



**The Abdus Salam
International Centre for Theoretical Physics**



2400-9

Workshop on Strongly Coupled Physics Beyond the Standard Model

25 - 27 January 2012

A view on strongly coupled EWSB

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A view on strongly coupled EWSB

&

Summary

Riccardo Rattazzi



ÉCOLE POLYTECHNIQUE
FÉDÉRALE DE LAUSANNE

Was the hierarchy problem a good problem?



Was the hierarchy problem a good problem?

If Yes, then:

What is the dynamics of Electroweak Symmetry Breaking ?

Is it weak or is it strong?

What about Flavor?

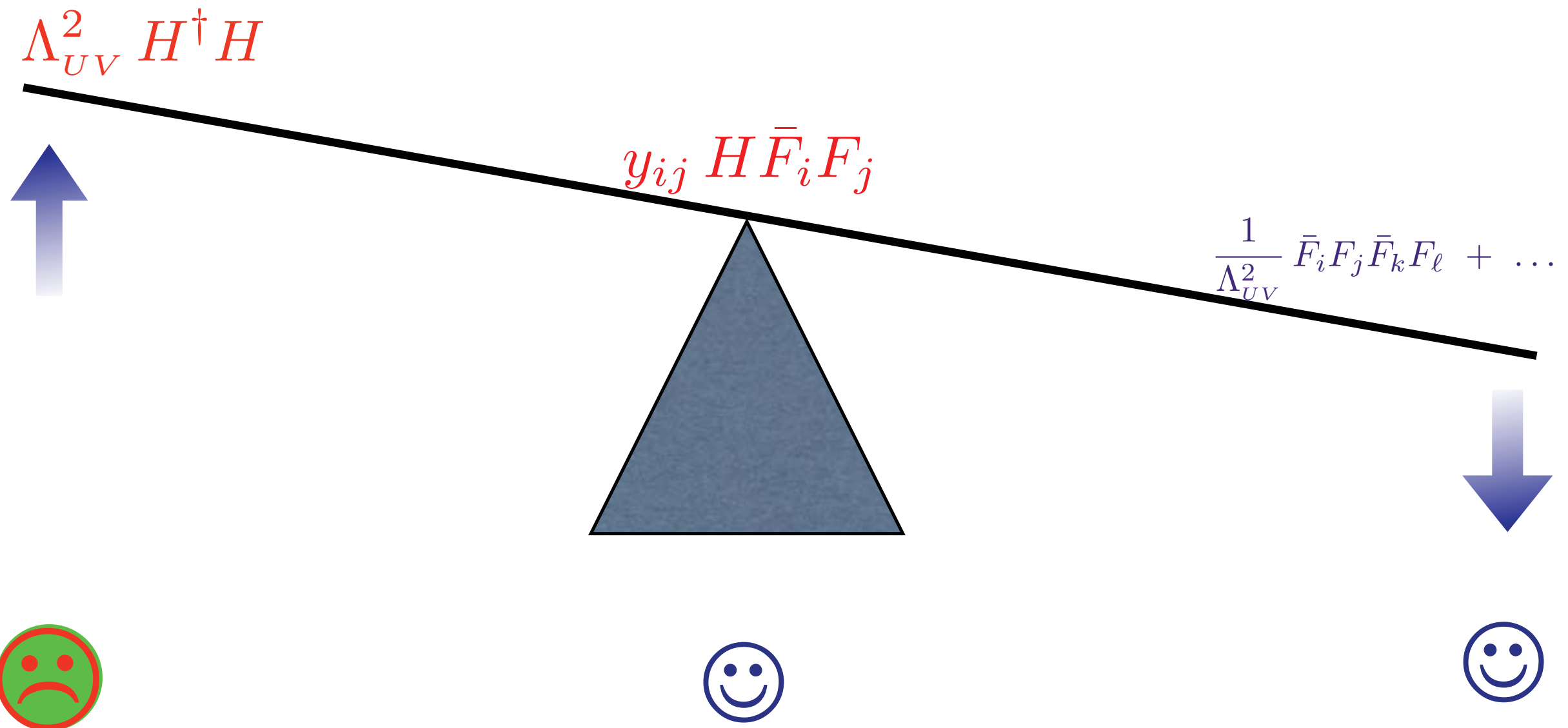
.....

I. Flavor

II. Higgs

Hierarchy see-saw

Standard Model up to some $\Lambda_{UV}^2 \gg 1 \text{ TeV}$

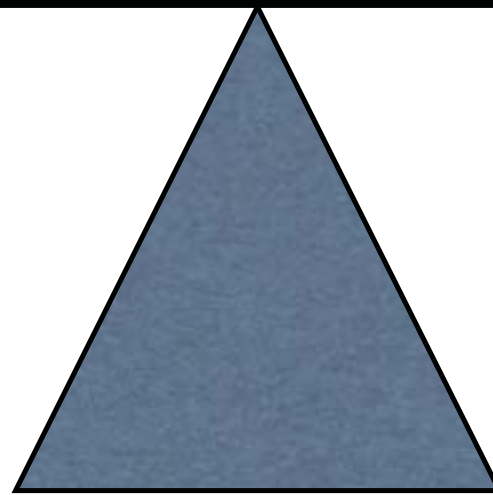


Natural SM with $\Lambda_{UV}^2 \lesssim 1 \text{ TeV}$

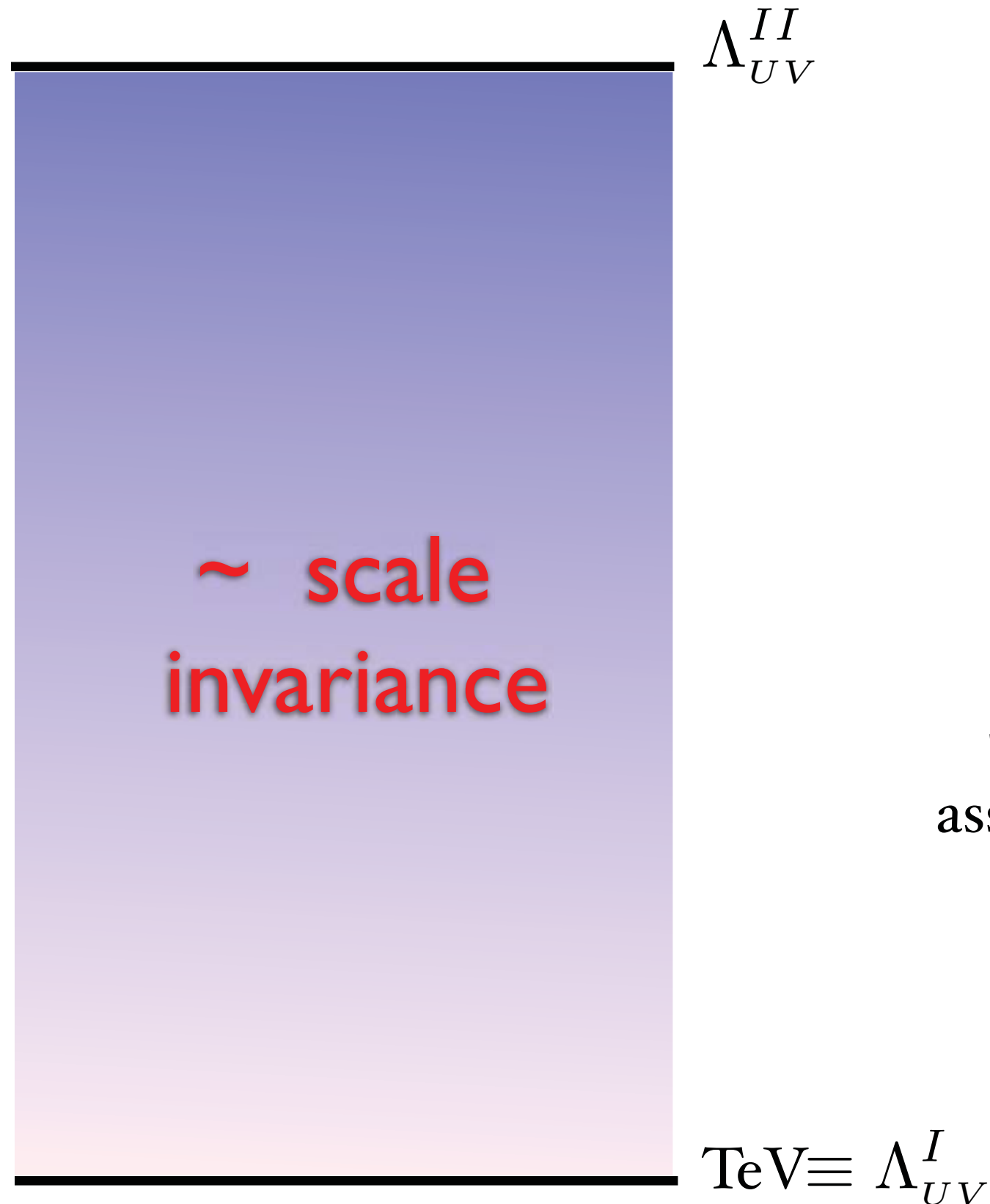
$$\Lambda_{UV}^2 H^\dagger H$$

$$y_{ij} H \bar{F}_i F_j$$

$$\frac{1}{\Lambda_{UV}^2} \bar{F}_i F_j \bar{F}_k F_l + \dots$$



Strongly coupled EWSB: basic picture



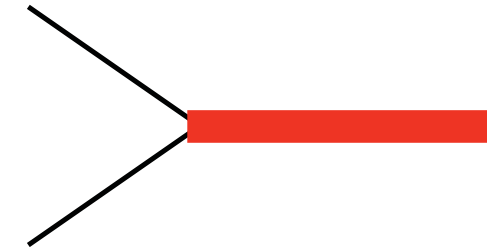
Use $\Lambda_{UV}^{II} \gg \text{TeV}$
to filter out unwanted
effects and produce a
realistic Flavor story

Should one, or should one not,
assume \sim conformal invariance?
ask J.F. Fortin and M. Luty

Three Ways to Flavor

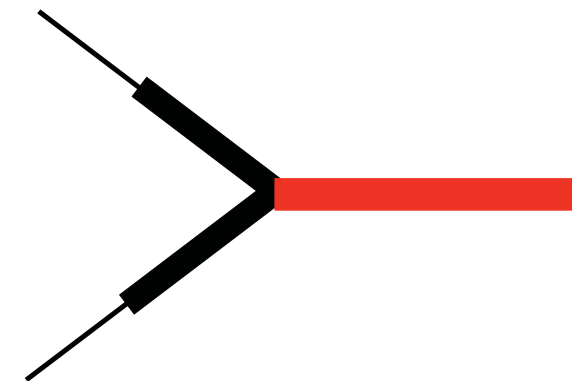
Bilinear: ETC, conformalTC

Dimopoulos, Susskind
Holdom
...
Luty, Okui



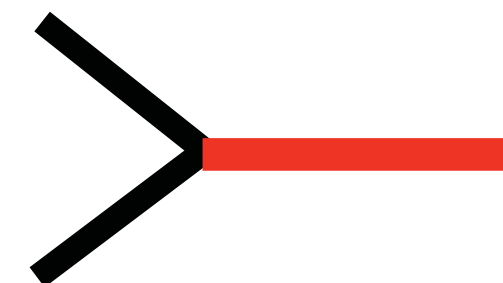
Linear: partial compositeness

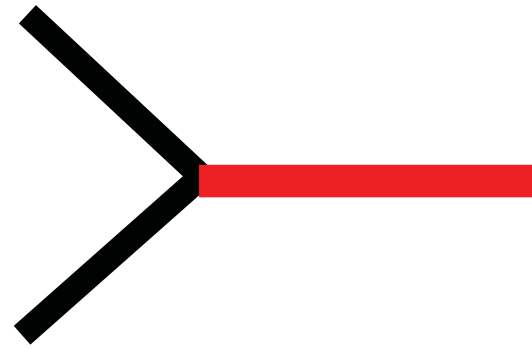
D.B. Kaplan
...
Huber
RS with bulk fermions



Total compositeness

ex: minimal RS
Rattazzi-Zaffaroni





$$\frac{g_\rho^2}{m_\rho^2} \bar{l}l\bar{l}l$$



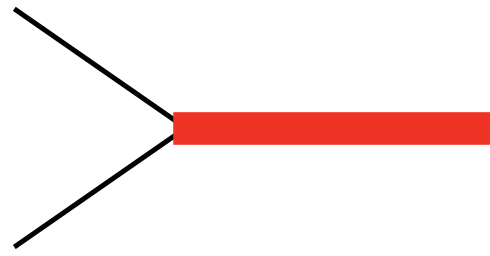
$$m_\rho > g_\rho \times 5 \text{ TeV} \sim \frac{50 \text{ TeV}}{\sqrt{N}}$$

$$\frac{g_\rho^2}{m_\rho^2} \bar{q}q\bar{q}q$$



$$m_\rho > g_\rho \times 3 \text{ TeV} \sim \frac{30 \text{ TeV}}{\sqrt{N}}$$

...and we haven't even broken flavor yet
let us move on!



Wishes ...

Flavor

$$\frac{1}{\Lambda_{UV}^{d_H-1}} H \bar{F} F + \frac{c}{\Lambda_{UV}^2} \bar{F} F \bar{F} F$$

wish d_H as close to 1 as possible

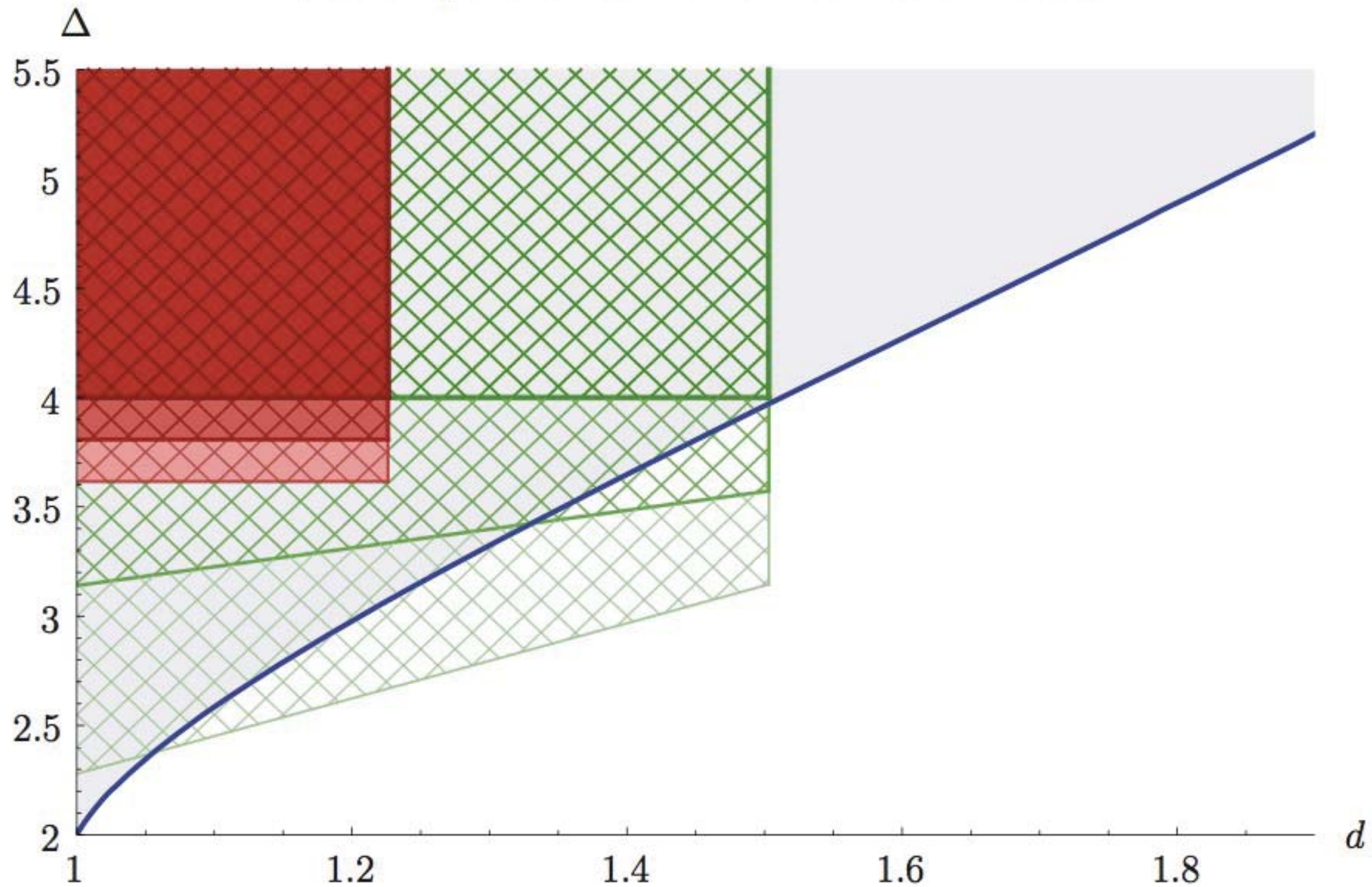
Hierarchy

$$(\Lambda_{UV})^{\Delta-4} H^\dagger H \quad \Delta \equiv \dim(H^\dagger H)$$

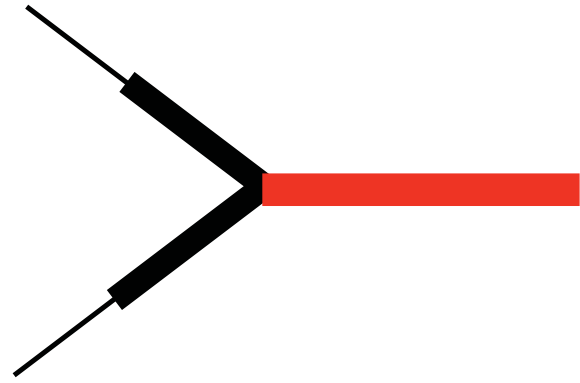
wish $\Delta > 4 - \epsilon$

... Constraints

Viable regions for Conformal Technicolor models



Poland, Simmons-Duffin, Vichi '11



$$\mathcal{L}_{Yukawa} = \epsilon_q^i q_L^i \mathcal{O}_q^i + \epsilon_u^i u_L^i \mathcal{O}_u^i + \epsilon_d^i d_L^i \mathcal{O}_d^i$$

Yukawas

$$Y_u^{ij} \sim \epsilon_q^i \epsilon_u^j g_\rho$$

$$Y_d^{ij} \sim \epsilon_q^i \epsilon_d^j g_\rho$$

$\Delta F=1$

$$\epsilon_q^i \epsilon_u^j g_\rho \times \frac{v}{m_\rho^2} \times \frac{g_\rho^2}{16\pi^2} \bar{q}^i \sigma_{\mu\nu} u^j G_{\mu\nu}$$

$\Delta F=2$

$$\epsilon_q^i \epsilon_d^j \epsilon_q^k \epsilon_d^\ell \times \frac{g_\rho^2}{m_\rho^2} (\bar{q}^i \gamma^\mu d^j) (\bar{q}^l \gamma_\mu d^\ell)$$

Bounds & and perhaps an interesting hint

my thanks to Isidori, Perez, Redi, Weiler

ϵ_k

$$m_\rho \gtrsim 20 \text{ TeV}$$

$\epsilon'/\epsilon, b \rightarrow s\gamma, d_n$

$$m_\rho \gtrsim \frac{g_\rho}{4\pi} \times (20 - 40) \text{ TeV}$$

?

LHCb

CP violation in D decays

$$m_\rho \simeq \frac{g_\rho}{4\pi} \times 10 \text{ TeV}$$

$$\Delta a_{CP} = a_{KK} - a_{\pi\pi} = -(0.82 \pm 0.21 \pm 0.11)\%$$

Curiously 'borderline', though connection with weak scale not too good
Obviously need a composite light Higgs to tune VEV

Tuning

$$\frac{v^2}{f^2} = \left(\frac{g_\rho \times 200 \text{ GeV}}{m_\rho} \right)^2 \lesssim 10^{-2}$$

$$\mu \rightarrow e\gamma$$

$$\frac{\sqrt{m_\mu m_e}}{m_\rho^2} \bar{\mu} \sigma_{\alpha\beta} e F^{\alpha\beta}$$

MEG: $\text{Br}(\mu \rightarrow e \gamma) < 2.4 \times 10^{-12}$

$$m_\rho \gtrsim 10^3 \text{ TeV}$$

Partial compositeness clearly cannot be the full story

Must assume strong sector possesses some flavor symmetry

Range of
possibilities



$$U(1)_e \times U(1)_\mu \times (1)_\tau$$

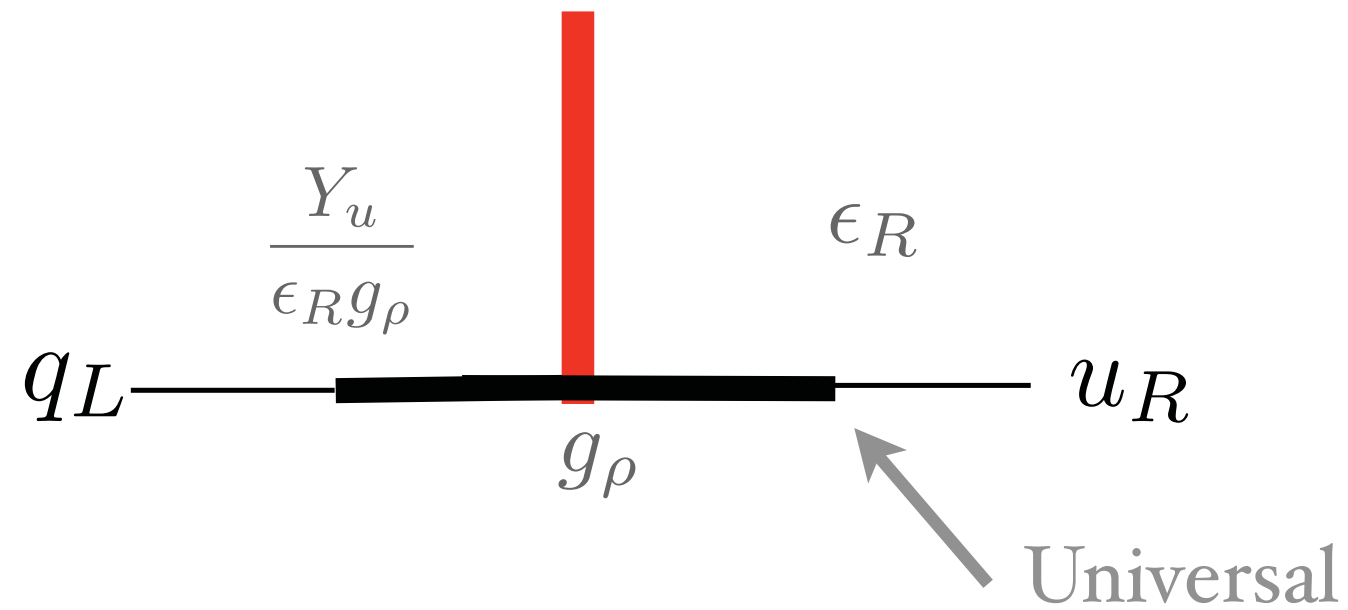
...

$$SU(3) \times SU(3) \times \dots$$

Basically the only case where it makes sense to invoke MFV

Redi, Weiler '11

Weiler's talk

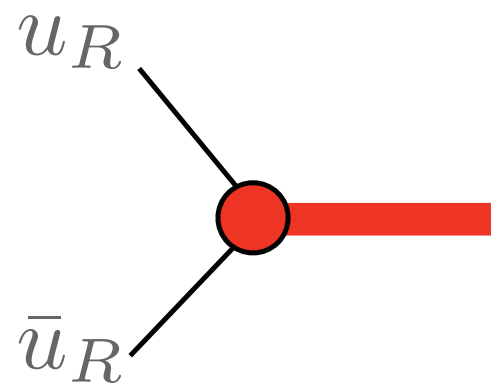


Observed m_t



$$\epsilon_R \gtrsim \frac{1}{g_\rho} > 0.1$$

Predict sizeable effects in right handed quarks



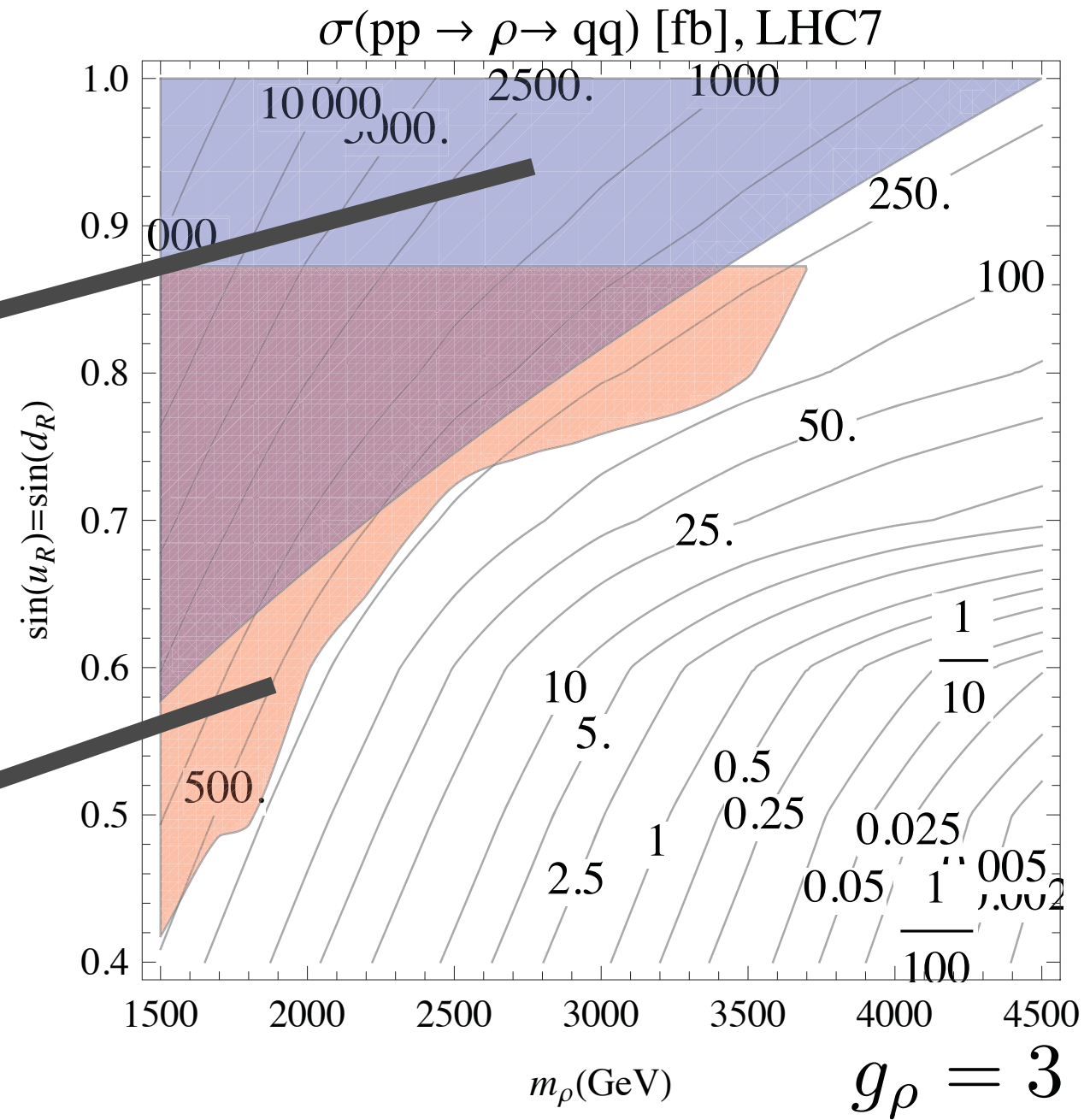
all possible resonances (Ex. massive gluon)

LHC7 bounds already relevant:

Di-jet bounds 35/pb

CMS-EXO-11-015
1/fb

Expected signals in di-jet.



General properties of ‘Strongly Coupled EWSB’

&

LHC Phenomenology

TeV

..... g'
..... ρ

broadly described by

$$m_\rho \quad g_\rho$$
$$m_\rho \sim g_\rho f$$
$$g_\rho \sim \frac{4\pi}{\sqrt{N}}$$

Redi's talk

top partners
lonely weirdo's
(ex. scalar octet, why not?)

see Dobrescu

100 GeV

$W_L^\pm, Z_L^0 + \star$

$q, \ell, \gamma, W_T, Z_T, g$

Composite

Elementary

◆ Technicolor $SO(4)/SO(3)$: ★ =nothing

Not feeling too well

◆ pseudo-NG Higgs $SO(5)/SO(4)$: ★ = h $W_L^\pm, Z_L^0, h \rightarrow \begin{pmatrix} H^+ \\ H_0 \end{pmatrix}$

extended cosets $SO(6)/SO(5)$, $SO(6)/SO(4) \times U(1)$, ... : additional light scalars

◆ pseudo-dilaton: ★ = χ does **not** fit in $SU(2)$ doublet

The main advantage of pseudo-NG Higgs

Manton '79
Hosotani '84

Georgi, Kaplan '84

Arkani-Hamed, Cohen, Katz, Nelson '02

Agashe, Contino, Pomarol '04

....

$$\hat{S} = \hat{S}_{TC} \times \frac{v^2}{f^2}$$

f = Goldstone decay const

EWPT are OK with mild tuning
(or maybe by Little Higgs mech)

$$\frac{v^2}{f^2} \sim 0.1 - 0.3$$

$$\epsilon_3 = \hat{S} \sim \frac{m_W^2}{m_\rho^2} \rightarrow 10^{-3}$$

Resonances still in the few-TeV-range

Collider Signals of Composite Higgs

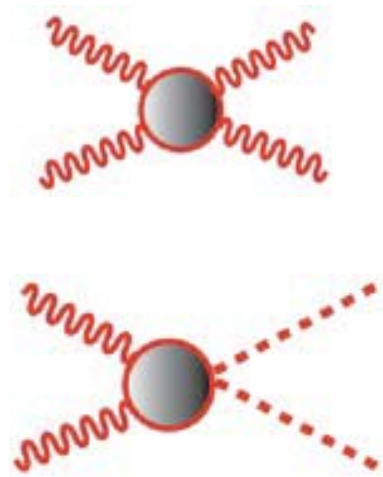
I) Direct

❖ production of resonances

(can be effectively modeled by 5D holographic realizations, or by deconstruction)

❖ strong scattering

Zeppenfeld



$$\left. \begin{array}{l} \text{LHC with } > 100 \text{ fb}^{-1} \\ \text{LHC with } > 300 \text{ fb}^{-1} \end{array} \right\} \frac{v^2}{f^2} > 0.3$$
$$\text{CLIC more realistically } \frac{v^2}{f^2} > 0.01$$

Contino, Grojean, Moretti, Pappadopulo, Piccinini, RR, Thamm '10 + to appear

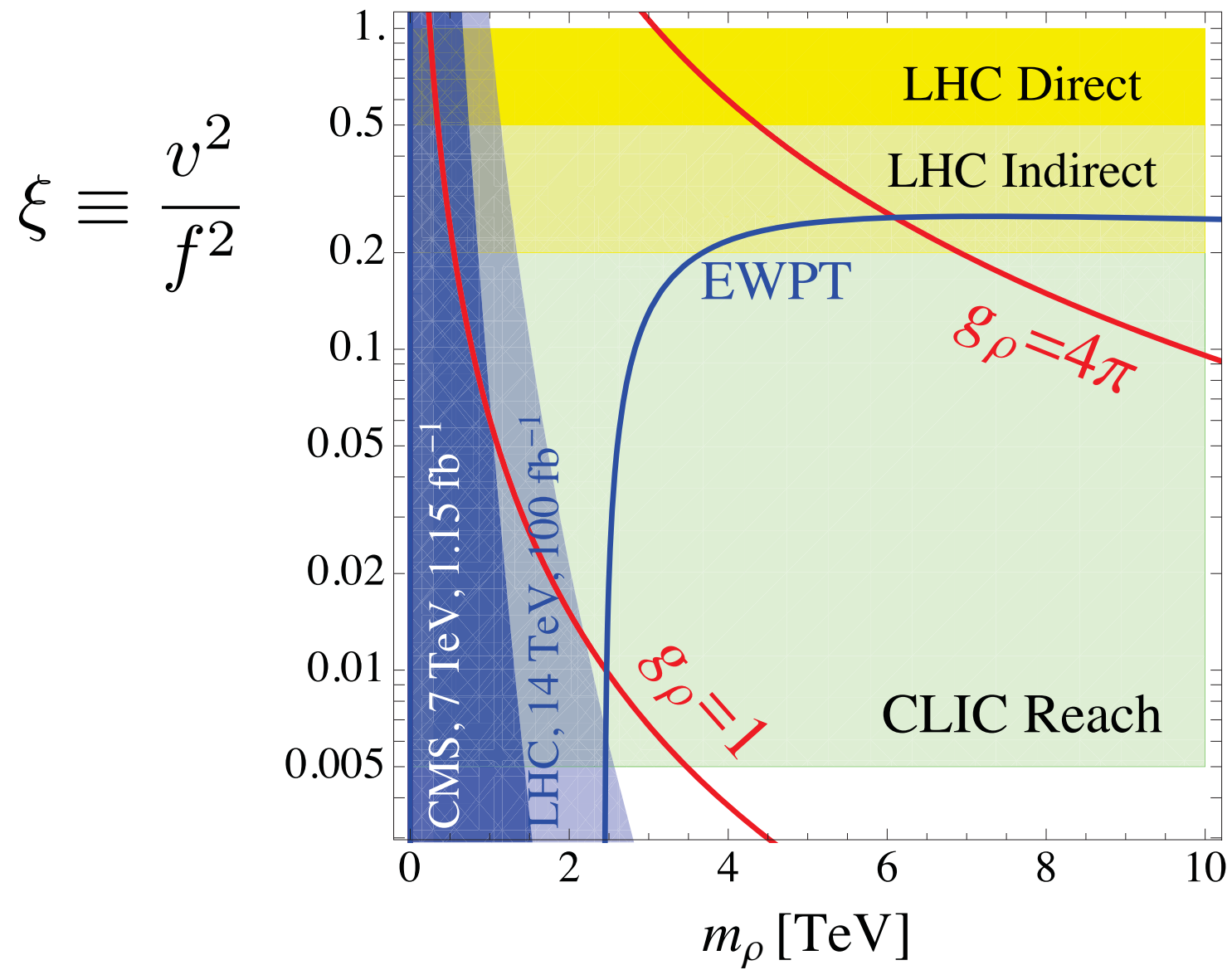
II) Indirect: $O(v^2/f^2)$ deviations from the Standard Model in Higgs production rates and branching ratios

Giudice, Grojean, Pomarol, Rattazzi 07

$$q \rightarrow \rho \leftarrow \bar{q} = \frac{g_W^2}{g_\rho} \ll g_W$$

$$\rho \rightarrow W_L W_L = g_\rho$$

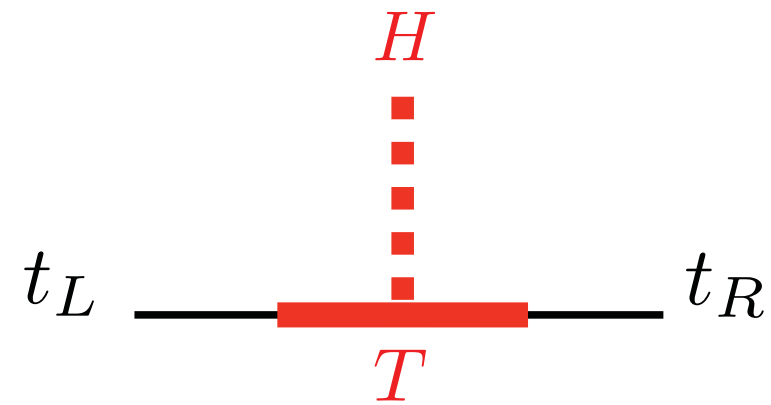
Weiler's talk



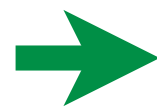
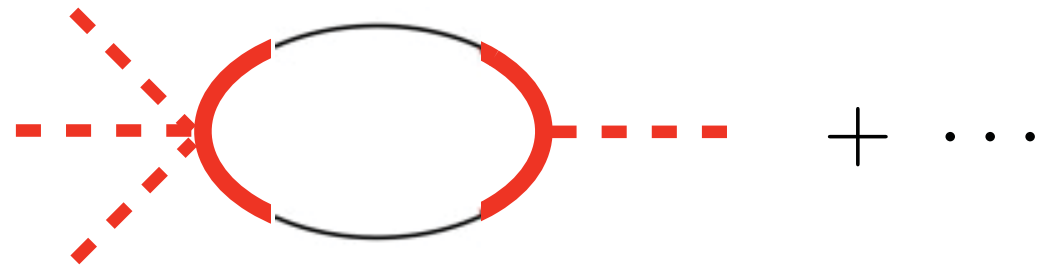
$$m_\rho \sim g_\rho f$$

m_h, m_t and colored resonances

talks by Redi & by Wulzer

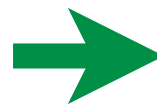


$$y_t \sim \frac{y_L y_R f}{M_T}$$



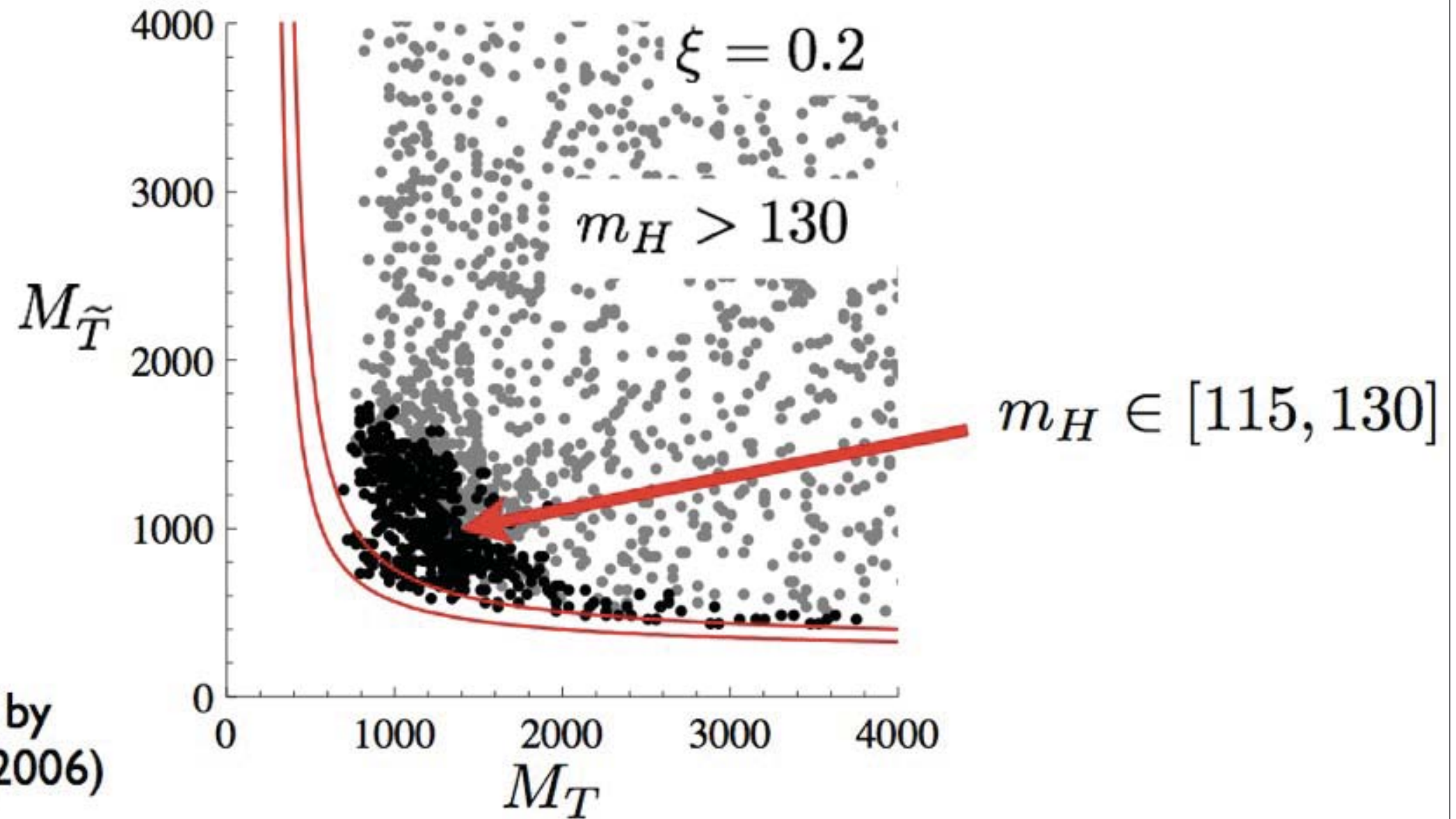
$$m_h \sim m_t \frac{M_T}{\pi f}$$

$$m_h < 130 \text{ GeV}$$



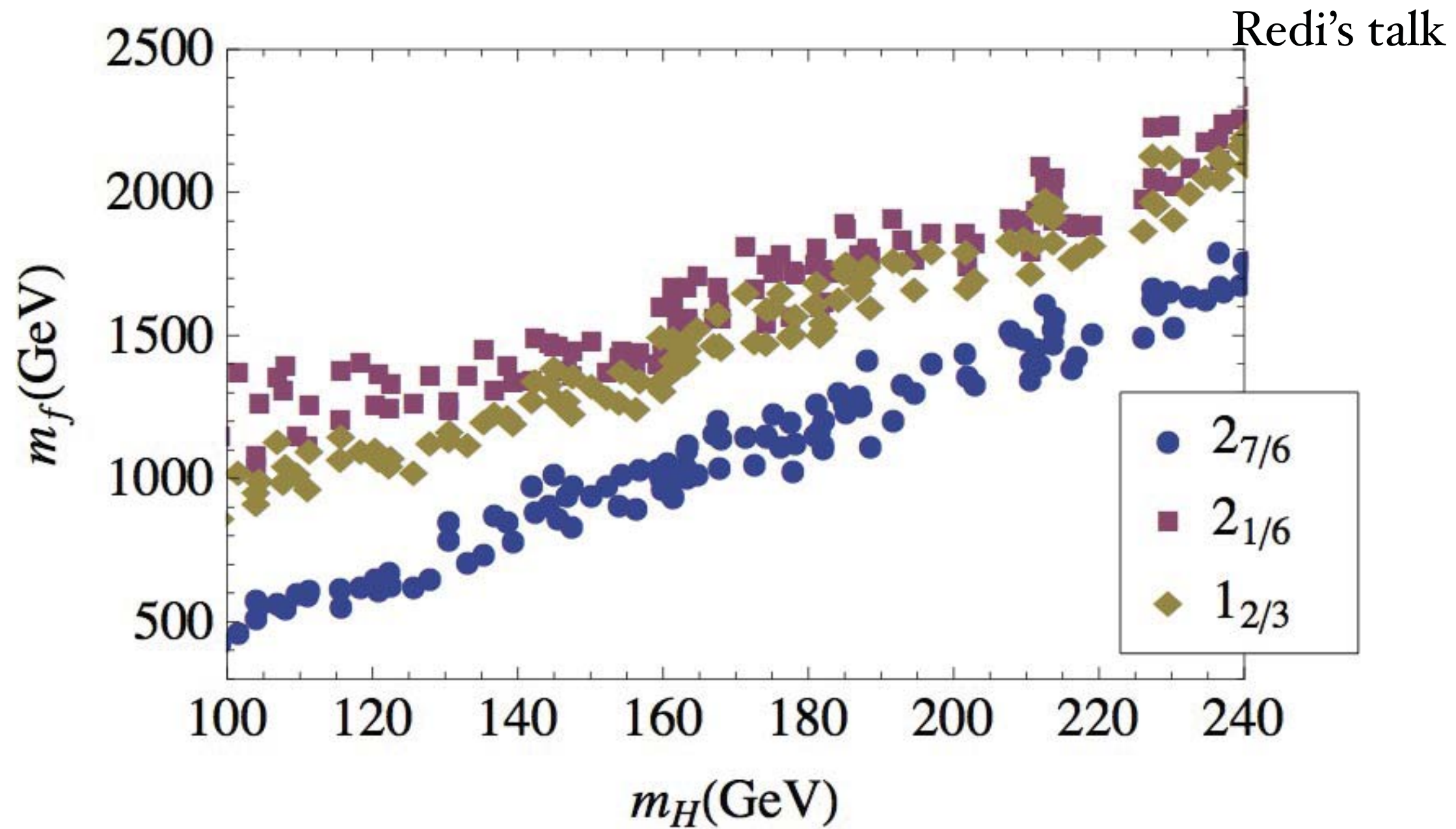
$$M_T \lesssim 1 \text{ TeV} \left(\frac{0.5}{\frac{v}{f}} \right)$$

Light Higgs wants Light Partners :



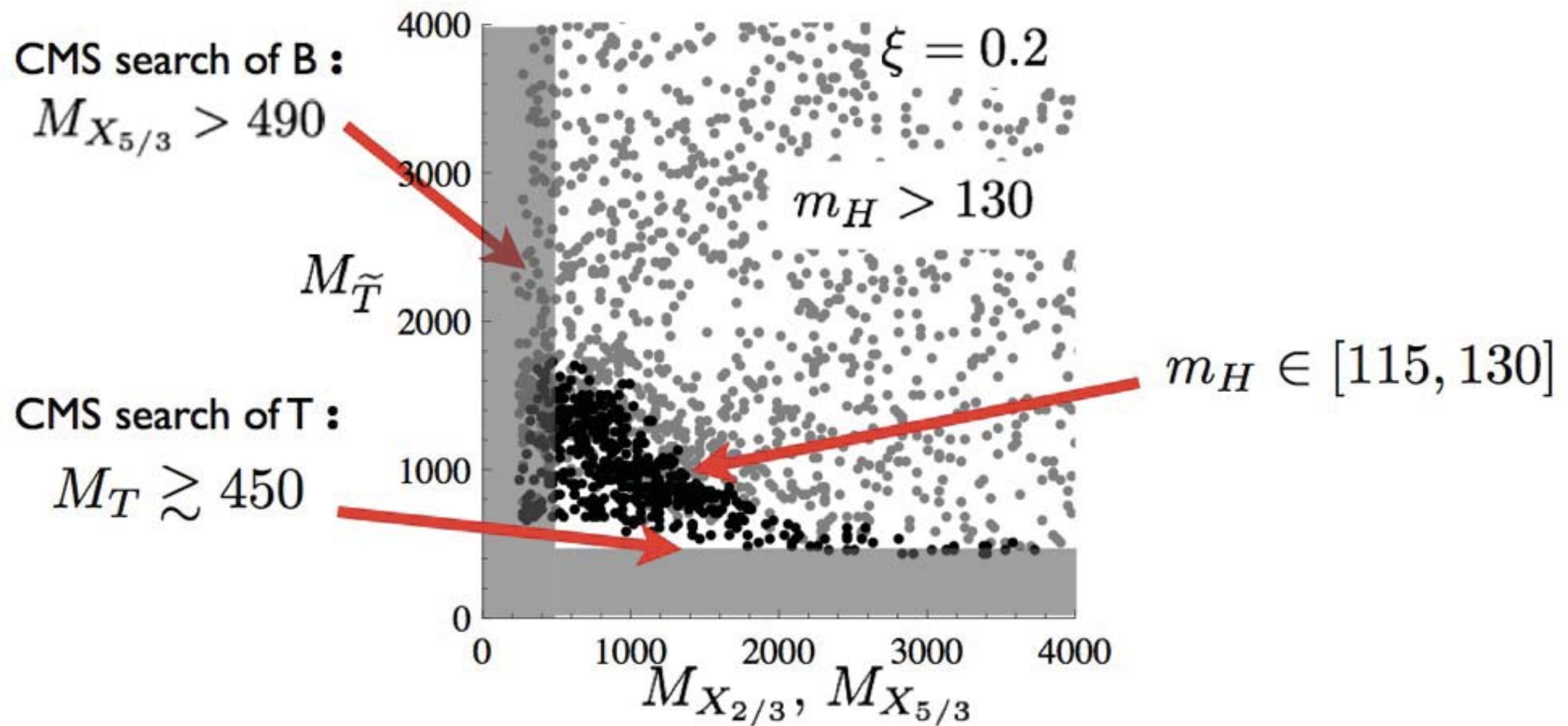
First noticed by
Contino et. al (2006)

Wulzer & Panico

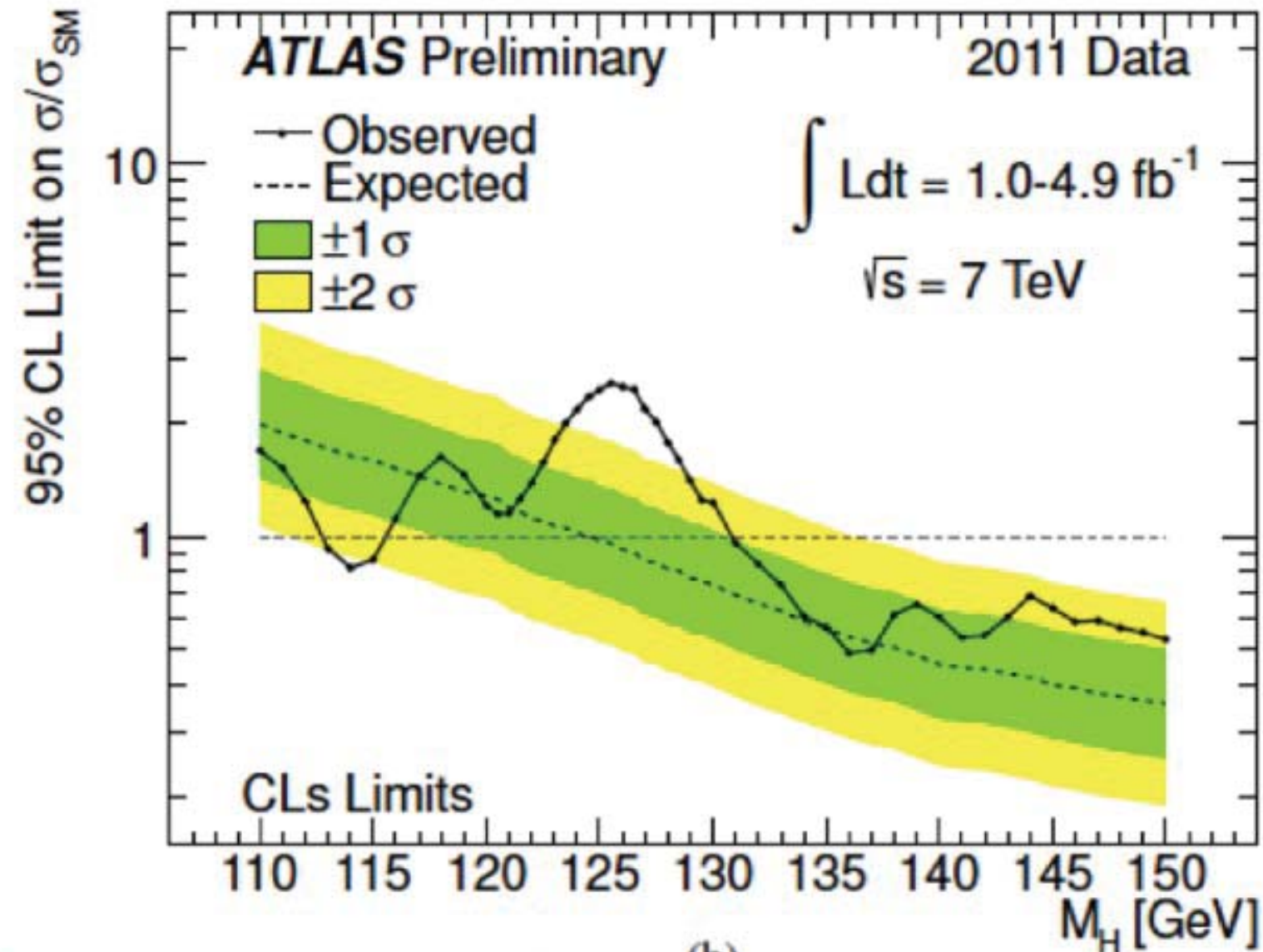


Would be interesting to explore m_h - m_f correlation in 'nicer' models, if they exist

LHC has **already probed** part of this plot :



Contino, Servant '08
Mrazek, Wulzer '09



(b)

Observed excess over SM for $m_H \sim 126$ GeV in:
 $H \rightarrow \gamma\gamma$ (2.8σ), $H \rightarrow ZZ^* \rightarrow 4l^\pm$ (2.1σ), $H \rightarrow WW^* \rightarrow l\nu l\nu$ (1.4σ).

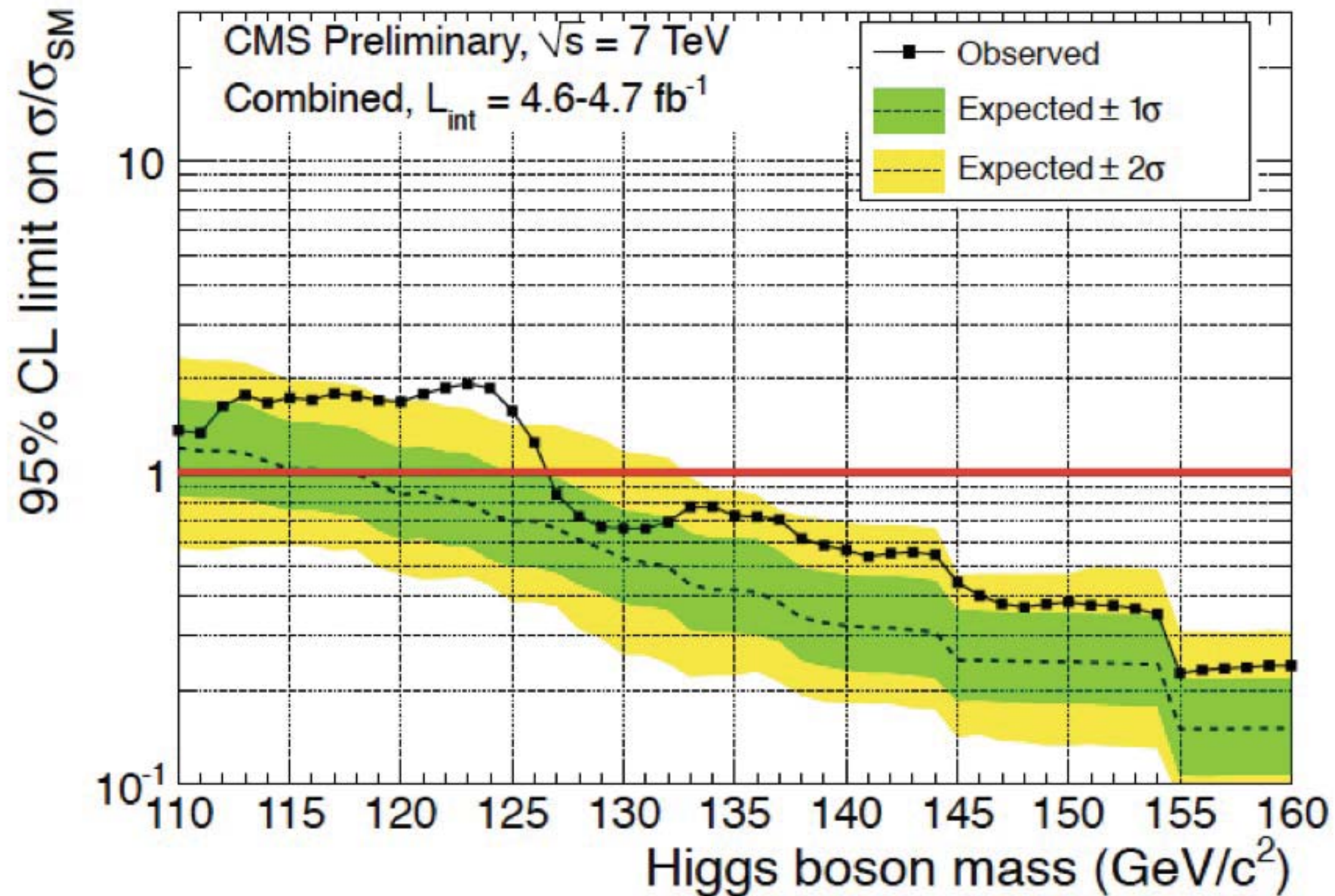
Combined: 3.6σ (but with look-elsewhere-effect 2.3σ)

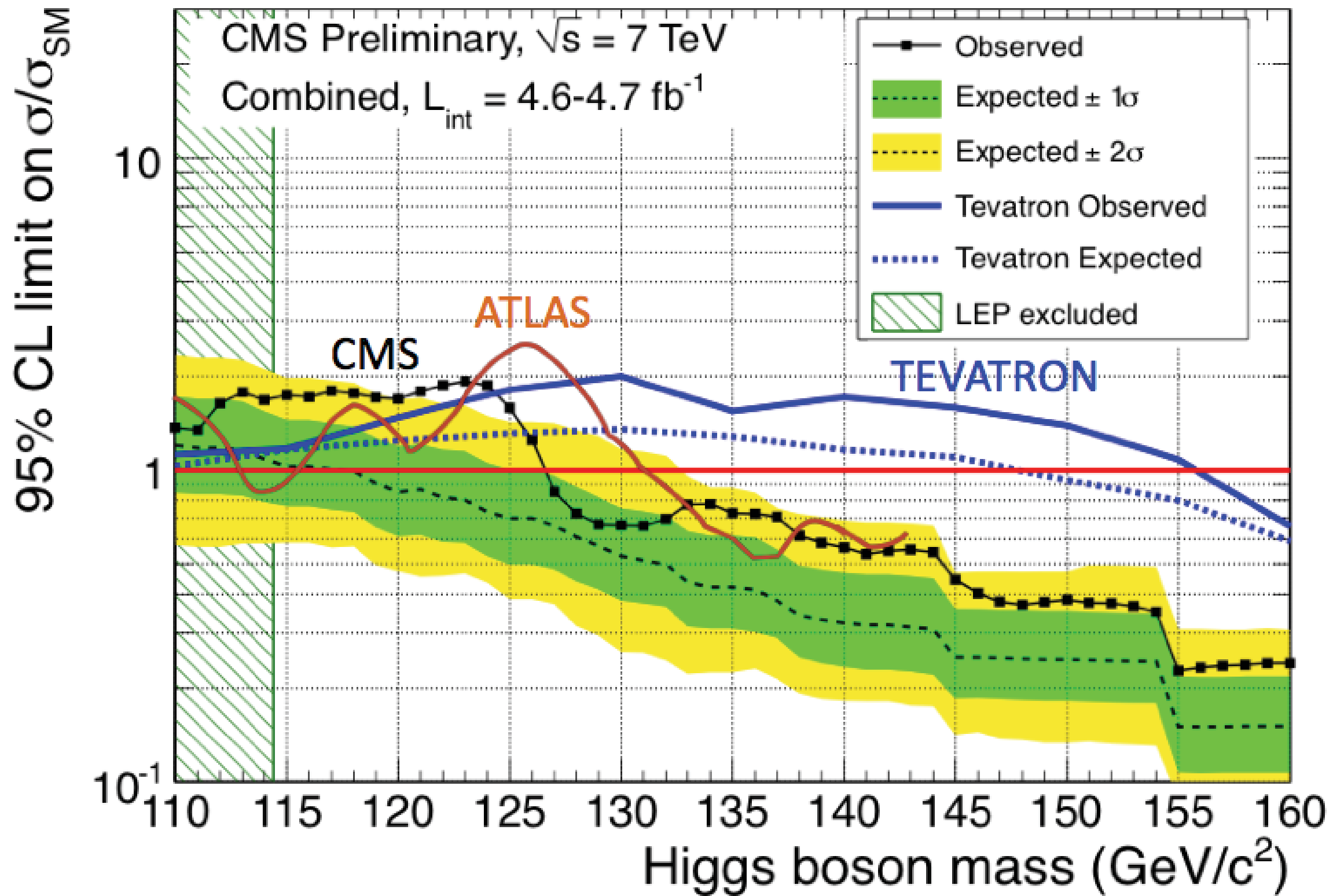


The most obvious "elsewhere" is CMS



Also in CMS there is an excess, but smaller (2.6σ)





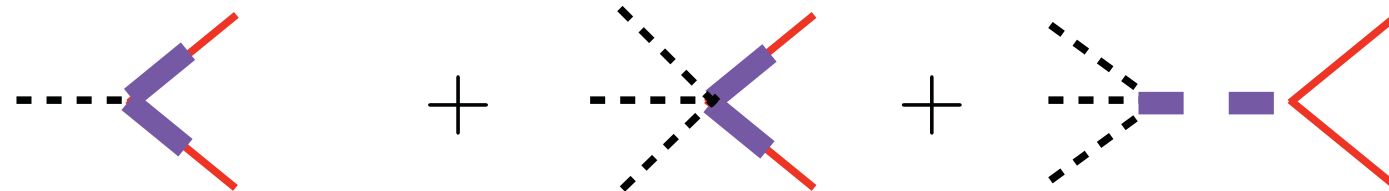
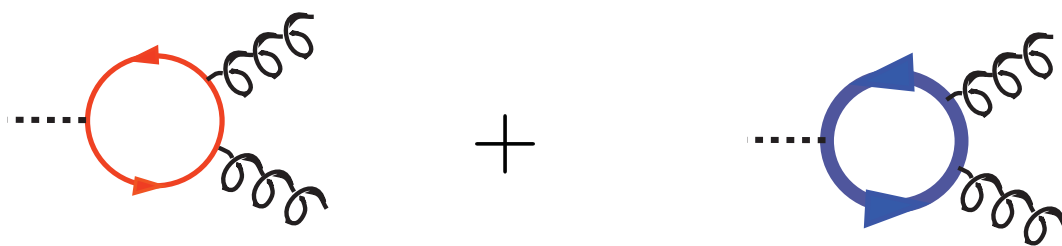
Higgs-mantics



Divination through Higgs

The **more** natural the theory the **more** the Higgs rates deviate from SM

$$\delta m_H^2 = \text{---} \text{---} \text{---} \text{---} \text{---} + \text{---} \text{---} \text{---} \text{---} \text{---} \sim 0$$

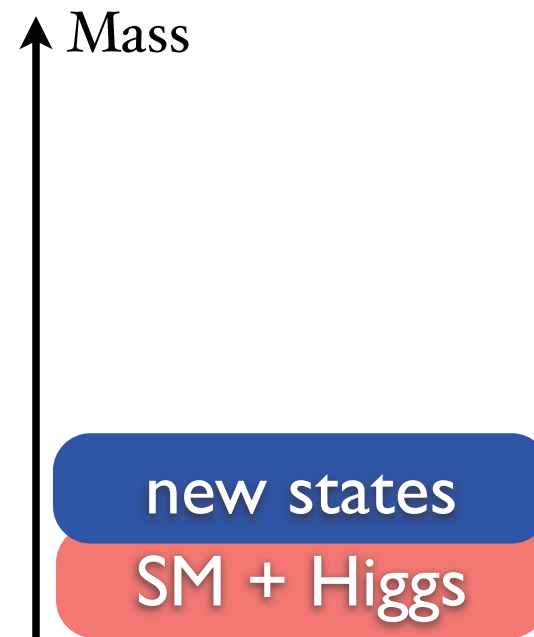


 = first probes into EWSB dynamics and into hierarchy puzzle

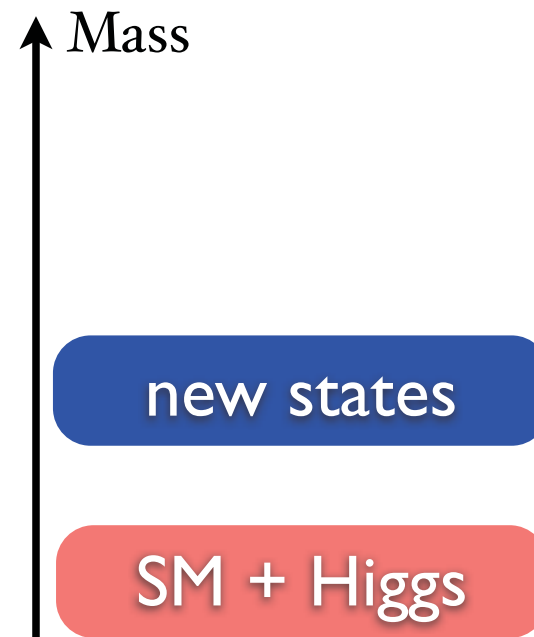
$115 \text{ GeV} \lesssim m_h \lesssim 130 \text{ GeV}$

lucky range to measure all couplings

It would be useful to develop a ‘Higgs diagnostic’: associate the possible patterns of deviation to broad/specific features of the underlying theory



Can use effective lagrangian to describe deviations from SM
= simple parametrization encompassing a large class of models



Can use effective lagrangian to describe deviations from SM
= simple parametrization encompassing a large class of models

General parametrization of *Higgslike scalar* h

Contino, Grojean, Moretti, Piccinini, RR '10

$$\begin{aligned}\mathcal{L} &= \frac{1}{2}(\partial_\mu h)^2 + \frac{M_V^2}{2} \text{Tr}(V_\mu V^\mu) \left[1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} + \dots \right] - m_i \bar{\psi}_{Li} \left(1 + c \frac{h}{v} \right) \psi_{Ri} + \text{h.c.} \\ &+ \frac{1}{2} m_h^2 h^2 + d_3 \frac{1}{6} \left(\frac{3m_h^2}{v} \right) h^3 + d_4 \frac{1}{24} \left(\frac{3m_h^2}{v^2} \right) h^4 + \dots \\ &+ c_g \frac{\alpha_s}{4\pi} \frac{h}{v} G_{\mu\nu} G^{\mu\nu} + c_\gamma \frac{\alpha}{4\pi} \frac{h}{v} F_{\mu\nu} F^{\mu\nu}\end{aligned}$$

c flavor universal in minimal flavor violating set up

◆ Standard Model: $a = b = c = d_3 = 1$ $c_g = c_\gamma = 0$

◆ $h =$ pseudo-Goldstone implies additional constraints

$SO(5)/SO(4)$ Pseudo-Goldstone Higgs

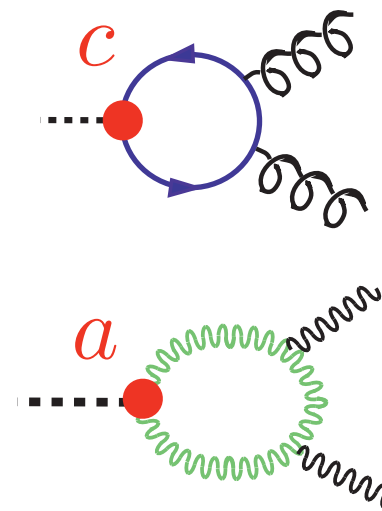
Agashe, Contino, Pomarol '04

$$a = \sqrt{1 - v^2/f^2} \quad b = 1 - 2v^2/f^2 \quad \text{model independent}$$

$$\left. \begin{aligned} c = d_3 &= \sqrt{1 - v^2/f^2} && \text{fermions in 4} \\ c = d_3 &= \frac{1 - 2v^2/f^2}{\sqrt{1 - v^2/f^2}} && \text{fermions in 5} \end{aligned} \right\} \text{model dependent}$$

$$c_g, c_\gamma \sim \frac{\alpha_t}{4\pi} \quad \text{controlled by small explicit } SO(5) \text{ breaking}$$

NEGLIGIBLE!



Interesting
inequalities

$$0 \leq a, |b| \leq 1$$

robust

$$0 < c < 1$$

in range favored by EWPT

In specific models just one free parameter $\xi \equiv \frac{v^2}{f^2}$

In general 4 parameters a, c_t, c_b, c_τ

$$\frac{\Gamma(h \rightarrow gg)}{\Gamma(h \rightarrow gg)|_{SM}} = \frac{\Gamma(h \rightarrow t\bar{t})}{\Gamma(h \rightarrow t\bar{t})|_{SM}} = c_t^2$$

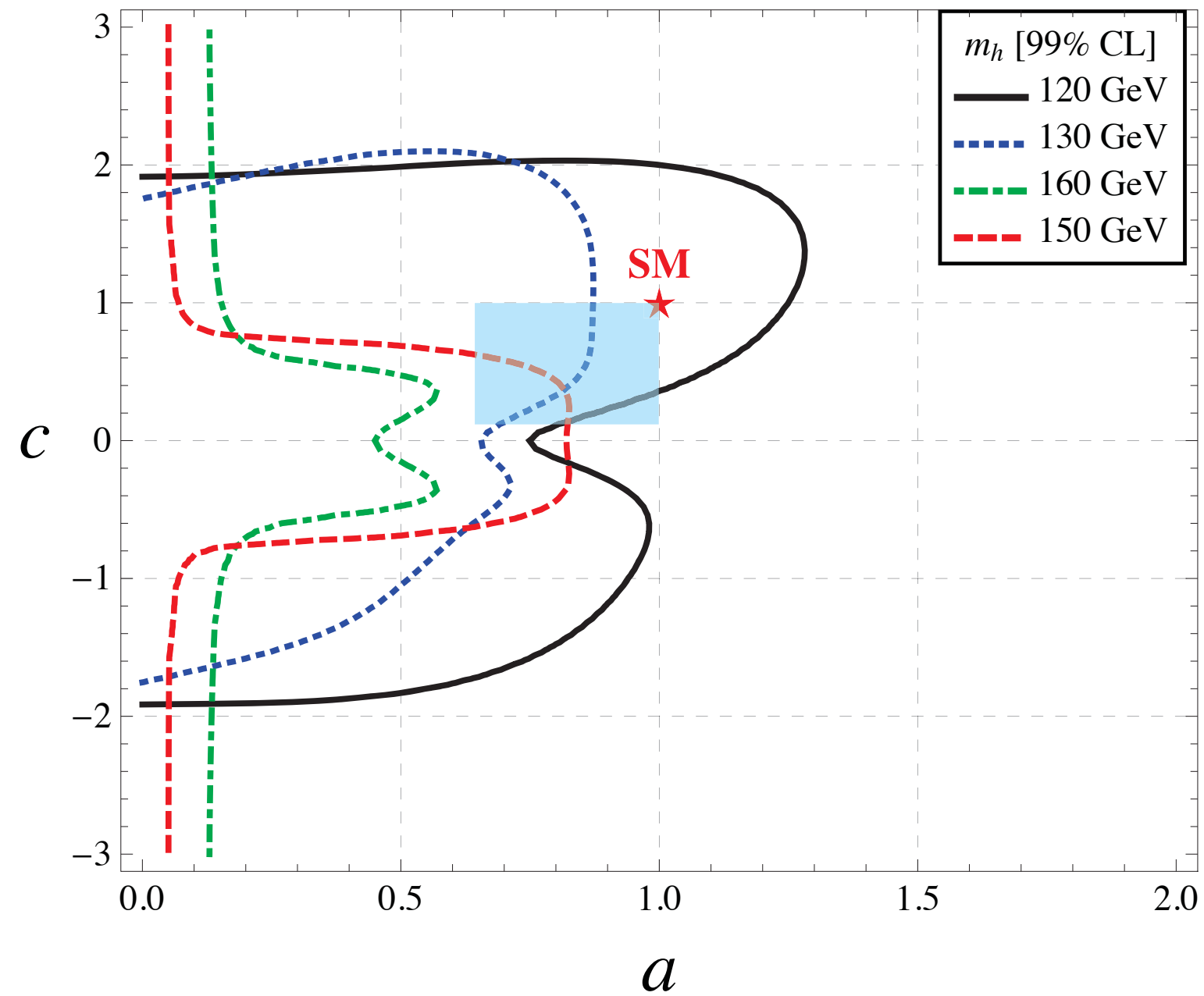
$$\frac{\Gamma(h \rightarrow f\bar{f})}{\Gamma(h \rightarrow f\bar{f})|_{SM}} = c_f^2$$

$$\frac{\Gamma(h \rightarrow \gamma\gamma)}{\Gamma(h \rightarrow \gamma\gamma)|_{SM}} = a^2 [1 + 0.28(1 - c_t/a)]^2 \sim a^2$$

$$\frac{\Gamma(h \rightarrow VV)}{\Gamma(h \rightarrow VV)|_{SM}} = a^2$$

In the preferred range all rates are reduced

Exclusion using CMS data [$\leq 4.7 \text{ fb}^{-1}$]



$$c_t = c_b = c_\tau \equiv c$$

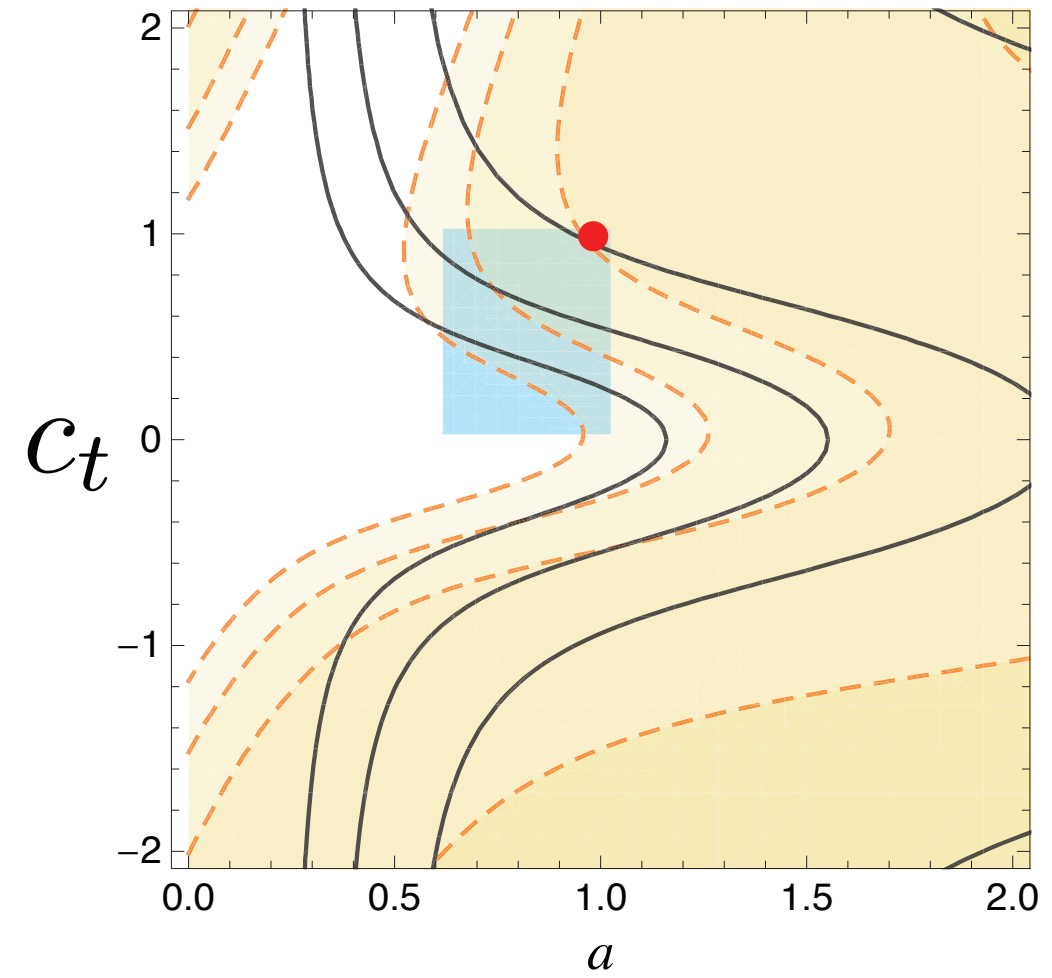
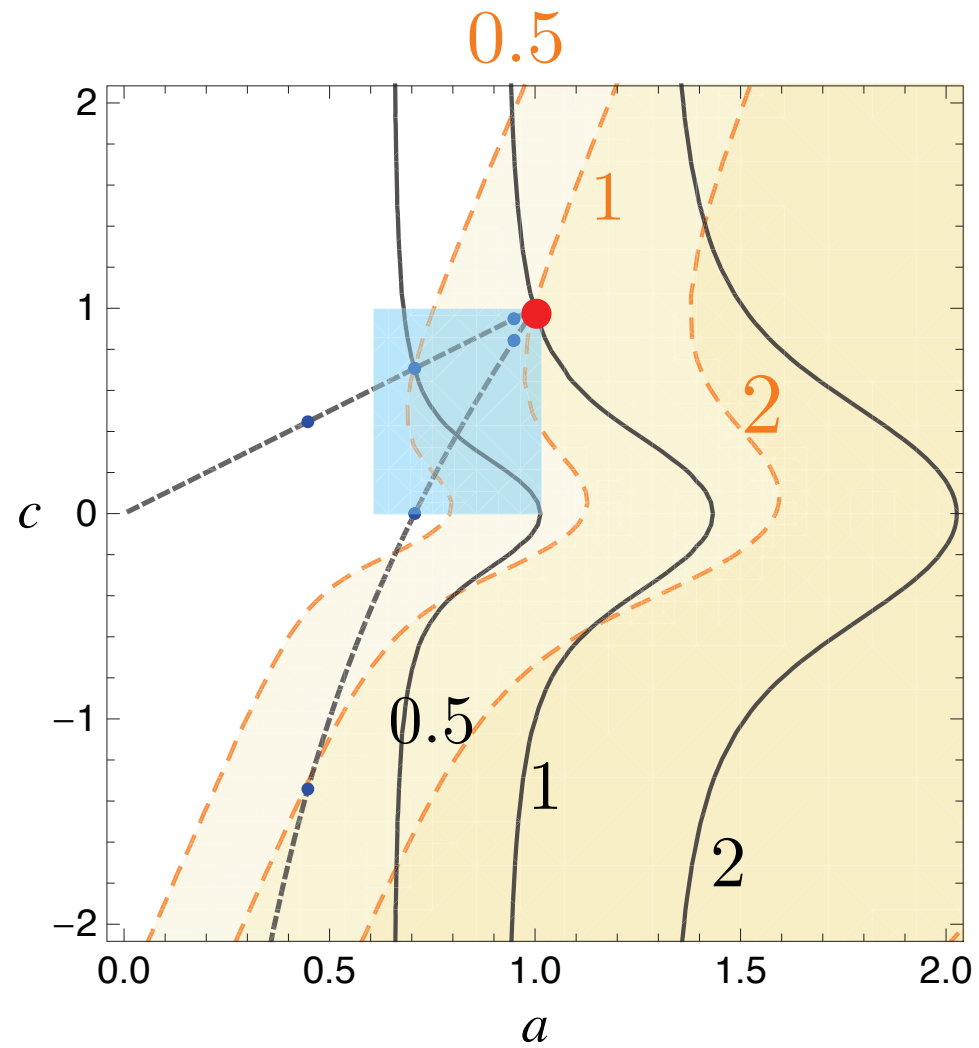
Azatov, Contino, Galloway to appear

R_{ZZ} —————

$R_{\gamma\gamma}$ - - - - -

$m_h = 125 \text{ GeV}$

Contino's talk



$$c_t = c_b = c_\tau \equiv c$$

$$c_b = c_\tau = 0.4$$

Can increase $R_{\gamma\gamma}$, but at the price of R_{bb}

$$\frac{v^2}{f^2} \ll 1$$

SILH effective lagrangian

$$\mathcal{L}_{eff} = \frac{c_H}{2f^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) + y_f \frac{c_y}{f^2} H^\dagger H \bar{\psi}_L H \psi_R - \frac{c_6 \lambda}{f^2} (H^\dagger H)^3$$

$$0 \leq a, b, c \leq 1$$

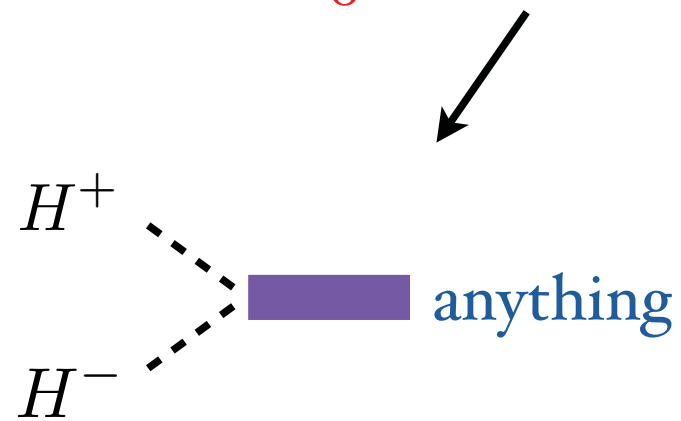
$$c_H, c_y > 0$$

true in larger class
including Little Higgs

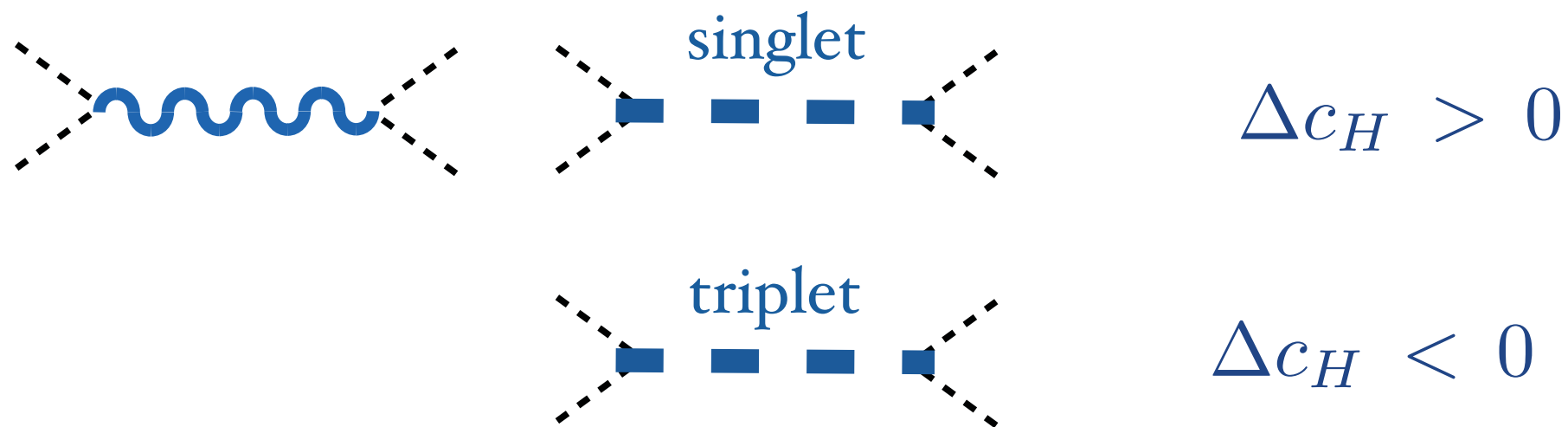
A dispersion relation for c_H

Low, Rattazzi, Vichi '09

$$c_H = \frac{f^2}{\pi} \int_0^\infty (\sigma_{+-}(s) - \sigma_{++}(s)) \frac{ds}{s}$$



c_H not positive definite, but almost so

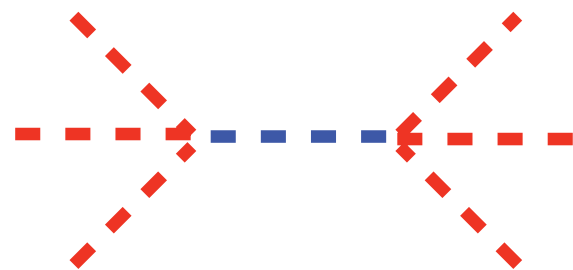


Scalar triplets do not dominate in known models addressing hierarchy

An exercise in Higgs diagnostic

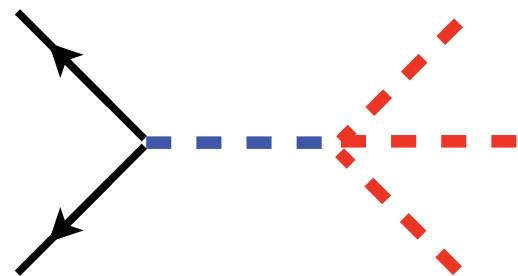
————— $H' = -\cos \beta H_2 + \sin \beta H_1$

————— $H = \cos \beta H_1 + \sin \beta H_2$

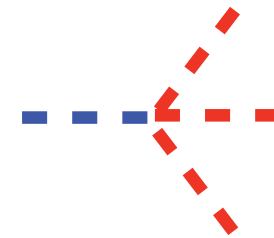


$\Delta c_H = 0$

dim 8 operator: quick decoupling in $h \gamma \gamma$ and $h W W$



sign depends on structure of quartic



MSSM

$(H_1^2 - H_2^2)^2$

$c_b > 1$

$c_t < 1$

Hall, Pinner, Ruderman '11

NMSSM

$H_1^2 H_2^2$

$c_b < 1$

$c_t > 1$

Other roads to increase Higgs couplings

Dilaton

$$\left\{ \begin{array}{l} a = \sqrt{b} = c = \frac{v}{f_D} \\ d_3 = \frac{5}{3} \frac{v}{f_D} + O(\epsilon) \\ c_g, c_\gamma = O(v/f_D) \end{array} \right. \quad \begin{array}{l} a, b, c \lesssim 1 \\ \\ \text{Yamawaki's talk} \end{array}$$

Non-Compact
coset space

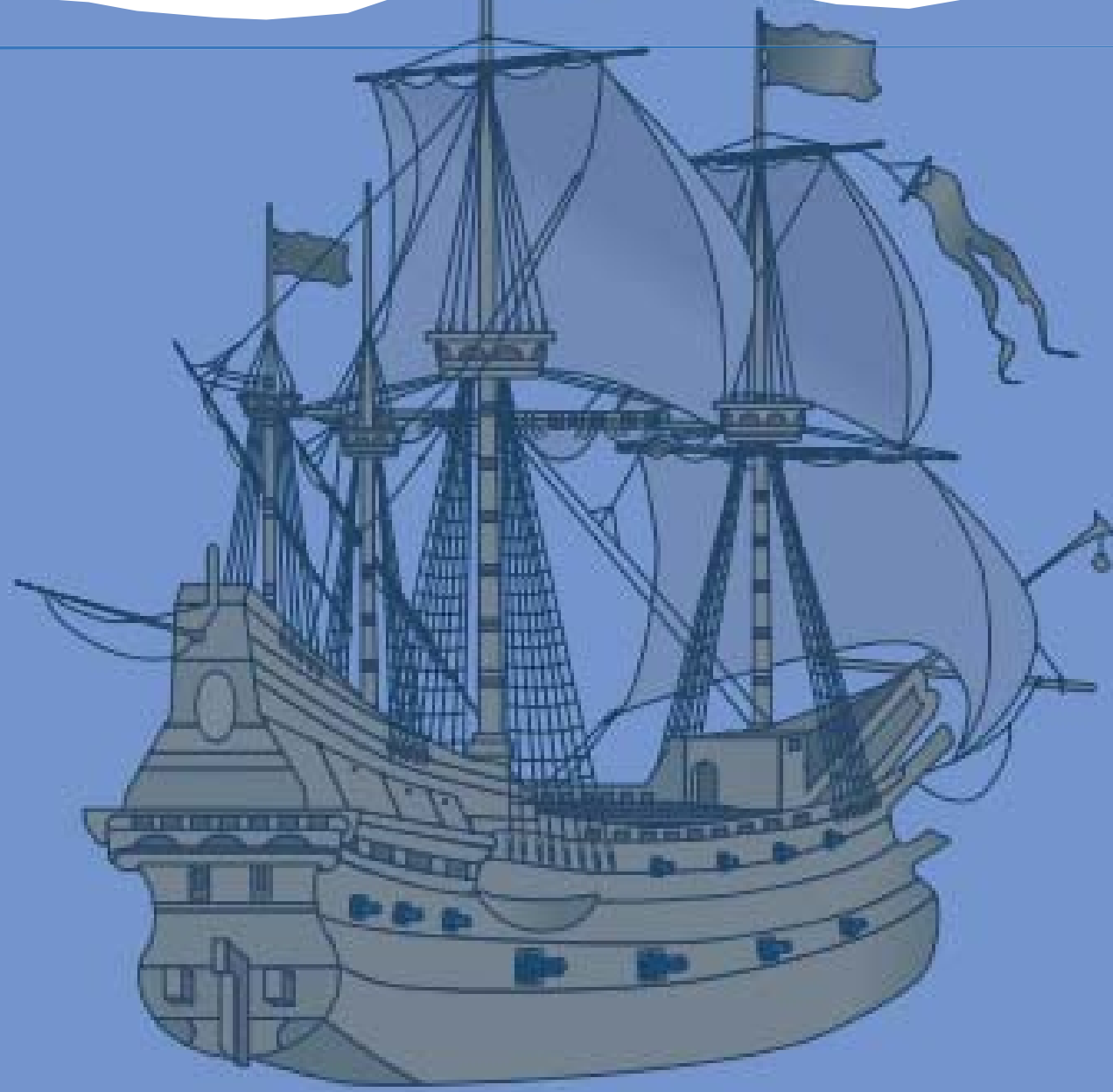
$$H \in SO(4, 1)/SO(4)$$

$$\left\{ \begin{array}{l} \frac{v^2}{f^2} \rightarrow -\frac{v^2}{f^2} \\ a = \sqrt{1 + v^2/f^2} \quad b = 1 + 2v^2/f^2 \end{array} \right. \quad \begin{array}{l} \text{Low's talk} \\ \\ \end{array}$$

No Unitary QFT as UV completion \rightarrow TeV scale Quantum Gravity ?



Higgs

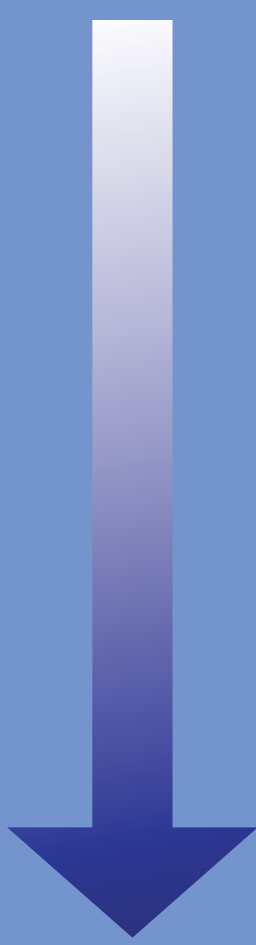


Natural Theory



Higgs

unNatural
Theory

- 
- RG extrapolation
 - speculation
 - move to Ising model

