



2455-3

Workshop on Portable X-ray Analytical Instruments for Cultural Heritage

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External-beam IBA methods for non-destructive analysis of Cultural Heritage Artefacts

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Outline

- Introduction to Ion Beam Analysis
- External beams
- IBA applications to Cultural Heritage
- Essential bibliography

Ion Beam Analysis techniques



Beam IN	Beam OUT	Analytical technique
ion	ion	RBS, NRA
ion	target	ERDA, SIMS, SNMS
ion	X-ray	PIXE
ion	Gamma-ray	PIGE, Activation Analysis
ion	hν	Ionoluminescence (IL)



General features of IBA

Multielemental

- Quantitative analysis ("traceability")
- High sensitivity (1-100 ppm in at/cm³; 10¹¹-10¹² in at/cm²)
- Surface analysis (10 Å 10 μm)
- Depth profiling
- Non-destructive
- No sample pre-treatment
- Microanalysis (lateral resolution <1 μ m)
- 2D mapping

Stopping power

The "stopping power" (the energy lost per unit lenght, dE/dx) is a macroscopic and measurable quantity, describing the average interaction of the ion with the material:





Particle Induced X-ray Emission

Emission of characterisic X-rays following ioniziation from incident ions



Energy of characteristic X-rays





X-ray production cross sections



Adavantages of PIXE

• very fast, high-sensitivity, **non-destructive** analysis

- quantitative analysis
- minimum energy of detected X-rays tipically ~1 keV

 \implies all the elements with $Z \ge 11$ are quantifible simultaneously

Limitations of PIXE

- no information on the organic components
- no direct information on chemical bonds

but... hypothesis on stoicheometry through quantitative and multielemental anaylisis

 no direct information on the stratigrappy and the depth distribution of the elements

but... Differential PIXE

Example of PIXE spectra



Quantitative analysis (thin target)

 $Y_{0}(Z) = N_{P} \cdot N_{Z} \cdot t \cdot \sigma_{Z,E0} \cdot (\alpha_{Z} \cdot \varepsilon_{Z} \cdot \Delta \Omega/4\pi)$ $Y_{0}(Z) = (Q/e)(N_{A}/A)(\rho_{Z}t) \cdot \sigma_{Z,E0} \cdot (\alpha_{Z} \cdot \varepsilon_{Z} \cdot \Delta \Omega/4\pi)$ defining $\eta_{Z} = (1/e)(N_{A}/A) \cdot \sigma_{Z,E0} \cdot (\alpha_{Z} \cdot \varepsilon_{Z} \cdot \Delta \Omega/4\pi)$ $Y_{0}(Z) = \eta_{Z} \cdot Q \cdot (\rho_{Z}t)$



Thick targets



Quantitative analysis (thick targets)

 $Y(Z) = (Q/e)(N_A/A)(\alpha_Z \cdot \varepsilon_Z \cdot \Delta \Omega/4\pi) \cdot \rho_Z \int_0^{1} \sigma_{Z,E} \cdot \exp(-\mu \cdot x/\cos\theta) \cdot dx$

 $Y(Z) = (Q/e)(N_A/A)(\alpha_Z \cdot \varepsilon_Z \cdot \Delta \Omega/4\pi)(\rho_Z/\rho) \int_{E_0}^{E_F} \sigma_{Z,E} \cdot \exp(-\mu \cdot x/\cos\theta) \cdot dE/S(E)$

$$F(Z) = Y_0(Z)/Y(Z) = \frac{\rho \cdot T \cdot \sigma_{Z,E0}}{\int_{E_0} \sigma_{Z,E} \cdot \exp(-\mu \cdot x/\cos\theta) \cdot dE/S(E)}$$

$$(\rho_Z t) = F(Z) \cdot Y(Z) / (\eta_Z \cdot Q)$$



2-detectors PIXE set-up

Target	X-rays	What is needed	Detector features
Low–Z elements	Low energy Minimum dead layers		Thin entrance window
	High cross sections	Small solid angles	Small active area
Medium– high–Z elements	High energy	Large solid angles	Large active area
	Low cross sections	Efficiency	Large active thickness

Detection efficiency for a 2-detectors PIXE set-up



PIGE

Particle Induced Gamma-ray Emission



Nuclear reactions with prompt emission of gamma -rays

Radiative capture (direct reaction)	a + A → B* → B + γ	²⁷ ΑΙ(p,γ) ²⁸ Si
Inelastic scattering	$a + A \rightarrow A^* + a'$ $A + \gamma$	²⁷ ΑΙ(p,p′γ) ²⁷ ΑΙ
Rearrangement collisions	$a + A \rightarrow C^* + c$ $C + \gamma$	²⁷ Al(p,αγ) ²⁴ Mg

List of proton-induced reaction

Element	Eγ (keV)	Nuclear origin	Transition	Detection limit (%)	Possible interferences
Li	429	⁷ Li(p,ny) ⁷ Be	429 + 0	0.01	As(427), B(429)
	478	⁷ Li(p,p'y) ⁷ Li	4 78 → 0	5×10 ⁻⁴	Be(478), Mn(478)
Ве	415	Be ⁹ (p,γ)B ¹⁰	2154 + 1740		λg (415)
	718	Be ⁹ (p, y)B ¹⁰	718 → 0		B(718)
	1023	$Be^9(p,\gamma)B^{10}$	1740 + 718		Ti(1022)
	1437	Be ⁹ (p, y) B ¹⁰	3590 → 2150		
	3562	Be ⁹ (p,ay)Li ⁶	3562 → 0	0.1	
в	429	¹⁰ B(p,a) ⁷ Be	429 - 0		As(427), Li(429)
	478	¹⁰ B(p,ay) ⁷ Be → ⁷ Li	478 - 0		Li(478), Mn(478)
	718	$10^{10}B(p,p'_{\gamma})^{10}B$	718 - 0		Be (718)
	2124	${}^{10}B(p,p'_{\gamma}){}^{10}B$	2124 + 0	5×10 ⁻³	
	4433	11 _{B(p,y)} 12 _C	4433 - 0		N (4433)

List of proton-induced reaction

Element	E ₇ (keV)	Nuclear origin	Transition	Detection limit (**)	Possible interferences
с	2357	¹² C(p, y) ¹³ N	2357 + 0	1	
N	1400 4433	$14_{N(p,\gamma)}^{15}$ 0 $15_{N(p,\alpha\gamma)}^{12}$ C	4433 - 0		Cr (1400) B(4433)
0	110 197	$18_{O(P,Y)}^{19}P$ $16_{O(P,Y)}^{19}P$ $16_{O(P,Y)}^{19}P$	110 + 0 197 + 0	5	F(110), W(111) F(197),Co(197),Ni(197), Ga(197),Ti(199),Ge(199) Ga(493)
F	110	¹⁹ F(p,p') ¹⁹ F ¹⁹ F(p,p') ¹⁹ F	110 + 0 197 + 0	2×10 ⁻⁴ 5×10 ⁻⁵	O(110), W(111) Co(197), Ni(197), Ga(197) Ti(199), Ge(199), O(197)
Na	439 1368 1633	$2_{Na}^{23}_{Na}^{P,p'\gamma}^{23}_{Na}^{23}_{Na}^{P,\gamma}^{24}_{Mg}^{23}_{Na}^{23}_{Na}^{P,\gamma}^{20}_{Ne}^{20}_{Ne}$	$439 \rightarrow 0$ 1368 $\rightarrow 0$ 1633 $\rightarrow 0$	10-3	Se(439) Mg(1368), Al(1368)

List of proton-induced reaction

Element	E ₇ (keV)	Nuclear origin	Transition	Detection limit (*1)	Possible interferences
Mg	170	²⁶ Mg (p, y) ²⁷ A1	1014 + 844		A1(170)
	390	²⁵ Mg (p,p') ²⁵ Mg	975 + 585		
	585	²⁵ Mg(p,p'γ) ²⁵ Mg	585 → O	5×10 ⁻³	
	844	²⁶ Mg (p, y) ²⁷ A1	844 → 0		A1(844)
	975	²⁵ Mg(p,p')) ²⁵ Mg	975 → 0	1	
	1014	²⁶ Mg(p, y) ²⁷ A1	1014 - 0		T1(1012), A1(1014)
	1368	²⁴ Mg(p,p'y) ²⁴ Mg	1368 - 0		Na(1368), Al(1368)
		27			
A)	170	~ Al(p,p'γ) ~ Al	1014 - 844		Mg(170)
	844	27 A1 (P, P'Y) 27 A1	844 + 0	2×10 ⁻³	Mg (844)
	1014	27 Al (p, p'y) 27 Al	1014 + 0	5×10 ⁻³	T1(1012), Mg(1014)
	1368	27 Al (p, ay) 24 Mg	1368 → 0		Na(1368), Mg(1368)
	1779	27 _{A1(p, y)} 28 ₅₁	1779 + 0		Si(1779), P(1779)
51	1 2 7 3	²⁹ Si(p,p'y) ²⁹ Si	1273 → 0	3	
	1779	²⁸ si(p,p'y) ²⁸ si	1779 → 0		A1(1779), P(1779)

PIGE cross sections

The cross sections are the superimposition of resonances (Breit-Wigner) on a continuum due to direct nuclear reactions



Examples of PIGE spectra



PIGE elemental analysis

The elemental concetrations (N_T) are obtained from measured quantities (i.e. gamma-ray peak areas) using physical models implementing the sample structure and the physical microscopic data and processes:

$$Y_{\gamma}(E_0,\theta) = \varepsilon_{abs}(E_{\gamma}) \cdot N_p \cdot \int_0^{E_0} N_T \cdot \sigma(E_0,\theta) / S(E) dE$$

The principal needed microscopic data are **stopping powers** and **differential cross sections** of the interaction (as well as the detector absolute efficiency)

PIGE analysis in cultural heritage

- The PIGE technique can be used for (semi-)quantitative determination of light elements like Na, Al or Si in infinitely thick targets
- The unknown elemental concentrations are typically deduced by comparing the γ-ray yields with those of **thick** standards of similar composition, without the detailed knowledge of the cross section

Reaction	E γ (keV)
^{23}Na (p, p', $\gamma)$ ^{23}Na	440
^{25}Mg (p, p', $\gamma)$ ^{25}Mg	585
^{24}Mg (p, p', $\gamma)$ ^{24}Mg	1369
^{27}Al (p, p', γ) ^{27}Al	844,1014
^{28}Si (p, p', $\gamma)$ ^{28}Si	1779
^{31}P (p, p', γ) ^{31}P	1266

 The crucial point is the difference between the stopping power of the unknown sample and that of the standard

Thick target gamma-ray yields



PIGE quantitative analysis: comparison with thick standards

 $C_{camp} = C_{rif} \cdot Y_{camp}(E_0) / Y_{rif}(E_0) \cdot S_{camp}(E_{1/2}) / S_{rif}(E_{1/2})$

 $E_{\frac{1}{2}}$ such as: $Y(E_0) = 2 \cdot Y(E_{\frac{1}{2}})$

The " $E_{\frac{1}{2}}$ " method is valid as long as the excitation function varies slowly with the energy





Rutherford Backscattering Spectrometry



Principles of RBS

For a given scattering angle θ , the energy E_1 of the incident ion (mass M_1) after the collision is only a function of the mass M_2 of the targt nuclei



$$K = \frac{\left[\sqrt{\left(\frac{M_2}{M_1}\right)^2 - \sin^2 \theta} + \cos \theta\right]^2}{\left(\frac{M_2}{M_1} + 1\right)^2}$$

larger ΔE for smaller M (light nuclei)

Larger ΔE for larger θ (backscattering)

The kinematic factor K



Elastic scattering cross section

The Rutherford formula:

$$\left(\frac{d\sigma}{d\Omega}\right)_{Ruth} = \left(\frac{Z_1 Z_2 e^2}{E}\right)^2 \frac{4}{\sin^4\left(\theta\right)} \frac{\left[\sqrt{1 - \left(\frac{M_1}{M_2}\sin\theta\right)^2} + \cos\theta\right]^2}{\sqrt{1 - \left(\frac{M_1}{M_2}\sin\theta\right)^2}}$$

 Z_1 Atomic number of the incident ion

- Z_2 Atomic number of the target nucleus
- E Energy of the incident ion
- M_1 Mass of the incident ion
- M_2 Mass of the target nucleus



Non-Rutherford cross sections





Evaluated and recommended experimental cross sections available from IBANDL web site (www-nds.iaea.org/ibandl/)

Depth scale of RBS

The signal from an atom at the sample surface will appear in the energy spectrum at a position KE_0 .

The signal from atoms of the same mass below the sample surface will be shifted by the amount of energy lost while the projectiles pass through the sample, both before (ΔE_{in}) and after a collision (ΔE_{out}) .



$$E_0 - E_1 = \left[\frac{Kx}{\cos\theta_1} \cdot \left(\frac{dE}{dx}\right)_{in} + \frac{x}{\cos\theta_2} \cdot \left(\frac{dE}{dx}\right)_{out}\right]$$

There exists a relation between the measured energy E_1 and the depth x at which the scattering took place
The features of RBS spectra



- Position of the signal (mass perception *i.e.* kinematic factor)
- Width of the signal (depth/thickness perception *i.e.* stopping force)
- Heigth of the signal (quantitative analysis of elemental composition *i.e. scattering cross section*)

Examples of RBS spectra





External beam

Advantages

direct analysis of artefacts having any shape and any size no sampling no charging, no preparation (conductive coating etc.) no heating, reduced damage risk easy sample positioning fast and efficient

Disadvantages

energy loss energy straggling beam lateral spread x-ray attenuation

Typical extraction windows

Material	Thickness (µm)	ΔE (keV)	σ _E (keV)	σ _θ (μm/mm)
AI	10	235	16	14
Kapton	8	130	9	6
Zr	2	75	7.3	15
Si ₃ N ₄	0.1	8	5	<1
	0.5	40	9	<2

Choice of external atmosphere

Air

Helium

N1.5620.42C.0003Ar.0094 Pressure=760. Path=1. cm

He Pressure=760, Path=1, cm



The use of an helium-saturated atmosphere in front of the X-ray detector is mandatory

External beam IBA of ancient manuscripts, ...ceramics,



PIXE analysis of the frontispiece of Pl.16,22, from Biblioteca Laurenziana in Florence



Analysis of the Ritratto di fanciullo by Luca Della Robbia – before restoration at the Opificio delle Pietre Dure in Florence







Micro-PIXE measurements of Portrait of Lucas de Leyde by Alfred Dürer A.Duval et al., (Louvre laboratory)



Micro-PIXE measurements of a Mexican gold alloy ornament G.Demortier and J.L.Ruvalcaba Sil (Namur)



...paintings

PIXE analysis of a painting by Lucas Cranach the Elder C. Neelmeijer et al. (Rossendorf Forschungszentrum, Dresda)





Example of PIXE spectra of two blue pigments







Pluteo 48, 34, f. 66 v°



Pluteo 48, 34, f. 41 v°

Extensive use of lapislazuli starting from XI century



Metal point drawings

LEONARDO DA VINCI STUDY OF A DRAPERY Roma, Istituto Nazionale per la Grafica

metal point, lead white red prepared paper



Characteristics of metal point drawings





The extension of the metallic agglomerates on the surface is some tens of µm The beam can pass through the trace and hit the preaparation

The beam size does not allow a detailed analysis

The contribution of the preparation must be taken into account

Nuclear microscopy



MicroPIXE analysis of metal point drawings Au Cu Pb

Four metallic points: silver, lead, gold, copper

Red preparation: cinnaber, yellow ochre, lead white, bone white





Micro-PIXE measurements of an Achemenide pendant (IV century BC)



Micro-PIXE measurements of Achemenide pendant (IV century



Differential PIXE

Consists in performing measurements on the same area with beams of different energies

At different energies proton beam ranges are different



By comparing X-ray spectra taken at different energies, stratigraphic information can be obtained

PIXE spectra at different energies



Blue paint layer (lapislazuli) on a substrate of calcium sulphate



Estimate of the paint layer thickness

$$\frac{Y_{\text{Al}}}{Y_{\text{Ca}}} = \frac{C_{\text{Al}}}{C_{\text{Ca}}} \frac{\int_{E_{\text{p}}}^{E_{\text{p}}-\Delta E_{\text{lap}}(t)} \sigma_{\text{X}}^{(\text{Al})}(E) e^{-\mu_{\text{lap}}^{(\text{Al})} \frac{x(E)}{\cos\theta}} \frac{dE}{S_{\text{lap}}(E)}}{e^{-\mu_{\text{lap}}^{(\text{Ca})} \frac{t}{\cos\theta}} \int_{E_{\text{p}}-\Delta E_{\text{lap}}(t)}^{0} \sigma_{\text{X}}^{(\text{Ca})}(E) e^{-\mu_{\text{white}}^{(\text{Ca})} \frac{x'(E)}{\cos\theta}} \frac{dE}{S_{\text{white}}(E)}}$$



Metal threads (Alhambra, Granada)



Enrichment of gold on the surface





"Incarnato"



paint layer: cinnabar (HgS, red pigment)+lead white

preparation: lead white

Ca and Fe are in the varnish

Lapis-lazuli pigment in paint layers



Lapis-lazuli is a blue pigment, mainly composed of lazurite (3Na₂O·3Al₂O₃·6SiO₂·2Na₂S)

Limited possibility of identifying lapis-lazuli by PIXE in canvas and wood paintings:

- low-energy X-rays absorption in the varnish and in the paint layer itself
- signal interference from other pigments

"Maddonna dei fusi", Leonardo da Vinci (1501)

Lapis-lazuli pigment in paint layers

PIXE spectra

PIGE spectra

Original Blue pigment mixed with Lead white (Ca and Fe from the varnish)

Restored Cobalt blue and Zinc white (used only from XIX century!)



Analysis of ancient Roman glasses



Roman glass mosaic tesserae from Villa Adriana, Tivoli (Italy)

Quantification of Na is of great importance for the characterizaztion of ancient glasses

Two basic typologies of Western glass:

- natron (high Na₂O, low K₂O and MgO)
 Roman and High Middle
 Ages
- plant ash (low Na₂O, high K₂O) since Middle Ages

Sodium in Roman glasses

X-rays fom the lightest elements strongly absorbed by crusts and *patinae*

coloured but more



Roman glass mosaic tesserae

2 mm



"freshly cut"



Sodium in Roman glasses



X-rays from the lightest elements strongly absorbed by crusts and *patinae*

Sodium in Roman glasses



Estimate of Na content by comparing gamma-ray yields to those of thick glass standards (NIST SRM) with certified Na₂O concentration

Concentration ranges perfectly compatible with the typical Roman sodalime-silica glass

	main oxides (%)				
glass colour	Na ₂ O	SiO ₂	CaO	PbO	
green	~20	55-60	5-9	1-3	
blue	~20	60-65	5-9	<0.1	
turquoise	~20	55-60	5-9	<0.3	
yellow	~15	55-60	5-9	5-8	
red	~10	35-40	5-9	30-35	

RBS: External vs Vacuum



- 3 MeV protons on target
- $\theta = 150^{\circ}$
- SiO₂ target

- Energy loss and energy straggling * in exit window and external path in atmosphere
- * 15 keV FWHM for 500 nm Si_3N_4 + 10 mm He

Gold alloy or gilding



The scabbard is made of a thick Au-Cu alloy (thickness > 10 μ m).



For comparison, the gilding of the statuette is about 2 μ m thick.

From the width of the Au signal it is possible to obtain the thickness of the gilding (dE/dx is known).



RBS analysis of a gilded bronze chandelier (XI century) from the Cathedral of Hildesheim, Germany

RBS study of glass corrosion



Leaching of Ca, K, Na from the interaction with moisture or water and formation of surface hydrate silicates (cfr. PIGE analysis)

Complementary PIXE/RBS

In samples with a layered structure the elemental depth profile is needed to correctly calculate absorption effects in PIXE

PIXE strenghts

- High sensitivity
- Excellent specificity

RBS strenghts

- Traceable accuracy
- Excellent depth resolution

RBS weaknesses

- Low sensitivity
- Poor mass resolution

PIXE weaknesses

- Poor traceability
- Poor depth resolution

Characterization of paint layers by simultaneous PIXE/RBS analysis



"La Bohémienne", Frans Hals (1630)



The canvas is schematized as carbon plus chalk (CaCO₃)

Ochre pigment (ematite) detected and quantified thanks to simultaneous PIXE/RBS measurements: $440 \cdot 10^{15}$ atoms/cm² Fe₂O₃ in 7000 · 10¹⁵ atoms/cm² of oil (C₁₃O₅)

Thanks for your attention!

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