

**2359-10**

**Joint ICTP-IAEA Workshop on Physics of Radiation Effect and its Simulation  
for Non-Metallic Condensed Matter**

*13 - 24 August 2012*

**Modeling of damage in ion irradiated semiconductors**

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Italy*



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**Dipartimento di Fisica, Università di Torino**

# **Modeling of damage in ion irradiated semiconductors**



Radiation damage is the general alteration of the operational properties of a semiconductor devices induced by ionizing radiation

Three main types of effects:

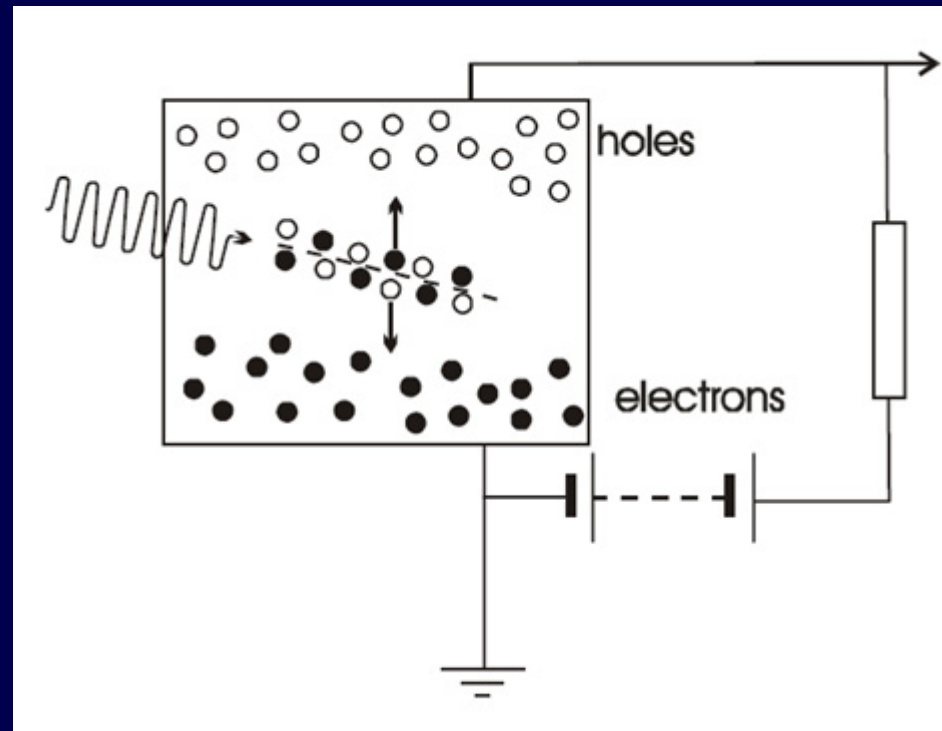
- **Transient ionization**. This effect produces electron-hole pairs; particle detection with semiconductors is based on this effect.
- **Long term ionization**. In insulators, the material does not return to its initial state, if the electrons and holes produced are fixed, and charged regions are induced.
- **Displacements**. These are dislocations of atoms from their normal sites in the lattice, producing less ordered structures, with long term effects on semiconductor properties.

V.A.J. van Lint, The physics of radiation damage in particle detectors, Nucl. Instrum. Meth. A253 (1987) 453.



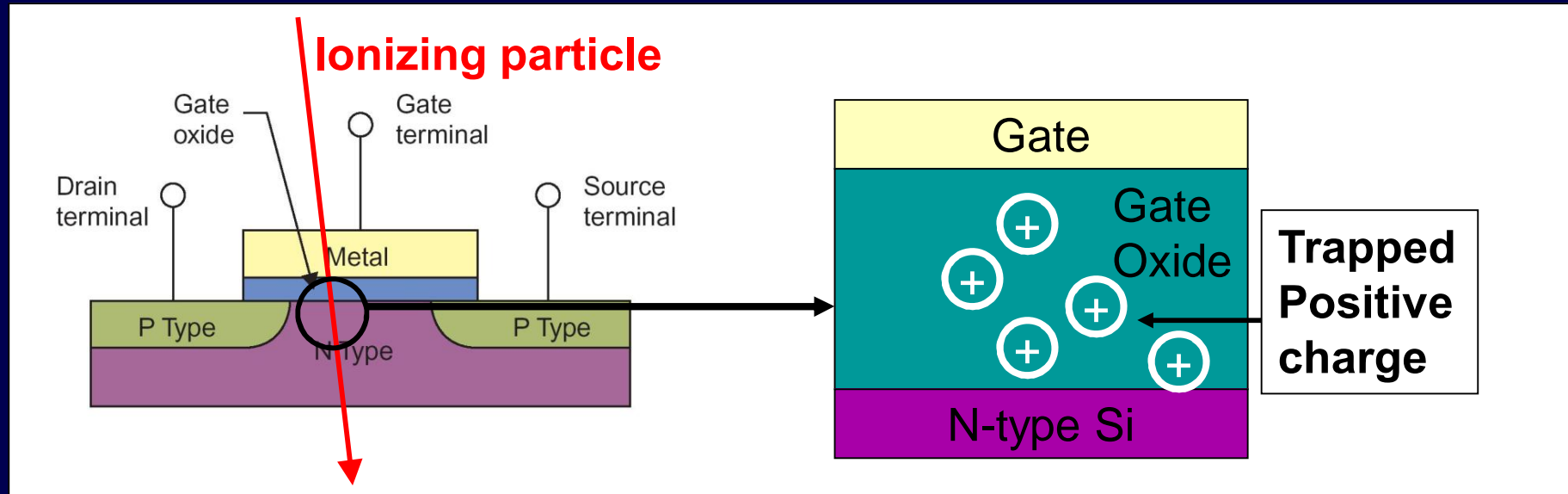
## Transient ionization.

This effect produces electron-hole pairs; particle detection with semiconductors is based on this effect. (IBIC)





**-Long term ionization.** In insulators, the material does not return to its initial state, if the electrons and holes produced are fixed, and charged regions are induced.



- **Parametric shifts** in transistors parameters due to the build-up of trapped positive charge and interface states caused by several low-LET particles striking a chip
- Total Ionizing Dose affects **dielectric layers** (e.g., gate oxide, isolation oxides)

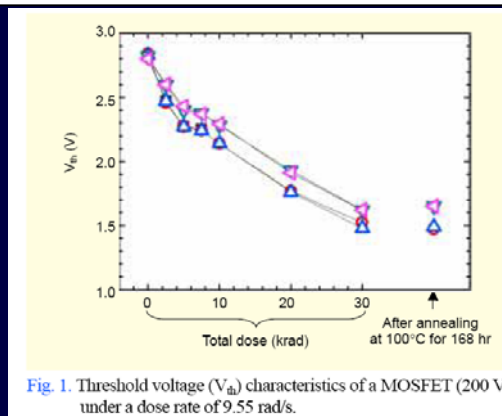


Fig. 1. Threshold voltage ( $V_{th}$ ) characteristics of a MOSFET (200 V) under a dose rate of 9.55 rad/s.

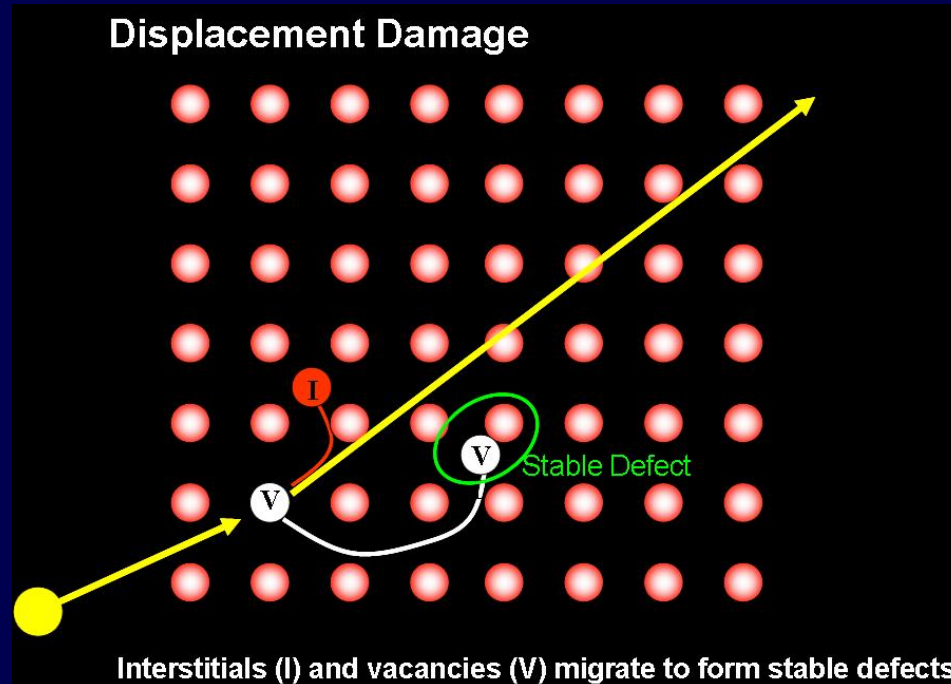
Young Hwan Lho, Ki Yup Kim  
*Radiation Effects on the Power MOSFET for space applications*

<http://etrij.etri.re.kr/Cyber/Download/PublishedPaper/2704/S27-04-14.pdf>

**G. Vizkelethy, "radiation effects in microelectronic devices", Thursday 9-10.30**



- **Displacements.** These are dislocations of atoms from their normal sites in the lattice, producing less ordered structures, with long term effects on semiconductor properties



PHYSICAL REVIEW

VOLUME 138, NUMBER 2A

19 APRIL 1965

# Defects in Irradiated Silicon: Electron Paramagnetic Resonance of the Divacancy

G. D. WATKINS AND J. W. CORBETT

<http://holbert.faculty.asu.edu/eee560/RadiationEffectsDamage.pdf>

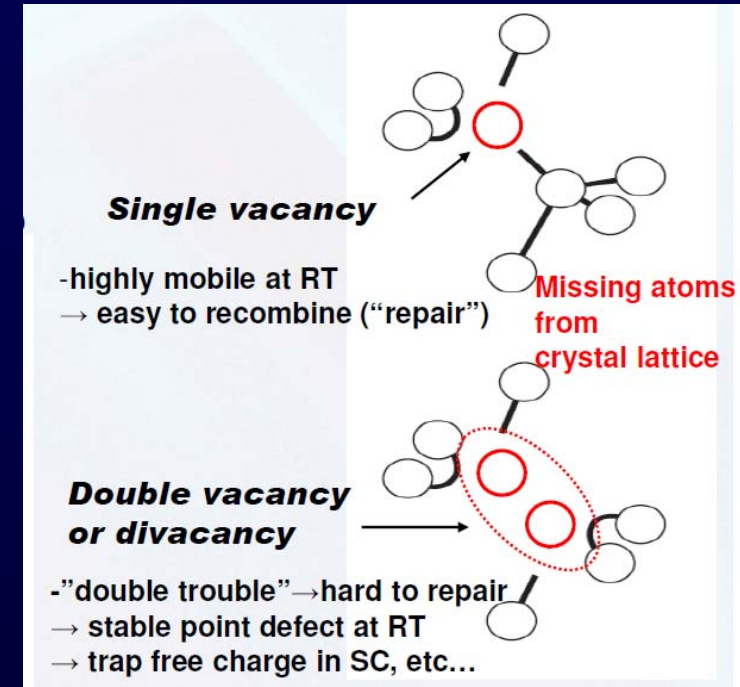
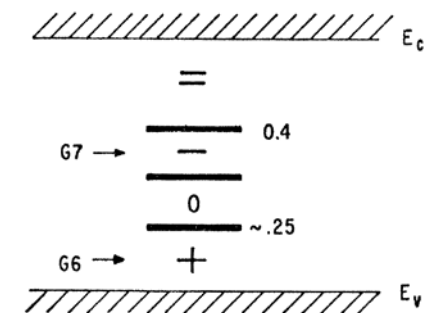
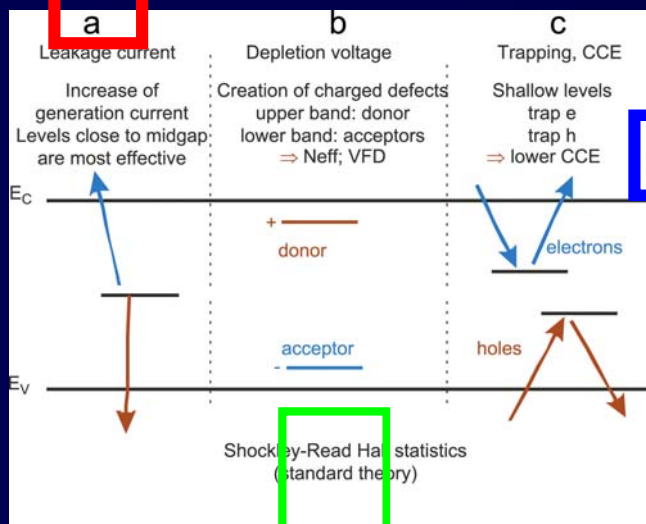
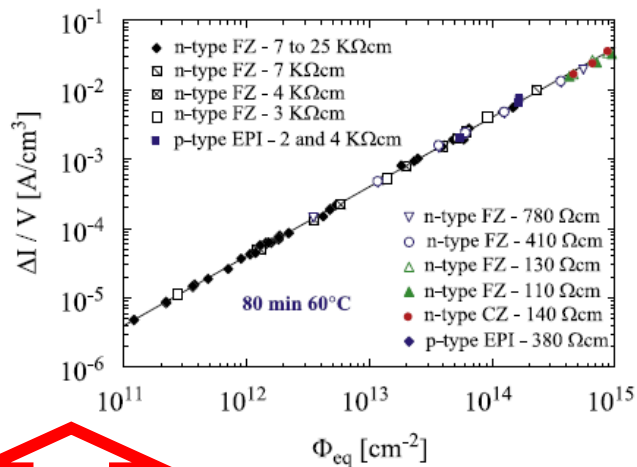


FIG. 14. Electrical levels associated with the divacancy. The level positions (in eV) are given to the nearest band edge. The charge states giving rise to the G6 and G7 spectra are indicated.

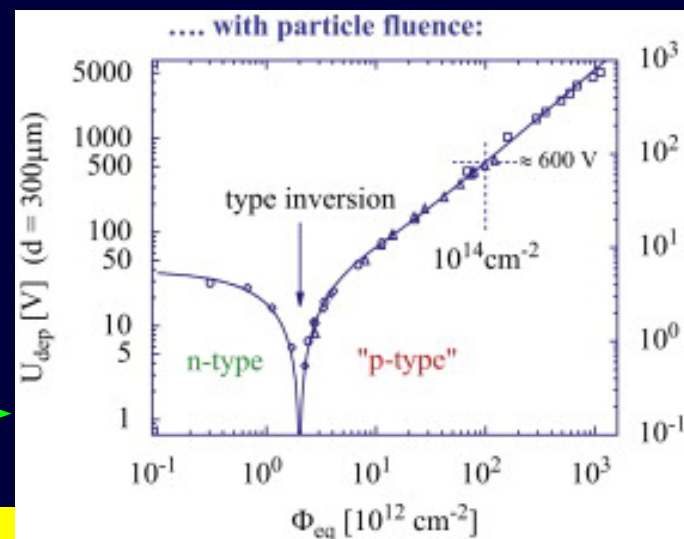
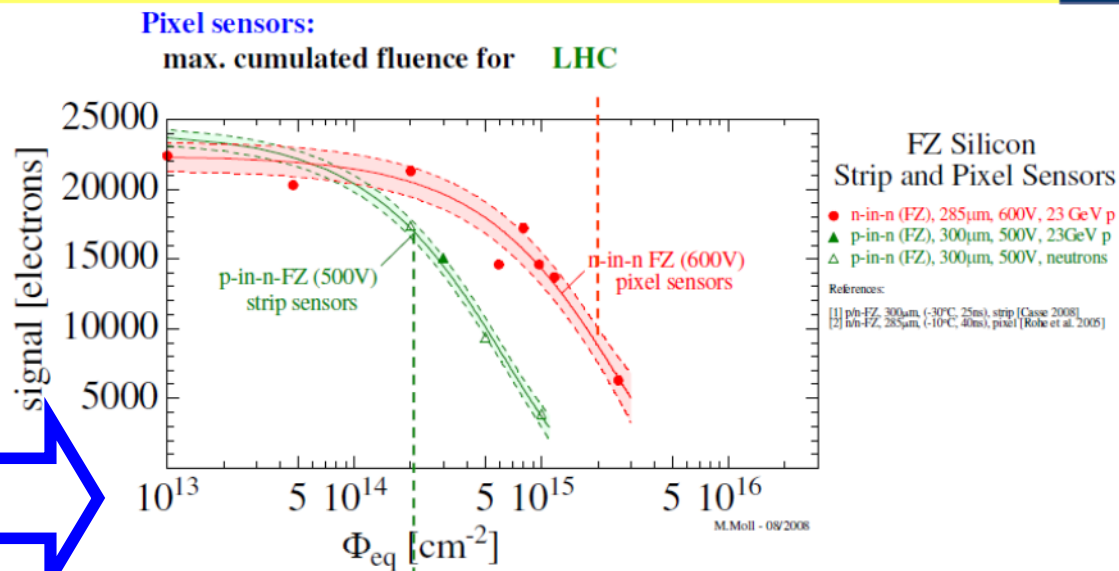




M. Bruzzi, M. Moll, RD50, 2010

<http://indico.cern.ch/getFile.py/access?contribId=9&sessionId=2&resId=1&materialId=slides&confId=81149>

## RD50 Signal degradation for LHC Silicon Sensors



Frank Hartmann, Silicon tracking detectors in high-energy physics  
Nuclear Instruments and Methods in Physics Research A 666 (2012) 25–46



# Shockley-Read-Hall Model

## Applet Recombination

### Excess carrier lifetime

$$\tau = \frac{1}{N_{\text{trap}} \cdot \sigma \cdot v_{\text{th}}}$$

Trap density

Capture cross  
section

Thermal velocity

Trieste  
15.08.2012

Joint ICTP-IAEA Workshop on Physics of Radiation Effect and its  
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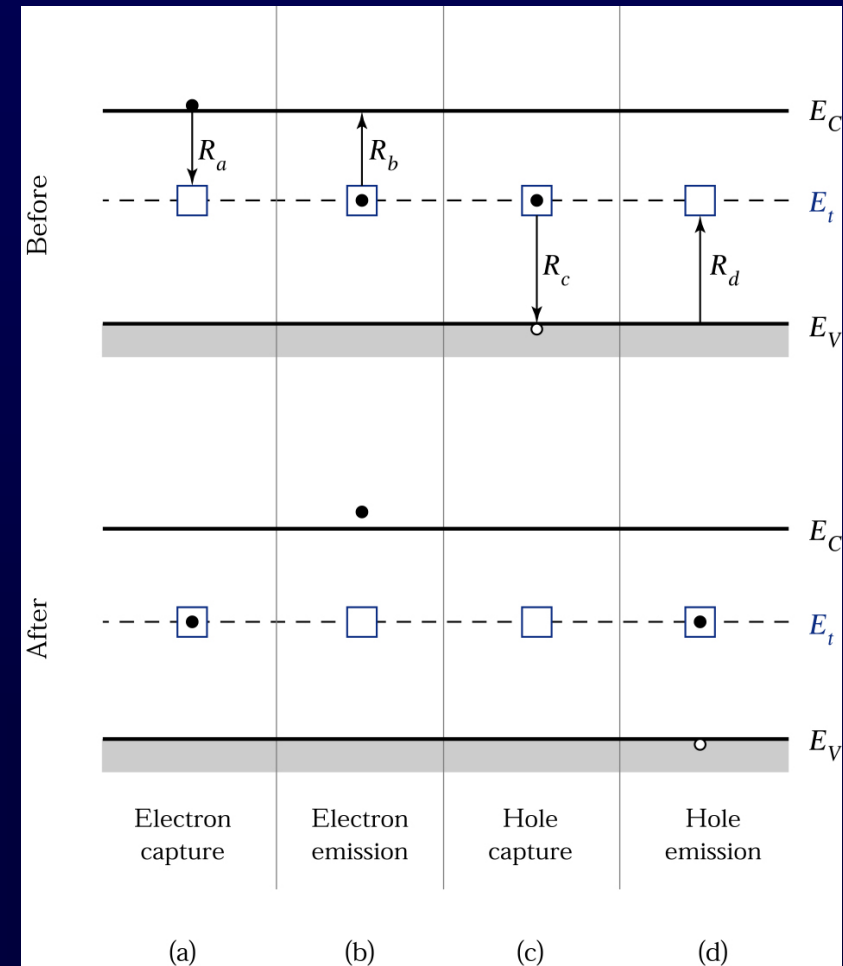


Figure 3.12.

Indirect generation-recombination processes





$$\tau = \frac{1}{N_{\text{trap}} \cdot \sigma \cdot v_{\text{th}}}$$

Trap density in  
pristine material

$$N_{\text{trap}} = N_{\text{trap}}^0 + k \cdot \Phi$$

Trap density induced  
by radiation

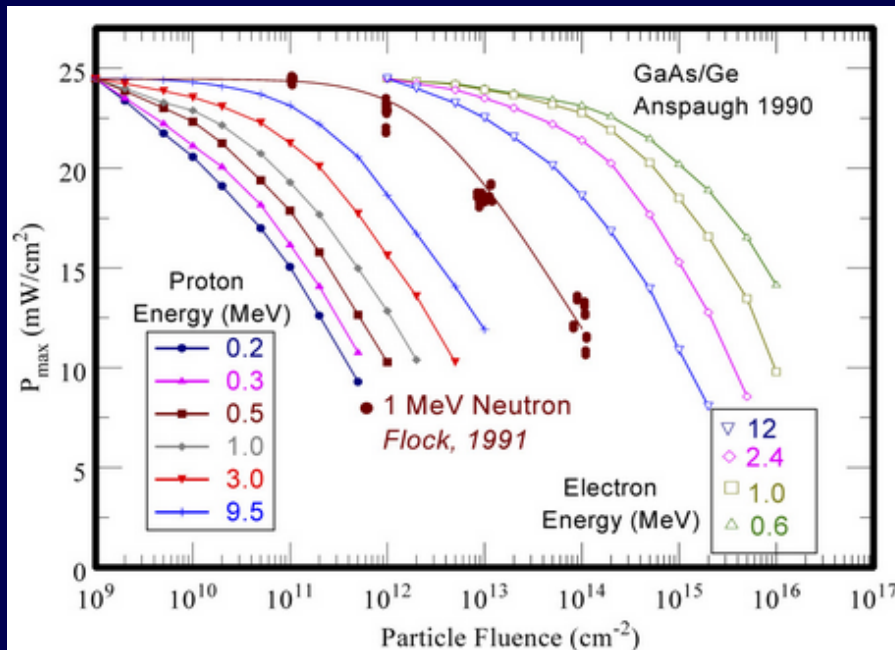
$$\frac{1}{\tau(\Phi)} = \frac{1}{\tau_0} + K \cdot \Phi$$

## Modeling radiation degradation in solar cells extends satellite lifetime

Robert J. Walters, Scott Messenger, Cory Cress, Maria Gonzalez and Serguei Maximenko

*A physics-based model of the effect of radiation on the performance of solar cells in space may enhance the on-orbit lifetime of Earth-orbiting spacecraft.*

3 January 2011, SPIE Newsroom. DOI: 10.1117/2.1201012.003417



**Figure 2.** Measured degradation of a single junction gallium arsenide (GaAs) solar cell under proton, electron,<sup>2</sup> and neutron irradiation.<sup>3</sup> These data can be used to empirically determine the energy dependence of the solar-cell degradation thereby enabling on-orbit performance prediction.  $P_{max}$ : Maximum power.

Space environment-> wide spectrum of ions (protons) and electrons.

To understand the performance of a solar cell in the space radiation environment, it is necessary to know how cell degradation depends on the energy of the irradiating particle.

<http://spie.org/x43655.xml>



## NIEL hypothesis:

the radiation damage is linear proportional to the non-ionizing energy loss of the penetrating particles (radiation) and this energy loss is again linear proportional to the energy used to dislocate lattice atoms (displacement energy).

Final concentration of defects depends only on NIEL and not on the type and initial energy of the particle.

Number of displacements (I-V pairs) is proportional to PKA energy (Kinchin-Pease:  $N = T/2TD$ ; T: PKA energy; TD: threshold energy to create a Frenkel pair).

Displacement damage dose:

$$D_d = \int \text{NIEL}(E) \cdot \frac{d\Phi}{dE} dE$$

UNITS:

NIEL:(Energy per unit length)/(material density):keV·cm<sup>2</sup>/g

(in high energy physics the displacement damage cross section (D) in MeV·mb is usually used)

D<sub>d</sub> : Energy per unit mass:keV/g

(G.P. Summers et al., IEEE Trans. Nucl. Sci., Vol. 40, pp. 1372, 1993)



# How to calculate NIEL from SRIM

10 MeV H<sup>+</sup> in  
Si 100 μm thick

1. Run SRIM and evaluate the total number of vacancy/ion W
2. Evaluate the energy required to create a vacancy M using the modified Kinchin-Pease relationship: the term 2 is due to the binding energy loss that SRIM assign to each vacancy  
Ed is the displacement energy
3. L is the device length and ρ is the mass density

**W=4.7 Vac/ion/μm**

**Ed=20 eV**

**M=52 eV/vac**

$$M = \left( \frac{E_d}{0.8} + 2 \right) \text{eV}$$

**ρ =2.3 g/cm<sup>3</sup>**

**L=100 μm**

$$\text{NIEL} = \frac{M \cdot \text{Vac}_{\text{Tot}}}{\rho \cdot R}$$

S. R. Messenger et al., *Using SRIM to Calculate the Relative Damage Coefficients for Solar Cells*, Prog. Photovolt: Res. Appl. 2005; 13:115–123



If  $Y$  is the physical observable (e.g. conductivity, maximum output power for solar cells, Charge Collection Efficiency (CCE) in radiation detectors), which characterizes a tested device subjected to radiation damage, its degradation can be modelled by the following phenomenological relationship:

Device characteristic after irradiation

$$\eta = \frac{Y}{Y_0} = 1 - K \cdot \Phi = 1 - K_{ed} \cdot D_d$$

Device characteristic  
before irradiation

Particle  
Fluence

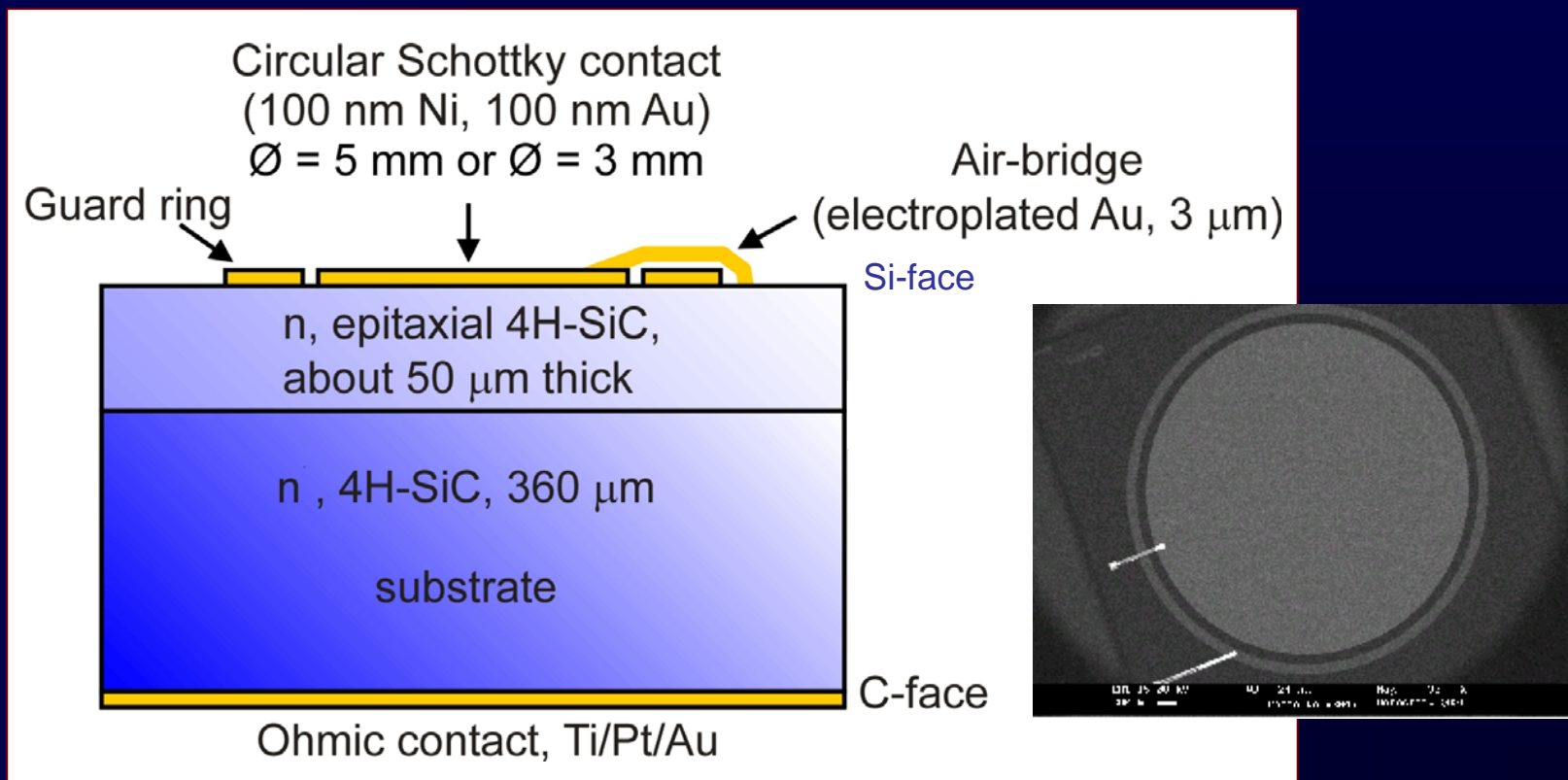
Equivalent  
damage  
factor

Displacement  
dose



# Samples

*Starting Material: 360  $\mu\text{m}$  n-type 4H-SiC by CREE (USA)*  
*Epitaxial layer from Institute of Crystal Growth (IKZ), Berlin, Germany*  
*Devices from Alenia Marconi System*





## **EXPERIMENTAL PROCEDURE:**

**Nuclear microprobe facility @ Ruđer Bošković Institute (Zagreb)**

**Irradiation of an area of  $5400 \mu\text{m}^2$  by 2 MeV and 1.5 MeV protons.**

**Final Fluence:**

**$1.2 \times 10^6$  protons/  $(68 \times 79) \mu\text{m}^2 \approx 2 \times 10^{10}$  protons/cm<sup>2</sup>**

**Applied bias voltage = 20 V, 40 V, 60 V, ... 120 V**

**Event by event data acquisition mode.**



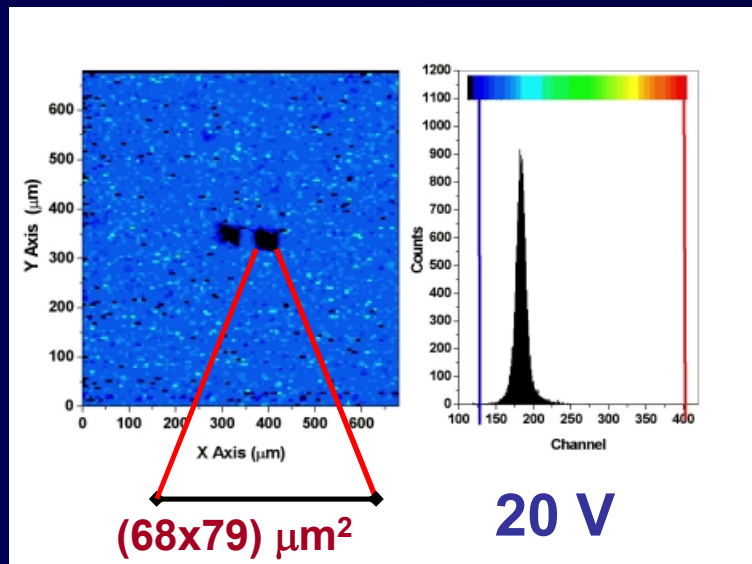


## OFF LINE ANALYSIS

For each scan (about  $10^8$  ions/cm<sup>2</sup>), pulse height spectra are recorded

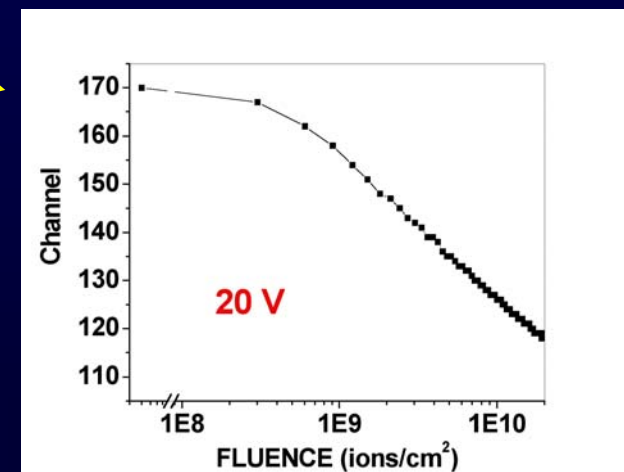
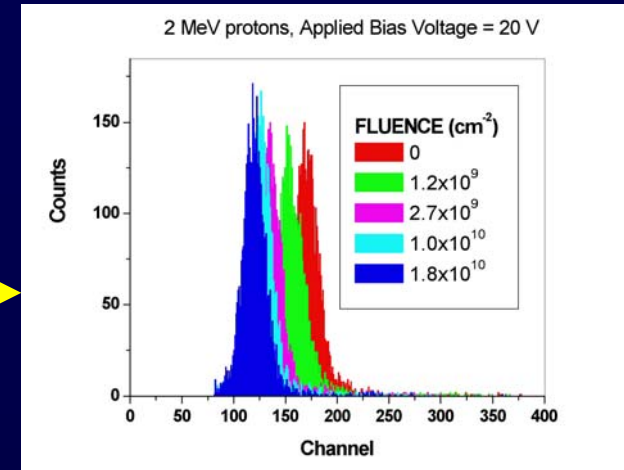
The median pulse height is evaluated as a function of ion fluence

## CONTROL



(650x650)  $\mu\text{m}^2$

IBIC map



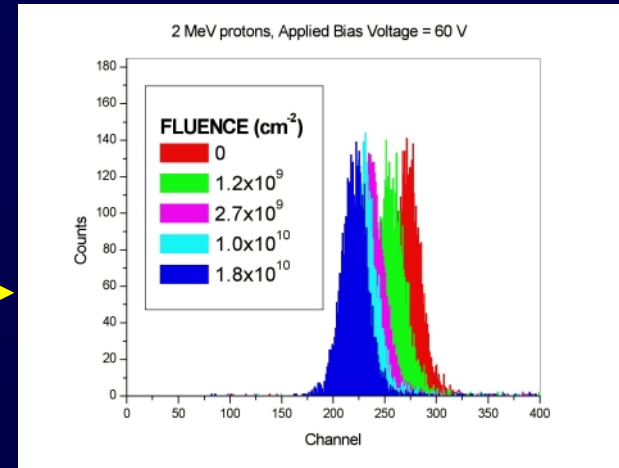




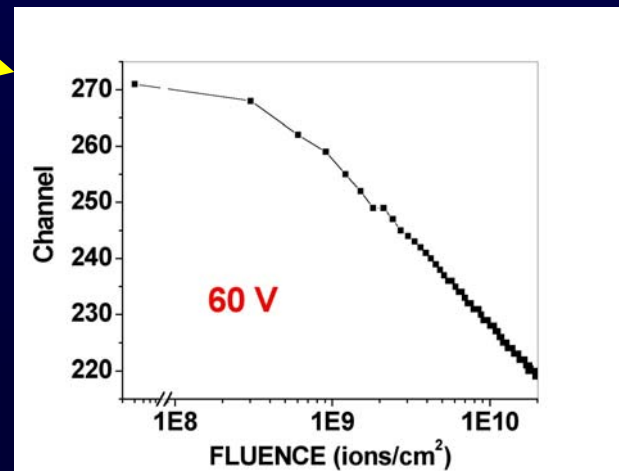
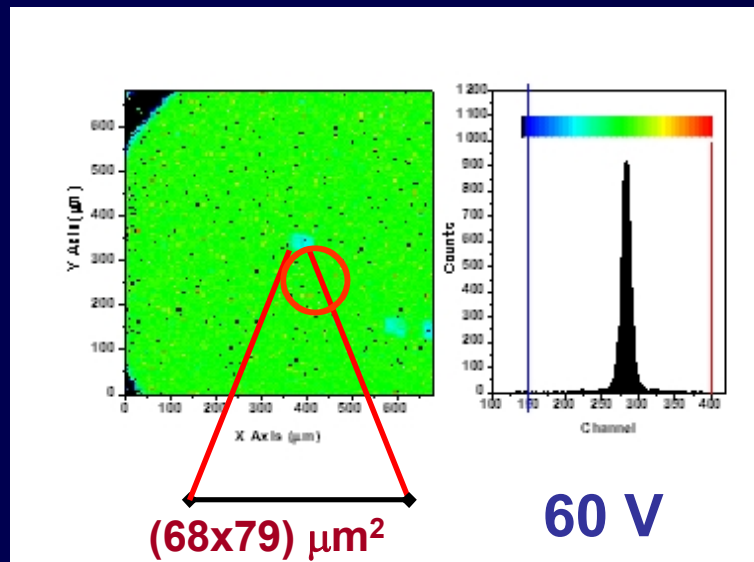
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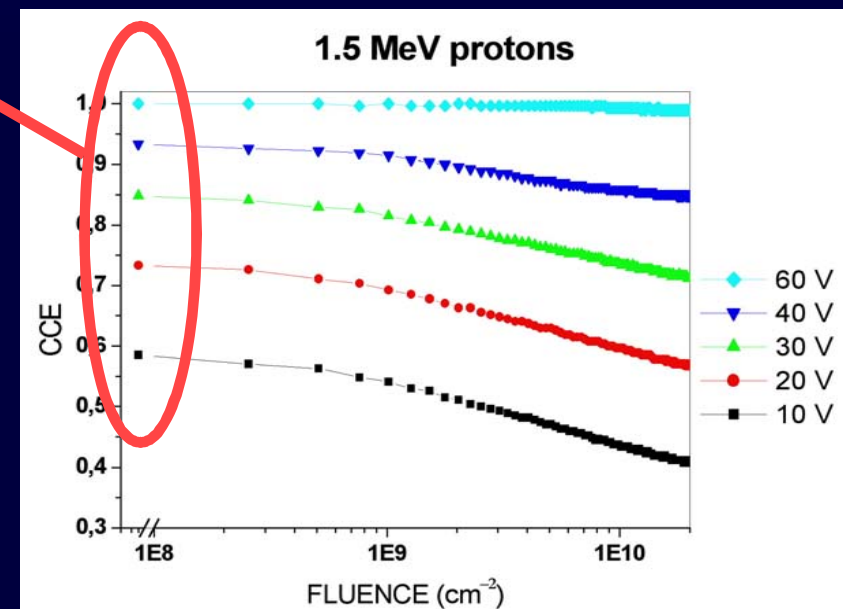
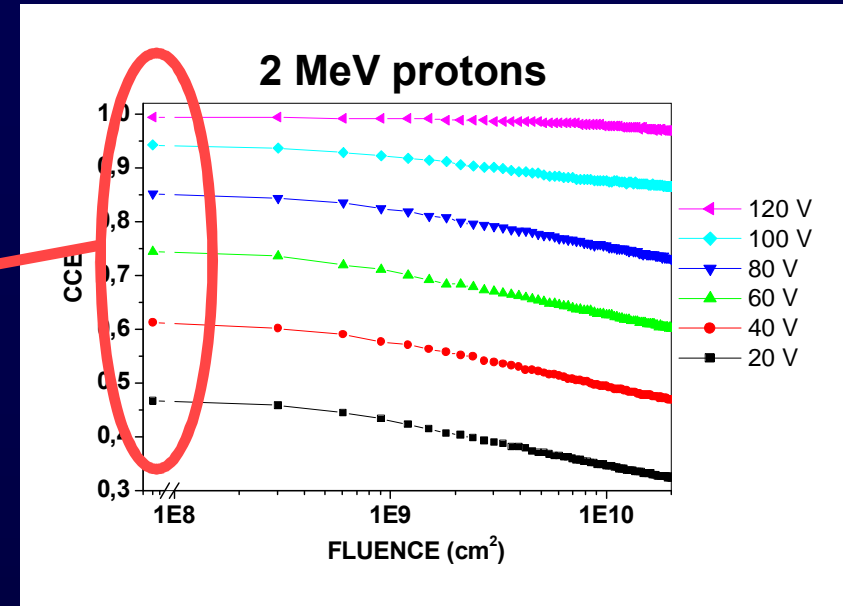
## CONTROL





**PRISTINE  
CONDITIONS**

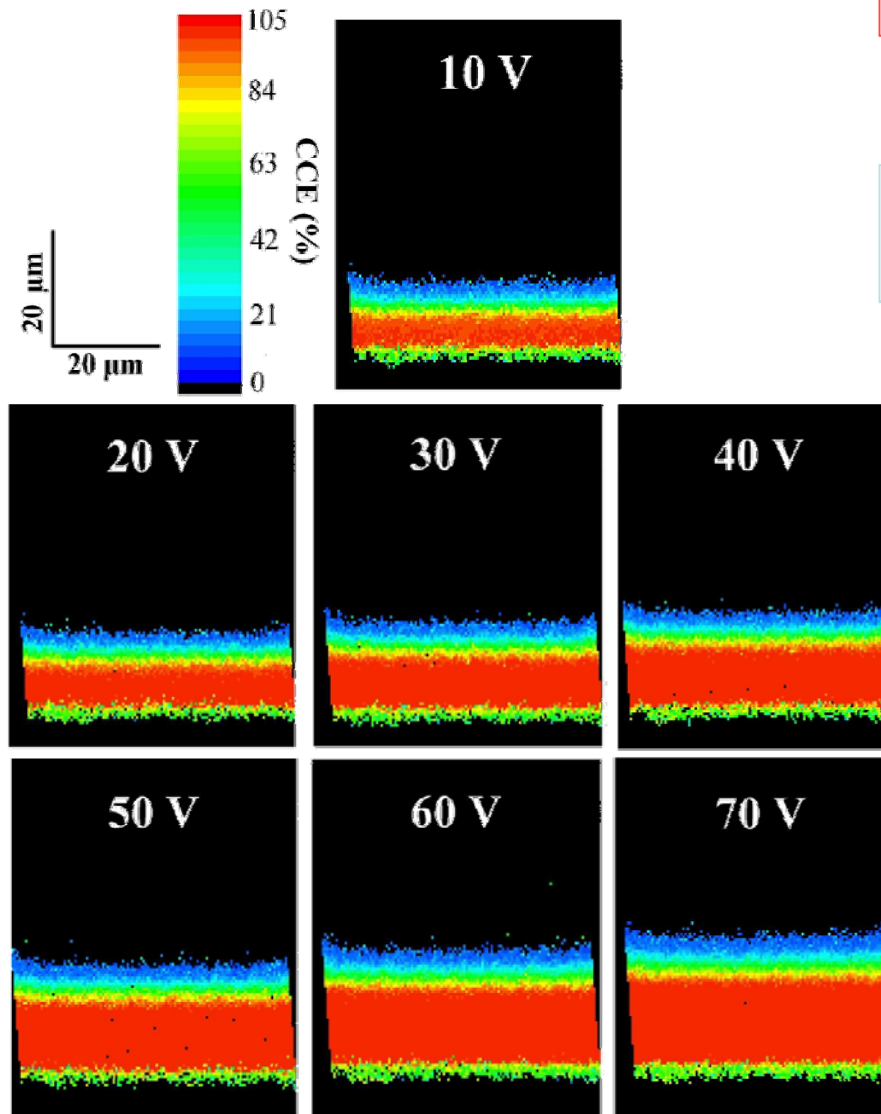
# Charge collection efficiency Vs. Ion Fluence



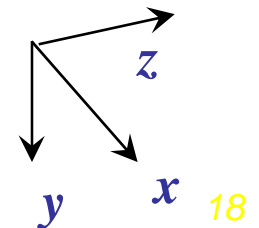
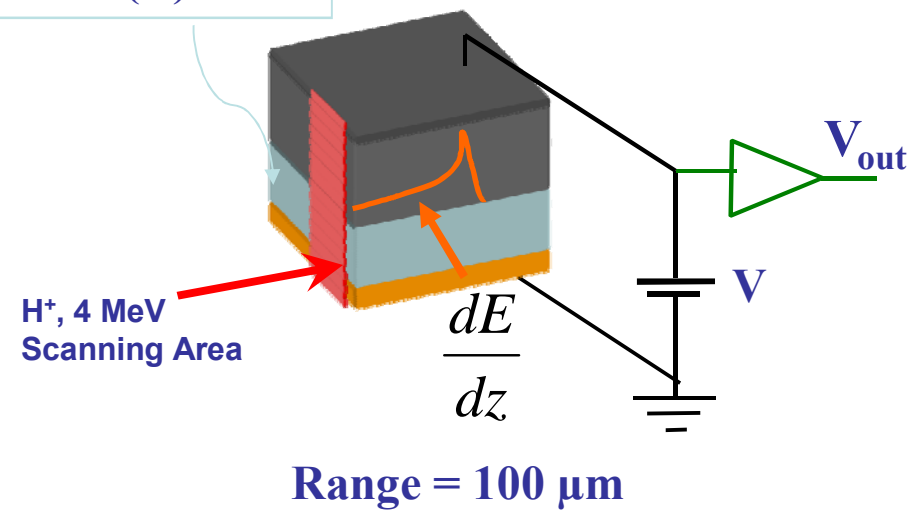


# Lateral IBIC

Protons, 4MeV on SiC



Depletion Region  
 $w$  (V)

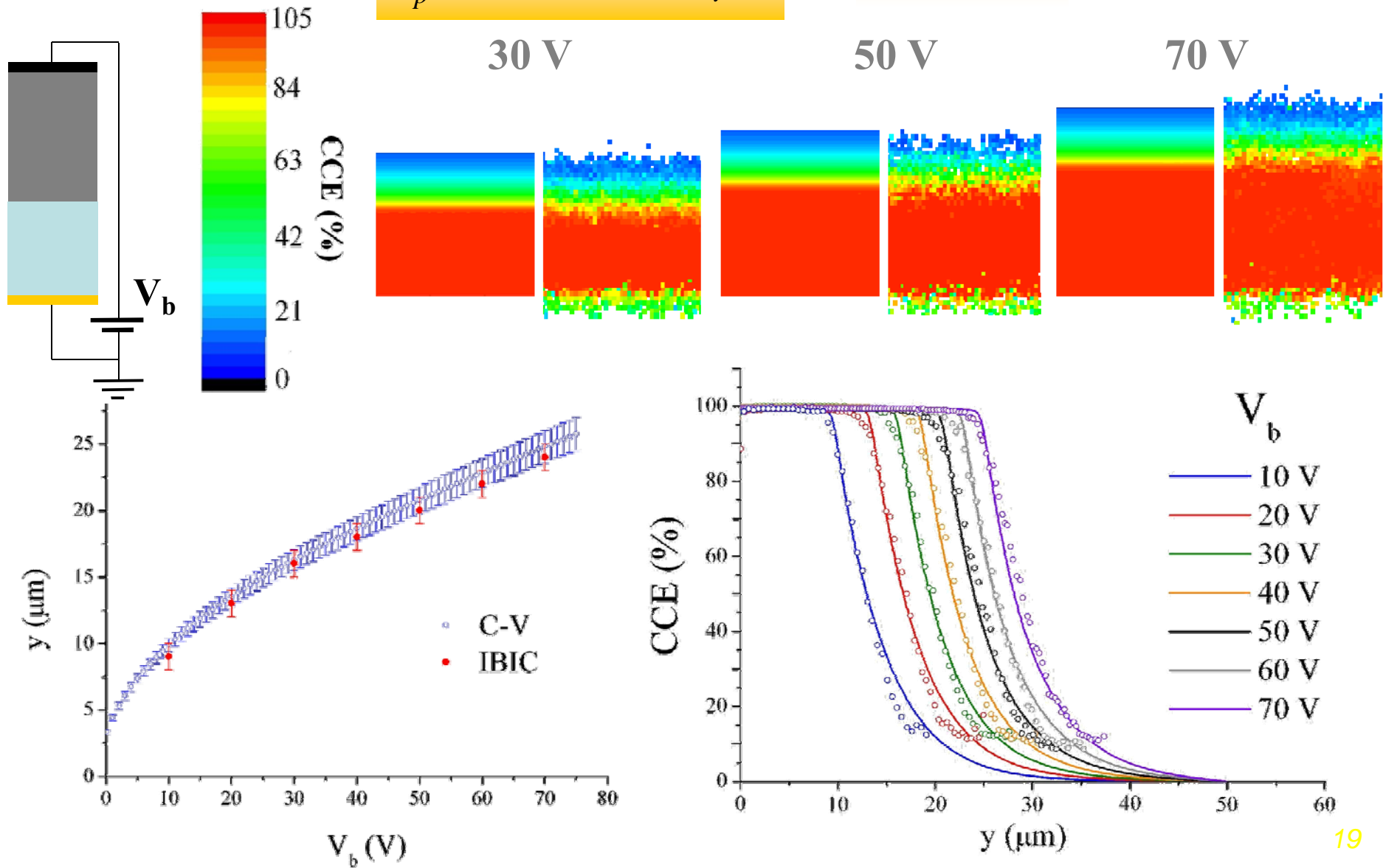




# Numerical Simulations

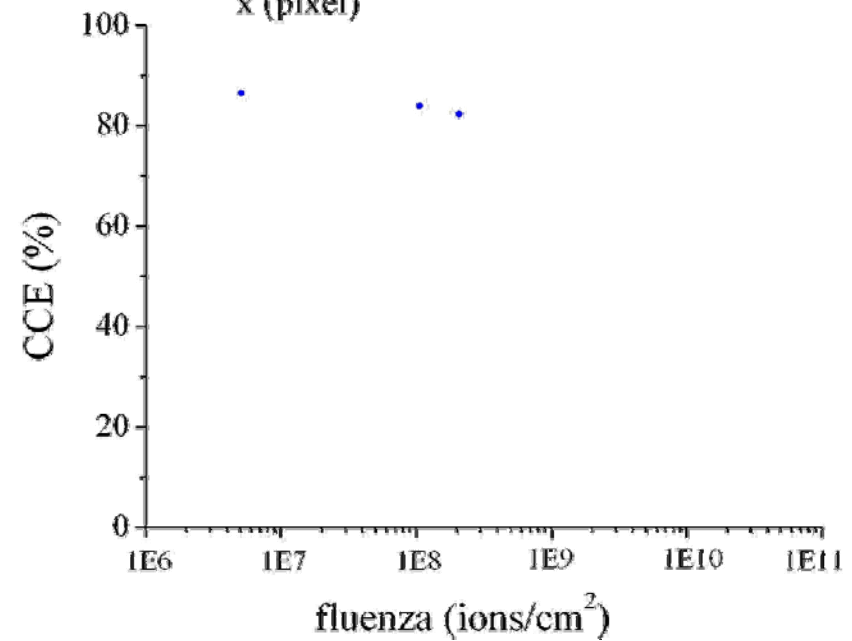
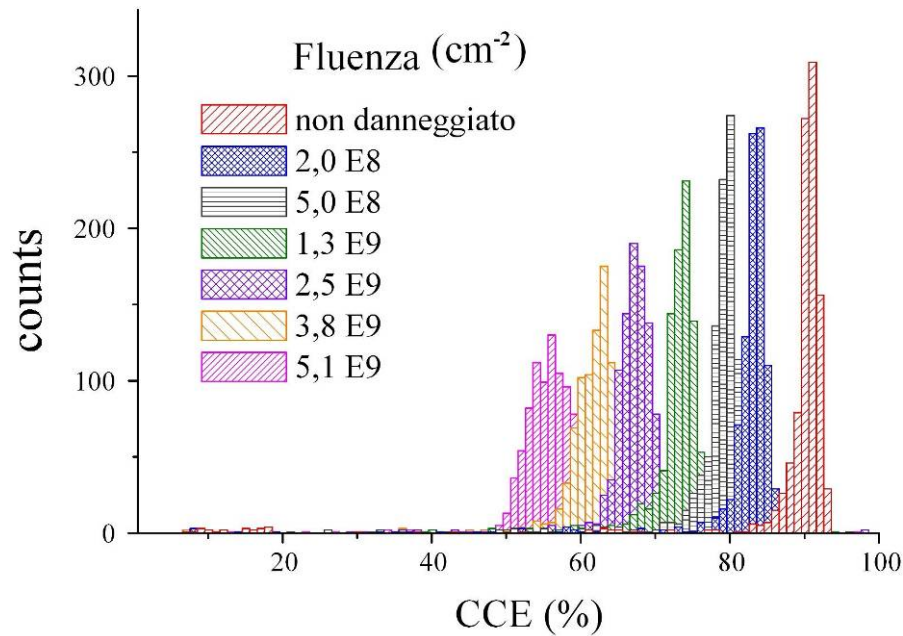
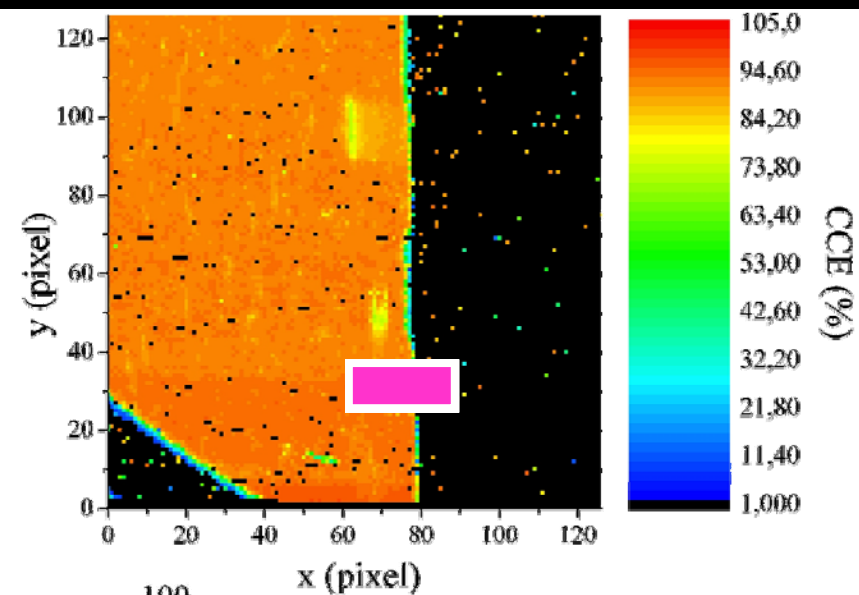
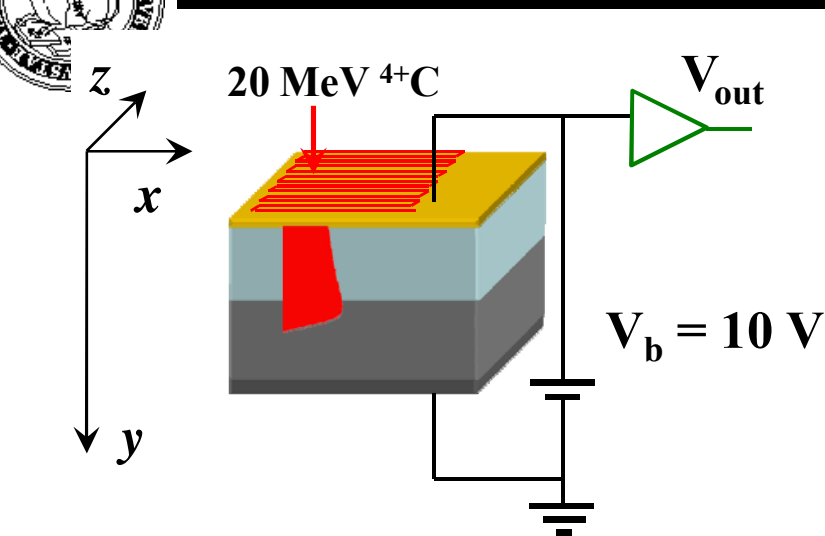
$$L_p = (4,9 \pm 0,3) \mu m$$

$$\tau_p \approx 80 ns$$





# Radiation Damage; Frontal IBIC

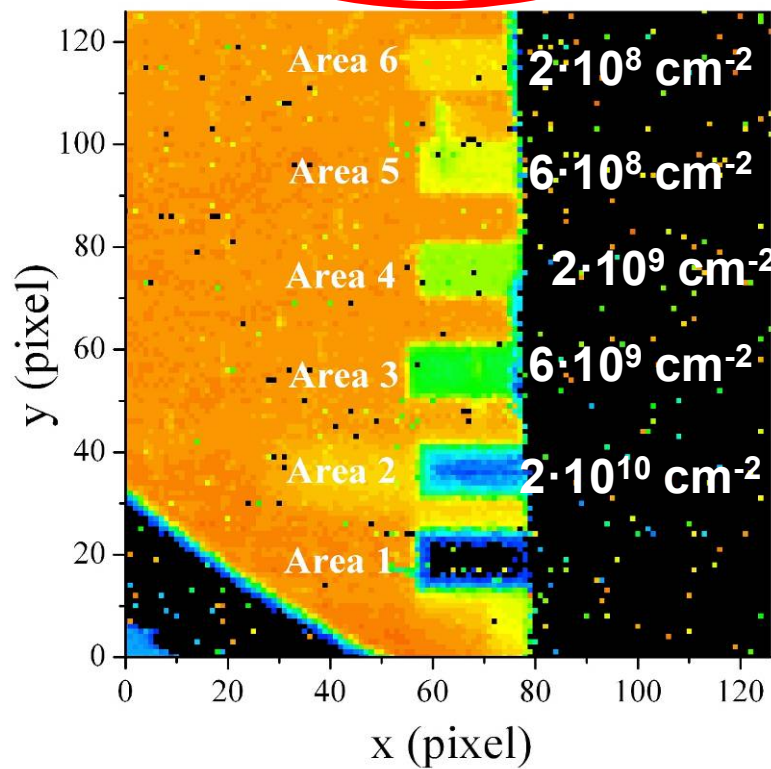




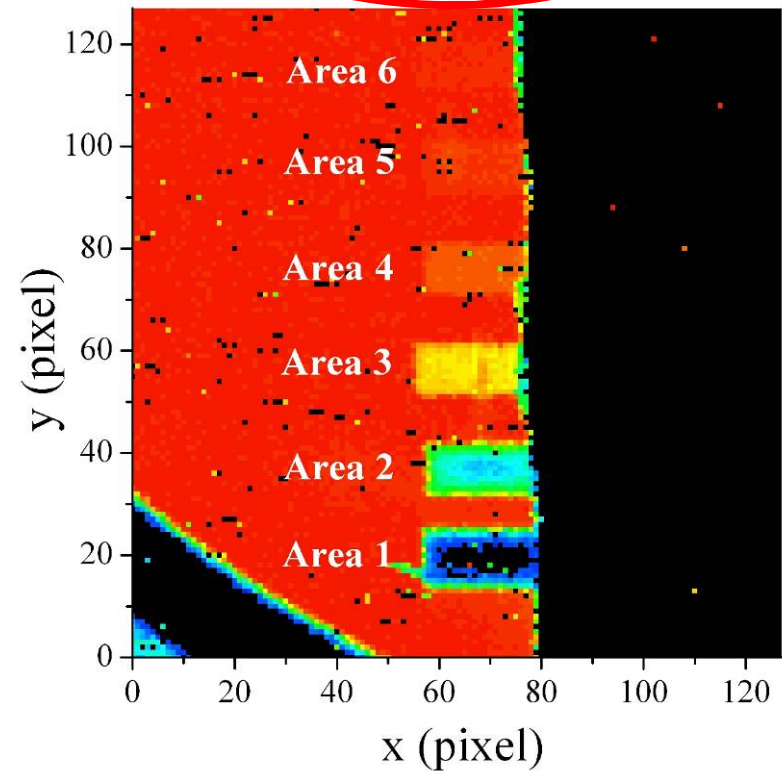


# Frontal IBIC

C, 20 MeV  
 $V_b = 10$  V



C, 20 MeV  
 $V_b = 50$  V

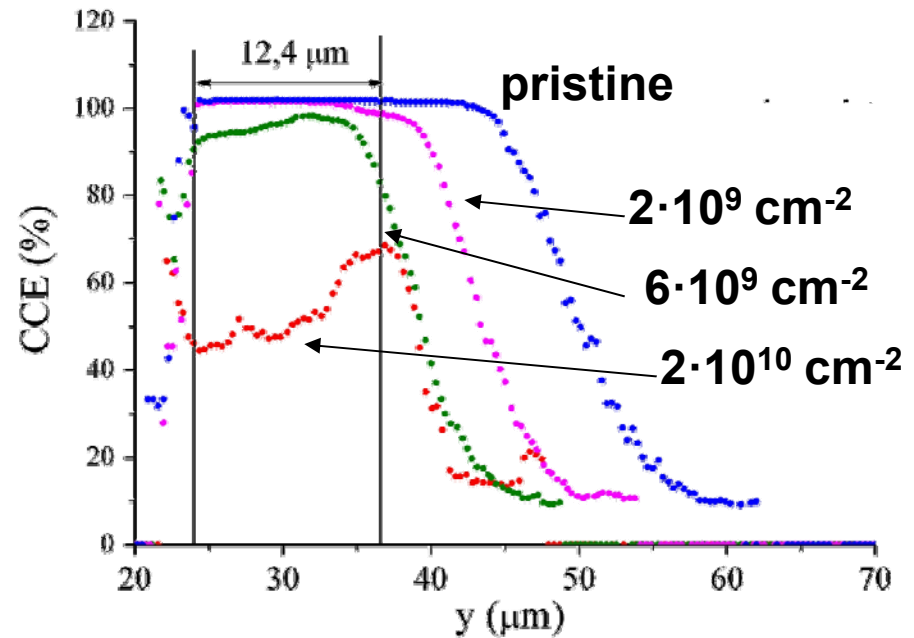
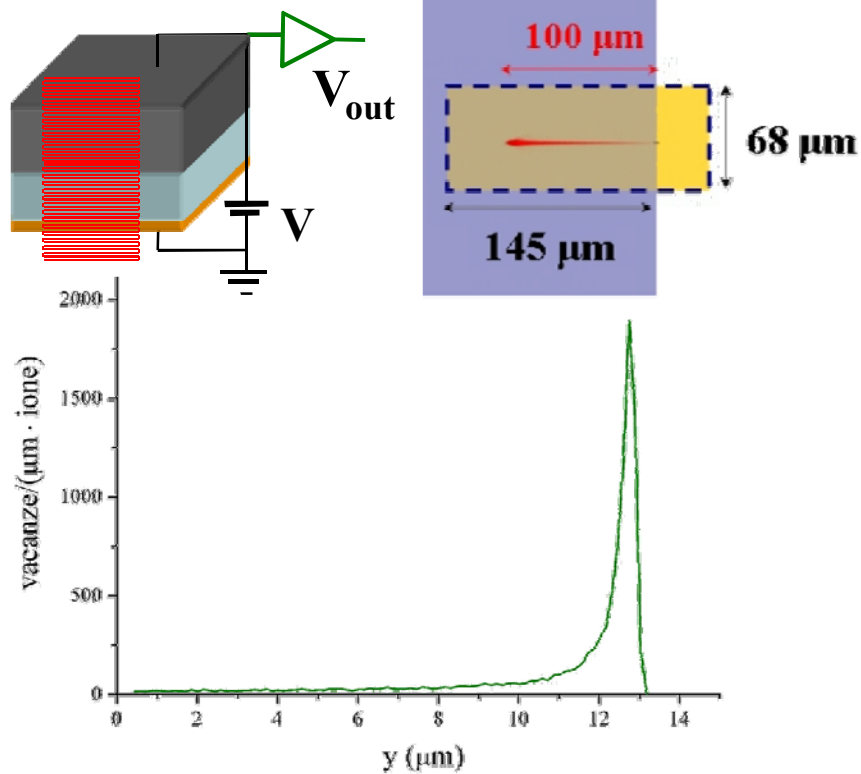
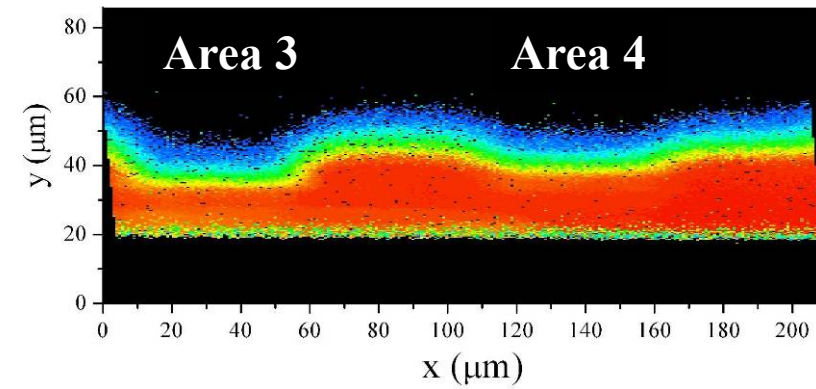
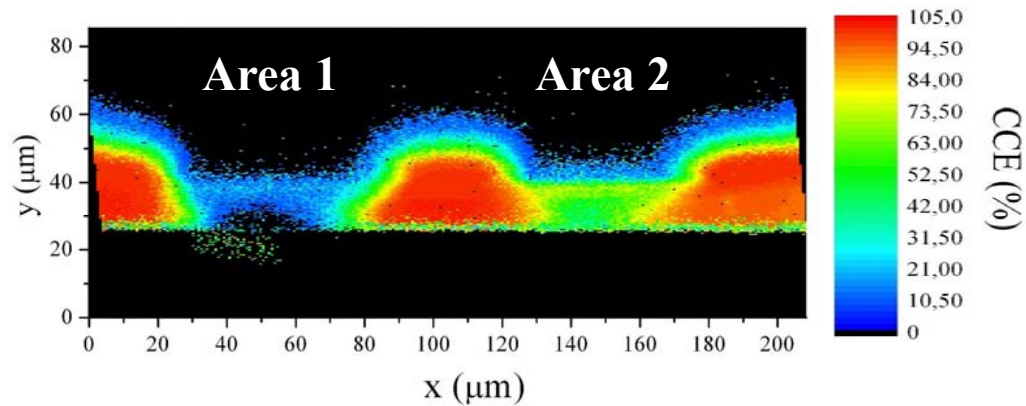


The CCE depends on the ion fluence and on the applied bias voltage



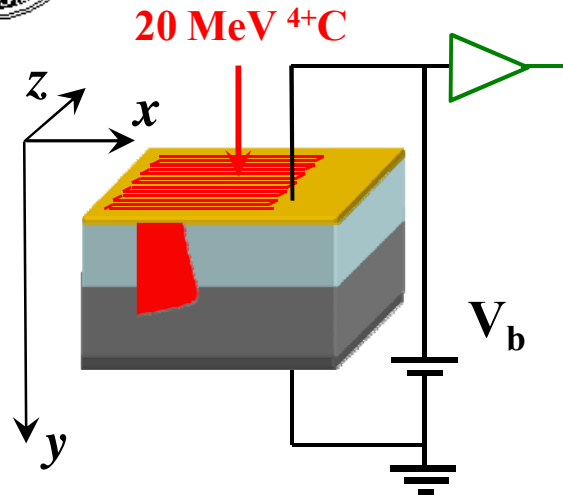
# Lateral IBIC

$$V_b = 50 \text{ V}$$

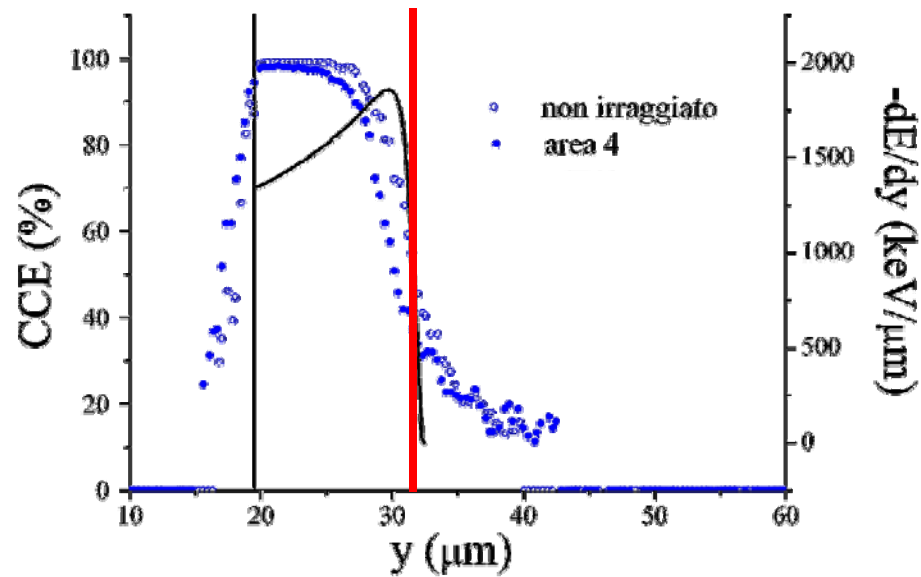




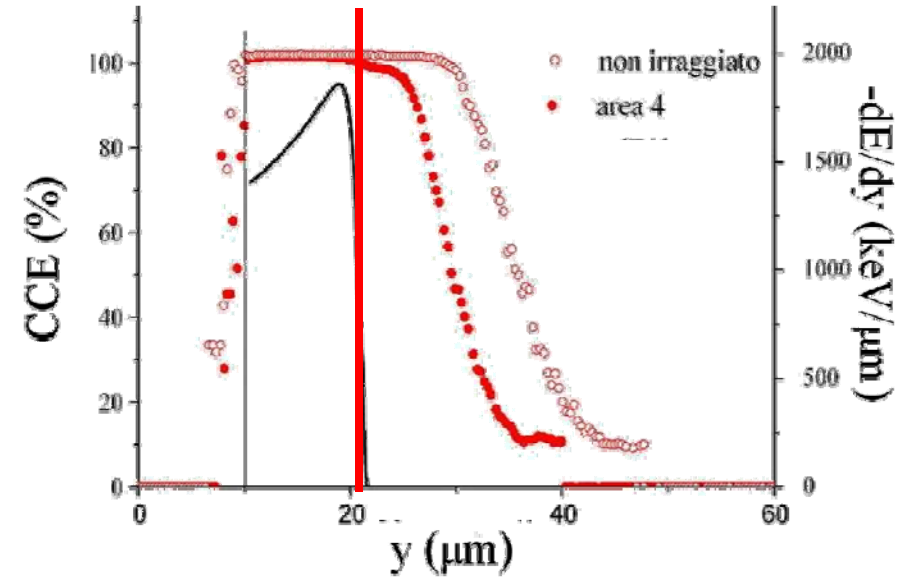
# Frontal IBIC



Area 4  
( $\Phi = 2 \cdot 10^9 \text{ cm}^{-2}$ )



10 V



50 V

# Lateral IBIC





- The performance degradation depends on
- Ion mass and energy
  - Polarization state
  - Free carrier generation profile (ion probe)

## Shockley-Read-Hall Model

$$\frac{1}{\tau(\Phi)} = \frac{1}{\tau_0} + K \cdot \Phi$$

**Definition of  
"radiation  
hardness"?**

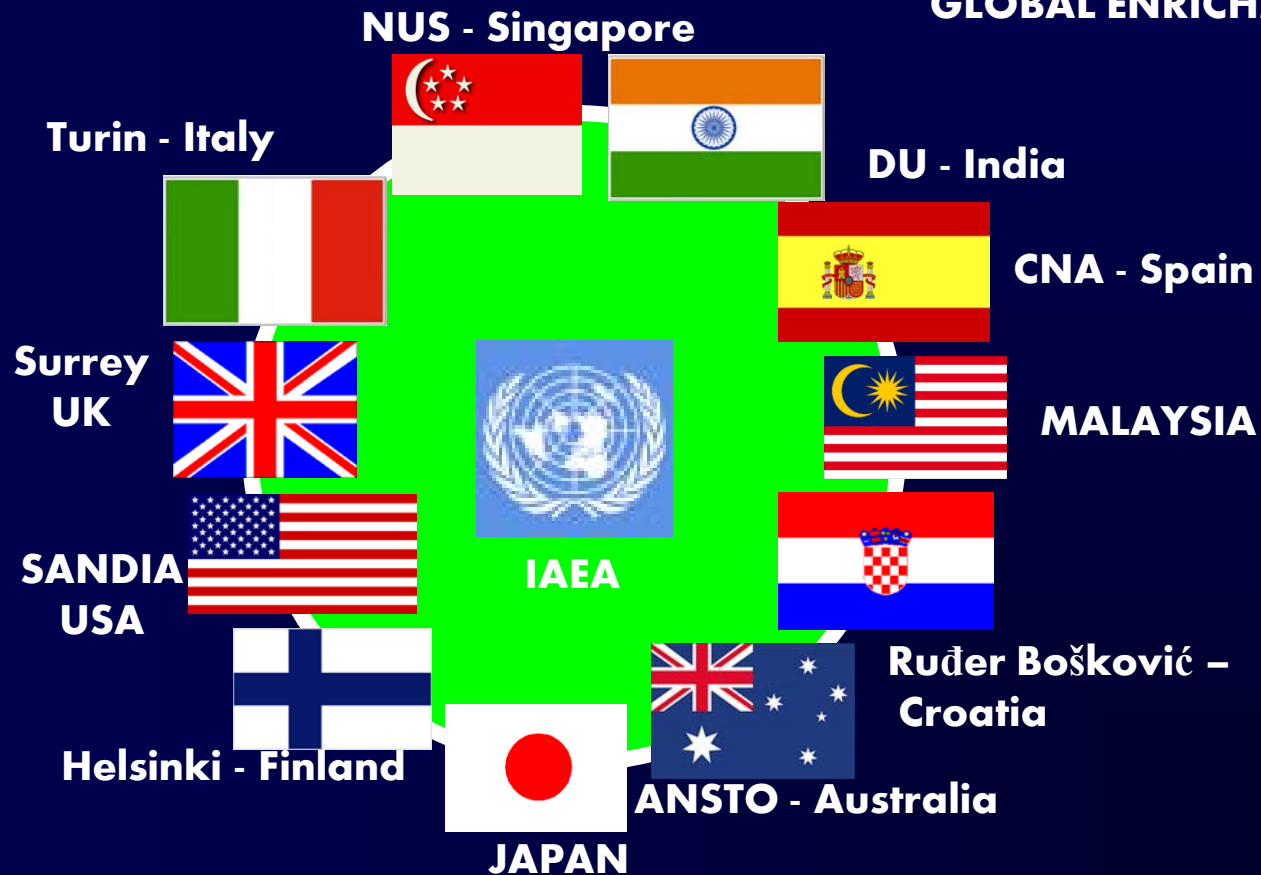
**Displacement dose**

$$\eta = \frac{Y}{Y_0} = 1 - K \cdot \Phi = 1 - K_{ed} \cdot D_d$$



IAEA Coordinate Research Programme (CRP) F11016 (2011-2015)  
“Utilization of ion accelerators for studying and modeling of  
radiation induced defects in semiconductors and insulators”

**COOPERATION AND MUTUAL  
UNDERSTANDING LEAD TO GROWTH AND  
GLOBAL ENRICHMENT**





IAEA Coordinate Research Programme (CRP) F11016 (2011-2015)  
“Utilization of ion accelerators for studying and modeling of  
radiation induced defects in semiconductors and insulators”

**Overall Objective:**

Use of ion accelerators for improved understanding of how radiation induced defects influence the electronic properties of semiconductor/insulator materials, leading to better understanding of how they degrade or improve the performances of devices in extreme and harsh radiation environments.

**Specific Research Objective:**

Deeper theoretical knowledge and experimental data on defects created by light and heavy ions; in terms of their type, density and effect on fundamental electronic properties of semiconductors and insulators.

**Expected Research Outputs:**

Definition of an experimental protocol to determine the key parameters for the characterization of the effects of radiation damage on semiconductor materials and devices.

Refined theoretical models for defect generation and for modelling their effect on electronic properties.



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# Definition of an experimental protocol

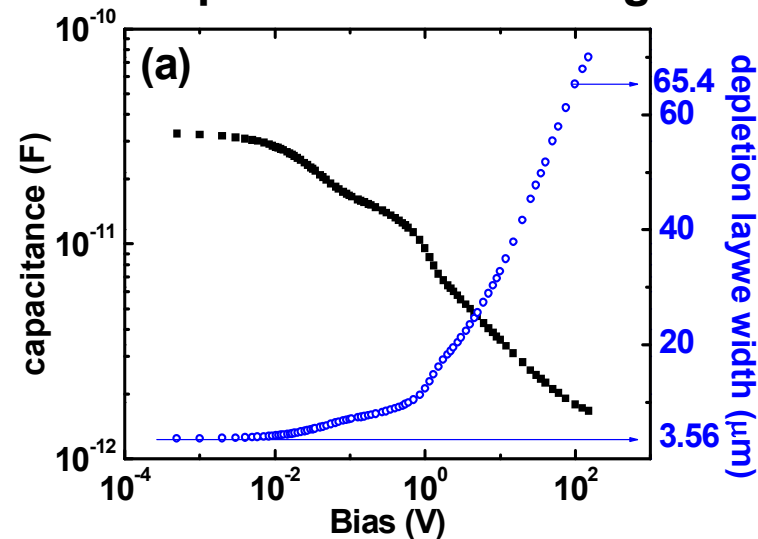
Hamamatsu  
S5821 p-i-n diode



**Experimental  
protocol**

✓ Commercial p-i-n diodes  
✓ **Electrical  
characterization**

## C-V characteristics Depletion width-voltage



Z. Pastuovic et al., IEEE Trans on Nucl. Sc. 56 (2009) 2457; APL (98) 092101 (2011)

Trieste  
15.08.2012

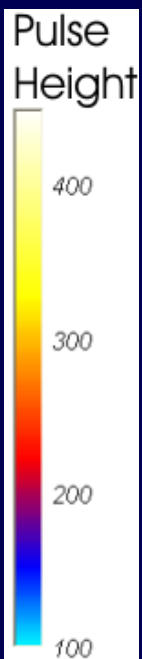
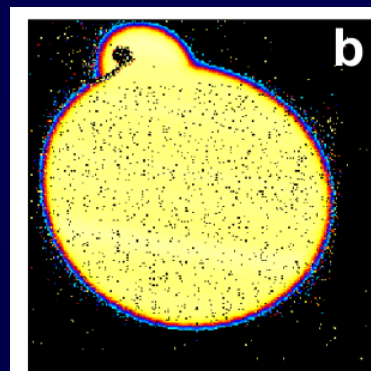
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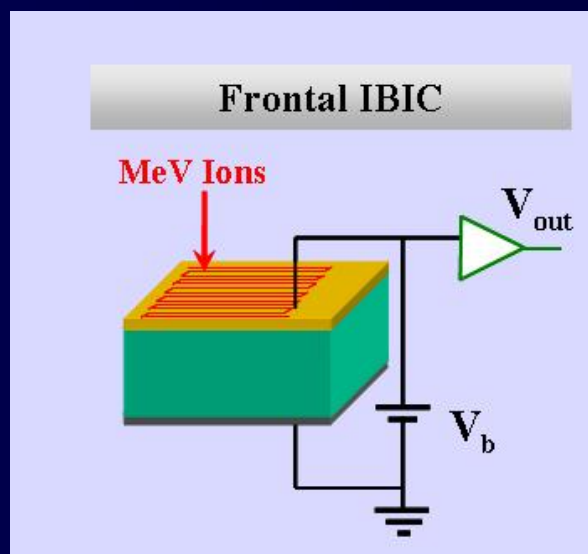


IBIC map on a pristine diode  
probed with a scanning  
1.4 MeV He microbeam;

Hamamatsu  
S5821 p-i-n diode



Uniform CCE map



Experimental  
protocol

- ✓ Commercial p-i-n diodes
- ✓ Electrical characterization
- ✓ IBIC map on pristine sample

Z. Pastuovic et al., IEEE Trans on Nucl. Sc. 56 (2009) 2457; APL (98) 092101 (2011)

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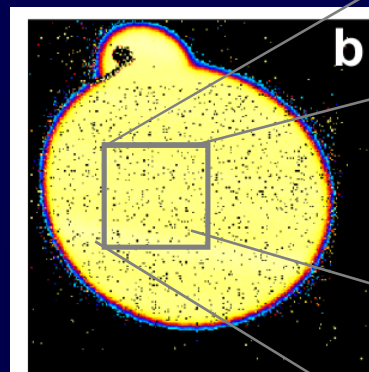
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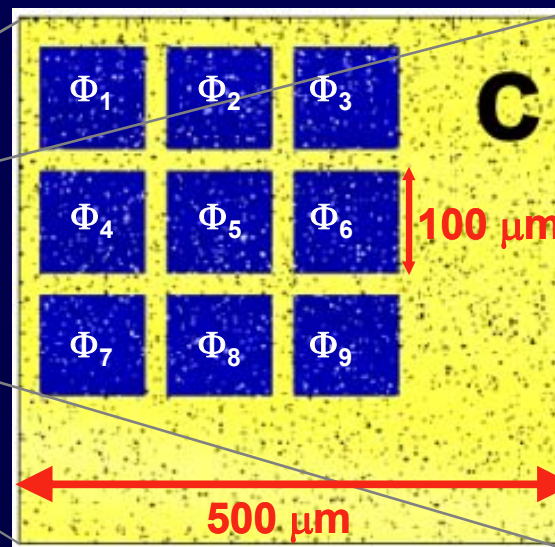
Hamamatsu  
S5821 p-i-n diode



IBIC map on a pristine diode  
probed with a scanning  
1.4 MeV He microbeam;



**ZOOM in view of the selected area for focused  
ion beam irradiation at different fluences  $\Phi$**



### Experimental protocol

- ✓ Commercial p-i-n diodes
- ✓ Electrical characterization
- ✓ IBIC map on pristine sample
- ✓ Irradiation of 9 regions at different fluences

Z. Pastuovic et al., IEEE Trans on Nucl. Sc. 56 (2009) 2457; APL (98) 092101 (2011)

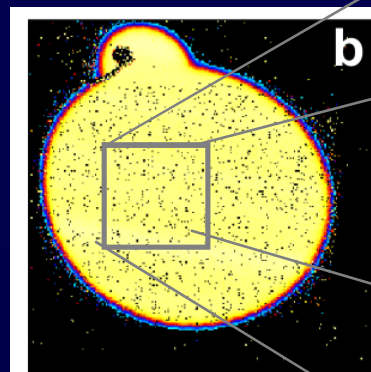




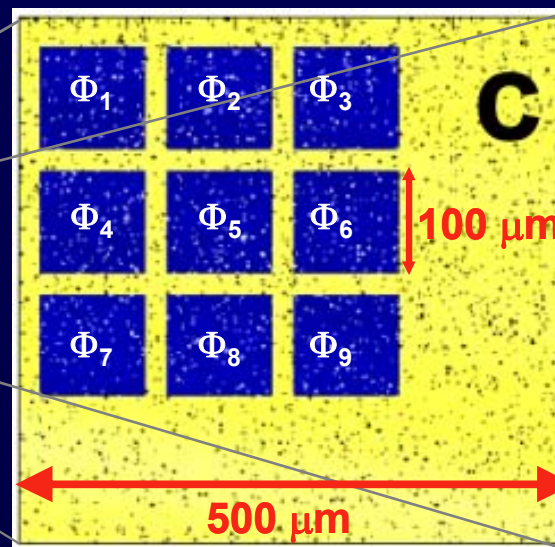
Hamamatsu  
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IBIC map on a pristine diode  
probed with a scanning  
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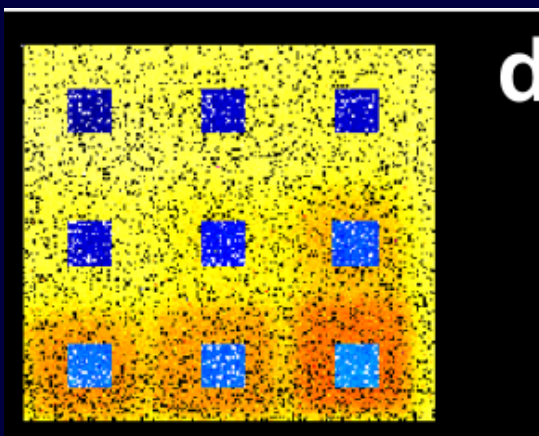
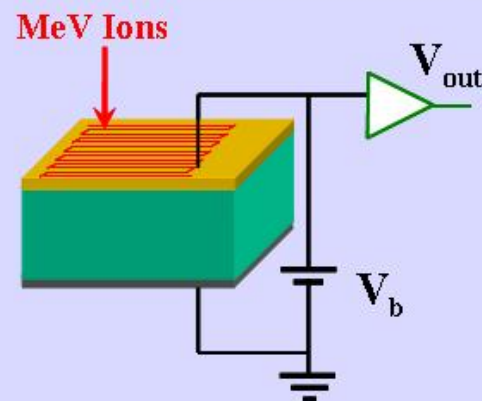
ZOOM in view of the selected area for focused  
ion beam irradiation at different fluences  $\Phi$



### Experimental protocol

- ✓ Commercial p-i-n diodes
- ✓ Electrical characterization
- ✓ IBIC map on pristine sample
- ✓ Irradiation of 9 regions at different fluences
- ✓ IBIC map of irradiated regions

### Frontal IBIC



a measured 2D distribution  
of the IBIC signal amplitude  
after irradiation

Z. Pastuovic et al., IEEE Trans on Nucl. Sc. 56 (2009) 2457; APL (98) 092101 (2011)

Trieste  
15.08.2012

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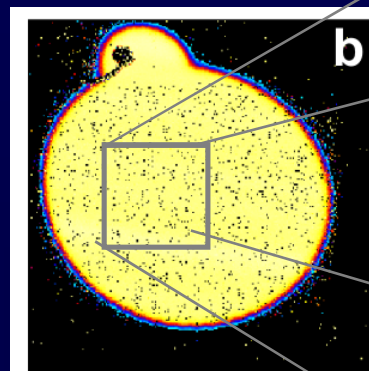




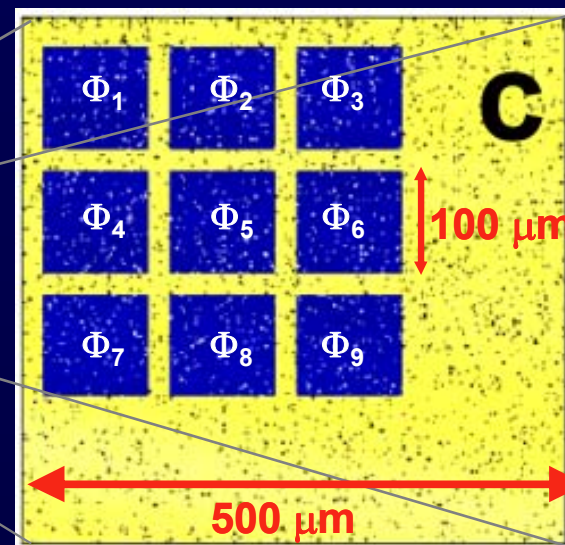
Hamamatsu  
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IBIC map on a pristine diode  
probed with a scanning  
1.4 MeV He microbeam;



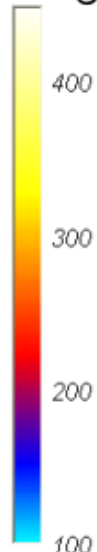
ZOOM in view of the selected area for focused  
ion beam irradiation at different fluences  $\Phi$



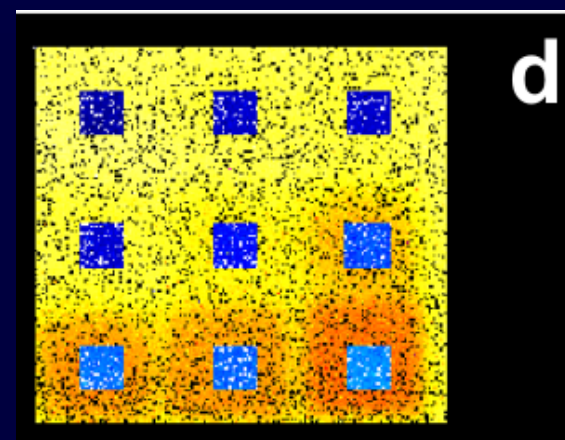
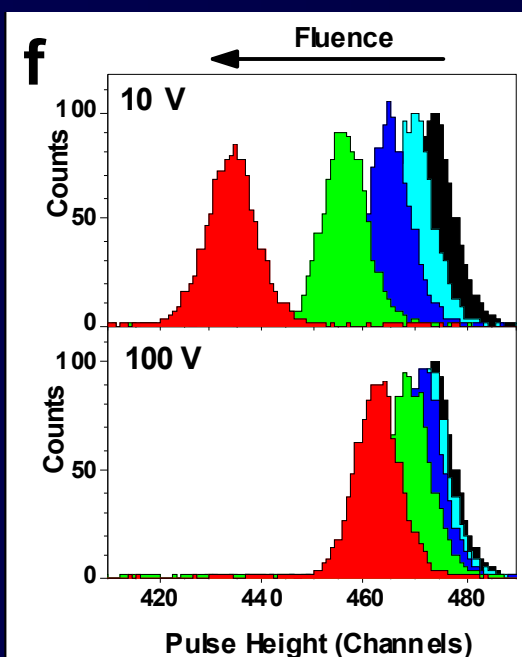
**Experimental  
protocol**

- ✓ Commercial p-i-n diodes
- ✓ Electrical characterization
- ✓ IBIC map on pristine sample
- ✓ Irradiation of 9 regions at different fluences
- ✓ IBIC map of irradiated regions
- ✓ Average pulse height as function of the damage

Pulse  
Height



IBIC spectra  
(bias voltage =  
10 V and 100 V)  
from the central  
regions of four  
of the areas  
shown in Fig. c



a measured 2D distribution  
of the IBIC signal amplitude  
after irradiation

Z. Pastuovic et al., IEEE Trans on Nucl. Sc. 56 (2009) 2457; APL (98) 092101 (2011)

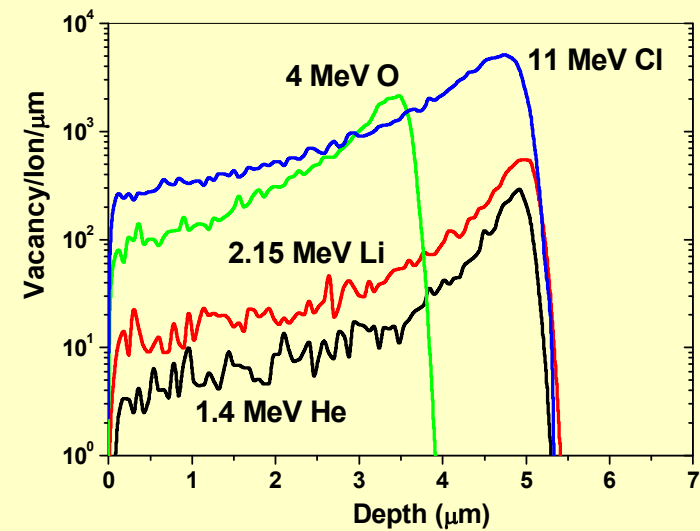
Trieste  
15.08.2012

Joint ICTP-IAEA Workshop on Physics of Radiation Effect and its  
Simulation for Non-Metallic Condensed Matter

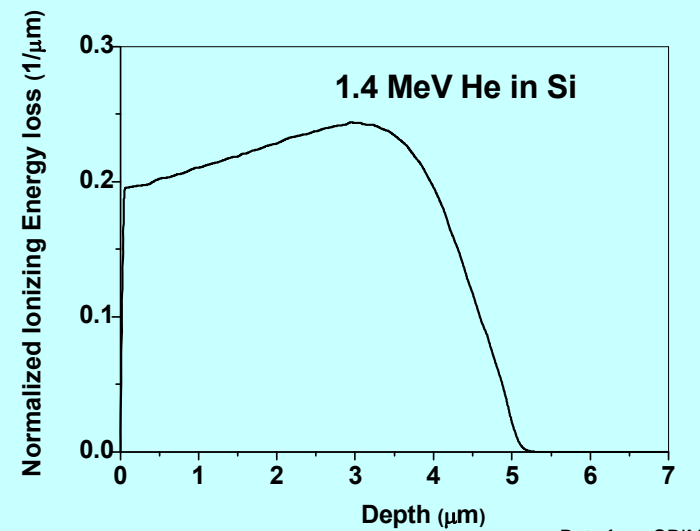
32

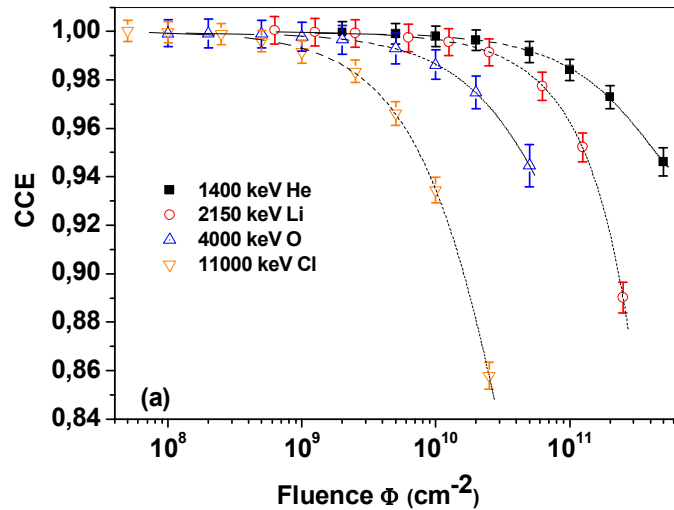


## Damaging Ions



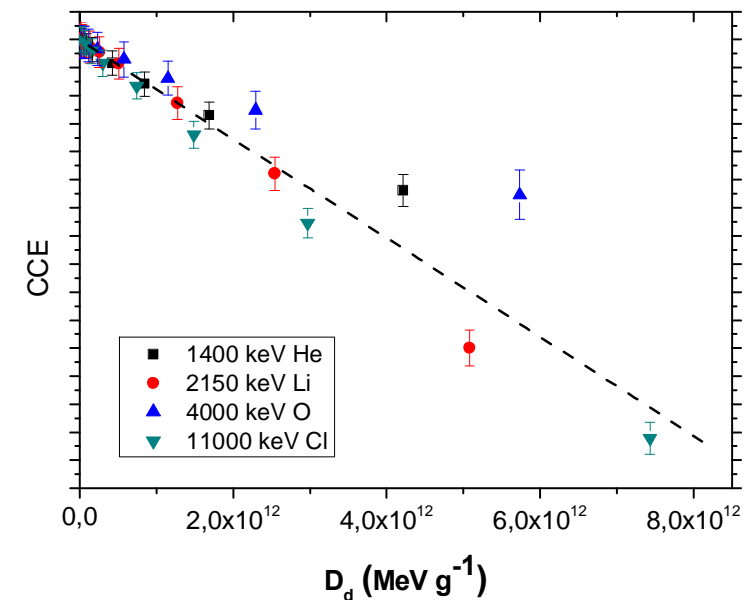
## Ion Probe



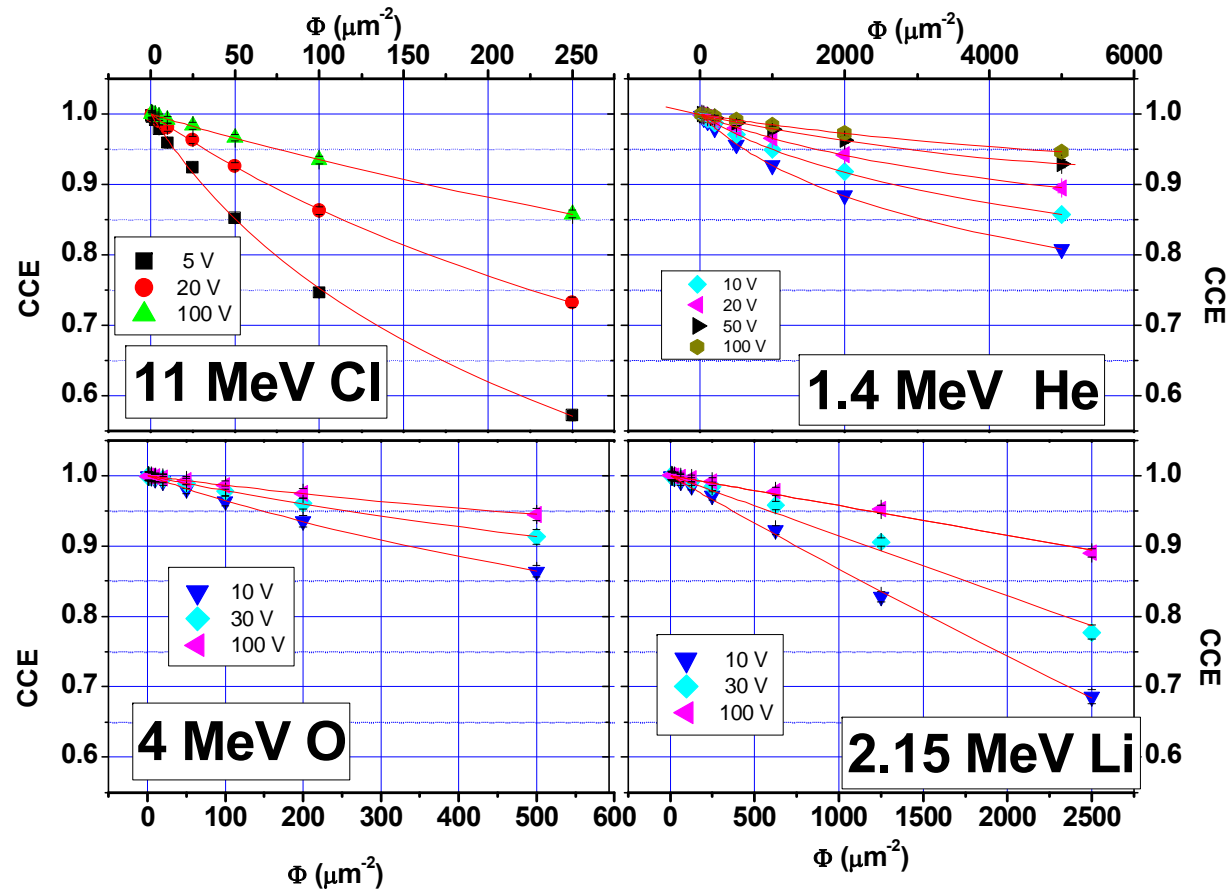


CCE behavior in regions damaged with different ions vs. ion fluence ( $\Phi$ ); the dashed lines are parabolic fits as guides for eyes.

**$V_{\text{bias}} = 100 \text{ V}$**   
**Fully depleted device**



The same data points shown in Fig. 4 for plotted against the adjusted damage dose  $D_d$ .



Measured CCE values for 1400 keV He ion detection in selected areas of biased Hamamatsu S5821 diodes irradiated with different fluences 1.4 MeV He, 2.15 MeV Li, 4.0 MeV O and 11 MeV Cl ions. The dashed lines are parabolic fits as guides for eyes.



IAEA Coordinate Research Programme (CRP) F11016 (2011-2015)  
“Utilization of ion accelerators for studying and modeling of  
radiation induced defects in semiconductors and insulators”

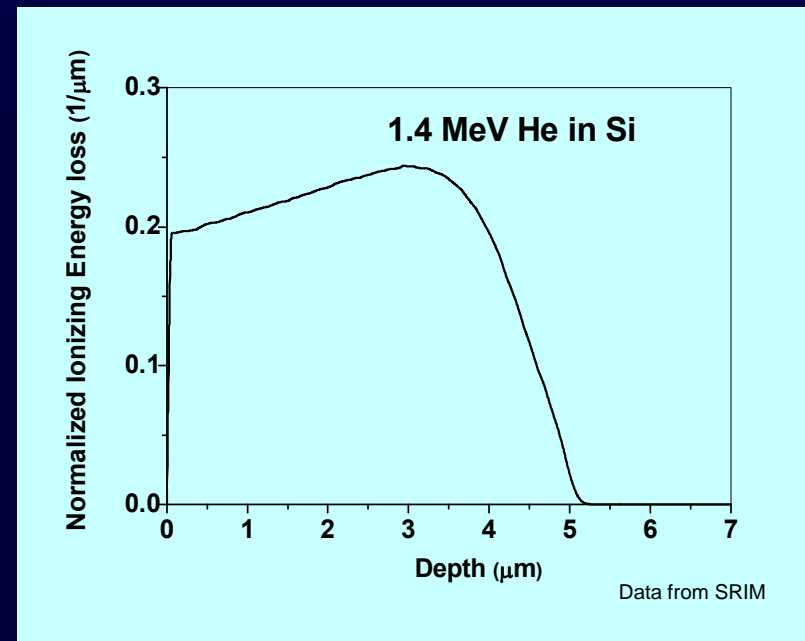
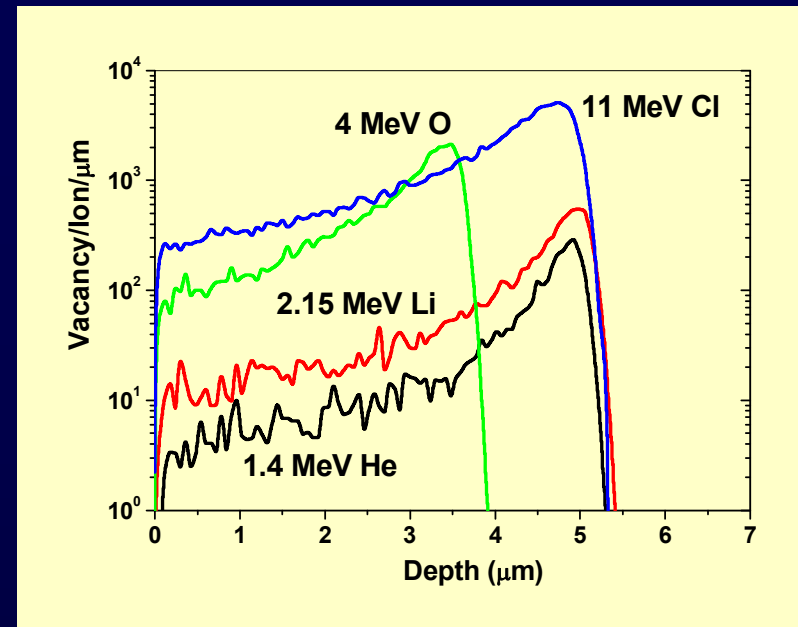
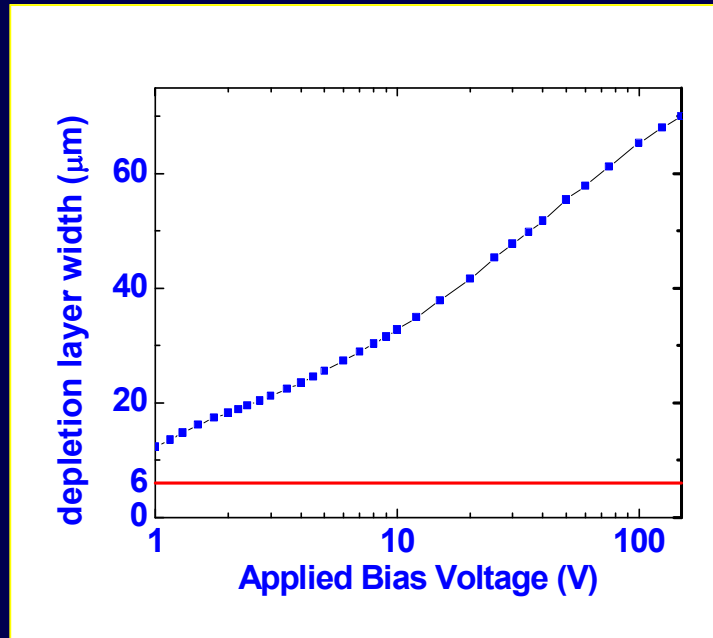
**Expected Research Outputs:**

Definition of an experimental protocol to determine the key parameters for the characterization of the effects of radiation damage on semiconductor materials and devices.

**Refined theoretical models for defect generation and for modelling their effect on electronic properties.**



## Fully depleted device





Fully depleted

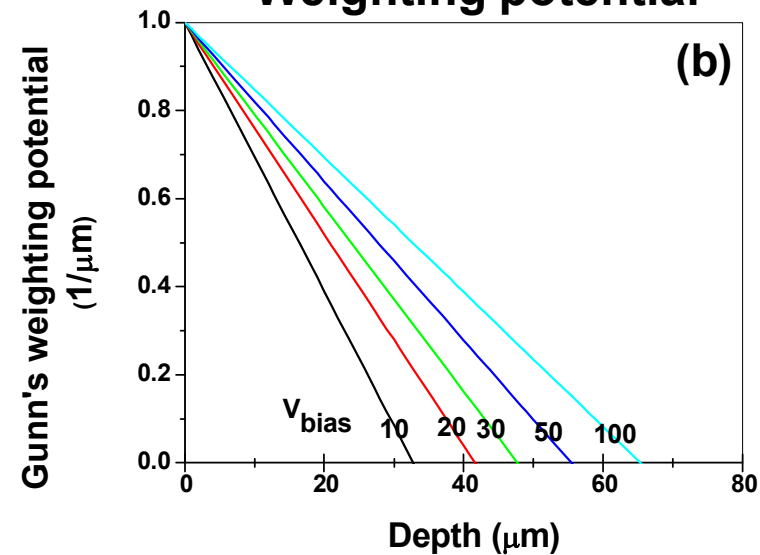


Ramo Theorem  
(no diffusion)

$$\phi = \frac{\partial \psi}{\partial V} = \begin{cases} \left(1 - \frac{x}{w}\right) & \text{for } x < w \\ 0 & \text{for } x > w \end{cases}$$

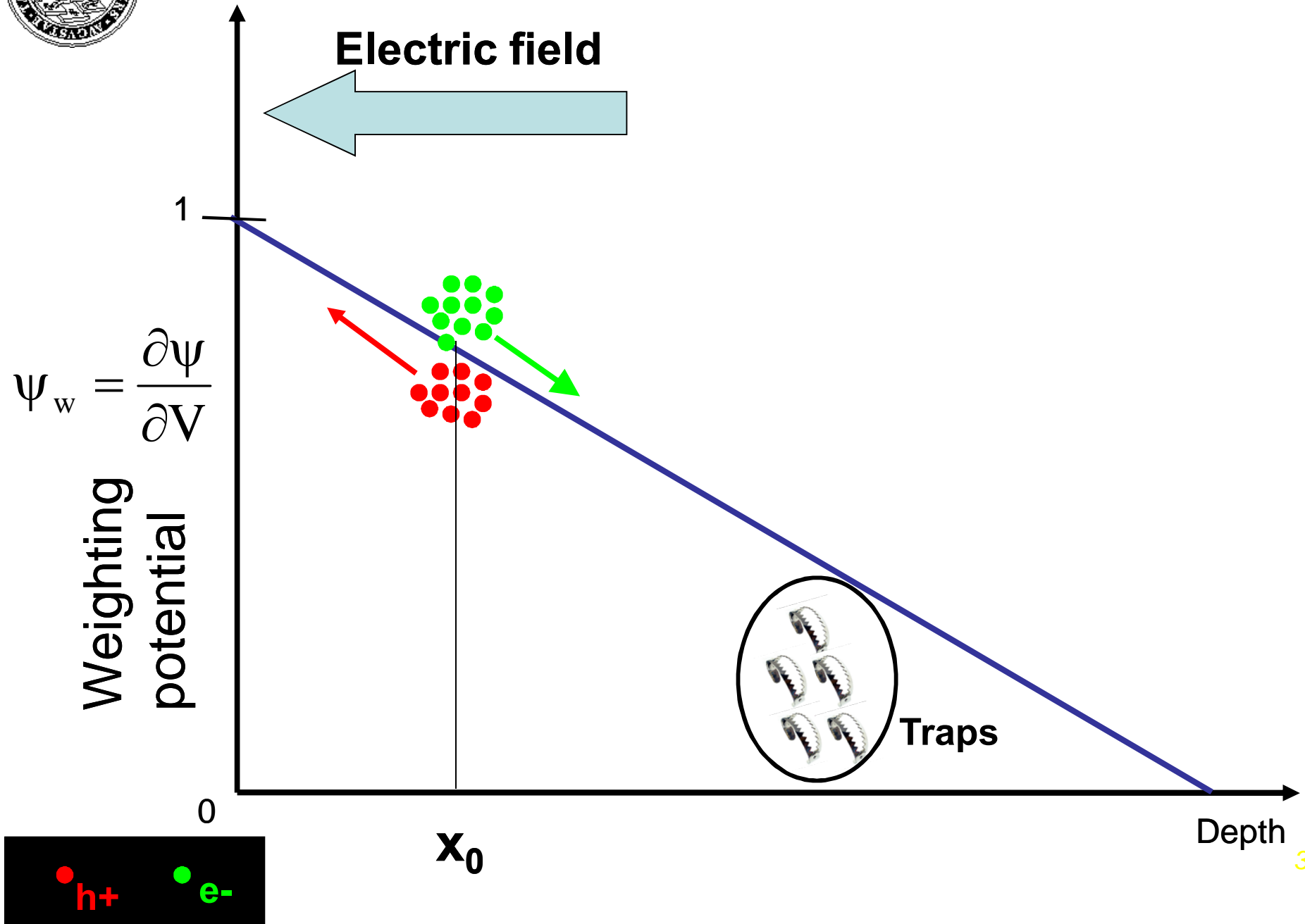
$$\left( \phi = \frac{\partial \psi}{\partial V_{\text{bias}}} \right)$$

Weighting potential





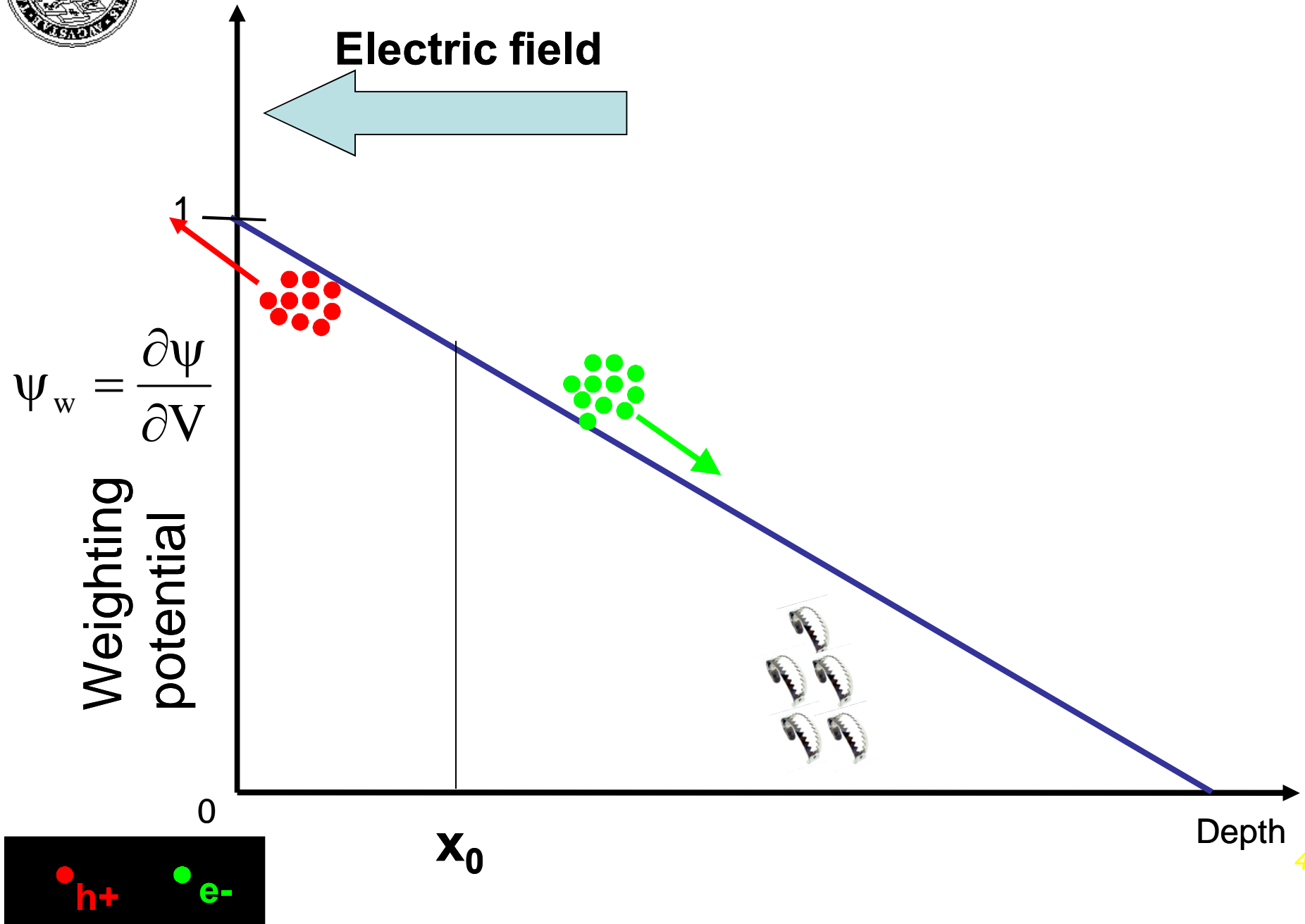
# Effects of localized recombination centres





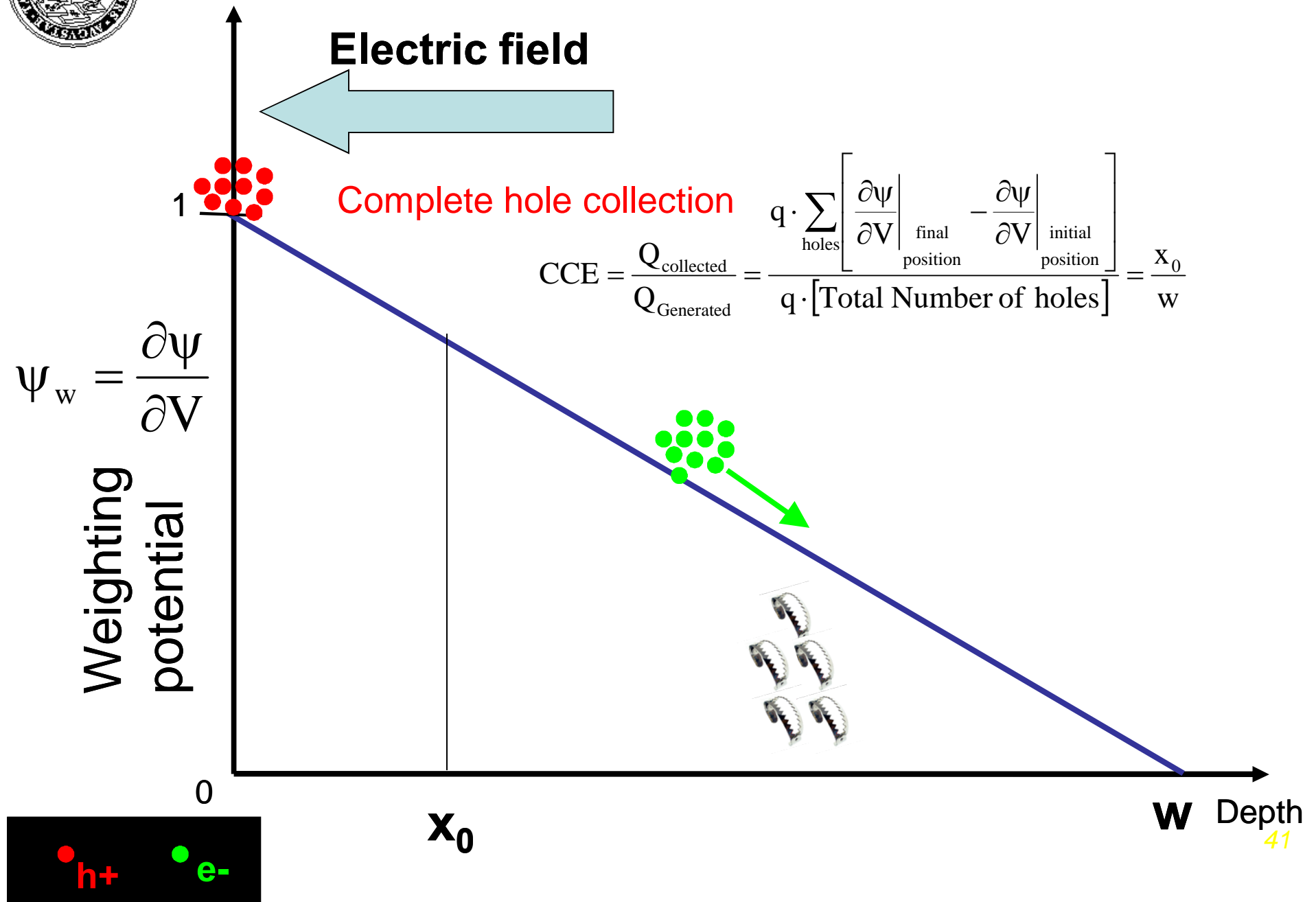


# Effects of localized recombination centres



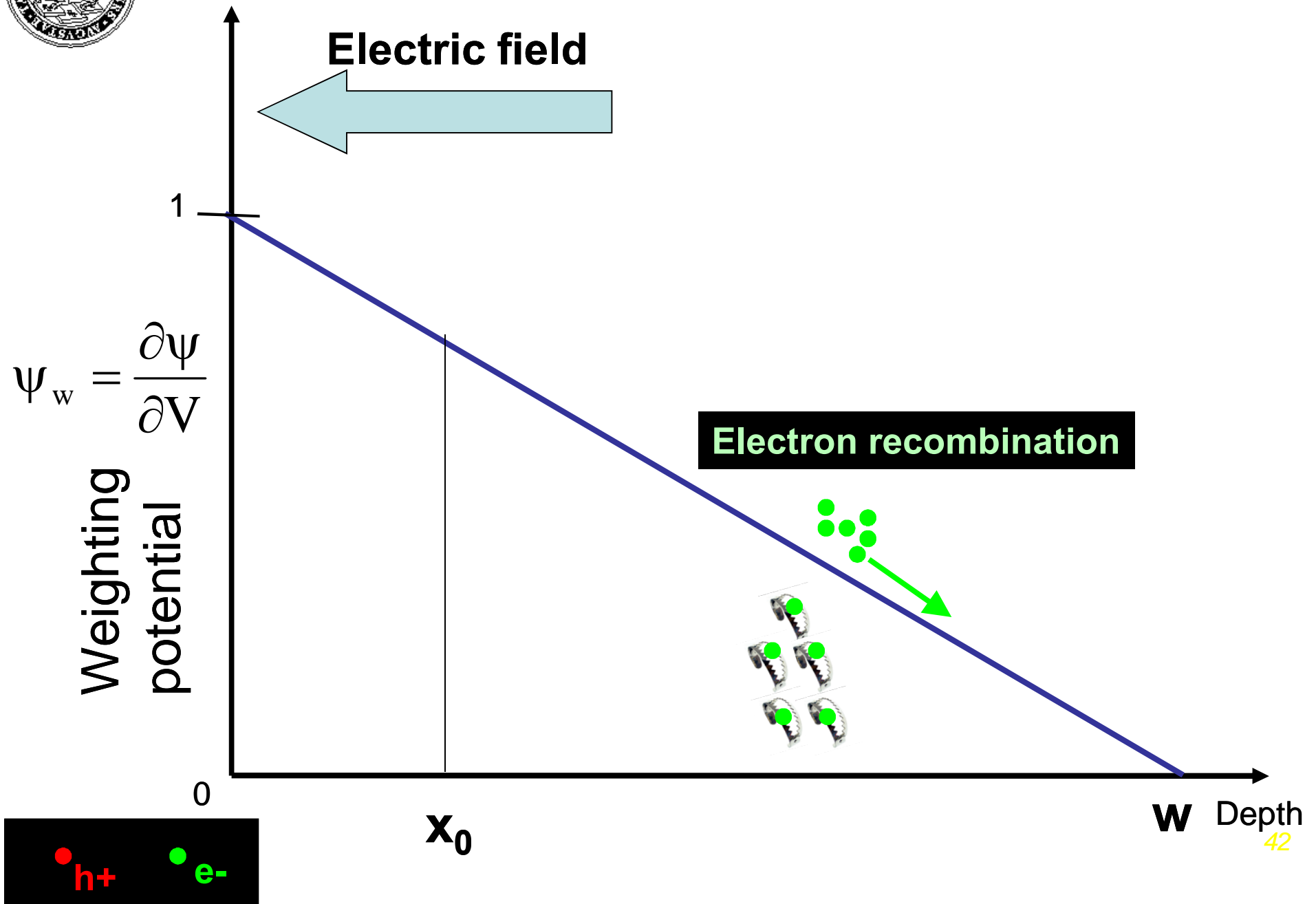


# Effects of localized recombination centres



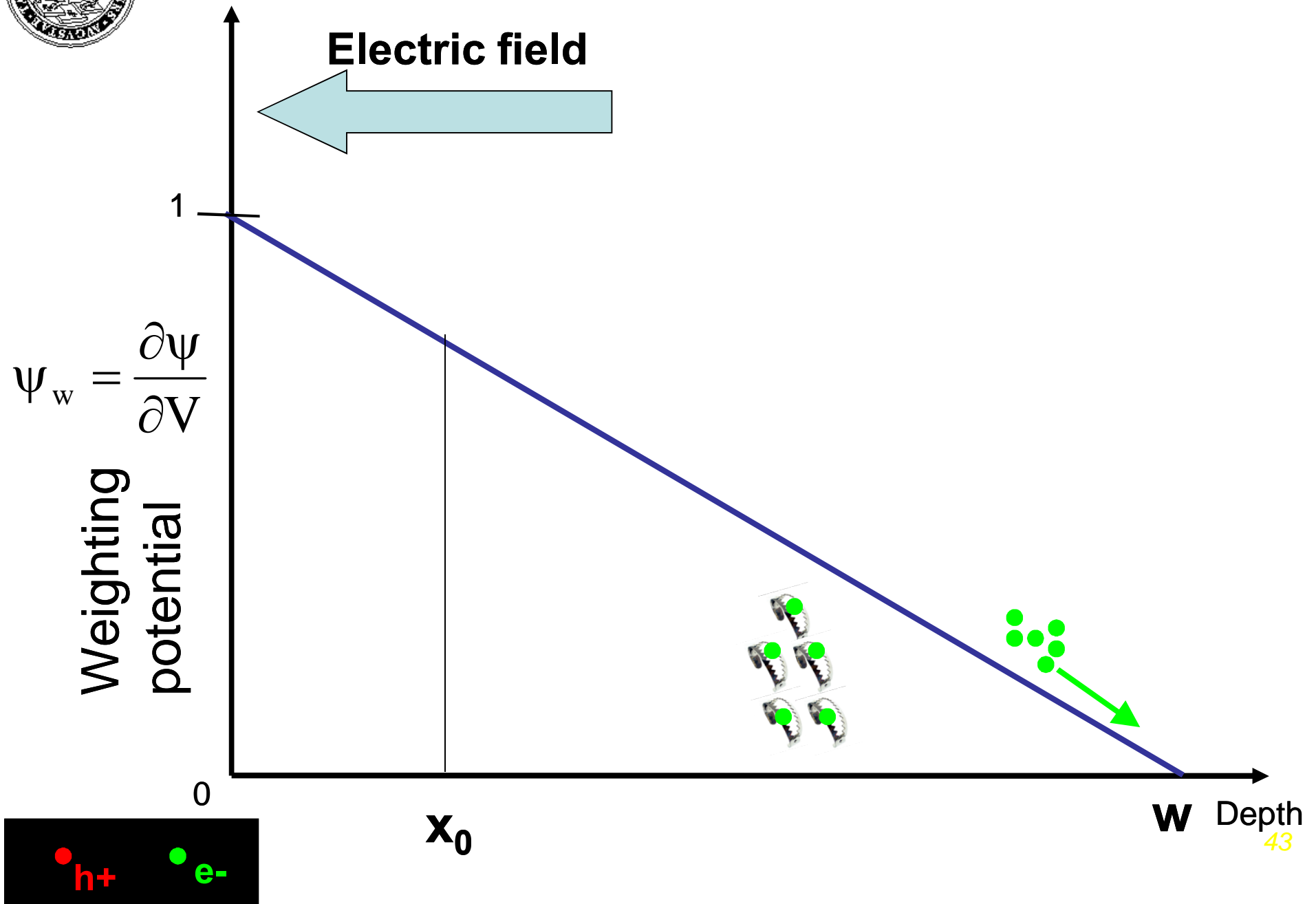


# Effects of localized recombination centres



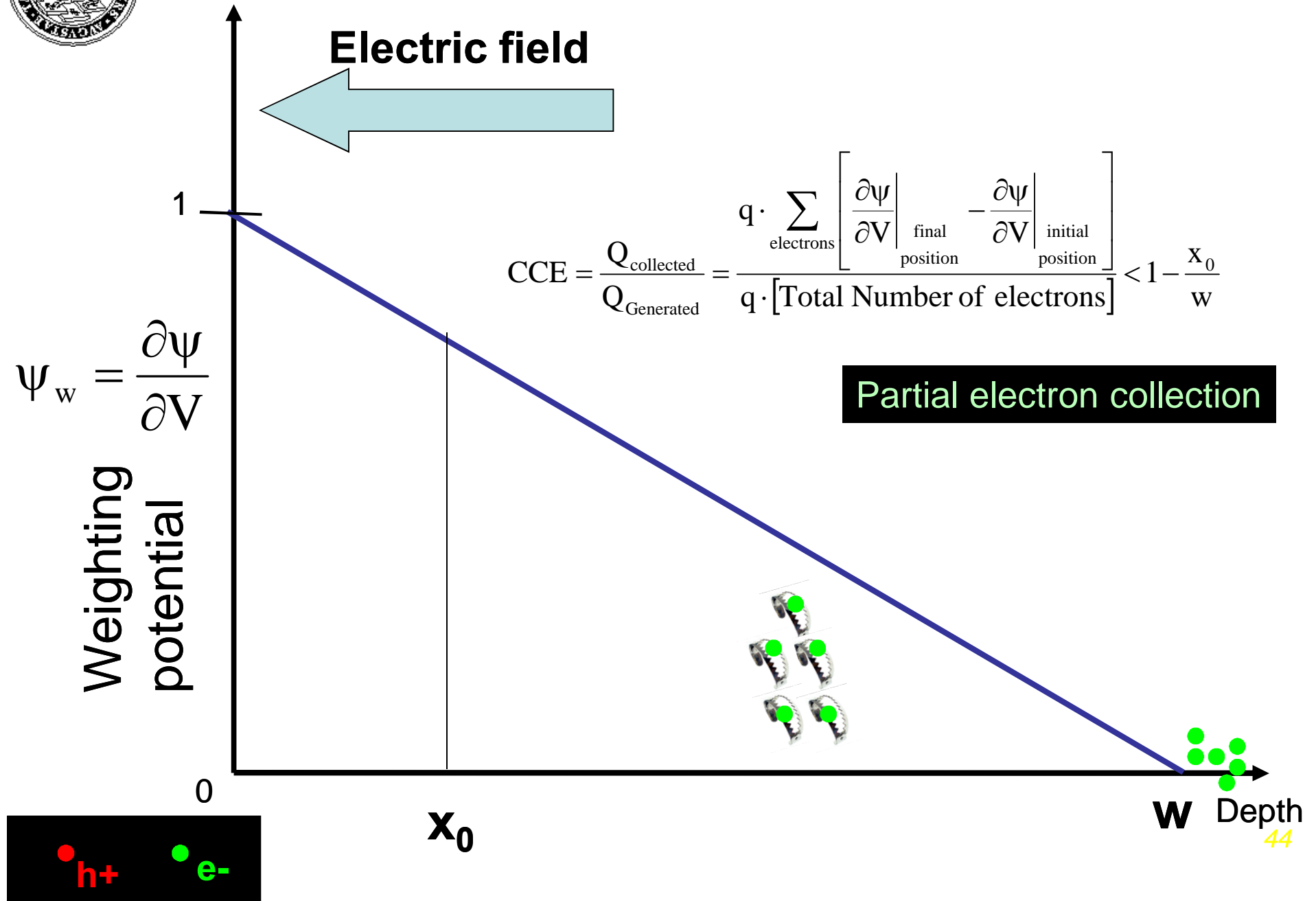


## Effects of localized recombination centres





# Effects of localized recombination centres





# Shockley-Read-Hall model

$$\frac{1}{\tau} = N_{\text{trap}} \cdot \sigma \cdot v_{\text{th}} = N_{\text{trap}}^0 \cdot \sigma^0 \cdot v_{\text{th}} + N'_{\text{trap}} \cdot \sigma' \cdot v_{\text{th}} = \frac{1}{\tau_0} + N'_{\text{trap}} \cdot \sigma' \cdot v_{\text{th}}$$

Diagram illustrating the Shockley-Read-Hall model equation, with variables defined by callouts:

- $\tau$ : Actual Carrier Lifetime
- $N_{\text{trap}}$ : Trap density in pristine material
- $\sigma$ : effective capture cross section in pristine material
- $v_{\text{th}}$ : Thermal velocity ( $\approx 10^7$  cm/s)
- $N_{\text{trap}}^0$ : Trap density in pristine material
- $\sigma^0$ : effective capture cross section in pristine material
- $N'_{\text{trap}}$ : Ion induced Trap density
- $\sigma'$ : capture cross section Of ion induced traps
- $\tau_0$ : Carrier Lifetime in pristine material



# Shockley-Read-Hall model

$$\frac{1}{\tau} = \frac{1}{\tau_0} + N'_{\text{trap}} \cdot \sigma' \cdot v_{\text{th}}$$

**Average number of active trap per vacancy**

Ion induced  
Trap density

Vacancy profile  
(from SRIM)

$$N'(x) = k \cdot \text{Vac}(x)$$





# Shockley-Read-Hall model

Average number of active trap per vacancy

Actual  
Carrier Lifetime

Carrier Lifetime  
in pristine material

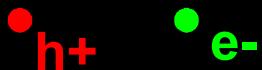
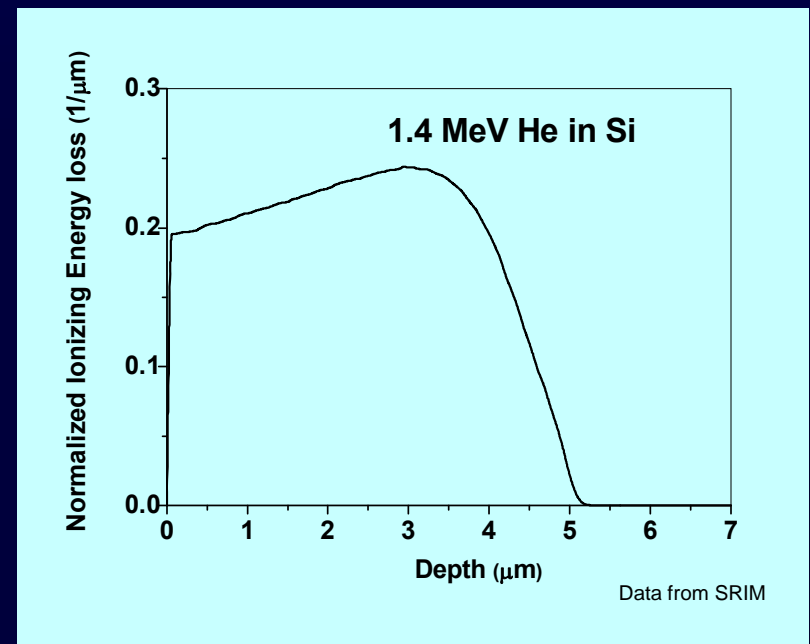
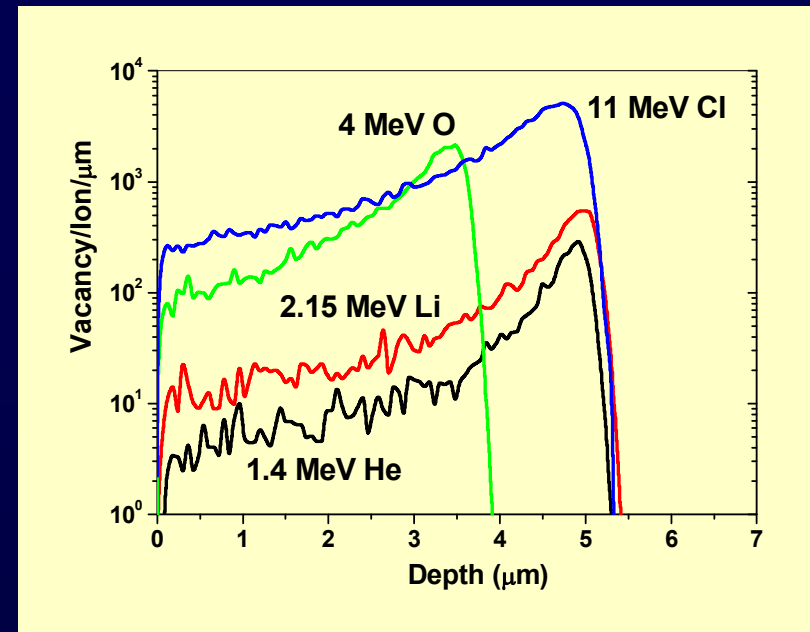
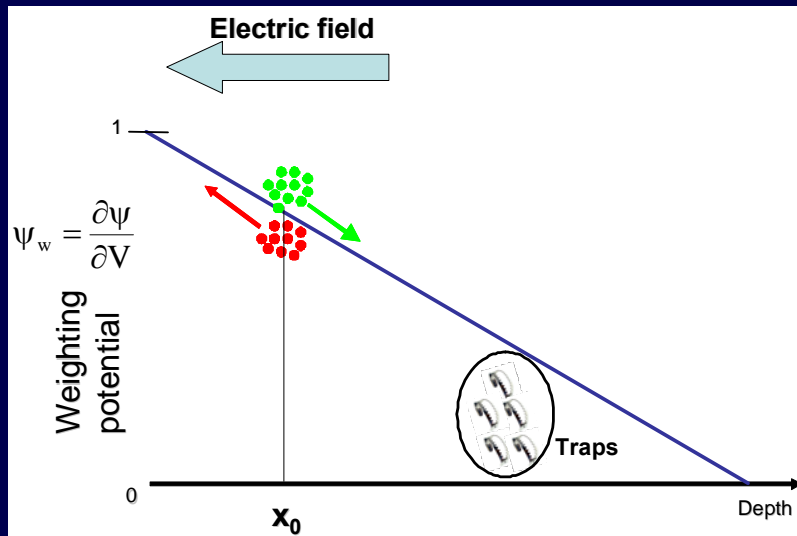
$$\tau(x, \Phi) = \frac{\tau_0(x)}{1 + k \cdot \text{Vac}(x) \cdot \sigma \cdot v_{th} \cdot \Phi \cdot \tau_0(x)}$$

Vacancy profile  
(from SRIM)

Thermal velocity  
( $\approx 10^7$  cm/s)

Ion fluence

effective capture cross section  
(from DLTS)





# Ramo Theorem (no diffusion)

## Induced charge

from the motion of electrons

$$\eta(x, \Phi) = \frac{1}{w} \cdot \int_x^w dy \cdot \exp \left[ - \int_x^y \frac{dz}{v_e(z) \cdot \tau_e(z, \Phi)} \right]$$

from the motion of holes

$$\eta(x, \Phi) = \frac{1}{w} \cdot \int_0^x dy \cdot \exp \left[ - \int_y^x \frac{dz}{v_h(z) \cdot \tau_h(z, \Phi)} \right]$$

$$\text{Drift Length} = v_h(z) \cdot \tau_h(z, \Phi) \gg w$$

**Low damage level**

**Linearization**

$$\eta(x, \Phi) \cong 1 - \Phi \cdot \left[ \frac{k_e \cdot \sigma_e \cdot v_{th}}{w} \cdot \int_x^w dy \cdot \int_x^y \frac{Vac(z)}{v_e(z)} dz + \frac{k_h \cdot \sigma_h \cdot v_{th}}{w} \cdot \int_0^x dy \cdot \int_y^x \frac{Vac(z)}{v_h(z)} dz \right]$$



# At high bias voltage Hole contribution negligible Saturation drift velocity Semi-analytical expression

$$CCE(\Phi) = 1 - k_e \cdot \sigma_e \cdot \frac{V_{th}}{\langle v_e \rangle} \cdot \left\{ \int_0^w dz \cdot \left[ \tilde{E}_{Ion}(z) \cdot Vac(z) \cdot \left( 1 - \frac{z}{w} \right) \right] \right\} \cdot \Phi \equiv 1 - K_e^* \cdot \Phi_e^*$$

Ion probe energy loss

Vacancy profile

Weighting potential

$$\Phi^* = \text{Effective Fluence} = \int_0^w dz \cdot \left[ \tilde{E}_{Ion}(z) \cdot Vac(z) \cdot \left( 1 - \frac{z}{w} \right) \right]$$

$$K_e^* = \text{effective damage factor} = k_e \cdot \sigma_e \cdot \frac{V_{th}}{\langle v_e \rangle}$$

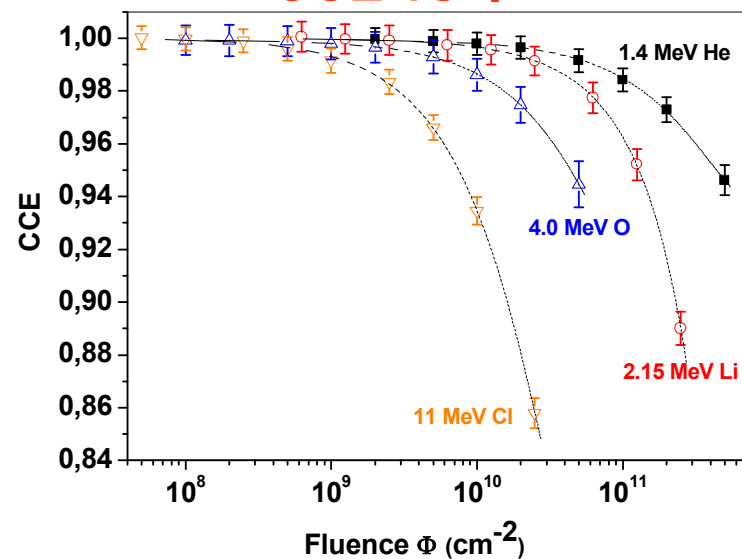
Average drift velocity

Average number of active trap per vacancy

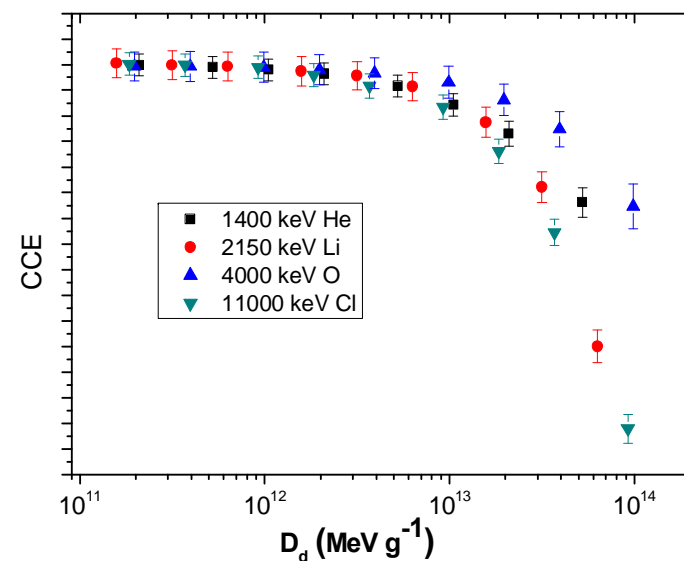
capture cross section of ion induced traps

$V_{\text{bias}} = 100 \text{ V}$

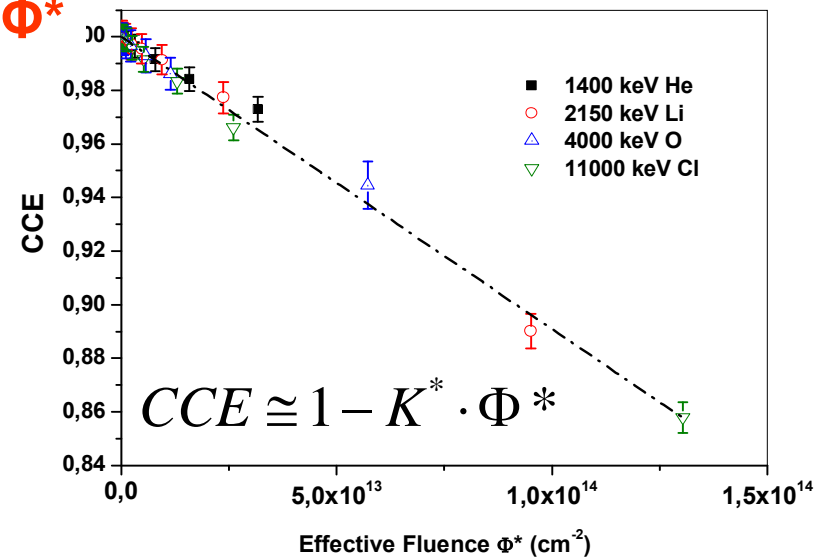
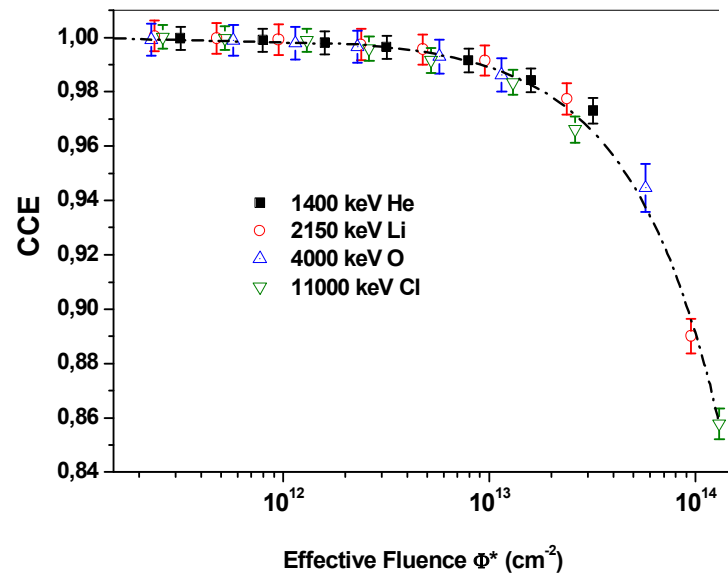
### CCE vs $\Phi$

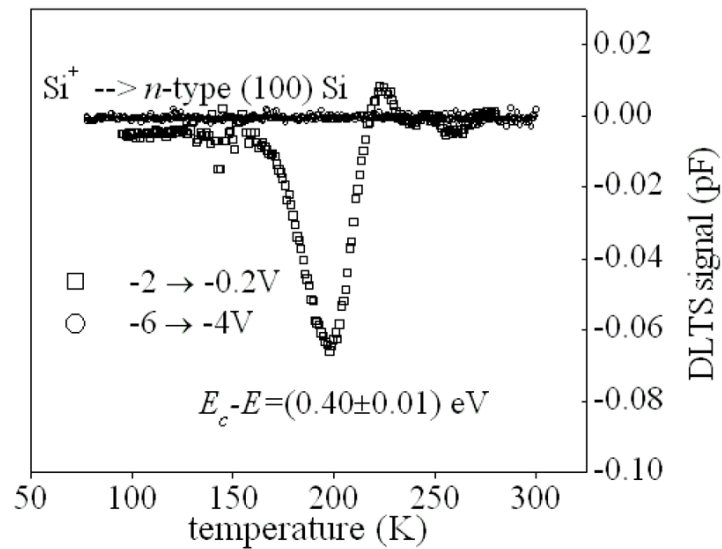


### CCE vs $D_d$



### CCE vs $\Phi^*$





**DLTS measurements  
singly V2(-/0) negatively charged divacanc**

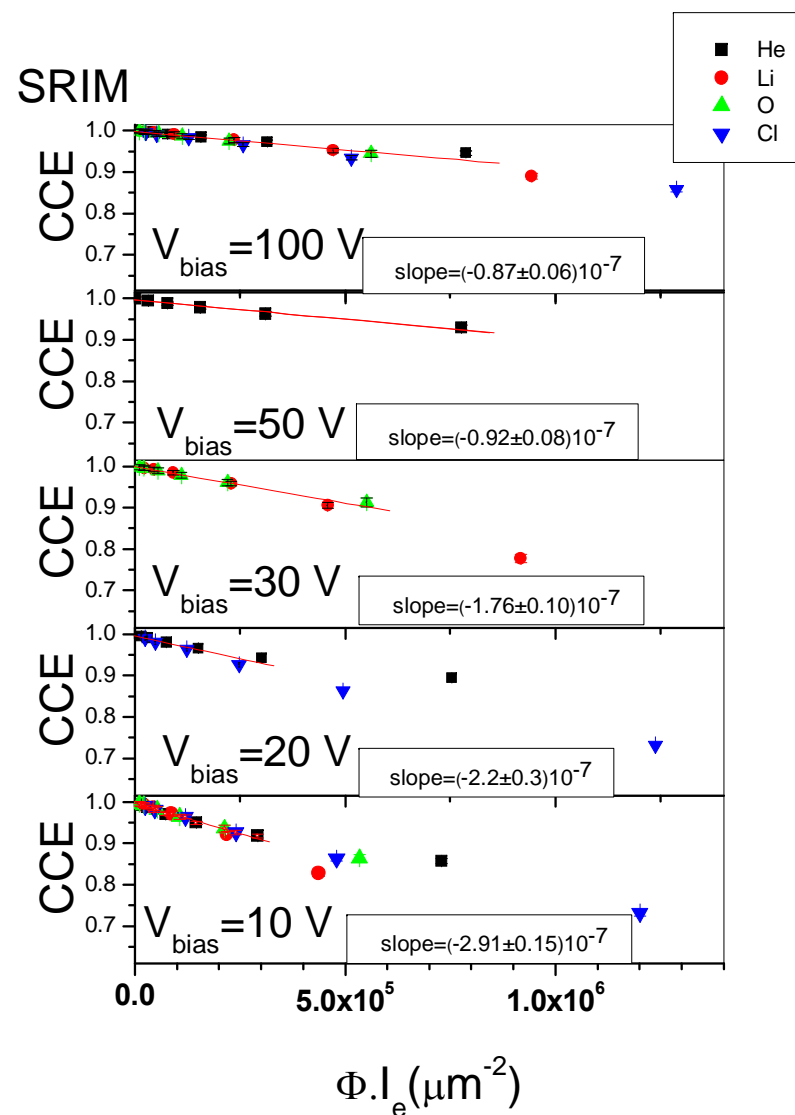
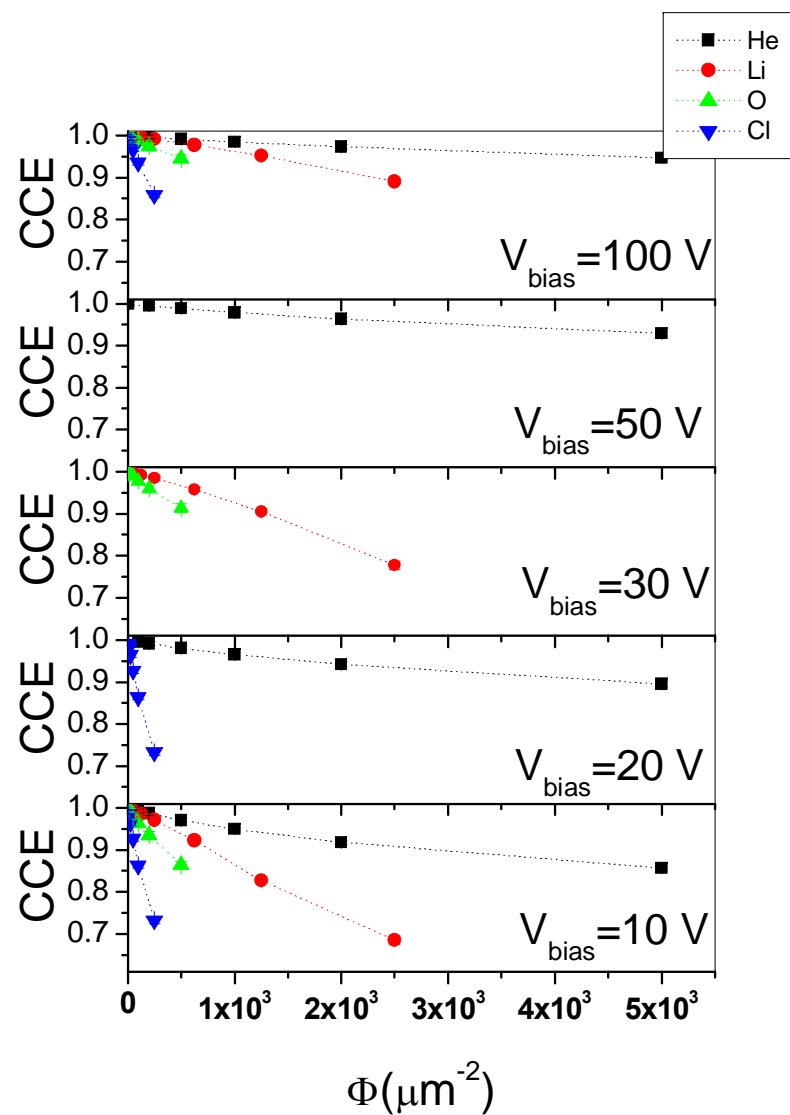
$$\sigma_e \approx 5 \cdot 10^{-15} \text{ cm}^2$$

$$K^* = \frac{k_e \cdot \sigma_e \cdot v_{th}}{v_e} = (1.09 \pm 0.02) \cdot 10^{-15} \text{ cm}^2.$$

$$k_e \approx 0.2$$

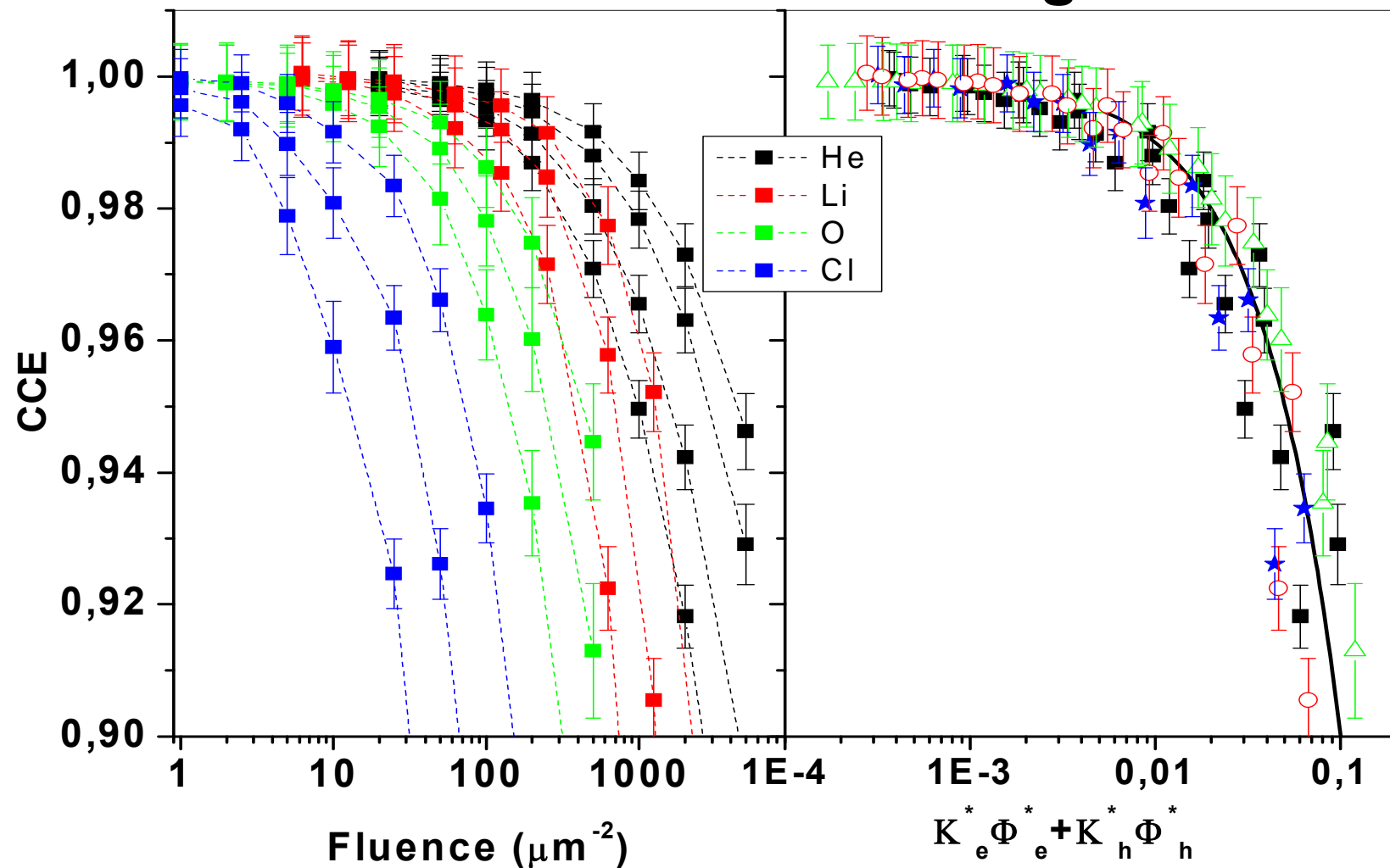
**i.e. 5 vacancy to generate an electrically stable trap in low doped n-type silicon**

**The  $K^*$  value is independent from the type and energy of the damaging and probing ions and is attributable only to the intrinsic radiation hardness of the material**





## At different bias voltages





## In the low damage regime

The degradation of the CCE of a semiconductor detector due to the damage induced by ions of different mass and energy can be interpreted on the basis of a simplified theory of the IBIC technique.

$$\text{CCE}(\Phi) \equiv 1 - K_e^* \cdot \Phi_e^*$$

Effective fluence

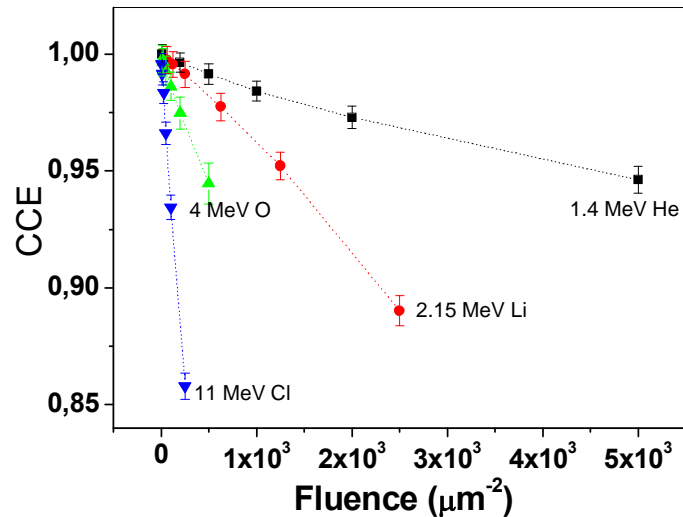
$$\Phi^* = \Phi \cdot \left\{ \frac{1}{d} \cdot \frac{1}{E_p} \int_0^{R_p} dx \frac{dE_p}{dx} \cdot \left[ \int_x^d dz [V(z) \cdot (d - z)] \right] \right\}$$

can be numerically calculated from the vacancy and ionization profiles extracted from the SRIM code.

Effective damage factor

$$K^* = \frac{k_e \cdot \sigma_e \cdot v_{th}}{v_e} = (1.09 \pm 0.02) \cdot 10^{-15} \text{ cm}^2.$$

the effective damage factor  $K^*$  is the slope of the CCE degradation as function of  $\Phi^*$  is proportional to the fraction of the electrically active trap per vacancy



**K\*** can be considered an index that would reliably rank the relative radiation hardness of semiconductors in order to optimize the selection procedure for devices working in high radiation environment.

Effective damage factor

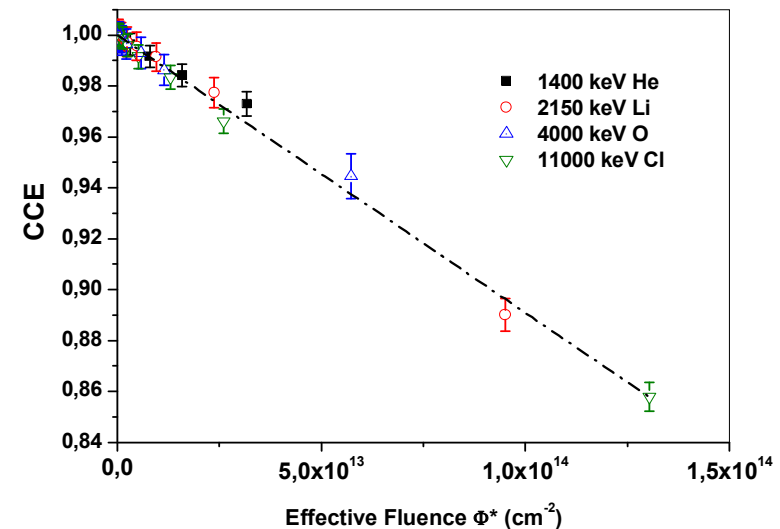
$$K^* = \frac{k_e \cdot \sigma_e \cdot v_{th}}{v_e} = (1.09 \pm 0.02) \cdot 10^{-15} \text{ cm}^2.$$

$\sigma$  : measured from DLTS

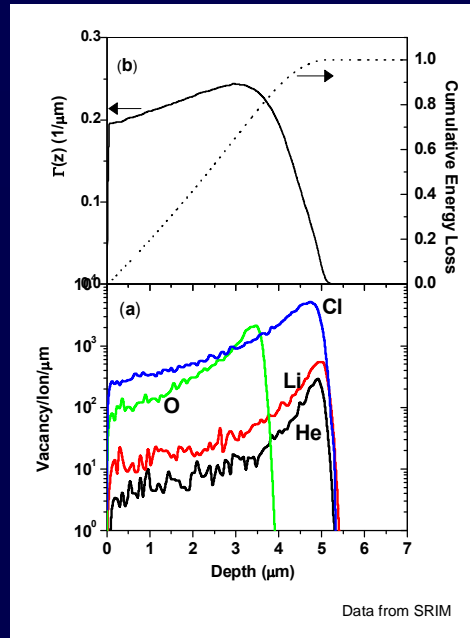
$v_{th}$ : thermal velocity

$v_e$ : electron average velocity

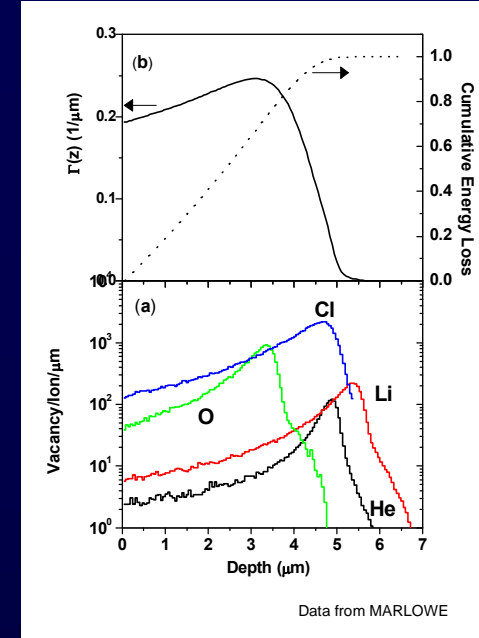
$k_e$ : average number of trap/vacancy



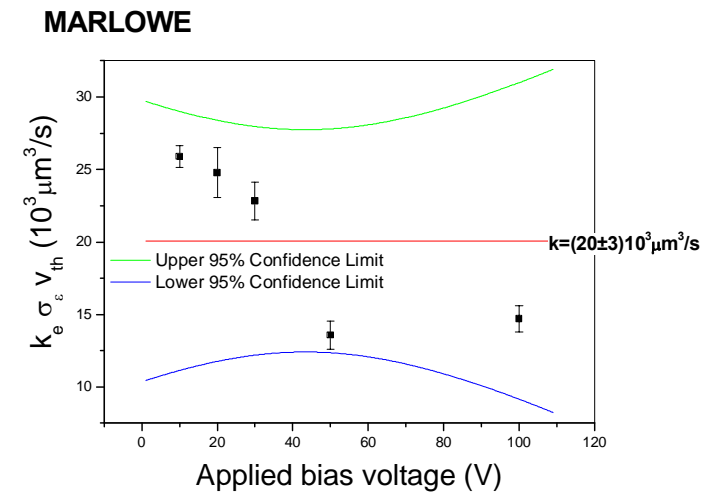
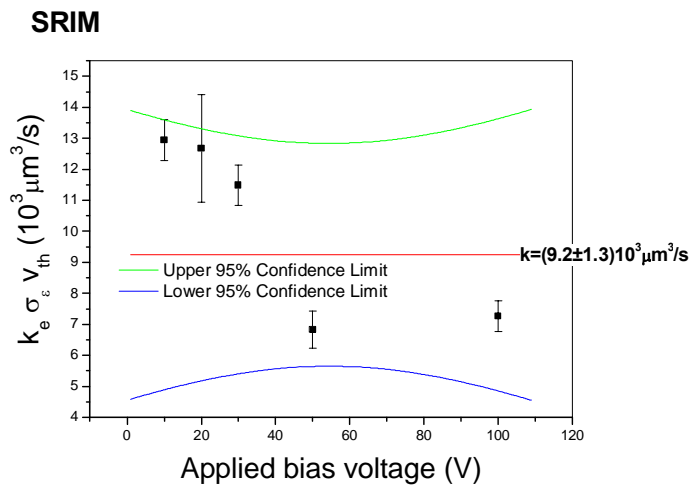
Approach more efficient to condense the CCE degradation data into a single curve than the phenomenological displacement damage dose analysis;  
NIEL is valid only in the case of constant vacancy profile.



**SRIM**



**MARLOWE**





IAEA Coordinate Research Programme (CRP) F11016 (2011-2015)  
“Utilization of ion accelerators for studying and modeling of  
radiation induced defects in semiconductors and insulators”

**Overall Objective:**

Use of ion accelerators for improved understanding of how radiation induced defects influence the electronic properties of semiconductor/insulator materials, leading to better understanding of how they degrade or improve the performances of devices in extreme and harsh radiation environments.

**Specific Research Objective:**

Deeper theoretical knowledge and experimental data on defects created by light and heavy ions; in terms of their type, density and effect on fundamental electronic properties of semiconductors and insulators.

**Expected Research Outputs:**

Definition of an experimental protocol to determine the key parameters for the characterization of the effects of radiation damage on semiconductor materials and devices.

Refined theoretical models for defect generation and for modelling their effect on electronic properties.



## Low Level of damage

Vacancy profile  
(from SRIM, MARLOWE; PAS)

Shockley-Read-Hall  
Recombination/trapping  
model

Electrostatics of the  
device (TCAD)

Trap cross section

Shockley-Ramo-Gunn Theorem  
Adjoint equation formalism  
Finite element method  
Monte Carlo method  
Semi-analytical approach in simple cases



Trap/vacancy ratio  
Radiation hardness