

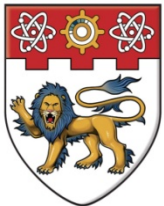
# Frustration-driven magnetic order on the Shastry-Sutherland lattice

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Workshop on Current Trends in Frustrated Magnetism  
Jawaharlal Nehru University, New Delhi

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**NANYANG**  
**TECHNOLOGICAL**  
**UNIVERSITY**



# Collaborators

## Theory:

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## Expt.:

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# Outline

- ❖ Rare earth tetraborides – a “new” family of Shastry-Sutherland compounds
- ❖ Generalized Shastry-Sutherland model
- ❖ Magnetization plateaus in  $\text{TmB}_4$
- ❖ Spin supersolid in the generalized SSM
- ❖ Proliferation of plateaus in the generalized SSM
- ❖ Conclusion

# “Other” realizations of the SSL model

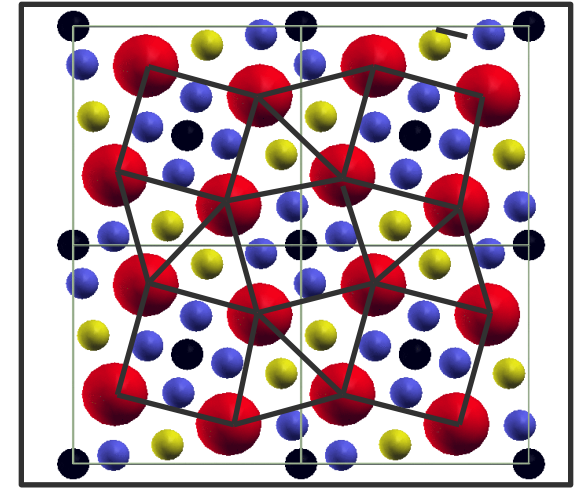
## ❖ Rare earth tetraborides:

$\text{TmB}_4$ ,  $\text{ErB}_4$ ,  $\text{HoB}_4$ ,  $\text{DyB}_4$ ,  $\text{GdB}_4$ ,  $\text{TbB}_4$

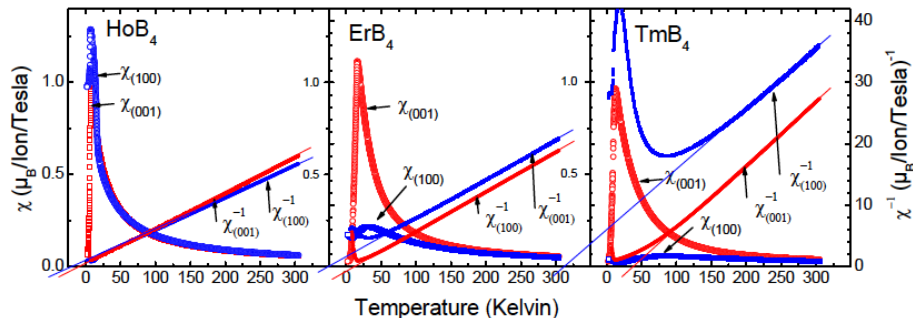
## ❖ $\text{R}_2\text{T}_2\text{M}$ : $\text{Yb}_2\text{Pt}_2\text{Pb}$ , $\text{Ce}_2\text{Pt}_2\text{Pb}$

❑ Weakly coupled layers

❑  $\text{R}^{3+}$  ions arranged in SSL geometry



	ZF order	$\mu_{\text{eff}}$ ( $\mu_B$ )	$\Theta$ (K)	$T_{\text{N1}}$	$T_{\text{N2}}$	$\sum J_{ij}$ (K)	D(K)
<b>TmB<sub>4</sub></b>	Ising-AFM ( $\pi, \pi$ )	6.6	-63	11.7	9.8	-4.8	-6.4
<b>ErB<sub>4</sub></b>	Ising-AFM ( $\pi, 0$ )	8.4	-22.7	15.3		-1.4	-4.6
<b>HoB<sub>4</sub></b>	Ising-AFM ( $\pi, \pi$ )	9.2	-12.7	7.4	6.3	-1.3	0.3

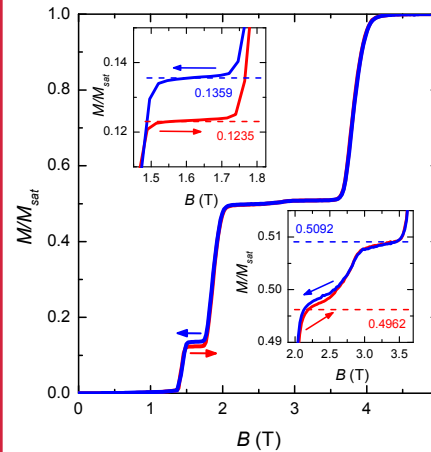


Mata's. et.al., J. Phys: Conf. Ser., 200, 032041 (2010)

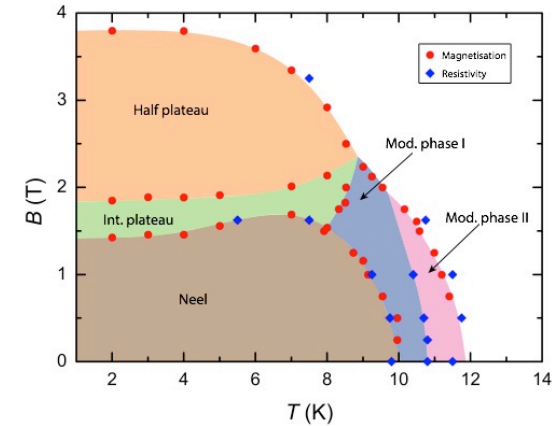
# Magnetization plateaus in $\text{RB}_4$

- Ground state has long range magnetic ordering in most of the rare earth tetraborides
- Field-induced plateaus observed in all members
- Sequence of plateaus differ across the family
- Multi-step melting of magnetic order observed in many  $\text{RB}_4$  compounds

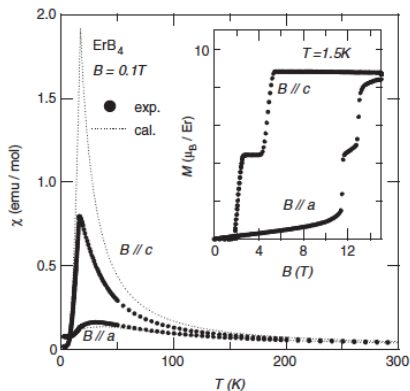
$\text{TmB}_4$



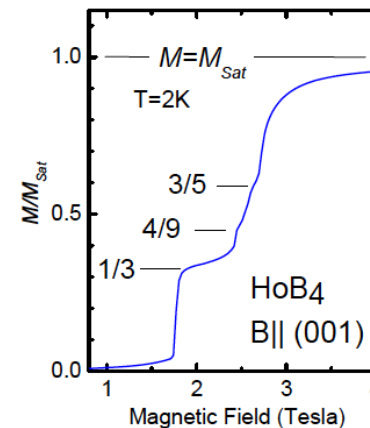
(a) magnetization plateaus,



(b) phase diagram



Uniform susceptibility and field dependent magnetization in  $\text{ErB}_4$



Magnetization plateaus in  $\text{HoB}_4$

# Rare earth tetraborides

## Generic features

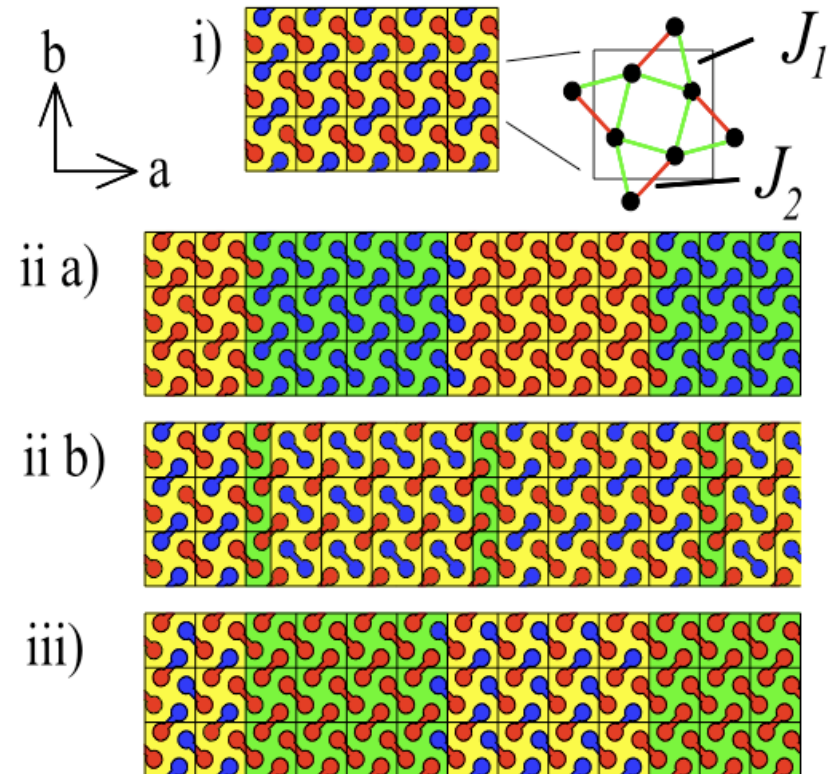
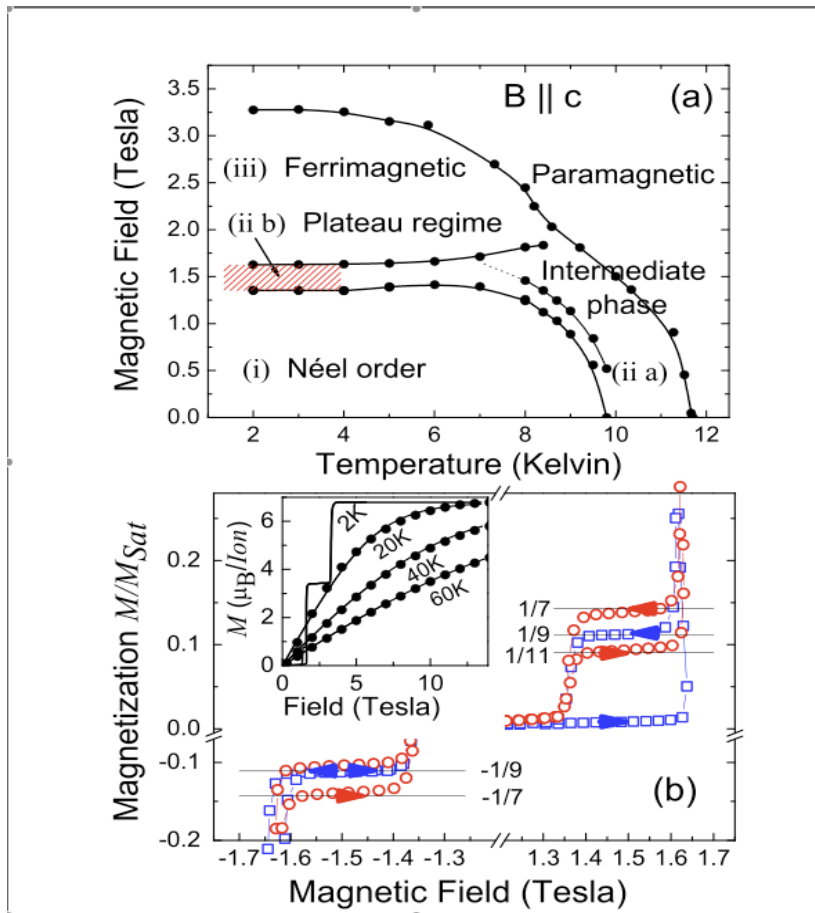
- Low saturation field ( $\sim 10\text{T}$ ) – low-T neutron scattering possible
- Span wide parameter regime including magnetic ground state at zero field
- Higher spins, single ion anisotropies  $\implies$  effective exchange anisotropy
- Additional interactions

*Extensive insight into the interplay of competing strong interactions and geometric frustration in the Shastry-Sutherland lattice*

Metallic ground state – interaction of itinerant electrons with localized magnetic moments in a frustrated configuration – interesting magneto-electric effects

# Magnetization Plateaus in $TmB_4$

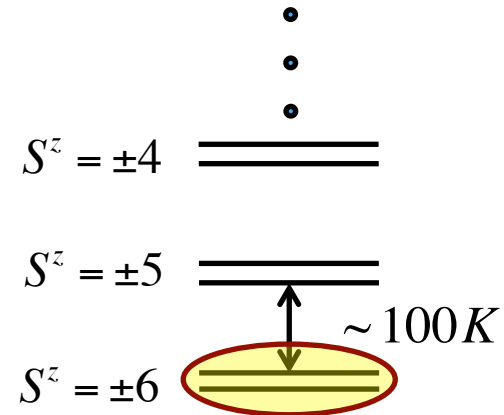
Stripe superstructures modulate underlying short-range structures



K. Siemensmeyer et. al., PRL 101, 177201 (2008)

# Low energy effective model

- Large magnetic moment for  $\text{Tm}^{3+}$ :  $S = 6$
- Large single-ion anisotropy:  $-D(S_i^z)^2, D/J \approx 5$



Effective low energy model involving the lowest 2 levels

$$H = \sum_{\langle i,j \rangle} J_{ij}^z S_i^z S_j^z + J_{ij}^{xy} (S_i^x S_j^x + S_i^y S_j^y)$$

$$J_{ij}^{xy} < 0$$

$$J_{ij}^z \gg |J_{ij}^{xy}|$$

Ising limit



Ferromagnetic exchange term – sign problem in QMC simulations alleviated

Stochastic Series Expansion QMC algorithm used for simulation

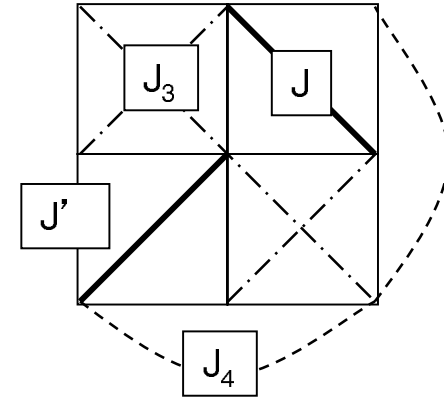


# Generalized Shastry-Sutherland model

- $S=1/2$  XXZ model with large Ising anisotropy
- $J$  and  $J'$  along the SSL lattice axes

*Longer range interactions mediated by itinerant electrons*

- NNN interaction ( $J_3$ ) along the diagonals of the plaquettes with no  $J$
- Additional 3<sup>rd</sup> neighbor interaction  $J_4$
- Same anisotropy for all interactions.



Rich variety of magnetic phases

Potentially realized in the different members of the rare-earth tetraborides

# Low energy effective model for $\text{TmB}_4$

Start with the generalized Shastry Sutherland model with  $J$  and  $J'$

➡ inconsistency with experimental observation

Ising limit: Extended  $1/3$  plateau followed by a direct transition to full saturation

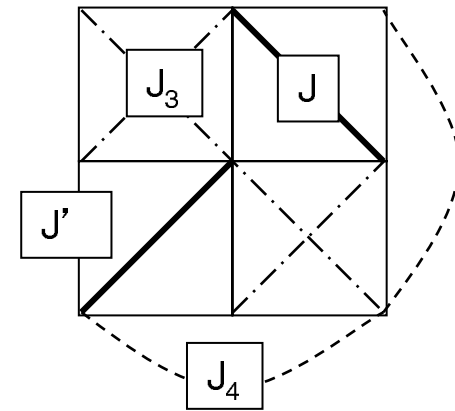
$\text{TmB}_4$ : Extended  $1/2$  plateau, no  $1/3$  plateau

*Need additional interactions*

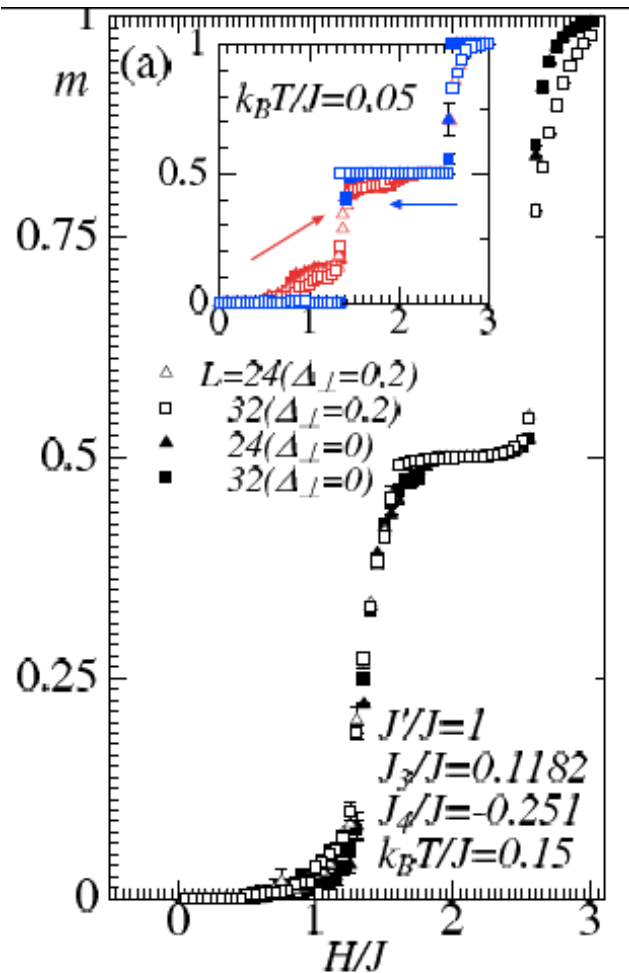
Longer range RKKY interactions mediated by itinerant electrons

- AFM  $J_3$  necessary to account for the appearance of  $1/2$  plateau
- FM  $J_4$  necessary to explain the suppression of  $1/3$  plateau

Together they explain the principal plateau structure observed in  $\text{TmB}_4$ .

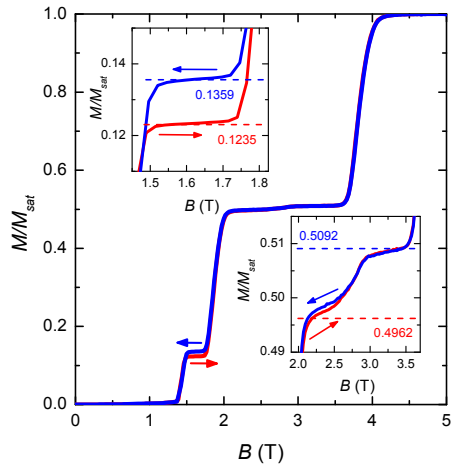


# Modeling TmB<sub>4</sub>



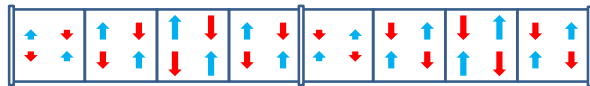
- ✓ Correct critical values for  $m/m_s=1/2$  plateau reproduced
- ✓ Correct saturation field reproduced
- ✓ No evidence of lower magnetization plateaus for the current model
- ✓ No evidence for “hysteresis” effects.

# Fractional plateau in $TmB_4$

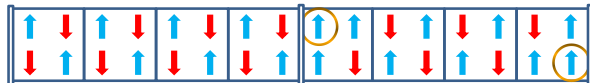


Fractional plateau and hysteresis in  $TmB_4$

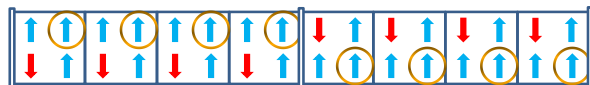
- Fractional plateau observed in  $TmB_4$  at  $m/m_s \sim 1/8$
- Magnetic hysteresis observed at the fractional plateau
- Neutron scattering  $\rightarrow$  modulated AFM ground state with incommensurate periodicity
- Provides simple explanation for observed magnetic behaviour
- Predict modulated structure for both fractional and  $1/2$  plateaus – need to be confirmed experimentally



Modulated AFM

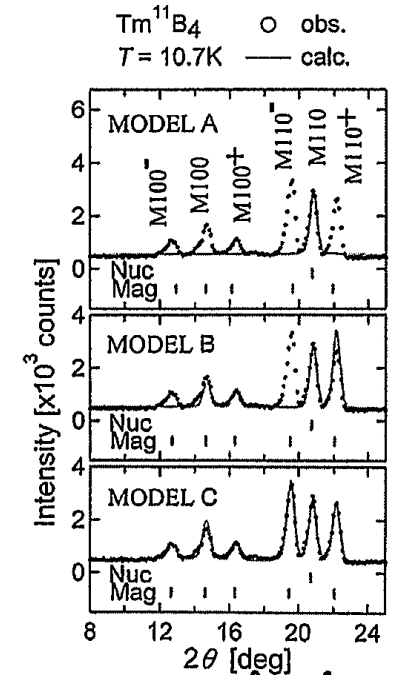
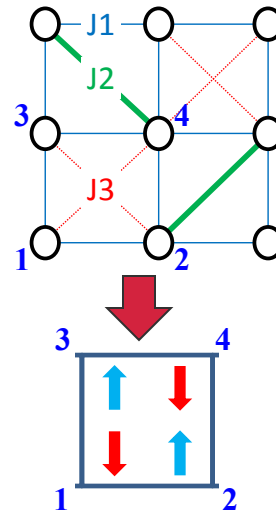


$1/8$  plateau



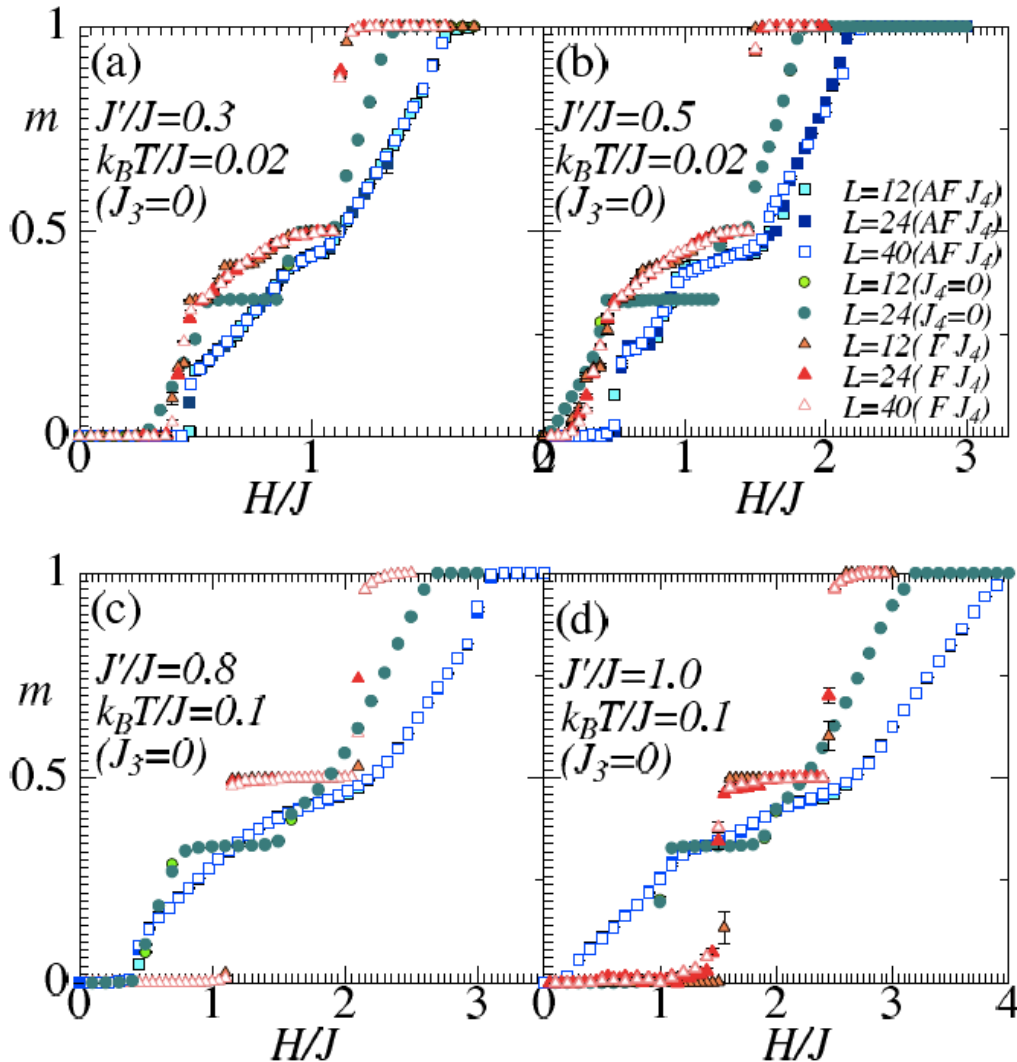
$1/2$  plateau

Schematic spin configuration



Neutron scattering data Michimura, et.al., 2009

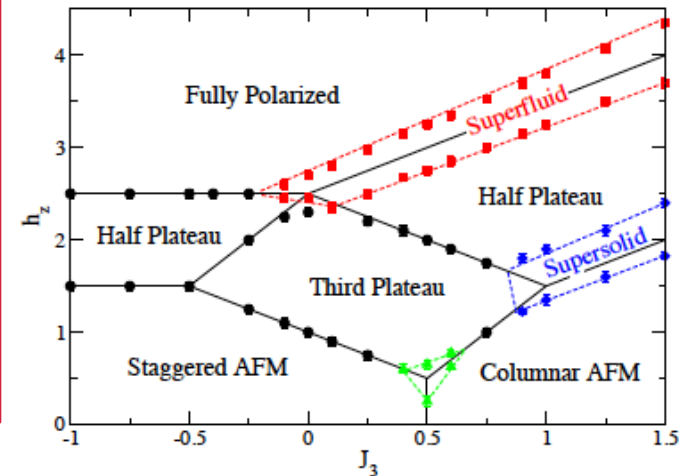
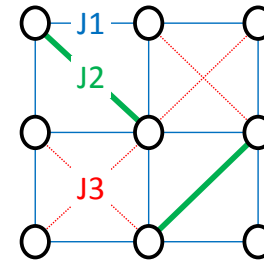
# Magnetization in generalized SSM



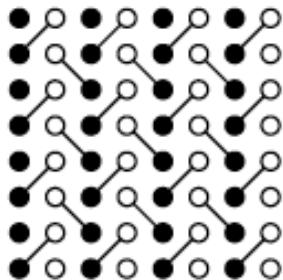
- Varied sequence of magnetization plateaus as the parameters are varied
- Fertile framework for investigating frustration driven field induced magnetic phases – plateaus, spins-supersolid (?)
- Potentially realizable in the different members of the rare earth tetraboride family of compounds
- Help identify dominant interactions driving observed magnetic phases

# Magnetization plateaus in extended SSM

- Effect of  $J_3$  explored in detail
- ZF:  $(\pi, \pi)$  AFM order for FM and weak AFM  $J_3$  in the Ising limit
- $(\pi, 0)$  AFM order for moderate to strong AFM  $J_3$  – observed in ErB4
- $1/3$  plateau persists to finite  $J_3$
- $1/2$  plateau appears for any  $J_3 \neq 0$
- Finite exchange interactions induce superfluidity at boundary between plateaus



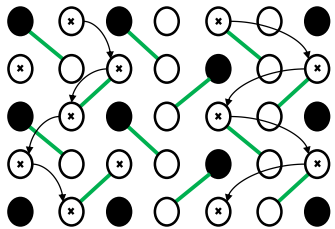
Magnetic phases driven by  $J_3$



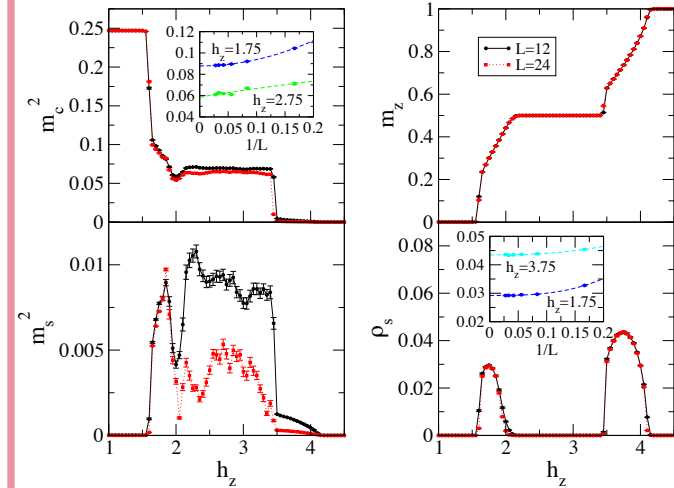
Columnar AFM order

# Spin supersolid in extended SSM

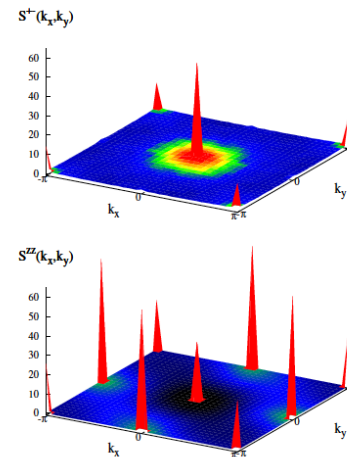
- Spin supersolid GS observed at densities close to, but less than half-filling
- Longitudinal AFM order at  $(\pi, 0)$  and  $(\pi, \pi)$
- Transverse AFM order at  $(\pi, \pi)$
- Simple mechanism based on delocalization of holes in the half-plateau by 1<sup>st</sup> order process
- Magnetization behaviour qualitatively similar to ErB<sub>4</sub>, but spin SSOL phase not yet reported



Delocalization of a single flipped spin at the  $\frac{1}{2}$  plateau



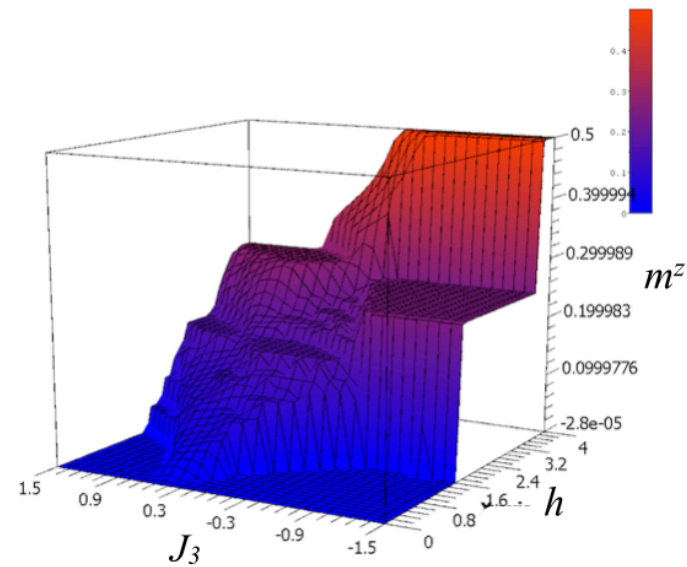
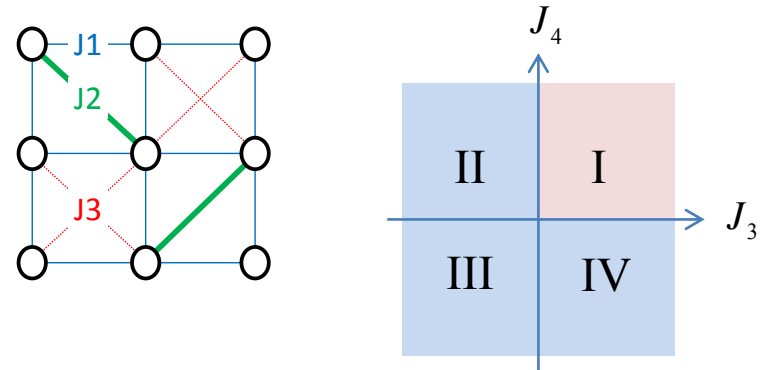
Simulation results showing the appearance of spin SSOL



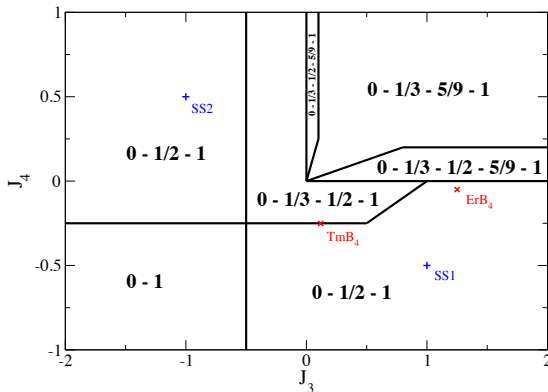
Transverse and longitudinal structure factors in the spin SSOL phase

# Magnetic phases in generalized SSM

- Inclusion of  $J_4$  changes plateau sequence significantly
- AFM  $J_3$  and  $J_4$  destabilises the  $1/2$  plateau – emergence of the  $5/9$  plateau
- Different structures for same plateau realised for different parameters
- Spin-SSOL stabilised over extended parameter ranges



Evolution of plateau sequence for finite  $J_4$  in the XXZ model



Plateau sequence in the Ising limit for finite  $J_4$



# Understanding plateaus in generalized SSM

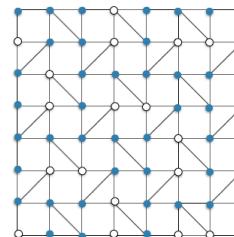
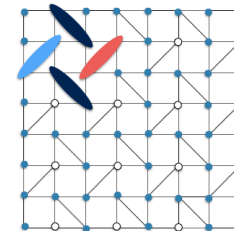
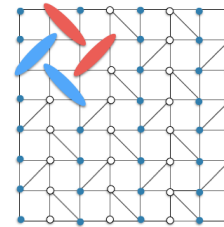
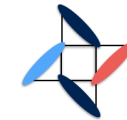
- Explain spin textures at plateaus in terms of a plaquette unit cell
- Construct a “pinwheel” around a square with no diagonal bond
- Many different configurations possible (for Ising spins)
- Local dimer states determine nature of spin modulation
- Many possibilities for same plaquette magnetic moment
- Leads to multiple distinct plateaus with same magnetization
- Possible because of additional interactions
- Stable for finite exchange - Confirmed by QMC simulations in XXZ model

$$|u\rangle = |\uparrow\uparrow\rangle$$

$$|d\rangle = |\downarrow\downarrow\rangle$$

$$|l\rangle = |\uparrow\downarrow\rangle$$

$$|r\rangle = |\downarrow\uparrow\rangle$$



Columnar AFM

1/2 plateau

1/3 plateau

# Electronic transport in rare earth tetraborides

- Itinerant electrons in rare earth tetraborides couple to local moments
- Electronic transport affected significantly by underlying magnetic texture
- Study within the framework of Shastry Sutherland Kondo lattice model (SSKLM)
- Control electronic transport by applied magnetic field and magnetism by driving current
- Small change in applied magnetic field changes magnetic structure – interesting magneto-electric phenomena

# Conclusions

- ❖ Interplay between geometric frustration, strong interaction and high magnetic field results in many novel quantum phases on the Shastry-Sutherland lattice
- ❖ Rare earth tetraborides present experimental realizations of many of these phases
- ❖ Metallicity makes these quantum magnets even more interesting
- ❖ Magnetic phases explored in great detail – transport promises new phases and phenomena

*The best is yet to come !*