





2469-15

## Workshop and Conference on Geometrical Aspects of Quantum States in Condensed Matter

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Holographic entanglement beyond classical gravity

Sean Hartnoll Stanford University

HOLOGRAPHIC ENTANGLEHENT BEYOND CLASSICAL GRAVITY W/ T. Borrella, X. Dong, V.L. Martin @ 1306.4682.

Radined density motives:

 $A < \phi_{-}$   $Q[\psi_{t},\psi_{-}] = \frac{1}{2} \int D\phi e^{-S(\phi)} \delta(\phi(A,E') - \psi_{+})$   $\times \delta(\phi(A,E') = \psi_{-})$ 

Clearly then:  $Trp^n = \frac{2n}{2n} \leftarrow partition function on \\ n-sheded cover:$ 

Rényi entropy:

Enlargement entropy

S = tim Sn = - tr (p (ogp)

small x expusion known from OPEs. Sn = - N 2 (2 ) ( 2 ) 2 h 2 1 1 ( Sin 1/2 ) 4 h

multiday -0 5 = - N ( = ) 2 1 2 1 (24+1) [ Cordy a Calculrate ] We manyed to implement the stategy exactly in an expossion in X. one by step: To each order in x, only a finite leading order: OWs "on southely decreasing words" John - Lkentkon - ... lmas higher orders: growings of OUS  $5 = -\left(\frac{x^4}{630} + \frac{2x^5}{693} + \frac{(5x^6}{4004} + \frac{x^7}{234} + \frac{167x^8}{36936} + 0(x^1)\right)$ onely any ong.

Gombi-Manay-Yin downed a nice formula for functional determinants on AlS3/7: log 2 | one loop = - I I log |1-95 | for metric fluctuations. or has conjugacy classes of opening classes opening class Shalegy: . find I far all is (Schothy confamilité) - generate P firall in -> privatine words. . find eigeniales of words · analytically continue to a -sl. Cross rateria 2c = (23-22)(24-2) (23-21) (24-32) Marked information only depends on this (4 pt for of fassit operators)

In well-sported pluse, mutual organistico vanistico.
In(L,L2) = S. (L1) + S. (L1) - S. (L, UL2)
However, general results ((ordy- (alexane), this
In 1- (vop correction.
Similarly in forus: (us):
Similarly in forus: (us):  after HP: $S = \frac{C}{6} \log \left( \frac{3}{2} \sin^{1/2} \frac{784}{2} \right)$ (1)
· below HP: // S = \( \lefta \lefta  \sin^2 \pmod \righta \righta \)
These are brown exact answers for CFTs at or and O femperature!
~ (1) is very fruite size corrections.
~ (1) is morning fruite size corrections. (2) is mossing Amixed when of desirts white S(R) \$ S(R) 1.
-> find these of 1- (ap.

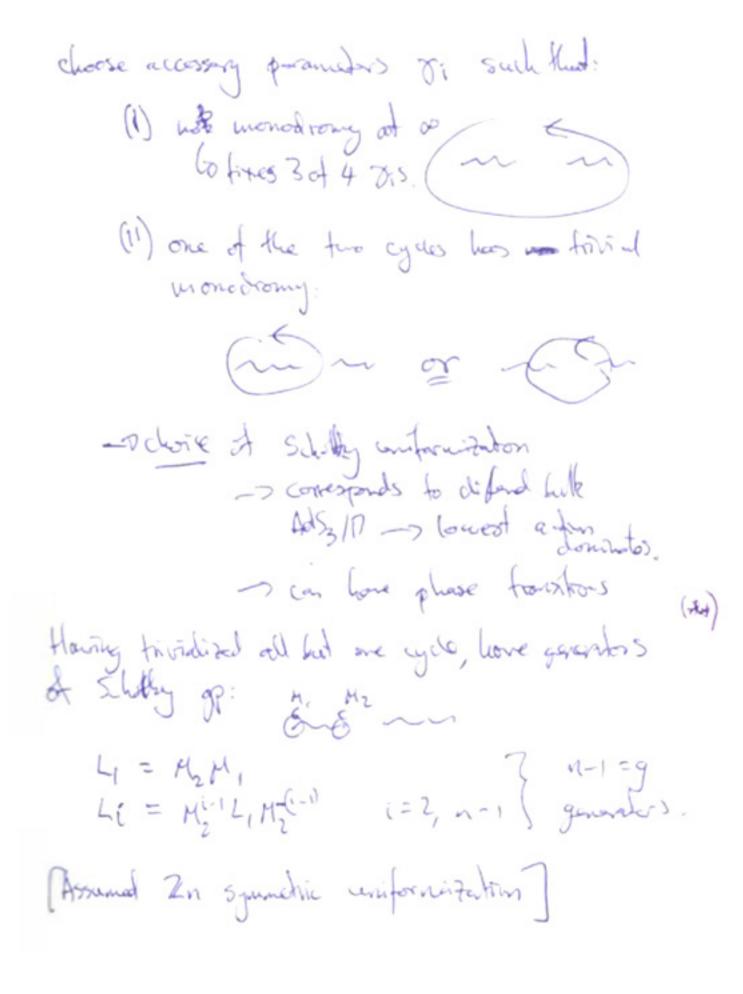
Similar for toras 4"(2)+=== (15-2)+7(-1)+7(-1)+7(2-2) 8 +8)4(8) =0 Faulkner ( following Eggat / Taktuch Thyon Should that on-shed bulk action of Ad3/1 Satisfied:  $\frac{\partial SE}{\partial z_i} = -\frac{cn}{6} \gamma_i$  of frintering monotony monotony = entarglement entropy. 35 = - (m CN ); the DT ensur. for two merveds on place. Interstyly feature (busin from RT) sund separation: large separation glase transition -> change of downant

Similar for torns ( 12 2) + 7 (-1) 17 7(22) P + 5) + (2) = 0 aulbuer ( following Eagraf / Tabilitud Eligan

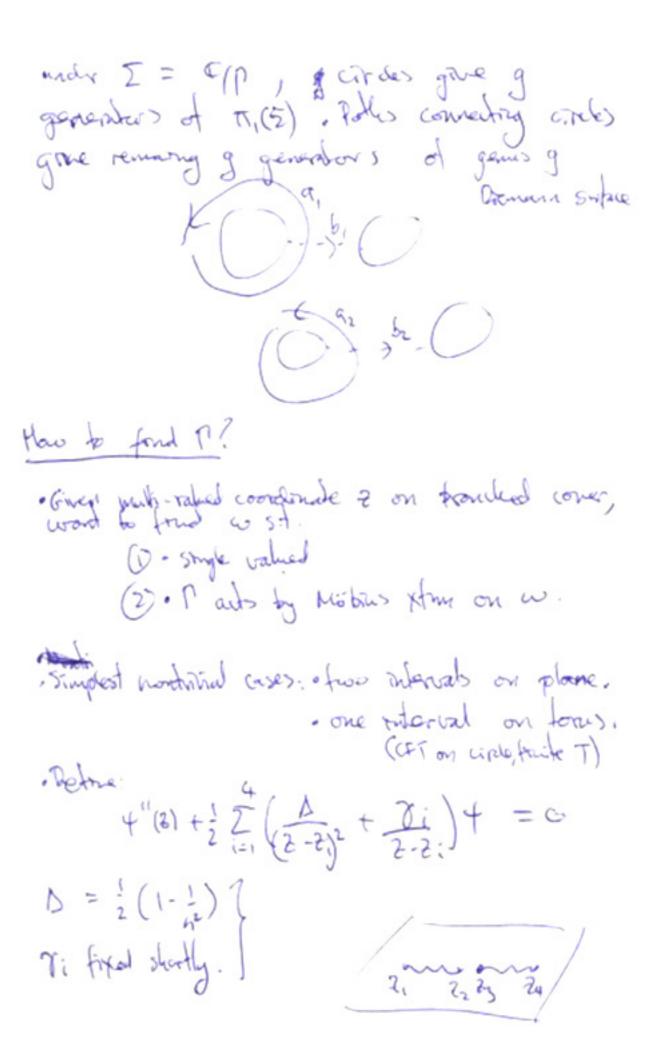
the RT ensuer for two merveds on place.

Johnstyy fective (buenon from RT) Small seprature: (engle separation)

glase transition -> change of downant windows zation.



Equ has 2 informed solve: $4, 4$ .  Define: $\omega = \frac{4(2)}{4(2)}$ new 2: $4 \sim (2-2)^{(1\pm 1/2)/2}$ $= 0  \omega \sim (2-2)^{1/2} \rightarrow 3$ single valued on $1 \rightarrow 1$ cover.
If we outegrate pair (4,12) oround where ( enclosing some De3, get mondroung:  (41) +> M(c) (41) M(c) = (ab) EPSO(2)
This fells as Alat for a to most be Hantstral;
Final step: too many quakets! $g = N-1$ eg. $N=2$ :  The two manhitial cycles
should be generated by one wit two generators.



AdS3: 482 = 252 + dudio near 3-00 (conformal body.) 751(2,0) acts via Mobius xfrus : WHIL(w) = awto ad-bc=1. 3 m) 12/(w) } = need to find P st. I = C/n. with ( sugge of Mistirus this. To Called Solothy informizedron Why rensonably? Mibris maps circles to circles: Sup The soldby go will be required by g elements of 951 (2,0), Conside 29 disjoind circles s.f Ci = Li(Ci)

5 in general difficult to compute. "outrageous" Ryu-Takny aragi proposal for theories with classical growing deads-It's frue! Hortnang Faulkner; Lewkouy at Hoddaren Connection sparetime ( - enternglement! -DGo beyond classical growity in complet rebry, Lo directly comple the talk priften functions for the Zu at one loop. We will obtain one-less corrections to the RT formula Step I: Schotlay unifornization Emskin's equations in 2+1 bulk: geometry is a quotent AdS3/p , with P < PSL(2,0) holography: ZCF(I) = Zbulk (2(AdS3/P) = I) for wi. I: not brown of a over region A. therefore need to: (i) find ? (ii) evaluate 2 (Al3/p)