Axions: Past, Present and Future

ICTP Summer School, 2015

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Axions

10⁻⁴³ GeV

Axions and axion-like-particles are the goldstone bosons of symmetries broken at some high scale fa

10² GeV

(SM)

10¹⁹ GeV

fa

The QCD axion (*a*) was introduced to solve the strong CP problem. This problem arises because instanton effects in QCD give rise to large CP violating effects. The axion dynamically solves this problem since it acquires a potential from these instantons which is minimized at a point where CP is restored.

Goldstone bosons that acquire a mass through a different source are called axion like particles (ϕ)

As goldstone bosons, these particles are light. By detecting them, we get a peek into ultra-high energy physics without having to build ultra-high energy colliders

Can easily be dark matter





New Ideas

Produce and detect

Super-radiance in astrophysical systems

Axion dark matter

NMR style searches for oscillating moments (CASPEr)

Super-radiance in Extremal Astrophysical Systems

Overview

Super-radiance can be extremely efficient in certain extremal rotating astrophysical systems, if there are light massive bosons (e.g. axions) that are coupled to the star.

Observations of such rotating objects constrain such particles.

Statistically significant gaps in rotation rates may imply existence of such particles.

Previous work limited to black-holes.

A.Arvanitaki et.al. (2009)

General instability, could also use milli-second pulsars. SR (in progress)

Radiation from Rotating Objects



Magnetic field not aligned with rotation.

Time varying magnetic dipole.

Dipole radiation at frequency Ω

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What if the magnetic field is aligned with the rotational axis?



Radiated photon must carry angular momentum.

Cannot couple to rigid axisymmetric star.



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Light degrees of freedom coupled to stellar medium.

At some level, there must be radiation!

Absorption



Angular momentum of the photon couples to moments of the stellar excitation.

Super-radiance (Inverse Absorption)



Non-zero Matrix element from Absorption. Will happen if kinematically allowed.

Super-radiance: The Kinematics γ



Solve for E' $E^{'} \approx m\Omega - E_{\gamma} > 0$

Super-radiance: The Kinematics γ , γ , (E_{γ}, m) Star E'



Photons of arbitrarily high energy can be emitted provided the angular momentum is also high.

High angular momentum => mode localized far from star => suppressed coupling.

Comparison



Non axi-symmetric systems.

Radiation at multiples of Ω

Instability of any absorptive, rotating system.

Continuum emission.

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Radiation at multiples of Ω

Instability of any absorptive, rotating system.

Continuum emission.

Absorption => Super-radiance usually sub-dominant to multipole radiation.

Massive Particles and Massive Stars



Particle of mass μ , star of mass M. Gravitationally bound states at $r_b \sim \frac{1}{GM\mu^2}$

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Bose enhancement => exponential amplification!

Massive Particles and Massive Stars



Bose enhancement => exponential amplification!

Could be efficient if there were new light particles coupled strongly enough to stellar medium.

Use observations of rotating black holes/pulsars to constrain and perhaps discover such particles.

Absorption in a Medium

Particle Ψ , mass μ , interacting with a medium moving at v^{α} .

 $\Box \Psi + \mu^2 \Psi + C v^{\alpha} \nabla_{\alpha} \Psi + V_{eff} (\Psi) = 0$

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$$\Psi(t) \propto \operatorname{Exp} \left(-\frac{Ct}{2} \right)$$

For positive C, mode is damped (absorbed). C is the absorption coefficient.

Particle Ψ , mass μ , medium rotates at Ω

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Same kinematic condition.

For large m, $(\mu - m\Omega) < 0$.

Absorption becomes emission.



Absorption occurs only inside the star (radius R)



Rate depends upon overlap of mode with the stellar medium.

Absorption occurs only inside the star (radius R)



Rate depends upon overlap of mode with the stellar medium.

Proportional to the probability of finding particle in the star.



Hydrogenic ψ_{nlm} with Bohr radius $r_b \sim \frac{1}{GM\mu^2}$

$$\psi_{nlm} \sim \left(\frac{r}{r_b}\right)^l \sim r^l \left(GM\mu^2\right)^l$$



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$$\Gamma_{nlm} \propto \left(\frac{r}{r_b}\right)^{2l+3} \propto \left(GM\mu^2 R\right)^{2l+3}$$

Efficient Super-radiance

$$\Gamma_{nlm} \propto \left(\frac{r}{r_b}\right)^{2l+3} \propto \left(GM\mu^2 R\right)^{2l+3}$$

For super-radiance, $\mu - m\Omega < 0$, with $l \ge |m|$

Very low mass, lowest angular momentum mode is super-radiant.

Large Bohr-radius.

High mass, only large angular momentum modes are superradiant.

Large Bohr-radius.

Most efficient $\mu \sim \Omega$

Extremal Objects

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Largest M, R consistent with Ω .
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Relativity $\Omega R \lessapprox 1$

Given μ , need extremal object at μ .

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Extremal Kerr Black-holes, Millisecond Pulsars.

(fastest pulsars at 642 Hz, 714 Hz)

Superradiance

Extremal Black Holes

Millisecond Pulsars

Absorption by gravity

Spin measurement is an evolving field, subject to astrophysical modeling

Systematic: Unknown close orbiting companions

One clean measurement in one clean system is good

Absorption through non-gravitational interactions

Spin and orbital issues well measured

Known clean systems

Good for particles that couple to number density (dark photons)

For axions, bounds depend on internal magnetic fields

Axion Dark Matter

Cosmic Axion Spin Precession Experiment (CASPEr)

D. Budker et.al, 2013

P.W. Graham, SR (2010,2013)

Axion Dark Matter

Photons



Early Universe: Misalignment Mechanism

Dark Bosons



Today: Random Field



Detect Photon by measuring time varying field

 $\vec{E} = E_0 \cos\left(\omega t - \omega x\right)$

$$a(t) \sim a_0 \cos\left(m_a t\right)$$

Spatially uniform, oscillating field

$$m_a^2 a_0^2 \sim \rho_{DM}$$

Correlation length ~ I/(m_a v) Coherence Time ~ I/(m_a v²) ~ I s (MHz/m_a)

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Detect effects of oscillating dark matter field

Resonance possible. Q ~ 10^{6} (set by v ~ 10^{-3})



Axions

Global symmetry broken at high scale f_a

Light Goldstone boson



So how can we detect high f_a axions?

Strong CP problem: $\mathcal{L} \supset \theta \, G \widetilde{G}$ creates a nucleon EDM $d \sim 3 \times 10^{-16} \, \theta \, e \, \mathrm{cm}$ the axion: $\mathcal{L} \supset \frac{a}{f_a} G \widetilde{G}$ creates a nucleon EDM $d \sim 3 \times 10^{-16} \, \frac{a}{f_a} \, e \, \mathrm{cm}$

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axion dark matter
$$ho_{
m DM} \sim m_a^2 a^2 \sim \left(200 {
m MeV}\right)^4 \left(rac{a}{f_a}
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m GeV}}{{
m cm}^3}$$

so today:
$$\left(\frac{a}{f_a}\right) \sim 3 \times 10^{-19}$$
 independent of f_a

axion gives all nucleons an oscillating EDM (kHz-GHz) independent of f_a , a non-derivative operator

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Taking $f_{\Phi} \sim 10^9$ GeV, this looks like a ~ fT a/c magnetic field

Neutron



Neutron in Axion Wind

Spin rotates about dark matter velocity

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General Axions

QCD Axion

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Neutron in QCD Axion Dark Matter



 $\left(\frac{a}{f_a}G\tilde{G}\right)$

QCD axion induces electric dipole moment for neutron and proton

> Dipole moment along nuclear spin

Oscillating dipole: $d \sim 3 \times 10^{-34} \cos(m_a t) \ e \ \mathrm{cm}$

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 $\left(\frac{\partial_{\mu}a}{f_a}\bar{N}\gamma^{\mu}\gamma_5N\right)$



$$H_N \supset \frac{a}{f_a} \vec{v_a} . \vec{S}_N$$

Spin rotates about dark matter velocity

Effective time varying magnetic field

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Measure Spin Rotation, detect Axion



 $\left(\frac{a}{f_a}G\tilde{G}\right)$

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Apply electric field, spin rotates



high nuclear spin orientation achieved in several systems, persists for $T_1 \sim$ hours



high nuclear spin orientation achieved in several systems, persists for $T_1 \sim$ hours applied E field causes precession of nucleus SQUID measures resulting transverse magnetization

> Larmor frequency = axion mass \implies resonant enhancement resonance \rightarrow scan over axion masses by changing B_{ext}





Limits on Axion-Nucleon Coupling



Limits on Axion-Nucleon Coupling








Summary

