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Joint ICTP-IAEA College on Identification and Assessment of Nationally Appropriate Mitigation Actions (NAMAs) in Energy System Development to Help Combat Climate Change

5 – 9 May 2014

Sensitivity Analysis and Interpretation of Model Results

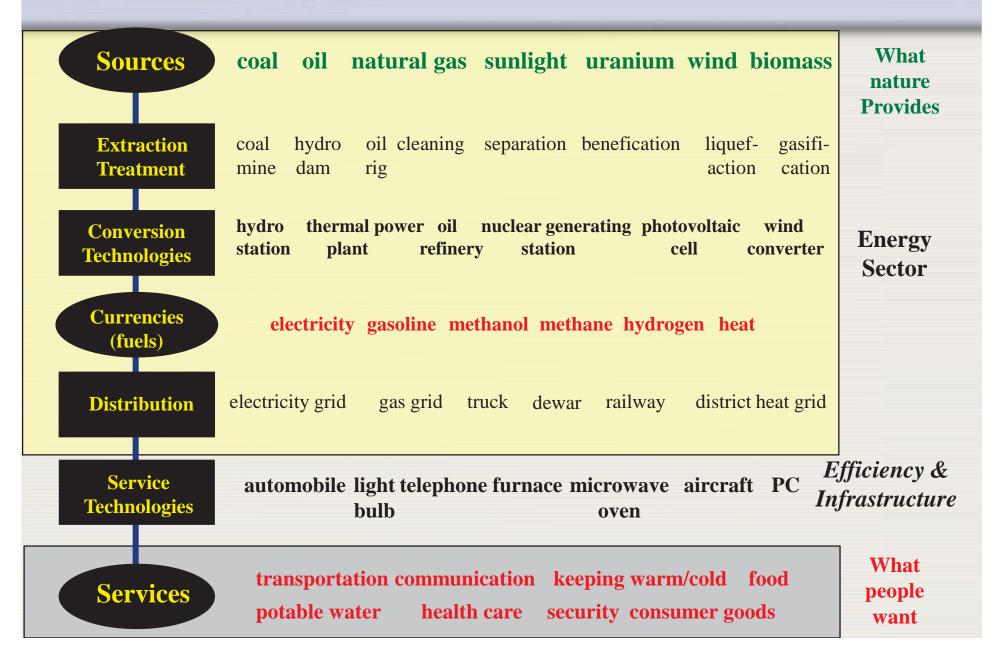
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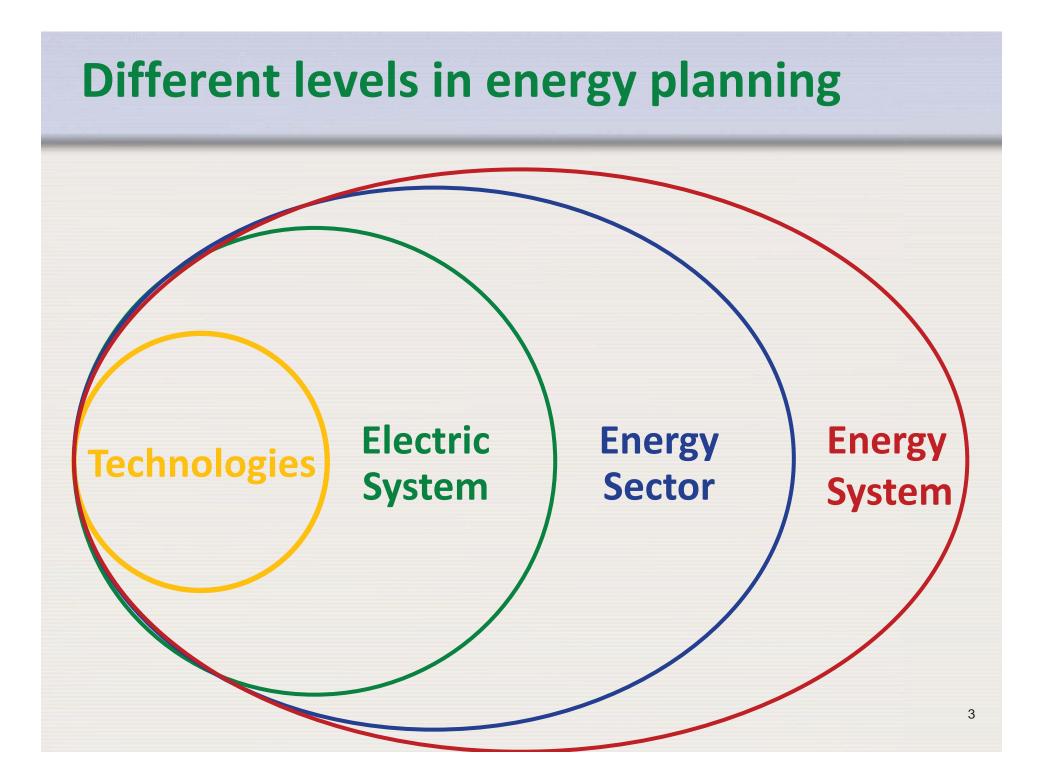
#### Sensitivity Analysis and Interpretation of Model Results

**H-Holger Rogner** 

International Institute for Applied Systems Analysis (IIASA) Royal Institute of Technology (KTH), Stockholm ICTP, 5 – 9 April 2014

#### **Architecture of the Energy System**





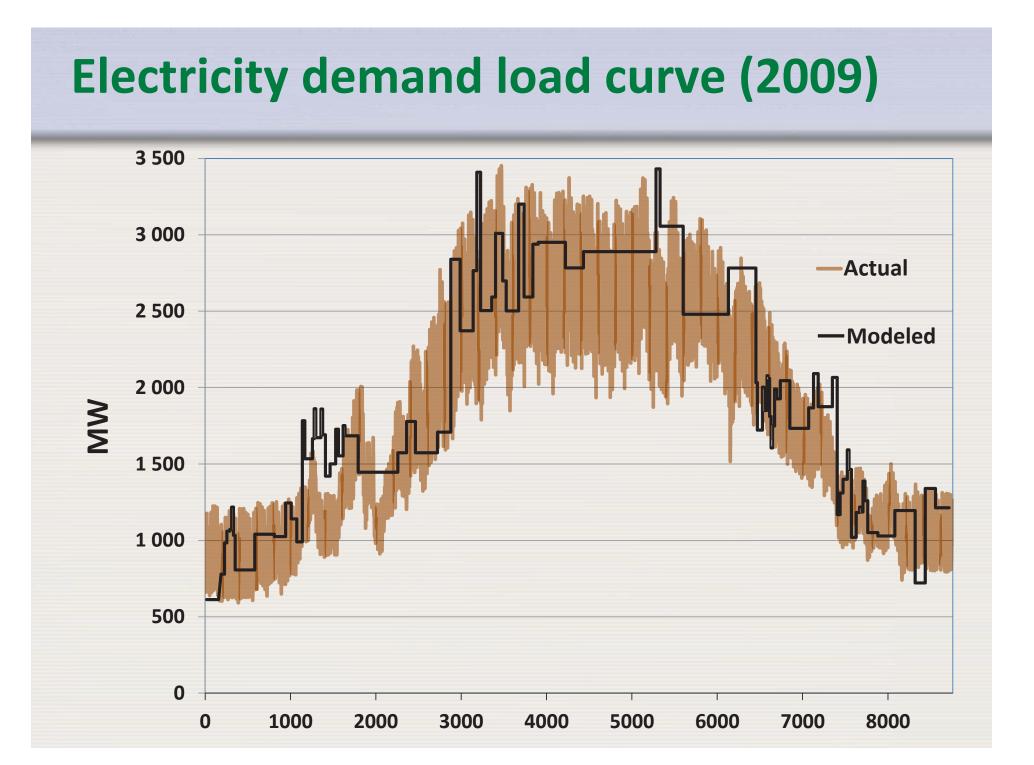
# Sensitivity analysis: How stable is your solution ?



### Why sensitivity analysis

Uncertainty in inputs and assumptions due to

- Lack of information
- Unknown or rather unknowable future
- Previously plausible assumptions no longer hold
- Testing different boundaries or resolution of detail
- Dynamic vs linear behavior



## Why sensitivity analysis

- Explore what if questions
- Protect against surprise
- Detect methodological shortcomings
- Appreciate uncertainty and develop a better understanding for it

#### **Modeling energy systems – Model design**

**Typical questions faced by energy analysts and planners:** 

- What is the cost-optimal energy mix that meets demand by 2030?
- What is the impact of escalating fossil fuel prices?
- What are the environmental impacts?
- How does the cost-optimal energy mix change with more stringent environmental regulation?
- What will be the consequence of market restructuring?
- What needs to be done to increase the share of cleaner technologies?

What will be consequences of introducing or phasing out nuclear power?

#### **Sensitivity Analysis**

- Future demand for energy
- Investment costs of new power plants and other energy facilities
- Operation and maintenance costs
- Fuel cost
- Performance of technologies (efficiency, plant factor, availability factor, etc.)
- Limits on production and construction of plants
- Import/export quantities and prices
- Environmental protection limits and costs

#### **Sensitivity analysis**

#### Parametric sensitivity analysis

- Assess robustness of a solution to changing assumptions (of parameters and constraints)
  - Assess which parameters are most sensitive to even small variation
  - Usually one parameter is varied everything else is kept constant

#### **Scenario analysis**

- Assess robustness of a solution to distinctly different sets of assumptions on parameters and constraints
- Note: Emphasis on internally consistency
- Assessment of different futures
- However the primary purpose of scenario formulation is to address "What if..." type of policy question to assess implications of introducing policies by comparative assessment of scenarios

#### **Scenario analysis**

#### Parametric sensitivity analysis

- Assess robustness of a solution to changing assumptions (of parameters and constraints)
  - Assess which parameters are most sensitive to even small variation
  - Usually one parameter is varied everything else is kept constant

### Sensitivity analysis with MESSAGE

min	C' *	X

Subject to  $A * x \ge b$  $u \ge x \ge /$ 

> result x<sup>\*</sup> range for c, b, l, u

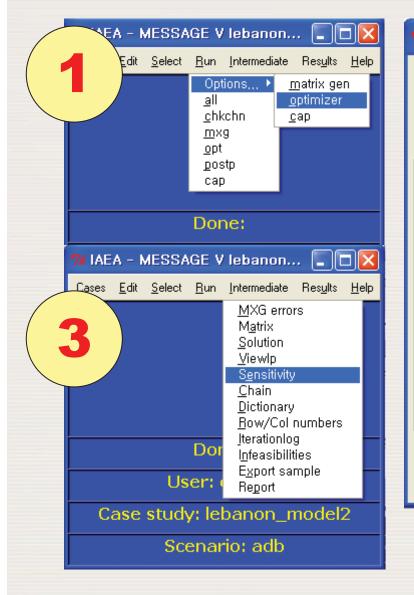
#### Notes on the sensitivity screen

- Parameters change in the original problem while the optimal basis remains the same
  - Objective coefficient
  - Constraint bound
  - Variable bound

Basis remains the same means that no other element comes into the solution, i.e. no other variable or equation reaches its upper or lower limit

Important! Variations assume that all other parameter remain fixed except the one in question

#### **Sensitivity in MESSAGE Solver**



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(2)	Set Optimizer Parameters					
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use basis	no	× •				
scale problem	yes	<b>_</b>				
solution method	simplex	<b>_</b>				
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		Cbigwaaa017 UPPER	-3.61192e+001	+1.00000e+020	+5.02192e+001	
		Cbigwaaa018 UPPER	-3.61192e+001	+1.00000e+020	+5.02192e+001	
		Cbigwaaa019 UPPER	-6.41480e+001	+1.00000e+020	+7.82480e+001	
			-3.61192e+001	+1.00000e+020	+5.02192e+001	
		Cbigwaaa021 UPPER	-1.50521e+002	+1.00000e+020	+1.64621e+002	
	12	Cbigwaaa022 UPPER		+1.00000e+020	+2.99168e+002	
	13	Cbigwaaa023 UPPER		+1.00000e+020	+3.39442e+002	•
		Absolute	Percentage	Description	Close	

#### **Shadow Prices**

### Are important so see how expensive restrictions are

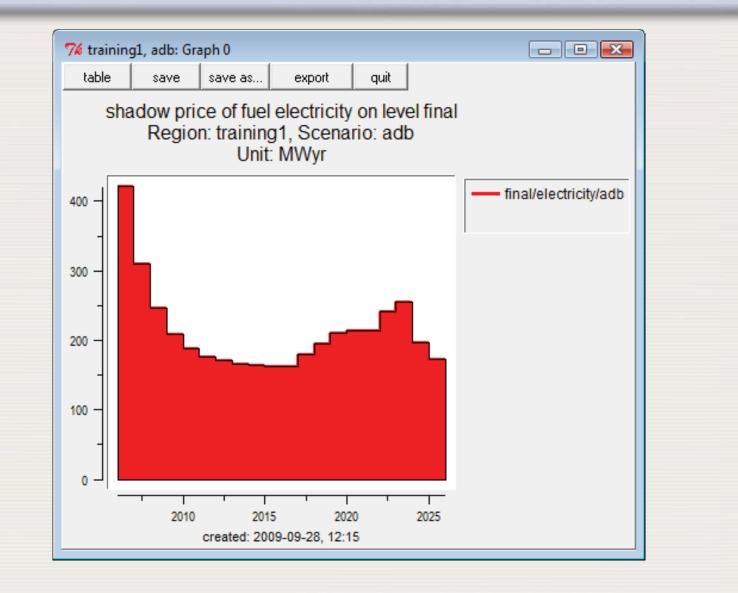
- At the upper limit: how much would the objective function value decrease if the limit would increased by one unit
- At the lower limit: how much would the objective function value decrease if the limit would decreased by one unit

#### **Shadow prices in the solution**

#### In interactive results screen

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#### **Shadow Price for Electricity**



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#### Which studies to conduct?

Number of sensitivity studies should be kept as reduced as possible

Too many sensitivity studies reduce credibility of the study and confuses interpretation of results:

negative perception by decision maker

Too few sensitivity studies may lead to many questions left open to the decision maker (What if?)

Studies should concentrate in a few important parameters to analyse range of validity of the optimal solution (How robust the solution is?)

