

# Dynamic color screening in diffractive DIS

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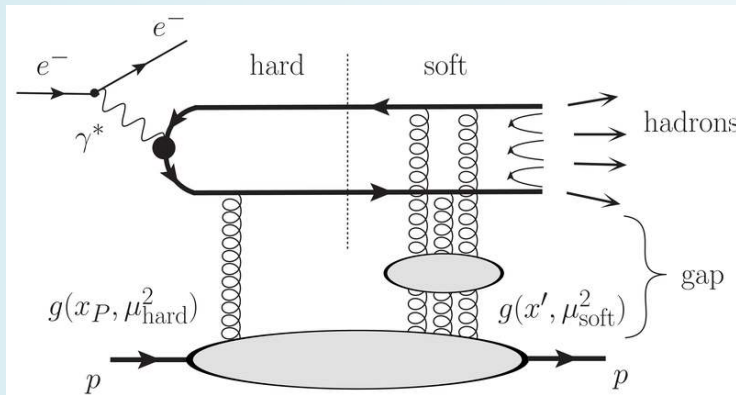
Based on arXiv:1511.06317



# Color screening in diffractive DIS

- Color exchange models as alternative to Regge based models
- Start with a inclusive hard process
- Effective color-singlet exchange via additional color exchanges
- Hard process assumed: corresponding non-diffractive
- Kinematics not affected ← Low momentum scales
- Color topology may change → Rearranged strings  
→ Large rapidity gaps, forward protons
- Original SCI model  
Random color exchanges, fixed probability.
- Construction principles, not based on amplitudes.

# Color screening in diffractive DIS



$$x = \frac{Q^2}{Q^2 + W^2}$$

$$x_P = x/\beta$$

$$W^2 = (P + q)^2$$

$$\beta = \frac{Q^2}{Q^2 + M_X^2}$$

- Amplitude for color screening (pQCD) [[hep-ph/0409119](#)], [[hep-ph/1005.3399](#)]
- Process described like inclusive, to factorization scale ( $\gamma g \rightarrow q\bar{q}$ )
- Longitudinal momentum  $x_P$  carried by first  $g$
- Secondary interaction of partons with proton gluonic field assume factorization
- Soft exchanges do not alter the momentum

# Color screening amplitude

- 1 gluon soft exchange:

$$e^{-ir \cdot k'_\perp} M_1 = i2\pi C_F \alpha_s e^{-ir \cdot k_\perp} \frac{1}{\Delta'_\perp{}^2} (e^{-ir \cdot \Delta'_\perp} - 1)$$

in cms frame  $P' + X$

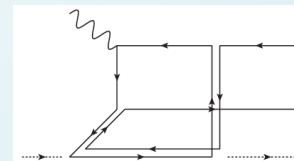
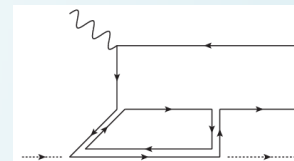
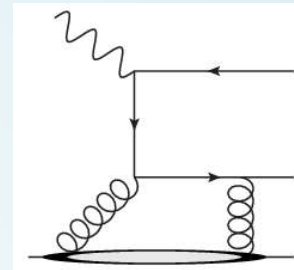
- Fourier w.r.t. to  $\Delta'_\perp$

$$e^{-ir \cdot k'_\perp} M_1 = e^{-ir \cdot k_\perp} iC_F \alpha_s \ln \frac{|b-r|}{|b|}$$

- For  $M_1, M_2, \dots, M_\infty$  gluons, exponentiates (large NC):

$$\mathcal{M} = e^{ir \cdot (k'_\perp - k_\perp)} \left( 1 - e^{iC_F \alpha_s \ln \frac{|b-r|}{|b|}} \right)$$

- Requirement for effective color singlet
- Dependence on event kinematics



# Probability for screening

- From amplitude to probability

- $M_{\text{diff}}(\mathbf{k}_{\perp}, \delta_{\perp})$

$$\propto \int d^2 r d^2 b M_g(x_{\mathbb{P}}; \mathbf{r}, \mathbf{b}) \mathcal{A}_{\text{DCS}}(\mathbf{r}, \mathbf{b}) e^{i\mathbf{r}\mathbf{k}_{\perp}} e^{i\mathbf{b}\delta_{\perp}}$$

- Ratio in impact parameter space

$$\frac{|M_{\text{diff}}(\mathbf{r}, \mathbf{b})|^2}{|M_{\text{incl}}(\mathbf{r}, \mathbf{b})|^2} = |\mathcal{A}_{\text{DCS}}(\mathbf{r}, \mathbf{b})|^2 \equiv P(\mathbf{r}, \mathbf{b})$$

- $P(r/b, \varphi) = \left| 1 - \exp \left( i C_F \alpha_s \ln \sqrt{1 + \frac{r^2}{b^2} - 2 \frac{r}{b} \cos \varphi} \right) \right|^2$

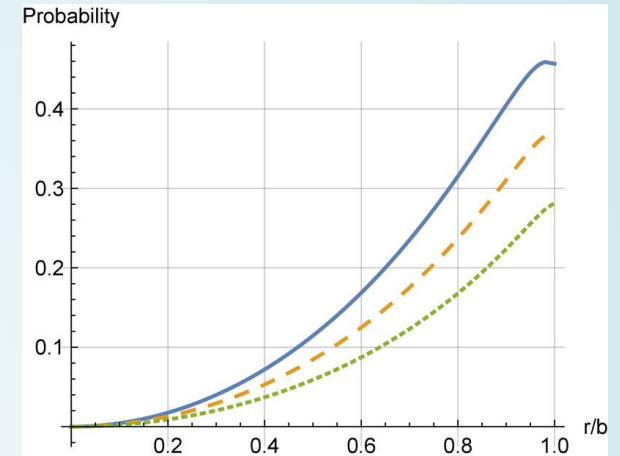
- Averaged over unobserved angle

$$P(r/b) = \int \frac{d\varphi}{2\pi} P(r/b, \varphi)$$

- $P(r/b)$  saturates  $\sim 0.4$

- $P(r/b)$  vanishes for  $r/b \rightarrow 0$   
 $\rightarrow$  Color transparency

- $\alpha_s$  essentially a normalization for  $P(r/b)$



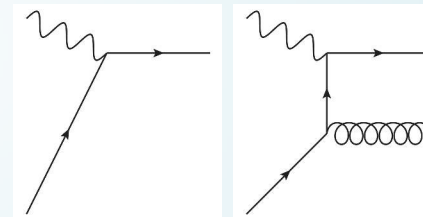
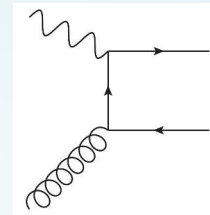
# Application in Monte Carlo

- Color screening dominated by the largest transverse size
- Associate  $r \sim 1/k_{\perp\min}$
- Typically  $k_{\perp\min} \simeq 1 \text{ GeV}$   
(hard kinematics,  $k_{\perp}$  distributions)
- Small  $k_{\perp}$  from random orientations  $\rightarrow$  introduce regulator  $\sim Q_0$
- $b \sim 1/q_{\perp}$  soft gluon exchange  
 $\Lambda_{\text{QCD}} < q_{\perp} < 1 \text{ GeV}$  (pQCD)
- Results in

$$\frac{r}{b} = \frac{q_{\perp}}{\sqrt{k_{\perp\min}^2 + k_{\perp 0}^2}}$$

# Application in Monte Carlo

- Different scales  $Q^2$ ,  $M_X^2$   
(possibly very different)
- Large logs  $\frac{M_X^2}{Q^2} = \frac{1}{\beta} - 1$
- Collinear factorization: DGLAP  
resums  $\sim \log Q^2$
- kT-factorization: CCFM evolution for  
 $\sim \log 1/x$
- Cascade:  $\gamma g \rightarrow q\bar{q}$   
Dominant process in low- $x$  DIS  
CCFM evolution  
Resummation in  $1/x$
- Lepto:  $\gamma q \rightarrow q$ ,  $\gamma q \rightarrow qg$ ,  $\gamma g \rightarrow q\bar{q}$   
DGLAP evolution



# Soft divergence

- For  $\gamma g \rightarrow q\bar{q}$  from ME  $\rightarrow$  soft divergence  
Energy splitting  $z, 1 - z$
- Uneven  $z$  possibly large  $x/x_n$
- $\gamma g \rightarrow q\bar{q}$  only for DDIS  $\log 1/z$  not resummed
- Part of  $\sigma$ :  $\gamma q \rightarrow q$  ME + DGLAP, splitting  $g \rightarrow q\bar{q}$   
resummation of leading logs in  $Q^2$

- Important at large masses

$$M_X^2 = \frac{m_q^2 + k_\perp^2}{z(1-z)}$$

- Interesting for LRG as well:  
Larger  $p_z \rightarrow$  no LRG (despite eff. color singlet)

same true for ISR



# DDIS from Cascade with DCS

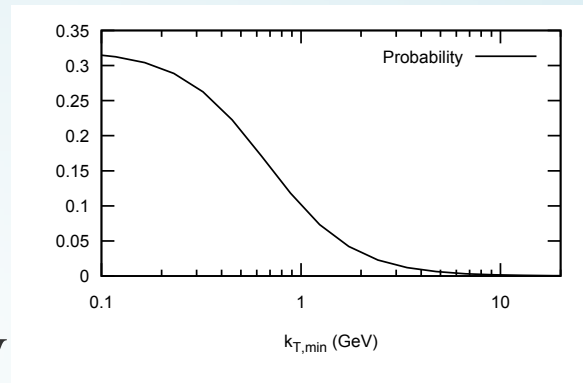
- Attempt to describe data in region:

$$2 \text{ GeV}^2 < Q^2 < 800 \text{ GeV}^2$$

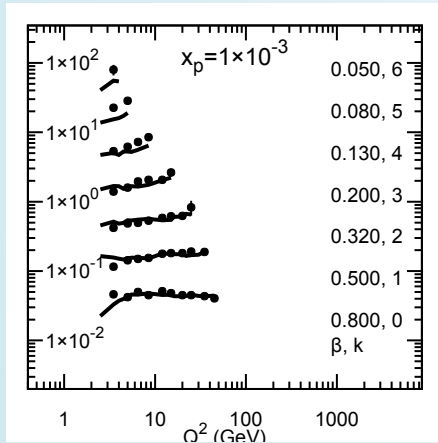
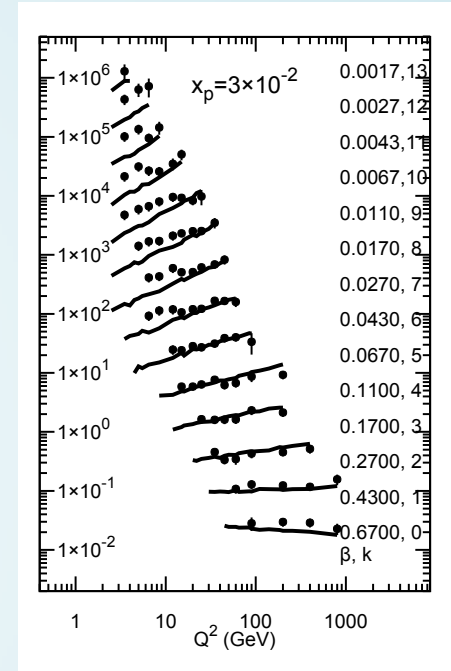
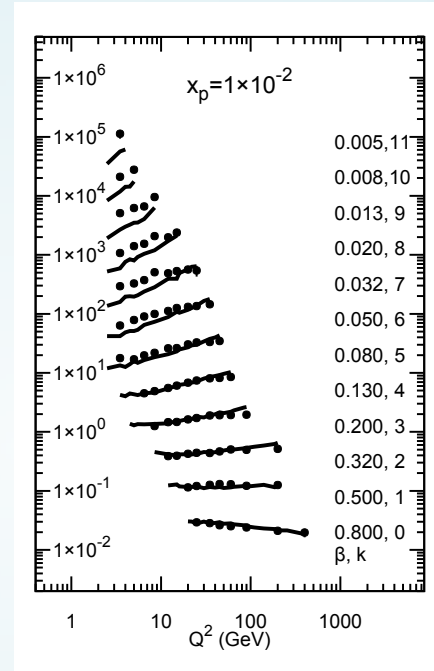
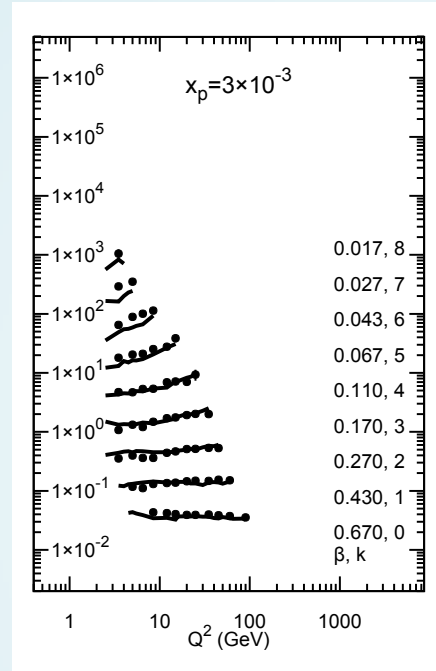
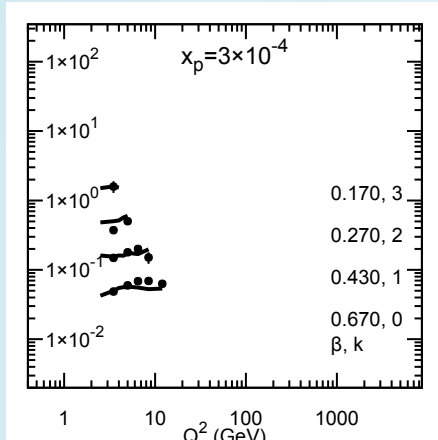
$$3 \times 10^{-4} < x_P < 3 \times 10^{-2}$$

$$1.7 \times 10^{-3} < \beta < 0.8$$

- Color screening, Cascade (CCFM)
- $q_{\perp} = 0.58 \text{ GeV}$ ,  $k_{\perp 0} = 0.72 \text{ GeV}$
- $\Lambda_{\text{QCD}} < q_{\perp} < k_{\perp 0} < Q_0$

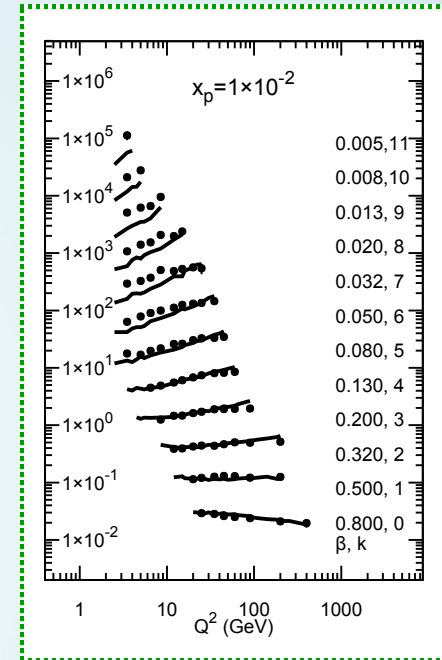
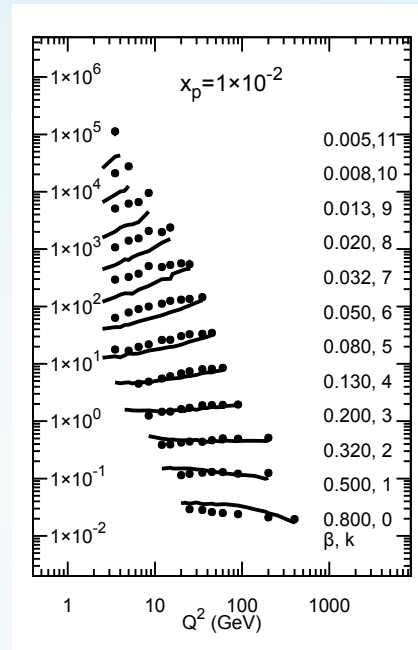
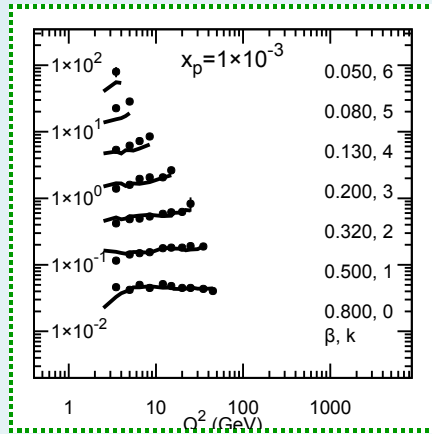
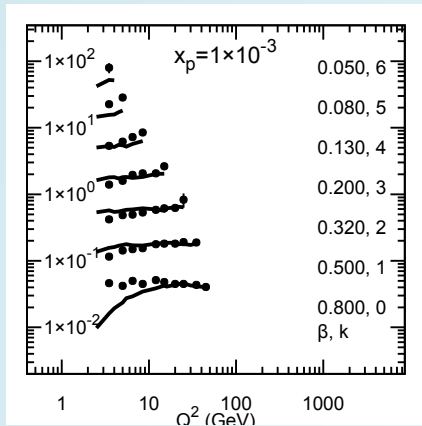


# DDIS from Cascade with DCS



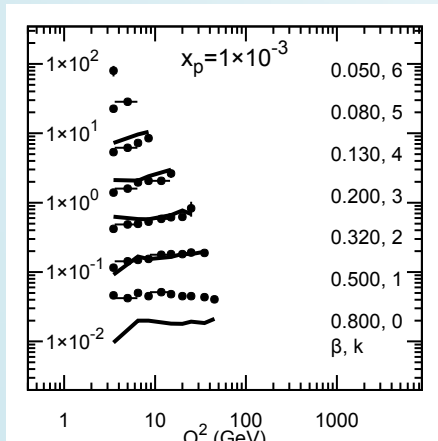
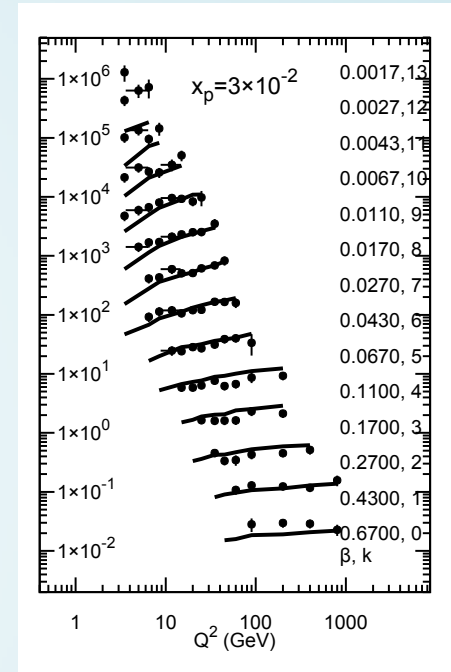
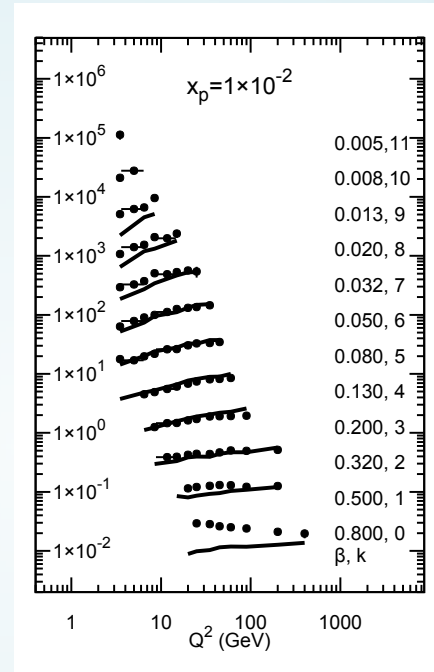
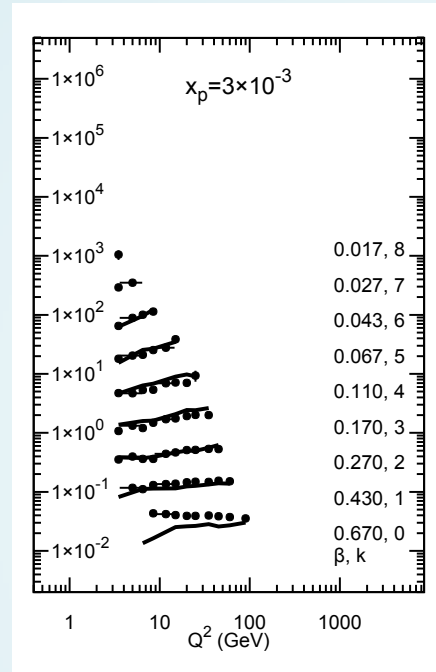
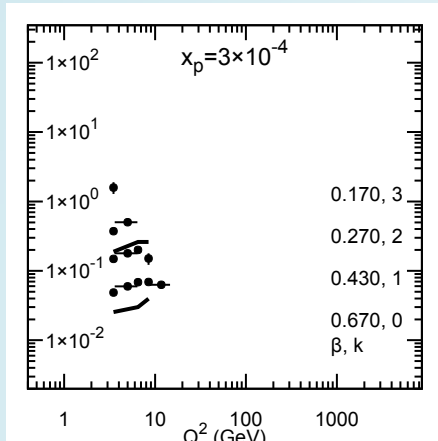
- $\sigma^{\text{diff}}$  defined as forward, proton-like,  $M_Y < 1.6 \text{ GeV}$
- Overall, agreement over a wide parameter range.
- Small  $\beta$ , low  $Q^2$ : Two different scales.

# Comparison with constant model



- Dynamic model: Improvement, not full agreement though
- Improvement most noticeable in  $\partial\sigma/\partial Q^2$

# Comparison with Lepto

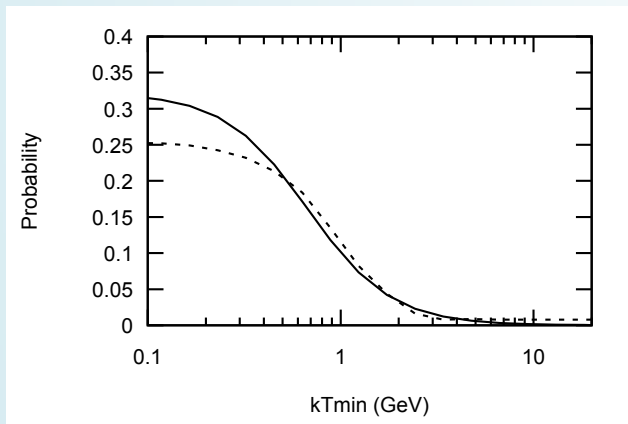


- Lepto (DGLAP)
- $q_{\perp} = 0.66 \text{ GeV}$ ,  $k_{\perp 0} = 0.89 \text{ GeV}$
- Overall worse global result
- Better in some areas: Low  $Q^2$  at large  $x_P$
- If dominantly  $q\bar{q} \rightarrow$  Large step in  $x$
- Better treated by QED ME + DGLAP parton branching

# Overlay free form fit on the model fit

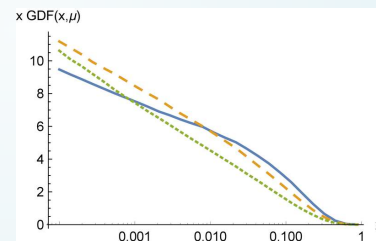
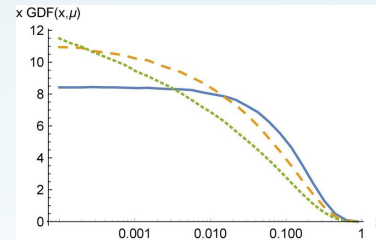
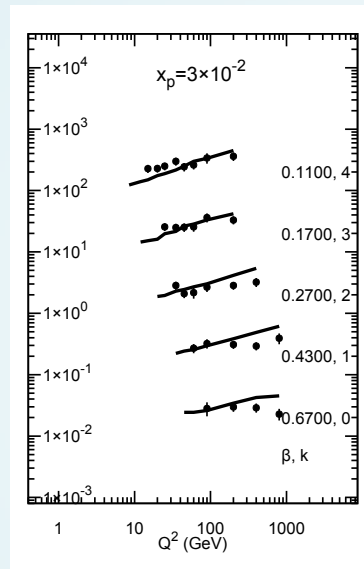
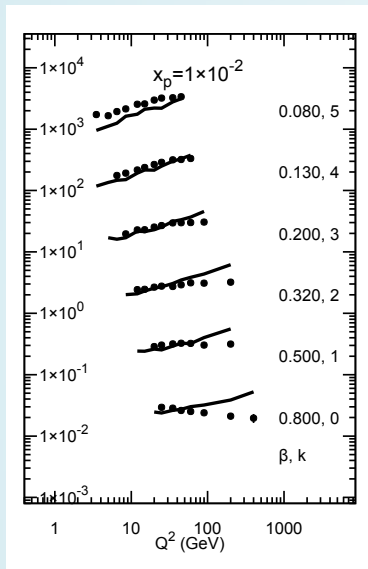
- Assume  $P(k_{\perp\min})$  free form, smooth

$$\min_{P(k_{\perp})} \left\{ \sum_{Q^2, \beta, x_P} \frac{(\sigma(Q^2, \beta, x_P) - \sigma^{\text{exp}}(Q^2, \beta, x_P))^2}{\text{Var}(\sigma^{\text{exp}}(Q^2, \beta, x_P))} + \sum \left( \alpha k_{\perp} \frac{\partial P}{\partial k_{\perp}} \right)^2 \right\}$$



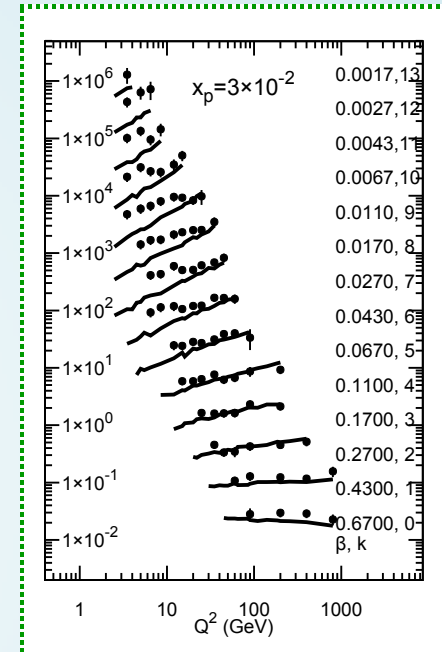
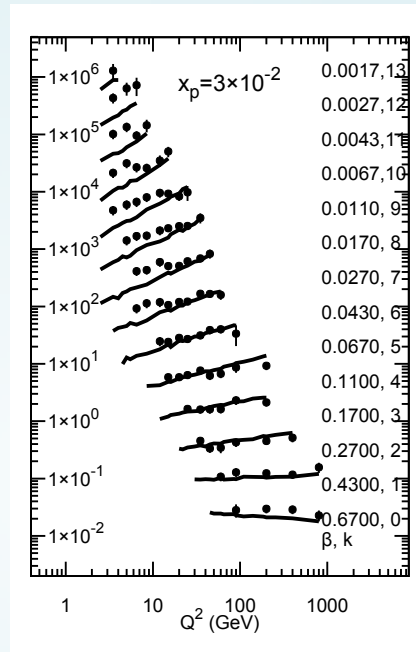
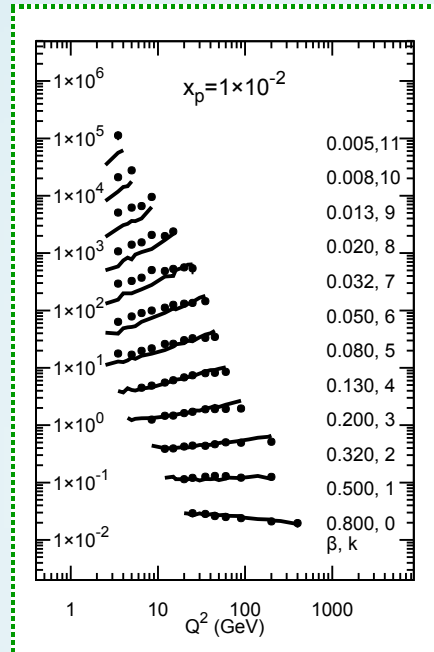
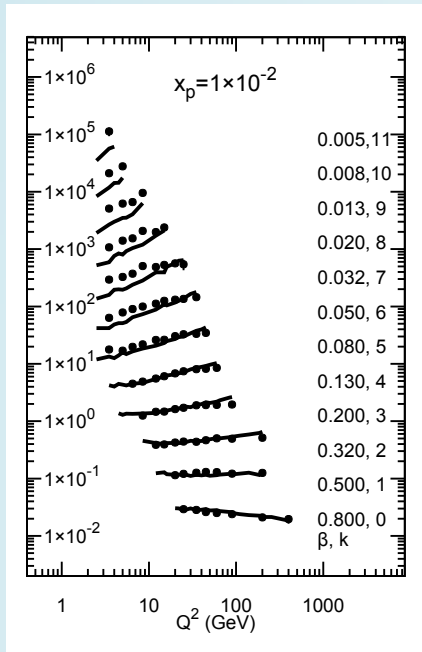
- Very similar result as screening model
- A posteriori reassuring

# UGDF dependence



- Substantial dependence,  $d\sigma/dQ^2$
- Constrain standard PDF from diffractive data?

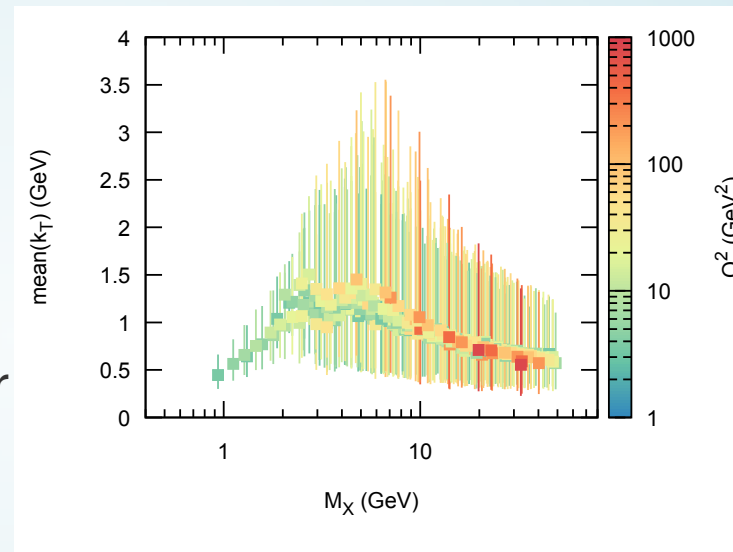
# Large rapidity gap



- Forward small-mass vs. **LRG**
- Require:  $\Delta\eta > 2$
- Gap observable sensitive to radiation pattern.
- Both  $\sigma_{r,FWD}^D$  and  $\sigma_{r,LRG}^D$  similar

# Distribution in $k_{\perp}$

- $P(k_{\perp}, \dots)$
- $k_{\perp} \sim \mathcal{N}(\ln k_{\perp})$
- PC of variation in  $M_X$
- Prediction from parton evolution
- Previous study:  $m_q^{\text{eff}}(\beta, Q^2)$  for dressed up quark, free parameter
- Difference DGLAP / CCFM





# Conclusions and outlook

- Novel implementation of color screening for DDIS
- Based on semisoft gluon exchanges, saturates, vanish at small size
- Event based dynamics ( $k_{\perp\min}$ )
- Use low- $x$  CCFM evolution for improved description at small  $\beta$
- $\sigma_{r,\text{FWD}}^D$  and  $\sigma_{r,\text{LRG}}^D$ , compared with HERA data
- Correlation of  $\langle k_{\perp} \rangle$  with  $M_X^2$
- Future: Deviation at large  $x_P$ , low  $Q^2$ , low  $\beta$