



**The Abdus Salam
International Centre for Theoretical Physics**



2400-6

Workshop on Strongly Coupled Physics Beyond the Standard Model

25 - 27 January 2012

The 4D Composite Higgs

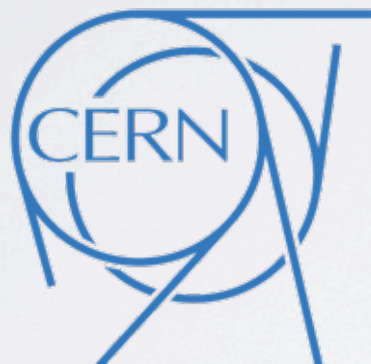
Michele Redi

INFN Florence/CERN

ITALY

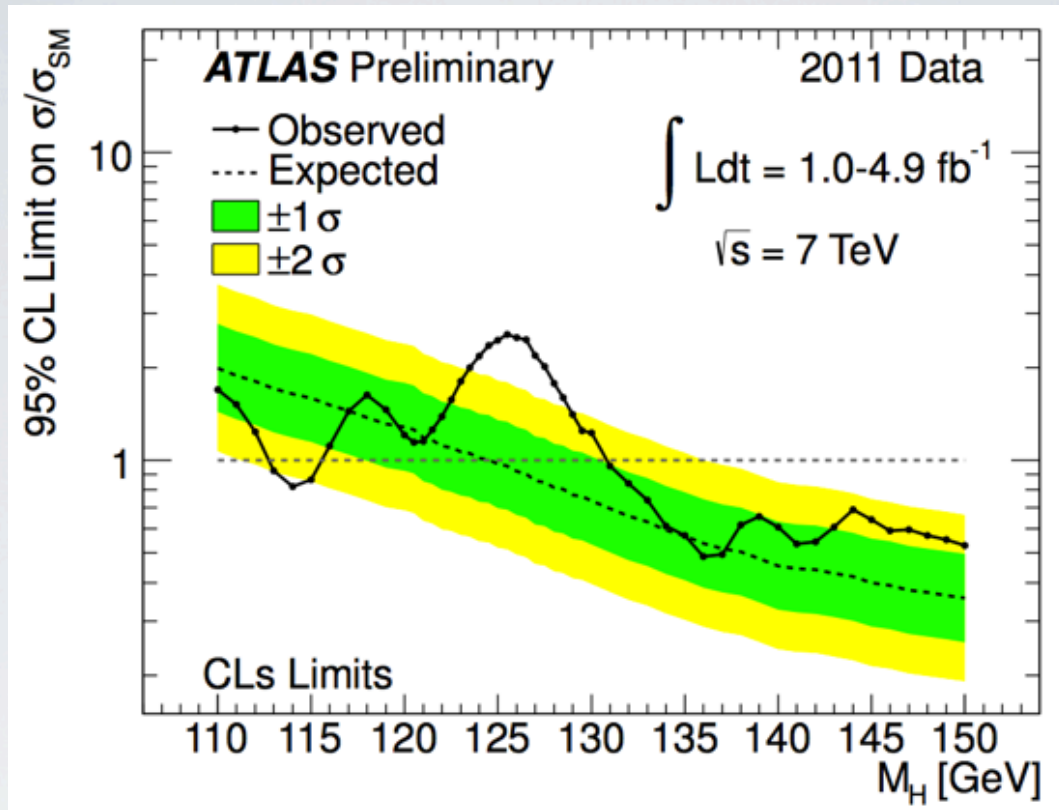
The 4D Composite Higgs

Michele Redi



with Stefania de Curtis
and Andrea Tesi
[arxiv:1110.1613\[hep-ph\]](https://arxiv.org/abs/1110.1613)
+ work in progress

Trieste, 27 January



Technicolor:



Light Higgs ok for composite models



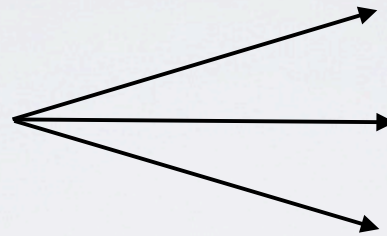
COMPOSITE HIGGS

Georgi, Kaplan '80s

Logical possibility:

Higgs doublet is a light remnant of strong dynamics.

Strong sector:
resonances +
Higgs bound state



spin 1

spin 1/2

spin 0.... $2\frac{1}{2}$

Two parameters:

m_ρ

g_ρ

$$\left(g_\rho = \frac{4\pi}{\sqrt{N}} \right)$$

Relieves hierarchy problem:

$$\delta m_h^2 \sim \frac{3\lambda_t^2}{4\pi^2} m_\rho^2$$

Particularly compelling if the Higgs is a Goldstone Boson:
 Massless at leading order:

Ex: $\frac{SO(5)}{SU(2)_L \otimes SU(2)_R} \longrightarrow GB = (2, 2)$ Agashe, Contino, Pomarol '04
 Contino, da Rold, Pomarol, '06

Low energy lagrangian:

$$\mathcal{L} = f^2 D_\mu \Sigma^i D^\mu \Sigma^i + \dots \xrightarrow{SU(2)_L \otimes SU(2)_R} \rho = \frac{m_W^2}{m_Z^2 \cos \theta_W} \approx 1$$

Extended Higgs sectors:

Ex: $\frac{SO(6)}{SO(5)}$ $\frac{SO(6)}{SO(4) \otimes U(1)}$ $\frac{SU(5)}{SU(4) \otimes U(1)}$ + ...


Gripaios, Pomarol, Riva, Serra '09

Mrazek, Pomarol, Rattazzi, MR, Serra, Wulzer '11

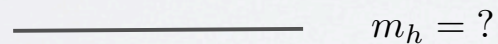
Main difference from techni-color is that f is not linked to v .
Increasing f CH approximates SM.

$$\text{TUNING} \sim \frac{v^2}{f^2}$$

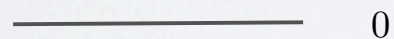
Spectrum:


$$m_\rho \sim 3 \text{ TeV}$$

$$m_\rho = g_\rho f$$

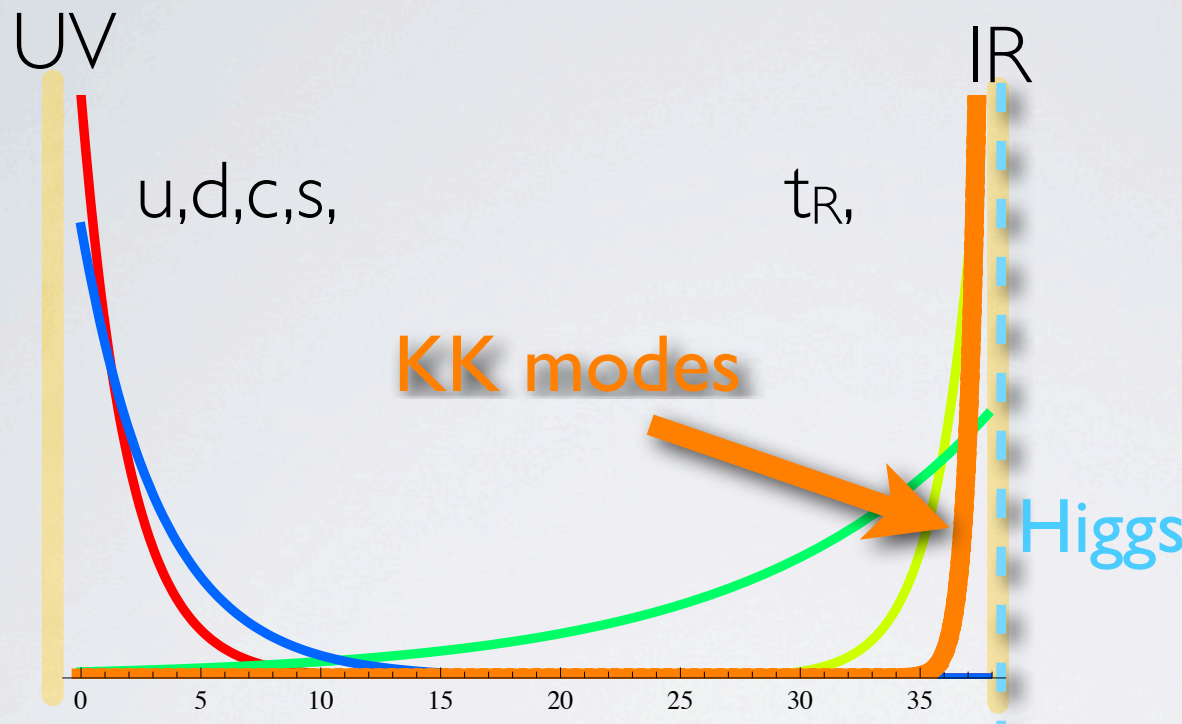

$$m_h = ?$$


$$m_W = 80 \text{ GeV}$$


$$0$$

Reasonable phenomenology can be obtained for $m_\rho \sim 3 \text{ TeV}$

Recent progress started with Randall-Sundrum constructions.



(Randall-Sundrum '99)

$$ds^2 = e^{-2kry}(-dt^2 + dx^2) + dy^2$$

5D = Effective description of strongly coupled theories

Arkani-Hamed, Porrati, Randall '01

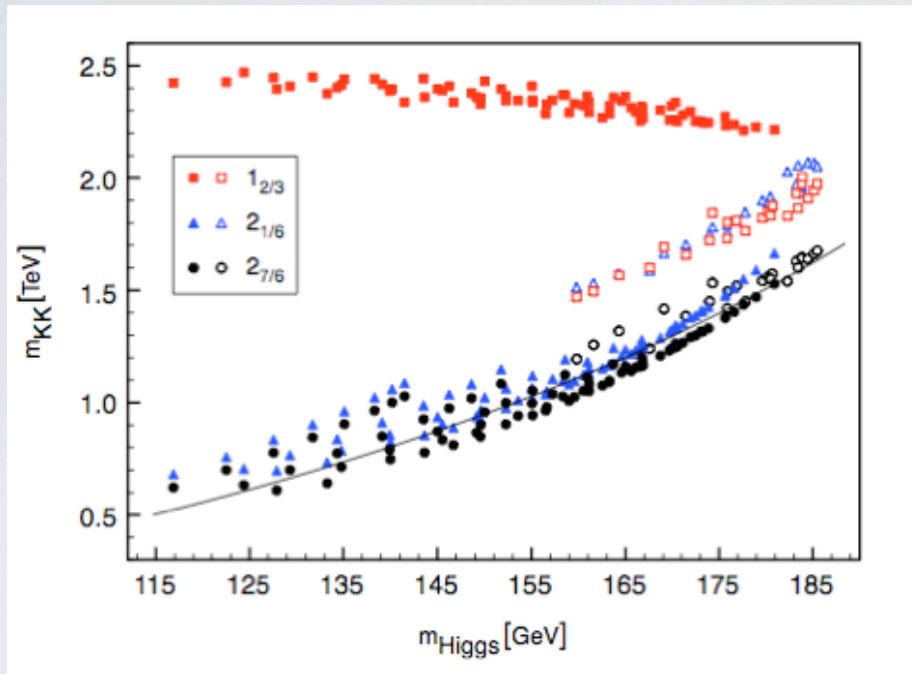
Rattazzi, Zaffaroni '01

Inspired by AdS/CFT but metric not very important.

Panico, Safari, Serone '10

Becciolini, MR, Wulzer '09

When 5D theory weakly coupled (large N), one can compute. CHM5:



(Contino, da Rold, Pomarol '06)

In practice the 5D theory cannot be very weakly coupled

$$\Lambda = \frac{16\pi^2}{g_5^2}$$

$$N_{eff} = \frac{\Lambda}{m_\rho}$$

$$\hat{S} \sim \frac{N_{eff} v^2}{16\pi^2 f^2}$$

Phenomenologically strong coupling required!

Necessary a useful 4D description:

- theoretical:
 - only very few resonances (1?) weakly coupled
 - relevant physics largely independent of 5D or AdS
 - what are the most general models?
- practical:
 - LHC will at best produce the lightest resonances
 - Simplified model useful for LHC

General picture:

Strong sector:
Higgs + (top)
 m_ρ g_ρ

λ_L λ_R g

←→

Gauging SU(3)×SU(2)×U(1)
mixing to fermionic operators

Elementary:
SM Fermions
+ Gauge Fields

They talk through linear couplings:

$$\mathcal{L}_{gauge} = g A_\mu J^\mu$$

$$\mathcal{L}_{mixing} = \lambda_L \bar{f}_L O_R + \lambda_R \bar{f}_R O_R \quad \xrightarrow{\tan \varphi \sim \frac{\lambda}{g_\rho}} \quad y \sim \frac{\lambda_L \lambda_R}{g_\rho}$$

Potential generated at 1-loop:

$$V(H) \propto \frac{m_\rho^4}{g_\rho^2} \frac{\lambda_{L,R}^2}{16\pi^2} \hat{V} \left(\frac{H}{f} \right)$$

Already on the market:

- Simplified two-sector model:

Contino, Kramer, Son, Sundrum '06

$(f \rightarrow \infty)$

- Low energy effects

Giudice, Grojean, Pomarol, Rattazzi '07

Barbieri, Bellazzini, Rychkov, Varagnolo '07

- 3-site model

Panico, Wulzer '11

Take G broken to H . Low energy lagrangian determined by symmetries. CCWZ:

$$U(\Pi) = e^{\frac{i\Pi\hat{T}\hat{a}}{f}} \quad U(\Pi') = gU(\Pi)h^\dagger(\Pi, g) \quad g \in G, \quad h \in H(x)$$

$$U^\dagger \partial_\mu U = iE_\mu^a T^a + iD_\mu^{\hat{a}} T^{\hat{a}}$$

GB lagrangian

$$\mathcal{L} = \frac{f^2}{2} D_\mu^{\hat{a}} D^{\mu\hat{a}}$$

Matter couplings,

$$\bar{\psi} \gamma^\mu (\partial_\mu + iE_\mu) \psi$$

Many ways to introduce spin-1 resonances...

We start from G/H

$$\frac{G_L \otimes G_R}{G_{L+R}} \quad \Omega \rightarrow g_L \Omega g_R^\dagger \quad + \quad \frac{G}{H}$$

and gauge $G_R + G$

$$\mathcal{L}_{2-site} = \frac{f_1^2}{4} \text{Tr} |D_\mu \Omega|^2 + \frac{f_2^2}{2} D_\mu^{\hat{a}} D^{\mu \hat{a}} - \frac{1}{4g_\rho^2} \rho_{\mu\nu}^A \rho^{A\mu\nu}$$

$$D_\mu \Omega = \partial_\mu \Omega - iA_\mu \Omega + i\Omega \rho_\mu$$

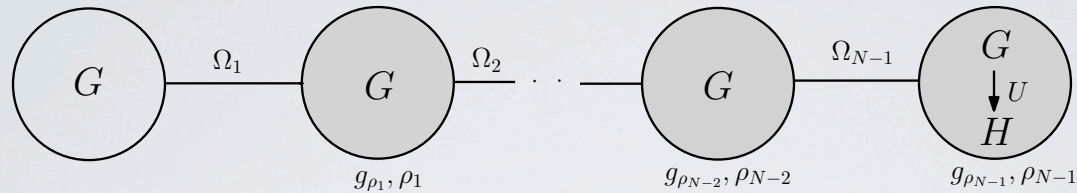
Natural to have H and G/H resonances.

In QCD these are vector and axial resonances.

We recover CCWZ for $f_2 \rightarrow \infty$

$$\mathcal{L} = \frac{f^2}{2} D_\mu^{\hat{a}} D^{\mu \hat{a}} - \frac{1}{4g_\rho^2} \rho_{\mu\nu}^a \rho^{\mu\nu a} + \frac{f'^2}{2} (\rho_\mu^a - E_\mu^a)^2$$

In general:



$$\mathcal{L}_{N\text{-sites}} = \sum_{n=1}^{N-1} \frac{f_n^2}{4} \text{Tr} |D_\mu \Omega_n|^2 + \frac{f_N^2}{2} \mathcal{D}_\mu^{\hat{a}} \mathcal{D}^{\mu \hat{a}} - \sum_{n=1}^{N-1} \frac{1}{4 g_{\rho_n}^2} \rho_{n, \mu\nu}^A \rho_n^{A\mu\nu}$$

$$D^\mu \Omega_n = \partial^\mu \Omega_n - i \rho_{n-1}^\mu \Omega_n + i \Omega_n \rho_n^\mu, \quad n = 1, \dots, N-1$$

GBs are

$$\Omega_n = \exp i \frac{f}{f_n^2} \Pi, \quad n = 1, \dots, N$$

$$\sum_{n=1}^N \frac{1}{f_n^2} = \frac{1}{f^2}$$

$$U' \equiv (\prod_{n=1}^{N-1} \Omega_n) U$$

For N large we recover the 5D theory.
Boundary conditions not rigid for f_N finite.

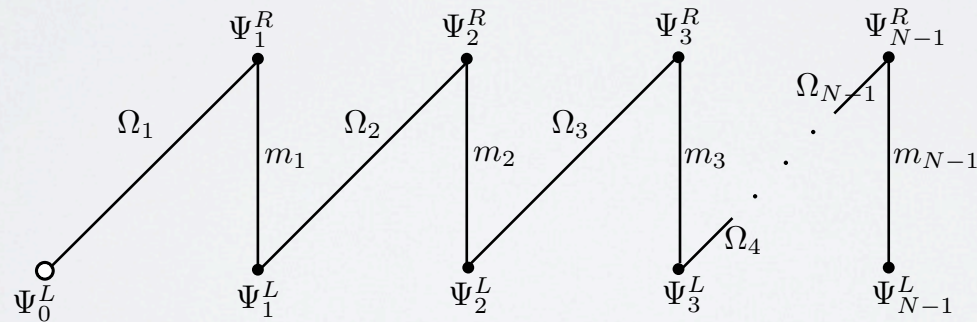
Fermions:

$$\mathcal{L}_{fermions} = \sum_{n=1}^{N-1} \bar{\Psi}_n^{(r)} \left[i \not{D}^{\rho n} - m_n^{(r)} \right] \Psi_n^{(r)} + \sum_{n=1}^{N-1} \Delta_n^{(r)} \left(\bar{\Psi}_{r,L}^{n-1} \Omega_n \Psi_{r,R}^n + h.c. \right)$$

$$D^\mu \Psi_n^{(r)} = \partial^\mu \Psi_n^{(r)} - i \rho_n^\mu \Psi_n^{(r)}$$

$$\mathcal{L}_{\frac{G}{H}} = m_\Psi \sum \bar{\Psi}_L^{(r), N-1} U(\Pi) P_A^{rs} U(\Pi)^\dagger \Psi_R^{(s), N-1} + h.c.$$

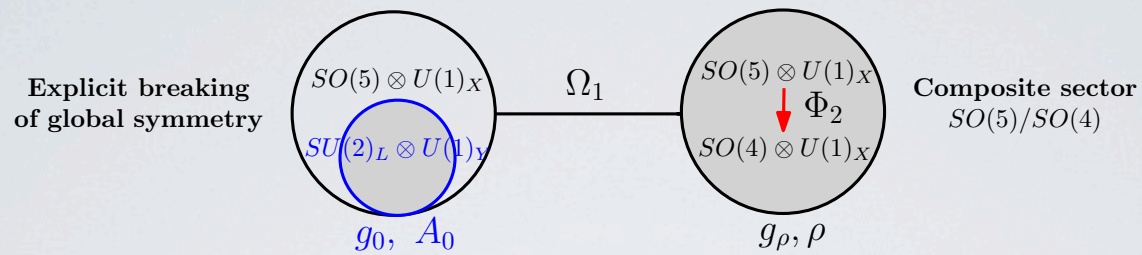
LR structure



Inspired by 5D.

MINIMAL 4D COMPOSITE HIGGS

- One resonance for each SM field



Minimal coset:

$$\frac{SO(5)}{SU(2)_L \otimes SU(2)_R}$$

Extra $U(1)_X$

$$Y = T_{3R} + X$$

Composite spin-1 lagrangian:

$$\mathcal{L}_{gauge} = \frac{f_1^2}{4} \text{Tr} |D_\mu \Omega_1|^2 + \frac{f_2^2}{2} (D_\mu \Phi_2) (D^\mu \Phi_2)^T - \frac{1}{4g_\rho^2} \rho_{\mu\nu}^A \rho^{A\mu\nu}$$

$$\Omega_1 = \mathbf{1} + i \frac{s_1}{h} \Pi + \frac{c_1 - 1}{h^2} \Pi^2$$

$$\Phi_2 = \phi_0 e^{-i \frac{\Pi}{f_2}} = \frac{1}{h} \sin \frac{h}{f_2} \left(h_1, h_2, h_3, h_4, h \cot \frac{h}{f_2} \right)$$

Spectrum:

$$\begin{aligned}m_{\rho}^2 &= \frac{g_{\rho}^2 f_1^2}{2} \\m_{a_1}^2 &= \frac{g_{\rho}^2 (f_1^2 + f_2^2)}{2} \\m_{\rho_X}^2 &= \frac{g_{\rho_X}^2 f_X^2}{2}\end{aligned}$$

SM fields are introduced adding kinetic terms for the sources

$$\mathcal{L}_{gauge}^{el} = -\frac{1}{4g_0^2} F_{\mu\nu}^a F_{\mu\nu}^a - \frac{1}{4g_{0Y}^2} Y_{\mu\nu} Y^{\mu\nu}$$

Physical parameters:

$$\begin{aligned}\frac{1}{g^2} &= \frac{1}{g_0^2} + \frac{1}{g_{\rho}^2} \\ \frac{1}{g'^2} &= \frac{1}{g_{0Y}^2} + \frac{1}{g_{\rho}^2} + \frac{1}{g_{\rho_X}^2} \\ m_{\rho_{aL}} &= \frac{m_{\rho}}{\cos \theta_L}, \quad \tan \theta_L = \frac{g_0}{g_{\rho}}\end{aligned}$$

Each SM fermion is associated to a rep of SO(5).

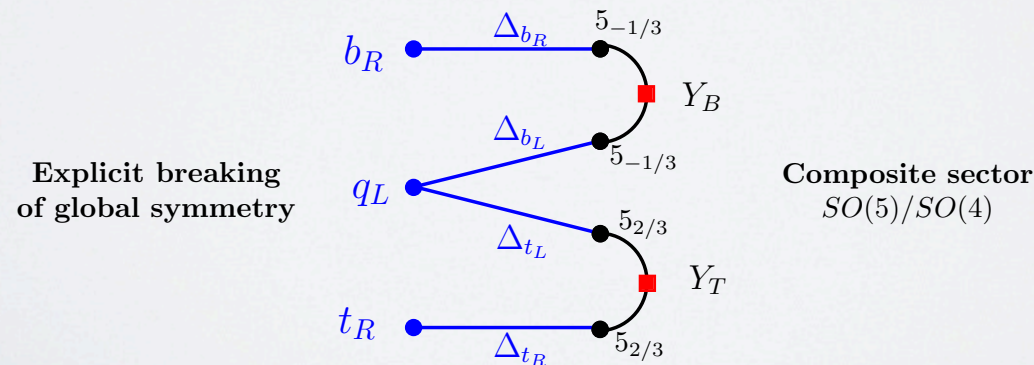
CHM5:

$$\mathbf{5}_{2/3} = (\mathbf{2}, \mathbf{2})_{2/3} \oplus (\mathbf{1}, \mathbf{1})_{2/3}, \quad (\mathbf{2}, \mathbf{2})_{2/3} = \begin{pmatrix} T & T_{\frac{3}{2} \frac{3}{2} \frac{3}{2}} \\ B & T_{\frac{3}{2} \frac{3}{2}} \end{pmatrix}$$

Left and right components correspond to different 5.

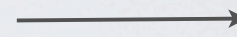
Down quarks

$$\mathbf{5}_{-1/3} = (\mathbf{2}, \mathbf{2})_{-1/3} \oplus (\mathbf{1}, \mathbf{1})_{-1/3}, \quad (\mathbf{2}, \mathbf{2})_{-1/3} = \begin{pmatrix} B_{-\frac{1}{3}} & T' \\ B_{-\frac{4}{3}} & B' \end{pmatrix}.$$

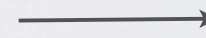


Third generation:

$$\begin{aligned}
 \mathcal{L}^{\text{CHM}_5} = & \mathcal{L}_{\text{fermions}}^{\text{el}} \\
 & + \Delta_{t_L} \bar{q}_L^{\text{el}} \Omega_1 \Psi_T + \Delta_{t_R} \bar{t}_R^{\text{el}} \Omega_1 \Psi_{\tilde{T}} + h.c. \\
 & + \bar{\Psi}_T (i \not{D}^\rho - m_T) \Psi_T + \bar{\Psi}_{\tilde{T}} (i \not{D}^\rho - m_{\tilde{T}}) \Psi_{\tilde{T}} \\
 & - Y_T \bar{\Psi}_{T,L} \Phi_2^T \Phi_2 \Psi_{\tilde{T},R} - m_{Y_T} \bar{\Psi}_{T,L} \Psi_{\tilde{T},R} + h.c. \\
 & + (T \rightarrow B)
 \end{aligned}$$



Explicit SO(5) breaking



Composite physics
SO(5)/SO(4)

$$\mathcal{L}_{\text{fermions}}^{\text{el}} = \bar{q}_L^{\text{el}} i \not{D}^{\text{el}} q_L^{\text{el}} + \bar{t}_R^{\text{el}} i \not{D}^{\text{el}} t_R^{\text{el}} + \bar{b}_R^{\text{el}} i \not{D}^{\text{el}} b_R^{\text{el}}$$

Masses:

$$m_t \sim \frac{v}{\sqrt{2}} \frac{\Delta_{t_L}}{m_T} \frac{\Delta_{t_R}}{m_{\tilde{T}}} \frac{Y_T}{f}$$

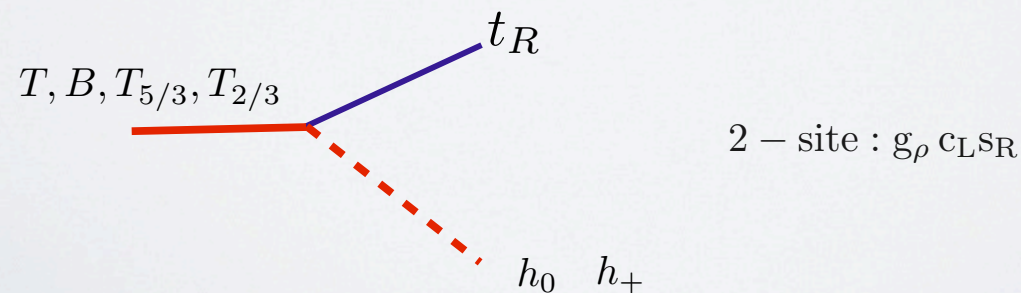
Relation to 2-site picture:

$$\mathcal{L}_{comp}^{gauge} = -\frac{1}{4}\rho_{\mu\nu}^A \rho^{A\mu\nu} + \frac{1}{2}m_\rho^2 \rho_\mu^a \rho^{a\mu} + \frac{1}{2}m_{a_1}^2 \rho_\mu^{\hat{a}} \rho^{\hat{a}\mu} + |\partial_\mu - ig_\rho \rho_\mu^a H|^2 \quad + \text{nl terms}$$

$$\mathcal{L}_{mix} = \frac{1}{2}m_\rho^2 \frac{g_0^2}{g_\rho^2} A_\mu^a A^{a\mu} - m_\rho^2 \frac{g_0}{g_\rho} A_\mu^a \rho^{a\mu} + g_0 \frac{f^2}{f_1^2} (\partial^\mu H^\dagger A_\mu H) + \dots$$

- Non linear GB structure included.
- Correlations of 2-site model removed.

Ex:



We can borrow 5D techniques and write the effective action of SM fields:

Contino, da Rold, Pomarol, '06

$$\begin{aligned}
 \mathcal{L}_{\text{eff}}^{\text{ferm}} &= \bar{q}_L \not{p} \left[\Pi_0^q(p^2) + \frac{s_h^2}{2} \left(\Pi_1^{q1}(p^2) \hat{H}^c \hat{H}^{c\dagger} + \Pi_1^{q2}(p^2) \hat{H} \hat{H}^\dagger \right) \right] q_L \\
 &+ \bar{u}_R \not{p} \left(\Pi_0^u(p^2) + \frac{s_h^2}{2} \Pi_1^u(p^2) \right) u_R + \bar{d}_R \not{p} \left(\Pi_0^d(p^2) + \frac{s_h^2}{2} \Pi_1^d(p^2) \right) d_R \\
 &+ \frac{s_h c_h}{\sqrt{2}} M_1^u(p^2) \bar{q}_L \hat{H}^c u_R + \frac{s_h c_h}{\sqrt{2}} M_1^d(p^2) \bar{q}_L \hat{H} d_R + h.c..
 \end{aligned}$$

$$\begin{aligned}
 \mathcal{L}_{\text{eff}}^{\text{gauge}} &= \frac{1}{2} P_{\mu\nu}^T \left[\left(\Pi_0(p^2) + \frac{s_h^2}{4} \Pi_1(p^2) \right) A_{aL}^\mu A_{aL}^\nu \right. \\
 &+ \left. \left(\Pi_Y(p^2) + \frac{s_h^2}{4} \Pi_1(p^2) \right) Y^\mu Y^\nu + 2s_h^2 \Pi_1(p^2) \hat{H}^\dagger T_L^a Y \hat{H} A_\mu^{aL} Y_\nu \right]
 \end{aligned}$$

Coleman-Weinberg effective potential:

$$V(h)_{\text{fermions}} = -2N_c \int \frac{d^4 p}{(2\pi)^4} \left[\ln \Pi_{b_L} + \ln (p^2 \Pi_{t_L} \Pi_{t_R} - \Pi_{t_L t_R}^2) \right]$$

$$V(h)_{\text{gauge}} = \frac{9}{2} \int \frac{d^4 p}{(2\pi)^4} \ln \left[1 + \frac{1}{4} \frac{\Pi_1(p^2)}{\Pi_0(p^2)} \sin^2 \frac{h}{f} \right]$$

Form factors are simple functions:

$$\widehat{\Pi}[m_1, m_2, m_3] = \frac{(m_2^2 + m_3^2 - p^2)}{p^4 - p^2(m_1^2 + m_2^2 + m_3^2) + m_1^2 m_2^2}$$

$$\widehat{M}[m_1, m_2, m_3] = -\frac{m_1 m_2 m_3}{p^4 - p^2(m_1^2 + m_2^2 + m_3^2) + m_1^2 m_2^2}$$

$$\Pi_{gauge}[m_V] = \frac{p^2}{p^2 - m_V^2}$$

Gauge potential:

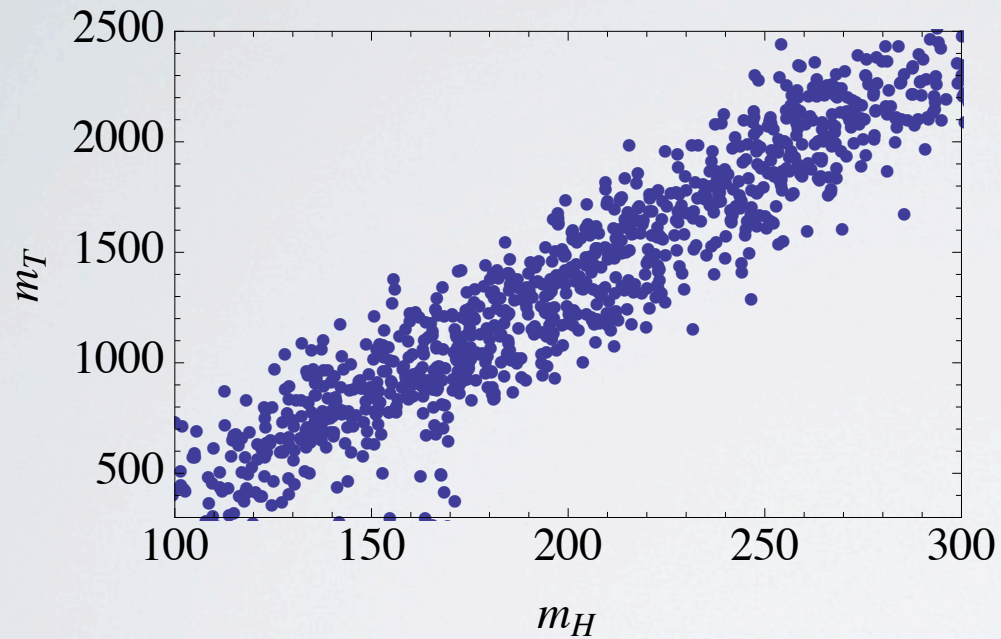
$$\begin{aligned} V(h)_{gauge} &\approx \int \frac{d^4 p}{(2\pi)^4} \frac{9}{8} \frac{\Pi_1}{\Pi_0} \sin^2 \frac{h}{f} \\ &= \frac{9}{4} \frac{1}{16\pi^2} \frac{g_0^2}{g_\rho^2} \frac{m_\rho^4 (m_{a_1}^2 - m_\rho^2)}{m_{a_1}^2 - m_\rho^2 (1 + g_0^2/g_\rho^2)} \ln \left[\frac{m_{a_1}^2}{m_\rho^2 (1 + g_0^2/g_\rho^2)} \right] \sin^2 \frac{h}{f} \end{aligned}$$

Potential is finite with a single SO(5) multiplet!

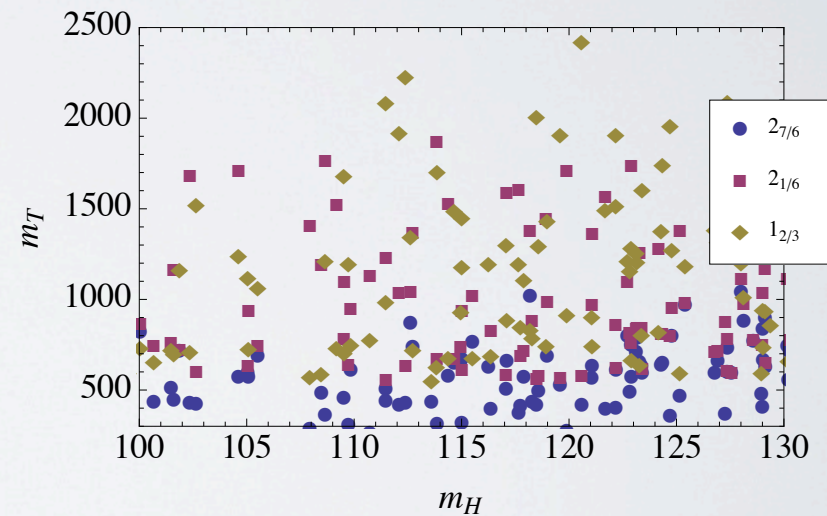
HIGGS MASS

General scan:

$$f = 500 \text{ GeV}$$

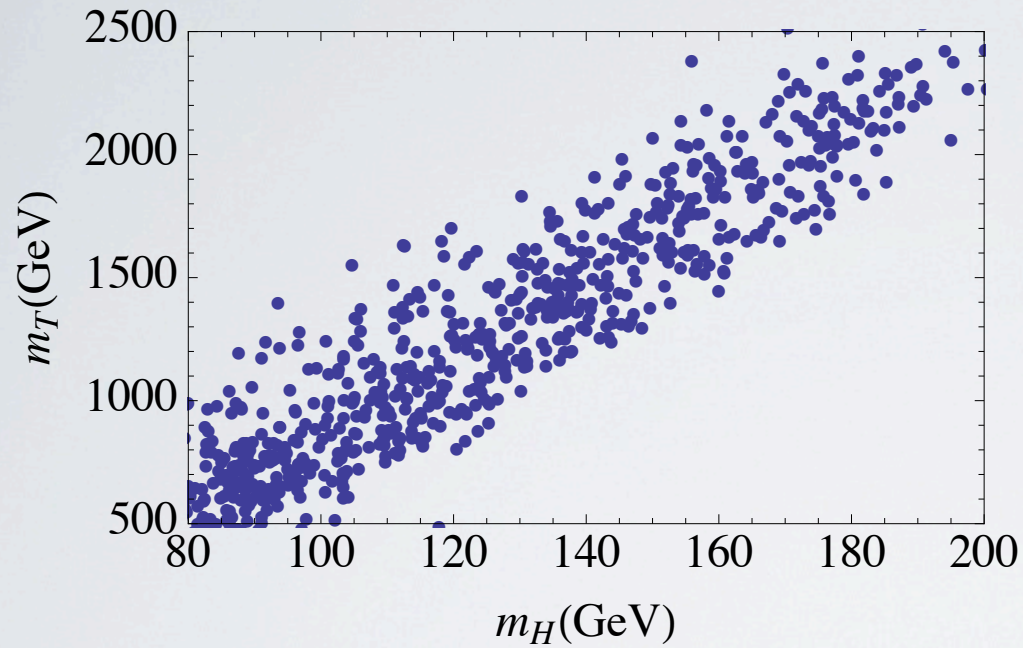


Low mass:

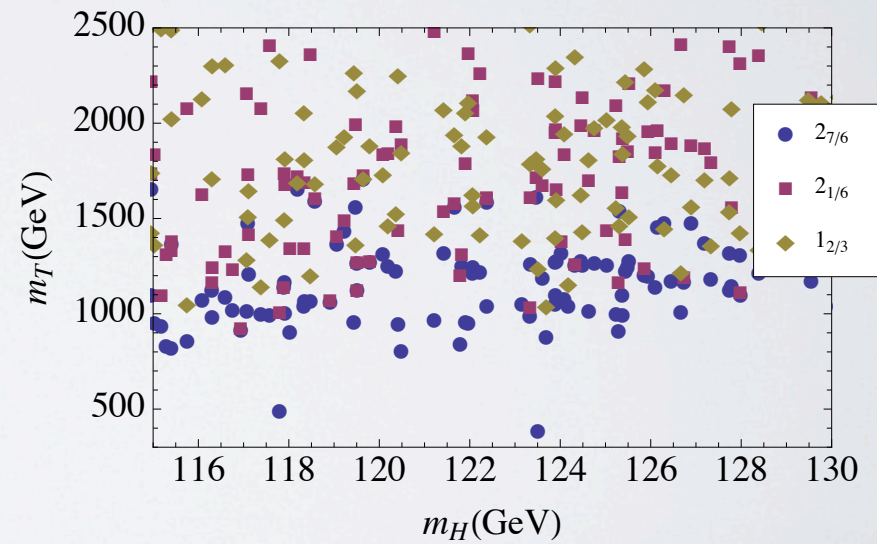


If $m_H = 125$ GeV, nearby fermionic partners.
Might be visible at LHC7!

$$f = 800 \text{ GeV}$$



Low mass:



Partners above experimental bound.

Large mixing:

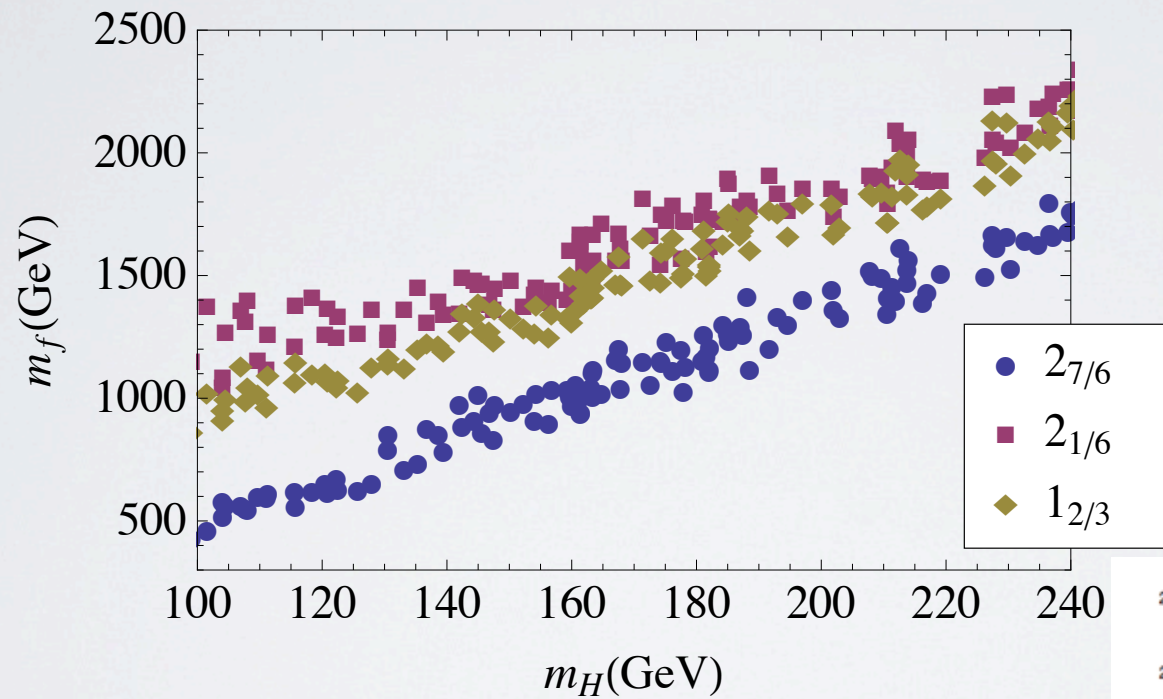
$$f = 500 \text{ GeV}$$

$$1.2 \leq \Delta_{t_L}/m_T \leq 1.8$$

$$0.7 \leq \Delta_{t_R}/m_{\tilde{T}} \leq 1.3$$

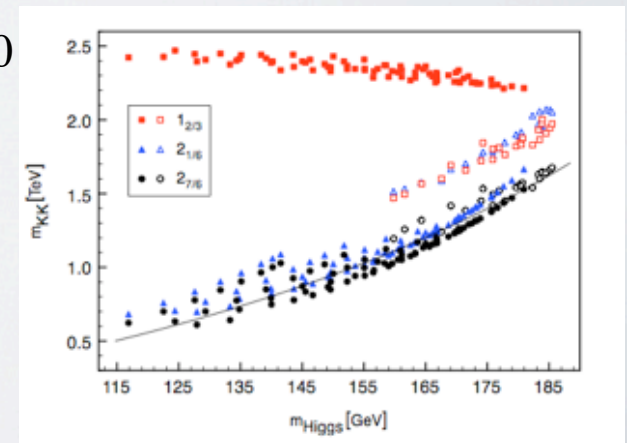
$$0.5 \leq Y_T \leq 3$$

$$-1.2Y_T \leq m_{Y_T} \leq -0.8Y_T$$



5D

Doublet lightest fermion



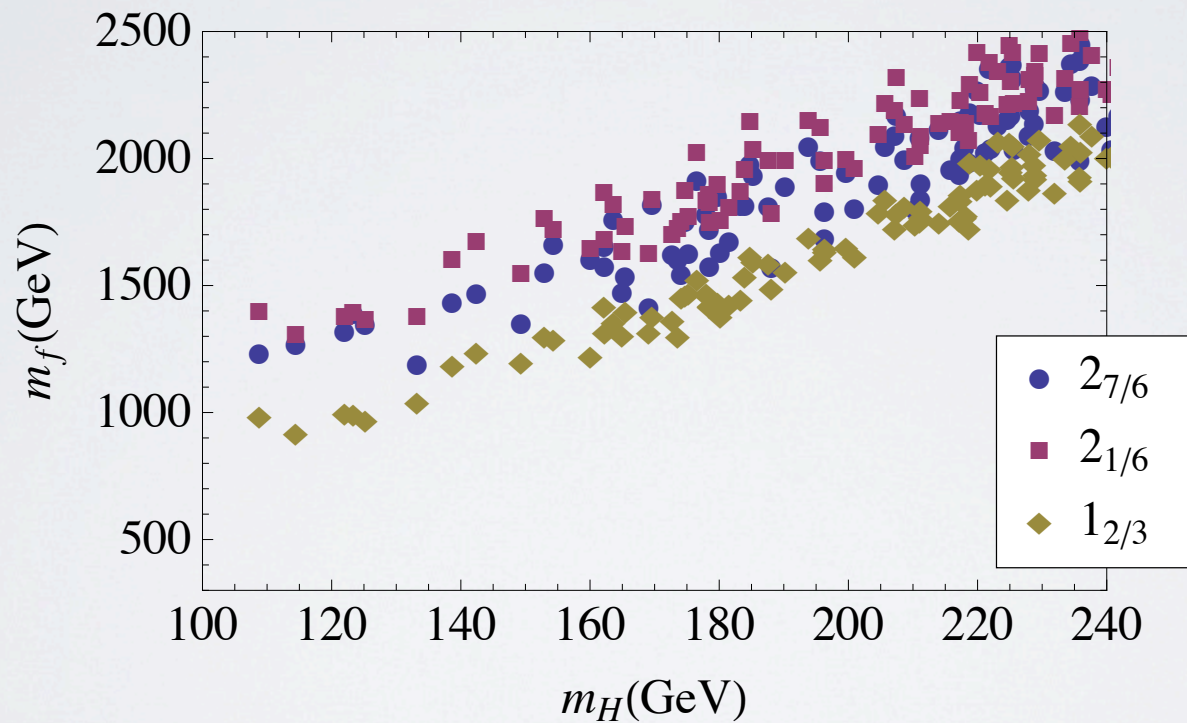
Moderate mixing:

$$0.6 \leq \Delta_{t_L}/m_T \leq 0.9$$

$$0.35 \leq \Delta_{t_R}/m_{\tilde{T}} \leq 0.7$$

$$0.5 \leq Y_T \leq 3$$

$$-0.5 \leq m_{Y_T} \leq 0.5$$



Singlet lightest fermion

SO(6)/SO(5):

5 GBs:

$$5 = (2, 2) + 1$$

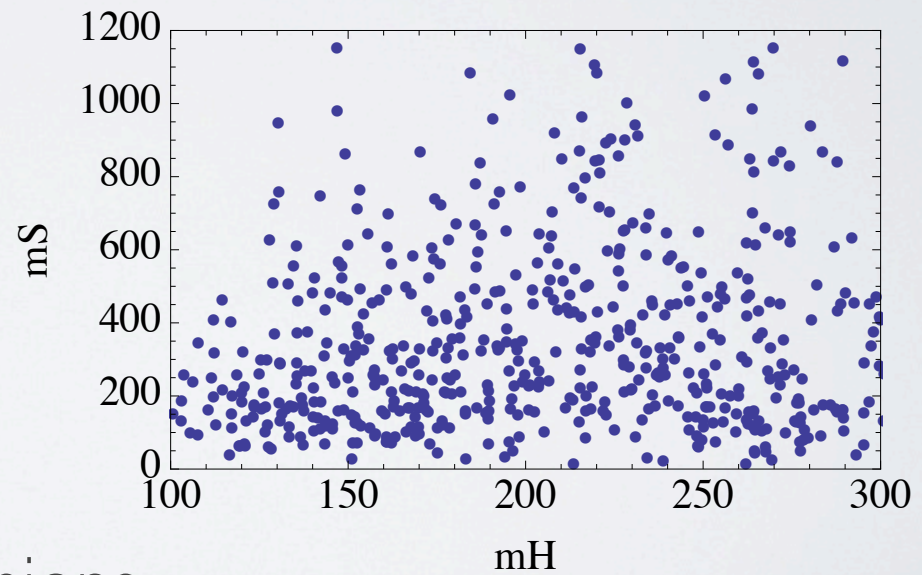
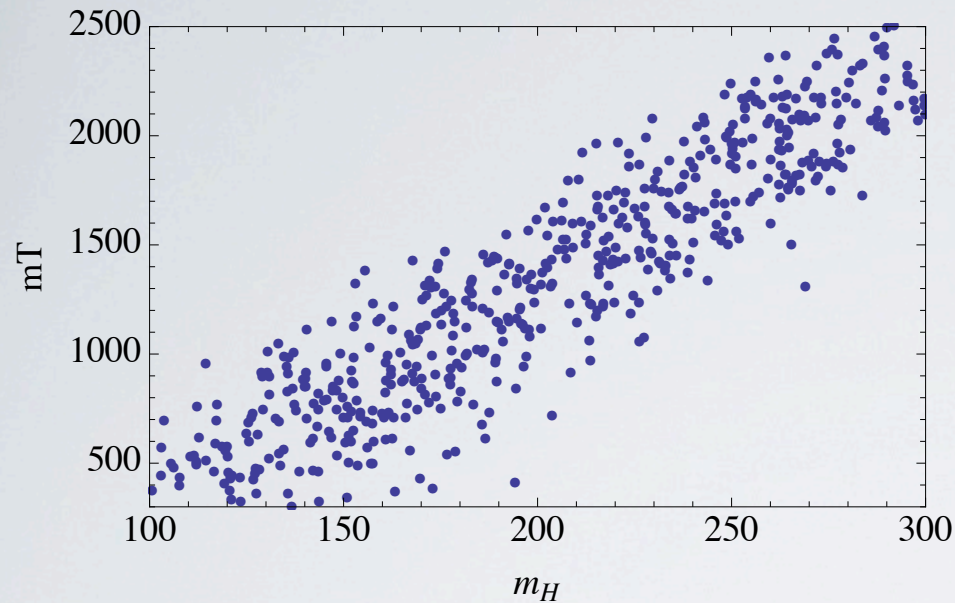
$$\Phi = \sin \frac{\varphi}{f} \left(\frac{h_1}{\varphi}, \frac{h_2}{\varphi}, \frac{h_3}{\varphi}, \frac{h_4}{\varphi}, \frac{s}{\varphi}, \cot \frac{\varphi}{f} \right). \quad \varphi = \sqrt{\vec{h}^2 + s^2}$$

Fermions can be embedded in the $6 = (2, 2) + 2 \times 1$

$$q_L \rightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} b_L \\ -ib_L \\ t_L \\ it_L \\ 0 \\ 0 \end{pmatrix} \quad t_R \rightarrow \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ i \cos \theta t_R \\ \sin \theta t_R \end{pmatrix}$$

For $\theta = \frac{\pi}{4}$ singlet becomes exact GB.

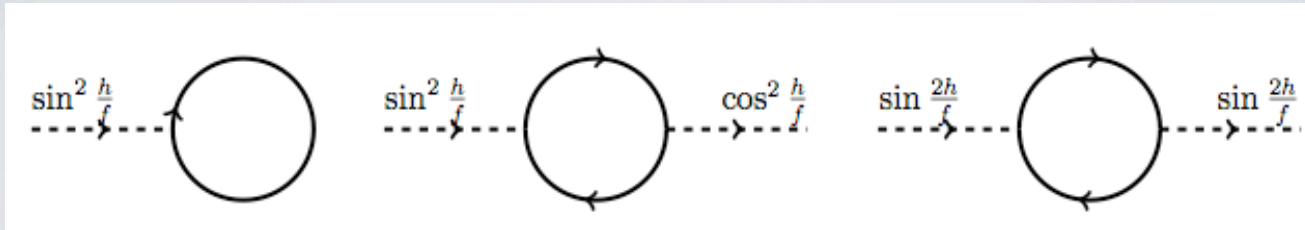
$$f = 500 \text{ GeV}$$



Same correlation Higgs-fermions.

Singlet typically heavier than Higgs unless $\theta \approx \frac{\pi}{4}$

NATURALNESS



$$\mathcal{L}_{Yuk} = y_t f \frac{s_h c_h}{h} (\bar{q}_L H^c t_R + h.c.) \longrightarrow V(h)_{Yuk} \sim N_c \frac{y_t^2}{4\pi^2} m_T^2 f^2 s_h^2 c_h^2$$

$$\mathcal{L}_{kin} = \frac{y_{tL}^2}{2y_T^2} s_h^2 \bar{t}_L \not{D}t_L + \frac{y_{tR}^2}{y_{\tilde{T}}^2} c_h^2 \bar{t}_R \not{D}t_R \longrightarrow V(h)_{kin}^{(1)} \sim N_c \frac{2y_{tR}^2 - y_{tL}^2}{32\pi^2} \frac{m_T^4}{y_T^2} s_h^2$$

Potential:

$$V(h) \approx \alpha s_h^2 - \beta s_h^2 c_h^2$$

Quartic is determined by top Yukawa,

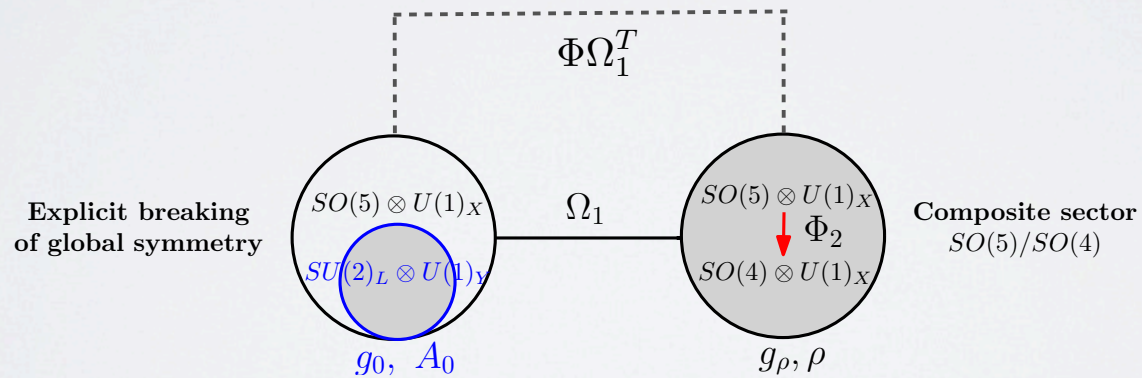
$$m_H \sim 0.3 y_t \frac{m_T}{f} v$$

NON MINIMAL TERMS

Most general 2-site lagrangian contains

$$\frac{f_0^2}{2} (D_\mu \Phi)(D^\mu \Phi)^T \quad \Phi = \Phi_2 \Omega_1^T$$

$$f^2 = f_0^2 + \frac{f_1^2 f_2^2}{f_1^2 + f_2^2}$$



Similar terms are considered in QCD.

Falkowski et al. '11
 Contino, Marzocca, Pappadopulo, Rattazzi '11

New term modifies interactions

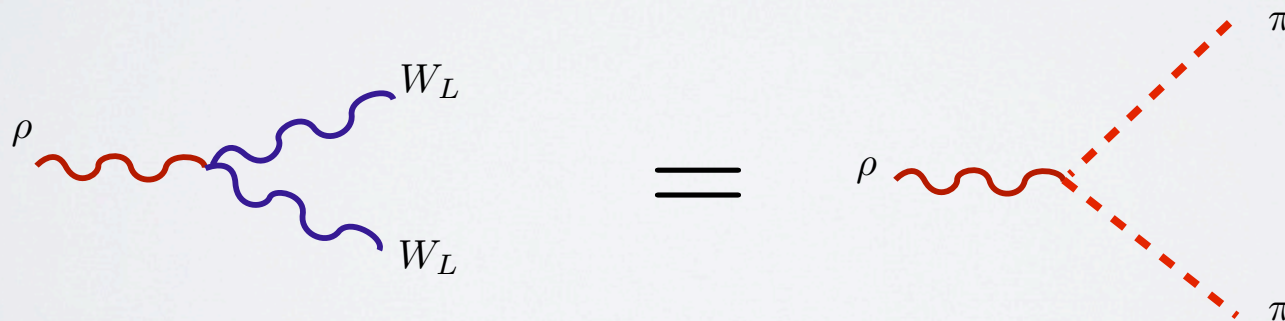
$$g_{\rho\pi\pi} = \frac{f^2 - f_0^2}{2f^2} g_\rho$$

$$(m_{a_1} \rightarrow \infty)$$

$$m_\rho^2 = 2 \frac{f^2}{f^2 - f_0^2} g_{\rho\pi\pi}^2 f^2$$

Coset resonance could give further modifications.

Phenomenology modified



$$\Gamma(\rho^3 \rightarrow Zh) = \Gamma(\rho^3 \rightarrow W^+W^-) = \frac{g_{\rho\pi\pi}^2}{192\pi} m_\rho$$

New term modifies S-parameter:

$$S = 4\pi v^2 \left(\frac{1}{m_\rho^2} + \frac{1}{m_{a_1}^2} \right) \frac{f^2 - f_0^2}{f^2}$$

S can vanish

$$f_0 = f$$

H and G/H resonances degenerate and do not participate to unitarization.

In QCD:

$$f_0^2 \sim -f^2$$

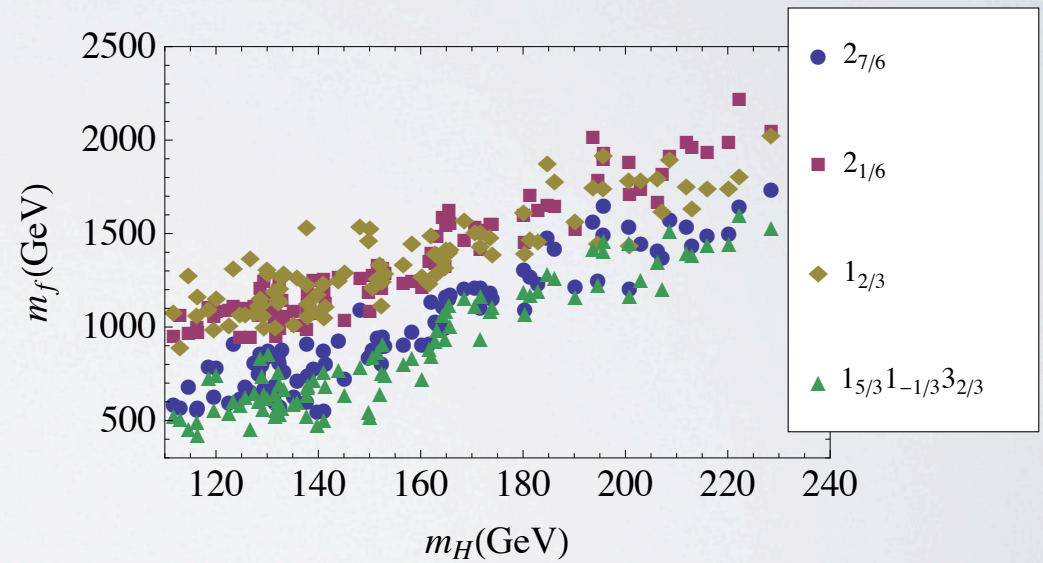
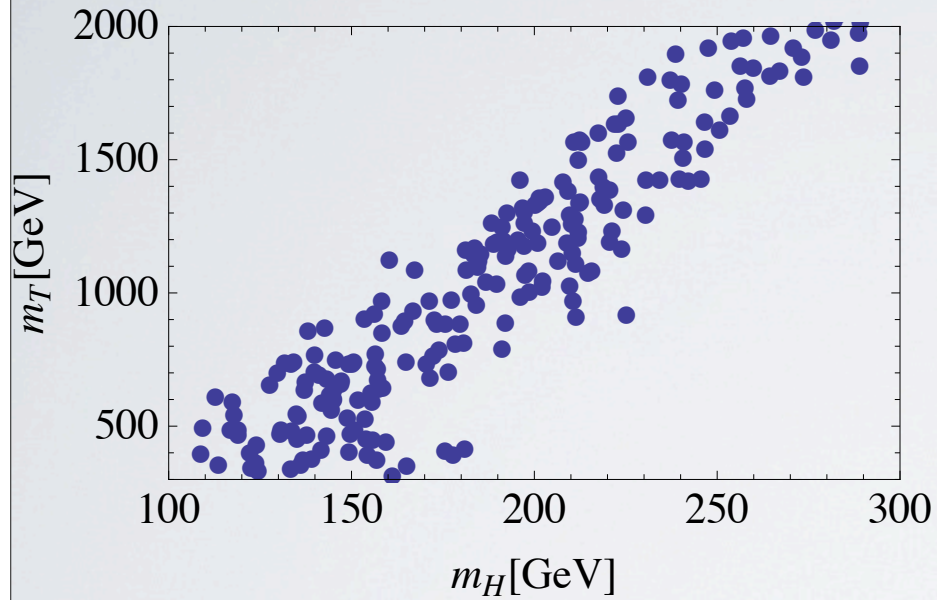
General?

CONCLUSIONS

- All relevant features of CHM can be reproduced from a 4D point view. First resonance sufficient for theory & LHC.
- In general a light Higgs requires light fermionic partners.
- More general models can be considered in 4D than 5D. Contributions to S and modified couplings.

CHM10

$$f = 500 \text{ GeV}$$



$$0.7 < \frac{\Delta t_L}{m_T} < 1.6,$$

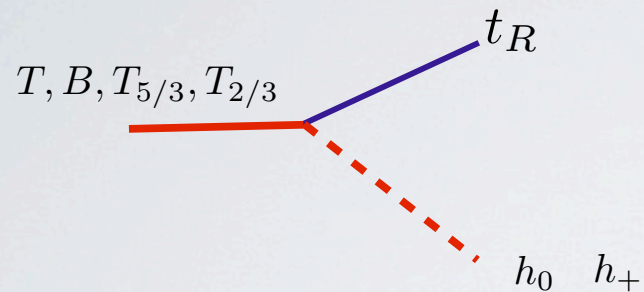
$$0.7 < \frac{\Delta t_R}{m_{\tilde{T}}} < 1.5$$

$$-0.4 < M_Y < -2.5,$$

$$0.5 < Y_T < 6$$

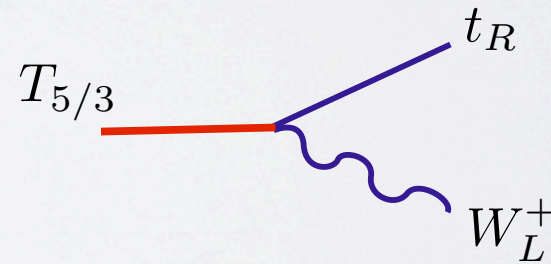
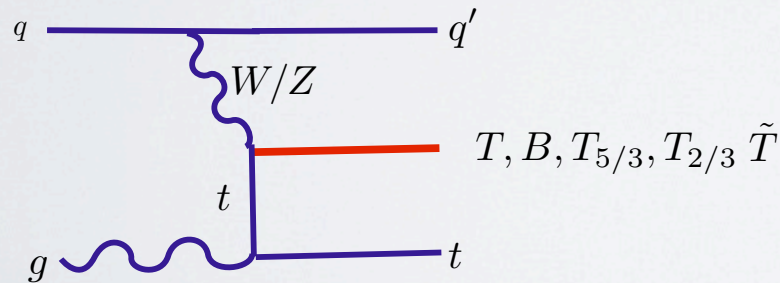
Correlations of 2 site model are modified:

$$Y_T \bar{\Psi}_{T,L} \Phi_2^T \Phi_2 \Psi_{\tilde{T},R} \longrightarrow \frac{Y_T}{2h} \sin \frac{2hf}{f_2^2} \text{Tr} \left[\left(\begin{array}{cc} T & T_{\frac{5}{3}} \\ B & T_{\frac{2}{3}} \end{array} \right)_L \cdot \left(\begin{array}{cc} h_0^\dagger & h_+ \\ h_+^\dagger & h_0 \end{array} \right) \right] \tilde{T}_R$$



$$\sim \frac{Y_T f}{f_2^2} c_{LSR} \quad \left(2\text{-site} : \frac{Y_T}{f} c_{LSR} \right)$$

Production and decay can be very different from 2 site



Relevant phenomenologically!