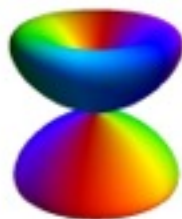
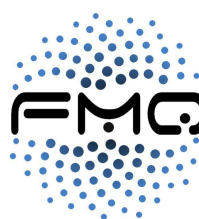


Spin-orbit Induced and Dynamics in Mott Insulating Iridates

George Jackeli

Max-Planck Institute & University of Stuttgart, Germany
Andronikashvili Institute of Physics, Tbilisi, Georgia

Workshop on Current Trends in Frustrated Magnetism
JNU, New Delhi, Feb 13, 2015



In collaboration with:

Theory:

G. Khaliullin (MPI Stuttgart) & J. Chaloupka (Uni Brno)

Experiment:

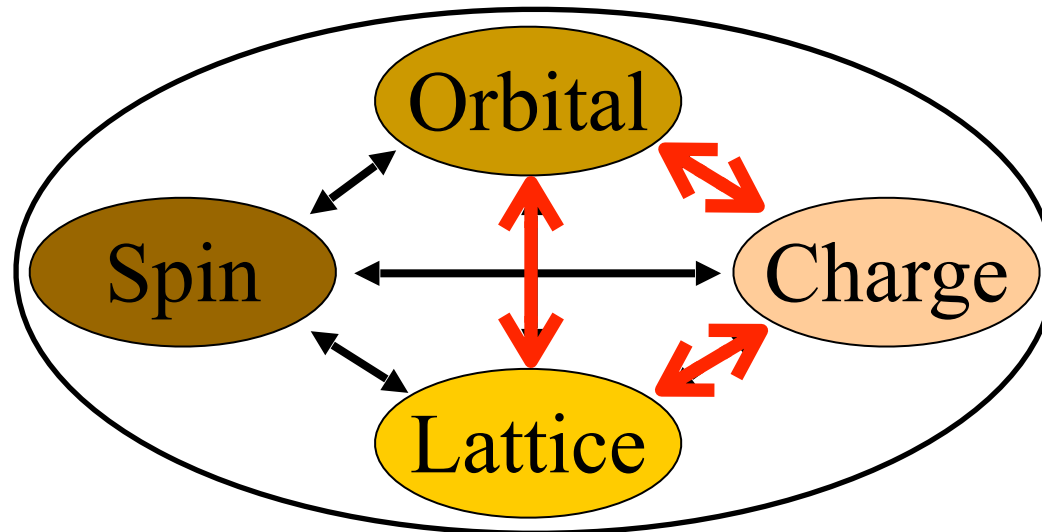
BJ. Kim (MPI Stuttgart),
V. Kataev (IFW Dresden) , H. Takagi (MPI Stuttgart & Uni Tokyo)

References:

- GJ & G.Khaliullin, PRL 102, 017205 (2009)
- 103, 067205 (2009)
- J.Chaloupka, GJ & G.Khaliullin, PRL 105, 027204 (2010)
- 110, 097204 (2013)
- Kim et al, PRL 109, 037204 (2012)
- 109, 157402 (2012)
- Bahr et al, PRB 180401(R) (2014)

Transition metal oxides: many challenges

- d- electrons are partially filled and not very extended
- Interactions dominate over kinetic energy
- Many degrees of freedom are at work



Metal to Magnetic Insulator

High-T_c Superconductivity
Colossal Magnetoresistance

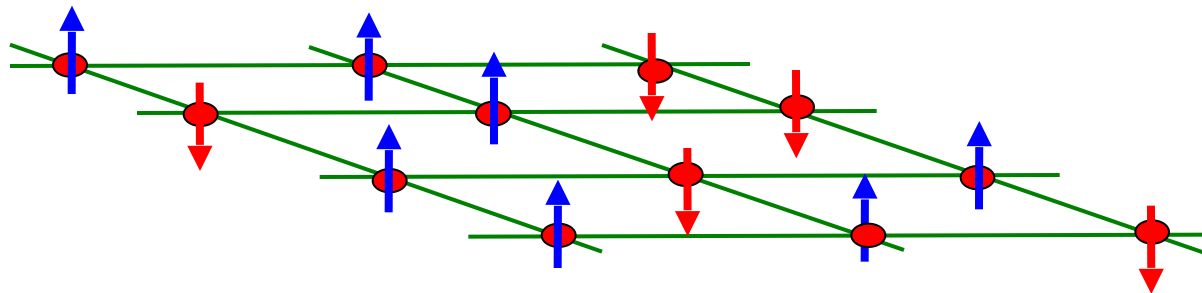
Unexpected variety of phases
and transitions between them

Most of the elements are Transition metals

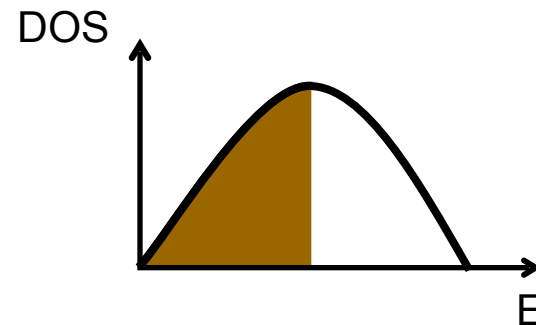
Group →	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	
↓ Period																			
1	1 H																		2 He
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne	
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar	
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr	
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe	
6	55 Cs	56 Ba		72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn	
7	87 Fr	88 Ra		104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Uut	114 Fl	115 Uup	116 Lv	117 Uus	118 Uuo	
Lanthanides			57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu		
Actinides			89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr		

Mott Insulator

one electron per site

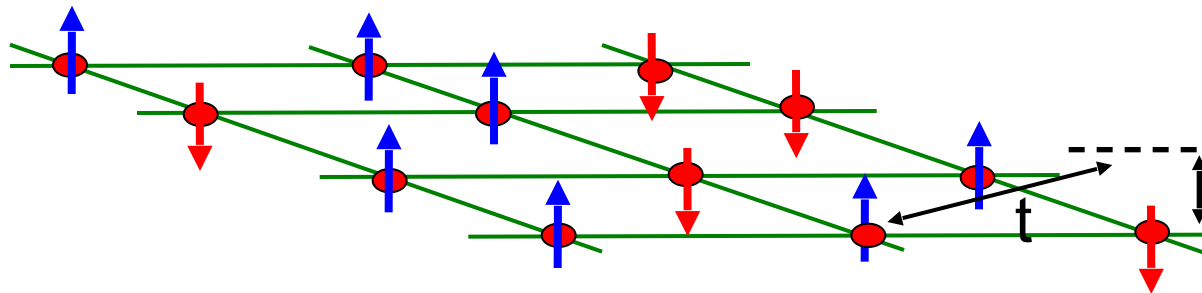


half-filled band: metal

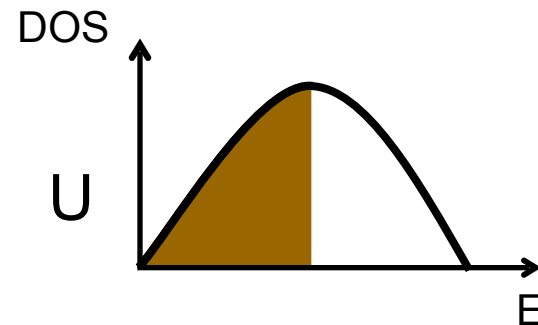


Mott Insulator

one electron per site

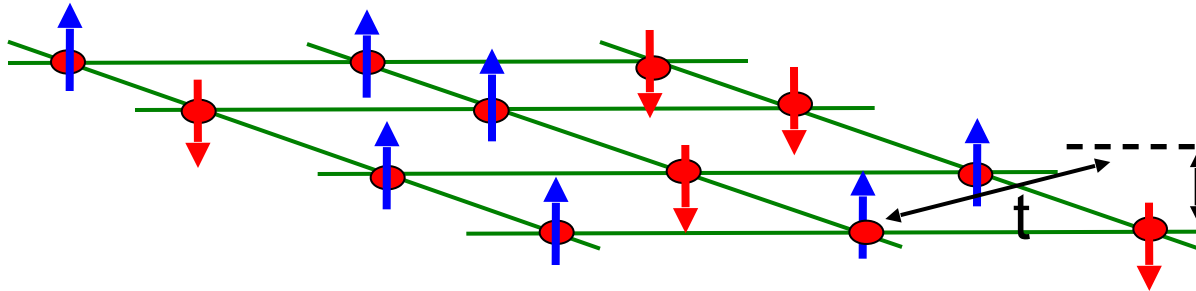


half-filled band: metal

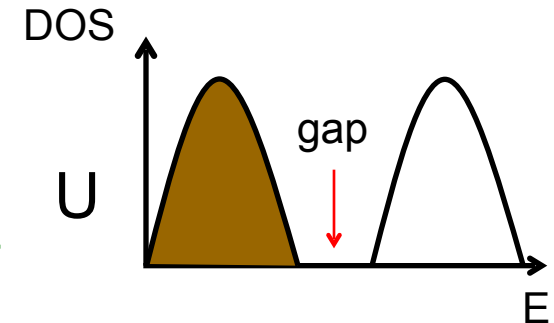


Mott Insulator

one electron per site



half-filled band: insulator

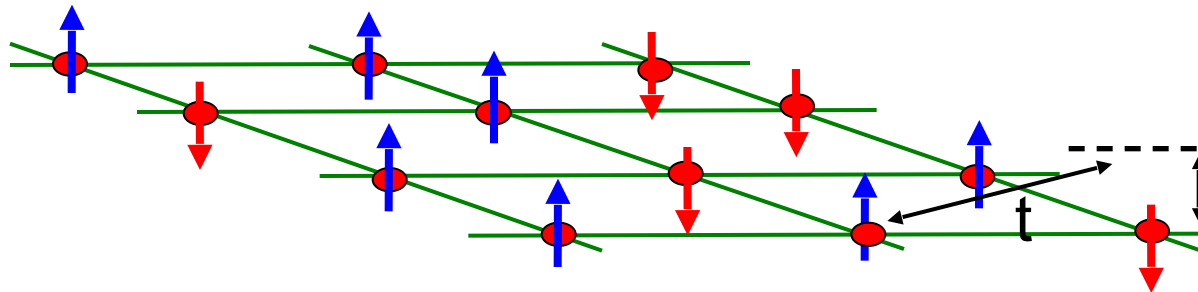


Sir Nevill Mott
(Nobel prize '77)

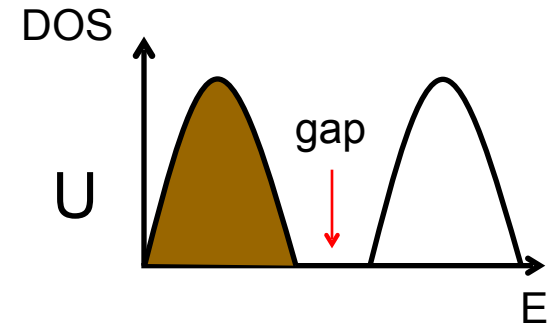
Coulomb repulsion $U \gg t$ Kinetic energy,
Charges become localized and gapped

Mott Insulator

one electron per site



half-filled band: insulator



Sir Nevill Mott
(Nobel prize '77)

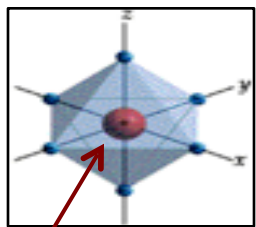
Coulomb repulsion $U \gg t$ Kinetic energy,
Charges become localized and gapped



Werner Heisenberg
(Nobel prize '32)

Low energy degrees are magnetic:
Spins interacting via Heisenberg exchange

$$H = J \sum_{ij} \left[\vec{S}_i \vec{S}_j - 1/4 \right] \quad J = \frac{4t^2}{U}$$



Transition metal ion

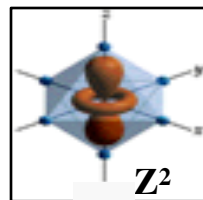
d-level



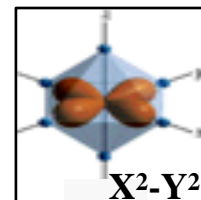
e_g



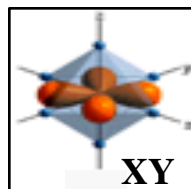
t_{2g}



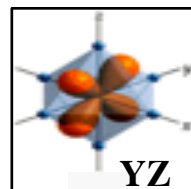
Z^2



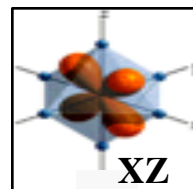
X^2-Y^2



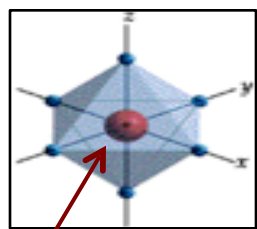
XY



YZ

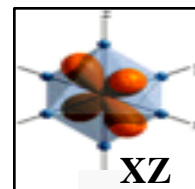
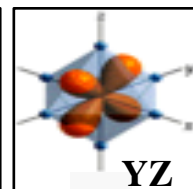
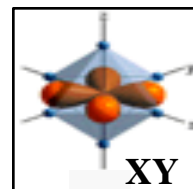
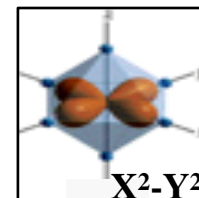
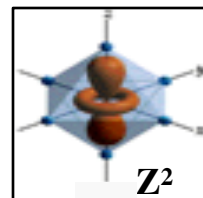
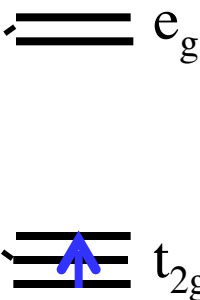


XZ



Transition metal ion

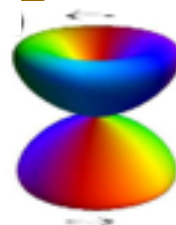
d-level



Unquenched angular momentum $L = -l_{\text{eff}} = 1$



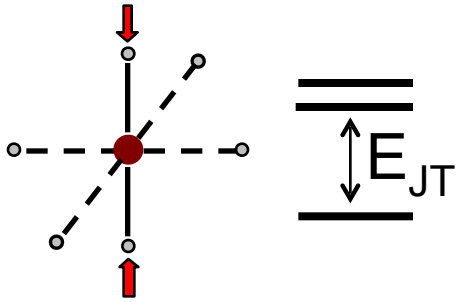
$$|l_z=0\rangle \equiv |xy\rangle$$



$$|l_z=\pm 1\rangle \equiv -\frac{1}{\sqrt{2}}(i|xz\rangle \pm |yz\rangle)$$

Three different couplings & regimes in spin-orbital systems

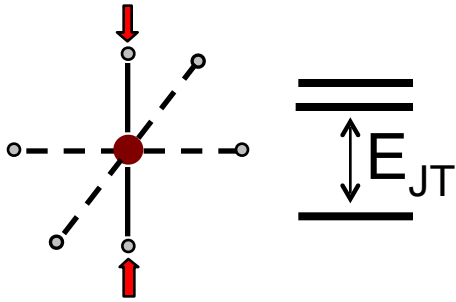
Jahn-Teller coupling- E_{JT}



orbitals are rigidly ordered:
spin-only Heisenberg model

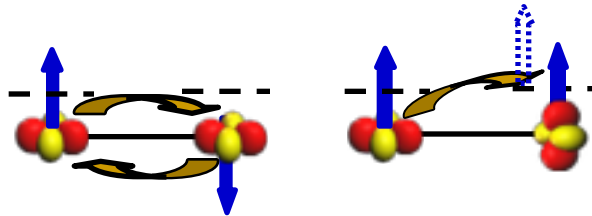
Three different couplings & regimes in spin-orbital systems

Jahn-Teller coupling- E_{JT}

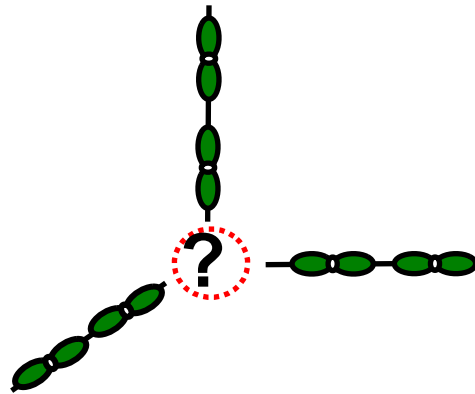


orbitals are rigidly ordered:
spin-only Heisenberg model

exchange interactions- J



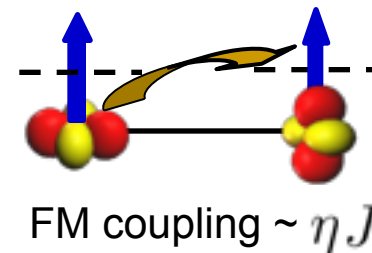
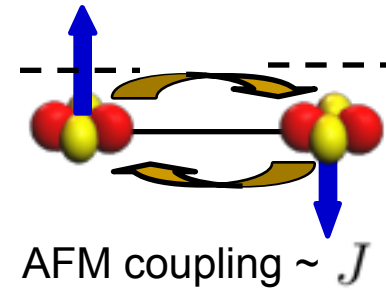
spin exchange depends on
orbital occupancy:
directional character of
orbitals induces frustration



Coupled spin-orbital model

$$H = J_{\text{AF}} \sum_{\langle ij \rangle} \left[\vec{S}_i \cdot \vec{S}_j / S^2 - 1 \right] O_{ij}^{\text{OF}}$$

$$- \sum_{\langle ij \rangle} \left[J_{\text{O}} + J_{\text{F}} \vec{S}_i \cdot \vec{S}_j / S^2 \right] O_{ij}^{\text{OAF}}$$



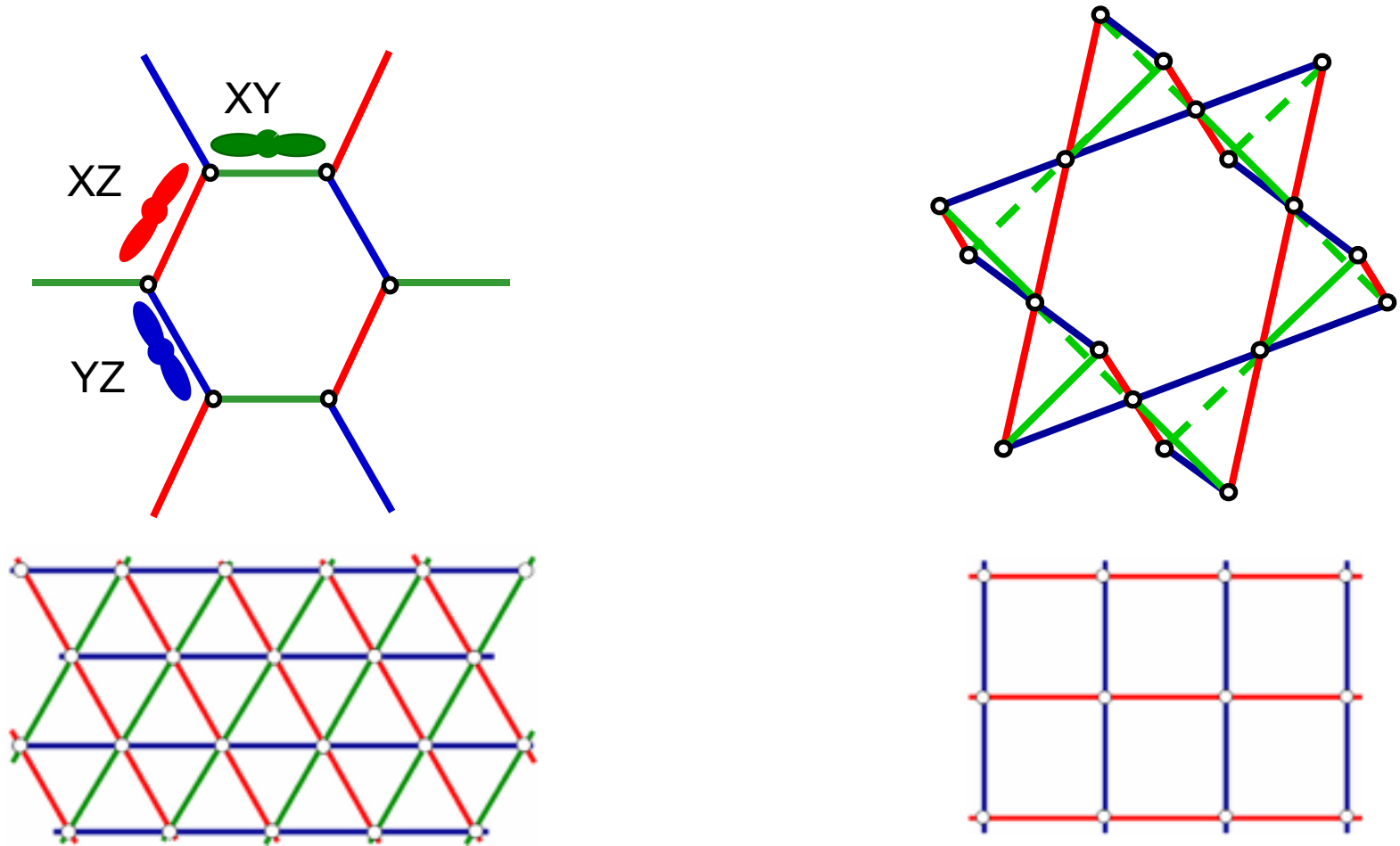
Exchange couplings:

$$J_{\text{AF}} \simeq J_{\text{O}} \sim J = t^2 / U$$

$$J_{\text{F}} \sim \eta J, \quad \eta = J_{\text{H}} / U \ll 1$$

Orbital degrees are static Pott's-like!

Directional orbitals on a family of lattices

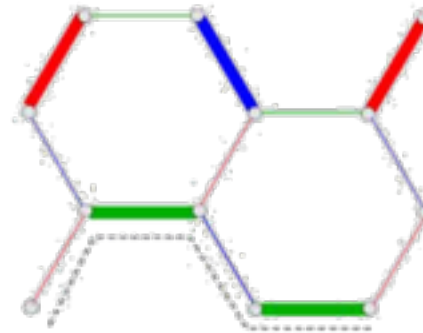
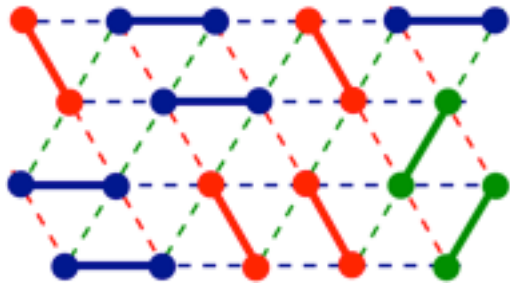


Ground state manifold: Hard core dimers

GJ & Ivanov PRB (2007)

GJ & Khomskii PRL (2008)

- Ground state manifold is spanned by hard-core dimer coverings



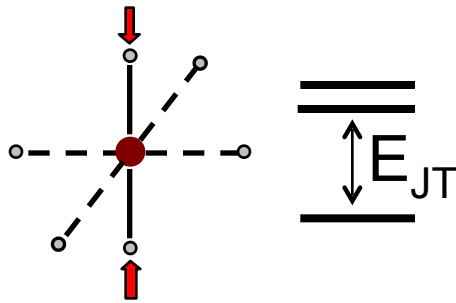
- Spins are bound into spin-singlet on dimer bonds: Spin gaped phase



- Extensive orientational degeneracy infinitely many ways of covering
Different coverings are orthogonal due to orbitals

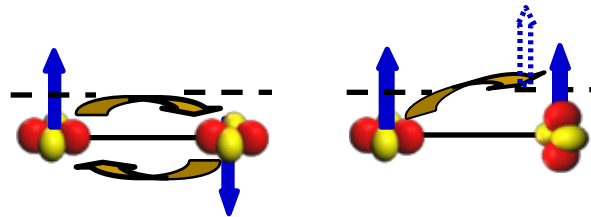
Three different couplings & regimes in spin-orbital systems

Jahn-Teller coupling- E_{JT}

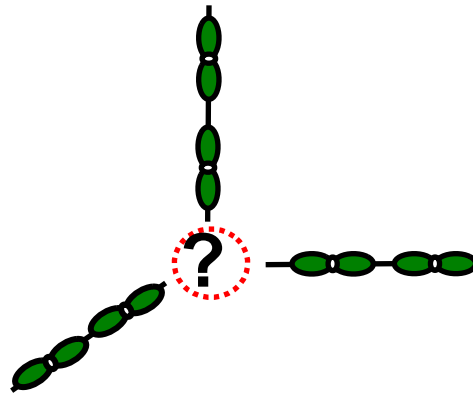


orbitals are rigidly ordered:
spin-only Heisenberg model

exchange interactions- J



spin exchange depends on
orbital occupancy:
directional character of
orbitals induces frustration



spin-orbit coupling- λ



spins & orbitals locally
entangled:
orbital frustration &
directional character are
converted to isospins

correlations



21 Sc 44.9559 Scandium	22 Ti 47.867 Titanium	23 V 50.9415 Vanadium	24 Cr 51.9961 Chromium	25 Mn 54.938 Manganese	26 Fe 55.845 Iron	27 Co 58.9332 Cobalt	28 Ni 58.6934 Nickel	29 Cu 63.546 Copper	30 Zn 65.4089 Zinc
39 Y 88.9058 Yttrium	40 Zr 91.224 Zirconium	41 Nb 92.9064 Niobium	42 Mo 85.94 Molybdenum	43 Tc 98 Technetium	44 Ru 101.07 Ruthenium	45 Rh 102.9055 Rhodium	46 Pd 106.42 Palladium	47 Ag 107.8682 Silver	48 Cd 112.411 Cadmium
71 Lu 174.967 Lutetium	72 Hf 178.49 Hafnium	73 Ta 180.9497 Tantalum	74 W 183.84 Tungsten	75 Re 186.207 Rhenium	76 Os 190.23 Osmium	77 Ir 192.217 Iridium	78 Pt 195.084 Platinum	79 Au 196.9666 Gold	80 Hg 200.59 Mercury



spin-orbit

correlations



21 Sc 44.9559 Scandium	22 Ti 47.867 Titanium	23 V 50.9415 Vanadium	24 Cr 51.9961 Chromium	25 Mn 54.938 Manganese	26 Fe 55.845 Iron	27 Co 58.9332 Cobalt	28 Ni 58.6934 Nickel	29 Cu 63.546 Copper	30 Zn 65.4089 Zinc
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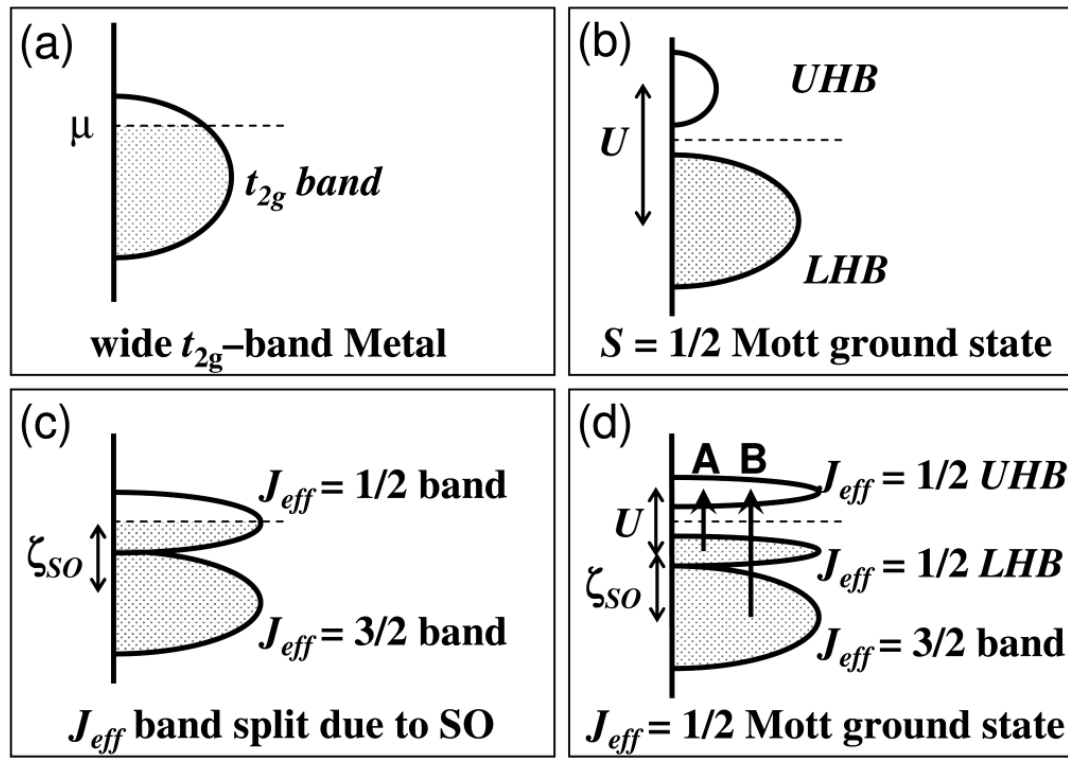
spin-orbit



with lucky atomic number **77**

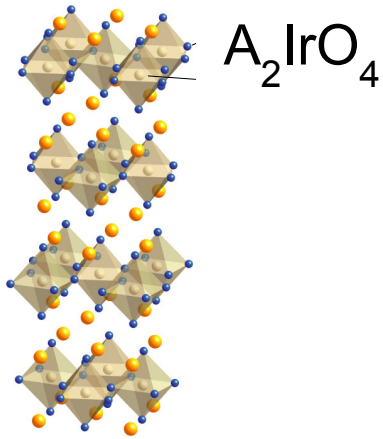
Novel $J_{\text{eff}} = 1/2$ Mott State Induced by Relativistic Spin-Orbit Coupling in Sr_2IrO_4

B. J. Kim,¹ Hosub Jin,¹ S. J. Moon,² J.-Y. Kim,³ B.-G. Park,⁴ C. S. Leem,⁵ Jaejun Yu,¹ T. W. Noh,² C. Kim,⁵ S.-J. Oh,¹
J.-H. Park,^{3,4,*} V. Durairaj,⁶ G. Cao,⁶ and E. Rotenberg⁷

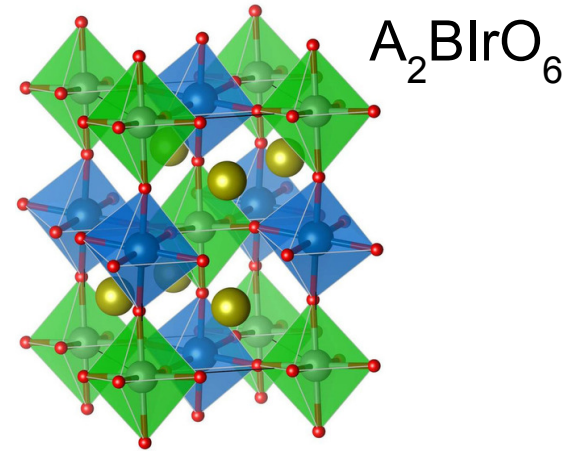
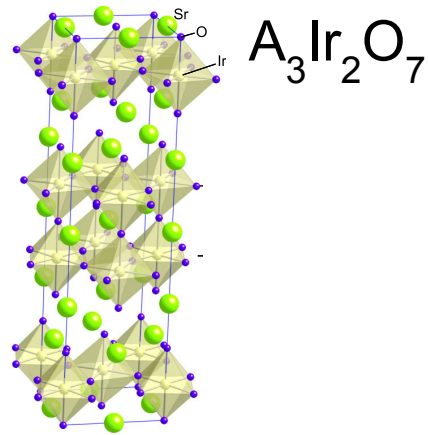


Spin-Orbit assisted Mott transition

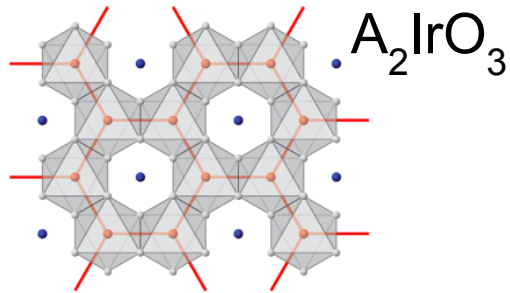
'Zoo' of Iridate compounds



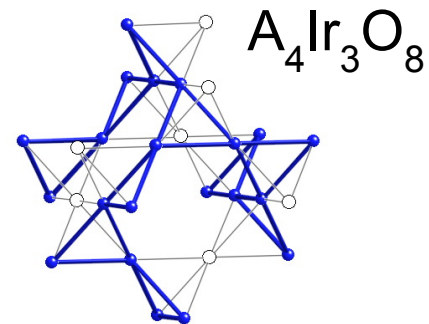
Talk: Ashim K.Pamarik



Talk: Arun Paremekanti

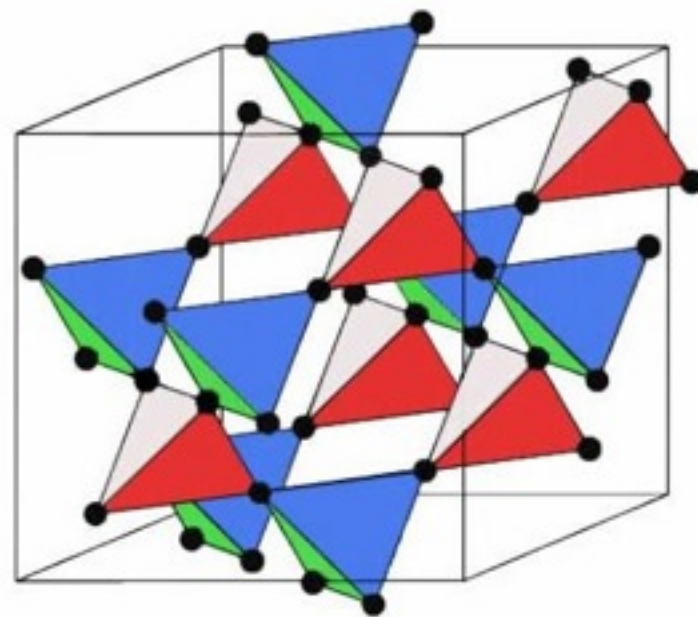
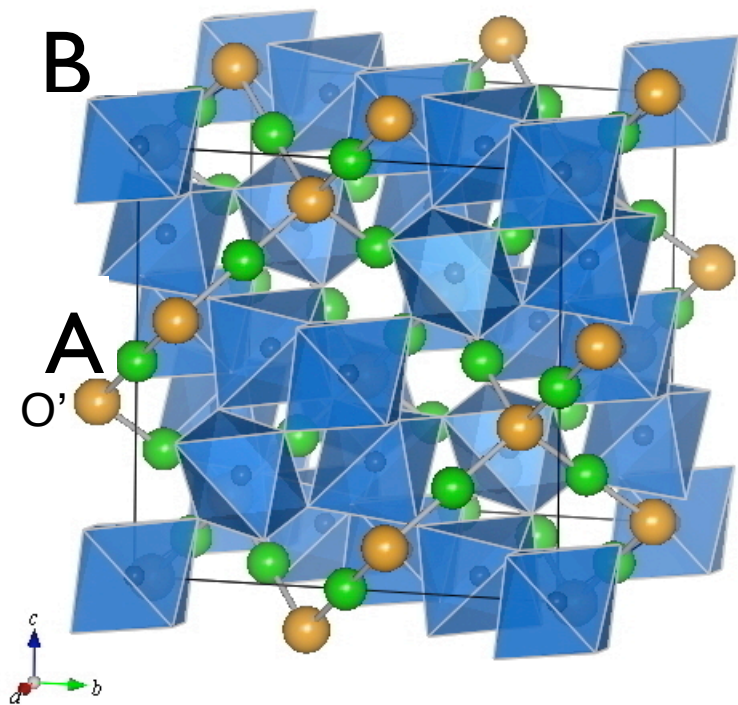


Talks: BJ Kim,
Yogesh Singh



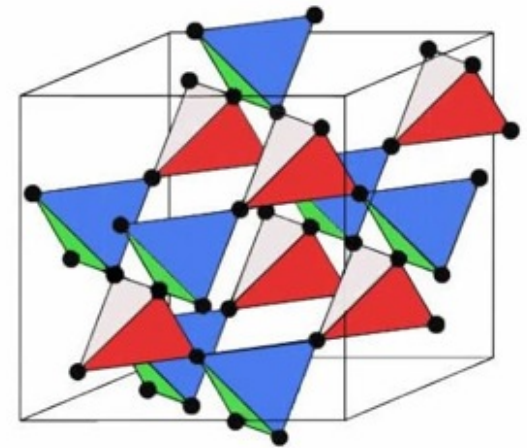
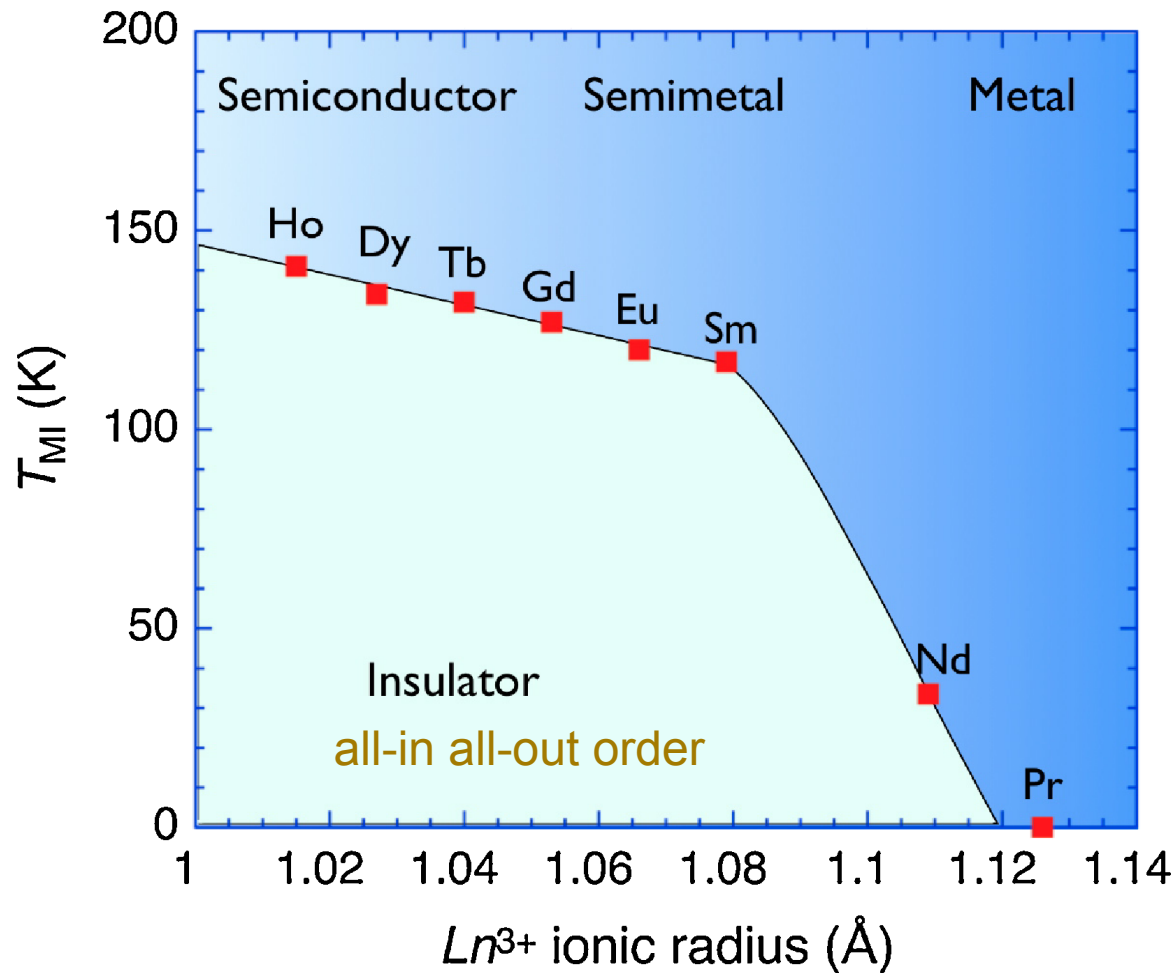
Talks: Philippe Mendels,
Yogesh Singh

Pyrochlore Iridates $\text{Sr}_3\text{Ir}_2\text{O}_7$



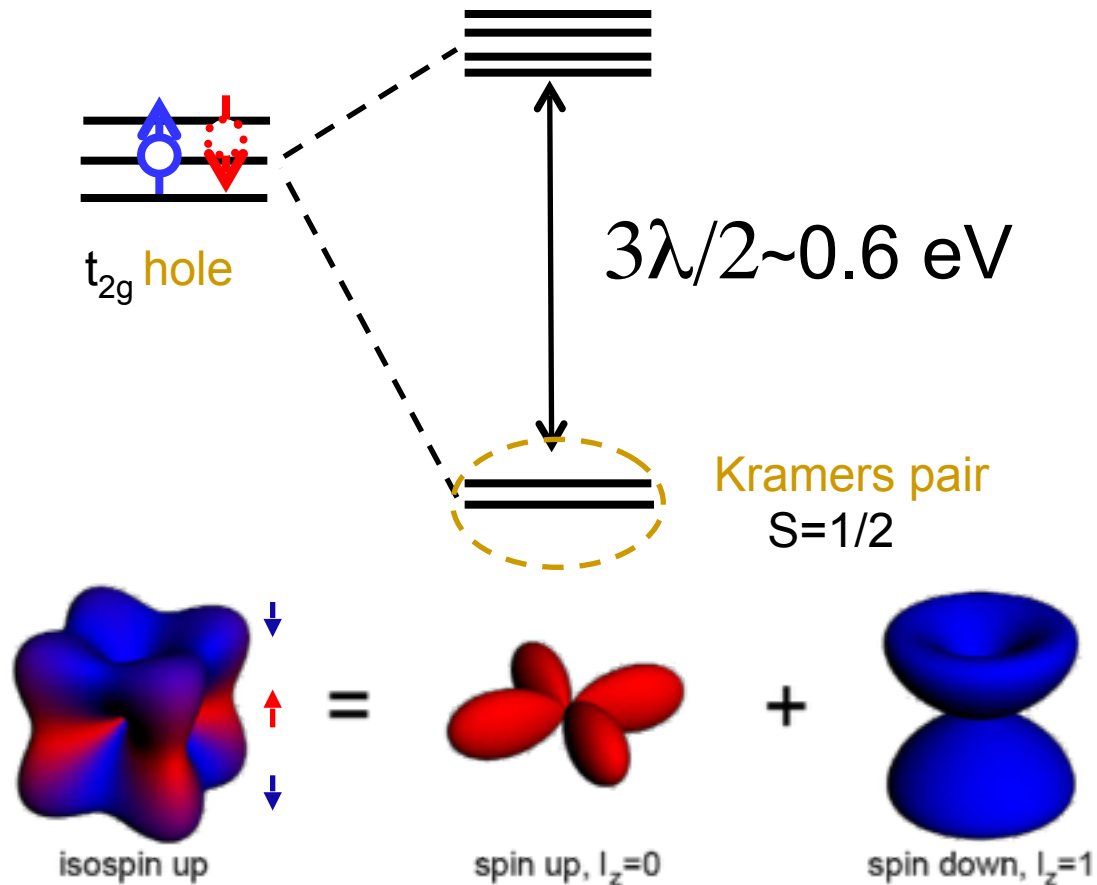
Pyrochlore Iridates $\text{Sr}_3\text{Ir}_2\text{O}_7$

Matsuhira et al, JPSJ (2011)

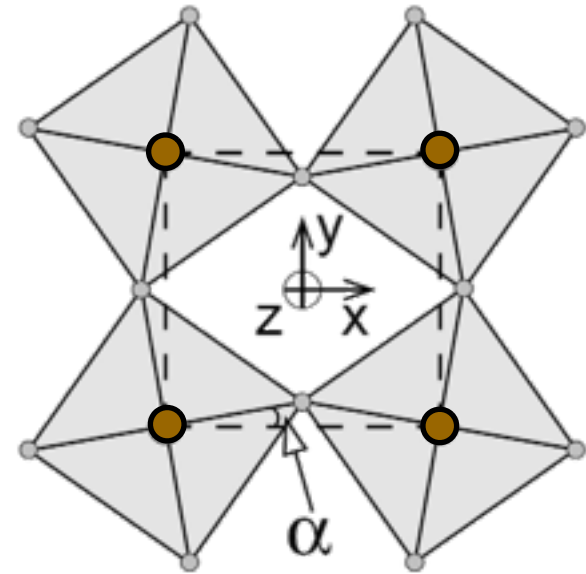
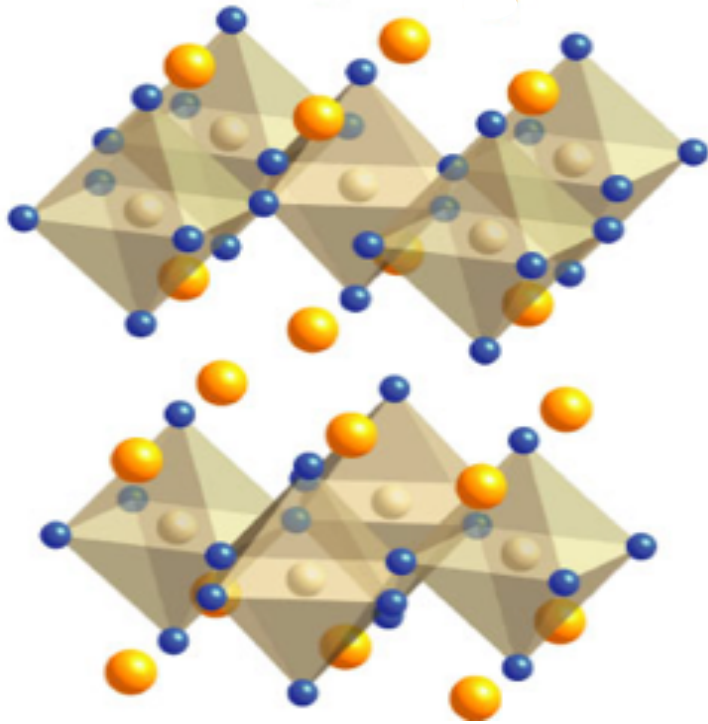


- single layer Sr_2IrO_4 : isotropic, nearly Heisenberg
- double layer $\text{Sr}_3\text{Ir}_2\text{O}_7$: anisotropic, nearly Ising
- hexagonal layered A_2IrO_3 : bond directional Ising
- Magnetically hidden octupolar order in Sr_2VO_4

Low energy Kramers doublet of Ir⁴⁺



Crystal structure of Sr_2IrO_4



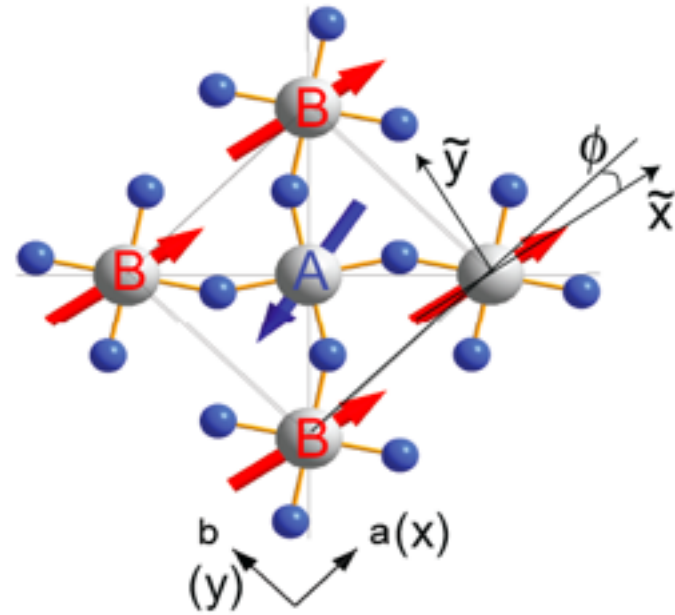
Staggered rotation of octahedra
around c-axis by $\alpha \sim 11^\circ$

Magnetic structure of Sr_2IrO_4

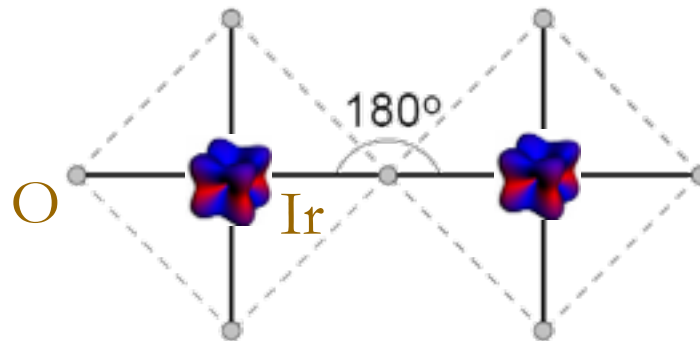
Cao et al., PRB '98

- FM moment $M_{\text{FM}} \sim 0.1 \mu_{\text{B}}$:
too small for a saturated FM

too large for weak a FM
[e.g. in La_2CuO_4 : $0.2 \times 10^{-2} \mu_{\text{B}}$]
- Canted AFM in xy-plane ?
Spin canting angle $\phi \sim \alpha$
Spins rigidly follow rotation of octahedra



Super-exchange between Isospins



$$\mathcal{H}_{ij} = J_1 \vec{S}_i \cdot \vec{S}_j + J_2 (\vec{S}_i \cdot \vec{r}_{ij})(\vec{r}_{ij} \cdot \vec{S}_j)$$

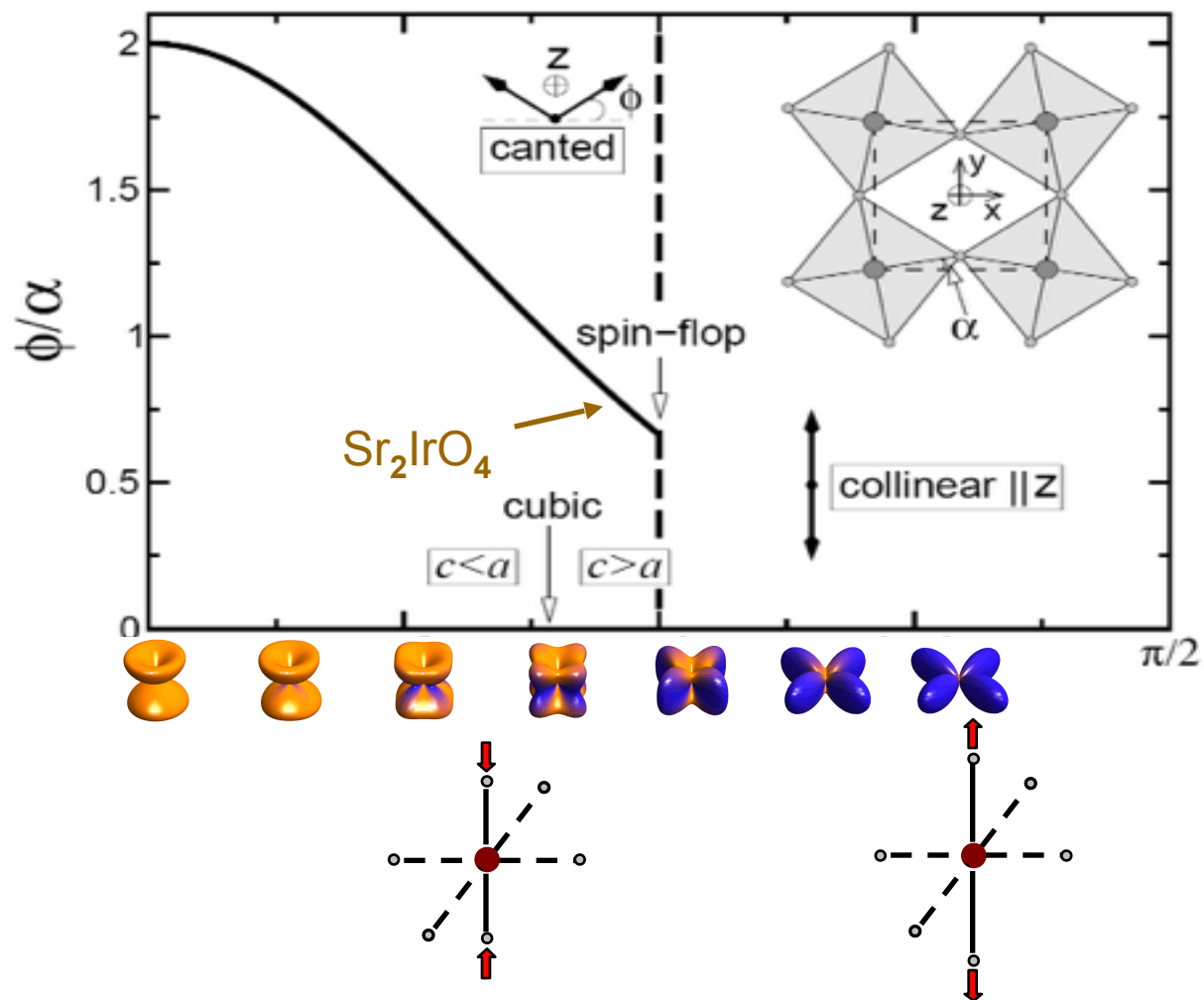
AF-Heisenberg and weaker “dipolar”

+

DM induced by oct. rotations

Magnetism anisotropies are set by distortions

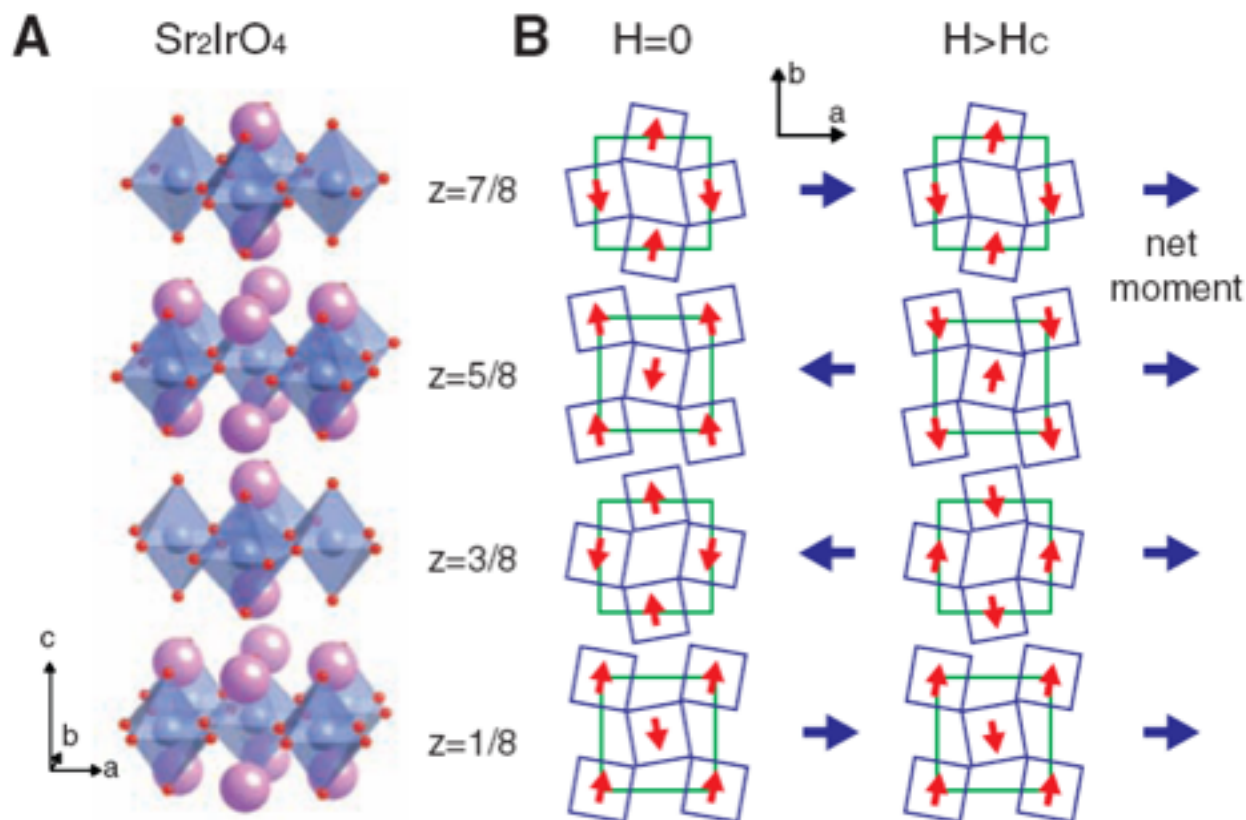
GJ & Khaliullin PRL (2009)



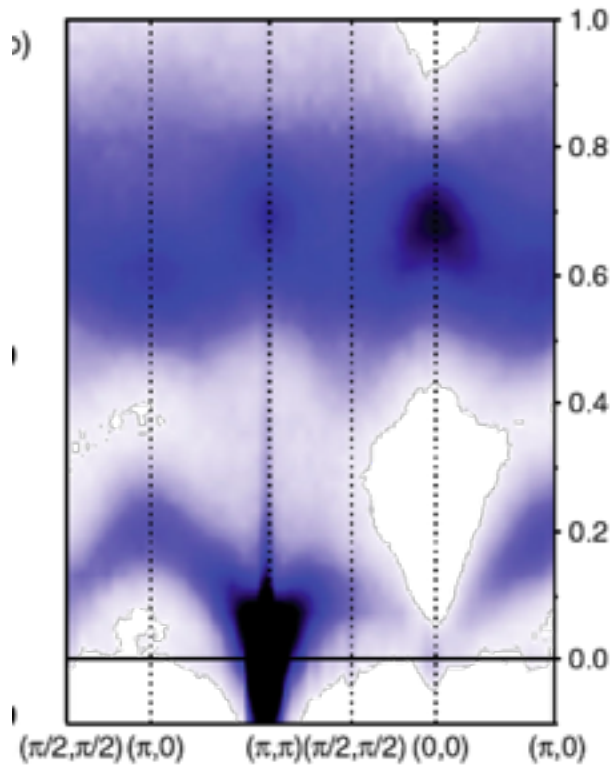
Phase-Sensitive Observation of a Spin-Orbital Mott State in Sr_2IrO_4

B. J. Kim,^{1,2*} H. Ohsumi,³ T. Komesu,³ S. Sakai,^{3,4} T. Morita,^{3,5} H. Takagi,^{1,2*} T. Arima^{3,6}

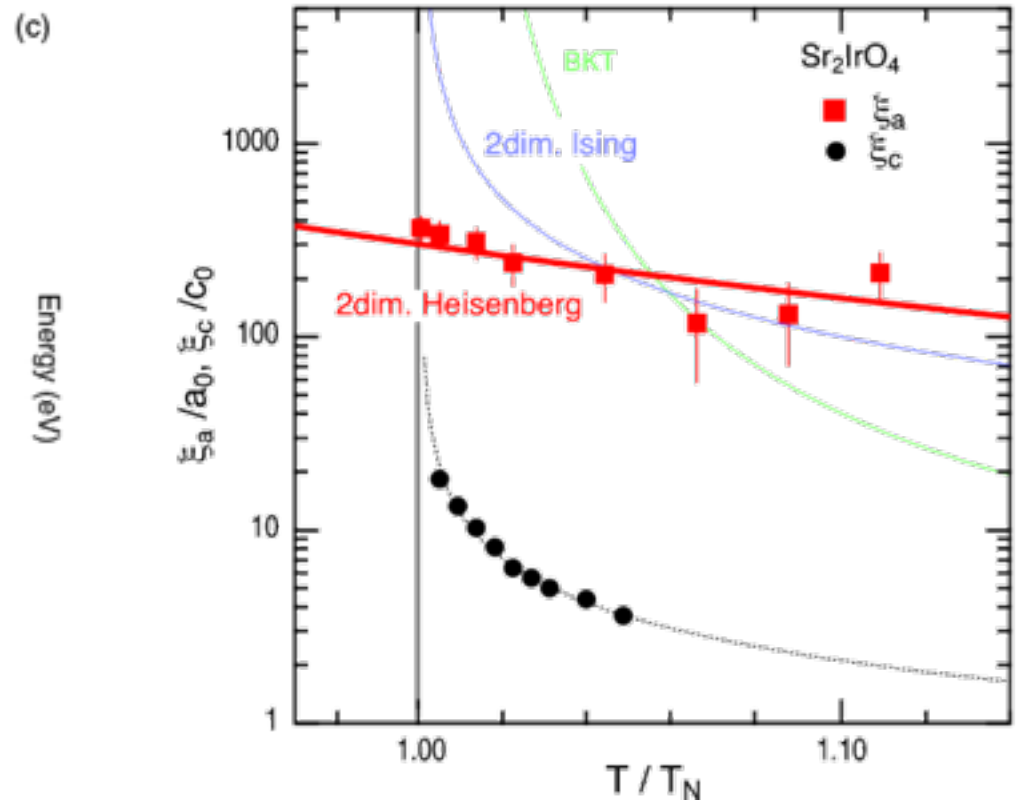
SCIENCE VOL 323 6 MARCH 2009



Heisenberg Magnetism of Sr_2IrO_4

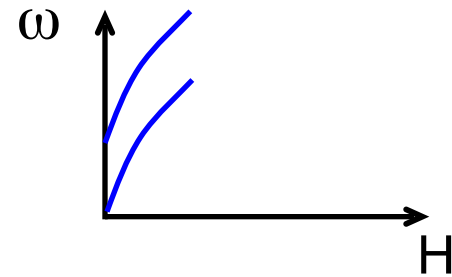
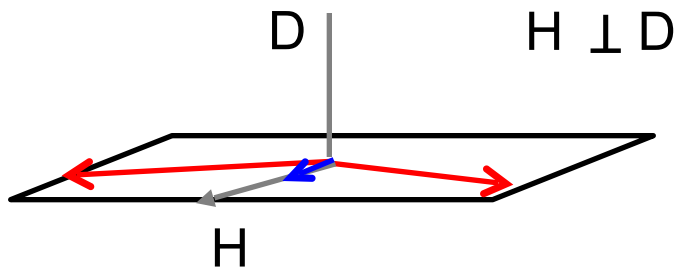
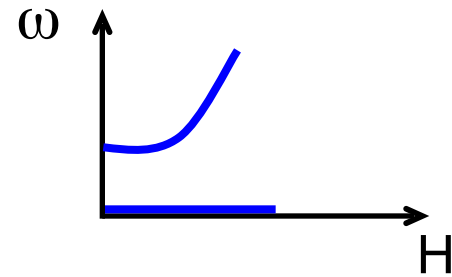
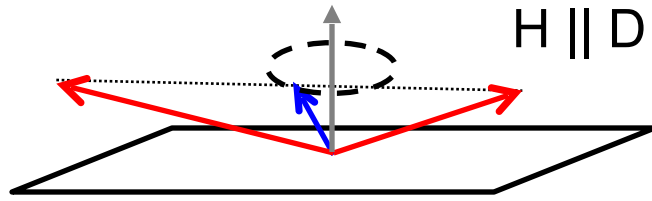


Kim et al, PRL (2012)



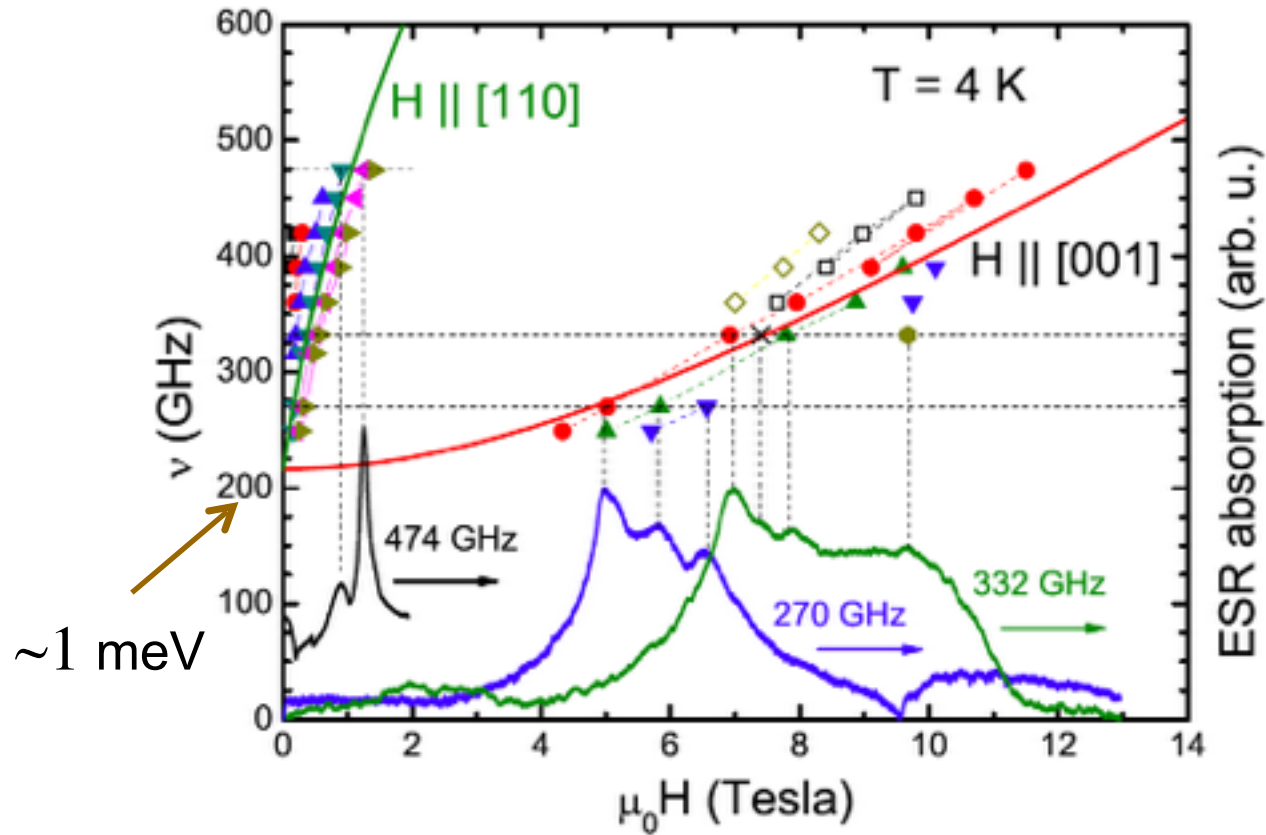
Fujiyama et al, PRL (2012)

Spin-Wave Modes



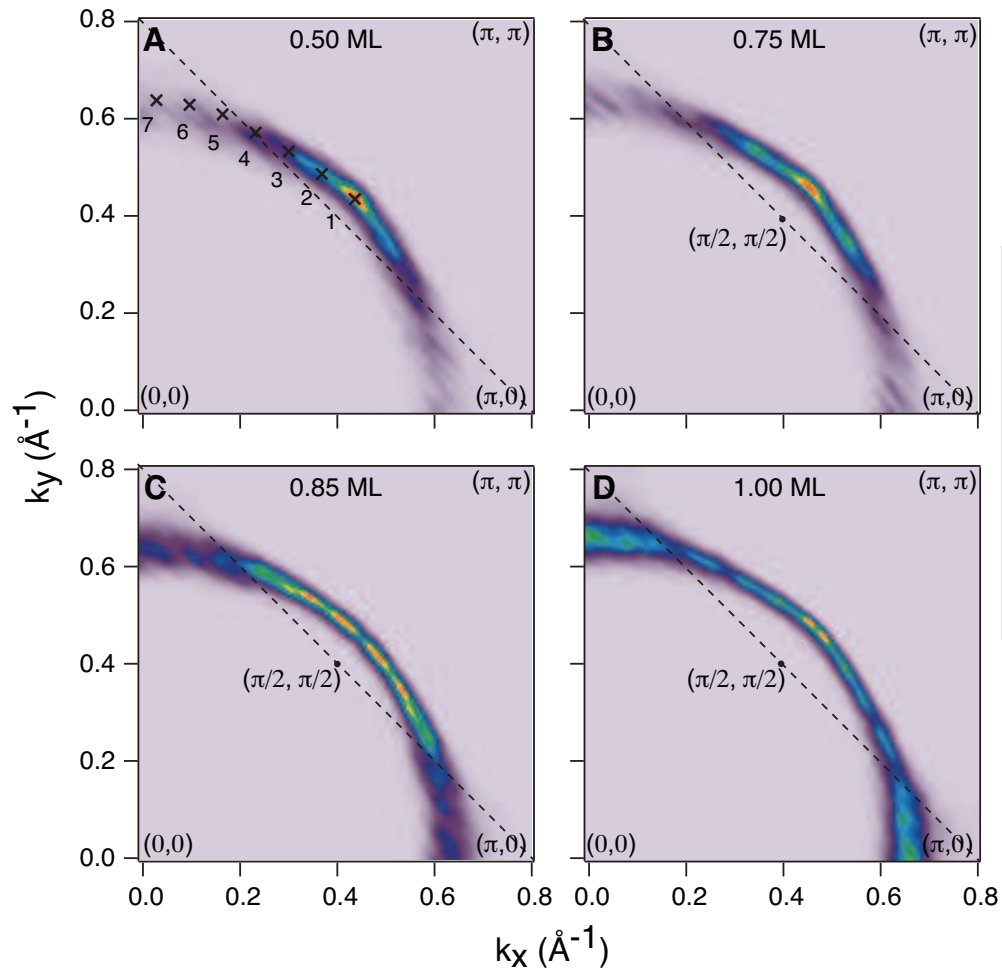
ESR spectra of Sr_2IrO_4

V.Kataev, GJ et al PRB (2014)



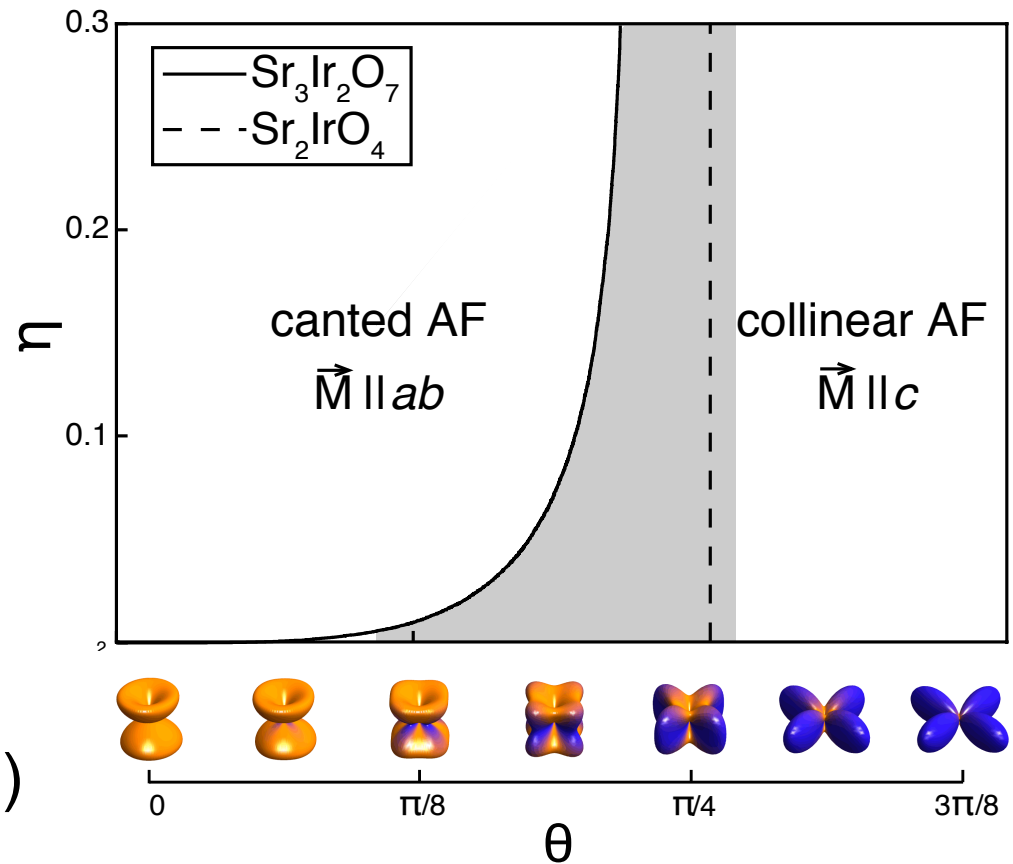
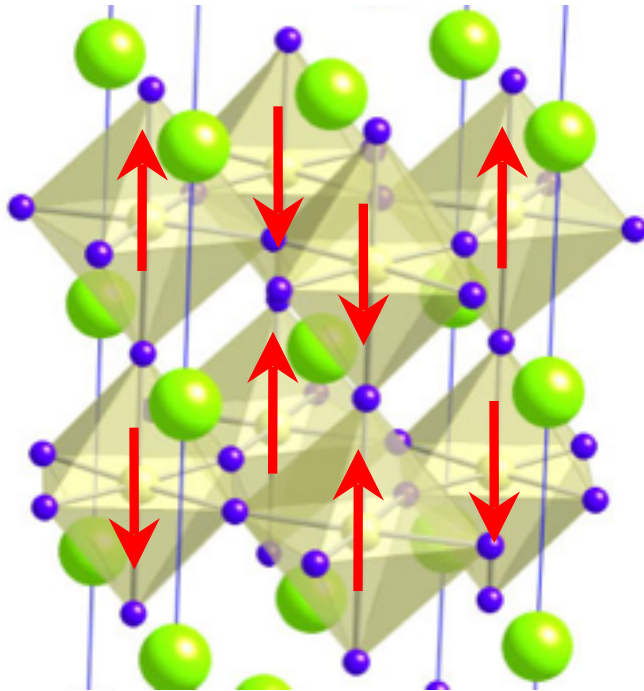
Fermi arcs in doped Sr_2IrO_4

BJ Kim et al Science (2015)



- single layer Sr_2IrO_4 : isotropic, nearly Heisenberg
- double layer $\text{Sr}_3\text{Ir}_2\text{O}_7$: anisotropic, nearly Ising
- hexagonal layered A_2IrO_3 : bond directional Ising

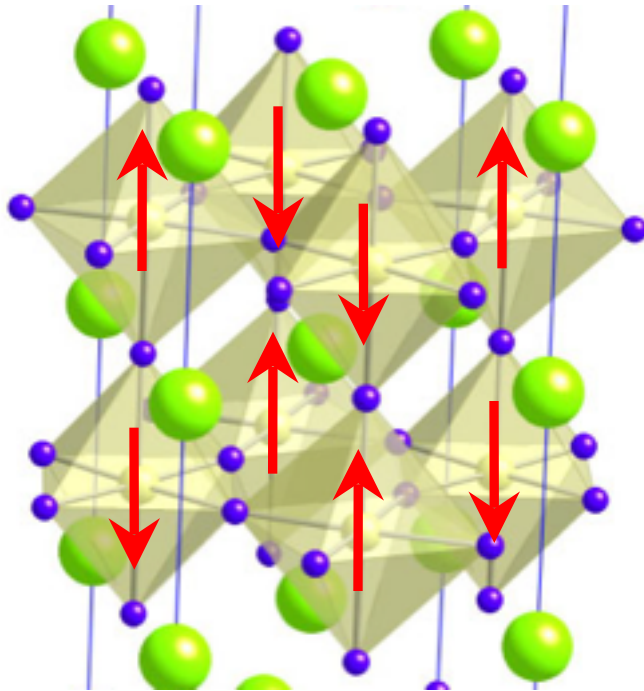
Magnetism of $\text{Sr}_3\text{Ir}_2\text{O}_7$



- c -axis AF (contrary to 214)

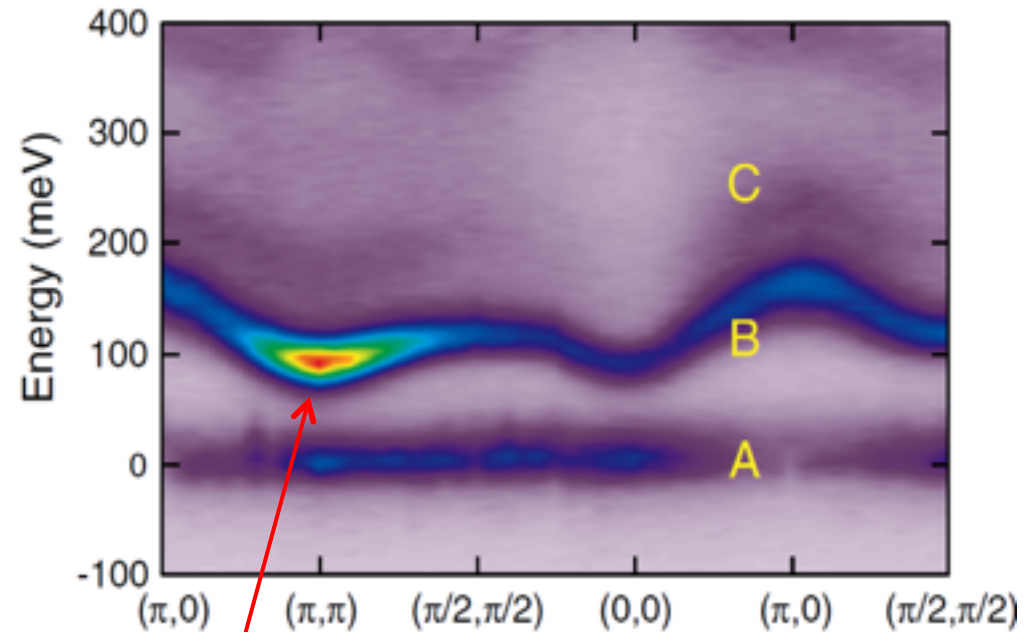
BJ Kim, GJ, et al, PRL (2012)

Magnetism of $\text{Sr}_3\text{Ir}_2\text{O}_7$



- c-axis AF (contrary to 214)

RIXS data

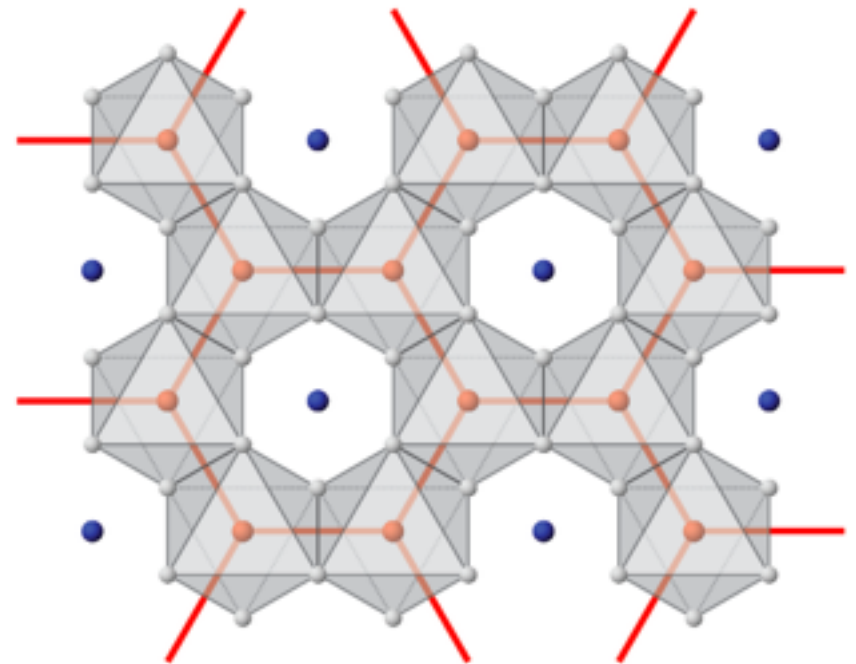
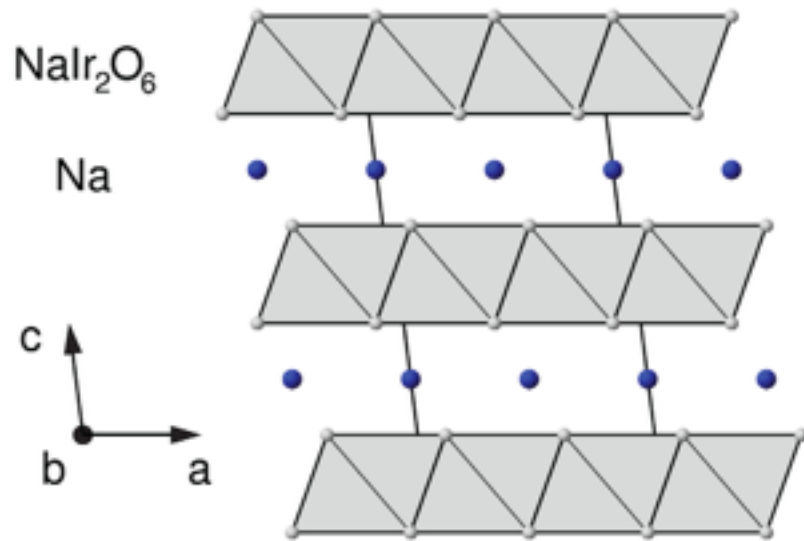


- Large magnon gap, Ising like spin dynamics

BJ Kim, GJ, et al, PRL (2012)

- single layer Sr_2IrO_4 : isotropic, nearly Heisenberg
- double layer $\text{Sr}_3\text{Ir}_2\text{O}_7$: anisotropic, nearly Ising
- hexagonal layered A_2IrO_3 : bond directional Ising

Hexagonal Iridates $A_2\text{IrO}_3$ ($A=\text{Na}, \text{Li}$)



Hexagonal Iridates $A_2\text{IrO}_3$ ($A=\text{Na}, \text{Li}$)

Two theory proposals based

GJ & G.Khaliullin, PRL'09

from Mott side:

as a candidate for a Quantum Spin Liquid

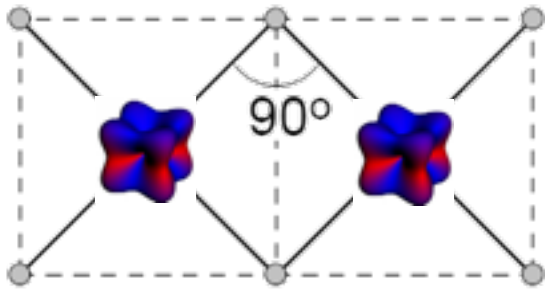
A.Shitade, H. Katsura, J. Kunes, XL Qi, SC Zhang, N.Nagaosa, PRL'09

from itinerant side:

as a candidate for a Topological Insulator and QSH effect

Superexchange Hamiltonian: 90°-bonds

GJ & G.Khaliullin PRL (2009)

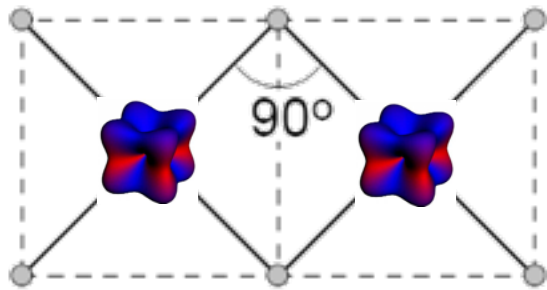


$$\mathcal{H}_{ij}^{(\gamma)} = JS_i^\gamma S_j^\gamma$$

Ising, γ -axis out of plane

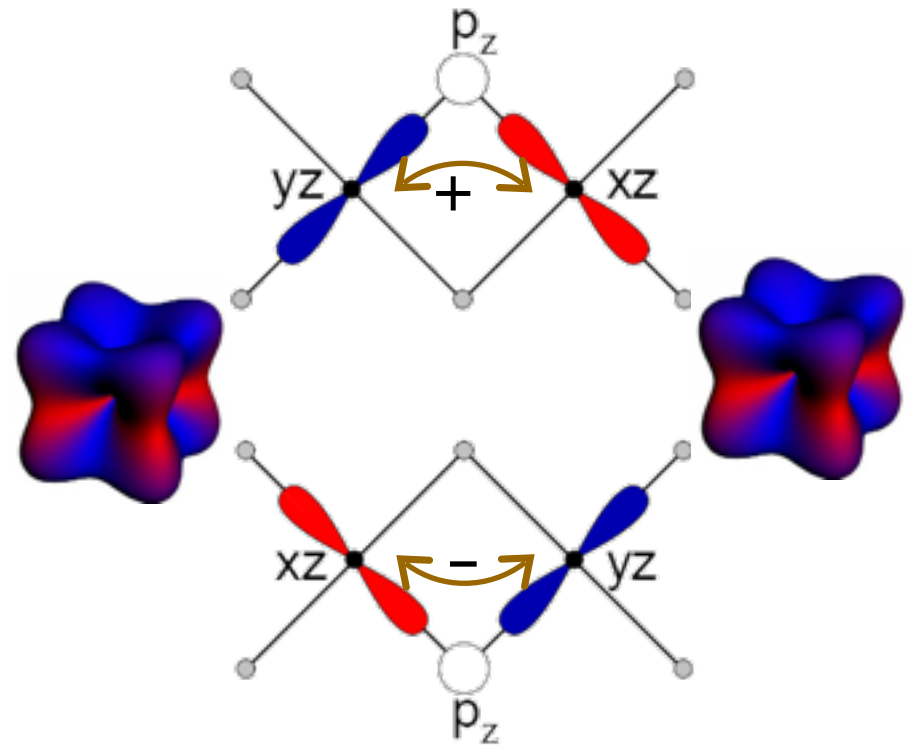
Superexchange Hamiltonian: 90°-bonds

GJ & G.Khaliullin PRL (2009)



$$\mathcal{H}_{ij}^{(\gamma)} = JS_i^\gamma S_j^\gamma$$

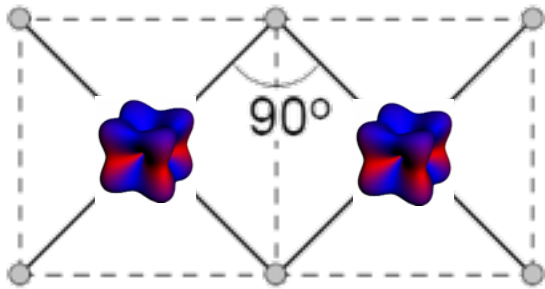
Ising, γ -axis out of plane



Destructive quantum interference
between two channels
Heisenberg term is suppressed

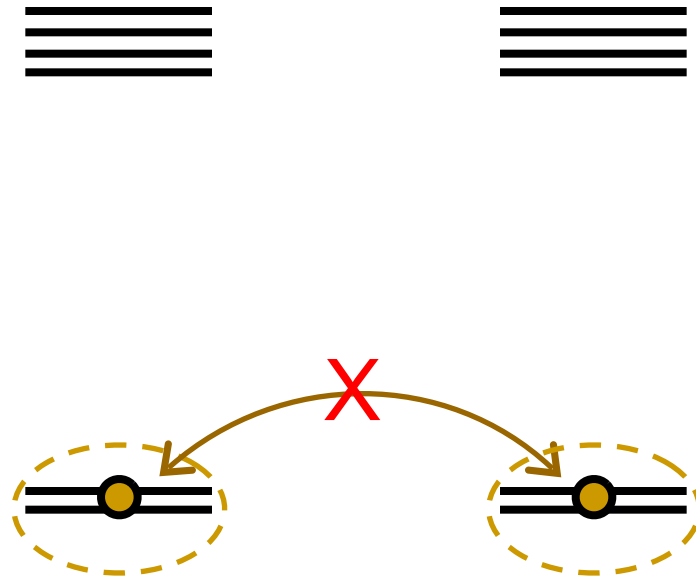
Superexchange Hamiltonian: 90°-bonds

GJ & G.Khaliullin PRL (2009)



$$\mathcal{H}_{ij}^{(\gamma)} = JS_i^\gamma S_j^\gamma$$

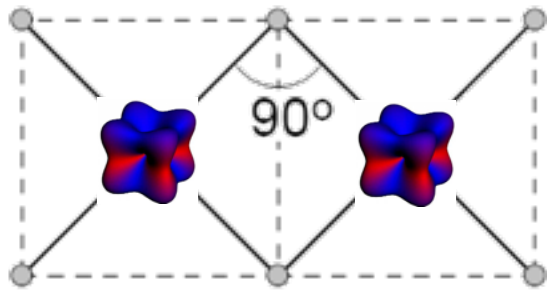
Ising, γ -axis out of plane



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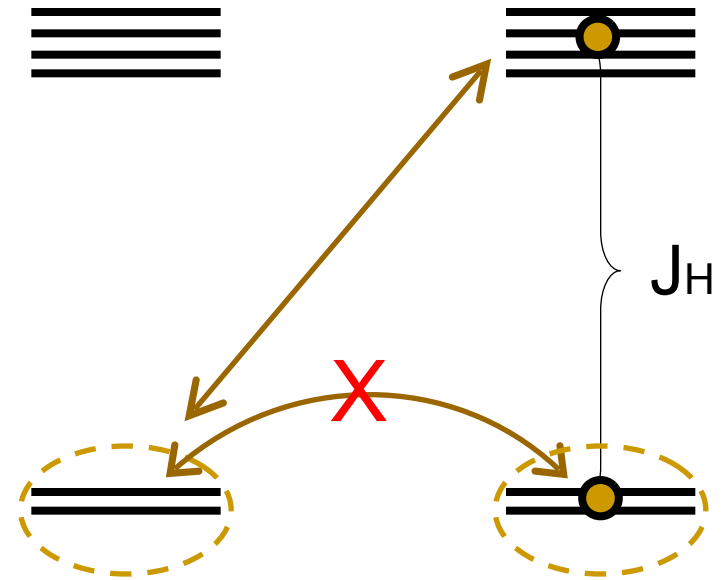
Superexchange Hamiltonian: 90°-bonds

GJ & G.Khaliullin PRL (2009)



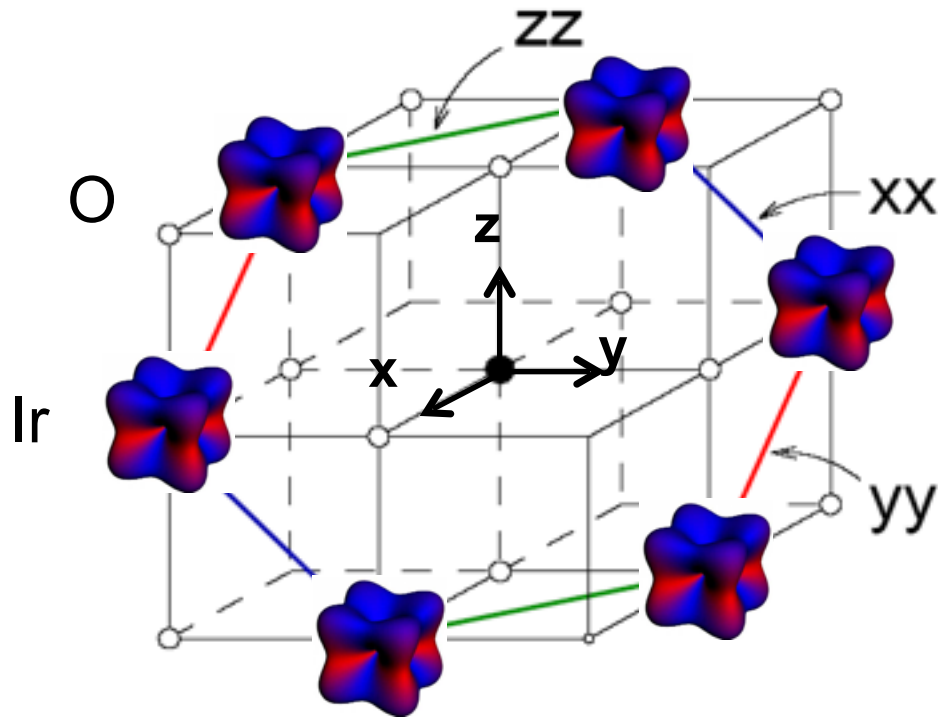
$$\mathcal{H}_{ij}^{(\gamma)} = JS_i^\gamma S_j^\gamma$$

Ising, γ -axis out of plane



Destructive quantum interference
between two channels
Heisenberg term is suppressed

Isospins on a Honeycomb layer of $A_2\text{IrO}_3$



$$\mathcal{H}_{ij}^{(\gamma)} = J S_i^\gamma S_j^\gamma$$

Kitaev Model

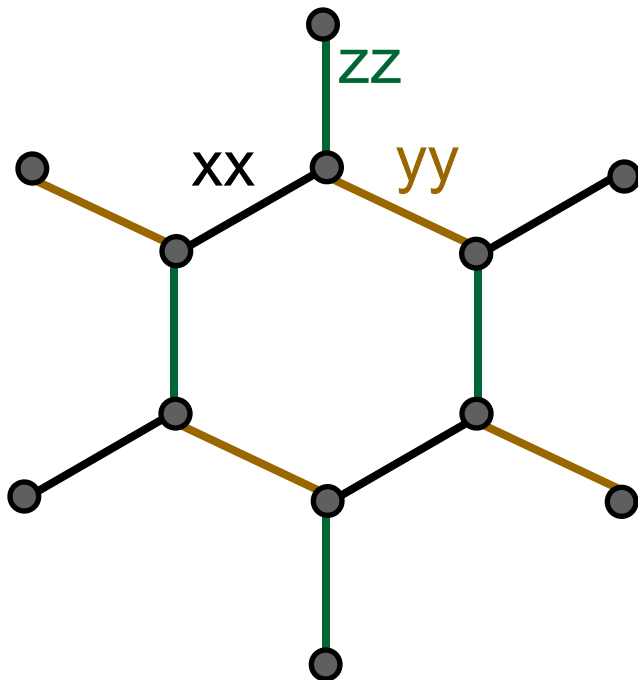
A.Kitaev, Ann. Phys'06

Kitaev Honeycomb Model

A. Kitaev, Ann. Phys'06

$$\mathcal{H}_{ij}^{(\gamma)} = JS_i^\gamma S_j^\gamma$$

- exactly soluble 2D quantum model



Kitaev Honeycomb Model

A. Kitaev, Ann. Phys'06

$$\mathcal{H}_{ij}^{(\gamma)} = JS_i^\gamma S_j^\gamma$$

- ❑ exactly soluble 2D quantum model
- ❑ spin liquid ground-state



Kitaev Honeycomb Model

A. Kitaev, Ann. Phys'06

$$\mathcal{H}_{ij}^{(\gamma)} = JS_i^\gamma S_j^\gamma$$

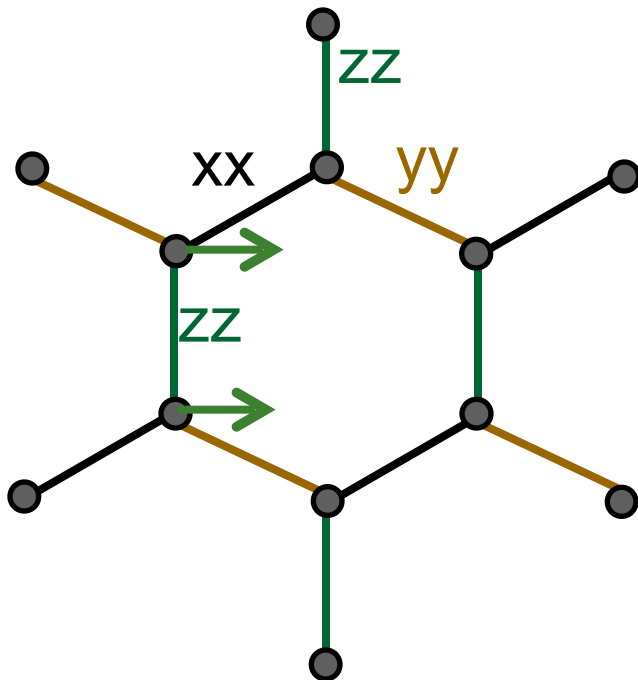


- exactly soluble 2D quantum model
- spin liquid ground-state
- Fractional excitations:
Majorana Fermions, Dirac spectrum
- only NN two-spin correlations
(Baskaran et al PRL'07)
- Exact dynamic spin structure factor
(Knolle et al PRL'14)

Kitaev Honeycomb Model

A. Kitaev, Ann. Phys'06

$$\mathcal{H}_{ij}^{(\gamma)} = JS_i^\gamma S_j^\gamma$$

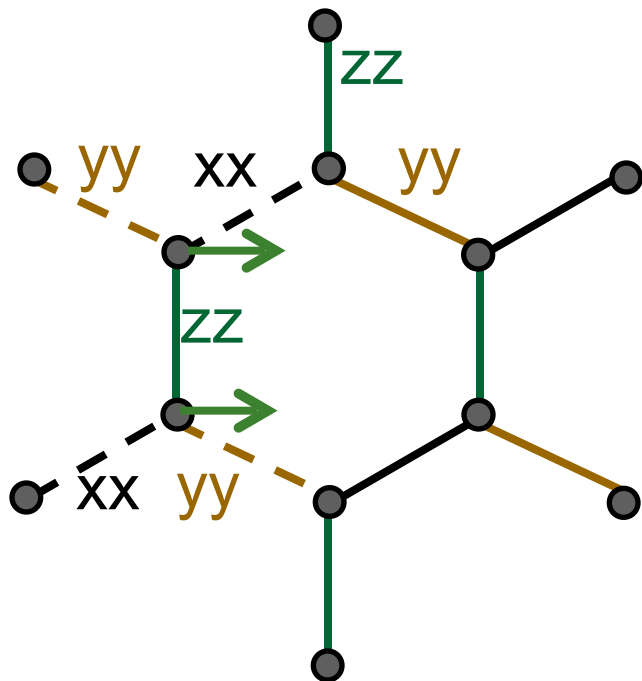


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A. Kitaev, Ann. Phys'06

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Majorana Fermions, Dirac spectrum
- only NN two-spin correlations
(Baskaran et al PRL'07)
- Exact dynamic spin structure factor
(Knolle et al PRL'14)

Experimental Findings

Susceptibility & Thermodynamics:

Singh and Gegenwart, PRB'10; Singh et al PRL'12

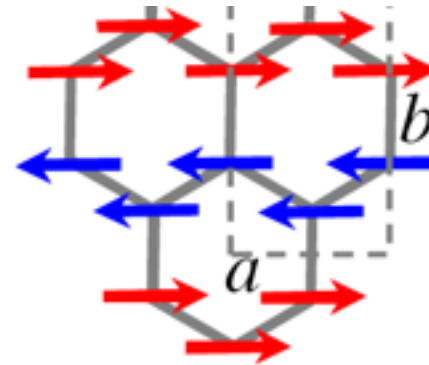
Ordering ~ 15K in both Na_2IrO_3 ($\theta = -125\text{K}$) & Li_2IrO_3 ($\theta = -33\text{K}$)

Zig-Zag order in Na_2IrO_3

XRS : Liu et al, PRB'11

INS: Choi, Coldea et al, PRL'12

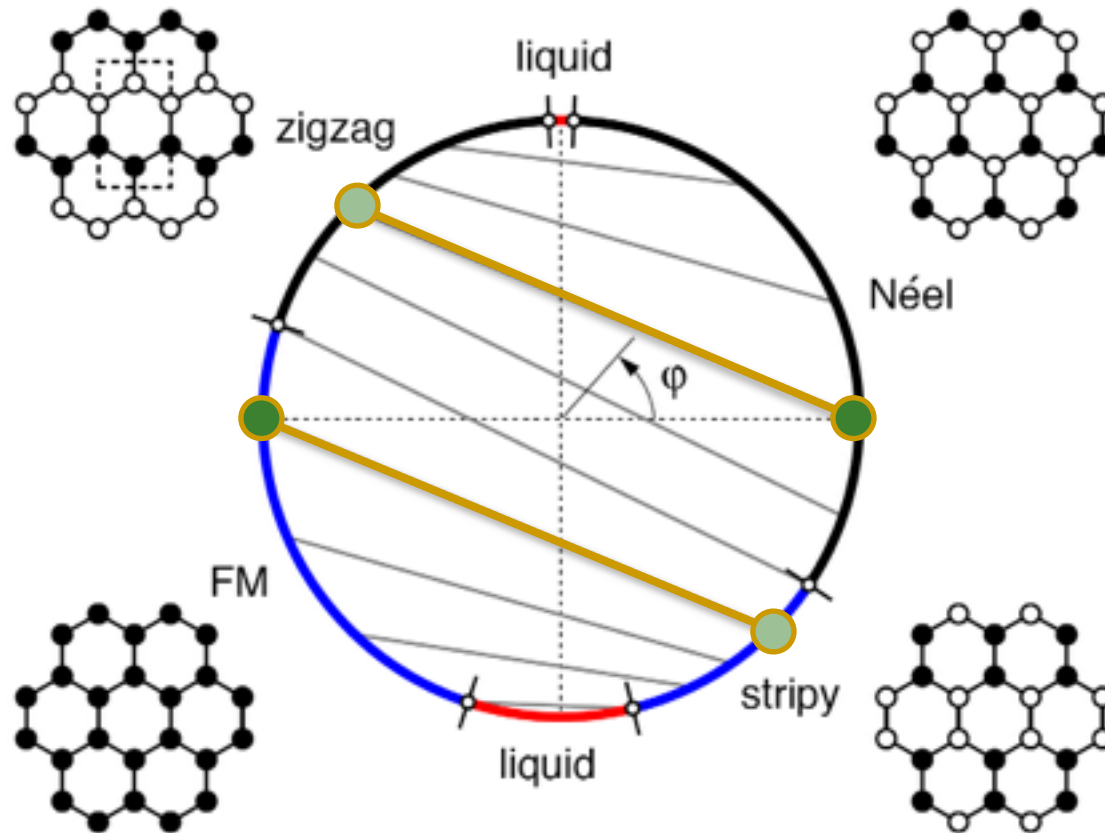
N&XR Diffraction: Ye et al PRB'12



Phase Diagram of Kitaev-Heisenberg Model

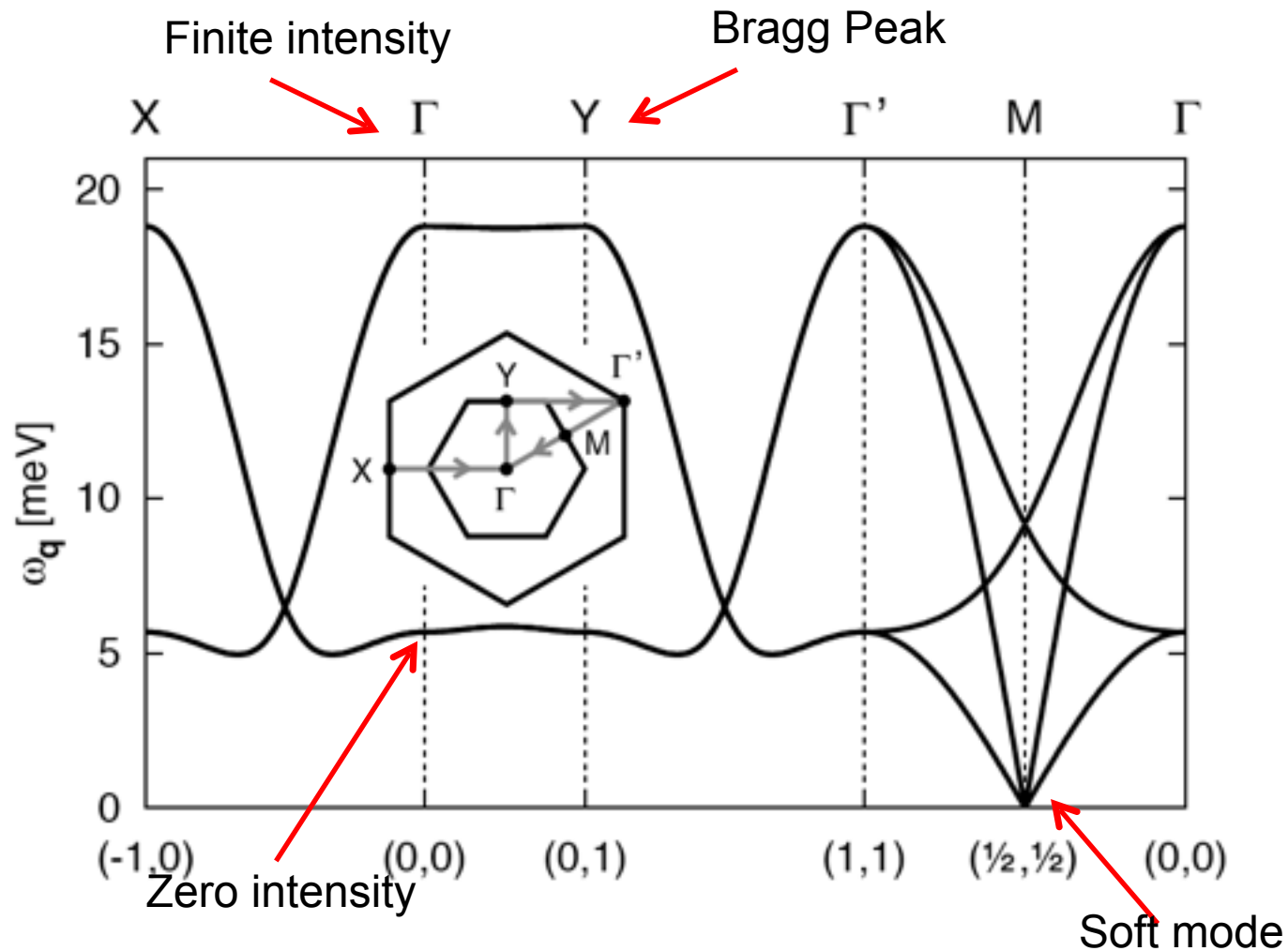
$$\mathcal{H}_{ij}^{(\gamma)} = 2K S_i^\gamma S_j^\gamma + J \mathbf{S}_i \cdot \mathbf{S}_j$$

$$K = A \sin \varphi \quad J = A \cos \varphi$$



J.Chaloupka, GJ & G.Khaliullin PRL (2013)

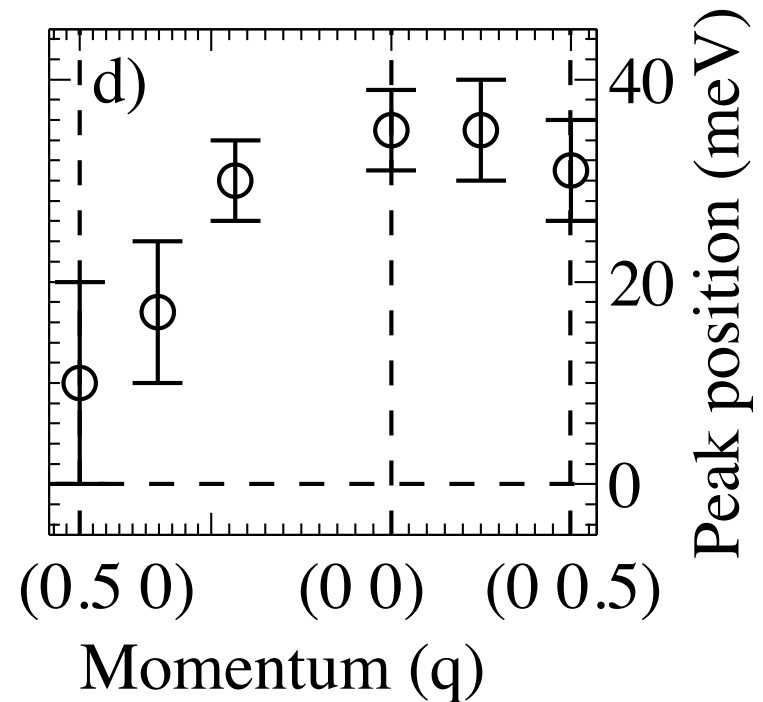
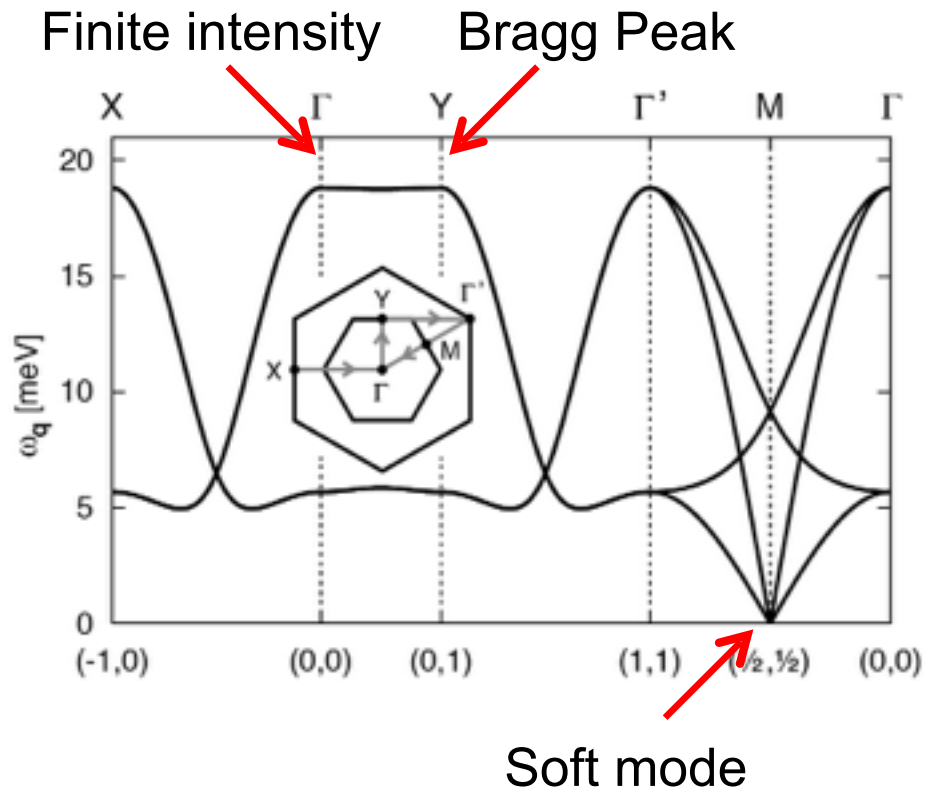
Spin-wave dispersions of Zigzag phase



Spin-wave dispersions of Zigzag phase

Chaloupka, GJ & Khaliullin PRL 2013

Gretarsson et al, PRB 2013



further neighbor exchange also stabilise zigzag

PHYSICAL REVIEW B **84**, 180407(R) (2011)

Kitaev-Heisenberg- J_2 - J_3 model for the iridates $A_2\text{IrO}_3$

Itamar Kimchi¹ and Yi-Zhuang You^{1,2}

PRL **108**, 127204 (2012)

PHYSICAL REVIEW LETTERS

week ending
23 MARCH 2012

Spin Waves and Revised Crystal Structure of Honeycomb Iridate Na_2IrO_3

S. K. Choi,¹ R. Coldea,¹ A. N. Kolmogorov,² T. Lancaster,^{1,*} I. I. Mazin,³ S. J. Blundell,¹ P. G. Radaelli,¹ Yogesh Singh,^{4,5}
P. Gegenwart,⁴ K. R. Choi,⁶ S.-W. Cheong,^{6,7} P. J. Baker,⁸ C. Stock,⁸ and J. Taylor⁸

PRL **108**, 127203 (2012)

PHYSICAL REVIEW LETTERS

week ending
23 MARCH 2012

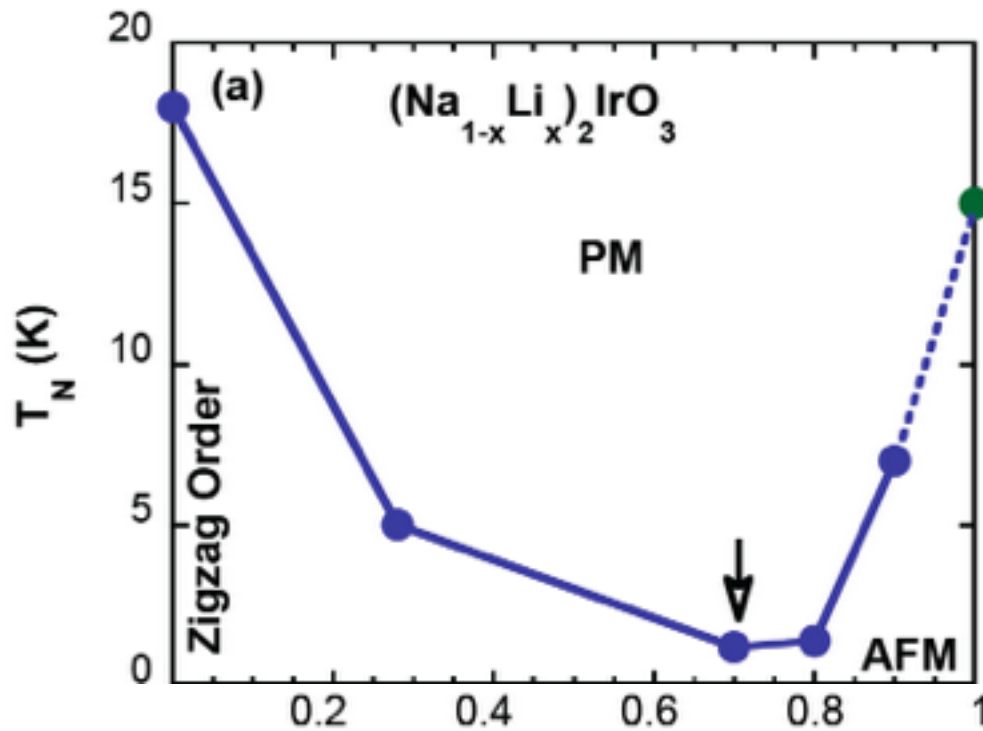
Relevance of the Heisenberg-Kitaev Model for the Honeycomb Lattice Iridates $A_2\text{IrO}_3$

Yogesh Singh,^{1,2} S. Manni,² J. Reuther,^{3,4} T. Berlijn,^{5,6} R. Thomale,⁷ W. Ku,^{5,6} S. Trebst,⁸ and P. Gegenwart²

PHYSICAL REVIEW B **88**, 220414(R) (2013)

Evolution of magnetism in the single-crystal honeycomb iridates $(\text{Na}_{1-x}\text{Li}_x)_2\text{IrO}_3$

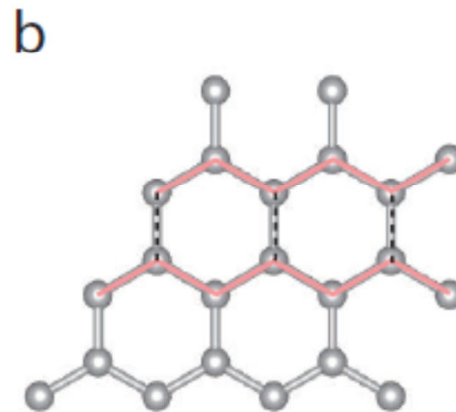
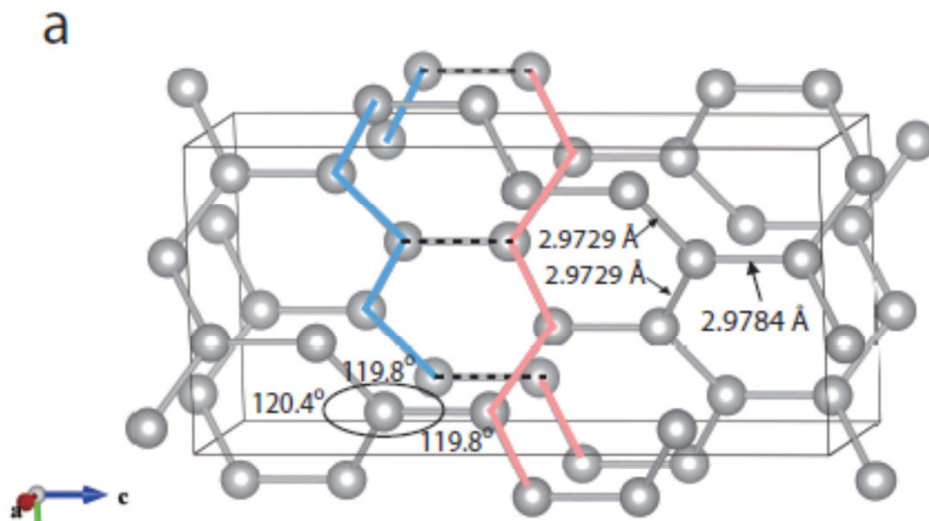
G. Cao,¹ T. F. Qi,¹ L. Li,¹ J. Terzic,¹ V. S. Cao,^{1,2} S. J. Yuan,^{1,3} M. Tovar,¹ G. Murthy,¹ and R. K. Kaul¹



Spiral Order (Coldea et al)

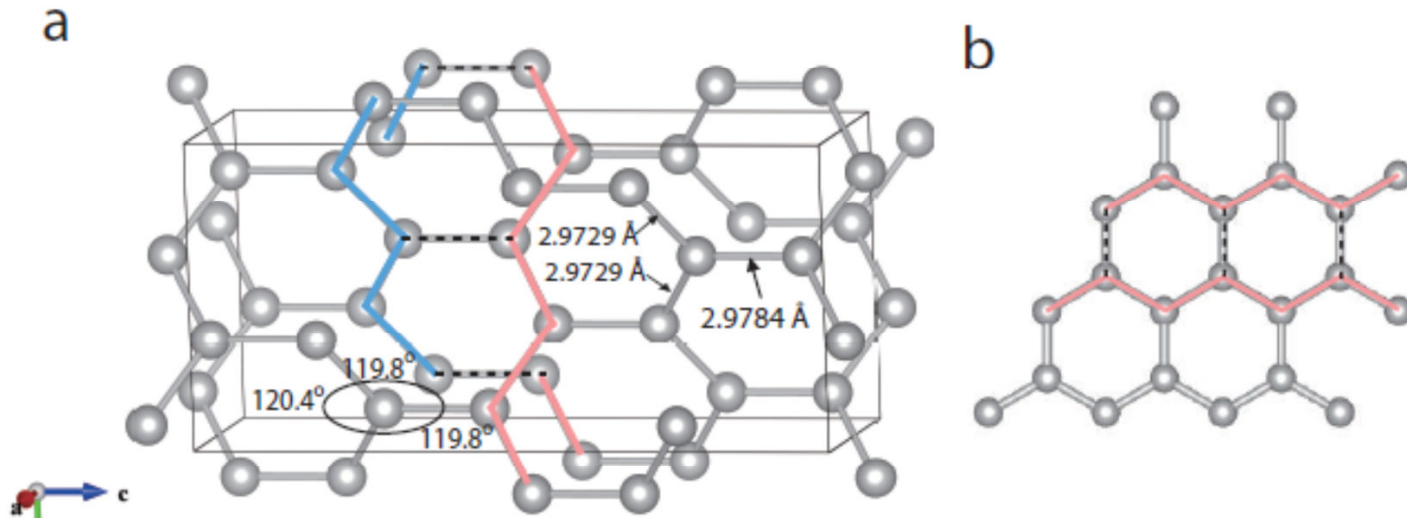
Hyper-Honeycomb $\beta\text{-Li}_2\text{IrO}_3$

T. Takayama et al, PRL'15

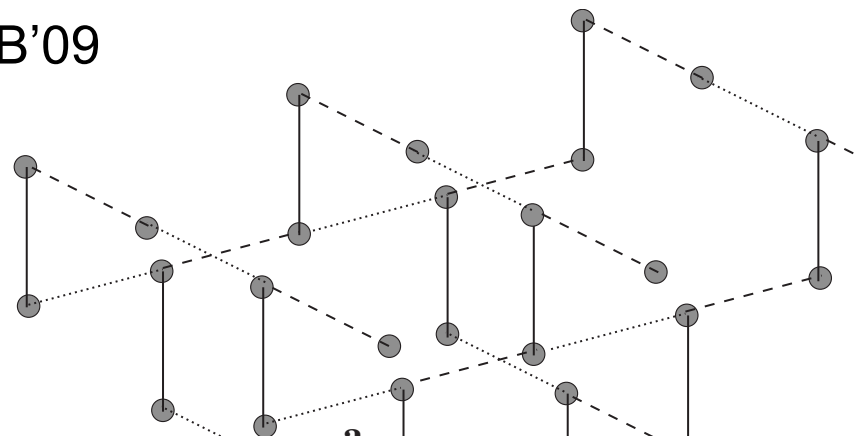


Hyper-Honeycomb $\beta\text{-Li}_2\text{IrO}_3$

T. Takayama et al, PRL'15

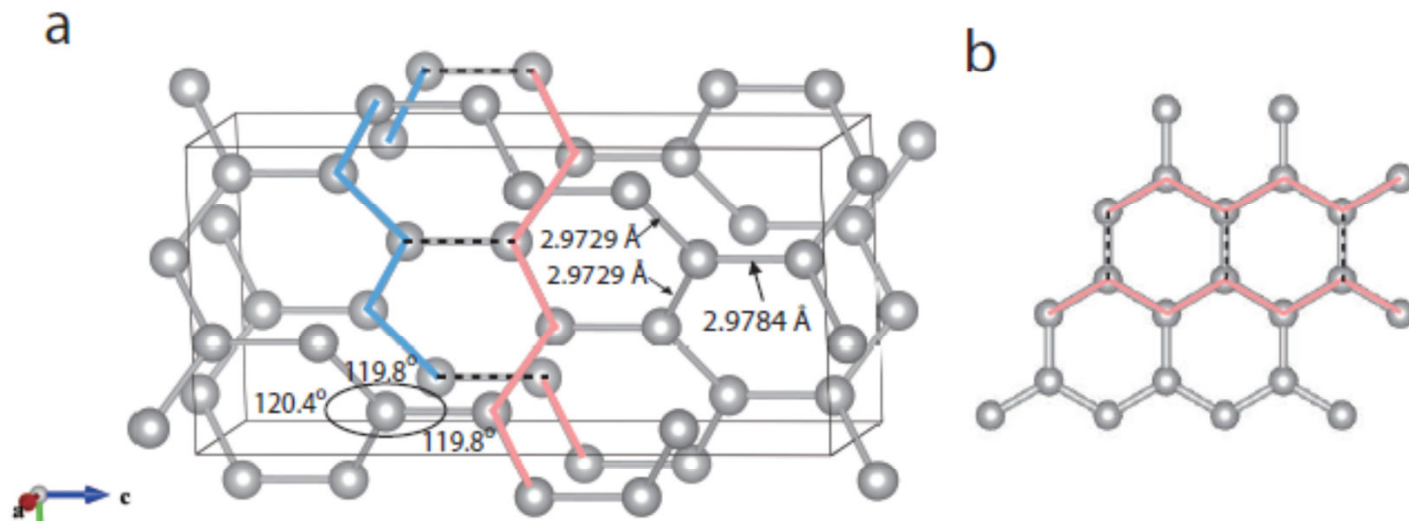


S.Mandal and N.Surendran, PRB'09

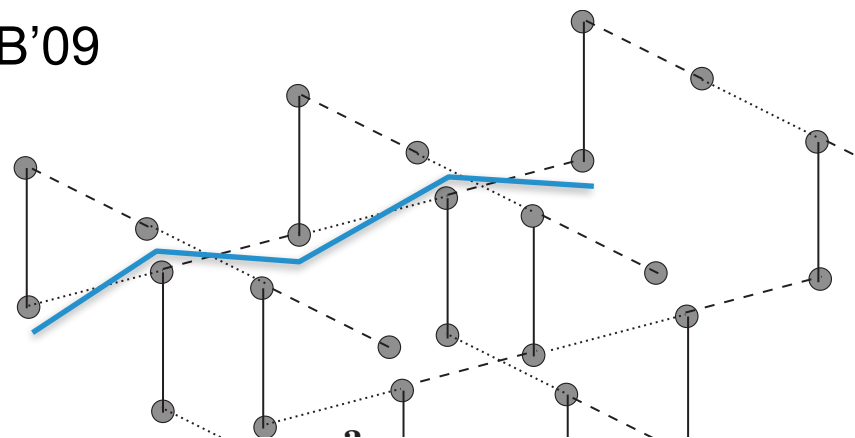


Hyper-Honeycomb $\beta\text{-Li}_2\text{IrO}_3$

T. Takayama et al, PRL'15

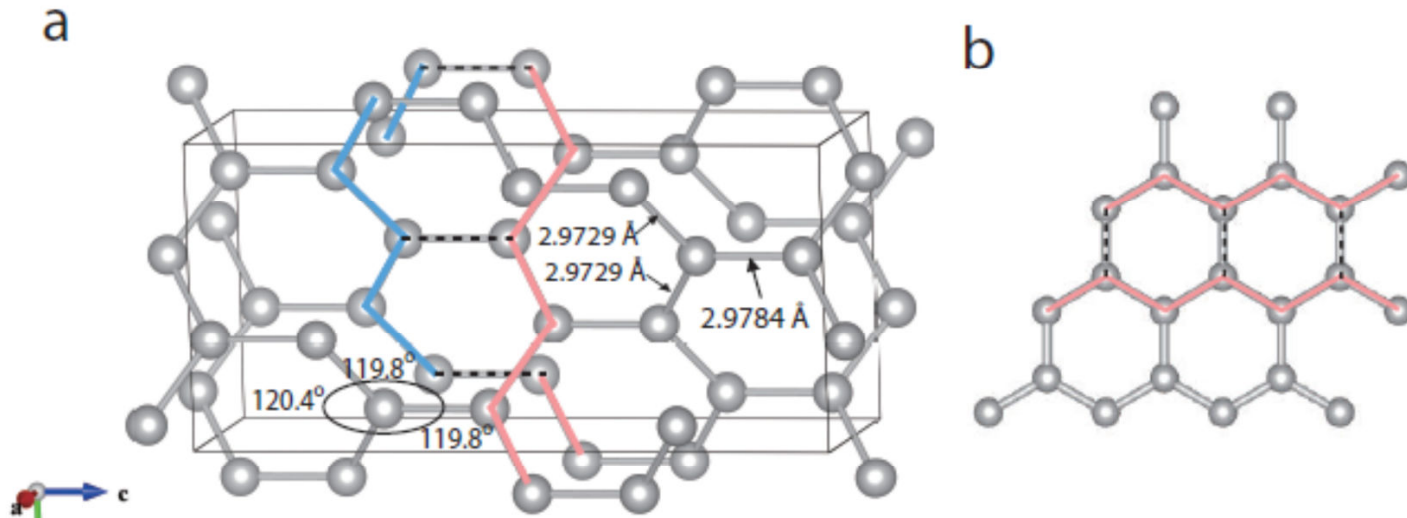


S.Mandal and N.Surendran, PRB'09

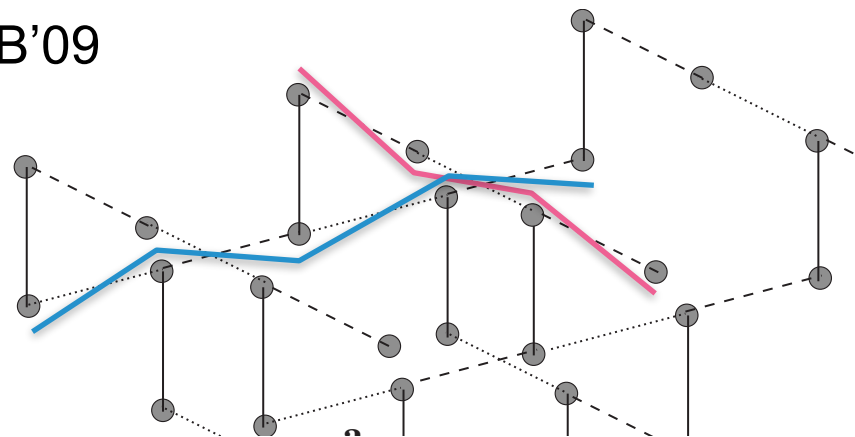


Hyper-Honeycomb $\beta\text{-Li}_2\text{IrO}_3$

T. Takayama et al, PRL'15



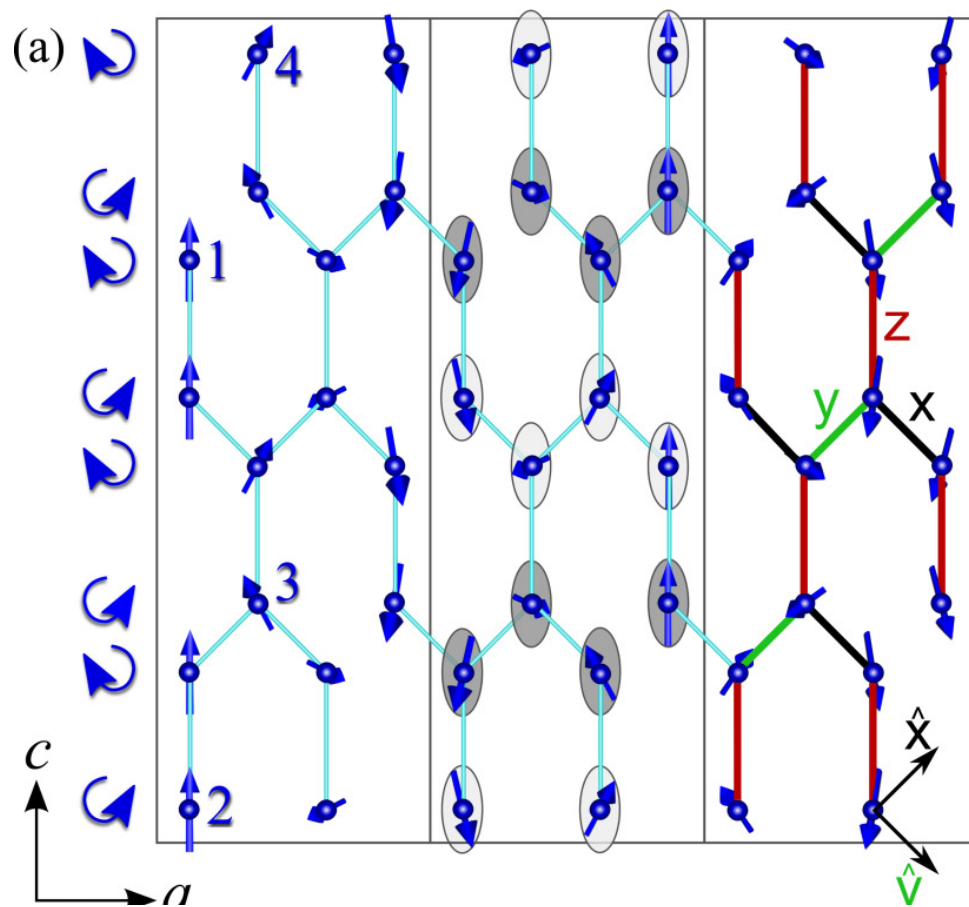
S.Mandal and N.Surendran, PRB'09





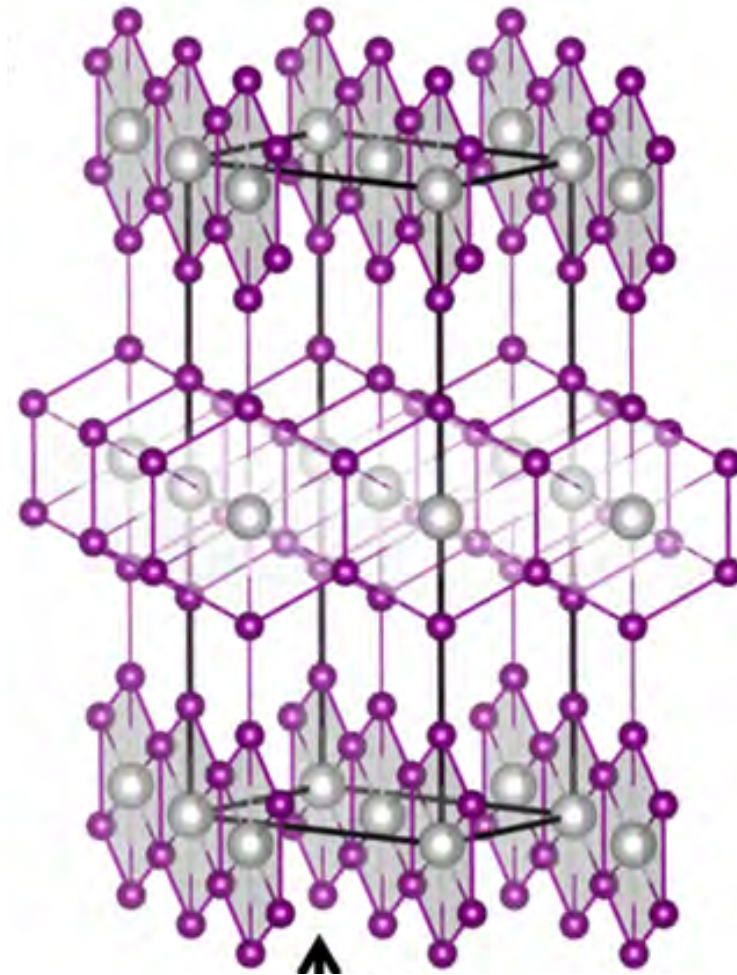
Unconventional magnetic order on the hyperhoneycomb Kitaev lattice in β -Li₂IrO₃: Full solution via magnetic resonant x-ray diffraction

A. Biffin,¹ R. D. Johnson,¹ Sungkyun Choi,¹ F. Freund,² S. Manni,² A. Bombardi,³ P. Manuel,⁴ P. Gegenwart,² and R. Coldea¹



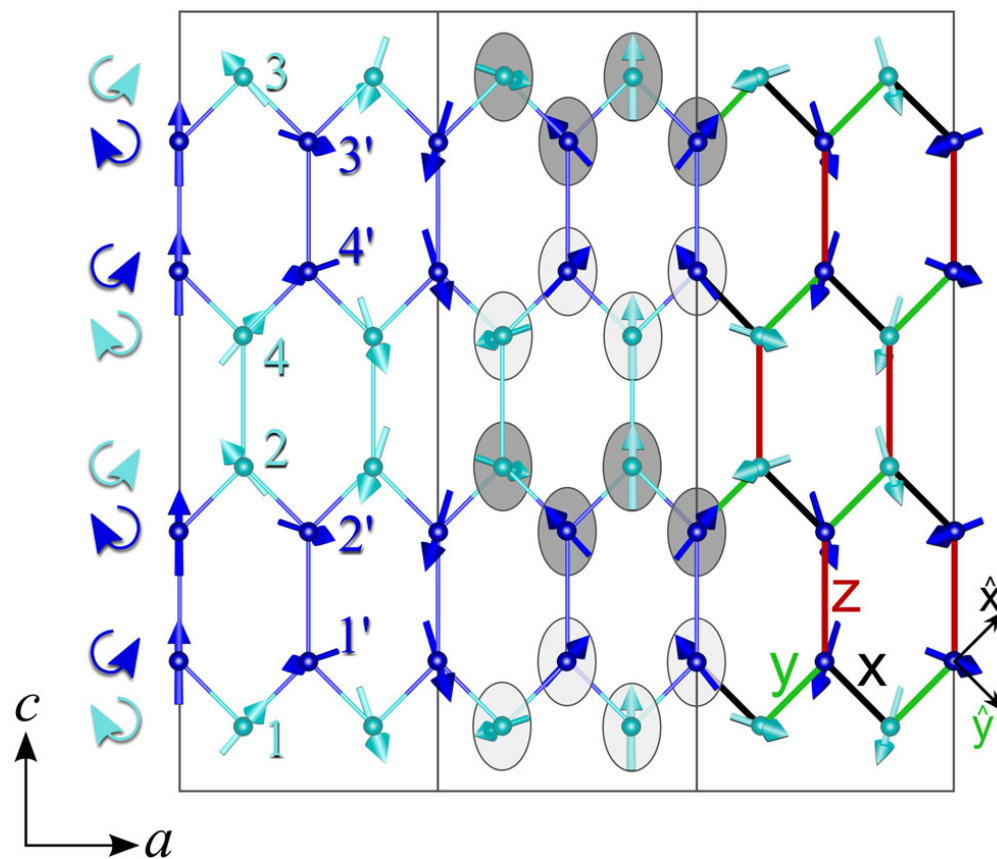
Harmonic-Honeycomb γ -Li₂IrO₃

Modic et al, Nature Comm.'15



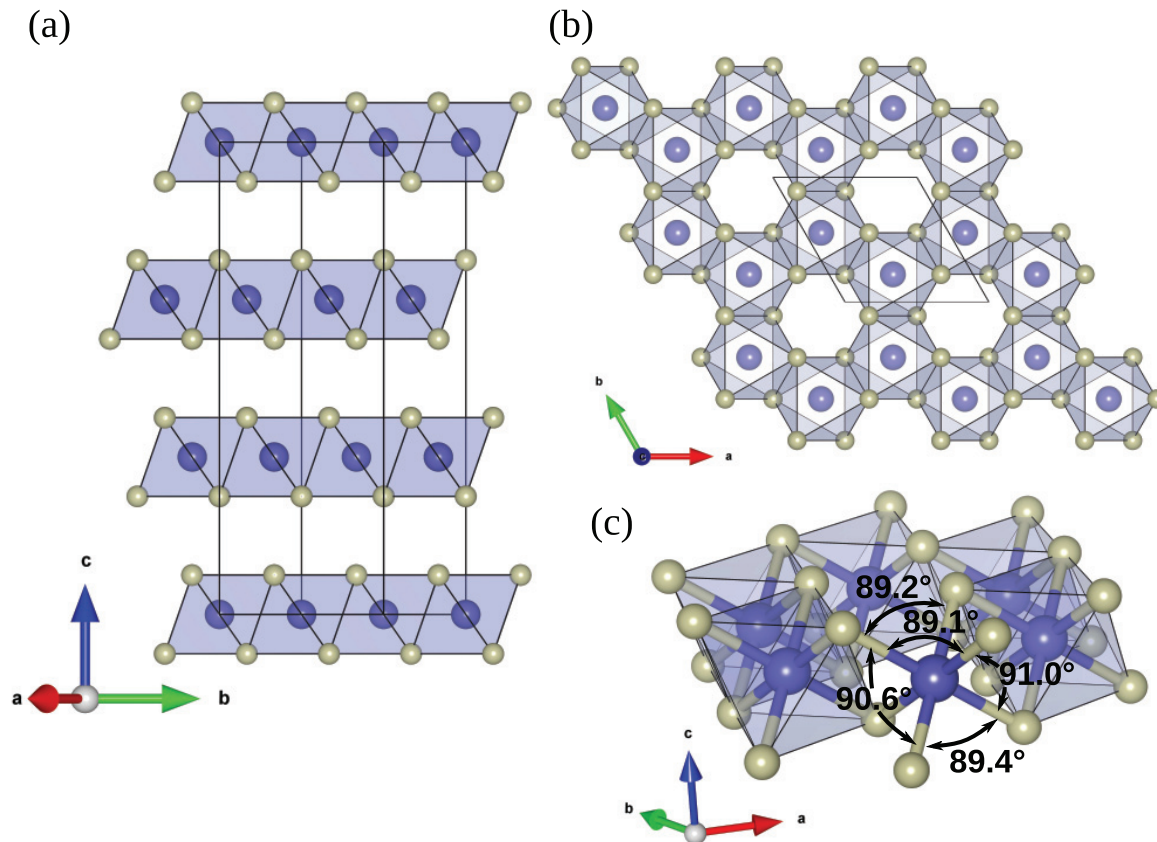
Noncoplanar and Counterrotating Incommensurate Magnetic Order Stabilized by Kitaev Interactions in γ -Li₂IrO₃

A. Biffin,¹ R. D. Johnson,¹ I. Kimchi,² R. Morris,¹ A. Bombardi,³ J. G. Analytis,^{2,4} A. Vishwanath,^{2,4} and R. Coldea¹



α -RuCl₃: A spin-orbit assisted Mott insulator on a honeycomb lattice

K. W. Plumb,¹ J. P. Clancy,¹ L. J. Sandilands,¹ V. Vijay Shankar,¹ Y. F. Hu,² K. S. Burch,^{1,3}
 Hae-Young Kee,^{1,4} and Young-June Kim^{1,*}



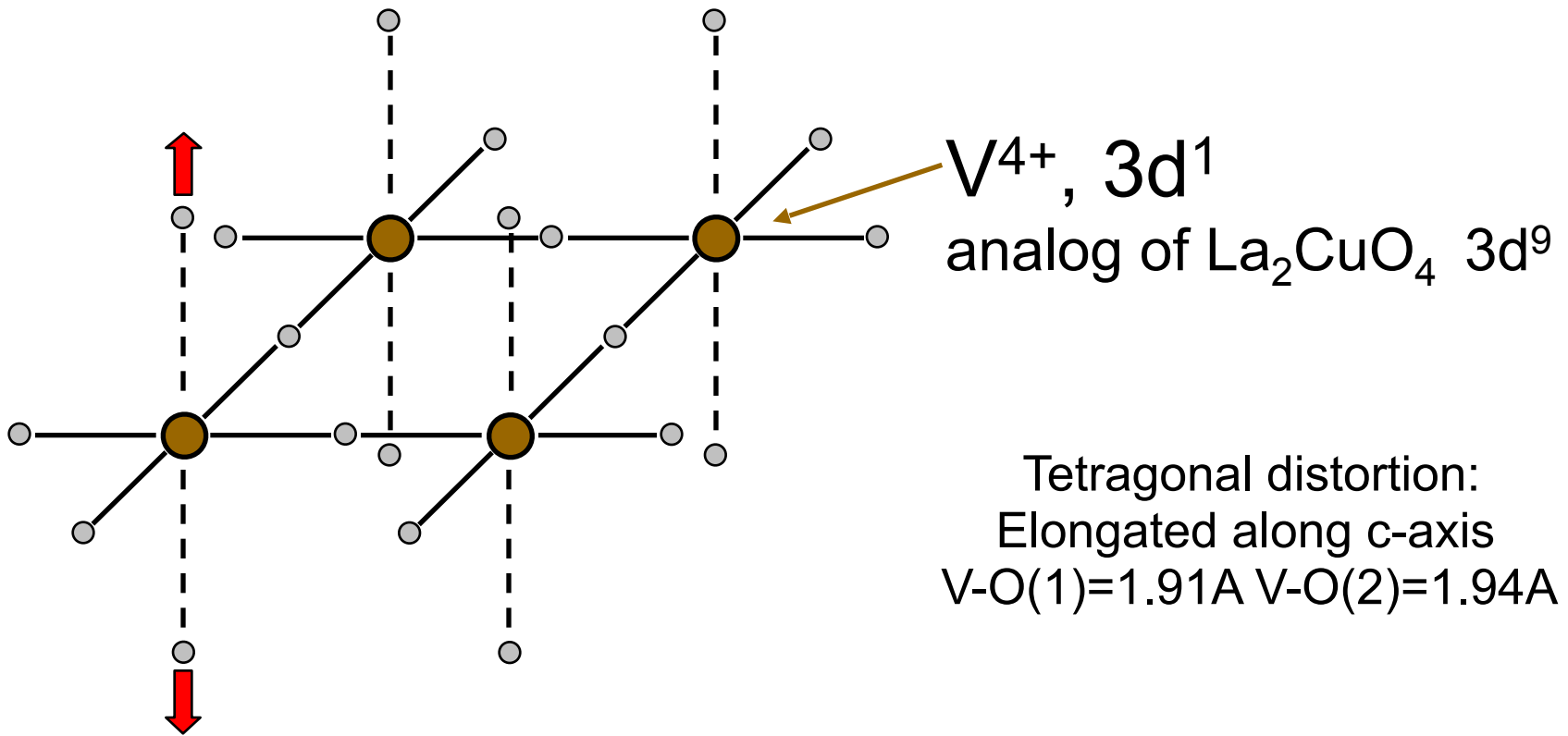
Optimistic Outlook

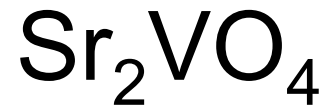
« IL EST BON DE SAVOIR QUE L'UTOPIE N'EST JAMAIS
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RÉALITÉ D'AUJOURD'HUI ÉTAIT L'UTOPIE D'HIER »

LE CORBUSIER

Crystal structure of Sr_2VO_4

Zhou et al., PRL '07





Cyrot et al., '90

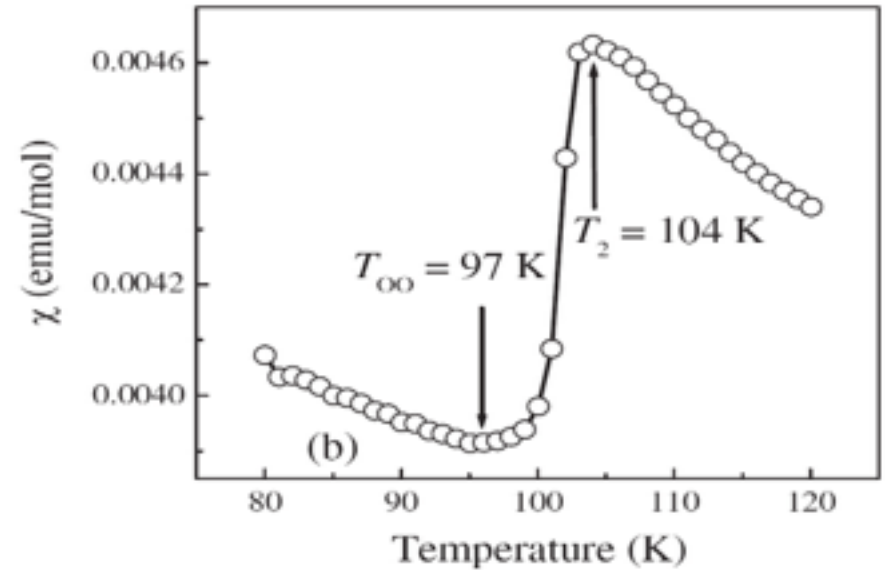
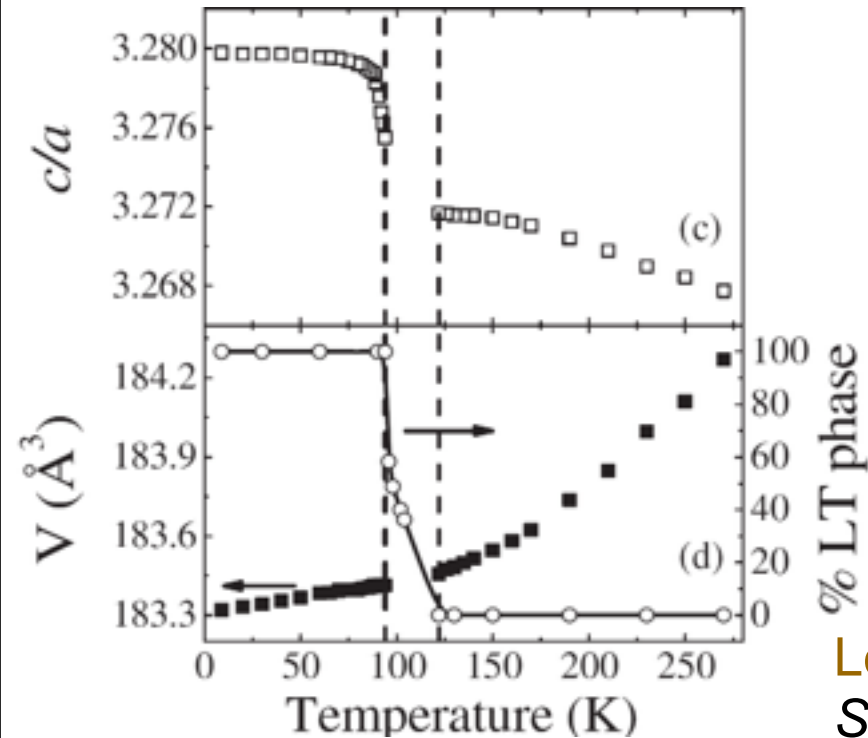
of 7–5 K. The value of the Néel temperature is very sample dependent. On some samples we have measured a Néel temperature as high as 100 K. We have not been able to observe antiferromagnetism with polarized neutrons. However, we note that

Phase transition in Sr_2VO_4

Zhou et al., PRL '07

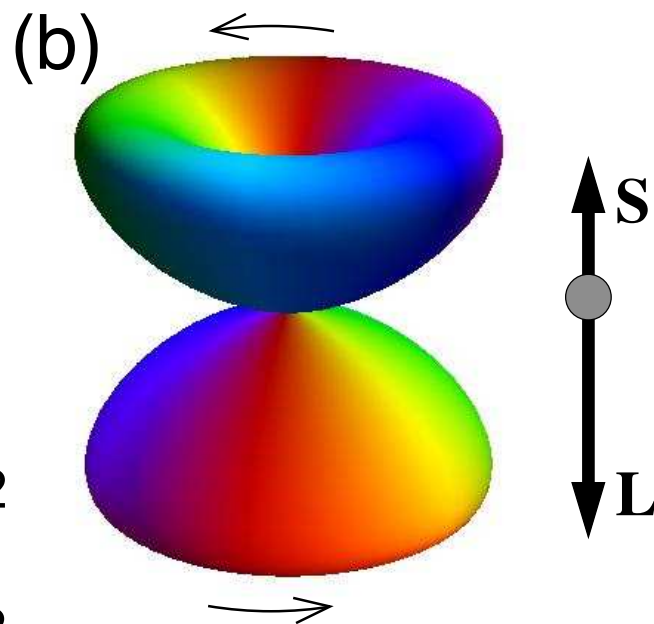
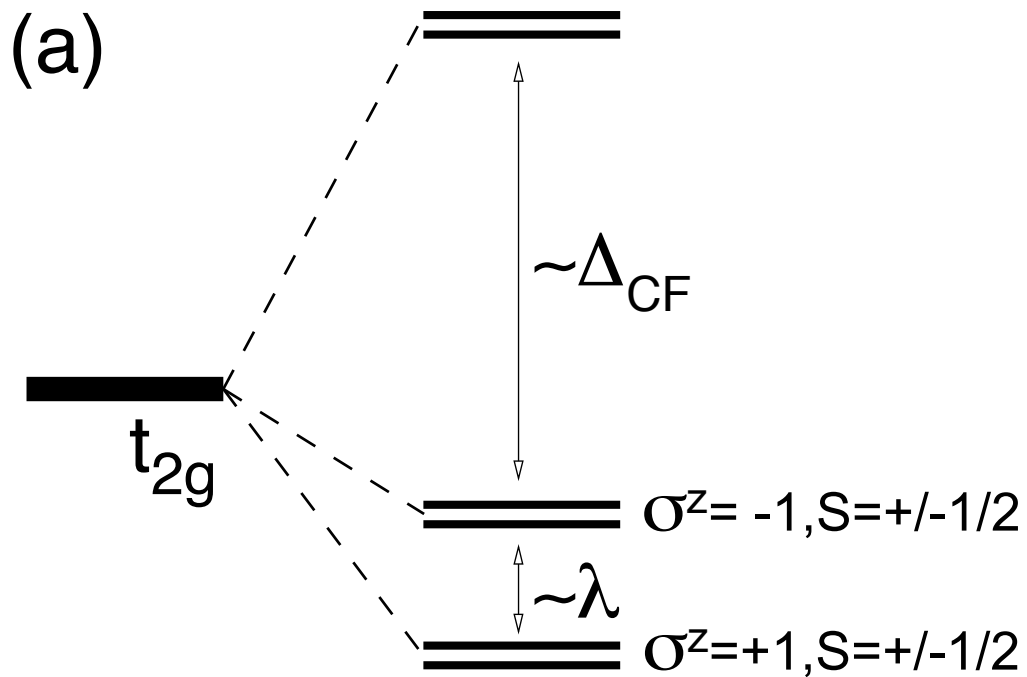
Sharp increase of c/a
Structure remains tetragonal

Sharp drop in spin susceptibility



Looks like 1st order magnetic transition...
So far no Bragg peaks seen by neutrons

Local Electronic Structure




Exchange coupling of Kramers doublets

GJ & G.Khaliullin PRL (2010)

$$\mathcal{H} = J \sum_{\langle ij \rangle} (\vec{s}_i \cdot \vec{s}_j + \frac{1}{4}) \underbrace{(1 \pm \sigma_i^x)(1 \pm \sigma_j^x)}_{\text{Inter-doublet transitions (non-negative, AFM coupling)}} - \frac{\delta}{2} \sum_i \sigma_i^z$$

Isospins

$\sigma^{x=+1}$ 

$\sigma^{x=-1}$ 

Inter-doublet transitions
(non-negative, AFM coupling)

spin-orbit splitting between doublets

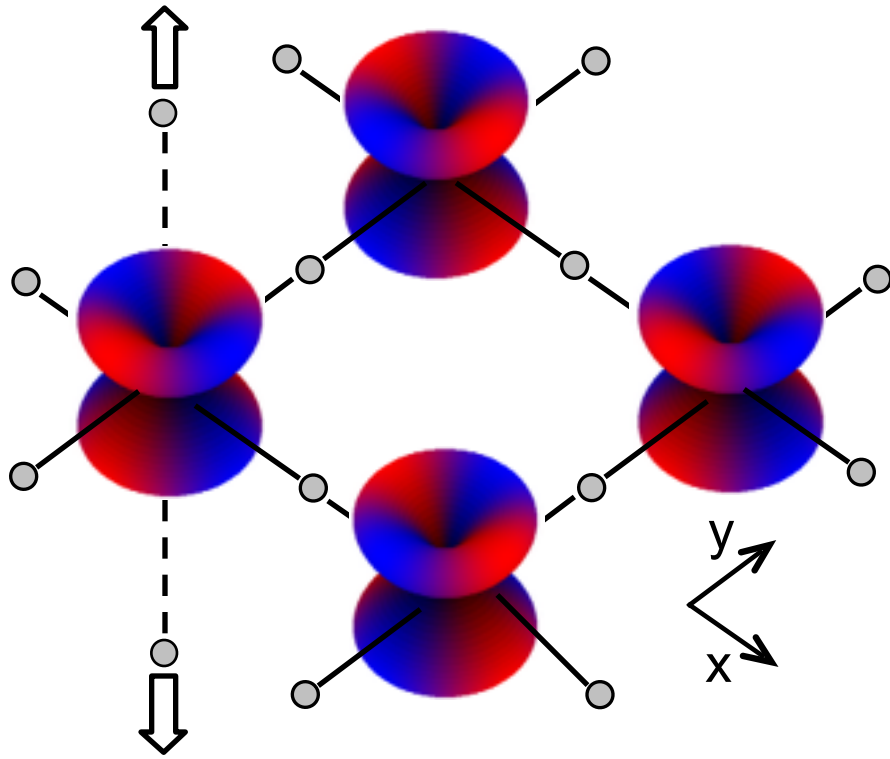
Exchange coupling of Kramers doublets

$$\mathcal{H} = J \sum_{\langle ij \rangle} \underbrace{\left(\vec{s}_i \cdot \vec{s}_j + \frac{1}{4} \right)}_{\text{nearly zero, only quantum energy is gained}} (1 \pm \sigma_i^x)(1 \pm \sigma_j^x) - \frac{\delta}{2} \sum_i \sigma_i^z$$

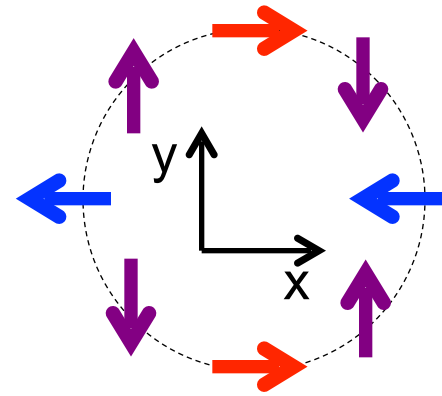
nearly zero,
only quantum
energy is gained

SO coupling
becomes relevant

Octupolar order

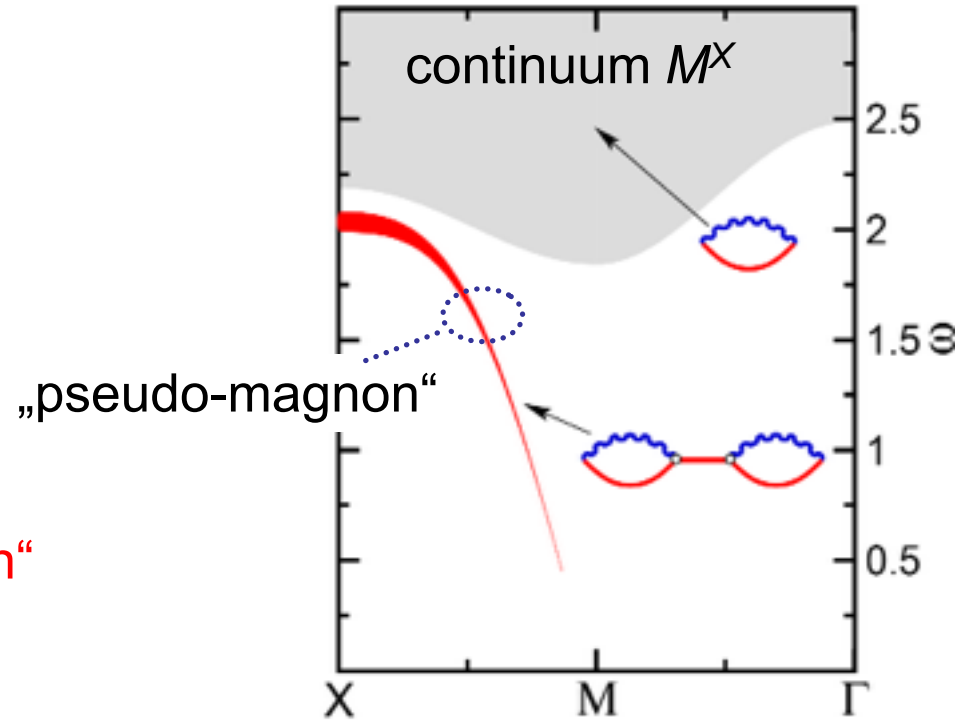
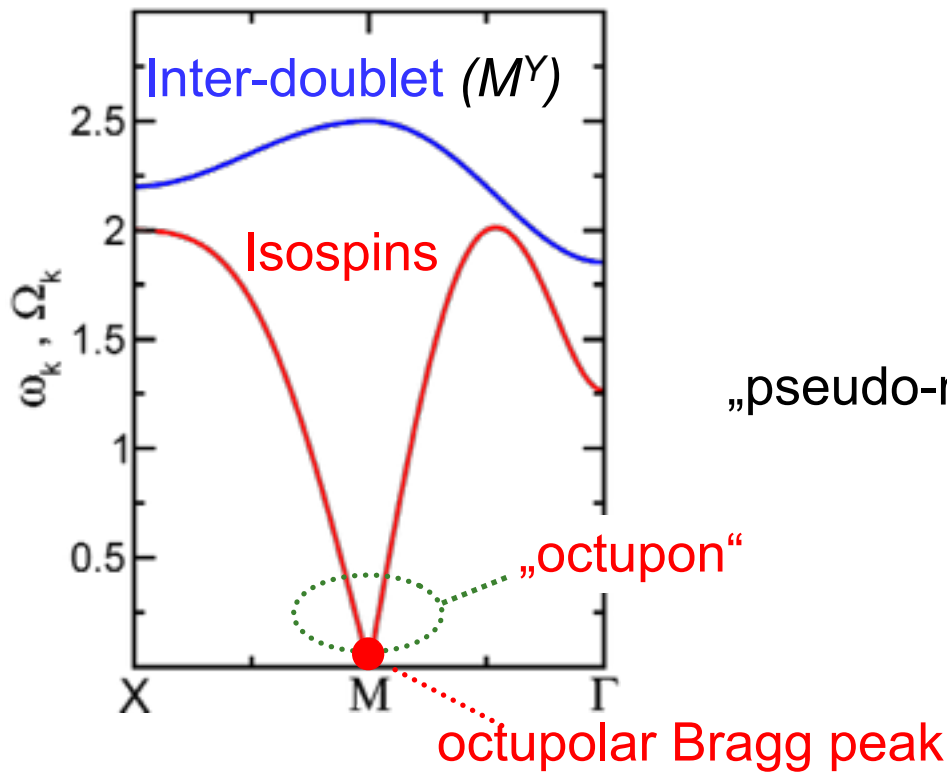


$$\langle \vec{S}_i \rangle = \langle \vec{l}_i \rangle = \vec{0}$$



$$\langle S^x [(l^x)^2 - (l^y)^2] \rangle \neq 0$$

Elementary vs Magnetic Excitations



$$M_i^y = e^{i\mathbf{Q}\mathbf{R}_i} (a_i + a_i^\dagger) \quad M_i^z \simeq \nu(1 - \kappa) e^{i\mathbf{Q}\mathbf{R}_i} (b_i - b_i^\dagger)$$

$$M_i^x \simeq (b_i + b_i^\dagger)(a_i + a_i^\dagger)$$

Hidden magnetic order in Sr_2VO_4 clarified with μ^+ SR

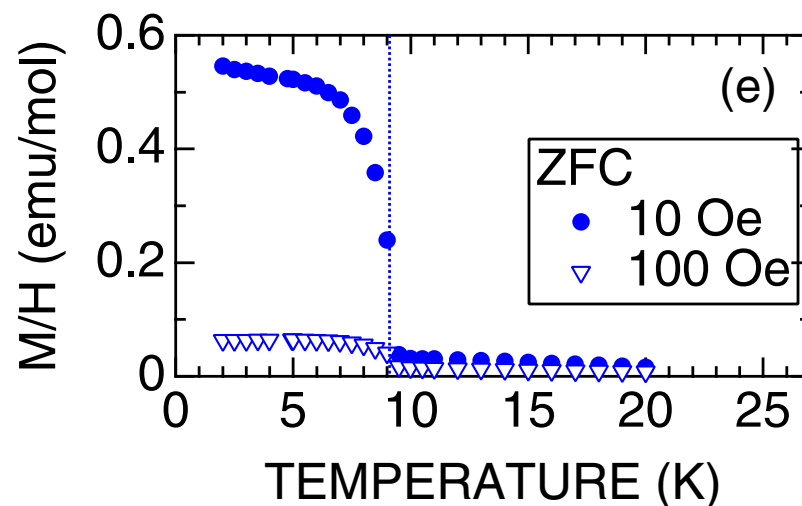
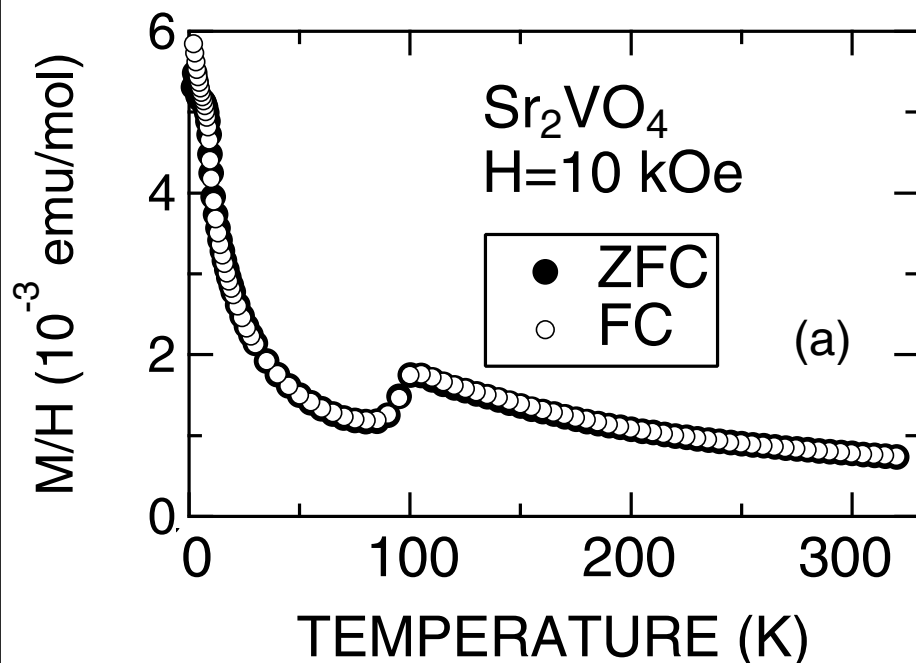
Jun Sugiyama,^{1,*} Hiroshi Nozaki,¹ Izumi Umegaki,¹ Wataru Higemoto,² Eduardo J. Ansaldo,³ Jess H. Brewer,^{3,4} Hiroya Sakurai,⁵ Ting-Hui Kao,^{5,6} Hung-Duen Yang,⁶ and Martin Månsson^{7,8}

In order to elucidate the magnetic ground state of Sr_2VO_4 , we have measured muon spin rotation and relaxation (μ^+ SR) spectra of a powder sample in the temperature range between 1.8 and 140 K. As a result, we have clarified that the transition at 105 K is not magnetic but structural and/or electric in origin and found the appearance of static antiferromagnetic (AF) order below 8 K. Moreover, the distribution of the internal AF field was found to be very broad, even at the lowest temperature measured. These results are consistent with the formation of an orbital-stripe order with collinear AF order for the magnetic ground state of Sr_2VO_4 .

Hidden magnetic order in Sr_2VO_4 clarified with $\mu^+\text{SR}$

Jun Sugiyama,^{1,*} Hiroshi Nozaki,¹ Izumi Umegaki,¹ Wataru Higemoto,² Eduardo J. Ansaldo,³ Jess H. Brewer,^{3,4} Hiroya Sakurai,⁵ Ting-Hui Kao,^{5,6} Hung-Duen Yang,⁶ and Martin Månsson^{7,8}

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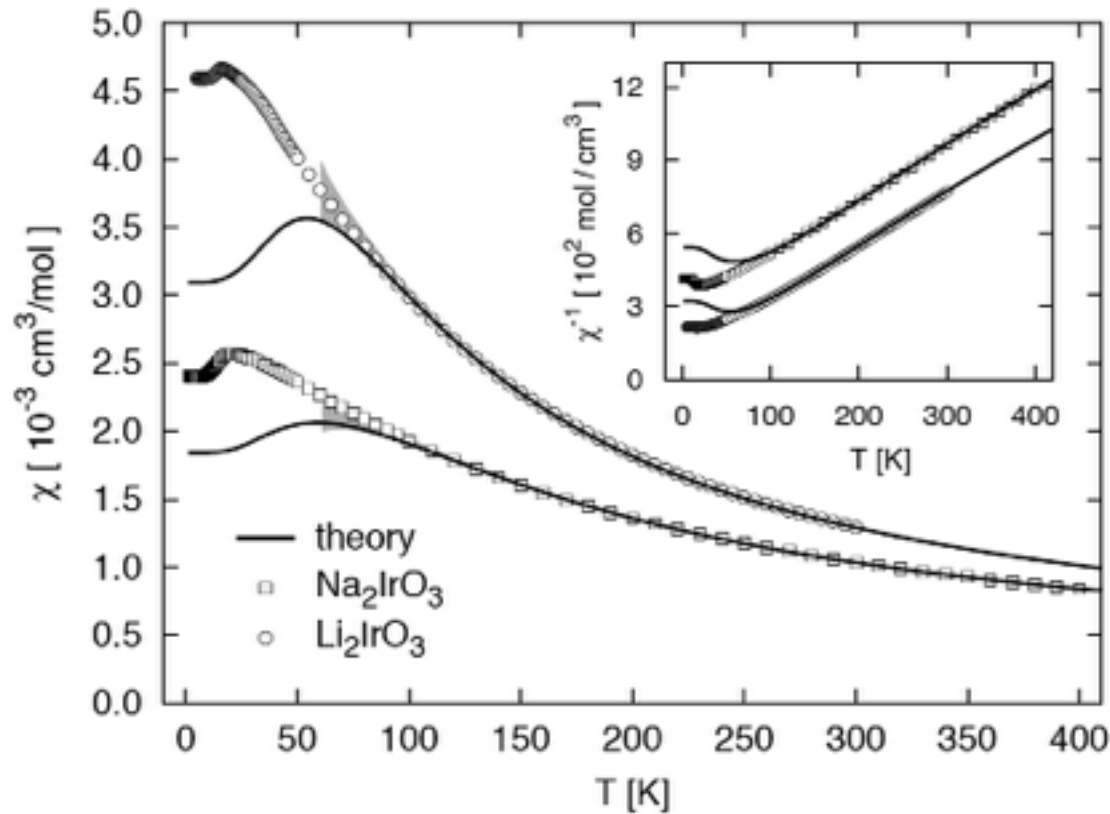


Optimistic Outlook

« IL EST BON DE SAVOIR QUE L'UTOPIE N'EST JAMAIS
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LE CORBUSIER

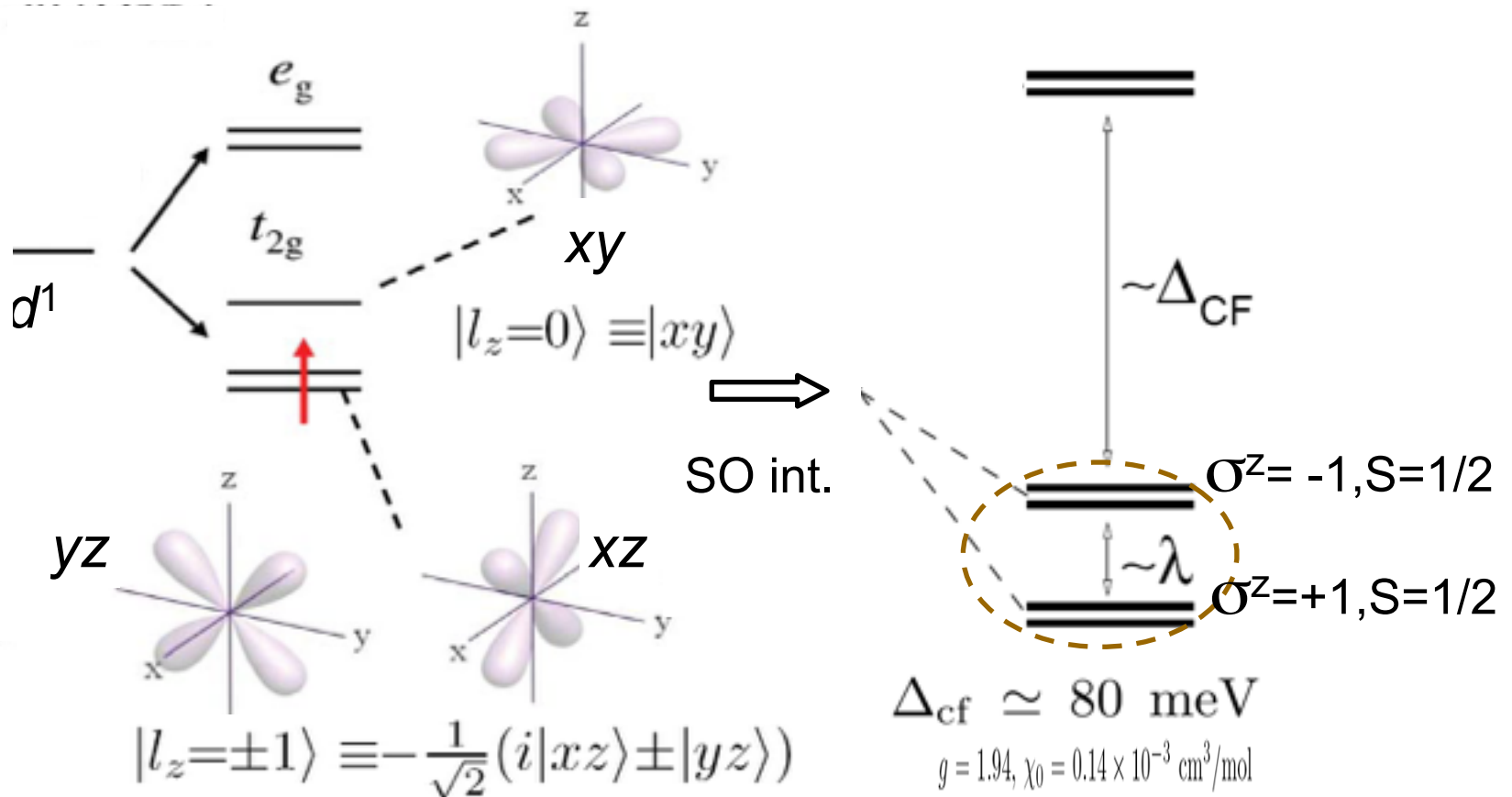
Susceptibility of Zigzag phase



$$2K = 21.0\text{meV}, J = -4.0\text{meV} \quad g = 1.78 \quad \chi_0 = 0.16 \times 10^{-3}\text{cm}^3/\text{mol}$$

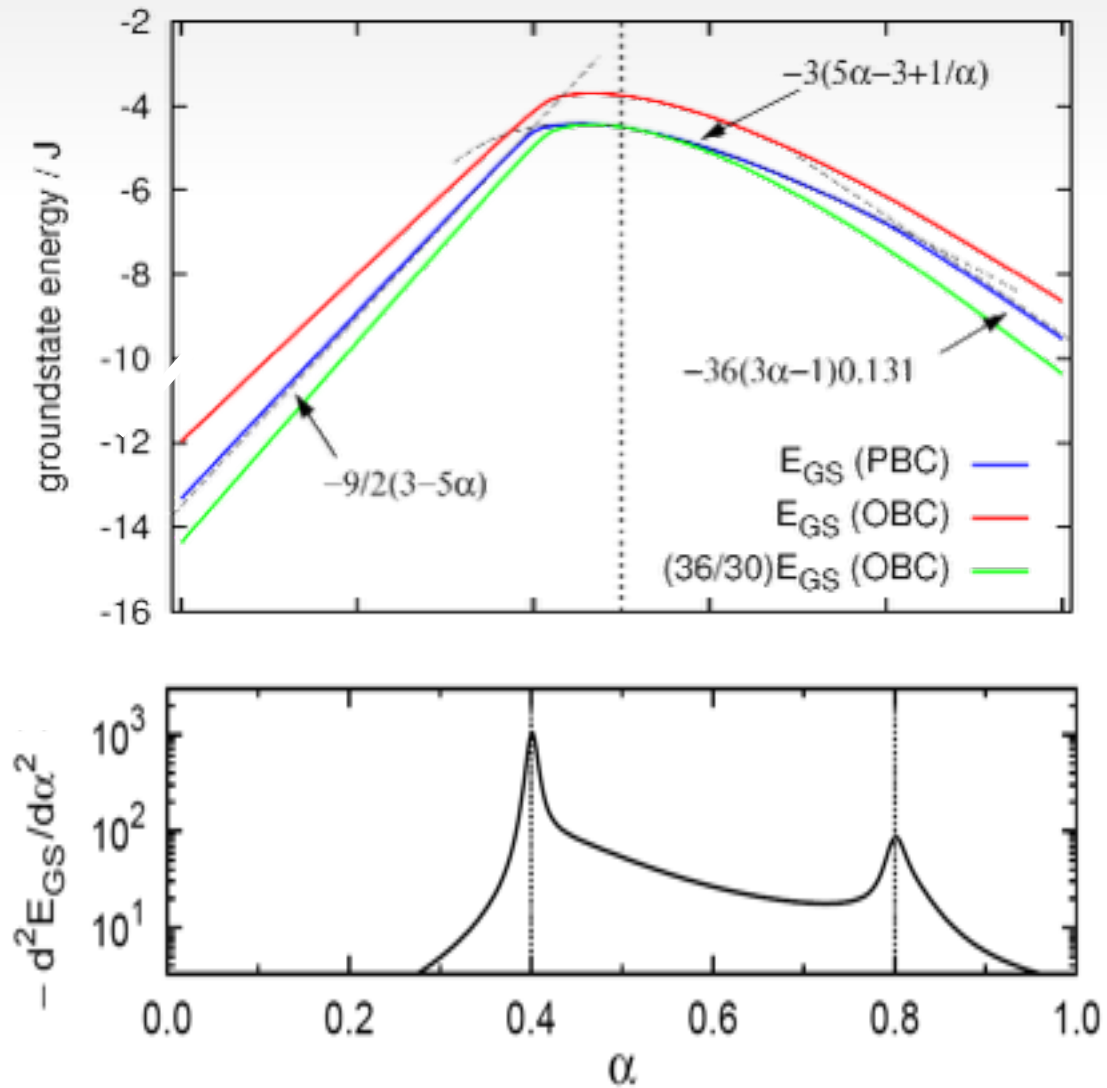
$$2K = 15.7\text{meV}, J = -5.3\text{meV} \quad g = 1.94, \chi_0 = 0.14 \times 10^{-3}\text{cm}^3/\text{mol}$$

Local Electronic Structure

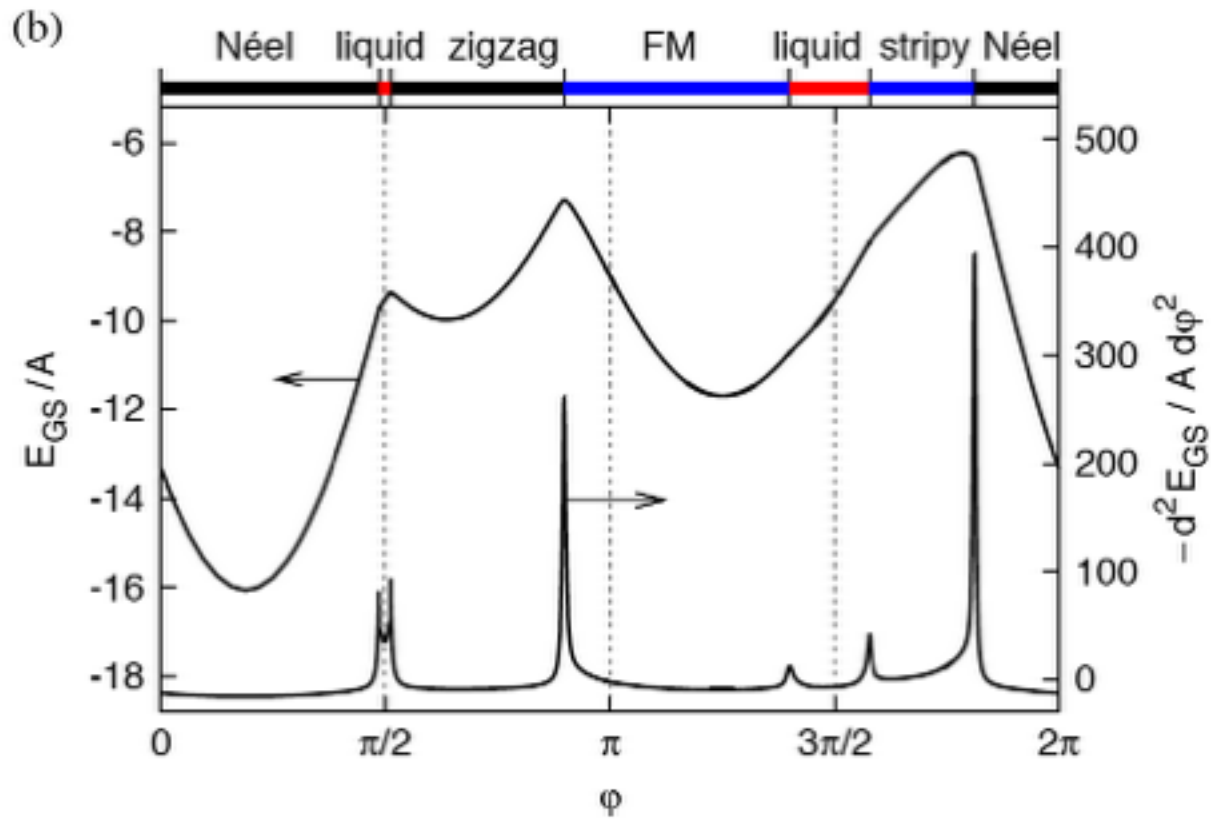


Tetragonal Field: Low energy quadruplet remains active
 Spin-orbit: Quadruplet is split into Kramers doublets

Exact Diagonalization Results



Exact Diagonalization Results



Dimer manifold & Valence bond crystal

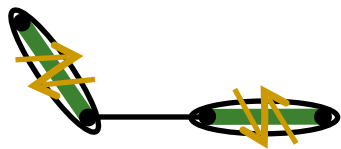
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□ Spin-singlet on dimer bonds: Spin gap



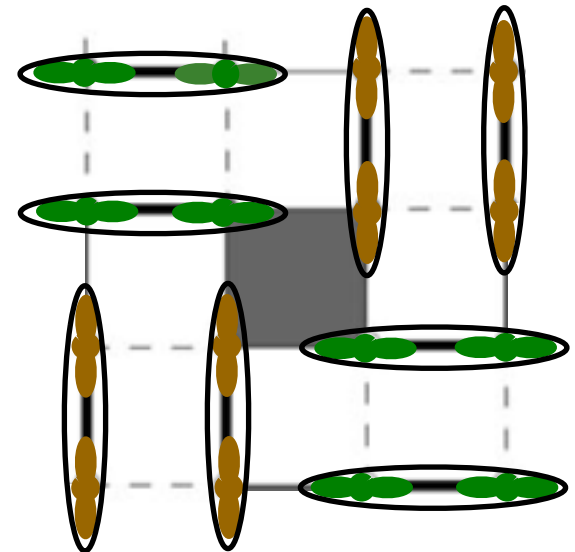
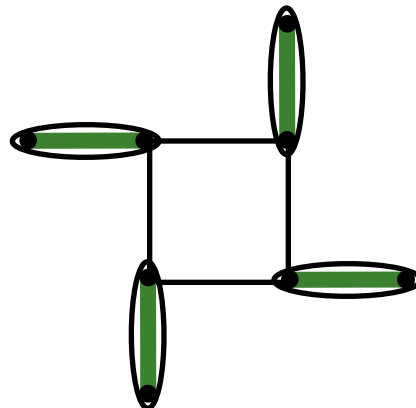
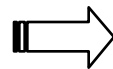
□ Extensively degenerate GS manifold:
hard-core dimer coverings of square lattice

□ Order-out-of-disorder by triplet fluctuations:
Maximize number of closed graphs



$S=1$

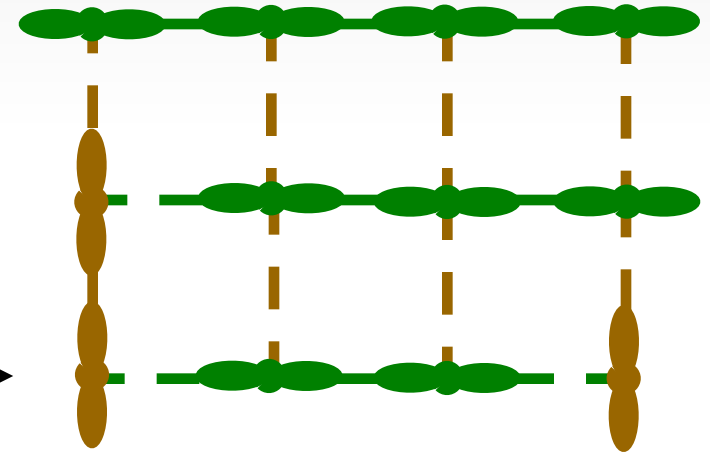
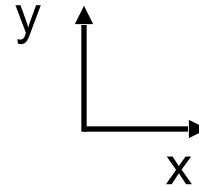
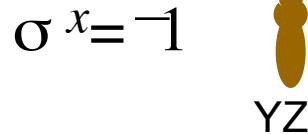
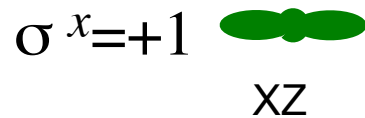
$S=0$



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- Dimensionality reduction due to orbitals:
Fragmentation in clusters of open/closed 1D AFM chains

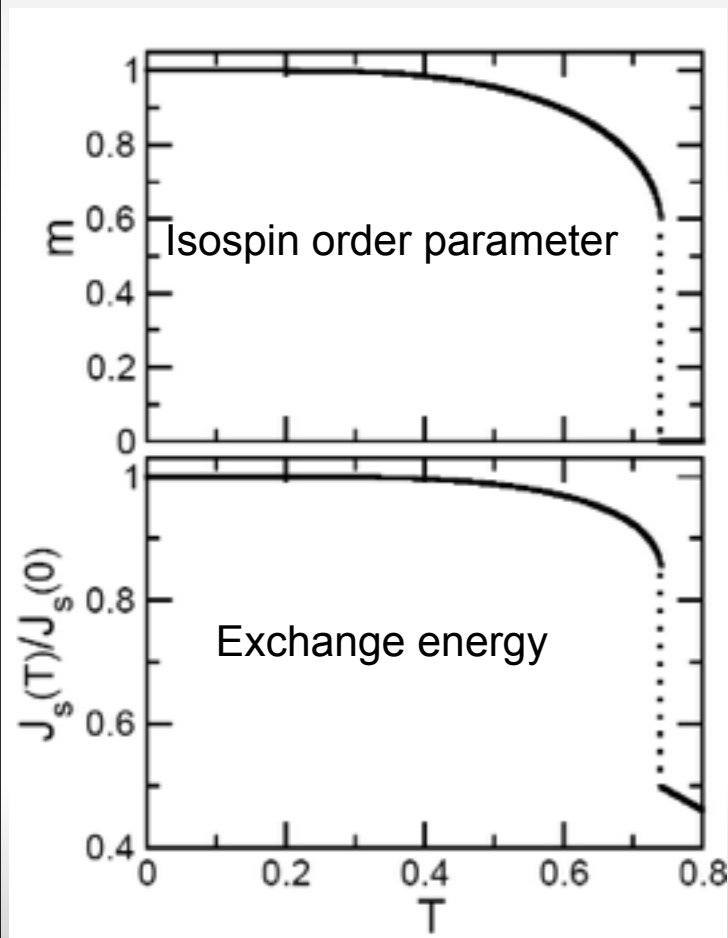
$$\mathcal{H} = J \sum_{\langle ij \rangle} (\vec{s}_i \cdot \vec{s}_j + \frac{1}{4})(1 \pm \sigma_i^x)(1 \pm \sigma_j^x)$$



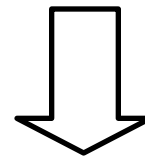
- Classical Neel state ($s_i s_j + 1/4 = 0$) has zero energy
- Shortest chains(=dimers) are favorable -> gain more quantum energy

Finite temperature transition in: Sr_2VO_4

The first order phase transition induced by an interplay between inter- and intra-doublet excitations.



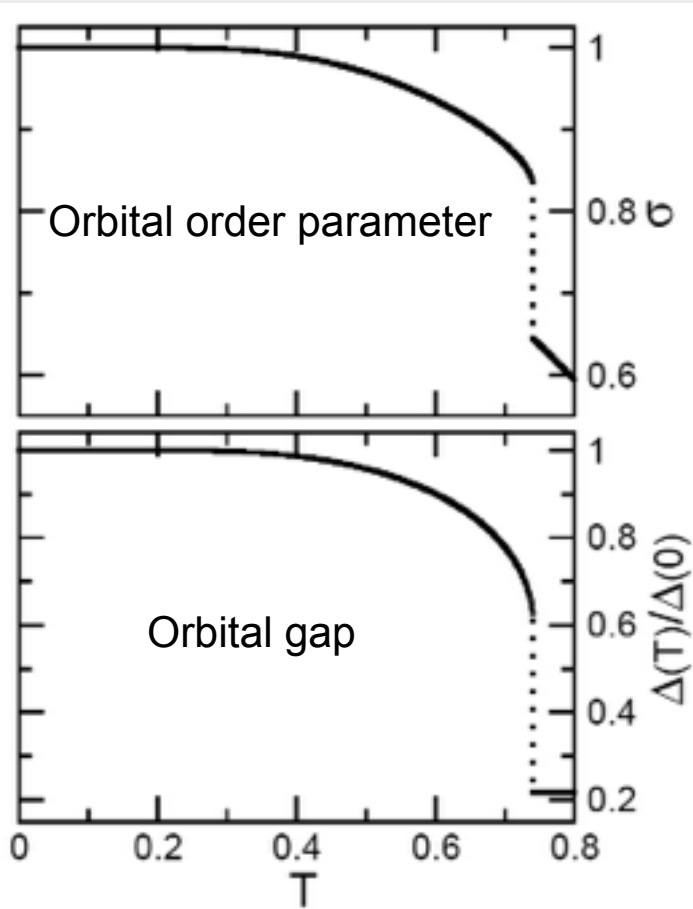
Isospin order parameter and exchange energy jump at the transition



Pronounced magnetoelastic effects explain an abrupt in-plane contraction of the crystal.

Jahn-Teller coupling acts in the same direction as magnetoelastic one amplifying the effect.

Finite temperature transition



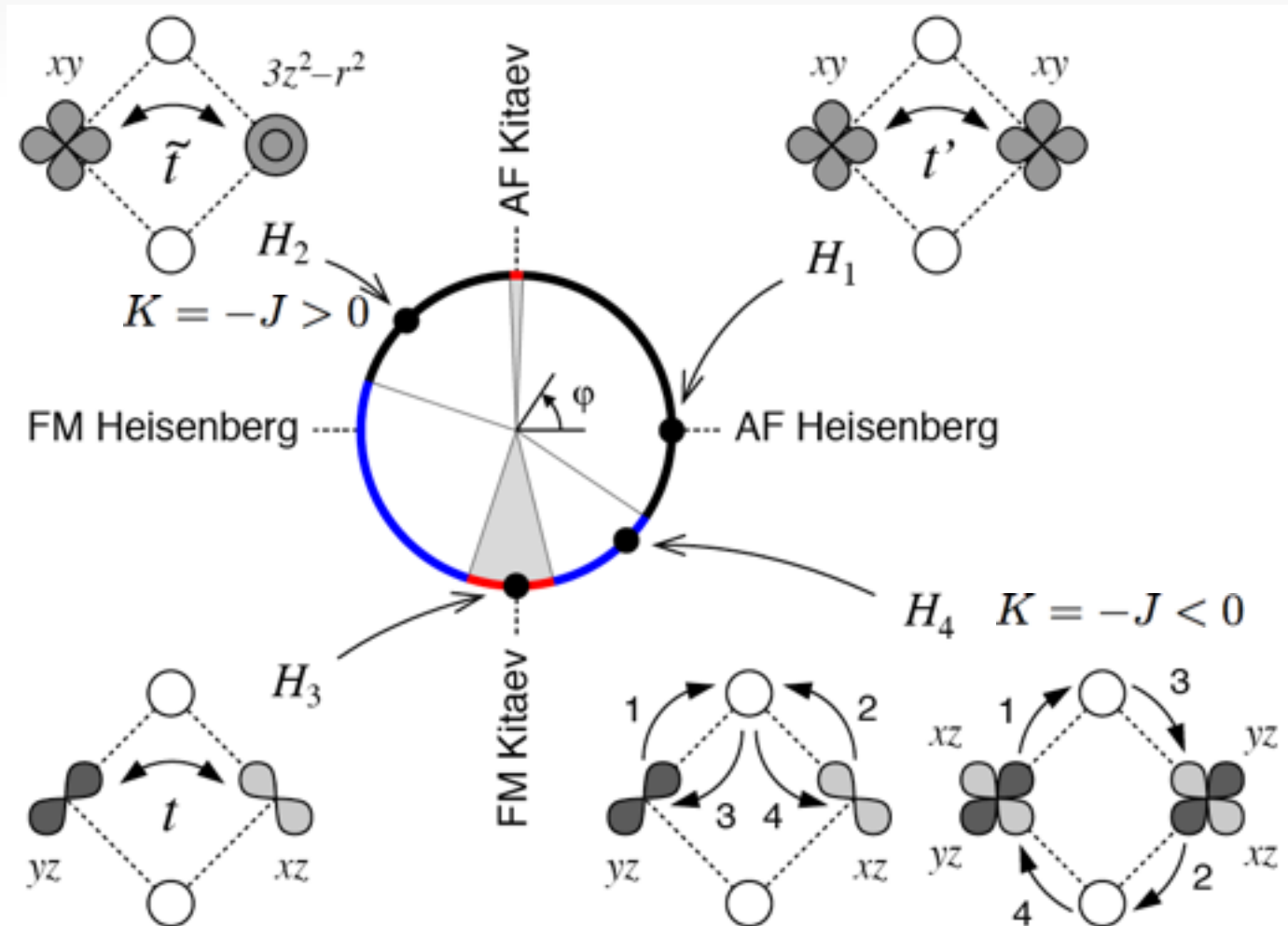
Abrupt enhancement of the population of low energy doublet

Its non-magnetic nature, vanishing g-factors, explains the drop of susceptibility

Examples of exchange processes

$$\mathcal{H}_{ij}^{(\gamma)} = 2K S_i^\gamma S_j^\gamma + J \mathbf{S}_i \cdot \mathbf{S}_j$$

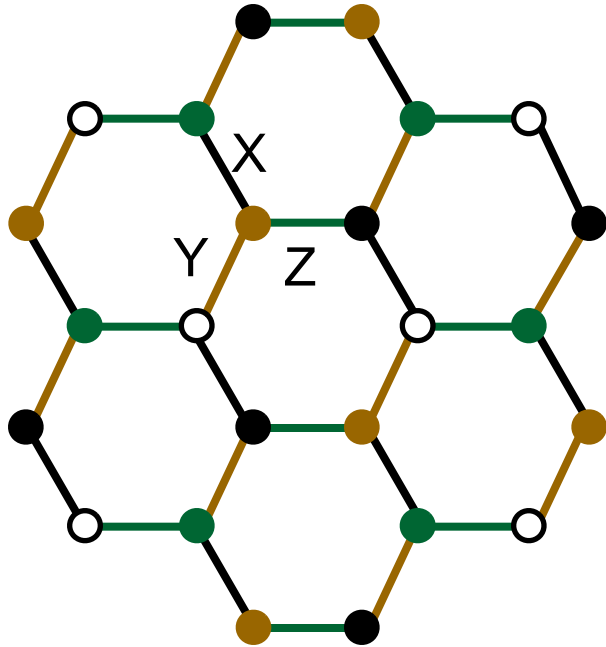
$$K = A \sin \varphi \quad J = A \cos \varphi$$



Kitaev-Heisenberg Model

$$\mathcal{H}_{ij}^{(\gamma)} = 2K S_i^\gamma S_j^\gamma + J \mathbf{S}_i \cdot \mathbf{S}_j$$

$$\tilde{\mathcal{H}}_{ij}^{(\gamma)} = 2[K + J] \tilde{S}_i^\gamma \tilde{S}_j^\gamma - J \tilde{\mathbf{S}}_i \cdot \tilde{\mathbf{S}}_j$$



○ original frame

● $(S^x, S^y, S^z) \rightarrow (S^x, -S^y, -S^z)$

● $(S^x, S^y, S^z) \rightarrow (-S^x, S^y, -S^z)$

● $(S^x, S^y, S^z) \rightarrow (-S^x, -S^y, S^z)$

$$\mathcal{H}_{ij}^{(z)} = S_i^x S_j^x + S_i^y S_j^y - S_i^z S_j^z \quad \Rightarrow \quad \mathcal{H}_{ij}^{(\gamma)} = -\tilde{\mathbf{S}}_i \cdot \tilde{\mathbf{S}}_j$$

further neighbor interactions explains zigzag phase

PHYSICAL REVIEW B **84**, 180407(R) (2011)

Kitaev-Heisenberg- J_2 - J_3 model for the iridates $A_2\text{IrO}_3$

Itamar Kimchi¹ and Yi-Zhuang You^{1,2}

PRL **108**, 127204 (2012)

PHYSICAL REVIEW LETTERS

week ending
23 MARCH 2012

Spin Waves and Revised Crystal Structure of Honeycomb Iridate Na_2IrO_3

S. K. Choi,¹ R. Coldea,¹ A. N. Kolmogorov,² T. Lancaster,^{1,*} I. I. Mazin,³ S. J. Blundell,¹ P. G. Radaelli,¹ Yogesh Singh,^{4,5}
P. Gegenwart,⁴ K. R. Choi,⁶ S.-W. Cheong,^{6,7} P. J. Baker,⁸ C. Stock,⁸ and J. Taylor⁸

PRL **108**, 127203 (2012)

PHYSICAL REVIEW LETTERS

week ending
23 MARCH 2012

Relevance of the Heisenberg-Kitaev Model for the Honeycomb Lattice Iridates $A_2\text{IrO}_3$

Yogesh Singh,^{1,2} S. Manni,² J. Reuther,^{3,4} T. Berlijn,^{5,6} R. Thomale,⁷ W. Ku,^{5,6} S. Trebst,⁸ and P. Gegenwart²

Magnetic excitation spectrum of Na_2IrO_3 probed with resonant inelastic x-ray scattering

H. Gretarsson,¹ J. P. Clancy,¹ Yogesh Singh,² P. Gegenwart,³ J. P. Hill,⁴ Jungho Kim,⁵ M. H. Upton,⁵ A. H. Said,⁵ D. Casa,⁵ T. Gog,⁵ and Young-June Kim^{1,*}

