



**The Abdus Salam  
International Centre for Theoretical Physics**



**2419-5**

**Workshop on Large Scale Structure**

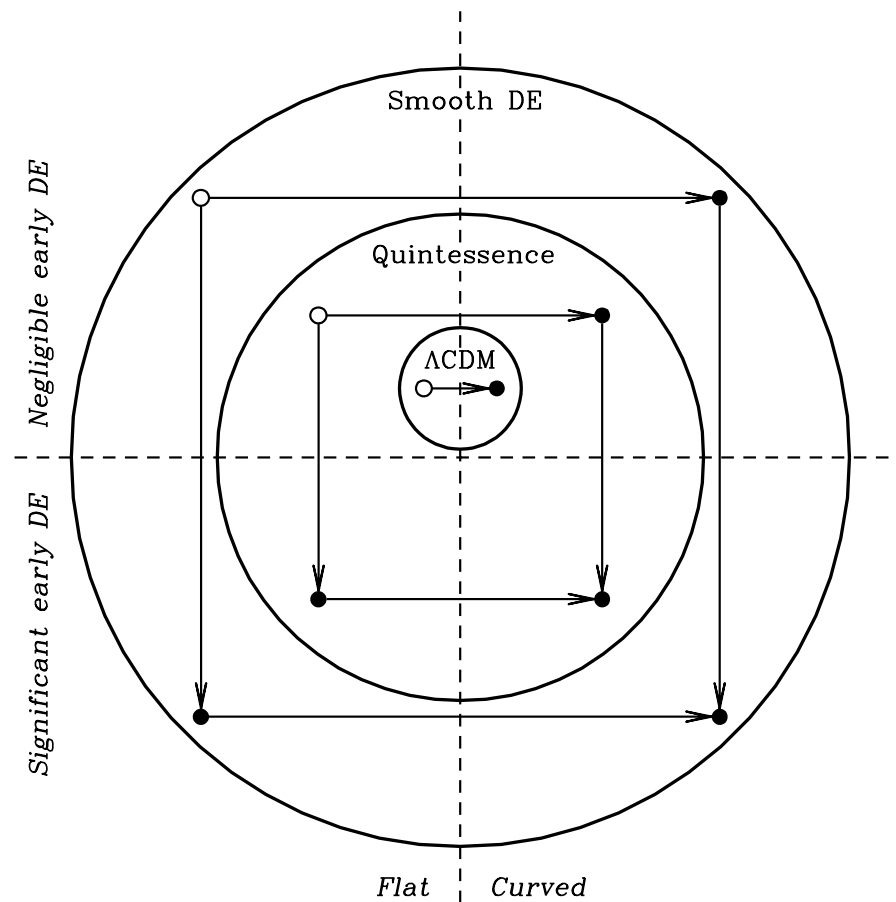
*30 July - 2 August, 2012*

**Falsifying LambdaCDM with clusters**

D. Huterer  
*University of Michigan*

# Falsifying LCDM with Galaxy Clusters

(and with future data in general)



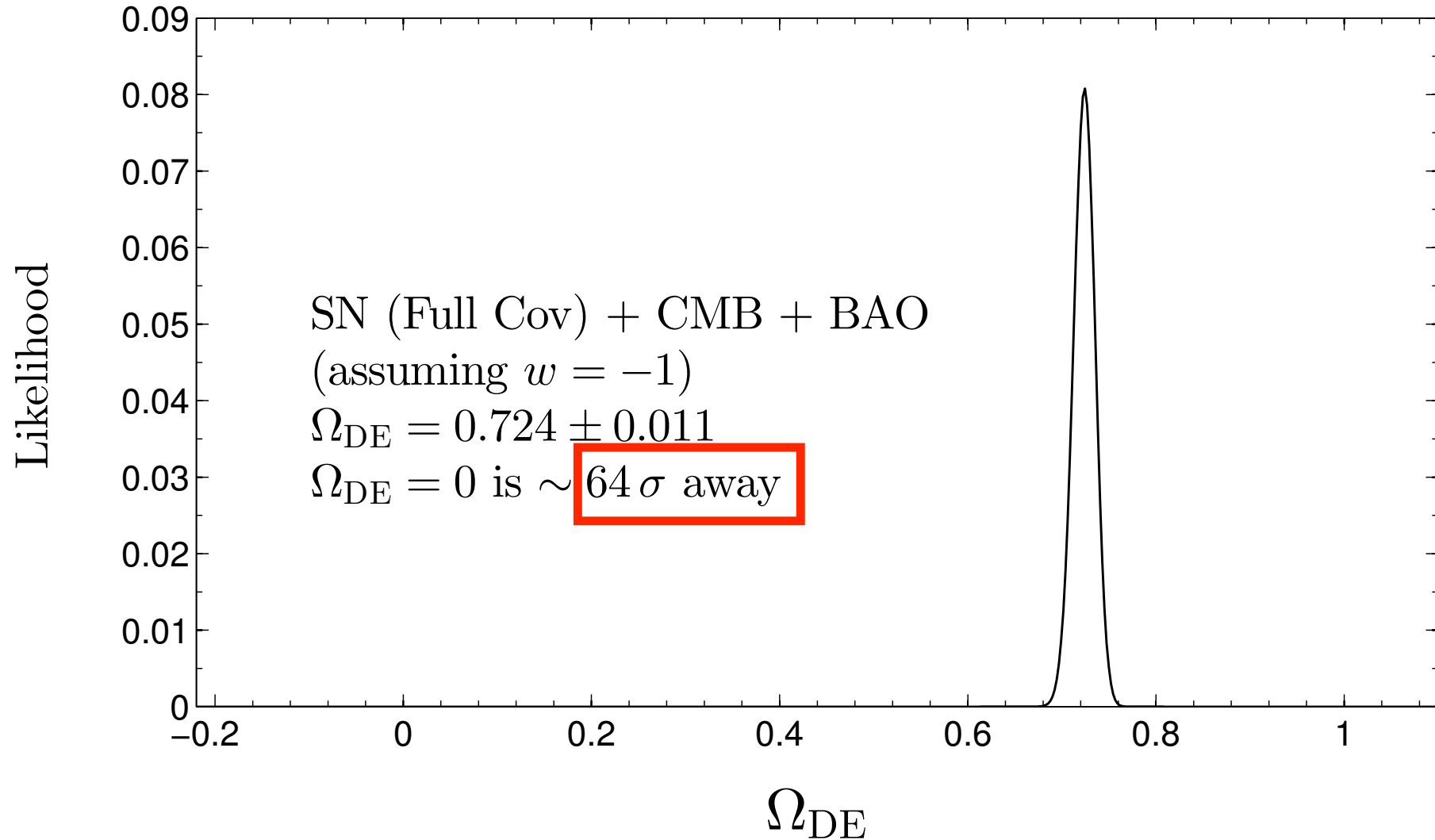
Dragan Huterer (University of Michigan)

Collaborators:

**Michael Mortonson** (Ohio State), Wayne Hu (Chicago)

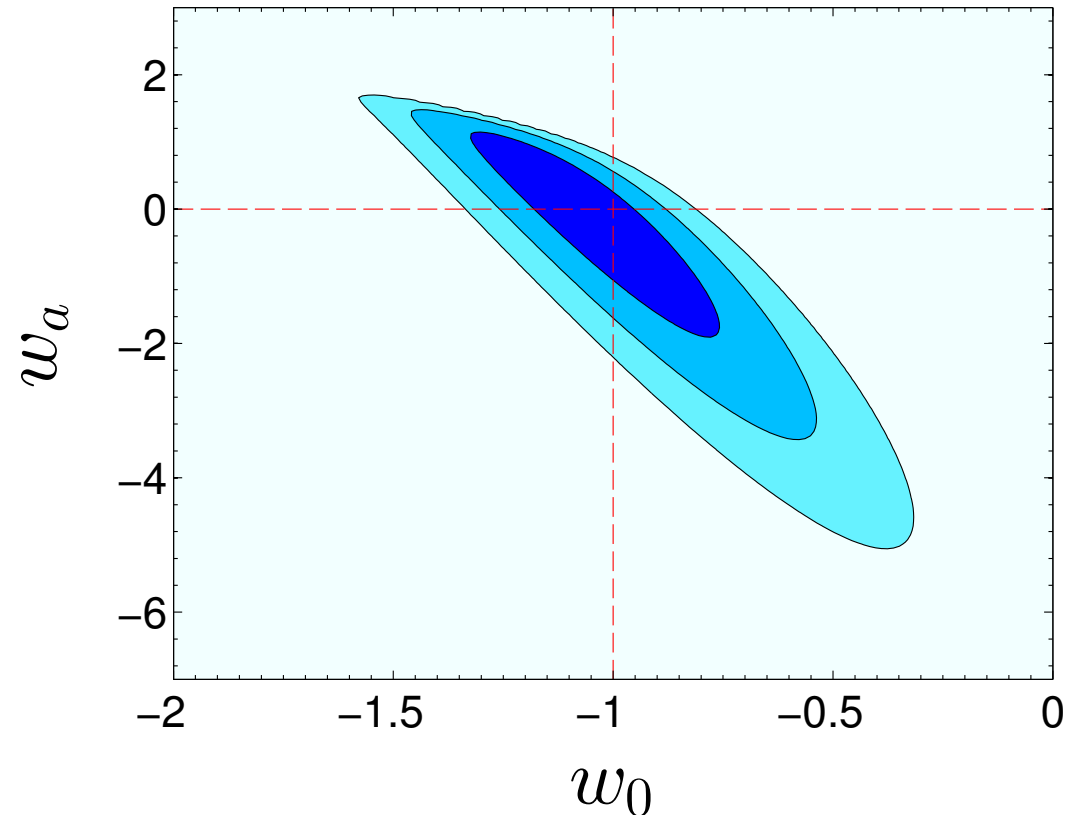
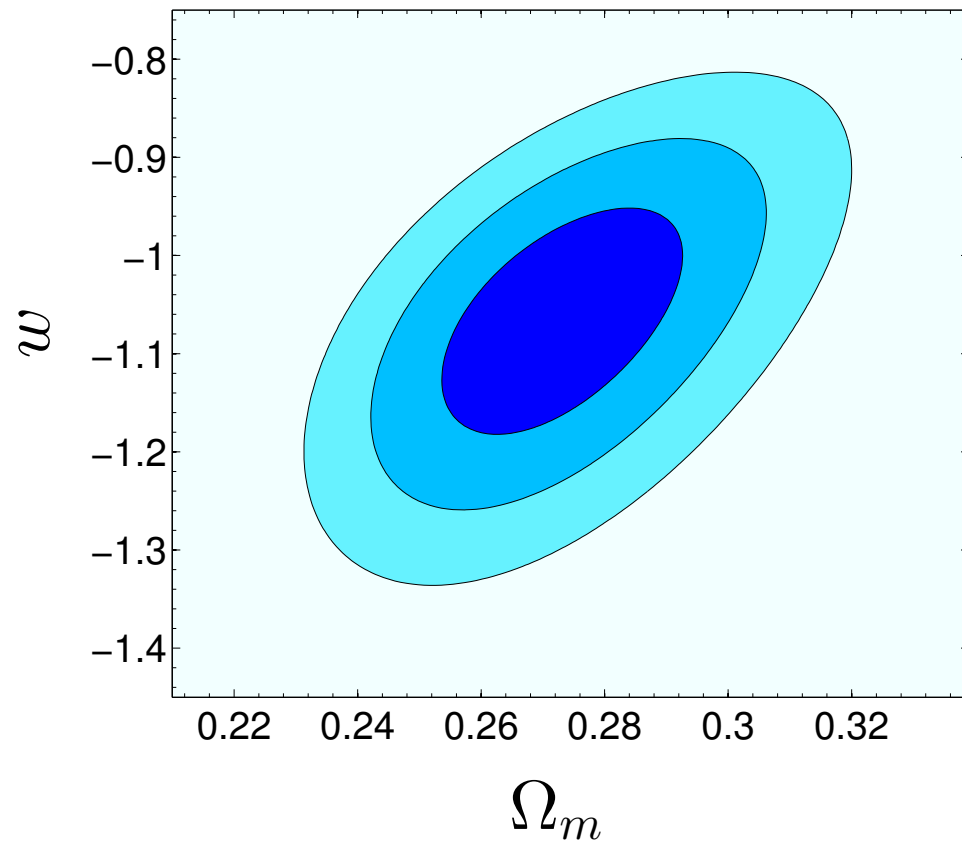
Eduardo Ruiz, Dan Shafer (Michigan)

# Current evidence for dark energy is impressively strong



Since the discovery of acceleration,  
constraints have converged to  $w \approx -1$

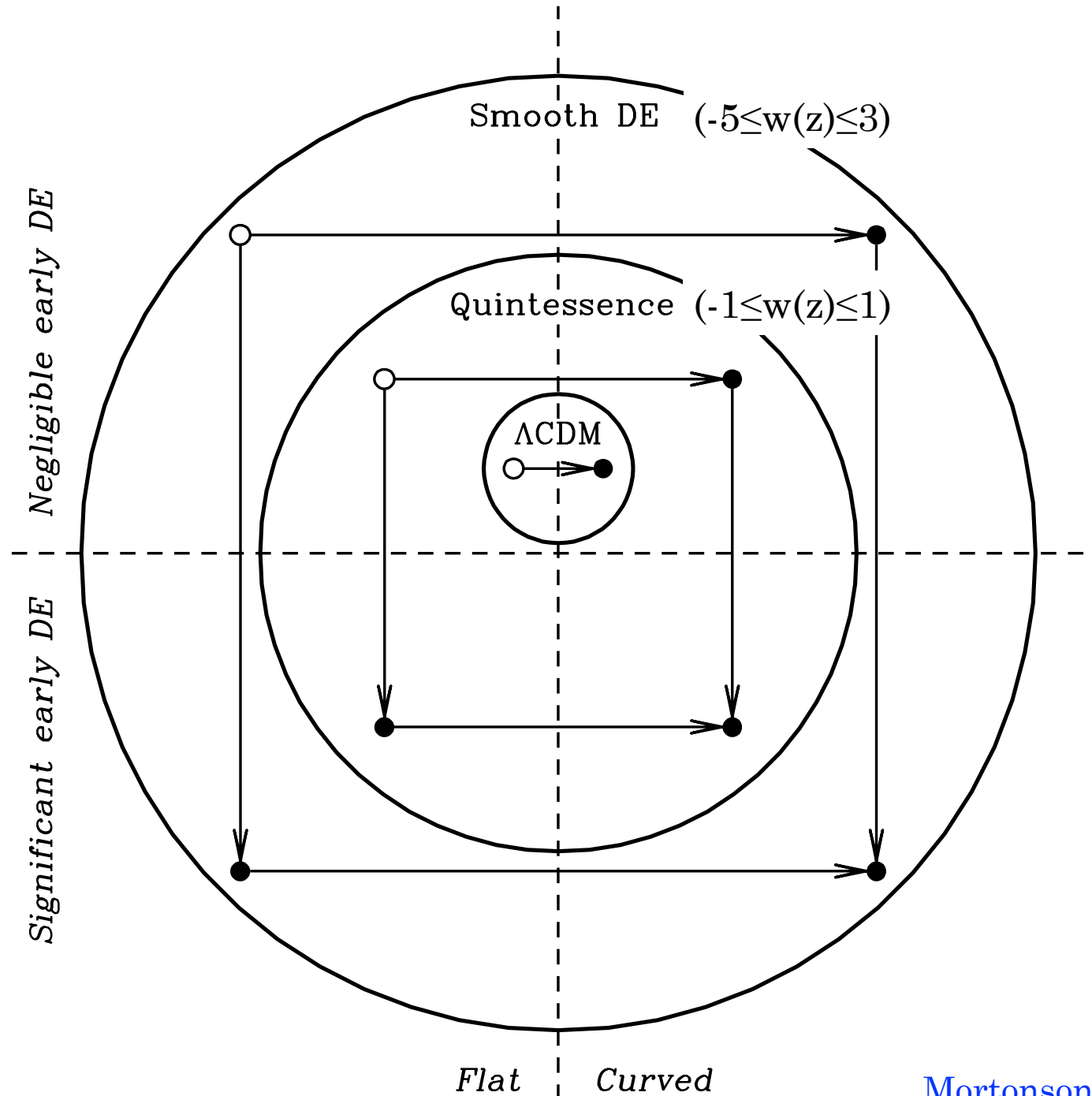
SN + BAO + CMB



# Underlying Philosophy

- The data are now consistent with  $\Lambda$ CDM, but that may change.
- So, **what observational strategies** do we use to determine which violation of Occam's Razor has the nature served us?
- Possible alternatives:  **$w(z) \neq -1$ , early DE, curvature  $\neq 0$ , modified gravity**, more than one of the above (?!)
- **Goal: to calculate predicted ranges in fundamental cosmological functions**  $D(z)$ ,  $H(z)$ ,  $G(z)$ , (and any other parameters/functions of interest), given current or future observations
- **... and therefore to provide 'target' quantities/redshifts** for ruling out classes of DE models with upcoming data (BigBOSS, DES, LSST, Euclid, .....)

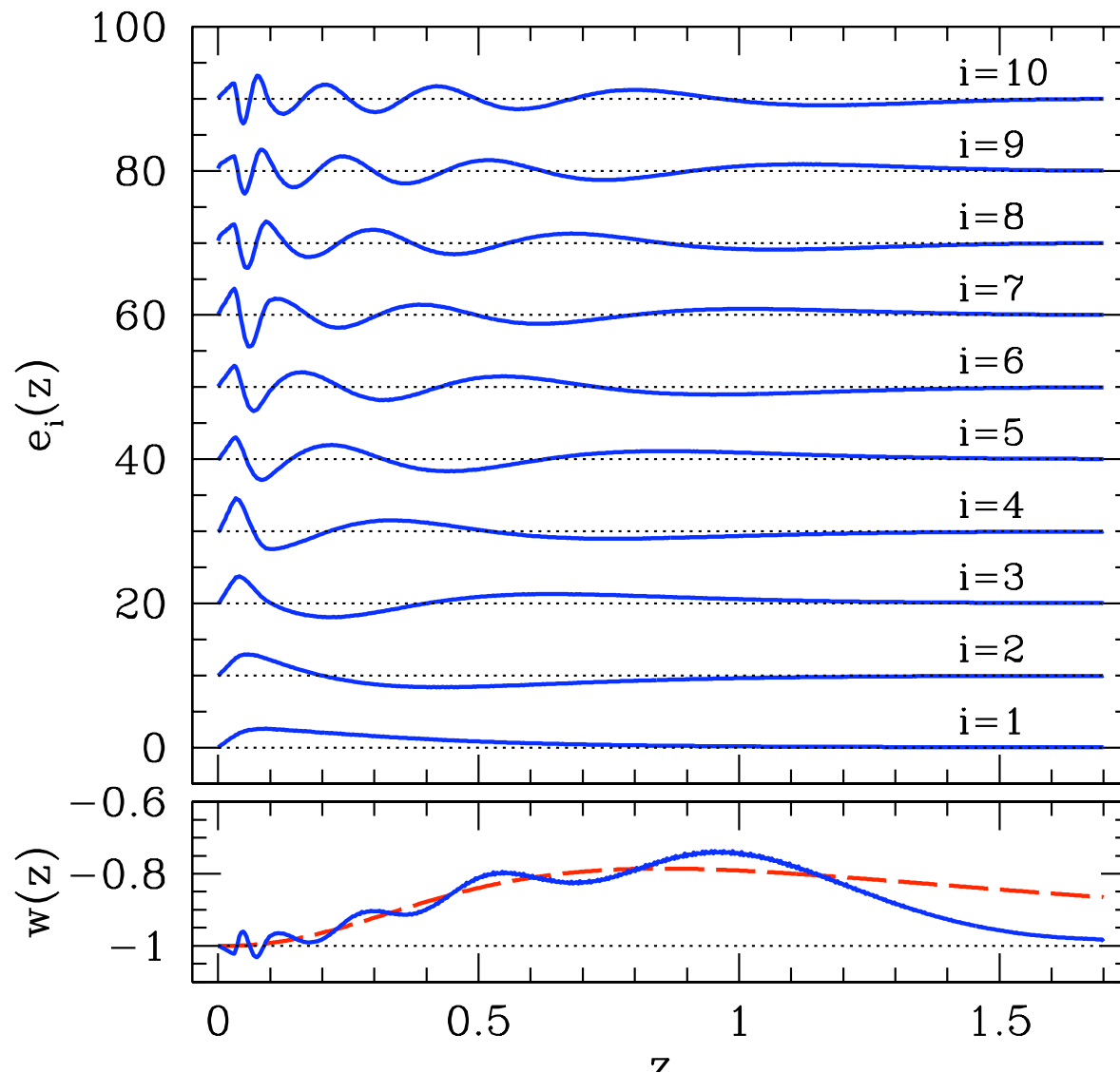
# DE Models and their complexity



# Modeling of DE

Modeling of low- $z$   $w(z)$ :  
Principal Components

$$w(z_j) = -1 + \sum_{i=1}^N \alpha_i e_i(z_j)$$



500 bins (so 500 PCs)  
 $0.03 < z < 1.7$

We use first  $\sim 10$  PCs;  
(results converge  $10 \rightarrow 15$ )

Fit of a **quintessence**  
model with **PCs**

# Methodology

1. Start with the parameter set:

$$\Omega_{\text{M}}, \Omega_{\text{K}}, H_0, w(z), w_{\infty}$$

-2. Use either the current data or future data  
(current = Union2 + WMAP + BAO<sub>z=0.35</sub> + H<sub>0</sub>)

3. Employ the likelihood machine

Markov Chain Monte Carlo likelihood calculation,  
between ~2 and ~15 parameters constrained

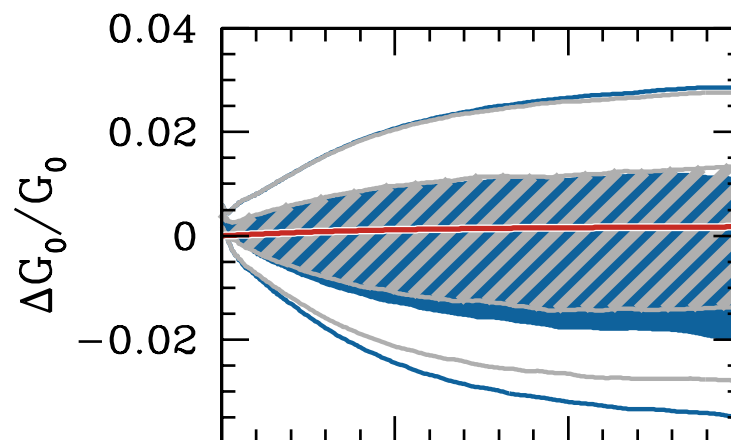
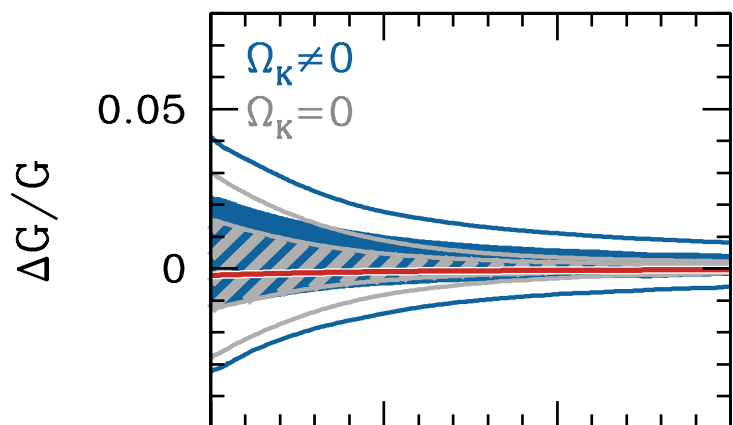
4. Compute predictions for D(z), G(z), H(z) (and  $\gamma(z)$ , f(z))



Current  
data

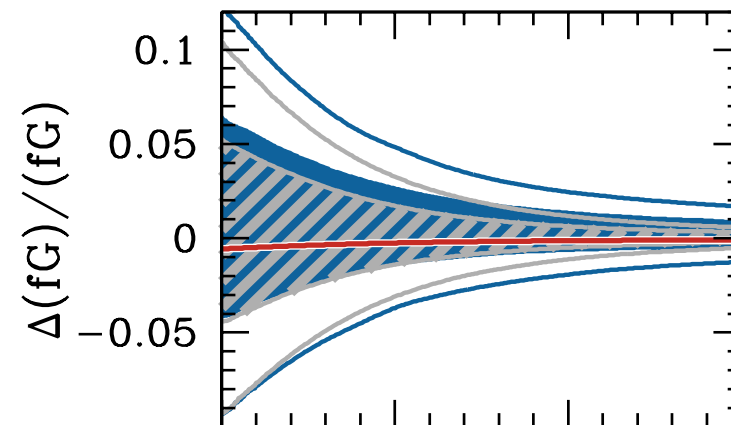
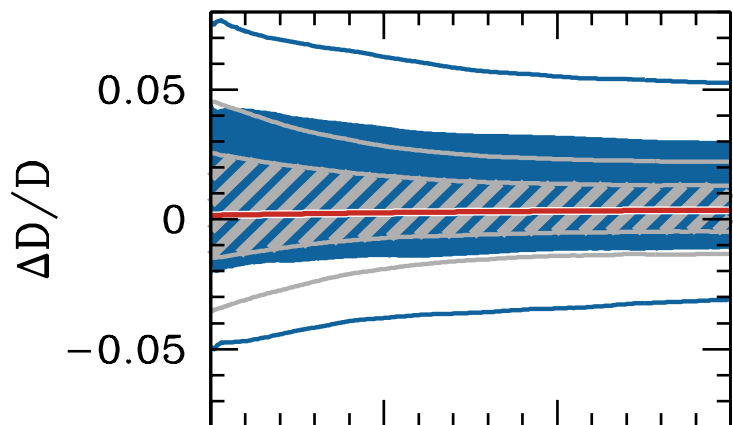
# $\Lambda$ CDM predictions - flat or curved

Growth  
to  $z=1000$



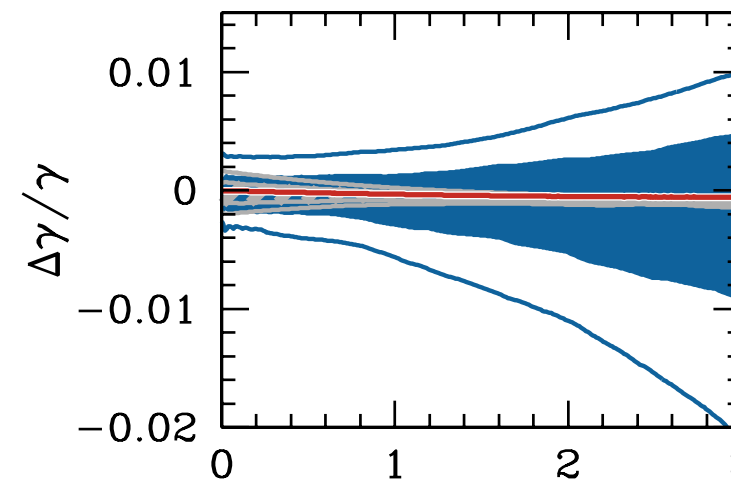
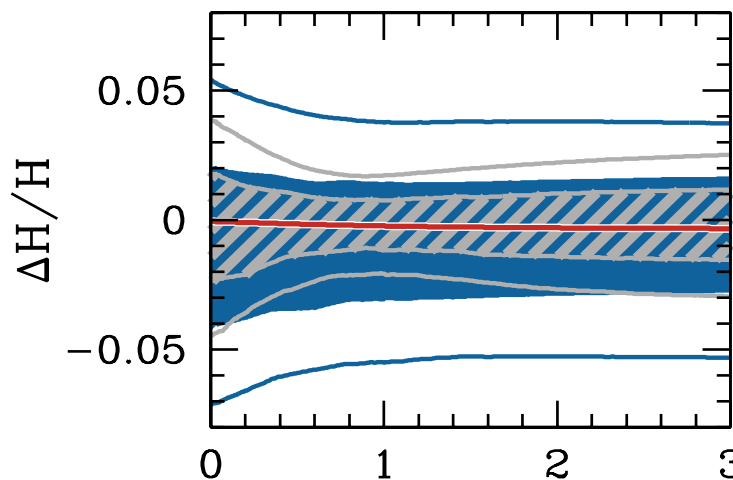
Growth  
to  $z=0$

Distance



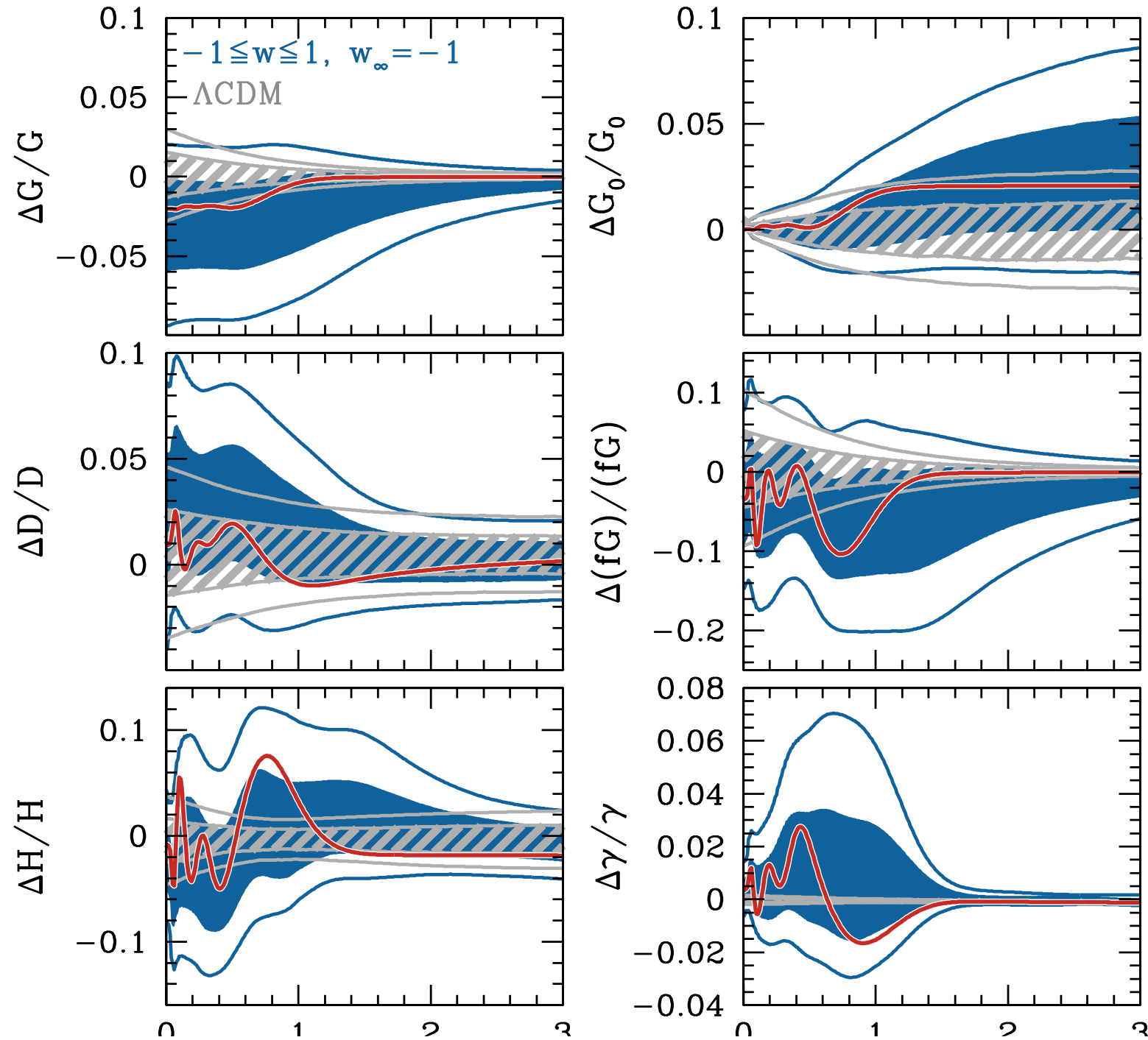
$f \times G$

Hubble  
parameter

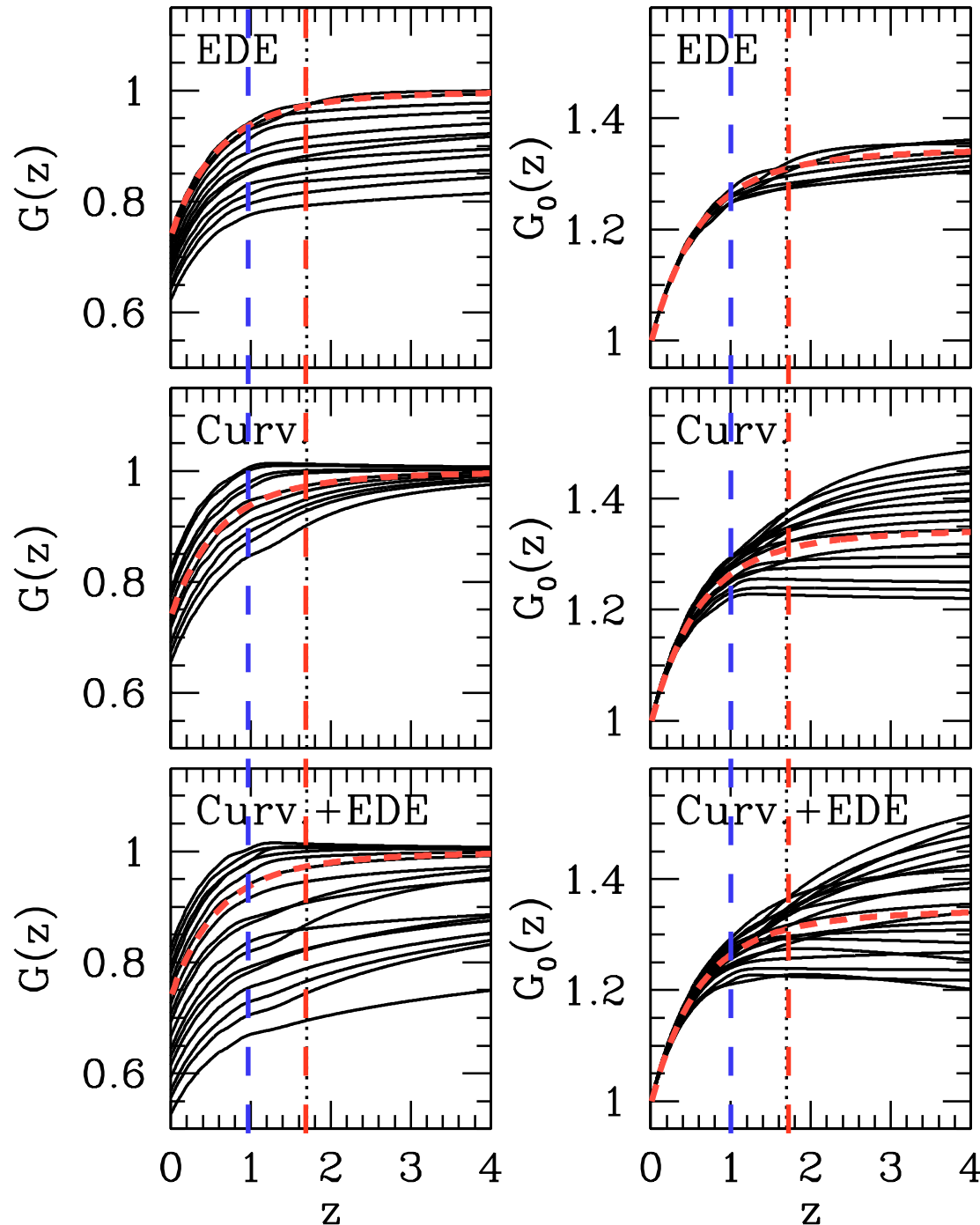


Growth index

Current data Quintessence predictions (flat, no Early DE)

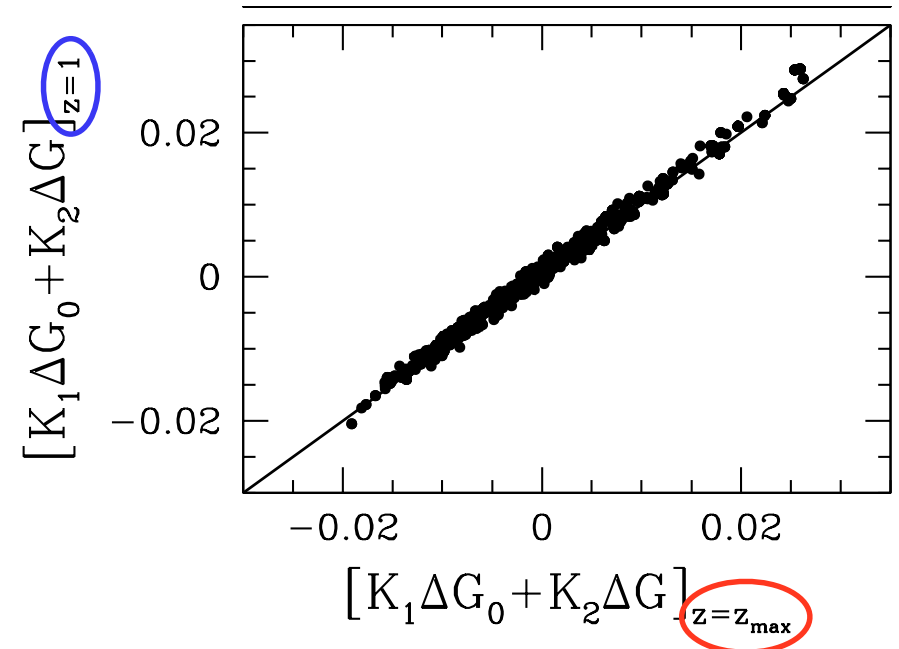


# Smooth DE with curvature and/or Early DE

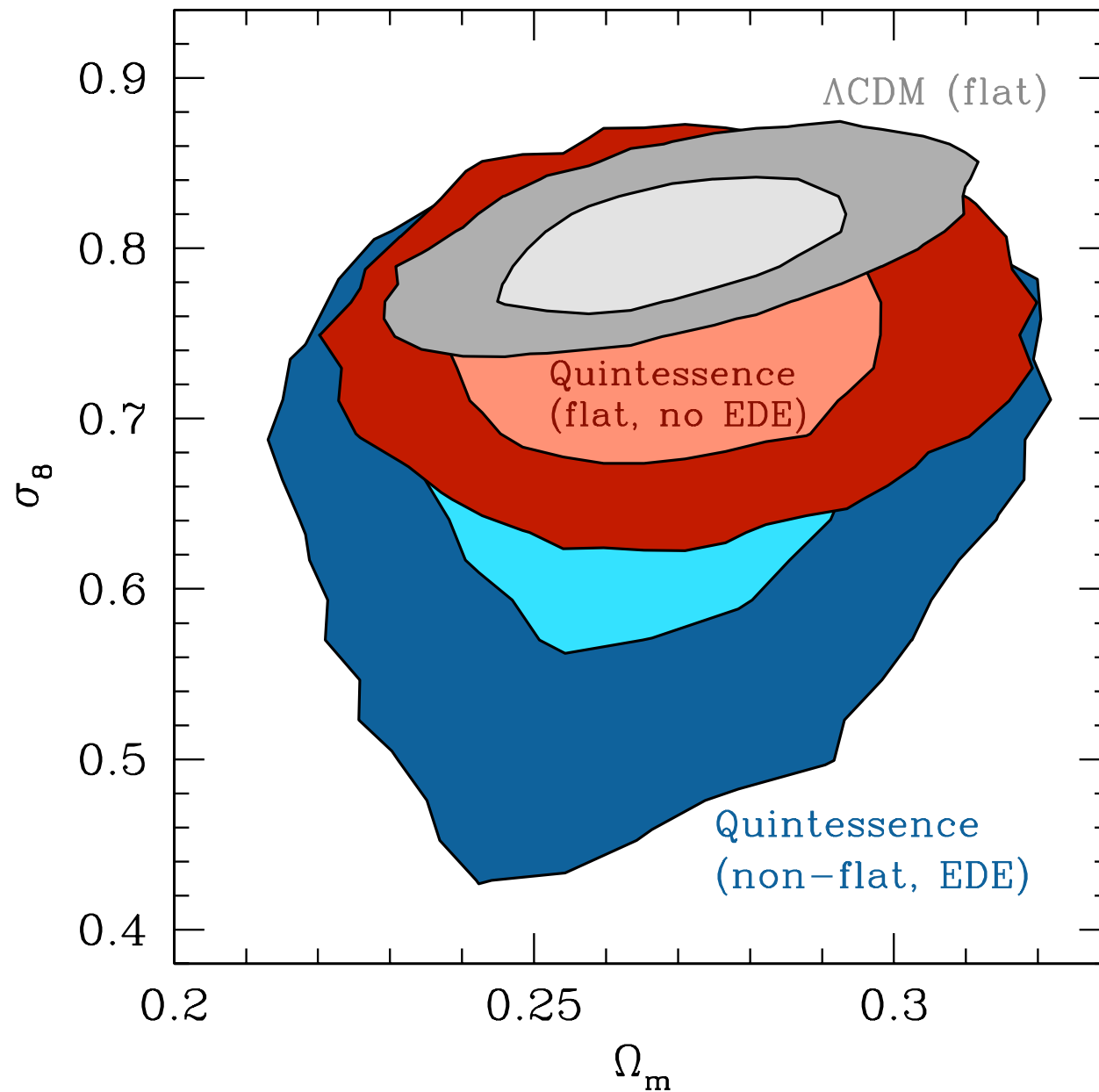


Some quantities  
are accurately predicted  
even in very general classes  
of DE models

(e.g. specific linear combination of  $G_0$   
and  $G$  evaluated at  $z=1$  vs  $z=z_{\max}$ )



From **current** data, projected down on  $\Omega_M$ - $\sigma_8$



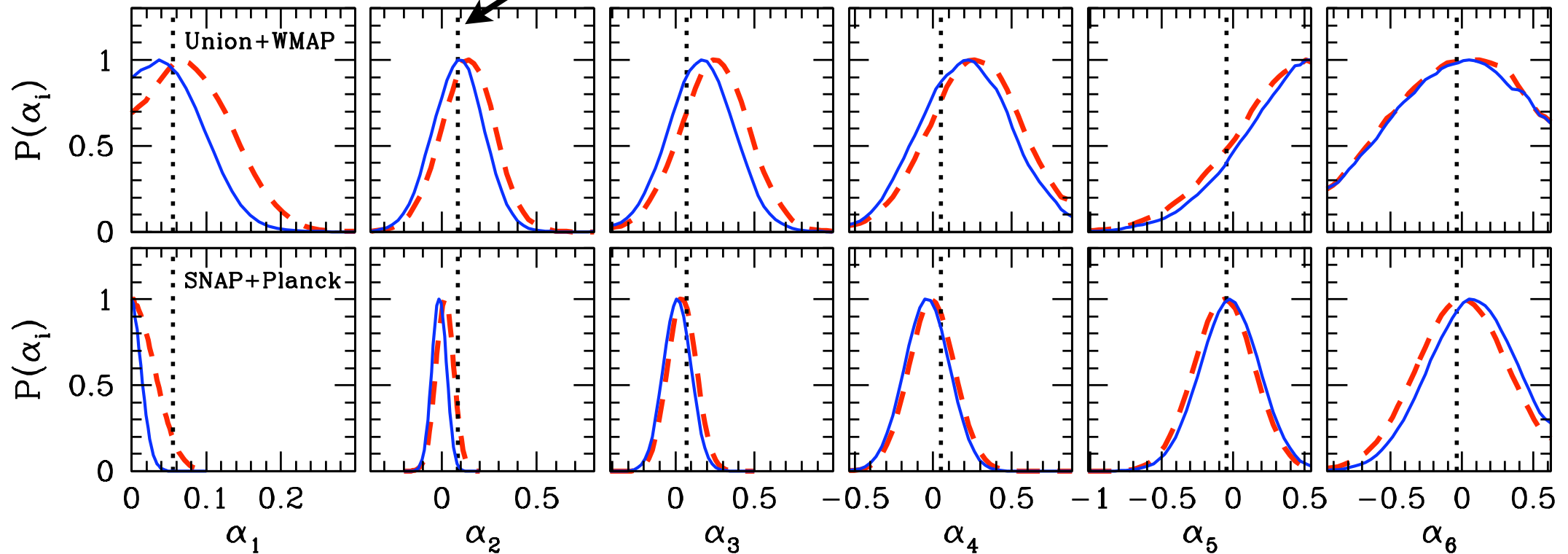
# In *principal*, constraints are good...

(components)

Top row:

Current Data

values for example  
quintessence model



Bottom Row:

Future Data  
(assumes  $\alpha_i=0$ )

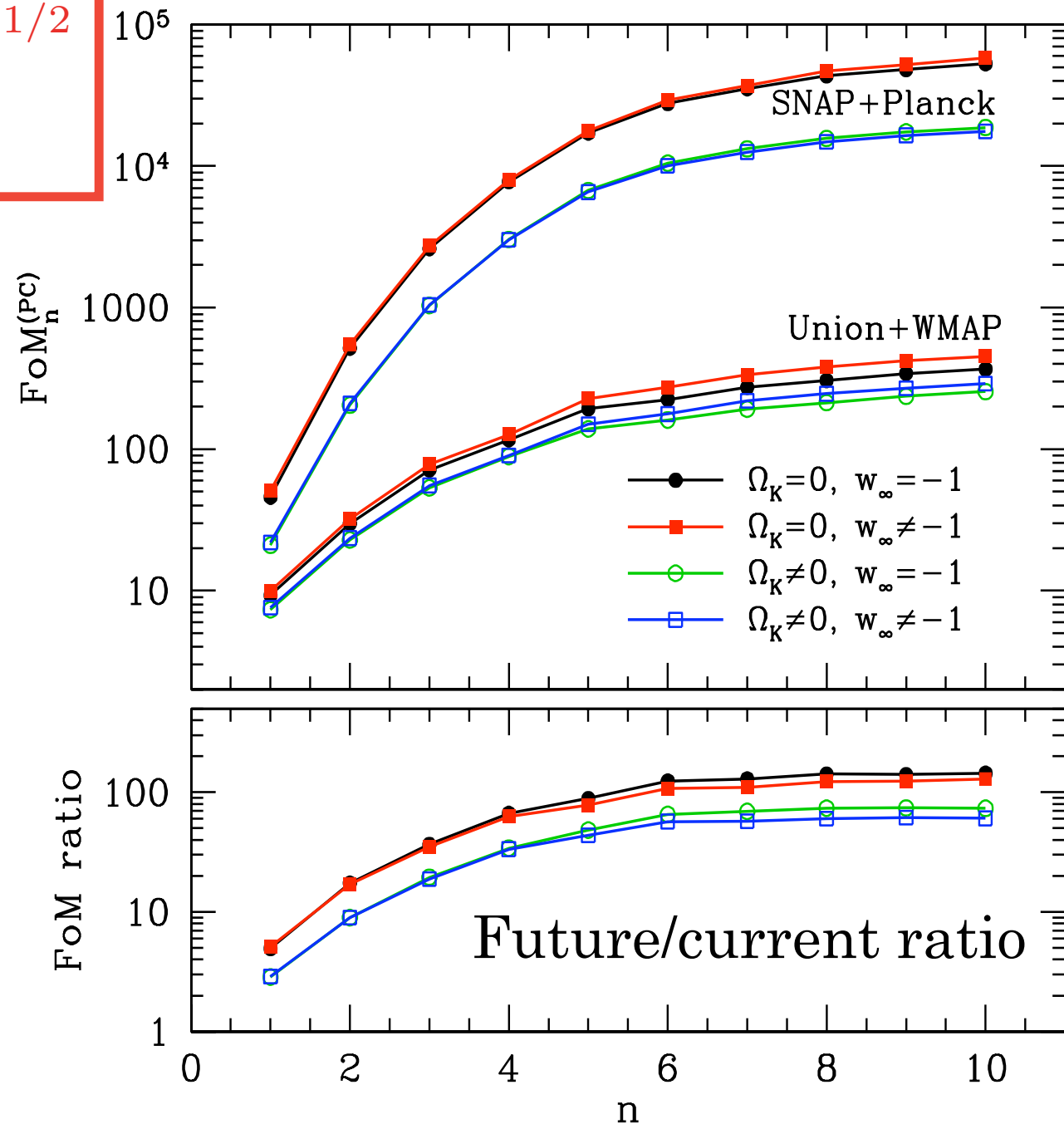
— Flat  
- - - Curved

# Generalizing FoM to many parameters - PCs of $w(z)$

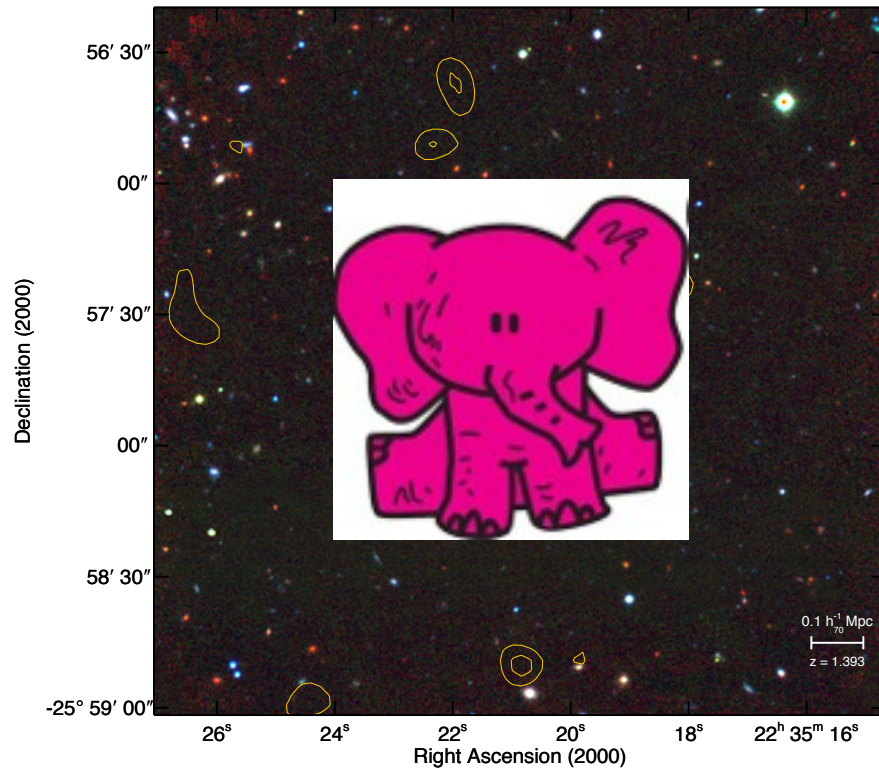
$$\text{FoM}_n^{(\text{PC})} \equiv \left( \frac{\det \mathbf{C}_n}{\det \mathbf{C}_n^{(\text{prior})}} \right)^{-1/2}$$

(proportional to volume  
of n-dim ellipsoid)

Full SN systematics degrade  
this FoM by factor 2-3  
(Ruiz et al, arXiv:1206.4781)



# Falsifying LCDM and Quintessence with “pink elephant” clusters



## Pink Elephant:

- any of various visual hallucinations sometimes experienced as a withdrawal symptom after sustained alcoholic drinking.

-*Dictionary.com*



# pink elephant, candidate 1.

## SPT-CL J0546-5345

Brodwin et al, arXiv:1006.5639

optical (grz); contours are SZ

optical (ri)+IRAC; contours are X-ray

$$z=1.067$$

$$M \approx (8 \pm 1) \cdot 10^{14} M_{\text{sun}}$$

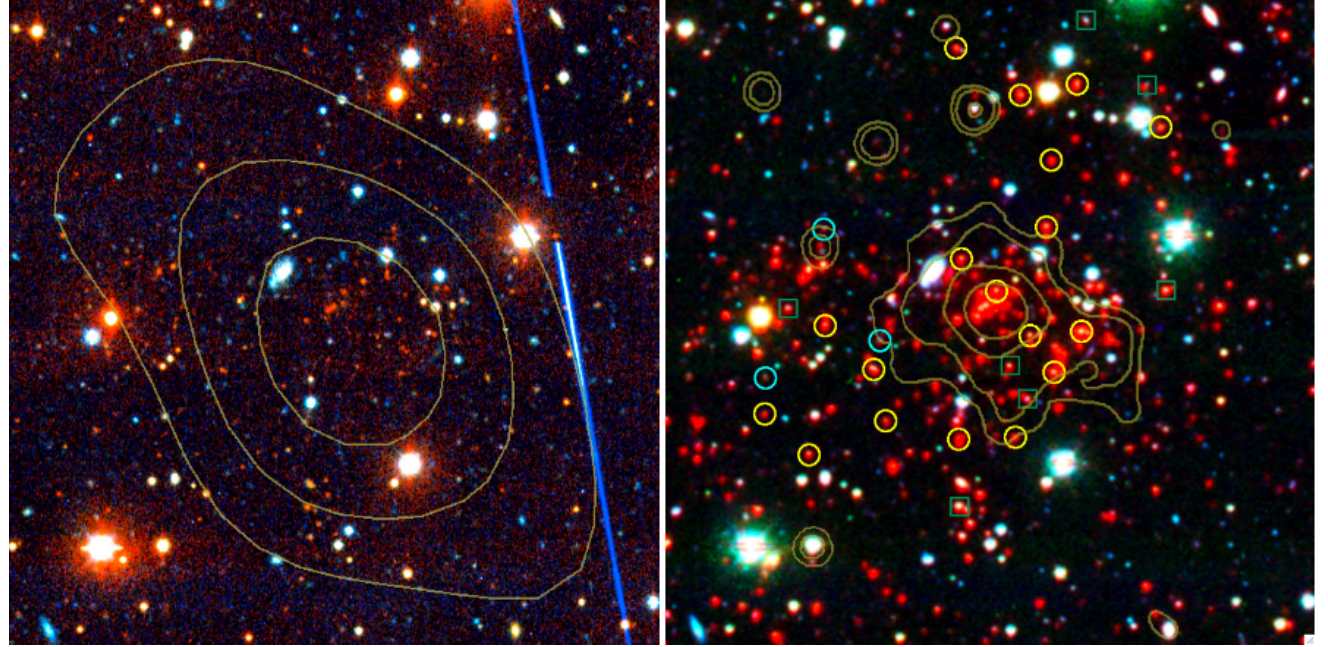


TABLE 2  
COMPARISON OF MASS MEASUREMENTS FOR SPT-CL J0546-5345

Mass Type	Proxy	Measurement	Units	Mass Scaling Relation	$M_{200}^{\text{a,b}}$ ( $10^{14} M_{\odot}$ )
Dispersion	<b>Biweight</b>	$1179^{+232}_{-167}$	km/s	$\sigma-M_{200}$ (Evrard et al. 2008)	<b><math>10.4^{+6.1}_{-4.4}</math></b>
	Gapper	$1170^{+240}_{-128}$	km/s	$\sigma-M_{200}$ (Evrard et al. 2008)	$10.1^{+6.2}_{-3.3}$
	Std Deviation	$1138^{+205}_{-132}$	km/s	$\sigma-M_{200}$ (Evrard et al. 2008)	$9.3^{+5.0}_{-3.2}$
X-ray	<b><math>Y_X</math></b>	$5.3 \pm 1.0$	$\times 10^{14} M_{\odot} \text{keV}$	$Y_X-M_{500}$ (Vikhlinin et al. 2009)	<b><math>8.23 \pm 1.21</math></b>
	$T_X$	$7.5^{+1.7}_{-1.1}$	keV	$T_X-M_{500}$ (Vikhlinin et al. 2009)	$8.11 \pm 1.89$
SZE	<b><math>Y_{\text{SZ}}</math></b>	$3.5 \pm 0.6$	$\times 10^{14} M_{\odot} \text{keV}$	$Y_{\text{SZ}}-M_{500}$ (A10)	<b><math>7.19 \pm 1.51</math></b>
	S/N at 150 GHz	7.69		$\xi-M_{500}$ (V10)	$5.03 \pm 1.13 \pm 0.77$
Richness	<b><math>N_{200}</math></b>	$80 \pm 31$	galaxies	$N_{200}-M_{200}$ (H10)	<b><math>8.5 \pm 5.7 \pm 2.5</math></b>
	$N_{\text{gal}}$	$66 \pm 7$	galaxies	$N_{\text{gal}}-M_{200}$ (H10)	$9.2 \pm 4.9 \pm 2.7$



# pink elephant, candidate 4: XMMU J2235.3-2557

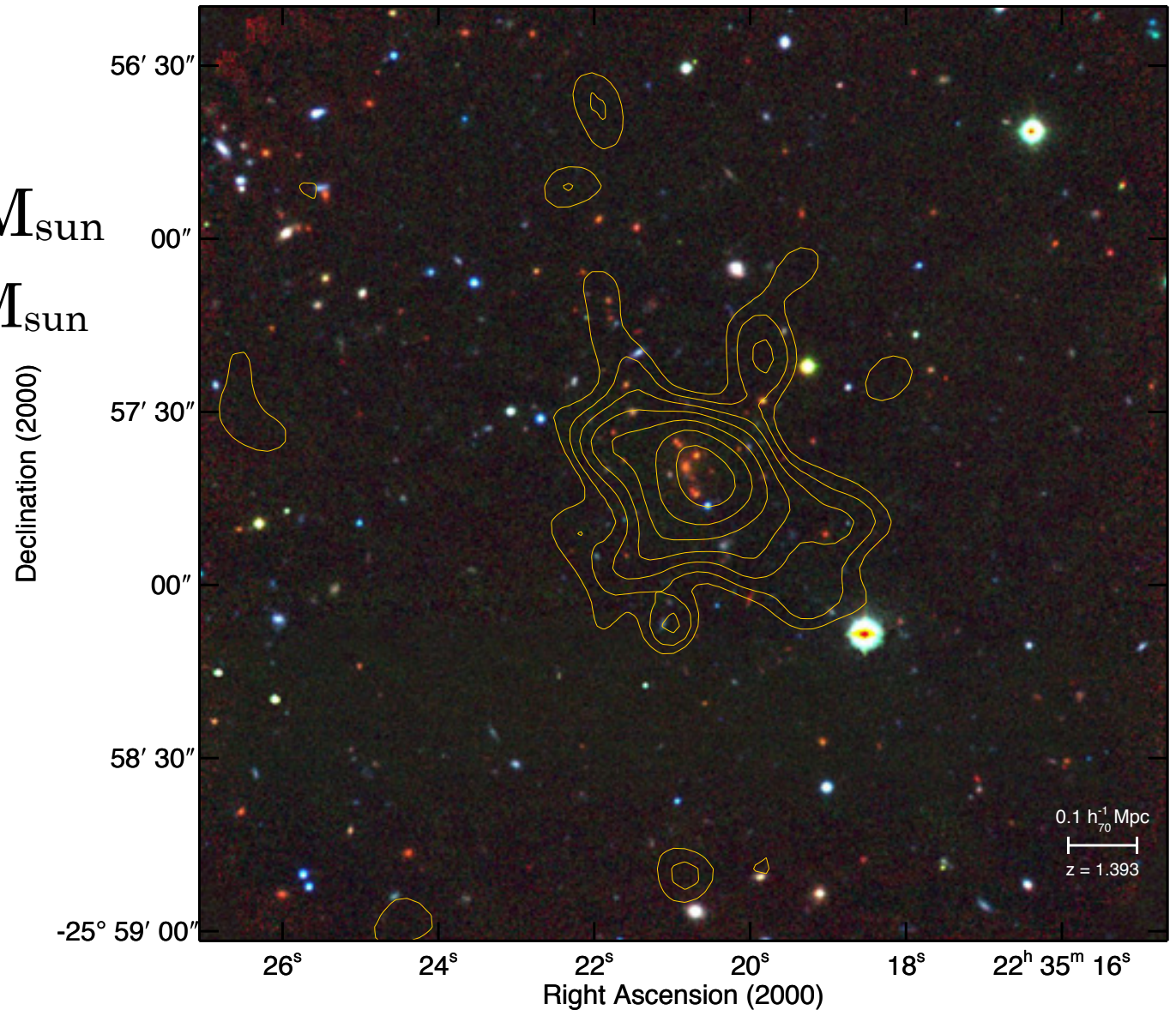
Mullis et al, 2005

Jee et al. 2008

$$z=1.39$$

$$M_{\text{x-ray}} \approx (7.7 \pm 4) \cdot 10^{14} M_{\text{sun}}$$

$$M_{\text{WL}} \approx (8.5 \pm 1.7) \cdot 10^{14} M_{\text{sun}}$$



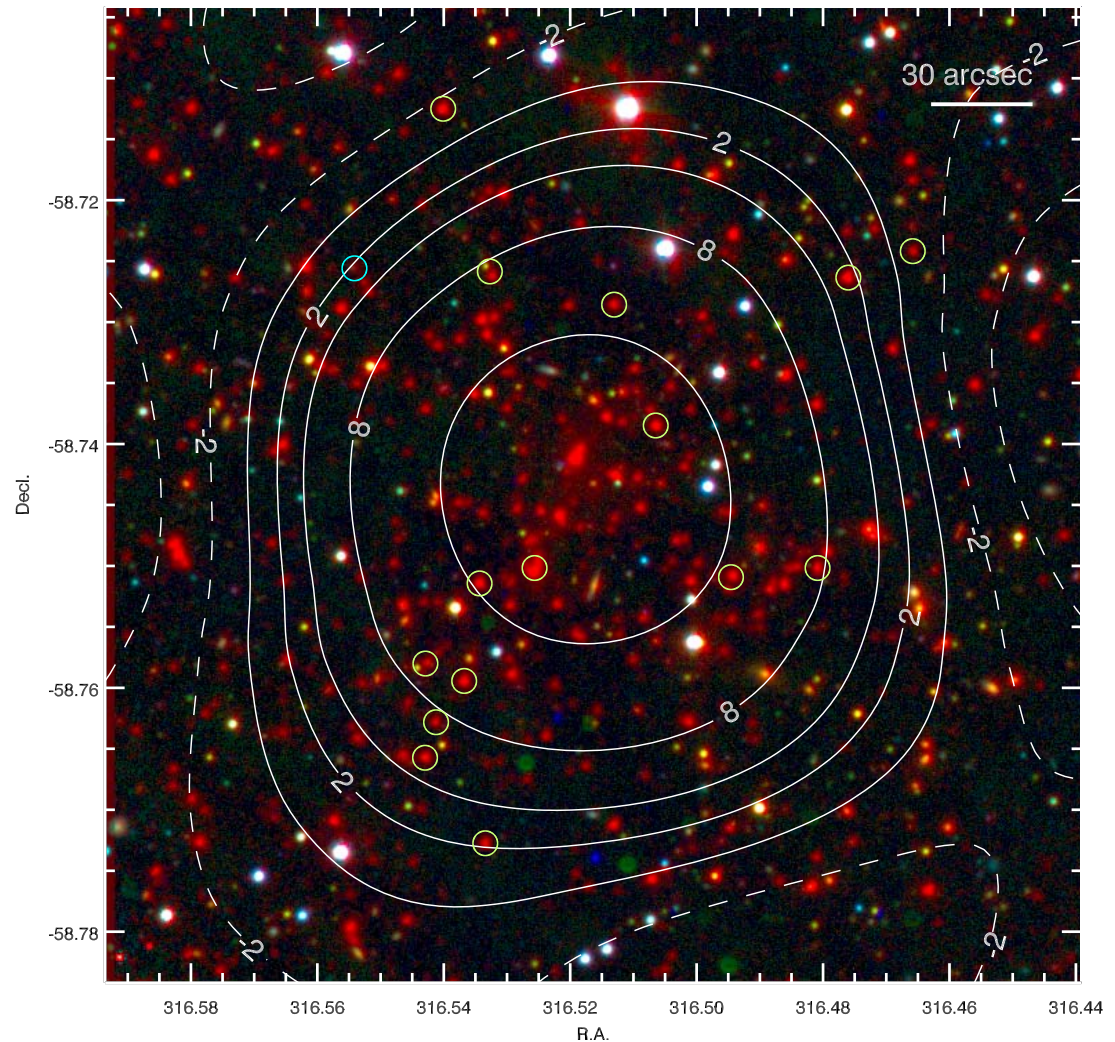
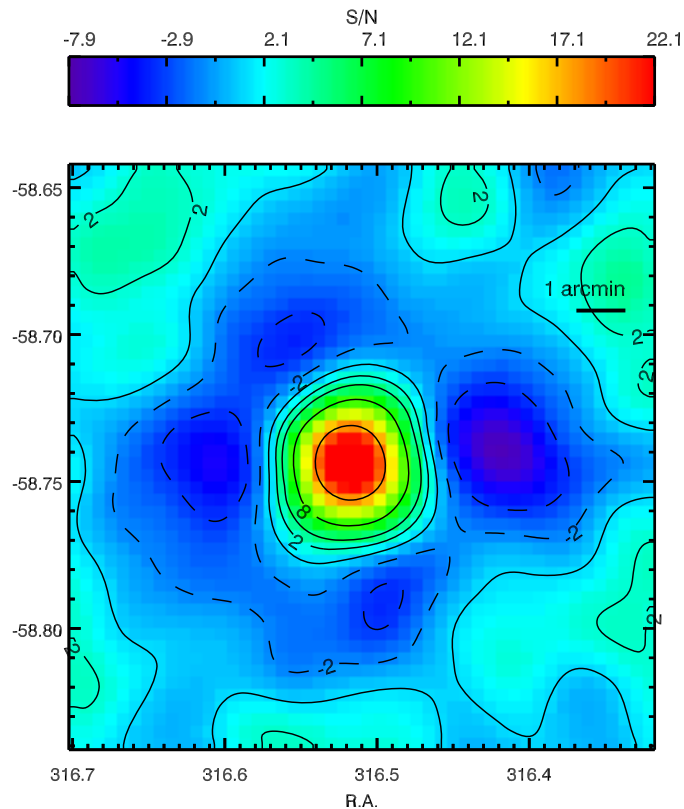
# pink elephant, candidate 5: SPT-CL J2106-5844

$z=1.132$

$M_{\text{SZ+x-ray}} \approx (1.27 \pm 0.21) \cdot 10^{15} M_{\text{sun}}$

Foley et al 2011

Williamson et al. 2011



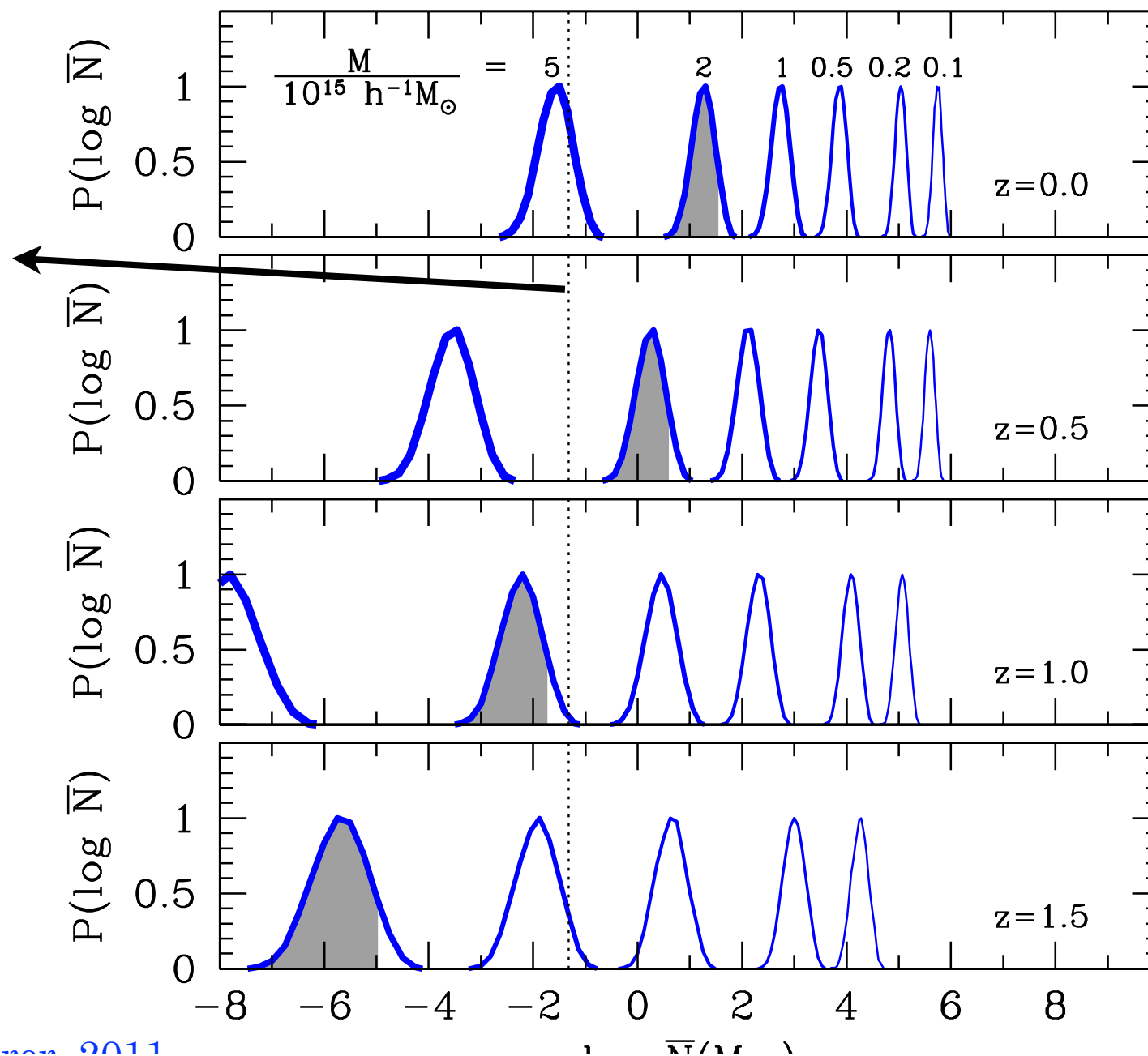
# Two sources of statistical uncertainty

1. **Sample variance** - the Poisson noise in counting rare objects in a finite volume
2. **Parameter variance** - uncertainty due to fact that current data allow cosmological parameters to take a range of values

# Parameter variance

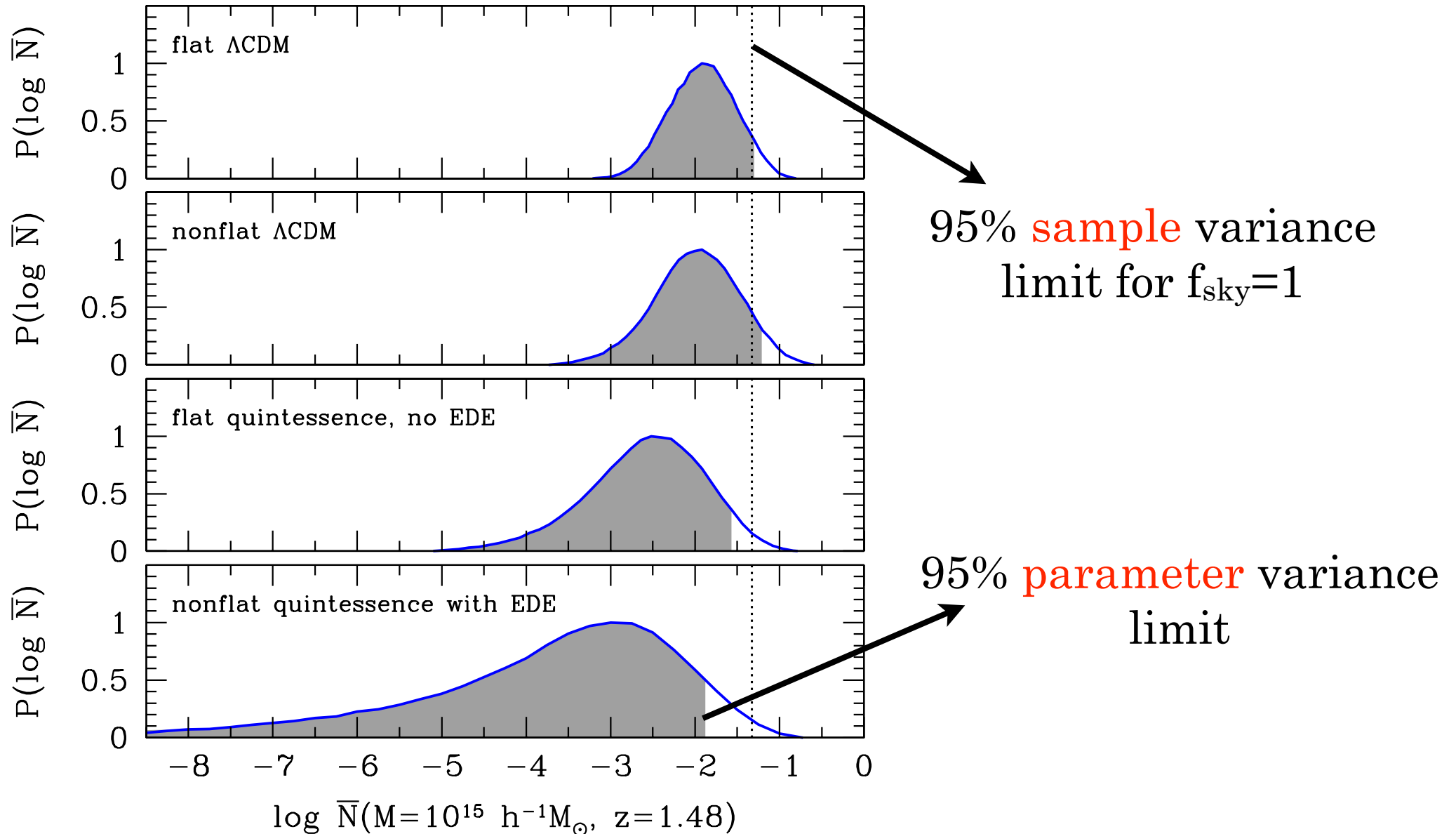
(due to uncertainty in cosmo parameters)

95% sample  
variance limit for  
seeing  $\geq 1$  clusters  
(for  $f_{\text{sky}}=1$ )





# Predicted abundance for $M > 10^{15} h^{-1} M_{\text{sun}}, z > 1.48$



Rule out  $\Lambda$ CDM  $\Rightarrow$  automatically rule out quintessence

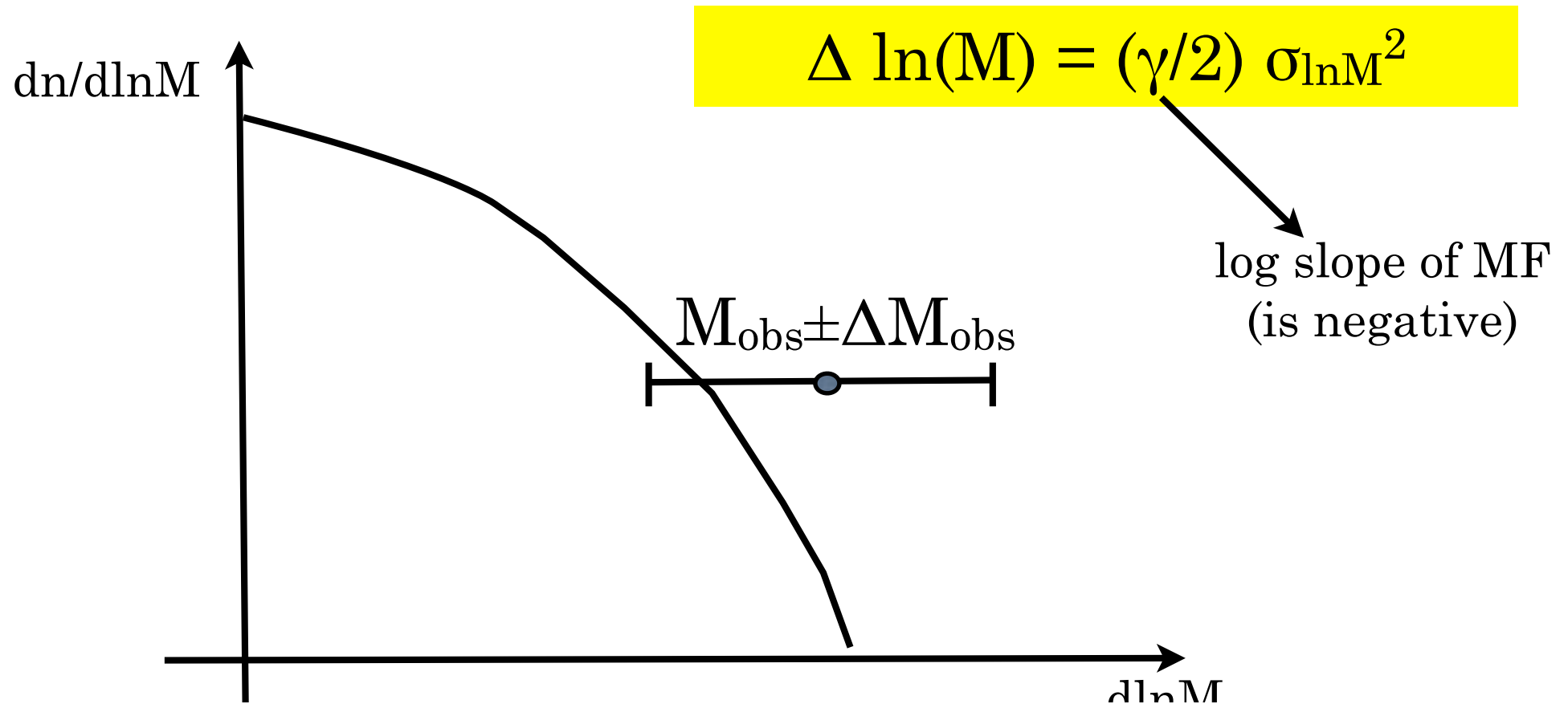


# Eddington bias

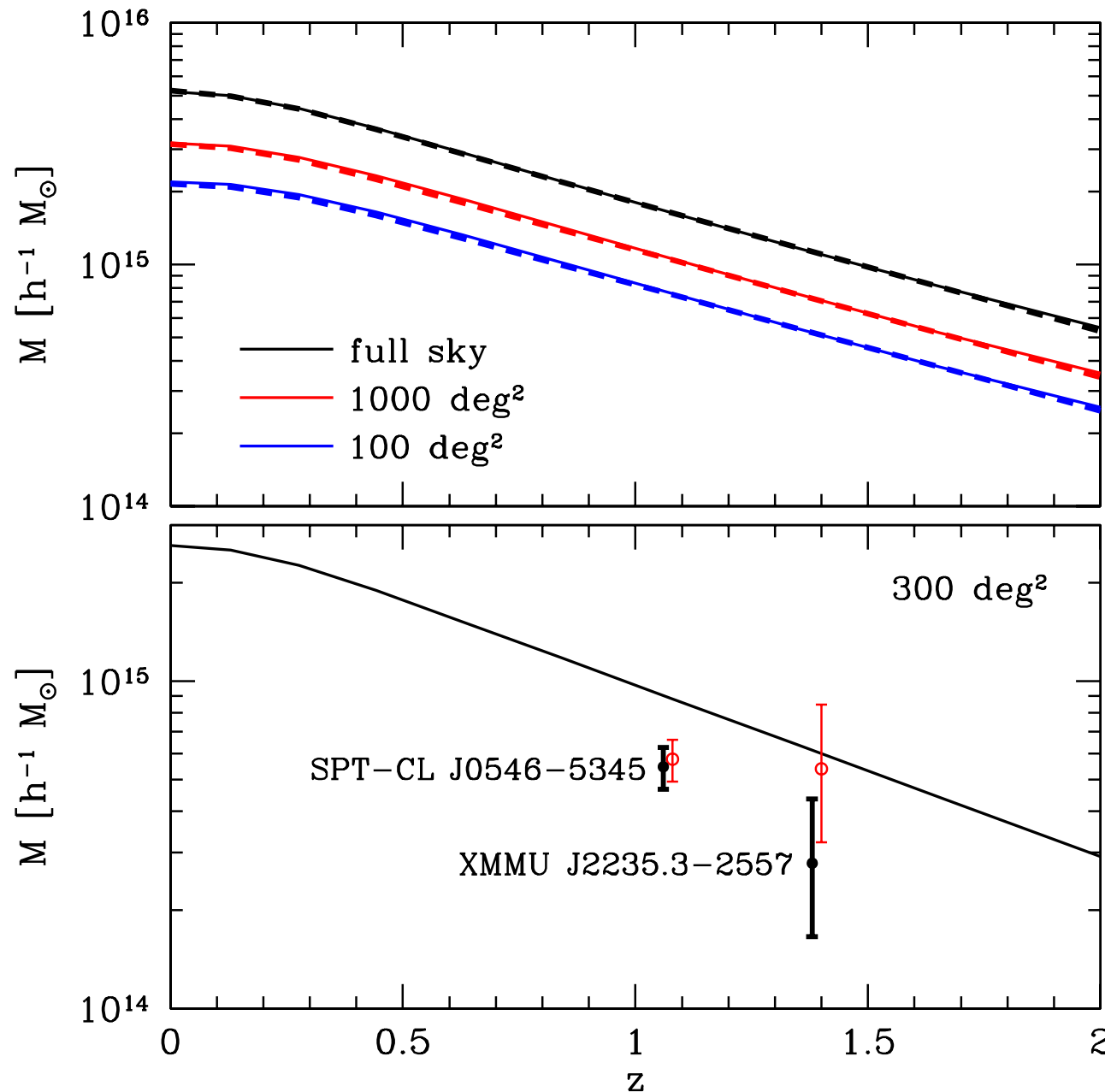
A.S. Eddington, MNRAS, 1913

For a steeply falling mass function,  
observed mass was more likely to be scattered into  
observed range from lower  $M$  than for higher  $M$

( $\neq$  Malmquist bias: more luminous objects are more likely to scatter into the sample)



# Results for the two pink elephant clusters vs. predictions for LCDM



Shown limits: 95% both  
sample and parameter  
variance for finding one  
cluster with  $>M$ ,  $>z$

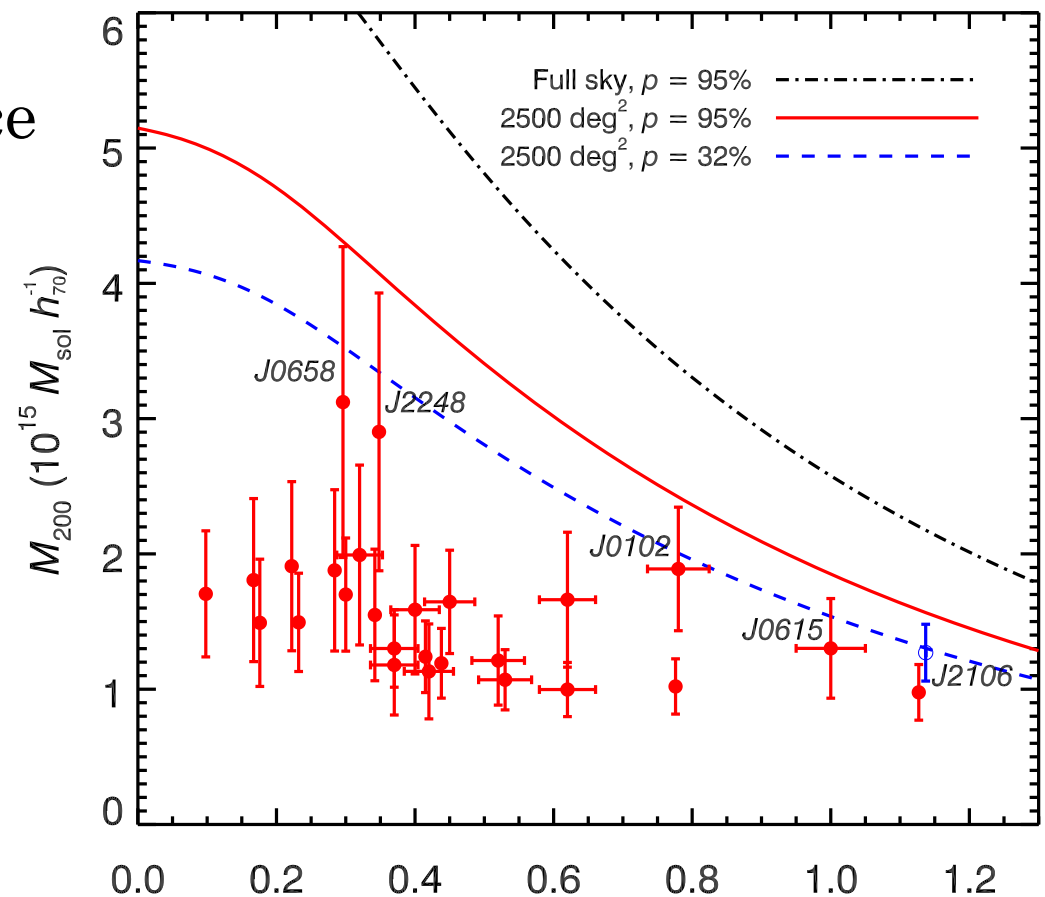
**black** error bars:  
masses  
corrected for  
**Eddington bias**

# Potentially useful product of paper:

**Fitting formulae** to evaluate  $N_{\text{clusters}}$  that rule out  $\Lambda\text{CDM}$  at a given

- ✓ mass and redshift
- ✓ sample variance confidence
- ✓ parameter variance confidence
- ✓  $f_{\text{sky}}$

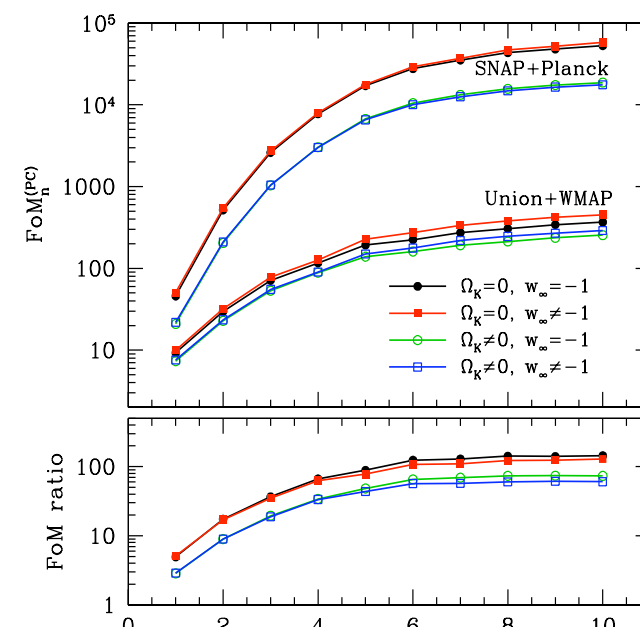
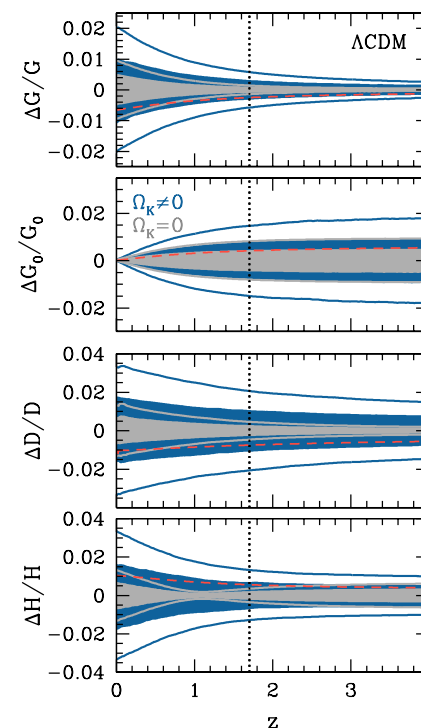
Williamson et al. 2011  
(SPT)





# Conclusions I: Falsifying DE

- Current (and, esp, future) data lead to strong predictions for  $D(z)$ ,  $G(z)$ ,  $H(z)$
- Examples:
  - **Flat LCDM**:  $H(z=1)$  to 0.1%,  $D(z)$ ,  $G(z)$  to 1% everywhere
  - **Quint**:  $D(z)$ ,  $G(z)$  to 5%; one-sided deviations
  - **Smooth DE**: tight consistency relations can still be found
  - **GR tests**:  $\gamma$  to 5% ( $\sim 0.02$ ) even with arbitrary  $w(z)$
- Total  $\text{FoM} = \det(\text{Cov})^{-1/2}$  improvement of  $>100$  in the future
- it's wise to keep eyes open for more exotic DE (and measuring PCs 3, 4, 5, 6...)



# Conclusions II: ‘Pink Elephants’

- It's important to be **careful** about the various **statistical**, not just systematic, effects in analyzing the abundance of rare, massive and distant clusters
- In particular, we find that the following effects have major effect on their likelihood
  - Parameter variance (in addition to sample variance)
  - Fair assessment of  $f_{\text{sky}}$
  - Eddington bias
- So far none of the detected clusters rules out any models (contrary to some claims in the literature)
- If an unusually massive/distant observed cluster observed tomorrow rules out LCDM, **it will rule out quintessence at the same time**