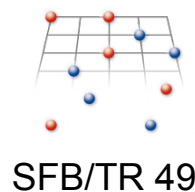
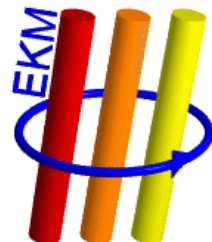
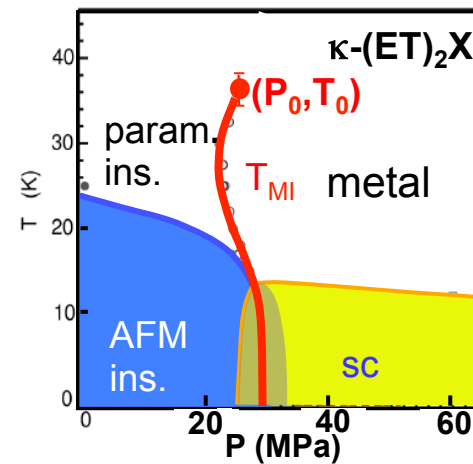


Mott criticality studied by dilatometry under ^4He -gas pressure on the quasi-2D organic charge-transfer salts $\kappa\text{-(BEDT-TTF)}_2\text{X}$

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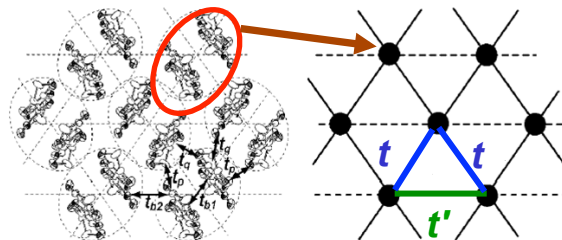
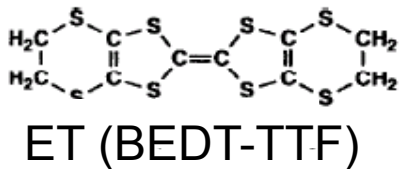
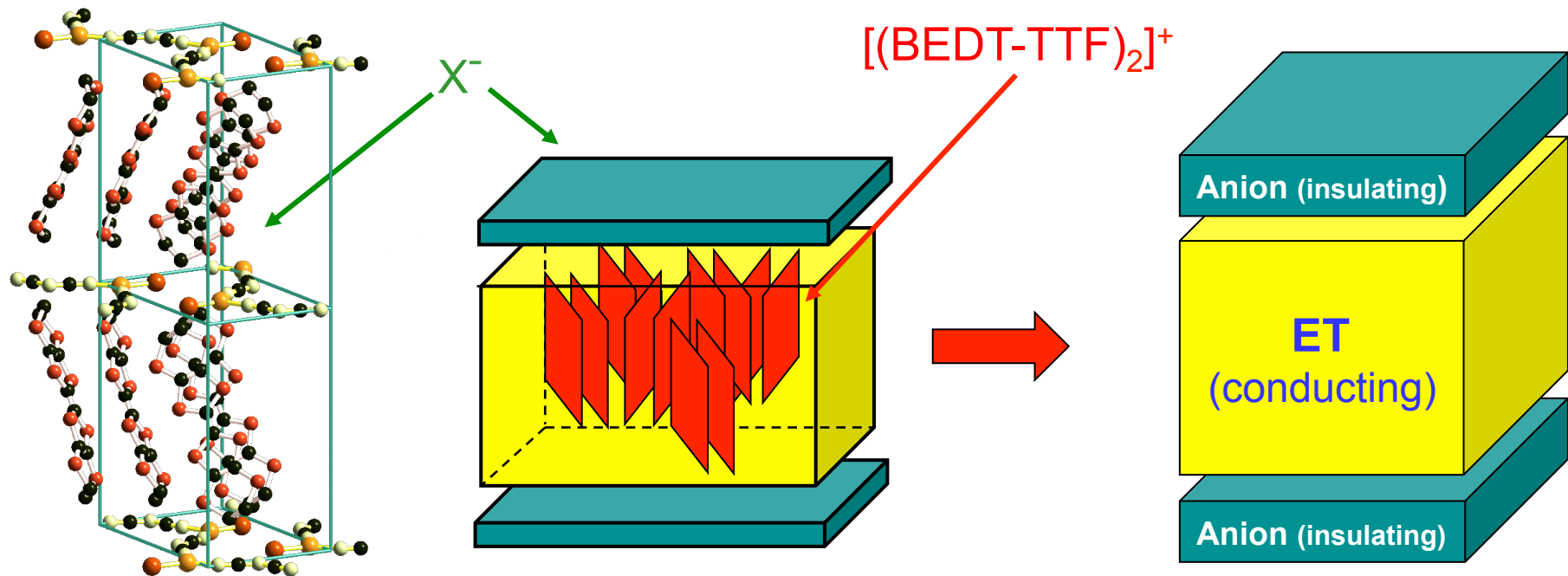
R. Kato

RIKEN, Japan

outline

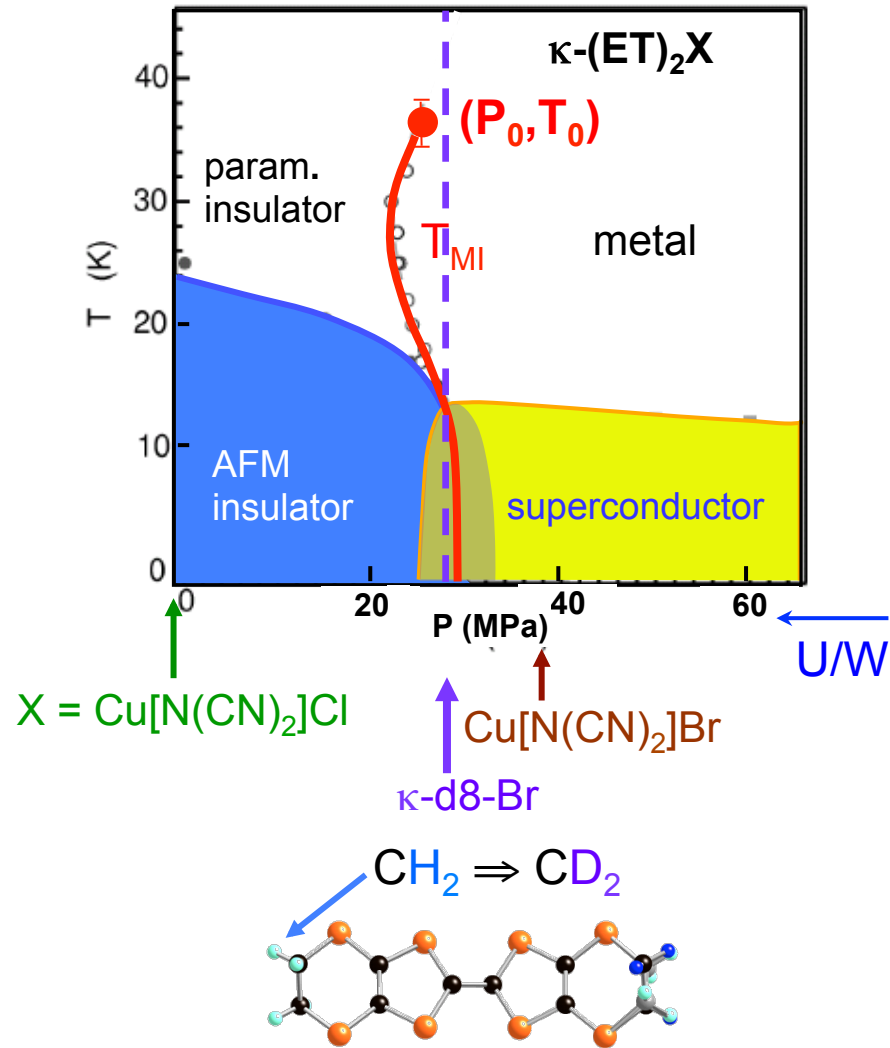
- organic charge-transfer salts
- phase diagrams
- spin-liquid: κ -(ET)₂Cu₂(CN)₃
- Mott criticality in κ -(ET)₂X
- valence-bond-solid: EtMe₃P[Pd(dmit)₂]₂
- summary and outlook

κ -(BEDT-TTF)₂X: charge-transfer salts



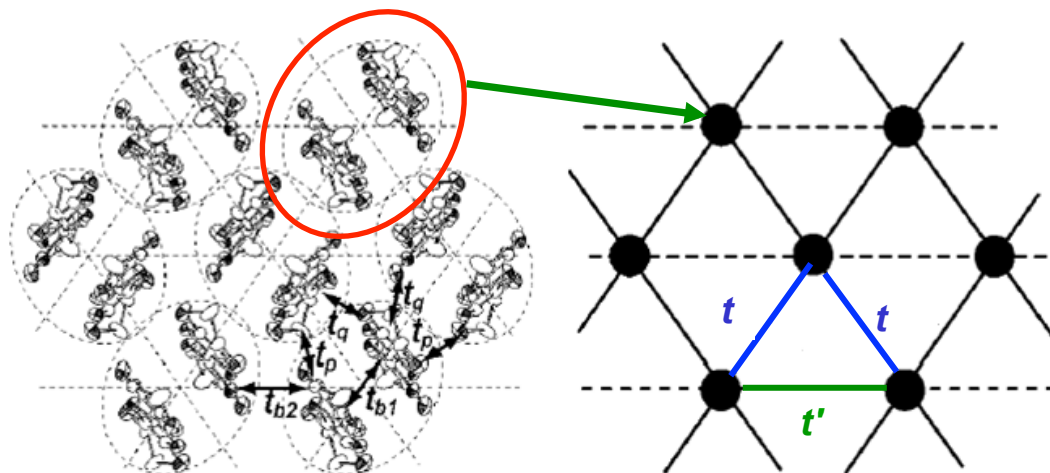
- κ -phase: “effective dimer model”: 1 hole/ dimer \Rightarrow half-filled conduction band
- $W \sim U_{\text{eff}}$: correlated π electrons

Mott criticality at the 2nd-order end-point (P_0, T_0)



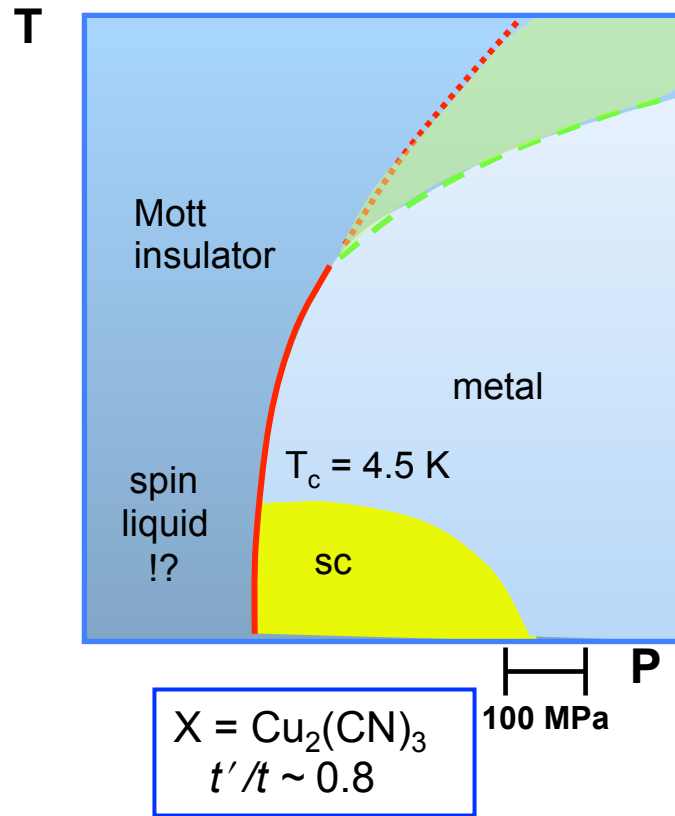
Lefebvre *et al.*, PRL **85**, 5420 (00)

effect-of-frustration



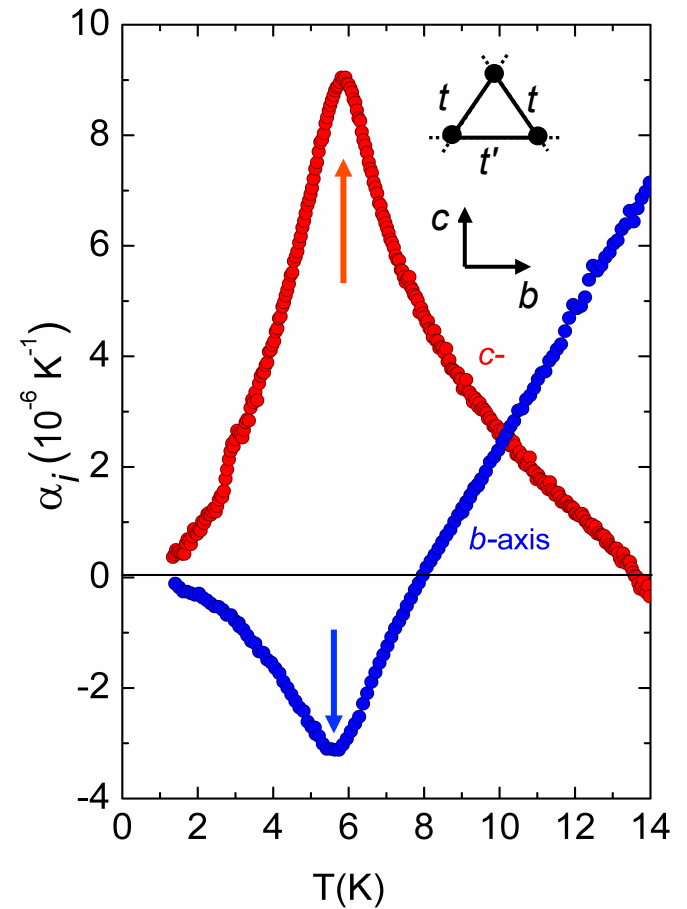
t'/t	$\kappa\text{-(ET)}_2\text{Cu}[\text{N}(\text{CN})_2]\text{Cl}$	$\kappa\text{-(ET)}_2\text{Cu}_2(\text{CN})_3$
ext. Hückel calc. Mori <i>et al.</i> , Chem. Soc. Jpn. 72 , 179 (99)	0.72	1.06
Komatsu <i>et al.</i> , JPSJ 65 , 1340 (96)		
<i>ab initio</i> calc. Kandpal <i>et al.</i> , PRL 103 , 067004 (09)	0.44	~ 0.8
Nakamura <i>et al.</i> , JPSJ 78 , 083710 (09)		

spin-liquid - κ -(ET)₂Cu₂(CN)₃



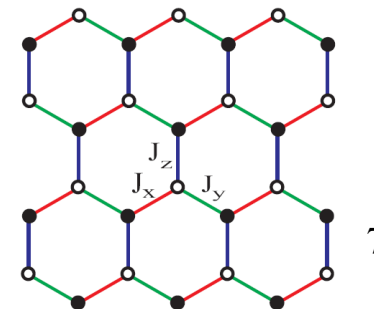
no long-range magnetic order down to 32 mK ($J = 250$ K)

Kurosaki *et al.*, PRL **95**, 177001 (05)
 Shimizu *et al.*, PRL **91**, 107001 (03)



R. S. Manna *et al.*, PRL **104**, 016403 (10)

Kitaev spin-liquid
 $A_2\text{IrO}_3$ ($A = \text{Na, Li}$)



Mott universality



crossover: $\delta, \beta, \gamma = 3, 0.5, 1$ (mean field values)

$\delta, \beta, \gamma = 4.81, 0.34, 1$ (3D Ising)

\Rightarrow liquid-gas universality (3D Ising)

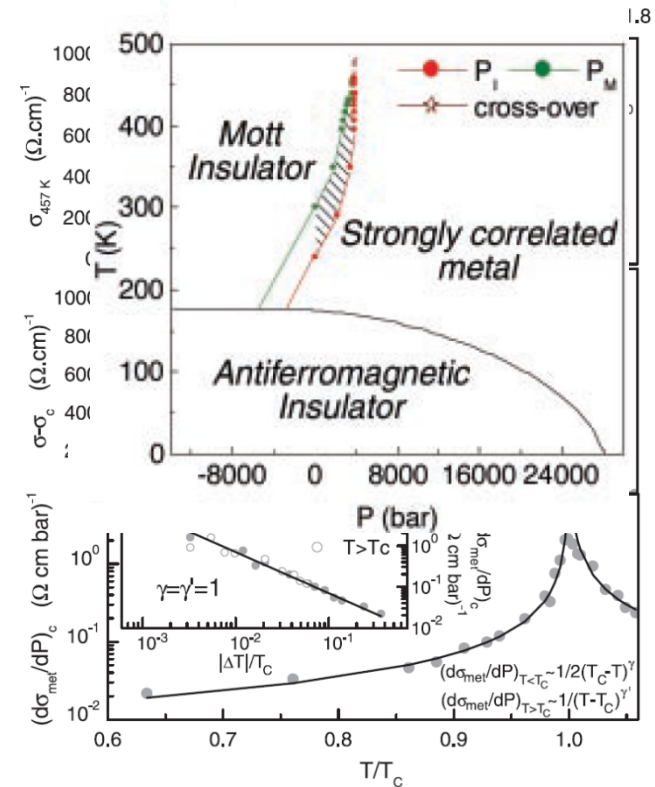
Limelette *et al.*, Science **302**, 89 (03)

DMFT of the Hubbard model: an order parameter for the finite temperature Mott end point

\Rightarrow Ising universality class, similar to the liquid-vapor transition

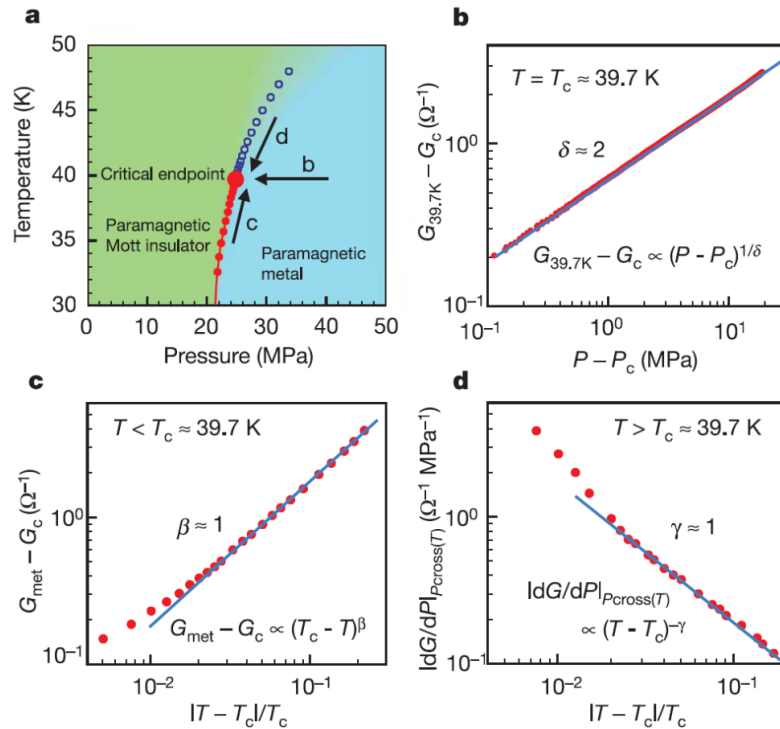
Castellani *et al.*, PRL **43**, 1957 (79)

Kotliar *et al.*, PRL **84**, 5180 (00)



controversy: κ -(ET)₂Cu[N(CN)₂]Cl

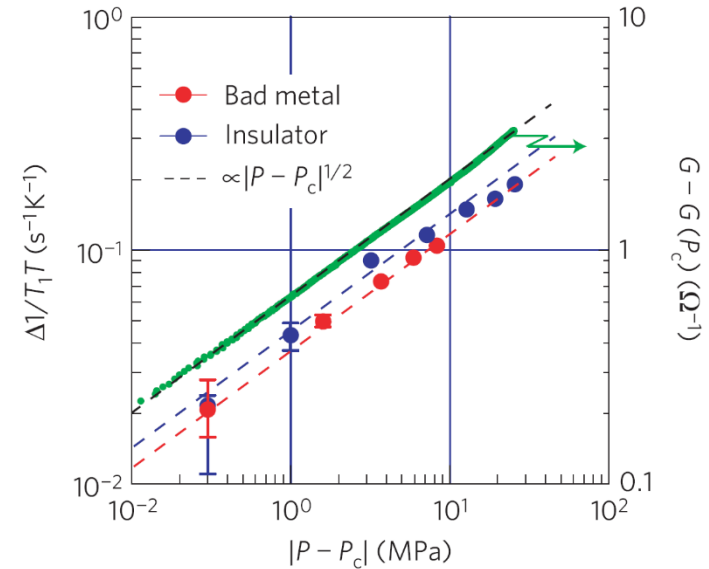
conductivity



$\delta, \beta, \gamma = 2, 1, 1$
unconventional Mott criticality

Kagawa *et al.*, Nature **436**, 534 (05)

¹³C-NMR



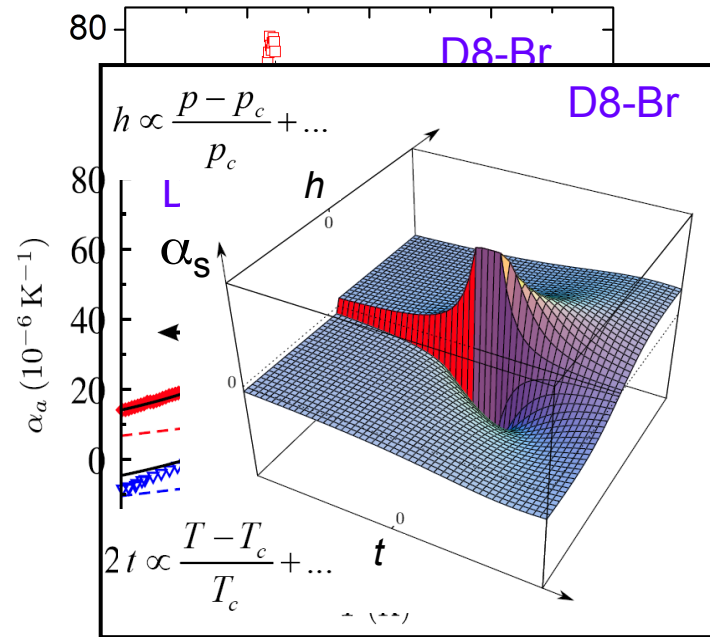
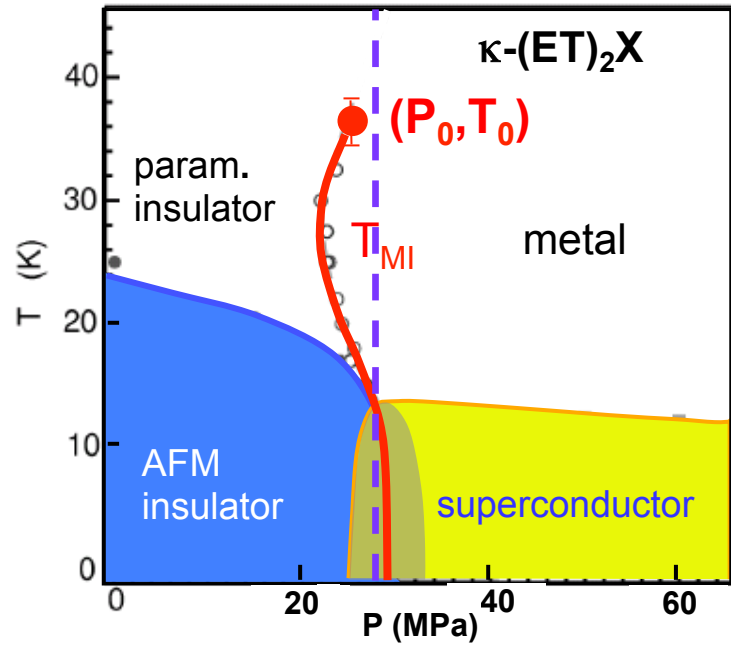
$\Delta 1/T_1 T \propto |P - P_c|^{1/2} \Rightarrow \delta = 2$
unconventional

Kagawa *et al.*, Nature Physics **5**, 880 (09)

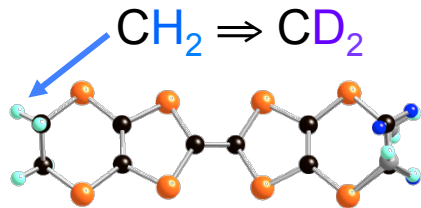
conductivity data of κ -(ET)₂Cu[N(CN)₂]Cl: coupling to the energy density dominates \Rightarrow consistent with 2D Ising universality class

Papanikolaou *et al.*, PRL **100**, 026408 (08)

Mott criticality at the 2nd-order end-point (P_0, T_0)



assumption: Grüneisen scaling
 - breakdown of Grüneisen scaling in the vicinity of a finite-temp. critical end point
 - consistent with 2D Ising universality class
 - large anomaly in alpha and sign change at the critical end-point (P_0, T_0)
 Souza et al., PRL **99**, 037003 (07)
 Souza et al., PRL **99**, 037003 (07)



thermal expansion measurements under He-gas pressure



experimental specifications

- high-resolution capacitive dilatometer ($5 \times 10^{-2} \text{ \AA}$)
- temperature range 1.4 - 293 K
- hydrostatic pressure range 0 - 250 MPa (helium as a pressure transmitting medium)
- magnetic field range 0 - 14 T

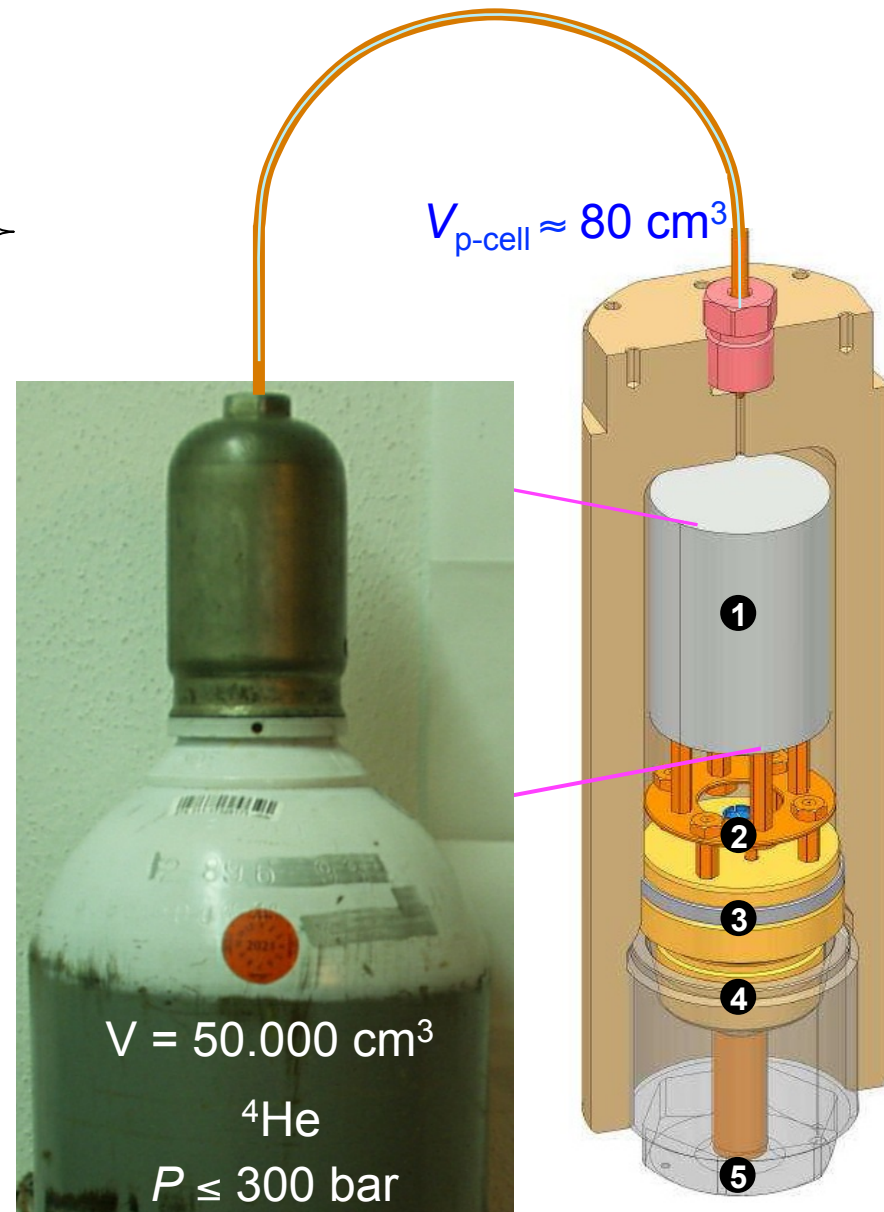
pressure cell and dilatometer

- 1 dilatometer cell
- 2 n-InSb pressure gauge ($\Delta P = \pm 0.1$ MPa)
- 3 seal
- 4 plug with electrical feed-throughs
- 5 retaining screw

Thermal expansion coefficient,

$$\alpha_i = \frac{1}{l_i} \left(\frac{\partial l_i}{\partial T} \right)_P$$

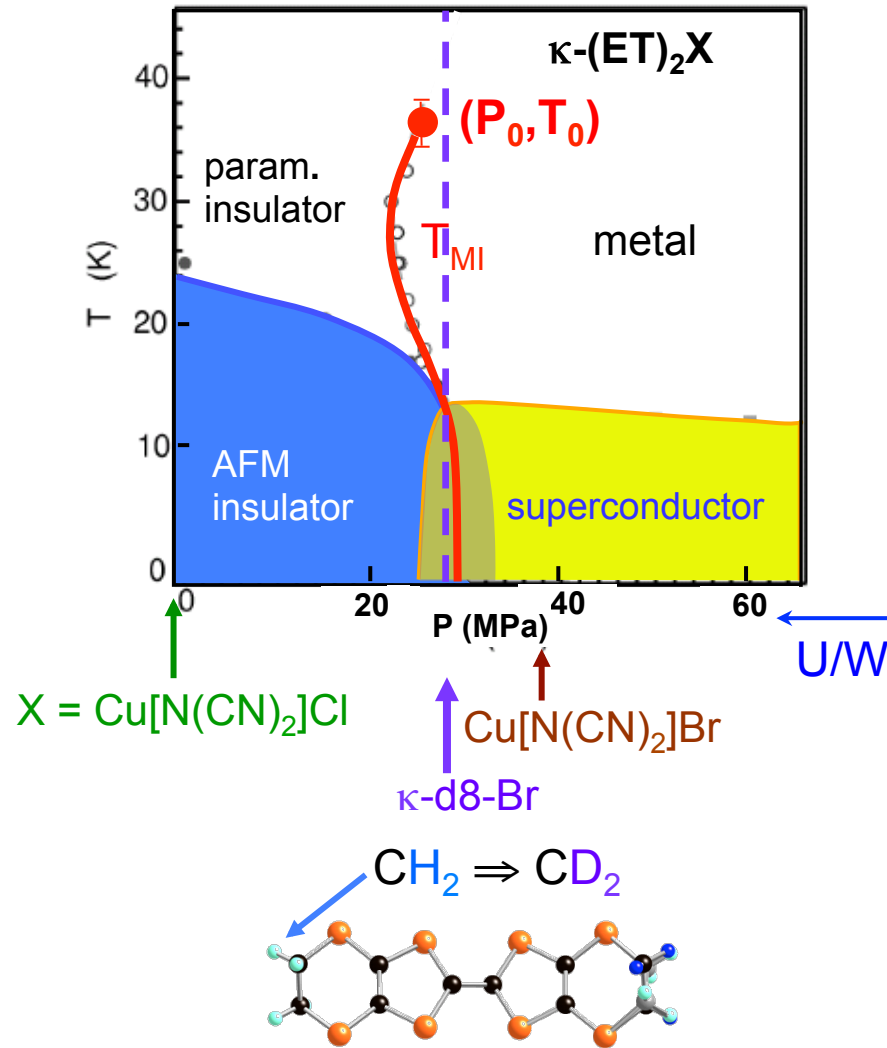
- constant-pressure condition
- ^4He (pressure-transmitting medium):
gas/ liquid phase
- pressure reservoirs:
gas bottle/ compressor with micropump



R. S. Manna, PhD thesis (12)

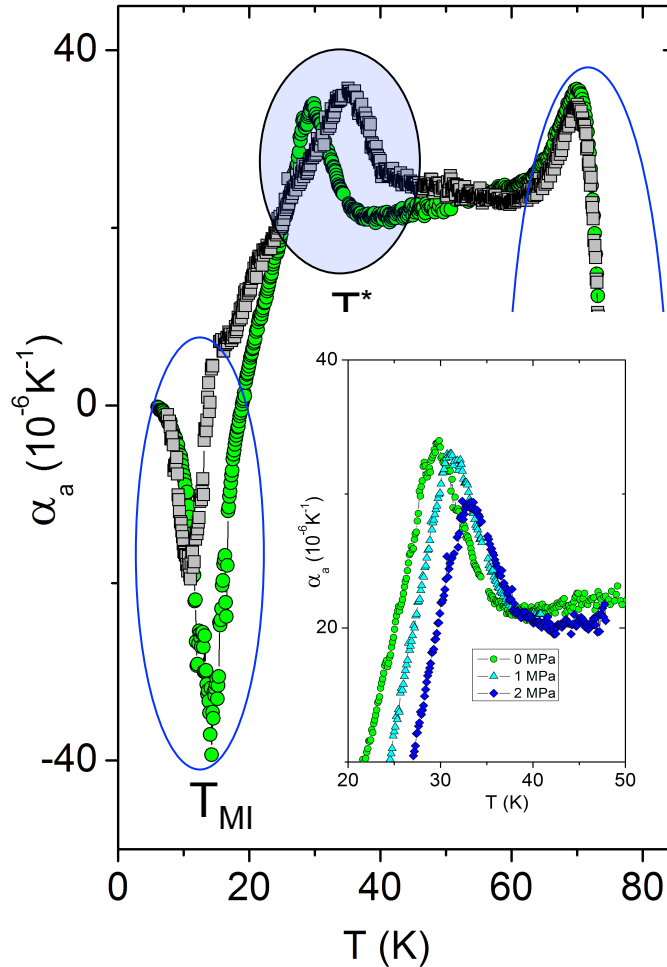
R. S. Manna *et al.*, Rev. Sci. Instrum. **83**, 085111 (12)

Mott criticality at the 2nd-order end-point (P_0, T_0)

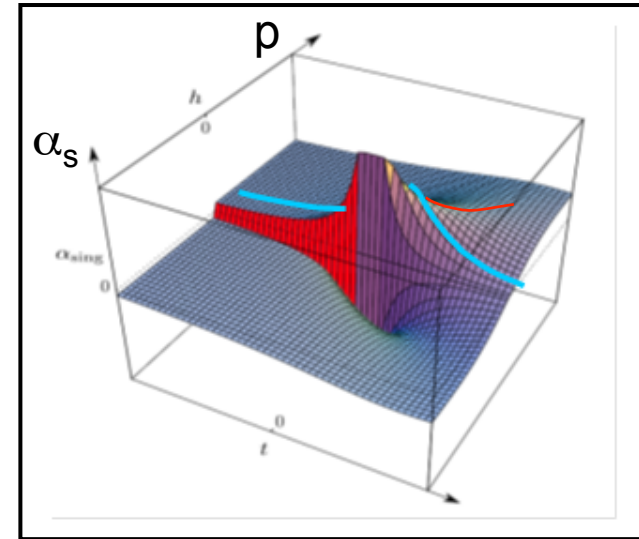


Lefebvre *et al.*, PRL **85**, 5420 (00)

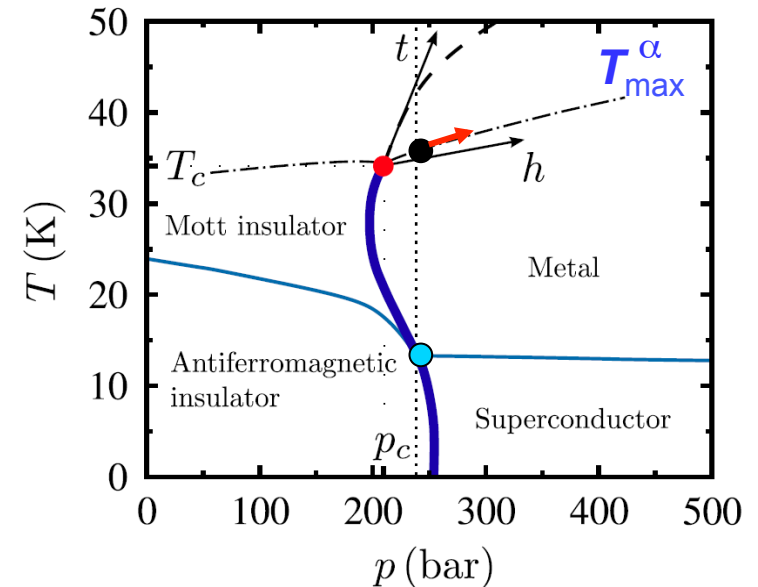
κ -D8-Br at finite pressure



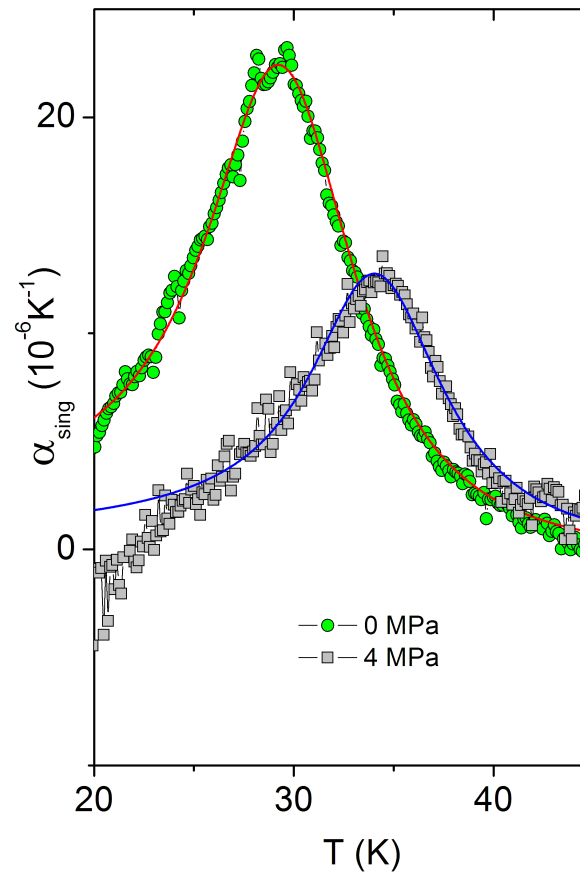
- T_g pressure independent, cf. Müller *et al.*, PRB (02)
- T_{MI} (1st-order) consistent with literature
- effect of pressure on T^* (2nd-order)



Bartosch *et al.*, PRL **104**, 245701 (10)



κ -D8-Br at finite pressure



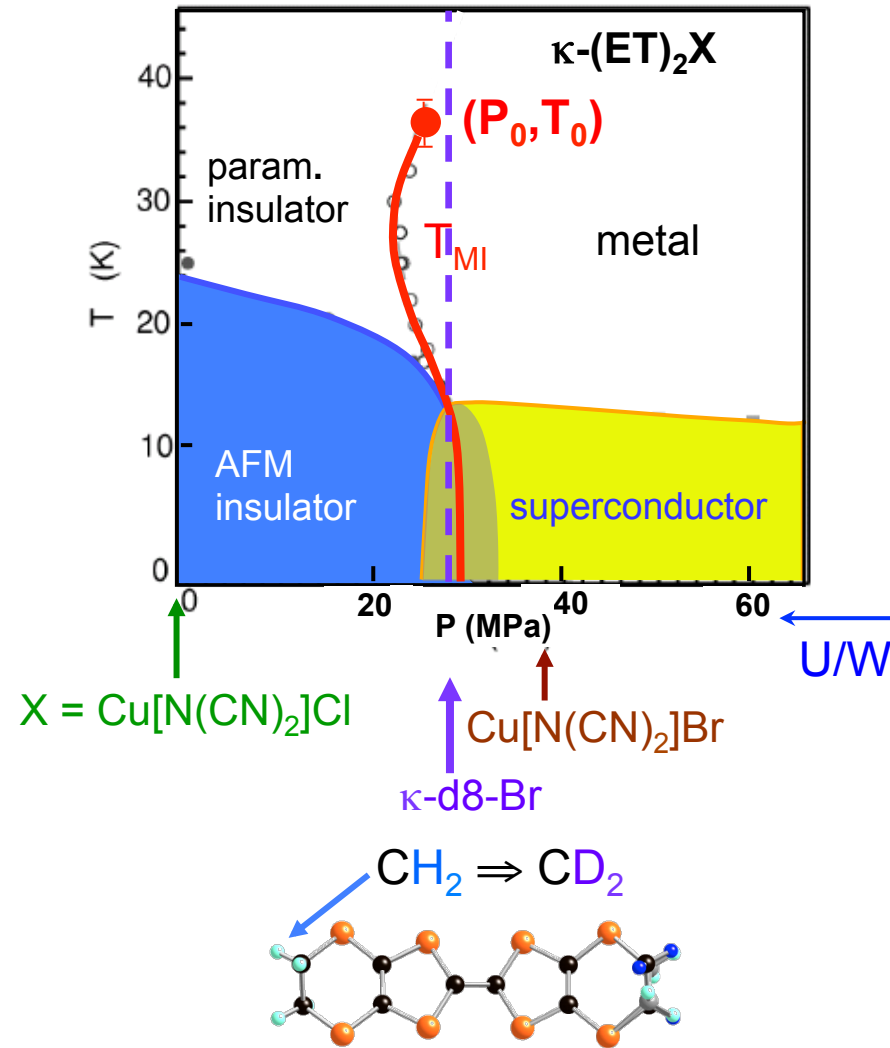
after subtracting a T-linear background

scaling theory: $\alpha_{\text{sing}} \propto \text{sgn}(h) (-t)^{-1+\beta}$

$$h \propto \frac{p-p_c}{p_c} + \dots \quad \text{and} \quad t \propto \frac{T-T_c}{T_c} + \dots$$

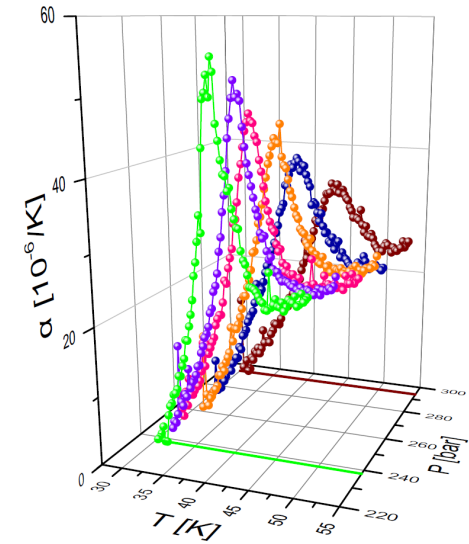
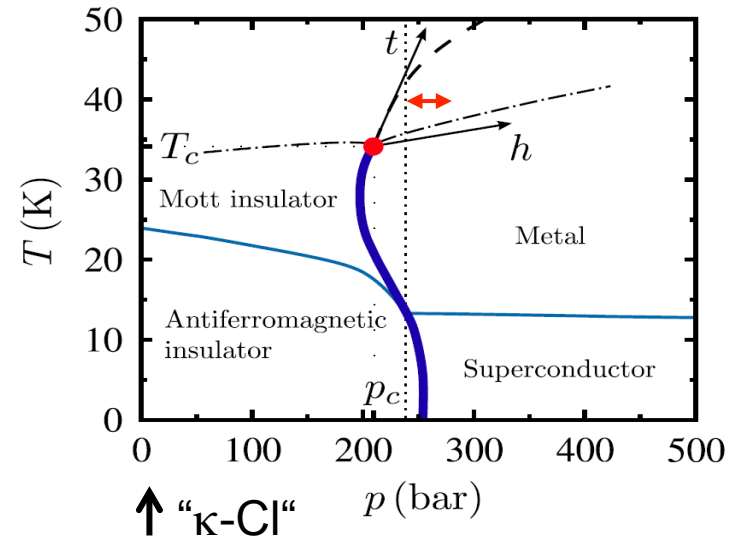
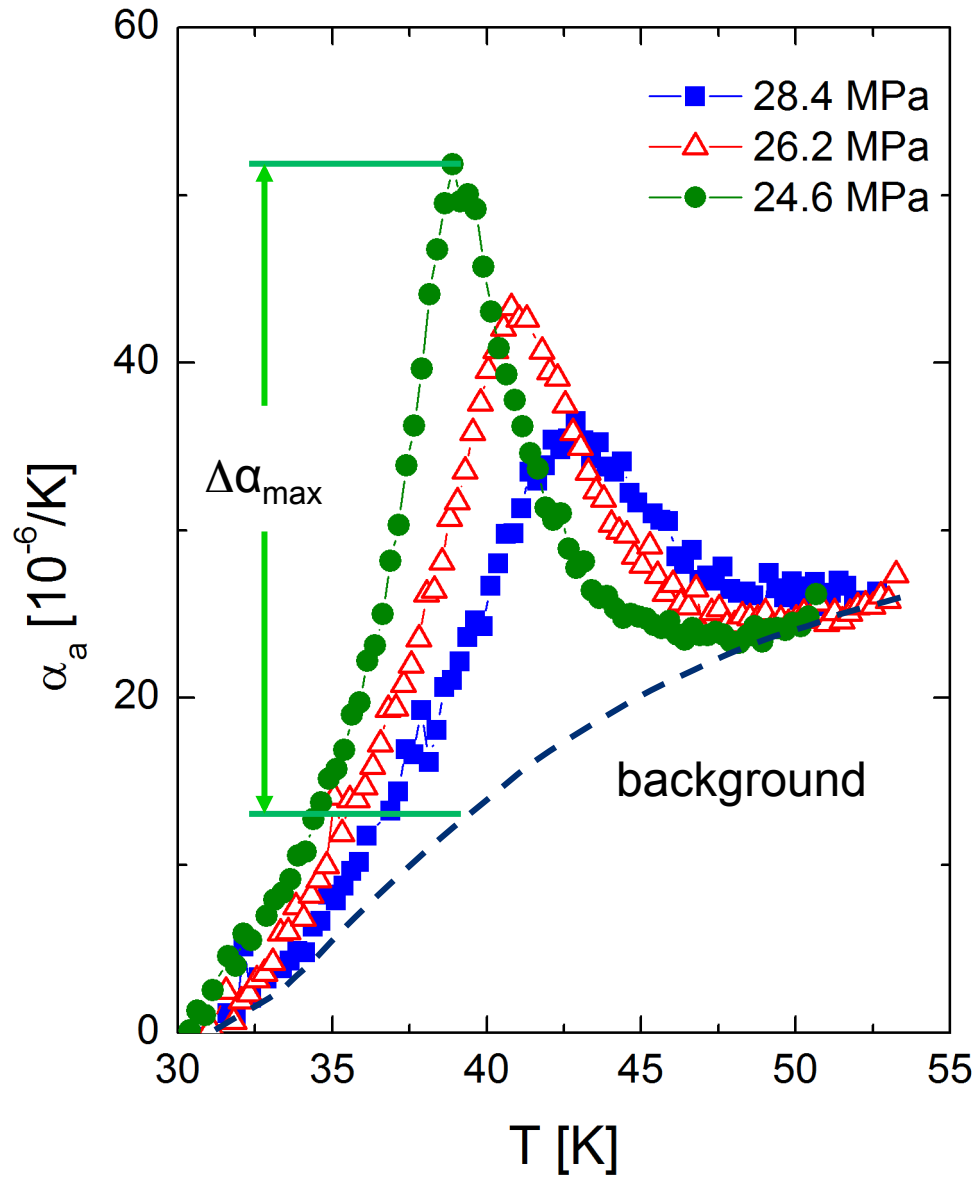
consistent with 2D Ising universality class

Mott criticality at the 2nd-order end-point (P_0, T_0)



Lefebvre *et al.*, PRL **85**, 5420 (00)

κ -Cl at finite pressure

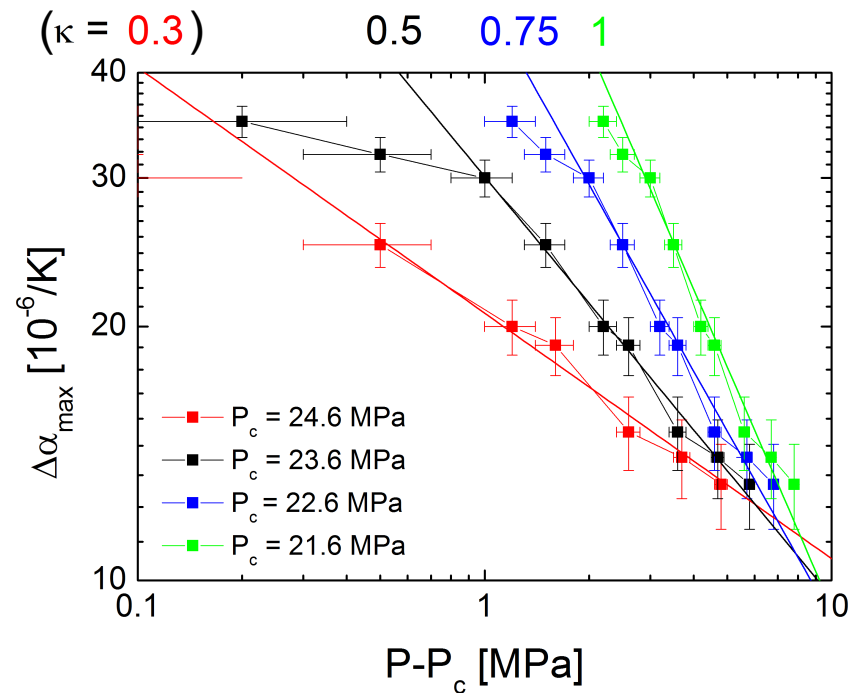


κ -CI at finite pressure

Scaling theory: $\Delta\alpha_{\max} \propto (P - P_c)^{-\kappa}$

Bartosch *et al.*, PRL **104**, 245701 (10)

$$\kappa = \frac{1 - \beta}{\beta + \gamma} = \begin{cases} 0 & \text{for "unconventional criticality" } (\beta = 1) \text{ ?!} \\ 7/15 & \text{for 2D Ising} \end{cases}$$



determination of κ
requires precise
knowledge of P_c !

crossover from 2D Ising ($\kappa \approx 0.5$) to mean-field ($\kappa \approx 0.3$) criticality?

Zacharias *et al.*, PRL **109**, 176401 (12)

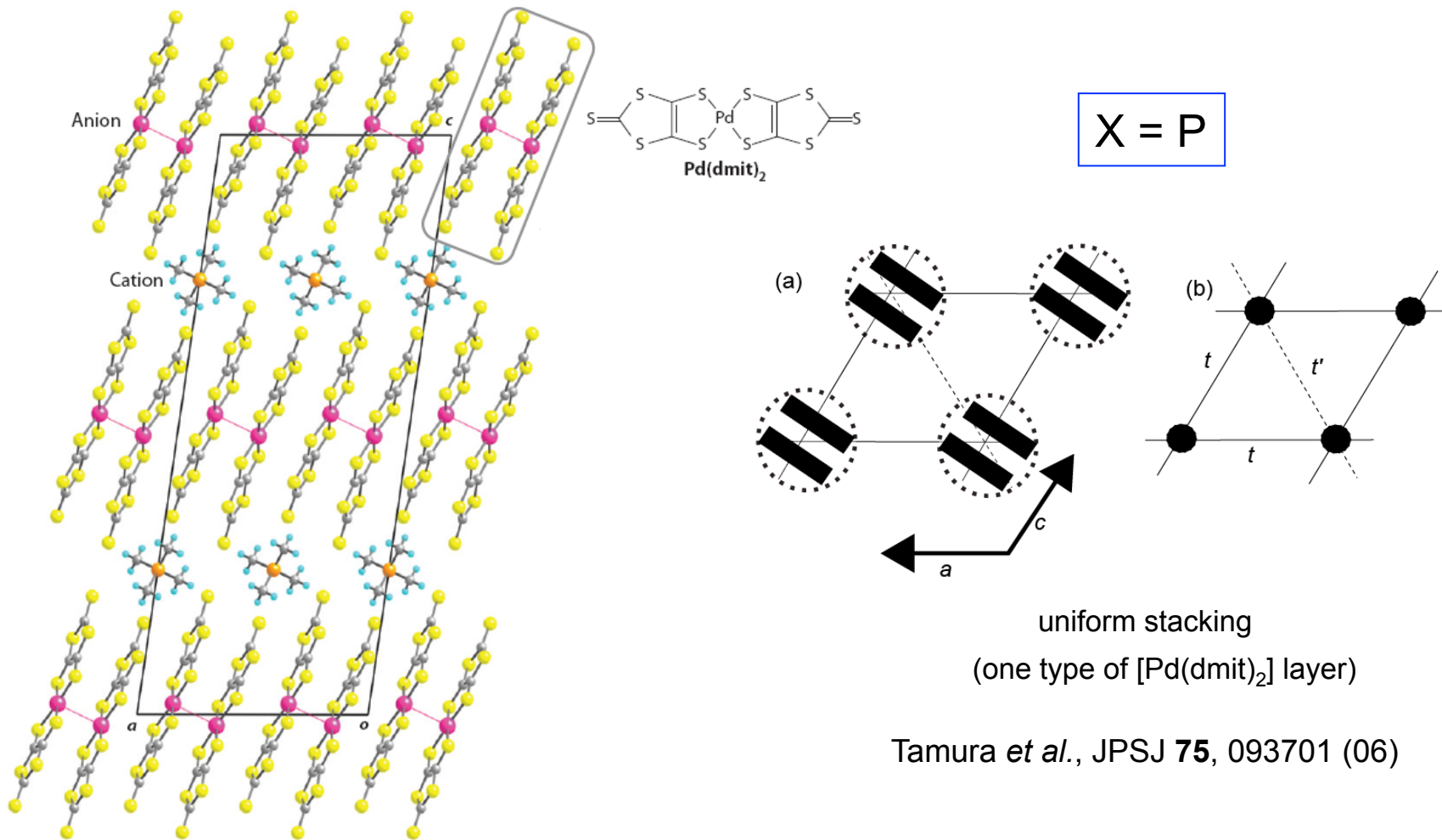
summary

- Thermal expansion measurements under ^4He -gas pressure have been performed on $\kappa\text{-(ET)}_2\text{X}$ for probing critical fluctuations.
- data of $\kappa\text{-D8-Br}$ and $\kappa\text{-Cl}$:
 - Mott critical end point is consistent with 2D Ising universality class.

outlook

- sample-to-sample variations
- determination of $P_c \Rightarrow \kappa = (1 - \beta)/(\beta + \gamma)$
- measurement in the insulating (low-P) regime \Rightarrow sign change in α !
- role of lattice degrees of freedom

EtMe₃X[Pd(dmit)₂]₂ (X = P/Sb)



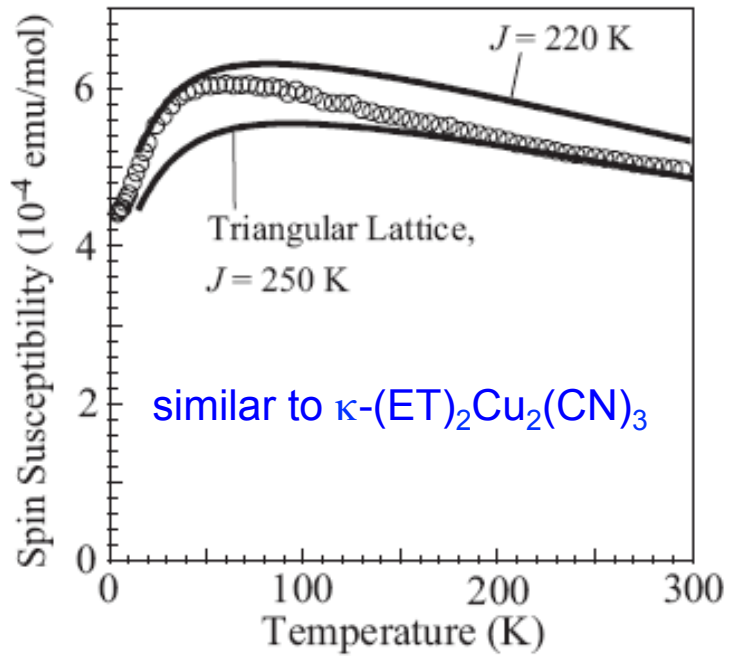
Tamura *et al.*, JPSJ **75**, 093701 (06)

Itou *et al.*, Nat. Phys. **6**, 673 (10)

K. Kanoda and R. Kato, Annu. Rev. Condens. Matter Phys. **2**, 167 (11)

EtMe₃X[Pd(dmit)₂]₂ – ground state properties

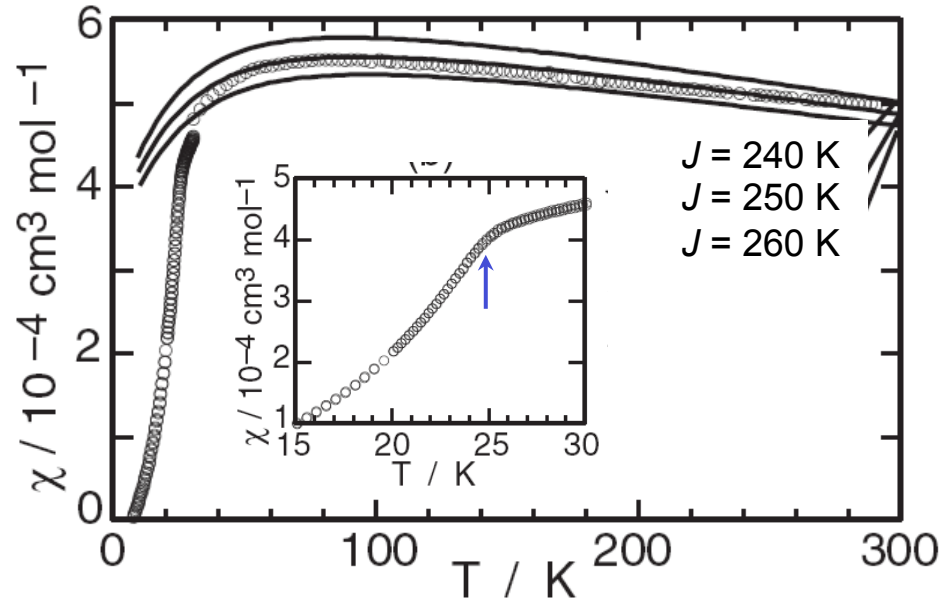
X = Sb ⇒ spin-liquid



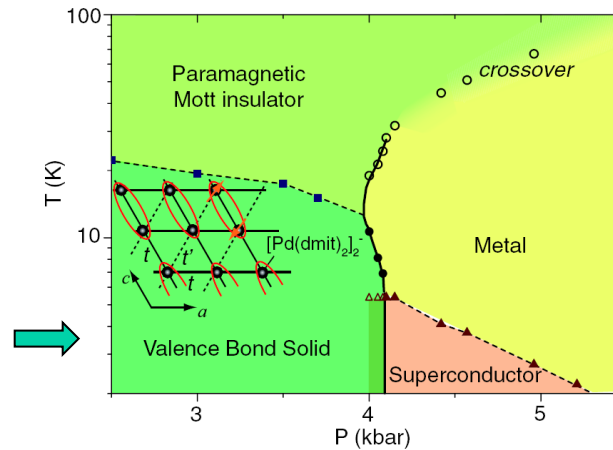
Itou *et al.*, PRB **77**, 104413 (08)

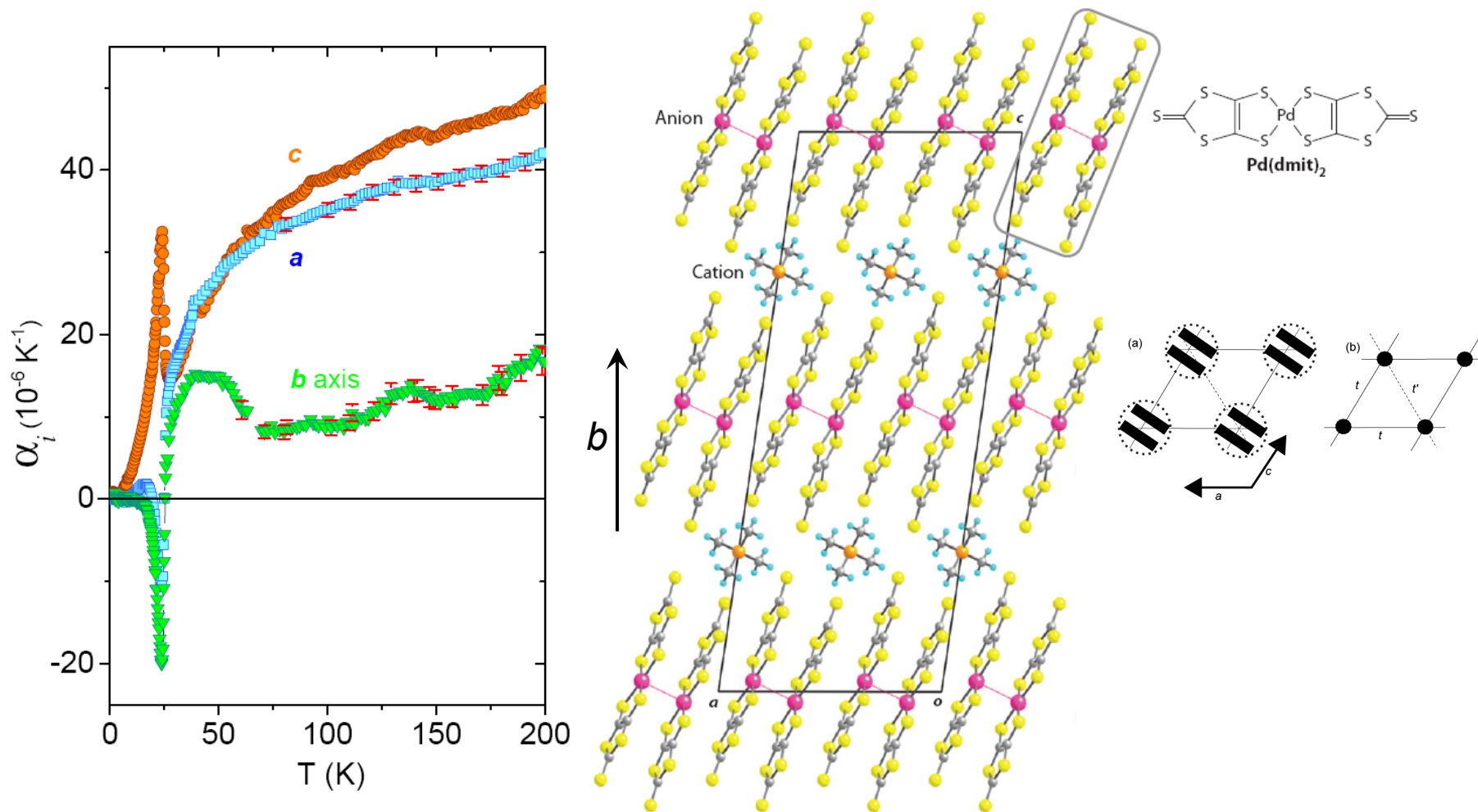
Shimizu *et al.*, PRL **99**, 256403 (07)

X = P ⇒ valence-bond-solid



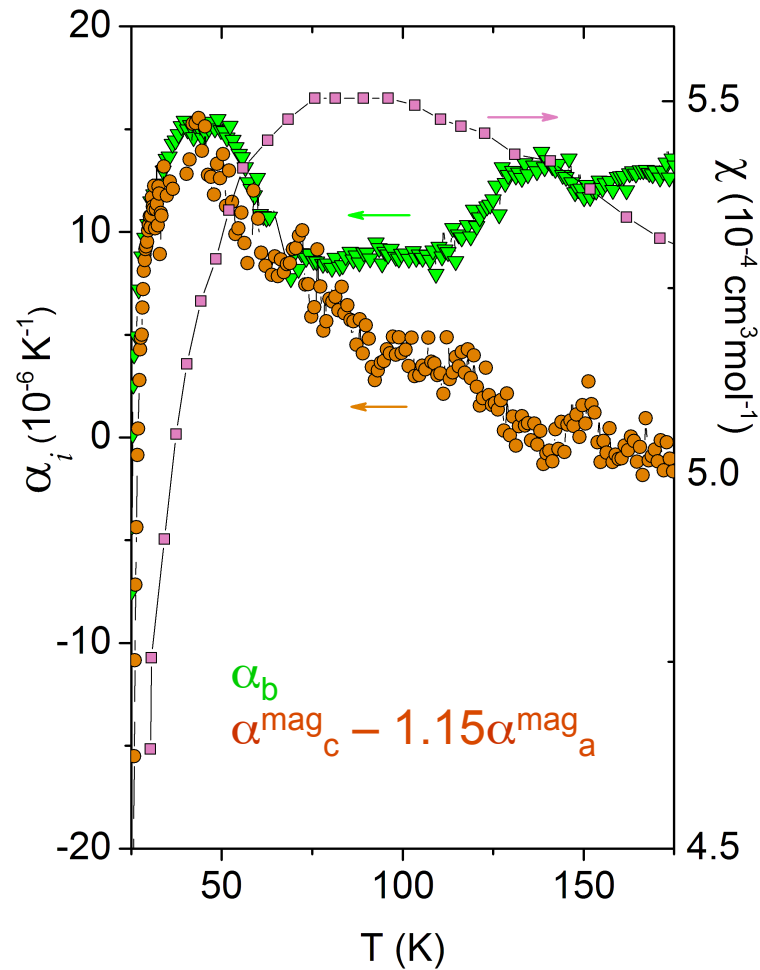
Tamura *et al.*, JPSJ **75**, 093701 (06)





- strongly anisotropic lattice distortions accompanying the formation of VBS
- weak in-plane α_a vs α_c anisotropy for $T > T_{\text{VBS}}$ suggests dominant contribution from EtMe₃P cations

anomalous thermal expansion in the paramagnetic region



Assumptions:

$$\alpha_a = \alpha_a^{\text{lat}} + \alpha_a^{\text{mag}}$$

$$\alpha_c = \alpha_c^{\text{lat}} + \alpha_c^{\text{mag}}$$

$$\alpha_c^{\text{lat}} = A\alpha_a^{\text{lat}}$$

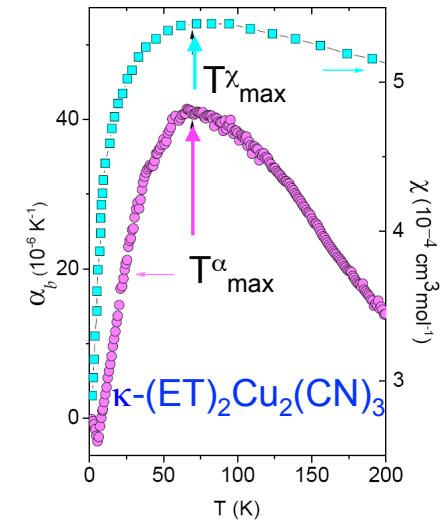
$$\alpha_c^{\text{mag}} = B\alpha_a^{\text{mag}}$$

anomalous contribution at $T_{\alpha_{\text{max}}}^{\alpha} \approx 40 \text{ K}$ due to the short-range afm correlation, cf. $T_{\chi_{\text{max}}}^{\chi} = 70 \text{ K}$

variation of $T_{\chi_{\max}}^{\chi} / T_{\max}^{\alpha} = T_{\chi_{\max}}^{\chi} / T_{\max}^C$ for low-D quantum magnets with different degree of frustration

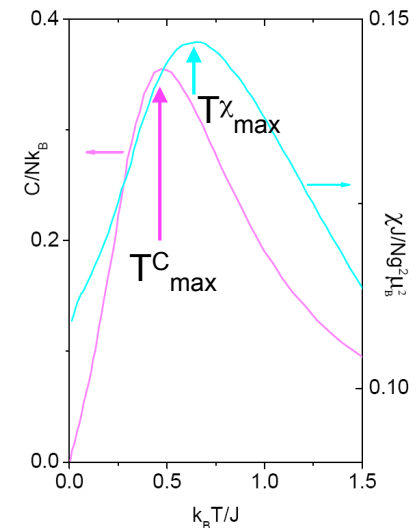
- for 2D triangular lattice $S = \frac{1}{2}$ Heisenberg afm ~ 1
- for Cs_2CuBr_4 : $J'/J = 0.74$
- for $\kappa\text{-(ET)}_2\text{Cu}_2(\text{CN})_3$: $J'/J = 0.64 - 0.74$

Shimizu *et al.*, PRL **91**, 107001 (03)
 R. S. Manna *et al.*, PRL **104**, 016403 (10)

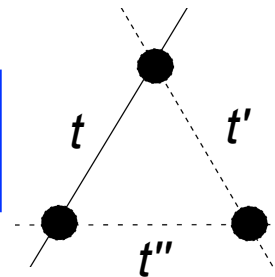


- for 1D uniform $S = \frac{1}{2}$ Heisenberg chain ~ 1.34 ,
 for alternating exchange variant ~ 3 and
 including next-nearest-neighbor interactions ~ 3.6

Klümper, Eur. Phys. J. B **5**, 677 (98)
 Bühler *et al.*, PRB **64**, 024428 (01)

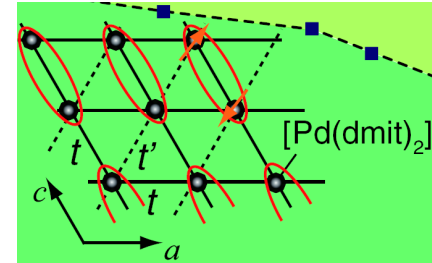
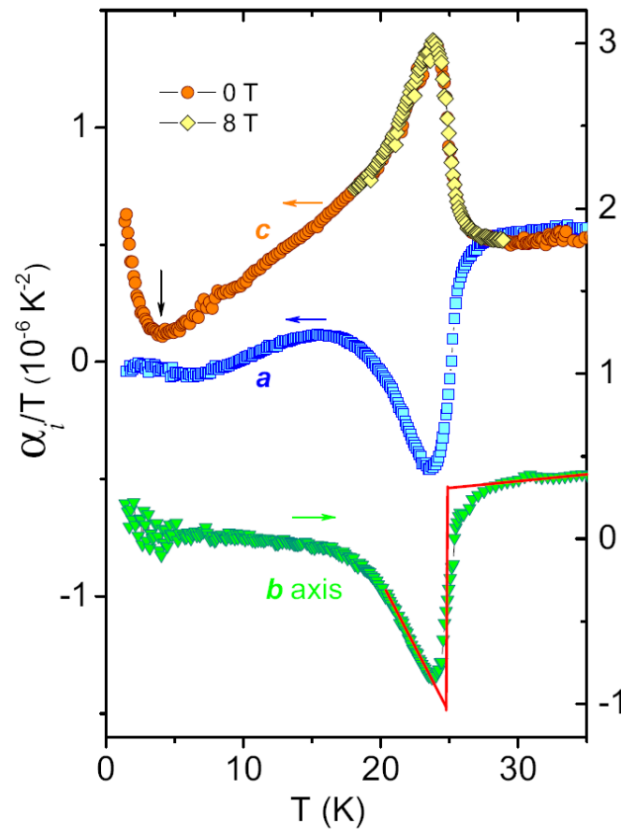


present case: $T_{\chi_{\max}}^{\chi} / T_{\max}^{\alpha} \approx 1.7 - 2.3$
 \Rightarrow suggests a more anisotropic (quasi-1D) scenario



R. S. Manna *et al.*, PRB **89**, 045113 (14)

lattice distortion at VBS transition



R. S. Manna *et al.*, PRB 89, 045113 (14)

- distinct and strongly anisotropic second-order phase transition into the low-T VBS phase at 25 K
- upon cooling c -axis (in-plane) contracts, a -axis (in-plane) expands while the dominant effect is along the b -axis (out-of-plane) which expands
- \Rightarrow pressure dependency comes from the out-of-plane component as the in-plane pressure effects cancel each other out (- 4.2 K/100 MPa)

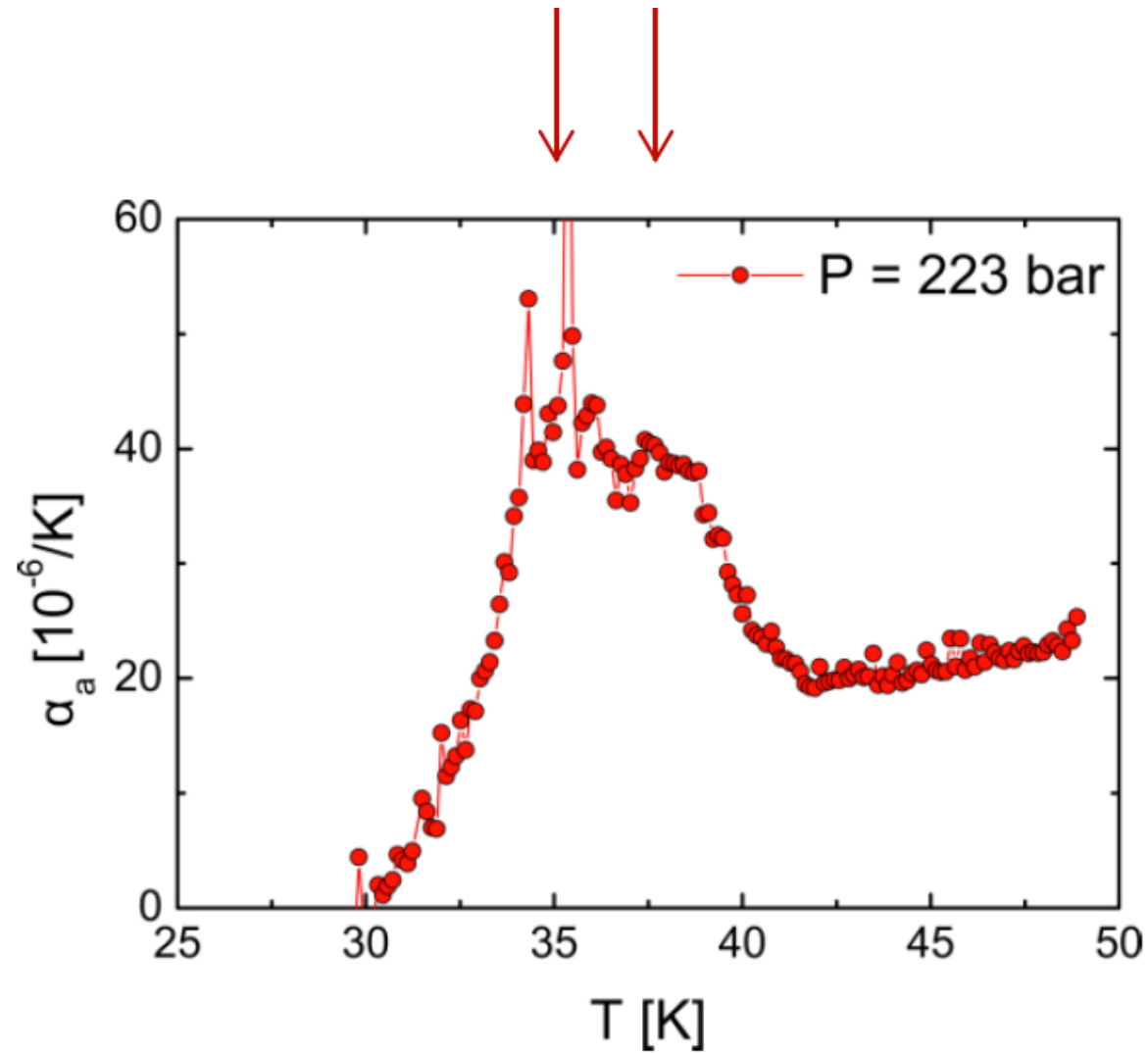
summary

- valence-bond-solid, $\text{EtMe}_3\text{P}[\text{Pd}(\text{dmit})_2]_2$
 - An anomalous contribution at $T_{\text{max}}^{\alpha} \approx 40$ K is found and assigned to the short-range afm correlations.
 - $T_{\text{max}}^{\chi} / T_{\text{max}}^{\alpha} \approx 1.7 - 2.3$ seems incompatible with quasi-2D triangular lattice (~ 1), rather compatible with a quasi-1D more anisotropic scenario.

outlook

- perform similar experiments for the spin-liquid (dmit-Sb) compound
- study the Mott criticality in dmit-salts vs ET-based compounds ?!

Thank you for your attention !

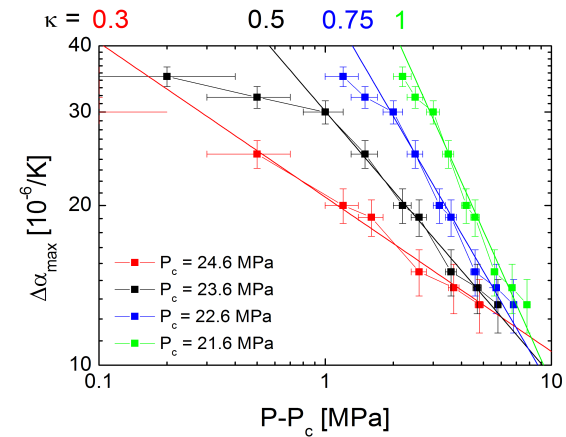
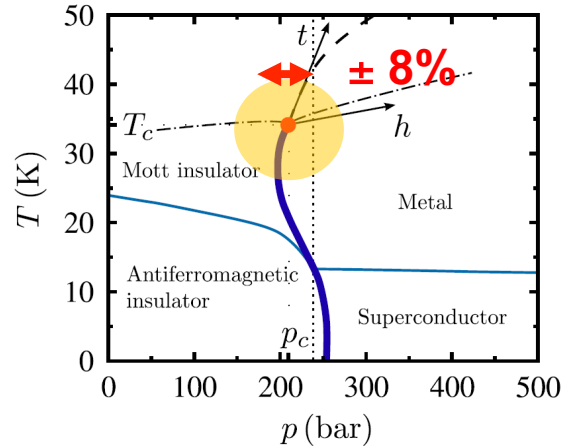


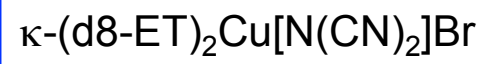
closer to P_0 : occurrence of double-peak structure, interference of another phase transition (intrinsic) or bicrystal (extrinsic)?

coupling to the lattice degrees of freedom

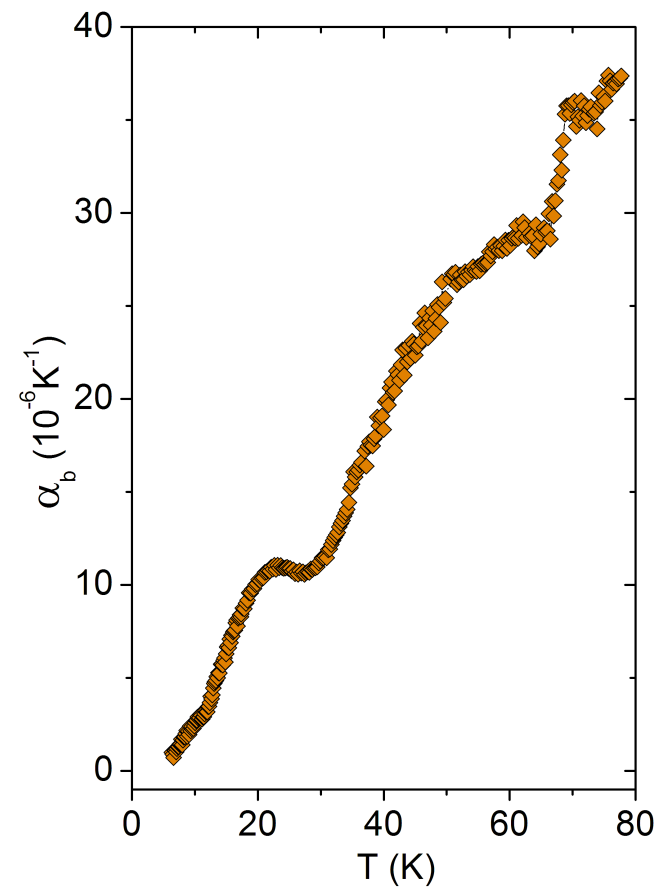
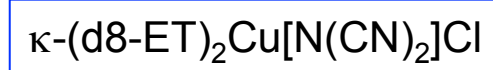
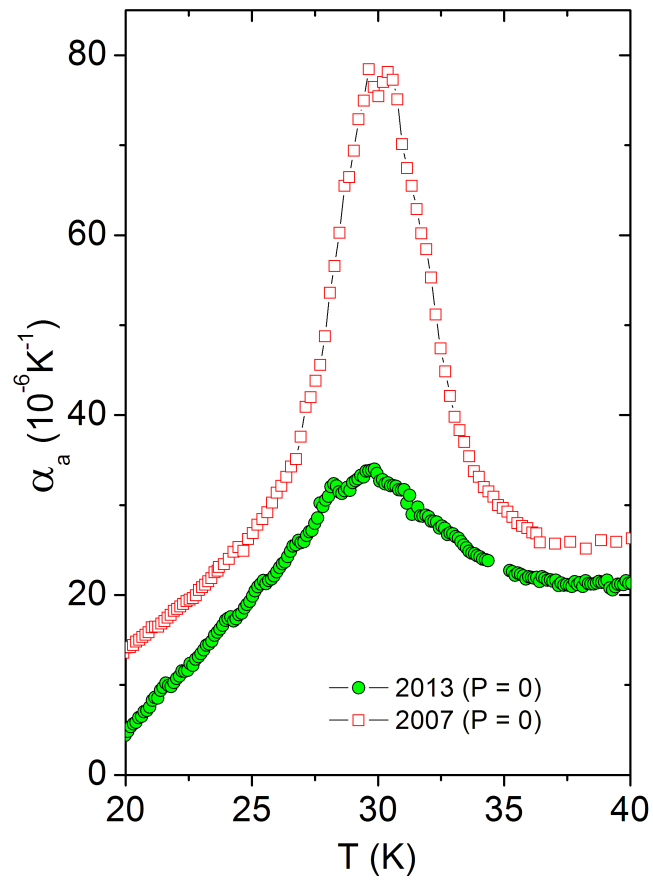
Zacharias *et al.*, PRL **109**, 176401 (12)

Approaching (P_0, T_0) : crossover to mean-field criticality ($\kappa_{MF} = 0.33$)





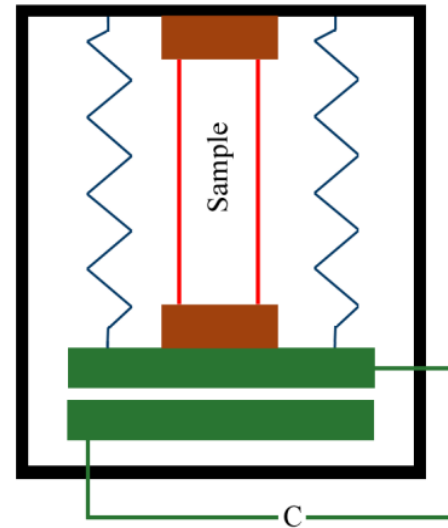
sample-to-sample dependency



high-resolution dilatometry



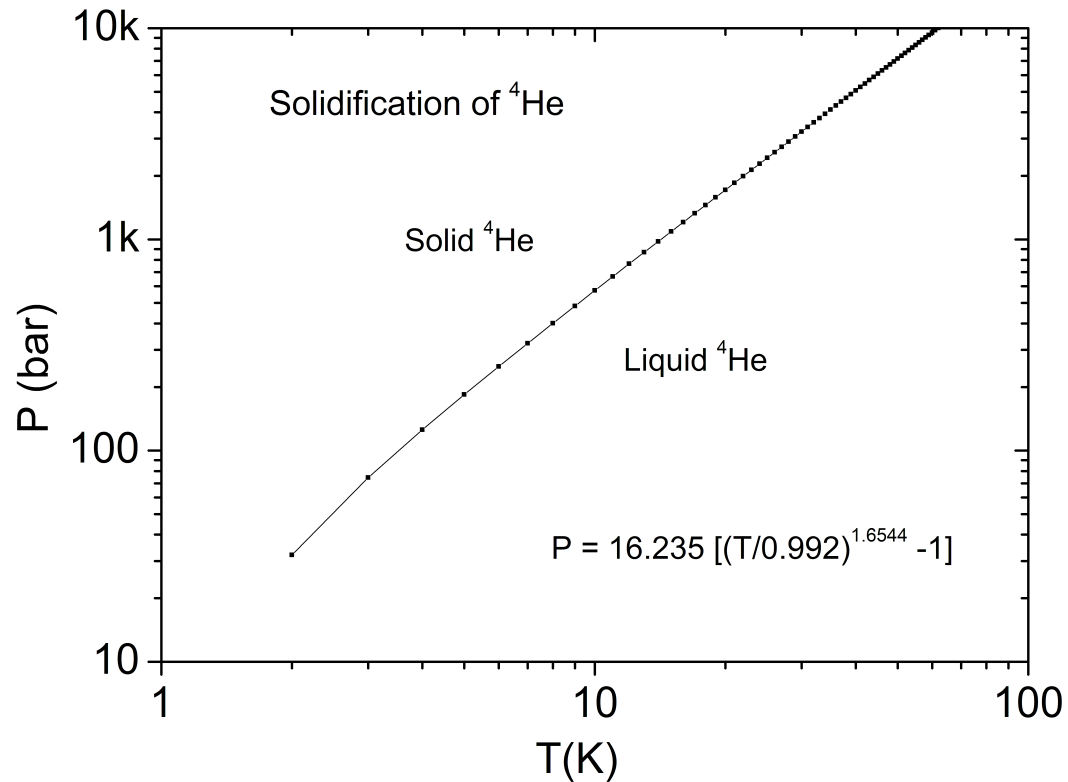
30 mm



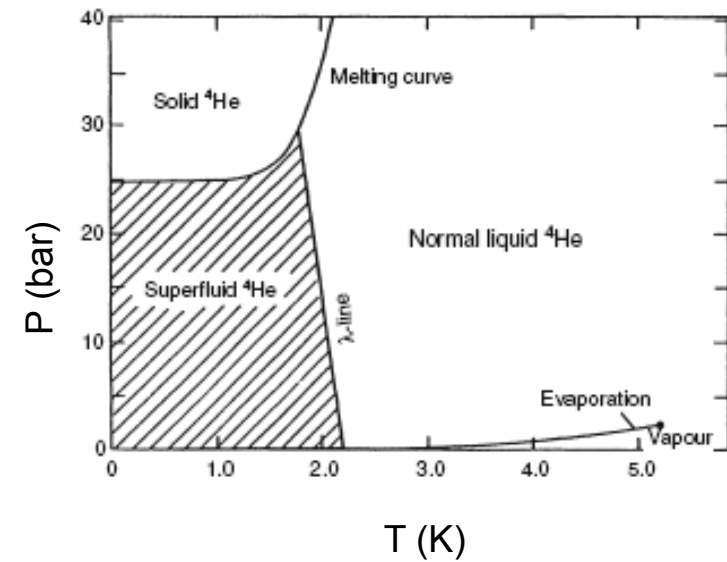
resolution: $\Delta l/l \sim 10^{-10}$ (for $l = 10$ mm)

Thermal expansion coefficient, $\alpha_i = \frac{1}{l_i} \left(\frac{\partial l_i}{\partial T} \right)_p$

experimental limitation

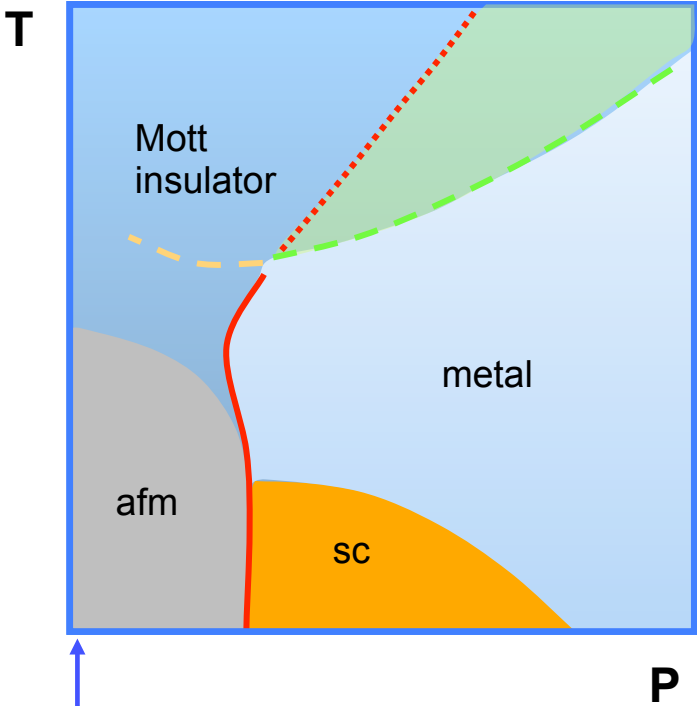


Langer, J. Phys. Chem. Solids **21**, 122 (61)



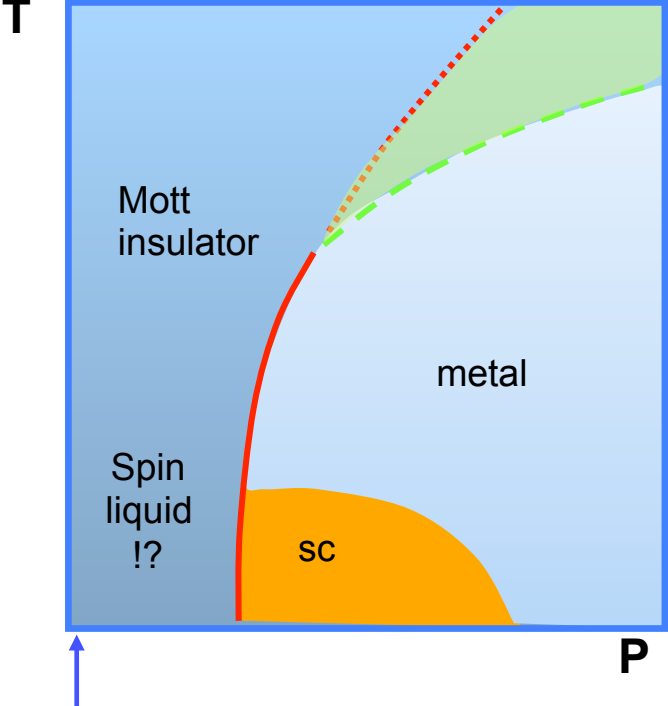
F. Pobell, *Matter and Methods at Low Temperatures*, Springer

Phase diagrams



$T_N \sim 27$ K, long-range magnetic order

Lefebvre *et al.*, PRL **85**, 5420 (00)



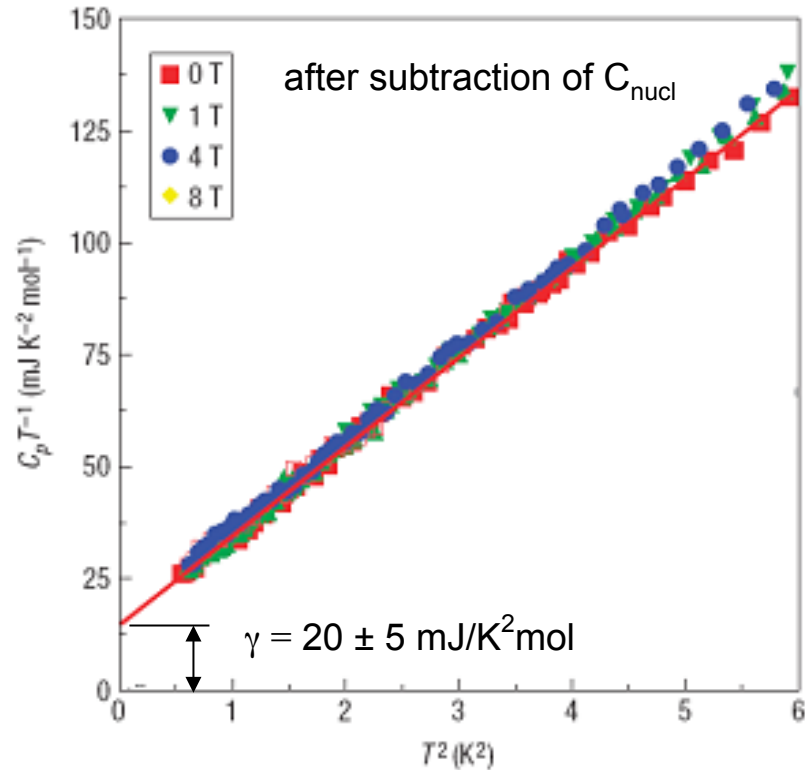
no long-range magnetic order down to 32 mK

Kurosaki *et al.*, PRL **95**, 177001 (05)

Shimizu *et al.*, PRL **91**, 107001 (03)

low-energy excitations

Specific heat

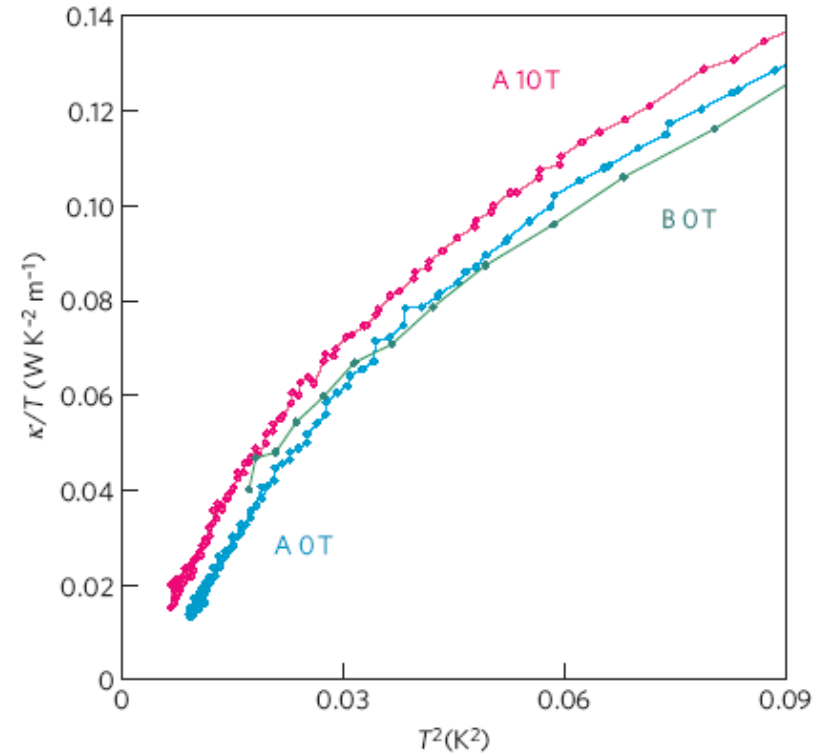


$$(C_P/T)_{T \rightarrow 0} = \gamma_0$$

'gapless spinons with a Fermi surface'

Yamashita *et al.*, Nat. Phys. **4**, 459 (08)

Thermal conductivity



$$(\kappa/T)_{T \rightarrow 0} = 0$$

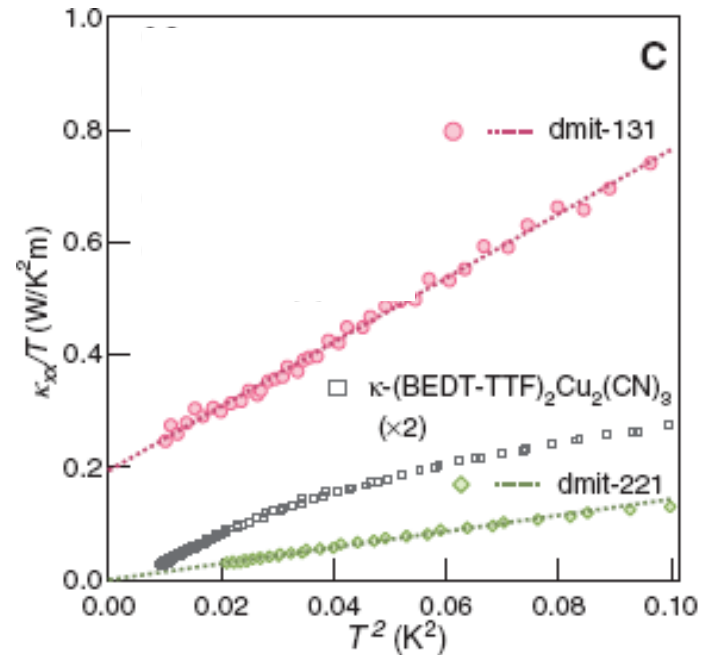
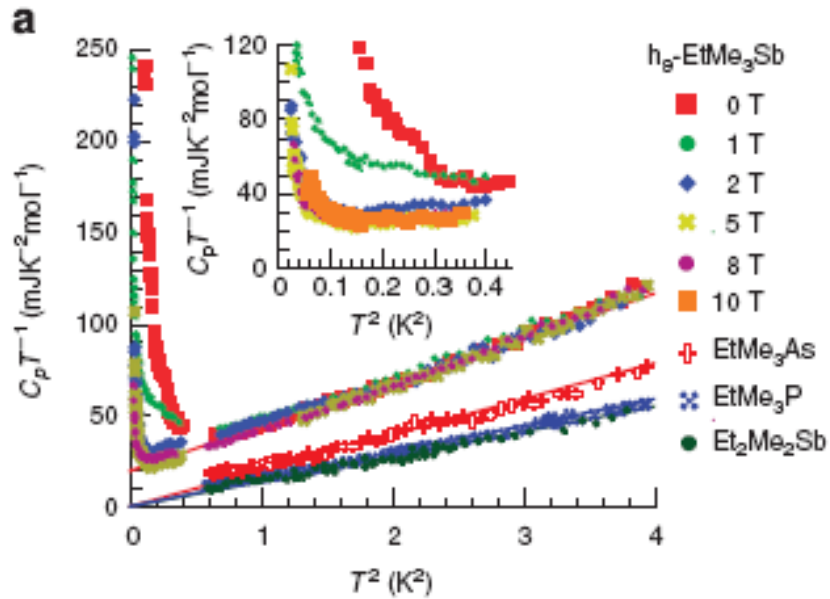
'spin gap of $\Delta = 0.46 \text{ K} \sim J/500$ '

Yamashita *et al.*, Nat. Phys. **5**, 44 (09)

low-energy excitations: $\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$

Specific heat

Thermal conductivity



'gapless spinons with a Fermi surface'

Yamashita *et al.*, Nat. Commun. **2**, 275 (11)

Yamashita *et al.*, Science **328**, 1246 (10)

Exponent	Ising ₂	Ising ₃	XY ₃	Heisenberg ₃
α	0(log)	0.110(1)	-0.015	-0.10
β	1/8	0.3265(3)	0.35	0.36
γ	7/4	1.2372(5)	1.32	1.39
δ	15	4.789(2)	4.78	5.11

$$C(t) \propto |t|^{-\alpha}$$

$$m(t) \propto (-t)^\beta, t \leq 0$$

$$\chi(t) \propto |t|^{-\gamma}$$

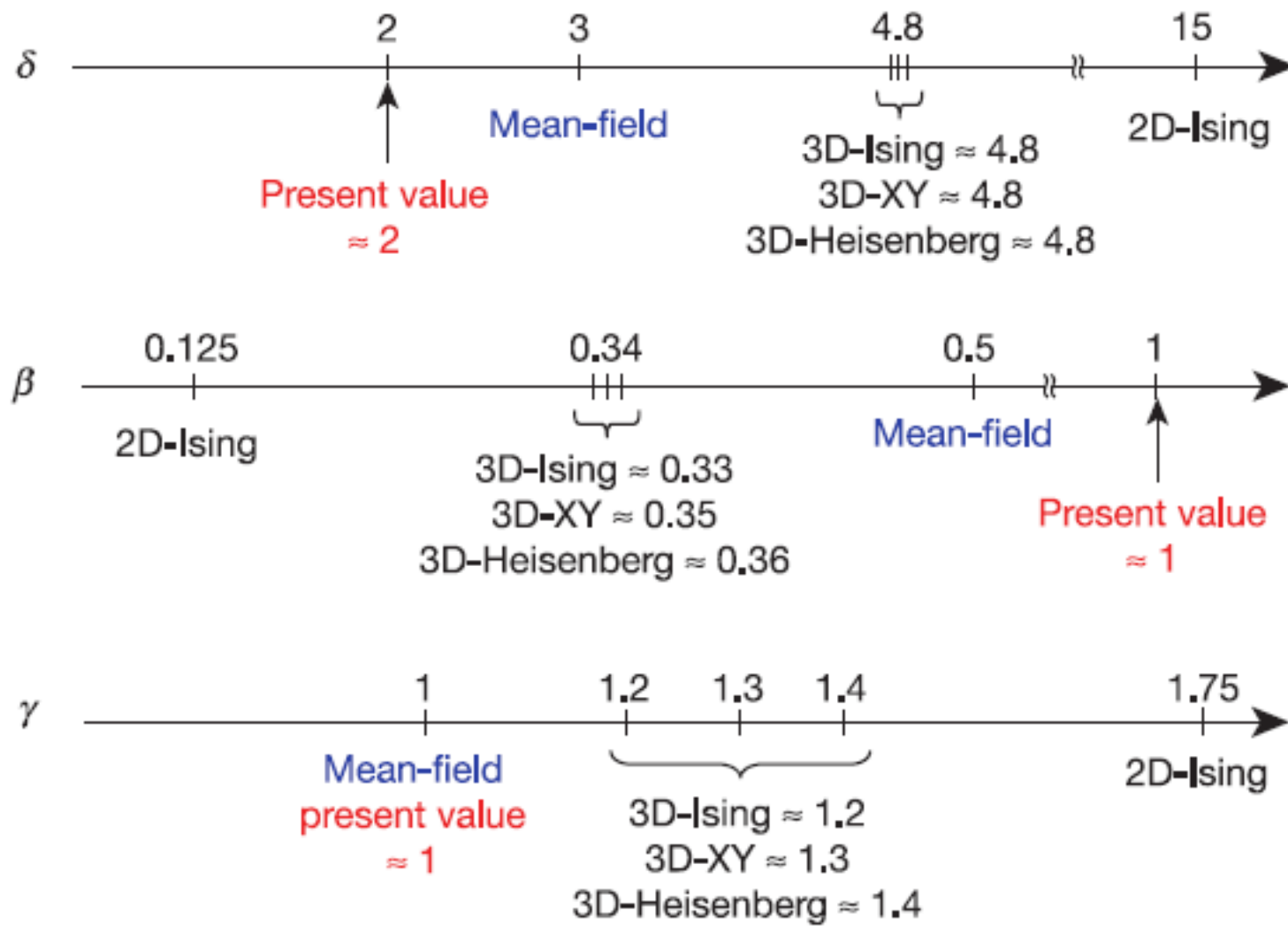
$$m(h) \propto |h|^{1/\delta} \text{sgn}(h), t = 0$$

$C(t)$ = sp. Heat

$m(t)$ = spontaneous magnetization

$\chi(t)$ = mag. Susceptibility

$m(h)$ = critical isotherm



- Lattice coupling changes the critical properties of the electronic system drastically so that eventually Landau mean-field behavior (corresponding to $m_f = 0.33$) prevails close to the Mott critical end point.

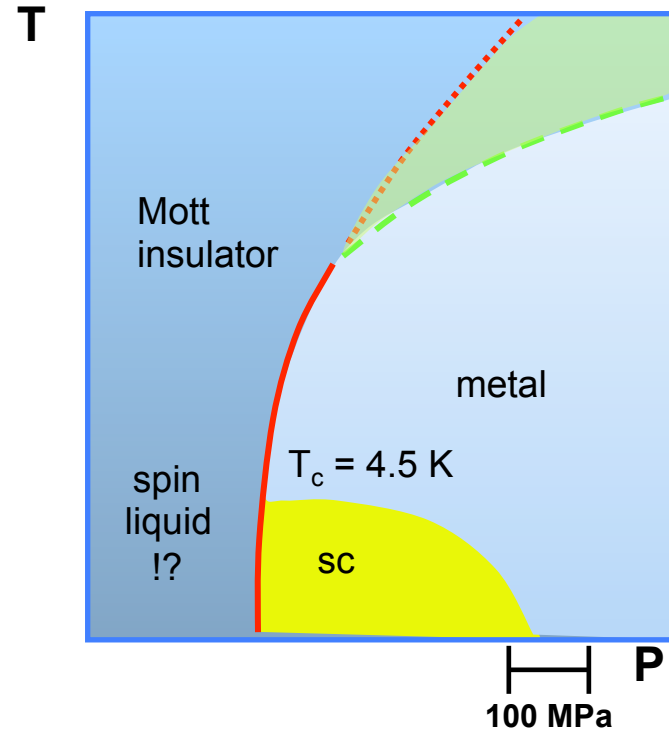
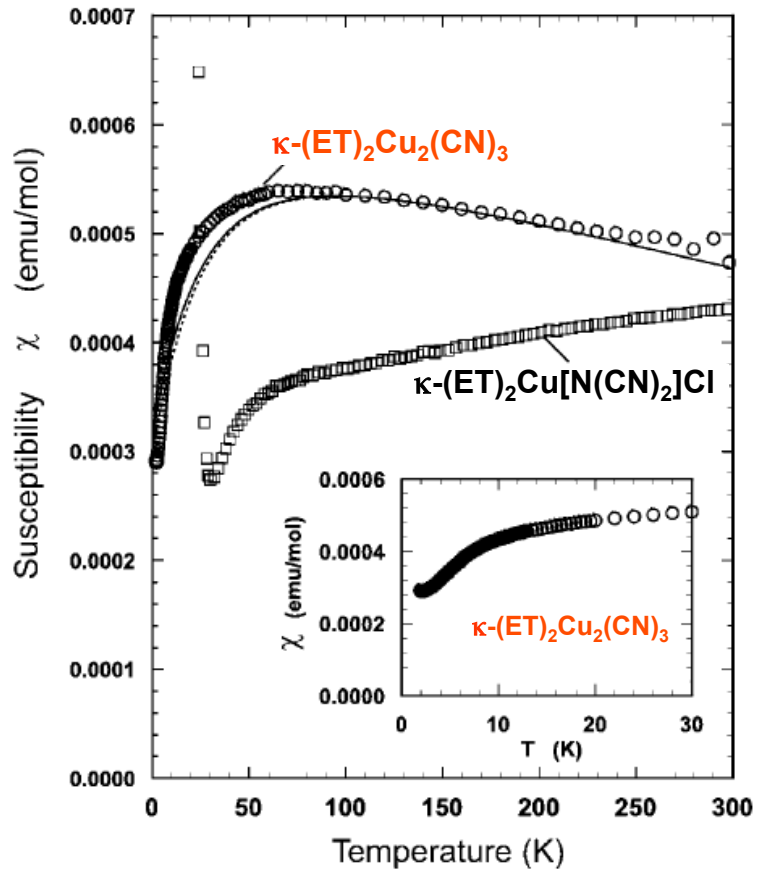
- κ -(BEDT-TTF)₂X systems yields a width of the Landau critical regime $\Delta T_0/T_0$ of about 8%, which is experimentally accessible the flattening of the preliminary α_{\max} vs $(p - p_0)$ data might indicate such a crossover behavior.

Zacharias *et al.*, PRL **109**, 176401 (12)

Crossover from 2D Ising ($\kappa \approx 0.5$) to mean-field ($\kappa \approx 0.3$) criticality?

Zacharias *et al.*, PRL **109**, 176401 (12)

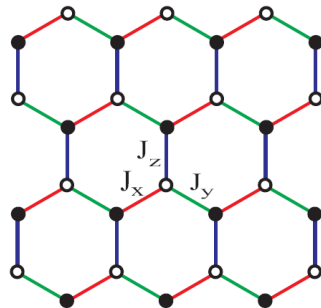
spin-liquid - $\kappa\text{-(ET)}_2\text{Cu}_2(\text{CN})_3$



$$X = \text{Cu}_2(\text{CN})_3$$

$$t'/t \sim 0.8$$

Kitaev spin-liquid
 A_2IrO_3 (A = Na, Li)



no long-range magnetic order down to 32 mK ($J = 250 \text{ K}$)

R. S. Manna *et al.*, PRL **104**, 016403 (10)

Kurosaki *et al.*, PRL **95**, 177001 (05)

Shimizu *et al.*, PRL **91**, 107001 (03)