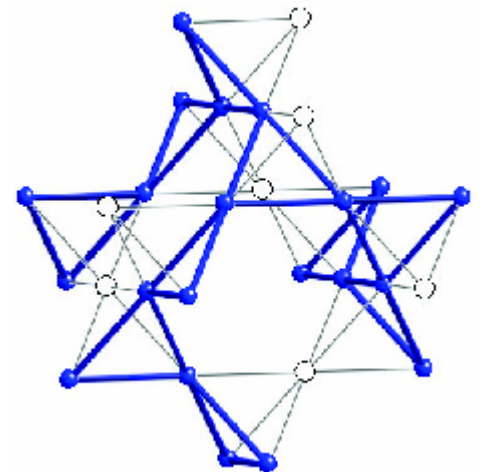


Novel Phases in Iridates

Yogesh Singh

Indian Institute of Science Education and Research, Mohali



Outline

- The Hyper-Kagome material $\text{Na}_4\text{Ir}_3\text{O}_8$
- The Honeycomb lattice iridates A_2IrO_3 (A = Na, Li)

The Hyper-Kagome material $\text{Na}_4\text{Ir}_3\text{O}_8$

Collaborators

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Yoshi Tokiwa, Jinkui Dong, and P. Gegenwart

University of Goettingen

Kwang-Yong Choi

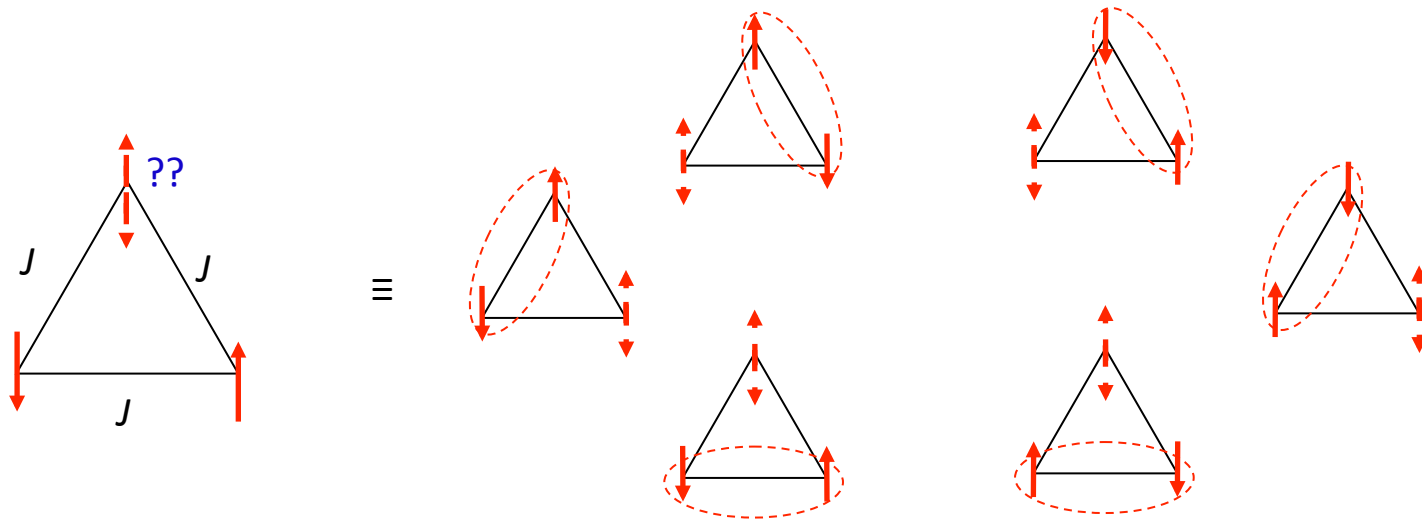
University of Seoul

Seung-Ho Baek

IFW Dresden

Spin Liquids in Geometrically Frustrated Magnets

Huge degeneracy



Spin-liquid: Quantum Disordered State of Strongly Interacting Spins

Recipe for Quantum Fluctuations

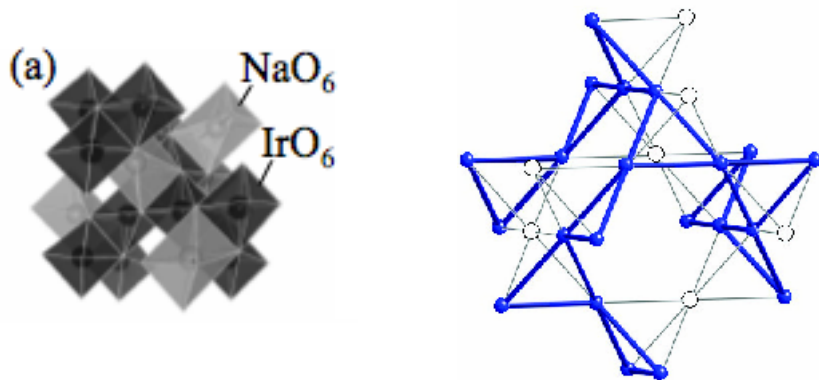
- Small spin $S = \frac{1}{2}$
- Low-Dimensionality and/or co-ordination
- Geometric Frustration

Most Candidate Spin Liquids are $S = \frac{1}{2}$ Quasi-Low-Dimensional Magnets

Na₄Ir₃O₈ : Possible 3D Spin Liquid?

Spin-Liquid State in the $S = 1/2$ Hyperkagome Antiferromagnet Na₄Ir₃O₈

Y. Okamoto *et al.*, PRL **99**, 137207 (2007)



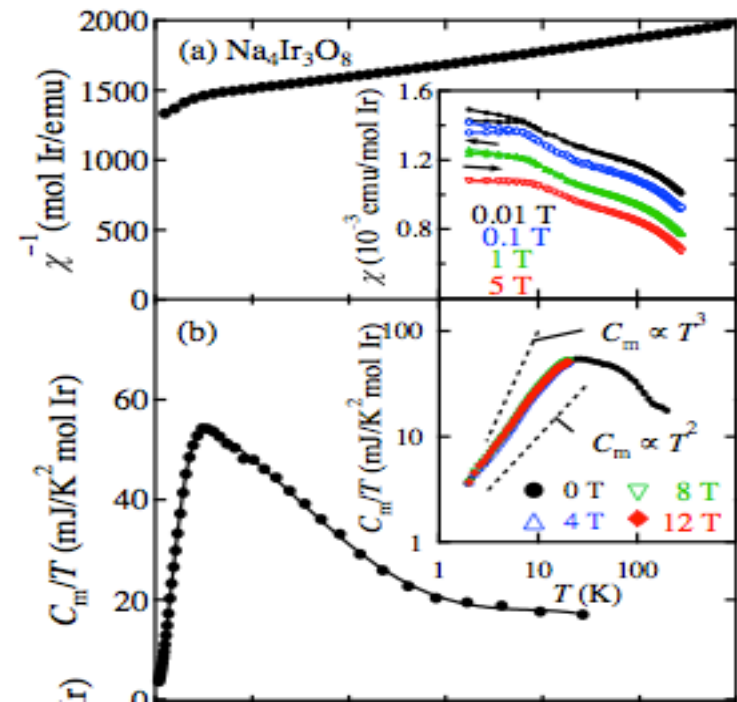
Hyper-Kagome

**Magnetic frustration
expected and seen**



TABLE I: Atomic parameters obtained by refining x-ray powder diffraction for Na₄Ir₃O₈ at room temperature with a space group $P4_132$. The cubic lattice constant is $a = 8.985$ Å. g of Na2 and Na3 are fixed to 0.75 according to Ref. [10].

		x	y	z	g	B (Å)
Ir	12d	0.61456(7)	$x + 1/4$	5/8	1.00	0.15
Na1	4b	7/8	7/8	7/8	1.00	2.6
Na2	4a	3/8	3/8	3/8	0.75	2.6
Na3	12d	0.3581(8)	$x + 1/4$	5/8	0.75	2.6
O1	8c	0.118(11)	x	x	1.00	0.6
O2	24e	0.1348(9)	0.8988(8)	0.908(11)	1.00	0.6



Predictions for $\text{Na}_4\text{Ir}_3\text{O}_8$

- J. M. Hopkinson, ..., Phys. Rev. Lett. **99**, 037201 (2007).

A classical Heisenberg model on the hyperkagome lattice predicts a spin nematic order with long range dipolar spin correlations is chosen at $T \approx 1$ K by an order-by-disorder mechanism

- M. J. Lawler... Phys. Rev. Lett. **100**, 227201 (2008).

Semi-classical spin-model of Heisenberg spins predicts a 120° coplanar magnetically ordered state. This was found to give way, through a quantum phase transition, to a gapped topological Z₂ 'bosonic' spin liquid phase when quantum fluctuations are turned on.

- Y. Zhou.... Phys. Rev. Lett. **101**, 197201 (2008).

- M. J. Lawler.... Phys. Rev. Lett. **101**, 197202 (2008).

Predicted gapless spin liquids with a Fermi surface of chargeless spinons which at low temperatures was found to be unstable to the formation of paired states with line nodes

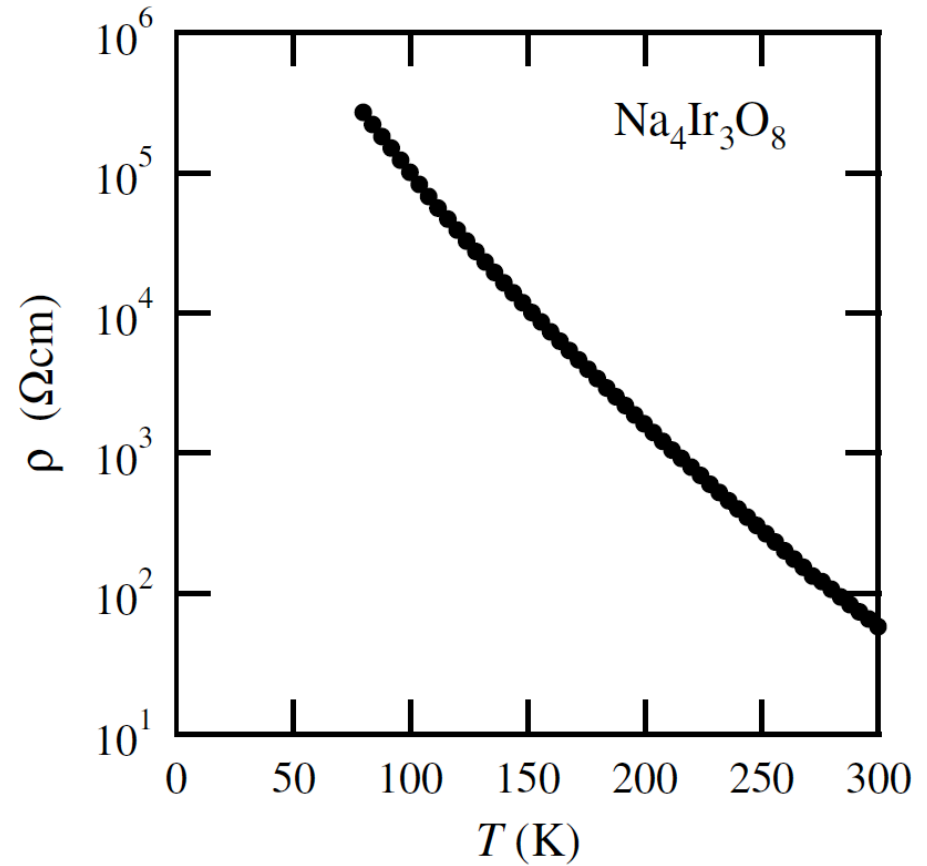
- G. Chen and L. Balents, Phys. Rev. B **78**, 094403 (2008).

Inclusion of spin-orbit coupling was shown to relieve the frustration in some regions of parameter space and might lead to ordering at low temperatures

$\text{Na}_4\text{Ir}_3\text{O}_8$: Resistivity

Insulator but near MIT

$$\Delta \approx 500 - 900 \text{ K}$$



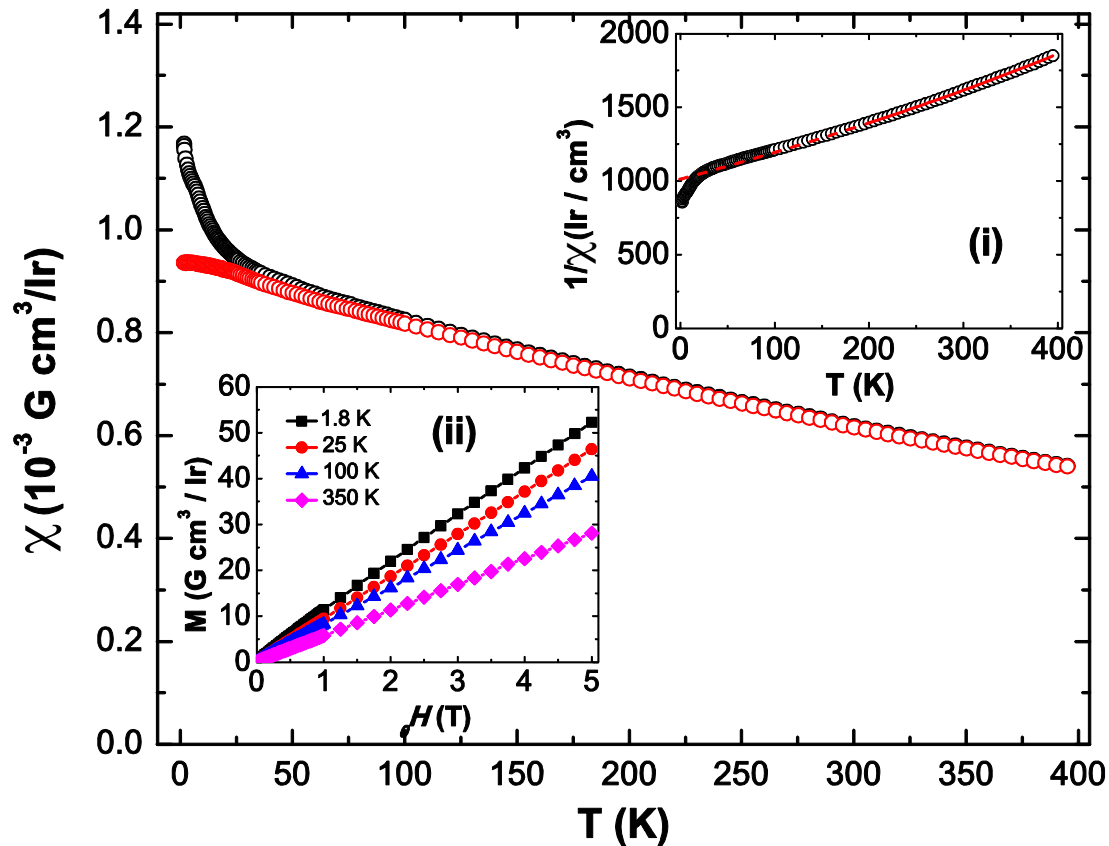
Magnetic Susceptibility

- Curie-Weiss fit to inverse susceptibility gives

$$\mathbf{S}_{\text{eff}} = 1/2, \theta \approx -600 \text{ K}$$

- No transition down to 1.8 K
- Intrinsic susceptibility 'saturates' below 20 K

$\chi_0 \sim \text{const. as in metal}$

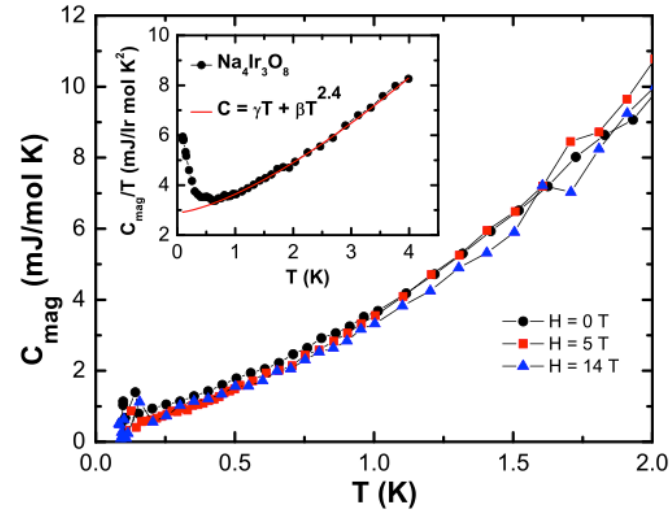
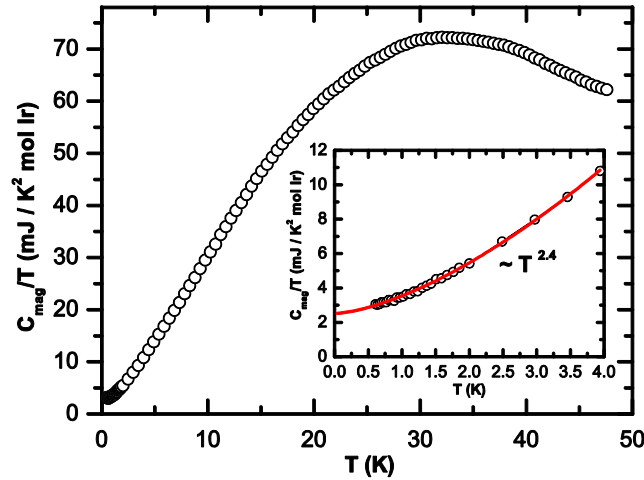


Gapless Spin Liquid !!

Heat Capacity and Thermal Conductivity

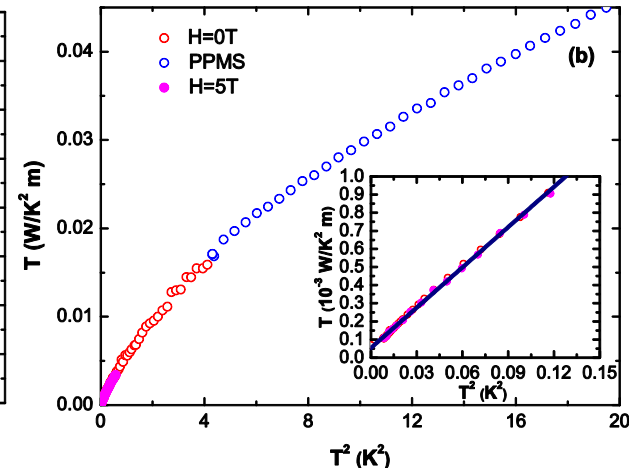
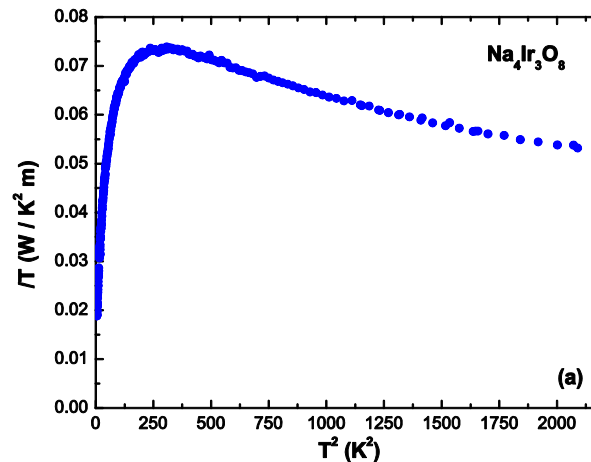
- No transition down to 100 mK
- Broad peak at around 30 K
- $C_{\text{mag}} \sim T^n$ ($2 < n < 3$)
- Finite $\gamma \sim 2\text{-}3$ mJ/mol K² as in a metal

Heat Capacity

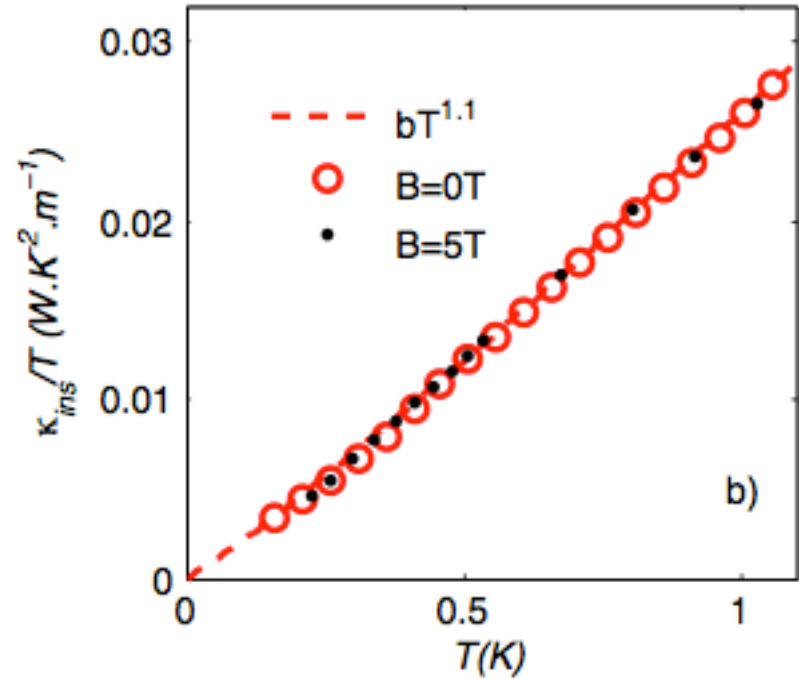
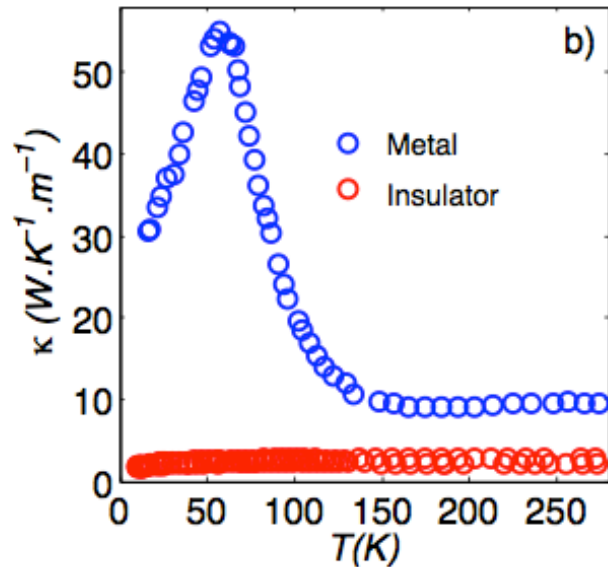
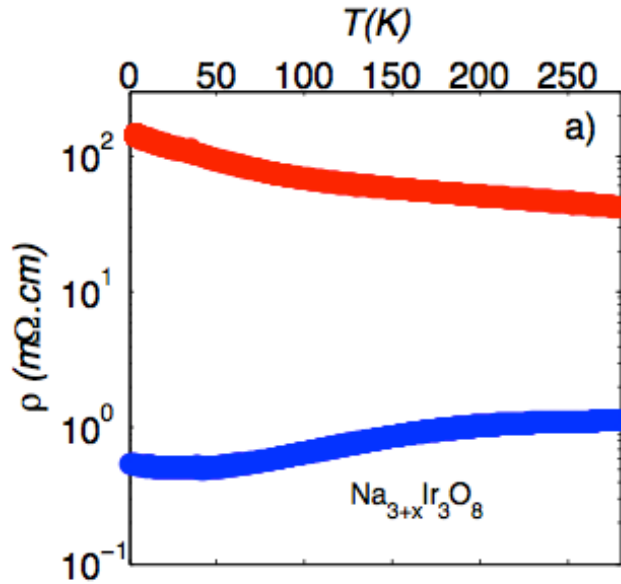


- No transition down to 75 mK
- $\kappa/T \rightarrow 0$ as $T \rightarrow 0$

Thermal Conductivity



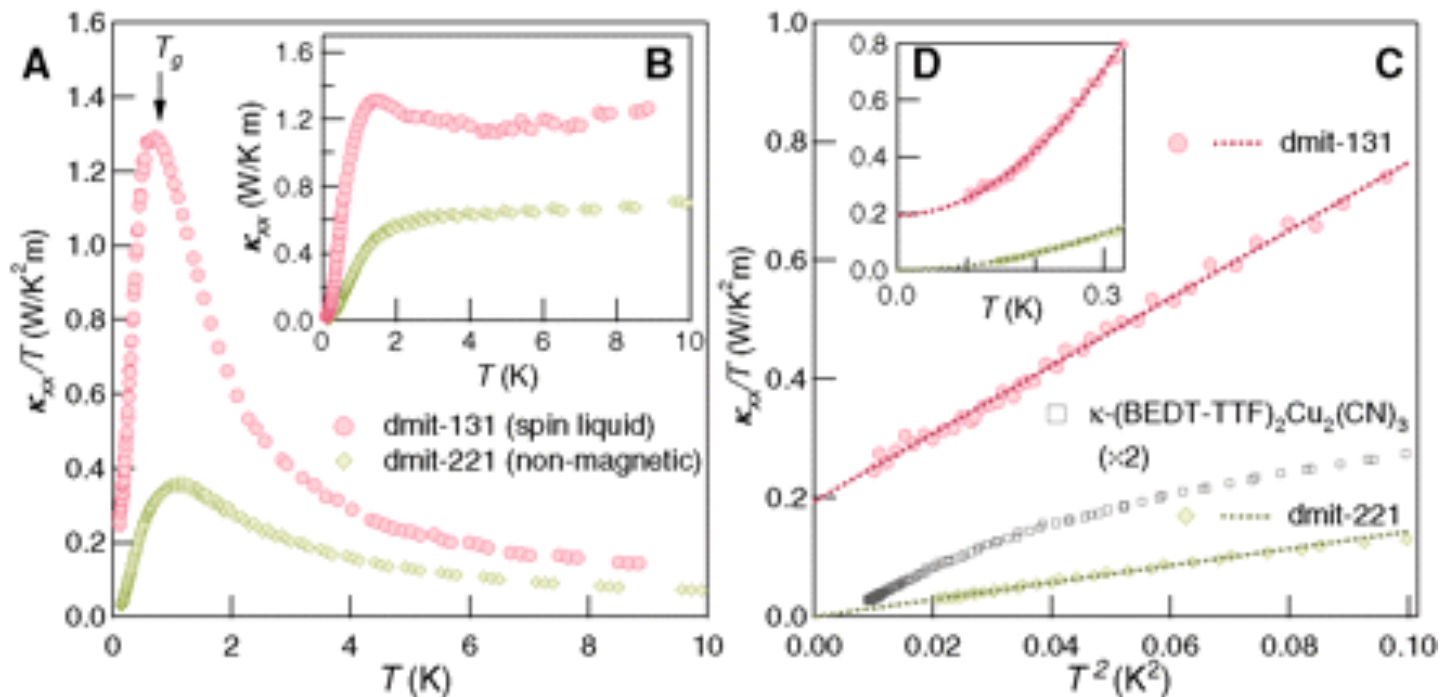
Thermal conductivity across the metal-insulator transition in single crystalline hyperkagome $\text{Na}_{3+x}\text{Ir}_3\text{O}_8$, B. Fauque, et al arxiv:1210:8792 (2014).



Comparison with other spin liquids

ET-dmit ($\kappa/T \approx 180 \text{ mW/K}^2 \text{ m}$, $\gamma \approx 20 \text{ mJ/mol K}^2$)

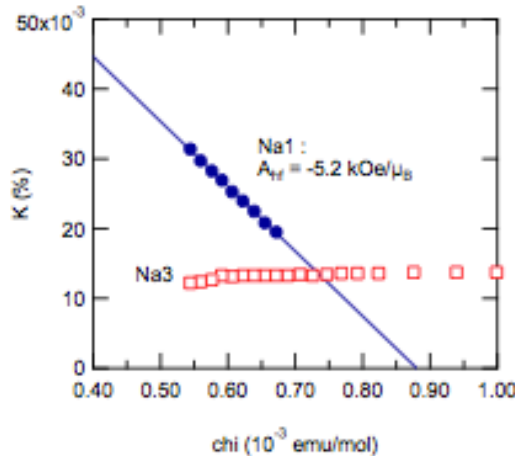
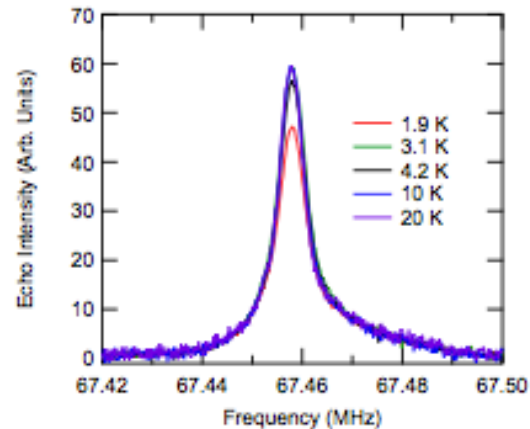
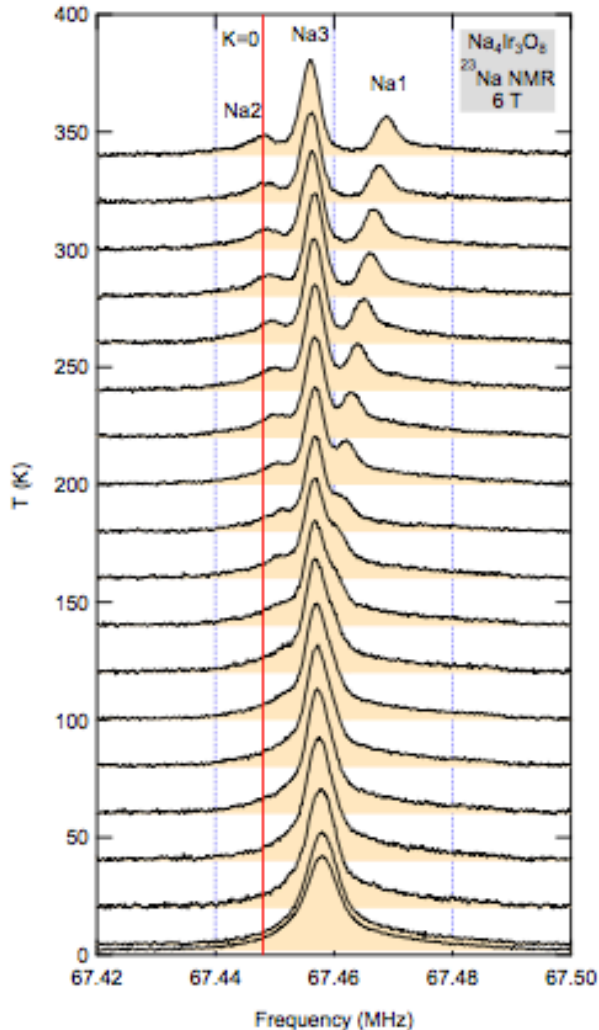
kappa- (BEDT-TTF) $_2$ Cu $_2$ (CN) $_3$ ($\kappa/T \rightarrow 0$, $\gamma \approx 20 \text{ mJ/mol K}^2$)



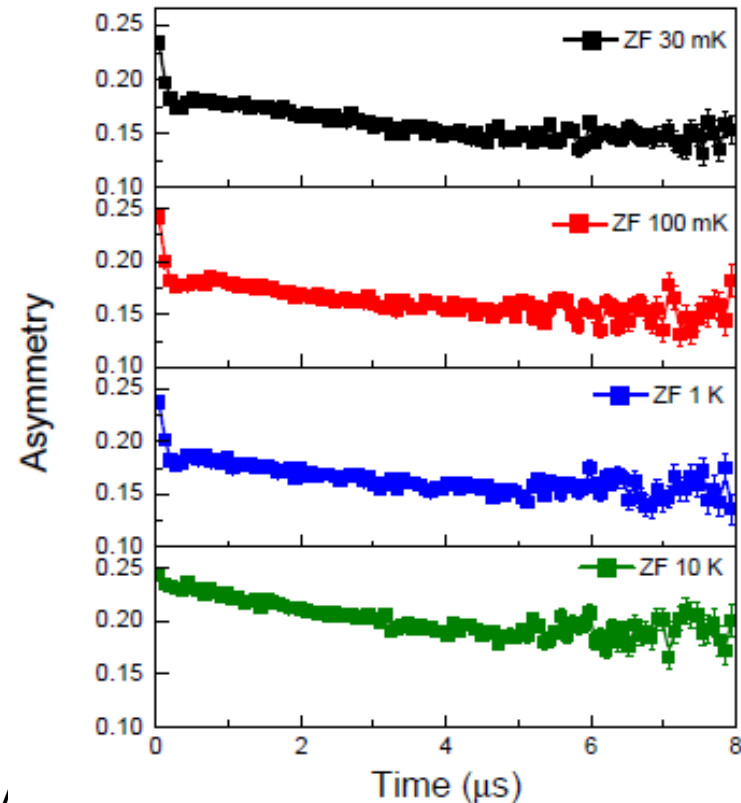
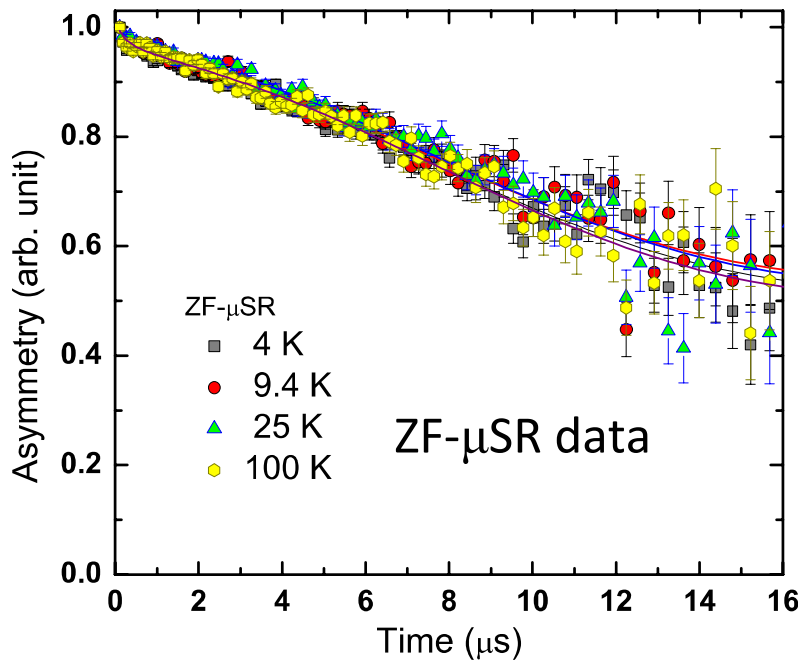
S. Nakajima *et al.*, J. Phys. Soc. Jpn. **81**, 063706 (2012).

^{23}Na NMR in $\text{Na}_4\text{Ir}_3\text{O}_8$

Seung-Ho Baek, IFW Dresden



- At high temperatures, three NMR lines appear due to three different crystallographic Na sites.
- There is no signature of static magnetism down to 2 K.
- For Na1, the hf coupling constant is estimated to be -5.2 kOe per Bohr magneton. (The negative sign means that the dominant hf coupling is due to the core polarization term.)
- For Na3, there is essentially no hf coupling, which allows to estimate non-spin contribution from the spin-lattice relaxation rate.



A fitting function $A_0 P_{ZF}(t) = A_1 G^{KT}(t, \Delta) \exp[-(\lambda t)^\beta] + A_{BG}$

→ $G^{KT}(t, \Delta)$ is a Kubo-Toyabe relaxation function due to nuclear moments.

→ The second moment of the field distribution $\Delta = 0.0904$ MHz is T-independent, supporting nuclear moments as its origin.

→ A_{BG} represents muons stopped outside the samples.

→ A (stretched) exponential function describes electronic spin fluctuations.

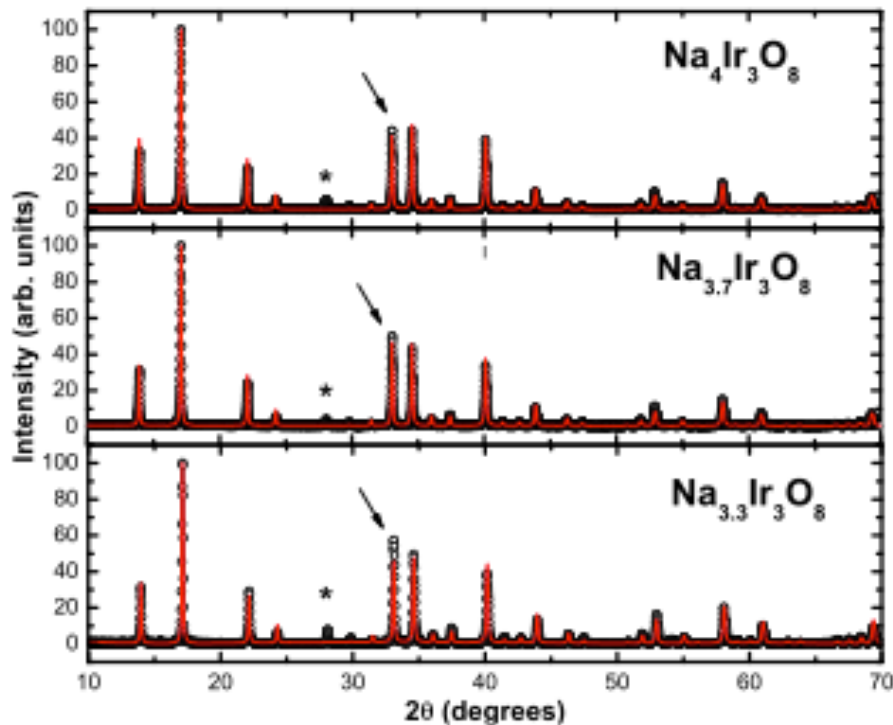
→ We observe no muon precessions down to $T = 1.4$ K. This means that no static electronic moments freeze or order and local moments are fluctuating at all measured temperatures.

→ The T-independent λ and $\beta = 1.2$ implies the persistence of a significant relaxation, indicative of electronic spin fluctuations with dynamics not set by a thermal scale.

- Perturb to Reveal
- Study $\text{Na}_{4-x}\text{Ir}_3\text{O}_8$
- Search for a nearby magnetic state
- Tune the system metallic

$\text{Na}_{4-x}\text{Ir}_3\text{O}_8$ ($x = 0 - 0.7$)

P4₁32 (213)

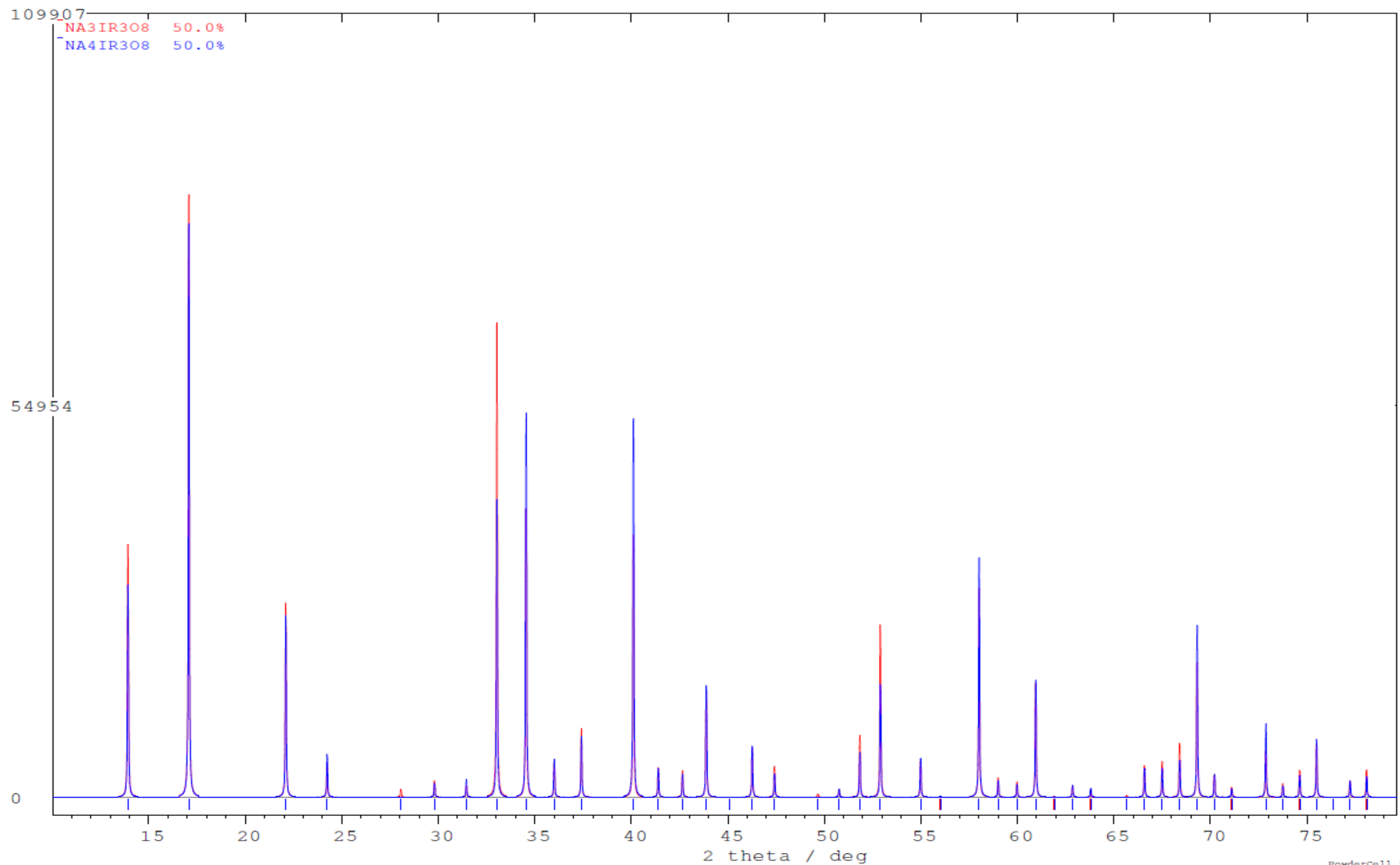


$\text{Na}_4\text{Ir}_3\text{O}_8$ $a = 8.981(2)$ Å						
atom	Wyck	x	y	z	Occ.	$B(\text{Å}^2)$
Ir	12d	1/8	0.141(3)	0.392(5)	1	0.4(1)
Na1	4a	3/8	3/8	3/8	1	1.8(6)
Na2	4b	7/8	7/8	7/8	0.71(1)	2.1(4)
Na3	12d	1/8	0.883(4)	0.131(2)	0.75	1.4(8)
O1	8c	0.142(6)	x	x	1	0.9(2)
O2	24e	0.124(6)	0.315(8)	0.352(4)	1	1.3(6)
$\text{Na}_{3.7}\text{Ir}_3\text{O}_8$ $a = 8.979(7)$ Å						
Ir	12d	1/8	0.137(3)	0.383(4)	1	0.8(3)
Na1	4a	3/8	3/8	3/8	1	2.2(1)
Na2	4b	7/8	7/8	7/8	0.64(1)	1.7(3)
Na3	12d	1/8	0.868(4)	0.129(4)	0.70(2)	2.4(8)
O1	8c	0.105(6)	0.105(6)	0.105(6)	1	1.0(7)
O2	24e	0.112(6)	0.335(8)	0.337(4)	1	2.1(3)
$\text{Na}_{3.3}\text{Ir}_3\text{O}_8$ $a = 8.980(3)$ Å						
Ir	12d	1/8	0.139(3)	0.386(5)	1	0.7(2)
Na1	4a	3/8	3/8	3/8	1	2.1(2)
Na2	4b	7/8	7/8	7/8	0.36(3)	2.6(4)
Na3	12d	1/8	0.876(4)	0.122(1)	0.64(2)	1.9(7)
O1	8c	0.105(6)	0.105(6)	0.105(6)	1	0.9(3)
O2	24e	0.112(6)	0.335(8)	0.337(4)	1	1.1(4)

Spin-orbit coupling induced semi-metallic state in the 1/3 hole doped hyper-kagome $\text{Na}_3\text{Ir}_3\text{O}_8$

Tomohiro Takayama^{1,*}, Akiyo Matsumoto², Jürgen Nuss¹, Alexander Yaresko¹, Kenji Ishii³, Masahiro Yoshida^{3,4}, Junichiro Mizuki^{3,4} & Hidenori Takagi^{1,2}

Comparison of $\text{Na}_4\text{Ir}_3\text{O}_8$ and $\text{Na}_3\text{Ir}_3\text{O}_8$ PXRD



Comparison of $\text{Na}_4\text{Ir}_3\text{O}_8$ and $\text{Na}_3\text{Ir}_3\text{O}_8$ structures

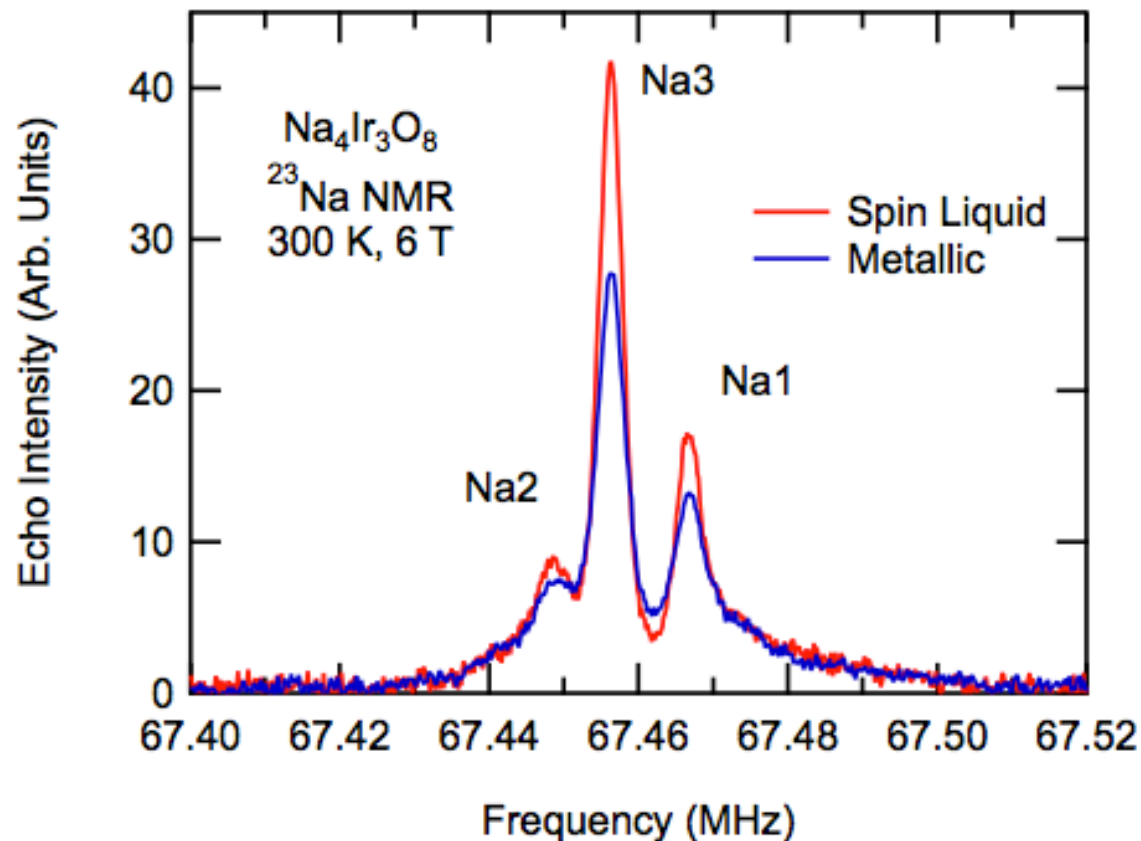
TABLE I: Atomic parameters obtained by refining x-ray powder diffraction for $\text{Na}_4\text{Ir}_3\text{O}_8$ at room temperature with a space group $P4_132$. The cubic lattice constant is $a = 8.985 \text{ \AA}$. g of Na2 and Na3 are fixed to 0.75 according to Ref. [10].

		x	y	z	g	$B \text{ (\AA)}$
Ir	12d	0.61456(7)	$x + 1/4$	5/8	1.00	0.15
Na1	4b	7/8	7/8	7/8	1.00	2.6
Na2	4a	3/8	3/8	3/8	0.75	2.6
Na3	12d	0.3581(8)	$x + 1/4$	5/8	0.75	2.6
O1	8c	0.118(11)	x	x	1.00	0.6
O2	24e	0.1348(9)	0.8988(8)	0.908(11)	1.00	0.6

Table 1 **Refined structural parameters of $\text{Na}_3\text{Ir}_3\text{O}_8$** . The space group is $P4_132$ (No. 213) and $Z = 4$, and the lattice constant is $a = 8.9857(4) \text{ \AA}$. g and U_{iso} denote site occupancy and isotropic displacement parameter, respectively. The final R indices are $R = 0.0133$ and $wR = 0.0287$.

Atom	site	g	x	y	z	$U_{\text{iso}} \text{ (\AA}^2\text{)}$
Ir	12d	1	0.61264(1)	$x + 1/4$	5/8	0.00802(4)
Na(1)	4b	1	7/8	7/8	7/8	0.0122(5)
Na(2)	8c	1	0.2570(2)	x	x	0.0138(4)
O(1)	8c	1	0.1144(2)	x	x	0.0105(6)
O(2)	24e	1	0.1364(3)	0.9071(2)	0.9186(2)	0.0111(4)

NMR: Metallic $\text{Na}_4\text{Ir}_3\text{O}_8$



The slightly metallic sample $x = 0.3$ reveals a very similar spectrum with reduced intensities of the 3 Na lines

Transport and Magnetism of $\text{Na}_{4-x}\text{Ir}_3\text{O}_8$

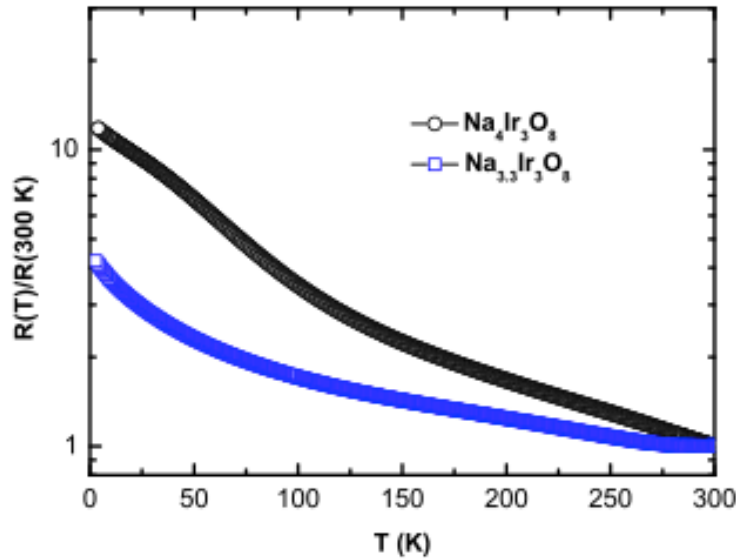


FIG. 2: (Color online) Resistance divided by the $T = 300$ K value $R(T)/R(300\text{K})$ versus T of $\text{Na}_{4-x}\text{Ir}_3\text{O}_8$ ($x = 0, 0.7$).

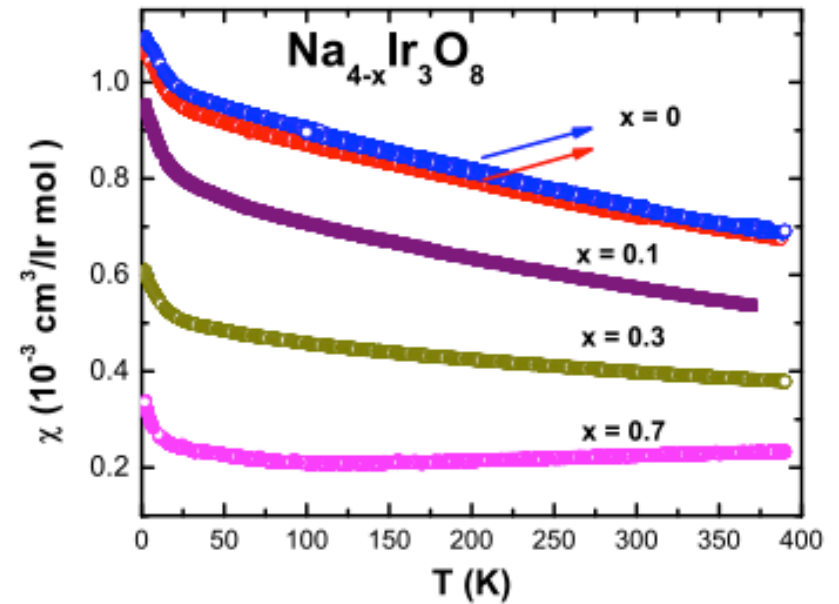


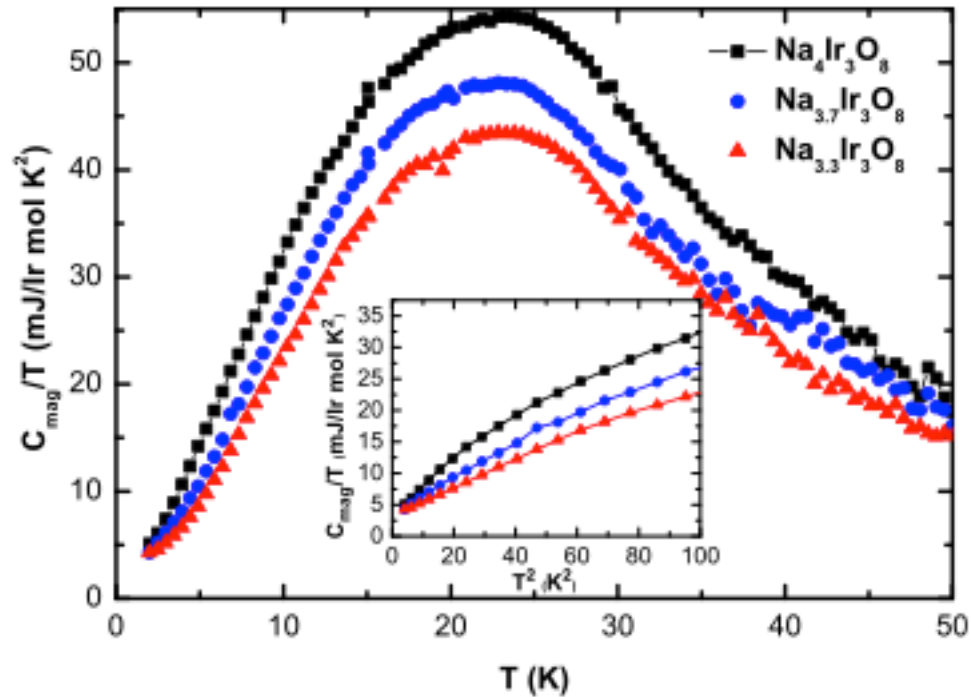
FIG. 3: (Color online) Magnetic susceptibility χ versus T of $\text{Na}_{4-x}\text{Ir}_3\text{O}_8$ ($x = 0, 0.1, 0.3, 0.7$) between $T = 2$ K and 400 K.

A. Balodhi, A. Thamizhavel, Yogesh Singh,
arxiv:1412:0455 (2014).

TABLE II: Parameters obtained from fits to the magnetic susceptibility data by the Curie-Weiss expression $\chi = \chi_0 + \frac{C}{T-\theta}$

x	χ_0 (10^{-4} cm ³ /Ir mol)	C (cm ³ K/Ir mol)	θ (K)
0	1.2(1)	0.39(1)	-568(9)
0.1	1.4(1)	0.33(2)	-512(6)
0.3	1.8(6)	0.28(3)	-509(7)
0.7			

Heat Capacity of $\text{Na}_{4-x}\text{Ir}_3\text{O}_8$



- The 25 K anomaly in C_{mag} is robust against hole doping
- **The anomaly could be an artifact of improper lattice subtraction**

Summary for $\text{Na}_4\text{Ir}_3\text{O}_8$

- $\text{Na}_4\text{Ir}_3\text{O}_8$ is a highly frustrated magnet with $\theta_w \approx -600$ K , no ordering $T > 100$ mK.
- Thermodynamic measurements as well as NMR and μSR strongly suggest SL ($T > 1$ K) with C and χ suggesting gapless excitations but $k/T \rightarrow 0$ as $T \rightarrow 0$.
- Freezing below 1K in μSR .
- Na-deficient samples show that SL is robust. No enhanced freezing observed in Na-deficient samples.

The Honeycomb lattice Iridates $A_2\text{IrO}_3$

Honeycomb-lattice iridates

Na_2IrO_3 and Li_2IrO_3

Kavita Mehlawat and Ashwini Balodhi

Soham Manni and P. Gegenwart

Sungkyun Choi and Radu Coldea

X. Liu, H. Gretarsson, Young-June Kim, J.P. Hill

R. Comin, A. Damascelli

Jason N. Hancock, D. van der Marel

T. Berlijn, W. Ku, ...

R. Thomale, J. Reuther, S. Trebst

Crystal synthesis and characterization

Structural refinement, μSR , INS

Resonant x-ray scattering

ARPES

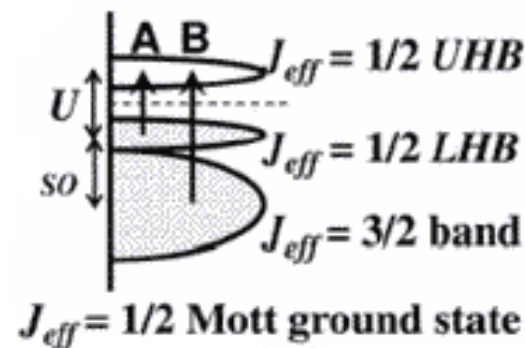
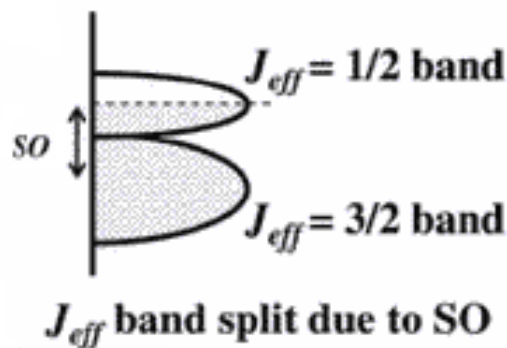
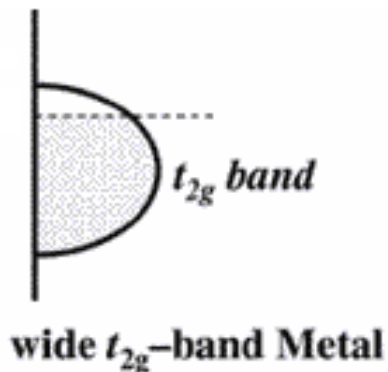
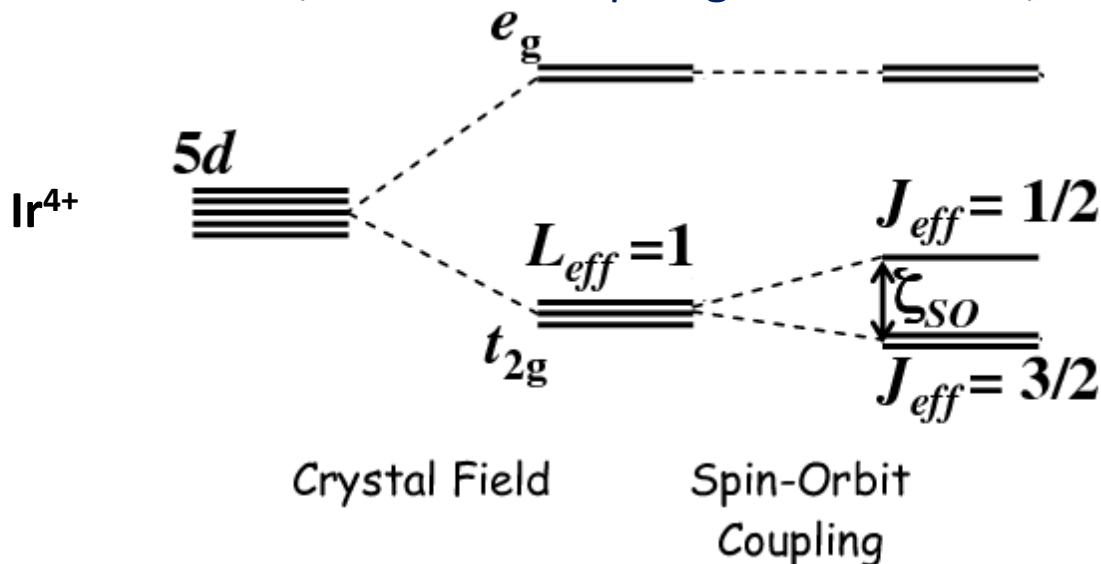
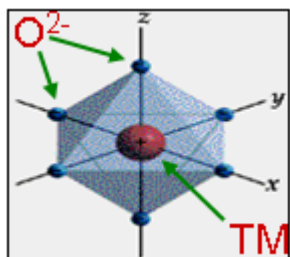
Optical conductivity

DFT calculations

finite-temperature FRG calculations

Introduction

Large spin-orbit coupling in **5d transition-metal oxides** → novel electronic states, e.g. **spin-orbit Mott insulators**, correlated topological insulators, ...



Spin-Orbit Mott Insulator

Heisenberg-Kitaev model

J. Chaloupka, G. Jackeli, G. Khaliullin PRL 2010

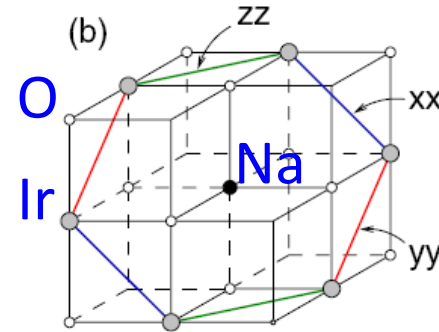
Kitaev model:

$$\begin{array}{l}
 (x) \\
 -S^x S^x \\
 \diagdown \\
 \text{---} -S^z S^z \text{---} (z) \\
 \diagup \\
 -S^y S^y \\
 (y)
 \end{array}$$

exact solution:

spin-liquid with fractional excitations

Direct hopping between NN Ir t_{2g} orbitals \rightarrow Heisenberg interaction

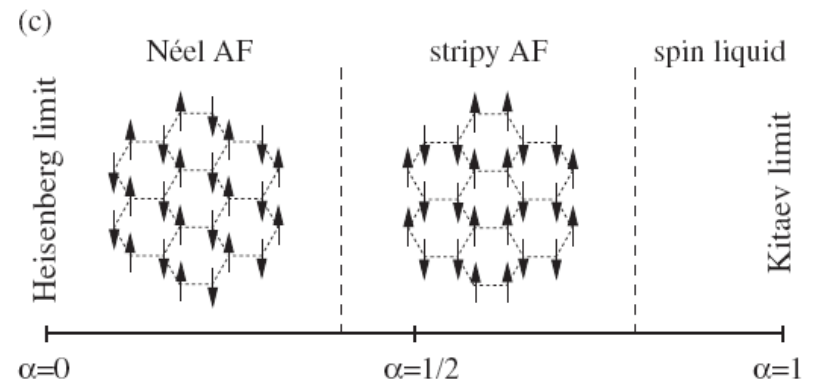


Na_2IrO_3

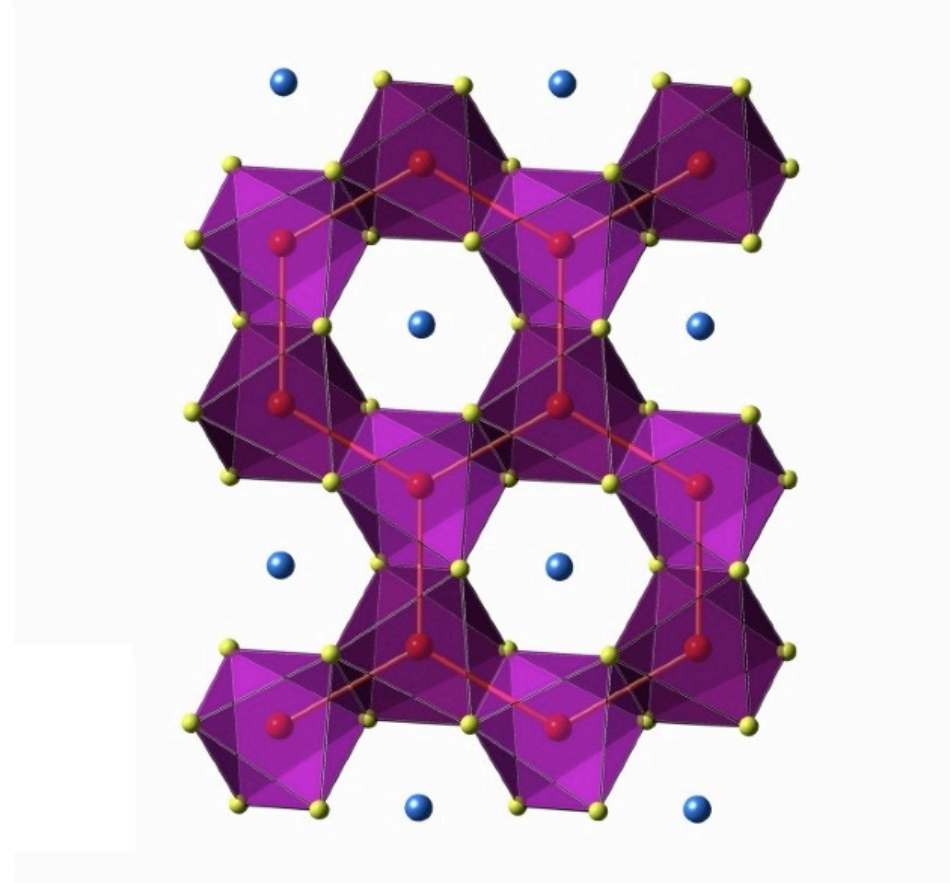
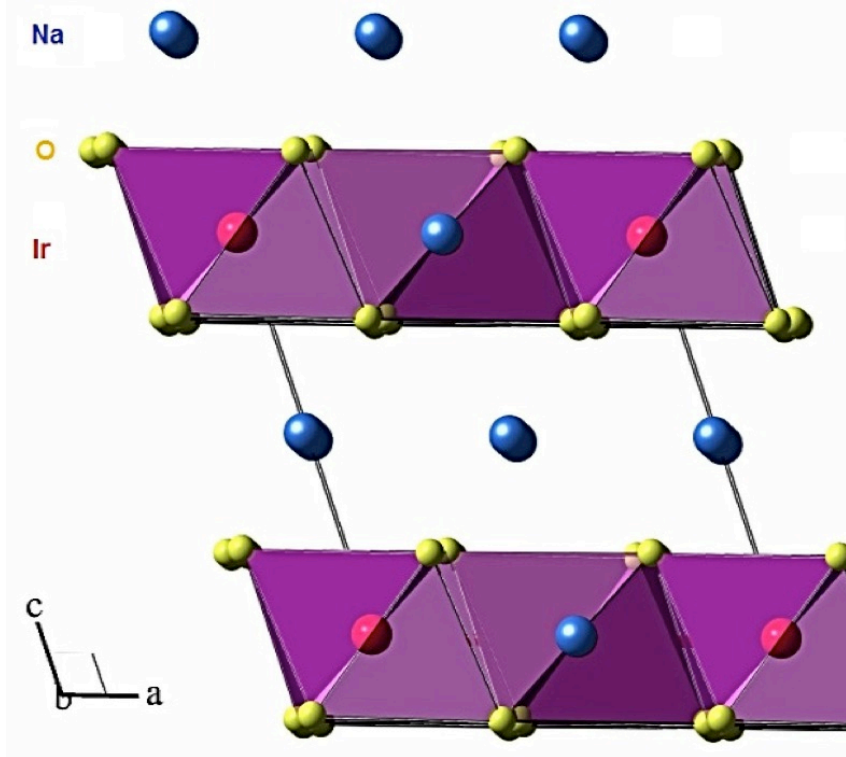
$$\mathcal{H}/J = (1 - \alpha) \sum_{\text{NN}} \mathbf{S}_i \cdot \mathbf{S}_j - 2\alpha \sum_{\text{NN}} S_i^\gamma S_j^\gamma$$

Heisenberg (AF)
unfrustrated

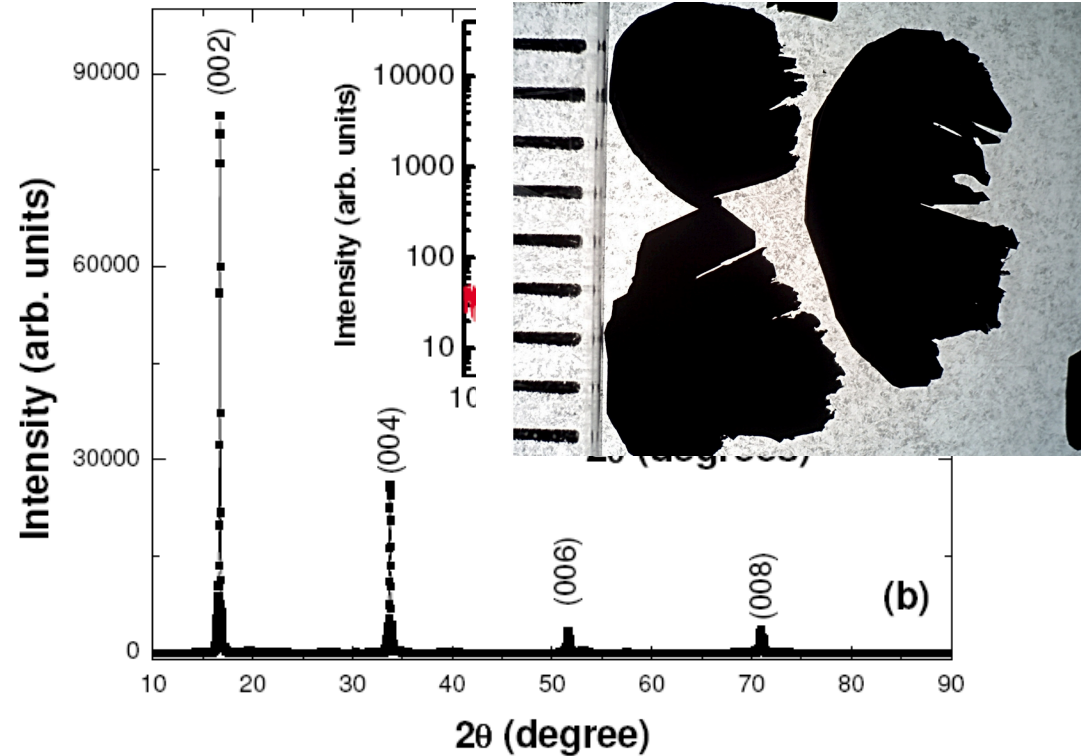
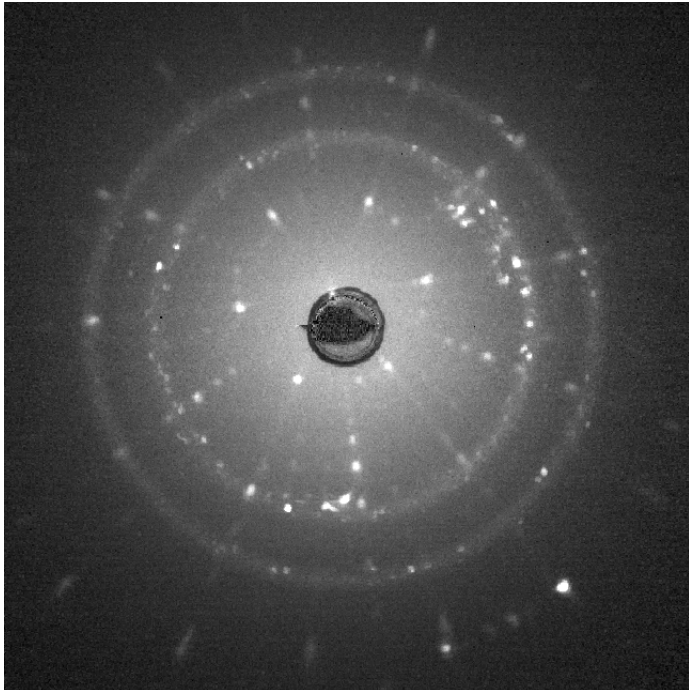
Kitaev (FM)



Structural properties

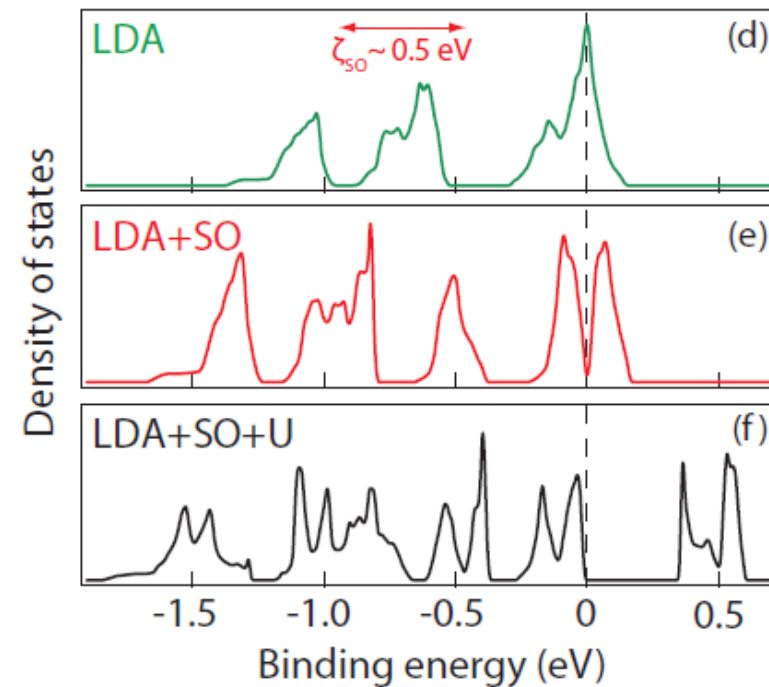
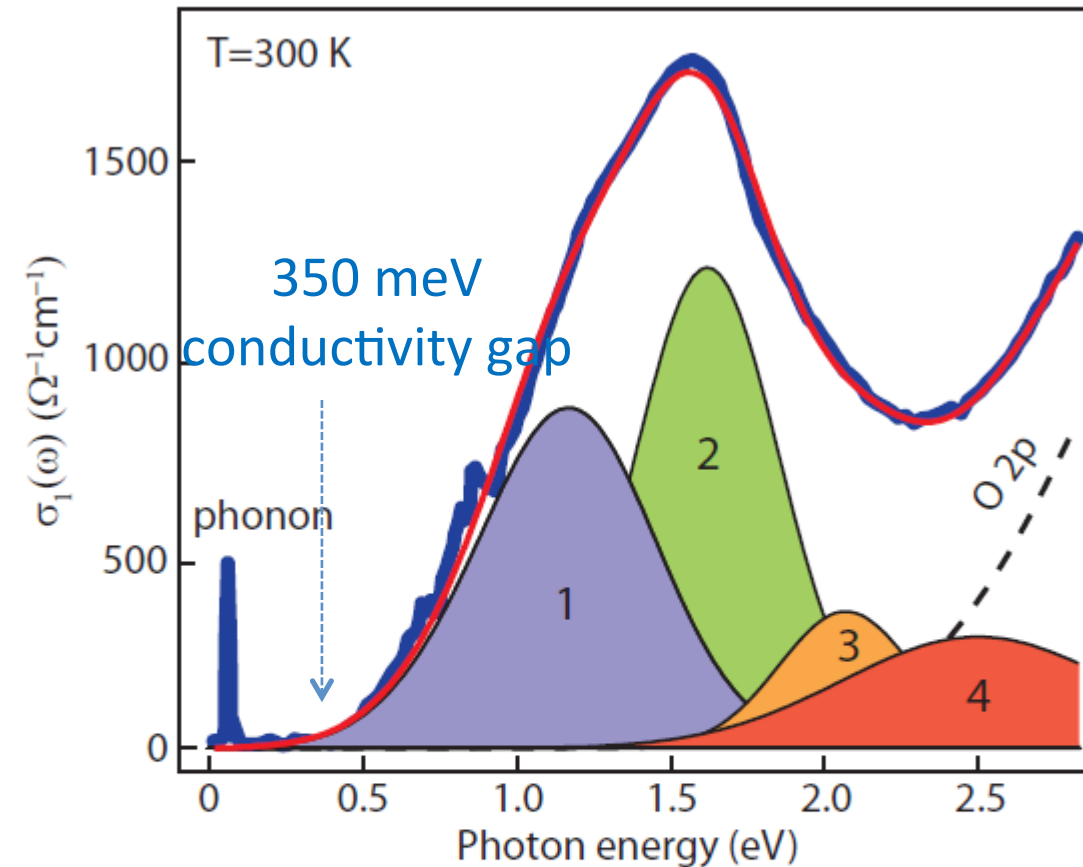


Synthesis of Na_2IrO_3



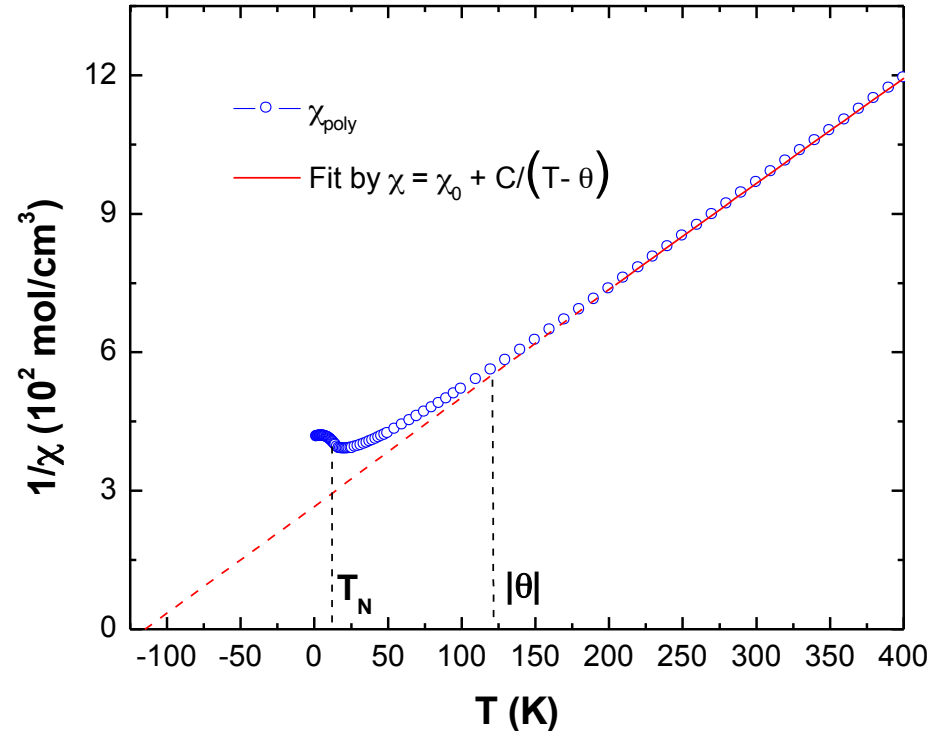
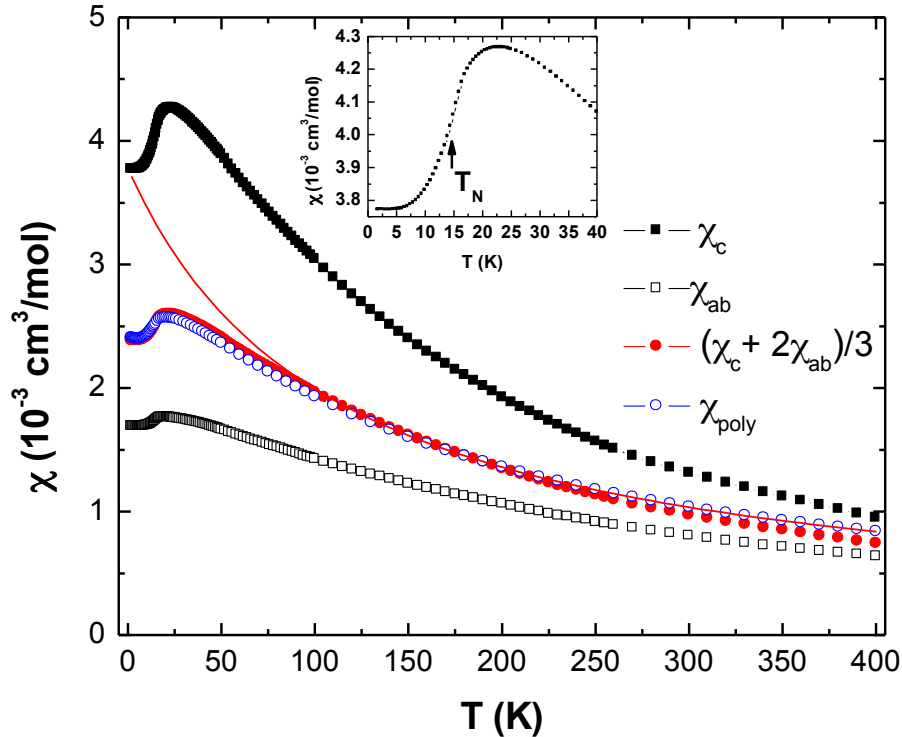
- Polycrystal: solid-state synthesis (900°C) from Na_2CO_3 and IrO_2
- Single crystal ($5 \times 3 \times 0.1 \text{ mm}^3$): Growth $T = 1050^\circ\text{C} - 1150^\circ\text{C}$

Optical spectroscopy



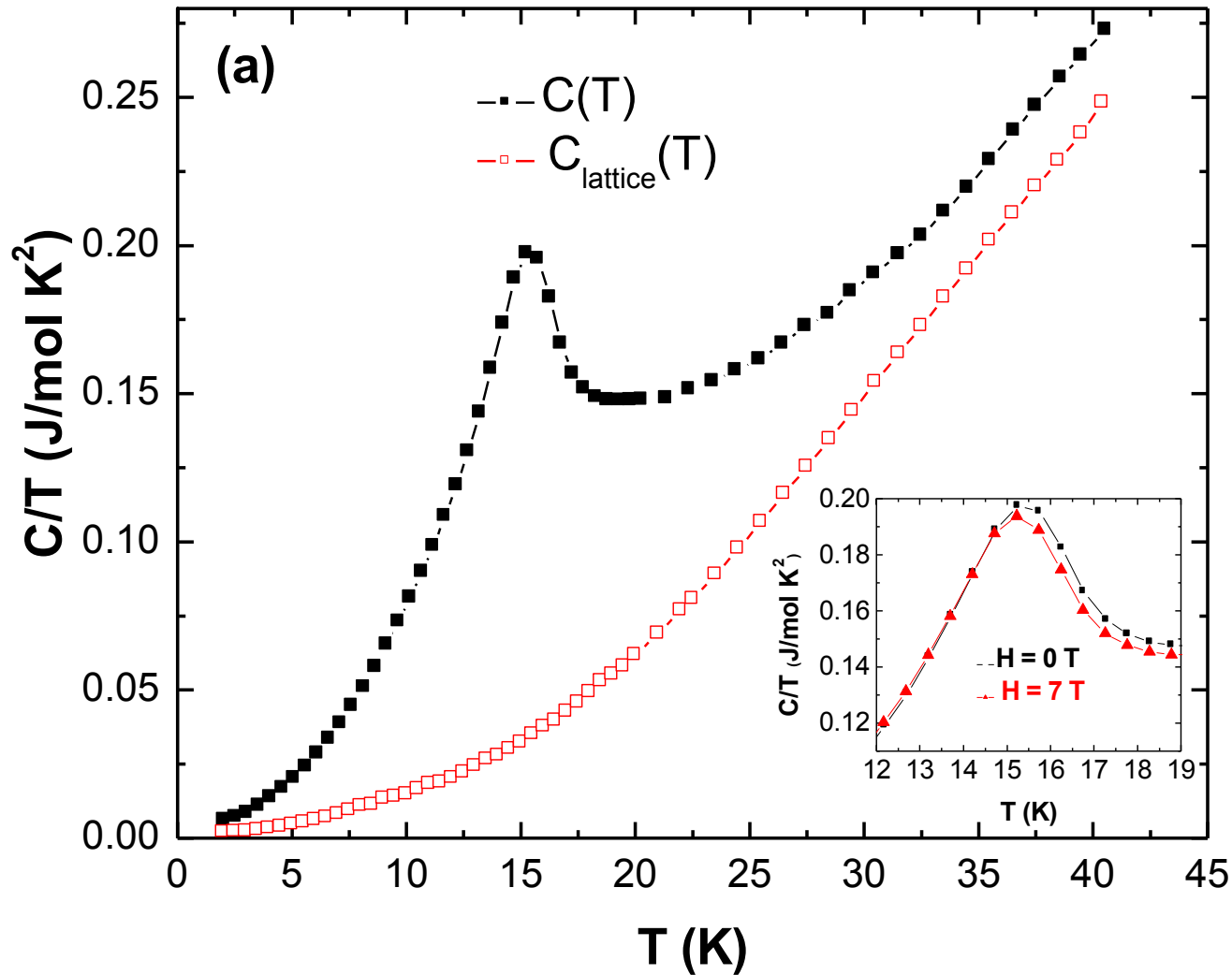
- 4-peak DOS from **trigonal CEF** and **SO coupling**
- Already SO opens gap, perfect fitting by including $U = 3\text{ eV}$ ($J_H = 0.6\text{ eV}$)

Magnetic susceptibility



- CW fit reveals $\mu_{\text{eff}} = 1.81\mu_B$ (assuming $g=2$) $\rightarrow S_{\text{eff}} = \frac{1}{2}$ state
 - χ anisotropy may result from trigonal crystal field (\rightarrow g-factor anisotropy)
 - Weiss temperature $\Theta = -120$ K but $T_N = 15$ K
- \rightarrow **large frustration** ($f = 8$)!

Heat capacity

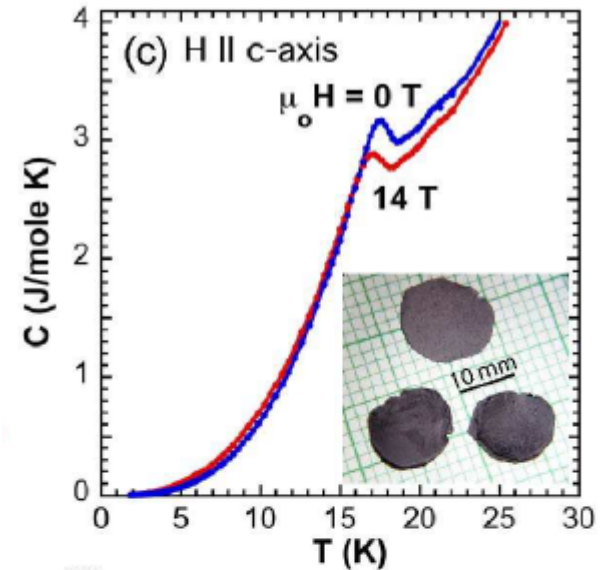
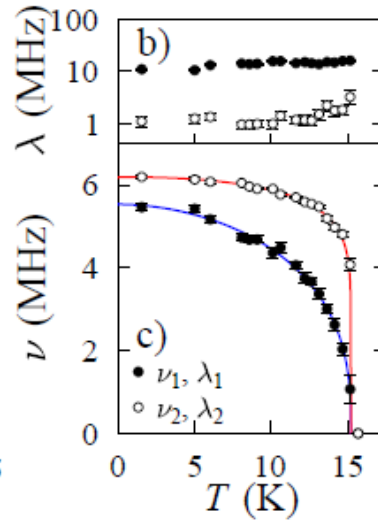
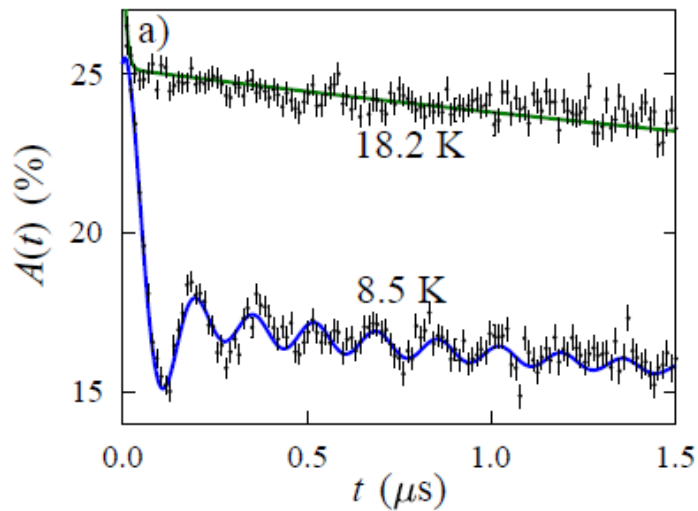


- C shows sharp lambda-like anomaly at $T_N = 15$ K
- Entropy $S(T_N) \approx 20\% R \ln 2$ only

Nature of Magnetic ordering

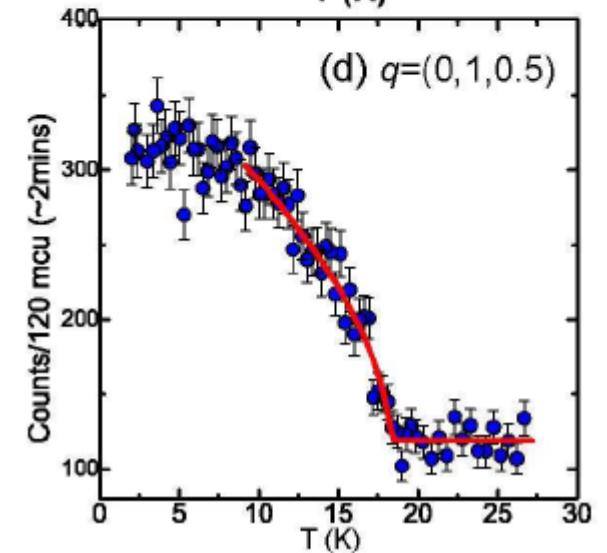
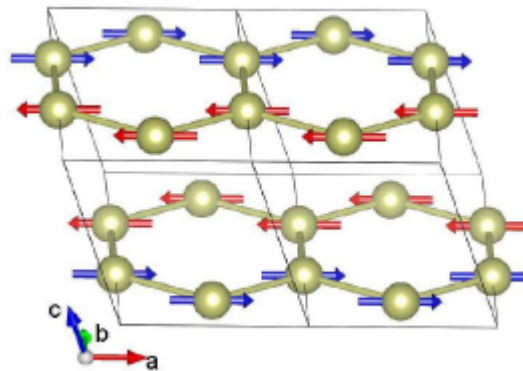
μ SR

S.K. Choi et al., PRL
108 (2012) 127204.



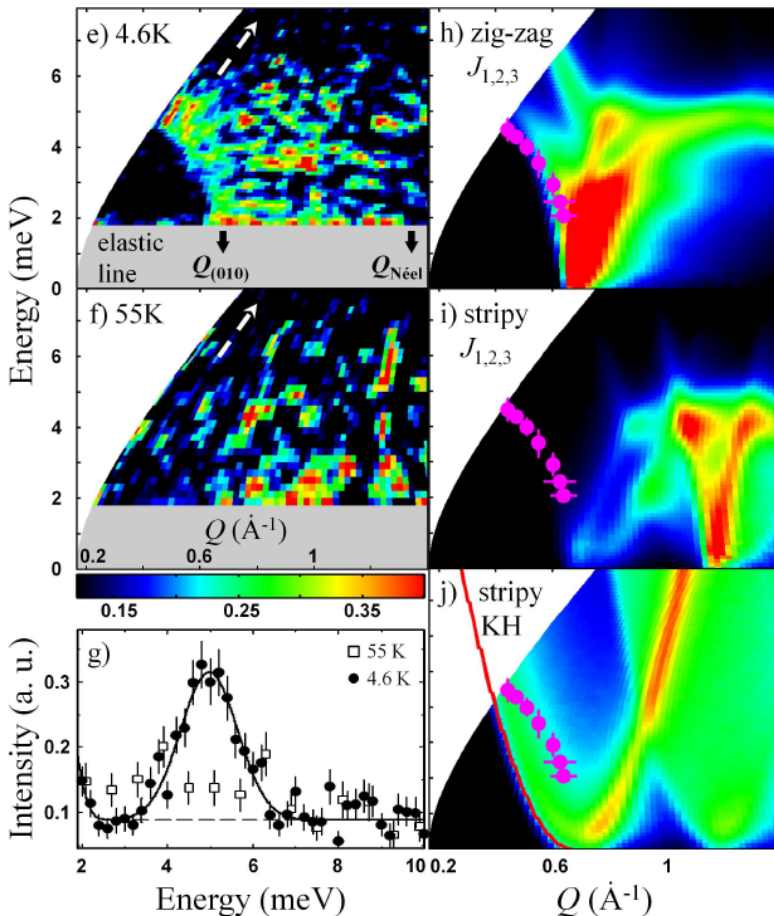
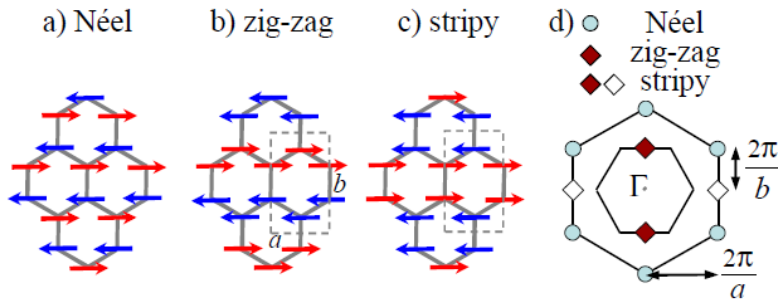
Neutron scattering:

- Zigzag-order AF stacked along c
- Ordered moment : $0.22 \mu_B$



Feng Ye et al. PRB 85 (2012) 180403(R).

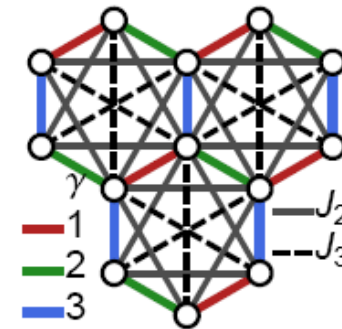
Powder INS: magnetic excitations



S.K. Choi et al. PRL **108**, 127204 (2012)

- Dispersion boundary for inelastic excitations at low Q, incompatible with Néel AF
- Data compatible with calculation for spin-wave dispersion for **zig-zag ordering in $J_1J_2J_3$ model** using $J_1 = 4.35$ meV, $J_2/J_1 = 0.75$, $J_3/J_1 = 0.9$
- Additional Kitaev term $\alpha \leq 0.2$

(I. Kimchi and Y.-Z. You, PRB 2011: **Kitaev-Heisenberg-J2-J3-Model**)



Magnetic excitations: RIXS

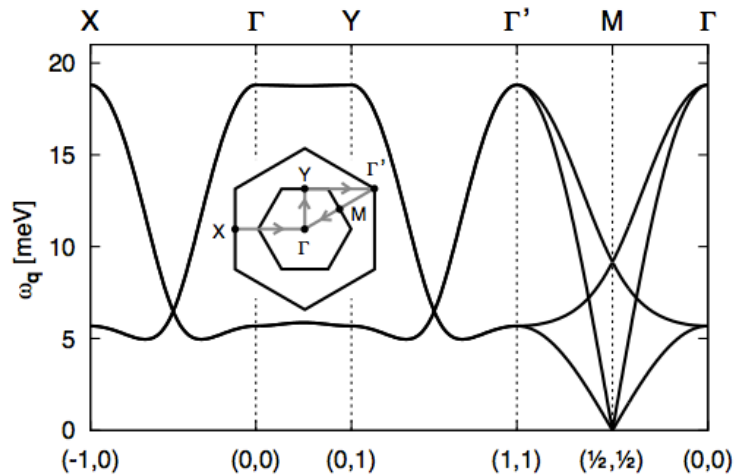
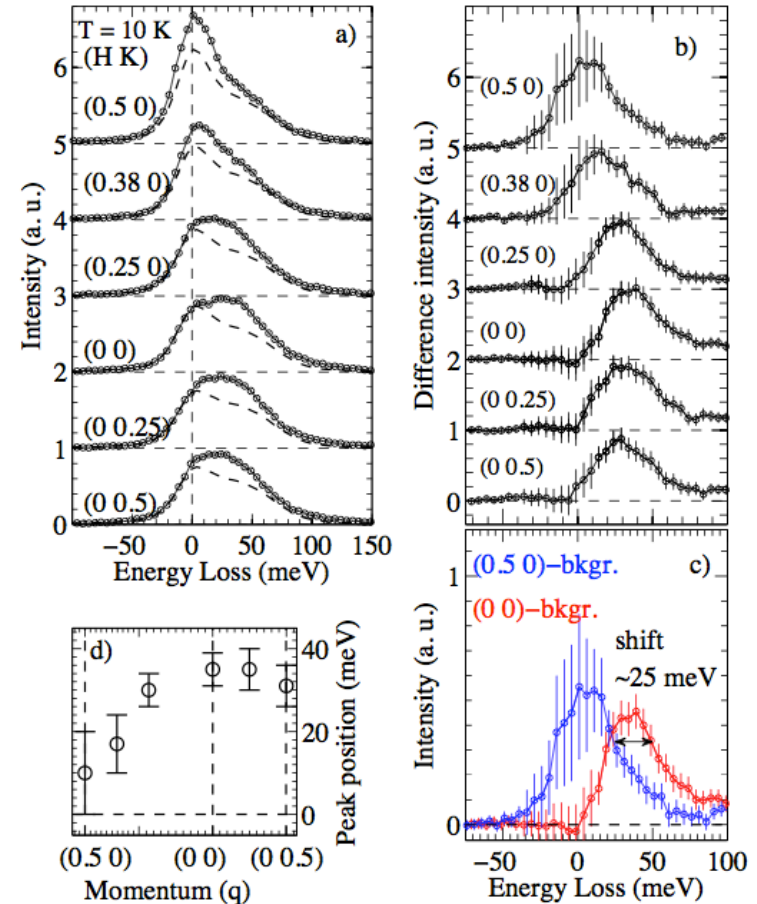


FIG. 3: Magnon spectra in the zigzag phase calculated using Eq. (4) with $(J, K) = (-4.01, 10.45)$ meV. The inset shows the path along the symmetry directions in the reciprocal space; notations of Ref. [4] are used.

[Jiří Chaloupka, George Jackeli, Giniyat Khaliullin](#)

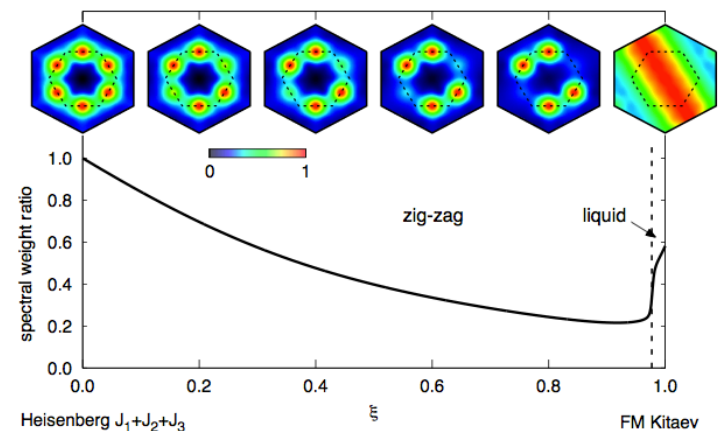
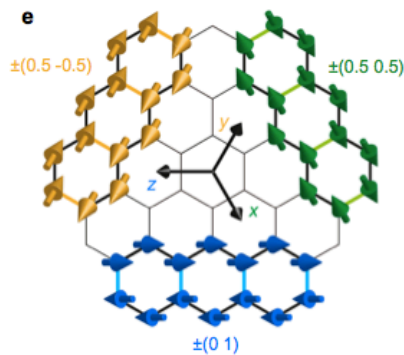
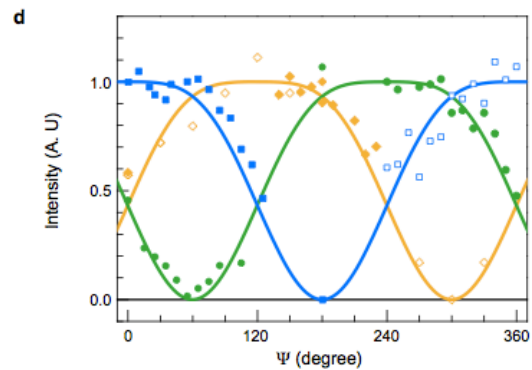
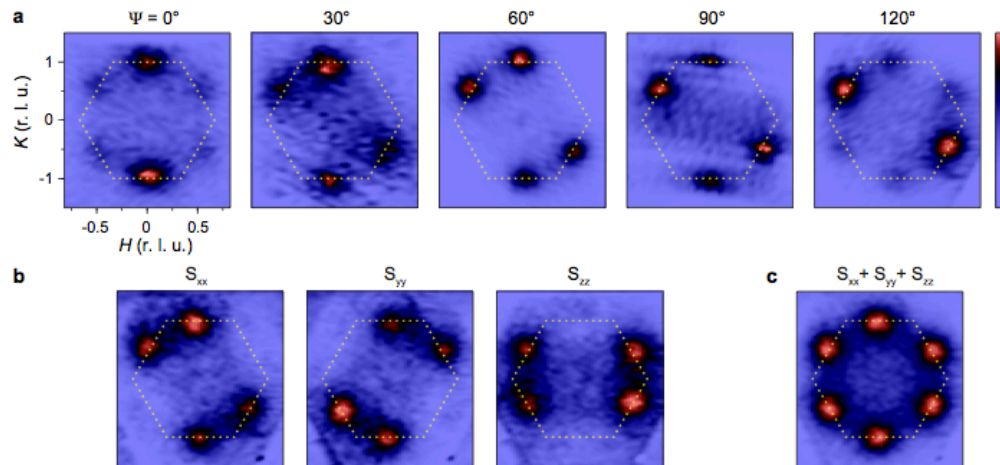
Phys. Rev. Lett. 110, 097204 (2013)



[H. Gretarsson, J. P. Clancy, Yogesh Singh, P. Gegenwart, J. P. Hill, Jungho Kim, M. H. Upton, A. H. Said, D. Casa, T. Gog, Young-June Kim](#)

Phys. Rev. B, 87, 220407 (R) (2013)

Direct Evidence of bond-directional exchange in Na_2IrO_3

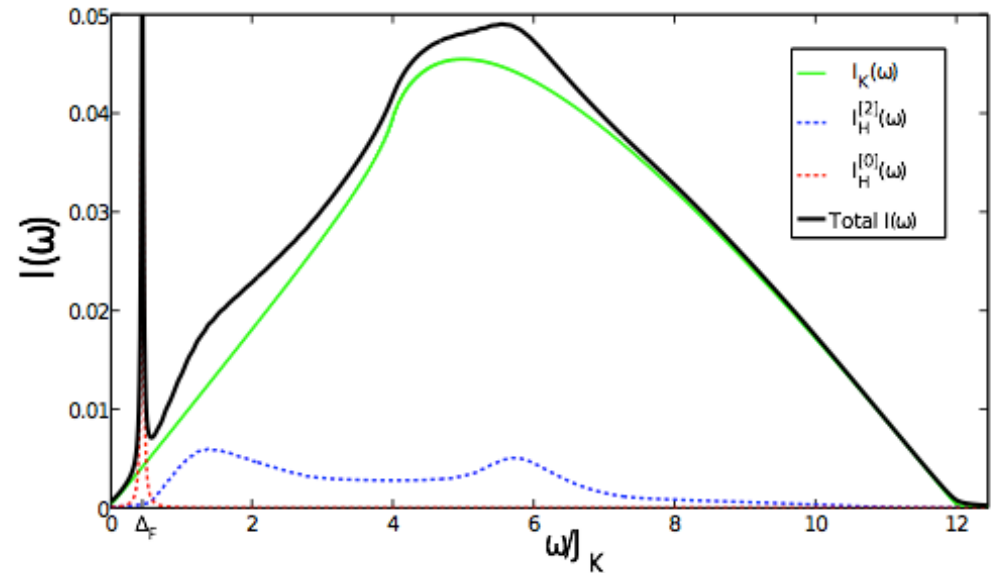


S. H. Chun, BJK, et al. (2015)

Prediction of Raman Response of Kitaev Spin-Liquid in $A_2\text{IrO}_3$

J. Knolle, Gia-Wei Chern, D. L. Kovrizhin, R. Moessner, and N. B. Perkins, PRL (2014)

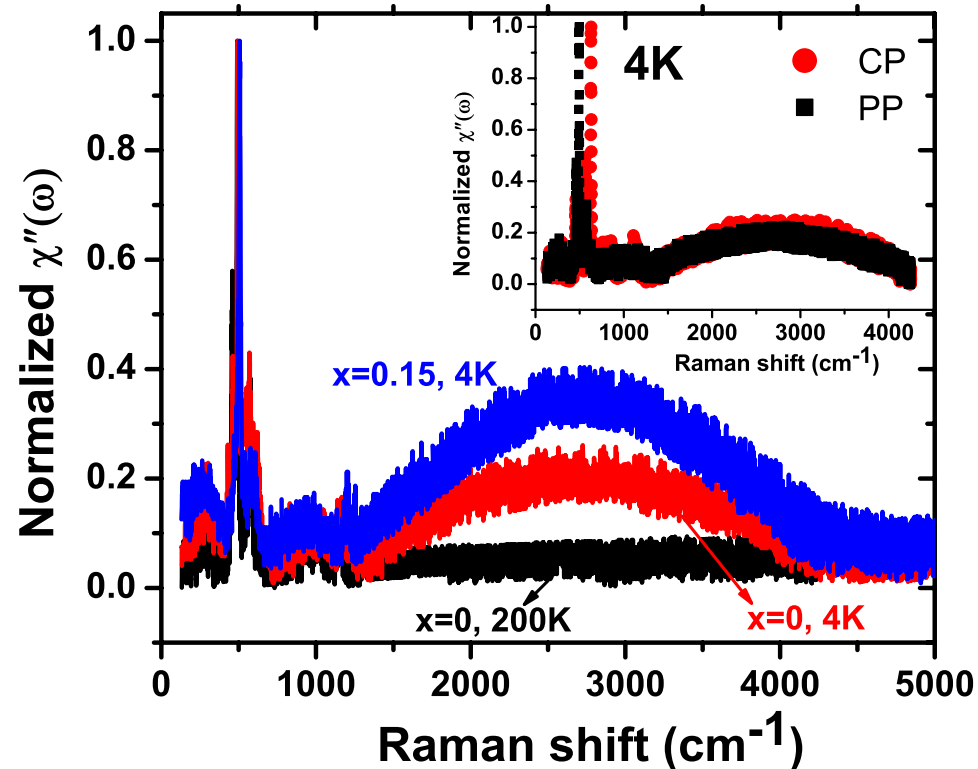
- Assumption: strong Kitaev limit, Heisenberg included as perturbation ($J_H/J_K = 0.1$)
- Kitaev contribution is a Broad Polarization independent band centered at $6J_K$ and band-edge at $12J_K$
- Heisenberg term leads to a sharp spike at $0.45J_K$
- Results expected to be robust to inclusion of other Heisenberg-like terms provided they are small.



Experimental Raman response of Na_2IrO_3

S.N. Gupta, D. K. Mishra, Kavita Mehlawat, A. Balodhi, D. V. S. Muthu, Yogesh Singh, and A. K. Sood, [arXiv:1408.2239](https://arxiv.org/abs/1408.2239) (2014)

- Observe a broad continuous Raman band centered at high energies
- The band is polarization independent
- $J_K = 60$ meV
- Band seen even below T_N



Summary for Na_2IrO_3

- Large frustration, $T_N = 15$ K, magnetic scale ~ 100 meV
- Inelastic Magnetic Scattering has shown dispersion consistent with dominant non-Heisenberg interactions
- Raman scattering shows a quasi-continuous, polarization independent band which is a spin liquid like response
- We estimate $J_K \sim 60$ meV.