

ALPS

Algorithms and Libraries for Physics Simulations

Bela Bauer

Station Q, Santa Barbara



Outline

- **First lecture:**
 - Overview of ALPS, introduction to main concepts
 - Preparation for the tutorial (blackboard)
- **Second lecture:**
 - Hands-on

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Please ask many questions!

The ALPS project

Provide open-source community-backed tools
for the simulation of strongly correlated
systems.

- Replace status quo of individual codes with reliable, tested, efficient and documented community codes relying on common file formats

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1. Standard file formats
2. Libraries
3. Evaluation tools
4. Applications

The ALPS collaboration

Release 2.0:

- Switzerland
 - B. Bauer, L. Gamper, J. Gukelberger, A. Hehn, S. Isakov, P. N. Ma, J. D. Picon, B. Surer, M. Troyer, P. Werner
- United States
 - L. D. Carr, A. Feiguin, J. Freire, D. Koop, P. Mates, E. Gull, E. Santos, V.W. Scarola, C. Silva, M. L. Wall
- Germany
 - S. Fuchs, S. Görtler, L. Pollet, U. Schollwöck, S. Trebst, S. Wessel
- Japan
 - R. Igarashi, H. Matsuo, S. Todo
- Austria
 - H. G. Evertz
- France
 - O. Parcollet
- Poland
 - G. Pawłowski

MPS applications:

- Switzerland
 - M. Dolfi, S. Keller, A. Kosenkov, T. Ewart, A. Kantian, T. Giamarchi, M. Troyer
- United States
 - B. Bauer

Key technologies

- Widely used object-oriented programming languages:
 - Performance-relevant parts implemented in **C++**
 - C++ code uses and follows coding practices of **Standard Library** and **Boost** libraries
 - Data analysis/evaluation code developed in **Python**
 - Extensive use of **NumPy/SciPy** and **Matplotlib** for computations and plotting
- Standard file formats:
 - **HDF5** (Hierarchical Data Format v5) binary format for efficient processing of large data sets
 - **XML** for human-readable input/output

Goals

- Provide **efficient implementation of standard algorithms** for solving physics problems, as well as testing and benchmarking new methods
- Facilitate **reproducibility** by providing **standardized file formats** and appropriate **provenance** mechanisms
- **Simplify** development of reliable simulation codes by providing **key libraries**
- Simplify data analysis by providing **powerful analysis tools**

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 - Local and cluster update algorithms for spin systems [spinmc]

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 - DMRG [dmrg]
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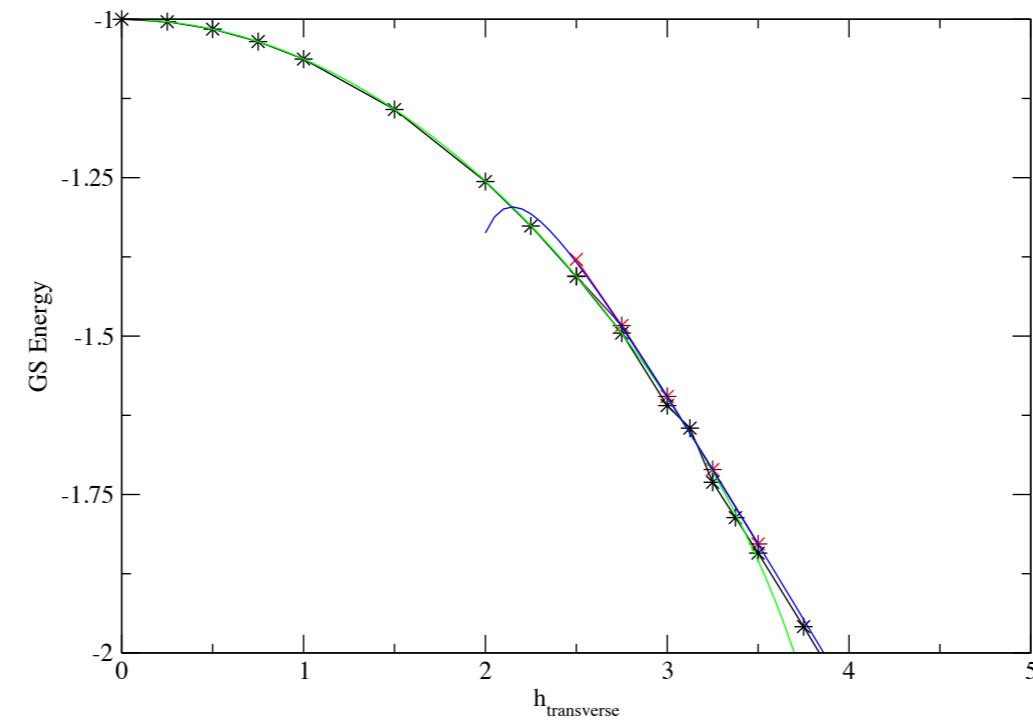
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Reproducibility

- So you ran a simulation, stored the result in a text file and made a figure:

```
My-Mac:~ bela$ tail -n 4 /Users/bela/iPEPS/results/iPEPS_BLBQ/run2/M2_P30_s10/measurements.dat
a 0 energy -2.12543
a 1 energy -2.20704
a 2 energy -2.12558
a 3 energy -2.20719
```



- 3 years later, you want to reproduce it for your thesis...
 - Which version of your code did you run?
 - What are the parameters?
 - Was any post-processing applied to the data?

Provenance tracking

Provenance tracking

- Provenance on Wiktionary:
 - 1 Place or source of origin. *Many supermarkets display the **provenance** of their food products.*
 - 2 (*archaeology*) The place and time of origin of some **artifact** or other object. *This spear is of Viking **provenance**.*
 - 3 (*art*) The history of ownership of a work of art *The picture is of royal **provenance**.*
 - 4 (*computing*) The copy history of a piece of data, or the intermediate pieces of data utilized to compute a final data element, as in a database record or web site (data provenance)
 - 5 (*computing*) The execution history of computer processes which were utilized to compute a final piece of data (process provenance)

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 - Who created this result, and when?
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 - What parameters were passed to the application?
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- **Make data & provenance accessible** to publishers, referees & readers
 - Reproducible papers

Good provenance habits

Whatever software you use,
practice good provenance habits!

- Use **descriptive** input formats, and well-defined & documented output formats
- **Store** input & output together
- **Don't hard-code** simulation parameters
- Use **versioning** software (SVN, Git) to keep track of source code revisions & record which version was used to perform simulations
- Keep track of **post-processing** steps
 - Perform all post-processing in **scripts rather than interactive tools**
 - **Store** post-processing information together with figure files and manuscripts

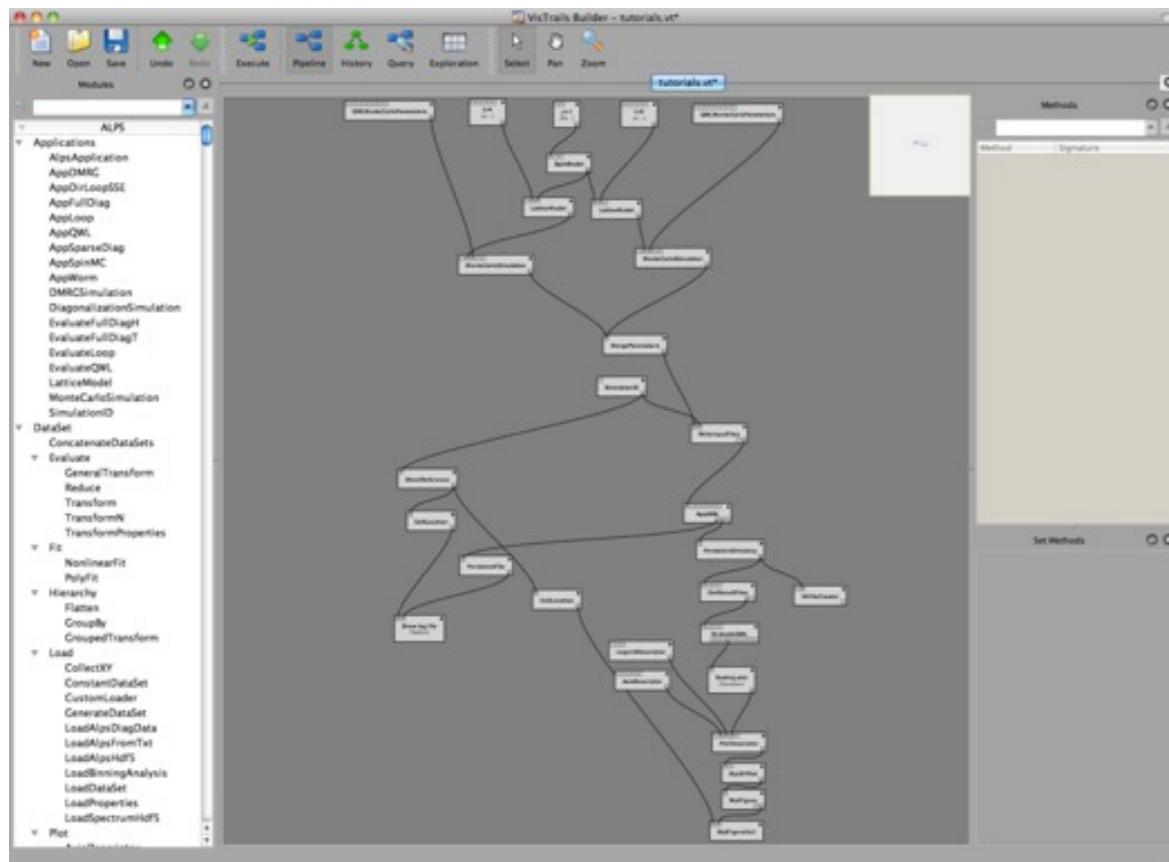
Advanced provenance tools

- VisTrails: Visual workflow and provenance management

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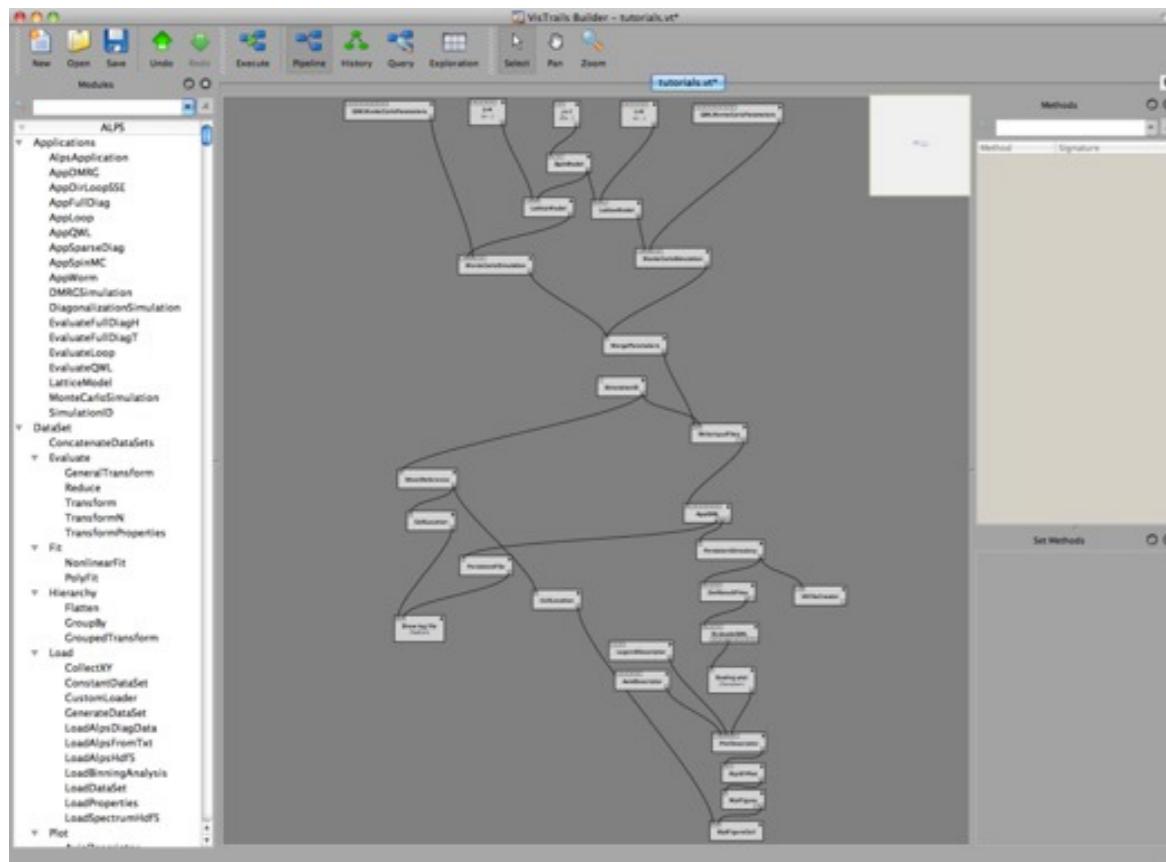
Visual workflows



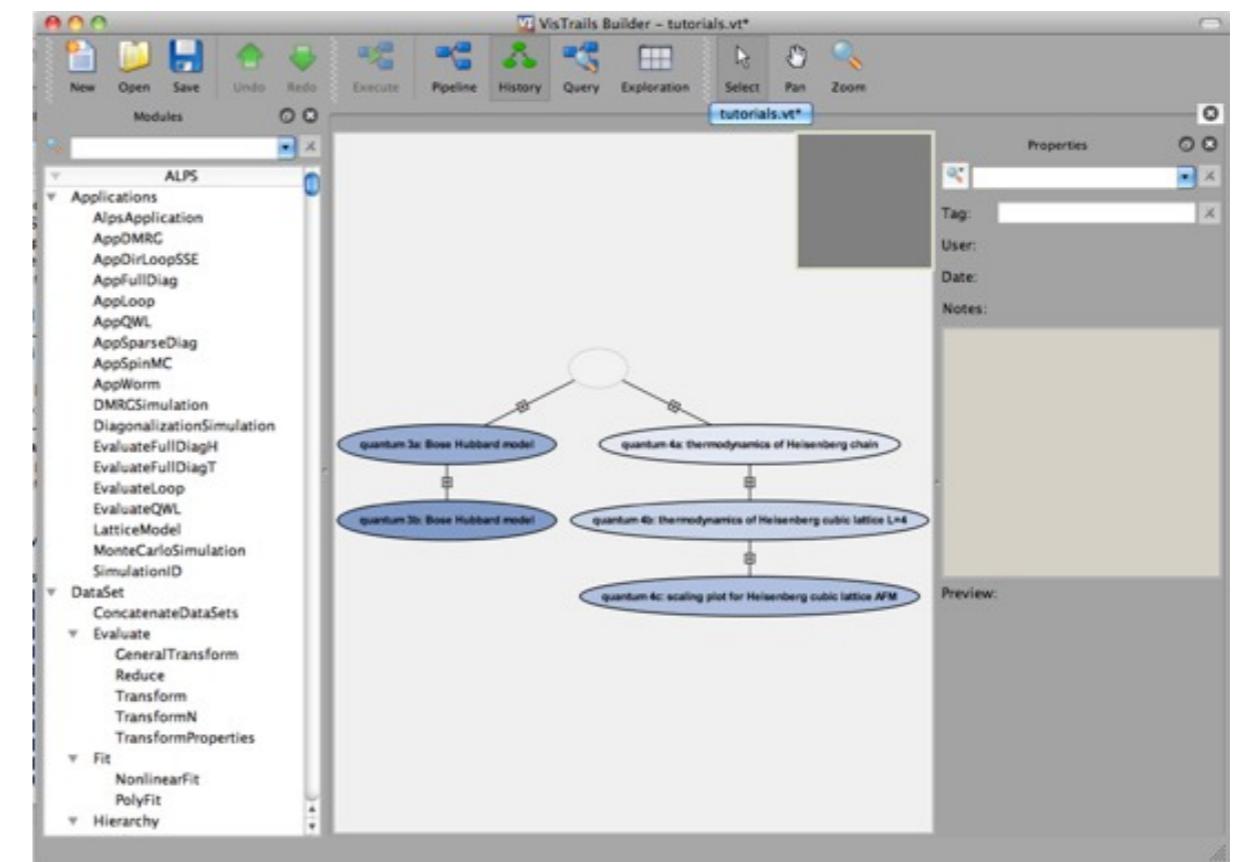
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- VisTrails: Visual workflow and provenance management

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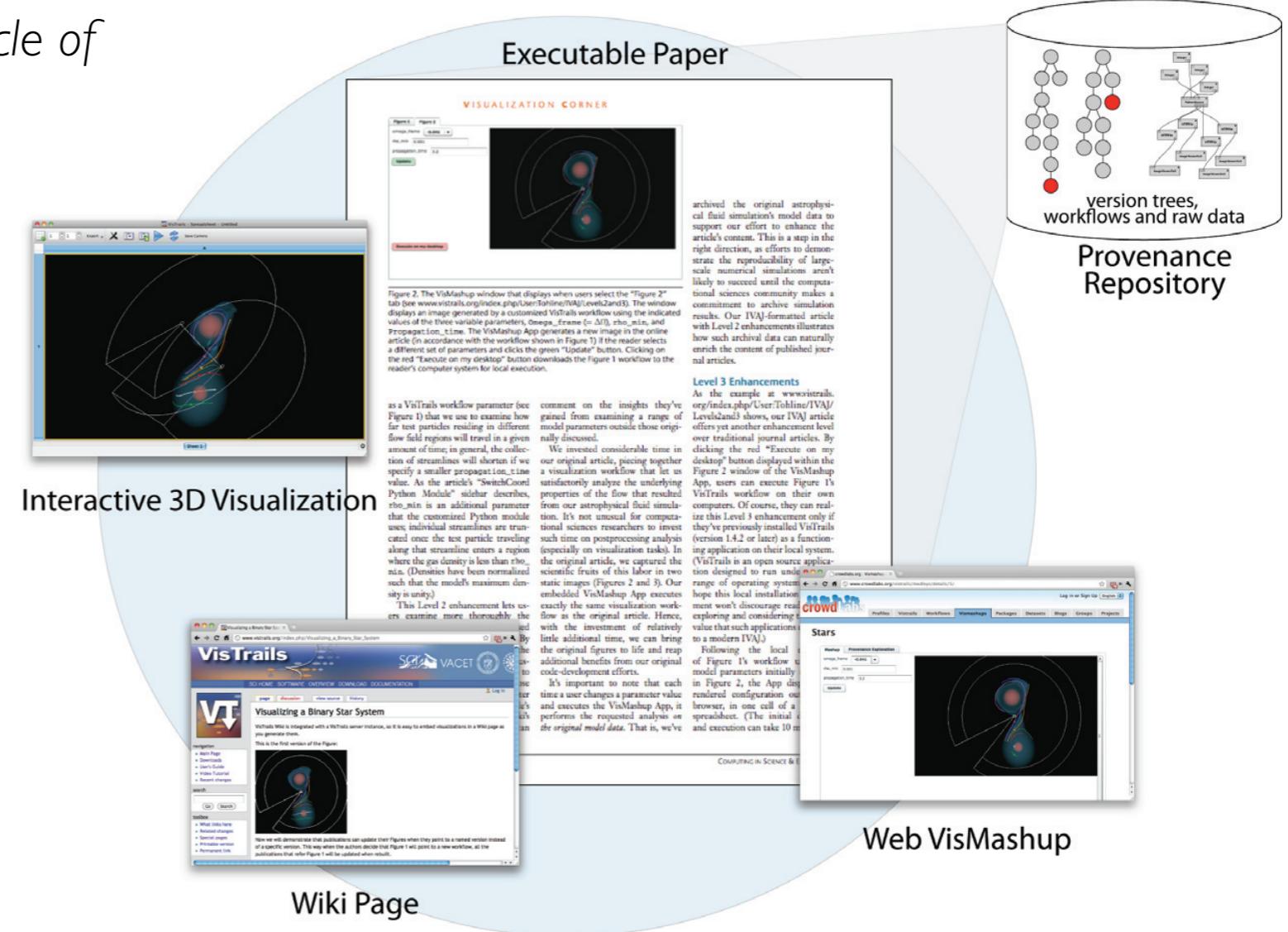


Exploration history



Executable papers

D. Koop et al, A Provenance-Based Infrastructure to Support the Life Cycle of Executable Papers, ICCS 2011



Executable papers

The screenshot shows a detailed view of an arXiv.org article page. At the top, the URL 'arXiv.org > cond-mat > arXiv:1101.2646' is visible. Below it, the article title 'The ALPS project release 2.0: Open source software for strongly correlated systems' is displayed. The authors listed are B. Bauer, L. D. Carr, H.G. Evertz, A. Feiguin, J. Freire, S. Fuchs, L. Gamper, J. Gukelberger, E. Gull, S. Guertler, A. Hehn, R. Igarashi, S.V. Isakov, D. Koop, P.N. Ma, P. Mates, H. Matsuo, O. Parcollet, G. Pawłowski, J.D. Picon, L. Pollet, E. Santos, V.W. Scarola, U. Schollwöck, C. Silva, B. Surer, S. Todo, S. Trebst, M. Troyer, M.L. Wall, P. Werner, S. Wessel. The submission date is 13 Jan 2011 (v1), last revised 23 May 2011 (this version, v4).

The main text describes the ALPS project, which is an open source software for simulating strongly correlated quantum lattice models. It includes details on XML and HDF5 data formats, libraries for code development, evaluation tools, and simulation programs. The software supports various numerical simulations like QMC, DMRG, and TEBD.

On the right side of the page, there's a sidebar titled 'Download:' with options for PDF and other formats. Below that is a section for 'Ancillary files' containing three file links. This section is circled in red. Further down the sidebar are sections for 'Change to browse by:', 'References & Citations', and 'Bookmark'.

Comments: 18 pages + 4 appendices, 7 figures, 12 code examples, 2 tables
Subjects: Strongly Correlated Electrons (cond-mat.str-el); Computational Physics (physics.comp-ph)
Journal reference: J. Stat. Mech. (2011) P05001
DOI: 10.1088/1742-5468/2011/05/P05001
Cite as: arXiv:1101.2646 [cond-mat.str-el]
(or arXiv:1101.2646v4 [cond-mat.str-el] for this version)

Executable papers

Journal of Statistical Mechanics: Theory and Experiment > Volume 2011 > May 2011

B Bauer et al *J. Stat. Mech.* (2011) P05001 doi:10.1088/1742-5468/2011/05/P05001

The ALPS project release 2.0: open source software for strongly correlated systems

B Bauer¹, L D Carr², H G Evertz³, A Feiguin⁴, J Freire⁵, S Fuchs⁶, L Gamper¹, J Gukelberger¹, E Gull⁷, S Guertler⁸, A Hehn¹, R Igarashi^{9,10}, S V Isakov¹, D Koop⁵, P N Ma¹, P Mates^{1,5}, H Matsuo¹¹, O Parcollet¹², G Pawłowski¹³, J D Picon¹⁴, L Pollet^{1,15}, E Santos⁵, V W Scarola¹⁶, U Schollwöck¹⁷, C Silva⁵, B Surer¹, S Todo^{10,11}, S Trebst¹⁸, M Troyer^{1,21}, M L Wall², P Werner¹ and S Wessel^{19,20}

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Abstract

References

Cited By

Figures

Tables

Supplementary Data



7e766f827f1bad8c8df574a0cc6135ce.vtl (45 kB file)

VisTrails file used to create figures 1 and 2.

Executable papers

[Journal of Statistical Mechanics: Theory and Experiment > Volume 2011 > May 2011](#)

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[Abstract](#) [References](#) [Cited By](#) [Figures](#) [Tables](#) [Supplementary Data](#)

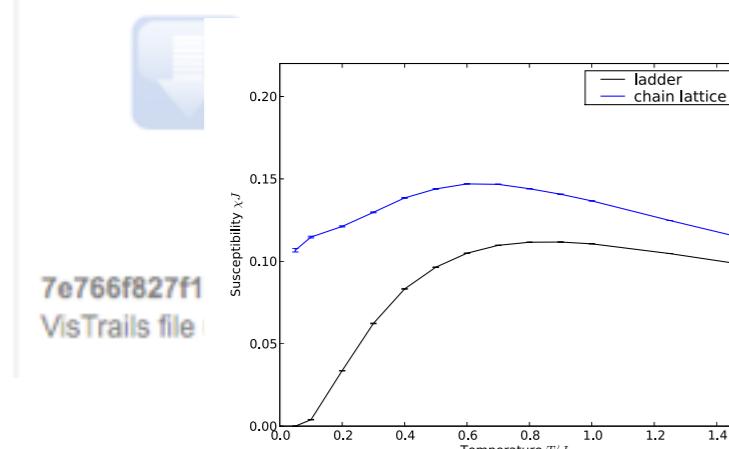


Figure 1. A figure produced by an ALPS VisTrails workflow: the uniform susceptibility of the Heisenberg chain and ladder. Clicking the figure retrieves the workflow used to create it. Opening that workflow on a machine with VisTrails and ALPS installed lets the reader execute the full calculation.

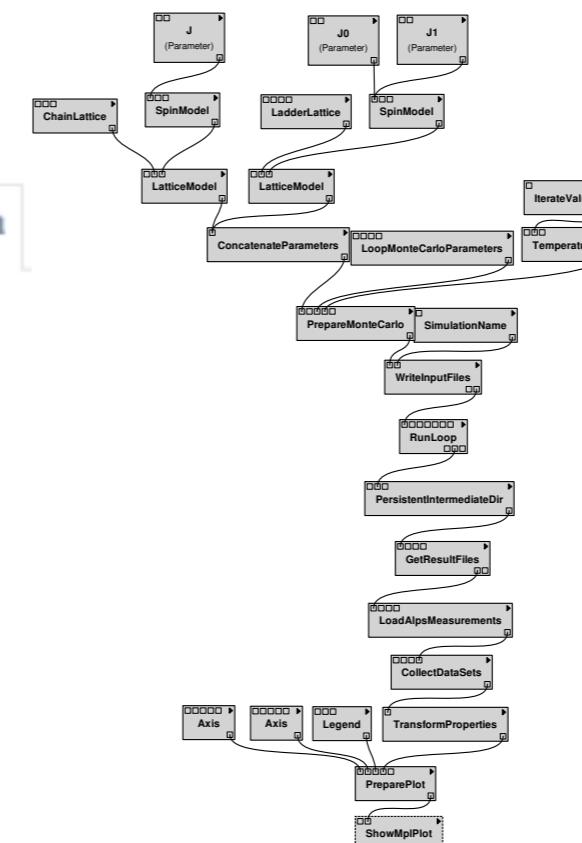
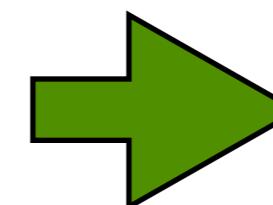


Figure 2. The workflow that created Fig. 1. The workflow image has been created by VisTrails for the specific workflow used to create the exact version shown in the figure. Clicking the figure retrieves the workflow.

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ALPS Libraries

- ALPS **scheduler**: Easy and highly efficient MPI parallelization of Monte Carlo codes
- **Observables**: Efficient accumulation of MC measurement data using MPI, scalable to 1000's of nodes
- **Model & lattice** library: Descriptive input parameters for local Hamiltonians
- **Parameters**: Input from XML, plain-text and command line
- **HDF5**: Powerful C++ and Python interfaces to HDF5 library

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Many of these can be used independently!

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- Centered around **DataSet** structure:

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import pyalps
help(pyalps.DataSet)

class DataSet(ResultProperties)
    | The DataSet class stores a set of data, usually in XY format, along with all the properties
    | describing the data, such as input parameters to the simulation etc.
    |
    | Members are:
    | * x, y - These contain the data and are expected to come as lists of Numpy arrays
    |           by many functions operating on DataSets. However, for user-supplied functions,
    |           other ways of representing data may be used.
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 - Create X vs Y plots (**pyalps.collectXY()**)

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 - Load data from XML or HDF5 into lists of **DataSet**s
 - Create X vs Y plots (`pyalps.collectXY()`)
- **Will be used extensively in Tutorials!**

Setting up ALPS simulations

Lattice

```
<LATTICE name="chain lattice" dimension="1">
  <PARAMETER name="a" default="1"/>
  <BASIS><VECTOR>a</VECTOR></BASIS>
</LATTICE>
```

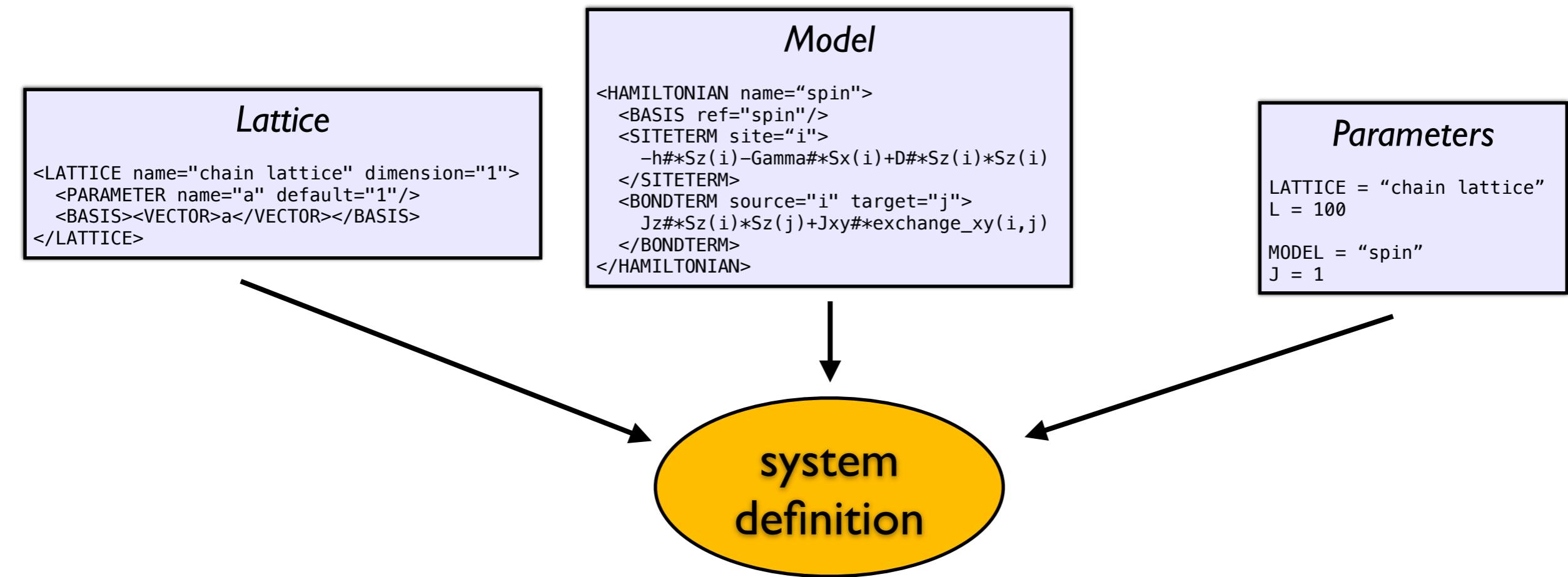
Model

```
<HAMILTONIAN name="spin">
  <BASIS ref="spin"/>
  <SITETERM site="i">
    -h##*Sz(i)-Gamma##*Sx(i)+D##*Sz(i)*Sz(i)
  </SITETERM>
  <BONDTERM source="i" target="j">
    Jz##*Sz(i)*Sz(j)+Jxy##*exchange_xy(i,j)
  </BONDTERM>
</HAMILTONIAN>
```

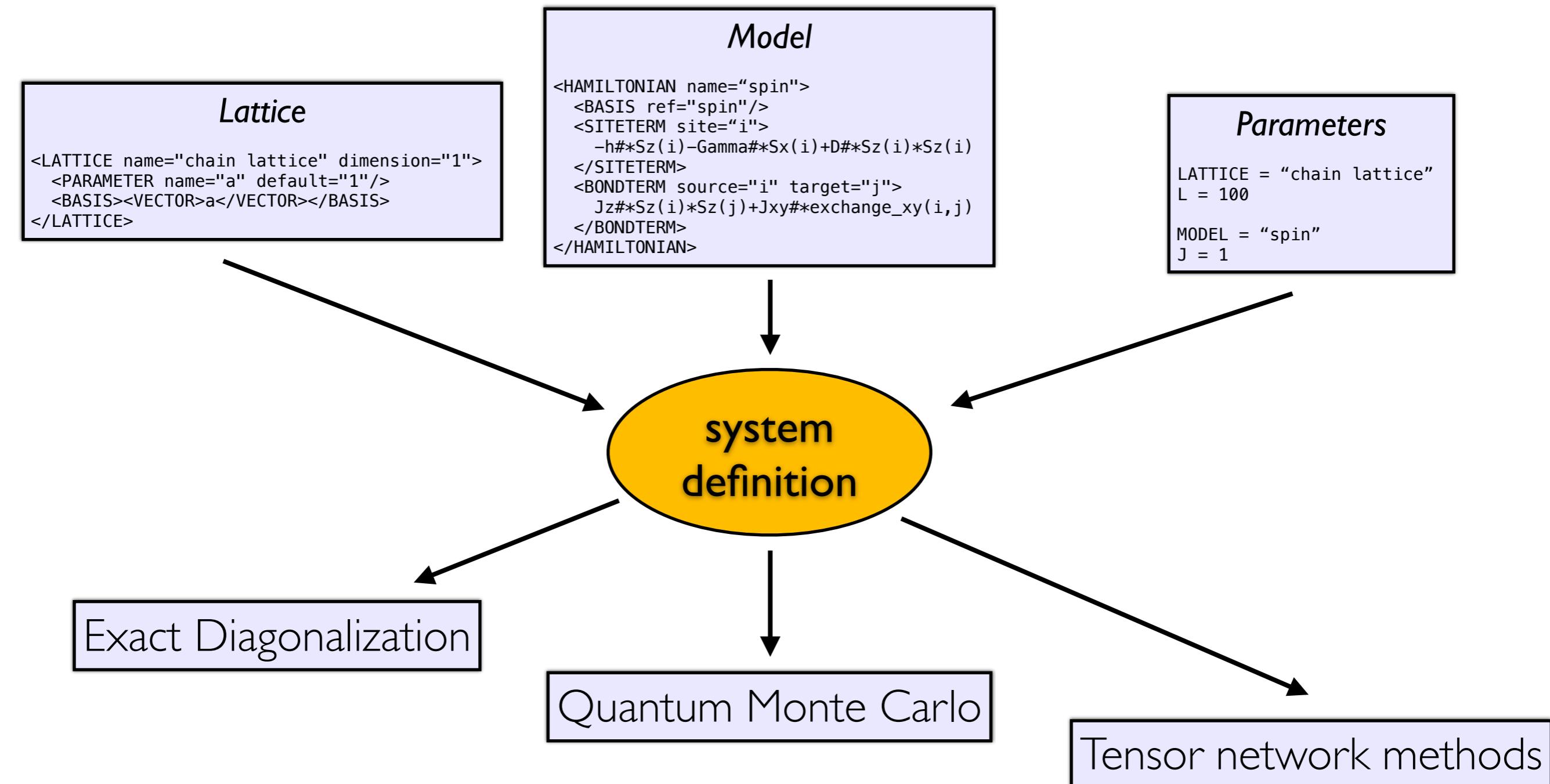
Parameters

```
LATTICE = "chain lattice"
L = 100
MODEL = "spin"
J = 1
```

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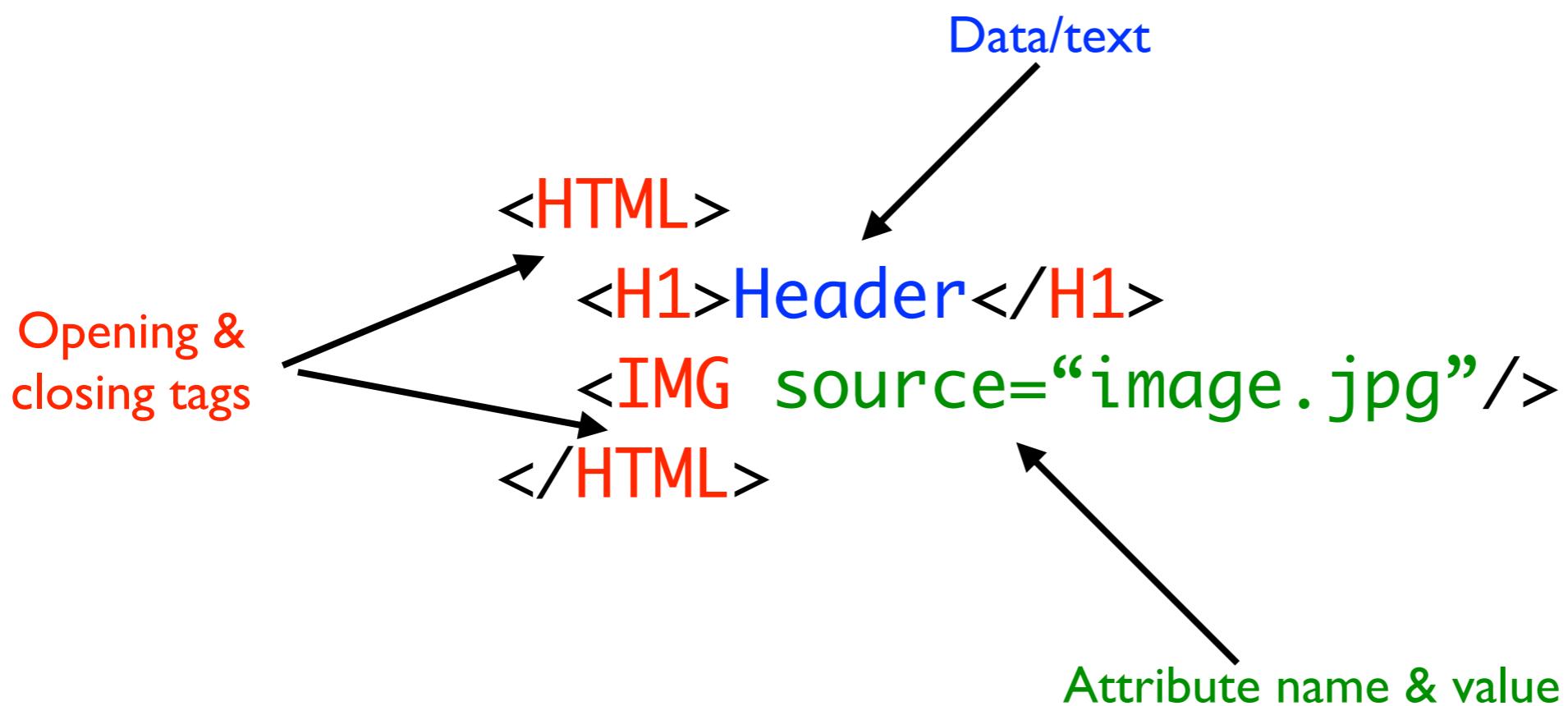


XML files

- Markup language: Text/data marked with tags
- Human and machine readable
- Example: HTML

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Lattice library

Lattice

```
{<LATTICE name="chain lattice" dimension="1">
  <PARAMETER name="a" default="1"/>
  <BASIS><VECTOR>a</VECTOR></BASIS>
  <RECIPROCALBASIS><VECTOR>2*pi/a</VECTOR></RECIPROCALBASIS>
</LATTICE>

<UNITCELL name="simple1d" dimension="1">
  <VERTEX/>
  <EDGE>
    <SOURCE vertex="1" offset="0"/>
    <TARGET vertex="1" offset="1"/>
  </EDGE>
</UNITCELL>

<LATTICEGRAPH name = "chain lattice">
  <FINITELATTICE>
    <LATTICE ref="chain lattice"/>
    <EXTENT dimension="1" size ="L"/>
    <BOUNDARY type="periodic"/>
  </FINITELATTICE>
  <UNITCELL ref="simple1d"/>
</LATTICEGRAPH>
```

Lattice library

Lattice



Unit cell

```
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</UNITCELL>

<LATTICEGRAPH name = "chain lattice">
  <FINITELATTICE>
    <LATTICE ref="chain lattice"/>
    <EXTENT dimension="1" size ="L"/>
    <BOUNDARY type="periodic"/>
  </FINITELATTICE>
  <UNITCELL ref="simple1d"/>
</LATTICEGRAPH>
```

- One vertex
- One edge

Lattice library



Lattice library – Example 2

```
<LATTICE name="square lattice" dimension="2">
  <PARAMETER name="a" default="1"/>
  <BASIS><VECTOR>a 0</VECTOR><VECTOR>0 a</VECTOR></BASIS>
  <RECIPROCALBASIS><VECTOR>2*pi/a 0</VECTOR><VECTOR>0 2*pi/a</VECTOR></RECIPROCALBASIS>
</LATTICE>

<UNITCELL name="simple2d" dimension="2">
  <VERTEX/>
  <EDGE><SOURCE vertex="1" offset="0 0"/><TARGET vertex="1" offset="0 1"/></EDGE>
  <EDGE><SOURCE vertex="1" offset="0 0"/><TARGET vertex="1" offset="1 0"/></EDGE>
</UNITCELL>

<LATTICEGRAPH name = "square lattice">
  <FINITELATTICE>
    <LATTICE ref="square lattice"/>
    <PARAMETER name="W" default="L"/>
    <EXTENT dimension="1" size="L"/>
    <EXTENT dimension="2" size="W"/>
    <BOUNDARY type="periodic"/>
  </FINITELATTICE>
  <UNITCELL ref="simple2d"/>
</LATTICEGRAPH>
```

Lattice library – Example 2

```
<LATTICE name="square lattice" dimension="2">
  <PARAMETER name="a" default="1"/>
  <BASIS><VECTOR>a 0</VECTOR><VECTOR>0 a</VECTOR></BASIS>
  <RECIPROCALBASIS><VECTOR>2*pi/a 0</VECTOR><VECTOR>0 2*pi/a</VECTOR></RECIPROCALBASIS>
</LATTICE>

<UNITCELL name="simple2d" dimension="2">
  <VERTEX/>
  <EDGE><SOURCE vertex="1" offset="0 0"/><TARGET vertex="1" offset="0 1"/></EDGE>
  <EDGE><SOURCE vertex="1" offset="0 0"/><TARGET vertex="1" offset="1 0"/></EDGE>
</UNITCELL>
```

- One vertex
- Two edges


```
<LATTICEGRAPH name = "square lattice">
  <FINITELATTICE>
    <LATTICE ref="square lattice"/>
    <PARAMETER name="W" default="L"/>
    <EXTENT dimension="1" size="L"/>
    <EXTENT dimension="2" size="W"/>
    <BOUNDARY type="periodic"/>
  </FINITELATTICE>
  <UNITCELL ref="simple2d"/>
</LATTICEGRAPH>
```

- Two sizes, L and W
- Periodic boundary conditions in both

Lattice library – Graph example

```
<GRAPH name="triangle" vertices="3">
  <EDGE type="0" source="1" target="2"/>
  <EDGE type="0" source="2" target="3"/>
  <EDGE type="0" source="3" target="1"/>
</GRAPH>
```

Lattice library – Graph example

```
<GRAPH name="triangle" vertices="3">
  <EDGE type="0" source="1" target="2"/>
  <EDGE type="0" source="2" target="3"/>
  <EDGE type="0" source="3" target="1"/>
</GRAPH>
```

- See **ALPS/lib/xml/lattices.xml**
- See <https://alps.comp-phys.org/mediawiki/index.php/Tutorials:LatticeHOWTO>
 - Simple graphs
 - Lattices with unit cells
 - Checking graphs & lattices
- Existing lattice: chain lattice, square, triangular, honeycomb, ...

Model library

Site basis

```
<SITEBASIS name="spin">
  <PARAMETER name="local_S" default="1/2"/>
  <QUANTUMNUMBER name="S" min="local_spin" max="local_spin"/> |S, Sz

$|S, S^z\rangle = \sqrt{S(S+1) - S^z(S^z+1)}|S, S^z + 1\rangle$   
 $S^-|S, S^z\rangle = \sqrt{S(S+1) - S^z(S^z-1)}|S, S^z - 1\rangle$   
 $S^z|S, S^z\rangle = S^z|S, S^z\rangle$


```



Model library

Site basis

{



Basis

{

|

```
<SITEBASIS name="spin">
  <PARAMETER name="local_S" default="1/2"/>
  <QUANTUMNUMBER name="S" min="local_spin" max="local_spin"/> |S, Sz+|S, Sz> = √S(S + 1) - Sz(Sz + 1)|S, Sz + 1>
  </OPERATOR>
  <OPERATOR name="Sz" matrixelement="Sz"/> S-|S, Sz> = √S(S + 1) - Sz(Sz - 1)|S, Sz - 1>
</SITEBASIS>
<CONSTRAINT quantumnumber="Sz" value="Sz_total"/>
<PARAMETER name="local_S#" value="local_S"/>
<PARAMETER name="local_S" value="1/2"/>
<SITEBASIS ref="spin">
```

 $|S, S^z\rangle$

$$S^+|S, S^z\rangle = \sqrt{S(S + 1) - S^z(S^z + 1)}|S, S^z + 1\rangle$$

$$S^-|S, S^z\rangle = \sqrt{S(S + 1) - S^z(S^z - 1)}|S, S^z - 1\rangle$$

$$S^z|S, S^z\rangle = S^z|S, S^z\rangle$$

Model library

Site basis

```
<SITEBASIS name="spin">
  <PARAMETER name="local_S" default="1/2"/>
  <QUANTUMNUMBER name="S" min="local_spin" max="local_spin"/> |S, Sz

$$S^+|S, S^z\rangle = \sqrt{S(S+1) - S^z(S^z+1)}|S, S^z+1\rangle$$


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$$S^z|S, S^z\rangle = S^z|S, S^z\rangle$$


```

Basis

```
{ <BASIS name="spin">
  <SITEBASIS ref="spin">
    <PARAMETER name="local_S#" value="local_S"/>
    <PARAMETER name="local_S" value="1/2"/>
  </SITEBASIS>
  <CONSTRAINT quantumnumber="Sz" value="Sz_total"/>
</BASIS>
```

Hamiltonian

```
{ <HAMILTONIAN name="spin">
  <PARAMETER name="J" default="0"/>
  <PARAMETER name="Jz" default="J"/>
  <BASIS ref="spin"/>
  <SITETERM site="i">
    -h#*Sz(i)-Gamma#*Sx(i)+D#*Sz(i)*Sz(i)
  </SITETERM>
  <BONDTERM source="i" target="j">
    Jz#*Sz(i)*Sz(j)+Jxy#*exchange_xy(i,j)+K#*biquadratic(i,j)
  </BONDTERM>
</HAMILTONIAN>
```

$$H_{\text{site}} = \sum_i (-hS_i^z - \Gamma S_i^x + DS_i^z S_i^z)$$

$$H_{\text{bond}} = \sum_{\langle i,j \rangle} \left(J_z S_i^z S_j^z + J_{xy} h_{ij}^{exc} + K h_{ij}^{blbq} \right)$$

Model library

Site basis

```
<SITEBASIS name="spin">
    <PARAMETER name="local_S" default="1/2"/>
    <QUANTUMNUMBER name="S" min="local_spin" max="local_spin"/>
    <QUANTUMNUMBER name="Sz" min="-S" max="S"/>
    <OPERATOR name="Splus" matrixelement="sqrt(S*(S+1)-Sz*(Sz+1))">
        <CHANGE quantumnumber="Sz" change="1"/>
    </OPERATOR>
    <OPERATOR name="Sminus" matrixelement="sqrt(S*(S+1)-Sz*(Sz-1))">
        <CHANGE quantumnumber="Sz" change="-1"/>
    </OPERATOR>
    <OPERATOR name="Sz" matrixelement="Sz*(Sz+1)">
        <CHANGE quantumnumber="Sz" change="0"/>
    </OPERATOR>
</SITEBASIS>
```

Basis

```
<BASIS name="spin">
    <SITEBASIS ref="spin"/>
    <CONSTRAINT>
        <PARAMETER name="J" default="0"/>
        <PARAMETER name="Jz" default="J"/>
    </CONSTRAINT>
</BASIS>
```

Hamiltonian

```
<HAMILTONIAN>
    <PARAMETER name="J" default="0"/>
    <PARAMETER name="Jz" default="J"/>
    <BASIS ref="spin"/>
    <SITETERM site="i">
        -h#*Sz(i)-Gamma#*Sx(i)+D#*Sz(i)*Sz(i)
    </SITETERM>
    <BONDTERM source="i" target="j">
        Jz#*Sz(i)*Sz(j)+Jxy#*exchange_xy(i,j)+K#*biquadratic(i,j)
    </BONDTERM>
</HAMILTONIAN>
```

Existing models:

- Boson & fermion Hubbard
- Spinless fermions
- t - J model
- SU(2) spins

$|S, S^z\rangle$

$= \sqrt{S(S+1) - S^z(S^z+1)}|S, S^z+1\rangle$

$= \sqrt{S(S+1) - S^z(S^z-1)}|S, S^z-1\rangle$

$= S^z|S, S^z\rangle$

$H_{\text{site}} = \sum_i (-hS_i^z - \Gamma S_i^x + D S_i^z S_i^z)$

$H_{\text{bond}} = \sum_{\langle i,j \rangle} (J_z S_i^z S_j^z + J_{xy} h_{ij}^{\text{exc}} + K h_{ij}^{\text{blbq}})$

3 Ways of running ALPS

- Command line:
 - Requires minimal external dependencies (can be built without Python)
 - Best suited for remote use on clusters etc.
 - Greatest flexibility
- Python
 - Both command-line and interactive use when used with IPython
 - Best suited for remote applications when Python is available
- VisTrails
 - Interactive use
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[i]Python

- **Python**: easily accessible, portable and widely used interpreted programming language
 - Currently tested against Python 2.7
 - Many tutorials, e.g.:
 - Chris Laumann's lectures
 - <https://wiki.python.org/moin/BEGINNERSGUIDE>
 - <https://docs.python.org/2/tutorial/>
- **IPython**: improved Interactive Python shell
- **IPython Notebook/Jupyter**:
 - Browser interface for IPython
 - Offers full advantage of both interactive and scripted tools for data analysis
 - Similar interface to Mathematica: code cells
 - **Will be used in tutorial.**

iPython Notebook

The screenshot shows an iPython Notebook interface. At the top, there's a toolbar with various icons for file operations, cell selection, and help. The title bar says "jupyter DMRG_Chain_Spectrum_Entanglement Last Checkpoint: Last Monday at 10:38 AM (autosaved)". Below the toolbar, the menu bar includes File, Edit, View, Insert, Cell, Kernel, and Help. A "Cell Toolbar" dropdown is set to "None". The main area has a header "Spectrum". A text block below it says: "We first explore the spectrum of the Heisenberg chain. In the following panel, we plot the spin triplet gap, which is the energy difference between the ground state in the $S_z = 1$ and the $S_z = 0$ sector. We then perform a fit to a polynomial using a method from NumPy." Two arrows point from the right side of the slide to this text block and the code cell below. The code cell (In [9]) contains Python code for loading data, calculating the spectral gap, and performing a linear fit. The output cell (Out[9]) shows a plot of the gap Δ versus $1/L$. The plot has a dashed line and blue 'x' markers.

```
In [9]: energy_data = pyalps.loadEigenstateMeasurements(pyalps.getResultFiles(prefix=chain_prefix), what=['Energy'])

p = pyalps.collectXY(energy_data, 'L', 'Energy', ('Sz_total'))

# Here we calculate the spectral gap by subtracting the energy for Sz=1 and Sz=0.
L = p[0].x
x = L**-1.0
gap = np.abs(p[0].y-p[1].y)

plt.plot(x, gap, 'x')

# We now perform a fit to the data.
# fit_order = 1 chooses a linear fit.
# For fit_order = 2, a quadratic fit is performed.
fit_order = 1
fit = np.polyfit(x, gap, fit_order)
fit_x = np.linspace(0, max(x), 100)
plt.plot(fit_x, np.poly1d(fit)(fit_x), 'r')

plt.xlabel('$1/L$')
plt.ylabel('$\Delta_{z=1}^z$ gap')

Out[9]: <matplotlib.text.Text at 0x116465550>
```

A scatter plot with a linear fit. The x-axis is labeled $1/L$ and ranges from 0.00 to 0.07. The y-axis is labeled $\Delta_{z=1}^z$ gap and ranges from 0.00 to 0.25. Blue 'x' markers show a linear increase, and a red line represents the linear fit.

$1/L$	$\Delta_{z=1}^z$ gap
0.015	0.065
0.022	0.085
0.030	0.115
0.065	0.220

Markup

- Double-click to edit, Shift-Enter to render
- Use LaTeX math annotations ($\$... \$$)

Source code

- Usual Python commands
- Execute with Shift-Enter

Inline figures from matplotlib
(see commands at top of notebook)

ALPS applications

- **Classical Monte Carlo:**
 - Local and cluster update algorithms for spin systems [spinmc]
- **Exact Diagonalization**
 - Full [fulldiag] and sparse [sparsediag] diagonalization
- **Quantum Monte Carlo:**
 - Stochastic Series Expansion (SSE) [dirloop_sse]
 - Loop code [loop]
 - Continuous-time worm algorithm [worm and dwa]
 - Extended ensemble (quantum Wang-Landau) algorithm [qwl]
- **Tensor network methods:**
 - DMRG [dmrg]
 - Time-evolving block decimation [tebd]
 - Matrix-product state implementations [mps_X]
- **DMFT**

The QMC applications

- Which QMC code should you use?
 - <https://alps.comp-phys.org/mediawiki/index.php/>
Comments: which code to choose for your calculation
- Looper:
 - Only for highly symmetric models ($U(1) \times Z_2$), but most efficient for those
- Directed Loop SSE:
 - More generic, high performance. Inefficient with a large number of states per site (soft-core bosons).
- Worm algorithm: Bose-Hubbard models
- Quantum Wang-Landau: Specific application for free energy & entropy calculations without thermodynamic integration

The DMRG applications

- DMRG:
 - Traditional DMRG code, good for simple $1d$ Hamiltonians but inefficient in more general cases
- TEBD:
 - Specific to time evolution, special models, more dependencies
- MPS:
 - Generic, modern implementation in MPS language
 - Ground state & time evolution methods in the same infrastructure
 - High-performance (up to 10,000 states), efficient for two-dimensional systems

Code	Time
ALPS MPS (our new code)	16 sec
ALPS DMRG [1, 21]	73 sec
ITensor [27]	24 sec
OSMPS [28]	40 sec

- Reference: *M. Dolfi et al, Comput. Phys. Commun. 185, 3430 (2014)*

Obtaining ALPS

<http://alps.comp-phys.org/>

Welcome to the ALPS project.

The ALPS project (Algorithms and Libraries for Physics Simulations) is an open source effort aiming at providing high-end simulation codes for strongly correlated quantum mechanical systems as well as C++ libraries for simplifying the development of such code. ALPS strives to increase software reuse in the physics community.

Announcement:

ALPS 2.1 has been released

Community

Check back regularly to read the latest news and information on the people contributing to the project.

User Forum

Go here to discuss the ALPS libraries and applications with the community of developers. This is the place to address any questions you encounter while using any codes of the ALPS project.

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Download and Installation

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Tutorials

[How to run ALPS applications](#)

[ALPS applications](#)

[latest/v2.2b - v2.1](#)

[Using ALPS libraries for your applications](#)

[latest/v2.2b - v2.1](#)

Documentation

[ALPS applications reference documentation](#)

[The ALPS libraries \(2.1.0\) API](#)

[The ALPS Python modules API](#)

[The HDF5 scheme documentation](#)

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Installation

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- **Binary:**
 - Available for Linux, Mac OS X, and Windows
 - Relies on VisTrails for Python interpreter & libraries
 - Easiest installation, least flexibility

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- **Versions:**
 - General recommendation: **most recent version possible!**
 - For the tutorials
 - For binary installation, use **pre-release 2.2.0b4**
 - For source installation, either **2.2.0b4 or SVN trunk**

License conditions

- ALPS license = variant of BSD license
- **Crucial condition:**
 - Use of **any ALPS** component requires citation of the ALPS papers:
A.F.Albuquerque et al., J. of Magn. and Magn. Materials 310, 1187 (2007) and
B. Bauer et al., J. Stat. Mech. (2011) P05001
 - Use of the DMFT codes additionally requires citation of E. Gull, P.Werner, S. Fuchs, B. Surer, T. Pruschke, and M. Troyer, Computer Physics Communications 182, 1078 (2011).
 - Use of the MPS codes requires additional citation of M. Dolfi et al., Computer Physics Communications 185, 3430 (2014).
- **For details, see CITATIONS.txt in source distribution**

Tutorials

- Will be done on lab workstations - **no installation necessary**
- If you would like to continue working on it later, ask me for installation help
- Today: **Two tutorials**
 - Quantum Monte Carlo
 - Density Matrix Renormalization Group

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- DWA-01 Simulating the Bose Hubbard model using dwa QMC code (revisiting tutorial MC-05)
- DWA-02 Density profile of a 3D optical lattice in a harmonic trap
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Exact diagonalization

- ED-01 Sparse Diagonalization (Lanczos)
- ED-02 Spin gaps of 1D quantum systems
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- ED-04 Conformal field theory description of 1D critical spectra
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- ED-06 Full Diagonalization

Density Matrix Renormalization Group (DMRG)

- DMRG-01 Density Matrix Renormalization Group Introduction
- DMRG-02 Calculating gaps
- DMRG-03 Calculating local observables
- DMRG-04 Calculating correlations

Dynamical Mean Field Theory (DMFT) solvers

- DMFT-01 An introduction to DMFT
- DMFT-02 CT-HYB: the CT-HYB QMC solver
- DMFT-03 CT-INT: the CT-INT QMC solver
- DMFT-04 Mott Transition
- DMFT-05 Orbitally Selective Mott Transition
- DMFT-06 Paramagnetic metal
- DMFT-07 The Hirsch-Fye solver
- DMFT-08 Setting a particular lattice

Time-Evolving Block Decimation (TEBD)

- TEBD-01 Quenches in the hardcore boson model
- TEBD-02 Time Evolution of a domain wall in the XX model

Trieste Summer School 2015 Tutorials

- Trieste tutorials

ALPS examples

The ALPS examples section contains examples of real simulations, which require more computation resources than most.

[/afs/ictp.it/public/b/bauer/](http://afs/ictp.it/public/b/bauer/)

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Trieste Summer School 2013 Tutorials

- Trieste tutorials

NPRC examples

The AI PR examples contain results from real simulations, which require more computation resources than in most

/afs/ictp.it/public/b/bauer/