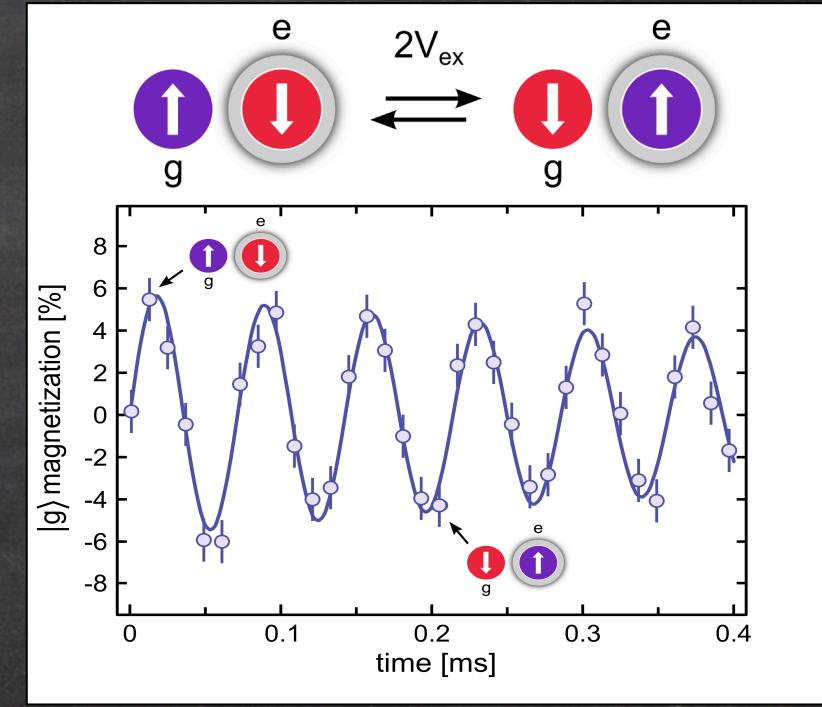
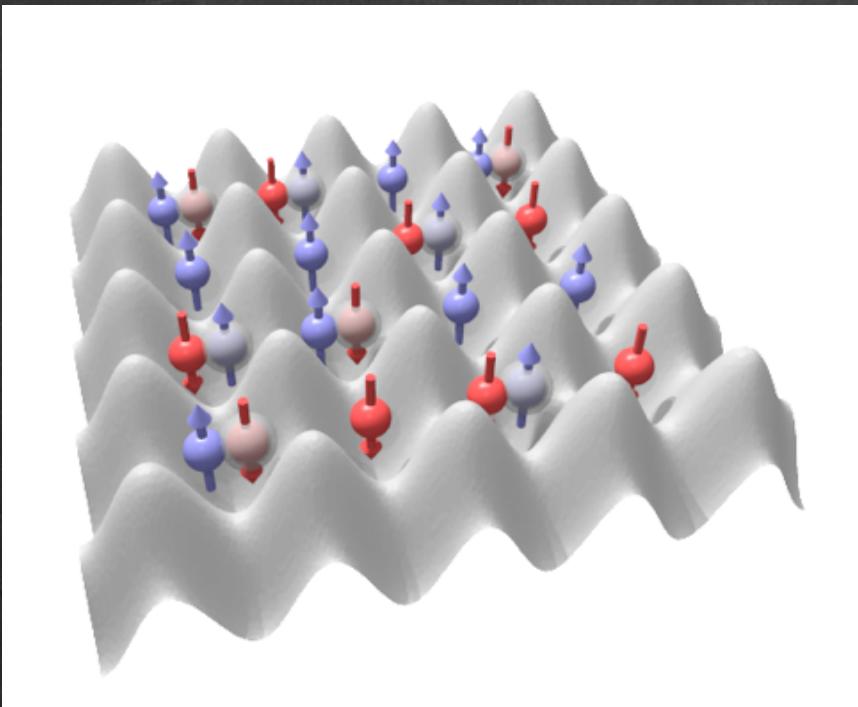


# Orbital magnetism with SU(N) fermions

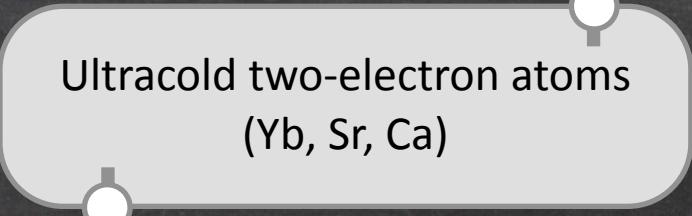
ESX 2014, Trieste, 29<sup>th</sup> October 2014



# Two-electron atoms

---

A valuable atomic platform for quantum science and technology



Ultracold two-electron atoms  
(Yb, Sr, Ca)



A valuable atomic platform for quantum science and technology

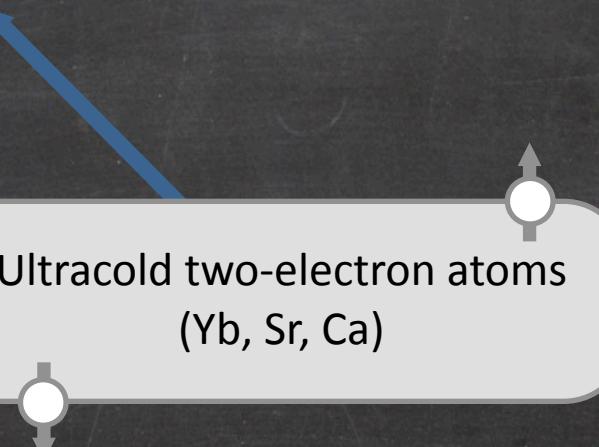
Metrology, optical clocks

B. J. Bloom et al., Nature (2014)

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New quantum simulation:  
 $SU(N)$  physics, gauge fields, ...

M. Cazalilla et al., NJP (2009)  
A. Gorshkov et al., Nat. Phys. (2010)  
D. Banerjee et al., PRL (2013)

Quantum information

A. J. Daley, Quantum Inf. Proc.. (2011)

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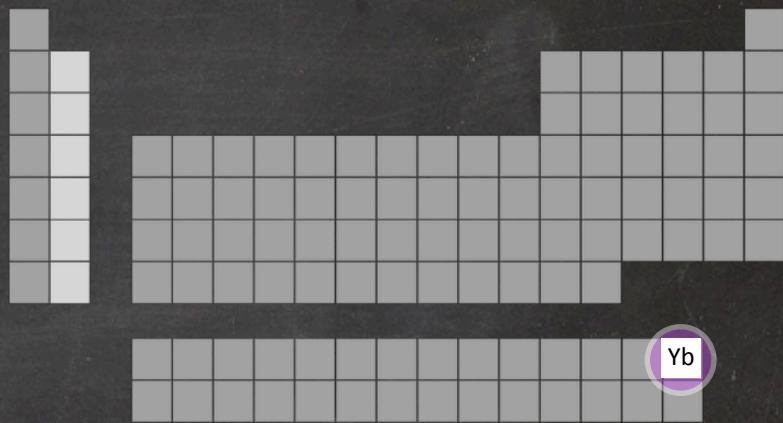
Quantum information

A. J. Daley, Quantum Inf. Proc.. (2011)

# Ytterbium

---

Alkaline-earth-like structure  
Electronic configuration [...]6s<sup>2</sup>



# Ytterbium

---

Alkaline-earth-like structure

Electronic configuration [...]6s<sup>2</sup>

$^1P_1$  —

$^3P_2$  —

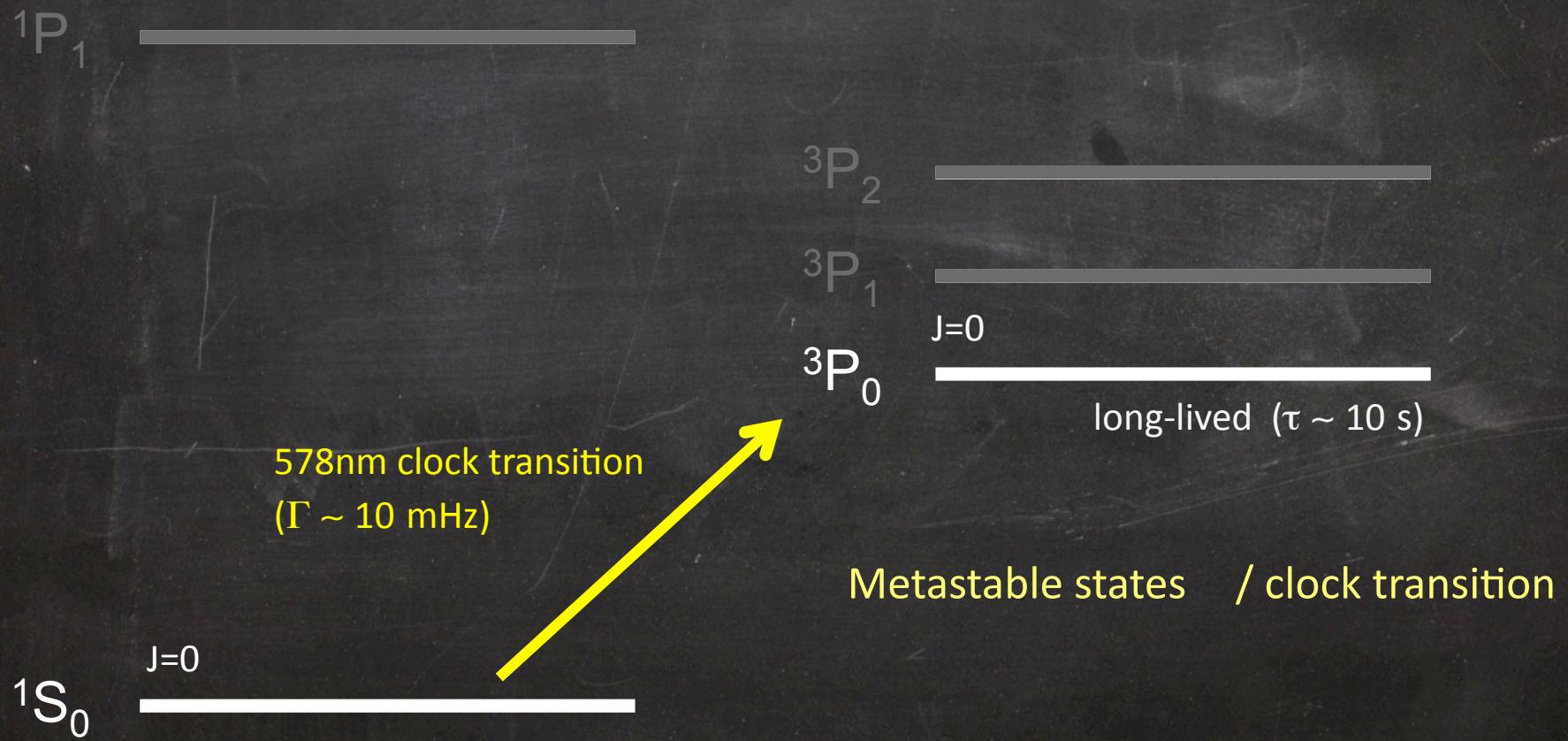
$^3P_1$  —

$^3P_0$  —

$^1S_0$  —

# Ytterbium

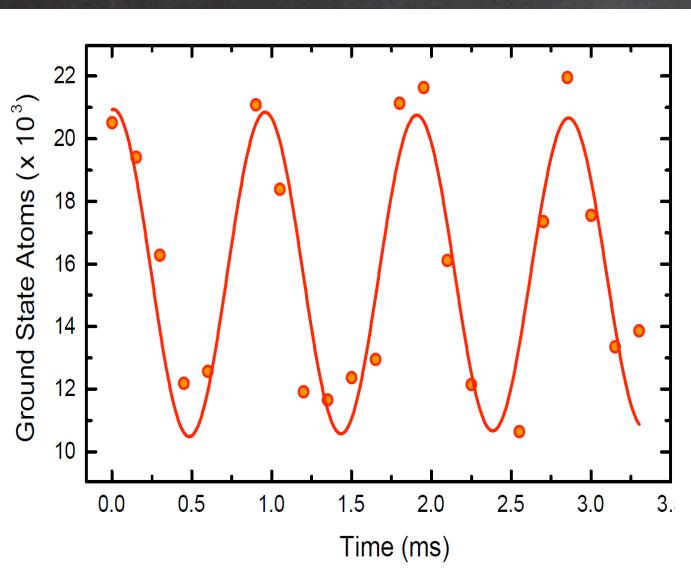
Alkaline-earth-like structure  
Electronic configuration [...]6s<sup>2</sup>



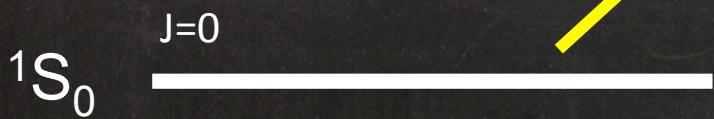
# Ytterbium



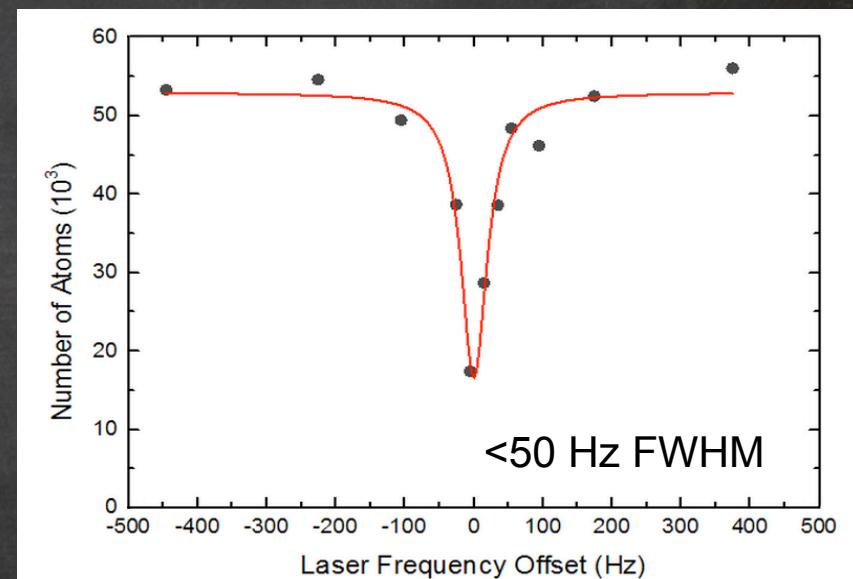
Rabi oscillations:



578nm clock transition  
( $\Gamma \sim 10$  mHz)



Clock transition spectrum @ 578nm  
in a magic-wavelength 3D lattice:



<50 Hz FWHM

$^3P_0$

J=0

long-lived ( $\tau \sim 10$  s)

Metastable states / clock transition

# Ytterbium

## Ytterbium

Alkaline-earth-like structure

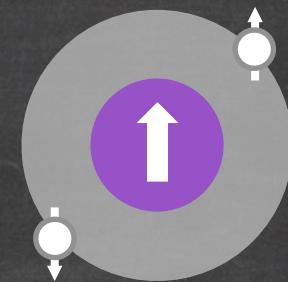
Electronic configuration [...]6s<sup>2</sup>

$^1P_1$

578nm clock transition  
 $(\Gamma \sim 10 \text{ mHz})$

$^1S_0$   
J=0

Metastable states / clock transition  
Nuclear spin / no hf coupling



nuclear spin I

$^3P_2$

$^3P_1$

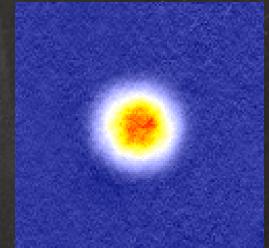
$^3P_0$

J=0

long-lived ( $\tau \sim 10 \text{ s}$ )

## Ultracold $^{173}\text{Yb}$ Fermi gas

$T \sim 10 \text{ nK} \sim 0.1 T_F$   
 $N = 10^4 \text{ atoms/spin}$

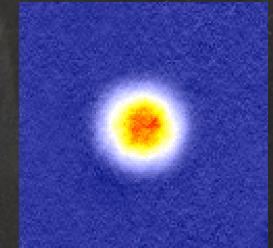


## Purely nuclear spin $I=5/2$

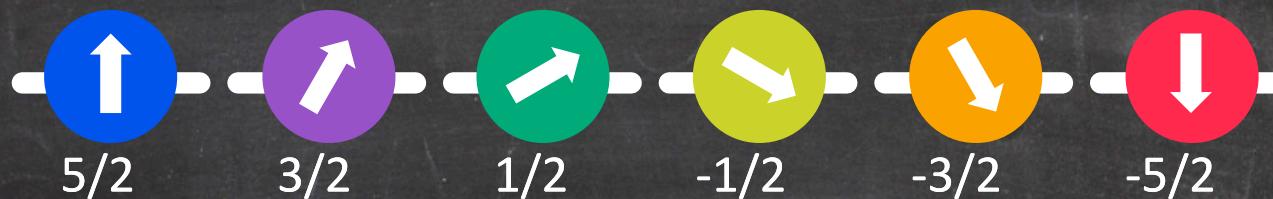


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Purely nuclear spin  $I=5/2$

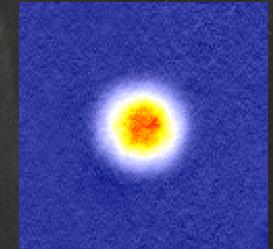


Same interaction between different spins  $\rightarrow$  SU(6) symmetry

M. Cazalilla et al., NJP 11, 103033 (2009)  
A. Gorshkov et al., Nat. Phys. 6, 289 (2010)

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A. Gorshkov et al., Nat. Phys. 6, 289 (2010)

No spin-changing collisions

$\rightarrow$  all mixtures are stable

# g-g spin-preserving collisions

---

$g_{+5/2}$



$g_{-5/2}$



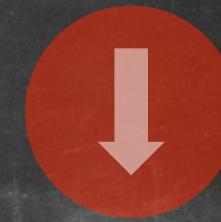
# g-g spin-preserving collisions

---

g +5/2



g -5/2



g -5/2



g +5/2



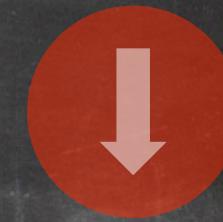
# g-g spin-preserving collisions

---

g  $+5/2$



g  $-5/2$



g  $+1/2$



g  $-1/2$



forbidden!

# Ytterbium $^3P_0$ Metastable state

Ytterbium

Nuclear + electronic degrees of freedom

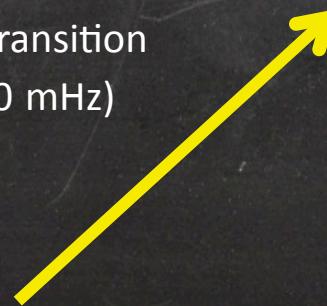
$^1P_1$

$^3P_2$

$^3P_1$

$^3P_0$

578nm  
clock transition  
 $(\Gamma \sim 10 \text{ mHz})$



$^1S_0$

Metastable states / clock transition

Nuclear spin / no hf coupling

# Ytterbium $^3P_0$ Metastable state

Ytterbium

Nuclear + electronic degrees of freedom

$^1P_1$

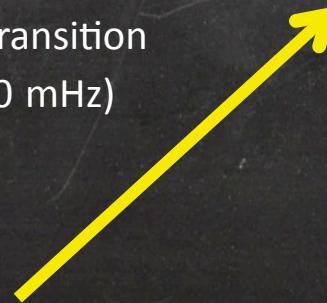
$^3P_2$

$^3P_1$

e

g

578nm  
clock transition  
 $(\Gamma \sim 10 \text{ mHz})$



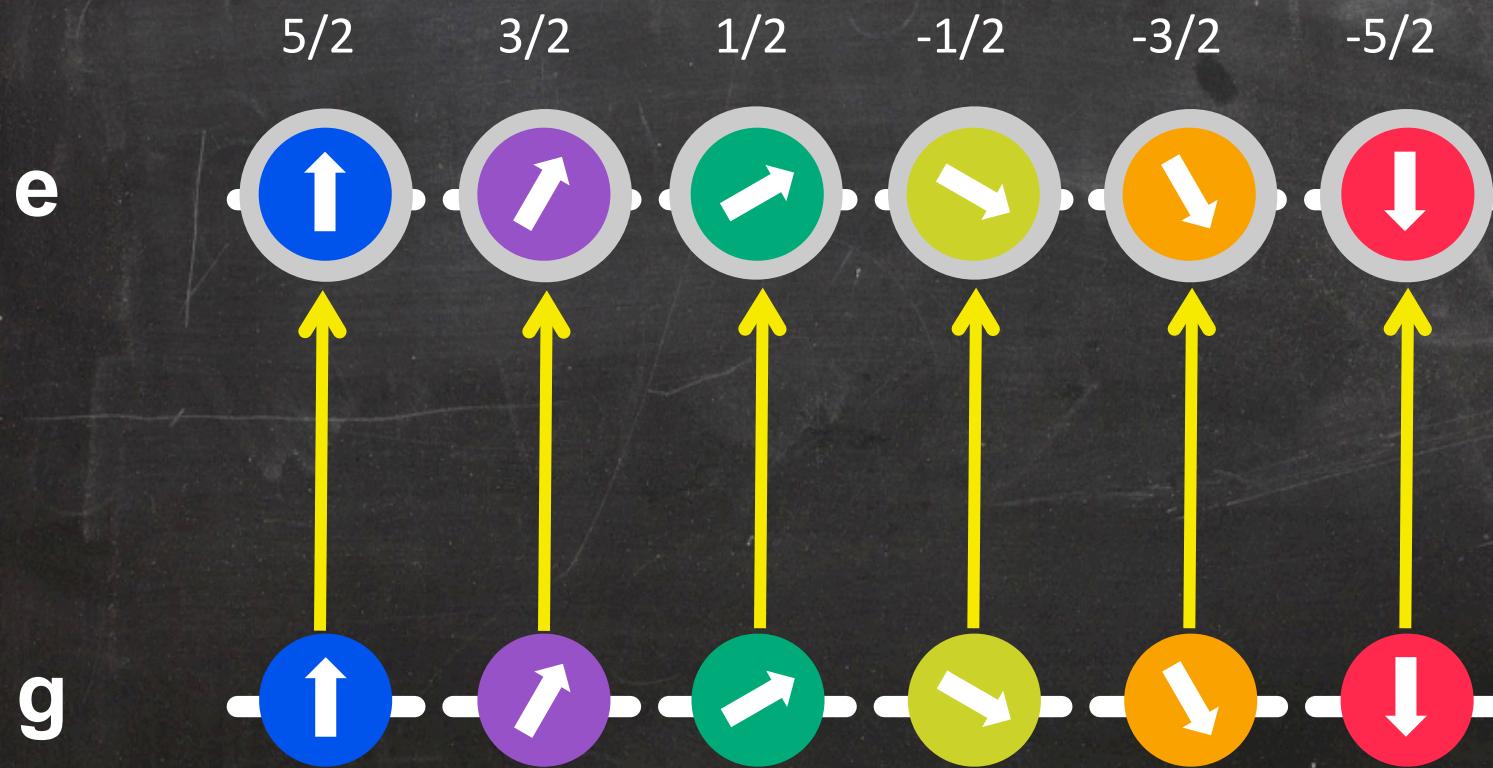
Metastable states / clock transition

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# Ytterbium ${}^3P_0$ Metastable state

Ytterbium

Nuclear + electronic degrees of freedom



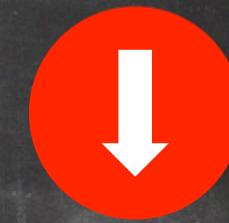
# g-e spin-exchange collisions

---

e  $+5/2$



g  $-5/2$



# g-e spin-exchange collisions

---

e  $+5/2$



g  $-5/2$



g  $+5/2$



e  $-5/2$

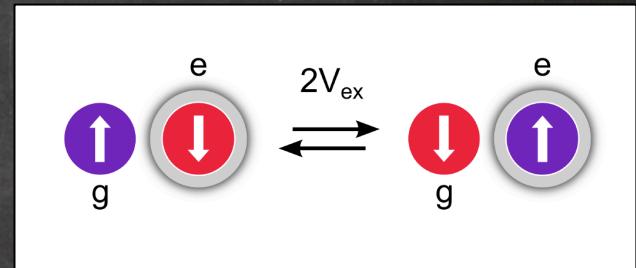


# g-e spin-exchange interaction

Two entangled internal degrees of freedom:

Coherent control of nuclear and electronic state

Quantum information processing



related spin-exchange dynamics in  
M. Anderlini et al., Nature 448, 452 (2007)

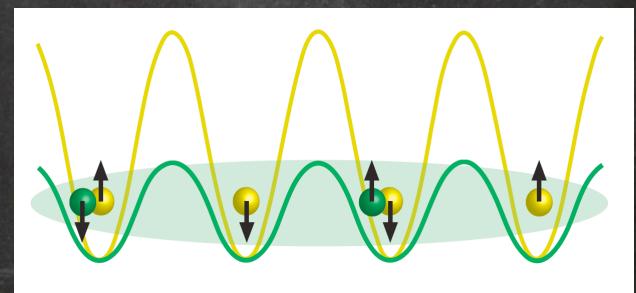
New quantum simulation of strongly-correlated systems:

Strong spin-orbital interaction:

Orbital magnetism, Kondo model

$$\hat{H} = -J_g \sum_{\langle i,j \rangle, \sigma} \hat{c}_{ig\sigma}^\dagger \hat{c}_{jg\sigma} + V_{ex} \sum_{i\sigma' \sigma} \hat{c}_{ig\sigma}^\dagger \hat{c}_{ie\sigma'}^\dagger \hat{c}_{ig\sigma'} \hat{c}_{ie\sigma}$$

SU(N) magnetism



A. Gorshkov et al., Nat. Phys. 6, 289 (2010)  
M. Foss-Feig et al., PRA. 81, 3-6 (2010)

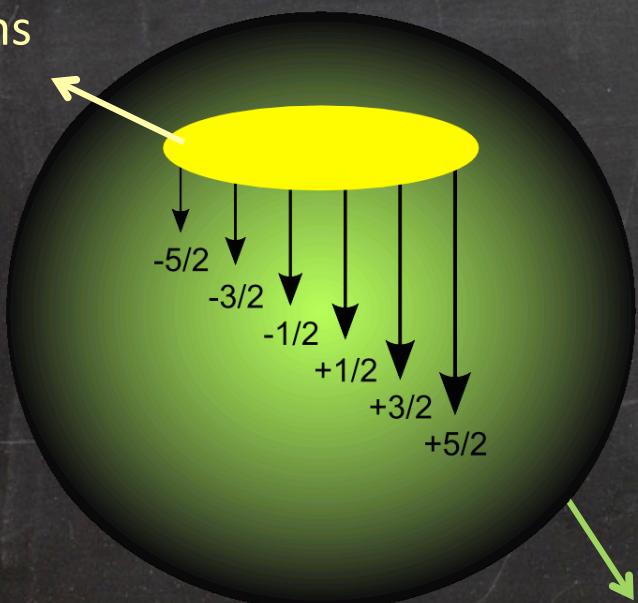
# Spin detection and manipulation

## Optical Stern-Gerlach detection

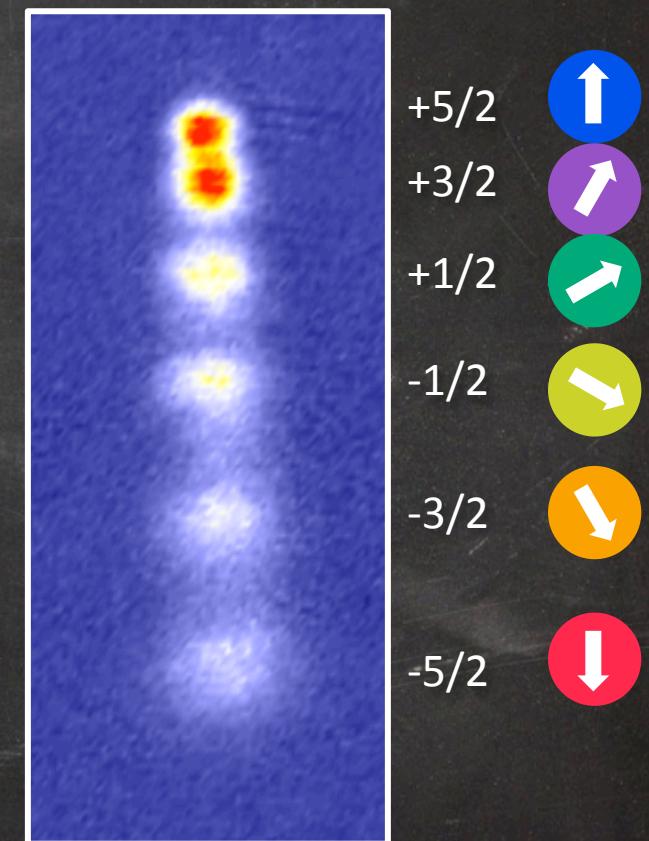
S. Taie et al., PRL (2010)

### State-dependent optical dipole force

atoms

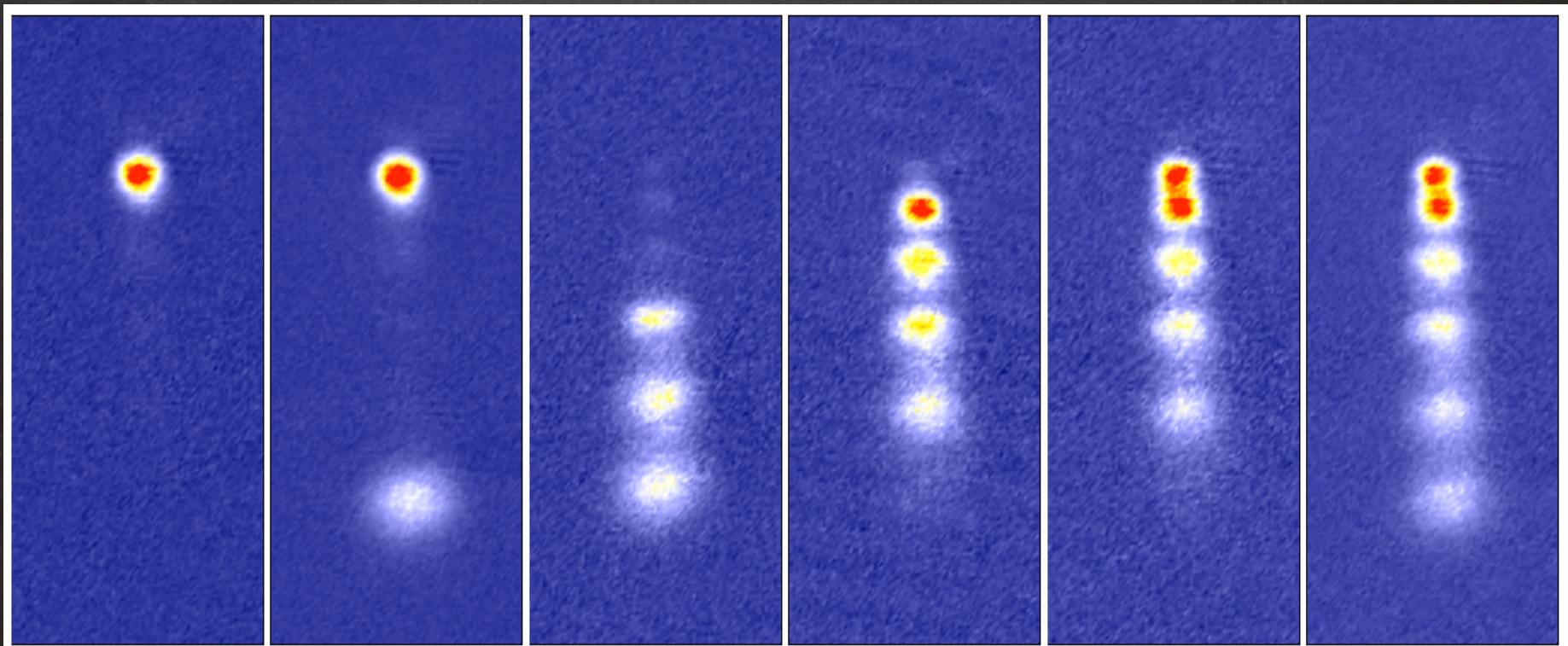


optical Stern-Gerlach beam  
556 nm,  $3000\Gamma$  detuning,  $\sigma^+$



# Spin detection and manipulation

$^{173}\text{Yb}$  Fermi gases in an arbitrary number of equally-populated components:



1 spin

2 spins

$\text{SU}(2)$

3 spins

$\text{SU}(3)$

4 spins

$\text{SU}(4)$

5 spins

$\text{SU}(5)$

6 spins

$\text{SU}(6)$

# g-e spin-exchange collisions

Two fermions (g+e) in a trap

A. Gorshkov et al., Nat. Phys. 6, 289 (2010)



Antisymmetrization of the two-particle state:

$$|eg^-\rangle \propto [g_1 e_2 - e_1 g_2] [ \uparrow_1 \downarrow_2 + \downarrow_1 \uparrow_2 ]$$

*orbital-antisymmetric  
spin-triplet*

$$|eg^+\rangle \propto [g_1 e_2 + e_1 g_2] [ \uparrow_1 \downarrow_2 - \downarrow_1 \uparrow_2 ]$$

*orbital-symmetric  
spin-singlet*

# g-e spin-exchange collisions

Two fermions (g+e) in a trap

A. Gorshkov et al., Nat. Phys. 6, 289 (2010)

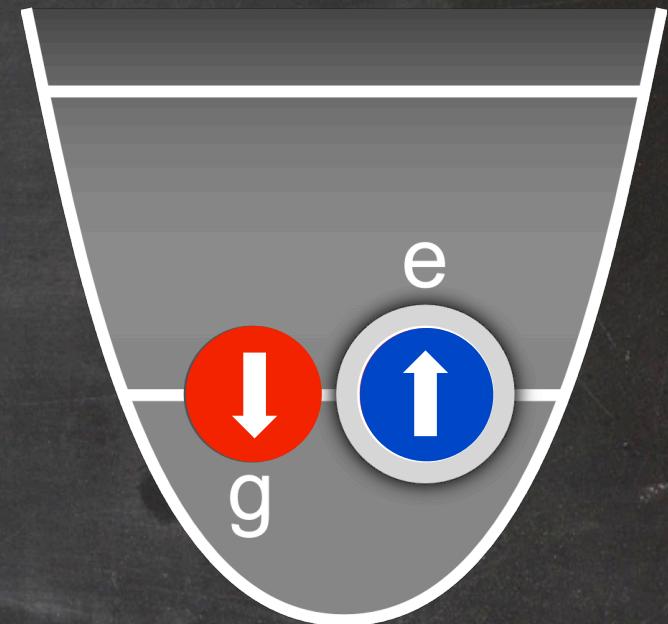
A local spin-exchange interaction between different "orbitals" arises:

$$\hat{H} = \begin{pmatrix} U_{eg}^+ & 0 \\ 0 & U_{eg}^- \end{pmatrix}$$

Different scattering lengths for the two states:

$$|eg^-\rangle \propto | \begin{matrix} e \\ \downarrow \\ g \end{matrix} \rangle + | \begin{matrix} e \\ \uparrow \\ g \end{matrix} \rangle$$

$$|eg^+\rangle \propto | \begin{matrix} e \\ \downarrow \\ g \end{matrix} \rangle - | \begin{matrix} e \\ \uparrow \\ g \end{matrix} \rangle$$



$$\begin{array}{c} U_{eg}^-(a_{eg}^-) \\ \hline \text{---} \\ U_{eg}^+(a_{eg}^+) \end{array} \quad \begin{array}{c} \uparrow \\ 2V_{ex} \\ \downarrow \end{array}$$

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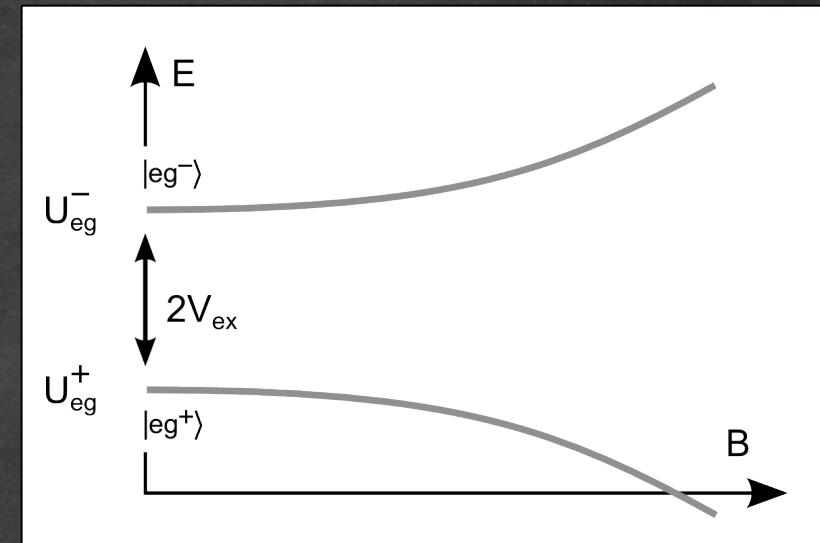


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# g-e spin-exchange oscillations

A magnetic field  $B$  induces a mixing between the two channels:

$$|\psi\rangle = \alpha|eg^+\rangle + \beta|eg^-\rangle$$

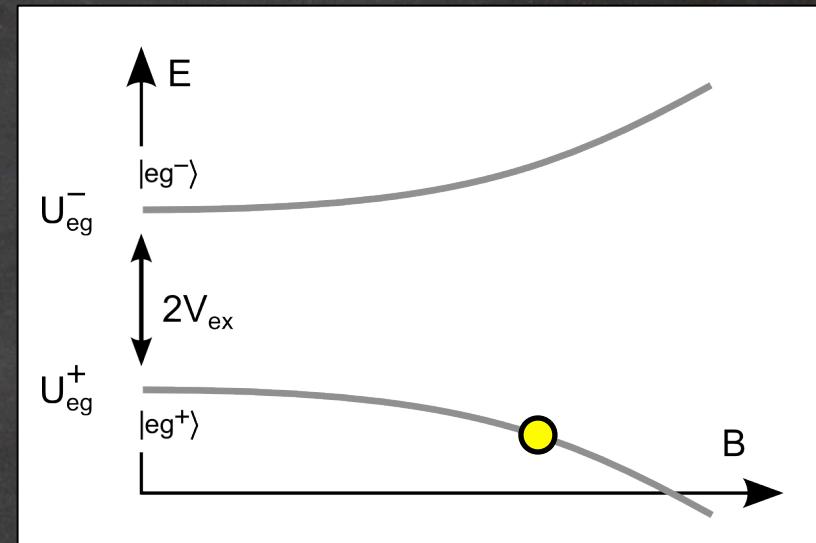


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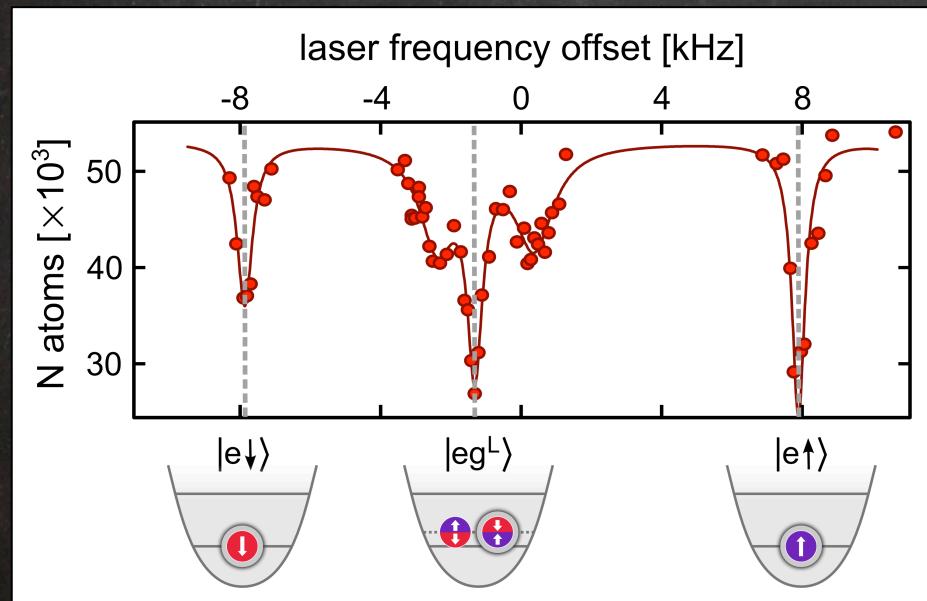
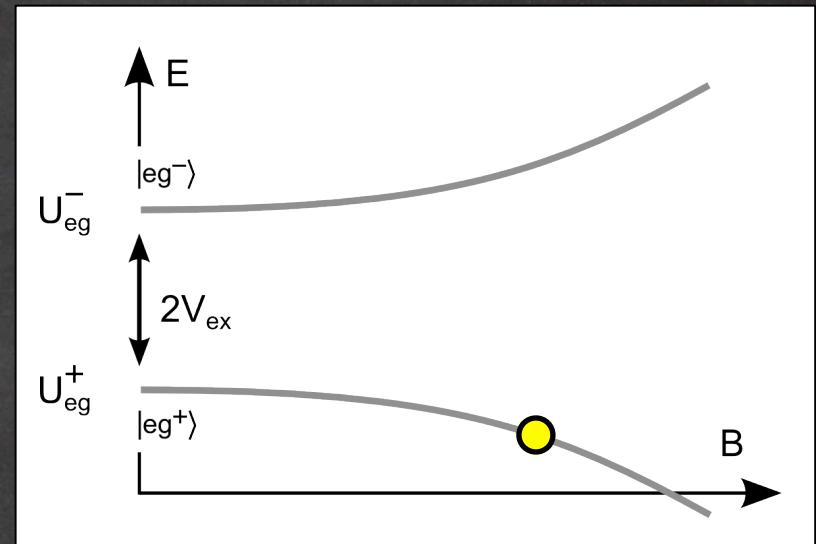


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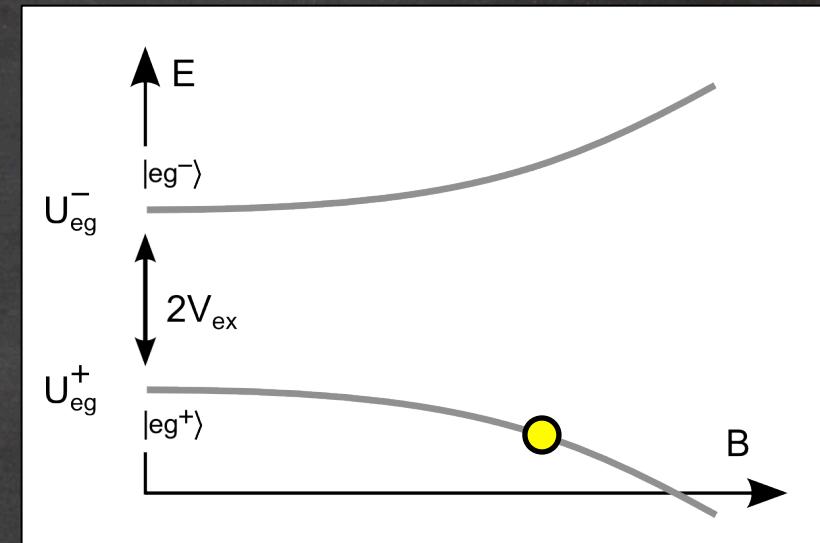
Spectrum of the 578nm clock transition  
in a 3D optical lattice

see related work by Fölling/Bloch group:  
F. Scazza et al., Nat. Phys. 10, 779–784 (2014)

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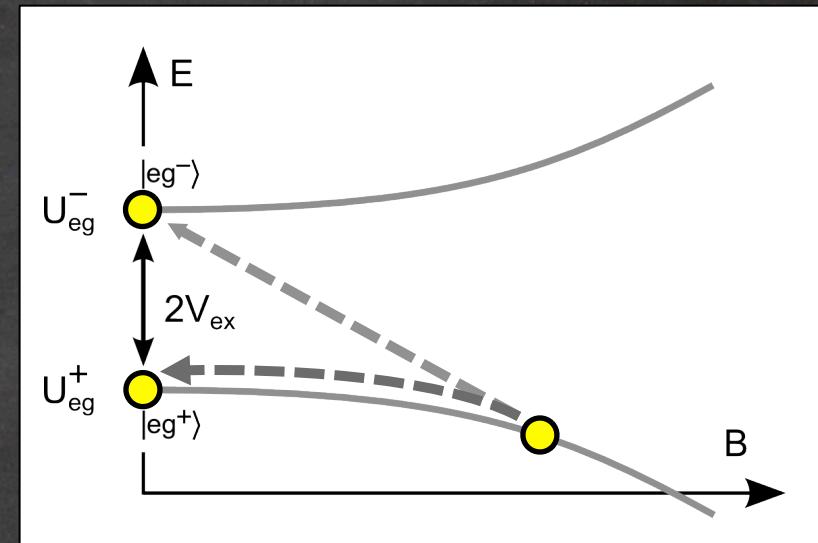


# g-e spin-exchange oscillations

A magnetic field  $B$  induces a mixing between the two channels:

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$B$  field quench



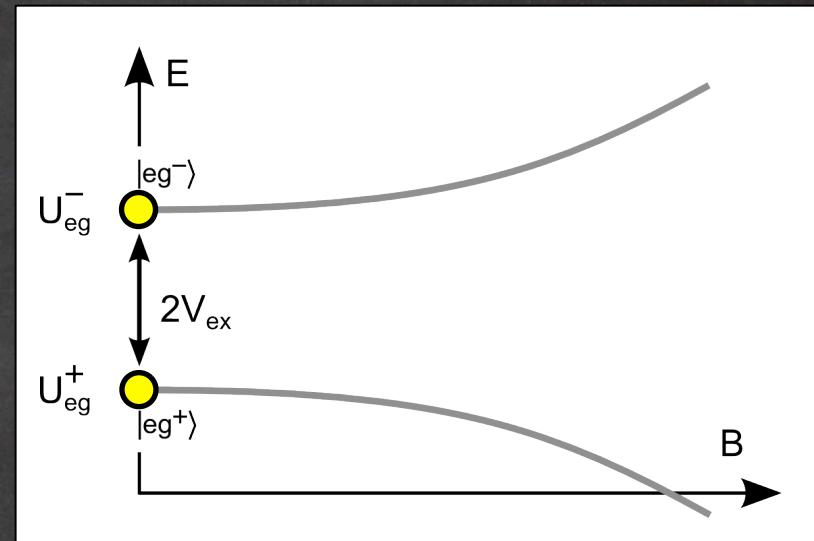
# g-e spin-exchange oscillations

A magnetic field  $B$  induces a mixing between the two channels:

$$|\psi\rangle = \alpha|eg^+\rangle + \beta|eg^-\rangle$$

$B$  field quench + free evolution

$$|\psi(t)\rangle = \alpha|eg^+\rangle + \beta e^{-i2V_{ex}t/\hbar}|eg^-\rangle$$



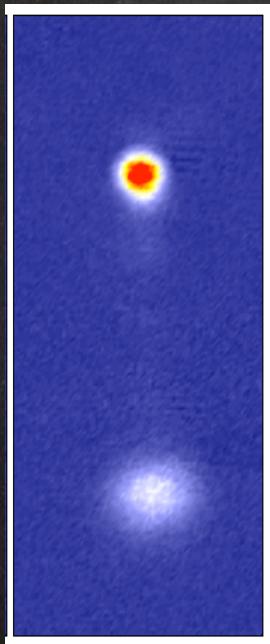
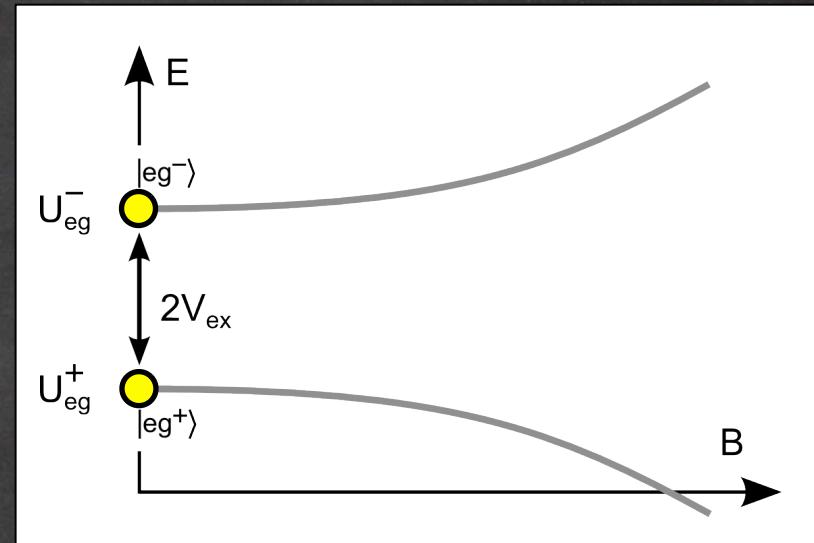
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Ground-state magnetization:

$$|\langle g \uparrow | \psi(t) \rangle|^2 = \frac{1}{2} + \alpha\beta \cos\left(\frac{2V_{ex}t}{\hbar}\right)$$

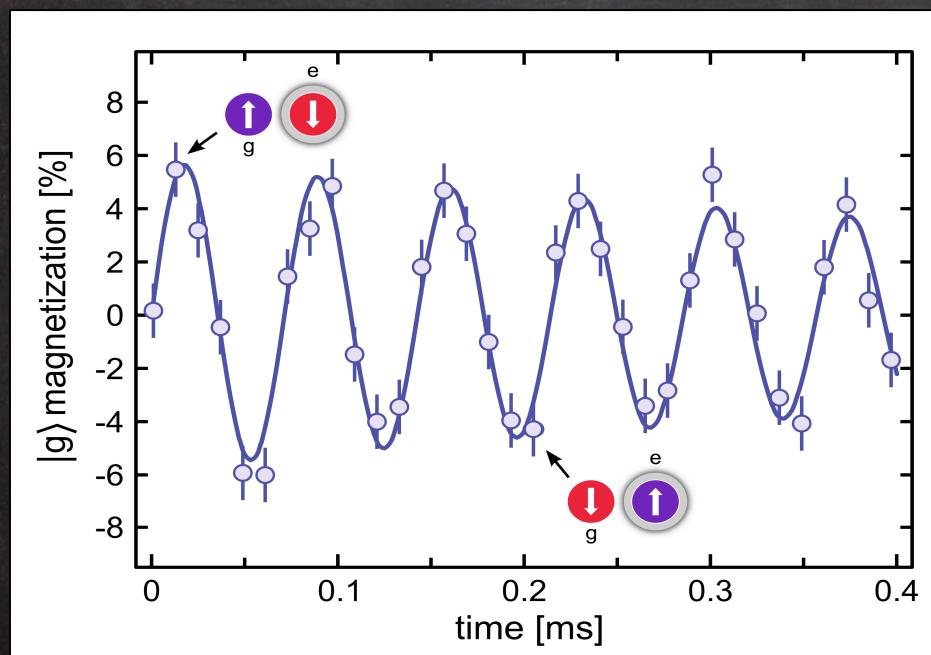
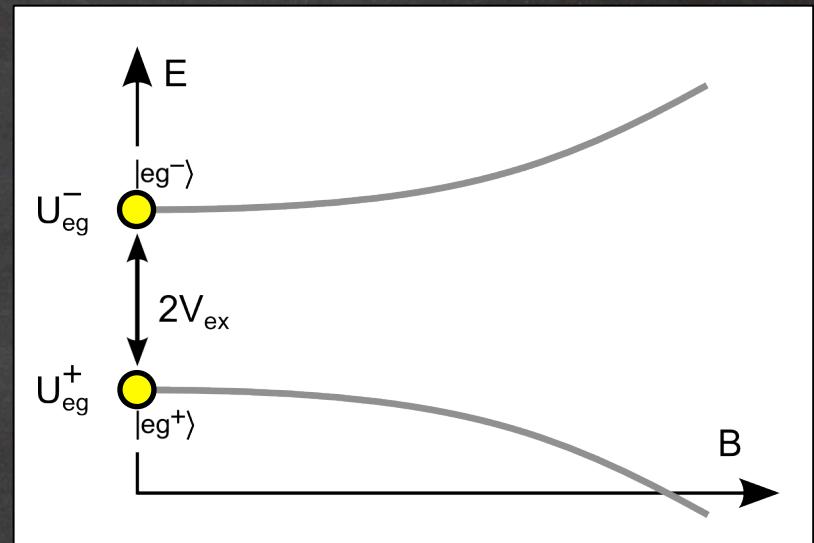
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Ground-state magnetization:

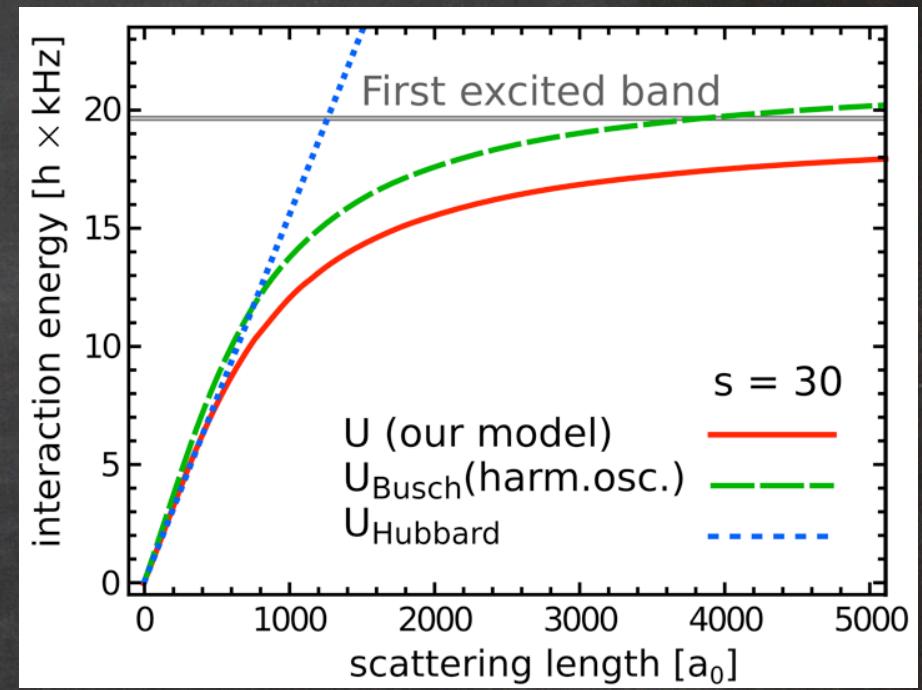
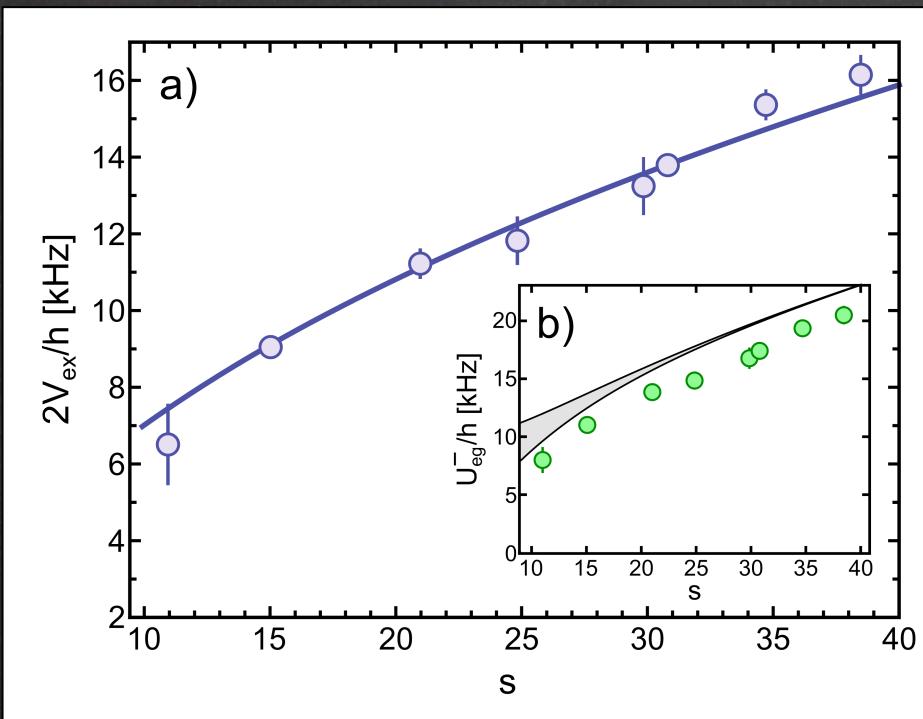
$$|\langle g \uparrow | \psi(t) \rangle|^2 = \frac{1}{2} + \alpha\beta \cos\left(\frac{2V_{ex}t}{\hbar}\right)$$

Direct observation of long-lived spin-exchange oscillations

# g-e spin-exchange interaction

Very large spin-exchange energy!!!

$$V_{ex} \gg k_B T$$



Strong repulsion in the  $|eg^-\rangle$  state, close to the lattice band separation

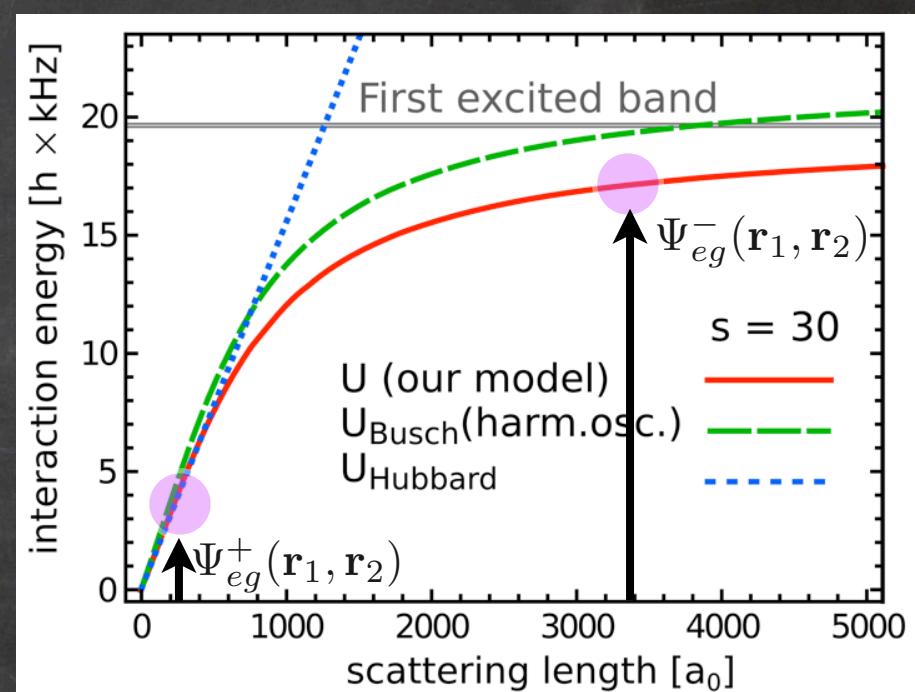
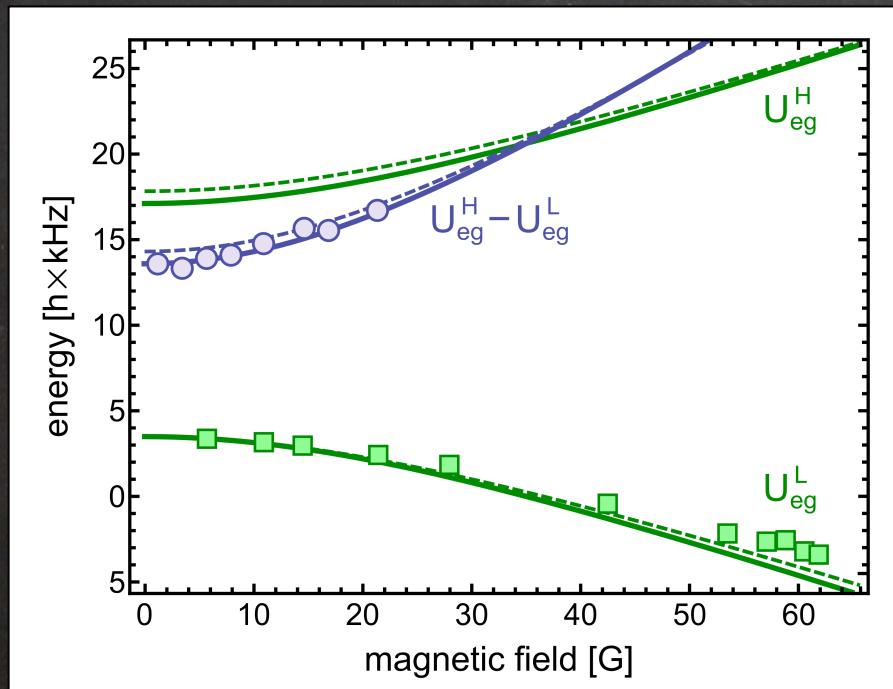
Beyond standard Hubbard treatment of interactions  
("fermionization" of spatial wavefunction)

T. Busch et al., Found. Phys. 28, 549 (1998)  
Zurn et al., PRL 108, 075303 (2012)

$$a_{eg}^+ = 220 a_0$$
$$a_{eg}^- = 3300 a_0$$

# g-e spin-exchange interaction

Very large spin-exchange energy!!!



Frank-Condon Factor necessary to take into account spatial wavefunction fermionization

$$\hat{H} = \begin{pmatrix} U_{eg}^+ & F\Delta B \\ F\Delta B & U_{eg}^- \end{pmatrix}$$

$$F = \iint d\mathbf{r}_1 d\mathbf{r}_2 \Psi_{eg}^+(\mathbf{r}_1, \mathbf{r}_2) \Psi_{eg}^-(\mathbf{r}_1, \mathbf{r}_2) < 1$$

$$\begin{cases} a_{eg}^+ = 220 a_0 \\ a_{eg}^- = 3300 a_0 \end{cases}$$

For more details...

G. Pagano, M. Mancini, G. Cappellini et al., *Nature Phys.* 10, 198 (2014)

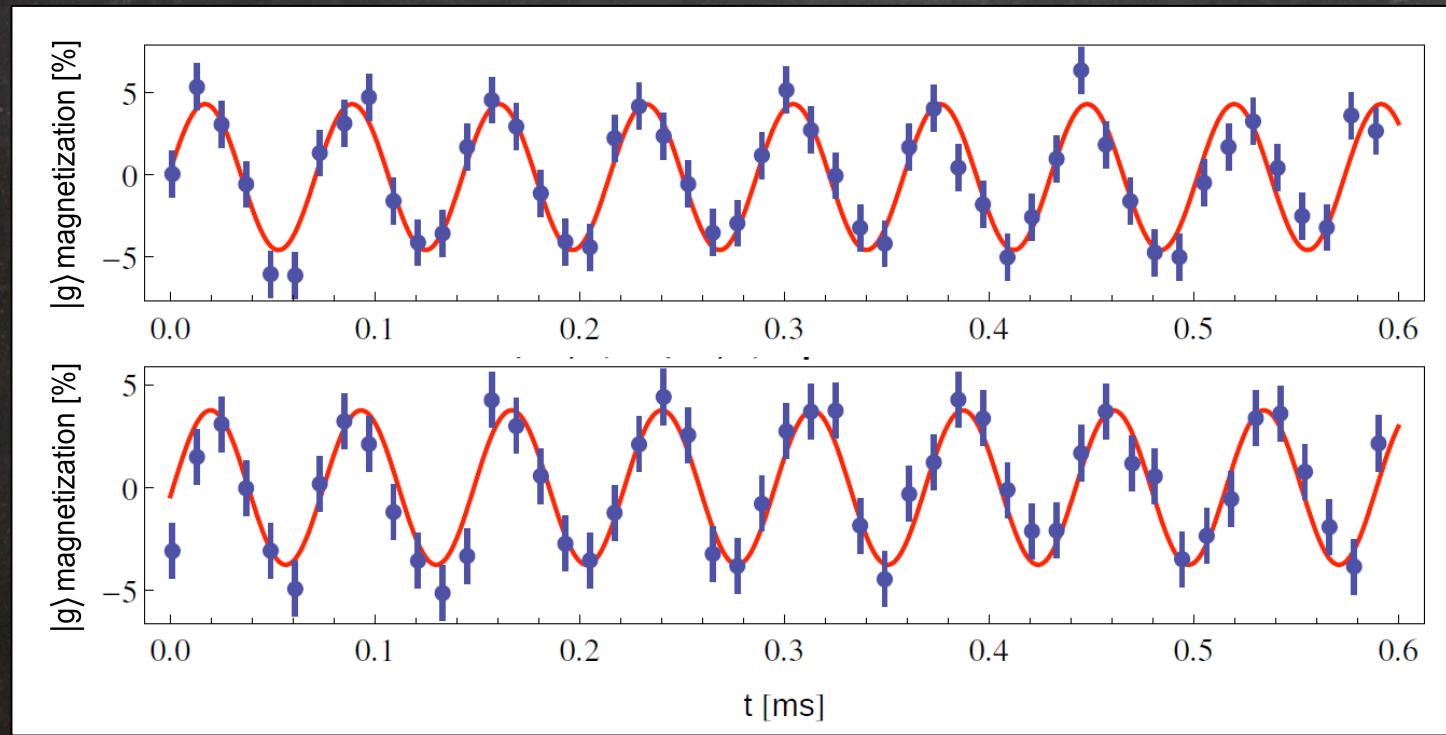
G. Cappellini, M. Mancini, G. Pagano et al., *PRL* 113, 120402 (2014) 

For more details...

G. Pagano, M. Mancini, G. Cappellini et al., Nature Phys. 10, 198 (2014)

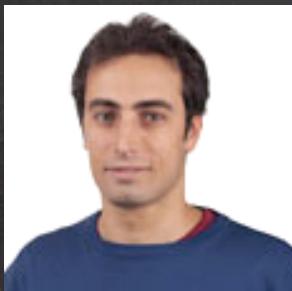
G. Cappellini, M. Mancini, G. Pagano et al., PRL 113, 120402 (2014) 

Measurement of spin-exchange frequency to probe the SU(N) symmetry

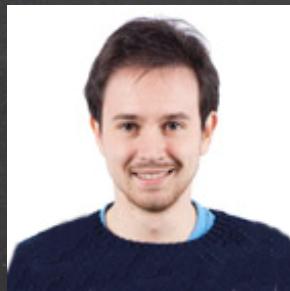


# Credits

Guido Pagano



Marco  
Mancini



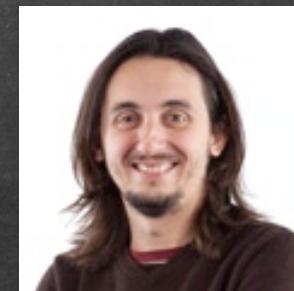
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Former members:  
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P. Lombardi



Jacopo  
Catani



Carlo  
Sias



Massimo  
Inguscio



Leonardo  
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Collaboration with Yb clock experiment @ INRIM (Torino): M. Pizzocaro, D. Calonico, F. Levi

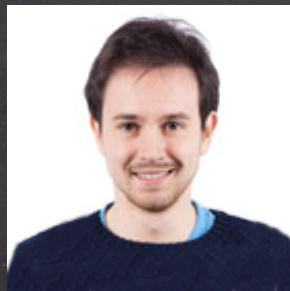
Funding from EU, ERC, MIUR, IIT



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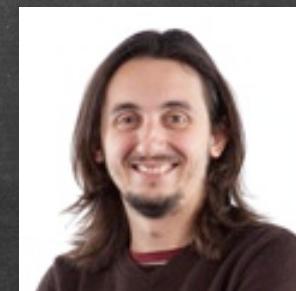
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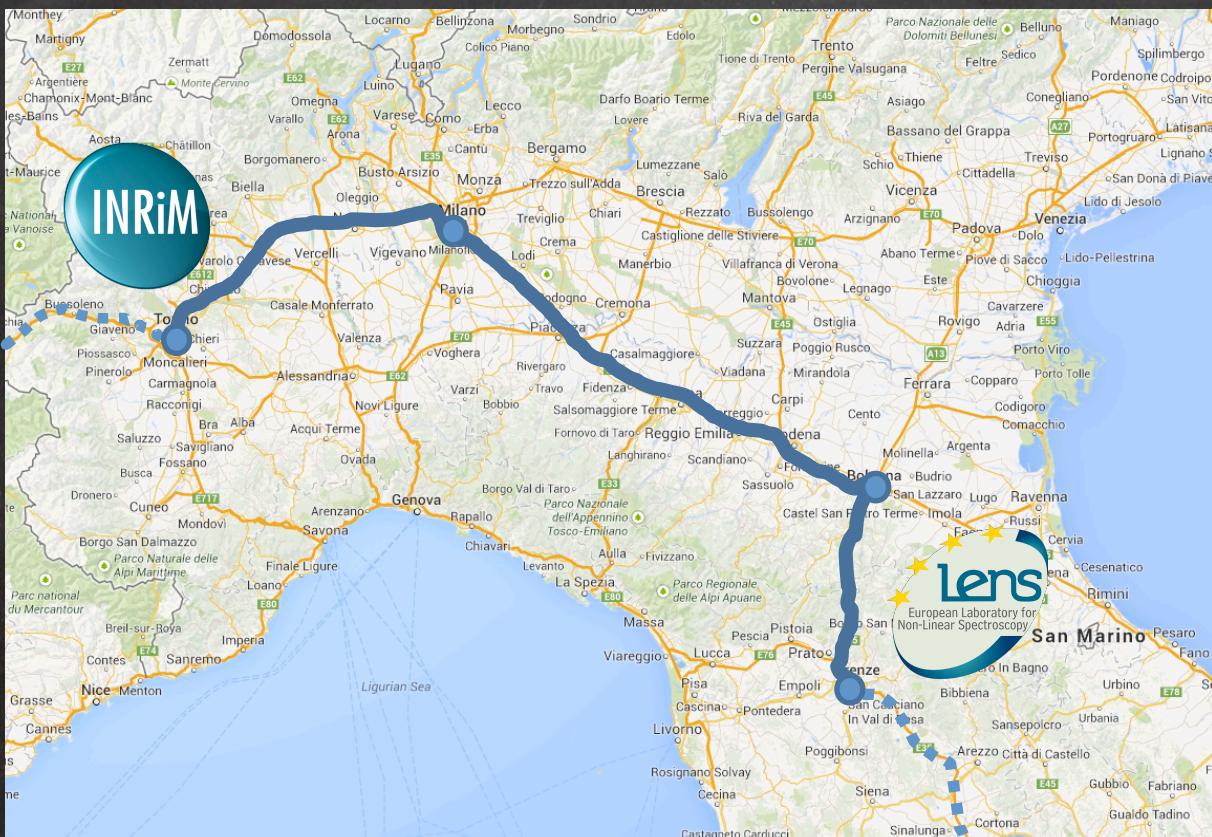


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# Thanks for your attention!

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620km-long dedicated  
optical frequency link

remote comparison  
between Yb experiments

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