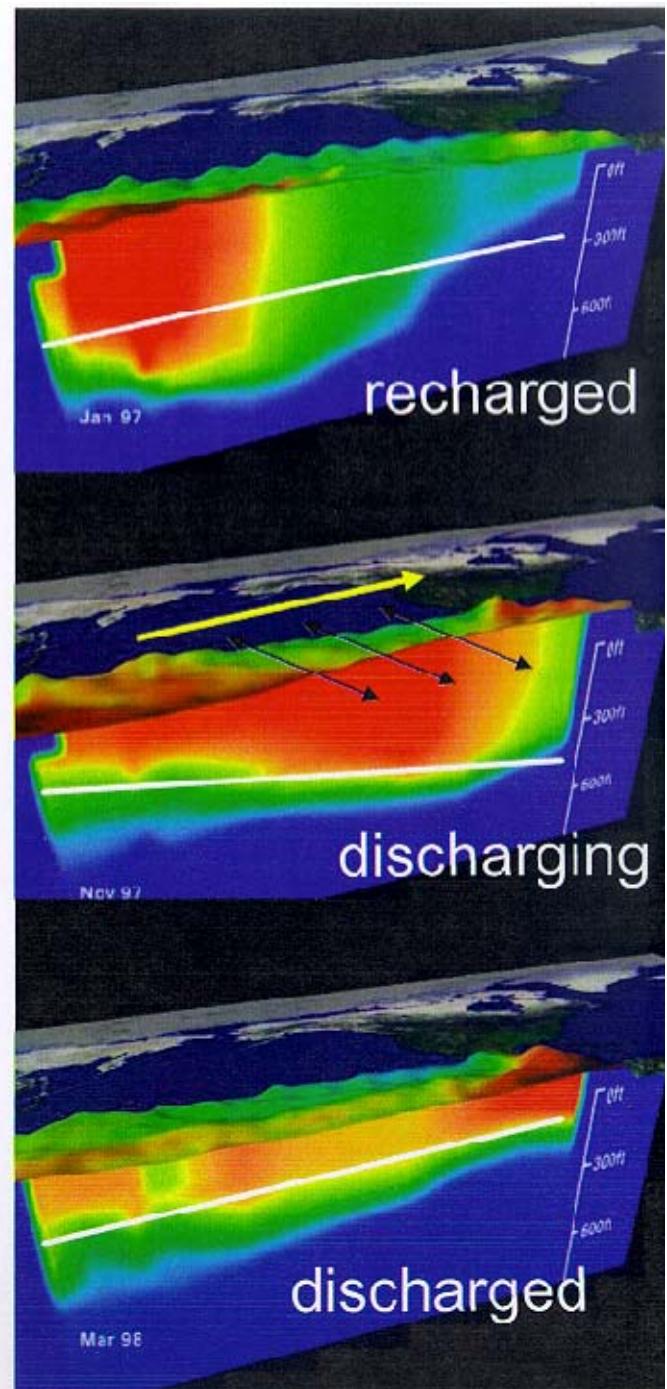


Meinen and McPhaden 2002

# Recharge/Discharge theory (Jin, 1997)



- Prior to El Nino heat content in equatorial region builds up
- During El Nino heat is “discharged” eastward and polewards



## Surface Layer Feedback Mechanism (Slow SST – Fast Wave Limit)

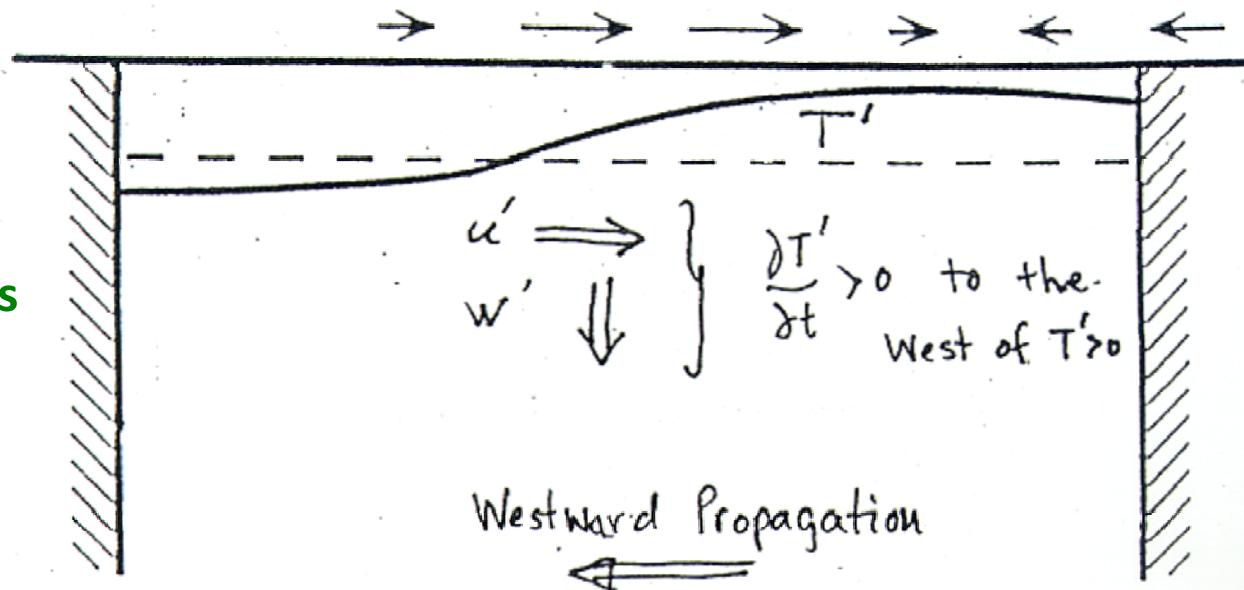
$\frac{\partial u}{\partial t}, \frac{\partial v}{\partial t}, \frac{\partial h}{\partial t} \approx 0$  - No Transient Wave Propagation

$$u' \frac{\partial(\overline{SST})}{\partial t}, w' \frac{\partial \bar{T}}{\partial z}$$

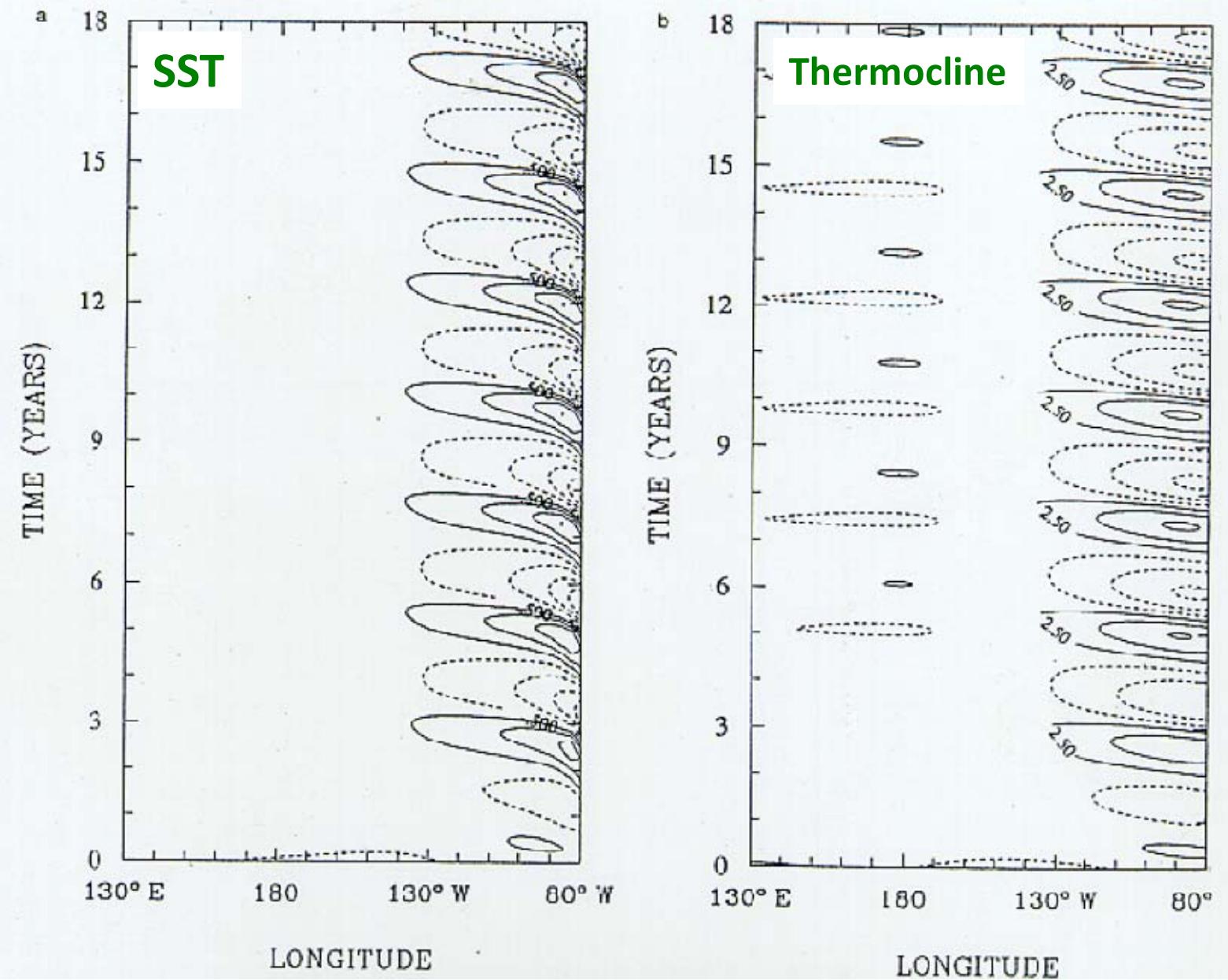
- Surface Feedback Amplify to the West SSTA

Surface Layer Feedback

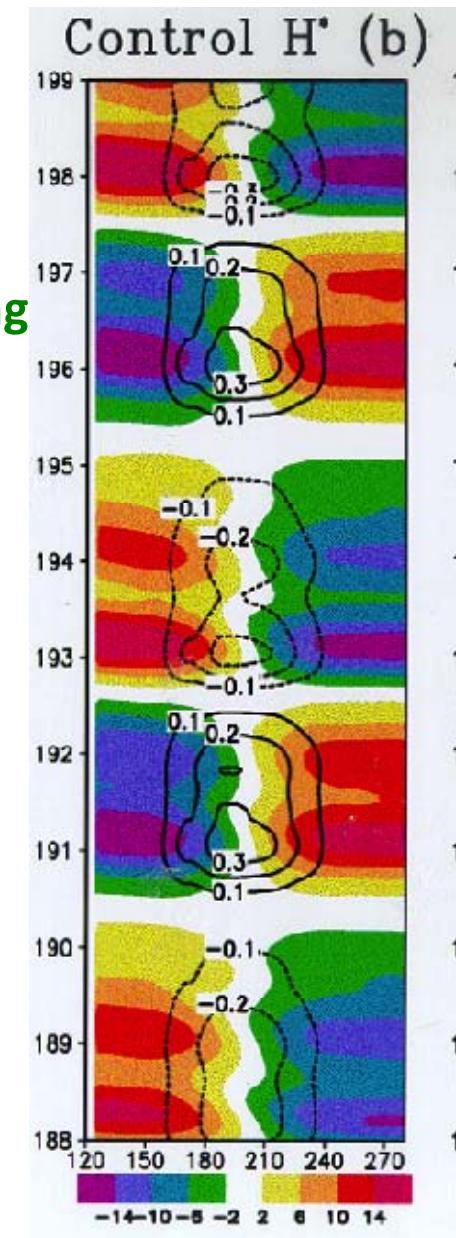
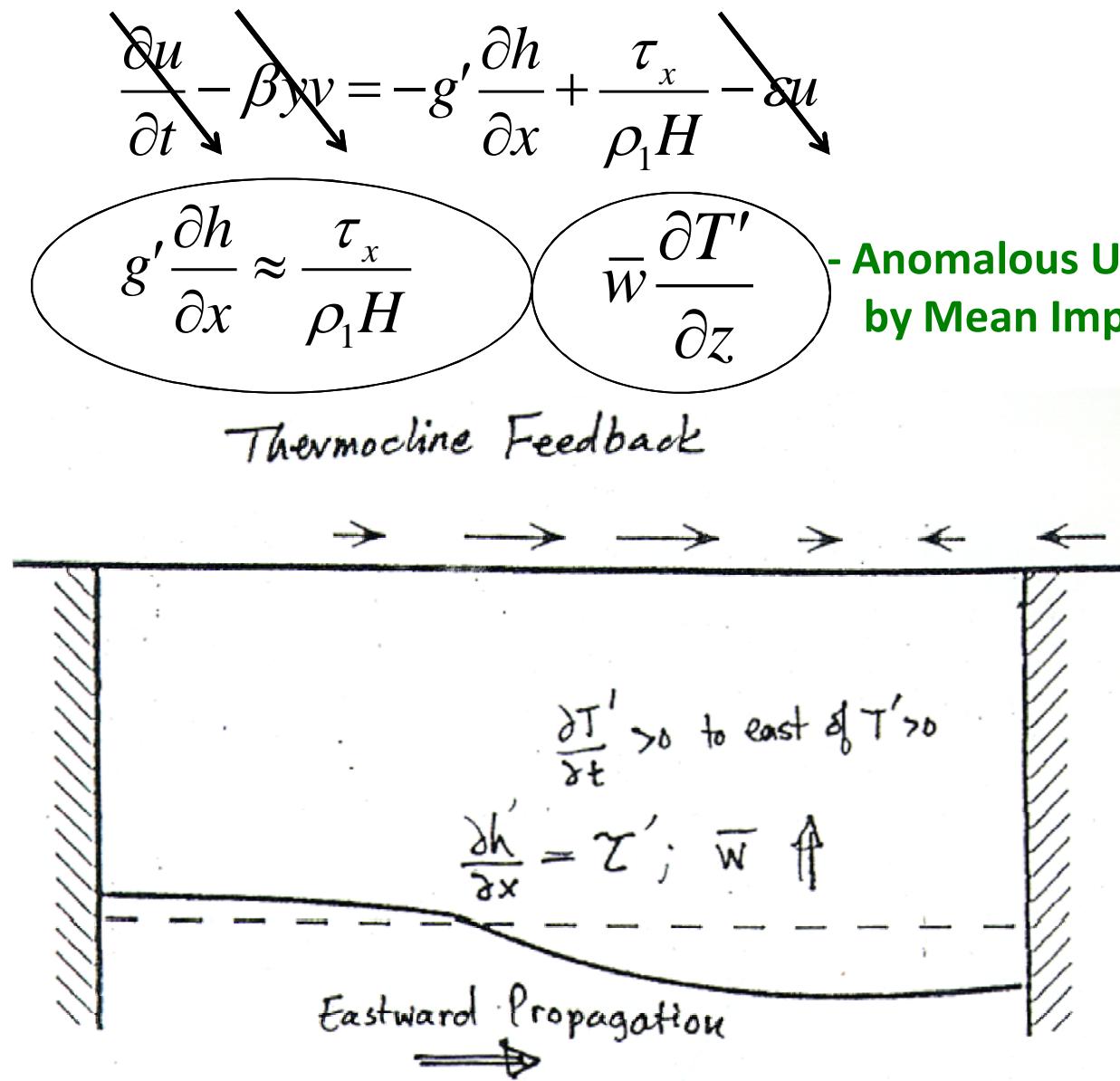
Thermocline  
Perturbations  
Unimportant



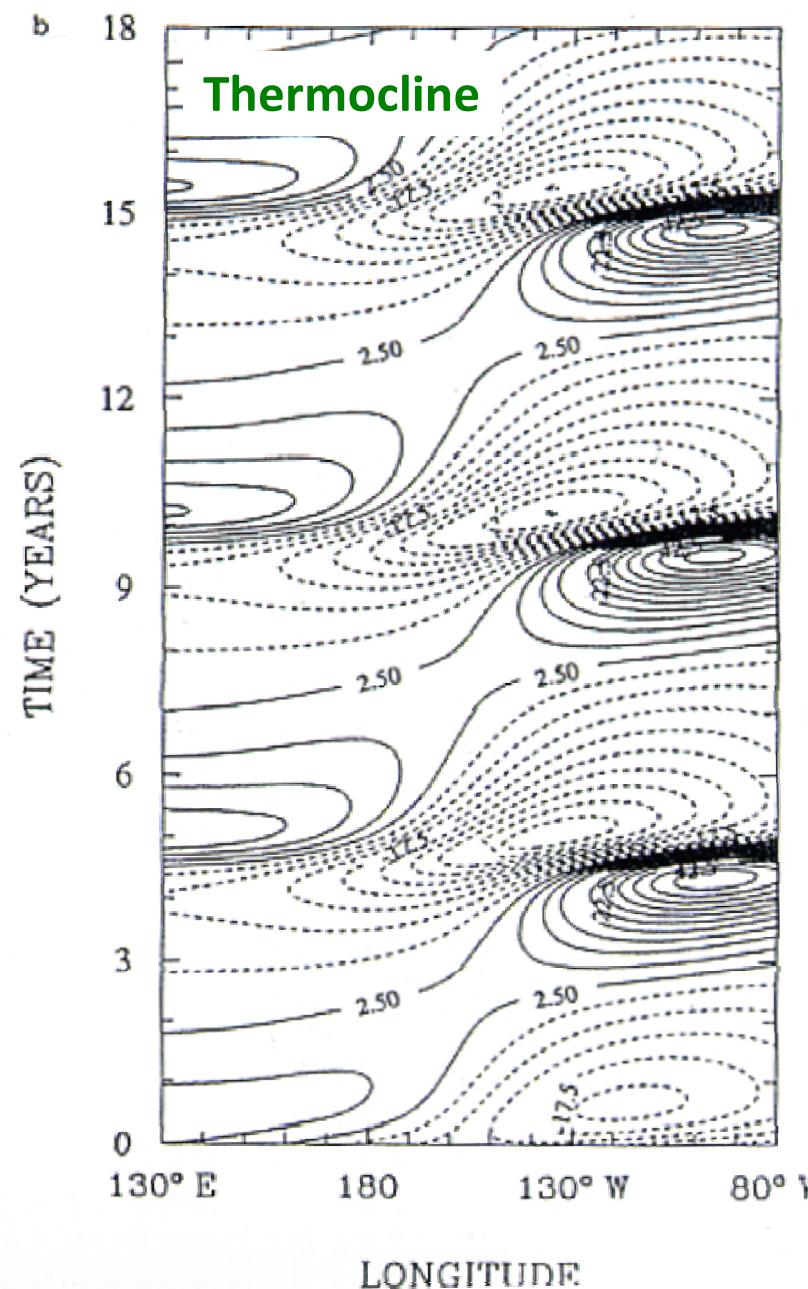
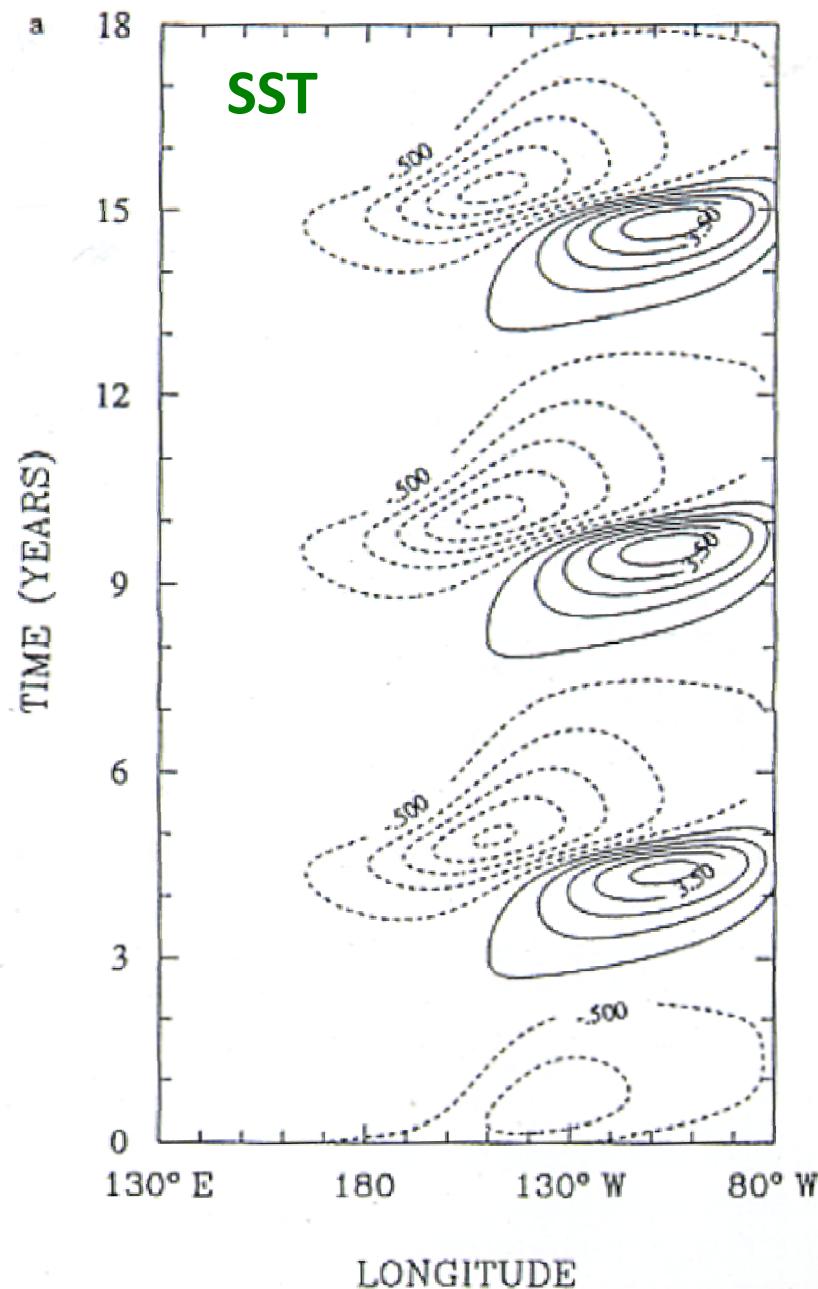
# Surface Layer Feedback Mechanism



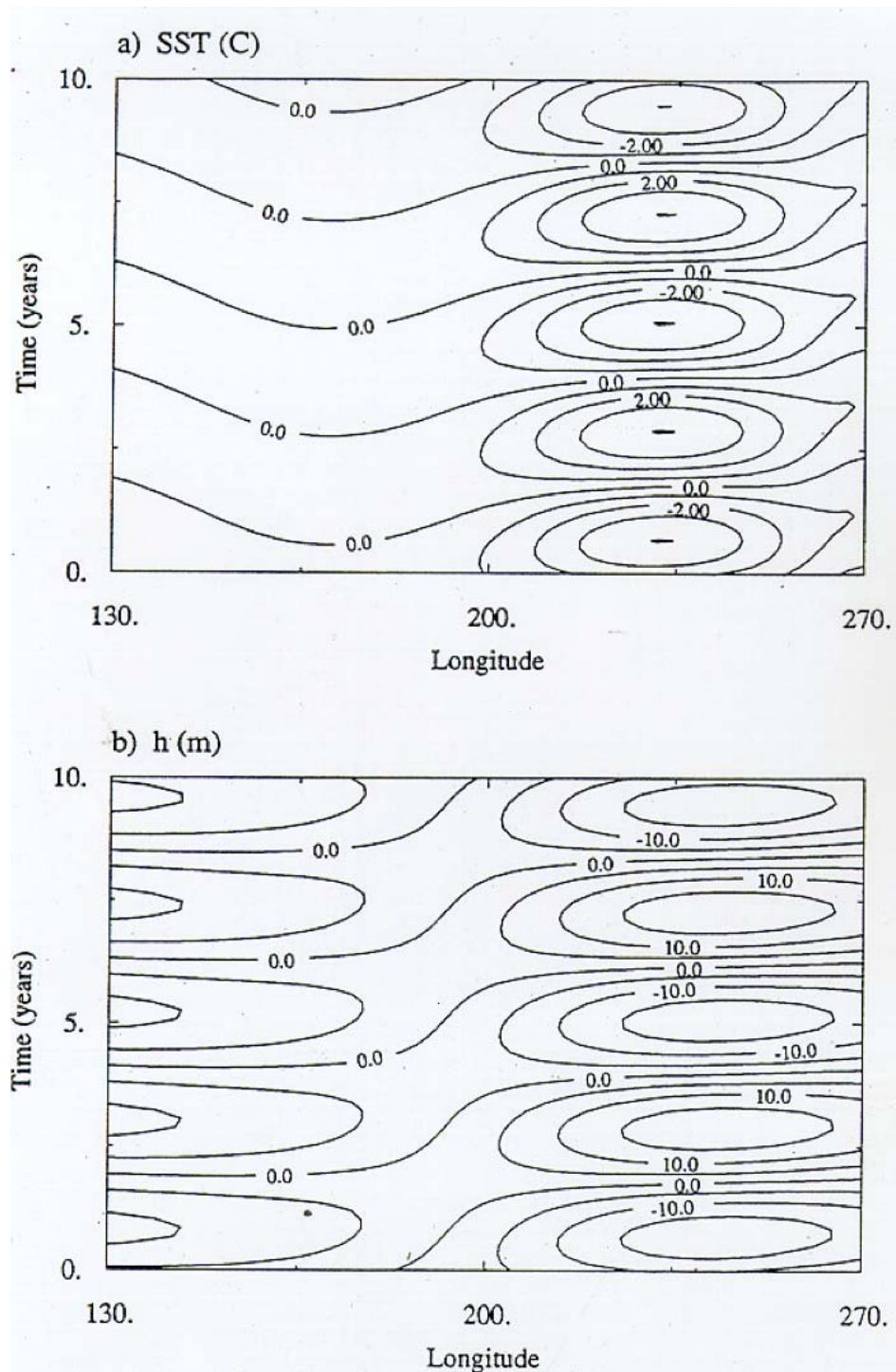
# Thermocline Feedback Mechanism (Slow SST – Fast Wave Limit)



# Thermocline Feedback Mechanism



# Mixing Both Mechanisms



# Outline

- **Free Equatorial Waves**
  - Rossby and Kelvin Wave
- **Forced Equatorial Waves**
  - Equatorial Sverdrup Balance
- **Coupled Problem**
  - Delayed Oscillator, Recharge Oscillator, Fast Wave – Slow SST

