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*6 - 17 August 2012*

**Exploring heavy-fermion quantum criticality in the extreme 3D limit**

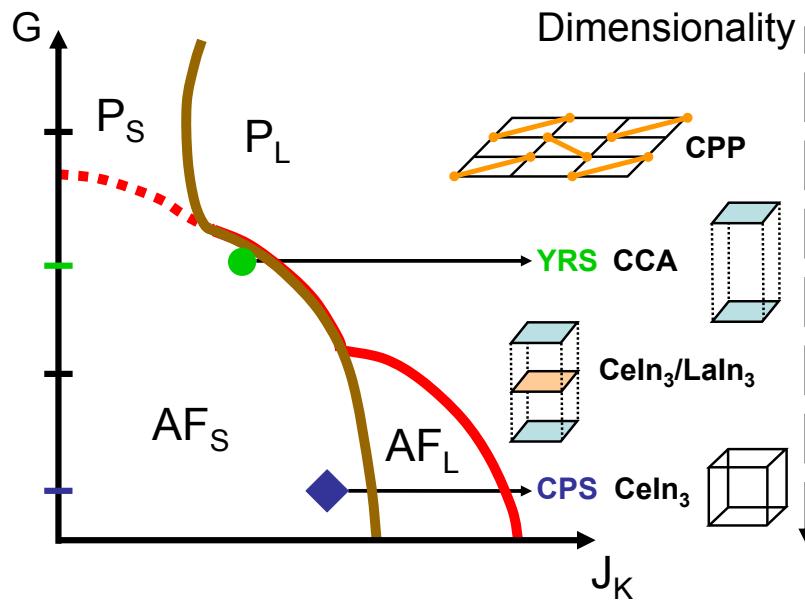
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# Exploring heavy-fermion quantum criticality in the extreme 3D limit

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# Exploring heavy-fermion quantum criticality in the extreme 3D limit

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- Heavy fermion quantum criticality: Historical perspective
- The case of  $\text{YbRh}_2\text{Si}_2$
- The new *cubic* material  $\text{Ce}_3\text{Pd}_{20}\text{Si}_6$
- Materials in the global phase diagram

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*1: ESS, Lund, 2: ILL, Grenoble, 3: ISIS, Oxon, 4: LLB, Saclay*

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*Rice University, USA*

**YbRh<sub>2</sub>Si<sub>2</sub>:** S. Friedemann\*, P. Gegenwart\*, C. Geibel, S. Hartmann\*, C. Krellner\*,  
N. Oeschler\*, S. Wirth, A. Pikul\*, S. Kirchner (& PKS), F. Steglich

*Max-Planck-Institut für Chemische Physics fester Stoffe, Dresden*

**P. Coleman**

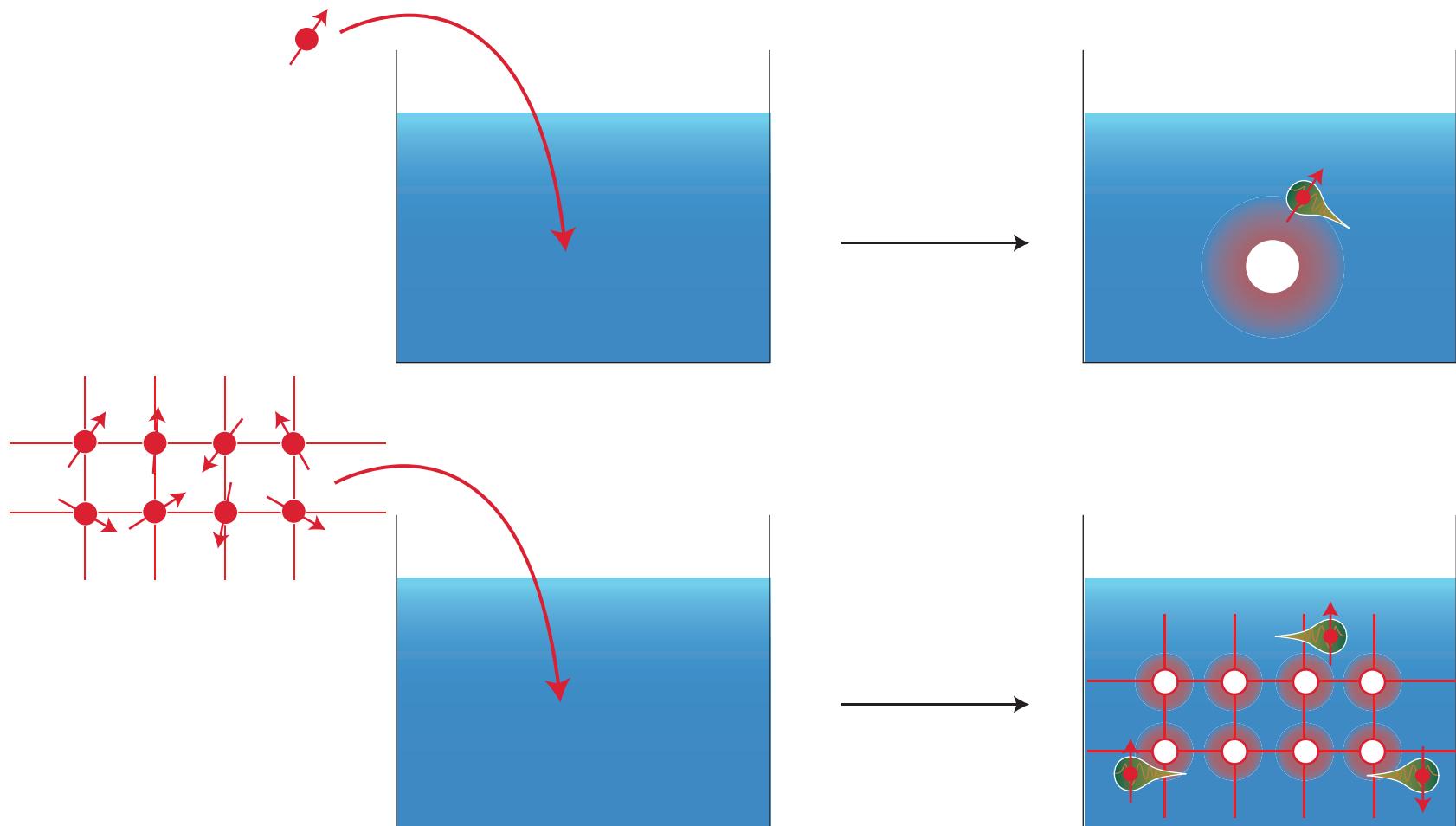
*Rutgers University, USA*



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Vienna University of Technology

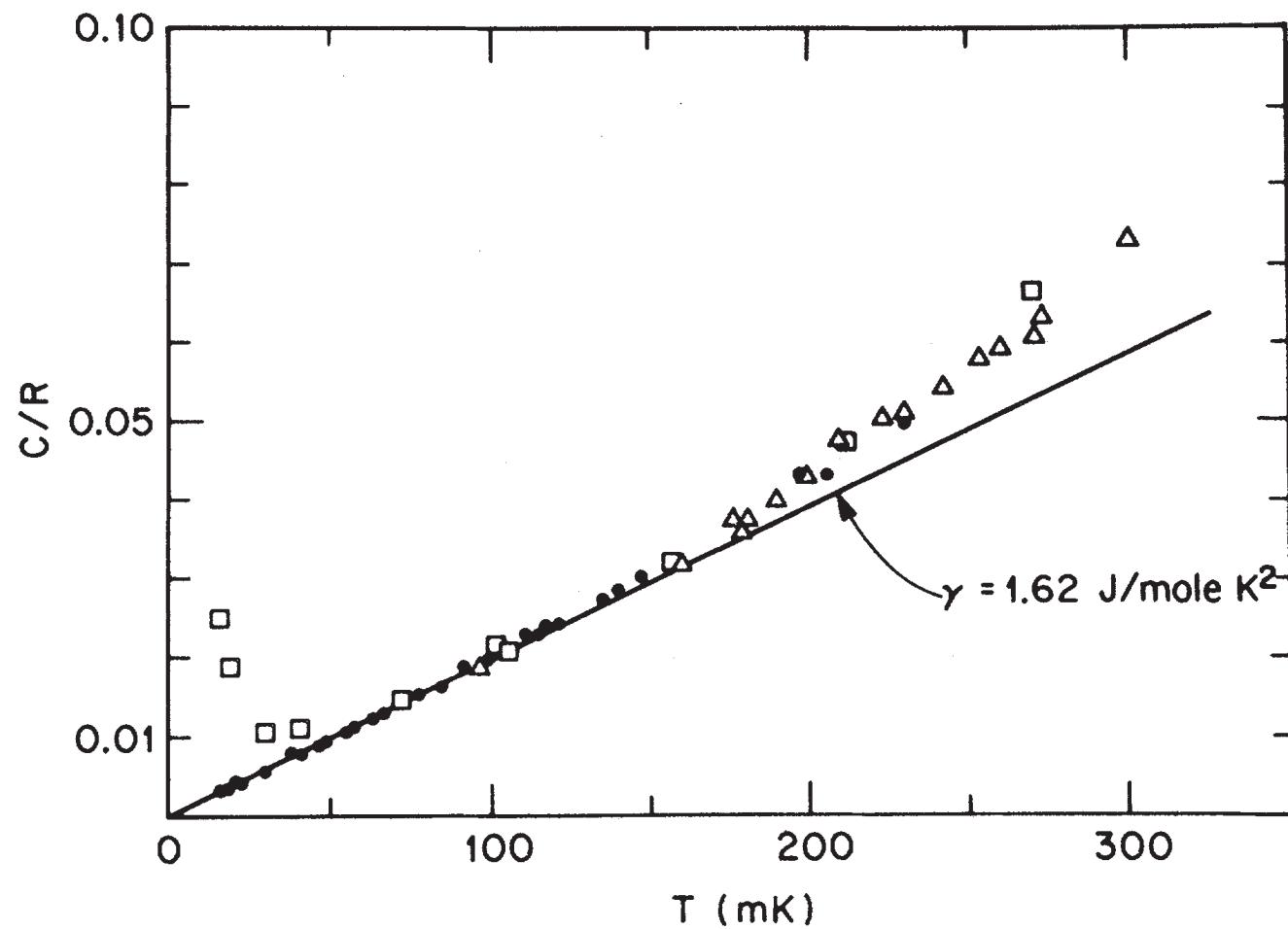


## Kondo effect and heavy fermion compounds



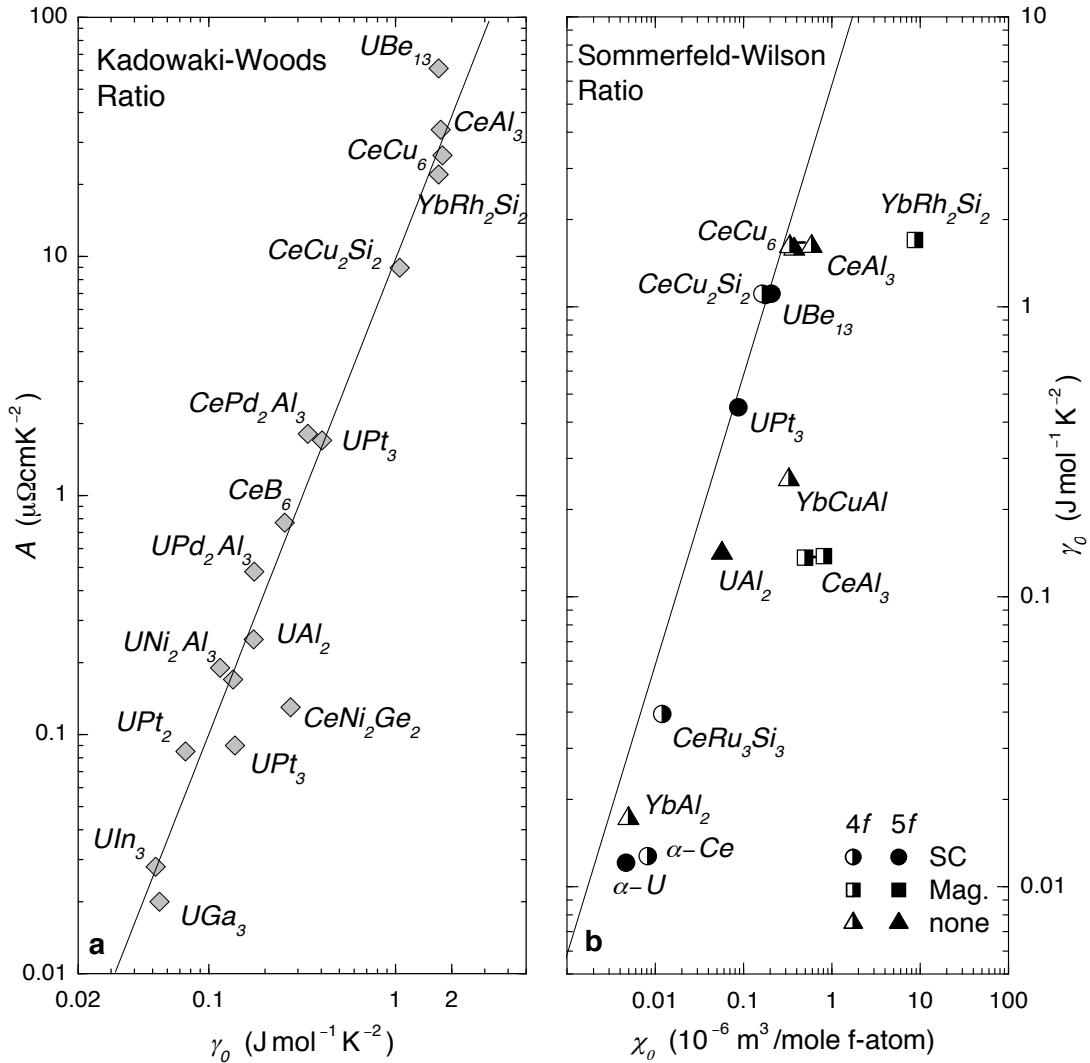
(Coleman, Nature Mater. 11 (2012) 185, news & views)

First heavy fermion/electron compound: CeAl<sub>3</sub>



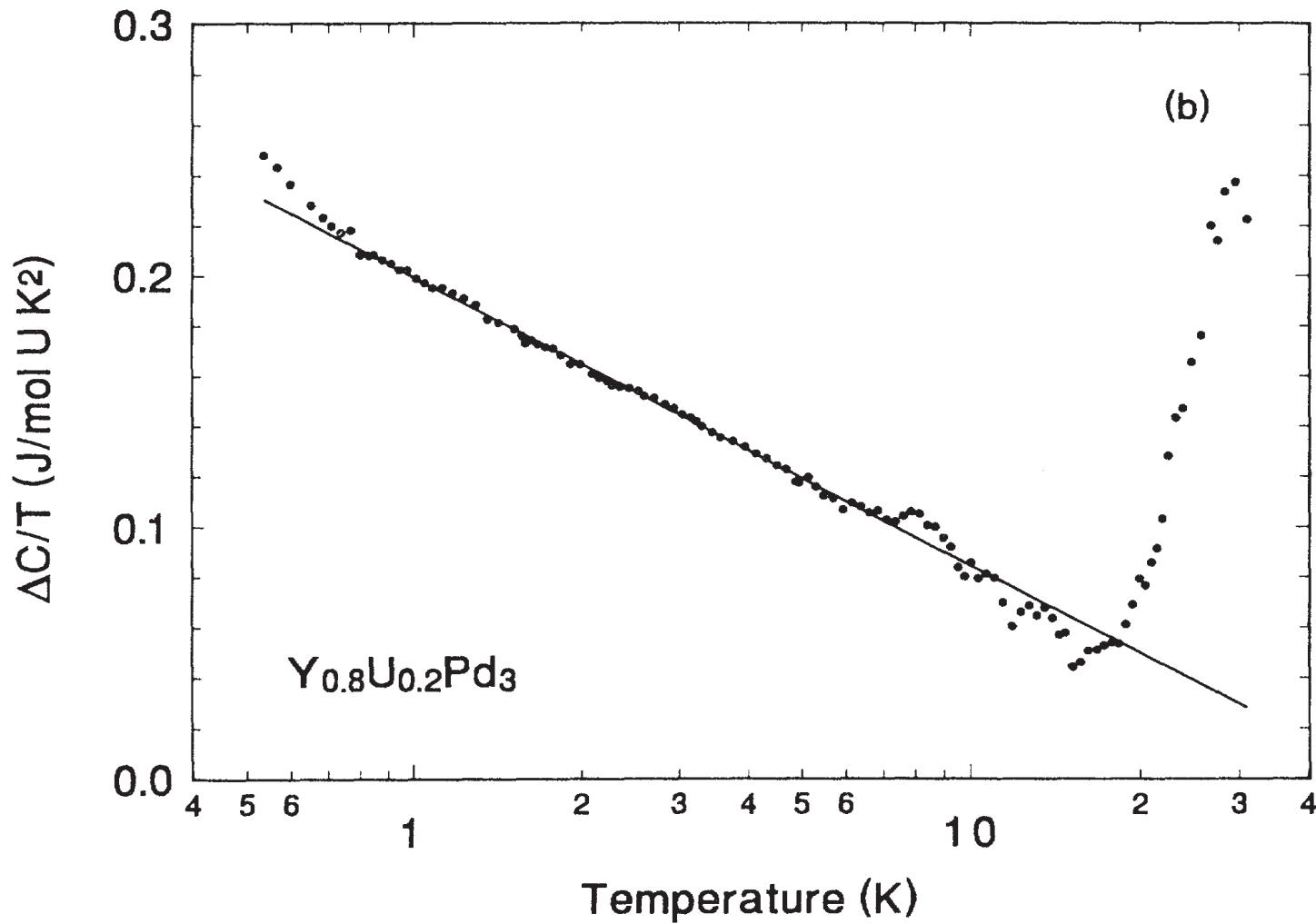
(Andres et al., Phys. Rev. Lett. 35 (1975) 1779.)

## Kadowaki – Woods plot



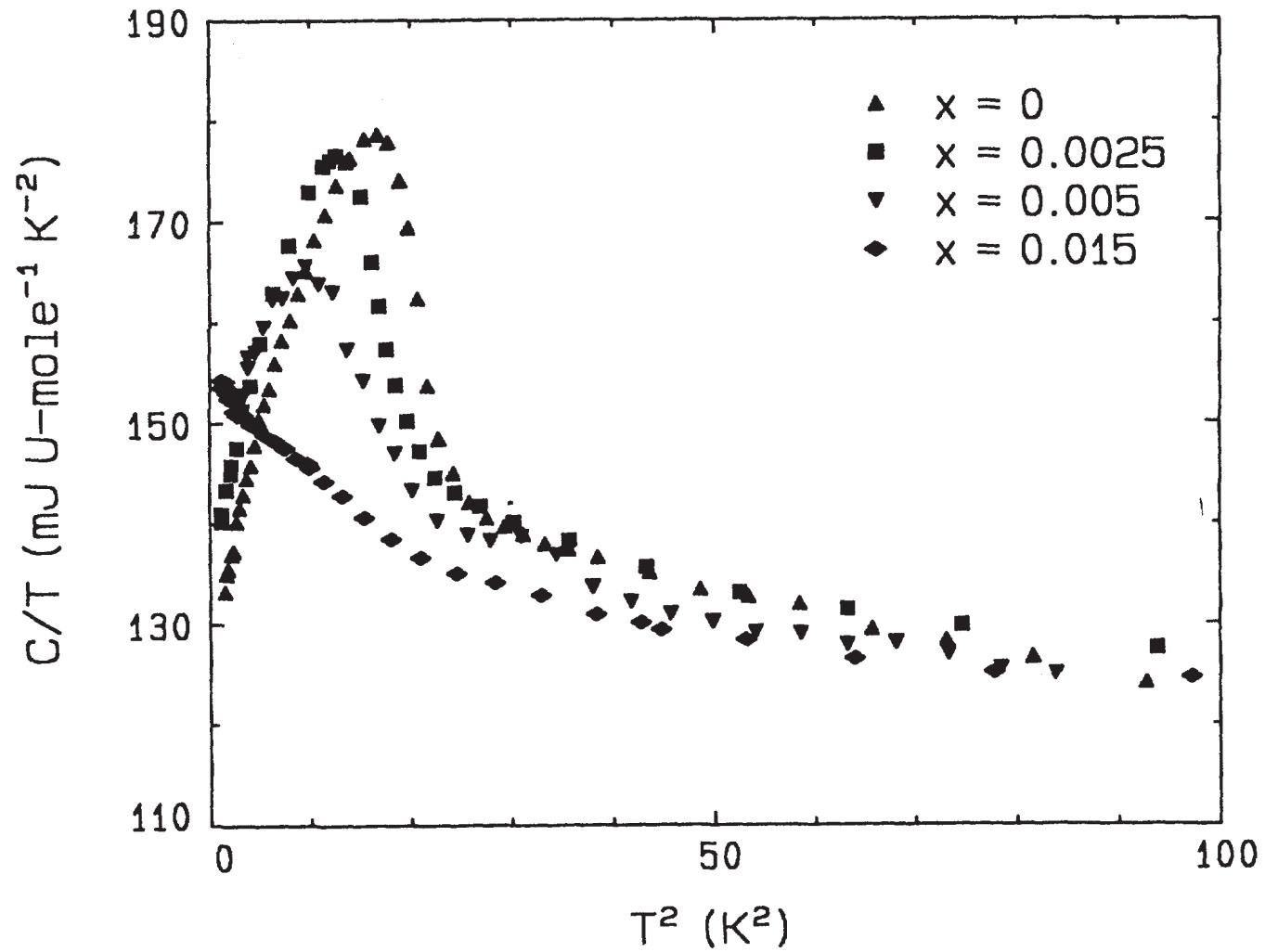
(Custers, PhD thesis, and Kadowaki & Woods, Solid State Commun. 58 (1986) 507)

Non-Fermi liquid behaviour:  $\text{Y}_{0.8}\text{U}_{0.2}\text{Pd}_3$



(Seaman et al., Phys. Rev. Lett. 67 (1991) 2881)

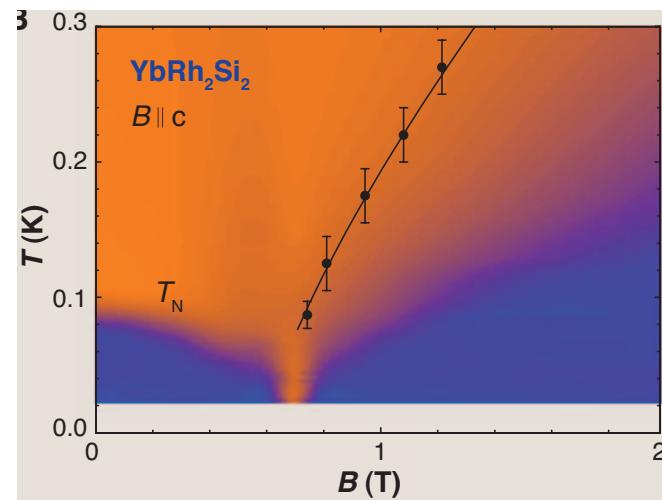
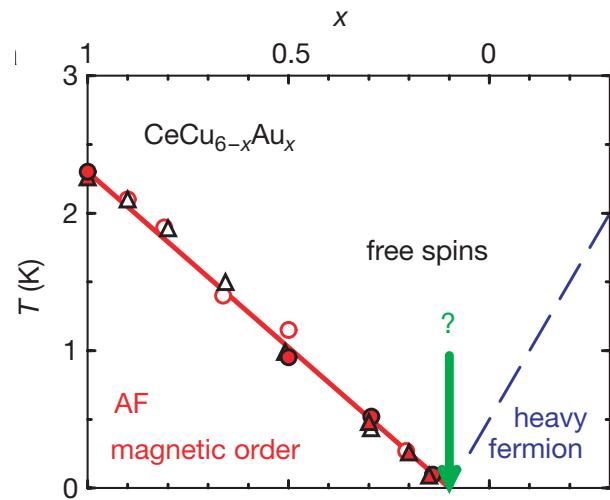
## Non-Fermi liquid near magnetic order: $U_{1-x}Th_xNi_2Al_3$



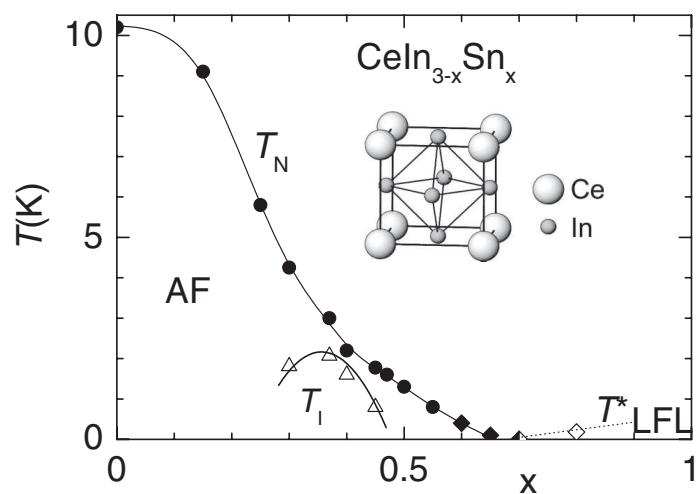
(Kim et al., Phys. Rev. B 47 (1993) 12403)

## NFL behaviour at quantum critical points

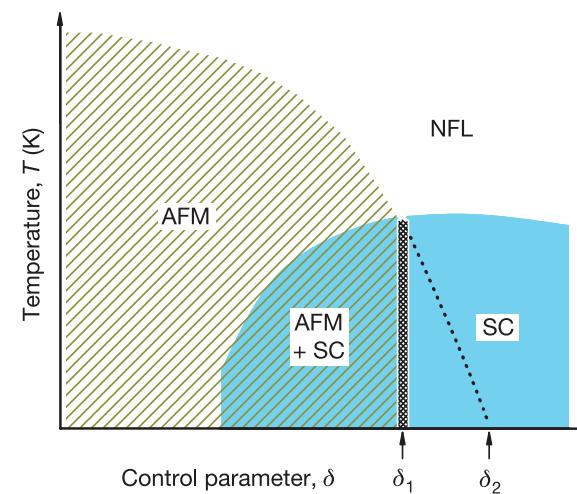
$\text{CeCu}_{6-x}\text{Au}_x$  (Schröder et al, Nature 2000)    $\text{YbRh}_2\text{Si}_2$  (Custers et al., Nature 2001)



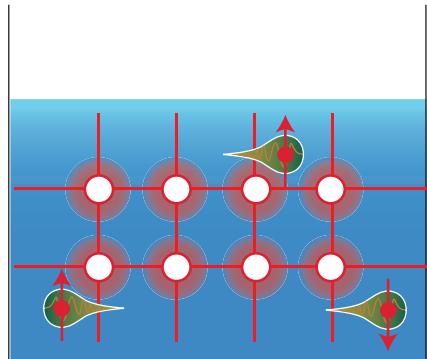
$\text{CeIn}_{3-x}\text{Sn}_x$  (Küchler et al, PRL 2006)



$\text{CeRhIn}_5$  (Park et al., Nature 2006)

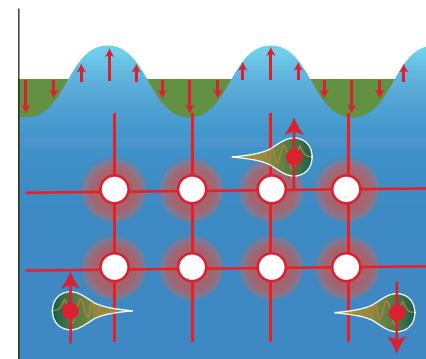


## Standard scenario: Spin density wave (SDW) formation



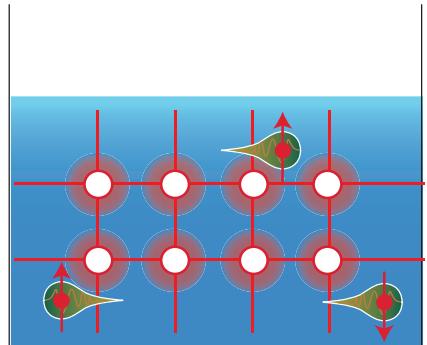
Paramagnet

(i) SDW



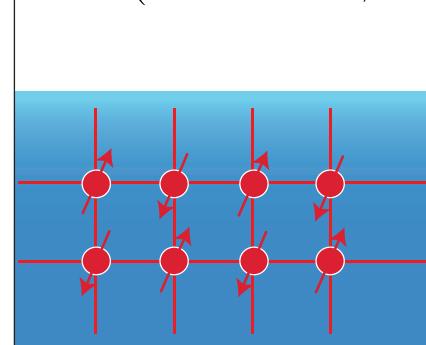
Itinerant antiferromagnet

## Alternative scenario in 2D: Kondo breakdown (Coleman, Si, Schröder, ...)



Paramagnet

(ii) KD

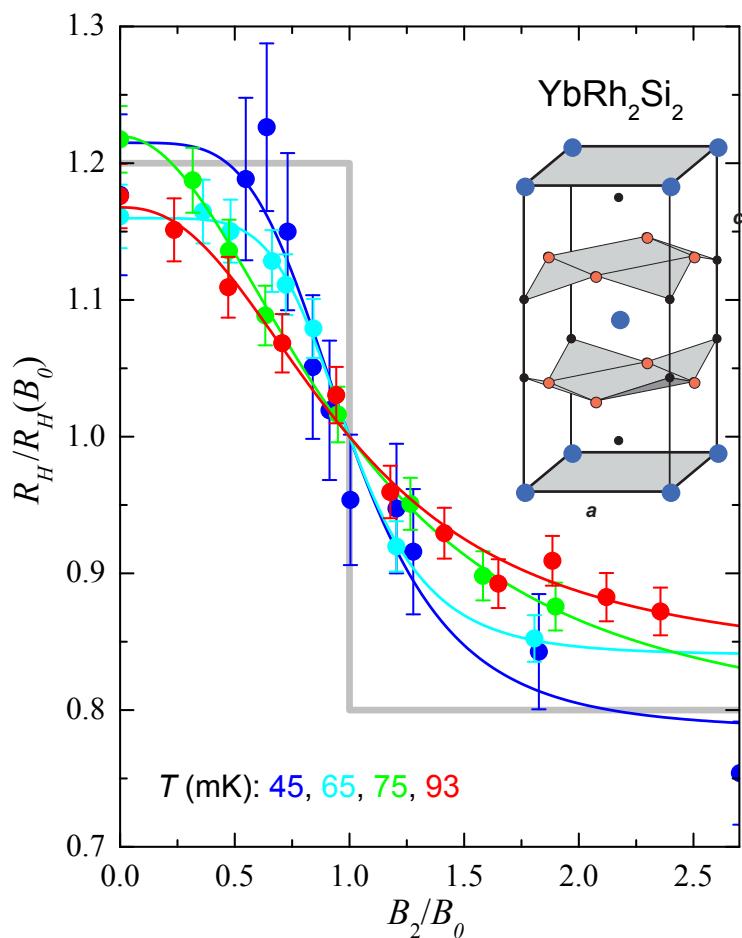


Local moment antiferromagnet

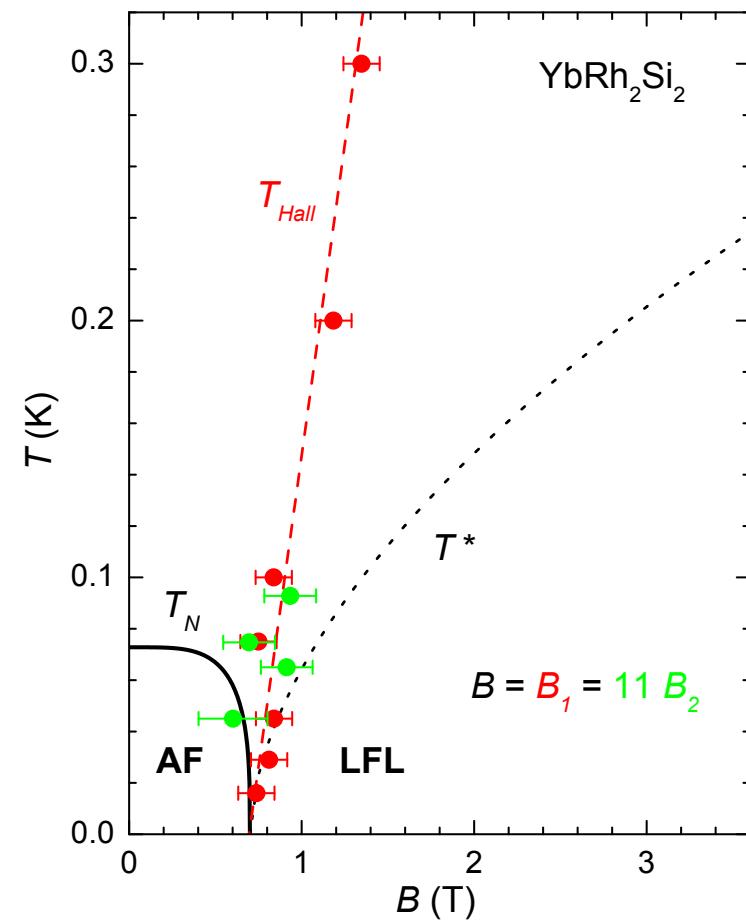
(Coleman, Nature Mater. 11 (2012) 185, news & views)

# Hall effect in tetragonal $\text{YbRh}_2\text{Si}_2$ with 2D spin fluctuations

Hall coefficient vs field



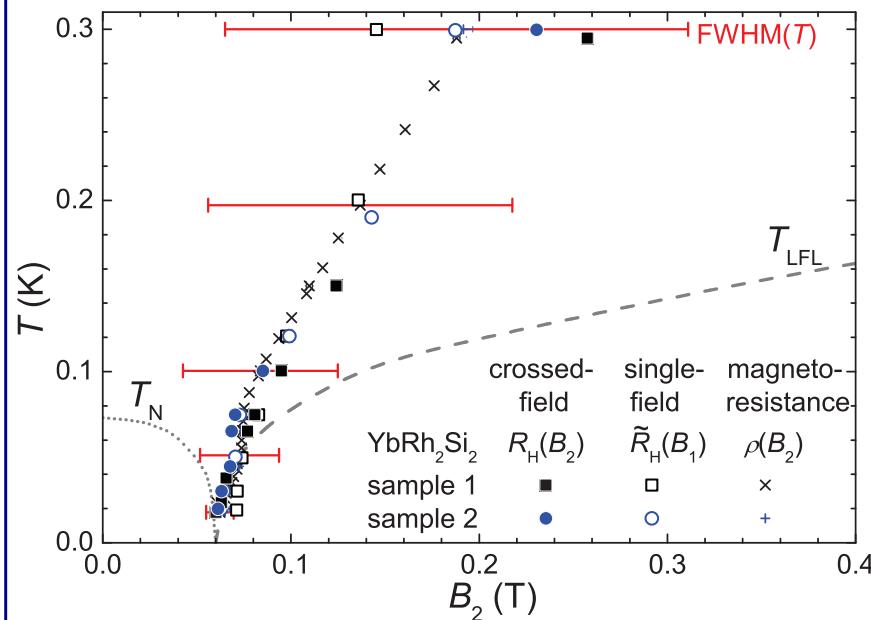
Phase diagram



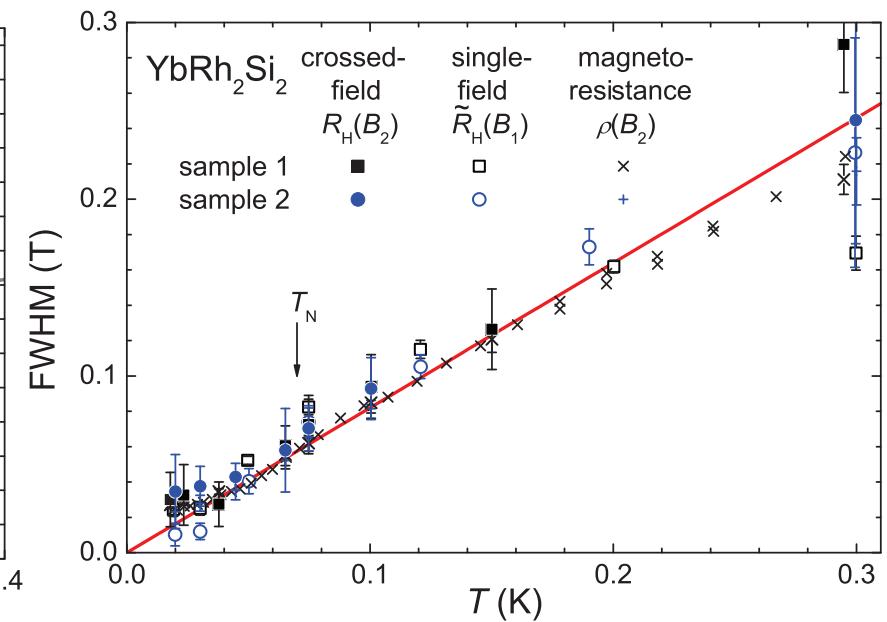
(SP et al., Nature 432 (2004) 881)

# Hall effect in tetragonal $\text{YbRh}_2\text{Si}_2$ with 2D spin fluctuations: Experiments on purest samples with enhanced resolution

Phase diagram



Crossover width



(Friedemann et al., PNAS 107  
(2010) 14547)

$\text{FWHM} \sim T$  (valid up to 1 K)

Suggested scenarios (list incomplete ...):

**Kondo breakdown/Orbital selective Mott transition:**

Kondo lattice, Kondo-Heisenberg, PAM, Bose-Fermi Kondo models, ...

*Coleman, Fabrizio, Kim, Kotliar, Pépin, Senthil, Si, Zaanen, ...*

**Lifshitz transition/Topological transition:**

2D Kondo lattice model, band picture ...

*Assaad, Vojta, Watanabe, ...*

**Valence transition/Valence criticality:**

PAM with  $U_{fc}$ , band picture ...

*Miyake, Norman, Watanabe, ...*

**Quantum tricritical point:**

Self-consistent renormalization theory for spin fluctuations

*Imada, Misawa, Yamaji*

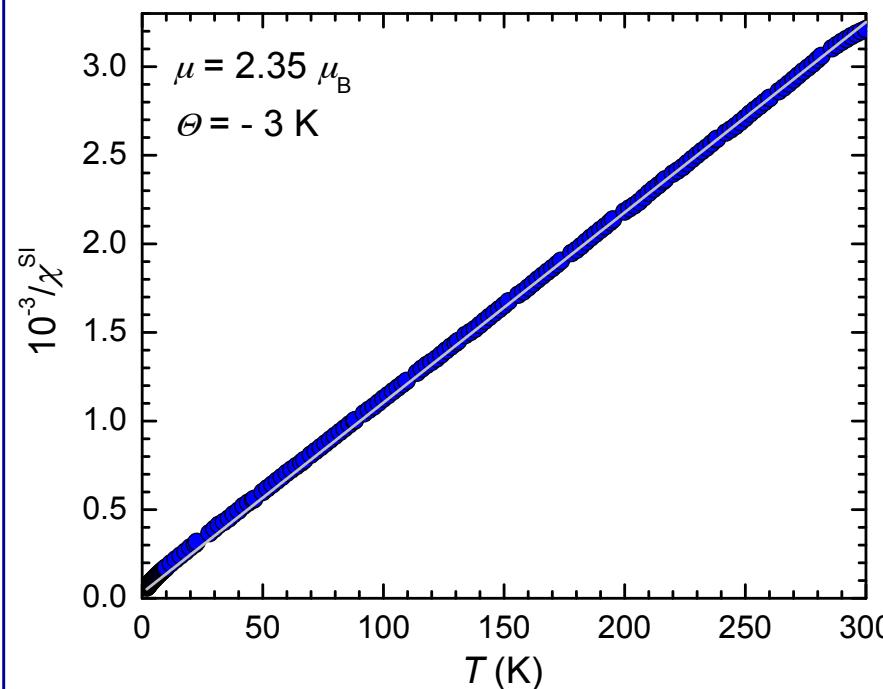
**Weak-field breakdown:**

Boltzmann transport theory

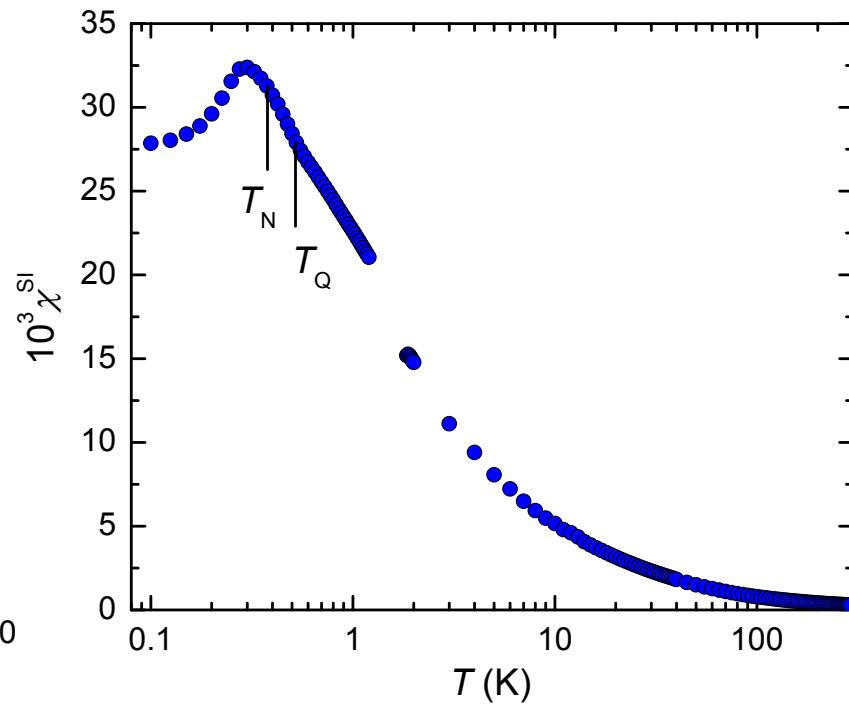
*Schofield*

## A new *cubic* material: Ce<sub>3</sub>Pd<sub>20</sub>Si<sub>6</sub>

Inverse susceptibility



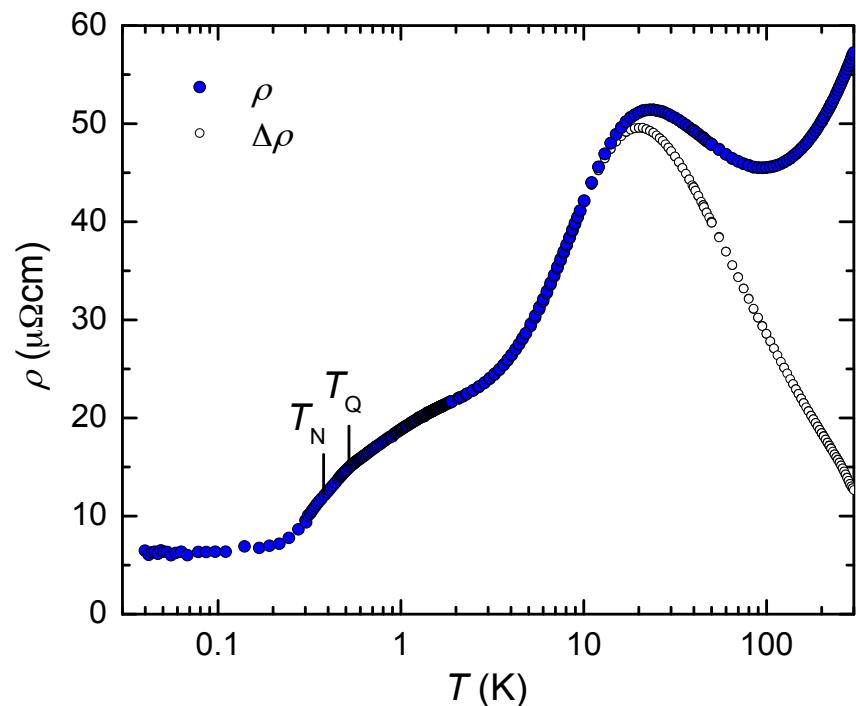
Susceptibility



$$\chi_0 = 10 \cdot 10^{-6} \text{ m}^3/\text{mol Ce}$$

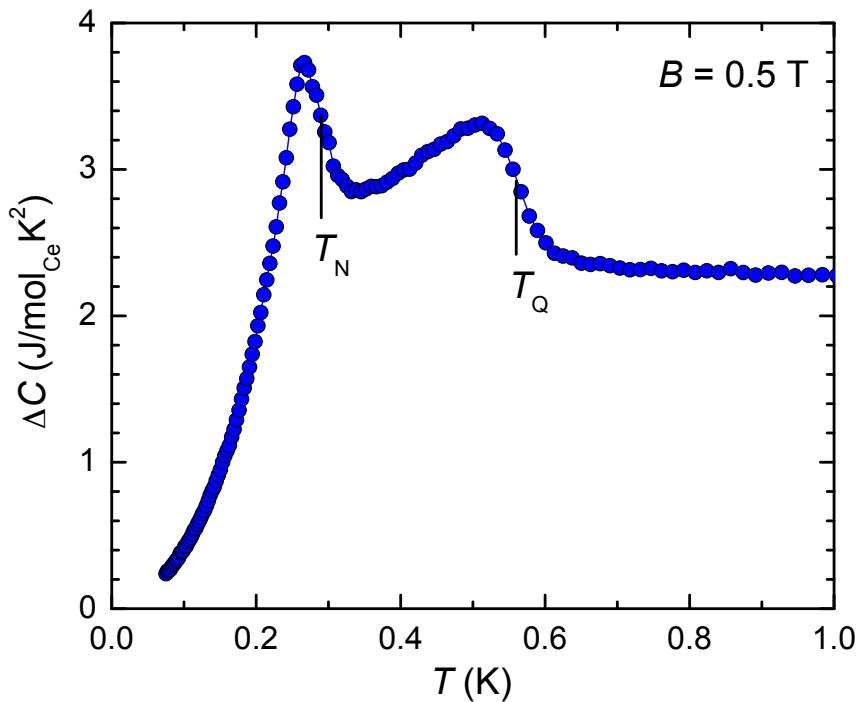
## A new *cubic* material: Ce<sub>3</sub>Pd<sub>20</sub>Si<sub>6</sub>

Electrical resistivity



$$\rho = \rho_0 + AT^2, A = 31 \mu\Omega\text{cm}$$

Electronic specific heat

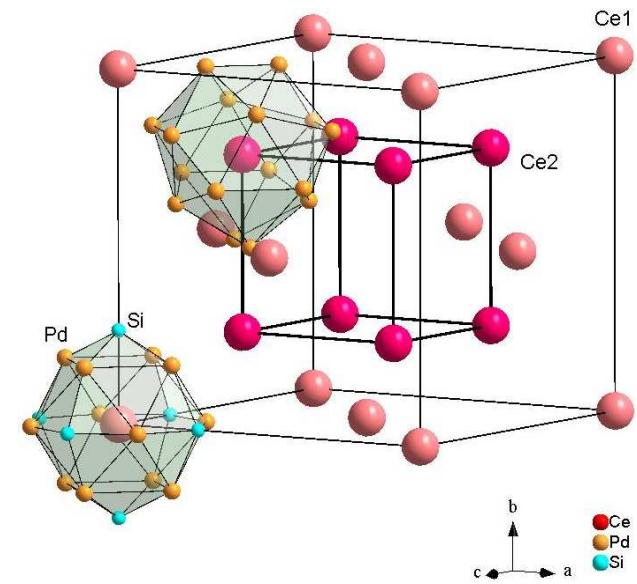
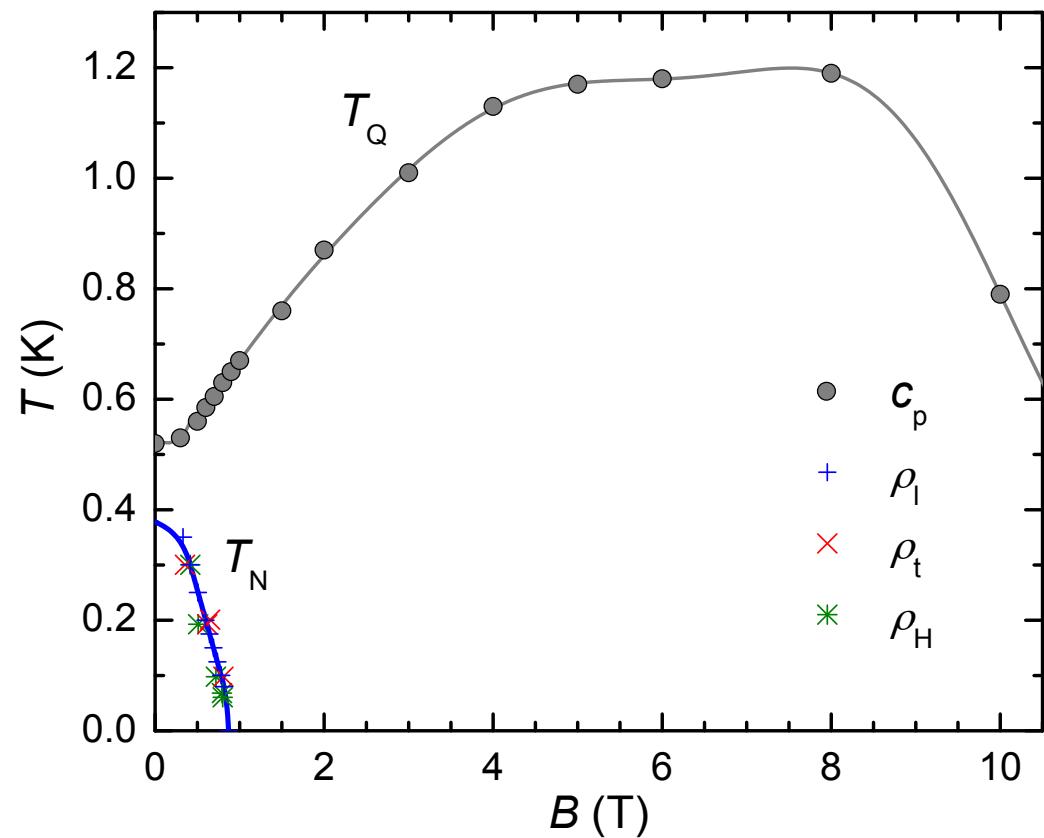


$$\Delta C/T = \gamma + \beta T^2, \gamma = 1.45 \text{ J/molK}^2$$

$$\text{KW: } A/\gamma^2 = 1.47 \cdot 10^{-5} (\Omega\text{m}/\text{K}^2)/(\text{J/molK}^2)$$

# A new *cubic* material: $\text{Ce}_3\text{Pd}_{20}\text{Si}_6$

Temperature-field phase diagram



Cubic,  $Fm\bar{3}m$

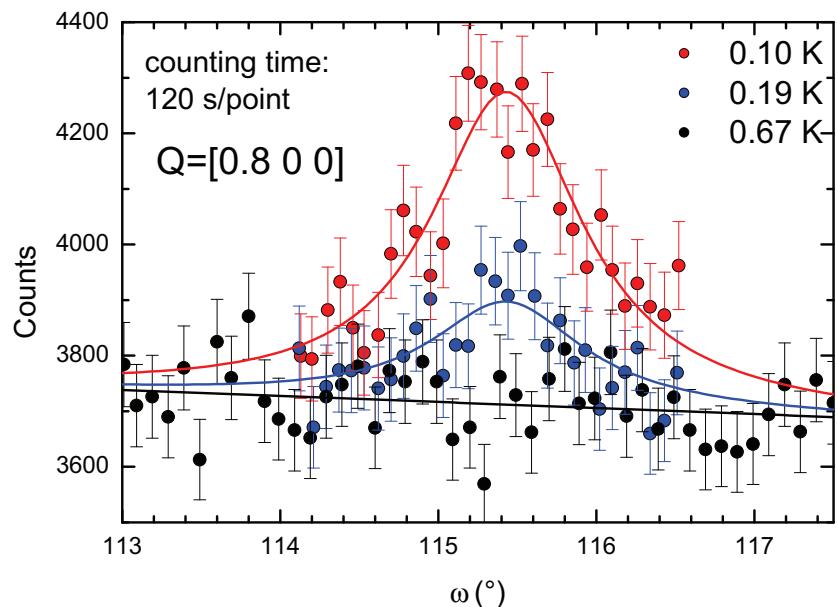
Ce1: fcc,  $4a$ ,  $\Gamma_7$ ,  $T_N$

Ce2: sc,  $8c$ ,  $\Gamma_8$ ,  $T_Q$

(Deen et al., Phys. Rev. B 81 (2010) 064427)

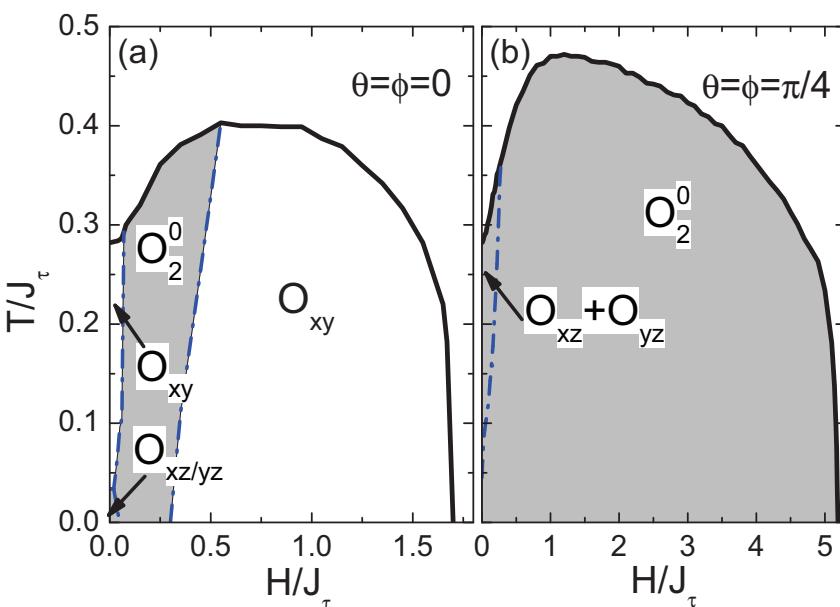
# Ordered phases in Ce<sub>3</sub>Pd<sub>20</sub>Si<sub>6</sub>

Below  $T_N$



(Lorenzer, Deen et al., ILL,  
unpublished)

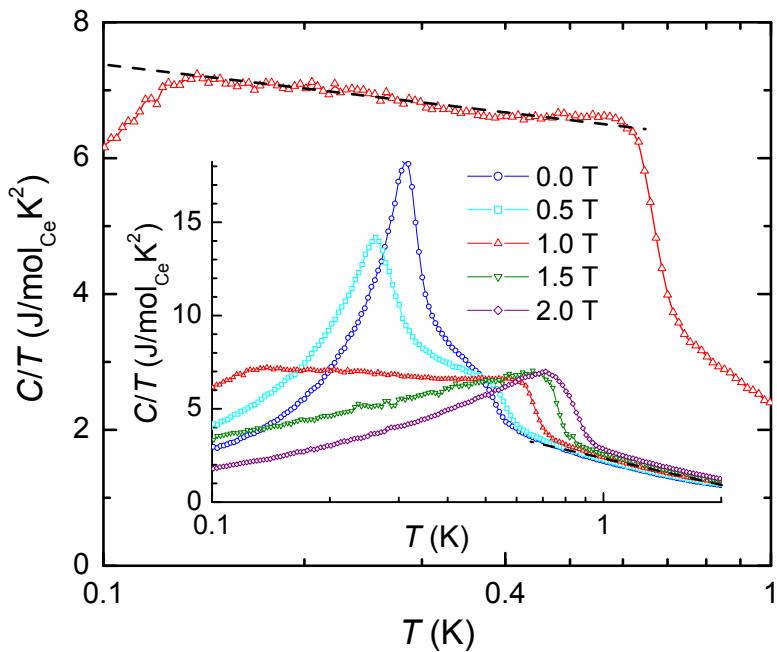
Below  $T_Q$



(Custers et al., Nature Mater. 11  
(2012) 189; SI)

# Non-Fermi liquid properties of Ce<sub>3</sub>Pd<sub>20</sub>Si<sub>6</sub>

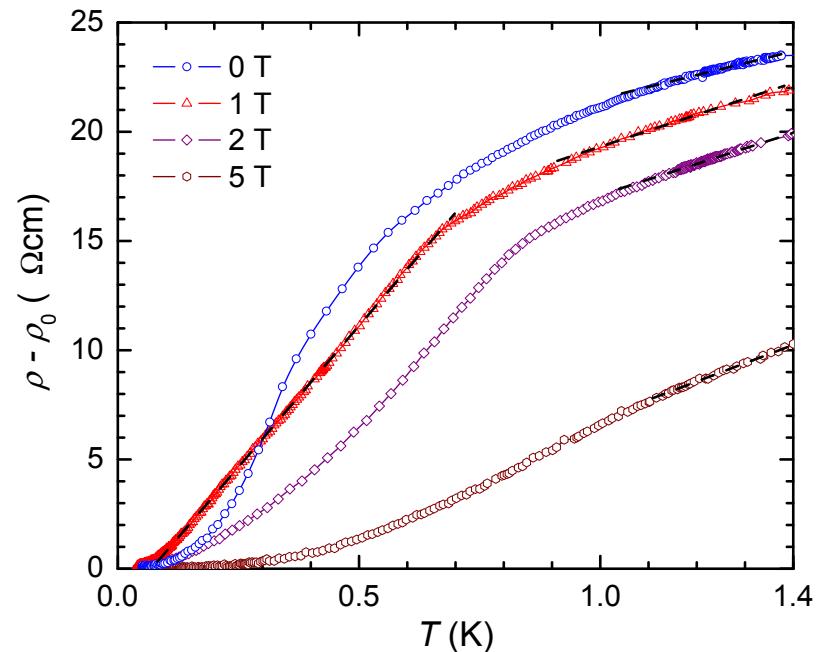
Specific heat



$$\Delta C/T \propto -\ln T$$

SDW (AFM,  $d = 3$ ):  
 $\Delta C/T = \gamma - b\sqrt{T}$

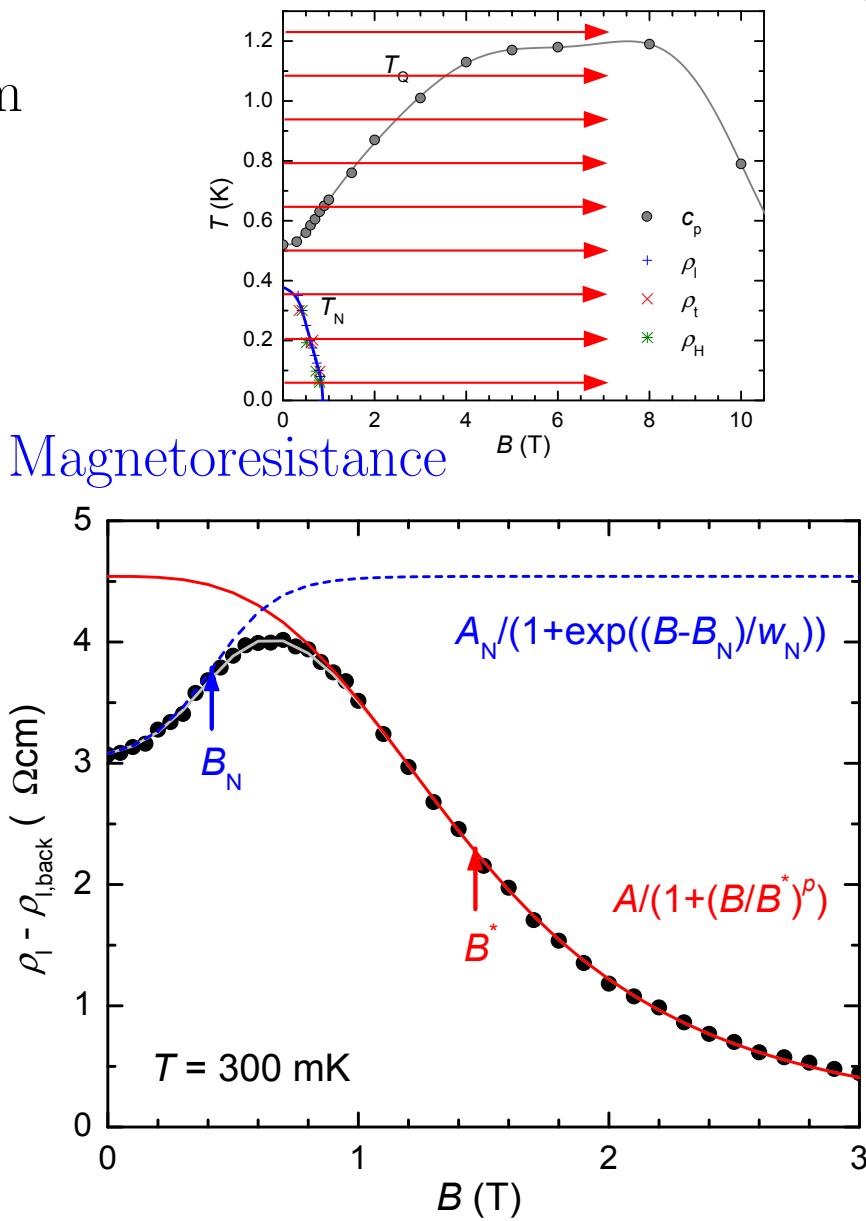
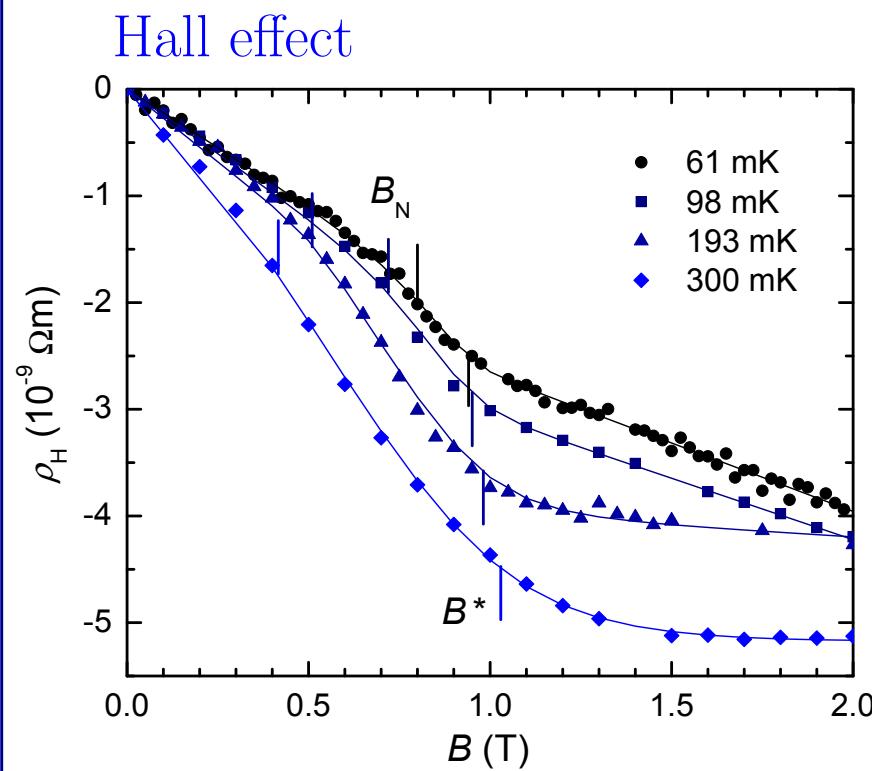
Electrical resistivity



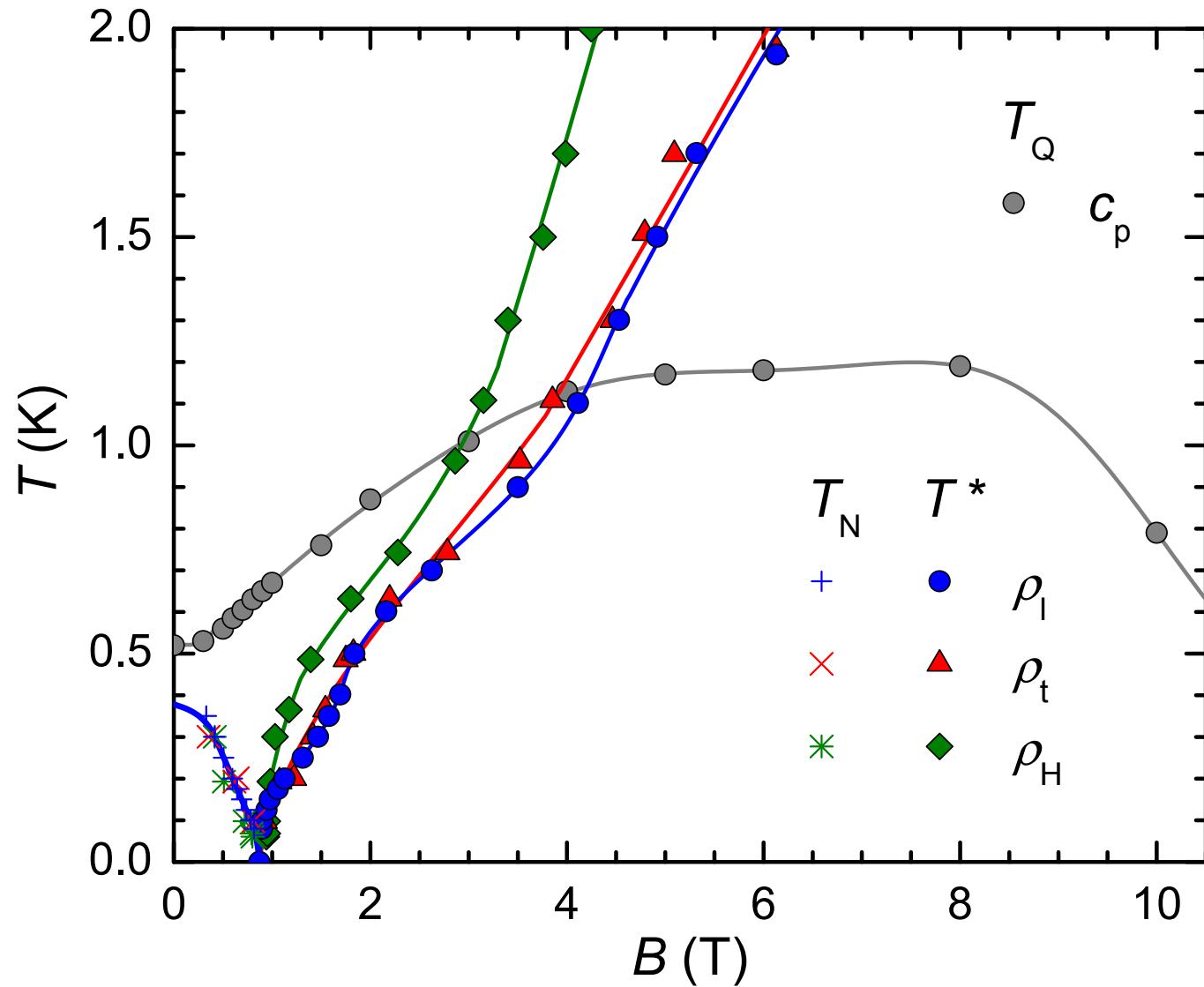
$$\Delta\rho \sim T$$

SDW (AFM,  $d = 3$ ):  $\Delta\rho \sim T^{3/2}$

## Isotherms crossing phase diagram

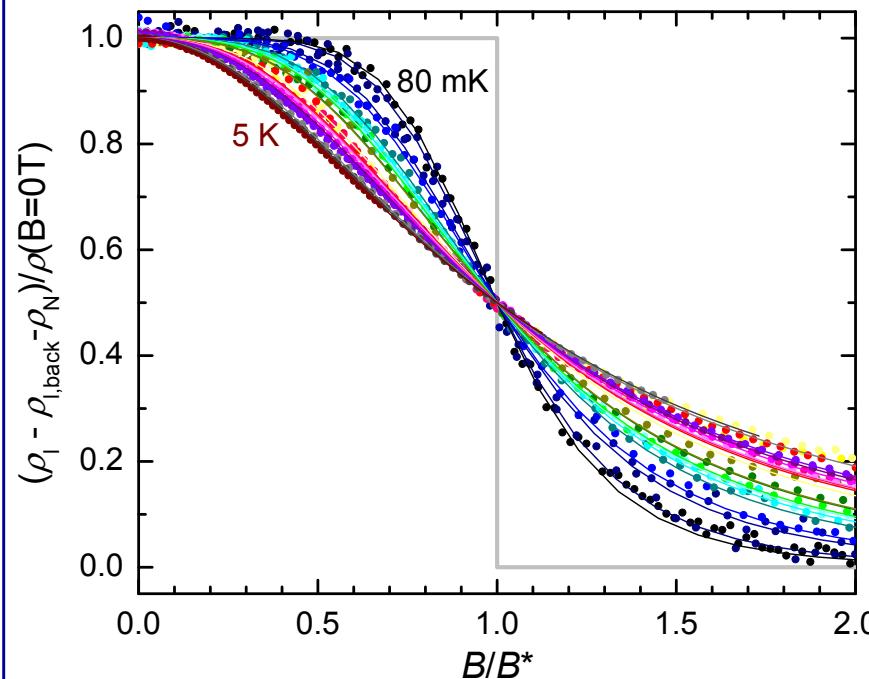


# Phase diagram of $\text{Ce}_3\text{Pd}_{20}\text{Si}_6$ with $T^*$ scale

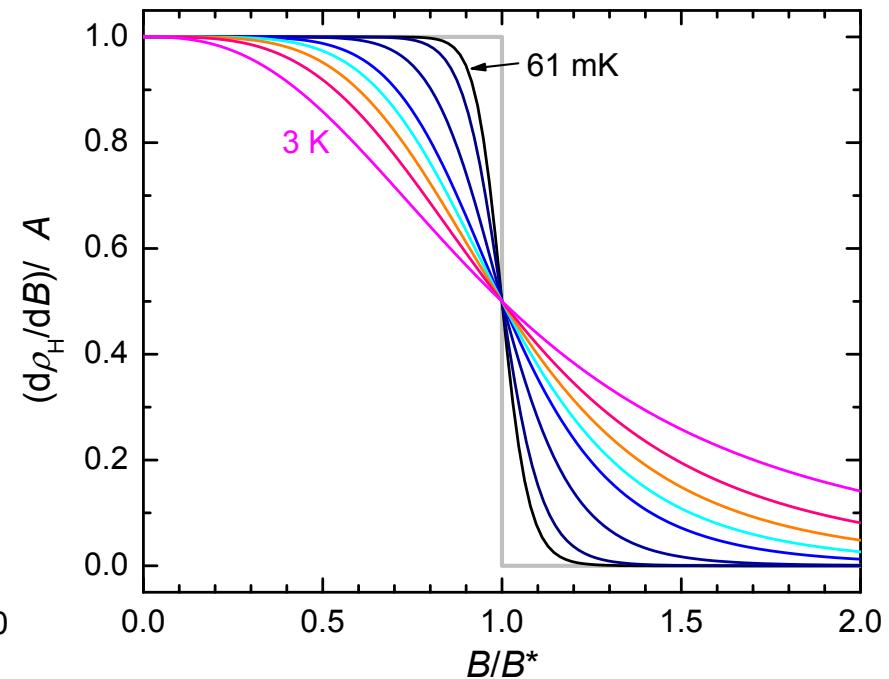


# Crossovers in magnetotransport of $\text{Ce}_3\text{Pd}_{20}\text{Si}_6$ at $B^*$

Longitudinal magnetoresistance

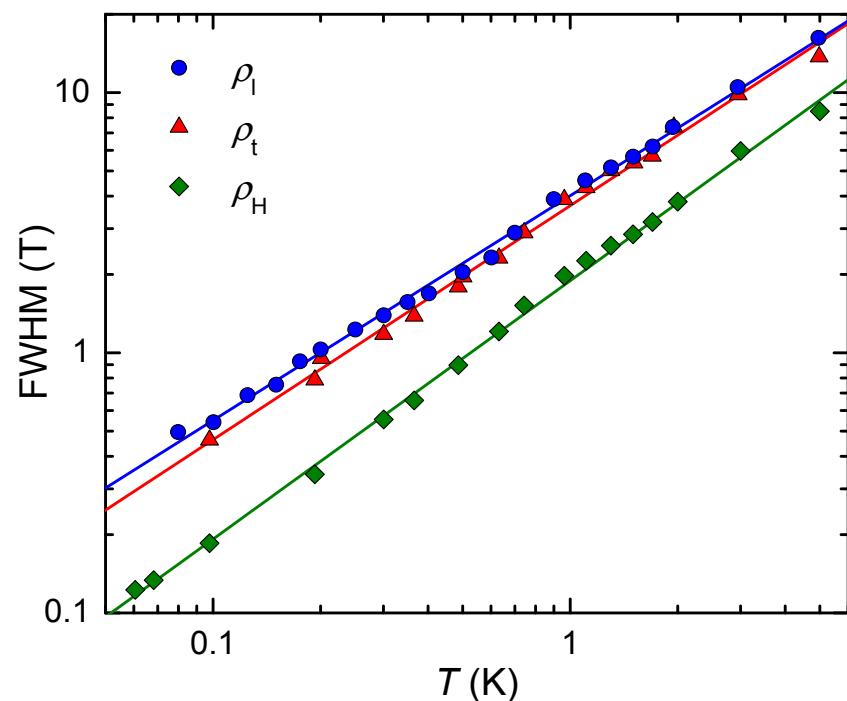


Differential Hall coefficient

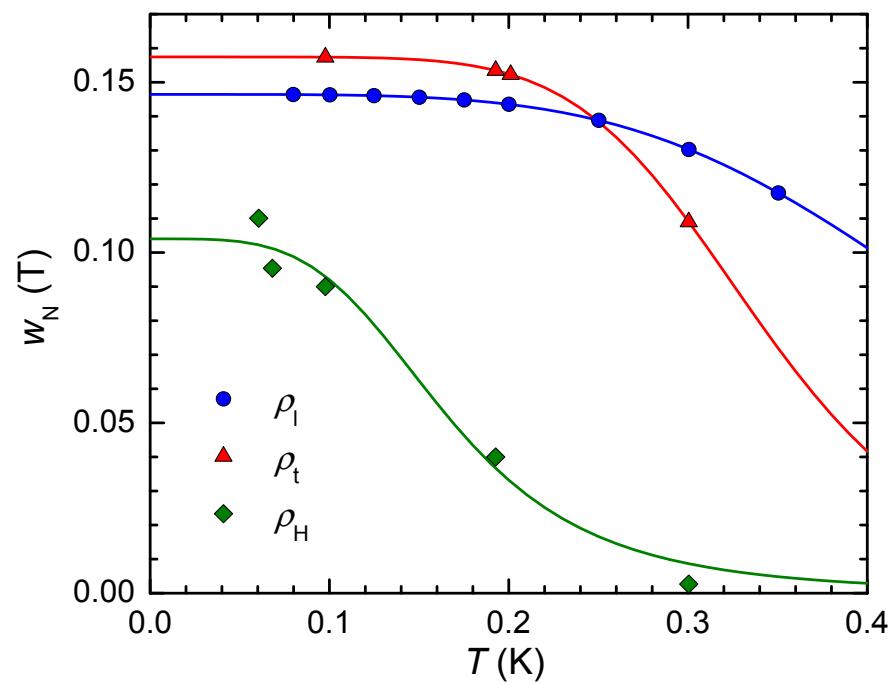


## Crossovers at $B^*$ vs transition at $B_N$

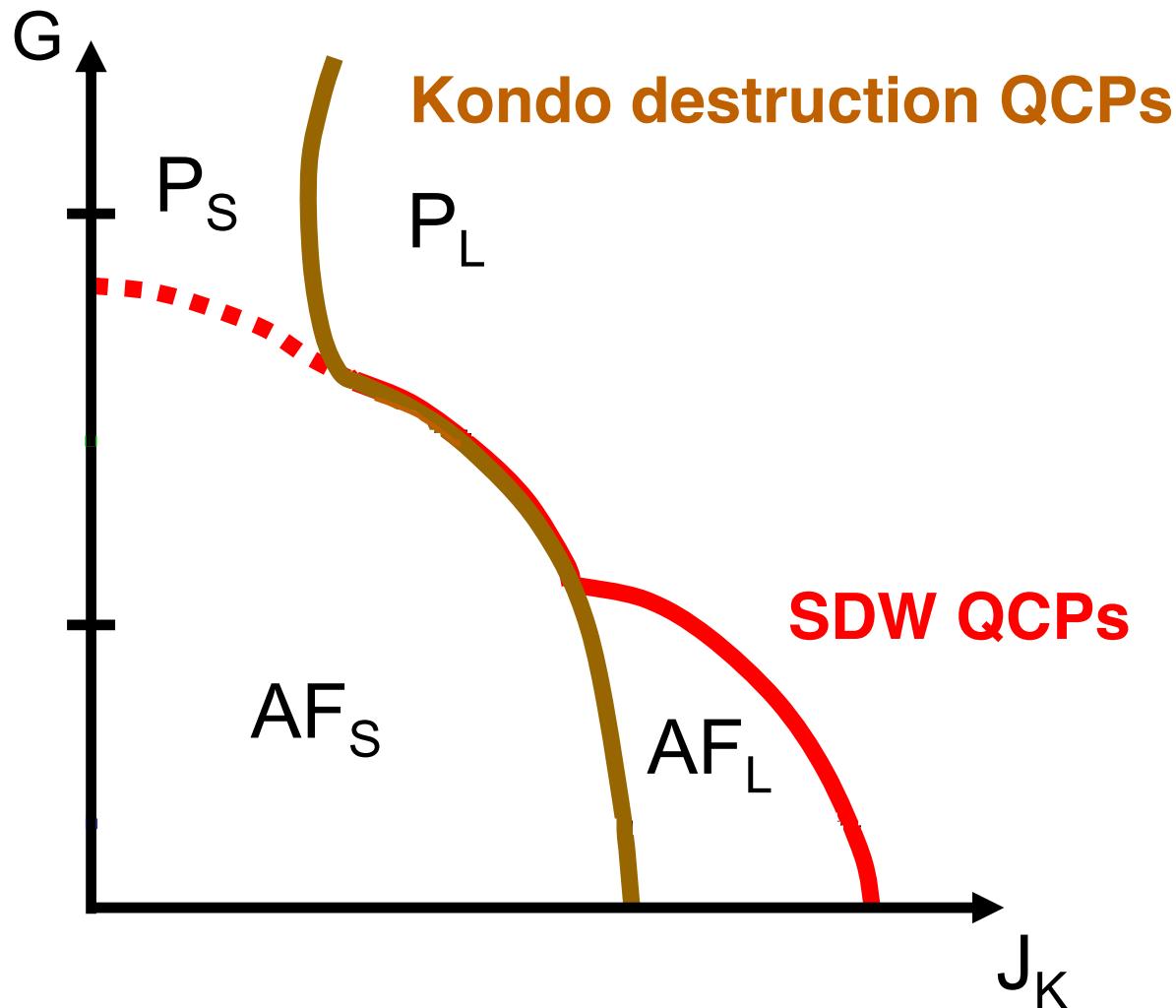
Width of crossover at  $B^*$



Width of transition at  $B_N$

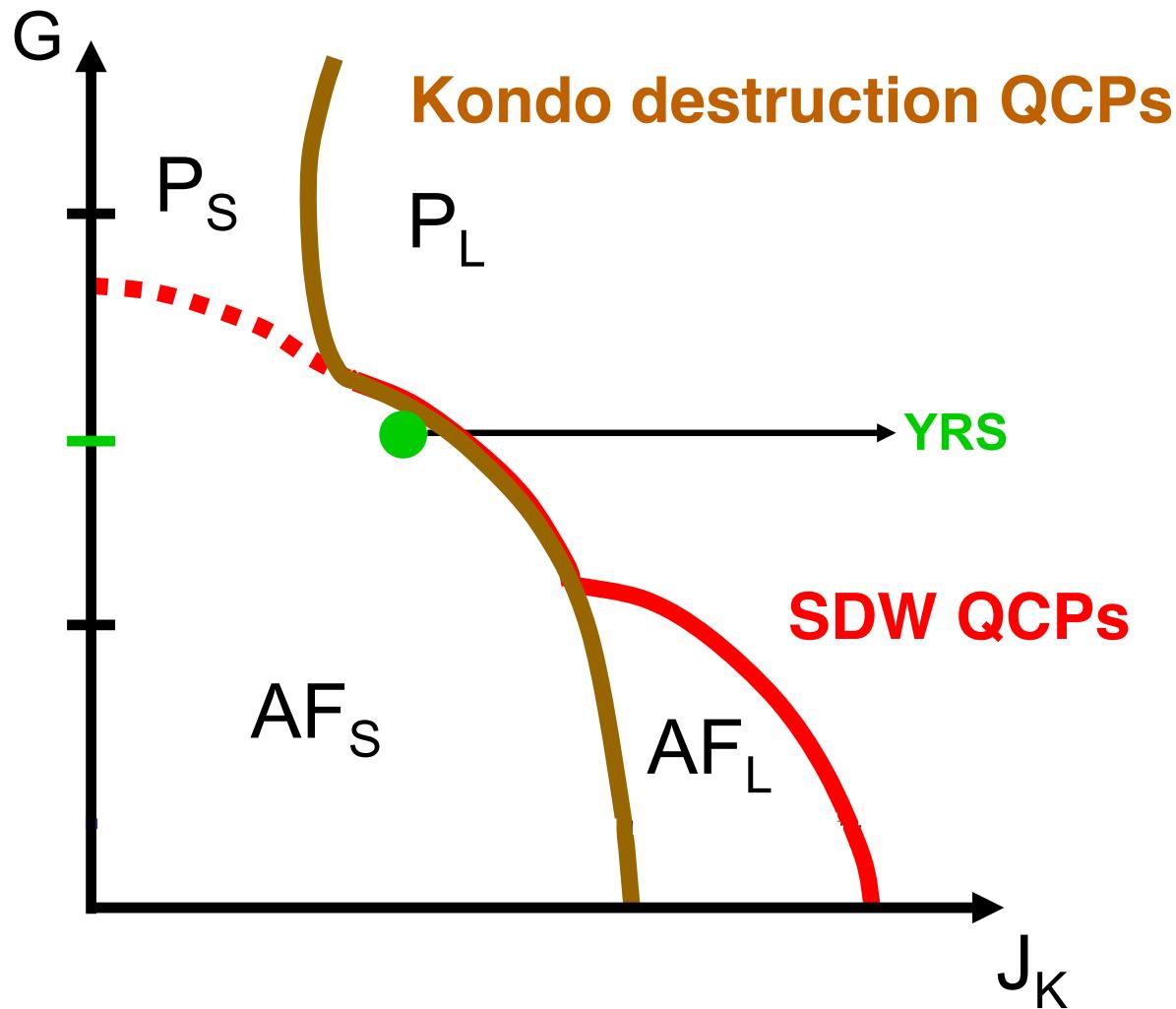


Suggested theoretical phase diagram at  $T = 0$



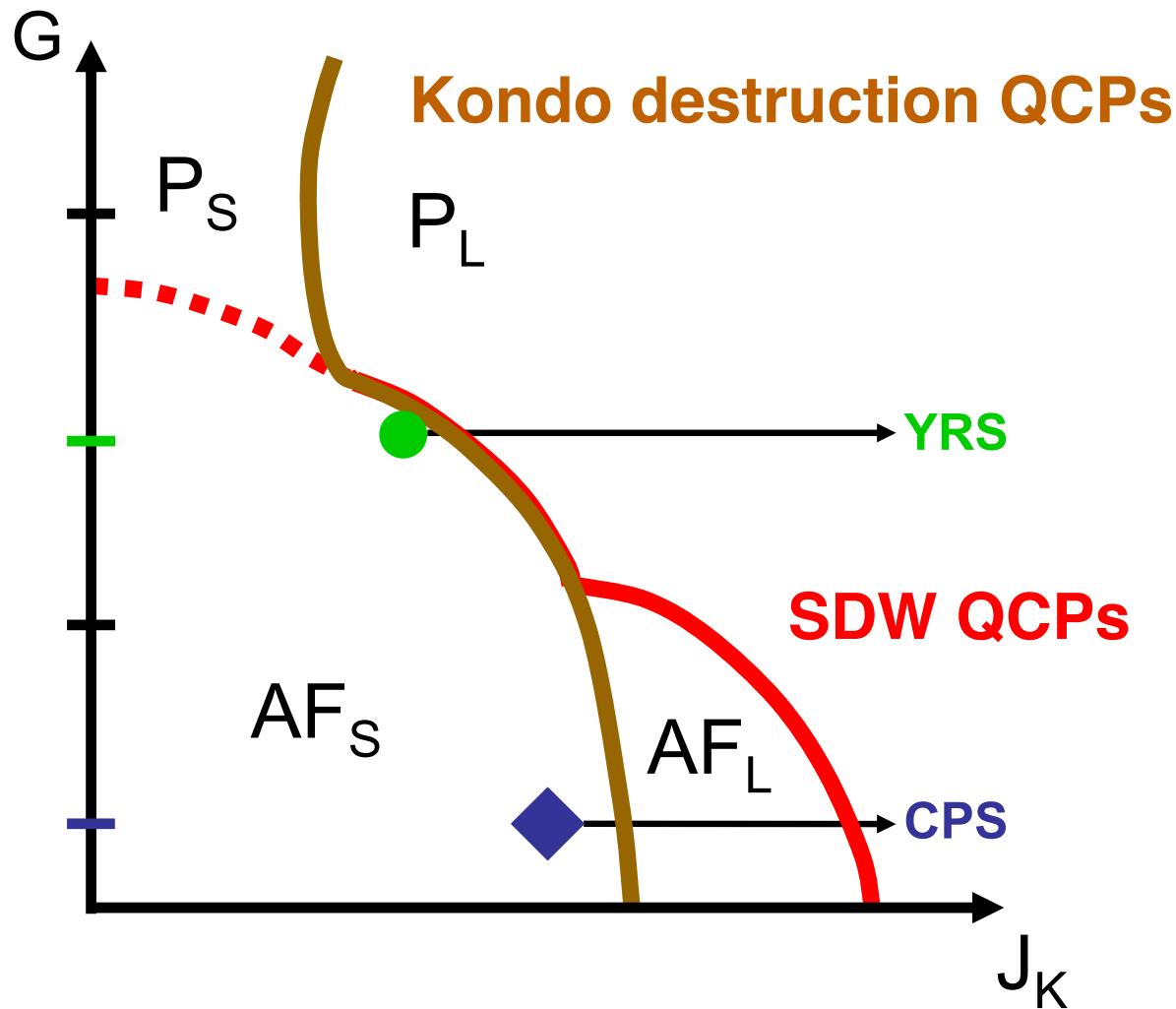
(Si, Physica B 378-380 (2006) 23; Phys. Stat. Sol. 247 (2010) 476; also: Coleman et al.)

Suggested theoretical phase diagram at  $T = 0$



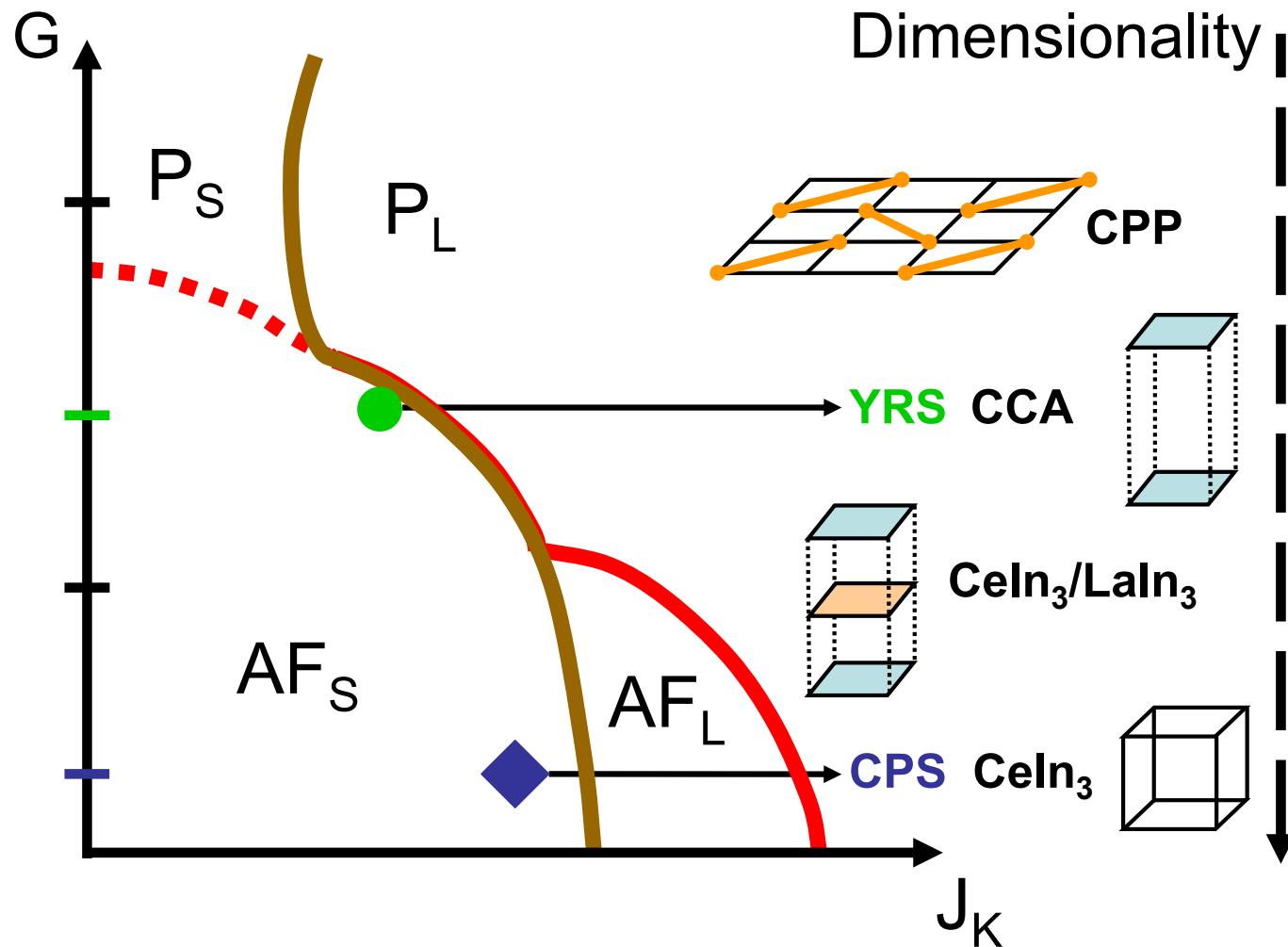
(Si, Physica B 378-380 (2006) 23; Phys. Stat. Sol. 247 (2010) 476)

Suggested theoretical phase diagram at  $T = 0$



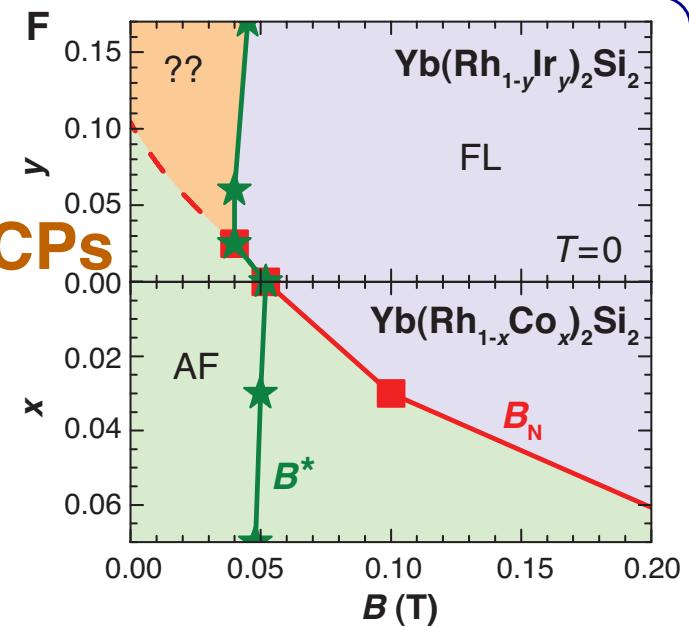
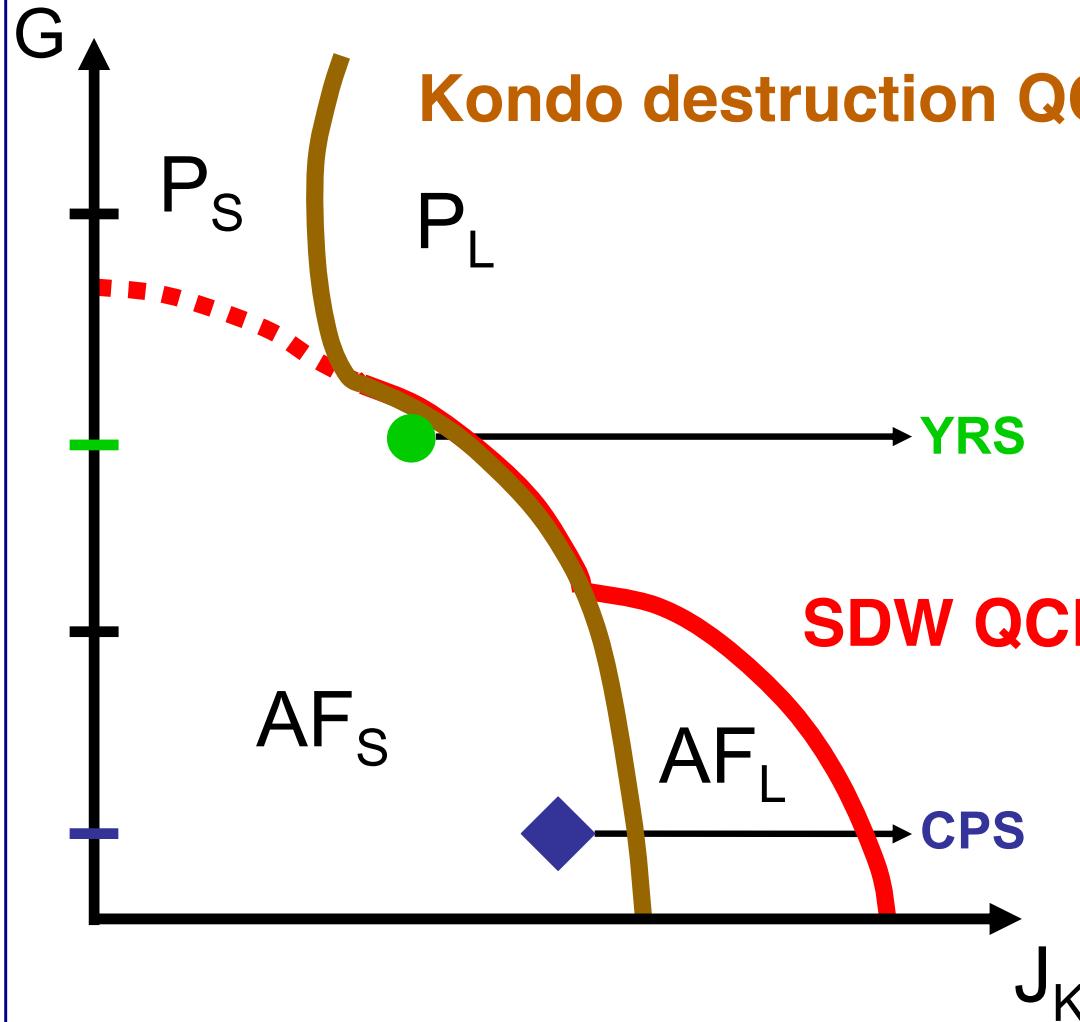
(Si, Physica B 378-380 (2006) 23; Phys. Status Solidi 247 (2010) 476)

## Materials-based global phase diagram



(Custers et al., Nature Mater. 11 (2012) 189)

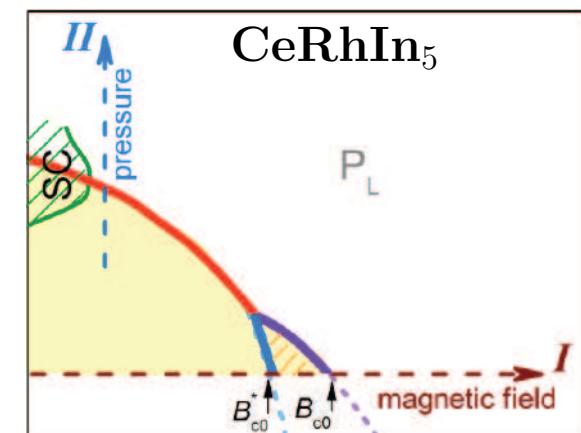
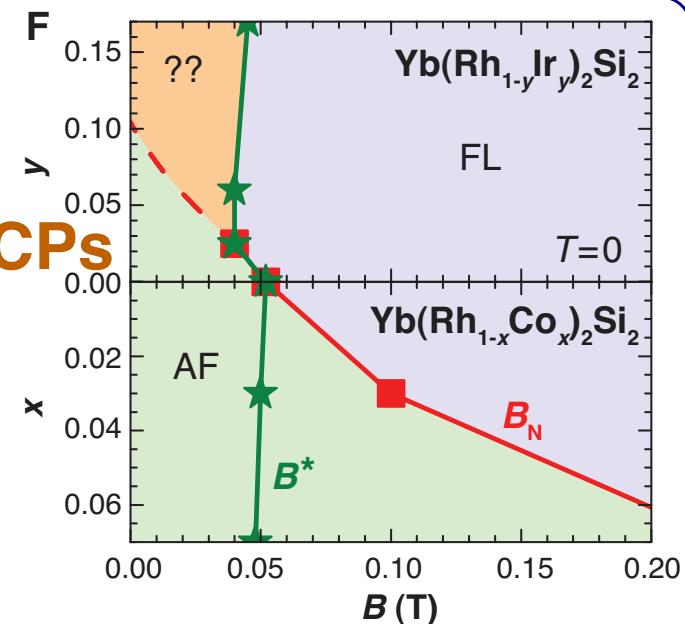
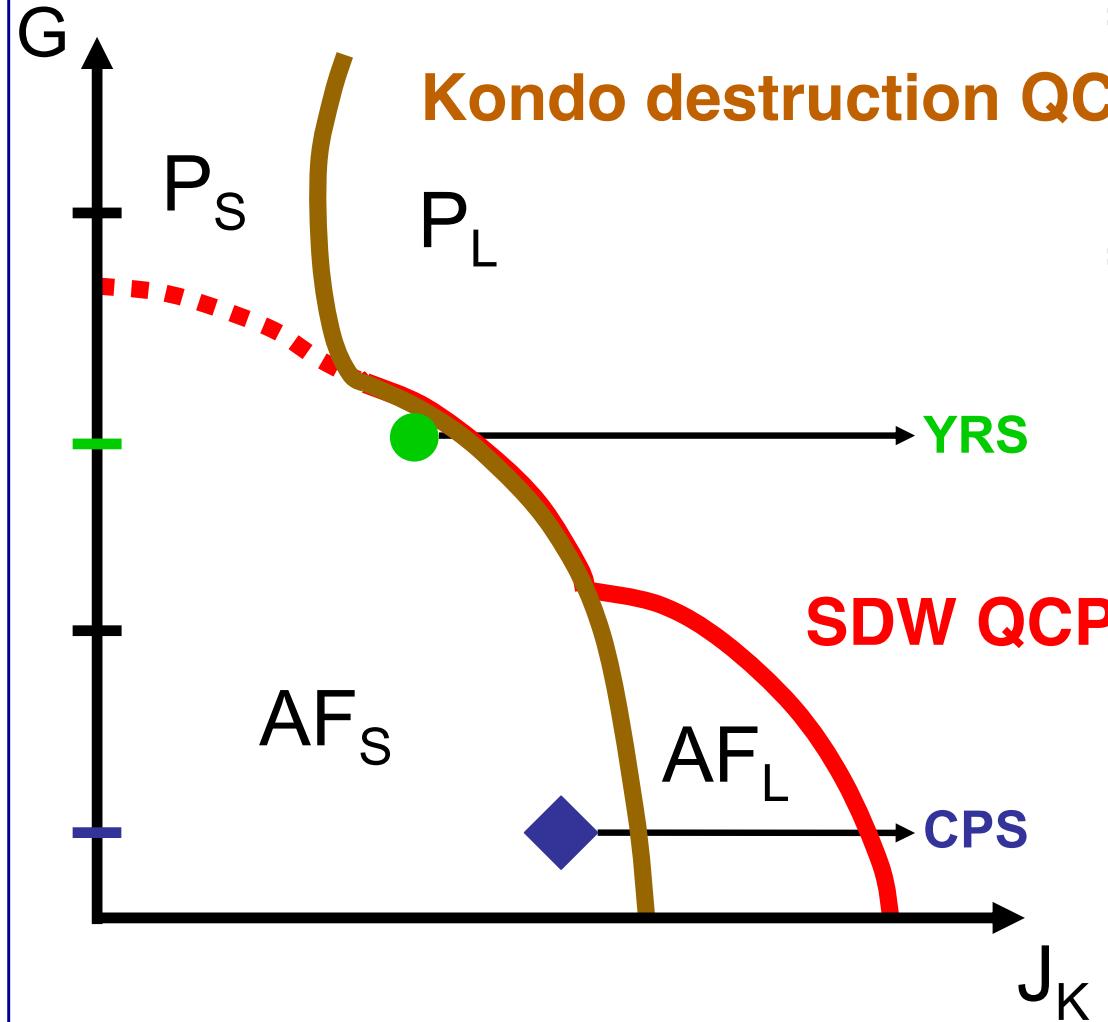
Materials-based global phase diagram



(Friedemann et al., Nat. Phys. 5 (2009) 465)

ICTP Trieste, August 13 - 17, 2012, 27

Materials-based global phase diagram



(Friedemann et al., Nat. Phys. 5 (2009) 465; Yuan et al., to appear 2012)

## Summary & Outlook

- Ce<sub>3</sub>Pd<sub>20</sub>Si<sub>6</sub>: New *cubic* quantum critical heavy fermion compound
- Crossover in magnetotransport with similar characteristics as in YbRh<sub>2</sub>Si<sub>2</sub>, at  $T \rightarrow 0$ :
  - Crossover position coincides with  $B_c$
  - Crossover width extrapolates to zero
- Important difference: QCP within other ordered phase!
  - Nature of this phase?
  - Nature of transition leaving this phase?
  - Can in Kondo breakdown scenario be related to higher dimensionality (lower  $G$ )
  - Other theoretical scenarios?
  - Extensions of theories to 3D?