

# Cosmological neutrinos after Planck

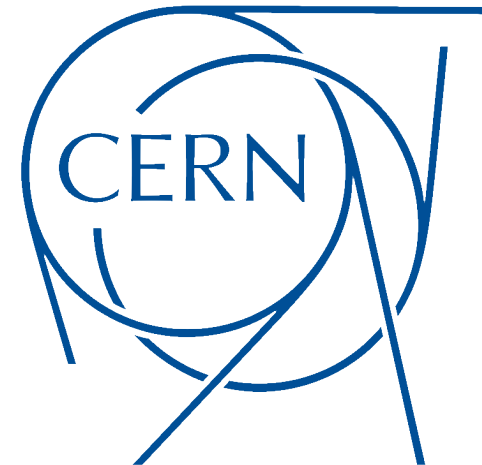
Jan Hamann

CERN



Workshop on the Origin  
of Neutrino Mass —  
From Majorana to LHC

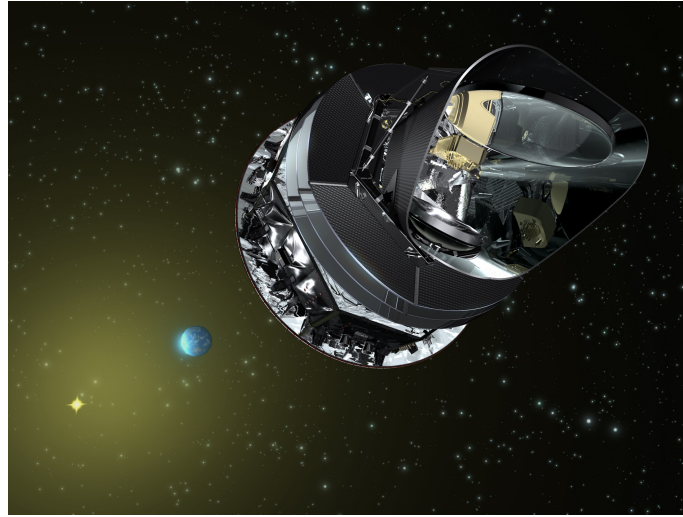
ICTP Trieste, 2-5 Oct 2013



# Planck at a glance



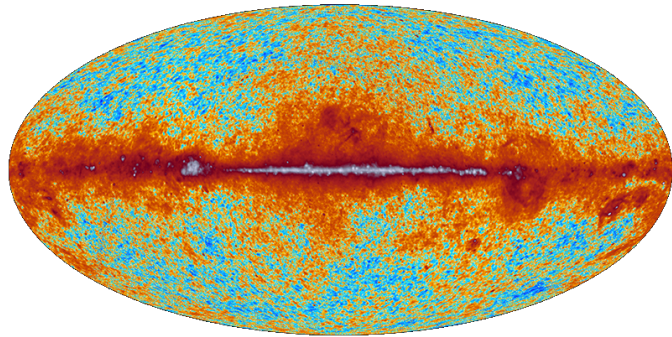
# Planck at a glance



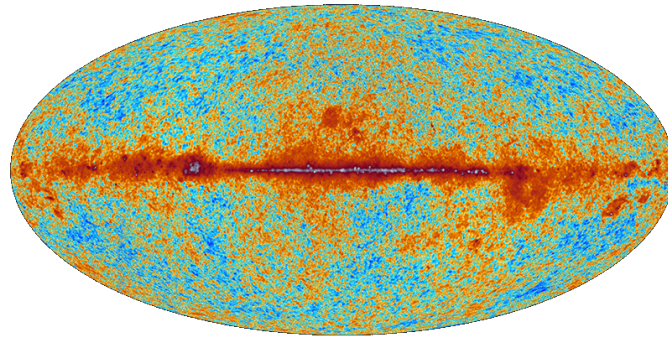
**Table 2.** *Planck* performance parameters determined from flight data.

		CHANNEL	$N_{\text{detectors}}^{\text{a}}$	$\nu_{\text{center}}^{\text{b}}$ [GHz]	SCANNING BEAM <sup>c</sup>		NOISE <sup>d</sup> SENSITIVITY	
					FWHM [arcmin]	Ellipticity	$[\mu\text{K}_{\text{RJ}} \text{s}^{1/2}][\mu\text{K}_{\text{CMB}} \text{s}^{1/2}]$	
LFI	{	30 GHz .....	4	28.4	33.16	1.37	145.4	148.5
		44 GHz .....	6	44.1	28.09	1.25	164.8	173.2
		70 GHz .....	12	70.4	13.08	1.27	133.9	151.9
		100 GHz .....	8	100	9.59	1.21	31.52	41.3
HFI	{	143 GHz .....	11	143	7.18	1.04	10.38	17.4
		217 GHz .....	12	217	4.87	1.22	7.45	23.8
		353 GHz .....	12	353	4.7	1.2	5.52	78.8
		545 GHz .....	3	545	4.73	1.18	2.66	0.0259 <sup>d</sup>
		857 GHz .....	4	857	4.51	1.38	1.33	0.0259 <sup>d</sup>

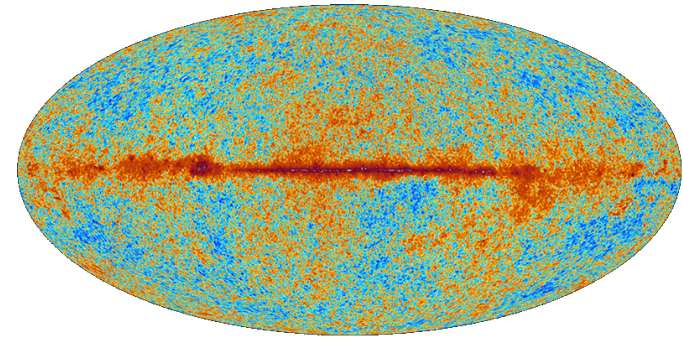
# Planck's view of the microwave sky



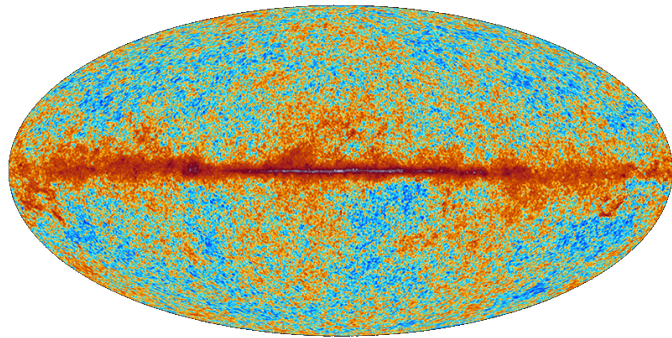
30 GHz



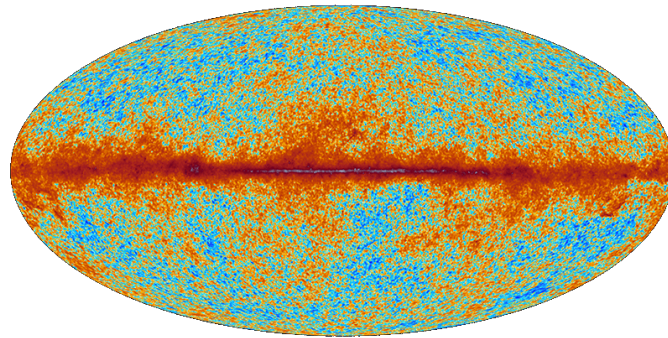
44 GHz



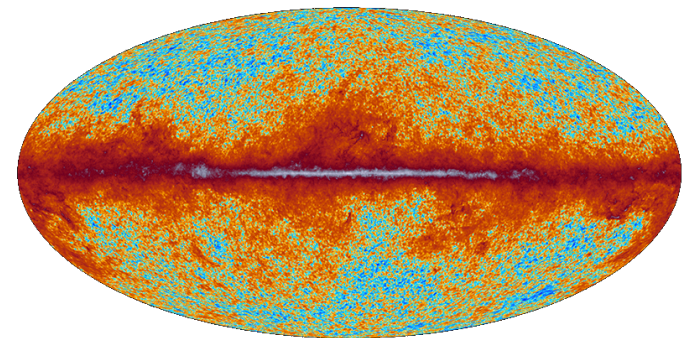
70 GHz



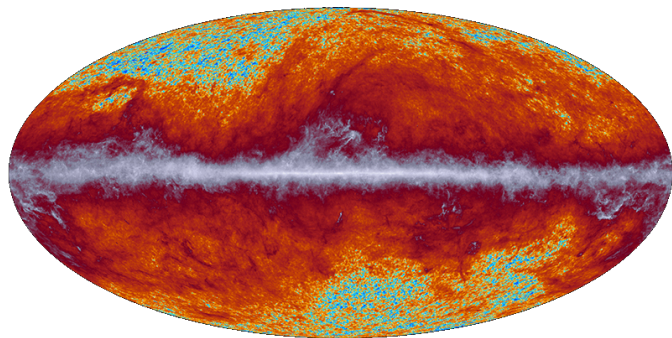
100 GHz



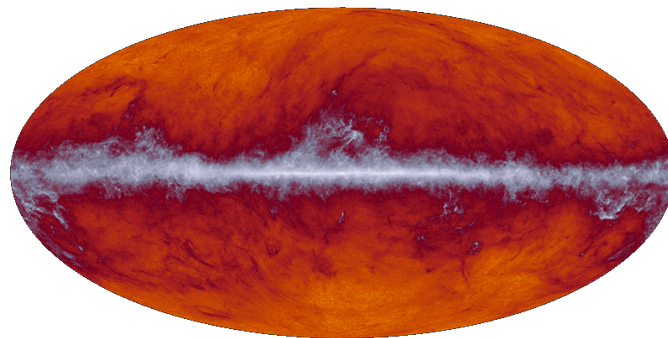
143 GHz



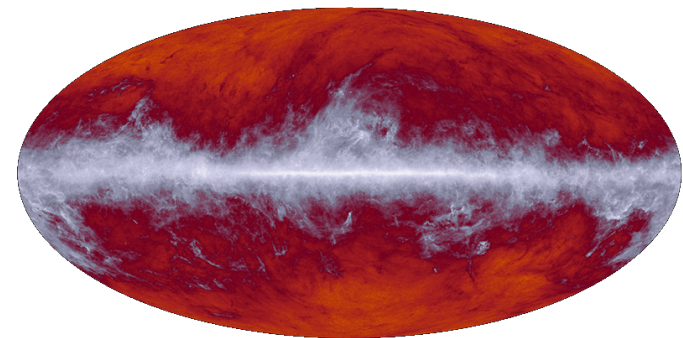
217 GHz



353 GHz

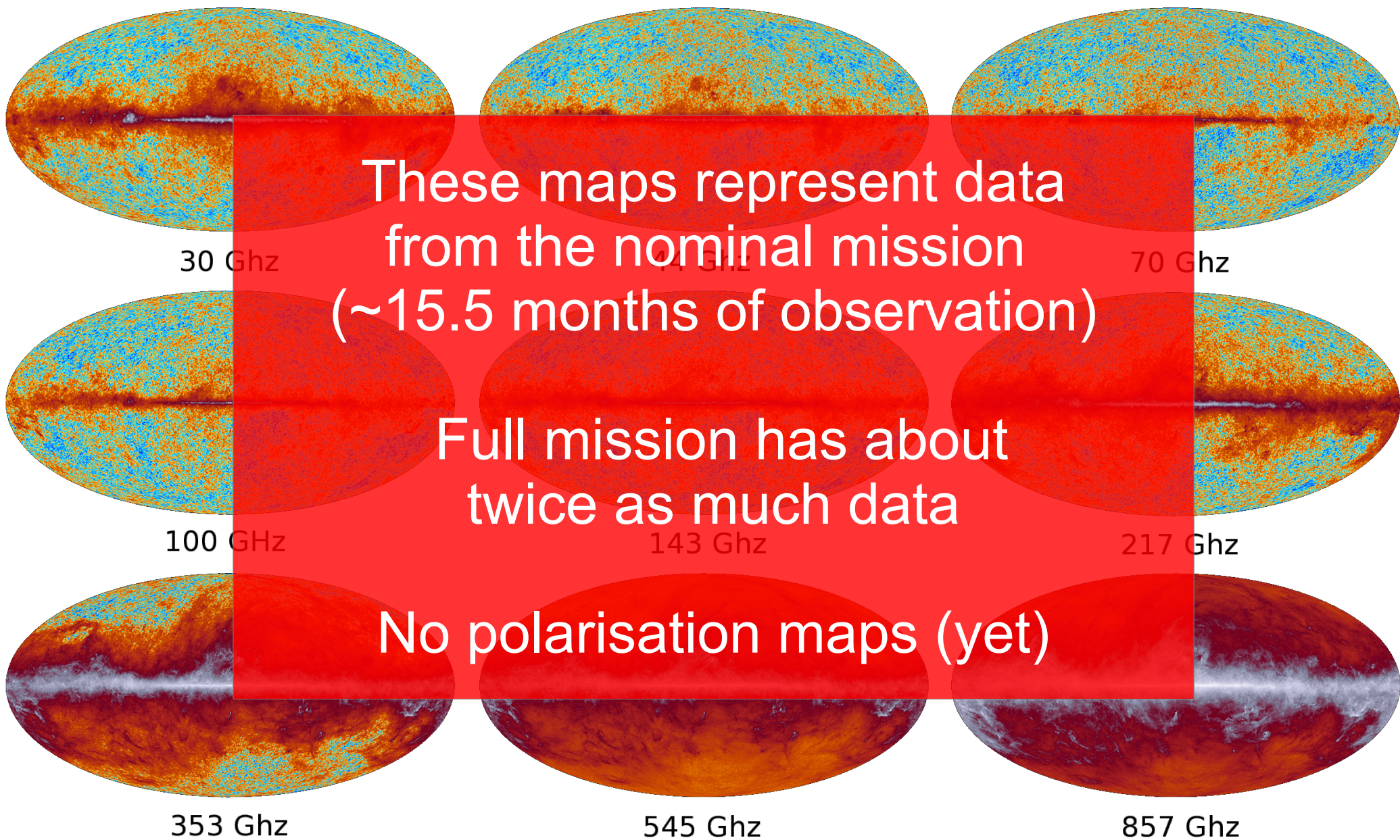


545 GHz

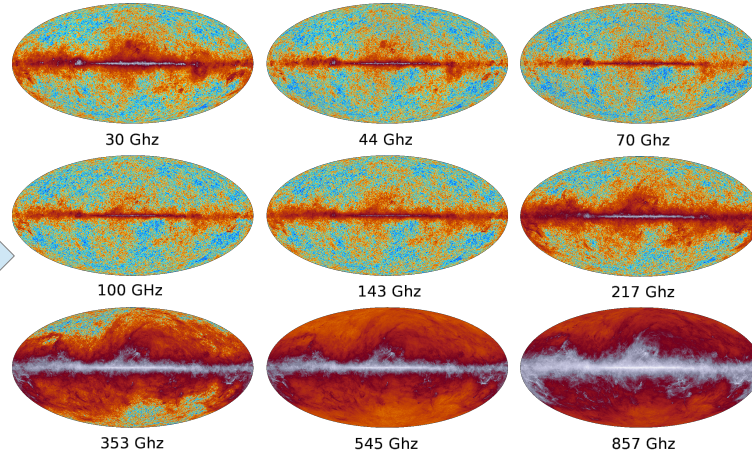


857 GHz

# Planck's view of the microwave sky

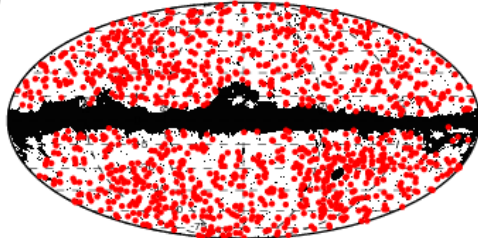


# Cosmological observables



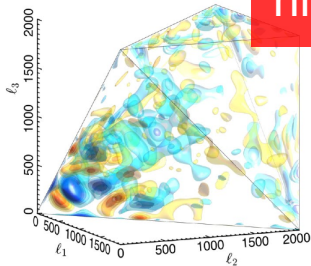
2-point correlation

SZ-effect

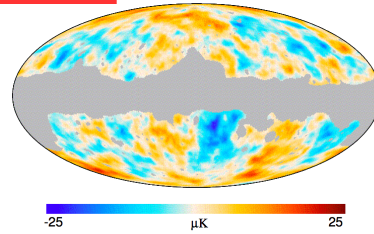


Galaxy clusters  
→ cluster mass function  
(when combined with X-ray data)

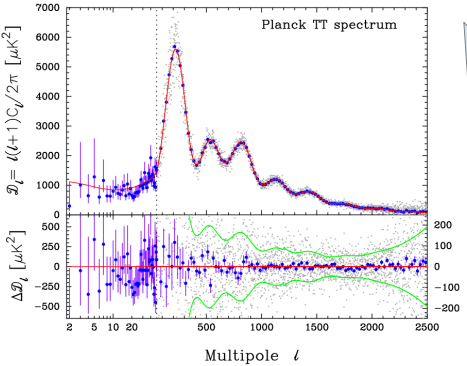
higher order correlations



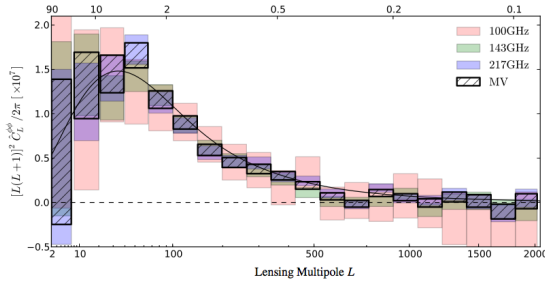
Primordial non-Gaussianity



Integrated Sachs-Wolfe effect



Angular power spectrum



Power spectrum of the lensing potential

What have we learnt about  
cosmology?

# A maximally boring Universe?



No real surprises, no paradigm changes



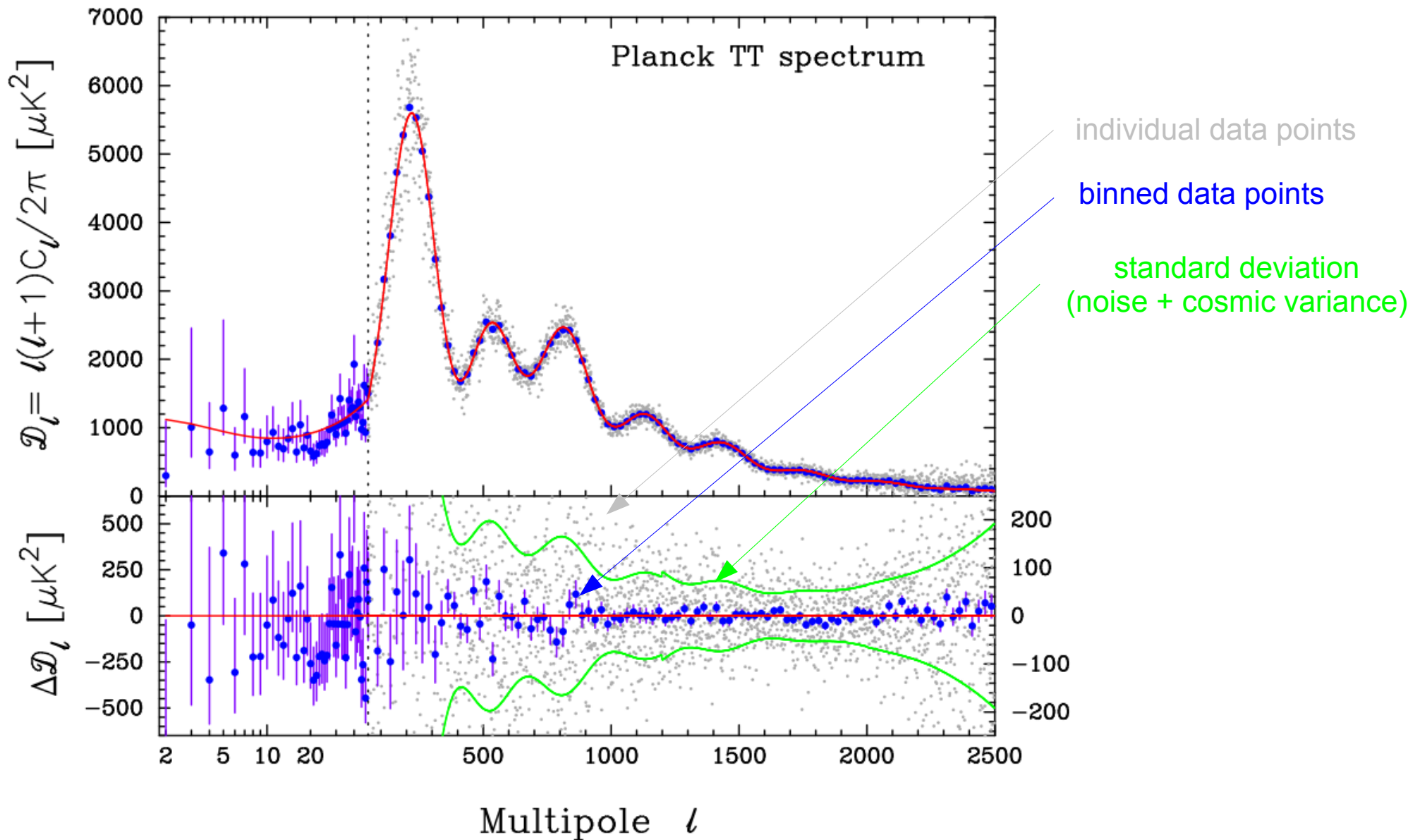
The cosmological “standard” ( $\Lambda$ CDM) model still stands strong



Significant improvements in constraints on nearly all interesting cosmological parameters



# Planck (temperature) angular power spectrum



# Goodness-of-fit of $\Lambda$ CDM

**Table 6.** Goodness-of-fit tests for the *Planck* spectra. The  $\Delta\chi^2 = \chi^2 - N_\ell$  is the difference from the mean assuming the model is correct, and the last column expresses  $\Delta\chi^2$  in units of the dispersion  $\sqrt{2N_\ell}$ .

Spectrum	$\ell_{\min}$	$\ell_{\max}$	$\chi^2$	$\chi^2/N_\ell$	$\Delta\chi^2/\sqrt{2N_\ell}$
100 $\times$ 100	50	1200	1158	1.01	0.14
143 $\times$ 143	50	2000	1883	0.97	-1.09
217 $\times$ 217	500	2500	2079	1.04	1.23
143 $\times$ 217	500	2500	1930	0.96	-1.13
All	50	2500	2564	1.05	1.62

# Different models/data combinations: “the grid”

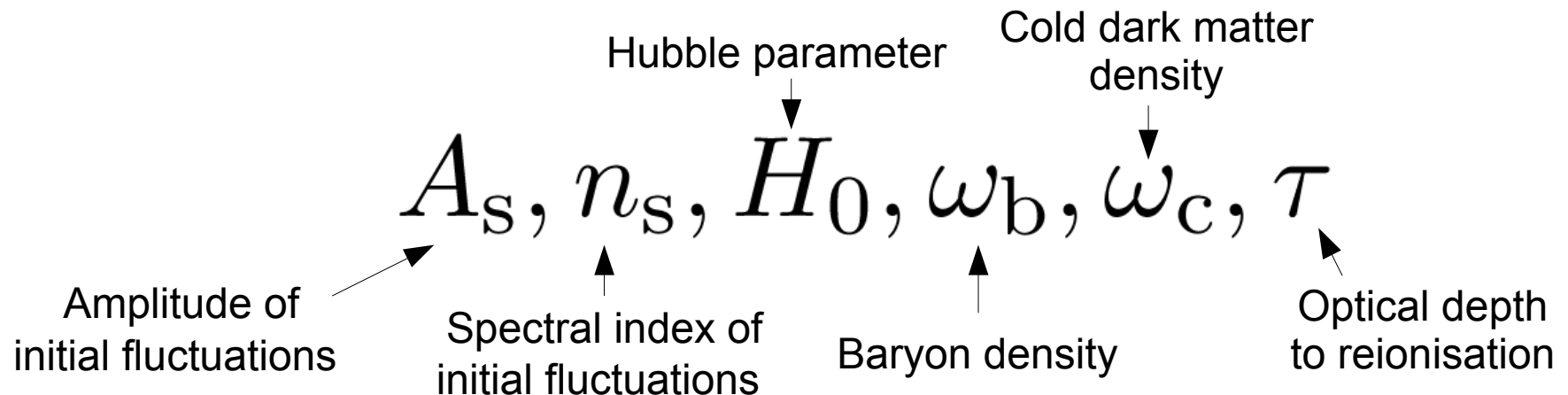
- Basic  $\Lambda$ CDM model plus eighteen different extensions
- Each of them fit with up to thirty-four combinations of Planck with external data sets
- Almost 400 pages of tables with parameter constraints
- Available online under:

[http://www.sciops.esa.int/index.php?project=planck&page=Planck\\_Legacy\\_Archive](http://www.sciops.esa.int/index.php?project=planck&page=Planck_Legacy_Archive)

- CMB data alone show no preference for extended models!

# The $\Lambda$ CDM model

Six cosmological parameters:



plus another 14 “nuisance” parameters for Planck data, describing

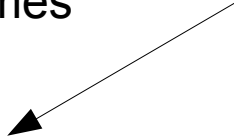
- perturbations from
  - the cosmic infrared background (4)
  - unresolved point sources (4)
  - the Sunyaev-Zeldovich effect (3)
- beam shape uncertainties (1)
- relative calibration uncertainties (2)

So what about neutrinos?

# Cosmological neutrinos

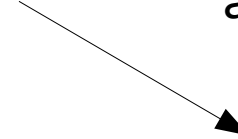
Cosmic neutrino background  
(decoupling at  $T \sim 1 \text{ MeV}$ )

at early times



Relativistic  
(radiation-like)

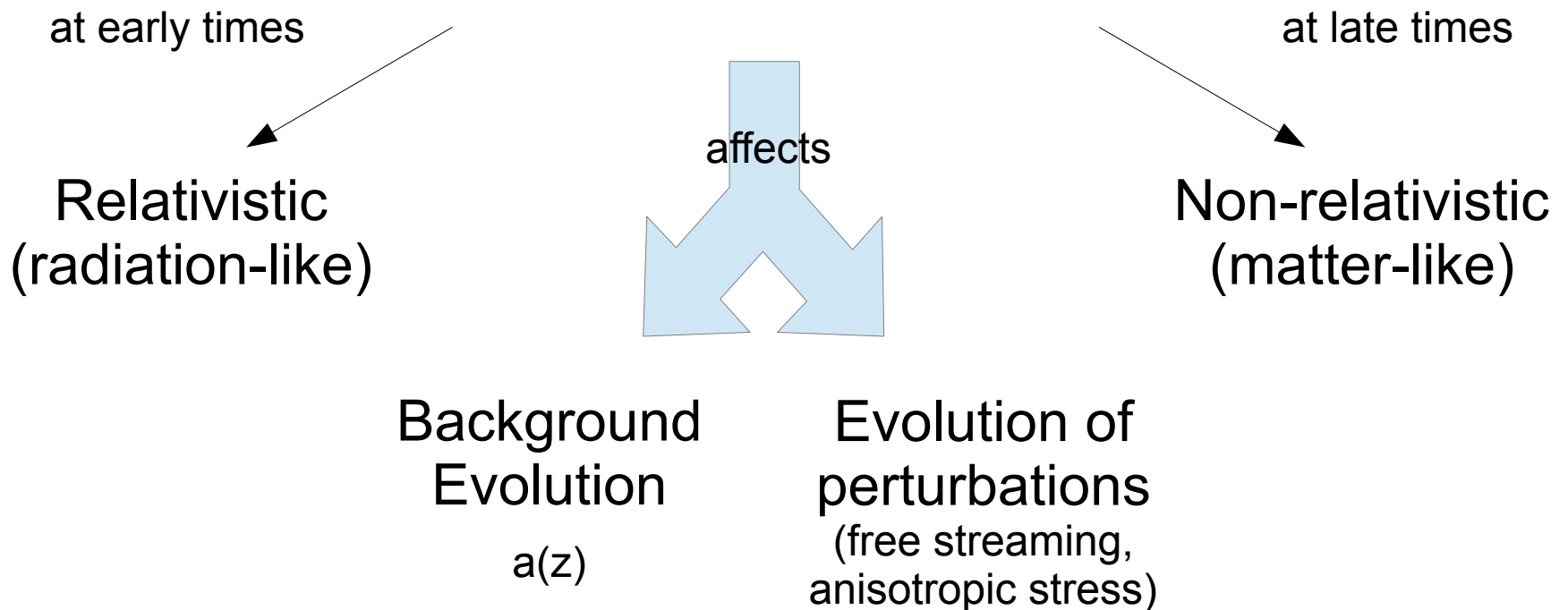
at late times



Non-relativistic  
(matter-like)

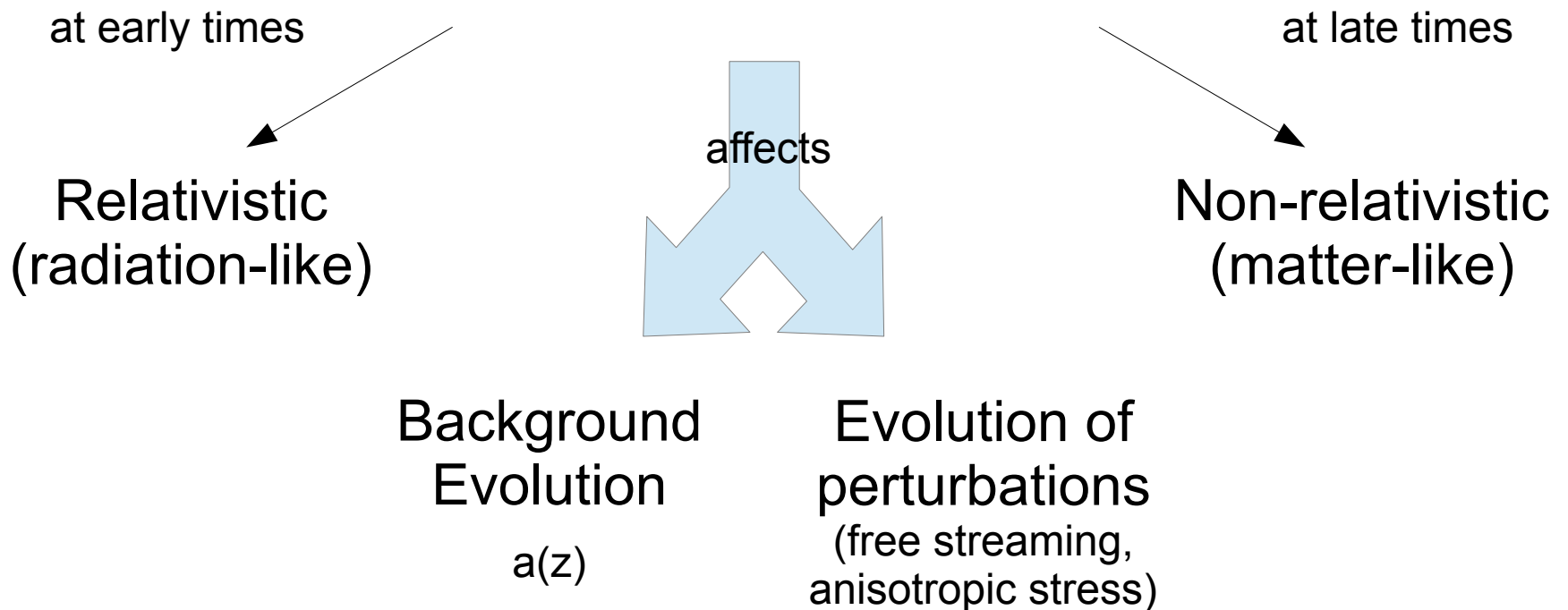
# Cosmological neutrinos

## Cosmic neutrino background (decoupling at $T \sim 1 \text{ MeV}$ )



# Cosmological neutrinos

## Cosmic neutrino background (decoupling at $T \sim 1 \text{ MeV}$ )



These are purely gravitational effects which do not care about “neutrino-ness” at all!



# Cosmological neutrinos: parameters

How much energy density do “neutrinos” contribute

at early times?

at late times?

photon energy density      Fermi-Dirac vs. Bose-Einstein      lower neutrino temperature

$$\rho_r = \rho_\gamma \left[ 1 + N_{\text{eff}} \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} \right]$$

radiation energy density      effective number of neutrino species

The diagram shows the equation for radiation energy density  $\rho_r$  as a function of photon energy density  $\rho_\gamma$  and the effective number of neutrino species  $N_{\text{eff}}$ . The equation is  $\rho_r = \rho_\gamma \left[ 1 + N_{\text{eff}} \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} \right]$ . Arrows point from descriptive text to the corresponding parts of the equation: 'photon energy density' points to  $\rho_\gamma$ ; 'radiation energy density' points to  $\rho_r$ ; 'Fermi-Dirac vs. Bose-Einstein' points to the  $\frac{7}{8}$  factor; 'effective number of neutrino species' points to  $N_{\text{eff}}$ ; and 'lower neutrino temperature' points to the  $\left( \frac{4}{11} \right)^{4/3}$  term.

Standard model/ $\Lambda$ CDM:  $N_{\text{eff}} = 3.046$

# Cosmological neutrinos: parameters

How much energy density do “neutrinos” contribute

at early times?

at late times?

photon energy density vs. Fermi-Dirac vs. Bose-Einstein lower neutrino temperature

$$\rho_r = \rho_\gamma \left[ 1 + N_{\text{eff}} \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} \right]$$

radiation energy density      effective number of neutrino species

neutrino energy density

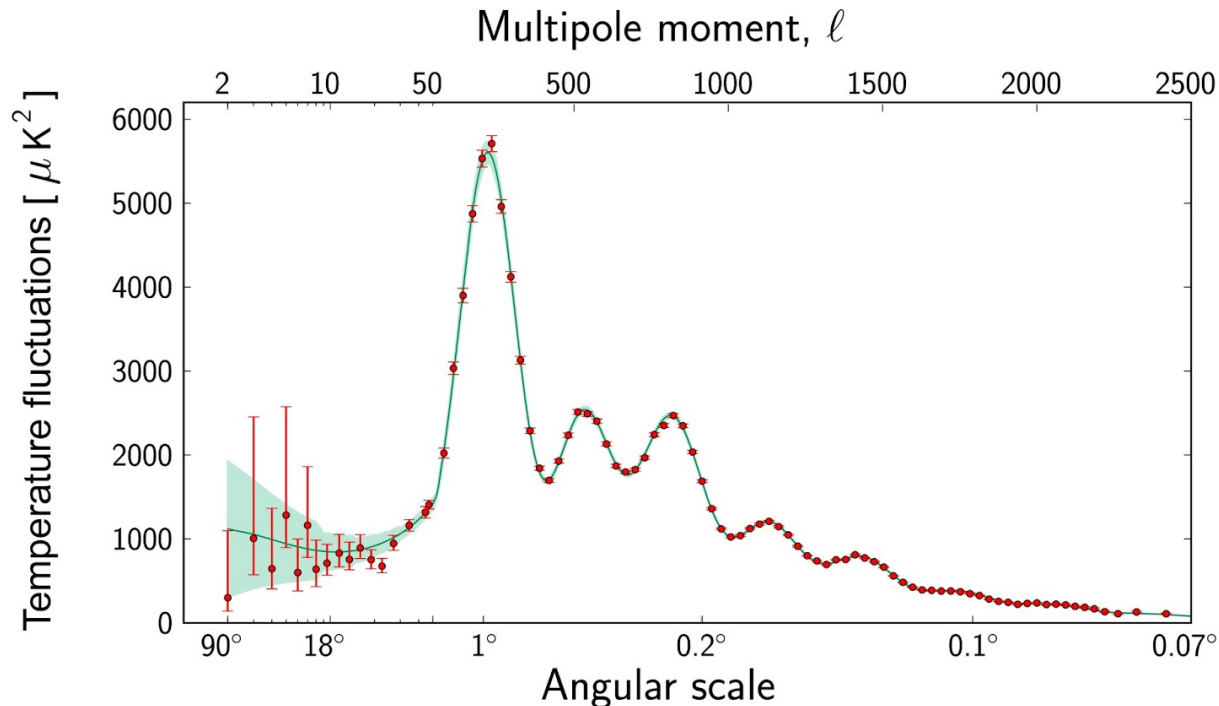
$$\Omega_\nu h^2 \approx \frac{\sum m_\nu}{93 \text{ eV}}$$

sum of neutrino masses

Standard model/ $\Lambda$ CDM:  $N_{\text{eff}} = 3.046$

$\Lambda$ CDM:  $\sum m_\nu = 0.06 \text{ eV}$

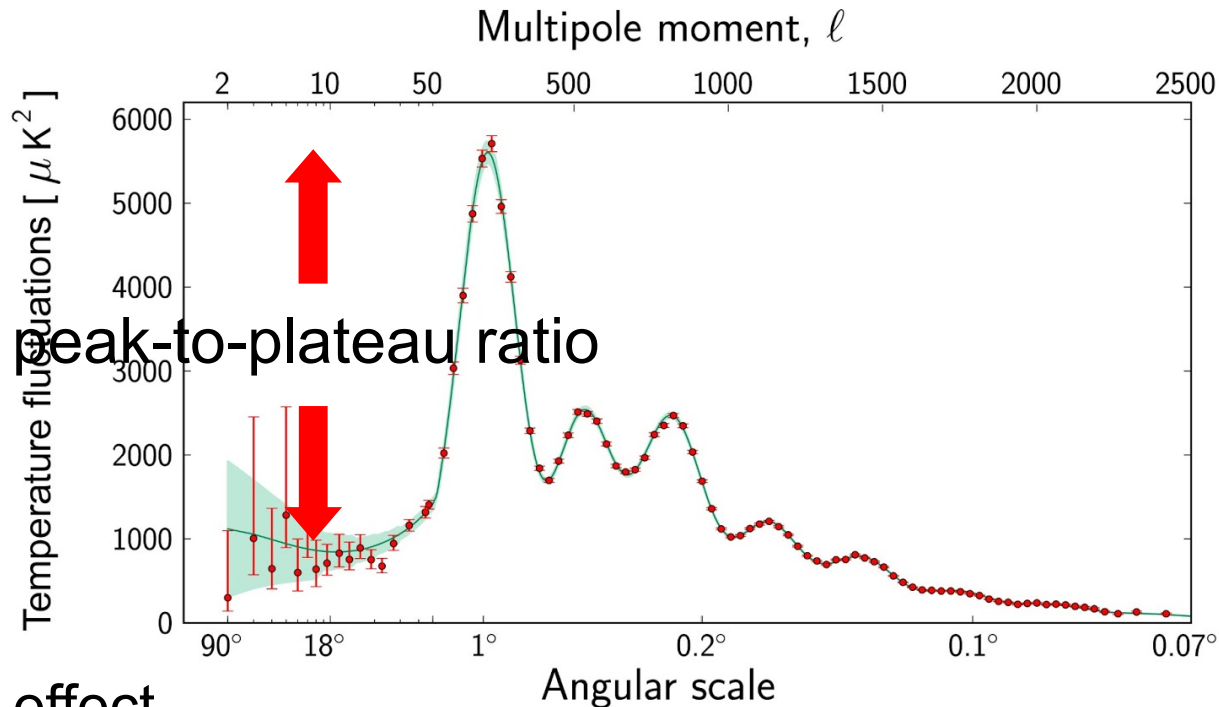
# Neutrino parameters: understanding degeneracies



- Parameters must be inferred from CMB power spectrum
- Adding parameters often introduces parameter degeneracies
- To understand degeneracy directions, look at parameter combinations that leave broad features of the spectrum unchanged

[e.g., Bashinsky & Seljak 2003; Lesgourgues et al. 2013; Archidiacono et al. 2013]

# Neutrino parameters: understanding degeneracies



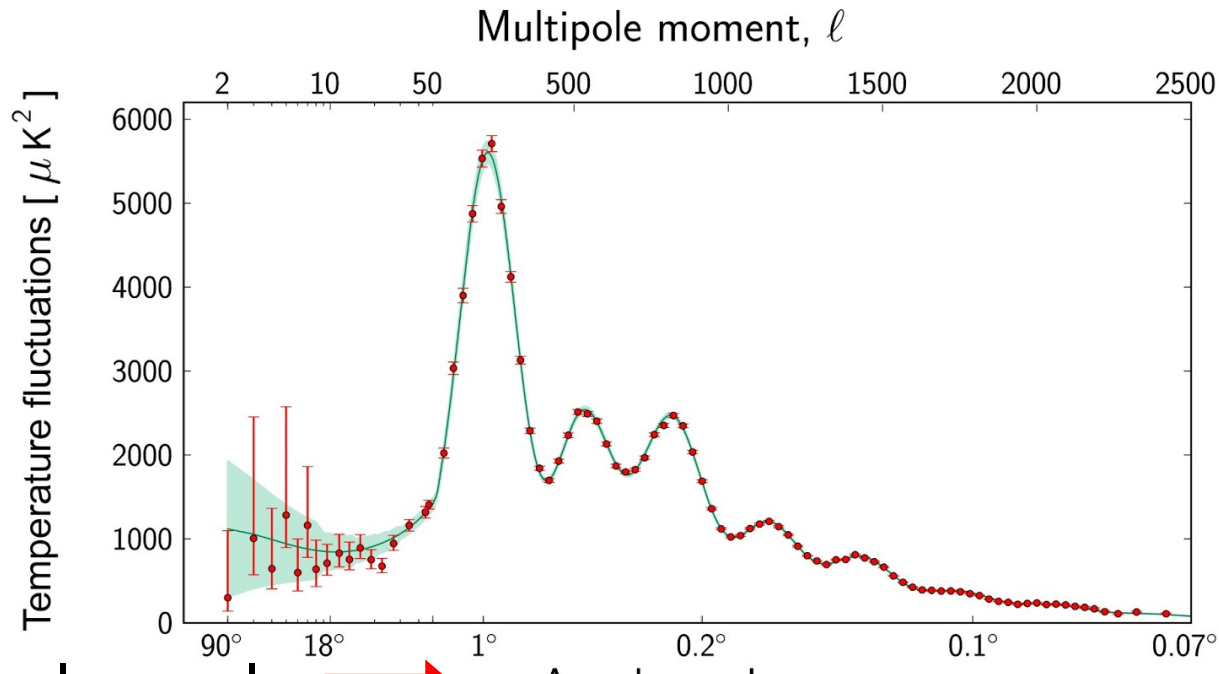
via early ISW effect  
related to redshift of  
matter-radiation equality

$$1 + z_{\text{eq}} = \frac{\omega_{\text{m}}}{\omega_{\gamma}} \frac{1}{1 + 0.2271 N_{\text{eff}}}$$

Photon energy density

Matter density

# Neutrino parameters: understanding degeneracies



$$\theta_s \equiv r_s(z_*) / D_A(z_*)$$

Redshift of decoupling

$$r_s(z_*) \equiv \int_{z_*}^{\infty} dz \frac{c_s(z)}{H(z)}$$

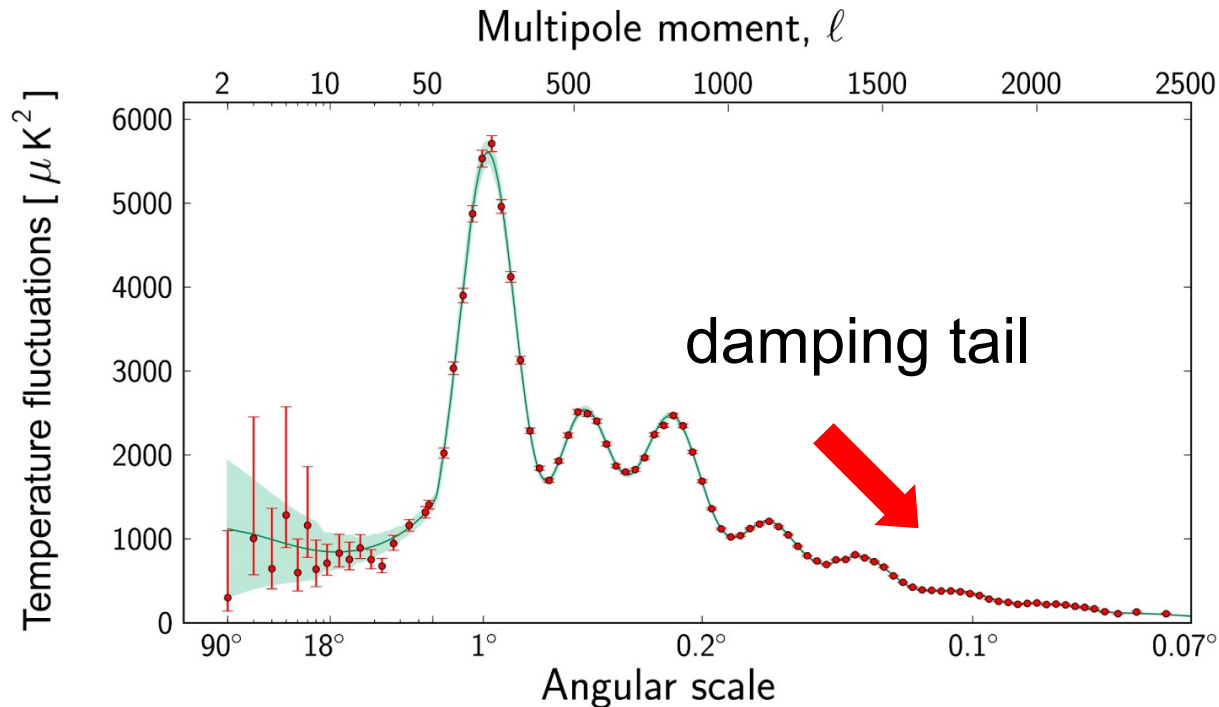
Sound horizon

Sound speed

$$D_A(z_*) \equiv \int_0^{z_*} \frac{dz}{H(z)}$$

Angular diameter distance

# Neutrino parameters: understanding degeneracies



$$\theta_d \equiv r_d(z_\star) / D_A(z_\star)$$

↑  
Photon diffusion scale

Accidental approximate  
degeneracy with  $n_s$ !

# Neutrino parameters: main degeneracy directions

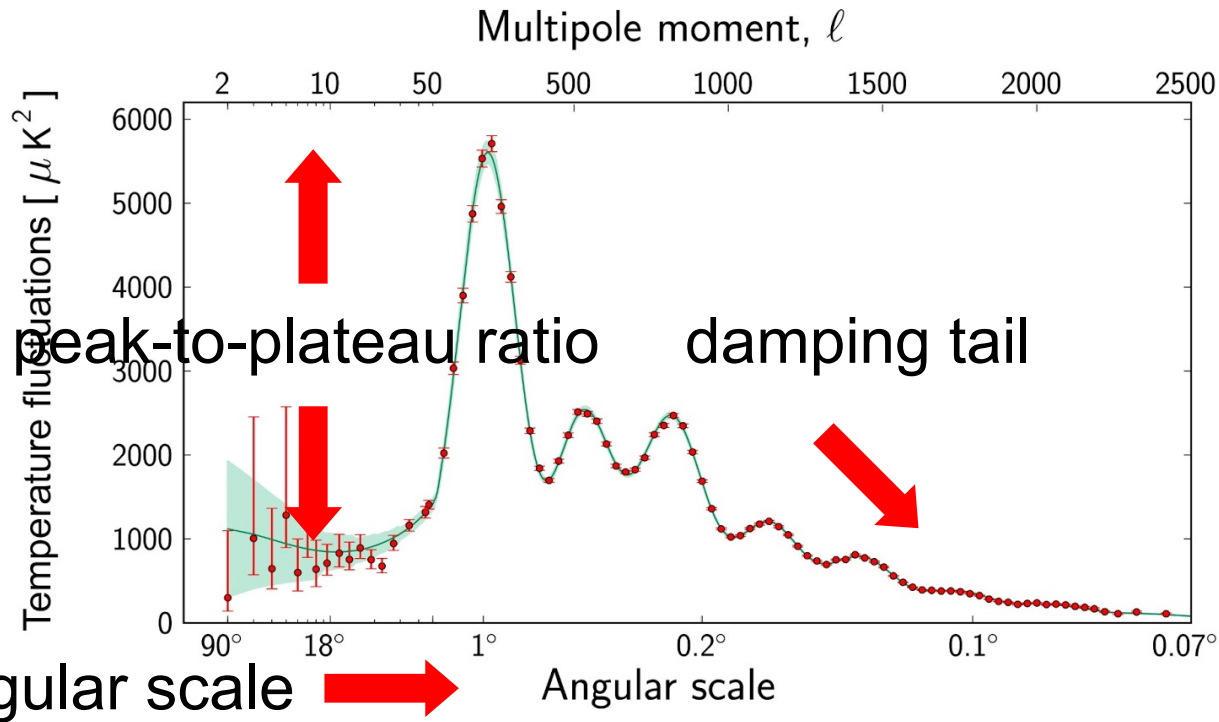
Increasing  $N_{\text{eff}}$  ...

- increases  $\omega_m$
- increases  $H_0$
- increases  $n_s$

Increasing  $\sum m_\nu$  ...

- does not affect  $\omega_m$  much
- decreases  $H_0$
- decreases  $n_s$

# Why are non-CMB data sets important?



- In  $\Lambda$ CDM, these three observables essentially depend only on  $\omega_m$ ,  $H_0$  and  $n_s$
- In extended models, often a dependence on a fourth parameter (e.g., neutrino mass, number of neutrinos, curvature, etc.)  $\rightarrow$  unconstrained direction
- External data (BAO, clusters, HST, lensing) can break degeneracy

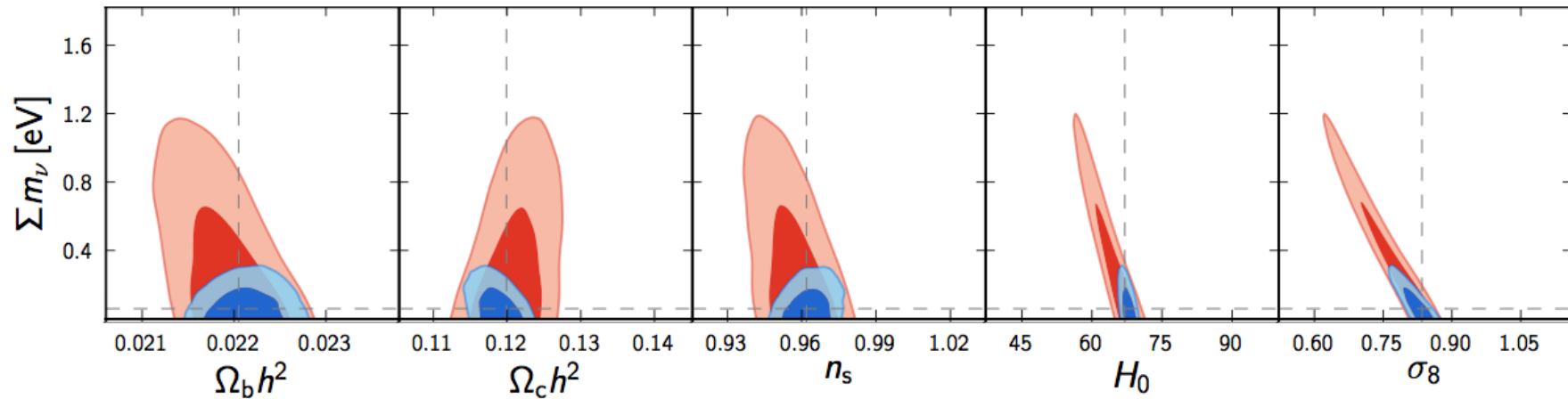


Constraints from  
Planck temperature  
+ WMAP large scale polarisation  
(+ ACT/SPT small scale temperature)  
(+ Baryon Acoustic Oscillation)  
data

# Neutrino mass constraints

*Planck + WP*

*Planck + WP + BAO*



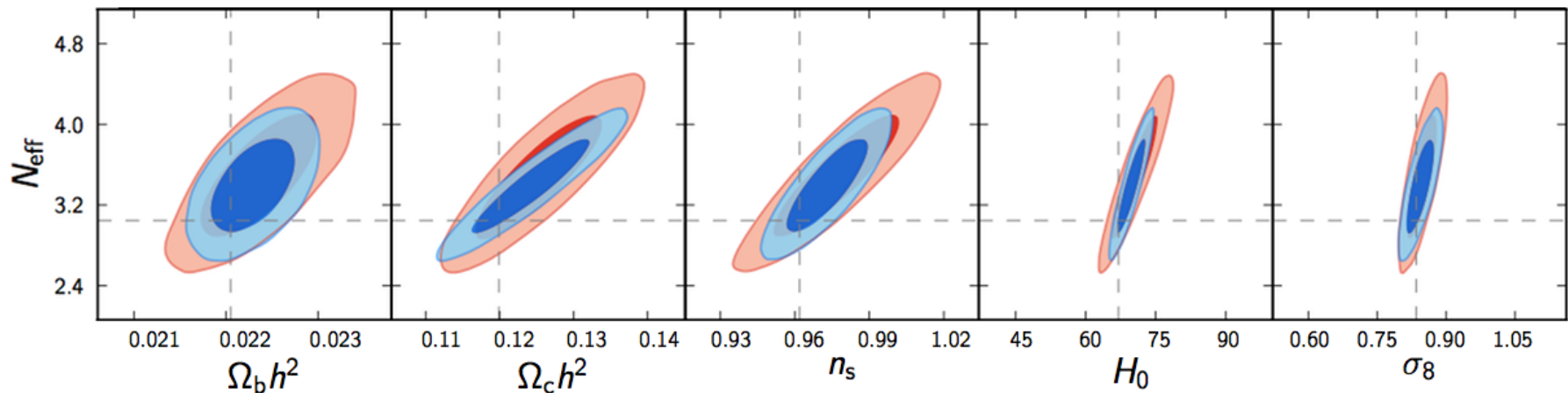
Parameter	<i>Planck+WP</i>		<i>Planck+WP+BAO</i>		<i>Planck+WP+highL</i>		<i>Planck+WP+highL+BAO</i>	
	Best fit	95% limits	Best fit	95% limits	Best fit	95% limits	Best fit	95% limits
$\Sigma m_\nu$ [eV] . . . . .	0.022	< 0.933	0.002	< 0.247	0.023	< 0.663	0.000	< 0.230

No evidence for neutrino masses

# Effective number of neutrino species

*Planck + WP*

*Planck + WP + BAO*



*Planck+WP*

*Planck+WP+BAO*

*Planck+WP+highL*

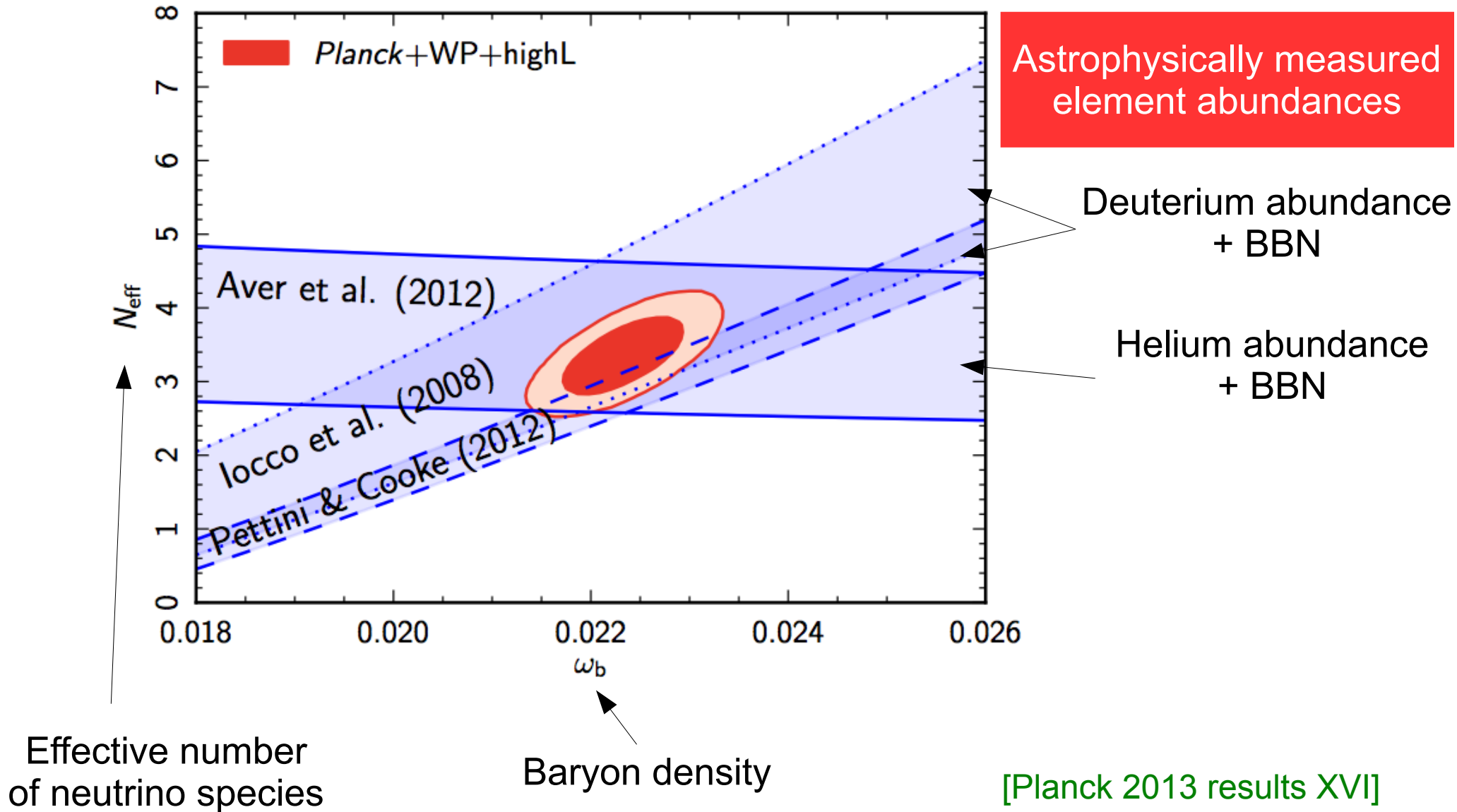
*Planck+WP+highL+BAO*

Parameter	<i>Planck+WP</i>		<i>Planck+WP+BAO</i>		<i>Planck+WP+highL</i>		<i>Planck+WP+highL+BAO</i>	
	Best fit	95% limits	Best fit	95% limits	Best fit	95% limits	Best fit	95% limits
$N_{\text{eff}}$ . . . . .	3.08	$3.51^{+0.80}_{-0.74}$	3.08	$3.40^{+0.59}_{-0.57}$	3.23	$3.36^{+0.68}_{-0.64}$	3.22	$3.30^{+0.54}_{-0.51}$

No evidence for extra (“dark”) radiation,  
but overwhelming evidence for existence of “neutrino” background

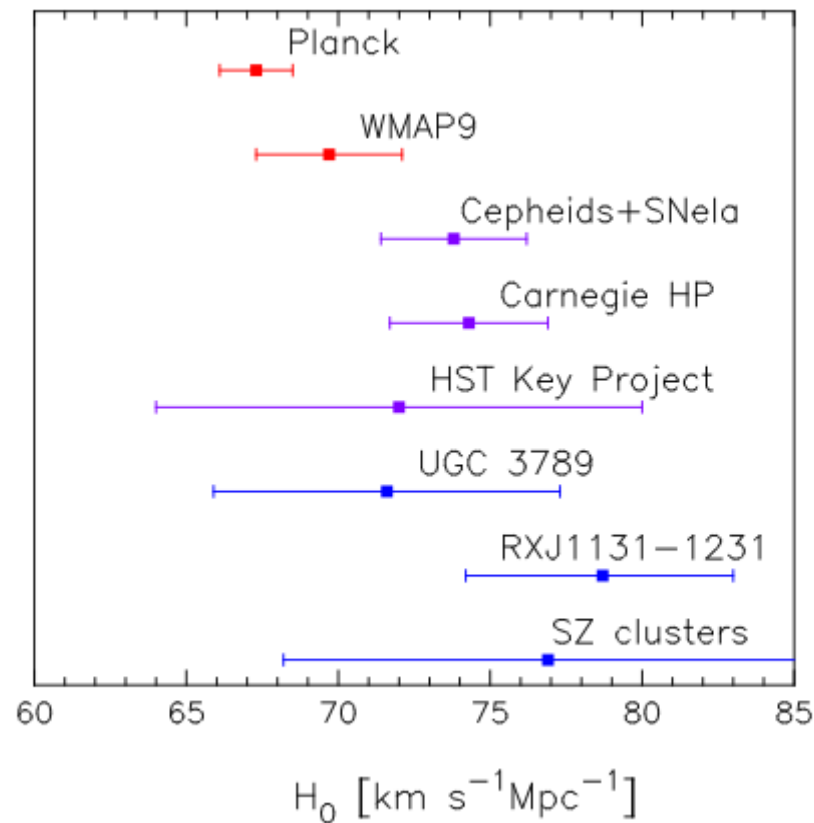
[Planck 2013 results XVI]

# Consistency with BBN and primordial element abundances



# Discrepancies (?)

- Local measurements of the Hubble parameter



In  $\Lambda$ CDM, CMB seems to prefer too small  
Values of the Hubble parameter?

# Discrepancies (?)

- Cluster counts: rms amplitude of  
matter perturbation  
at scale of  $8 h^{-1}$  Mpc

$\sigma_8 (\Omega_m/0.27)^{0.3} = 0.782 \pm 0.010$	Planck clusters + X-ray
$\sigma_8 (\Omega_m/0.27)^{0.3} = 0.869 \pm 0.023$	CMB
- Galaxy shear measurements:

$\sigma_8 (\Omega_m/0.27)^{0.46} = 0.774 \pm 0.040$	CFHTLenS
$\sigma_8 (\Omega_m/0.27)^{0.46} = 0.891 \pm 0.031$	CMB

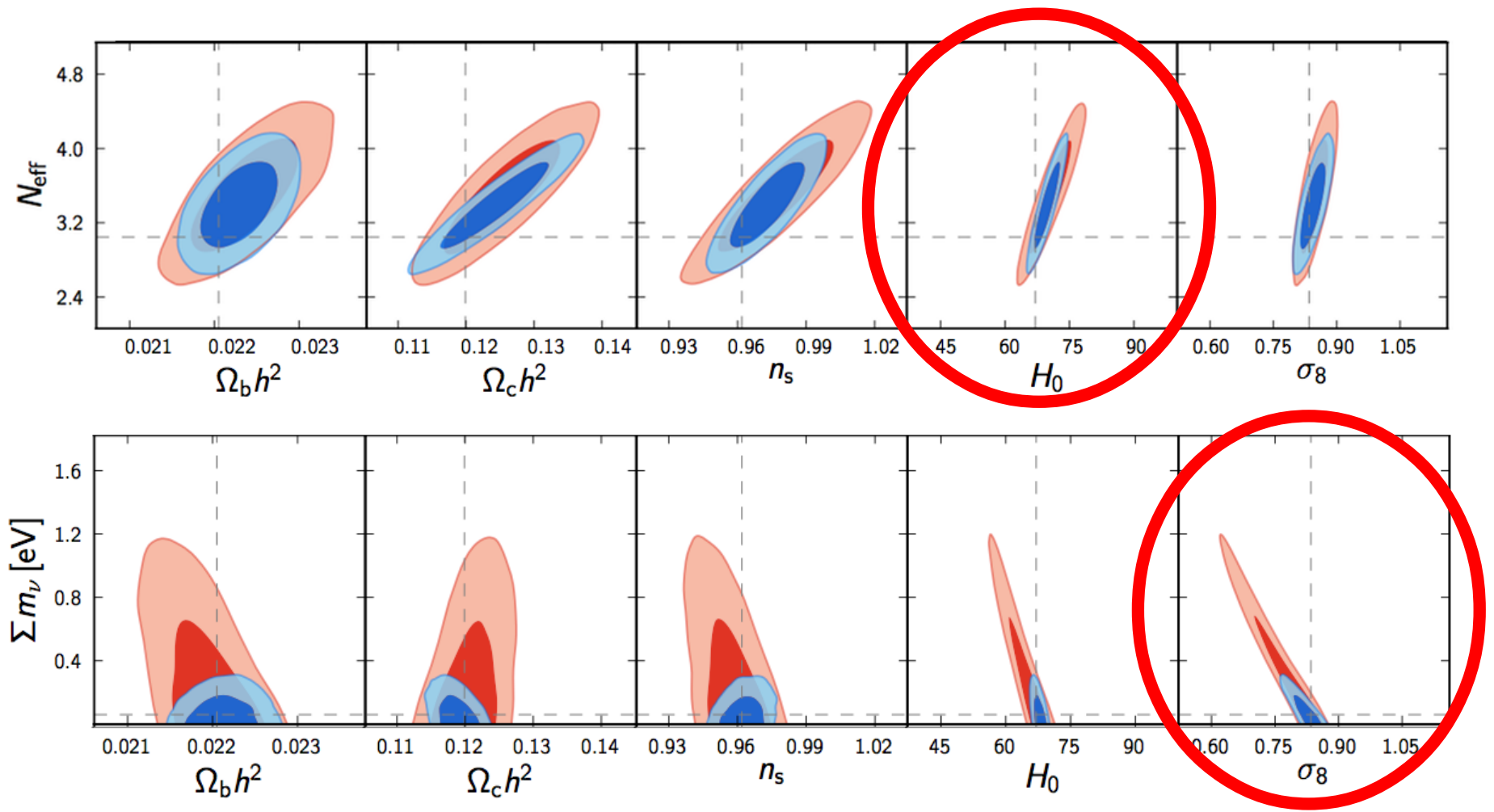
In  $\Lambda$ CDM, CMB seems to have a preference for too much power on small scales?

# Consistency with other data sets

- Parameter discrepancies could imply underestimated systematical uncertainties or bias in either data set
- Parameters are not directly measured, but rather inferred from the data  
→ Discrepancy is model-dependent!
- Are we perhaps looking at the wrong model?
- If so, what model could resolve the discrepancies?

# Look at degeneracies

Extra radiation can enhance  $H_0$



Hot dark matter can suppress  $\sigma_8$



# Sterile neutrinos as a solution?

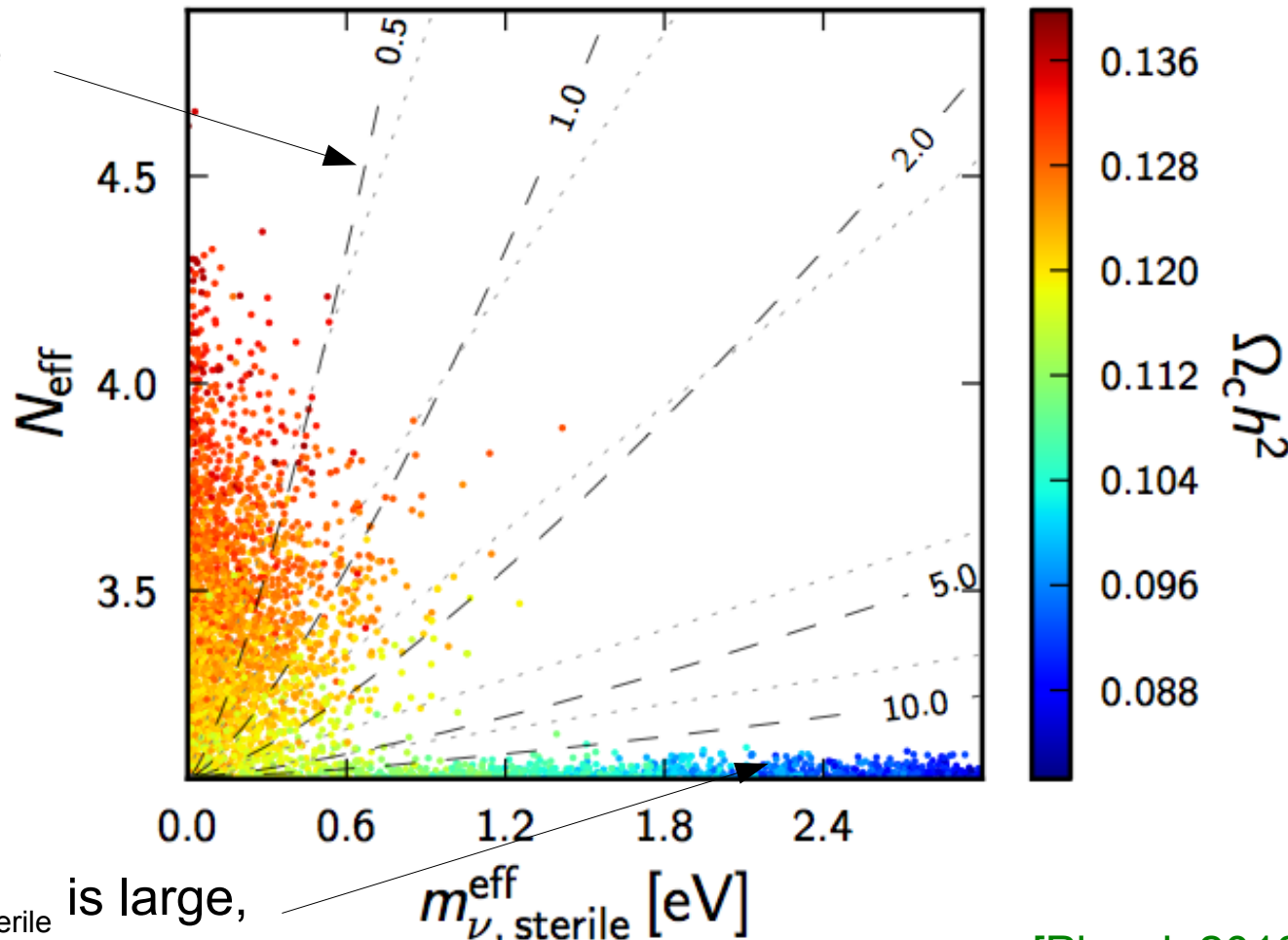
- Consider standard active neutrinos plus additional light particles (could be, e.g., sterile neutrinos)
- Characterised by two parameters:
  - Energy density when relativistic:  $\Delta N_{\text{eff}} = N_{\text{eff}} - 3.046$
  - Energy density today:  $m_{\nu, \text{sterile}}^{\text{eff}} \equiv (94.1 \omega_{\nu, \text{sterile}}) \text{ eV}$

effective mass is equal to  
physical mass if  $\Delta N_{\text{eff}} = 1$

# Curing discrepancies using hot dark matter?

CMB data only: no evidence

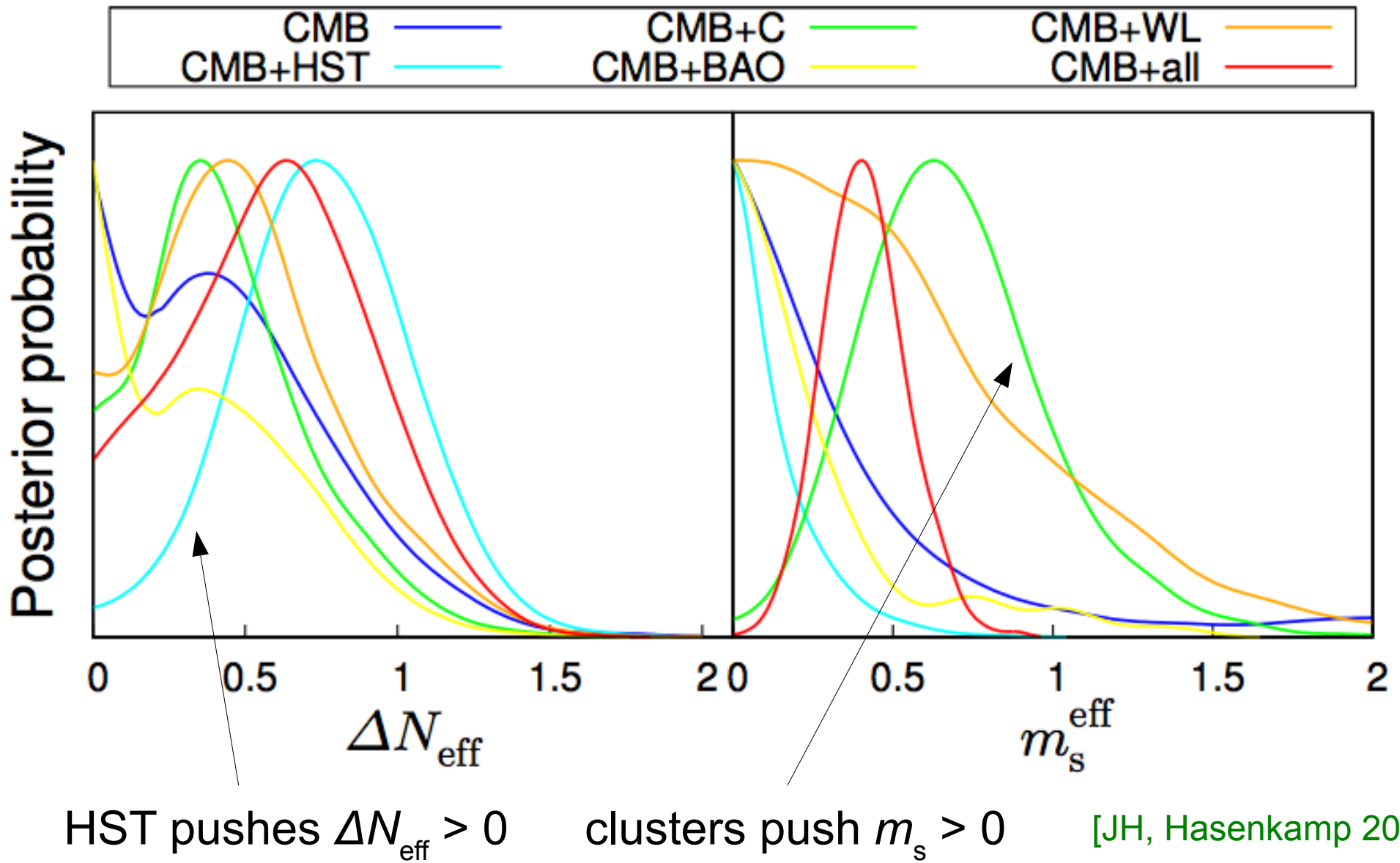
Lines of constant physical  $m_{\text{sterile}}$   
Dotted: thermal  
Dashed: D-W



Physical  $m_{\text{sterile}}$  is large,  
replaces part of CDM

[Planck 2013 results XVI]

# Curing discrepancies using hot dark matter?



# Curing discrepancies using hot dark matter?

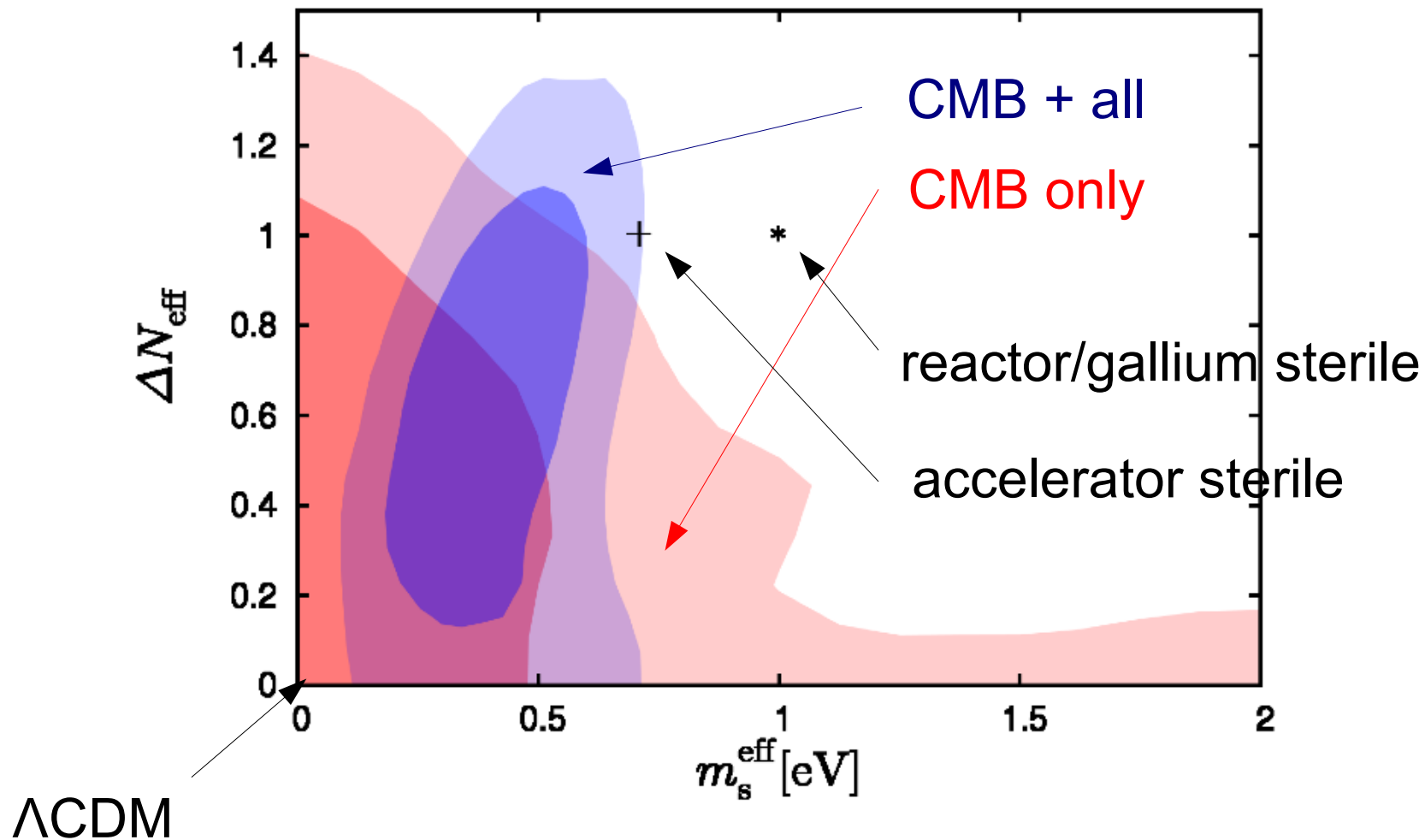
**Table 2.** Best fit effective  $\chi^2$  for various combinations of data sets in the vanilla (v) and sterile (s) models: total and individual contributions.

Data	$-2 \ln \mathcal{L}_{\max}^{\text{tot}}$	$-2 \ln \mathcal{L}_{\max}^{\text{CMB}}$	$-2 \ln \mathcal{L}_{\max}^{\text{HST}}$	$-2 \ln \mathcal{L}_{\max}^{\text{C}}$	$-2 \ln \mathcal{L}_{\max}^{\text{BAO}}$	$-2 \ln \mathcal{L}_{\max}^{\text{WL}}$	Model
CMB	9802.5	9802.5	—	—	—	—	v
	9802.3	9802.3	—	—	—	—	s
CMB+HST	9808.4	9803.6	4.8	—	—	—	v
	9803.2	9802.4	0.8	—	—	—	s
CMB+C	9818.1	9815.3	—	2.8	—	—	v
	9806.5	9806.3	—	0.1	—	—	s
CMB+BAO	9804.1	9802.7	—	—	1.4	—	v
	9804.0	9802.3	—	—	1.8	—	s
CMB+WL	9808.5	9804.2	—	—	—	4.3	v
	9806.4	9804.5	—	—	—	1.9	s
CMB+all	9825.2	9811.3	2.0	4.6	6.7	0.6	v
	9812.0	9807.4	2.2	0.2	1.7	0.5	s

No serious discrepancy remaining  
 → can combine data sets

$$\Delta\chi_{\text{eff}}^2 = 13.2$$

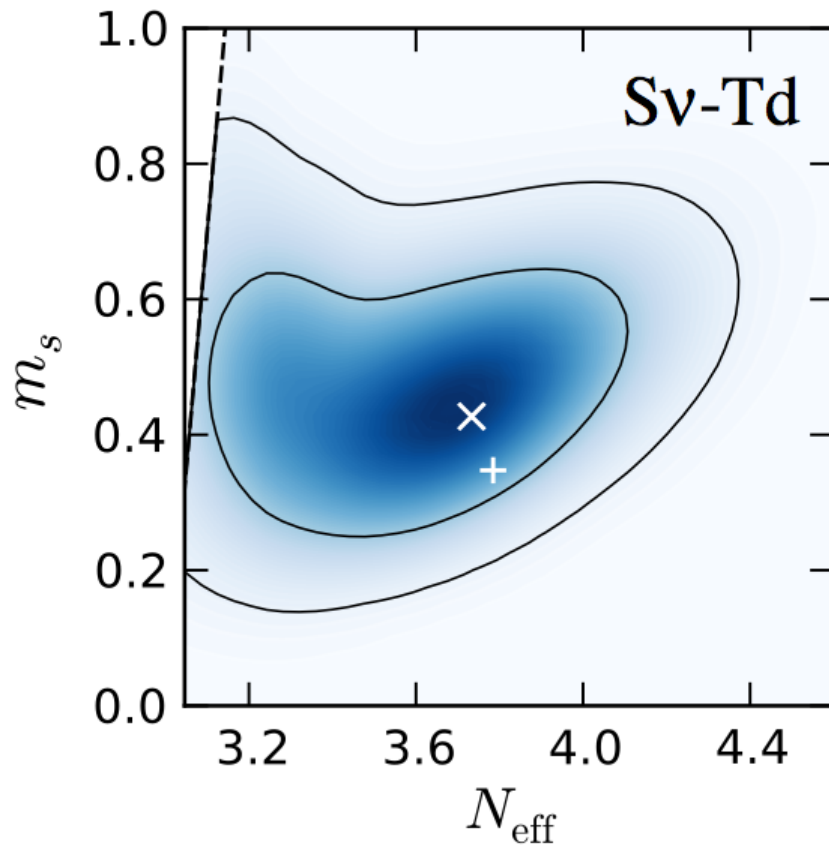
# Curing discrepancies using hot dark matter?



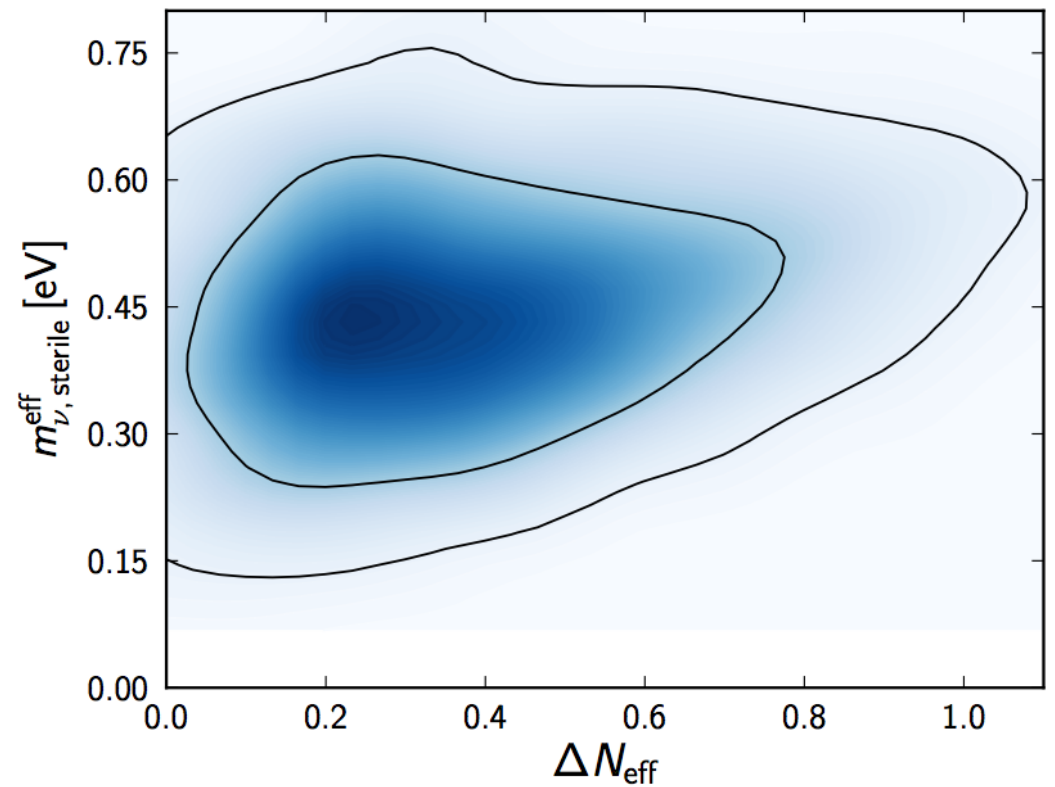
Hints for a hot dark matter component?

*(assumption: non-CMB data can be trusted!)*

# Curing discrepancies using hot dark matter?

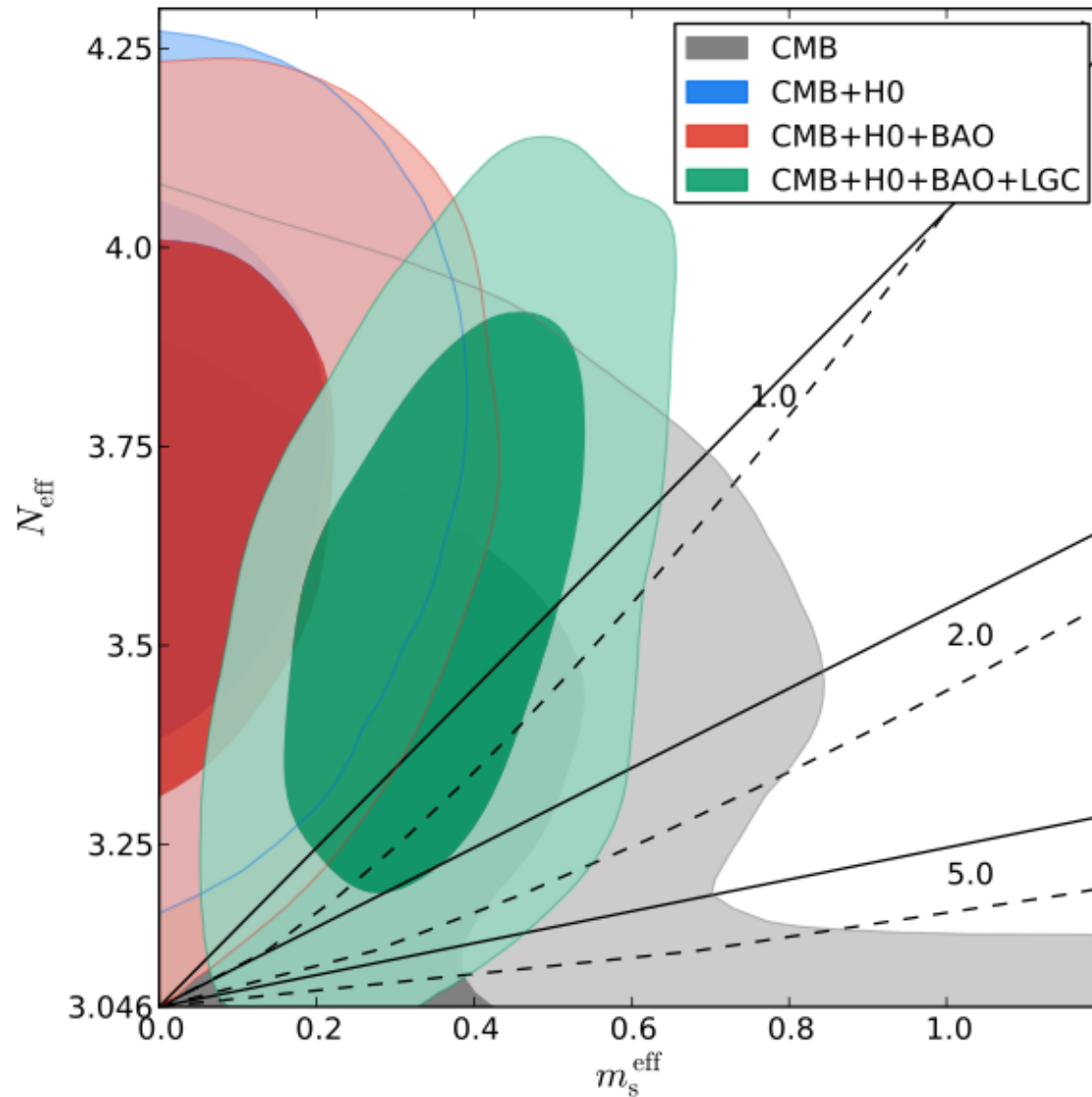


[Wyman, Rudd, Vanderveld & Hu 2013]



[Battye & Moss 2013]

# Curing discrepancies using hot dark matter?



# Conclusions

- Planck has delivered an exquisite measurement of the CMB temperature anisotropies, extracting close to the maximum achievable amount of information from this observable
- The  $\Lambda$ CDM model continues to provide an overall very good description of CMB data
- Some discrepancies with non-CMB cosmological data: unknown systematics or sign of new physics?
- Possible to resolve discrepancies with an additional hot dark matter component. Could be interpreted as a light sterile neutrino, but preferred parameter region is not compatible with reactor/accelerator/gallium-preference, unless sterile production can be suppressed
- Planck full mission data (including polarisation data) will be released next year