## Double Parton Scattering cross section limit from same-sign W bosons pair production in di-muon final state at LHC

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Introduction Analysis Results





#### Introduction



#### Analysis

- Motivation
- Strategy
- Background evaluation
- Multi Variate Analysis
- Systematics



**Results** 

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## **DPS** theory

• in the case of **two identical processes** with **no parton longitudinal correlation**:

$$\sigma_{DPS}^{incl}(s) = \frac{1}{2} \int d^2 \beta \left( A(\beta) \right)^2 (\sigma^{incl})^2 \tag{1}$$

all the unknown correlation of partons in transverse dimension are contained inside ∫ d<sup>2</sup>β (A(β))<sup>2</sup> that is usually indicated as the inverse value of the effective cross section:

$$\sigma_{eff} = \frac{1}{2} \cdot \frac{(\sigma^{incl})^2}{\sigma_{DPS}^{incl}}$$
(2)

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## State of the art

Lack of angular and momentum correlations  $\rightarrow$  DPS signature

- State of the art for  $\sigma_{eff}$  measurements:
  - 4 jets
  - 3 jets+γ
  - W + 2 jets



In all of these measurements the DPS contribution is extracted indirectly since SPS associated processes have a much higher cross section.

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## DPS in same sign WW

#### Pros

- the same sign muons final state presents a clean signature (better described than jets enviroments)
- the DPS cross section for such a final state is comparable to the SPS corresponding one.

#### Cons

- expected cross section around 5 fb for a single flavour leptonic final state
- with 19.7 fb<sup>-1</sup> we can realistically only put a limit



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## DPS in same sign WW



Signatures:

- absence of lepton angular and momentum correlation
- no direct production of jets

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### Gen Level studies

# W and Muons Gen Level kinematic DPS vs SPS comparison



W bosons in SPS events are expected to be more boosted due to the necessity of balancing the energy of the associated jets.

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### Gen Level studies

# W and Muons Gen Level kinematic DPS vs SPS comparison



For the same reason we expected the  $p_{\rm T}$  of the muons to be discriminant observable for DPS events.

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### Gen Level studies

#### W and Muons Gen Level topologic DPS vs SPS comparison



One can also think to use the SPS relative separation between W bosons that is expected to be different from the DPS one since the energy balance is not a constrain for DPS events.

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- WZ, W  $\gamma$  and ZZ:
  - one missed lepton needed in order to emulate ssWW
  - cross section higher than the DPS cross section by a factor of  $\sim 10^2$

#### • Drell-Yan, W + jets, QCD and tt+jets:

- no direct production if same sign muons final state
- huge cross section w.r.t. the DPS makes the contribution from misreconstructed muons (e.g. coming from jets) not negligible.

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#### Datasets

#### **DATA samples:** Run2012 19.7 $fb^{-1}$ .

Sample

DoubleMuRun2012A-22Jan2013-v1 DoubleMuParkedRun2012B-22Jan2013-v1AOD DoubleMuParkedRun2012C-22Jan2013-v1AOD DoubleMuParkedRun2012D-22Jan2013-v1AOD

#### MC samples: Summer12\_DR53X-PU\_S10\_START53\_V7A

Sample	Cross Section [pb]
WW_DoubleScattering_8TeV-pythia8	0.59 ± 0.02(LO)
Wp(m)Wp(m)qq_8TeV-madgraph	0.34 ± 0.03(LO)
WZ_TuneZ2star_8TeV_pythia6_tauola	33 ± 3(NLO)
WGstarToLNu2Mu_TuneZ2star_8TeV-madgraph-tauola	$1.9 \pm 0.2$ (LO)
ZZ_TuneZ2star_8TeV_pythia6_tauola	7.6 ± 0.3(NLO)
DYJetsToLL_M-50(10-50)_TuneZ2Star_8TeV-madgraph-tarball	18206 ± 100(NNLO)
TTJets_MassiveBinDECAY_TuneZ2star_8TeV-madgraph-tauola	234 ± 20(NNLO)
WJetsToLNu_TuneZ2Star_8TeV-madgraph-tarball	37509 ± 1300(NNLO)
QCD_Pt_20_MuEnrichedPt_15_TuneZ2star_8TeV_pythia6	134680 ± 100%(LO)

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- Define a base selection on the path of other WW analysis, keeping that as much loose as possible in order to save DPS statistics.
- Study the misidentified muons contribution in this selection
- Define a set of independent (as much as possible) sensitive variables to provide an input for a MVA (BDT in this case)
- Put a limit on DPS yield using the modified frequentist approach (CombineHiggs tool)

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## Selection

#### • Trigger: HLT\_Mu17\_TkMu8

- Muons: two tight muons (standard working point):
  - Normalized  $\chi^2 < 10$ .
  - The muon track reconstructed within the tracker volume, should have at least one valid pixel hit.
  - There should be hits registered in at least two muon stations by each of the muon tracks.
  - The number of valid hits in the muon chambers used in the global muon fit should be at least 1.
  - The transverse impact parameter, calculated w.r.t. beamspot position, should be less than 0.2 mm.
- **Missing energy**: MET Type0Type1 (PU) corrected and shift in xy plane corrected

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#### **Base selection**

The most sensitive independent observables will be put as input for a MVA. Therefore we did not optimized the selection (as it would be for a cut based analysis).

#### Base selection summary

Muon object definition	POG Tight Muons Muons relative isolation: $I < 0.12$ Muons impact parameter: $d_{xy} < 0.02$ cm
Keeping the DPS efficiency as high as possible	At least two same sign muons Veto on third muon with $p_T < 10 \text{GeV}$ $p_{T\mu}^{leading} > 20 \text{GeV}$ $p_{T\mu}^{subleading} > 10 \text{GeV}$
Reducing contribution from QCD multijet	$  p_{\mathrm{T}}{}^{leading}_{\mu}   +   p_{\mathrm{T}}{}^{subleading}_{\mu}   > 45 \mathrm{GeV}$ $E_{\mathrm{T}}^{\mathrm{miss}} > 20 \mathrm{GeV}$
Avoiding Z mass peak	$20 < M_{inv} < 75 \text{GeV} \text{ or } M_{inv} > 105 \text{GeV}$

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### Data driven: fake muons

A large part of background is expected to come from events in which one (or two) muons coming mainly from heavy-flavour decays are misidentified as coming from a *prompt* decay of W or Z boson. Definitions:

- fake muons: any sources but W or Z decay
- prompt muons: coming from a W or Z boson decay

A data driven method has been studied in order to evaluate the contribution from fake muons mainly related to QCD and Wjets events, due to the lack of statistics and the not precise description of misidentified muons in MC.

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## Data driven: Strategy

- Define a loose and a tight selection.
- 2 Select a fake/prompt muons enriched sample from data.
- Evaluate respectively the fake/prompt ratios (tight/loose)
- Subtract the contamination to the fake ratio coming from EWK processes
- Use those ratios for weighting (based on *p*<sub>T</sub> and η) data events passing different conditions: Tight-Loose, Loose-Loose and Tight-Tight
- Use the sum of this weights to evaluate contribution from fake-fake and prompt-fake events
  - Fake ratio: the ratio of the number of muon passing the tight selection over muons passing the loose one in the fake muon control sample
  - Prompt ratio: it is defined as tight to loose ratio in a prompt lepton control sample obtained with a selection of Z boson production events

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### Data driven method

The total yield of events with one prompt and one fake muon can be evaluated by  $\sum^{i} N_{pf}^{i}$ , while the fake-fake events yield is obtained by  $\sum^{i} N_{ff}^{i}$ . (Details in backup)

Events	
N <sub>TT</sub>	$1539\pm40$
N <sub>TL</sub>	$4492\pm67$
N <sub>LL</sub>	$3974 \pm 63$
Evaluated prompt-fake yield	$709\pm7$
Evaluated fake-fake yield	$381 \pm 4$

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## **BDT** training

The idea is to use the BDT estimator to get a response shape with the highest possible DPS sensitivity.

- *signal* sample using opposite sign DPS MC events passing the offline base selection but with opposite sign request.
- background sample has been constructed mixing up the three main background in our base selection (properly reweighted): QCD, W + jets and WZ. For training QCD and W + jets sample, we used data-driven observables evaluated in an independent way.

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## **BDT** input observables

- leading muon (µ<sub>1</sub>) p<sub>T</sub>
- subleading muon (μ<sub>2</sub>) p<sub>T</sub>
- E<sub>T</sub><sup>miss</sup>
- $M_T(\mu_1, \mu_2)$  di-muon invariant transverse mass
- Δφ(μ<sub>1</sub>, μ<sub>2</sub>)
- $\Delta \phi(\mu_1, E_{\mathrm{T}}^{\mathrm{miss}})$
- $\Delta \phi(\mu_2, E_{\mathrm{T}}^{\mathrm{miss}})$
- Δφ(μ<sub>1</sub> + μ<sub>2</sub>, E<sub>T</sub><sup>miss</sup>): where μ<sub>1</sub> + μ<sub>2</sub> is the vector sum of muon four-momenta

• 
$$m_T(W_{1/2}) = \sqrt{2 \cdot p_T^{\mu_{1/2}} \cdot E_T^{\text{miss}} \cdot (1 - \cos(\Delta \phi(\mu_{1/2}, E_T^{\text{miss}})))}$$

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## **BDT** input observables

#### Yellow band shows the systematic uncertainty

- leading muon (µ<sub>1</sub>) p<sub>T</sub>
- subleading muon (µ<sub>2</sub>) p<sub>T</sub>
- E<sub>T</sub><sup>miss</sup>
- M<sub>T</sub>(μ<sub>1</sub>, μ<sub>2</sub>) di-muon invariant transverse mass
- Δφ(μ<sub>1</sub>, μ<sub>2</sub>)
- $\Delta \phi(\mu_1, E_T^{\text{miss}})$
- $\Delta \phi(\mu_2, E_T^{\text{miss}})$
- $\Delta \phi(\mu_1 + \mu_2, E_T^{\text{miss}})$
- $m_T(W_1)$
- m<sub>T</sub>(W<sub>2</sub>)



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## **Systematics**

#### Systematics summary

Source	DPS	SPS	WZ	ZZ	$W\gamma^*$	Fake-Fake	Prompt-Fake
Luminosity	2.5	2.5	2.5	2.5	2.5	-	-
PU re-weighting	0.5	0.3	0.5	0.1	0.7	-	-
Trigger and Muon id	0.1	0.1	0.1	0.1	0.1	-	-
MET	0.8	1.4	0.4	4.0	2.2	-	-
Fake-Fake normalization	-	-	-	-	-	60	-
Prompt-Fake normalization	-	-	-	-	-	-	30
MC normalization	4.0	10.0	10.0	4.0	10.0	-	-
Total	4.8	10.4	10.3	6.2	10.6	60	30





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#### Result for BDT observable and sample yields



Yellow band shows the systematic uncertainty

Sample	Events $\pm$ stat. $\pm$ syst.
DPS	$15.0 \pm 0.5 \pm 0.7$
SPS	$30 \pm 1 \pm 3$
WZ	$263 \pm 3 \pm 30$
ZZ	$40 \pm 1 \pm 2$
W <sub>\gamma</sub> *	$86 \pm 3 \pm 9$
Prompt-Fake	$709 \pm 7 \pm 213$
Fake-Fake	$381 \pm 4 \pm 229$
Total	$1523 \pm 9 \pm 314$
Data	1539



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## Limit setting

Statistical interpretation of the results is performed with the  $CL_s$  method, which is based on the modified frequentist approach Limits are estimated by fitting BDT shape

95% CLs	BDT
Expected	r < 2.001
Expected $\pm 1\sigma$	[1.443,2.778]
Expected $\pm 2\sigma$	[1.085,3.691]
Observed	r < 1.897





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#### Final result

The observed limit can be read as a limit on the DPS same sign W boson cross section of

$$\sigma_{WW}^{DPS} < r_{observed} \cdot \sigma_{WW}^{MC} = 1.897 \cdot 0.59 \, \text{pb} = 1.12 \, \text{pb}.$$







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### Summary

- A search for the same-sign W-pair DPS events in the di-muon final state is done using data with  $\sqrt{s} = 8$  TeV and an integrated luminosity of 19.7  $fb^{-1}$
- BDT response shape gives the limit estimation, excluding at 95% CLs a signal strength r > 1.897 (28 DPS events), with an expected exclusion of r > 2.01 (30 DPS events), which means an upper limit on  $\sigma_{WW}^{DPS} < 1.12 \ pb$  at 95% of confidence level.
- Considering the two scattering to be independent and no correlation between interacting partons, one can put in relation the limit on  $\sigma_{WW}^{DPS}$  with the  $\sigma_{eff}$  using the factorization formula:

$$\sigma_{eff} > rac{(\sigma_{W o l
u})^2}{2 \cdot (BR^2_{W o l
u}) \cdot \sigma^{DPS}_{WW}} = 5.91 \, \mathrm{mb}.$$

# Thank you for your attention!

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D. Ciangottini DPS in same sign WW (CMS-PAS-FSQ-13-001)

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#### Other sensitive observable Gen Level comparison



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#### **Double Parton scattering in Pythia**



Moreover the two interactions are generated independently from each other.

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#### Reco/Gen efficiency for the base selection

MC sample	Efficiency (%)
DPS	$18\pm0.7$
SPS ++	$26 \pm 0.1$
SPS –	$27 \pm 0.2$
Drell-Yan	$0.00020 \pm 0.00007$
WZ	$2.64\pm0.03$
ZZ	$0.48\pm0.01$
tt	$0.044 \pm 0.004$
$W-\gamma^*$	$3.1 \pm 0.1$
Wjets	$0.06\pm0.02$
QCD	$0.0006 \pm 0.0006$

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### Data driven method

- Tight selection: identical to the analysis selection
- Loose selection: same as above but I<0.4 and d<sub>xy</sub> < 0.2 cm</li>
- Fake and prompt muons enriched regions are needed for the evaluation of the fake and prompt ratio

Fake control sample	Prompt control sample
HLT_Mu17 or HLT_Mu8	HLT_Mu17_TkMu8
Only one POG tight muon	Only two opposite sign POG tight muon
$p_{\mathrm{T}}^{\mu} > 10\mathrm{GeV}$	$p_{\rm T}^{\mu_1} > 20 {\rm GeV}$ and $p_{\rm T}^{\mu_2} > 10 {\rm GeV}$
$E_{ m T}^{ m miss} <$ 20 GeV	70 GeV < M <sub>inv</sub> < 110 GeV
$\sqrt{2 \cdot p_{\mathrm{T}}^{\ \mu} \cdot E_{\mathrm{T}}^{miss} \cdot (1 - \mathit{cos}(\Delta \phi(\mu, E_{\mathrm{T}}^{miss})))} < 20  \mathrm{GeV}$	only $\mu_2$ studied for prompt ratio

We choose this fake region as it shows a good agreement with the isolation spectra expected for our fake muons (backup)



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## Data driven method

The prompt muon contamination fraction, electroweak (EWK) contamination, has been studied.

- tight selection  $\rightarrow$  numerator of the fake ratio
- $\bullet$  loose selection  $\rightarrow$  denominator of the fake ratio

Correction based on MC has been applied.



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### Data driven method

# Corrected fake ratio as function of $p_{\rm T}$ on the right and $\eta$ on the left:

<i>p</i> <sub>T</sub> range [GeV]	$0 < \eta < 1$	$1 < \eta < 1.4$	$1.4 < \eta < 2$	$2 < \eta < 2.4$
$10 < p_{\rm T} < 15$	$0.291 \pm 0.003$	$0.319 \pm 0.004$	$0.355 \pm 0.005$	$0.369 \pm 0.007$
$15 < p_{\rm T} < 20$	$0.232 \pm 0.003$	$0.264 \pm 0.005$	$0.295 \pm 0.006$	$0.318 \pm 0.009$
$20 < p_{\rm T} < 25$	$0.216 \pm 0.005$	$0.241 \pm 0.009$	0.277±0.010	$0.302 \pm 0.015$
$25 < p_{\rm T} < 35$	0.207±0.010	$0.249 \pm 0.017$	$0.281 \pm 0.019$	$0.304 \pm 0.030$
$p_{\rm T} > 35$	$0.204 \pm 0.020$	$0.234 {\pm} 0.033$	$0.281 \pm 0.034$	$0.274 \pm 0.054$



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#### Shape evaluation

Two different methods to evaluate the distributions from the fake-fake and prompt-fake events:

- Method 1: Depending upon the transverse momentum and pseudo-rapidity of the two muons, event by event weights (N<sup>i</sup><sub>ff</sub> and N<sup>i</sup><sub>pf</sub>) are applied using fake and prompt ratio
- Method 2: Expected number of prompt-fake and fake-fake events are calculated by summing over the event weights, whereas shapes are extracted using the events passing the selection by reversing the isolation cut, *i.e.*, *I* > 0.12.

Both methods have shown compatible (within uncertainties) results. Method 1 has been adopted to evaluate the final results, Method 2 has been used to get an independent sample for BDT training.



### **Control regions**

#### **Opposite sign control region selection**

Yellow band shows the systematic uncertainty

 $\begin{array}{l} \label{eq:post_star} \begin{array}{l} \mbox{POG Tight Muons} \\ \mbox{At least two opposite sign muons} \\ \mbox{Veto on third muon with } \mbox{$\rho_T$} < 10 \mbox{ GeV} \\ \mbox{$\rho_T$}_{\mu}^{leading} > 20 \mbox{ GeV} \\ \mbox{$\rho_T$}_{\mu}^{subleading} > 10 \mbox{ GeV} \\ \mbox{$\rho_T$}_{\mu}^{leading} | + |\mbox{$\rho_T$}_{\mu}^{subleading} | > 45 \mbox{ GeV} \\ \mbox{$E_T$}_{miss} > 20 \mbox{ GeV} \\ \mbox{$20 \mbox{ GeV}$} < \mbox{$Min_V$} < 75 \mbox{ GeV of $Min_V$} > 105 \mbox{ GeV} \end{array}$ 

• **ρ**<sub>Tμ2</sub>

E<sup>miss</sup><sub>T</sub>

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### **Control regions**

#### Same sign control region selection

Yellow band shows the systematic uncertainty

POG Tight Muons
At least two same sign muons
Veto on third muon with $p_{\rm T}$ < 10 GeV
$p_{T}_{\mu}^{leading} > 20  \text{GeV}$
$p_{T_{\mu}}^{subleading} > 10  \text{GeV}$
$ p_{\mathrm{T}\mu}^{\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $
$E_{\rm T}^{\rm miss} > 20  {\rm GeV}$
$20 \text{ GeV} < M_{inv} < 75 \text{ GeV} \text{ or } M_{inv} > 105 \text{ GeV}$

Sample	Events
DPS	-
SPS	$1.000 \pm 0.001$
WZ	$7.00 \pm 0.03$
ZZ	$2.00 \pm 0.01$
WGstar	55 ± 1
Prompt-Fake	-
Fake-Fake	$1116 \pm 12$
Total	$1193 \pm 13$
Data	1272



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### **Systematics**

All the systematics uncertainties are applied as normalization factor to the BDT shapes used in this analysis, except for the BDT uncertainty for which we used a distribution uncertainty.

- Luminosity (2.5%): an uncertainty on the luminosity estimation of 2.5% is directly translated into an uncertainty on the yields for both signal sample and all background samples for which the yield is not determined from data.
- MC pileup reweighting (0.1-0.7%): The effects on MC distributions (signal and background) are evaluated varying event-by-event mean value of PU by ±1.
- Theoretical uncertainty (4-10%): the respective cross sections are varied within their theoretical uncertainties.



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• Muon reconstruction and identification (0.1%): the uncertainty due to a different muon reconstruction and identification efficiency between data and Monte Carlo have been considered, varying the weight with a gaussian function with  $\sigma$  equal to the uncertainties.



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### **Systematics**

•  $E_{\rm T}^{\rm miss}$  uncertainties (0.4-2.2%): the uncertainty related to  $E_{\rm T}^{\rm miss}$  has different sources. In order to estimate those sources we compared the final yields for different  $E_{\rm T}^{\rm miss}$  recontruction. The  $E_{\rm T}^{\rm miss}$  components varied in that recontrustions follow the prescription of the  $E_{\rm T}^{\rm miss}$  POG syst tools.

https://twiki.cern.ch/twiki/bin/view/CMSPublic/SWGuidePATTools#MET\_Systematics\_Tools



### **Systematics**

#### Data-driven fake muon evaluation:

- difference in jet kinematic spectra between fake enriched control region and signal region may lead to a different fake muon scenario.
- different quark content in W+jets and tt processes w.r.t. QCD one



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### **Systematics**

In order to face the first source prompt-fake and fake-fake muons yield evaluation with MC calculated along with jet  $p_{\rm T}$  threshold of 25 GeV sample calculation as been compared to the one used and the one obtained by pure QCD MC ratios evaluation.

	Prompt-fake	Fake-fake
Simulated sample	$586\pm 6$	$152\pm2$
Jet $p_{\rm T}$ >25 GeV threshold sample	$510\pm5$	$161\pm2$
No jet threshold	$\textbf{709} \pm \textbf{7}$	$\textbf{381} \pm \textbf{4}$



### **Systematics**

Using MC ratios from QCD samples: prompt-fake muons yield on W+jets simulated events compared to the simulation expectation.

Events	Prompt-fake
N <sub>TT</sub>	$125\pm11$
N <sub>TL</sub>	$404\pm20$
N <sub>LL</sub>	$48\pm7$
Evaluated yield	$95\pm 6$
Simulated yield	125

These systematic uncertainties are added in quadrature to give a total systematic uncertainty of 60% for fake+fake sample and of 30% for prompt+fake events.



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• **BDT uncertainty:** we varied, within the uncertainty, the muon  $p_{\rm T}$  (considering the resolution less than 3%) and the  $E_{\rm T}^{\rm miss}$  (with shapes used for systematics above) that are given as input to the BDT. This is the only background for which we took a shape systematics and not an overall normalization factor.

#### **Prompt ratio:**

<i>p</i> <sub>T</sub> range [GeV]	$0 < \eta < 1.4$	$1.4 < \eta < 2.4$
$10 < p_{\rm T} < 15$	0.70±0.01	0.75±0.01
$15 < p_{\rm T} < 20$	$0.757 \pm 0.008$	$0.81 \pm 0.01$
$20 < p_{\rm T} < 25$	$0.806 \pm 0.006$	$0.86 \pm 0.01$
$25 < p_{\rm T} < 35$	$0.899 \pm 0.003$	$0.929 \pm 0.005$
$p_{\mathrm{T}} > 35$	$0.97 {\pm} 0.01$	$0.97 \pm 0.02$

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For event *i* passing TT selection the corresponding weight are  $N_{pf}^{i}$  and  $N_{ff}^{i}$ :

$$N_{pf}^{i} = -\frac{1}{(p_{1} - f_{1}) \cdot (p_{2} - f_{2})} \cdot [(1 - p_{2}) \cdot (1 - f_{1}) \cdot p_{1} \cdot f_{2} + (1 - p_{1}) \cdot (1 - f_{2}) \cdot p_{2} \cdot f_{1}]$$
$$N_{ff}^{i} = \frac{1}{(p_{1} - f_{1}) \cdot (p_{2} - f_{2})} \cdot f_{1} \cdot f_{2} \cdot (1 - p_{1}) \cdot (1 - p_{2})$$

while case leading muon passing tight selection and subleading one passing only loose selection:

$$N_{pf}^{i} = \frac{1}{(p_{1} - f_{1}) \cdot (p_{2} - f_{2})} \cdot [(1 - f_{1}) \cdot f_{2} \cdot p_{1} \cdot p_{2} + (1 - p_{1}) \cdot f_{1} \cdot f_{2} \cdot p_{2}]$$
$$N_{ff}^{i} = \frac{1}{(p_{1} - f_{1}) \cdot (p_{2} - f_{2})} \cdot p_{2} \cdot (1 - p_{1}) \cdot f_{2} \cdot f_{1}$$

for events with *loose* leading muons and *tight* subleading one, a simple substitution of  $p_1$  in  $p_2$  and  $f_1$  in  $f_2$  can provide the weights needed.

Finally, weights for events in which both muons are not passing tight requirements but succeed in passing the loose one are the following:

$$egin{aligned} N^{i}_{pf} &= -rac{2}{(p_{1}-f_{1})\cdot(p_{2}-f_{2})}\cdot f_{1}\cdot f_{2}\cdot p_{1}\cdot p_{2} \ N^{i}_{ff} &= rac{1}{(p_{1}-f_{1})\cdot(p_{2}-f_{2})}\cdot f_{1}\cdot f_{2}\cdot p_{1}\cdot p_{2} \end{aligned}$$

Charge misidentification control region selection

$$\begin{array}{l} \mbox{POG Tight Muons} \\ \mbox{At least two same sign muons} \\ \mbox{Veto on third muon with } \mbox{$p_T$}_{\mu} < 10 \, \mbox{GeV} \\ \mbox{$p_T$}_{\mu}^{leading} > 20 \, \mbox{GeV} \\ \mbox{$p_T$}_{\mu}^{leading} > 10 \, \mbox{GeV} \\ \mbox{$|p_T$}_{\mu}^{leading}| + |\mbox{$p_T$}_{\mu}^{subleading}| > 45 \, \mbox{GeV} \\ \mbox{$E_T$}_{miss} > 20 \, \mbox{GeV} \\ \mbox{$M_{inv}$} > 20 \, \mbox{GeV} \\ \end{array}$$

From MC matching studies in DY and tt samples, no contribution from charge misID

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#### Correlation Matrix (signal)



#### Correlation Matrix (background)



= 990

#### **BDT** response validation

51/26

#### BDT response in same sign control region



This additional cross check, in addition to the standard training checks (in backup), confirms a stable BDT response for a set of independent samples.

# Systematic uncertainties summary (% variation on final total yield)

Source	Background syst. (%)	Signal syst. (%)
Luminosity	0.8	2.5
PU reweight	0.2	0.5
Muon reconstruction and ID	0.1	0.1
E <sub>T</sub> miss	0.1	0.8
Fake Muons	27	-
MC normalization	3.2	4.0
Total	27.2	4.8

	$\sigma_{\rm GS09}$	$\sigma_{ m MSTW_0}$	$\sigma_{\rm MSTW_1}$	$\sigma_{\rm MSTW_2}$
$W^+W^-$	0.546	0.496	0.409	0.348
$W^+W^+$	0.321	0.338	0.269	0.223
$W^-W^-$	0.182	0.182	0.156	0.136
	R			
	0.784	1.00	1.00	1.00

Parton correlation effect

J. R. Gaunt et al., *Same-sign W pair production as a probe of double parton scattering at the LHC* 

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### MC driven reweight

MC normalization has been performed for the considered integrated luminosity, trigger and isolation.

Sample	Weights
WW DPS	$0.0138 \pm 0.0008$
WW SPS	$0.056 \pm 0.001$
WZ	$0.025 \pm 0.002$
$W\gamma^*$	$0.089 \pm 0.006$
ZZ	$0.0165 \pm 0.0008$
Drell-Yan ( $\rightarrow II$ )	$2.0 \pm 0.1 (M_{inv} > 50  GeV)$
$(M_{inv} > 10 \text{ GeV})$	$8.0 \pm 0.5 (M_{inv} < 50  GeV)$
tī	$0.39 \pm 0.03$
$W(\rightarrow l\nu)$	14 ± 1
QCD multijet	145 ± 5
$(p_{ m T}>20{ m GeV},p_{ m T\mu}>15{ m GeV})$	

- Drell-Yan and tt
   contribution from charge misidentification is negligible for muons and therefore they are not
   included in same sign distributions.
- Due to the lack of statistics and the not precise description of misidentified muons in MC, W+jets, tt and QCD multijet contribution have been evaluated data-driven.

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## **BDT** input observables

#### Yellow band shows the systematic uncertainty

#### leading muon (µ<sub>1</sub>) p<sub>T</sub>

- subleading muon  $(\mu_2) p_T$
- Ernis
- M<sub>T</sub>(µ<sub>1</sub>, µ<sub>2</sub>) di-muon invariant transverse mass
- $\Delta \phi(\mu_1, \mu_2)$
- $\Delta \phi(\mu_1, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_2, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_1 + \mu_2, E_{\mathrm{T}}^{\mathrm{miss}})$
- $m_T(W_1)$
- $M_{T}(W_{2})$



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## **BDT** input observables

#### Yellow band shows the systematic uncertainty



- subleading muon (µ<sub>2</sub>) p<sub>T</sub>
- Ernis
- M<sub>T</sub>(µ<sub>1</sub>, µ<sub>2</sub>) di-muon invariant transverse mass
- $\Delta \phi(\mu_1, \mu_2)$
- $\Delta \phi(\mu_1, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_2, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_1 + \mu_2, E_{\rm T}^{\rm miss})$
- $m_T(W_1)$

 $m_T(W_2)$ 





## **BDT** input observables

#### Yellow band shows the systematic uncertainty

- leading muon ( $\mu_1$ )  $p_1$
- subleading muon ( $\mu_2$ )  $p_{
  m T}$
- E<sup>miss</sup>
- M<sub>T</sub>(µ<sub>1</sub>, µ<sub>2</sub>) di-muon invariant transverse mass
- $\bigcirc \quad \Delta\phi(\mu_1,\mu_2)$
- $\Delta \phi(\mu_1, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_2, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_1 + \mu_2, E_{\rm T}^{\rm miss})$
- $m_T(W_1)$

 $m_T(W_2)$ 



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## BDT input observables

#### Yellow band shows the systematic uncertainty

- leading muon ( $\mu_1$ )  $p_{
  m I}$
- subleading muon ( $\mu_2$ )  $p_T$
- E<sup>mis</sup>
- M<sub>T</sub>(µ<sub>1</sub>, µ<sub>2</sub>) di-muon invariant transverse mass
- $\bigcirc \quad \Delta\phi(\mu_1,\mu_2)$
- $\Delta \phi(\mu_1, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_2, E_T^{\text{miss}})$
- $\Delta \phi(\mu_1 + \mu_2, E_{\rm T}^{\rm miss})$
- $m_T(W_1)$

 $m_T(W_2)$ 





## **BDT** input observables

#### Yellow band shows the systematic uncertainty

- leading muon ( $\mu_1$ )  $p_{
  m I}$
- subleading muon ( $\mu_2$ )  $p_T$
- E<sup>mis</sup>
- M<sub>T</sub>(µ<sub>1</sub>, µ<sub>2</sub>) di-muon invariant transverse mass
- Δφ(μ<sub>1</sub>, μ<sub>2</sub>)
- $\Delta \phi(\mu_1, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_2, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_1 + \mu_2, E_{\rm T}^{\rm miss})$
- $m_T(W_1)$

 $m_T(W_2)$ 



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## BDT input observables

#### Yellow band shows the systematic uncertainty

- leading muon ( $\mu_1$ )  $p_{
  m I}$
- subleading muon ( $\mu_2$ )  $p_T$
- E<sup>mis</sup>
- M<sub>T</sub>(µ<sub>1</sub>, µ<sub>2</sub>) di-muon invariant transverse mass
- $\Delta \phi(\mu_1, \mu_2)$
- $\Delta \phi(\mu_1, E_T^{\text{miss}})$
- $\Delta \phi(\mu_2, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_1 + \mu_2, E_{\rm T}^{\rm miss})$
- $m_T(W_1)$

 $m_T(W_2)$ 





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- $m_T(W_1)$

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- $\Delta \phi(\mu_1, \mu_2)$
- $\Delta \phi(\mu_1, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_2, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_1 + \mu_2, E_T^{\text{miss}})$
- $m_T(W_1)$

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- leading muon ( $\mu_1$ )  $p_{
  m I}$
- Subleading muon ( $\mu_2$ )  $p_{
  m T}$
- E<sup>mis</sup>
- M<sub>T</sub>(µ<sub>1</sub>, µ<sub>2</sub>) di-muon invariant transverse mass
- $\Delta \phi(\mu_1, \mu_2)$
- $\Delta \phi(\mu_1, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_2, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_1 + \mu_2, E_{\rm T}^{\rm miss})$
- $m_T(W_1)$

 $m_T(W_2)$ 



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## BDT input observables

#### Yellow band shows the systematic uncertainty

- leading muon ( $\mu_1$ )  $p_{
  m I}$
- Subleading muon ( $\mu_2$ )  $p_{
  m T}$
- E<sup>mis</sup>
- M<sub>T</sub>(µ<sub>1</sub>, µ<sub>2</sub>) di-muon invariant transverse mass
- $\Delta \phi(\mu_1, \mu_2)$
- $\Delta \phi(\mu_1, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_2, E_{\rm T}^{\rm miss})$
- $\Delta \phi(\mu_1 + \mu_2, E_{\rm T}^{\rm miss})$
- $m_T(W_1)$

m<sub>T</sub>(W<sub>2</sub>)

