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International Centre for Theoretical Physics**



**2223-Presentations**

**Winter College on Optics in Imaging Science**

*31 January - 11 February, 2011*

**Digital Holographic Microscopy Workshop**

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ORGULLO UN



# Digital Holographic Microscopy Workshop (Digital In-line Holographic Microscopy)

**Jorge Garcia-Sucerquia**

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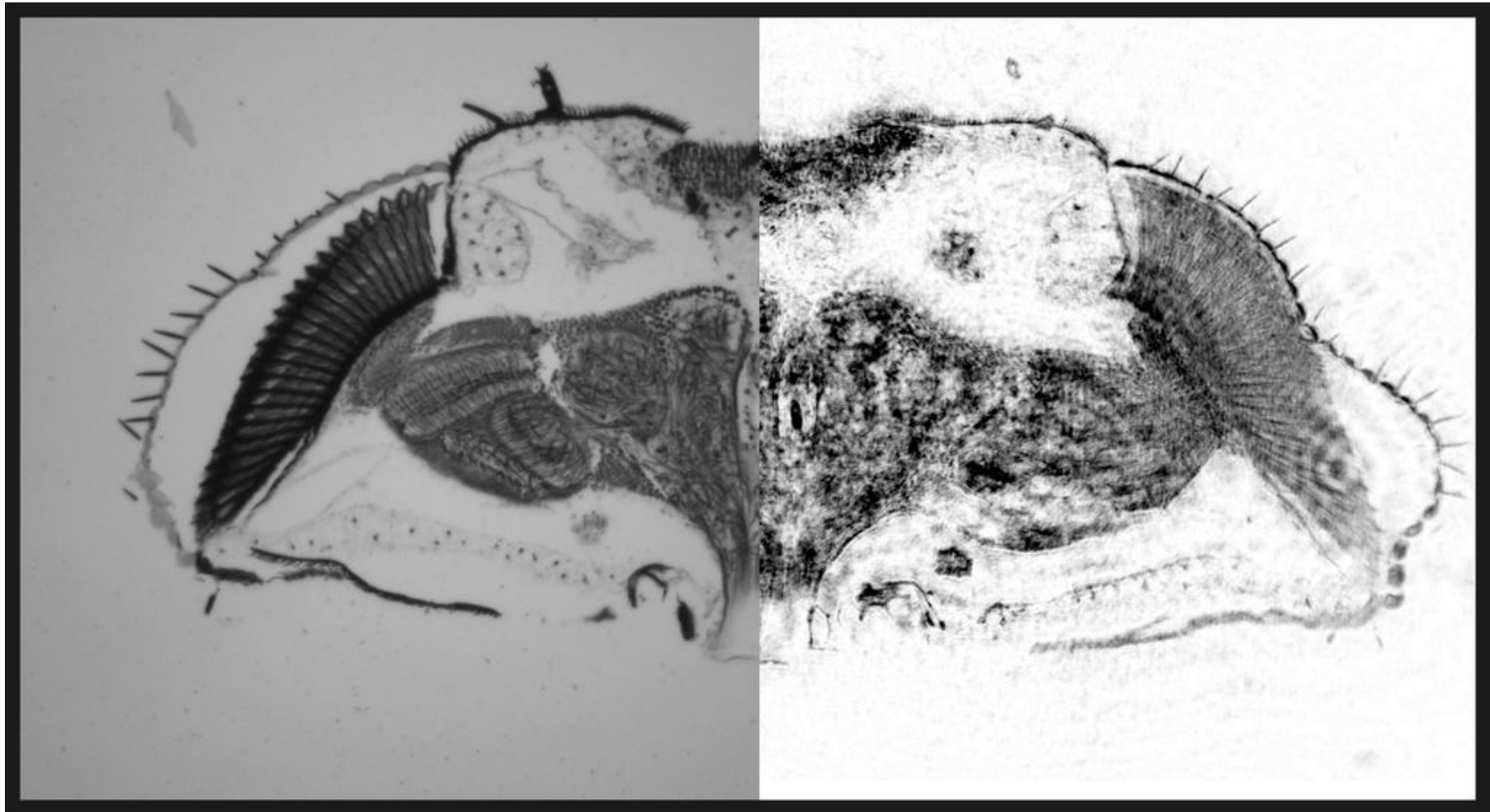


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**International Centre for Theoretical Physics**

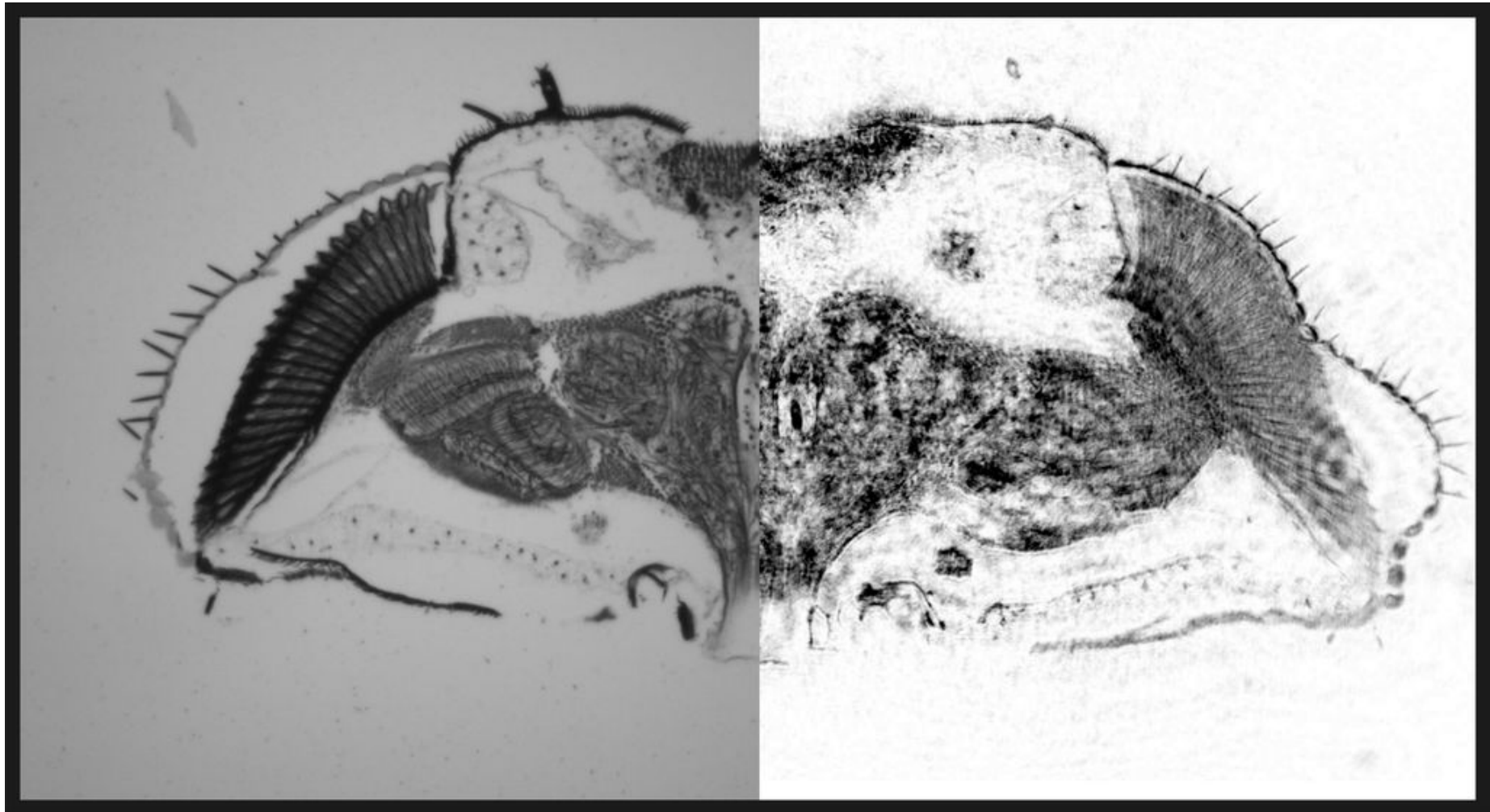
Winter College on Optics in Imaging Science, Trieste 2011

ciencia, tecnología e innovación para el país

**Why should you do digital in-line holographic microscopy?**

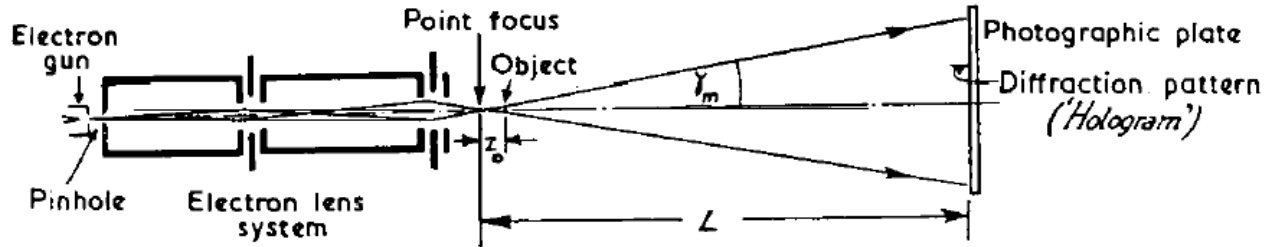


# Why should you not do digital in-line holographic microscopy?

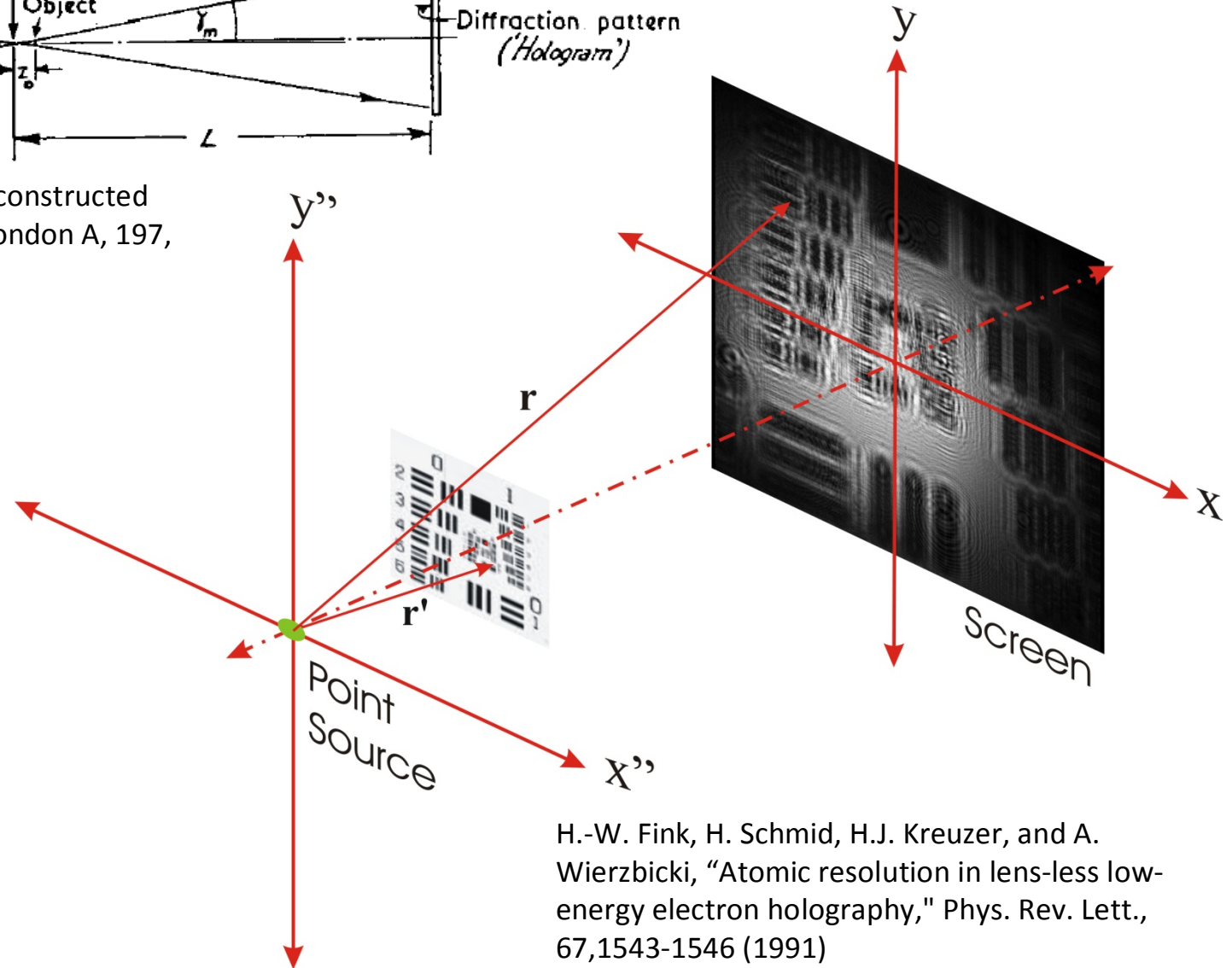


# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Recording



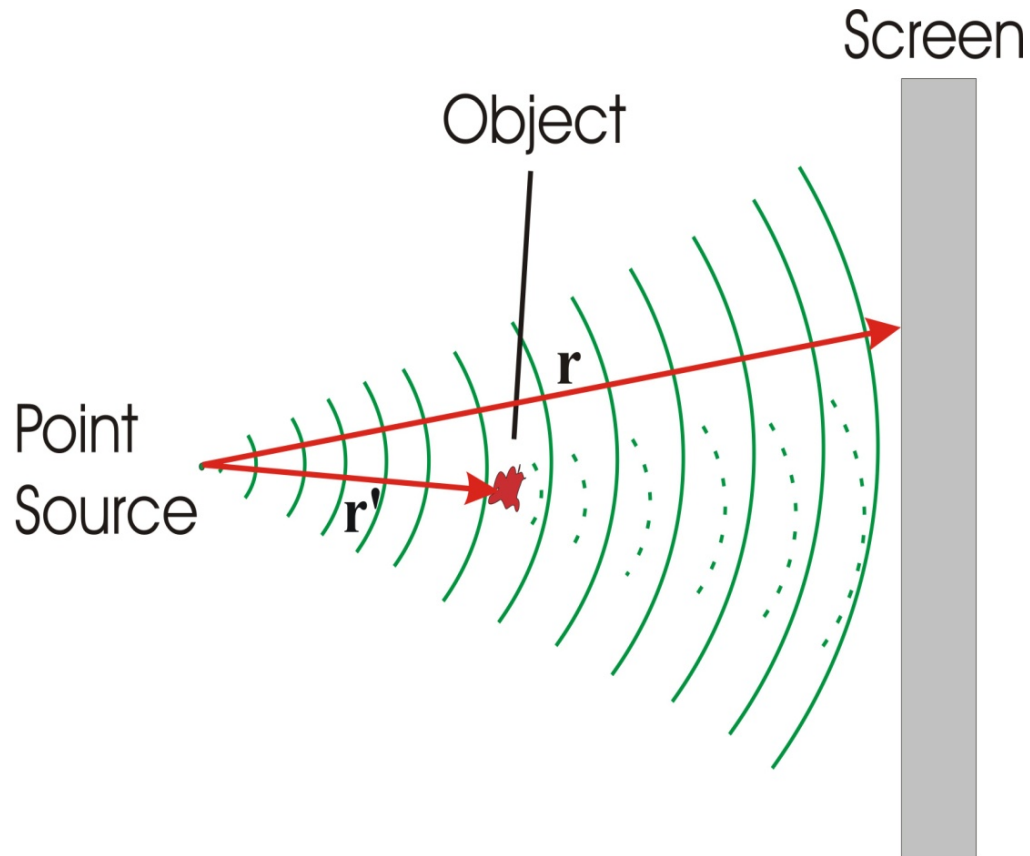
D. Gabor, "Microscopy by reconstructed wave-fronts," Proc. R. Soc. London A, 197, 454, (1949)



H.-W. Fink, H. Schmid, H.J. Kreuzer, and A. Wierzbicki, "Atomic resolution in lens-less low-energy electron holography," Phys. Rev. Lett., 67,1543-1546 (1991)

# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Recording



$$I(\mathbf{r}) = \left| A_{ref}(\mathbf{r}) + A_{scat}(\mathbf{r}) \right|^2$$

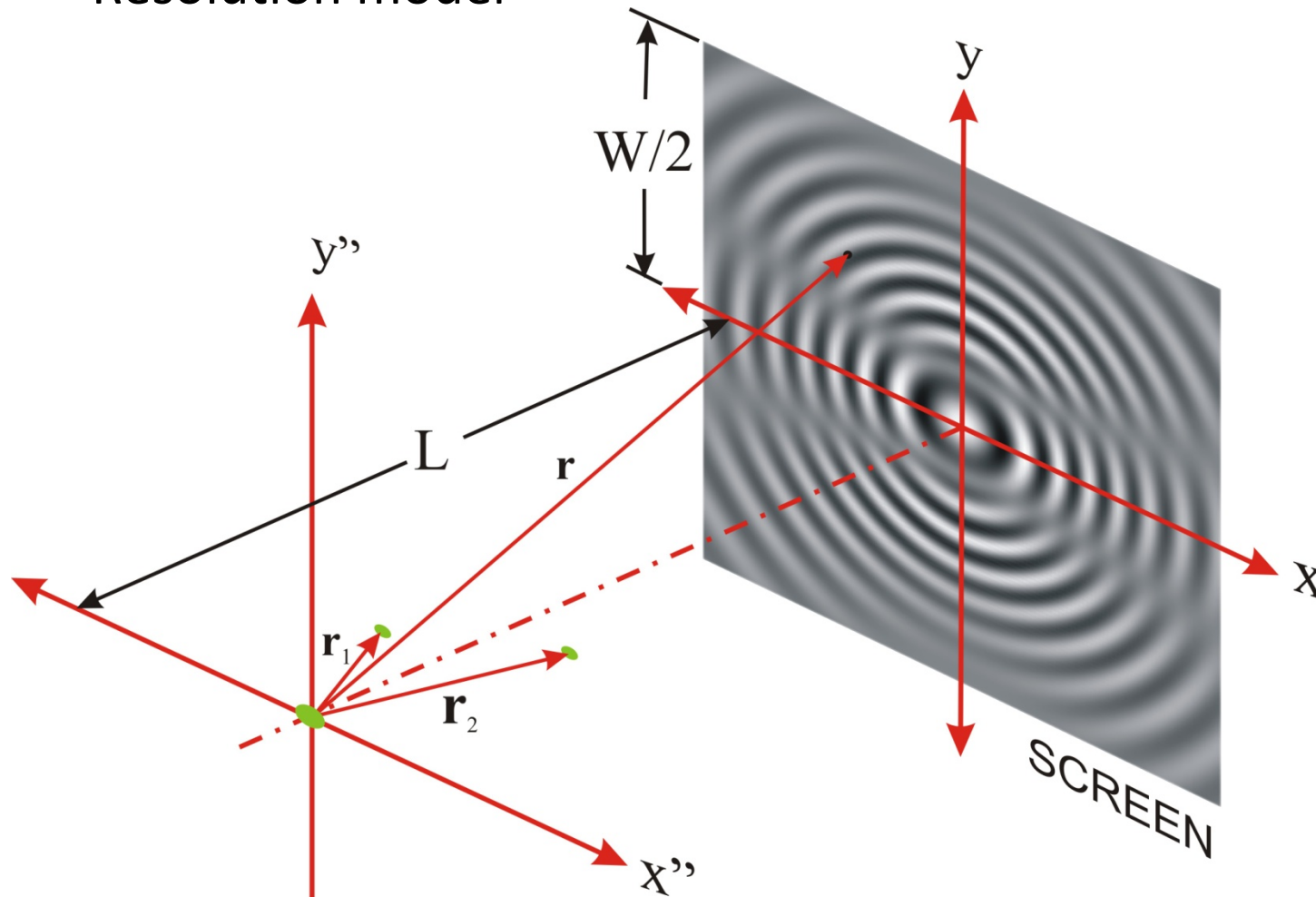
Prepared hologram

$$\tilde{I}(\mathbf{r}) = I(\mathbf{r}) - \left| A_{ref}(\mathbf{r}) \right|^2$$

$$\tilde{I}(\mathbf{r}) = [A_{ref}^*(\mathbf{r})A_{scat}(\mathbf{r}) + A_{ref}(\mathbf{r})A_{scat}^*(\mathbf{r})] + \left| A_{scat}(\mathbf{r}) \right|^2$$

# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Resolution model



$$A(\mathbf{r}) = A_{ref} \frac{\exp[ikr]}{r} + A_1 \frac{\exp[ik|\mathbf{r} - \mathbf{r}_1|]}{|\mathbf{r} - \mathbf{r}_1|} + A_2 \frac{\exp[ik|\mathbf{r} - \mathbf{r}_2|]}{|\mathbf{r} - \mathbf{r}_2|}$$

# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Resolution model

$$I(\mathbf{r}) = \left| A_{ref} \frac{\exp[ikr]}{r} + A_1 \frac{\exp[ik|\mathbf{r} - \mathbf{r}_1|]}{|\mathbf{r} - \mathbf{r}_1|} + A_2 \frac{\exp[ik|\mathbf{r} - \mathbf{r}_2|]}{|\mathbf{r} - \mathbf{r}_2|} \right|^2$$

$$\tilde{I}(\mathbf{r}) = I(\mathbf{r}) - \frac{A_{ref}^2}{r^2}$$

$$= \frac{\cancel{A_1^2}}{|\mathbf{r} - \mathbf{r}_1|^2} + \frac{\cancel{A_2^2}}{|\mathbf{r} - \mathbf{r}_2|^2} + 2 \frac{\cancel{A_1 A_2}}{|\mathbf{r}_1 - \mathbf{r}_2|^2} \cos \left[ k \left( |\mathbf{r} - \mathbf{r}_1| - |\mathbf{r} - \mathbf{r}_2| \right) \right]$$

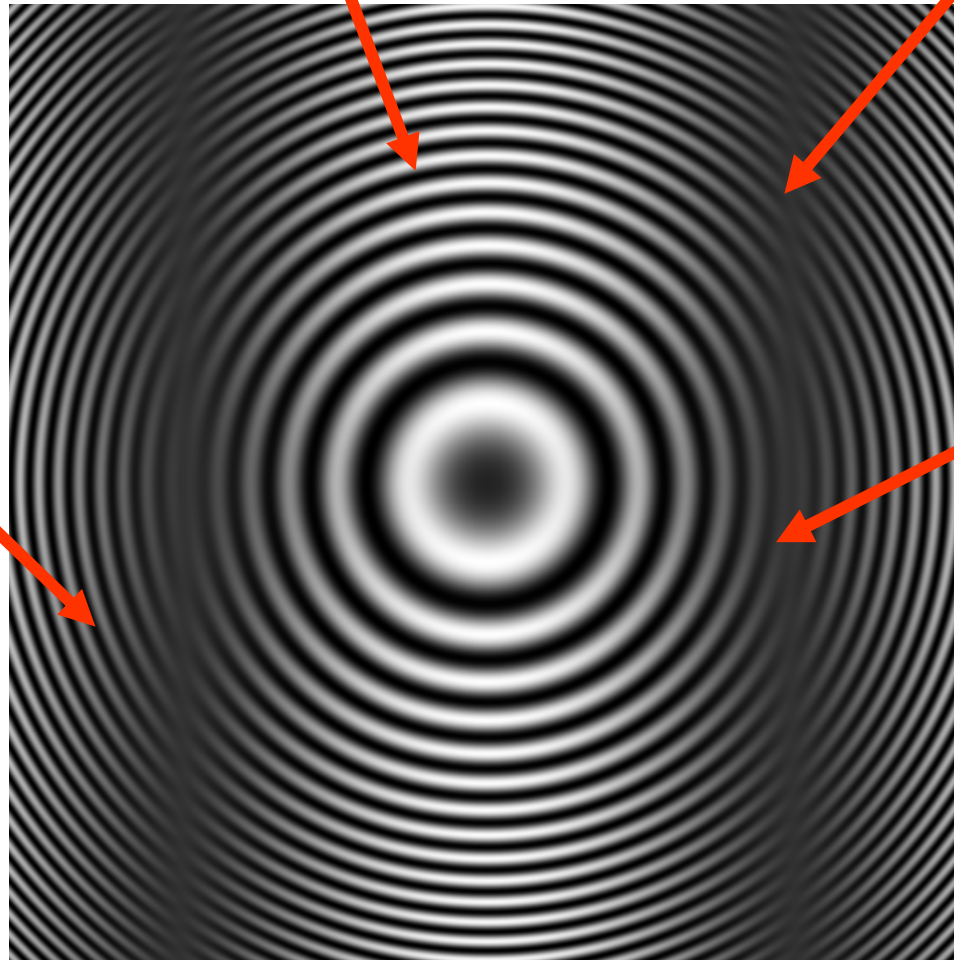
$$+ \left\{ 2 \frac{A_{ref} A_1}{r |\mathbf{r} - \mathbf{r}_1|} \cos \left[ k \left( r - |\mathbf{r} - \mathbf{r}_1| \right) \right] + 2 \frac{A_{ref} A_2}{r |\mathbf{r} - \mathbf{r}_2|} \cos \left[ k \left( r - |\mathbf{r} - \mathbf{r}_2| \right) \right] \right\}$$



# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Lateral Resolution  $|\mathbf{r}_1| = |\mathbf{r}_2|$

$$\tilde{I}(\mathbf{r}) = 4 \frac{A_0 A_1}{r |\mathbf{r} - \mathbf{r}_1|} \cos\left[k(2r - |\mathbf{r} - \mathbf{r}_1| - |\mathbf{r} - \mathbf{r}_2|)/2\right] \cos\left[k(|\mathbf{r} - \mathbf{r}_1| - |\mathbf{r} - \mathbf{r}_2|)/2\right]$$

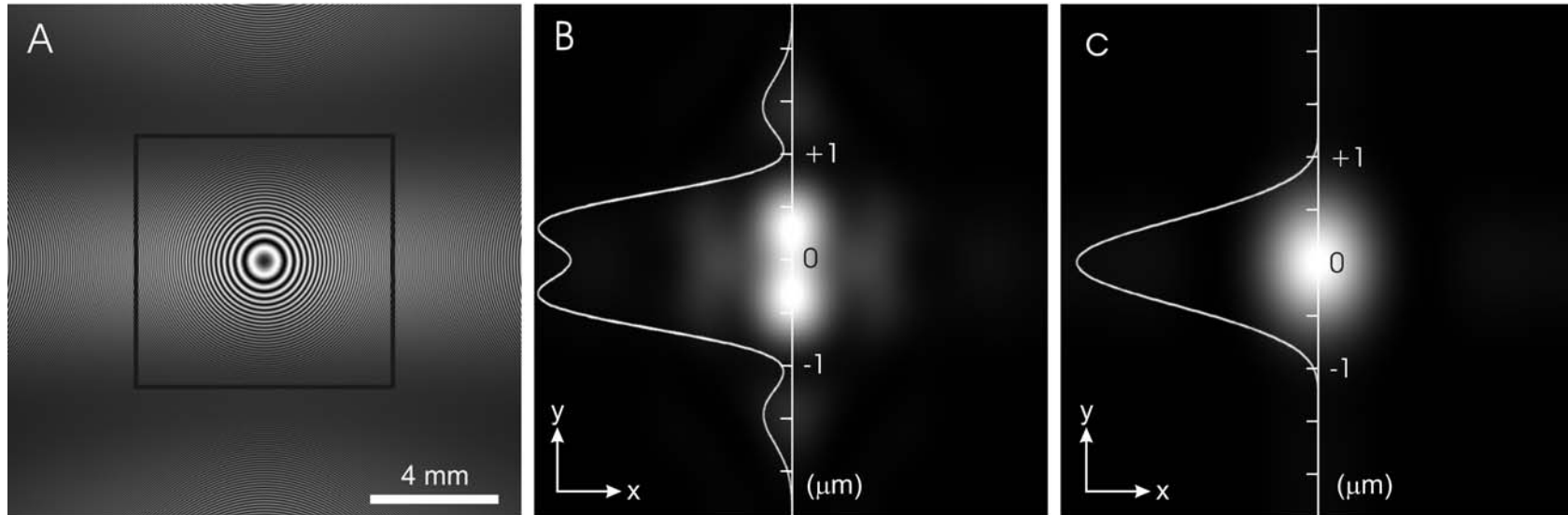


INFORMATION  
ABOUT POINT  
SOURCE TO  
PARTICLES  
DISTANCE

INFORMATION  
ABOUT THE  
PARTICLE  
SEPARATION

# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Lateral Resolution



Test of lateral resolution. A: simulated hologram of two points close to the optical axis and  $0.8 \mu\text{m}$  apart, taken with a blue laser  $\lambda=4730\text{\AA}$  with an aperture of 0.5 (0.28 for the inner square). B: reconstruction from the full hologram with the insert showing submicron resolution. C: the same for the smaller hologram losing resolution.

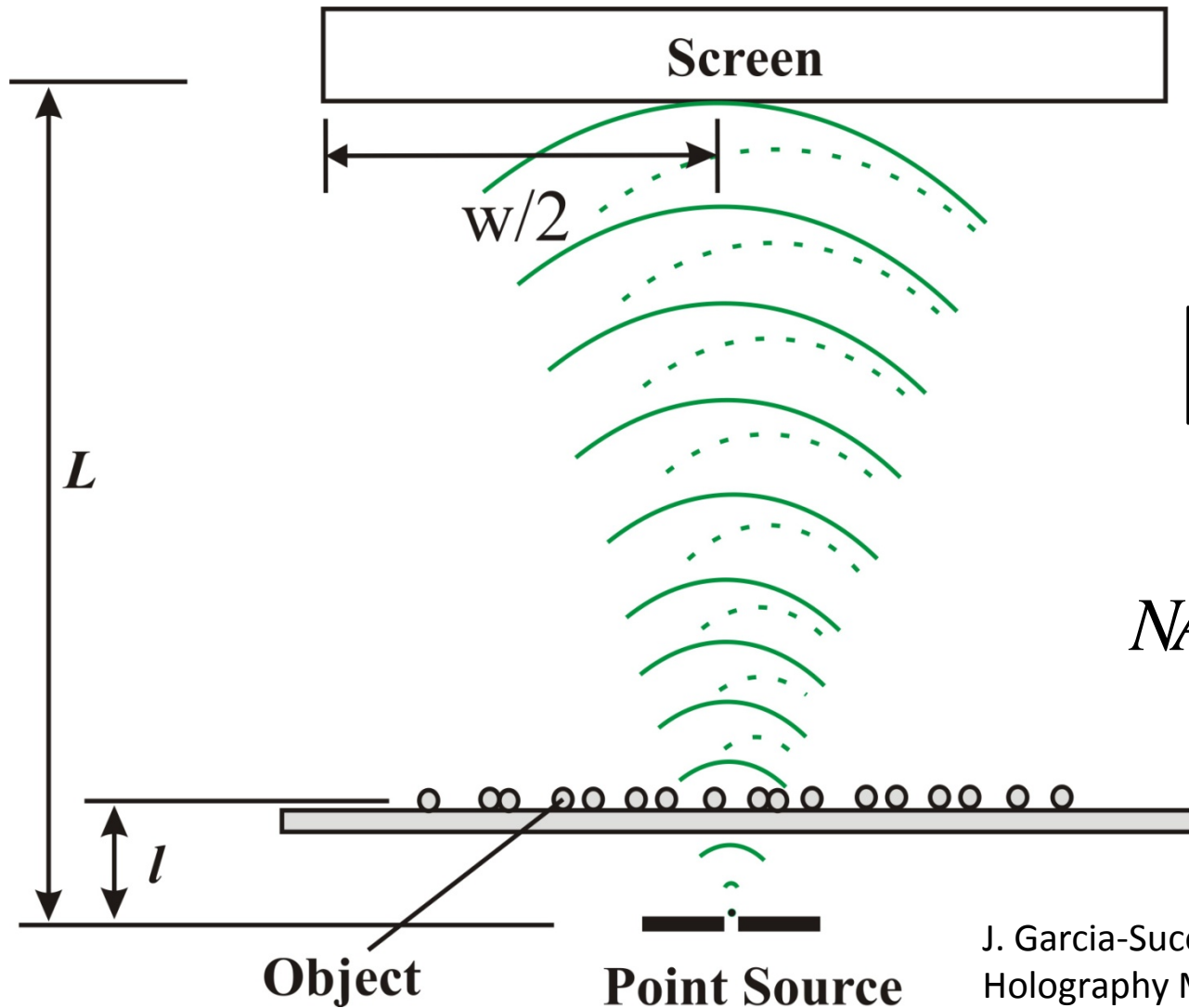
$$|\mathbf{r}_2 - \mathbf{r}_1| \geq \frac{\lambda}{2NA}$$

S.K. Jericho, et. al, "Submersible Digital In-line Holographic Microscope", *Rev Sci Instrum*, **77**, 043706-1, 043706-10, (2006)

J. Garcia-Sucerquia, et. al. "Digital In-line Holography Microscopy," *Appl. Opt.* **45**, 836-850 (2006) .

# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Lateral Resolution



$$|\mathbf{r}_2 - \mathbf{r}_1| \geq \frac{\lambda}{2NA}$$

$$NA = \frac{W}{2\sqrt{(W/2)^2 + L^2}}$$

J. Garcia-Sucerquia, et. al. "Digital In-line Holography Microscopy," Appl. Opt. **45**, 836-850 (2006)

# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- **Practical recording of in-line holograms**

1. Point source

2. Recording device

- ✓ Number of pixels
- ✓ Pixel dimensions
- ✓ Width-Height
- ✓ Spectral responsivity
- ✓ Acquisition frame rate
- ✓ Communication protocol
- ✓ .....

3. Point-source to recording device distance

- ✓ Numerical aperture

4. Point-source to sample distance

- ✓ High spatial frequency fringes

# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Practical recording of in-line holograms

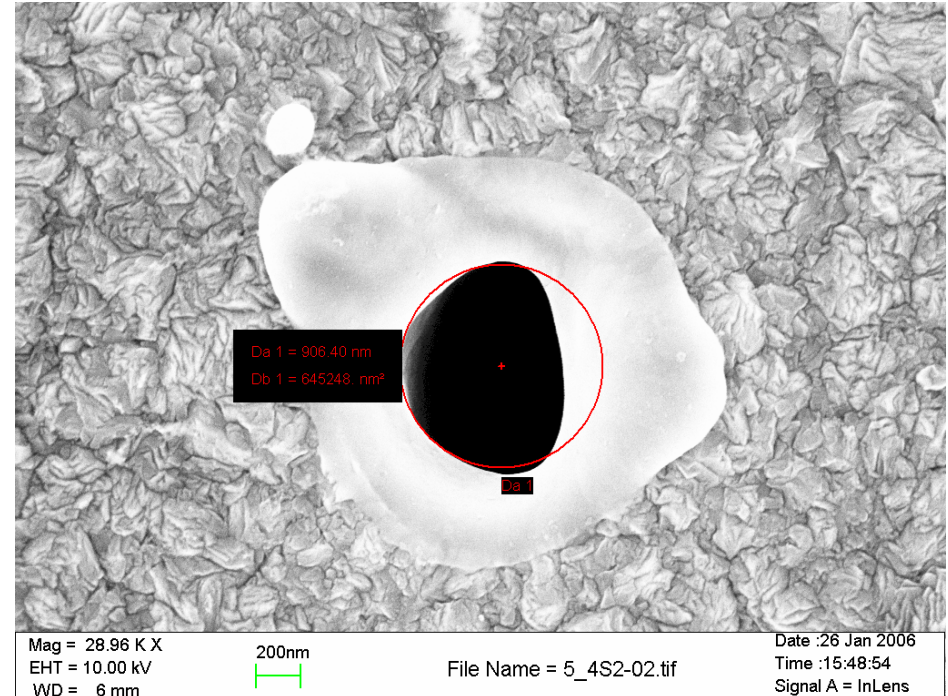
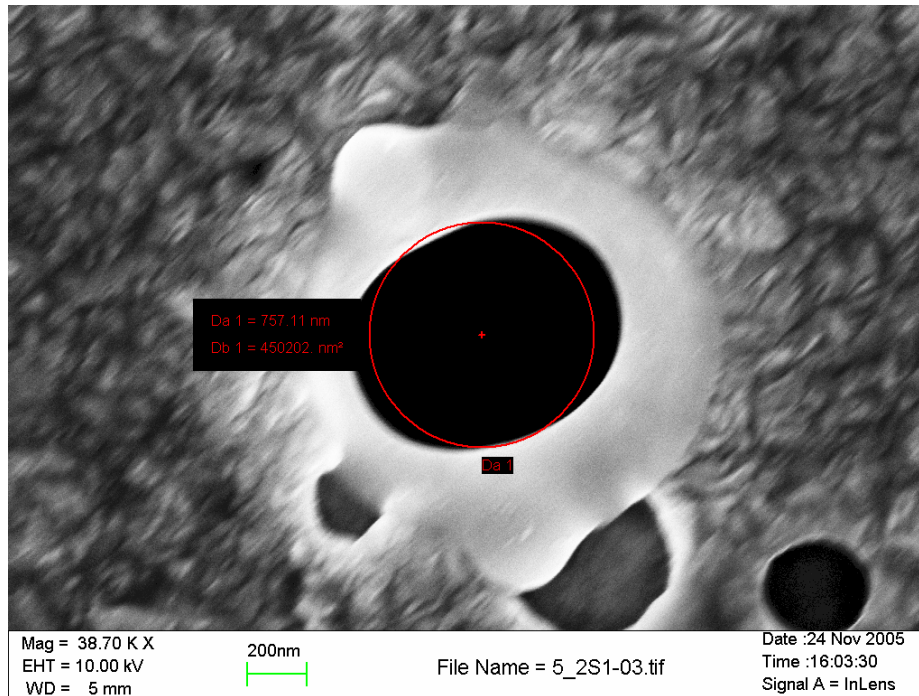
1. Point source



# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Practical recording of in-line holograms

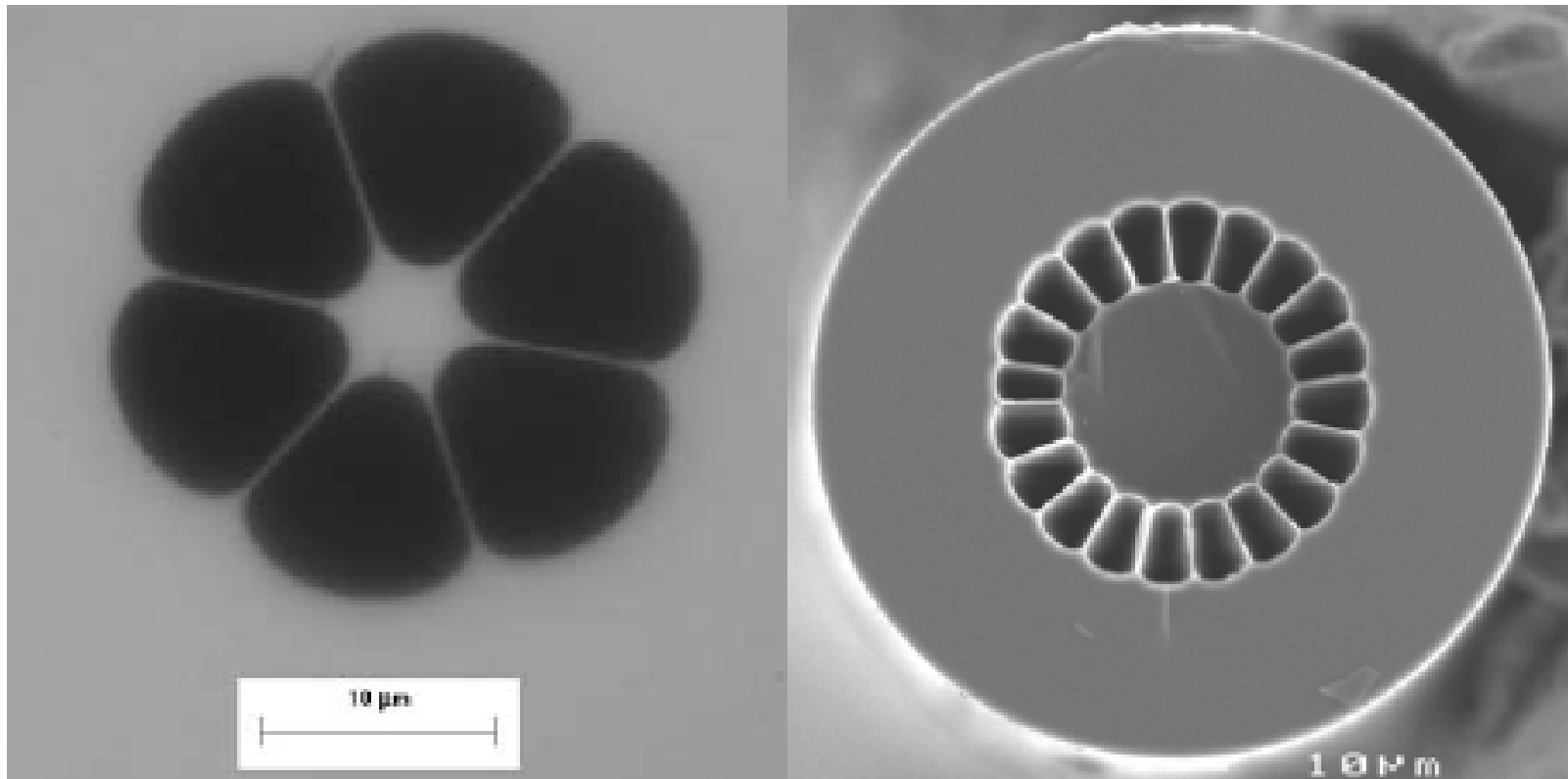
1. Point source



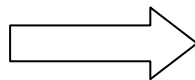
# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Practical recording of in-line holograms

1. Point source



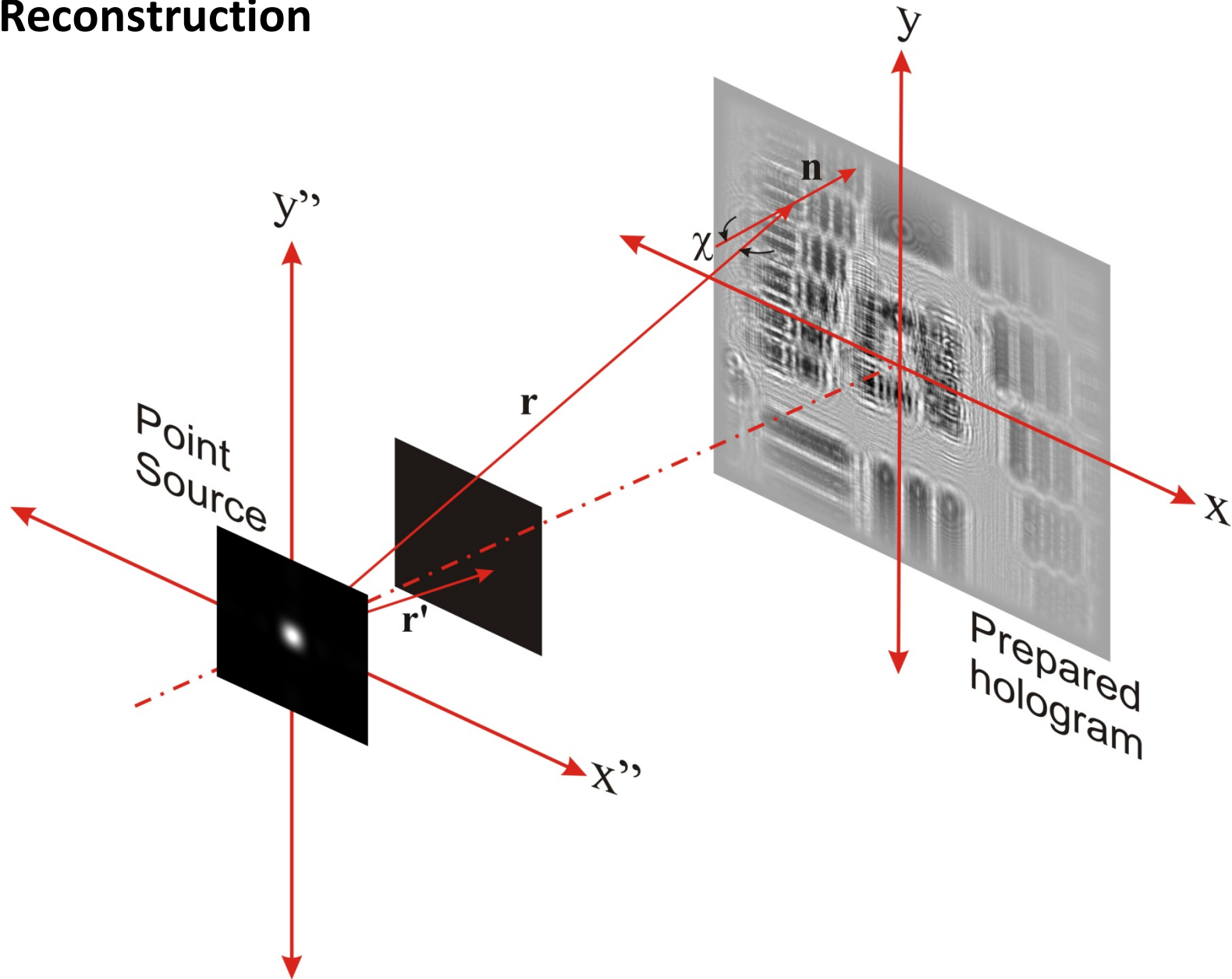
Highest NA 0.65  
Wavelength = 0.45  $\mu\text{m}$



Theoretical resolution = 0.36  $\mu\text{m}$

# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Reconstruction





# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Reconstruction

$$A_{scat}(\mathbf{r}') = -\frac{i}{2\lambda} \iint_{Screen} \tilde{I}(\mathbf{r}) A_{ref}(\mathbf{r}) \frac{\exp[-ik|\mathbf{r}-\mathbf{r}'|]}{|\mathbf{r}-\mathbf{r}'|} (1 + \cos \chi) dS_r$$

Fresnel-Kirchhoff diffraction formula.

$$A_{scat}(\mathbf{r}') = -\frac{i}{\lambda} \iint_{Screen} \tilde{I}(\mathbf{r}) A_{ref}(\mathbf{r}) \frac{\exp\left[-ik\left(r - \frac{|\mathbf{r} \cdot \mathbf{r}'|}{r}\right)\right]}{|\mathbf{r}-\mathbf{r}'|} dS_r$$

Fresnel-Kirchhoff in the Fraunhofer approximation.

$$A_{ref}(\mathbf{r}) = A_{ref} \frac{\exp[ikr]}{r}$$

Reference wave.

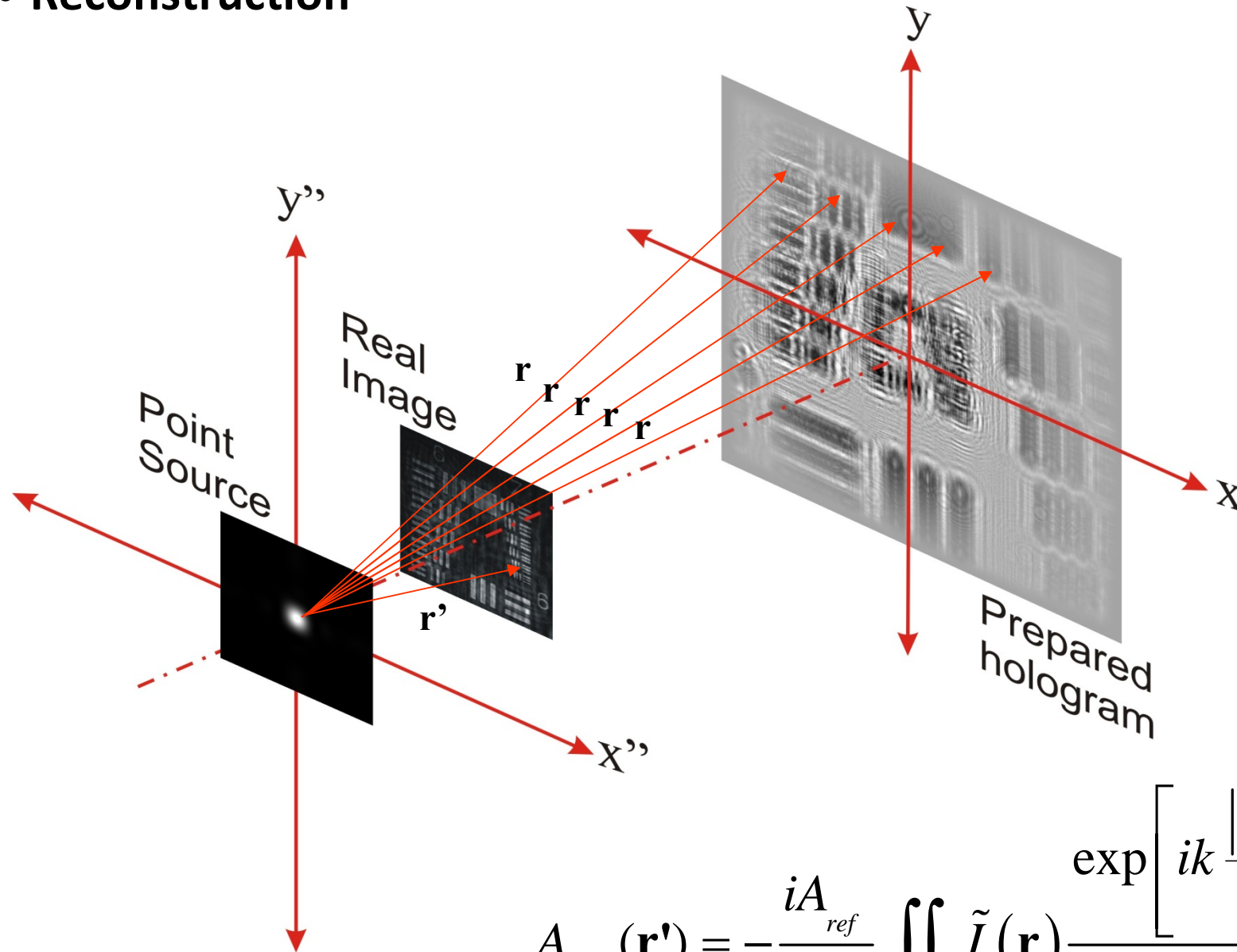
$$A_{scat}(\mathbf{r}') = -\frac{iA_{ref}}{r\lambda} \iint_{Screen} \tilde{I}(\mathbf{r}) \frac{\exp\left[ik\frac{|\mathbf{r} \cdot \mathbf{r}'|}{r}\right]}{|\mathbf{r}-\mathbf{r}'|} dS_r$$

Kirchhoff-Helmholtz transform.

J. J. Barton, "Photoelectron holography," Phys. Rev. Lett. **61**, 1356–1359 (1988).

# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

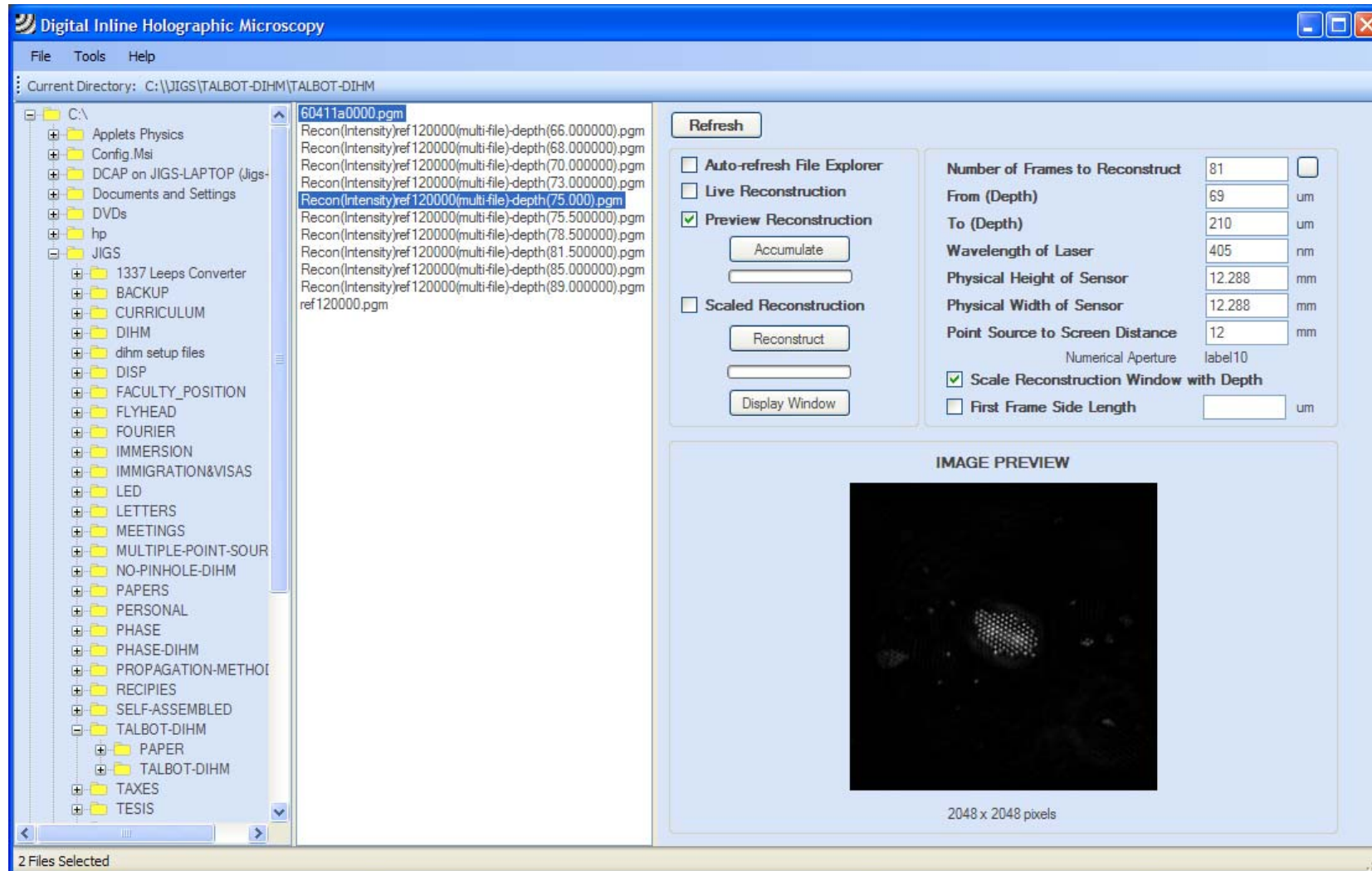
- Reconstruction



$$A_{scat}(\mathbf{r}') = -\frac{iA_{ref}}{r\lambda} \iint_{Screen} \tilde{I}(\mathbf{r}) \frac{\exp\left[ik \frac{|\mathbf{r} \cdot \mathbf{r}'|}{r}\right]}{|\mathbf{r} - \mathbf{r}'|} dS_r$$

# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Commercial reconstruction software



H.J. Kreuzer, US Patent 6,411,406 B1, June 25, 2002 "Holographic Microscope and Method of Hologram Reconstruction"

Resolution Optics™  
<http://www.resolutionoptics.com>

# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- **Practical reconstruction of in-line holograms**
  1. What is the need of using a prepared hologram?
  2. Had Gabor the chance of removing the zeroth order of diffraction?
  3. What is the role of the wavelength in the reconstruction process?
  4. What parameters should be controlled to avoid aliasing?
  5. Is the scaling trustable in DIMH?

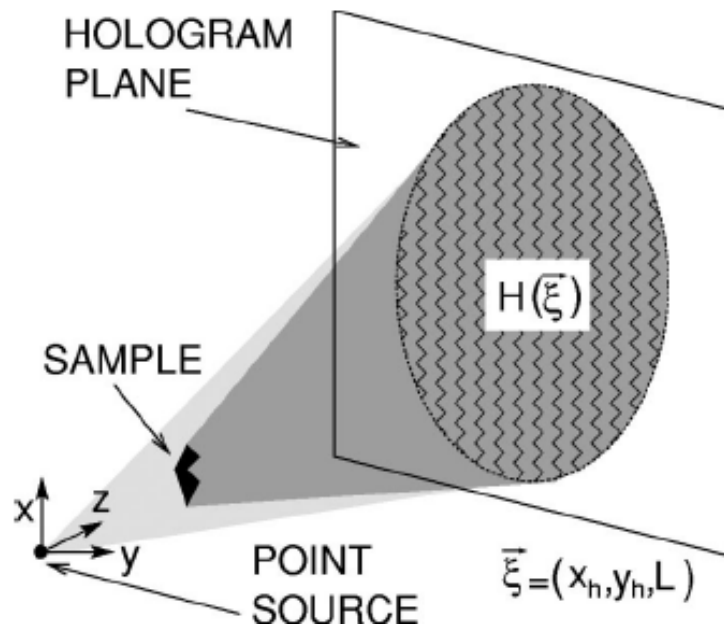
# DIGITAL IN-LINE HOLOGRAPHIC MICROSCOPY

- Playing with Gabor's hologram

## Gabor's hologram in a modern perspective

L. Repetto,<sup>a)</sup> F. Pellistri,<sup>b)</sup> E. Piano, and C. Pontiggia

*Dipartimento di Fisica dell'Università di Genova, Via Dodecaneso, 33-16146 Genova, Italy*



$$U(\mathbf{P}) = \int P_{\xi}(X-x_h, Y-y_h) H(x_h, y_h) dx_h dy_h,$$

$$\xi = \frac{L}{z_0} (L - z_0),$$

$$P_{\xi}(x_h, y_h) = e^{ik \sqrt{x_h^2 + y_h^2 + \xi^2}}.$$

L. Repetto, F. Pellistri, E. Piano, C. Pontiggia,  
"Gabor's Hologram in a Modern Perspective",  
AJP, Vol. **72**, 964- 967 (2004)