

# Fe-based superconductors: role of the magnetic impurities

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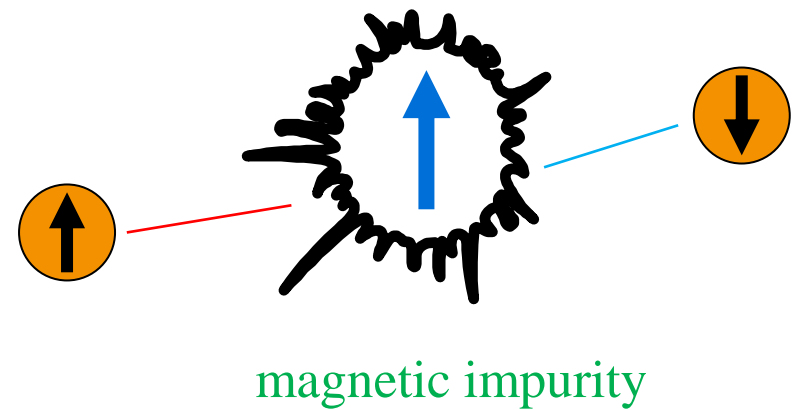
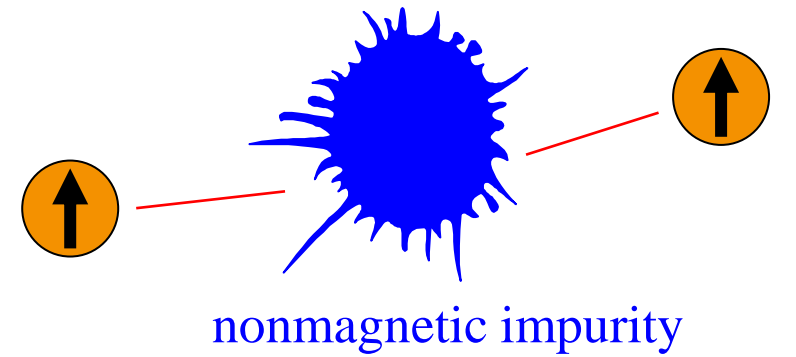
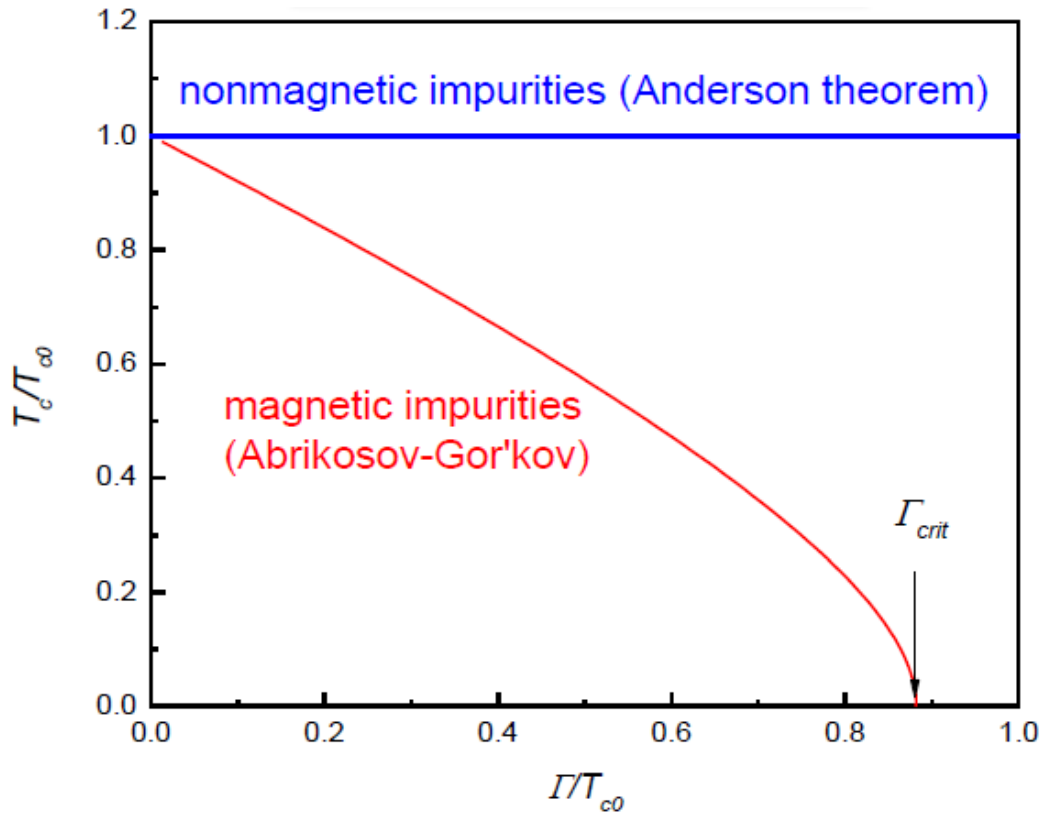
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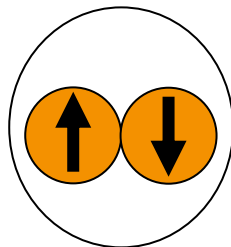
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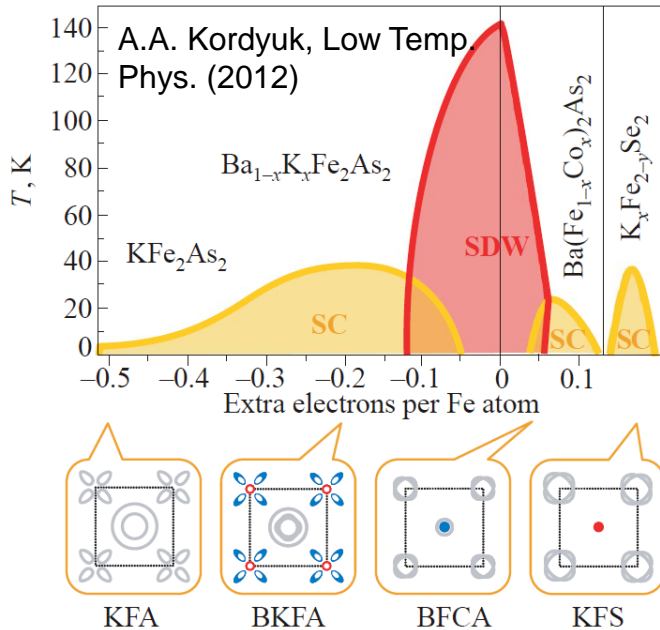
# Effect of impurity scattering: single-gap $s$ -wave system



Singlet cooper pair

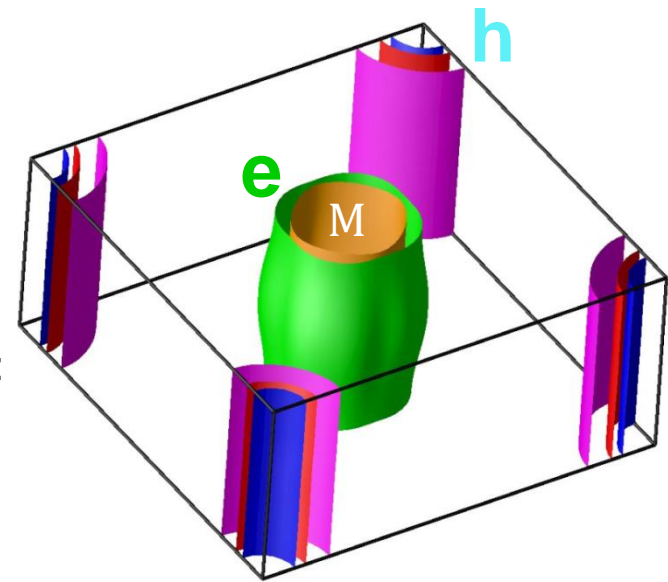


# Fe-based superconductors

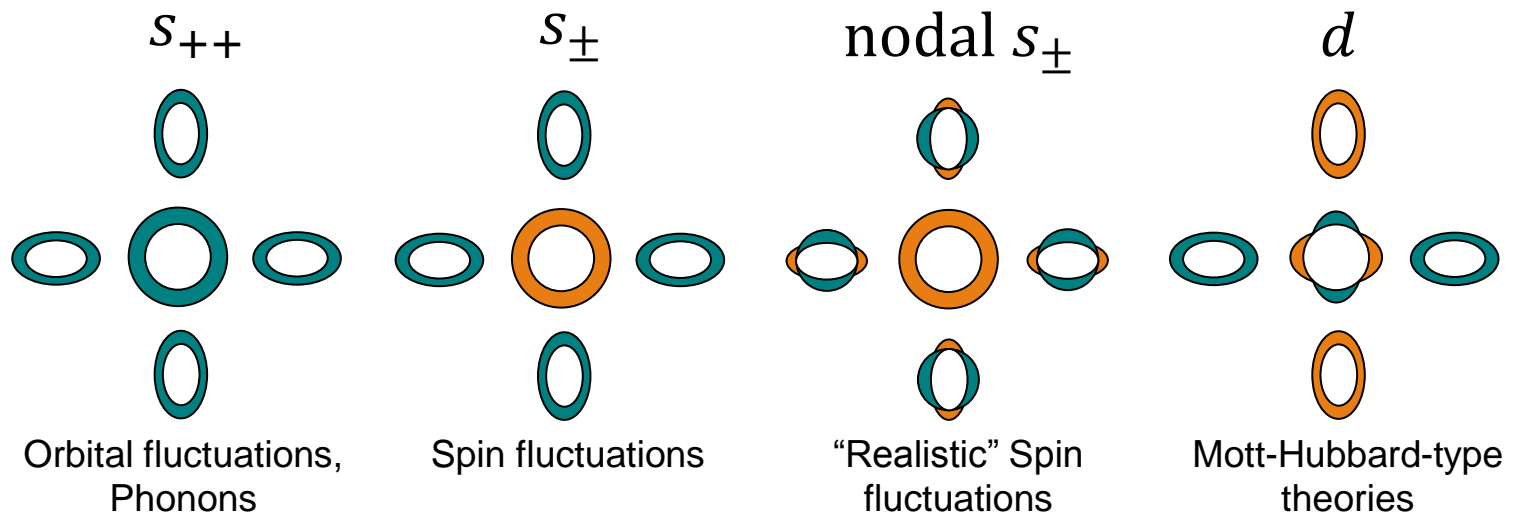


**DFT result:**  
 $\text{Fe}^{2+}$   $3d^6$ -states  
 form the FS

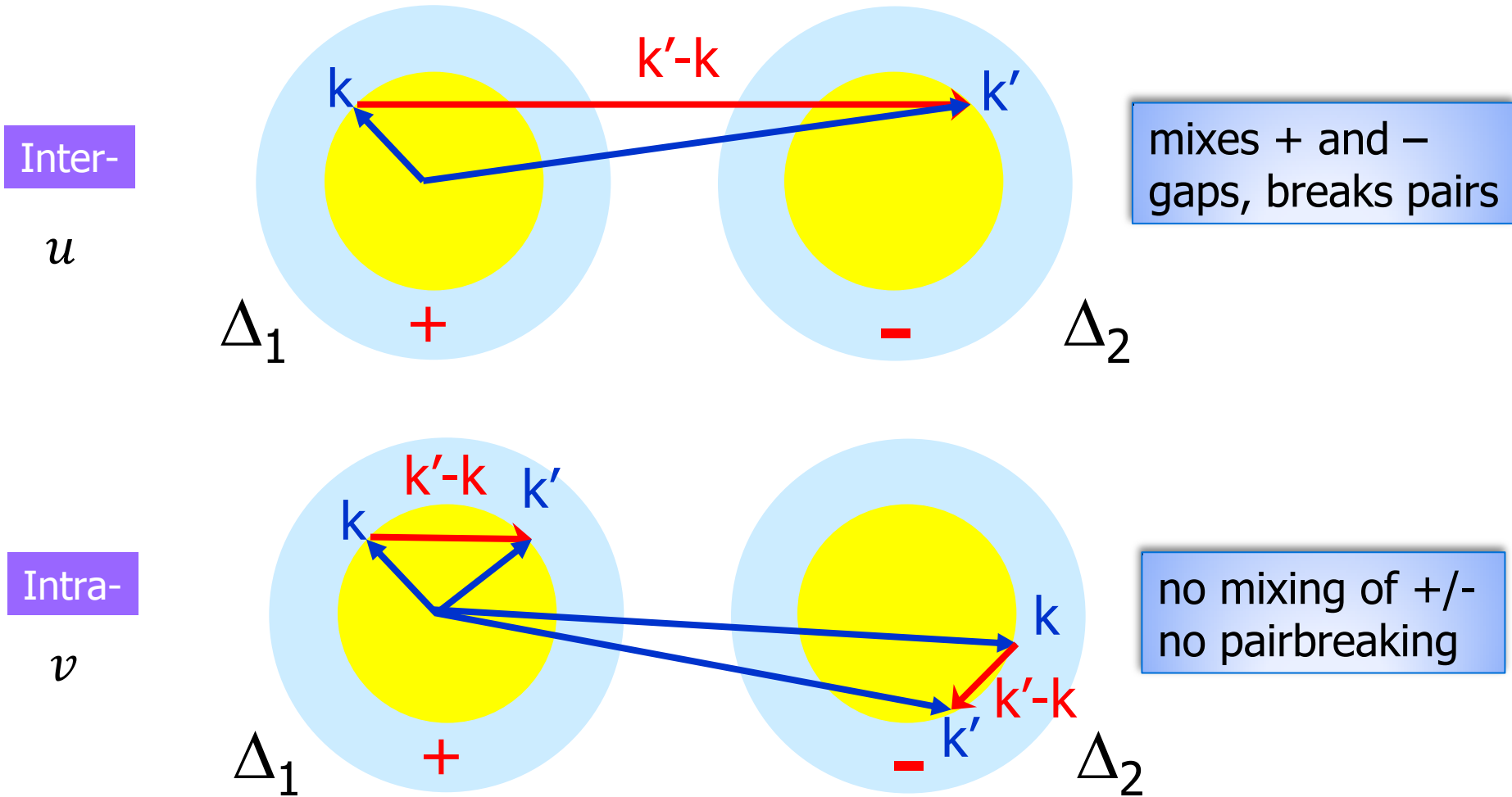
Weak CEF splitting:  
 all 5 orbitals ( $d_{x^2-y^2}$ ,  
 $d_{3z^2-r^2}$ ,  $d_{xy}$ ,  $d_{xz}+d_{yz}$ )  
 are near the Fermi  
 level



## Symmetry proposals for FeBS



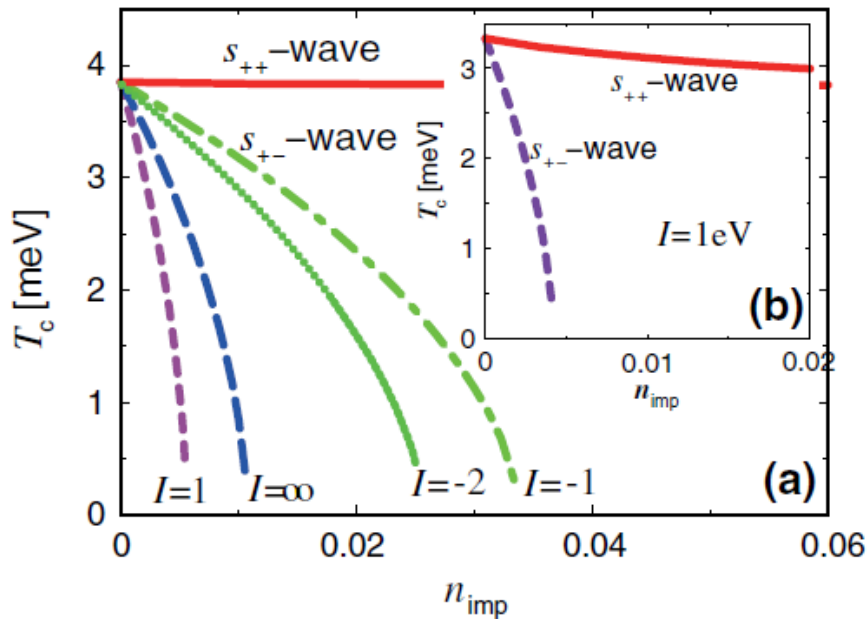
# Inter- and intraband nonmagnetic impurity scattering in the 2-band $s_{\pm}$ system



A.A. Golubov and I.I. Mazin, PRB 55, 15146 (1997), Physica C 243, 153 (1995)

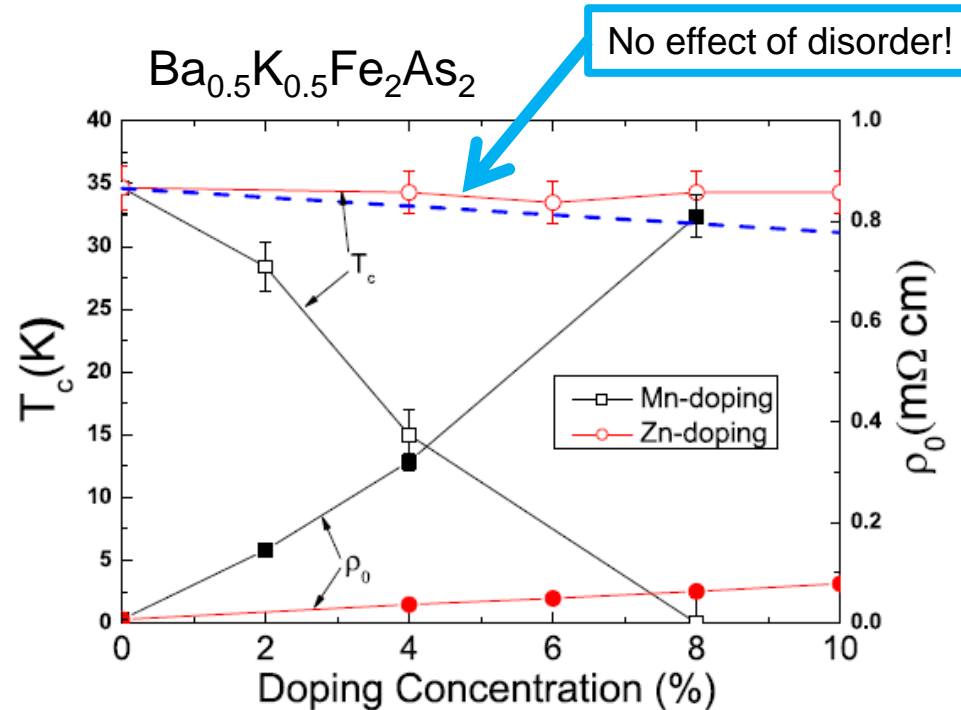
P.J. Hirschfeld, MMK, and I.I. Mazin, Rep. Prog. Phys. 74, 124508 (2011)

## Non-magnetic vs. magnetic impurities



Theory: suppression of  $T_c$  by non-magnetic impurities

S. Onari, H. Kontani, PRL 103, 177001 (2009)

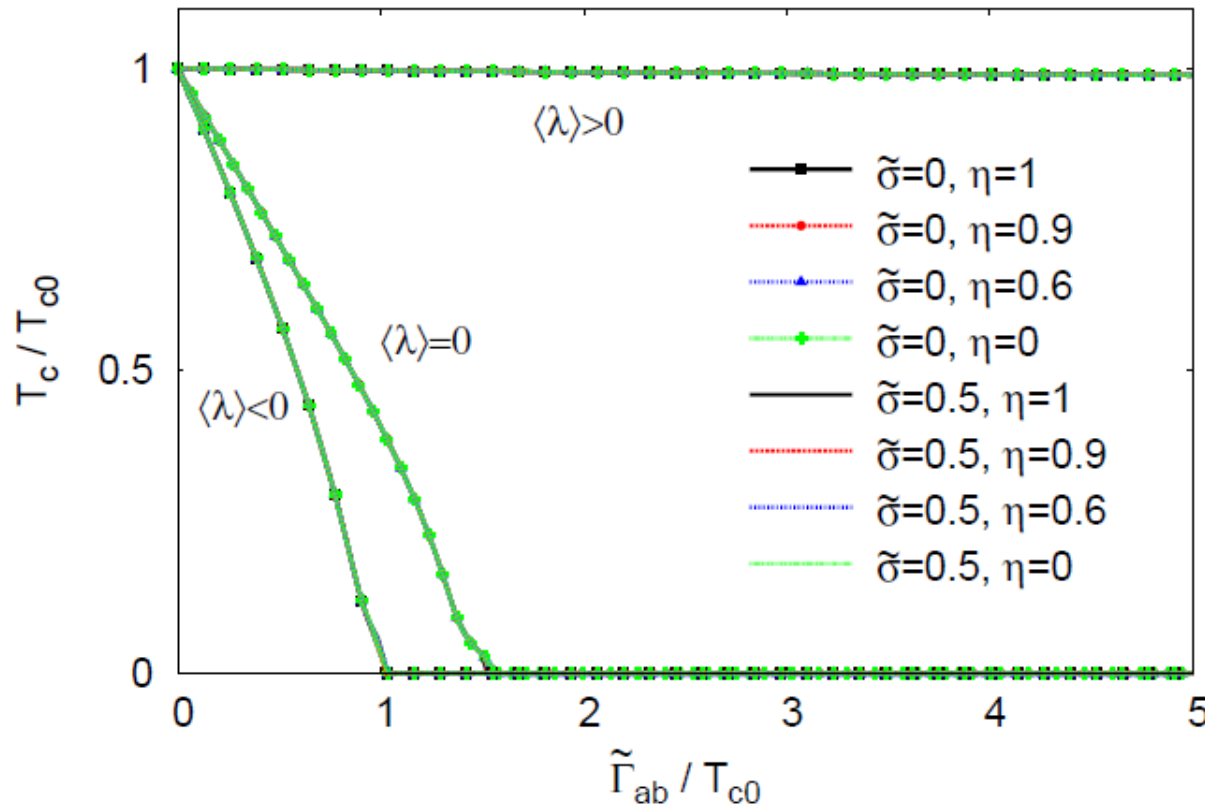


For Zn (non-magnetic impurity) the suppression of  $T_c$  is negligible

Magnetic impurities (Mn) suppress  $T_c$ ,  $\Delta T_c / (1\% \text{Mn}) = -4.2\text{K}$

P. Cheng et al., PRB 81, 174529 (2010)

# Non-magnetic impurities in a two-band $s_{\pm}$ state: universal scattering rate



Interband and  
intraband impurities  
 $v^2 = u^2 \eta$

Impurity strength  
$$\tilde{\sigma} = \frac{\pi^2 N_a N_b u^2}{1 + \pi^2 N_a N_b u^2}$$

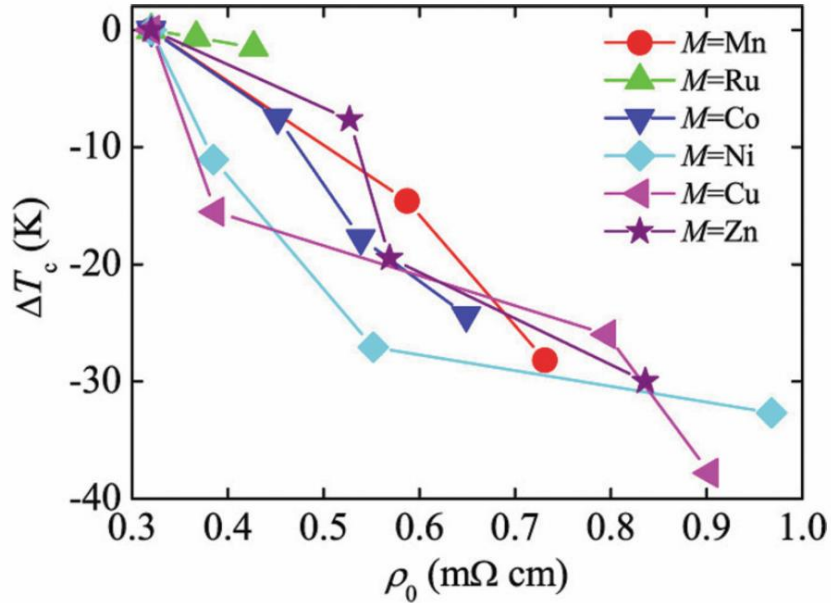
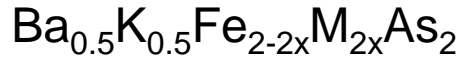
$\tilde{\sigma} \rightarrow 0$ : Born limit  
 $\tilde{\sigma} \rightarrow 1$ : unitary limit

Scattering rate  
$$\Gamma_{a(b)} = n_{\text{imp}} \pi N_{b(a)} u^2 (1 - \tilde{\sigma})$$

Averaged coupling constant

$$\langle \lambda \rangle_{FS} = \frac{N_a}{N} (\lambda_{aa} + \lambda_{ab}) + \frac{N_b}{N} (\lambda_{ba} + \lambda_{bb})$$

## Experiment: disorder



J. Li et al., PRB 85, 214509 (2012)

## Irradiation studies

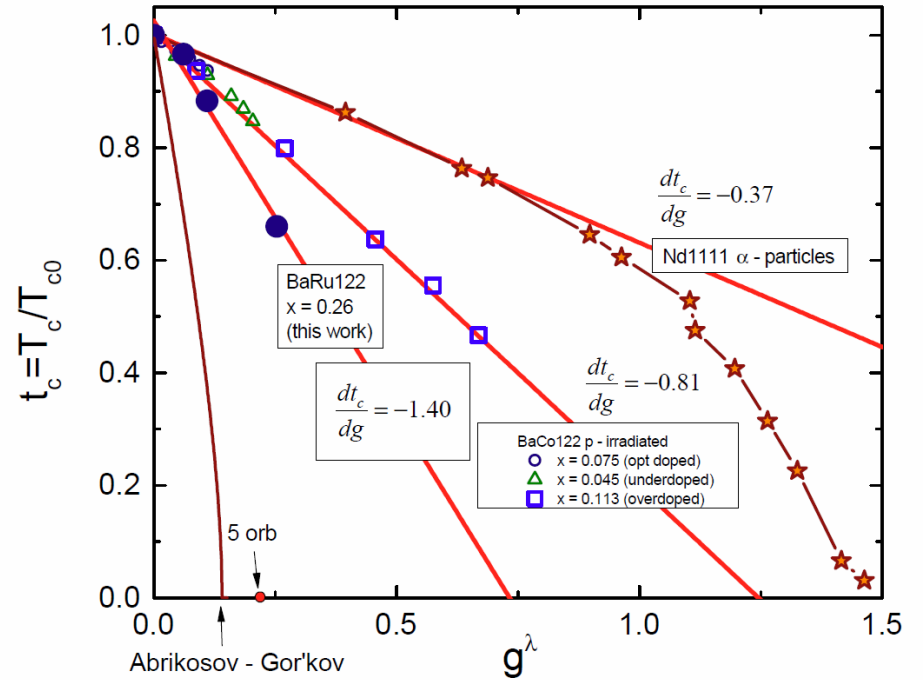


FIG. 3. (Color online) Comparison of the  $T_c$  suppression by three irradiation techniques used to introduce artificial disorder in iron - pnictides. The single effective dimensionless scattering rate,  $g^\lambda$ , was calculated from the penetration depth and resistivity, see text for description. Abrikosov - Gor'kov theory for an isotropic  $s$ -wave superconductor with magnetic impurities (solid line) and a critical scattering rate within 5 band  $s_\pm$  model [6] are also shown.

R. Prozorov et al., arXiv:1405.3255v1

# Effect of impurity scattering: Born limit

Single-band case:  $1 = 2T_c\lambda\pi N_0 \sum_{0 < \omega_n \leq \omega_D} \left( \frac{\tilde{\phi}_n}{\Delta} \frac{1}{\tilde{\omega}_n} \right)_{T_c}$

Nonmagnetic (magnetic) impurities:

$$\begin{cases} \tilde{\omega}_n = \omega_n + \frac{\Gamma_a}{2} \frac{\tilde{\omega}_n}{\sqrt{\tilde{\omega}_n^2 + \tilde{\phi}_n^2}} \\ \tilde{\phi}_n = \Delta \pm \frac{\Gamma_a}{2} \frac{\tilde{\phi}_n}{\sqrt{\tilde{\omega}_n^2 + \tilde{\phi}_n^2}} \end{cases}$$

$\left( \frac{\tilde{\phi}_n}{\Delta} \frac{1}{\tilde{\omega}_n} \right)_{T_c} = \frac{1}{\omega_n} \rightarrow T_c = 1.13\omega_D e^{-1/\lambda N_0}$   
**Anderson's theorem**  
 impurities cancel out!

$\left( \frac{\tilde{\phi}_n}{\Delta} \frac{1}{\tilde{\omega}_n} \right)_{T_c} = \frac{1}{\omega_n + \Gamma_a}$

impurity scattering rate  $\Gamma_a = \pi N_0 n_{\text{imp}} u^2$

$T_c$  is suppressed compared to the clean case ( $T_{c0}$ )!  $\ln \frac{T_{c0}}{T_c} = \Psi \left( \frac{1}{2} + \frac{\Gamma_a}{2\pi T_c} \right) - \Psi \left( \frac{1}{2} \right)$

Magnetic interband-only impurities in the 2-band case:

if  $\Delta_a = -\Delta_b$  then  $\left( \frac{\tilde{\phi}_{\alpha n}}{\Delta_\alpha} \frac{1}{\tilde{\omega}_{\alpha n}} \right)_{T_c} = \frac{1}{\omega_n} \rightarrow T_c$  is not suppressed ( $s_\pm$ )



# T-matrix approximation for the impurity self-energy

$$i\tilde{\omega}_{an} = i\omega_n - \Sigma_{0a}(\omega_n) - \Sigma_{0a}^{\text{imp}}(\omega_n), \quad \tilde{\phi}_{an} = \Sigma_{2a}(\omega_n) + \Sigma_{2a}^{\text{imp}}(\omega_n)$$

$$\hat{\Sigma}^{\text{imp}}(\omega_n) = n_{\text{imp}} \hat{\mathbf{U}} + \hat{\mathbf{U}} \hat{\mathbf{g}}(\omega_n) \hat{\Sigma}^{\text{imp}}(\omega_n)$$

$$\Sigma_{aa}^{\text{imp}} = I + J \Sigma_{ba}^{\text{imp}} + I \Sigma_{aa}^{\text{imp}}$$

$$\Sigma_{ba}^{\text{imp}} = J + I \Sigma_{ba}^{\text{imp}} + J \Sigma_{aa}^{\text{imp}}$$

$n_{\text{imp}}$  is the impurity concentration  
 $I$  and  $J$  are the impurity potentials

Impurity potential  $\hat{\mathbf{U}} = \begin{pmatrix} I\hat{S} & J\hat{S} \\ J\hat{S} & I\hat{S} \end{pmatrix}$

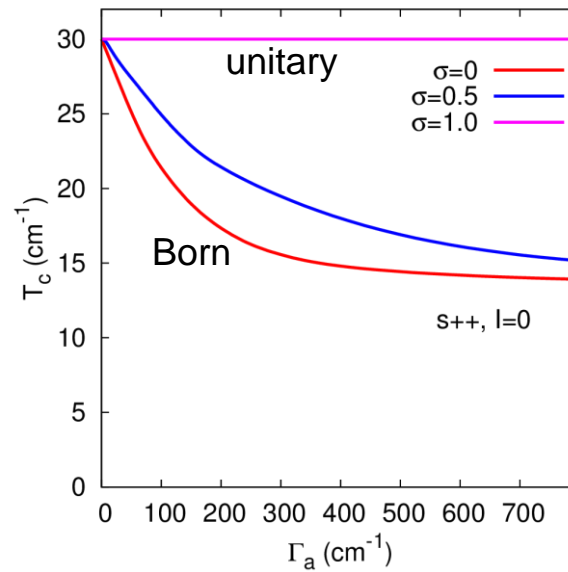
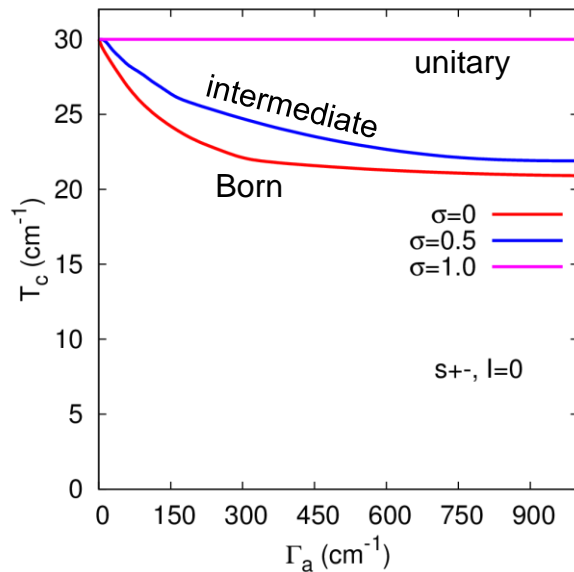
Generalized cross-section parameter  
 (helps to control the approximation)

$$\sigma = \frac{\pi^2 J^2 s^2 N_a N_b}{1 + \pi^2 J^2 s^2 N_a N_b} \rightarrow \begin{cases} 0, & \text{Born} \\ 1, & \text{unitary} \end{cases}$$

Effective impurity scattering strength

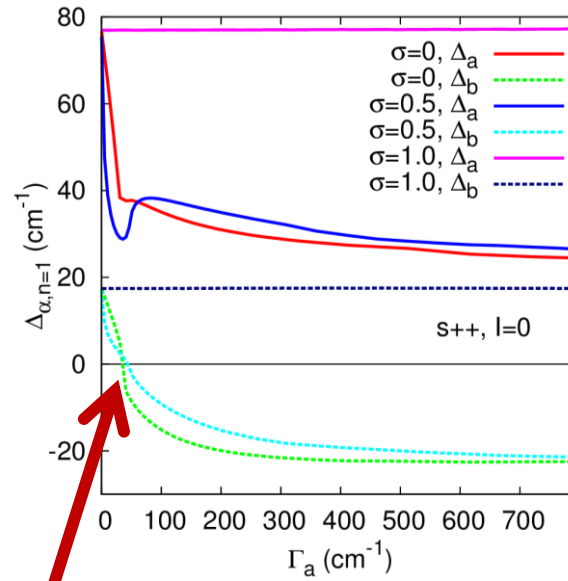
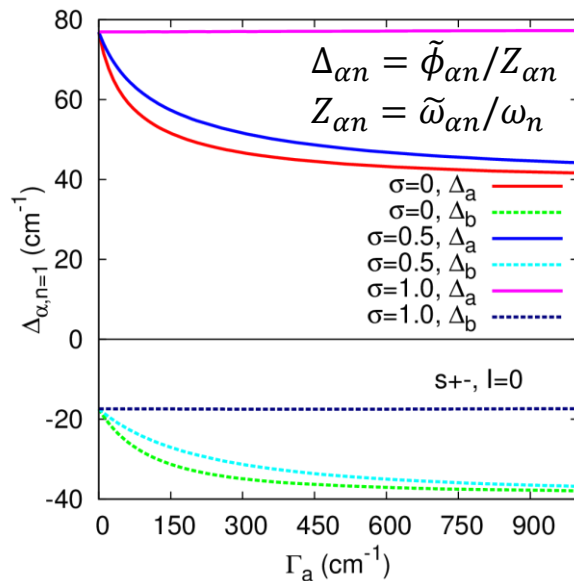
$$\Gamma_{a,b} = \frac{2n_{\text{imp}}\sigma}{\pi N_{a,b}} \rightarrow \begin{cases} 2\pi J^2 s^2 n_{\text{imp}} N_{b,a}, & \text{Born} \\ \frac{2n_{\text{imp}}}{\pi N_{a,b}}, & \text{unitary} \end{cases}$$

# Interband magnetic impurities: results for the $s_{\pm}$ and $s_{++}$ systems



**Interband-only impurities do not destroy  $s_{\pm}$  superconductivity**

This confirms qualitative arguments that  $s_{\pm}$  state with magnetic disorder behave like the  $s_{++}$  state with non-magnetic impurities [Golubov, Mazin (1995,1997)] and agrees with the Born limit results [Li, Wang, EPL 88, 17009, (2009)].



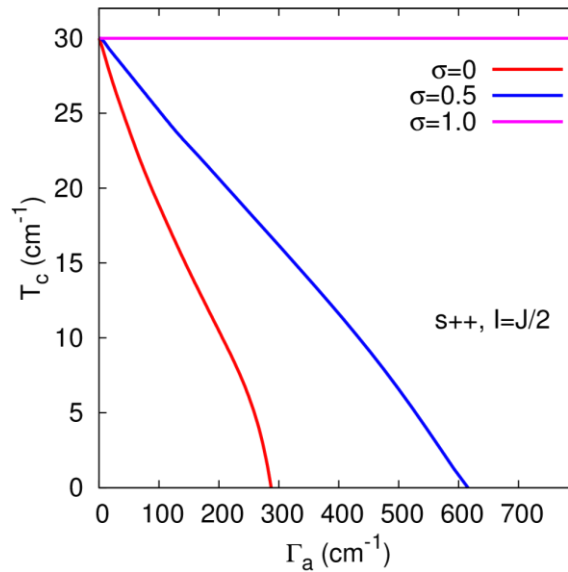
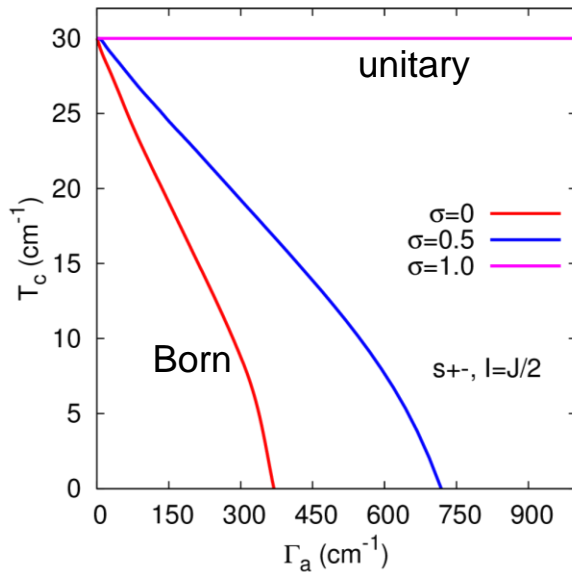
**$s_{++} \rightarrow s_{\pm}$  transition!**

Then  $T_c$  **saturates** since the **interband-only impurities do not destroy  $s_{\pm}$  state**.

It is the only way for the  $s_{++}$  state to be robust against the magnetic disorder.

Smaller gap changes sign for  $\Gamma > 40$  cm $^{-1}$ !

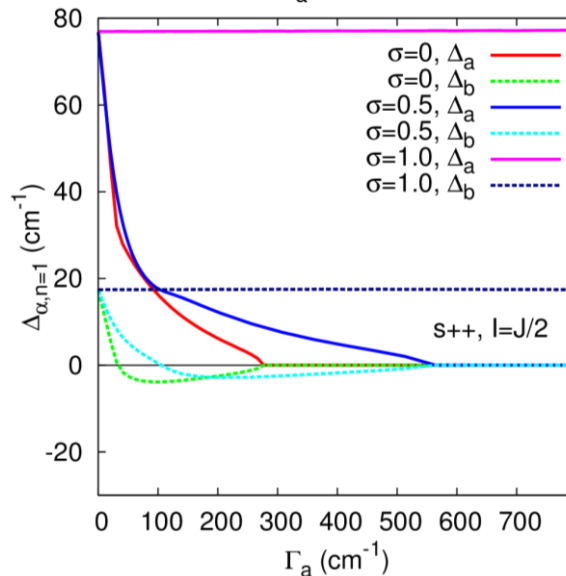
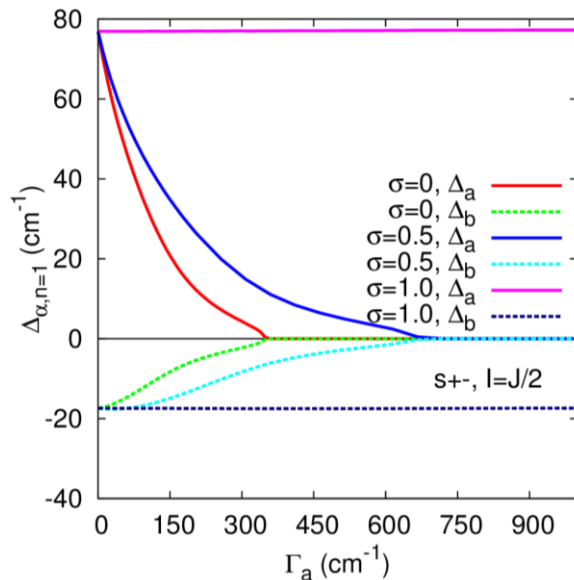
# Finite intraband magnetic disorder: $s_{\pm}$ and $s_{++}$ systems



**Interband-only**  
impurities **do not**  
destroy  $s_{\pm}$   
superconductivity, but  
**intraband do!**

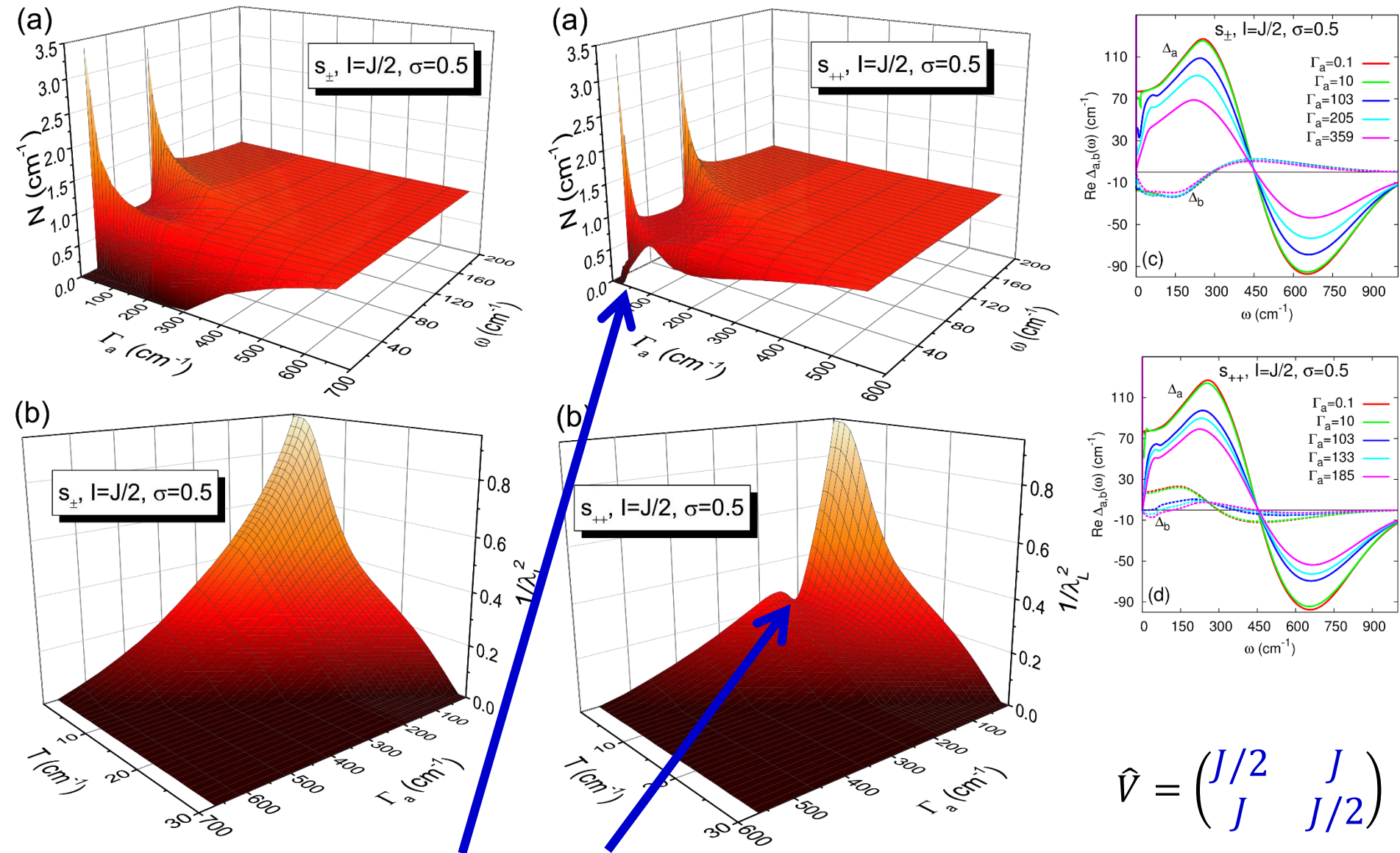
Finite intraband  
disorder finally suppress  
 $T_c$  to zero.

$s_{++} \rightarrow s_{\pm}$  transition  
can't save  $s_{++}$  state  
from being  
destroyed.



The only exception here is the  
unitary limit ( $\sigma = 1$ ). At  $T \rightarrow T_c$ :  
$$\tilde{\omega}_{an} = \omega_n + i\Sigma_{0a}(\omega_n) + \frac{\Gamma_a}{2} \text{sgn}(\omega_n)$$
  
$$\tilde{\phi}_{an} = \Sigma_{2a}(\omega_n) + \frac{\Gamma_a}{2} \frac{\tilde{\phi}_{an}}{|\tilde{\omega}_{an}|}$$

# DOS and penetration depth in $s_{\pm}$ and $s_{++}$ systems



$s_{++} \rightarrow s_{\pm}$  transition

$$\hat{V} = \begin{pmatrix} J/2 & J \\ J & J/2 \end{pmatrix}$$

$\sigma \rightarrow 0$ : Born limit  
 $\sigma \rightarrow 1$ : unitary limit

## Conclusions

- The  $T_c$  suppression is much slower than suggested in AG theory
- There are few exceptional cases with the saturation of  $T_c$  for the finite amount of magnetic impurities:
- (1)  $s_{\pm}$  superconductor with the purely interband impurity scattering potential.
- (2)  $s_{++}$  state with the interband-only scattering due to the  $s_{++} \rightarrow s_{\pm}$  transition.

Since this transition goes through the gapless regime, there should be clear signatures in the thermodynamics of the system. Therefore, it may manifest itself in optical and tunneling experiments, as well as in a photoemission and thermal conductivity on Fe-based superconductors and other multiband systems.

- (3) the unitary scattering limit