

# Strongly Correlated Superconductivity: the case of the Iron Pnictides and Chalcogenides.

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Work done in collaboration with

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nature  
physics

LETTERS

PUBLISHED ONLINE: 12 OCTOBER 2014 | DOI: 10.1038/NPHYS3116

## Spin dynamics and orbital-antiphase pairing symmetry in iron-based superconductors

Z. P. Yin\*, K. Haule and G. Kotliar

C. Aron and G. Kotliar arxiv: 1401.0331



Analytic theory of Hund's metals: a renormalization group perspective

Workshop on Probing and Understanding Exotic  
Superconductors and Superfluids

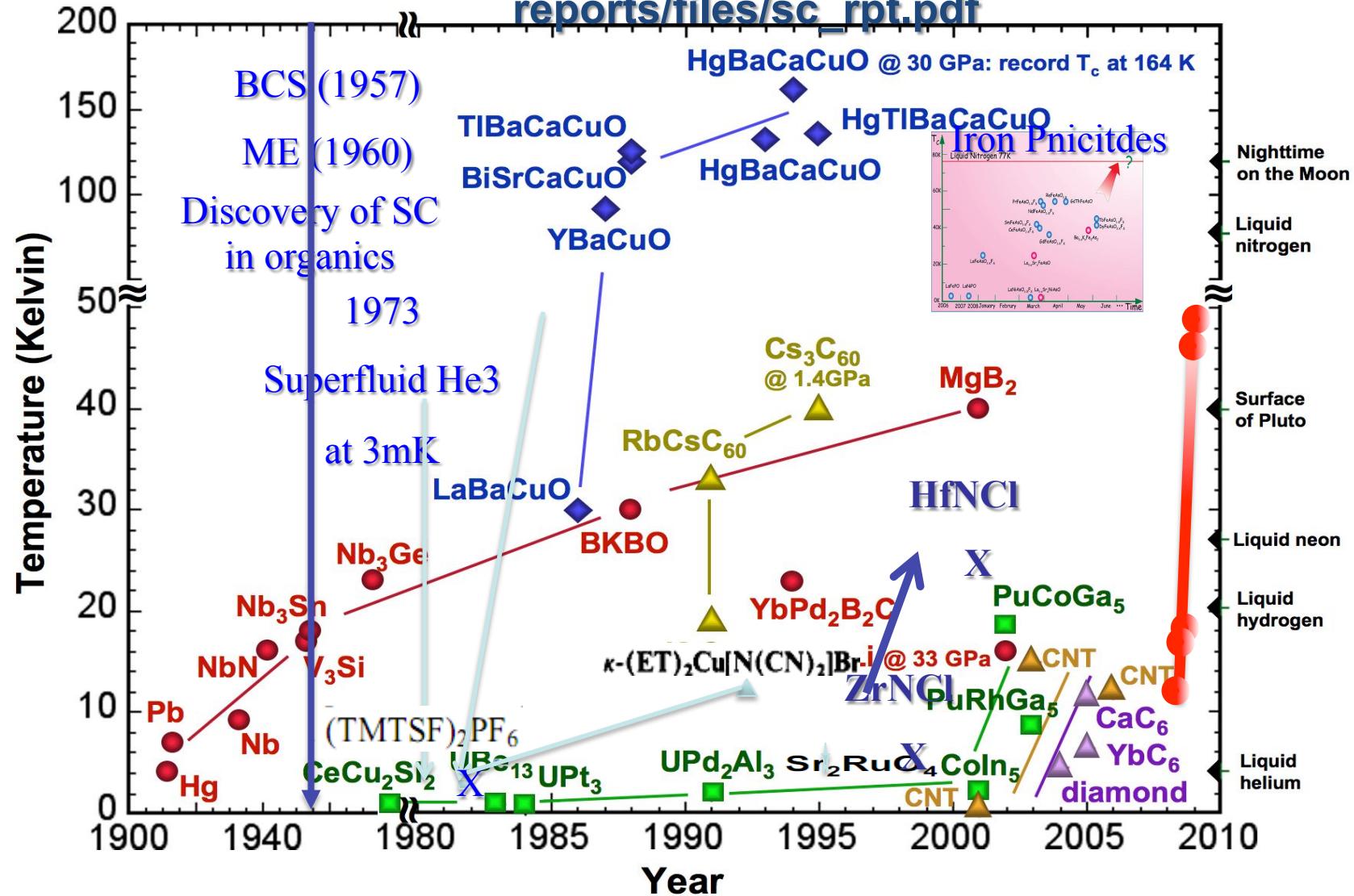
(Trieste, 27-31 October 2014).

1

# “ $T_c$ vs. Time”

[http://science.energy.gov/~media/bes/pdf/reports/files/sc\\_rpt.pdf](http://science.energy.gov/~media/bes/pdf/reports/files/sc_rpt.pdf)

2



<http://www.sc.doe.gov/bes/reports.lists.html>

Band Theory. Fermi Liquid Theory (Landau 1957).

Density Functional Theory (Hohenberg Kohn Sham 1964)

$$-\nabla^2 / 2 + V_{KS}(r)[\rho] \psi_{kj} = \varepsilon_{kj} \psi_{kj}$$

Reference Frame for  
Weakly Correlated  
Systems.

$$\rho(r) = \sum_{\varepsilon_{kj} < 0} \psi_{kj}^*(r) \psi_{kj}(r)$$

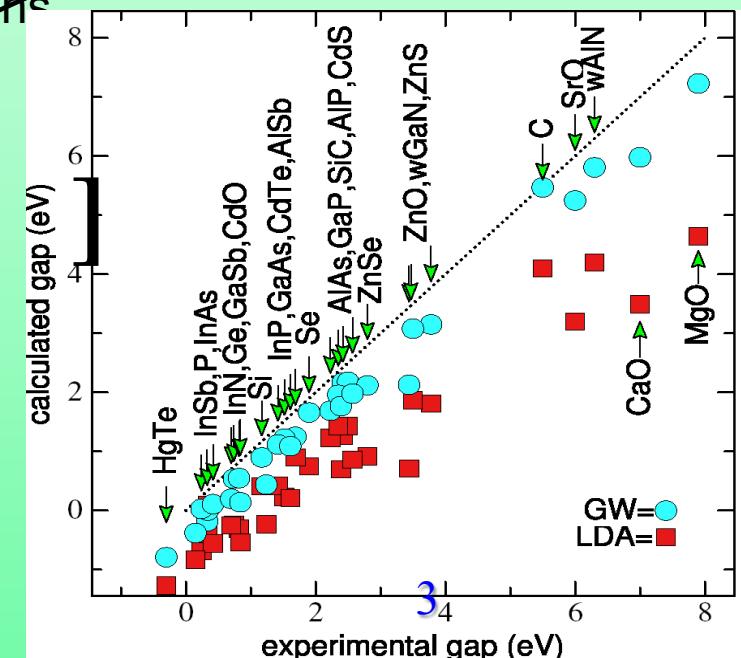
Excellent binding energies and structures /Starting point for perturbation theory GW (Hedin) in the screened Coulomb interactions

$$G^{-1} = G_{0KS}^{-1} + [ \quad \xrightarrow{\text{}} \quad - V_{KS} ]$$

Migdal Eliashberg. Controlled approximations as long as the coupling is not too strong and if

$$\omega_D \ll \varepsilon_F$$

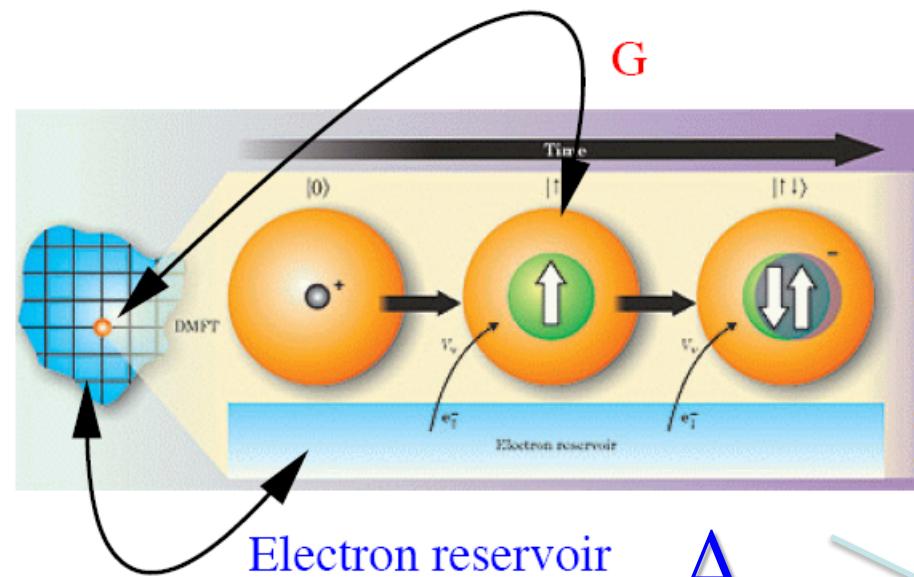
weak coupling instabilities- BCS superconductivity...





# DMFT Self consistent quantum impurity model. Reference system to study correlated electrons materials

A. Georges, G. Kotliar, W. Krauth, and M. J. Rozenberg, Rev. Mod. Phys. 68, 13 (1996)



$$\chi(\mathbf{q}, i\omega) = \text{Diagram 1} + \text{Diagram 2} + \dots$$

Diagram 1 shows a loop with a shaded block labeled  $\Gamma$ . Diagram 2 shows two blocks labeled  $\Gamma$  connected by a line.

Two particle  
irreducible vertex  
function

1 particle  
irreducible self  
energy

LDA+DMFT , Quantum  
Embedding. G. Kotliar, S. Y.  
Savrasov, K. Haule, V. S.  
Oudovenko, O. Parcollet, and C.  
A. Marianetti,RMP. 78, 865  
(2006)

$$G(\omega, r, r') = \frac{1}{[\omega + \nabla^2 + \mu \cdot \mathbf{V}_{st} - \chi_{\alpha R}^*(r) \Sigma(i\omega)_{\alpha\beta} \chi_{\beta R}(r')]} \quad \downarrow$$

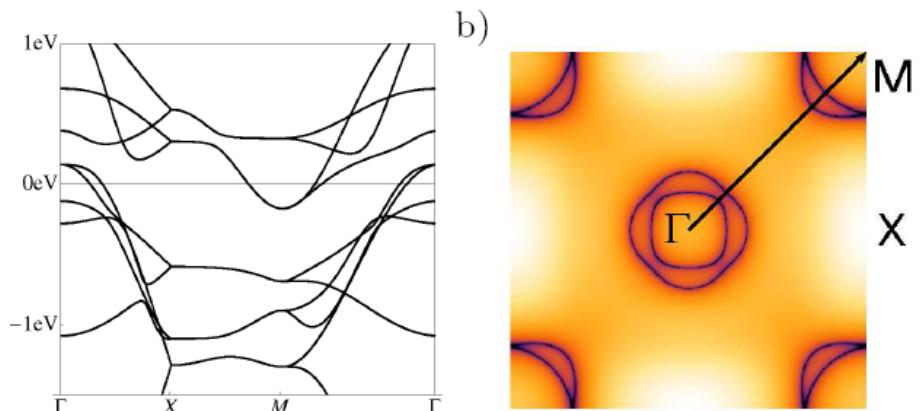
# (2008) Superconductivity in La<sub>x</sub>FeAsO<sub>1-x</sub>F<sub>x</sub>

La<sup>+++</sup> O<sup>--</sup> (LaO)<sup>+</sup> ionic-insulating  
(FeAs)<sup>-</sup> layers active block

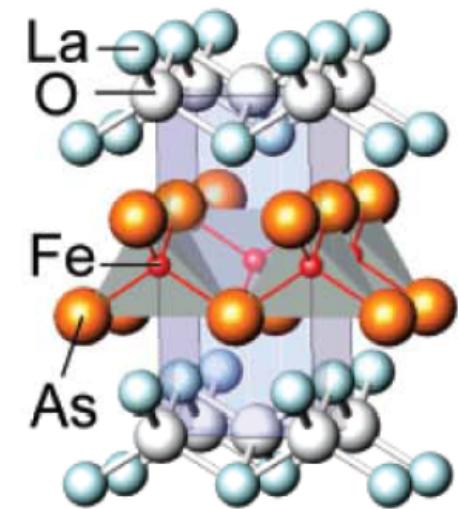
Atomic iron , [Fe] 3d6 4s2. [As]

Atomic arsenic [Ar] 3d10 4s2 4p3

Fe<sup>++</sup> d6 As<sup>---</sup> p6



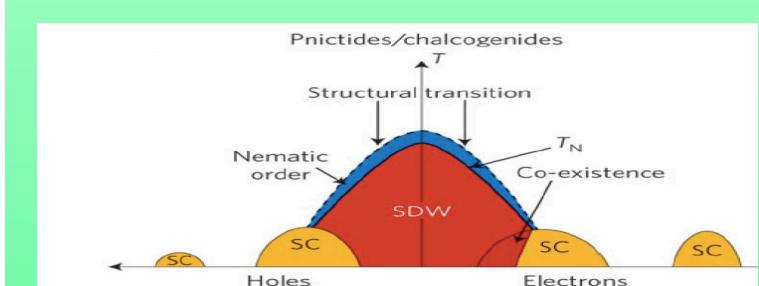
## Real Space Picture



## Momentum Space Picture

Doped Mott Insulators ?

Weakly correlated  
Itinerant magnets?  
Hunds metals ? <sup>3</sup>



# Early DMFT predictions



PRL 100, 226402 (2008)

PHYSICAL REVIEW LETTERS

week ending  
6 JUNE 2008

## Correlated Electronic Structure of $\text{LaO}_{1-x}\text{F}_x\text{FeAs}$

K. Haule, J. H. Shim, and G. Kotliar

*Department of Physics, Rutgers University, Piscataway, New Jersey 08854, USA*

(Received 9 March 2008; published 2 June 2008)

Parent  
Compound is  
a (bad)semi-  
metal.

phonon mediated. Indeed an explicit calculation of the phonon coupling constants within the DFT, using the code of Ref. [5], gives a value too small to explain the observed critical temperature ( $T_c < 1$  K).

Unconventional SC

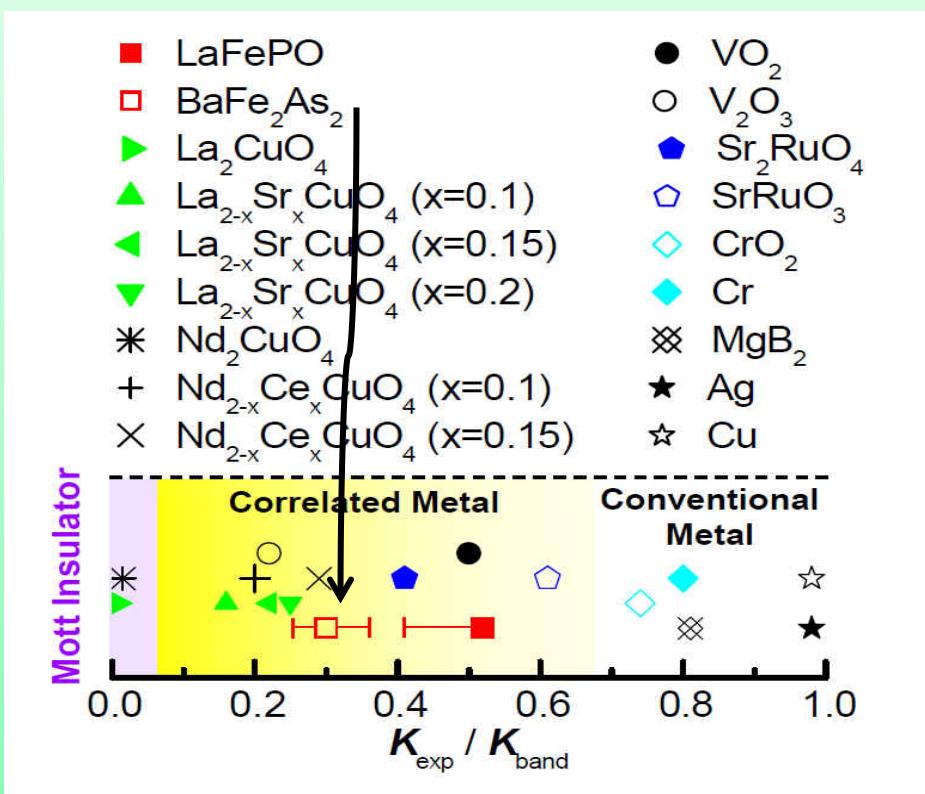
**Phonon  $T_c < 1$  K**

Fermi level. The band velocity and effective mass are considerably enhanced (3–5 times) while the scattering rate still remains large. Finally, the hole pockets around  $\Gamma$  remain highly scattered.

Importance of correlations

**Mass enhancement 3-5**

# Optical Spectroscopy can be used to determine the mass enhancement relative to the band theory mass (LDA)



LDA+DMFT had predicted correlation effects  $m/m^* \sim .3 - .2$  this WAS seen in OPTICS.

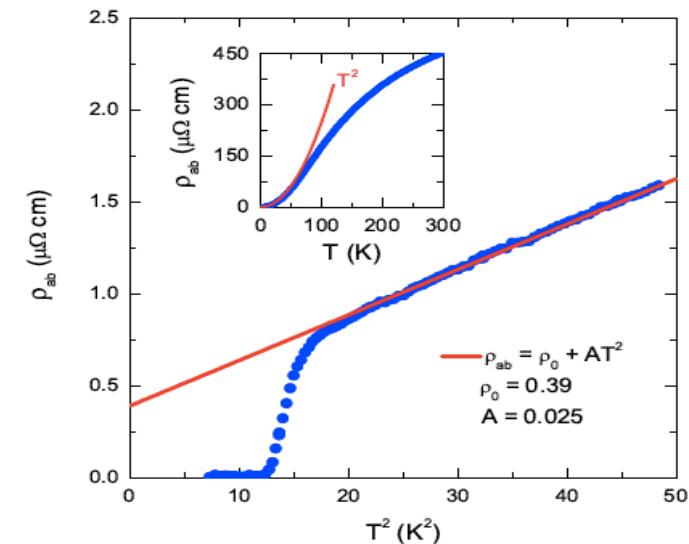
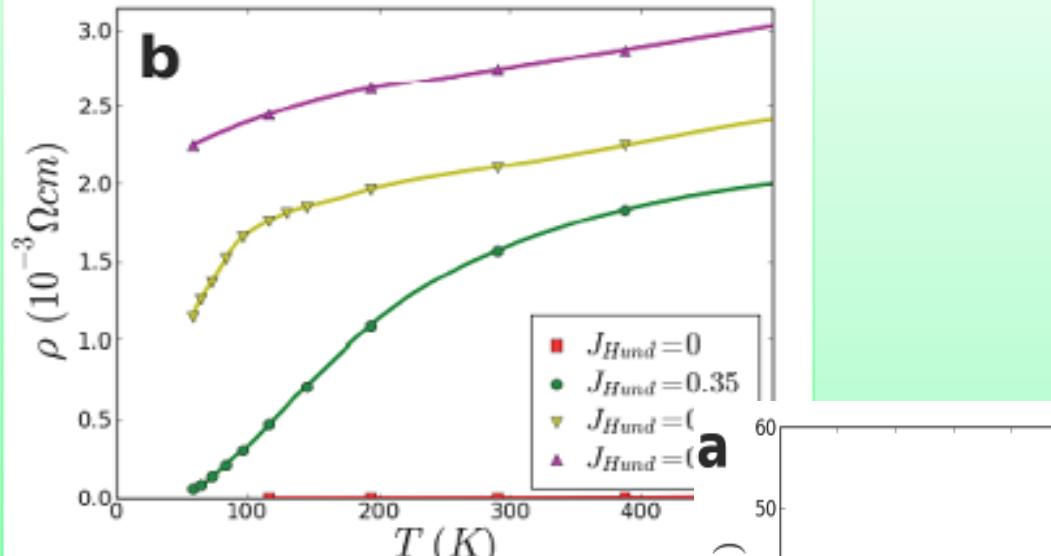
But proximity to the Mott transition can also induce Motness.

# Coherence–incoherence crossover in the normal state of iron oxypnictides and importance of Hund’s rule coupling

K Haule<sup>1</sup> and G Kotliar

Department of Physics, Rutgers University, Piscataway, NJ 08854, USA  
E-mail: [haule@physics.rutgers.edu](mailto:haule@physics.rutgers.edu)

New Journal of Physics 11 (2009) 025021



PRL 111, 027002 (2013)

PHYSICAL REVIEW LETTERS

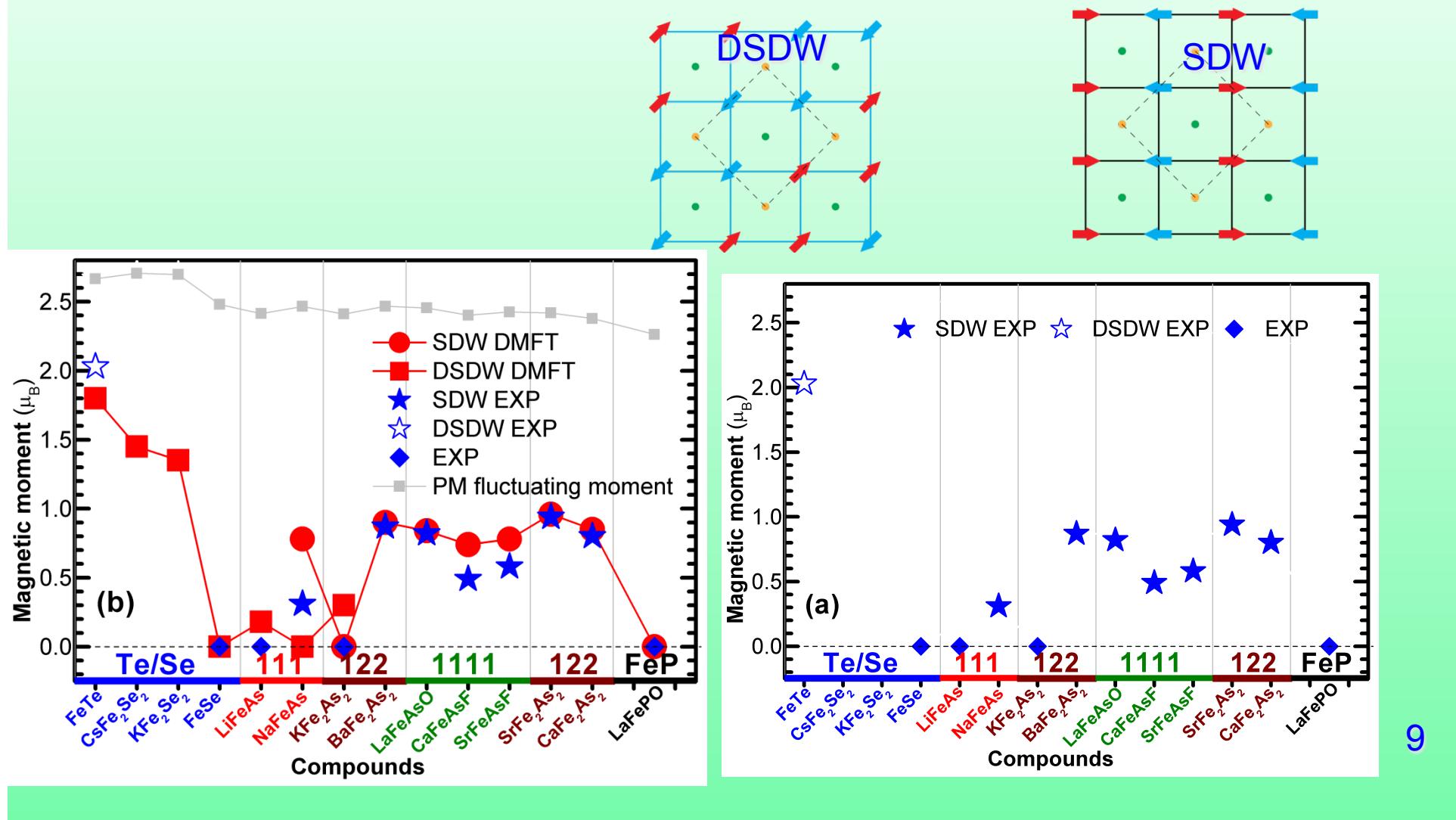
week ending  
12 JULY 2013

## Evidence of Strong Correlations and Coherence-Incoherence Crossover in the Iron Pnictide Superconductor $\text{KFe}_2\text{As}_2$

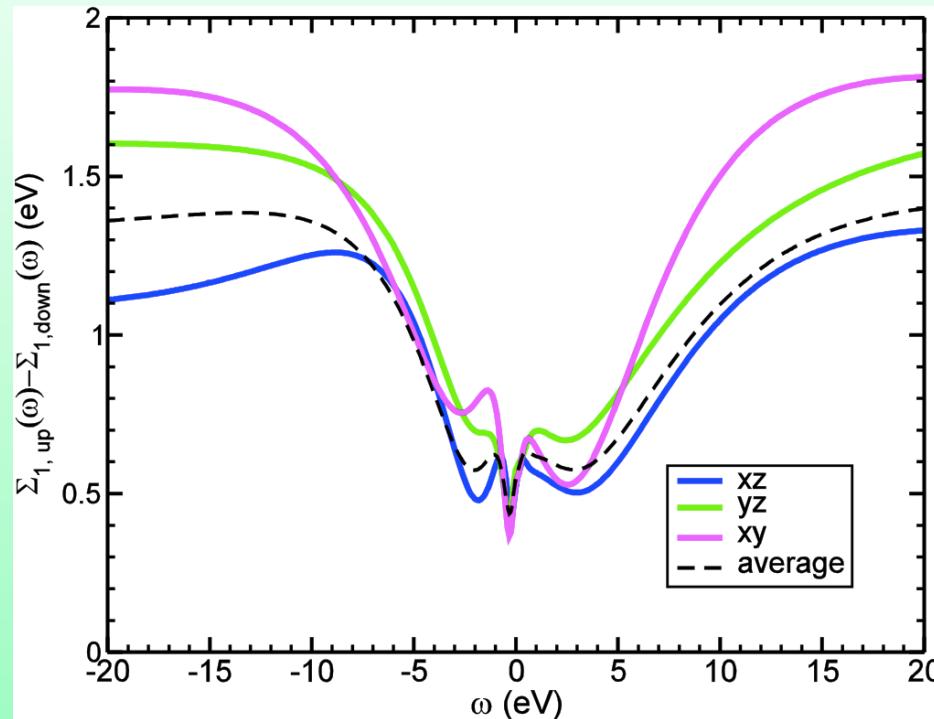
F. Hardy,<sup>1,\*</sup> A. E. Böhmer,<sup>1</sup> D. Aoki,<sup>2,3</sup> P. Burger,<sup>1</sup> T. Wolf,<sup>1</sup> P. Schweiss,<sup>1</sup> R. Heid,<sup>1</sup> P. Adelmann,<sup>1</sup> Y. X. Yao,<sup>4</sup> G. Kotliar,<sup>5</sup> J. Schmalian,<sup>6</sup> and C. Meingast<sup>1</sup>

All families share the same Fermi layers  $\text{FeAs}_2$ , similar bands

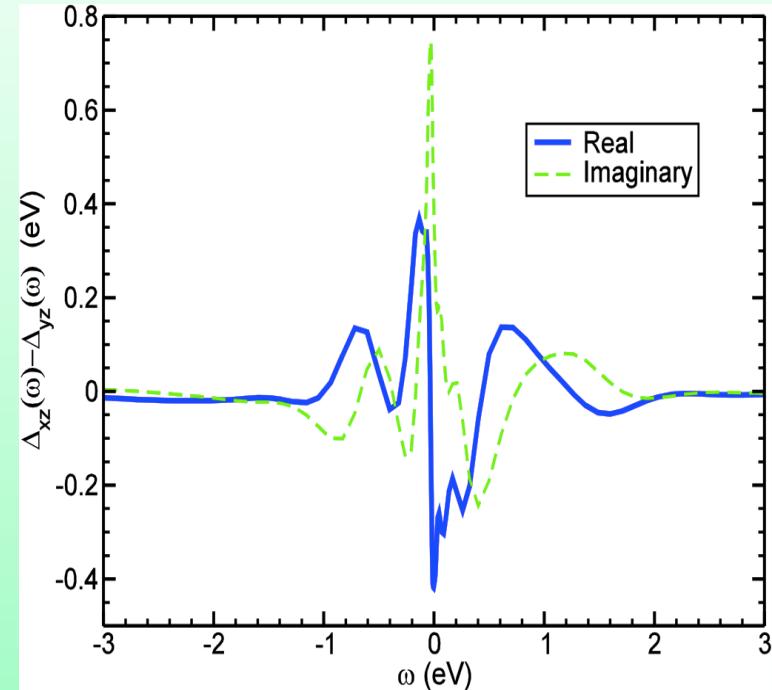
What governs the strength of the magnetism among the families ? Big window, same local interactions for all materials. Variations are in the one electron H0.



# Understanding the Stripe Phase ( and by extension the nematic phase above it )



Spin polarization large at high energy



Orbital polarization large at low energy  
(300 meV)

Spin moment lives at high energy and orbital polarization at low energy

Hundness 101 :  $Uc_2 \sim N W$ ,  $Uc_1 \sim N^5$  Orbitally degenerate systems tend to be metallic unless degeneracy is lifted

$d_5 \rightarrow d_6$

$U+4J$

$d_5 \rightarrow d_4$

$d_6 \rightarrow d_7$

$d_6 \rightarrow d_5$

VanderMarel Sawatzky

PRB 37 , 10674 (1988)

Fe d<sub>6</sub> configuration is much more metallic than the d<sub>5</sub> configuration of Mn.  
No Mott blocking!!!

$$H_{Kondo} = \sum_{k\alpha, \beta k'} J_{\alpha\beta} d_{\alpha}^{+} \vec{\sigma} d_{\beta} \cdot c_{\alpha k}^{+} \vec{\sigma} c_{\beta k'}$$

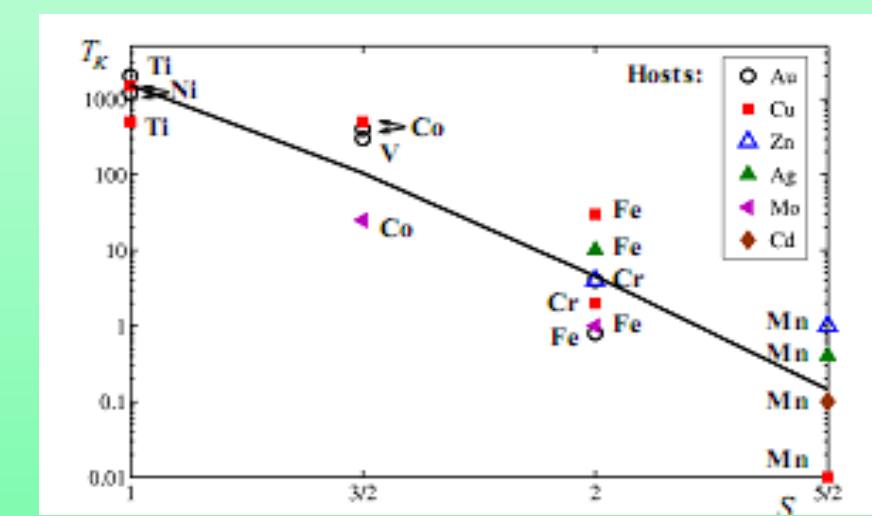
$$J_{\alpha\beta} = J$$

$$T_K = e^{-\frac{1}{\rho J N}}$$

$$J_{\alpha\beta} = J \delta_{\alpha\beta}$$

$$T_K = e^{-\frac{N}{\rho J}}$$

L<sub>1</sub> Extreme low energy scale Hundness reduce  
L<sub>2</sub> in the coherence scale of the resonance by  $N^2$   
(1973).



J. R. Schrieffer J. Applied Physics 32 , 1143 (1967)

# Hundness 102 RG Eq for the Hunds metal. C. Aron and GK arxiv: 1401.0331 M orbitals N spins

Intermediate  
assymptotic  
multichannel fixed  
point K=2.N

$$H_{\text{int}} = \dots + J_0 S^\alpha (\psi_{m\sigma}^\dagger \frac{\sigma_{\sigma\sigma'}^\alpha}{2} \psi_{m\sigma'}) + K_0 T^a (\psi_{m\sigma}^\dagger \frac{\tau_{mm'}^a}{2} \psi_{m'\sigma}) + I_0 S \quad \text{FERROMAGNETIC SIGN}$$

for hole doping!

(4)

$$\beta_J = -\frac{N}{2} \left(1 - \frac{M}{2} J\right) \left(J^2 + \frac{C_2^T}{2M} I^2\right) + \dots, \quad \text{liquid fixed point}$$

$$\beta_K = -\frac{M}{2} \left(1 - \frac{N}{2} K\right) \left(K^2 + \frac{C_2^S}{2N} I^2\right) + \dots, \quad \text{is delayed Schrieffer effect for a long time}$$

$$\beta_I = -\frac{MN}{4} \left[ \left(\frac{4}{M} J + \frac{4}{N} K - J^2 - K^2\right) I + \left(\frac{C_3^T}{NC_2^T} + \frac{C_3^S}{NC_2^S}\right) I^2 + \left(\frac{1}{4} - \frac{C_2^T}{2M} - \frac{C_2^S}{2N}\right) I^3 \right] + K_0 = \frac{2}{N} \left[ \frac{1}{\Delta E^-} + \frac{N+n_d}{n_d+1} \frac{1}{\Delta E^+} \right] V^2,$$

$$I_0 = 4 \left[ \frac{1}{n_d} \frac{1}{\Delta E^-} + \frac{1}{n_d+1} \frac{1}{\Delta E^+} \right] V^2,$$



See also Akahnjee and Tsevlik PRB 87, 195137 (2013)  
and Tsen and Coleman PRL (2012)

# Simple Impurity model

Explains the origin of the low energy scale in the model with Hunds coupling.

$$T_K^K \approx \exp(-2/MK_0)D_0, T_K^I \approx \exp(-4/M^2I_0)D_0 \\ \text{and } T_K^J \approx \exp(-2/NJ_0)D_0 \text{ if } J_0 > 0,$$

$$q \equiv M/N$$

$$T_K(d) \approx \exp(-q/d) T_K^K .$$

Explains the dependence of the coherence scale of the impurity on filling.

d distance from half filled shell.

- Explains particle hole asymmetry around d<sup>6</sup> Co doping on Fe vs K doping on Ba. d6. neq.d5

Explain the power laws observed in the optical conductivity of other Hunds metals SrRuO<sub>3</sub> Y. S. Lee et al., Phys. Rev. B 67, 113101 (2003).and in DMFT studies of 3 band models ( Werner P. Werner, E. Gull, M. Troyer, and A. J. Millis, Phys.Rev. Lett. 101, 166405 (2008).)

Explains the different formalizations of the spin and orbital susceptibilities above the Fermi liquid coherence scale.

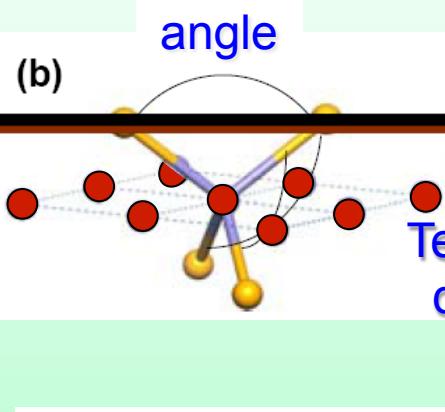
$$\chi_{S/T}(T) \sim \frac{1}{T} \exp \left( - \int_T^{D_0} \frac{dD}{D} \gamma_{S/T} (J_i(D)) \right) ,$$

$$MN(K^2 + C_2^S I^2/2)/2.$$

$$MN(J^2 + C_2^T I^2/2)/2$$

# Landscape of Materials: Nature Materials

10,:932–935:(2011)

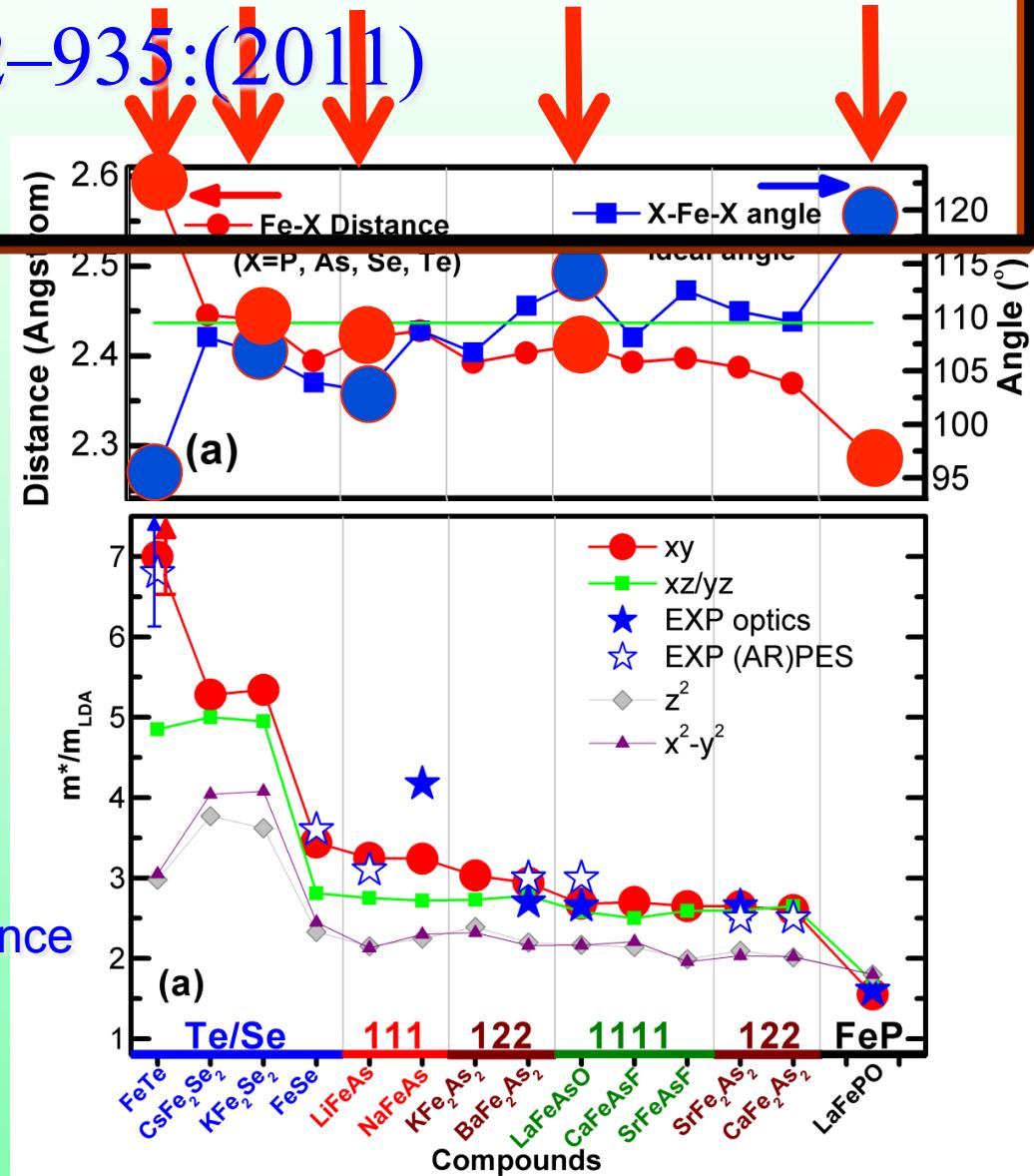


Tendency to orbital differentiation as correlations increase.



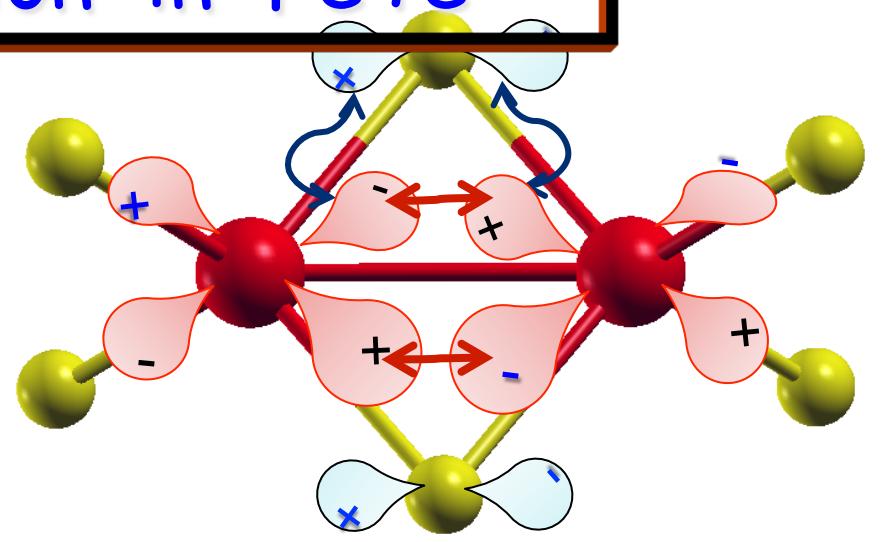
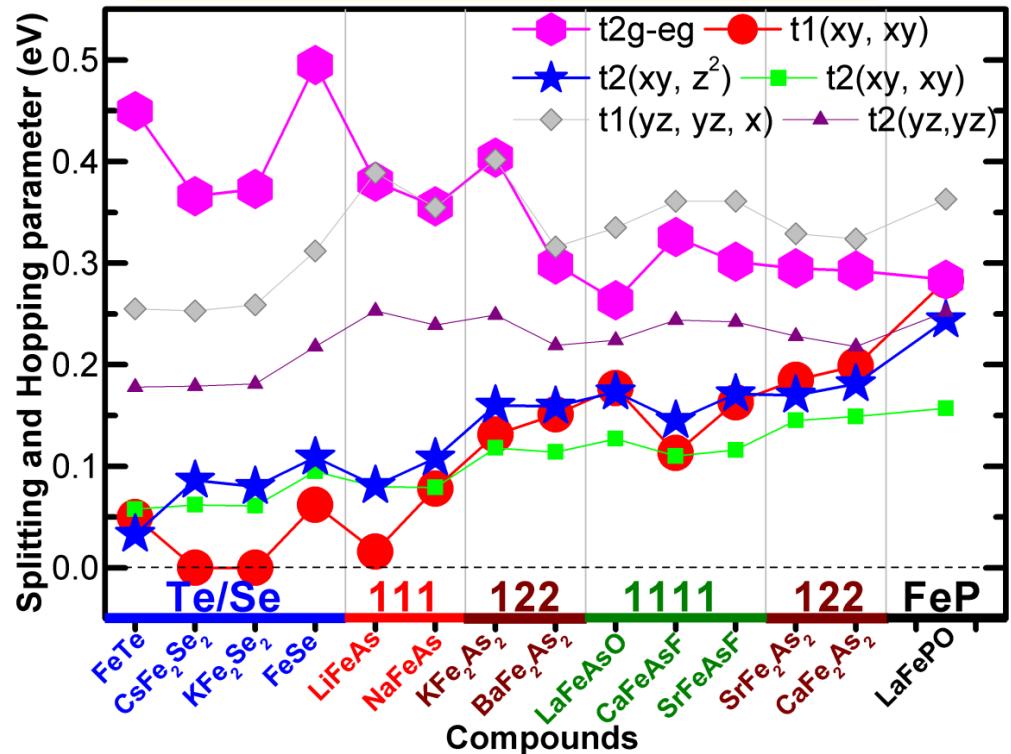
Overall trend consistent with Fe-As distance

Hybridization with pnictogen



# Orbital Differentiation and Kinetic frustration in FeTe

## Effective low energy hoppings



$$t_{xy,xy}^{direct} < 0$$

$$t_{xy,xy}^{As} > 0$$

$t^{As}$  usually larger, but not

when pnictogen height large

Destructive interference leads to kinetic frustration

Factors that govern the correlation ndLiebsch Ishida Phys. Rev. B 81, 054513 (2008) Yin Haule and Kotliar Phys. Rev. B 86, 195141 (2012)

## ORBITAL DIFFERENTIATION

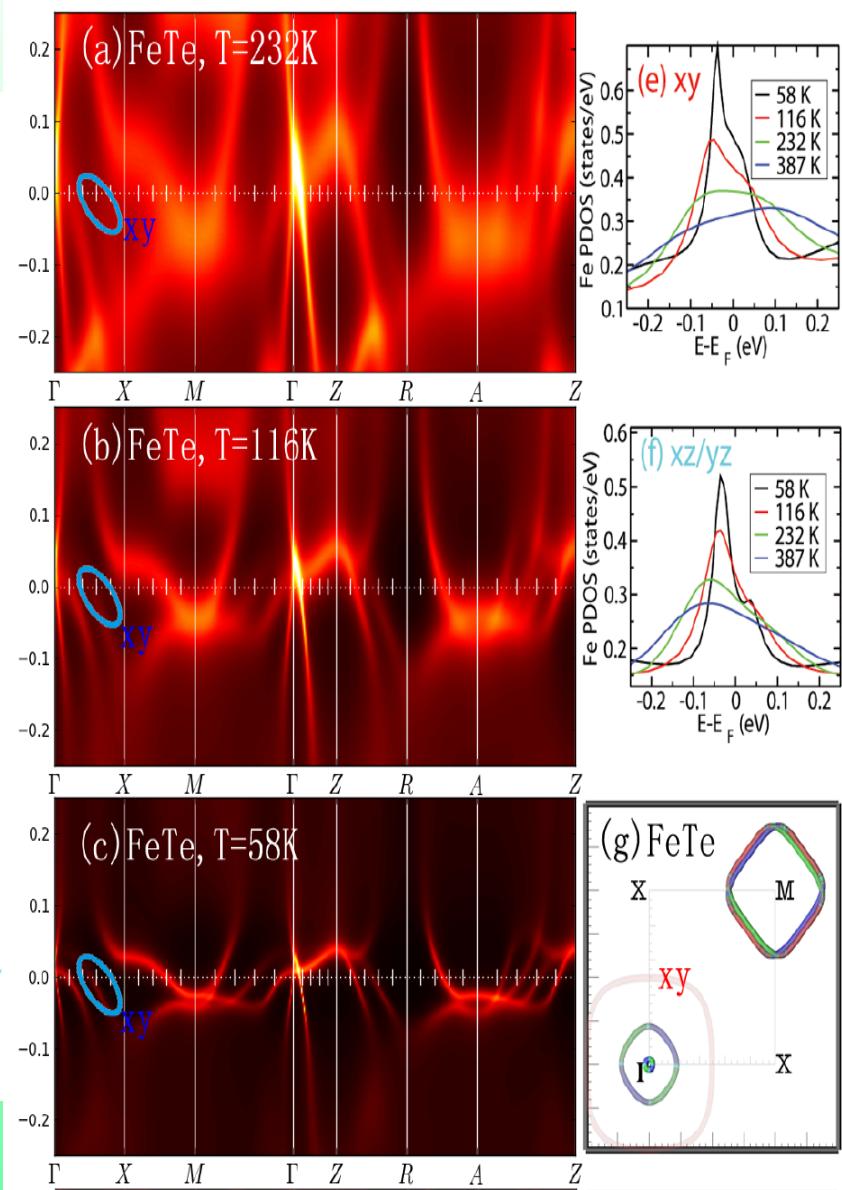
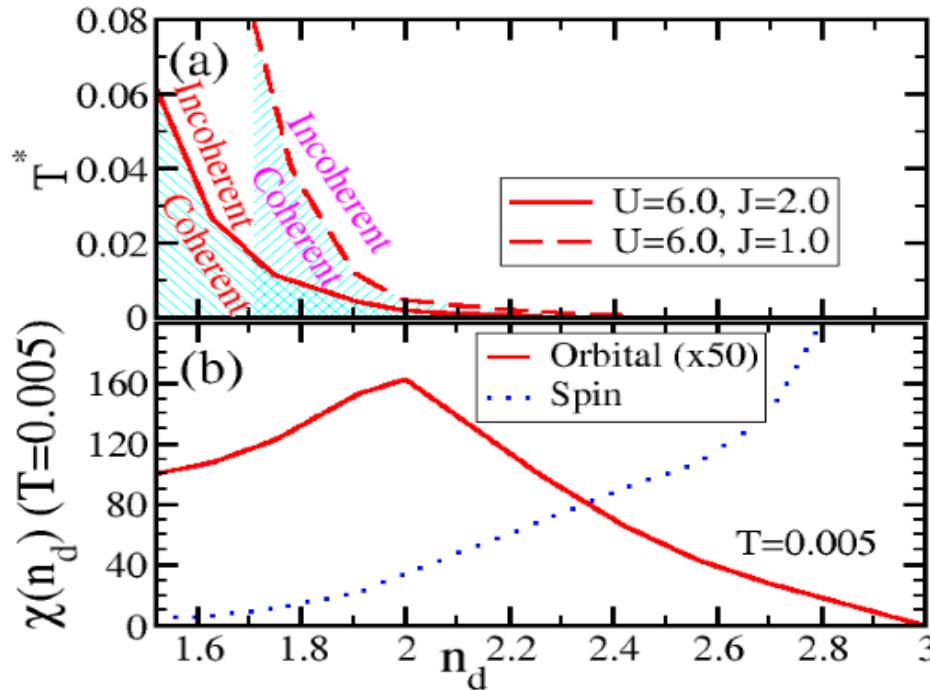


FIG. 4: (color online) (a) The coherent temperature; and (b) the spin and orbital susceptibility, as a functional of  $n_d$  for a three band model with  $J_H = 2.0$  (solid lines) and  $J_H = 1.0$  (dash lines).

Theory: H. Park , K. Haule and GK

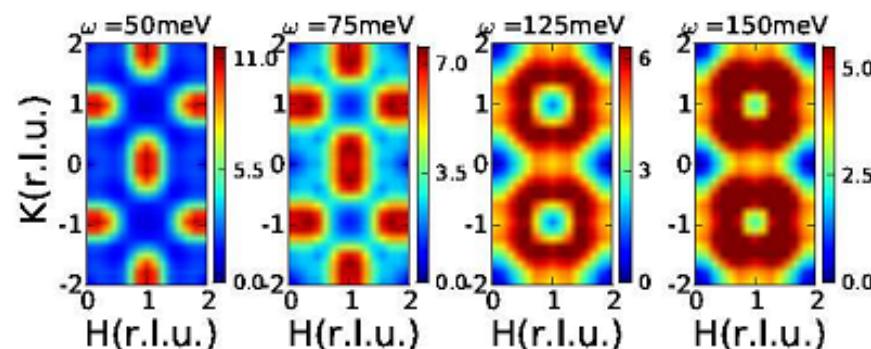
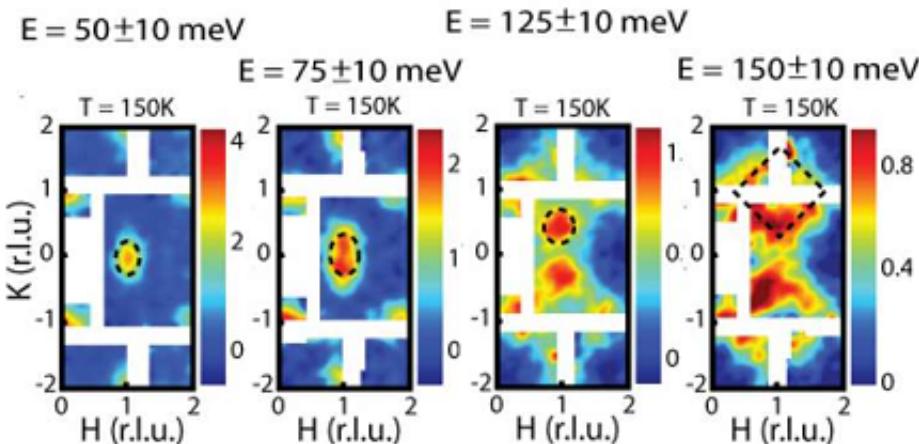
Phys. Rev. Lett. 107, 137007 (2011).

L Harriger H. Luo M. Liu T. Perring C Frost  
H. Ju M. Norman and Pengcheng Dai :  
PRB 84, 054544

$$SJ_{1a} \approx 59.2 \text{ meV}$$

$$SJ_{1b} \approx -9.2 \text{ meV}$$

$$SJ_2 \approx 13.6 \text{ meV}$$

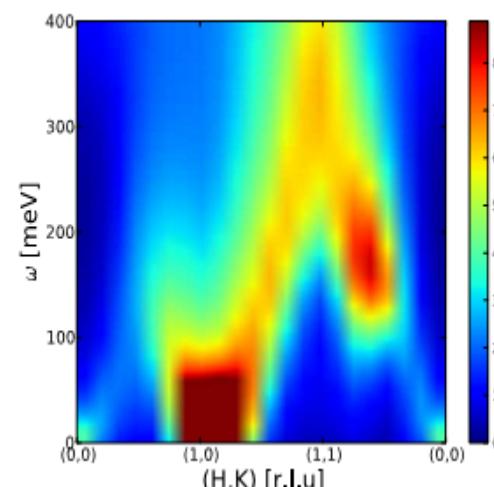
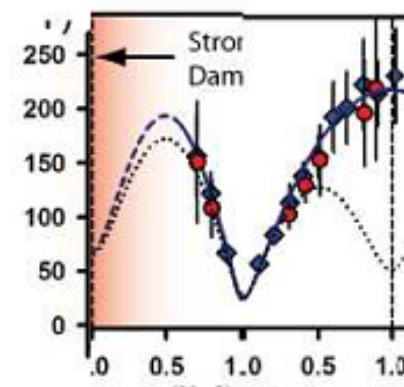


$$S(\mathbf{Q}, \hbar\omega) = |F(\mathbf{Q})|^2 \frac{\chi''(\mathbf{Q}, \hbar\omega)}{1 - \exp(-\hbar\omega/k_B T)}.$$

$$\chi(\mathbf{q}, i\omega) = \langle \text{Diagram 1} \rangle + \langle \text{Diagram 2} \rangle + \langle \text{Diagram 3} \rangle + \dots$$

Diagram 1: A single loop with a shaded central region labeled  $\Gamma$ .

Diagram 2: A sequence of three loops connected by vertical lines, with shaded regions labeled  $\Gamma$  at the top and bottom of each loop.



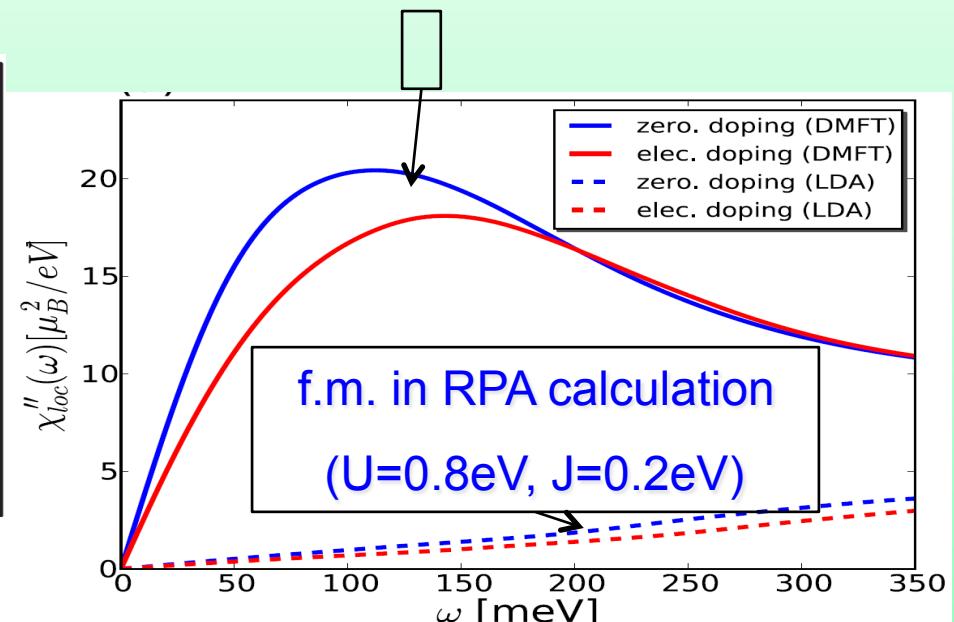
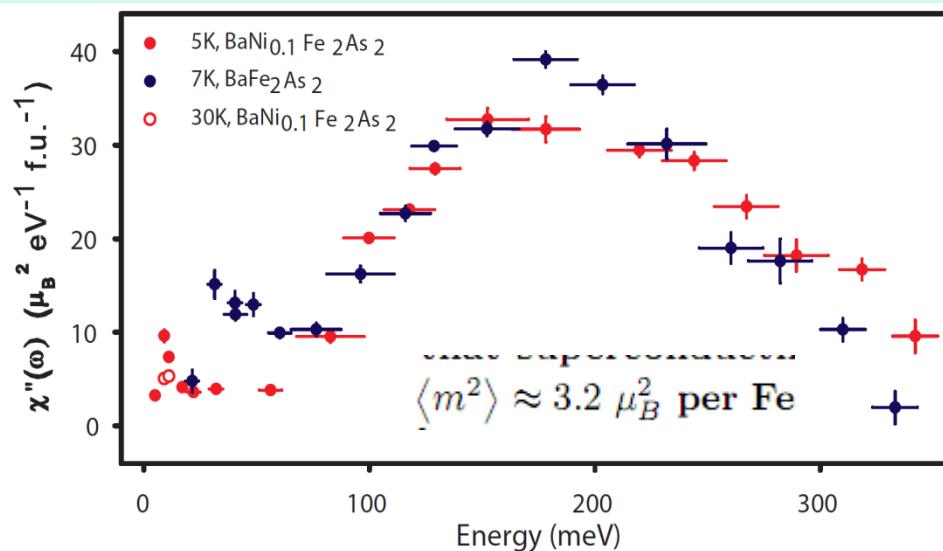
# Needed absolute intensities

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Fluctuating moment by neutrons:

$$\langle u^2 \rangle = \int \frac{d\omega}{\pi} n(\omega) \chi''(\omega)$$

Experiment by Liu ... Pengcheng Dai



Large fluctuating moment can not be explained by a purely itinerant model- doping dependence different than in localized model.  
Understandable in the Hunds metal picture.

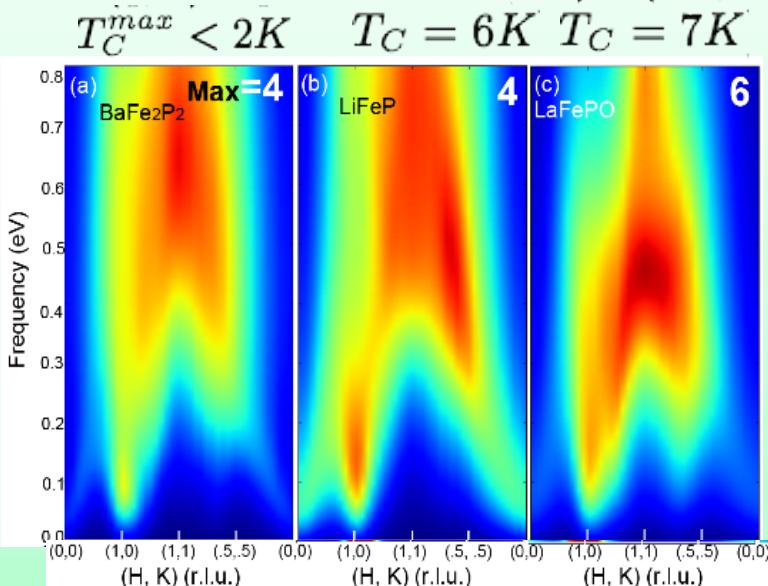
Nature Physics 8, 376-381 (2012)

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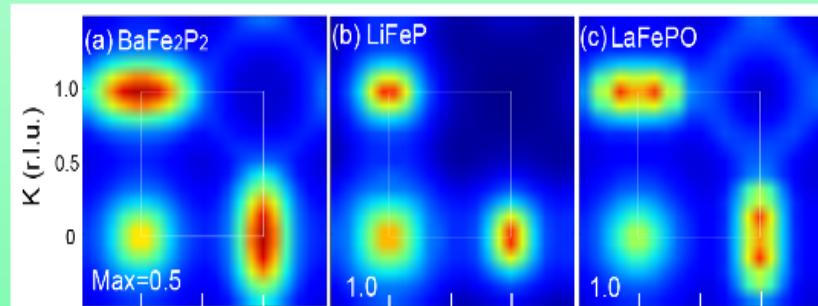
Nature of magnetic excitations in superconducting  $BaFe_{1.9}Ni_{0.1}As_2$

Mengshu Liu,<sup>1</sup> Leland W. Harriger,<sup>1</sup> Huiqian Luo,<sup>2</sup> Meng Wang,<sup>2,1</sup> R. A. Ewings,<sup>3</sup> T. Guidi,<sup>3</sup> Hyowon Park,<sup>4</sup> Kristjan Haule,<sup>4</sup> Gabriel Kotliar,<sup>4</sup> S. M. Hayden,<sup>5</sup> and Pengcheng Dai<sup>1, 2, 6,\*</sup>

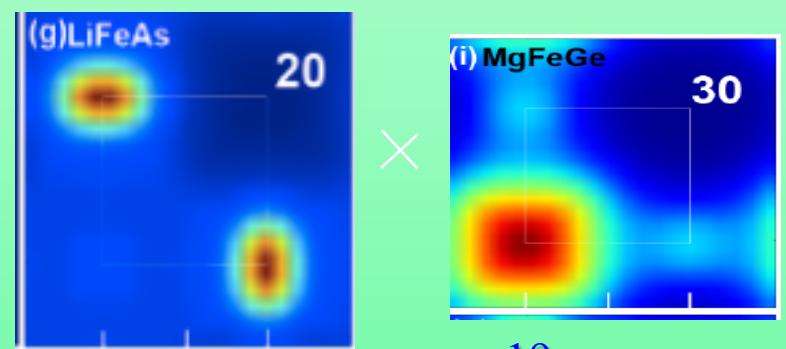
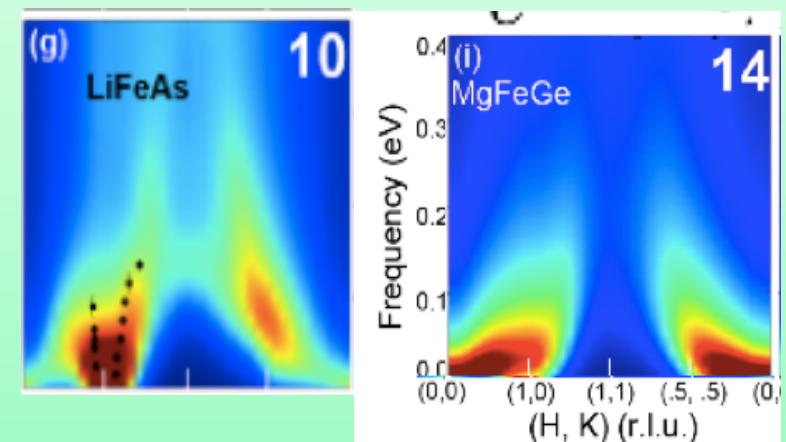
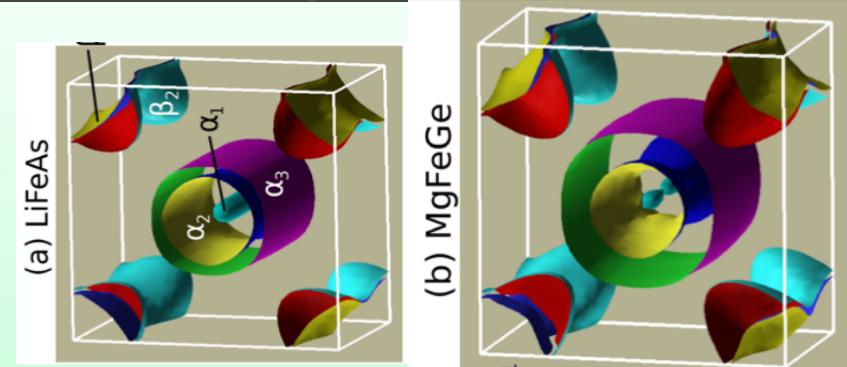
# Evaluation of $S(q, \omega)$ for many families



Very small low energy intensity  
competing order at (0,0)!

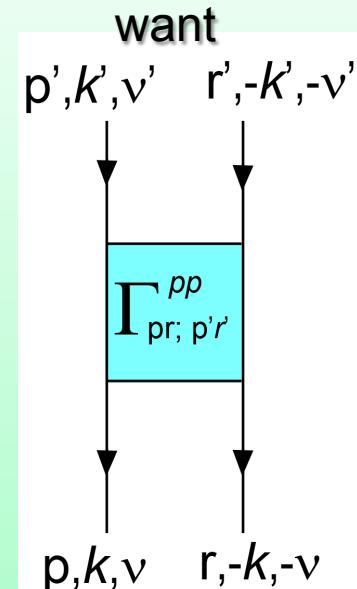
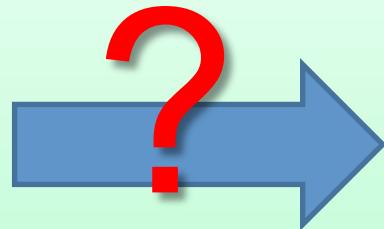
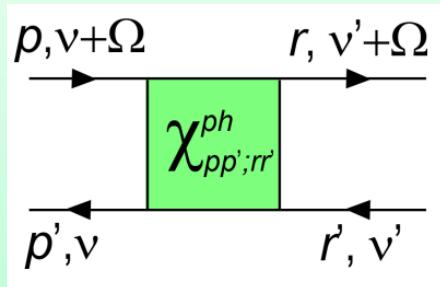


Z. Yin K. Haule and G. Kotliar Nature Physics Letters (2014)

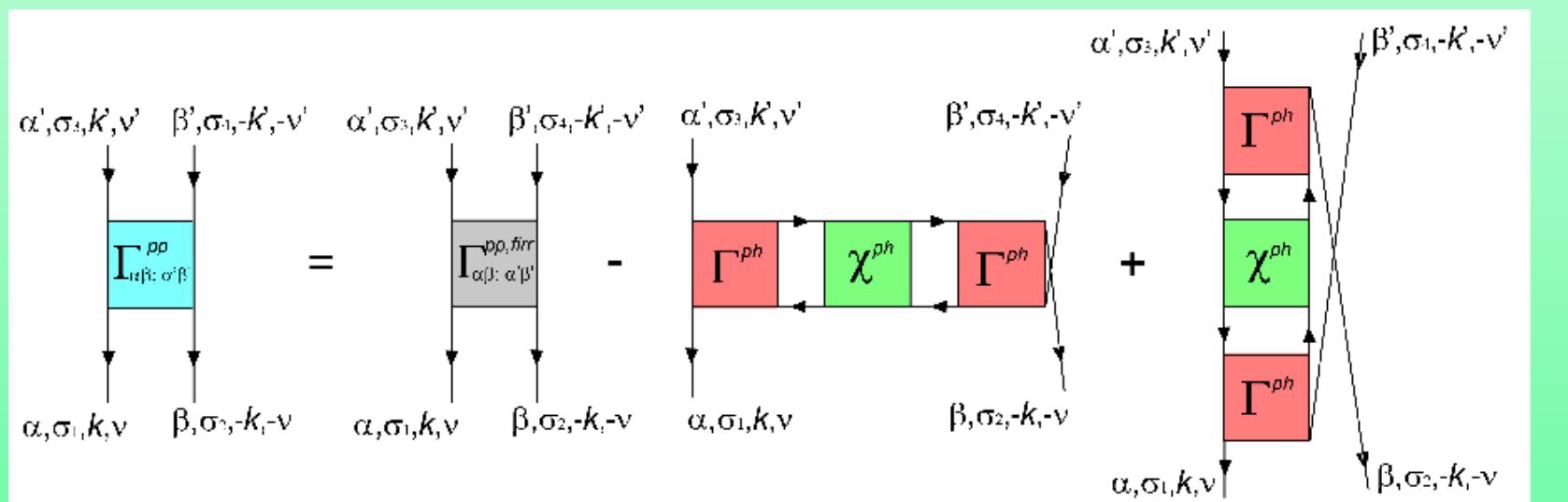


Z. Yin K. Haule and G. Kotliar  
Nature Physics Letters (2014)

have particle hole



We can compute particle-particle vertex using local irreducible objects. :



# Pairing function

$$\Delta(k)\alpha\beta = \langle d_\alpha(-k)d_\beta(k) \rangle$$

$\Delta_{\alpha\beta}(k)$  is diagonal

$$\Delta_{\alpha\beta}(k) = \Delta_{\alpha\alpha}(k)\delta_{\alpha\beta}$$

$$\begin{bmatrix} \Delta_{eg} & 0 & 0 & 0 \\ 0 & \Delta_{xz} & 0 & 0 \\ 0 & 0 & \Delta_{yz} & 0 \\ 0 & 0 & 0 & \Delta_{xy} \end{bmatrix}$$

$$\Delta_\alpha(kx, ky) = \Delta_{nnn,\alpha} \cos(kx) \cos(ky) + \Delta_{nn,\alpha} (\cos(kx) + \cos(ky))/2$$

$$|\Delta_{nn,\alpha}| \ll |\Delta_{nnn,\alpha}|$$

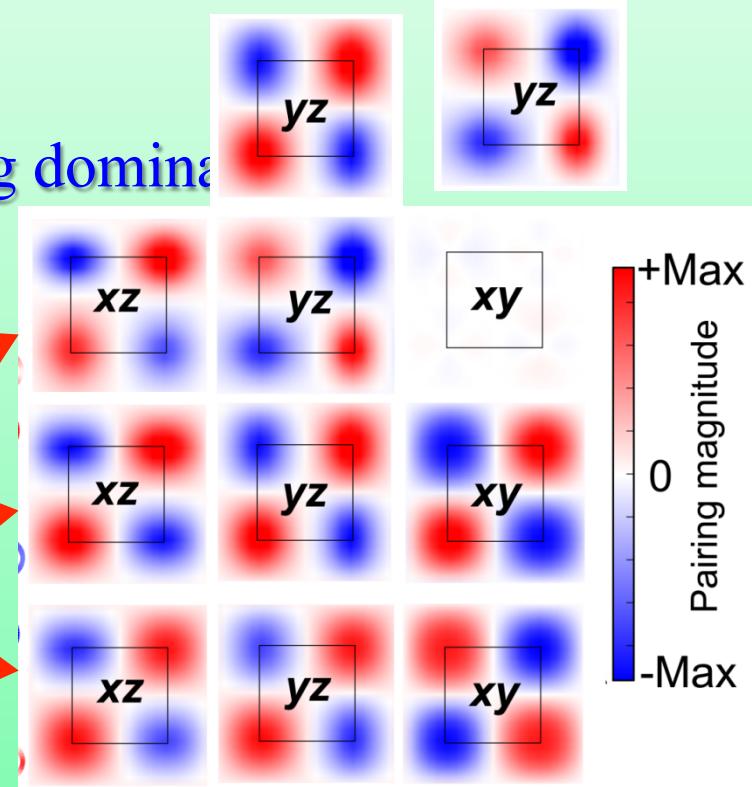
- Second nearest neighbor pairing dominates

Different combinations of the signs  $\Delta_{nnn,\alpha}$  of the (xz, yz, xy) orbitals produce different pairing symmetry on the Fermi surface.

d-wave:  $(1, -1, 0)$

Kuroki - Mazin  $S^{+-}$  :  $(1, 1, 1)$

A new antiphase  $S^{+-}$  :  $(1, 1, -1)$

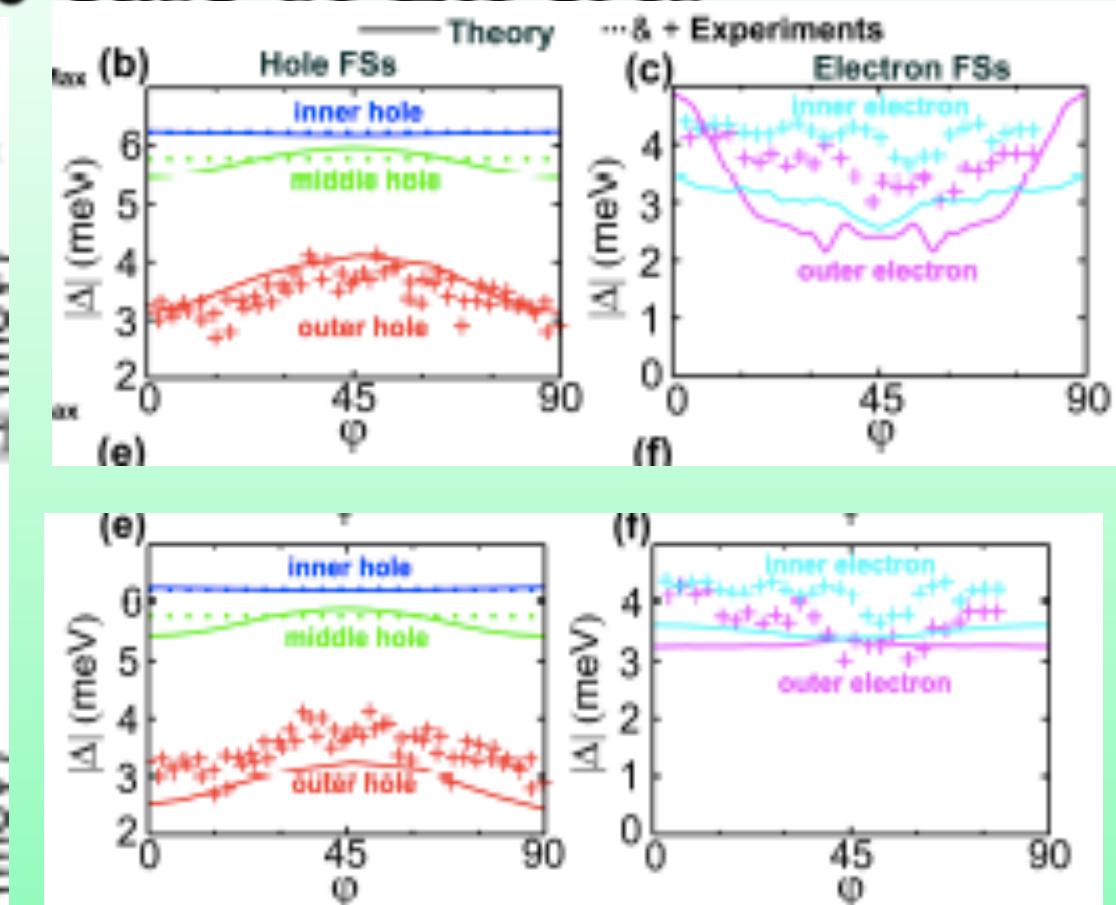
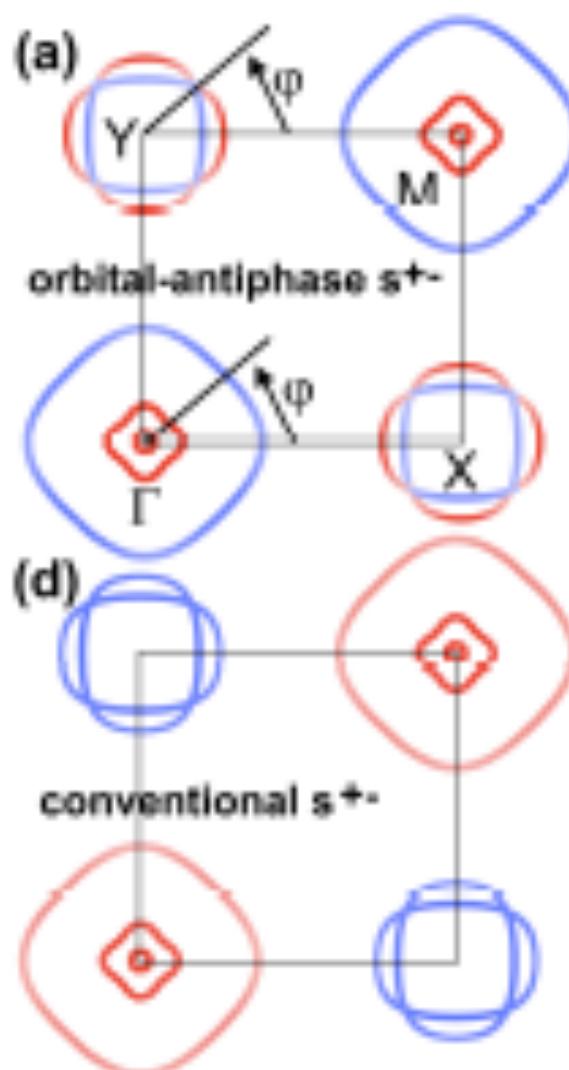


They are very close in energy and almost degenerate!

Z.P. Yin, K. Haule, G. Kotliar, Nature Physics Letters 2014

# Conventional vs antiphase orbital s+- the case of LiFeAs

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Experimental Results from Review : Borisenko,S.  
V. et al Symmetry 4, 251-264 (2012);

Theory: Yin Haule and GK, Nature Physics  
Letters (2014)      22

## Local Self-Energy Approach for Electronic Structure Calculations

N. E. Zein,<sup>1,2</sup> S. Y. Savrasov,<sup>2</sup> and G. Kotliar<sup>3,4</sup>

<sup>1</sup>RRC “Kurchatov Institute”, Moscow 123182, Russia

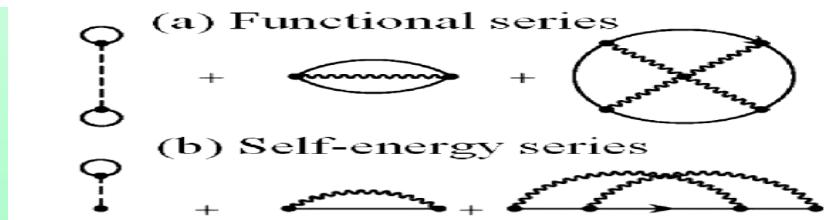
<sup>2</sup>Department of Physics, University of California, Davis, California 95616, USA

<sup>3</sup>Center for Material Theory, Department of Physics and Astronomy, Rutgers University, Piscataway, New Jersey 08854, USA

<sup>4</sup>École Polytechnique, 91128 Palaiseau Cedex, France

(Received 29 November 2005; published 7 June 2006)

Using a novel self-consistent implementation of Hedin’s *GW* perturbation theory, we calculate space- and energy-dependent self-energy for a number of materials. We find it to be local in real space and rapidly convergent on second- to third-nearest neighbors. Corrections beyond *GW* are evaluated and shown to be completely localized within a single unit cell. This can be viewed as a fully self-consistent implementation of the dynamical mean field theory for electronic structure calculations of real solids



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## Many-Body Effects in Iron Pnictides and Chalcogenides: Nonlocal Versus Dynamic Origin of Effective Masses

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We apply the quasiparticle self-consistent *GW* approximation (QSGW) to some of the iron pnictide and chalcogenide superconductors. We compute Fermi surfaces and density of states, and find excellent agreement with experiment, substantially improving over standard band-structure methods. Analyzing the QSGW self-energy we discuss nonlocal and dynamic contributions to effective masses. We present evidence that the two contributions are mostly separable, since the quasiparticle weight is found to be essentially independent of momentum. The main effect of nonlocality is captured by the static but nonlocal QSGW effective potential. Moreover, these nonlocal self-energy corrections, absent in, e.g., dynamical mean field theory, can be relatively large. We show, on the other hand, that QSGW only partially accounts for dynamic renormalizations at low energies. These findings suggest that QSGW combined with dynamical mean field theory will capture most of the many-body physics in the iron pnictides and chalcogenides.

$$\Sigma(k, \omega) \approx \Sigma(k) + |R\alpha\rangle \sum_{locRR\alpha\beta} (\omega) \langle R\beta|$$

# Studying the d<sup>5</sup> : the case of LaMnPO. [Mn analog of LaFePO]

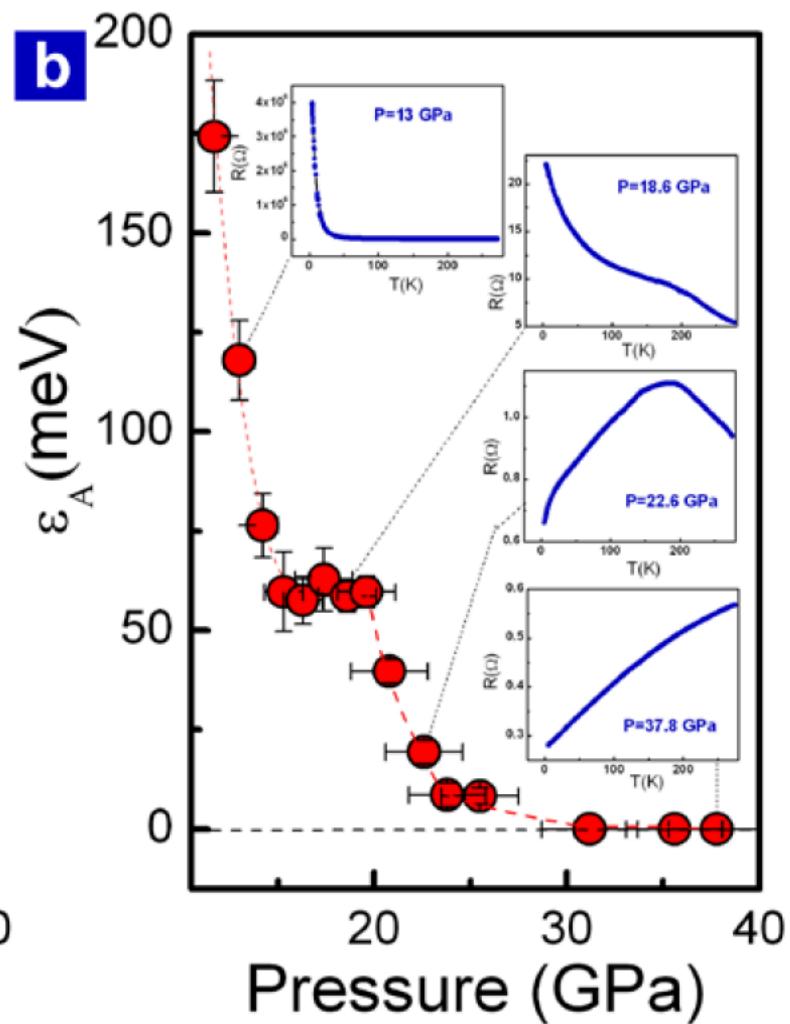
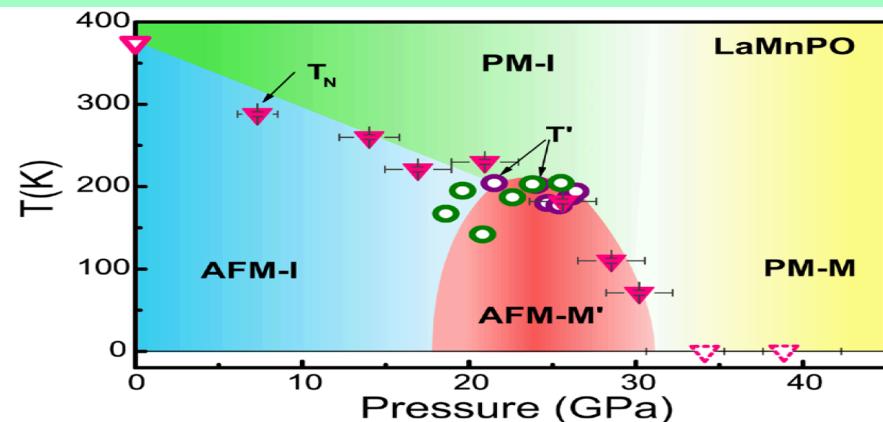
Observation of antiferromagnetic order collapse in the pressurized insulator LaMnPO

Jing Guo, J. W. Simonson, Liling Sun, Qi Wu,  
Gabriel Kotliar, Meigan Aronson, Zhongxi

From antiferromagnetic insulator to correlated metal

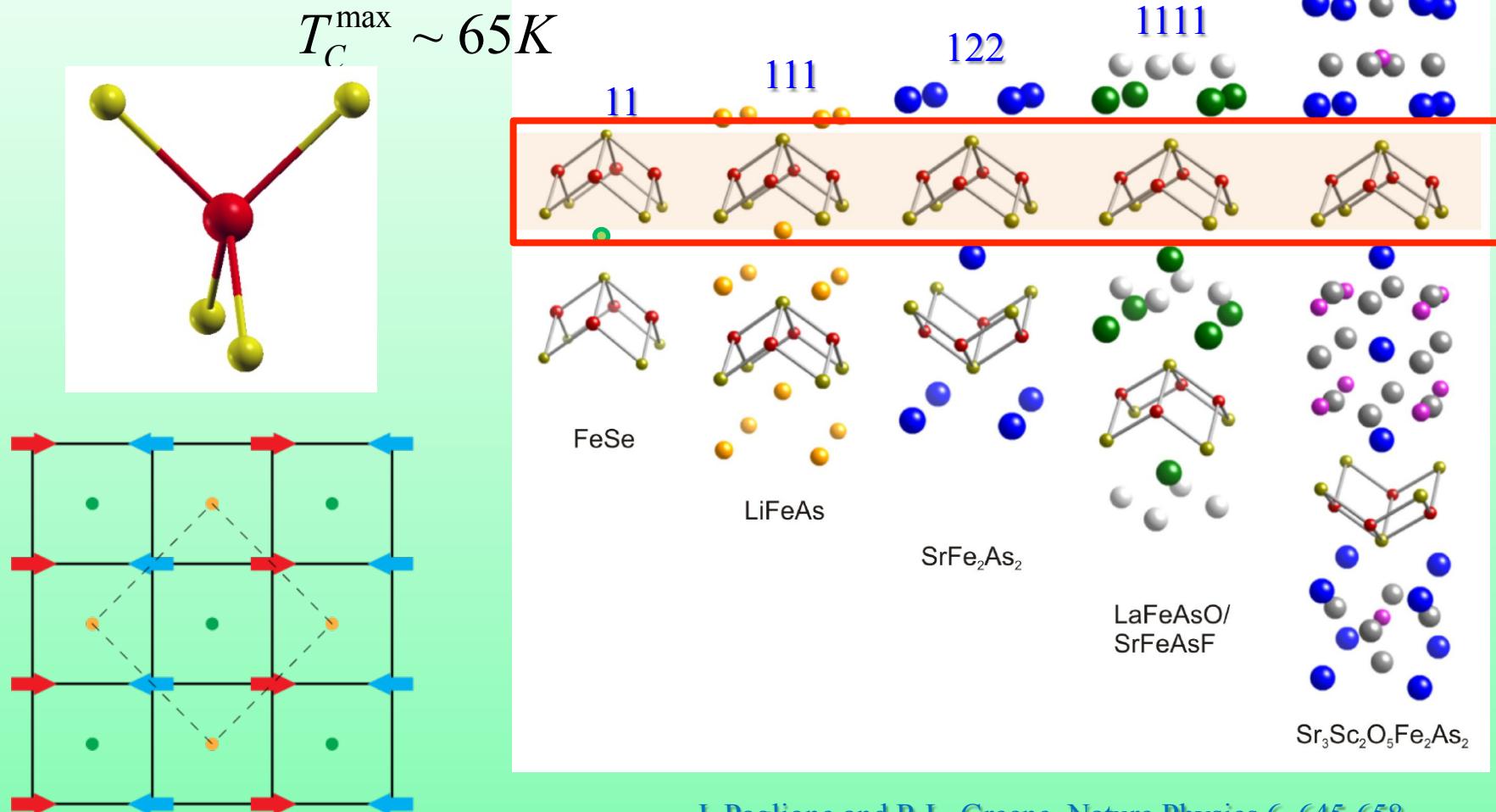
J. W. Simonson, Z. P. Yin, M. Pezzoli, J. Guo, J. G. Hu, H.-J. Lin, C. T. Chen, C. Marques, V. G. Kotliar, D. N. Basov, L. H. Tassie, J. W. Lynn, and J. A. Wilson

Proc. Natl. Acad. Sci 109, 11333–11338 (2012)



# Landscape of Fe based SC

First discovery in 2008: LaFeAsO<sub>1-x</sub>F<sub>x</sub>, H. Hosono, JACS 130, 3296 (2/13/2008) 32522



J. Paglione and R L. Greene, Nature Physics 6, 645-658  
(2010).

# Density-functional calculations of the electronic structures and magnetism of the pnictide superconductors BaFeAs<sub>2</sub> and BaFeSb<sub>2</sub>

J. H. Shim, K. Haule, and G. Kotliar

Phys. Rev. B **79**, 060501(R) – Published 1 February 2009

We investigate the structural, electronic, and magnetic properties of the hypothetical compound BaFePn<sub>2</sub> ( $Pn = As$  and Sb), which is isostructural to the parent compound of the high-temperature superconductor LaFeAsO<sub>1-x</sub>F<sub>x</sub>. Using density-functional theory, we show that the Fermi surface, electronic structure, and spin-density wave instability of BaFePn<sub>2</sub> are very similar to the Fe-based superconductors. Additionally, there are very dispersive metallic bands of a spacer Pn layer, which are almost decoupled from FePn layer. Our results show that experimental study of BaFePn<sub>2</sub> can test the role of charge

Journal of the Physical Society of Japan **83**, 025001 (2014)

<http://dx.doi.org/10.7566/JPSJ.83.025001>

## Enhanced Superconductivity up to 43 K by P/Sb Doping of Ca<sub>1-x</sub>La<sub>x</sub>FeAs<sub>2</sub>

Kazutaka Kudo<sup>1,2\*</sup>, Tasuku Mizukami<sup>1</sup>, Yutaka Kitahama<sup>1</sup>,  
Daisuke Mitsuoka<sup>1</sup>, Keita Iba<sup>1</sup>, Kazunori Fujimura<sup>1</sup>,  
Naoki Nishimoto<sup>1</sup>, Yuji Hiraoka<sup>1,2</sup>, and Minoru Nohara<sup>1,2</sup>

internal coordinates of Ba (0.95, 0.95, z<sub>Ba</sub>), Ba (0.75, 0.25,  
, z<sub>Pn</sub>).  
0 is ex-

AsO

35

41

42

51

12

67

.55

# Thanks for your attention!

Z

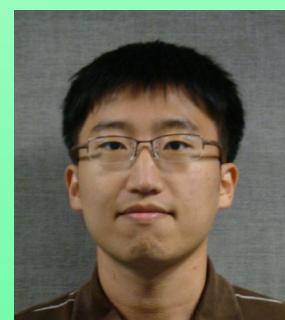
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Experimentalists .

Pengcheng Dai (Rice)

Dimitri Basov (UCSD)

Meigan Aronson ( Stony Brook)