

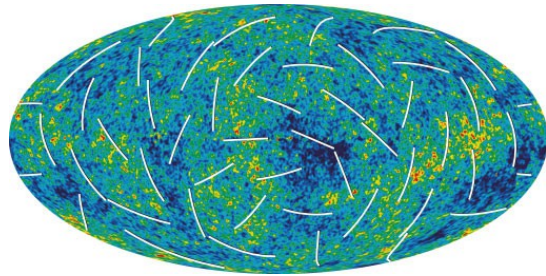
Evidence for sterile neutrinos from precision cosmology?

Yvonne Y. Y. Wong
RWTH Aachen

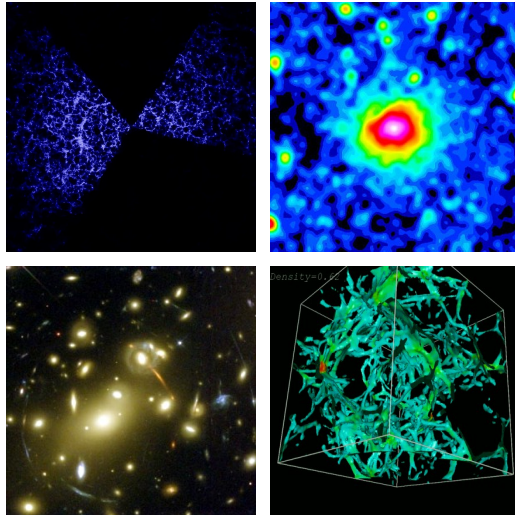
BeNe 2012, Trieste
September 17 – 21, 2012

Precision cosmological probes...

Probes of inhomogeneities

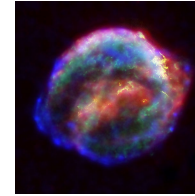


CMB
temperature
& polarisation
anisotropies

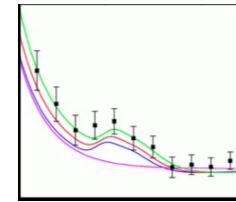


Large-scale
matter
distribution

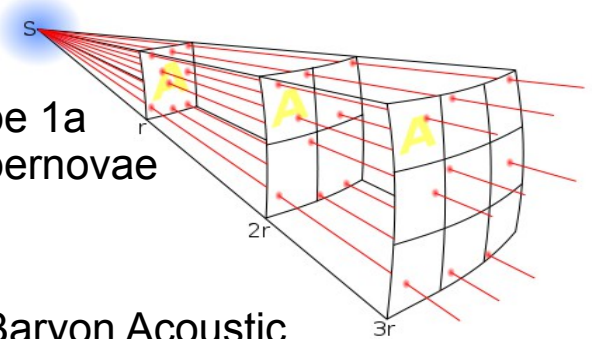
Distance vs redshift



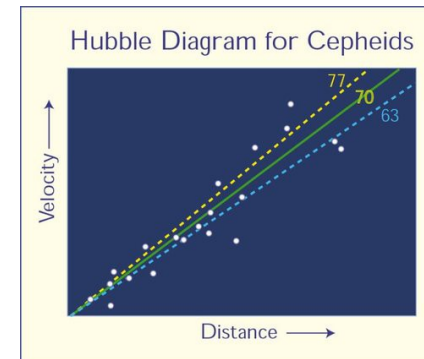
Type 1a
supernovae



Baryon Acoustic
Oscillation scale



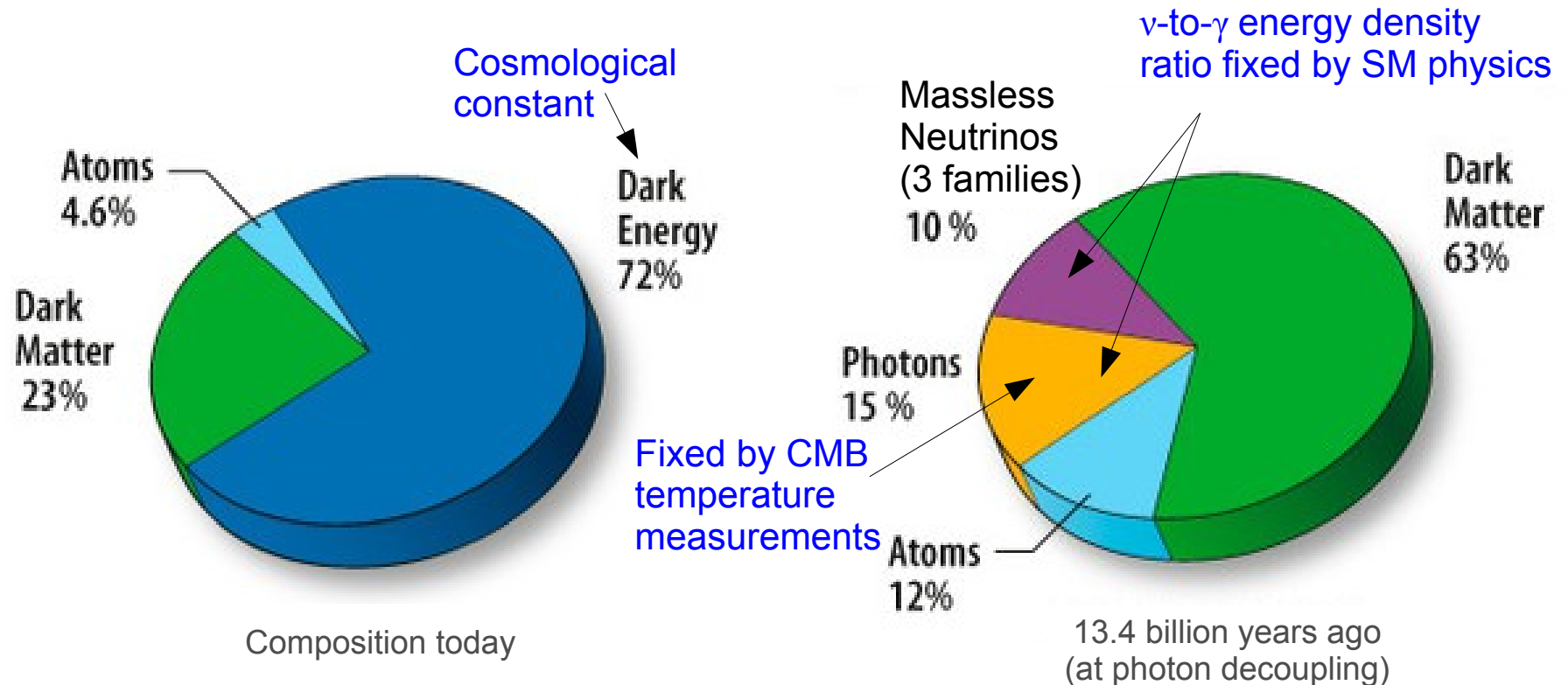
Local Hubble expansion rate



$$H_0 = 100 h \text{ km/s/Mpc} \\ = 73.8 \pm 2.4 \text{ km/s/Mpc}$$

The concordance flat Λ CDM model...

- The **simplest** model consistent with **present observations**.



Plus flat spatial geometry+initial conditions
from single-field inflation

Neutrino energy density (standard picture)...

- Neutrino decoupling at $T \sim O(1)$ MeV. ← Fixed by weak interactions

- After e^+e^- annihilation ($T \sim 0.2$ MeV):

- **Temperature:**

$$T_v = \left(\frac{4}{11} \right)^{1/3} T_\gamma$$

Assuming instantaneous decoupling

- **Number density** per flavour:

$$n_v = \frac{6}{4} \frac{\zeta(3)}{\pi^2} T_v^3 = \frac{3}{11} n_\gamma$$

Photon temperature, number density, & energy density

- **Energy density** per flavour:

$$\rho_v = \frac{7}{8} \frac{\pi^2}{15} T_v^4 = \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} \rho_\gamma$$

$$\frac{3\rho_v}{\rho_\gamma} \sim 0.68$$

- If **massive**, then at $T \ll m$: $\rho_v = m_v n_v \longrightarrow \Omega_{v,0} h^2 = \frac{m_v}{94 \text{ eV}}$

Hot dark matter (not within vanilla Λ CDM)

Extending the “neutrino” sector...

- Any particle species whose production is associated with some **thermal process** and that **decoupled while relativistic at relatively late times** [$T < O(100)$ MeV] will behave (more or less) like a neutrino as far as cosmological observations are concerned.

$$\begin{aligned} \sum_i \rho_{\nu,i} + \rho_X &= N_{\text{eff}} \left(\frac{7}{8} \frac{\pi^2}{15} T_\nu^4 \right) \\ &= (3.046 + \Delta N_{\text{eff}}) \rho_\nu^{(0)} \end{aligned}$$

Three SM neutrinos

Other light stuff:
sterile neutrinos,
eV-mass axions,
hidden photons,
etc.

Neutrino temperature per definition

Corrections due to
non-instantaneous decoupling,
finite temperature effects in the EM plasma,
and flavour oscillations

Plan...

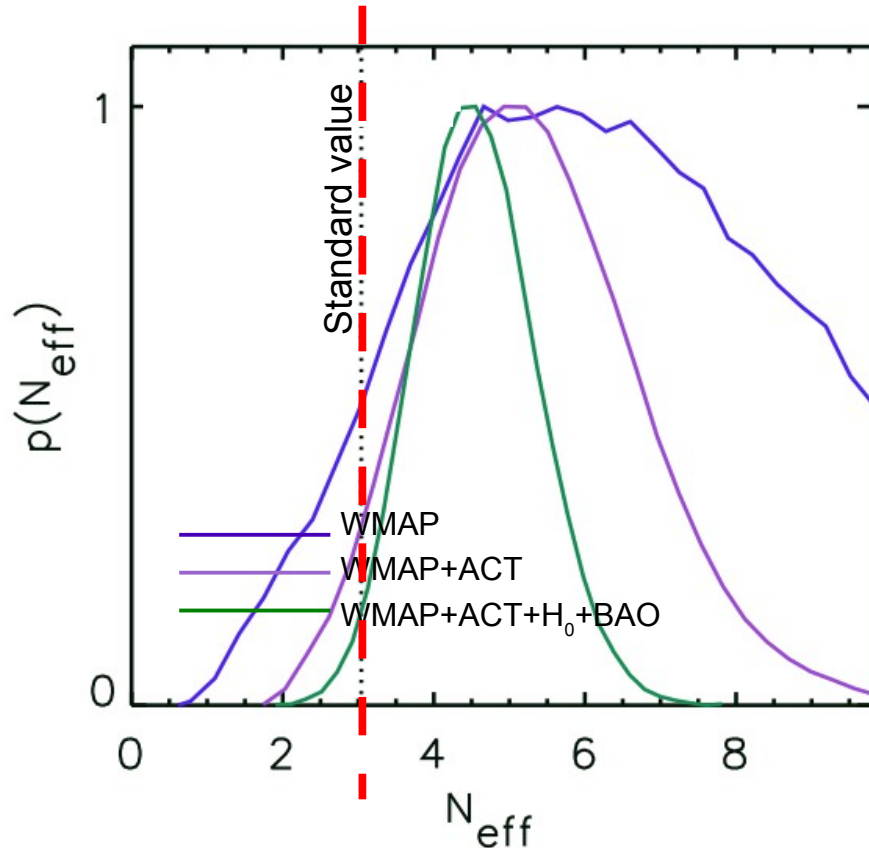
- Evidence of $N_{\text{eff}} > 3$ from **CMB and large-scale structure** observations.
- Connection to the **short baseline sterile neutrino**.

- Bonus slides: **Big bang nucleosynthesis**

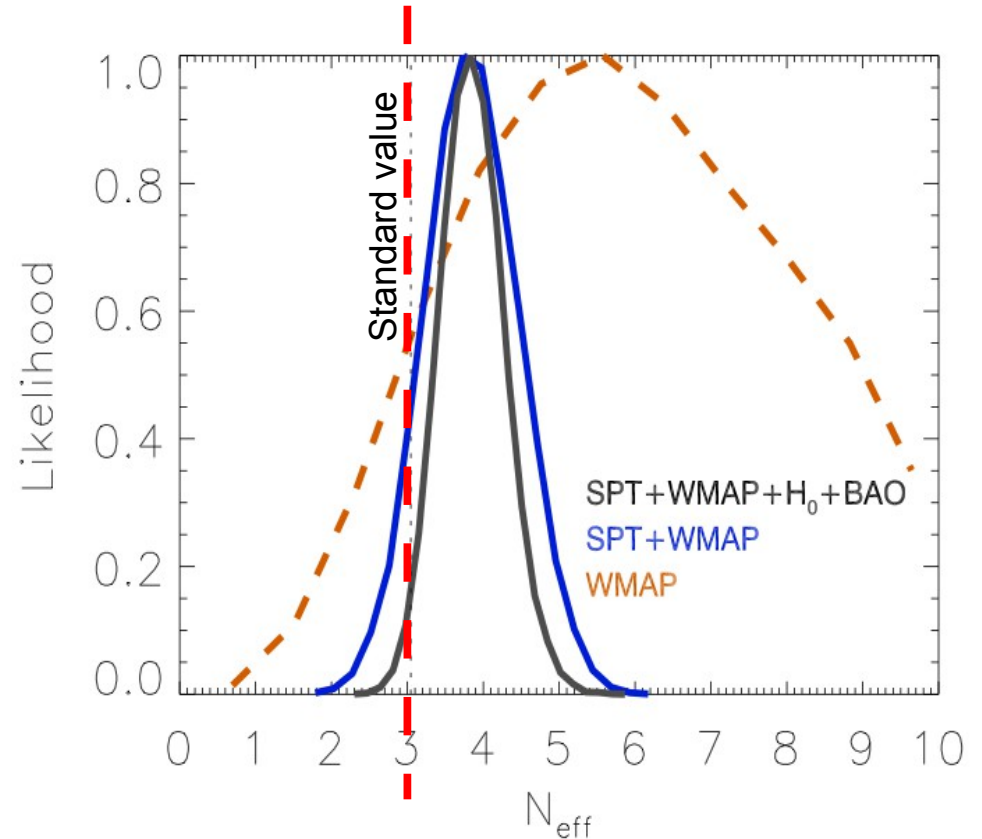
1. CMB+large-scale structure...

Evidence for $N_{\text{eff}} > 3$ from CMB+LSS...

- Recent CMB+LSS data appear to **prefer $N_{\text{eff}} > 3$** !



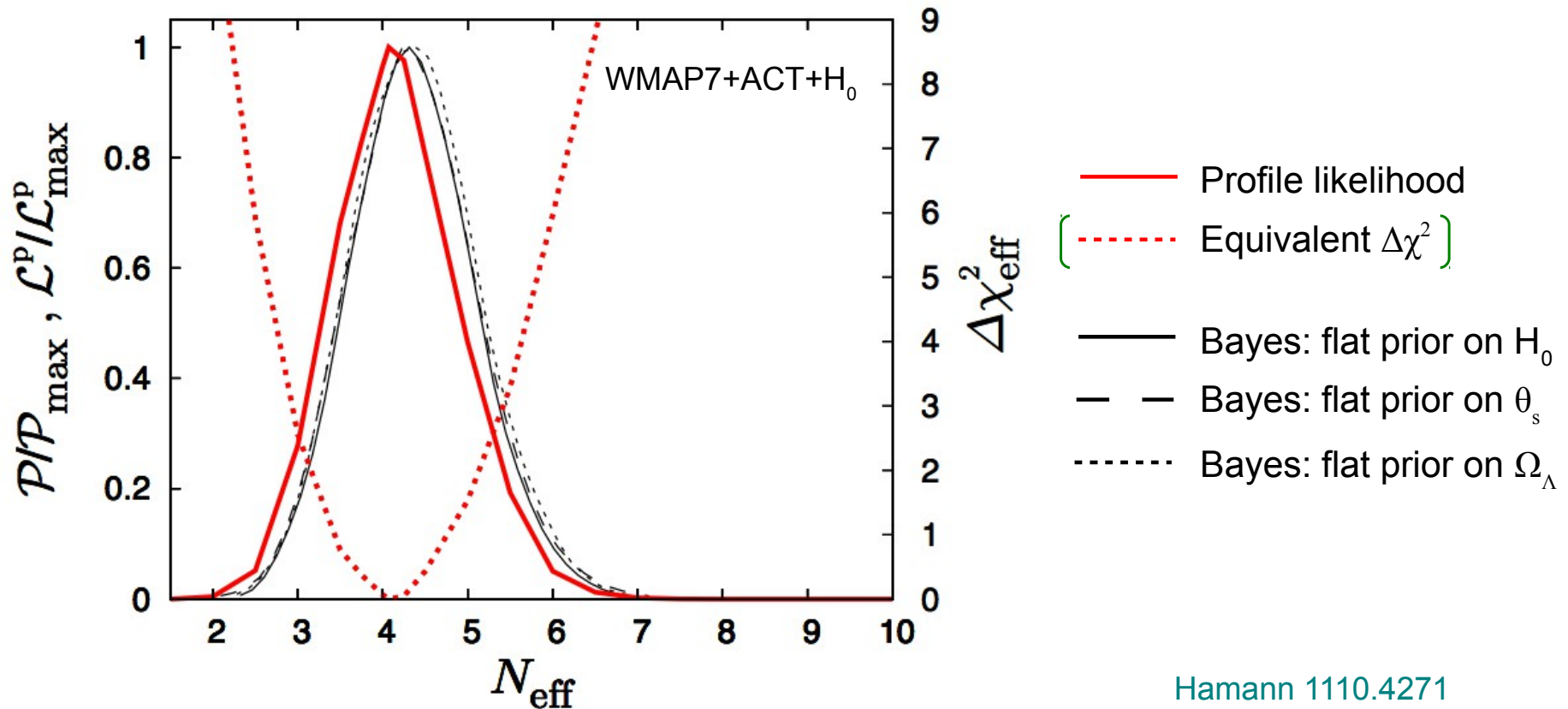
Dunkley et al. [Atacama Cosmology Telescope] 2010



Keisler et al. [South Pole Telescope] 2011

Preference for $N_{\text{eff}} > 3$ is **not** driven by priors...

- The **profile likelihood** also peaks at $N_{\text{eff}} > 3$!



Not limited to ACT, SPT...

W-7=WMAP-7

- Many model+data combinations find $N_{\text{eff}} > 3$ at 95% – 99% C.L.
 - Central value $N_{\text{eff}} \sim 4$.

Model	Data	N_{eff}
Λ CDM + N_{eff}	W-7+BAO+ H_0	$4.34^{+0.86}_{-0.88}$
	W-7+LRG+ H_0	$4.25^{+0.76}_{-0.80}$
	W-7+ACT	5.3 ± 1.3
	→ W-7+ACT+BAO+ H_0	4.56 ± 0.75
	W-7+SPT	3.85 ± 0.62
	→ W-7+SPT+BAO+ H_0	3.85 ± 0.42
	→ W-7+ACT+SPT+LRG+ H_0	$4.08^{(+0.71)}_{(-0.68)}$
	→ W-7+ACT+SPT+BAO+ H_0	3.89 ± 0.41
	W-7+CL+SPT+BAO+ H_0	(< 3.74)
$N_{\text{eff}} + f_\nu$	W-7+CMB+BAO+ H_0	$4.47^{(+1.82)}_{(-1.74)}$
	→ W-7+CMB+LRG+ H_0	$4.87^{(+1.86)}_{(-1.75)}$
$N_{\text{eff}} + \Omega_k$	W-7+BAO+ H_0	4.61 ± 0.96
	→ W-7+ACT+SPT+BAO+ H_0	4.03 ± 0.45
$N_{\text{eff}} + \Omega_k + f_\nu$	→ W-7+ACT+SPT+BAO+ H_0	4.00 ± 0.43
$N_{\text{eff}} + f_\nu + w$	W-7+CMB+BAO+ H_0	$3.68^{(+1.90)}_{(-1.84)}$
	W-7+CMB+LRG+ H_0	$4.87^{(+2.02)}_{(-2.02)}$
$N_{\text{eff}} + \Omega_k + f_\nu + w$	→ W-7+CMB+BAO+SN+ H_0	$4.2^{+1.10(+2.00)}_{-0.61(-1.14)}$
	→ W-7+CMB+LRG+SN+ H_0	$4.3^{+1.40(+2.30)}_{-0.54(-1.09)}$

→ =
>95% C.L.

Not limited to ACT, SPT...

but...

W-7=WMAP-7

- Many model+data combinations find $N_{\text{eff}} > 3$ at 95% – 99% C.L.

- Central value $N_{\text{eff}} \sim 4$.

→ =
>95% C.L.

→ = uses
cluster data

- One exception:** cluster abundance prefers a more “standard” value:

$$N_{\text{eff}} < 3.74 \text{ (95 \% C.L.)}$$

(N_{eff} restricted to ≥ 3)

Burenin & Vikhlinin 2012

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Abazajian et al., “Light sterile neutrinos: a white paper”, 2012

Essentially a WMAP result...

W-7=WMAP-7

- Data combinations are **not** independent.

- All use CMB data from WMAP.

→ Planck will provide an independent check!

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→ = uses
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How does it work...

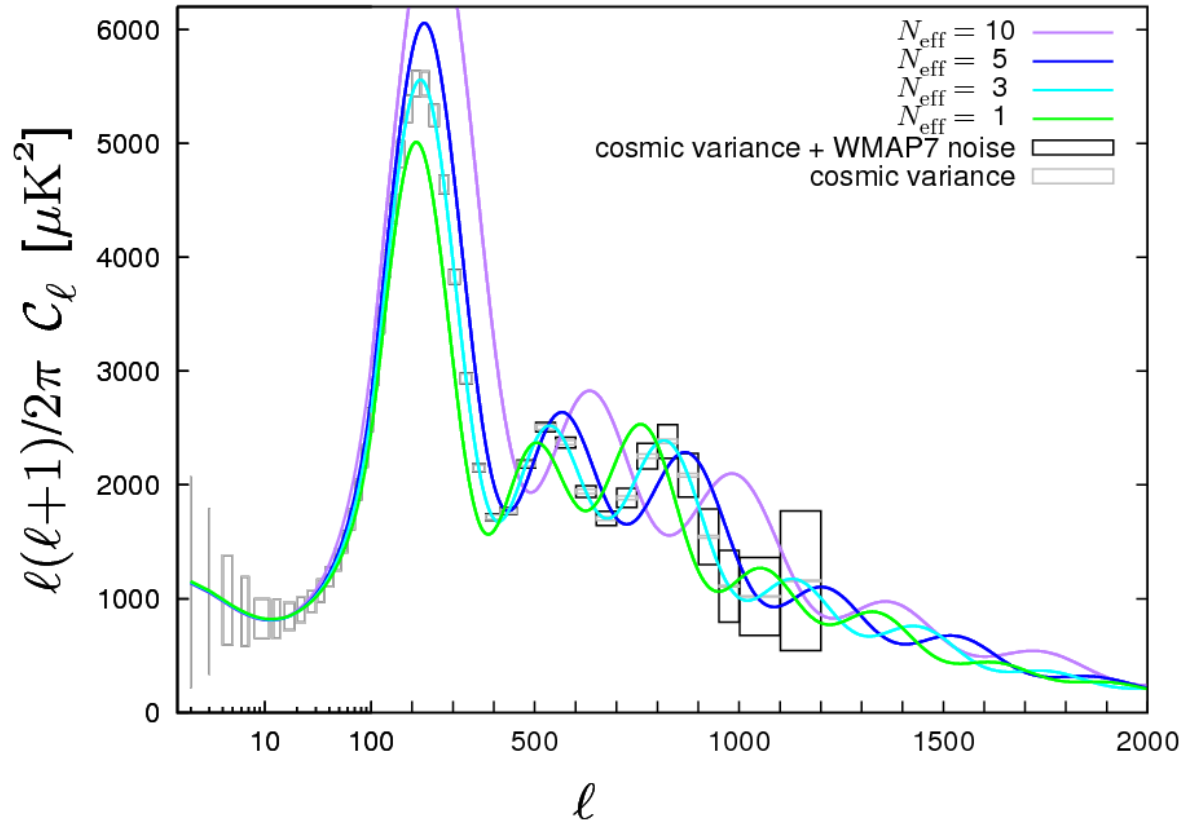
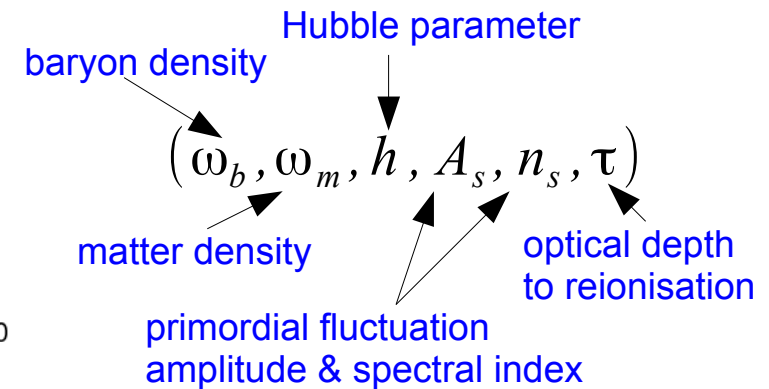


Figure courtesy of J. Hamann

- N_{eff} looks easy to detect..
- But we also use the **same data** to measure at least 6 other cosmological parameters:



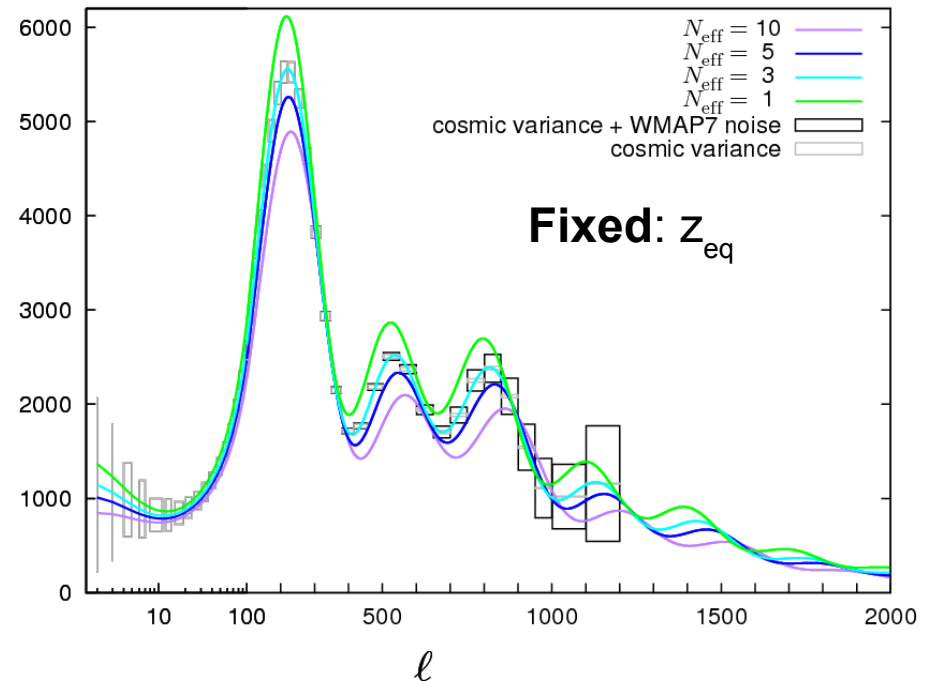
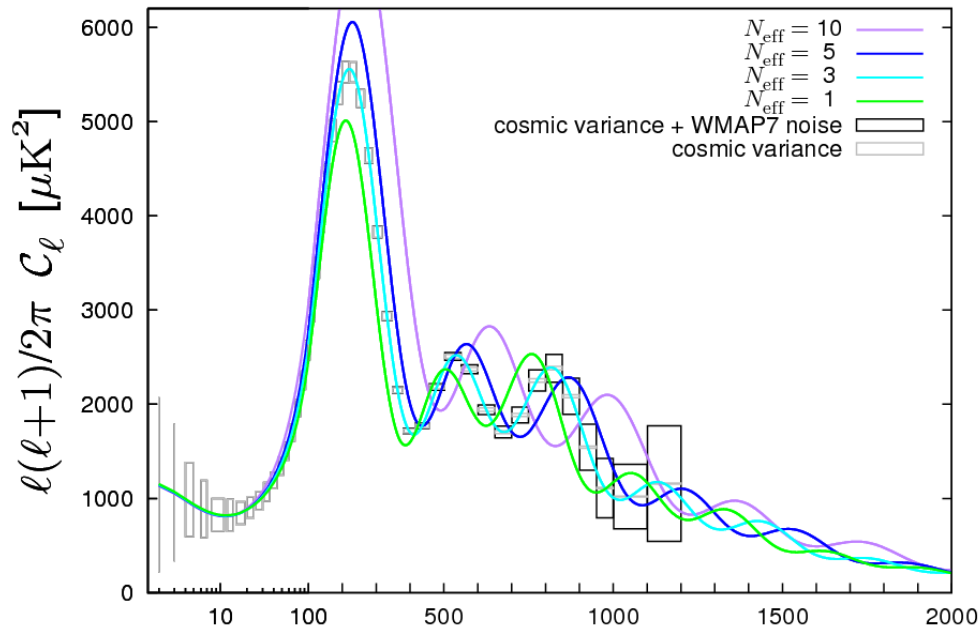
- Plenty of **parameter degeneracies!**

What the CMB really probes: equality redshift...

- Ratio of 3rd and 1st peaks sensitive to the redshift of **matter-radiation equality** via the early ISW effect.

Exact degeneracy between the physical matter density ω_m and N_{eff} .

$$1 + z_{\text{eq}} = \frac{\omega_m}{\omega_r} \frac{\omega_m}{\omega_y} \frac{1}{1 + 0.2271 N_{\text{eff}}}$$



What the CMB really probes: sound horizon...

- Peak positions depend on:

$$\theta_s = \frac{r_s}{D_A}$$

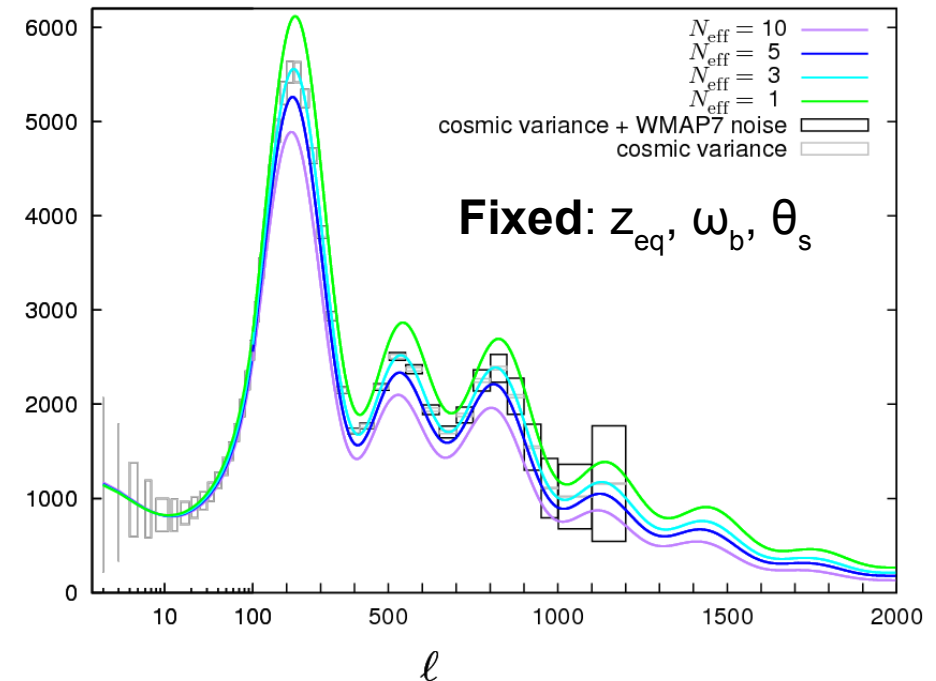
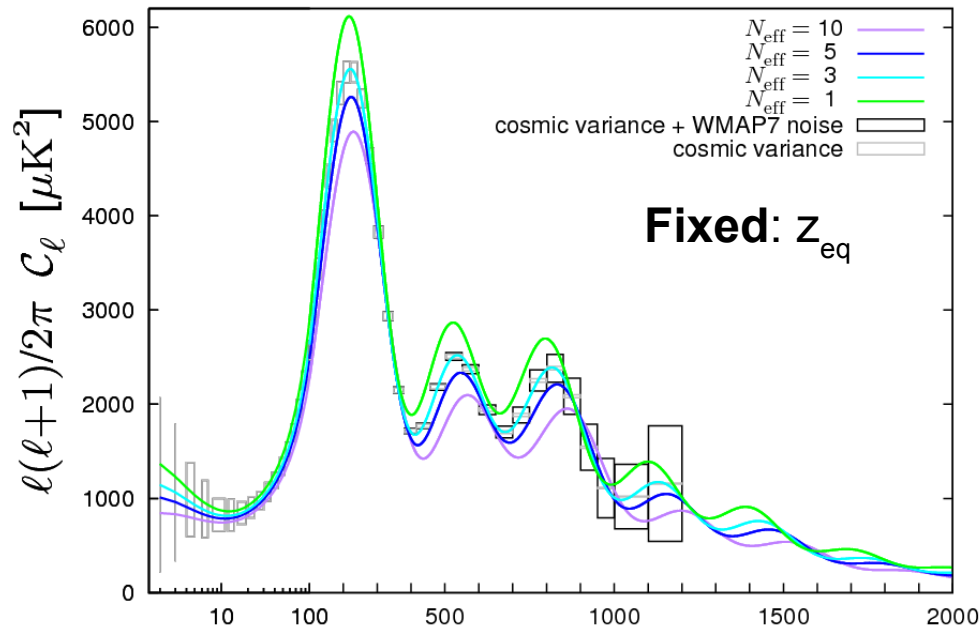
r_s ← Sound horizon at decoupling
 D_A ← Angular distance to the last scattering surface

Flat Λ CDM

Fixed z_{eq}, ω_b

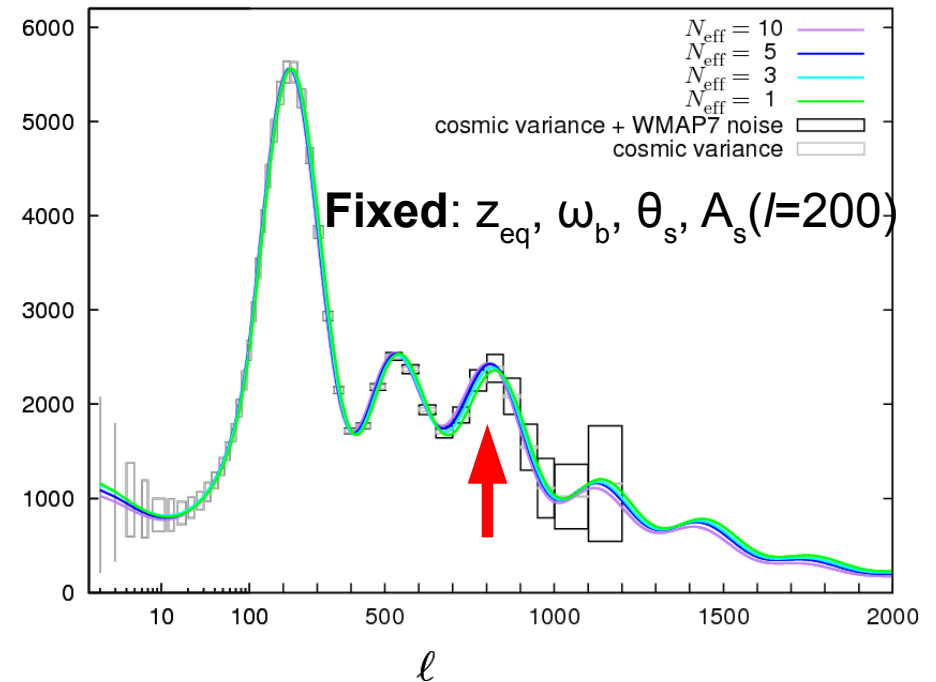
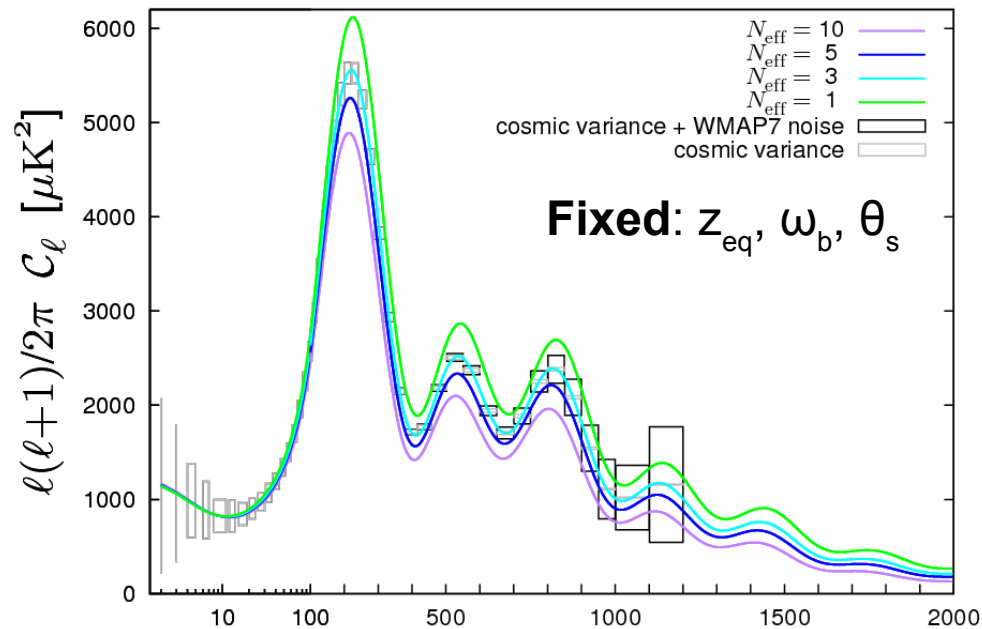
Exact degeneracy between ω_m and the Hubble parameter h .

$$\theta_s \propto \frac{(\omega_m h^{-2})^{-1/2}}{\int_{a_*}^1 \frac{da}{\sqrt{\omega_m h^{-2} a^{-3} + (1 - \omega_m h^{-2})}}}$$

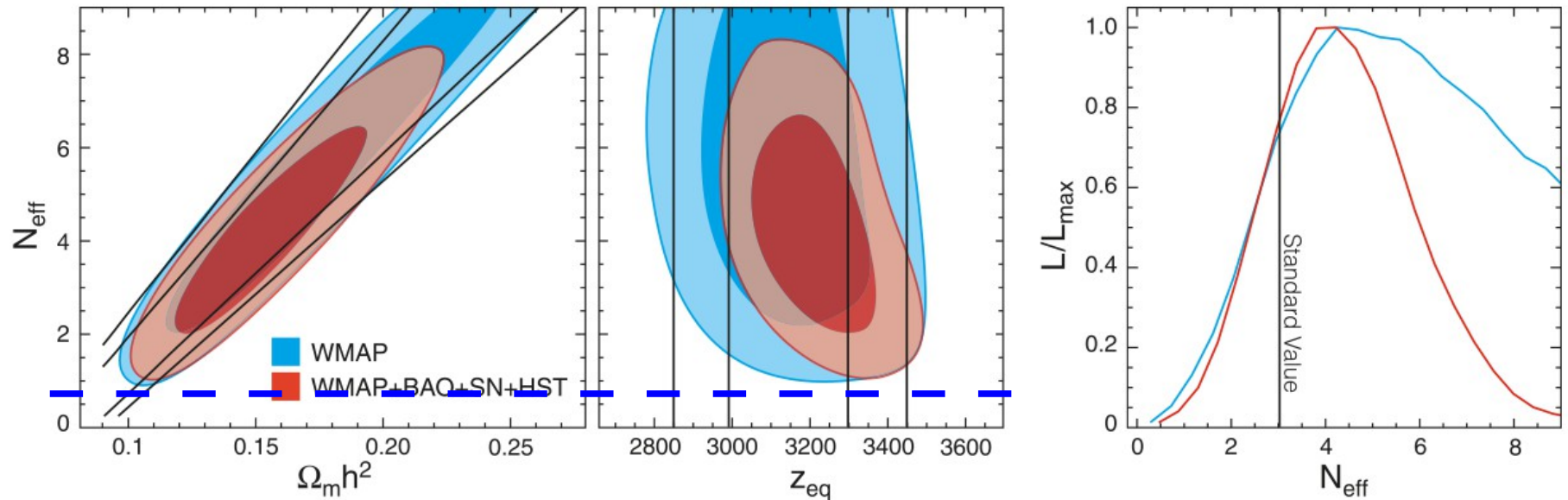


What the CMB really probes: anisotropic stress...

- Apparent (i.e., not physical) partial degeneracies with **primordial fluctuation amplitude** A_s and **spectral index** n_s .
- However, **free-streaming** particles have **anisotropic stress**.
- **First real signature of N_{eff} in the 3rd peak!**



- Measurement of the third peak (since WMAP-5) gives **lower limit on N_{eff} from WMAP alone** (without supplementary large-scale structure data).

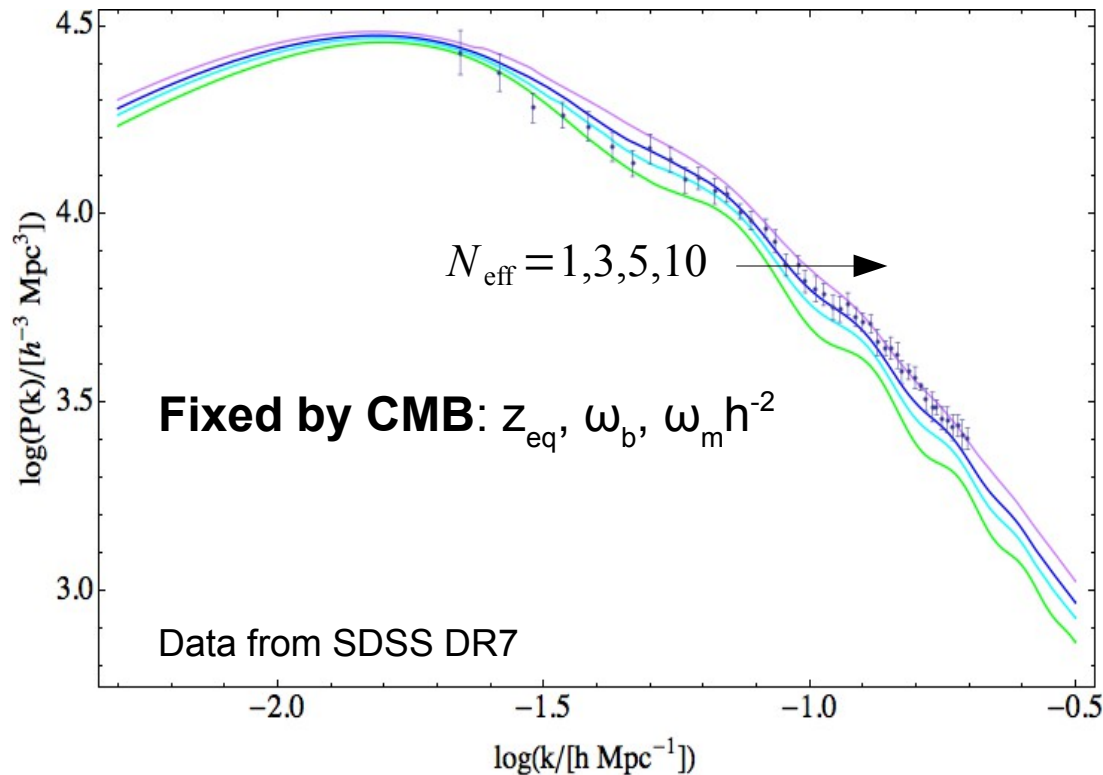


Komatsu et al. [WMAP5] 2008

- Upper limit** requires combination of WMAP with other observations to break the remaining $N_{\text{eff}}-\omega_m-h$ **parameter degeneracies**.
 - Pinning down either ω_m or h will do!
 - from local ($z < 0.1$) expansion rate measurements

Breaking degeneracies with large-scale structure...

Large-scale matter power spectrum



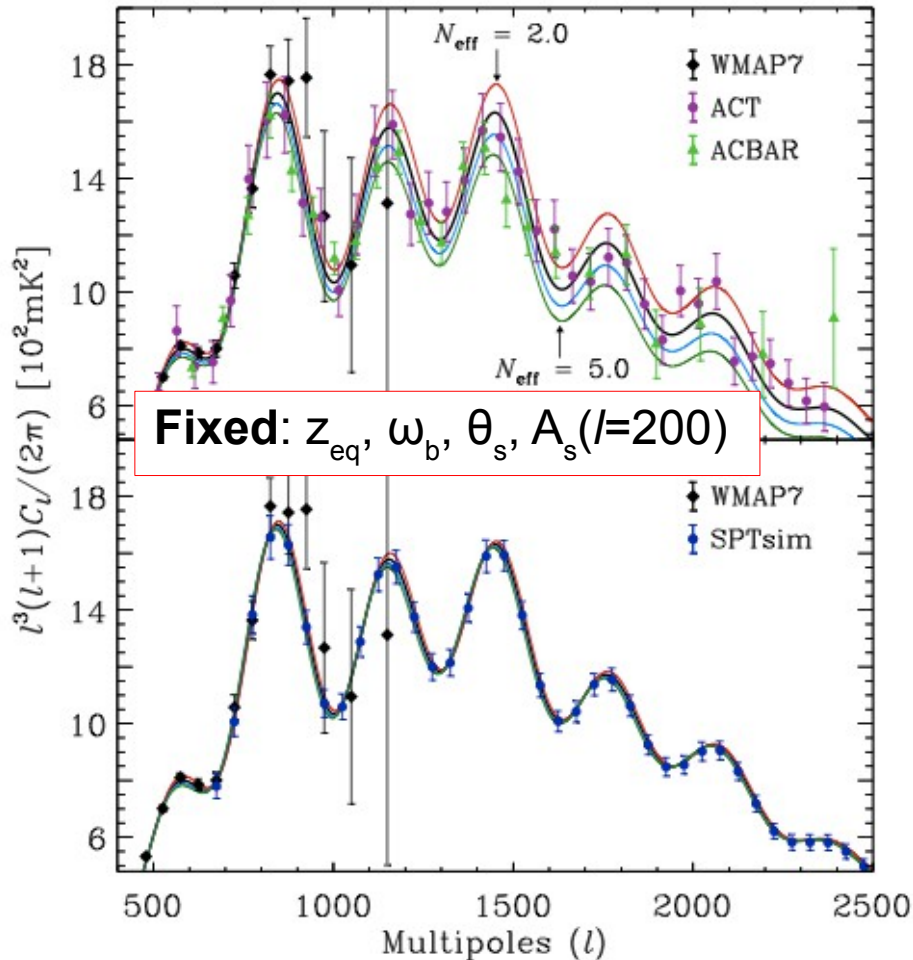
- The **shape** of the matter power spectrum is additionally sensitive to the **baryon fraction**:

$$f_b \equiv \frac{\omega_b}{\omega_m}$$

Fixed by CMB

- The **larger** N_{eff} , the **smaller** $f_b \rightarrow$ more power at large k .
- (Can partially offset this effect with **massive neutrinos**.)

Breaking degeneracies with the CMB damping tail...



- **ACT** data available since 2010; **SPT** since 2011; also measured by **Planck**.

- Probe **photon diffusion scale**:

$$\theta_d = \frac{r_d}{D_A} \quad \leftarrow \text{Diffusion scale at decoupling}$$

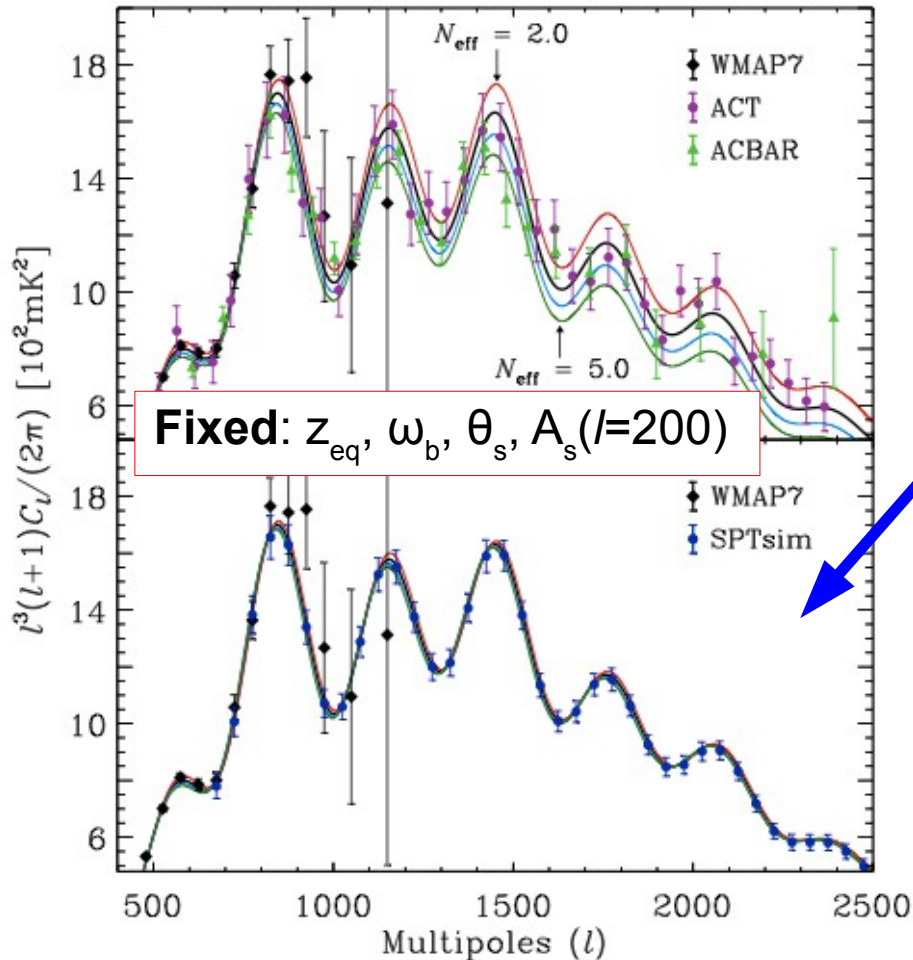
- Combined with **sound horizon measurement**:

$$\frac{\theta_d}{\theta_s} = \frac{r_d}{r_s} \propto \omega_m^{1/4}$$

Fixed z_{eq}, ω_b

Breaks (nearly) all N_{eff} degeneracies, robust against low-redshift uncertainties in D_A , e.g., w_{DE}, Ω_k .

Breaking degeneracies with the CMB damping tail...



- **The $N_{\text{eff}} - Y_p$ degeneracy!**
- With ω_b fixed by WMAP, the **Helium fraction** Y_p determines the **free electron density** → affects **photon diffusion length**.
- Current strategy:
 - Either fix Y_p at 0.24 → 0.25.
 - Or apply a BBN consistency relation.
- **Not** an exact degeneracy; can be resolved by **Planck**.

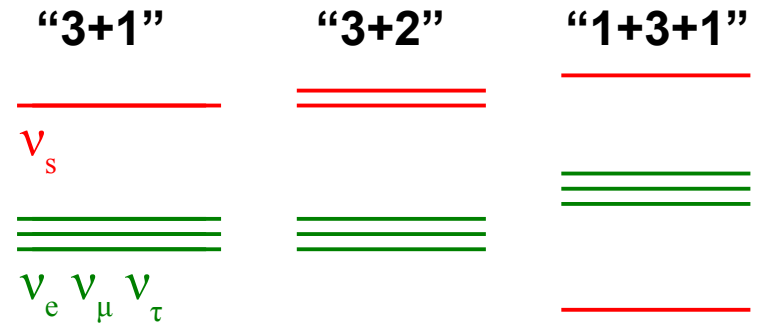
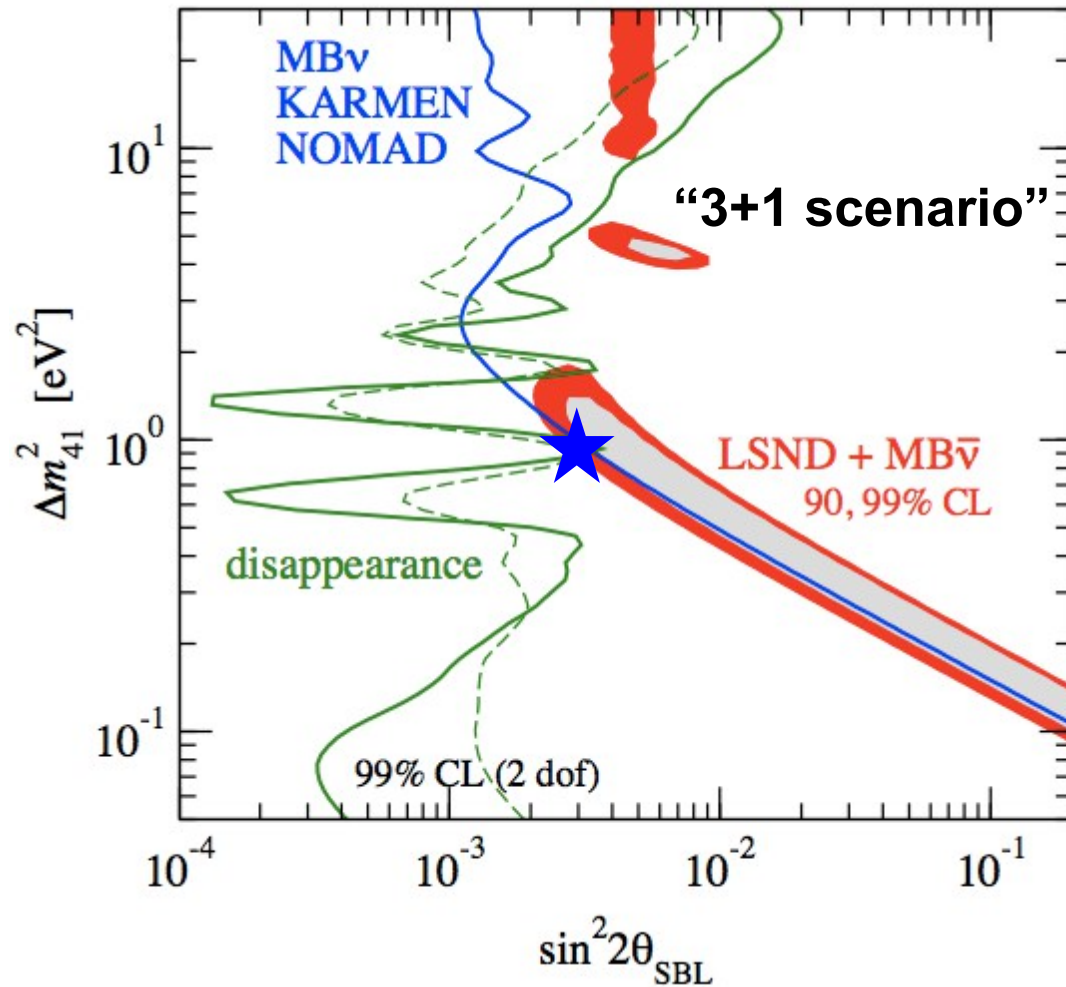
A quick recap on N_{eff} ...

- The WMAP measurement of the **acoustic peaks alone** does **not** completely constrain N_{eff} because of **parameter degeneracies**:
 - $N_{\text{eff}} - \omega_m$
 - $N_{\text{eff}} - h$ (via $\omega_m - h$ and $N_{\text{eff}} - \omega_m$)
 - $N_{\text{eff}} - Y_p$
- Degeneracies can be **broken** with measurements of
 - CMB damping tail $\longrightarrow \omega_m$ (Y_p with Planck)
 - Large-scale structure distribution $\longrightarrow \omega_m$
 - Local Hubble expansion rate $\longrightarrow h$
- Preference for $N_{\text{eff}} > 3$ appears to be robust against model assumptions.

2. Connection to the short baseline sterile neutrino...

Experimental anomalies & the sterile ν interpretation...

- Experiments **at odds** with the standard **3-neutrino interpretation** of global neutrino oscillation data:
 - **LSND** ($\bar{\nu}_e$ appearance)
 - **MiniBooNE** anti-neutrinos ($\bar{\nu}_e$ appearance)
 - **Short baseline reactor experiments** (re-evaluation of neutrino fluxes) ($\bar{\nu}_e$ disappearance)
- If interpreted as oscillation signals \rightarrow a 4th (or more) **sterile neutrino** with $\Delta m^2 \sim \mathcal{O}(1 \text{ eV}^2)$ and $\sin^2 2\theta > 10^{-3}$.



- “3+1” best-fit: $\Delta m_{41}^2 \sim 1 \text{ eV}^2$

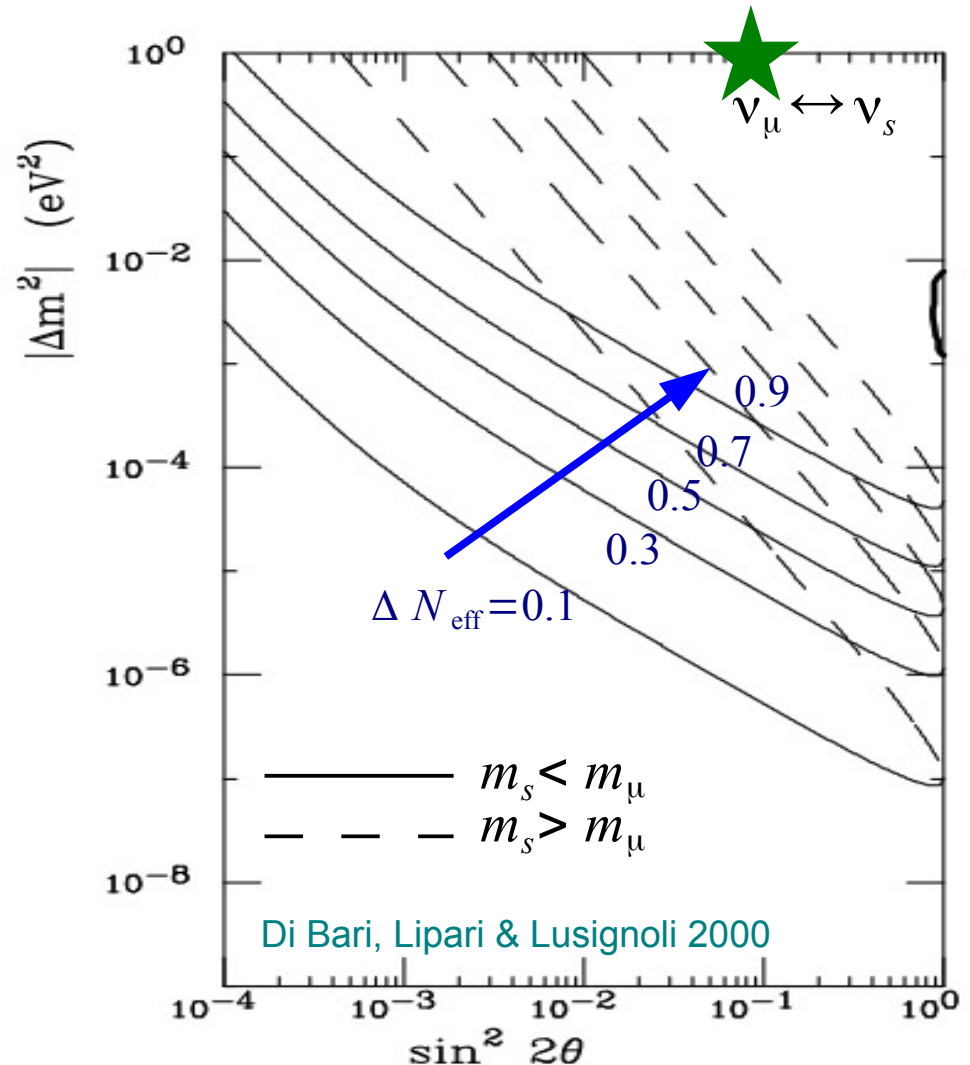


$$m_s \sim 1 \text{ eV}$$

If lightest neutrino mass $\sim 0 \text{ eV}$

Light sterile neutrinos and N_{eff} ...

- SBL-preferred Δm^2 and mixing favour the **production and thermalisation** of sterile neutrinos in the early universe via $\nu_\alpha \leftrightarrow \nu_s$ **oscillations** + ν_α **scattering**.
- Can easily produce an **excess** relativistic energy density of $\Delta N_{\text{eff}} \sim 1$.
- Sterile states have the **same temperature** as the SM neutrinos.

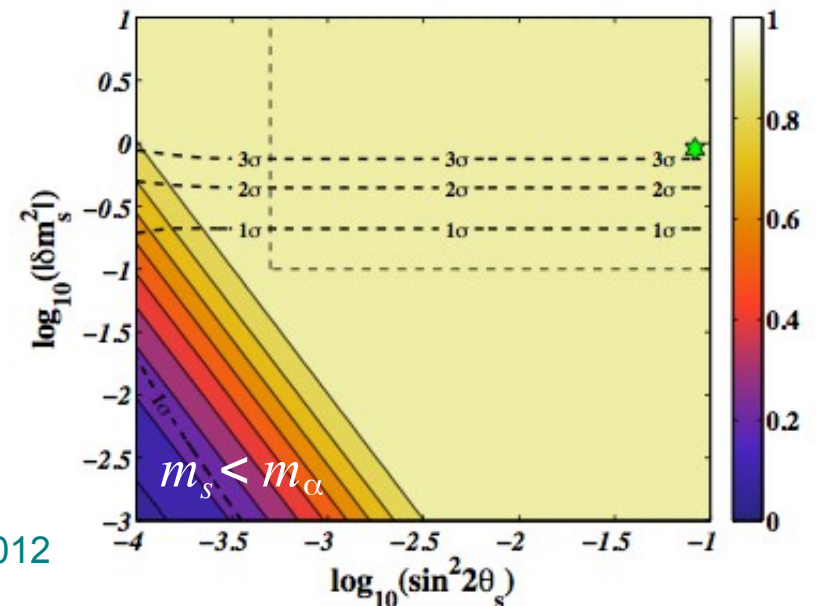
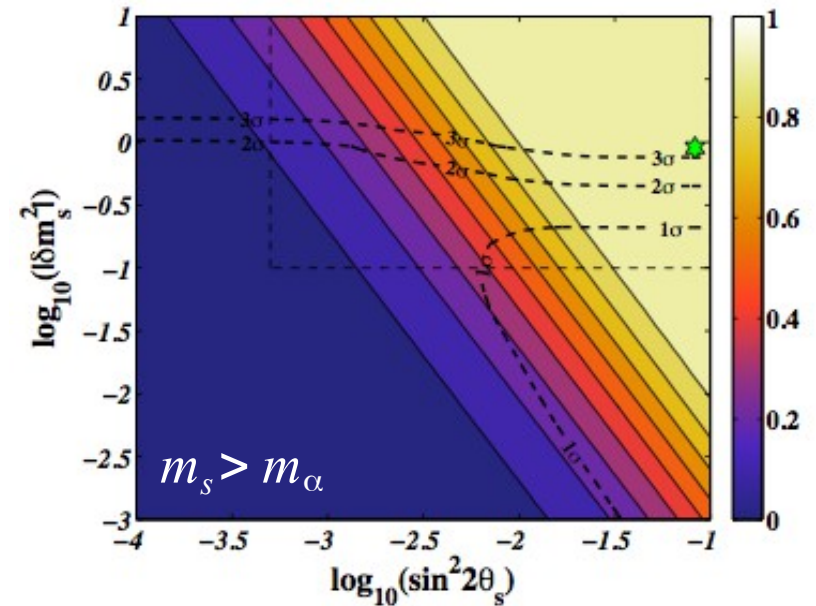


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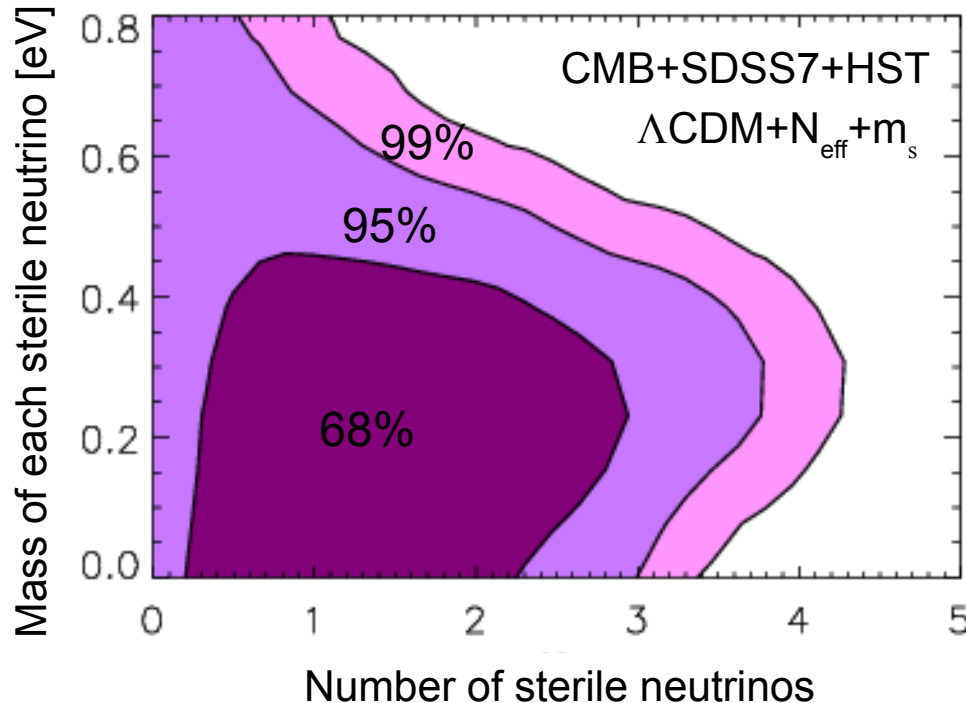
→ Can easily produce an **excess** relativistic energy density of $\Delta N_{\text{eff}} \sim 1$.

→ Sterile states have the **same temperature** as the SM neutrinos.



Can the short baseline sterile neutrino explain $N_{\text{eff}} > 3$?

- **Short answer:** Not so easy.
- **Reason:** eV mass neutrinos **violate CMB+LSS hot dark matter bounds**.



- 3+1 thermalised sterile:
 $m_s < 0.48 \text{ eV}$ (95% C.I.)

Lab best-fit: $m_s \sim 1 \text{ eV}$

- 3+2 thermalised sterile:
 $m_{s1} + m_{s2} < 0.9 \text{ eV}$ (95% C.I.)

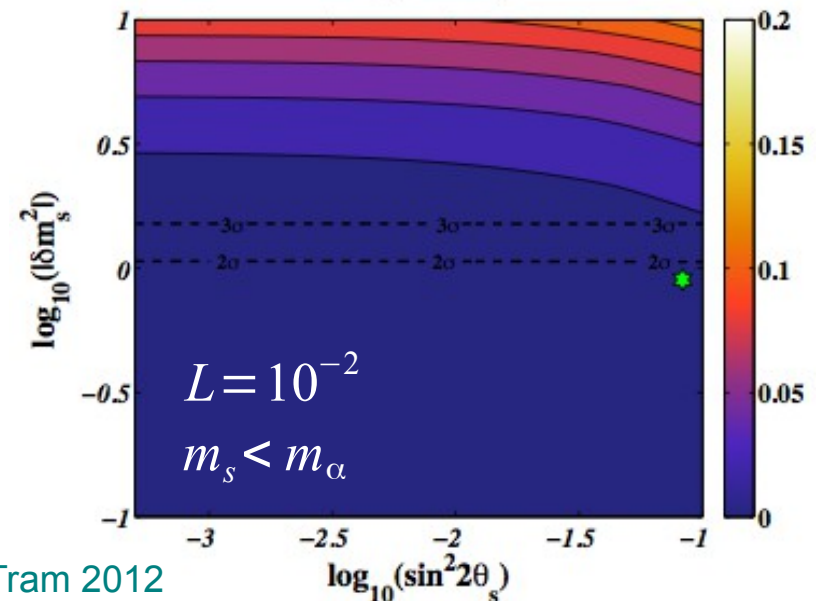
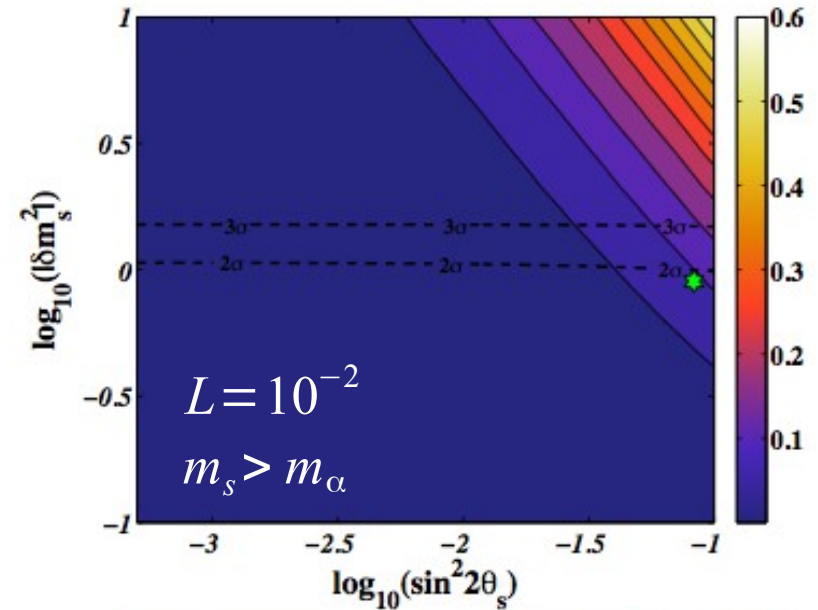
Lab best-fit: $m_{s1} \sim 0.7 \text{ eV}$, $m_{s2} \sim 0.9 \text{ eV}$

Is there a way out? Plan A...

- **Suppress** sterile neutrino thermalisation using, e.g., **a large lepton asymmetry** ($L \gg B \sim 10^{-10}$).

Foot & Volkas 1995

- Generating a large lepton asymmetry requires **new physics**.
- If complete suppression, then $N_{\text{eff}} > 3$ must be explained by some **other physics** (sub-eV thermal axions, hidden photons, etc.?)



Hannestad, Tamborra & Tram 2012

Grin, Smith, and Kamionkowski, Axion constraints in non-standard thermal histories, arXiv:0711.1352 [astro-ph]; **Kawasaki, Nakayama, and Senami**, Cosmological implications of supersymmetric axion models, arXiv:0711.3083 [hep-ph]; **Feng, Tu and Yu**, Thermal Relics in Hidden Sectors, arXiv:0808.2318 [hep-ph]; **Nelson and Walsh**, Chameleon vector bosons, arXiv:0802.0762 [hep-ph]; **Ackermann, Buckley, Carroll, and Kamionkowski**, Dark Matter and Dark Radiation, arXiv:0810.5126 [hep-ph]; **Mahato**, Torsion, Dirac Field, Dark Matter and Dark Radiation, gr-qc/0603134; **Jäckel, Redondo, and Ringwald**, Signatures of a hidden cosmic microwave background, arXiv:0804.4157 [astro-ph]; **Hasenkamp**, Dark radiation from the axino solution of the gravitino problem, arXiv:1107.4319 [hep-ph]; **Kobayashi, Takahashi, Takahashi, and Yamaguchi**, Dark Radiation from Modulated Reheating, arXiv:1111.1336 [astro-ph.CO]; **Feng, Rentala and Surujon**, WIMPless Dark Matter from an AMSB Hidden Sector with No New Mass Parameters, arXiv:1111.4479 [hep-ph]; **Hooper, Queiroz, and Gnedin**, Non-Thermal Dark Matter Mimicking An Additional Neutrino Species In The Early Universe, arXiv:1111.6599 [astro-ph.CO]; **Menestrina and Scherrer**, Dark Radiation from Particle Decays during Big Bang Nucleosynthesis, arXiv:1111.0605 [astro-ph.CO]; Aslanbeigi, **Robbers, Foster, Kohri, and Afshordi**, Phenomenology of Gravitational Aether as a solution to the Old Cosmological Constant Problem, arXiv:1106.3955 [astro-ph.CO]; **Chen and Lin**, Cosmon as the Modulon: Non-Gaussianity from Dark Energy, arXiv:1104.0982 [hep-ph]; **Das and Weiner**, Late Forming Dark Matter in Theories of Neutrino Dark Energy, astro-ph/0611353; **Nakayama, Takahashi, and Yanagida**, A theory of extra radiation in the Universe, arXiv:1010.5693 [hep-ph]; **Fischler and Meyers**, Dark Radiation Emerging After Big Bang Nucleosynthesis?, arXiv:1011.3501 [astro-ph.CO]; **Dreiner, Hanussek, Kim, and Sarkar**, Gravitino cosmology with a very light neutralino, arXiv:1111.5715 [hep-ph]; **Foot**, Mirror dark matter cosmology – predictions for Neff[CMB] and Neff[BBN], arXiv:1111.6366 [astro-ph.CO]; **Jeong and Takahashi**, Light Higgsino from Axion Dark Radiation, arXiv:1201.4816 [hep-ph]; **Kaplan, Krnjaic, Rehermann, and Wells**, Dark Atoms: Asymmetry and Direct Detection, arXiv:1105.2073 [hep-ph]; **Cicoli**, Large extra dimensions and light hidden photons from anisotropic string vacua, arXiv:1111.0790 [hep-th];

Is there a way out? Plan B...

- Failing to suppress ν_s thermalisation, exploit **parameter degeneracies** in the CMB+LSS to **engineer a good fit**.
- No room for play within the Λ CDM model, but **extensions of Λ CDM** can help to **relax** the hot dark matter constraint on m_s :
 - Non-standard dark energy equation of state.
 - Modified gravity.
 - Non-flat spatial geometry.
 - Even more massless degrees of freedom.
 - ...

Elgarøy & Kristiansen 2011; Hamann, Hannestad, Raffelt & Y³W 2011
Giusarma et al. 2012; Motohashi, Starobinsky & Yokoyama 2012;
Joudaki, Abazajian & Kaplinghat 2012

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 - ...

1 x 1 eV sterile neutrino
can be reasonably
accommodated.

1 x 2eV or 2 x 1 eV is
still problematic...

Is there a way out? Plan B...

Modified gravity scenario to explain accelerated expansion in lieu of dark energy

- **An example:** accommodating 1eV sterile neutrinos with $f(R)$ gravity:

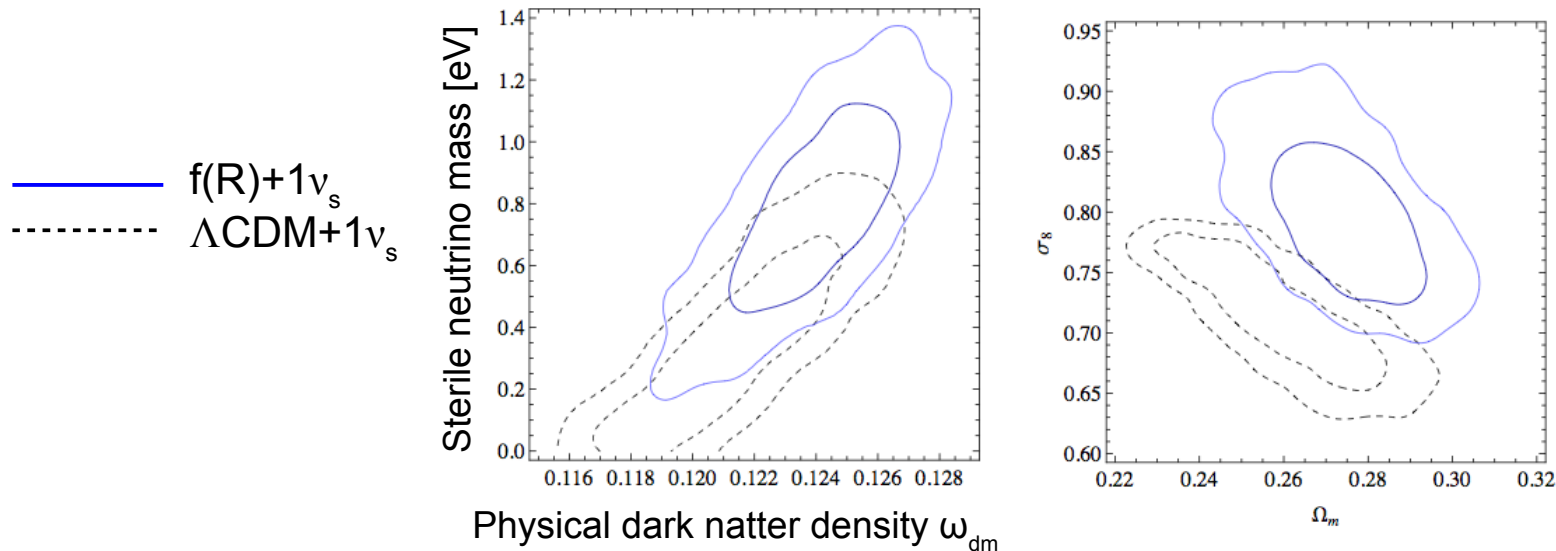
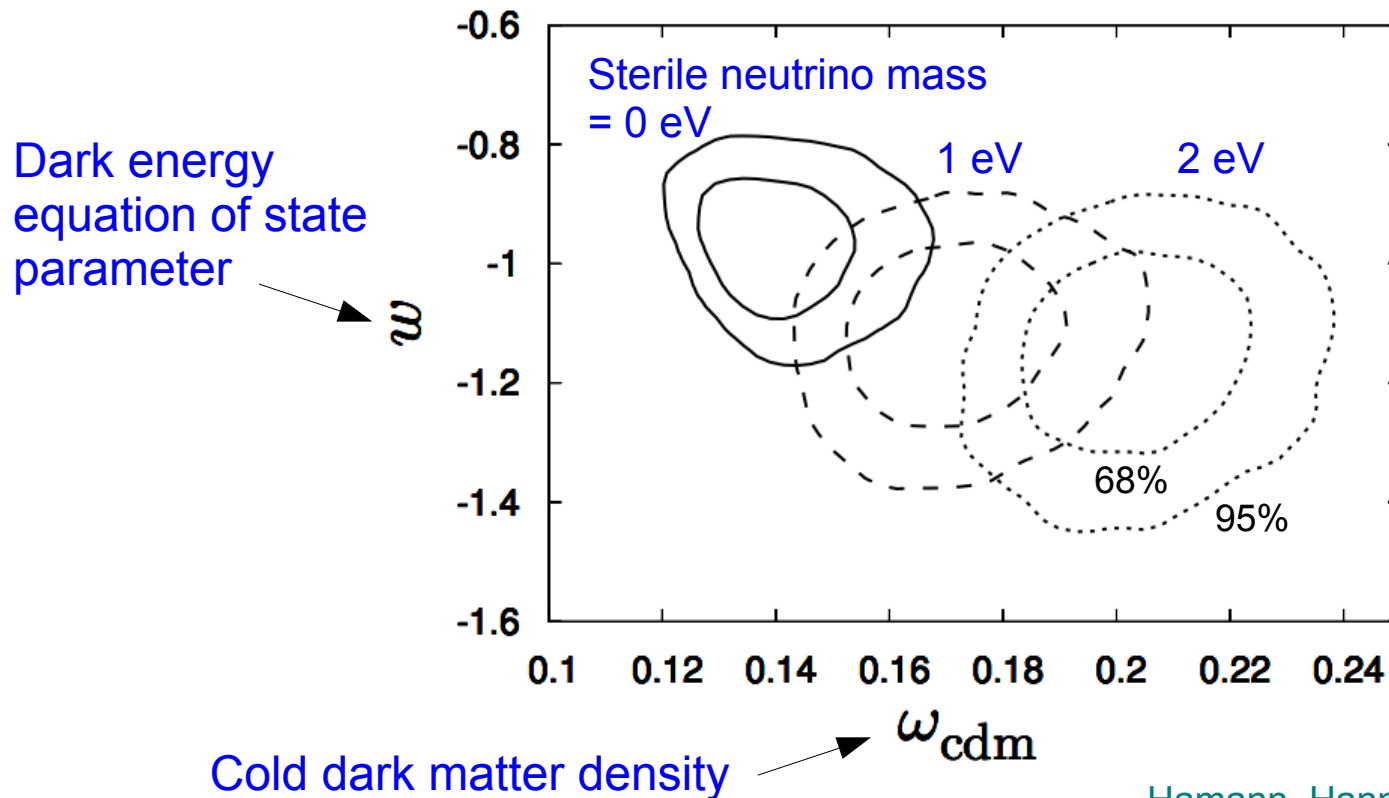


FIG. 1: 1 and 2σ contours of the sterile neutrino mass (left) and σ_8 (right) for the cases with three massless and one massive neutrinos in the Λ CDM model (dashed black) and $f(R)$ gravity (solid blue). $\chi^2_{\text{eff}} = 3774.1$ and 3767.0, respectively.

Necessary side effects...

- Exploiting parameter degeneracies also implies that other (unrelated) cosmological parameter values will change.



Planck and N_{eff} ...

- If N_{eff} is as large as 4, it will be settled **almost immediately** by Planck (launched May 14, 2009; public data release early 2013).

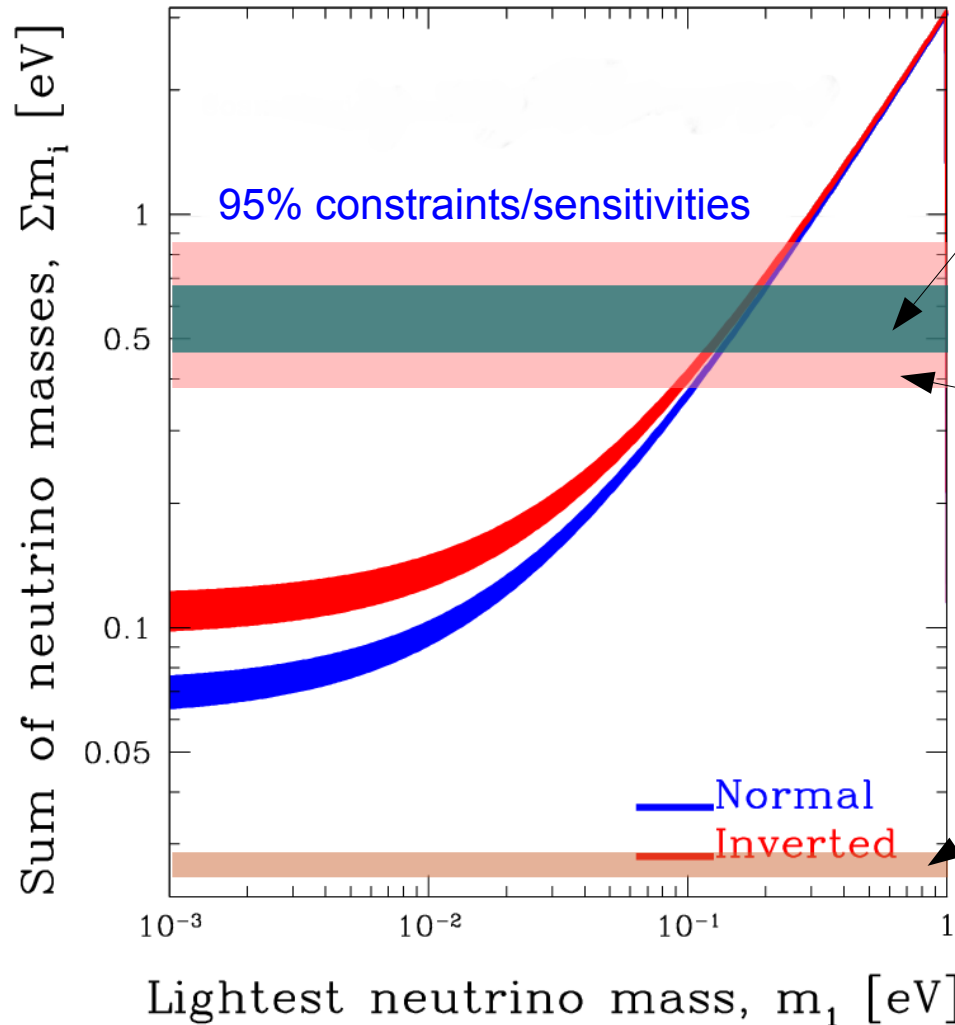
68% sensitivities

Experiment	f_{sky}	θ_b	$w_T^{-1/2}$ [μ K']	$w_P^{-1/2}$ [μ K']	ΔN_ν TT	ΔN_ν TT+TE+EE	ΔN_ν (free Y) TT+TE+EE
Planck	0.8	7'	40	56	0.6	<u>0.20</u>	<u>0.24</u>
ACT	0.01	1.7'	3	4	1	0.47	0.9
ACT + Planck					0.4	0.18	0.24
CMBPOL	0.8	4'	1	1.4	0.12	0.05	0.09

Bashinsky & Seljak 2004

Helium fraction
as a free parameter

Planck and neutrino mass...



Current constraints

Band = model complexity

Planck alone (1 year) **2013**
(+ current LSS probes → not much improvement)

Perotto et al. 2006

Not quite good enough to
rule in or rule out 1 eV
sterile neutrinos
definitively...

Planck+Euclid (lensing+galaxy clustering)
~ **2025**

Hamann, Hannestad & Y³W 2012

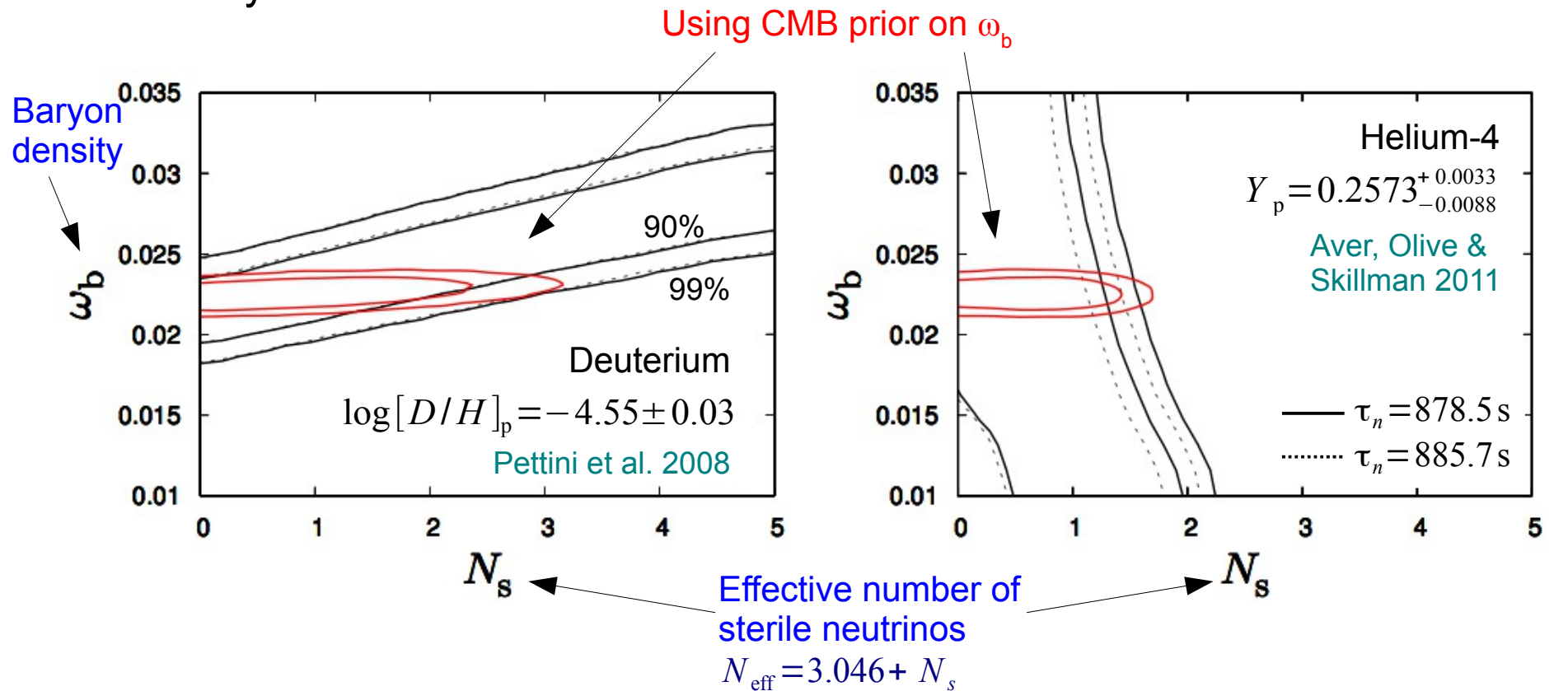
Summary...

- Current precision cosmological data show a preference for extra **relativistic degrees of freedom** (beyond 3 neutrinos).
- **Sterile neutrino** interpretation of short baseline neutrino anomalies does not quite fit into the simplest picture though...
 - 3+2: **Too many** for BBN
 - 3+1, 3+2: **Too heavy** for CMB/LSS
- Non-trivial **extensions to Λ CDM** can reasonably accommodate 1 x 1 eV fully thermalised sterile neutrino species.
- **Planck with tell** (at least part of the story).

3. Extra slides: BBN

Evidence for $N_{\text{eff}} > 3$ from BBN...

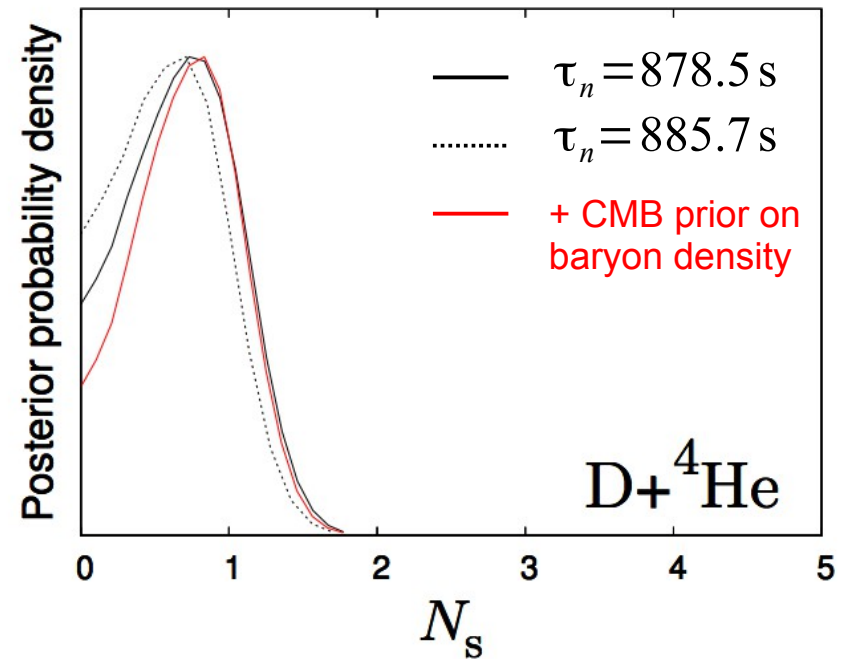
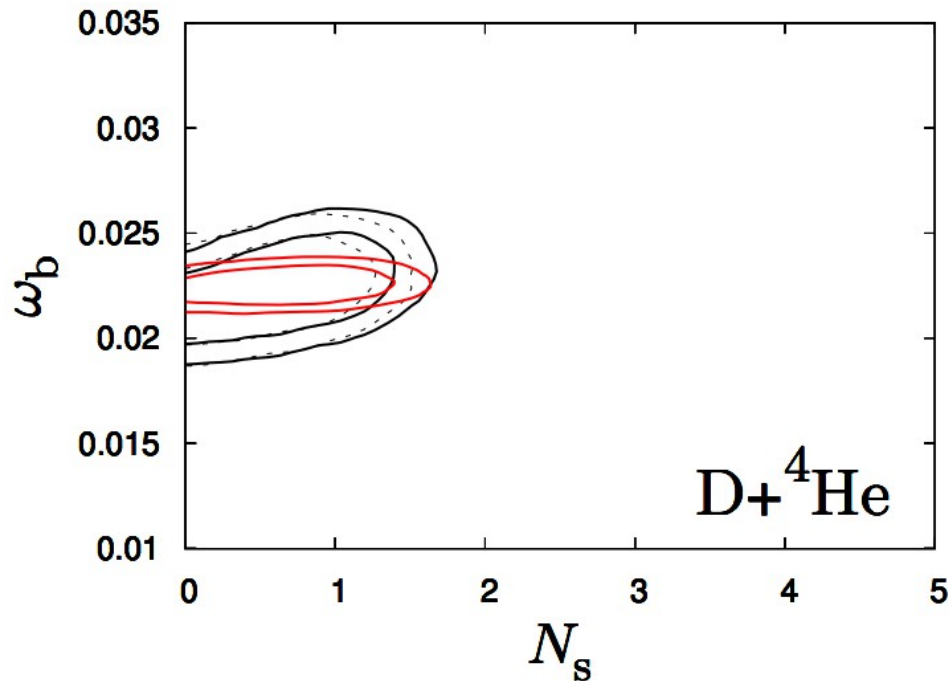
- Light element abundances are sensitive to excess relativistic energy density.



Hamann, Hannestad, Raffelt & Y³W 2011

Evidence for $N_{\text{eff}} > 3$ from BBN...

- Mild preference for $N_{\text{eff}} > 3$ (or $N_s > 0$) from Deuterium+Helium-4.
- But $N_s = 2$ is **strongly disfavoured**.



Quick fix: degenerate BBN...

- Introduce a **neutrino chemical potential** (= $O(0.1)$ **lepton asymmetry**).
- Then even $N_s = 3$ is **allowed** by BBN.

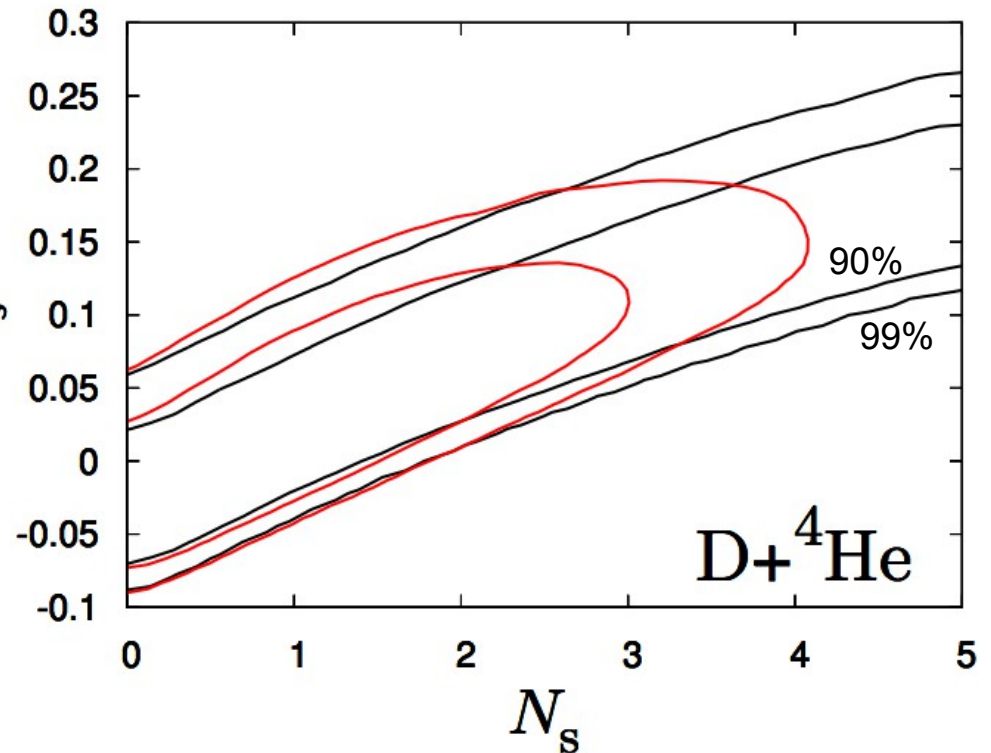
Lepton asymmetry

$$L \equiv \frac{n_{\nu_\alpha} - n_{\bar{\nu}_\alpha}}{n_\gamma}$$

$$= \frac{1}{12\zeta(3)} \left(\frac{T_\nu}{T_\gamma} \right)^3 (\pi^2 \xi + \xi^3)$$

Neutrino chemical potential

ξ



Question: How to simultaneously get $L = O(0.1)$ and $B = O(10^{-10})$?