

2583-16

Workshop on Coherent Phenomena in Disordered Optical Systems

26 – 30 May 2014

**Tunneling Spectroscopy of Fluctuating and Localized Preformed
Coopers Pairs in Highly Disordered Superconducting Films**

Claude CHAPELIER
INAC-SPSMS-LaTEQS, CEA-Grenoble
France

Tunneling spectroscopy of fluctuating and localized preformed Coopers pairs in highly disordered superconducting films

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T. Baturina, *Institute of semiconductor Physics - Novosibirsk*

V. Vinokur, *Material Science Division, Argonne National Laboratory - Argonne*

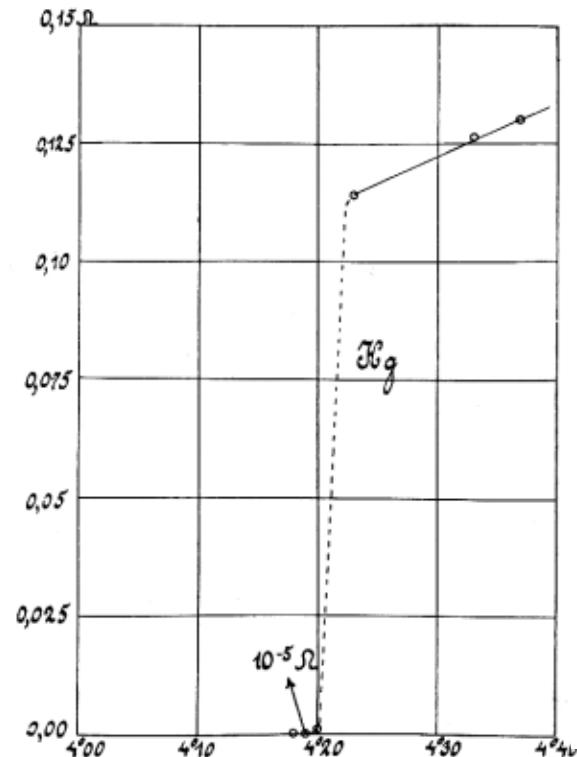
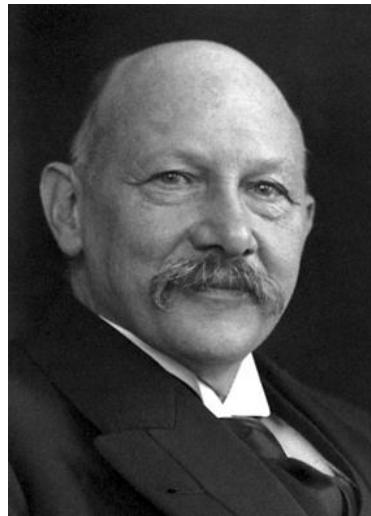
M. Baklanov, A Satta, *IMEC - Leuven*

Maoz Ovadia, Dan Shahar, *The Weizmann Institute of Science*

Mikhail Feigel'man, *L. D. Landau Institute for Theoretical Physics*

Lev Ioffe, *Serin Physics laboratory, Rutgers University*

Superconductivity in pure metals and alloys ...



Kamerlingh Onnes, H., "Further experiments with liquid helium. C. On the change of electric resistance of **pure metals** at very low temperatures, etc. IV. The resistance of **pure mercury** at helium temperatures." *Comm. Phys. Lab. Univ. Leiden*; No. 120b, 1911.

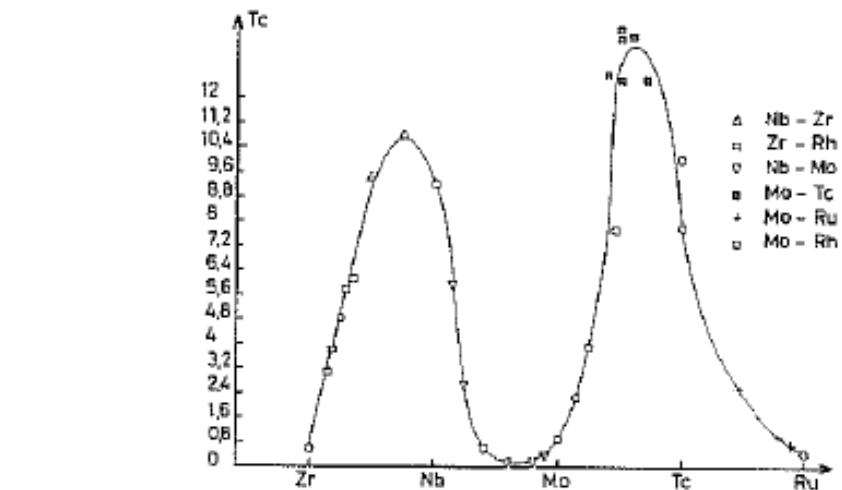
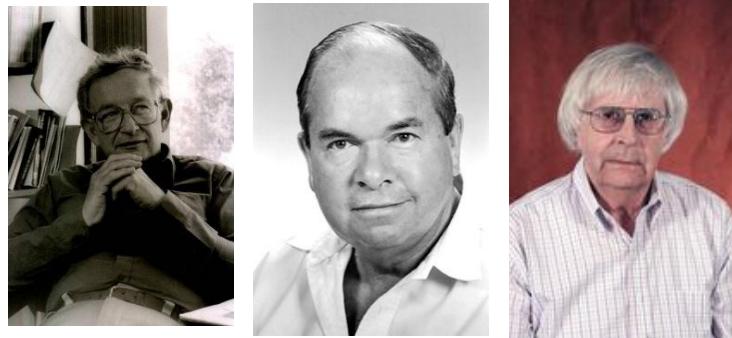


FIG. I.11. — Variation de T_c dans les alliages à base de Zr, Nb, Mo, Tc et Ru (voir ROBERTS).

J.P. Burger
la supraconductivité des métaux, des alliages et des films minces (Ed. Masson)

Superconductivity and disorder



P.W. Anderson, *J. Phys. Chem. Solids.* **11**, 26, (1959)

A.A. Abrikosov & I.P. Gorkov, *Sov. Phys. JETP* **8**, 1090, (1959)

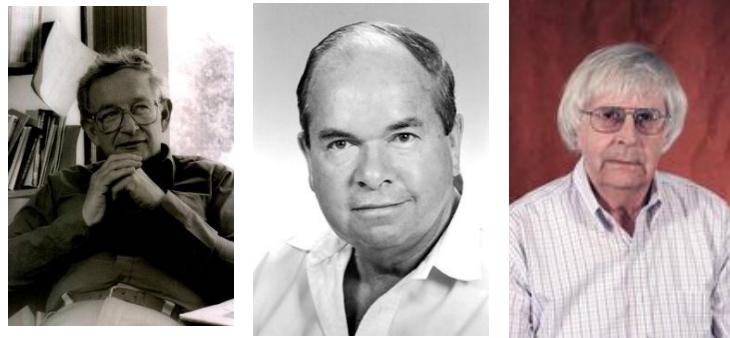
➤ Weak disorder : Anderson's theorem

BCS superconductivity can be built on pairing of exact time reversal symmetric eigenstates

$$k_F l_e > 1$$

→ T_c and Δ insensitive to weak disorder

Superconductivity and disorder



P.W. Anderson, *J. Phys. Chem. Solids.* **11**, 26, (1959)

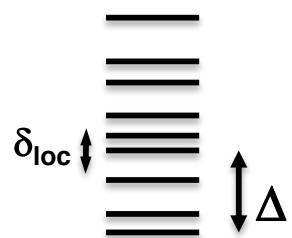
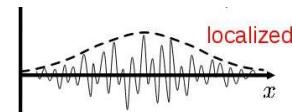
A.A. Abrikosov & I.P. Gorkov, *Sov. Phys. JETP* **8**, 1090, (1959)

➤ Weak disorder : Anderson's theorem

BCS superconductivity can be built on pairing of exact time reversal symmetric eigenstates as long as :

$$k_F l_e > 1$$

→ T_c and Δ insensitive to weak disorder



➤ Strong disorder $k_F l_e \leq 1$

BCS state can survive even if single particles are localized as long as mean level spacing δ_{loc} is smaller than SC gap Δ :

$$1 = U \int_{\varepsilon < \omega_D} \frac{1}{\sqrt{\varepsilon^2 + \Delta^2}} v(\varepsilon) d\varepsilon \rightarrow \delta = \frac{1}{v \zeta_{loc}^d} < \Delta$$

Density-of-states Localization volume

Kapitulnik, Kotliar, *PRL* (1985), *PRB* (1986)

Ma & Lee, *PRB* (1985)

Sadowskii, *Phys. Rep.* (1997)

Ghosal *et al.*, *PRL* (1998) ; *PRB* (2001)

Feigel'man *et al.*, *PRL* (2007) ; *Ann.Phys.* (2010)

Porkrovsky, Falco, Natterman *PRL* (2010)

Bouadim *et al.* *Nature Physics* (2011)

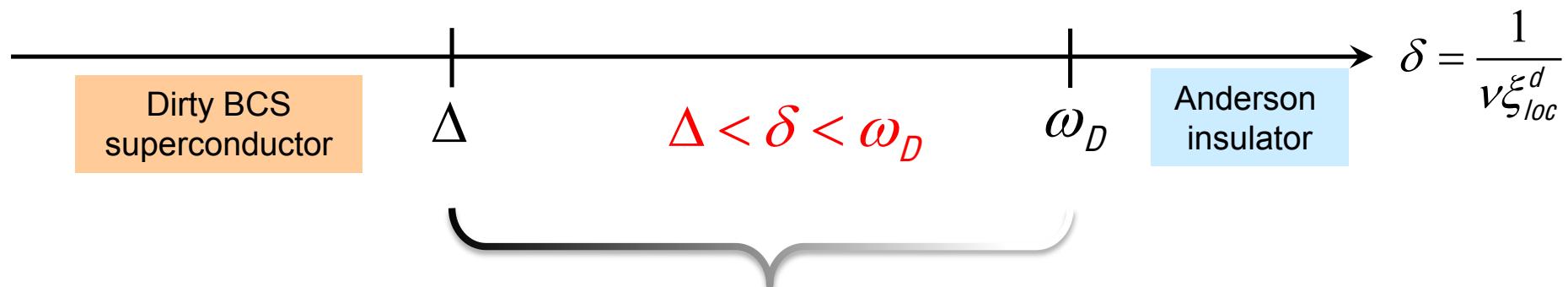
Localized superconductors

Michael Ma and Patrick A. Lee

Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139

(Received 10 June 1985)

Thus, for $\rho\Delta_0L^d < 1$, $\Delta(\mathbf{r})$ can no longer be uniform, while for $\rho\omega_DL^d < 1$, superconductivity definitely ceases to exist. The question is whether it survives in between.



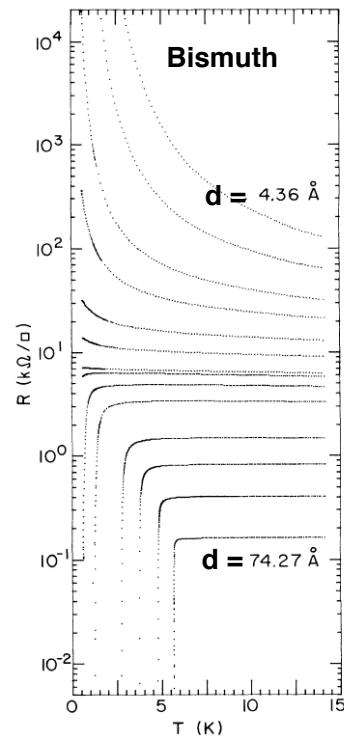
Q1: Do Cooper pairs vanish with T_c or get localized ?

Q2: Nature of the ensuing insulating state ?

Superconductor-insulator transition (SIT) in thin films

Measure of disorder: sheet resistance

Amorphous films

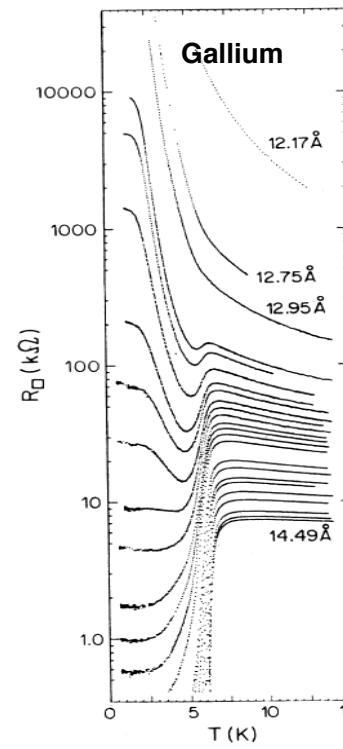


D.B. Haviland, Y. Lui, A.M. Goldman, *PRL* 62, 2180 (1989)

- Continuous decrease of T_c
- Cooper pairing suppressed at the SIT

$$R = \frac{\rho}{d}$$

Granular films



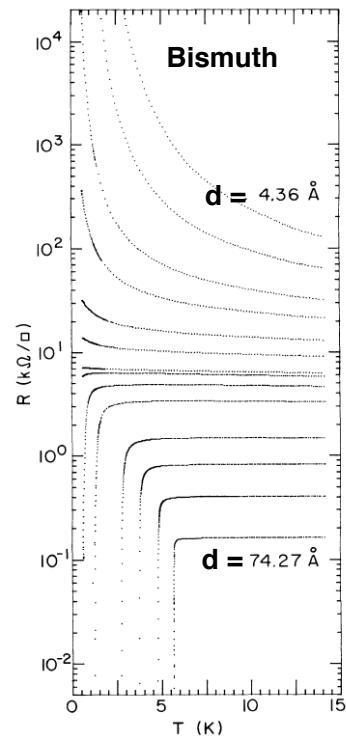
H. M. Jaeger, et al. *Phys.Rev.B* 34, 4920 (1986)

- SIT due to phase fluctuations
- Cooper pairs localized in grains

Superconductor-insulator transition (SIT) in thin films

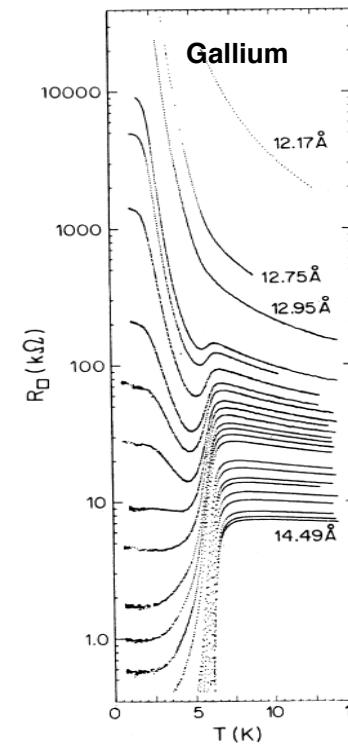
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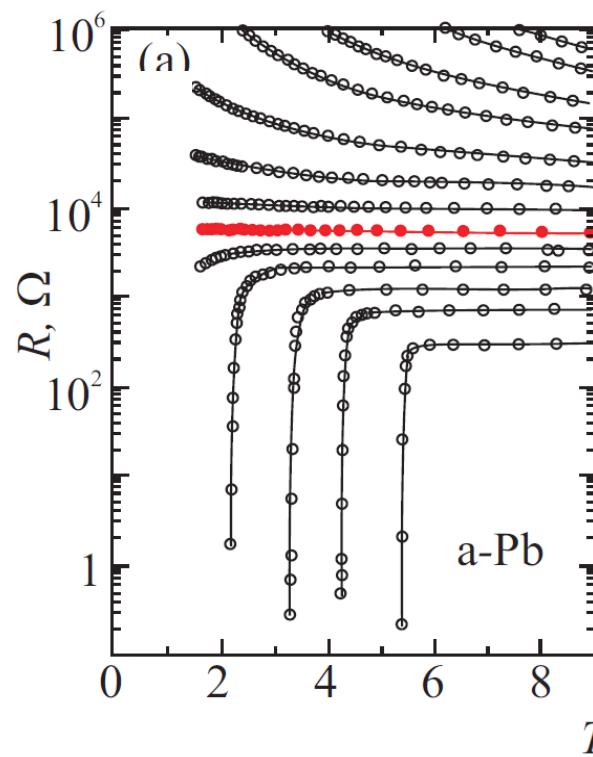
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Superconductor-insulator transition (SIT) in thin films

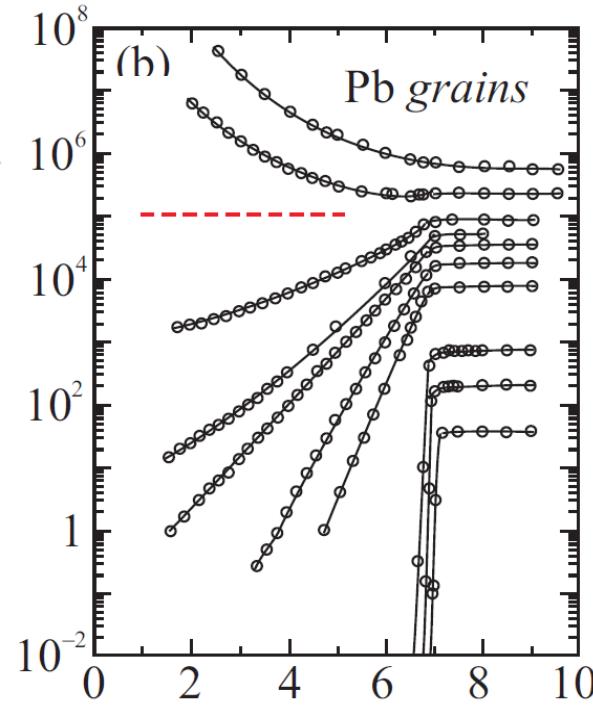
Uniform system



Frydman, A., *Physica C : Superconductivity* **391**, 189 (2003)

- Continuous decrease of T_c
- Cooper pairing suppressed at the SIT

Granular system



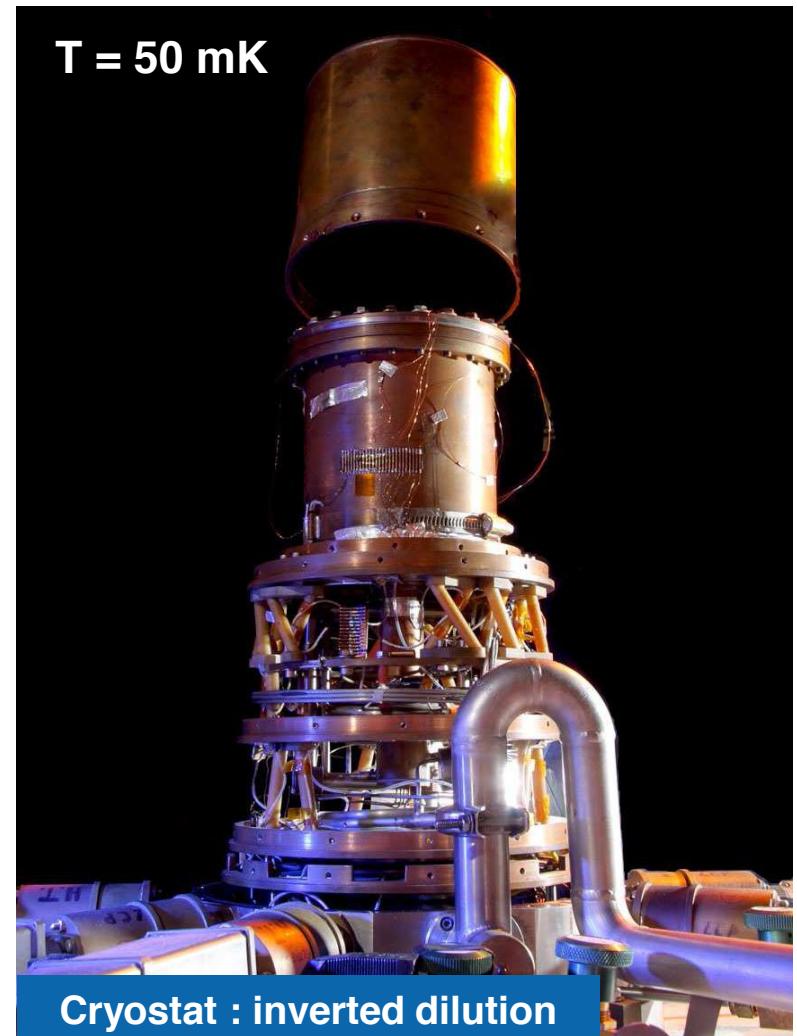
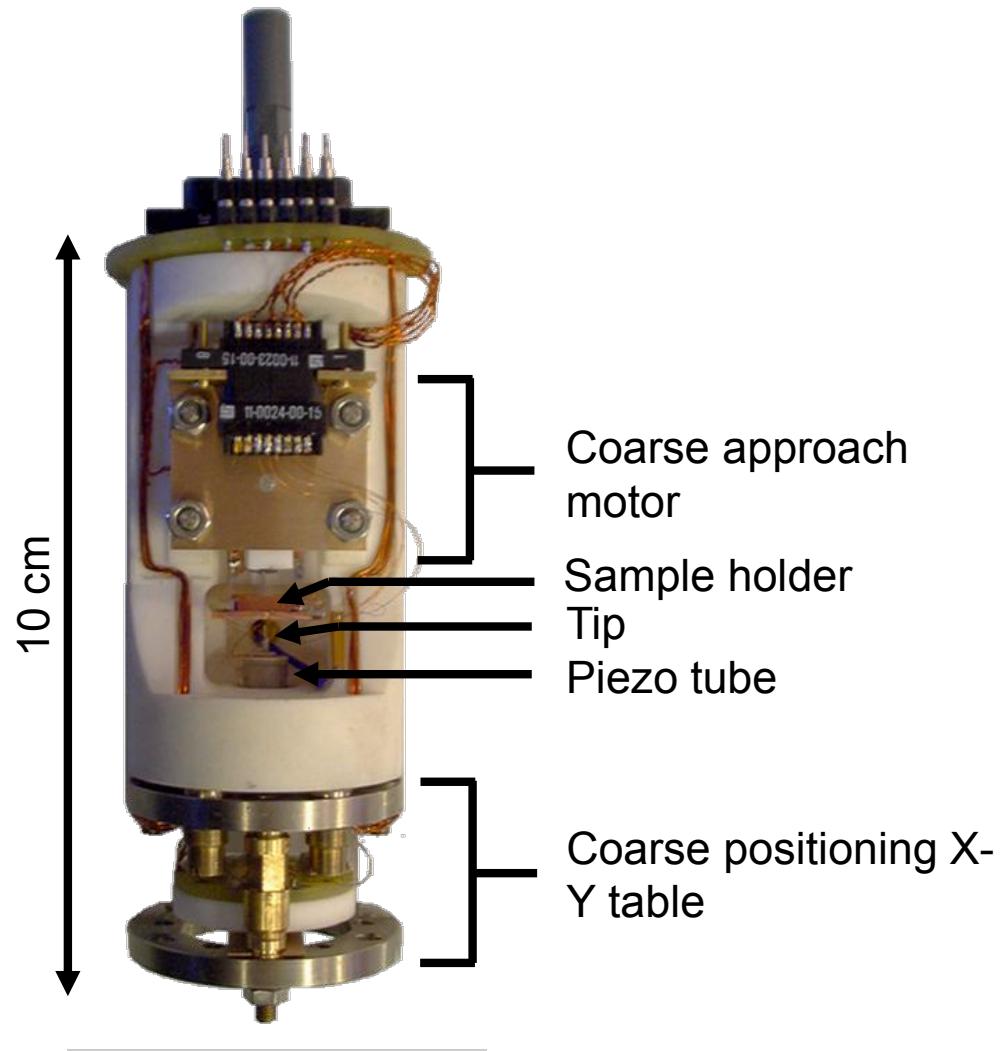
Hsu, S.-Y., and Valles, J. M. *Phys. Rev. B* **48**, 4164 (1993)

- SIT due to phase fluctuations
- Cooper pairs localized in grains

Continuous decrease of T_c

→ Homogeneously disordered films

Scanning Tunneling Microscopy : experimental set-up

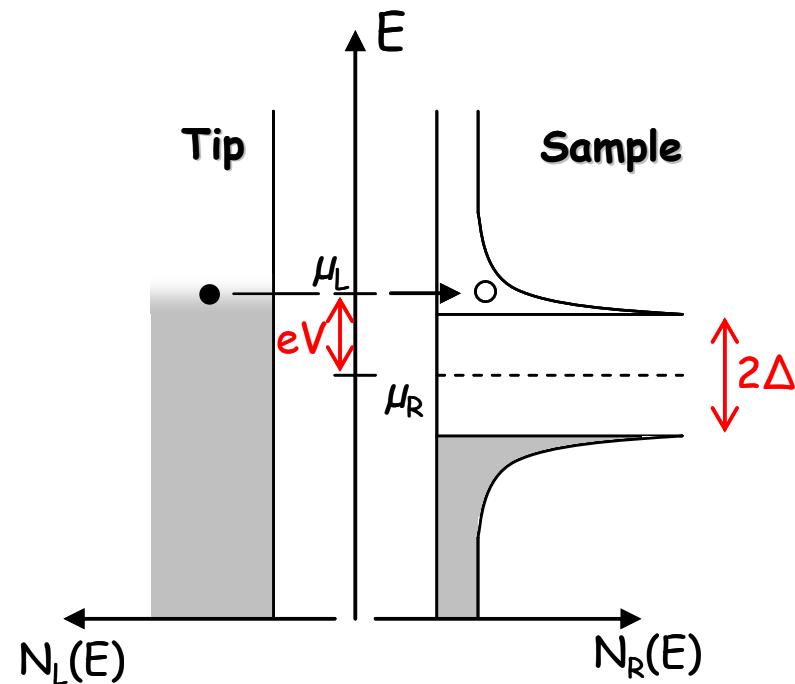


➤ Combined transport & spectroscopy measurements

Scanning Tunneling Spectroscopy

Measurement of the Density-Of-States (DOS)

$$G(V) = \frac{dI}{dV} \propto \int d\varepsilon N_s(\varepsilon) \left(-\frac{\partial f_T(\varepsilon + eV)}{\partial V} \right)$$



$N_s(\varepsilon)$: density of states of the sample

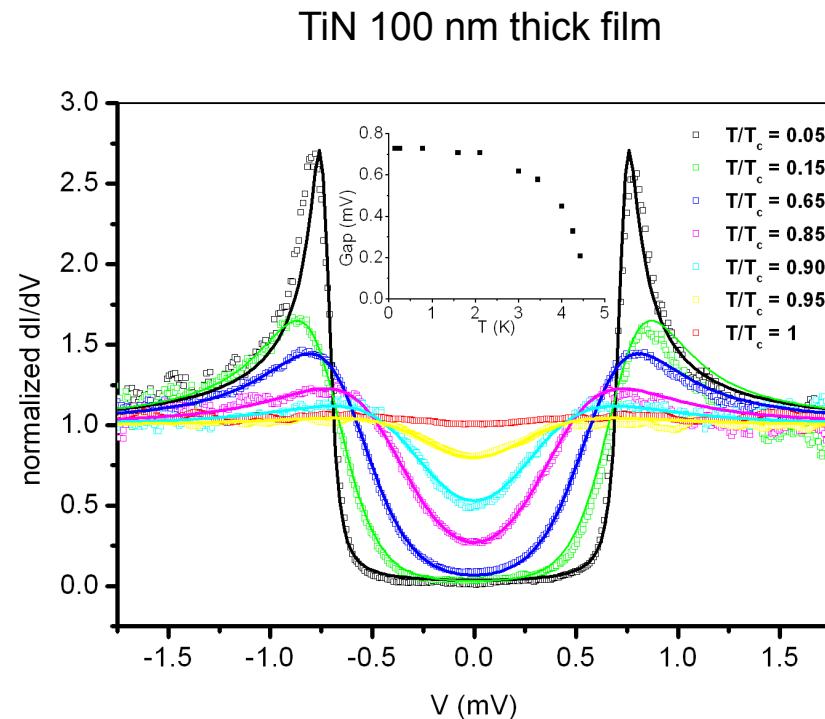
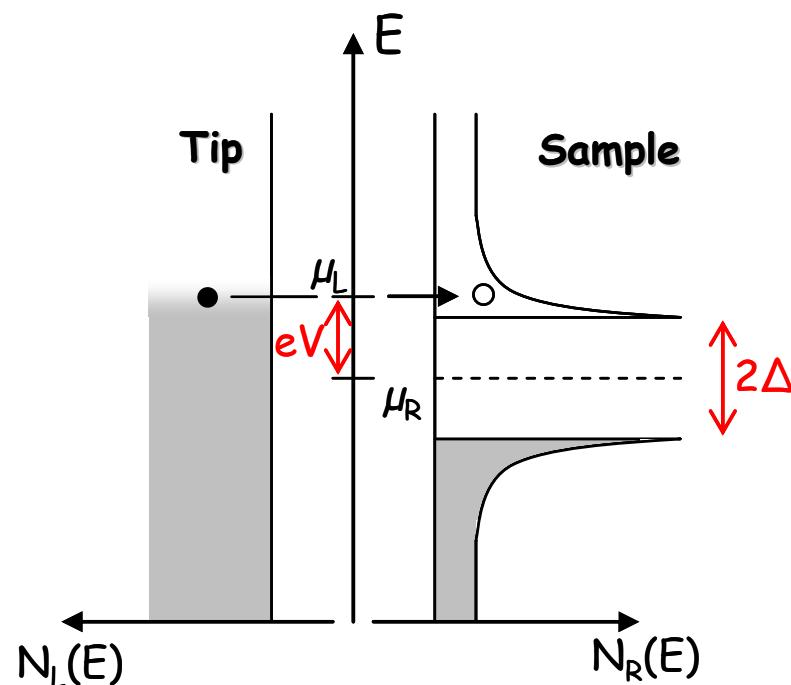
$f_T(\varepsilon)$: Fermi-Dirac distribution

$\Delta(T)$: superconducting gap

Scanning Tunneling Spectroscopy

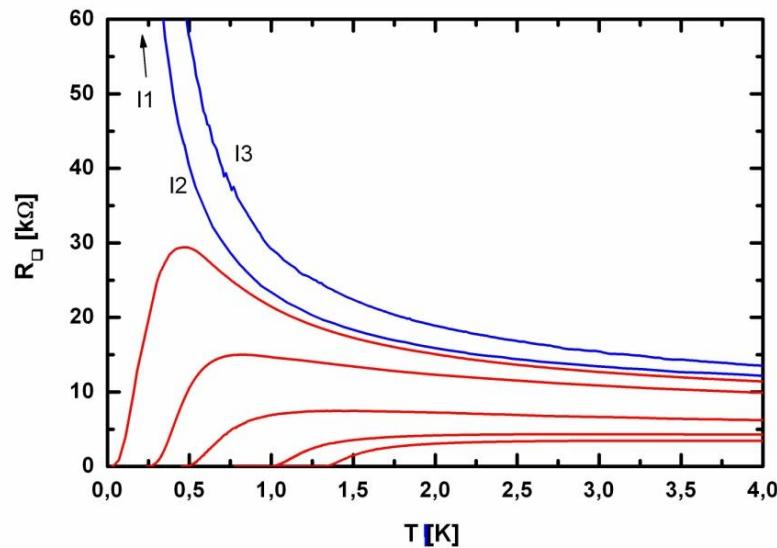
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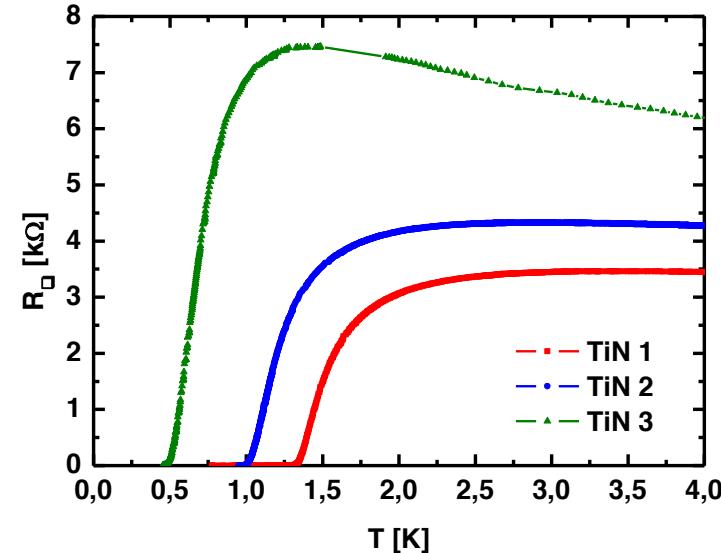
W. Escoffier, et al., PRL 93, 217005, (2004)

TiN Superconductor-Insulator transition



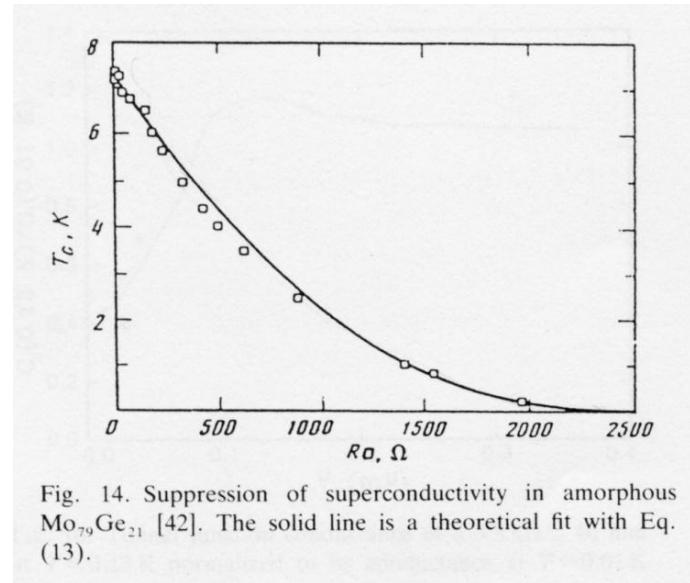
T. I. Baturina, et al. PRL 99, 257003 (2007)

TiN 1 : 3.6 nm, grown at 400 ° C
TiN 2 : 5.0 nm, grown at 350 ° C
TiN 3 : 5.0 nm, grown at 350 ° C + plasma etching



Sacépé et al., PRL 101, 157006 (2008)

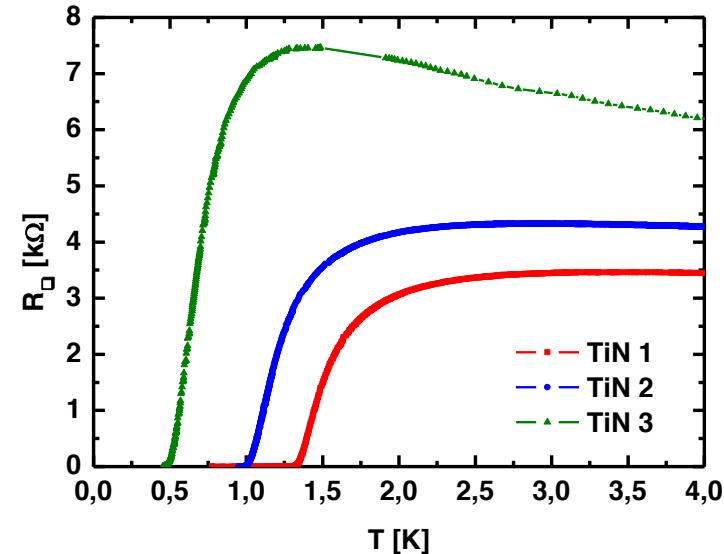
Fermionic scenario



$$\frac{T_c}{T_c^{bulk}} = e^\gamma \left(\frac{1/\gamma - \sqrt{r/2} + r/4}{1/\gamma + \sqrt{r/2} + r/4} \right)^{1/\sqrt{2r}}$$

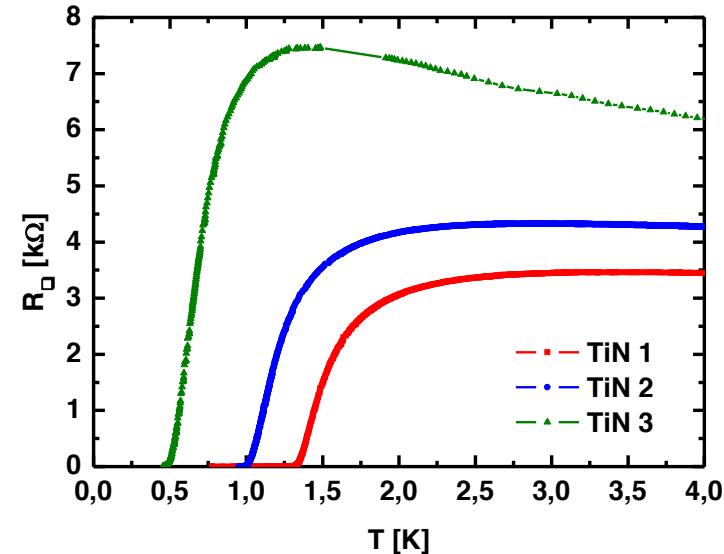
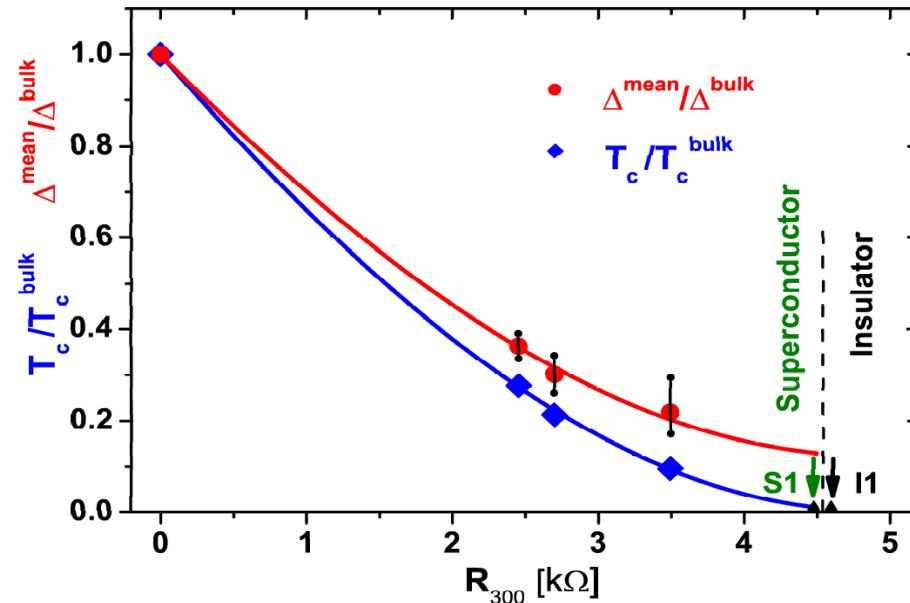
$$r = \frac{R_\square e^2}{\pi h} \quad \gamma = 6.2$$

A. M. Finkel'stein, *Physica B* **197**, 636, (1994)



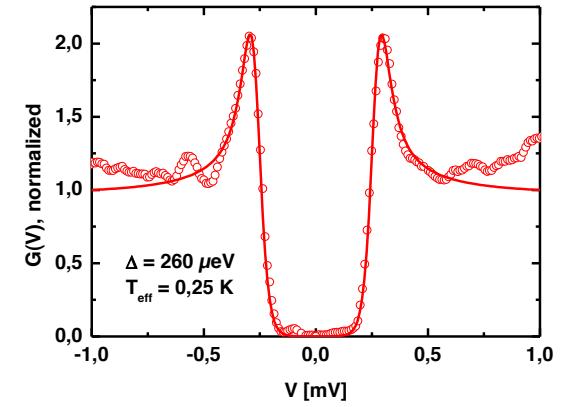
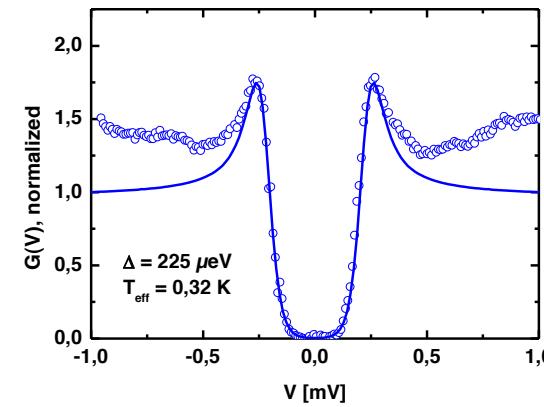
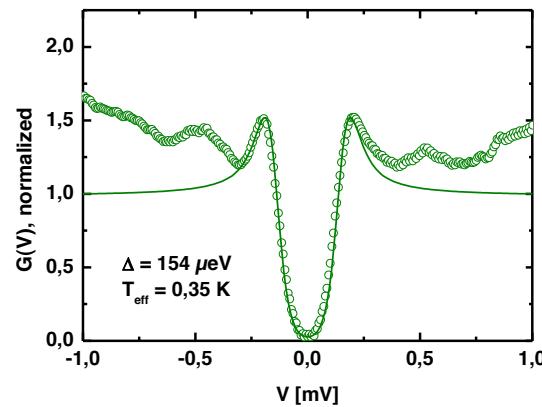
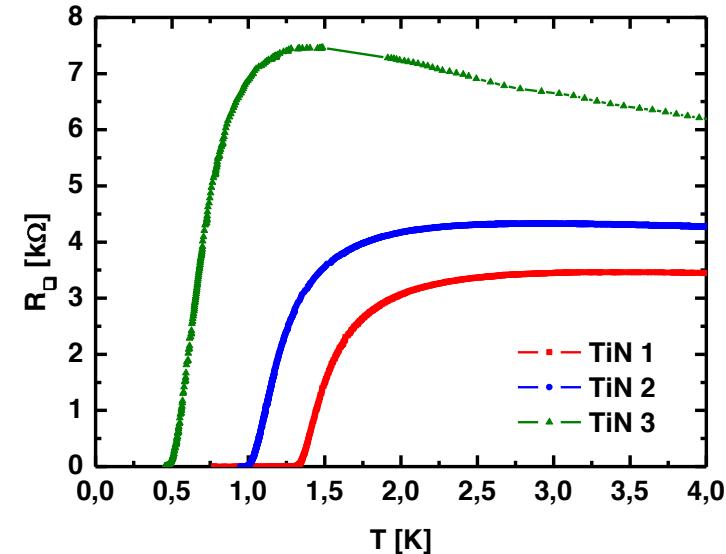
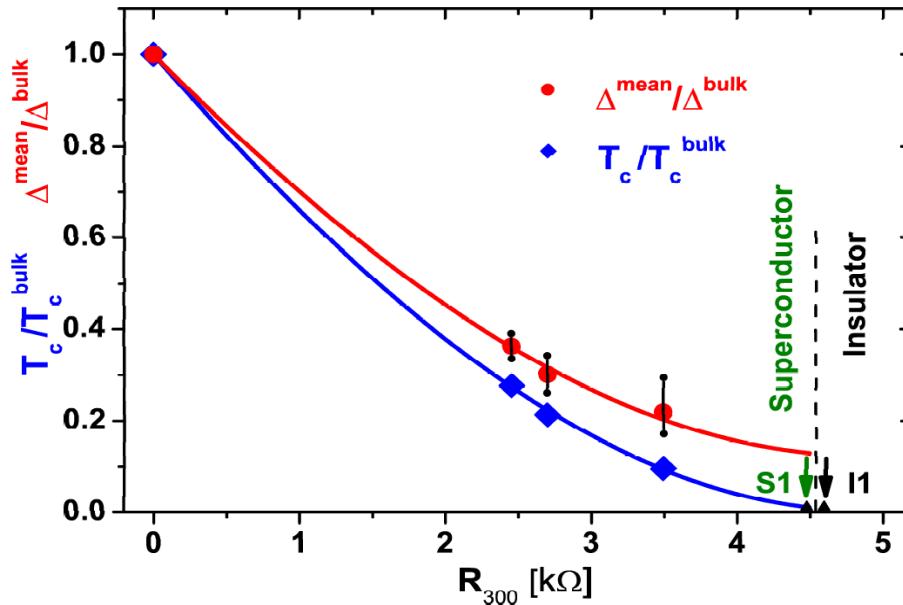
Sacépé et al., *PRL* **101**, 157006 (2008)

TIN Superconductor-Insulator transition



Sacépé et al., PRL 101, 157006 (2008)

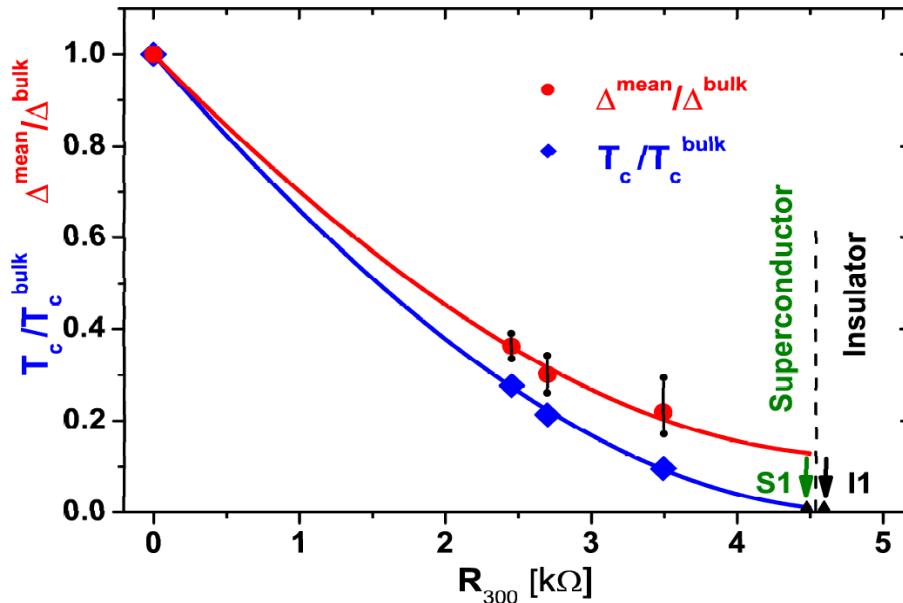
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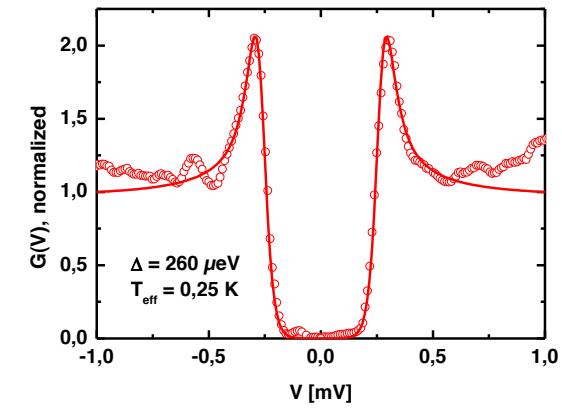
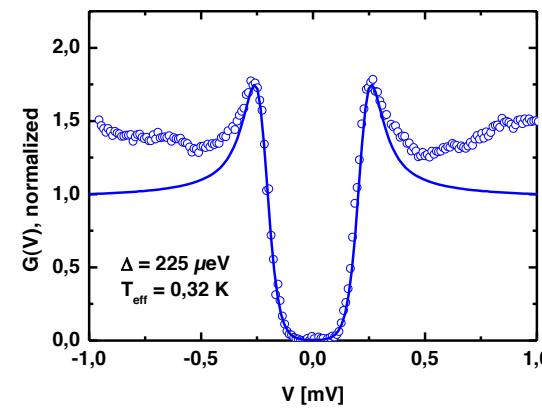
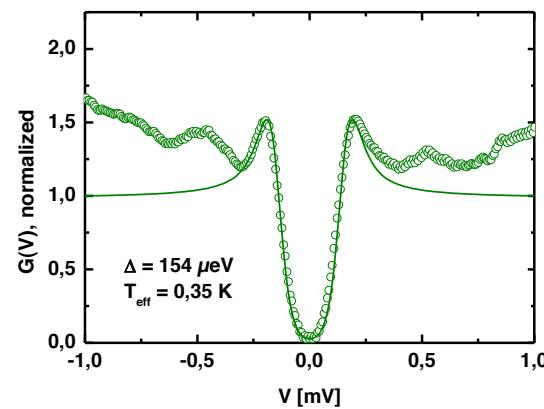
← Increasing disorder

Sacépé et al., PRL 101, 157006 (2008)

TIN Superconductor-Insulator transition



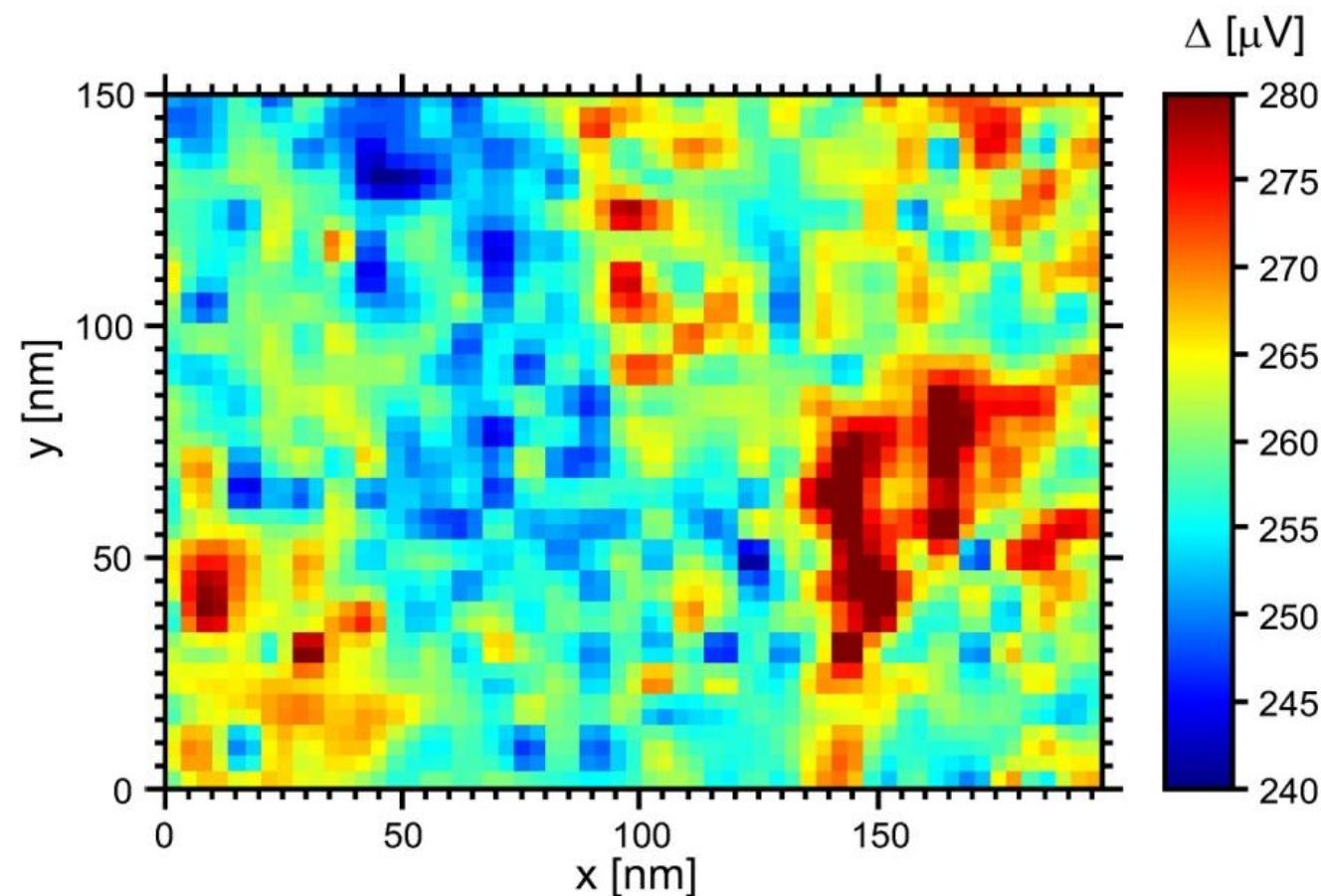
$T_c [\text{K}]$	Δ / T_c
4.7	1.8
1.3	2.3
1	2.6
0.45	4



← Increasing disorder

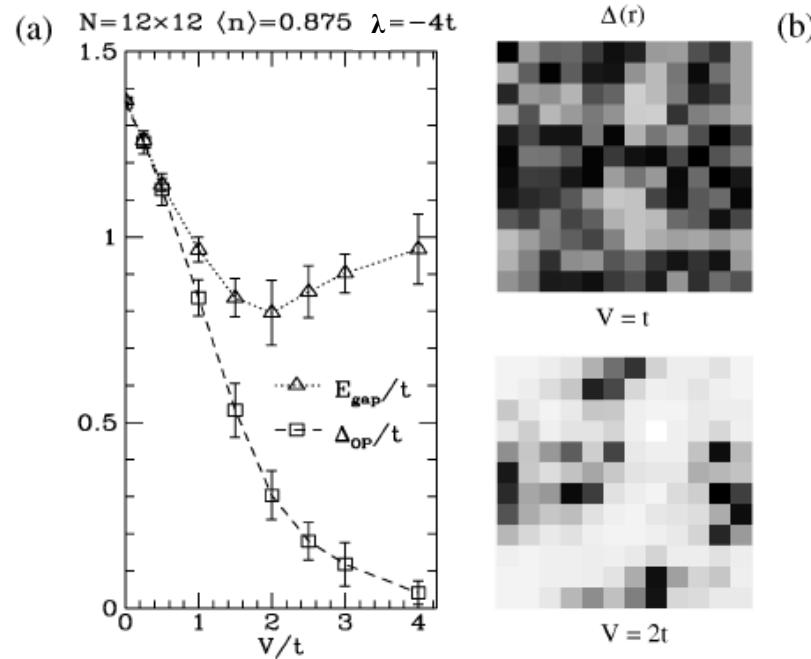
Sacépé et al., PRL 101, 157006 (2008)

TiN 1 ($T_c = 1.3$ K)



Anderson localization and superconducting pairing

A. Ghosal, M. Randeria, N. Trivedi, *PRL 81*, 3940, (1998) & *PRB 65*, 014501 (2001)



Anderson model :

$$H_0 = -t \sum_{\langle i, j \rangle, \sigma} (c_{i\sigma}^\dagger c_{j\sigma} + h.c.) + \sum_{i,\sigma} (V_i - \mu) n_{i\sigma}$$

Hopping parameter : t

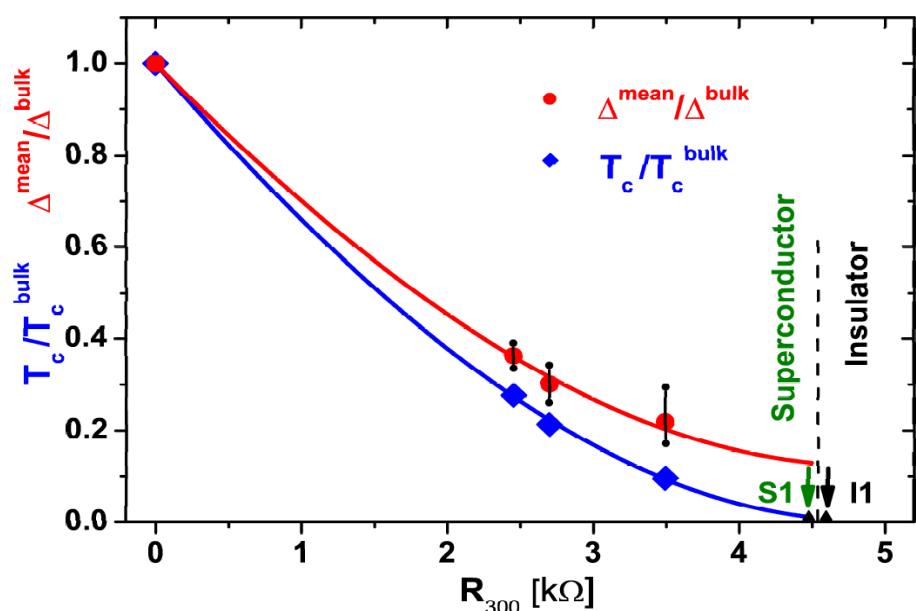
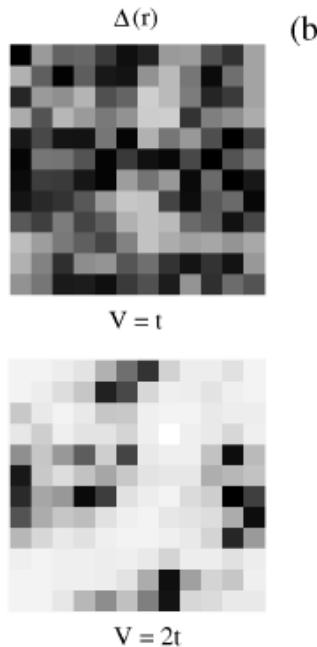
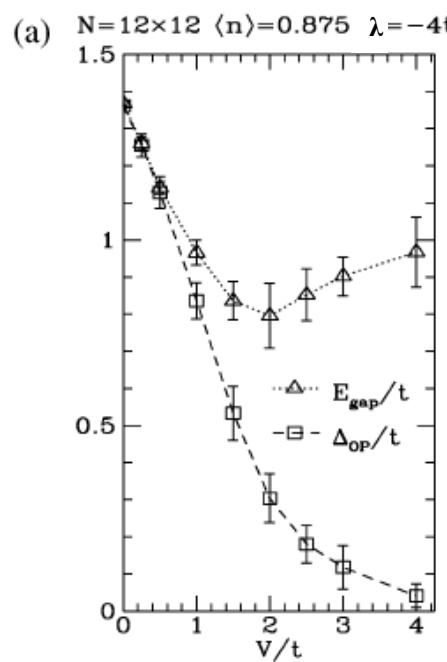
On-site disorder : V_i

Attractive interaction λ :

$$H_{\text{int}} = -\lambda \sum_i n_{i\uparrow} n_{i\downarrow}$$

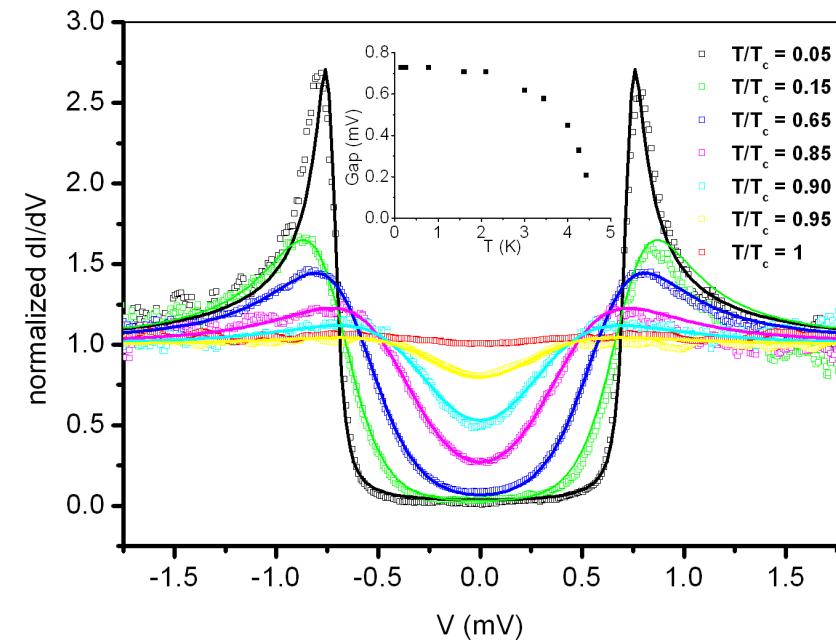
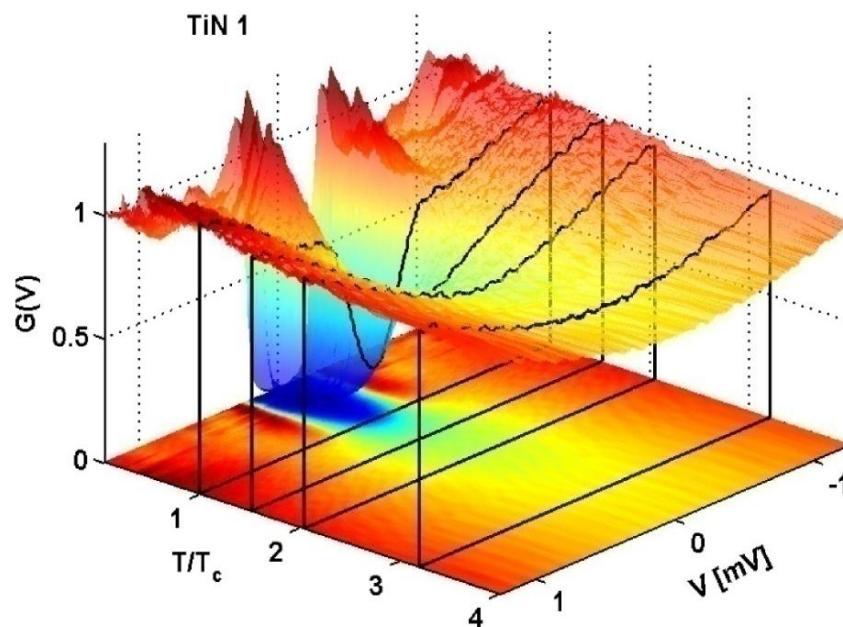
Anderson localization and superconducting pairing

A. Ghosal, M. Randeria, N. Trivedi, *PRL 81*, 3940, (1998) & *PRB 65*, 014501 (2001)

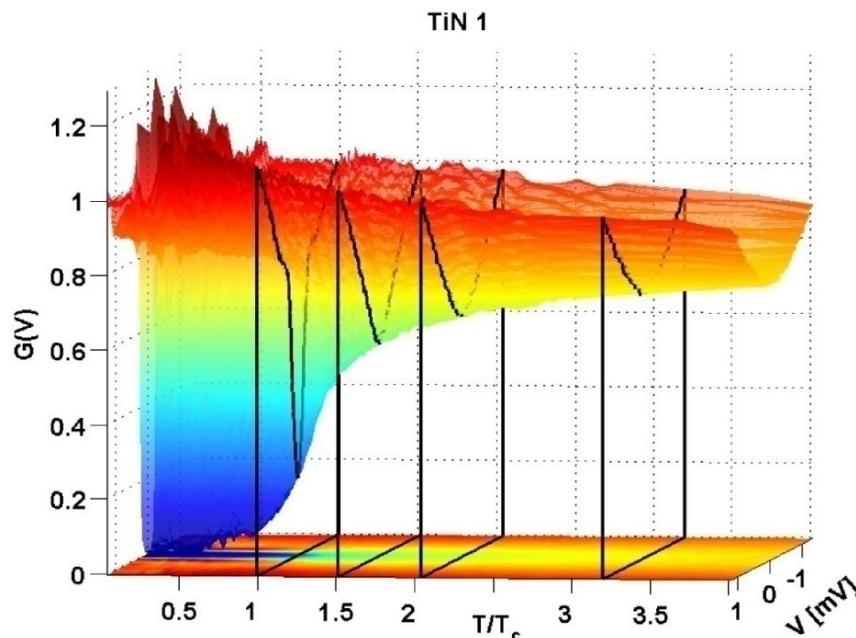


$T_c [K]$	Δ/T_c
4.7	1.8
1.3	2.3
1	2.6
0.45	4

Thermal evolution of the superconducting gap

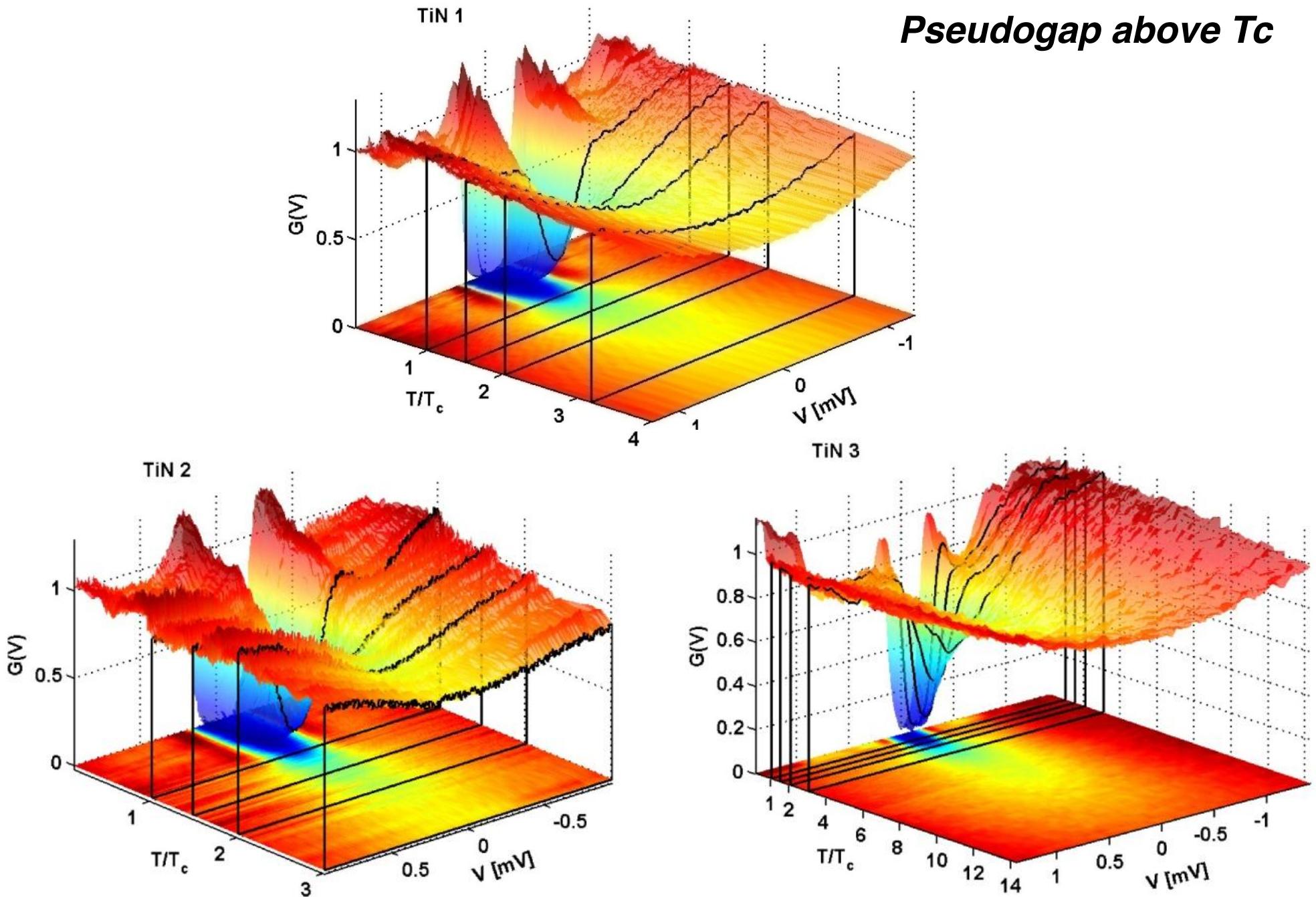


W. Escoffier, et al., *PRL* **93**, 217005, (2004)



B. Sacépé, et al., *Nature Communications* (2010)

Thermal evolution of the superconducting gap



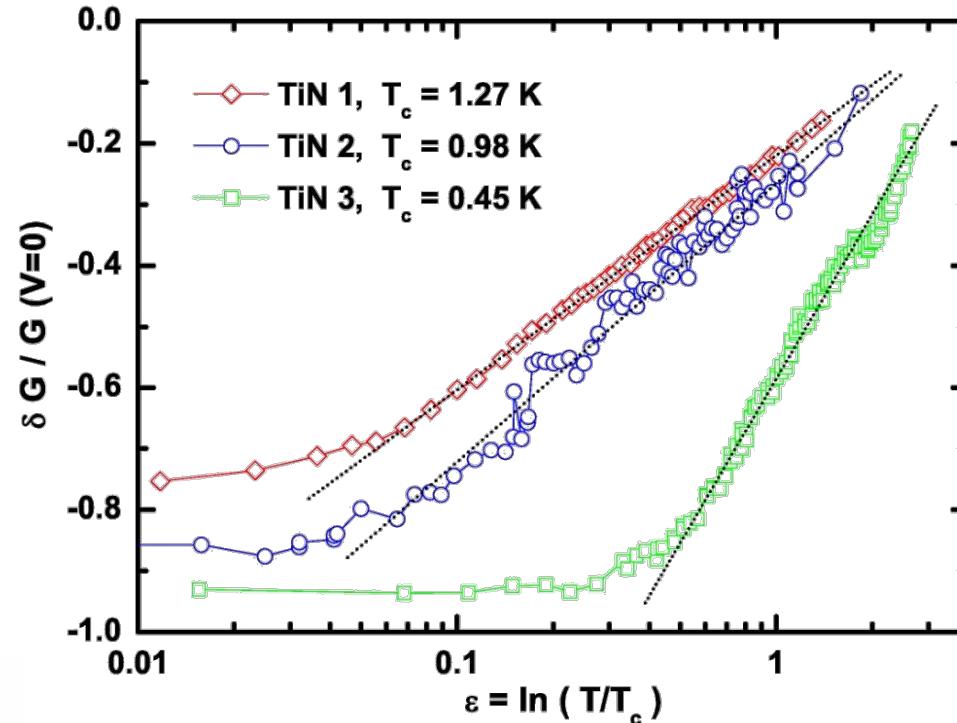
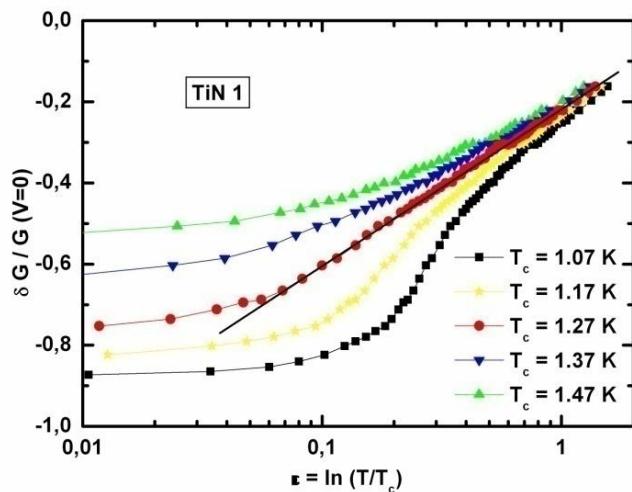
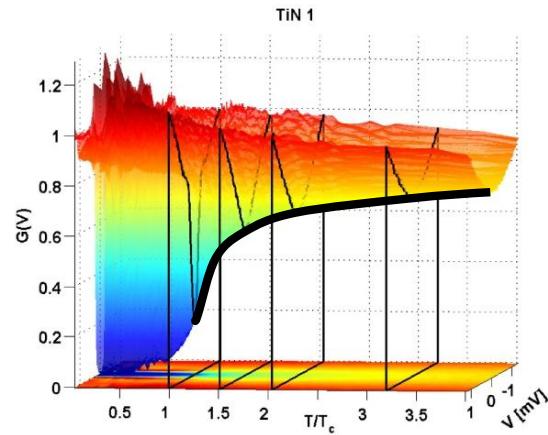
Pseudogap

Superconducting fluctuations correction to the DOS

A. Varlamov and V. Dorin, Sov. Phys. JETP 57, 1089, (1983)

$$\frac{\delta G}{G}(eV = 0) = -2Gi \ln(\ln \frac{T_c}{T})$$

$$Gi = \frac{\hbar}{16e^2} R_{\square}$$



Slopes increase with $G_i \sim R_{\square}$

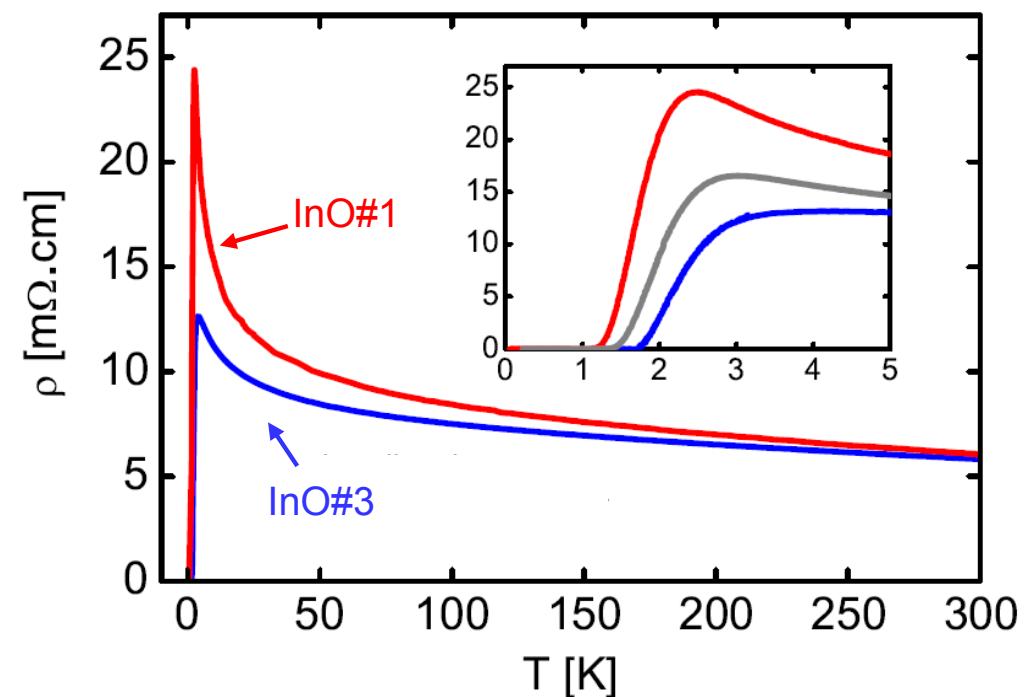
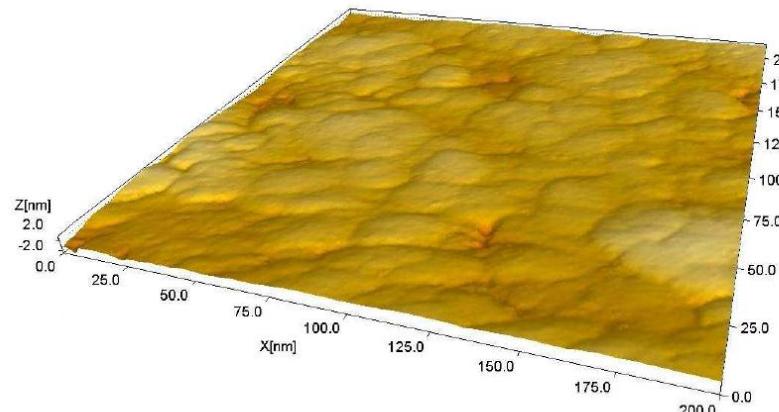
B. Sacépé, et al., Nature Communications (2010)

Amorphous Indium Oxide

Samples: e-gun evaporation of high purity In_2O_3 onto Si/SiO_2 substrate under O_2 pressure

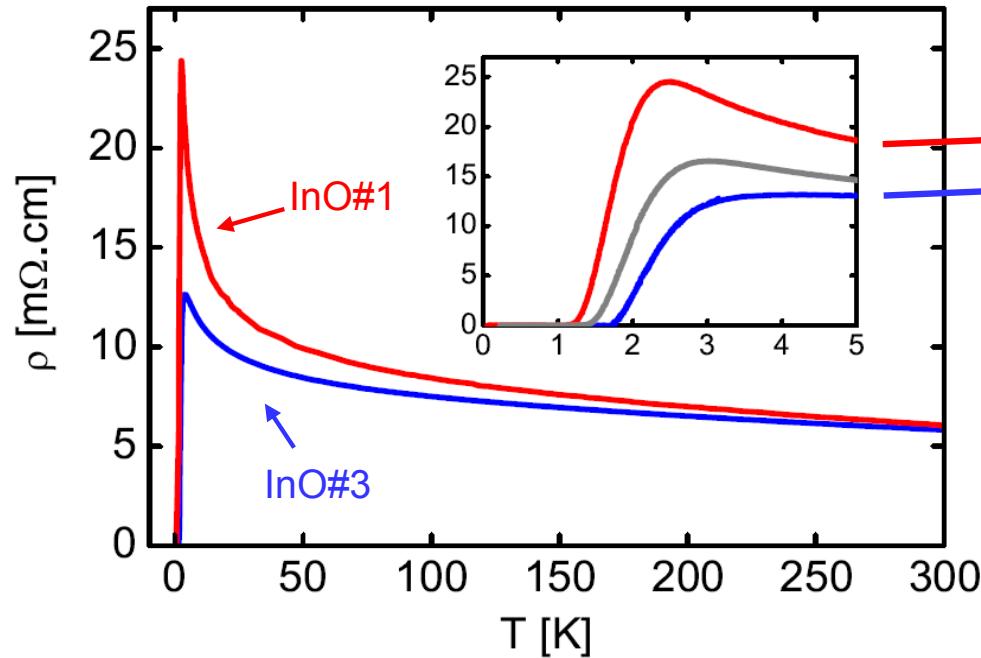
D. Shahar, Weizmann Institute of Science

Thickness: 15 nm (red & grey) and 30 nm (bleu) – 3D regime

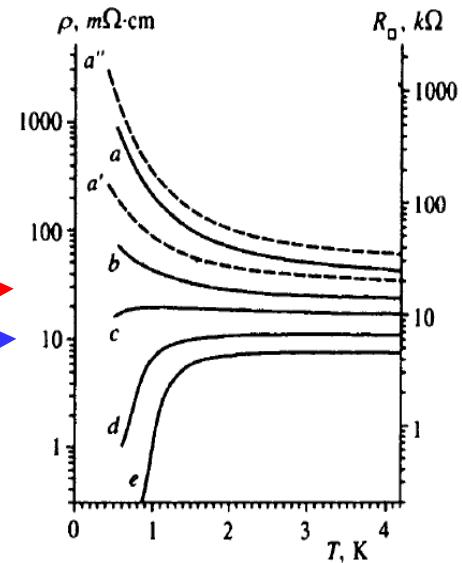


Nearly critical samples

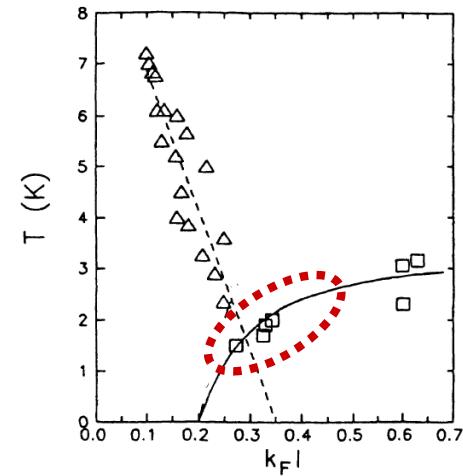
High disorder (red) and low disorder (blue)



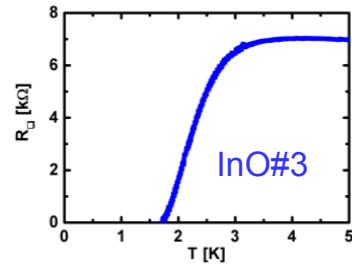
- $k_F l_e \sim 0.4 - 0.5 < 1 \rightarrow$ localized regime (Ioffe-Regel criterion)
- T_c comprised between 1K and 2K
- Carrier density : $N = 3.5 \times 10^{21} \text{ cm}^{-3}$



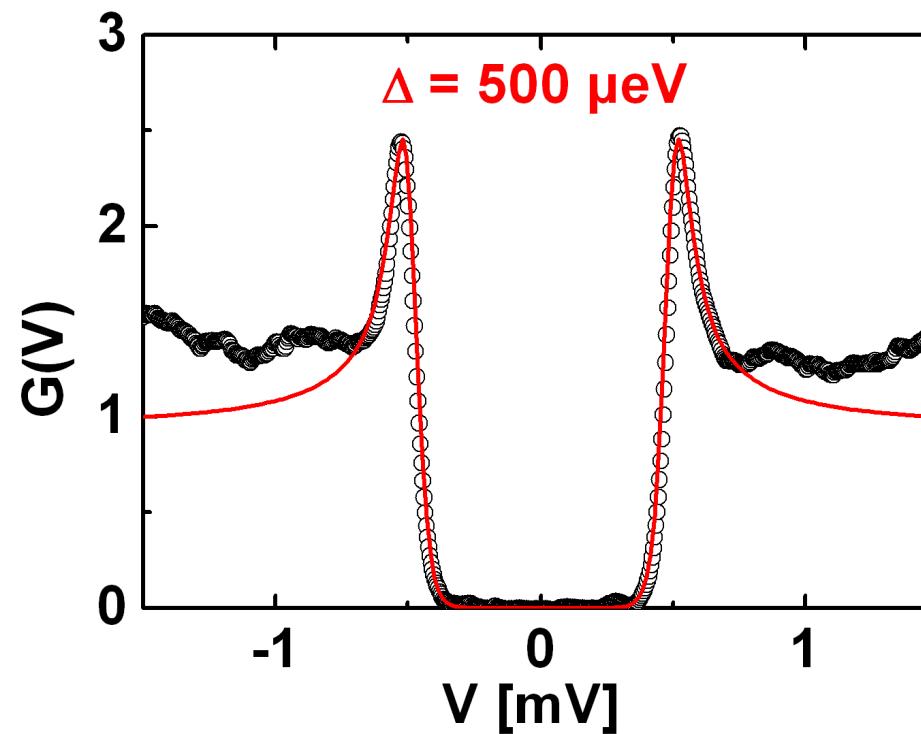
V. F. Gantmakher et al., JETP 82, 951 (1996)



D. Shahar and Z. Ovadyahu, Phys. Rev. B 46, 10917 (1992)



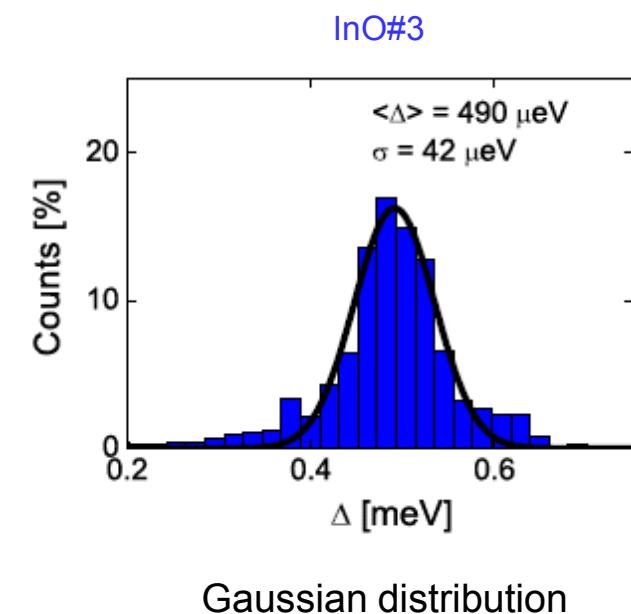
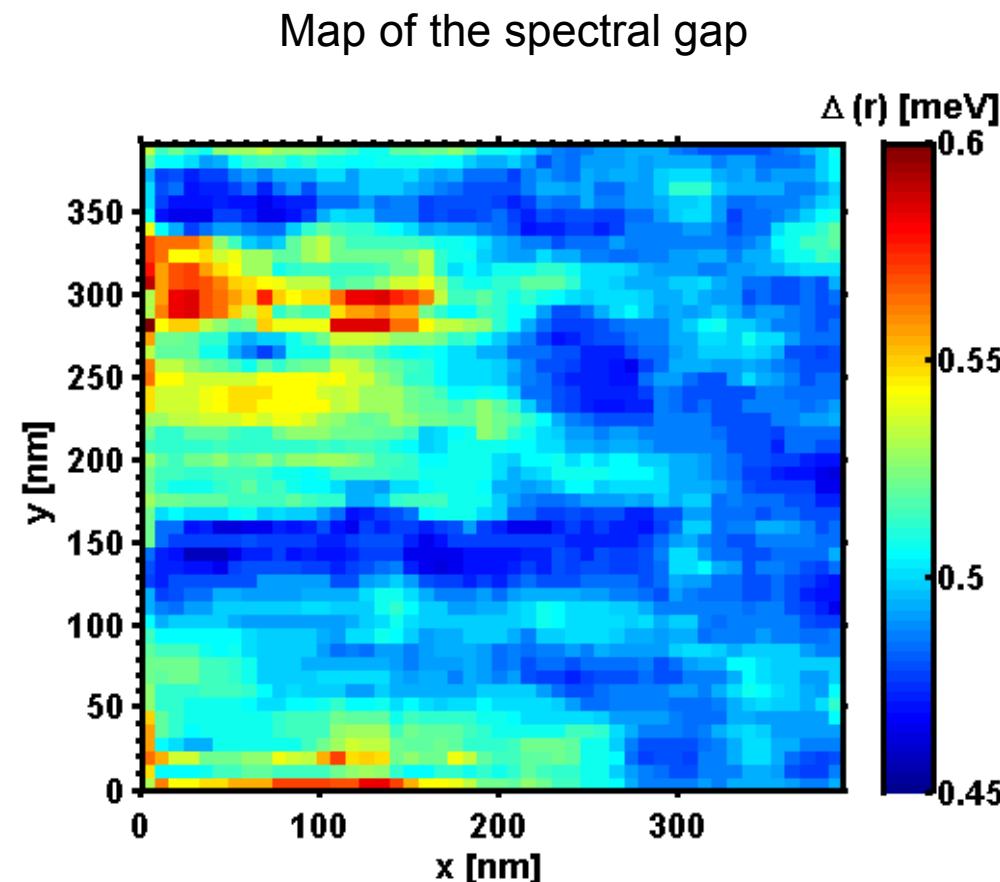
Typical spectrum measured at 50 mK



Fit : s -wave BCS density of states

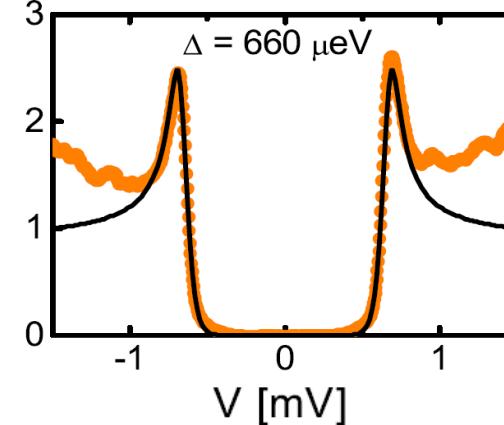
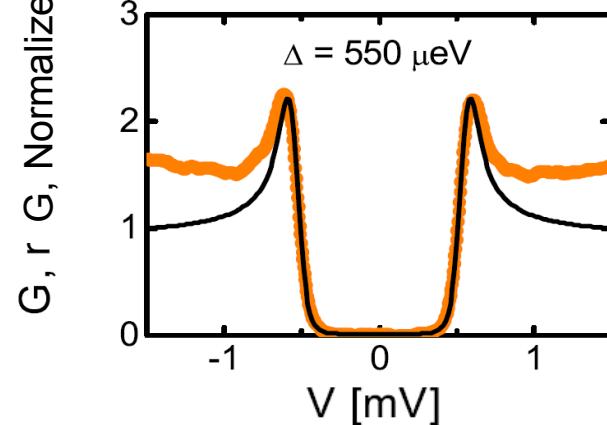
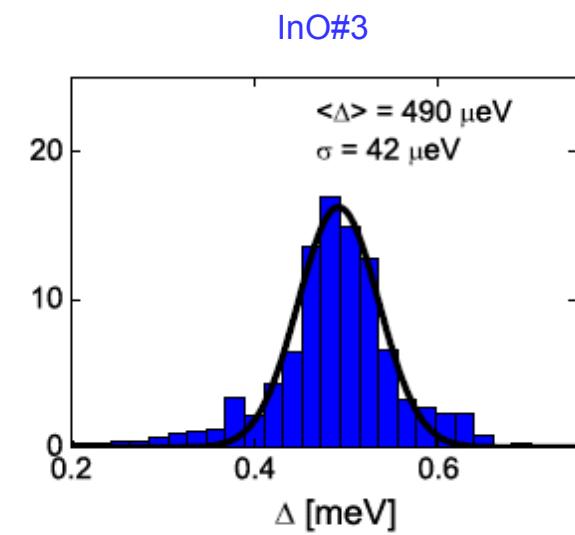
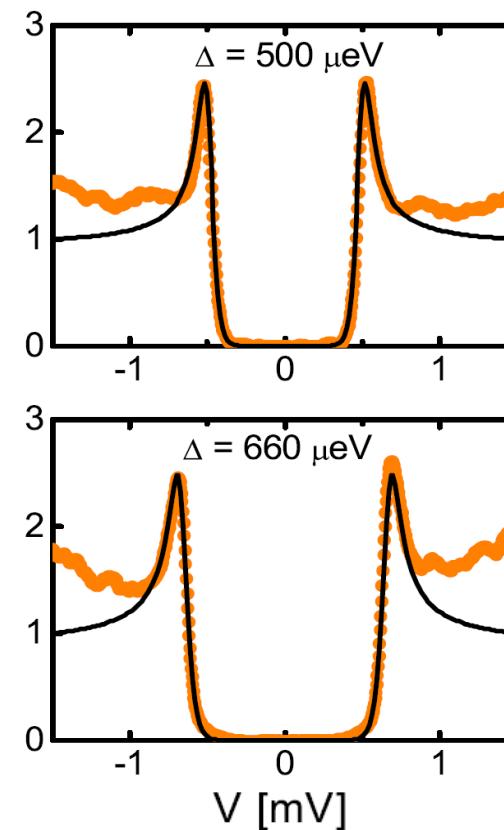
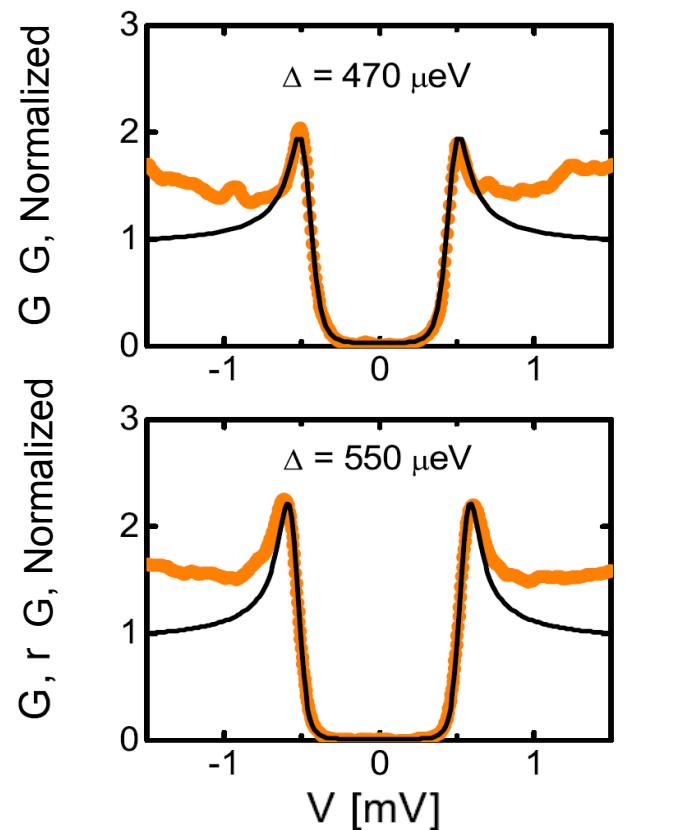
- Absence of quasi-particle excitations at low energies

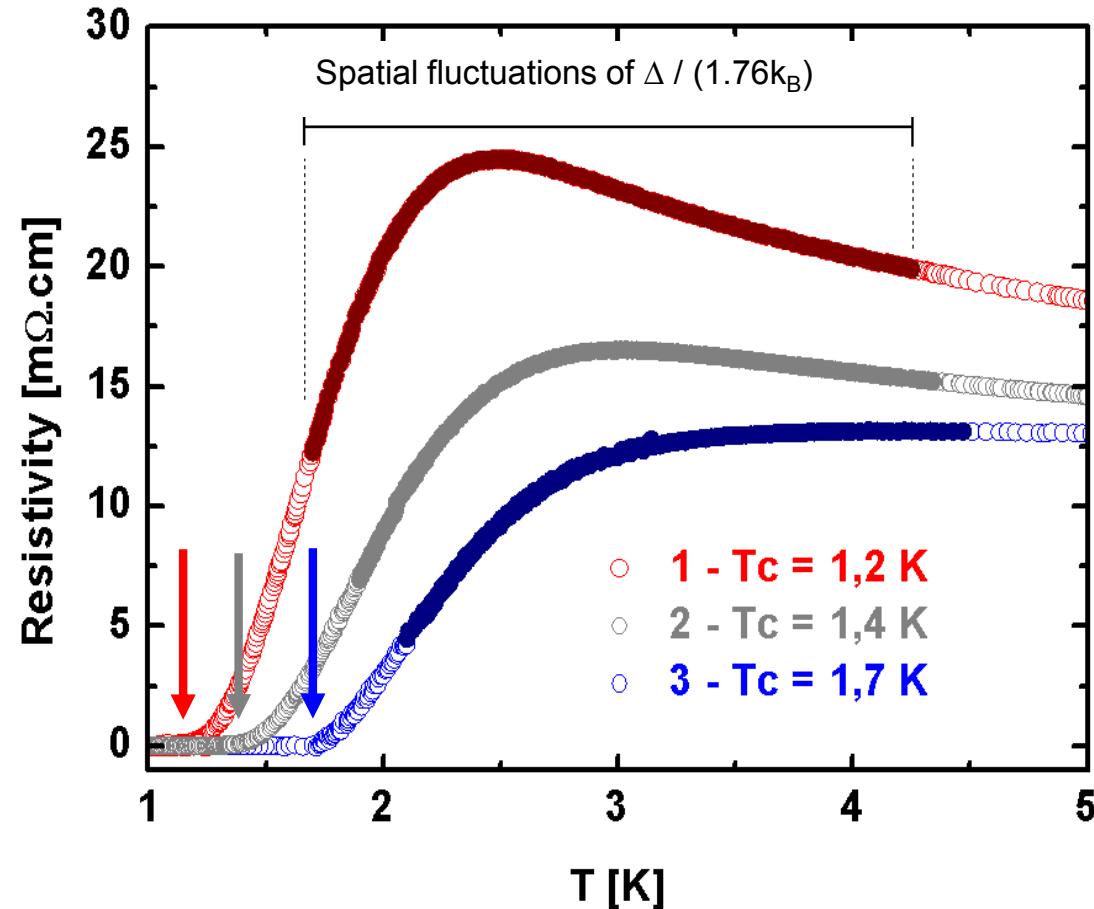
Spatial fluctuations of the spectral gap $\Delta(r)$



Spatial fluctuations of the spectral gap $\Delta(r)$

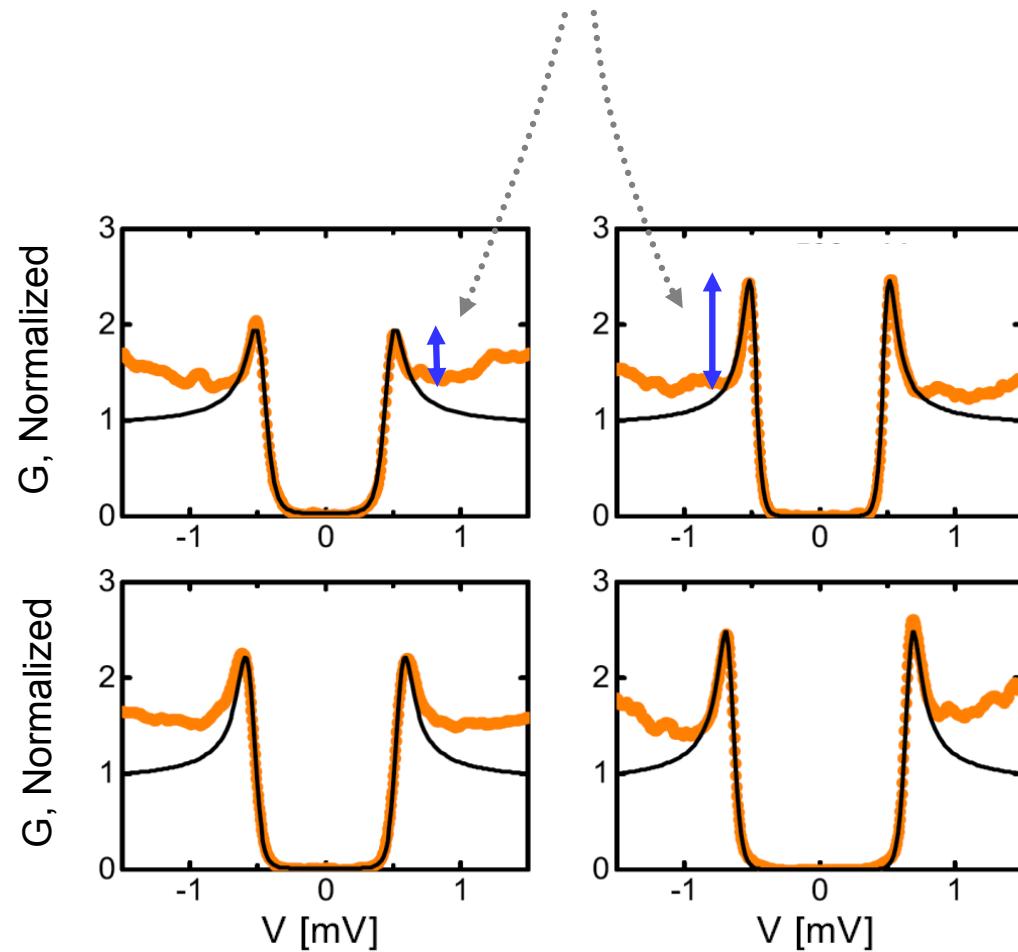
Spectra measured at different locations ($T=50\text{mK}$)



Fluctuations of $\Delta(r)$ and superconducting transition

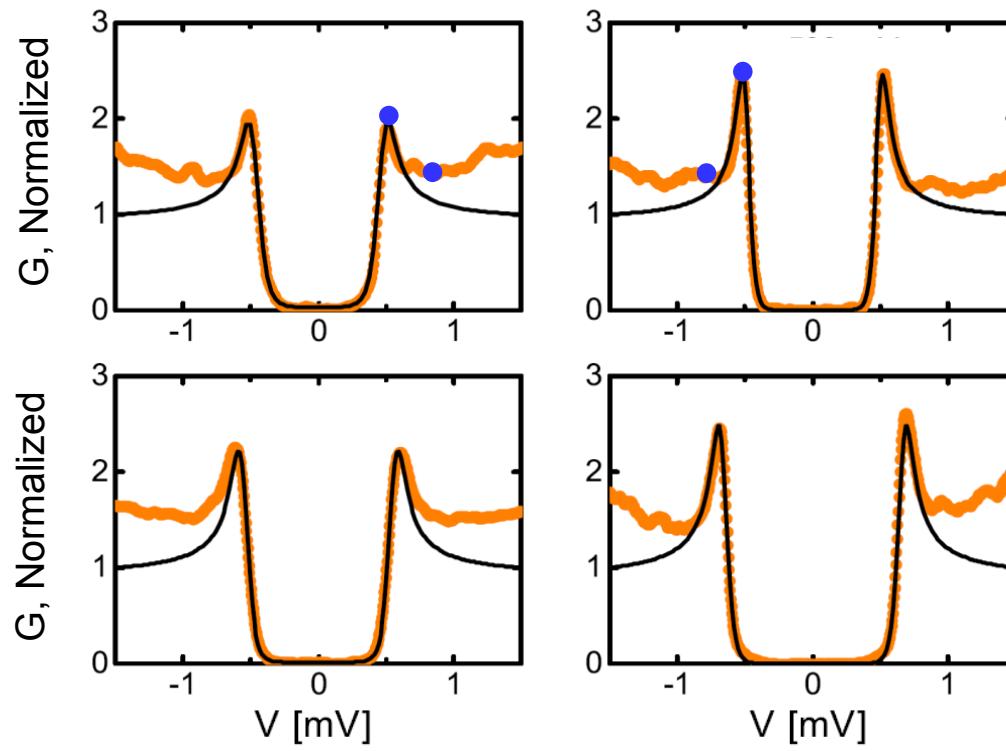
$$3 \leq \frac{\Delta(r)}{k_B T_C} \leq 5.5$$

Spatial fluctuations of the coherence peaks height

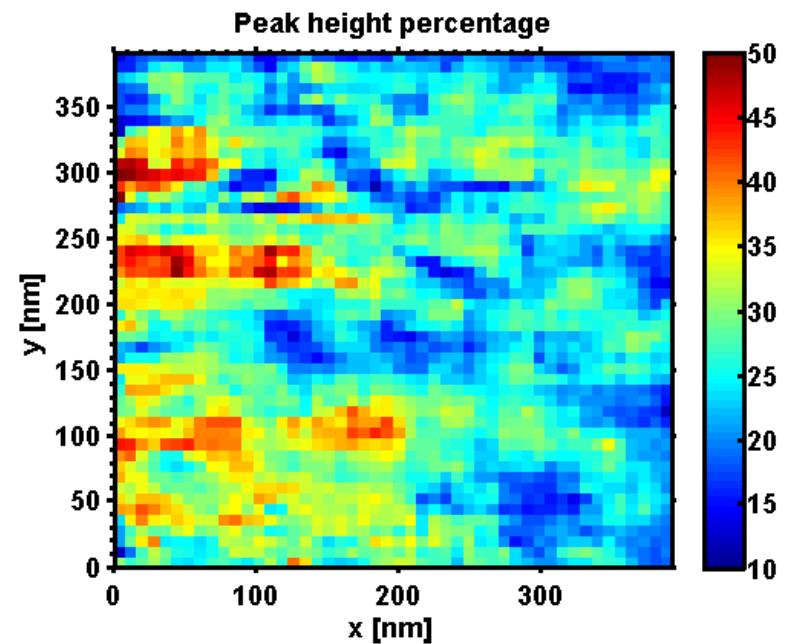


Spatial fluctuations of the coherence peaks height

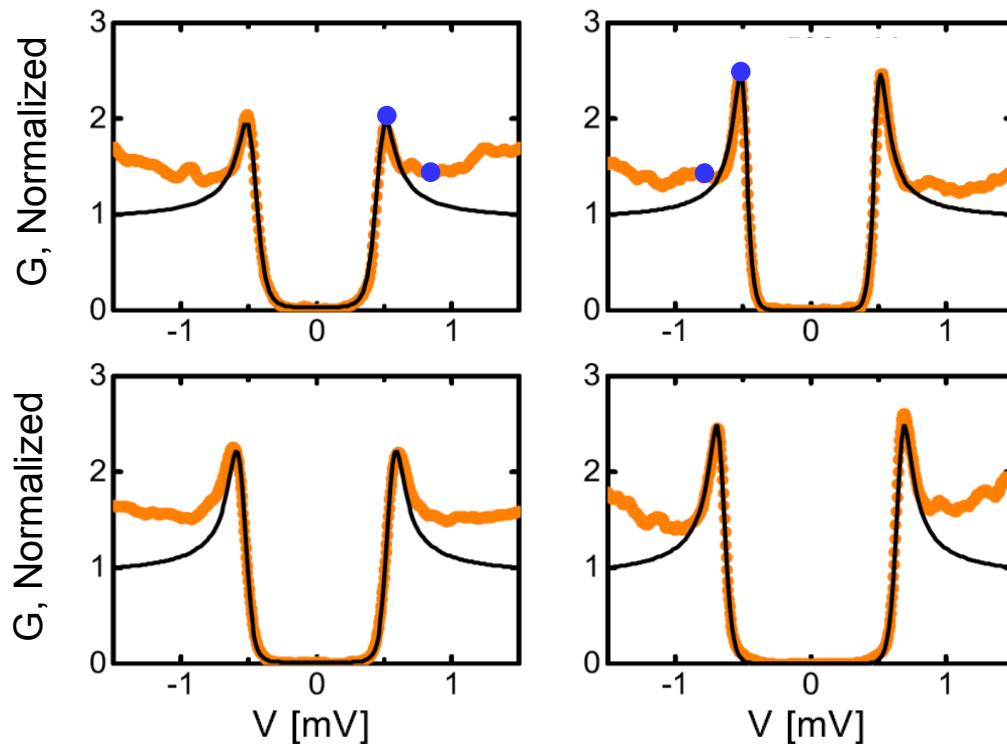
Statistical study



$$R = \frac{G(\Delta) - G(eV > \Delta)}{G(eV > \Delta)}$$



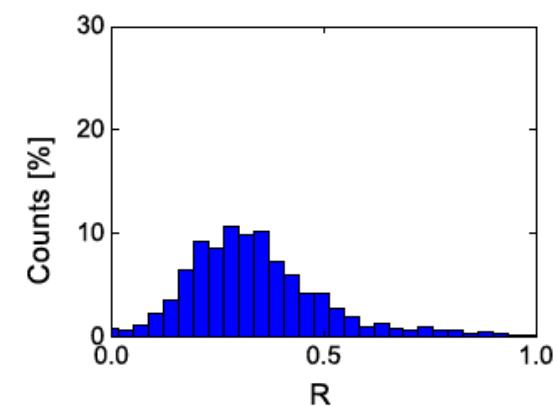
Spatial fluctuations of the coherence peaks height



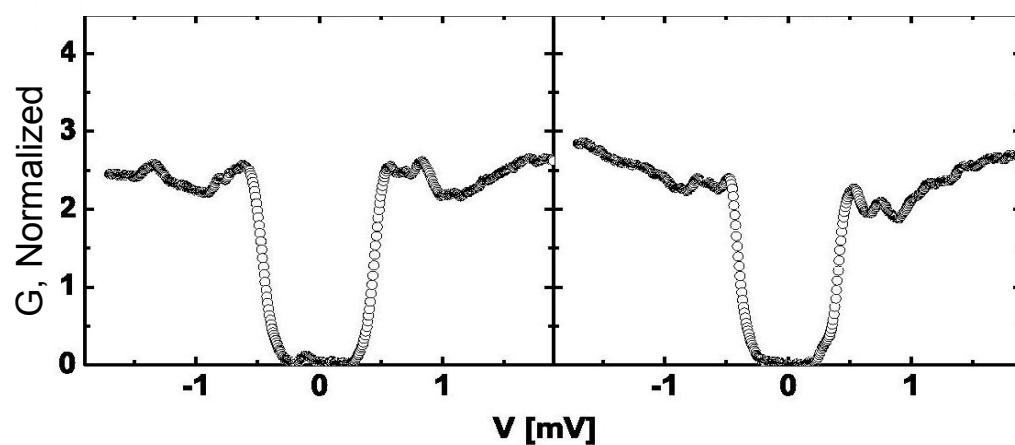
Statistical study

$$R = \frac{G(\Delta) - G(eV > \Delta)}{G(eV > \Delta)}$$

InO#3



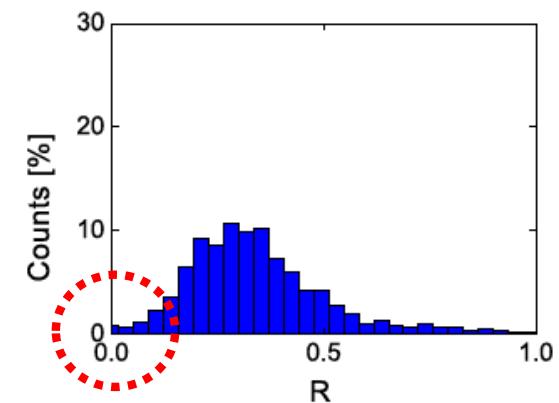
*Full spectral gap
without coherence peaks*



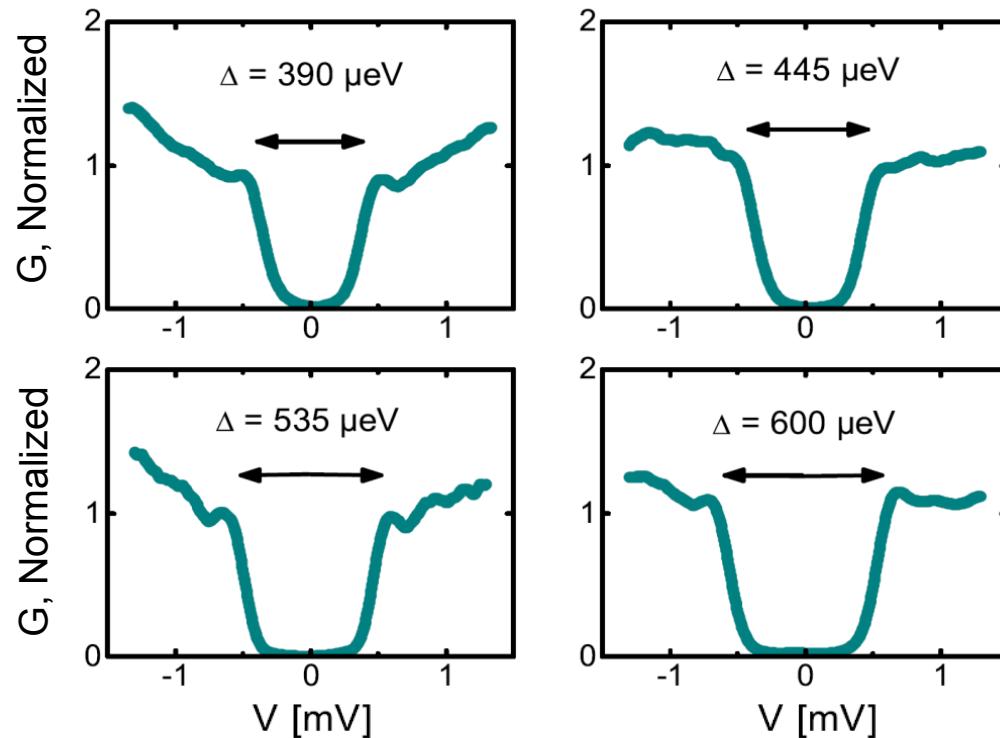
Statistical study

$$R = \frac{G(\Delta) - G(eV > \Delta)}{G(eV > \Delta)}$$

InO#3



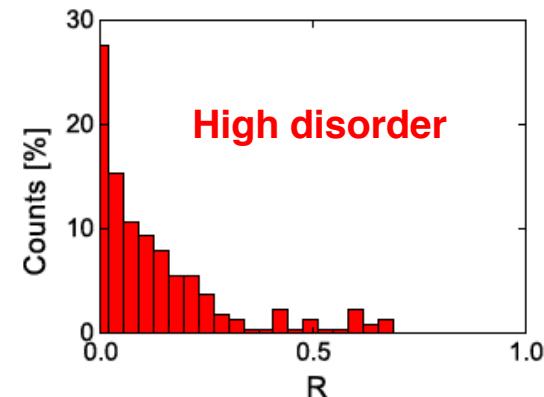
*Full spectral gap
without coherence peaks*



Statistical study

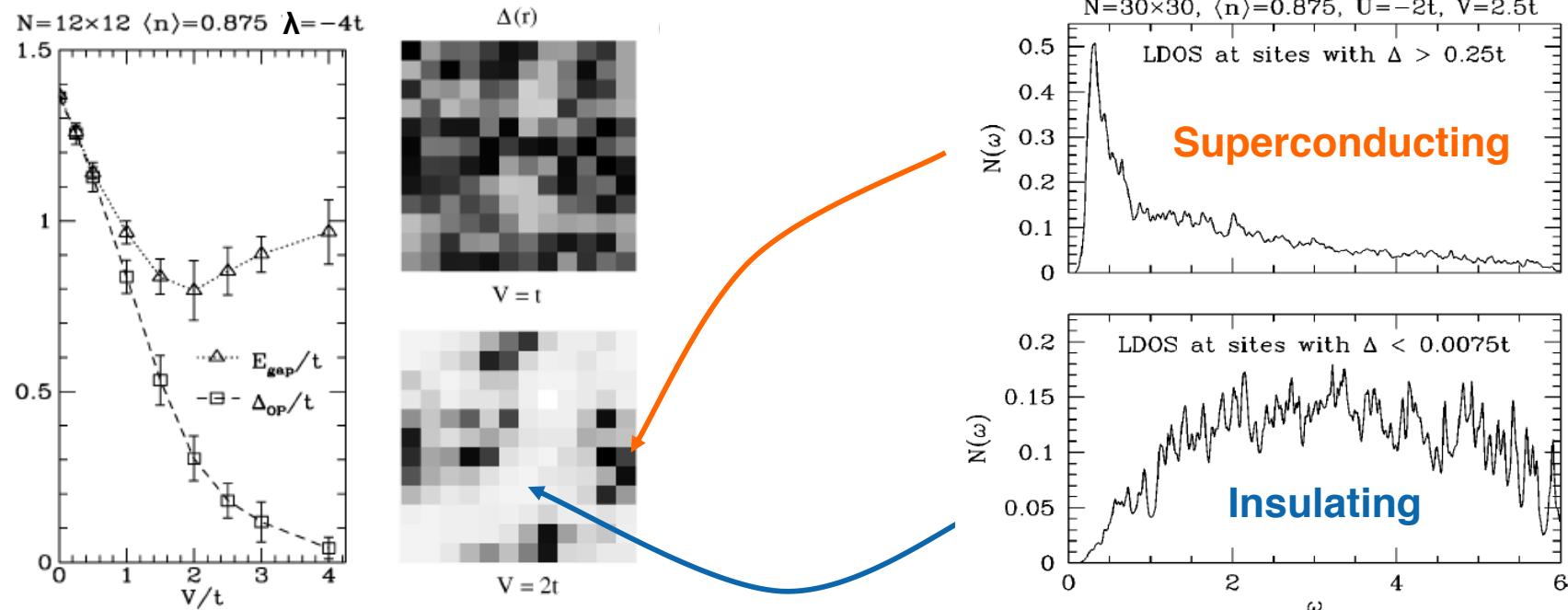
$$R = \frac{G(\Delta) - G(eV > \Delta)}{G(eV > \Delta)}$$

InO#1

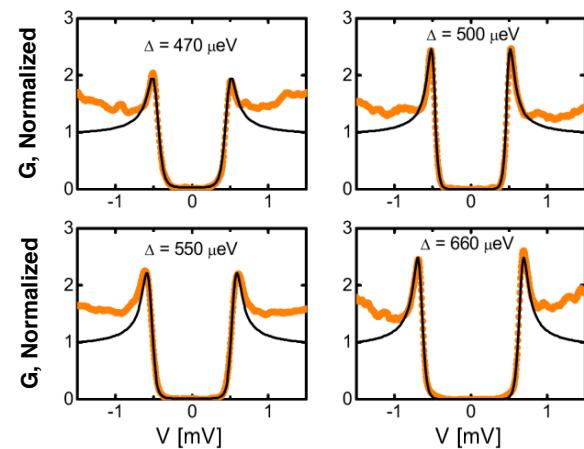


Signature of localized Cooper pairs

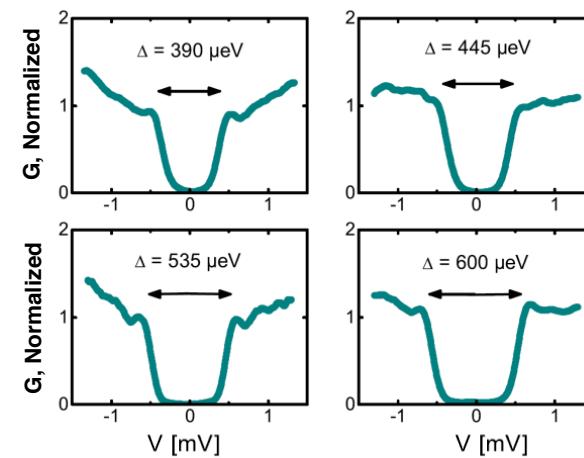
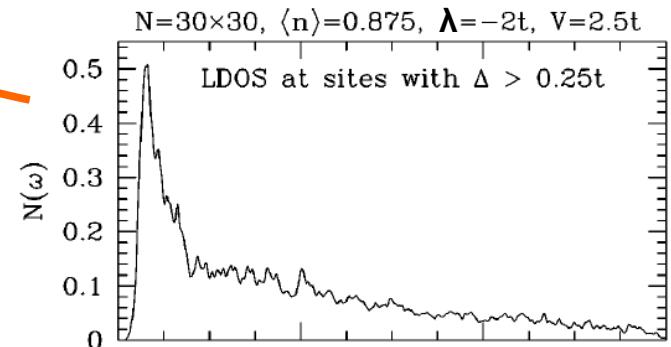
A. Ghosal, M. Randeria, N. Trivedi, *PRL 81*, 3940, (1998) & *PRB 65*, 014501 (2001)



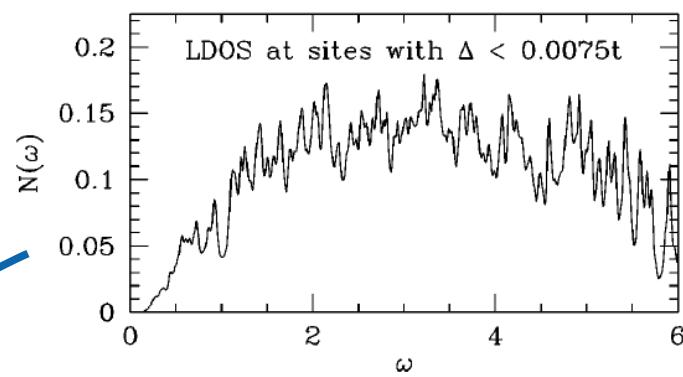
Signature of localized Cooper pairs



Superconducting gap Δ
⇒ delocalized Cooper pairs

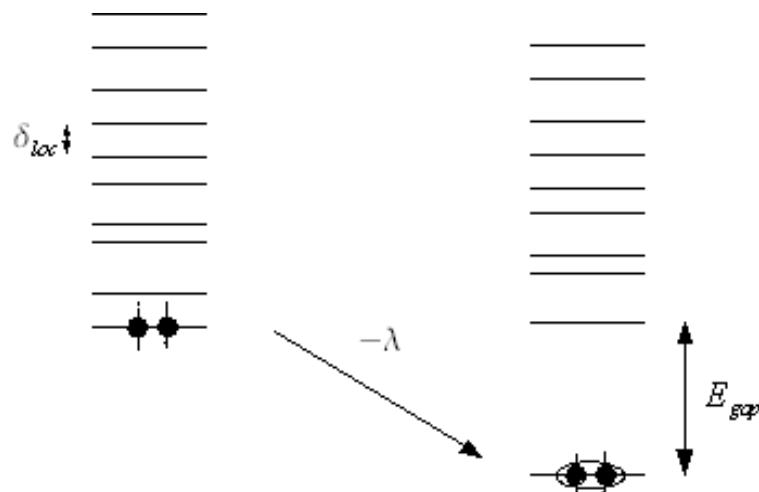
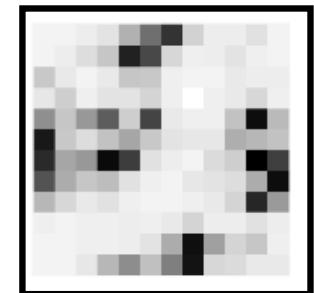


« Insulating » gap E_{gap}
⇒ Localized Cooper pairs



Insulating gap due to Cooper pairing

- P. W. Anderson, *J. Phys. (Paris) Colloq.* 37, C4-339 (1976)
 M. Ma, and P. A. Lee, *PRB* 32, 5658, (1985)
 K. A. Matveev and A. Larkin, *PRL*. 78, 3749, (1997)
 A. Ghosal, et al. *PRL* 81, 3940, (1998) and *PRB* 65, 014501 (2001)
 M. Feigel'man, et al. *PRL* 98, 027001, (2007)
 M. Feigel'man, et al. *Ann. Phys.* 325, 1390 (2010)
 M. Feigel'man, et al. *PRB* 82, 184534 (2010)



In the lowest order: $E_{gap} \sim \lambda \delta_{loc} \square \frac{\lambda}{v \xi_{loc}^3}$

Reduced BCS Hamiltonian built on eigenstates of the Anderson problem

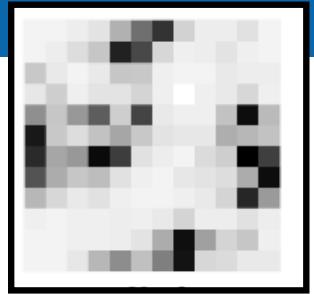
$$H = \sum_{j\sigma} \epsilon_j c_{j\sigma}^\dagger c_{j\sigma} - \frac{\lambda}{\nu_0} \sum_{j,k} M_{jk} c_{j\uparrow}^\dagger c_{j\downarrow}^\dagger c_{k\uparrow} c_{k\downarrow}$$

$$M_{jk} = \int d\mathbf{r} \psi_j^2(\mathbf{r}) \psi_k^2(\mathbf{r}),$$

In the high-disorder regime when $\delta_{loc} > \Delta$

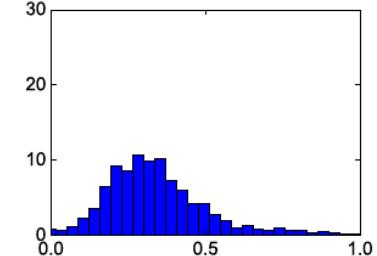
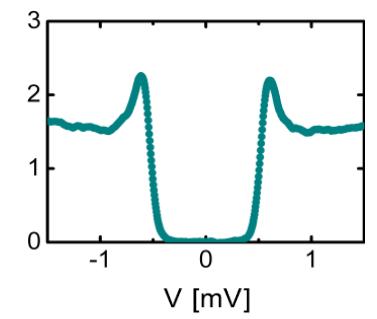
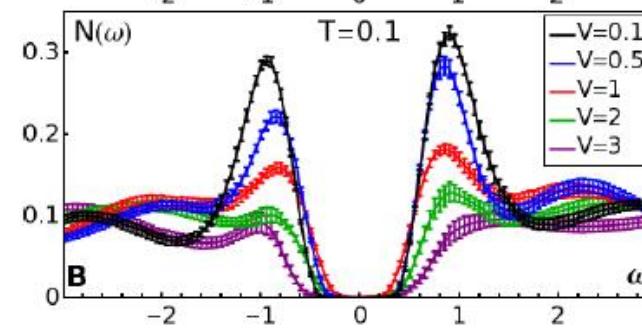
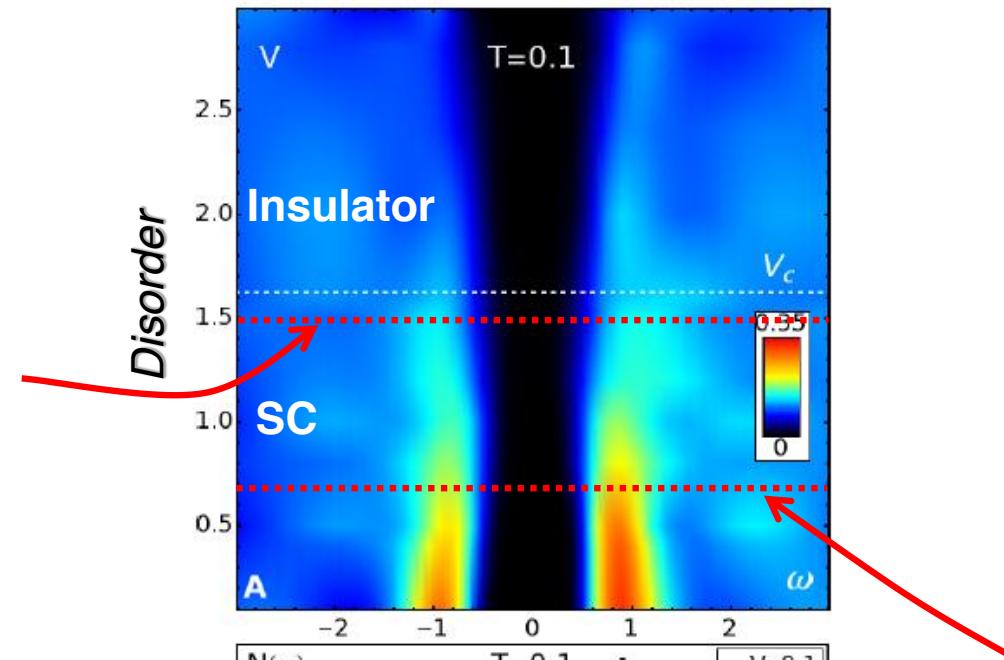
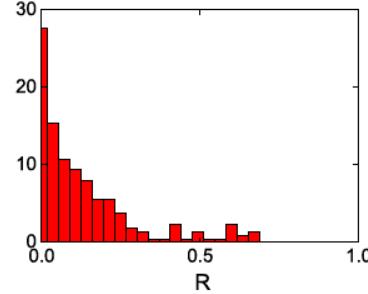
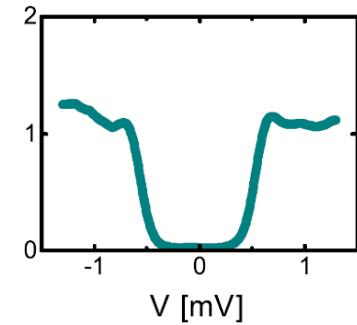
$$M_{jk} \approx \delta_{jk} \int dr \psi_j^4(r) \approx \delta_{jk} \frac{1}{\xi_{loc}^3}$$

Insulating gap due to Cooper pairing



BdG + Quantum Monte Carlo simulations

K. Bouadim, Y. Loh, M. Randeria, N. Trivedi, *Nature Physics* (2011)

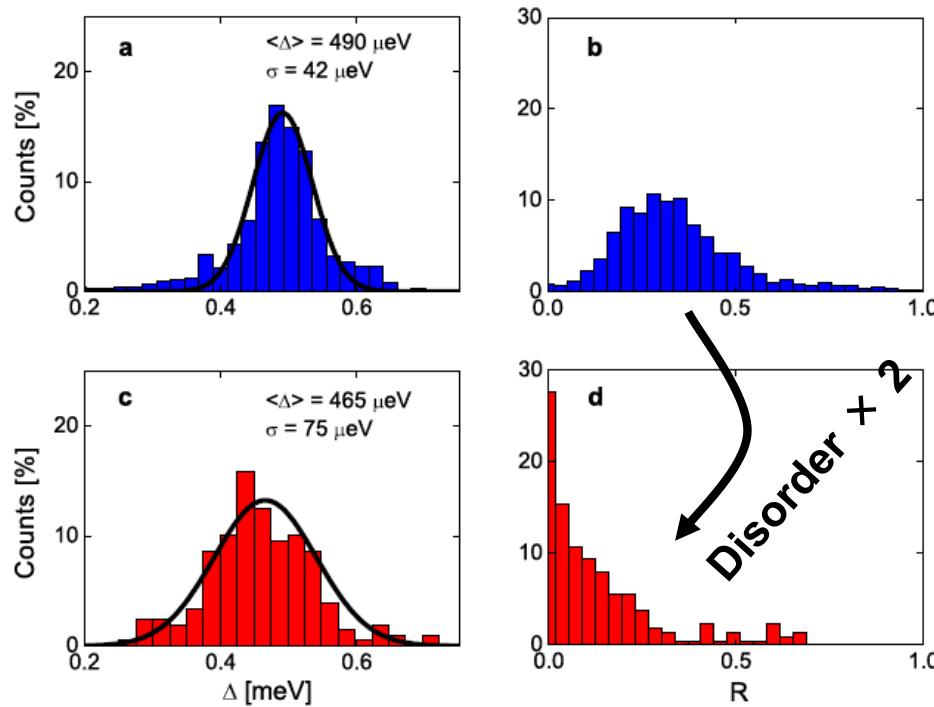


Superconductivity near the mobility edge

M. Feigel'man, et al., *PRL* ('07)

M. Feigel'man, et al, *Ann. Phys.* ('10)

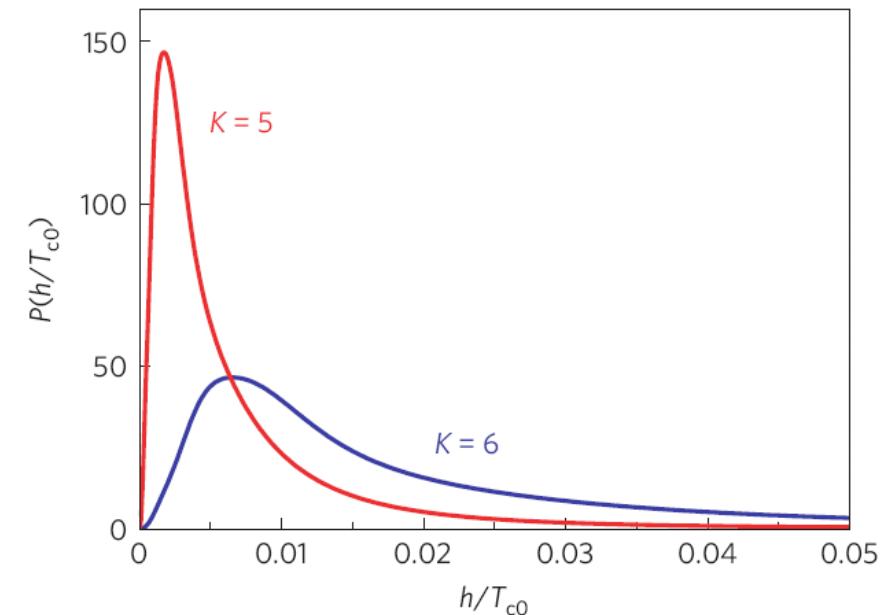
M. Feigel'man, et al, *PRB* ('10)



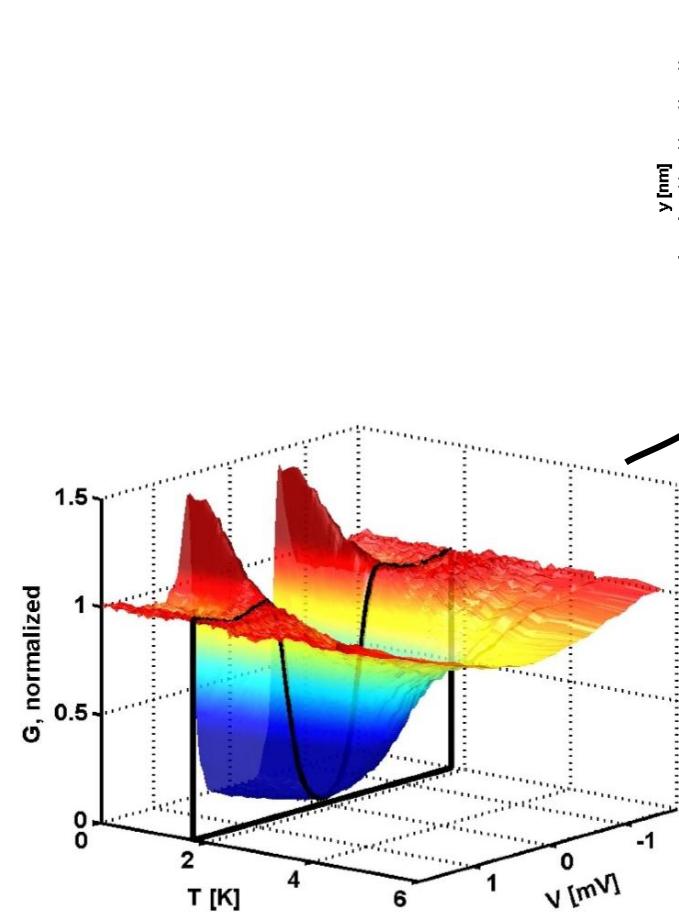
- **Proliferation of localized « Cooper »-pairs
when approaching the SIT**

Simulations on the Bethe lattice

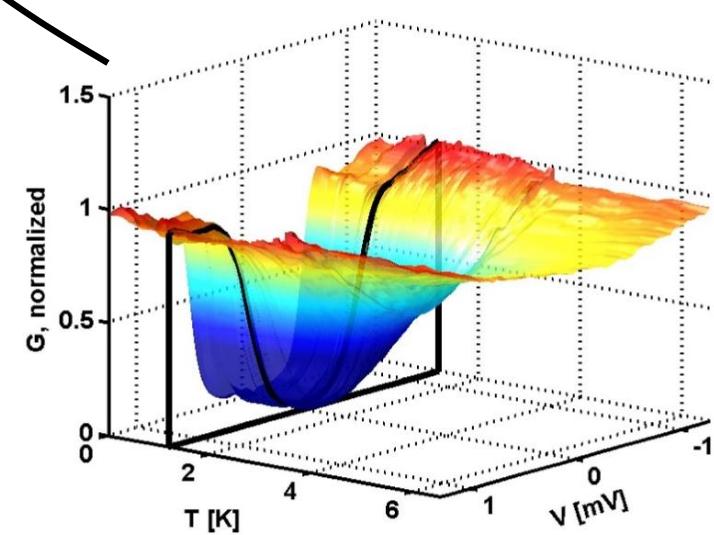
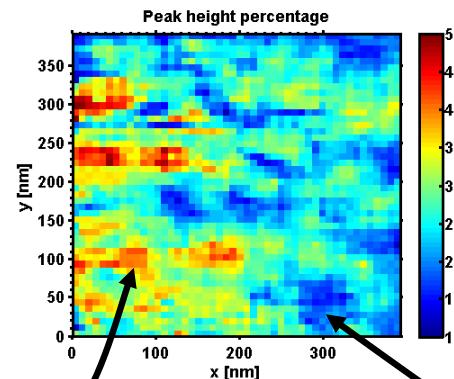
Lev Ioffe, Misha Feigel'man



Self-induced inhomogeneities

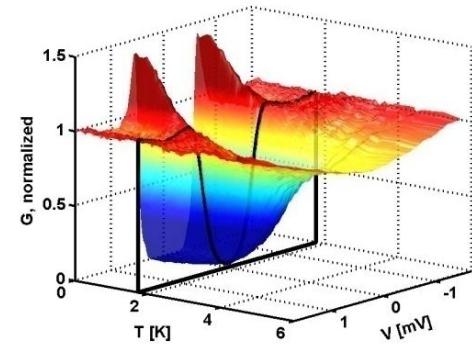


Condensation of preformed Cooper-pairs

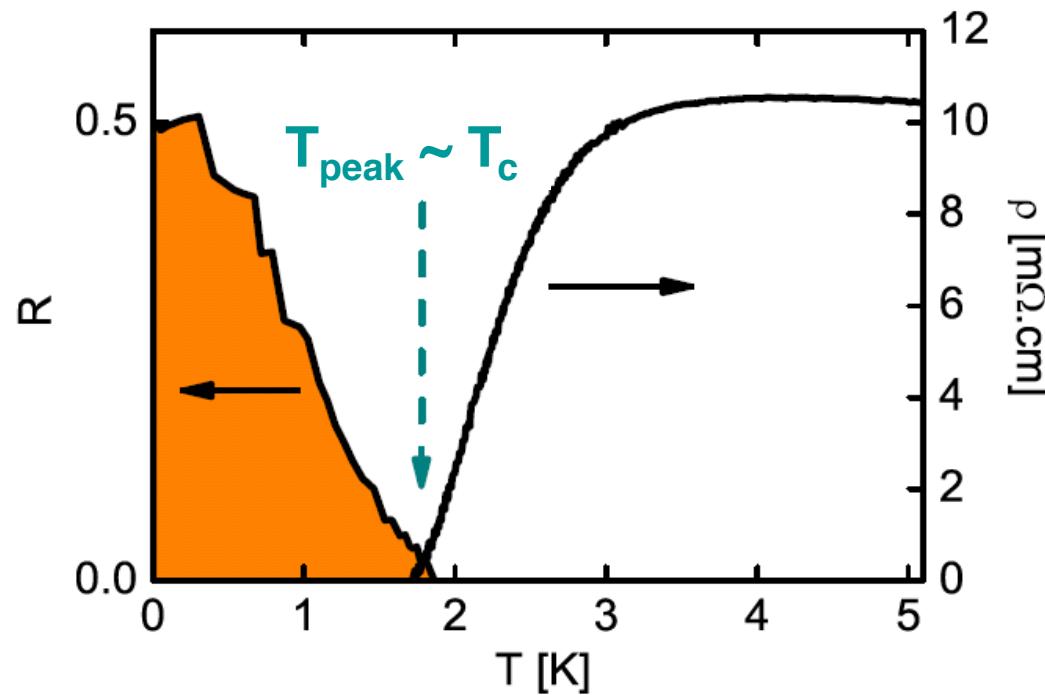


Localization of preformed Cooper-pairs

Definition of T_c

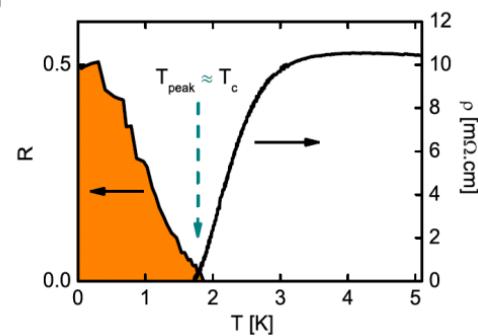


*Macroscopic quantum phase coherence
probed at a local scale*

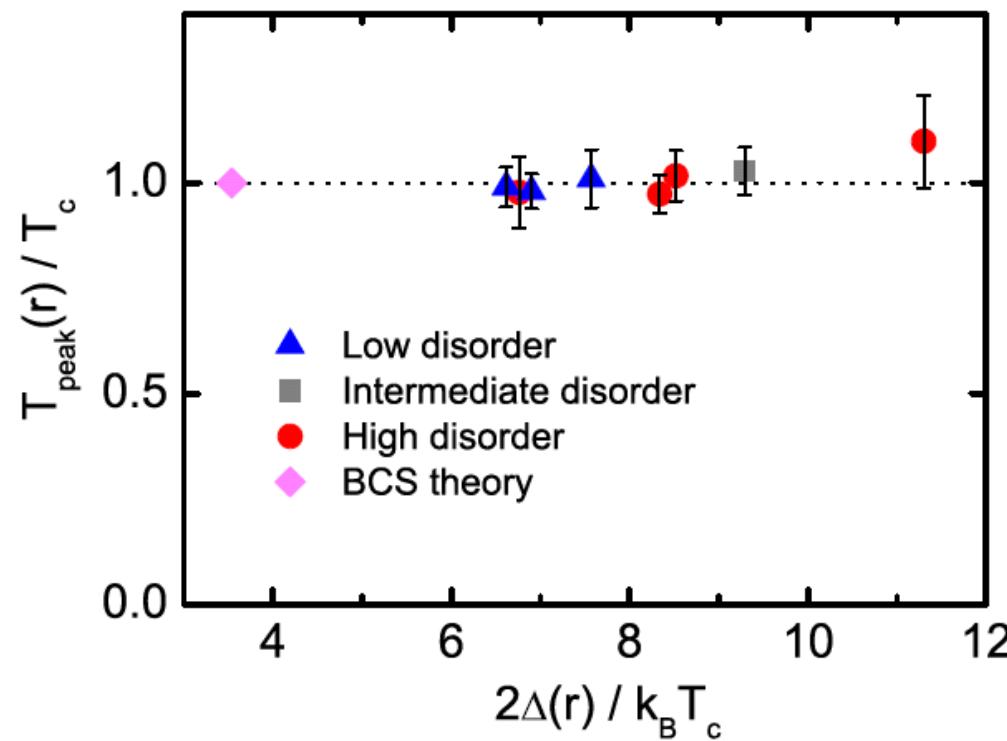


- BCS peaks appear along with superconducting phase coherence

Definition of T_c



*Macroscopic quantum phase coherence
probed at a local scale*



- BCS peaks appear along with superconducting phase coherence

Superconductivity beyond the mobility edge

M. Feigel'man *et al.*, *Phys. Rev. Lett.* **98**, 027001, (2007)

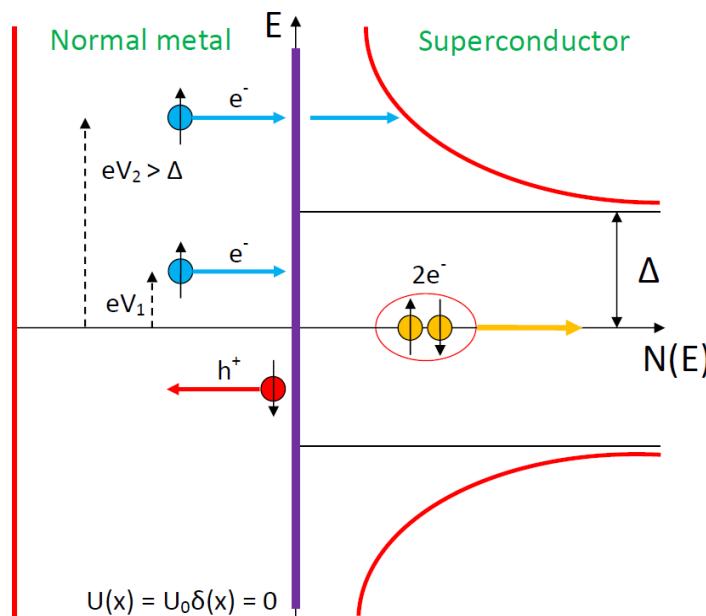
M. Feigel'man *et al.*, *Ann. Phys.* **325**, 1390 (2010)

BCS model built on fractal eigenfunctions of the Anderson problem

$$\Rightarrow E_{\text{gap}} = \Delta_p + \Delta_{\text{BCS}}$$

- Δ_p “parity gap”: pairing of 2 electrons in localized wave functions
- Δ_{BCS} “BCS gap”: long-range SC order between localized pairs

How to measure the SC order parameter ?



Superconductivity beyond the mobility edge

M. Feigel'man *et al.*, *Phys. Rev. Lett.* **98**, 027001, (2007)

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How to measure the SC order parameter ?

- Tunneling spectroscopy
(single-particle DOS)

Tunnel barrier

- Point-contact spectroscopy
(Andreev reflection = transfer of pairs)

Transparent interface

$$E_{\text{gap}} = \Delta_p + \Delta_{\text{BCS}}$$

“parity gap” 

“BCS gap” 

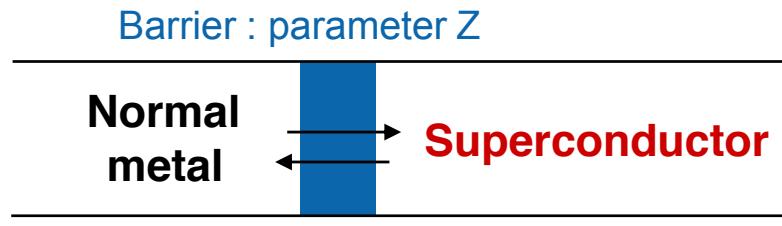
$$\cancel{E_{\text{gap}} = \Delta_p + \Delta_{\text{BCS}}}$$

“BCS gap” 

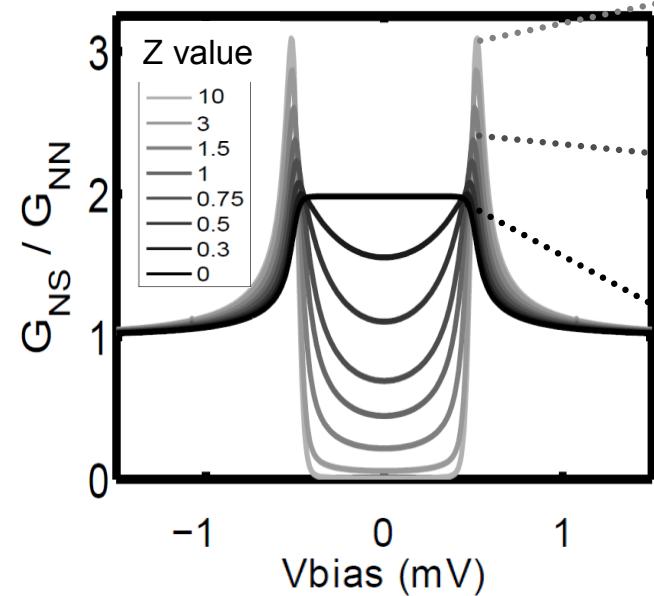
Point-Contact Andreev Spectroscopy

Conductance of a N/S contact

Blonder, G. E., Tinkham, M., and Klapwijk T.M. *Phys. Rev. B* **25**, 7 4515 (1982)



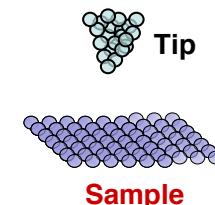
Transmission : $T = 1 / (1 + Z^2)$



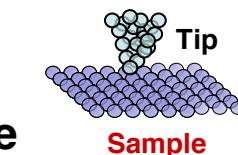
- Single-particle transfer $\sim T$
- Two-particles transfer $\sim T^2$

Tunnel regime

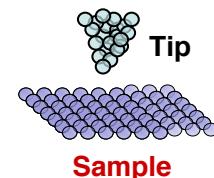
$$Z \gg 1$$



Contact regime



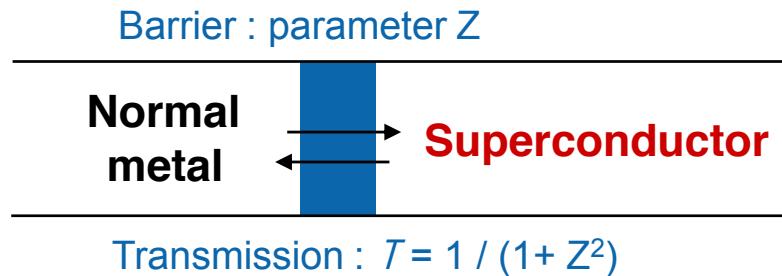
$$Z \sim 1$$



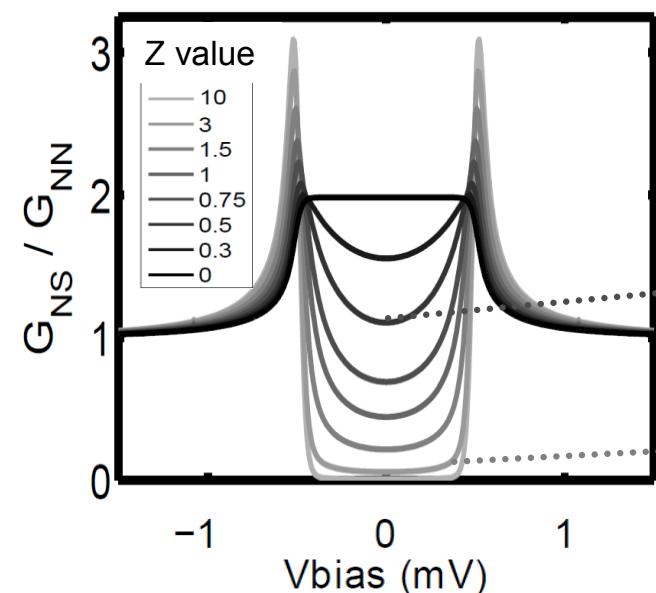
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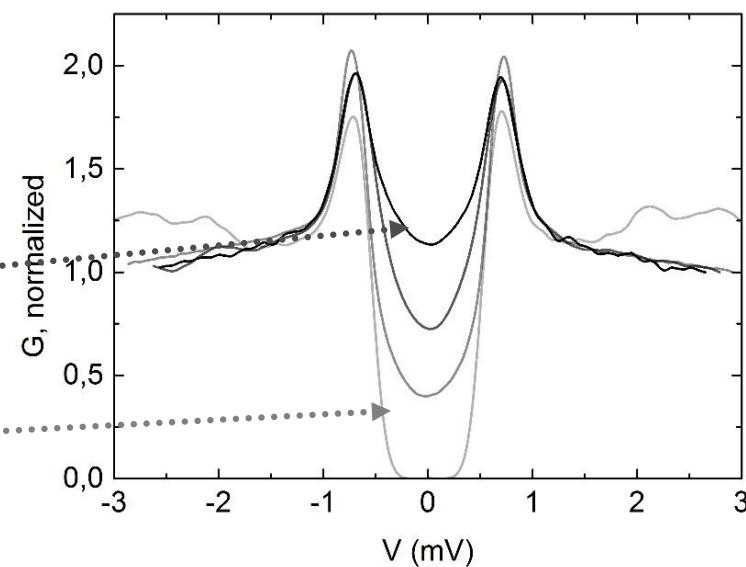
Blonder, G. E., Tinkham, M., and Klapwijk T.M. *Phys. Rev. B* **25**, 7 4515 (1982)

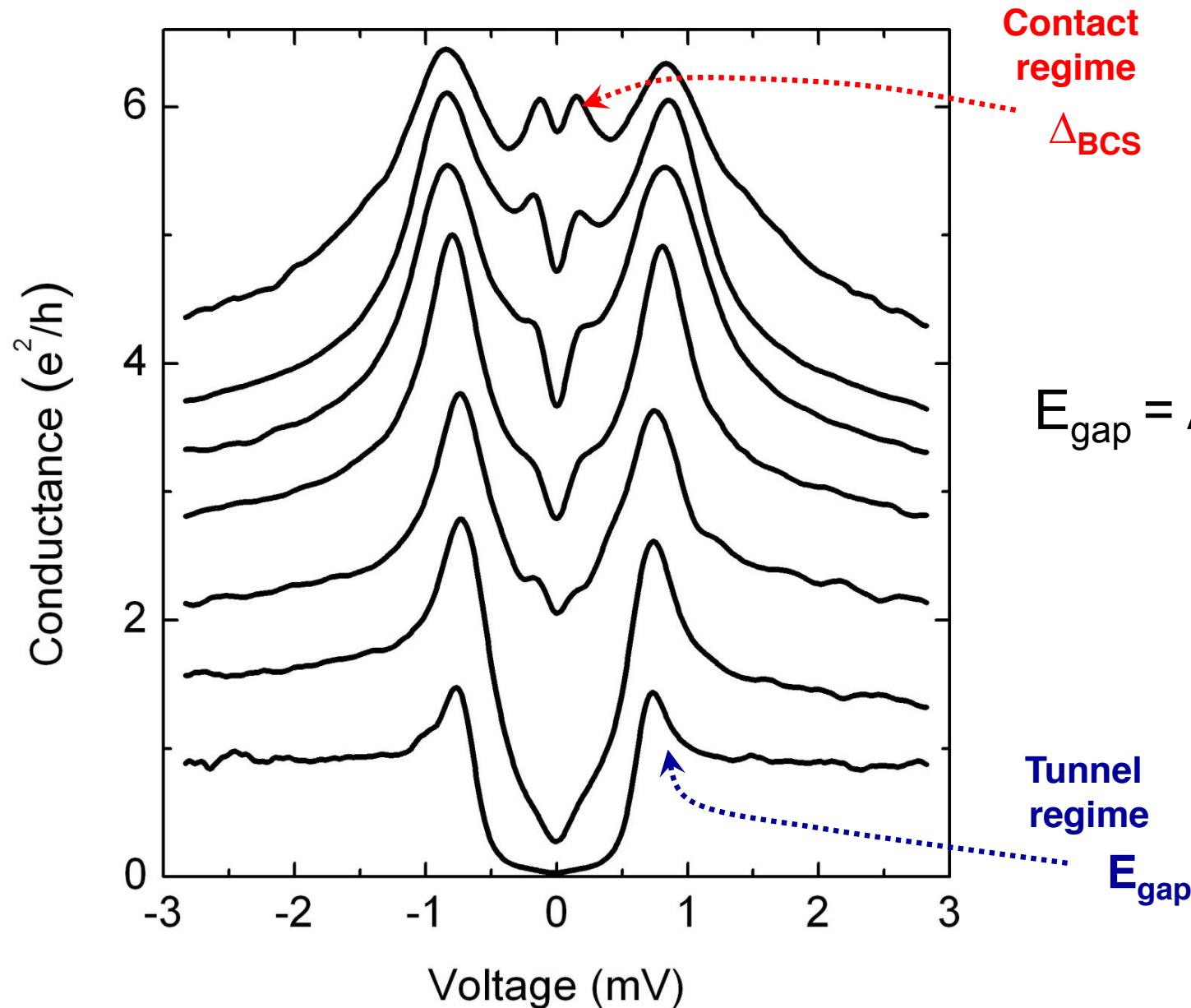


- Single-particle transfer $\sim T$
- Two-particles transfer $\sim T^2$

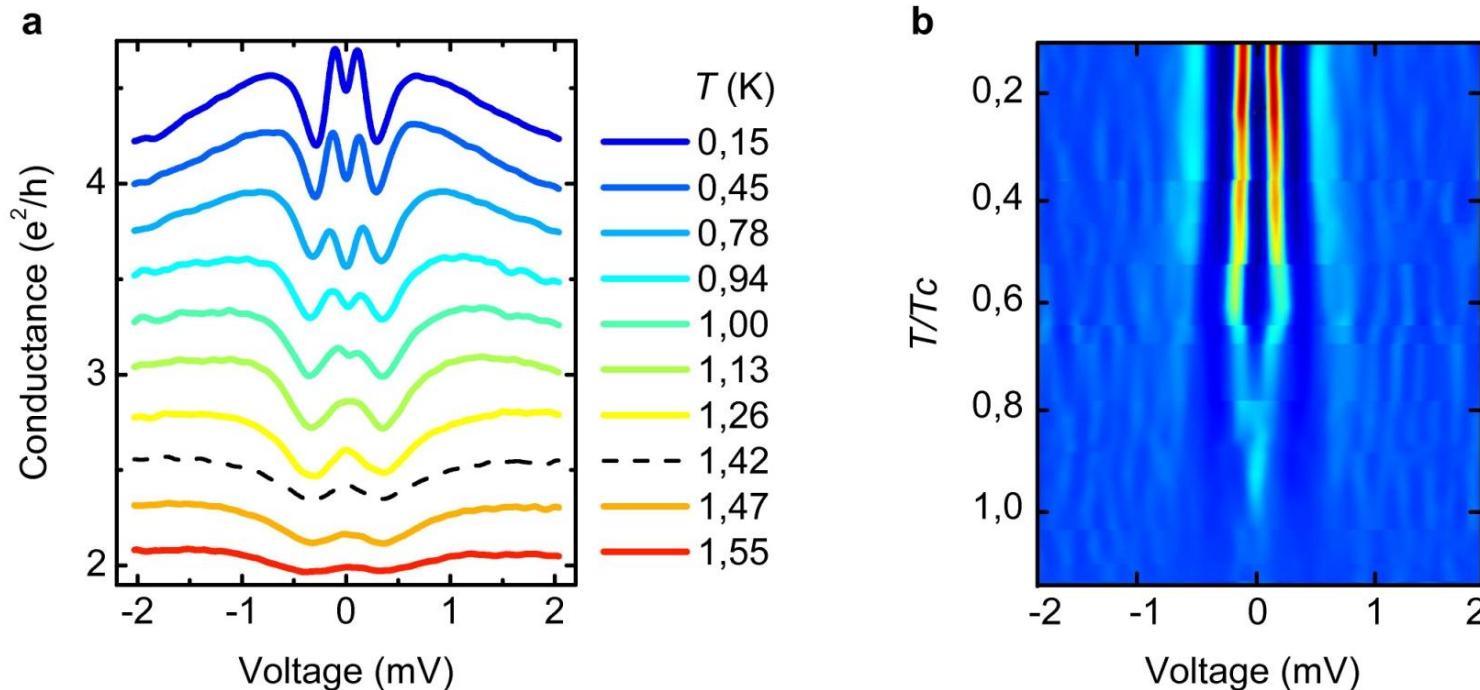


**Point contact spectroscopy on InOx
Far from SIT ($R = 600\Omega$, $T_c = 3K$)**



From tunnel to contact in a-InOx

T-evolution of Andreev signal

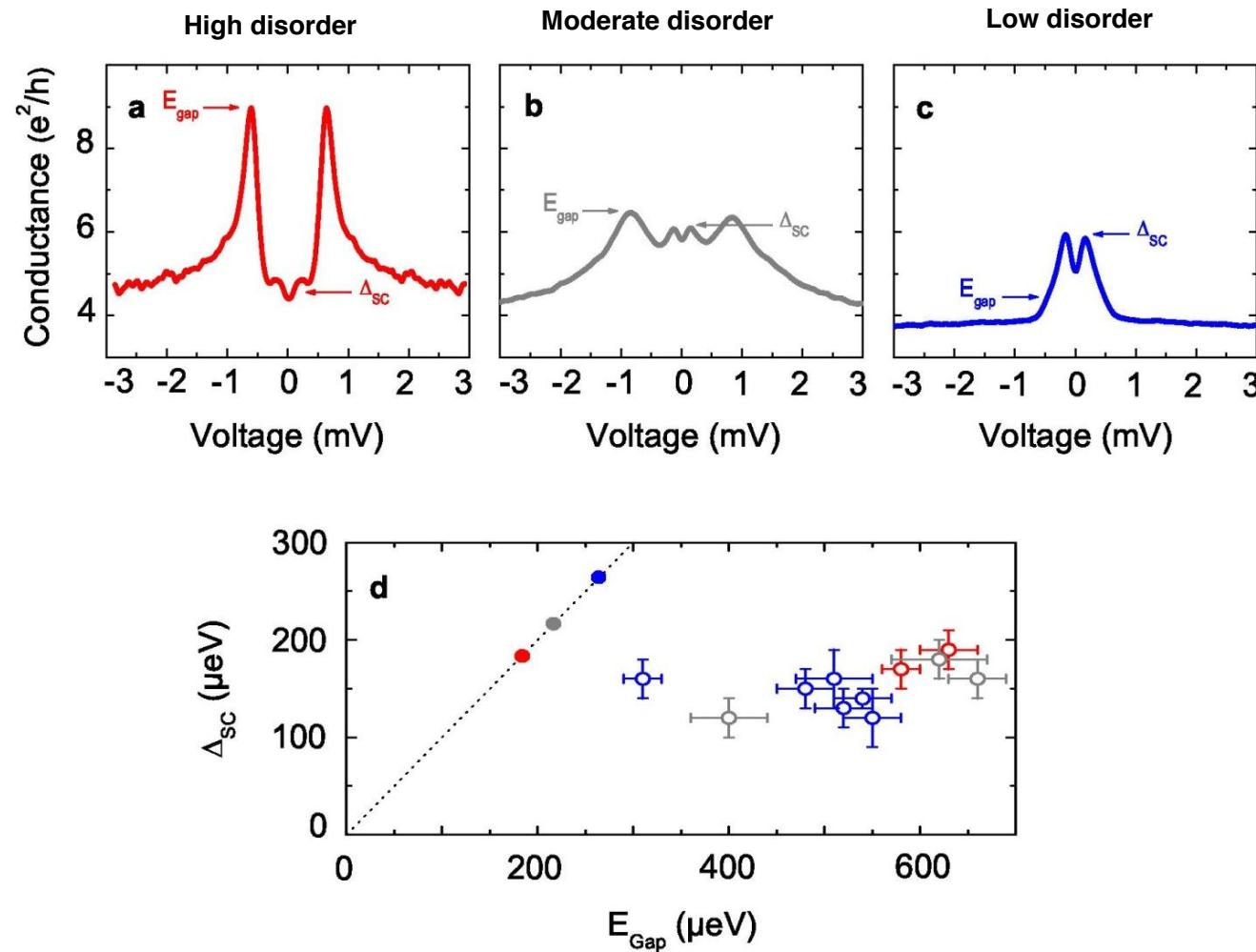


$$E_{\text{gap}}(T) = \Delta_p + \Delta_{\text{BCS}}(T)$$

- E_{gap} evolves between 0 and $\sim 3\text{-}4 T_c$
- Δ_{BCS} evolves between 0 and $\sim T_c$

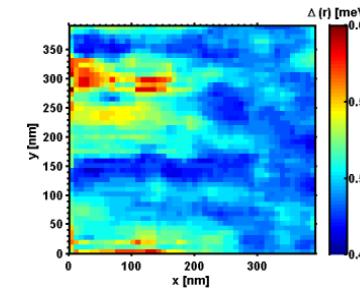
➤ E_{gap} and Δ_{BCS} evolve on distinct temperature range
 ➤ Δ_{BCS} : local signature of SC phase coherence

Disorder-dependence of Andreev signal

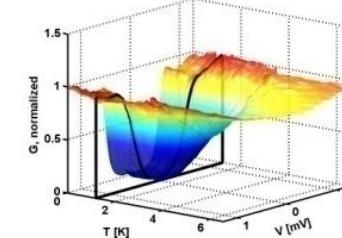
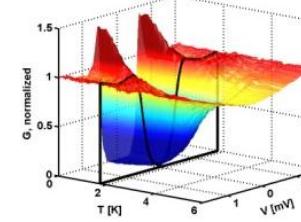


Conclusion : Fluctuation and localization of preformed Cooper pairs in InO_x

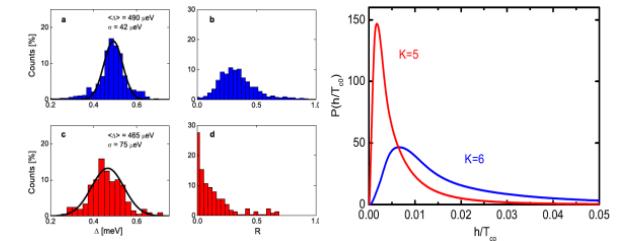
- Inhomogeneous superconducting state at $T < T_c$



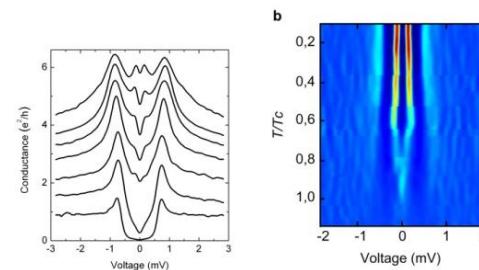
- Preformed Cooper-Pairs above T_c



- The lack of coherence peaks at $T \ll T_c$ is the signature of localization



- SIT occurs through the localization of Cooper-pairs



- Distinct energy scales for pairing and coherence