

**2583-8**

**Workshop on Coherent Phenomena in Disordered Optical Systems**

***26 – 30 May 2014***

**Non-equilibrium Dynamics in "Electron Glasses"**

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# Non-equilibrium dynamics in « electron glasses »

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*Bar Ilan University (Israel)*

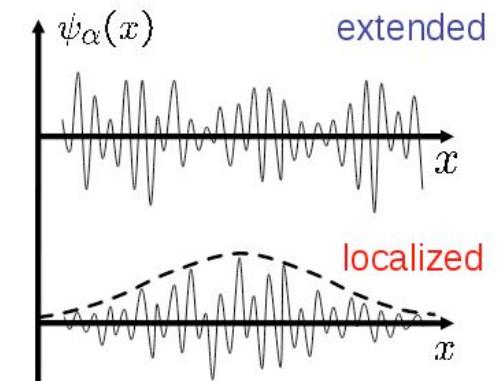
- **Introduction**
- *First period* :  $\text{InO}_x$  and granular Al prototypes
- *Second period* : thermal activation and new phenomena

# Anderson localization of electrons

Disorder



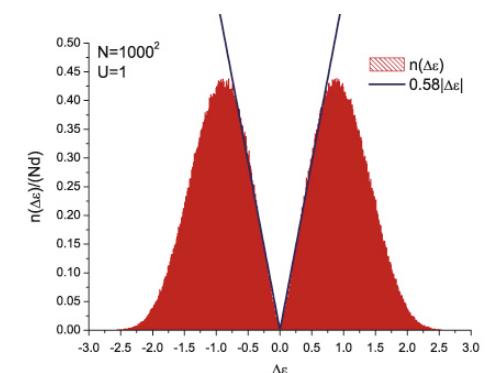
1958 Anderson :  
disorder localizes quantum states



Coulomb repulsion matters



1975 Efros, Shklovskii :  
Coulomb repulsion adds constraints  
on the arrangement of localized  
electrons → coulomb gap



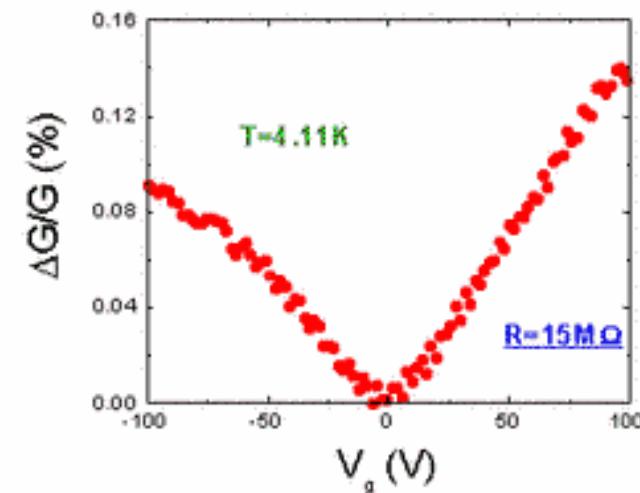
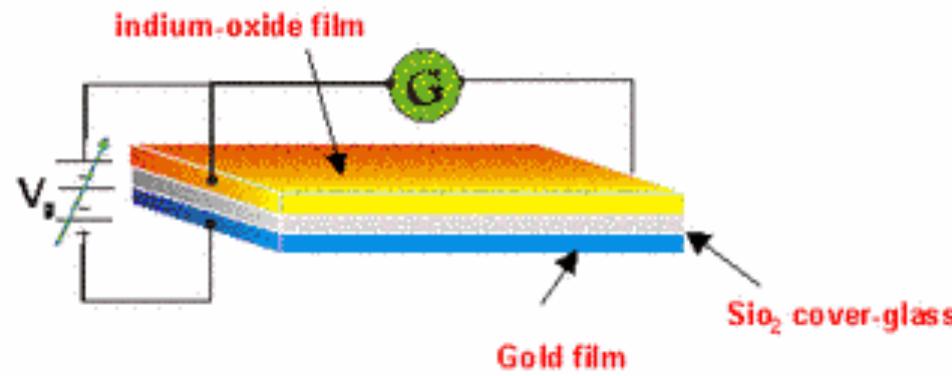
2006 Altshuler et al (Basko ...)  
Many-body localization

# Electronic Coulomb glass ?

J. H. Davies, P. A. Lee and T. Rice (1982):

*localized electrons + unscreened coulomb repulsion → highly correlated → new glass (finite T glass transition?)*

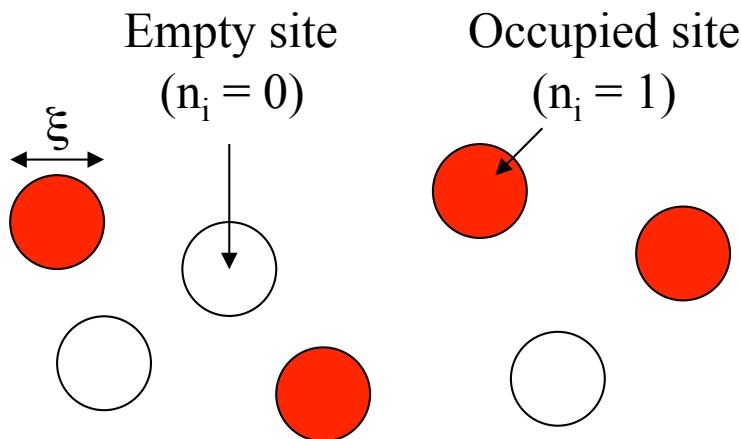
Ben Chorin et Ovadyahu (1991): *anomalous field effect and very slow relaxation of conductance in insulating indium oxide*



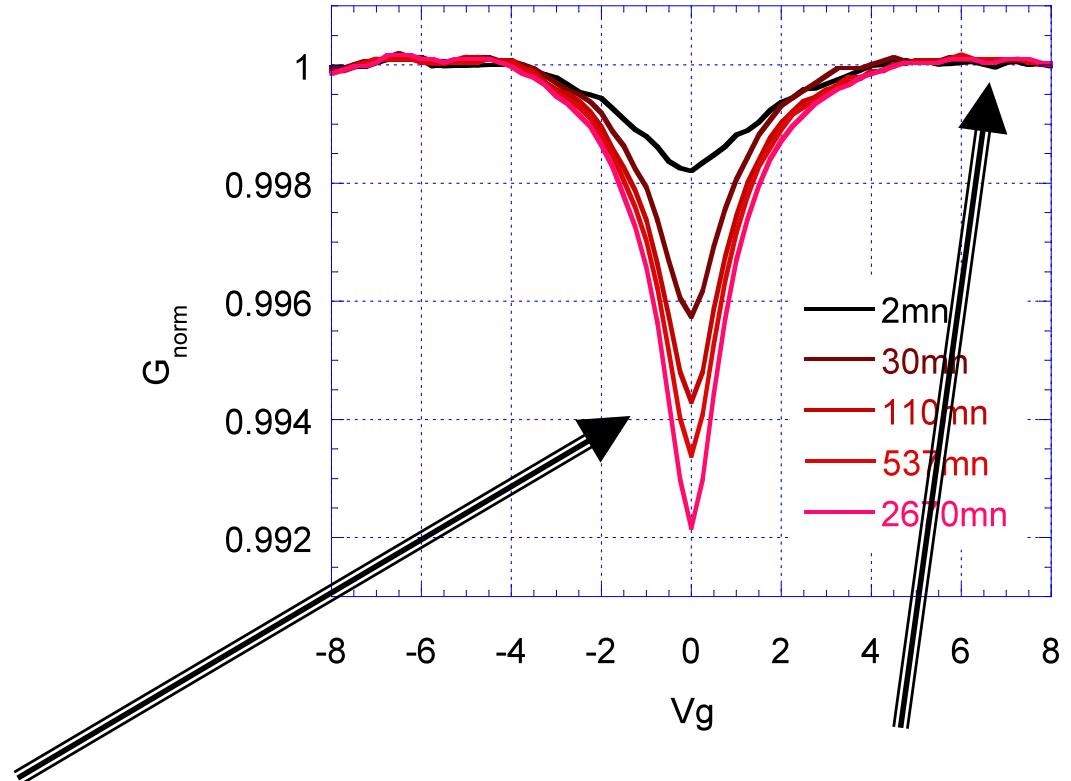
*Manifestation of the electron (Coulomb ?) glass in indium oxide ...*

# Electron Coulomb glass interpretation

## Electron Coulomb glass model



Fixed gate voltage  $V_g=0$ :  
system proceeds slowly to the equilibrium state (of minimum conductance)



After fast gate voltage change:  
system in a highly excited state  
(higher conductance)

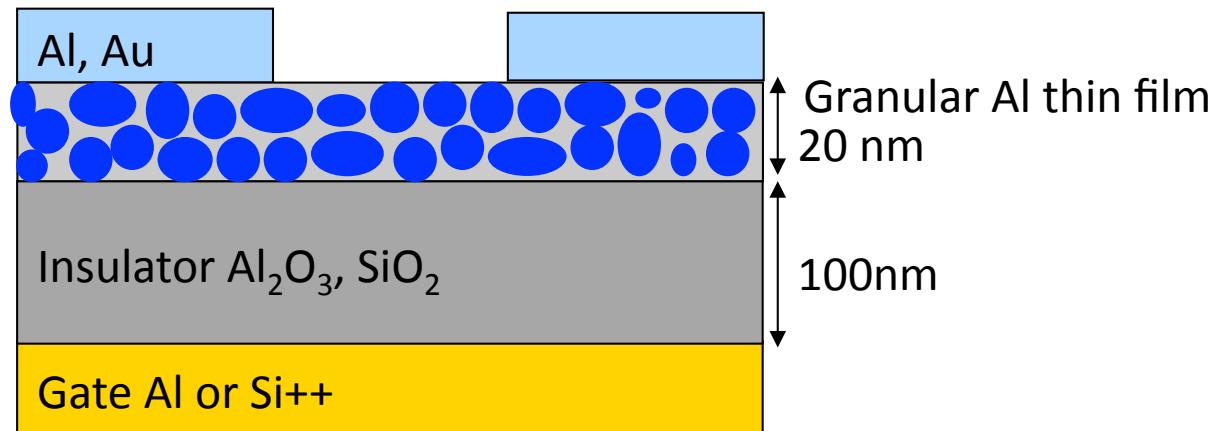
# A few words on the theory side

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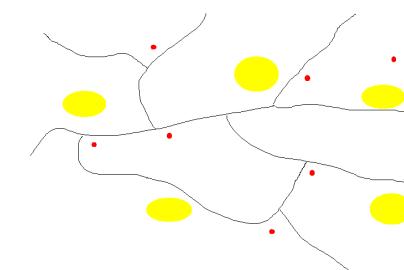
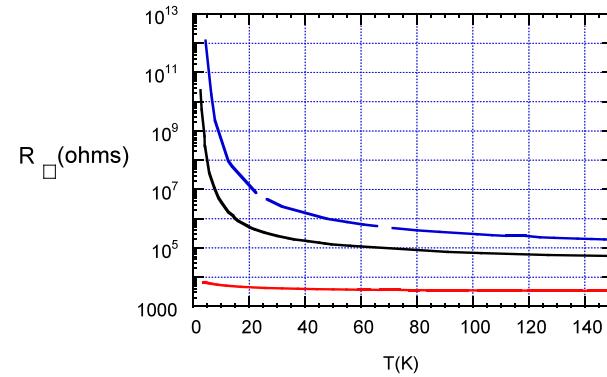
- **Analytical approach** (M. Muller et al., Dobrosavljevic et al.)
  - mean field → glass transition at  $T_g$
- **Monte-Carlo simulations :**
  - Coulomb repulsion slows down relaxation to equilibrium
  - during relaxation: diffusive carriers get localized, effective temperature decreases
  - no observation of  $T_g$  (on site disorder)
  - Limitations: not too low T, not « very » long times, classical limit (no quantum tunneling)

- *Introduction*
- *First period : InO<sub>x</sub> and granular Al prototypes*
- *Second period : thermal activation and new phenomena*

# Experiments on granular Al films

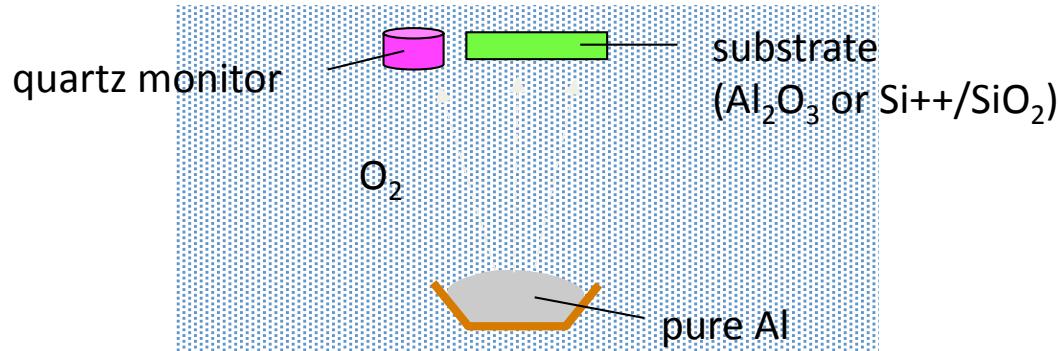


- Electrical conductance measurements
- Relaxation after excitation
  - to excite apply a **gate field**, a non ohmic bias, a higher temperature excursion, an E.M. radiation



# Insulating granular Al films

Reactive evaporation :  $\text{Al} + \text{O}_2$

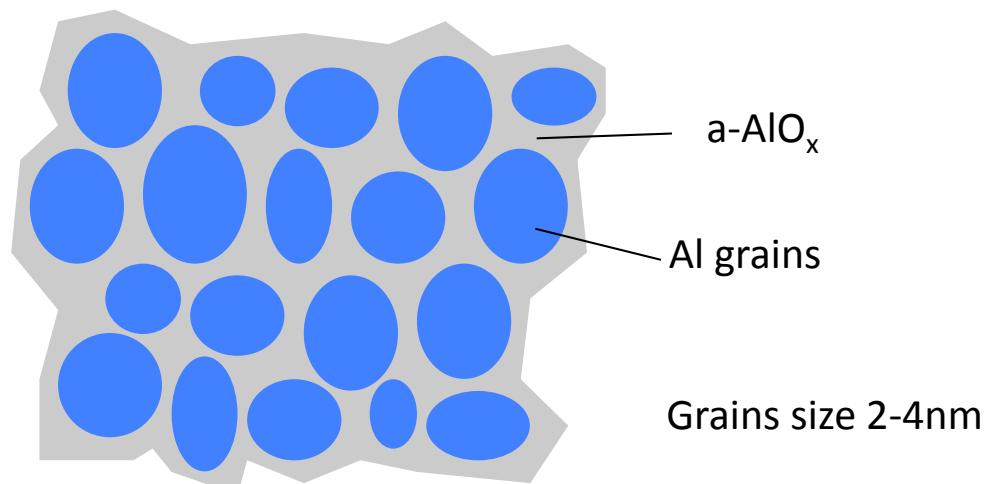


Parameters :

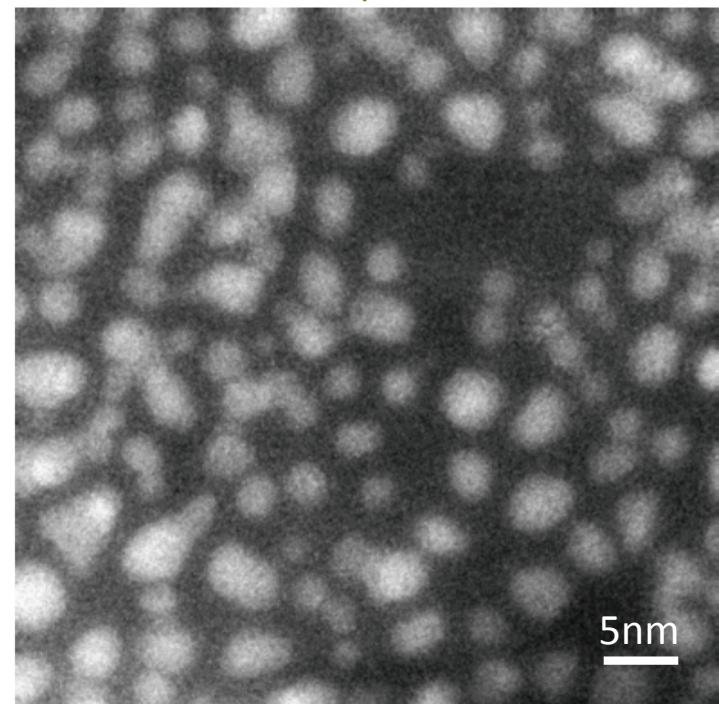
- $\text{O}_2$  ( $p \approx 2 \times 10^{-5}$  mbar)
- Al evaporation rate  $\approx 2 \text{\AA/s}$

## Structure of the films

Crystalline Al grains separated by  
an amorphous alumina tissue phase

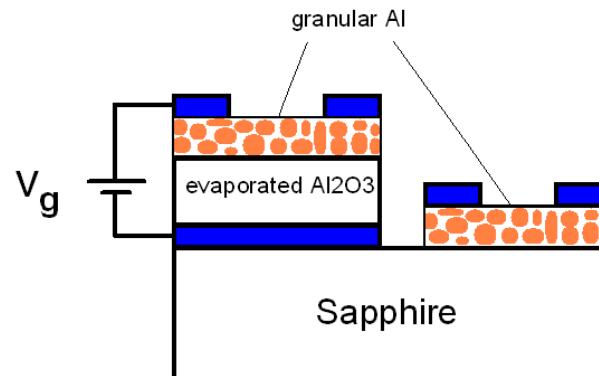
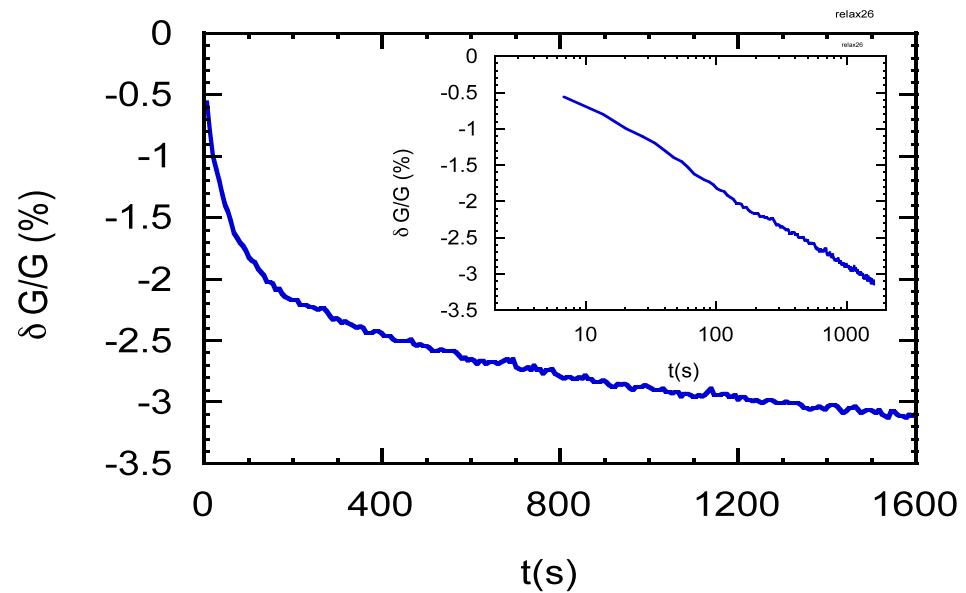
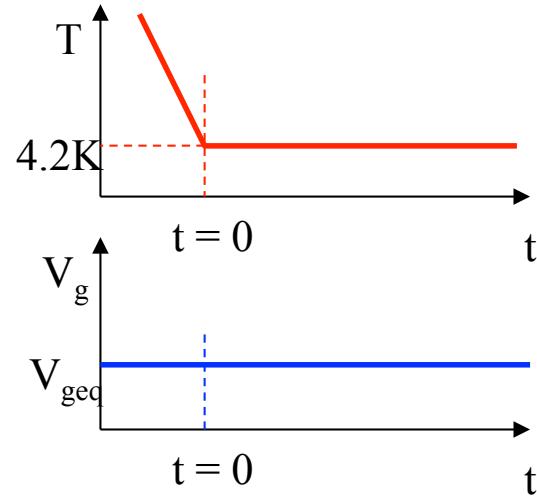


TEM picture



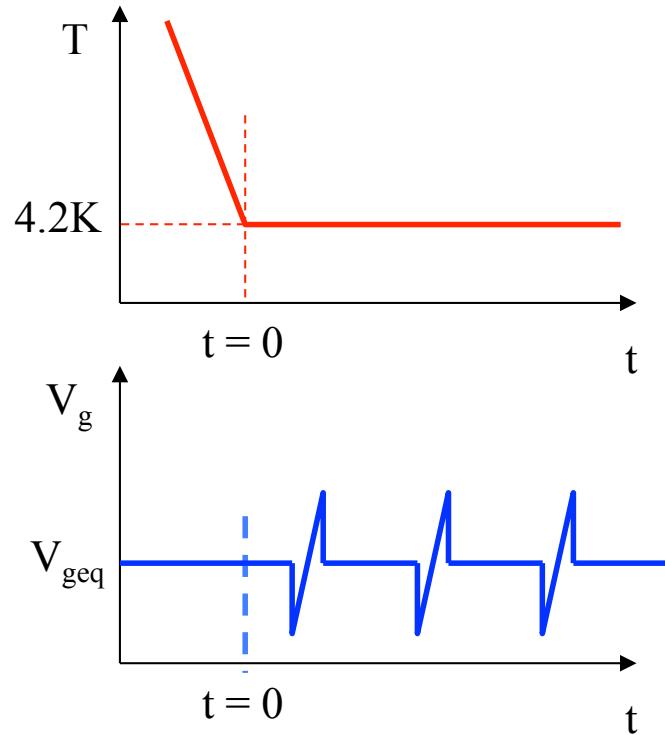
# Out of equilibrium effects

Never ending slow conductance relaxation after a quench

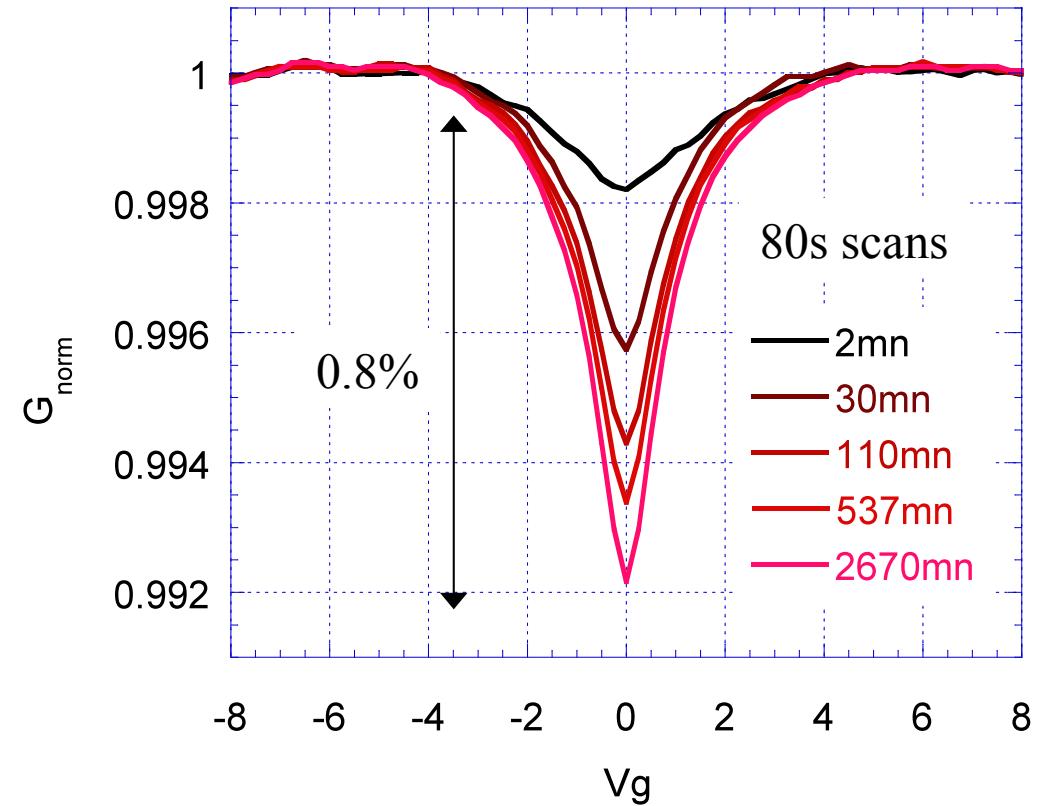


# Out of equilibrium effects

$G(t, V_g)$  after a quench at 4.2K



$R_\square = 30\text{M}\Omega$  at 4.2K

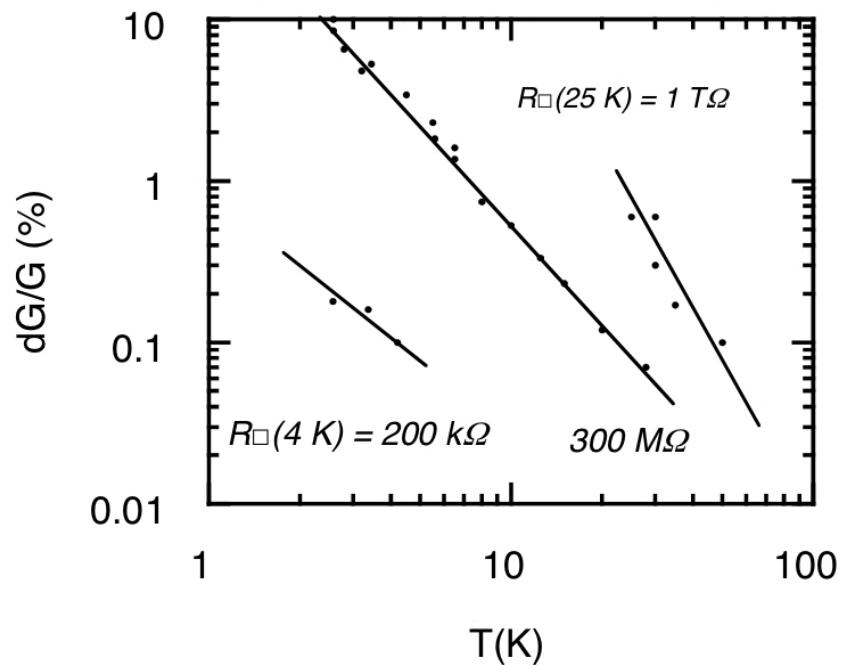


- Field effect anomaly (the “cusp” or “dip”)
- Amplitude grows like  $\ln(t)$
- + thermal memory

# Is this a small effect ?

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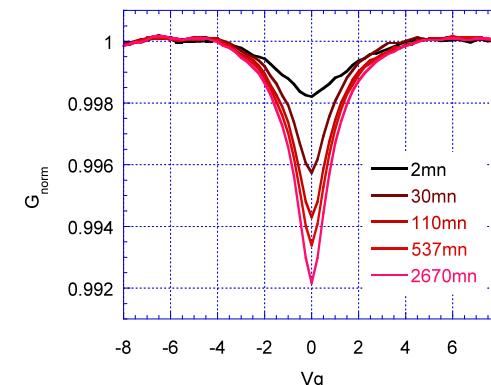
- the anomaly is **always** seen in gran Al insulating films
- it is most prominent (in %):
  - at low T (most measurements at 4K)
  - in more insulating samples
  - when measured fast



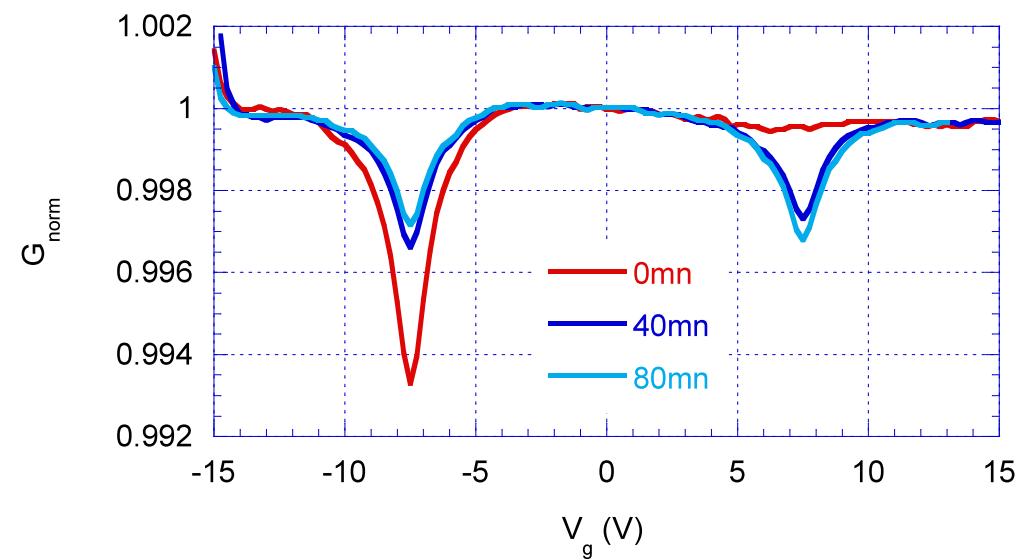
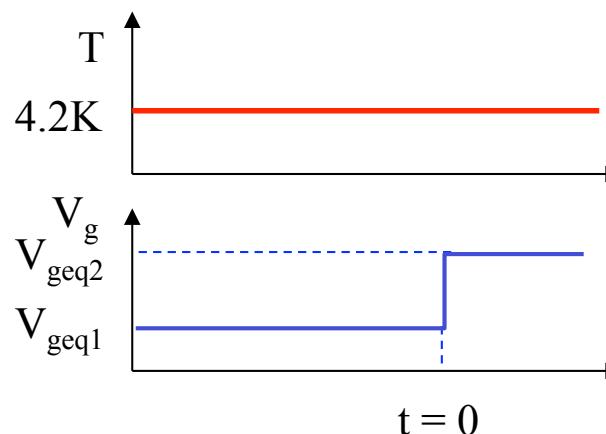
- for practical reasons we study samples where the anomaly is not so large ( $\leq 1\%$ ) but **it can be a large effect** (several tens of %)

# Cusp dynamics

Recall: after a cooling

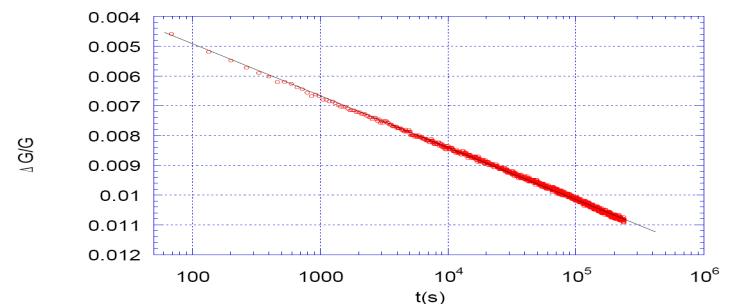


After a gate voltage change:



Formation of a new dip and erasure of the old one:

$\Rightarrow \Delta G \sim -\ln t$ ? but see later ...



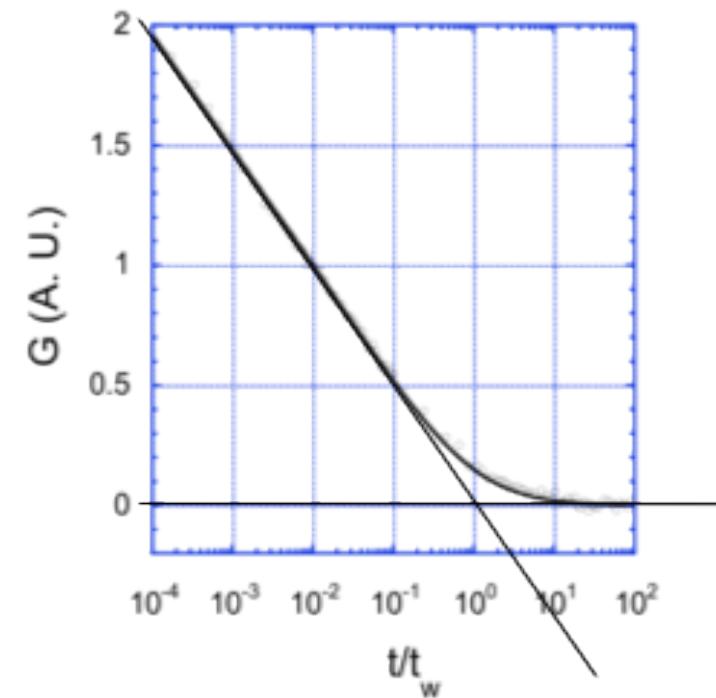
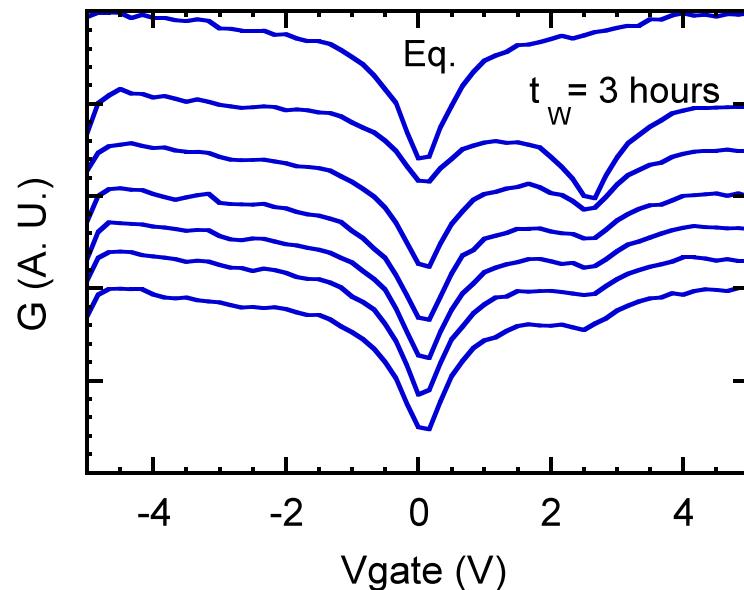
# Is the dynamics activated ?

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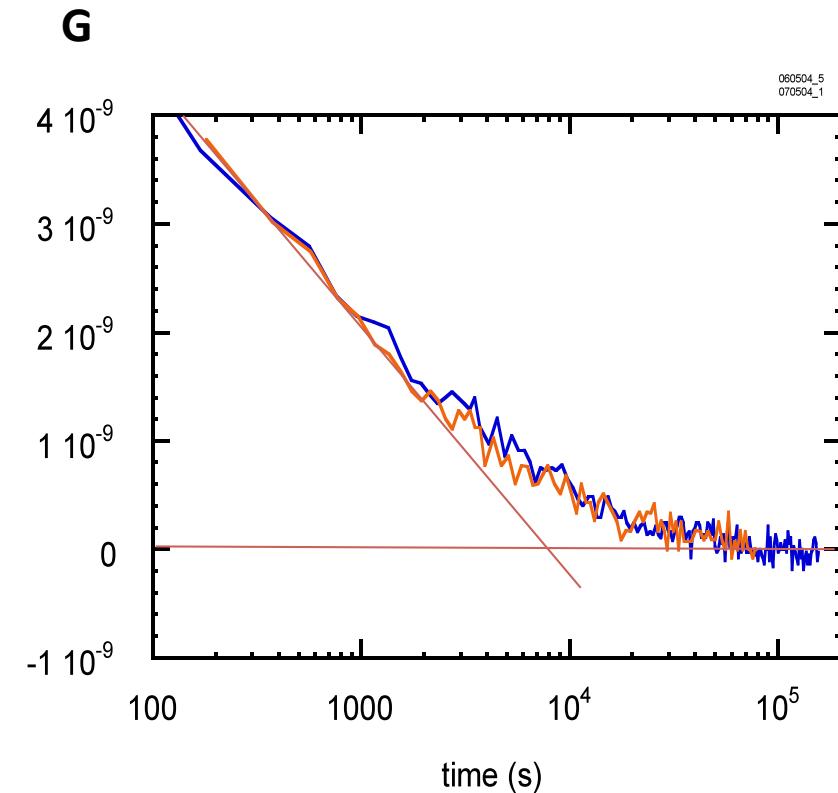
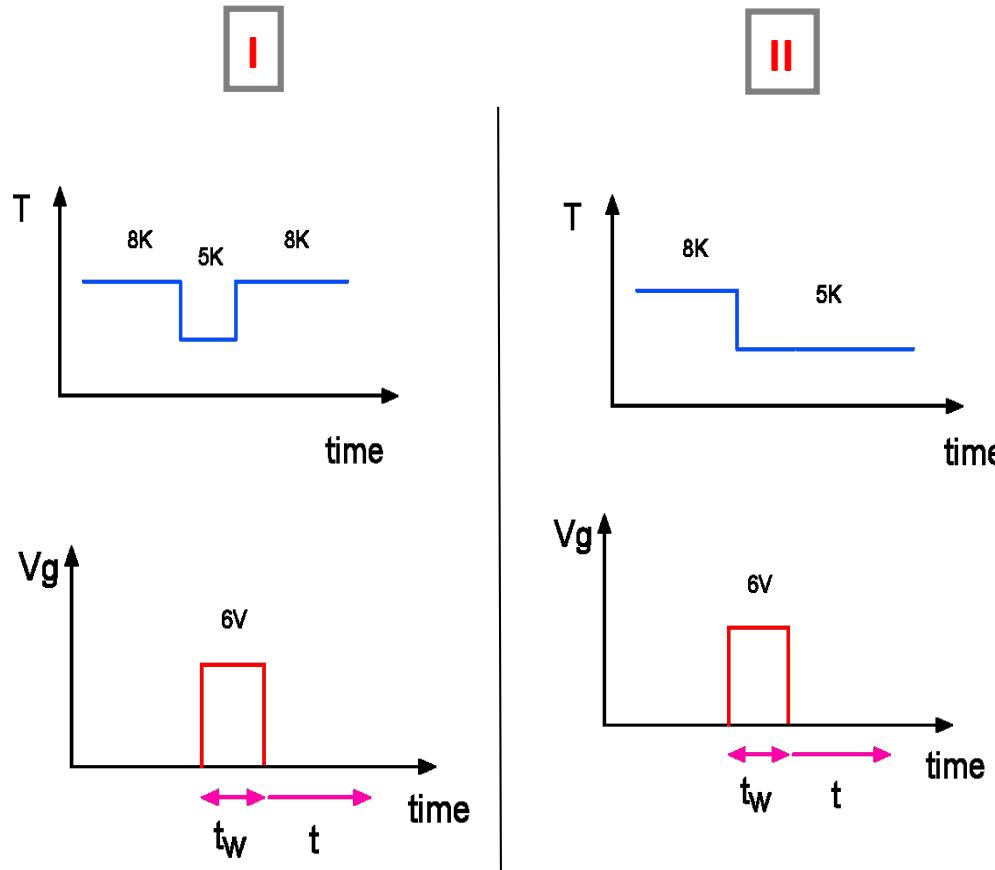
Is the dynamics accelerated when T is increased ? (it would explain why the dip becomes very faint)

But how to detect a change of the dynamics if it has no characteristic time ?

→ look at the erasure time of a previously formed dip



# Is the dynamics activated ?

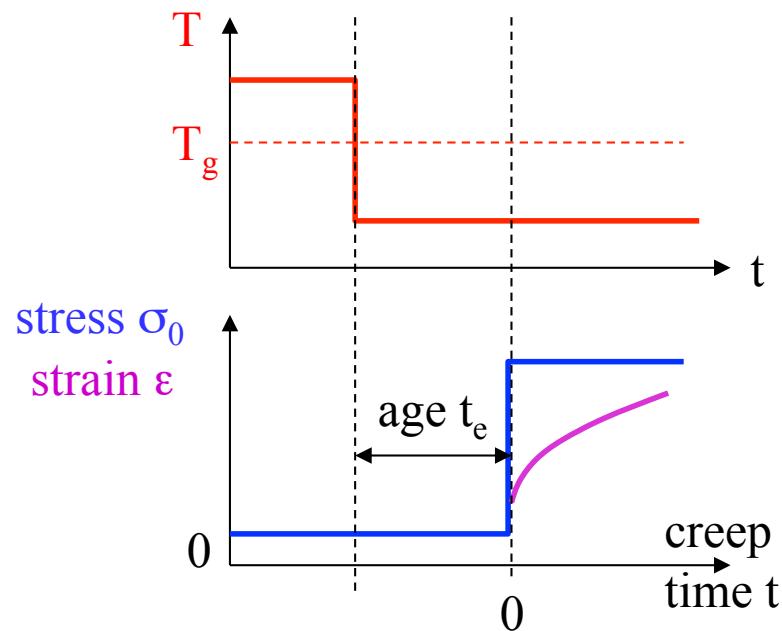


→ dynamics is not activated (in this  $T$  range)

# If it is a glass ... does it age ?

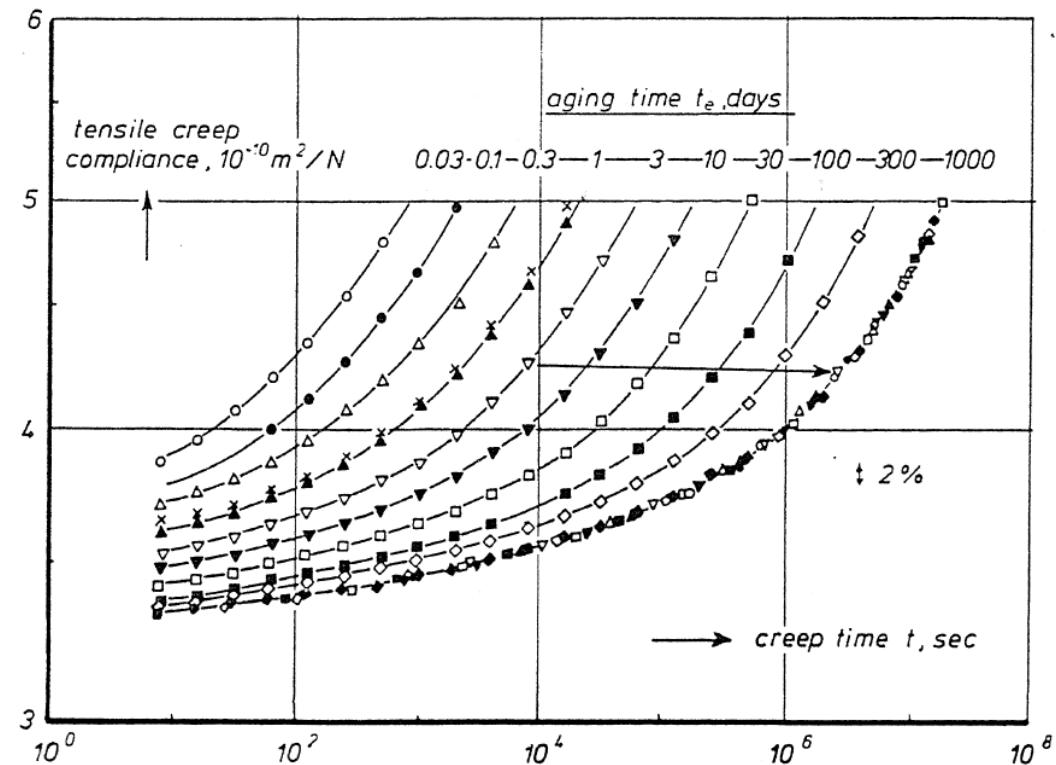
AGEING:

Ex: creep tests on polymers



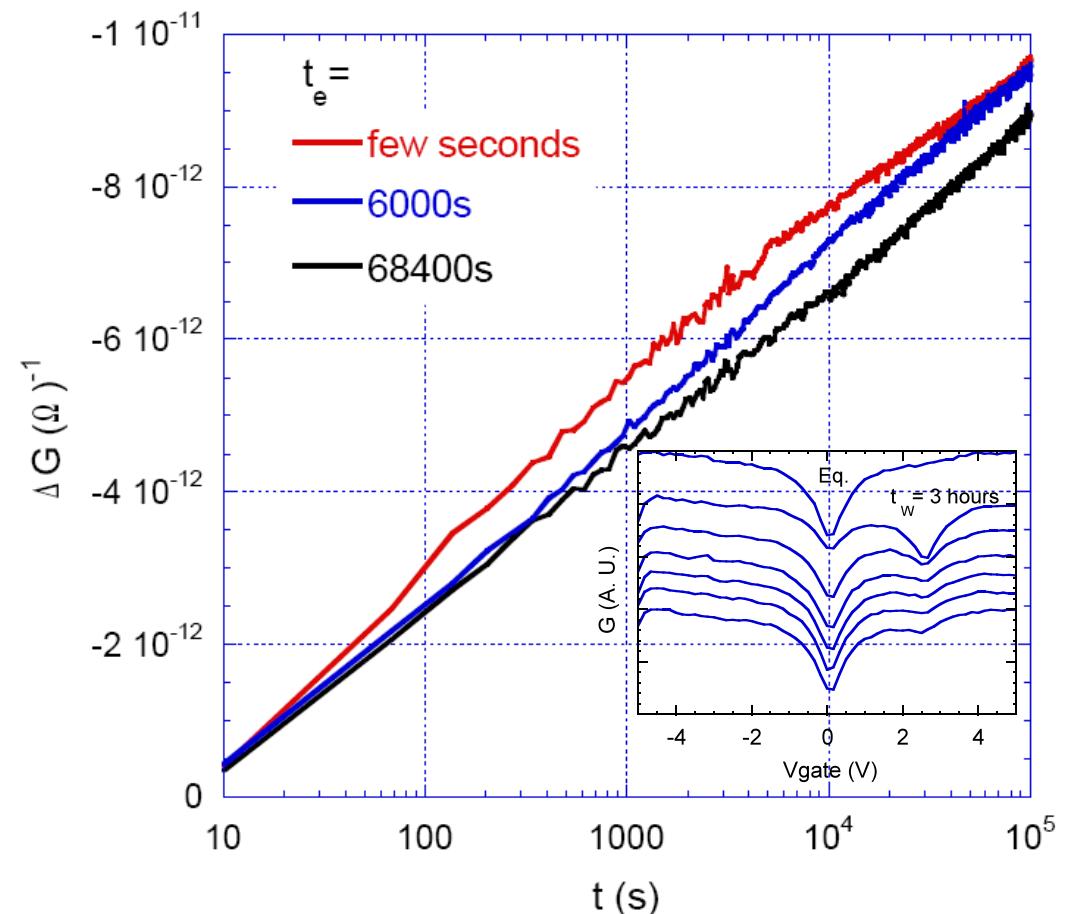
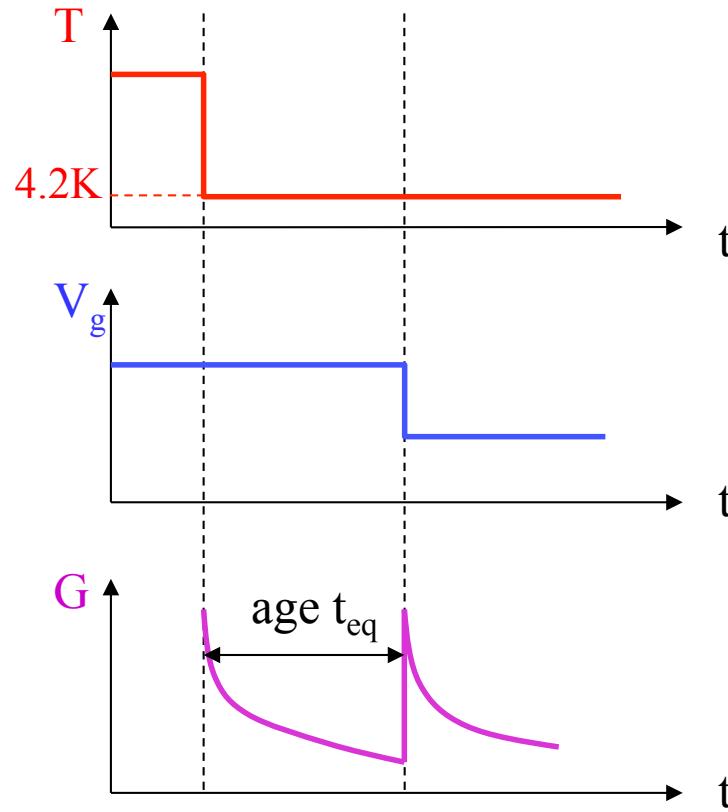
The dynamics depends  
on time: the « older » the  
system, the slower the  
response to a stimulus !

$$\text{Creep compliance } (t) = \epsilon (t) / \sigma_0$$



*PVC quenched from  $90^\circ\text{C}$  to  $40^\circ\text{C}$  ( $T_g = 80^\circ\text{C}$ )*  
*L.C.E Struik, 1978*

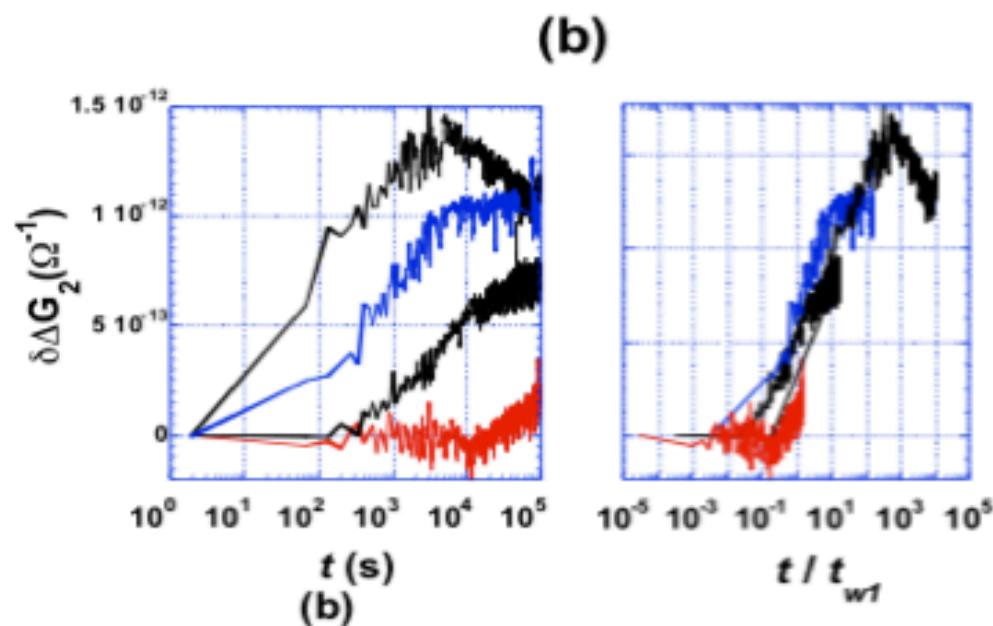
# Standard ageing protocol (1)



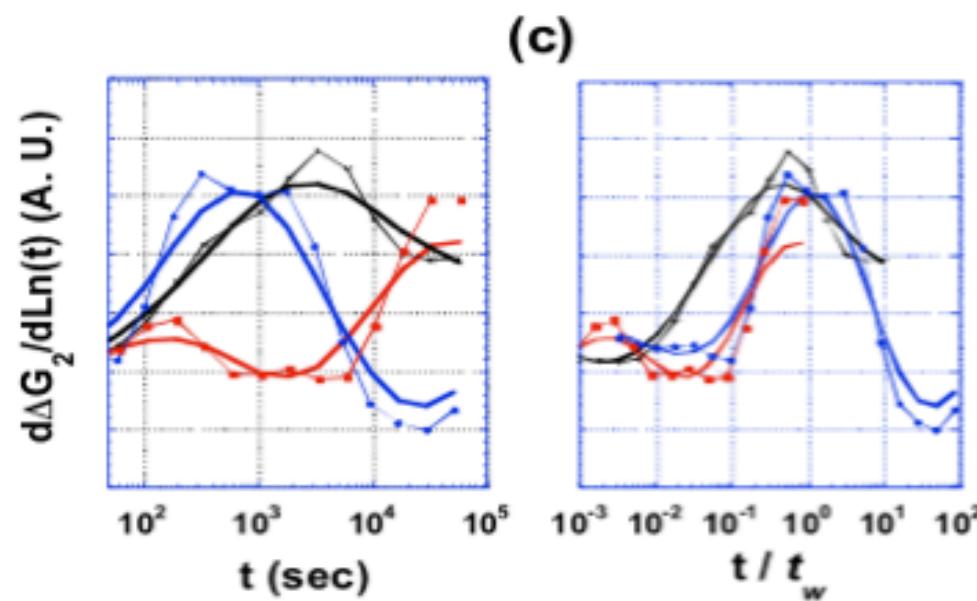
New dip growth: NOT like  $\ln(t)$  when  $t_{eq}$  NOT very large  
(i.e. when system has not already aged !)

# Standard ageing protocol

Departures from pure  $\ln(t)$  relaxation scale with  $t_{w1}$



Effective relaxation time distribution  $d\Delta G_2/d\ln(t)$  scales with  $t_{w1}$

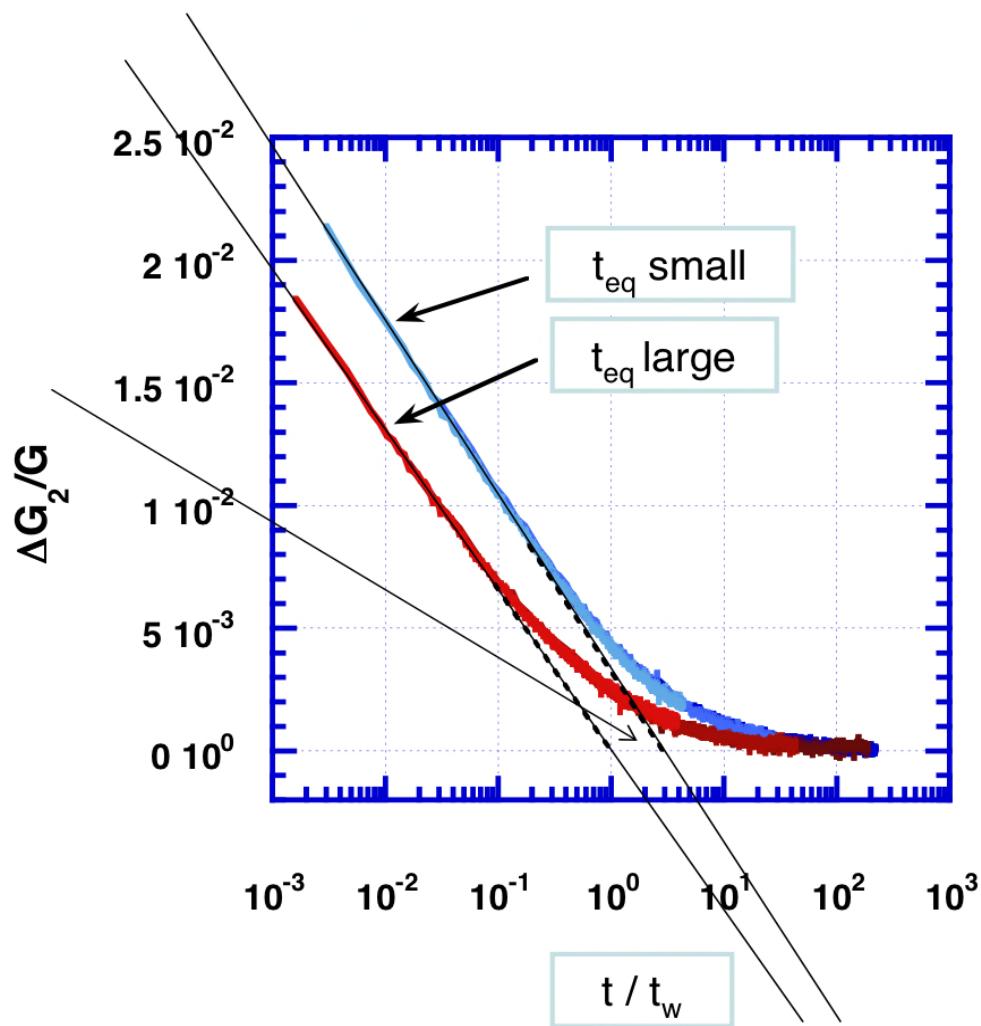


# Ageing in the two dip protocol

Indeed when  $t_{eq}$  is small:

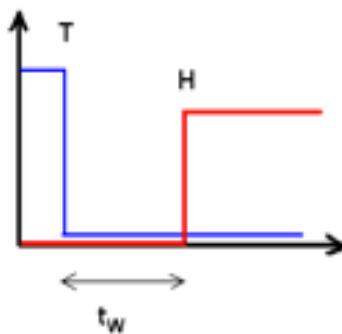
$$t_{erasure} > t_w$$

$$(here t_{erasure} = 3 t_w)$$

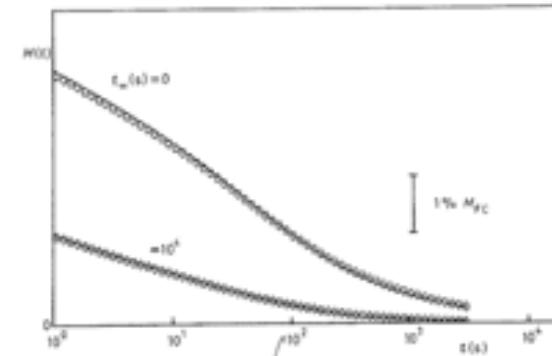
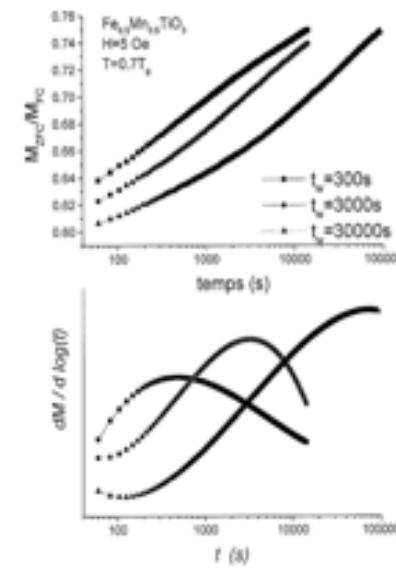
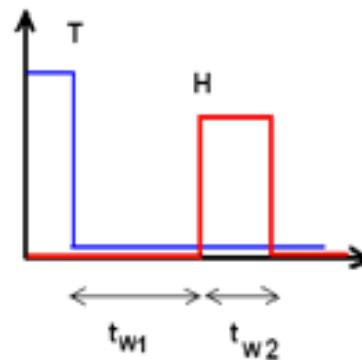


# equivalent spin glasses protocols

\* Zero field cooled  
relaxation (ZFC):



\* Isothermal remanent  
magnetization (IRM):



# Universal behaviour ?

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- Very strong similarity between *amorphous*  $\text{InO}_x$  and *granular* Aluminium
- Similar effects observed in :
  - $\text{In}_2\text{O}_{3-x}$ ,  $\text{Tl}_2\text{O}_{3-x}$
  - Granular Al
  - Ultra thin Pb, Bi films, thin Be films
  - Signs in icosahedral insulating quasicrystal i-AlPdRe
  - Discontinuous metal films Au, Ni, Ag, Al etc (?)

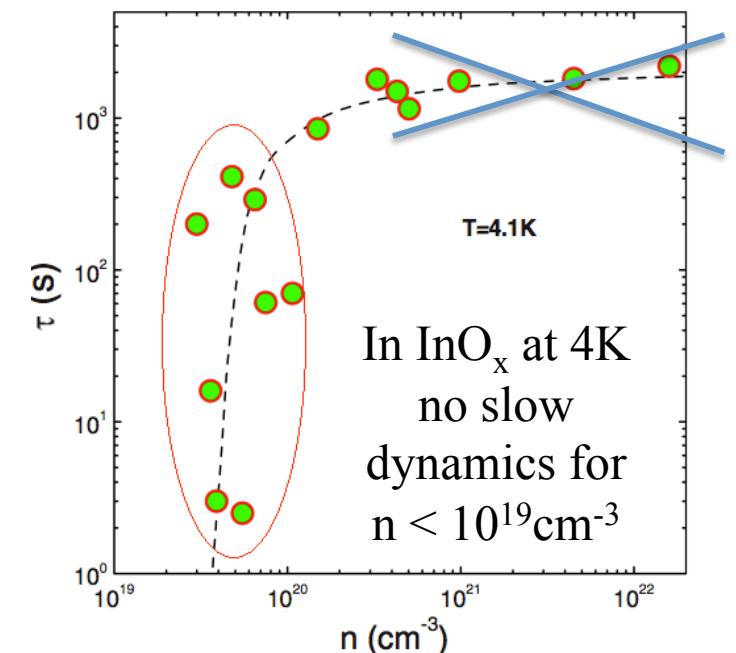
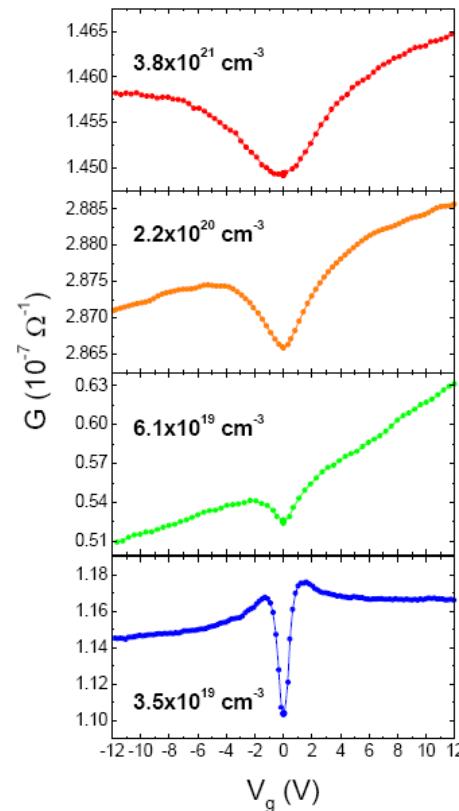
# Universal behaviour ?

No similar phenomenology in doped semiconductors\*, WHY ?

\*But see Popovic et al.

Suggestion (*Ovadyahu, HUJ*):

« Because high enough carrier density (or number of carriers in a localization volume) is necessary »



- *Introduction*
- *First period :  $InO_x$  and granular Al prototypes*
- *Second period : thermal activation and new phenomena*

# Why study other systems ?

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« ... and the materials we've heard about in this conference (MoGe etc...) could also be good candidates ! »

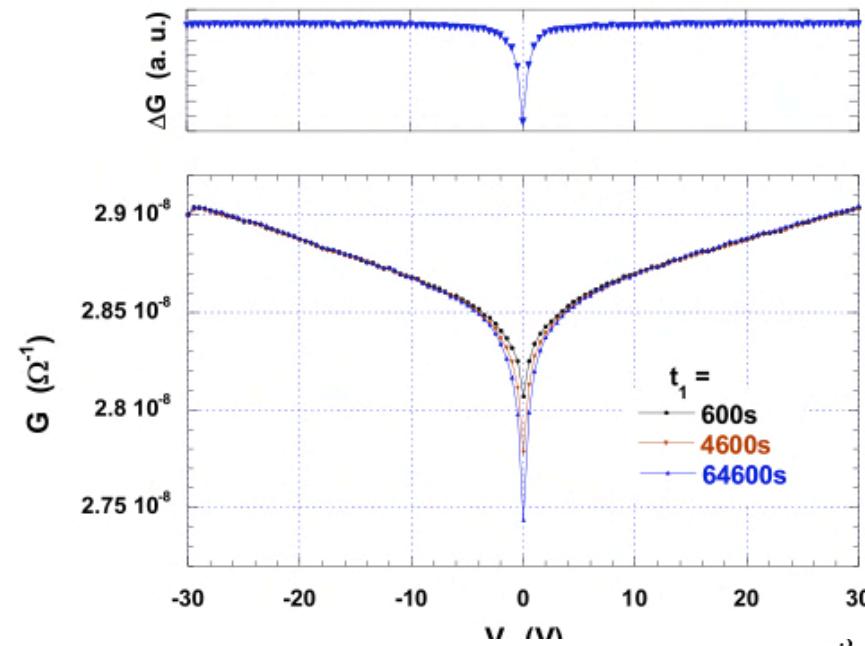
→ *Study  $Nb_{1-x}Si_x$*

Adkins et al (1984) :  
discontinuous gold films :  
- activated dynamics ?  
- field effect seen at high T ?

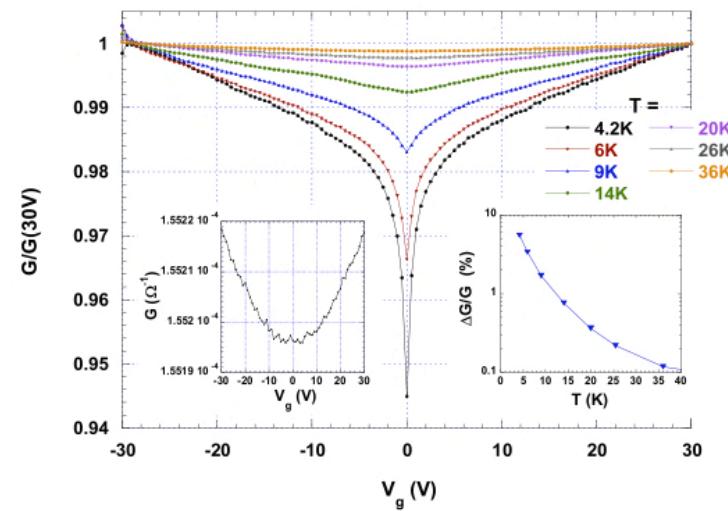
→ *Study discontinuous metals*

# $\text{Nb}_{1-x}\text{Si}_x$

Growth of a field effect anomaly after a quench

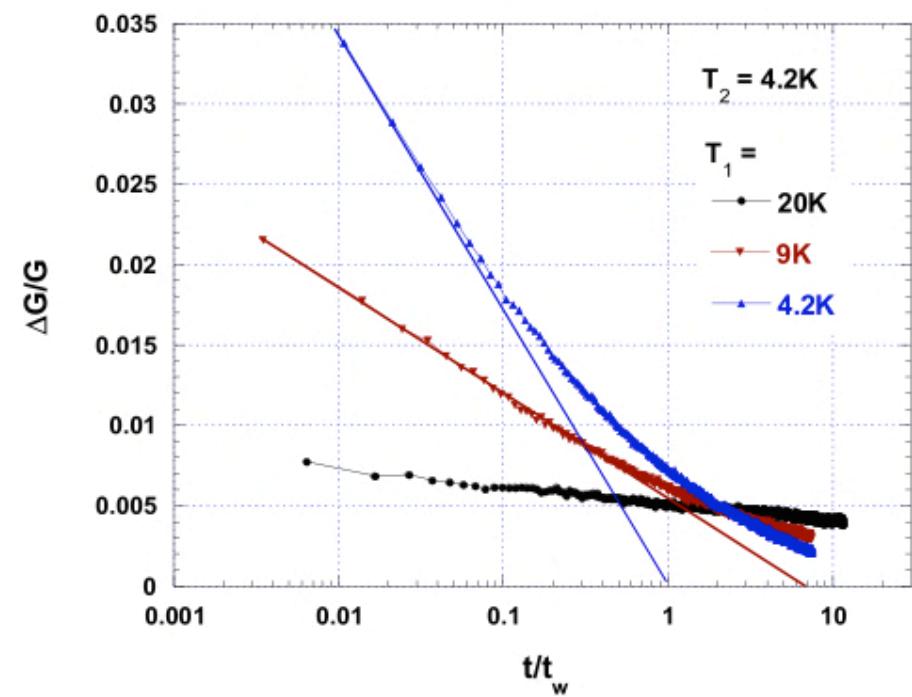
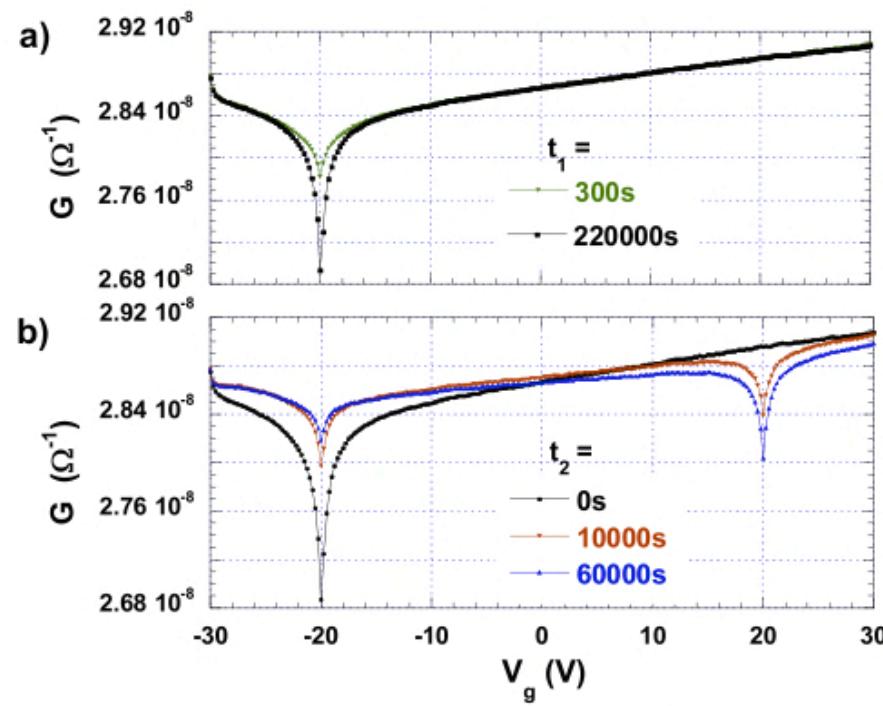


T dependence of the field effect anomaly

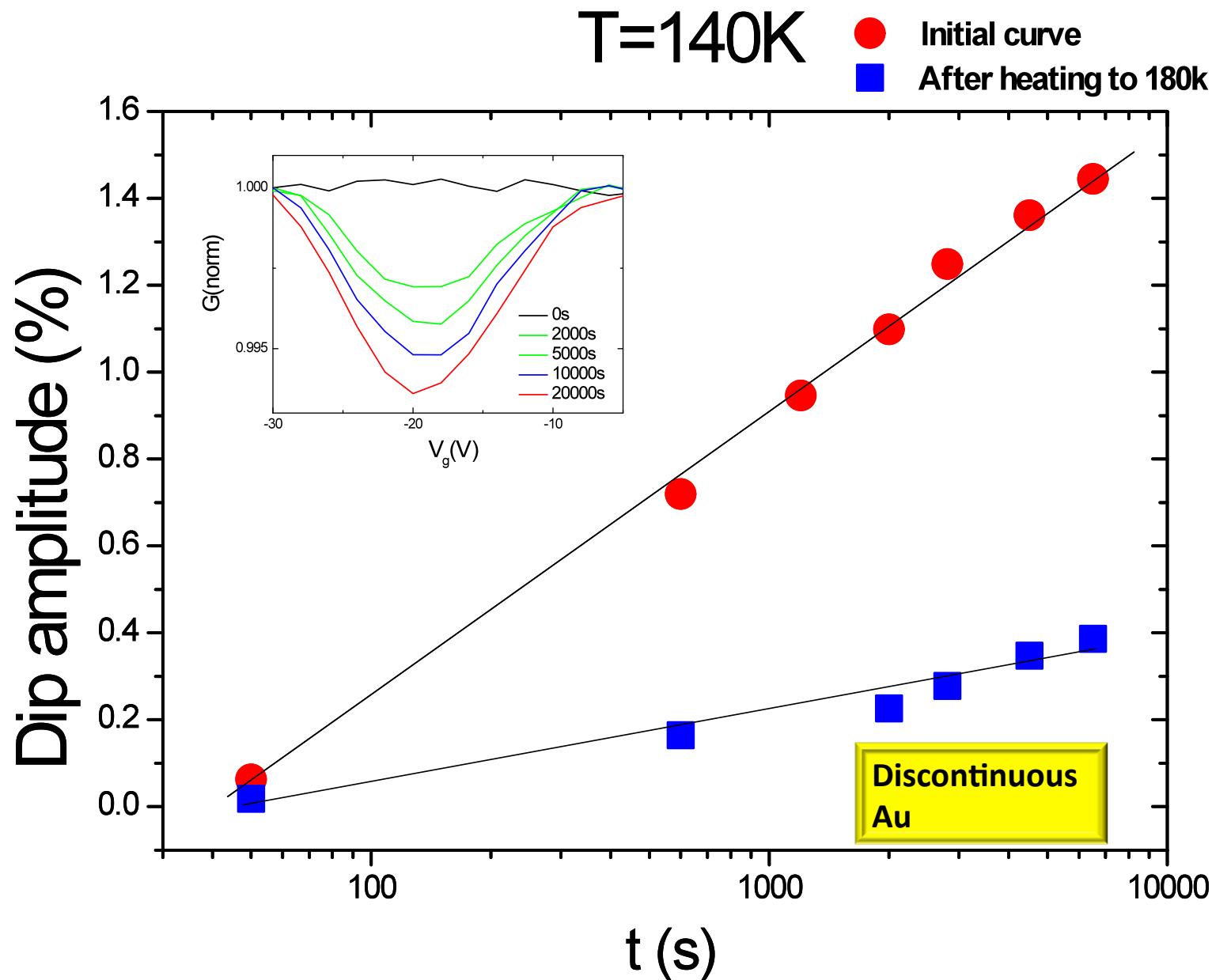


# $\text{Nb}_{1-x}\text{Si}_x$

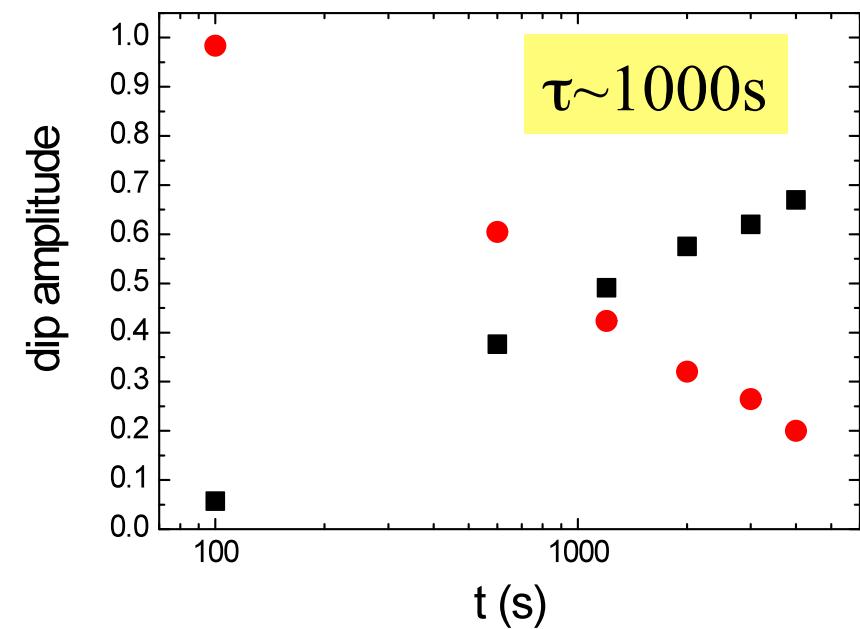
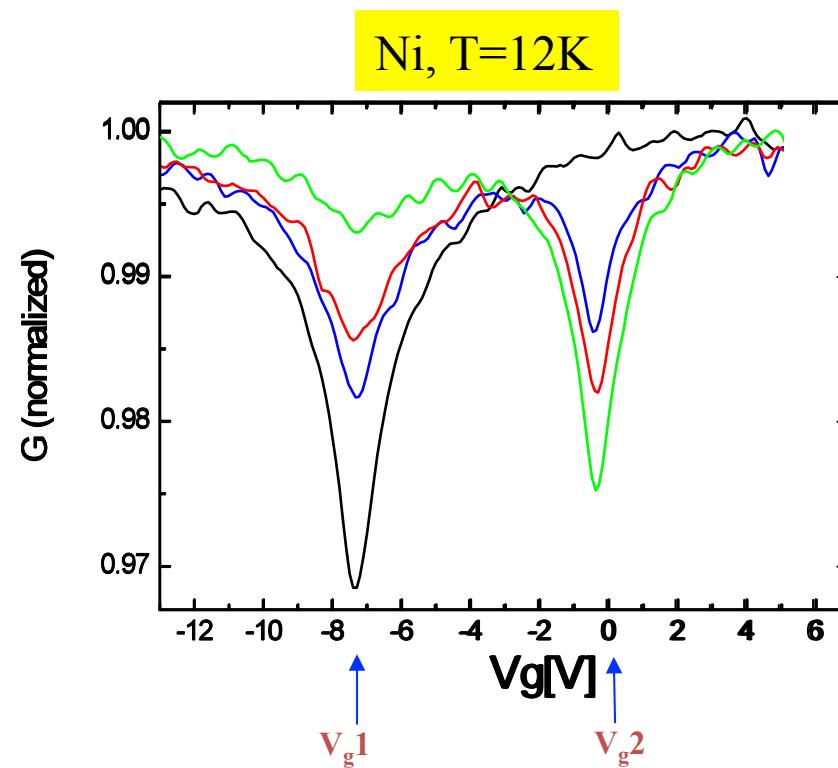
Demonstration of the T dependent dynamics :



# Discontinuous metals: activation

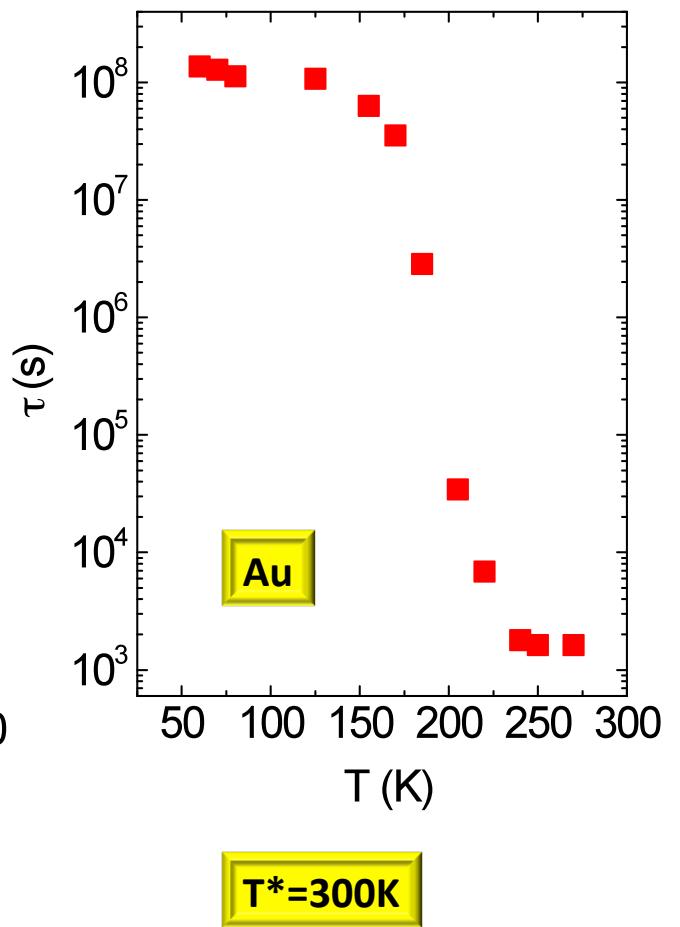
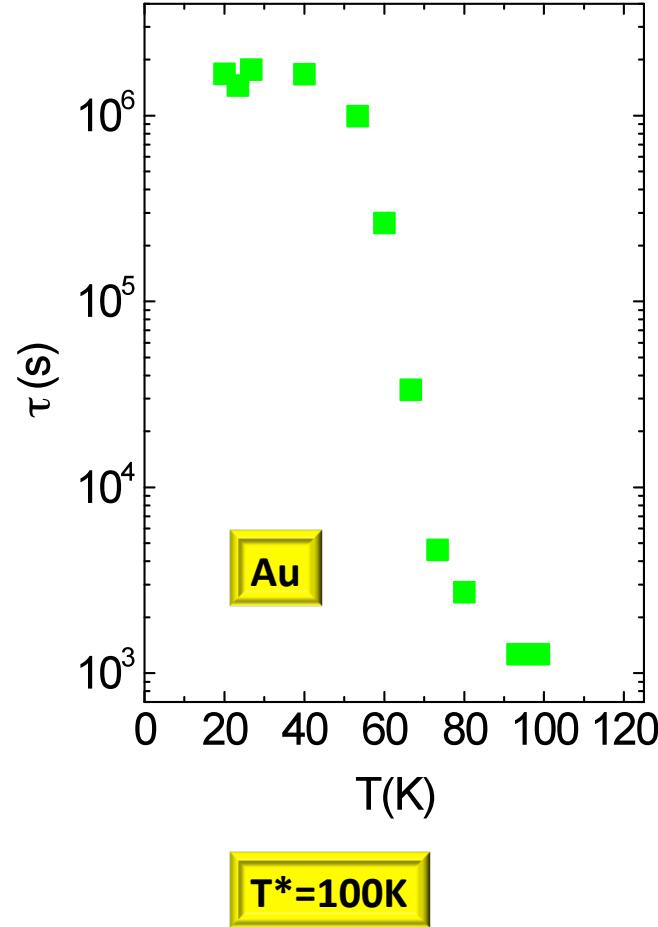
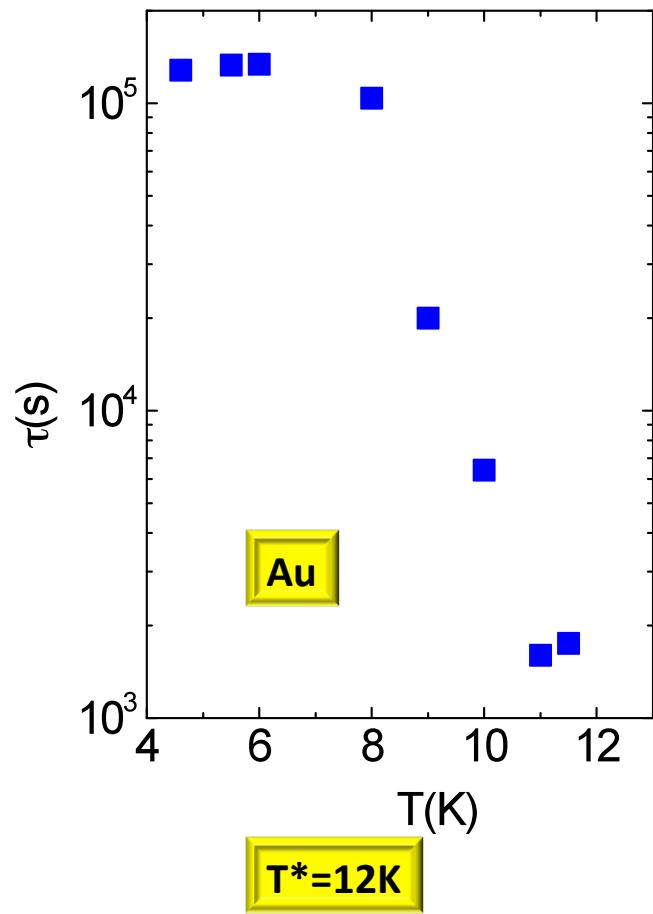


# Discontinuous metals: activation

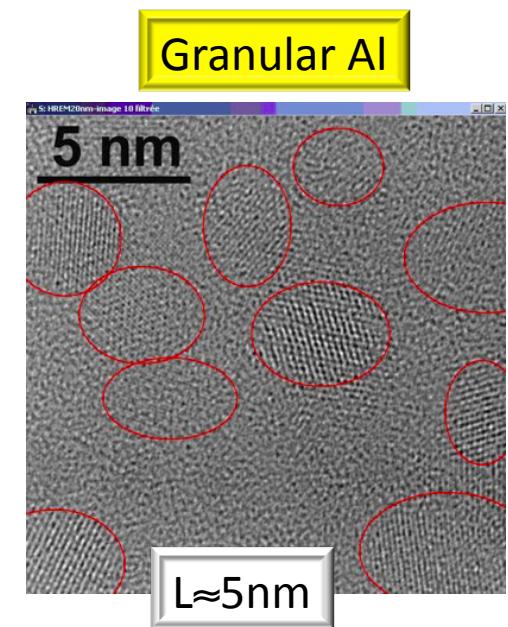
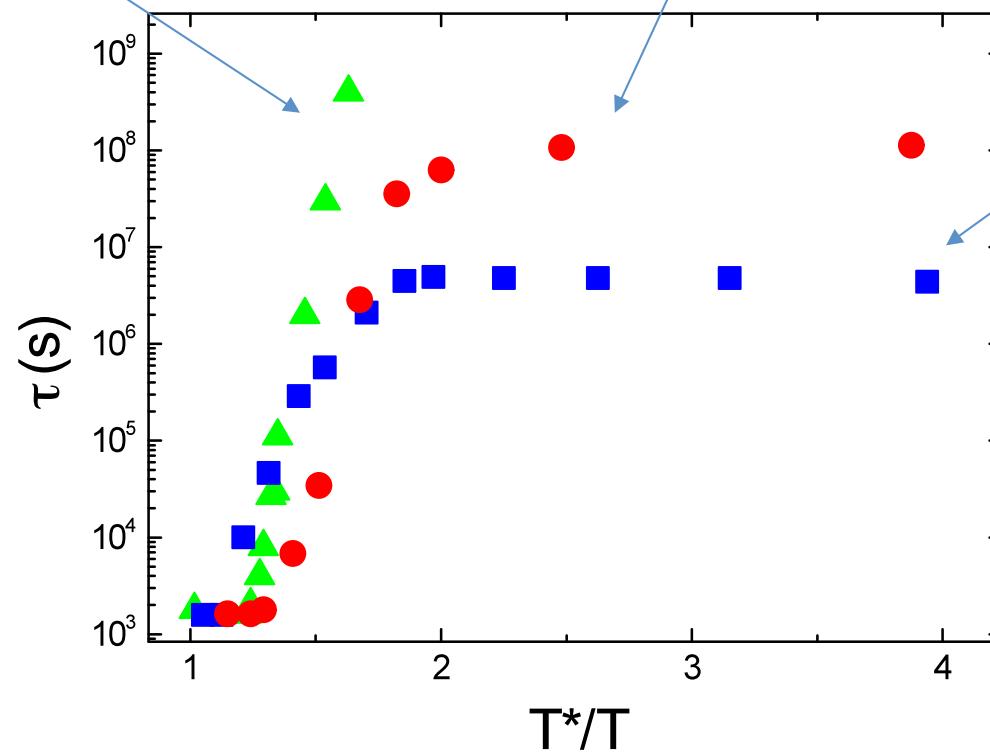
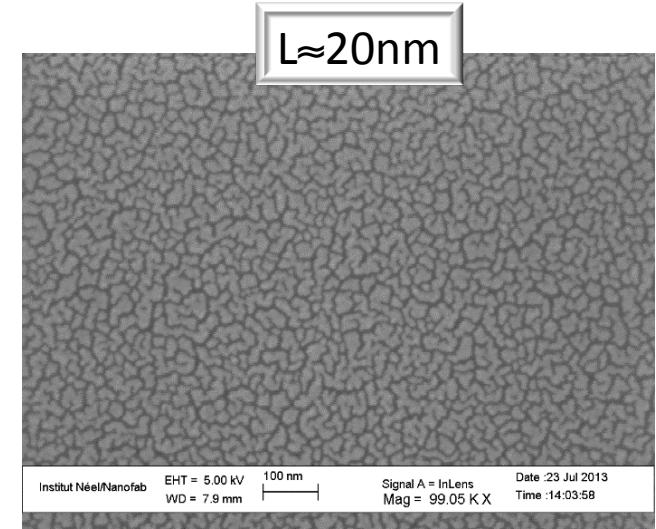
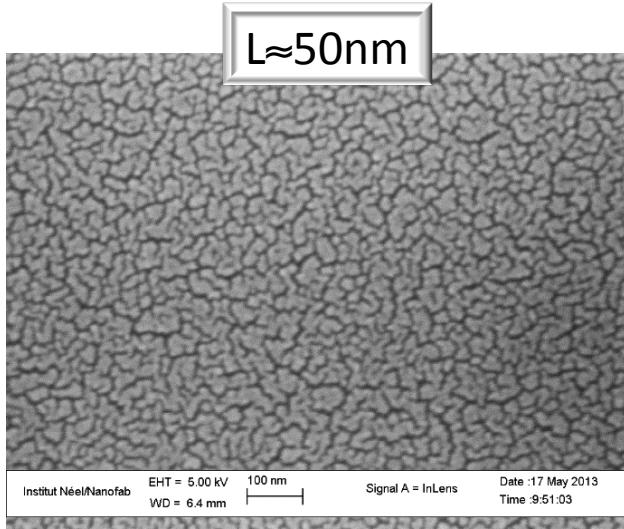
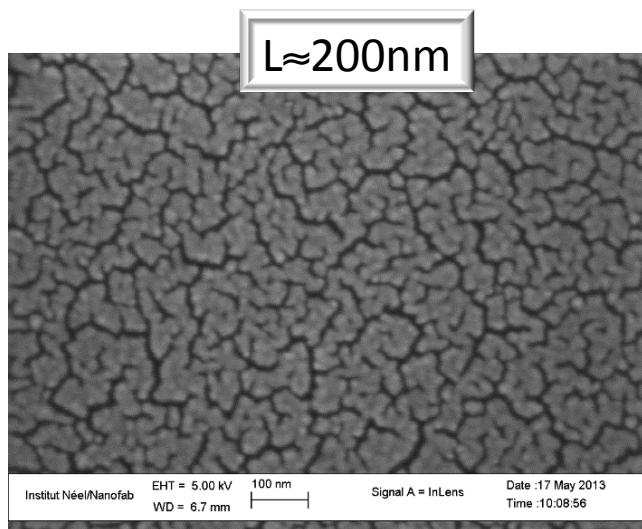


Recall: to determine the T dependence of the dynamics:  $V_{g1}$  at  $T^*$  and  $Vg2$  at  $T \neq T^*$  (here  $T < T^*$ )

# Discontinuous metals: activation

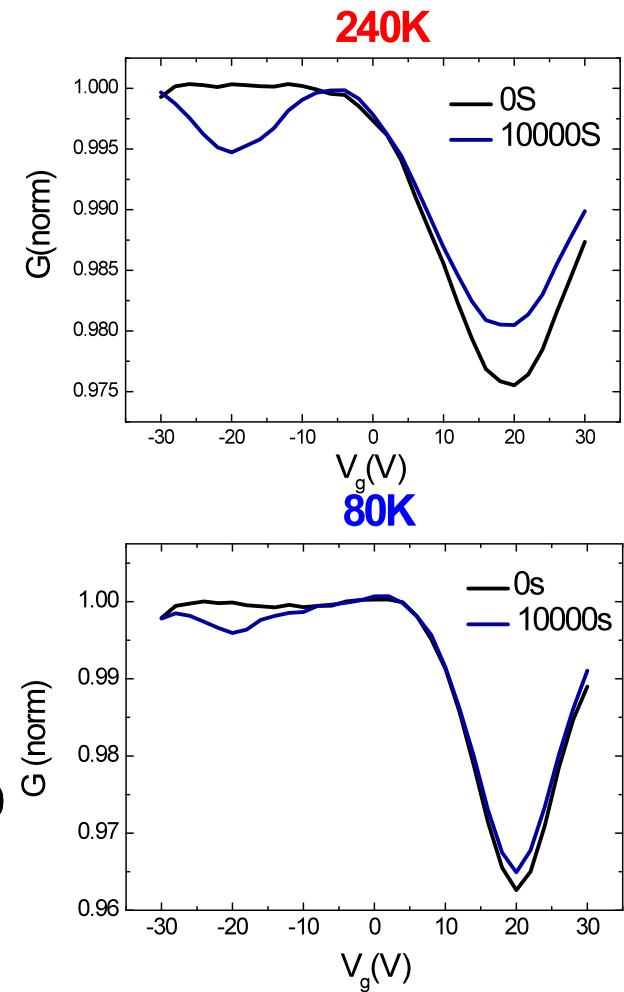
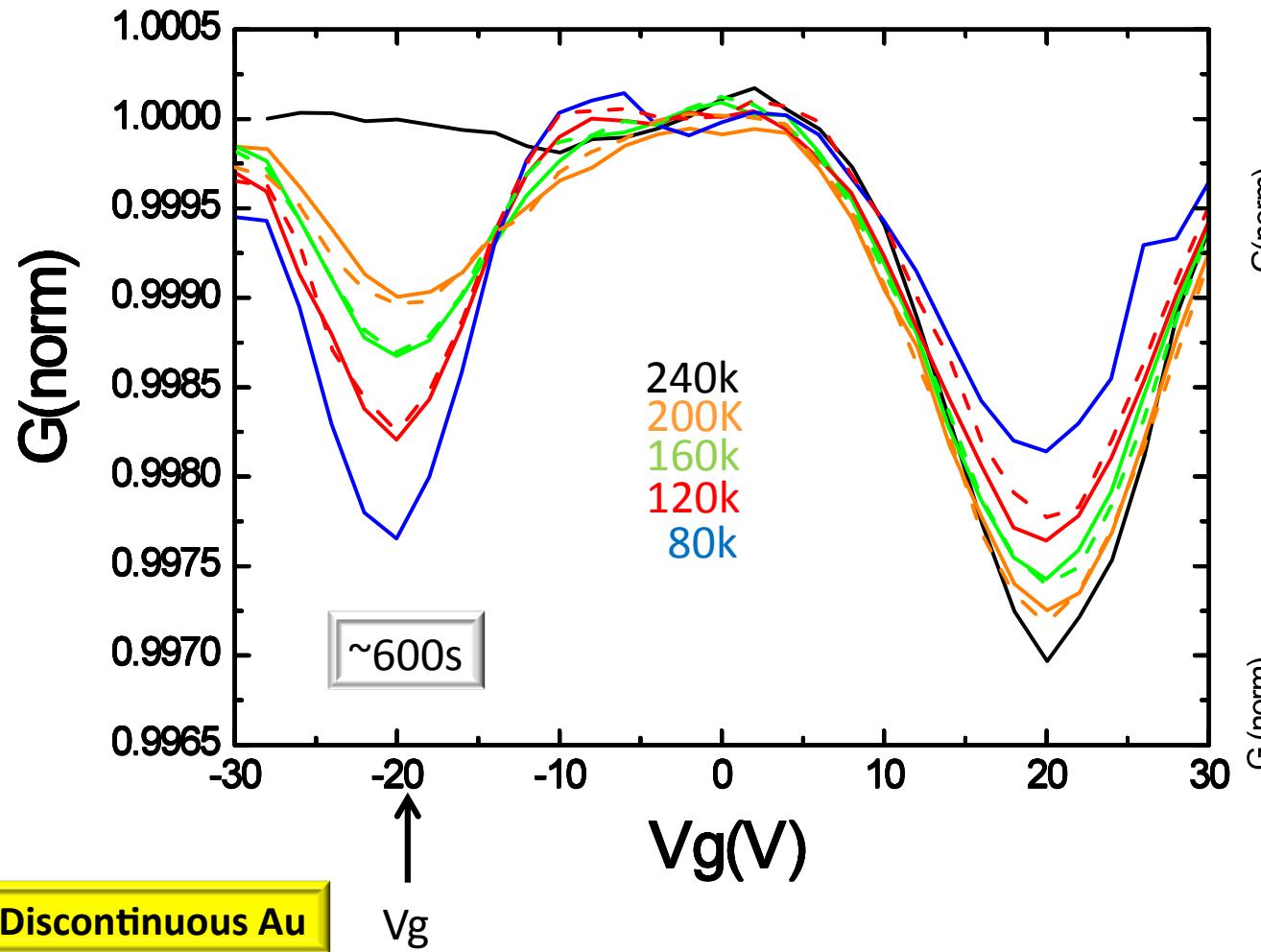


$$\tau = f(T^*/T)$$



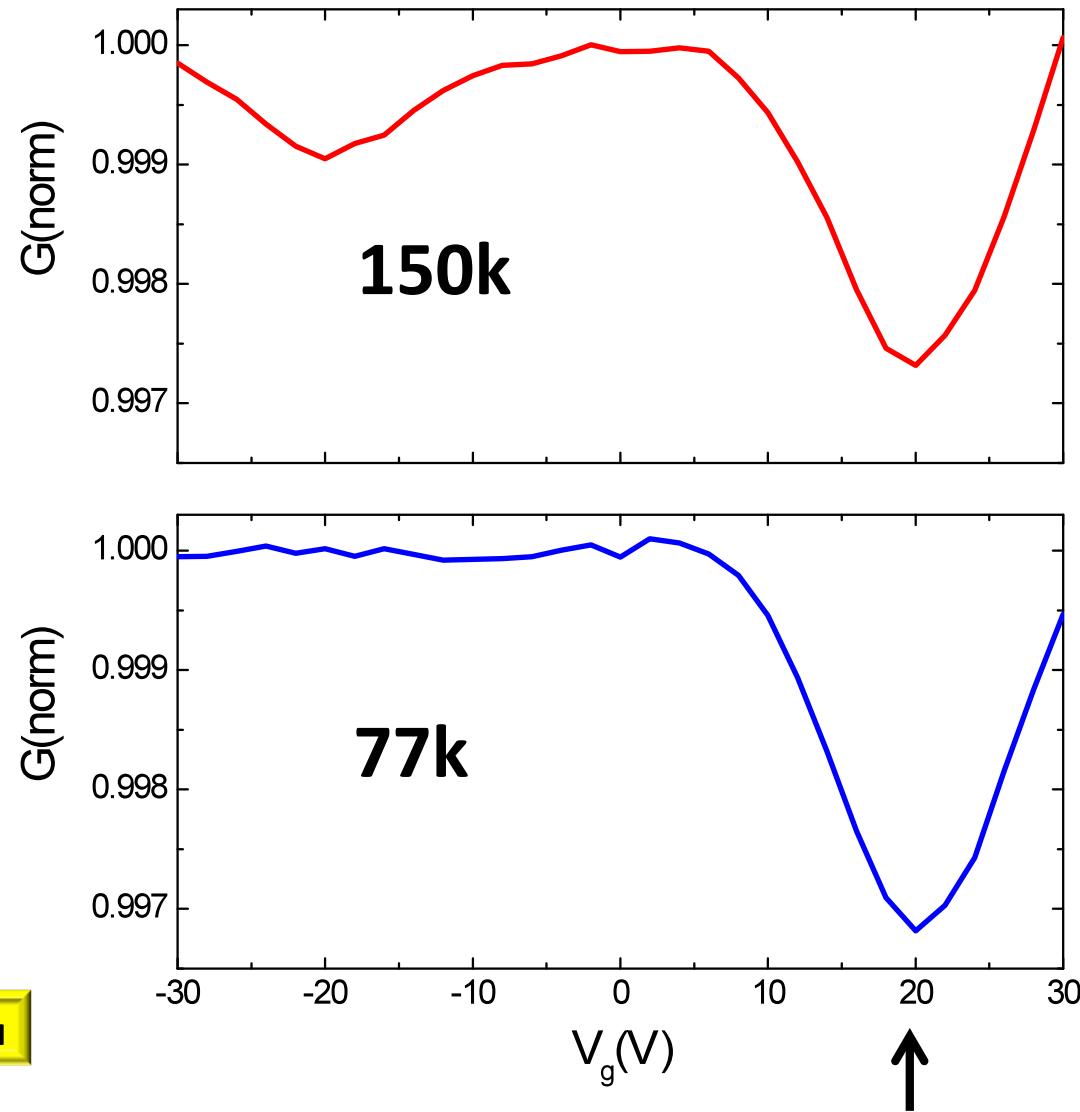
# Discontinuous metals: cooling effect !

+ thermal history memory



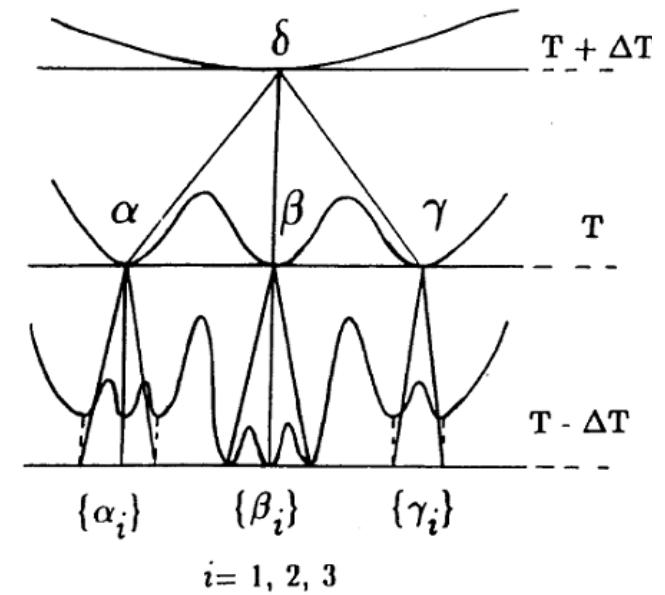
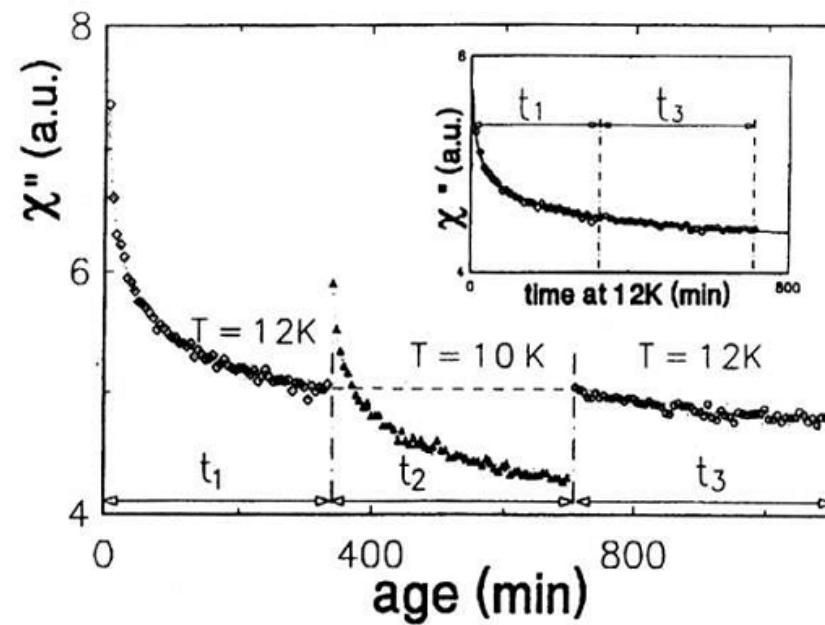
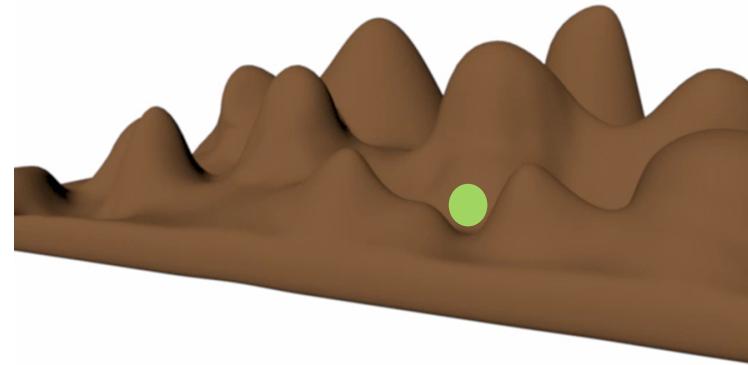
# Discontinuous metals: cooling effect

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# Discontinuous metals: Temperature chaos ?

System's configuration space :



# references

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- Papers by :
  - Z. Ovadyahu and coll. (Jerusalem University)
  - J. Delahaye and T. Grenet (Grenoble, France)
  - A. Frydman et al. (Bar Ilan Univ., Israel)

An (almost) up-to-date review in the book:

*The Electron Glass* (M. Pollak, M. Ortuno and A. Frydman)  
Cambridge University Press (2013)